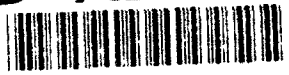


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JOHNS HOPKINS UNIVERSITY  
HOMEWOOD RESEARCH ADMINISTRATION  
CHARLES AND 34TH STREET  
BALTIMORE MD 21218

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Since the beginning of the funding of the grant, we established a substantial effort in the area of connectionist optimization algorithms, relaxation networks, and geometrical learning algorithms. All of the above are highly interconnected research projects. We have achieved several significant results that have increased our understanding of the computational capabilities and limitations, of connectionist and constraint network. Our most significant contributions thus far are in the area of parallel complexity of constraint networks, comparative experimentation with learning algorithms and geometric concept learning. Our results in the area of parallel constraint networks are the subject of several publication in first rate journal and conferences. Our experimental research achieves the best results on several well established benchmarks. Most notably our group achieved the best results (in terms of prediction accuracy) in the area of protein folding. The technical result of research investigations are summarized in the following sections.

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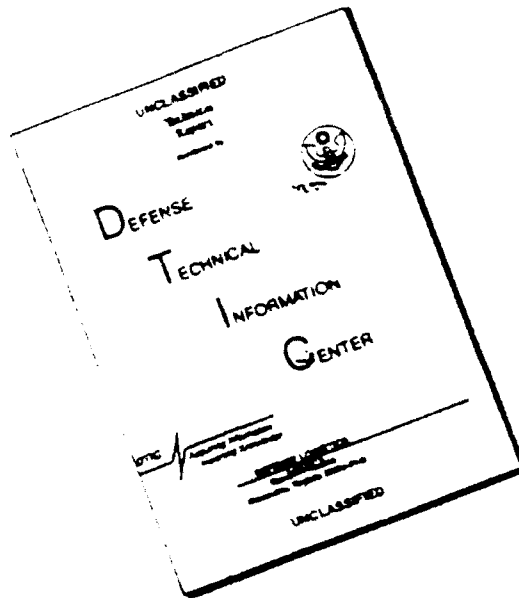
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**FAX COVER SHEET**

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**TO:** Marilyn Ramsey

**COMPANY:** ONR

**FAX NUMBER:** (202) 404-7951

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**FROM:** Joan Warfield *JW*

**TITLE:** Sponsored Projects Officer

**FAX NUMBER:** (301) 338-7775      **TELEPHONE NUMBER:** (301) 338-8668

**DATE:** January 25, 1993      **TIME:** 4:15 P.M.      **OPERATOR:** JW

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**SHOULD YOU ENCOUNTER DIFFICULTY IN RECEIVING THIS DOCUMENT,  
PLEASE CONTACT US AT (301) 338-8668.**

**MESSAGE:** Marilyn, Attached is the requested copy the final report for Grant No. AFSOR-89-0151. As stated in Dr. Kasif's (P.I) letter, his report was forwarded to his program director along with his proposal in June. The hard copy of this document will be sent by first class mail tomorrow. It is my understanding that the pending NCE will be released as soon as possible.

If you have questions, please contact me at (410) 516-8668.

Prof. Simon Kasif  
Department of Computer Science  
The Johns Hopkins University  
Baltimore, MD 21218  
410-516-8296  
KASIF@CS.JHU.EDU

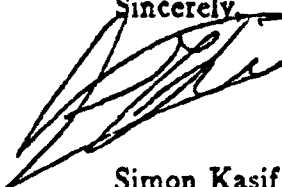
January 25, 1993

Dr. Mark Jacobs  
Program Director  
AFOSR-NM  
Bolling Airforce Base  
Washington, DC 20332-6448

Dear Dr. Jacobs

Enclosed please find the final technical report for the research on "Computational Complexity of Connectionist and Constraint Networks" supported by grant AFOSR-89-0151. I sent a similar document in June as part of a new proposal, but apparently it was misplaced. We have several on-going experimental validation projects to test the programs developed with partial support from AFOSR. When this work is completed we shall send you an update. Our research had a strong impact on a number of areas, for example we effectively closed the study of parallel complexity of local consistency in constraint networks and we developed the best known methods for constructing non-axis parallel decision trees. I would appreciate any comments you may have on our research.

Sincerely,



Simon Kasif

Final Report: 1992  
Complexity of Connectionist and Constraint-Satisfaction  
Networks

Simon Kasif

Department of Computer Science  
The Johns Hopkins University  
Baltimore, Md 21218  
KASIF@CS.JHU.EDU  
301-338-8296

## 1 General Progress Summary and Overall Impact

Since the beginning of the funding of the grant, we established a substantial effort in the area of connectionist optimization algorithms, relaxation networks, and geometric learning algorithms. All of the above are highly interconnected research projects. We have achieved several significant results that have increased our understanding of the computational capabilities and limitations of connectionist and constraint networks. Our most significant contributions thus far are in the area of parallel complexity of constraint networks, comparative experimentation with learning algorithms and geometric concept learning. Our results in the area of parallel constraint networks are the subject of several publications in first rate journals and conferences. Our experimental research achieves the best results on several well established benchmarks. Most notably our group achieved the best results (in terms of prediction accuracy) in the area of protein folding. The technical results of our research investigations are summarized in the following sections.

## 2 Theoretical Analysis of Relaxation Networks

Relaxation networks are a special case of constraint satisfaction networks and have been used in optimization, truth maintenance systems, and computer vision. These networks utilize local constraint propagation techniques to achieve local stability (local consistency in propositional constraint networks). One of the stated objectives of the research proposal was to increase our understanding of local optimization (search) techniques in such networks. In [KD92] we provide a complete characterization of achieving local stability (consistency) in symbolic relaxation networks. The results of these investigation are reported in several

papers Our results are summarized in a collection of papers [Kas90, Kas86, Kas89, KD91, KD92, KD91]

### 3 Theoretical Analysis of Discrete Hopfield Nets

We completed our investigation of Discrete Hopfield Nets. Our results are summarized in [KBDS91, KBDS93]. In addition to obtaining several lower bounds for the complexity of finding local minima (stable state) in Hopfield networks, we also studied the complexity of finding a new stable when the network is perturbed by modifying one of the weights by a tiny amount (one bit).

### 4 Parallel Problem Solving and State Space Search

Our group at Johns Hopkins recently obtained a substantial result on very large state-space search. The first part of this work attacked the problem of 6-piece chess end-game analysis, a long-time outstanding problem in computational chess and AI. The chess end-game analysis was done by Lewis Stiller, a graduate student in our AI group, who implemented an extremely large search-space exploration on the Connection Machine. His program has found 6-piece chess positions that require more than 240 moves to achieve a forced win. The methodology is also applicable to other search problems in symmetry groups. The results are published in [Sti91a, Sti91b, Sti92a, Sti92b]. This work is considered a fundamental breakthrough in the computational chess community, and has received wide publicity in the popular press (e.g., Scientific American, London Times, Washington Post).

As a side project we have discovered an efficient parallel algorithm to compute string statistics for molecular-dynamics simulations [Sti92b]. The algorithm is being used currently on the CM2 in Los Alamos.

Our research program in parallel AI programming also had an important educational side-effect. The PI developed a regular programming workshop on parallel programming the Connection Machine. Graduate and undergraduate students implemented many diverse applications on the CM such as semantic networks, constraint networks, path planning with obstacles, geometric algorithms, a cellular automata model of the heart, psychophysical models and more. Subsequently, many of these students spent summers at National Laboratories such as NRL, SRC, and Los Alamos working on important applications.

### 5 Design and Analysis of Algorithms for Machine Learning

With partial funding from the grant we started a set of new investigations of machine learning algorithms. The results of these studies are documented below.

#### 5.1 Comparative Studies of Learning Methods

We are conducting a comprehensive set of experiments that compare (on a range of real world applications) the performance of backpropagation algorithms to nearest neighbor

methods learning and other methods. The experiments are performed by David Heath (funded by the project) and Scott Cost and are co-supervised by Steven Salzberg and the PI. Salzberg studied the comparative effectiveness of the backpropagation algorithm and an instance based learning algorithms on the problem of predicting protein folding. The results are documented in [CS90b]. A comprehensive comparative study of connectionist learning and instance based methods has been completed and is a subject of a of a journal paper [CS90a].

## 5.2 Experimental Analysis of Backpropagation

We completed experimentation with two heuristics approaches to improve the efficiency and accuracy of backpropagation in connectionist networks. The first approach is based on a scaling (multiple resolution) approach to learning. Instead of teaching the network the exact concept, we train the network on a series of approximations (refinements) of the concept. The first approximation is very crude, and therefore we allow a very large error. As the approximations become more accurate, we require increasing accuracy from the network. The preliminary experiments using this strategy were relatively disappointing in terms of improving performance for various classes of problems. While we found applications where the method improves performance (measured as the number of iterations to learn the concept class) in a majority of cases the new algorithm was comparable in speed and accuracy to the old one. Our findings which will appear in a forthcoming report.

## 5.3 Geometric Concept Learning

We (as well as many others) observed that there are fundamental links between geometric partitioning algorithms and machine learning. We used combinatorial techniques and computational geometry to study basic properties of learning algorithms. This investigation is the main topic of a Ph.D. thesis by David Heath. David Heath's research has been supervised by Kasif and was fully funded by AFOSR. Preliminary results from his thesis have been published in [HKK<sup>+</sup>91, SHDK91, Hea91, HKS92] Below we briefly describe these topics.

## 5.4 Limited Memory Learning

The majority of learning algorithms (including connectionist algorithms) use limited memory (a fixed size network) during learning. We addressed the problem of the complexity of learning when the algorithm is allowed to store only the generalization. It cannot store the entire set of examples and process them off-line. One way to abstract this restriction is by enforcing a limited memory requirement. That is, the algorithm is restricted to some small number of memory locations. We recently completed a paper where we establish fundamental bounds on the number of steps necessary and sufficient to learn concepts when the learning module is not allowed to store all examples. The paper is the first of its kind to establish a fundamental trade off in the number of steps required to learn a concept and the size of the generalization used by the algorithm. Our results are summarized in [HKK<sup>+</sup>91]

## 5.5 Learning with Helpful Teacher

Research in theoretical machine learning focuses on the complexity of learning a concept class independent of particular learning architectures. In general, this research does not address the following important questions. What are the strengths and weaknesses of a learning algorithm when applied to a particular learning problem? How do particular algorithms compare with each other? What is the right way to teach a given concept to a particular learning machine? Does providing additional examples always help learn a given concept?

We address some of these questions in the context of nearest neighbour and other learning methods. A theoretical model is introduced where the teacher knows the learning algorithm and chooses examples in the best way possible. We call this the Helpful Teacher model, and note that it often requires a very small number of examples to learn a concept. We prove some lower and upper bounds for a variety of geometric concept classes. This is joint work with Art Delcher, David Heath, and Steven Salzberg. Our initial findings on this topic are summarized in [SHDK91] where we also discuss the implications of our results for current experimental research.

We also addressed the problem of the complexity of being a Helpful teacher. We show that the complexity of presenting the best possible set of examples for geometric problems is NP-hard. In the process of solving this problem we produced several new computational geometry results [Hea91, D.92].

## 5.6 Learning Oblique Decision Trees

We recently began investigating the following natural generalization of perceptrons. Given two sets of points (e.g., blue/red) in  $n$ -dimensions and an integer  $K$ , find a hyperplane that partitions the set into two categories such that at most  $K$  points are misclassified. We proved this by transformation from the dual problem, namely given a set of  $N$  linear inequalities, is there a feasible solution that excludes at most  $K$  inequalities. This problem is NP-complete by an easy transformation from 3SAT.

This result should be contrasted with the existing complexity results on the scalability of learning in networks. The majority of the NP-completeness results such as Judd's and Blum and Rivest's that address the representation issue. That is, find a boolean function (threshold circuit) of a certain architecture which is consistent with the training set. But when the network does backpropagation, it usually stops when a certain accuracy is achieved, or alternatively in the case of boolean functions, the network is partially consistent with training set. The question above directly addressed the problem of learning a function with a given accuracy. Our complexity result shows that this problem is difficult even for a single hyperplane.

We got interested in learning with given accuracy when we were thinking about geometric versions of decision trees, where the decision surfaces are allowed to be linear combinations of features. Such decision trees generate space partitioning by convex polyhedra. The majority of practical work on decision trees seem to address axis-parallel decision trees (e.g., ID3). We recently developed a new algorithm for decision tree induction based on the approximate constraint solving paradigm. We developed a general constraint solving



technique that allows us to solve approximate linear programming problems. A simple instance of this class of problems is finding a solution to a set of linear inequalities such that the largest number of such inequalities is satisfied. Our algorithm allows us to synthesize the smallest known decision trees for several applications such as breast cancer diagnosis and classification of astronomical data while preserving the prediction accuracy of previous methods. Our results are described in [HKS92].

## 6 Summary

To summarize, we have developed a strong research program in several areas. Our main contributions thus far are in the area of parallel complexity of constraint networks, and basic properties of geometric partitioning algorithms with applications to learning.

Our results in the area of parallel constraint networks are the subject of several publications in first rate journals and conferences. Our group's experimental research achieves the best results on several well established benchmarks. Most notably we achieved the best performance (in terms of prediction accuracy) in the area of protein folding, improving on the back propagation algorithm. We studied several fundamental geometric partitioning problems that have direct implications on lower and upper bounds on the number of examples needed to learn geometric concepts. We introduced a new model that allows us to derive lower bounds on the number of examples required for learning geometric concepts. The model also allows us to study the computational complexity of teaching rather than learning. We also derived the simplest known complexity result for the scalability of learning in networks, namely approximate learning of a perceptron. We developed a set of programs that construct non-axis-parallel decision trees which are significantly smaller than previously constructed trees for the same domains.

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