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A DETECTOR FOR STATIONARY GAS BUBBLES: FEASIBILITY STUDIES

G. Albin P. Massell W. Mints J. Himm SHAY211992

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Naval Medical Research and Development Command Bethesda, Maryland 20889-5044

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system's ability to detect bubbles categorically (i.e., "bubbles" or "no bubbles"). To predict the S/N ratio for single bubbles in water, we have been used mathematical simulations of vibrating bubbles in conjunction with measurements of the system noise. Solutions have been obtained for the equation of motion outside of a bubble vibrating in a liquid or in an elastic solid using both an approximate analytic technique (namely, the Method of Perturbation) and a more accurate numerical technique (a Galerkin method).

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I. INTRODUCTION

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Symptoms of decompression sickness (DCS) typically are assumed to result from the formation of gas bubbles in blood or extravascular tissue. Information on extravascular bubbles has been severely limited by the lack of any noninvasive method of observing them.

In a previous report (NMRI Technical Report 91-39, Basic Operation of a Detector for Stationary Gas Bubbles¹), we discussed a system constructed at the Jet Propulsion Laboratory (JPL) that uses ultrasound to detect stationary gas bubbles. We call the system the 'JPL swept frequency bubble detector', or simply the 'bubble detector'. The bubble detector can, in principle, enable the quantitative measurement of the sizes and numbers of stationary extravascular bubbles. Its theory of operation depends on these facts: 1) gas bubbles are the softest objects in tissue, and consequently undergo the largest deformations when vibrating in a sound field, 2) although vibrations are linear at sufficiently small deformations, they become increasingly nonlinear at larger deformations², and 3) nonlinear vibrations contain harmonics and subharmonics -- that is, the vibrations contain multiple frequency components even when the driving signal is monotonal. In theory therefore, when tissue is driven to vibration by externally applied sound of moderate amplitude, any harmonics or subharmonics in the sound backscattered from the tissue should be attributable to gas bubbles rather than to stiffer objects. More specifically, the bubble detector is designed to exploit the 'second harmonic' component of the energy backscattered by vibrating bubbles (the component having the frequency twice that of the driving signal).

A brief description of the bubble detector is offered here. The reader should look to reference 1 for a more comprehensive discussion.

The bubble detector uses a transmitting pressure transducer to broadcast a swept-frequency sound pressure field onto a target and a receiving pressure transducer to detect the sound backscattered from the target. It then filters out all frequency components in the output signal except for either the second harmonic or the 'fundamental' (the component having the same frequency as the driving signal), as desired. The filtered signal is then processed to give two types of conditioned output signals. In the 'range' mode the system produces an amplitude spectrum (i.e., a plot of amplitude versus frequency) in which the independent variable is the difference in frequency between the transmitted and received signals. This frequency offset is proportional to the time delay between sound transmission and reception of the backscattered sound from the target. The distance from the transducer head to the target is calculated from the corresponding frequency offset.

In the 'frequency response' ('FRC') mode, the system generates a spectrum in which the independent variable is the frequency of the transmitted signal (referred to hence as the 'forcing frequency' or 'driving frequency') and the dependent variable is the amplitude of the backscattered signal from any targets that are at a certain preselected distance from the transducer head. This output shows the 'frequency response' of the system consisting of both the bubble and the bubble detector; that is, it shows how strongly the system responds to its input as a tunction of the input frequency. In theory, this information should enable one to assay a bubble population: the location of a

resonance peak in the spectrum depends on the bubble diameter and the peak size is proportional to the number of bubbles at that diameter. The transducers supplied by JPL operate over a frequency range of ~1-7 Mhz, which encompasses the main resonance frequencies of bubbles in H_2O of roughly 0.9-6.0 microns diameter, so we can reasonably expect to be able to identify bubbles in this size range.

The first technical report in this series dealt with the basic operation of the bubble detector. As it was being written, the following goals had been achieved:

- A computer routine that uses an approximate, analytic solution to the differential equations describing a vibrating bubble to compute the amplitude of the second harmonic component of the sound radiated from a bubble *in a viscous liquid* as a function of the frequency of incident sound.
- 2) A protocol for preparing calibration standards consisting of known bubble populations by trapping gas bubbles in transparent hydrogels and determining the sizes and numbers of bubbles in the gels microscopically.
- 3) Indications that, through conducting preliminary, semi-quantitative experiments with bubbles in hydrogels, the signal/noise ratio of the system as delivered was unacceptably low.

We report here on our continuation of bubble detection studies. The work generally has been directed toward redesigning the original system to remove shortcomings that

In NMRI Technical Report 91-39, it was stated that the transducers operated over the frequency range 0.2-5 MHz, encompassing the main resonance frequencies of bubbles of ~1-20 μ m diameter. This statement was erroneous. By direct measurement, the frequency response of the bubble detector system as a whole is reasonably strong over the range of ~1-7 MHz; the manufacturer of the transducers states that the transducers were *designed* for operation over the 2-10 MHz range.

severely limited its utility, and determining whether the output signal-to-noise (S/N) ratio is high enough to enable quantitative analysis of the data for bubbles up to 6 μ m diameter. We eventually had to evaluate the S/N ratio using theory rather than empiricism because we have found bubbles this small to be too short-lived *in vitro* to permit their examination using both the bubble detector and a suitable microscope (the latter being used to establish bubble size). In fact, the theory discussed in Section V on the stability of bubble populations in a closed system suggests that it is impractical to extend the lifetimes of such small bubbles to sufficient length for our purposes in a system of constant surface tension.

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The following new goals have been achieved and will be discussed in this report:

- Replacing the analogue AM tuner, which was provided with the original system for demodulating AM signals, with a commercially available signal analyzer capable of digital demodulation. This improves the system's S/N ratio somewhat. More importantly, the signal analyzer has been interfaced with a PC upon which digitized data can be stored, which makes the numerical data available to us for the first time.
- Exploring strategies for preparing suitable calibration standards consisting of quasi-stable bubbles trapped in polymer gels.
- 3) Elucidating whether small spherical bubbles can be stabilized (for the purpose of producing calibrants) without invoking complicated mechanisms involving variable surface tension or variable permeability at the bubble surface.

Developing and exploring a mathematical simulation of the growth and shrinkage of bubbles in a closed system with finite surface tension.

- 4) Developing an approximate, analytic solution to the differential equations describing a vibrating bubble in an *elastic solid* and coding it as computer routines. This approach uses linearized elastic theory (valid for small deformations) to model the elastic stress associated with oscillations and nonlinear elastic theory to describe the potentially large elastic stress present at the bubble wall at rest.
- 5) Writing into computer code a more accurate, numerical solution to the differential equations describing a vibrating bubble in a viscous liquid and in an elastic solid.
- 6) Measuring system noise has been measured.

7) Estimating the S/N ratio of the system for single bubbles in the size range for which the system was designed by using the system noise measurements and the predictions of the mathematical models.

The mathematical simulations mentioned in items 4 and 5 will allow computation of the amplitude of the 2nd harmonic component of the sound radiated from a bubble as a function of the frequency of incident sound.

The analytic expressions noted in item 4 can be evaluated quickly enough on even a modest computer to make them useful for deducing the sizes and numbers of bubbles in a sample containing an unknown bubble population using an iterative curve-fitting/parameter estimation approach, as follows:

We will fit a curve to the voltage amplitude versus driving frequency data provided by the bubble detector in its 'frequency response' mode, with the values of bubble diameter and bubble number taken as adjustable parameters to be optimized in the curve-fitting routine. The data-fitting will consist of minimizing the sum of squares of error (SSE) using a Marquardt least-squares algorithm.³ The SSE is a measure of the goodness-of-fit of the model to the data. The independent variable is the driving frequency, the dependent variable is the voltage amplitude, and for an unknown target sample the parameters to be estimated are bubble radius and bubble number. The Marquardt algorithm is an iterative routine that systematically adjusts the values of each unknown parameter 'B' based on the value of $\partial(SSE)/\partial B$ in the current iteration.

The numerical solutions mentioned in item 5 are much more CPU-intensive than the analytic expressions, but presumably more accurate, and will be used to evaluate the accuracy of the analytic solutions. There is a lack of experimental verification of any theory's predictions regarding the 2nd harmonic component of bubble oscillations.

The simulation of bubble dynamics (listed as item 3 above) indicates that quasi-stable bubbles of diameters $<100 \,\mu$ m cannot be obtained in a system of constant surface tension. Our own efforts to obtain small, quasi-stable bubbles (mentioned above in item 2) produced no results to the contrary: we were unsuccessful in attempts to prepare suitable calibration standards containing bubbles in the size range of interest.

The mathematical descriptions of bubble behavior from items 4 and 5 enable us to estimate the output voltage amplitude that should be observed for a 6 μ m bubble driven

at its main resonance frequency. (Thic is the strongest output signal that would be observed n any bubble of $\leq 6 \ \mu$ m diameter at any driving frequency.) By comparison with the measured noise floor, we have estimated the S/N ratio. The result of this estimate casts some doubt on the practicality of quantitatively studying individual bubbles in the 0.9-6 μ m range. The proper course of action may be to study larger bubbles, thus increasing the S/N ratio without improving any electronic components. This necessitates the purchase of pressure transducers designed to operate over a lower frequency range than the pair originally supplied. The size range of stationary bubbles that are most relevant to DCS is unknown, so there is no reason to insist upon studying bubbles of any particular size range so long as the size is physiologically plausible.

II. ADDING DIGITAL AM SIGNAL DEMODULATION TO THE SYSTEM

A. Impetus for adding digital AM demodulation

As noted in the Introduction, the bubble detector has two operating modes: the 'range' mode, in which the signal is Fourier-transformed to give information on bubble location, and the 'frequency response', or FRC mode, in which the signal is demodulated to give information about the sizes and numbers of bubbles.

For the frequency response mode, the bubble detector (as delivered by JPL) included a section for analogue demodulation of amplitude modulated (AM) signals; i.e. an AM tuner. The tuner consisted of a local oscillator, a mixer, and a low-pass filter. It was noted in reference 1 that the tuner section was a significant noise source. It was noted also that the bubble detector's output signal was analog and that no means had been provided for digitizing or recording the output, preventing meaningful data analysis. In addition, the output was not an amplitude spectrum, as expected from a system intended to function as a spectrum analyzer, but rather was the sum of waveforms of various frequencies, each waveform associated with one of the acoustic targets in front of the pressure transducers. This sort of output does not lend itself readily to objective analysis.

In order for the bubble detector to have potential as a research tool, the problems noted above must be overcome. Replacing the AM tuner with a digital signal analyzer capable of AM signal demodulation can solve all three of them. Digital signal processing does not contribute appreciably to noise, commercially available digital

processors normally can be interfaced with computers on which data can be stored and processed, and we will see that the output of an AM demodulator for this system is an amplitude spect. um whose relationship with the physical system under study is easy to conceptualize.

B. <u>Hardware</u>

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Demodulating an AM signal is equivalent to recovering the amplitude versus time information; for this system the input frequency is a linear function of time, and therefore the demodulated signal is equivalent to a spacetrum of amplitude versus forcing frequency. A Hewlett-Packard 3561A signal analyzer was chosen for the task. This machine cannot actually demodulate signals, but it can separate a signal into its real and imaginary parts. These are captured and sent to a FC, on which the amplitude is computed at each time point simply by taking the square root of the sum of the squares of the real and imaginary parts. The HP 3561A simultaneously carries out a fast Fourier transformation (FFT) on the signal, thus performing the range mode task at the same time as it handles the FRC mode function.

C. Software

The Appendix contains the HP Basic program used to remotely control the HP 3561A and the HP 3325A signal generator from an IBM-compatible PC in which a Hewlett-Packard Basic Language Processor card has been installed. The program runs measurement 'cycles', pausing between cycles for a user-selectable length of time. During each cycle the program 1) prompts the bubble detector to make a series of measurements, 2) extracts the raw output from these measurements from the signal

analyzer, 3) converts them to amplitude-versus-forcing frequency spectra for the FRC output, 4) averages the spectra from multiple measurements (i.e., uses 'signal averaging') to minimize white noise, 5) subtracts from the spectrum a signal-averaged "background" measurement taken at the beginning of the experiment when bubbles are absent, 6) stores the result to hard disk, and 7) plots the result on a Hewlett-Packard printer. The user chooses an appropriate target for the background measurement. For example, if bubbles are to be formed in an acoustical target during the experiment, one chooses as background the target itself before the introduction of bubbles.

Simultaneously, the 3561A also performs an FFT on the data for the range mode output. The result is transferred to the PC along with the FRC spectrum and is then printed. A few examples of the final outputs from both the FRC and range modes are shown in the following section.

The program allows the user to select values of the following operating parameters:

- 1) frequency range of the frequency sweep (i.e., the start and stop frequencies)
- 2) sweep time

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- 3) voltage amplitude generated by the 3325A signal generator
- 4) analyzer frequency 'span' (explained below)
- 5) 'start frequency' for the analyzer (explained below)
- 6) number of sweeps to be averaged together during the cycle in which the background noise is measured
- number of sweeps to be averaged together during each cycle in which a signal is measured

8) how long to pause between cycles

D. <u>On the selection of operating parameters</u>

We will now consider the analyzer's start frequency, its frequency span, and how to chose each correctly. The HP 3561A analyzer captures all signals having frequencies between the start frequency and the sum of [start frequency + frequency span]. Higher and lower frequencies are filtered out. Therefore, the span is the bandwidth of the captured signals. The user wants the signal analyzer to capture the output signal only while the signal generator is performing a frequency sweep. The synchrony between these two instruments is realized by having the analyzer triggered by the generator at the *start* of the sweep. The analyzer also should *stop* capturing data at the same time as the sweep is completed. In other words, the 'time record' captured by the analyzer should be the same duration as the sweep time. The correct choice of span ensures this, as we discuss now.

The HP 3561A analyzer always collects $2^{10} = 1024$ digital samples per time record. The sample rate is thereby determined:

sample rate =
$$(1024 \text{ samples})/(\text{length of time record})$$
 [1]

The sample rate is always $2.56 \cdot \text{span}$. Because the time record length should equal the sweep time, we see by inspection that

span =
$$400/(sweep time)$$
 [2]

where the span is in Hz and the sweep time is in seconds. The program automatically selects the correct span for a given sweep time, and vice-versa. One must manually select the start frequency such that signals of interest have frequencies greater than the start frequency and less than [start frequency + span].

As an illustration, the frequency of the signal received from an acoustical target is given by

$$f_{signal} = \frac{2 \text{ (bandwidth of sweep, Hz)} \cdot \text{(distance, cm)}}{(sweep time, sec)} \cdot \text{(velocity of sound, ~1.5 · 105 cm/sec in water)} [3]$$

where the 'distance' in the numerator is measured between the transducer head and the target¹. For example, a 0.2-second sweep from 1 MHz to 7 MHz yields a signal of 1.3 kHz for a bubble located 3.25 cm from the transducers (the transducer head is shaped to optimize performance for a distance of roughly 3.25 cm). If we record a time record for a 0.2-second sweep, the frequency span will be 2 kHz (as shown in Equation [2]). We might set the start frequency at 1 kHz to capture all signals between 0.8 and 2.8 kHz, thus ensuring that the target associated with the 1.3 kHz signal is detected.

In the FRC mode any signals within the frequency span are lumped together in the conversion to amplitude, so that there is no resolution of frequencies for any signals that fall within the frequency span. Therefore, for the example given there is no frequency resolution in the FRC mode for signals ranging from 0.8 to 2.8 kHz. The most precise statement we could make about a bubble's location, based only on the information from

the FRC mode output, would be that its distance from the transducer head is between 2 cm and 7 cm.

Although the range mode *does* give us the information necessary for deducing the distances of bubbles from the transducers, the presence of more than one bubble will lead to ambiguity about which peak in the range mode spectrum corresponds to which peak(s) in the FRC mode. In other words, associating bubble sizes with bubble locations may be a hit-or-miss procedure.

One further point: whereas there is a large DC noise component and also some noise at 60 Hz, the start frequency should be set no lower than a few hundred Hz so that these spurious components are digitally filtered out by the 3561A before further signal processing.

III. THE OUTPUT SIGNAL

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In this section examples of the system's output signal will be shown and discussed for various acoustical targets. In all cases the amplitude of the 2nd harmonic component of the backscattered signal is plotted.

All measurements in this section were made under the following conditions:

sweep time = 0.2 sec span = 2 kHz (therefore, time record length = 0.2 sec) sweep start frequency = 2 MHz sweep stop frequency = 10 MHz windowing = flattop signal averaging: 15 time records averaged target distance ~ 3.25 cm

The frequency range is that over which the transducer pair was *designed* to operate, not necessarily the optimal range. The measurements were made using signal averaging over 15 frequency sweeps. It was observed that the averaged signal changes negligibly after ~5 averages, and therefore after 15 averages the uncorrelated noise has been minimized, so that 15 averages yields the same result as would averaging indefinitely.

Figures 1a and 1b show measurements made when the transmitted signal is reflected from a slab of Wall-Gone sound absorber. The upper plots are the FRC mode outputs and the lower ones are the range mode outputs (explained in the Introduction). The FRC portion of Figure 1a is called a 'background' measurement and the FRC portion of Figure 1b is a measurement of [signal + background - background]. There is no



FIGURE 1A: OUTPUT SIGNAL; ACOUSTICAL TARGET IS WA'L-GONE; BACKGROUND MEASUREMENT.



FIGURE 1B: OUTPUT SIGNAL; ACOUSTICAL TARGET IS WALL-GOME; SIGNAL MINUS BACKGROUND.

background subtraction being performed on the range mode output. Because Figure 1b was obtained simply by repeating the background measurement, its FRC output should show nearly zero voltage, as it does. The time at which the signal was measured is recorded in the header of each plot.

In Figure 2, we see similar measurements made with a 3-mm-thick slab of polyacrylamide (PAAm) gel sitting on top of the Wall-Gone. There are no bubbles in the gel.

Under each FRC plot we record the "positive area" between the x-axis and the positive portion of the curve and the "negative area" between the x-axis and the negative portion of the curve, computed using trapezoidal integration. They are useful indices that quantify the results in an easily understood way.

Figures 1b and 2b demonstrate that subtracting an appropriate background can reduce the noise by at least an order of magnitude. It is seen that the residual after background subtraction is much greater with the PAAm target (Figure 2) than with the Wall-Gone. This observation has been reproduced in several additional measurements with both PAAm and Wall-Gone (not shown). Obviously, the backscattered signal changes appreciably from one measurement cycle to the next when replicate measurements are made with a PAAm gel. The reason for this change is not yet clear.

The lumpiness of the frequency responses seen in the background measurements in Figures 1 and 2 results from beating between two or more signals of similar frequencies. To understand this, consider that in the experiment of Figure 2 the bubble detector is receiving signals reflected from both the front and back surfaces of the



FIGURE 2A: OUTPUT SIGNAL; ACOUSTICAL TARGET IS A 3 MM-THICK PAAM GEL MOUNTED ON WALL-GONE; BACKGROUND MEASUREMENT.



FIGURE 2B: OUTPUT SIGNAL; ACOUSTICAL TARGET IS A 3 MM-THICK PAAM GEL MOUNTED ON WALL-GONE; SIGNAL MINUS BACKGROUND.

PAAm gel simultaneously. Because the signal from the back surface has travelled $2 \cdot 3$ mm = 6 nm farther (or ~0.4 μ sec longer), its offset frequency should be ~160 Hz higher. The range mode output does in fact show two distinct frequency components separated by 160 Hz. This is taken to mean that the signal analyzer is receiving two signals that differ in frequency by 160 Hz. When they are summed together for the FRC display, the beat phenomenon appears as a 160-Hz oscillation in the amplitude. Since the time of one measurement was 0.2 second, about 32 of these beats should appear in the FRC plot, as is the case.

IV. ATTEMPTS TO PREPARE SUITABLE CALIBRATION STANDARDS

For calibrating the bubble detector, it is necessary to have standards that are subject to assay by some reliable independent method. We have prepared bubble samples of the sort that we anticipate using as calibrants and used them in some preliminary measurements intended to estimate the bubble detector's S/N ratio. We plan to use calibrants consisting of bubbles trapped in transparent hydrogels and to assay them using differential interference microscopy. Our approach is described below.

A. <u>Methods</u>

To produce the gels, aqueous solutions were prepared in the following compositions:

solution A

0.20 g/cm³ acrylamide monomer 0.01 g/cm³ N,N⁻-methylene-bis-acrylamide crosslinking monomer 1.0 μ l/cm³ N,N,N⁻,N⁻-tetramethylethylenediamine accelerator

solution B

variable 0.2-6 mg/cm³ ammonium persulfate initiator

Prior to mixing the solutions, each was sparged with nitrogen to remove dissolved oxygen, which inhibits many vinyl polymerizations⁴. Each solution was passed through a filter having a 0.22- μ m nominal pore size to remove particles that otherwise would severely confuse the microscopic examination. Equal amounts of solutions 'A' and 'B' then were mixed and the resulting solution was cast between either a pair of cleaned glass plates or a glass microscope slide and a glass cover slip. In experiments during the period covered by this report, the plates (or the microscope slide and cover slip) were separated by a 150 μ m-thick plastic spacer designed for use in casting electrophoresis gels. The monomer solution 'sandwich' was placed under vacuum for a few minutes (variable length of time). The polymerization was then allowed to proceed at ambient pressure at least until gelation occurred. Bubbles that formed by cavitation at the reduced pressure were trapped in the finished gel.

In some experiments the monomer solution was chilled to 0 °C and maintained at that temperature before and during sparging with N_2 , to increase the concentration of dissolved N_2 . Thus, the overpressure in the monomer solution, defined as [partial pressure of dissolved gas] + [hydrostatic pressure], would be higher under vacuum and would persist even after the sample had been returned to ambient hydrostatic pressure. In other experiments, a detergent (Tween 40) was added to the monomer solution to reduce the surface tension.

In order to be useful, the calibration standards must be the same size when they are interrogated ultrasonically as when they were assayed microscopically. Accordingly, the stability of these bubbles over time was tested by examining some of them under a bright field microscope over several hours' time while leaving the gel membrane sandwiched between the glass plates. Our plan was to assay the calibration standards microscopically and use the bubble detector to interrogate them within 24 h of their production; during that time their dehydration would be prevented by storage in an enclosed container whose interior was kept at the dew point by the presence of standing water.

B. <u>Results</u>

Briefly, *free* bubbles that initially were smaller than 50 μ m in diameter survived no more than a few hours before disappearing in any of the experiments. Bubbles larger

than 100 μ m survived for many hours, although their sizes were not measured accurately enough over time to allow a more precise statement about their size stability. Adding detergent to the monomer solution or keeping the monomer solution chilled during sparging with N₂ dramatically increased the number of bubbles formed, but neither treatment had the effect of stabilizing the small bubbles over several hours. Bubbles formed spontaneously at ambient pressure in the chilled monomer solution upon its removal from the ice bath.

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The shrinkage and disappearance of bubbles was easily viewed at magnification $190 \times$. The collapsing bubbles left behind spherical, water-filled cavities in the gel matrix that were clearly visible as discontinuities. By staining the gel with food coloring we could be sure of which spherical cavities contained gas and which contained water -- the gas phases transmitted more light since the dye was excluded from them.

In some experiments, a thin film of bone wax was smeared onto one spot on a microscope slide before the monomer solution was cast onto the slide. Bone wax is very hydrophobic and was found to be an excellent nucleation site, as expected. Even small bubbles persisted many hours on the bone wax. This was expected because the bone wax pretents an irregular surface with numerous crevices, and it is known that some bubbles in crevices can remain static indefinitely⁵. However, they are unsuitable for use as calibration standards because no reasonably complete mathematical description of the nonlinear dynamics of either non-spherical bubbles or of bubbles at a solid boundary is available.

V. SIMULATION OF THE GROWTH AND SHRINKAGE OF BUBBLES IN A CLOSED SYSTEM WITH FINITE SURFACE TENSION

A requisite for calibration standards for the bubble detector is that the bubbles must remain constant in size for enough time to permit their examination under a microscope and their ultrasonic interrogation. This means that they must be stable over a period of at least a few hours.

To give us an idea of how such stable calibrants might be prepared, a model was developed that predicts bubble diameter changes as a function of time in a closed system. Ideally, one would do this by solving the unsteady state continuity equation with radial symmetry. However, the continuity equation for this system is partial differential equation (PDE) because of the spatial, as well as temporal, variation in solute concentration. Solving a PDE was felt to be more time-consuming than this analysis warranted. Instead, we simplified the mathematics considerably by assuming that the flux of gas from the bubble surface is proportional to the mass transfer coefficient evaluated for a sphere in a quiescent liquid at steady-state (see Equations [4] and [11] below). The assumption of steady-state implies that the radius of the sphere, the solute concentration at the surface of the sphere, and the solute concentration far from the sphere, all are time-invariant. We also neglected the convective flux associated with bulk flow toward or away from the sphere as its size changes. All of the above simplifications are justified when the bubble size is changing sufficient slowly, and therefore are suitable for a study whose goal was to identify conditions leading to time-invariant bubble sizes.

Thermal, viscous, and compressibility effects were ignored, which invalidates the model at very small diameters (i.e., below $10 \,\mu$ m for a surface tension of 73 dyn/cm), when implosion is rapid and internal pressures are high. This is inconsequential for our application: first, we are uninterested in knowing precisely when a fast-shrinking bubble disappears; second, the system *in toto* is unaffected by these very small bubbles because they contain too little gas to be of consequence. The partial pressure of water in the gas phase is taken to be the vapor pressure of water at ambient temperature. Its dependency on either hydrostatic pressure and temperature is ignored, but again, these effects are significant only for tiny bubbles.

A. Mathematical details

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For a single spherical bubble the mole flux of gas away from its surface is

$$J = k \left(C^{surf} - C^{\infty} \right)$$
[4]

where $J = mole flux, mol/(cm^2-sec);$

k = external mass transfer coefficient, cm/sec;

 C^{surf} = concentration of dissolved gas at the <u>outer</u> bubble surface, mol/cm³;

 C^{∞} = concentration of dissolved gas far from the surface, mol/cm³.

We now make the following reasonable assumptions:

a. There is equilibrium between phases across the phase interface.

b. There is no resistance to mass transport in the gas phase, so that the partial pressure of gas at the inner bubble surface "P ^{surf}" simply equals its bulk value "P ^{bub}" in the bubble.

c. The concentration of dissolved gas C_{dis} is related to the partial pressure of gas with

which it would be in equilibrium P_{dis} according to a concentration-independent partition coefficient K (i.e., $C_{dis} = KP_{dis}$), which is a statement of Henry's Law. Equation [4] now becomes

$$\mathbf{J} = \mathbf{k} \mathbf{K} \left(\mathbf{P}^{\mathsf{bub}} \cdot \mathbf{P}^{\infty} \right)$$
 [5]

We further note that P^{bub} equals the difference between the hydrostatic pressure within the bubble and the vapor pressure of H₂O, and we account for the surface tension effect:

$$\mathbf{P}^{\mathsf{bub}} = \mathbf{\varphi} + 2\sigma / \mathbf{R} - \mathbf{P}_{\mathsf{H2O}}$$
 [6]

where ρ = ambient hydrostatic pressure, dyn/cm²;

 σ = surface tension, dyn/cm.

The mass balance on the gas inside the bubble (assuming sphericity) gives us

$$J = -1/(4\pi R^2) dn/dt$$
[7]

where R = bubble radius, cm;

n = number of moles of gas inside the bubble, mol.

Assuming ideal gas, we have

$$n = [P^{bub}(4/3)\pi R^3]/(R_G T)$$

= [(\vartheta + 2\sigma /R - P_{H2O}) (4/3)\pi R^3]/(R_G T) [8]

and
$$dn/dt = 4\pi/(R_G T) [(\Theta - P_{H2O})R^2 + (4/3)R\sigma] dR/dt$$
 [9]

where $R_G = gas law constant$, 82,057 atm-cm³/mol-°K;

T = absolute temperature, °K.

We can now combine Equations [5], [6], [7], and [9] to yield an ordinary differential equation for the rate of change of the bubble radius:

$$dR/dt = \frac{-kKR_{G}T(\theta - P_{H2O} + 2\sigma/R - P^{\infty})}{[\theta - P_{H2O} + (4/3)\sigma/R]}$$
[10]

To compute the mass transfer coefficient we use the result that, for a sphere in a quiescent liquid at steady-state the dimensionless Sherwood Number is 2.0^6 , so that

or
$$k = D / R$$
 [11]

where D is the diffusivity (cm^2/sec). Substitution into Equation [10] gives

$$dR/dt = \frac{-DKR_{G}T(\theta - P_{H20} + 2\sigma/R - P^{\infty})}{R[\theta - P_{H20} + (4/3)\sigma/R]}$$
[12]

Or, when more than one bubble is present, we can write Equation [12] in this form for bubble i:

$$dR_{i}/dt = \frac{-DKR_{G}T(\theta - F_{H20} + 2\sigma/R_{i} - P^{\infty})}{R_{i}[\theta - P_{H20} + (4/3)\sigma/R_{i}]}$$
[13]

Equation [12] or [13] is easily solved analytically for the special case of constant P^{∞} , that is, an infinitely large system in which the bubbles have no effect on the bulk concentration of dissolved gas. For the *finite* closed system, a mass balance shows that

$$dC^{\infty}/dt = K dP^{\infty}/dt = -(1/V_1) \Sigma dn_i/dt$$
[14]

for i = 1 to N bubbles, where V_L = the volume of the condensed phase, in cm³. Then for each bubble i, Equation [9] can be substituted into Equation [14] to yield

$$-K dP^{\infty}/dt = 4\pi / (V_L R_G T) \Sigma ([(P - P_{H2C}) R_i^2 + 4/3 R_i \sigma] dR_i/dt) [15]$$

This is integrated to yield

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$$P^{\infty} = P_0^{\infty} - 4\pi / (3KV_LR_GT) \left[(\varrho - P_{H2O})(\Sigma R_i^3 - \Sigma R_{0,i}^3) + 2\sigma (\Sigma R_i^2 - \Sigma R_{0,i}^2) \right] [16]$$

where P_0^{∞} = initial partial pressure of dissolved gas in the condensed phase, atm. All summations are from i = 1 to N, where N is the number of bubbles.
Therefore, Equations [13] and [16] define this system; Equation [13] must be solved for each bubble in turn, simultaneously with Equation [16]. We did this using a 4thorder Runge-Kutta numerical routine.

B. Simulation results

Understanding the simulation results is easier if one keeps in mind the definition of 'critical radius'. This is the radius of a bubble that would be in both mechanical and thermodynamic equilibrium with the condensed phase, so that there would be no mass flux at its surface and its size would not change with time. To derive an expression for R_{crit} , remember that the driving force for mass transport is $(P^{hub} - P^{\infty})$, or

driving force =
$$(P + 2\sigma/R - P_{H2O} - P^{\infty})$$
 [17]

A quasi-stable bubble thus can be defined mathematically as one for which the right side of Equation [17] is near zero; that is, $P^{bub} = P^{\infty}$. R equals the critical radius when the driving force is zero, so we can solve Equation [12] for the critical radius:

$$\mathbf{R}_{\rm crit} = \frac{2\sigma}{(\mathbf{P}^{\infty} + \mathbf{P}_{\rm H2O} - \mathbf{\rho})$$
 [18]

When $R > R_{crit}$ the bubble grows and when $R < R_{crit}$ it shrinks. In an unbounded system where P^{∞} = constant the growth or shrinkage is monotonic. In a finite system in which P^{∞} is a time-dependent variable, a bubble may alternately grow and shrink as P^{∞} fluctuates and R_{crit} fluctuates with it. To further understand the simulation results, it should be noted that two bubbles of different sizes cannot simultaneously be equilibrated with the same condensed phase because their internal pressures differ, and that a larger bubble must always be either growing faster or shrinking slower than a smaller bubble. These observations lead to the conclusion that any closed system must ultimately reach one of two possible final states:

1) all of the bubbles have collapsed, or

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2) only one bubble remains, and it is the one that was largest initially.

So, we see that bubbles initially grow or shrink depending upon whether their radii are greater than or less than the initial critical radius of the system. Each bubble later grows or shrinks depending upon the current value of R_{crit} , which depends on the history of bubble size changes in the system. Ultimately, all of the bubbles collapse or else only one bubble remains.

Unless specially noted, the example simulations to be discussed were computed at the following conditions:

ambient pressure $\theta = 1$ ATA; temperature T = 293.16 °K (20 °C); surface tension $\sigma = 72.75$ dyn/cm (its value at 20 °C for the air/H₂O system); vapor pressure of water P_{H2O} = 0.02307 atm (its value at 20 °C); volume of the condensed phase V_L = 0.015 cm³; diffusivity = $3 \cdot 10^{-5}$ cm/sec, which is its approximate value for nitrogen in H₂O at 20°C⁷; partition coefficient K = $6.34 \cdot 10^{-7}$ mol/(cm³-atm), which is its approximate value

for nitrogen in H₂O at 20 $^{\circ}C^{8}$.

The system volume V_L also will be seen to be critical to this analysis. Its value of 0.015 cm³ was chosen because this is the volume of a membrane of dimensions 1 cm × 1 cm × 150 μ m, which are roughly the expected dimensions of a calibration standard.

Figure 3 shows simulation results for a case in which five relatively small bubbles are posited in a condensed phase originally containing a partial pressure of 1 atmosphere absolute (1 ATA) of dissolved gas. R_{crit} in this system initially is 60 μ m (the critical diameter is 120 μ m). All of the bubbles eventually collapse, the smaller ones disappearing first; the partial pressure of dissolved gas eventually rises to 1.004 ATA but this is not high enough to prevent the largest bubble from collapsing, i.e., to bring $R_{crit} < R$ for the largest bubble.

In the second example, shown in Figure 4, all conditions are the same as in Figure 3 except for the initial sizes of the bubbles. Two of the bubbles initially are larger than the critical diameter of $120 \,\mu$ m. An inspection of the numerical results from which this plot was made shows that the bubble that initially is $180 \,\mu$ m in diameter grows slowly for 23 h and then begins to shrink very slowly as P^{∞} is depleted by the largest bubble, which will continue its slow monotonic growth as it asymptotically approaches equilibrium with the rest of the closed system.

A pseudo-stable state is reached in Figure 4 because two of the bubbles are large enough to significantly influence the amount of dissolved gas. Growth of a sufficiently large bubble always reduces the driving force for diffusion to that bubble by depleting P^{∞} , and shrinkage of a sufficiently large bubble always reduces the driving force for that





bubble by augmenting P^{∞} . Sufficiently small bubbles won't affect P^{∞} enough to stabilize their sizes.

In Figure 5, we see an instance of a substantial initial overpressure in the condensed phase. The initial P^{∞} is 3 ATA, giving a critical diameter of 1.4 μ m. Although it is difficult to see on the plot, the bubbles initially are very different in size, ranging from 5 μ m to 200 μ m diameter. They all grow rapidly at first; the smaller ones begin shrinking as P^{∞} declines. At time = 5.8 h, P^{∞} has been reduced to 1 ATA by the bubble growth. Eventually, only one bubble will remain. But, after about 6 h the bubbles are almost static in size over many hours. This is because the driving force for mass diffusion is small since $\varrho \sim P^{\infty}$ and the surface tension term $2\sigma/R$ is small (see Equation [15]).

It is evident from studying Figures 4 and 5 that bubbles having diameters much greater than 100 μ m remain fairly static in size over several hours when the overpressure is small and the surface tension is that of the air/H₂O system. That is, they are pseudo-stable for our purposes. Bubbles much smaller than 100 μ m cannot be stabilized at a surface tension of 73 dyn/cm.

Figure 6 illustrates a simulation done with the surface tension set at $\sigma = 5$ dyn/cm, which may be possible to achieve using surfactants. The initial value of P^{∞} is 1 ATA, so that a slight 'overpressure' exists only because of the contribution of water vaper. Still, the critical diameter is only 8.6 μ m because of the low surface tension. None of the bubbles is larger than 60 μ m diameter at the start. The results are qualitatively similar to those in Figure 5 in that we eventually obtain a pseudo-stable system after an initial



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period of relatively rapid changes. The stability again occurs because of the small driving force, with $\rho_{m}P^{\infty}$ and $2\sigma/R$ being small. In this hypothetical system we have succeeded in stabilizing bubbles smaller than 200 μ m.

Can bubbles smaller than 20 μ m be stabilized if both the surface tension and the overpressure are *extremely* small? In Figure 7, P[∞] is 0.99 ATA initially, the surface tension is 5 dyn/cm, so the critical diameter is 15 μ m. The bubbles are initially 5, 10, 15, 20, and 30 μ m in diameter. The bubbles that begin life with diameters of 15 μ m or less still are not stabilized: they all collapse within 36 h. The larger bubbles, which grow, will not stabilize until they are large enough to deplete the dissolved gas surrounding them; this does not happen within the first 100 h of the simulation, by which time they both are larger than 90 μ m in diameter. It does not seem possible to maintain stable bubbles smaller than ~100 μ m without an implausibly large concentration of bubbles, although it certainly would be possible in a much smaller system.



VI. NOISE MEASUREMENTS

We attempted to quantify the amount of electronic noise generated by the system's various noise sources. Of primary interest is the amount of noise present when the divide-by-2 circuit is in use, because this is the output from which we hope to deduce bubble sizes by analyzing the 2nd harmonic component of the sound radiated from bubbles. Because the amplitude of harmonic distortion products normally depends on the amplitude of the input signal, the 2nd harmonic noise should increase with the amplitude of the input signal. This is borne out by the data.

A. Approach and methods

In the following discussion, we report the ratio, in decibels (dB), of V^{2h} to V_{max}^{fund} for various input voltage levels, where V^{2h} is the RMS (root mean square) voltage amplitude of the <u>2nd harmonic distortion</u> and V_{max}^{fund} is the <u>maximum possible</u> RMS amplitude voltage of the <u>fundamental component</u> of the output signal. V_{max}^{fund} was measured by reflecting the transmitted signal off of the surface of a lead brick with the divide-by-2 circuit bypassed; lead is an excellent sonic reflector because of the mismatch in mechanical impedance between lead and water, and the observed output signal amplitude therefore is taken to be maximized in this experiment for a given input voltage amplitude.

V^{2h} was measured by reflecting the transmitted signal off of a slab of Wall-Gone rubber sound absorber with the divide-by-2 circuit in use and no bubbles apparent. Using Wall-Gone as the acoustical target is more realistic as a physiological analogue than measuring noise with a hard target in place. Although ideally we might expect the signal in this configuration to be immeasurably small, in fact we observe a substantial 2nd harmonic component generated by 2nd harmonic distortion in the front end components (consisting of the transducers, the divide-by-2 circuit, a power amplifier in line between the signal generator and the transmitting transducer, and a mixer), and by nonlinear vibration of the Wall-Gone rubber. On the other hand, noise levels are considerably lower with Wall-Gone as the target than with a hard target, because less energy is reflected to the receiving transducer from the Wall-Gone than from a hard target.

The scheme for characterizing noise levels using the ratio V^{2h}/V_{max}^{fund} was chosen because the results are relevant to the system's S/N ratio for measurements of gas bubbles. Although the reader probably finds this elevance mysterious now, we will explain it in section VIII, 'Estimating the Signal/Noise Ratio'. Note for now that V^{2h}, <u>not</u> V_{max}^{fund} , is considered the magnitude of noise.

All mea. ements were made under the following conditions:

"range" mode in use sweep time = 0.1 sec span = 4 kHz (therefore, time record length = 0.1 sec) sweep start frequency = 0.2 MHz sweep stor frequency = 5 MHz windowing = flattop signal averaging: 20 time records averaged target distance = 3.25 cm

Recall from the Introduction that, in the range mode, the output signal appears as a spectrum of voltage amplitude versus offset frequency Δf , where Δf is proportional to the distance from the transducer head to the target. In the experiments of this section the output spectrum contained a voltage spike at a frequency $\Delta f \sim 2.1$ kHz, which corresponds to a distance of 3.25 cm in water. The reported voltage was read at the maximum of the peak at 2.1 kHz. Noise at other frequencies was negligible compared with the noise at 2.1 kHz.

B. <u>Results</u>

Table 1 shows the noise level measured over a five-fold range of input voltage levels. Inspection of the rightmost column in the table reveals that the noise level is essentially constant at ~-37 dB relative to the maximum output signal level at input voltages greater than 2 V.

As an incidental (but important) observation, we see from the entries in the third column that the system's frequency response (i.e., output voltage at the fundamental frequency \div input voltage) is nearly linear over the input voltage range of 2.5 to 4 V peak-to-peak from the signal generator, suggesting that this is an advantageous operating range. From additional measurements (not shown) it has been observed that the linear frequency response occurs over the same range of input amplitudes even when Wall-Gone is the acoustical target. The substitution of Wall-Gone for lead attenuates the output signal by 94% consistently, regardless of input amplitude. It is suggested therefore that the appearance of nonlinear frequency response is a much stronger function of V_{in} than of V_{out}.

3325A signal generator	V ^{2h}	V_{\max}^{fund}	V^{2h}/V_{max}^{fund}
1 V peak-to-peak	47.42 µV RMS	0.793 mV RMS	- 31 dB
1.5	90.78	1.523	- 35
2	136.1	2.288	- 36
2.5	181.0	3.0.32	- 36
3	229.6	3.826	- 37
3.5	268.7	4.4 3 \	- 38
4	301.6	4.969	- 37
4.5	332.1	5.398	·· 37
5	357.3	5.781	- 37

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TABLE 1: System Noise

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VII. THEORY OF VIBRATING BUBBLES

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A. Approximate analytic solutions via the perturbation method

The motion of a free, spherical gas bubble in an <u>incompressible</u> condensed phase has been described by solving the equation of motion, i.e., the momentum balance, for the condensed phase. This equation is found to be an ordinary nonlinear differential equation. Since the system is spherically symmetric (given a homogeneous, isotropic medium.) the only spatial dimension of importance is the radial coordinate r. If the equation is written at the outer bubble surface, we obtain^{9,10}

$$\mathbf{R}\mathbf{R}'' + (3/2)(\mathbf{R}')^2 = 1/\rho_1[\mathbf{P}_{in}(t) - 2\sigma/\mathbf{R} - \mathbf{r}_{\mathbf{R}}]$$
[19]

where R = R(t) is the bubble radius at time t, cm;

R' = dR/dt; $R'' = d^{2}R/dt^{2};$ $\rho_{L} = \text{density, } g/\text{cm}^{3};$ $P_{\text{in}}(t) = \text{the pressure at the inner surface of the bubble at time t, atm;}$ $\sigma = \text{surface tension, } dyn/\text{cm};$ $\tau_{R} = \text{radial stress at the outer bubble surface, } dyn/\text{cm}^{2}.$

The term τ_R arises when we apply the boundary condition that radial stresses are continuous across the bubble surface. In section C we show how this stress term is rewritten in terms of strain or rate of strain, depending on what constitutive equation is valid for the condensed phase. For now, let us assume that the bubble resides in a Newtonian fluid. In section C we will show that this leads us to calculate $\tau_R = \rho^{out} + 4\mu R^2/R$, where ρ^{out} is the hydrostatic pressure at the outer surface of the bubble.

Prosperetti^{10,11} found an approximate, analytic solution to Equation [19] for a sinusoidally oscillating ambient pressure, that is for a bubble in an externally applied sound field. The mathematics are quite complicated and we will only summarize some of the major features here. For more details see the Appendix of reference 1. For a reasonably complete discussion of the mathematics one must look to Prosperetti's papers^{10,11}.

Prosperetti replaces $\rho^{out}(t)$ with $\rho_0(1 \cdot e \cos(\Omega t))$, i.e. ρ_0 is the mean ambient pressure, ϵ is the amplitude of sound waves imposed on the bubble, and the frequency of that sound is Ω . The internal pressure $P_{in}(t)$ is represented by a polytropic expression $P_{in} = P_{in,eq} (R_0/R(t))^{3t} - 4\mu_{th}R'/R_0$, where R_0 is the equilibrium radius, κ is the "effective polytropic exponent", $P_{in,eq}$ is the internal pressure corresponding to $R = R_0$, and μ_{th} is a so-called 'thermal viscosity' introduced as an *ad hoc* corrective term to compensate for the polytropic expression's inability to account for phase shifts between pressure and temperature. Prosperetti also defines an 'acoustic viscosity' μ_{ac} that arises from momentum transfer from the bubble to the liquid. The thermal and acoustic viscosities have the same units as a "real" viscosity and each is a "damping" term, meaning that it appears in the momentum balance as a multiplier to the velocity term R'. Accordingly, Prosperetti combines all three viscosities into an "effective viscosity" $\mu_{eff} = + \mu_{th} + \mu_{ac}$. Equation [19] now becomes

 $RR^* + (3/2)(R^{\prime})^2 = \frac{1}{\rho_L} \left[P_{in,eq} \left(\frac{R_0}{R(t)} \right)^3 - \Theta_0 (1 - \epsilon \cos(\Omega t)) - 2\sigma / R - 4\mu_{eff} R^{\prime} / R \right]$ [20]

Expressions for the polytropic exponent, thermal viscosity, and acoustic viscosity all are calculated from a separate analytic solution to the system of six partial differential equations that comprise the <u>linearized</u> equations of continuity, motion, and energy in both phases. The condensed phase is considered compressible in the linearized governing equations, even though the nonlinear Equations [19] and [20] are written for incompressible liquids. (In fact, the acoustic damping term is zero for an incompressible medium.) Linearized equations are valid for small perturbations from equilibrium -- in this case, for small amplitude vibrations -- but keep in mind that no information on harmonics, subharmonics, or phase shifts is contained in a linearized treatment of a vibrating system. The mechanics of solving this system of equations are exceptionally complicated.

Next, the substitution $R(t) = R_0 (1 + x(t))$ is made into equation [20]. The dimensionless variable 'x' is seen to be a fractional perturbation of the bubble radius R(t) from its equilibrium value R_0 . The problem is made tractable by discarding all x, x', and x" terms that are raised to powers of 4 or greater, but note that retaining the 2nd and 3rd power terms retains the essential effect of the nonlinearity (provided x is small).

Finally, algebraic solutions to the resulting equation are obtained by a "perturbation" technique first advanced by Krylov, Bogolyubov, and Mitropolsky¹². Each solution is valid when the forcing frequency Ω is 'near' one of the system's resonance frequencies.

We are particularly interested in the 2nd harmonic component of the solutions, which is found by retaining only the terms that are of frequency 2Ω , since that component will be measured by the bubble detector. It turns out that the mathematical system (and presumably the physical system likewise, if its mathematical description is accurate) is 'catastrophic': as the forcing frequency is swept through the various resonance frequencies there are discontinuous jumps between stable solutions, and there is hysteresis behavior that causes the location of these jumps to depend on whether the forcing frequency is being swept upward or downward.

The procedure summarized above yields an algebraic expression for the amplitude of the oscillations of R as a function of forcing frequency and all other relevant parameters. This is readily converted to the amplitude of the radiated pressure wave corresponding to it, denoted $\|P_{rad}\|$, by solving the linearized 'wave equation' in the liquid (in fluid mechanics a wave equation is simply the equation of motion written for a compressible medium in which a wave is being propagated). If desired, only the 2nd harmonic component of the radial oscillations can be included, and we designate the pressure amplitude of that component as $\|P_{rad}^{2h}\|$.

The fact that the values of the parameters κ ' and ' μ ' (used below) are estimated using first order expansions (linearizations) of the terms in the mass, energy, and momentum balances means that they are valid only for a linear system. Their usage when analyzing this nonlinear system is an *ad hoc* approach necessitated by the difficulty of the mathematics.

Clearly, the analytic solution incorporates several questionable assumptions and

computational simplifications. Its value is that it can be computed rapidly enough to make it useful in the iterative data-fitting routine mentioned in the Introduction to this report, with which the equilibrium bubble radius R_0 will be estimated for an unknown bubble by comparing observed resonance frequencies with the predicted values.

B. Numerical solutions via the Galerkin Spectral Method

Given our reservations about the reliability of the analytic solution discussed in section A, we would like to have a means of numerically solving the equations governing a vibrating bubble without resorting to so many simplifying assumptions. This new solution could be used to evaluate the accuracy of the analytic solution in the absence of direct experimental verification, which is unlikely to appear any time soon. We are willing to trade computational economy for accuracy with the numerical solution.

Kamath and Prosperetti¹³ used a Galerkin spectral method to solve the governing equations and found significant deviations of the analytic solution from the numerical results when the driving amplitude was high enough. As will be discussed shortly, the mathematical description that Prosperetti evaluated using the Galerkin method is in some ways more sophisticated, in other ways more simplified than the description he evaluated earlier using a perturbation technique. This confuses a comparison of the results from the two solutions. The reader should look to reference 14 for an overview of Galerkin techniques. Here, we will review the particulars of how Prosperetti (and we) used the Galerkin spectral method on our system.

The Galerkin method is used to reduce the partial differential equations to a system of ordinary differential equations, which subsequently are solved using the Gear method.

The result consists of the value of R, the bubble radius, as a function of time at some forcing frequency Ω . This time domain information can be converted to an amplitude spectrum via Fourier transformation. To get the <u>steady state</u> solution one integrates until steady state oscillations are attained, then Fourier transforms the time domain data from only the last oscillation cycle. If one is interested in the amplitude of only the 2nd harmonic component as a function of Ω , then the amplitude at frequency 2Ω is extracted from the spectrum. Once the steady state radial amplitude at frequency 2Ω has been computed over a range of Ω 's, we can construct the spectrum of amplitude versus Ω . Also, the amplitude of R at frequency 2Ω can be converted to $\|P_{rad}^{-2h}\|$ by solving the aforementioned linearized wave equation in the condensed phase. In sections D and E, we will present results in an alternative form that does not involve Fourier transformation: we show the maximum bubble radius attained during a steady state oscillation.

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In Prosperetti, Crum, and Commander,¹⁵ simplified governing equations are derived from the conservation equations for mass, momentum, and energy for both the gas in the buoble and the liquid outside the bubble, along with boundary conditions at the gasliquid interface (i.e., the bubble wall). Based on several reasonable assumptions, and several order of magnitude comparisons that show certain quantities to be negligible, the authors are able to reduce the original system of six partial differential equations (i.e., the conservation equations) to one partial differential equation and two ordinary differential equations.

Two basic assumptions are that the gas is perfect and the bubble maintains a

spherical shape. An order of magnitude argument shows that, near the main resonance frequency of a bubble in forced oscillation, the Mach number M_B of the bubble wall, referred to the speed of sound in the gas, is extremely small; i.e. $M_B = \dot{R}/c_G$ is close to zero. Using this approximation it can be shown¹³ that the radial gradient in pressure inside the bubble is negligible compared with the temporal variation of pressure; i.e., the pressure is almost uniform spatially within the bubble. An estimate of viscous shear in the gas shows it to be negligible. Based on these results it can be shown that the momentum balance equation for the gas reduces to the simple statement that gas pressure is a function only of time.

Some further assumptions, which involve the bubble wall temperature and vapor effects, are less important, because the system equations would still be tractable without them. An order of magnitude estimate shows that, owing to the greater thermal inertia of liquid than gas, the temperature at the bubble surface is almost unperturbed from the ambient temperature provided there is not too much heat being alternately consumed and released by the evaporation and condensation of vapor. The authors ensure the validity of this approximation in their mathematical construct by neglecting vapor altogether. In the physical world, they suggest (based on their order of magnitude estimates) that the approximation is valid for bubbles in H₂O at temperatures up to about 50 °C. In other words, the liquid must be sufficiently cool. With the use of this approximation the equation of energy in the liquid phase can be dispensed with; otherwise, it would be needed for determining the boundary condition on the energy equation in the gas phase.

In addition, both slow and fast diffusion of the gas in and out of the bubble are known to have negligible dynamical effects. Thus, diffusion is ignored entirely and we assume the bubble boundary is impervious to the gas. Fast diffusion refers to diffusion with time scale the order of one period of the oscillation; slow diffusion (often called rectified diffusion) refers to diffusion with a time scale of, for example, thousands of periods in which the total gas contents and/or the equilibrium radius of the bubble may change.

Under the stated assumptions, the system of equations to be solved becomes:

a) Radial dynamics equation:

We use Keller's equation for a gas bubble in a compressible liquid.

$$(1 - \dot{R}/c) R\ddot{R} + 3/2(1 - \dot{R}/(3c)) \dot{R}^{2} =$$

$$1/\rho_{L}(1 + \dot{R}/c + (R/c) d/dt)p_{B} - 1/\rho_{L}(1 + \dot{R}/c) p_{A}(t + R/c)$$
[21]

where R = R(t) is the bubble radius at time t, ρ_L is the density of the liquid, 'c' is the speed of sound in the liquid, p_B is the pressure in the liquid just outside the bubble, and $p_A(t)$ is the ambient pressure (in radial equation P_A is evaluated at time = t + R/c). Keller's equation is valid when the Mach number of the bubble wall is sufficiently small so that quantities proportional to its square may be neglected. We assume $p_A(t) = p_{\infty} (1 - \epsilon \cdot \sin(\omega t))$. A balance of the normal stresses across the bubble surface yields:

$$p_{R} = p_{R}(t) = p - 2\sigma/R - 4\mu_{L}(\dot{R}/R)$$
[22]

where μ_L = liquid viscosity.

b) Pressure equation:

This equation relates the internal pressure to the temperature gradient. Since the internal pressure p is assumed to be uniform throughout the bubble; p is independent of r; it depends only on 't'.

$$\vec{p} = 3/R(((\gamma - 1)K \cdot (\partial T/\partial r))_R - \gamma p R)$$
[23]

c) Temperature equation:

This is also called the energy equation.

$$\gamma p/((\gamma - 1) T) \left[\frac{\partial T}{\partial t} + \frac{1}{(\gamma p)} ((\gamma - 1) K \frac{\partial T}{\partial r} - \frac{1}{3} r \dot{p}) \frac{\partial T}{\partial r} \right] - \dot{p} = \nabla \cdot (K \nabla T)$$
[24]

where K(T) is the thermal conductivity of air. Based on data for 200 °K < T < 3000 °K, Kamath and Prosperetti suggest using the linear function K(T) = 5.528 T + 1165.

Boundary conditions for system:

The temperature on the bubble surface equals the constant exterior temperature T_{∞} .

Initial conditions for system:

Bubble is at rest with equilibrium radius R_0 .

Internal pressure has value $p_0 = (2 \sigma / K_0) + p_{\pi}$

Temperature is constant throughout bubble; its value is T_{μ} .

Let us define a scaled radial variable y = r/R(t) to be used instead of r.

A dependent variable τ (y,t) is defined by $\tau = \int_{T_u}^{T} K(\mathbf{e}) d\mathbf{\theta}$ where K(T) is defined above.

The Galerkin method is used to replace spatial partial derivatives (i.e., those involving the variable 'y') with finite linear combinations of Chebyshev polynomials $T_k(y)$. Specifically, we represent $\tau(y,t)$ as an infinite sum of shifted Chebyshev polynomials $\Phi_k(y) = T_{2k}(y) - 1$. Let the coefficients be denoted $a_k(t)$. Denote by τ_N the series truncated after N terms; $\tau_N = \sum_{k=1}^N a_k(t) \Phi_k(y)$

The pressure and temperature equations involve spatial derivatives. Using the expression for τ_N we can convert these spatial derivatives into finite linear combinations $\sum_{k=1}^{N} e_k(t) T_k(y) \quad \text{where the } e_k(t) \text{ are functions of the } a_k(t).$

With these techniques, the temperature equation is reduced to a system of ordinary differential equations which can be integrated in time. Following Kamath and Prosperetti's approach we used a four-term Chebyshev expansion. The system must be integrated for many (usually more than 10) cycles before the system reaches steady-state oscillations. For certain parameter values there may be more than one stable solution; if

so, the solution that arises in any given problem will depend on the initial conditions used for that problem. In other words, the bistability/hysteresis effect, well established for the analytic solution with resonance frequencies (see the preceding section), appears as well in the numerical solution.

C. Derivation of the normal stress at the surface of a spherical cavity

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The boundary condition on the equation of motion in the medium surrounding a bubble (Equation [19]) is different for a liquid than for a solid because different constitutive equations govern the mechanical behavior of the two types of media.

The continuity equation for an incompressible substance with spherical symmetry can be written either

$$(1/r^2) \partial(r^2 v_r) / \partial r = 0$$
 [25a]

$$(1/r^2) \partial(r^2 u_r) / \partial r = 0$$
 [25b]

where v_r = radial velocity and u_r = radial displacement. Velocity is simply the time derivative of displacement: $v_r = \partial u_r / \partial t$. Integration yields

$$v_r = A_1(t)/r \qquad [26a]$$

or
$$u_r = A_2(t)/r$$
 [26b]

where A $_1(t)$ and A $_2(t)$ are integration factors to be evaluated later. The boundary condition on the continuity equation is continuity of either velocity or displacement at

the bubble surface:

or

$$\mathbf{v}_{\mathbf{r}|\mathbf{r}=\mathbf{R}} = \mathbf{d}\mathbf{R}/\mathbf{d}\mathbf{t} = \mathbf{R}^{\prime}$$
 [27a]

$$\mathbf{u}_{\mathbf{r}}|_{\mathbf{r}=\mathbf{R}} = \mathbf{R} - \mathbf{R}_{\mathbf{E}}$$
 [27b]

where R_E = bubble radius at which the medium surrounding the bubble is undeformed, which in general is <u>not</u> the same as the equilibrium radius R_0 . It follows from Equations [26] and [27] that

$$v_r = R^2 R^2 / r^2$$
 [28a]

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$$u_r = R^2 (R \cdot R_F) / r^2$$
 [28b]

The boundary condition on the equation of motion is continuity of the radial stresses across the phase interface:

$$-\mathbf{P}_{\rm in} + 2\sigma/\mathbf{R} = \mathbf{\tau}_{\rm R}$$
 [29]

where τ_R is the radial stress at r = R.

We are obeying the following incomprehensible arbitrary convention on signs of stress components, taken almost verbatim from reference 9:

The stress τ_{ij} , due to action by material on the positive side of the surface on the material on the negative side, is positive if the line of action is along positive spatial coordinate x_{ij} .

Conversely, the stress exerted from the negative side of the surface on the material on the positive side is positive if the line of action is along negative x_1 .

Now we will apply the constitutive equations. For a Newtonian liquid, the stress tensor components are linearly related to the components of the rate of strain tensor:

$$\boldsymbol{\tau}_{ij} = -\mathbf{P}\boldsymbol{\delta}_{ij} + \boldsymbol{\Delta}_{ij} \qquad [30]$$

where P = hydrostatic pressure, atm;

1

 $\boldsymbol{\delta}_{ij}$ = Kronecker delta, defined thus:

 $\delta_{ij} = 1$ when i=j, and $\delta_{ij} = 0$ when $i\neq j$;

 μ = viscosity, dyn/cm;

 Δ = component of the rate of strain tensor.

The components of the *linearized* rate of strain tensor are linear functions of velocity vector gradients. For satisfying the boundary condition with spherical symmetry we need only know the radial normal stress τ_{rr} . It is found from the radial normal component of the rate of strain, which in spherical coordinates is given by

$$\Delta_{\rm rr} = 2 \,\partial v_{\rm r} / \partial r \qquad [31]$$

And so the boundary condition equation [29] is solved by $\tau_R = \tau_{rr}|_{r=R}$, which is readily evaluated; the boundary condition for a Newtonian liquid becomes

$$P_{out} + 2\sigma/R = P_{in} - 4\mu R'/R \qquad [32]$$

For a linearly elastic solid, by definition the stress tensor components are linearly related to the components of the strain tensor¹⁶:

$$\tau_{ii} = \lambda (\epsilon_{11} + \epsilon_{22} + \epsilon_{33}) \delta_{ii} + 2\mu \epsilon_{ii} \qquad [33]$$

where λ and μ are the Lamé constants;

ł

 ϵ = small strain tensor component;

 $\boldsymbol{\varepsilon}_{11} \boldsymbol{\varepsilon}_{22}$, and $\boldsymbol{\varepsilon}_{33}$ are the normal strain components.

(By longstanding convention, the second Lamé constant unfortunately is denoted by the same Greek letter as is the viscosity of a liquid.) Equation [33] does not appear at first to contain the hydrostatic pressure, but we can make the substitution¹⁶

$$P = -B(\epsilon_{11} + \epsilon_{22} + \epsilon_{33})$$

= -(\lambda + 2)(\epsilon_{11} + \epsilon_{22} + \epsilon_{33}) [34]

where $B = bulk modulus, dyn/cm^2$. Equation [33] now becomes

$$\tau_{ij} = [-P - (2\mu/3)(e_{11} + e_{22} + e_{33})]\delta_{ij} + 2\mu e_{ij}$$
[35]

The continuity equation tells us that in an *incompressible* system the sum of the normal strain components $(e_{11}+e_{22}+e_{33})$ is zero, so we can simplify the constitutive relation to

$$r_{ij} = -P\delta_{ij} + 2\mu e_{ij}$$
 [36]

In *linearized* elastic theory the strain tensor components are linear functions of displacement vector gradients. For this spherically symmetric system we need to obtain the radial normal stress from the radial normal strain, which in spherical coordinates is given by

$$\mathbf{e}_{rr} = \partial \mathbf{u}_r / \partial \mathbf{r}$$
 [37]

And so the boundary condition again is solved by $\tau_R = \tau_{rr}|_{r=R}$. This radial normal stress component is given by

$$\tau_{\rm rr}|_{\rm r=R} = -P - 4\mu (R - R_{\rm E})/R$$
 [38]

at the bubble surface. Finally, let us replace the Lamé constant with the more familiar Young's modulus E. For an incompressible solid $\mu = E/3$. Our final expression for the linearized elastic boundary condition is therefore

$$P_{out} + 2\sigma/R = P_{in} - (4E/3)(R-R_E)/R$$
 [39]

Linearized elastic theory is valid for small deformations. At larger strains we require the nonlinear theory, in which expressions for the strain components are calculated from gradients in the displacement vector without discarding terms of order 2 and higher. The mathematics involved in computing our boundary condition for this kind of system are well beyond the scope of this report. Fortunately, the result has been published¹⁷:

$$\tau_{\rm rr}|_{\rm r=R} = -P - (1/6)E \left[5 - 4(R_{\rm E}/R) - (R_{\rm E}/R)^4\right]$$
[40]

The boundary condition on the equation of motion for large elastic deformations is given by

$$P_{out} + 2\sigma/R = P_{in} - (1/6)E [5 - 4(R_E/R) - (R_E/R)^4$$
 [41]

This boundary condition approaches the one for a linear elastic solid (equation [39]) in the limit as $R \rightarrow R_E$.

So, the appropriate boundary condition is substituted into the equation of motion (Equation [19]) and that equation is solved either analytically or numerically to yield a description of an oscillating gas bubble. To obtain the analytic solution it is necessary to assume linear elasticity when modelling oscillations in a solid, so Equation [39] must be used to calculate the elastic stress on the bubble wall arising from oscillations of the radius about its static value R_0 . However, the nonlinear Equation [40] is used to compute the elastic stress imposed on the wall of the static bubble, i.e. the stress arising from the difference between R_0 and R_E . Thus, in the analytic solution we have a linear oscillatory stress superimposed on a nonlinear static stress. When using the Galerkin method the nonlinear Equation [40] is used for all calculations of elastic stress.

There is one potential complication when figuring the boundary condition for a vibrating bubble in an elastic solid. The following relations are true for the strain and elastic stress in the solid surrounding the bubble:

for
$$R > R_E \epsilon_{rr} < 0$$
 and $\tau_{rr} < 0$, [42a]
for $R \le R_E \epsilon_{rr} = 0$ and $\tau_{rr} = 0$, [42b]

where $R_E =$ bubble radius at which the medium surrounding the bubble is undeformed. (The strain and stress are negative when $R > R_E$ because of our arbitrary sign convention.) Equation [42] says that the bubble pushes against the solid when $R > R_E$, but doesn't pull on it when $R < R_E$; that is, the solid does not adhere to the bubble wall. Consequently, the boundary condition is discontinuous at $R = R_E$. If a bubble is made to oscillate in size such that its radius is greater than R_E during expansions and less than R_E during contractions, then its boundary condition is discontinuous in time. Describing such a system mathematically would present formidable challenges. We therefore limit ourselves to analyzing systems for which R is never less than R_E during vibration. Experimentally, if a bubble is formed by cavitation in a solid then $R_E = 0$ and the discontinuous boundary condition can never exist. If, on the other hand, the solid phase is formed by solidifying a liquid around a gas bubble that is at its equilibrium radius R_0 then we expect that $R_E = R_0$, and if the bubble radius is made to oscillate about R_0 (in response to sound waves, for instance) then the boundary condition is discontinuous in time.

D. Results: Bubbles in a viscous liquid

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and

Using FORTRAN programs that implement the models discussed above, we have generated the graphs shown below. In all these graphs, we show the maximum bubble radius attained during an oscillation after the system is in a steady state mode. The maximum value is given as a function of the driving frequency; the latter is expressed as a ratio of driving frequency to natural frequency of the bubble.

The expression 'Galerkin Method' in the graph headings refers to the program that implements the Keller equation (see above) for bubble oscillations. In this program the differential equation modeling heat flow across the bubble wall is solved numerically using the Galerkin spectral method. The expression 'Perturbation Method' refers to the program which implements Rayleigh's equation (with the addition of thermal and acoustic regarding damping terms as discussed above, and a natural frequency ω_0 for the bubble which depends on the driving frequency ω). The graphs are based on approximate analytic solutions proposed by Prosperetti¹⁰. These two methods are used for the case of a bubble in water driven by a sound wave with a small amplitude (0.3)atm). For the associated graphs, see Figures 8 and 9. Figures 10 and 11 are graphs for the case of a bubble in water driven by a sound wave with a larger amplitude (0.6 atm). For this larger amplitude, which we use as well for the last four figures, we use another program based on Rayleigh's equation without the enhancements described above. The program, which we refer to as the 'Simple Model', solves the differential equation using a very accurate numerical method. Use of a numerical solution makes unnecessary certain analytic approximations required in the perturbation approach. The greater numerical accuracy achieved allows the simple model to handle large driving amplitudes which lead to numerical instabilities using the perturbation theory approach.








E. Results: Bubbles in an elastic solid

The last four figures apply to the case of an elastic solid with a shear modulus of $8 \cdot 10^5$ dyne/cm². This is a low value for the shear modulus and indicates a soft elastic solid. For example, this shear modulus would be typical of a fairly high-concentration polyacrylamide gel.¹⁸ Figure 12 (Galerkin Method) and Figure 13 (Simple Model) describe the case of a bubble for which $R_0 = R_{\pi}$ (recall that the latter is the radius at which there is no strain in the solid). This means that, at mechanical equilibrium, the solid is unstrained and the bubble wall is not subject to elastic stress. We use a common value of 10 μ m, because bubbles of this size are of interest. For Figure 14 (Galerkin Method) and Figure 15 (Simple Model), we consider the case of a bubble for which $R_0 > R_E$. We allow for large deformations; the nonlinear stress-strain relation is described by Equation 40. Here, $R_0 = 10 \,\mu$ m, $R_E = 5 \,\mu$ m.

In general, there are two stable solutions to both Rayleigh's and Keller's equation for values of the frequency ratio that lie in the resonance bands. The perturbation program will always find both these solutions since it has analytic expressions for them. The situation for the Galerkin program and the simple model program is more involved. The stable solution that is numerically calculated in these programs depends on the initial conditions; in general, starting with the bubble at rest and with radius R_0 leads to the solution with the smaller amplitude. Finding initial conditions that lead to another stable solution involves some numerical experimentation. For these differential equations only at most two stable solutions have been found to exist in any resonance band; however it is possible others exist. For the case described in Figure 13 we were

able to find such initial conditions (initial radius = $2 \cdot R_0$ cm, and initial velocity = R_0 cm/sec); therefc e we display both solutions. As the system is stiffened, either by increasing the shear modulus or by decreasing R_E , the two solutions may coalesce into a single one. One has to consider this possibility when one is unable to find more than one stable solution.





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VIII. ESTIMATING THE SIGNAL/NOISE RATIO

We can use the models presented in section VII to estimate the ratio of [the sound pressure amplitude at the 2nd harmonic frequency radiated by a spherical bubble to the receiving transducer] to [the sound pressure amplitude at the fundamental frequency radiated by the transmitting transducer]. This tells us the "line loss" attendant with measuring a bubble. For instance, if P_{out} is one-tweatieth of P_{in} then the line loss is 95% or 13 dB. If we assume that the bubble detector's overall frequency response is linear (that is, V_{out} is a linear function of V_{in}) then for this example V_{out} would be 13 dB below its maximum attainable value.

In section VI, 'Noise Measurements', we reported a relative noise level equal to the ratio of [the 2nd harmonic noise level] to [the maximum attainable level of the fundamental of the output signal]. Therefore, by inspection, we can estimate the S/N ratio of the system by dividing the line loss associated with a given bubble by the relative noise level as reported in section VI. In this section we discuss the estimated S/N ratio for single spherical bubbles of various sizes in water.

The line loss estimates were made using the analytic solution to the governing equations. The line loss is predicted to be only a weak function of the amplitude of the driving signal within the range of 0 to 0.5 atm sound pressure amplitude. The analytic solution is valid only at small amplitudes (i.e., small driving pressures), and the model yielded nonsensical results when it was extended to higher transmitted pressures,

precluding meaningful comment at this time about what happens with these stronger driving signals.

For a bubble in water the line loss is estimated to be ~ 31 dB for a 6 μ m-diameter bubble and ~ 34.5 dB for a 0.9 μ m-diameter bubble at transmitted sound pressure amplitudes of up to 0.5 atm.

Combining the predicted line loss with the noise measurements of section VI, we estimate the S/N ratio. At a setting of 3 V P-P on the 3325A signal generator the S/N ratio is estimated to be 6 dB for a 6 μ m-diameter bubble and only -2.5 dB for a 0.9 μ m-diameter bubble. This is uncomfortably low. There is no further improvement in the S/N ratio to be gained by signal averaging, because extensive signal averaging has been used already when obtaining the noise measurements. However, it is obvious from the sample data from section III that the noise level can be reduced by at least an order of magnitude by subtracting a judiciously chosen background measurement from the signal, which gives hope that the system may be sensitive enough to detect individual bubbles.

If the S/N ratio proves unacceptably low in practice, then for a remedy we may consider that the simulation results show that the signal level from a bubble is roughly proportional to the bubble diameter. Therefore, the S/N ratio could be increased, without replacing the existing electronic components with more linear components, by investigating larger bubbles. This approach would require that we replace the existing transducers with a pair designed for a lower frequency range, which would encompass the resonance frequencies of larger bubbles.

IX. CONCLUSIONS

The bubble detector has been redesigned and provided with appropriate software. It now has the potential to be of use.

Simulations of bubble oscillations have yielded important insights. These simulations, combined with measurements of the system noise, suggest that it may be difficult to detect a small ($\leq 6 \mu$ m diameter) bubble whose main resonance frequency is within the range over which the transducers are sensitive. A separate simulation of bubble size dynamics suggests that such small bubbles would be difficult to stabilize for the purpose of calibration. We also have learned via simulation that the signal strength increases linearly with bubble diameter and that bubble stability improves with size. Obviously, it may be advantageous to replace the present transducers with a pair that functions over a frequency range that encompasses the resonance frequencies of larger bubbles, and we are investigating that possibility. In the meantime, experiments will be undertaken to determine whether the existing system is capable of *ex vivo* detection of gas bubbles in dog spinal cords during and after decompression.

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APPENDIX

HP Basic Program to Control HP 3325A Signal Generator

and HP 3561A Signal Analyzer

APPENDIX: HP Basic Program to Control HP 3325A Signal Generator

and HP 3561A Signal Analyzer

! THIS PROGRAM LISTS THE INITIAL SETTINGS FOR THE 3325A SIGNAL 10 ! GENERATOR, THE HP3561A SIGNAL ANALYZER, AND THEN OFFERS THE 20 30 ! OPPORTUNITY TO CHANGE SOME OF THESE DEFAULT SETTINGS. IT ALSO ! TRIGGERS THE EXPERIMENT, EXTRACTS THE DATA FROM THE TIME BUFFER IN 40 ! THE 3561A, CONVERTS THE DATA TO AN AMPLITUDE-VERSUS-TIME SPECTRUM 50 ! (WHICH, BECAUSE OF THE NATURE OF THE EXPERIMENT IS ALSO AN 60 ! AMPLITUDE-VERSUS-FORCING FREQUENCY SPECTRUM), AVERAGES IT OVER A 76 **! USER-SELECTABLE NUMBER OF REPEAT MEASUREMENTS, SUBTRACTS THE** 80 90 ! "BACKGROUND" (OR BASELINE) MEASUREMENT, STORES THE DATA 100 ! FOR LATER USE, AND PLOTS IT TO BOTH THE SCREEN AND A PRINTER. 110 ! 120 OPTION BASE 1 **! MINIMUM NUMBER OF ELEMENTS IN AN ARRAY IS 1** 130 PRINTER IS CRT **! PRINTS TO SCREEN** 140 RANDOMIZE ! CHANGE SEED OF RANDOM NUMBER GENERATOR 150 ! ! THIS ARRAY TO BE USED TO FILL THE BUFFER 160 INTEGER Zero(514) 170 MAT Zcro = (0)! AT I/O PATH '@Tag' WITH ZEROES ! IN BETWEEN TRACE DUMPS FROM THE SIG ANALYZER. 180 190 ! 200 INTEGER Tag field(350), Range, Rec size 210 INTEGER Raw data(30,1024) BUFFER 220 INTEGER Raw raw data(1024) BUFFER **! FOR READING TRACE FROM BUFFER** 230 INTEGEk Raw trace(401) 240 INTEGER N, Limit, Sweeps, Sweep back, Ii, 18 250 REAL Amplitude(512), Backgrnd(512), Negarea, Posarea 260 REAL Trace data(401) ! FOR CONVERTING BINARY TRACE DATA TO VOLTAGES 270 DIM Name\$[15],File\$[30] ! FOR NAMING THE OUTPUT FILES 280 ! 290 ASSIGN @Anz TO 711 **! OPEN THE I/O PATHS** 300 ASSIGN @Siggen TO 717 310 ASSIGN @Header TO BUFFER [350];FORMAT OFF 320 ASSIGN @Time buff TO BUFFER Raw raw data(*);FORMAT OFF 330 ASSIGN @Tag TC BUFFER [1028];FORMAT OFF 340 1 350 GOSUB Set defaults 360 GOSUB Display default 370 GOSUB Change default 380 GOSUB Init siggen 390 GOSUB Init anz 400 ! 410 ! 420 BEEP (INT(RND*5127)+81),1 430 GOSUB How_many 440 GOSUB Index 450 ! 460 Name\$="\HPBLP\DATA\" 470 File\$ = Namc\$&"STRT"&VAL\$(Istart)&".BCK" 480 BEEP (INT(RND*5127)+81),1

490 ! 500 ! MEASURING BACKGROUND 510 ! 520 INPUT "HIT 'ENTER' TO MAKE A BACKGROUND MEASUREMENT ", Dummy\$ 530 PRINT "" 540 PRINT "NOW COLLECTING THE BACKGROUND MEASUREMENT" 550 PRINT " ! INDEX N = 0 IF MAKING BACKGROUND MEASUREMENT. 560 N = 0! N = 1 IF COLLECTING REGULAR DATA 570 580 OUTPUT @Anz;"NAVG";Sweep back **! TRACE DATA ARE TIME AVERAGED OVER** 590 ! "Sweep back" NUMBER OF SWEEPS 1 3561A SELF-CALIBRATION 600 OUTPUT @Anz;"SCAL" 610 WAIT 3 ! WAIT FOR 3561A SELF-CAL 620 OUTPUT @Anz;"STRT" **! START TIME AVERAGE** 630 FOR li=1 TO Sweep back 640 GOSUB Trigger system 650 GOSUB Read data 660 WAIT Sweep_time **! WAIT FOR SIG GEN TO CYCLE BACK** 670 NEXT Ii 680 GOSUB Convert and sum 690 MAT Backgrnd = Amplitude 700 GOSUB Store data 710 GOSUB Integrate 720 GOSUB Plot data 730 DUMP GRAPHICS **! PIXEL-BY-PIXEL DUMP OF SCREEN TO EXTERNAL PRINTER** 740 ! 750 CONTROL @Tag.3;1 **! MAKE SURE BUFFER POINT WRITER IS ON 1ST BYTE** 760 OUTPUT @Tag;Zero(*) ! FILL BUFFER WITH 514 INTEGER ZEROES 770 ! 780 GOSUB Read_trace **! DUMP TRACE FROM SIG ANALYZER TO BUFFER** 790 GOSUB Scale trace 800 GOSUB Plot trace 810 DUMP GRAPHICS **! PRINTING TRACE BY DUMPING SCREEN TO PRINTER** 820 ! 830 ! COLLECTING DATA 840 ! 850 N = 1! INDEX N = 0 IF MAKING BACKGROUND MEASUREMENT, 860 ! N = 1 IF COLLECTING REGULAR DATA 870 OUTPUT @Anz;"NAVG";Sweeps / TRACE IS TIME-AVERAGED OVER "Sweeps" 880 **! NUMBER OF SWEEPS** 890 BEEP (INT(RND*5127)+81),1 900 ! 910 PRINT " 920 INPUT "HIT 'ENTER' TO START DATA COLLECTION", DummyS 930 OUTPUT @Anz; STRT ! START TIME AVERAGE 940 FOR I8=Istart TO (1000+Istart) ! CAN DO UP TO 1000 COLLECTION CYCLES 950 File\$ = Name\$&"AMP"&VAL\$(18)&".DAT" 960 PRINT " 970 PRINT " 980 BEEP (INT(RND*5127)+81,1)99() PRINT "NOW ON COLLECTION CYCLE NUMBER ";18 1000 PRINT " 1010 PRINT ** OUTPUT @Anz;"SCAL" ! SIG AN CALIBRATES ITSELF 1020

1030 WAIT 3 ! WAIT FOR 3561A SELF-CAL 1040 OUTPUT @Anz;"STRT" **! START TIME AVERAGE** 1050 FOR Ii=1 TO Sweep 1060 GOSUB Trigger system 1070 GOSUB Read datay 1080 WAIT Sweep time ! WAIT FOR SIG GEN TO CYCLE BACK TO "START" 1090 NEXT Ii GOSUB Convert_and_sum 1100 1110 ŧ. 1120 MAT Amplitude = Amplitude Backgrnd ! SUBTRACTING THE "BACKGROUND"" 1130 **! MEASUREMENT BEFORE PROCEEDING** 1140 **GOSUB** Store data BEEP (INT(RND*5127)+81),1 1150 1160 1 1170 **GOSUB** Integrate 1180 **GOSUB** Plot data 1190 DUMP GRAPHICS 1200 ! 1210 CONTROL @Tag,3;1 1220 OUTPUT @Tag;Zero(*) 1230 ! 1240 GOSUB Read trace 1250 GOSUB Scale trace 1260 **GOSUB** Plot trace DUMP GRAPHICS **127**0 1280 1 1290 PRINT "CYCLE COMPLETE; PAUSING BEFORE NEXT CYCLE" 1300 PRINT " 1310 PRINT " 1320 PRINT " 1330 WAIT Waittime 1340 NEXT I8 1350 ! ! CLOSE THE I/O PATHS 1360 ASSIGN @Path TO * 1370 ASSIGN @Header TO * 1380 ASSIGN @Time buff TO * 1390 ASSIGN @Tag TO * 1400 ! 1410 STOP 1420 ! 1430 Set_defaults: 1 1440 ! SET DEFAULTS FOR PARAMETERS 1450 ! 1460 ! DEFAULTS FOR SIGNAL GENERATOR 1470 ! 1480 Sweep start f=1 ! START SWEEP AT 1 MHz 1490 Strt_sweep_unit\$="MH" ! MEGAHERTZ 1500 ! 1510 Sweep_stop_f=10 ! **STOP SWEEP AT 7** 1520 Stop sweep unit\$="MH" ! MEGAHERTZ 1530 ! 1540 Signal amp=3 ! AMPLITUDE IS 3 1550 Sig_amp_unit\$="VO" ! VOLTS 1560 !

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1570 !
         SET DEFAULTS FOR ANALYZER
1580 !
1590 Start freq anz=1 !
                     START OF FREQUENCY SPAN IS AT 0.8
1600 Strt f anz_unit$="KHZ" ! KILOHERTZ
1610 !
1620 Span_freq_anz=2 !
                       SPAN OF FREQUENCIES IS 2
1630 Span_f_anz_unit$="KHZ" ! KILOHERTZ
1640 !
1650 Sweep_time = .4/Span_freq_anz
                                 ! SWEEP TIME DEPENDS ON SPAN
1660 !
1670 Rcc_size=1
1680 !
1690 RETURN
1700 !
1710 Display default:
                   1
1720 !
                    SHOW CHANGEABLE DEFAULTS
1730 !
1740 PRINT "YOU ARE CONTROLLING THE HP 3325A SIG GEN, THE HP 3561A SIG AN."
1750 PRINT "AND THE REST OF THE BUBBLE DETECTOR FROM THIS PC."
1760 PRINT "
1770 PRINT "
1780 PRINT "SOME OF THE DEFAULT SETTINGS ON THESE DELICATE INSTRUMENTS"
1790 PRINT "ARE HARD-CODED IN THIS IMMENSELY COMPLICATED PROGRAM, WHICK"
1800 PRINT "SHOULD BE TOUCHED ONLY BY HIGHLY TRAINED, AUTHORIZED PERSONNEL."
1810 PRINT "HOWEVER, OTHER SETTINGS CAN BE SELECTED EVEN BY AN"
1820 PRINT "IGNORANT LAYMAN LIKE YOURSELF."
1830 PRINT FOR INSTANCE, THE START AND STOP FREOS FOR THE SWEEP."
1840 PRINT "THE TIME TO COMPLETE A SWEEP, AND THE AMPLIFUDE OF THE SWEEP"
1850 PRINT "CAN BE CHANGED. IN ADDITION, FOR THE ANALYZER, THE START FREQ"
1860 PRINT "AND FREQ SPAN CAN BE CHANGED."
1870 PRINT "NOT ONLY THAT, BUT YOU CAN SELECT HOW MANY SWEEPS WILL DE"
1880 PRINT "TIME-AVERAGED INTO EACH CYCLE, AND HOW LONG THE SYSTEM"
1890 PRINT "PAUSES BETWEEN CYCLES. WHY, IT'S LIKE LIVING IN SPACE !!!"
1900 PRINT "
1910 PRINT "
1920 INPUT "PLEASE HIT THE ENTER KEY", Dummy$
1930 RETURN
1940 Display setting:
                  1
1950 PRINT ""
1960 PRINT "THE SETTINGS FOR THESE INSTRUMENTS ARE."
1970 PRINT "
1980 PRINT "FOR THE SIGNAL GENERATOR"
1990 PRINT "
2000 PRINT * 1 SWEEP START FREQ =";Sweep start_f;Strt_sweep unit$
2010 PRINT " 2 SWEEP STOP FREQ = ";Sweep_stop_{;Stop_sweep_unit$
2020 PRINT " 3 SWEEP TIME = ";Sweep_time;"SECONDS"
2030 PRINT * 4 SIGNAL AMPLITUDE = ";Signal amp;Sig amp unit$
2040 PRINT ""
2050 PRINT "FOR THE ANALYZER"
2060 PRINT ""
2070 PRINT " 5 START FREQ =";Start freq anz;Strt f anz unit$"
2080 PRINT * 6
               FREQ SPAN = ";Span_freq_anz;Span_f_anz_unit$
2090 PRINT "
2100 RETURN
```

```
2110 !
2120 Change default:
                    1
                  CHANGE ANY OF THE DEFAULTS?????
2130 !
2140 !
2150 GOSUB Display setting
2160 !
2170 First question:
                  1
2180 !
2190 INPUT "DO YOU WISH TO CHANGE ANY OF THE SETTINGS (Y OR N) ?", Reply$
2200 SELECT Reply$
2210 CASE "N", "n"
2220 RETURN
2230 CASE "Y", "y"
2240 GOTO Make_changes
2250 CASE ELSE
2260 PRINT "PLEASE RESPOND WITH Y OR N"
2270 GOTO First question
2280 END SELECT
2290 !
2300 Make_changes:
                    ŧ
2310 !
                  MAKE CHANGES IN SOME PARAMETERS
2320 !
2330 INPUT 'PLEASE INDICATE (BY NUMBER) WHICH PARAMETER SHOULD BE CHANGED"
2340 SELECT
2350 !
2360 CASE 1
2370 1
2580 INPUT "PLEASE ENTER THE NEW SWEEP START FREQ", Sweep start f
2390 PRINT "WHAT ARE THE UNITS (CHOOSE FROM THE FOLLOWING)"
2400 PRINT **
2410 PRINT *
                   HZ
                             HERTZ"
2420 PRINT *
                   KH
                           KILOHERTZ"
2430 INPUT *
                   MH
                           MEGAHERTZ",Strt sweep unit$
2440 GOTO Change default
2450 !
2460 CASE 2
2470 !
2480 INPUT "PLEASE ENTER THE NEW SWEEP STOP FREQ", Sweep stop f
2490 PRINT "WHAT ARE THE UNITS (CHOOSE FROM THE FOLLOWING)"
2500 PRINT **
                   HZ
                             HERTZ'
2510 PRINT *
2520 PRINT *
                   KH
                           KILOHERTZ<sup>*</sup>
2530 INPUT *
                   MH
                           MEGAHERTZ*, Stop_sweep_unit$
2540 GOTO Change default
2550 !
2560 CASE 3
2570 1
2580 INPUT "PLEASE ENTER THE NEW SWEEP TIME, IN SECONDS", Sweep time
        ! IF CHANGE SWEEP TIME, CHANGE SPAN, TOO
2590
     Span freq anz = .4/Sweep time
2600
2610
     Span f anz unit$="KHZ"
2620 GOTO Change default
2630 !
2640 CASE 4
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2650 ! 2660 INPUT "PLEASE ENTER THE NLW SIGNAL AMPLITUDE", Signal amp 2670 PRINT "WHAT ARE THE UNITS (CHOCSE FROM THE FOLLOWING)" 2680 PRINT ** 2690 PRINT * VO VOLTS" 2700 PRINT " MV MILLIVOLTS" 2710 PRINT * VR VOLTS RMS^{*} 2720 INPUT * MR MV RMS*,Sig amp unit\$ 2730 GOTO Change default 2740 ! 2750 CASE 5 2760 ! 2770 INPUT "PLEASE ENTER THE NEW START FREQ FOR THE ANALYZER", Start freq anz 2780 PRINT "WHAT ARE THE UNITS (CHOOSE FROM THE FOLLOWING)" 2790 PRINT " 2800 PRINT " HZ HERTZ" 2810 PRINT " KHZ KILOHERTZ" 2820 INPUT " MHZ MEGAHERTZ",Strt f anz unit\$ 2830 GOTO Change default 2840 ! 2850 CASE 6 2860 1 2870 INPUT "PLEASE ENTER THE NEW SPAN FREQ FOR THE ANALYZER", Span freq anz 2880 PRINT "WHAT ARE THE UNITS (CHOOSE FROM THE FOLLOWING)" 2890 PRINT ** 2900 PRINT * HZ HERTZ" 2910 PRINT " KHZ KILOHERTZ" 2920 INPUT " MHZ MEGAHERTZ^{*},Span f anz unit\$ 2930 ! IF CHANGE SPAN, CHANGE SWEEP TIME, TOO: 2940 IF Span f anz units = "HZ" THEN Sweep time = 400/Span freq anz 2950 IF Span f anz unit\$="KHZ" 'THEN Sweep time=.4/Span freq anz 2960 IF Span f anz units="MHZ" THEN Sweep time=.0004/Span freq anz 2970 GOTO Change default 2980 ! 2990 CASE ELSE 3000 ! 3010 PRINT "PLFASE CHOOSE AN INTEGER FROM 1 TO 6" 3020 GOTO Change_default 3030 ! 3040 END SELECT 3050 RETURN 3060 1 3070 Init siggen: ! 3080 ! INITIALIZE THE SIGNAL GENERATOR 3090 ! 3100 OUTPUT @Siggen;"ST";Sweep start f;Strt sweep unit\$ 3110 OUTPUT @Siggen;"SP";Sweep stop f;Stop sweep unit\$ 3120 OUTPUT @Siggen; TI"; Sweep_time; "SE" 3130 CUTPUT @Siggen;"AM";Sigual amp;Sig amp unit\$ 3140 OUTPUT @Siggen;"RF2" 3150 ! 3160 RETURN 3170 ! 3180 Init_anz: !

3190 ! INITIALIZE THE ANALYZER 3200 ! SEE HP MANUALS FOR THE MEANINGS OF THE FOLLOWING HP-IB MNEMONICS 3210 OUTPUT @Anz;"TACM" ! TIME CAFTURE MODEL 3220 OUTPUT @Anz;"SF";Start)req anz;Strt f anz unit\$ 3230 OUTPUT @Anz; "SP"; Span freq anz; Span f anz unit 3240OUTPUT @Anz;"AVTI"! USING TIME AVERAGING ON THE 3551A3250OUTPUT @Anz;"FLAT"! CHOOSE FLATTOP WINDOWING3260OUTPUT @Anz;"SLTA"! DEFINE T RACE 'A' 3270 OUTPUT @Anz;"VSFS.3MVRM" **! SET VERTICAL SCALE FOR TRACE** I DISPLAY ON FRONT PANEL OF 3561A 3280 3290OUTPUT @Anz;"VSLI"! LINEAR VERTICAL SCALE3300OUTPUT @Anz;"MAG"! CHOOSE MAGNITUDE DISPLAYED3310OUTPUT @Anz;"SLTB'! DEFINE TRACE 'B'3320OUTPUT @Anz; TIRE"! REAL TIME DISPLAY 3330 OUTPUT @Anz;"TBNR1REC" ! ONE TIME RECORD AT A TIME IN THE BUFFER 3340 OUTPUT @Anz;"TRGR" 3350 OUTPUT @Anz;"EXT" 3360 OUTPUT @Anz; "SLOPNEG" ! FXTERNAL TRIGGER; TRIGGERED BY NEGATIVE SLOPE 3370 ! 3380 PRINT "WAITING WHILE ANALYZER IS BEING INITIALIZED" 3390 WAIT 5 3400 ! 3410 ! DO ONE AUTORANCE ON THE 3561A SIGNAL ANALYZER: 3420 OUTPUT @Siggen;"SC" ! START CONTINUOUS RUN ON 3325A 3430 WAIT .5 3440 OUTPUT @Anz;"SARG" ! DO ONE AUTORANGE ONLY 3450 PRINT ** 3460 PRINT "WAITING FOR SIGNAL ANALYZER TO AUTORANGE" 3470 PRINT " 3480 ! 3490 WAIT 8 ! WAIT FOR COMPLETION OF AUTORANGING 3500 OUTPUT @Anz;"SCAP" ! INTO TIME CAPTURE MODE 3510 WAIT Sweep time +.5 3520 OUTPUT @Anz; "DTBB" ! DUMPING TIME BUFFER IN BINARY TO PC 3530 TRANSFER @Anz TO @Header;COUNT 350,WAIT 3540 CONTROL @Header,5;35 ! GET RANGE FROM HEADER 3550 ENTER @Header;Range 3560 Factor = 4/3*10^((Range + 4.812)/20)/32768 ! FOR CONVERTING TIME BUFFER DATA 3570 **! FROM BINARY TO VOLTAGE** 3580 ! 3590 OUTPUT @Anz;"ACAL OFF" ! DISABLES AUTOCALIBRATION OF 3561A 3600 OU (PUT @Anz;"ARNG OFF" ! DISABLES AUTORANGING OF 3561A 3610 OUTPUT @Siggen;"SS" ! RESETS 3325A SIG GEN 3620 RETURN 3630 ! 3640 How many: ! HOW MANY SWEEPS TO PERFORM PER CYCLE 3650 **! AND HOW LONG BETWEEN CYCLES** 3660 ! 3170 PRINT " 3680 PRINT ** 3690 INPUT "HOW MANY SWEEPS PER CYCLEDURING REGULAR DATA COLLECTION (1 TO 20) ?", Sweeps 3700 IF Sweeps > 20 OR Sweeps < 1 THEN How_many 3710 !

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3720 How many back: ! HOW MANY SWEEPS DURING BKGD MEASUREMENT
3730 INPUT "HOW MANY SWEEPS PER CYCLE DURING ...
                  ...BACKGROUND MEASUREMENT (1 TO 30) ?", Sweep back
3740 IF Sweep back>30 OR Sweep_back<1 THEN How many_back
3750 !
3760 How long:
3770 INPUT "HOW LONG (IN SECONDS) BETWEEN CYCLES ?", Waittime
3780 IF Waittime < 10 THEN
3790 PRINT "TOO SHORT AN INTERVAL; CHOOSE A TIME OF AT LEAST 10 SEC"
3800 GOTO How long
3810 END IF
3820 1
3830 PRINT **
3840 RETURN
3850 !
3860 Index:
               ١
3870 INPUT "THE DATA FILES WILL BE NUMBERED, STARTING WITH NUMBER ---, Istart)
3880 PRINT ""
3890 RETURN
3900 !
3910 Trigger system: ! BEGIN THE DATA COLLECTION
3920 !
3930 OUTPUT @Anz;"SCAP"
                           ! ANALYZER IN START CAPTURE MODE
3940 WAIT Sweep time+.5
3950 OUTPUT @Siggen;"SSSS" ! THE FIRST "SS" RESETS THE SIGNAL GEN
3960
                   ! AND THE SECOND STARTS THE SWEEP
3970 WAIT Sweep time
                       ! WAIT FOR SWEEP TO FINISH BEFORE
3980
                 ! TRYING TO READ TIME BUFFER
3990 RETURN
4000 !
4010 Read data:
                ! GET BUFFERED DATA FROM THE ANALYZER
4020 !
4030 IF N=0 THEN Limit=Sweep back ! N=0 MEANS BKGD BEING MEASURED
4040 IF N=1 THEN Limit=Sweeps
                                ! N=1 MEANS REGULAR DATA BEING COLLECTED?
4050 PRINT *
               ON SWEEP ";li;" OF ";Limit
4060 PRINT "
4070 !
4080 CUTPUT @Anz;"DTBB"
4090 New read:
                1"
4100 CONTROL @Header,3;1
4110 CONTROL @Time buff,3;1
4120 TRANSFER @Anz TO @Header;COUNT 350,WAIT
4130 TRANSFER @Anz TO @Time buff;COUNT 2048,WAIT
4140 MAT Raw_data(Ii,*) = Raw_raw_data
4150 RETURN
4160 !
4170 !
4180 Convert and sum: ! GET AN AVERAGE FOR THE DATA CVER SEVERAL SWEEPS
4190 !
4200 PRINT ""
4210 IF N=0 THEN
                           ! N≈0 MEANS BKGD BEING MEASURED
4220 Limit=Sweep back
4230 PRINT "NOW AVERAGING OVER THE ";Limit;" SWEEPS"
4240 END IF
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4250 IF N=1 THEN
                           ! N=1 MEANS REGULAR DATA BEING COLLECTED
4260 Limit = Sweeps
4270 PRINT "NOW AVERAGING OVER THE ":Limit;" SWEEPS AND SUBTRACTING BACKGROUND"
4280 END IF
4290 !
4300 FOR J=1 TO 512
4310
      Amplitude(J) = 0
4320
      FOR li=1 TO Limit
       ! CONVERT TO AMPLITUDE AND DO TIME AVERAGING SIMULTANEOUSLY
4330
4340
        Amplitude(J) = SQRT(Raw data(Ii,2*J-1)^2 + Raw data(Ii,2*J)^2) + Amplitude(J)
4350
     NEXT Ii
4360 NEXT J
4370 MAT Amplitude = Amplitude*(Factor/Limit))
4380 RETURN
4390 !
4400 !
4410 Store data:
                  ! STORE AMPLITUDE SPECTRUM AFTER SUBTRACTING BACKGROUND
4429 !
4430 CREATE BDAT File$,512,8
4440 ASSIGN @Path TO File$
4450 OUTPUT @Path;Amplitude(*)
4460 !
4470 RETURN
4480 !
                     ! FIND AREA UNDER VOLTAGE AMPLITUDE SPECTRUM;
4490 Integrate:
4500
                     !SEPARATE POSITIVE AND NEGATIVE CONTRIBUTIONS TO TOTAL AREA
4510 Area=0
4520 Fosarea=0
4530 Negarea = 0
4540 FOR Int=1 TO 512
4550
      Area = (Amplitude(Int) + Amplitude(Int + 1)) + Area
4560
      IF Amplitude(Int)> = 0 AND Amplitude(Int+1)> = 0 THEN
4570
       Posarca = Posarca + Amplitudc(Int) + Amplitudc(Int + 1)
4580
      ELSE
4590
        IF Amplitude(Int) \leq = 0 AND Amplitude(Int + 1) \leq = 0 THEN
4600
         Negarea = Negarea + Amplitude(Int) + Amplitude(Int + 1)
4610
        ELSE
4620
         IF Amplitude(Int)>0 AND Amplitude(Int+1)<0 THEN
          Posarea = Amplitude(Int)*Amplitude(Int)/(Amplitude(Int)-Amplitude(Int+1))+Posarea
4630
          Negarea = Amplitude(Int + 1)*(1 + Amplitude(Int)/(Amplitude(Int + 1)-Amplitude(Int))) + Negarea
4640
4650
         ELSE
4660
          IF Amplitude(Int)<0 AND Amplitude(Int+1)>0 THEN
4670
            Posarca = Amplitude(Int + 1)*(1 + Amplitude(Int)/(Amplitude(Int + 1)-Amplitude(Int))) + Posarca
            Negarea = Amplitude(Int)*Amplitude(Int)/(Amplitude(Int)-Amplitude(Int+1))+Negarea
4680
4690
          END IF
4700
         END IF
4710
       END IF
     END IF
4720
4730 NEXT Int
4740 !
4750 IF Strt sweep unit$="HZ" THEN Startf=Sweep start f/1.E+6
4760 IF Strt sweep unitS = "KH" THEN Startf = Sweep start f/1.E+3
4770 IF Strt sweep units = "MH" THEN Startf = Sweep start f
4780 IF Stop sweep unit$="HZ" THEN Stopf=Sweep stop f/1.E+6
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4790 IF Stop sweep units "KH" THEN Stopl= Sweep stop f 11 + 3
4800) IF Stop sweep units "MH" THEN Stopl=Sweep stop f
4810 !
                                            2 CONVERTS TO aV MH2
4820 Arca = Arca*,5*(Stopf-Startf)*1.E.+0.512
4830 Posarea = Posarea* 5*(Stopt-Startf)*1 E + 6 -512
                                             * CONVERTS TO $5 MHz
4840 Negarea Negarea* 5*(Stopf-Startf)*1E = 6/512
                                              CONVERTS TO IN MILE
4850 !
4500 RETURN
4570 !
                * DISPLAY THE DATA ON SCREEN
4880 Plot data
4890 !
4x0_CLEAF SCREEN - FALFHA DISPLAY RETAINED AS GRAPHICS DISPLAY IS CALLED UP
4910 GCLF - C
4920 GINH
4930 1
4940 EDETERMINE HOW FAR THE Y ANIS SHOULD EXTEND
4950 REAL Absamp(512)
4960 MAT Absamp - ABS(Amplitude) - COSVERT Amplitude MATRIX TO MAGNITUDES
                                * DETERMINE MAGNITUDE OF LARGEST Y VALUE
4970 Max = MAX(Absamp(*))
4980 Yhm=100*(INT(Max*LE+4)+1) ! MAX VALUE ON VAXIS, FLOT IN MICROVOLTS
4921 1
                            PLABEL THE PLOT AND THE AXES
5000 IF N=0 THEN
5010 MOVE 28,95
502) LABEL 'BACKGROUND @ 'ATIMES(TIMEDATE)A' 'ADATES(TIMEDATE)
                      PN = 1; SIGNAL BEING MEASURED
5030 ELSE
5040 MOVE 50,95
5050 LABEL "SIGNAL (# "& TIMES(TIMEDATE)
5060 END IF
5070 !
5080 MCVE 9,75
5090 Label$ = "Voltage"
3100 FOR I=1 TO 7
5110 LABEL Label$[I,I]
5120 NEXT I
5130 1
5140 MOVE 13,80
5150 Label$="Amplitude"
5160 FOR I=1 TO 9
5170 LABEL Label $[1,1]
5180 NEXT I
5190 !
5200 MOVE 41,17
5210 LABEL "Forcing Frequency (MHz)"
5220 MOVE 18,89
5230 LABEL VAL$(Ylim)&" uV"
5240 MOVE 22.58
5250 LABEL "0 uV"
5260 MOVE 15.29
5270 LABEL VAL$(-Ylim)&" uV"
5280 MOVE 36,23
5290 !
5300 IF Strt sweep units = "HZ" THEN LABEL VALS(Sweep_start_f/1.E+6)
5310 IF Strt_sweep_units = "KH" THEN LABEL VALS(Sweep_start f/1 E+3)
5320 IF Strt sweep units = "MH" THEN LABEL VALS(Sweep_start_f)
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5330 MOVE 106.23
5340 IF Stop sweep unit$ = "HZ" THEN LABEL VAL$(Sweep stop f/1.E+6)
5350 IF Stop sweep unit = "KH" THEN LABEL VALS(Sweep stop f/1.E+3)
5360 IF Stop sweep units = "MH" THEN LABEL VALS(Sweep stop f)
5370 !
5380 MOVE 6,9
5390 LABEL USING "17A,S6D.2D,15A";"POSITIVE AREA IS ", Posarca," microvolts-MHz"
5400 MOVE 6.4
5410 LABEL USING "17A,SoD.2D,15A ","NEGATIVE AREA IS ", Negarea," microvolts-MHz"
5420 1
                               ! POSITION THE GRAPH ON THE CRT
5430 VIEWPORT 38,108,30,90
5440 WINDOW 0, Sweep time, (-Ylim/1.E+6), (Ylim/1.E+6) ! SIZE THE AXES
5450 AXES Sweep_time/10,(Ylim/1.E+6)/10,0,0
                                          ADD TICK MARKS
5400 1
5470 PEN 1
5480 D_x = (Sweep time/(Rec size))/512
5490 X = 0
5500 MOVE 0, Amplitude(1)
5510 FOR 1=1 TO 512
5520 DRAW X, Amplitude(1)
                          ! PLOT THE DATA
5530 = X = X + D_X
5540 NEXT 1
5550 RETURN
5500 1
5570 Read trace:
                ! READ THE MAGNITUDE TRACE FROM THE 3561A.
              ! MAGNITUDE HAS BEEN TIME-AVERAGED ON THE 3561A.
5580
5590 OUTPUT ((Anz; SLTA" ! ACTIVATE TRACE A, THE MAGNITUDE TRACE
5000 OUTPUT @Anz;"DSTB"
                                 ! DUMP ACTIVE TRACE AND HEADER DATA
5010 TRANSFER @Anz TO @Tag;END,WAIT ! TRANSFER TO BUFFER ON I'C
5620 CONTROL @Tag,5;5 POSITION THE BUFFER FOINT READER TO BYTE 5
5630 ENTER @Tag;Raw trace(*) ! READ THE DATA FROM THE TRACE INTO AN ARRAY
5640 !
5650 P.ETURN
5660 !
5670 Scale trace:
                ! CONVERT BINARY DATA TO VOLTAGE
5680 FOF It=1 TO 401
5690 Trace data(lt)=10.^(Raw trace(lt)*.005/20.) ! CONVERTS TO VOLTAGE
5700 NEXT It
5710 RETURN
5720 !
5730 Plot trace: ! DISPLAY THE TRACE FROM THE 3561A ON SCREEN
5740 !
5750 CLEAR SCREEN ! ALPHA DISPLAY RETAINED AS GRAPHICS DISPLAY IS CALLED UP
5760 GCLEAR
5770 GINIT
5780 !
5790 Maxi=MAX(Trace data(*))
5800 Ymax=100*(INT(Maxi*i.E+4)+1) ! MAX VALUE OF Y; PLOTTING IN MICROVOLTS
     ! DETERMINE HOW FAR THE Y-AXIS STIOULD _XTEND:
5810
5820 Ylim = Ymax
5830 !
5840 IF N=0 THEN
                           ! LABEL THE PLOT AND THE AXES
5850 MOVE 47,95
5860 LABEL "BACKGROUND TRACE"
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5870 ELSE ! N = 1; SIGNAL BEING MEASURED 880 MOVE 50,94 890 IABEL "SIGNAL TRACE" 5900 END IF 5910 1 5920 MOVE 9,75 5930 Label\$="Voltage" 5940 FOR I=1 TO 7 5950 LABEL LabelS[1,1] 5960 NEXT I 5970 1 5980 MOVE 13,80 5990 Label\$="Amplitude" 6000 FOR I=1 TO 9 6010 LABEL LabelS[I,I] 6020 NEXT I 6030 1 6040 MOVE 42,17 6050 LABEL "Offset Frequency (kHz)" 6060 MOVE 18,89 6070 LABEL VAL\$(Ymax)&" uV" 6080 MOVE 22,29 6090 LABEL "0 uV" 6100 ! 6110 IF Strt f anz units="HZ" THEN Start_freq_anz=Start_freq_anz/1.E+3 6120 IF Strt f anz units="MHZ" THEN Start freq anz=Start_freq_anz*1.E+3 6130 IF Span f anz units="HZ" THEN Span freq anz=Span_freq_anz/1.E+3 6140 IF Span f anz_unit\$="MHZ" THEN Span_freq_anz=Span_freq_anz*1.E+3 6150 I 6160 MOVE 36,23 6170 LABEL VAL\$(Start_freq_anz) 6180 MOVE 106,23 6190 LABEL VAL\$(Start_freq_anz+Span_freq_anz) 6200 · 6210 VIEWPORT 38,108,30,90 **! POSITION THE GRAPH ON THE CRT** 6220 WINDOW 0,Span_freq_anz,0,(Ylim/1.E+6) ! SIZE THE AXES 6230 AXES Span_freq_anz/10,(Ylim/1.E+6)/10,0,0 ! ADD TICK MARKS 6240 ! 6250 PEN 1 6260 Dx=Span_freq_anz/400 6270 X = 06280 MOVE 0, Trace_data(1) 6290 FOR It = 1 TO $\overline{401}$ 6300 DRAW X, Trace data(It) ! PLOT THE DATA 6310 X = X + Dx6320 NEXT It 6330 RETURN 6340 ! 6350 END