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AGARD-R-766

# NORTH ATLANTIC TREATY ORGANIZATION

# ADVISORY GROUP FOR AEROSPACE RESEARCH AND DEVELOPMENT

(ORGANISATION DU TRAFLE DE L'ATLANTIQUE NORD)

AGARD Report No.766

# AGARD ENGINE DISC CO OPERATIVE TEST PROGRAMME

by

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This publication was sponsored by the Structures and Materials Panel of AGARD.



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Published August 1988

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ISBN 92-835-0475-5



Printed by Specialised Printing Services Limited 40 Chigwell Law 2 Jughton, Essex IG10312

# PREFACE

The Structures and Materials Panel has been involved in studies of fatigue and fracture of critical jet engine components for many years. In 1982 a Sub-committee on "Damage Tolerance Concepts for Critical Engine Components" was formed to study the overall philosophy and the implications of introducing damage tolerance concepts (DTC) into the design and use of critical engine components.

The damage tolerance philosophy offers potential cost savings of considerable magnitude when compared with a "safelife" approach provided such a concept can be implemented with an assurance that current safety standards will not be prejudiced. As an example of possible cost savings, it has been estimated that over 80% or enguae discs have ten or more low cycle fatigue lives remaining when discarded under "safe-life" rules, and it is the useful remaining life that DTC aims to exploit in service. Aprint from economic advantages, the DTC approach offers a practical method for using modern high-strength disc materials that could be rejected by the application of "safe-life" conditions of usage.

In 1983 the Sub-committee on Damage Tolerance Concepts for Critical Engine Components, under the chairmanship of D.A.Fanner (UK), organized a Cooperative Test Programme on Damage Tolerance in Titanium Alloy Engine Disc Materials. A separate Sub-committe on Engine Discs Cooperative Tests (TX-114) was formed to direct this activity. Over the years the following Panel members participated in the sub-committee:

A.Ankara (TU) H.M.Burte (US) H.J.G.Carvalhinhos (PO) M.N.Clark (CA), Chairman 1983-85 D.Coutsouradis (BE) J.J.De Luccia (US) G.L.Denman (US) A.Deruyttere (BE) M.Doruk (TU) W.Elber (US) D.A.Fanner (UK) J.J.Kacprzynski (CA) Chairman 1986-R.Labourdette (FR) J.S.L.Leach (UK) A.Salvetti (IT) R.Schmidt (US) H.P.van Leeuwen (NL) W.Wallace (CA) H.Zocher (GE)

The cooperative tests were performed by twelve laboratories represented by

J.Foth, IABG, GE A.Frediani, Univ. of Pisa, IT C.Gostelow, RAE UK C.Harmsworth, AFML, US C.Howland, RR, UK R.H.Jeal, RR, UK E.U.Lee, NADC, US A.Liberge, CEAT, FR N.McLeod, RR, UK A.J.A.Mom, NLR, NL T.Pardessus, CEAT, FR M.D.Raizenne, NAE, CA W.Schütz, IABG, GE P.Sooley, Univ. of Toronto, CA J.Telesman, NASA, US M.Yanishevsky, OETE, CA C.Wilkinson, RR, UK

The coordinators of the programme were:

for Europe – A.J.A.Mom for North America – M.D.Raizenne

As a result of the very large size of the test programme, it appeared to be convenient from an administrative point of view to divide it into a Core Programme followed by Supplemental Programmes. In the Core Programme all the laboratories performed identical fatigue and fracture tests for one material at constant amplitude and at room temperature. A summary of these tests is included in the present report, and all the test data are stored at the National Aeronautical Establishment of the National Research Council of Canada and are available on request. In the Supplementary Programme, now in progress, three materials are tested at room temperature and with load patterns represented by TURBISTAN. High temperature tests of fatigue and crack growth will be performed in a separate programme.

The part of the Cooperative Engine Disc Test Programme completed to date produced very valuable results and represents a significant progress in implementation of damage tolerance concepts to life evaluation of engine critical components. Many thanks to all who contributed to this very difficult activity and particularly to the participants and the coordinators. Special thanks are due to R.H.Jeal, who, in spite of his busy professional life at Rolls Royce, was a catalyst and strong supporter of the programme.

Many thanks to participating laboratories and particularly to:

NLR -- for producing programme reports, bookkeeping, fractography tests and analysis of test data.

Rolls Royce - for supplying engine discs and producing test specimens.

NAE - for data collection, statistical analysis, presentation and storing,

QETE - for fractography tests on selected specimens.

During the execution of this test programme, close cooperation has been developed with participants of other panels' activities and particularly with the Short Cracks Test Cooperative Programme. Not only did the chairman of that subcommittee, H.Zocher, participate as an Engine Dises Sub committee member, but also both coordinators, Dr P.R.F.dwards and Dr J.C.Newman volunteered to participate actively. Their contribution is greatly appreciated. As a result of the cooperation of these two Sub-committees an additional joint test programme has been formulated. It is now in progress and the results will be included in future reports.

The objectives of the Engine Discs Cooperative Test Programme have been aeby yed. Even more than was planned has been achieved. This is demonstrated by the fact that each of the participating laboratories independently produced results as good as the others. This may diminish the reluctance to use other's data for life determination of critical components.

The second unplanned achievement was the development of close friendships between the participants. As a result of the, a person performing a difficult and risky life evaluation of a critical engine component can consult his friends in other NATO countries. This may help in finding better solutions to our common problems.

The development of close cooperation of professionals of NATO countries was a dream of Theodore von Karman and it is a pleasure to see that it has been achieved.

J.J.Kaeprzynski Chairman 1986--Sub-Committee on Engine Disc Cooperative Test Programme

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# ABSTRACT

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This report describes the initial results of an AGARD test programme on tatigue behaviour of engine disc materials. The first phase of this programme, the Core Programme, was aimed at test procedure and specimen standardisation and calibration of the various laboratories. A detailed working document has been prepared and is included in this report. It describes the testing fundamentals and procedures and includes the analysis procedures used for handling the test data.

\* \* \*

Ce rapport presente les premiers resultats d'un programme de tesis de l'AGARD sur le comportement en tatigue des matériaux constitutifs des disques de moteur. La premiere phase de ce programme, appele le programme Core, a pour objectif de normaliser les procédures d'essai et les échantillons et de procéder à l'étalonnage des appareils de mesure défenus par les différents laboratoires. Un document de travail défaille à été propare. Il est joint à ce rapport, il fournit une description des principes des tests et des procédures utilisées, y compris les procédures d'analyse mises en œuvre pour le dépouillement des données de test.

Des tests sur le début et la progression des fissurations de fatigue ont eté executes sur du maieriel 1/6A/4V à température ambante, avec chargement à amplitude constante, en utilisant quare cehantillons differents, composes du même matériau. L'Ensemble des resultats à cié analyse statistiquement afin de noter d'eventuels écarts significatifs dans le comportoment des matériaux, en fonction de l'endroit du prelèvement sur le disque, dús aux paramètres de labrication et aux techniques employées par les différents laboratoires.

AGARD ENGINE DISC COOPERATIVE TEST PROGRAMME

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SUMMARY

This report describes the initial results of an AGARD test programme on fatigue behaviour of engine disc materials. The first phase of this programme, the CORE programme, was aimed at test procedure and specimen standardization and calibration of the various laboratories. A detailed working document has been prepared and is included in this report. It describes the testing fundamentels and procedures and includes the analysis procedures used for handling the test data.

Fatigue crack initiation and proposition testing were performed on Ti-bAl-4V material under room temperature and constant amplitude loading conditions using four different specimen designs. All results were statistically analysed for possible significant differences in material behaviour due to disc processing variables, specimen location in the disc or testing laboratory.

1. PREFACE

The results in this report are a collaborative effort of the following participants and their representatives (in parenthesis the ordename of each participant used throughout the text is indicated):

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#### 2. INTRODUCTION

The AGARD engine disc cooperative test programme is a joint international effort to address the problem of fatigue crack growth and fracture of disc materials under operational loading conditions. Knowledge of fatigue and iracture characteristics is a major requirement before a damage tolerance disc lifing approach can be successfully implemented. These aspects are discussed in Reference [1] of which details are given below.

For airframe structures, the damage tolerance design approach was introduced by the USAF in 1970, and it has been effectively applied since then on a number of civil and military airctait (MLL-STD-1730 and MLL-A-BJ44). However, for engine components, damage tolerant design has been a recent development. Application of this design approach, with respect to disc lifting, is currently under consideration and occasionally applied. A specification or engine damage tolerance requirements, listed as MLL-STP-1781, his recently been developed.

Nevertheless, most discs are currently designed based upon the so-called safe-life philosophy. Both design approaches are concisely reviewed below.

## Safe life design

Currently sate life design is still the most widely used approach in the lifing of engine discs. In this respect, "safe life" means that parts are designed for a finite service life during which no significant damage will occur. No critical defects are assumed to be present in the new structure and no inspections are required during the design life. After reaching the safe life limit, the part is retired from service.

With respect to aircraft engine discs, the safe life is defined as the number of cycles at which, statistically, one of every 1000 components will develop a crack of 0.8 mm (1/32 in) surface length. This crack size has been chosen because:

at this size, high cycle fatigue (HCF) crack growth under vibratory conditions would not yet occur,
 this crack size was, for existing materials, significantly smaller than the critical crack size for

rupture, and (3) a 0.8 mm crack was considered to be the smallest crack detectable.

The safe life design of discs implies that 999 out of 1000 components are rejected based on the statistical probability of a crack forming without actually requiring the presence of a detectable crack. From economic considerations this is not very attractive. It has been shown [2-4] that owing to a large scatter in the time to initiate and  $g^{\rm crimedic}$  -reack to a detectable size, most of these retired components still have considerable service life left. If components could be withdrawn from service based on the presence of a actual crack, then a much better usage of this inherent available life would become possible. This latter approach is in essence the basis of the damage tolerance design philosophy.

## Lamage tolerance design

In damage tolerance design, the possibility of a crack or defect present in a new structure is accounted tor. Assuming that crack growth can be predicted in critical locations under operational loading conditions, safe inspection intervals can be established. Regular inspections will then screen out those components which have insufficient life to be returned to service, as indicated in Figure 1. As can be seen from this figure, the inspection interval is based on the maximum allowable crack size in service, a, the minimum reliably detectable crack size by means of non destructive inspection (NDI) or other techniques, a, and the availability of crack growth data.

a, the winnum reliably detected to that size of motion in the detected of the availability of crack growth data. From the foregoing it is clear that several key design parameters are required before the damage tolerance lifing approach can be successfully implemented: - the operational load history of discs.

- the operational load miscory of discs, - material crack growth data for the appropriate loading conditions, and

- the suitability of NDI or other techniques for the reliable detection of very small cracks.

In recent years considerable progress has been made in inspection capability. It has been claimed [5] that under proper inspection conditions, working with well motivated people and very special equipment, cracks of 0.375 mm surface length and 0.125 mm depth can be detected at the 90 % prosability/95 % confidence level. At present, however, it seems more realistic to assume a crack detection capability for cracks of at least 0.750 x 0.375 mm [6].

With respect to monitoring of operational load parameters, several systems are presently in use, e.g. the AID (Aircraft Integrated Data) and EUM (Engine Usage Monitoring) Systems. Proper analysis of the recorded signai to enable accurate determination of life consumation or crack growth prediction is, however, still in an exploratory stage. A considerable amount of work in this area is being performed by the Turbistan working group, with the goal of developing a standard or reference load sequence for gas turbine discs [7].

The third basic requirement, essential for application of the damage tolerance philosophy, is knowledge about material crack growth and fracture behaviour under operational conditions. This is the area which the current AGARD cooperative test programme addresses. An extensive amount of data and a basic understanding of material tatigue crack growth behaviour is needed before damage tolerance lifing procedures can be 'mplemented. By adopting the common effort of a number of laboratories. Throad data base and an improved knowledge and understanding of the testing techniques could be realised. This was achieved by the first phage of this collaborative programme.

## 3. TEST PROGRAMME OBJECTIVES

The major objectives of this AGARE coordinated programme are:

- the determination of material behaviour, crack initiation and propagation characteristics under
- realistic engine conditions, and
- the examination of the ability of fracture mechanics to predict crack growth behaviour in discs under service c. ditions.

The first phase, the CORE programme, was aimed at test and specimen standardisation and tamiliarisation, and collibration of the different laboratories. The second phase, the COPPLEMENTARY programme, will specifically address parameters representative of real service operation-like mission loading, sequence and dwell effects, temperature, fatigue thresholds, etc. In addition, like prediction methods, their applicability and limitations, will be addressed in this phase.

The major objectives of the CORE programme are:

- fumiliarisation of various laboratories in North America and Europe with new test techniques, such as the potential drop technique for crack length measurement and automated data and friend.
- standardization of test specimens and test techniques for engine disc materials,
  calibration of the various laboratories via a round robin test programme in order to gain confidence in
- calibration of the various laboratories via a round robin test programme in order to gain confidence in each other's results, and
- material data collection, using Ti-6Al-4V, for verification of lite prediction techniques used in damage tolerance design of engine discs,
- identification and documentation of data analysis techniques.

The set-up of the CORE programme, the test procedures and the results are presented in the following sections.

## 4 CORE PROGRAMME

#### 4.1 CORE Programme Set-Up

The CORE programme test matrix is shown in Table 1. Each laboratory performed all the tests in the matrix for comparison and calibration purposes. The test matrix consisted of a series of fatigue life tests (unnotched and notched specimens) and a series of crack propagation tests (compact tension and corner crack specimens). With these data, both the safe life and the damage tolerance approach could be addressed.

All testing was performed under load control, constant amplitude and room temperature conditions. The tatigue load levels were chosen to achieve realistic lifetimes to failure and/or crack propagation rates. For valid comparison of the individual laboratory test results, a working document detailing the procedures for instrumentation, measurement, testing and data acquisition was developed and is included in this report as Appendix A. Coordinators, one from Europe and one from North-America, were selected to oversee the programme and to collate and analyse the data.

## 4.2 Specimens

# 4.2.1 Specimen types/background

For standardisation purposes four specimens were selected for fatigue life and crack propagatic: testing. One of the goals of the programme was to establish specimens as stindards and thus encourage other laboratories to use them. In this way a broad data base using these specimen gcimetries would be created. The selected specimens are shown in Figure 2. The specimen shown in Figure 2a is a smooth

cylindrical specimen (designated as 10F-specimen) used for fatigue life testing. The flat double edge notched specimen with a K = 2.2 (designated as K 2.2 specimen), figure 2b, is also used in fatigue iff testing. However, apart from the life to failure the life to frack initiation for better: life to a certain crack size) can also be determined. The well known ASTM empact type, also called compart tender specimen (designated CT-specimen) with a through thickness notch is shown in Figure 2c. This specime is used for crack propagation testing in the so-called long crack progime, there the crack comparts is in rmally two-dimensional and the initial crack length is much larger than the erain size of the material. The total da/dN-dK curve including the fatigue threshold,  $dK_{\rm beck}$  can be determined using this specimen. The specime idesigned speciment is shown in Figure 2d, is the correct crack specime idesignated (T-specime). This specime to crack propagation testing is the so-called long crack regime, where the crack generics), this specime total da/dN-dK curve including the fatigue threshold,  $dK_{\rm beck}$  can be determined using this specime). This specime to a designed specifically for crack propagation testing of disc naterials to simulate the same threedimensional stress fields as those encountered in critical blocations such as belt holes. In this respect, it is necessary to refer to Pickard et al. 8. Who have shown that the crack propagation curve obtained with CC-specimens clearly fulls below the curve generated with CI-specimens. As a result, when comparing specimen crack growth data with crack growth in an actual disc, the latter will be veliced with CC-specimen data, whereas the use of CI-data could result in an underestimation of iffe wells is the discuster of two. Bearing this in mind it was considered essential that both types of crack propagation specimena fe used in the programme. As well, the CC-specimen was considered ideal for determining short crack effects

## 4.2.2 Specimen machining and location

All specimens for the (OKE programme were machined by Rolls-Koyce. The specimens were extracted from two nominally identical fam disc forgings supplied to Rolls-Koyce. The specimens were extracted from two nominally identical fam disc forgings supplied to Rolls-Koyce. The specimen forging venders, the forgings were made from Ti-6A1-4V in the solution treated and aged (SIA) condition. The disc cut-apdrawing indicating the location of each individual specimen is shown in Figure 1. The orientation of the specimen crack planes in relation to the forging directions was specified so it would be the same as encountered in service. The distribution of specimens was arranged such that three North-American and three European indocations obtained complete sets of specimens from one disc, and the remaining laboratories obtained complete sets of specimens from the other disc, as seen in Figure 3. This would allow possible differences in material behaviour between the two discs to be identified and to familitate the exchange of material from the two discs for metallurgical examplation.

#### 4.2.3 Basic material properties

Basic material properties for these discs were determined by Polls-Rivee. These are given in Table 1, and are compared with the "Material Specification minimum value" (i.e. the lowest acceptable property values expected from such forgings). In general, the measured properties were equal to or "effect than the specified minima. The sole exception to this was the 150 °C ductility (C RA) which was slightly low. However, this anomaly was ameliorated by the elongation measured from the same specimen.

It was concluded that the two discs supplied formed a good basis for this conjective programme.

#### 4.2.4 Microstructure

The microstructure of the Ti-bAl+AV disc material, which was in the STA (solution tradit and agent) condition, consisted of equiaxed a-phase in a transformed  $\beta$ -matrix containing coarse actualar a (Figure 4). Occasional a-alignments were observed as seen in Figure 5.

The amount of a-phase, determined with quantitative metallography, was about 467, cross-sections were repared in three perpendicular directions: in the plane of the disc, perpendicular to the disc plane in the radial direction and perpendicular to the disc plane in the circumferential direction. No obvious affecteds in microstructure in these three directions were observed.

Texture differences between selected specimens were determined by the RAF. For this purpose slices were prepared from tested specimens, see Figure 6. Note that the surface on which the texture measurement was performed was a radial plane perpendicule to the disc plane. Slices for the texture determination were prepared in m specimens CC 14, 16, 18, 20 and 22 from both discs. Specimens CC 14, 16 and 18 were selected to indicate radial texture variation.

An indication of texture in a material can be obtained by the use of pole figures. In the following a short explanation of the construction and purpose of pole figures is given.

Crystallographic planes, axes and angles can be represented on a sphere, known as the reference or polar sphere, when a crystal is assumed to be small compared to the sphere and to be located at its centre. One way to represent the crystal planes on the sphere is to erect perpendiculars to the planes. These plane normals are made to pass through the sphere centre and to intersect the spherical surface at points known as the poles of the planes. The array of poles on the sphere form a sole tigure, which represents the orientation of the crystal planes. In profice it is more convenient to use a map of the sphere known as the stereographic projection. This enclose a two-dimensional representations of the pole figure. Such representations are commonly used to compare textures, which are preferred orientations of crystal planes within a polycrystalline sample. To do this the stereographic projection is aligned to the overall geometrical features of the specimen and the number of grains in "drious ranges of orientation are then indicated in it by a series of contour lines. The experimental information is usually obtained trom the relative intensities of X-ray reflections from the polycrystal at various angular settings.

The pule figures of the selected specimens are shown in Figure 7 , or disc LWMP /200 and in Figure 8 for disc WGWMD 1113. Each set of figures (a) through (f) shows the  $\{0002\}$  pole figures, whereas the figures (g) through (1) show rite (i00) pole figures, (a) through (1) show rite (i00) pole figures, whereas the positions in the discs. (Note that the specimens CC 20 and CC 22 of disc WGWMD 1113 where processed in a slightly different way. Instead of the  $\{110\}$  (equivalent to (1120) in deraxis notation) for various were determined, even the event interves  $\Psi(P)$ . However, this does not alter the conclusions.) The figures (a), (b) and (c) give an indication of the texture itself and the texture variation in the axial direction (specimens CC 14, CC 16 and CC 18 respectively, see also Figure 3 for their detailed position) and figures (d), (e) and (C 22 respectively). The figures show that the texture 1 differences between the discs are relatively small. If a strong texture would exist then much higher figures for the contour levels would have been encountered. As mentioned before, these contour levels indicate relative densities of crystallo-

greater variation in texture in the axial direction than disc LWMD 2000 (Figure 7). In the radial direction the variation was less than that displayed in the axial case. In fact, very 'iftle d'ifterence was observed between specimen positions (C 20 and CC 2). Discussions with RAE indicated that the observed texture and texture differences were not very marked, even between the two discs, and that these dif-ferences would not be expected to result in appreciable changes in material properties.

## 5. TEST PROCEDURES

## 5.1 General

All testing was done according to the "Working document for the AGARD cooperative test programme of titanium allow engine disc material" (9). During the actual test phase of the programme, as a result of data generation and testing experience, this document was modified and amended and is included as Appendix A

#### 5.2 Potential drop crack measurement rechnique

An interesting aspect of the test programme was that crack initiation and crowth was monitored by means of the potential drop (PD) technique. This technique requires that a constant current be passed through the specimen and the electrical potential over the crack plane be measured by two prides 1 cated on opposite sides of the crick. If the relationship between track length and woltage is known, as see 1 Figures An and Appendix A for the CL and CC specimen respectively, an accurate determination of rack length can be achieved.

The advantage of the PD method is that crack length detection is also possible it a closed furnace and that automated data collection is easily attained. Additionally, the average crack length instead of the surface crack length as in the case of optical measurements, thankes in crack in st curvature are thus accounted for.

A typical set-up for fatigue testing and crack length measurement is shown in Figure 7. When the apart from the notch voltage, a reference voltage is measured to account for temperature effects and conout variations. Thermosectric effects and drift of the system are eliminated by taking the difference it two measurements, one with current-on, ne with content-of

# 5.3 Example description of grack length measurement using the PF technique

o illustrate how the actual procedure for crack growth measurement was performed, the foll was. example using a to specimen is given. An instrumented corner crack speciment was periodiant, the poly with that for reasons of simplicity both the moth probe wires and the reference wires were would be the same edge). In the actual test programme, to prevent the occurrence of a reference potential charge due to crack growth the reference probes were would at a location at which the potential field were to also for by crock growth, i.e. at the out site corner.

The result of a preliminary test on the dummy specimen shows in Figure 3. Is presented to Figure the figure illustrates the importance of the location of the reference probes, clearly showing to ne-crease in reference potential as a result if being located in the vicinity of the creating crease.

The actual chack growth curve (average crack length versus cicles) was constructed after adjoration of the motch wolfage versus crack length. For this purpose the average crack size of the crici for four was determined first. The specimen was deliberately broken open and the mean of five fracture softwar-crack length readings were taken; two at the side suffaces, i.e. the sufface crick lengths, the five three at angles of 22.5°, s5° and 07.5°. This averaging rethind resulted in this a very sin r difference three at angles of 22.5°, s5° and 07.5°. crack length readings were taken; two at the side surfaces i.e. the surface crick lengths, the transmission  $(2,5)^2$ ,  $(3^2)$  and  $(1,5)^2$ . This averaging rether resulted in this very sine fitter entries in the solution of the transmission of the solution of the solu

Figure 12 also shows the relation between the pathon black model and size and an end of the or the specime scale during the test this curve indicate that the optical measurement indicate state of a specime scale during the test. This curve indicates that the optical measurement indicate make the average crack length as defined by the calibration curve. The course of this effect is the oracs troct con-vature at the specimen surface, as seen in Figure 15. This example learly thus rates the advintage of the PD method for crack length determination over the optical method, he addition, the PD method sector tivity is very good. The system shown in Figure 9 allows chances in crack course to be detected with better than 5um sensitivity.

In Figure 13 another reature can also be seen. In the early of the test, testion was interrupte for heat tinting in order to have at additional data point for calibration. This data point, also -plitted in Figure 12, lies exactly on the calibration curve, giving additional contidence in the adopted metrid

The collibration procedure described above for the CC specimen is similar to that used for the c Specime with the exception that the calibration curve for this specime is similar to that uses for the similar bull the calibration curve for this specime is similar to third order bipment. I function, However, mesurement of the final average crack size from the fracture sortice as was done for the U specimen, is sufficient to fix the position of the calibration curve.

## 5.4 Test procedure variations

Although the procedures for testing are described in detail, there were still variations between laboratories in the actual testing techniques. This was due to: bardware limitations; differences in programmes for computer controlled fatigue testing; and differences in the way the potential drop method applied. Some of the more important variations in test procedures are documented below.

The major variations in test procedures concern the potential drop measurement technique. In purticular, the CC specimen PD-data was not aiways obtained or could not be easily analysed because of slight differences in probe wire attachment. In one case of a CT specimen, both the humul foll PD method and the optical crack length measurement techniques were employed. (The RUNUL foll is on electrically conductive tape which is adhesively bonded to the specimen so that surface crack growth, which extends into the toil, can be measured). The Rumul foil was attached to one side of the Cl-specimen, giving PD crack length data

-4

## only for that particular surface.

The PD-measurement technique itself was performed in different ways. The recommended procedure is show in Figure A5 of Appendix A. In the procedure both current-on and current-of: measurements are done at kimum load within the limetrame of one second, however, because of hardware limitations, the time meeded for two successive measurements of motch and reference voltages was sometimes in excess of one second. Thus, these voltage readings at times could not be measured simultaneously. This problem was accentuated with the K 2.2 specimen, where two motch voltages and one reference voltage had to be measured simultaneously. In addition, the current should be stabilized between current-on and current-off measurements.

The above problem was overcome either by lengthening the time at load for these particular measurement cycles or by doing notch and reference measurements in successive cycles. If the first method was applied the maximum time at load had in one case to be increased from 1 to 1.3 seconds; in arother case from 1 to 4 seconds. Other laboratories adopted the second method: the execution of PD measurements in successive cycles.

both methods might have an effect on the term results. An increased time at maximum load (for the measurement cycles) could enhance the dwell effect although this effect is probably very minor. Promeasurements in successive cycles might give, at very high crack growth rates, a minor shift in crack growth data but this can be simply overcome by counting the cycles during the actual notch measurement (the current-off and reference voltage will change only slowly).

## 5. RESULTS

The test results for the four specimens tested are discussed individually in the following subsections.

## 6.1 Smooth cylindrica, LCF specimens

b.1.1 General introduction

All test results are presented in Table 3 and are shown graphically in Figure 14. Note that, unlike engineering convention, the stress range as the independent variable is plotted on the horizontal axis and the cycles to failure on the vertical axis for commonality with the statistical analyses of the results (uext sections). The results appear to indicate that the LWMD 7200 disc data are slightly above the WGWD 113 disc data. This agrees with the data in Table 2. A statistical analysis of the results was performed to detect possible differences in material behaviour for the two discs, or for particular locations in the discs, or to indicate deviating trends in the results of individual haboratories. The analysis involved the establishment of linear relationships between stress and lite based on a log-normal distribution, the establishment of confidence intervals for these curves, and tests on the validity of the application it the linear model.

for linear expression used in the statistical analysis was:

 $Y = A + b\lambda$  in which Y = logN  $X = \Delta c$  N = number of cycles to failure $\Delta c = stress range$ 

The statistical analysis was performed according to the procedures described in ASTM standard Practice E 739-80 [10]. A short summary is given in Appendix B.

## 6.1.2 Statistical handling of the smooth cylindrical LCF specimer data

An initial statistical analysis was performed on all the data, except the one run-out, CEAL UCF 38 which tailed in the thread after 16,262 cycles. The results, see Figure 15, show that data obtained at very high stress levels (stress range  $\sim 875$  MPa) exhibited large scatter causing a major shift in the position of the mean curve for all the results. The high stress range of 875 MPa which is near or above the minimum specified tensile strength for the material as seen in lable 2. For this reason these test data were omitted from the statistical analysis. The results obtained in the lower stress ranges of 700 to 830 MPa had more appropriate lives to failure of 7006 to 500,000 cycles with less scatter.

The data were reanalysed and the resultant mean curve and the 95.7 confidence interval are shown in figure 16. The meaning of the confidence interval is that, based on the analysis of a series of independent data sets, we may expect that 95.7 of the computed intervals will include the mean curve. Or, in other words, the statement "the sean curve (of the total distribution) liss within the computed interval" has a 95.2 probability of being correct (see Peference [10]). Figure 16 also shows the computed statistical parameters A and B (which are the maximum likehood estimators of A and B, the line-coefficients) and their intervals for a 90 and 95.2 confidence level. In addition, the variance and the parameters indicating the correctness of the linearity hypothesis are indicated. These parameters are described in more detail in Appendix b.

As can be seen from the computed statistical data (see Fig. 16) the linearity hypothesis, for all results, was invalid. However, the rejection of the linearity hypothesis is caused by a single data point ( $\Delta\sigma$  = 8.28 MPa, N = 4.37 cycles, disc WGMD 1113). When the statistical data handling was repeated with the omittence of this particular test point, the linearity hypothesis was shown to be valid. For reasons of simplicity, the assumption of linearity in the range of 2000 - 50,000 cycles to failure was therefore considered to be appropriate. The linear model was also used in all subsequent analysis. (Note: the particular data point was not removed in the analysis).

6.1.3 Statistical comparison of individual laboratories, discs and disc locations

Figures 17 through 28 show the outcome of the subsequent statistical analyses in which various comparisons were made as follows: 1. individual disc results with respect to the overall data,

2. individual laboratory results with regard to the respective disc data (and corresponding confidence intervals) and with regard to the overall data, and

3, various disc locations with regard to the respective disc data.

figures 17 and 18 show the test results and associated median curves and confidence intervals for discs WGMUD 1113 and LMMD 7200 respectively. The statistical parameters are also given. The results show that the assumption of a linear relationship is valid for the LMMD 7200 disc data but that this assumption is incorrect for the WGMMD 1113 disc data. This was caused by the single data point discussed in Section 6.1.2 resulting in a sceep line coefficient B (i.e. slope) for disc WGMMD 1113.

A comparison between the individual median curves for the two discs, as constructed in the Figures 17 and 18, with the overall median curve for all results, Figure 16, is shown in Figure 19. In this figure, the test data for disc WGMMD 113 tend to fall slightly below the disc LMMD 7200 data as mentioned in Section 6.1.1. for the somewhat higher stress ranges. At these highest stress ranges ( $\Delta c \approx 820$  MPa) the maximum difference in fatigue life is about a factor of 1.5.

gure 10 shows the overall median curve and the median curve for disc WGWMD 1113. The individual fitted curves of the , x laboratories which tested this disc are also plotted. Most of the individual curves fall within the 95 % confidence interval for the overall curve. However, some data fall outside this interval. This behaviour may be expected since the number of specimens tested per laboratory was small.

In Figure 21 a similar comparison is made. However, the overall median curve and associated contidence interval have been omitted and the indicated 95 % confidence interval now relates to disc WGMD [11] only. In this case the individual laboratory curves fall within the wider 95 % confidence interval. Although there is a clear difference in line coefficients for the various laboratories and a slight shift in the line position, there is no major indication that the results from an individual laboratory clearly fall outside the scatter band.

Figures 22 and 23 are equivalent to Figures 20 and 21 but now refer to disc LWMD 7200. Most of the individual laboratory curves for this disc run almost parallel to the overall median curve and the disc median curve with one exception, which shows a more steep relationship. Figure 23 also shows that all in-dividual curves fall within the 95 % confidence interval for the disc median curve. Thus there is no indication of clearly deviating results for indivi !ual laboratories.

During disc design and production the intention was to obtain homogeneous properties throughout the disc. The test results enabled us to check whether this objective was met. To this end different locations in the disc were identified (see Figure 24) which could provide an indication about radial and axial variations in morerial behaviour. Figures 25 and 26 show, for the respective discs, a comparison of the fitted relationships for various radial locations with respect to the median disc curve. Figures 27 and 28 show similar comparisons for different axial locations.

The results indicate that differences do occur due to location. However, these differences appear to be insignificant. In Figure 25, disc WGWMD 1113, the RIM area tends to be superior with respect to the MID and BORE locations at the higher stress range, but it is inferior at lower stress ranges. This behaviour is not very logical. If the RIM area would indeed have superior fatigue properties than one would expect that this superiority would manifest itself over the entire life regime, especially because it is not expected that the failure mode would change significantly in this particular regime, and thus that in would result in an upward shift of the fatigue life curve. The observed line-crossings of the RiM, MID and BORE life lines are therefore most probably the result of normal scatter in the test data and the re-fatively small batches used for this location analysis. Another important point supporting the above conclusion is that one would expect that a certain trend in material behaviour for various locations would be similar for both discs. However, in comparing Figures 25 and 26 such a trend could not be observed. Figure 26 for example, disc LWMD /200, shows that the RIM, MID and RORE locations are essentially similar in fatigue behaviour.

A comparison with respect to axial locations for both discs was made in Figures 27 and 28. Line-crossings were also observed in Figure 27, disc WGWMD 1113, MID and AFT locations. In addition, the two discs do not show similar behaviour for the various locations, which would have been expected if there was a trend in material properties for a certain location. In Figure 28 the fitted curves, per location, are grouped closer together although the MID results tend to be somewhat lower.

In reviewing the above obtained location relationships all results seem to suggest that there is no apparent material inhomogeneity in relation to LCF tatigue properties for the various locations studied in this analysis.

## 6.2 Flat double edge notched K<sub>p</sub> 2.2 specimens

### 6.2.1 Introduction

For the K 2.2 specimens both the life to crack initiation and the life to failure were determined. Life to crack initiation was defined as the number of cycles at which a 1.7 increase in potential drop value was obtained. The actual crack size for a 1.2 PD increment was estimated by breaking open one of the (dummy) specimens at the 1.7 PD increase level, as seen in Figure 29. The crack shape was semi-elliptical distribution areas depth of about 0.6 mm, with a surface length of 1.6 mm. and had a maximum crack depth of about 0.6 mm, with a surface length of 1.6 mm. All test data are presented in Table 4. The life to failure results for both discs are shown in

Figure 30. Again, unlike engineering convention but for commonality with the statistical analyses, the stress range as the independent variable is plotted on the horizontal axis whereas the cycles to failure are plotted on the vertical axis. Figure 31 shows the life to initiation and the life to failure for disc LWND 7200 only. Figure 30 shows that the spread in results for the K 2.2 specimens is smaller than for the LCF specimens. This effect is especially evident for the high stress levels. Another finding (see the LCF specimens. This effect is especially evident for the high stress levels. Another finding osce Table 4) is that life to initiation and life to failure are closely related. Furthermore the life to in-itiation, as defined, accounts for the greitest part (~ 85-95%) and the total life of the specimen. This occurs because of the fairly large crack size associated with an initiation level of 1% PD increment. Almost no difference in notched fatigue behaviour between the two discs was observed. However, in order to detect possible trends in material behaviour between the two discs, and hetween individual laboratories and disc locations, similar statistical analyses were performed as on the LCF data.

6.2.2 Statistical handling of the K 2.2 data An initial statistical analysis was performed on all data, excluding the run-outs (in total three), shown in Figure 32. The single data point at the highest stress range ( $\Delta \sigma = 1091$  MPa, N<sub>f</sub> = 38 cycles) af-iects the position (Å) and the line coefficient (B) (i.e. slope) of the median curve in the area of in-terest, the life regime between 1000 and 100,000 cycles. Following the procedure adopted for the LCF spe-cimens, this data point was omitted from all subsequent statistical analysis. The remaining data were

1.

again statistically analysed and the results are shown in Figure 33, together with the 95 % confidence interval for the median curve. As can be seen the linearity hypothesis for the median curve was determined to be correct in this life regime.

6.2.3 Statistical comparison of individual laboratories, discs and disc locations

Figures 34 through 45 show the outcome of the statistical analyses in which the following comparisons were made:

1. individual disc results with respect to the overall data,

2. individual laboratory results with regard to the respective disc data (and corresponding confidence intervals) and with regard to the overall data, and

3. various disc locations with regard to the respective disc data.

Figures 34 and 35 show the test data and fitted relationships including the 95 % confidence intervals, for discs WGMD 113 and LMMD 7200 respectively. The assumption of linearity for the median curve was justified, as can be seen from the statistical parameters. A comparison between the median curves of the two individual discs with the overall median curve for all results (Fig. 33) is shown in Figure 36. The individual median curves lie close to the overall median curve and, in addition, line-crossing was observed. Both facts suggest that there is no apparent difference in the notched fatigue behaviour of the two discs.

In Figure 37 the overall median curve and the median curve for disc WGWMD lills are shown and, in addition, the fitted curves for the six individual laboratories which tested this disc have been plotted. All individual curves iall within the 95 % confidence interval of the overall median curve. In Figure 38 a similar comparison is made, however, the overall curve and its associated confidence interval have been omitted and the 95 % confidence interval now relates to disc WGMMD lills only. Although some difference in line positions and coefficients can be observed there is no indication that the results of individual laboratories clearly fall outside the scatter band.

The individual laboratory curves for disc LMMD 7200 are shown in Figures 39 and 40. These curves have a wider spread than in the case of disc WGWD 1113. Figure 39 shows that not all individual curves fall completely within the 95 % confidence interval for the overall median curve. However, Figure 40 shows that these curves fall within the 95 % contidence interval of the disc median curve. Because of the small size of the individual batches no firm conclusions can be drawn about the significance of the variation in individual laboratory test results.

A comparison in notched tarigue behaviour between different locations in the discs was also made. Figure 41 shows the identification of the various radial and axial locations used in the subsequent analysis. Figures 42 and 43 show for both discs the comparison in fatigue behaviour of the radial locations with the median disc curves. Similar comparisons with respect to the various axial locations are shown in Figures 44 and 45. The results indicate that the variations between different disc 'ocations are very small; there is no apparent material inhomogeneity with respect to the notched fatigue properties for both discs.

6.3 Corner Crack (CC) and Compact Tension Type (CT) Specimens

#### 6.3.1 Data Analysis

Fatigue crack growth data from 33 corner crack and 35 compact tension type specimens were collected and analysed. Typically for each specimen data set, 50 pairs of crack length and excit count data were provided for the analysis. The data were provided in the as recorded condition in order to facilitate the use of a common smoothing technique.

Four smoothing techniques were considered for the da/dN analysis procedure: the secant method, the modified difference method, the seven point incremental polynomial method and the total polynomial method. The seven point incremental polynomial technique was ultimately chosen because there were sufficient numbers of data points available in each data set, the technique is recommended in the current ASIM standard or fatigue crack growth rate testing, Reference 11., and it possessed sufficient smoothing capability to identity possible trends in the data.

The seven point incremental polynomial method for computing da/dN as a function of  $\Delta K$  is described in detail in Reference (11), briefly the technique involves fitting a second-order polynomial oparabola) to sets of seven successive values of observed crack length. The form of the equation for the local fit of crack length is:

$$a_{1} = b0 + b1 \left(\frac{N_{1} - C_{1}}{C_{2}}\right) + bz \left(\frac{N_{1} - C_{1}}{C_{2}}\right)^{2}$$
  
where  $C_{1} = \frac{1}{2} - \left(\frac{N_{1} - 3}{C_{2}} + \frac{N_{1} + 3}{C_{2}}\right)$   
 $C_{1} = -1 - \left(N_{1} - \frac{N_{1} - 3}{C_{2}} + \frac{N_{1} - 3}{C_{2}}\right)$ 

 $C_2 = \frac{1}{2} \left( \frac{N_{i+3} - N_{i-3}}{1 - 3} \right)$ 

and b0, b1 and b2 are regression parameters. The rate of crack growth, da/dN, is obtained by taking the first derivative of the above equation with respect to N:

$$da_{1}/dN_{1} = -\frac{b_{1}}{c_{2}} + 2b_{2} \left(N_{1} - C_{1}\right)/C_{2}^{2}$$

The value of  $a_1$  is used for the calculation of the corresponding  $dK_1$ . The stress intensity solutions for the CT and CC specimens are described in Sections 3.3.3 and 3.4.4 of Appendix A respectively.

## 6.3.2 Fatigue Crack Growth Rate Description

In order to utilize the data generated in this analysis for design and life prediction efforts, a curve fitting model is usually applied to the data. A number of curve fitting models have been proposed to describe the signoidal shape of the crack growth rate curve. Miller and Gallacher [12] describe an ASTM round robin programme where ten different models were used. One of the most successful models and one of two models selected for this analysis is the table lookup procedure. In this technique tabulated values or dard AN and AK values are obtained at regular log da/AN intervals. To build the table, the data for each specimen geometry were combined and sorted by da/AN. At selected intervals of da/AN, the data were averaged and a mean da/AN and  $\Delta K$  values estimation of the mean performance of the data sthus obtained. The mean crack growth curves are described by 36 pairs of data for the corner crack specimen geometry and by 32 pairs of data for the compact tension specimen geometry. The mean data are also presented in Tables 5 and 6. Standard deviation data for da/AN and also so and b. Standard deviation data for da/AN and also so and b. Standard deviation data for da/AN and also so and b.

A second model utilized to describe the crack growth behaviour is the power law or Paris model [13]. This model assumes that the crack propagation behaviour over discrete ranges of da/dN is linear and can thus be described by the equation:

 $da/dN = C\Delta K^{ii}$ 

To obtain the coefficients C and n, the crack propagation data in the assumed upper linear portion of the data were selected by specimen geometry and a least-squares regression line was fitted. The results are shown in Table 7 and in Figure 47. The fitted lines in Figure 47 show an excellent correlation with the mean data obtained using the table lookup model described above.

## 6.3.3 Test results

0	icat icadita	
Th	e data sets of	da/dN versus AK are presented in Figures 46 through 63:
Figure	46	The data for each laboratory are identified as a common group for interlaboratory comparisons,
Figure	47	Mean data and power law lines are presented for the two specimen geometries,
Figure	48	The CC data for the two discs are compared,
Figure	49	The CT data for the two discs are compared,
Figures	50 and 51	The data for the two discs, LWMD 7200 and WOWMD 1113, are compared, and
Figures	52 through 63	The data sets for each laboratory are compared to the combined mean data for the
		two specimen geometries, CC and Cl.

In figures 46 to 51, one trend in the data appears consistently. As evident in the mean data in Figure 47, the CT specimen produces a higher crack growth rate than the CC specimen, especially in the high  $\alpha$  4K ranges. The compact tension data are the more conservative of the two specimen geometries, At  $\alpha$ K = 16 MPaim the difference is a factor of 1.42 and at  $\alpha$ K = 40 MPaim the factor increases to 1.75. This effect was also noted for Ti-6Al-4V in Reference [8] using the same compact tension and corner crack specime geometries.

## 2. FRACIOGRAPHY

Fractographic investigations were carried out by QETE [14] and NLR on both CT and UC specimens. Striation spacings on the fracture surface determined by means of scanning electron microscopy have been compared with the macroscopically observed crack growth rates, determined by the PD method or by optical means. The results of the comparison are shown in Figure 64 for both a CT and a CC becimen. In Table 8 a detailed comparison is given for the CT-specimen.

The results indicate that in general, at the lower  $\Delta K$  values, the measured striation spacings are larger than the macroscopically determined cyclic crack growth by a factor of approximately 1.7. This situation is reversed at high  $\Delta K$  values. This behaviour may be explained by the following considerations. At lower  $\Delta K$  values striktions are difficult to observe. Only the larger ones tend to be found, resulting in an overestimation of crack growth rate. At higher  $\Delta K$  values non-cyclic crack growth, e.g. microvoid coalescence, can contribute such that striation spacing does not reflect the overall (higher) crack growth rate.

In figure 65 an illustration is given of the fractographic appearance of specimen CC 8 at various locations [14]. From these photographs it is clear that microscopic crack growth directions at the lower  $\Delta K$  values can deviate considerably from the macroscopic growth direction, indicating a strong micro-structural effect, at higher  $\Delta K$  values, microscopic crack growth aligns itself more with the overall crack growth direction.

## E. DISCUSSION

The major objectives of the CORE programme were:

 familiarisation of the participating laboratories with new test techniques, e.g. the potential drop technique and automated data collection;

standardization of test specimens and test techniques for engine disc materials;

- calibration of the participating laboratories to gain confidence in each other's results; and - material data collection, using Ti-fAl-4V, for verification of life prediction techniques used in

 material data collection, using Fi-bAl=4V, for verification of life prediction techniques used in damage tolerance design of engine discs.

The programme succeeded almost completely in the realization of the above objectives. Standard test specimens were selected and test techniques were developed and standardized. The participants, and in addition other laboratories, adopted the new test procedures for their own research programmes and even require that testing under contract be carried out according to the standardized procedures.

As all laboratories applied the same test procedures, their results could easily be compared. A detailed statistical analysis was performed to indicate possible deviating trends in individual laboratory test results. However, the analysis did not confirm any such behaviour. Individual iaboratory results iail within expected scatterbands and there was no obvious trend indicating a particular test outcome for

certain laboratories. This is an important result because the participants have now been mutually cali-brated, which will give confidence in each other's future test results without the need of continuous duplication.

In the current programme a large amount of data was generated, both in the LCF life area as well as in the crack propagation area. The data will be used as baseline data for the SUPPLEMENTARY programme in which the effect of subcycles, spectrum loading (simple and complex sequences) and different materials (with different grain size) will be investigated. At that stage the baseline test data will be used for Computing material behaviour and will serve as input for the various life prediction models to be applied. In the SUPPLEMENTARY programme the applicability and limitations of these models will be addressed.

In the SUPPLEMINTARY programme the applicability and limitations of these models will be addressed. The applied testing procedures, making use of PD measurement rechniques and automated data collect-ion, proved to be very effective. The accuracy of the system can be brought to a high level if good quality equipment is used, together with a careful PD-instrumentation of the specimens. Ultimately a better than 5 µm crack length sensitivity could be obtained for CC-specimens and about a 10 µm sensitivity for CT-specimens. It should be realized that this accuracy is based on the real average crack length. Even if the same accuracy could be realized with optical measurements the PD-method would still be in favour because the optical method only provides a surface crack length. The difference in crack sizes obtained can be quite large; with the CT-specimens differences of about 1 mm in crack length between the surface and the average value were measured.

#### CONCLUSIONS 9.

- 1. Standardization of test specimens and testing procedures allowed comparison and calibration of participating laboratories.
- The statistical analysis of all test results indicated no deviating test outcome for individual laboratories. All laboratories fall within expected scatterbands.
- The CORE programme collaborative effort generated a large amount of data in both the LCF area and the crack propagation area. The data will be used as baseline data for the SUPPLEMENTARY programme and serve as input for the life prediction models to be applied at that stage.
- The two specimen types, CT and CC, provided fatigue crack growth information for through thickness and surface/corner crack flaw geometries. 4.
- The fatigue crack growth data results indicated that the CC crack growth rate data were between 30 to 50 percent slower than the CT data for given values of AK between 15 and 35 MPa/m. Two numerical techniques, the table lookup procedure and the Paris law technique, proved suitable as 5.
- 6. curve fitting models.
- The PD technique is extremely accurate in measuring small tlaw sizes in the CC-specimen geometry. A crack length measurement sensitivity down to 5  $\mu$ m s  $^{-1}$  be realised. 7.

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Type of test Test specimen Number of specimens		LCF life / cr	ack formation	Crack propagation		
		Smooth cylindrical	tlat notched   K <sub>t</sub> = 2.2	corner crack	ASTM CT	
		6 h		f	j	
potentia CRACK drop			+	+	+	
DETECTION TECHNIQUES	optical			+		
χo	al	total life	tetal life + initial crack termation	"short" craek range	total da/dN - AK curve	

TABLE 1 CORE Programme test matrix

Note: All tests conducted at room temperature

		TABLE 1	2		
Minimum	specified and	measured	material	properties	for
	the	two discs.	tested		

Mate	rial specification	Minimum t	measured values
	minimum value	disc WGWMD 1113	disc LWMD 7200
Room temperature			
tensile strength, MPa	900	949	969
0.2% yield strength, MPa	830	856	865
% elongation	10	11.0	. 11
% reduction in area	25	29.9	26
150 °C tensile strength, MPa	770	799	819
0.2% yield strength, MPa	650	672	692
% elongation	14	15	14
% reduction in area	35	34.4	41
rotating bend fatigue test			
10 <sup>7</sup> cycles, MPa	440*	460	4-+0
LCF tatigue test, $R = 0$			
10 <sup>4</sup> cycles, MPa			
bore	772	890	870
web	772	835	860
rim	77.2	772	890
3/2			
fracture toughness, MN/m <sup>3/2</sup>	49.5	53.7	52.3

\* minimum value not specified; target minimum is 440 MPa.

.1

# TABLE 3 Fatigue life test results on LCF specimens (R=0.1)

# DISC WOWMD 1113

laboratory	specimen no.	stress amplitude ∆o MPa	cycles to failure <sup>N</sup> t	laboratory	specimen no.	stress amplitude Δο MPa	cycles to failure <sup>N</sup> f
UT	LCF 2 LCF 6 LCF 4 LCF 5 LCF 1 LCF 1	800 800 775 775 750	2850 2340 4790 5150 13540	KR	LCF 33 LCF 35 LCF 36 LCF 34 LCF 38 LCF 37	878 828 788 788 742 742	3 437 5067 5687 21217 14515
QE	LCF 19 LCF 16 LCF 18 LCF 17 LCF 17 LCF 14 LCF 15	800 775 775 750 750 760	3509 5665 7050 8851 12484 40343	NL	LCF 23 LCF 21 LCF 25 LCF 22 LCF 20 LCF 24	875 800 775 775 750 750	<1 3151 8605 7264 9457 19426
NR	LUF 12 LCF 7 LCF 9 LCF 8 LCF 10 LCF 11	800 800 750 750 725 700	1800 1900 12100 8800 18500 42000	RA	LCF 31 LCF 27 LCF 28 LCF 32 LCF 29 LCF 30	880 790 750 750 720 720	<1 5982 8545 13284 22474 15209

# DISC LWMD 7200

AF	LCF 19 LCF 18 LCF 16 LCF 14 LCF 14 LCF 17 LCF 15	800 775 775 750 750 750	3928 4672 5632 16140 25933	CE	LCF 33 LCF 35 LCF 36 LCF 34 LCF 38 LCF 37	878 837 788 788 742 742	40 3136 8508 5440 >16262 23076
ND	LCF 5 LCF 2 LCF 3 LCF 6 LCF 4 LCF 1	825 800 775 750 725 -	3831 6235 8174 21709 41222	IA	LCF 27 LCF 29 LCF 30 LCF 32 LCF 28 LCF 31	878 878 810 810 742 742	1158 348 3298 4466 12805 14656
NS	LCF 9 LCF 8 LCF 7 LCF 12 LCF 10 LCF 10 LCF 11	809 809 779 766 751 747	2679 2350 5510 11016 8156 11327	PI	LCF 22 LCF 23 LCF 24 PCF 25 LCF 20 LCF 21	800 800 775 775 750 750	3071 2472 6874 4724 9964 7540

labo- ratory	specimen no.	stress amplitude Δσ MPa	cycles to "1% crack initiation" N <sub>i</sub>	cycles to failure N <sub>t</sub>	labora- tory	specimen no.	stiess amplitude Ac MPa	cycles to "12 crack initiation" <sup>N</sup> i	cycles to tailure N <sub>f</sub>
UT	Kt 5 Kt 1 Kt 4 Kt 4 Kt 6 Kt 3	775 775 625 625 475 475	3420 4202 8484 10630 22764 31717	3476 4247 8920 10999 23856 33026	ĸĸ	K 36 Kt 40 Kt 35 Kt 39 Kt 37 Kt 38	700 562 562 562 486 486	5950 6700 13000 17500 20500 34000	6700 7900 14000 19500 23500 36500
QF.	K 17 Kt 14 Kt 15 Kt 13 Kt 18 Kt 18 Kt 16	775 775 625 525 475 475	3501 3301 - 7701 41686 36601	3701 3726 10952 8826 43730 38826	NL	Kt 25 Kt 26 Kt 23 Kt 24 Kt 27 Kt 28	775 775 625 625 475 475	3026 3301 16941 16207 27101 21501	3557 3714 18584 11436 29352 34118
NR	K 10 K 5 K 7 K 11 K 8 K 7 K 12	775 775 625 625 475 475	2707 2750 10090 8875 29500 38500	2771 2841 11191 8921 30061 39551	KA	Kt 31 Kt 32 Kt 29 Kt 33 Kt 30 Kt 34	775 775 625 625 475 475	2832 3023 11357 11349 48748 256511	3288 3810 17342 12176 51337 256511

# TABLE 4 Fatigue life test results on K<sub>t</sub> 2.2 specimens (R=0.1)

DISC WGWND 1113

# DISC LWMD 7200

AF	K 14 Kt 13 Kt 17 Kt 16 Kt 18 Kt 18 Kt 15	775 775 625 625 475 475	2037 2704 8131 9043 21775 59499	2334 3039 9254 9768 23053 61568	CE	Kt 38 Kt 35 Kt 37 Kt 39 Kt 40 Kt 36	698 562 562 428 428 -	4691 19832 13811 201594 36500 -	5230 20599 14953 211330 40190
ND	K t K t 5 K t 4 K t 6 K t 2 K t 3	775 625 625 475 475 -	2150 5850 9200 46950 27300 -	2765 6038 10258 48995 29800	lA	Kt 32 Kt 33 Kt 34 Kt 31 Kt 36 Kt 29	780 776 627 616 528 475	2040 2510 6550 7340 12300 863756	2466 3639 7317 9040 13180 >63750
NS	Kt 9 Kt 12 Kt 7 Kt 8 Kt 11 Kt 10	775 775 625 625 500 500	4050 2575 9200 8950 27000 25100	4340 2890 9660 9810 29350 27120	ΡI	Kt 26 Kt 23 Kt 27 Kt 28 Kt 24 Kt 24 Kt 25	1091 775 625 625 550 471	28 3010 5964 7888 17024 *55197	38 3182 6800 8855 17933 255197

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da/dN m/cycle	Std.dev. m/cycle	∆K MPa√m	Data Sets	da/dN m/cycle	Std.dev. m/cycle	∆K MPa√m	Data Sets
5.92E-09	1.41E-09	12.50	11	4.91E-07	1.40E-08	28.00	40
1.08E-08	1.42E-09	12.89	40	5.47E-07	1.94E-08	29.04	40
1.51E-08	1.01E-09	13.43	40	6.11E-07	1.77E-08	30.21	40
1.99E+08	1.85E-09	13.78	40	6.64E-07	1.44E-08	31.03	40
2.95E-08	4.19E-09	14.22	40	7.28E-07	1.97E-08	32.58	40
4.33E-08	4.11E-09	15.06	40	7.98E-07	1.96E-08	33.65	40
6.49E~05	6.58E-09	16.07	40	8.65E-0/	1.82E-08	34.72	40
9.10E-08	7.81E-09	17.33	40	9.44E-07	2.99E-08	35.93	40
1.15E-07	8.78E-09	18.31	40	1.05E-06	3.17E-08	36.78	40
1.4/E-U/	9.10E-09	19.46	40	1.17E-06	3.55E-08	37.77	40
1.75E-07	7.94E-09	20.19	40	1.31E-06	4.80E-08	39.32	40
2.04E-07	L.04E-08	21.66	40	1.47E-06	5.29E-08	40.83	40
2.46E-0/	1.15E-08	22.48	40	1.67E-06	6.79E-08	42.12	40
2.79E-07	9.83E-09	23.07	40	1.88E-06	7.01E-08	43.83	40
3.12E-07	9.31E-09	24.48	40	2.12E-06	7.97E-08	45.13	40
3.55E-07	1.45E-08	25.06	40	2.44E-06	1.09E-07	46.41	40
4.02E-07	1.22F-08	26.19	40	2.89E-06	1.69E-07	48.42	40
4.47E-0/	1.32E-08	27.66	40	4.10E-06	6.49E-07	51.16	40

TABLE 5 Mean failgue crack growth rate data for CC specimens 1247 Data Sets

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TABLE 6 Mean fatigue crack growth rate data for UT specimens 1365 Data Sets

da/dN m/cycle	Std.dev. m/cycle	∆K MPa√m	Data Sets	da/dN m/cycle	Std.dev. m/cycle	∆K MPa√m	Data Sets
6.50E-09	1.19E-09	10.98	39	2.68E-07	6.95E-09	20.90	40
1.22E-08	2.45E-09	12.30	40	2.93E-07	8.35E-09	21.31	40
2.15E-08	3.04E-09	12.42	40	3.25E-07	9.70E-09	22.14	40
3.64E-08	5.21E-09	13.70	40	3.58E-07	1.01E-08	22.94	40
5.39E-08	4.86E-09	14.84	4Ū	4.01E-07	1.19E-08	23.61	40
7.40E-08	6.64E-09	15.15	40	4.49E-07	1.56E-08	24.65	40
9.39E-08	4.90E-09	16.16	40	5.04E-07	1.65E-08	25.87	40
1.08E-07	3.57E-09	16.18	40	5.58E-07	1.88E-08	26.65	40
1.19E-07	3.87E~09	16.98	40	6.34E-07	2.68E-08	27.66	40
1.33E-07	3.91E-09	17.21	40	7.53E-07	3.61E-08	29.07	40
1.45E-07	5.00E-09	17.64	40	9.08E-07	5.54E-08	30.77	40
1.64E-07	6.08E-09	18.30	40	1.12E-06	6.64E-08	32.29	40
1.80E-07	3.95E-09	18.48	40	1.29E-06	7.07E-08	33.28	40
1.98E-07	6.32E-09	19.06	40	1.75E-06	1.73E-07	35.97	40
2.19E-07	8.78E-09	19.90	40	2.84E-06	6.75E-07	38.62	40
2.47E-07	7.26E-09	20.27	40	5.24E-06	1.55E-06	42.14	8
	1						

TABLE 7 Power law FCGR data

Specimen geometrv	Applicable da/dN range (m/cycle).	с	n
CT	8.26E-08 to 1.20E-06	8.3979E-12	3.395
CC	1.80E-07 to 1.96E-06	2.5987E-14	2.951

TABLE 8 Comparison between measured striation spacing and calculated macroscopic growth rate based on PD-data for specimen CT 12 (disc WGWAD 1113)

Distance from notch (mm)	∆K MPa√m	Striation spacing (um) measured from tracture surface at:				Macroscopic crack growth	Relation between macroscopic growth	
		ŧw	1 1	1 W	mean value	PD-data	striation spacing	
1	15.0	0.084		0.054	0.069	.046	0,52	
1.5	15.8	0.103		0.087	0.095	. 065	0.68	
2.0	16.6	0.150	0.177	0.690	0.139	.085	0.61	
2.5	17.5	0.164	0.168	0.155	0,162	.112	0.69	
3.0	18.3	0.152	0.198	0.217	0.189	.141	0.75	
3.5	19.3	0.178	0.277	0.277	0.244	.161	0.66	
4.0	20.3	0.284	0.291	0.221	0.265	.187	0.71	
4.5	21.3	0,235	0.325	0.335	0.298	, 215	0.72	
5.0	22.5	0.245	0.398	0.504	82د.0	.251	0.66	
5.5	23.7	0.297	0.342	0.322	0.320	.281	0.88	
6.0	25.0	0.417	0.355	0.414	0.395	.315	0.80	
6.5	26.5	0.291	0.462	0.493	0.415	.418	1.01	
7.0	28.2	0.459	0.455	0.568	0.494	. 512	1.04	
7.5	30.0	0.453	0.660	0.723	0.612	.577	0.94	
8.0	32.1	0.612	0.881	0.726	0.740	.682	0.92	
8.5	34.4	0.657	0.702	0.918	0.759	.807	1.06	
9.0	36.8	0.902	0.781	1.10	0.929	.986	1.06	
9.5	39.7	1.77	1.06	1.45	1.43	1.29	0.90	
10.0	43.0	1.12	1.12	0.974	1.08	1.70	1.57	
10.5	46.8	1.21	1.70	1.33	1,41	2.4	1.70	
11.0	51.4	2.27		2.05	2.16	3.7	1.71	

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Fig. 1 Schematic of damage tolerance lifing approach



Depolished in axial direction  $\frac{1.6}{100}$  (0.8) BREAK CORNERS

a) CYLINDRICAL UNNOTCHED LCF SPECIMEN







b) FLAT DOUBLE EDGE NOTCHED SPECIMEN (K  $_1 \approx 2.2$ )

GAUGE LENGTH TO BE CONCENTRIC WITH THREADED ENDS AND TO HAVE SURFACE FINISH 0.4



d) CORNER CRACK SPECIMEN

c) CT-SPECIMEN

Fig. 2 Specimens used in the programme



Fig. 3 Disc cut-up drawing indicating location of each specimen for the AGARD engine disc programme 3a Overview of specimen positions



SPECIMEN TYPE		Ţ	BLANK SIZE	į.	QUANTITY	POS	-NOS	SECTIONS
SMOOTH CYLINDRICAL	LCF	•	90+2350.000		39	1	39	00
DOUBLE EDGE NOTCHED	×,22	•	85+18 SQ mm	•	14	1	44	сс
ASTM COMPACT TYPE	CT.	•	36+34+15 mm	•	23	. –	21	вB
COPNER CRACK	ÇÇ.	:	93×73 \$0 mm	Ì	26	1	26	ΔA



Fig. 3 Continued. 3b Cross-sections showing individual specimen positions

[	DISC WG	WMD 1113		DISC LWMD 7200				
SET No	LABORATORY	TYPE	POSITION	SET No	LABORATORY	TYPE	POSITION	
		LCF	1.6	7	ND	LCF	2 6.13	
		K, 22	1-6			K, 2.2	16	
1	UT	C1	1.3			СТ	1 - 3	
		CC	4.6			CC	1-3	
	NR	LCF	7-12	8	NS	LCF	: 7.12	
2		K, 22	7-12			K, 22	7 12	
		CT	4-6			CT	4-6	
		CC	1-3			СС	4-6	
··	•	LCF	14-19	9	AF	LCF	14 19	
		K, 2.2	. 13 18			к, 22	13 18	
3	or	ст	7.9			СТ	7 9	
		сс	79			cc	7 9	
		L C F	20 25	10	PI	LCF	20 25	
		K, 2.2	23 28			K, 22	23-28	
4	NL	CT	, 10 12			CT	1ū-12	
í.		cc	14- 'ô			ĊĊ	14 16	
		LCF	27 32	11	IA	LCF	27 - 32	
5	RA	κ,22	29 34			K, 2 2	29-34	
		ст	13 15			CT	13-15	
		cc	17 19			CC	17 19	
6	RR	I CF	33 38	12	CE	LCF	33 38	
		K, 22	35 -40			K, 22	35-40	
		ст	16 18			ст	16 18	
		cc	20 22			сс	20 22	







Fig. 4 Microstructure of Ti-6Al-4V disc material, showing equiaxed  $\alpha$  (white phase) in a transformed  $\beta$  matrix (dark phase) containing coarse, actual  $\sigma$ 

Fig. 5 Microstructure of Ti-6A1-4V disc material showing occasional α-alignments



Fig. 6 Preparation of slices from CC specimens for texture measurements



Fig. 7 -0002 . Pole figures indicating texture variation in the disc, disc LWMD 7200



Fig. 7 (cont.)  $\geq 110^{\circ}$  Pole figures indicating texture variation in the disc; disc LWMD 7200



Fig. 8  $^{+}0002^{+}$  Pole figures indicating texture variation in the disc; disc WGWMD 1113

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Fig. 8 (cont,)  $\pm 110^{\pm}$  Pole figures indicating texture variation in the disc; disc WGWMD 1113

2.3



Fig. 9 Instrumentation for fatigue testing and crack growth measurement



Fig. 10 Potential drop instrumentation of dummy corner crack specimen. The 50 ...m diameter notch probe wires are located on hoth sides of a 100 ...m deep starter notch (not visible). N.B. For actual test specimens the reference probes should not be welded on the same edge (see text)









Fig. 13 Markings on fracture surface of corner crack specimen

2.5



Fig. 14 Fatigue life test results for LCF specimens



Fig. 15 Fitted relationship between fatigue life and stress range for all LCF data on both discs; 95% confidence interval for the entire median curve is also indicated



Fig. 16. Fitted relationship between fatigue life and stress range for all LCF data in the appropriate stress range, life regime (see section 6.1.2).



Fig. 17 - Fitted relationship between fatigue life and stress range for the WGWMD 1113 disc data


Fig. 18 Fitted relationship between fatigue life and stress range for the LWMD 7200 disc data



Fig. 19 Comparison of the fitted linear relationships for the individual discs with the overall fitted curve. The  $95^{4}$  confidence interval is for the overall curve



Fig. 20 Comparison between the overall median curve for both discs, the median curve for disc #GWMD 1113 and the fitted curves for the 6 associated individual laboratories. The 95% confidence interval relates to the overall curve



Fig. 21 Comparison between the median curve (and associated 95% confidence interval) for disc WGWMD 1113 and the individual laboratories

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Fig. 22 comparison between the median curve for both discs, the median curve for disc LWMD 7200 and the fitted curves for the 6 associated laboratories. The 955 confidence interval relates to the overall curve.



Fig. 23 Comparison between the median curve (and associated 95% confidence interval) for disc LWMD 7200 and the individual laboratories

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Fig. 24. Selection of specimens for control of material property variations in radial and axial directions.



Fig. 25 Comparison between various radial locations in the disc with the disc median larve and its associated 957 confidence interval



Fig. 26 Comparison between various radial locations in the disc with the disc median curve and its associated 95° confidence interval



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Fig. 27 Comparison between various axial locations in the disc with the disc median curve and its associated 95° confidence interval



Fig. 28. Comparison between various axial locations in the disc with the disc median curve and its associated  $95^\circ$  confidence interval



Fig. 29. Size of the fatigue crack at a 1° increase in PD-level for the  $K_{\rm f}$  2.2 specimen



Fig. 30. Test results  $K_{\frac{1}{2}}(2,2)$  specimens; life to failure



Fig. 31. Test results K  $_2$  .2 specimens, fisc LWMD 7200 only. Both initiation life and life to failure are indicated



Fig. 32 Fitted relationship between fatigue life and stress range for all K  $_{\rm L}$  2.2 data. The 95% confidence interval has also been indicated



Fig. 33 Fitted relationship between fatigue life and stress range for all K 2.2 data in the appropriate life regime; the 95% confidence interval for the median curve is also indicated



Fig. 34 Fitted relationship between fatigue life and stress range for the WGWMD 1113 disc data



Fig. 35 Fitted relationship between fatigue life and stress range for the LWWD 7200 disc data



Fig. 36 Comparison of the fitted median curves for the individual discs with the overall median curve. The 951 confidence interval relates to the overall curve



Fig. 37 - imparison between the overall median curve for both discs, the median curve of disc WGWMD 1113 and the fitted curves for the 6 associated indi idual laboratories. The 957 confidence interval relates to the overall curve.



Fig. 38 Comparison between the median curve (and associated 95% confidence interval) of disc WGWMD 1113 and the curves for the individual laboratories



Fig. 39 Comparison between the overall median curve for both discs, the median curve of disc LWMD 7200 and the fitted curves for the 6 associated individual laboratories. The 955 confidence interval relates to the overall curve



Fig. 40 Comparison between the median curve (and associated  $95^\circ$  confidence interval) of disc LWMD 7200 and the curves for the individual laboratories



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Fig. 41 Selection of specimens for control of material property variation in radial and axial directions



Fig. 42 Comparison between various radial locations in the disc with the disc median curve and its associated 95% confidence interval



Fig. 43 Comparison between various radial locations in the disc with the disc median curve and its associated 95% confidence interval



Fig. 44. Comparison between various axial locations in the disc with the disc median curve and its associated 951 confidence interval



Fig. 45. Comparison between various axial locations in the disc with the disc median curve and its associated 95° confidence interval











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Fig. 64. Comparison between measured scription spacing and macroscopic crack growth rates for specimens CT 12 and CC 8 (disc WGWMD 1113).





RIGHT SIDE OF CRACK SURFACE AT a = 0.6 mm  $(\Delta K = 17.3 \text{ MPa}\sqrt{m})$ 



LEFT SIDE OF CRACK SURFACE AT a = 2.14 mm  $(\Delta K = 33.2 \ MPa\sqrt{m})$ 

45<sup>0</sup> LINE AT a = 2 78 mm {ΔK = 36.7 MPa√m}



 $45^{\circ}$  LINE AT a = 4 23 mm ( $\Delta K = 51.4 \text{ MPa}\sqrt{m}$ )



RIGHT SIDE OF CRACK SURFACE AT a = 4 23 mm  $(\Delta K = 55.6 \text{ MPa}\sqrt{m})$ 

Fig. 65 Fractographic appearance of specimen CC 8

#### NLR TR 86019 L

## REVISED WORKING DOCUMENT FOR THE AGARD COOPERATIVE TEST PROGRAMME ON TITANIUM ALLOY ENGINE DISC MATERIAL by A.J.A. Moma

## SUMMARY

This revised working document provides a detailed lay-out for the tests to be performed in the AGARD cooperative test programme on titanium alloy engine disc material.

#### CONTENTS

- 1 INTRODUCTION
- 2 SPECIMENS
- 3 TEST PROCEDURES
  - 3.1 Smooth cylindrical specimen
  - 3.1.1 General
    - 3.1.2 Test conditions
  - 3.2 Flat double edge notched specimen

    - 3.2.1 General 3.2.2 Loading axiality 3.2.3 Procedure for PD instrumentation and
    - measurement
  - 3.2.4 Test conditions 3.3 Compact Type (CT) specimen
    - - 3.3.1 General 3.3.2 Procedure for PD instrumentation and
      - measurement
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    - 3.4.1 General
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    - 3.4.3 Procedure for PD instrumentation and
    - measurement
    - 3.4.4 Test conditions
- 4 FORMAT FOR THE DELIVERY OF TEST RESULTS
- 5 REFERENCES

2 tables

15 figures

#### 1. INTRODUCTION

This report provides a working document for the actual test procedures of the AGARD Engine Disc This report provides a working document for the actual test procedures of the AGARD Engine Disc Material Testing programme. A<sub>i</sub>art from the specimen design and testing procedure, the report includes a detailed description of the potential drop (PD) measurement system. The standard test procedure as de-scribed herein is the basis for the collaborative testing as performed in the AGARD CORE programme, for which the objectives and goals have already been presented [1]. Table Al shows the testing matrix of the CORE programme.

2. SPECIMENS

Four standard test specimens have been selected, two for LCF - - esting and two for crack propagation testing:

smooth cylindrical specimen, K = 1, LCF-life, see Figure Al-a;

Smooth Cyllingfical specimen, K = 1, Lorlite, See Figure Al-a, flat double edge notched specimen, K = 2.2, LCF-life, see Figure Al-b; ASTM CT (compact type)-specimen, crack propagation, see Figure Al-c; Corner crack (CC)-specimen, crack propagation, see Figure Al-d.

All spectatenes for the CORE programme have been machined at one location from Ti-bAl-4V material, which was obtained from disc forgings, delivered by Rolls Royce, Derby. The orientation of the specimens was selected in such a way that the envisioned crack plane corresponded to the crack plane to be expected in service i.e. radial and perpendicular to the disc plane.

- 3. TEST PROCEDURES
- 3.1 Smooth cylindrical specimen (Figure Al-a)
- 3.1.1 General

Simple LCT lift tests will be performed on this specimen. Check firstly the loading axiality of the test bench/specimen combination by the measurement of axial strains on opposite sides of the specimen test section under elastic loading conditions. The loading axiality is considered acceptable if the maximum difference in these strains is below 5.7.

3.1.2 Test conditions

- i. Laboratory air, room temperature.
- 2. Trapezoidal loading waveform; R = 0.1, f = 0.25 Hz; see Figure A2.

. Selection of stress levels:

Based on available Ti-6Ai-4V LCF-life data (see Figure A3) it is estimated that for anticipated lives of 2000, 7000 and 25000 cycles the following stress levels should be chosen. (Note: selected stress levels refer to the low end of the scatterband because actual testing is to be performed at R = 0.1, while the data in Figure A3 are for R = 0.1.):

N (cycles)	stress range (MN/m <sup>2</sup> )
2000	850
7000	800
25000	750

Tests should start at the 750  $MN/m^2$  stress level. Select additional stress levels (based on the initial test result) to obtain data for the total 2000 – 25,000 cycles range. Note: test preferably two specimens at each stress level!

4. The 0-€ hysteresis loop should be identified (recorded) for each specimen at each stress level. The 0-€ loop changes especially during the very early portion of the fatigue life (perhaps only the first few cycles). Thereafter a steady state condition is reached. Try to record a number of c-€ loops until steady state conditions exist. The results may later be used for deriving various life relations. The storage of the hysteresis data may be done in a plotted format or digitised for follow-on computer analysis.

#### 3.2 Flat double edge notched specimen (Figure Al-b)

3.2.1 General

Simple LCF tests will be performed on this specimen; however, apart from the number of cycles to failure the number of cycles to "initiate" a certain crack will also be measured. Crack initiation is determined by using the potential drop (PD) measurement technique which is able to register small cracks.

#### 3.2.2 Loading axiality

Check the loading axiality of the test frame/specimen combination by the measurement of axial strains on the opposite surfaces under elastic loading conditions. The loading axiality is considered acceptable if the maximum difference in strains is 5 %.

3.2.3 Procedure for PD instrumentation and measurement (Figure A4)

- Attach at each notch one set of potential probes diagonally at opposite corners. Use Ti-wire (for
  reasons of convenience Pt-wire might also be used) with a diameter of ca. 0.3 0.5 mm.
  Weld the wire exactly at the corner so that the contact area is not greater than 0.5 x 0.5 mm
  - (Figure A4) Welding equipment which may be used is e.g.:

crack initially) can be used as the reference.

- from Hughes Aircraft Systems (Weybridge Surrey, UK): MCW 550 MC power supply + VTA-90 weld head, or:
- from Unitek, California: type 125 power supply + type 32F weld head.
- The Ti-wires will probably be connected to (Cu) potential cables which are connected to the voltmeter. Ensure that the two dissimilar metal joints (Ti/Cu) for each set are at the same temperature in order to avoid thermally induced voltages.
- 3. Apart from the two notch voltages a reference voltage should also be measured. Attach the T<sup>2</sup>-wire reference leads to the reference block as indicated in Figure A4. The reference block is made out of the same material as the specimen (in this case Ti-6Al-4V). Mount the reference block to the machine trame close to the specimen. Note: It may be difficult, because of limited equipment capabilities, to measure 3 voltages (2 notch voltages in the reference voltage). In that case one of the notch voltages (the one which does not
- 4. Design a system which is suitable to realise a uniform current distribution through the specimen. Individual laboratories may choose their own approach tailored to their equipment capabilities. Figure A4 shows one of the possibilities for a current input system.
- 5. Check for good insulation between specimen and machine frame.

- Measure the notch and reference PD values during the test at both current on and current off conditions (Figure A5). Correct the "current on" values with the "current off" values.
- 7. Plot the normalized notch voltages (v<sub>notch</sub>/v<sub>ref</sub>) versus cycles and determine the crack formation life value, for this purpose defined as the number of cycles at which the normalized notch voltage is 1 % above the initial value. Note that fluctuations in V<sub>ref</sub> (e.g. due to noise) may obscure the 1 % level (this is especially the case if v<sub>ref</sub> is relatively small compared to V<sub>notch</sub>). In that case it would be appropriate to neglect V<sub>ref</sub>, provided that the fluctuations are not the result of temperature or current variations.
- 8. Assure that during the fatigue test enough voltage readings are made to enable an accurate cyclic life determination at the 1 % increase level of the normalized potential.
- 9. Preliminary tests showed that a 1 % increase in PD value corresponded with a crack of 0.6 mm depth and 1.75 mm surface length.

3.2.4 Test conditions

- 1. Laboratory air, room temperature.
- 2. Trapezoidai loading waveform; R = 0.1; f = 0.25 Hz, see Figure A2.
- 3. Selection of stress levels.

Based on available Ti-6A1-4V notched LCF life data (see Figure A6 for K = 2.5) the following nominal stress levels are chosen for anticipated total lives of respectively 2000, 7000 and 25000 cycles:

nominal stress range (MPa)
775
625
'>

Note that the data indicated in Figure A6 refer to a specimen with a K of 2.5 whereas the flat double edge notched specimen contains two notches with a K of 2.2. Adjust the applied stress ranges if test results show this to be necessary. Test two specimens at each stress level; begin with the 625 MPa level.

3.3 Compact type (CT) specimen (Figure Al-c)

3.3.1 General

Crack propagation tests will be performed on this specimen using the same trapezoidal waveform as already mentioned before. Crack length measurement is carried out by using the PD technique, making use of a calibration formula.

3.3.2 Procedure for PD instrumentation and measurement (see also Figure A7)

- 1. Drill and tap holes (M3) and attach current input and output studs at the locations indicated in Figure A7. The stud 'ocation must be checked and should be within 0.2 mm.
- 2. Attach current leads also to the reference block. The reference block must be of the same material as the specimen.
- 3. Check for good insulation between specimen and machine frame (infinite resistance). The specimen may be insulated by insulation of the loading pins within the clevis or by insulation of the clevis to the machine, e.g. by attaching the (threaded end of the) clevis to the swivel as e.g. shown in Figure A4.
- 4. Weld PD wires to the edge of the notch at diagonally opposite corners. Use Ti-wire with a diameter of about 0.3 - 0.5 mm. Ensure that the contact area of the weld is not greater than 0.5 x 0.5 mm. For reasons of convenience Pt-wire may also be used instead of Ti-wire. Ti-wire, however, diminishes thermal voltages.
- 5. Attach the Ti PD wires to the potential cables which are connected to the voltmeter. Ensure that the two dissimilar metal joints are at the same temperature to avoid thermally induced voltages.
- Measure the notch voltage and adjust current to give an initial voltage in the range 1.6 1.9 mV. This should correspond to a current of approximately 7.5 A.
- 7. Attach the reference wires (also Ti) to the reference block such that the measured PD is approximately equal to the notch voltage.
- Attach the reference wires to potential cables leading to the voltmeter. Ensure the same temperature at the two dissimilar metal joints.
- 9. Support all PD wires such that no weld failures will occur during the test.
- 10. Allow the PD signals to stabilise before the start of the test.

#### APPENPIX A

- 11. Record at the onset of the test the notch and reference PD values and the corresponding crack length for calibration purposes.
- Record during the test, at appropriate intervals, the notch and reference PD values. Data sampling 12. should be done such that at least 100 but no more than 500 data prints are recorded.
- 13. Record the final notch and reference PD values at the end of the test. Determine the final average crack length (see also point 14) on the fracture surface. The results are to be used for calibration purposes.
- 14. The final average crack length is easily determined by heat tinting (~ 30 min. at 500 °C; lower temperatures may also be spplied) and a subsequent tensile test resulting in specimentailure. If heat tinting is to be avoided, because e.g. the tracture surface will be used for detailed fractographic investigation, the final crack length can also be measured either in the scanning electron microscope or directly by optical means dependent on the visibility of the transition between the Latigue and overload area.
- 15. The final average crack length is determined by averaging 5 measurements taken at 0, 25, 50, 75 and 100 % of the specimen width.
- 16. Calculate the crack length for all data points, making use of the well known final crack length, out of the calibration curve (Figure A8  $\{2\}$ ) or the calibration formula:

$$\frac{V/V_{0}}{V_{ref}/V_{ref}} \approx A + A_{j} \left(\frac{a}{b}\right) + A_{2} \left(\frac{a}{b}^{2}\right) + A_{3} \left(\frac{a}{b}^{3}\right)$$
(1)

in which V = notch voltage ۰.

- notch voltage at the start of the test (crack size 0)

V re: = reference voltage

۲ ret<sub>o</sub> = reference voltage at the start of the test

with	А	÷	0.5766
	Α,	÷	1.9169
	A2	=	-1.0712
	A <sup>2</sup> 3	-	1.6898

or (in reversed notation):

$$-\frac{a}{\kappa} = B + B_1 \frac{v/v_o}{v_e ef} + B_2 \left[\frac{v/v_o}{v_r ef}\right]^2 + B_3 \left[\frac{v/v_o}{v_r ef}\right]^3$$
(2)

with

 $\begin{array}{rcl} 5 &= -0.5051 \\ B_1 &= & 0.8857 \\ B_2 &= & -0.1398 \\ B_3^2 &= & 2.398.10^{-4} \end{array}$ 

For example: with  $\left(\frac{a}{w}\right)_{\text{firal}}$  the value of  $\frac{V_{\text{firal}}/V_{\text{o}}}{V_{\text{ref}_{\text{firal}}}/V_{\text{ref}_{\text{o}}}}$  can be

calculated. Making use of the final, measured notch voltage ("inal), the final reference voltage ) and the initial reference voltage  $V_{ref_{in}}$  the value of the initial metch voltage  $V_{ref_{in}}$ (V ref<sub>finai</sub>

final (according to the calibration curve) can be calculated. This value may not correspond to the actually measured initial notch voltage, which may be due to an inaccuracy in final crack length measurement (or averaging method) or to the effect of plastic zone formation (see also point 18). Making use of this <u>calculated</u> initial motch voltage the crack length at every data point (V versus N) can now be calculated with equation (2).

- 17. The use of V may obscure the results if the noise level is high and if V ref is small compared to  $v_{notch}$ . In that case  $v_{ref}$  may be neglected provided that the fluctuations in  $v_{ref}$  are not the result of current or temperature variation.
- 18. During the initial part of the test on the CT-specimens the notch voltage will firstly increase and atterwards stabilize, see Figure A9. This is one of the reasons not to use the measured initial notch voltage for crack length calculation but instead the calculated initial notch voltage (see also point 16).

3.3.3 Test conditions

- 1. Laboratory air, room temperature.
- 2. Trapezoidal loading waveform (NB: see also point 6); R = 0.1; f = 0.25 Hz, see Figure A2.
- For Ti-disc materials we are especially interested in crack growth rates between approximately 3  $5.10^{-5}$  and  $10^{-3}$  mm/cycle. This refers to crack growth rates normally encountered in service. Therefore, and also based on Figure AlO (3], the  $\Delta K$ -values mentioned further on have been selected for the tests.
- 4. Precrack the first specimen at  $\Delta K = 13.5 \text{ MN/m}^{3/2}$  ( $\Delta 2 = 5.87 \text{ kN}$ ) and continue the test with the same load. Stop the test at  $\Delta k = 55 \text{ MN/m}^{3/2}$  ( $K_{max} = 60 \text{ MN/m}^{3/2}$ ); this corresponds with a crack length of about 11.5 mm.

Caution: because of the crack front curvature at the specimen surface the surface crack length underestimutes the average crack length. Therefore, build in some additional safety. For the calculation of the stress intensity factor the tollowing formula is used (valid for a/W between 6.2 and 1):

$$K_{I} = \frac{P}{B/W} \cdot f(a/W) \text{ where}$$

$$f(\frac{a}{W}) = \frac{2 + a/W}{(1 - a/W)^{3/2}} \{0.886 + 4.64a/W - 13.32(a/W)^{2} + 14.72(a/W)^{3} - 5.6(a/W)^{4}\}$$

to facilitate the calculation of  $K_{\tau}$ , values of f(a/W) are tabulated in Table A2 for specific values of a/W.

5. With the first specimen, starting at  $\Delta K = 13.5 \text{ MN/m}^{3/2}$ , the crack growth curve is determined for

growth rate values above  $10^{-4}$  mmm/ cycle. Extrapolate the crack growth curve to  $10^{-5}$  mmm/cycle and determine the corresponding  $\Delta K$  value. Start the test with the second specimen at this value and con-tinue (with the same load applied) the test until a/W = 0.65. The third specimen may be used to check the data already obtained with the two previous tests.

- Precracking and load shedding may be applied to prevent very long initiation times. If load shedding recracking and load shedding may be applied to prevent very ong initiation times, it load shedding is performed then this should be done according to ASTM E 647 (latest revision). Precracking is carried out using sinusoidal loading. During the actual uses trapezoidal loading should be applied; however, in the case of low crack growth rates, which seriously retard the test duration, sinusoidal loading (5 Hz) is also allowed. In that case the test should be stopped at high load and at regular intervals if so required for the PD measurements, see Figure All. Ensure that both current on and current of measurements are carried out when the current, and hence the signal, is sufficiently stabilised.
  - Compare the crack growth rates for the high and low frequency waveforms.
- 3.4 Corner crack (CC) specimen (Figure Al-d)

5.4.1 General

Crack propagation tests in the "physically" short crack regime will be performed on this specimen using the same trapezoidal waveform as already mentioned before. Crack length measurement is carried out by using the PD technique, making use of a calibration formula.

3.4.2 Loading axiality

Check the loading axiality of the test bench/specimen combination by the measurement of axial strains (under elastic loading conditions) on opposite surfaces. The loading axiality is considered acceptable if the maximum difference in strains is 5.7.

3.4.3 Procedure for FD instrumentation and measurement (see also Figure Al2) The procedure outlined below is based on a detailed Rolls Royce PD measurement procedure. Where necessary some minor deviations from this procedure have been made. Note: The PD technique is optional for this specimen! Crack growth should also be measured optically

(see further on, point 13).

- 1. Spot wold a 50 µm Ø titanium probe wire\* to each support wire, see Figure Al2. Heat input should be preferably lower than 0.5 Watt-second.
- 2. Assemble the 4 PD lead support wires\* in a ceramic holder using refractory cement. If desired the support wires may also be eliminated: twist in this case the two fine 50 um wires from the notch to the measurement points.
- Whenever possible the support wires and the PD probes should be of the same base material as the test piece; for this programme pure Ti-wires are recommended; however, Pt wires may also be used.
- Cement the ceramic block to one of the faces of the test piece not containing the notch and spot weld a probe wire on either side of the notch as shown in Figure Al2. It is critical for the probe wire to be located right on the edge of the notch because the PD calibration is strongly dependent 3. on z, the separation of the probes (see Figure Al3 [2]).

- 4. Spot weld the remaining wires to the test piece away from the notch as shown in Figure Al2. These will be used to monitor a reference potential. The reference wires may also be welded on one of the 3 edges not containing the notch.
- 5. Check each wire for good electrical connection.

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- Check that the specimen grips are fully insulated from the machine and that they are correctly aligned (see above). 6.
- Mount the specimen inc. the machine, being careful not to disturb the welds. 7.
- Attach current leads to the two specimen, or to another (e.g. the specimen grips) location assuring 8. good current uniformity (see also remarks about the flat double edge notched specimen)
- 9. Secure 2 thermocouples to test piece as shown in Figure Al2 (only optional, not necessary for COREprogramme).
- 10. Make the necessary connections (PD, thermocouple etc.) to the measurement system.
- 11. Switch current on: 15A. (If equipment capabilities do not allow this current then choose your own value.) At this current the PD value over the crack will increase from about 100 µV to over 2000 µV.
- 12. Allow the PD signals to stabilise.
- 13. Surface crack length measurements should in principle be carried out by optical means, e.g. by a travelling microscope arrangement. Don't use replicas because this may affect crack growth behaviour. The PD measurement system may be used solely if it turns out that the accuracy gained by the PD method is at least equal to the optical measurement accuracy. The resolution of the optical crack length measurement should be better than 0.05 mm. Try to avoid stopping the machine for crack length measurement; dwell effects at load can alter tatigue crack growth behaviour. Take photographs if this will help in crack growth measurement.
- 14. Start the test using a constant load amplitude and grow the crack to a/W = 0.5 maximum. Clearly this will be determined by the fracture toughness of the material.
- 15. Record at appropriate crack lengths the corresponding notch and reference PD values for current on and off conditions (Figure A5).
- 16. Avoid breaking the specimen juring the fatigue test. Stop the test at a/W = 0.5 maximum (this depends on  $K_{max}$ , see further) and measure the final motch voltage. This is necessary for obtaining the final notch voltage/crack length pair for calibration purposes. To prevent static crack growth during the final measurement it is recommended to stop the test at  $\Delta K$  = 55 MN/m<sup>3/2</sup> (or  $\kappa_{max} = 60 \text{ MN/m}^{3/2}$ ).
- 17. Measure the final average crack length on the fracture surface (and the initial crack length used in the calibration where possible). The optical measurement of the final crack length can easily be performed after heat tinting th specimen at the end of the test (e.g. 30 minutes at 500 °C although a temperature as low as 350 ° may also be used) and by a subsequent tensile test to failure.

Heat tinting may negatively affect the recognition of detailed features on the fracture surface of the specimen. If individual laboratories would like to perform a fracture surface investigation at is therefore recommended not to heat tint but to measure the final crack length in the scanning electron microscope, or by optical means if the distinction between fatigue and overload area can be easily recognised

- 18. The final average crack length is obtained by averaging 5 radial measurements taken at  $0^{\circ}$ , 22.5°, 45°, 67.5° and 90° starting from the crack corner.
- 19. The calibration procedure of notch voltage to crack length for the CC-specimer is as follows:
  determine the final, average crack length and the corresponding notch voltage;
  draw a straight line from this data point to the origin (this may be performed if 2/W << 0.05,</li> see Figure Al3);
  - compare the slope of this line to the slope of the calibration curve (Figure Al3).

3.4.4 Test conditions

- 1. Laboratory air; room temperature.
- 2. Trapezoidal loading waveform (N.B. see also point 5): R = 0.1: f = 0.25 Hz, see Figure A2.
- For Ti-disc materials in the "short" crack regime we are interested in crack growth rates between 3. approximately 5.10<sup>-5</sup> and 10<sup>-3</sup> mm/ cycle. This refers to crack growth rates normally encountered in service. Therefore select a  $\Delta K$ -value of about 15 MPa $\star$ m to start with at a  $\approx 0.5$  mm (see also point 6).

The stress intensity actor at the specimes surface can be calculated using the formula:

 $K_{I} = 1.16 - \frac{2}{\pi} \sigma \sqrt{\pi a}$ , approximately valid for  $\frac{a}{W} < 0.2$  surface

For higher values of  $\frac{a}{\omega}$  the formula has the following form:

$$K_{1_{surface}} = \begin{cases} 1.12 - 0.13 \ \frac{a}{W} + 1.84 \ \left(\frac{a}{W}\right)^{2} + 0.11 \left(\frac{a}{W}\right)^{3} + 0.8 \left(\frac{a}{W}\right)^{4} \left\{\frac{2}{\pi}, \sqrt{\pi a}\right\} \end{cases}$$

A graphical representation is given in Figure Al4 [4].

It is clear from this figure that the stress intensity factor at an angle of 45° is different from K surface. At a/W = 0.5 K  $_{45^{\circ}}$  is more than 10 T lane. Surface. Because the PD technique provides information on the mean crack size it is therefore logical to use also a mean K-value for the calculation of crack propagation data. The K<sub>mean</sub> is easily derived trom K<sub>surface</sub> as shown below.

Based on the data given in a paper of Pickard [5] the ratio between K and  $K_{45^c}$  has been plotted in Figure Al5. Assuming a quadratic curve through the data points (only for a/W > 0.5 is there some deviation) the value of  $K_{45^{\circ}}$  can be expressed in terms of K surface:

 $K_{45^{\circ}} = \{0.94 - 0.18 (a/W)^2\} K_{surface}$ 

The  $K_{mean}$ , for this purpose simply defined as  $\frac{K_{45^{\circ}} + K_s}{2}$  inface, is now easily derived:

$$K_{\text{mean}} = \frac{K_{45^{\circ}} + K_{\text{surface}}}{2}$$

= (0.97-0.09 (a/W)<sup>2</sup>}K surface.

For the tinal calculation of the test results the two above given equations for k surface  $\int_{a}^{b} \int_{a}^{b} \int_{a$ 0.2 and a/W > 0.2) should therefore simply be multiplied with the factor  $(0.97-0.09 (a/W)^2)$  to derive a K \_\_\_\_\_. In the following, for reasons of simplicity and also because the actual difference is only small, only the  $\rm K_{surface}$  values will be given for describing the test conditions.

5. Initiate a tatigue crack from the notch using an alternating stress of 540  $MN/m^2$  (Maximum stress =  $600 \text{ MN/m}^2$ ; R = 0.1). This corresponds to an alternating stress intensity at the side surfaces of the specimen of  $\Delta K = 11.2 \text{ MN/m}^{3/2}$  (a = 0.25 mm),

specimen of  $\Delta K = 11.2 \text{ MN/m}^{-1}$  (a = 0.25 mm), 3/2At an alternating stress intensity  $\Delta K = 11.2 \text{ MN/m}^{-3/2}$  the crack growth rate is estimated to be  $2.10^{-5}$  mm/cycle (see Figure AlO [3]). This means that if the normal test frequency were to be used (15 cycles/minute) every 0.1 mm of crack growth would take about 5 hours. Therefore initially a test

frequency of 5 Hz is recommended. A crack size increment of 0.1 mm (5000 cycles) will then occur within ~ 1000 seconds (~ 15-20 minutes). Return to a frequency of 15 cycles/minute when a = 0.5 mm. If the load is held constant during the test this will give the following  $\Delta K$  levels at the corresponding surface crack lengths:

a(mm)	$\Delta K(MN/m^{3/2})$
0.25	11.2
0.5	15.8
1.0	22.4
2.0	31.6
6.0	88

If the above stress intensities are used the appropriate and realistic crack growth rate values (between  $10^{-4}$  and  $10^{-3}$  mm/cycle) occur in the physically short crack regime.

If the crack growth rates encountered do not agree with the above indicated values then the applied stress levels should be corrected so that appropriate crack growth the same obtained. Consult the coordinators. In coordination with the first laboratory doing the test they will decide which adjustments should be made and communicate the new stress levels to all other laboratories.

6. It the stress intensity used for crack initiation is too low then a higher (e.g. 20% higher) stress intensity may be chosen. If the crack initiates at the higher stress intensity a subsequent load reduction may be carried out (if necessary) to obtain appropriate crack growth rates (between  $10^{-4}$ and  $10^{-3}$  mm/cycle) between a = 0.5 + 2 mm. This procedure will be illustrated by the following simple example:

a = 0.25 mm, assume at  $\Delta K$  = 11.2 MN/m<sup>3/2</sup> ( $\Delta \sigma$  = 540 MN/m<sup>2</sup>;  $\sigma$  : 60 + 600 MN/m<sup>2</sup>) no crack initiation; then increase stress level 20 %;

 $a = 0.25 \text{ mm}, \Delta K = 13.4 \text{ MN/m}^{3/2}$ 

 $(\Delta c = 650 \text{ MN/m}^2; c : 72 + 722 \text{ MN/m}^2).$ 

## AFPENDIX A

If the load is held constant then this will result in:

a (num)	$\Delta K(at \Delta \sigma = 650$	MN/m²)	∆K (at	۵c	= 540	MN/m²)
0.25	13.4					
0,30	14.7					
0.35	15.8	reduce	1080 10	🗕 i	3.2	
0.40	16.9	origina	ii ievei	1	4.1	
0.50	18.9			1	5.8	

#### continue testing at this load level

- 7. Test the 3 specimens such that a reliable determination of the total crack growth curve is obtained.
- 4. FORMAT FOR THE DELIVERY OF TEST RESULTS

All CORE programme results should be sent in to the coordinators according to the following format: Smooth cylindrical specimen

- 1. Specimen number
- Stress level (Ac); MN/m<sup>2</sup>
- 3.
- Cycles to failure N Additional comments, if necessary. 4.

Flat double edge notched specimen 1. Specimen Lumber 2

- 2.
- Specimen Lumber Stress level ( $\Delta\sigma$ ); MN/m<sup>2</sup> Cycles to crack formation (1 %), N<sub>i</sub> 3.
- Cycles to failure N Additional comments, if necessary. s.

Compact type specimen 1. Specimen number

- $da/dN = \Delta K$  curve on supplied graphical paper 2.
- usion as curve on supplied graphical paper 50 data sets (a versus N) representing the total a versus N curve. The data delivered by the various laboratories will all be handled similarly, using a secant procedure, to obtain represen-3. tative da/dN- AK curves
- Additional comments, if necessary. 4.

Corner crack specimen

- Specimen number da/dN ΔK curve on supplied graphical paper
- but data sets (a versus N) representing the total a versus N curve. The data delivered by the various laboratories will all be handled similarly, using a secant procedure, to obtain representative da/dN-  $\Delta K$  curves 3.
- 4 Additional comments, if necessary.
- 5. REFERENCES
- Proposal for an AGARD coordinated international test programme on damage telerance in titanium alloy engine discs; presented at AGARD SMP meeting in Vimeiro, Portugal, 1983 i. Mom. A.J.A.
- Hicks, M.A., A comparison of theoretical and experimental methods of calibrating the electrical 2. Pickard, A.C. potential drop technique for crack length determination; Int. Journ. of Fracture,  $\underline{20},$  1982, pp. 91-101
- Powell, B.E., Duggan, T.V., The influence of minor cycles on low cycle fatigue crack propagation, int. Fournal of Fatigue, January 1982, pp. 4-14 3. Jeal, R.
- The development of advanced specimen testing and analysis cechniques applied to 4. Pickard, A.C., Brown, C.W., Hicks, M.A. fracture mechanics lifing of gas turbine components, in: ASME International Conference on Advances in Life Prediction Methods; Ed. by D.A. Woodford and J.R. Whitehead, published by ASME, New York, 1983
- Stress intensity factors for cracks with circular and elliptic crack fronts, determined by 3D finite element methods, Numerical Methods in Fracture Mechanis; Pineridge Press, pp. 599-614 (1980), Swansea, UK 5. Pickard, A.C.

# APPENDEX A

# TABLE A: Overview of CORE programme; number of specimens indicated for each individual laboratory. All tests at room temperature

Type of t	est	LCF-life / crack formation		crack pro	crack propagation		
Test spec	lmen	smooth cylindrical	flat notched $k_t \sim 2.2$	corner crack	ASTM CI		
Number of	specimens	6	. b	ر	3		
Crack	potential drop		+	+ <sup>*)</sup>	+		
detection	optical			+			
g	al		only initial crack formation	"short" crack range	total da/dN = ∆K curve		

\*) = optional

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$$K = -\frac{P}{b \cdot W} = t(\frac{a}{w})$$

 $f(\frac{a}{k}) = \frac{2 + a/k}{(1 - a/k)^{3/2}} (0.586 + 4.64 a/k - 13.32(a/k)^2 + 14.72(a/k)^3 - 5.6(a/k)^3)$ 

d'	a/w	r(a/h)	.i '	a's -	f(a/W)
0	0.244	4.848	3.5	0.374	6,886
6.3	0+248	4.899	4.0	4.998	
0.2	0.252	4.950		6	7.613
0.3	0.256	5.002 1	5.0	0.437	8.011
0.4	0.260	5.054 1	5.5	6.256	8
0.5	063	5.107	t. (	: • + /	8. 446
0.6	0.267	5.159	6.5	ي داد د	9.40
0.7	0.271	5.212	7.0		16.014
0.8	0.275	5.000	2.5		10.00
0.9	U .79	5.35	8.0	0.352	11.440
1.0	0.283	5.372	8.5	1 0.571	12.55
1.1	087	5.427	4.1	1	13.15
1	0.290	5.48.	9.5	0.5.0	1
1.3	0.294	5.537	10.0	1 1.6.1	12.503
• 4	0.298	5.593	10.5	0.6.8	16.711
i.5	0.302	5.649	11.15	. 66	15
· . (,	0.366	5.205	11.5	0.68	in the
1.7	0.310	5.75	12.0	5. TUN	
1.8	0.315	5.8.0	12.5	9.125	
1.4	- C. SL.	J.5/8		}	
1.0	9.3.1	5.936		1	
- · î	0.340	6.236		1	
1.0	9.360	6,352			1

talculation of ((a'k) for ASD) is specified with k = 26 mm. a' = real crick length starting from botch root<math>a' = defined distance from crack tip to centerline of the length boles(a = a' + 6.35 mm for this specimen)



Fig. Al. Specimens used in the AGARD programme


Fig. A2 Load waveform used in CORE programme



Fig. A3  $(T_1+6A)=4V$  plain specimen fatigue life scatterband (based on various data, R=0)



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6.5

Fig. A4 Setsup of current and voltage wiring for PD-measurement



Fig. 45 PD-measurement at current off and current on conditions



Fig. A6 - Fatigue life scatterband for notched Ti-6A+-4V specimens  $(R_{\rm f}+2.5)$ 



 $F_{T,R_{\rm c}}(AT)$  Set up of PD-measurement avaient to CT spectment

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Fig. A8 Finite element PD-analysis for CT-specimen normalised to  $V/V_O = 1$  at a/W = 0.244 [2]



Fig. A9 PD-signal shows start up effect during testing of CT specimens



Fig. A10 Crack growth data for T1-6A-4V CT-specimens [3]



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Fig. All Potential drop data sampling at high frequency CT-specimen testing



Fig. A12 PD-instrumentation of corner erack specimen. Note: the exact distance between reference leads is not important; this only results in a reference voltage which is about the same as the initial notch voltage.







Fig. Al4 -Variation of normalised stress intensity with erack length for the corner creek geometry  $\{4\}$ 



Fig. A15. Relation between  $k_{\rm surface}$  and  $k_{\rm 45^{10}}$  for CC-specimen.

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#### APPENDIX B

The statistical analysis of the LCE and  $K_{1}$  25.2 data is based on the procedures described in ASTM E739 "Standard practice for statistical analysis of linear or linearized stream-life (c-N) latigue data". A short summary of the procedure applied in the current ACARD programme is presented below.

in which

the statistical analysis is based on the assumption that the S-N relationship can be approximated by a straight line for a specific interval of stress. The following line equation was used:

$$Y = K + BX$$
$$Y = \log S$$
$$X = \chi_{C}$$

The coefficients A and B of this linear model can be calculated according:

$$\begin{split} \widehat{\mathbf{x}} &= \widehat{\mathbf{y}} + \widehat{\mathbf{b}}\widehat{\mathbf{x}} \\ \widehat{\mathbf{b}} &= -\frac{\sum_{i=1}^{k} (\lambda_{i} - \widehat{\mathbf{x}}) (\mathbf{y}_{i} - \widehat{\mathbf{y}})}{\sum_{i=1}^{k} (\lambda_{i} - \widehat{\mathbf{x}})^{2}} \\ \widehat{\mathbf{x}} &= -\frac{\sum_{i=1}^{k} (\lambda_{i} - \widehat{\mathbf{x}})^{2}}{k} \\ \widehat{\mathbf{x}} &= -\frac{\sum_{i=1}^{k} (\lambda_{i} - \widehat{\mathbf{x}})^{2}}{k} \\ \widehat{\mathbf{y}} &= -\frac{\sum_{i=1}^{k} (\lambda_{i} - \widehat{\mathbf{x}})}{k} - (average | \widehat{\mathbf{x}}_{i} | value) \\ \widehat{\mathbf{y}} &= -\frac{\sum_{i=1}^{k} (\lambda_{i} - \widehat{\mathbf{x}})}{k} - (average | \widehat{\mathbf{y}}_{i} | \cdot aiue) \\ \widehat{\mathbf{y}} &= -iai | iai | iai$$

A and B are called the maximum likerihood estimators of a and B. (the symbol "caret" (\*) denotes estimate; the symbol "overlart" (\*) denotes average).

Sec. Sec.

to estimate the variance of the normal distribution for log X the following expression is requiremented

$$\gamma_{i=1} = \frac{\sum_{j=1}^{k} (\gamma_{j} - \hat{\gamma}_{j})^{2}}{k - 2}$$

is which:  $\widehat{Y}_{i} = \widehat{X}_{i} + \widehat{B} X_{i}$ 

the term k-2 is used instead of 4 to make  $\gamma^2$  an unbiased estimator of the normal population varian e  $\gamma^2$ .

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The confidence intervals for A and B are gives by:

$$\begin{split} \widehat{A} &= \mathbf{t}_{p} \cdot \widehat{\mathbf{y}} = \left[ \frac{1}{k} + \frac{\overline{\mathbf{x}}^{-2}}{\sum_{i=1}^{k} (\mathbf{y}_{i} - \overline{\mathbf{x}})^{2}} \right]^{\frac{1}{2}} \\ \widehat{B} &= \mathbf{f}_{p} \cdot \mathbf{y} = \left[ -\frac{k}{k+i} (\mathbf{x}_{i} - \overline{\mathbf{x}})^{2} \right]^{-\frac{1}{2}} \end{split}$$

The value of to is read from the t-distribution using the desired value of the confidence levels, associated with the contracted interval (see Table 61). The entry parameter in the degree of threads of t) square k = 1 for the two above equations.

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#### APPENDIX B

### Conflaence band for the entire median S - S curve

The confidence band for the entire log N - Ac curve is calculated using the following equation:

$$\mathbf{Y} = \hat{\mathbf{A}} + \hat{\mathbf{B}}\mathbf{X} + \sqrt{2\mathbf{F}_{\mathbf{p}}^{2}} \begin{bmatrix} \frac{1}{\mathbf{k}} + \frac{(\mathbf{X} - \tilde{\mathbf{X}})^{2}}{\sum_{\mathbf{i}=1}^{k} (\mathbf{X}_{\mathbf{i}} - \tilde{\mathbf{X}})^{2}} \end{bmatrix}^{k_{2}}$$

in which  $F_p$  is given in Table B2. This table contains two entry parameters  $n_1$  and  $n_2$ , which are the statistical degrees of freedom for F. For the above equation  $n_1 = 2$  and  $n_2 = k-2$ .

### Testing of the applicability of the linear model

The linearity control test can only be performed if  $t^{1}e$  programme was planned such that tests were performed at at least three different  $X_{i}$  levels ( $\Delta c$  - levels) and that at least one of the tests was auplicated.

auplicated. The procedure is as follows: Assume 1) the log life of the j-th replicate specimen tested at the i-th level of X is given the value  $Y_{ij}$ 

2) fatigue tests were conducted at  $\ell$  different values of X

3)  $m_{i}$  replicate values of Y are observed at each  $X_{i}$ 

then the hypothesis of linearity is rejected when the computed value of

$$\frac{\sum_{\substack{i=1\\j=1}^{k}}^{k} \mathbf{m}_{i} (\widehat{\mathbf{Y}}_{i} - \overline{\mathbf{Y}}_{i})^{2} / (k-2)}{\sum_{\substack{i=1\\j=1}}^{k} \sum_{\substack{j=1\\j=1}}^{m} (\mathbf{Y}_{ij} - \overline{\mathbf{Y}}_{i})^{2} / (k-k)}$$

exceeds  $F_p$ , where the value of  $F_p$  is read from Table B2 for the chosen significance level of 95 t. This table has two entry parameters  $n_1$  and  $n_2$ ; for this case  $n_1 = k - 2$  and  $n_2 = k - k$ . Note that the total number of specimens tested is given by

$$k = \sum_{i=1}^{i} m_i$$

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12. Distribution 9	Statement	This document is d policies and regula Outside Back Covo	listributed in accordance wit tions, which are outlined on ers of all AGARD publication	h AGARD the ms
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# REPORT DOCUMENTATION PAGE

## 14. Abstract

This report describes the initial results of an AGARD test programme on fatigue behaviour of engine disc materials. The first phase of this programme, the Core Programme, was aimed at test procedure and specimen standardisation and calibration of the various laboratories. A detailed working document has been prepared and is included in this report. It describes the testing tund-mentals and procedures and includes the analysis procedures used for handling the test data.

Fatigue crack initiation and propagation testing was performed on 1i-6Al-4V material under room temperature and constant amplitude loading conditions using four different specimen designs. All results were statistically analysed for possible significant differences in material behavour due to disc processing variables, specimen location in the disc or testing laboratory.

This publication was sponsored by the Structures and Materials Panel of AGARD.

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This publication was sponsored by the Structures and Materials Panel of AGARD.	tis publication was sponsored by the Structures and Materials Panel of AGARD.
15BN 42 835-0175-5	S-S240-S8-26 NR
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Printed by Specialised Printing Services Limited 40 Chigwell Lane, Loughton, Essex IG10 3TZ

ISBN 92-835-0475-5

