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THE USE OF NUMERICAL METHODS AND MICROCOMPUTERS IN UNDERGRADUATE EXPERIMENTS

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THE USE OF NUMERICAL METHODS AND MICROCOMPUTERS IN UNDERGRADUATE EXPERIMENTS

by

Mark R. Stevens

A Thesis Submitted to the Graduate

Faculty of Rensselaer Polytechnic Institute

in Partial Fulfillment of the

Requirements for the Degree of

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ABSTRACT

Advancements in the semiconductor industry in the last few years have led to more inexpensive and powerful microcomputers. It is inevitable that students will encounter some type of computer system at lower levels in the educational system. A vital part of a student's education should be to learn how to operate and utilize these systems. As the appearance of computers in educational institutions increases it is logical that they should be used in laboratory settings where their speed and analytical capabilities can be exploited for taking and analyzing data.

The analytical power of a microcomputer in experiments is demonstrated through the use of numerical methods to solve the differential equations of motion. Both Heun's method (a second order Runge-Kutta method) and a fourth order Predictor-Corrector method are used to calculate approximate solutions to the equations of motion for physical systems. These rather tedious calculations are performed quickly with the computer and provide solutions for differential equations which are difficult or impossible to solve analytically in closed form. These methods are used to simulate and analyze the motion of a rotating disk and a physical pendulum, both including friction and air resistance. The motion of each system is recorded and plotted by the microcomputer. The Pascal software written allows comparison of the data with the numerical solution and will also calculate constants of the actual motion through a curve fitting iterative process.

The ensuing laboratory setup of disk, pendulum and computer is then used in two college freshman experiments and one experiment at the level of a college junior. These exercises teach the power, speed and versatility of the computer in the laboratory; the power, usefulness and accuracy of numerical method solutions; and the characteristics of rotational and harmonic motion including the effects of friction and air resistance on each system.

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1. INTRODUCTION AND HISTORICAL REVIEW

No field of science has advanced more rapidly in the past decade than the field of semiconductors and computers. The impact of smaller, faster, more efficient and affordable computing systems has been felt by the business and scientific community alike. This continuing trend has made the presence of personal computers (or microcomputers) in classrooms and laboratories no longer a luxury, but more of a necessity. With a great part of industry utilizing and depending on microcomputers it becomes extremely important that students currently in educational institutions become familiar with the use and possible applications of such systems.

Currently, most technical institutions do a good job of teaching their students the languages used on mainframe computers. Courses are offered in most higher level languages as well as the more specialized, lower level languages such as Assembler. There are even courses available which teach personal computing and the use of applications software. Unfortunately, an important area rich in possibilities is often overlooked. The speed, versatility and analytical capability of even the simplest microcomputers lend themselves to use in scientific laboratories. The introduction of such systems into the laboratory opens a wide variety of educational opportunities to students. These opportunities not only include analytical and computational possibilities but allow greater insight into physical processes through data collection and analysis.

There are a number of ways to utilize the capabilities of a microcomputer in the laboratory. Firstly, they can be used for data acquisition. Experiments can be conducted and controlled using continuously updated data from static sensors. Position and velocity calculations can be recorded by making repeated measurements in microseconds using an internal clock. Secondly, the analysis of data is greatly facilitated by a microcomputer. Curve fitting, differentiation, integration and simulations are all possible utilizing numerical techniques. Any combination of these capabilities in the laboratory would be an important addition to a student's education.

Three experiments were developed for the purpose of teaching physics while demonstrating the power of microcomputers. Two of these are suitable for a freshman in college, and one is designed for the more advanced level of a junior. To demonstrate data collecting capability a physical pendulum and rotating disk were selected for investigation. Utilizing a notched wheel and photogates the microcomputer is used to take rapid measurements of the passing notches and record the resulting angular velocity of the motion as a function of time. Once the data is taken and recorded it is analyzed with the aid of the computer. Two numerical methods for solving differential equations are used to simulate the motion of each system. Heun's method is used for the freshman experiments and a fourth order Predictor-Corrector method for the junior experiment. Two computer systems are also needed. To take and analyze the data for the two freshman experiments a TRS - 80 Color Computer is used. A Zenith Z-140 personal computer is also employed because of a requirement for greater accuracy and speed for an iterative curve fitting routine in the junior's experiment.

The above selection of physical systems and numerical methods accomplishes a number of goals. First, it allows the student to more thoroughly investigate the physics involved with harmonic motion including frictional and viscous damping. The effects of varying different parameters are easily observed and verified with the experimental setup. Second, the usefulness of the computer is readily apparent in the ease in which the system records and plots the angular velocity of the motion. This aspect of the motion would be difficult to measure without the computer. Finally, using the numerical method demonstrates the power of the computer in calculating approximate solutions to normally unsolvable differential equations. Letting the student examine the accuracy of such methods builds confidence in the technique. After the completion of these experiments the student should feel comfortable using the computer and have a good

appreciation for the versatility and capabilities of the microcomputer in the laboratory. Armed with this experience the student should be more apt to utilize this powerful tool in his continued education and research.

2. THEORY

2.1 Physics Theory

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Numerous physical systems are suitable for investigation using a computer. In choosing the physical pendulum and rotating disk two goals are met. First, both systems are relatively simple, easily constructed and understood. Second, in the case of the pendulum the differential equations of motion are not solvable analytically. Thus it is a good system for demonstrating the power and application of a numerical method. Also, because of the difficulty of solution, the physical pendulum is not often seen in the laboratory, and certainly not with targe angle oscillations including frictional and viscous damping. While the solution to the rotating disk is less complicated, addition of viscous damping again demonstrates the numerical method as well as the concept of terminal velocity.

2.1.1 The Physical Pendulum

The simple pendulum all students learn about is actually an idealization of a physical pendulum. Any real pendulum is necessarily a physical pendulum. In developing the equations of motion we define d as the distance from the rotation axis to the center of mass, θ as the angle between the line from the pivot through the center of mass and the vertical and I is the moment of inertia of the oscillating body (Figure 2.1.1).

In the absence of any damping, using ω as the angular velocity, the equation of motion is

$$I\frac{d\omega}{dt} = -mgd \sin\theta$$

where m is the total mass and g is the acceleration due to gravity.¹ Solving this equation for ω and comparing it to the actual motion of a pendulum we can determine



Figure 2.1.1. The Physical Pendulum

the system parameters such as the moment of inertia, providing damping can be neglected.

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Unfortunately, friction and damping are inseparable parts of any real system. Naturally this affects the equations of motion. In the case of viscous damping the force can be approximated as being proportional to some power of the linear velocity of the resisting body moving through the viscous medium. In our case the major source of air resistance is due to plates fixed to the pendulum at a distance l. The torque resulting from this force is always opposed to the direction of motion and modifies the previous equation to

$$I\frac{d\omega}{dt} = -mgd \sin\theta \pm kl(k\omega)^n$$

where n is an integer and k is a constant that accounts for the geometry of the plates as well as the proportion of the force to the velocity.² The plus or minus is only necessary for even values of n as the sign of ω will change this term correctly for odd n م برند د د د ر

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values. In actuality the force is dependent on a polynomial which is a function of the velocity. However, since only one term dominates, and for the sake of simplicity, we will only use one term in the polynomial. The factor k will also vary depending on the state (temperature, pressure, humidity) of the viscous fluid that the system is in.

Finally, the pivot in the laboratory is made as close to ideal as possible by utilizing ball bearings but it also provides a frictional damping which must be considered. Because the friction involved in the bearing is rolling friction and the magnitude is small, its effect can be considered constant and opposite to the direction of motion. Denoting this constant opposing torque by f, the final equation of motion is

$$I\frac{d\omega}{dt} = -mgd \sin\theta \pm kl(k\omega)^n \pm f$$

The exact solution of any of these equations is difficult, except when the small angle approximation $(\sin\theta = \theta)$ is made for the undamped case. An accurate approximate solution to these equations can be obtained though, through the application of numerical methods.

2.1.2 The Accelerated Disk

Generally students learn about terminal velocity by considering a sky diver or an object dropped from a tall building. By using a rotating disk it is easy to demonstrate this concept in the laboratory. In developing the equation of motion for this system r is defined as the radius from the axis of rotation to the point where the accelerating weight is attached, ω is the angular velocity and I is again the moment of inertia of the disk (Figure 2.1.2). Using simple Newtonian mechanics we know that mg - T = ma where T is the tension in the cord and a is the downward acceleration of the mass. We also know that the torque caused by the weight is given by $Tr = I\frac{d\omega}{dt}$. Noting that a = $r\frac{d\omega}{dt}$ we can eliminate the acceleration between the two equations and solve for the tension T. Thus, neglecting damping, the total torque acting on the disk can be written³ T ALLER CLUCKN REPORT AREAST RECENT SUCCESSION DESCRIPTION REPORT PROVES BOARDY IN



Figure 2.1.2. The Accelerated Disk

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$$I\frac{d\omega}{dt} = \frac{mgrI}{I+mr^3}$$

In order to attain a terminal velocity the effects of air resistance must be included. Again the viscous damping force is proportional to some power of the linear velocity of the plates on the disk which cause most of the resistance. This modifies the total torque to be

$$I\frac{d\omega}{dt} = \frac{mgrI}{I+mr^2} - kl(k\omega)^n$$

where l is the distance to the center of the resisting plates and k is the proportionality constant. This equation of motion would demonstrate terminal velocity, however we have neglected the rolling resistance of the bearings. Including this effect we obtain

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$$I\frac{d\omega}{dt} = \frac{mgrI}{I+mr^2} \cdot kl(k\omega)^n \cdot f$$

where f again represents this constant factor. Again, terminal velocity is achieved when the net torque is zero.

As was the case with the simple pendulum, these equations of motion considering the viscous forces are not easy to solve analytically. We again turn to numerical methods to provide accurate approximate solutions to this motion.

2.2 Mathematical Theory

Numerical methods exist for a variety of mathematical tasks. We are concerned with only those methods useful in solving second order differential equations. Different methods have advantages and disadvantages involving speed, accuracy and application. Numerical techniques for solving differential equations are divided into one step and multistep methods. Both types of methods are utilized in the simulation routines for the experiments. The primary one step technique is the Runge-Kutta method while the Predictor-Correcto: method is representative of the multistep techniques.

2.2.1 Runge-Kutta Methods

Runge-Kutta methods are designated as one step methods because they only require the initial conditions in order to calculate a solution. Because of this capability they are also classified as being self starting. They approximate the value for the next point of the solution to a differential equation given an incremental step size for the independent variable using only the value of the point before. The general one step method is an iteration that takes the form ⁴

$$y_{i+1} = y_i + h\Phi(x_i, y_i; h)$$
 $i = 0, 1, ..., n-1$

The function $\Phi(x_i, y_i; h)$ is called the increment function and tells us how to proceed from

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an estimated y_i for $y(x_i)$ to the next point y_{i+1} for $y(x_{i+1})$. The variable h is the step size taken with the independent variable. The definition of the function $\Phi(x_i, y_i; h)$ depends on the particular method.

If we think of differential equations as specifying the slope of the solution at points in space we can construct flow fields which give us an idea of the form of the solution. For example, the differential equation y' = y(2 - y) has the flow field shown in Figure 2.2.1.⁵ As we move from the point x_i to x_{i+1} the nature of the flow field governs the change in the solution y(x) between the two points. It makes sense to sample the flow field between the points and then specify the increment function as a weighted average of the samplings. Thus

$$\Phi_{\mathbf{k}}(\mathbf{x}_{i},\mathbf{y}_{i};\mathbf{h}) = \mathbf{A}_{1} \mathbf{f}(\boldsymbol{\theta}_{1},\boldsymbol{\gamma}_{1}) + \mathbf{A}_{2} \mathbf{f}(\boldsymbol{\theta}_{2},\boldsymbol{\gamma}_{2}) + \ldots + \mathbf{A}_{k} \mathbf{f}(\boldsymbol{\theta}_{k},\boldsymbol{\gamma}_{k})$$

The problem reduces to choosing the weights A_j and the specific sample points (θ_j, γ_j) in the interval.

Before specifying how the Runge-Kutta method selects these weights, we need to digress to the more familiar Taylor series method. If we expand our function in a Taylor series we have

$$y(x_1) = y(x_0) + y'(x_0)h + y''(x_0)\frac{h^2}{2!} + y^k(x_0)\frac{h^k}{k!} + y^{k+1}(\theta)\frac{h^{k+1}}{(k+1)!}$$

When y(x) is sufficiently differentiable the more terms carried, the more accurate the approximation. Since we are given y'(x) = f(x,y) (our equation to solve) we can calculate the higer order derivatives as necessary. Our increment function is then⁶

$$\Phi_{k} = T_{k}(x,y;h) = f(x,y) + f'(x,y)\frac{h}{2} + \ldots + f^{k-1}(x,y)\frac{h^{k-1}}{k!}$$

The difficulty with this method is that it requires the knowledge of the higher order derivatives. As a result, higher order Taylor methods are rarely used.



Figure 2.2.1. Example Flow Field

The German mathematicians C. Runge and M. W. Kutta sought to circumvent the problem of higher order derivatives inherent in the Taylor method. The basis for the Runge-Kutta method is to choose the sampling points and weighting functions A_j so that they agree as well as possible with the increment function for the equivalent Taylor series method. Note that the familiar Euler's method $y_{i+1} = y_i + hf(x_i, y_i)$ is both a first order Taylor series and Runge-Kutta method. The simplest way to demonstrate the method is to use an example.

For a second order Runge-Kutta method we need two sample points. Choosing the points (x_i, y_i) and $(x_i + \beta h, y_i + \beta h f(x_i, y_i))$, where β is undetermined, the increment function is of the form

$$\Phi_2(\mathbf{x}_i, \mathbf{y}_i; \mathbf{h}) = \mathbf{A}_1 \mathbf{f}(\mathbf{x}_i, \mathbf{y}_i) + \mathbf{A}_2 \mathbf{f}(\mathbf{x}_i + \beta \mathbf{h}, \mathbf{y}_i + \beta \mathbf{h} \mathbf{f}(\mathbf{x}_i, \mathbf{y}_i))$$

We want to match this with the Taylor series increment function

$$T_2(x_i, y_i; h) = f(x_i, y_i) + \frac{h}{2}[f_x(x_i, y_i) + f_y(x_i, y_i)f(x_i, y_i)]$$

To do this we expand the function associated with A_2 in a Taylor series yielding

$$f(\mathbf{x}_i + \beta \mathbf{h}, \mathbf{y}_i + \beta \mathbf{h}f(\mathbf{x}_i, \mathbf{y}_i)) = f(\mathbf{x}_i, \mathbf{y}_i) + f_{\mathbf{x}}(\mathbf{x}_i, \mathbf{y}_i)\beta \mathbf{h} + f_{\mathbf{y}}(\mathbf{x}_i, \mathbf{y}_i)\beta \mathbf{h}f(\mathbf{x}_i, \mathbf{y}_i) + \mathbf{E}$$

where the remainder E is of the form Ch^2 . Substituting into Φ_2 and collecting like terms we find '

$$\Phi_{2}(\mathbf{x}_{i},\mathbf{y}_{i};\mathbf{h}) = (\mathbf{A}_{1} + \mathbf{A}_{2})f(\mathbf{x}_{i},\mathbf{y}_{i}) + \mathbf{A}_{2}h[\beta f_{\mathbf{x}}(\mathbf{x}_{i},\mathbf{y}_{i}) + \beta f_{\mathbf{y}}(\mathbf{x}_{i},\mathbf{y}_{i})f(\mathbf{x}_{i},\mathbf{y}_{i}) + \mathbf{C}h]$$

Comparing this with $T_2(x_i, y_i; h)$ we get a fairly close match if $A_1 + A_2 = 1$ and $A_2\beta = \frac{1}{2}$. This means that

$$\Phi_2(\mathbf{x}_i, \mathbf{y}_i; \mathbf{h}) = \mathbf{T}_2(\mathbf{x}_i, \mathbf{y}_i; \mathbf{h}) + \mathbf{A}_2 \mathbf{C} \mathbf{h}^2$$

so the error in approximating the function is partly due to the error in the Taylor expansion $T_2(x_i, y_i; h)$ of the order Bh^2 and to the error in matching $T_2(x_i, y_i; h)$ of the order A_2Ch^2 . Looking at the relationship of the coefficients we see that $A_2 = \frac{1}{2\beta}$ and $A_1 = 1 - \frac{1}{2\beta}$. There are an infinite number of solutions for these parameters, however a natural choice is $\beta = \frac{1}{2}$ yielding

$$y_{i+1} = y_i + hf(x_i + \frac{h}{2}, y_i + \frac{h}{2}f(x_i, y_i))$$

This is the modified Euler's method where the sampling point is one half of the way into the interval. Another choice is $\beta = 1$ which yields

This is Heun's method and it samples the flow field at the beginning and the end of the interval and gives each value an equal weight. Figure 2.2.2 is a graphic example of how the sampling method works for Heun's method. Both of these methods are of second order and have the same magnitude of error, proportional to h^2 . Heun's method will be used extensively.

It is possible to use this technique to develop higher order methods, the benefit being greater accuracy, the cost being increased calculation time. A popular fourth order method which will also be employed is⁴

$$y_{i+1} = y_i + \frac{h}{6}[K_1 + 2K_2 + 2K_3 + K_4]$$

where

$$K_{1} = f(x_{i}, y_{i})$$

$$K_{2} = f(x_{i} + \frac{h}{2}, y_{i} + \frac{h}{2}K_{1})$$

$$K_{3} = f(x_{i} + \frac{h}{2}, y_{i} + \frac{h}{2}K_{2})$$

$$K_{4} = f(x_{i} + h, y_{i} + hK_{3})$$

Note that this method samples the midpoint of the interval twice and five calculations are required to step to the next point where the whole process is repeated. Accuracy can also be improved by taking smaller steps. In fact, it is possible to vary the step size h based on the behavior of the solution to maintain the error of the approximation below some established limit. Such variable step techniques as well as convergence and error analysis are thoroughly discussed in the references.⁹

The algorithm used for the fixed step 4th order Runge-Kutta method is as follows.

1. Calculate the slope values at the starting point (K_1) .



Figure 2.2.2. Runge-Kutta Sampling Method

2. Use the estimated slope to calculate the solution's value at one half the interval.

3. Use the estimated value to find the slope at one half the interval (K_{γ}) .

4. Use this slope to again calculate the solution at one half the interval.

5. Use the estimated value to find the slope at one half the interval (K_{3}) .

6. Use this slope to calculate the solution value at the end of the interval.

7. Use the estimated value to find the slope at the end of the interval (K_4) .

8. Calculate the solution's value at the end of the interval using the weighted average of the slope values K_1 to K_4 .

9. Use the final point as the new initial point and return to step 1.

2.2.2 Predictor-Corrector Methods

The one step methods descussed above only require one point to calculate the next point after sampling the flow field in the interval. This necessarily requires a great number of calculations for each point (five for the fourth order method above). There is

a class of numerical procedures called linear multistep methods which use "back values" $y_n, y_{n+1}, \ldots, y_{n+k-1}$ to determine y_{n+k} . These methods, one of which is the Predictor-Corrector, use the past history, or trends, of the numerical solution at equally spaced points $x_n, x_{n+1}, \ldots, x_{n+k-1}$ to estimate the solution at $x = x_{n+k}$. The general form for a multistep method is ¹⁰

$$y_{n+k} = -\sum_{j=1}^{k} a_{j} y_{n+j} + h \sum_{j=1}^{k} \beta_{j} f(x_{n+j}, y_{n+j})$$

where again y' = f(x,y). It is called a linear k - step method because it is linear in y_{n+j} and $f(x_{n+j}, y_{n+j})$ and it requires k back values to calculate y_{n+k} . Normally we demand that $a_k = 1$ and that $|a_0| + |\beta_0| > 1$. If $\beta_k = 0$ then the method is explicit. If $\beta_k \neq 0$ then the value of y_{n+k} is needed to evaluate the right side of the equation to solve for y_{n+k} and the method is implicit. The greatest advantage of this type of method is that we can save the past evaluations of $f(x_{n+j}, y_{n+j})$ and then only need to make several evaluations of f(x,y) to obtain y_{n+k} . This reduces the calculations required below that of comparable Runge-Kutta methods speeding calculation times. These methods are not self starting because they require a certain number of back values before they can proceed. A one step method is generally employed to start a multistep method.

In practice, the implicit and explicit methods described above are used in pairs. The explicit method is used to predict the solution's value at a point and this value is then used in the implicit method to correct the initial solution value. This is the origin of the name Predictor-Corrector. The most popular methods are Adams methods. These are quadrature methods based on aproximations to the integral of the form ¹¹

$$\int_{x_{n+k-1}}^{x_{n+k}} f(x) dx \simeq h[A_0 f(x_n) + A_1 f(x_{n+1}) + ... + A_k f(x_{n+k})]$$

Graphically the method is demonstrated in Figure 2.2.3.



Figure 2.2.3. Quadrature Methods

An explicit Adams-Bashforth method looks like

$$y_{n+k} - y_{n+k-1} = h[A_0f_n + A_1f_{n+1} + ... + A_{k-1}f_{n+k-1}]$$

and an implicit Adams-Moulton method has the form

$$\mathbf{y}_{\mathbf{n+k}} \cdot \mathbf{y}_{\mathbf{n+k-1}} = \mathbf{h}[\mathbf{A}_0\mathbf{f}_{\mathbf{n}} + \mathbf{A}_1\mathbf{f}_{\mathbf{n+1}} + \ldots + \mathbf{A}_k\mathbf{f}_{\mathbf{n+k}}]$$

where $f_m = f(x_m, y_m) = y'_m$. It turns out that the error of a k step explicit method is of the same order as a k-1 step implicit method. If the error is of the same order it reduces the number of iterations needed for the corrector to produce an accurate value limiting the number of calculations. For that reason the Predictor-Corrector pairs usually differ by one step and the corrector is normally applied once, although it can be iterated several times.

Using the fourth order Runge-Kutta method described earlier to start the multistep method it seems logical to maintain the same level of accuracy with a fourth order Predictor-Corrector method. Using interpolatory numerical integration techniques the A_j s for different order methods can be specified and standard values are given in the references. Identifying \overline{y} as the predicted solution value to be used in the implicit corrector we can combine the three step Adams-Bashforth predictor

$$\tilde{y}_{n+3} = y_{n+2} + \frac{h}{12} [23f_{n+2} - 16f_{n+1} + 5f_n]$$

with the two step Adams-Moulton corrector

$$y_{n+3} = y_{n+2} + \frac{h}{12} [5f(x_{n+3}, \bar{y}_{n+3}) + 8f_{n+2} - f_{n+1}]$$

to obtain a fourth order method requiring three back points and only two evaluations. Note that in comparison the same order Runge-Kutta method requires five calculations to obtain the same point. This indicates that the Predictor-Corrector method should be significantly faster. This method can also be used in variable step techniques and the resulting error monitored.¹² Variable step techniques are not really necessary, however, if the solutions to the differential equation are generally well behaved.

2.2.3 Extension to Higher Order Differential Equations

Up to this point the methods discussed only addressed first order differential equations. The equations of motion we are concerned with are second order differential equations. To apply the preceding methods to higher order equations we first convert the nth order equation into an equivalent system of n first order equations. Thus $u_1(x) = y(x), u_2(x) = y'(x), \ldots, u_n(x) = y^{n-1}(x)$. Then using vector notation we set

$$\mathbf{u} = \begin{vmatrix} u_0(\mathbf{x}) \\ u_1(\mathbf{x}) \\ \vdots \\ \vdots \\ u_n(\mathbf{x}) \end{vmatrix} \qquad \mathbf{F}(\mathbf{x}, \mathbf{u}(\mathbf{x})) = \begin{vmatrix} u_1(\mathbf{x}) \\ u_2(\mathbf{x}) \\ \vdots \\ f(u_1(\mathbf{x}), u_2(\mathbf{x}), \dots, u_n(\mathbf{x})) \end{vmatrix}$$

This gives an equivalent first order system of equations in vector form where

$$\mathbf{u'}(\mathbf{x}) = \mathbf{F}(\mathbf{x}, \mathbf{u}(\mathbf{x}))$$

and $\mathbf{u}(\mathbf{x}_0) = \mathbf{u}_0$ are the initial conditions.¹³ Now we just apply the numerical methods to the vector equation and calculate vector quantities. As an example, Euler's method becomes

$$\mathbf{u}_{i+1} = \mathbf{u}_i + \mathbf{h}\mathbf{F}(\mathbf{x}_i, \mathbf{u}_i)$$

and one step methods take the form

$$\mathbf{u}_{i+1} = \mathbf{u}_i + \mathbf{h}\Phi(\mathbf{x}_i, \mathbf{u}_i; \mathbf{h})$$

This automatically produces the value of the function and any derivative up to the order of the original equation at any given point. In the physical systems considered previously this vector technique gives us the value of the angular displacement and angular velocity automatically at each point.

The algorithm for the fourth order Predictor-Corrector method is as follows.

- 1. Calculate the first three back points with a one step method.
- 2. Calculate the initial functional values at each of the three back points (f_1, f_2, f_3) .
- 3. Apply the predictor and estimate \bar{y}_{n+3} .

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- 4. Calculate the function's value f_{n+3} at the estimated point \overline{y}_{n+3} .
- 5. Apply the corrector to obtain a more accurate y_{n+3} .

7. Return to step 3 (functional values are stored in memory and moved up for each pass).

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3. EXPERIMENTAL APPARATUS AND DATA ACQUISITON

3.1 Experimental Setup

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Both the physical pendulum and rotating disk use the modified TRS-80 Color Computer system from Radio Shack (Appendix A). For the junior's experiment a Zenith Z-140 PC with 8087 math coprocesser was also used. The heart of this experimental apparatus is the hardware used to measure the angular velocity of either system. This setup can actually measure the angular velocity of any physical configuration you wish to attach to the slotted disk (Figure 3.1). The motion is recorded through the use of a ten centimeter diameter slotted aluminum disk mounted on a ball bearing hub. There are ninety slots equally spaced around the circumference of the disk. Straddling the slotted area of the disk are two photogates which are capable of signalling as each slot passes. The light beam is broken as the solid portion of the disk between the slots passes when the disk rotates. Since we know the angular position of each notch the angular velocity of the disk is easily calcualated by counting the number of notches that pass in one tenth of a second.

In order to convert the signal from the photogates into a usable (countable) signal for the computer, a hardware circuit is used to convert the signal and provide the input to the cartridge slot of the TRS-80 (Figure 3.2). This circuit actually counts edges and not notches. Thus each photogate will register two counts (two edges) for every notch. Considering the redundant photogates there are actually four counts per notch. This duplicity must be taken into account when calculating the velocity.

Attached to the slotted disk is another thirty centimeter diameter aluminum disk. For the terminal velocity experiment all that is required is the addition of two adjustable plates for air resistance. Two rectangular plates measuring 21 centimeters by 17 centimeters were mounted 22 centimeters from the center axis for this purpose. To construct a physical pendulum all that is needed is a weight to unbalance the disk.





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Figure 3.2. Counting Circuit

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3.2 Software

the slotted disk as a foundation.

The hardware described above provides a physical system and a means of measurement but the photogate signals must be converted into meaningful data and analyzed by programmed routines. There are several sets of programs listed in Appendix B. Two different programing languages were used. 6809 Assembler was used in the procedures for taking the data and plotting as well as the screen driver routines. These routines can then be linked to the interactive Pascal main program by using DEFT Pascal Workbench. ¹⁴ Both of the freshman experiments use this language and the TRS-80 system exclusively. For the junior level experiment only the data acquisition and conversion uses the TRS-80 and DEFT Pascal. The data must then be input into the Zenith Z-140 PC where the analysis routine used is written in Turbo Pascal. ¹⁵

All of the routines use the same technique to record the data. The signal from the photogates automatically increments a 6809 register by one for each pulse. Every tenth of a second the contents of the register is recorded in a vector of data points and zeroed to receive the next set of signals from the photogates. This data vector is then used by each routine. Only the Jpendata routine actually converts the counts directly into angular velocities for input into the Zenith microcomputer.

The structure of both of the routines for the rotating disk (Airwheel) and the physical pendulum (Freshpen) are essentially the same. Initially the student chooses to take data or run a simulation of the motion. If he chooses to take data the subroutine instructs the student how to simultaneously release the system (pendulum or disk) and trigger the counting routine. The data can then be plotted for viewing. After viewing the data the student may continue or terminate the program. Continuing, the program returns to the starting point where the data can be taken again, if necessary, or analyzed with the help of the simulation. Once in the simulation subroutine the physical parameters of the system are entered and the treatment of the air resistance selected. One can choose to neglect air resistance or include it linearly or quadratically in the differential equations. The step size in time for use in Heun's method must be selected next. Heun's method is used to calculate the simulated motion which is plotted and compared to the actual data points. The previous simulation calculated is also plotted so that trends can be indentified. The program then allows changes in the step size, treatment of the air resistance and the initial conditions, in that order. If no changes are desired the student may elect to terminate the program or return to the beginning to repeat the simulation or take new data.

The Physpend program on the Zenith PC is a little more powerful and sophisticated than the above two routines in keeping with the Zenith's capabilities. When the program is initiated there are five options available to the student. First, selecting Takedata permits entering the data points provided by the Jpendata program. After the data is entered it may be plotted and also shifted if necessary. The routine then loops back to the beginning where the student can select the simulation option. Here, as above, the type of configuration is selected, the physical parameters of the system entered, and the time step specified. Now, however, due to the greater computing power of the Zenith, the fourth order Predictor-Corrector method is used to provide a more accurate approximate solution. The simulation may then be plotted. If a simulation has already been done then a second simulation can be calculated and plotted. If data has been taken and simulations completed the data can be compared graphically with each simulation and each simulation compared to the other. A printed version of the plot can be obtained using the print screen key command. Examples of such output are in Appendix C. The Smallangle option uses the small angle

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approximation and stores the resulting calculated motion as a first simulation so that the accuracy of this approximation can be investigated. Finally, with the Compare option the computer will calculate either the moment of inertia, coefficient of friction or the coefficient of air resistance for the physical pendulum. This routine uses an iterative technique and calculates the simulated motion and compares it with the data file point by point. If the value is outside the tolerance set by the student, it will abort the calculation, increment the variable and recalculate the motion until all data points are within the tolerance or until an upper limit, also set by the student, is reached. Here the accuracy of the numerical method is very important. This was the primary reason for selecting a fourth order Predictor-Corrector method. The final value for the selected variable is output and the procedure returns to the options menu at the beginning of the program. At any time when returned to this menu the program can be terminated by selecting the Quit option. The flow charts and program listings in Appendix B provide further details. ANTICAL PARTICIPAL PROPERTY PARTICIPAL PARTI

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4. DISCUSSION

4.1 Goals and System Selection

Several goals were established in designing the experiments which incorporate the preceding theory and equipment. First and foremost, the experiments need to teach a meaningful concept in physics. Secondly, with the current power and availability of microcomputers the student should be taught to appreciate the value of such systems in the laboratory, whether in taking or analyzing data. Finally, the student should be introduced to methods which are available for problems without analytical solutions. These three experiments accomplish all of these goals. 0000 000

The selection of the physical system investigated is of obvious importance in attaining all of the above goals. The choice must lend itself to computer data acquisition and analysis, as well as the application of a numerical method, while involving more than trivial physics. Obviously there are numerous possibilities. The area of mechanics was selected due to the sparsity of existing experiments on mechanical systems. Also, as equations of motion are in differential form, these systems lend themselves to numerical analysis. In choosing the specific experiment an endeavor was made to find systems which perhaps have been addressed in courses yet are seldom seen in demonstrations or laboratories.

Every student learns about terminal velocity in his introductory physics course. Perhaps he may even solve a representative problem concerning a falling sky diver, but sky diving is difficult to demonstrate in the laboratory. The rotating disk with air resistant fins is a compact system which easily demonstrates this concept. It also reinforces the concepts of rotational motion and the moment of inertia of a rigid body. Measuring the angular velocity of such a system by hand would be unreasonably difficult, so the ease of recording this motion with the slotted disk and TRS - 80 provides a good demonstration of a microcomputer's power and usefulness. Finally, the equations of motion for this system are not analytically solvable when viscous forces are taken into account. Thus the power and application of a numerical method is easily demonstrated. The rotating disk in a viscous retarding fluid is a suitable choice considering the desired goals.

No one can deny the importance of harmonic motion in modern physics. Often the concept is introduced with the aid of a spring-mass system or simple pendulum. Unfortunately, pendulums in real life are actually physical pendulums and their oscillations are not always small. The physical pendulum and large angle oscillations are often avoided, or treated superficially, due to their more complicated nature and difficult solution. It is very appropriate, however, for our purposes. This system helps present the ideas of harmonic motion and the effects of external forces. Over, under and critical damping are easily ivestigated as well as the real world effects of friction in the bearings of the apparatus. The accuracy and application of the standard small angle approximation can be investigated and the concepts of rotational motion and the moment of inertia reinforced. The computer's ability to easily record this motion again demonstrates its value in the laboratory. Numerical methods are definitely applicable to this system because, even neglecting damping forces, an analytical solution to the equations of motion is not possible without the small angle approximation. Thus the power and application of a numerical method is easily shown. In view of the desired goals the physical pendulum is also a suitable, and possibly more flexible system to investigate.

4.2 Experimental Design

Using the above goals and physical systems three experiments were developed. Two of these are intended for college freshmen and are done exclusively with the TRS -80 computer. The third experiment is intended for college juniors in physics and thus requires greater knowledge and initiative. It also requires a Zenith Z-140 PC computer

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or comparable IBM compatible system. The instructions for all three experiments reflect the different levels of expertise in their presentation and detail (Appendix D).

The structure of both of the freshman experiments are similar. First, the laboratory setup and general concepts are introduced. Because freshmen are not as familiar with the theory involved the second section reviews the necessary physics and the equations of motion for each system. The instructions for the execution of the experiment are then given, including specific questions that must be answered. The moment of inertia is calculated for each system using standard shapes and the parallel axis theorem. The initial parameters of the setup and initial conditions are measured and recorded. To make the operation of the computer more transparent the terminal velocity experiment requires the student to calculate a few of the data points by hand using the improved Euler's method. This is a good exercise to help the student recognize the power of the computer and understand how the numerical method is applied. Next the actual motion of the disk or pendulum is recorded. The student then uses the computer and the programed numerical method to create a plot of the expected theoretical motion. He then compares the theoretical and actual motion in order to draw conclusions about the effects of viscous forces and the values of certain constants. The configuration of the system can then be changed, the new motion recorded, compared to theory, and similar conclusions can be drawn. Finally, the accuracy of the numerical method and its dependence on the step size is investigated pointing out the possible limitations and concerns of numerical methods.

The experiment intended for juniors is concerned with the physical pendulum only. It is much less structured than the two freshman experiments. The instructions only cover the necessary information to operate the programs on both of the computers. Some areas of interest are suggested, however the scope and depth of the investigation is left up to the student's own initiative. The student can easily investigate a large number of things because of the greater versatility and power of the Zenith computer. Areas include, but are not limited to, small and large angle oscillations, the small angle approximation, the coefficient of rolling friction in the ball bearings, all categories of viscous damping, the accuracy of the calculated moment of inertia compared to the computer's value obtained through curve comparison, and so forth. The accuracy of the numerical method with varying time step size can also be investigated in a similar manner to the freshman experiments. The lack of structure and dependence on student initiative is designed to help develop the student's natural curiosity, good experimental methods and techniques.

In the fall of 1987 the two freshman experiments were given to selected college physics majors as part of their normal junior laboratory course. The juniors were instructed to rigorously tax the software and experimental setup as a means of trouble shooting and debugging. As a result of their thorough investigation minor changes in software were affected, however the entire system as a whole ran smoothly. More importantly, the objectives set for these experiments seemed to be genuinely met. Most students indicated that the exercises were valuable in conveying the concepts of terminal velocity and harmonic motion. They also felt the experiments reinforced the usefulness of the computer in the laboratory and demonstrated an application of a pertinent numerical method. The junior's experiment was not tested in this manner, but when the freshman experiments were given to the juniors they were not provided the instructions in Appendix D. Instead their instructions were less structured, much like those intended for the juniors. The performance of the juniors on these experiments indicates that the design and structure of the junior's experiment should also successfully meet the stated goals.

4.3 Limitations and Possible Improvements

As is normally the case, these experiments have some limitations and are subject to improvements. While large angle oscillations can be accommodated for the pendulum, excessively large angles (greater than 120 degrees) will cause plots to go off the screen for displacement graphs. Likewise, if the angular velocity is large the resulting graphs will also go off the screen. This can be handled by properly selecting the system, or by changing the plotting scale in the program if necessary. Thus, the setup will accomodate any configuration of pendulum and disk, subject to some common sense.

There are also several areas where errors can be introduced. First, because the notched disk has a fixed number of notches, the values recorded for the angular velocity form a discrete set. If the actual value for the angular velocity is between two of these values it will be rounded down to the lower value. Accuracy is less important for the freshman experiments as comparisons are graphical and the resolution is less necessary. For the junior's experiment the accuracy of the data is much more important since numerical calculations are conducted with the actual values for the angular velocity. A suggested improvement would be to increase the number of notches on the disk. Doubling the number of notches would cut the inaccuracy in taking the data in half. The angular velocity values would still form a discrete set, but there would be twice the number of values.

Another source of inaccuracy and a potential problem is the initiation of the counting routine and the simultaneous release of either the disk or pendulum. Since all of the simulations assume that the initial angular velocity is zero, any motion before the computer begins to take data will make it impossible to match the data curve. For the two freshman experiments there is no recourse but to retake the data. The program for the Zenith PC does have a routine that will shift the data to correct for initiation
problems. Remedies for this difficulty take two forms. First, it should be possible to utilize some sort of electronically controlled mechanism to release the pendulum or disk at the same time the counting routine is initiated from the keyboard. This would reduce the error significantly. Another option would be to use the data itself to provide an initial value for the angular velocity. This would only work if the system was already moving when the computer began to take data. If it was not in motion the resulting accuracy would be no better than if the system had been released by hand.

Finally, it seems to be counter productive to take data with one microcomputer and then input numerical values by hand into another. The Zenith PC is capable of accepting input through its RS 232 serial port. Although the TRS - 80 uses an 8 bit processor as opposed to the Zenith's 16 bit processor it would be possible for the TRS -80 to transmit its data to the Zenith. This was explored, however modifications to the peripheral TRS - 80 where the data was taken seemed to preclude any transmission back out of the system. It should also be possible to take data directly with the Zenith through the RS 232 serial port or an expansion slot. This was not explored as thoroughly because of the existing data taking capabilities of the TRS - 80. Certainly this is the way to proceed in the future considering the limited speed and memory of the TRS - 80 compared to the Zenith PC.

5. CONCLUSIONS

With the institutional desire to provide a complete and practical education it has become important to expose students to the power and versatility of microcomputers in the laboratory. This is becoming increasingly important as these systems are more readily available in universities and industry. The incorporation of the physical pendulum, rotating disk and a numerical method for solving differential equations into the laboratory using a microcomputer helps accomplish these goals. The computer is used as an educational tool to teach the applicable physics of each system. Using the same computer to collect and analyze the data demonstrates its power and versatility. Finally, the use of a numerical technique demonstrates a powerful and useful method for solving analytically difficult problems.

There are other possible structures for the experiments presented which could accomplish the same results. The limited exposure to current students seems to indicate, however, that the proposed experiments will be successful in fulfilling the purpose for which they were designed. As needs change or capabilities in the laboratory increase the systems and software are easily modified to accommodate different physical configurations or changed emphasis for each experiment. A great number of possibilities exist for similar exercises and their development should be looked into in the interest of keeping education in step with technology and its practical application.

APPENDIX A: The Modified TRS-80

The physics department at Rensselaer Polytechnic Institute has been investigating the use of computers in the laboratory for educational purposes for several years. The original concept was to have a central unit running the main software routines and a number of peripheral terminals. This structure permits small groups of students in the freshman laboratory to have simultaneous access to a computer. The initial system implemented was made up of TRS-80 Color Computers. In order to establish the desired network (Figure A.1) some simple hardware modifications were made and software was developed to link the network together.

The hardware modification primarily consisted of "piggy backing" an AM 2732 chip at the U13 location on the circuit board (Figure A.2). This creates a greater memory storage area for down loaded programs. The serial port can be used to transmit the programs to the peripheral stations, however our systems were modified to transmit through the cassette port. This allows the connection of the serial printer to the main unit without disturbing the system. The cartridge port on the central unit is used for the standard peripherals such as disk drives.

In order to send programs to the substations a down loading routine was developed. The resident BASIC language was abandoned in favor of DEFT Pascal Workbench. This language package allows programing in either Pascal or 6809 Assembler language. ¹⁴ It can compile either language into a standard object code. Programs and subroutines or procedures can then be linked together and a final program generated in binary machine language. This binary code is then run using the execute command on the TRS-80. This package allows the different parts of a program to be written in the most convenient language and then incorporated into the main program. The entire procedure is executed through the use of a short BASIC program. The following pages list the BASIC language program used to initiate the down loading



Figure A.1. TRS-80 Network Setup

procedure and the main routine and subroutines written in 6809 Assembler. The resulting program will transmit any binary program from the central unit down to the work stations. Since theoretically it is possible to transmit in either direction some subroutines have been included for the reverse procedure, although they are not used in the down loading program (Dump).

When down loading a program it is possible to leave the resident BASIC in the peripheral computer intact. The following down loading routine overwrites the resident programing (it actually makes it unavailable for use) in order to allow for more efficient screen usage, better graphics and more available program memory. As a result, driving routines for the screen must be sent with the down loaded program or else the monitor will not function as desired. These driver routines include clearing the screen (cls), graphics (plot) and keyboard input and polling. The 6809 Assembler language listings of the routines follow the down load program listings. In order to insure that DEFT Pascal 1225

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Figure A.2. Color Computer Circuit Layout

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10 REM $2000-2100 DUMP PROGRAM
20 REM $220-7F00 BUFFER
30 REM
40 PCLEAR 1:CLEAR 50,&H1F00:CLS
50 INPUT"DRIVE";D
60 DRIVE D
70 LINE INPUT"FILENAME: ";A$
80 A$=A$+".BIN"
90 LOADM A$,&H2000
95 DRIVE 0
100 LOADM "DUMP.BIN"
110 REM DISK OFF
120 POKE &HFF40,0
130 PRINT"HIT ANY KEY TO TRANSFER"
140 IF INKEY$="" THEN 140
150 PRINT"SENDING ... "
160 EXEC &H2000:GOTO 130
```

DOWNLOAD PROGRAM IN 6809 ASSEMBLER

*DOWNLOAD OF PROGRAM * \$4200-\$6200 * SETUPNET EXT SETWRITE EXT WRITEBLK EXT * MAIN START ORCC #\$50 LBSR SETUPNET LBSR SETWRITE LDX #\$4200 LDY #\$6200

LBSR WRITEBLK

RTS END

```
* 8/24/86
* SUBROUTINES TO HANDLE NETWORK
 FAST VERSION
PUBLIC SETUPNET
PUBLIC SETWRITE
PUBLIC SETREAD
PUBLIC SETNONE
PUBLIC SETBUSY
PUBLIC CLRBUSY
PUBLIC READBLK
PUBLIC WRITEBLK
PUBLIC NETREAD
PUBLIC NETWRITE
PUBLIC NETBUSY
NETSTART RMB 2
NETLENGTH RMB 2
NETERROR RMB 2
PUBLIC NETSTART
PUBLIC NETLENGTH
PUBLIC NETERROR
*PORT BITS:
* PA7 BUSY IN
                  0 = BUSY
* PA6 DATA IN
* PA5 READ CONTROL
                     0=ACTIVE
* PA4 WRITE CONTROL 0=ACTIVE
* PA3 DATA OUT
* PA2 BUSY OUT
                  0=ACTIVE
 NETREAD:
  NETSTART=START OF BUFFER
  NETLENGTH = LENGTH OF BUFFER
NETREAD LDX NETSTART, PCR GET START ADDRESS
LDY NETLENGTH, PCR AND LENGTH
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TITLE /NETWORK SUBROUTINES/

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DESCRIPTION DESCRIPTION

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BSR READBLK STY NETLENGTH, PCR **CLRA** STD NETERROR, PCR ERROR CODE RTS ***NETWRITE:** NETSTART=START ADDRESS NETLENGTH=NUMBER OF BYTES TO WRITE NETWRITE LDX NETSTART, PCR GET START ADDRESS LDY NETLENGTH, PCR AND LENGTH LBSR WRITEBLK CLRA CLRB STD NETERROR, PCR RTS *SETUPNET SETS UP PIA REGISTERS DISABLES TRANSMIT, RECEIVE **EXIT: A.CC CHANGED** SETUPNET LDA #\$34 STA SFF20 LDA \$FF21 MAKE DDR ANDA #\$F8 STA \$FF21 LDA #\$3E 1100 000I STA \$FF20 LDA #\$04 MAKE DR ORA \$FF21 STA \$FF21 LDA \$FF23 CB2=INPUT ANDA #\$7 CB2 INTERRUPTS OFF **STA \$FF23** RTS SETNONE LDA #\$34 INITIAL BITS STA \$FF20 RTS

* SETWRITE SETS 8T28 TO WRITE EXIT: A,CC CHANGED SETWRITE LDA \$FF20 ORA #\$20 ANDA #\$EF STA \$FF20 RTS * SETREAD SETS 8T28 TO READ **EXIT: A,CC CHANGED** SETREAD LDA \$FF20 ANDA #\$DF ORA #\$10 STA \$FF20 RTS SETBUSY PULLS BUSY LINE LOW **EXIT: A,CC CHANGED** SETBUSY LDA \$FF20 ANDA #\$FB STA \$FF20 RTS **CLRBUSY RELEASES BUSY LINE** EXIT: A,CC CHANGED **CLRBUSY LDA \$FF20** ORA #\$04 STA \$FF20 RTS

* FUNCTION NETBUSY : BOOLEAN;

NETBUSY CLR 4,S RETURN VALUE=FALSE CLR 5.S TST \$FF21 CHECK BIT 7 BMI NB1 1=NOT BUSY INC 5.S 0 = BUSYNB1 RTS READBLK **READS DATA FROM NETWORK: MUST BE IN READ MODE:** ENTRY: X=BUFFER START ADDRESS Y = BUFFER LENGTHEXIT: A.CC CHANGED X = ADRESS OF LAST BYTE + 1Y=# OF BYTES ACTUALLY READ Z=1 & B=0: NO ERROR Z=0 ERROR: CODE IN B; **\$FF BUFFER OVERRUN READBLK PSHS U,Y,CC SAVE REGISTERS** BSR SETREAD **ORCC #\$50 NO INTERRUPTS** LDU #\$FF20 U=PORT ADDRESS ***WAIT FOR VALID START OF TRANSMISSION** SYNCS LDY #6 SYNC BSR BYTE GET A BYTE CMPA #\$16 SYNC? BNE SYNCS LEAY -1,Y BNE SYNC SYNC1 BSR BYTE WAIT FOR START FLAG CMPA **#\$16 BEQ SYNC1** CMPA #2 BNE SYNCS *READ LENGTH **BSR BYTE GET HIGH BYTE** PSHS D SAVE D BSR BYTE GET LOW BYTE **STA 1,S PUT ON STACK** PULS Y GET LENGTH CMPY 1,S TOO BIG? BHI ERR STY 1,S SAVE ACTUAL LENGTH

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DATA BSR BYTE GET DATA BYTE
STA .X+ STORE IT
LEAY -1.Y DONE?
BNE DATA
EXIT LBSR SETNONE DRIVERS OFF
PULS CC,Y,U
TSTB SET Z FOR ERROR FLAG
RTS BYE
ERR LDB #$FF FLAG ERROR
LDY #0 NO BYTES READ
BRA EXIT
* BYTE READS A BYTE
  ENTRY: U=$FF20
  EXIT: A=NEW BYTE
      B=0
       U = $FF20
       X,Y: UNCHANGED
BYTE LDD #$0940 A = BIT COUNT B = BIT MASK FOR PORT
PSHS A
WAIT BITB ,U WAIT FOR START BIT
BEQ WAIT
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NOP CENTERING DELAY
NOP
BYTEL LDB, U GET BIT
LSLB SHIFT INTO A
LSLB
ROLA
TFR B,B DELAY SOME MORE
NOP
NOP
DEC ,S ANY MORE BITS?
BNE BYTEL
PULS B.PC
 WRITEBLK
  SENDS BLOCK OF DATA
* FORMAT:
  VALUE COUNT EXPLANATION
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* \$16 10 SYNC BYTES

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\$02 1 START INDICATION HIGH BYTE OF LENGTH \$HH 1 \$LL LOW BYTE 1 **\$XX \$HHLL 'LENGTH' DATA BYTES** ENTRY: X=START ADDRESS OF BLOCK **Y=LENGTH OF BLOCK** EXIT: X = END ADDRESS + 1**D.CC CHANGED** Y,U UNCHANGED WRITEBLK PSHS Y,CC SAVE ADDRESS LBSR SETWRITE ORCC #\$50 LDY #10 SEND 10 SYNC BYTES WB1 LDA #\$16 \$16=SYNC BYTE BSR OUT LDA #70 DELAY ONE BYTE TIME WBD DECA BNE WBD LEAY -1,Y **BNE WB1** LDA #02 START SEQUENCE BSR OUT LDA 1,S HIGH ORDER LENGTH BSR OUT LDA 2,S AND LOW ORDER BSR OUT LDY 1.S WBL LDA ,X + GET BYTE BSR OUT LEAY -1, Y SEE IF DONE BNE WBL LBSR SETNONE PULS CC,Y,PC **OUT SENDS ONE BYTE TO NETWORK** ENTRY: A=BYTE EXIT: A,B=0**CC CHANGED** OUT LDB #10 START BIT + 8 DATA + 1 STOP PSHS B LDB #\$08

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ORB \$FF20 PA3(DATA BIT) = 1; BRA OUT3 OUT1 ASLA NEXT BIT INTO CARRY BCC OUT2 IF A ZERO,BRANCH ORB #\$8 ELSE SET TO 1 BRA OUT3 OUT2 ANDB #\$F7 SET TO ZERO BRA OUT3 PRESERVE TIMING OUT3 STB \$FF20 SEND THE BIT NOP DELAY SOME NOP NOP DEC ,S DONE? BNE OUT1 PULS B,PC BYE

END

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```
GSTART EQU 0 START SCREEN
GEND EQU 2 END SCREEN
GY EQU 4
GX EQU 5
GFLAG EQU 6
*PUBLIC ROUTINES
PUBLIC CLS PASCAL CALL
PUBLIC CLRTOP PASCAL CALL
PUBLIC CURSOR PASCAL CALL
PUBLIC GSELECT PASCAL
PUBLIC GSETUP PASCAL CALL
PUBLIC GSHOW PASCAL/ASM
PUBLIC PLOT PASCAL CALL
PUBLIC SETT ASM CALL
PUBLIC PUTC CALLED BY PATCHED PASIO
PUBLIC GETCURSOR PASCAL CALL
PUBLIC INVERSETEXT PASCAL CALL
PUBLIC VPRINT PASCAL CALL
PUBLIC GETKEY
PUBLIC INKEY
*EXTERNAL REFERENCES
CSET EXT
* GSELECT
  SETS GLOBAL POINTER TO GRAPHICS CONTROL BLOCK
  CALL: GSELECT(BLKADD:INTEGER)
GSELECT LDX 4.S GET ADDRESS
STX $88
RTS
 GSETUP(BLKADD,STARTADD,ENDADD:INTEGER)
* BLKADD=ADDRESS OF CONTROL BLOCK
* STARTADD=ADDRESS OF SCREEN START
  ENDADD=ADDRESS OF SCREEN END
       IF ZERO, DEFAULTS TO 6143+STARTADD
* STACK FRAME:
BLKADD EQU 8
STARTADD EQU 6
```

DRIVER ROUTINES FOR THE MODIFIED TRS-80

ENDADD EQU 4

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LCCCCC

```
GSETUP LDY BLKADD,S
LDD STARTADD,S
STD GSTART, Y SAVE START ADDRESS
LDD ENDADD,S
BNE GSETUP1
LDD #6143
ADDD STARTADD,S
GSETUP1 STD GEND, Y SAVE END ADDRESS
CLR GX,Y
CLR GY,Y
CLR GFLAG,Y
RTS
* GSHOW DISPLAYS SCREEN
GSHOW LDD [$88] GET START ADDRESS
BSR SETSAM SET ADDRESS
 STA $FFC3 SET SAM MODE CONTROL REGISTER
 STA $FFC5
 LDA #248 SET VDG CONTROL
 STA 65314
 RTS
* SETSAM SETS SAM TO ADDRESS IN A
          (HIGH 7 BITS)
     CLEARS GRAPHICS MODE BITS
SETSAM ANDA #$FE MASK OFF ADDRESS BITS
 LDX #$FFD4
STS1 STA ,--X CLEAR BIT
 CMPX #$FFC0 DONE?
 BEQ STS2
 LSLA GET NEXT BIT
 BCC STS1
 STA 1,X SET SAM BIT IF 1
 BRA STS1
 STS2 RTS
  CLEAR ROUTINES
 * CLEAR TOP
 CLRTOP LDD#256
 BRA CLR
 * CLEAR WHOLE SCREEN
 CLS LDD #6144
```

CLR LDY \$88 LDX GSTART.Y LEAX D,X CLR1 LDD #\$FFFF TST GFLAG,Y **BEQ CLR2 CLRA** CLRB CLR2 STD ,--X CMPX GSTART,Y BHI CLR2 CLR GY.Y CLR GX,Y RTS * PUTC HANDLES CHARACTER OUTPUT PUTC PSHS D,X,Y,U SAVE THINGS LDY \$88 GET POINTER ANDA #\$7F MAKE <128 CMPA #\$20 CONTROL CHAR.? **BLO CONTROLCHAR** LBSR PUTCOK DISPLAY IT LDB GX,Y UPDATE CURSOR; ADDB #5 ADD ONE CHAR. WIDTH BCS PUTC1 CRLF IF PAST END CMPB #251 OR TOO FAR RIGHT **BLS PUTC2** PUTC1 BSR CRLF PULS D,X,Y,U,PC BYE PUTC2 STB GX,Y UPDATE X PULS D,X,Y,U,PC BYE CONTROLCHAR CMPA #\$0D CR? BNE NOCRLF **BSR CRLF DO CRLF** PULS D,X,Y,U,PC NOCRLF CMPA #\$0A LF: BNE NOLF BSR LF DO LF PULS D,Y,X,U,PC

XXXXXXX

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```
NOLF CMPA #8 BACKSPACE?
BNE PUTCEXIT NO, INVALID CHAR
* DO BACKSPACE
LDD GY,Y BACK UP ONE CHAR.
CMPB #5 BEGINNING OF LINE?
BHS BACK1
CMPA #9 TOP OF SCREEN?
BLO PUTCEXIT
SUBA #9 NO, BACK UP ONE LINE
CLRB TO COLUMN 251
BACK1 SUBB #5 BACK UP ONE WIDTH
STD GY,Y
LDA #$20 PRINT SPACE
BSR PUTCOK
PUTCEXIT PULS D,X,Y,U,PC BYE
CRLF CLR GX, Y X = 0 DOES CR
LF LDA GY,Y Y+9 DOES LF
ADDA #9
CMPA #191-9 PAST END?
BHI SCROLL IF YES, SCROLL IT
STA GY.Y
RTS
* SCROLL
SCROLL PSHS D.X.Y.U SAVE THINGS
LDX GSTART, YSTART
LEAU 32*9,X ONE LINE DOWN
LDY GEND, Y END ADDRESS
PSHS Y
TFR X.Y
* PARTIALLY UNFOLLED LOOP
* MOVES ONE SCAN LINE (32 BYTES)
* AT A TIME
SCROLLOOP PULU D,X GET 4 BYTES
STD ,Y + + STORE THEM
STX , Y + +
PULU D.X ETC
STD ,Y++
STX ,Y++
PULU D.X
```

STD ,Y++ STX ,Y++ PULU D,X STD ,Y++ STX ,Y++ PULU D,X STD ,Y++ STX ,Y++

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PULU D,X STD ,Y + +STX ,Y + +PULU D,X STD ,Y++STX,Y++PULU D,X STD ,Y++STX,Y + +CMPU ,S SEE IF DONE **BLO SCROLLOOP** LDD #\$FFFF CLEAR BOTTOM LINE SCRL1 STD ,Y++STD ,Y++STD, Y + +STD ,Y + +CMPY ,S SEE IF DONE **BLO SCRL1** LEAS 2,S CLEAR STACK PULS D, Y, X, U, PC BYE PUTCOK DRAWS CHARACTER ENTRY: Y = ADDRESS OF DESCRIPTOR A=CHARACTER STACK USAGE: **3,S BYTE COUNT** 1-2,S STORAGE **0.S SHIFT VALUE** PUTCOK SUBA #\$20 OFFSET FOR NON-PRINTING CHARACTERS LDB #\$8 BYTES PER CHAR PSHS B LOOP COUNTER MUL INDEX TO CHARACTER LEAU CSET, PCR BASE OF CHARACTERS LEAU D.U ADDRESS OF CHAR LBSR SETT GET PIXEL ADDRESS, BIT LSLB ADJUST BIT SO MUL DOES SHIFT PSHS B,X SAVE SHIFT FACTOR, RESERVE 2 BYTES CMPX BEND, Y PAST END? **BHS PUTCO3** PUTCO2 LDA ,U+ GET CHAR BYTE LDB ,S GET SHIFT FACTOR BEQ PUTCNS DON'T SHIFT IF ALREADY OK MUL SHIFT CHAR BYTE PUTCNS STD 1,S STORE SHIFTED VALUE LDA #\$F8 GET MASK BYTE LDB ,S GET SHIFT FACTOR **BEQ PUTCNS1 MUL SHIFT MASK**

×71 × 1 × 1 × 1 × 1 × 1 × 1 × 1

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PUTCNS1 TST GFLAG,Y **BEQ NORMCHAR** COMA FLIP MASK COMB ANDA ,X RESET BITS OF BACKGROUND ANDB 1.X **BRA BITCHAR** NORMCHAR ORA ,X SET BITS OF BACKGROUND ORB 1,X BITCHAR EORA 1,S FLIP BITS CHAR EORB 2.S STD ,X STORE IT ON SCREEN LEAX \$20,X NEXT ROW CMPX BEND, Y OFF SCREEN? **BHS PUTCO3** DEC 3,S ANY MORE BYTES? **BNE PUTCO2** PUTCO3 PULS D,X,PC PLOT SETS/RESETS PIXEL CALL: PLOT(X,Y,FLAG :INTEGER) PASSED: **B.S: X LOW** A,S: X HIGH 9,6: Y LOW 8,S: Y HIGH 7.S: MODE 0 = DOT ON6,S: HIGH MODE (UNUSED) 4-5,S: LINK ADDRESS 2-3,S: RETURN ADDRESS 0-1,S: SAVED GX,GY CC CHANGED PLOT LDY \$88 GET POINTER

LDD GY,Y PSHS D LDA 9,S A=Y COORD LDB \$B,S B=X COORD STD BY,Y BSR SETT CMPX GEND,Y BHI DOTEND TST 7,S BEQ DOTCLEAR DOTSET ORB ,X BRA DOTPUT

DOTCLEAR COMB ANDB ,X DOTPUT STB ,X DOTEND PULS D STD GY,Y RTS * CURSOR MOVES CURSOR TO X,Y CALL: CURSOR(X,Y:INTEGER) STACK FRAME: 7.S: X LOW 6,S: X HIGH 5,S: Y LOW 4,S: Y HIGH 2-3,S: LINK ADDRESS 0-1,S: RETURN ADDRESS **CURSOR LDY \$88** LDB 7,S LDA 5,S STD GY,Y RTS SETT SETS UP ENTRY: GY = YGX = XY=POINTER TO CONTROL BLOCK EXIT: BYTE ADDRESS IN X BIT # IN A BIT IN B SETT LDD GY,Y LSRA RORB **LSRA** RORB LSRA RORB ADDD GSTART,Y TFR D,X LDA GX.Y ANDA #7 PSHS Y LEAY SHFTB, PCR

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`.#a^_#<u>a</u>*_#a*_#a*_#a*_#a*_#a*

.ta*.fa*.da*.d

```
LDB A.Y
PULS Y.PC
SHFTB FDB $8040
FDB $2010
FDB $0804
FDB $0201
 GETCURSOR RETURNS POSITION TO PASCAL
 CALL: GETCURSOR(VAR X,Y:INTEGER)
 STACK FRAME:
         6-7,S: ADDRESS OF X
         4-5,S: ADDRESS OF Y
         2-3,S: LINK ADDRESS
         0-1,S: RETURN ADDRESS
GETCURSOR LDY $88
CLRA
LDB GY,Y
STD [4.S]
LDB GX.Y
STD [6,S]
RTS
 INVERSETEXT: SETS INVERSE FLAG TO VALUE FROM PASCAL
*
 CALL: INVERSETEXT(FLAG:BOOLEAN)
 STACK FRAME:
         5,S: BOOLEAN FLAG
         4.S: UNUSED
        2-3,S: LINK
        0-1,S: RETURN ADDRESS
INVERSETEXT LDA 5,S
LDY $88
STA GFLAG.Y
RTS
 VPRINT
  PRINTS VERTICAL STRING
  CALL: VPRINT(S:STRING)
  STACK FRAME:
          5-N,S: STRING
           4,S: LENGTH
```

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2-3,S: LINK 0-1,S: RETURN ADDRESS **VPRINT LDY \$68** LDB GX.Y CMPB #251 CHECK X COORD **BLS VP1** LDB #251 VP1 STB GX.Y LDB 4,S GET LENGTH LEAX 5.S GET POINTER TO STRING PSHS U SAVE DYNAMIC LINK (FOR PASCAL) PSHS B,X SAVE STRING INFO VPL LDA GY,Y MOVE PRINT LOCATION CMPA #183 AT BOTTOM OF SCREEN? **BLS VPL1** LDA #183 VPL1 ADDA #9 DOWN 9 COLUMNS STA GY,Y STORE IT PULS B,X GET INFO TSTB SEE IF DONE **BEQ VPEND** DECB LDA ,X+ GET CHAR PSHS B,X SAVE INFO LBSR PUTCOK **BRA VPL** VPEND PULS U,PC DFTPOLLKEY EXT PASCAL CALL **FUNCTION INKEY:CHAR** * WAITS FOR A KEY TO BE PRESSED **RETURNS ASCII CODE OF KEY** * STACK: **5.S: RETURN FUNCTION BYTE** 2-3,S: LINK 0-1,S: RETURN ADDRESS INKEY LBSR DFTPOLLKEY **BEQ INKEY** STA 5,S RTS * PASCAL CALL * FUNCTION GETKEY:CHAR;

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* SCANS KEYBOARD ONCE * RETURNS ZERO IF NO KEY * GETKEY LBSR DFTPOLLKEY STA 5,S RTS * END

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CHARACTER SET FOR DRIVER SUBROUTINES

PUBLIC CSET CSET FCB \$00,\$00,\$00,\$00,\$00,\$00,\$00 FCB \$20,\$20,\$20,\$20,\$20,\$00,\$20,\$00 FCB \$50,\$50,\$50,\$00,\$00,\$00,\$00 FCB \$50,\$50,\$F8,\$50,\$F8,\$50,\$50,\$00 FCB \$20.\$38.\$60.\$30.\$28.\$70.\$20.\$00 FCB \$68,\$68,\$10,\$20,\$20,\$58,\$58,\$00 * FCB \$20,\$50,\$50,\$20,\$68,\$50,\$28,\$00 FCB \$20,\$70,\$A8,\$20,\$20,\$A8,\$70,\$20 FCB \$30,\$20,\$40,\$00,\$00,\$00,\$00 FCB \$10.\$20.\$40.\$40.\$40.\$20.\$10.\$00 FCB \$20,\$10,\$08,\$08,\$08,\$10,\$20,\$00 FCB \$00,\$48,\$30,\$78,\$30,\$48,\$00,\$00 FCB \$00.\$20.\$20.\$F8.\$20.\$20.\$00.\$00 FCB \$00,\$00,\$00,\$30,\$30,\$20,\$40 FCB \$00.\$00.\$00.\$78.\$00.\$00.\$00 FCB \$00,\$00,\$00,\$00,\$30,\$30,\$00 FCB \$08,\$08,\$10,\$20,\$20,\$40,\$40,\$00 FCB \$30,\$48,\$48,\$48,\$48,\$48,\$48,\$30,\$00 FCB \$20,\$60,\$20,\$20,\$20,\$20,\$70,\$00 FCB \$30,\$48,\$08,\$10,\$20,\$40,\$78,\$00 FCB \$30,\$48,\$08,\$30,\$08,\$48,\$30,\$00 FCB \$08,\$18,\$28,\$48,\$78,\$08,\$08,\$00 FCB \$78,\$40,\$70,\$08,\$08,\$48,\$30,\$00 FCB \$10,\$20,\$40,\$70,\$48,\$48,\$30,\$00 FCB \$78,\$08,\$08,\$10,\$20,\$40,\$40,\$00 FCB \$30,\$48,\$48,\$30,\$48,\$48,\$30,\$00 FCB \$30,\$48,\$48,\$38,\$08,\$10,\$20,\$00 FCB \$00,\$30,\$00,\$00,\$30,\$00,\$00 FCB \$00,\$30,\$00,\$00,\$30,\$10,\$20,\$00 FCB \$08,\$10,\$20,\$40,\$20,\$10,\$08,\$00 FCB \$00,\$00,\$78,\$00,\$78,\$00,\$00,\$00 FCB \$40,\$20,\$10,\$08,\$10,\$20,\$40,\$00 FCB \$30,\$48,\$08,\$10,\$20,\$00,\$20,\$00 * FCB \$30,\$48,\$58,\$58,\$40,\$48,\$30,\$00 FCB \$F8,\$40,\$20,\$10,\$20,\$40,\$F8,\$00 FCB \$30,\$48,\$48,\$78,\$48,\$48,\$48,\$00 FCB \$70,\$48,\$48,\$70,\$48,\$48,\$70,\$00 FCB \$30,\$48,\$40,\$40,\$40,\$48,\$30,\$00 FCB \$70,\$48,\$48,\$48,\$48,\$48,\$48,\$70,\$00 FCB \$78,\$40,\$40,\$70,\$40,\$40,\$78,\$00 FCB \$78,\$40,\$40,\$70,\$40,\$40,\$40,\$00 FCB \$30,\$48,\$40,\$58,\$48,\$48,\$38,\$00 FCB \$48,\$48,\$48,\$78,\$48,\$48,\$48,\$00 FCB \$70,\$20,\$20,\$20,\$20,\$20,\$70,\$00 FCB \$08,\$08,\$08,\$08,\$08,\$48,\$30,\$00 FCB \$48,\$48,\$50,\$60,\$50,\$48,\$48,\$00 FCB \$40,\$40,\$40,\$40,\$40,\$40,\$78,\$00 FCB \$48,\$78,\$78,\$48,\$48,\$48,\$48,\$00

FCB \$48,\$68,\$68,\$58,\$58,\$48,\$48,\$00
FCB \$78,\$48,\$48,\$48,\$48,\$48,\$48,\$78,\$00
FCB \$70,\$48,\$48,\$70,\$40,\$40,\$40,\$00
FCB \$30,\$48,\$48,\$48,\$68,\$58,\$38,\$00
FCB \$70,\$48,\$48,\$70,\$50,\$48,\$48,\$00
FCB \$30,\$48,\$40,\$30,\$08,\$48,\$30,\$00
FCB \$70,\$20,\$20,\$20,\$20,\$20,\$20,\$00
FCB \$48,\$48,\$48,\$48,\$48,\$48,\$48,\$48,\$30,\$00
FCB \$48,\$48,\$48,\$48,\$48,\$48,\$30,\$30,\$00
FCB \$48,\$48,\$48,\$48,\$78,\$78,\$48,\$00
FCB \$48,\$48,\$30,\$30,\$30,\$48,\$48,\$00
FCB \$88,\$88,\$50,\$20,\$20,\$20,\$20,\$00
FCB \$78,\$08,\$10,\$20,\$20,\$40,\$78,\$00
FCB \$78,\$60,\$60,\$60,\$60,\$60,\$78,\$00
FCB \$40,\$40,\$20,\$20,\$10,\$08,\$08,\$00
FCB \$78,\$18,\$18,\$18,\$18,\$18,\$78,\$00
FCB \$20,\$70,\$A8,\$20,\$20,\$20,\$20,\$00
FCB \$00,\$10,\$20,\$78,\$20,\$10,\$00,\$00
FCB \$60,\$60,\$20,\$10,\$00,\$00,\$00
FCB \$00,\$00,\$ 38, \$ 08, \$ 38, \$ 48, \$ 38, \$ 00
FCB \$40,\$40,\$70,\$48,\$48,\$48,\$70,\$00
FCB \$00,\$00,\$38,\$40,\$40,\$40,\$38,\$00
FCB \$08,\$08,\$38,\$48,\$48,\$48,\$38,\$00
FCB \$00,\$00,\$30,\$48,\$78,\$40,\$38,\$00
FCB \$10,\$28,\$20,\$70,\$20,\$20,\$20,\$00
FCB \$00,\$00,\$30,\$48,\$48,\$38,\$08,\$30
FCB \$40,\$40,\$70,\$48,\$48,\$48,\$48,\$48,\$00
FCB \$20,\$00,\$60,\$20,\$20,\$20,\$70,\$00
FCB \$10,\$00,\$10,\$10,\$10,\$10,\$50,\$20
FCB \$40,\$40,\$40,\$50,\$60,\$50,\$48,\$00
FCB \$60,\$20,\$20,\$20,\$20,\$20,\$70,\$00
FCB \$00,\$00,\$78,\$78,\$78,\$48,\$48,\$00
FCB \$00,\$00,\$40,\$70,\$48,\$48,\$48,\$00
FCB \$00,\$00,\$30,\$48,\$48,\$48,\$48,\$30,\$00
FCB \$00,\$00,\$70.\$48.\$48,\$70,\$40,\$40
FCB \$00,\$00,\$38,\$48,\$48,\$38,\$08,\$08
FCB \$00,\$00,\$58,\$60,\$40,\$40,\$40,\$00
FCB \$00,\$00,\$38,\$40,\$30,\$08,\$70,\$00
FCB \$20,\$20,\$70,\$20,\$20,\$28,\$10,\$00
FCB \$00,\$00,\$48,\$48,\$48,\$48,\$48,\$38,\$00
FCB \$00,\$00,\$48,\$48,\$48,\$30,\$30,\$00
FCB \$00,\$00,\$48,\$48,\$48,\$78,\$78,\$00
FCB \$00,\$00,\$48,\$48,\$30,\$48,\$48,\$00
FCB \$00,\$00,\$48,\$48,\$48,\$38,\$08,\$30
FCB \$00,\$00,\$ 78, \$ 08, \$ 10, \$ 20,\$78, \$ 00
FCB \$10,\$20,\$20,\$40,\$20,\$20,\$10,\$00
FCB \$20,\$20,\$20,\$20,\$20,\$20,\$20,\$20,\$00
FCB \$40,\$20,\$20,\$10,\$20,\$20,\$40,\$00
FCB \$48,\$B0,\$00,\$00,\$00,\$00,\$00,\$00
FCB \$50,\$A8,\$50,\$A8,\$50,\$A8,\$50,\$A8
END

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## **REQUIRED ADDITIONS TO PASCALIB/EXT FROM DEFT**

TYPE GBLK1 = RECORD STARTADD :INTEGER; ENDADD: INTEGER; GY : CHAR; GX: CHAR; INVERSEFLAG: BOOLEAN; END;

**PROCEDURE GSELECT (VAR BLK: GBLK1);** 

PROCEDURE GSETUP (VAR BLK: GBLK1; STARTADD, ENDADD: INTEGER);

**PROCEDURE GSHOW;** 

**PROCEDURE CLS;** 

**PROCEDURE CLRTOP;** 

**PROCEDURE CURSOR** (X,Y: INTEGER);

**PROCEDURE GETCURSOR (VAR X,Y: INTEGER);** 

**PROCEDURE PLOT (X,Y,MODE: INTEGER);** 

**PROCEDURE INVERSETEXT (FLAG: BOOLEAN);** 

**PROCEDURE VPRINT (S: STRING);** 

**PROCEDURE GETKEY: CHAR;** 

**PROCEDURE INKEY: CHAR;** 

# **APPENDIX B: Operating Programs**

The routines written for these experiments are primarily in Pascal. The programs for the TRS-80 Color Computer were written with DEFT Pascal Workbench and any differences or embellishments to ISO Standard Pascal are in the cited manuals. The Physpend program was written with Turbo Pascal from Borland International and its variations from ISO Standard Pascal are also documented. <sup>17</sup> Commenting on the TRS-80 routines has been minimized due to limited memory, however logic flow charts precede the listings as necessary. Standard conventions on "pretty printing" have been used for readability. The common subroutines were written in 6809 Assembler and commented accordingly.



Figure B.1. Freshpen and Airwheel Main Routine



Figure B.2. Takedata Procedure

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Figure B.3. Freshpen Simulate Procedure

**PROGRAM** Freshpendulum (input, output); LABEL 1; TYPE vector = ARRAY [1..2] OF real; datapoints = ARRAY [1..11] OF vector; point = ARRAY [1..2] OF integer; data = ARRAY [1..64] OF integer; simdata = ARRAY [1..256] OF point; VAR select : char; buffer : data; \*\*\*\*\*\* **PROCEDURE** Setup ; EXTERNAL; **PROCEDURE** Count (address : integer); EXTERNAL; **PROCEDURE** Graph (address : integer); EXTERNAL; \*\*\*\*\*\*\* FUNCTION Yes : Boolean; VAR ch : char; BEGIN readln (ch); IF ch = 'Y' THEN Yes := true ELSE Yes := false END: PROCEDURE Noprime (pendconst : real; VAR upass, uprime : vector): BEGIN

```
uprime[1] := upass[2];
 uprime[2] := - pendconst * sin(upass[1]);
END;
```

{\*

**PROCEDURE** Lprime (pendconst, airlength, airconst : real; VAR upass, uprime : vector);

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```

```
BEGIN
   uprime[1] := upass[2];
   uprime[2] := - pendconst * sin(upass[1]) - airconst *
                   airlength * upass[2];
 END;
                                                                    * * * }
PROCEDURE Sqprime (pendconst, airlength, airconst : real;
              VAR upass, uprime : vector);
 BEGIN
   uprime[1] := upass[2];
   IF upass[2] < 0
    THEN
      uprime[2] := - pendconst * sin(upass[1]) +
                airconst * sqr(airlength * upass[2])
    ELSE
      uprime[2] := - pendconst * sin(upass[1])
               - airconst * sqr(airlength * upass[2])
 END;
PROCEDURE Takedata (VAR buffer : data);
  VAR
   i : integer;
   inchar : char;
  BEGIN
   cls;
   writeln ('Hit any key to start timing.');
   inchar := Inkey;
   Cirtop;
   writeln ('Collecting . . .');
   Count (Buffer[1]);
   writeln ('Do you wish to see the data points? (Y/N)');
   IF Yes THEN
     BEGIN
       writeln ('Hit any key when you are finished with');
      writeln ('the data.');
      writeln;
       writeln ('Are you ready to plot? (Y/N)');
      IF Yes THEN
        BEGIN
          cls;
          Graph(Buffer[1]);
          inchar := Inkey;
        END;
     END; { then }
  END;
```

```
63
```

# **PROCEDURE** Heun (pendconst, airlength, airconst deltat:real; VAR thetadot : datapoints; VAR i : integer; acase : char): VAR k1, k2, utemp : vector; j : integer; BEGIN CASE acase OF 'N' : BEGIN utemp[1] := thetadot[i, 1];utemp[2] := thetadot[i,2];Noprime (pendconst, utemp, k1); FOR j := 1 TO 2 DO utemp[j] := thetadot[i,j] + deltat \* k1[j];Noprime (pendconst, utemp, k2); FOR j := 1 TO 2 DO thetadot[i+1,j] := thetadot[i,j] + deltat \*(k1[i] + k2[i])/2;END; { case of N } 'L' : BEGIN utemp[1] := thetadot[i,1];utemp[2] := thetadot[i,2];Lprime (pendconst,airlength,airconst,utemp,k1); FOR j := 1 TO 2 DO utemp[j] := thetadot[i,j] + deltat \* k1[j]; Lprime (pendconst, airlength, airconst, utemp, k2); FOR j := 1 TO 2 DO thetadot[i+1,j] := thetadot[i,j] + deltat \* (k1[j] + k2[j])/2;END; { case of L } 'Q' : BEGIN utemp[1] := thetadot[i,1]; utemp[2] := thetadot[i,2];Sqprime (pendconst,airlength,airconst,utemp,k1); FOR j := 1 TO 2 DO utemp[j] := thetadot[i,j] + deltat \* k1[j]; Sqprime (pendconst,airlength,airconst,utemp,k2); FOR j := 1 TO 2 DO thetadot[i+1,j] := thetadot[i,j] + deltat \*(k1[j] + k2[j])/2;**END** { case of Q } END; { case } END; { Heun }

**PROCEDURE** Simulate (buffer : data);

LABEL 1,2,3,4,5,6,7;

#### CONST

g = 9.81;conv = 0.34906585;

### VAR

acase, curve, inchar : char; mass, cmdistance, imoment theta1, airlength airconst, pendconst, deltat : real; i, j, subint, int : integer; thetadot : datapoints; theta, omega : simdata;

### BEGIN

# cls;

int := 0; 7: writeln ('Enter the mass of the pendulum.'); readln (mass); writeln ('Enter the distance to the center of mass.'); readln (cmdistance); writeln ('Enter the moment of inertia.'); readln (imoment); pendconst := mass \* g \* cmdistance / imoment; cls; writeln ('In conducting the simulation you may'); writeln ('neglect air resistance, include it with'); writeln ('a term linear in velocity or a term'); writeln ('quadratic in velocity. Enter: '); N - Neglect air resistance'); writeln (' writeln (' L - Include it linearly'); writeln (' Q - Include quadratic term'); readln (acase): IF NOT (acase IN ['N','L','Q']) THEN BEGIN writeln ('Not a proper response.'); GOTO 1; END; 2: cls: writeln ('Enter the initial angle (rad).'); readln (theta1); IF acase IN ['L','Q'] THEN BEGIN writeln ('Enter the distance from the pivot to '); writeln ('the center of the plates.'); readln (airlength); writeln ('Enter the coefficient of air');

writeln ('resistance.');

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```
readln (airconst);
    END:
5: cls;
  writeln ('Do you wish to plot the displacement or ');
  writeln ('velocity? Enter:');
               D - Displacement');
  writeln ('
               V - Velocity');
  writeln ('
  readln (curve);
  IF NOT (curve IN [D','V']) THEN
    BEGIN
      writeln ('Not a proper response.');
     GOTO 5;
    END:
6: writeln('Enter the step size, delta t, to be used in');
  writeln ('the simulation. (Multiples of .025 or ');
  writeln ('divisors of .025 down to .0025 only for ');
  writeln ('graphing purposes.)');
  readln (deltat);
  writeln("The simulation will plot the data, the last');
  writeln ('simulation and one point at a time for the');
  writeln ('new simulation. Hit S if you wish to stop');
  writeln ('the plot. After you are fininshed viewing');
  writeln ('the plot hit any key to continue the ');
   writeln ('program.');
3: writeln
  writeln('Are you ready to plot the simulation? (Y/N)');
  IF Yes THEN
    BEGIN
      cls;
      Graph (Buffer[1]);
      FOR k := 1 TO int DO
       BEGIN
         IF curve = 'V' THEN
           Plot (omega[i,1],omega[i,2],0)
         ELSE
           Plot (theta[i,1],theta[i,2],0);
       END:
      IF deltat < .025 THEN
       BEGIN
         subint := round(.025/deltat);
         int := 255;
       END
      ELSE
       BEGIN
         subint := 1;
         int := round(6.375/deltat);
       END:
      theta[1,1] := 0;
      omega[1,1] := 0;
      theta[1,2] := 190 - round(theta1*100);
      omega[1,2] := 190;
      CASE curve OF
```
'D': Plot(theta[1,1],theta[1,2],0); 'V': Plot(omega[1,1],omega[1,2],0) END;  $\{ case \}$ thetadot[1,1] := theta1;thetadot[1,2] := 0.0;FOR i := 1 TO int DO BEGIN FOR i = 1 TO subint DO Heun (pendconst, airlength, airconst, deltat, thetadot, j, acase); theta[i+1,2] := 190 - round(abs(thetadot))[subint + 1, 1] \* 100); omega[i+1,2] := 190 - round(abs(thetadot[subint + 1, 2])/conv \*3);IF subint = 1 THEN BEGIN theta[i+1,1] := round(i\*deltat/.025);omega[i+1,1] := theta[i+1,1];END ELSE BEGIN theta[i+1,1] := i;omega[i+1,1] := i;END: thetadot[1,1] := thetadot[subint+1,1];thetadot[1,2] := thetadot[subint+1,2];CASE curve OF 'D': Plot(theta[i+1,1],theta[i+1,2],0);'V': Plot(omega[i+1,1],omega[i+1,2],0)END; { case } Plot(omega[i+1,1],5,0); { mark progress } IF Getkey = 'S' THEN GOTO 4; END;  $\{ for \}$ END { then } ELSE GOTO 3; 4: inchar :- Inkey; cls: writeln ('Do you wish to change the step size? (Y/N)'); IF Yes THEN GOTO 6; writeln ('Do you wish to change the initial air'); writeln ('resistance constants? (Y/N)'); IF Yes THEN GOTO 2: writeln ('Do you wish to change the way that air'); writeln ('resistance is considered? (Y/N)'); IF Yes THEN GOTO 1: writeln ('Do you wish to change the mass or moment'); writeln ('of inertia? (Y/N)'); IF Yes

THEN GOTO 7; END; { Simulate }

#### \*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*

BEGIN { Freshpendulum }
Setup;
cls;

writeln ('Welcome to the pendulum datataking and '); writeln ('comparison program. This program will '); writeln ('allow you to determine the best way to'); writeln('incorporate air resistance in the equations'); writeln ('of motion and an approximate value for the'); writeln ('coefficient of air resistance. You may '); writeln ('also investigate the accuracy of the '); writeln ('numerical method as you change the size '); writeln ('of the step in time.'); writeln: 1: writeln ('Do you wish to take data or run a '); writeln ('simulation? Enter:'); writeln (' T - Takedata'); writeln (' S - Simulate'); readln (select); CASE select OF 'T': Takedata (buffer): 'S': Simulate (buffer) ELSE BEGIN writeln ('Not a proper response.'); **GOTO** 1: END END: { case } cls: writeln ('Do you wish to continue the program? (Y/N)'); **IF Yes THEN** GOTO 1; END. { Freshpendulum }



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Figure B.4. Airwheel Simulate Procedure

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**PROGRAM** Airwheel (input,output);

```
LABEL 1;
 TYPE
  vector = ARRAY[1..2] OF real;
  calcvals = ARRAY[1..11] OF vector;
  point = ARRAY[1..2] OF integer;
  data = ARRAY[1..64] OF integer;
  simdata = ARRAY[1..256] OF point;
 VAR
  select : char;
  omega : simdata;
  buffer : data;
              *******
                                                        ***}
PROCEDURE Setup; EXTERNAL;
PROCEDURE Count (address : integer); EXTERNAL;
PROCEDURE Graph (address : integer); EXTERNAL;
{********
                                                ***********
FUNCTION Yes : boolean;
 VAR
  ch : char;
 BEGIN
  readln (ch);
  IF ch = 'Y' THEN Yes := true ELSE Yes := false
 END;
             *******
                                               ***********
PROCEDURE Noprime (wheelconst : real; VAR upass, uprime :
             vector):
 BEGIN
  uprime[1] := upass[2];
   uprime[2] := wheelconst;
 END;
PROCEDURE Lprime (wheelconst, airlength, airconst, imoment:
```

real; VAR upass, uprime : vector);

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```
BEGIN
   uprime[1] := upass[2];
  uprime[2] := wheelconst - airconst * airlength/imoment
             * upass[2];
 END;
                       *****
PROCEDURE Sqprime(wheelconst, airlength, airconst, imoment:
             real; VAR upass, uprime : vector);
 BEGIN
   uprime[1] := upass[2];
   uprime[2] := wheelconst - airconst/imoment *
                sqr(airlength * upass[2]);
 END;
                           ******
PROCEDURE Takedata (VAR buffer : data);
 VAR
   i : integer;
   inchar : char;
 BEGIN
   cls;
   writeln ('Hit any key to start timing');
   inchar := Inkey;
   clrtop;
   writeln (Collecting . . .');
   Count (Buffer[1]);
   writeln ('Do you wish to see the data points? (Y/N)');
   IF Yes THEN
    BEGIN
      writeln ('Hit any key when you are finished with');
      writeln ('the data.');
      writeln;
      writeln ('Are you ready to plot? (Y/N)');
      IF Yes THEN
       BEGIN
         cls:
         Graph (Buffer[1]);
         inchar := Inkey:
       END;
    END; { then }
  END; { takedata }
                   ********
```

PROCEDURE Heun (wheelconst, airlength, airconst, imoment, deltat : real; VAR thetadot : calcvals;

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```
VAR i : integer, acase : char);
VAR
 k1, k2, utemp : vector;
 j : integer;
BEGIN
 CASE acase OF
   'N' :
    BEGIN
      utemp[1] := thetadot[i,1];
      utemp[2] := thetadot[i,2];
      Noprime (wheelconst, utemp, k1);
      FOR j := 1 TO 2 DO
        utemp[j] := thetadot[i,j] + deltat * k1[j];
      Noprime (wheelconst, utemp, k2);
      FOR j := 1 TO 2 DO
        thetadot[i+1,j] := thetadot[i,j] + deltat *
                       (k1[i] + k2[i])/2;
    END; { case of N }
   'L' :
     BEGIN
      utemp[1] := thetadot[i,1];
      utemp[2] := thetadot[i,2];
      Lprime (wheelconst, airlength, airconst, imoment,
             utemp, k1);
      FOR j := 1 TO 2 DO
        utemp[j] := thetadot[i,j] + deltat * k1[j];
      Lprime (wheelconst, airlength, airconst, imoment,
             utemp, k2);
      FOR j := 1 TO 2 DO
        thetadot[i+1,j] := thetadot[i,j] + deltat *
                       (k1[j] + k2[j])/2;
     END; { case of L }
    'Q' :
     BEGIN
       utemp[1] := thetadot[i,1];
       utemp[2] := thetadot[i,2];
       Sqprime (wheelconst, airlength, airconst, imoment,
             utemp, k1);
       FOR j := 1 TO 2 DO
        utemp[j] := thetadot[i,j] + deltat * k1[j];
       Sqrime (wheelconst, airlength, airconst, imoment.
             utemp, k2;
       FOR j := 1 TO 2 DO
        thetadot[i+1,j] := thetadot[i,j] + deltat *
                       (k1[j] + k2[j])/2;
     END; { case of Q }
  END; { case }
END; { Heun }
```

LABEL 1,2,3,4,5,6;

# CONST

g = 9.81;conv = 0.34906585;

## VAR

```
inchar, acase : char;
mass, aradius, imoment, airlength, airconst, wheelconst,
deltat : real;
i, j, subin, int : integer;
thetadot : calcvals;
omega : simdata;
```

# BEGIN

cls: int := 0;writeln ('The simulation solves the equation of '); writeln ('motion for the accelerated wheel using'); writeln ('Heuns method.'); writeln: 6: writeln ('Enter the moment of inertia for the wheel.'); readln (imoment); writeln ('Enter the radius of the disk to the cord.'); readln (aradius); writeln ('Enter the mass of the accelerating weight.'); readln (mass): wheelconst := mass\*g\*aradius/(imoment+mass\*sqr(aradius)); cls: writeln ('In conducting the simulation you may '); writeln ('neglect air resistance, include it with a'); writeln('term linear in velocity or a term quadratic'); writeln ('in velocity. Enter:'); N - Neglect air resistance'); 1: writeln (' writeln (' L - Include it Linearly'); writeln (' **Q** - Include the Quadratic term'); readly (acase); IF NOT (acase IN ['N','L','Q']) THEN BEGIN writeln ('Not a proper response.'); GOTO 1; END; 2: cls; IF acase IN ['L','Q'] THEN BEGIN writeln ('Enter the radius to the center of the'); writeln ('plates.'); readln (airlength); writeln ('Enter the coefficient of air');

```
writeln ('resistance.');
     readln (airconst);
   END;
5: writeln('Enter the step size, delta t, to be used in');
  writeln ('the simulation. (Multiples of .025 or ');
  writeln ('divisors of .025 down to .0025 only for ');
  writeln ('graphing purposes.)');
  readln (deltat);
  writeln ('The simulaton will plot the data, the last');
  writeln('simulation and one point at at time for the');
  writeln ('new simulation. Hit S if you wisht to ');
  writeln ('stop the plot. After you are finished ');
  writeln ('viewing the plot hit any key to continue');
  writeln ('the program.');
3: writeln:
  writeln('Are you ready to plot the simulation? (Y/N)');
  IF Yes THEN
    BEGIN
     cls;
     Graph (Buffer[1]);
     FOR i := 1 TO int DO
       Plot(omega[i,1],omega[i,2],0);
     IF deltat < .025 THEN
       BEGIN
         subint := Round(.025/deltat);
         int := 255;
       END
     ELSE
       BEGIN
         subint := 1;
         int := Round(6.375/deltat);
       END;
      omega[1,1] := 0;
      omega[1,2] := 190;
      Plot(0,190,0);
      thetadot[1,1] := 0.0;
      thetadot[1,2] := 0.0;
      FOR i := 1 TO int DO
       BEGIN
         FOR j := 1 TO subint DO
          Heun (wheelconst, airlength, airconst, imoment,
               deltat, thetadot, j, acase);
         omega[i+1,2] := 190 - Round(abs
                    (thetadot[subint + 1,2])/conv * 4);
         IF subint = 1
           THEN omega[i+1,1] := Round(i*deltat/.025)
           ELSE omega[i+1,1] := i;
         thetadot[1,1] := thetadot[subint+1,1];
         thetadot[1,2] := thetadot[subint+1,2];
         Plot(omega[i+1,1],omega[i+1,2],0);
         Plot(omega[i+1,1],5,0); { mark progress }
         IF Getkey = 'S' THEN GOTO 4;
```

END;  $\{ for \}$ END { then } ELSE GOTO 3; 4: inchar := Inkey; cls: writeln ('Do you wish to change the initial step '); writeln ('size? (Y/N)'); IF Yes THEN GOTO 5; writeln ('Do you wish to change the initial air'); writeln ('resistance constants? (Y/N)'); IF Yes THEN GOTO 2; writeln ('Do you wish to change the way air '); writeln ('resistance is considered? (Y/N)'); IF Yes THEN GOTO 1; writeln ('Do you wish to change the values for the'); writeln ('moment of inertia or the accelerating '); writeln ('weight? (Y/N)'); IF Yes THEN GOTO 6; END; { simulate }

```
BEGIN { Airwheel }
```

```
Setup;
 cls;
  writeln ('Welcome to the rotational motion lab.');
  writeln ('This program will allow you to measure');
  writeln ('the rotational velocity of a wheel with a');
  writeln ('given moment of inertia when under a');
  writeln ('constant torque (provided by gravity). The');
  writeln ('effects of air resistance can also be ');
  writeln ('measured. After data is taken a simultion');
  writeln ('may be run to investigate the moment of');
  writeln ('inertia of the system, and the dependence');
  writeln ('of the torque due to air resistance on the');
  writeln ('velocity. You will also be able to ');
  writeln ('investigate the accuracy of the numerical');
  writeln ('method as you change the size of the step');
  writeln ('in time.');
  writeln:
1: writeln ('Do you wish to take data or run the');
  writeln ('simulation? Enter:');
```

```
writeln (' T - Takedata');
writeln (' S - Simulate');
readln (select);
CASE select OF
```

'T' : Takedata (buffer);

'S' : Simulate (buffer) ELSE BEGIN writeln ('Not a proper response.'); GOTO 1; END END; { case } cls; writeln ('Do you wish to continue the program? (Y/N)'); IF Yes THEN GOTO 1; END. { Airwheel } 

```
PROGRAM Jpendata (input, output);
  vector = ARRAY[1..2 \text{ OF real};
  datapoints = ARRAY[1..65] OF vector;
  data = ARRAY[1..64] OF integer;
  buffer : data;
  omega : datapoints;
  inchar : char:
            ******
PROCEDURE Setup; EXTERNAL;
PROCEDURE Count (address : integer); EXTERNAL;
        PROCEDURE Takedata (VAR buffer : data);
```

```
cls;
 writeln ('Hit any key to start timing.');
 inchar := Inkey:
 clrtop;
 writeln ('Collecting . . .');
 Count(Buffer[1]);
END; { Takedata }
```

```
* * }
```

PROCEDURE Convertdata (buffer: data;VAR omega: datapoints);

```
CONST
 conv = 0.34906585;
```

# VAR

LABEL 1;

TYPE

VAR

{\*\*\*\*

BEGIN

i : integer;

# BEGIN

```
cls:
writeln ('Converting data . . .');
omega[1,1] := 0.0;
omega[1,2] := 0.0;
FOR i := 1 TO 64 DO
 BEGIN
   omega[i+1,1] := 0.1 * i;
```

```
omega[i+2,2] := buffer[i]/4 * conv
    END; \{ for \}
 END; { Convertdata }
PROCEDURE Outputdata (omega : datapoints);
 LABEL 1,2;
 VAR
   outfile : text;
   inchar, select : char;
   start, stop, i : integer;
 BEGIN
   cls;
 1: writeln ('What output device do you want to use? ');
   writeln ('Enter:');
   writeln ('
                P - Printer');
   writeln ('
                S - Screen');
   readln (select);
   IF NOT (select IN ['P','S']) THEN
     BEGIN
      writeln ('Not a proper response.');
      GOTO 1;
     END;
   CASE select OF
     'P':
      BEGIN
        rewrite (outfile,':-2');
                                           Omega');
        writeln (outfile,'
                          Time
        FOR i := 1 TO 65 DO
          writeln (outfile,omega[i,1]:12,'
                 omega[i,2]:12);
        close (outfile);
       END; \{ case of P \}
     'S':
       BEGIN
        writeln ('The data will be written one screen');
        writeln ('at a time. When you are finished ');
        writeln('with a screen hit any key to view the');
         writeln ('next screen of data points.');
         writeln:
         writeln ('Hit any key to start the output.');
        inchar := Inkey;
         start := 1;
         stop := 16;
      2: cls;
         writeln ('
                     Time
                                      Omega');
         FOR i := start TO stop DO
          writeln (omega[i,1]:12,'
                                      ',omega[i,2]:12);
```

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```
inchar := Inkey;
      start := stop + 1;
      stop := stop + 16;
      IF stop \leq = 64 THEN GOTO 2;
    END { case of S }
writeln ('This routine collects the data from the');
writeln ('pendulum, converts and outputs it for');
writeln ('manual input into the Zenith program.');
writeln ('Hit any key to proceed.');
Convertdata (buffer, omega);
writeln ('Do you wish to take another set of data?');
IF inchar = 'Y' THEN GOTO 1;
```

END; { case } END; { Outputdata }

BEGIN { Jpendata }

inchar := Inkey; 1: Takedata (buffer);

> writeln ((Y/N)); inchar := Inkey;

END. { Jpendata }

Outputdata (omega);

cls; Setup;

writeln:

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Figure B.6. Physpend Simulate Procedure

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Figure B.8. Procedure Runge4 and PredictCorrect



Figure B.9. **Physpend Compare Procedure** 

{ This is the physical pendulum data collection and simulation routine for the laboratory. The Takedata procedure requires input by hand as it is very dependent on the physical set up and hardware used in the lab. This program is designed to simulate the motion of a physical pendulum treating it as a simple pendulum or physical pendulum under no constraints, air resistance, friction or a combination. Comparison of the motion using the small angle approximation is also possible. An additional feature allows the calculation of the moment of inertia, friction coefficient or air resistance coefficient for an arbitrary physical pendulum by fitting a simulated curve for the system to the actual data using an iterative process. The code that follows was developed on an AT® PC6300 using Turbo Pascal. The laboratory system uses a TRS-80 Color Computer and DEFT Pascal Workbench to take data and a Zenith PC and Turbo Pacal to run this software. This code was written by Mark R. Stevens. }

PROGRAM PhysPendulum (input, output, simdata, pendata);

LABEL 1, 2, 3;

#### TYPE

vector = ARRAY [1..2] OF real; pastpoints = ARRAY [1..4] OF vector; datafile = FILE OF vector;

## VAR

response, simselect : char; datataken, sim1complete, sim2complete : boolean; simdata1, simdata2, pendata : datafile;

FUNCTION Yes : boolean;

{ This function is used whenever a response is requested of a yes or no nature. It is used extensively throughout the program and procedures. }

## VAR

ch : char;

# BEGIN readln (ch); IF ch IN ['y','Y'] THEN Yes := true ELSE Yes := false END;

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# **PROCEDURE** Takedata (VAR datataken : boolean);

{ This procedure may be modified for direct input. Currently it is set up to accept inputed datafrom the keyboard. 64 data points, specifically. }

LABEL 1;

# VAR

omega : vector; select : char; i : integer;

## BEGIN

writeln ('Do you wish to use the data currently on '); writeln ('the disk? (Y/N)'); IF Yes THEN GOTO 1; rewrite (pendata); omega[1] := ord('V');{ Label data as a velocity plot. } omega[2] := 0.0;write (pendata, omega); writeln ('Currently the pendulum data must be input '); writeln ('by hand. First input the configuration of'); writeln('the pendulum. Are you expecting to neglect'); writeln('friction, consider air resistance, etc.'); writeln('Enter:'); writeln (' N - No constraints'); A - Air resistance only'): writeln (' writeln (' F - Friction effects only'); writeln (' **B** - Both friction and air resistance'): readln (select); omega[1] := ord(select); writeln ('Enter the pendulum constant (m\*g\*d/I), if'); writeln ('known, otherwise enter zero.'); readln (omega[2]); write (pendata, omega); writeln ('If air resistance is considered, enter the'); writeln ('length to the center of the plates.'); readln (omega[1]); writeln ('Enter the initial angle.'); readln (omega[2]); write (pendata,omega); omega[1] := 0.0; { These two data spots are reserved }  $omega[2] := 0.0; \{ for airconst and frictconst which \}$ write (pendata,omega); { are unknowns for the data } writeln ('Enter the data points one point at a time,'); writeln ('with time first followed by the value for'); writeln ('omega separated by a space. Continue '); writeln ('entering data until all 64 points are '); writeln ('entered. You should also change the sign');

# PROCEDURE Shiftdata (VAR pendata : datafile);

## VAR

temp : vector; tshift : real;

## BEGIN

reset (pendata); clrscr; writeln('Shifting the data is possible in both'); writeln('directions. A shift of more than a few'); writeln('tenths of a second is not recommended. It'); writeln('would be better to take new data. Note:'); writeln('one pixel on the screen is .01 seconds.'); writeln: writeln('Enter the shift for the data(include sign).'); readln (tshift); seek (pendata, 5); WHILE NOT eof(pendata) DO BEGIN read (pendata, temp); temp[1] := temp[1] + tshift;seek (pendata, FilePos(pendata) - 1); write (pendata, temp); END; close (pendata); END; { shiftdata }

## **PROCEDURE** Axis;

## BEGIN

draw (10, 10, 10, 189, 5); draw (10, 110, 620, 110, 5); END; 86

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```
PROCEDURE DataPlot (VAR plotdata : datafile);
{ This procedure takes whatever datafile it is given and
 plots the data with crosses and with labels which are
 included in the first three vector values.}
 LABEL 1;
 VAR
   x1, y1, x2, y2, config : integer;
   buff, temp, temp2 : vector;
   curve : char;
 BEGIN
   clrscr;
   graphmode;
   hires;
   Axis;
   reset (plotdata);
   read (plotdata, temp);
   config := round(temp[1]);
   curve := chr(config);
   read (plotdata, temp, buff,temp2);
   config := round(temp[1]); { Get labeling data }
   writeln('Data Config = ',chr(config),' m^*g^*d/I = ',
          temp[2]:5:3,'Airlength = ',buff[1]:5:3,
          ' Theta(0) = ', buff[2]:5:3);
   WHILE NOT eof(plotdata) DO
     BEGIN
      read (plotdata, buff);
      x2 := round(buff[1] * 100) + 10;
      y2 := 110 - round(buff[2] * 10);
      draw (x2, y2-2, x2, y2+2, 5);
      draw (x2-4, y2, x2+4, y2, 5);
     END; { while }
   close (plotdata);
1 : writeln ('Are you done with the plot? (Y/N)');
   IF Yes
     THEN textmode
     ELSE GOTO 1
  END;
PROCEDURE Plot (VAR plotdata : datafile);
```

{ This procedure takes the datafile it is given and plots it with labels which are included in the first four vector values. }

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LABEL 1;
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# VAR

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```
x1, y1, x2, y2, config, scale : integer;
buff, temp, temp2 : vector;
curve : char;
```

# BEGIN

```
clrscr;
  graphmode;
  hires:
  Axis:
  reset (plotdata);
  read (plotdata, temp);
  config := round(temp[1]);
  curve := chr(config);
  IF curve IN ['v','V'] THEN
   BEGIN
     scale := 10:
     writeln ('Velocity plot');
    END
  ELSE
    BEGIN
     scale := 40;
     writeln ('Displacement');
    END;
  read (plotdata, temp, buff,temp2);
  config := round(temp[1]); { Get labeling data }
  writeln('Config = ',chr(config),' m^*g^*d/I = ',
          temp[2]:5:3,' Airlength = ',buff[1]:5:3,
          ' \text{Theta}(0) = ', \text{buff}[2]:5:3);
  writeln('
                  Frict Coef = ',temp2[1]:5:3,
          'Air Coef = ',temp2[2]:5:3);
  read (plotdata, buff);
  x2 := round(buff[1] * 100) + 10;
  y2 := 110 - round(buff[2] * scale);
   WHILE NOT eof(plotdata) DO
    BEGIN
      x1 := x2;
      y1 := y2;
      read (plotdata, buff);
      x2 := round(buff[1] * 100) + 10;
      y2 := 110 - round(buff[2] * scale);
      draw (x1, y1, x2, y2, 5);
    END; { while }
   close (plotdata);
1 : writeln ('Are you done with the plot? (Y/N)');
   IF Yes
    THEN textmode
    ELSE GOTO 1
 END;
```

## **PROCEDURE** Smallangle (VAR simdata : datafile);

{ This procedure utilizes the small angle approximation to calculate the motion of a physical pendulum under no constraints. It allows comparison simulations to be calculated to the more exact numerical solution. Such comparisons identify when the small angle approximation is a reasonable assumption and when it is not. }

# CONST

g = 9.81;delta\_t = 0.01;

## VAR

time, imoment, mass, itheta, theta, cmdistance, pconst : real; buffer, temp : vector; i : integer; curve : char;

# BEGIN

writeln; writeln('Enter the pendulum mass in kilograms.'); readln (mass); writeln ('Enter the distance from the pivot to the'); writeln ('center of mass.'); readln (cmdistance); writeln('Enter the moment of inertia for the system.'); readln (imoment); writeln ('Enter the initial angle in radians.'); readln (itheta); pconst := mass \* g \* cmdistance / imoment; rewrite (simdata); writeln('Do you wish to plot displacement or '); writeln ('velocity? Enter:'); writeln (' **D** - Displacement'); writeln (' V - Velocity'); readln (curve); buffer[1] := ord(curve); buffer[2] := 0.0;write (simdata, buffer); buffer[1] := ord('N'); { Label data } buffer[2] := pconst; temp[1] := 0.0;temp[2] := itheta;write (simdata, buffer, temp); temp[2] := 0.0;write (simdata,temp);{ zero values for frictconst and } time := 0.0;{ airconst }

```
buffer[1] := time;
   buffer[2] := itheta;
   write (simdata, buffer);
   FOR i := 1 TO 640 DO
    BEGIN
      time := time + delta t;
      buffer[1] := time;
      IF curve IN ['d','D'] THEN
       buffer[2] := itheta * cos(sqrt(pconst) * time)
      ELSE
       buffer[2] := -itheta * sin(sqrt(pconst) * time)
                   * sqrt(pconst);
      write (simdata, buffer);
    END; \{ for i \}
   close (simdata);
 END; { Smallangle }
                        *******
PROCEDURE Noprime(pendconst: real; VAR upass, uprime:vector);
{ This is the "slope" vector function derived when the
 differential equation for the unconstrained physical
 pendulum is decoupled. }
 BEGIN
   uprime[1] := upass[2];
   uprime[2] := - pendconst * sin(upass[1])
 END:
                   ********
PROCEDURE Airprime (pendconst, fairlength, airconst : real;
                VAR upass, uprime : vector);
{ This is the "slope" vector function derived when the
  differential equation for the physical pendulum including
  air resistance is decoupled. }
  BEGIN
   uprime[1] := upass[2];
   IF upass[2] < 0
     THEN
      uprime[2] := -pendconst * sin(upass[1]) +
                 airconst * sqr(fairlength * upass[2])
     ELSE
      uprime[2] := -pendconst * sin(upass[1])
                - airconst * sqr(fairlength * upass[2])
  END:
```

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```
PROCEDURE Frprime (pendconst, frictconst : real; VAR upass,
               uprime : vector);
{ This is the "slope" vector function derived when the
 differential equation for the physical pendulum including
 friction is decoupled. }
 BEGIN
   uprime[1] := upass[2];
   IF upass[2] < 0
     THEN
      uprime[2]:= -pendconst * sin(upass[1]) + frictconst
     ELSE
      uprime[2]: = -pendconst * sin(upass[1]) - frictconst
 END:
PROCEDURE Bothprime (pendconst, fairlength, frictconst,
               airconst: real;VAR upass,uprime: vector);
{ This is the "slope" vector function derived when the
  differentail equation for the physical pendulum including
  friction and air resistance is decoupled}
  BEGIN
   uprime[1] := upass[2];
   IF upass[2] < 0
     THEN
       uprime[2] := -pendconst * sin(upass[1]) + airconst
               * sqr(fairlength * upass[2]) + frictconst
     ELSE
       uprime[2] := -pendconst * sin(upass[1]) - airconst
               * sqr(fairlength * upass[2]) - frictconst
  END;
PROCEDURE Runge4 (pendconst, airlength, frictconst, airconst,
               delta t: real;select: char;VAR ypast:
               pastpoints; i : integer);
{ This is the fourth order Runge-Kutta method used to start
  the fourth order predictor-corrector method used. It
  returns up to three back values for the function and its
  first derivative given the values from the point before
  in the array ypast. }
  VAR
    ytemp, k1, k2, k3, k4 : vector;
    j : integer;
```

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```
BEGIN
 CASE select OF
   'p','P','n','N' :
    BEGIN
      Noprime (pendconst, ypast[i], k1);
      FOR i := 1 TO 2 DO
        ytemp[j] := ypast[i,j] + delta t * k1[j]/2;
      Noprime (pendconst, ytemp, k2);
      FOR j := 1 TO 2 DO
        ytemp[j] := ypast[i,j] + delta_t * k2[j]/2;
      Noprime (pendconst, ytemp, k3);
      FOR j := 1 TO 2 DO
        ytemp[j] := ypast[i,j] + delta t * k3[j];
      Noprime (pendconst, ytemp, k4);
      FOR j := 1 TO 2 DO
        ypast[i+1,j] := ypast[i,j] + delta_t *(k1[j] +
                       2^{k}[i] + 2^{k}[i] + k_{i}[i]/6;
     END; \{ case of P, N \}
   'a','A' :
     BEGIN
      Airprime (pendconst, airlength, airconst, ypast[i],
               k1);
      FOR i := 1 TO 2 DO
        ytemp[j] := ypast[i,j] + delta_t * k1[j]/2;
      Airprime (pendconst,airlength,airconst,ytemp,k2);
      FOR j := 1 TO 2 DO
        ytemp[j] := ypast[i,j] + delta t * k2[j]/2;
      Airprime (pendconst,airlength,airconst, ytemp,k3);
      FOR j := 1 TO 2 DO
        ytemp[j] := ypast[i,j] + delta t * k3[j];
      Airprime (pendconst,airlength,airconst,ytemp,k4);
      FOR j := 1 TO 2 DO
        ypast[i+1,j] := ypast[i,j] + delta t *(k1[j] + .)
                        2^{k}[j] + 2^{k}[j] + k_{i}[j]/6;
     END; { case of A }
   'f','F' :
     BEGIN
      Frprime (pendconst, frictconst, ypast[i], k1);
      FOR j := 1 TO 2 DO
        ytemp[i] := ypast[i,j] + delta t * k1[j]/2;
      Frprime (pendconst, frictconst, ytemp, k2);
      FOR_j := 1 TO 2 DO
        ytemp[j] := ypast[i,j] + delta t * k2[j]/2;
      Frprime (pendconst, frictconst, ytemp, k3);
      FOR j := 1 TO 2 DO
        ytemp[j] := ypast[i,j] + delta_t * k3[j];
       Frprime (pendconst, frictconst, ytemp, k4);
       FOR j := 1 TO 2 DO
        ypast[i+1,j] := ypast[i,j] + delta_t *(k1[j] +
                        2^{k}[j] + 2^{k}[j] + k4[j])/6;
     END; \{ case of F \}
    "b', "B' :
```

```
BEGIN
       Bothprime (pendconst, airlength, frictconst,
               airconst, ypast[i], k1);
       FOR i := 1 TO 2 DO
         ytemp[j] := ypast[i,j] + delta t * k1[j]/2;
       Bothprime (pendconst, airlength, frictconst,
                airconst, ytemp, k2);
       FOR j := 1 TO 2 DO
         ytemp[j] := ypast[i,j] + delta t * k2[j]/2;
       Bothprime (pendconst, airlength, frictconst,
                airconst. vtemp, k3);
       FOR j := 1 TO 2 DO
         ytemp[j] := ypast[i,j] + delta t * k3[j];
       Bothprime (pendconst, airlength, frictconst,
                airconst, ytemp, k4);
       FOR j := 1 TO 2 DO
         ypast[i+1,j] := ypast[i,j] + delta t *(k1[j] +
                        2^{k}[i] + 2^{k}[i] + k_{i}[i]/6;
      END; { case of B }
   END; { case }
 END; { Runge4 }
PROCEDURE PredictCorrect (pendconst, airlength, frictconst,
                    airconst, delta t: real; select :
                    char; VAR ypast : pastpoints; VAR
                    k1, k2, k3 : vector);
 VAR
   k4, ytemp : vector;
   j : integer;
 BEGIN
   FOR j := 1 TO 2 DO { predictor }
     ytemp[j]:= ypast[3,j] + delta_t *(23*k3[j] - 16*k2[j])
              + 5*k1[j])/12;
   CASE select OF
     'p','P','n','N': Noprime (pendconst, ytemp, k4);
     'a','A' : Airprime (pendconst, airlength, airconst,
                     ytemp, k4);
     'f','F': Frprime (pendconst, frictconst, ytemp, k4);
     'b','B': Bothprime (pendconst,airlength,frictconst,
                      airconst.ytemp.k4);
   END; { case }
   FOR_j := 1 TO 2 DO
                           { corrector - single iteration }
     ypast[4,j]:= ypast[3,j] + delta t *(5*k4[j] + 8*k3[j])
                - k2[j])/12;
   k1 := k2; \{ Move functions up for next pass \} 
   k2 := k3;
   k3 := k4;
   ypast[3] := ypast[4]; { Move to next point }
```

## **END;** { **PredictCorrect** }

PROCEDURE Multistep (pendconst,airlength,theta,frictconst, airconst,delta\_t: real; curve,select: char; VAR simdata : datafile);

{ This is the numerical calculation for the simulation using a fourth order predictor-corrector method constructed from a three stage Adams-Bashforth method and a two stage Adams-Moulton method. The resulting multistage method is not self starting and requires three back points in order to begin predicting and correcting. The three back points are provided by the initial conditions and the fourth order Runge-Kutta method employed above. The error from the Runge-Kutta method is as good as the predictor-corrector method being used so no problems should arise as a result of the generation of the first three points. It is relatively fast (5 seconds for 600 data points) and has fourth order accuracy. }

## VAR

k1, k2, k3, k4, ytemp, buffer : vector; ypast : pastpoints; time : real; i, j, subint, int : integer;

#### BEGIN

```
rewrite (simdata);
IF delta_t < 0.01 THEN
 BEGIN
   subint := ROUND(0.01/delta t);
   int := 640;
 END
ELSE
 BEGIN
   subint := 1;
   int := ROUND(6.4/delta t);
 END;
buffer[1] := ord(curve);
buffer[2] := 0.0;
write (simdata, buffer);
buffer[1] := ord(select); { label data }
buffer[2] := pendconst;
ytemp[1] := airlength;
ytemp[2] := theta:
write (simdata, buffer, ytemp);
ytemp[1] := frictconst;
ytemp[2] := airconst;
```

```
write (simdata, ytemp);
 time := 0.0;
 ypast[1,1] := theta;
 ypast[1,2] := 0.0;
 buffer[1] := time:
 IF curve IN ['d','D']
   THEN buffer[2] := ypast[1,1]
   ELSE buffer[2] := 0.0;
 write (simdata, buffer);
                             ',buffer[2]);}
{ writeln (LST, buffer[1], '
 FOR i := 1 TO 2 DO{ Calculate first three back points.}
   BEGIN
     time := time + delta t;
    Runge4 (pendconst, airlength, frictconst, airconst,
           delta t, select, ypast, i);
    IF delta t \ge 0.01 THEN
      BEGIN
        buffer[1] := time;
        IF cu ve IN ['d'.'D']
          THEN buffer[2] := ypast[i+1,1]
          ELSE buffer[2] := ypast[i+1,2];
        write (simdata, buffer);
      { writeln (LST, buffer[1],'
                                    ',buffer[2]);}
      END; \{ if \}
   END; { for i }
 CASE select OF
   'p','P','n','N' :
     BEGIN
      Noprime(pendconst, ypast[1], k1);{ The initial }
      Noprime(pendconst, ypast[2], k2); { functional }
      Noprime(pendconst,ypast[3],k3);{ values for use }
     END; { case of P }
                                 { in PredictCorrect }
   'a','A' :
     BEGIN
       Airprime (pendconst, airlength, airconst, ypast[1],
               k1);
       Airprime (pendconst, airlength, airconst, ypast[2],
               k2):
       Airprime (pendconst, airlength, airconst, ypast[3],
               k3):
     END; { case of A }
    'f'.'F' :
     BEGIN
       Frprime (pendconst, frictconst, ypast[1], k1);
       Frprime (pendconst, frictconst, ypast[2], k2);
       Frprime (pendconst, frictconst, ypast[3], k3);
     END; { case of F }
    'b','B' :
     BEGIN
       Bothprime (pendconst, airlength, frictconst,
                airconst, ypast[1], k1);
       Bothprime (pendconst, airlength, frictconst,
```

```
airconst, ypast[2], k2);
      Bothprime (pendconst, airlength, frictconst,
               airconst, ypast[3], k3);
    END; \{ case of B \}
   END; { case }
 FOR i := 1 TO int DO
   BEGIN
    FOR j := 1 TO subint DO
      BEGIN
        time := time + delta t;
       PredictCorrect (pendconst, airlength, frictconst,
                     airconst, delta t, select, ypast,
                     k1, k2, k3);
      END; { for j }
    buffer[1] := time;
    IF curve IN ['d','D']
      THEN buffer[2] := ypast[4,1]
      ELSE buffer[2] := ypast[4,2];
     write (simdata, buffer);
   { writeln (LST, buffer[1],'
                                ',buffer[2]);}
   END; \{ for i \}
 close (simdata);
END; { Multistep }
```

PROCEDURE Simulate (VAR simcomplete : boolean; VAR simdata: datafile);

{ This procedure runs the simulation when the user requests the simulation option from the main menu. }

### LABEL 2;

## CONST

g = 9.81;

VAR

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curve, select : char; imoment, mass, airlength, theta, cmdistance, delta\_t : real; pconst, frictconst, airconst : real;

## BEGIN

writeln ('The simulation will proceed based on the'); writeln ('physcical configuration you are using.');

# 2 : writeln;

writeln ('Enter the system configuration:');

- writeln (' P Simple Pendulum');
- writeln (' N No constraints (friction or air)');

- writeln (' A Air resistance only');
- writeln (' F Friction only');

```
B - Both air resistance and friction'):
writeln ('
readln (select);
CASE select OF
 'p','P' :
   BEGIN
     writeln('Enter the length of the pendulum in');
     writeln('meters.');
     readln (cmdistance);
     writeln ('Enter the initial angle in radians.');
     readln (theta);
     writeln ('Enter the step size, delta t, to be ');
     writeln ('used in the simulation.(Multiples of');
     writeln ('.01 or divisors of .01 down to .001');
     writeln ('only for graphing purposes.)');
     readln (delta t);
     writeln ('Do you wish to plot the displacement');
     writeln ('or velocity, Enter;'):
     writeln ('
                   D - Displacement');
     writeln ('
                   V - Velocity'):
     readln (curve):
     pconst := g/cmdistance;
     Multistep (pconst, 0, theta, 0, 0, delta t, curve,
              select, simdata);
   END; { case of P }
  'n','N','a','A','f','F','b','B' :
   BEGIN
     airlength := 0.0;
     airconst := 0.0;
     frictconst := 0.0:
     writeln('Enter the pendulum mass (in kg).');
     readln (mass);
     writeln ('Enter the distance from the pivot to');
     writeln ('the center of mass.');
     readln (cmdistance);
     writeln ('Enter the moment of inertia for the');
     writeln ('pendulum.');
     readln (imoment);
     IF select IN ['a','A'] THEN
       BEGIN
         writeln ('Enter the distance to the center');
         writeln ('of the square plates.');
         readln (airlength);
         writeln ('Enter the coefficient of air');
         writeln ('resistance.');
         readln (airconst);
       END;
     IF select IN ['f','F'] THEN
       BEGIN
         writeln ('Enter the friction coefficient.');
         readln (frictconst);
       END:
     IF select IN ['b','B'] THEN
```

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BEGIN
         writeln ('Enter the distance to the center');
         writeln ('of the square plates.');
         readln (airlength);
         writeln ('Enter the coefficient of air');
         writeln ('resistance.'):
         readln (airconst);
         writeln ('Enter the friction coefficient.');
         readln (frictconst)
       END:
      writeln ('Enter the initial angle in radians.');
      readln (theta);
      pconst := mass * g * cmdistance / imoment;
      writeln ('Enter the step size, delta t, to be');
      writeln ('used in the simulation.Multiples of');
      writeln ('.01 or divisors of .01 down to .001');
      writeln ('for graphing purposes.)');
      readln (delta t);
      writeln ('Do you wish to plot the displacement'):
      writeln ('or velocity. Enter:');
      writeln ('
                    D - Displacement');
      writeln ('
                    V - Velocity');
      readln (curve);
      Multistep (pconst,airlength,theta,frictconst,
               airconst,delta_t,curve,select,simdata)
    END { case of NOT P }
   ELSE
    BEGIN
      writeln ('Not a valid selection.');
      GOTO 2
    END; { else }
 END; { case }
 simcomplete := true;
END; { Simulate }
```

\*\*\*\*\*\*\*\*\*\*\*\*\*\*

**PROCEDURE** Compare (VAR pendata : datafile);

{ This procedure compares the measured data from the lab with the motion calculated by the numerical method. It calculates the moment of inertia, coefficient of air resistance or the coefficient of friction for the pendulum by fitting the simulated curve to the curve of the actual motion. This routine is the slowest because the simulation must be recalculated iteratively as the value of imoment, aircon or frictconst is a variable and must be incremented until a proper fit is obtained. }

LABEL 3, 4, 5, 6;

CONST

g = 9.81;xtolerance = 0.004; delta\_t = 0.01;

## VAR

cselect, calcvar : char; intolerance : boolean; mass, imoment, airlength, theta, cmdistance, pendconst, frictconst, airconst, ytolerance, ilimit,flimit,alimit, iincrement,fincrement,aincrement,istart,fstart, astart, time : real; buffer, k1, k2, k3 : vector; ypast : pastpoints; i : integer;

## BEGIN

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3 : writeln ('In what physical configuration was the '); writeln ('data taken?'); writeln (' N - No constraints'); A - Air resistance only'); writeln (' writeln (' F - Friction effects only'); B - Both friction and air resistance'); writeln (' writeln (' Q - Quit and return to the main menu.'); readin (cselect); IF cselect IN ['n','N','a','A','f','F','b','B'] THEN BEGIN reset (pendata); read (pendata, buffer);{skip velocity plot label} read (pendata, buffer); IF round(buffer[1]) ord(cselect) {see if the } THEN { data was taken in the indicated } BEGIN { configuration. } writeln ('The data was not taken in the "', cselect,'" configuration.'); GOTO 3 END; { then } END { then } ELSE IF cselect IN ['q','Q'] **THEN GOTO 5** ELSE BEGIN writeln ('Response not allowed.'); GOTO 3: END; { else } 6: writeln ('Which constant do you wish to calculate?'); writeln ('Enter:'); writeln (' I - Moment of inertia'); writeln (' F - Coefficient of friction'); writeln (' A - Coefficient of air resistance'); readln (calcvar); IF NOT (calcvar IN ['i','I','f','F','a','A']) THEN

```
BEGIN
   writeln ('Not an allowed response.');
   GOTO 6
 END: { IF NOT }
writeln('The comparison procedure requires certain');
writeln ('incremental values, starting points and');
writeln ('limits. The first value needed is the ');
writeln ('tolerance for the accuracy of the');
writeln('calculated omega, or y coordinate. Enter');
writeln ('the y tolerance (.2 is a good start).');
readln (ytolerance);
writeln ('The next entries deal with the starting');
writeln('value or lower limit, an increment and an');
writeln ('upper limit to the value of the constant');
writeln ('to be calculated.');
CASE calcvar OF
 'a'.'A' :
   BEGIN
     writeln ('Enter the starting value for the');
     writeln ('coefficient of air resistance.');
     readln (astart):
     writeln ('Enter the amount to be incremented');
     writeln ('each pass. WARNING: The smaller');
     writeln ('the increment the longer the');
     writeln ('calculation.');
     readln (aincrement);
     writeln ('Enter the upper limit on the');
     writeln ('coefficient of air');
     writeln ('resistance.'):
     readln (alimit);
   END; { case of A }
  'f'.'F':
   BEGIN
     writeln ('Enter the starting value for the');
     writeln ('coefficient of'):
     writeln ('friction.');
     readln (fstart);
     writeln ('Enter the amount to be incremented');
     writeln ('each pass. WARNING: The smaller');
     writeln ('the increment the longer the');
     writeln ('calculation.');
     readln (fincrement);
     writeln ('Enter the upper limit for the');
     writeln ('coefficient of friction.');
     readln (flimit);
   END; \{ case of F \}
  'i','I' :
   BEGIN
     writeln ('Enter the starting value for the');
     writeln ('moment of inertia.');
     readln (istart);
     writeln ('Enter the amount to be incremented');
```

<sup>1</sup>8````8``8``8``\$<sup>\$</sup>`\$<sup>\$</sup>8`\$\$**\$`**\$\$**\$`\$**\$\$`\$**\$\$**\$<mark>``\$\$``\$\$``\$\$``\$\$``\$\$``\$\$``\$\$``\$</mark>

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```
writeln ('each pass. WARNING: The smaller');
    writeln ('the increment the longer the');
    writeln ('calculation.');
    readln (iincrement);
    writeln ('Enter the upper limit for the');
    writeln ('moment of inertia.');
    readln (ilimit);
   END; { case of I }
 END; \{ case \}
writeln ('Enter the total mass of the pendulum.');
readln (mass);
writeln ('Enter the distance from the pivot to the');
writeln ('center of mass.');
readln (cmdistance);
imoment := istart; airconst := astart;
frictconst := fstart;
CASE cselect OF
 'a','A' :
   BEGIN
     CASE calcvar OF
       'a'.'A' :
        BEGIN
          writeln ('Enter the distance to the');
          writeln ('center of the plates.');
          readln (airlength);
          writeln ('Enter the moment of inertia');
          writeln ('for the pendulum.');
          readln (imoment)
         END; \{ case of A \}
       'f','F' :
         BEGIN
          writeln('Friction cannot be considered');
          writeln ('in this set up.');
           GOTO 3
         END; { case of F }
       'i','I' :
         BEGIN
           writeln ('Enter the distance to the');
           writeln ('center of the plates.');
           readln (airlength);
           writeln ('Enter the coefficient of air');
           writeln ('resistance.');
           readln (airconst);
         END { case of I }
      END; { case }
    END; \{ case of A \}
   'f','F' :
    BEGIN
      CASE calcvar OF
        'a','A' :
         BEGIN
           writeln ('Air resistance is not');
```

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writeln ('considered in this set up.'); GOTO 3 END; { case of A } 'f','F': BEGIN writeln ('Enter the moment of inertia'); writeln ('for the pendulum.'); readln (imoment) END; { case of F } 'i','I' : BEGIN writeln ('Enter the coefficient of'); writeln ('friction.'); readln (frictconst) END; { case of I } END; { case } END; { case of F } 'n','N' : BEGIN IF calcvar IN ['a','A','f','F'] THEN BEGIN writeln ('Neither air resistance or'); writeln ('friction are considered in '); writeln ('this configuration.'); GOTO 3 END; { then } END;  $\{ case of N \}$ 'b','B' : BEGIN writeln ('Enter the distance to the center '); writeln ('of the plates.'); readln (airlength): CASE calcvar OF 'a','A' : BEGIN writeln ('Enter the coefficient of'); writeln ('friction.'); readln (frictconst); writeln ('Enter the moment of inertia'); writeln ('for the pendulum.'); readln (imoment) END; { case of A } 'f','F' : BEGIN writeln ('Enter the coefficient of air'); writeln ('resistance.'); readln (airconst): writeln ('Enter the moment of inertia'); writeln ('for the pendulum.'); readln (imoment) END;  $\{ case of F \}$ 'i','I' :

```
BEGIN
             writeln ('Enter the coefficient of');
             writeln ('friction.');
            readln (frictconst);
             writeln ('Enter the coefficient of air');
             writeln ('resistance.');
             readln (airconst)
           END; { case of I }
        END; { case }
      END; \{ case of B \}
   END; { case }
   writeln ('Enter the initial angle in radians.');
   readln (theta);
   pendconst := mass * g * cmdistance / imoment;
4 : CASE calcvar OF
    'a'.'A' :
      BEGIN
        airconst := airconst + aincrement;
        IF airconst > alimit THEN
         BEGIN
           writeln ('The coefficient of air');
           writeln ('resistance exceeds the limit.');
           writeln ('Either the tolerance is too');
           writeln ('strict or the value is not ');
           writeln ('between the start value and ');
           writeln ('the upper limit.');
           GOTO 5
         END:
      END; \{ case of A \}
     'f','F' :
      BEGIN
        frictconst := frictconst + fincrement;
        IF frictconst > flimit THEN
         BEGIN
           writeln ("The coefficient of friction");
           writeln ('exceeds the limit. Either the');
           writeln ('tolerance is too strict or the');
           writeln ('actual value is not between ');
           writeln ('the start value and the limit.'):
           GOTO 5
          END:
      END; \{ case of F \}
     'ï'.Τ':
      BEGIN
        imoment := imoment + iincrement;
        pendconst := mass * g * cmdistance / imoment;
        IF imoment > ilimit THEN
          BEGIN
            writeln ('The moment of inertia exceeds');
            writeln('the limit. Either the tolerance');
            writeln ('is too strict or the actual');
            writeln ('value is not between the start');
```

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writeln ('value and the upper limit.');
        GOTO 5
      END;
   END; { case of I }
END; \{ case \}
seek (pendata, 6); { Skip labels and the first few }
ypast[1,1] := theta; { points calculated by the }
ypast[1,2] := 0.0; { Runge-Kutta method which are }
                  { difficult to incorporate into }
time := 0.0;
FOR i := 1 TO 2 DO { the comparison. }
 BEGIN
   time := time + delta t;
   Runge4 (pendconst,airlength,frictconst,airconst,
          delta t,cselect,ypast,i);
 END; { for i \overline{}
CASE cselect OF
  'p','P','n','N' :
   BEGIN
     Noprime (pendconst, ypast[1], k1);
     Noprime (pendconst, ypast[2], k2);
     Noprime (pendconst, ypast[3], k3);
   END; { case of P }
  'a','A' :
   BEGIN
     Airprime (pendconst,airlength,airconst,
             ypast[1], k1);
     Airprime (pendconst,airlength,airconst,
             ypast[2], k2);
     Airprime (pendconst,airlength,airconst,
             ypast[3], k3);
   END; { case of A }
  'f','F' :
   BEGIN
     Frprime (pendconst, frictconst, ypast[1], k1);
     Frprime (pendconst, frictconst, ypast[2], k2);
     Frprime (pendconst, frictconst, ypast[3], k3);
    END; \{ case of F \}
  'b','B' :
    BEGIN
     Bothprime (pendconst, airlength, frictconst,
              airconst, ypast[1],k1);
     Bothprime (pendconst, airlength, frictconst,
              airconst, ypast[2],k2);
     Bothprime (pendconst, airlength, frictconst,
              airconst, ypast[3],k3);
    END; \{ case of B \}
  END; \{ case \}
 WHILE NOT eof(pendata) DO
  BEGIN
    read (pendata, buffer);
    intolerance := false;
    WHILE NOT intolerance DO
```

```
BEGIN
         time := time + delta t;
         PredictCorrect(pendconst,airlength,
                     frictconst, airconst, delta t,
                     cselect, ypast, k1, k2, k3);
         IF abs(buffer[1] - time) < xtolerance
           THEN intolerance := true;
       END; { while not }
      IF abs(buffer[2] - ypast[4,2]) > = ytolerance
       THEN GOTO 4
    END; { while not }
   close (pendata);
   CASE calcvar OF
    'a','A' :
      BEGIN
        writeln ('The coefficient of air resistance');
        writeln ('for this system is:');
        writeln (airconst:6:4)
      END:
    'f','F' :
      BEGIN
        writeln ('The coefficient of friction for');
       writeln ('this system is:');
        writeln (frictconst:6:4)
      END:
    ï',T' :
      BEGIN
        writeln ('The moment of inertia for this');
        writeln ('system is:');
        writeln (imoment:6:4,' kg-m**2')
      END:
   END; { case }
5: writeln:
 END; { Compare }
```

#### 

**PROCEDURE** Compplot (VAR file1, file2 : datafile);

{ This routine plots two data files for comparison. It uses the organic Turbo Pascal routines discussed in the comments for the Plot Procedure. }

## LABEL 1;

#### VAR

x1, x2, y1, y2, config, scale : integer; buff, temp, temp2 : vector; curve : char;

## BEGIN

clrscr;

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graphmode;
hires;
Axis:
reset (file1);
read (file1,temp);
curve := chr(round(temp[1]));
IF curve IN ['d','D']
 THEN scale := 40
 ELSE scale := 10;
read (file1, temp, buff, temp2); { read labels }
config := round(temp[1]);
writeln (curve,' PLOT 1: Config = ',chr(config),
       m^{*}g^{*}d/I = ',temp[2]:5:3,' Airlength = ',
       buff[1]:5:3,' Theta(0) = ', buff[2]:5:3);
writeln ('
               Frict Coef = ',temp2[1]:5:3,
       'Air Coef = '.temp2[2]:5:3);
read (file1.buff);
x2 := round(buff[1] * 100) + 10;
y2 := 110 - round(buff[2] * scale);
WHILE NOT eof(file1) DO
 BEGIN
   x1 := x2;
   y1 := y2;
   read (file1, buff);
   x2 := round(buff[1] * 100) + 10;
   y2 := 110 - round(buff[2] * scale);
   draw (x1, y1, x2, y2, 5);
 END; { while not }
close (file1):
reset (file2);
read (file2, temp);
curve := chr(round(temp[1]));
IF curve IN ['d','D']
  THEN scale := 40
  ELSE scale := 10;
read (file2, temp, buff, temp2);
config := round(temp[1]);
writeln (curve,' PLOT 2: Config = ',chr(config),
        m^{*}g^{*}d/I = ',temp[2]:5:3,' Airlength = ',
        buff[1]:5:3,' Theta(0) = ', buff[2]:5:3);
                Frict Coef = ',temp2[1]:5:3,
writeln ('
        'Air Coef = ',temp2[2]:5:3);
read (file2.buff):
x2 := round(buff[1] * 100) + 10;
y_2 := 110 - round(buff[2] * scale);
WHILE NOT eof(file2) DO
  BEGIN
    x1 := x2;
    y1 := y2;
    read (file2, buff);
    x2 := round(buff[1] * 100) + 10;
    y2 := 110 - round(buff[2] * scale);
```

draw (x1, y1, x2, y2, 5); END; { while not } close (file2); 1 : writeln ('Are you done with the plot? (Y/N)'); IF Yes THEN textmode ELSE GOTO 1 END; { Compplot }

**PROCEDURE** Compdata (VAR file1, file2 : datafile);

{ This routine plots the data and simulation files for comparison. File1 is the data file. It uses the organic Turbo Pascal routines discussed in the comments for the Plot Procedure. }

LABEL 1;

#### VAR

x1, x2, y1, y2, config, scale : integer; buff, temp, temp2 : vector; curve : char;

## BEGIN

```
clrscr;
graphmode;
hires;
Axis;
reset (file1);
read (file1,temp);
curve := chr(round(temp[1]));
read (file1, temp, buff, temp2);
config := round(temp[1]); { Get labeling data }
writeln('Data Config = ',chr(config),' m*g*d/I = ',
      temp[2]:5:3, Airlength = ', buff[1]:5:3,
      ' Theta(0) = ', buff[2]:5:3);
WHILE NOT eof(file1) DO
 BEGIN
   read (file1, buff);
   x2 := round(buff[1] * 100) + 10;
   y_2 := 110 - round(buff[2] * 10);
   draw (x2, y2-2, x2, y2+2, 5);
   draw (x2-4, y2, x2+4, y2, 5);
 END; { while }
close (file1):
reset (file2):
read (file2, temp);
curve := chr(round(temp[1]));
IF curve IN ['d','D']
 THEN scale := 40
```

```
ELSE scale := 10;
  read (file2, temp, buff, temp2);
  config := round(temp[1]);
  writeln (curve,' Plot Config = ',chr(config),
          m^{*}g^{*}d/I = ',temp[2];5:3,' Airlength = ',
         buff[1]:5:3,' Theta(0) = ', buff[2]:5:3);
  writeln ('
                  Frict Coef = ',temp2[1]:5:3,
          'Air Coef = ',temp2[2]:5:3);
  read (file2, buff);
  x2 := round(buff[1] * 100) + 10;
  y2 := 110 - round(buff[2] * scale);
   WHILE NOT eof(file2) DO
    BEGIN
      x1 := x2;
      v1 := v2;
      read (file2, buff);
      x2 := round(buff[1] * 100) + 10;
      y2 := 110 - round(buff[2] * scale);
      draw (x1, y1, x2, y2, 5);
    END; { while not }
  close (file2);
1 : writeln ('Are you done with the plot? (Y/N)');
  IF Yes
    THEN textmode
    ELSE GOTO 1
 END; { Compdata }
 BEGIN { Physpendulum }
   assign (simdata1, 'A:SIMDATA1.DAT');{ This is Turbo }
   assign (simdata2, 'A:SIMDATA2.DAT');{ Pascal's method }
   assign (pendata, 'A:PENDATA.DAT'); {of assigning file }
   datataken := false; { variables to disk files, not by }
   sim1complete := false; { rewrites. }
   sim2complete := false;
   writeln ('Welcome to the Physical Pendulum data ');
   writeln ('collection and simulation program.');
1 : writeln;
   writeln ('Enter T to Takedata, S to Simulate, C to');
   writeln ('Compare the data with the numerical');
   writeln ('solution and calculate the moment of ');
   writeln ('inertia, A to calculate data using the');
   writeln ('Small Angle approximation, or Q to Quit.');
   readln (response);
   CASE response OF
     'q','Q' : HALT;
     'a','A' :
      BEGIN
        writeln('The small angle approximation routine');
        writeln('has been calculated assuming a system');
        writeln('of no constraints (no air resistance ');
```

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```
writeln ('or friction). If comparisons');
  writeln('evaluating the appropriate use of the');
  writeln ('small angle approximation are going ');
  writeln ('to be made, insure that the');
  writeln ('simulations are done using the No');
  writeln ('constraints (N) option. The small');
  writeln ('angle routine stores its data in the');
   writeln ('first simulation file so comparison ');
   writeln ('simulations are second simulations.');
  Smallangle (simdata1);
  sim1complete := true;
   writeln ('Do you wish to plot the results'):
   writeln ('obtained using the small angle');
   writeln ('approximation? (Y/N)');
  IF Yes
    THEN Plot (simdata1);
 END; { case of A }
't'.'T' :
 BEGIN
  IF datataken
    THEN
      BEGIN
       writeln('Any new data taken will destroy');
       writeln ('the current data. Do you wish');
       writeln ('to take new data? (Y/N)');
       IF Yes
         THEN Takedata (datataken)
         ELSE GOTO 1
      END { then }
    ELSE Takedata (datataken);
   writeln ('Do you wish to plot the data? (Y/N)');
   IF Yes
    THEN DataPlot (pendata):
   writeln ('Do you wish to shift the data? (Y/N)');
   IF Yes THEN
    BEGIN
   3 : Shiftdata (pendata);
      writeln ('Do you wish to plot the shifted');
      writeln ('data? (Y/N)');
      IF Yes
       THEN DataPlot (pendata);
      writeln ('Do you wish to shift the data');
      writeln ('again? (Y/N)');
      IF Yes
        THEN GOTO 3:
    END:
 END; \{ case of T \}
's','S' :
 BEGIN
   IF sim1complete
    THEN
      BEGIN
```

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writeln ('A simulation has been ');
   2 : writeln ('completed. Do you wish to');
       writeln ('resimulate, calculate a second');
       writeln ('simulation or return to the');
       writeln ('main menu? Enter');
       writeln (' R - Resimulate ');
       writeln (' S - Second simulation ');
       writeln (' Q - Quit, return to main menu');
       readln (simselect);
       CASE simselect OF
         'q','Q' : GOTO 1;
        'r','R' :
          BEGIN
            Simulate (sim1complete, simdata1);
            writeln ('Do you wish to plot the');
            writeln ('simulation? (Y/N)');
            IF Yes
             THEN Plot (simdata1);
          END; \{ case of R \}
         's','S' :
          BEGIN
            Simulate (sim2complete, simdata2);
            writeln ('Do you wish to plot the');
            writeln ('simulation? (Y/N)');
            IF Yes
             THEN Plot (simdata2);
          END { case of S }
         ELSE
          BEGIN
            writeln ('Not an allowed response.');
            GOTO 2
          END; { else }
       END; { case }
     END { then }
    ELSE
     BEGIN
       Simulate (sim1complete, simdata1);
       writeln ('Do you wish to plot the');
       writeln ('simulation?(Y/N)');
       IF Yes
         THEN Plot (simdata1);
     END; { else }
 END; { case of S }
'c','C' :
 BEGIN
  IF datataken
    THEN
      BEGIN
        Compare (pendata);
       GOTO 1
      END { then }
    ELSE
```

BEGIN writeln ('Data must first be taken in'); writeln ('order to run the comparison'); writeln ('and calculate any of the'); writeln ('constants.'); GOTO 1 END; { else } END { case of C } ELSE BEGIN writeln ('Not a proper response.'); GOTO 1 END; { else } END; { case } IF datataken AND sim1complete THEN BEGIN writeln ('Do you wish to graphically compare'); writeln ('the plot of the data and the first'); writeln ('simulation? (Y/N)'); IF Yes THEN Compdata (pendata, simdata1); END; { then } IF datataken AND sim2complete THEN BEGIN writeln ('Do you wish to graphically compare'); writeln ('the plot of the data and the second'); writeln ('simulation? (Y/N)'); IF Yes THEN Compdata (pendata, simdata2); END; { then } IF sim1complete AND sim2complete THEN BEGIN writeln('Do you wish to graphically compare'); writeln('the two simulations? (Y/N)'); IF Yes THEN Compplot (simdata1, simdata2) END; { then } GOTO 1 END. { Physpendulum }

SUBROUTINES FOR "DROP" MODIFIED FOR USE IN "FRESHPEN" 10/19/85 \* BRIAN DAVIS MODIFIED BY MARK STEVENS 8/19/87 \* PUBLIC ROUTINES PUBLIC SETUP PUBLIC DRAWCURS DRAW CURSOR PUBLIC COUNT COLLECT DATA POUBLIC GRAPH GRAPH DATA \*EXTERNAL REFERENCES PUTC EXT SETT EXT \* TIME LOCATION : CHANGE TO LOW MEMORY IF ROM'ED TIME RMB 1 SETUP ORCC #\$50 LEAX IRQ, PCR STX \$10D LDA #\$7E STA \$10C LDA #\$BF STA \$FF52 PB6= INPUT CLR \$FF50 RTS \* INTERRUPT HANDLER **IRQ TST \$FF02 CLEAR INTERRUPT FLAG** DEC TIME,PCR RTI \* PASCAL CALL: **PROCEDURE COUNT (STARTADD:INTEGER)** \* STARTADD IS STARTING ADDRESS OF BUFFER

\* BUFFER : ARRAY OF INTEGER

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\* INITIAL STACK: STARTADD EQU 6 START OF BUFFER ADDRESS \* 4-5.S: LINK \* 2-3.S: RETURN ADDRESS \* 0-1,S: SAVED U \* SETUP COUNT PSHS U SAVE LINK LDU STARTADD,S LDX #\$FF01 TURN OFF PIA INTERRUPTS BSR CLRINT INC \$FF03 60 HZ IRQ ON ANDCC #\$EF ENABLE INTERRUPTS LDA #64 PSHS A COUNT ON STACK LDX **#\$F**F50 SYNC WAIT UNTIL IRQ TRAN CLRB TRANSITIONS = 0LDA #\$6 STA TIME, PCR COUNT FOR 1/10 SECOND LDA ,X GET PORT VALUE TRAN1 CMPA ,X CHANGE? **BEQ TRAN2** INCB YES, INCREMENT TRANSITION COUNT LDA ,X NEW PORT VALUE TRAN2 TST TIME.PCR CHECK TIME **BNE TRAN1** CLR ,U+ CLEAR HIGH BYTE OF INTEGER STB, U+ STORE POINT DEC .S SEE IF DONE BNE TRAN ORCC #\$50 PULS A,U,PC **CLRINT CLEARS INTERRUPTS** X = ADDRESS OF PIA CRA**CLRINT LDA .X** ANDA #\$FE STA X LDA 2.X ANDA #\$FE STA 2.X RTS \* PASCAL CALL:

ประเทศที่เป็นในให้และหน่ามาต่ามาต่างก่อ แก่ต่างก่อ แก่สามหัติเมริตาสามันต์ได้เหลือแล้วตามและต่างก่องต่างการเป็น

\* PROCEDURE GRAPH (STARTADR : INTEGER)

\* STARTADR IS AN ADDRESS : BUFFER[1] \* PLOTS LOW ORDER BYTES OF ARRAY \* PLOTS 64 POINTS, IE \* BUFFER[1] - BUFFER[64] \* STACK: START EQU 6 \* 4-5,S: LINK \* 2-3,S: RETURN ADDRESS \* 0-1,S: SAVED U \* \$88 CONTAINS POINTER TO CURRENT **GRAPHICS CONTROL BLOCK** \* FORMAT OF GRAPHICS CONTROL BLOCK: (ADDRESS IN Y REG) \* 0-1. Y = SCREEN START ADDRESS\* 2-3, Y = SCREEN END ADDRESS \* 4. Y = GRAPHICS Y COORD.5, Y = GRAPHICS COORD.**GRAPH PSHS U SAVE LINK** LDU START, S U = START ADDRESSLDY \$88 Y = CONTROL BLOCK POINTER CLR 5, Y X COORD = 0\* LOOP TO PLOT/UNPLOT LEAU 1.U POINT TO LOW BYTE GLP LDA ,U++LDB #180 SCALE Y MUL SUBA #191 COMA STA 4, Y STORE Y LBSR SETT GET THE ADDRESS 'BIT COMB FLIP BIT MASK ANDB ,X RESET BIT STB ,X PUT IT ON SCREEN LDA 5.Y X = X+4ADDA #4 STA 5.Y BNE GLP **GRAPHRET PULS U,PC** \* PASCAL CALL DRAWCURS(X,Y:INTEGER)

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\* DRAWS CURSOR AT COORDINATES \* PERFORMS SCALING \* 7,S:X COORD 5.S:Y COORD DRAWCURS LDY \$88 LDA 5,S GET Y LDB#180 SCALE IT MUL SUBA #186 CURSOR IS 4 BYTES HIGH- 186 ADJUSTS COMA FOR HEIGHT SO BOTTOM IS ABOVE POINT LDB 7,S X = X+4LSLB LSLB STD 4,Y PUT INTO GY,GX PSHS U SAVE LINK LBSR SETT LDA #4 LEAU ARROW, PCR PSHS D CURS1 LDA, U+ LDB 1,S MUL ASLB ROLA EORA ,X EORB 1.X STD,X LEAX \$20,X CMPX 2.Y **BHI CURSEX** DEC ,S **BNE CURS1** CURSEX PULS D,U,PC ARROW FDB \$10A0 FDB \$C0E0

END

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# **APPENDIX C: Example Plots**

Any plot the Physpend routine displays on the screen of the Zenith Z-140 PC can be printed using the print screen command and a graphics capable printer. Before running Physpend the DOS command "graphics" must be executed. The following example plots include a data plot, a comparison of data to a simulation, a comparison of two simulations, a plot of the displacement and angular velocity for the same system, and an example of solution instability with increasing step size.



Data Config =  $b = \frac{w + g + d}{I} = 0.033 \text{Airlength} = 0.220 \text{ Theta}(0) = 1.571 \text{ Are you done with the plot? (Y/N)}$ 

Figure C.1. Data Plot





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Figure C.3. Simulation 1 vs. Simulation 2



Figure C.4. Angular Velocity vs. Displacement



Figure C.5. Numerical Method Instability

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# **APPENDIX D: Experiment Instructions**

Experimental background and instructions were developed for each of the experiments. The instructions for all three experiments are included in this appendix. The level of difficulty and detail of the instructions were matched to the expected capabilities of the students. The freshmen are expected to complete the experiment and turn in their laboratory notebooks after two ninety minute periods, while the juniors are given one week and are required to submit a more formal report.

## NUMERICAL METHODS AND ROTATIONAL MOTION (VISCOUS DAMPING - TERMINAL VELOCITY)

# I. INTRODUCTION

In this experiment we will consider the rotational motion of a disk with adjustable plates which resist the disk's motion through the air. The disk will be accelerated by applying a constant torque. The rotational inertia of the rigid body will be calculated by breaking it into parts and finding the rotational inertia of each by knowing the mass and shape of each. The total rotational inertia is simply the sum of the individual parts.

After calculating the moment of inertia the angular velocity plot of the system will be calculated using the improved Euler's method and a comparison made to the actual angular velocity curve measured by the microcomputer. By adjusting the fins the effect of air resistance on the velocity of the wheel will be investigated.

The apparatus consists of a thirty centimeter aluminum disk and a hub of smaller diameter, both mounted on an axle with ball bearings. We also have a notched disk which allows us to measure the rotation of the body and two adjustable rectangular plates provide air resistance.

### **II. THEORY REVIEW**

The viscous damping force that affects the disk can be approximated as being proportional to some power of the linear velocity of the plates. The total torque acting on the disk can be written

$$I\frac{d\omega}{dt} = \frac{mgrI}{I+mr^2} - kl(\omega)^n$$

where k is a constant which describes the damping force, l is the distance from the rotational axis to the center of the plates, r is the moment arm of the accelerating weight, and n is an integer. As the disk begins to accelerate under an applied torque the viscous damping force applies a retarding torque slowing down the angular acceleration. Finally, the disk reaches a contant "terminal" angular velocity at which point the net torque acting on the disk is zero.

The exact solution of this motion in practice is quite difficult. The applicaton of the improved Euler's method to this motion lets us study the behavior of this system in detail. We can see the effect of varying k and n and compare the calculated solution to the actual motion as measured by the microcomputer.

### **III. PROCEDURE AND ANALYSIS**

## Part A

To find the rotational inertia of the system from the mass and shape of the individual parts use the unassembled parts found next to the balance. <u>DO NOT</u> <u>DISASSEMBLE THE APPARATUS TO BE USED IN PART C.</u> Measure the mass and

all relevant dimensions and compute the resulting rotatinal inertia. Estimate the uncertainty for each of the parts and the overall uncertainty of the calculated value of the rotational inertia. Show all of the measurements, calculations and uncertainties in the form of a table.

### Part B

Noting in this case that

$$\frac{\mathrm{d}\omega}{\mathrm{d}t} = \frac{\mathrm{mgr}}{\mathrm{I} + \mathrm{mr}^2} \cdot \mathrm{kl}(\mathrm{k}\omega)^n$$

we can apply the improved Euler's method to calculate and plot the angular velocity of the system. Remember that the improved Euler's method first computes the value of angular velocity one half of the way into the first interval.

$$\omega_{0.5} = \omega_0 + a_0(\frac{\Delta t}{2})$$

Then using this value we calculate

$$\boldsymbol{a}_{0.5} = \frac{\mathrm{mgr}}{\mathrm{I} + \mathrm{mr}^2} - \mathrm{kl}(\mathbf{k}_{0.5})^n$$

Finally we obtain

$$\boldsymbol{\omega}_1 = \boldsymbol{\omega}_0 + \boldsymbol{a}_{0.5} \Delta \mathbf{t}$$

To calculate the value of  $\omega$  for the next point the initial value  $\omega_0$  is replaced with  $\omega_1$ and the above steps are repeated. Notice that we are simply using the slope of the angular velocity curve one half way through the time interval and we add that change to the preceding value of  $\omega$  at the beginning of the interval. Calculate and plot the first twenty points for the motion using t = 0.1 seconds and k = 0.4. Measure 1 and d from the apparatus and use your calculated value for the rotational inertia from Part A. You might want to tabulate your values for a and  $\omega$  to aid in calculation and plotting.

Will increasing the length of the time interval increase or decrease the accuracy of the numerical method in approximating the actual motion? Why?

# Part C

We are using the microcomputer to measure the angular velocity of the rotating disk. It will also use an equivalent numerical method to calculate the angular velocity curve for comparison to the data. The microcomputer will count slots in the notched wheel every 0.1 seconds. It plots the resulting angular velocity curve, the slope of which is the angular acceleration, a.

Turn on the microcomputer and initiate the Airwheel program. Follow the instructions given and enter the appropriate data when prompted.

First, orient the plates so that they cause a minimum amount of air resistance. Wind up the string with the 500 gram mass. Release the wheel and <u>simultaneously</u> press any key on the microcomputer to take the data. Input your values from Part A and Part B in the simulation, choosing the no air resistance option, and compare the calculated curve with the actual motion. Are the curves the same? If not, why?

#### Part D

Take data again but adjust the plates for maximum air resistance. Run the simulation now using I from part C. Again try to match the calculated curve with the actual angular velocity curve by varying values of k and n. Which model for the viscous force is closest to the actual motion? What is the value for k?

Adjust the plates to some intermediate position and measure the angular velocity. Again match the curve with the computer calculated angular velocity. Is the same model for the viscous force still the most accurate? What happens to the value of k? What happens to the value for the terminal angular velocity?

If you changed the mass accelerating the wheel would it affect the terminal velocity? How?

# Part E

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Test the accuracy of the numerical method when you vary the time interval. What happens to the value for the terminal velocity for large time intervals? How large can  $\Delta t$  be before the difference between the curves becomes significant? For a more dramatic demonstration of the sensitivity of this type of numerical method to the step size load the Freshpen program for a physical pendulum and vary the step size for the harmonic motion calculation. Why would the improved Euler's method be more sensitive to  $\Delta t$  for the oscillating function obtained for harmonic motion than to the angular velocity curve for the rotating disk that approaches a terminal value?

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# NUMERICAL METHODS AND THE PHYSICAL PENDULUM (FREE AND DAMPED HARMONIC MOTION)

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# I. INTRODUCTION

In this experiment we will use numerical methods to investigate the oscillation of a physical pendulum. We will examine both undamped and damped oscillations. The rotational inertia of the pendulum will be calculated by breaking it into parts and finding the rotational inertia of each part by knowing the mass and shape of each. The total rotational inertia is simply the sum of the individual parts.

After calculating the moment of inertia the motion of the pendulum will be recorded by the microcomputer. A numerical method equivalent to the improved Euler's method (called Heun's method) is then employed by the computer to simulate the motion.

The apparatus consists of a thirty centimeter diameter aluminum disk with a hub and slotted disk for measuring rotation. It also has two rectangular plates which provide viscous damping and a weight to offset the center of mass from the axis of rotation.

#### **II. THEORY REVIEW**

For an undamped physical pendulum the equation of motion is

$$I\frac{d\omega}{dt} = -mgd \sin\theta$$

where d is the distance from the rotation axis and  $\theta$  is measured from the vertical. In the case of viscous damping the force providing the damping torque can be approximated as being proportional to some power of the linear velocity of the resisting plates. This torque always opposes the direction of motion and modifies the equation of motion to

$$I\frac{d\omega}{dt} = -mgd \sin\theta \pm kl(k\omega)^n$$

where l is the distance from the rotation axis to the center of the plates, k is a constantwhich describes the damping force, and n is an integer.

The exact solution to either of these equations is difficult, except when the small angle approximation  $(\sin\theta = \theta)$  is made for the undamped case. The application of the numerical method to this system allows us to study the motion in detail. The effects of varying n and k can be investigated and values for the actual system determined.

#### **III. PROCEDURE AND ANALYSIS**

# Part A

To find the rotational inertia from the mass and shape of the individual parts use the unassembled parts found next to the balance. <u>DO NOT DISASSEMBLE THE</u> <u>APPARATUS TO BE USED IN PART B.</u> Measure the mass and all relevant dimensions and compute the resulting rotational inertia. (Note: The parallel axis theorem might be useful here.) Estimate the uncertainty for each of the parts and the overall uncertainty of the calculated value of the rotational inertia. Show all of the measurements, calculations and uncertaincies in the form of a table.

Calculate the distance from the rotation axis to the center of mass and record the total mass of the pendulum.

#### Part B

We are using the microcomputer to measure the angular velocity of the pendulum. It will also use the numerical method to calculate the angular velocity given input data and will compare it to the actual data curve. The microcomputer will count slots in the notched wheel every 0.1 seconds and will plot the resulting angular velocity. Note that it only plots the absolute value of the angular velocity.

Turn on the microcomputer and initiate the Freshpen program. Follow the instructions given and enter the appropriate data when prompted.

First, orient the plates so that they cause a minimum amount of air resistance. Set the pendulum to the starting angle for the desired motion. Make sure you measure and record the starting angle for the oscillation. Release the pendulum and <u>simultaneously</u> press any key on the microcomputer to take the data. Input your values from Part A into the simulation, choosing the no air resistance option, and compare the calculated curve to the actual motion. Are they the same? If not, why? What is the calculated period of the motion?

Adjust the input values for I until you match the actual angular velocity curve. Record this value. What is the period of the actual motion?

# Part C

Take the data again but adjust the plates for maximum air resistance. Run the simulation now using I from Part B. Again match the calculated curve with the actual angular velocities by adjusting the values of k and n. What value of n seems to be the closest to the actual measured motion? What is the value for k? What is the period of motion for this configuration? Compare it to the period in Part B. Explain any differences.

Adjust the plates to an intermediate position and again measure the angular velocity with the microcomputer. Are the values for n and k the same? If not, why?

#### Part D

Use the simulation routine and determine a value for k that results in a critically damped system. How might you provide such damping in the laboratory? Discuss what happens to the period, rotational inertia, d, and the value of k if a heavier weight were used to unbalance the disk. Would critical damping require a larger or smaller value for k in this case?

## Part E

Test the accuracy of the numerical method when you vary the time interval. What happens as you increase the step size? At what value for  $\Delta t$  does the calculated curve seem to develop a significant error? Why does this error occur? If the angular velocity function were not oscillatory and approached some asymptotic value would the numerical method be as sensitive to the size of the step in time? For verification load the Airwheel program and investigate the effect of changing step size in the terminal

velocity simulation.

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### NUMERICAL METHODS AND THE PHYSICAL PENDULUM

This experiment allows you to investigate the harmonic motion of a real physical pendulum utilizing a microcomputer to take the data and compare it to the calculated motion derived using numerical methods. The setup consists of two systems; the modified TRS-80 system for taking data, and the Zenith Z-140 PC used for analysis. Each time data is taken it must be input into the Zenith for analysis.

The data is taken by means of a notched wheel and two photogates. The motion of whatever physical configuration you construct is recorded by counting the tripping of the photogates as the notches pass. There are 90 notches on the wheel and the count is recorded every 0.1 second. The resulting data yields an angular velocity plot. Using the known angular displacement of each notch the integer counts are converted to radians per second and displayed for transfer into the Zenith. To take data turn on the TRS-80 system. Insert the program disk and type RUN "DUMP". Respond "0" to the drive prompt and enter "JPENDATA" for the filename. The down loaded program will then instruct you on the procedure for taking and displaying the data.

Once data is taken you will want to analyze it with the Zenith. To do this insert the Zenith program diskette. Turn the system on. At the prompt enter GRAPHICS. This will allow you to print the plots from the screen by using the PrtSc key. Then enter PHYSPEND. The program will then give you instructions for analysis. The program will accept the input data, calculate the motion for small angle approximations, motion with friction and air resistance and even the motion of a simple pendulum. You are able to compare two simulations, or either simulation with the data. Any plot can be printed with the Print Screen command. The simulation utilizes a 4th order Predictor-Corrector method to approximate the solution to the differential equations of motion (you should know what the equations are). The accuracy of this method can be tested by varying the time step size. It is accurate enough to calculate the actual values of different factors for the physical pendulum by using an iterative process. It will calculate the motion and compare it to the data point by point until it gets a fit, subject to the limits you give it.

Utilizing the computer and software as a tool you should ivestigate the physical pendulum for large and small angle oscillations, large and small moments of inertia, large and negligible friction effects and the simple pendulum and small angle approximations verses the actual system. None of the physics theory is difficult and you should readily verify the effects of varying parameters (such as the moment of inertia, friction coefficient, etc.) on the motion of the pendulum. What you investigate is up to you, but areas of interest include, but are not limited to,

- at what angle is the small angle approximation no longer appropriate?
- the acutal moment of inertia of the pendulum.
- the coefficient of friction in the bearings.

- the effects and coefficient of air resistance.

- variations in the accuracy of the numerical method with changing time intervals.

# **ENDNOTES**

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5 Ibid., p. 354.

6 Ibid., p. 362.

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9 Ibid., pp. 373-393.

10 Ibid., p. 399.

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12 Ibid., p. 408.

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14 DEFT Pascal Workbench User's Guide (: DEFT Systems Inc., 1984).

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