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J. J. Molitoris

Submarine & Antisubmarine Warfare Department



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# Elementary and Advanced

# Computer Projects

# for the Physics Classroom and Laboratory

# J.J. Molitoris

# Center for Naval Analyses 4401 Ford Avenue Alexandria, VA 22304

# <u>Abstract</u>

A series of computer based student research projects and programs for use in the physics classroom and laboratory is described.

The commercial programs are SPF/PC, MS Word,  $T^3$ , Symphony, Mathematica, and FORTRAN. The authors' programs assist data analysis in particular laboratory experiments and make use of the Monte Carlo and other numerical techniques in computer simulation and instruction. The one dimensional Ising model is presented as a good example of the application of both analytical and simulation techniques in physics. The consistent use of this project based teaching approach in a college physics program enhances the students' education and interest.

An article for the Journal of College Science Teaching.

# I. Introduction

Computer programs in general and Computer Assisted Instruction (CAI) in particular have not lived up to their promise in physics education. Part of the reason for this is perhaps resistance from students and physicists who have not grown up with computers. People, like the objects of physics, have a tendency to resist change (inertia). The impact of the computer is perhaps so great as to require essential modifications in teaching style.<sup>1</sup> Physicists can be quite radical in frontier research (where computers are firmly established in a new scientific triad: experiment, theory, and computation), but very conservative in everyday teaching.<sup>2,3</sup>

However, the Personal Computer (PC) has been around since the 1970's and has just become ubiquitous in the 1980's. Small size and low price ensure wide availability. Hence, perhaps the time is ripe in the 1990's and beyond for educators and students to take full advantage of the PC. Indeed, computer literacy is today one of the important outcomes of a quality education. Computers and computer programs are now a common part of the techniques which aim to improve physics teaching.<sup>1-5</sup> The lecture method, where the information passes from the notes of the instructor to the notes of the student without going through the mind of either, is hopefully on the decline.

What is CAI and how can computers be effectively used? Computers can be used to teach information, skills, and even critical or scientific thinking<sup>4</sup> through a series of interactive computer based lessons - for drill and practice, games, tutoring,

problem-solving, and simulations.<sup>5,6</sup> The goal of CAI is obviously not only to teach by drill and practice the physics concepts which a student has missed in class. However, such drill and practice can be useful<sup>7</sup> in certain circumstances. One must select material to teach in any physics course since you can't cover the whole 700 page text in one year (although many professors try to)! Also, a CAI program for pre-medical students could help them prepare for the MCATs and thus give the instructor more freedom to teach a novel and creative course. Likewise, a CAI program for engineering students could help the students prepare for engineering courses, and allow the instructor the same liberty. Further, in cases where the student/faculty ratio is large (as in many first year courses), the computer can provide the one-on-one environment that is more conducive to education.

# II. Computer Based Research Projects

One of the best ways to use computers in physics education, and the focus of our discussion here, is as a tool in individual student research projects for simulating both simple and more complicated phenomena.<sup>5</sup> The instructor must be very knowledgeable about all the projects, perhaps having done them himself/herself in advance. The instructor can integrate the projects into a standard course by an appropriate choice of topics and with in-class student presentations or progress reports. The student must interact significantly with the instructor, who guides him/her through the project. The student

needs to spend much time in the library researching the project in the appropriate journals and books. The instructor can provide a list of references to get the student started. In some cases, the student can also do a related laboratory experiment.

Computational physics projects can help to make a course more contemporary by including exciting information about chaos, fractals, relativity, quantum mechanics, and particle physics. They can reduce drudgery and show the new emphasis on numerical rather than analytic solutions to problems.<sup>1,5</sup> Analytic skills can also be enhanced by emphasizing calculus methods and techniques. Computer projects can help to insure that students improve their conceptual understanding, as well as retain essential facts. Through the computer's speed and power, one can connect the simple physics to help the student understand complex physical or engineering problems.

Computer assisted instruction and simulations are not, however, intended to become a substitute for the teacher.<sup>8</sup> They can only supplement the essential human component of education. Administrators (as well as teachers) must have adequate training in computer use (be computer literate) and be supportive of faculty innovation for computers to be effective. Schools and colleges need to have the requisite financial, programming, and technical support for the instructor.

Clearly computers are not a panacea: they are not the answer to all the problems in physics education. But they can be a powerful instrument to reinforce and supplement the lessons of the classroom. A good CAI program or assigned research project

can motivate some students to spend time researching at the library or inspire them to think and ask questions of their peers and instructors.

We are interested specifically in the application of personal computer hardware and software to a high school or college/university physics environment. What is first necessary is a laboratory of computers dedicated for use by physics students. Assuming a class size of ten to twenty students, a minimum of ten computers is needed. (For departments that lack money, a few personal computers is certainly better than none at all.) These computers need not be IBM compatible, but we have chosen that as the standard. In fact, we have used Zenith computers. Machines of the IBM AT type (Z-200 series) based on the 80286 chip or even the 80386 chip (Z-300 series) are preferred over those which use the slower 8088 chip. The computers could all be linked to a laser printer (HP Laserjet Series II) or, as we have done, two or three computers can share a high quality text/graphics printer (Epson EX-800 or FX-850).

Each machine can be outfitted with two 1.2 MB floppy drives for efficient file transfer and backup. An 80287 math coprocessor is useful for speed in numerical computations and increasing the system recalculation speed. A 20 MB hard drive will do, but 80 to 100 MB will be much better in the long run. For example, if one is to do complicated calculations with advanced students, the 800 routine IMSL FORTRAN libraries alone require 20 MB.

Color monitors make it easier to maintain the students'

interest in this age of color graphics, television, and video. VGA graphics with 640 by 480 pixels is the current high resolution standard and is available with the Z-549 and many other video cards.

Such a physics laboratory<sup>5,9</sup> can be started in numerous ways. For the high school/college/university without much money, a single computer with the necessary hardware and software could be purchased by the instructor for less than \$3000. If funds are not available from a departmental budget or the administration, often a local foundation (like the Kiwanis Foundation in Allentown) will provide a grant of up to \$2000. Grants are also available from many other sources including the military, the National Science Foundation, and organizations like the Pew Charitable Trust.

# III. Commercial Programs

There is a plethora of available programs for an IBM compatible personal computer.<sup>10</sup> What is useful to students and professors of physics are a screen manager (e.g. SPF/PC 2.1), word processor (Microsoft Word 4.0), scientific word processor  $(T^3 2.21)$ , spreadsheet (Lotus Symphony 2.0), symbolic mathematics package (Mathematica 2.0) and a programming language (Ryan McFarland FORTRAN 2.4)

SPF/PC is a Systems Productivity Facility for the PC costing about \$100. It allows you to edit ASCII files, execute DOS commands from a command processor, and even define your own user applications. The computer helps us to manage information, and

programs like SPF/PC aid us in managing the computer. Microsoft Word is a well known word processing program and sells for about \$200. The word processor is used by the student and professor to compose, modify, correct, and finally print research papers. It is useful for both local and global revision, the latter being done on a printed hard copy.

 $T^3$  is the scientific word processing system on which this document was prepared (cost \$600). It is essential for the typing of mathematical equations for lab reports, lab write-ups, tests, and research papers. Symphony can be used as a word processor or data base manager, as well as a spreadsheet (cost \$400). We like the look and feel of Symphony as a spreadsheet over that of Lotus 123. The instructor can use Symphony to keep a record of grades. Both the students and the professor can use it to tabulate numbers and plot graphs.

Mathematica is a numeric, symbolic, and graphical system for doing mathematics by computer (cost \$800). It is able to differentiate and integrate symbolically, numerically evaluate a definite integral, numerically solve a differential equation using a 4th order Runge-Kutta method, solve eigenvalue and eigenvector problems, do matrix multiplication, simply plot functions in two or three dimensional contour or perspective and in color, and also perform many other useful tasks.

FORTRAN is still the language of science and engineering in industry and government laboratories (alth..gh C is becoming a powerful competitor). RM/FORTRAN (cost \$400) is one implementation of this powerful and useful programming language.

It is important that the student learn to program not only as a useful and marketable skill, but also because this helps one to think about how to approach problems in general. Furthermore, the content and operation of one's own program is more manifest and easily adaptable than say a spreadsheet or other commercial program.

# IV. A Computer Programming Laboratory

We mention here a computer laboratory<sup>5,9</sup> which has been used successfully at both Muhlenberg College and Cedar Crest College in Allentown with both introductory and advanced students. A copy of the laboratory hand-out is available on request from the author. The laboratory exercise is called <u>Computers and</u> <u>Programming</u> and the students take about two lab periods (4 hours) to complete the activity. This instruction is useful because throughout the students' four year long physics education, computer programs are used to aid the experimental data analysis and for simulations.

The object of the exercise is to study computers and FORTRAN programming. The basic history of computers and their use is discussed as well as the essentials of FORTRAN programming. It is really remarkable that today a personal computer has a mass less than 50 kg (some notebook computers even less than 1 kg), occupies less than 1/2 square meter, and can do more than the 130 Megagram 140 square meter 1946 University of Pennsylvania ENIAC could.

By the end of the laboratory, the student has created a simple

FORTRAN program to (for example) find the average and standard deviation of n numbers. Clearly, the physics major needs to go beyond this introductory laboratory exercise. This can happen through a formal course in computer science, course related projects, and/c<sup>-</sup> a summer research project. Course related computer projects are most useful since they stimulate interest in physics and allow the students a unique way to demonstrate their understanding.

# V. CAI and Computer Programs for Student Research Projects

A CAI package of 114 programs in 12 volumes on general physics from vectors to atomic and nuclear physics is available from Cross Educational Software for about \$300. These programs feature extensive graphics with animation, color, and sound. A summary of other available software may be found in the literature.<sup>10</sup>

The programs written by the author have been developed and tested for use by first year advanced and also upper class physics students. The basic idea is that the student works on his/her own computer program as part of a research project. The programs and projects described here should thus be a guide to the professor and student. As part of this project based approach to physics eduation, the student should present one or more talks on the project. These oral presentations can be done in class, at a specially scheduled mini-conference, or even at a local physics society meeting (NSTA, AAPT, or APS). If the presentations are to be done in class as part of a course, the

intructor can choose one or two readings from appropriate journals (e.g. <u>Scientific American</u> or <u>Physics Today</u>) or books for the students to read for the class. In this way, all the students can take part in a discussion about the project and the project becomes part of the material studied for the course.

These computer projects have been used in the classroom and laboratory, as well as outside formal class meetings. This naturally requires student interest and commitment. Actually, students enjoy the projects and programs and consider them important parts of their physics education. The programs are especially relevant for a course in Classical Mechanics, Nuclear Physics, or Statistical Physics and as supplements to other courses. The excellent graphics enhance the learning of material and retain the students' interest. The organization of the programs are logical and apparent to the user. All responses to program questions have an indicated default value.

The Monte Carlo program *monte* (development initiated by Dr. Pat Bronson) begins by spelling out the words Monte Carlo on the screen using the BASIC random number generator. After a title page comes some general information about the Monte Carlo method and probability theory.<sup>11,12</sup> At this point, one is presented with a menu which allows s/he to quit the program, obtain further information about the Monte Carlo technique, learn about the random walk, nuclear decay, the absorption of pions, or scattering processes. There are numerous references in the literature to the Monte Carlo method.<sup>13-17</sup>

The Math Tutor program math (development initiated by Chris

Brueningsen) allows students the opportunity to be introduced to and/or review scientific notation, basic algebra, trigonometry, and the calculus. The physics major needs to go beyond this and learn about methods of numerical integration, random numbers, and how to numerically solve differential equations. Programs numint and numode facilitate this study.

Other computer software available to aid the data analysis of laboratory experiments<sup>9</sup> include: *vector* and *sumxy* for a force table experiment; *kinem* for a linear air track experiment; *plotit*, *linzer*, *quazer*, *linlst*, and *qualst* for any experiment which requires plotting data or linear or quadratic least squares fits (zero-intercept or regular); *shm* for a pendulum simple harmonic motion experiment; and *consmom* for a planar air table experiment.

Most of these programs are written in FORTRAN and require EGA graphics and a numerical coprocessor. Output may be directed to the screen, an Epson compatible printer, a Laserjet compatible printer, or a Hewlett-Packard 7475 plotter. The quadratic least squares program *qualst* is part of the 1990 Plot88 shareware collection. EGA/VGA graphics from any BASIC program or Mathematica plot may be dumped to the HP 7475 plotter using a program called *markplot* developed by a computer science student (Mark Hyatt) at Muhlenberg College.

Some classical mechanics programs are: *lissaj* which draws Lissajous figures; *pendorb* which draws phase space orbits for a pendulum; *shmorb* which draws phase space orbits for a mass on a spring in simple harmonic motion; *realfall* which solves the

equations of motion for a spherical object falling in a fluid medium using 4th order Runge-Kutta methods; and *real2d* which does the same thing but for two dimensional projectile motion. The program *chaos* generates time series and the bifurcation diagram for the logistic difference equation, as well as allowing an investigation of the dynamics of the damped forced nonlinear pendulum. *Mandel* and *mandplt* allow an investigation of the Mandelbrot set and *koch* studies the Koch fractal.

For electricity and magnetism, the program *electric* allows one to plot electric field vectors for n point charges. *Equipot* plots the equipotential lines for a single point charge and *equidip* plots the equipotential lines for a dipole.

The program random allows an investigation of the randomness of the pseudo-random numbers generated by an IMSL FORTRAN routine and some other algorithms. *Ranwalk* implements the one to three dimensional random walk using the Monte Carlo method. *Isingcan* allows the Monte Carlo study of the one dimensional Ising model with regard to the total energy and the magnetization. Comparison is made to the complicated exact theoretical formulae in both *isingcan* and *ranwalk*.

Several other programs are also available free on request from the author. *Impact* studies the material impact of a right circular metal cylinder on an anvil. Computer software related to nuclear physics - in particular the Fermi gas model of the ground and excited states, giant quadrupole resonances, and a shock model of central nucleus-nucleus collisions - are *ftfermcm*,

quad, and shockcm. Clearly, there are unlimited possibilities for student research projects.

# VI. Some Sample Results and The Ising Model

Let us consider some of the graphical results of the student research projects and computer programs. On the computer, all of the figures would be displayed in color. Figure 1 shows a Lissajous figure from program *lissaj*, which occurs in the study of two dimensional oscillations in a Classical Mechanics course. The curve is closed because the motion repeats itself at regular intervals of time. Figure 2 shows a stage in the development of the Koch fractal from program *koch*. This curve has a fractal or fractional dimension of 1.26, i.e. it is between a line and a plane in dimensionality.

Figure 3 shows a chaotic time series from program *chaos*. Here, one studies the complex, irregular, and apparently random behaviour of many physical phenomena. The values of x in this discrete sequence for times 0, 1, 2, ... have no obvious pattern. Figure 4 shows the velocity-time curve for the free fall case (straight line) and the realistic fall of a .05 cm steel sphere falling in air, as simulated with program *realfall*. Notice that the object achieves terminal speed after about 2 seconds. Figure 5 shows the probability of being at a particular distance r from the origin in a three dimensional three step random walk, from program *ranwalk*. We take fixed steps of unit size with the angles  $\theta$  and  $\phi$  chosen randomly. The computer simulation

probability (boxes) and the analytic theory (solid line) agree very well.

To be more specific, we now consider the Ising model simulation in more detail. A more mathematical discussion of this and some of the other research projects is available on request.<sup>18-21</sup> Many of these projects are discussed in a number of computer simulation and modeling books<sup>22-25</sup> but not always in sufficient detail. The Ising model attempts to simulate the structure of a ferromagnet.

The system considered is an array of N lattice sites or spins at temperature T. Each lattice site has an associated spin  $\sigma_j = \pm 1$ . The Hamiltonian or total energy for the n dimensional Ising model involves an interaction strength *a*, the single particle magnetic moment  $\mu$ , and the external magnetic field B. The actual value of *a* depends upon more detailed theory. We consider here the one dimensional Ising model (n = 1).

The analytic formulae for the energy U = U(B,T) and magnetization M = M(B,T) can be obtained exactly using statistical physics and are quite complicated.<sup>18</sup> One would certainly not be able to guess them from any data or simulation. However, the analytic theory is essential and in the one dimensional case tractable.

Program *isingcan* implements the one dimensional Ising model discussed above using the Monte Carlo method. The program is available free of charge on request from the author. The user inputs the size of the ring or the number of spins N, the temperature T, and the magnetic field B ... be studied. The

program then either loops over a range of B values at fixed T or a range of T values at fixed B, as chosen by the user. The number of Monte Carlo steps  $n_m$  and number of initial configurations  $n_c$  are also input.

An IMSL random number subroutine is used to set  $\sigma_i = +1$  if a uniform [0,1] random number is greater than 0.5 and -1 otherwise. This first ensemble or configuration of spins is then run through the n<sub>m</sub> Monte Carlo steps.

In each step, a spin (say j) is randomly selected and the change in energy from flipping that spin computed. If the energy change is less than or equal to zero, then the spin is flipped. The Monte Carlo approach aims to minimize the energy or relax the system towards thermal equilibrium. Otherwise a temperature dependent Boltzmann factor is computed. If a random number is less than or equal to this factor, then the spin is flipped. This procedure is repeated N times.

The energy and magnetization after relaxation are saved after the  $n_m$  Monte Carlo steps. Then the procedure is repeated for a new ensemble or initial configuration.

Shown in Figure 6 is a comparison between the computer simulation (boxes) and the analytic theory (solid line) for B = 1and a range of temperatures. The lattice size or number of spins is 100. At zero temperature, all of the spins tend to align with the magnetic field, as one would expect. For higher temperatures, the thermal energy of the system tends to destroy the alignment. The agreement of the simulation with the exact results is quite remarkable.<sup>18</sup>

# VII. Summary and Conclusions

Typically, an advanced student would work on a research topic like the Ising model for a semester or more. Such research projects have strengthened the physics major at Muhlenberg College. Over the past three years about 90% of the graduating physics majors have worked on Monte Carlo and other computer projects. For the past three summers, 50% of our majors were involved in a for pay Summer Science Program at Muhlenberg utilizing computational research projects.

This system of programs remains under development. It will be extended and modified by the author and his students over time. Any of the topics in the chaos, koch, monte, isingcan, quad, random, ranwalk, realfall, real2d, and other programs make excellent review and research topics for the physics student.

As we have seen, computer based student research projects in general have a vital role as a powerful innovative teaching tool. This approach to physics education is based on the premise that students benefit from well-structured material, graphic presentation, and supplementary ideas and instruction. Through simulation programs and the laboratory interfacing of computers, students can learn through analyzing, exploring, and manipulating their environment.

Our thanks to the many students who have worked on these programs including Robin Balla, Dave Brown, Scott Kaeppel, Rory Klinger, Jeff Mahn, Joe Maselli, Kathy Massopust, Brennan Milligan, Drew Paulson, Chris Scott, and Matt Wingate. We are also grateful to Barbara Negus of the Center for Naval Analyses

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# Appendix: List of Manufacturers

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# Figures

Figure 1: A Lissajous figure for two dimensional oscillations.

Figure 2: The Koch fractal with fractional dimension 1.26.

Figure 3: A chaotic time series from the logistic difference equation.

Figure 4: The velocity versus time for vacuum and realistic fall.

Figure 5: The three step three dimensional random walk probability function.

Figure 6: The magnetization versus temperature in the one dimensional Ising model.

# Lissajous Figure



Figure 1: A Lissajous figure for two dimensional oscillations.

koch curve

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Figure 6: The magnetization versus temperature in the one dimensional Ising model.



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