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Segmentation of Synthetic Aperture Radar (SAR) Images of Ocean Surface by the Texture Energy Transform Method

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A texture energy transform approach has been chosen for the study of texture analysis and classification in digital images. It is based on the idea of detecting the degree of similarity between the spatial variation of image pixels and a set of chosen mask filters. Feature measures which characterize the texture are simpler to compute as compared with other approaches based on auto-correlation functions, digital transform methods, spatial gray tone co-occurrence probabilities, auto-regression models, etc.. An algorithm was developed for the segmentation of SAR ocean surface images into regions with and without directional streaks. Excellent results are obtained in which surface areas with relatively rough and calm water are identified.

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SEGMENTATION OF SYNTHETIC APERTURE RADAR (SAR) IMAGES OF OCEAN SURFACE BY THE TEXTURE ENERGY TRANSFORM METHOD

Introduction

Texture analysis is an important aspect of image classification and segmentation tasks. It is fundamental to some applications such as metal surface analysis, radiographic diagnosis, identification of different terrains in aerial photographs, isolating special regions in natural scenes, etc.. The subject has been studied quite extensively [1]. Different statistical approaches have been employed to evaluate quantitative feature measures from image pixel data for texture characterization. Despite the ingenious ideas used and the success accomplished in classifying the images chosen in the previous researches, most texture analysis approaches still have limitations. They were applied to a limited categories of images and may not work well in general. All of them require tedius time-consuming machine processing.

Recently, Laws [2] introduced a different kind of approach to texture measures which he called the texture energy transform. In this approach, texture features are evaluated in a spatial-statistical sequence of small mask convolutions followed by moving
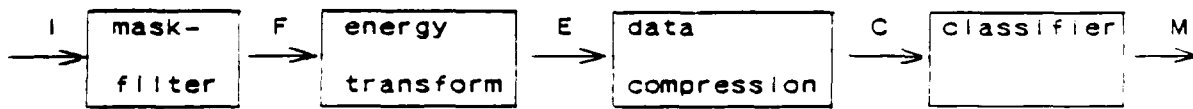
window averaging. The results are closely related to the degree of
match between the pixel neighbourhoods and the set of chosen masks.
In addition to possessing an intuitive physical reasoning in the
formulation, these features are also simpler to compute. Application
of this approach to texture classification yielded better results
than other standard techniques based on second order gray level
statistics [2,3]. It can also be made invariant to changes in
luminance, contrast, and rotation without the use of histogram
equalization or other preprocessing.

In this report, we present the results of texture segmentation
of SAR images of ocean surface using this new technique. It is a
continuation of the task reported previously where similar images
were classified by the gray-tone co-occurrence matrix approach [4].
The previous results obtained are not as good as we had hoped for
which prompted the search for a different processing method. Our
objective of mapping the image into two kinds of regions
differentiated by the presence and absence of pixel streak patterns
has been successful. Physically speaking, this separation process
identifies the areas of ocean surface where significant difference
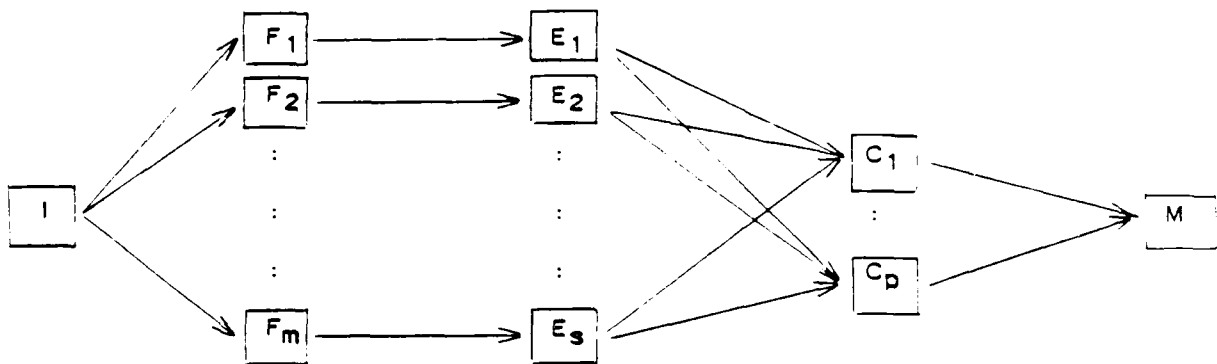existed in terms of surface wind patterns and wave structures.

Texture Energy Transform Approach

The processing sequence of the texture energy transform approach
to image segmentation is outlined in Figure 1. The operation steps
involved are shown in the upper part of the figure with the
associated frames of data attached below. A more detailed

description of the first two steps is shown in Figure 2.

```
I   ┌──────────┐   F   ┌──────────┐   E   ┌──────────┐   C   ┌──────────┐   M
───▶│  mask-   │─────▶│  energy  │─────▶│  data    │─────▶│classifier│─────▶
    │          │       │          │       │          │       │          │
    │  filter  │       │transform │       │compression│      │          │
    └──────────┘       └──────────┘       └──────────┘       └──────────┘
```

(a) Operation sequence

(b) Image frame sequence

Fig. 1.   Texture energy transform approach.

The original image, I, is first filtered by a set of micro-filter convolution masks with integer elements to generate the set of F plane images.   The pixel data in an F plane image is a function of the original image and the chosen filter.   They can assume negative as well as positive values.   These filtered images are plane frames of data in the processing sequence and may not represent recognizable images.   The filtered F plane images are then processed by evaluating statistics of data within a scanning macro-window and assigning the result to the center pixel to produce the E plane

Images. This is a continuous region-to-point transformation

```
┌─────────────────┐          ┌─────────────────┐          ┌─────────────────┐
│ original image  │   ⟹     │ filtered image  │   ⟹     │ texture energy  │
│        I        │          │        F        │          │ plane image E   │
└─────────────────┘          └─────────────────┘          └─────────────────┘
     micro-mask filter            macro-window statistics         data
        convolution                    computation              compression
```
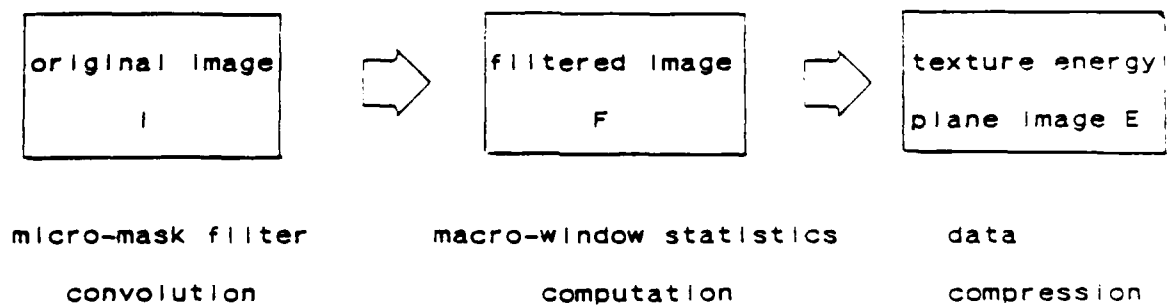
Fig. 2.   Spatial-statistical processing sequence.

where a pixel in a E plane image acquires a number descriptive of its immediate neighbourhood in the original image. The size of the convolution mask is chosen to be comparable to that of the typical texture primitives of the original image. The macro-window should have a size appropriate to cover one kind of texture region most of the time and two kinds of regions along the boundary of region separation. It is chosen so that the statistics evaluated will reveal the difference when it is located within different regions. These statistics are more representative of local spatial variations than typical frequency domain measures and are suitable for textures with short coherence length or correlation distance. To reduce the required processing time, the dimensions of masks and windows are chosen sufficiently small to be physically reasonable for the images under study.

If there are many E plane images chosen, an optional step may be

taken to compress them into a small number of principal component C plane images which still carry enough discriminating information. This can be achieved by using the Hotelling transform which picks out the orthogonal image components with the largest variance [5].

The texture energy plane images or the principal component plane images are the input to the classifier which assign each pixel the proper texture label to produce the final segmented image M. Classification is simple if texture classes are known and training samples are available. Clustering and segmentation algorithms must be used in addition to that of the classification algorithm if texture classes are unknown and have to be identified.

Experimental Methods

In the first step of the texture processing, the original image is filtered by a set of convolution masks. These masks are constructed as two dimensional matrix multiplication of the linear masks shown in Figure 3. These linear masks are called Lattice Aperture Waveform Sets of order three, five and seven. The names of the vectors are mnemonics for level, edge, spot, wave, ripple, undulation, and oscillation. All of them are symmetrically weighted toward their center. Except for the level vectors, the sum of all the elements in each equates to zero. Linear vectors of length three form the basis since the longer ones can be derived in terms of these three through repeated linear convolution.

Figure 4 shows the nine square filter masks generated by the

three linear vectors of length three.   Any 3 by 3 mask can be

$$L3 = (1, 2, 1)$$

$$E3 = (-1, 0, 1)$$

$$S3 = (-1, 2, -1)$$

$$L5 = (1, 4, 6, 4, 1)$$

$$S5 = (-1, 0, 2, 0, -1)$$

$$R5 = (1, -4, 6, -4, 1)$$

$$E5 = (-1, -2, 0, 2, 1)$$

$$W5 = (-1, 2, 0, -2, 1)$$

$$L7 = (1, 6, 15, 20, 15, 6, 1)$$

$$E7 = (-1, -4, -5, 0, 5, 4, 1)$$

$$S7 = (-1, -2, 1, 4, 1, -2, -1)$$

$$W7 = (-1, 0, 3, 0, -3, 0, 1)$$

$$R7 = (1, -2, -1, 4, -1, -2, 1)$$

$$O7 = (-1, 6, -15, 20, -15, 6, -1)$$

Fig. 3.   Center-weighted mask filters.

expressed as a unique linear combination of them.   The names of these
masks attached underneath are coined by the names of the two linear
vectors constituting the column and row vectors of the corresponding
matrix of the mask.   5 by 5 and 7 by 7 as well as non-square
rectangular masks can be formed in a similar fashion.   Figure 5 shows
four 5 by 5 masks which were found to be most useful in the
experimental work done by Laws [2].   The structure of these masks as
the matrix product of the elements in the basis set helps to simplify
the algorithm and reduce the computation time in the step of

convolution filter processing.

$$
\text{L3L3} = \begin{vmatrix} 1 & 2 & 1 \\ 2 & 4 & 2 \\ 1 & 2 & 1 \end{vmatrix} \quad
\text{L3E3} = \begin{vmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{vmatrix} \quad
\text{L3S3} = \begin{vmatrix} -1 & 2 & -1 \\ -2 & 4 & -2 \\ -1 & 2 & -1 \end{vmatrix}
$$

$$
\text{E3L3} = \begin{vmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ 1 & 2 & 1 \end{vmatrix} \quad
\text{E3E3} = \begin{vmatrix} 1 & 0 & -1 \\ 0 & 0 & 0 \\ -1 & 0 & 1 \end{vmatrix} \quad
\text{E3S3} = \begin{vmatrix} 1 & -2 & 1 \\ 0 & 0 & 0 \\ -1 & 2 & -1 \end{vmatrix}
$$

$$
\text{S3L3} = \begin{vmatrix} -1 & -2 & -1 \\ 2 & 4 & 2 \\ -1 & -2 & -1 \end{vmatrix} \quad
\text{S3E3} = \begin{vmatrix} 1 & 0 & -1 \\ -2 & 0 & 2 \\ 1 & 0 & -1 \end{vmatrix} \quad
\text{S3S3} = \begin{vmatrix} 1 & -2 & 1 \\ -2 & 4 & -2 \\ 1 & -2 & 1 \end{vmatrix}
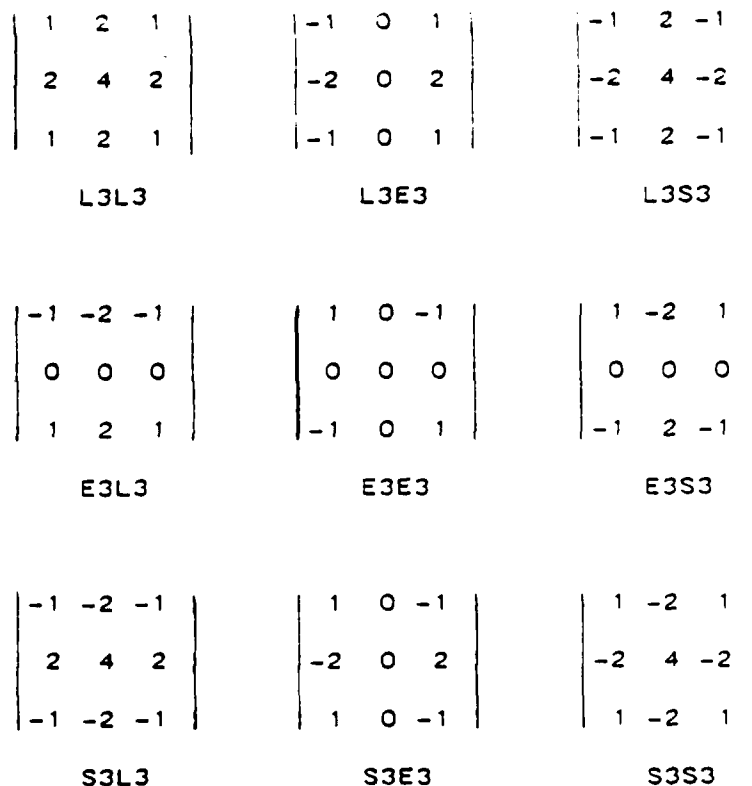$$

Fig. 4. 3 by 3 center-weighted mask filters.

Each mask filter has a unique combination of elements.
Convolution will produce a plane of positive or negative numbers of
larger magnitude if the spatial pixel data variation of the original
image, I, matches closely that of the mask. A homogeneous image
region which shows no textural structure, or a textural region whose
spatial structure differs from that of the mask will result in
smaller numbers. The data in the F plane image reveals the degree of
textural similarity between the mask and the corresponding immediate
vicinity in image I. Pixels located within different textural

primitives in image I will have numerical values of different levels in plane. Hence, the transformation from I to F provides a
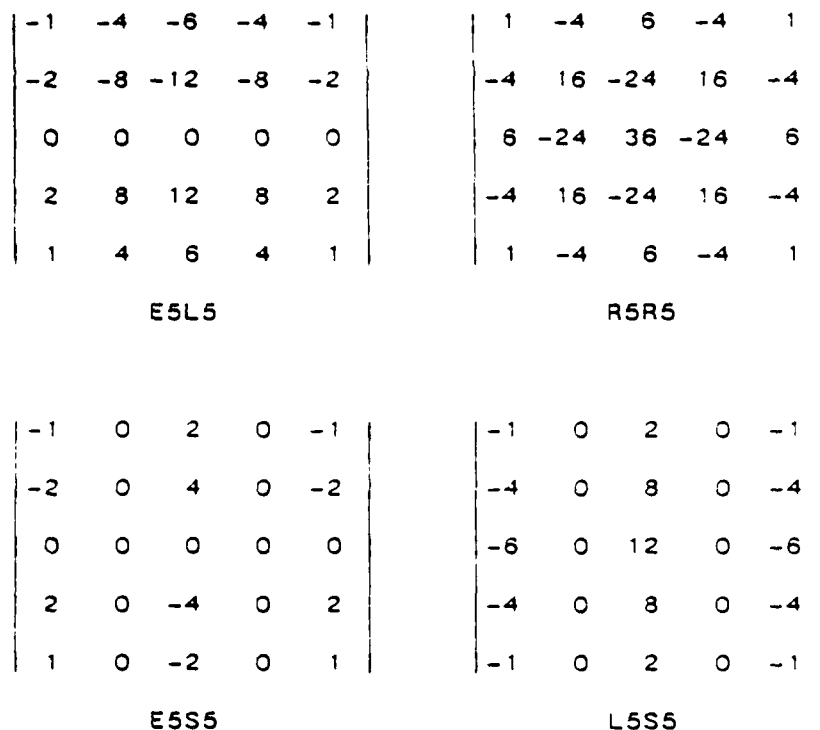
$$\begin{vmatrix} -1 & -4 & -6 & -4 & -1 \\ -2 & -8 & -12 & -8 & -2 \\ 0 & 0 & 0 & 0 & 0 \\ 2 & 8 & 12 & 8 & 2 \\ 1 & 4 & 6 & 4 & 1 \end{vmatrix} \qquad \begin{vmatrix} 1 & -4 & 6 & -4 & 1 \\ -4 & 16 & -24 & 16 & -4 \\ 6 & -24 & 36 & -24 & 6 \\ -4 & 16 & -24 & 16 & -4 \\ 1 & -4 & 6 & -4 & 1 \end{vmatrix}$$

E5L5   R5R5

$$\begin{vmatrix} -1 & 0 & 2 & 0 & -1 \\ -2 & 0 & 4 & 0 & -2 \\ 0 & 0 & 0 & 0 & 0 \\ 2 & 0 & -4 & 0 & 2 \\ 1 & 0 & -2 & 0 & 1 \end{vmatrix} \qquad \begin{vmatrix} -1 & 0 & 2 & 0 & -1 \\ -4 & 0 & 8 & 0 & -4 \\ -6 & 0 & 12 & 0 & -6 \\ -4 & 0 & 8 & 0 & -4 \\ -1 & 0 & 2 & 0 & -1 \end{vmatrix}$$

E5S5   L5S5

Fig. 5.   5 by 5 center-weighted mask filters.

separation step among different texture primitives. The pattern and the steepness in separation among the texture primitives vary among the different masks.

Familiar statistics such as mean, variance, standard deviation, range, maximum, minimum, skewness, kurtosis, and etc. can be chosen as the texture feature representation in the macro-window processing of F plane images to generate E plane images. Laws concluded in his study that variance or standard deviation alone is sufficient in extracting the necessary information. If all mask filters chosen in

the convolution process have zero sum elements, the F plane image is
essentially a zero mean pixel field. Variance is an average of
squared deviation from the mean. With a vanishing mean value, the
variance becomes the average of the squared pixel values within the
macro-window. In this sense, each pixel's value in E plane image is
an energy measure of its macro-window neighbourhood in the F plane.
To simplify the calculation and still maintain esentially the same
statistical meaning, the average of the absolute values within the
macro-window was chosen as the statistic and its value is assigned to
the center pixel of the window in the E plane image.

For each selection of the mask and statistic combination, there
is one feature measure of the texture. Since the choice of the
statistic is a fixed one, the number of masks chosen determines the
number of features to be computed and the number of E plane images to
be generated. The discriminating power of a feature is judged by the
F-ratio statistic calculated from the available training sample image
data by the following formula from [6],

F=(variance of inter-class sample means)/(combined
        intra-class variance)

A good choice of feature will generate values with small variance
from texture samples of the same type and significantly different
mean values of samples of different types. Better choices of
features will produce higher F-ratio statistics. The statistica:
meaning of the F-ratio also depends upon the number of the samples
involved. The comparison of these ratios has to be made on equal

·)

number of samples to yield accurate judgement. With many choices of
features available for characterization of differences among the
textural categories, the proper combination of them to generate the
best accuracy of discrimation can be obtained through discriminant
analysis under certain statistical criteria [2,7]. In the procedure
of segmenting an image, the feature vector composed of chosen feature
elements evaluated for each pixel's neighbourhood is compared with
the feature vectors evaluated by the same formulas from known
training samples of each class. A pixel is classified as belonging
to the class whose centroid vector has the least distance separation
from the feature vector evaluated in its vicinity.

Experimental Results and Discussions

Figures 6a,7a,and 8a show the images which we wish to segment
using the texture energy transform method. These are sub-images
obtained during the SIR-B mission on October 11, 1984. Each one has
a size of 512 by 512 pixels. The area covered is outside the U.S.
east coast with the center geographic location around 37 degree north
and 74 degree west. By carefully examining these images, we can
realize that there are two kinds of textures present. First, the
pixel variations indicate directional streak patterns. In other kind
of texture, the pixel variation seems homogeneously random. The
appearance of these two textures indicates the difference in the
radar back-scattering characteristics from different areas of ocean
surface. Our image segmentation objective is to separate these two
textural areas where contrasting surface meteorological conditions
existed when the image was recorded.

According to Laws' research, 5 by 5 masks were more powerful than the 3 by 3 masks, and much simpler to process than 7 by 7 masks. By detailed comparison, we found that the 5 by 5 mask is big enough to cover an essential part of a typical texture primitive in these images. We chose to try the masks shown in Figure 5 first. Four training samples with size of 64 by 64 pixels of streak areas and non-streak areas were located in each image.

Since there are only two classes of texture to be separated, the complicated discriminant analysis is not necessary in this problem. Each five by five mask was convolved with each of the training samples and the average of absolute values of the convolution was then computed. There are small differences between these two kinds of textures and the results are not much better than what had been achieved using the co-occurrence matrix method [4]. However, mask filters E5L5 and L5S5 did produce consistently more difference than the other two filters. E5L5 is a horizontal edge mask and L5S5 is a vertical line detector. This fact indicates that the edge and line detector masks can separate image regions with streaks and without streaks more effectively than masks which discover textural detail in other aspects. Attention was shifted toward finding the best possible line detector masks which are zero-sum and made of simple integer components. Judgement was made on tests done with the training samples of each image. The most powerful masks found this way are shown in Figures 9, 10, and 11 for the images in Figures 6a, 7a, and 8a respectively. The two masks shown in each figure are a 90 degree transpose of each other. One of
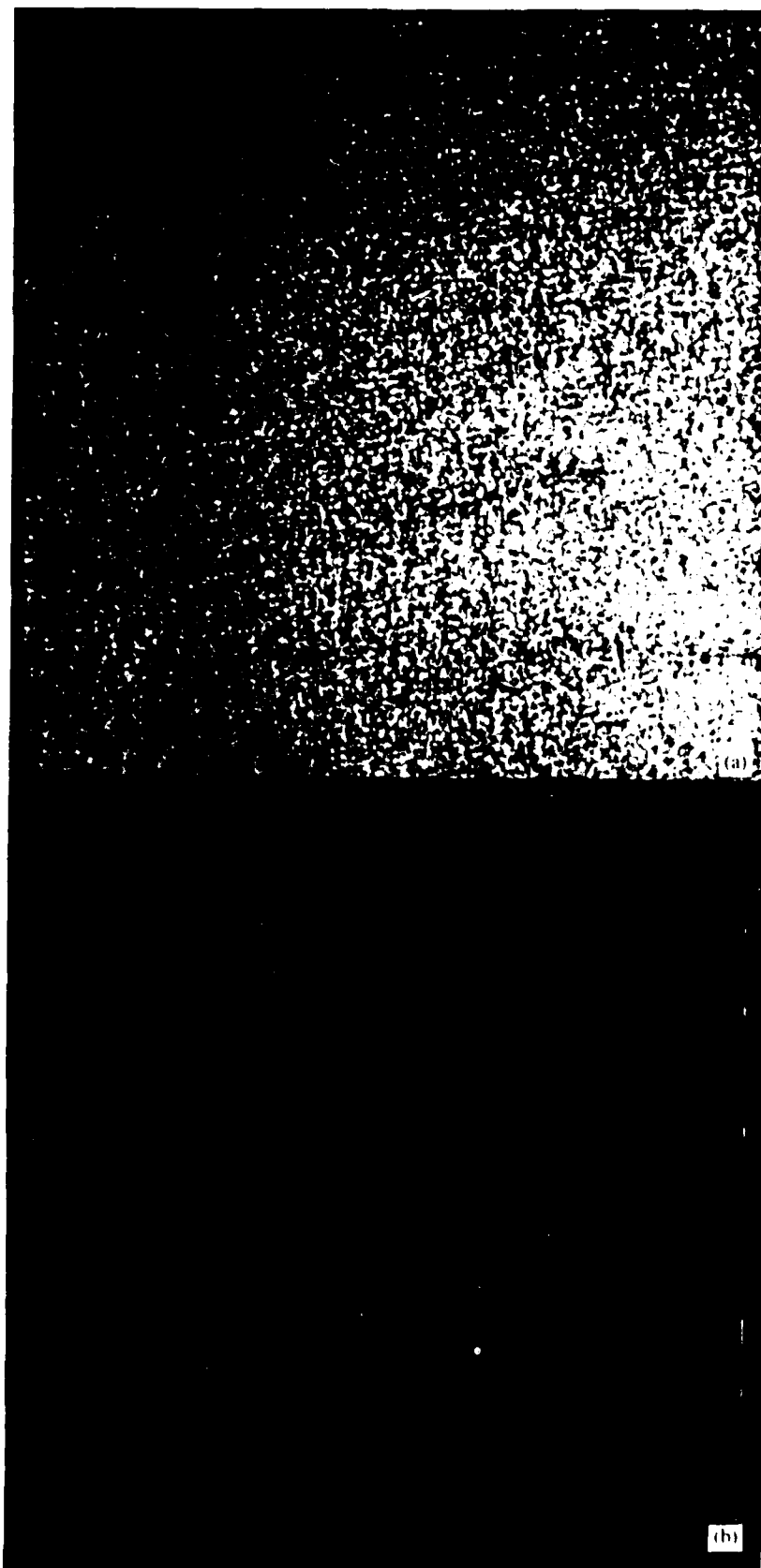
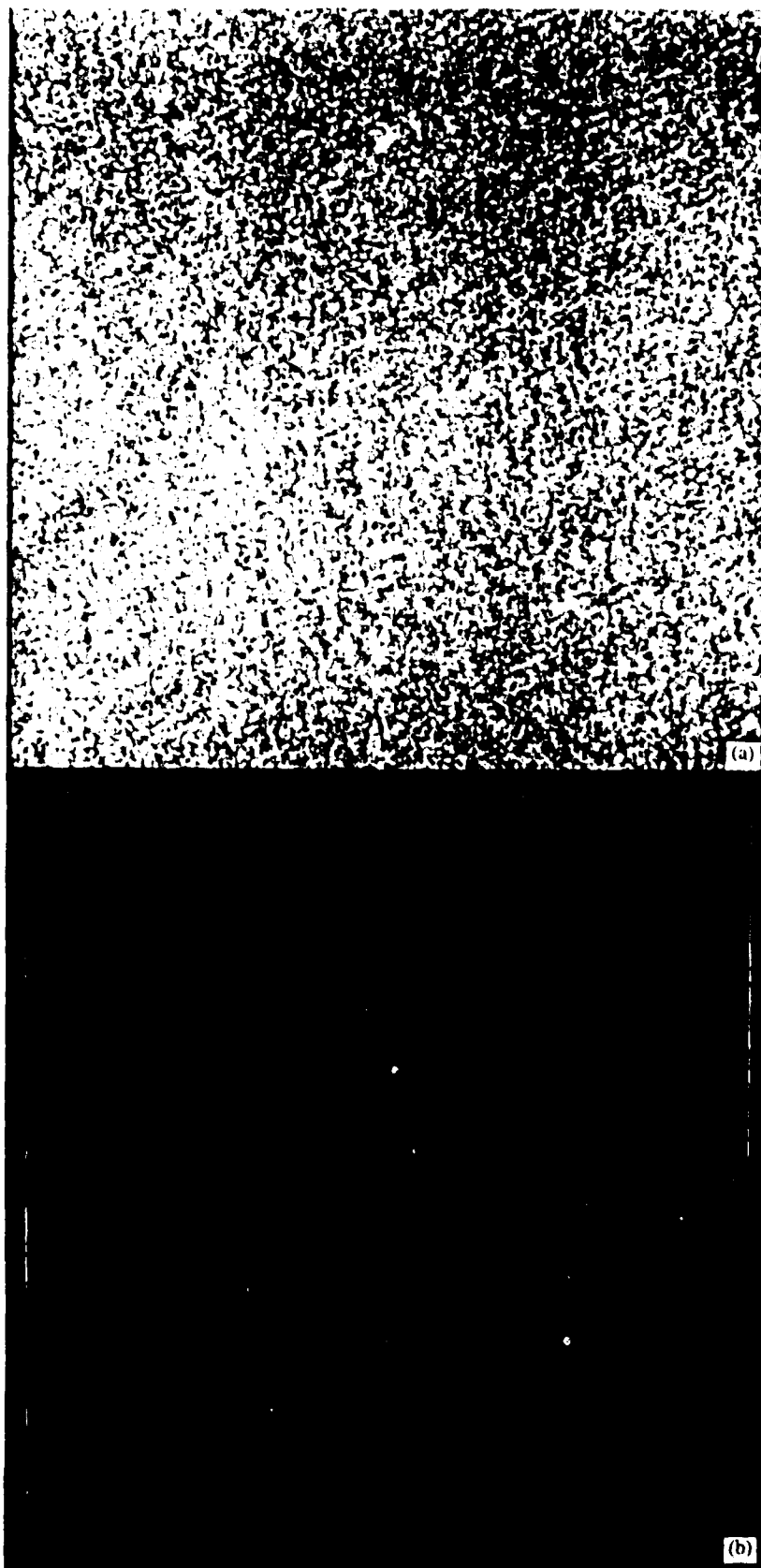Fig. 6. SAR ocean surface image and its segmentation map.

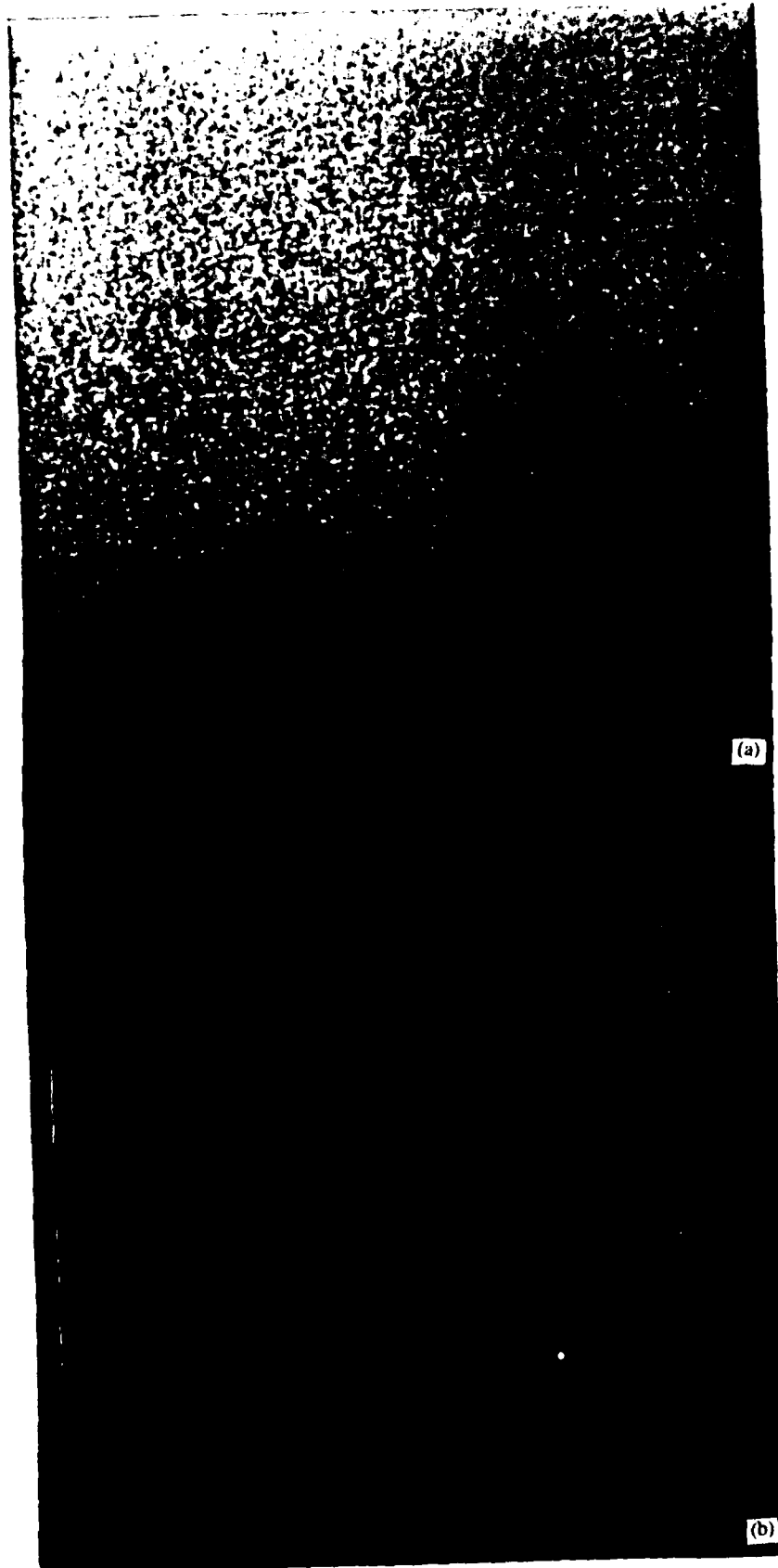Fig. 7. SAR ocean surface image and its segmentation map.

Fig. 8. SAR ocean surface image and its segmentation map.

$$
\begin{vmatrix}
-11 & -2 & 0 & 2 & 11 \\
-11 & -2 & 0 & 2 & 11 \\
-11 & -2 & 0 & 2 & 11 \\
-11 & -2 & 0 & 2 & 11 \\
-11 & -2 & 0 & 2 & 11
\end{vmatrix}
\qquad
\begin{vmatrix}
-11 & -11 & -11 & -11 & -11 \\
-2 & -2 & -2 & -2 & -2 \\
0 & 0 & \_0 & 0 & 0 \\
2 & 2 & 2 & 2 & 2 \\
11 & 11 & 11 & 11 & 11
\end{vmatrix}
$$

Fig. 9.   Mask filter chosen for image in Fig. 6a.

$$
\begin{vmatrix}
-2 & -1 & 0 & 1 & 2 \\
-2 & -1 & 0 & 1 & 2 \\
-2 & -1 & 0 & 1 & 2 \\
-2 & -1 & 0 & 1 & 2 \\
-2 & -1 & 0 & 1 & 2
\end{vmatrix}
\qquad
\begin{vmatrix}
-2 & -2 & -2 & -2 & -2 \\
-1 & -1 & -1 & -1 & -1 \\
0 & 0 & 0 & 0 & 0 \\
1 & 1 & 1 & 1 & 1 \\
2 & 2 & 2 & 2 & 2
\end{vmatrix}
$$

Fig.10.   Mask filter chosen for image in Fig.7a.

$$
\begin{vmatrix}
-5 & -4 & 0 & 4 & 5 \\
-5 & -4 & 0 & 4 & 5 \\
-5 & -4 & 0 & 4 & 5 \\
-5 & -4 & 0 & 4 & 5 \\
-5 & -4 & 0 & 4 & 5
\end{vmatrix}
\qquad
\begin{vmatrix}
-5 & -5 & -5 & -5 & -5 \\
-4 & -4 & -4 & -4 & -4 \\
0 & 0 & 0 & 0 & 0 \\
4 & 4 & 4 & 4 & 4 \\
5 & 5 & 5 & 5 & 5
\end{vmatrix}
$$

Fig.11.   Mask filter chosen for image in Fig.8a.

them detects the vertical lines and edges and the other detects the horizontal counterparts. Both were utilized simultaneously as the direction of the streaks can be random. Applying these pairs of filters to the corresponding training samples and taking the sum of the two average absolute values in each case yields two-point scatter plots. Two threshold levels for each image to separate the streak and non-streak textures as well as a transition region were

determined. Static threshold levels chosen this way were incorporated into the process to classify the corresponding whole image.

Starting at the upper left corner, the mask filters in Figures 9, 10, and 11 were scanned pixel by pixel to compute convolution through the whole image. A moving macro-window of size 33 by 33 pixels was chosen so that there is a precisely defined center location. The macro-window is also scanned pixel by pixel through the image. At each position in the scanning process, the sum of the average absolute values of the convolutional results of the two perpendicular masks within the window was taken. This sum is then adjusted to eliminate the influence due to the difference in the mean pixel value within the window at each position in the original image. This adjusted sum is compared with the two threshold levels to determine the center pixel's classification. Segmentation results are shown in Figures 6b, 7b, and 8b for the images in Figures 6a, 7a, and 8a respectively. Pseudo colors are used for clarification. Green color is assigned to the streak textural regions and the blue color is assigned to the non-streak textural regions. The transition regions are cyan. Sixteen pixels around the edge could not be classified and are colored red. The threshold levels are adjustable. The threshold level chosen for streaked regions of Figure 6 was more stringent. As a consequence, less area was classified as streaked region in Figure 6 as compared to those in the other two images. The lower left corner of Figure 6 was not accurately classified because the original pixel data there was incomplete. The size of the macro-window can be varied, but its optimum size may not be easy to find.

In some parts of these images the perception does change somewhat as
the window size varies or as the average pixel intensity within the
window varies. However, careful scrutiny of the corresponding
images shows that these results do present accurate maps which
separate the two kinds of textures.

Conclusions

The texture energy transform is the latest method developed for
texture analysis of images. It is based on a spatial-statistical
approach in which texture features are determined by the degree of
match between pixel neighbourhood of the image and a set of chosen
mask filters. The method is conceptually simple and consumes less
computation time than most other established texture classification
techniques. It was applied to segmentation of synthetic aperture
radar(SAR) images of ocean surface into regions with and without
directional streaks. Excellent results were obtained. However, the
set of masks incorporated in the analysis, which worked well, are
masks detecting lines and edges rather than the standard set
originally proposed to discover essentially all possible spatial
variations. This fact indicates that the textural difference between
the regions with and without streaks are subtler than we anticipated.
The distinction can be recognized without much difficulty with naked
eyes but it may not be easy to establish by algorithms based on
various conventional texture discriminating methods. Since both the
co-occurrence matrix method and the texture energy transform method
produced the same level of difference in feature measures between the
two kinds of the training samples, we believe they are almost equally

powerful in texture analysis. For the SAR ocean surface images we
tried to segment, it appears more efficient to search for the
existence of lines or edges rather than for two different kinds of
textures. It is unlikely that any other powerful texture analysis
method will be able to discern these two regions in terms of clear
cut texture dissimilarity.

The size of the micro-filter masks and the macro-window for
texture energy evaluation are determined individually for each task
under investigation to match the intrinsic spatial texture variations
and each textural region's typical extent of coverage. The masks
suggested by Laws [2] cover a very general case in which many kinds
of drastically different textures are involved. Laws masks are
derived by a two dimensional matrix multiplication of two linear
vectors which are obtained from sequence of convolutions with three
vectors of length three. Choice of these masks can simplify the mask
convolution calculation and save processing time. The optimum
combination of masks which make the set for the feature vector
components can be determined through F-ratio statistic test and
discriminant analysis with the training samples. For simpler
problems with fewer classes of textures to segment, like the one
studied in this report, one or two feature measures which yield
clearly different range of values among different classes may be
enough and the F-ratio test is not necessary. Proper workable masks
can be found by trial and error and the textural identification can
be done with threshold level separation instead of the complicated
statistical classifications.

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