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VARIABLE-RESOLUTION IMAGERY FOR FLIGHT SIMULATION

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PREFACE

The research described here was conducted by the University of Dayton Research Institute (Contract No. F33615-90-C-0005) for the Armstrong Laboratory/Aircrew Training Research Division (AL/HRA) under Work Unit 1123-03-85, Flying Training Research Support. Laboratory contract monitor was Ms. Patricia Ann Spears; task monitor was Dr. Byron J. Pierce. Portions of this research were performed while one of the authors (YYZ) was supported by the USAF-UES Summer Faculty Research Program, Contract No. F49620-88-C-0053.

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VARIABLE-RESOLUTION IMAGERY FOR FLIGHT SIMULATION

SUMMARY

For spatial discrimination tasks, the center of the visual field is more sensitive than the visual periphery. This observation is relevant to the design of visual simulators in that it suggests that information can be removed in the peripheral parts of a simulator image without affecting the quality of the simulation. If this can be done, then smaller, less expensive computer systems can be used to store, manipulate, and transmit imagery at a given level of fidelity. Although there are differences in sensitivity across the visual field, in most cases central and peripheral sensitivity can be equated if the peripheral stimulus is appropriately magnified. Rather than applying spatially varying magnification, we processed images using a spatially varying operator that low-pass filtered (i.e., blurred) the images relatively little at their center and progressively more at greater distances from the center. The result is called a variable-resolution image. A series of such images processed at various levels was used to estimate the blur gradient that was just detectable by human observers. Wide-field (80° diameter), complex, real-world images were used in order to approximate the imagery used in visual simulators. It was possible to obtain (from the variable-resolution imagery) imagery suitable for use in visual simulation since the processing techniques described here are consistent with a formalism which allows appropriately filtered images to be efficiently sampled and hence represented with less information. Based on the variable-resolution functions determined to be near threshold for our observers, we can generate effective variable-resolution visual imagery using, at most, one-quarter of the information associated with conventional imagery.

GENERAL INTRODUCTION

The research described here was designed to perceptually evaluate variable-resolution imagery whose spatial frequency content decreases as a function of distance from its center (Zeevi, Porat, & Geri, 1990). Such imagery is potentially relevant to the design of visual simulators in that it can be made to appear, to a human observer, to be equivalent to an image whose spatial frequency content is equally high at all points. Once an equivalent

variable-resolution image is found, formal procedures (Clark, Palmer, & Lawrence, 1985; Zeevi & Shlomot, 1993) exist for efficiently sampling the image. The more efficient sampled image can then be used in place of the original image in the visual simulator.

We begin here with a brief discussion of conventional, position-invariant image processing techniques in order to distinguish them from the position-varying techniques used in the present study. We discuss some of the characteristics of images processed by our technique, as well as the concept of local bandwidth, and briefly describe a formal technique for appropriately sampling non-uniform imagery. Following this general introduction, two experiments designed to perceptually evaluate variable-resolution imagery are described.

Conventional Image Processing

Conventional techniques of image processing, which are carried out in the context of linear systems theory, are applicable only when the systems used to operate on (or process) the image are *linear and position-invariant*. Under these conditions, it is possible to operate on an image either in the space domain (by convolution) or in the frequency domain (by filtering). For example, operations in the space domain include smoothing an image in order to improve the signal-to-noise ratio, or extracting edges in order to perform pattern recognition or contour identification. The corresponding operations in the frequency domain would be low-pass and band-pass filtering, respectively. The operation, in the space domain, can be represented formally as:

$$l_{o}(x,y) = \iint l_{i}(x',y') \cdot k(x-x',y-y') dx' dy'$$

$$\stackrel{\Delta}{=} l_{i}(x,y) * * k(x,y)$$
(1)

where $l_i(x',y')$ and $l_o(x,y)$ denote the input and output images, respectively, k(x-x',y-y') is the convolution kernel which represents the mask used to operate on the image, and the double asterisk (**) denotes a two-dimensional convolution. In the spatial frequency domain, the

corresponding expression is obtained by Fourier transforming Equation 1 yielding:

$$L_o(\omega_x, \omega_y) = L_i(\omega_x, \omega_y) \cdot K(\omega_x, \omega_y)$$
(2)

where L_o and L_i are the spatial frequency spectra of the input and output images, respectively, and $K(\omega_x, \omega_y)$ is the modulation transfer function (MTF) of the system. An example of an image generated using a discrete implementation of the convolution operation of Equation 1 is shown on the right in Figure 1. The original unprocessed image is shown on the left. The convolution was performed with a 39 x 39-pixel gaussian kernel. The summation kernel was position-invariant and thus the image has been low-pass filtered (i.e., blurred) equally at all positions.

Variable-Resolution Imagery

In order to process images in a *position-varying* fashion similar to that taking place in the visual system, we cannot, for the reasons described above, apply the classical techniques of linear systems theory. It is necessary, therefore, to devise techniques which are analogous to convolution and other linear operations, but which are not position-invariant. The technique we have chosen involves operating on a fixed-resolution image with a system whose characteristics vary from point to point. Thus, the kernel, k(x-x',y-y'), shown in Equation 1, which is a function only of the differences between pairs of variables along the two spatial coordinates, becomes k(x,x',y,y'), which is a function of the two stimulus independent variables and the two response independent variables. Thus, in this case:

$$l_{o}(x,y) = \iint l_{i}(x',y') \cdot k(x,x',y,y') dx' dy$$
(3)

In accordance with Zeevi, Peterfreund, and Shlomot (1988), we will refer to the function $l_o(x,y)$ as a variable-resolution image. An example of a variable-resolution image is shown on the right in Figure 2. Again, the original unprocessed image is shown on the left. The image was processed using a discrete implementation (see Methods, Experiment 1) of the integral operation shown in



Convolution



Figure 2 Variable Resolution Produced Using a Position-Varying Gaussian Kernel Equation 3. The processing was performed with a gaussian kernel whose size varied from $1 \ge 1$ pixels, at the center of the image, to 49 x 49 pixels at the edge of the image.

Since Equation 3 is not of the form which defines a convolution, the Fourier transform cannot be applied to it, and thus an MTF cannot be defined for the system (filter) which was used to operate on the image. Since it is not possible to condition the spectral distribution of an image by multiplying it by the transfer function of the system, it is always necessary to operate in the space domain by solving the integral equation which represents the operation of a filter whose form depends on position.

Unlike the convolution operation of Equation 1, which can be performed only in the context of linear, position-invariant systems, the integral operation described by Equation 3 may transform a bandlimited signal into a signal whose bandwidth is not limited. In the case of systems which are linear and position-invariant, this cannot occur as can be concluded most easily from an examination of the operation in the frequency domain. Since the convolution integral is transformed into the product of the spectrum of the input signal and that of the MTF of the system, it is clear that no extra frequency components can be introduced. It is well known, however, that nonlinear systems introduce frequency components which are not present in the input signal. Extra frequency components or bandwidth expansion can also result from a superposition integral of the type shown in Equation 3, which represents a linear but position-varying operation.

Bandwidth expansion of an input signal by the addition of frequency components is more often encountered in the case of nonlinear operations (i.e., nonlinear systems). However, this type of bandwidth expansion can also result from the operation of a system which is linear but *position-varying*. Consider a signal which is bandlimited and thus satisfies the Nyquist condition. If the signal is transformed by distorting the position axis, the resulting signal no longer satisfies the Nyquist condition in that the signal is no longer bandlimited. The process of distortion is analogous in a way to FM modulation of a bandlimited signal which introduces extraneous frequency components (in fact, extends the band to infinity). The distorted signal, therefore, cannot be represented by a discrete set of samples.

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Locally-Bandlimited Imagery

According to classical sampling theory (Jerri, 1977), a signal (or image) must be convolved with a sinc function (low-pass filtered) prior to being sampled so that its bandwidth is appropriately (inversely) related to the required sampling interval. This filtering operation projects the image into a space of *bandlimited functions* (BLFs) so that it can be represented using a finite sampling rate. There are infinitely many such spaces, denoted B^{Ω} , each defined by its associated bandwidth, Ω (see e.g., Zeevi & Shlomot, 1993).

There are certain conditions, however, under which an image can be represented by a finite number of samples even if it is not bandlimited. For example, if we had begun with a bandlimited image and applied our variable-resolution procedure to it, the resulting image would no longer be bandlimited. However, because the underlying distortion function, used to alter the spatial distribution of information in the image, is of a form for which an inverse exists (cf., Clark, *et al.*, 1985), that inverse can be used to restore the image to one whose information is distributed uniformly and which is again bandlimited. In this case, the generalized sampling procedure can be applied and the resulting variable-resolution image can be completely represented by a finite set of samples. Images which are not bandlimited but can be converted to bandlimited images by the application of the inverse of a distortion function are said to belong to the space of *locally-bandlimited functions* (LBLFs). This space is denoted by B_{γ}^{Ω} , where Ω is now the local bandwidth (see below), and γ corresponds to the associated distortion function.

As noted earlier, in the case of variable-resolution images the integration kernel is *spatially varying* and therefore the associated integral operation (Equation 3) is not a convolution. Nevertheless, assuming that the integration kernel is a sinc-function, this operation projects images onto a well-defined space of LBLFs (Zeevi & Shlomot, 1993). Analogous with the bandwidth which defines each space of BLFs, there is a measure, called *local-bandwidth*, which defines each space of LBLFs. The concept of local bandwidth may at first appear to be ill-defined in that it seems to be self-contradictory according to the uncertainty principle. According to this principle, in order to have a limited bandwidth, the function has to be of infinite extent and the information regarding the bandwidth (which determines in turn the resolution in frequency) is determined in relation to the entire extent of the signal. The term local bandwidth implies that the frequency characteristics are derived from local properties, hence the

contradiction. It is therefore important to elaborate on this issue. The concept of local bandwidth can best be understood in the context of signal representation in the combined position-frequency space where a different bandwidth can be specified for each position (within the limitations imposed by the joint uncertainty; Gabor, 1946). Thus, one interpretation of local bandwidth is that the local properties of the image can be used to determine a transformation of it which will produce a globally bandlimited image (i.e., one that belongs to B^{Ω}). Another interpretation of the local bandwidth can be understood in the context of a position-varying MTF analogous to the one introduced by Zadeh (1952) in his analysis of time-varying systems. In analogy to the formalism proposed by Zadeh, the MTF is a function of both position and frequency, and as such, one can formally define the local bandwidth for a given position. Similarly, Horiuchi (1968) proposed that if a signal can be obtained by the inverse Fourier-like operation defined as follows:

$$f(x) = \frac{1}{2\pi} \int_{-\pi W(x)}^{\pi W(x)} F(x, \omega) \exp(i\omega x) d\omega$$
(4)

where $F(x,\omega)$ is a position-dependent, Fourier-like, transform of f(x), then the signal has a position-varying bandwidth W(x). Zeevi and Shlomot (1993) extended the concept of position-varying bandwidth by showing that any signal which belongs to B_{γ}^{Ω} , is also characterized by a local bandwidth.

Once an analogy is drawn between uniform and nonuniform operations, the concepts of "local bandwidth" and " B_{γ}^{Ω} " (and their application to the generation of variable resolution imagery) become relatively simple and straightforward. It should be stressed that the proposed technique for projecting a given image into B_{γ}^{Ω} is the proper way of dealing with the issue of variable resolution in that the resultant local properties are well-defined, and in that such an image can be represented by a (finite) set of samples and reconstructed without any aliasing effects even though it is not bandlimited and as such does not satisfy the Nyquist condition. Further, such a technique permits additional nonuniform processing in the form of nonuniform pyramids and other schemes (Peterfreund & Zeevi, 1992; Zeevi *et al.*, 1988).

Sampling Nonuniform Images

If an image has been transformed (e.g., into a variable-resolution image) by a known

distortion function, there are in principle two ways by which it can still be represented by adiscrete set of samples. First, the signal can be restored (undistorted) and then represented like any other bandlimited signal. Image reconstruction is then performed in accordance with the provisions of the Whittaker-Shannon sampling theorem using an interpolation filter in the form of a sinc function (cf., Jerri, 1977). Stated another way, if an image can be projected into the space of BLFs by a transformation along the spatial axis, then it can be adequately represented by a discrete set of samples. The second way of representing a transformed image by a discrete set of samples is to distort and position the interpolation functions (sinc functions) nonuniformly in accordance with the positional distortion function, and then represent the signal even though it is not bandlimited and as such does not satisfy the Nyquist condition (Clark *et al.*, 1985; Zeevi & Shlomot, 1993).

If the distortion function, as described above, is not known, or if it is not known whether the image even belongs to the space of LBLFs, a number of theoretical and practical questions arise. For example, if it is not known what type of nonuniform processing was used on a given bandlimited image to generate a variable resolution image, how can it be determined whether the latter belongs to any space of LBLFs and, if so, to which of the infinite number of such spaces? Theoretically, in order to determine whether an image belongs to a particular space of LBLFs, one would have to first apply the nonuniform filter which would project that (or any other) image into that space. If the resultant image is identical to the original one, this implies that the image belonged to the space to start with, and that the space itself is a so-called reproducing kernel space (Aronszajn, 1950). Since there are infinitely many such spaces, it is not possible of course to proceed in this way. The alternative, practical, approach is to devise techniques for estimating a distortion function which optimally matches the nonuniform distribution of information over the image field. The techniques might be based on estimating statistically the rate of zero-crossings from a number of images, or by estimating the effective local bandwidth which characterizes the representation of the image in some combined position-frequency space, such as those based on the Gabor scheme, the Wigner distribution, or the complex spectrogram (cf., Zeevi & Shlomot, 1993). Estimation of the optimal distortion function will determine which of the infinite number of locally bandlimited image spaces the given image fits best in the sense of having a minimal distance from the original image according to some criterion. Several techniques have been proposed by Zeevi and Shlomot (1993) for estimating the distortion function which best represents a given image in that once the corresponding projection to the (well-defined) space of LBLFs is performed, a minimal least-mean-square error results.

In the context of the present study, the problems are somewhat simpler because either the exact distortion function, corresponding to a given image, is known or the type of nonuniform processing applied to a bandlimited image is known and, as such, can be used in estimating the distortion function. As a practical matter, we need to determine how to nonuniformly distribute the sampling points such that the interpolated variable resolution image will be transformed into an LBLF. Starting with a standard (uniform-resolution) image, how can one devise a nonuniform filter which will result in the desired distribution of resolution across the image while at the same time providing a formalism which satisfies certain theoretical constraints related to the proper representation of the image by a set of sampling points and the reconstruction of the image from that set with no aliasing effects?

Sampling Locally Bandlimited Images

The purpose of development of the variable resolution technique is its eventual application in efficient image representation in flight simulators (and other types of high-fidelity, wide field-of-view display systems). Thus, for the purpose of image storage and/or manipulation, it is desired to exploit the variable-resolution properties of the image such that the data set can be reduced accordingly. In fact, this is the very reason for generating variable resolution imagery. In some flight simulators, computer-generated images are stored and manipulated as a discrete set of points, (i.e., a two-dimensional erray of samples). The question then is, how should the sampling points be nonuniformly distributed over the image field such that they adequately represent the image in the sense that the variable resolution image can be reconstructed from this set of sampling points. Intuitively, it is clear that as the data become more sparsely distributed as a result of variable resolution processing, the required density of sampling points decreases. A sampling theorem for images which belong to B_Y^{Ω} was first introduced by Clark, *et al.* (1985). This theorem was extended by Zeevi and Shlomot (1993) to allow images to be sampled using other than rectilinear patterns. As stated earlier, Zeevi and Shlomot also showed that the kernel which projects images into B_Y^{Ω} is a reproducing kernel. A formalism for reconstructing an image, f(x), from a properly chosen set $\{x_n\}$ of nonuniformly distributed samples will now be described.

To highlight the analogy that exists between uniform and nonuniform sampling schemes and to better understand the latter, we consider first the case of uniform sampling. Let $g(\mathbf{x})$ belong to the space B^{Ω} (i.e., assume that the area of support, Ω , defined by its spectrum is limited), and let the periodicity matrix, U, represent the periodic extension of the spectrum, $G(\omega)$, associated with the sampling operation. Then, $g(\mathbf{x})$ can be reconstructed (interpolated) from its samples along the uniform grid, $\mathbf{x}_n = \mathbf{V}\mathbf{n}$, [where the sampling matrix, V, satisfies the condition that the inner product of U and V equals a constant times the identity matrix, (i.e., $\mathbf{U}^t \mathbf{V} = 2\pi \mathbf{I}$)], according to the following formula:

$$g(\mathbf{x}) = |\det \mathbf{V}| \cdot \sum_{n} g(\mathbf{x}_{n}) \cdot \phi(\mathbf{x} - \mathbf{V}\mathbf{n})$$
(5)

where $g(x_{\mu})$ represent amplitudes of the interpolation function, $\phi(x)$, defined by,

$$\phi(\mathbf{x}) \stackrel{\Delta}{=} \frac{1}{4\pi^2} \iint_{\Omega} \exp(i\omega^t \mathbf{x}) \, d\omega \tag{6}$$

Thus $\phi(x)$ represents the Fourier transform of a rectangular pulse of unit height and dimension Ω x Ω (i.e., a 2-D sinc function).

We now extend the above theorem to include functions which belong to B_{γ}^{Ω} . If $g(\mathbf{x})$ is a globally BLF (i.e., if $g(\mathbf{x}) \in B^{\Omega}$), then $f(\mathbf{x})$ is a LBLF (i.e., $f(\mathbf{x}) \in B_{\gamma}^{\Omega}$), if and only if, a distortion function, $\gamma(\mathbf{x})$, exists such that $f(\mathbf{x}) = g[\gamma(\mathbf{x})]$ (i.e., such that $f(\mathbf{x})$ can be expressed as a function of g, and hence is also a member of B^{Ω}). Note that if $\gamma(\mathbf{x}) = \mathbf{x}$, then the two above-described spaces become identical. Such an LBLF can be reconstructed from the properly distributed set of samples, $\{\mathbf{x}_n\}$, where $\mathbf{x}_n = \gamma^{-1}(\mathbf{V} \cdot \mathbf{n})$, according to the following formula:

$$f(\mathbf{x}) = g[\gamma(\mathbf{x})] = |\det \mathbf{V}| \cdot \sum_{n} g(\mathbf{V}\mathbf{n}) \cdot \phi[\gamma(\mathbf{x}) - \mathbf{V}\mathbf{n}]$$
$$= |\det \mathbf{V}| \cdot \sum_{n} f(\mathbf{x}_{n}) \cdot \phi[\gamma(\mathbf{x}) - \mathbf{V}\mathbf{n}]$$
(7)

which represents interpolation using "uniformized" samples. Note that the effect of $\gamma(x)$ was to change the distance between pulses resulting in nonuniform sampling and a partial overlap of $G(\omega)$. The resulting function is not bandlimited and hence aliasing could occur.

The implementation of the above formalism can be better understood by considering the reconstruction of a one-dimensional signal in which case Equation 7 becomes:

$$f(x) = \sum_{n=-\infty}^{\infty} f(x_n) \cdot \operatorname{sinc}[\gamma(x) - n]$$
(8)

where sinc(x) $\stackrel{\Delta}{=}$ sin(πx)/ πx .

Substituting $\gamma(x) = W(x) \cdot x$ into Equation 8 yields:

$$f(x) = \sum_{n=-\infty}^{\infty} f(x_n) \cdot \operatorname{sinc}[W(x) \cdot x - n]$$
(9)

where W(x) provides a measure of the sampling density and of the local bandwidth. As noted above, if $\gamma(x) = x$, the function f(x) belongs to B^Q. Indeed, in that case, W(x) = 1 and we have uniform sampling density, and Equation 9 becomes the standard equation of interpolation from a uniformly distributed set of samples.

EXPERIMENT 1. PERCEPTUAL ASSESSMENT OF WIDE-FIELD, VARIABLE-RESOLUTION IMAGERY

INTRODUCTION

The well-documented variations in spatial discrimination across the visual field (Levi, Klein, & Aitsebaomo, 1985; Rovamo & Virsu, 1979; Virsu, Näsänen, & Osmoviita, 1987) suggest that conventional, position-invariant processing techniques cannot produce images which are efficiently matched to the human visual system. In order to match the spatial inhomogeneities of the human visual system, images must be processed in a position-varying manner. This would be necessary, for instance, to effectively implement high resolution over a wide field of view given limited computational and bandwidth resources (Zeevi *et al.*, 1990). Techniques have recently been developed (Peterfreund & Zeevi, 1990; 1992; Zeevi & Shlomot, 1993; Zeevi *et al.*, 1988) for filtering images by position-varying techniques in a manner analogous to the low-pass filtering performed prior to sampling with fixed sampling rate (i.e., position-invariant sampling).

As noted above, the information processing capability of the human visual system decreases from the center of the visual field to the visual periphery. A so-called cortical magnification factor (CMF) can be specified which relates the sensitivity at a given retinal eccentricity to that at the fovea. The CMF is presumed to reflect the relatively greater number of cortical cells associated with a given retinal area near the fovea as compared to an equivalent area in the periphery (Daniel & Whitteridge, 1961; Talbot & Marshall, 1941; Van Essen, Newsome & Maunsell, 1984). Thus, it follows that, for those visual tasks that can be scaled, the number of cortical cells stimulated can be equated for stimuli in the center and periphery if the latter are appropriately magnified.

In Experiment 1, test images were generated using a position-varying filter whose bandwidth decreased as a function of distance from the center of the image. The specific functions tested were chosen to approximate the observed variation in the CMF across the visual field (Rovamo & Virsu, 1979). There are disagreements in the literature as to the specific function that relates CMF to eccentricity (Dow, Snyder, Vautin & Bauer, 1981; Levi *et al.*, 1985; Rovamo & Raninen, 1984), but this issue is not addressed here. Rather, several candidate linear functions were chosen that differed in central blur (at 8° eccentricity), peripheral blur (at 40° eccentricity), and the blur gradient between 8° and 40° eccentricity. The function that produced a blur gradient which was just discriminable from an unprocessed image was taken as the distortion function which may in turn be used to efficiently sample (i.e., subsample) real-world images such as those used in visual simulators. Although the processing performed here is not strictly an image magnification, there is some analogy in the change in spatial frequency content of the images resulting from these two procedures. Thus, given that formal procedures have been developed for sampling and generating variable-resolution imagery (Clark *et al.*, 1985; Zeevi *et al.*, 1988), this imagery may be most useful for producing efficient visual simulation.

METHOD

Generation of Variable-Resolution Images

A locally bandlimited variable resolution image can be produced only by using a projection technique, similar to that described by Equation 3, wherein a (variable) sinc function is used as the integration kernel. Such a technique is computationally intensive and relatively difficult to implement, we have, therefore, chosen an alternative technique which uses an integration kernel based on a gaussian function whose space constant varied with position in the image. Although this approach does not conform to any complete formalism, which might otherwise be used to fully characterize the resulting image for the purposes of further processing and representation, it is sufficient for obtaining preliminary psychophysical data.

Because we desire the final variable-resolution image to be radially symmetric (i.e., to display the same amount of degradation at all points equidistant from the center), it is convenient to first transform the original image from cartesian to polar coordinates before applying the various distortion functions that determine how the low-pass characteristics change across the image space. In fact, the polar-coordinate representation is inherently appropriate for generating variable-resolution imagery in that it allocates a larger area to central areas of the cartesian version of the image than to peripheral ones. Also, it presents the image data points in an ordered manner that makes the integration (or summation in the discrete case) more convenient. After the integration operation was performed, the image was transformed back into the cartesian coordinate system. Variable-resolution images were then generated using a discrete implementation of the integral operation described by Equation 3:

$$l_o(x,y) = \sum_{m} \sum_{n} l_i(x',y') \cdot k(x,y,x',y')$$
(10)

where k is the gaussian summation kernel (see Appendix A). The width of the kernel varied along both the radial and angular coordinates and was determined by sampling a function of the form:

$$k(x, x', y, y') = \exp\left[-\left[\frac{(x-x') + (y-y')}{D}\right]\right]$$
(11)

where x' and y' are the coordinates of the image pixel over which the summation kernel was centered, and D is the effective width $(\pm 1\sigma)$ of the gaussian. The summation kernels varied in size from 3 x 3 to 13 x 13 pixels. Following the summation operation, the image was transformed back into the cartesian coordinate system. A transformation from cartesian to polar coordinates and back may result in approximation errors since sampling is discrete and hence not all transformed points can be accurately represented in both coordinate planes. At the level of resolution used in the present study, the transformation did not generate any noticeable image degradation which might have been mistaken for variable resolution.

The linear functions shown in Figure 3 were chosen to vary the parameters which specified the integration kernel as a function of distance from the center of the image. These functions were chosen to approximate, to varying degrees, the cortical magnification functions (CMFNs) derived from anatomical and psychophysical data (Dow *et al.*, 1981; Rovamo & Virsu, 1979). The full set of functions shown in Figure 3 allows an assessment of central blur, peripheral blur, and blur gradient, although all of these factors were not tested independently of the others. Linear functions were considered acceptable since they give a good approximation to published CMFNs. For instance, between 8° and 40° eccentricity, the CMFN suggested by Rovamo and Virsu is nearly linear and varies from 7 to 9 (corresponding here to our kernel size) over that range.

The stimuli used in the present study extended from 8° to 40° eccentricity. The central portion of the stimulus was removed for two reasons. First, the CMFN changes rapidly near the fovea and the available display resolution was not high enough to give an accurate representation in that portion of the visual field. Second, it was expected that observers would find it difficult to distribute their attention over a stimulus area that was 80° in diameter. This would have been especially difficult if they were asked also to attend to visual detail presented at or near the fixation point.

Observers

The observers were two males (SF and GG) and one female (KV) who were 25, 41, and





24 years of age, respectively. All observers had normal uncorrected vision. Observers SF and KV were paid for their participation, while observer GG was one of the authors.

Stimuli and Apparatus

Two real-world aerial photographs were digitized, and four stimulus templates were constructed by pairing each half of the two photographs with its mirror image and removing a portion of the center of the image. One-half of each stimulus was then low-pass filtered (i.e., blurred) in accordance with one of the functions of Figure 3. Two of the stimulus templates, corresponding to one blur gradient (much higher than those used in the present study) applied to the left half of each image, are shown in Figure 4. The programs used to produce the stimulus templates for both Experiments 1 and 2 are presented in Appendix B. The full stimulus set consisted of 108 images. Of these, 84 were test stimuli corresponding to the four image templates each processed at one of the 21 filter gradients. The remaining 24 stimuli were control stimuli consisting of each image template processed on both sides by one of seven (i.e., 1 x 1 through 13 x 13) kernels. An equal number of test and control stimuli were presented in each session. The functions in only one panel of Figure 3 were tested in a given session, which included presentation of all four image templates. In a given session, the test stimuli were presented with the unprocessed image appearing on the right 10 times and on the left 10 times. Each control stimulus was accordingly presented 20 times per session since no distinction could be made between the left and right halves of these stimuli. Between two and four sessions were run for each observer under the four conditions corresponding to panels of Figure 3. All stimuli were presented 1m from the observer and they extended radially for 40° from a fixation point located at the center of the image. Stimulus duration was 167 msec. The observer was seated and used a chin and head rest to maintain a constant position relative to the screen.

All image presentation and data collection were under the control of a Silicon Graphics Iris workstation. The stimuli were presented using the green channel of a Sony Superdata CRT projector (Model VPH-1270Q), and a rear-projection screen (Lumiglass 350, Stewart Film Screen Corp.). Subject responses were made using a mouse interfaced with the computer. Display luminance was measured using a Photo-Research Model 1500 photometer. The gamma-function for the green CRT channel was measured and linearized using an 8-bit look-up





Figure 4 Two of the Image Templates Used in Experiment 1 table. In addition, a luminance measurement was obtained at 24 equally spaced points between the center and edge of the display area in order to correct for the luminance gradient caused by the projector optics and the directional properties of the rear-projection screen. The luminance gradient was corrected off-line by appropriately adjusting the 8-bit gray scale of each stimulus image. The mean luminance of the stimuli was 0.5 fL.

A set of MTFs for the display system was calculated from horizontal and vertical line-spread functions associated with lines of lighted pixels located at the center of the display and at points 12° and 28° from the center in both directions along the horizontal meridian. Measurements were made using a Photo-Research (Model PR-719) Spatial Scanner, and software (see Appendix C) that implemented the procedures for calculating MTFs described by Kelly (1992). The horizontal and vertical MTFs calculated for the display system are shown in Figures 5a and 5b, respectively. The horizontal MTFs (each calculated from a vertical line of pixels) were virtually identical at all points tested across the screen. There were, however, differences in the vertical MTFs for those same points. As a result, a residual blur gradient was effectively added to all horizontally oriented stimulus features. However, as the data of Figure 5b show, this gradient was relatively small and in a direction opposite to that of the gradients evaluated in the present study. Further, in the present study, an unprocessed image was presented on all trials, and because both the horizontal and vertical MTFs measured at a given distance from the center of the image were similar, no differential response would be expected based on the measured differences in display MTF. The data presented here should, however, be taken as conservative estimates of the observers' sensitivity to image blur since higher sensitivity would be expected had the residual blur been removed.

Procedure

Each experimental session began with a 5-10 min period of adaptation to the low ambient illumination of the experimental room. The observers then viewed, for 2-3 min, the center of an illuminated screen, which was the same size and had the same mean luminance as the experimental stimuli. The observer initiated the experimental session using a mouse, and the first stimulus appeared within 3-4 sec. The observers were asked to respond as to which half of the image appeared to be more blurred. There were 3-4 sec between the observer's response and the next









stimulus. The experimental session consisted of between 320 and 480 stimulus presentations broken up into three subsessions each consisting of as close to one-third of the trials as possible. The observers controlled the amount of time between each subsession and could also initiate rest periods within the subsessions by delaying their response. A mean-luminance screen was present between stimuli and during all rest periods.

RESULTS

The discrimination data obtained from the three observers are summarized in Figures 6a, 6b, and 6c, respectively. The data for both the bomber and city images were similar and so all data were pooled for each observer. The four plots associated with each observer correspond to the four sets of variable-resolution functions tested. Based on the percentage of correct responses (%C), three levels were used to categorize the observers' ability to discriminate an unprocessed image from an image processed according to each of the functions within each set. The dark-shaded areas of Figure 6 encompass the variable-resolution functions that were discriminated more than 85% of the time, while the white areas encompass the functions that were discriminated at near the chance level (<65%C). The functions discriminated between 65% and 85% of the time were defined as being at or near threshold, and are identified by the gray-shaded areas in the figure.

The data of Figure 6 show that observer SF was able to discriminate the low-pass filtered images somewhat better than observer GG who, in turn, was somewhat more sensitive than observer KV. Despite these quantitative differences, all observers showed qualitatively similar patterns of sensitivity across the four sets of stimuli tested. For instance, whereas discrimination performance declined as the size of the integration kernel applied to the peripheral edge of the image was decreased, the decline could be compensated by a (generally smaller) increase in the size of the kernel used at the more central edge of the image.

DISCUSSION

The second function from the top in the third panel of Figure 3 most closely approximates the human CMFN suggested by Rovamo and Virsu (1979). When the data for all three observers





SIZE OF INTEGRATION KERNEL (pixels)



are taken together, this function is at or near threshold as defined in the present study. Of course, many of the other functions are also at or near threshold by that definition. It was not the purpose of the present study to estimate the CMFN, but rather to use the CMFN as an initial estimate of the threshold blur gradient for wide-field imagery.

The slope of the CMFN that produced a minimally discriminable image in the present study was very similar to the slopes estimated from luminance and contrast sensitivity data (Johnston, 1987; Rovamo, 1983; Rovamo, Virsu, & Näsänen,1978). This similarity at least suggests that the discrimination of blurred images may be dependent on image properties defined by such fundamental measures as component spatial frequency and orientation. Further, similar data have been obtained here for visually diverse, complex images, suggesting that the visual equivalence of variable-resolution images is independent of local variations in image detail.

The data of Figure 6 will be used below (see General Discussion) to estimate the minimal sampling rate required to adequately represent typical real-world imagery. In the context of image representation schemes recently reported (Ebrahimi & Kunt, 1991; Porat & Zeevi, 1988), these data may be used to generate efficient imagery that consists of only those spectral components to which each region of the visual field is sensitive (cf. Zeevi *et al.*, 1990).

EXPERIMENT 2: BLUR DISCRIMINATION AS A FUNCTION OF IMAGE CONFIGURATION AT 15° AND 30° ECCENTRICITY

INTRODUCTION

The data of Experiment 1 suggest that wide-field images processed using position-varying filters can appear preattentively similar to an unprocessed image for certain processing gradients. Furthermore, processing near the center of the image can be effectively exchanged for processing in the periphery in such a way as to maintain the perceptual equivalence of the image and its unprocessed counterpart. In Experiment 2, sensitivity to image blur was measured for circular and radial-segment apertures of various sizes. Data were obtained at 15° and 30° eccentricity in order to determine whether there are differences in the spatial properties of the visual mechanisms

underlying the detection of image blur at these two eccentricities.

METHOD

Observers

Data were obtained from three observers, one of whom (GG) participated in Experiment 1. Observers CT and DW were males, 20 and 26 years of age, respectively. Each had normal uncorrected vision. Observers CT and DW were unaware of the purpose of the study, and each was paid to participate in this experiment.

Stimuli and Apparatus

Three images were used as stimuli in this experiment. Two of the images were those used in Experiment 1, and the third was a black-and-white, one cycle/degree, radial square wave. The stimuli were chosen to represent three levels of spatial homogeneity (bombers, lowest; square wave, highest). The 1024 x 1024 x 8-bit images were processed by convolution (Equation 1) with gaussian kernels again varying in size from 3 x 3 to 13 x 13 pixels. The test stimuli were produced by applying either a circular or radial-segment aperture (see Figure 7) on both sides of the fixation point of both the original and processed images. The apertures were centered at either 15° or 30° along the horizontal meridian. The sets (circular and radial-segment) of stimuli presented at 15° eccentricity had areas of 8.4, 16.8, 25.2, 33.5, and 41.9 deg². The sets presented at 30° eccentricity had areas of 16.8, 33.5, 50.3, 67.0, and 83.8 deg² (i.e., corresponding to a magnification factor of two relative to the stimuli presented at 15°). The display system was identical to that used in Experiment 1.

Procedure

The testing procedure was identical to that of Experiment 1. In a given experimental session, all three stimuli and all five stimulus areas were tested (30 repetitions for each of the 15 conditions) for one eccentricity, one stimulus configuration, and one level of processing (i.e., blurring). Three randomized blocks of trials were run in each session, with the three stimulus types processed at one kernel size determining the block. For each of the three stimulus types, the five stimulus areas were tested in a random order as a sub-block. Each experimental session



Figure 7 The Circular and Radial-Segment Apertures Used to Define the Stimuli Used in Experiment 2 consisted of 450 trials, and required about 45 min to complete. For each observer, between three and five experimental sessions were run for each combination of eccentricity, stimulus configuration, and kernel size.

RESULTS

Shown in Figure 8 is a typical set of response functions used to estimate blur discrimination thresholds. The data of Figure 8 were obtained at 15° eccentricity for the lowest level of stimulus homogeneity (i.e., H1, the bombers) and represent an average over all three observers. The two sets of data in each panel correspond to either the circular (filled circles) or radial-segments stimuli, and the five panels correspond to the five stimulus areas tested. The data points in each panel show the proportion of correct responses as a function of the size of the summation kernel used to process the stimuli. As the summation kernel increases in size, the amount of blur increases and the proportion of trials for which the processed stimulus is discriminated from its unprocessed counterpart also increases. The functions placed through the data in each panel of Figure 8 represent the best fitting Weibull distribution of the form:

$$P = 1 - 0.5 \exp\left[-\left(\frac{K}{K_t}\right)^s\right]$$
(12)

where P is the proportion of correct responses, K is the kernel size, K_t is the threshold kernel size (corresponding to P = 0.816), and s determines the steepness of the function. The function of Equation 12 was fitted to the data using the SigmaPlot Scientific Graph System (Jandel Scientific). The horizontal dotted line in the figure indicates a proportion correct of 0.816, which was taken as the threshold response level.

Blur thresholds, estimated from response functions like those of Figure 8, are plotted in Figure 9 as a function of stimulus area for both of the eccentricities tested (15° and 30°) and for all three levels of stimulus homogeneity (H1-H3). The functions obtained for both the circular and radial-segment stimuli show a general decrease in blur threshold as stimulus area is increased, although the decrease was generally greater for the data obtained at 15°. There appears also to be






Figure 9 Blur Thresholds as a Function of Stimulus Area

a difference between the two eccentricities tested in the relative decrease in blur threshold for the two stimulus configurations. In order to test this difference, *t*-tests were performed on each of the differences between the two curves in each of the panels of Figure 9. Because five *t*-tests were performed for each eccentricity/homogeneity condition, the level of significance for the tests described here was reduced to p=0.01. The asterisks placed along the upper axis in each panel indicate the stimulus areas for which the blur thresholds for the circle and radial-segment stimuli were significantly different at this level. The computed *t*-values and degrees of freedom for each of the significant differences indicated by asterisks in the figure were as follows: $t_{af=18} = 3.92$, p<0.002 (H1/33.5); $t_{cc} = 5.28$, p<0.001 (H1/41.9); $t_{18} = 3.23$, p<0.01 (H2/25.2); $t_{20} = 3.06$, p<0.01 (H2/41.9); and $t_{18} = 3.16$, p<0.01 (H3/25.2). As can be seen in Figure 7, the smallest circle and radial-segment stimuli are very similar in shape, and so little or no difference between the stimulus configurations would be expected for those areas. While only five of the thirty differences tested were statistically significant, all of the significant differences were found among the three largest areas at 15° eccentricity.

Shown in Figure 10 is the difference in blur threshold between the 15° and 30° eccentricity conditions for both the circle and radial-segment stimuli and for the only two stimulus areas (16.8 and 33.5 deg²) tested at both eccentricities. For both stimulus areas, the difference in blur threshold between the two eccentricities tested was significantly different from zero for the circles (16.8: t_{18} = 1.00, p<0.01; 33.8: t_{16} = 4.04, p<0.002) but not for the radial segments (16.8: t_{18} = 0.42, p>0.50; 33.8: t_{18} = 0.14, p>0.80).

DISCUSSION

The data of Figure 9 show that there is a general decrease in blur discrimination threshold with increases in stimulus size. This is true for both the circular and segmental stimuli presented at both 15° and 30° eccentricity. There is also an indication in some of the functions that blur threshold has reached an asymptote and is even increasing for the largest stimulus areas. This effect suggests a functional limit to the size of the excitatory portion of the perceptual receptive field (Westheimer, 1967). The fact that the increase in threshold is more obvious for the segmental stimuli further suggests that the perceptual receptive field for these stimuli may be



Figure 10 Difference in Blur Thresholds Between 15° and 30° Eccentricity

organized differently than for circular stimuli. These possibilities will be discussed further below.

The decrease in blur threshold with increases in stimulus area is generally greater for the stimuli presented at 15° suggesting that the effective magnification factor of two applied to the 30° stimuli did not fully compensate for the effect of stimulus area. It should be noted, however, that the difference in the threshold change is larger for the 15° stimuli due mainly to the relatively high threshold at the smallest stimulus size. Given that real-world stimuli were used for homogeneity levels H1 and H2, it is possible that this high threshold is related to the chance absence within the smallest aperture of those stimulus features that are most easily discriminated under the conditions of the present study. This interpretation is supported by the generally lower thresholds at all stimulus sizes for the square-wave stimuli, which were most spatially homogeneous. It is concluded, therefore, that a CMF of two adequately equates the blur discrimination data obtained at 15° and 30° eccentricity.

The difference in blur threshold obtained using circular and segmental stimuli is more obvious and only statistically significant at 15° eccentricity. Although some of the differences at 30° were relatively large, the variability at that eccentricity was also higher thus rendering the differences statistically insignificant. This is not an explanation for the relevant differences between 15° and 30° eccentricity, however, since the divergence at high stimulus areas, of the functions corresponding to the circular and segmental stimuli, is consistent only at 15° for the homogeneity levels tested. Thus, the data of Figure 9 suggest that at 15° eccentricity (and presumably at lesser eccentricities), the visual information required to discriminate image blur is not summated within a constant eccentricity. Rather, the perceptual summation area is more nearly circularly symmetrical. On the other hand, perceptual summation at 30° extends over a relatively large area and is generally unaffected by the spatial distribution of the stimulus.

As noted earlier, two of the areas tested at 15° eccentricity correspond to areas tested also at 30° eccentricity. As can be seen in the data of Figure 10, the difference in blur threshold between 15° and 30° eccentricity for these two areas is much larger for the circular stimuli than for the segmental stimuli. It was concluded above, based on the data from all stimulus areas tested, that a CMF of two was sufficient to equate the blur discrimination data obtained at 15° and 30°. That conclusion is consistent only with the circular data of Figure 10. There appears, however, to be no significant difference in the blur thresholds obtained at the two eccentricities when segmental stimuli are used. This is further evidence of a difference in the spatial properties of perceptual fields at different eccentricities.

GENERAL DISCUSSION

In the case of the variable-resolution images used in the present study, the distortion function is derived from physiological and psychophysical data that describe how visual processing capability decreases with eccentricity. Since the distortion function is known, there are two ways of representing the variable-resolution image by a discrete set of samples without generating artifacts. First, the image can be transformed such that it can be properly represented by a uniform set of samples. This is done by using the inverse of the distortion function to produce a bandlimited image (without loss of information) and then sampling the image uniformly in accordance with the standard Nyquist criterion (Jerri, 1977). Stated another way, if an image can be bandlimited by a transformation which appropriately distorts the spatial axis, then it can be adequately represented by a discrete set of samples. The second way of representing a variable-resolution image by a discrete set of samples is to sample it nonuniformly at a rate determined by the form of the distortion function. The image can then be reconstructed using interpolation functions (i.e., sinc functions distorted in accordance with the nonuniform spatial distortion function). Thus, in this case, the variable-resolution image can be represented by a finite set of sampling points even though it is not bandlimited and as such does not satisfy the Nyquist condition.

In the context of the present study and the applications discussed earlier, we start from a uniform-resolution image and generate a variable-resolution image. The operation performed in this case can be viewed as filtering which is analogous to the bandpass filter applied prior to uniformly sampling an image. The low-pass filtering is performed in our case by convolving the image with a gaussian. This operation does not satisfy the requirement of projecting an image onto the space of BLFs in that the associated measure is an effective bandwidth (Gabor, 1946) and hence is only approximate. [For examples of variable-resolution images generated by filtering with a nonuniform sinc function, see Zeevi *et al.* (1988) and Peterfreund and Zeevi (1992)]. In

the case of nonuniform sampling, the filter applied prior to sampling is nonuniform. In other words, its properties (corresponding bandwidth) vary as a function of position in accordance with visual requirements.

Efficient Sampling of Variable-Resolution Imagery

Numerous image processing and compression techniques have been developed for representing visual images efficiently. These are, in general, based on the redundancy in natural images and the 2-D spatial frequency selectivity of the human visual system (Baddeley & Hancock, 1991; Field, 1987; Reed, Ebrahimi, Marqués, & Kunt, 1991). Variable-resolution imagery takes advantage of another salient property of the human visual system--its spatial inhomogeneity. One practical advantage of variable-resolution imagery, as defined here (see Equation 2), is that it can be adequately (by a visual criterion) sampled by fewer points than its fixed-resolution counterparts. The variable-resolution technique described here was developed to efficiently represent images used in high-fidelity, wide field-of-view displays (Geri, Zeevi, & Porat, 1990). Thus, for the purposes of image storage, manipulation, and transmission, it is desired to exploit the variable-resolution properties of the image such that the data set can be reduced accordingly. The question then is, how should the sampling points be nonuniformly distributed over the image field such that they adequately represent the image in the sense that the variable-resolution image can be reconstructed from this set of sampling points? Intuitively, it is clear that as the data become more sparsely distributed as a result of variable-resolution processing, the required density of sampling points decreases. In theory, the sampling rate appropriate for a given variable-resolution image is determined by the local bandwidth as discussed above. In practice, we do not have an exact measure of the local bandwidth, therefore we have chosen to use the distortion function to obtain the appropriate sampling rate for our variable-resolution images. As noted by Zeevi & Shlomot (1993), the local bandwidth is related to the derivative of the distortion function. According to the sampling theorem for images which belong to the space of LBLFs (Zeevi & Shlomot, 1993), the set of nonuniformly distributed sampling points can be obtained by applying the inverse of the distortion function to the uniform grid. This has been done in one dimension using as a distortion function one of the functions of Figure 3 that was found to be at or near threshold for all of the observers tested in Experiment 1.

Shown on the left in Figure 11 is the chosen distortion function. Shown at the top right in the same figure is a set of uniformly-spaced sampling points (i.e., pixels) corresponding to one-half (from center to edge) of a cross-cut through an image. Shown at the bottom right in Figure 11 is the nonuniform set of sampling points that corresponds to the chosen distortion function. In this case, the operation results in a reduction by a factor of about two in the number of points required for the representation. This would correspond to a reduction of about four when the full two-dimensional image is represented at the indicated sampling rate. It should be noted that this is a conservative estimate of the savings that might be expected from variable-resolution processing of *static* imagery in that the psychophysical technique used here for assessing the perceptual equivalence of the processed and unprocessed images was designed to detect very small differences in the appearance of the images. Much larger differences in the images might be tolerated if the perceptual criterion was recognition or identification, and the associated sampling efficiency in that case would be significantly greater.





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APPENDIX A

The program, *vresfb.c*, used to generate variable-resolution imagery.

Modified: 05-DEC-90 Code was added to allow the processing of binary image files instead of the large ASCII files as originally coded. This program must now be linked with iotools.o Filename: Filename: Filename: Forsig A, Vrana - UDRI Fortan Modified Date: Fortan Modified Date: Fortan Modified Date: Fortan Modified: Fortan Modif Each output pixel represents the average of $K \propto K$ pixels where K is the dimension of the "receptive field" over which the original image is locally averaged. The size of the receptive field, as a function of eccentricity (R), is determined by; $K=B^{4}R+C$, where B and C are constants determined by the particular cortical magnification function chosen. Define the maximum size of the image, in pixels, in one dimension INTEGER MAX IMAGE SIZE PARAMETER (MAX_IMAGE_SIZE = 1024) Define the maximum number of chars in the filename of the image INTEGER MAX NAME SIZE PARAMETER (MAX_NAME_SIZE = 64) Define the maximum size of the weighting kernal INTEGER MAX GAUSS KERNEL PARAMETER (MAX_GAUSS_KERNEL = 75) Define the maximum size for the fmage header INTEGER MAX HEADER SIZE PARAMETER (MAX_HEADER_SIZE = 316) Define the value to be used for Pl. REAL*8 FILE=a:vresfb.f * PAGE=1

```
OPEN(UNIT=10, FILE=imege_name, ACCESS='SEQUENTIAL', ERR=1000, STATUS='OLD', READONLY)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      OPEN(UNIT=20, FILE=file_name, ACCESS='SEQUENTIAL', ERR=4000, STATUS='UNKNOUN')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   Get cmf constants from user
WRITE (SCREEN.*) 'Enter kernel constants (i.e., kl <space> k2 <ret>)'
READ (KEYBOARD,*) kl, k2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Get the name of the output file

MRITE (SCREEN*) 'Enter the name of the output file : *

READ (KEVBOARD,10) file_name
                   mode(1:) = 'r'
mode(2:) = 'r'
mode(2:) = CHAR(0)
in handle = open bfile(image_name, mode, error_code)
wRTE (SCREEN,*) error code
WRTE (SCREEN,*) in handle
IF(error code .ME. 0) THEN
IF(error code .ME. 0) THEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      mode(1:) = 'w'
mode(2:) = 'w'
mode(2:) = CHAR(0)
mode(3:) = CHAR(0)
wrife (SCREEW 'P) error code
wrife (SCREEW 'P) out handle
Wrife (SCREEW 'P) out handle
IF(error code .WE. 0) THEN
IF(error code .WE. 0) THEN
202 mode(1;) = 'r'

202 mode(2;) = CUMI(0)

202 mode(2;) = CUMI(0)

202 mode(2;) = CUMI(0)

202 mode(2;) = CUMI(0)

202 mode(2;) = TUT

202 mode(2;) = 'r'

203 m
```

File=a:vresfb.f * PAGE=3

```
228:
229: C This routine calculates the variable resolution image and returns it
230: C in the out array.
                                                                                                                                                                                                                                                                                                                                                                 Do calculations
Get radial delta value for 40 degrees maximum (degrees per pixel)
dop = 40.0 / half size
WRITE (SCREEN, *) **** Filtering image'
WRITE (SCREEN, *) ****, *
DO 330 x = 0, size-1
DO 330 y = 0, size-1
                                                                                                                                                                                                                                                                                        Isas Converting to Cartesian coordinates'
                                                                                                                                                                                                                                                                               dummy1 = read_bfile(in_handle, num_bytes, c_image(0))
                                                                                                                                                                          weight(y,x,kernel) = w
write(15,98) x, y, w
                                                                                                         'sway Reading image'
                                                                                                                                   uRilfE(SCREEN,*)num_bytes, 'bytes to be read'
                                                                                                                                                                                                                                        error code = close bfile(in handle)
WRITE (SCREEW,*) error code
IF (error code .NE. 0) THEN
GOTO 2010
                                                                                                                                                  READ(10,*)(c_image(d),d=0,num_bytes-1)
                                                                                                                                                                                                                           CLOSE(10, ERR=2010, STATUS='KEEP')
                                                          ENDIF
                                                                                                                      num_bytes w size*size
                                                                                                        WRITE (SCREEN,*)
                                                                                           close(15)
                                                                                                                                                                                                 ENDIF
                                                                                                                                                                                                                                                                     ENDIF
                                                                                                                                                                                                               Close file
                                                                             CONTINUE
                                                                                                                                                                                                                                                                                                                   200 CONTINUE
   LIRITE
                                                                             5
```

FilE=a:vresfb.f * PAGE=4

t = (image(ypn, zpm)*u = month u = weight(abch, abam,kernel) NIM ensures we don't go past end of image ypn = NIM (y + n, size-1) ypn = NAX (ypn, 0) xpm = NAX (xm, 0) tym = NAX (xm, 0) tym = MAX (zm, 0) tym = MAX (zm, 0) tym = MAX (zm, 0) t = (image(ypn, zpm)*u) + t IF (WSLM .LT. 0.0001) THEN WRITE(SCREEM,*) 'MSLM = 0 x = ',x,'Y = ',Y dummy1 = write_bfile(out_handle, num_bytes, c_image(0)) WRITE (SCREEN *) 'Mumber of bytes written = ', dummy1 IF (dummy1 .WE. rum_bytes) THEN GOTO 4010 WRITE (SCREEM.*) '==> Converting to linear array.'
D0 400 x = 0 size-1
D0 400 y = 0, size-1
course. 1ABS(m) -t, t absn = 1ABS(n) WRITE(SCREEN,*) '==> Scaling image', mi, ma WRITE (SUREEN.*) *==> Writing image' WRITE(20,500) (c image(d),d=0,num_bytes-1) FORMAT(16(1%,13.3)) ELSE out(y, x) = NINT(t/wsum) ENDIF Close file CLOSE(20, ERR≖4030, STATUS≖'KEEP') t = 0.0 weum = 0.0 bo 320 m = -k, k abem = 1A po 320 n = -k, CONTINUE ENDIF CONTINUE CONTINUE

fltE=a:vresfb.f * PAGE=5

WRITE (SCREEN,*) 'Could not open', file_name, '\bfor writing.' WRITE (SCREEN,'(AI3A)') 'UNIX error code *', error_code, '.' STOP error_code = close bille(out_handle)
if (crrcr_code wf. 0))"HEH
if (Fror_code wf. 0)"HEH
if (fror code wf. 0)"HEH
if (fror wf. 0)"HHH
if (fror wf. 0)]
if (fr WRITE (SCREEN,*) 'Error reading from ', image name, '\b.'
WRITE (SCREEN,'(AI3A)') ' UNIX error code =', error_code, '.'
STOP WRITE (SCREEN,*) 'Error writing to', file name, '\b.' WRITE (SCREEN,'(AI3A)') ' UNIX error code =', error_code, '.' STOP WRITE (SCREEN,*) 'Error closing', file name, '\b.'
WRITE (SCREEN,'(AI3A)') ' UNIX error code =', error_code, '.'
STOP

FILE=a:vresfb.f * PAGE=6

APPENDIX B

The programs used in the experimental portion of Experiments 1 and 2. Programs opaste.c, slice.c, and vcirc.c were used to generate the experimental stimuli from the unprocessed original images and the associated variable-resolution images. Program scale.c was used to apply the luminance gamma-correction as well as the correction for luminance variations across the image caused by projector optics and the directional properties of the rear-projection screen. Program segs.c was used to present the experimental stimuli and collect the observers' (csuonses in Experiment 2, and was similar to the program used for this purpose in Experiment 1. Finally program asegs.c was used to analyze the observers' responses.

/* value to set gap to /* max number of chars in filename */ /* default image extension */ /* max number of pixels in one line */ /* The number of pixels between images */ * Modified: 16-NOV-90 Added the gap size to the command-line argument list in order to allow the user to controll the gap-size when executing this program. Modified: 06-DEC-90 Fixed problem of entering the default gap size and having the program continue waiting fro input of a gap size. opeste.c Craig A. Vrana 25-SEP-89 06-DEC-90 buffer1 [MAX_INAGE_SIZE] buffer2[MAX_INAGE_SIZE] but_line_buf[MAX_INAGE_SIZE], *p2, *p2; *p3; input left(FileNAME SIZE) input right(FileNAME SIZE), output[FileNAME_SIZE], side to use(2) gap_size[5]; 64 1024 60 Program: Created by: Creation date: Last Modified: void main(int argc,char *argv[]) (2 byte: word: W define BACKGROUND # define FileNANE SIZE # define MAGE EXTENSION # define MAX_IRAGE_SIZE # define GAP_ gap, in_size1, in_size2, out_size, typedef unsigned char typedef unsigned int include <stdio.h> include <string.h> include <ctype.h> <u>n</u> byte word char ٤ -

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* * *

FilE=a:opeste.c * PAGE=1

FllE=a;opaste.c * PAGE=2

/* get which half of each image to use */
printf ("Enter r or l for the half of the images to paste to gether: ");
scanf ("%s", side to use);
side to use[0] = Toupper(side to use[0]);
printf("Using %s side of images."n", side to use); fprintf (stderr, "Could not open %s for reading. \n", input_left); /* get right input filename */
printf ("Enter right side input filename (.IMG): ");
scanf ("Xs", input_right); strcpy(input_left, argv[1]); strcpy(input_right, argv[2]); strcpy(side to_use, argv[4]); strcpy(side to_use, argv[4]); strcpy(gap size, argv[5]); gap = ((int)atoi(gap_size)/2)*2; printf("Using %d pixel gap between images.\n", gap); /* get left input filename */
printf ("Enter left side input filename (.1MG): ");
scanf ("Xs", input_left); /* get the gap size in pixels */ printf ("Enter gap size in pixels: <‰d>", GAP); if(scanf ("‰d", %gap) != 1) { printf("Did not receive a gap size.\n");
gap = GAP; /* get output filename */
printf ("Enter output filename (.IMG): ");
scanf ("Xs", output); /* open input file and setup buffer */
if ((inl=fopen(input_left, "r")) == NULL) strcat (input_left, IMAGE_EXTENSION); fprintf(stdout,"argc = %d\n", argc); /* append .img if necessary */
if (strrchr(input_left, '.')==KULL) *out; *in1, *in2. if(argc |= 6) else (FILE ~ J ~ J 1

```
while (side_to_use[0] == 'L') /* Paste teft halves of images together*/
                                                                                                                         fprintf (stderr, "Could not open %s for reading.\n", input_right);
exit (1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      /* read in one input line */
if (fread (buffer1, sizeof(byte), in_size1, in1) !* in_size1)
break;
if (fread (buffer2, sizeof(byte), in_size2, in2) !* in_size2)
if (break;
                                                                                                                                                                                                                                                    fprintf (stderr, "Could not open %s for writing.\n", output);
exit (1);
                                                                                                                                                                                                                                                                                                                                                                                                            printf("\nThe two input images are different sizes.\n");
                                                                                                                                                                                                                                                                                                       in_size1 = 1024; /* Change here for larger images */
in_size2 = 1024; /* Change here for larger images */
                                                                                          /* open input file and setup buffer */
if ((in2=fopen(input_right, "r")) == NULL)
                                                             strcat (input_right, IMAGE_EXTENSION);
                                                                                                                                                                           /* append .img if necessary */
if (strrchr(output, '.')==NULL)
strcat (output, IMAGE_EXTENSION);
                                                                                                                                                                                                                    /* open output file */
if ((out=fopen(output, "w")) == NULL)
                              /* append .img if necessary */
if (strrchr(input_right, '.')==WULL)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     p1 = buffer1;
p2 = buffer2 + in_size2/2;
                                                                                                                                                                                                                                                                                                                                    if(in_size1 == in_size2)
                                                                                                                                                                                                                                                                                                                                                         out_size = in_size1;
                                                                                                                                                                                                                                                                                                                                                                                                                               /* close files */
fclose(in1);
fclose(in2);
fclose(in2);
fclose(out);
exit(-1);
exit (1);
                                                                                                                                                                                                                                                                                                                                                                                          else
                                                                                                                                                                                                                                                                                                                                                                      ~
                                                                        ~
           ~
                                                                                                                                                ~
                                                                                                                                                                                                                                                                          ~
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              Ļ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    \widehat{}
```

FilE=a:opaste.c * PAGE=3

```
/* The following loop reads in the first half the output image from
the left side image (pointed to by pl) and the second half of the
right side image (pointed to by p2) and combines them in the output
buffer line by line. */
                   /* The following loop reads in the first half the output image from
the left side image (pointed to by pl) and the second half of the
right side image (pointed to by p2) and combines them in the output
buffer line by line. */
                                                                                                                                                                                                                                                                                                                                                                                                    while (side to use [0] == 'R') /* Paste right halves of images together*/
                                                                                                                                                                                                                                                                                                                                                                                                                                                 break;
if (fread (buffer2, sizeof(byte), in_size2, in2) != in_size2)
break;
                                                                                                                                                                                                                                                                                                                                                                                                                         /* read in one input line */
if (fread (bufferl, sizeof(byte), in_sizel, in]) != in_sizel)
                                                                                                                                                                                                                                                                                      out_line_buf[(p1-buffer1)+in_size1/2] = BACKGROUND;
                                                                                                                                                                                                                                          out_line_buf((p1-buffer1)+in_size1/2) = *p2;
                                                                                                                                                                                                                                                                                                                                                                  fwrite(out line buf, sizeof(byte), out size, out);
/* for each line in the input file */
                                                                                                                                                                                  out_line_buf[pi-buffer1] = BACKGROUND;
                                                                                                                                     : *p1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      .
.
                                                                                                               if(pl-buffer1 <= in_size1/2-gap/2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(p1-buffer1 <= in_size1/2-gap/2)
                                                                                                                                  out_line_buf [p1-buffer1]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   out_line_buf [p1-buffer1]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 while (p1 < buffer1+in_size1/2)
<
                                                                    while (p1 < buffer1+in_size1/2)
(
                                                                                                                                                                                                                   if(p1-buffer1 >= gap/2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           = buffer1;
= buffer2 + in_size2/2;
= buffer1 + in_size1;
                                                                                                                                                                                                                                                                                                                       14:
54:
14:
                                                                                                                                                                                                                                                                  else
                                                                                                                                                             else
                                                                                                                                                                                              ~
                                                                                                                                                                                                                                                                             J
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```

FilEsa:opaste.c * PAGE=4

```
/* print termination message */
printf("\n- %s - successfully opasted to - %s - \nand written to - %s -.\n",
input_left, input_right, output);
                                                                                       out_line_buf[(p1-buffer1)+in_size1/2] = BACKGROUND;
                                                          out_line_buf[(p1-buffer1)+in_size1/2] = *p2;
                                                                                                                                               furite(out line buf sizeof(byte), out size, out); /^{\pm} for each line in the inp. [if \frac{\pi}{2}]
                      out_line_buf(p1-buffer1) = BACKGROUND;
                                            if(p1-buffer1 >= gap/2)
{
                                                                                                                                                                                                                      /* close files */
fclose(in1);
fclose(in2);
fclose(in2);
fclose(out);
                                                                 )
else
                                                                                                             clse
                                                                                                                                                                             fflush(out);
                                                                                                                                                                                                                                                           /* main */
                             ~
                                                                                               ~
                                                                                                                                   ~
                                                                                                                                                        ~
```

filtEsa:opaste.c * PAGEs5

```
#define BLACK 0 /* used for the focal point */
#define DIVISOR 5 /* divides radius by this to get inner circle radius */
#define BACKGROUND 104 /* the shade of grey used to blank portions of the
image */
                                                                           This program recieves the filename of image on the command line.
It transforms the image so that it has a dual pie-slice window rather
into its normal rectangular window. A circular area in the center of the
image is set to the value of 128. The size of this area can be
adjusted by changing the value of DIVISOR at the beginning of the
program. The size of the area varies inversely to the value of DIVISOR.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               printf("Incorrect number of parameters.\n");
printf("Usage: slice input_image output_image angle (.IMG assumed)\n");
return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          /* check if correct number of parameters on command line */
if (argc i= 4)
(
                                                                                                                                                                                                                                                                                                                                                                                                                                                  śtream buffer1[16*1024],
stream buffer2[16*1024],
headerT64+256],
in image name[64] = "0",
out image name[64] = "0",
temp_string[32] = "0",
val;
           stice.c
11-SEP-90
Craig A. Vrana
17-SEP-90
Craig A. Vrana
                                                                                                                                                                                                                                                                                                                                                                                          size,
radius,
result = NULL,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     strcpy(in image name, argv[1]);
strcpy(out image name, argv[2]);
strcpy(temp_string, argv[3]);
                                                                                                                                                                                                                                                                                                                   void mein(int argc, char *argv[])
                                                                                                                                                                                                                                                                                                                                                   *file in,
*Tile out;
angle;
slope;
         Filename:
Created:
Programmer:
Last Modified:
Modified By:
                                                                                                                                                                               #include <stdio.h>
#include <string.h>
#include <string.h>
                                                                                                                                                                                                                                                                                 #define PI M_PI
                                                                                                                                                                                                                                                                                                                                                                                                                                                       static char
                                                                                                                                                                                                                                                                                                                                                                        float
                                                                                                                                                                                                                                                                                                                                                   FILE
                                                                                                                                                                                                                                                                                                                                                                                               Ĕ
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                                                                                                                                                         ì
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FiltE=a:s(ice.c * PAGE=1

```
printf("An angle of 0 degrees would create a blank image\n");
exit();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       /* read in image and write out circular version */
for (y=(-size); y<size; y++)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                  )
if (result = setvbuf(file in, stream buffer1, |OFBF
sizeof(stream_buffer1)) i≣ MULL)
                                                                                                                                                                                                                                                                                                            printf("\nIncorrect type or size of buffer1.\n");
                                                                                                                                                                                                                                                                                                                                                                                                                                        printf("\nIncorrect type or size of buffer2.\n");
                                                                                                                                                                                                                                                                                                                                            /* try to open temporary output file */
if ((file_out=fopen(out_image_name, "wb"))==NULL)
<
                                                                                                                                                                                                                                                                                                                                                                              printf("Unable to open %s\n", out_image_name);
return;
                                                                                                                                                                                                                                             printf("Unable to open X\n", in_image_name);
return;
                                                                                                                                                                                                              /* try to open input file */
if ((file_in=fopen(in_image_name, "rb"))==WULL)
{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       result = fscanf(file_in, "%c", &val);
if(result == EOF)
                                                                                                                                                                   else if (strrchr(out_image_name, '.')==NULL)
                                                                                                /* append .img if necessary */
if (strrchr(in_image_name, '.')=NULL)
                                                                                                                                                                                        strcat(out_image_name, ".img");
                                                                                                                              strcat(in image_name, ".img");
strcat(out_image_name, ".img");
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         /* determine radius of image */
size = 1024 / 2;
                                                                           slope = tan((angle/2.0)*PI/180.0);
      angle = (float)atof(temp_string);
if(angle == 0.0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for (x=(-size); x<size; x++)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Ļ
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FILE=a:slice.c * PAGE=2

```
)
if ((float)x<sup>#</sup>x+(float)y<sup>#</sup>y <= (float)size<sup>#</sup>size & 
(float)x<sup>#</sup>x+(float)y<sup>#</sup>y >= (float)(size/DIVISOR)<sup>#</sup>(size/DIVISOR))
                                               printf("\nError reading or writing a file.\n");
break;
         printf("Got to the end of the image\n");
                                                                                                       fprintf(file_out, "%c", BACKGROUND);
                                                                                                                                                                                                                                                                                  printf("\nError reading or writing a file.\n");
                                                                                                                                                                                     fprintf(file_out, "%c", BACKGROUND);
                                                                     fprintf(file_out, "%c", val);
                                                                                                                          )
else if ((float)x*x+(float)y*y <= 2)
                                                                                                                                                                                                                                                                                                                                                      printf("Slicing successfully completed.\n");
                                                                                                                                                  fprintf(file_out, "%", BLACK);
                                                                                                                                                                                                       )
if(ferror(file_in) i= MULL)
<
                                                                                                                                                                                                                                                             if(ferror(file_in) != NULL)
                                                                                                                                                                                                                                                                                                                    /* close files */
fclose(file_in);
fclose(file_out);
                                                                               )
else
                                                                                                 J
                                                                                                                                                                      else
                                                                                                                                                                                                                                                                                                                                                                     /* main */
                                                                                                                                            Ų
                                                                                                                                                                                               ~
                                                                                                                                                                                                                                                  \widehat{}
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165:
```

FILE=a:slice.c * PAGE=3

2 ~~ 1 Fileneme: vcfrc.c Created: 02-007-89 (from original dated MAY-89) Programmer: Christopher Voltz Last Modified: 12-UUM-91 Modified By: Craig A. Vrana This program recieves the fileneme of image on the command line. It transforms the fileneme of image on the command line. It transforms the fileneme of fileneme of the size of this area can be its normal recieves the vindow. A circular area in the center of the image is set to the value of DIVISOR at the beginning of the program. The size of the area varies inversely to the value of DIVISOR. 1 -Modified on 27-JUN-90: Modification to make the inner circle on the test stimuli to be equal to 1/5 the radius of the image. DIVISOR was changed from 4 to 5. /* Size of one dimension of square image. *
 /* used for the focal point
 /* divide radius by this to get inner radius
 /* the level used for the background /* These values are not correct since the a-/* section is always blanked out. Modified on 12-JUN-91: Modification made to vastly decrease processing speed from several minutes down to approximately 5 seconds. This was accomplished by changing fscanf statements to getc and fprintf statements to putc. Also several calculations were moved outside of the most intensive Modified on 24-0CT-90: Modification to make the inner and outer circles on the stimuli adjustable. Changed image size constant to define statement. void main(int argc, char *argv[]) *file_in, *file_out; size, radius, /* Image section radii */ #define A INNER 0 #define A INNER 100 #define B UNER 101 #define B UNER 191 #define C INNER 191 #define D INNER 380 #define E UNER 381 #define E UNER 381 on 1024 #define IMAGE SIZE 1024 #define BLACK #define DIVISOR #define BACKGROUND 104 #include <stdio.h>
#include <string.h>
#include <math.h> [0006. FILE Ĩnt 2 ٤

filte=a:vcirc.c * PAGE=1

```
printf("Incorrect number of parameters.\n");
printf("Usage: voirc input_name output_name inner outer\n");
return;
                                                                                                                                                              /* check if correct number of parameters on command line */
if (argc 1= 5)
<
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                )
if (result = setvbuf(file_in, stream_buffer1, _10FBF,
sizeof(stream_buffer1)) 15 MULL)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        printf("\nlncorrect type or size of buffer1.\n");
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                /* try to open output file */
if ((file_out=fopen(out_image_name, "w"))==NULL)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           printf("Unable to open X\n", in_image_name);
                                                                                                                                                                                                                                                                                                                                                                                                                                       /* try to open input file */
if ((file_in=fopen(in_image_name, *r*))==WULL)
c
                                                                                                                                                                                                                                                                                                                                                                                              else if (strrchr(out_image_name, '.')==MULL)
                                        Y;
outer_sqrd,
outer_sqrd,
X_sqrd;
Stream buffer1[16*1024],
stream buffer2[15*1024],
header[64+556],
in image name[64] = "0",
in image name[64] = "0",
outer_string[64] = "0",
outer_string[64] = "0",
outer_string[64] = "0",
outer_string[64] = "0",
                                                                                                                                                                                                                                                                                                                         /* append .img if necessary */
if (strrchr(in_image_name, '.')==NULL)
                                                                                                                                                                                                                                                                                                                                                       strcat(in image_name, ".img");
strcat(out_image_name, ".img");
                                                                                                                                                                                                                                                                                                                                                                                                                 strcat(out_image_name, ".img");
                                                                                                                                                                                                                                                                         strcpy(in_image_name, argv[1]);
strcpy(out image_name, argv[2]);
strcpy(inner_string, argv[3]);
strcpy(outer_string, argv[4]);
inner,
outer,
result = NULL,
                                 ×
                                                                                        static char
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return;
                                                float
                                                                                                                                                                                                                                            ~
                                                                                                                                                                                                                                                                                                                                              Ų
                                                                                                                                                                                                                                                                                                                                                                            ~
                                                                                                                                                                                                                                                                                                                                                                                                         <u>ل</u>
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ~
```

FILE=a:vcirc.c * PAGE=2

```
printf("\nError reading or writing a file.\n");
break;
                                                                                                                                                         .
/* read in image and write out circular version */
for (y≖(-size); y<size; y++)
(
                         )
if (result = setvbuf(file out, stream buffer2, _10FBF,
sizeof(stream_buffer2)) i= NULL)
                                                         printf("\nincorrect type or size of buffer2.\n");
                                                                                                                                                                                                                                                                                                                                                                                                                                                  printf("\nError reading or writing a file.\n");
       printf("Unable to open %s\n", out_image_name);
return;
                                                                                                                                                                                                                                                 val = (char)getc(file_in);
if ((x_sqrd + Y_sqrd) <= outer_sqrd &&
    (x_sqrd + Y_sqrd) >= inner_sqrd)
                                                                                                                                                                                                                                                                                             else if ((x_sqrd + y_sqrd) <= 2)
{
                                                                                                                                                                                                                                                                                                                                                     putc(BACKGROUND, file_out);
                                                                                                                    /* determine radius of image */
size = IMAGE_SIZE / 2;
                                                                                                                                                                                                                                                                                                                   putc(BLACK, file_out);
                                                                                                                                                                                                                                                                                 putc(val, file_out);
                                                                                                                                                                                                                for (x=(-size); x<size; x++)
                                                                                                                                             outer_sqrd = (float)outer*outer;
inner_sqrd = (float)inner*inner;
                                                                                                                                                                                                                                                                                                                                                                      )
if(ferror(file_in) != NULL)
(
                                                                                                                                                                                                                                x_sqrd = (float)x*x;
                                                                                                                                                                                                                                                                                                                                                                                                                         if(ferror(file_in) != NULL)
<
                                                                                          inner = stoi(inner_string);
outer = stoi(outer_string);
                                                                                                                                                                                               y_sqrd = (float)y*y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   /* close files */
fclose(file_in);
fclose(file_out);
                                                                                                                                                                                                                                                                                                                                      else
(
                                                                                                                                                                                                                                                                            Ų
                                                                                                                                                                                                                           Ļ
                                                                                                                                                                                                                                                                                                                                                                                                                 1
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FilE=a:vcirc.c * PAGE=3

180: 182: printf("vcirc completed successfully.\n"); 183: /* main */

FILE=a:vcirc.c * PAGE=4



file=a:scale.c * PAGE=1

```
for(j=0; j<1024; j++)
                                                                     fp = foren(outfile "w+");
for(i=J; i<1024; i++)</pre>
                                                                        Ļ
                                                                     118
```

FILE=a:scale.c * PAGE=2

```
)
scaled = (double)image_array[x][y] * factor;
low = (int)scaled;
high = low + 1;
image_array[x][y] = (short)((scaled-(double)low)*
(double)[gamma[high]-gamma[low]);
(double)gamma[(ow]+0.5);
                                                                                                                                                                                                                                                                                                                                                            factor = 1.00 / (C1*exp(-LAM1*radius) + C2*exp(-LAM2*radius));
factor /= divisor;
                                                              /*-----
                                                                                                                                                                                                                                                                                                      radius = sqrt((double)((x-511)*(x-511)+(y-511)*(y-511)));
if(radius > 512.0)
                                                                                                                                                                                                                                                              divisor = 1.00 / (C1*exp(-LAM1*512.0) + C2*exp(-LAM2*512.0));
                                                                                                                                                                                                     fp = fopen("/usr1/images/calibration/big_scrn.cal", "r");
for(x=0; x<256; x++)</pre>
                                                                                                                                                                                                                           fgets(color_string, 10, fp);
gamma[x] = ātoi(color_string);
   {
putc(image_array[i][j], fp);
                                                                                                       color_string[10];
                                                                                                                                                                                                                                                                                                                               factor = 1.00;
                                                                                                                                                                                                                                                                                           for(y=0; y<1024; y++)
                                                                                                                                                                                                                                                                             for(x=0; x<1024; x++)
                                                                                                                     gamma[256],
high,
low,
                                                                                                                                                               double divisor,
factor,
scaled,
radius;
                                                                                        *fp;
                                                                                                                                            ××
élse
```

FILE=a:scele.c * PAGE=3



FILE=a:scale.c * PAGE=4

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-** 1 157 /* Luminance value to clear screens to. */
27 /* Number of times image appears in test. */
27 /* Value of escape character in decimal. */
"fix92.img/0" /* for long bell. */
24 /* Length of filenames in characters. */
1000 /* Arbitrary -- used to size list array */
10 /* Controls the mix of the random list */
10 /* Controls the number of rest periods. */
11 /* For short bell. 12-SEP-91 Modifications were made to the pvrs.c program to get this version. The modification made on this date allowed for another subject response file to be entered without having to restart the entire program. Also a comment was allowed for that is placed into the raw file and also the summary file by the analysis program seg_enalyze. /*-----/* Length of time before test starts. This program was created for Dr. George Geri of the University of Dayton Research Institute, Williams Air Force Base, Arizona. 06-AUG-90 Modifications were made to the dvs program to get this version. The modifications involved the method of data collection and not the operating stucture of this program. The purpose of this program is to gather the responses of test subjects to segmented image stimuli. segs.c Craig A. Vrana - UDRI 08-DEC-89 15-JUN-92 Program: Created by: Date Created: Last Modified: #define Max NAME LENGTH 64 #define Max TRIALS #define Max FACTOR #define NUMBER OF SCANS #define EST DIVISOR #define SHORT IMAGE PRESENTED 20 <sys/types.h> <time.h> #define FIXATION_POINT #define LONG #define MAX_NAME_LENGTH #define MAX_TRIALS <gl.h>
<gl.h>
<device.h>
<stdio.h> #define START_DELAY #define BACKGROUND #define IMA(#define ESC #include #include #include #include /*---۴ -

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FilE=a:segs.c * PAGE=1

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<pre>/************************************</pre>	/********* * moin * *********/	main(argc,argv) int argc; char [*] argv[]; ć	<pre>char correct_response, temp_string[128], comment_string[128];</pre>	<pre>int i = 0 list index = 0, trials, trials_between_breaks;</pre>	long response; FILE *output;	struct tm *curtime; time_t bintime;	<pre>if (argc < 3) /* If no file names entered on command line. ask_file_names(); /* Ask for the list and response file names. selse strcpy (listfile, argv[1]); /* Get the image listfile name. strcpy (datafile, argv[2]); /* Get the subject datafile name. strcpy (datafile, argv[2]); /* Get the subject datafile name. strcpy (datafile, argv[2]); /* Get the subject datafile name. strcpy (datafile, argv[2]); /* Get the subject datafile name. strcpy (datafile, argv[2]); /* Get the subject datafile name. strcpy (datafile, argv[2]); /* Get the subject datafile name. strcpy (datafile, argv[2]); /* Get the subject datafile name. strcpy (datafile, argv[2]); /* Get the subject datafile name. strcpy (datafile, argv[2]); /* Get the subject datafile name. strcpy (datafile, argv[2]); /* Get the subject datafile name. strcpy (datafile, argv[2]); /* Get the subject datafile name. strcpy (datafile, argv[2]); /* Get the subject datafile name. strcpy (datafile, argv[2]); /* Get the subject datafile name. strcpy (datafile, argv[2]); /* Get the subject datafile name. strcpy (datafile, argv[2]); /* Get the subject datafile name. strcpy (datafile, argv[2]); /* Get the subject datafile name. strcpy (datafile, argv[2]); /* Get the subject datafile name. strcpy (datafile, argv[2]); /* Get the subject datafile name. strcpy (datafile, argv[2]); /* Get the subject datafile name. strcpy (datafile, argv[3]); /* Get the subject datafile name. strcpy (datafile, argv[3]); /* Get the subject datafile name. strcpy (datafile, argv[3]); /* Get the subject datafile name. strcpy (datafile, argv[3]); /* Get the subject datafile name. strcpy (datafile, argv[3]); /* Get the subject datafile name. strcpy (datafile, argv[3]); /* Get the subject datafile name. strcpy (datafile, argv[3]); /* Get the subject datafile name. strcpy (d</pre>	<pre>time(&bintime): /* Get seconds since 00:00:00 GMT, 01-JAN-70 */ curtime = localitime(&bintime); /* Convert to localitime. */ trials = get_list(); /* Open listfile, det. # of trials, & load. */ if(trials == NULL)</pre>
2323328828282828	C2C22	~8888888		833: 53 833: 58 833: 58	56 57	88.5 <u>5</u> 5		1125:

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flLE=a:segs.c * PAGE=2
filE=a:segs.c * PAGE=3

* • * 1 * /* Set up the graphics display mode, window colormap */ /* Clear the front and back buffs and load fixation. */ ** -/4 Prepend '/usr1/images/mean_92/data/' to datafile*/ 1 while(access(datafile, 0) == NULL)/* Check to see if data file exists. */ < /* Continue displaying until all images shown. printf("Data file already exists.\nchoose another response file.\n"); printf("\nEnter the name of the subject response file : "); scanf("Xs", datafile); add_directory(); /* Prepend '/usrl/images/mean_92/data/' to datafil /* Prepend '/usr1/images/mean_92/data/' to datafile. /* Get first image name. /* Get name to parse. randomize list(trials); /* Create a random list of images to display. trials_between_breaks = (int)(trials/REST_DIVISOR); /* Wait for the middle mouse button to start test. if(list_index % trials_between breaks == 0 && Tint)(list_index / trials_between_breaks) != REST_DIVISOR) /* Load the named image into an array in memory. fprintf(output, "Raw data file name: Xs\n" datafile);
fprintf(output, "Test started: Xs", asctime(curtime));
fprintf(output, "Total trials: Xd\n", trials);
fprintf(output, "Comment: Xs\n\n", comment_string);
filush(output); /* Add ".img" to image name if necessary. printf("Enter'a comment to be placed in the raw file.\n"); gets(comment_string); printf("Aborting due to no stimuli in list file.\n"); output = fopen(datafile, "w+"); /* Open output datafile. strcpy(imagefile, list_array[list_index++]); strcpy(temp_string, imagefile); jf(temp_string[2] == '_') correct_response = 'R'; correct_response = 'L'; if(temp_string[1] ≖ 's') correct_response = 'S'; get_start(); sleep(START_DELAY); add_directory(); graph_init(); clear_screens(); add_extension();) ff[ush(stdin); load_image(); exit(); while(1) else 1 else

```
/* Get name to parse.*/
                                                                               -
                                   furts(imagefile, output);
display image(); /* Move the image from memory display and time it.*/
time_display(); /* Display the image for NUMBER_OF_SCANS frames. */
                                                                                                                                        /^* Ring bell only for wrong response when images are different */
                                                                                                                                                                                                                                                                                        /* Ring bell only for wrong response when images are different */
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               -
                                                                                                                                                                                                                                                                                                           jf((correct_response i= 'R') Lt (correct_response i= 'S'))
                                                                                                                                                           jf((correct_response i= 'L') #6 (correct_response i= 'S'))
                                                                        response = get_response(); /* Get mouse button pushed by subject.
switch(responsë)
ć
                                                                                                                                                                                                                                                                                                                                                                                                                                                           printf("Value returned from get_response not valid.\n");
graph reset();
exit();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if(list_index < trials) /* If there are more images to display.
(
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               strcpy (imagefile, list_array[list_index++]);
strcpy(temp_string, imagefile);
if(temp_string[2] == '_')
                                                                                                                                                                                                                               fputs("\tCorrect\n", output);
                                                                                                                                                                                                                                                                                                                                                                                 fputs("\tCorrect\n", output);
                                                                                                                                                                                ringbell();
fputs("\tWrong\n", output);
                                                                                                                                                                                                                                                                                                                                ringbell();
fputs("\tWrong\n", output);
                                                                                                                                                                                                                                                  break;
case RIGHTMOUSE;
fputs("\tRight\t", output);
                                                                                                           case LEFTMOUSE:
    fputs("\tLeft\t", output);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        correct_response = 'S';
                                                                                                                                                                                                                                                                                                                                                                                                         case ESC:
fclose(output);
graph reset();
exit();
          get_start();
sieep(3);
                                                                                                                                                                                                                                                                                                                                                                                                    break;
                                                                                                                                                                                                                                                                                                                                                             else
                                                                                                                                                                                                              else
                                                                                                                                                                                                                                                                                                                                                                                                                                                    default
                                                                                                                                                                                                                                                                                                                       Ļ
                                                                                                                                                                                                                                                                                                                                                      ~
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filE=a:segs.c * PAGE=4

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FilE=a:segs.c * PAGE=5

<pre></pre>

Filte=a:segs.c * PAGE=6

·. ·. 2 print(#Writer the nume of the subject response file : ");
print(#Writer the nume of the subject response file : ");
print(#Writer the nume of the subject response file : ");
print(#Writer the nume of the subject response file : ");
print(#Writer the nume of the subject response file : ");
print(#Writer the nume of the subject response file : ");
print(#Writer the nume);
print(#Writer the -USERS: main clear_screens CALLS: PARAM: LOCAL: FilEma:segs.c * PAGE=7

Globitv_image_stravy[1] (Globitv_image] (display_image] (display_image] (display_image] (display_image] (cettrife(28.0,1151,1023,image array); (cettrife(28.0,1151,102,image array); (cettrife(28.0,112,102,image array); (cettrife

:

Filte=a:segs.c * PAGE=8

dor((); fp = form(listfle, "r"); control = fcent(fp, "fs", temp_string); freturn_value = fcent(fp, "fs", temp_string); for(i=0; i=1NME_MESENTED; i=+); for(i=0; i=1NME_MESENTED; i=+); for(i=0; i=1NME_MESENTED; i=+); philo(creturn_value = fcent(fist, i=+); philo(creturn_value); philo(creturn="fat"string); philo(creturn="f

FilE=a:segs.c * PAGE=9

FilE=a:segs.c * PAGE=10

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```
*
                                                                                                                                                                                                                                                                                    /*----
                                                                                                                                                              fp = fopen("calibration/vs.cal", "r");
ringbell();
for ("Using calibration file for non-corrected images.\n\n");
for (i=0; i<256; i++)
</pre>
                                                                                                                                                                                                           fgets(color_string, 10, fp);
color_value = atoi(color string);
mapcolor(256+i, color_value, color_value);
                      device(LEFIMOUSE); /* Enable mouse as queued input device.
qdevice(MIDDLEMOUSE);
qdevice(RIGHTMOUSE);
qdevice(KEYBD);
                                                                                              printf("Cannot find calibration file.\n\n");
printf("Using linear gamma for corrected images.\n\n");
for(i=0; i<256; i++)</pre>
          /* Set bell to long beep.
                                                                                if(access("calibration/vs.cal", 0) i= NULL)
                                                                                                                                                                                                                                                                                                                                                                    /*** graph_reset ***/
/*** graph_init ***/
                                                                                                                               mapcolor(256+i, i, i, i);
                                                                                                                                                                                                                                                                                                                                                                                                          int i,j;
char val;
                                                                                                                                                                                                                                                                                                                                                                                                                                          656: load_image()
657: (
658: int i,j;
659: char ve
                                                                                                                                                                                                                                                                                                                                                                                                                     653:
654:
                                                                                                                                                                                                                                                                                                                                                                                                                                    655:
                                                                                                                                                                                                                                                                                                                                                                                                            652
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2

FilE=a:segs.c * PAGE=11

```
mont();
for form(image(ile, "");
for(i=0; i<(02; i+1)-)
for(i=0; i<(02; i+1)-)
for(i=0; i<(02; i+1)-)
for(i=0; i<(02; i+1)-)
for(i=0; i<(03; i+1)-)
for(i=0; i<(13) = getc(fp)+256;
form(i=0; i<(13) = getc(fp)+256;
form(i=0; i<(13) = getc(fp)+256;
form(i=0; i<(13) = getc(fp)+256;
form(i=0; i<(14) = 0;
form(i=0; i<(13) = i<
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    printf("Error: Failed to find %s.\n", imagefile);
abort();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             * restore color map *
                                                                                        if(access(imagefile, 4) I= NULL)
  *fp;
index = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      714:
715:
716:
716:
718: restore_color_map()
719: (
FILE
                                                                                                                              Ļ
660:
6665:
6665:
6665:
667:
```

FilE=8:segs.c * PAGE=12

```
/*-----
                                                                                               getmcolor(i+256, red+i, green+i, blue+i);
                                                                                                                                                     /*** time_display ***/
                                                                                                                                                             *************************
                                                                                                *********************
                                                                                                    while(timer<(NUMBER_OF_SCANS-1))
                                                                        for(i=0; i<256; i++)
                                                                                                                        int timer = 0;
                                                                                                                                               swapbuffers();
                                                                                                                                     gsync();
timer++;
```

.

(DOW = Day of Veek) The only difference from the above is that the standard is compared with a portion of the image that has been processed with the variable resolution processing program using an 'a' coefficient of 3. The name of this image file also denotes that the standard is displayed to the left of the processed image because the 's' is to the left of the processing level number. where 'z' is a letter representing the original image. The 's s03' denotes that the level 3 image is compared to itself. The '.img' denotes the file as a binary image The only difference from the above is that the standard is displayed to the right of the processed portion of the image. Additional information can be added to the filename beyond the 4th character and before the '.img' suffix without affecting the operation of this program up to the point where the filename length reaches the limits of the UNIX file system or the constant MAX_NAME_LENGTH. Changed the constant MAX PROCESSING LEVEL to 100 from 20 to be able to handle image numbers up to 99. Also changed the allign-ment on the output to the summary file so that image numbers less than 10 allign with the right column of image numbers 10 or greater. This was done by placing a field width of 2 in front of the integer format character in two fprintf statements. This program was written to analyze the raw data files produced by the variable-resolution study program. The format of the raw data file is as follows: Changed the operation of the program to calulate the percent correct for the new version of the variable resolution study. The new vres study program is named vrs. It places a left or Right response of the subject into the data file instead of the original Same or Different. 15-MAY-92 Added the ability to analyze several data files at one time. name.raw DOW Mon Day Hr:Mn:Sc Year Craig A. Vrana - UDRI 12-JAN-90 15-MAY-92 Result Image filename is of the forms: Response Created by: Date Created: Last Modified: file. Raw data file name: Test started: Blank line Image filename R Reason modified: zs_s03.img z03s.img zs03.img ٤

FILE=a:asegs2.c * PAGE=1

flLE=a:asegs2.c * PAGE=2

-* ÷ -* 2 /#================================== /* Length of filenames in characters. 10000 /* Arbitrary -- used to size arrays. /* Access code for files. 100 /* Levels of processing. 2 /* Number of possible images in test. process array(MAX PROCESSING LEVEL)(NUMBER OF RESPONSES); angle afray(MAX ANGLES)(NUMBER OF RESPONSES); same array(MAX PROCESSING_LEVEL)(NUMBER_OF RESPONSES); angles(MAX ANGLES); temp_angles(MAX_ANGLES); char letter; int level[MAX PROCESSING LEVEL][NUMBER OF RESPONSES]; int angle[MAX_ANGLES][NUMBER_OF_RESPONSES]; char location; name_Brray[MAX_TRIALS][MAX_NAME_LENGTH], response_array[MAX_TRIALS][MAX_MAME_LENGTH], result_array[MAX_TRIALS][MAX_NAME_LENGTH], *infile[MAX_NAME_LENGTH], *outfile[MAX_NAME_LENGTH]; * Constant Definitions * %% #include <gl.h>
%% *define <gl.h
%% *defi

.

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filts=a:asegs2.c * PAGE=3

* return_value≖fscanf(input_file, "Xs Xs Xs", name_string, response_string; result_string); /* Get all the different image segments and count how many there are.*/ for(i≈0; i<MAX_ANGLES; i++) { jf((name_string[0] != image_array[i].letter) && (i < image_number)) /* Initialize the char string that contains everything in an angle. */
strcpy(angle_chars, "0123456789,\0"); /* Get all the different image letters and count how many there are. for(i=0; i<MAX_IMAGES; i++) (/* Copy first five lines from .raw file to .sum file. */ fgets(long_string, 100, input file); fgets(long_string, output file); furs(long_string, output file); furs(long_string, output file); furt.(long_string, output file); flusn(output_file); flusn(output_file); standard_array[image_number].letter = name_string[0]; image_array[image_number++].letter = name_string[0]; break; /* Load arrays from .raw file and close .raw file. */ else if(name_string[0] == image_array[i].letter) strcpy(name_array(index), name_string); strcpy(response_array[index], response_string); strcpy(result_array[index], result_string); index++; if(return_value]= NULL && return_value != EOF) < output_file = fopen(outfile, "w+"); continue; break; else (Ų $\hat{}$ ~ $\overline{}$ ÷. Ļ

FilE=a:asegs2.c * PAGE=4

```
printf("Unknown data found when scanning for segments\n");
                                                                                                                                                                                                                                                                                if((temp_angle != temp_angles[i]) & (i < number_of_angles))
                                                                                                                      angle_length = strspn(&name_string[7], angle_chars);
for(j=0; )<angle_length; j+∓)
<
               angle length = strspn(&name string(5), angle_chars);
for()=0; j angle_length; j++)
                                                                                                                                                                                                                                                                                                                                                               temp_angles[number_of_angles++] = temp_angle;
break;
                                                                                                                                                                                       angle string[]] = '\0';
temp_angle = (float)atof(angle_string);
                                                                        angle_string[]] = '\0';
temp_angle = (float)atof(angle_string);
                                         angle_string[j]=name_string[5+j];
if (angle_string[j] == '')
angle_string[j] = '.';
                                                                                                                                                        angle_string[]]=name_string[7+j];
if (angle_string[] == ' ')
angle_string[] = '.';
                                                                                                                                                                                                                                                                                                                                                                                                                        )while(return_value > 0 25 return_value i= EOF);
                                                                                                                                                                                                                                                                                                                élse if(temp_angle == temp_angles[i])
                                                                                                            eise if(name_string[6] == '_')
<
if(name_string[4] == '_')
<
                                                                                                                                                                                                                                                                                                                                                                                                                                                               )while(files++ <argc);
                                                                                                                                                                                                                                                                                                 continue;
                                                                                                                                                                                                                                                                                                                                break;
                                                                                                                                                                                                                                                                                                                                                                                                                                               fclose(infile);
                                                                                                                                                                                  \sim
                                                                                                                                                                                                                                 else
(
                                                                                                                                                                                                                                                                                                                                        >
{else
                                                                                                                                                                                                                                                        ~
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                                                                                                                                                                                                                                                                                                                                                                                 1
                                                                                                  1
```

FilE=a:asegs2.c * PAGE=5

```
/* Tally the results of all images from the loaded arrays. ^{\star}/
                                                                                                                                                                                                                                                                                                                        angle string[j] = '\0';
temp angle = (float)atof(angle string);
/* printf("angle %d = %5.1f\n<sup>m</sup>, i, temp_angle); */
                                                                                                                                                                                                                                                          angle length = strspn(&temp string[5], angle_chars);
for(j=0; j<angle_length; j++)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                           printf("Unknown data found when scanning input\n");
exit(-1);
                                                                                                                                                                                                              /* For every trial */
                                                                                                                                                                                                                                                                                     angle_string[j]=temp_atring[5+j];
if (angle_string[j] == ''')
angle_string[j] = '.';
                                                                        temp_angle = temp_angles[j];
temp_angles[j] = Temp_angles[i];
temp_angles[i] = temp_angle;
                                                     if(temp_angles[j] < temp_angles[i])</pre>
/* Sort the angles into ascending order */
                                                                                                                                                                                                                             strcpy(temp_string, name_array[i]);
if(temp_string[4] == '_')
<
                                    for(j=i+1; j<number_of_angles; j++)
</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for(j=0; j<number_of_angles; j++)
{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(angles[j] == temp_angle)
                  for(i=0; i<number_of_angles-1; i++)
                                                                                                                                                                                                                                                                                                                                                            else if(temp_string[6] == '_')
(
                                                                                                                     angles[i] = temp_angles[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            angle_number = j;
                                                                                                                                               angles[i] = temp_angles[i];
                                                                                                                                                                                                         for(i=0; i<index; i++)
{
                                                                                                                                                                                                                                                                                                                                                                               continue;
                                                                                                     ~
                                                                                                                                                                                                                                                                                                                 ~
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    1
                                                                                                                                                                                                                                                                                                                                                                                      else
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                                                                                                                              ~
```

FILE=a:asegs2.c * PAGE=6

```
total = image_array[j].angle[i][CORRECT] +
    image_array[j].angle[i][WROWG];
percent_correct = (float)image_array[j].angle[i][CORRECT] / (float)total;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             total = angle_array[i](CORRECT] + angle_array[i](MROMG];
percent_correct = (float)angle_array[i][CORRECT] / (float)total;
percent_correct *= 100.00;
                                                                                                                                                                                                                                                                                                                                                                                                                        /* Calculate percentages from tallies and store in .sum file. */
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        fprintf(output_file, "Seg >: X5.1f Percent Correct: X6.2f",
angles(i), percent_correct);
                                                                                               ++image_array[j].angle[angle_number][CORRECT];
break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if(angle_array[i][CORRECT]==0 && angle_array[i][WRONG]==0)
                                                                                                                                                                                                                               ++ image_array(j].engle[angle_number][uRONG];
break;
                                                                                                                                                                                                                                                                                                                                                                   Xc", image_array[i].letter);
                                                                                                                                                                                                             if(image_array[j].letter == temp_string[0])
                                                                            if(image_array[j].letter == temp_string[0])
                                                                                                                                                                                                                                                                                                                          ~
                       if(strcmp(result_array[i], "Correct") == NULL)
(
                                                                                                                                                                                                                                                                                                                      /* Put headers in the output file.
fprintf(output file, "\t\t
for (i=0; i<image_number; i++)</pre>
                                       ++angle_array(angle_number){CORRECT];
for(j=0; j<1mage_number; j++)
ć
                                                                                                                                                                          ++angle_array[angle_number][WRONG];
for(j=0; j<imaga_number; j++)
ć
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         sum total = 0;
for(j=0; j<image_number; j++)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                             for(i=0; i<number_of_angles; i++)</pre>
                                                                                                                                                                                                                                                                                                                                                                  fprintf(output_file, "\t
                                                                                                                                                                                                                                                                                                                                                                                        fprintf(output_file, "\n");
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      continue;
                                                                                                                                                                                                                                                         \widehat{}
                                                                                                                                   \widehat{}
                                                                                                                                                                                                                                                                     1
                                                                                                                                             else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 Ų
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                                                                                                                                                                                                                                                                                          \hat{}
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filtera:asegs2.c * PAGE=7

```
/* Tally the results of the same images from the loaded arrays. */
                                                                                                                                                                                                                                                                                                                                                                                                                                                ++standard_array[j].angle[angle_number][LEF1];
break;
                                                                                                                                                angle length = strspn(&temp string[7], angle_chars); for(j=0; j<angle_length; j+\overline{\tau})
                                                                                                                                                                                                                                                                                                                                                                                                                               if(standard_array[j].letter == temp_string[0])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(standard_array[j].letter == temp_string[0])
                                  fprintf(output_file, "\tXd frials\n", sum_total);
percent correct *= 100.00;
sum total += total;
{printf(output_file, "\tX6.2f",percent_correct);
                                                                                                                                                                                                                                                                                                                                                                                  if(strcmp(response_array[i], "Left") == NULL)
(
                                                                                                                                                                                                                angle_string[j] = '\0';
temp_angle = (float)atof(angle_string);
                                                                                                                                                                           angle_string[]=temp_string[7+j];
if (angle_string[j] == ' ')
angle_string[j] = '.';
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ++same array[angle_number][R]GH1];
for(j=0; j<image_number; j++)
                                                                                                                                                                                                                                                                                                                                                                                                  ++same array(angle_number)(LEF1);
for(j=U; j<image_number; j++)
                                                                                                                      strcpy(temp_string, name_array[i]);
if(temp_string[6] *= '_')
                                                                                                                                                                                                                                                                                                   for(j=0; j<number_of_angles; j++)
<
                                                                                                                                                                                                                                                                                                                           if(angles[j] == temp_angle)
                                                                                                                                                                                                                                                                                                                                              angle_number = j;
                                                                                               for(i=0; i<index; i++)
{
                                                                                                                                                                                                                                                                       continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                         Ų
                                                                                                                                                                                                                                                                                                                                        -
                                                                                                                                                                                                        ~
                                                                                                                                                                                                                                           )
(else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                else
                                                                                                                                                                                                                                                                                                                                                                  \sim
                                              ~
```

```
(float)total;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      *
                                                                                                                                                                                                                                                                                                                                                                                                                             /* Calculate percentages from tallies and store in .sum file. */
                                                                                                                                                                                                               X6.2f",
          ++standard_array[j].angle[angle_number] [RIGHT];
break;
                                                                                                                                                                  total = same_mrray[i][LEFI] + same_mrray[i][RJGHT];
percent_left = (float)same_mrray[i][LEFI] / (float)total;
percent_left *= 100.00;
                                                                                                                                                                                                                                                                            total = standard array[j].angle[i][LEFT] +
    standard array[j].angle[i][RIGHT];
percent_left = (float)standard_array[j].angle[i][LEFT] /
                                                                                                                               if(same_array[i][LEFT]==0 && same_array[i][R[GHT]==0)
                                                                                                                                                                                                              fprintf(output_file, "Seg >: X5.1f Percent Left:
angles[i], percent_left);
                                                                                                                                                                                                                                                                                                                                                   fprintf(output_file, "\tXd trials\n", sum_total);
                                                                        fprintf(output_file, "\n\nSame image comparison\n");
                                                                                                                                                                                                                                                                                                                percent left *= 100.00;
sum totāl += total;
{prīntf(output_file, "\tX6.2f",percent_left);
                                                                                                                                                                                                                                                   sum total = 0;
for(j=0; j<image_number; j++)
                                                                                                            for(i=0; i<number_of_angles; i++)
                                                                                                                                                                                                                                                                                                                                                                                                                                                      * ask file *
*************
                                                                                                                                                                                                                                                                                                                                                                                                           /*** main ***/
                                                                                                                                                                                                                                                                                                                                                                                                                                             ************
                                                                                                                                                 continue;
                                                                                                                                                                                                                                                                                                                                                                               fclose(outfile);
```

FilE=a:asegs2.c * PAGE=9

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filE=a:asegs2.c * PAGE=10

APPENDIX C

The program, *mtf.c*, used to calculate the MTFs of the wide-field display used in the present study. The program was written to implement the procedures for calculating the MTF described by Kelly (1992).

```
reference of the second second
```

FILE=a:kellymtf.c * PAGE=1

```
printf("Usage: mtfnew raw_file cal_file scrn_height line_sep c_ratio\n");
return(-1);
pixels.height=1000.0,
procession
procession
procession
file
fierd_fields(20);
file
fierd_fields(20);
file
fierd_fields(20);
fierdfields(20);
fierdfiel
```

FilE=a:kellymtf.c * PAGE=2

/* 6. Divide the sum calculated in step 4 by the sum calculated in step 5. This number is the centroid of the peak in fractions of elements. */ 3. Set all elements in the first 56 elements to zero, which are less than half of the peak value found in step 2. $^{\star}/$ /* 4. Sum the value of each element multiplied by its element number(i.e. 1-56). */ /* 2. Find the pixel or element with the largest value in the first 56 elements. */ /* 5. Sum the value of each of the first 56 elements. *//* 7. Repeat steps 2 through 6 for the last 55 elements. */ centroid1 += meas_data[i]*(double)(i);) fclose(fptr); printf("Closed the calibration file.\n"); fscanf(fptr "X*f Xf", &input); meas data[i] = (double)input; prinff("X8.4lf\n",meas_data[i]); meas_data[i] = (double)0; if (meas_data[i] < peak1) peak2 = meas_data[i]; peak1 = meas_data[i]; if(meas_data[i] > peak2) if(meas_data[i] > peak1) sum1 += meas_data[i]; for (i=56; i<111; i++) { for (i=56; i<111; i++) for (i=0; i<56; i++) (for (i=0; i<56; i++) centroid1 /= sum1; peak2 /= 2; peak1 /= 2; ~ ~ ~ Ļ /* 3. Ų ~ ~

FILE=a:kellymtf.c * PAGE=3

/* 8. Take the diffence between the two centroids. This is the distance between the two calibration peaks in units of sensor pixels or elements. */ printf("Ran out of input data before finished reading file.\n"); exit(-1); ∕★★★★★★★★★★★★★★★★★★★★ APPLY TRAPEZOIDAL WINDOW FUNCTION calib = ((centroid2 - centroid1) * calratio) / (double)512.0; npts = (int)(((double)display_lines+256.000)/calib+0.5); calratio = (double)display_lines / (double)separation; printf("\n\n%8.4e\n%8.4e\n",centroid1,centroid2); centroid2 += meas data[i]*(double)(i-56); sum2 += meas_data[i]; if(fscanf(fpčr, "X*f Xf", Linput) == 0) } centroid2 = centroid2/sum2 + (double)56.00; /* 9. Perform the following calculation: meas_data[i] = (double)0;) data[i] = input; printf("%8.4[f\n",data[i]); if (meas_data[i] < peak2) (dft_i[i] = (double)0;
dft_r[i] = (double)0; fptr = fopen(name1,"r"); for (i=0; i<111; i++) for(i=0; i<512; i++) (fclose(fptr); Ļ /* Ų ~ 238: 238: 238: 238: 238: 85 22

FILE=a:kellymtf.c * PAGE=4

File=a:kellymtf.c * PAGE=5

flLE=a:kellymtf.c * PAGE=6

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