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NUMERICAL ANALYSIS OF COMPOSITE DIELECTRICS:
PRELIMINARY RESULTS FOR TWO DIMENSIONS

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INTRODUCTION

The use of composite materials and structures to provide characteristics unattainable directly from the constituent materials is well known. Perhaps the most widespread example is steel-reinforced concrete for structural applications wherein the high tensile strength of the steel in conjunction with the high compressive strength of the concrete yields a composite material with structural properties far superior to those of either component. More recently, work has been undertaken to apply this principle to the development of dielectric materials for energy storage applications. It is anticipated that this technology will provide materials for use in capacitors with greater energy density, lower loss, and higher breakdown resistance. This report describes the results of an effort to analytically model the net or resultant dielectric behavior of such composite dielectric materials.

The net dielectric behavior of a randomly interspersed composite is dependent on the spatial dimensionality (1-D vs. 2-D vs. 3-D), domain geometries (domain size, domain shape, stratification, etc.), and interconnection effects (percolation). This collective dependence is only partly understood. One averaging law which is useful to the experimentalist because of its relative ease in dealing with multiple components is [1]

$$\epsilon^\alpha = \sum v_k \epsilon_k^\alpha \quad (1)$$

where ϵ is the net dielectric permittivity of the composite while ϵ_k is the dielectric permittivity component occupying volume fraction v_k . The exponential factor α depends on the geometry of the constituent components and has been rigorously derived for only the special cases of layers oriented perpendicular to the applied electric field and layers oriented along the direction of the electric field [2]. For the case of layers oriented perpendicular to the applied electric field, $\alpha = -1$ and equation 1 may be interpreted as harmonic averaging. For the case of layers oriented along the direction of the applied electric field, $\alpha = +1$ and equation 1 may be interpreted as arithmetic averaging. Although no obvious physical significance may be immediately attached to the case of $\alpha = 0$, it may be interpreted as geometric averaging. No generalized analytic expression for α exists, and a primary goal of this work is to develop a numerical technique to obtain this factor for different composites.

DIELECTRIC PERMITTIVITY

The dielectric permittivity ϵ relates an applied electric field to the induced displacement field arising as a result of the applied electric field. This relationship is usually written

$$D_i = \epsilon_{ij} E_j \quad (2)$$

where both the displacement D_i and electric field E_j are vector

quantities and the dielectric permittivity ϵ_{ij} is a tensor of rank two over the spatial indices i, j . The summation convention applies to the repeated index j . In the case of isotropic media, equation 2 takes the vector form

$$\mathbf{D} = \epsilon \mathbf{E} \quad (3)$$

with ϵ now written as a scalar quantity. In all practical cases, the dielectric permittivity is a complex quantity and may be denoted

$$\epsilon = \epsilon' + j \epsilon'' \quad (4)$$

wherein $j = \sqrt{-1}$. The Kramers-Kronig relationship, based on time-causality considerations, specifies that the real and imaginary parts of ϵ are not independent. In engineering applications, the complex nature of ϵ is more commonly referred to by the use of the loss tangent, defined as

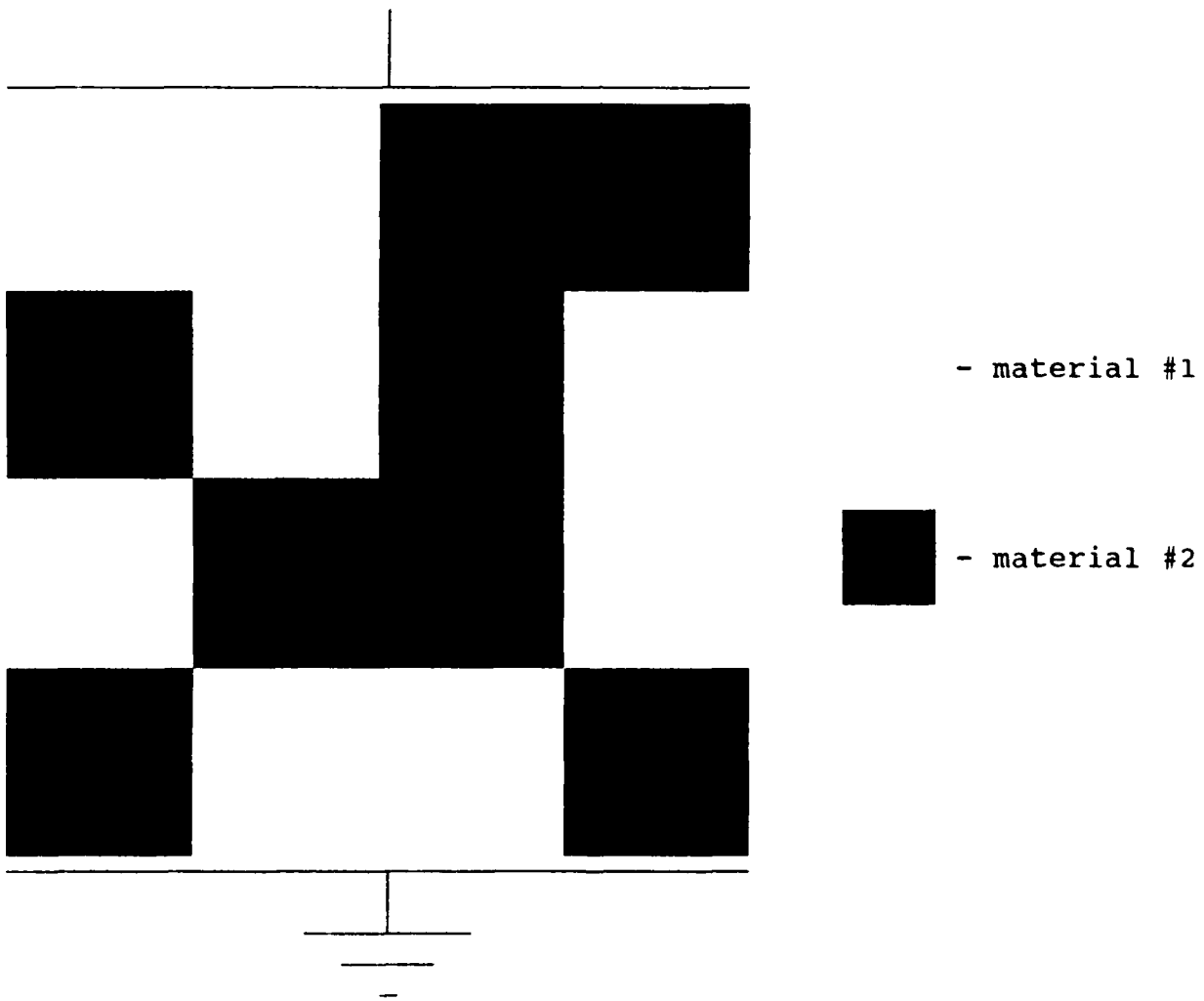


Figure 1. Parallel plate capacitor with composite dielectric.

$$\tan \delta \equiv \epsilon'' / \epsilon' \quad (5)$$

For many common insulators, the loss tangent is on the order of 10^{-4} , and consequently $\tan \delta$ is often approximated by δ . For the purposes of this report, ϵ'' will be taken as zero; the more general case will be treated in a subsequent report.

COMPOSITE DIELECTRIC STRUCTURE

The composite dielectric structure can be modeled as a collection of interconnected domains, with the material properties of each domain being distinct. Figure 1 illustrates a cross-sectional view of a parallel plate capacitor employing a dielectric composed of two distinct materials.

In order to analyze the structure, we superimpose a pixel grid on the specimen. The pixel grid is chosen such that the material within any pixel is homogeneous. This is illustrated in

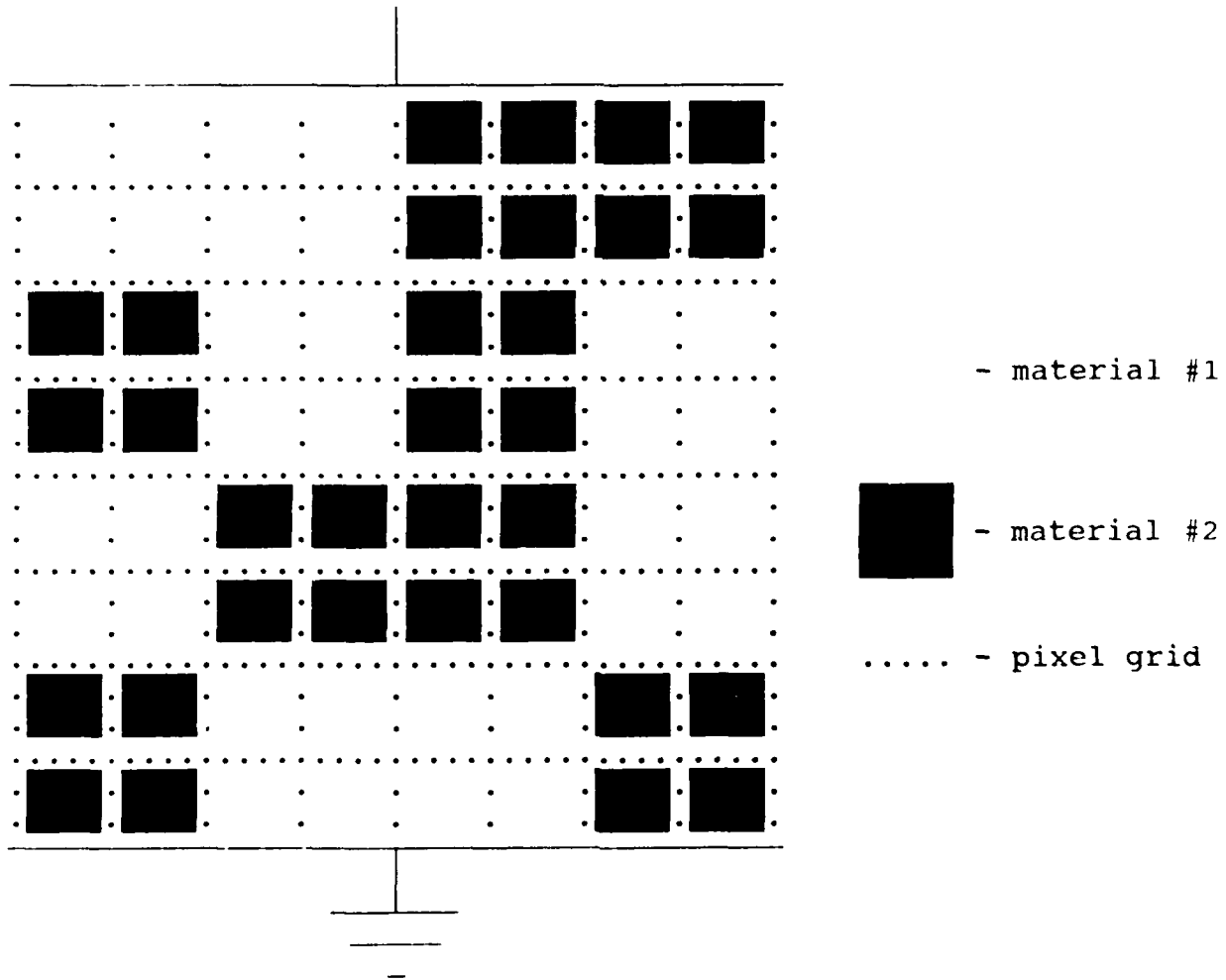


Figure 2. Parallel plate capacitor with composite dielectric showing superimposed pixel grid.

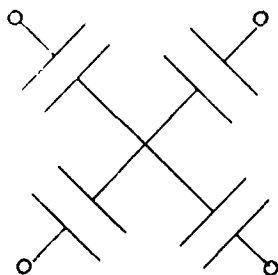


Figure 3. Four-terminal network pixel element model.

Figure 2. The pixel grid forms a Cartesian coordinate system with one axis parallel and one axis perpendicular to the applied electric field. The dielectric properties of the material within any pixel are assigned by means of the pixel grid coordinate system.

We can consider each pixel site as a four-terminal network and can model all nearest-neighbor interactions of any pixel by considering the array of nodes formed at the pixel intersections. This is sufficient to assign a vector displacement to each pixel. The four-terminal network within each pixel is comprised of a set of four capacitors, each connected between a common node at the center of the pixel and one of the corners as illustrated in Figure 3. The value associated with each capacitor is simply the size-normalized capacitance between the pixel center and any corner.

We can redraw the composite dielectric pixel grid of Figure 2 with the four-terminal equivalent network substituted for each pixel element, and obtain the electrical network shown in Figure 4. This network may be analyzed by means of Kirchoff's Laws as applied to the displacement field D in the static case or displacement current dD/dt in the dynamic case.

NETWORK ANALYSIS

In the application of Kirchoff's Laws to the analysis of the equivalent electrical network, we are confronted with the choice of using either mesh analysis or nodal analysis. We choose to employ nodal analysis for the following reasons:

- 1) The numerical solution is more stable using nodal analysis than using mesh analysis. Essentially, as one traverses the composite network, the nodal solution transitions smoothly from pixel to pixel and the relative differences in currents are small, whereas with mesh analysis we may see alternations in the sense of the loop currents which greatly increases the relative differences in currents. From a numerical standpoint, this choice is important in avoiding truncation errors.

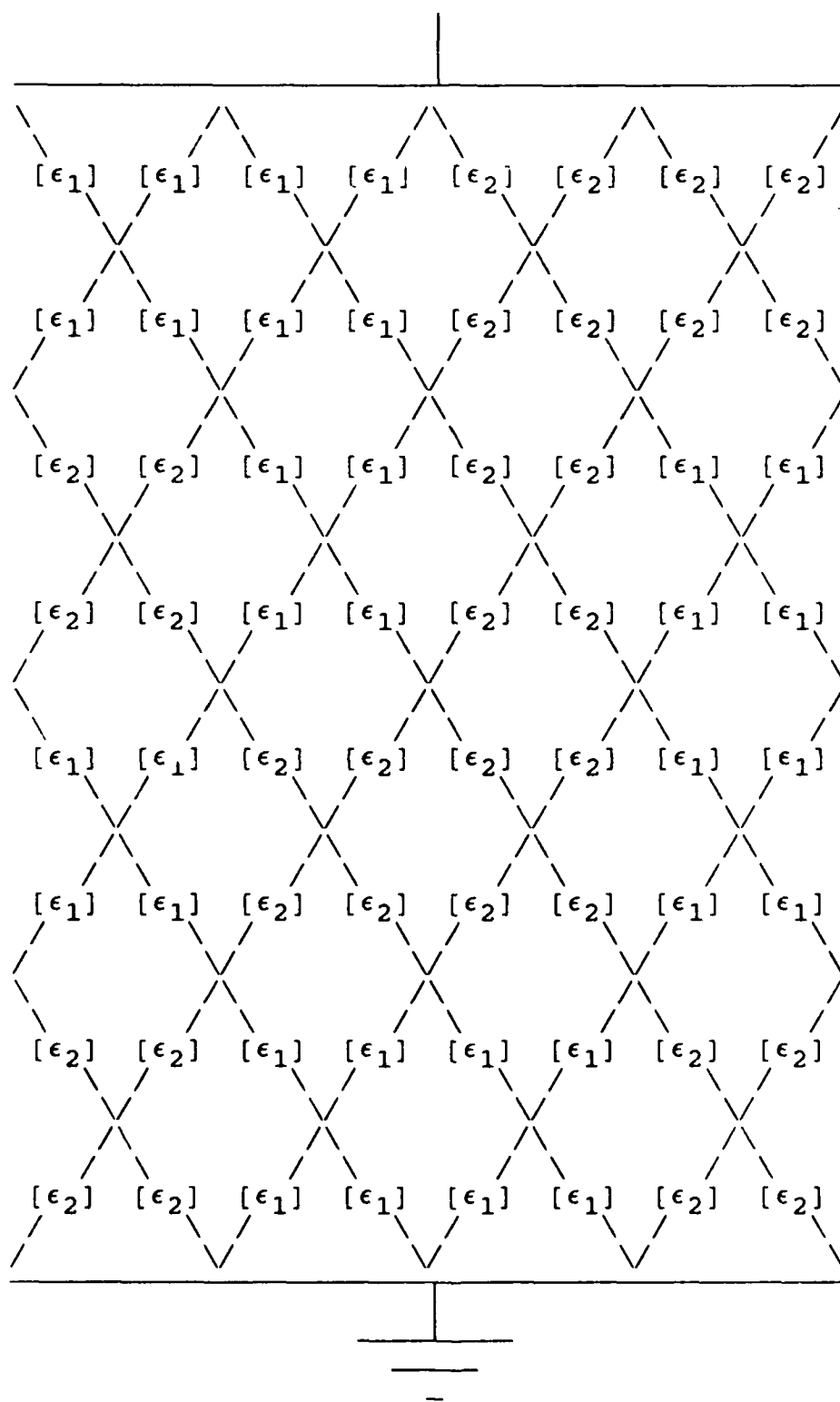


Figure 4. Composite dielectric equivalent electrical circuit where the circuit components have been numbered with subscripts 1 and 2 to correspond with the material components of Figure 2.

2) The boundary conditions are more readily implemented using nodal analysis. This includes both the excitation and lateral boundaries.

Implementation of the nodal analysis results in a succinct description of the network. The currents I_{ij} between the i th node and its nearest neighbors are described by

$$\sum I_{ij} = 0 \quad (5)$$

for all nodes except along the excitation plane. A normalized current is applied to nodes along the excitation plane, for which we may write

$$\sum I_{ij} = j \omega \quad (6)$$

where $j\omega$ is the complex radian frequency of the excitation. The summation is taken over the nearest neighbor nodes. The size normalized admittance of the capacitor elements between nodes i and j may be written

$$Y_{ij} = j \omega \epsilon_{ij} \quad (7)$$

Equation 7 may be substituted into equations 5 and 6 using Ohm's Law and the potentials at nodes i and j , resulting in

$$\sum \epsilon_{ij} (V_i - V_j) = 0 \quad (8)$$

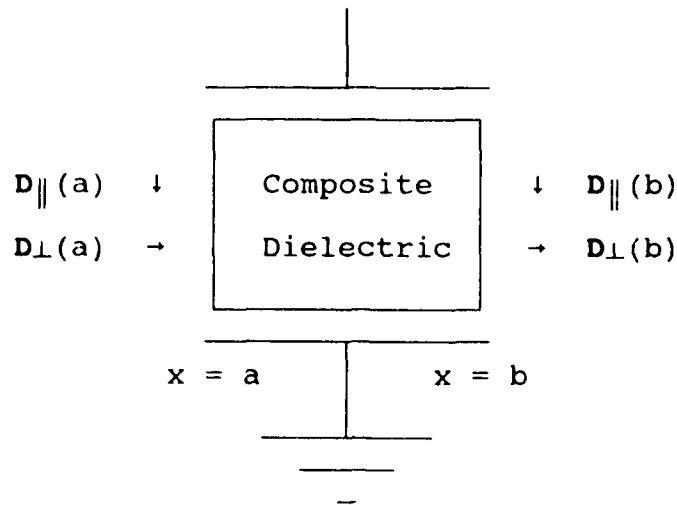
for most nodes and

$$\sum \epsilon_{ij} (V_i - V_j) = 1 \quad (9)$$

for nodes on the excitation plane. The solution of the nodal equations varies with frequency since the ϵ_{ij} of the constituent materials are in reality frequency dependent with the different materials having different frequency dependencies.

BOUNDARY CONDITIONS

In the formulation of the network to be solved, we encounter two common types of boundary conditions concerning the displacement field at the lateral boundaries. The first condition is that of 'insulating' sides, wherein we consider the dielectric specimen to be electrically isolated along the lateral boundaries. In this case, the normal component of the displacement field D is considered to be zero at the lateral boundaries. For simplicity, we also assume that fringing electric fields are nonexistent. This boundary condition is applicable to the analysis of isolated samples or lattice cells with mirror-symmetry-plane boundaries. The second condition is that of 'periodic' boundaries, wherein we consider the dielectric specimen to be a repeated cell in a cyclic lattice structure. In this case, the normal component of displacement field is non-zero and the same at both boundaries, as is the tangential component



'Insulating'	'Periodic'
$D_{ }(a) \neq D_{ }(b) \neq 0$	$D_{ }(a) = D_{ }(b) \neq 0$
$D_{\perp}(a) = D_{\perp}(b) = 0$	$D_{\perp}(a) = D_{\perp}(b) \neq 0$

Figure 5. Lateral boundary conditions on the composite dielectric.

of D . The two types of boundary conditions are illustrated in Figure 5.

COMPUTER IMPLEMENTATION OF THE NETWORK

The equivalent electrical network representing the composite dielectric may be conveniently solved using computer methods. An important prerequisite to obtaining a solution is the development of an appropriate scheme for identifying both pixel grid nodes and the internodal capacitances. In the scheme adopted here, the pixel grid nodes are numbered sequentially starting from the ground electrode and terminating with the excitation electrode. The internodal capacitances are identified as elements in a two-dimensional array. The numbering scheme is illustrated in Figure 6.

The node numbering scheme is not arbitrary, but is chosen in such a fashion as to maximize the stability of the numerical solution. By beginning at the ground electrode and moving along planes of increasing potential, we can minimize truncation errors. The number of nodes in the pixel grid depends on the lateral boundary conditions. The node numbering schemes for both 'insulating' and 'periodic' boundary conditions are illustrated in Figure 7.

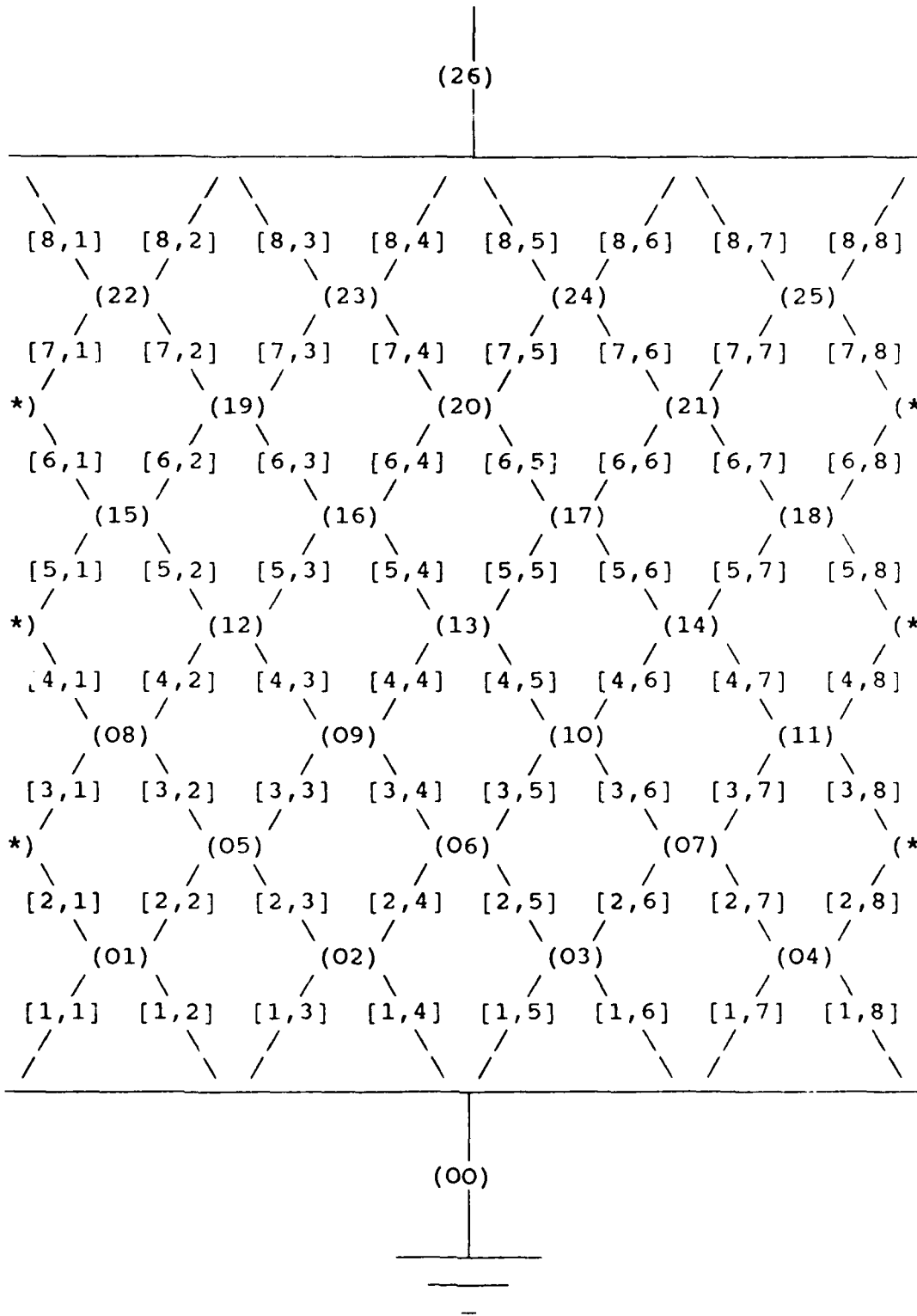


Figure 6. Pixel grid nodes (round brackets) and internodal capacitance (square brackets) numbering scheme for the case of 'insulating' boundary conditions.

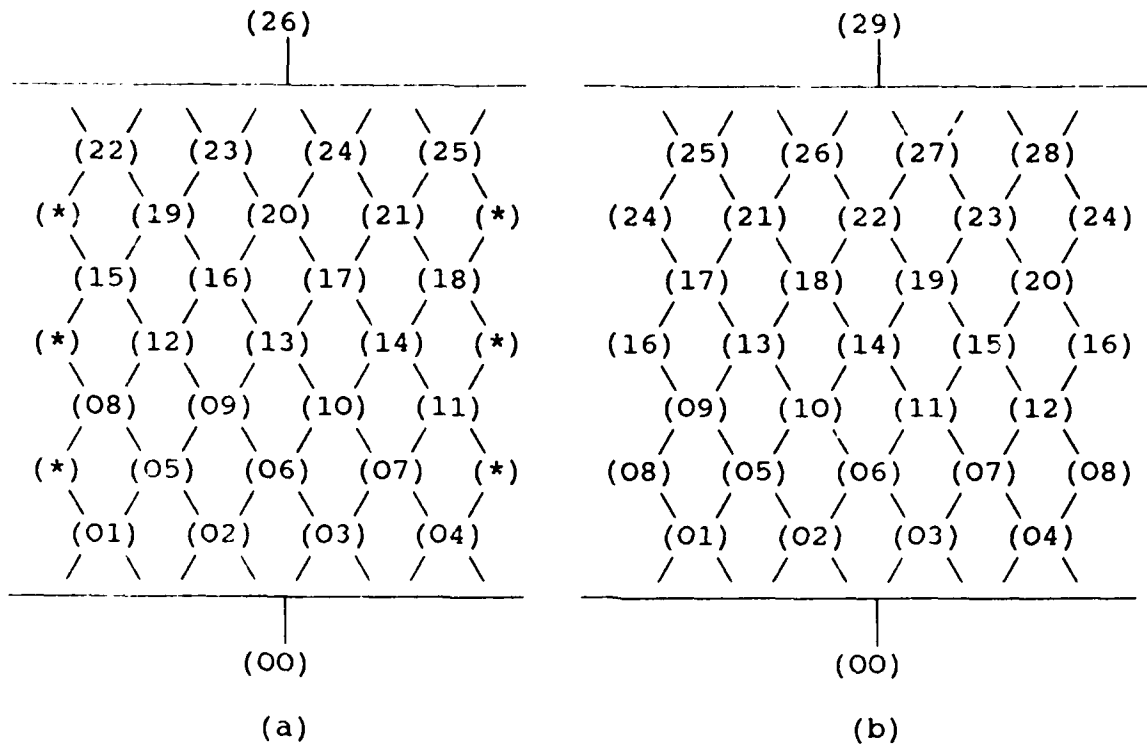


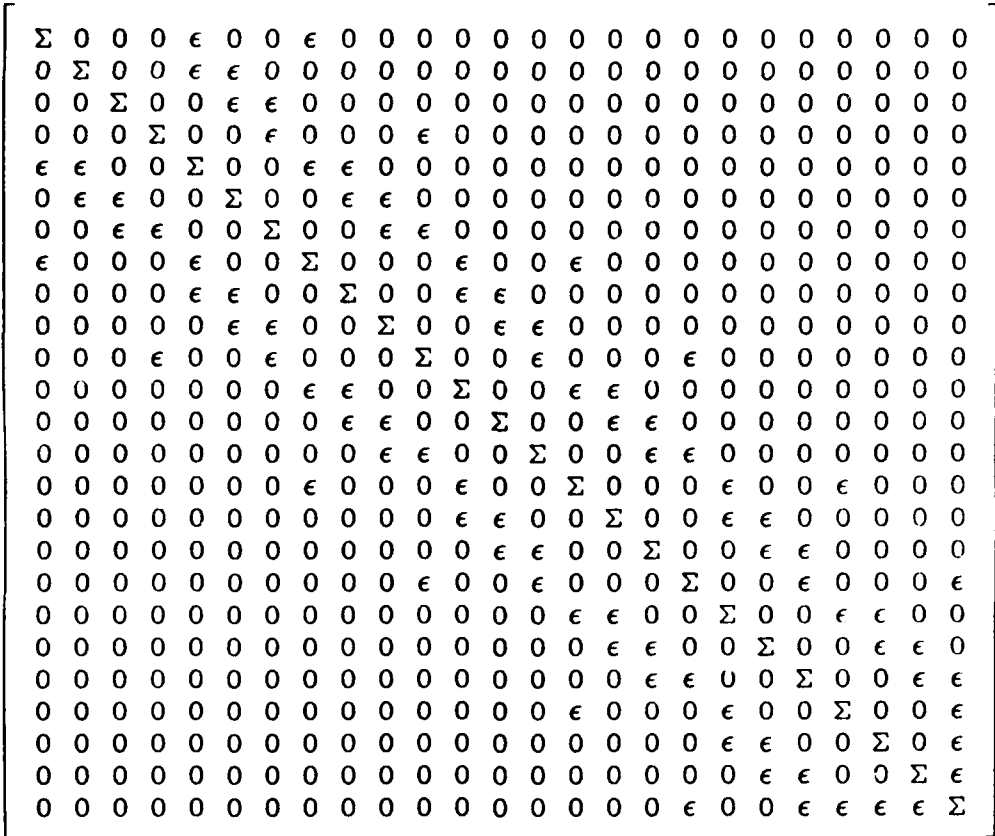
Figure 7. Node numbering scheme in the case of a) 'insulating' and b) 'periodic' boundary conditions. In the case of 'insulating' boundary conditions, the internodal capacitances along the starred (*) paths are obtained from series connection of the constituent internodal capacitances. In the case of 'periodic' boundary conditions, the nodes at one boundary effectively 'wrap around' to the other boundary.

INTERACTION MATRIX

Expansion of equations 8 and 9 over the entire pixel grid will yield a set of simultaneous equations which must be solved to obtain the unknown nodal potentials. Once the nodal potentials are known, the net dielectric permittivity is calculated as the quotient of the excitation displacement current and the excitation potential. The full set of equations takes the form

$$\{ I \} = \{ \epsilon \} \{ V \} \quad (10)$$

where $\{ I \}$ is a column vector of the generalized displacement currents, $\{ V \}$ is a column vector of the nodal potentials, and $\{ \epsilon \}$ is the interaction matrix describing the composite dielectric. The interaction matrix is in general a sparse symmetric matrix, with the sparseness arising from the fact that only nearest-neighbor interaction terms are non-zero. Except for the extrema, there are only five non-zero terms in any row, hence the degree of sparseness increases approximately as the square of the matrix



Σ = summation of internodal capacitances

ε = internodal capacitance term

Figure 8. Interaction matrix showing the location of non-zero terms using the chosen node numbering scheme.

size. The location of the non-zero elements in the matrix depends upon the node numbering scheme employed, and we have chosen a node numbering scheme such that the interaction matrix is 'banded' with the non-zero terms clustered about the main diagonal. The form of this matrix is illustrated in Figure 8.

Using the 'banded' interaction matrix as shown provides a distinct computational speed and memory size advantage over the use of a 'non-banded' matrix with arbitrary non-zero element locations. The execution speed in the 'banded' case is proportional to the square of the matrix size, whereas in the 'non-banded' case execution speed is proportional to the cube of the matrix size. Memory size is conserved using the 'banded' form since only a small segment of the matrix is operated upon at any time. In this case, the size of the interaction matrix which may be evaluated is limited only by the range of computer addresses available and the time required to perform the calculations.

VERIFICATION OF NUMERICAL SOLUTION

The accuracy of the numerical solution obtained here has been tested in several ways. The first test involved calculation of the exponential averaging factor α for the known cases of stratified layers parallel to the excitation and perpendicular to the excitation. In both cases, for permittivities ϵ_1 and ϵ_2 such that $\epsilon_1/\epsilon_2 < 10^9$ (limited by the computer implementation), the results of the numerical solution were as expected. The second test involved examining the stability of the numerical solution as the grid size was changed for a fixed distribution of constituent materials. No variations in the numerical output were detected as the grid size was varied from 4x4 pixels (26 nodes) to 40x40 pixels (3161 nodes).

The third test involved comparing numerical solutions employing different implementations of node numbering and matrix inversion routines. Essentially, the final version of the numerical analysis code grew out of three earlier, less efficient but computationally accurate implementations. The first code employed a node numbering scheme which started at the center of the dielectric and spiraled outward to the boundaries. This code also employed the matrix inversion routine resident in the programming language. The second version employed the same node numbering scheme but substituted L-U decomposition for matrix inversion. The third version also used the same node numbering scheme, but employed Gaussian elimination in evaluating the interaction matrix. All three versions employed back substitution to verify the numerical solutions. No differences were found between the test case solutions obtained by these versions and the final version.

The fourth and final case involved comparing the current numerical results to those obtained in an earlier work [3]. Again, the current numerical results were in good agreement with the earlier work.

PRELIMINARY RESULTS

The computer code has been used to examine the variation in exponential averaging factor α with the ratio of constituent permittivities in a two-component composite dielectric. Figures 9 through 12 show the results obtained for ϵ_1/ϵ_2 ratios of 1.1, 10, 100, and 1000 respectively. Each figure shows the value of α as a function of constituent volume ratio. Each data point represents the calculated behavior of a capacitor with the indicated volume fractions of constituent dielectrics. For each calculation, the spatial distribution of the constituent dielectrics is determined by a random number generator, the interaction matrix is evaluated to determine the net dielectric permittivity, and Equation (1) is solved iteratively for α . One can see from these figures that the behavior of the exponential averaging factor depends on the constituent permittivity ratio and that the behavior falls into three general categories:

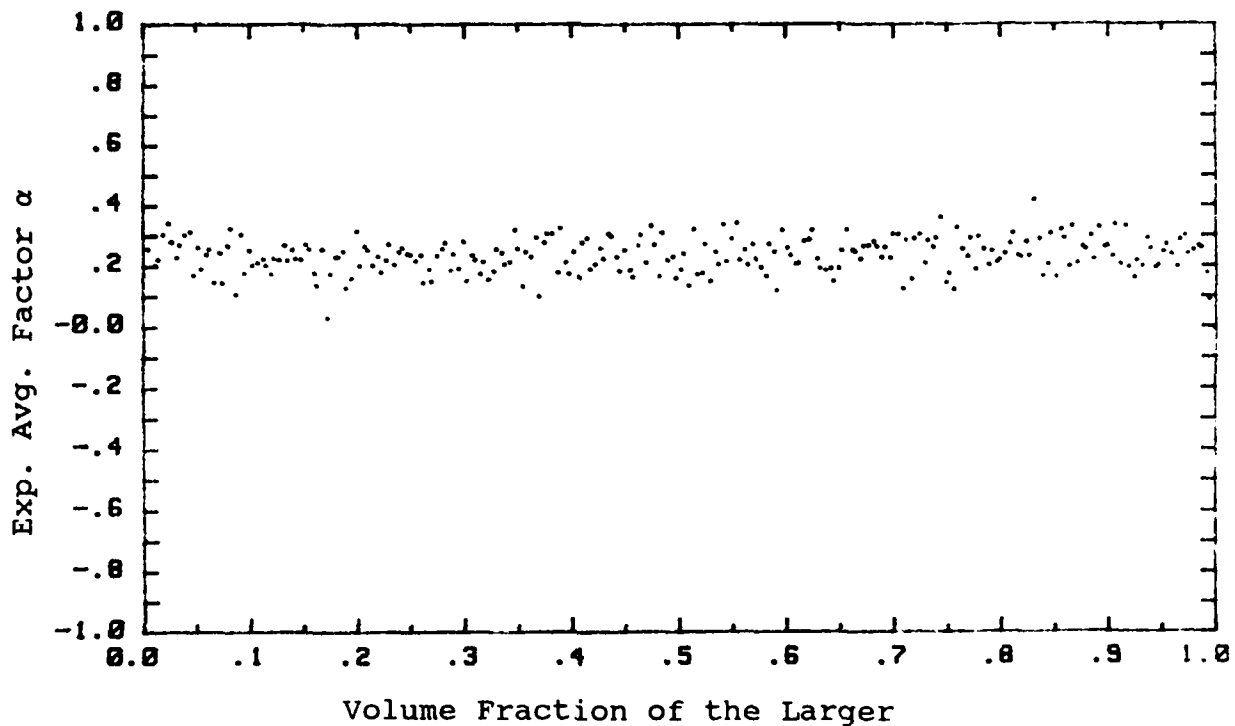


Figure 9. Exponential averaging factor α as a function of constituent volume ratio V_1/V_2 for permittivity ratio $\epsilon_2/\epsilon_1 = 1.1$.

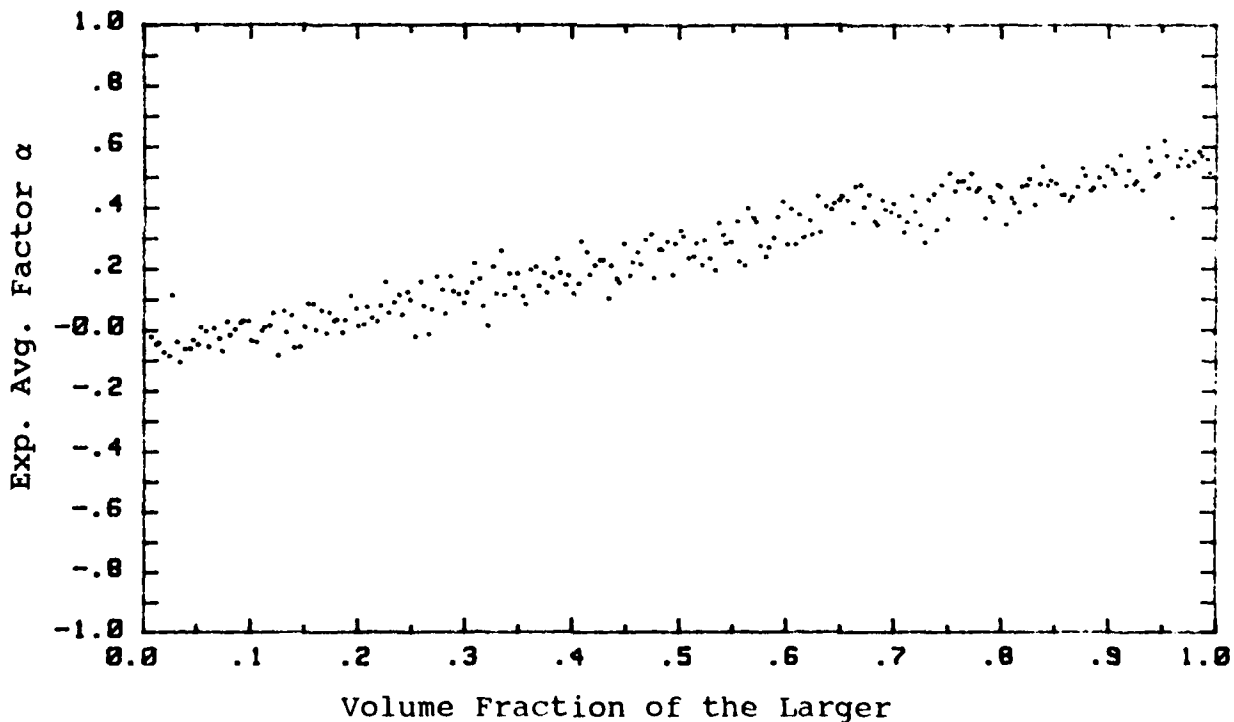


Figure 10. Exponential averaging factor α as a function of constituent volume ratio V_1/V_2 for permittivity ratio $\epsilon_2/\epsilon_1 = 10$.

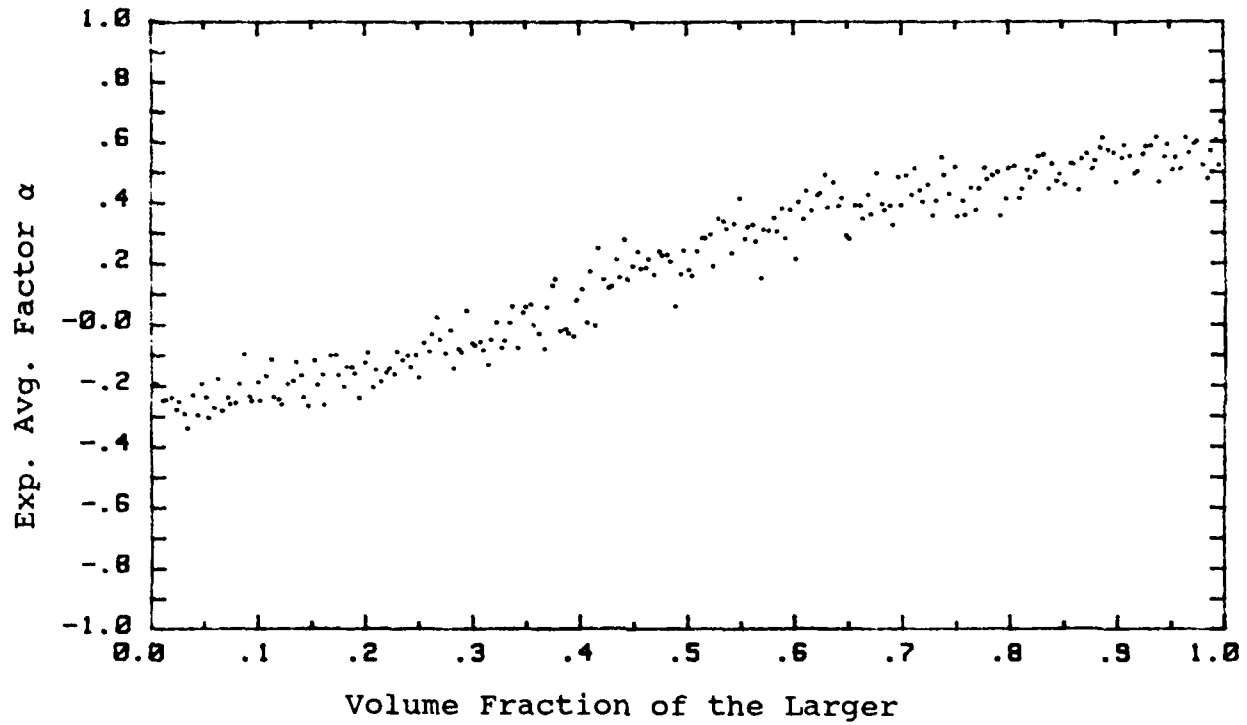


Figure 11. Exponential averaging factor α as a function of constituent volume ratio V_1/V_2 for permittivity ratio $\epsilon_2/\epsilon_1 = 100$.

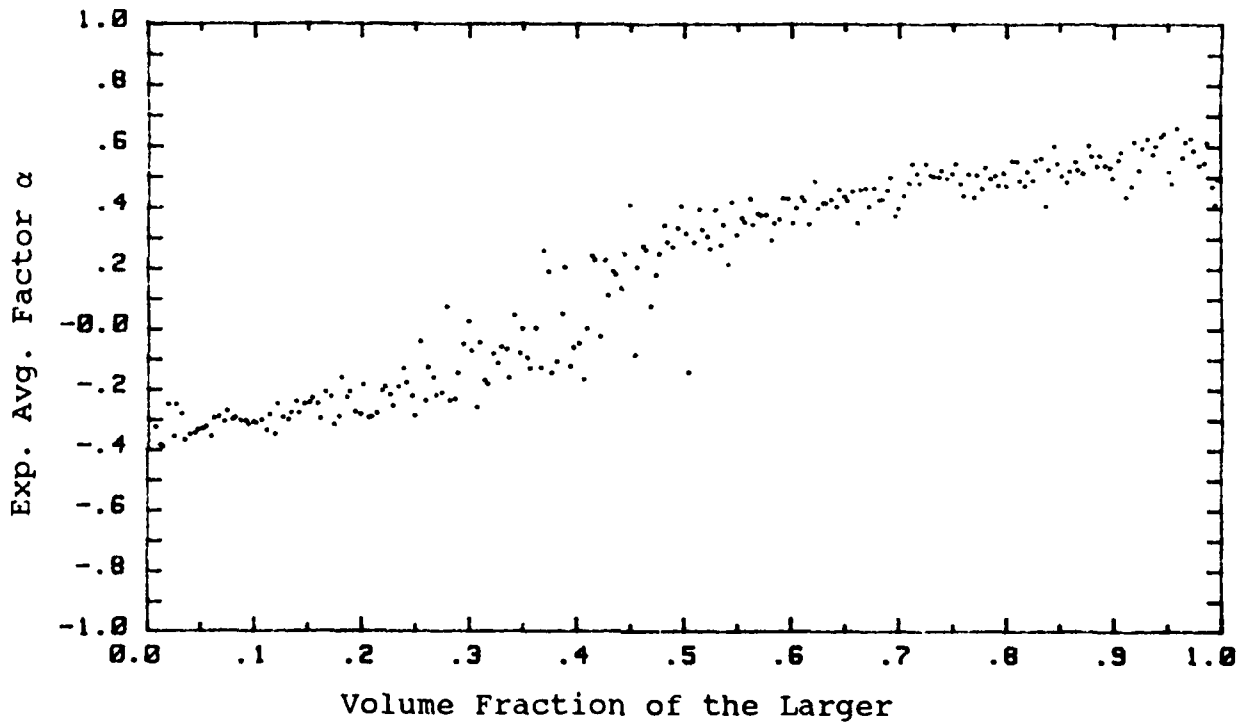


Figure 12. Exponential averaging factor α as a function of constituent volume ratio V_1/V_2 for permittivity ratio $\epsilon_2/\epsilon_1 = 1000$.

a) $\epsilon_1/\epsilon_2 \approx 1$ - the exponential averaging factor α is essentially constant and of value ≈ 0.25 .

b) $2 \leq \epsilon_1/\epsilon_2 \leq 100$ - α is approximately linearly dependent on the constituent volume ratio.

c) $\epsilon_1/\epsilon_2 > 100$ - α exhibits a nonlinear constituent volume ratio dependence arising from percolation effects.

Several more cases will need to be examined to determine more accurately the limits of these behavioral categories.

FUTURE WORK

The identification of the exponential averaging factor α as falling into behavioral categories dependent upon the constituent permittivity ratio is of considerable engineering significance. Once the behavioral boundaries are established, it will be possible to develop simple expressions approximating α for the various behavioral categories. Future work in this area should thus include:

a) Evaluation of a sufficient number of test cases to determine the limits of the behavioral categories.

b) Development of engineering tables and approximations for practical determination of α in engineering applications.

c) Extension to the case of complex permittivity, including artificial dielectrics such as dielectric-metal composites.

d) Extension to 3-dimensional sample geometries.

e) Analysis of the nature of percolation effects observed for large constituent permittivity ratios, in particular, analysis of the effects of constituent grain size.

f) Analysis of composites with three or more components.

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[3] S. Wallin, "Dielectric Properties of Heterogeneous Media," Doctoral Dissertation, Department of Physics and Astronomy, University of Wyoming, Laramie, Wyoming, 1985, 148 pp.

Appendix I

Two-Dimensional Numeric Analysis Program

```

10  ! < < < < < < < "DIEL_LR62D" > > > > > > > >
20  ! * - * - * - * - * - * - * - * - * - * - * - * - * - * - * - *
30  ! A main program to evaluate a 2 dimensional composite dielectric
40  ! response for a pixel network of capacitors.
50  !
60  ! * - * - * - * - * - * - * - * - * - * - * - * - * - * - * - *
70  PRINT " MEMORY IS";VAL(SYSTEM$( "AVAILABLE MEMORY" ))/8;"(reals)"
80  OPTION BASE 1
90  DATA 1,2,4,7,11,16,22,29,37          ! Dielectric data for option
100 COM /Pass/ Relay                     ! for sharing to subs
110 COM /Pixel/ Chdr$(80),Dhdr$(80),INTEGER Lxtnt,Pixel(1:180,1:180)
120 DIM Hpiv(1:202),Hpr(1:20302)        ! dim to reasonable size
130 DIM Hdr$(80)                         ! available string for headers
140 DIM Admt(0:3),Admsav(0:3)           ! neighbor admittance values
150 INTEGER Xt(0:3),Yt(0:3)             ! neighbor addresses
160 COM /Memr/ Graf(1:256,1:4),Ahdr$(80),Bhdr$(80),INTEGER Rep,Kwd !trials mem
170 !***> COM areas can be reaccessed with next RUN if identical name & sizes
180 !***> nb., max Lside >= .5 + sqrt(.25 + 2*(max dim - 1) )
190 LET Start=TIMEDATE
200 INTEGER Lside,Kond,Nodesz
210 INTEGER Ptrn,Nd,Nd1,Nd2,Xkin,Ykin,Xcnt,Ycnt,Xaddr,Yaddr,Boxes,Slant,Sprss
220 INTEGER Qdrnt,Rptr,Trans,Pose,Grpt,Tls,Sctr,Itmp,Occp
230 INTEGER Hzmax,Hxymax,Hpremax,Hopped,Hsteps,Hnd,Hcnt,Zcnt,Znd
240 INTEGER Cnmb,Qmat,Hnd1,Hnd2,Hleft,Hright
250 DIM Diel(1:9),Frpx(0:9),Msd$(60)
260 DIM Fln$(60)
270 !DIM Hpiv(1:128),Hpr(1:8192) ! set to max physical storage
280 LET Grpt=1                            ! Initialize the data storage counter
290 ! * - * - * - * - * - * - * - * - * - * - * - * - * - * - * - *
300 ! for which the integer variables roles are:
310 ! Relay = an available common pass variable
320 ! Lside = the # of pixel capacitor elements encounter along an edge
330 !         of the square of pixels
340 ! Tls = Lside or Lside/2 if 2x2 tiling
350 ! Qdrnt = quadrant pixel array expanding switch, 0=off & 1=on
360 ! Px_tot = total # of pixels in square = Lside*Lside
370 ! Kond = the boundary condition on the sides of the overall composite
380 !         capacitor, 1) insulating sides or 2) periodic or sides which
390 !         wrap around
400 ! Nodesz = the maximum number of interaction nodes in forming
410 !         network, with 0 as the ground or base plate, 1 as center
420 !         node, and the final node number for the top plate.
430 !         Its value is: L*L/2-L+2 + (IF Periodic=1)*(L/2-1).
440 !

```

```

450 |          OVERALL CAPACITOR FROM NODES
460 |          |
470 |          |
480 |          |----- top node or plate
490 |          | X X X X X X X X X X
500 |          |   X X X X X X X X X X
510 |          | X X X X X X X X X X
520 |          |   X X X X X X X X X X
530 |          | X X X X X X X X X X center node at midpoint
540 |          |   X X X X X X X X X X
550 |          | X X X X X X X X X X
560 |          |   X X X X X X X X X X
570 |          | X X X X X X X X X X
580 |          |----- base node or plate
590 |          |
600 |          |-----
610 |          |
620 |          |
630 |          |
640 |          |
650 |          |
660 |          |
670 |          |
680 |          |
690 |          |
700 |          |
710 |          |
720 |          |
730 |          |
740 |          |
750 |          |
760 |          |
770 |          |
780 |          |
790 |          |
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810 |          |
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830 |          |
840 |          |
850 |          |
860 |          |
870 |          |
880 |          |
890 |          | * - * - * - * - * - * - * - * - * - * - * - * - * - * - * - *
300 | PRINT
910 | PRINT " > > > Happy capacitor composite adventures in 2 dimensions < < <"
920 | PRINT "           preformed on ";DATE$(TIMEDATE);
930 | PRINT " at ";TIME$(TIMEDATE)
940 | PRINT
950 | | * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
960 | | The hopper reduction subarray:                               S. Wallin, July 1990
970 | | _____ . . . . . > large symmetric sparse matrix .
980 | | 1,1|

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1530 INPUT "Quad fold symmetry expansion of pixel grid? 0) No 1) Yes",Qdrnt
1540 IF Qdrnt<0 THEN STOP
1550 LET Qdrnt=1+(Qdrnt=1)
1560 SELECT Ptrn
1570 CASE =0
1580   IF Lxtnt<2 THEN
1590     PRINT " Are Pixels there in memory? ..idled ..start again"
1600     STOP
1610   END IF
1620   IF Lxtnt>181 THEN PRINT " .. there may be too many Pixels"
1630   REDIM Pix1(1:Lxtnt,1:Lxtnt)
1640   LET Lside=Lxtnt*Qdrnt*Tls
1650   PRINT " From internal memory via COM, Pixels";Lxtnt;"x";Lxtnt;"", title,"
1660   IF Chdr$<>" THEN PRINT Chdr$
1670   IF Dhdr$<>" THEN PRINT Dhdr$
1680   CASE =1
1690     INPUT " Enclose (in ""s) file name to contain pixel pattern?",Fln$
1700     IF Fln$="" THEN STOP
1710     IF POS(Fln$,":")=0 THEN Fln$=Fln$&Msd$
1720     DISP " File named """;Fln$;"" ([";LEN(Fln$);"] characters)";
1730     DISP " is being read from storage"
1740     ASSIGN @Pixsrc TO Fln$,FORMAT OFF
1750     ENTER @Pixsrc;Chdr$,Dhdr$;Lxtnt ! NB header assigned length of 80
1760     PRINT " Pixels contained in file """;Fln$;"" , entitled with"
1770     PRINT Chdr$
1780     PRINT Dhdr$
1790     REDIM Pix1(1:Lxtnt,1:Lxtnt) ! read initial Pix1(*) array
1800     ENTER @Pixsrc;Pix1(*) ! retrieve pixels from file
1810     ASSIGN @Pixsrc TO * ! close file
1820     LET Lside=Lxtnt*Qdrnt*Tls ! actual Pixel side anticipated
1830     PRINT
1840   CASE ELSE ! Generate pixels
1850     DISP "How big a capacitor pixel grid in elements/side? ";
1860     INPUT "(even %, max ~180 int addr lmt)",Lside
1870     IF Lside<0 THEN STOP
1880     IF Lside<>SHIFT(SHIFT(Lside,1),-1) THEN
1890       PRINT " Odd";Lside;"Pixel length changed to even";
1900       LET Lside=SHIFT(SHIFT(Lside,1),-1)
1910       PRINT Lside
1920     END IF
1930     IF Lside=0 THEN Lside=2
1940     LET Lxtnt=Lside ! initial Pixel side length
1950     LET Lside=Lside*Qdrnt*Tls ! Pixel side length anticipated
1960     IF Lside>182 THEN PRINT " ... near integer addressing limit"
1970   END SELECT ! end Ptrn test
1980   PRINT
1990   IF Tls=2 OR Qdrnt=2 THEN PRINT " Pixels now measures";Lside;"x";Lside
2000   PRINT " Pattern=";Ptrn;"";Lside;"x";Lside;
2010   IF Tls=1 THEN PRINT "pixels,";
2020   IF Tls=2 THEN PRINT "tiled pixels,";
2030   IF Kond=1 THEN PRINT " insulated on ""D"" field parallel to edge."
2040   IF Kond=2 THEN PRINT " periodic or voltage wrapping around at edges."
2050   LET Nodesz=SHIFT(Lside*Lside,1)-Lside+2+(Kond=2)*(SHIFT(Lside,1)-1)
2060   ALLOCATE REAL Dspic(Lside,Lside),Potnt(Lside,Lside) ! to be programmed

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2070 !***> Initializing
2080 MAT Diel= (0)
2090 DISP "Dielectric sources? ";
2100 DISP "1) data input(programmed) 2) keyboard ";
2110 INPUT "3) by progression",Nd
2120 IF Nd=0 THEN Nd=2
2130 SELECT Nd
2140 CASE =1
2150     FOR Nd1=1 TO 9
2160         READ Diel(Nd1)
2170     NEXT Nd1
2180 CASE =2
2190     FOR Nd1=1 TO 9
2200         DISP "Give dielectric value at";Nd1;
2210         INPUT "? (or enter negative if to cease)",Diel(Nd1)
2220         IF Diel(Nd1)<0 THEN
2230             LET Diel(Nd1)=0
2240             LET Nd1=9
2250         ELSE
2260             PRINT "diel[";Nd1;"]=";PROUND(Diel(Nd1),-4);";";
2270         END IF
2280     NEXT Nd1
2290 CASE =3
2300     INPUT "Dielectric value of pixel type ""[1]"?",Tmp
2310     DISP "Multiplier of progression for each succeeding value ";
2320     INPUT "to fill {2},{3},...,{9} ?",Tmp1
2330     FOR Nd1=1 TO 9
2340         Diel(Nd1)=Tmp
2350         Tmp=Tmp*Tmp1
2360         PRINT "diel[";Nd1;"]=";PROUND(Diel(Nd1),-4);";";
2370     NEXT Nd1
2380 CASE ELSE
2390     STOP
2400 END SELECT
2410 PRINT
2420 LET Sprss=1
2430 IF Nodesz<32 THEN
2440     INPUT "Surpress screen listing details, 0) No 1) Yes?",Sprss
2450     IF Sprss<0 THEN STOP
2460 END IF
2470 INPUT "Any overall repeats?",Rep
2480 IF Rep<0 THEN STOP
2490 IF Rep=0 THEN LET Rep=1
2500 INPUT "Desire transpose of pixel grid? 0) No 1) Yes",Pose
2510 IF Pose<0 THEN STOP
2520 LET Pose=1+BIT(Pose,0)
2530 REM " Solution acheived by a sparse matrix reduced pivoting technique"
2540 !***>> Overall repetition, may require additional editing
2550 LET Kwd=4 ! user has selected to program for 4 data columns
2560 REDIM Graf(1:Rep,1:Kwd)
2570 FOR Rptr=1 TO Rep
2580     LET Relay=Rptr 17/27/90
2590     MAT Frpx= (0)
2600     !**> if Ptrn=0 internal or Ptrn=1 then Pixels read from file

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2610 IF Ptrn=2 THEN CALL Pixl2d_fill
2620 IF Ptrn=3 THEN CALL Pixl2d_rand
2630 IF Ptrn=4 THEN CALL Pixl2d_tilt
2640 IF Ptrn=5 THEN CALL Pixl2d_ellps
2650 IF Ptrn=6 THEN CALL Pixl2d_strat
2660 IF Ptrn=7 THEN CALL Pixl2d_cbox
2670 IF Ptrn=8 THEN CALL Pixl2d_ellp2
2680 IF Tls=2 THEN
2690   LET Xkin=SIZE(Pixl,1)           ! redimensioning
2700   LET Ykin=SIZE(Pixl,2)
2710   LET Nd1=Xkin+Ykin
2720   LET Nd2=SHIFT(Xkin*Ykin,-2)   ! 4*Xkin*Ykin
2730   REDIM Pixl(1:1,1:Nd2)
2740   FOR Xcnt=(Xkin-1) TO 0 STEP -1
2750     FOR Ycnt=Ykin TO 1 STEP -1
2760       LET Pixl(1,Xcnt*2*Ykin+Ycnt)=Pixl(1,Xcnt*Ykin+Ycnt)
2770     NEXT Ycnt
2780   NEXT Xcnt
2790   REDIM Pixl(1:Nd1,1:Nd1)       ! set new array dimen
2800   FOR Xcnt=Xkin TO 1 STEP -1     ! tiling 2x2
2810     FOR Ycnt=Ykin TO 1 STEP -1
2820       LET Itmp=Pixl(Xcnt,Ycnt)
2830       LET Xaddr=SHIFT(Xcnt,-1)  ! effective 2* op
2840       LET Yaddr=SHIFT(Ycnt,-1)
2850       LET Pixl(Xaddr,Yaddr)=Itmp
2860       LET Pixl(Xaddr-1,Yaddr)=Itmp
2870       LET Pixl(Xaddr,Yaddr-1)=Itmp
2880       LET Pixl(Xaddr-1,Yaddr-1)=Itmp
2890     NEXT Ycnt
2900   NEXT Xcnt
2910 END IF
2920 IF Qdrnt=2 THEN
2930   LET Nd2=SIZE(Pixl,1)+SIZE(Pixl,2)
2940   LET Nd1=SHIFT(Nd2,1)
2950   REDIM Pixl(1:Nd2,1:Nd2)       ! redim to dble quad duplic
2960   FOR Xcnt=Nd1 TO 1 STEP -1
2970     LET Xaddr=Nd2+1-Xcnt         ! quad complement X counter
2980     LET Xkin=SHIFT(Xcnt+1,1)    ! effectively DIV 2 op
2990     LET Ykin=BIT(Xcnt+1,0)      ! effectively odd<=>even op
3000     FOR Ycnt=1 TO Nd1
3010       LET Yaddr=Nd2+1-Ycnt      ! quad complement Y counter
3020       LET Itmp=Pixl(Xkin,Ycnt+Nd1*Ykin)
3030       LET Pixl(Xcnt,Ycnt)=Itmp  ! Itmp takes care of redim elements
3040       LET Pixl(Xaddr,Ycnt)=Itmp
3050       LET Pixl(Xcnt,Yaddr)=Itmp
3060       LET Pixl(Xaddr,Yaddr)=Itmp
3070     NEXT Ycnt
3080   NEXT Xcnt
3090 END IF
3100 LET Lside=SIZE(Pixl,1)          ! update Pixl extent along edge
3110 LET Px_tot=Lside*Lside
3120 LET Boxes=SHIFT(Lside,1)
3130 IF Boxes<1 THEN PRINT "WARNING! may be too small of a pixel grid"
3140 LET Nodesz=SHIFT(Lside*Lside,1)-Lside+2+(Kond=2)*(SHIFT(Lside,1)-1)

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3150      !***> Tranpose of Pixel grid
3160      LET Trans=Pose ! if loop then use next line
3170      !FOR Trans=1 TO Pose
3180      IF Trans=2 THEN          ! Tranpose
3190          PRINT " TRANSPOSING"
3200          FOR Xcnt=1 TO Lside
3210              FOR Ycnt=(Xcnt+1) TO Lside
3220                  LET Itmp=Pixl(Ycnt,Xcnt)      ! swap Xcoordinate<->Ycoordinate
3230                  LET Pixl(Ycnt,Xcnt)=Pixl(Xcnt,Ycnt)
3240                  LET Pixl(Xcnt,Ycnt)=Itmp
3250              NEXT Ycnt
3260          NEXT Xcnt
3270      END IF
3280      !***> Evaluation of pixel type volume fractions
3290      IF NOT (Sprss) OR Lside<81 THEN PRINT "  Pixels";Lside;"x";Lside
3300      FOR Xcnt=Lside TO 1 STEP -1
3310          FOR Ycnt=1 TO Lside
3320              Frpx(Pixl(Xcnt,Ycnt))=Frpx(Pixl(Xcnt,Ycnt))+1
3330              IF NOT (Sprss) OR Lside<40 THEN PRINT " ";VAL$(Pixl(Xcnt,Ycnt));
3340          NEXT Ycnt
3350          IF NOT (Sprss) OR Lside<40 THEN PRINT
3360      NEXT Xcnt
3370      MAT Frpx= Frpx/(Px_tot)
3380      PRINT " Volume %s: ";
3390      FOR Nd=1 TO 9
3400          IF Frpx(Nd)<>0 THEN PRINT PROUND(100*Frpx(Nd),-1);"%=>[";Nd;"],";
3410      NEXT Nd
3420      PRINT
3430      IF Frpx(0)<>0 THEN PRINT "WARNING! check pixels"
3440      DISP " .. wait";Rptr;"of";Rep;".. solving node interact matrix,";
3450      DISP Nodes;"by";Nodesz;"from time ";TIME$(TIMEDATE)
3460      LET Tmp=TIMEDATE          ! Benchmarker
3470      !***> HOP technique of sparse matrix reduction
3480      PRINT " Solving INTERACTION matrix";Nodesz;"x";Nodesz;"via hopper"
3490      LET Hxymax=Lside          ! size of Hopper for matrix reduction
3500      LET Hzmax=(1.0+Hxymax)*Hxymax DIV 2      ! memory reduction capabilities
3510      LET Hsteps=Nodesz
3520      LET Hpremax=Hzmax-Hxymax
3530      REDIM Hpiv(1:Hxymax),Hpr(1:Hzmax)
3540      LET Hleft=1              ! markers of node #s on left insl BC
3550      LET Hright=Boxes        ! markers of node #s on right insl BC
3560      MAT Hpiv= (0)
3570      MAT Hpr= (0)
3580      LET Znd=0                ! to previous row tri-diag accum
3590      FOR Hnd=1 TO Hxymax      ! Filling hopper work array
3600          IF NOT (Sprss) THEN PRINT " node's ";VAL$(Hnd);" neighbors are";
3610          FOR Sctr=0 TO 3      ! Diagonal or self interact terms
3620              IF Kond=1 THEN CALL Cvndi(Hnd,Lside,Sctr,Xt(Sctr),Yt(Sctr))
3630              IF Kond=2 THEN CALL Cvndp(Hnd,Lside,Sctr,Xt(Sctr),Yt(Sctr))
3640              LET Admt(Sctr)=Diel(Pixl(Xt(Sctr),Yt(Sctr)))
3650              IF Kond=1 THEN          ! adj for insl BC on Pixel grid
3660                  IF Hnd=Hleft THEN      ! test if left side node
3670                      IF NOT (BIT(Sctr,0)) THEN
3680                          IF BIT(Sctr,1) THEN      ! make series admit combo

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3690         IF Xt(2)<Lside THEN
3700             LET Admsav(0)=Diel(Pixl(Xt(2)+1,1))
3710             LET Admt(2)=Admt(2)*Admsav(0)/(Admt(2)+Admsav(0))
3720             LET Admsav(2)=Admt(2) ! save for later use
3730         END IF
3740         ELSE ! reuse former upper admit combo
3750             IF Hnd>1 THEN LET Admt(0)=Admsav(2) ! pass by on 1st node
3760             END IF ! end of Sctr=0,2 test
3770         END IF ! end of insl BC Pixel test
3780     END IF ! end of Hnd=Hleft test
3790     IF Hnd=Hright THEN ! test if right side node
3800         IF BIT(Sctr,0) THEN
3810             IF BIT(Sctr,1)=1 THEN ! make series admit combo
3820                 IF Xt(3)<Lside THEN
3830                     LET Admsav(1)=Diel(Pixl(Xt(3)+1,Lside)) ! cmbn above ngrbr
3840                     LET Admt(3)=Admt(3)*Admsav(1)/(Admt(3)+Admsav(1))
3850                     LET Admsav(3)=Admt(3) ! save for later use
3860                 END IF
3870                 ELSE ! reuse former admit combo
3880                     IF Hnd>Boxes THEN LET Admt(1)=Admsav(3) ! Skip 1st pass
3890                     END IF ! end of Sctr=0 test
3900                 END IF ! end of insl BC Pixel test
3910             END IF ! end of Hnd=Hright test
3920         END IF ! end if for Kond=1 test
3930         LET Hpr(Znd+Hnd)=Hpr(Znd+Hnd)+Admt(Sctr)
3940         IF NOT (Sprss) THEN PRINT " (";VAL$(Xt(Sctr));", ";VAL$(Yt(Sctr));")"
3950     NEXT Sctr
3960     SELECT Kond
3970     CASE =1
3980         LET Hnd1=FNNi(Xt(0),Yt(0),Lside,1)
3990         LET Hnd2=FNNi(Xt(1),Yt(1),Lside,1)
4000     CASE =2
4010         LET Hnd1=FNNp(Xt(0),Yt(0),Lside,1)
4020         LET Hnd2=FNNp(Xt(1),Yt(1),Lside,1)
4030     CASE ELSE
4040         PRINT " out of bounds, boundary condition, in HOPper"
4050     END SELECT
4060     IF NOT (Sprss) THEN PRINT " w/ lower nodes";Hnd1;"&";Hnd2
4070     IF Hnd1<0 OR Hnd2<0 THEN PRINT " Warning node (*) addresses?"
4080     IF Hnd1<Hnd AND Hnd1>0 THEN
4090         LET Hpr(Znd+Hnd1)=Hpr(Znd+Hnd1)-Admt(0)
4100     END IF
4110     IF Hnd2<Hnd AND Hnd2>0 THEN
4120         LET Hpr(Znd+Hnd2)=Hpr(Znd+Hnd2)-Admt(1)
4130     END IF
4140     IF Kond=1 THEN ! increment insl BC left & right node #
4150         IF Hnd=Hleft THEN LET Hleft=Hleft+Lside-1
4160         IF Hnd=Hright THEN LET Hright=Hright+Lside-1
4170     END IF
4180     LET Znd=Znd+Hnd ! loop count accumulator
4190     NEXT Hnd ! end of set up of work matrix
4200     LET Zcnt=0
4210     IF NOT (Sprss) THEN
4220         FOR Xcnt=1 TO Hxymax ! printout HOPper

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4230     FOR Ycnt=1 TO Xcnt
4240         PRINT PROUND(Hpr(Zcnt+Ycnt),-3),
4250     NEXT Ycnt
4260     PRINT
4270     LET Zcnt=Zcnt-Xcnt
4280     NEXT Xcnt
4290 END IF
4300 FOR Hopped=1 TO Hsteps-1           | Let the pivoting begin, & drip dry
4310     LET Hnd=Hxymax+Hopped           | count of oncoming node number
4320     LET Hpiv(1)=1                   | normalize to 1st element pivot vectr
4330     LET Hnrm=1/Hpr(1)               | normalizing multiplier
4340     LET Zcnt=2                       | convert array storage for 1st colmn
4350     FOR Hcnt=2 TO Hxymax             | set pivot vector
4360         LET Hpiv(Hcnt)=Hpr(Zcnt)*Hnrm
4370         LET Zcnt=Zcnt+Hcnt
4380     NEXT Hcnt
4390     !***> one can output pivot here for backsub later
4400     IF NOT (Sprss) THEN
4410         PRINT " At reduction";Hopped;"the pivots are:"
4420         FOR Hcnt=Hxymax TO 1 STEP -1
4430             PRINT PROUND(Hpiv(Hcnt),-4);
4440         NEXT Hcnt
4450         PRINT
4460     END IF
4470     LET Zcnt=1                       | initialize filling counter
4480     FOR Xcnt=2 TO Hxymax               | heart of pivoting
4490         IF Hpiv(Xcnt)<>0 THEN           | sparseness efficiency =0, no-op
4500             FOR Ycnt=2 TO Xcnt         | adj each array row with pivot vectr
4510                 IF Hpiv(Ycnt)<>0 THEN | sparseness efficiency =0, no-op
4520                     LET Hpr(Zcnt+Ycnt)=Hpr(Zcnt+Ycnt)-Hpr(Zcnt+1)*Hpiv(Ycnt)
4530                 END IF
4540             NEXT Ycnt
4550         END IF
4560         LET Zcnt=Zcnt+Xcnt
4570     NEXT Xcnt
4580     LET Zcnt=0                       | initialize filling counter lower
4590     FOR Xcnt=1 TO Hxymax-1
4600         FOR Ycnt=1 TO Xcnt             | hopping along for shake up
4610             LET Hpr(Zcnt+Ycnt)=Hpr(Zcnt+Ycnt+1+Xcnt)
4620         NEXT Ycnt
4630         LET Zcnt=Zcnt+Xcnt
4640     NEXT Xcnt
4650     FOR Ycnt=1 TO Hxymax               | feed hopper, clear last row
4660         LET Hpr(Hpremax+Ycnt)=0
4670     NEXT Ycnt
4680     SELECT Hnd
4690     CASE <Hsteps                       | feed unless over lg array extent
4700         IF NOT (Sprss) THEN PRINT " node's ";VAL$(Hnd);" neighbors are";
4710         FOR Sctr=0 TO 3                 | with diagonal or self interact terms
4720             IF Kond=1 THEN CALL Cvndi(Hnd,Lside,Sctr,Xt(Sctr),Yt(Sctr))
4730             IF Kond=2 THEN CALL Cvndp(Hnd,Lside,Sctr,Xt(Sctr),Yt(Sctr))
4740             LET Admt(Sctr)=Diel(Pixl(Xt(Sctr),Yt(Sctr)))
4750             IF Kond=1 THEN               | adj for insl BC on Pixel grid
4760                 IF Hnd=Hleft THEN       | test if left side node

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4770         IF NOT (BIT(Sctr,0)) THEN
4780             IF BIT(Sctr,1) THEN ! make series admit combo
4790                 IF Xt(2)<Lside THEN
4800                     LET Admsav(0)=Diel(Pix1(Xt(2)+1,1))
4810                     LET Admt(2)=Admt(2)*Admsav(0)/(Admt(2)+Admsav(0))
4820                     LET Admsav(2)=Admt(2)! save for later use
4830                 END IF
4840             ELSE ! reuse former upper admit combo
4850                 IF Hnd>1 THEN LET Admt(0)=Admsav(2)! pass by on 1st node
4860                 END IF ! end of Sctr=0,2 test
4870             END IF ! end of ins1 BC Pixel test
4880         END IF ! end of Hnd=Hleft test
4890         IF Hnd=Hright THEN ! test if right side node
4900             IF BIT(Sctr,0) THEN
4910                 IF BIT(Sctr,1)=1 THEN ! make series admit combo
4920                     IF Xt(3)<Lside THEN
4930                         LET Admsav(1)=Diel(Pix1(Xt(3)+1,Lside))! cmbn above ngr
4940                         LET Admt(3)=Admt(3)*Admsav(1)/(Admt(3)+Admsav(1))
4950                         LET Admsav(3)=Admt(3)! save for later use
4960                     END IF
4970                 ELSE ! reuse former admit combo
4980                     IF Hnd>Boxes THEN LET Admt(1)=Admsav(3)! Skip 1st pass
4990                     END IF ! end of Sctr=0 test
5000                 END IF ! end of ins1 BC Pixel test
5010             END IF ! end of Hnd=Hright test
5020         END IF ! end if for Kond=1 test
5030         LET Hpr(Hzmax)=Hpr(Hzmax)+Admt(Sctr)
5040         IF NOT (Sprss) THEN PRINT " (";VAL$(Xt(Sctr));",";VAL$(Yt(Sctr));"
5050     NEXT Sctr
5060     SELECT Kond ! with off diagonal terms
5070     CASE =1
5080         LET Hnd1=FNNi(Xt(0),Yt(0),Lside,1)
5090         LET Hnd2=FNNi(Xt(1),Yt(1),Lside,1)
5100     CASE =2
5110         LET Hnd1=FNNp(Xt(0),Yt(0),Lside,1)
5120         LET Hnd2=FNNp(Xt(1),Yt(1),Lside,1)
5130     END SELECT ! to SELECT Kond
5140     IF NOT (Sprss) THEN PRINT " w/ lower nodes";Hnd1;"&";Hnd2
5150     IF Hnd1<0 OR Hnd2<0 THEN PRINT " Warning node <=> addresses?"
5160     IF Hnd1<Hnd AND Hnd1>0 THEN
5170         LET Hnd1=Hnd1+Hzmax-Hnd
5180         LET Hpr(Hnd1)=Hpr(Hnd1)-Admt(0)
5190     END IF
5200     IF Hnd2<Hnd AND Hnd2>0 THEN
5210         LET Hnd2=Hnd2+Hzmax-Hnd
5220         LET Hpr(Hnd2)=Hpr(Hnd2)-Admt(1)
5230     END IF
5240     CASE =Hsteps ! top node is contact node
5250     FOR Ycnt=1 TO Lside ! diagonal
5260         Hpr(Hzmax)=Hpr(Hzmax)+Diel(Pix1(Lside,Ycnt))
5270         LET Hnd1=Hzmax-Boxes+SHIFT(Ycnt-1,1) ! off diagonal node #
5280         LET Hpr(Hnd1)=Hpr(Hnd1)-Diel(Pix1(Lside,Ycnt))
5290     NEXT Ycnt
5300     END SELECT ! to SELECT Hnd

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5310 IF NOT (Sprss OR Hnd>Hsteps) THEN
5320   FOR Ycnt=1 TO Hxymax           ! cont printout of HOPper
5330     PRINT PROUND(Hpr(Hpremax+Ycnt),-3),
5340     NEXT Ycnt
5350     PRINT
5360   END IF
5370   IF Kond=1 THEN                 ! increment 1nsl BC left & right node #
5380     IF Hnd=Hleft THEN LET Hleft=Hleft+Lside-1
5390     IF Hnd=Hright THEN LET Hright=Hright+Lside-1
5400   END IF
5410 NEXT Hopped
5420 IF NOT (Sprss) THEN PRINT " Hopper funnels down to";Hpr(1)
5430 !***> Hpr(1) contains the end of the interaction reduction
5440 ! LET Hpiv(Hsteps)=1/Hpr(1)      ! backsubstitute for solution vector
5450 ! FOR Hcnt=(Hsteps-1) TO 1 STEP -1
5460 !   LET Hpiv(Hcnt)=0
5470 !   FOR Zcnt=Hcnt TO Hsteps
5480 !     LET Hpiv(Hcnt)=Hpiv(Hcnt)-Pivotstorg(Hcnt,1+Zcnt-Hcnt)*Hpiv(Zcnt)
5490 !   NEXT Zcnt
5500 ! NEXT Hcnt
5510 PRINT " ... at ";TIME$(TIMEDATE);" inversion excution ";
5520 PRINT "time took";PROUND(TIMEDATE-Tmp,-1);"seconds"
5530 DISP
5540 LET Resp=Hpr(1)                 ! principal diel resp
5550 !***> Pixl displacement field/current & potentials
5560 ! FOR Ycnt=1 TO Lside
5570 !   FOR Xcnt=1 TO Lside
5580 !     Slant=(Xcnt+Ycnt) MOD 2
5590 !     Xaddr=Xcnt-Boxes-Slant      ! (x,y) of node upper to pixel
5600 !     Yaddr=Ycnt-Boxes
5610 !     CALL Xy_to_node(Nd1,Xaddr,Yaddr,Lside,Kond)
5620 !     Xaddr=Xcnt-Boxes+Slant-1    ! (x,y) of node lower to pixel
5630 !     Yaddr=Ycnt-Boxes-1
5640 !     CALL Xy_to_node(Nd2,Xaddr,Yaddr,Lside,Kond)
5650 !     IF Nd1<>Nd2 AND Nd1>0 AND Nd2>0 THEN
5660 !       Dsplc(Xcnt,Ycnt)=Diel(Pixl(Xcnt,Ycnt))*(Hpiv(Nd1)-Hpiv(Nd2))
5670 !       Potnt(Xcnt,Ycnt)=(Hpiv(Nd1)+Hpiv(Nd2))/2
5680 !     END IF
5690 !     IF Nd2=0 AND Nd1>0 THEN
5700 !       Dsplc(Xcnt,Ycnt)=Diel(Pixl(Xcnt,Ycnt))*Hpiv(Nd1)
5710 !       Potnt(Xcnt,Ycnt)=Hpiv(Nd1)/2
5720 !     END IF
5730 !   NEXT Xcnt
5740 ! NEXT Ycnt
5750 !***> additional modification of Potential & Displacement array fields
5760 ! IF Kond=1 THEN
5770 !   FOR Ycnt=2 TO (Lside-2) STEP 2
5780 !     FOR Nd=-1 TO 1 STEP 2
5790 !       LET Xcnt=(Nd+1)*Boxes+(Nd=-1) ! (Xcnt,Ycnt) refer to pixel
5800 !       LET Xaddr=Nd*(Boxes-1)        ! (Xaddr,Yaddr) refer to node
5810 !       LET Yaddr=Ycnt-Boxes
5820 !       CALL Xy_to_node(Nd1,Xaddr,Yaddr+1,Lside,Kond)! node # upper
5830 !       CALL Xy_to_node(Nd2,Xaddr,Yaddr-1,Lside,Kond)! node # lower
5840 !       IF Nd1<>Nd2 AND Nd1>0 AND Nd2>0 THEN ! Evaluate along side nodes

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5850      LET Tmp1=Diel(Pix1(Xcnt,Ycnt+1))! Upper dielectric pixel
5860      LET Tmp2=Diel(Pix1(Xcnt,Ycnt))! Lower dielectric pixel
5870      LET Vt1=Hpiv(Nd1)
5880      LET Vt2=Hpiv(Nd2)
5890      IF Tmp1<>0 AND Tmp2<>0 THEN Tmp=(Vt1*Tmp1+Vt2*Tmp2)/(Tmp1+Tmp2)
5900      LET Potnt(Xcnt,Ycnt+1)=(Vt1+Tmp)/2! Pix1 volts
5910      LET Potnt(Xcnt,Ycnt)=(Vt2+Tmp)/2
5920      IF Tmp1<>0 AND Tmp2<>0 THEN
5930          LET Dsp1c(Xcnt,Ycnt+1)=(Vt1-Vt2)/(1/Tmp1+1/Tmp2)
5940      END IF
5950      LET Dsp1c(Xcnt,Ycnt)=Dsp1c(Xcnt,Ycnt+1)! Displacement mag.
5960      END IF
5970      NEXT Nd
5980      NEXT Ycnt
5990      END IF
6000      MAT Potnt= Potnt*(Resp)      ! Normalizing to 1 volt across sample
6010      MAT Dsp1c= Dsp1c*(Resp)      ! & sum of displacements along row=diel
6020      LET Nd1=1                    ! sign provider for following loop
6030      FOR Xcnt=1 TO Lside
6040          LET Resp2=Resp2+Nd1*(Dsp1c(Xcnt,Boxes)-Dsp1c(Xcnt,Boxes+1))
6050          LET Nd1=-Nd1
6060      NEXT Xcnt
6070      LET Resp2=Resp2/2            ! dielectric response perp to E
6080      !***> Should be end of calculations, printouts follow
6090      !***> Printout of the dielectric pixel array
6100      IF NOT (Sprss) AND Lside<13 THEN
6110          PRINT "DIELECTRIC PIXEL ARRAY, 2-dimensional,";Lside;"by";Lside
6120          FOR Xcnt=Lside TO 1 STEP -1
6130              FOR Ycnt=1 TO Lside
6140                  PRINT USING "DDDD.D,#";PROUND(Diel(Pix1(Xcnt,Ycnt)),-1)
6150              NEXT Ycnt
6160          PRINT
6170          NEXT Xcnt
6180      END IF
6190      !***> Printout of the hopper array
6200      !****> Find the series<->parallel factor
6210      LET Tmp1=FNWnr(Diel(*),FrpX(*),Resp,Tmp,9)
6220      PRINT
6230      PRINT "Composite Dielectric Response Tensor Components:"
6240      PRINT " principal=";Resp
6250      PRINT " & series<->parallel factor ="
6260      PRINT PROUND(Tmp1,-3);"(+/-";PROUND(Tmp,-4);"% iteration error)"
6270      PRINT
6280      IF Sprss=0 THEN
6290          PRINT "PIXEL VOLTAGES 2-dimensional,";Lside;"by";Lside
6300          Tmp=FNMatprnt(Potnt(*),-Lside)
6310          PRINT "PIXEL DISPLACEMENT FIELD MAGNITUDES,";Lside;"by";Lside
6320          Tmp=FNMatprnt(Dsp1c(*),-Lside)
6330      END IF
6340      !***> NOTE: Tranpose used then it is an additional cycle to Rptr
6350      Graf(Grpt,1)=Rptr+Tmp/100
6360      Graf(Grpt,2)=FrpX(1)
6370      Graf(Grpt,3)=Resp
6380      Graf(Grpt,4)=Tmp1

```

```

6390     LET Grpt=Grpt+1           ! Increment storage counter
6400     !NEXT Trans
6410     NEXT Rptr
6420     !***> output repeat calculations
6430     LET Bhdr$="( "&VAL$(Lside)&"x"&VAL$(Lside)&")"
6440     IF Tls=1 THEN LET Bhdr$=Bhdr$&" elmnts"
6450     IF Tls=2 THEN LET Bhdr$=Bhdr$&"/(2x2s)"
6460     IF Kond=1 THEN LET Bhdr$=Bhdr$&" InslBC"
6470     IF Kond=2 THEN LET Bhdr$=Bhdr$&" PrdcBC"
6480     LET Bhdr$=Bhdr$&" Sparse"      ! solution by sparse methods
6490     IF Qdrnt=2 THEN LET Bhdr$=Bhdr$&" 4fold"
6500     IF Ptrn=0 THEN Bhdr$=Bhdr$&" intrnl,"
6510     IF Ptrn=1 THEN Bhdr$=Bhdr$&" "&Fln$
6520     IF Ptrn=2 THEN Bhdr$=Bhdr$&" USER,"
6530     IF Ptrn=3 THEN Bhdr$=Bhdr$&" RANDOM,"
6540     IF Ptrn=4 THEN Bhdr$=Bhdr$&" SLANT,"
6550     IF Ptrn=5 THEN Bhdr$=Bhdr$&" ELLIPSE,"
6560     IF Ptrn=6 THEN Bhdr$=Bhdr$&" STRAT,"
6570     IF Ptrn=7 THEN Bhdr$=Bhdr$&" BOXES,"
6580     LET Occp=LEN(Bhdr$)
6590     LET Bhdr$[1+Occp]=RPT$(" ",80-Occp)  ! pad with blanks
6600     LET Bhdr$[60]=" "&DATE$(TIMEDATE)&" "&TIME$(TIMEDATE)
6610     LET Dhdr$=Bhdr$
6620     IF Rep=1 THEN PRINT " for the case abbreviated .."
6630     IF Rep=1 THEN PRINT Bhdr$
6640     IF Rep>1 THEN
6650       PRINT " Summary of";Rep;"repeat variations: (as programmed)"
6660       FOR Rptr=1 TO Rep
6670         PRINT " Case";((Rptr-1) DIV Pose)+1;"",PROUND(Graf(Rptr,1),-3),
6680         PRINT PROUND(Graf(Rptr,2),-3),PROUND(Graf(Rptr,3),-3),
6690         PRINT PROUND(Graf(Rptr,4),-3)
6700       NEXT Rptr
6710       DISP " Save repeat info (array form,";SIZE(Graf,1);"x";SIZE(Graf,2);
6720       INPUT ")? 0) No 1) Definitely",Nd1
6730       IF Nd1=1 THEN
6740         DISP " Enclose (in """"s) new file name to send info vectors to?";
6750         INPUT " (null=use old file)",Fln$
6760         IF POS(Fln$,";")=0 THEN Fln$=Fln$&Msd$
6770         INPUT " Title, (up to 80 characters)",Ahdr$
6780         LET Ahdr$[1+LEN(Ahdr$)]=RPT$(" ",80-LEN(Ahdr$))! pad with blanks
6790         DISP " File named """;Fln$;""" ([";LEN(Fln$);"] characters)";
6800         DISP " to contain repeat info"
6810         PRINT " File """;Fln$;"""'s user and description headers are ";
6820         PRINT "(2 lines):"
6830         PRINT Ahdr$
6840         PRINT Bhdr$
6850         IF Fln$="" THEN
6860           INPUT " Enter the filename to be created? null=stop",Fln$
6870           IF Fln$="" THEN STOP
6880           DISP " Enter file""";Fln$;"""'s storage size limit in bytes ("";
6890           DISP VAL$(256+8*Rep*Pose*Kwd);")";
6900           INPUT "?",Nd1
6910           IF Nd1<1048 THEN Nd1=1048      ! 1 kiloBYTE min
6920           CREATE Fln$,Nd1

```

```

6930     ELSE
6940         IF POS(Fln$,";")=0 THEN Fln$=Fln$&Msd$
6950     END IF
6960     ASSIGN @Infostr TO Fln$;FORMAT OFF
6970     OUTPUT @Infostr;Ahdr$,Bhdr$,Rep,Kwd,Graf(*),END
6980     ASSIGN @Nodstr TO *
6990 END IF
7000 END IF
7010 !***> Pixel file output choice
7020 LET Ndl=0
7030 IF Ptrn<>i THEN INPUT " Save last pixel grid? 0)No 1)Yes",Ndl
7040 IF Ndl=i THEN
7050     DISP " Enclose (in ****s) new file name to send pixel pattern to?";
7060     INPUT " (null=use old file)",Fln$
7070     IF POS(Fln$,";")=0 THEN Fln$=Fln$&Msd$
7080     INPUT " Title (up to 80 characters) if null then default label",Chdr$
7090     LET Dhdr$=Bhdr$
7100     DISP " File named """;Fln$;"" ("";LEN(Fln$);" characters)";
7110     DISP " contains the pixel grid"
7120     PRINT " File """;Fln$;""'s header is "
7130     PRINT Hdr$
7140     IF Fln$<>"" THEN
7150         DISP " Give file""";Fln$;""'s max capacity limit in bytes";
7160         DISP "? ("";VAL$(128+SHIFT(Px_tot,-1));"");
7170         INPUT " ",Ndl
7180         IF Ndl<256 THEN Ndl=256
7190         CREATE Fln$,Ndl
7200     ELSE
7210         INPUT " Enter the existing filename?",Fln$
7220         IF POS(Fln$,";")=0 THEN Fln$=Fln$&Msd$
7230     END IF
7240     ASSIGN @Pixstr TO Fln$;FORMAT OFF
7250     OUTPUT @Pixstr;Hdr$,Lside,Pixl(*),END
7260     ASSIGN @Pixstr TO *
7270 END IF
7280 !***> Interaction file output choice
7290 PRINT RPT$( " ",25);"...elapsed";PROUND(TIMEDATE-Start,-1);
7300 PRINT "sec for completion at ";TIME$(TIMEDATE)
7310 PRINT " MEMORY IS";VAL$(SYSTEM$( "AVAILABLE MEMORY" ))/8;"(reals)"
7320 LET Lxtnt=Lside          ! update COM /Pixel/ ie Pixl(*) size
7330 END
7340 ' || || || || || || || || || || || || || || || || || || || || || ||
7350 DEF FNN1(INTEGER Xn,Yn,Lszn,Lup)
7360 ! Returns the node number for a square Pixel grid network
7370 ! of capacitors for case of insulated sides.
7380 ! (Xn,Yn) 2D coordinates of Pixel leading to the nearest node
7390 ! If Lup=1 then Pixl above node, else Pixl below node
7400 INTEGER Xhf,Ysw,Ndb,Lyr
7410 LET Lup=BIT(Lup,0)
7420 LET Lyr=SHIFT(Lszn,1)          ! in essence divides by 2
7430 IF Xn>0 AND Xn<=Lszn AND Yn>0 AND Yn<=Lszn THEN
7440     LET Ndb=1
7450     IF Xn=1 AND Lup THEN LET Ndb=0
7460     IF Xn=Lszn AND NOT (Lup) THEN LET Ndb=SHIFT(Lszn*Lszn,1)-Lszn+2

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8010 | Hfsz1 = half of Pixel grid size, Lsz1 (then Lsz1 must be even)
8020 INTEGER Lyr1,Sw1,Ovr1,Nodmax1,Hfsz1
8030 IF BIT(Lsz1,0) THEN PRINT " warning, odd Pixel grid extent"
8040 LET Nodmax1=SHIFT(Lsz1*Lsz1,1)-Lsz1+2
8050 LET Hfsz1=SHIFT(Lsz1,1)           ! effectively DIV 2 operation
8060 SELECT Nod1
8070 CASE <1
8080     LET Xout1=0
8090     LET Yout1=0
8100 CASE >=Nodmax1
8110     LET Xout1=Lsz1+1
8120     LET Yout1=Xout1
8130 CASE ELSE
8140     LET Lyr1=i+((Nod1-1) DIV (Lsz1-1))   ! for Bilayer
8150     LET Ovr1=1+((Nod1-1) MOD (Lsz1-1))   ! for # Nodes in Bilayer
8160     LET Sw1=(Ovr1>Hfsz1)                 ! 0=lower 1=upper in Bilayer
8170     IF Sw1 THEN LET Ovr1=Ovr1-Hfsz1     ! adjust for # Nodes in upper
8180     LET Xout1=SHIFT(Lyr1,-1)-1+Sw1+BIT(Scrp,1)
8190     LET Yout1=SHIFT(Ovr1,-1)-1+Sw1+BIT(Scrp,0)
8200 END SELECT
8210 SUBEND
8220 | II II II II II II II II II II II II II II II II II II II II II II II II
8230 SUB Cvndp(INTEGER Nodp,Lszp,Scrp,Xoutp,Youtp)
8240 | Converts a node number of layering scheme into the (x,y)
8250 | coordinates of neighboring nodes
8260 | IN   Nodp = node number
8270 | IN   Lszp = Pixel extent along either X or Y
8280 | IN   Scrp = selection adjacent Pixel neighbor to node
8290 |       (0= X lower,Y lower; 1= X lower,Y higher;
8300 |       2= X higher, Y lower; 3= X higher, Y higher)
8310 | OUT Xoutp = X coordinate address outcome
8320 | OUT Youtp = Y coordinate address outcome
8330 | internal variables:
8340 |   Ovrp = overflow counter
8350 |   Nodmaxp = maximum node for given Pixel grid size, Lszp
8360 |   Hfszp = half of Pixel grid size, Lszp (then Lszp must be even)
8370 INTEGER Ovrp,Nodmaxp,Hfszp
8380 IF BIT(Lszp,0) THEN PRINT " warning, odd Pixel grid extent"
8390 LET Hfszp=SHIFT(Lszp,1)           ! effectively DIV 2 operation
8400 LET Nodmaxp=SHIFT(Lszp*Lszp,1)-Hfszp+1
8410 SELECT Nodp
8420 CASE <1
8430     LET Xoutp=0
8440     LET Youtp=0
8450 CASE >=Nodmaxp
8460     LET Xoutp=Lszp+1
8470     LET Youtp=Xoutp
8480 CASE ELSE
8490     LET Xoutp=1+((Nodp-1) DIV Hfszp)     ! for slab of X
8500     LET Ovrp=1+((Nodp-1) MOD Hfszp)     ! for # Nodes within slab
8510     LET Youtp=SHIFT(Ovrp,-1)+BIT(Scrp,0)-BIT(Xoutp,0)
8520     LET Xoutp=Xoutp+BIT(Scrp,1)
8530     IF Youtp>Lszp THEN Youtp=Youtp-Lszp
8540 END SELECT

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8550 SUBEND
8560 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
8570 DEF FNMatprnt(MatrX(*),INTEGER Ordr)
8580 |***> Printout of an array sized Ordr x Ordr & @ element Spcs wide
8590   CUM /Pass/ Relay
8600   INTEGER Sbcx,Sbcy,Sbcyy,Sbc,Typ
8610   LET Sbc=SGN(Ordr)           ! Reverse printout of rows indicator
8620   LET Psict=0                 ! Psict is the biggest element magnitude
8630   FOR Sbcy=1 TO ABS(Ordr)
8640     FOR Sbcx=1 TO ABS(Ordr)
8650       IF Psict<ABS(MatrX(Sbcx,Sbcx)) THEN LET Psict=ABS(MatrX(Sbcx,Sbcx))
8660     NEXT Sbcx
8670   NEXT Sbcy
8680   IF Psict>0 THEN LET Typ=2-INT(LGT(Psict))
8690   IF Typ=4 OR Typ=5 THEN Typ=3
8700   IF Typ=-1 THEN Typ=0
8710   FOR Sbcy=1 TO ABS(Ordr)
8720     LET Sbcyy=Sbc+Sbcy+(ABS(Ordr)+1)*(1-Sbc)/2
8730     FOR Sbcx=1 TO ABS(Ordr)
8740       SELECT Typ
8750         CASE =0
8760           PRINT USING "00000,*";PROUND(MatrX(Sbcx,Sbcyy),0)
8770         CASE =1
8780           PRINT USING "000.0,*";PROUND(MatrX(Sbcx,Sbcyy),-1)
8790         CASE =2
8800           PRINT USING "00.00,*";PROUND(MatrX(Sbcx,Sbcyy),-2)
8810         CASE =3
8820           PRINT USING "0.000,*";PROUND(MatrX(Sbcx,Sbcyy),-3)
8830         CASE ELSE
8840           LET Typ=SGN(Typ)*99
8850         END SELECT
8860     NEXT Sbcx
8870     IF ABS(Typ)<>99 THEN PRINT
8880   NEXT Sbcy
8890   IF Typ=99 THEN PRINT " . . . array too small to format"
8900   IF Typ=-99 THEN PRINT " . . . array too big to format"
8910   RETURN I
8920 FNEND
8930 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
8940 DEF FNWnr(Diel(*),FrpX(*),Din,Pcterr,INTEGER Nth)
8950 |***> Object of function to find alf satisfying 1=SUM of(vol*diel^alf)
8960 |***> where vol=fractional volumes
8970 |***>       diel=(species permittivity)/(composite permittivity)
8980 |***>       alf= constant exponential between -1 & +1 (series<->parallel)
8990   CUM /Pass/ Relay
9000   INTEGER Spk,Arnd
9010   IF Din=0 OR MAX(FrpX(*))>=1 THEN
9020     LET Alf1=0
9030     LET Pcterr=1.E-99
9040     PRINT " .. series <=> parallel factor at or beyond limits"
9050   ELSE
9060     LET Gsum=0
9070     LET Gdev=0
9080     FOR Sok=1 TO Nth

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9090     LET Gratio=0
9100     IF DieI(Spk)>>0 AND Frpx(Spk)>>0 THEN
9110         LET Gratio=LOG(DieI(Spk)/Din)
9120         LET Gsum=Gsum+Frpx(Spk)*Gratio
9130         LET Gdev=Gdev+Frpx(Spk)*Gratio*Gratio
9140     END IF
9150 NEXT Spk
9160 LET Alf1=-2*Gsum/Gdev
9170 LET Gsum=Gsum+Gdev           ! Initial guess of sum
9180 LET Try=1                    ! Optimize sign in iterations
9190 LET Alf0=0
9200 LET Arnd=1
9210 WHILE ABS(Alf1-Alf0)>>.000000001
9220     LET Gdev=0
9230     LET Gsum=0
9240     FOR Spk=1 TO Nth
9250         LET Gratio=DieI(Spk)/Din     ! relative permittivity to composite
9260         LET Gwk=0                     ! a term @ species to sum
9270         IF Gratio<>0 AND Frpx(Spk)>>0 THEN
9280             LET Gwk=Frpx(Spk)*Gratio*Alf1
9290             LET Gsum=Gsum+Gwk         ! sum function (as described)
9300             LET Gdev=Gdev+LOG(Gratio)*Gwk ! 1st derivative
9310         END IF
9320     NEXT Spk
9330     LET Pcterr=Gsum
9340     LET Gsum=Alf1*(Gsum-1)/Gdev
9350     LET Gdev=Alf1*Alf1-Try*Gsum
9360     IF Gdev<0 THEN Gdev=Gdev+2*Try*Gsum
9370     LET Alf2=SGN(Alf1)*SQR(Gdev)
9380     IF Arnd MOD 2=0 AND ABS(Alf2-Alf1)>>ABS(Alf1-Alf0) THEN Try=-Try
9390     LET Alf0=Alf1                ! bumping iterations
9400     LET Alf1=Alf2
9410     LET Arnd=Arnd+1              ! incrementor
9420 END WHILE
9430 IF Abs(Alf1)<.0000001 THEN
9440     LET Pcterr=100*(Pcterr-1)
9450 ELSE
9460     LET Pcterr=100*(Pcterr*(1/Alf1)-1)
9470 END IF
9480 END IF
9490 RETURN Alf1
9500 FNEND
9510 ! | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
9520 SUB Pix12d_tilt
9530 ! * * * * *
9540 ! This program is for patterning a dielectric bond grid (rectangular
9550 ! type) with a binary mixture. The interface is approximately flat
9560 ! at a tilted angle. (Say like a tilted glass of water)
9570 !
9580 ! +-----+
9590 ! |         |
9600 ! |         |
9610 ! |         |
9620 ! |         |
9620 ! * * * * *

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```

9630 DEG
9640 COM /Pass/ Relay
9650 COM /Pixel/ Chdr$(80),Dhdr$(80),INTEGER Lbonds,Pixel(1:180,1:180)
9660 INTEGER Accum,Opt,Ip,Jp
9670 REDIM Pixel(1:Lbonds,1:Lbonds)
9680 PRINT
9690 PRINT " Makes an bond grid pattern with a binary mixture whose ";
9700 PRINT " interface level sits at a selected volume fraction & tilt."
9710 INPUT "Request the desired volume percentage of the 1st component",Cmp
9720 INPUT "& request the desired tilt angle (in degrees)",Degtilt
9730 PRINT "The requested volume is";Cmp;"% & tilt angle is";Degtilt;"deg"
9740 PRINT "for a square grid of bonds of size";Lbonds;"x";Lbonds;"."
9750 DISP "Decide fate of straddlers ";
9760 INPUT "1) pixel pop/volume demand 2) individual volume sway",Optn
9770 LET Cmp=Cmp/100
9780 LET Pmc=1-Cmp
9790 | * * * * *
9800 | From the information of the two components & the angle of tilt
9810 | then interfacial level can be drawn across the grid window.
9820 | * * * * *
9830 LET Sn=ABS(SIN(Degtilt)) ! Sine
9840 LET Cs=ABS(COS(Degtilt)) ! Cosine
9850 LET Crit=MIN(Sn,Cs)/MAX(Sn,Cs)/2 ! Critical volume transition
9860 Dgmin=MIN(Sn,Cs)/(Sn+Cs) ! A transition on the diagonal
9870 LET Dgsn=Sn/(Sn+Cs) ! Diagonal threshold at Crit vol
9880 LET Dgcs=1-Dgsn ! & its complement
9890 SELECT Cmp ! y-intercept for different cases
9900 CASE <=Crit
9910 LET Cpt=SQR(2*Cmp*Dgsn*Dgcs)
9920 CASE >=(1-Crit)
9930 LET Cpt=1-SQR(2*Pmc*Dgsn*Dgcs)
9940 CASE ELSE
9950 LET Cpt=(Cmp-.5)/(1+2*Crit)+.5
9960 END SELECT ! Done computing diagonal intercept
9970 PRINT "The level has slope";PROUND(Sn/Cs,-2);"& a diag-intercept of";
9980 PRINT PROUND(Cpt,-3);"."
9990 | * * * * *
10000 | The array will be filled according to whether the element
10010 | happens to be on one or the other side of the tilt line.
10020 | If an element is crossed through by the tilt line then
10030 | the element will be assigned to the componet possessing
10040 | the greatest volume deficit as the pixels are filled.
10050 | * * * * *
10060 LET Vbias=0 ! Initialize keep tabs of excess
10070 LET Accum=0 ! Initialize totals counter
10080 FOR Ip=1 TO Lbonds
10090 FOR Jp=1 TO Lbonds
10100 Diag=Jp*Dgsn+Ip*Dgcs-.5 ! Diag intercept @pixel
10110 Dif=Diag-Cpt*Lbonds ! Distance offset on diag
10120 REM PRINT PROUND(Diag,-2);PROUND(Dif,-2); ! Matrix calc out
10130 SELECT Dif
10140 CASE <=-.5
10150 Pixel(Ip,Jp)=1 ! Assign 1st component
10160 CASE >=.5

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10710     ELSE
10720         LET Pxs=INT(Rq*Sqrs*.01+.5)
10730         IF Pxs>Sqrs-Fill+1 THEN LET Pxs=Sqrs-Fill+1
10740     END IF
10750     PRINT " Component [";VAL$(When);"] is assigned";Pxs;"pixels"
10760 END IF
10770 LET Xp=Fill-Frdm
10780 IF Xp>Lpix THEN
10790     LET Xp=Xp-Lpix
10800     LET Yp=Yp+1
10810     LET Frdm=Frdm+Lpix
10820 END IF
10830 IF Pxs>0 THEN LET Pixl(Xp,Yp)=When
10840     Pxs=Pxs-1
10850 NEXT Fill
10860 PRINT
10870 ****> lotto-ing or random mixing
10880 FOR Fill=1 TO Sqrs
10890     LET Frdm=INT(1+RND*Sqrs)
10900     IF Fill<>Frdm AND Frdm<=Sqrs THEN
10910         LET Xp=1+((Fill-1) MOD Lpix)
10920         LET Yp=1+((Fill-1) DIV Lpix)
10930         LET Xq=1+((Frdm-1) MOD Lpix)
10940         LET Yq=1+((Frdm-1) DIV Lpix)
10950         LET Pixtmp=Pixl(Yp,Xp)
10960         LET Pixl(Yp,Xp)=Pixl(Yq,Xq)
10970         LET Pixl(Yq,Xq)=Pixtmp
10980     END IF
10990 NEXT Fill
11000 SUBEND
11010 * 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00
11020 SUB Pixlzd_fill
11030 ****> Subprogram to output a pixel array hand filled by user
11040 COM /Pass/ Relay
11050 COM /Pixel/ Chdr$(80),Dhdr$(80),INTEGER Lpix,Pixl(1:180,1:180)
11060 INTEGER Xpix,Ypix,Fill,Xp,Yp
11070 REDIM Pixl(1:Lpix,1:Lpix)
11080 MAT Pixl= (0)
11090 FOR Xpix=1 TO Lpix
11100     FOR Ypix=1 TO Lpix
11110         CLEAR SCREEN
11120         PRINT
11130         FOR Xp=Lpix TO 1 STEP -1
11140             FOR Yp=1 TO Lpix
11150                 PRINT USING "00,*";Pixl(Xp,Yp)
11160             NEXT Yp
11170             PRINT
11180         NEXT Xp
11190         PRINT
11200         DISP "Filling at (";Xpix;",";Ypix;")";
11210         INPUT " specify species type with integer 1..9",Newpix
11220         LET Newpix=Newpix MOD 10
11230         LET Pixl(Xpix,Ypix)=Newpix
11240     NEXT Ypix

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11250 NEXT Xpix
11260 CLEAR SCREEN
11270 FOR Xp=Lpix TO 1 STEP -1
11280   FOR Yp=1 TO Lpix
11290     PRINT USING "00,>";Pixl(Xp,Yp)
11300   NEXT Yp
11310   PRINT
11320 NEXT Xp
11330 SUBEND
11340 ! [] [] [] [] [] [] [] [] [] [] [] [] [] [] [] [] [] [] [] [] [] []
11350 SUB Pixl2d_ellps
11360 ! > > > Subprogram to fill a pixel window with an ellipse < < <
11370 COM /Pass/ Relay
11380 COM /Pixel/ Chdr$(80),Dhdr$(80),INTEGER Lwndw,Pixl(1:180,1:180)
11390 INTEGER Opt,Xp,Yp
11400 REDIM Pixl(1:Lwndw,1:Lwndw)
11410 PRINT "Choice of filling pixel grid with an ellipse"
11420 DISP "Volume percentage of [1]s to be filled by ellipse";
11430 INPUT " (>.5 then host)",Vlm
11440 LET Vlm=Vlm/100
11450 DISP "Type 1 or 2 to opt for ";
11460 INPUT "1) eccentricity or 2) axis ratio",Opt
11470 DEG
11480 IF Opt=1 THEN
11490   INPUT " Eccentricity?",Ecn
11500   IF ABS(Ecn)>1 THEN PRINT " Too eccentric"
11510   LET Mnjr=SQR(1-Ecn*Ecn)
11520 ELSE
11530   INPUT " Ratio (minor axis)/(major axis)?",Mnjr
11540   IF ABS(Mnjr)>1 THEN Mnjr=1/Mnjr
11550   LET Ecn=SQR(1-Mnjr*Mnjr)
11560 END IF
11570 INPUT " Angle of major axis w.r.t. horizontal in degrees?",Mang
11580 PRINT "The ellipse characteristics are:"
11590 PRINT " eccentricity=";PROUND(Ecn,-4);
11600 PRINT " , axis ratio=";PROUND(Mnjr,-4);" , &"
11610 IF Vlm>.5 THEN LET Vlm=.5-Vlm
11620 LET Major=SQR(ABS(Vlm)/Mnjr/PI)
11630 LET Minor=Mnjr*Major
11640 PRINT " measures a sexy";PROUND(2*Minor,-4);
11650 PRINT "by";PROUND(2*Major,-4);"w.r.t fraction of pixel window."
11660 FOR Xp=1 TO Lwndw
11670   LET Xpos=((Xp-Lwndw DIV 2)-.5)/Lwndw
11680   IF ABS(Xpos)>.5 THEN PRINT " Warning.. touches window edge"
11690   LET Xcs=Xpos*COS(Mang)
11700   LET Xsn=Xpos*SIN(Mang)
11710   FOR Yp=1 TO Lwndw
11720     LET Ypos=((Yp-Lwndw DIV 2)-.5)/Lwndw
11730     IF ABS(Ypos)>.5 THEN PRINT " Warning.. touches window edge"
11740     LET Xpos=Xcs-Ypos*SIN(Mang)
11750     LET Ypos=Ypos*COS(Mang)+Xsn
11760     LET Gfct=(Ypos/Major)^2+(Xpos/Minor)^2
11770     IF Gfct>1 THEN Pixl(Xp,Yp)=2-(1-SGN(Vlm))/2
11780     IF Gfct<=1 THEN Pixl(Xp,Yp)=1+(1-SGN(Vlm))/2

```



```

12870 IF Fix=0 THEN
12880 LET Fix=Past
12890 ELSE
12900 LET Past=Fix
12910 END IF
12920 PRINT " Shell";Shell;"containing";SHIFT(Per1,-SHIFT(Cntr,-1));
12930 PRINT "pixels is assigned component type, [";VAL$(Fix);"]; "from";
12940 IF Cntr THEN PRINT " center."
12950 IF NOT (Cntr) THEN PRINT " corner."
12960 FOR Lcnt=1 TO SHIFT(Shell,-Cntr)
12970 IF Cntr THEN
12980 LET Pix1(Cntrk-Shell+1,Cntrk-Shell+Lcnt)=Fix
12990 LET Pix1(Cntrk+Shell,Cntrk+Shell-Lcnt+1)=Fix
13000 LET Pix1(Cntrk-Shell+Lcnt,Cntrk+Shell)=Fix
13010 LET Pix1(Cntrk+Shell-Lcnt+1,Cntrk-Shell+1)=Fix
13020 ELSE
13030 LET Pix1(Shell,Lcnt)=Fix
13040 LET Pix1(Lcnt,Shell)=Fix
13050 END IF
13060 NEXT Lcnt
13070 NEXT Shell
13080 SUBEND
13090 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
13100 REM A subroutine to make a Pixel grid with an ellipse inclusion
13110 REM imbedded in a host. The ellipse component is always the smaller
13120 REM of the two components and thus is symmetric with respect to the
13130 REM fractional volume filling factor. Since this is limited to only
13140 REM two components then the volume of the 2nd is used as the variable.
13150 COM /Pixel/ Chdr$(80),Dhdr$(80),INTEGER Lxtnt,Pix1(1:180,1:180)
13160 INTEGER Aparm,Abdf,Gde,Pdf,Ptst,Prq,Sqrs,Swup,Swpxs,Xp,Yp

```

Appendix II

Plot Program for Numerical Solutions

```
10  !  &  &  &  &  &  &  &  &  &  &  &  &  &  &  &
20  !  "PLOT_NWK" is a program designed to input dielectric data from
30  !  network simulations and plot it.                      July 1990
40  COM /Memr/ Vctrs(1:505,1:5),Hdra$(80),Hdrb$(80),Sfil$(64),INTEGER Dmx,Dmy
50  INTEGER Kif,Xpt,Ypt,Plt,Xlmn,Ylmn,Rpt,Subj,Mach,Eff,Cpy
60  DIM C1b$(1),H1b$(40),X1b$(40),Y1b$(40)
70  LET Kif=0
80  CLEAR SCREEN
90  PRINT RPT$(" ",24);"A GRAPH IS WORTH"
100 PRINT RPT$(" ",24);"MANY DATA POINTS"
110 PRINT RPT$(" ",27);DATE$(TIMEDATE);" at ";TIME$(TIMEDATE)
120 PRINT
130 !***> Data preparation
140 INPUT " Indicate data source: 0=internal via COM /Memr/ 1=file ",Kif
150 IF Kif<0 THEN STOP
160 IF Kif=1 THEN
170   INPUT " Name the data source""file""",Sfil$
180   PRINT " Data comes from""";Sfil$;"":
190   ASSIGN @Sourc TO Sfil$;FORMAT OFF
200   ENTER @Sourc;Hdra$,Hdrb$,Dmx,Dmy
210   REDIM Vctrs(1:Dmx,1:Dmy)
220   ENTER @Sourc;Vctrs(*)
230   ASSIGN @Sourc TO *
240 ELSE
250   PRINT " Data internal:"
260   IF Dmx>0 AND Dmy>0 THEN REDIM Vctrs(1:Dmx,1:Dmy)
270 END IF
280 PRINT Hdra$
290 PRINT Hdrb$
300 PRINT " Data stored as array( 1 :";Dmx;" , 1 :";Dmy;" )":
310 IF Dmx<1 OR Dmy<1 THEN PRINT " ???"
320 IF Dmx>0 AND Dmy>0 THEN PRINT
330 LET Kif=0
340 INPUT " Type: 0) to skip listing 1) to list array",Kif
350 IF Kif<0 THEN STOP
360 IF Kif=1 THEN
370   FOR Xpt=1 TO Dmx
380     FOR Ypt=1 TO Dmy
390       PRINT Vctrs(Xpt,Ypt),
400     NEXT Ypt
410   PRINT
420   NEXT Xpt
430   WAIT .5
440 END IF
```

```

450 LET Subj=0
460 INPUT "Plot manner? defined later=0 ser<=>prll=1, diel=2 LOGS=3",Subj
470 IF Subj<0 THEN STOP
480 IF Subj=0 THEN LET Subj=1 ! Defaults to Series<=>Parallel plot
490 LET Xlmn=0
500 DISP "Enter column vector 1..";VAL$(Dmy);" for X axis ";
510 INPUT "data?",Xlmn
520 IF (Subj=1 OR Subj=2) AND Xlmn=0 THEN LET Xlmn=2 ! Default in ser<=>prll
530 LET Aaa=MAXREAL
540 LET Zzz=MINREAL
550 FOR Xpt=1 TO Dmx
560 LET Tst=Vctrs(Xpt,Xlmn)
570 IF Tst<Aaa THEN LET Aaa=Tst
580 IF Tst>Zzz THEN LET Zzz=Tst
590 NEXT Xpt
600 IF Subj=1 THEN
610 LET Xlow=0
620 LET Xhigh=1
630 ELSE
640 DISP "Minimum of X axis data is ";Aaa;" , what shall be minimum for";
650 INPUT " plot?",Xlow
660 DISP "Maximum of X axis data is ";Zzz;" , what shall be maximum for";
670 INPUT " plot?",Xhigh
680 END IF
690 IF Subj=3 THEN
700 LET Xlow=LGT(ABS(Xlow))
710 LET Xhigh=LGT(ABS(Xhigh))
720 END IF
730 LET Xspan=Xhigh-Xlow
740 LET Xavg=(Xhigh+Xlow)*.5
750 IF Subj=3 THEN PRINT " LOG ";
760 PRINT " X axis of plot to range from ";Xlow;"to ";Xhigh;"."
770 LET Ylmn=0
780 DISP "Enter column vector 1..";VAL$(Dmy);" for Y axis ";
790 INPUT "data?",Ylmn
800 IF Subj=1 AND Ylmn=0 THEN LET Ylmn=4 ! Default in ser<=>prll case
801 IF Subj=2 AND Ylmn=0 THEN LET Ylmn=3 ! Default to permittivity case
810 LET Aaa=MAXREAL
820 LET Zzz=MINREAL
830 FOR Xpt=1 TO Dmx
840 LET Tst=Vctrs(Xpt,Ylmn)
850 IF Tst<Aaa THEN LET Aaa=Tst
860 IF Tst>Zzz THEN LET Zzz=Tst
870 NEXT Xpt
880 IF Subj=1 THEN
890 LET Ylow=-1
900 LET Yhigh=1
910 ELSE
920 DISP "Minimum of Y axis data is ";Aaa;" , what shall be minimum for";
930 INPUT " plot?",Ylow
940 DISP "Maximum of Y axis data is ";Zzz;" , what shall be maximum for";
950 INPUT " plot?",Yhigh
960 END IF
970 IF Subj=3 THEN

```

```

980 LET Ylow=LGT(ABS(Ylow))
990 LET Yhigh=LGT(ABS(Yhigh))
1000 END IF
1010 LET Yspan=Yhigh-Ylow
1020 LET Yavg=(Yhigh+Ylow)*.5
1030 LET Eff=0
1040 IF Subj=1 THEN
1050 INPUT "Overlay an effective medium [EM] curve for 2D? no=0 yes=1",Eff
1060 IF Eff<0 THEN STOP
1070 LET Eff=BIT(Eff,0)
1080 IF Eff THEN INPUT "Enter permittivity ratio for EM curve",Rem
1090 IF Rem<0 THEN STOP
1100 IF Rem=0 THEN LET Eff=0
1110 END IF
1120 IF Subj=3 THEN PRINT " LOG ";
1130 PRINT " Y axis of plot to range from ";Ylow;" to ";Yhigh;". "
1140 SELECT Subj
1150 CASE =0
1160 INPUT "Title?",H1b$
1170 IF H1b$="" THEN H1b$=Hdra$(1,40)
1180 INPUT "X axis label?",X1b$
1190 INPUT "Y axis label?",Y1b$
1200 CASE =1
1210 LET H1b$="RANDOM 2D NETWORKS"
1220 LET X1b$="Volume fraction of the larger"
1230 LET Y1b$="Averaging Parameter"
1240 CASE =2
1250 LET H1b$="RANDOM 2D NETWORKS"
1260 LET X1b$="Volume fraction of the larger"
1270 LET Y1b$="Permittivity"
1280 CASE =3
1290 INPUT "LOG Title?",H1b$
1300 IF H1b$="" THEN H1b$=Hdra$(1,40)
1310 INPUT "LOG X axis label?",X1b$
1320 INPUT "LOG Y axis label?",Y1b$
1330 END SELECT
1340 INPUT " Plot data 0) by points 1) by lines",Plt
1350 IF Plt<0 THEN STOP
1360 IF Plt=0 THEN
1370 INPUT " Type a single letter character for the plot points",Clb$
1380 INPUT " Character size in % of Xs of the graph width? ie 1,2,...",Csz
1390 IF Csz=0 THEN LET Csz=1 ! Default
1400 END IF
1410 IF Mach=0 THEN
1420 INPUT "Hardcopy of plot? 0=none 1=to printer 2=to plotter",Mach
1430 IF Mach<0 THEN STOP
1440 END IF
1450 IF Mach=2 THEN
1460 INPUT "Max speed of plotter pen? (~1-20, in cm/s)",Speed
1470 IF Speed<0 THEN Stop
1480 IF Speed=0 THEN LET Speed=10
1490 END IF
1500 WAIT 1
1510 CLEAR SCREEN

```

```

1520 KEY LABELS OFF
1530 !***> Begin plotting
1540 GINIT
1550 PLOTTER IS CRT,"INTERNAL"
1560 GRAPHICS ON
1570 FOR Cpy=0 TO (Mach>0)
1580     VIEWPORT 20,120,15,85                ! NEAR FULL SIZE SCREEN
1590     IF Subj=3 THEN
1600         VIEWPORT 40,95,35,90
1610     ELSE
1620         VIEWPORT 30,110,35,90
1630     END IF
1640     WINDOW Xlow,Xhigh,Ylow,Yhigh
1650     IF Plt=0 THEN
1660         FOR Xpt=1 TO Dmx
1670             LET Xx=Vctrs(Xpt,Xlmn)
1680             !IF Subj=1 THEN Xx=1-Xx        ! IF COMPLEMENTING NEEDED
1690             LET Yy=Vctrs(Xpt,Ylmn)
1700             IF Subj=3 THEN
1710                 LET Xx=LGT(ABS(Xx))
1720                 LET Yy=LGT(ABS(Yy))
1730             END IF
1740             MOVE Xx,Yy
1750             CSIZE Csz,.5
1760             LORG 5
1770             IF Clb$="" THEN
1780                 LET Clb$="+"
1790                 IF Subj<>1 AND Dmx<100 THEN LET Clb$=VAL$(Xpt)
1800             END IF
1810             LABEL Clb$
1820         NEXT Xpt
1830     ELSE
1840     !***> curve higher by a std deviation
1850     ! FOR Xpt=2 TO Dmx-1
1860     !     LET Xx=Vctrs(Xpt,1)
1870     !     LET Yy=Vctrs(Xpt,3)+Vctrs(Xpt,6)
1880     !     LINE TYPE 3
1890     !     PLOT Xx,Yy
1900     ! NEXT Xpt
1910     ! PENUP
1920     !***> central curve
1930     FOR Xpt=1 TO Dmx
1940         LET Xx=Vctrs(Xpt,Xlmn)
1950         !IF Subj=1 THEN Xx=1-Xx        ! IF COMPLEMENTING NEEDED
1960         LET Yy=Vctrs(Xpt,Ylmn)
1970         IF Subj=3 THEN
1980             LET Xx=LGT(ABS(Xx))
1990             LET Yy=LGT(ABS(Yy))
2000         END IF
2010         LINE TYPE 1
2020         PLOT Xx,Yy
2030     NEXT Xpt
2040     PENUP
2050     END IF

```

```

2060      IF Eff THEN                                ! overlay effective medium curve
2070      FOR Xpt=1 TO 200
2080      LET Xx=Xpt/201
2090      Aaa=(Rem-1)*(2*Xx-1)
2100      LET Dyf=.5*(Aaa+SQR(Aaa*Aaa+4*Rem))
2110      LET Yy=FNWnr(Rem,Xx,Dyf,Zzz)
2120      IF ABS(Zzz)>.000001 THEN PRINT " Warning! Ser<=>Prll difficulties"
2130      LINE TYPE 1
2140      PLOT Xx,Yy
2150      NEXT Xpt
2160      END IF
2170      IF Subj=1 THEN
2180      AXES .05,.1,0,-1,2,1
2190      AXES .05,.1,1,1,2,1
2200      ELSE
2210      FRAME
2220      END IF
2230      !***> set labels
2240      CLIP OFF
2250      LORG 4
2260      MOVE Xavg,Yhigh+.08*Yspan
2270      CSIZE 4,.6
2280      LABEL H1b$
2290      LORG 4
2300      MOVE Xavg,Ylow-.16*Yspan
2310      CSIZE 4,.6
2320      LABEL X1b$
2330      MOVE Xlow-(.1+(Subj=1)*.04)*Xspan,Yavg
2340      DEG
2350      LDIR 90
2360      LORG 4
2370      LABEL Y1b$
2380      IF Subj=1 THEN
2390      CSIZE 2.4,.6
2400      LORG 1
2410      MOVE Xlow-.092*Xspan,Ylow
2420      LABEL "Series-like"
2430      LORG 7
2440      MOVE Xlow-.092*Xspan,Yhigh
2450      LABEL "Parallel-like"
2460      LDIR 0
2470      LORG 5
2480      CSIZE 2.2,.6
2490      LET Zzz=Ylow-.04*Yspan
2500      FOR Xgf=Xlow TO Xhigh STEP .1
2510      MOVE Xgf-.01,Zzz
2520      LABEL USING "D.D":Xgf
2530      NEXT Xgf
2540      LET Aaa=Xlow-.05*Xspan
2550      FOR Ygf=Ylow TO Yhigh STEP .2
2560      MOVE Aaa,Ygf+.01
2570      !LDIR 90
2580      LABEL USING "DD.D":Ygf
2590      NEXT Ygf

```



```

2600 END IF
2610 LORG 1
2620 LDIR 0
2630 MOVE Xlow-.19*Xspan,Ylow-.30*Yspan
2640 CSIZE 2,.6
2650 LABEL Hdra$
2660 MOVE Xlow-.19*Xspan,Ylow-.35*Yspan
2670 LABEL Hdrb$
2680 SELECT Mach
2690 CASE =1
2700     DUMP GRAPHICS CRT
2710     WAIT 2
2720     LET Cpy=2
2730 CASE =2
2740     GINIT
2750     PLOTTER IS 705,"HPGL"
2760     GSEND "VS"&VAL$(Speed)
2770 END SELECT
2780 NEXT Cpy
2790 KEY LABELS ON
2800 PEN 0
2810 END
2820 DEF FNWnr(Dratio,Frxp,Din,Pcterr)
2830 !***> Object of function to find alf satisfying 1=SUM of(vol*diel^alf)
2840 !***> where vol=fractional volumes
2850 !***>     diel=(species permittivity)/(composite permittivity)
2860 !***>     alf= constant exponential between -1 & +1 (series<->parallel)
2870     INTEGER Spk,Arnd
2880     IF Din=0 OR Frpx>=1 THEN
2890         LET Alf1=0
2900         LET Pcterr=1.E-99
2910         PRINT " .. series <=> parallel factor at or beyond limits"
2920     ELSE
2930         IF Dratio>0 AND Frpx>0 AND Frpx<1 THEN
2940             LET Gratio=LOG(1/Din)
2950             LET Gsum=(1-Frpx)*Gratio
2960             LET Gdev=(1-Frpx)*Gratio*Gratio
2970             LET Gratio=LOG(Dratio/Din)
2980             LET Gsum=Gsum+Frpx*Gratio
2990             LET Gdev=Gdev+Frpx*Gratio*Gratio
3000         END IF
3010         LET Alf1=-2*Gsum/Gdev
3020         LET Gsum=Gsum+Gdev           ! Initial guess of sum
3030         LET Try=1                   ! Optimize sign in iterations
3040         LET Alf0=0
3050         LET Arnd=1
3060         WHILE ABS(Alf1-Alf0)>.000000001
3070             LET Gsum=0
3080             LET Gdev=0
3090             LET Gratio=1/Din       ! relative permittivity to composite
3100             LET Gwk=0              ! a term @ species to sum
3110             IF Gratio<>0 AND Frpx>0 AND Frpx<1 THEN
3120                 LET Gwk=(1-Frpx)*Gratio^Alf1
3130                 LET Gsum=Gwk       ! sum function (as described)

```


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