# A Method of Identifying Supersonic Projectiles Using Acoustic Signatures 

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## 1. INTRODUCTION

The function of the round discrimination system (RDS) is to improve the scoring accuracy of the remote equipment target system (RETS) currently being used for live-fire training at training centers worldwide. The RDS, which interfaces directly with the RETS, discriminates among different main gun kinetic energy (KE), high-explosive antitank (HEAT), and high-explosive incendiary (HEI) and machine gun (ball and tracer) training practice (TP) ammunition from the following armored vehicles: all M1 Abrams series main battle tanks, the M60A3 main battle tank, and the M2/3 Bradley Fighting Vehicle (BFV). This system can determine whether the incoming projectile could produce a kill during live fire exercises.

The RDS program was conducted in three phases. The first phase was a feasibility test. Acoustic signatures of medium- to large-caliber projectiles from the three types of armored vehicles were collected; these signatures were found to have distinct acoustic features, allowing the program to continue. In the second phase, acoustic signatures of the $35-\mathrm{mm}$ tank precision gunnery in-bore device (TPGID) rounds and small-caliber machine gun rounds were collected so that the database could be completed. An algorithm and a brassboard were developed on the acoustic signature discriminants found. The major discriminants used include the duration of the supersonic shock wave, the location of the round relative to the acoustic sensors, and the terminal velocity of the round. In the third phase, verification/validation, a field test was conducted at Aberdeen Proving Ground (APG), MD. A working brassboard correctly discriminated $90 \%$ of the rounds fired. Finally, the RDS brassboard was demonstrated as a proof-ofconcept to the sponsor, the Seventh Army Training Command (7th ATC) in Grafenwoehr, Germany.

This report summarizes the background material, the round discrimination algorithm, and the current RDS brassboard design. The test data, software development, and system components are mentioned in the discussion.

## 2. BACKGROUND

2.1 RDS Program. The RDS program was initiated by the Army Materiel Command Field Assistance in Science and Technology Junior (AMC-FAST Jr.) engineers at the U.S. Army Research Laboratory (ARL), in response to a request by the AMC-FAST Science Advisor at the 7th ATC in 1992. The request from the 7th ATC reads as follows: "The 7th ATC requires a target RDS, which identifies the round
location within an area which extends 1 m beyond the target edge and classifies the round type into four band size categories: $<20 \mathrm{~mm}, 20-30 \mathrm{~mm}, 30-90 \mathrm{~mm}$, and $>90 \mathrm{~mm}$." At the very least, the Commander of the 7th ATC wanted a system able to discriminate between projectiles $<30 \mathrm{~mm}$ (small caliber and BFV main gun projectiles) and $>30 \mathrm{~mm}$ (M1A1 main gun projectiles) with a per unit (system) cost of around $\$ 5 \mathrm{k}$. Table 1 identifies the projectile's group by band and caliber. Several sensor technologies were explored as potential candidates, including acoustics, infrared, radar, and video. The acoustic approach was chosen for two reasons: cost and the ability to exploit the uniqueness of acoustic signatures of armored vehicle rounds.

Table 1. Projectiles Tested

| Projectile <br> Caliber <br> (In-bore) <br> (mm) | Projectile <br> Caliber <br> (In-flight) <br> (mm) | Projectile <br> Nomenclature | Projectile <br> Description | Projectile <br> Group by <br> Band <br> $(\mathrm{mm})$ | Projectile <br> Group by <br> Caliber <br> (mm) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 7.62 | 7.82 | M59 | Ball | $<20$ | 7.62 |
| 7.62 | 7.82 | M62 | Tracer | $<20$ | 7.62 |
| 12.7 | 12.95 | M33 | Ball | $<20$ | 12.7 |
| 12.7 | 12.95 | M17 | Tracer | $<20$ | 12.7 |
| 25 | 16.2 | M910 | TPDS-T | $<20$ | 25 KE |
| 25 | 25 | M793 | TP-T | $20-30$ | 25 HEI |
| 35 | 35 | XM? | TPL-T | $30-90$ | 35 TPGID |
| 35 | 35 | DM18 | HEAT-TP-T | $30-90$ | 35 TPGID |
| 35 | 35 | DM68 | HEAT-TP-T | $30-90$ | 35 TPGID |
| 105 | 63.5 | M724 | TPDS-T | $30-90$ | $105 / 120 \mathrm{KE}$ |
| 120 | 38 | M865 | TPCSDS-T | $30-90$ | $105 / 120 \mathrm{KE}$ |
| 105 | 105 | M490 | TP-T | $>90$ | $105 / 120 \mathrm{HE}$ |
| 120 | 120 | M831 | HEAT-TP-T | $>90$ | $105 / 120 \mathrm{HE}$ |

2.2 RETS. The RETS, as seen in Figure 1, uses vibration sensors (also called hit sensors) that are attached to the target and connect to the RETS electronic control unit (ECU). When the sensors detect a hit, the ECU conveys a hit signal to a range control tower via a hardwired or radio link. This activates an electromechanical mechanism that lowers the plywood tank target, thus indicating a kill. A deficiency of the current system is the absence of a mechanism to discriminate between rounds, locate the rounds, and activate the target only in response to those rounds that can produce a kill. A $12.7-\mathrm{mm}$ ( .50 cal .) machine gun round, for example, can currently be credited with killing a T-72 tank target. RETS can be


Figure 1. Remote equipment target system.
fooled by debris from ricocheting rounds or by small-caliber machine gun fire onto the target, simulating a main gun round vibration pattern. As a result, armor kills by non-armor-defeating projectiles erroneously inflate the training unit's score. In addition, this deficiency prohibits an accurate after-action evaluation of the trainee's ability to choose the proper ammunition for the mission at hand. The RDS eliminates this deficiency and increases the accuracy of the training process.

## 3. RDS CONCEPT

An extensive literature search of existing scoring systems and potential signature-producing technologies was undertaken. The techniques investigated included using video cameras, colored tracers, lasers, radar, and acoustics. Many were dismissed due to cost, practicality, or lack of technology. The two most promising concepts recommended by the FAST Jr. team were analysis of acoustical signatures and radar signatures of the passing projectile. Analysis of the radar signature approach was subsequently deemed not feasible due to high cost. It was determined that the simplest and most cost-effective method of discrimination would be an acoustic approach.

In order to explore the feasibility of an acoustic RDS system, a three-test program was proposed that included participants from three ARL directorates-the Weapons Technology Directorate (WTD), the Survivability/Lethality Analysis Directorate (SLAD), and the Sensors, Signatures, Signal and Information (S3I) Processing Directorate. A test matrix was developed to include all possible rounds and engagement distances used on a live-fire gunnery range during a Combined Arms Live-Fire Exercise (CALFEX), as dictated by FM 17-12-1 and FM 23-1. The first part was a feasibility test, where acoustical signature data
were collected and analyzed. The test data were used to determine if acoustic signal discrimination between projectile data at the extreme firing ranges of the 7th ATC interest array were possible. The second part of the program extended the data collection effort for projectile discrimination by collecting data on projectiles within the extremes investigated in part 1. During the third part, a brassboard RDS was constructed and tested at APG. This test included all the projectiles used on the live-fire gunnery range. Subsequent to verification of the brassboard system's ability to discriminate effectively and efficiently, the system was to be demonstrated at the 7th ATC.

The projectiles fired during parts 1 and 2 of the test program are those actually fired on live-fire gunnery ranges and are listed in Table 1. The projectile's in-flight caliber determined its band group. No large-caliber service rounds were considered in the test program due to cost and because they are not used in live-fire training exercises. However, large-caliber service rounds could be added to the acoustic database at a later date.

### 3.1 Acoustic Round Discrimination Technique.

3.1.1 Background. As a supersonic projectile travels, several shocks from the projectile are propagated to the surrounding air. These shocks are created from the projectile's bow, surface features on the projectile's body, and the tail. A sensitive air pressure gauge placed in the path of the shock waves will register what is typically referred to as the N-Wave. The characteristics of the N-Wave are directly dependent on the geometry of the projectile, the projectile's velocity, the location of the shock origination relative to the pressure gauge, and the condition of the ambient air. Other discontinuous features of the projectile, such as fins or threads, will contribute to additional characteristic features on the N-Wave. Figure 2 graphically depicts the shock cone formed from supersonic projectiles, while Figure 3 shows the characteristic N -Wave pressure profile.
3.1.2 Theory and Formulation. A body traveling through the air faster than the ambient speed of sound will generate a conic shock profile. The shock pressure profile shape is directly dependent on the object's form. Air is compressed against the leading part of the object. Since the object is traveling faster than the time required for the air to re-expand ahead of the object, a conic shock front is generated. A sensitive pressure gauge some distance away from the object's trajectory will register the lead shock as a time-pressure discontinuity. As the body passes, the compressed air expands, and the local pressure


Figure 2. M865 shock cone shadow-shlieren photograph.


Figure 3. M865 N-Wave pressure profile.
decreases. As surface features on the object create shocks, the profile sensed by the pressure gauge register these as small positive discontinuities. As the local pressure decreases towards the tail of the object, the local pressure reaches a neutral pressure area that is equivalent to the ambient pressure. Pressure aft of the neutral area continues to decrease below ambient. If the object has surface features in the aft region, the shock also appears as positive discontinuities in the pressure profile.

On the tail, the object wake is made to fall back into the area previously occupied by the object. Turbulent eddies are created by the air viscosity interaction with the object surface. These eddies trail into the wake core and support a region of low pressure. As the energy in the eddies dissipates in the wake, the region collapses, showing up as the final shock in the pressure profile. This is called the tail shock, where the low pressure changes to ambient. Other eddies trailing off the object may show up after the tail shock as strong variations in pressure. In some cases, the objects shape could generate second and third generations of low pressure wake cores, resulting in what appears as several tail shocks.

The magnitude, duration, and shape of the N -Wave for an ogive body of revolution, small-caliber shaped projectile, traveling at or faster than the speed of sound, were calculated (Whitham 1952). Expressed for large distances, in general terms, the shock overpressure is,

$$
\begin{equation*}
\frac{p}{p_{o}}=2^{1 / 4} \gamma(\gamma+1)^{-1 / 2}\left(M^{2}-1\right)^{1 / 8}\left[\int_{0}^{y_{0}} F(y) d y\right]^{1 / 2} O^{-3 / 4} \tag{1}
\end{equation*}
$$

where
p = overpressure,
$\mathrm{p}_{\mathrm{o}}=$ ambient pressure,
$\gamma=$ ratio of specific heats of air (1.4),
$\mathrm{M}=$ Mach number,
y = a characteristic curve relationship between x and O ,
$\mathrm{x}=$ distance along the axis from the bow,
O = offset distance,
$\mathrm{F}(\mathrm{y})=\mathrm{a}$ function used to solve the differential equation determining the flow past the body of revolution.

This equation formed the basis of the theory for acoustic round discrimination. By simplifying the generalized results into simple equations (Skochko 1966), one can calculate the pressure and total duration of the N -Wave by:

$$
\begin{align*}
\frac{p}{p_{0}} & =\frac{(.53)\left(M^{2}-1\right)^{1 / 8}}{O^{3 / 4}}\left(\frac{D}{L^{1 / 4}}\right) \\
T & =\frac{(1.82) O^{1 / 4} M}{a\left(M^{2}-1\right)^{3 / 8}}\left(\frac{D}{L^{1 / 4}}\right) \tag{2}
\end{align*}
$$

where
$\mathrm{a}=$ ambient air speed of sound (meters/second),
$\mathrm{D}=$ projectile diameter (meters),
$\mathrm{L}=$ projectile length (meters),
$\mathrm{T}=$ total duration (seconds).

Theoretically, a properly emplaced sensitive pressure gauge can measure the N -Wave of passing projectiles. Additionally, if the ambient air conditions, the projectile location, and velocity relative to the pressure gauge, were known, the projectile could be identified. A system, constructed to gather data and perform analysis for projectile identification.

### 3.2 Acoustic Location and Velocity Technique.

3.2.1 Background. Determination of the projectile's location and final velocity was performed with a proven acoustical technique constructed of simple pressure sensitive devices that were linked to a clock. This technology was developed by the ARL Human Research and Engineering Directorate (HRED) for small-caliber projectiles (Kalb, unpublished). Three microphones were arranged in a line in front of a target and placed perpendicular to the projectiles flight path (see Figure 4). It allowed the projectile's location above the microphone array to be determined. On HRED ranges, the projectile and range are known prior to firing, enabling the projectile's velocity to be derived from ballistic firing tables. Three additional microphones were added to the HRED setup to create the RDS microphone setup (see Figure 5). The additional microphones were placed directly in front of the original three microphones, yielding a second location for redundancy in case a microphone was damaged or failed. The two center microphones


Figure 4. HRED microphone array.
provided the projectile's velocity. Knowing the spatial position of each sensor and measuring the time each was triggered by the passing projectile's supersonic shock wave, one can closely approximate the location and velocity at the target.
3.2.2 Theory and Formulation. The projectile's shock wave can be visualized as an infinite cone traveling with the projectile. The ambient speed of sound and the projectile's velocity result in the classic shock angle expression:

$$
\begin{equation*}
\alpha=\sin ^{-1}\left(\frac{a}{v}\right)=\sin ^{-1}\left(\frac{1}{M}\right), \quad M=\frac{v}{a} \tag{3}
\end{equation*}
$$



Figure 5. Microphone array and target setup.
where
$\alpha=$ shock angle $\left({ }^{\circ}\right)$
$\mathrm{M}=$ Mach number,
$\mathrm{v}=$ projectile velocity (meters/second),
a = ambient speed of sound (meters/second).

This relationship assumes that the cone form is maintained, subsequent to its time of arrival, throughout the distance of the shock wave propagation.

The projectile is assumed to be traveling parallel to the Y-axis striking the target at coordinates ( $\mathrm{X}, \mathrm{Y}, \mathrm{Z}$ ). Microphones 1, 2, and 3 are placed in the front right, front center, and front left, respectively. Microphones 4,5 , and 6 are placed in the back right, back center, and back left. These location microphones (LM) are referred to as LM1-LM6. The microphone centers for microphones $1-6$ are located at $(\mathrm{X}+1, \mathrm{Y}, \mathrm{Z}),(\mathrm{X}, \mathrm{Y}, \mathrm{Z}),(\mathrm{X}-1, \mathrm{Y}, \mathrm{Z}),(\mathrm{X}+1, \mathrm{Y}+1, \mathrm{Z}),(\mathrm{X}, \mathrm{Y}+1, \mathrm{Z})$, and ( $\mathrm{X}-1, \mathrm{Y}+1, \mathrm{Z})$, respectively. Figure 5 shows the microphone placement relative to the target and the coordinate system used.

On the arrival of the shock cone at each microphone, a total of five time differences $\left(\mathrm{T}_{1}, \mathrm{~T}_{2}, \mathrm{~T}_{3}, \mathrm{~T}_{4}\right.$, and $\mathrm{T}_{5}$ ) are recorded. Two time differences are needed for each location array and one time difference for the velocity determination. $T_{1}-T_{5}$ are defined as follows:
$\mathrm{T}_{1}=$ Time difference between LM2 and LM1,
$\mathrm{T}_{2}=$ Time difference between LM3 and LM2,
$\mathrm{T}_{3}=$ Time difference between LM5 and LM2,
$\mathrm{T}_{4}=$ Time difference between LM5 and LM4,
$\mathrm{T}_{5}=$ Time difference between LM6 and LM5.

The time differences $T_{1}$ and $T_{2}$ are measured from a moving sound source and can be related to a hypothetical source that originates from a point in a vertical plane defined by LM1, LM2, and LM3. The transformed time difference from each microphone pair defines a hyperbola of ambiguity, which is the set of all point sources which produce this same arrival time difference. The intersection of these hyperbolas locates the point source through which the projectile traveled ( $\mathrm{X}, \mathrm{Z}$ ). Figure 6 is an example of the hyperbolas of ambiguity.


Figure 6. Projectile location by intersection of hyperbolas of ambiguity.

The altered difference in arrival time between the center and right microphone pair, $D_{1}$, can be determined from the following equation:

$$
\begin{equation*}
\mathrm{D}_{1}=\frac{\left(\mathrm{R}_{\mathrm{C}}-\mathrm{R}_{\mathrm{R}}\right)}{\mathrm{a}}=\frac{\mathrm{T}_{1}}{\cos (\alpha)} \tag{4}
\end{equation*}
$$

where
$R_{C}=$ in-plane distance from center microphone to projectile location (meters),
$\mathrm{R}_{\mathrm{R}}=$ in-plane distance from right microphone to projectile location (meters),
and the difference in arrival time between the left and center microphone pair, $\mathrm{D}_{2}$, is:

$$
\begin{equation*}
\mathrm{D}_{2}=\frac{\left(\mathrm{R}_{\mathrm{L}}-\mathrm{R}_{\mathrm{C}}\right)}{\mathrm{a}}=\frac{\mathrm{T}_{2}}{\cos (\alpha)} \tag{5}
\end{equation*}
$$

where
$R_{L}=$ in-plane distance from left microphone to projectile location (meters).

It is useful to note that a positive time indicates that the source is to the right of the midpoint of a microphone pair and that a negative time indicates that the source is to the left.

The sound source location is related to the microphone positions by using the law of cosines. On the right side triangle:

$$
\begin{equation*}
\mathrm{R}_{\mathrm{R}}^{2}=\mathrm{R}_{\mathrm{C}}^{2}+\mathrm{A}^{2}-2 \mathrm{R}_{\mathrm{C}} \mathrm{~A} \cos \theta=\left(\mathrm{R}_{\mathrm{C}}-\mathrm{aD}_{1}\right)^{2}=\mathrm{R}_{\mathrm{C}}^{2}-2 \mathrm{R}_{\mathrm{C}} \mathrm{aD} \mathrm{D}_{1}+\mathrm{a}^{2} \mathrm{D}_{1}^{2} \tag{6}
\end{equation*}
$$

where

$$
\mathrm{A}=\text { microphone separation distance }(1 \mathrm{~m}),
$$

$\theta=$ angle from microphone array axis to $\mathrm{R}_{\mathrm{C}}$.

Similarly for the left side triangle:

$$
\begin{equation*}
\mathrm{R}_{\mathrm{L}}^{2}=\mathrm{R}_{\mathrm{C}}^{2}+\mathrm{A}^{2}-2 \mathrm{R}_{\mathrm{C}} \mathrm{~A} \cos (\pi-\theta)=\left(\mathrm{R}_{\mathrm{C}}+\mathrm{aD}_{2}\right)^{2}=\mathrm{R}_{\mathrm{C}}^{2}+2 \mathrm{R}_{\mathrm{C}} \mathrm{aD}_{2}+\mathrm{a}^{2} \mathrm{D}_{2}^{2} \tag{7}
\end{equation*}
$$

where $\cos (\pi-\theta)=-\cos (\theta)$.

Subtracting equation 6 from 7 yields:

$$
\begin{equation*}
4 R_{C} A \cos \theta=2 R_{C} a\left(D_{2}+D_{1}\right)+a^{2}\left(D_{2}^{2}-D_{1}^{2}\right) . \tag{8}
\end{equation*}
$$

From geometry, the offset distance of the projectile from the center microphone is:

$$
\begin{equation*}
\mathrm{R}_{\mathrm{C}}=\sqrt{\mathrm{Z}^{2}+\mathrm{X}^{2}} . \tag{9}
\end{equation*}
$$

Solving equations 8 and 9 for $Z$ yields:

$$
\begin{equation*}
Z=R_{C} \cos \theta=a\left(D_{2}+D_{1}\right)\left(\frac{R_{C}+\frac{a\left(D_{2}-D_{1}\right)}{2}}{2 A}\right) \tag{10}
\end{equation*}
$$

Rearranging equation 9 for X yields:

$$
\begin{equation*}
\mathrm{X}=\sqrt{\mathrm{R}_{\mathrm{C}}^{2}-\mathrm{Z}^{2}} \tag{11}
\end{equation*}
$$

The projectile location for microphones 4,5 , and 6 can be solved using the same equations with the substitution of $D_{4}$ and $D_{5}$.

Knowing that the position of the microphones are fixed and the projectile is assumed to be perpendicular to the array, one can approximate the velocity. The velocity is determined by taking the difference in position of the center microphones and dividing by the difference in arrival times of the center microphones.

$$
\begin{equation*}
\mathrm{v}_{\mathrm{P}}=\frac{\left(\mathrm{Y}_{\mathrm{LM} 2}-\mathrm{Y}_{\mathrm{LM} 5}\right)}{\mathrm{T}_{5}} \tag{12}
\end{equation*}
$$

where
$\mathrm{V}_{\mathrm{P}}=$ predicted projectile velocity (meters/second),
$\mathrm{Y}_{\mathrm{LM} 2}=\mathrm{y}$ position of LM2 (meters),
$\mathrm{Y}_{\mathrm{LM5}}=\mathrm{y}$ position of LM5 (meters).
3.2.3 Alternate Acoustic Location and Velocity Technique. Another location and velocity prediction algorithm based on microphone detection of supersonic shock waves was developed and used on Yuma Proving Ground (YPG) test ranges (Stallings 1992). Stallings' technique does not require any special microphone placement. The only requirement to locate projectiles and determine velocity is to have at least 4 noncoplanar microphones. Three of the microphones form a triangle in the target plane, and the other microphone is placed in front of the others. Generally, the more microphones used, the better the location accuracy that can be provided. Better location accuracy is also accomplished when the microphones lie close to the target plane and the hits lie in or near the center of the microphone array. The input variables for accurate round location are meteorological data (to include temperature, humidity, wind speed, and wind direction), a velocity estimate, fall angle estimate, target position, gun position, microphone positions, and microphone trigger times. Location errors magnify when input values are not precisely known. Stallings showed, through YPG tests, that errors as small as $2-3 \mathrm{~cm}$ are common.

Stallings' technique first assumes that the projectile hits the target at the center of mass. The theoretical times that the shock wave was detected by each microphone are then calculated. The actual microphone times are compared to the calculated times. The output variables, projectile location, and velocity are incrementally adjusted around the initial guess until the difference between calculated and actual times is within a predetermined tolerance. This is a time-intensive algorithm that converges to the solution in approximately 30 s on a fast personal computer. The algorithm could be optimized to reduce inefficiencies in the program. There are two iterative nested processes within the algorithm. Stallings believes that one of these can be eliminated to accelerate the program.

The Stallings algorithm cannot predict location in real time. Real time results are essential for proper integration with RETS. Since this technique was developed for test ranges, many of the input variables are known to a large accuracy at the testing range. There is no knowledge of the gun firing position on the training range. For the purpose of RDS, the gun position represents the greatest source of error for this technique and would significantly impact scoring accuracy.

## 4. LIVE-FIRE TESTING

A series of live-fire tests was designed to investigate the hypothesis that acoustic signatures could be used to discriminate round types. The smallest and largest projectiles within the test matrix were selected for the initial test of the feasibility of the hypothesis. The logic was that if the data obtained during the initial testing showed that the characteristics of the respective N -Waves permitted discrimination between the projectile extremes, then, and only then, would a second live-fire test be conducted. The second livefire test would be a data collection effort to compile the N -Wave data of the remaining projectiles at different intervals of velocity. Once the data were collected and analyzed, an algorithm would be developed to produce round discrimination. Subsequently, the algorithm would be integrated with a computer/breadboard. A third live-fire test would be conducted to validate the algorithm and the RDS breadboard's performance. Needless to say, the success of this last test series was highly dependent on the results obtained within the feasibility and data collection tests.

These tests were formally described as the feasibility test, data collection test, and verification/validation test. The breakdown of rounds and ranges used within each test series is given in Table 2.

The data collected during the first two parts of the live-fire program were used to standardize the method of collecting the N -Wave data and the specific parameters used in the N -Wave calculation. To increase the amount of data acquired, several sensors were used for each shot. The parameters considered for the N-Wave calculations were: ambient air temperature, projectile velocity, caliber, length, and offset distance. Each live-fire test setup consisted of a fixed reference target and five high-fidelity microphones arranged such that the projected distance form the target center was $1,3,6,9$, and 12 m , respectively, to the microphones. Each projectile hit on the target was scored using a video scoring system, and the offset distance from the projectile to the microphones was calculated, generating one parameter for consideration. The projectile's velocity was measured with a Weibel radar system, designed specifically for projectile velocity measurement. The dimensions of each round were known, and meteorological data were measured.

To ensure that there was no unintentional biasing of the data, the order of fire was randomized to the extent practical. Theoretically, if an experiment involving different round types is conducted, the test

Table 2. Proposed Round and Firing Range Breakdown for Each Test

| Test Type | Round Type | Range <br> (m) |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Feasibility | 120-mm M865 | 400 |  | 2,500 |
|  | 120-mm M831 | 400 |  | 2,500 |
|  | $105-\mathrm{mm}$ M 724 | 400 |  | 2,500 |
|  | 105-mm M 490 | 400 |  | 2,500 |
|  | $25-\mathrm{mm}$ M910 | 400 |  | 2,000 |
|  | 25-mm M793 | 400 |  | 2,000 |
| Data Collection | $120-\mathrm{mm}$ M 865 |  | 1,250 |  |
|  | $120-\mathrm{mm} \mathrm{M} 831$ |  | 1,250 |  |
|  | $105-\mathrm{mm}$ M 724 |  | 1,250 |  |
|  | $105-\mathrm{mm}$ M490 |  | 1,250 |  |
|  | $35-\mathrm{mm}$ DM18 | 400 | 1,250 |  |
|  | 35-mm DM68 | 400 | 1,250 |  |
|  | 25-mm M910 |  | 1,250 | 2,500 |
|  | $25-\mathrm{mm}$ M793 |  | 1,250 | 2,500 |
|  | 12.7 -mm M33 | 400 | 900 |  |
|  | $7.62-\mathrm{mm}$ M59 | 400 | 900 |  |
| Verification/Validation | $120-\mathrm{mm}$ M865 | TBD ${ }^{\text {a }}$ |  |  |
|  | $120-\mathrm{mm} \mathrm{M} 831$ |  |  |  |
|  | $105-\mathrm{mm} \mathrm{M} 724$ |  |  |  |
|  | $105-\mathrm{mm} \mathrm{M} 490$ |  |  |  |
|  | $35-\mathrm{mm}$ DM18 |  |  |  |
|  | 35-mm DM68 |  |  |  |
|  | $25-\mathrm{mm}$ M910 |  |  |  |
|  | 25-mm M793 |  |  |  |
|  | $12.7-\mathrm{mm}$ M33 |  |  |  |
|  | 7.62-mm M59 |  |  |  |

${ }^{\mathrm{a}}$ To be determined.
conditions should be identical for all round types so that the round differences can be detected. Since reality dictates that the process of extracting data is never the same each time, randomization reduces the average effect of any irrelevant factors, and the errors in the response are independently and randomly distributed over the population. Conversely, if rounds are systematically tested, i.e., all of a particular round are tested at one time, then the true response of that round cannot be separated from the extraneous factors such as weather conditions that contributed to the response.
4.1 Feasibility Test. The first part of the live-fire program was intended to be a small effort. Originally, the $120-\mathrm{mm}$ HEAT and KE training projectiles were scheduled to be fired at the closest and farthest engagement distances, and the data were compared to the $25-\mathrm{mm}$ armor-piercing (AP) and HE training projectiles at their extreme engagement distances. The extremes of the test matrix were designed to envelop the velocity expected in real use. According to the simplified N-Wave calculations, the N Wave pressure and time duration produced from the largest projectile at its slowest velocity, far from the microphone, was expected to approach the N -Wave pressure and time duration of the smallest projectile at its fastest velocity, close to the microphone. If the round type of these two projectiles could be discriminated, round discrimination using N -Wave data would be considered feasible.
4.1.1 Test Purpose. The purpose of this test was to determine if the N -Wave data collected with a particular configuration of high-fidelity microphones could be used to discriminate the round types fired. The largest projectile, the $120-\mathrm{mm}$ M831, at its slowest velocity was to be compared to the $25-\mathrm{mm}$ M910 at its fastest velocity. If the N-Wave data from the same offset distance were separable, then these N -Waves of supersonic projectiles could be used to perform round discrimination at the target.

Due to the extremely high operational cost of M1/M1A1 tanks, and the prospect of incurring prohibitively high maintenance costs at the turn of the fiscal year, it was decided to advance a portion of the data collection effort into the feasibility study. Consequently, all $120-\mathrm{mm}, 105-\mathrm{mm}$, and $25-\mathrm{mm}$ projectiles were fired during the feasibility test. The $120-\mathrm{mm}$ rounds were fired from an M1A1 Abrams tank, the $105-\mathrm{mm}$ projectiles were fired from a M60A3 tank, and all the $25-\mathrm{mm}$ rounds were fired from an M2 BFV. Table 3 describes the actual rounds fired during the feasibility test. With the modification of the test schedule, the sample set increased by $50 \%$ and would provide better parameter estimates in the statistical analysis for this phase of the test program.

Table 3. Actual Round and Firing Range Breakdown for the Feasibility Test

| Round Type | Range <br> $(\mathrm{m})$ |  |  |
| :---: | :---: | :---: | :---: |
| 120-mm M865 | 400 | 1,000 | 1,700 |
| 120-mm M831 | 400 | 1,000 | 1,700 |
| 25-mm M910 | 400 | 1,000 | 1,400 |
| 25-mm M793 | 400 | 1,000 | 1,400 |
| 105-mm M724 | 400 | 1,000 | 1,700 |
| 105-mm M490 | 400 | 1,000 | 1,700 |

4.1.2 N-Wave Characteristics. The acoustic signature for each projectile was studied specifically for seven different characteristics. These were positive peak pressure, negative peak pressure, positive phase duration, negative phase duration, total duration, peak net pressure impulse, and peak absolute pressure impulse. The variables are illustrated in Figure 7. The data were compared to N-Wave formulas and analyzed using advanced statistical methods. Shadowgraphs of the projectiles in midflight from previous tests were compared to the N -Wave data to relate the signature features to the surface features of the projectiles. This comparison helped determine if certain N -Wave features were truly dependent on the projectile geometry or were the results of an environmental influence, such as a ground reflection.

The seven characteristics of the acoustic signature were essential to the N -Wave data comparisons. The N -Wave formulae were used as a theoretical guide to help test the hypothesis of round discrimination. The real N -Wave data were used to empirically refine the N -Wave formulae. These formulae provided an engineering basis for the round discrimination algorithm used on the breadboard.
4.1.3 Data Acquisition and Reduction. The data acquisition system consisted of two systems for recording and one system for sensing. The sensors were high-fidelity microphones able to operate in the range of overpressures encountered. These sensors were high-value items and were not intended as an all-weather solution to a fielded RDS. The priority lay in obtaining high-fidelity signals to accurately record the N -Wave phenomenon. The N -Wave data from several projectiles, at several offset distances, traveling at various velocities, had to be studied and analyzed. The two recording systems served a dual purpose. Each system had a specific deficiency-poor resolution in either time or voltage levels. Each was able to complement the other in that respect. The secondary purpose was to provide a backup recording system in the event of a malfunction during the live-fire test.

Reduction of the data was performed on a personal computer (PC). The data from each channel were converted into ASCII files. These files were read into a data processing program called DADisp (DSP Development Corporation 1991). This software had the capability to read the data, convert them into engineering units, and perform a series of calculations. Among those were the calculation of net pressure impulse and absolute pressure impulse. Along with these calculations and plots, DADisp helped to determine the pressure peaks and durations. At times, the signals were clipped. In an effort to maximize the resolution in the ordinate, the recording window was set as small as possible. At times, the recording devices were preset on low. As a result, hard data on the maximum levels were lost. DADisp software helped curve-fit the peaks, restoring the data with at least $\pm 10 \%$ accuracy.

(s)


Time (s)

(s)

(s)

Figure 7. Seven parametric features of the N-Wave.
4.1.4 Instrumentation. $\mathrm{B} \& \mathrm{~K}$ microphones are high-grade laboratory instruments with the following specifications: sensitivity of $-56-\mathrm{dB}$ sound pressure level (SPL), flat frequency response from less than 5 Hz to 50 kHz , and dynamic range up to 178 dB SPL with $3 \%$ distortion. Each B\&K microphone unit is comprised of a type $41361 / 4-\mathrm{in}$ microphone, a type 2639 preamplifier, and a type 2801 AC or a type 2804 DC power supply. The cost per unit is $\$ 3.5 \mathrm{k}-\$ 4 \mathrm{k}$ in small quantities.

The outputs of the microphones were connected by $150-\mathrm{ft}$ BNC cables to three TEAC digital audio tape (DAT) recorders and a Hewlett-Packard (HP) digital oscilloscope, model no. HP 54112D, controlled by a PC located behind a berm. The three DAT recorders had a total of six wide-band channels (two channels per DAT) with $48-\mathrm{kHz}$ sampling rate and 14 -bit resolution per channel. The HP digital oscilloscope had four input channels with $1-\mathrm{MHz}$ sampling rate per channel and 8 -bit resolution per channel. The PC communicated with the oscilloscope through the IEEE port. A data acquisition program written in C language was developed to automatically dump 64 kB of data per channel onto the PC's hard disk when the scope was triggered and to reset the scope to wait for the next trigger. Both types of recording instruments were used to provide both time resolution and amplitude resolution.
4.1.5 Acoustic Signatures. Live-fire tests were conducted at the H -field facility at APG, Edgewood Area (EA). Data collected during the feasibility test are summarized in Appendix A. The target was positioned up on top of a berm at the end of the field. The firing platform was moved to each firing station. After some calibration rounds were fired, the testing for each projectile type was performed. A cursory look at the data, while still on the field, indicated that the signals for each round type was distinct. Qualitatively, it was surmised that round discrimination was feasible. A subsequent closer look, within the laboratory confirmed this fact, quantitatively, and is discussed in section 5.

The M831 and M490 rounds possessed distinctly different N-Wave shapes. The M490 round produced the classic N-Wave, as seen in Figure 8, while the M831 round had several interval shocks on the negative phase of the N -Wave. As the offset distance varied, the level and occurrence of the shocks changed. This indicated that the shock was produced from a surface feature and was merging with the tail shock. The time relation of shock travel and the distance to the ground disputed the idea that it was a ground reflection (Ritzel and Gottlieb 1982). These observations were distinct to the M831 round and not the M865.



Figure 8. M831 and M490 comparisons.

It was speculated that these pressure differences are due to shock interaction with the fins, and the nonogival geometry of the M831 round. The M831 round has the stand-off fuse and the concave taper to the body, as opposed to the convex taper of the ogive. The body slims down aft of the body for aerodynamic flight. The bottle nose feature may create a separation, causing a shock, unless it is isentropically ramped. If the surface aft of the body turning away from the flow is of sufficient gradient, another separation would occur, creating more shocks. A detailed summary of the resultant data is included in Appendix B. Figure 9 shows the same comparison between the M793 and M910 fired from a BFV. The slimmer AP rounds shows the classic N -Wave while the HE round has the secondary tail shock.


Figure 9. M793 and M910 signature comparisons.
4.1.6 Round Location and Velocity Determination Data. The RDS acoustic location system consisted of six electret microphones. Each microphone was connected so that it acted as a variable resistor when exposed to sound. In response to the acoustic shock wave, the current in the microphone wires increased.

The current was converted to a voltage signal by a signal conditioning card. The six pulses were recorded on two DATs. LM1, LM2, and LM3 were recorded on DAT 1, and LM4, LM5, LM6, and LM2 were recorded on DAT 2. LM2 was recorded on both DATs so that all six microphone trigger times could be related to one time base. The DAT clock was synchronized to the Weibel radar clock. Each channel was played back through a Nicolet digital oscilloscope and manually reduced for the time passed until shock detection (see Appendix C). The accuracy of these times was within $\pm 21 \mu \mathrm{~s}$. The time difference pulses $\mathrm{T}_{1}-\mathrm{T}_{5}$ were then calculated.
4.2 Data Collection Test. The result of the feasibility test suggested that round discrimination using acoustic signatures was possible and the data collection test should proceed. The ammunition used in the data collection test is shown in Table 4. This portion of the project was originally intended to be the major data collection effort. However, since all of the main gun data needed for the M60A3, M1/A1, and M2 were collected during the feasibility test, all that remained were the TPGID and small arms.

Table 4. Actual Breakdown of Rounds and Ranges for Data Collection Test

| Round Type | Range <br> (m) |  |  |
| :---: | :---: | :---: | :---: |
| 35-mm DM18 | 400 | 1,000 | 1,700 |
| 35-mm DM68 | 400 | 1,000 | 1,700 |
| 35-mm TPL-T | 400 | 1,000 | 1,400 |
| 12.7-mm M33 | 400 | 1,000 |  |
| 12.7-mm M17 | 400 | 1,000 |  |
| 7.62-mm M59 | 400 | 600 | 800 |
| 7.62-mm M62 | 400 | 600 | 800 |

The small arms ammunition used on a training range is either ball or tracer. The tracer ammunition was studied as an independent round type since the effect of the tracer was postulated to have an effect on the N-Wave. It was theorized that the pyrotechnic material would increase the duration since it would add energy to the wake. The degree of effect was pure conjecture. Only one type of $35-\mathrm{mm}$ TPGID was supposed to be tested. Before the data collection test occurred, two new types of TPGID rounds, DM68 and the TPL-T, were obtained for testing. These were surplus obtained from a lot which had just undergone proof-testing with the U.S. Army's Combat Systems Test Activity (CSTA). These rounds were tested independently of the DM18. Their diameter and length were unchanged, but the surface features
were different. The DM68 and the TPL-T have a sharp pointed cone attached to a cylinder body, as opposed to the DM18, which has an ogive shape. It was speculated that there would be a slight change in the N -Wave but that the change would not be significant.

The purpose of the data collection test was to complete the database of projectile signatures expected on a U.S. Army training range. These signatures were needed to develop the RDS algorithm and form the basis of all assumptions and work. Once the data were collected and reduced, a major milestone in the project would have been reached.

To perform the test, an M1A1 Abrams tank was needed to fire the TPGID ammunition. A Mann barrel, a device constructed for precise single-shot testing of small arms ammunition, was used to perform the $7.62-\mathrm{mm}$ and $12.7-\mathrm{mm}$ shots. The Mann barrel consisted of a towed gun carriage and two barrel assemblies, one for each caliber.

The effort to field a calibrated pressure sensor was deemed impractical after considering the number of sensors needed to cover all the U.S. Army live-fire gunnery ranges. This made any parameter not dependent on the pressure levels very attractive. The total duration was one parameter that seemed to be most consistent, and discriminating. The same seven variables examined in the feasibility test were studied in the data collection effort, in the likelihood that the total duration failed as a discriminator with inclusion of the additional data.

The same two recording systems used during the feasibility test were employed for the data collection test. A third recorder was added. This was a digital transient data recorder card mounted in a PC. It had 12 -bit resolution in the ordinate, with a $250-\mathrm{kHz}$ sampling rate. This was deemed sufficient response for the $7.62-\mathrm{mm}$ rounds. The resultant plots were much smoother in appearance, and the accuracy of the data was enhanced.

Five B\&K high-fidelity microphones were set up at $1 \mathrm{~m}, 3 \mathrm{~m}, 6 \mathrm{~m}, 9 \mathrm{~m}$, and 12 m , respectively, to the left of the bull's-eye in front of the target. In addition, three low-cost ( $\$ 150.00$ each) high-fidelity microphones from Countryman were set up next to the $\mathrm{B} \& \mathrm{~K}$ microphones at $3 \mathrm{~m}, 6 \mathrm{~m}$, and 9 m . The Countryman microphones were much more ruggedized and rain resistant than the B\&Ks.

A new data collection system was used. The system consisted of a 486 Extended Industry Standard Architecture (EISA) computer, two four-channel 1-MHz EISA data acquisition cards, and a graphical programming software tool called LabView for Windows. The system emulated an eight-channel highspeed ( 250 kHz per channel) digital oscilloscope with the programming capabilities of a PC. The acoustic signatures of the microphones were automatically captured and displayed on the monitor, scaled, truncated, and stored on the hard disk after each tank round was fired. This new system greatly reduced the data processing and reduction time. The same four-channel $1-\mathrm{MHz} \mathrm{HP}$ digital oscilloscope was used as a backup system.

Post-test data analysis showed that the Countryman microphones did not have the $65-\mathrm{dB}$ dynamic range necessary to capture the supersonic shock wave of large projectiles. For small rounds such as 12.7 mm and the 7.62 mm , the Countryman microphones responded well.

A second series of live-fire tests was also conducted at H-Field facility at the APG, EA. Data from these tests are compiled in Appendix D. The same equipment used during the feasibility test was employed during the data collection test. The target was positioned on top of the same berm used during the feasibility tests. The firing platforms were moved to specific firing stations. After some calibration rounds were fired, the testing for each projectile type was performed. An immediate look at the data on the field indicated that the signals for the small-caliber rounds were different from the main gun rounds. This observation was subsequently verified during the detailed analysis.

The bulk of the data considered was from the transient data recorders. The resolution in the abscissa and ordinate made the data optimal when performing data reduction. Figure 10 shows the typical plot of a $35-\mathrm{mm}$ DM18 projectile raw data, fired from $1,700 \mathrm{~m}$ at the $9-\mathrm{m}$ offset distance.* See Appendix E for details. Appendix F summarizes the microphone positions and associated shock detection times.

[^0]
(s)

Figure 10. Raw data of $35-\mathrm{mm}$ DM18 at $9-\mathrm{m}$ offset, fired from $1,700 \mathrm{~m}$.

## 5. ANALYSIS OF LIVE-FIRE DATA

The live-fire data was analyzed using two distinct approaches. The first was an engineering approach, based on Whithams formula, that described a mathematical model which related the physical properties and events. This model was thought to be adequate for predicting occurrences within and beyond the test matrix. The second approach used advanced statistical analysis. By analyzing the data on the variables, a empirical model was constructed to predict within the test matrix.
5.1 Variables Investigated. The seven variables investigated were as follows: positive peak pressure, negative peak pressure, positive phase duration, negative phase duration, total duration, peak net pressure impulse, and peak absolute pressure impulse. It was hypothesized that the positive peak pressure and negative peak pressure generated from the main gun rounds would be so much stronger than the BFV rounds that merely sensing the levels would provide discrimination. Subsequent calculations negated this hypothesis. A small round close to the sensor would appear stronger than a large round far from the sensor. The drop in peak pressure with distance was estimated to be roughly to the power of $1 / 5$ th.

The predictions of time durations were greatly varied over round type. According to the time duration formula, the total duration is strongly related to the diameter of the projectile. Since the rounds all have distinct diameters, and the other variables of the time duration formula can be quantified, time duration should be a pronounced discriminator. Time duration does not require any calibration. All that is needed is an accurate, high-speed clock. The intervals of positive and negative pressure phase time durations can also be used to identify the originator of an N -Wave.

There was much speculation that the environment would significantly influence the variables mentioned. The temperature of the ambient air, humidity, air density, wind, and dust were thought to be capable of distorting the perfect N -Wave such that the N -Wave of a small round fired on a cold day at sea level might appear the same as a large projectile N -Wave fired at high altitude on a hot day. To attempt to evaluate the N -Wave, a measure of the energy imparted to the atmosphere was used. The total duration pressure impulse is simply the integral of the entire N -Wave pressure curve. The value of the pressure impulse at some point in time along the N -Wave is the net value of energy contributed to the local environment. As the projectile flies through space, the KE is transferred by the viscous effects of the surrounding fluid. The majority of the energy transfer is performed in the nearly isentropic compression of the local air, thus the bow and tail shock. A small percentage of the energy is consumed in viscous losses, such as the trailing wake eddies, flow separation, friction heating of the projectile, and the losses incurred by a not perfectly isentropic compression of the air.

The total duration pressure impulse shows the entire amount of net energy imparted to the surrounding fluid. The negative value at the end of the total duration pressure impulse curve is due to energy loss to the surrounding fluid. The projectile passes through a point in space and momentarily displaces the air. The energy transferred to the nearly isentropic bow shock radiates from the bow. The air moves a little, but the energy in the shock travels at the local speed of sound. As the projectile passes, the local energy state of the air returns to the original level, plus any energy imparted to it by projectile kinetic losses. The air shocks back into the wake as the wake eddies dissipate energy and collapse. This marks the end of the energy transference. The net effect is a negative value. The value should be approximately equal to the losses imparted to the air, which result in local heating of the air.

The peak value of the total duration pressure impulse curve demonstrates the total duration energy transferred from the travelling projectile to the local air, at that instant in time. The energy transfer of the projectile is strictly a function of speed and projectile shape. Ambient air conditions have a negligible
effect on this value. As a result, a projectile could be discriminated by this feature without regard to the environmental conditions. Another method of using this variable is to consider the absolute contribution of energy transference.

The absolute pressure impulse is taken when considering all the values of the N -Wave as positive only. In this manner, the absolute total duration of energy transfer is considered. This works such that any losses in the projectile's flight are included into this value and can further separate the groups of projectiles for discrimination.

Three different engineering methods of analyzing the data were pursued. The first method was the use of the seven variables in conjunction with the time duration and the overpressure formulations. This method would provide the discriminant algorithm with a theoretically derived mathematical model that employed thermodynamic relationships. This model could be used to discriminate rounds if the live-fire data matched the calculated results. If not, a modification of this formulation could be performed, resulting in quasi-empirical formulation.

The other two methods were similar to each other in process. A Fourier transform of the data could produce key frequency features that could be used to discriminate the projectiles. Another method of transfer analysis is called Wavelet analysis. Using this method, the signal is transferred into the domain of a discrete function, rather than the continuous function of the frequency domain. By picking a discrete function, the signal is transferred by taking the convolution integral. This method works if there is a specific shape to each N -Wave when normalized in the abscissa and ordinate.

The results from the live-fire data collection efforts were N -Waves that were extremely similar in shape. The Wavelet theory would not work since the normalized shape of the N -Waves were so closely matched. A Fourier analysis was initially performed (Hulet 1992), showing extremely promising results (see Figures 11-14). The peak frequency for the 12.7 mm was 3.58 kHz ; the 7.62 mm was 4.15 kHz . Unfortunately the data had undergone some smoothing process, and the resulting Fourier analysis yielded artificial suppressing frequency peaks. When the ARL live-fire data were transformed, the results did not yield adequate discriminants. The Fourier transform was shown to relate only to the duration intervals.

Since the durations were strongly related to a rounds specific dimensions and the transformation techniques were clearly influenced by the durations, the time duration formula was selected as the best


Figure 11. $7.62-\mathrm{mm}$ projectile at $1,500 \mathrm{~m}$.


Figure 12. FFT of $7.62-\mathrm{mm}$ projectile at $1,500 \mathrm{~m}$.


Figure 13. $12.7-\mathrm{mm}$ projectile at $1,500 \mathrm{~m}$.


Figure 14. FFT of $12.7-\mathrm{mm}$ projectile at $1,500 \mathrm{~m}$.
possible, practical method of discrimination. The need to calibrate sensitive pressure gauges for a mass production item was impractical. Therefore, all the variables that required pressure levels, such as positive and negative pressure, peak value of total duration pressure impulse, total duration, and absolute pressure impulse, were disregarded. These data were retained for use in the event that the time durations could not be used to perform a high rate of round discrimination.

The total time duration was compared to the data and found to compare well. The resulting computed durations were constantly proportional to the data. This indicates that the earlier assumption, that the formula could be applied to large-caliber, non-ogival-shaped projectiles was good. The fairly constant proportionality for each projectile resulted in a stochastic modification of the duration formula with a shape constant.

### 5.2 Feasibility Study.

5.2.1 Live-Fire Data. An empirical model was developed from the feasibility test data to determine the feasibility of round discrimination. The following sections describe the data analyzed and statistical tests implemented. The analysis begins with examination of the $1,000-\mathrm{m}$ data and ends with three models developed using a statistical tool known as discriminant analysis. The number of rounds in the analysis from each round type is listed in Table 5. As described earlier, for each round fired, five signatures were collected from microphones placed $1,3,6,9$, and 12 m , respectively, from the center of the target.

Table 5. Number of Rounds Analyzed in Feasibility Study

| Distance <br> $(\mathrm{m})$ | 25 mm |  | 105 mm |  | 120 mm |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | M793 | M910 | M490 | M724 | M831 | M865 |
| 400 | 4 | 3 | 3 | 2 | 3 | 3 |
| 1,000 | 3 | 3 | 3 | 3 | 3 | 3 |
| 1,400 | 3 | 3 | - | - | - | - |
| 1,700 | - | - | 3 | 3 | 3 | 2 |

The 7th ATC's original minimum requirement was to distinguish between rounds $<30 \mathrm{~mm}$ from those $>30 \mathrm{~mm}$. A more ambitious task was undertaken to try to distinguish among all the round types. This goal produced six categories for discrimination: $25-\mathrm{mm}$ KE, $25-\mathrm{mm}$ HEI, $105-\mathrm{mm} \mathrm{KE}, 105-\mathrm{mm}$ HEAT,
$120-\mathrm{mm}$ KE, and $120-\mathrm{mm}$ HEAT. The data collected from the signatures, location study, and Weibel radar were all candidates for inclusion in the models for discrimination.
5.2.2 1,000-m Data. Preliminary analyses to determine the feasibility of discriminating different round types were initially performed on the $1,000-\mathrm{m}$ data. Statistical tests were performed on each variable, and at each microphone separately. These tests sought to determine if one of the variables could be used to discriminate the six round types. These tests also sought to determine the optimal microphone distance for future implementation.

The $1-\mathrm{m}$ microphone often produced saturated signals. The actual offset distance fell into four regions. Region 1, data collected from both the $1-\mathrm{m}$ and $3-\mathrm{m}$ microphones, had offset distances less than 4 m . Region 2, data collected from the $6-\mathrm{m}$ microphone, had offset distances from 4 m to 7 m . Region 3 has offset distances $>7 \mathrm{~m}$ and up to 10 m . Region 4 offset distances were $>10 \mathrm{~m}$.

The Kruskal-Wallis test was used to test the hypothesis that the six round types have equivalent mean values in comparison to the alternative, which is that at least two round types differ. This nonparametric test performed an analysis on the ranks of the data rather than the actual data values. The ranks started with 1 for the smallest value among the six round types. The largest value from all six round types received a rank of N , the number of test data from the six populations. The advantage of the nonparametric test was that the test did not require assumptions of normality of the data or homogeneity of variances (HOV)-that is, equality of variance among the groups. Appendix M provides an example of implementing the Kruskal-Wallis test and provides detailed results of the test for each variable.

The results of the Kruskal-Wallis test performed on each variable indicate that at least two round types differed from each other in each of the four regions. To determine exactly which round types differed, the corresponding multiple comparison test was implemented. In summary, most of the variables distinguished between the small and large-caliber rounds-that is, $<30 \mathrm{~mm}$ vs. $>30 \mathrm{~mm}$-satisfying the 7th ATC's minimum requirement. The only variable that did not was negative phase duration in regions 3 and 4.

All the other variables in each region distinguished between large HEAT and large KE rounds. The $105-\mathrm{mm}$ and $120-\mathrm{mm}$ training HEAT rounds were not statistically different from each other, nor were the
$105-\mathrm{mm}$ and $120-\mathrm{mm}$ training KE rounds. But the $105-\mathrm{mm}$ and $120-\mathrm{mm}$ training HEAT rounds were statistically different from the $105-\mathrm{mm}$ and $120-\mathrm{mm}$ training KE rounds.

For some variables, the two smaller-caliber rounds were distinguishable from each other. These results are summarized with the following notation:

$$
25 \mathrm{~K} \neq 25 \mathrm{H} \neq(105 \mathrm{~K}=120 \mathrm{~K}) \neq(105 \mathrm{H}=120 \mathrm{H}) .
$$

The round types are listed in order from lowest average rank to the highest. Parentheses around two round types indicate there is no significant difference between the rounds. What the nonparametric analyses indicated was that many of the variables under consideration were good candidates for discriminating at least the small-caliber rounds from the large-caliber rounds for $1,000-\mathrm{m}$ data. The duration and pressure impulse values were good for discriminating the rounds in the four categories grouped previously (i.e., small KE, small HEAT, large KE, and large HEAT). The first region (offset distance $<4 \mathrm{~m}$ ), representing data collected close to the flight of the round, was the hardest region in which to discriminate. The facts provided a guide to the placement of the microphones for future tests.
5.2.3 Analysis of Data From All Ranges. The preliminary analysis of the data at the $1,000-\mathrm{m}$ range indicated that several of the variables were independently able to separate the round types. The goal was to find one or more variables that could separate the round types and was insensitive to range. As mentioned in the previous analyses, it was difficult in some cases to separate the M724 from the M865 rounds and difficult to separate the M490 and the M831 rounds from each other. Therefore, in the next analyses, the discrimination was among 4 groups (not 6): M910, M793, M724/M865, and M490/M831.

- Visual Inspections. Various plots of the signature variables of interest vs. microphone distance were examined to determine if there were obvious trends in the data that separated the round types, independent of the range. Positive peak pressure was plotted in Figure 15. Some separation in the data between the large-caliber rounds and the small-caliber rounds was observed. However, among the large-caliber rounds, separating the HEAT from the KE rounds over all the distances is not easy. This indicated that positive peak pressure is sensitive to range and would not be a good candidate for discrimination.

Upon examining the plots of total duration vs. microphone offset distance for each firing position (range), little change in the shape of the curves was observed. Figure 16 shows all the ranges together


Figure 15. Positive peak pressure vs. microphone distance for all firing positions.


Figure 16. Total duration vs. microphone distance for all firing positions.
on one graph. This plot suggested that total duration is not sensitive to range and is a good candidate for discriminating round types. If microphone offset distance is known, the type of round can be determined based on the magnitude of the total duration. In some cases, the round can be determined independent of the microphone offset distance. For instance, if the total duration were $>1,500 \mu \mathrm{~s}$, the round would be a large HEAT round (M831 or M490), independent of the microphone offset distance. However, if the total duration were $600 \mu \mathrm{~s}$, one could not be certain if it were a large HEAT round with a microphone offset distance $<2 \mathrm{~m}$, or a small HEAT round, M793, with a microphone offset distance of approximately 12 m . These observations led to conclude that total duration alone cannot be use to discriminate among the rounds, and a more objective and quantifiable way to combine variables and separate the groups was needed.

### 5.2.4 Discriminant Analysis for All Ranges.

- General. Discriminant analysis is a statistical technique which uses linear combinations of variables to determine if one or more variables will categorize the populations (round types), and it is described by Marriott (1990) in the following way:

Given a set of multivariate observations on samples, known with certainty to come from two or more populations, the problem is to set up some rule which will allocate further individuals to the correct population of origin with minimal probability of misclassification. This problem and sundry elaboration of it give rise to discriminatory analysis.

In linear regression, one develops a linear model with one or more explanatory (independent) variables $x_{i}$ 's to describe the response (dependent) variable $y$. A linear equation is of the form:

$$
\mathrm{y}=\mathrm{B}_{0}+\mathrm{B}_{1} \mathrm{x}_{1}+\mathrm{B}_{2} \mathrm{x}_{2}+\mathrm{B}_{3} \mathrm{x}_{3}+\mathrm{B}_{4} \mathrm{x}_{4}+\ldots . .
$$

where the coefficients $\mathrm{B}_{\mathrm{i}}$ 's are linear. The $\mathrm{x}_{\mathrm{i}}$ 's can take a nonlinear form such as x raised to a power or a functional form as the natural logarithm or exponent.

In the application of categorizing (or classifying) the round into the four groups (M910, M793, M724/M865, and M490/M831), round type is not a measurable response; therefore, univariate regression
analysis is not appropriate. The multivariate tool, discriminant analysis, allows us to form one or more functions, where the value of the function(s), in combination, categorizes the round types.

$$
\begin{gathered}
f_{1}=a_{0}+a_{1} x_{1}+a_{2} x_{2}+a_{3} x_{3}+a_{4} x_{4}+\ldots \\
f_{2}=b_{0}+b_{1} x_{1}+b_{2} x_{2}+b_{3} x_{3}+b_{4} x_{4}+\ldots \\
f_{3}=c_{0}+c_{1} x_{1}+c_{2} x_{2}+c_{3} x_{3}+c_{4} x_{4}+\ldots \\
\cdot \\
\cdot \\
\cdot \\
f_{n}=z_{0}+z_{1} x_{1}+z_{2} x_{2}+z_{3} x_{3}+z_{4} x_{4}+\ldots .
\end{gathered}
$$

Only variables that are not highly correlated with one another and contribute significantly are selected into the model. Forming the functions is performed in a stepwise fashion, with the most "significant variable" that most separates (and therefore discriminates) among the round types entering the model first. Given that this first variable is in the model, the next variable, which is not highly correlated with the variable(s) already in the model and would contribute most from the remaining significant variables, is entered into the model. This process continues until no variable can satisfy the two aforementioned conditions.

Several criteria are available for entering significant variables into the model (SPSS Inc. 1990a). Wilk's Lambda was used in this analysis. Wilk's Lambda is the ratio of the within-groups sum of squares to the total sum of squares when the discriminant scores (the $f_{i}$ 's) are the dependent variables, and the group is the independent variable.

The tolerance for correlation of variables was set at 0.1 . Tolerance is the amount of linear association between the incoming variable and the variable(s) already in the model. It is equal to $1-\mathrm{R}_{\mathrm{i}}{ }^{2}$, where $\mathrm{R}_{\mathrm{i}}{ }^{2}$ is the squared multiple correlation coefficient. Variables with small tolerance values (and therefore large $R_{i}{ }^{2}$ values) are not entered into the model.

These analyses were performed using a statistical software package called SPSS. With a set of functions to characterize the discrimination, a territorial map of the categories of at most two dimensions is provided. This procedure is explained in more detail, with actual data from the test program, in the next paragraph.

- Discriminatory Functions for Live Fire Data Set. Wilk's Lambda criterion was implemented for the model development of the live fire data set. Total duration was the first variable to enter the model and is the one variable that best separates the round types into their appropriate groups. As described earlier, total duration alone cannot guarantee correct classification of all the rounds. The stepwise process continued with the following variables:


## 1. Total Duration

2. Peak of Absolute Pressure Impulse
3. Velocity
4. Microphonic Off-Set Distance
5. Negative Peak Pressure
6. Positive Peak Pressure
7. Subtotal Duration (addition of positive and negative phases).

These 7 variables were able to correctly classify $99.50 \%$ of the round types. As shown in Table 6. There was one misclassification: M793 classified as M910.

Table 6. Classification Result for Original Seven Variables

| Actual Group | No. of Cases | Predicted Group Membership |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\begin{array}{r} 1 \\ \text { M910 } \\ \hline \end{array}$ | $\begin{gathered} 2 \\ \mathrm{M} 793 \\ \hline \end{gathered}$ | $\begin{gathered} 3 \\ \text { M724/M865 } \\ \hline \end{gathered}$ | $\stackrel{4}{\text { M490/M831 }}$ |
| 1. M910 | 36 | $\begin{gathered} 36 \\ 100 \% \end{gathered}$ |  |  |  |
| 2. M793 | 36 |  | $\begin{gathered} 35 \\ 97.2 \% \end{gathered}$ |  |  |
| 3. M724/M865 | 61 |  |  | $\begin{gathered} 61 \\ 100 \% \end{gathered}$ |  |
| 4. M490/M83 | 69 |  |  |  | $\begin{gathered} 69 \\ 100 \% \end{gathered}$ |

If one looks back at Figure 16 (total duration vs. microphone distance), some curvature in the data is seen. The natural logarithm (In) of total duration will linearize the plot as shown in Figure 17. Repeating the discriminant analysis process, the natural logarithm of total duration is the first variable to enter the model. Continuing the analysis, the model contains the following variables:

1. $\ln$ (Total Duration)
2. Offset Distance
3. Velocity
4. Total Duration
5. Peak of Absolute Pressure Impulse
6. Negative Peak Pressure
7. Peak of Pressure Impulse.


Figure 17. $\ln$ (total duration) vs. microphone distance.

These variables produced all correct classification results. Note that both the natural logarithm and raw units of total duration entered into the model. Although the two are not independent of one another, they pass the tolerance criterion. However, the pooled within-groups correlation between the two is 0.88 . To avoid problems with multicollinearity, an unstable model as a result of highly correlated explanatory variables, it was not advisable to keep both of these variables in the model.

From the seven variables listed previously, subsets of variables were formed in search of smaller models that may be equally successful. Three reduced models will be explained in the following sections.

- Reduced Model A. From the set of variables produced in the aforementioned model, $\ln$ (total duration) and microphone offset distance were used to form a discriminating model that requires just one function:

$$
\begin{equation*}
f_{1}=-84.059+12.774 \ln (\text { Total Duration })-0.523 \text { Microphone Distance. } \tag{15}
\end{equation*}
$$

When the frequency of the $f_{1}$-values are plotted in histogram form, as shown in Figure 18, four clusters are produced, which represent the four groups of interest. The histograms do not overlap, indicating correct classifications for all the groups were achieved. The values on the abscissa are the $\mathrm{f}_{1}$-values. Below that, the class centriod is provided in two forms. The relative location of the centroid compared to the group histogram is given first. Each group is numbered as 1 for $25-\mathrm{mm} \mathrm{KE}, 2$ for $25-\mathrm{mm}$ HEI, 3 for Large KE, and 4 for Large HEAT. The f-value of the centriod is provided next. The limit values are the greatest value of the group starting from the left. These limits provide the following functional mapping:

$$
\begin{align*}
\mathrm{f}_{1} & \leq-9.02 \quad \text { M910 }(25 \mathrm{KE}) \\
-9.02<\mathrm{f}_{1} & \leq-2.39 \quad \text { M793 ( } 25 \mathrm{HEI} \text { ) } \\
-2.39<\mathrm{f}_{1} & \leq 4.78 \quad \text { M724, M865 (Large KE) } \\
\mathrm{f}_{1} & >4.78 \quad \text { M490, M831 (Large HEAT). } . \tag{16}
\end{align*}
$$



Figure 18. Feasibility phase model A: histogram of group classes.

- Reduced Model B. Referring back to the set of seven variables that include ln(total duration), other combinations of variables were considered that would classify all the rounds correctly. Consider the variables $\ln$ (total duration) and velocity. The discriminant analysis requires two functions as shown in equation 17, resulting in $98.03 \%$ of the data correctly classified. Of the misclassified data, one M910 round was classified as an M793, and three M793 rounds were predicted as M910's (see Table 7).

$$
\begin{align*}
& \mathrm{f}_{1}=-42.451+5.994 \ln (\text { Total Duration })+0.00129 \text { Velocity } \\
& \mathrm{f}_{2}=-2.800+0.529 \ln (\text { Total Duration })+0.00650 \text { Velocity. } \tag{17}
\end{align*}
$$

Table 7. Classification Result for $\ln$ (Total Duration) and Velocity.

| Actual Group | No. of Cases | Predicted Group Membership |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\begin{gathered} 1 \\ \text { M910 } \end{gathered}$ | $\begin{gathered} 2 \\ \text { M793 } \end{gathered}$ | $\begin{gathered} 3 \\ \text { M724/M865 } \end{gathered}$ | $\begin{gathered} 4 \\ \text { M490/M831 } \end{gathered}$ |
| 1. M910 | 36 | $\begin{gathered} 35 \\ 97.2 \% \end{gathered}$ |  |  |  |
| 2. M793 | 36 |  | $\begin{gathered} 33 \\ 91.7 \% \end{gathered}$ |  |  |
| 3. M724/M865 | 61 |  |  | $\begin{gathered} 61 \\ 100 \% \end{gathered}$ |  |
| 4. M490/M831 | 69 |  |  |  | $\begin{gathered} 69 \\ 100 \% \end{gathered}$ |

- Limitations on Model B. As mentioned earlier, the data gathered from the $1-\mathrm{m}$ microphone to the target was not reliable. Therefore, only the data collected from a distance $>3 \mathrm{~m}$ was considered in the analysis. With the same variables $\ln$ (total duration) and velocity, $100 \%$ correct classification was achieved with the model.

$$
\begin{align*}
& \mathrm{f}_{1}=-68.539+9.719 \ln (\text { Total Duration })+0.000994 \text { Velocity } \\
& \mathrm{f}_{2}=-3.652-0.397 \ln (\text { Total Duration })+0.00650 \text { Velocity. } \tag{18}
\end{align*}
$$

The data plotted in ( $\mathrm{f} 1, \mathrm{f} 2$ ) space is shown in a scatterplot in Figure 19. The data point is denoted with the group number. The "*" indicates the group centroid. Because of the graphics output from SPSS, overlapping points are not shown. The number of points indicated on the scatterplot may not add up to the number of cases actually analyzed, and misclassified cases may be difficult to visualize. Classification results are provided in the table for models where misclassification occurs.


Figure 19. Feasibility phase model B: scatterplot.

The territorial map in Figure 20 shows the boundaries for each group in $\left(f_{1}, f_{2}\right)$ space. These boundaries are constructed such that any point in a group in the $f_{1}-f_{2}$ plane would be closer to that group centroid than any other group centroid. This is useful for predicting the group membership of an unknown round.


Figure 20. Feasibility phase model B: territorial map.

The process of selecting subsets of variables from the base set continues. The remaining variables: peak of absolute pressure impulse, negative peak, and peak of pressure impulse are difficult to obtain in the field because the microphone would have to be more finely calibrated.

- Reduced Model C. A third and quite different reduced model was considered. Total duration is the single variable that best discriminates among the groups of rounds. If this variable were collected from a microphone placed on each side of the target, collectively the rounds should be identified uniquely. Although our test array of five microphones was on the same side of the target, the data from two microphones were carefully selected to determine if discrimination were possible with nothing more than two total durations. A two-function discrimination model was developed from the 6 - and $12-\mathrm{m}$ microphones:

$$
\begin{align*}
& f_{1}=-17.186+0.0115 \text { Total Duration } 6+0.00331 \text { Total Duration } 12 \\
& f_{2}=-0.0887-0.0317 \text { Total Duration } 6+0.02651 \text { Total Duration } 12 . \tag{19}
\end{align*}
$$

The assumptions for an optimal model is normality of the independent variables and equal covariance matrices of each group. Box's $M$ test was used to check the equality of covariance matrices based on the determinants of the matrices. Box's M test is also sensitive to the normality assumption. Of the three models developed previously, only Model $\mathbf{C}$ did not pass Box's $M$ test for equality of covariance matrices. This indicates that the model is not statistically optimal, and problems may arise in predicting rounds. In spite of this, the model predicted all correctly, as shown in Table 8, and the scatterplot and territorial map in Figures 21 and 22, respectively, show good separation among the groups.

- Verification of the Feasibility Models. Each of the three models described in the previous section represents the best classification rate since all of the data was used to develop the model. Often, live fire tests are conducted to verify that the model is truly adequate. This verification was expected to be performed later in the program when all round types had been incorporated into the final model(s). To check the adequacy of the current feasibility models, a portion of the data was taken for model development. The remaining data were reserved for testing the model, a form of goodness-of-fit. Stratified random sampling of two-thirds of data was implemented for adjusting the coefficients associated with the variables in each of the three models listed previously. Stratification was performed by randomly selecting one round from each round type at each range to be reserved for testing the model adequacy. The other rounds were used for the model development.


Figure 21. Feasibility phase model $C$ : scatterplot.


Figure 22. Feasibility phase model C : territorial map.

All three resulting models performed well. Each adjusted model correctly predicted all of the rounds used to develop the model, and each model correctly predicted each of the reserved rounds. Additionally, a set of theoretical data was created in a blind study to test the adequacy of Model C with two total durations. Twelve theoretical total duration values were computed for the various round types as if the microphones collecting acoustical signatures were placed on each side of the target. These values were placed in the discriminatory function. The resulting discriminant values correctly predicted the group membership for each round type, as seen in Table 9.

Table 8. Classification Result for Two Total Durations

| Actual Group | No. of <br> Cases | Predicted Group Membership |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 <br> M910 | 2 <br> M793 | 3 <br> M724/M865 | 4 <br> M490/M831 |
| 1. M910 |  | 9 <br> $100 \%$ |  |  |  |
| 2. M793 | 9 |  | 9 <br> $100 \%$ |  |  |
| 3. M724/M865 | 15 |  |  | 15 |  |
| 4. M490/M831 | 18 |  |  | $100 \%$ |  |

Table 9. Verification Results

| Actual Group | No. of <br> Cases | Predicted Group Membership |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 <br> M910 | 2 <br> M793 | 3 <br> M724/M865 | 4 <br> M490/M831 |
| 1. M910 | 3 | 3 | $400 \%$ |  |  |

- Feasibility Test Conclusion. Acoustical signatures, particularly total duration of the N -Wave curve, can be used to discriminate between the following round types:
- small- and large-caliber rounds
- large ( 105 - or $120-\mathrm{mm}$ ) HE and large KE training rounds
- $25-\mathrm{mm}$ HEI and KE training rounds.

With the use of discriminant analysis, three models that correctly classify $100 \%$ of the rounds have been developed. These models contain the following variables:

- total duration and microphone offset distance
- total duration and velocity ( $>3 \mathrm{~m}$ )
- two total durations.
5.2.5 Location and Velocity Data. During the feasibility test, the six microphones were set up in two triangular arrays as shown in Figure 23 (see Appendix C for exact microphone locations). The time differences, microphone and target locations, and meteorological data were processed through the Stallings algorithm discussed in 3.2.3. The data were first reduced for velocity prediction. The Stallings algorithm predicted the velocity, on the average, within $2 \%$ of the actual velocity verified by radar. The locations were, on the average 20 cm from the actual video scored locations (see Appendix G). The error was mostly due to microphone placement. The projectile hits did not go through the center of the microphone array. The microphones were purposely placed low to the ground to keep them from being hit and to see what errors would be generated.

Six M831 projectiles, fired from the $1,000 \mathrm{~m}$ position, were analyzed to study the effects of input data on the accuracy of the predicted location. Table 10 shows how a change in each input value of meteorological data, fall angle, and gun position affects the projectile location.

The error associated with the microphone positions depends on the contribution of that microphone when determining the location. If the projectile flies close to a microphone, the algorithm weights that microphone's data such that it provides a larger contribution to the output location. Generally, the average survey error of all the microphones will be close to the average scoring error. The survey error was typically around 1 mm for each microphone with the use of a precision theodolite and an experienced


Figure 23. Feasibility test microphone array and target setup.

Table 10. Input Values Effect on Location

| Input Values | Change for Each | Additional Change in Location (mm) |
| :---: | :---: | :---: |
| Meteorological Data |  |  |
| Temperature <br> Wind <br> Humidity | $\begin{gathered} 1^{\circ} \\ 1 \mathrm{~m} / \mathrm{s} \end{gathered}$ <br> Any Humidity | $\begin{gathered} 3 \\ 4 \\ 3 \max \end{gathered}$ |
| Ballistics |  |  |
| Fall Angle | 1 mil | 3.6 |
| Gun Position |  |  |
| X | 1 m | 5 |
| Y | 1 m | 0.5 |
| Z | 1 m | 4 |

surveyor. Errors associated with microphone times also depended on that microphone's contribution. There is more of an effect on location for slower projectiles since their shock waves are more oblique. The errors associated with meteorological data and fall angle are considered relatively small. The major downfall with the Stallings technique is the dependence on knowing the gun's position. Elevation changes, Z , are not that great on a training range. The major errors come from not knowing an accurate range and deflection of the gun position relative to the target. The Stallings technique was eliminated as a candidate for RDS location algorithm because it was slow and had large potential gun position errors.

### 5.3 Collection Phase.

5.3.1 Live-Fire Data. The next phase of testing began with the purpose of expanding the existing data set to include: $7.62-\mathrm{mm}$ ball (M59) and tracer (M62) rounds, $12.7-\mathrm{mm}$ ball (M33) and tracer (M17) rounds, and three $35-\mathrm{mm}$ TPGID (old HEAT DM18, new HEAT DM68, and KE simulator) rounds. This phase is designated as the collection phase. Randomization of rounds for testing took place as much as possible with the tight test schedule and small budget.

Since changing the firing platform for each round at each range was time-consuming, several rounds of the same size were fired at one range before moving the platform to another range. The goal was to divide the sample in half so that two groups of rounds of the same type were fired on two different days to average out any effects due to weather conditions. This was not always accomplished. The DM18 and DM68 round were late arriving. The DM68 and the TPGID KE simulators had not been type classified. The $7.62-\mathrm{mm}$ and $12.7-\mathrm{mm}$ rounds were fired first. Ball and tracer rounds were completely randomized. When the $35-\mathrm{mm}$ KE was type classified, it was randomized with the DM18. The DM68 was tested with the DM18 on the last two days. However, the duration data for the last two days was not available for the analyses. Table 14 lists the number of rounds reduced that were included from each type in the analysis.

The ball and tracer rounds are listed separately in Table 11, but there was little interest in discriminating between them in this study. There were some differences in total duration and velocity. The average velocity of the tracer rounds at each range was greater than the ball rounds for both 7.62 mm and 12.7 mm . The average total duration of the tracer rounds was approximately $13 \mu \mathrm{~s}$ greater than the

Table 11. Number of Rounds Analyzed in Collection Phase

| Distance <br> $(\mathrm{m})$ | 7.62 mm |  | 12.7 mm |  | 35 mm |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | M59 | M62 | M33 | M17 | DM68 | KE <br> Simulator |
| 400 | 3 | 4 | 5 | 4 | 3 | 3 |
| 600 | 3 | 4 | - | - | - | - |
| 800 | 3 | 3 | - | - | - | - |
| 1,000 | - | - | 4 | 4 | 4 | 3 |
| 1,700 | - | - | - | - | 3 | 3 |

ball rounds for both 7.62 mm and 12.7 mm with the exception of the 7.62 mm at 800 m . For this combination, the average ball round was $230 \mu \mathrm{~s}$ greater than the tracer round. More investigation is required to determine what caused this large difference at 800 m . See Appendix E for tables of total duration and velocity values. For the remaining analyses, the ball and tracer rounds of 7.62 mm will be treated as one group as well as the $12.7-\mathrm{mm}$ rounds.
5.3.2 Discriminate Analysis for Empirical Model Formation. The entire data set, from both the feasibility and collection phases, had a total of 8 groups: $7.62 \mathrm{~mm}, 12.7 \mathrm{~mm}, \mathrm{M} 910, \mathrm{M} 793,35-\mathrm{mm}$ TPGID KE simulator, DM18 and DM68, M724 and M865, and M490 and M831. A cursory analysis performed on the data before the complete data set was reduced indicated that prediction would be good overall. However, within the TPGID groups, only $66 \%$ of the rounds could be classified correctly.

A total of $34 \%$ of the DM18/DM68 rounds were predicted as TPGID KE simulator rounds. Likewise, $34 \%$ of the TPGID KE simulator rounds were predicted as DM18/DM68 rounds. An encouraging point was that these rounds were still classified as $35-\mathrm{mm}$ TPGID. Upon examination of these two round types, we found that the velocities of KE training rounds at each range were on the average $250 \mathrm{~m} / \mathrm{s}$ slower than the $120-\mathrm{mm}$ KE training rounds. To continue the analysis, the $35-\mathrm{mm}$ TPGID rounds were combined into one group resulting in seven groups for discrimination.

- Model I: Total Duration, Microphone Distance, and Velocity. Based on the three models developed during the feasibility phase, discriminant functions were formed first with variables $\ln$ (total duration) and microphone distance. Unlike the one-function model formed for the four groups in that phase, the model
for seven groups required two functions. However, misclassification was high, particularly between the M910 group and 12.7 mm . The misclassification rate was $17 \%$.

The next attempt was to form a model with variables $\ln$ (total duration) and velocity, as in Model B. This model produced $88 \%$ correct classification of the groups. Only the M490/M831 rounds were without misclassification. TPGID was the most difficult of all the groups to classify correctly.

Finally, all three variables- $\ln$ (total duration), microphone offset distance, and velocity-were included to produce a two-function model (see equation 20). This resulted in a good classification rate of $97.85 \%$ as shown in Table 12. From the scatterplot of the data in ( $f_{1}, f_{2}$ ) space (Figure 24), one can see why several $7.62-\mathrm{mm}$ rounds (group 1) were classified as 12.7 mm (group 2); the functional values were closer to the centroid of group 2. Likewise, several M910 rounds (group 3) were misclassified as 12.7 mm (group 2) since their values were closer to that centroid. The misclassified rounds could be easily identified by overlaying the territorial map (Figure 25) on the scatterplot (Figure 24). (The pattern numbers in the territorial map form the border lines between the groups.)

$$
\begin{align*}
\mathrm{f}_{1}= & -87.510+13.594 \ln (\text { Total Duration }) \\
& +0.00413 \text { Velocity }-0.529 \text { Microphone Offset Distance } \\
\mathrm{f}_{2}= & 6.592-1.928 \ln (\text { Total Duration }) \\
& +0.00650 \text { Velocity }+0.0671 \text { Microphone Offset Distance. } \tag{20}
\end{align*}
$$

This model was tested with data collected during the verification/validation phase. The groups' centroids listed in Table 13 are necessary for determining the group membership of the unknown rounds fired. The boundary conditions are set at $f_{1}(-20,20)$ and $f_{2}(-4,4)$. Any rounds producing values of $f_{1}$ and $f_{2}$ outside these boundaries were classified as an unknown round.

- Model II: Three Variables at 6 m . As discussed earlier, the field equipment array had two highfidelity microphones placed 6 m from the center of the target. The same variables used in the previous model were considered, but the coefficients were based on the $6-\mathrm{m}$ microphone data only. The classification rate for this model (see equation 21) was close to the Model I with $97.12 \%$ correct as shown in Table 14. The centroids, scatterplot, and territorial map are provided (see Table 15 and Figures 26 and 27 , respectively). The boundary conditions are $f_{1}(-20,20), f_{2}(-4,4)$, and $f_{3}(-4,4)$. This model was denoted as Empirical Model II and tested in the verification/validation phase.

$$
f_{1}=-95.122+14.681 \ln \text { (Total Duration) }
$$

$$
+0.00432 \text { Velocity }-0.5122 \text { Microphone Offset Distance }
$$

$$
f_{2}=5.512-1.878 \ln (\text { Total Duration })
$$

+0.00618 Velocity +0.258 Microphone Offset Distance
$\mathrm{f}_{3}=-9.133-0.202 \ln ($ Total Duration $)$

- 0.00041 Velocity +1.987 Microphone Offset Distance.

Table 12. Classification Results for $\ln$ (Total Duration), Microphone Offset Distance and Velocity

| Actual Group | No. of Cases | Predicted Group Membership |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\begin{gathered} 1 \\ 7.62 \mathrm{~mm} \end{gathered}$ | $\begin{gathered} 2 \\ 12.7 \mathrm{~mm} \end{gathered}$ | $\begin{gathered} 3 \\ \text { M } 910 \end{gathered}$ | $\begin{gathered} 4 \\ \text { M793 } \end{gathered}$ | $\begin{gathered} 5 \\ \text { TPGID } \end{gathered}$ | $\begin{gathered} 6 \\ \text { M724/ } \\ \text { M865 } \end{gathered}$ | $\begin{gathered} 7 \\ \text { M490/ } \\ \text { M831 } \end{gathered}$ |
| 1. 7.62 mm | 59 | $\begin{gathered} 54 \\ 91.5 \% \end{gathered}$ |  |  |  |  |  |  |
| 2. 12.7 mm | 65 |  | $\begin{gathered} 65 \\ 100.0 \% \end{gathered}$ |  |  |  |  |  |
| 3. M910 | 29 |  |  | $\begin{gathered} 26 \\ 89.7 \% \end{gathered}$ |  |  |  |  |
| 4. M793 | 29 |  |  |  | $\begin{gathered} 29 \\ 100.0 \% \end{gathered}$ |  |  |  |
| 5. TPGID | 29 |  |  |  |  | $\begin{gathered} 29 \\ 100.0 \% \end{gathered}$ |  |  |
| 6. M724/M865 | 56 |  |  |  |  |  | $\begin{gathered} 56 \\ 100.0 \% \end{gathered}$ |  |
| 7. M490/M831 | 65 |  |  |  |  |  |  | $\begin{gathered} 65 \\ 100.0 \% \end{gathered}$ |

NOTE: Cases correctly classified: $97.85 \%$.

Table 13. Discriminant Functions Group Centroids

| Group | $\mathrm{f}_{1}$ | $\mathrm{f}_{2}$ |
| :---: | :---: | :---: |
| M62/M59 | -13.170 | -0.621 |
| M17/M33 | -8.676 | -0.609 |
| M910 | -6.346 | 2.030 |
| M793 | -1.686 | -0.990 |
| DM18/DM68/TPL-T | 1.800 | 0.581 |
| M724/M865 | 9.119 | 2.207 |
| M490/M831 | 14.447 | -1.810 |



Figure 24. Model I: scatterplot.


Figure 25. Model I: territorial map.

Table 14. Model II Classification Results

| Actual Group | No. of Cases | Predicted Group Membership |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\stackrel{1}{7.62 \mathrm{~mm}}$ | $\stackrel{2}{12.7 \mathrm{~mm}}$ | $\begin{gathered} 3 \\ \text { M910 } \end{gathered}$ | $\begin{gathered} 4 \\ \text { M793 } \end{gathered}$ | $\stackrel{5}{\text { TPGID }}$ | $\begin{gathered} 6 \\ \text { M724/ } \\ \text { M865 } \end{gathered}$ | $\begin{gathered} 7 \\ \text { M490/ } \\ \text { M831 } \end{gathered}$ |
| 1. 7.62 mm | 17 | $\begin{gathered} 15 \\ 88.2 \% \end{gathered}$ | ! |  |  |  |  |  |
| 2. 12.7 mm | 17 |  | $\begin{gathered} 17 \\ 100.0 \% \end{gathered}$ |  |  |  |  |  |
| 3. M910 | 9 |  |  | $\begin{gathered} 8 \\ 88.9 \% \end{gathered}$ |  |  |  |  |
| 4. M793 | 9 |  |  |  | $\begin{gathered} 9 \\ 100.0 \% \end{gathered}$ |  |  |  |
| 5. TPGID | 18 |  |  |  |  | $\begin{gathered} 18 \\ 100.0 \% \end{gathered}$ |  |  |
| 6. M724/M865 | 16 |  |  |  |  |  | $\begin{gathered} 16 \\ 100.0 \% \end{gathered}$ |  |
| 7. M490/M831 | 18 |  |  |  |  |  |  | $\begin{gathered} 18 \\ 100.0 \% \end{gathered}$ |

NOTE: Cases correctly classified: $97.12 \%$.

Table 15. Model II Group of Centroids

| Group | $\mathrm{f}_{1}$ | $\mathrm{f}_{2}$ | $\mathrm{f}_{3}$ |
| :---: | ---: | ---: | :---: |
| 7.62 | -14.276 | -0.582 | -0.191 |
| 12.7 | -9.323 | -0.583 | 0.011 |
| M910 | -6.790 | 1.826 | 0.145 |
| M793 | -1.598 | -0.893 | 1.060 |
| TPGID | 2.035 | 0.474 | -0.474 |
| M724/M865 | 9.811 | 2.089 | 0.160 |
| M490/M831 | 15.726 | -1.697 | -0.100 |

- Model III: Two Total Durations. The final empirical model, equation 22, includes two total duration variables as constructed in the feasibility phase (Model C). The data from the $9-\mathrm{m}$ microphone were the most discriminating, and the $3-\mathrm{m}$ microphone data were the second most discriminating. Although an effort was made to use the data measured at 6 m , the data at 3 m and 9 m were the least correlated as well as the most discriminating. The correlation between the total duration values at 9 m


Figure 26. Model II: scatterplot.


Figure 27. Model II: territorial map.
and 6 m is 0.94 . This high correlation between explanatory variables can cause a problem known as multicollinearity in which the coefficients are very sensitive. The goal is to obtain coefficients that are robust so that the model will be valid under various conditions.

$$
\begin{align*}
\mathrm{f}_{1}= & -16.158-0.000608 \text { Total Duration }(3-\mathrm{m} \mathrm{Mic}) \\
& +0.0199 \text { Total Duration }(9-\mathrm{m} \text { Mic) } \\
\mathrm{f}_{2}= & 0.200+0.0316 \text { Total Duration }(3-\mathrm{m} \text { Mic) } \\
& -0.0233 \text { Total Duration }(9-\mathrm{m} \text { Mic) } . \tag{22}
\end{align*}
$$

The correct classification rate for this model was lower than the other two models at $89.69 \%$ (see Table 16). The difficulty in discriminating occurred for rounds 35 mm and smaller. The scatterplot and territorial map (Figures 28 and 29) respectively show this from the location of the group centroids. The centroids of three smallest rounds $-7.62 \mathrm{~mm}, 12.7 \mathrm{~mm}$, and M910 are very close as are the centroids of M793 and TPGID. The boundary values for the discriminant functions below are $f_{1}(-15,25)$ and $f_{2}(-4,4)$. The group centroids are provided in Table 17.

The three models developed in this collection phase were tested against a new set of data during the verification/validation test along with the brassboard system. Those results are given in section 9 .
5.3.3 Location and Velocity Data Reduction. The microphones were placed in the H configuration, two lines of three microphones each (Figure 30). For this study, the intersection of Hyperbolas of Ambiguity method was used to calculate offset distance. The predicted locations were on average 24 cm away from the actual video scored locations, and the predicted velocities were within $3 \%$ (see Appendix H). Errors in location and velocity are mostly due to the projectile's incoming angle. The projectile must travel parallel to the centerline connecting the two center microphones for the calculation to be accurate. As this incoming angle increases, the calculated errors increase quadratically.

## 6. RDS ALGORITHM DEVELOPMENT

6.1 Theoretical Formulation Technique. The total duration formula described in equation 2 was based on test data with small-caliber projectiles fired from M14 and AR15 rifles (Kalb, unpublished). The constant value of 1.82 was used in the formula for small-caliber ogival bodies. A new variable was created for this constant and named the acoustic shape constant, K. During phase I and II of the data collection testing, each K was solved for by rearranging Schochko's (1966) formula for K and plugging in the known values.

Table 16. Model III Classification Results

| Actual Group | No. of Cases | Predicted Group Membership |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\begin{gathered} 1^{1} \mathrm{~mm} \end{gathered}$ | $\stackrel{2}{12.7 \mathrm{~mm}}$ | $\begin{gathered} 3 \\ \text { M910 } \end{gathered}$ | $\begin{gathered} 4 \\ \text { M793 } \end{gathered}$ | $\stackrel{5}{\text { TPGID }}$ | $\begin{gathered} 6 \\ \text { M724/ } \\ \text { M865 } \end{gathered}$ | $\begin{gathered} 7 \\ \text { M490/ } \\ \text { M831 } \end{gathered}$ |
| 1. 7.62 mm | 17 | $\begin{gathered} 15 \\ 88.2 \% \end{gathered}$ | ! |  |  |  |  |  |
| 2. 12.7 mm | 15 |  | $\begin{gathered} 12 \\ 80.0 \% \end{gathered}$ | $\begin{gathered} 3 \\ 20.0 \% \end{gathered}$ |  |  |  |  |
| 3. M910 | 9 |  |  |  | $\begin{gathered} 7 \\ 77.8 \% \end{gathered}$ |  |  |  |
| 4. M793 | 9 |  |  |  | $\stackrel{6}{66.7 \%}$ | $\begin{gathered} 3 \\ 33.3 \% \end{gathered}$ |  |  |
| 5. TPGID | 18 |  |  |  |  | $\begin{gathered} 18 \\ 100.0 \% \end{gathered}$ |  |  |
| 6. M724/M865 | 14 |  |  |  |  |  | $\begin{gathered} 14 \\ 100.0 \% \end{gathered}$ |  |
| 7. M490/M831 | 15 |  |  |  |  |  |  | $\begin{gathered} 15 \\ 100.0 \% \end{gathered}$ |

NOTE: Cases correctly classified: $\mathbf{8 9 . 6 9 \%}$.


Figure 28. Model III: scatterplot.


Figure 29. Model III: territorial map.

Table 17. Model III Group of Centroids

| Group | $\mathrm{f}_{1}$ | $\mathrm{f}_{2}$ |
| :---: | ---: | ---: |
| 7.62 | -10.574 | 0.198 |
| 12.7 | -8.561 | 0.515 |
| M910 | -8.036 | -0.132 |
| M793 | -3.415 | -0.581 |
| TPGID | -1.444 | 0.037 |
| M724/M865 | 6.787 | -0.878 |
| M490/M831 | 22.815 | 0.464 |

$$
\begin{equation*}
K=\frac{T a\left(M^{2}-1\right)^{3 / 8} L^{1 / 4}}{O^{1 / 4} M D} \tag{23}
\end{equation*}
$$

An averaged $K$ value was then determined over the velocities and offset distances tested. Since each projectile has unique physical properties (diameter and length) and $K$ value, equation 23 was rearranged to equate the projectile physical dependents on one side with the measured values on the other. The projectile dependents were grouped together and labeled the projectile shape value (PSV). The formula becomes

$$
\begin{equation*}
\operatorname{PSV}=\frac{\mathrm{D}}{\mathrm{~L}^{1 / 4}} \mathrm{~K}=\frac{\mathrm{Ta}\left(\mathrm{M}^{2}-1\right)^{3 / 8}}{(O)^{1 / 4} \mathrm{M}} \tag{24}
\end{equation*}
$$



Figure 30. Data collection test microphone array and target setup.

Table 18 contains the empirical PSV and category for each projectile type tested. The measured values were input into equation 3 after the raw analysis. Next, the measured were compared to the empirical values. The system identifies the projectile type by calculating the smallest measured empirical PSV differential.

After the data were analyzed and the measured values were input into equation 24 , the next step was to check to see how these values compared with tabular values. This was accomplished by finding the difference of the measured PSV from microphone 1 and the theoretical PSV and selecting the projectile type that best agrees.

$$
\begin{equation*}
\text { PSV1 }=\frac{\mathrm{D}}{\mathrm{~L}^{1 / 4}} \mathrm{~K}=\frac{(\mathrm{T} \text { Mic } 1) \mathrm{a}\left(\mathrm{M}^{2}-1\right)^{3 / 8}}{(\mathrm{O} \text { Mic } 1)^{1 / 4} \mathrm{M}}, \tag{25}
\end{equation*}
$$

Table 18. Average Projectile Shape Values

| Gun <br> Caliber <br> $(\mathrm{mm})$ | Projectile Type | Diameter <br> $(\mathrm{mm})$ | Length <br> $(\mathrm{m})$ | Average <br> K | Average <br> PSV | Projectile <br> Category <br> $(\mathrm{mm})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 7.62 | M59 (ball) | 7.82 | 0.032 | 2.08 | 0.038 | 7.62 |
| 7.62 | M62 (tracer) | 7.82 | 0.034 | 2.16 | 0.039 | 7.62 |
| 12.7 | M33 (ball) | 12.95 | 0.059 | 2.11 | 0.056 | 12.7 |
| 12.7 | M17 (tracer) | 12.95 | 0.059 | 2.21 | 0.058 | 12.7 |
| 25 | M910 (KE-TP) | 16.20 | 0.076 | 1.99 | 0.062 | 25 KE |
| 25 | M793 (HEI-TP) | 25.00 | 0.115 | 2.18 | 0.093 | 25 KE |
| 35 | TPL (KE-TPGID) | 35.00 | 0.180 | 2.04 | 0.110 | 35 |
| 35 | DM18 (HE-TPGID) | 35.00 | 0.180 | 2.12 | 0.114 | 35 |
| 35 | DM68 (HE-TPGID) | 35.00 | 0.180 |  |  | 35 |
| 105 | M724 (KE-TP) | 63.50 | 0.256 | 1.72 | 0.154 | $105 / 120 \mathrm{KE}$ |
| 120 | M865 (KE-TP) | 38.00 | 0.468 | 3.71 | 0.170 | $105 / 120 \mathrm{KE}$ |
| 105 | M490 (HEAT-TP) | 105.00 | 0.654 | 2.50 | 0.291 | $105 / 120 \mathrm{KE}$ |
| 120 | M831 (HEAT-TP) | 120.00 | 0.844 | 2.37 | 0.296 | $105 / 120 \mathrm{KE}$ |

PSV1 = PSV for HM1
Remainder1 = abs (PSV1- PSV).

The remainders were ranked from the smallest to the largest. In the same manner, the PSV for microphone 2 is solved for

$$
\begin{equation*}
\text { PSV2 }=\frac{\mathrm{D}}{\mathrm{~L}^{1 / 4}} \mathrm{~K}=\frac{(\mathrm{T} \text { Mic } 2) \mathrm{a}\left(\mathrm{M}^{2}-1\right)^{3 / 8}}{(\mathrm{O} \text { Mic } 2)^{1 / 4} \mathrm{M}} \tag{26}
\end{equation*}
$$

PSV2 = PSV for HM2
Remainder2 $=$ abs(PSV2- PSV).

The remainders are ranked from smallest to largest.

If both rankings agree, that is the projectile type predicted. If not, there are three possible cases where the ranks are different. In case 1, PSV1 is closer and greater than round type A, and PSV2 is closer and lesser than round type B. This yields two positive remainders for round type A and two negative remainders for round type B. Round type B is selected. In case 2, PSV1 is closer and greater than round
type A, and PSV2 is closer and lesser than round type B. Round type A is selected. In case 3, PSV1 is closer and lesser than round type A, and PSV2 is closer and greater than round type B. Take the average of PSV1 and PSV2 and reevaluate the remainder to find the round type.

Figure 31 shows the projectile terminal velocity plotted against PSV. It can be seen that some PSV's from different round types overlap at extreme conditions. All of the projectiles fired have well-defined velocities at known ranges (see Table 2). If a PSV is computed and there are two possibilities, the correct round type can be selected if referenced to the velocity axis. For instance, the $12.7-\mathrm{mm}$ and $25-\mathrm{mm}$ KE rounds have similar PSV's. If the terminal velocity of the projectile fired was greater than $850 \mathrm{~m} / \mathrm{s}$, the $12.7-\mathrm{mm}$ round could be ruled out as a possible choice since it cannot achieve that velocity. This model was called the theoretical model.

### 6.2 Hybrid.

6.2.1 Discriminatory Analysis for PSV. The quasi-empirical formulation for PSV is a function of the same significant variables used in the empirical model, total duration, microphone offset distance, and velocity. The theoretical and the empirical results were combined to form a "hybrid" model. The PSV will be used in the discriminant analysis.

From the data collected in the feasibility phase and data collection phase, the projectile shape was tested to determine if it could serve as a discriminator of the seven groups. Discriminant analysis was implemented with the model based on the data collected from the $6-\mathrm{m}$ microphone. This distance was chosen since this was the same location for the high-fidelity microphones as planned for the live-fire validation test. The classification of the remaining data was performed for a sensitivity check of the model.

The model with projectile shape alone resulted in 8 misclassifications and 94 correct classifications for a success rate of $92.16 \%$. The shape variable was added to the database of variables to determine if it were a superior discriminant variable when compared to the other variables. Using the discriminant analysis models, PSV was found to improve the performance of the classifications. PSV's were first to enter the model with $\ln$ (total duration) following. The correct classification rate dropped to $85.29 \%$. Although total duration was allowed to enter the model based on the tolerance criterion, the pooled group correlation between shape and $\ln ($ total duration $)$ was 0.814 .


Figure 31. $\ln$ (total duration) vs. velocity.

Velocity became the variable to enter the model after PSV. This was intuitively appealing, since PSV was basically replacing $\ln$ (total duration) in the earlier model formed with $\ln$ (total duration) and velocity. If we compare plots of $\ln$ (total duration) vs. velocity (Figure 31) with PSV vs. velocity (Figure 32), we notice that the relative positions of the round groups are similar. The plot with PSV forms tighter groupings.

The two-function model with variables PSV and velocity, equation 27, provided a $99.02 \%$ correct classification rate from the $6-\mathrm{m}$ data, with one $25-\mathrm{mm}$ KE misclassified as a $12.7-\mathrm{mm}$ round. The discriminatory functions $F_{1}$ and $F_{2}$ plotted in Figure 33 resembles the data in the original units of PSV vs. velocity Figure 32.

$$
\begin{align*}
& F_{1}=-22.757+144.233 \text { PSV }+0.00500 \text { Velocity } \\
& F_{2}=-3.904-10.733 \text { PSV }+0.00632 \text { Velocity. } \tag{27}
\end{align*}
$$

6.2.2 Model Implementation for Prediction. A model was developed that separated the seven types of rounds with good success. The true test of the adequacy of the model would come when additional rounds were fired in the verification/validation phase (section 9). How is the two-function model implemented once the data are collected? First, the centroids of each group were calculated for both functions as provided in Table 19.

Table 19. Group Centroids

| Group | $\mathrm{F}_{1}$ | $\mathrm{~F}_{2}$ |
| :---: | :---: | :---: |
| 7.62 | -14.765 | -1.296 |
| 12.7 | -11.495 | -0.909 |
| M910 | -8.781 | 1.716 |
| M793 | -5.610 | -0.787 |
| TPGID | -1.338 | 0.848 |
| M724/M865 | 7.800 | 2.678 |
| M490/M831 | 25.093 | -1.586 |

Second, boundary conditions for $F_{1}$ and $F_{2}$ were determined to guard against signals outside of the target area of interest. This is not really necessary since the round location method would not allow the


Figure 32. PSV value vs. velocity.


Figure 33. Discriminatory functions F1 and F2.
target to drop if the round did not hit the target. But to implement the round discrimination method independently of the round location method, boundary conditions are necessary. The boundary area is a simple rectangular area in $F_{1}$ and $F_{2}$ space. The minimum and maximum values for each function is: $F_{1}(-17.0,29.0)$ and $F_{2}(-4.5,5.5)$.

When an unknown round is fired at the target, the total duration, microphone offset distance, and velocity will be collected, and the PSV will be computed. Then values of $F_{1}$ and $F_{2}$ are computed for this round. The distance is calculated between the unknown round and each group centroid. The minimum distance will dictate the classification of the unknown round.

Because two microphones will be placed on each side of the target in the verification/validation test to collect total duration data, two pair of discriminant scores will be computed, one for the left microphone and one for the right. It is possible that the minimum distance of the discriminant score for the left microphone classifies the unknown round into a different group as the right. In that case, the final group assignment would be the smallest of those two minimum distances.

## 7. SOFTWARE DEVELOPMENT

A microprocessor was determined to be the most effective way to process the input data using the model, perform decisions, and execute commands. The RDS needed to take the data developed by the sensors after a round was sensed. The signals for location and acoustic signature were to be processed, and the values of that process utilized by the prediction model. Once a prediction was made as to round type and location of hit, commands based on a decision of "kill," "hit but no kill," and "no hit" would command the RETS system. A $486 \mathrm{PC} / 104$ embedded computer was selected as the microprocessor due to the ease of programming, ability to use peripherals (disk drives, monitors, and keyboards), and accessibility to remote sites. Additional hardware consisted of power supplies, a floppy drive, a hard drive, and three electronic interface boards. The boards were designed and fabricated at ARL. They were the location interface board, the sensor interface board, and the A/D board. To control the computer, special software was generated.

The software for the RDS system was developed in Microsoft $C$ to run under an IBM PC or compatible platform. The I/O devices used to collect the signal wave forms and counter values were memory-mapped devices which enabled a high rate of data transfer. Two data files were created to run
the program. The first file is called "locate.dat" and contained microphone and target coordinates needed to calculate round location. The second file was called "shapes.dat," and it contained "shape values" needed to categorize rounds for identification.

The program began with a series of questions to initialize the system. The first question asked whether or not results will be transmitted back to a remote location. The second question asked whether or not raw data and results will be saved onto the hard disk. If data and results are to be saved, a file name was specified. Finally, the program asked what type of target was being used for the training exercise.

The system waited for a hardware trigger signal from any one of the location microphones. The trigger was caused by the shock from a projectile flying by any of the location microphones. While the system polled the trigger line, a 2,000 -point circular buffer was being continuously filled with data collected through the high-fidelity microphones and into the dual-channel analog-to-digital board at a rate of 250 kHz per channel.

When triggered, 1,000 points of shock wave data were collected from each high-fidelity microphone. A total of 12,000 points of shock wave data were collected from each high-fidelity microphone when the circular buffer data were added. The circular buffer contained pretrigger data which ensured the entire wave form of the shock wave was preserved in case the shock wave reached the high-fidelity microphones before the location microphones which triggered the collection.

Counter values were next read in from the quartz counter board. There were five counters, and each measured the relative delay of the shock wave as it passed between adjacent location microphones. Figure 34 shows how the counters were set up in relation to the location microphones. Each counter was controlled by a pair of location microphones; Counter 0 by LM1 and LM2, Counter 1 by LM2 and LM3, Counter 2 by LM2 and LM5, Counter 3 by LM4 and LM5, and Counter 4 by LM5 and LM6. Counters started counting when either one of its controlling microphones encountered the shock wave and stopped when its other controlling microphone encountered the shock wave (both controlling microphones could start or stop the counter). Knowing the rate at which the counters counted and the counter values when they stopped, the time delays of the shock wave between microphones are then determined. In addition to the counters, four data bits were read to determine which of the microphones in each pair started each counter counting. The sign of the counters was adjusted accordingly from these four data bits to show if the round came from the left or the right.


Figure 34. Location microphones.

Using the counter values, the location of the round on the target, the offset distances of the round from the high-fidelity microphones, and the round velocity were calculated. The round velocity was calculated first using Counter 2. The location and offset distances were calculated using velocity and Counters 0 , 1,3 , and 4.

Using the shock wave length, round velocity, and round offset distance from the high-fidelity microphones, the round type was determined. To calculate the shock wave length, the wave form data was first passed through a five-point moving average smoothing filter to eliminate random noise. Next, the data was truncated to 500 points to eliminate the data points before and after the shock wave. The shock wave length was found by performing a point-by-point differentiation of the remaining 500 -point wave form, picking out the two peaks. The separation between the two peaks corresponded to the shock wave length. Figures 35 a through $35 d$ graphically illustrate the process of finding the shock wave length.

After the round location and type had been determined, the program checked if the round hit inside the kill area and if the round type could kill the target type. If both of these conditions were true, the program would signal the RETS to lower the target. The RDS would accept a signal from the RETS vibration sensor, which indicates a round striking the target. The round type, location, and velocity was radioed back to a remote site via a modem and hand-held radio. The system was reset to the initial values.


Figure 35a. N -wave ( $12,000 \mathrm{pts}$ ).


Figure 35c. Truncated filtered N -wave ( $1,000 \mathrm{pts}$ ).


Figure 35b. Filtered N-wave ( $12,000 \mathrm{pts}$.


Figure 35d. Point-by-point differentiation (1,000 pts).

## 8. BRASSBOARD

8.1 Theory of Operation. The RDS brassboard was a stand-alone system that directly interfaced with the RETS. The RDS sent a kill signal to the RETS when the system discriminates the round. It is a modular PC-based system, and it has its own radio communication link to the range control tower. The RDS brassboard was made of off-the-shelf components except for the two electronic interface boards. The system operates on $110-\mathrm{V} / 60-\mathrm{Hz}$ or $220-\mathrm{V} / 50-\mathrm{Hz}$ AC power.

Prior to running the RDS, software initialization was required with each power up. Temperature, target type, microphone positions relative to the target, and kill zone information must be entered by the user. There was a storage option where all raw data could be stored on the hard disk for post-test analysis. After initialization, the system established radio communication with the tower. When this connection was established, the RDS was set. As a round flew through the sensor array, the RDS was triggered by shock wave impinging on one of the location microphones. The two high-fidelity microphones captured the shock wave. The RDS computer calculated the durations, the Cartesian position of the round, and the velocity of the round.

With the durations, the microphone offset distances (derived from the location information), and the velocity, the RDS identified a round type. If that round satisfied the kill criteria for that particular target type and it was within the kill zone, the RDS sent a "target down" signal to the ECU of the RETS. The RETS lowered the target as if it received a target down signal from the vibration sensors. The round identification, location, and velocity information was transmitted back to the tower. Another PC in the tower displayed a picture identification of the round, an " X " on a tank silhouette target, and the velocity (see Figure 37). The RDS transmitted results to the tower each time the system was triggered, regardless if the kill criteria was satisfied. It took 2 s for the RDS to process and transmit data, but it took $10-15 \mathrm{~s}$ if the storage option was enabled. During the processing time, any other incoming round would be ignored. The RDS brassboard logged the vibration input. It was not part of an algorithmic decision. The RDS was PC compatible. This enabled the designers to use DOS and Windows application software and hardware to develop the discrimination algorithms (Figure 36) and the communication system.


Figure 36. Algorithm flow chart.

### 8.2 Construction.

8.2.1 Location Interface Board. The location interface board (LIB) was a 6 -in $\times 6$-in printed circuit board (PCB) that incorporated a similar circuit designed by Dr. Joel Kalb of the Human Research and Engineering Directorate (HRED) for his round location system. The RDS's version had six electret microphone inputs instead of four. The additional inputs were the right front and left front microphones. The microphone front-end electronics, threshold comparator, debouncing latches, and time difference gates were identical to Dr. Kalb's (Kalb, unpublished).


Figure 37. Tank silhouette.

The LIB provided power to the six-electrode microphones and measured the time delays between location microphones. The board had outputs from five time difference gates and four direction registers. The gates measured the time delays between pairs of microphones: front left and front center, front right and front center, back left and back center, back right and back center, and front center and back center. Each gate sent a pulse when one of the two microphones was triggered, and it sent another pulse when the second microphone was triggered. Each direction register associated a negative or a positive sign to each time difference gate except for the two center microphones. It was assumed that the shock wave would impinge upon the front row of the array before the back row. The outputs of the LIB fed directly into the PC/104 computer through the counters and I/O's mini-module. The time duration and direction of fire calculations were done by software.

In addition, the LIB had a NPN transistor circuit for the target down signal. When the discrimination algorithm determined that the target should be lowered, the computer sent a 5 -ms pulse to the circuit. The circuit acted as a driver and sent an inverted pulse (HIT SIG) to the ECU of the RETS to lower the target. Refer to LIB circuit diagrams for further details (Figure 38).


Figure 38. Location interface board circuits.
8.2.2 Sensors Interface Board. The sensors interface board (SIB) was also a 6 -in $\times 6$-in PCB. It contained circuits for the high-fidelity microphones ( $\mathrm{B} \& \mathrm{~K}$ 's and Countrymans), the vibration sensors, and additional electronics for future use such as the switches and LED's. Only the circuits for the B\&K microphones and the vibration sensors were used. The RDS brassboard used two high-fidelity B\&K microphones to capture the supersonic shock waves. The interfacing circuit was a simple voltage divider with gain of $1 / 4$ and impedance buffer. The two outputs were fed directly into the A/D's.

The SIB had two vibration sensor inputs. The vibration circuit was identical to the one in the RETS ECU except for the hit sensor failure circuit (TM9-6920-442-14\&P). As soon as one of the two vibration sensors was triggered, the circuit produced a $5-\mathrm{V}, 1-10-\mathrm{ms}$ output, signifying a tagged hit. This HIT signal was fed into the computer by a register on the A/D board. Refer to SIB circuit diagrams for further details (Figure 39).


Figure 39. Sensor interface board circuits.
8.2.3 A/D Board. The A/D board was a $4-\mathrm{in} \times 4-\mathrm{in}$ PCB with a PC/104 bus connector that stacks onto the PC/104 computer. It had two 12-bit analog-to-digital converters (ADC) with track and hold. The ADC's, part no. MAX120 from Maxim Integrated Products, ran on a $4-\mathrm{MHz}$ clock and sampled at a $250-\mathrm{kHz}$ rate. The A/D board had encoding and decoding logic that enabled the data bus from the ADC's to interface directly with the $\mathrm{PC} / 104$ bus. The digitized data from the ADC's were continuously being dumped on the bus. The computer took the data and stored them in a circular buffer. When one of the location microphone was triggered by the shock wave, the BIGOR gate from the LIB sent a pulse to the computer through a register on the $\mathrm{A} / \mathrm{D}$ board to collect 10,000 more data points. After the 10,000 th point, the computer stopped the ADC's from dumping anymore data onto the bus. The ADC's remained in this state until the computer finished with the discrimination algorithm. The $A / D$ board also accepted the HIT signal from the SIB. The software logged the HIT signal, but it did not use the signal in any decision process. Refer to the A/D board circuit diagrams for future details (Figure 40).


Figure 40. $\mathrm{A} / \mathrm{D}$ board circuit diagram.

## 9. RDS INTEGRATION WITH RETS.

9.1 Electronics Packaging. The RDS brassboard system architecture is shown in Figure 41. The system was housed in a 24 -in $\times 20$-in $\times 12$-in stainless steel box with a sealed lid. The box will protect the electronics from rain and fragment debris. On the outside of the box, there were six location microphone input connectors (MIC1 to MIC6), two high-fidelity microphone input connectors (B\&K1 and B\&K2), two vibration sensor input connectors (VIB1 and VIB2), one target signal down output connector (HIT SIG), a parallel port, a serial port, a VGA monitor input, and a keyboard input. Eight $40-\mathrm{ft}$-long, shielded, twisted pair cables connected the microphones to the RDS unit. A $20-\mathrm{ft}$ cable connects the HIT SIG output to the RETS's ECU.


Figure 41. RDS system diagram.

The core of the RDS brassboard was the PC/104 embedded computer. The computer was composed of four 4 -in $\times 4$-in stackable modules: a $486-25 S X$ CPU core module with a math coprocessor, a hard/floppy disk controller mini-module, a SVGA mini-module and a counter, and a I/O's mini-module. The embedded computer only required a single $+5-\mathrm{V}, 750-\mathrm{mA}$ power supply for operation. The PC/104 embedded architecture was chosen because it is compact and modular. During the development phase, a more sophisticated computer system could be assembled by stacking more mini-modules. A minimodule can be a flash memory card, a data acquisition card, an I/O card, or a communication card. The RDS brassboard only used four modules. Only the 486-25SX core module and the counters and I/O's mini-module were needed for operation after system initialization.
9.2 ECU Connection. The RDS brassboard interfaces with the RETS with no modification. Due to time, budget and proprietary RETS hardware constraints it was impossible to incorporate the RDS outputs into the RETS's communication system without working and consulting with Paramax System Corp., the main RETS contractor. Instead, a separate radio communication subsystem for the RDS was designed and used. In the future, however, the RDS outputs would be incorporated into the RETS's CCU, and the results would be displayed in the control tower.

The RDS interfaced with the RETS through the ECU of the RETS. It hooked up to the RETS by disconnecting all vibration sensors from the ECU. Then, connecting two of those vibration sensors to the RDS vibration sensor inputs, VIB1 and VIB2, and connecting the RDS's target down signal output, HIT SIG, to one of the hit sensor inputs on the ECU, the hardware connection was then complete.
9.3 Radio Communication to Tower. In addition to the program written for the RDS hardware, a second program was written for the RDS system to interpret results sent to a remote site from the target area. As mentioned earlier, the target area and remote site communicated through a modem and hand-held radio at each site. The RDS computer communicated with the modem through a serial port. The modem was a Kantronics modem running at 9,600 baud while the radio was a Motorola GP300 VHF radio with an operating range of 146 MHz to 174 MHz . The radio frequency used was dependent on the usable frequency bands at each test site.

## 10. VERIFICATION/VALIDATION TEST

10.1 Purpose. The primary purpose of the test was to verify the performance of the RDS brassboard and validate the system's operational capabilities within the spectrum of live-fire conditions expected on a U.S. Army training range. A secondary purpose was to allow private contractors the opportunity to verify/validate their own round identification systems and/or collect data that may assist in the future development of RDS for use on U.S. Army training ranges.

The verification test was conducted from 23 Jun- 1 Jul 1993 at the high velocity range, APG, MD. A RETS lifter was used. Two $6-\mathrm{ft} \times 6-\mathrm{ft} \times 2-\mathrm{ft}$ concrete blocks were placed to the left of the target to protect the RDS brassboard and radio communication system. The RDS was connected to the RETS ECU. The 7th ATC training environment was replicated as best as possible. A berm was built around the lifter to simulate the target pit. Discrimination microphones were attached to $1-\mathrm{m}$-long stakes. Location array
microphones were attached to stakes and located 20 cm above ground level. Support data for the test included Weibel radar velocity data, video scoring on the target, local meteorological data, and survèy data. The test plan called for all training projectile types fired in the feasibility and data collection tests to be fired. The verification/validation test firing matrix and test results are presented in Appendix K. Average velocity errors of $3 \%$ and average location errors of 9 cm were observed.
10.2 Statistical Summary of Data at APG. Five models were constructed in sections 4 and 5 , and each was evaluated against its ability to predict the rounds fired during the validation test. The five models include PSV formulation with equation 25 (Whitham's theoretical model), the three empirical models, and the Hybrid model.

The three empirical models and the Hybrid model that used discriminant analysis were not statistically optimal since the assumption of equality covariances for all the groups was not met. This indicated that the estimate of pooled covariance matrix was a biased estimate of the true but unknown covariance matrix. It was not surprising that Model III, with two total durations as variables in the model, did not have equal covariance matrices, since the covariances were not equal when only four groups were considered during the feasibility phase. Attempting to achieve this for seven groups to discriminate makes it even harder for all the models considered. Model II came closest to having equal convariances. However, it should be noted that due to these inequalities, some of the coefficients may be unstable. Nevertheless, using pooled estimates of the covariance matrix for each analysis resulted in robust algorithms for most of the models, based on the results from this phase of testing.

Table 20 summarizes the number of rounds correctly classified by each model. Four of the models performed comparably at around $90 \%$; however, empirical Model III performed the worse. One problem with Model III stemmed from the microphone array. Two total durations were selected from the five microphones collecting the signatures. This change in configuration made the coefficients for the algorithm unreliable. The model resulted in poor prediction especially for the $25-\mathrm{mm}$ rounds. The model predicted a $12.7-\mathrm{mm}$ round in each case.

Model I used data from all the microphones. This fact made it appear that there were five times more independent shots than there actually were. The five duration values obtained from one shot were not independent outcomes, and the velocities paired with each of the five durations were the same.

Table 20. Model Comparison-Number of Correct Classifications

| Round | No. of Rounds | Theoretical | Empirical |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | I | II | III | Hybrid |
| 7.62 mm | 3 | 3 | 1 | 1 | 1 | 3 |
| 12.7 mm | 9 | 9 | 9 | 9 | 6 | 9 |
| M910 | 9 | 9 | 8 | 9 | 0 | 9 |
| M793 | 5 | 5 | 4 | 3 | 0 | 4 |
| TPGID | 15 | 15 | 15 | 15 | 14 | 15 |
| M724/M865 | 10 | 8 | 9 | 9 | 4 | 9 |
| M490/M831 | 11 | 6 | 10 | 9 | 5 | 7 |
| Total | 62 | 55 | 56 | 55 | 30 | 56 |
| Percent Correct |  | 89\% | 90\% | 89\% | 48\% | 90\% |

Model II has the greatest appeal of the three empirical models. The algorithm was developed from the 6 -m microphone which is suited for the final microphone array. One data set of duration, microphone distance, and velocity corresponds to one round tested.

The theoretical model and the Hybrid model are favored, since they have a theoretical basis and provide prediction results equal to or greater than the other models. Although equation 25 was derived from smaller-caliber rounds, the model performed quite well, as did the Hybrid. Both models (as well as Models I and II) have redundancy incorporated in them. They only require one high-fidelity microphone for discrimination. The other microphone acts as a check and as a backup system if the other microphone malfunctions during training exercises.

Unusually high duration signatures measured for the large-caliber rounds became a problem during testing. These readings were at least $50 \%$ higher than expected, and they did not occur consistently on the same microphone. This affected Model III more than the other models because both microphones are required for round classification. It was hypothesized that the large durations were due to reflections off the concrete block protecting the instrumentation. If this were true, one would expect the effect to be greatest for the microphone closest to the concrete wall; however, this did not explain the high signal received from the microphone on the far side when the microphone closest to the wall recorded values as expected. The source of the reflection is unlikely to be from the ground. The problem was not resolved in this phase of the program.

## 11. DEMONSTRATION RESULTS AT 7TH ATC

The RDS brassboard and a backup system were transported to Grafenwoehr, Germany, for a live fire demonstration. On 14 July 1993, the RDS was set up in front of target V-16 on Range 117. Target V-16 was located approximately $1,500 \mathrm{~m}$ from the initial firing line. This target was chosen in order to get the best engagement ranges for both small-caliber and large-caliber weapons. The microphones and target locations were surveyed in the same manner as in previous tests (see Figure 30). Five different projectile types were fired from an M1A1, an M1A1 outfitted with TPGID, and an M2. Each vehicle was fired from a random location on the range. An orange kill zone was painted on the target. Thermal blankets were placed in the same area (see Figure 42). If projectiles were determined to be in that area, the RETS would be sent information to lower the target. During the pre-test, 9 out of 12 projectiles were identified correctly by the theoretical model, and the RETS system lowered the target when signaled by the RDS. The stored data was analyzed on-site to determine why the three projectiles were not identified. On-site data reduction revealed that acoustic reflections were being captured within the prescribed window being analyzed. These reflections were assumed to be only ground reflections.


Figure 42. Kill zone.

These reflections sometimes caused an error in the total duration pulse period. A longer determination of total duration pulse period caused the algorithm to incorrectly identify the projectile. The predemonstration test matrix and results are located in Appendix L.

In an effort to separate any ground reflection from the N -Wave, the target was raised approximately 0.5 m for the demonstration test on 15 July 1993. The store mode was turned off so the RDS would compute real-time data reduction. The M1A1 with TPGID fired 10 projectiles. Only 3 of 10 TPGID rounds were identified as TPGID's. Similar results were recorded with the other projectile types fired. Problems were also encountered with the RETS interface. The RETS shorted during the demonstration and did not respond to the RDS communication. At that time, it was not known why the RDS performed so poorly. It was thought that ground reflections seen from the previous day caused the problems.

On the following day, the RDS was set up again with the store mode activated. Many projectiles were fired to gather data in the field. Due to rain, most of the data were not useful. Upon our retum to APG, the pretest data were analyzed. It was determined that reflections were coming from the ground and from the top of the microphone stake. When the projectiles were fired around the microphone height or higher, the reflections were very close in time to the original N -Wave or even superimposed on the N -wave (see Figure 43). These reflections were mathematically determined to initiate from the flat surface on top of the microphone support stake (see Figure 44).


Figure 43. Microphone output due to a reflected N-Wave.


Figure 44. Microphone support stake.

The microphone location relative to the stake and ground surface was measured during this test. The shock's speed, projectile's speed, and, therefore, the Mach angle were also measured. The location of the projectile was hand scored at the conclusion of the test. The pressure time history of the N -Waves was recorded. Therefore, the distance that the shock wave traveled over time could be calculated. This value is represented as DIST1 and DIST2 for high-fidelity microphones 1 and 2. This distance was compared with the actual distance the shock wave would have traveled if reflected from the ground or the stake. The stake reflection represents the actual distance the shock wave traveled from the projectile to the microphone using the stake as a reflecting surface. By comparing the calculated reflection distance with those due to the ground or stake it can be shown in Table 21 that at least five of the projectiles had their N -Waves reflected off of the stake. Only those projectiles fired above the microphones had their shock waves reflected off of the stake. Only three of the five caused algorithm problems when computing N -Wave duration.

As a consequence of raising the target in the demonstration test, the projectiles were fired higher relative to the ground level. This separated the time between N -Wave and ground reflections but caused the problem of stake reflections. They were even more prevalent than during the pretest and resulted in the poor demonstration results. The problem could have been resolved by using a tripod to hold the microphone or angling the top of the stakes.

Table 21. 7th ATC Demonstration Results Analysis

| $\begin{aligned} & \text { Round } \\ & \text { No. } \end{aligned}$ | Mach Angle (rad) | Time diff 1 <br> ( $\mu \mathrm{s}$ ) | Time diff 2 <br> ( $\mu \mathrm{S}$ ) | Dist1 <br> (m) | Dist2 <br> (m) | Hand Scored Locations |  | $\begin{aligned} & \text { Ground } \\ & \text { refl } \\ & (\mathrm{m}) \end{aligned}$ | Stake refl <br> (m) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | $\begin{gathered} \mathrm{X} \\ (\mathrm{~m}) \end{gathered}$ | $\begin{gathered} \mathrm{Z} \\ (\mathrm{~m}) \end{gathered}$ |  |  |
| 1 | 0.27 | 4,092 |  | 1.3 |  | 0.552 | 0.229 | 1.2 |  |
| 2 | 0.37 | 1,000 | 1,000 | 0.3 | 0.3 | 0.305 | 0.686 | 1.7 | 0.3 |
| 3 | 0.48 | 516 | 476 | 0.2 | 0.1 |  |  |  |  |
| 4 | 0.61 | 1,004 | 1,316 | 0.3 | 0.4 |  |  |  |  |
| 5 | 0.58 |  |  |  |  |  |  |  |  |
| 6 | 0.38 | 2,364 |  | 0.7 |  | 0.641 | 1.842 | 2.8 | 1.2 |
| 7 | 0.38 | 1,828 | 1,616 | 0.6 | 0.5 | 0.787 | 1.334 | 2.3 | 0.7 |
| 8 | 0.31 | 4,112 | 3,900 | 1.3 | 1.2 | 1.029 | 0.203 | 1.0 |  |
| 9 | 0.31 | 3,724 | 4,428 | 1.2 | 1.4 | 0.457 | 0.210 | 1.2 |  |
| 10 | 0.66 | 928 |  | 0.2 |  | 1.422 | 0.734 | 1.7 | 0.3 |
| 11 | 0.56 | 2,940 | 2,228 | 0.8 | 0.6 | 1.168 | 1.524 | 2.5 | 0.5 |
| 12 | 0.60 |  | 6,176 |  | 1.7 |  |  |  |  |

## 12. CONCLUSIONS/RECOMMENDATIONS/FUTURE PLANS

The goal of this project was to determine if round discrimination were feasible using acoustic signatures. If it were, the secondary goal was to build a RDS to perform on a live-fire gunnery range. The first goal was achieved without any doubt. The models created, both theoretical and empirical, worked very well. The sensors used were excellent laboratory instruments. The data recording and analysis equipment was well chosen for this endeavor and produced an excellent database. The extent of the database was more than sufficient for the analyses. The intellectual contribution from outside agencies was tremendous and directly impacted the success of the program.

The secondary goal was only partially achieved. Hampered by technical problems, the final demonstration at the 7th ATC was not the great success desired. Although the RDS performed extremely well on the last days of the validation/verification test, the weather and unforeseen technical problems precluded a favorable result at Grafenwoehr. This can be most likely attributed to the urgent nature of having to demonstrate the RDS before the planned development date. The models were incorporated into a powerful, flexible system that allowed for easy modification. The instrumentation was extremely reliable laboratory equipment but was severely affected by the outdoor environment. Because of the time devoted to hardware performance after the verification test, little attention was given to the reflection phenomenon discovered during the verification test. Ultimately, this problem manifested itself into a significant major technical problem during the final demonstration.

A retrospective analysis sheds new light on these problems. Apparently, the shock incident to the wood microphone stand was reflected. The reflection was actually returning to the microphone before the N -Wave duration was completed. In differentiating the signal, additional peaks were encountered, and incorrect durations were calculated. This is the primary reason smaller rounds were being calculated as large tank training rounds. The RETS equipment failed to perform due to the electronic short in the RETS, affecting the testing on the third day. If these small problems are allowed to be worked out, there is a high degree of confidence that a working RDS could be used on a live-fire gunnery range.

A test plan has been developed to continue the RDS development. Future modifications include employing different microphone setups. A possible setup involves discrimination microphones that reside on ground level so only one N-Wave signature will be analyzed. Improvements to the data acquisition and reduction program will be made. The N -Wave period can be better determined by using maximum and minimum peaks, zero crossings, as well as the slopes. Ruggedizing the microphone hardware will greatly enhance the survivability in the rain and snow. These concepts will be field tested on a U.S. Army training range, such as Fort Knox or Fort Stewart, that closely resembles the terrain of Grafenwoehr. The data will be analyzed and correlated with the N -Wave signatures that already reside in the data base.

For a future demonstration of the proof-of-concept, the same RDS brassboard should be used with a new high-fidelity four-microphone system. Two low-cost high-fidelity microphones with high sensitivity should be used to process the N -Waves of small rounds, and two pressure transducers with high-dynamic range should be used to process the N -Waves of large tank rounds. Both microphones and transducers must be environment-resistant and ruggedized. The current RDS hardware must be modified to
accommodate two additional transducer inputs. The signal processing algorithm must be modified to isolate the N -Wave from its reflection. The discrimination algorithm should incorporate durations from the transducers. Several more field tests are needed to characterize the responses of the pressure transducers. There is a high degree of confidence that these improvements to the hardware and the algorithm will allow the RDS to perform at its potential and permit total achievement of the goals of this project.

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## APPENDIX A:

FEASIBILITY TEST RANGE DATA

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| E669 | 982＇I | $\overline{\text { c }}$ | 48 | ［t | $\square 9$ | LSI | ¢G：8z：IL | 26／Ez／6 | ＂ | ＂ | 82 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ع169 | ¢ $¢$ ¢ | $19 \%$ | 68 | $8 \varepsilon$ | $\pm 9$ | 6 SI | 88：9z：11 | Z6／£Z／6 | ＂ | $\cdots$ | $\angle 2$ |
| E6S＇9 | SGZO | \％9\％ | 9.4 | 95 | $\square 9$ | 8 SI | 90：もて：II | て6／EZ／6 | ＂ | ＂ | 92 |
| \＆18＇9 | SELO－ | 29＇乙 | $\mathrm{C}^{\prime} / 2$ | 69 | 59 | 8 SI | 91：Ez：II | Z6／Ez／6 | ＂ | ＂ | Gz |
| عとL＇9 | Sc00 | $19 \%$ | 08 | ＇19 | $\pm 9$ | 9 GI | てع：てて：II | 乙6／Ez／6 | ＂ | ＂ | ゅて |
| EtG＇9 | SLEO | E9\％ | $\downarrow 9$ | 69 | $\pm 9$ | 9 GI | 08：61：II | 26／EZ／6 | ＂ | ＂ | $\varepsilon 乙$ |
| EOS $\angle$ | Sャで0 | $19 \%$ | 8.8 | IS | $\varepsilon 9$ | 9 GI | 80： $21: I L$ | 26／Ez／6 | ＂ | ＂ | てZ |
| E669 | SOt 0 | 69.2 | 88 | ＇IS | $\varepsilon 9$ | $9 \cdot \mathrm{GI}$ | $\varepsilon ¢: \angle \mathrm{F}: 0 \mathrm{l}$ | 26／Ez／6 | ＂ | ＂ | IZ |
| E8E\％ | SE00 ${ }^{-}$ | $69 \%$ | 88 | IS | $\varepsilon 9$ | 9 GL | あち：9\％：0L | 26／Ez／6 | ＂ | ＂ | 02 |
| ع189 | G9G0 | $69 \%$ | 88 | ＇IS | $\varepsilon 9$ | 9 GI | もでど：01 | Z6／Ez／6 | ＂ | ＂ | 61 |
| E69＇G | SLLO－ | $19 \%$ | 88 | IS | $\varepsilon 9$ | $9 . \mathrm{GI}$ | ع1：68：01 | Z6／Ez／6 | ＂ | ＂ | 81 |
| \＆SU＇9 | S8t0 | $89^{\circ} \mathrm{Z}$ | 88 | IS | $\varepsilon 9$ | $9 . \mathrm{GI}$ | LG：GE：01 | て6／عz／6 | ع6LW | Gz | 4 |
| \＆ 299 | Sbで0 | $10 \cdot \varepsilon$ | 89 | 0zz | 98 | $9 . L Z$ | GI：61：GI | Z6／zz／6 | $\cdots$ | ＂ | 91 |
| $\varepsilon ¢ 9.9$ | S9E0 | $10 . \varepsilon$ | 89 | 622 | 98 | S $\angle L$ | 81：81：GI | Z6／zZ／6 | ＂ | ＂ | SI |
| 8649 | SZIO | $20 \varepsilon$ | $\angle \mathrm{S}$ | －0¢z | 98 | ${ }^{+} \mathrm{L} L$ | Sl：LI：GI | 26／22／6 | ＂ | $\cdots$ | OI |
| ع¢8．9 | ¢SZ＇0 | 66.2 | て＇S | ＇0¢z | 98 | S $\angle L$ | Gs：GI：GI | 26／Zて／6 | LE8W | ＂ | $\varepsilon 1$ |
| EL69 | SLZO | tst | $\tau 9$ | OZて | 98 | † $\angle 乙$ | 0t：EL：GI | 26／z2／6 | ＂ | ＂ | ZI |
| EZL＇9 | SILO | Stio | 99 | ＇IEz | 98 | $\varepsilon \angle L$ | L0：LI：GI | 26／zz／6 | ＂ | $\cdots$ | L |
| 8069 | SOLO | $\angle \mathrm{E}$ \％ | 19 | $0 ¢$ | 98 |  | ع¢：60：G1 | 26／2z／6 | ＂ | ＂ | 01 |
| Et0\％ | SILO | ES ${ }^{\text {b }}$ | ZG | －0¢z | 98 |  | IS：LO：GI | て6／てz／6 | 598W | 021 | 6 |
| £ 669 | GUE\％ | $80^{\circ} \mathrm{E}$ | $0 \downarrow$ | ＇GEz | 98 | S $\angle 2$ | 1も：8¢：も | 26／22／6 | $\cdots$ | ${ }^{\prime}$ | 8 |
| E¢69 | SLZ\％ | LT＇ | 8＇ | OZZ | $\angle 8$ | 697 |  | 26／22／6 | ＂ | ＂ | $\angle$ |
| EL69 | ceto | $60 \varepsilon$ | GG | － 9 ¢ | $\angle 8$ | $0 \angle Z$ | 0ヶこてども | 26／2て／6 | $\cdots$ | $\cdots$ | 9 |
| ELZ＇L | GEt 0 | L＇E | $6{ }^{6}$ | ＇9Ez | $\angle 8$ | 697 | －10：LE：ち | 26／22／6 | 06\％N | ＂ | G |
| E6L＇9 | S000 | 0で | $8{ }^{\text {\％}}$ | ＇8દ | $\angle 8$ | 6.92 | 00：ちですI | Z6／こて／6 | ＂ | $\cdots$ | † |
| $\varepsilon ¢^{\circ} 0^{\circ}$ | SELO | 0です | L＇9 | ＇İZ | $\angle 8$ | でLZ | 80：02：\％1 | 26／2て／6 | ＂ | $\cdots$ | $\varepsilon$ |
| $\varepsilon \angle O L$ | SEZ\％ | こで | 0.9 | ＇8¢て | $\angle 8$ | $0 \angle Z$ | z1：cl：\％ | 26／22／6 | $\cdots$ | ＂ | z |
| E9G9 | S850 | aN | 09 | ＇8¢2 | $\angle 8$ | $0 \angle L$ | 00：LE：01 | 26／2て／6 | †ZLW | G01 | 1 |
| （u） | （u） |  | （s／u）SM | （अәр） 1 M | \％ | （ ） | $\mathrm{S}=\mathrm{W}: \mathrm{H}$ |  |  | （Lum） |  |
| Z | $\lambda$ | ON HOVW |  | NIM | WกH 7ay | dWGL |  |  | BdスL | Bd人L | \＃ |
| NOILVJOT 2 VdWI |  | 7VNINさgl |  | SNOILIC | NOOLAW |  | AWIL | Glva | as | Nกכ | as |


| aN | aN | aN | 60 | ＇ 81 | 86 | ¢ 91 | 00：とて：ぁI | 26／8 $\overline{\text { a } / 6 ~}$ | をてLW | S01 | 95 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CEL＇$\angle$ | LIE0 | 097 | 9.1 | 82 | 86 | $\downarrow$ ¢ SI | 91：01：LI | 26／82／6 | ${ }^{\prime \prime}$ | $\cdots$ | SS |
| 4069 | $\varepsilon \angle Z 0^{-}$ | Sçz | $\underline{9}$ | 62 | 86 | $\varepsilon \cdot \mathrm{SI}$ | 6G：80：LI | 26／82／6 | ＂ | ＂ | bs |
| LOF9 | \＆ $200^{-}$ | $09 \%$ | 91 | － 0 | 86 | Z＇SI | －L： $20: 11$ | 26／82／6 | ＂ | ＂ | \＆G |
| L6て＇9 | $\angle z \varepsilon^{\circ}$ | 8 C \％ | 9.1 | b | 86 | ISI | zS：GO：II | 26／82／6 | ＂ | ＂ | 25 |
| aN | CN | ON | 01 | GI | 86 | $1 \cdot \mathrm{GI}$ | 00：L0：LI | 26／82／6 | IE8W | ＂ | IS |
| 4189 | LSZ0 | 78＇$\varepsilon$ | $\varepsilon \cdot 1$ | 81 | 86 | I＇GI | 20：L0：LI | 26／8z／6 | ＂ | ＂ | OG |
| LS9＇9 | $\varepsilon \varepsilon 1 \%$ | $98^{\prime} \varepsilon$ | LO | ${ }^{0}$ | 86 | $1 \cdot \mathrm{SL}$ | IG：89：01 | Z6／8Z／6 | ＂ | ＂ | $6{ }^{6}$ |
| $\angle G O L$ | $\varepsilon \angle L 0^{-}$ | $98^{\circ} \mathrm{E}$ | ［＇I | 698 | 86 | 0 GL | て下： $29: 01$ | Z6／8Z／6 | ＂ | ＂ | 80 |
| $\angle 989$ | ¢9L0 | ¢8\％ | 1.1 | ＇IZ | 86 | L＇SL | 9¢：Z®：01 | 26／8Z／6 | ＂ | ＂ | $\angle \mathrm{t}$ |
| aN | aN | aN | 60 | ＇898 | 86 | 2． Gl | 00：Zて：0L | 26／8z／6 | ＂ | ＂ | 96 |
| aN | aN | aN | 80 | 8 | 86 | 0 GI | 00：Lz：01 | 26／8Z／6 | ＂ | ＂ | St |
| aN | ON | £8＇$\varepsilon$ | 29 | $\checkmark$ | \＄8 | －11 | 68：0S：6 | 26／Gz／6 | ＂ | ＂ | to |
| aN | aN | S8＇$\varepsilon$ | S L | ＇L9 | 98 | F＇LI | て¢：97：6 | 26／Sz／6 | $\cdots$ | $\cdots$ | Et |
| aN | aN | ¢8\％ | L＇8 | ＇ZL | ¢8 | も＇LI | 9ع：とャ：6 | Z6／SZ／6 | 998W | 021 | て |
| ع06．9 | Sz90 | $6 \varepsilon^{\circ} \mathrm{E}$ | $\angle L$ | ＇GS | 29 |  | Lg：0Z：ZI | Z6／£z／6 | $\cdots$ | ＂ | L |
| $\varepsilon \varepsilon \varepsilon 9$ | SSF\％ | $\angle \subset \subset$ | $\angle L$ | ＇GG | 29 | $\varepsilon \angle L$ | LL：0z：ZI | Z6／Ez／6 | ＂ | ＂ | 06 |
| とLZでL | S810 | $15 \varepsilon$ | 02 | It | 29 | でくI | ع¢：61：ZI | z6／Ez／6 | ＂ | ＂ | $6 \varepsilon$ |
| E16．9 | GL90 |  | $\downarrow$ ¢ | 80 | 29 | 1＇LL | cc：81： 21 | Z6／£Z／6 | ＂ | ＂ | $8 \varepsilon$ |
| $\varepsilon 189$ | SLLO |  | FOL | 17 | 29 | でLI | 60：81： 21 | Z6／Ez／6 | ＂ | ＂ | $L \varepsilon$ |
| ع09 4 | GZて0 | $\downarrow \varepsilon \varepsilon$ | 94 | Gs | 19 | 2゙91 | 90：96：II | 26／EZ／6 | ＂ | ＂ | 98 |
| $\varepsilon 2 \square^{\circ} \mathrm{L}$ | 9820 | $9 \varepsilon \varepsilon$ | G8 | OS | 29 | で91 | L0：Gtill | Z6／£Z／6 | ＂ | ＂ | $5 \varepsilon$ |
| aN | aN | เでと | 276 | 97 | 29 | で91 | $\varepsilon G: \varepsilon t: I I$ | 26／£Z／6 | ＂ | ＂ | $\downarrow \varepsilon$ |
| aN | aN | Lて＇$¢$ | 76 | ＇¢ | $\varepsilon 9$ | 6 Sl | E\％：0\％：IL | Z6／EZ／6 | ＂ | ＂ | $\varepsilon \varepsilon$ |
| aN | aN | ¢ ¢ ¢ | 2＇8 | ¢ $\varepsilon<$ | 79 | 1.91 | 90：68：LI | 26／£Z／6 | 016W | ＂ | て¢ |
| ELLCLL | Sos 0 | $19 \%$ | て＇8 | －8E | $\square 9$ | 0.91 | LG：E\＆：LI | Z6／EZ／6 | ＂ | ＂ | I $\varepsilon$ |
| EL8 $\angle$ | 9820 | $19 \%$ | S8 | ＇$\downarrow$ | $\square 9$ | 0.91 | LI：$¢ ¢: 1 \mathrm{~L}$ | Z6／EZ／6 | ＂ | ＂ | $0 \varepsilon$ |
| ¢ $¢ \angle$ | 9960 | $19 \%$ | 8. | OS | $\varepsilon 9$ | 8 Gl | Z¢：Z¢：LI | 26／EZ／6 | \＆6LW | SZ | 62 |
| （ $\mathbf{u}$ ） | （［1） |  | （s／w）SM | （马әр）аM | \％ | （D） | S：W：H |  |  | （ $\mathrm{u} \\| \mathrm{u}$ ） |  |
| Z | $\lambda$ | ON HOVW |  | NIM | WกH＇7 ${ }^{\text {dy }}$ | dWGL |  |  | 9dXl | Gd久L | \＃ |
| NOIL $\forall 207.10 \forall \mathrm{dWI}$ |  | 7VNIWAIS | SNOLLICNOJ Law |  |  |  | GWIL | giva | ＇ay | NกD | ad |


| ¿SLC9 | E6E0－ | 181 | $z 2$ | zzz | 86 | 261 | 02：EE9 | 76／88／6 | ＂ |  | ${ }^{58}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2099 | E660－ | 281 | 97 | sLz | 86 | $\varepsilon 61$ | 05：0¢91 | 26／88／6 | ＂ | ＂ | ¢8 |
| L859 | عоz\％－ | 181 | ¢て | zzz | 86 | F61 | Li：0¢9 | 76／88／6 | ＂ |  | ${ }^{2} 8$ |
| aN | an | an | 82 | 692 | 86 | $\varepsilon 61$ | 00：9z：91 | 76／88／6 | ＂ |  | 18 |
| an | aN | an | 92 | 292 | 86 | 261 | 0¢：cz：91 | 76／88／6 |  |  | 08 |
| an | an | an | z | T92 | 86 | $\varepsilon 61$ | 00：5z：91 | 26／88／6 | ${ }_{66 L W}$ |  | 62 |
| an | an | 42 | 12 | 885 | 86 | $\varepsilon 61$ | Esfris | Z6／88／6 |  |  | 82 |
| an | an | $49 \%$ | Iz | Litz | 86 | $\varepsilon 61$ | $8 \mathrm{Cl}: 87 \cdot 91$ | 26／88／6 |  |  | « |
| aN | an | 997 | 87 | btz | 86 | 561 | 9z：zz：9t | 26／88／6 |  |  | 9 |
| aN | an | 92 | 92 | 652 | 86 | 261 | Iz：1z：9t | 76／88／6 |  |  | $\varsigma^{5}$ |
| an | an | ¢8\％ | 92 | $\bigcirc$ | 66 | 981 | 92：07：91 | 76／88／6 |  |  | 『 |
| $\angle 889$ | csion | 182 | $\angle 1$ | ＇zzz | 86 | $\angle 81$ | 25：6199 | 76／88／6 |  |  | $\varepsilon<$ |
| 4192 | 4480 | čz | 92 | siz | 86 | 981 | 9z：s0：91 | 26／88／6 | ． |  | z |
| $\angle 89 \%$ | 4880 | 997 | 92 | 502 | 86 | ¢8i | LS：E0：91 | 76／88／6 | ． | ＂ | L |
| an | aN | an | 97 | 501 | 86 | 981 | 00：Ls：si | 76／88／6 |  |  | 02 |
| an | an | an | 92 | 5012 | 86 | 981 | 0¢：9\％：G1 | 26／88／6 | ＂ | ． | 69 |
| an | an | an | 92 | c90 | 86 | $\mathrm{c}_{88}$ | 00：99：St | 26／88／6 |  |  | 89 |
| an | an | un | 92 | ${ }^{9} 0$ | 86 | $\mathrm{c}_{681}$ | 00：z\％：91 | 26／88／6 |  |  | 49 |
| aN | aN | an | 92 | ¢90 | 86 | 981 | 00：09：91 | 26／88／6 | 016 N | ${ }_{5}$ | 99 |
| L699 | ¢890－ | $8{ }^{8} \mathrm{z}$ | Sz | z102 | 86 | 92 L | 8c：cist | 76／88／6 | $\cdots$ | ． | 99 |
| 4669 | LEE0 | ¢st | $\ddagger{ }^{\text {¢ }}$ | 702 | 86 | Z 21 | Lb：zi：St | 26／88／6 | ＂ | ＂ | $\pm 9$ |
| LSL9 | $\angle b \tau 0$ | 6 F | で | 666 | 86 | 9 g 21 | 66：12：St | 26／88／6 | ＂ |  | $\varepsilon 9$ |
| an | an | an | F | \＆iz | 86 | ¢ 21 | 00：90：51 | 26／88／6 |  | ＂ | 29 |
| an | an | an | $\varepsilon \tau$ | 612 | 46 | 691 | 00：10：St | 26／88／6 | 066W | ＂ | 19 |
| L999 | ع100－ | 26 \％ | 67 | ＇991 | 46 | ${ }_{\text {L }} \mathrm{LL}$ | 99：69：71 | 26／88／6 | $\cdots$ | ＂ | 09 |
| LS69 | Esio－ | 16. | 61 | 991 | 46 | $\varepsilon \angle 1$ | 89：89：71 | 26／88／6 | ＂ | ＂ | 69 |
| $\angle 669$ | £IIO－ | $\varepsilon 6 \varepsilon$ | 90 | Tzz | 86 | 99 | Ss：semi | 26／88／6 |  | $\cdots$ | 89 |
| aN | an | an | Hit | $\bigcirc$ | 86 | 99 | 0：0¢： 0 | 26／88／6 | bZLW | sot | Ls |
| （iu） | （u） |  | （s／u）SM | （89p）aM | \％ | （0） | SWW |  |  | （uwi） |  |
| z | $\lambda$ | On HJVW |  | NIM | WกH 79u | dW3L |  |  | 3dxL | IdxL | － |
| NOILVJO7LJVdWI |  |  | SNOLILANOJASN |  |  |  | awil | auva | Ca | NกO | ax |


| Les9 | ¢zzio- | عİ | -9 | 82 | 19 | t9r | po:zzzil | 26/66/6 | * |  | 2 II |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12SL | LS80 | It | $6{ }^{\circ}$ | ${ }^{\circ}$ | 29 | 29 | 6¢:Lz:zi | 26/68/6 | " |  | 1 II |
| $190{ }^{\circ}$ | 8190- | 418 | ז9 | Ls | 29 | z9 | os:90:z | 26/6z/6 |  |  | 0 OH |
| an | an | an | $\mathrm{c}^{9}$ |  | 19 | z91 | 00:69:II | 26/68/6 | 998N | $\cdots$ | 601 |
| 100 L | 4020 | 80 Z | 69 | ${ }^{\circ} \mathrm{Oc}$ | 29 | F91 | 80:69:11 | 26/68/6 |  | . | 801 |
| 100\% | LSt ${ }_{\text {ct }}$ | 602 | $\underline{7}$ | 92 | 29 | L91 | LE:66:IL | 26/62/6 |  | . | 201 |
| 1969 | Etzo. | 402 | 99 | ${ }^{158}$ | 29 | 991 | bp:96:IL | 26/62/6 |  |  | 901 |
| H89 | ع20\%- | $0{ }^{2}$ | $9 \varepsilon$ | ${ }^{6}$ | $\square 9$ | g<L | 88:97:11 | 26/62/6 |  |  | 901 |
| an | an | aN | 89 | LS¢ | 99 | 081 | 00:1z:Il | 26/68/6 | IE8N | 0 uz | \%01 |
| 1299 | Etio | Iç | 87 | II | 0 | s9t | 90:z\%:01 | 26/68/6 |  |  | 801 |
| 1629 | $\varepsilon \angle \varepsilon 0^{-}$ |  | $\varepsilon ¢$ | 7 | 04 | F9r | bz:os:0t | 26/68/6 | * | " | 201 |
| 1689 | 6680. | 198 | 4 | $\stackrel{L 2}{ }$ | 69 | $\varepsilon 9$ | 2z:88:01 | 26/68/6 | $\cdots$ |  | 101 |
| L 104 | ¢880 | isg | 29 | 81 | 69 | 671 | 68:60:01 | 26/62/6 |  | . | (1)1 |
| an | an | an | z9 | H | 69 | 871 | 00:zo:01 | 26/62/6 | tzLN |  | 66 |
| 1819 | 4670 | 102 | Z | $\mathrm{Si}^{\text {si }}$ | 69 | 971 | 21:10:01 | Z6//6//6 |  | . | 86 |
| Ltic | ع0\%\%- | 6 i 2 | 18 | 01 | IL | sin | vz:69:6 | 26/62/6 | . | " | 46 |
| an | an | 681 | 68 | ¢ | 02 | cıI | ss:99:6 | 26/68/6 | " | " | 96 |
| $\underline{1992}$ | 4920 | $\underline{s i z}$ | 89 | I | 92 | 6 zl | 00:98:6 | 26/67/6 |  |  | ${ }_{56}$ |
| an | an | an | 89 | - | $s_{L}$ | L2I | 00: Sce 6 | z6/68/6 | 066 W | s0t | ${ }^{\square} 6$ |
| an | an | 181 | 92 | 887 | 86 | 1.61 | 02:L8:99 | 26/88/6 | " |  | $\varepsilon 6$ |
| L889 | £ ¢ \% | 181 | $\varepsilon \tau$ | ${ }^{152}$ | 86 | 261 | 66:9999 | 26/88/6 | . |  | 26 |
| 4169 | Et50. | 181 | 91 | ¢9\% | 86 | $z 61$ | 0:9\%99 | 76/88/6 | , |  | 16 |
| Ltec | L560 | 881 | 12 | Lsz | 86 | 261 | Lz:Sc9\% | 76/88/6 |  |  | 06 |
| 442 | と12\% | 281 | $\pm 2$ | cscz | 86 | ${ }^{161}$ | ¢9:¢¢9t | 26/88/6 |  | " | 68 |
| Lzo' | EfE0- | 181 | $\varepsilon \tau$ | ${ }^{0} \mathrm{O} 2$ | 86 | ${ }^{161}$ | 97:¢¢99 | 26/88/6 | " | " | 88 |
| 4624 | LE1' | 181 | 92 | 972 | 86 | ${ }^{161}$ | L¢:¢¢9 | 26/87/6 |  | " | $\angle 8$ |
| 460 L | EbFO. | 281 | ¢ | -ssz | 86 | $z 61$ | 91:¢¢9 | 26/88/6 |  |  | 98 |
| an | an | an | 81 | \%98 | 86 | ع61 | 00:ze.9 | 76/88/6 | E6LW | ${ }_{5}$ | 98 |
| (u) | (u) |  | (s/w)SM | (3ap)am | \% | ( $)$ | s:W:H |  |  | (umu) |  |
|  | , | $\frac{\text { ONHOVW }}{\text { TVNIWZAL }}$ |  | $\frac{\text { SIM }}{\text { SNOIII }}$ | WกН 'тя | dWal | gWil | alva | $\frac{\mathrm{adXL}}{\text { ar }}$ | $\frac{\mathrm{BdNL}}{\text { NnO }}$ | \# |



| L88．9 | L9\％ 0 | $59 \%$ | $\varepsilon 9$ | ¢ $\downarrow$ | ZS | 9＇t | 0で：8t：$¢ 1$ | 26／0¢／6 | ＂ | ＂ | 891 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L09 ${ }^{\circ}$ | $\angle 00^{\circ}$ | $6 \dagger^{\prime} \mathrm{E}$ | $\dagger$ ¢ | ＇68 | $\pm G$ | t＇tu | ปて：६๕：¢ | 26／08／6 | ＂ | ＂ | L91 |
| aN | aN | aN | て＇9 | 91 | $\varepsilon G$ | でも | 00：6z：$¢ 1$ | 26／08／6 | 016W | Gz | 991 |
| $\angle L Z \cdot L$ | $\angle \mathrm{LZO}$ | $8{ }^{\circ} \mathrm{t}$ | $\varepsilon 9$ | ¢ $¢$ | 69 | でとI | Iz：¢¢： LI | 26／08／6 | ＂ | ＂ | 991 |
| $\angle \mathrm{L}$ CL | $\angle E \varepsilon^{\circ} 0$ | $80^{\circ} \mathrm{t}$ | ZS | ＇$\downarrow$ | 69 | $\varepsilon ¢ 1$ | 99：0¢：11 | 26／0ع／6 | ＂ | ＂ | 691 |
| $\angle$ LG $\angle$ | LOZ 0 | $05^{\circ}$ | L＇ | も $\varepsilon$ | 69 | $\varepsilon \varepsilon!$ | 6\％：68：LI | 乙6／0¢／6 | ＂ | ＂ | ¢91 |
| $\underline{0+L}$ | L6Z\％ | $00^{\circ}$ | 69 | ＇z¢ | 09 | S＇EI | 99：98：LI | 26／0ع／6 | ＂ | ＂ | 291 |
| $\angle \square て ゙ L$ | $\angle 90^{\circ}$ | $66^{\circ} \mathrm{t}$ | Z＇G | 62 | 69 | $0 \cdot 1$ | S0：を¢：II | 26／0ع／6 | ＂ | $\cdots$ | 191 |
| $\angle L L^{\circ} \mathrm{L}$ | $\angle Z{ }^{\circ} \mathrm{O}$ | LG＇t | 6.7 | † $\varepsilon$ | 19 | $\varepsilon ¢ 1$ | 8z：SI：LI | 26／08／6 | 998W | ＂ | 091 |
| $\angle E l \cdot L$ | $\angle \mathrm{tO} 0$ | ع0＇$¢$ | でG | ¢¢ | 29 | 9 CI | 0S：20：LI | Z6／0¢／6 | ＂ | ＂ | 6 SI |
| $\angle \square \varepsilon ์ \angle$ | $\angle 000$ | ＋0¢ | LE | $\angle$ | 29 | $9{ }^{\circ} \mathrm{E}$ I | 86：90：LI | 26／0E／6 | ＂ | ＂ | 8SI |
| LEt $\stackrel{\text { L }}{ }$ | $\angle E[0$ | $20^{\circ} \mathrm{E}$ | L® | CV | 29 | $9 . \varepsilon 1$ | $\varepsilon \mathrm{E}: 50: 11$ | 26／0ع／6 | $\ldots$ | ＂ | LSI |
| L6EL | $\angle 89^{\circ} 0$ | S0＇E | $0{ }^{\circ}$ | 15 | 29 | 9 El | 81：00：11 | 26／0ع／6 | ＂ | ＂ | 9 SI |
| $\angle t S$ | L9G0 | 50\％ | $0{ }^{\circ}$ | 酎 | 29 | 6.1 | 00：20：11 | 26／0ع／6 | ＂ | ＂ | GSI |
| $\angle E+\angle$ | $\angle 980$ | ع0＇$\varepsilon$ | Z＇G | ¢ | $\angle 9$ | I＇tI | ¢¢：G7：01 | 26／0ع／6 | IE8N | 02I | DGI |
| aN | aN | $8 て ゙ て$ | 9 G | ＇0z | 90 | でI | ャて：8て：91 | 26／6Z／6 | ＂ | ＂ | £GI |
| aN | aN | 1どて | 9 G | Oz | 97 | て＇81 | Lヵ：LZ：91 | 26／62／6 | ＂ | ＂ | ZSI |
| aN | aN | เどて | 9 G | ＇0Z | $9{ }^{\text {b }}$ | で81 | てL：LZ：91 | 26／6z／6 | ＂ | ＂ | ISI |
| aN | aN | LでZ | 69 | IZ | Gt | ［81 | £t：9z：91 | 26／62／6 | ＂ | ＂ | OGI |
| aN | aN | $6 \varepsilon \%$ |  | ¢ | St | 181 | 60：97：91 | 26／6z／6 | ＂ | ＂ | 6 tl |
| 166. | 8980 ${ }^{-}$ | $98 Z$ | でL | LI | St | 0.81 | ¢t：ちz：91 | 26／62／6 | ＂ | ＂ | 861 |
| aN | aN |  | 8.4 | IV | Gt | 981 | £¢：とて：91 | 26／62／6 | ＂ | ＂ | L t I |
| aN | aN | S\＆ | 8. | ＇IZ | St | S＇81 | 11：とで91 | 26／62／6 | ＂ | ＂ | 9bl |
| L6E＇L | L89 0 | LでZ | 08 | ＇S | 91 | ¢ 81 | 6e：てz：91 | 26／62／6 | ＂ | ＂ | StI |
| aN | aN | 9 9゙て | 06 | \％ | Sb | \＆81 | LS：1て：91 | 26／62／6 | ＂ | ＂ | D $\square_{\text {I }}$ |
| aN | aN | Gzて | 88 | てz | St | ع＇81 | LS：0Z：91 | 26／62／6 | ＂ | ＂ | EbI |
| aN | aN | LてZ | $\underline{5}$ | 81 | Gt | 2＇81 | F0：G0：91 | 26／62／6 | ＂ | $\cdots$ | 2 tL |
| aN | aN | $8 \varepsilon \square$ | で8 | $\cdot 62$ | ¢t | $1 \cdot 81$ | 10：70：91 | 26／62／6 | 0t6W | SZ | 101 |
| （ ${ }^{\text {a }}$ ） | （u） |  | （s／u）SM | （\％วр） A M | \％ | （ $)$ | S：W：H |  |  | （umu） |  |
| Z | $\lambda$ | ON HOVW |  | NIM |  | dW3L |  |  | Bdhl | Gdd． | \＃ |
| NOILVOO7 LJVdWI |  | TVNIWyal | SNOLLICNOJ Law |  |  |  | GWLL | glva | ad | NกS | ad |


| Lzel | EzLio | 697 | 69 | ＇$\varepsilon$ | $\varepsilon 9$ | 9 9It |  | 26／08／6 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| LISL | E9\％\％－ | 097 | 14 | L 2 | 29 | \＄SI | $00 \%$ crit | 26／108／6 |  |  | $\frac{161}{061}$ |
| 412 | ¢ど\％ | 192 | L 2 | $\stackrel{1}{ }$ | 29 | ＋G1 | 91：zat | \％6／108／6 | ＊ | ＂ | 681 |
| LSEL | $\angle 590$ | 197 | 92 | 08 | $\varepsilon 9$ | 9 gat | Ls：1z：\％ | 26／08／6 |  | ． | 88 t |
| L0t\％ | 980－ | 092 | 9. | $0 \varepsilon$ |  | 9 gl | ¢¢：で； | 26／08／6 | ， | ＂ | 48 |
| $\angle 29 \%$ | ELtio | 192 | $\underline{19}$ | 6 | ${ }^{\text {\％}}$ | 9 9t | co：rzi | z6／08／6 |  |  | 981 |
| LEIL | Etto | 192 | $\stackrel{1}{6}$ | \％ | \％9 | ¢GI | be：0zit | 76／08／6 | ＂ | $\cdots$ | 981 |
| 建 | 8LI ${ }^{\text {－}}$ | 092 | $\stackrel{t}{4 \%}$ | Lz | ${ }^{29}$ | Cit | 60：90：71 | 26／08／6 |  |  | ¢81 |
| $\angle L L^{\circ} \mathrm{L}$ | Esto－ | 192 | $\underline{64}$ | \％z | \％9 | lit | 00：00：41 | 26／08／6 | 86LN |  | 881 |
| L912 | ع0¢て－ | an | 69 |  | ¢ | ¢ | 00：99：Et | 26／08／6 | － | ＂ | 281 |
| L6IC | $\angle 860$ | an |  | 61 | $\varepsilon ¢$ | ¢も | 00：9c：\＆ | z6／08／6 |  |  | 181 |
| $\angle 828$ | E60\％－ | an | $\stackrel{\text { rg }}{19}$ |  |  | \＆ | 00：9c：¢ | 26／08／6 | ＂ | ＂ | 085 |
| L994 | $\angle t t^{\circ} 0$ | an | rg | $\frac{61}{61}$ | $\varepsilon ¢$ | ¢ | 00：9c：Et | 26／08／6 |  |  | 621 |
| $\angle 8 L^{2}$ | $\angle z \varepsilon_{0}$ | an | ${ }^{\text {L＇}}$ |  |  | ¢ | 00：cspel | 26／0E／6 | ＂ | $\cdots$ | 84 |
| 4208 | $\stackrel{560}{ }$ | $\frac{\mathrm{an}}{\mathrm{aN}}$ | $\frac{69}{69}$ | \％i | ${ }_{\square}^{69}$ | cit | in：Scs：ci | 26／106／6 | $\cdots$ | $\cdots$ | 44 |
| LSI 8 | $\stackrel{\angle 880}{L z \varepsilon i}$ | $\frac{\mathrm{aN}}{\mathrm{an}}$ | $\frac{69}{69}$ | 01 | $\bar{¢} \bar{¢}$ | ¢ii | 00：cs：ci | 26／08／6 |  |  | 941 |
| 209 L | Lze |  |  | 01 | $\varepsilon ¢$ | ¢ ${ }^{\text {b }}$ | 00：csci | 26／08／6 | ＂ |  | SLI |
| L889 | LEL0 | an | $\frac{69}{14}$ | ， | ${ }_{\square}$ | tit | cl：pfect | 26／08／6 |  | ＂ | tLI |
| L $\mathbf{H}^{\text {ct }}$ | Lt00 | ter | 12 | 0 | \％9 | bit | $L \mathrm{LF} \mathrm{C} ; ¢ \mathrm{El}$ | z6／08／6 | ＂ |  |  |
| L61／2 | $\angle 690$ | \＆¢¢ | 0 | $\underline{1}$ | ${ }_{\text {¢ }}$ | tit | to zicict | z6／08／6 |  |  | zLI |
| Lot＇ | $\angle 4{ }^{\circ} \mathrm{L}$ | $\mathrm{csq}_{6}$ | TL |  |  | － 71 | 8： 1 ¢c：¢ | 26／08／6 | ＂ | $\cdots$ | LLI |
| $\underline{469}$ | Eczo | 298 | $\stackrel{69}{1 / 2}$ | ¢ | $\stackrel{9}{69}$ | bit |  | 26／08／6 |  |  | 021 |
| $46 L^{\circ}$ | 4810 | $\stackrel{109}{998}$ | 48 | ${ }_{L} \mathcal{L}$ | ¢¢ | ¢ね1 | w7\％6\％：EL | 26／08／6 | ${ }^{066}$ | sz | 691 |
| LZSL | $4 t z 0$ | $9 \varepsilon \varepsilon$ | （s／u）SM | （3ap）CM | 6 | （3） | SW W ： H |  |  | （uu） |  |
| （w） | （u） | ON HOVW |  | NIM | WกH 73\％ | dWEI |  |  | ad＜L | IdxL | \＃ |
| z | $\chi$ | TYNiNzai |  | sNolut | Iaw |  | WIL | alva | ad | NnO | ad |

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APPENDIX B:
PROJECTILE CHARACTERISTICS DATA FROM FEASIBILITY TEST PHASE

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400 meter Data


400 meter Data

| shot | Round I | mici | Pos P | Neg P1 | Neg P2 | A1 | A2 | A3 | Atot | Peak | ABS | cal |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | type |  | Pa | Pa | Pa | msec 1 | msec | msec | msec | mPa-s | mPa-s | $\mathrm{Pa} / \mathrm{V}$ |
|  |  | , |  |  |  |  |  |  |  |  |  |  |
| 3. | M724 | 1 | 909.8 | 3200.0 | - | 107 | 587 | - | 694 | 52.6 | 1646.0 | 365.39 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 6 | 2857.3 | 1632.7 | - | 455 | 483 | - | 938 | 442.4 | 925.1 | 816.357 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 9 | 1332.6 | 1243.8 | - | 509 | 544 | - | 1053 | 365.3 | 723.0 | 177.68 |
|  |  | 1 |  |  |  |  |  |  |  |  |  |  |
|  |  | $12!$ | 1231.0 | 957.5 | - | 542 | 592 | - | 1134 | 281.6 | 586.7 | 854.877 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 4 | M724 | 1 | 913.5 | 3197.2 | - | 123 | 577 | - | 700 | 57.0 | 1644.0 | 365.39 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 6 | 3061.3 | 1836.8 | - | 459 | 484 | - | 943. | 453.8 | 942.0 | 816.357 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 9 | 1332.6 | 1243.8 | - | 5061 | 554 | $\cdot$ | 1060 | 362.8 | 731.4 | 177.68 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 12 | 1293.5 | 1017.3 | - | 343 | 604 | - | 1147 | 301.3 | 627.2 | 854.877 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | , |  |  |  | ! |  |  |  |  |  |  |
| 61 | M4901 | 1 |  |  |  | ! |  |  |  |  |  | 365.39 |
|  |  | i |  |  |  |  |  |  |  |  |  |  |
|  |  | 6 | 5306.3 | 3061.3 ! | - | 7311 | 897 | $\because$ | 1628 | 1329.0 | 2575.0 | 816.357 |
|  |  |  |  |  |  | 1 |  |  |  |  |  |  |
|  |  | 9 | 2785.3 | 1915.5 | - | 8531 | 986 | - | 1839 | 1132.8 | 1990.8 | 177.68 |
|  |  |  |  |  |  | 1 |  |  |  |  |  |  |
|  |  | 12 | 1658.5 | 1547.3 | - | 897! | 1084 | - | 1981 | 810.2 | 1629.3 | 854.877 |
|  |  | , |  |  |  | $!$ |  |  |  |  |  |  |
|  |  | I |  |  |  | , | - |  |  |  |  |  |
| 7 | M490 | 1 |  |  |  |  |  |  |  | + |  | 365.39 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 61 | 5102.2 | 2857.3 | - | 7271 | 1020 | - | 1747 | 1267.8 | 2523.0 | 816.357 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 9\| | 3282.9 | 3000.0 | - | 8391 | 980 | - | 1819 | 1236.7 | 2086.7 | 177.68 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 12 | 1658.5 | 1547.3 | - | 9061 | 1063 | - | 1969 | 779.2 | 1581.5 | 854.877 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 8 | M490 | 1 |  |  |  |  |  |  |  |  |  | 365.39 |
|  |  |  |  |  |  | ! |  |  |  |  |  |  |
|  |  | 61 | 5510.4 | 3061.3 | - | 805 | 874 | $\cdot$ | 1679 | 1425.1 | 2776.0 | 816.357 |
|  |  | - |  |  |  |  |  |  |  |  |  |  |
|  |  | 91 | 3260.6 | 2872.2 | - | 927 | 9681 | -1 | 1895 | 1456.6 | 2330.6 | 177.68 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 12 | 1658.5 | 1709.8 | - | 9731 | 1076 | - | 2049 | 856.0 | 1745.0 | 854.877 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | + |  |  |  |  |  |  |  |  |  |  |
|  |  | 1 |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  | ! |  |  |  |  |  |  |
|  |  | - |  |  |  |  |  |  |  |  |  |  |
|  |  | ! |  |  |  | ! |  |  |  |  |  |  |
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|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |

400 meter Data

| shot | Round I | mic | Pos P | Neg P1 | Neg P2 ! | A1 | A2 | A3 | Atot | Peak 1 | ABS | cal |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | type |  | Pa | Pa | Pa | msec: | msec | msec | msec m | mPa-s | mPa-s | $\mathrm{Pa} / \mathrm{V}$ |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 167 | M910 | 1 | 1607.2 | 2479.1 | -1 | 104 | 146 | - | 250 | 111.5 | 304.3 | 854.877 |
|  |  |  |  |  | ! |  |  |  |  |  |  |  |
|  |  | 6 | 817.2 | 760.5 | - | 1681 | 188 | - | 356 | 61.01 | 148.1 | 809.08 |
|  |  |  |  | 1 |  |  |  |  |  |  |  |  |
|  |  | 9 | 466.8 | 466.8 | - | 2131 | 189 | - | 402 | 67.1 | 112.9 | 2745.83 |
|  | , |  |  |  |  | + |  |  |  |  |  |  |
|  |  | 12 | 407.3 | 448.01 | - | 2181 | 224 | - | 442 | 54.2 | 109.5 | 2036.37 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | 1 |  |  |  |  |  |  |  |  |  |  |  |
| 168 | M910! | 11 | 1043.01 | 1282.3 | - | 126 | 155 | - | 281 | 76.1 | 193.5 | 854.877 |
|  |  |  |  |  |  | 1 |  |  |  |  |  |  |
|  |  | 6 | 946.6 | 639.2 | - | :74 | 224 | - | 398 | 73.1 | 142.8 | 809.08 |
|  |  |  |  |  |  | $!$ |  |  |  |  |  |  |
|  |  | 9 | 466.8 | 466.8 | $-1$ | $217!$ | 2211 | - | 438 | 68.3 | 116.8 | 274583 |
|  |  |  |  |  |  | i |  |  |  |  |  |  |
|  |  | 12 | 346.2 | 285.1 | -1 | 2301 | 243 | - | 463 | 43.2 | 78.1 | 2036.37 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | I |  |  |  |  |  |  |  |  |  |  |
| 169 | M910 | 1 | 1205.4 | 1521.7 | - | 119 | 153 | - | 272 | 88.8 ! | 22.0 | 854.877 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 6 | 825.3 | 639.21 | - - | 171 | 196 | - | 367 | \| 68.31 | 138.7 | 809.08 |
|  | + |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 9 | 411.8 | 411.8 | - | 219 | 192 | -1 | 411 | \| 62.7 | 101.1 | 2745.83 |
|  |  |  |  |  |  | $\bigcirc$ |  |  |  |  |  |  |
|  |  | 12) | 407.3 | 346.2 | -1 | 2101 | 239 | - | 449 | - 47.5] | 93.1 | 2036.37 |
|  |  |  |  |  |  | , |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 184 | M793 | 1 1) | 1444.7 | 957.5 | 1521.7 | 1791 | 1131 | 141 | 4331 | \| 159.3| | 383.0 | 854.877 |
|  |  |  |  |  |  | ! |  |  |  |  |  |  |
|  |  | 6 | 881.9 | 493.5 | 744.4 | 270 | 170 | 119 | 559 | 102.1 | 216.7 | 809.08 |
|  |  | I |  |  |  |  |  |  |  |  |  |  |
|  |  | 9 | 604.1 | 411.9 | 549.2 | 289 | 209 | 114 | 612 | -94.8 | 19.3 | 2745.83 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 12 | 427.6 | 346.2 | 386.9 | 3301 | 228 | 102 | 660 | \| $81.2 \mid$ | 155.9 | 2036.37 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  | : |  |  |  |  |  |  |
| 185 | M793 | 1 | 1607.2 | 1196.8 | 2000.4 | 1641 | \| 101 | 139 | 404 | \| 167.9| | 435.0 | 854.877 |
|  |  |  |  |  |  | -1 | I |  |  |  |  |  |
|  |  | $6!$ | 995.2 | 493.5 | 776.7 | 249 | 152 | 136 | 537 | \| 1115 | 236.7 | 809.08 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 9 | 631.5 | 439.3 | 631.5 | 291] | 193 | 126 | 610 | \| 104.5 | 213.1 | 2745.83 |
|  |  |  |  |  |  |  | I |  |  |  |  |  |
|  |  | 12 | 407.3 | 285.1 | 448.0 | - 3371 | 182 | 119 | 638 | [ 85.8] | 153.8 | 2036.37 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 186 | M793 | 1 | 1444.7 | 957.51 | 1598.6 | \| 1761 | 117 | 140 | 433 | 3 156.6 | 382.5 | 854.877 |
|  |  |  |  |  |  | 1 | $\square$ |  |  |  |  |  |
|  |  | 61 | 1027 | 493.5 | \| 776.7 | 2581 | 180 | 121 | 559 | 91108.3 | 238.0 | 809.08 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 9 | 659.0 | 439.3 | 631.5 | \| 282 | | ! 218 | 118 | 618 | 8. 99.31 | \| 210.3 | 2745.83 |
|  |  |  |  |  |  |  | - |  |  |  |  |  |
|  |  | 12 | 488.7 | 325.8 | 427.6 | \| 319 | - 231 | 106 | 656 | 6 ] $85.0 \mid$ | 165.4 | 2036.37 |

1000 meter Data


1000 meter Data

| shot R | Round |  | Pos P | Neg P1 | Neg P2; | A1 A2 | A3 | Atot | Peak | ABS | cal |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | type |  | Pa | Pa | Pa | msec / msec | msec | msec | mPa-s | mPa -s | $\mathrm{Pa} / \mathrm{V}$ |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  | ! |  |  |  |  |  |
| 58 | M724 | 3 | 5645.4 | -3658.8 | - | 377 ! 440 | - | 817 | 995.9 | 1893.6 | 188.79 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 6 | 1914.6 | -1556.6 | - | $465 i \quad 532$ | - | 997 | 388.6 | 835.9 | 730.78 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 9 | 1249.3 | -1166.0 | $\cdot$ | 536 i 557 | - | 1113 | 356.5 | 701.6 | 333.15 |
|  |  |  |  |  | , |  |  |  |  |  |  |
|  |  | 12 | 1112.0 | -947.0\| | - | 362: 639 | - | 1201 | 306.6 | 641.5 | 257.43 |
|  |  |  |  |  |  |  |  |  |  |  | - |
| 59 | M724 | $3!$ | 3658.8 | -3186.0 | - | 375 - 441 | $-1$ | 816 | 758.6 | 1515.9 | 188.79 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 6 | 1914.6 | -1556.6 | - | 471 ! 522 | - | 993 | 386.9 | 827.1 | 730.78 |
|  |  | 1 |  |  |  |  |  |  |  |  |  |
|  |  | 9 | 1249.3 | -1186.0 | - | 531: 578 | - | 1109 | 355.5 | 707.1 | 333.15 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 12 | 1109.0 | -943.0 | - | $5651 \quad 632$ | - | 1197 | 301.0 | 630.4 | 257.43 |
|  |  |  |  |  | 1 |  |  |  |  |  |  |
| 601 | \| M724| | 3 . | 3775.8 | -3422.1 | - | 359. 422 | - | 781 | 803.7 | 1599.5 | 188.79 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 6 | 1914.6 | -1468.9 | - | 453i 531 | - | 984 | 388.3 | 828.9 | 730.78 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 91 | 1249.3 | -1186.0 | - | 535: 568 | - | 1103! | 361.3 | 721.9 | 333.15 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 12 | 1109.5 | -965.4] | -1 | 357: 6381 | - | 1195 | 297.3 | 622.6 | 257.43 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 631 | M $490 \mid$ | 3 | 8374.6 | -3961.5 | -4018.0 | 569. $\quad 458$ | 412 | 1439 | 1597.7 | 3711.6 | 188.79 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 6 | 2828.1 | -1921.9 | -2016.5 | $740 \quad 573$ | 409 | 1722 | 1090.9 | 2326.6 | 730.78 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 9 | 2203.3 | -1435.9 | -1499.2 | 898.616 | 406 | 1920 | 969.2 | 1664.4 | 333.15 |
|  | ! |  |  |  |  |  |  |  |  |  | 257 |
|  |  | 12 | 1735.0 | -1112.0 | -1256.0 | 963 i 701 | 403 | 2067 | 824.7 | 1667.4 | 257.43 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 64 | M 490 | 3 | 7807.4 | -2142.9 | -4538.8 | $585 i \quad 219$ | 661 | 1465 | 2187.0 | 4125.4 | 188.79 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 61 | 2828.1 | -1556.6 | -2382.31 | 7161 445 | 594 | 1755 | 1090.2 | 2288.9 | 730.78 |
|  | , |  |  |  | - |  |  |  |  |  |  |
|  |  | 91 | 2018.5 | -1186.0 | -1625.8 | 8681511 | 564 | 1914 | 941.3 | 1885.3 | 333.15 |
|  |  |  |  | 1 | 1 |  |  |  |  |  |  |
|  |  | 12 | 1733.0 | -1011.0 | -1351.0 | 953: 598 | 535 | 2086 | 811.5 | 1651.3 | 257.43 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 65 | M490 | 3 | 6745.4 | -2595.9 | -3801.0 | 642366 | 537 | 1545 | 2062.8 | 3997.5 | 188.79 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 6 | 2828.1 | -1651.6 | -2016.9 | 759 ${ }^{\text {i }} 600$ | 454 | 1813 | 1034.6 | 2204.1 | 730.78 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 9 | 1998.9 | -1312.6 | -1499.2 | 918: 651 | 416 | 1985 | 936.5 | 1864.3 | 333.15 |
|  |  |  |  |  |  | 979: 727 | 405 | 2111 | 766.6 | 1583.3 | 257.43 |
|  |  | 12 | 1495.7 | -1063.2 | -1207.4 | 979: 727 | 405 | 211 | 766.6 | 1583.3 |  |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  | , |  |  |  |  |  |  |  |  |  |  |
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|  | ! |  |  |  |  |  |  |  |  |  |  |
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|  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |

1000 meter Data


1700 meter Data

| shot | Round I | mic | Pos P | Neg P1 | Neg P2 | A1 | A2 A3 | Atot | Peak | ABS | $\mathrm{cal}^{\text {cal }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | type |  | Pa | Pa | Pa | msec | msec : msec | msec | mPa -s | mPa - | $\mathrm{Pa} / \mathrm{V}$ |
|  |  |  |  |  |  |  | : |  |  | 15787 | 189.575 |
| 110 | M865 | 3 | 3317.6 | 2843.6 | - | 477 | 4601 | 937 | 881.1 | 1578.7 | 189.575 |
|  |  |  |  |  |  |  | ! |  |  |  |  |
|  |  | 6 | 2176.3 | 1696.1 | - | 576 | 532 | 1108 | 561.2 | 1026.7 | 774.493 |
|  |  |  |  | ! |  |  |  |  |  |  |  |
|  |  | 9 | 1497.8 | 1310.61 | - | 635 | 6091 | 1244 | 519.5 | 943.5 | 374.45 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 12 | 943.9 | 943.91 | - | 685 | 6531 | 1338 | 381.4 | 701.8 | 269.693 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 111 | M865 | 3 | 3791.5 | 3200.0 | - | 480 | 441 | 921 | 945.5 | 1691.7 | 189.575 |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 6 | 222.8 | 1843.3i | - | 540 | 524 | 1064 | 575.5 | 1091.1 | 774.493 |
|  |  |  |  | i |  |  | 1 |  |  |  |  |
|  |  | 9 | - | -i | $\cdots$ | - | -i | - | - | - | 774.493 |
|  |  |  |  | ; |  |  | ! |  |  |  |  |
|  |  | 12 | - | -i | -: | - | -: | - | - | - | 269.693 |
| , |  |  |  | . |  |  |  |  |  | 35300 | 189575 |
| 105 | M831 | 3 | 5987.1 | 2737.6 | 3213.5 | 711 | 5311395 | 1637 | 2041.0 | 3530.0 | 189.57 |
|  |  |  |  | - |  |  |  |  |  | 25000 | 774.493 |
|  |  | 6 | 2904.4 | 2129.9 | 1936.2 | 859 | $780 \mid 297$ | 1936 | 1156.5 | 2500.0 | 774.493 |
|  |  |  |  | 19659 | 1546.5 | 932 | 9661220 | 2118 | 1167.5 | 2404.8 | 374.45 |
|  |  | 9 | 2389.0 | 1965.9 | 1546.5 |  | 9661 |  |  |  |  |
|  |  |  | 685 | 1483.31 | 1078.8 | 1062 | $10641 \quad 134$ | 2260 | 987.1 | 1977.1 | 269.693 |
|  |  | 12 | 1685.6 |  |  |  |  |  |  |  |  |
|  |  |  |  | 1895.81 | 3674.0 | 664 | 3111543 | 1518 | 2068.0 | 3810.0 | 189.575 |
| 106 | M831 | 3. | 6224.5 | 1895.8 | 3674.0 | 664 | 311 543 |  |  |  |  |
|  |  |  |  | 1572 |  | 890 | 4981495 | 1883 | 1415.8 | 2622.3 | 774.493 |
|  |  | 61 | 3268.4 | 1572.2 | 2176.3 | 890 | 4981 |  |  | - . |  |
|  |  |  |  |  |  | 958 | 731\| 419 | 2108 | 1283.6 | 2407.2 | 374.45 |
|  |  | 9 | 2433.9 | 1497.8 | 1685.0 |  | $731 \quad 419$ |  |  |  |  |
|  |  |  |  |  |  |  | 8801288 | 2224 | 987.2 | 1835.4 | 269.693 |
|  |  | 12 | 1618.2 | 1213.61 | 1146.2 | 1056 |  | 224 |  |  |  |
|  |  |  |  | 4377 | 3673.9 | 626 | 5461325 | 149.7 | 2204.7 | 4144.4 | 189.575 |
|  |  |  | 085 | 2176.3 | 2176.3 | 819 | 6461353 | 1818 | 1541.4 | 2906.6 | 774.493 |
|  |  | 6 | 350. |  |  |  | $!$ |  |  |  |  |
|  |  | 9 | 2714.8 | 1404.2 | 18723 | 979 | 6291465 | 2073 | \| 1348.5 | 2489.8 | 374.45 |
|  |  |  |  | ! |  |  | : |  |  |  |  |
|  |  | 12 | 1955.8 | 1011.31 | 1415.9 | 1040 | 6401 575 | 2255 | \| 1053.7 | 2047.6 | 269.693 |
|  |  |  |  |  |  |  | ; |  |  |  |  |
|  | I |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  | . |  |  |  |  |
|  |  |  |  |  |  |  | - ! |  |  |  |  |
|  |  |  |  |  |  |  | $!$ |  |  |  |  |
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|  |  |  |  |  |  |  | ! |  |  |  |  |

## 1700 meter Data

| shot | Round | mic | Pos P | Neg P1 | Neg P2 | AI | A2 | A3 | Atot | Peak | ABS | cal |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | type |  | Pa | Pa | Pa | msec | msec | msec | msec | mPa-s | mPa-s | $\mathrm{Pa} / \mathrm{V}$ |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 101 | M724 | 3 | 3440.0 | 2843.6 | - | 334 | 4571 | - | 841 | 708.8 | 1411.8 | 189.575 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 6 | 2029.2 | 1649.7 | - | 473 | $555 i$ | - | 1028 | 4220 | 908.0 | 774.493 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 9 | 1217.0 | 1265.6 | - | 540 | 5941 | - | 1134 | 369.1 | 766.2 | 374.45 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 12 | 876.5 | 879.2 | - | 594 | 6171 | 1211 | 302.5 | 597.8 | 269.7 |  |
|  |  |  |  |  |  |  | - |  |  |  |  |  |
| 102 | M724 | 3 | 3437.0 | 2843.6 | - | 384 | 4551 | - | 839 | 718.4 | 1416.0 | 189.575 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 6 | 1835.6 | 1556.7 | - | 492 | 534\| | - | 1626 | 407.6 | 855.4 | 774.493 |
|  |  |  |  |  |  |  | - |  |  |  |  |  |
|  |  | 9 | 1310.6 | 1265.6 | - | 547 | 605 | - | 1152 | 383.1 | 795.2 | 374.45 |
|  |  |  |  |  |  | 592 | 6391 | - | 1231 | 316.9 | 639.1 | 269.693 |
|  |  | 12. | 976.3 | 946.6 | - | 592 | 639 | - | 1231 | 316.9 | 63.1 | 269.69 |
|  |  |  |  |  |  |  |  |  |  | 746.1 | 14733 | 189.575 |
| 103 | M724 | 3 | 3674.0 | 2963.0 |  | 373 | 445 |  | 818 | 746.1 | 1473.3 | 189.575 |
|  |  |  | 17426 | 16497 |  | 486 | 535 |  | 1021 | 423.7 | 900.0 | 774.493 |
|  |  | 6 | 1742.6 | 1649.7 |  |  |  |  |  |  |  |  |
|  |  | 9 | 1310.6 | 13143 |  | 533 | 616\| |  | 1149 | 396.0 | 831.4 | 374.45 |
|  |  | 9 |  |  |  |  |  |  |  |  |  |  |
|  |  | 12 | 976.3 | 979.0 |  | 611 | 619 |  | 1230 | 334.1 | 676.2 | 269.693 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 95 | M490 | 1. | 4507.5 | 3949.1 | 4508.5 | 513 | 475 | 497 | 1485 | 1191.1 | 3651.1 | 901.668 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 6 | 2997.3 | 2036.9 | 2137.6 | 746 | 608 | 436 | 1790 | 1114.3 | 2421.0 | 774.493 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 9 | 2175.6 | 1613.9 | 1613.9 | 901 | 6571 | 410 | 1968 | 1043.5 | 2101.0 | 374.45 |
|  |  |  |  |  |  |  |  |  |  |  | 17845 | 269.693 |
|  |  | 12 | 1786.9 | 1340.0 | 1264.9 | 962 | 778 | 372 | 2112 | 841.8 | 1784.5 | 269.693 |
| : |  |  |  |  |  |  |  |  |  |  |  |  |
| 97 | M490 | 3 | 5532.6 | 2489.1 | 3200.0 | 648 | 442 | 513 | 1603 | 1676.8 | 3339.4 | 189.575 |
|  |  |  |  |  |  |  |  |  |  |  | 22490 | 774.493 |
|  |  | 6 | 2904.4 | 1595.5 | 1889.8 | 782 | 560 | 508 | 1850 | 1094.7 | 2249.0 | 774.493 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 9 | 2059.5 | 1217.0 | 1591.4 | 926 | 5881 | 504 | 2018 | 987.5 | 1934.7 | 374.45 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 12 | 1415.9 | 1011.3 | 1213.6 | 1008 | 6491 | 486 | 2143 | 781.1 | 1596.2 | 269.693 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 98 | M490 | 3 | 7400.0 | 3437.0 | 5000.0 | 544 | 3561 | 561 | 1461 | 1972.4 | 62528 | 189.575 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 6 | 3051.5 | 2036.9 | 2176.3 | 755 | 5761 | 487 | 1818 | 1195.8 | 2492.4 | 774.493 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 9 | 2246.7 | 1497.8 | 1591.4 | 900 | 6891 | 434 | 2023 | 1066.6 | 2134.3 | 374.45 |
|  |  |  |  |  |  | 983 | 782 | 401 | 2166 | 860.0 | 1777.0 | 269.693 |
|  |  | 12 | 1685.6 | 1213.6 | 1213.6 | 983 | 782 | 401 | 2166 | 860.0 |  |  |
|  |  | - |  |  |  |  |  |  |  |  |  |  |
|  |  | - |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | - |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |

1700 meter Data

| shot | Round | mic | Pos P | Neg P1 | . e g P2 | A1 | A2 i | A3 | Atot | Peak | ABS | cal |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | type |  | Pa | Pa | Pa | msec | msec | msec | msec | mPa-s | mPas | $\mathrm{Pa} / \mathrm{V}$ |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 145 | M910 | $1)$ | 791.3 | 799.8 | - | 157 | 195 | - | 352 | 687.0 | 161.1 | 850.87 |
|  |  |  |  | 1 |  |  | , |  |  |  |  |  |
|  |  | 6 | 617.8 | 428.4 ! | - | 207 | 205 | - | 412 | 54.7 | 105.0 | 823.791 |
|  |  | 1 |  | 1 |  |  |  |  |  |  |  |  |
|  |  | 91 | 363.2 | 349.31 | - | 211 | 239 | - | 450 | 44.4 | 924 | 345.866 |
|  |  |  |  | 1 |  |  |  |  |  |  |  |  |
|  |  | 12 | 242.7 | 269.71 | - | 239 | 2381 | - | 477 | 36.7 | 72.6 | 269.693 |
|  |  |  |  |  |  |  | 1 |  |  |  |  |  |
| 146 | M910 | 1 | 1114.6 | 1284.8 | - | 127 | 176 | - | 303 | 78.5 | 210.7 | 850.87 |
|  |  |  |  | 1 |  |  |  |  |  |  |  |  |
|  |  | 6 | 716.7 | 551.9 | - | 185 | 190\| | - | 375 | 63.6 | 123.9 | 823.791 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 9 | 377.01 | 377.0 | - | 205 | 218 | - | 423 | 45.5 | 94.7 | 345.866 |
|  |  | , |  |  |  |  |  |  |  |  |  |  |
|  |  | 12 | 337.1 | 323.6 | - | 206 | 2551 | - | 461 | 42.2 | 90.1 | 269.693 |
|  | 1 |  | ! | ! |  | , |  |  |  |  |  |  |
| 148 | M910 | 1 | 791.3 | 961.51 | - | 143 | 172 ! | - | 315 | 66.8 | 199.4 | 850.87 |
|  |  |  |  | - |  |  |  |  |  |  |  |  |
|  |  | 61 | 1021.5 | 799.11 | + | 149] | 186 | - | 335 | 84.3 | 170.0 | 823.791 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 91 | 520.6 | 486.71 | - | 189 | 212 | - | 401 | 56.9 | 120.5 | 345.866 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 12 | 418.0 | 431.5 |  | 201 | 245 |  | 446 | 53.0 | 120.3 | 269.693 |
|  |  |  |  | 1 |  |  |  |  |  |  |  |  |
| 123 | M793 | 1 | 1438.0 | 1191.2 | 13529 | 206 | 167 | 155 | 528 | 178.0 | 432.7 | 850.87 |
|  | , |  | ! |  |  |  |  |  |  |  |  |  |
|  |  | 6 | 617.8 | 469.6 | 568.4\| | 323\| | 218 | 124 | 665 | 104.5 | 2224 | 823.791 |
|  |  | ! |  |  |  |  |  |  |  |  |  |  |
|  |  | $9!$ | 453.1 | 411.61 | 411.6 | 343 | 282 | 101 | 726 | 83.6 | 183.2 | 345.866 |
|  |  | 1 |  | ${ }^{\text {P }}$ |  |  |  |  |  |  |  |  |
|  |  | 121 | 364.1 | 377.6! | 364.1 | 370 | 325 | 73 | 768 | 78.0 | 165.8 | 269.693 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 124 | M793 | 1 | 1361.4 | 1038.1 \| | 1191.2 | 222 | 176 | 145 | 543 | 168.4 | 398.9 | 850.87 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 6 | 972.1 | 626.1 | 675.5 | 288 | 212 | 140 | 640 | 128.0 | 276.4 | 823.791 |
|  |  |  |  |  |  |  |  |  |  |  |  | 345.866 |
|  |  | 9 | 605.3 | 453.1 | 473.8 | 341 | 255 | 114 | 710 | 110.4 | 220.0 | 345.866 |
|  |  |  |  | ! |  |  |  |  |  |  |  |  |
|  |  | 12 | 548.9 | 431.5 | 404.5 | 368 | 3201 | 66 | 754 | 89.9 | 187.6 | 269.693 |
|  |  |  |  |  |  |  |  |  |  |  | 5040 | 85087 |
| 125 | M793 | 1 1 | 1676.2 | 1429.5 | 1676.2 | 196 | 1501 | 158 | 504 | 196.0 | 504.0 | 850.87 |
|  |  |  |  | - |  |  |  |  |  |  |  |  |
|  |  | $6 i$ | 823.8 | 676.1 | 676.1 | 304 | 2671 | 103 | 674 | \| 119.8 | 269.1 | 823.791 |
|  |  | I |  |  |  |  |  |  |  |  |  |  |
|  |  | 91 | 494.6 | 477.31 | 477.3 | 330 | 312 | 91 | 733 | - 941.0 | 211.2 | 345.866 |
|  |  |  |  | - |  |  |  |  |  |  |  |  |
|  |  | 12 | 418.0 | 364.1 | 364.1 | 344 | 357 | 78 | 778 | - 81.3 | 174.4 | 269.693 |

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APPENDIX C:
MICROPHONE DATA FROM FEASIBILITY TEST PHASE

Intentionally left blank.

All coordinates are in meters.
22SEP92
1 m microphone 6 m microphone 12 m microphone

| $\mathrm{x}: 1700.104$ | $\mathrm{y}: 0.157$ | z: 5.694 |
| :--- | :--- | :--- |
| $\mathrm{x}: 1697.448$ | $\mathrm{y}: 5.284$ | z: 5.282 |
| $\mathrm{x}: 1696.780$ | $\mathrm{y}: 1.641$ | z: 5.109 |

23SEP92
1m microphone
3 m microphone
6 m microphone
9 m microphone
12 m microphone

| $\mathrm{x}: 1700.104$ | $\mathrm{y}: 0.157$ | z: 5.523 |
| :--- | :--- | :--- |
| $\mathrm{x}: 1697.835$ | $\mathrm{y}: 1.702$ | z: 4.072 |
| $\mathrm{x}: 1697.448$ | $\mathrm{y}: 5.284$ | z: 5.118 |
| $\mathrm{x}: 1697.044$ | $\mathrm{y}: 8.485$ | z: 5.054 |
| $\mathrm{x}: 1696.780$ | $\mathrm{y}: 11.641$ | $\mathrm{z}: 4.944$ |

24SEP92
lm microphone 3 m microphone 6 m microphone 9 m microphone 12m microphone

| $\mathrm{x}: 1700.104$ | $\mathrm{y}: 0.157$ |
| :--- | :--- |
| $\mathrm{x}: 1697.835$ | $\mathrm{y}: 1.702$ |
| $\mathrm{x}: 1697.448$ | $\mathrm{y}: 5.284$ |
| $\mathrm{x}: 1697.044$ | $\mathrm{y}: 8.485$ |
| $\mathrm{x}: 1696.780$ | $\mathrm{y}: 11.641$ |

z: 5.548
$x: 1697.835 \quad y: 1.702 \quad$ z: 5.109
$x: 1697.448 \quad y: 5.284 \quad$ z: 5.139
$\mathrm{x}: 1696.780 \quad \mathrm{y}: 11.641 \quad$ z: 5.023

25SEP92
1 m microphone
3 m microphone
6 m microphone

| $\mathrm{x}: 1700.104$ | $\mathrm{y}: 0.157$ | z: 5.551 |
| :--- | :--- | :--- |
| $\mathrm{x}: 1697.835$ | $\mathrm{y}: 1.702$ | z: 5.112 |
| $\mathrm{x}: 1697.448$ | $\mathrm{y}: 5.284$ | z: 5.115 |
| $\mathrm{x}: 1697.044$ | $\mathrm{y}: 8.485$ | z: 5.075 |
| $\mathrm{x}: 1696.780$ | $\mathrm{y}: 11.641$ | z: 5.039 |

28SEP92
1 m microphone
3 m microphone
6 m microphone
9 m microphone
12 m microphone

| $\mathrm{x}: 1700.104$ | $\mathrm{y}: 0.157$ | z: 5.547 |
| :--- | :--- | :--- |
| $\mathrm{x}: 1697.835$ | $\mathrm{y}: 1.702$ | z: 5.096 |
| $\mathrm{x}: 1697.448$ | $\mathrm{y}: 5.284$ | z: 5.139 |
| $\mathrm{x}: 1697.044$ | $\mathrm{y}: 8.485$ | z: 5.066 |
| $\mathrm{x}: 1696.780$ | $\mathrm{y}: 11.641$ | z: 5.014 |

29SEP92
1 m microphone

| $\mathrm{x}: 1700.104$ | $\mathrm{y}: 0.157$ | z: 5.541 |
| :--- | :--- | :--- |
| $\mathrm{x}: 1697.835$ | $\mathrm{y}: 1.702$ | z: 5.090 |
| $\mathrm{x}: 1697.448$ | $\mathrm{y}: 5.284$ | z: 5.121 |
| $\mathrm{x}: 1697.044$ | $\mathrm{y}: 8.485$ | z: 5.087 |
| $\mathrm{x}: 1696.780$ | $\mathrm{y}: 11.641$ | $\mathrm{z}: 5.008$ |

30SEP92

| lm microphone | $\mathrm{x}: 1700.104$ | $\mathrm{y}: 0.157$ | $\mathrm{z}: 5.547$ |
| :--- | :--- | :--- | :--- |
| 3 m microphone | $\mathrm{x}: 1697.835$ | $\mathrm{y}: 1.702$ | $\mathrm{z}: 5.108$ |
| 6m microphone | $\mathrm{x}: 1697.448$ | $\mathrm{y}: 5.284$ | $\mathrm{z}: 5.136$ |
| 9 m microphone | $\mathrm{x}: 1697.044$ | $\mathrm{y}: 8.485$ | $\mathrm{z}: 5.084$ |
| 12 m microphone | $\mathrm{x}: 1696.780$ | $\mathrm{y}: 11.641$ | $\mathrm{z}: 5.026$ |

## FEASIBILITY TEST ROUND LOCATION MICROPHONE POSITIONS:

All coordinates are in meters.

Array 1

21SEP92

| sensor 1 | $\mathrm{x}: 1697.846$ | $\mathrm{y}:-4.458$ | $\mathrm{z}: 3.385$ |
| :--- | :--- | :--- | :--- |
| sensor 2 | $\mathrm{x}: 1697.151$ | $\mathrm{y}: 0.128$ | $\mathrm{z}: 4.691$ |
| sensor 3 | $\mathrm{x}: 1696.569$ | $\mathrm{y}: 4.278$ | $\mathrm{z}: 5.226$ |
| sensor 4 | $\mathrm{x}: 1699.552$ | $\mathrm{y}:-5.346$ | $\mathrm{z}: 5.976$ |
| sensor 5 | $\mathrm{x}: 1699.348$ | $\mathrm{y}: 0.009$ | $\mathrm{z}: 4.949$ |
| sensor 6 | $\mathrm{x}: 1699.222$ | $\mathrm{y}: 5.276$ | $\mathrm{z}: 5.977$ |

Array 2

28SEP92

| sensor 1 | $\mathrm{x}: 1697.852$ | $\mathrm{y}:-4.444$ | $\mathrm{z}: 3.382$ |
| :--- | :--- | :--- | :--- |
| sensor 2 | $\mathrm{x}: 1697.108$ | $\mathrm{y}: 0.125$ | $\mathrm{z}: 4.468$ |
| sensor 3 | $\mathrm{x}: 1696.554$ | $\mathrm{y}: 4.277$ | $\mathrm{z}: 5.222$ |
| sensor 4 | $\mathrm{x}: 1699.520$ | $\mathrm{y}:-5.323$ | $\mathrm{z}: 5.969$ |
| sensor 5 | $\mathrm{x}: 1699.475$ | $\mathrm{y}: 0.056$ | $\mathrm{z}: 4.901$ |
| sensor 6 | $\mathrm{x}: 1699.238$ | $\mathrm{y}: 5.273$ | $\mathrm{z}: 5.972$ |

Change during testing

| sensor 1 | $\Delta \mathrm{x}: 0.006$ | $\Delta \mathrm{y}: 0.014$ | $\Delta \mathrm{z}:-0.003$ |
| :--- | :--- | :--- | :--- |
| sensor 2 | $\Delta \mathrm{x}:-0.043$ | $\Delta \mathrm{y}:-0.003$ | $\Delta \mathrm{z}:-0.223$ |
| sensor 3 | $\Delta \mathrm{x}:-0.015$ | $\Delta \mathrm{y}:-0.001$ | $\Delta \mathrm{z}:-0.004$ |
| sensor 4 | $\Delta \mathrm{x}:-0.032$ | $\Delta \mathrm{y}: 0.023$ | $\Delta \mathrm{z}: 0.002$ |
| sensor 5 | $\Delta \mathrm{x}: 0.127$ | $\Delta \mathrm{y}: 0.047$ | $\Delta \mathrm{z}:-0.048$ |
| sensor 6 | $\Delta \mathrm{x}: 0.016$ | $\Delta \mathrm{y}:-0.003$ | $\Delta \mathrm{z}:-0.025$ |

## FEASIBILITY TEST GUN POSITIONS:

All coordinates are in meters.
400 meter Range
22SEP92

| M60 | x: 1299.993 | y: 24.205 | z: 3.735 |
| :--- | :--- | :--- | :--- |
| M1A1 | x: 1299.666 | y: 24.539 | z: 3.558 |

23SEP92
M2 $\quad$ x: $1299.901 \quad y: 23.715 \quad$ z: 4.023
1000 meter Range
28SEP92

| M1A1 | $\mathrm{x}: 700.059$ | $\mathrm{y}: 6.717$ | z:2.335 |
| :--- | :--- | :--- | :--- |
| M60 | $\mathrm{x}: 700.017$ | $\mathrm{y}: 9.122$ | $\mathrm{x}: 4.282$ |
| M2 | $\mathrm{x}: 699.711$ | $\mathrm{y}: 9.160$ | $\mathrm{x}: 4.617$ |

1700 meter Range
29SEP92

| M60 | x: 0.024 | y: 1.739 | z: 4.007 |
| :--- | :--- | :--- | :--- |
| M1A1 | x: 0.033 | y: 2.299 | z: 3.723 |

1400 meter Range
29SEP92
M2 x: $299.572 \quad y: 4.877 \quad$ z: 4.510

400 meter Range
30SEP92
M1A1 x: $1299.639 \quad y: 24.031 \quad$ z: 3.489
$\begin{array}{llll}\text { M2 } & \text { x: } 1300.034 & y: 24.603 & \text { x: } 4.012\end{array}$

| RD. |  | Offset Distance |  |  |  |  | Arrival Time |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NO. | HMic1 | HMic2 | HMic3 | HMic4 | HMic5 | LMic1 | LMic2 | LMic3 | LMic4 | LMic5 | LMic6 |
| Consec. | (m) | (m) | (m) | (m) | (m) | (msec) | (msec) | (msec) | (msec) | (msec) | (msec) |
| 1 | 0.969 | ND | 4.870 | ND | 11.151 | DNA | DNA | DNA | DNA | DNA | DNA |
| 2 | 1.381 | ND | 5.357 | ND | 11.574 | 8.560 | 0.000 | 4.080 | 11.400 | 0.864 | 7.840 |
| 3 | 1.359 | ND | 5.445 | ND | 11.669 | 8.400 | 0.000 | 4.240 | 11.200 | 0.832 | 8.160 |
| 4 | 1.109 | ND | 5.491 | ND | 11.757 | 8.560 | 0.000 | 4.960 | 11.400 | 0.816 | 9.040 |
| 5 | 1.603 | ND | 5.242 | ND | 11.413 | 8.480 | 0.000 | 2.560 | 11.400 | 1.340 | 7.120 |
| 6 | 1.309 | ND | 5.135 | ND | 11.360 | 8.960 | 0.000 | 2.960 | 12.200 | 1.420 | 7.600 |
| 7 | 1.245 | ND | 5.274 | ND | 11.511 | 8.640 | 0.000 | 3.640 | 12.000 | 1.340 | 8.240 |
| 8 | 1.248 | ND | 5.246 | ND | 11.482 | 8.720 | 0.000 | 3.480 | 12.100 | 1.340 | 8.080 |
| 9 | 1.350 | ND | 5.461 | ND | 11.687 | 8.360 | 0.0000 | 4.290 | 11.250 | 0.730 | 8.190 |
| 10 | 1.234 | ND | 5.141 | ND | 11.378 | 9.040 | 0.0060 | 3.440 | 11.900 | 0.808 | 7.360 |
| 11 | 1.064 | ND | 5.588 | ND | 11.866 | 8.160 | 0.000 | 5.360 | 11.100 | 0.744 | 9.680 |
| 12 | 1.225 | ND | 5.268 | ND | 11.508 | 9.040 | 0.000 | 3.600 | 12.000 | 0.768 | 7.440 |
| 13 | 1.143 | ND | 5.263 | ND | 11.516 | 8.880 | 0.000 | 3.640 | 12.200 | 1.520 | 8.400 |
| 14 | 1.099 | ND | 5.376 | ND | 11.638 | 8.640 | 0.000 | 4.080 | 12.200 | 1.460 | 8.960 |
| 15 | 0.962 | ND | 5.101 | ND | 11.379 | 9.440 | 0.000 | 3.760 | 13.000 | 1.520 | 8.640 |
| 16 | 0.933 | ND | 5.214 | ND | 11.496 | 9.280 | 0.000 | 4.040 | 12.800 | 1.480 | 8.960 |
| 17 | 0.833 | 2.951 | 5.844 | 9.025 | 12.177 | 8.000 | 0.000 | 7.550 | 11.860 | 1.875 | 13.400 |
| 18 | 0.888 | 2.910 | 6.026 | 9.222 | 12.379 | 7.920 | 0.000 | 8.760 | 11.870 | 1.930 | 14.720 |
| 19 | 1.353 | 2.967 | 5.014 | 8.113 | 11.233 | 9.120 | 0.000 | 3.680 | 12.600 | 1.820 | 9.000 |
| 20 | 1.870 | 3.739 | 5.781 | 8.833 | 11.928 | 6.960 | 0.000 | 4.240 | 10.500 | 1.680 | 9.360 |
| 21 | 1.491 | 3.196 | 5.227 | 8.309 | 11.421 | 8.640 | 0.000 | 3.600 | 11.900 | 1.760 | 8.800 |
| 22 | 1.982 | 3.728 | 5.575 | 8.596 | 11.680 | 7.520 | 0.000 | 3.440 | 10.700 | 1.840 | 8.320 |
| 23 | 1.043 | 2.805 | 5.112 | 8.246 | 11.379 | 9.360 | 0.000 | 4.560 | 12.900 | 1.800 | 9.920 |
| 24 | 1.214 | 3.129 | 5.473 | 8.596 | 11.723 | 8.160 | 0.000 | 4.880 | 11.800 | 1.760 | 10.500 |
| 25 | 1.323 | 3.300 | 5.678 | 8.798 | 11.923 | 7.680 | 0.000 | 5.360 | 11.100 | 1.680 | 10.600 |
| 26 | 1.074 | 2.907 | 5.241 | 8.373 | 11.505 | 8.880 | 0.000 | 4.800 | 12.500 | 1.760 | 10.100 |
| 27 | 1.822 | 2.865 | 4.338 | 7.388 | 10.492 | 10.200 | 0.000 | 0.700 | 13.800 | 1.920 | 5.680 |
| 28 | 1.853 | 2.951 | 4.417 | 7.457 | 10.557 | 10.100 | 0.000 | 0.880 | 13.600 | 1.880 | 5.800 |


| RD. |  | Offset Distance |  |  |  |  | Arrival Time |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NO. | HMic1 | HMic2 | HMic3 | HMic4 | HMic5 | LMic1 | LMic2 | LMic3 | LMic4 | LMic5 | LMic6 |
| Consec. | (m) | (m) | (m) | (m) | (m) | (msec) | (msec) | (msec) | (msec) | (msec) | (msec) |
| 29 | 2.353 | 3.734 | 5.049 | 7.983 | 11.034 | 8.400 | 0.000 | 1.200 | 11.600 | 1.840 | 5.680 |
| 30 | 2.432 | 3.910 | 5.276 | 8.200 | 11.244 | 7.920 | 0.000 | 1.630 | 11.000 | 1.760 | 6.240 |
| 31 | 2.217 | 3.833 | 5.438 | 8.411 | 11.475 | 7.760 | 0.000 | 2.440 | 10.800 | 1.800 | 7.040 |
| 32 | ND | ND | ND | ND | ND | 6.320 | 0.000 | 0.760 | 8.400 | 1.240 | 3.840 |
| 33 | ND | ND | ND | ND | ND | 5.280 | 0.000 | -0.640 | 7.200 | 1.280 | 1.600 |
| 34 | ND | ND | ND | ND | ND | 9.600 | 0.000 | -1.560 | 12.600 | 1.480 | 1.960 |
| 35 | 1.904 | 3.638 | 5.505 | 8.535 | 11.623 | 7.600 | 0.000 | 3.640 | 10.400 | 1.200 | 8.000 |
| 36 | 2.097 | 3.755 | 5.458 | 8.453 | 11.527 | 7.680 | 0.000 | 3.200 | 10.400 | 1.280 | 7.400 |
| 37 | 1.290 | 3.138 | 5.383 | 8.494 | 11.617 | 8.320 | 0.000 | 5.000 | 11.470 | 1.225 | 9.790 |
| 38 | 1.483 | 3.021 | 4.946 | 8.028 | 11.141 | 9.680 | 0.000 | 3.600 | 13.070 | 1.290 | 8.380 |
| 39 | 1.750 | 3.542 | 5.536 | 8.592 | 11.690 | 9.440 | 0.000 | 5.840 | 12.700 | 1.160 | 10.780 |
| 40 | 0.863 | 2.582 | 4.980 | 8.131 | 11.272 | 10.000 | 0.000 | 4.880 | 13.430 | 1.275 | 9.910 |
| 41 | 1.457 | 3.029 | 4.989 | 8.075 | 11.189 | 9.360 | 0.000 | 3.520 | 12.470 | 1.315 | 8.120 |
| 42 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 43 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 44 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 45 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 46 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 47 | 1.358 | 2.572 | 5.715 | 8.834 | 11.949 | 6.590 | 0.000 | 5.810 | 9.850 | 0.605 | 9.970 |
| 48 | 1.546 | 2.713 | 5.784 | 8.884 | 11.989 | 6.160 | 0.000 | 5.440 | 9.310 | 0.615 | 9.540 |
| 49 | 1.147 | 2.409 | 5.626 | 8.764 | 11.888 | 7.040 | 0.000 | 6.030 | 10.330 | 0.450 | 10.200 |
| 50 | 1.274 | 2.247 | 5.300 | 8.412 | 11.526 | 7.730 | 0.000 | 4.700 | 11.070 | 0.645 | 9.010 |
| 51 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 52 | 0.769 | 1.826 | 5.090 | 8.250 | 11.387 | 8.820 | 0.000 | 5.030 | 12.760 | 1.625 | 10.350 |
| 53 | 0.879 | 2.167 | 5.456 | 8.613 | 11.747 | 7.740 | 0.000 | 5.770 | 11.550 | 1.525 | 11.100 |
| 54 | 1.465 | 2.707 | 5.844 | 8.958 | 12.070 | 6.000 | 0.000 | 5.200 | 9.710 | 1.625 | 10.360 |
| 55 | 1.598 | 2.467 | 5.354 | 8.426 | 11.521 | 7.120 | 0.000 | 3.600 | 10.840 | 1.560 | 8.480 |
| 56 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |


| RD. |  | Offset Distance |  |  |  |  | Arrival Time |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NO. | HMicl | HMic2 | HMic3 | HMic4 | HMic5 | LMic1 | LMic2 | LMic3 | LMic4 | LMic5 | LMic6 |
| Consec. | (m) | (m) | (m) | (m) | (m) | (msec) | (msec) | (msec) | (msec) | (msec) | (msec) |
| 57 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 58 | 1.416 | 2.585 | 5.689 | 8.799 | 11.910 | 6.530 | 0.000 | 5.560 | 9.730 | 0.530 | 9.670 |
| 59 | 1.444 | 2.628 | 5.733 | 8.843 | 11.953 | 6.695 | 0.000 | 5.465 | 9.850 | 0.520 | 9.530 |
| 60 | 1.034 | 2.259 | 5.486 | 8.630 | 11.757 | 7.685 | 0.000 | 5.880 | 11.020 | 0.640 | 10.210 |
| 61 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 62 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 63 | 1.213 | 2.208 | 5.290 | 8.410 | 11.527 | 8.000 | 0.000 | 4.215 | 11.890 | 1.690 | 9.370 |
| 64 | 1.461 | 2.340 | 5.284 | 8.374 | 11.477 | 7.665 | 0.000 | 3.615 | 11.390 | 1.615 | 8.500 |
| 65 | 1.424 | 2.873 | 6.167 | 9.312 | 12.438 | 5.360 | 0.000 | 6.315 | 9.210 | 1.640 | 11.620 |
| 66 | ND | ND | ND | ND | ND | DNA | DNA | DNA | UNA | DNA | DNA |
| 67 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 68 | - ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 69 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 70 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 71 | 2.201 | 2.681 | 5.092 | 8.059 | 11.108 | 7.765 | 0.000 | 1.615 | 11.310 | 1.520 | 5.910 |
| 72 | 2.192 | 2.653 | 5.056 | 8.024 | 11.074 | 7.965 | 0.000 | 1170 | 11.430 | 1.430 | 5.740 |
| 73 | 1.344 | 2.432 | 5.512 | 8.622 | 11.734 | 7.460 | 0.000 | 4.825 | 11.070 | 1.275 | 9.580 |
| 74 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 75 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 76 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 77 | ND | ND | ND | ND | ND | 11.890 | 0.000 | 3.410 | 16.060 | 2.010 | 8.970 |
| 78 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 79 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 80 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 81 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 82 | 1.101 | 2.419 | 5.675 | 8.820 | 11.948 | 6.920 | 0.000 | 4.930 | 11.350 | 2.715 | 11.140 |
| 83 | 1.520 | 3.037 | 6.388 | 9.543 | 12.675 | 4.720 | 0.000 | 6.105 | 9.100 | 2.745 | 12.370 |
| 84 | 1.329 | 2.674 | 5.903 | 9.038 | 12.160 | 6.130 | 0.000 | 5.025 | 10.500 | 2.755 | 11.130 |


| RD. |  | Offset Distance |  |  |  |  | Arrival Time |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NO. | HMic1 | HMic2 | HMic3 | HMic4 | HMic5 | LMic1 | LMic2 | LMic3 | LMic4 | LMic5 | LMic6 |
| Consec. | (m) | (m) | (m) | (m) | (m) | (msec) | (msec) | (msec) | (msec) | (msec) | (msec) |
| 85 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 86 | 1.662 | 2.933 | 6.052 | 9.156 | 12.262 | 5.465 | 0.000 | 4.610 | 9.670 | 2.730 | 10.640 |
| 87 | 2.454 | 2.759 | 4.926 | 7.839 | 10.866 | 7.670 | 0.000 | 0.180 | 11.820 | 2.885 | 5.480 |
| 88 | 1.562 | 2.813 | 5.935 | 9.043 | 12.152 | 5.855 | 0.000 | 4.485 | 10.070 | 2.735 | 10.560 |
| 89 | 1.841 | 3.365 | 6.700 | 9.848 | 12.974 | 3.550 | 0.000 | 6.285 | 7.780 | 2.780 | 12.500 |
| 90 | 1.970 | 2.371 | 4.858 | 7.866 | 10.936 | 8.010 | 0.000 | 1.025 | 12.280 | 2.785 | 6.650 |
| 91 | 1.538 | 2.891 | 6.092 | 9.216 | 12.332 | 5.490 | 0.000 | 5.080 | 9.740 | 2.680 | 11.180 |
| 92 | 0.951 | 2.418 | 5.782 | 8.949 | 12.087 | 6.885 | 0.000 | 5.690 | 11.440 | 2.735 | 12.010 |
| 93 | ND | ND | ND | ND | ND | 9.390 | $0.0(1)$ | 7.190 | 14.220 | 2.720 | 13.940 |
| 94 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 95 | 2.206 | 2.736 | 5.182 | 8.136 | 11.193 | 7.090 | 0.000 | 1.680 | 10.880 | 2.105 | 6.570 |
| 96 | ND | ND | ND | ND | ND | 10.100 | 0.000 | 5.050 | 14.590 | 2.775 | 11.550 |
| 97 | 1.981 | 3.156 | 6.142 | 9.194 | 12.287 | 4.860 | 0.000 | 4.630 | 8.390 | 1.965 | 9.900 |
| 98 | 0.606 | 1.749 | 5.088 | 8.254 | 11.399 | 8.800 | 0.000 | 4.940 | 13.150 | 2.420 | 11.030 |
| 99 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 100 | 1.796 | 3.178 | 6.373 | 9.478 | 12.594 | 4.160 | 0.000 | 6.780 | 7.250 | 0.545 | 11.170 |
| 101 | 1.458 | 2.763 | 5.947 | 9.059 | 12.180 | 5.940 | 0.000 | 6.230 | 9.140 | 0.825 | 10.710 |
| 102 | 1.358 | 2.683 | 5.898 | 9.020 | 12.146 | 6.010 | 0.060 | 6.420 | 9.200 | 0.705 | 10.960 |
| 103 | 1.121 | 2.397 | 5.630 | 8.763 | 11.894 | 6.930 | 0.000 | 6.420 | 10.270 | 0.740 | 10.890 |
| 104 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 105 | 1.734 | 3.223 | 6.529 | 9.663 | 12.792 | 3.680 | 0.000 | 6.510 | 7.530 | 2.140 | 12.310 |
| 106 | 0.912 | 2.323 | 5.664 | 8.820 | 11.961 | 6.990 | 0.000 | 5.920 | 11.110 | 2.190 | 11.840 |
| 107 | 1.985 | 1.966 | 4.282 | 7.295 | 10.385 | 8.980 | 0.000 | 0.340 | 13.120 | 2.335 | 5.550 |
| 108 | 1.560 | 2.155 | 4.948 | 8.010 | 11.114 | 7.920 | 0.000 | 2.550 | 11.980 | 2.210 | 7.980 |
| 109 | ND | ND | ND | ND | ND | PNA | DNA | DNA | DNA | DNA | DNA |
| 110 | 1.704 | 3.040 | 6.208 | 9.310 | 12.425 | 4.800 | 0.000 | 6.370 | 8.130 | 0.965 | 10.910 |
| 111 | 2.100 | 2.574 | 5.036 | 8.007 | 11.073 | 7.800 | 0.000 | 2.180 | 10.940 | 1.090 | 6.180 |
| 112 | 1.060 | 2.405 | 5.685 | 8.827 | 11.961 | 6.990 | 0.000 | 6.720 | 10.510 | 0.960 | 11.430 |


| RD. |  | Offset Distance |  |  |  |  | Arrival Time |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NO. | HMic1 | HMic2 | HMic3 | HMic4 | HMic5 | LMic1 | LMic2 | LMic3 | LMic4 | LMic5 | LMic6 |
| Consec. | (m) | (m) | (m) | (m) | (m) | (msec) | (msec) | (msec) | (msec) | (msec) | (msec) |
| 113 | 1.254 | 2.058 | 5.066 | 8.169 | 11.289 | 8.360 | 0.000 | 4.620 | 11.770 | 1.100 | 9.290 |
| 114 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 115 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 116 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 117 | 1.245 | 2.835 | 6.294 | 9.469 | 12.617 | 4.840 | 0.000 | 5.030 | 9.820 | 4.225 | 12.440 |
| 118 | 1.648 | 2.800 | 5.841 | 8.920 | 12.026 | 5.295 | 0.000 | 3.025 | 9.930 | 4.030 | 10.080 |
| 119 | 2.652 | 2.993 | 5.093 | 7.949 | 10.966 | 6.465 | 0.000 | -0.160 | 10.990 | 4.125 | 6.280 |
| 120 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 121 | 1.868 | 3.478 | 6.988 | 10.173 | 13.324 | 2.635 | 0.000 | 5.895 | 7.610 | 4.400 | 13.540 |
| 122 | 2.022 | 2.321 | 4.734 | 7.721 | 10.797 | 7.155 | 0.000 | 0.370 | 11.930 | 4.110 | 7.060 |
| 123 | 1.993 | 3.264 | 6.330 | 9.400 | 12.499 | 4.175 | 0.000 | 3.230 | 8.820 | 4.155 | 10.330 |
| 124 | 2.364 | 2.468 | 4.562 | 7.482 | 10.533 | 7.060 | 0.000 | -0.350 | 11.840 | 4.335 | 6.410 |
| 125 | 1.504 | 2.720 | 5.835 | 8.933 | 12.048 | 5.335 | 0.000 | 3.155 | 10.140 | 4.185 | 10.320 |
| 126 | 2.323 | 3.228 | 5.910 | 8.882 | 11.940 | DNA | DNA | DNA | DNA | DNA | DNA |
| 127 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 128 | 1.897 | 3.295 | 6.493 | 9.596 | 12.711 | DNA | DNA | DNA | DNA | DNA | DNA |
| 129 | 2.654 | 2.662 | 4.505 | 7.357 | 10.383 | DNA | DNA | DNA | DNA | DNA | DNA |
| 130 | 2.363 | 3.086 | 5.609 | 8.551 | 11.598 | DNA | DNA | DNA | DNA | DNA | DNA |
| 131 | 1.643 | 3.103 | 6.387 | 9.517 | 12.645 | DNA | DNA | DNA | DNA | DNA | DNA |
| 132 | 1.714 | 2.594 | 5.450 | 8.498 | 11.593 | DNA | DNA | DNA | DNA | DNA | DNA |
| 133 | 2.545 | 2.374 | 4.174 | 7.069 | 10.116 | DNA | DNA | DNA | DNA | DNA | DNA |
| 134 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 135 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 136 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 137 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 138 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 139 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |
| 140 | ND | ND | ND | ND | ND | DNA | DNA | DNA | DNA | DNA | DNA |


|  | $\sum_{i}^{e}$ | $\begin{aligned} & \widehat{O} \\ & 0 \\ & 0 \\ & E \\ & E \end{aligned}$ | $\underset{a}{c}$ | 佼 | 号 | 交 | ¢ | ते | 号 | $\left\|\begin{array}{l} n \\ n \\ n \end{array}\right\|$ | $\frac{1}{3}$ | $\mid \bar{\square}$ | 交 | 佼 | 家 | $\underset{N}{9}$ | $0$ | $\mid$ | － |  | ¢ |  | ¢ | $\stackrel{0}{\square}$ | $\stackrel{\substack{0}}{\substack{0}}$ | 足 | N | $\bar{Z}$ | － |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\sum_{i}^{0}$ | $\begin{array}{\|c\|} \hline 0 \\ 0 \\ E \\ E \end{array}$ | $\bar{z}$ | $\overline{0}$ | $\bar{Z}$ | $\bar{i}$ | $5 \stackrel{0}{9}$ | $0$ | $\dot{B}_{6}^{2}$ | $\begin{aligned} & \substack{\infty \\ \vdots \\ \vdots \\ \hline} \end{aligned}$ | $\frac{4}{2}$ | $\bar{a}$ | $\frac{1}{2}$ | 度 | $\mid \bar{Z}$ | ie | $\stackrel{\boxed{\infty}}{\stackrel{\infty}{\square}}$ | $\begin{aligned} & \underset{\infty}{\infty} \\ & \underset{\sim}{2} \end{aligned}$ | $\frac{\mathrm{N}}{2}$ | $\frac{\stackrel{n}{2}}{2}$ | $\begin{array}{\|c} \underset{\sim}{c} \\ \hline \end{array}$ | $\stackrel{9}{7}$ | $$ | $\begin{array}{\|l\|} \hline \stackrel{y}{4} \\ 0 \end{array}$ | $\stackrel{\leftrightarrow}{2}$ | $\begin{aligned} & \underset{\text { N}}{\text { N }} \end{aligned}$ | $$ | $\bar{Z}$ | ${ }_{0}^{\infty}$ | O20 |
| $\stackrel{\pi}{2 x}$ | $\|\underset{y}{\underset{y}{*}}\|$ | $O$ 0 0 $\vdots$ $\underline{5}$ | $\overline{\mathbf{Z}}$ | $\bar{Z}$ | $\bar{Z}$ | $\bar{Z}$ | $58$ |  |  | $\begin{gathered} \text { c } \\ 0 \\ \end{gathered}$ | $\bar{S}$ | $\frac{\dot{\alpha}}{\bar{\alpha}}$ | $\vec{\alpha}$ | $\stackrel{\Sigma}{\Sigma}$ | $\bar{\alpha}$ | $\hat{C}$ | $0$ | $\begin{aligned} & \stackrel{\rightharpoonup}{\overleftarrow{C}} \\ & \dot{=} \end{aligned}$ | $\frac{2}{9}$ | $\stackrel{n}{0}$ | $\begin{aligned} & \mathrm{O} \\ & \stackrel{0}{6} \end{aligned}$ | $\left.\begin{array}{\|c\|} \hline 6 \\ 0 \\ 0 \end{array} \right\rvert\,$ |  | $\begin{aligned} & \dot{8} \\ & \stackrel{0}{0} \end{aligned}$ | $\begin{aligned} & 0 \\ & \hline 0 \\ & 0 \end{aligned}$ | $\stackrel{\rightharpoonup}{\hat{N}}$ | $0$ | $\bar{Z}$ | $\begin{aligned} & \stackrel{\rightharpoonup}{\mathrm{N}} \end{aligned}$ | $\stackrel{\square}{0}$ |
|  | $\frac{0}{2}$ | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 0 \\ & \underline{e} \\ & \hline \end{aligned}$ | $\mid \underset{Z}{C}$ | $\boldsymbol{Z}$ | $\bar{z}$ | $\bar{\Omega}$ | $\frac{9}{7}$ | $\bar{\square}$ | $\bar{a}$ | $\begin{aligned} & \hline 8 \\ & \hline \end{aligned}$ | $\frac{2}{\square}$ | $\frac{\checkmark}{2}$ | $\frac{\mathbf{\varepsilon}}{\mathbf{Z}}$ | $\vec{\Delta}$ | $\bar{z}$ | $\xrightarrow[i]{\hat{n}}$ | $\begin{aligned} & \stackrel{\rightharpoonup}{\mathrm{O}} \mathrm{C} \end{aligned}$ | $\underset{\sim}{\infty}$ |  | $\left\lvert\, \begin{gathered} \hat{8} \\ \substack{c} \end{gathered}\right.$ | $\begin{aligned} & \mathbf{\infty} \\ & \stackrel{y}{\infty} \\ & \underset{\infty}{2} \end{aligned}$ | $\begin{array}{\|c\|} \hline \frac{n}{\lambda} \\ \underset{m}{m} \end{array}$ | $\begin{aligned} & \mathbf{W} \\ & \stackrel{\rightharpoonup}{2} \\ & \hline \end{aligned}$ | $\begin{array}{\|c\|} \stackrel{\omega}{n} \\ \cdots \end{array}$ | $\begin{aligned} & \underset{\sim}{m} \\ & \underset{\sim}{n} \end{aligned}$ | $\begin{gathered} \stackrel{8}{8} \\ \underset{m}{2} \end{gathered}$ | $\left\|\begin{array}{l} \dot{\delta} \\ \underset{m}{9} \end{array}\right\|$ | $$ | $\begin{aligned} & 0 \\ & \overrightarrow{0} \\ & \mathrm{~m} \end{aligned}$ | \％ |
|  | $\|\underset{j}{\mathrm{~N}}\|$ | $\begin{aligned} & O \\ & 0 \\ & 0 \\ & \underline{O} \\ & E \end{aligned}$ | $\underset{\sim}{\mathbf{a}}$ | 得 | $\stackrel{\Sigma}{2}$ | Z | $5$ | $5$ | $\overline{3}$ | $8$ | $5$ | $\frac{1}{\mathbf{Z}}$ | $\frac{\Sigma}{\bar{Z}}$ | $\bar{i}$ | $\underset{\sim}{Z}$ | Co | $0$ | $0$ | $0$ | $8$ | $8$ | $\begin{array}{\|l\|} \hline \stackrel{C}{0} 0 \\ 0 \end{array}$ | $\begin{aligned} & 8 \\ & \hline 8 \\ & \hline \end{aligned}$ | $\hat{C}_{\mathbf{C}}^{\mathbf{c}}$ | O | $\begin{aligned} & 8 \\ & \hline 0 \\ & 0 \end{aligned}$ | $8$ | $\bar{Z}$ |  | O |
|  | $\sum_{j}^{U}$ | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & E \\ & E \end{aligned}$ | $\underset{\sim}{\alpha}$ | 氐 | 咅 | $\begin{aligned} & \mathbb{8} \\ & \overline{0} \end{aligned}$ | $\begin{gathered} \substack{2 \\ N \\ N} \end{gathered}$ | $1$ | $\frac{s}{s}$ |  | $2$ | $\bar{i}$ | $\underset{\sim}{z}$ | $\underset{\sim}{\alpha}$ | $$ | 俭 | $\stackrel{i n}{n}$ | $\frac{\Gamma}{\infty}$ | $\begin{aligned} & \vec{\infty} \\ & \underset{n}{2} \\ & \hline \end{aligned}$ | R | $$ | $\begin{array}{\|l\|} \hline \stackrel{8}{8} \\ \\ \hline \end{array}$ | $$ | $\stackrel{\rightharpoonup}{N}$ | $\begin{aligned} & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & 9 \\ & N \\ & N \end{aligned}$ | $\begin{aligned} & \mathrm{M} \\ & \\ & \end{aligned}$ | 家 | $\begin{aligned} & \stackrel{\rightharpoonup}{乌} \\ & \stackrel{y}{2} \end{aligned}$ | － |
|  | $\left\|\begin{array}{c} 4 \\ i \\ \sum \end{array}\right\|$ | $\bar{\varepsilon}$ | \％ | 令 | 亿 | 2 | $2$ | 之 | 合 | $\begin{aligned} & \underset{\sim}{\mathbf{~}} \\ & \underset{\sim}{2} \end{aligned}$ | $10$ | $8$ | 亿 | 合 | 吕 | $\stackrel{\substack{n\\ \\}}{ }$ | $\stackrel{\substack{n \\=}}{2}$ | $\stackrel{\stackrel{20}{0}}{\stackrel{0}{8}}$ | － |  | $\stackrel{0}{0}$ | $\stackrel{N}{N}$ | $\begin{aligned} & \stackrel{2}{2} \\ & \underset{7}{2} \end{aligned}$ | $\stackrel{7}{\square}$ | N <br> $\stackrel{\text { N}}{ }$ | $\begin{aligned} & \stackrel{n}{n} \\ & \stackrel{n}{2} \end{aligned}$ | $\left\|\begin{array}{c} 7 \\ 0 \\ \hdashline \\ \hdashline \end{array}\right\|$ | \％ | $\stackrel{\wedge}{a}$ |  |
| 苞 | $\sum_{i}^{\mathbb{U}}$ | $\hat{\underline{g}}$ | \％ | Z | 亿 | 亿 | $\underset{\infty}{9}$ | Z | $2$ |  | $\frac{\square}{z}$ | $10$ | $\frac{Q}{z}$ | $8$ | 吕 | $\begin{gathered} N \\ \infty \\ \infty \end{gathered}$ |  |  | $\left\lvert\, \begin{aligned} & n \\ & 0 \\ & 0 \end{aligned}\right.$ | $\left.\right\|_{\infty} ^{n}$ | $\left.\begin{aligned} & \infty \\ & \infty \\ & \infty \\ & \infty \end{aligned} \right\rvert\,$ | $\left\|\begin{array}{l} \underset{0}{0} \\ 0 \\ \infty \end{array}\right\|$ | $\|\stackrel{\rightharpoonup}{\hat{N}}\|$ | $\left\lvert\, \begin{aligned} & \overline{i n} \\ & \infty \end{aligned}\right.$ | $\left\lvert\,\right.$ | $\underset{\infty}{\underset{7}{9}}$ | $\left\|\begin{array}{l} n \\ n \\ \infty \end{array}\right\|$ | $\|z\|$ | $\left\|\begin{array}{c} 1 \\ \infty \\ \infty \\ \infty \end{array}\right\|$ | $\stackrel{\sim}{9}$ |
|  | $\sum_{i}^{5}$ | $\bar{E}$ | Q | $\stackrel{Q}{z}$ | $\bigcirc$ | \％ | $\frac{\mathrm{N}}{\mathbf{n}}$ | $\square$ | 号 | $\begin{gathered} 78 \\ 0 \\ 0 \end{gathered}$ | $8$ | $\hat{Z}$ | 2 | Q | 吕 | $\left\|\begin{array}{c} \underset{1}{c} \\ \stackrel{y}{2} \end{array}\right\|$ | $\begin{gathered} \underset{\sim}{c} \\ \end{gathered}$ | $\begin{gathered} 9 \\ \underset{1}{2} \end{gathered}$ | $\left\lvert\, \begin{aligned} & \infty \\ & \underset{6}{6} \\ & \text { in } \end{aligned}\right.$ | $\begin{gathered} \mathrm{N} \\ \mathrm{i} \end{gathered}$ | $\left\|\begin{array}{c} 0 \\ \stackrel{0}{0} \\ i \end{array}\right\|$ | $\begin{gathered} 8 \\ 0 \\ 0 \\ i n \end{gathered}$ | $\begin{gathered} \hat{\mathbf{n}} \\ \stackrel{y}{i} \end{gathered}$ | $\left\lvert\, \begin{gathered} \stackrel{\substack{0}}{\substack{1}} \mid \end{gathered}\right.$ | $\begin{aligned} & \infty \\ & 0 \\ & 0 \\ & i \end{aligned}$ | $\begin{gathered} \infty \\ \stackrel{\infty}{n} \\ i \end{gathered}$ |  | $18$ | $\begin{aligned} & \text { A } \\ & \infty \\ & \infty \end{aligned}$ |  |
|  | $\underset{\underline{I}}{\underset{y}{x}}$ | E | $2$ | Q | $\mathrm{Q}$ | Z | $\stackrel{n}{2}$ | $\frac{Q}{z}$ | 亿 | $\begin{aligned} & \infty \\ & \infty \\ & \infty \\ & \infty \end{aligned}$ | $8$ | $\bar{z}$ | 吕 | $\stackrel{Q}{Z}$ | Q | $\begin{aligned} & \infty \\ & \mathbf{B} \\ & \stackrel{y}{\mathrm{C}} \end{aligned}$ | $\stackrel{\substack{\mathbf{C} \\ \stackrel{\rightharpoonup}{N}}}{ }$ | $\begin{aligned} & 8 \\ & \vdots \\ & \dot{N} \end{aligned}$ | $\begin{aligned} & \perp \\ & \infty \\ & \dot{N} \end{aligned}$ | $\underset{\substack{\infty \\ \underset{\sim}{\infty} \\ \hline}}{ }$ | $\left\|\begin{array}{l} \infty \\ 6 \\ \underset{i}{c} \end{array}\right\|$ | $\left\|\begin{array}{l} n \\ \substack{n \\ i} \end{array}\right\|$ | $\left\|\begin{array}{l} \infty \\ \underset{\sim}{0} \\ \underset{\sim}{2} \end{array}\right\|$ | $\left\|\begin{array}{l} \underset{\mathrm{H}}{0} \\ \underset{0}{2} \end{array}\right\|$ | $\begin{aligned} & n \\ & \underset{\sim}{n} \\ & \end{aligned}$ | $\begin{aligned} & \hat{N} \\ & \stackrel{N}{N} \end{aligned}$ | $\stackrel{\underset{C}{N}}{\substack{1 \\ \hline}}$ | $8$ | $\stackrel{\substack{\mathrm{m}}}{ }$ | $\stackrel{\infty}{\sim}$ |
|  | $\sum_{i}^{\sum}$ | $\bar{E}$ | \％ | $\stackrel{\square}{2}$ | $\bigcirc$ | 亿 | む̇ | 2 | 合 | $\left\|\begin{array}{c} \infty \\ \underset{6}{6} \\ \mathrm{~N} \end{array}\right\|$ | $8$ | $\hat{z}$ | 亿 | Z | Z | $\underset{\sim}{\underset{\sim}{2}}$ | $\underset{\sim}{\underset{N}{N}}$ | $\underset{\rightarrow}{\circ}$ | $2$ |  | $\begin{aligned} & \mathrm{O} \\ & \stackrel{1}{2} \end{aligned}$ | $\stackrel{0}{2}$ | $\stackrel{\substack{2 \\ \\ \hline}}{ }$ | $\left\lvert\, \begin{aligned} & 8 \\ & \hline 8 \\ & \hline 1 \end{aligned}\right.$ | $\stackrel{\rightharpoonup}{\underset{\sim}{2}}$ | $\stackrel{\underset{\sim}{\infty}}{\stackrel{8}{0}}$ | $\stackrel{\sim}{N}$ | $2$ |  | $\stackrel{\sim}{0}$ |
| $\stackrel{8}{*}$ | $\begin{aligned} & 0 \\ & 2 \end{aligned}$ | $\dot{0}$ 0 0 0 0 | 7 | $\underset{\sim}{7}$ | \％ | む | \％ | 9 | 今 | \％ |  |  | 5 |  | $\mathfrak{n}$ | \＃ | $\stackrel{10}{2}$ | $\stackrel{\circ}{\circ}$ | $\stackrel{n}{2}$ | $\vdots$ | 20 | \％ | $\square$ | O－ | 8 | す | $\stackrel{8}{8}$ | \％ | ف0 | $\stackrel{0}{6}$ |


| RD. |  | Offset Distance |  |  |  |  | Arrival Time |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NO. | HMic1 | HMic2 | HMic3 | HMic4 | HMic5 | LMic1 | LMic2 | LMic3 | LMic4 | LMic5 | LMic6 |
| Consec. | (m) | (m) | (m) | (m) | (m) | (msec) | (msec) | (msec) | (msec) | (msec) | (msec) |
| 169 | 1.982 | 2.823 | 5.576 | 8.593 | 11.665 | 7.220 | 0.000 | 3.070 | 10.200 | 0.910 | 7.480 |
| 170 | 1.650 | 2.581 | 5.498 | 8.563 | 11.658 | 7.580 | 0.000 | 3.830 | 10.570 | 0.755 | 8.310 |
| 171 | 1:430 | 2.664 | 5.816 | 8.928 | 12.043 | 6.925 | 0.000 | 5.575 | 10.010 | 0.790 | 7.700 |
| 172 | 1.864 | 2.067 | 4.555 | 7.583 | 10.669 | 9.580 | 0.000 | 0.910 | 12.700 | 0.830 | 5.220 |
| 173 | 1.736 | 2.318 | 5.029 | 8.070 | 11.157 | 8.740 | 0.000 | 2.080 | 11.770 | 0.810 | 6.460 |
| 174 | 1.873 | 2.841 | 5.712 | 8.755 | 11.838 | 6.870 | 0.000 | 3.810 | 9.820 | 0.860 | 8.290 |
| 175 | 1.424 | 1.989 | 4.858 | 7.946 | 11.055 | DNA | DNA | DNA | DNA | DNA | DNA |
| 176 | 2.369 | 2.527 | 4.665 | 7.590 | 10.632 | DNA | DNA | DNA | DNA | DNA | DNA |
| 177 | 2.707 | 3.159 | 5.343 | 8.205 | 11.210 | DNA | DNA | DNA | DNA | DNA | DNA |
| 178 | 2.606 | 3.013 | 5.204 | 8.083 | 11.097 | DNA | DNA | DNA | DNA | DNA | DNA |
| 179 | 1.649 | 2.493 | 5.365 | 8.425 | 11.519 | DNA | DNA | DNA | DNA | DNA | DNA |
| 180 | 2.130 | 2.841 | 5.455 | 8.440 | 11.499 | DNA | DNA | DNA | DNA | DNA | DNA |
| 181 | 2.747 | 3.622 | 6.181 | 9.100 | 12.121 | DNA | DNA | DNA | DNA | DNA | DNA |
| 182 | 1.847 | 2.208 | 4.766 | 7.790 | 10.873 | DNA | DNA | DNA | DNA | DNA | DNA |
| 183 | 4.180 | 4.969 | 8.147 | 11.175 | 14.234 | DNA | DNA | DNA | DNA | DNA | DNA |
| 184 | 1.955 | 3.009 | 5.920 | 8.963 | 12.046 | DNA | DNA | DNA | DNA | DNA | DNA |
| 185 | 2.222 | 3.632 | 6.819 | 9.915 | 13.019 | 3.670 | 0.000 | 5.860 | 6.880 | 1.685 | 11.210 |
| 186 | 1.618 | 2.742 | 5.784 | 8.869 | 11.972 | 7.015 | 0.000 | 4.120 | 10.470 | 1.530 | 9.300 |
| 187 | 2.173 | 3.328 | 6.273 | 9.312 | 12.390 | 5.390 | 0.000 | 4.205 | 8.600 | 1.580 | 9.200 |
| 188 | 2.117 | 3.437 | 6.544 | 9.623 | 12.719 | 4.595 | 0.000 | 5.195 | 7.850 | 1.645 | 10.540 |
| 189 | 1.878 | 2.480 | 5.132 | 8.151 | 11.229 | 8.295 | 0.000 | 1.655 | 11.740 | 1.555 | 6.520 |
| 190 | 1.715 | 2.862 | 5.896 | 8.975 | 12.074 | 6.535 | 0.000 | 4.475 | 10.020 | 1.615 | 9.630 |
| 191 | 2.065 | 3.239 | 6.221 | 9.273 | 12.358 | 4.485 | 0.000 | 4.490 | 8.740 | 1.620 | 9.680 |
| 192 | 1.986 | 3.287 | 6.394 | 9.477 | 12.576 | 5.145 | 0.000 | 5.160 | 8.440 | 1.655 | 10.45 |

APPENDIX D:
DATA COLLECTION TEST RANGE DATA

Intentionally left blank.


| RD. | GUN | RD. | DATE | TIME | MET CONDITIONS |  |  |  | TERMINAL | IMPACT LOCATION |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| \# | TYPE | TYPE |  |  | TEMP | REL. HUM. | WINDS |  | MACH NO. | Y | Z |
|  | (mm) |  |  | H:M:S | (C) | \% | WD(deg) | WS(m/s) |  | (m) | (m) |
| 29 | - | " | 4/5/93 | 14:12:19 | 6.6 | 64 | 53. | 4.4 | 2.0 | -0.2137 | 3.389 |
| 30 | " | " | 4/5/93 | 14:23:24 | 6.6 | 64 | 65. | 4.6 | 2.0 | 0.5578 | 4.107 |
| 31 | " | " | 4/5/93 | 14:25:25 | 6.8 | 64 | 58. | 4.3 | 2.1 | 0.2793 | 4.173 |
| 32 | " | M33 | 4/5/93 | 14:27:25 | 6.8 | 64 | 63. | 3.7 | ND | ND | ND |
| 33 | " | ${ }^{\prime}$ | 4/5/93 | 14:32:32 | 6.8 | 64 | 65. | 3.6 | 1.7 | ND | ND |
| 34 | " | " | 4/5/93 | 14:36:39 | 7.0 | 65 | 53. | 4.0 | 1.8 | ND | ND |
| 35 | " | " | 4/5/93 | 14:42:57 | 6.8 | 63 | 58. | 3.4 | 1.8 | ND | ND |
| 36 | " | " | 4/5/93 | 14:56:49 | 7.1 | 64 | 49. | 4.3 | 2.0 | 0.3273 | 3.070 |
| 37 | " | " | 4/5/93 | 14:58:45 | 7.1 | 63 | 56. | 3.9 | 1.7 | ND | ND |
| 38 | " | " | 4/5/93 | 15:02:38 | 7.0 | 64 | 57. | 4.5 | 1.8 | ND | ND |
| 39 | " | " | 4/5/93 | 15:05:30 | 7.1 | 63 | 80. | 4.0 | 2.0 | -0.0799 | 4.581 |
| 40 | " | " | 4/5/93 | 15:09:13 | 7.2 | 64 | 71. | 4.4 | 1.9 | 0.0749 | 4.325 |
| 41 | " | " | 4/5/93 | 15:10:51 | 7.3 | 64 | 63. | 4.7 | 1.7 | ND | ND |
| 42 | " | " | 4/5/93 | 15:13:52 | 7.3 | 63 | 52. | 4.4 | 1.7 | ND | ND |
| 43 | " | " | 4/5/93 | 15:16:16 | 7.3 | 64 | 62. | 4.5 | 1.9 | -1.5507 | 3.863 |
| 44 | " | " | 4/5/93 | 15:18:38 | 7.3 | 64 | 61. | 5.6 | 2.0 | 0.263 | 4.375 |
| 45 | 7.62 | M62 | 4/6/93 | 10:03:06 | 6.0 | 58 | 57. | 7.3 | 1.4 | 0.3988 | 4.730 |
| 46 | Mann | M59 | 4/6/93 | 10:16:50 | 6.4 | 57 | 63. | 8.3 | 1.3 | 0.1527 | 4.151 |
| 47 | " | " | 4/6/93 | 10:18:51 | 6.5 | 56 | 62. | 8.9 | 1.3 | -0.2308 | 4.558 |
| 48 | " | M62 | 4/6/93 | 10:20:43 | 6.8 | 56 | 69. | 7.4 | 1.4 | -0.2004 | 4.598 |
| 49 | " | " | 4/6/93 | 10:22:49 | 6.8 | 56 | 59. | 7.7 | 1.3 | 0.0002 | 4.410 |
| 50 | " | M59 | 4/6/93 | 10:25:10 | 7.1 | 56 | 54. | 9.0 | 1.3 | -0.5658 | 4.487 |
| 51 | " | M62 | 4/6/93 | 10:26:54 | 7.3 | 56 | 59. | 9.6 | 1.4 | -0.5264 | 4.361 |
| 52 | 12.7 | M17 | 4/6/93 | 13:33:45 | 10.7 | 47 | 60. | 7.2 | 1.4 | ND | ND |
| 53 | Mann | " | 4/6/93 | 13:42:06 | 10.4 | 46 | 59. | 8.0 | 1.4 | 0.5712 | 4.696 |
| 54 | " | M33 | 4/6/93 | 13:44:17 | 10.5 | 45 | 65. | 8.1 | 1.3 | 0.0318 | 3.439 |
| 55 | " | " | 4/6/93 | 13:46:45 | 10.8 | 47 | 71. | 8.1 | 1.3 | -0.186 | 3.188 |
| 56 | " | " | 4/6/93 | 14:05:38 | 10.6 | 46 | 69. | 7.9 | 1.3 | 0.7876 | 4.176 |


| RD. | GUN | RD. | DATE | TIME | MET CONDITIONS |  |  |  | $\begin{aligned} & \text { TERMINAL } \\ & \text { MACH NO. } \end{aligned}$ | IMPACT LOCATION |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| \# | TYPE | TYPE |  |  | TEMP | REL. HUM. | WINDS |  |  | Y | Z |
|  | (mm) |  |  | H:M:S | (C) | \% | WD(deg) | WS (m/s) |  | (m) | (m) |
| 57 | " | " | 4/6/93 | 14:08:12 | 10.7 | 45 | 80. | 9.0 | 1.3 | 1.0217 | 3.785 |
| 58 | " | M17 | 4/6/93 | 14:11:57 | 10.6 | 44 | 64. | 8.4 | 1.5 | -1.3249 | 4.693 |
| 59 | " | " | 4/6/93 | 14:15:12 | 10.6 | 44 | 64. | 9.9 | 1.5 | 1.0534 | 4.913 |
| 60 | " | " | 4/6/93 | 14:18:33 | 10.7 | 45 | 68. | 8.3 | 1.5 | 0.5658 | 5.133 |
| 61 | " | M33 | 4/6/93 | 14:21:08 | 10.9 | 44 | 50. | 8.6 | 1.3 | ND | ND |
| 62 | 7.62 | M62 | 4/6/93 | 15:08:53 | 10.8 | 42 | 73. | 8.4 | 1.7 | 0.3539 | 4.294 |
| 63 | Mann | " | 4/6/93 | 15:19:33 | 11.1 | 43 | 66. | 8.5 | 1.7 | -0.062 | 4.112 |
| 64 | " | M59 | 4/6/93 | 15:21:20 | 10.8 | 42 | 67. | 8.6 | 1.7 | -0.1317 | 4.238 |
| 65 | " | M62 | 4/6/93 | 15:22:19 | 10.8 | 42 | 68. | 8.8 | 1.7 | 0.3402 | 3.973 |
| 66 | " | M59 | 4/6/93 | 15:23:28 | 10.8 | 42 | 70. | 8.1 | 1.6 | -0.1763 | 4.139 |
| 67 | " | " | 4/6/93 | 15:24:09 | 10.9 | 42 | 62. | 7.6 | 1.7 | -0.3942 | 4.123 |
| 68 | " | M62 | 4/6/93 | 15:25:47 | 10.8 | 43 | 64. | 8.3 | 1.7 | -0.3049 | 4.280 |
| 69 | 35 | DM18 | 4/7/93 | 10:48:00 | 9.9 | 47 | 352. | 4.8 | ND | ND | ND |
| 70 | TIPGID | " | 4/7/93 | 10:53:43 | 10.1 | 46 | 0. | 4.5 | S | PII) | ND |
| 71 | " | " | 4/7/93 | 10:55:50 | 10.1 | 46 | 359. | 4.5 | 2.5 | ND | ND |
| 72 | " | " | 4/7/93 | 10:58:43 | 10.1 | 46 | 2. | 3.3 | 2.5 | ND | ND |
| 73 | " | TPL-T | 4/7/93 | 10:02:19 | 10.1 | 46 | 359. | 4.5 | 3.1 | ND | ND |
| 74 | " | ${ }^{\prime}$ | 4/7/93 | 11:04:40 | 10.3 | 46 | 1. | 5.1 | 3.1 | ND | ND |
| 75 | " | DM18 | 4/7/93 | 11:09:53 | 10.5 | 46 | 346. | 5.2 | 2.4 | 0.6263 | 3.896 |
| 76 | " | TPL-T | 4/7/93 | 11:34:07 | 11.5 | 47 | 349. | 3.9 | 3.1 | 0.1648 | 4.089 |
| 77 | " | DM18 | 4/7/93 | 11:36:22 | 11.6 | 47 | 349. | 4.5 | 2.5 | 0.7707 | 4.567 |
| 78 | " | TPL-T | 4/7/93 | 11:37:56 | 11.7 | 49 | 352. | 3.6 | 3.1 | 0.0248 | 3.613 |
| 79 | " | DM18 | 4/7/93 | 11:42:38 | 12.1 | 48 | 4. | 4.4 | 2.5 | 1.0961 | 3.860 |
| 80 | " | TPL-T | 4/7/93 | 11:43:00 | 12.0 | 48 | 355. | 3.9 | 3.1 | 0.3734 | 3.505 |
| 81 | 35 | TPL-T | 4/7/93 | 13:57:30 | 13.4 | 51 | 115. | 1.6 | 3.8 | ND | ND |
| 82 | TIPGID | " | 4/7/93 | 14:01:54 | 13.3 | 51 | 102. | 1.9 | 3.8 | -0.0546 | 4.267 |
| 83 | " | " | 4/7/93 | 14:15:53 | 13.1 | 48 | 113. | 2.4 | 3.8 | 0.0085 | 4.008 |
| 84 | " | DM18 | 4/7/93 | 14:17:13 | 13.2 | 49 | 122. | 2.3 | 2.9 | -0.2 | 4.742 |


| RD. | GUN | RD. | DATE | TIME | MET CONDITIONS |  |  |  | TERMINAL | IMPACT LOCATION |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| \# | TYPE | TYPE |  |  | TEMP | REL. HUM. | WINDS |  | MACH NO. | Y | Z |
|  | (mm) |  |  | H:M:S | (C) | \% | WD(deg) | WS(m/s) |  | (m) | (m) |
| 85 | " | " | 4/7/93 | 14:19:58 | 13.5 | 49 | 128. | 1.8 | 2.9 | -0.0491 | 4.268 |
| 86 | " | " | 4/7/93 | 14:21:10 | 13.4 | 49 | 122. | 1.5 | 2.9 | -0.5449 | 4.430 |
| 87 | " | TPL-T | 4/7/93 | 14:22:38 | 13.3 | 49 | 123. | 2.1 | 3.9 | 0.0302 | 4.112 |
| 88 | 35 | TPL-T | 4/7/93 | 15:07:32 | 14.1 | 48 | 104. | 2.9 | 2.4 | ND | ND |
| 89 | TIPGID | DM18 | 4/7/93 | 15:10:06 | 14.0 | 48 | 111. | 3.5 | 2.1 | ND | ND |
| 90 | " | TPL-T | 4/7/93 | 15:12:40 | 14.2 | 48 | 112. | 3.6 | 2.4 | 0.3719 | 3.673 |
| 91 | " | DM18 | 4/7/93 | 15:24:49 | 13.6 | 49 | 127. | 1.9 | 2.0 | -1.1667 | 4.013 |
| 92 | " | TPL-T | 4/7/93 | 15:26:02 | 13.9 | 49 | 120. | 1.9 | 2.4 | -0.2488 | 5.227 |
| 93 | " | DM18 | 4/7/93 | 15:27:42 | 13.7 | 50 | 121. | 2.4 | 2.0 | -1.0879 | 4.114 |
| 94 | " | TPL-T | 4/7/93 | 15:29:05 | 13.4 | 49 | 115. | 2.2 | 2.4 | 0.0701 | 4.556 |
| 95 | " | DM18 | 4/7/93 | 15:30:33 | 13.4 | 49 | 115. | 2.0 | 2.1 | -0.1515 | 4.288 |
| 96 | 12.7 | M17 | 4/8/93 | 11:06:46 | 10.4 | 28 | 82. | 3.3 | 2.0 | -0.2146 | 4.602 |
| 97 | Mann | M33 | 4/8/93 | 11:08:37 | 10.4 | 29 | 75. | 3.6 | 2.1 | 0.3322 | 4.554 |
| 98 | ," | " | 4/8/93 | 11:13:47 | 10.8 | 29 | 74. | 3.1 | 2.0 | 0.0656 | 4.316 |
| 99 | " | " | 4/8/93 | 11:16:58 | 10.9 | 33 | 77. | 2.8 | 2.0 | 0.1268 | 4.631 |
| 100 | " | " | 4/8/93 | 11:19:08 | 10.8 | 34 | 72. | 2.9 | 2.1 | 0.1647 | 4.261 |
| 101 | " | " | 4/8/93 | 11:19:54 | 10.9 | 34 | 76. | 2.7 | 2.1 | 0.1647 | 4.211 |
| 102 | " | " | 4/8/93 | 11:20:55 | 11.0 | 35 | 79. | 2.4 | 2.0 | 0.3106 | 4.180 |
| 103 | " | " | 4/8/93 | 11:24:19 | 10.9 | 37 | 76. | 2.3 | 2.1 | -1.2304 | 4.346 |
| 104 | " | " | 4/8/93 | 11:26:01 | 11.0 | 37 | 75. | 2.1 | 2.1 | -1.2948 | 4.340 |
| 105 | " | " | 4/8/93 | 11:27:38 | 11.1 | 38 | 78. | 1.9 | 2.1 | -1.3645 | 4.395 |
| 106 | " | " | 4/8/93 | 11:30:25 | 11.3 | 39 | 83. | 2.0 | 2.1 | -1.4346 | 3.167 |
| 107 | " | " | 4/8/93 | 11:33:26 | 11.6 | 38 | 99. | 1.7 | 2.1 | -1.3139 | 3.541 |
| 108 | " | " | 4/8/93 | 11:34:18 | 11.6 | 38 | 99. | 1.7 | 2.1 | -1.3424 | 3.510 |
| 109 | " | " | 4/8/93 | 11:36:45 | 11.5 | 38 | 87. | 1.9 | 2.1 | 0.9299 | 4.498 |
| 110 | " | " | 4/8/93 | 11:38:42 | 11.5 | 37 | 95. | 1.7 | 2.1 | 1.1778 | 4.753 |
| 111 | " | " | 4/8/93 | 11:39:36 | 11.5 | 37 | 92. | 1.7 | 2.1 | 1.1793 | 4.673 |
| 112 | " | " | 4/8/93 | 11:41:45 | 11.6 | 37 | 99. | 1.6 | 2.1 | 1.2093 | 3.748 |


| RD. | GUN | RD. | DATE | TIME | MET CONDITIONS |  |  |  | TERMINAL | IMPACT LOCATION |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| \# | TYPE | TYPE |  |  | TEMP | REL. HUM. | WINDS |  | MACHNO. | Y | Z |
|  | (mm) |  |  | H:M:S | (C) | \% | WD(deg) | WS (m/s) |  | (m) | (m) |
| 113 | " | " | 4/8/93 | 11:43:02 | 11.6 | 37 | 102. | 1.3 | 2.1 | 1.188 | 3.529 |
| 114 | " | " | 4/8/93 | 11:44:13 | 11.5 | 28 | 88. | 2.1 | 2.1 | 0.9888 | 3.512 |
| 115 | " | " | 4/8/93 | 11:46:51 | 11.6 | 37 | 103. | 1.8 | 2.0 | 1.195 | 3.630 |
| 116 | " | " | 4/8/93 | 11:48:22 | 11.7 | 38 | 121. | 1.2 | 2.1 | 1.1598 | 3.727 |
| 117 | " | " | 4/8/93 | 11:49:46 | 11.8 | 38 | 121. | 1.2 | 2.1 | 1.139 | 3.339 |
| 118 | " | M17 | 4/8/93 | 11:50:50 | 11.8 | 38 | 102. | 1.0 | 2.1 | 0.4572 | 3.711 |
| 119 | 12.7 | M33 | 4/8/93 | 14:03:46 | 15.1 | 35 | 94. | 2.2 | 2.1 | 0.0334 | 4.152 |
| 120 | Mann | M17 | 4/8/93 | 14:15:09 | 15.0 | 33 | 78. | 1.4 | 2.1 | -0.1314 | 4.214 |
| 121 | " | " | 4/8/93 | 14:16:52 | 15.1 | 33 | 92. | 1.6 | 2.1 | -0.2068 | 3.736 |
| 122 | ${ }^{\prime}$ | " | 4/8/93 | 14:18:13 | 15.1 | 32 | 92. | 2.2 | 2.1 | -0.4208 | 4.292 |
| 123 | " | M33 | 4/8/93 | 14:19:23 | 15.3 | 32 | 90. | 2.3 | 2.1 | 0.1546 | 3.897 |
| 124 | " | " | 4/8/93 | 14:21:14 | 15.4 | 31 | 96. | 2.2 | 2.1 | -0.135 | 3.693 |
| 125 | 35 | DM18 | 4/8/93 | 15:05:20 | 16.7 | 31 | 86. | 4.0 | 2.8 | 0.0246 | 4.372 |
| 126 | TIPGID | DM68 | 4/8/93 | 15:16:03 | 16.3 | 34 | 87. | 3.8 | 3.0 | -0.1415 | 4.607 |
| 127 | " | $\cdots$ | 4/8/93 | 15:17:27 | 16.3 | 34 | 87. | 3.8 | 3.0 | -0.1808 | 4.429 |
| 128 | " | " | 4/8/93 | 15:18:19 | 16.3 | 33 | 85. | 3.8 | 2.9 | -0.1237 | 4.322 |
| 129 | " | DM18 | 4/8/93 | 15:19:14 | 16.3 | 33 | 87. | 3.5 | 2.9 | -0.0951 | 4.226 |
| 130 | 35 | DM68 | 4/9/92 | 9:19:37 | 8.6 | 100 | 71. | 4.1 | 2.0 | -0.4724 | 4.873 |
| 131 | TIPGID | DM18 | 4/9/92 | 9:34:49 | 8.8 | 100 | 78. | 3.6 | 2.0 | 0.1653 | 4.754 |
| 132 | " | DM68 | 4/9/92 | 9:37:54 | 8.7 | 100 | 82. | 3.5 | 2.0 | 0.0732 | 4.653 |
| 133 | " | " | 4/9/92 | 9:40:02 | 8.8 | 100 | 82. | 3.1 | 2.0 | 0.2015 | 4.996 |
| 134 | " | DM18 | 4/9/92 | 9:42:33 | 8.8 | 100 | 78. | 3.6 | 2.0 | -0.9863 | 3.644 |
| 135 | " | " | 4/9/92 | 9:46:11 | 8.9 | 100 | 78. | 3.5 | 2.0 | 0.2626 | 4.081 |
| 136 | 35 | DM68 | 4/9/92 | 10:16:39 | 9.1 | 100 | 92. | 1.7 | 2.5 | 0.2093 | 4.224 |
| 137 | TIPGID | " | 4/9/92 | 10:31:41 | 9.5 | 100 | 75. | 1.0 | 2.5 | -0.401 | 4.220 |
| 138 | " | DM18 | 4/9/92 | 10:33:21 | 9.6 | 100 | 76. | 0.7 | 2.5 | 0.162 | 3.698 |
| 139 | " | " | 4/9/92 | 10:35:01 | 9.4 | 100 | 57. | 0.7 | 2.5 | 0.412 | 3.565 |
| 140 | " | DM68 | 4/9/92 | 10:37:15 | 9.4 | 100 | 61. | 0.7 | 2.5 | -0.5789 | 4.083 |

INTENTIONALLY LEFT BLANK.

APPENDIX E:
PROJECTILE CHARACTERISTICS DATA FROM COLLECTION TEST PHASE

INTENTIONALLY LEFT BLANK.

| Shot | Round | Ch! | Pos P1 | Neg P11 | Neg P2 | A1 | A2 | A3 | ATot | Peak | ABS | Cal |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Type |  | Pa | Pa | Pa | msec | msec | msec | msec | mPasec | mPa-soc | Pa/Volt |
| 20 | M62 | 1 |  |  |  | 112 | 216 |  | 256 |  |  |  |
|  |  | 21 |  |  |  | 128 | 232 |  | 268 |  |  |  |
|  |  | 31 |  |  |  | 156 | 288 |  | 320 |  |  |  |
|  |  | 41 |  |  |  | -180 |  |  | 340 |  |  |  |
|  |  | 81 |  |  |  | 204 |  |  | 380 |  |  |  |
|  |  |  |  | 1 |  |  |  |  |  |  |  |  |
| 21 | M59 | 1 |  | ! |  | 272 |  |  | 524 |  |  |  |
|  |  | 2 |  |  |  | 268 |  |  | 516 |  |  |  |
|  |  | 31 |  |  |  | 2641 |  |  | 524 |  |  |  |
|  |  | 4 |  |  |  | 260 |  |  | 524 |  |  |  |
|  |  | 8 |  |  |  | 248 |  |  | 516 |  |  |  |
|  |  | 1 |  |  |  |  |  |  |  |  |  |  |
| 22 | M62 | 1 |  |  |  | 116 | 208 |  | 260 |  |  |  |
|  |  | 2 |  |  |  | 128 |  |  | 304 |  |  |  |
|  |  | 3 |  |  |  | 168 |  |  | 324 |  |  |  |
|  |  | 4 |  |  |  | 184 |  |  | 360 |  |  |  |
|  |  | 81 |  |  |  | 212 |  |  | 380 |  |  |  |
|  |  |  |  | ! |  |  |  |  |  |  |  |  |
| 23 | M59 | 11 |  |  |  | 320 |  |  | 604 |  |  |  |
|  |  | 2 |  |  |  | 308 |  |  | 592 |  |  |  |
|  |  | 31 |  |  |  | 292 |  |  | 568 |  |  |  |
|  |  | 4. |  |  |  | 276 |  |  | 572 |  |  |  |
|  |  | 8 |  | ! |  | 308 |  |  | 556 |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 25 | M62 | 1 |  |  |  | 104 |  |  | 196 |  |  |  |
|  |  | 2 |  |  |  | 116 |  |  | 240 |  |  |  |
|  |  | 31 |  |  |  | 156 |  |  | 308 |  |  |  |
|  |  | 4 |  | + |  | 184 |  |  | 336 |  |  |  |
|  |  | 81 |  | ! |  | 212 |  |  | 380 |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 26 | M59 | 1 |  |  |  | 260 |  |  | 516 |  |  |  |
|  |  | 2 |  |  |  | 268 |  |  | 508 |  |  |  |
|  |  | 3 |  |  |  | 248 |  |  | 524 |  |  |  |
|  |  | 4 |  |  |  | 272 |  |  | 520 |  |  |  |
|  |  | 8 |  |  |  | 300 |  |  | 548 |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 28 | M17 | 1 |  |  |  | 112 | 192 | 220 | 272 |  |  |  |
|  |  | 2 |  |  |  | 116 | 196 | 224 | 272 |  |  |  |
|  |  | 3 |  |  |  | 152 | 252 |  | 324 |  |  |  |
|  |  | 4 |  |  |  |  |  |  |  |  |  |  |
|  |  | 8 |  |  |  | 212 | 336 |  | 412 |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 29 | M17 | 1 |  |  |  | 92 | 156 | 188 | 228 |  |  |  |
|  |  | 2 |  |  |  | 104 | 164 |  | 244 |  |  |  |
|  |  | 3 |  |  |  | 148 | 252 |  | 320 |  |  |  |
|  |  | 4 |  |  |  | 184 | 288 |  | 364 |  |  |  |
|  |  | 8 |  |  |  | 208 |  |  | 396 |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 30 | M17 | 1 |  |  |  | 104 | 172 | 200 | 256 |  |  |  |
|  |  | 2 |  |  |  | 124 | 2001 |  | 284 |  |  |  |
|  |  | 3 |  |  |  | 160 | 260 |  | 340 |  |  |  |
|  |  | 4 |  |  |  | 176 | 296 |  | 376 |  |  |  |
|  |  | 8 |  |  |  | 200 |  |  | 408 |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 3 i | M17 | 1 |  |  |  | 96 | 168 | 192 | 248 |  |  |  |
|  |  | 2 |  |  |  | 120 | 200 |  | 276 |  |  |  |
|  |  | 3 |  |  |  | 152 | 268 |  | 336 |  |  |  |
|  |  | 4 |  |  |  | 180 | 300 |  | 368 |  |  |  |
|  |  | 8 |  |  |  | 216 |  |  | 408 |  |  |  |
|  | + |  |  |  |  |  |  |  |  |  |  |  |


| Shot | Round I | Chl | Pos P | Neg P1 | Neg P2 | A1 | A2 | A3 | ATot | Peak | ABS | Cal |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Type\| |  | Pa | Pa | Pa | msec | msec | msec | msec | mPa-sec | mPa -sec | $\mathrm{Pa} / \mathrm{Volt}$ |
| 36 | M33 | 1 |  |  |  | 521 | 116 |  | 180 |  |  |  |
|  |  | 2 |  |  |  | 116 | 196 |  | 256 |  |  |  |
|  |  | 31 |  |  |  | 164 |  |  | 336 |  |  |  |
|  |  | 4 |  |  |  | 184 |  |  | 364 |  |  |  |
|  |  | 8 |  |  |  | 216 |  |  | 388 |  |  |  |
|  |  | I |  |  |  |  |  |  |  |  |  |  |
| 38 | M33 | 1 |  |  |  | 132 | 252 |  | 288 |  |  |  |
|  |  | 2 |  |  |  |  |  |  |  |  |  |  |
|  | + | 31 |  |  |  |  |  |  |  |  |  |  |
|  | i | $4!$ |  |  |  | 172 |  |  | 332 |  |  |  |
|  |  | 81 |  |  |  | 204 |  |  | 372 |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 39 | M33 | 11 |  |  |  | 108 | 188 | 216 | 256 |  |  |  |
|  |  | 2 |  |  |  | 116 | 204 |  | 268 |  |  |  |
|  |  | 3 |  |  |  | 152 | 272 |  | 332 |  |  |  |
|  |  | 41 |  |  |  | 184 |  |  | 364 |  |  |  |
|  |  | 8 |  |  |  | 208 |  |  | 400 |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 40 | M331 | 1 |  |  |  | 108 | 180 |  | 256 |  |  |  |
|  |  | 2 |  |  |  | 116 | 196 |  | 264 |  |  |  |
|  |  | 31 |  |  |  | 152 | 264 |  | 316 |  |  |  |
|  |  | 4 |  |  |  | 172 |  |  | 3601 |  |  |  |
|  |  | 8 |  |  |  | 220 |  |  | 396 |  |  |  |
|  | i |  |  |  |  |  |  |  |  |  |  |  |
| 43 | M331 | $1!$ |  |  |  | 124 |  |  | 272 |  |  |  |
|  |  | 21 |  |  |  |  |  |  |  |  |  |  |
|  |  | 3 |  |  |  | 144 |  |  | 296 |  |  |  |
|  |  | 4 |  |  |  | 168 |  |  | 348 |  |  |  |
|  |  | 8 |  |  |  | 212 |  |  | 392 |  |  |  |
|  |  | ! |  |  |  |  |  |  |  |  |  |  |
| 44 | M33 | 11 |  |  |  | 100 |  |  | 248 |  |  |  |
|  | - | 21 |  |  |  | 120 |  |  | 272 |  |  |  |
|  |  | 31 |  |  |  | 164 |  |  | 320 |  |  |  |
|  |  | 4 |  |  |  | 176 |  |  | 360 |  |  |  |
|  | , | 81 |  |  |  | 204 |  |  | 388 |  |  |  |
|  | I | + |  |  |  |  |  |  |  |  |  |  |
| 45 | M621 | 1 | 868.74 | -466.28 | -578 | 96 | 164 |  | 212 | 34.58 | 77.14 | 693.88 |
|  |  | 2 | 554.2 | -365.29 | -476.75 | 112 | 176 |  | 228 | 30.69 | 65.93 | 557.27 |
|  |  | 3 | 259.07 | -224.41 | -224.41 | 124 | 228 |  | 264 | 18.64 | 39.29 | 357.35 |
|  |  | 4 | 127.99 | 127.99 | -141.64 |  | 148 |  | 276 | 13.99 | 27.46 | 324.86 |
|  |  | 8 | 85.56 | 85.56 | -110.81 |  | 164 |  | 304 | 9.82 | 20.13 | 107.47 |
|  |  | \| |  |  |  |  |  |  |  |  |  |  |
| 46 | M59 | $1)$ | 1102.56 | -738.91 | -857.62 | 92 | 168 |  | 200 | 45.76 | 101.51 | 693.88 |
|  |  | 2 | 677.63 | -503.25 | -571.2 | 108 | 188 |  | 216 | 34.74 | 73.73 | 557.27 |
|  |  | 3. | 218.34 |  | -248.35 | 140 |  |  | 252 | 17.48 | 35.34 | 357.35 |
|  |  | 41 | 191.46 |  | -174.56 | 156 |  |  | 288 | 15.74 | 29.71 | 324.86 |
|  |  | 81 | 85.42 |  | -91.57 | 204 |  |  | 308 | 11.59 | 21.47 | 107.47 |
|  |  | + |  |  |  |  |  |  |  |  |  |  |
| 47 | M591 | 1 | 879.14 |  | -643.92 | 96 | 176 |  | 200 | 36.37 | 79.88 | 693.88 |
|  |  | 2 | 749.25 \| |  | -575.94 | 100 |  |  | 200 | 30.67 | 68.07 | 557.27 |
|  |  | 31 | 197.26 |  | -244.78 | 148 |  |  | 240 | 19.13 | 38.12 | 357.35 |
|  |  | 41 | 209.21 |  | -230 | 148 |  |  | 292 | 18.19 | 37.68 | 324.86 |
|  |  | 8 | 125.42 |  | -145.95 | 160 |  |  | 308 | 13.14 | 26.66 | 107.47 |
|  |  | - |  |  |  |  |  |  |  |  |  |  |
| 48 | M621 | 11 | 867.35 | -469.8 | -573.14 | 92 | 150 |  | 204 | 34.71 | 76.42 | 693.88 |
|  |  | 21 | 647.55 | -373.93 | -429.65 | 100 | 160 |  | 208 | 29.99 | 59.71 | 557.27 |
|  | + | $3!$ | 275.16 | -257.29 | -286.95 | 136 | 212 |  | 264 | 22.18 | 46.4 | 357.35 |
|  |  | 41 | 183.22 |  | -175.43 | 152 |  |  | 292 | 16.63 | 31.48 | 324.86 |
|  |  | 81 | 114.35 |  | -129.61 | 164 |  |  | 300 | 11.78 | 22.25 | 107.47 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |


| Shot | Round | Ch | Pos P1 | Neg P1 | Neg P2 | A11 | A2 | A31 | ATot | Peak | ABS | Cal |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Type |  | Pa | Pa | Pal | msec | msec | mseci | msec | mPa-sec | mPa-sec | Pa Nolt |
| 491 | M62 | 1 | 814.61 | -491.26 | -650.86 | 104 | 164 |  | 220 | 40.37 | 86.55 | 693.88 |
|  |  | 2 | 667.05 | -429.65 | -492.07 | 108 | 180 |  | 232 | 33.17 | 73.04 | 557.27 |
|  |  | 3 | 303.031 | -308.74 | -273.011 | 128 | 240 |  | 280 | 23.05 | 54.99 | 357.35 |
|  |  | 4 | 176.4 |  | -194.92 | 156 |  |  | 308 | 16.81 | 36.17 | 324.86 |
|  |  | 8 | 96.4 |  | -110.4 | 192 |  |  | 320 | 12.31 | 22.15 | 107.47 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 50 | M59 | 1 | 768.12 |  | -618.24 | 100 |  |  | 204 | 37.19 | 75.93 | 693.88 |
|  |  | 2 | 818.63 |  | -663.15 | 96 |  |  | 200 | 33.44 | 75.75 | 557.27 |
|  |  | 3 | 331.62 |  | -355.92 | 120 |  |  | 252 | 23.08 | 48.56 | 357.35 |
|  |  | 4 | 190.37 |  | -159.18 | 140 |  |  | 280 | 13.47 | 26.27 | 324.86 |
|  |  | 8 | 91.14 |  | -107.8 | 184 |  |  | 320 | 11.22 | 20.37 | 107.47 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 51\| | M62 | 1 | 899.96 | -473.92 | -636.29 | 100 | 152 |  | 208 | 37.45 | 80.84 | 693.88 |
|  |  | 2 | 818.07 | -455.29 | -534.42 | 96 | 156 |  | 208 | 34.07 | 78.18 | 557.27 |
|  |  | 3 | 189.39 |  | -198.68 | 140 |  |  | 252 | 17.74 | 36.19 | 357.35 |
|  |  | 41 | 239.75 |  | -215.71\| | 136 |  |  | 292 | 17.83 | 40.74 | 324.86 |
|  |  | 8 | 114.46 |  | -159.5 | 196 |  |  | 312 | 17.31 | 37.94 | 107.47 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 531 | M17 | 1 | 1600.08 | -636.31 | -880.53 | 136 | 220 |  | 320 | 69.94 | 166.96 | 693.88 |
|  |  | 2 | 1121.22 | -528.85 | -655.35 | 144 | 244 |  | 344 | 55.45 | 137.09 | 557.27 |
|  |  | 3 | 594.27 |  | -472.77 | 172 |  |  | 416 | 56.61 | 141.02 | 357.35 |
|  |  | 4 | 214.41 |  | -159.18 | 184 |  |  | 412 | 24.96 | 57.05 | 324.86 |
|  |  | 8 | 164 |  | -154 | 228 |  |  | 456 | 25.33 | 48.62 | 107.47 |
| 1 |  |  |  |  |  |  |  |  |  |  |  |  |
| 54 | M33 | 1 | 3244.57 | -1350.9 | -2178 | 104 | 168 |  | 248 | 118.58 | 313.22 | 693.88 |
|  |  | 21 | 1207.04 | -692.13 | -959.061 | 128 | 224 |  | 2961 | 69.21 | 161.19 | 557.27 |
|  |  | 31 | 438.47 | -401.66 | -453.121 | 168 | 308 |  | 376 | 44.11 | 108.05 | 357.35 |
|  |  | 4 | 322.59 |  | -307.97 | 192 |  |  | 416 | 32.37 | 77.13 | 324.86 |
|  |  | 81 | 150.36 |  | -179.16 | 2481 |  |  | 444 | 24.34 | 47.51 | 107.47 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 55 | M331 | 1 | 3046.8 | -1323.9 | 2427.181 | 104 | 160 |  | 248 | 132.13 | 329.48 | 693.88 |
|  |  | 2 | 1263.33 | -767.92 | -1151.3 | 132 | 208 |  | 292 | 79.94 | 181.31 | 557.27 |
|  |  | 31 | 373.07 |  | -399.161 | 1761 |  |  | 368 | 40.54 | 83.12 | 357.35 |
|  |  | 41 | 295.3 |  | -290.11 | 196 |  |  | 412 | 33.4 | 69.67 | 324.86 |
|  |  | 8 | 250.52 |  | -275.35 | 224 | I |  | 472 | 32.81 | 62.17 | 107.47 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 56 | M33 | 1 | 1779.1 | -754.9 | -1165.21 | 132 | 216 |  | 296 | 80.31 | 189.8 | 693.88 |
|  |  | 2 | 941.23 | -580.12 | -682.11 | 144 | 2601 |  | 332 | 59.35 | 142.8 | 557.27 |
|  |  | 31 | 352.34 |  | -366.64 | 204 |  |  | 396 | 39.82 | 82.55 | 357.35 |
|  |  | 4 | 191.34 |  | -184.52\| | 228 |  |  | 412 | 24.57 | 44.52 | 324.86 |
|  |  | 8 | 143.26 |  | -154.331 | 272 |  |  | 448 | 24.27 | 48.97 | 107.47 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 57 | M33 | 1 | 1788.81 | -864.6 | -1230.2 | 132 | 216 |  | 300 | 88.87 | 217.68 | 693.88 |
|  |  | 21 | 711.07 | -468.7 | -599.04 | 160 | 268 |  | 344 | 54.05 | 116.39 | 557.27 |
|  |  | 3 | 369.14 |  | -311.25 | 184 |  |  | 400 | 35.98 | 82.06 | 357.35 |
|  |  | 4 | 306.18 |  | -215.87 | 224 |  |  | 428 | 27.94 | 58.8 | 324.86 |
|  |  | 8 | 181.52 |  | -226.02 | 240 |  |  | 476 | 27.8 | 64.88 | 107.47 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 58 | M17 | 1 | 1004.04 | -498.2 | -498.2 | 144 | 224 |  | 320 | 58.33 | 116.24 | 693.88 |
|  |  | 2 | 1526.4 | -730.57 | -730.7 | 128 | 216 |  | 316 | 73.99 | 156.87 | 557.27 |
|  |  | 3 | 326.6 | -225.8 | -225.8 | 172 | 248 ! |  | 344 | 38.77 | 73.22 | 357.35 |
|  |  | 4 | 326.6 | -273.7 | -275.9 | 196 | 300 : |  | 396 | 32.33 | 67.56 | 324.86 |
|  |  | 8 | 183.4 |  | -185.07 | 224 |  |  | 436 | 27.02 | 54.04 | 107.47 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 59 | M17 | 1 | 1380.12 | -571 | -661.27 | 140 | 2201 |  | 324 | 67.05 | 146.74 | 693.88 |
|  |  | 2 | 664.26 | -351.1 | -466.43 | 156 | 244 |  | 344 | 48.77 | 98.89 | 557.27 |
|  |  | 3 | 289.58 |  | -267.3 | 180 |  |  | 388 | 29.84 | 62.91 | 357.35 |
|  |  | 4 | 271.58 |  | -220.91 | 188 |  |  | 420 | 28.37 | 61.7 | 324.86 |
|  |  | 8 | 182.06 |  | -199.15 | 236 |  |  | 460 | 25.841 | 56.6 | 107.47 |
|  |  |  |  |  | $\square$ |  |  |  |  |  |  |  |


| Shotl | Pound | Ch | Pos P | Neg P1 | Neg P2 | A1 | A2 | A3 | ATot | Peak | ABS | Cal |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Type |  | Pa | Pa | Pa | msec | msec | msec | msec | mPa -sec | mPa -sec | $\mathrm{Pa} /$ Volt |
| 60 | M17 | 1 | 1425.92 | -562.7 | -774.37 | 136 | 228 |  | 328 | 63.01 | 152.63 | 693.88 |
|  |  | 2 | 891.07 | -417.4 | -557.83 | 148 | 240 |  | 344 | 52.39 | 117.98 | 557.27 |
|  |  | 3 | 260.86 |  | -266.98 | 184 |  |  | 388 | 32.29 | 63.66 | 357.35 |
|  |  | 4 | 220.58 |  | -241.7 | 216 |  |  | 416 | 31.55 | 64.01 | 324.86 |
|  |  | 8 | 185.5 |  | -184.7 | 216 |  |  | 488 | 25.07 | 52.11 | 107.47 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 62 | M62 | 1 | 1741.63 | -661.96 | -807.67 | 72 | 128 |  | 176 | 39.48 | 100.93 | 693.88 |
|  |  | 2 | 862.65 | -396.77 | -565.63 | 92 | 144 |  | 196 | 29.93 | 66.74 | 557.27 |
|  |  | 3 | 335.91 |  | -368.78 | 120 |  |  | 248 | 25.21 | 58.7 | 357.35 |
|  |  | 4 | 165.03 |  | -163.41 | 136 |  |  | 264 | 13.86 | 27.75 | 324.86 |
|  |  | 8 | 130.9 |  | -167.44 | 152 |  |  | 280 | 12.78 | 27.92 | 107.47 |
|  |  |  |  |  |  |  |  |  |  |  | 97 81 | 693.88 |
| 63 | M62 | 1 | 1772.16 | -597.43 | -854.86 | 72 | 128 |  | 180 | 39.87 | 107.81 |  |
|  |  | 2 | 755.66 | -401.2 | -571.2 | 92 | 140 |  | 188 | 31.18 | 65.47 | 557.27 |
|  |  | 3 | 294.81 |  | -255.5 | 116 |  |  | 228 | 16.73 | 34.67 | 357.35 |
|  |  | 4 | 180.95 |  | -167.3 | 148 |  |  | 264 | 15.8 | 30.12 | 324.86 |
|  |  | 8 | 78.67 |  | -81.57 | 172 |  |  | 276 | 9.03 | 17.61 | 107.47 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 64 | M59 | 1 | 1602.16 |  | -831.96 | 72 |  |  | 172 | 36.68 | 96.87 | 693.88 |
|  |  | 2 | 967.42 |  | -650.33 | 84 |  |  | 180 | 33.58 | 76.12 | 557.27 |
|  |  | 3 | 291.13 |  | -301.35 | 116 |  |  | 232 | 19.71 | 38.95 | 357.35 |
|  |  | 4 | 255.99 |  | -216.68 | 132 |  |  | 252 | 15.46 | 30.45 | 324.86 |
|  |  | 8 | 113.92 |  | -113.31 | 156 |  |  | 296 | 10.99 | 21.77 | 107.47 |
|  |  |  |  |  |  |  |  |  | 172 | 41.16 | 111.01 | 693.88 |
| 65 | M62 | 1 | 2042.77 | -686.2 | -988.08 | 68 | 120 |  |  |  |  | 557.27 |
|  |  | 2 | 797.45 | -432.44 | -545.57 | 84 | 144 |  | 196 | 29.55 | 66.79 | 357.35 |
|  |  | 3 | 356.99 |  | -291.95 | 104 |  |  | 240 | 19.88 | 48.48 | 357.35 |
|  |  | 4 | 179.32 |  | -165.03 | 136 |  |  | 260 | 13.6 | 26.16 | 324.86 |
|  |  | 8 | 123.92 |  | -146.6 | 176 |  |  | 312 | 14.5 | 28.45 | 107.47 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 66 | M59 | 1 | 1613.26 |  | -832.65 | 72 |  |  | 168 | 38.08 | 95.55 | 693.88 |
|  |  | 2 | 980.79 |  | . 597.39 | 80 |  |  | 172 | 32.06 | 73.07 | 557.27 |
|  |  | 3 | 350.56 |  | -297.67 | 104 |  |  | 224 | 18.01 | - 38.72 | 357.35 |
|  |  | 4 | 187.77 |  | -182.57 | 152 |  |  | 256 | 14.84 | 31.83 | 324.86 |
|  |  | 8 | 133.05 |  | -186.79 | 172 |  |  | 304 | 15.29 | 40.55 | 107.47 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 671 | M59 | 1 | 1958.81 |  | -1053.3 | 80 |  |  | 180 | 42.4 | 118.61 |  |
|  |  | 2 | 1175.3 |  | -719.43 | 80 |  |  | 176 | 34.53 | 82.13 | 557.27 |
|  |  | 3 | 376.29 |  | -351.27 | 104 |  |  | 224 | 18.79 | 44.42 | 357.35 |
|  |  | 4 | 250.14 |  | -229.03 | 136 |  |  | 260 | 14.75 | 31.37 | 324.86 |
|  |  | 8 | 105.97 |  | -146.49 | 168 |  |  | 292 | 11.99 | 24.33 | 107.47 |
|  |  |  |  |  |  |  |  |  | 184 | 353.29 | 92.75 | 693.88 |
| 68 | M62 | 1 | 1560.53 |  | -727.88 | 76 |  |  | 188 | 34.77 | 81.77 | 557.27 |
|  |  | 2 | 1102 |  | -650.61 | 84 |  |  | 228 | 17.69 | 32.84 | 357.35 |
|  |  | 3 | 237.28 |  | -222.63 | 124 |  |  | 264 | 15.28 | 32.1 | 324.86 |
|  |  | 4 | 215.71 |  | -210.84 | 132 |  |  | 288 |  | 26.98 | 107.47 |
|  |  | 8 | 130.04 |  | -151.54 | 160 |  |  | 288 | 14.08 |  |  |
|  |  |  |  |  |  |  | 680 |  | 848 | 120.85 | 267.61 | 700.68 |
| 73 | TPL-T | 1 | 629.21 | -403.58 | -555.64 | 392 | 705 |  | 872 | 110.47 | 239.03 | 554.026 |
|  |  | 2 | 725.22 | -369.54 | -492.48 | 420 |  |  | 924 | 91.431 | 205.91 | 350.769 |
|  |  | 3 | 422.32 |  | -359.34 | 436 |  |  | 944 | 94.485 | 201.32 | 319.416 |
|  |  | 4 | 395.44 |  |  | 504 |  |  | 964 | 85.586 | 176.83 | 105.102 |
|  |  | 8 | 274.52 |  | -347.99 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  | 820 | 113.15 | 237.01 | 700.68 |
| 74 | TPL-T | 1 | 602.55 |  | -507.99 | 388 |  |  | 860 | 118.31 | 249.41 | 554.026 |
|  |  | 2 | 501.67 |  | -523.83 | 408 |  |  | 908 | 93.81 | 199.18 | 350.769 |
|  |  | 3 | 434.95 |  | -393.91 | 420 |  |  | 940 | 99.01 | 217.53 | 319.416 |
|  |  | 4 | 486.79 |  | -392.88 | 416 |  |  | 976 | 85.03 | 176.74 | 105.102 |
|  |  | 8 | 282.34 |  | -332.02 | 480 |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |


| Shot | Round | Ch | PosPl | Neg P1\| | Neg P2: | A1 | A2 | A3 | ATot | Peak | ABS | Cal |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Type |  | Pal | Pa | PaI | msec | msecl | msec | msec | mPa-sec | mPa-sec | PaNolt |
| 75 | DM18 | 1 | 3501.95 |  | -3503.3 | 140 | 2881 | 388 | 516 | 175.83 | 1186.95 | 700.68 |
|  |  | 2 | 2411.68 |  | -1853.2 | 252 | 3521 | 476 | 588 | 244.21 | 563.95 | 554.026 |
|  |  | 3 | 900.768 |  | -900.74 | 320 | 456\| |  | 716 | 155.46 | 348.85 | 350.769 |
|  |  | 4 | 603.687 |  | -573.97 | 368 |  |  | 780 | 119.12 | 244.29 | 319.416 |
|  |  | 8 | 483.884 |  | -479.37 | 392 |  |  | 856 | 111.21 | 221.53 | 105.102 |
|  |  |  |  |  |  |  | 1 |  |  |  |  |  |
| 761 | TPL-T | 1 | 3505.5 |  | -3499.9 | 120 | ; |  | 484 | 161.4 | 1112.27 | 700.68 |
|  |  | 2 | 2772.62 |  | -2178.11 | 232 | , |  | 548 | 286.78 | 645.11 | 554.026 |
|  |  | 31 | 1139.65 |  | -996.89 | 300 |  |  | 684 | 172.84 | 380.29 | 350.769 |
|  |  | 4 | 780.66 |  | -708.15 | 356 |  |  | 756 | 144.84 | 299.88 | 319.416 |
|  |  | 8 | 513.74 |  | -509.85 | 404 |  |  | 816 | 123.08 | 249.02 | 105.102 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 77 | DM18 | 1 | 3505.5 |  | -2454.41 | 232 | 1 |  | 552 | 293.44 | 725.2 | 700.68 |
|  |  | 2 | 2251.8 |  | -1621.91 | 268 | , |  | 608 | 235.02 | 525.04 | 554.026 |
|  |  | 3 | 867.45 |  | -807.82 | 332 |  |  | 708 | 142.65 | 300.05 | 350.769 |
|  |  | 4 | 748.71 |  | -658.961 | 364 | + |  | 788 | 132.24 | 286.73 | 319.416 |
|  |  | 8 | 411.58 |  | -426.19 | 412 | I |  | 816 | 102.94 | 198.63 | 105.102 |
|  |  |  |  |  |  |  | + |  |  |  |  |  |
| 78 | TPL-T | 1 | 3505.51 |  | -3499.9 | 84 | ! |  | 432 | 133.64 | 1192.5 | 700.68 |
|  |  | 2 | 2772.6 |  | -2470.11 | 220 |  |  | 528 | 313.76 | 714.9 | 554.026 |
|  |  | 31 | 1096.85 |  | -1038.9 | 304 | ! |  | 676 | 177.85 | 394.76 | 350.769 |
|  |  | 4 | 793.75 |  | -703.35 | 352 |  |  | 752 | 146.31 | 299.39 | 319.416 |
|  |  | 8 | 519.44 |  | -524.79 | 416 |  |  | 848 | 127.89 | 260.38 | 105.102 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 791 | DM18 | 1 | 3505.5 |  | -3046.5 | 216 |  |  | 524 | 335.45 | 839.39 | 700.68 |
|  |  | 21 | 2139.37 |  | -1665.1 | 2681 |  |  | 612 | 239.62 | 538.97 | 554.026 |
|  |  | 31 | 864.65 |  | -874.47 | 328 |  |  | 724 | 155.69 | 341.65 | 350.769 |
|  |  | 4 | 705.91 |  | -645.54 | 372 |  |  | 796 | 133.93 | 279.19 | 319.416 |
|  |  | 81 | 501.65 |  | -524.77 | 416 |  |  | 860 | 122.87 | 253.84 | 105.102 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 80 | TPL-T\| | 1 | 3505 |  | -3500 | 76 |  |  | 416 | 129.8 | 1315.22 | 700.68 |
|  |  | 2 | 2772.6 |  | -2211.9 | 228 |  |  | 540 | 292.8 | 666.7 | 554.026 |
|  |  | 3 | 1120.7 |  | -990.2 | 296 |  |  | 684 | 173.92 | 394 | 350.769 |
|  |  | 4 | 872 |  | -746.2 | 352 |  |  | 764 | 151.85 | 321.3 | 319.416 |
|  |  | 8 | 5261 |  | -524.8 | 400 |  |  | 820 | 125.82 | 258.83 | 105.102 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 82 | TPL-T | 1 | 3503.3 | -2598.11 | -3503.3i | 132 | 3081 |  | 480 | 181.72 | 995.49 | 700.68 |
|  |  | 2 | 2770.11 | -1332.3 | -2526.5 | 212 | 3401 |  | 508 | 295.34 | 715.53 | 554.026 |
|  |  | 3 | 1346.21 | -686 | -1093.71 | 280 | 4721 |  | 636 | 179.5 | 393.72 | 350.769 |
|  |  | 4 | 904.58 | -538.2 | -755.74 | 336 | 556 |  | 716 | 144.46 | 312.97 | 319.416 |
|  |  | 8 | 526.5 |  | -526.5 | 384 | 6281 |  | 776 | 127.78 | 259.6 | 105.102 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 83 | TPL-T | 1 | 3505 |  | -3500 | 104 |  |  | 464 | 148.54 | 1116.15 | 700.68 |
|  |  | 2 | 2772.6 |  | -2506.71 | 212 |  |  | 500 | 326.49 | 721.92 | 554.68 |
|  |  | 3 | 1147.37 |  | -1109.11 | 284 |  |  | 644 | 183.8 | 401.43 | 350.769 |
|  |  | 4 | 826.01 |  | -758.611 | 348 |  |  | 724 | 149.2 | 305.96 | 319.416 |
|  |  | 8 | 526.031 |  | -524.771 | 384 |  |  | 796 | 126.28 | 252.67 | 105.102 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 84 | DM18 | 1 | 3503.3 |  | -2360.5 | 228 | 316 | 448 | 532 | 294.83 | 685.26 | 700.68 |
|  |  | 2 | 2672.6 | -846.48 | -2114.2 | 232 | 3321 | 436 | 544 | 266.72 | 610.92 | 554.026 |
|  |  | 3 | 1052.4 | -458.15 | -1065.3 | 3001 | 4201 |  | 648 | 172.35 | 374.4 | 350.769 |
|  |  | 4 | 808.761 | -331.24 | -753.28 | 344 | 4801 |  | 732 | 140.52 | 299.85 | 319.416 |
|  |  | 8 | 525.51 | -525.41 | -525.41 | 380 |  |  | 792 | 123.26 | 248.85 | 105.102 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 85 | DM18 | 1 | 3505 |  | -2988.41 | 212 |  |  | 508 | 335.57 | 804.05 | 700.68 |
|  |  | 2 | 2772.621 |  | -2414.71 | 236 |  |  | 532 | 306.2 | 684.47 | 554.026 |
|  |  | 3 | 1060.73 ! |  | -1087.7 | 308 |  |  | 668 | 178 | 382.3 | 350.769 |
|  |  | 4 | 793.75 |  | -761.81 | 352 |  |  | 748 | 143.52 | 302.34 | 319.416 |
|  |  | 8 | 526.77 |  | -524.8 | 400 |  |  | 816 | 128.3 | 256.35 | 105.102 |
|  | - |  |  |  |  | - |  |  |  |  |  |  |


| Shot 1 | Roundi | Ch! | Pos P1 | Neg P1 | Neg P21 | A11 | A2 | A3 | ATot | Peak | ABS | Cal |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Type |  | Pa | Pa | Pa | msec | msec | msec | msec | mPa-sec | mPa-sec | PaNolt |
| 86 | DM18 | 1 | 3505.5 |  | -2469.9 | 224 |  |  | 528 | 307.64 | 703.97 | 700.68 |
|  |  | 2 | 2772.6 |  | -2691.7 | 208 |  |  | 528 | 257.71 | 701.73 | 554.026 |
|  |  | 3 | 1055.8 |  | -1101.4 | 304 |  |  | 652 | 178.96 | 385.45 | 350.769 |
|  |  | 4 | 825.05 |  | -809.4 | 352 |  |  | 732 | 152.14 | 316.88 | 319.416 |
|  |  | 8 | 513.21 |  | -524.77 | 408 |  |  | 800 | 122.5 | 237.49 | 105.102 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 87 | TPL-T | $1]$ | 3505.5 |  | -3500 | 132 |  |  | 476 | 191.48 | 1025.6 | 700.68 |
|  |  | 21 | 2772.6 |  | -2400.6 | 220 |  |  | 508 | 303.39 | 678.77 | 554.026 |
| i |  | 31 | 1118.25 |  | -1053.3 | 292 |  |  | 644 | 177.46 | 381.85 | 350.769 |
| I |  | 4 | 899.16 |  | -765 | 340 |  |  | 728 | 150.19 | 323.82 | 319.416 |
| I |  | 8 | 508.06 |  | -507.54 | 408 |  |  | 804 | 121.7 | 237.65 | 105.102 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 901 | TPL-T | 1 | 3505 |  | -3500 | 56 |  |  | 464 | 81.27 | 1328.2 | 700.68 |
| $\square$ |  | 2 | 2583.15 |  | -2077.9 | 236 |  |  | 568 | 281.98 | 646.8 | 554.026 |
|  |  | 3 | 1062.48 |  | -948.131 | 3001 |  |  | 696 | 171.07 | 391.58 | 350.769 |
|  |  | 4 | 832.08 |  | -652.57 | 336 |  |  | 772 | 133.89 | 293.7 | 319.416 |
| . |  | 8 | 506.5 |  | -468.2 | 392 |  |  | 836 | 115.25 | 232.6 | 105.102 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 911 | DM18 | 1. | 3256 |  | -2327.7 | 248 |  |  | 584 | 285.3 | 675.6 | 700.68 |
|  |  | 21 | 2772.6 |  | -2766.5 | 180 |  |  | 536 | 209.6 | 788.1 | 554.026 |
|  |  | 31 | 1071.9 |  | -1132.9 | 296 |  |  | 672 | 175.4 | 403.8 | 350.769 |
|  |  | 4 | 832.1 |  | -652.6 | 336 |  |  | 772 | 133.89 | 293.7 | 319.416 |
|  |  | 8 | 425.45 |  | -424.6 | 404 |  |  | 820 | 104.6 | 206.5 | 105.102 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 921 | TPL-T | 1 | 3505 |  | -1915 | 232 |  |  | 576 | 266.9 | 611.4 | 700.68 |
|  |  | 2 | 2346.6 |  | -1731.6 | 244 |  |  | 592 | 243.1 | 565.6 | 554.026 |
|  |  | 3 | 1102.1 |  | -1003.9 | 296 |  |  | 688 | 169 | 382.7 | 350.769 |
|  |  | 4 | 782.3 |  | -708.8 | 356 |  |  | 760 | 138.2 | 295.5 | 319.416 |
|  |  | 8 | 435.5 |  | -451.6 | 416 |  |  | 816 | 112.4 | 223.7 | 105.102 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 931 | DM18 | 1 | 3331 |  | -2329.8 | 248 |  |  | 588 | 286.7 | 689.3 | 700.68 |
|  |  | 2 | 2772.6 |  | -2766.8 | 204 |  |  | 552 | 242.2 | 758.5 | 554.026 |
|  |  | 3 | 1055.8 |  | -1101.4 | 300 |  |  | 680 | 171.4 | 392.4 | 350.769 |
|  |  | 4 | 739.5 |  | -711 | 348 |  |  | 760 | 135.3 | 294.1 | 319.416 |
|  |  | 8 | 485.5 |  | -491.9 | 400 |  |  | 844 | 111 | 227.2 | 105.102 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 94 | TPL-T | 1 | 3505.5 |  | -2492 | 220 |  |  | 548 | 314.9 | 771.5 | 700.68 |
|  |  | 2 | 2511.9 |  | -1900 | 236 |  |  | 572 | 257 | 590 | 554.026 |
|  |  | 3 | 1042.84 |  | -1006 | 308 |  |  | 700 | 171.2 | 380.8 | 350.769 |
|  |  | 4 | 752.56 |  | -658.9 | 356 |  |  | 768 | 136.7 | 281.8 | 319.416 |
|  |  | 8 | 494.7 |  | -457.5 | 392 |  |  | 840 | 113.2 | 226.8 | 105.102 |
|  |  |  |  |  |  |  |  |  |  |  |  | 70068 |
| 95 | DM18 | 1 | 3505.5 |  | -2722.8 | 2281 |  |  | 556 | 312.5 | 766.7 | 700.68 |
|  |  | 21 | 2500 |  | -1992.1 | 252 |  |  | 588 | 252.9 | 594.2 | 554.026 |
|  |  | 3 | 878.3 |  | -935.2 | 316 |  |  | 708 | 152.5 | 348.2 | 350.769 |
|  |  | 41 | 683.9 |  | -629.31 | 3601 |  |  | 776 | 125.9 | 274.3 | 319.416 |
|  |  | 8 | 439 |  | -448.11 | 412 |  |  | 852 | 106.2 | 216.1 | 105.102 |

## APPENDIX F:

MICROPHONE DATA FROM COLLECTION TEST PHASE

Intentionally left blank.

## DATA COLLECTION HIGH FIDELITY MICROPHONE POSITIONS:

All coordinates are in meters.
30 Mar 93

| 3-m hub | $\mathrm{x}:-1.512$ | $\mathrm{y}: 1697.509$ | $\mathrm{z}: 1.388$ |
| :--- | :--- | :--- | :--- |
| 6-m hub | $\mathrm{x}:-5.022$ | $\mathrm{y}: 1697.238$ | $\mathrm{z}: 1.506$ |
| 9-m hub | $\mathrm{x}:-8.270$ | $\mathrm{y}: 1697.001$ | $\mathrm{z}: 1.450$ |
| 12-m hub | $\mathrm{x}:-11.432$ | $\mathrm{y}: 1696.818$ | $\mathrm{z}: 1.380$ |

Microphone Elevations, top of microphone:

| Hub Reference | 31 Mar 93 | 5 Apr 93 | 6 Apr 93 | 7 Apr 93 |
| :---: | :---: | :---: | :---: | :---: |
| 3-m hub | 2.723024 | 2.723024 | 2.726072 | 2.738264 |
| 6-m hub | 2.86236 | 2.853216 | 2.86236 | 2.856264 |
| 9-m hub | 2.80636 | 2.80636 | 2.812456 | 2.818552 |
| 12-m hub | 2.7516 | 2.711976 | 2.699784 | 2.6754 |

## DATA COLLECTION ROUND LOCATION MICROPHONE POSITIONS:

All coordinates in meters.
30 MARCH93

| sensor 1 | $x:-.0242$ | $y: 1697.945$ | $z: 1.516$ |
| :--- | :--- | :--- | :--- |
| sensor 2 | $x: 2.798$ | $y: 1698.901$ | $z: 1.685$ |
| sensor 3 | $x:-0.192$ | $y: 1698.927$ | $z: 1.692$ |
| sensor 4 | $x:-3.230$ | $y: 1698.966$ | $z: 1.692$ |
| sensor 5 | $x:-1.796$ | $y: 1698.902$ | $z: 1.692$ |
| sensor 6 | $x:-2.205$ | $y: 1698.915$ | $z: 1.725$ |

8 APR 93
$10^{\circ}$ Rotation, Counter Clockwise about sensor 3

| sensor 1 | $x:-0.006$ | $y: 1697.976$ | $z: 1.654$ |
| :--- | :--- | :--- | :--- |
| sensor 2 | $x: 2.772$ | $y: 1699.465$ | $z: 1.719$ |
| sensor 3 | $x:-0.192$ | $y: 1698.927$ | $z: 1.692$ |
| sensor 4 | $x:-3.150$ | $y: 1698.448$ | $z: 1.607$ |
| sensor 5 | $x: 2.953$ | $y: 1698.460$ | $z: 1.698$ |
| sensor 6 | $x:-2.974$ | $y: 1697.498$ | $z: 1.666$ |

## DATA COLLECTION GUN POSITIONS:

All coordinates in meters.

## References

| 1700 M Position | x: 0 | y: 0 | z: 0 |
| :--- | :--- | :--- | :--- |
| 1000 M Position | x: -7.181 | y: 700.252 | z: 0.244 |
| 800 M Position | x: -8.530 | y: 900.249 | z: 0.801 |
| 600 M Position | x: -11.340 | y: 1100.137 | z: -0.175 |
| 400 M Position | x: -23.602 | y: 1299.785 | z: -0.534 |

30MAR 93
7.62 mm Muzzle
x: 22.583
y: 1299.923
z: 0.676
5 APR 93
7.62 Muzzle
x: -6.296
y: 900.175
z: 1.990
6 APR 93
.50 cal Muzzle
7.62 Muzzle

| x: -5.230 | y: 700.283 | z: 1.490 |
| :--- | :--- | :--- |
| x: -22.074 | y: 1299.934 | z: 0.737 |

7APR 93
35 mm Muzzle

| $\mathrm{x}:-5.487$ | $\mathrm{y}: 698.197$ | $\mathrm{z}: 2.051$ |
| :--- | :--- | :--- |
| $\mathrm{x}:-22.813$ | $\mathrm{y}: 1298.062$ | $\mathrm{z}: 1.370$ |
| $\mathrm{x}:-1.967$ | $\mathrm{y}: 1882$ | $\mathrm{z}: 1.778$ |

35 mm Muzzle
$x:-1.967 \quad y: 1.882 \quad z: 1.778$

8 APR 93
0.50 cal Muzzle

35 mm Muzzle
$x:-22.126 \quad y: 1299.823 \quad z: 0.736$

2 APR 93
35 mm Muzzle
35 mm Muzzle

| $\mathrm{x}:-1.900$ | $\mathrm{y}:-1.877$ | z: 1.819 |
| :--- | :--- | :--- |
| $\mathrm{x}:-8.713$ | $\mathrm{y}: 698.340$ | $\mathrm{z}: 2.063$ |

Offset Distance


$\underset{\sim}{\circ} \dot{\sim}$

|  | $\sum_{i}^{0}$ |  | $\underset{\Delta}{\Sigma}$ | $\underset{0}{2}$ |  |  | $\underset{\Delta}{K}$ |  |  | $\stackrel{\sim}{\infty}$ | $\stackrel{\infty}{\infty}$ | $\left\lvert\, \begin{aligned} & \underset{\sim}{\infty} \\ & \underset{\sim}{2} \end{aligned}\right.$ |  |  |  |  | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\frac{8}{8}$ | $\underset{\sim}{c}$ |  | $\begin{gathered} \stackrel{n}{2} \\ \underset{\sim}{2} \end{gathered}$ |  | ন্নি |  | Z | $\underset{\sim}{Z}$ | K | K | $\stackrel{\text { ¢ }}{7}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\sum_{i}^{0}$ |  |  | $\ll$ |  | $\Sigma_{0}^{K}$ | $\underset{\Delta}{\Sigma}$ | $\frac{<}{2}$ |  |  | $\begin{array}{l:l} 8 \\ \\ \end{array}$ | $\frac{\underset{m}{m}}{m}$ |  | $\frac{S}{n} \frac{n}{n}$ |  |  |  |  | 葆荷 | $\stackrel{y}{4}$ | $\stackrel{n}{\underset{\sim}{\sim}}$ |  | $\begin{aligned} & \infty \\ & \infty \\ & m \end{aligned}$ |  | $\underset{B}{\Sigma}$ | K | Z | 茴 | $\stackrel{12}{\text { ì }}$ |
|  | $\sum_{i}^{C}$ |  |  | $\mathbb{Z}$ |  | $\underset{\sim}{<}$ | $\underset{a}{\Sigma}$ | $\underset{\Delta}{\mathbb{Z}}$ | $\underset{a}{\pi}$ |  |  | $$ |  |  |  |  | $\stackrel{n}{n}$ | $\begin{aligned} & \stackrel{\sim}{0} \\ & \underset{\sim}{2} \end{aligned}$ |  |  | $$ | $\begin{aligned} & \hat{8} \\ & \underset{\sim}{8} \\ & \hline \end{aligned}$ | $\frac{8}{8}$ |  | $\underset{0}{<}$ | $\underset{a}{Z}$ | 葆 | Z | ¢ |
| $\sqrt{5}$ | $\sum_{i}$ | $\begin{aligned} & \overrightarrow{0} \\ & 0 \\ & \underline{0} \end{aligned}$ |  | 处 | $\underset{a}{\Sigma}$ | $\sum_{Q}^{<}$ |  | $\underset{\sim}{\underset{O}{4}}$ | $\underset{\Delta}{\mathbb{Z}}$ |  | $\stackrel{n}{n}$ | $\stackrel{7}{7}$ |  |  | $\frac{2}{2}$ | $\stackrel{n}{n}$ | $\stackrel{O}{n}$ | $\stackrel{\iota!}{\|c\|}$ |  |  | $\frac{0}{i}$ |  | $\frac{n}{n}$ |  | $\underset{\Delta}{\Sigma}$ | 元 | 葆 | Z | $\stackrel{\square}{\sim}$ |
|  | $\|\underset{y}{\boldsymbol{O}}\|$ | $\begin{aligned} & \widetilde{O} \\ & \text { O} \\ & \text { En } \end{aligned}$ | $\frac{1}{2}$ | Z | ＜ | $\underset{\square}{<}$ | $\underset{i}{<}$ | $\underset{\sim}{\underset{\alpha}{4}}$ | 名 |  | $\stackrel{\unrhd}{=}$ | $\begin{aligned} & 8 \\ & \hline \end{aligned}$ | $\begin{aligned} & 0 \\ & \infty \\ & \dot{\sim} \end{aligned}$ |  |  | $\begin{aligned} & 0 \\ & \hat{0} \\ & \hat{i} \end{aligned}$ | $\stackrel{8}{8}$ | $\infty$ | $\underset{\sim}{<} \underset{\sim}{\infty}$ |  | $\stackrel{セ 2}{\infty}$ |  | $\begin{aligned} & \substack{0 \\ \text { in } \\ \hline} \end{aligned}$ |  | Z | $\mathbb{Z}$ | 茖 | 葆 | $\frac{\stackrel{8}{8}}{}$ |
|  | $\underset{\substack{0}}{\stackrel{\rightharpoonup}{2}}$ | $\begin{aligned} & \widehat{O} \\ & \stackrel{0}{s} \end{aligned}$ | $\bar{O}$ |  | $\underset{\Delta}{4}$ | $\underset{\Delta}{K}$ | $\underset{\sim}{\alpha}$ | $\underset{\square}{\boldsymbol{Z}}$ | $\begin{aligned} & \mathbb{Q} \\ & \underset{Q}{2} \end{aligned}$ |  | $\stackrel{y}{8}$ | O | 若 |  |  |  | 동 | 둥 | 亿号 |  | O8 |  | O |  | Z | $\underset{0}{\Sigma}$ | $\underset{0}{k}$ | $<$ | \％ |
|  | $\sum_{i}^{0}$ | $\hat{\xi}$ | $\stackrel{\text { ¢ }}{\text { ¢ }}$ | － | $\stackrel{\text { N }}{\substack{0 \\=1}}$ | \％ | $\bigcirc$ |  | 2 |  | $乏$ | $\left\lvert\, \begin{aligned} & \text { O20} \\ & \\ & \hline \end{aligned}\right.$ | $\begin{aligned} & 0 \\ & 0 \\ & =0 \end{aligned}$ | 12 |  |  |  | $\underset{\infty}{\infty}$ |  |  | $\stackrel{\stackrel{\rightharpoonup}{7}}{\underset{\sim}{2}}$ | $\stackrel{\rightharpoonup}{3} \stackrel{9}{2}$ | $\stackrel{\underset{\sim}{6}}{\underset{\sim}{2}}$ |  | 吕 | $\begin{aligned} & \infty \\ & \underset{\sim}{\dot{\alpha}} \end{aligned}$ | $\begin{aligned} & \infty \\ & \underset{y}{\infty} \\ & \underset{\sim}{2} \end{aligned}$ | Nin | － |
|  | $\mid \underset{\substack{\mathrm{E}}}{\stackrel{\rightharpoonup}{U}}$ | $\bar{E}$ |  | $\left\|\begin{array}{c} \infty \\ \infty \end{array}\right\|$ | $\stackrel{n}{\infty}_{\substack{0 \\ \infty}}$ | $\frac{\Omega}{z}$ | $\stackrel{Q}{\mathbf{z}}$ | 吕 | $8$ |  | $\stackrel{Q}{z}$ | $\underset{\infty}{\infty}$ | $\stackrel{\sim}{\infty}$ |  | $\overline{2}$ | $\hat{z}$ | 区 | $\begin{array}{\|c\|} \hline \\ \infty \end{array}$ | $\begin{array}{c\|c\|c} \infty \\ \infty & \infty \\ \infty & \underset{\sim}{n} \\ \infty & \infty \end{array}$ |  | $\begin{gathered} N \\ \substack{0 \\ \infty} \end{gathered}$ | $\begin{gathered} \substack{c \\ \infty \\ \hline \\ \hline \\ \hline \\ \hline} \end{gathered}$ | $\begin{aligned} & \neq \\ & \substack{\infty\\ } \end{aligned}$ |  | 吴 | $\stackrel{\stackrel{\rightharpoonup}{6}}{\dot{\circ}}$ | $\stackrel{\stackrel{\rightharpoonup}{2}}{\underset{\infty}{\infty}}$ | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | 衰 |
|  | $\underset{y}{3}$ | $\underline{\xi}$ | $\begin{aligned} & \infty \\ & \infty \\ & \infty \\ & \sim \end{aligned}$ | $\stackrel{a}{\lambda}$ | $\begin{gathered} 8 \\ \underset{4}{n} \\ \end{gathered}$ | $\hat{Z}$ | $8$ | Q | $\stackrel{Q}{Z}$ |  | 2 2 | $\begin{gathered} \text { N} \\ \text { in } \end{gathered}$ | $\begin{gathered} 0 \\ \hline \end{gathered}$ | $\hat{N}_{3}^{3}$ | $\frac{1}{2}$ | 乞 | $\begin{gathered} 10 \\ 6 \\ e \end{gathered}$ | $\begin{aligned} & \mathbf{C} \\ & \\ & \end{aligned}$ |  |  | $\frac{\stackrel{n}{4}}{1}$ | $\begin{gathered} \text { An } \\ \\ \end{gathered}$ | $\begin{gathered} 7 \\ 7 \\ 7 \end{gathered}$ |  | $\bigcirc$ | $\begin{gathered} \infty \\ \infty \\ \infty \\ n \end{gathered}$ | $\stackrel{\stackrel{\rightharpoonup}{\circ}}{\stackrel{\circ}{\circ}}$ |  | － |
|  | $\sum_{i}$ | $\bar{\xi}$ | $\stackrel{\substack{9 \\ \hdashline}}{2}$ | $\stackrel{8}{\underset{\sim}{i}}$ | $\stackrel{\rightharpoonup}{\stackrel{N}{\mathrm{~N}}}$ | $\stackrel{Q}{\mathrm{z}}$ | $\hat{Z}$ | $\hat{z}$ | $\hat{z}$ |  | 2： |  |  |  | $\frac{\square}{2} \frac{1}{2}$ |  | $\stackrel{\Xi}{\square}$ | $\stackrel{\stackrel{\rightharpoonup}{4}}{\underset{\sim}{i}} \mid$ | $\underset{\sim}{\stackrel{O}{\mathrm{~N}}} \stackrel{\rightharpoonup}{\mathrm{~N}}$ |  | $\stackrel{\otimes}{\infty}$ |  | $\stackrel{2}{8}$ | $\underset{\sim}{9}$ | $\bar{z}$ |  | 8 | $\begin{aligned} & \underset{\sim}{~} \\ & \underset{\sim}{2} \end{aligned}$ | $\stackrel{\sim}{2}$ |
|  | $\sum_{\bar{I}}^{\underline{J}}$ | $\varepsilon$ | $\left\lvert\, \begin{aligned} & 0 \\ & 10 \\ & 0 \end{aligned}\right.$ | － | $\underset{\sim}{7}$ | 吕 | 亿 | Z | \％ |  | \％ 2 | $\stackrel{+}{+}$ |  |  |  |  | $\left\lvert\, \begin{gathered} \underset{N}{\mathrm{~N}} \end{gathered}\right.$ | $\stackrel{\square}{6}$ |  | $\stackrel{\infty}{\sim}$ | $\stackrel{\text { din }}{\substack{\infty \\-1}}$ |  | $\underset{\sim}{\infty}$ | $\bigcirc$ | z | $\stackrel{0}{9}$ | $\begin{gathered} \text { ò } \\ \hline 0 \end{gathered}$ | $\stackrel{N}{N}$ | $\xrightarrow{\sim}$ |
| $1 \%$ | $\begin{aligned} & 0 \\ & \mathbf{Z} \end{aligned}$ | $\begin{aligned} & \dot{0} \\ & \dot{0} \\ & 0 \end{aligned}$ | N |  | － | N | ¢ | \＃ | ¢ | e |  | ¢ | 8 |  | 7 |  | $\underset{7}{7}$ | \＃ | 48 | \％ | $\underset{\sim}{\infty}$ | \％ 9 | 응 | in | ก | in | ［17 | 용 | $\bigcirc$ |


|  | $\begin{array}{l\|l} 0 \\ \underset{y}{0} \\ \dot{0} \\ \text { en } \end{array}$ | $1 \begin{aligned} & 0 \\ & 4 \\ & \vdots \end{aligned}$ | $\left\lvert\, \begin{gathered} n \\ \mathbf{~} \\ \hline \end{gathered}\right.$ |  | $\left\|\begin{array}{c} \infty \\ \stackrel{8}{\infty} \\ \underset{m}{2} \end{array}\right\|$ | $\underset{\Delta}{\Sigma}$ | $\underset{\Delta}{\mathbb{Z}}$ | $\left\|\begin{array}{l} n \\ \underset{n}{n} \end{array}\right\|$ | $\stackrel{\sim}{n}$ |  | $\begin{gathered} 9 \\ \infty \\ N \end{gathered}$ | $\underset{\sim}{\infty} \underset{\sim}{\infty}$ |  |  | $\underset{\square}{\Sigma}$ | 侣汉 | < | 苜 | $\mathfrak{c}$ | $\stackrel{N}{7}$ | $\stackrel{N}{N}$ | 茴 | $\begin{aligned} & \infty \\ & \vdots \\ & \vdots \\ & \end{aligned}$ | $\underset{0}{<}$ | $\underset{a}{z}$ | － | ＋ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\underset{\substack{o \\ \infty \\ \hline}}{ }$ | $\left\lvert\, \begin{aligned} & \text { 茳 } \\ & \hline \end{aligned}\right.$ | $\left\|\begin{array}{l} \stackrel{\rightharpoonup}{\mathbf{C}} \\ -1 \end{array}\right\|$ | $\left\|\begin{array}{l} \stackrel{8}{e} \\ \stackrel{N}{i} \end{array}\right\|$ | $\underset{\square}{\mathbb{Z}}$ | Z | $\begin{aligned} & \infty \\ & \infty \\ & m \\ & m \end{aligned}$ |  |  | $\begin{gathered} n \\ \mathrm{~N} \\ \mathrm{n} \end{gathered}$ |  |  | $\underset{0}{4}$ | 亿 | K | $\underset{a}{c}$ | $\leqslant$ | $\begin{gathered} \stackrel{\rightharpoonup}{6} \\ \dot{N} \end{gathered}$ | $\stackrel{1}{0}$ | $\begin{aligned} & 0 \\ & \stackrel{0}{n} \\ & \text { N } \end{aligned}$ | $\stackrel{O}{9}$ | $\stackrel{\substack{\infty \\ \infty \\ \hline}}{ }$ | $\underset{\Delta}{\gtrless}$ | $\underset{z}{<}$ | $\begin{gathered} \underset{\substack{0}}{\substack{2}} \end{gathered}$ | 遃 |
|  |  | $\left\lvert\, \begin{gathered} 0 \\ \substack{n \\ 0} \end{gathered}\right.$ | $\left\lvert\, \begin{aligned} & 0 \\ & 0 \\ & \underset{\sim}{0} \\ & \hline \end{aligned}\right.$ | $\begin{aligned} & \mathrm{F} \\ & \hline 0 \end{aligned}$ | $\stackrel{8}{\substack{0 \\ i}}$ | $\mathbf{z}$ | $\underset{\square}{Z}$ |  | $$ |  | $\begin{gathered} \mu \\ \underset{\sim}{4} \end{gathered}$ |  | $\frac{4}{\square}$ | $\underset{\square}{\Sigma}$ | 灾 | 家伿 | $\underset{\square}{\mid}$ | $\underset{\Delta}{\Sigma}$ | $\begin{aligned} & 10 \\ & \stackrel{N}{6} \end{aligned}$ |  | $\frac{0}{0}$ |  | $\stackrel{8}{8}$ | $\underset{0}{<}$ | $\underset{0}{Z}$ | $\begin{array}{l\|l\|l} \substack{8 \\ \hline \\ \hline \\ \hline} \end{array}$ | $\frac{n}{7}$ |
| E |  | $\frac{尺}{\mathrm{~N}}$ | $\begin{gathered} 0 \\ 0 \\ 0 \\ \vdots \end{gathered}$ | $\stackrel{\circ}{6}$ | $\begin{array}{\|c} \stackrel{\circ}{\circ} \\ \stackrel{-1}{-} \end{array}$ | Z | $\bar{\Delta}$ | $\underset{\sim}{N}$ | 읃 | $\frac{n}{x}$ | $\stackrel{\infty}{\stackrel{\infty}{\sim}}$ | $\stackrel{2 n}{\stackrel{n}{\Omega}}$ | $\underset{\Delta}{z}$ | 希 | Z | 之《 | $\underset{Z}{k}$ | $\underset{\sim}{\Sigma}$ | $\stackrel{L 0}{0}$ | $\underset{\sim}{N}$ | $\stackrel{\unrhd}{\infty}$ | $\stackrel{\text { 각 }}{2}$ | $\stackrel{\underset{C}{\infty}}{\stackrel{\infty}{\circ}}$ |  |  |  | O |
|  | $\sum_{\substack{\mathrm{N}}}$ | $\underset{\sim}{\infty}$ | $\begin{aligned} & \underset{8}{8} \\ & \dot{8} \end{aligned}$ | $\stackrel{O}{i}$ | $\left\|\begin{array}{c} \mathbf{c} \\ \underset{c}{2} \end{array}\right\|$ | Z | $\underset{a}{z}$ | $\left\lvert\, \begin{gathered} \mathrm{N} \\ \mathrm{in} \end{gathered}\right.$ | ¢ |  | $\begin{aligned} & \infty \\ & \infty \\ & \infty \end{aligned}$ | $\begin{aligned} & 0 \\ & 10 \\ & 6 \end{aligned}$ | $\underset{a}{c}$ | $\underset{\square}{4}$ | Z | 亿 | 茴 | $\stackrel{\gtrless}{Z}$ |  |  |  | $\stackrel{4}{6}$ |  |  |  |  | \％ |
|  | $\underset{y}{c}$ | ©్ర్రి\| | 呂 | $\hat{C}_{5}^{8}$ | $\begin{array}{\|c} \hline 8 \\ \hline 0 \end{array}$ | $\underset{\sim}{Z}$ | $\underset{\sim}{Z}$ | $0$ | 응 |  | $0$ |  | $\underset{a}{c}$ | K | 《 |  | $\underset{0}{\mathbb{Z}}$ |  |  |  |  |  |  |  |  |  | ᄋ్ర్ర |
|  | $\sum_{i}^{2}$ | $\underset{\sim}{\stackrel{\rightharpoonup}{n}}$ | $\begin{gathered} \text { No } \\ \stackrel{\rightharpoonup}{e} \end{gathered}$ | $\begin{aligned} & \dot{8} \\ & \stackrel{y}{i} \\ & \underset{\sim}{2} \end{aligned}$ | $\begin{gathered} \text { İ } \\ \text { n } \end{gathered}$ | $\bigcirc$ | $\stackrel{\infty}{\infty}$ |  |  | $\stackrel{\rightharpoonup}{x}$ | $\underset{7}{7}$ | $\underset{=}{\sim}$ | 亿 | \％ | $\bigcirc$ | 又 | $\mathrm{Z}$ |  |  |  |  | ne | $\stackrel{\infty}{\square}$ | $\bar{Z}$ |  | $\stackrel{8}{8}$ | $\stackrel{7}{7}$ |
|  | $\sum_{i}^{U}$ <br> E | $l_{0}^{9}$ | $\stackrel{18}{2}$ | $\begin{array}{\|c} \hat{N} \\ \end{array}$ | $\stackrel{\infty}{6}$ | Z | $\left.\right\|_{\substack{n \\ \infty \\ \hline}}$ | $\begin{aligned} & 9 \\ & \infty \end{aligned}$ | $$ | ${\underset{c}{\infty}}_{\infty}^{\infty} \mid \underset{\sim}{\underset{\sim}{c}}$ | $\underset{\sim}{\infty}$ |  | $\frac{1}{z}$ | $18$ | Q | 亿号 | \％ |  |  | $\underset{\sim}{\mathrm{N}}$ |  |  |  | 亿 |  |  | － |
| $\frac{\stackrel{\pi}{2}}{\bar{\phi}}$ |  | $\frac{\underset{0}{6}}{\overrightarrow{6}}$ | $\frac{\ddot{C}}{7}$ | $\stackrel{9}{9} \frac{9}{7}$ | $\begin{aligned} & \text { N్O } \\ & \hline \end{aligned}$ | $2$ | $\left.\begin{gathered} 8 \\ \\ i n \end{gathered} \right\rvert\,$ | $\stackrel{n}{n}$ |  |  | $\underset{\sim}{\underset{\sim}{2}} \underset{\substack{2}}{ }$ |  | Z | Z | $\hat{z}$ | $2 \%$ | \％ |  | $\stackrel{i}{\mathrm{a}} \underset{\mathrm{~m}}{\mathrm{~m}}$ | $\stackrel{i}{9}$ |  |  |  | $\bar{z}$ | $\overline{\mathrm{F}}$ | $\overline{\mathrm{B}}$ | $\stackrel{\infty}{\sim}$ |
|  | $\underset{\underline{I}}{\underset{y}{2}}$ | N | $\stackrel{\square}{-}$ | $\stackrel{\left.\begin{array}{l} \mathrm{N} \\ \mathrm{C} \end{array} \right\rvert\,}{ }$ | $\frac{\infty}{\infty}$ | $\mathrm{Z}$ | $\underset{\substack{N \\ \underset{N}{N} \\ \hline}}{ }$ | $\left\|\begin{array}{l} 08 \\ \text { in } \end{array}\right\|$ | Nすべ | $\stackrel{\sim}{\text { N }}$ N | $\stackrel{\infty}{\sim}$ | $\stackrel{8}{\circ}$ | q | $12$ | \％ | 亿令 | 2 | N | ن | $\underset{\sim}{\mathrm{N}}$ | הi |  |  | $\Sigma$ |  | － | $\stackrel{\text { N／}}{\sim}$ |
|  | $\sum_{i}^{U}$ | － | $\stackrel{\infty}{1}$ | $$ | $\begin{aligned} & \underset{\sim}{\mathrm{N}} \end{aligned}$ | Z | $\xrightarrow{\sim}$ | $\stackrel{\sim}{0}$ |  | $\underset{\sim}{\mathrm{N}} \underset{\underset{\sim}{2}}{\underset{\sim}{2}}$ | 采 |  | $\stackrel{\circ}{2}$ | \％ | Z | $\frac{2}{2}$ | 2 |  | $\stackrel{-}{-}$ |  |  | － |  | \％ |  | $\stackrel{ }{ }$ | $\stackrel{\rightharpoonup}{3}$ |
| 0 | $\begin{aligned} & 0 \\ & \mathbf{z} \end{aligned}$ | ก | $\infty$ | in | O | $\overline{6}$ | N | 3 | \％ |  |  |  | ล | R | K | $N \sim$ | $\pm$ | N | $\bigcirc$ |  | A | $\mathfrak{N}$ | $\infty$ | － | － | $\infty$ | $\infty$ |


$\therefore \dot{\sim}$

| RD. |  | Offset Distance |  |  |  |  |  | rival Tim |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NO. | HMic1 | HMic2 | HMic3 | HMic4 | HMic5 | LMic1 | LMic2 | LMic3 | LMic4 | LMic5 | LMic6 |
| Consec. | (m) | (m) | (m) | (m) | (m) | (msec) | (msec) | (msec) | (msec) | (msec) | (msec) |
| 113 | 1.242 | 2.814 | 6.246 | 9.485 | 12.649 | 0.000 | 3.345 | 1.660 | 6.745 | 2.325 | 4.890 |
| 114 | 1.078 | 2.618 | 6.046 | 9.285 | 12.449 | 0.000 | 3.910 | 1.635 | 6.565 | 2.930 | 4.690 |
| 115 | 1.311 | 2.850 | 6.265 | 9.500 | 12.663 | 0.000 | 3.390 | 1.705 | 6.545 | 2.285 | 4.650 |
| 116 | 1.351 | 2.849 | 6.243 | 9.473 | 12.636 | 0.000 | 3.420 | 1.675 | 6.470 | 2.325 | 4.580 |
| 117 | 1.093 | 2.718 | 6.180 | 9.423 | 12.588 | 0.000 | 3.580 | 1.690 | 6.935 | 2.550 | 5.045 |
| 118 | 0.972 | 2.196 | 5.545 | 8.773 | 11.934 | 0.000 | 5.160 | 1.485 | 5.455 | 4.150 | 3.580 |
| 119 | 1.390 | 2.094 | 5.219 | 8.410 | 11.560 | DNA | DNA | DNA | DNA | DNA | DNA |
| 120 | 1.481 | 2.021 | 5.076 | 8.257 | 11.405 | DNA | DNA | DNA | DNA | DNA | DNA |
| 121 | 1.048 | 1.643 | 4.895 | 8.115 | 11.275 | DNA | DNA | DNA | DNA | DNA | DNA |
| 122 | 1.643 | 1.899 | 4.820 | 7.986 | 11.129 | DNA | DNA | DNA | DNA | DNA | DNA |
| 123 | 1.126 | 2.030 | 5.280 | 8.493 | 11.651 | DNA | DNA | DNA | DNA | DNA | DNA |
| 124 | 0.981 | 1.676 | 4.958 | 8.182 | 11.343 | DNA | DNA | DNA | DNA | DNA | DNA |
| 125 | 1.610 | 2.243 | 5.269 | 8.439 | 11.582 | DNA | DNA | DNA | DNA | DNA | DNA |
| 126 | 1.867 | 2.317 | 5.185 | 8.323 | 11.455 | DNA | DNA | DNA | DNA | DNA | DNA |
| 127 | 1.701 | 2.152 | 5.090 | 8.248 | 11.387 | DNA | DNA | DNA | DNA | DNA | DNA |
| 128 | 1.584 | 2.106 | 5.113 | 8.284 | 11.428 | DNA | DNA | DNA | DNA | DNA | DNA |
| 129 | 1.484 | 2.055 | 5.114 | 8.295 | 11.443 | DNA | DNA | DNA | DNA | DNA | DNA |
| 130 | 2.213 | 2.388 | 4.982 | 8.066 | 11.169 | DNA | DNA | DNA | DNA | DNA | DNA |
| 131 | 1.988 | 2.634 | 5.528 | 8.657 | 11.775 | DNA | DNA | DNA | DNA | DNA | DNA |
| 132 | 1.891 | 2.497 | 5.407 | 8.545 | 11.667 | DNA | DNA | DNA | DNA | DNA | DNA |
| 133 | 2.230 | 2.846 | 5.649 | 8.749 | 11.854 | DNA | DNA | DNA | DNA | DNA | DNA |
| 134 | 1.479 | 1.060 | 4.114 | 7.331 | 10.487 | DNA | DNA | DNA | DNA | DNA | DNA |
| 135 | 1.317 | 2.235 | 5.428 | 8.627 | 11.774 | DNA | DNA | DNA | DNA | DNA | DNA |
| 136 | 1.458 | 2.284 | 5.410 | 8.597 | 11.738 | DNA | DNA | DNA | DNA | DNA | DNA |
| 137 | 1.575 | 1.864 | 4.821 | 7.994 | 11.133 | DNA | DNA | DNA | DNA | DNA | DNA |
| 138 | 0.932 | 1.937 | 5.254 | 8.479 | 11.635 | DNA | DNA | DNA | DNA | DNA | DNA |
| 139 | 0.825 | 2.100 | 5.482 | 8.715 | 11.874 | DNA | DNA | DNA | DNA | DNA | DNA |
| 140 | 1.532 | 1.649 | 4.613 | 7.796 | 10.939 | DNA | DNA | DNA | DNA | DNA | DNA |

APPENDIX G:
LOCATION DATA FROM FEASIBILITY TEST PHASE

Intentionally left blank.

| RD. | PREDICTED IMPACT LOCATION ON TARGET |  |  | Error Analysis |  | Error Analysis | PREDICTED | Error Analysis | EA | Array |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NO. | X | Y | Z | del Y | $\operatorname{del}$ Z | Offset Distance | Velocity | $\Delta$ Vel | $\Delta \mathrm{V}$ | Config |
| Consec. | (m) | (m) | (m) | m | m | m | $\mathrm{m} / \mathrm{s}$ | $\mathrm{m} / \mathrm{s}$ | \% |  |
| 1 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 2 | 1701.13 | 0.443 | 7.210 | -0.208 | -0.137 | 0.249 | 1442 | 23 | 2 | 2,4,5,6 |
| 3 | 1701.13 | 0.349 | 7.196 | -0.214 | -0.143 | 0.257 | 1467 | -10 | 1 | 2,4,5,6 |
| 4 | 1701.12 | 0.221 | 6.970 | -0.216 | -0.177 | 0.279 | 1476 | -19 | 1 | 2,4,5,6 |
| 5 | 1701.14 | 0.569 | 7.506 | -0.134 | -0.233 | 0.269 | 1108 | -29 | 3 | 2,4,5,6 |
| 6 | 1701.14 | 0.616 | 7.181 | -0.181 | -0.208 | 0.276 | 1068 | 6 | 1 | 2,4,5,6 |
| 7 | 1701.14 | 0.459 | 7.105 | -0.184 | -0.172 | 0.252 | 1104 | -25 | 2 | 2,4,5,6 |
| 8 | 1701.14 | 0.508 | 7.104 | -0.203 | -0.171 | 0.265 | 1105 | -36 | 3 | 2,4,5,6 |
| 9 | 1701.13 | 0.360 | 7.142 | - 0.245 | $\underline{-0.099}$ | 0.264 | 16018 | -32 | $\underline{2}$ | 2,4,5,6 |
| 10 | 1701.15 | 0.640 | 7.108 | -0.235 | ${ }_{-0.205}$ | 0.312 | 1571 | -17 | 1 | 2,4,5,6 |
| 11 | 1701.11 | 0.068 | 6.903 | -0.183 | -0.180 | 0.257 | 1505 | 40 | 3 | 2,4,5,6 |
| 12 | 1701.15 | 0.628 | 7.061 | -0.353 | -0.148 | 0.383 | 1615 | -49 | 3 | 2,4,5,6 |
| 13 | 1701.14 | 0.462 | 7.063 | -0.207 | -0.230 | 0.310 | 1016 | 24 | 2 | 2,4,5,6 |
| 14 | 1701.13 | 0.357 | 6.946 | -0.232 | -0.153 | 0.278 | 1041 | 7 | 1 | 2,4,5,6 |
| 15 | 1701.14 | 0.563 | 6.779 | -0.198 | -0.146 | 0.246 | 1020 | 24 | 2 | 2,4,5,6 |
| 16 | 1701.14 | 0.466 | 6.778 | -0.221 | -0.155 | 0.270 | 1035 | 12 | 1 | 2,4,5,6 |
| 17 | 1701.07 | -0.704 | 6.140 | 0.219 | -0.087 | 0.236 | 890 | -11 | 1 | 2,4,5,6 |
| 18 | 1701.05 | -0.940 | 5.707 | 0.225 | -0.014 | 0.225 | 919 | -30 | 3 | 2,4,5,6 |
| 19 | 1701.12 | 0.283 | 6.978 | 0.282 | -0.165 | 0.327 | 896 | -2 | 0 | 2,4,5,6 |
| 20 | 1701.09 | -0.226 | 7.426 | 0.191 | -0.043 | 0.196 | 892 | -10 | 1 | 2,4,5,6 |
| 21 | 1701.12 | 0.202 | 7.194 | 0.203 | -0.201 | 0.286 | 916 | -32 | 3 | 2,4,5,6 |
| 22 | 1701.11 | 0.046 | 7.663 | 0.199 | -0.160 | 0.255 | 909 | -21 | 2 | 2,4,5,6 |
| 23 | 1701.12 | 0.153 | 6.724 | 0.222 | -0.181 | 0.286 | 916 | -21 | 2 | 2,4,5,6 |
| 24 | 1701.10 | -0.172 | 6.853 | 0.227 | -0.120 | 0.257 | 862 | 25 | 3 | 2,4,5,6 |
| 25 | 1701.09 | -0.315 | 6.963 | 0.180 | -0.150 | 0.234 | 945 | -51 | 5 | 2,4,5,6 |
| 26 | 1701.11 | 0.030 | 6.785 | 0.225 | -0.192 | 0.296 | 917 | -18 | 2 | 2,4,5,6 |
| 27 | 1701.17 | 1.142 | 7.164 | 0.193 | -0.251 | 0.317 | 875 | 16 | 2 | 2,4,5,6 |
| 28 | 1701.17 | 1.087 | 7.210 | 0.198 | -0.217 | 0.294 | 894 | 0 | 0 | 2,4,5,6 |


| RD. | PREDICTED IMPACT LOCATION ON TARGET |  |  | Error Analysis |  | Error Analysis | PREDICTED | Error Analysis | EA | Array |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NO. | X | Y | Z | del Y | del Z | Offset Distance | Velocity | $\Delta \mathrm{Vel}$ | $\Delta \mathrm{V}$ | Config |
| Consec. | (m) | (m) | (m) | m | m | m | $\mathrm{m} / \mathrm{s}$ | $\mathrm{m} / \mathrm{s}$ | \% | Conb |
| 29 | 1701.15 | 0.758 | 7.999 | 0.207 | -0.266 | 0.337 | 904 | -15 | 2 | 2,4,5,6 |
| 30 | 1701.14 | 0.542 | 8.060 | 0.243 | -0.187 | 0.307 | 907 | -16 | 2 | 2,4,5,6 |
| 31 | 1701.13 | 0.333 | 7.938 | 0.172 | -0.225 | 0.284 | 931 | -42 | 4 | 2,4,5,6 |
| 32 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 33 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 34 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 35 | 1701.11 | 0.068 | 7.647 | 0.217 | -0.224 | 0.311 | 1178 | -33 | 3 | 2,4,5,6 |
| 36 | 1701.12 | 0.180 | 7.821 | 0.245 | -0.218 | 0.328 | 1133 | 6 | 1 | 2,4,5,6 |
| 37 | 1701.10 | -0.072 | 6.975 | 0.247 | -0.162 | 0.296 | 1156 | 8 | 1 | 2,4,5,6 |
| 38 | 1701.14 | 0.591 | 6.665 | 0.084 | 0.248 | 0.262 | 1137 | 20 | 2 | 2,4,5,6 |
| 39 | 1701.11 | -0.025 | 6.492 | 0.210 | 0.781 | 0.809 | 1191 | 9 | 1 | 2,4,5,6 |
| 40 | 1701.12 | 0.260 | 6.502 | 0.195 | -0.169 | 0.258 | 1129 | 23 | 2 | 2,4,5,6 |
| 41 | 1701.13 | 0.418 | 7.076 | 0.207 | -0.173 | 0.270 | 1114 | 43 | 4 | 2,4,5,6 |
| 42 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 43 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 44 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 45 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 46 | DNA | DNA | DNA |  |  |  |  |  | - | - ... - |
| 47 | 1701.12 | -0.124 | 6.979 | -0.039 | -0.112 | 0.118 | 1300 | 11 | 1 | 2,4,5,6 |
| 48 | 1701.12 | -0.145 | 7.197 | -0.028 | -0.140 | 0.142 | 1295 | 19 | 1 | 2,4,5,6 |
| 49 | 1701.12 | -0.074 | 6.792 | -0.059 | -0.135 | 0.147 | 1415 | -102 | 7 | 2,4,5,6 |
| 50 | 1701.12 | 0.269 | 6.931 | -0.012 | -0.114 | 0.115 | 1291 | 14 | 1 | 2,4,5,6 |
| 51 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 52 | 1701.12 | 0.319 | 6.455 | 0.008 | -0.158 | 0.159 | 857 | 20 | 2 | 2,4,5,6 |
| 53 | 1701.12 | -0.043 | 6.546 | 0.020 | -0.139 | 0.140 | 875 | 10 | 1 | -2,4,5,6 |
| 54 | 1701.12 | -0.266 | 7.124 | -0.007 | -0.177 | 0.178 | 847 | 22 | 3 | 2,4,5,6 |
| 55 | 1701.12 | 0.314 | 7.309 | 0.003 | -0.172 | 0.172 | 874 | 13 | 1 | 2,4,5,6 |
| 56 | DNA | DNA | DNA |  |  |  |  |  |  |  |


| RD. | PREDICTED IMPACT LOCATION ON TARGET |  |  | Error Analysis |  | Error Analysis | PREDICTED | Error Analysis | EA | Array |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NO. | X | Y | $\underline{Z}$ | del Y | $\operatorname{del}$ Z | Offset Distance | Velocity | $\Delta$ Vel | $\Delta \mathrm{V}$ | Config |
| Consec. | (m) | (m) | (m) | m | m | m | $\mathrm{m} / \mathrm{s}$ | $\mathrm{m} / \mathrm{s}$ | \% |  |
| 57 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 58 | 1701.12 | -0.052 | 7.034 | -0.061 | -0.0197 | 0.114 | 1343 | -2 | 0 | 2,4,5,6 |
| 59 | 1701.12 | -0.005 | 7.038 | -0.148 | -0.081 | 0.169 | 1352 | -16 | 1 | 2,4,5,6 |
| 60 | 1701.12 | 0.080 | 6.675 | -0.093 | -0.108 | 0.142 | 1270 | 68 | 5 | 2,4,5,6 |
| 61 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 62 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 63 | 1701.12 | 0.390 | 6.841 | -0.143 | -0.084 | 0.166 | 836 | 16 | 2 | 2,4,5,6 |
| 64 | 1701.12 | 0.466 | 7.135 | -0.129 | -0.138 | 0.189 | 859 | 13 | 2 | 2,4,5,6 |
| 65 | 1701.11 | -0.548 | 6.856 | -0.135 | -0.159 | 0.209 | 844 | 3 | 0 | 2,4,5,6 |
| 66 | DNA | DNA | DNA |  |  | -- |  |  | - | - |
| 67 | DNA | DNA | DNA |  |  |  | ----- | - --------- |  |  |
| 68 | DNA | DNA | DNA |  |  | -- |  | - | - | - --- |
| 69 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 70 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 71 | 1701.13 | 0.945 | 7.670 | -0.098 | -0.033 | 0.103 | 908 | 1 | 0 | 2,4,5,6 |
| 72 | 1701.13 | 0.996 | 7.634 | -0.119 | -0.017 | 0.120 | 942 | -6 | 1 | 2,4,5,6 |
| 73 | 1701.12 | 0.169 | 7.410 | -0.112 | -0.523 | 0.535 | 898 | 63 | 7 | 2,4,5,6 |
| 74 | DNA | DNA | DNA |  |  |  |  |  | - |  |
| 75 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 76 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 77 | 1701.13 | 1.222 | 6.130 |  |  |  | 838 | 77 | 9 | 2,4,5,6 |
| 78 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 79 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 80 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 81 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 82 | 1701.12 | -0.110 | 6.657 | -0.093 | -0.070 | 0.117 | 620 | 2 | 0 | 2,4,5,6 |
| 83 | 1701.11 | -0.857 | 6.667 | -0.076 | -0.060 | 0.097 | 624 | -2 | 0 | 2,4,5,6 |
| 84 | 1701.12 | -0.288 | 6.844 | -0.105 | -0.087 | 0.136 | 614 | 6 | 1 | 2,4,5,6 |


| RD. | PREDICTED IMPACT LOCATION ON TARGET |  |  | Error Analysis |  | Error Analysis | PREDICTED | Error Analysis | EA | Array |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NO. | X | Y | Z | del Y | del Z | Offset Distance | Velocity | $\Delta \mathrm{Vel}$ | $\Delta \mathrm{V}$ | Config |
| Consec. | (m) | (m) | (m) | m | m | m | $\mathrm{m} / \mathrm{s}$ | $\mathrm{m} / \mathrm{s}$ | \% |  |
| 85 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 86 | 1701.12 | -0.361 | 7.171 | -0.082 | -0.074 | 0.111 | 618 | 6 | 1 | 2,4,5,6 |
| 87 | 1701.13 | 1.239 | 7.857 | -0.102 | -0.060 | 0.118 | 613 | 6 | 1 | 2,4,5,6 |
| 88 | 1701.12 | -0.259 | 7.105 | -0.084 | -0.078 | 0.115 | 617 | 2 | 0 | 2,4,5,6 |
| 89 | 1701.11 | -1.139 | 6.860 | -0.074 | -0.083 | 0.112 | 623 | 0 | 0 | 2,4,5,6 |
| 90 | 1701.13 | 1.045 | 7.399 | -0.088 | -0.052 | 0.102 | 626 | 0 | 0 | 2,4,5,6 |
| 91 | 1701.11 | -0.454 | 6.982 | -0.089 | -0.065 | 0.111 | 626 | 3 | 0 | 2,4,5,6 |
| 92 | 1701.12 | -0.272 | 6.409 | -0.101 | -0.072 | 0.124 | 617 | 4 | 1 | 2,4,5,6 |
| 93 | 1701.118 | -0.095 | 5.457 |  |  |  | 618 | 2 | 0 | 2,4,5,6 |
| 94 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 95 | 1701.12 | 0.626 | 7.867 | 0.141 | -0.206 | 0.249 | 729 | -2 | 0 | 2,4,5,6 |
| 96 | 1701.12 | 0.349 | 5.865 |  |  |  | 617 | 26 | 4 | 2,4,5,6 |
| 97 | 1701.12 | -0.554 | 7.556 | 0.151 | -0.115 | 0.190 | 747 | -2 | 0 | 2,4,5,6 |
| 98 | 1701.12 | 0.163 | 6.291 | 0.134 | -0.160 | 0.209 | 663 | 19 | 3 | 2,4,5,6 |
| 99 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 100 | 1701.12 | -0.855 | 7.032 | 0.072 | 0.039 | 0.082 | 1337 | -143 | 11 | 2,4,5,6 |
| 101 | 1701.12 | -0.441 | 6.939 | 0.048 | -0.048 | 0.068 | 1146 | 50 | 4 | 2,4,5,6 |
| 102 | 1701.12 | -0.469 | 6.831 | 0.096 | -0.040 | 0.104 | 1214 | -16 | 1 | 2,4,5,6 |
| 103 | 1701.12 | -0.264 | 6.677 | 0.121 | $-0.056$ | 0.133 | 1190 | 7 | 1 | 2,4,5,6 |
| 104 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 105 | 1701.12 | -1.156 | 6.853 | 0.133 | -0.042 | 0.140 | 728 | -11 | 2 | 2,4,5,6 |
| 106 | 1701.12 | -0.362 | 6.462 | 0.119 | -0.101 | 0.156 | 703 | 3 | 0 | 2,4,5,6 |
| 107 | 1701.12 | 1.305 | 7.257 | 0.152 | -0.216 | 0.265 | 712 | 2 | 0 | 2,4,5,6 |
| 108 | 1701.12 | 0.583 | 7.179 | 0.124 | -0.178 | 0.217 | 711 | -2 | 0 | 2,4,5,6 |
| 109 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 110 | 1701.12 | -0.671 | 7.077 | 0.058 | -0.016 | 0.060 | 1085 | -4 | 0 | 2,4,5,6 |
| 111 | 1701.12 | 0.742 | 7.638 | 0.115 | -0.117 | 0.164 | 1059 | 2 | 0 | 2,4,5,6 |
| 112 | 1701.12 | -0.323 | 6.538 | 0.100 | -0.007 | 0.101 | 1080 | -12 | 1 | 2,4,5,6 |


|  | RrBictrod | Tloc | Ontageri | ${ }_{\text {Lerer }}^{\text {deir }}$ | dinis |  | REDICTED | $\frac{\text { cract }}{\text { analys }}$ | ${ }_{\text {EV }}^{\text {EV }}$ | ${ }_{\text {Aray }}^{\text {Comif }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Comece | ${ }_{\text {min }}^{\text {m }}$ | $\frac{(m)}{\substack{(m) \\ 0 \times 29}}$ | ${ }_{\substack{(m) 9 \\ 6898}}^{(2)}$ | $\xrightarrow{\substack{\text { m } \\ 0.91}}$ | ${ }^{\text {．}} 103$ | ${ }_{\text {m }}^{\text {m }}$ | ${ }_{\text {m／s }}^{\substack{\text { mas }}}$ |  | ${ }_{3}$ | 24.55 |
| 113 <br> 114 <br> 1 <br> 1 |  | Dina |  |  |  |  |  |  |  |  |
| ${ }^{115}$ | DNA | dNA | DNA |  |  |  |  |  |  |  |
| ${ }^{16}$ | dNa | DNA | DNa |  |  |  |  | 1 | $\bigcirc$ | ${ }^{24,56}$ |
|  | ${ }^{10012}$ | ${ }^{-1.060}$ | ation | ${ }_{\text {a }}^{0.130}$ | $\frac{0}{0.100}$ | 0.028 | ${ }_{40}^{40}$ |  |  |  |
| ${ }_{119}^{19}$ | ${ }^{\text {iola }}$ | ${ }_{0}^{0.889}$ | ${ }_{80 \mathrm{~m} 7}$ | 0201 | ${ }^{\text {douch }}$ | 0202 | ${ }_{6}^{67}$ | $\bigcirc$ | $\bigcirc$ | 2.45 |
|  | DNA | DNA |  |  |  |  |  |  |  |  |
|  |  | －1871 | ${ }_{5}^{5,57}$ | ${ }^{1028}$ | ${ }^{1389}$ | 0.46 | ${ }^{94}$ | ${ }^{12}$ | － | 2546 |
| 退 |  | －080 | ${ }_{229} 229$ |  |  | 020 | ${ }_{4} 6$ | 4 | 1 |  |
| ${ }^{124}$ | ${ }^{100.12}$ | 1.07 | ${ }^{7595}$ | ${ }^{0.320}$ | ${ }^{\text {a }}$ O2022 | ${ }^{0.302}$ |  | $\frac{6}{2}$ | $\stackrel{1}{0}$ | － |
|  |  | $\stackrel{\text { On4 }}{\text { On4 }}$ |  |  |  |  |  |  |  |  |
| $\frac{126}{127}$ | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 咢碗 | ond | ${ }^{\text {DNA }}$ | PNA |  |  |  |  |  |  |  |
| ${ }^{120}$ | DNA | －DNA | dina |  |  |  |  |  |  |  |
| － | DNA | DNA | ${ }_{\text {dNA }}^{\text {DNA }}$ |  |  |  |  |  |  |  |
| ${ }^{133}$ | DNA | DNA |  |  |  |  |  |  |  |  |
| ${ }^{134}$ | DNa | DNA | Din |  |  |  |  |  |  |  |
| ${ }^{106}$ | ${ }_{\text {DNA }}^{\text {DNA }}$ | DNA | dNa |  |  |  |  |  |  |  |
| ${ }_{137}$ | DNA | DNA | dNa |  |  |  |  |  |  |  |
| ${ }^{138}$ | DNA | DNA | dNA |  |  |  |  |  |  |  |
| ${ }_{13}{ }^{\text {1 }}$ | DNA | ${ }^{\text {DNA }}$ | ${ }_{\text {DNA }}$ |  |  |  |  |  |  |  |


| RD. | PREDICTED IMPACT LOCATION ON TARGET |  |  | Error Analysis |  | Error Analysis | PREDICTED | Error Analysis | EA | Array |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NO. | X | Y | Z | del Y | $\operatorname{del}$ Z | Offset Distance | Velocity | $\Delta$ Vel | $\Delta \mathrm{V}$ | Config |
| Consec. | (m) | (m) | (m) | m | m | m | $\mathrm{m} / \mathrm{s}$ | $\mathrm{m} / \mathrm{s}$ | \% |  |
| 141 | DNA | DNA | DNA |  |  |  |  |  |  | ... .-..... |
| 142 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 143 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 144 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 145 | 1701.12 | -1.059 | 8.778 | 1.746 | -1.387 | 2.230 | 791 | -13 | 2 | 2,4,5,6 |
| 146 | 1701.121 | 0.549 | 7.510 |  |  |  | 799 | 6 | 1 | 2,4,5,6 |
| 147 | 1701.132 | 3.784 | 8.746 |  |  |  | 802 | 22 | 3 | 2,4,5,6 |
| 148 | 1701.13 | 2.216 | 4.874 | -3.079 | 3.067 | 4.345 | 690 | 117 | 17 | 2,4,5,6 |
| 149 | DNA | DNA | DNA |  |  | .... | -... | ... $\cdot$. . |  |  |
| 150 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 151 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 152 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 153 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 154 | 1701.13 | 0.344 | 7.516 | 0.023 | -0.079 | 0.083 | 1004 | 25 | 3 | 2,4,5,6 |
| 155 | 1701.14 | 0.503 | 7.636 | 0.064 | -0.089 | 0.109 | 1011 | 21 | 2 | 2,4,5,6 |
| 156 | 1701.15 | 0.579 | 7.466 | 0.008 | -0.069 | 0.069 | 1013 | 21 | 2 | 2,4,5,6 |
| 157 | 1701.12 | 0.079 | 7.516 | 0.058 | -0.079 | 0.098 | 1038 | -13 | 1 | 2,4,5,6 |
| 158 | 1701.11 | 0.020 | 7.471 | -0.013 | -0.124 | 0.124 | 1028 | 5 | 0 | 2,4,5,6 |
| 159 | 1701.11 | 0.008 | 7.236 | 0.039 | -0.099 | 0.107 | 1004 | 26 | 3 | 2,4,5,6 |
| 160 | 1701.11 | 0.044 | 7.577 | 0.083 | -0.100 | 0.130 | 1470 | 58 | 4 | 2,4,5,6 |
| 161 | 1701.11 | 0.030 | 7.351 | 0.027 | -0.104 | 0.107 | 1494 | 27 | 2 | 2,4,5,6 |
| 162 | 1701.12 | 0.204 | 7.525 | 0.093 | -0.118 | 0.150 | 1459 | 68 | 5 | 2,4,5,6 |
| 163 | 1701.11 | 0.050 | 7.658 | 0.157 | -0.141 | 0.211 | 1526 | 0 | 0 | 2,4,5,6 |
| 164 | 1701.12 | 0.171 | 7.341 | 0.176 | -0.124 | 0.215 | 1588 | -69 | 4 | 2,4,5,6 |
| 165 | 1701.12 | 0.145 | 7.431 | 0.102 | -0.154 | 0.184 | 1546 | -27 | 2 | 2,4,5,6 |
| 166 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 167 | 1701.10 | -0.114 | 7.622 | 0.121 | -0.015 | 0.122 | 1158 | 30 | 3 | 2,4,5,6 |
| 168 | 1701.16 | 0.335 | 6.722 | 0.132 | -0.335 | 0.360 | 1138 | 102 | 9 | 2,4,5,6 |


| RD. | PREDICTED IMPACT LOCATION ON TARGET |  |  | Error Analysis |  | Error Analysis | PREDICTED | Error Analysis | EA | Array |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NO. | - | Y | Z | del $Y$ | del Z | Offset Distance | Velocity | $\Delta$ Vel | $\Delta \mathrm{V}$ | Config |
| Consec. | (m) | (m) | (m) | m | m | m | $\mathrm{m} / \mathrm{s}$ | $\mathrm{m} / \mathrm{s}$ | \% |  |
| 169 | 1701.12 | 0.136 | 7.544 | 0.111 | -0.017 | 0.112 | 1136 | 7 | 1 | 2,4,5,6 |
| 170 | 1701.11 | 0.059 | 7.212 | 0.128 | -0.015 | 0.129 | 1221 | 3 | 0 | 2,4,5,6 |
| 171 | 1701.09 | -0.412 | 6.876 | 0.159 | 0.041 | 0.164 | 1230 | -1 | 0 | 2,4,5,6 |
| 172 | 1701.17 | 1.024 | 7.164 | 0.153 | -0.057 | 0.163 | 1195 | 11 | 1 | 2,4,5,6 |
| 173 | 1701.15 | 0.632 | 7.257 | 0.065 | -0.060 | 0.088 | 1188 | 11 | 1 | 2,4,5,6 |
| 174 | 1701.11 | -0.081 | 7.433 | 0.128 | -0.016 | 0.129 | 1168 | -1 | 0 | 2,4,5,6 |
| 175 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 176 | DNA | DNA | DNA |  |  | --7 | - - . - - |  |  | - |
| 177 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 178 | DNA | DNA | DNA |  |  |  | - --- | -- - - - |  |  |
| 179 | DNA | DNA | DNA |  |  |  |  |  |  | - |
| 180 | DNA | DNA | DNA |  |  |  | $\cdots$ |  |  | .-.--- |
| 181 | DNA | DNA | DNA |  |  |  |  | - |  |  |
| 182 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 183 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 184 | DNA | DNA | DNA |  |  |  |  |  |  |  |
| 185 | 1701.004 | -1.265 | 7.325 | 0.092 | 0.002 | 0.092 | 901 | -16 | 2 | 2,4,5,6 |
| 186 | 1701.097 | -0.222 | 7.193 | 0.079 | -0.056 | 0.096 | 894 | -4 | 0 | 2,4,5,6 |
| 187 | 1701.076 | -0.572 | 7.658 | 0.099 | -0.031 | 0.103 | 892 | -3 | 0 | 2,4,5,6 |
| 188 | 1701.04 | -0.945 | 7.412 | 0.092 | -0.005 | 0.092 | 892 | -6 | 1 | 2,4,5,6 |
| 189 | 1701.14 | 0.563 | 7.488 | 0.094 | -0.131 | 0.161 | 879 | 9 | 1 | 2,4,5,6 |
| 190 | 1701.09 | -0.377 | 7.223 | 0.144 | -0.006 | 0.144 | 873 | 14 | 2 | 2,4,5,6 |
| 191 | 1701.07 | -0.637 | 7.485 | 0.174 | 0.032 | 0.177 | 883 | 2 | 0 | 2,4,5,6 |
| 192 | 1701.06 | -0.838 | 7.304 | 0.115 | 0.023 | 0.118 | 884 | -1 | 0 | 2,4,5,6 |

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APPENDIX H:
ANGLE CORRECTION TECHNIQUE

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A method to theoretically correct the velocity is to employ a system of a family of hyperbolas, and solve for the speed. This is an iterative method, since more than one of the variables are unknown. Referring to Figure $\mathbf{H}-1$, the following is defined:
where
$\mathrm{D}_{\mathrm{ST}}=$ Distance between mic 1 and P1.
$\mathrm{h}=$ Elevation of projectile above ground plane.
M $=$ Mach Number.
$\beta=$ Azimuth Deviation.
$y_{f}=$ Equation for Shock Front.
$\mathrm{y}_{\mathrm{h}}=$ Equation for lead Hyperbola.
$y_{h 2}=$ Equation for succeeding Hyperbola.
$y_{s}=$ Equation for line going through mic 1 and mic 2.
c $\quad=$ true distance for correct velocity calculation.


Figure H-1. Hyperbola created by cone intersecting ground plane.

First one must consider that the conic section that intersects a plane that is parallel to the conix axis will form a hyperbola of the following form:

$$
\begin{equation*}
y_{h}=b \sqrt{\frac{x^{2}}{a}-1} \tag{9}
\end{equation*}
$$

The angle of the shock cone is $\Theta=\sin ^{-1} 1 / \mathrm{M}$. The slope of the shock cone can be written as

$$
\begin{equation*}
\lim _{x \rightarrow \infty} \frac{d y_{h}}{d x}=m_{h} \tag{30}
\end{equation*}
$$

Taking the derivative of the hyperbolic equation yields

$$
\begin{aligned}
\frac{d y_{h}}{d_{x}} & =\frac{d\left(b U^{1 / 2}\right)}{d x} \\
U & =\frac{x^{2}}{a}-1 \\
d y_{h} & =\frac{b}{\sqrt{a-\frac{a^{2}}{x^{2}}}}
\end{aligned}
$$

$$
\begin{equation*}
\lim _{x \rightarrow \infty} \frac{d y_{h}}{d x}=\lim _{x \rightarrow \infty} \frac{b}{\sqrt{a-\frac{a^{2}}{x^{2}}}}=\frac{b}{\sqrt{a}} \tag{31}
\end{equation*}
$$

The distance from the origin to where the hyperbola intersects the x -axis is where $\mathrm{x}^{2}=\mathrm{a}$. This is shown as

$$
\begin{align*}
y & =b \frac{\sqrt{x^{2}}}{a}-1 \\
\frac{x^{2}}{a}-1 & =0 \\
\frac{x^{2}}{a} & =1 \\
x^{2} & =a \tag{32}
\end{align*}
$$

This is the point where the shock cone generated by the projectile intersects the microphone, as depicted in Figure $\mathrm{H}-2$.


Figure H-2. Shock cone geometry.

Using Figure $\mathrm{H}-2$, we are able to say that

$$
\begin{equation*}
\frac{\sqrt{a}}{h}=\sqrt{M^{2}-1} \tag{33}
\end{equation*}
$$

This implies a solution for the magnitude of a plus solving for d ,

$$
\begin{align*}
a & =h^{2}\left(M^{2}-1\right) \\
\frac{b}{\sqrt{a}} & =\sqrt{M^{2}-1} \\
b & =\sqrt{a\left(M^{2}-1\right)}=h\left(M^{2}-1\right) \tag{34}
\end{align*}
$$

By knowing the length of D , since it intersects the trajectory at P 1 , we know the y value at mic 1 .

$$
\begin{equation*}
\mathrm{y}_{1}=\mathrm{D}_{\mathrm{ST}} \sin \beta . \tag{35}
\end{equation*}
$$

The value of $x$ also needs to be solved and can be done by substituting the result of $y$ into the solution for x of the intersecting hyperbolic equation.

Now the point of mic 1 is known in Cartesian coordinates. Substituting $\cot \beta$ for $m_{f}$ into the equation that describes the line of mic 1 and mic 2 , we can define the intercept, $\mathrm{f}_{2}$.

$$
\begin{align*}
& y_{h}=b \sqrt{\frac{x_{h}^{2}}{a}-1} \\
& x_{h}^{2}=a\left[\left(\frac{y_{h}}{b}\right)^{2}+1\right] \\
& x_{1}=\sqrt{a\left[\left(\frac{y_{h}}{b}\right)^{2}+1\right]}  \tag{36}\\
& f=y_{s}-x_{s} \cot \beta \tag{37}
\end{align*}
$$

or

$$
\begin{align*}
\mathrm{f} & =\mathrm{y}_{1}-\mathrm{x}_{1} \beta \\
\mathrm{y}_{\mathrm{s}} & =\mathrm{y}_{1}+\left(\mathrm{x}_{\mathrm{s}}-\mathrm{x}_{\mathrm{s}}\right) \cot \beta . \tag{38}
\end{align*}
$$

To find the Cartesian values for mic 2, we repeat the substitution, but for the second hyperbola.

$$
\begin{align*}
& \mathrm{y}_{2}=\left(\mathrm{D}_{\mathrm{ST}+1 \mathrm{~m}) \sin \beta}\right. \\
& \mathrm{y}_{2}=\mathrm{y}_{1}+\left(\mathrm{x}_{2}-\mathrm{x}_{1}\right) \cot \beta \\
& \mathrm{x}_{2}=\left(\mathrm{Y}_{2}-\mathrm{Y}_{1}\right) \tan \beta+\mathrm{x}_{1} . \tag{39}
\end{align*}
$$

Knowing the values of $x_{2}$ and $y_{2}$ is the key to finding $c$. We write the equation for the hyperbola intersecting mic 2 at $\mathrm{Dt}=0$. This is identical to the first hyperbola except it is displaced along the x -axis by value $c$. Transforming $x^{\prime}=x+c$,

$$
\begin{equation*}
\mathrm{y}_{\mathrm{h} 2}=\mathrm{b} \sqrt{\frac{\left(\mathrm{x}_{\mathrm{h} 2}-\mathrm{c}\right)^{2}}{\mathrm{a}}-1} \tag{0}
\end{equation*}
$$

Solving the equation for c ,

$$
\begin{align*}
y_{2} & =(D+1 m) \sin \beta \\
x_{2} & =\left(y_{2}-y_{1}\right) \tan \beta+x_{1} \\
c & =x_{2} \sqrt{[ }\left[\left(\frac{y_{2}}{b}\right)^{2}+1\right] \tag{41}
\end{align*}
$$

With c determined, the corrected velocity should be calculated as

$$
\begin{equation*}
\mathrm{V}=\frac{\mathrm{c}}{\mathrm{~T}_{2}} \tag{42}
\end{equation*}
$$

For this method to work, an initial guess must be made for the Mach number. On the first guess, we assume c is 1 m . For an increase in azimuth deviation, a, the true velocity length, c , is decreasing. As well, the further to the left or right of the centerline, c becomes even smaller. With any azimuth deviation, the predicted velocity will always be higher. The resulting c , based on the higher Mach number, will be calculated to slightly less than reality. The resultant updated velocity will be more accurate.

It can be shown geometrically that an iterative process of updating the velocity and Mach number and calculating a new value for $\mathbf{c}$ will eventually converge to the true velocity rapidly. For the purpose of the RDS, one, maybe two, iterations would be all that was necessary. The true test of this method lay in processing the data obtained from the data collection test.

Unfortunately, the method did not work. It was determined that the fault did not lay in the theory but in the assumptions. It was assumed that the azimuth deviation would be known. The method of finding the azimuth deviation was not accurate. The solution for the true velocity is strongly related to that angle. As a result, this method could not be used.

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## APPENDIX I:

LOCATION DATA FROM DATA COLLECTION TEST

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| RD. | PREDICTED IMPACT LOCATION ON TARGET |  |  | Error Analysis |  | Error Analysis | PREDICTED | Error Analysis | EA | Array |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NO. | X | Y | Z | del X | del Z | miss distance | Velocity | del Vel | del V | Config |
| Consec. | (m) | (m) | (m) | m | m | m | $\mathrm{m} / \mathrm{s}$ | $\mathrm{m} / \mathrm{s}$ | \% |  |
| 1 | ND | ND | ND |  |  |  |  |  |  |  |
| 2 | ND | ND | ND |  |  | - |  |  |  |  |
| 3 | ND | ND | ND |  |  |  |  |  |  |  |
| 4 | ND | ND | ND |  |  |  |  |  |  |  |
| 5 | 1700.948 | -0.420 | 4.344 | 0.197 | -0.053 | 0.204 | 580 | -14. | 2 | 1,2,3,4 |
| 6 | 1700.948 | -0.230 | 4.575 | 0.049 | -0.401 | 0.404 | 595 | -8. | 1 | 1,2,3,4 |
| 7 | 1700.948 | -0.405 | 4.369 | 0.332 | 0.209 | 0.393 | 599 | -9. | 2 | 1,2,3,4 |
| 8 | 1700.948 | -0.363 | 4.246 | 0.190 | -0.086 | 0.208 | 582 | -10. | 2 | 1,2,3,4 |
| 9 | 1700.948 | -0.223 | 4.361 | 0.154 | -0.146 | 0.212 | 583 | -8. | 1 | 1,2,3,4 |
| 10 | 1700.948 | -0.265 | 4.325 | 0.219 | -0.050 | 0.224 | 587 | -9. | 2 | 1,2,3,4 |
| 11 | 1700.948 | -0.312 | 4.283 | 0.199 | -0.100 | 0.223 | 602 | -10. | 2 | 1,2,3,4 |
| 12 | 1700.948 | -0.590 | 4.236 | 0.181 | -0.075 | 0.196 | 604 | -13. | 2 | 1,2,3,4 |
| 13 | 1700.948 | -0.803 | 3.930 | 0.193 | -0.048 | 0.199 | 552 | -18. | 3 | 1,2,3,4 |
| 14 | 1700.948 | -0.598 | 4.346 | 0.180 | -0.064 | 0.192 | 608 | -16. | 3 | 1,2,3,4 |
| 15 | ND | ND | ND |  |  |  |  |  |  |  |
| 16 | ND | ND | ND |  |  |  |  |  |  |  |
| 17 | ND | ND | ND |  |  |  |  |  |  |  |
| 18 | ND | ND | ND |  |  | -- | $\cdots$ | - . . . |  |  |
| 19 | ND | ND | ND |  |  |  |  |  |  |  |
| 20 | ND | ND | ND |  |  |  |  |  |  |  |
| 21 | ND | ND | ND |  |  |  | 346 | -18. | 5 | 1,2,3,4 |
| 22 | 1700.948 | -0.003 | 4.112 | 0.054 | 0.232 | 0.238 | 388 | -13. | 3 | 1,2,3,4 |
| 23 | ND | ND | ND |  |  |  | 343 | -19. | 6 | 1,2,3,4 |
| 24 | ND | ND | ND |  |  |  |  |  |  |  |
| 25 | 1700.948 | -0.300 | 3.721 | 0.032 | 0.128 | 0.132 | 397 | -15. | 4 | 1,2,3,4 |
| 26 | ND | ND | ND |  |  |  | 346 | -15. | 4 | 1,2,3,4 |
| 27 | ND | ND | ND |  |  |  |  |  |  |  |
| 28 | ND | ND | ND |  |  |  |  |  |  | , |


| RD. | PREDICTED IMPACT LOCATION ON TARGET |  |  | Error Analysis |  | Error Analysis | PREDICTED | Error Analysis | EA | Array |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NO. | X | $Y$ | Z | del X | del Z | miss distance | Velocity | del Vel | del V | Config |
| Consec. | (m) | (m) | (m) | m | m | m | $\mathrm{m} / \mathrm{s}$ | $\mathrm{m} / \mathrm{s}$ | \% |  |
| 29 | ND | ND | ND |  |  |  | $\cdots$ | - |  |  |
| 30 | ND | ND | ND |  |  |  |  | --........... |  |  |
| 31 | ND | ND | ND |  |  |  |  |  |  |  |
| 32 | ND | ND | ND |  |  |  |  |  |  |  |
| 33 | ND | ND | ND |  |  |  |  |  |  |  |
| 34 | ND | ND | ND |  |  |  |  |  |  |  |
| 35 | ND | ND | ND |  |  |  |  |  |  |  |
| 36 | 1700.948 | 0.135 | 3.278 | 0.193 | -0.208 | 0.283 | 650 | 6. | 1 | 1,2,3,4 |
| 37 | 1700.948 | 0.936 | 8.308 |  |  |  | 579 | 3. | 1 | 1,2,3,4 |
| 38 | 1700.948 | -2.708 | 3.332 |  |  |  | 642 | -35. | 5 | 1,2,3,4 |
| 39 | 1700.948 | -0.285 | 4.666 | 0.205 | -0.085 | 0.222 | 677 | -12. | 2 | 1,2,3,4 |
| 40 | 1700.948 | -0.135 | 4.468 | 0.210 | -0.144 | 0.254 | 636 | 15. | 2 | 1,2,3,4 |
| 41 | 1700.948 | -1.073 | 7.683 |  |  |  | 563 | 5. | 1 | 1,2,3,4 |
| 42 | 1700.948 | 3.068 | 6.288 |  |  |  | 560 | 24. | 4 | 1,2,3,4 |
| 43 | 1700.948 | -1.687 | 3.903 | 0.136 | -0.039 | 0.142 | 650 | -10. | 1 | 1,2,3,4 |
| 44 | 1700.948 | 0.041 | 4.531 | 0.222 | -0.156 | 0.271 | 670 | 13. | 2 | 1,2,3,4 |
| 45 | ND | ND | ND |  |  |  |  |  |  |  |
| 46 | 1700.783 | 0.011 | 4.096 | 0.142 | 0.055 | 0.152 | 435 | -13. | 3 | 1,2,3,4 |
| 47 | 1700.783 | -0.276 | 4.684 | 0.045 | -0.127 | 0.134 | 448 | 0. | 0 | 1,2,3,4 |
| 48 | 1700.783 | -0.243 | 4.587 | 0.043 | 0.011 | 0.044 | 465 | -8. | 2 | 1,2,3,4 |
| 49 | 1700.783 | -0.093 | 4.520 | 0.093 | -0.111 | 0.145 | 425 | 6. | 1 | 1,2,3,4 |
| 50 | 1700.783 | -0.600 | 4.534 | 0.034 | -0.047 | 0.058 | 451 | -6. | 1 | 1,2,3,4 |
| 51 | 1700.783 | -0.551 | 4.496 | 0.025 | -0.136 | 0.138 | 460 | 3. | 1 | 1,2,3,4 |
| 52 | ND | ND | ND |  |  |  |  |  |  |  |
| 53 | ND | ND | ND |  |  |  |  |  |  |  |
| 54 | ND | ND | ND |  |  |  |  |  |  |  |
| 55 | ND | ND | ND |  |  |  |  |  |  |  |
| 56 | 1700.783 | 0.794 | 4.323 | -0.007 | -0.147 | 0.147 | 449 | 2. | 0 | 1,2,3,4 |


| RD. | PREDICTED IMPACT LOCATION ON TARGET |  |  | Error Analysis |  | Error Analysis | PREDICTED | Error Analysis | EA | Array |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NO. | X | Y | Z | del X | del Z | miss distance | Velocity | del Vel | del V | Config |
| Consec. | (m) | (m) | (m) | m | m | m | $\mathrm{m} / \mathrm{s}$ | $\mathrm{m} / \mathrm{s}$ | \% |  |
| 57 | 1700.783 | 0.992 | 3.818 | 0.030 | -0.033 | 0.044 | 453 | -15. | 3 | 1,2,3,4 |
| 58 | 1700.783 | -1.227 | 4.668 | -0.098 | 0.026 | 0.101 | 504 | -13. | 2 | $1,2,3,4$ <br> $1,2,3,4$ |
| 59 | 1700.783 | 1.073 | 4.915 | -0.019 | -0.002 | 0.019 | 498 | -8. |  |  |
| 60 | 1700.783 | 0.522 | 5.185 | 0.044 | -0.051 | 0.067 | 500 | -9. | 2 |  |
| 61 | ND | ND | ND |  |  |  |  |  |  |  |
| 62 | ND | ND | ND |  |  |  |  | 3. | 1 | 1,2,3,4 |
| 63 | 1700.783 | -0.264 | 4.213 | 0.202 | -0.101 | 0.226 | 574 | -14. | 2 | 1,2,3,4 |
| 64 | 1700.783 | -0.341 | 4.225 | 0.210 | $\bigcirc$ | $\frac{0}{0.266}$ | 555 | 8. | 2 | 1,2,3,4 |
| 65 | 1700.783 | 0.104 | 4.094 | 0.236 | -0.121 | 0.213 | 544 | 9. | 2 | 1,2,3,4 |
| 66 | 1700.783 | -0.378 | 4.208 | 0.202 | -0.057 | 0.231 | 550 | 8. | 1 | 1,2,3,4 |
| 67 | 1700.783 | -0.618 | 4.180 | 0.224 0.211 | -0.108 | 0.237 | 560 | 10. | 2 | 1,2,3,4 |
| 68 | 1700.783 | -0.516 | 4.388 | 0.211 |  |  |  |  |  |  |
| 69 | ND | ND | ND |  |  | - |  |  |  |  |
| 70 | ND | ND | ND |  |  | - |  |  |  |  |
| 71 | ND | ND | ND |  |  | - |  |  |  |  |
| 72 | ND | ND | ND |  |  | ---3-3-3 | .-- - - |  |  |  |
| 73 | ND | ND | ND |  |  | ---7- |  |  |  |  |
| 74 | ND | ND | ND |  |  |  |  |  |  |  |
| 75 | ND | ND | ND |  |  | 0.117 | 1085 | -39. | 4 | 1,2,3,4 |
| 76 | 1700.823 | 0.260 | 4.156 | -0.096 | -0.067 | 0.105 | 877 | -39. | 4 | 1,2,3,4 |
| 77 | 1700.823 | 0.873 | 4.588 | -0.103 | -0.021 | 0.122 | 1097 | -51. | 5 | 1,2,3,4 |
| 78 | 1700.823 | 0.140 | 3.653 | -0.115 | -0.011 | 0.081 | 877 | -37. | 4 | 1,2,3,4 |
| 79 | 1700.823 | 1.177 | 3.871 | $\underline{-0.084}$ | -0.060 | 0.104 | 1103 | -57. | 5 | 1,2,3,4 |
| 80 | 1700.823 | 0.458 | 3.565 | -0.084 |  |  |  |  |  |  |
| 81 | ND | ND | ND |  |  |  |  |  |  |  |
| 82 | ND | ND | ND |  |  | 0.132 | 1327 | -27. | 2 | 1,2,3,4 |
| 83 | 1700.823 | -0.107 | 4.071 | 0.115 | -0.0.035 | 0.123 | 1023 | -26. | 3 | 1,2,3,4 |
| 84 | 1700.823 | -0.318 | 4.776 | 0.118 |  |  |  |  |  |  |




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APPENDIX J:
VERIFICATION/VALIDATION TEST DATA

Intentionally left blank.

| $\begin{gathered} \mathrm{RD} \\ \# \end{gathered}$ | $\begin{gathered} \text { PREDICTED } \\ \text { Velocity } \\ \mathrm{m} / \mathrm{s} \\ \hline \end{gathered}$ | $\begin{array}{\|c\|} \hline \text { PREDICTED Loc } \\ \mathrm{x} \\ \mathrm{Z} \end{array}$ |  | PREDICTED ROUND TYPE |  | PREDICTED OFFSET DISTANCE |  | HIT <br> TARGET <br> KZONE | TARGET WENT DOWN | $\begin{gathered} \text { VELOCITY } \\ \text { ERROR } \\ \% \end{gathered}$ | $\begin{gathered} \text { LOCATION } \\ \text { ERROR } \\ (\mathrm{m}) \\ \hline \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\begin{gathered} x \\ (\mathrm{~m}) \\ \hline \end{gathered}$ | $\begin{gathered} \mathrm{Z} \\ (\mathrm{~m}) \end{gathered}$ | Formulation | Statistical | 1 |  |  |  |  |  |
| 1 | 1158.08 | 0.081 | 3.870 | 35 TPGID | TPGID KE | 6.405 | 6.505 |  |  | -1.4 |  |
| 2 | 1165.50 | 0.189 | 2.987 | 35 TPGID | TPGID KE | 6.028 | 6.307 | * | * | -. 8 | 0.075 |
| 3 | 922.08 | -0.349 | 2.564 | 35 TPGID | TPGID HEAT | 6.475 | 5.706 |  | ? | -2.3 | 0.074 |
| 4 | 923.36 | -0.039 | 3.007 | 35 TPGID | TPGID HEAT | 6.257 | 6.100 | * | * | -1.6 | 0.077 |
| 5 | 1030.13 | -0.042 | 3.227 | 35 TPGID | TPGID KE | 6.293 | 6.172 |  |  |  | . 067 |
| 6 | 1016.00 | 1.004 | 3.080 | 35 TPGID | TPGID KE | 5.256 | 7.150 |  |  | - 3 | 0.082 |
| 7 | 834.90 | -0.093 | 3.045 | 35 TPGID | TPGID HEAT | 6.297 | 6.070 |  |  | -1.1 | 0.050 |
| 8 | 848.54 | -1.147 | 3.139 | 35 TPGID | TPGID HEAT | 7.336 | 5.089 |  |  | -2.8 | . 076 |
| 9 | 849.62 | 0.556 | 3.257 | 35 TPGID | TPGID HEAT | 5.764 | 6.721 | * |  | -. 8 | 0.096 |
| 10 | 718.26 | 0.107 | 2.899 | 35 TPGID | TPGID HEAT | 6.090 | 6.231 | * |  | -2.2 | 0.060 |
| 11 | 870.70 | -0.747 | 2.125 | 35 TPGID | TPGID HEAT | 6.802 | 5.269 | * | * | -3.7 | 0.065 |
| 12 | 356.47 | 0.347 | 5.486 | 12.7 | TPGID HEAT | 6.013 | 7.098 |  |  |  |  |
| 13 | 848.18 | 0.916 | 2.451 | 35 TPGID | TPGID HEAT | 5.205 | 6.930 |  |  | 1 | 0.094 |
| 14 | 723.33 | -0.156 | 3.377 | 35 TPGID | TPGID HEAT | 6.445 | 6.118 |  |  | 2.3 | 0.067 0.096 |
| 15 | 724.77 | -0.215 | 1.759 | 35 TPGID | TPGID HEAT | 6.270 | 5.743 |  | * | -2.8 | $0.090$ |
| 16 | 718.65 | 0.363 | 2.203 | 35 TPGID | LARGE HE | 5.732 | 6.349 | * | * | -1.5 |  |
| ${ }^{17}$ | 1430.62 | -0.216 | 2.074 | 25 KE | TPGID KE | 6.301 5883 | 5.745 6.171 |  |  | -3.5 | $0.134$ |
| 18 | 951.25 | 0.215 | 2.080 | Large heat | LARGE HE | 5.883 66.610 | 6.171 5.444 | * | * | --8.7 | 0.099 |
| 19 | 1434.21 | -0.548 | 2.120 | LARGE KE | TPGID KE | 6.610 | 5.444 5.256 |  |  | -4.9 | 0.110 |
| 20 | 1454.55 | -0.708 | 1.946 | LARGE KE | TPGID KE | 6.773 5.836 | 6.202 | * | * | -. 7 | 0.155 |
| 21 | 845.85 | 0.255 | 1.984 | LARGE KE | TPGID HEAT | 5.836 | 6.202 | * | * | . 0 | 0.081 |
| 22 | 1300.39 | 0.446 | 1.915 | LARGE KE | LARGE KE | 5.623 | 6.403 5.455 |  |  | -2.8 |  |
| 23 | 1237.24 | -0.489 | 1.404 | LARGE HEA | LARGE HE | 6.552 | 5.455 |  |  | -3.0 | 0.145 |
| 24 | 1233.05 | -0.624 | 3.512 | LARGE KE | TPGID KE | 6.922 | 5.705 |  |  | -3.0 | 0.145 |
| 25 | 702.74 | 0.366 | 2.646 | 25 HE | TPGID HEAT | 5.776 | 6.425 | * | * | -1.2 | 0.058 |
| 26 | 743.08 | -0.403 | 4.665 | Larce heat | LARGE HE | 7.111 | 6.408 |  |  | -2.5 |  |
| 27 | 773.69 | 0.599 | 4.234 | Large heat | LARGE HE | 6.038 | 7.097 |  |  | -1.4 |  |
| 28 | 763.94 | 0.311 | 3.632 | 35 TPGID | LARGE HE | 6.084 | 6.619 | * | * | -1.3 | 0.082 |
| 29 | 669.46 | 0.445 | 1.432 | 12.7 | 7.62 OR 12.7 | 5.614 | 6.407 |  |  |  |  |
| 30 | 683.64 | 0.437 | 2.906 | 12.7 | 7.62 OR 12.7 | 5.725 | 6.541 |  |  |  |  |
| 31 | 730.99 | 0.762 | 3.393 | 12.7 | 7.62 OR 12.7 | 5.584 | 6.997 |  |  |  |  |
| 32 | 603.59 | -0.432 | 1.841 | 7.62 | 7.62 OR 12.7 | 6.469 | 5.546 |  | ? |  |  |
| 33 | 533.12 | 0.68 | 5.331 | 12.7 | 7.62 OR 12.7 | 6.436 | 7.538 |  |  |  |  |
| 34 | 594.27 | -2.295 | 5.991 | 12.7 | 7.62 OR 12.7 | 9.205 | 5.710 |  |  |  |  |
| 35 | \| 564.10 | -0.879 | 5.812 | 12.7 | 7.62 OR 12.7 | 7.959 | 6.582 |  |  |  |  |
| 36 | 591.19 | -0.408 | 4.055 | 12.7 | 7.62 OR 12.7 | 6.853 | 6.099 |  |  |  |  |
| 37 | 597.55 | -0.519 | 1.593 | 12.7 | 7.62 OR 12.7 | 6.588 | 5.412 |  |  |  |  |
| 38 | 383.47 | -0.051 | 2.269 | 7.62 | 7.62 OR 12.7 | 6.156 | 5.914 |  |  |  |  |
| 39 | 364.37 | 0.647 | 3.302 | 7.62 | 7.62 OR 12.7 | 5.536 | 6.684 |  |  |  |  |
| 40 |  |  |  |  |  |  |  |  |  |  |  |
| 42 | 797.45 | 0.293 | 1.588 | 25 HE | 7.62 OR 12.7 | 5.738 | 6.263 |  |  |  |  |
| 43 | 805.96 | -0.421 | 2.396 | 25 HE | 7.62 OR 12.7 | 6.481 | 5.640 |  |  |  |  |
| 44 | 1258.26 | -0.985 | 2.748 | 25 KE | 7.62 OR 12.7 | 7.060 | 5.182 |  |  |  |  |
| 45 | 1249.61 | 0.072 | 2.516 | 25 KE | 7.62 OR 12.7 | 6.020 | 6.135 |  |  |  |  |
| 46 | 863.93 | -1.301 | 4.278 | 25 KE | 7.62 OR 12.7 | 7.760 | 5.451 |  |  |  |  |
| 47 | 848.54 | 0.436 | 2.666 | 25 KE | 7.62 OR 12.7 | 5.720 | 6.504 | * |  |  |  |
| 48 | 863.93 | 0.141 | 3.710 | 25 KE | 7.62 OR 12.7 | 6.261 | 6.509 |  |  |  |  |
| 49 |  |  |  |  |  |  |  |  |  |  |  |
| 50 | … |  |  |  |  |  |  |  |  |  |  |
| 51 52 |  |  |  |  | 7.62 OR 12.7 | 7.678 | 4.334 | * | * |  |  |
| 52 | 1154.36 | -1.670 -2.109 |  | 25 KE | 7.62 OR 12.7 | 8.089 | 3.888 |  | * |  |  |
| 53 54 | 1150.06 | -2.109 0.025 | 1.488 | 25 KE | 7.62 OR 12.7 | 5.977 | 6.000 | * |  |  |  |



| $\begin{gathered} \text { RD. } \\ \# \end{gathered}$ | GUN POS. <br> (m) | $\begin{gathered} \text { ROUND } \\ \text { TYPE } \\ \text { (mm) } \\ \hline \end{gathered}$ | DATE | $\begin{aligned} & \text { TIME } \\ & \mathrm{H}: \mathrm{M}: \mathrm{S} \end{aligned}$ | TERMINAL VELOCTTY ( $\mathrm{m} / \mathrm{sec}$ ) | VIDEO SCORING LOCATION |  | OFFSET <br> (m) | $\begin{gathered} \text { DISTANCE } \\ (\mathrm{m}) \\ \hline \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | HORIZ | VERT |  |  |
|  |  |  |  |  |  | (m) | (m) | 1 | 2 |
| 1 | 800 | 35 TPGID KE | 6/23/93 | 13:23:55 | 1142.18 |  |  |  |  |
| 2 | " | 35 TPGID KE | 6/23/93 | 13:29:54 | 1156.61 | 0.118 | 3.012 | 6.042 | 6.276 |
| 3 | " | 35 OLD HEAT | 6/23/93 | 14:42:50 | 901.42 | -0.420 | 2.584 | 6.490 | 5.664 |
| 4 | " | 35 NEW HEAT | 6/23/93 | 15:38:59 | 908.96 | -0.099 | 3.056 | 6.263 | 6.075 |
| 5 | 1200 | 35 TPGID KE | 6/23/93 | 16:10:17 | NA | -0.090 | 3.273 | 6.308 | 6.139 |
| 6 | " | 35 TPGID KE | 6/23/93 | 16:13:50 | 1013.41 | 0.951 | 3.143 | 5.270 | 7.118 |
| 7 | " | 35 OLD HEAT | 6/23/93 | 16:21:56 | 825.50 | -0.142 | 3.056 | 6.305 | 6.033 |
| 8 | " | 35 NEW HEAT | 6/23/93 | 16:25:51 | 825.05 | -1.218 | 3.164 | 7.379 | 5.028 |
| 9 | 1700 | 35 TPGID KE | 6/23/93 | 17:09:16 | 843.22 | 0.465 | 3.288 | 5.777 | 6.679 |
| 10 | $\cdots$ | 35 NEW HEAT | 6/23/93 | 17:13:16 | 702.55 | 0.049 | 2.910 | 6.087 | 6.187 |
| 11 | " | 35 TPGID KE | 6/23/93 | 17:21:54 | 839.64 | -0.810 | 2.141 | 6.829 | 5.217 |
| 12 | " | 35 TPGID KE | 6/23/93 | 17:24:44 | NA |  |  | 6.218 | 6.213 |
| 13 | " | 35 TPGID KE | 6/23/93 | 17:29:05 | 848.95 | 0.847 | 2.388 | 5.208 | 6.891 |
| 14 | " | 35 NEW HEAT | 6/23/93 | 17:31:24 | 707.04 | -0.220 | 3.397 | 6.466 | 6.049 |
| 15 | " | 35 NEW HEAT | 6/23/93 | 17:40:09 | 705.15 | -0.290 | 1.699 | 6.290 | 5.711 |
| 16 | " | 35 NEW HEAT | 6/23/93 | 17:43:28 | 708.16 | 0.292 | 2.148 | 5.732 | 6.315 |
| 17 | 800 | 105 KE | 6/24/93 | 10:58:24 | 1382.3 | -0.285 | 2.010 | 6.296 | 5.729 |
| 18 | " | 105 HEAT | 6/24/93 | 11:44:24 | 943.8 | 0.146 | 1.965 | 5.863 | 6.157 |
| 19 | " | 105 KE | 6/24/93 | 11:51:11 | 1382.9 | -0.593 | 2.032 | 6.605 | 5.423 |
| 20 | " | 105 KE | 6/24/93 | 11:54:37 | 1387.2 | -0.787 | 1.869 | 6.791 | 5.220 |
| 21 | 1200 | 105 HEAT | 6/24/93 | 13:30:44 | 839.7 | 0.199 | 1.840 | 5.805 | 6.203 |
| 22 | $\cdots$ | 105 KE | 6/24/93 | 13:35:08 | 1300.2 | 0.402 | 1.847 | 5.602 | 6.406 |
| 23 | 1800 | 105 KE | 6/24/93 | 14:32:40 | 1203.0 |  |  | 6.218 | 6.213 |
| 24 | " | 105 KE | 6/24/93 | 15:23:19 | 1196.7 | -0.619 | 3.657 | 6.922 | 5.757 |
| 25 | " | 105 HEAT | 6/24/93 | 15:29:07 | 694.6 | 0.411 | 2.608 | 5.674 | 6.488 |
| 26 | " | 105 HEAT | 6/24/93 | 15:39:13 | 725.3 |  |  | 6.218 | 6.213 |
| 27 | " | 105 HEAT | 6/24/93 | 15:45:08 | 762.9 |  |  | 6.218 | 6.213 |
| 28 | " | 105 HEAT | 6/24/93 | 15:48:55 | 754.1 | 0.340 | 3.709 | 6.029 | 6.678 |
| 29 | 400 | 12.7 | 6/25/93 | 12:47:07 | NA | NA | NA | NA | NA |
| 30 | " | 12.7 | 6/25/93 | 12:50:22 | NA | NA | NA | NA | NA |
| 31 | * | 12.7 | 6/25/93 | 12:56:36 | NA | NA | NA | NA | NA |
| 32 | " | 7.62 | 6/25/93 | 13:10:13 | NA | NA | NA | NA | NA |
| 33 | 800 | 12.7 | 6/25/93 | 13:51:09 | NA | NA | NA | NA | NA |
| 34 | " | 12.7 | 6/25/93 | 13:55:19 | NA | NA | NA | NA | NA |
| 35 | " | 12.7 | 6/25/93 | 13:59:27 | NA | NA | NA | NA | NA |
| 36 | " | 12.7 | 6/25/93 | 14:01:44 | NA | NA | NA | NA | NA |
| 37 | " | 12.7 | 6/25/93 | 14:03:15 | NA | NA | NA | NA | NA |
| 38 | " | 7.62 | 6/25/93 | 14:10:50 | NA | NA | NA | NA | NA |
| 39 | " | 7.62 | 6/25/93 | 14:16:25 | NA | NA | NA | NA | NA |
| 40 | " | 7.62 | 6/25/93 | 14:19:12 | NA | NA | NA | NA | NA |
| 42 | 600 | 25 HE | 7/1/93 | 10:54:00 | NA | NA | NA | NA | NA |
| 43 | " | 25 HE | 7/1/93 | 10:55:00 | NA | NA | NA | NA | NA |
| 44 | " | 25 KE | 7/1/93 | 11:15:00 | NA | NA | NA | NA | NA |
| 45 | " | 25 KE | 7/1/93 | 11:18:00 | NA | NA | NA | NA | NA |
| 46 | 1700 | 25 KE | 7/1/93 | 11:30:00 | NA | NA | NA | NA | NA |
| 47 | " | 25 KE | 7/1/93 | 11:33:00 | NA | NA | NA | NA | NA |
| 48 | " | 25 KE | 7/1/93 | 11:43:00 | NA | NA | NA | NA | NA |
| 49 | " | 25 HE | 7/1/93 | 11:45:00 | NA | NA | NA | NA | NA |
| 50 | " | 25 HE | 7/1/93 | 11:46:00 | NA | NA | NA | NA | NA |
| $\square$ |  | 25 HE | 7/1/93 | 11:48:00 | NA | NA | NA | NA | NA |
| 52 | 1000 | 25 KE | 7/1/93 | 14:15:00 | NA | NA | NA | NA | NA |
| 53 | " | 25 KE | 7/1/93 | 14:20:00 | NA | NA | NA | NA | NA |
| 54 | " | 25 KE | 7/1/93 | 14:22:00 | NA | NA | NA | NA | NA |


| 55 | " | 25 KE | 7/1/93 | 14:27:00 | NA | NA | NA | NA | NA |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 56 | " | 25 HE | 7/1/93 | 14:29:00 | NA | NA | NA | NA | NA |
| 57 | " | 25 HE | 7/1/93 | 14:53:00 | NA | NA | NA | NA | NA |
| 58 | " | 25 HE | 7/1/93 | 14:55:00 | NA | NA | NA | NA | NA |
| 59 | " | 25 KE | 7/1/93 | 14:56:00 | NA | NA | NA | NA | NA |
| 60 | " | 25 KE | 7/1/93 | 14:58:00 | NA | NA | NA | NA | NA |
| 61 | " | 25 KE | 7/1/93 | 15:01:00 | NA | NA | NA | NA | NA |
| 62 | " | 25 HE | 7/1/93 | 15:04:00 | NA | NA | NA | NA | NA |
| 63 | " | 120 HE | 7/1/93 | 16:28:00 | NA | NA | NA | NA | NA |
| 64 | " | 120 KE | 7/1/93 | 16:36:00 | NA | NA | NA | NA | NA |
| 65 | " | 120 KE | 7/1/93 | 16:38:00 | NA | NA | NA | NA | NA |

## APPENDIX K

STATISTICAL ANALYSIS OF 1,000-m DATA

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## Implementing Kruskal-Wallis Test: An Example

The Kruskal-Wallis nonparametric test was implemented in the feasibility test phase for the $1,000-\mathrm{m}$ data. An example of the test procedure is provided in this appendix. The null hypothesis (the hypothesis that is to be rejected) is that the six round types have identical distributions (and therefore equal means) vs. the altemative that at least two round types differ.

The advantage of a nonparametric test over a parametric test is that the test does not require the assumptions of normality of the data or homogeneity of variances among the groups. This test performs analysis of variance on the ranks of the data. The ranks start with 1 for the smallest value among all the six round types. If more than one response value is the same (that is, there are ties), then these tied values would be assigned the average rank. This test was performed on each variable separately and at four regions corresponding to the data collected from the microphones. The data from the 1 - and $3-\mathrm{m}$ microphones were grouped into one region since the $1-\mathrm{m}$ microphone had incomplete data. The range of offset distances in meters for each region is as follows:

Region $1 \leq 4$
$4<$ Region $2 \leq 7$
$7<$ Region $3 \leq 10$
$10<$ Region 4.

An example of the analysis provided for this test is for the positive peak pressures collected at the microphone stationed 12 m from the center of the target, region 4.

Table K-1. Example of Positive Peak Pressure From Region 4

| 25 mm |  | 105 mm |  | 120 mm |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| HE <br> $(\mathrm{Pa})$ | KE <br> $(\mathrm{Pa})$ | HEAT <br> $(\mathrm{Pa})$ | KE <br> $(\mathrm{Pa})$ | HEAT <br> $(\mathrm{Pa})$ | KE <br> $(\mathrm{Pa})$ |
| 481.40 | 376.00 | 1495.70 | 1109.00 | 1508.30 | 1088.00 |
| 483.98 | 401.60 | 1733.00 | 1109.50 | 1800.00 | 1109.50 |
| 499.41 | 404.20 | 1735.00 | 1112.00 | 1987.00 | 1145.00 |

Table K-2. Order Values and Ranks

| Round (mm) | Ordered Values (Pa) | Rank | Rank with Ties |
| :---: | :---: | :---: | :---: |
| 25 KE | 376.00 | 1 | 1 |
| 25 KE | 401.60 | 2 | 2 |
| 25 KE | 404.20 | 3 | 3 |
| 25 HEI | 481.40 | 4 | 4 |
| 25 HEI | 483.98 | 5 | 5 |
| 25 HEI | 499.41 | 6 | 6 |
| 120 KE | 1088.00 | 7 | 7 |
| 105 KE | 1109.00 | 8 | 8 |
| 105 KE | \#109sism | 9 |  |
| 120 KE | आ以5\% | 10 | 9ૐ |
| 105 KE | 1112.00 | 11 | 11 |
| 120 KE | 1145.00 | 12 | 12 |
| 105 HEAT | 1495.70 | 13 | 13 |
| 120 HEAT | 1508.30 | 14 | 14 |
| 105 HEAT | 1733.00 | 15 | 15 |
| 105 HEAT | 1735.00 | 16 | 16 |
| 120 HEAT | 1800.00 | 17 | 17 |
| 120 HEAT | 1987.00 | 18 | 18 |

All the positive peak pressure values from Table K-1 are ordered and then ranked. Table K-2 lists the ordered values and the corresponding rank. The two values with ranks 9 and 10 are the same and therefore should be given the same rank. The fourth column provides the rank correction by assigning the average of the two tied ranks, 9.5. These values become the data for which the analysis will be based (see Table K-3).

Table K-3. Ranks of Positive Peak Pressure

|  | $25-\mathrm{mm}$ <br> M793 | $25-\mathrm{mm}$ <br> M910 | $105-\mathrm{mm}$ <br> M490 | $105-\mathrm{mm}$ <br> M724 | $120-\mathrm{mm}$ <br> M831 | $120-\mathrm{mm}$ <br> M865 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 4 | 1 | 13 | 8 | 14 | 7 |
|  | 5 | 2 | 15 | 9.5 | 17 | 9.5 |
| sum of <br> ranks | 15 | 6 | 16 | 11 | 18 | 12 |

The test statistic, T, for the Kruskal-Wallis test is computed the following way (Conover 1980):

$$
T=\frac{1}{S^{2}}\left(\sum_{i=1}^{\mathrm{k}=6} \frac{\mathrm{SR}^{2}}{\mathrm{n}_{\mathrm{i}}}-\frac{\mathrm{N}(\mathrm{~N}+1)^{2}}{4}\right),
$$

where
SR = sum of the ranks as given in Table K-3, and

$$
S^{2}=\frac{1}{\mathrm{~N}-1}\left(\sum_{\mathrm{i}=1}^{\mathrm{N}} \operatorname{Rank}_{\mathrm{i}}^{2}-\frac{\mathrm{N}(\mathrm{~N}+1)^{2}}{4}\right)
$$

The test statistic, is compared to the chi-square distribution with 5 (6 groups - 1 ) degrees of freedom at the $\alpha=0.05$ level. (The chi-square test provided an approximate quantile since the exact distribution was not available.)

The calculated test statistic of 15.794 is significant at the alpha $=0.01$ level. This indicates at least two groups differ in their average rank. To determine which ones differ, pairwise comparisons were performed. Two groups, i and j , would be statistically different if the following inequality is satisfied:

$$
\left|\frac{S R_{i}}{n_{i}}-\frac{S R_{j}}{n_{j}}\right|>t\left[S^{2} \frac{N-1-T}{N-k}\right]^{1 / 2}\left[\frac{1}{n_{i}}-\frac{1}{n_{j}}\right]^{1 / 2}
$$

The " t " is the t -distribution with $\mathrm{N}-\mathrm{k}$ degrees of freedom at the $1-\alpha / 2$ quantile. For this data set, if two average ranks differ more than 3.01, then the two groups are significantly different at the $\alpha=0.05$ level. The ordered average rank for each group is listed in Table K-4.

Table K-4. Ordered by Average Rank

| $25-\mathrm{mm} \mathrm{M} 910$ | 2.00 |
| :---: | ---: |
| $25-\mathrm{mm} \mathrm{M} 93$ | 5.00 |
| $105-\mathrm{mm} \mathrm{M} 724$ | 9.50 |
| $120-\mathrm{mm} \mathrm{M} 665$ | 9.50 |
| $105-\mathrm{mm} \mathrm{M} 490$ | 14.67 |
| $120-\mathrm{mm} \mathrm{M} 831$ | 16.33 |

To summarize the results, the following notation is used for this example and for the other N-Wave variables in Table K-5. The round types are listed in order from lowest average rank to the highest. Parentheses around two or more round types indicate there is no significant difference between (or among) the rounds. The short-hand notation to summarize the results for positive peak pressures from region 4 is:

$$
(25 \mathrm{~K}=25 \mathrm{H}) \neq(105 \mathrm{H}=120 \mathrm{H}) \neq(105 \mathrm{~K}=120 \mathrm{~K}) .
$$

To conserve space, H and K are abbreviated for HEI or HEAT and KE, respectively. The result for example tells us:

- $25-\mathrm{mm}$ KE is not significantly different from $25-\mathrm{mm}$ HEI in average rank.
$-25-\mathrm{mm}$ KE and HE are significantly different from both round types of size 105 and 120 mm .
$-105-\mathrm{mm}$ HE is not significantly different from $120-\mathrm{mm}$ HE.
$-105-\mathrm{mm} \mathrm{KE}$ is not significantly different from $120-\mathrm{mm}$ KE.
- The large HEAT rounds ( 105 mm and 120 mm ) are significantly different from the large KE rounds ( 105 mm and 120 mm ).

Table K-5. Multiple Comparison Results

| Variable | Region | Notational Summary |
| :---: | :---: | :---: |
| Positive Peak Pressure | $\begin{aligned} & 1 \\ & 2 \\ & 3 \\ & 4 \end{aligned}$ | $\begin{aligned} & (25 \mathrm{~K}=25 \mathrm{H}) \neq(105 \mathrm{~K}=120 \mathrm{~K}) \neq(105 \mathrm{H}=120 \mathrm{H}) \\ & (25 \mathrm{H}=25 \mathrm{~K}) \neq(105 \mathrm{~K}=120 \mathrm{~K}) \neq(105 \mathrm{H}=120 \mathrm{H}) \\ & 25 \mathrm{~K} \neq 25 \mathrm{H} \neq(105 \mathrm{~K}=120 \mathrm{~K}) \neq(105 \mathrm{H}=120 \mathrm{H}) \\ & (25 \mathrm{~K}=25 \mathrm{H}) \neq(105 \mathrm{~K}=120 \mathrm{~K}) \neq(105 \mathrm{H}=120 \mathrm{H}) \end{aligned}$ |
| Negative Peak Pressure | $\begin{aligned} & 1 \\ & 2 \\ & 3 \\ & 4 \end{aligned}$ | $\begin{aligned} & (25 \mathrm{~K}=25 \mathrm{H}) \neq(105 \mathrm{H}=105 \mathrm{~K}=120 \mathrm{H}=120 \mathrm{~K}) \\ & (25 \mathrm{H}=25 \mathrm{~K}) \neq(105 \mathrm{~K}=[105 \mathrm{H})=120 \mathrm{H})=120 \mathrm{~K}] \\ & (25 \mathrm{~K}=25 \mathrm{H}) \neq(105 \mathrm{~K}=105 \mathrm{H}=120 \mathrm{H}=120 \mathrm{~K}) \\ & (25 \mathrm{H}=25 \mathrm{~K}) \neq(105 \mathrm{~K}=120 \mathrm{~K}=105 \mathrm{H}=120 \mathrm{H}) \end{aligned}$ |
| Positive Phase Duration | $\begin{aligned} & 1 \\ & 2 \\ & 3 \\ & 4 \end{aligned}$ | $\begin{aligned} & 25 \mathrm{H} \neq 25 \mathrm{~K} \neq(105 \mathrm{~K}=120 \mathrm{~K}) \neq(105 \mathrm{H}=120 \mathrm{H}) \\ & 25 \mathrm{H} \neq 25 \mathrm{~K} \neq 105 \mathrm{~K} \neq 120 \mathrm{~K} \neq 105 \mathrm{H} \neq 120 \mathrm{H} \\ & 25 \mathrm{H} \neq 25 \mathrm{~K} \neq 105 \mathrm{~K} \neq 120 \mathrm{~K} \neq 105 \mathrm{H} \neq 120 \mathrm{H} \\ & 25 \mathrm{H} \neq 25 \mathrm{~K} \neq 105 \mathrm{~K} \neq 120 \mathrm{~K} \neq 105 \mathrm{H} \neq 120 \mathrm{H} \end{aligned}$ |
| Negative Phase Duration | $\begin{aligned} & 1 \\ & 2 \\ & 3 \\ & 4 \end{aligned}$ | $\begin{aligned} & (25 \mathrm{H}=25 \mathrm{~K}) \neq(105 \mathrm{H}=120 \mathrm{~K}=105 \mathrm{~K}=120 \mathrm{H}) \\ & (25 \mathrm{H}=25 \mathrm{~K}) \neq(105 \mathrm{~K}=[120 \mathrm{~K}=105 \mathrm{H})=120 \mathrm{H}] \\ & (25 \mathrm{~K}=[25 \mathrm{H})=\{105 \mathrm{~K}]=105 \mathrm{H}=120 \mathrm{~K}=120 \mathrm{H}\} \\ & (25 \mathrm{~K}=[25 \mathrm{H})=\{105 \mathrm{~K}]=105 \mathrm{H}=120 \mathrm{~K}=120 \mathrm{H}\} \end{aligned}$ |
| Total Duration | $\begin{aligned} & 1 \\ & 2 \\ & 3 \\ & 4 \end{aligned}$ | $\begin{aligned} & (25 \mathrm{~K}=25 \mathrm{H}) \neq(105 \mathrm{~K}=120 \mathrm{~K}) \neq 120 \mathrm{H}=105 \mathrm{H}) \\ & 25 \mathrm{~K} \neq 25 \mathrm{H} \neq 105 \mathrm{~K} \neq 120 \mathrm{~K} \neq(105 \mathrm{H}=120 \mathrm{H}) \\ & 25 \mathrm{~K} \neq 25 \mathrm{H} \neq(105 \mathrm{~K}=120 \mathrm{~K}) \neq(105 \mathrm{H}=120 \mathrm{H}) \\ & 25 \mathrm{~K} \neq 25 \mathrm{H} \neq 105 \mathrm{~K} \neq 120 \mathrm{~K} \neq 105 \mathrm{H} \neq 120 \mathrm{H} \end{aligned}$ |
| Peak Pressure Impulse | $\begin{aligned} & 1 \\ & 2 \\ & 3 \\ & 4 \end{aligned}$ | $\begin{aligned} & 25 \mathrm{~K} \neq 25 \mathrm{H} \neq(105 \mathrm{~K}=120 \mathrm{~K}) \neq(105 \mathrm{H}=120 \mathrm{H}) \\ & 25 \mathrm{~K} \neq 25 \mathrm{H} \neq 105 \mathrm{~K} \neq 120 \mathrm{~K} \neq 105 \mathrm{H} \neq 120 \mathrm{H} \\ & 25 \mathrm{~K} \neq 25 \mathrm{H} \neq 105 \mathrm{~K} \neq 120 \mathrm{~K} \neq 105 \mathrm{H} \neq 120 \mathrm{H} \\ & 25 \mathrm{~K} \neq 25 \mathrm{H} \neq 105 \mathrm{~K} \neq 120 \mathrm{~K} \neq 105 \mathrm{H} \neq 120 \mathrm{H} \end{aligned}$ |
| Peak of Absolute Pressure Impulse | $\begin{aligned} & 1 \\ & 2 \\ & 3 \\ & 4 \end{aligned}$ | $\begin{aligned} & 25 \mathrm{~K} \neq 25 \mathrm{H} \neq(105 \mathrm{~K}=120 \mathrm{~K}) \neq(105 \mathrm{H}=120 \mathrm{H}) \\ & 25 \mathrm{~K} \neq 25 \mathrm{H} \neq 105 \mathrm{~K} \neq 120 \mathrm{~K} \neq 105 \mathrm{H} \neq 120 \mathrm{H} \\ & 25 \mathrm{~K} \neq 25 \mathrm{H} \neq 105 \mathrm{~K} \neq 120 \mathrm{~K} \neq 105 \mathrm{H} \neq 120 \mathrm{H} \\ & 25 \mathrm{~K} \neq 25 \mathrm{H} \neq 105 \mathrm{~K} \neq 120 \mathrm{~K} \neq 105 \mathrm{H} \neq 120 \mathrm{H} \end{aligned}$ |
| Negative Phase Pressure Impulse | $\begin{aligned} & 1 \\ & 2 \\ & 3 \\ & 4 \end{aligned}$ | $\begin{aligned} & 25 \mathrm{~K} \neq 25 \mathrm{H} \neq(105 \mathrm{~K}=120 \mathrm{~K}) \neq(105 \mathrm{H}=120 \mathrm{H}) \\ & 25 \mathrm{~K} \neq 25 \mathrm{H} \neq 105 \mathrm{~K} \neq 120 \mathrm{~K} \neq(120 \mathrm{H}=105 \mathrm{H}) \\ & 25 \mathrm{~K} \neq 25 \mathrm{H} \neq 105 \mathrm{~K} \neq 120 \mathrm{~K} \neq 105 \mathrm{H} \neq 120 \mathrm{H} \\ & 25 \mathrm{~K} \neq 25 \mathrm{H} \neq 105 \mathrm{~K} \neq 120 \mathrm{~K} \neq(120 \mathrm{H}=105 \mathrm{H}) \end{aligned}$ |

Most of the variables at each region can distinguish between large- and small-caliber rounds ( 25 mm vs. 105 mm or 120 mm ). The only variable that cannot is negative phase duration in regions 3 and 4 . The results of the pairwise multiple comparison tests for each region on each variable indicate that we can
not discriminate among all six round types. A general conservative result is the relationship as seen for the positive peak pressure:

$$
(25 \mathrm{~K}=25 \mathrm{H}) \neq(105 \mathrm{~K}=120 \mathrm{~K}) \neq(105 \mathrm{H}=120) .
$$

For some variables in some of the regions, the two small-caliber rounds were distinguishable:

$$
25 \mathrm{~K} \neq 25 \mathrm{H} \neq(105 \mathrm{~K}=120 \mathrm{~K}) \neq(105 \mathrm{H}=120 \mathrm{H}) .
$$

For the most part, there is good agreement of the observed values with the statistical nonparametric results. However, on occasion, there are a few results that do not appear intuitive. Take for instance, negative phase duration plotted against offset distance in Figure K-1. In regions three and four, the $25-\mathrm{mm}$ HE and KE rounds are not significantly different from each other by the Kruskal-Wallis test, as indicated by the parentheses () around $25 \mathrm{~K}=25 \mathrm{H}$, in Table K-5. Furthermore, all of the large-caliber rounds are not significantly different from each other, as indicated by the braces \{\}. These two results should be obvious from the plot. What is not intuitive is the nonparametric test indicating that $25-\mathrm{mm}$ HEI and $105-\mathrm{mm}$ KE are not significantly different. From the plot, one would think that they should be different. This result shows that by analyzing the data using the ranks, large differences in magnitude of the response variable in the original units may be masked.

Conversely, the nonparametric test can be very powerful in detecting small differences in magnitude if the ranks of the data within a round type are close together. This is illustrated in Figure K-2 for the peak net pressure impulse. The smallest ranks are the 25 KE rounds followed by the 25 HEI . Then, in order for regions $1-4$, the ranking is as follows: $105 \mathrm{KE}, 120 \mathrm{KE}, 105 \mathrm{HEAT}$, and 120 HEAT.

What we have shown in these analyses is that many of the variables under consideration are good candidates to discriminate among at least the small-caliber rounds from the large-caliber rounds. In some regions for some variables, all the rounds are significantly different from each other. For the most part, the first region, representing data collected closes to the flight of the round $(<4 \mathrm{~m})$, is the hardest region to discriminate. This result is a guide to the placement of the microphones in future tests.


Figure K-2. Microphone offset distance vs. peak net pressure impulse for rounds fired at $1,000 \mathrm{~m}$.

APPENDIX L:
PREDEMONSTRATION TEST DATA

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| $\begin{gathered} \text { RD. } \\ \# \end{gathered}$ | GUN POS. <br> (m) | ROUND <br> TYPE <br> (mm) | DATE | $\begin{gathered} \text { TIME } \\ \mathrm{H}: \mathrm{M}: \mathrm{S} \end{gathered}$ | $\begin{gathered} \text { TERMINAL } \\ \text { VELOCITY } \\ (\mathrm{m} / \mathrm{s}) \\ \hline \end{gathered}$ | HAND SCORED LOCATION |  | $\begin{array}{cr}\text { OFFSET DISTANCE } \\ \text { (m) } & \text { (m) }\end{array}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | HORIZ | VERT |  |  |
|  |  |  |  |  |  | (m) | (m) | 1 | 2 |
| 1 | 1410 | 120(M865) | 7/14/93 | 12:24:25 | NA | 0.552 | 1.229 |  |  |
| 2 | 1130 | 120 (M831) | 7/14/93 | 12:26:56 | NA | 0.305 | 1.686 |  |  |
| 3 | 430 | 12.7 (M17) | 7/14/93 | 12:31:16 | NA |  |  |  |  |
| 4 | 430 | 7.62 (M62) | 7/14/93 | 12:32:27 | NA |  |  |  |  |
| 5 | 430 | 7.62 (M62) | 7/14/93 | 12:32:41 | NA |  |  |  |  |
| 6 | 960 | 35 (DM18) | 7/14/93 | 12:44:43 | NA | 0.641 | 2.842 |  |  |
| 7 | 960 | 35 (DM18) | 7/14/93 | 12:46:15 | NA | 0.787 | 2.334 |  |  |
| 8 | 1000 | 25 (M910) | 7/14/93 | 12:54:27 | NA | 1.029 | 1.203 |  |  |
| 9 | 1000 | 25 (M910) | 7/14/93 | 12:56:39 | NA | 0.457 | 1.210 |  |  |
| 10 | 1000 | 25 (M793) | 7/14/93 | 12:57:13 | NA | 1.422 | 1.734 |  |  |
| 11 | 1000 | 25 (M793) | 7/14/93 | 12:57:55 | NA | 1.168 | 2.524 |  |  |
| 12 | 1410 | 35 (DM18) | 7/14/93 | 12:58:49 | NA |  |  |  |  |


| $\begin{gathered} \mathrm{RD} . \\ \# \\ \hline \end{gathered}$ | PREDICTED <br> Velocity (m/s) | PREDICTED LOC |  | PREDICTED ROUND TYPE |  |  | PREDICTED OD |  | HITTARGETZONE | $\begin{gathered} \text { TARGET } \\ \text { WENT } \\ \text { DOWN } \\ \hline \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | (m) | (m) | Formulation | Statistical | Hybrid | 1 | 2 |  |  |
| 1 | 1229.45 | 2.78 | 2.305 | Large KE | Large HE | Large KE | 3.466 | 8.545 | no | no |
| 2 | 902.73 | -4.188 | -8.289 | Large KE | Large HE | Large KE | 7.860 | 4.932 | no | no |
| 3 | 719.42 | 0.544 | 1.206 | 12.7 | 7.62 | 25KE | 5.462 | 6.681 | no | no |
| 4 | 573.64 | -0.489 | 2.014 | 7.62 | 7.62 | 12.7 | 6.451 | 5.563 | yes | yes |
| 5 | 601.69 | -0.37 | 1.988 | 12.7 | 35 | 25KE | 6.326 | 5.687 | yes | yes |
| 6 | 894.01 | 0.536 | 2.907 | 35 | 35 | 35 | 5.609 | 6.504 | no | no |
| 7 | 890.67 | 0.687 | 2.358 | 35 | 35 | 35 | 5.390 | 6.629 | yes | yes |
| 8 | 1093.20 | 0.511 | 4.652 | 25 KE | 7.62 | 25 KE | 6.155 | 6.950 | no | no |
| 9 | 1069.52 | -0.436 | 4.792 | 25 KE | 7.62 | 25 KE | 7.093 | 6.097 | nо | no |
| 10 | 536.48 |  |  | LargeKE | 35 | 35 |  |  | no | no |
| 11 | 624.71 | 1.307 | 3.370 | 25HE | 7.62 | 25HE | 4.903 | 7.398 | no | no |
| 12 | 585.65 |  |  | 35 | 35 | 35 |  |  | no | no |

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| a | $=$ ambient speed of sound, meters/second |
| :---: | :---: |
| A | $=$ microphone separation distance, 1 meter |
| C | $=$ true distance for correct velocity calculation |
| D | $=$ projectile diameter, meters |
| $\mathrm{D}_{\mathrm{i}}$ | $=$ arrival time difference, $\mathrm{i}=1-4$ |
| $F(y)$ | $=$ is a function used to solve the differential equation determining the flow past the body of revolution |
| h | $=$ elevation of projectile above ground plane |
| K | $=$ shape constant, 1.82 |
| L | $=$ projectile length, meters |
| $\mathrm{L}_{\text {Mi }}$ | $=$ location microphone, $\mathrm{i}=1-6$ |
| M | $=$ Mach number |
| O | $=$ offset distance, perpendicular distance from projectile trajectory to mic, meters |
| p | = overpressure |
| $\mathrm{p}_{0}$ | $=$ ambient pressure |
| $\mathrm{R}_{\mathrm{C}}$ | $=$ in-plane distance from center microphone to projectile location, meters |
| $\mathrm{R}_{\mathrm{L}}$ | $=$ in-plane distance from left microphone to projectile location, meters |
| $\mathrm{R}_{\mathrm{R}}$ | $=$ in-plane distance from right microphone to projectile location, meters |
| T | $=$ total duration pulse period, seconds |
| T | $=$ time difference between microphone 2 and 1 |
| $\mathrm{T}_{2}$ | $=$ time difference between microphone 3 and 2 |
| $\mathrm{T}_{3}$ | $=$ time difference between microphone 5 and 2 |
| $\mathrm{T}_{4}$ | $=$ time difference between microphone 5 and 4 |
| $\mathrm{T}_{5}$ | $=$ time difference between microphone 6 and 5 |
| V | $=$ projectile velocity, meters/second |
| $V_{P}$ | $=$ predicted projectile velocity, meters/second |
| x | $=$ distance along the axis from the bow |
| y | $=$ describes a characteristic curve relationship between x and 0 |
| $\mathrm{y}_{\mathrm{f}}$ | $=$ equation for shock front |
| $y_{\text {h }}$ | $=$ equation for lead hyperbola |
| $\mathrm{y}_{\mathrm{h} 2}$ | $=$ equation for succeeding hyperbola |
| $\mathrm{Y}_{\text {LM2 }}$ | $=\mathrm{y}$ position of microphone 2 , meters |
| $\mathrm{Y}_{\text {LM5 }}$ | $=\mathrm{y}$ position of microphone 5 , meters |
| $\mathrm{Y}_{\text {LMi }}$ | $=\mathrm{y}$ position of microphone i |
| $\mathrm{y}_{\mathrm{s}}$ | $=$ equation for line going through mic 1 and mic 2 |
| $\alpha$ | $=$ shock angle, ${ }^{\circ}$ |
| $\beta$ | $=$ azimuth deviation |
| $\gamma$ | $=$ ratio of specific heats of air (1.4) |
| $\theta$ | $=$ angle from microphone array axis to $\mathrm{R}_{\mathrm{C}}$ |

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[^0]:    *The N-wave appears upside down because the signal from the microphone was increased by an inverting amplifier.

