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DESIGN METHODS FOR OPTIMIZING EFFICIENCY OF THE SERIES RESONANT CONVERTER OPERATING ABOVE RESONANCE

> by Francis Aloysius Fahy Capt, USAF

A thesis submitted in partial fulfillment of the requirements for the degree of

Master of Science

University of Washington

1988

Chairperson of the Supervisory Committee: Professor Thomas H. Sloane Department of Electrical Engineering

- Design methods for optimizing efficency of the series resonant converter (SRC) operating above resonance are presented. Included in the power loss analysis is the development of expressions for individual component power losses as a function of the transformer turn ratio n, the circuit characteristic impedance R₀, and other design variables. Results of the operating efficiency are graphically represented as a function of n and R₀ for a hypothetical SRC circuit with 100W output power and 50KHz switching frequency with discussion of results following. (SE pages)



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bу

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Master's Thesis

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CHAPTER 1

INTRODUCTION

In the past several years, there have been a number of technical papers written to aide the design of the series resonant converter (SRC). Francis C. Schwarz introduced the SRC as a converter with a high power/weight ratio and efficient semiconductor switching characteristics [1]. The typically high operating efficiency of the SRC results from the reduction of switching losses. The reduction of switching losses allows very high frequency operation which provides the advantage of size reduction of the components. The reduction in component sizing ultimately reduces the weight of the converter. These advantages of the SRC have been utilized in aerospace power supply system applications.

After Schwarz presented the improved SRC, other research followed with the purpose of obtaining a more complete analysis of the SRC [2]. Stuart and King modified the analysis of Schwarz and derived closed-form steadystate equations for the SRC [3]. Results of their research includes expressions for normalized currents and voltages as a function of the 'retard angle', often called the diode conduction angle. Vorperian and Cuk followed with a rigorous dc analysis of the SRC which expressed the gain or dc-to-dc conversion ratio as a function of the switching frequency, resonant frequency, inductance, and load resistance [4]. Most recently, Witulski and Erickson have considered steady-state SRC operation with the intent to minimize component stress [5]. Their analysis of converter operation and component stress is based on a normalized output-plane model. With the same motivation as the aforementioned authors, to aid the design of the SRC, this thesis seeks to develop design methodologies for maximizing steady-state operating efficiency of the SRC above resonance.

The primary task of this thesis is to develop an analytical expression for the efficiency of the SRC as a function of the transformer turn ratio n and the characteristic impedance R_0 of the series L-C resonant circuit. To determine this efficiency, a systematic analysis of the power losses for the individual components is required. Due to the series configuration of the SRC, the same current flows through all components. Determination of component losses as a function of n and R_0 can be simplified if the series current can be expressed as a function of n and R_0 . Analytic models must be utilized to develop expressions for the power losses in the individual components.

Before developing these expressions relating losses of each component to the design parameters n and R_{o} , the basic operation of the SRC must be understood. In Chapter 2 a general discussion of converter waveforms and operation above resonance is presented. Chapter 3 introduces and defines the design parameters the normalized output-plane analytical model. Chapters 4 contains development of loss expressions for each of the components of the SRC. In Chapter 5, total power losses are computed for a specific converter configuration. The efficiency of this particular converter is graphically represented as a function of the transformer turn ratio n, and tank characteristic impedance Ro. Also included in Chapter 5 is detailed explanation of the analytical results and suggestions for design strategies which produce SRC's which operate with maximum efficiency.

CHAPTER 2

ABOVE-RESONANCE CONVERTER OPERATION

The topology of the series resonant converter (SRC) considered here is shown in Figure 2.1(a). The SRC, a type of dc-to-dc converter, produces a dc output voltage Vo across the load resistance R_{-} . Input power is provided by the two equal-valued input voltage sources V_{01} and V_{02} . The converter is composed of two switching transistors Q_1 and Q_{e} with corresponding anti-parallel diodes D_{1} and D_{e} , a series inductance L and capacitance C that compose the L-C resonant tank circuit, an ideal two-winding transformer, a rectifying diode bridge $DB_1 - DB_2$, an output filter capacitor C_{Θ} , and a load resistance R_L. In fabricating the SRC, the two separate voltage sources Voi and Voe are derived from a single voltage source V_{IN} by using a pair of capacitors C_{IN} as a voltage divider as seen in Figure 2.1(b). Square-wave voltage excitation of the L-C tank circuit is created by switching transistors Q_1 and Q_2 with a 50% duty cycle to produce ac currents in the L-C resonant tank circuit. The L-C tank current $i_{\mathbf{x}}$ is transformed and rectified to create the desired dc output current $I_{\mathbf{o}}$. The output filter capacitor Co provides the filtering necessary to provide an output voltage which is essentially purely dc.

Assuming the SRC components to be ideal or lossless,

the values of the dc output voltage V_{0} and the output current I_{0} are dependent on the input voltage V_{0} , where

$$V_{\odot} = V_{\odot 1} = V_{\odot 2} \qquad (2.1),$$

the natural resonant frequency fo of the L-C tank circuit, where

$$f_o = 1/[2\pi(LC)^{*/2}]$$
 (2.2),

the switching frequency f_{s} of the transistors, the characteristic impedance R_{o} of the tank circuit, where

$$R_0 = (L/C)^{1/2}$$
 (2.3),

the transformer turn ratio n defined by the number of primary turns N_P and the number of secondary turns N_P as

 $n = N_{\rm H}/N_{\rm H}$ (2.4),

and the load resistance R_{L} .

By defining the normalized voltage conversion ratio M and the normalized output current J as,

$$M = V_{o}/nV_{o} \qquad (2.5)[5],$$

where M < 1, and

$$J = nR_{o}I_{o}/V_{o} \qquad (2.6)[5],$$

many expressions describing SRC operation can be generalized.

When the L-C tank circuit is excited by a square-wave voltage with a switching frequency f_{B} which is higher than the natural resonant frequency fo of the L-C tank, the sequence of events for steady-state operation is:

(a) Initially, the tank current i_x is negative. Transistor Q_1 is ON and Q_m is off. Because i_x is negative, diode D_1 is ON and V_{G1} is connected through diode D_1 to the series L-C circuit producing the circuit topology shown in Figure 2.2(a). The voltage across the series L-C circuit V_T is

$$V_{\tau} = V_{\sigma} + V_{\sigma}/n \qquad (2.7),$$

During this period, the tank current i_x is flowing from the series L-C circuit back into the voltage source V_{001} . At a time defined as T_A , the sinusoidal current in the series L-C circuit reaches an instantaneous value of zero.

(b) Between time T_A and $T_B/2$, the tank current is positive and transistor Q_1 is ON. Thus, V_{O1} is connected to the series L-C circuit, the circuit configuration is shown in Figure 2.2(b). The positive tank current i_X conducts through the switching transistor Q_1 and rectifying diode bridge diodes DB₁ and DB₂. The voltage across the the L-C tank V_T is,

$$V_{T} = V_{0} - V_{0}/n$$
 (2.8).

Current is flowing from the voltage source $V_{{\scriptstyle {\bf 0}\, 1}}$ over this interval.

(c) To begin the second half of the switching period, transistor Q_1 is turned OFF forcing the continuous tank current, which is positive, to commutate diode D_1 ON. The voltage source V_{OE} is connected to the tank circuit through D_1 . The circuit topology during this interval is shown in Figure 2.2(c). The voltage across the L-C tank V_T is,

$$V_{T} = -V_{O} - V_{O}/n$$
 (2.9).

In this interval, the tank current i_x flows through antiparallel diode D_m and bridge diodes DB_1 and DB_{30} and is half-wave symmetrical to the current previously conducted

in diode D_1 . Current is being supplied to $V_{\odot E}$. Eventually, as in the case of current conduction in diode D_1 during the preceding half cycle, i_X reaches an instantaneous value of zero.

(d) In the final interval of the switching cycle, i_{x} is negative while Q_{1} is ON. The equivalent circuit during this interval is seen in Figure 2.2(d). Current is flowing through Q_{\pm} and DB_± and DB₄. The current supplied by V_{0±} to the series L-C circuit and is half-wave symmetrical to the current conducted in Q_{1} in the previous half cycle. The voltage V_T is,

$$V_{\tau} = -V_{\sigma} + V_{\sigma}/n$$
 (2.10).

This interval ends when Q_{e} is turned OFF. When Q_{e} is turned OFF, the current in the resonant tank is negative and is equal to the value used in the beginning of the analysis (i.e. (a)).

The switching sequence briefly presented above results in two possible waveforms for the L-C tank current i_x depending on circuit parameters. The two possibilities are shown in Figure 2.3. In either case, the anti-parallel diode always conducts current before its respective switching transistor [4]. Thus, the conduction sequence

for above resonance excitation over half a switching period is D_1 , Q_1 , or D_2 , Q_2 . By sectionalizing the waveform according to the conducting switching device for the corresponding segment (i.e., Q_1 , Q_2 , D_1 , or D_2), the current waveform can be described as piecewise sinusoidal.

For a given output voltage V_{\odot} , the expression for the L-C tank current i_x waveform is a function of V_{\odot} , M, J, R_☉, f_☉, and f_☉. In preparation for expressing the tank current i_x as a function of these arguments, they are now defined. The angular resonant frequency w_☉ is defined as

$$w_{D} = 2\pi f_{D} = (LC)^{-1/2}$$
 (2.11),

and the ON-time of the anti-parallel diode T_A is defined as

 $T_{A} = (1/w_{D}) \operatorname{arccos[(1 - M^{e} - KM^{e})/(MK + M + 1)]}$ (2.12)[6].

Also requiring definition are the switching period T_{a} defined as,

 $T_{e} = 1/f_{e}$ (2.13),

and circuit parameter K, which is

Each segment of the current waveform can be expressed as a sinusoidal function with a frequency equal to the angular resonant frequency (w_D) of the L-C tank circuit over a closed interval.

During the time interval when D_1 or Q_1 conduct current (0 < t < $T_{g}/2$), the SRC circuit configuration is shown in Figure 2.2(a) and (b). The expression for the segment of the current waveform characterized by current conduction in the anti-parallel diode D_1 is

> $i_x(t) = (V_B/R_D)[1 + M(K + 1)] \sin[w_D(t - T_A)]$ 0 < t < T_A (2.15)[6],

The expression for the segment of the current waveform characterized by current conduction in the switching transistor Q1 is

> $i_x(t) = (V_{@}/R_{O})[1 + M(K - 1)] sin[w_{O}(t - T_{A})]$ $T_{A} < t < T_{B}/2$ (2.16)[6].

During the second half of the switching period characterized by current conduction in D_{Ξ} and Q_{Ξ} , the SRC

10

(2.14).

circuit configuration is shown in Figure 2.2(c) and (d). The half-wave symmetry of i_x permits utilization of equations (2.15) and (2.16) for the current conduction in D_e and Q_e respectively by changing the sign of the equations.

As stated earlier, the waveform for the L-C tank current i_x has two possible shapes depending on the circuit parameters M and K [6]. The difference between the current waveforms shown in Figure 2.3, is that the peak of the current waveform occurs before the current commutates from the switching transistor to the opposing anti-parallel diode in Figure 2.3(a) or at the instant of commutation as in Figure 2.3(b). The expression determining the value of the peak L-C tank current I_{xF} developed by Vorperian and Cuk states the following conditions, if

$$1 - M - KM = \langle 0$$
 (2.17),

then

$$I_{xP} = (V_{o}/R_{o})(1 - M + MK)$$
 (2.18)[6],

which corresponds to $I_{\times P}$ occurring before current commutation as in Figure 2.3(a).

If however

$$1 - M - KM^{2} > 0$$
 (2.19),

then

$$I_{XP} = (V_{P}/R_{P})[(1 - M^{P})MK(MK + 2)]^{1/P} \qquad (2.20)[6],$$

which corresponds to $I_{x,P}$ occurring at the instant of commutation as in Figure 2.3(b). Determination of the peak tank current is important for the evaluation of component stress as well as peak flux in the resonant inductor L.

The output voltage V_o of the SRC is dependent on the waveform of i_x , the load resistance R_{\perp} and the transformer turn ratio n. The value of the average output current I_o is the average of the reflected and full-wave rectified L-C tank current. In steady-state operation, there can be no average current in the output filter capacitor C_o , thus the average dc output voltage V_o is the product of the average output current I_o and the load resistance R_{\perp} .

In recent technical papers, the normalized voltage conversion ratio M, has been used to describe the SRC operation. Analytical models and transcendental equations used to solve for M have been developed by Vorperian and Cuk[4], and Witulski and Erickson[5]. Graphic representation of the normalized voltage conversion ratio for operation above resonance as a function of the normalized frequency and normalized load resistance R is shown in Figure 2.4 [6].











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Figure 2.2 Circuit Switching Configurations





Figure 2.4 Normalized Voltage Conversion Ratio

CHAPTER 3

DESIGN VARIABLES AND ANALYSIS METHOD

The purpose of this research is to analyze the efficiency of the series resonant converter (SRC) operating above resonance by determining the power losses for each of the circuit components. Losses to be computed include conduction and switching losses of semiconductor devices, losses in the series resonant or tank capacitor C, and the core and winding losses of the series resonant or tank inductor L. Expressions for component losses are developed as functions of the transformer turn ratio n, the characteristic impedance $R_{\rm p}$.

For the analysis of operating efficient of the SRC, the user-specified dependent variables are defined to be the input voltage V_{\odot} , output voltage V_{\odot} , and output current I_{\odot} . Independent design variables are the characteristic impedance R_{\odot} of tank circuit, switching frequency f_{\odot} , and transformer turn ratio n. Aside from operating efficiency which evaluated here, other important design criteria include energy storage in the inductor L and capacitor C and component stress.

Final analysis of converter efficiency requires development of expressions as functions of the independent

design variables for the peak inductor current, rms tank current, instantaneous tank current, and average current through switching transistors and anti-parallel diodes. The most suitable method for examining the domain of the independent variables is the the normalized output-plane model developed by Witulski and Erickson [5]. The normalized output-plane model defines an operating point of the converter to be on the M-versus-J plane. The the M axis represents the normalized voltage conversion ratio which has been defined in (2.5). The Y axis of this plane represents values of the normalized output current J previously defined in (2.6). The normalized output-plane model provides uncomplicated solutions for values of inductance L and capacitance C, component stress, peak currents, and resonant frequency. These values are all necessary for evaluation of component losses.

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Mapping operating points on the M-versus-J plane from the design variables n and R_{\odot} is quite simple. Conversion of the ordered pair of n and R_{\odot} for a particular V_{\odot} , V_{\odot} , and I_{\odot} provides unique paired values of M and J by using equations (2.5) and (2.6).

The normalized frequency is computed from an **iterative solution** of the transcendental equation (3.1) for a particular operating point on the M-versus-J output-

plane.

$$J = (2/\gamma)(1 + [1 + (1 - M^{2})] \times \tan^{2}(\gamma/2)]^{1/2}$$
(3.1)[5].

This normalized switching frequency is related to the switching frequency by

$$\gamma = \pi f_{o}/f_{e} \qquad (3.2).$$

For a particular switching frequency f_{e} , the values of f_{o} , L, and C, can be calculated as

$$f_{\mathbf{D}} = f_{\mathbf{B}} \boldsymbol{\gamma} / \boldsymbol{\pi} \tag{3.3},$$

$$L = R_0 / (2\pi f_0)$$
 (3.4),

and

$$C = 1/(2\pi f_{e}R_{e})$$
 (3.5).

These values are necessary for the evaluation of operating efficiency and the fabrication of an actual SRC because certain expressions concerning component loss cannot be stated solely as functions of $R_{\rm D}$ and n.

Once design variables are known, calculation of

21 component and total power losses for the resonant circuit operating under these particular parameters is possible. These losses are developed in Chapter 4 which follows.

CHAPTER 4 COMPONENT LOSS EXPRESSIONS

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To simplify the analysis and development of expressions for the individual component losses, it is assumed that the circuit waveforms are not significantly affected by component and circuit parasitics. As shown in Chapter 2, the waveforms of the SRC operated above resonance exhibit half-wave symmetry. Based on this symmetry, component power loss can be calculated over either half the switching period.

4.1 SWITCHING TRANSISTOR LOSSES

In the analysis of power losses for switching transistors Q_1 and Q_2 of Figure 2.1, two types of losses are considered. The first type is conduction loss occurring during the ON time of the transistor. The second type of loss considered is transistor switching losses which occur during the transistor's transition between the ON and OFF states. Losses associated with the turning ON of the transistor during the transition between the OFF and ON states are assumed negligible. Justification of this assumption is based on the waveform of i_x . Review of Figure 2.3 shows the natural commutation of the tank current i_x from the anti-parallel diode to its corresponding switching transistor. In this commutation, the diode is turning OFF at zero current and the transistor is turning ON with no collector current.

Due to the half-wave symmetry of i_x , the collector current i_c waveform in each switching transistors is identical. The expression for the conduction loss of both transistors $P_{e.on}$, is the integral of the product of the transistor collector-emitter voltage $v_{ce}(t)$ and the instantaneous current through each transistor $i_x(t)$ over the entire ON time t_{on} multiplied by twice the reciprocal of the switching period. The expression for $P_{e.on}$ is

$$P_{\Theta,ON} = (2/T_{\Theta}) \int_{V_{CE}}^{t} (t) i_{x}(t) dt \qquad (4.1).$$

Reviewing SRC operation in Chapter 2, the limits of equation (2.16) show that each of the switching transistors are in the ON state for only a portion of the switching period. Assuming $v_{ce}(t)$ is time independent when the transistor is ON, the collector-emitter saturation voltage V_{cenar} replaces $v_{ce}(t)$ in (4.1). By substituting Vcesat for $v_{ce}(t)$ in equation (4.1), the new expression for $P_{e.on}$ is

$$P_{\text{P,DN}} = (2/1_{\text{B}}) V_{\text{CEBAT}} \int_{i_{\text{X}}}^{i_{\text{X}}/2} dt \qquad (4.2).$$

$$T_{\text{A}}$$

It is possible to compute $P_{e,oN}$ by integrating (4.2). Since collector current exists only during the ON time, this integration is equivalent to calculating the average switching transistor current I_e , where

$$I_{m} = \frac{T_{s}^{2}}{T_{A}} \int_{A}^{a_{x}(t)dt} (4.3).$$

However, given an operating point on the M-versus-J plane and switching period, a less cumbersome calculation is given.

Adapting the work of Vorperian and Cuk for above resonant excitation [4], the normalized voltage conversion ratio M can be expressed a function of the average switching transistor current $I_{\mathbf{D}}$ and the average antiparallel diode current $I_{\mathbf{D}}$, such that

$$M = (I_{e} - I_{p}) / (I_{e} + I_{p})$$
(4.4),

where $I_{\boldsymbol{\omega}}$ is previously defined in equation (4.3), and

$$I_{D} = (2/T_{B}) \int_{0}^{T_{A_{i_{x}}(t)dt}} (4.5).$$

By adding the integer one to both sides of (4.4), the results are

$$M + 1 = (2I_{p})/(I_{p} + I_{p})$$
(4.6),

Equating the sum of the I_{Θ} and I_{D} to be the average output current I_{Θ} multiplied by the transformer turn ratio n such that

$$\mathbf{I}_{\mathbf{G}} + \mathbf{I}_{\mathbf{D}} = \mathbf{n}\mathbf{I}_{\mathbf{G}} \tag{4.7},$$

and substituting (4.7) into (4.6), results in a new expression for the average switching transistor current,

$$I_{o} = n I_{o} (M + 1) / 2$$
 (4.8).

Substituting the expression for M given in (2.5) into (4.8) provides an expression for I_{ee} as a function of the circuit parameters n, I_{e} , V_{e} , and V_{e} , where

$$I_{e} = (V_{o}/V_{o} + n)I_{o}/2$$
 (4.9).

Since n, I_{\odot} , V_{\odot} , and V_{\odot} are user-defined circuit parameters, the value for I_{\odot} has been determined without integrating equation (4.3). Therefore, $P_{\odot, \odot N}$ is simply

$$P_{0.0N} = V_{CEBAT} I_0 (V_0 / V_0 + n)/2$$
 (4.10).

Calculation of switching losses requires evaluation of

the instantaneous collector current and collector-emitter voltage during the transistor's transition from the ON and OFF state. As stated before, power losses during the turning ON of the transistor are neglected due to the natural commutation of current from the anti-parallel diode to its corresponding transistor. Therefore, only losses associated with turning OFF the transistor will be considered.

The transistor losses are modeled by the transistor turn-OFF characteristics shown in Figure 4.1. Assuming the collector current ic exhibits a linear fall with a the fall time tr, the approximation for the turn-OFF losses $P_{a.TURN-OFF}$ for both transistors is expressed as

$$P_{B,TURN-OFF} = 2V_{G} i_{x}(T_{S}/2) t_{F}$$
 (4.11).

Using equation (2.15) or (2.16), the value for the instantaneous current at the time of transistor turn OFF is easily calculated. All other variables in equation (4.11) are predetermined, thus computation of $P_{a,TURN-OFF}$ is quite simple. Combining the results for the switching and conduction losses provides total component losses for the switching transistors P_a , such that

Po = Po.on + Po.turn-off

(4.12).

4.2 ANTI-PARALLEL DIODE LOSSES

Analysis for the losses in the anti-parallel diodes, D_1 and D_n is similar to the analysis of power losses in the switching transistors; however, because of the relatively rapid turning ON and OFF of the diodes, it is assumed that the switching losses are negligible. Therefore, the only losses for the anti-parallel diodes requiring an expression are the conduction losses ($P_{D,ON}$).

As in the case of the switching transistors, it is assumed that when the diodes are ON, the voltage across the junction of the diode (V_D) is constant. Due to the halfwave symmetry of the L-C tank current i_x , the ON time current waveforms of the two diodes are identical. Therefore, the conduction losses for each of the diodes D_1 and D_E are equal. The conduction losses in both diodes can be expressed as

$$P_{\mathbf{D},\mathbf{DN}} = (2/T_{\mathbf{B}}) \nabla_{\mathbf{D}} \int_{\mathbf{i}_{\mathbf{X}}(t) dt}$$
(4.13)

These limits of integration correspond with the diode conduction interval when the diode current is given by (2.15). Integration of (4.13) is equivalent to calculating the average anti-parallel diode current I_{p} . However, using

28 an analysis similar to the one used for calculating ON-time losses for the switching transistors will produce a simplified result.

From the expression for M in equation (4.4), subtracting the integer one from both sides of (4.4) results in,

$$M - 1 = -2I_{p}/(I_{p} + I_{p})$$
(4.14).

Substituting equation (4.7) into (4.14) and solving for $I_{\mbox{\scriptsize p}}$ results in

$$I_p = nI_p(1 - M)/2$$
 (4.15).

Substituting the expression for M (2.5) into (4.15), the final results for $I_{\mathcal{D}}$ are

$$I_{p} = I_{0}(n - V_{0}/V_{0})/2 \qquad (4.16).$$

Therefore, the expression for conduction losses for both diodes, $P_{D,ON}$ is

$$P_{p,oN} = V_p I_0 (n - V_0 / V_0) / 2$$
 (4.17),

which is in terms of known design and user-defined

parameters. Since the conduction losses are the only losses considered for anti-parallel diodes, the total power loss for the anti-parallel diodes $P_{\mathbf{p}}$ is

$$P_{p} = V_{p} I_{0} (n - V_{0} / V_{0}) / 2 \qquad (4.18).$$

4.3 RECTIFYING BRIDGE DIODE LOSSES

The expression for the loss in the four bridge diodes, $DB_1 - DB_4$, P_{DD} is simplified by assuming losses due to turning ON and turning OFF are negligible due to the unforced commutation between each pair of diodes in the bridge. Another assumption is the ON voltage for each bridge diode V_{DD} is constant. By declaring all bridge diodes to be identical and knowing that the average current through each bridge diode is identical, the power losses in the bridge $P_{DD,ON}$ can be expressed as

$$P_{DB,ON} = 2V_{DB} I_0 \qquad (4.19).$$

Since $P_{DD,ON}$ is the only loss considered for the bridge diodes $DB_1 - DB_4$, the expression for P_{DD} is

$$P_{DB} = 2V_{DB} I_{D}$$
 (4.20).

An interesting observation is the expression for the

rectifying bridge loss P_{DB} is solely dependent on the diode voltage drop (V_{DB}) and the user-defined average output current I_D and is independent of the design variables R_D and n.

4.4 SERIES INDUCTOR LOSSES

Analysis of losses in the inductor P_{\perp} is divided into two sections. The first section is concerned with developing the expression for the inductor winding loss $P_{\perp,w}$. The second section is concerned with developing an expression for the inductor core loss $P_{\perp,c}$ which includes hysteresis loss, residual loss, and eddy current loss. Combining the two expressions results in a single expression for the total power losses in the inductor,

$$P_{L} = P_{L,w} + P_{L,c}$$
 (4.21).

The inductor winding resistive loss is expressed as a function of the winding resistance R_w and the root mean square (rms) value of the series L-C circuit current I_{XRMB} , such that

$$P_{L,w} = I_{xems} = R_w \qquad (4.22).$$

The winding resistance can be expressed as a function of the number of turns on the inductor N_{\perp} , the mean length per turn l_{μ} , the copper resistivity p, the window area of the core A_{μ} , and the fill factor $k_{\mu\mu}$ such that

$$R_{\omega} = N_{\perp} = N_{\perp} = 1_{\omega} \rho / (k_{\omega} A_{\omega}) \qquad (4.23).$$

Solution of equation (3.4) provides the value of the inductor L for a particular set of user-defined variables and design variables n and R_0 . For a specific magnetic core with permeability μ , cross sectional area A_c , and mean path length of the magnetic core l_c , the number of turns on the inductor N_c can be computed as

$$N_{L} = [L]_{C} / (A_{C} \mu)]^{2/2}$$
(4.24).

Now that the expression for the winding resistance has been determined, an expression for I_{xems} is required.

The definition of the rms value of a periodic function f(t) is

$$rms = [(1/(T)) f^{e}(t) dt]^{1/e}$$
 (4.25).

To determine the rms value for i_x , the following integration is required,

$$I_{xRMB} = [(2/T_B) \quad i^{e}_{x}(t) \, dt]^{1/e}$$
 (4.26).

Using the expression for i_x in equations (2.15) and (2.16) and the expression for T_A (2.12), equation (4.26) is converted to

$$I_{XRMS} = (V_{0}/R_{0})((2/T_{0})[\int_{A}^{T_{A}}((1 + MK + M) \sin(w_{0}(t + T_{2}))] = dt + \int_{A}^{T_{A}}((1 + MK - M) \sin(w_{0}(t + T_{A}))] = dt]^{1/2}$$

$$(4.27).$$

Performing the operations prescribed in equation (4.27) results in

$$I_{XRMB} = (V_B/R_D) ((1/T_B) [(1 + MK + M) = (T_A + (1/2w_D) \sin(2w_D(-T_A))) + (1 + MK - M) = (T_B/2 - T_A - 1/(2w_D) \sin(2w_D(T_B/2 - T_A)))] = (4.28).$$

Combining the results of equations (4.23) and (4.28) and substituting into (4.22) provide an expression for the inductor winding losses $P_{L,w}$.

The second type of loss in the inductor L considered is the inductor core loss $P_{L,C}$. Victor E. Legg expressed the total inductor core loss $P_{L,C}$ at low flux densities as an equivalent AC core resistance $R_{\perp,\Box}$ [7]. Legg's equation (4.29) expresses the equivalent resistance $R_{\perp,\Box}$ as the sum of three inductor core loss factors: the hysteresis loss factor $R_{\perp,H}$; the residual loss factor $R_{\perp,R}$; and the eddy current loss factor $R_{\perp,\Xi}$; such that

$$R_{L,C} = R_{L,H} + R_{L,R} + R_{L,E}$$
 (4.27).

The hysteresis loss factor is the product of the core permeability μ , the series inductor value L, the switching frequency f_B, the maximum flux level B_M, and an experimentally-obtained hysteresis loss coefficient a, such that

$$\mathbf{R}_{\perp,\mathbf{H}} = \mathbf{a}\mathbf{B}_{\mathbf{H}}\mathbf{\mu}\mathbf{L}\mathbf{f}_{\mathbf{B}} \tag{4.30}.$$

The residual loss factor $R_{\perp,R}$ is the product of the magnetic core permeability μ , the series inductor value L, switching frequency f_{\pm} and an experimentally-obtained hysteresis residual loss coefficient c, such that

$$R_{L,R} = CFLf_{B} \qquad (4.31).$$

The eddy current loss factor $R_{\perp,E}$ is the product of the magnetic core permeability μ , the series inductor value L, the square of the switching frequency fs, and an

experimentally-obtained eddy current loss coefficient e, such that

$$R_{\text{L},\text{E}} = e \mu L f_{\text{B}}^{\text{E}} \qquad (4.32).$$

As stated earlier, the summation of equations (4.30)through (4.32) provide the value of the equivalent core resistance $R_{-,c}$, which multiplied with the square of the rms value series L-C circuit current results in the expression for inductor core loss, where

$$P_{\text{L},\text{c}} = R_{\text{L},\text{c}} I_{\text{XRMB}}^{\text{e}}$$
(4.33).

The only variable in the expression for $P_{L,C}$ that has not been previously determined is the maximum flux level B_{H} . From electromagnetic theory, the expression for the maximum flux level B_{H} is a function of the core permeability μ , the number of turns on the inductor N_L (4.24), the mean path length of the magnetic core l_{C} , and the peak of the L-C tank current I_{XP} (2.18) or (2.20), where

 $B_{m} = \mu N_{L} I_{xm} / I_{C} \qquad (4.34).$

An expression for the both inductor core and winding

losses, and ultimately an expression for the total inductor loss in terms of known design and circuit parameters has been developed.

4.5 SERIES CAPACITOR LOSSES

The model used to represent the non-idealities of the series capacitor C is shown in Figure (4.2). The model consists of an effective series inductance (ESL), the capacitance C, an effective parallel resistance (EPR) which models the dissipative quality of the charged capacitor, and the effective series resistance (ESR). In the analysis of capacitor power losses, the effects of the ESL and EPR are neglected. The only parasitic element to be considered is the ESR. Therefore the expression for total capacitor losses P_c is

 $P_{c} = I_{xRMB} ESR \qquad (4.35),$

where the value of I_{XRMB} is expressed in equation (4.28) and the value of ESR is determined experimentally.





Figure 4.2 Non-Ideal Capacitor Model

CHAPTER 5

RESULTS AND EVALUATION OF DESIGN METHODS

In the previous chapter, analytical expressions were developed for the determination of individual component losses. The total component loss P_{TOTAL} is the summation of the individual component losses and is expressed as

$$P_{TOTAL} = P_{\Theta} + P_{D} + P_{DB} + P_{L} + P_{C} \qquad (5.1).$$

The expression for operating efficiency η of the series resonant converter (SRC) is

$$\eta = (1 - P_{\text{TOTAL}} / V_{\text{D}} I_{\text{D}}) \times 100\%$$
 (5.2).

In this a chapter, the operating efficiency of a hypothetical SRC circuit is presented as a function of the transformer turn ratio n and the characteristic impedance R_{o} . A brief explanation of results and a presentation of design strategies follows.

5.1 ANALYTICAL RESULTS

In order to use the expressions developed in this thesis to evaluate SRC operating efficiency, certain circuit parameters and user-specified dependent variables must be given. The dependent circuit parameters for the hypothetical SRC circuit are given in Table 5.1.

Using the variables given in Table 5.1, the computer program presented in Appendix A is used to calculate the efficiency utilizing the expressions developed in Chapter 4. Figure 5.1 depicts the three-dimensional plot of the efficiency as function of the ordered pair (n_1,R_0) for values of n between 0.5001 and 0.7758 and values of R_0 between 0.0500 and 6.262.

Figure 5.1 shows that for a particular value of n, there exists a maximum value of efficiency and a corresponding value for the changing characteristic impedance R_0 . Evaluation of the individual component losses will help explain the occurrence of the maximum value of efficiency for the individual value of n. The easiest method of analyzing the three dimensional efficiency plot is to traverse the plot on a constant transformer turn ratio n line analyzing the individual component losses as a function of the characteristic impedance R_0 .

There are several elements of the component losses that are independent of R_0 and stay constant for a particular value of n. The first is the loss in the bridge diodes P_{DP}

which is expressed in equation (4.20) as a function of the output current I_{\odot} and the forward voltage drop of the diode $V_{\odot \odot}$. For this hypothetical SRC circuit, $P_{\odot \odot}$ is 14W, which represents 14% of the 100W output power of the total converter. Other types of losses that are independent of R_{\odot} are the conduction losses in the switching transistor $P_{\odot, \odot N}$ (4.10) and anti-parallel diode $P_{\odot, \odot N}$ (4.17). The summation of the conduction losses in these two components effect the efficiency of the hypothetical SRC are totally dependent on the transformer turn ratio n, but not R_{\odot} .

Although the losses due to Po, TURN-DEF (4.11) and PL.C (4.33) are dependent on R_0 , their effects on efficiency are quite negligible. With an output power of 100W, theses losses, Potturn-off and PL, c are typically 1.5W. However, at extremely high values of R_o and n, these losses become significant. The factor causing the greatest fluctuation in the efficiency is the losses due to the parasitic resistances which include the inductor winding resistance R_{μ} and the effective series resistance (ESR) of the capacitor. At turn ratio n, as the increasing values of characteristic impedance Ro relate to increasing values of inductance L. This increasing inductance produces lower values of Ixems. The increase in inductor value limits the variation of the L-C tank current i_x about its zero average value, consequently reducing the value of Ixema. However,

the reduction in rms current does not necessarily result in a decrease in resistive losses. The value of R_{μ} is increased due to the increase in the number of turns N_ required to produce the value of inductance L specified. The effects of the decreasing I xRMB and increasing resistance R_{\mu} on the resistive losses P_REBT at a particular value of n as a function of R_0 are shown in Figure 5.2. Figure 5.2 shows a distinct operating point where resistive losses are minimized. The shape of the curve in Figure 5.2 shows the direct effects of the value of R_0 on the occurrence of a maximum efficiency point for a particular value of n.

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5.2 DESIGN STRATEGIES AND RECOMMENDATIONS

When designing an SRC for above-resonance excitation, several general rules apply. Operating the SRC with a normalized voltage conversion ratio M close to unity reduces the conduction losses of the switching transistor and anti-parallel diodes when the ON voltage of the diode is significantly greater than the transistor's ON voltage. The input voltage range of the dual voltage sources Voi and Voe in Figure 2.1 determines the value of the transformer turn ratio n required to provide the constant output voltage Vo and output current Io. When maximizing converter efficiency, the value of n is determined from the operating conditions; the value of R_{\odot} is chosen to minimize the losses for that particular value of n. When certain circuit parameters are unknown or cannot be experimentally determined, the value of R_{\odot} should be selected to minimize the resistive power losses since the resistive losses have the strongest effect on optimum efficiency point.

A number of enhancements can be made to future versions of this analysis which may improve the estimation of total power losses of the SRC. A recommendation is to include circuit parasitics in the expressions used in the design method. Inclusion of the voltage drops of the switching devices and bridge diodes in the derivations of the expressions for the current waveforms can perhaps provide more accurate values of normalized voltage conversion ratio M. Defining the output voltage Vo as

$$V_{\rm O} = I_{\rm O}R_{\rm L} \tag{5.3},$$

the adjusted normalized voltage conversion ratio M' which includes ON-time voltage drops, is expressed as

 $M' = (V_0 + 2V_{00})/n[V_0 - qV_0 - (1 - q)V_{0.0N}]$ (5.4),

where q is a weighting factor between 0 and 1/2. Substituting the values of M' from (5.5) for the normalized voltage conversion ratio M in equation (3.1) will result in new values of f_0 , L, and C for a given set of user-defined dependent variables and ordered pair (n,R₀).

Other recommendations include:

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a) the development of additional expressions for the transformer core and winding power losses,

b) the adjustment of the value of circuit inductance L to compensate for the effective series inductance (ESL) of the capacitor,

c) the analysis of the effect of inductor core material and dimensions on SRC efficiency, and

d) the development of an expression for inductor core losses operating at high magnetic flux densities due to the fact that Legg's equation (4.27) is valid in magnetic core applications involving low magnetic flux densities.

5.3 CONCLUSION

A method for analyzing SRC operating efficiency has

been presented. Included in the analysis is the development of expressions relating operating efficiency to the design variables n and R_o, and given circuit parameters. The operating efficiency is graphically represented as a function of the n and R_o for a hypothetical SRC circuit followed by a brief explanation of the results and possible enhancements to the proposed design method.

Table 5.1 User-Defined Dependent Variables

<u>Circuit Dependent Variables</u> $V_{B} = 20V$ $V_{D} = 10V$ $I_{D} = 10A$ $f_{B} = 50 \text{ kHz}$

Transistor Specifications

 $V_{CESAT} = 0.2V$ $t_{\tau} = 50 \times 10^{-7} \text{ sec}$

Diode Specifications

 $V_{\mathbf{D}} = V_{\mathbf{DB}} = 0.7V$

Inductor Core Specifications

 $\mu_{R} = 26 \quad vol = 22.69 \times 10^{-6} \text{ m}^{3} \qquad A_{C} = 0.1990 \times 10^{-3} \text{ m}^{2}$ $l_{C} = .1074 \text{ m} \qquad l_{W} = 0.0622 \text{ m} \qquad A_{W} = 0.426 \times 10^{-3} \text{ m}^{2}$ $k_{W} = 0.2 \quad a = 4.0 \times 10^{-6} \quad c = 96 \times 10^{-6} \quad e = 7.0 \times 10^{-7}$

Capacitor Specifications

ESR = 0.1 ohms



LIST OF REFERENCES

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Appendix A: Fortran Program Code

States-

	•				
υυυ	FRANCIS A FAHY FORTRAN PROGRAM COM FOR SERIES RESONANT PROGRAM LOSSES INTEGER II, III, IV, I REAL*4 PI, VG, FO, ROM *M, F1, VQ, VD, PDB, PQ, P *N1, N, FS, TF, Z, ILP, PE *RHO, PTOTAL, PCORE, PR OPEN (UNIT = 6, FILE	PUTING LOSSES CONVERTER IV, A, IIIV, AA EGA, L, C, TS, GAMD D, PCOND, K1, K2, J RM, VCP, VOL, TA, J EST, CSR, LPT, RAG = 'B: MISCP, OU'	MA, K, I, J, RO, I IRMS, IOFF, PT BMAX, PERMMAX C, EFFIC, SRMS, I', STATUS =	LEN, AREA. JRNOFF, .UR. B, .AVIN, KVIN 'NEV')	
c	OPEN(UNIT = 8. FILE OPEN(UNIT = 9. FILE	= 'B: 1LP. OUT' = 'B: 1RMS. OUT'	STATUS = 1 STATUS = 1	.NEM.) NEM.)	
00000	The following const for the calculation All parameter value	ants are design of losses in 1 s labeled in ND	n parameters the series ro (S.	required esonant conve	erter.
	V is the ouput volt on-state voltage dr switching frequency permeability of the BMAX is the maximum LEN is path length core, RHO is the r CSR is the capacito turn length, KWIN is	age, VG is the op, VD is the o core, VOL is t allowable fluc of the core, AD esistivity of t r series resist s the fill fact	input voltag iode on-sta it voltage, U the volume of ctuation of f REA is the cr the transform tances, LPT tor, and AVII	ge, VQ is the te voltage dr JR is the rel f the core, the flux dens ross sectiona mer windings is the core I is the core	e transistor op, FS is th ative il area of th for Cu, winding e window area
с с с	GAMMA, the normalize	ed switching fr	equency, is	intialized a	t 1 x 10-5.
101	VRITE(7,101) FORMAT(' N WRITE(8,102)	RO	EFFICIENCY	·	
102	FORMAT(' N	RO	ILP	FCORE'>	
103	FORMAT(' N	RO	N 1	IRMS	PREST)
104	WRITE(6,104) FORMAT(' N V = 10.00 TF = 50E-9 VG = 20.00 VQ = 0.2 VD = 0.7 FS = 50E3 I = 10.00 UR = 26 VOL = 22.69E-06 BMAX = 0.20 LEN = 0.1074 AREA = 0.1990E-03 RHO = 1.75E-08 CSR = 0.1 LPT = 0.0622 AVIN = 4.26E-04 KWIN = 2.0E-01	RO	PCOND	PTURNOFF')	

PI = 3.14159 N = 5.001E+01 RO = 5E-02c č M = V/(N + VG)' J = RO * (N * I)/VG С c c SOLVE FOR GAMMA AS A FUNCTION OF M AND J c GAMMA ≈ .00001 IF (M. EQ. 1.0) GO TO 5 DO 30 II = 1, 3 GAMMA = GAMMA + 1E0 CALL F(M, GAMMA, J, F1) IF (F1 . EQ. 0) GO TO 4 IF (F1 .GT. 0) GO TO 1 30 CONTINUE GAMMA = 3.2DO 40 111 = 1.101 GAMMA = GAMMA - 1E-1 CALL F(M, GAMMA, J, F1) IF (F1 .EQ. 0) GO TO 4 IF (F1 .LT. 0) GO TO 2 CONTINUE 40 2 DO 50 IV = 1,10GAMMA = GAMMA + 1E-2 CALL F(M, GAMMA, J, F1) IF (F1 .EQ. 0) GO TO 4 IF (F1 .GT. 0) GO TO 3 50 CONTINUE DO 60 IIV = 1,103 GAMMA = GAMMA - 1E-3 CALL F(M, GAMMA, J, F1) IF (F1 .EQ. 0) GD TO 4 IF (F1 .LT. 0) GO TO 6 60 CONTINUE DO 70 IIIV = 1, 10 GAMMA = GAMMA + 1E-46 CALL F(M, GAMMA, J, F1) IF (F1 .GE. 0) GO TO 4 CONTINUE 70 5 GAMMA = PI FO = GAMMA * FS / FI 4 С c c SOLVE FOR COMPONENT SIZE AND INDUCTOR TURNS NI ċ с PERM = UR * 1260E-09 L = RO / (2E0 * PI * FO)C = 1/(2E0 * PI * FO * RO)

```
K = J * GAMMA/(2E0 * M)
      N1 = SQRT(L * LEN / (AREA * PERM))
с
č
      TS = 1 / FS
      ROMEGA = 2E0 * PI * FO
с
с
С
      COMPUTE TRANSISTOR TURNOFF LOSSES
  .
с
      IOFF = ROMEGA * C * VG * SQRT((1 - M * M) * M * K * (M * K + 2E0))
      PTURNOFF = (2E0 * VG) * IOFF * TF / TS
с
č
      COMPUTE PEAK CURRENT AND PEAK CAPACITOR VOLTAGE
С
      Z = 1 - N - (M * N) * K
IF (Z .LE. OEO) THEN
ILP = ROMEGA * C * VG * (1 - M + M * K)
      ELSE
        ILP = IOFF
      END IF
С
      VCP = VG * M * K
C
c
      COMPUTE MAXIMUM CORE PERMEABILITY
С
      PERMMAX = VOL * BMAX * BMAX/(L * ILP * ILP)
      IF (PERMMAX .LT. PERM) THEN
      EFFIC = 0
      GO TO 160
      ELSE
        GO TO 55
      END IF
С
      COMPUTE FLUX DENSITY (B)
С
С
  55 B = PERM * N1 * ILP/LEN
С
с
      COMPUTE CONDUCTION LOSSES IN SWITCHING DEVICES AND BRIDGE
¢
      IAVEOUT IS AVERAGE OUTPUT CURRENT
с
č
      PDB = 2E0 * VD * I
PQ = 1 * VQ * (1 + M) * N / 2E0
PD = 1 * VD * (1 - M) * N / 2E0
      PCOND = PDB + PQ + PD
С
      COMPUTE RMS CURRENT IRMS
С
с
      TA = (1/ROMEGA) + ACOS((1 + M + (1 + M + K))/(M + (K + 1) + 1))
С
      K1 = ROMEGA * C * VG * (1 + M * (K + 1))
```

```
*ROMEGA * (TE BED - TA -) / (4ED * ROMEGA -) ->
       IRMS = SQRI(SIRME)
С
С
       COMPUTE CORE LOSSES
С
       RAC = (7.0E-09 * FS * FS + 96E-06 * FS + 4.0E-06 * E * FS * 1E04)
      ** UR * L
       PCORE = RAC * IRMS * IRMS
¢
C D
       COMPUTE RESISTIVE LOSSES (PREST)
       PREST = (N1 * N1 * LPT * RHO/(AWIN * KWIN) + CSE) * IRMS * IRMS
c
c
       COMPUTE TOTAL POWER LOSSES
č
       FTOTAL = PCOND + PCORE + PREST + PTURNOFF
c
       COMPUTE EFFICIENCY
С
       EFFIC = (1 - PTOTAL/(V * 1)) * 100
       IF (EFFIC . LT. DEO) THEN
        \begin{array}{l} \text{EFFIC} = 0 \\ \text{GO TO } 160 \end{array} 
       END IF
С
с
с
       PRINT OUT VALUES
        WRITE(8,621) N. RO, ILP, PCORE
        WRITE (6, 621) N, RO, PCOND, PTURNOFF
        FORMAT (4 (E12.6, 1X))
 621
        WRITE(9,622) N.RO, N1, IRMS, PREST
        FORMAT (5 (E12.6, 1X))
 622
        WRITE (7,620) N.RO, EFFIC
FORMAT (3 (E12.6,1X))
 160
 620
        RO = RO * 1.05
 151
        CONTINUE
 150
        N = N * 1.05
RO = 5E-02
 111
 100 CONTINUE
       CLOSE (UNIT = 6)
       CLOSE (UNIT = 7)
       CLOSE (UNIT = 8)
       CLOSE (UNIT = 9)
       STOP
      END
С
С
       DEFINE SUBROUTINE TO SOLVE FOR GAMMA FROM
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       TRANSCENDENTAL EQUATION FOR M AND J
      SUBROUTINE F(XX, YY, ZZ, F1)
       DOUBLE PRECISION X, Y, Z, DIFF, AA, BB, CC
       REAL*4 F1, XX, YY, ZZ
      X = DBLE(XX)
       Y = DELECTI
       Z = DELE(ZZ)
       AA = Y/2D0
```

1933 Coloring

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BE = DTAN(AA) * DTAN(AA) CC = Z * AA DIFF = BE - ((X * X) * BE + (Z * Y) + (CC * CC)) IF (DIFF .LT. ODO) F1 = -1 IF (DIFF .EQ. ODO) F1 = 0 IF (DIFF .GT. ODO) F1 = 1 RETURN END

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