

4

AD-A196 955

OFFICE OF NAVAL RESEARCH

Contract N00014-86-K-0043

TECHNICAL REPORT No. 72

DTIC FILE COPY

Analysis of Thermodynamic and Transport Properties  
of  $\text{La}_{2-x}\text{M}_x\text{CuO}_4$  and  $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$  Superconductors

by

A. Langner, D. Sahu and Thomas F. George\*

Prepared for Publication

in

Physical Chemistry of High-Temperature Superconductors

Edited by D. L. Nelson and T. F. George

American Chemical Society Symposium Series

Departments of Chemistry and Physics  
State University of New York at Buffalo  
Buffalo, New York 14260

June 1988

Reproduction in whole or in part is permitted for any purpose of the  
United States Government.

This document has been approved for public release and sale;  
its distribution is unlimited.

DTIC  
ELECTE  
JUN 28 1988  
S E D

88 4

REPORT DOCUMENTATION PAGE				Form Approved OMB No. 0704-0188	
1a. REPORT SECURITY CLASSIFICATION Unclassified			1b. RESTRICTIVE MARKINGS		
2a. SECURITY CLASSIFICATION AUTHORITY			3. DISTRIBUTION/AVAILABILITY OF REPORT Approved for public release; distribution unlimited		
2b. DECLASSIFICATION/DOWNGRADING SCHEDULE					
4. PERFORMING ORGANIZATION REPORT NUMBER(S) UBUFFALO/DC/88/TR-72			5. MONITORING ORGANIZATION REPORT NUMBER(S)		
6a. NAME OF PERFORMING ORGANIZATION Depts. Chemistry & Physics State University of New York		6b. OFFICE SYMBOL (if applicable)	7a. NAME OF MONITORING ORGANIZATION		
6c. ADDRESS (City, State, and ZIP Code) Fronczak Hall, Amherst Campus Buffalo, New York 14260			7b. ADDRESS (City, State, and ZIP Code) Chemistry Program 800 N. Quincy Street Arlington, Virginia 22217		
8a. NAME OF FUNDING/SPONSORING ORGANIZATION Office of Naval Research		8b. OFFICE SYMBOL (if applicable)	9. PROCUREMENT INSTRUMENT IDENTIFICATION NUMBER Contract N00014-86-K-0043		
8c. ADDRESS (City, State, and ZIP Code) Chemistry Program 800 N. Quincy Street Arlington, Virginia 22217			10. SOURCE OF FUNDING NUMBERS		
			PROGRAM ELEMENT NO.	PROJECT NO.	TASK NO.
					WORK UNIT ACCESSION NO.
11. TITLE (Include Security Classification) Analysis of Thermodynamic and Transport Properties of $La_{2-x}M_xCuO_4$ and $YBa_2Cu_3O_{7-\delta}$ Superconductors					
12. PERSONAL AUTHOR(S) A. Langner, D. Sahu and Thomas F. George					
13a. TYPE OF REPORT		13b. TIME COVERED FROM _____ TO _____		14. DATE OF REPORT (Year, Month, Day)	15. PAGE COUNT
16. SUPPLEMENTARY NOTATION Prepared for Publication in <u>Physical Chemistry of High-Temperature Superconductors</u> , edited by D. L. Nelson and T. F. George (American Chemical Society Symposium Series)					
17. COSATI CODES			18. SUBJECT TERMS (Continue on reverse if necessary and identify by block number)		
FIELD	GROUP	SUB-GROUP	HIGH-T <sub>c</sub> SUPERCONDUCTORS, GINZBURG-LANDAU THEORY, THERMODYNAMIC, AND TRANSPORT PROPERTIES, s- AND d-WAVES. THEORETICAL ANALYSIS, LARGE SOMMERFELD COEFFICIENTS.		
19. ABSTRACT (Continue on reverse if necessary and identify by block number)					
Anisotropic Ginzburg-Landau theory for coupled s-wave and d-wave order parameters is used to analyze the unique thermodynamic and transport properties of the new $La_{2-x}(Ba,Sr)_xCuO_4$ and $YBa_2Cu_3O_{7-\delta}$ superconductors. This simple phenomenological approach is used to explain the prevalence of the large Sommerfeld coefficients of the specific heat, the existence of multiple specific heat anomalies, the ultrasonic attenuation peak, and model the anisotropic critical field data as observed in oriented samples.					
20. DISTRIBUTION/AVAILABILITY OF ABSTRACT <input checked="" type="checkbox"/> UNCLASSIFIED/UNLIMITED <input checked="" type="checkbox"/> SAME AS RPT <input type="checkbox"/> DTIC USERS			21. ABSTRACT SECURITY CLASSIFICATION Unclassified		
22a. NAME OF RESPONSIBLE INDIVIDUAL Dr. David L. Nelson			22b. TELEPHONE (Include Area Code) (202) 696-4410	22c. OFFICE SYMBOL	

Physical Chemistry of High-Temperature Superconductors

Edited by D. L. Nelson and T. F. George

American Chemical Society Symposium Series

Analysis of Thermodynamic and Transport Properties  
of  $\text{La}_{2-x}\text{M}_x\text{CuO}_4$  and  $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$  Superconductors

A. Langner, D. Sahu and Thomas F. George

Departments of Physics and Chemistry  
239 Fronczak Hall  
State University of New York at Buffalo  
Buffalo, New York 14260

Accession For	
NTIS GRA&I	<input checked="" type="checkbox"/>
DTIC TAB	<input type="checkbox"/>
Unannounced	<input type="checkbox"/>
Justification	
By _____	
Distribution/	
Availability Codes	
Dist	Avail and/or Special
A-1	



Anisotropic Ginzburg-Landau theory for coupled s-wave and d-wave order parameters is used to analyze the unique thermodynamic and transport properties of the new  $\text{La}_{2-x}(\text{Ba},\text{Sr})_x\text{CuO}_4$  and  $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$  superconductors. This simple phenomenological approach is used to explain the prevalence of the large Sommerfeld coefficients of the specific heat, the existence of multiple specific heat anomalies, the ultrasonic attenuation peak, and model the anisotropic critical field data as observed in oriented samples.

Following the discovery by Bednorz and Müller [1] of "high-temperature" superconductivity in the rare-earth copper oxides, there have been numerous investigations of the anisotropic electronic [2,3] and magnetic [3-7] properties of these materials. It is now well recognized that any successful theory of superconductivity for the high- $T_c$  oxides must include the quasi-two-dimensional nature of the Cu-O planes; the theory must provide, in addition, for a coupling between the planes [8,9]. One of the best known theories of the new superconductors is the resonating-valence-bond (RVB) model of Anderson [10] which describes the onset of superconductivity as a Bose condensation of quasi-particle pairs within a large-U Hubbard model. It has been shown by Kotliar [11] and Inui, et al [12] that the superconducting order parameter of this model possesses s-wave and d-wave components, the latter being favored at large U and near half-filling. At low temperatures the mixed (s+d)-state is favored, similar to that found in the heavy-fermion superconductor  $\text{U}_{1-x}\text{Th}_x\text{Be}_{13}$  [13-15]. It is interesting to note that the low-temperature behavior of the penetration depth,  $\lambda(T)$  [16], the large Sommerfeld coefficients of the specific heat,  $\gamma$  [17,18], the enhancement of the sound velocity and ultrasonic attenuation [19,20], and the thermopowers [17] of the  $\text{La}_{2-x}(\text{Sr},\text{Ba})_x\text{CuO}_4$  (called 214) and  $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$  (called 123)

materials are very similar to the heavy-fermion systems. This leads us to believe, as has been suggested on the basis of high-resolution X-ray scattering experiments, [21] that s- and d-wave coupling may exist in the high- $T_c$  superconductors.

### Model

In this work we apply anisotropic Ginzburg-Landau (GL) theory [22], previously extended by us to include coupled s-wave and d-wave superconducting order parameters [23], to qualitatively analyze the single-crystal and oriented-film data on the 214- and 123-materials. In particular we think that the large Sommerfeld coefficients  $\gamma = 5$  mJ/mol  $K^2$  [4,24,25] and 9 mJ/mol  $K^2$  [18,20] for the 40 K and 90 K superconductors, respectively, the anomalous peak in the ultrasonic attenuation at  $T \sim 0.9 T_c$  [19,20], the upturn in the  $Hc_2(T)$  curve [6,7], and the anisotropy in the magnetic properties of these materials can be explained in the context of coupled (s+d)-wave states. A brief investigation of the (s+d)-wave state on a square lattice has been reported previously [26] and will be compared with the full three-dimensional results. We are aware that the limitations on any mean-field-theory description of the high- $T_c$  materials, namely the Brout condition, due to critical fluctuations is very restrictive [27]; however, the qualitative agreement of the GL theory with experiment deserves mention.

As is done in the GL-theory for a single even-parity order parameter, we write the free energy density difference between the superconducting state and the normal state as an expansion in even powers of the complex gap function  $\Delta(\vec{k})$ , which is related to the anomalous thermal average  $\langle c_{\vec{k}\uparrow}^\dagger c_{\vec{k}\downarrow} \rangle$  of the microscopic theory [28], where  $c_{\vec{k}\uparrow}$  is the electron annihilation operator with wave vector  $\vec{k}$  and spin  $\uparrow$ . However, for the multiple-order parameter case we must expand  $\Delta(\vec{k})$  as a linear combination of the angular momentum basis functions  $\{Y_j(\hat{k})\}$ ,

$$\Delta(\vec{k}) = \sum_{j=0}^2 \eta_j(k) Y_j(\hat{k}) = \sum_{j=0}^2 \Delta_j(k) \exp(i\theta_j) Y_j(\hat{k}) \quad , \quad (1)$$

where  $Y_0$ ,  $Y_1$  and  $Y_2$  are analogous to the s,  $d_{x^2-y^2}$  and  $d_{xy}$  atomic orbitals.  $Y_0$  and  $Y_2$  both belong to the  $A_{1g}$  irreducible representations of the  $D_{4h}$  (tetragonal) and the  $D_{2h}^{1g}$  (orthorhombic) point groups, while  $Y_1$  degenerates from a  $B_{2g}$  to an  $A_{1g}$  representation in going over from  $D_{4h}$  to  $D_{2h}^{1g}$ -symmetry. The consequence of this is to induce some low-angular-momentum s-d  $x^2-y^2$  coupling as described below. Generating the invariant terms of the free-energy density, as previously described [29], we can write the free-energy difference between the superconducting and normal state for a tetragonal lattice as

$$F_s - F_n = \int d^3r [ s_q + T + GS + GT + b^2/(8\pi) ] \quad , \quad (2a)$$

$$L \cdot s_q = \sum_{j=0}^1 (\alpha_j \Delta_j^2 + \beta_j \Delta_j^4) + \Delta_0^2 \Delta_1^2 (\gamma_1 + \delta_1 \cos 2\theta_1) \quad , \quad (2b)$$

$$\mathcal{F}_T = \alpha_2 \Delta_2^2 + \beta_2 \Delta_2^4 + \Delta_0^2 \Delta_2^2 (\gamma_2 + \delta_2 \cos 2\theta_2) + \Delta_0 \Delta_2 \cos \theta_2 (\lambda_2 + \mu_{20} \Delta_0^2 + \mu_{22} \Delta_2^2) , \quad (2c)$$

$$\mathcal{F}_{GS} = \sum_{j=0}^1 |\alpha_j| \xi_{jp}^2 [ |D_x \eta_j|^2 + |D_y \eta_j|^2 ] + M_{01} [ (D_x \eta_0)(D_x \eta_1)^* - (D_y \eta_0)(D_y \eta_1)^* + cc ] , \quad (2d)$$

$$\mathcal{F}_{GT} = \sum_{j=0}^2 |\alpha_j| \xi_{jz}^2 |D_z \eta_j|^2 + |\alpha_2| \xi_{2p}^2 [ |D_x \eta_2|^2 + |D_y \eta_2|^2 ] + \sum_{j=0}^1 M_{j2} [ (D_x \eta_j)(D_x \eta_2)^* + (-1)^j (D_y \eta_j)(D_y \eta_2)^* + cc ] + M_z [ (D_z \eta_0)(D_z \eta_2)^* + cc ] . \quad (2e)$$

Here we define the coherence lengths,  $\xi_{j\ell}$ , as  $\xi_{j\ell}^2 = \hbar^2 / [2m_{j\ell} |\alpha_j|]$ ,  $\alpha_j = A_j(T-T_c)$ , where  $j$  refers to the species and  $\ell$  the orientation ( $p$  refers to the  $xy$ -plane), as is done in GL-theory for axial symmetry. The gauge-invariant differential operators are defined as  $D_\zeta = (\partial/\partial\zeta - i\phi_{inv} A_\zeta)$  ( $\zeta = x, y, z$ ), with vector potential  $\vec{A}$  and  $\phi_{inv} = 2\pi/\phi_0$ ,  $\phi_0 = hc/(2e)$  being the flux quantum. The coupling terms in the gradient expressions are characterized by reciprocal effective masses,  $M_{ij} = \hbar^2/4m_{ij}$ . The phase angles  $\theta_1$  and  $\theta_2$  are taken relative to  $\theta_0$ , the phase of  $\eta_0$ , thus ensuring the gauge invariance of Eq. (2). We use  $b^2/8\pi$  to represent the internal magnetic field energy density.

Equation (2) has been subdivided into terms arising from a two-dimensional analysis of the square  $xy$ -planes,  $\mathcal{F}_{sg}$  and  $\mathcal{F}_{GS}$ , and the additional terms required to analyze tetragonal systems,  $\mathcal{F}_T$  and  $\mathcal{F}_{GT}$ . Reduction of the symmetry to an orthorhombic point group adds an additional term of the form  $\Delta_0 \Delta_1 \cos \theta_1$  to Eq. (2c) and destroys the axial symmetry of the gradient terms. In light of the smallness of the orthorhombic distortion and prevalence of twinning in the copper oxide superconductors [30], we assume the  $\Delta_0 \Delta_1$  term to act as a perturbation on the free energy of the tetragonal lattice and ignore the effect of reduced symmetry on the gradient terms. It is interesting to note that the two d-wave states above do not couple directly to each other up to order  $\ell = 2$  of the relative orbital angular momentum of the Cooper pairs.

## Results

We have performed a full minimization of the free energy with respect to the  $\Delta_i$ 's,  $\theta_i$ 's and the vector potential  $\vec{A}$  to obtain a self-consistent picture of the thermodynamics and spatial variation of the order parameters which reproduces the dominant features of the single-crystal data of the high-T oxides. Even though many parameters appear in Eq. (2), we understand the basic physics in simple qualitative terms. The simplest scenario is that of the

coexistence of a highly anisotropic  $d_{x^2-y^2}$ -state,  $\Delta_1$ , responsible for the quasi-two-dimensional character of these materials, with a nearly isotropic, mixed  $(s+d)$ -state, possibly characterizing the "holon"-pair hopping within the RVB picture [31]. As determined by Kotliar [11], the transition temperature,  $T_1$ , of the  $d$ -state is higher than that of the mixed state. A schematic picture of the relative magnitudes of the order parameters is given in Fig. 1. The relative phases are  $\theta_1 = \pi/2$  and  $\theta_2 = \pi$  near the transition temperatures. The small amount of  $\Delta = \Delta_0 + \Delta_2$  state persisting above the onset temperature,  $\bar{T}$ , is a consequence of the small perturbation to Eq. (2) caused by a shift from tetragonal to orthorhombic symmetry. Perhaps in a naive way, this may be viewed as adding the three-dimensional character necessary for the onset of superconductivity [9]. The existence of  $d$ -wave states, consequently gapless superconductivity, would explain the large observed Sommerfeld coefficients, while the multiple transitions of these states would explain the two specific heat anomalies observed near  $T_c$  [32,33].

We feel that the peak in the ultrasound attenuation results from the oscillations of the relative phases  $\theta_1$  and  $\theta_2$  about their equilibrium values  $\theta_1 = \pi/2$  and  $\theta_2 = \pi$ , as suggested by Kumar and Wolfe [13] in a different context. Defining  $\omega_j^2 = \partial^2 \mathcal{F}_L / \partial \theta_j^2$  ( $j = 1, 2$ ), where  $\mathcal{F}_L = \mathcal{F}_{sq} + \mathcal{F}_T$ , the oscillation frequencies are given by

$$\omega_1^2 = 4\Delta_0^2 \Delta_1^2 \delta_1 \quad , \quad (3a)$$

and

$$\omega_2^2 = \Delta_0 \Delta_2 (\lambda_2 - 8\Delta_0 \Delta_2 \delta_2 + \mu_{20} \Delta_0^2 + \mu_{22} \Delta_2^2) \quad . \quad (3b)$$

There will be a sharp onset of these oscillations at  $\bar{T}$  which will correspond to the attenuation peak at  $T = 0.9 \bar{T}$ .

We next consider the variation of the upper critical field,  $H_{c2}$ , with orientation and temperature. Using a straightforward variational approach on the linearized form of Eq. (2), we have derived the differential GL equations, the full details of which will be presented elsewhere. For the sake of simplicity we assume a  $(s+d)$ -wave mixed state with  $\Delta_0 = \Delta_2 = \Delta_m$  and  $\xi_{0p} = \xi_{2p} = \xi_m$  and write differential equations for fields parallel,  $H_{\parallel}$ , and perpendicular,  $H_{\perp}$  to the  $xy$ -plane. For  $H_{\parallel} = (H, 0, 0)$  and  $\vec{A} = (0, -zH, 0)$ , we have,

$$\Delta_m - (\xi_m \phi_{inv} Hz)^2 \Delta_m + \xi_m^2 (d^2 \Delta_m / dz^2) = 0 \quad , \quad (4a)$$

$$\Delta_1 - (\xi_{1p} \phi_{inv} Hz)^2 \Delta_1 + \xi_{1z}^2 (d^2 \Delta_1 / dz^2) = 0 \quad . \quad (4b)$$

Similarly, for  $H_{\perp} = (0, 0, H)$  and  $\vec{A} = (0, xH, 0)$ , we have

$$(\alpha_m - \lambda_2) \Delta_m - (\alpha_m \xi_m^2 + 2M_{02}) (\phi_{inv} Hx)^2 \Delta_m + (\alpha_m \xi_m^2 + 2M_{01}) (d^2 \Delta_m / dx^2) = 0, \quad (4c)$$

$$\Delta_1 - (\xi_{1p} \phi_{\text{inv}} H_x)^2 \Delta_1 + \xi_{1p}^2 (d^2 \Delta_1 / dx^2) = 0 \quad (4d)$$

These equations are decoupled and can readily be solved for  $H_{c2}$  within the harmonic oscillator approximation to yield

$$\begin{aligned} H_{c2}^{\parallel} &= (\phi_{\text{inv}} \xi_{1p} \xi_{1z})^{-1}, \quad H_{c2}^{\perp} = (\phi_{\text{inv}} \xi_{1p}^2)^{-1} \\ H_{c2} &= (1 - \lambda_2 / \alpha_m) [\phi_{\text{inv}} (\xi_m^2 + 2M_{02} / \alpha_m)]^{-1} \end{aligned} \quad (5)$$

Figure 2 gives the variation of the critical fields with temperature for  $\xi_{1z} < \xi_m < \xi_{1p}$ . For  $H_{c2}^{\parallel}$  the upper critical field is always determined by the smallest coherence length  $\xi_{1z}$  (0 K)  $\sim 7\text{\AA}$ . For  $H_{c2}^{\perp}$  the upper critical field becomes the larger between  $H_{c2}^{\perp}$  and  $H_{c2}^{\parallel}$  as given above. This may explain the discrepancy in the reported 0 K values of the in-plane coherence length ( $\xi_{1p}(0) \sim 34\text{\AA}$ ,  $\xi_m(0) \sim 22\text{\AA}$ ), as well as the kink in the  $H_{c2}$  data.

The variation of the lower critical field,  $H_{c1}$ , with orientation and temperature for the mixed state can be approximated by the expression  $H_{c1} = (\Phi_0 / 4\pi \lambda_{\text{eff}}^2) \ln(\kappa_{\text{eff}})$  [34], which is valid for large values of the GL-parameter,  $\kappa_{\text{eff}} = \lambda_{\text{eff}} / \xi_{\text{eff}}$ . For this case the variation of the internal field occurs mainly in a region where the order parameters exhibit their maximum values. One can therefore obtain the penetration depth,  $\lambda_{\text{eff}}$ , by casting the current relations into the form of the London equation,  $\vec{\nabla} \times \vec{b} = -\lambda_{\text{eff}}^{-2} \vec{a}$ . The results for  $H_{c1}^{\parallel}$  and  $H_{c1}^{\perp}$  are,

$$H_{c1}^{\parallel}: \lambda_{\parallel}^{-2} = 2\lambda_m^{-2} + \lambda_{1z}^{-2} + \lambda_z^{-2} \quad (6a)$$

$$H_{c1}^{\perp}: \lambda_{\perp}^{-2} = 2\lambda_m^{-2} + \lambda_{1p}^{-2} + \lambda_p^{-2} \quad (6b)$$

where the same assumptions on  $\Delta_0$  and  $\Delta_2$  were made as for the calculation of  $H_{c2}$ . At temperatures near  $T_c = T_1$  the lower critical field should behave as  $\lambda_1^{-2}$  since it is proportional to the square of the order parameter. Consequently the anisotropy of  $H_{c1}$  should go as the square of the anisotropy of  $H_{c2}$ . At lower temperatures the influence of the coupling terms  $\lambda_{p2}^{-2}$  and  $\lambda_{z2}^{-2}$  makes predictions more difficult. The anticipated behavior of  $H_{c1}^{\perp}$  for several values of the coupling terms is given in Fig. 3. We are at present not aware of any single-crystal  $H_{c1}$  studies over the entire temperature range 0 -  $T_c$ .

### Summary

We have analyzed the thermodynamic, magnetic and ultrasound attenuation data on oriented samples of the high- $T_c$  superconductors within the context of anisotropic Ginzburg-Landau theory for coupled, even-parity superconducting states. We are able to present a consistent interpretation of the data in terms of the coexistence of a quasi-two-dimensional d-wave state, with critical temperature  $T_1 = T_c$  and a more isotropic mixed (s+d)-wave state with critical temperature  $T_m < T_c$ . We predict the possibility of a "kink" in the temperature dependence of the lower critical field near  $0.9T_c$ , which should be tested by experiments on single crystals.

### Acknowledgments

This research was supported by the Office of Naval Research.

### Literature Cited

1. Bednorz, J. G.; Müller, K. A. Z. Phys. B 1986, 64, 188.
2. Tozer, S. W.; Kleinsasser, A. W.; Penney, T.; Kaiser, D.; Holtzberg, F. Phys. Rev. Lett. 1987, 59, 1768.
3. Dinger, T. R.; Worthington, T. K.; Gallagher, W. J.; Sandstrom, R. L. Phys. Rev. Lett. 1987, 58, 2687.
4. Batlogg, B.; Ramirez, A. P.; Cava, R. J.; von Dover, R. B.; Rietman, E. A. Phys. Rev. B 1987, 35, 5340.
5. Hidaka, Y.; Enomoto, Y.; Sukuki, M.; Oda, M.; Murakami, T. Jpn. J. Appl. Phys. 1987, 26, L377.
6. Worthington, T. K.; Gallagher, W. J.; Dinger, T. R. Phys. Rev. Lett. 1987, 59, 1160.
7. Moodera, J. S.; Meservey, R.; Tkaczyk, J. E.; Hao, C. X.; Gibson, G. A.; Tedrow, P. W. Phys. Rev. B 1988, 37, 619.
8. Gulacsi, Zs.; Gulacsi, M.; Pop, I. Phys. Rev. B 1988, 37, 2247.
9. Wen, X.-G.; Kan, R. Phys. Rev. B 1988, 37, 595.
10. Anderson, P. W. Science 1987, 235, 1196.
11. Kotliar, G. Phys. Rev. B 1987, 37, 3664.
12. Inui, M.; Doniach, S.; Hirschfeld, P. J.; Ruckenstein, A. E. Phys. Rev. B 1988, 37, 2320.
13. Kumar, P.; Wolfle, P. Phys. Rev. Lett. 1987, 59, 1954.
14. Rauchschalbe, U.; Steglich, F.; Stewart, G. R.; Giorgi, A. L.; Fulde, P.; Maki, K. Europhys. Lett. 1987, 3, 751.
15. Rauchschalbe, U.; Bredl, C. D.; Steglich, F.; Maki, K.; Fulde, P. Europhys. Lett. 1987, 3, 757.
16. Cooper, J. R.; Chu, C. T.; Zhou, L. W.; Dunn, B.; Grüner, G. Phys. Rev. B 1988, 37, 638.
17. Cheong, S. W.; Brown, S. E.; Fisk, Z.; Kwok, R. S.; Thompson, J. D.; Zirngiebl, E.; Grüner, G.; Peterson, D. E.; Wells, G. L.; Schwarz, R. B.; Cooper, J. R. Phys. Rev. B 1987, 36, 3913.
18. von Molnar, S.; Torressen, A.; Kaiser, D.; Holtzberg, F.; Penney, T. Phys. Rev. B 1988, 37, 3762.
19. Xu, M-F.; Baum, H-P.; Schenstrom, A.; Sarma, B. K.; Levy, M.; Sun, K. J.; Toth, L. E.; Wolf, S. A.; Gubser, D. U. Phys. Rev. B 1988, 37, 3675.
20. Bhattacharya, S.; Higgins, M. J.; Johnston, D. C.; Jacobson, A. J.; Stokes, J. P.; Lewandowski, J. T.; Goshorn, D. P. Phys. Rev. B 1988, 37, 5901.
21. Horn, P. M.; Keane, D. T.; Held, G. A.; Jordan-Sweet, J. L.; Kaiser, D. L.; Holtzberg, F.; Rice, T. M. Phys. Rev. Lett. 1987, 59, 2772.
22. Morris, R. C.; Coleman, R. V.; Bhandari, R. Phys. Rev. B 1972, 8, 895. Spatial and not k-space anisotropy is implied here.
23. Sahu, D.; Langner, A.; George, T. F. unpublished.
24. Ferreira, J. M.; Lee, B. W.; Dalichaouch, Y.; Torikachvili, M. S.; Yang, K. N.; Maple, M. B. Phys. Rev. B 1988, 37, 1580.
25. Kumagai, K.; Nakamichi, Y.; Watanabe, I.; Nakamura, Y.; Nakajima, H.; Wada, N.; Lederer, P. Phys. Rev. Lett. 1988, 60, 724.



26. Langner, A.; Sahu, D.; George, T. F. Proceedings of the Conference on Superconductivity and Applications, ed. by H. S. Kwok (Elsevier, New York, 1988).
27. Kapitulnik, A.; Beasley, M. R.; Castellani, C.; DiCastro, C. Phys. Rev. B 1988, 37, 537.
28. Baskaran, G.; Zou, Z.; Anderson, P. W. Solid State Commun. 1987, 63, 973.
29. The term  $\Delta_0 \Delta_2 \cos \theta_2 [\lambda_2 + \mu_2 (\Delta_0^2 + \Delta_2^2)]$  of Ref. [23] is too restrictive since  $\Delta_2$  and  $\Delta_0$  need not have the same coefficients to be invariant terms.
30. You, H; Axe, J. D.; Kan, X. B.; Moss, S. C.; Lin, J. Z.; Lam, D. J. Phys. Rev. B 1988, 37, 2361.
31. Wheatly, J. W.; Hsu, T. C.; Anderson, P. W. Phys. Rev. B 1988, 37, 5897.
32. Inderhees, S. E.; Salamon, M. B.; Goldenfeld, N.; Rice, J. P.; Pazol, B. G.; Ginsberg, D. M.; Liu, J. Z.; Crabtree, G. W. Phys. Rev. Lett. 1988, 60, 1178.
33. Butera, R. A. Phys. Rev. B 1988, 37, 5909.
34. Fetter, A. L.; Hohenberg, P. C. In Superconductivity; Parks, R. D., Ed.; Marcel Dekker, New York, 1969; p. 817 ff.

### Figure Captions

Figure 1. Schematic temperature dependence of the superconducting order parameters, where  $\Delta_m$  is for the mixed (s+d)-state and  $\Delta_1$  for the pure  $d_{x^2-y^2}$ -state.  $T_1$  and  $T = a = T_m$  are the critical temperatures of the mixed and pure states, respectively, and  $T = b = \bar{T}$  is the onset temperature.

Figure 2. Schematic temperature dependence of the upper critical field,  $H_{c2}$ . The dashed curves are not experimentally observable.  $H_{c2}^{\parallel}$  is the field parallel to the ab-plane, and  $H_{c2}^{\perp}$  is the field parallel to c-axis.  $T = a = T_m$  and  $T = b = \bar{T}$ .

Figure 3. Schematic temperature dependence of the lower critical field,  $H_{c1}$ . The dashed curves represent the effect of the coupling terms  $\lambda_p^{-2}$  and  $\lambda_z^{-2}$ .  $T = a = T_m$  and  $T = b = \bar{T}$ .

Fig. 1

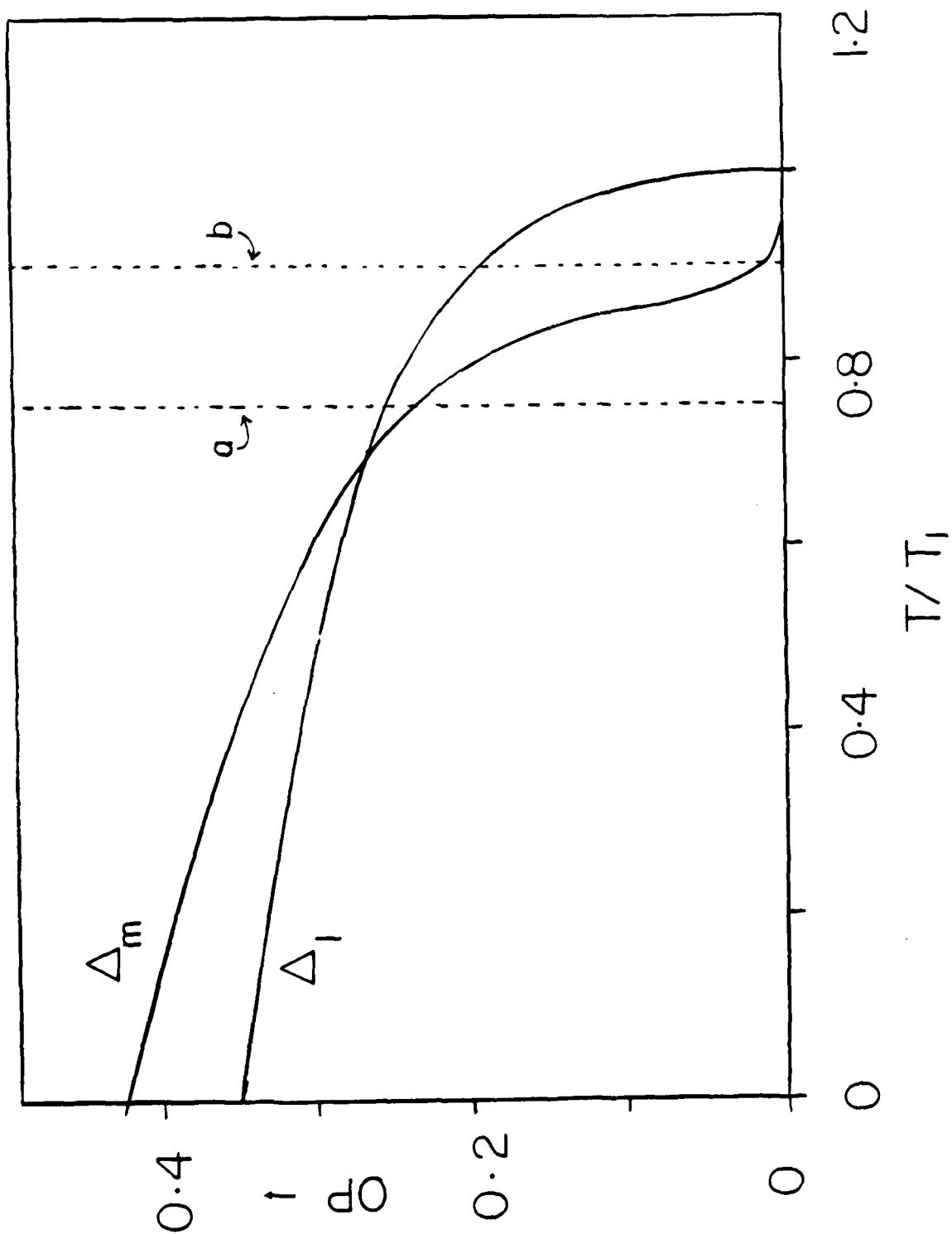


Fig. 2

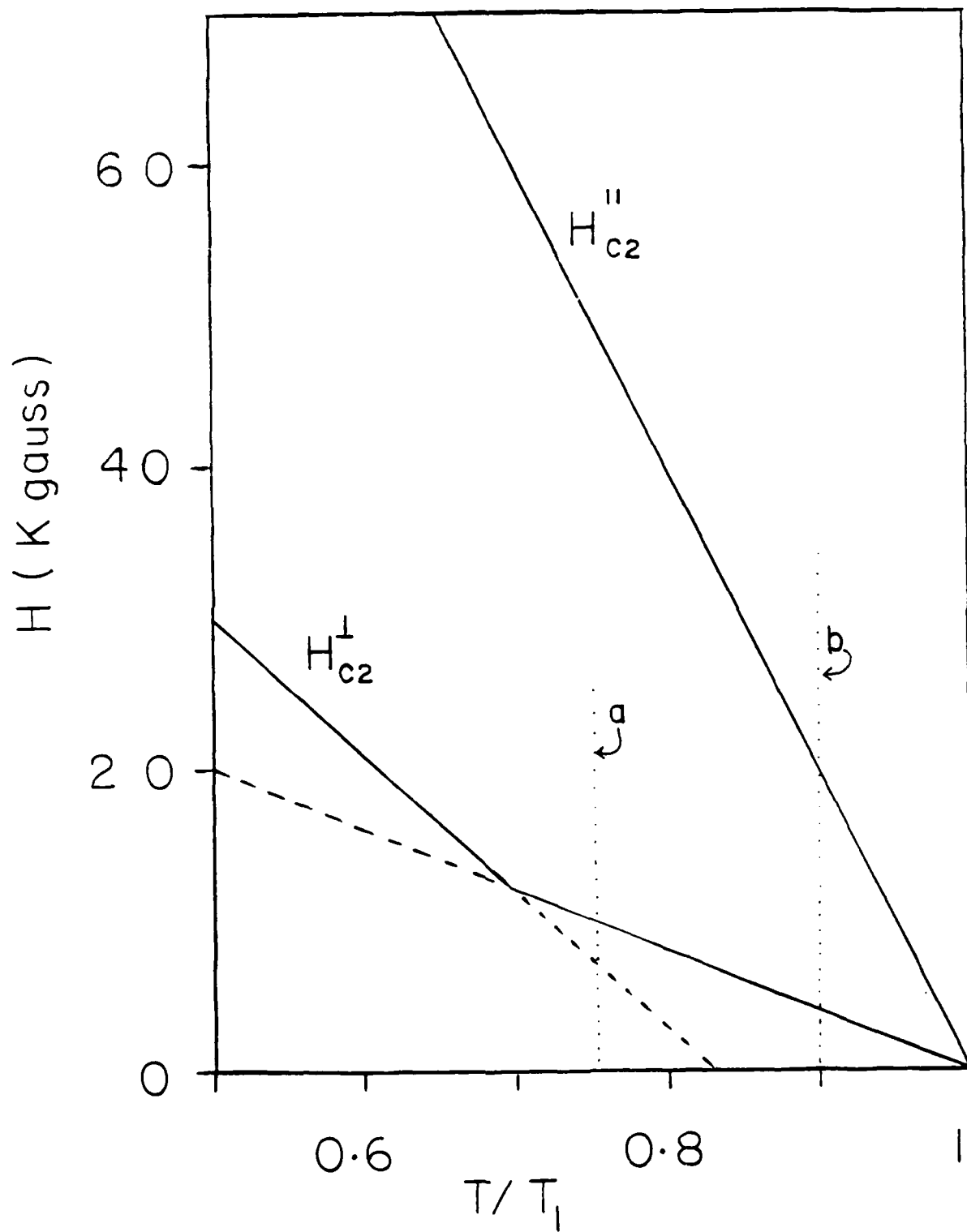
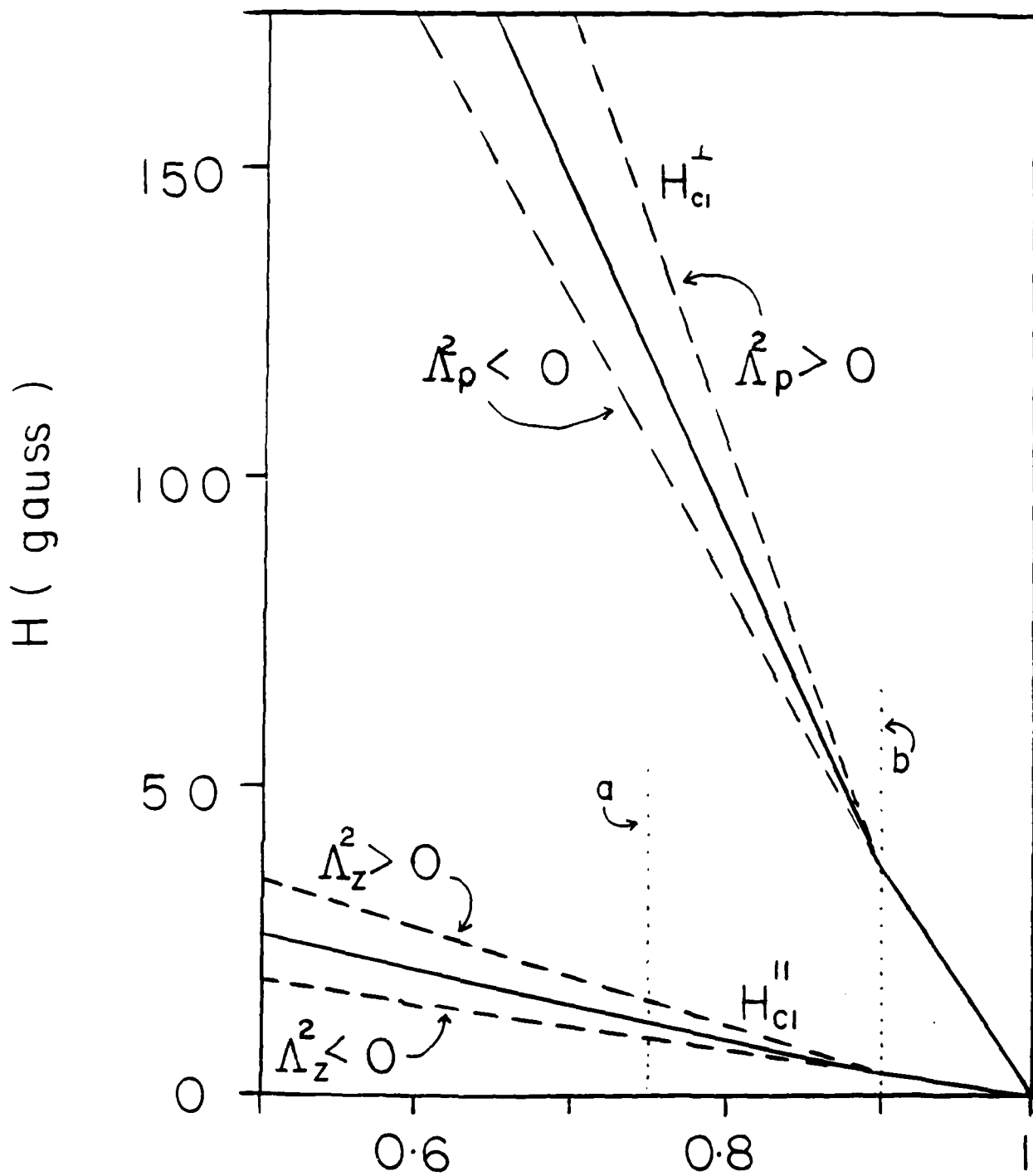


Fig. 3



TECHNICAL REPORT DISTRIBUTION LIST, GEN

	<u>No. Copies</u>		<u>No. Copies</u>
Office of Naval Research Attn: Code 1113 800 N. Quincy Street Arlington, Virginia 22217-5000	2	Dr. David Young Code 334 NORDA NSTL, Mississippi 39529	1
Dr. Bernard Douda Naval Weapons Support Center Code 50C Crane, Indiana 47522-5050	1	Naval Weapons Center Attn: Dr. Ron Atkins Chemistry Division China Lake, California 93555	1
Naval Civil Engineering Laboratory Attn: Dr. R. W. Drisko, Code L52 Port Hueneme, California 93401	1	Scientific Advisor Commandant of the Marine Corps Code RD-1 Washington, D.C. 20380	1
Defense Technical Information Center Building 5, Cameron Station Alexandria, Virginia 22314	12 high quality	U.S. Army Research Office Attn: CRD-AA-IP P.O. Box 12211 Research Triangle Park, NC 27709	1
DTNSRDC Attn: Dr. H. Singerman Applied Chemistry Division Annapolis, Maryland 21401	1	Mr. John Boyle Materials Branch Naval Ship Engineering Center Philadelphia, Pennsylvania 19112	1
Dr. William Tolles Superintendent Chemistry Division, Code 6100 Naval Research Laboratory Washington, D.C. 20375-5000	1	Naval Ocean Systems Center Attn: Dr. S. Yamamoto Marine Sciences Division San Diego, California 91232	1
		Dr. David L. Nelson Chemistry Division Office of Naval Research 800 North Quincy Street Arlington, Virginia 22217	1

ABSTRACTS DISTRIBUTION LIST, 056/625/629

Dr. J. E. Jensen  
Hughes Research Laboratory  
3011 Malibu Canyon Road  
Malibu, California 90265

Dr. C. B. Harris  
Department of Chemistry  
University of California  
Berkeley, California 94720

Dr. J. H. Weaver  
Department of Chemical Engineering  
and Materials Science  
University of Minnesota  
Minneapolis, Minnesota 55455

Dr. F. Kutzler  
Department of Chemistry  
Box 5055  
Tennessee Technological University  
Cookeville, Tennessee 38501

Dr. A. Reisman  
Microelectronics Center of North Carolina  
Research Triangle Park, North Carolina  
27709

Dr. D. DiLella  
Chemistry Department  
George Washington University  
Washington D.C. 20052

Dr. M. Grunze  
Laboratory for Surface Science and  
Technology  
University of Maine  
Orono, Maine 04469

Dr. R. Reeves  
Chemistry Department  
Rensselaer Polytechnic Institute  
Troy, New York 12181

Dr. J. Butler  
Naval Research Laboratory  
Code 6115  
Washington D.C. 20375-5000

Dr. Steven M. George  
Stanford University  
Department of Chemistry  
Stanford, CA 94305

Dr. L. Interante  
Chemistry Department  
Rensselaer Polytechnic Institute  
Troy, New York 12181

Dr. Mark Johnson  
Yale University  
Department of Chemistry  
New Haven, CT 06511-8118

Dr. Irvin Heard  
Chemistry and Physics Department  
Lincoln University  
Lincoln University, Pennsylvania 19352

Dr. W. Knauer  
Hughes Research Laboratory  
3011 Malibu Canyon Road  
Malibu, California 90265

Dr. K.J. Klaubunde  
Department of Chemistry  
Kansas State University  
Manhattan, Kansas 66506

ABSTRACTS DISTRIBUTION LIST, 056/625/629

Dr. G. A. Somorjai  
Department of Chemistry  
University of California  
Berkeley, California 94720

Dr. J. Murday  
Naval Research Laboratory  
Code 6170  
Washington, D.C. 20375-5000

Dr. J. B. Hudson  
Materials Division  
Rensselaer Polytechnic Institute  
Troy, New York 12181

Dr. Theodore E. Madey  
Surface Chemistry Section  
Department of Commerce  
National Bureau of Standards  
Washington, D.C. 20234

Dr. J. E. Demuth  
IBM Corporation  
Thomas J. Watson Research Center  
P.O. Box 218  
Yorktown Heights, New York 10598

Dr. M. G. Lagally  
Department of Metallurgical  
and Mining Engineering  
University of Wisconsin  
Madison, Wisconsin 53706

Dr. R. P. Van Duyne  
Chemistry Department  
Northwestern University  
Evanston, Illinois 60637

Dr. J. M. White  
Department of Chemistry  
University of Texas  
Austin, Texas 78712

Dr. D. E. Harrison  
Department of Physics  
Naval Postgraduate School  
Monterey, California 93940

Dr. R. L. Park  
Director, Center of Materials  
Research  
University of Maryland  
College Park, Maryland 20742

Dr. W. T. Peria  
Electrical Engineering Department  
University of Minnesota  
Minneapolis, Minnesota 55455

Dr. Keith H. Johnson  
Department of Metallurgy and  
Materials Science  
Massachusetts Institute of Technology  
Cambridge, Massachusetts 02139

Dr. S. Sibener  
Department of Chemistry  
James Franck Institute  
5640 Ellis Avenue  
Chicago, Illinois 60637

Dr. <sup>Arnold</sup> Arnold Green  
Quantum Surface Dynamics Branch  
Code 3817  
Naval Weapons Center  
China Lake, California 93555

Dr. A. Wold  
Department of Chemistry  
Brown University  
Providence, Rhode Island 02912

Dr. S. L. Bernasek  
Department of Chemistry  
Princeton University  
Princeton, New Jersey 08544

Dr. W. Kohn  
Department of Physics  
University of California, San Diego  
La Jolla, California 92037



ABSTRACTS DISTRIBUTION LIST, 056/625/629

Dr. F. Carter  
Code 6170  
Naval Research Laboratory  
Washington, D.C. 20375-5000

Dr. Richard Colton  
Code 6170  
Naval Research Laboratory  
Washington, D.C. 20375-5000

Dr. Dan Pierce  
National Bureau of Standards  
Optical Physics Division  
Washington, D.C. 20234

Dr. R. Stanley Williams  
Department of Chemistry  
University of California  
Los Angeles, California 90024

Dr. R. P. Messmer  
Materials Characterization Lab.  
General Electric Company  
Schenectady, New York 22217

Dr. Robert Gomer  
Department of Chemistry  
James Franck Institute  
5640 Ellis Avenue  
Chicago, Illinois 60637

Dr. Ronald Lee  
R301  
Naval Surface Weapons Center  
White Oak  
Silver Spring, Maryland 20910

Dr. Paul Schoen  
Code 6190  
Naval Research Laboratory  
Washington, D.C. 20375-5000

Dr. John T. Yates  
Department of Chemistry  
University of Pittsburgh  
Pittsburgh, Pennsylvania 15260

Dr. Richard Greene  
Code 5230  
Naval Research Laboratory  
Washington, D.C. 20375-5000

Dr. L. Kesmodel  
Department of Physics  
Indiana University  
Bloomington, Indiana 47403

Dr. K. C. Janda  
University of Pittsburgh  
Chemistry Building  
Pittsburg, PA 15260

Dr. E. A. Irene  
Department of Chemistry  
University of North Carolina  
Chapel Hill, North Carolina 27514

Dr. Adam Heller  
Bell Laboratories  
Murray Hill, New Jersey 07974

Dr. Martin Fleischmann  
Department of Chemistry  
University of Southampton  
Southampton SO9 5NH  
UNITED KINGDOM

Dr. H. Tachikawa  
Chemistry Department  
Jackson State University  
Jackson, Mississippi 39217

Dr. John W. Wilkins  
Cornell University  
Laboratory of Atomic and  
Solid State Physics  
Ithaca, New York 14853

ABSTRACTS DISTRIBUTION LIST, 056/625/629

Dr. R. G. Wallis  
Department of Physics  
University of California  
Irvine, California 92664

Dr. D. Ramaker  
Chemistry Department  
George Washington University  
Washington, D.C. 20052

Dr. J. C. Hemminger  
Chemistry Department  
University of California  
Irvine, California 92717

Dr. T. F. George  
Chemistry Department  
University of Rochester  
Rochester, New York 14627

Dr. G. Rubloff  
IBM  
Thomas J. Watson Research Center  
P.O. Box 218  
Yorktown Heights, New York 10598

Dr. Horia Metiu  
Chemistry Department  
University of California  
Santa Barbara, California 93106

Dr. W. Goddard  
Department of Chemistry and Chemical  
Engineering  
California Institute of Technology  
Pasadena, California 91125

Dr. P. Hansma  
Department of Physics  
University of California  
Santa Barbara, California 93106

Dr. J. Baldeschwieler  
Department of Chemistry and  
Chemical Engineering  
California Institute of Technology  
Pasadena, California 91125

Dr. J. T. Keiser  
Department of Chemistry  
University of Richmond  
Richmond, Virginia 23173

Dr. R. W. Plummer  
Department of Physics  
University of Pennsylvania  
Philadelphia, Pennsylvania 19104

Dr. E. Yeager  
Department of Chemistry  
Case Western Reserve University  
Cleveland, Ohio 41106

Dr. N. Winograd  
Department of Chemistry  
Pennsylvania State University  
University Park, Pennsylvania 16802

Dr. Roald Hoffmann  
Department of Chemistry  
Cornell University  
Ithaca, New York 14853

Dr. A. Steckl  
Department of Electrical and  
Systems Engineering  
Rensselaer Polytechnic Institute  
Troy, New York 12181

Dr. G.H. Morrison  
Department of Chemistry  
Cornell University  
Ithaca, New York 14853