

2.5 1.8 

SALLARREAGE ASSAULT STATER MATTER AND STATES STATES STATES STATES STATES STATES AND STATES AND STATES AND STATES



AD-A193

San Diego, California 92152

# MARINE PHYSICAL LABORATORY

SCRIPPS INSTITUTION OF OCEANOGRAPHY

# ITERATIVE METHOD FOR THE ESTIMATION OF SHOT AND SEA FLOOR DEPTHS USING HYDROPHONE STREAMER DATA

Richard K. Brienzo



## MPL TECHNICAL MEMORANDUM 398

MPL-U-57/87

Approved for public release; distribution unlimited. January 1988

SECURITY	CLASSIFIC	ATION OF	THIS PAGE	

#### ----DOCUMENTATION DACE

1a. REPORT SECURITY CLASSIFICATION UNCLASSIFIED	16 RESTRICTIVE MARKINGS					
2a. SECURITY CLASSIFICATION AUTHORITY	3. DISTRIBUTION / AVAILABILITY OF REPORT					
26. DECLASSIFICATION / DOWNGRADING SCHEDULE	Approved for public release; distribution unlimited.					
4. PERFORMING ORGANIZATION REPORT NUMBER(S)	5. MONITORING ORGANIZATION REPORT NUMBER(S)					
MPL Technical Memorandum 398 [MPL-U-57/87]						
6a. NAME OF PERFORMING ORGANIZATION 6b. OFFICE SYMBOL (If applicable)	7a. NAME OF MONITORING ORGANIZATION					
Marine Physical Laboratory MPL	Department of the Navy					
6c. ADDRESS (City, State, and ZIP Code) University of California, San Diego Scripps Institution of Oceanography San Diego, CA 92152	7b. ADDRESS (City, State, and ZIP Code) 800 North Quincy Street Arlington, VA 22217-5000					
8a. NAME OF FUNDING / SPONSORING 8b. OFFICE SYMBOL	9. PROCUREMENT INSTRUMENT IDENTIFICATION NUMBER					
Office of Naval Research ONR	N00014-87-K-0010					
Bc. ADDRESS (City, State, and ZIP Code)	10. SOURCE OF FUNDING NUMBERS					
Department of the Navy 800 North Quincy Street	PROGRAM PROJECT TASK WORK UNIT					
Arlington, VA 22217-5000	ACCESSION NO.					
11. TITLE (Include Security Classification) Iterative Method for the Estimation of Shot and Sea Floor Depths Using Hydrophone Streamer Data						
12 PERSONAL AUTHOR(S) Richard K. Brienzo						
13a. TYPE OF REPORT     13b. TIME COVERED     14. DATE OF REPORT (Year, Month, Day)     15 PAGE COUNT       tech memo     FROM     TO     .Tanuary 1988     17						
15. SUPPLEMENTARY NOTATION						
17. COSATI CODES 18. SUBJECT TERMS	(Continue on reverse if necessary and identify by block number)					
FIELD GROUP SUB-GROUP marine re sea floor	marine refraction, streamer hydrophone, shot depth, sea floor depth					
19. ABSTRACT (Continue on reverse if necessary and identify by block	number)					
When explosive charges are used as sound sources in marine refraction experiments, a streamer hydrophone is often trailed near the surface by the vessel which launches the charges. The output of the streamer hydrophone is used to monitor the detonations, and after correcting for the time spent in traveling from the shot to the streamer hydrophone, provides a time origin for each shot. If three arrivals are present (the direct water path and two reflections), then information about the shot depth and sea floor depth may also be obtained.						
Since the ship that launches the charges generally steams away from the drop site, incorrect results are obtained if vertical raypaths are assumed. In this report, a method which does not assume vertical ray,						
paths is derived to find shot and sea floor depths. Inputs are the distance traveled from the drop site when the						
detonation first appears on the streamer hydrophone output, and the time differences between the three						
obtained during a refraction experiment conducted on the Monterey Deep-Sea Fan.						
20 DISTRIBUTION ( AVAILABILITY OF ABSTRACT 21 ABSTRACT SECURITY CLASSIFICATION						
22a NAME OF RESPONSIBLE INDIVIDUAL	RS INCLASSIFIED					
W. S. Hodgkiss	22b TELEPHONE (Include Area Code) 22c. OFFICE SYMBOL 619-534-1798					
W. S. Hodgkiss DD FORM 1473, 34 MAR 83 APR edition may be used	AS         UNCLASSIFIED           22b         TELEPHONE (Include Area Code)         22c. OFFICE SYMBOL           619-534-1798         MPT,           until exhausted         SECURITY CLASSIFICATION OF THIS BACE					

& U.S. Government Printing Office: 1986-607-044

. . .

and the second

..

### Table of Contents

Abstract	iii
1. Introduction	1
2. Derivation	4
3. Algorithm	12
4. Example	14
Appendix: Fortran-77 program	16



Page

2222

25232

53335.24

......

INSPECTED

# Iterative method for the estimation of shot and sea floor depths using hydrophone streamer data

Richard K. Brienzo

Marine Physical Laboratory Scripps Institution of Oceanography University of California, San Diego San Diego, CA. 92152

### ABSTRACT

When explosive charges are used as sound sources in marine refraction experiments, a streamer hydrophone is often trailed near the surface by the vessel which launches the charges. The output of the streamer hydrophone is used to monitor the detonations, and after correcting for the time spent in traveling from the shot to the streamer hydrophone, provides a time origin for each shot. If three arrivals are present (the direct water path and two reflections), then information about the shot depth and sea floor depth may also be obtained.

Since the ship that launches the charges generally steams away from the drop site, incorrect results are obtained if vertical raypaths are assumed. In this report, a method which does not assume vertical raypaths is derived to find shot and sea floor depths. Inputs are the distance traveled from the drop site when the detonation first appears on the streamer hydrophone output, and the time differences between the three arrivals. A Fortran-77 program which implements the method is listed and its use is illustrated on data obtained during a refraction experiment conducted on the Monterey Deep-Sea Fan.

# Iterative method for the estimation of shot and sea floor depths using hydrophone streamer data

### 1. Introduction

Marine refraction experiments are conducted using an impulsive airgun or explosive charges as a sound source. A typical experiment (Figure 1) might have one vessel utilized as a receiving station with a hydrophone, or a hydrophone array, deployed in the water column. A second vessel (called the shooting ship) steams away from the receiving ship and drops explosive charges into the water. Acoustic energy travels along numerous paths in going from the shot to the array. Since there is a general increase in sound speed with depth in the sediment, much of the energy that enters the sediment is refracted back into the water column and received at the array. Analysis of this received data yields information about the velocity and attenuation structure in the sediment.

When explosive charges are used, a hydrophone (called a streamer hydrophone) is often trailed near the surface by the shooting ship while charges are being launched. Streamer hydrophones are used during marine refraction experiments to monitor the detonations. Output from the streamer hydrophone is telemetered to the receiving ship via a radio voice channel and recorded along with data from the array. Streamer hydrophone output indicates when the shot detonates, and after correcting for the time spent in traveling from the shot to the streamer hydrophone, provides a time origin for each shot. Additionally, if three arrivals can be seen on the streamer hydrophone output, estimates of the shot and sea floor depths may be obtained.

An example of this type of data is given in Figure 2. The top nine time series are the array data and the bottom time series is the output of the streamer hydrophone. In the streamer data, the pulse at 0.32 seconds is the arrival which travels from the shot directly to the streamer hydrophone. The second arrival (at 1.51 seconds) is a bottom reflection, and the third arrival (at 3.69 seconds) is a surface reflection - bottom reflection. Energy appears at the array approximately 14.7 seconds after it arrives at the streamer hydrophone.

Ray paths corresponding to the arrivals on the streamer channel are illustrated in Figure 3(a). The first arrival is denoted (D), the second arrival (B), and the third (SB). The shooting ship moves a horizontal distance x from the drop site. The water column is modeled as a two layer medium. Layer boundaries are specified by the surface, shot depth  $(d_1)$ , and sea floor depth  $(d_1 + d_2)$ . Each layer is assumed to have a constant sound speed  $(v_1 \text{ and } v_2)$ . This is not a very good model of a velocity profile for the water column, but if mean values for each layer are found from the velocity profile, the method gives satisfactory results.



#### Figure 1. Refraction experiment.

ALTERNA REPORT STORAGE ALTER SOUTHER WATER

A hydrophone array is deployed at mid-depth in the water column. The shooting ship steams away from the array and drops explosive charges into the water. There is a general increase in sound speed with depth in the sediment, so much of the acoustic energy that enters the sediment is refracted back into the water column. Analysis of this data yields information about velocity and attenuation in the sediment.


Figure 2. Hydrophone array and streamer data.

ľ

The top 9 time series are array data, bottom time series is the output of the streamer hydrophone. Three arrivals are present on the streamer channel (at .32, 1.51, and 3.69 seconds). Energy appears at the array approximately 14.7 seconds after the first arrival at the streamer hydrophone.

If the angles in Figure 3(a) are small (i.e. the ship does not travel very far from the drop site), then the raypaths are almost vertical, and the time difference between the second and third arrivals  $(\Delta t_{2,3})$  is due to the extra distance that the (SB) ray travels in layer 1. In this case the third (SB) arrival reaches the hydrophone  $2t_0$  seconds after the second (B) arrival (see Figure 3(b)). From this, the depth of the first layer is given by

$$d_1 = \frac{1}{2} \Delta t_{2,3} v_1$$

where  $\Delta t_{2,3}$  is the time difference between the second (B) and third (SB) arrivals, and  $v_1$  is the velocity in layer 1.

The depth of the second layer is found from the time differences between the direct (D) and bottom reflected (B) paths. If the angles are small, then  $t_1$  and  $(t_2 - t_3)$  are approximately the same, and it takes the bottom reflected path  $2t_3$  seconds longer to reach the hydrophone. The depth of the second layer is then given by

$$d_2 = \frac{1}{2} \Delta t_{1,2} v_2$$

where  $\Delta t_{1,2}$  is the time different between the direct (D) and second (B) arrivals, and  $v_2$  is the velocity in layer 2.

In general, the horizontal distance x will not be zero (it is not in the best interest of the ship's crew to remain over the site where an explosive charge has been dropped). This method will give incorrect depths for nonzero distances x since the raypaths are not vertical.

#### Non-zero ranges

When the distance x is not zero, it is necessary to correct for the difference between the vertical distances  $d_1$  and  $d_2$  and the actual length of the raypaths. Since the depths  $d_1$  and  $d_2$  are unknown, the angles  $\alpha_1$  and  $\alpha_2$  are also unknown. The strategy will be to initially use the values  $\hat{d}_1$  and  $\hat{d}_2$  found by assuming vertical ray paths. Then, given x, corresponding angles  $\alpha_1$  and  $\alpha_2$  may be found. These angles are then used to include the effect of non-vertical ray paths in the calculation of depths  $d_1$  and  $d_2$ . Since  $\hat{d}_1$  and  $\hat{d}_2$  are not exact,  $\alpha_1$  and  $\alpha_2$  are not exact, and the calculated  $d_1$  and  $d_2$  will not be correct, but will be closer to the correct values than  $\hat{d}_1$  and  $\hat{d}_2$  to obtain successively closer values to the correct depths.







5

activities and accesses in presented in success in properties of the second presented in ASSESSED RADIADA 7

Relations for finding  $\alpha_1$  and  $\alpha_2$  from  $d_1$  and  $d_2$  are derived from the geometry of the ray paths. From Figure 4(a),

$$\tan(\alpha_1) = \frac{x}{d_1 + 2d_2} \qquad \alpha_1 = \arctan\left(\frac{x}{d_1 + 2d_2}\right) \qquad (1)$$

From Figure 4(b),

$$\tan(\alpha_2) = \frac{x_1}{d_1}$$
 and  $\tan(\alpha_2) = \frac{1/2x_2}{(d_1 + d_2)}$  (2)

Equating these last two expressions and solving for  $x_2$  gives

$$\frac{x_1}{d_1} = \frac{1/2x_2}{(d_1 + d_2)}$$

$$x_2 = \frac{2(d_1 + d_2)x_1}{d_1}$$

The total distance is  $x = x_1 + x_2$ . Using this to find  $x_1$  gives

 $x_1 = x - x_2$ 

$$x_1 = x - \frac{2(d_1 + d_2)x_1}{d_1}$$

$$x = x_1 \left[ 1 + \frac{2(d_1 + d_2)}{d_1} \right]$$

$$x_{1} = \frac{x}{\left[1 + \frac{2(d_{1} + d_{2})}{d_{1}}\right]}$$

From this and equation (2),

$$\tan(\alpha_2) = \frac{x_1}{d_1} = \frac{x}{d_1 \left[1 + \frac{2(d_1 + d_2)}{d_1}\right]} = \frac{x}{(3d_1 + 2d_2)}$$



Figure 4.

Therefore,

$$\alpha_2 = \arctan\left(\frac{x}{3d_1 + 2d_2}\right) \tag{3}$$

These equations (summarized below) give the angles  $\alpha_1$  and  $\alpha_2$  in terms of the depths  $d_1$  and  $d_2$ 

$$\alpha_1 = \arctan\left(\frac{x}{d_1 + 2d_2}\right) \tag{4a}$$

$$\alpha_2 = \arctan\left(\frac{x}{3d_1 + 2d_2}\right) \tag{4b}$$

Estimated depths (assuming vertical raypaths)  $\hat{d}_1$  and  $\hat{d}_2$  may be substituted into (4) to obtain estimates of the angles  $\alpha_1$  and  $\alpha_2$ . These angles  $\ldots$  then be used along with the time delays to find depths  $d_1$  and  $d_2$ . Since these depths are now calculated using non-vertical ray paths, they will be closer to the correct shot and seafloor depths. Expressions for  $d_1$  and  $d_2$  in terms of  $\alpha_1$ ,  $\alpha_2$ , and the time delays are derived next.

From Figure 5, the time difference between the third and second arrivals is

$$\Delta t_{2,3} = (2t_0 + 2t_3 + t_4) - (2t_1 + t_2)$$

$$= \left(\frac{2d_1}{v_1\cos(\alpha_2)} + \frac{2d_2}{v_2\cos(\alpha_2)} + \frac{d_1}{v_1\cos(\alpha_2)}\right) - \left(\frac{2d_2}{v_2\cos(\alpha_1)} + \frac{d_1}{v_1\cos(\alpha_1)}\right)$$

$$= \left(\frac{3}{\cos(\alpha_2)} - \frac{1}{\cos(\alpha_1)}\right) \frac{d_1}{v_1} + \left(\frac{2}{\cos(\alpha_2)} - \frac{2}{\cos(\alpha_1)}\right) \frac{d_2}{v_2}$$

 $\alpha_1$  and  $\alpha_2$  are known (from equations (4a) and (4b)), so define the constants

$$k_1 = \frac{3}{\cos(\alpha_2)} - \frac{1}{\cos(\alpha_1)}$$

$$k_2 = \frac{2}{\cos(\alpha_2)} - \frac{2}{\cos(\alpha_1)}$$

then  $\Delta t_{2,3}$  may be written as

للمشايطين

لدينيذ

$$\Delta t_{2,3} = \frac{k_1}{\nu_1} d_1 + \frac{k_2}{\nu_2} d_2 \tag{5}$$

The difference between the second and first arrivals is (Figure 5)

$$\Delta t_{1,2} = (2t_1 + t_2) - t_D$$

$$= \left(\frac{2d_2}{v_2\cos(\alpha_1)} + \frac{d_1}{v_1\cos(\alpha_1)}\right) - \frac{1}{v_1}\sqrt{d_1^2 + x^2}$$

$$= \left(\frac{2d_2}{v_2} + \frac{d_1}{v_1}\right) \frac{1}{\cos(\alpha_1)} - \frac{1}{v_1} \sqrt{d_1^2 + x^2}$$
(6)

Solving (5) for  $d_1$  gives

$$d_1 = \frac{v_1}{k_1} \Delta t_{23} - \frac{k_2}{k_1} \frac{v_1}{v_2} d_2 \tag{7}$$

The expression in (7) may be used in (6) for the  $d_1$  enclosed in parentheses ( $d_1$  under the radical will be replaced later)

$$\Delta t_{1,2} = \frac{1}{\cos(\alpha_1)} \left[ \frac{2d_2}{v_2} + \frac{1}{v_1} \left( \frac{v_1}{k_1} \Delta t_{2,3} - \frac{k_2}{k_1} \frac{v_1}{v_2} d_2 \right) \right] - \frac{1}{v_1} \sqrt{d_1^2 + x^2}$$

$$= \frac{1}{\cos(\alpha_1)} \left[ \frac{2d_2}{v_2} + \frac{\Delta t_{2,3}}{k_1} - \frac{k_2}{k_1} \frac{d_2}{v_2} \right] - \frac{1}{v_1} \sqrt{d_1^2 + x^2}$$

$$= d_2 \left( \frac{2}{v_2 \cos(\alpha_1)} - \frac{k_2}{k_1 v_2 \cos(\alpha_1)} \right) + \frac{\Delta t_{2,3}}{k_1 \cos(\alpha_1)} - \frac{1}{v_1} \sqrt{d_1^2 + x^2}$$

$$\sqrt{d_1^2 + x^2} = \left( \frac{2v_1}{v_2 \cos(\alpha_1)} - \frac{k_2v_1}{k_1 v_2 \cos(\alpha_1)} \right) d_2 + \left( \frac{v_1 \Delta t_{2,3}}{k_1 \cos(\alpha_1)} - v_1 \Delta t_{1,2} \right)$$
(8)

To simplify the above expression, define

$$c_1 = \frac{2v_1}{v_2\cos(\alpha_1)} - \frac{k_2v_1}{k_1v_2\cos(\alpha_1)}$$



Figure 5.

$$c_{2} = \frac{v_{1} \Delta t_{2,3}}{k_{1} \cos(\alpha_{1})} - v_{1} \Delta t_{1,2}$$

and (8) may be written as

$$\sqrt{d_1^2 + x^2} = c_1 d_2 + c_2 \tag{9}$$

Next, substitute the expression for  $d_1$  from (7) into (9) and square both sides.

$$\left(\frac{v_1}{k_1}\Delta t_{2,3} - \frac{k_2}{k_1}\frac{v_1}{v_2}d_2\right)^2 + x^2 = c_1^2 d_2^2 + 2c_1c_2d_2 + c_2^2$$

$$\left(\frac{v_1 \Delta t_{2,3}}{k_1}\right)^2 - \frac{2v_1^2 k_2 \Delta t_{2,3}}{k_1^2 v_2} d_2 + \left(\frac{k_2 v_1}{k_1 v_2}\right)^2 d_2^2 + x^2 = c_1^2 d_2^2 + 2c_1 c_2 d_2 + c_2^2$$

$$\left[\left(\frac{k_2v_1}{k_1v_2}\right)^2 - c_1^2\right]d_2^2 + \left[-\frac{2v_1^2k_2\Delta t_{2,3}}{k_1^2v_2} - 2c_1c_2\right]d_2 + \left[\left(\frac{v_1\Delta t_{2,3}}{k_1}\right)^2 - c_2^2 + x^2\right] = 0$$

This is in the form  $a d_2^2 + b d_2 + c = 0$  and the quadratic formula may be used to solve for  $d_2$ . Once  $d_2$  is known,  $d_1$  may be found from equation (7)

$$d_1 = \frac{v_1}{k_1} \Delta t_{2,3} - \frac{k_2}{k_1} \frac{v_1}{v_2} d_2$$

This estimate of the shot depth  $(d_1)$  and seafloor depth  $(d_1+d_2)$  includes the effect of nonvertical ray paths since angles  $\alpha_1$  and  $\alpha_2$  were used in the calculation. These values of  $d_1$  and  $d_2$  are then used to calculate new values for  $\alpha_1$  and  $\alpha_2$ , and the process is repeated.  $d_1$  and  $d_2$  should converge to constants within a few iterations. 

### **Required** inputs

a) differences in time of arrivals  $\Delta t_{1,2}$  and  $\Delta t_{2,3}$ .

b) distance the ship has traveled from the drop site at the time of detonation.

 $x = (\text{ship's speed}) \times (\text{detonation time} - \text{time charge was launched}).$ 

c) average sound speed  $v_1$  and  $v_2$  in layers 1 and 2.

Outputs

- a) shot depth  $(d_1)$
- b) distance from shot to sea floor  $(d_2)$ . Bottom depth is then given by  $d_1 + d_2$ .
- 1. Find approximate values for  $d_1$  and  $d_2$  by assuming vertical raypaths

$$\hat{d}_1 = \frac{1}{2} \Delta t_{2,3} v_1$$

$$\hat{d}_2 = \frac{1}{2} \Delta t_{1,2} v_2$$

2. Calculate  $\alpha_1$  and  $\alpha_2$ 

$$\alpha_1 = \arctan(\frac{x}{\hat{d}_1 + 2\hat{d}_2})$$

$$\alpha_2 = \arctan(\frac{x}{3\hat{d}_1 + 2\hat{d}_2})$$

122222

3. Calculate constants  $k_1$  and  $k_2$ 

$$k_1 = \frac{3}{\cos(\alpha_2)} - \frac{1}{\cos(\alpha_1)}$$

$$k_2 = \frac{2}{\cos(\alpha_2)} - \frac{2}{\cos(\alpha_1)}$$

4. Calculate constants  $c_1$  and  $c_2$ 

$$c_{1} = \frac{2v_{1}}{v_{2}\cos(\alpha_{1})} - \frac{k_{2}v_{1}}{k_{1}v_{2}\cos(\alpha_{1})}$$

$$c_{2} = \frac{v_{1} \Delta t_{2,3}}{k_{1} \cos(\alpha_{1})} - v_{1} \Delta t_{1,2}$$

5. Calculate coefficients for the quadratic formula

$$a = \left(\frac{k_2 v_1}{k_1 v_2}\right)^2 - c_1^2$$

$$b = -\frac{2v_1^2 k_2 \Delta t_{2,3}}{k_1^2 v_2} - 2c_1 c_2$$

$$c = \left(\frac{v_1 \Delta t_{2,3}}{k_1}\right)^2 - c_2^2 + x^2$$

6. Find depths  $d_2$  and  $d_1$ 

$$d_2 = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$d_1 = \frac{v_1}{k_1} \Delta t_{2,3} - \frac{k_2}{k_1} \frac{v_1}{v_2} d_2$$

7. Use  $d_1$  and  $d_2$  found in step 6 as the next  $\hat{d}_1$  and  $\hat{d}_2$  in step 2 and repeat.

After  $d_1$  and  $d_2$  have converged to constants,  $d_1$  gives the shot depth and  $(d_1 + d_2)$  gives the sea floor depth.

Junior

### 4. Example

A Fortran-77 program which implements the algorithm on page 12 is given in the Appendix. To illustrate its use, shot and seafloor depths will be found using the data presented in Figure 2. This particular data was obtained from a refraction experiment conducted on the Monterey Deep-Sea Fan in 1981 by the Marine Physical Laboratory. The research vessel FLIP (FLoating Instrument Platform) was moored in 2800 meters of water and utilized as a receiving station. A 20 element hydrophone array was deployed at mid-depth in the water column. The output of nine of these hydrophones along with the hydrophone streamer data is shown in Figure 2.

A Navy tug steamed away from FLIP and dropped explosive charges (Mk 94 SUS + 256# TNT) into the water at ranges between 3.5 km to 37 km from FLIP. As each shot was launched the radar range between FLIP and the tug, and the time, were recorded. Velocity of the tug was obtained from this information. The distance traveled from the drop site by the tug when the detonation arrived at the streamer hydrophone could then be calculated.

Mean velocities were obtained by integrating the velocity profile between the surface and 1820 meters for layer 1, and from 1820 meters to 2800 meters for layer 2.

122222.3

The following input to the program



produces the output



These are reasonable values for this experiment. The shot depth of 1788 meters is within the rather large uncertainty of the detonation device. A bathymetric map of the area shows the sea floor depth to be between 2800 meters at FLIP and 3200 meters at a range of 32 km from FLIP.

### Acknowledgements

This work was funded by the Office of Naval Research, Code 1125 (formerly Code 425).

Appendix: Fortran-77 program

Implements the algorithm on page 12

c Iterative method to find shot depth (d1) and seafloor depth (d1 + d2)
c from hydrophone streamer data.

C ------

real k1, k2

できないとう

c ----- Input ----write(6,\*) 'Enter mean velocity in layer 1 (meters/sec)' read(5,\*) v1 write(6,\*) 'Enter mean velocity in layer 2 (meters/sec)' read(5,\*) v2 write(6,\*) 'Enter first and second arrival time difference (sec)' read(5,\*) dt12 write(6,\*) 'Enter second and third arrival time difference (sec)' read(5,\*) dt23 write(6,\*) 'Enter distance ship traveled from drop site (meters)' read(5,\*) x write(6,\*) 'Enter maximum number of iterations to perform' read(5,\*) iter

c Step 1.
c Estimate d1 and d2 by assuming ray paths are vertical dhat1 = .5 \* dt23 \* v1 dhat2 = .5 \* dt12 \* v2

```
c ----- Refine the solution -----
do 100 i=1,iter
c Step 2.
alpha1 = atan( x / (dhat1 + 2.*dhat2) )
alpha2 = atan( x / (3.*dhat1 + 2.*dhat2) )
```

c Step 3. k1 = 3./cos(alpha2) - 1./cos(alpha1)k2 = 2./cos(alpha2) - 2./cos(alpha1)

c Step 4. c1 = 2.\*v1/(v2\*cos(alpha1)) - k2\*v1/(k1\*v2\*cos(alpha1)))c2 = v1\*dt23/(k1\*cos(alpha1)) - v1\*dt12

Step 6.

c Note: The solution to the quadratic formula is -b +/- sqrt ...

c For the data used in this example the minus sign gives c the correct result.

\_\_\_\_\_

d2 = (-b - sqn(b\*b-4.\*a\*c)) / (2.\*a)d1 = v1\*dt23/k1 - k2\*v1\*d2/(k1\*v2)

c Make these values of d1 and d2 the new estimates, and repeat. dhat1 = d1 dhat2 = d2

100 continue

С

```
c ----- Output -----
write(6,*) 'snot depth: ', d1
write(6,*) 'sea floor depth: ', d1+d2
```

stop end



