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## Where Solitons May Be Hiding in DNA and Their Possible Significance in RNA Transcription

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We find that the hydrogen bond stretch bands of the double helix appear to be nonlinear enough to support solitary wave energy concentration. Coupling this fact to predictions of our selfconsistent theory of helix melting gives rise to speculations of a mechanism for base pair melting in RNA transcription which is consistent with the known energy needs of that process.

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Several recent papers have discussed the possibility of solitary waves in double helical DNA associated with the belical acoustic modes (1). The work was stimulated by observations in DNA of resonant microwave absorption (2). Papers have also appeared which have disputed the theoretical predictions of the likelihood of such solitary waves (3) and papers have also appeared which challenge the experimental observations (4). Solitary wave phenomena require nonlinear effects and both experimental observations (5) and theoretical analysis (6) indicate that helix acoustic modes are quite linear in their dispersion and amplitude dependence. In our theoretical studies of helix lattice dynamics of DNA we have found that a different region of the DNA spectrum is far more nonlinear (7) and seems to satisfy the quantitative requirements for selitary wave effects.

The highly nonlinear modes are the hydrogen bond stretch modes at  $16 - 120 \text{ cm}^{-1}$ . These modes have been observed in both low frequency Raman sourcesting (8) and Fourier transform infrared absorption (9) experiments. In both cases the modes have been seen to soften in frequency with increasing tensors ture. We have predicted theoretically that these modes are temperature to be in agreement with observations (10).

The same vibrational modes have played a central role in the theory the belig melting that we have developed based on belical lattice dynamics. The temperature dependence discussed above, coupled with thermal expansion of leid naturally to hydrogen bond breakup and belig melting. These results the 'or poly(dC)-poly(dC) predict melting at a temperature in this approach with observations. In that work all the parameters were fitted to spectral date at room temperature and no parameters were fitted to melting. (11)

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Helix melting is an essential element in many biological processes. For example, it is essential in the process of RNA transcription. Recent reviews of this process reaffirm the belief that energy must flow into the RNA polymerase complex from its surroundings (12). The ability of solitary wave effects to concentrate excitations in these bands would help in understanding the problems with energy flow in these processes. This biological role for nonlinear effects to in line with the original suggestions of solitary wave significance in biological processes (13).

In this paper we discuss our helical lattice dynamics results for the monlinear modes and show how these results can be used to extract parameters moded to evaluate the possibilities of nonlinear concentration. We then use the theory of molting developed to give order of magnitude estimates of the splitudes needed to induce base pair molting, and discuss the significance of these results for RNA transcription.

## ... Hudroscen Rend Stretch Medes in the Double Helix

be our stude of the vibrational modes of the double helix we have found
control bands which can be characterized as vibrations that compress the
control bands between base pairs. There are overlapping bands for all combinations of the pairs and several pass bands in this region should exist regardcontrol bands compared (14). Dispersion curves, i.e., the change in frequency
control of the displacements from one unit cell to the next. These
control bands been address frequencies. In one case the local minimum is

be extended about either end i.e. the total  $\theta$  range can run from  $-180^{\circ}$  <  $\theta \leq 180^{\circ}$  or  $0 \leq \theta < 360^{\circ}$ . The curves would have symmetry about the extension as the positive and negative phase shifts are connected by time reversal invariance. Correlating frequency with energy, and phase shift with wavevector and hence momentum for these excitations, one can relate these curves to particles with energy vs. momentum relations approximated by

$$E = E_{o} + \frac{(\Delta p)^{2}}{2m}$$
(1)

The effective mass m is then

$$m = \frac{(\Delta p)^2}{2\Delta E}$$
$$m = \frac{(\hbar^2 \Delta q^2)}{2\Delta \hbar \omega_d}$$
$$\frac{m}{\hbar} = \frac{\Delta q^2}{2\Delta \omega_d}$$

if a is the lattice spacing

$$\frac{\mathrm{ma}^2}{\hbar} = \frac{(\Delta\theta)^2}{2\Delta\omega_{\mathrm{d}}}$$
(2)

where  $\theta$  is in radians and  $\Delta \omega_{d}$  is the change in frequency due to dispersion effects for a shift in the phase from cell to cell of  $\Delta^{c}$ . In the solitary wave analysis by Davydov (13) the wave equation for such a system is given by the nonlinear Schreedinger Equation in one dimension

$$\left(i\hbar\frac{\theta}{4t} + \frac{\hbar^2}{2m}\frac{\theta^2}{2z^2} + G[\psi]^2\right)\psi(z,t) = 0$$
(3)

with the substitutions

$$x = z/a$$
  $\tau = \frac{ht}{2ma^2}$  and  $g = \frac{ma^2G}{h^2}$  (4)

this becomes

$$(\mathbf{i} \frac{\partial}{\partial \tau} + \frac{\partial^2}{\partial x^2} + 2\mathbf{g}|\psi|^2) \quad \psi(\mathbf{x},\tau) = 0$$
 (5)

which has the solitary wave solution

$$\psi = \frac{1}{2} \sqrt{g} \quad e^{i(2kx - \omega\tau)} \quad \operatorname{sech}[\frac{g(x - 4k\tau)}{2}] \tag{6}$$

with

$$\omega = 4(k^2 - \frac{g^2}{16})$$
  $k = \frac{maV}{fh}$  (7)

where V is the velocity of the centroid of the solitary wave. Concentration of the excitation occurs in the square wave excitation case (13) for  $g \ge g_{cr}$  where

$$g_{\rm cr} \approx \frac{\pi^2}{4k} \tag{8}$$

and ? is the extent of the initial excitation along x.

The term  $G[x]^2$  is a measure of how the energy is lowered by increased concontration of the probability amplitude. In our selfconsistent temperature dependent lattice calculations we have found that the hydrogen bond stretch modes are anharmonic, i.e. they lower in frequency as the excitation level in temperature increase, we have found this shift in frequency to be in rouch corrected with the observed frequency shift from low temperature to room to a nature (10). This decrease in every with increase in correctative of acquiring provides the selftripping effect which cohences concentration of the constant on the selftripping effect which cohences concentration of the constant on the selftripping effect which cohences concentration of the constant on the selftripping effect which cohences concentration of the constant on the selftripping effect which cohences concentration of the constant on the selftripping effect which cohences concentration of the constant on the selftripping of the temperature of the temperature of the constant on the selftripping of the temperature of the temperature of the constant on the selftripping of the temperature of the constant on the selftripping temperature of the temperature of tempera

room temperature. For vibrational systems the mean wave amplitude squared is proportional to the temperature. The frequency is seen to drop with increasing temperature and hence mean squared amplitude.

We can estimate G for particular excitation modes from Figure 2. In Equation 3,  $|\psi|^2$  is a normalized nondimensional squared wave amplitude. We associate  $\Delta |\psi|^2$  with  $\frac{\Delta T}{T}$  for regions of curve in Figure 2. We also associate the appropriate  $\Delta E$  with  $\hbar\Delta\omega_A$  over that  $\Delta T$ .  $\Delta\omega_A$  is the change in frequency due to anharmonicity not dispersion. Then:

$$\frac{G}{f_1} = \frac{\Delta \omega}{\Delta T/T}$$
(9)

Using this and Eqs. (2) in Eqn. (4)

$$g = \frac{ma^2}{f_1} \times \frac{G}{f_1} = \frac{(\Lambda \psi)^2}{2\Lambda \omega_d} \frac{\Lambda \omega_A}{\Lambda T/T}$$
(10)

For the 85 cm<sup>-1</sup> band from Figures 1 and 2 at T z room temperature we estimate z = 10. For reasons discussed in the next section we estimate  $l_{min}$  the minimum initial size of the excitation to be 2.5 in units of a. For this value  $g_{cT} = 1$ . One can expect nonlinear concentration of excitations in these bands in DNA. In Figure 2 one can see that G would be even larger at the higher levels of excitation needed for helix melting.

ILI. Discussion

From the review of RNA transcription, the basic process, a "step", fuses an ENA nucleotide to the proving SNA transcript. For each step a DNA base prin is split on the downstream side, a DNA ~ RNA hybrid base pair is formed, a DNA ~ RNA hybrid base pair is split, a DNA base pair upstream is reformed, and

a polymerization event in the RNA backbone takes place. As a result of the backbone chemistry a pyrosphophate group is removed from the nucleoside triphosphate (NTP) which is the source of the added RNA section. The pyrophosphate group is later hydrolized but not at a site directly connected to the other operations. The overall energy flow in the transcription complex is such that on the average 0.5 kcal/mole transcribed must be absorbed by the complex from its surroundings.

For the purposes of this discussion we will explore ways in which energy introduced into the complex can bring about base pair melting. The free energy needed to melt a GC pair is generally accepted to be 3.5 kcal/mole and that for an AT pair 1 kcal/mole (12). If inflow of this amount of energy occurred the net energy requirements of transcription would easily be met. The reason to consider this form of energy transfer to the transcription complex is that we believe it would involve the nonlinear hydrogen bond stretch modes. In our theory of melting we calculate the vibrational fluctuations D on each hydrogen bond where  $D = - uu_{-}$  and u a is the displacements of atoms from equilibrium due to phonon amplitude. The selfconsistent softening of the bond and thermal expansion are calculated based on D. The softening and expansion lead to a melting of the hydrogen bonds. In this sense D, which grows with excitation hered here pair in poly(dC)-poly(dC) we found that when a hydrogen lend has  $0 = 0.050 \Delta^2$  melting occured (11).

We also investigated the contribution of individual vibrational basis D(a)to the total fluctuation D as seen in Figure 3. The hydrogen bond stretch band

at 95 - 100 cm<sup>-1</sup> at 340K has  $D(\omega) \approx 5.5 \times 10^{-3}$  Å from the entire band. Ignoring the contributions of other bands one would only have to increase the excitation of this band by a factor of 7.27 to bring on melting from the energy in this band alone. Since the thermal occupation is about 2 phonons at this temperature one would require 214-15 phonons to bring about melting. The energy of  $\approx 14$ phonons is approximately the 3.5 kcal/mole generally associated with the binding energy of GC base pairs. The localization to the hydrogen bond of these excitations is in the localized amplitudes calculated and plotted in Figure 3.

If we consider melting a GC base pair in terms of the needed energy in one mode while all others are in thermal equilibrium at room temperature a different estimation is appropriate. One still needs a total D z 0.004 A The thermal activation of all modes at room temperature is  $D_{p} \approx 0.028$  A (7). The needed additional fluctuation is  $\Delta D = 0.012 \text{ A}^{-1}$ . For  $D(\omega)$  of the 95-100 cm<sup>-1</sup> band  $D(\omega) = 0.0055$  to make up this difference the excitation level would have to 2.8 times that at 343K. This requires z 6 phonons in a packet arriving at the base pair adjacent to the melted region. The thermal activation level is  $\pm$  2. The mean large fluctuation value from Bose-Einstein statistics is  $\approx$  4-5. Such a concentration of energy may be achieved by capturing energy from the concoundings as is apparently needed to explain the energetics of DNA transcription. Such an excitation could travel in unmelted DNA without disrupting the  $D_{CC}$  as the D(s) for all bands is less for base pairs far from a melted section. 0 ( ) (or the 95-100 cm band is about half the value at a cell( $\infty$ ) as for cell (()) in t to the rait, as seen in Figure 3. When the energy propagates into the coll inclusion to the molt the change in localized mode behavior greatly increases fluecontinuing liteles and disrupts the base pair.

It is an interesting question as to whether the RNA polymerase is a proper thermodynamic engine which runs on a directed f]ow of energy or is driven bv thermal fluctuations many believe as (12).If effects can be shown to in fact exist in solitary wave DNA one will have come a long way to showing that the RNA polymerase can be a proper thermodynamic engine. Energy from the hydrolysis of pyrophosphate could be absorbed before the thermalization of this energy. The entire helix could act as an antenna for the absorption greatly increasing the fraction of energy absorbed before thermalization. The processing and concentration of energy would occur as the energy propagated on the one dimensional helix to the region of transcription.

In the earlier section we estimated l the initial size of the excitation as being at least 2 2.5 base units in length. This is based on the idea of a planar longitudinal wave or shock wave from pyrophosphate hydrolysis impinging on a section of DNA helix from the side. A helical structure is just what's needed to convert such an external excitation into a short wavelength excitation in the internal coordinates of the DNA because of k-conservation selection rules. For some forms of excitation a 10 fold helix would select excitations of 10 has pair wavelength or  $\theta = 36^{\circ}$  on dispersion curves such as Figure 1. To generate a hydrogen bond stretch wave where compression of either strand leads to compression of the hydrogen bonds the wavelength would be 5 base pairs or

 $72^{\circ}$ . We have consociated half this wavelength with the minimum extend of the initial square wave excitation and set  $\ell = 2.5$ . Short wavelengths can lead to more localized wave packets and localization or concentration is needed to efficiently celt base pairs adjacent the already melted area. It is interesting

to speculate on how the existence of a small integer-fold helical structure for DNA interacts with the need for energy transfer in process such as transcription in early evolution of the system.

Better nonlinear models of wave propagation more appropriate to the case of dispersive optical modes would allow a more quantitative estimate of many of the energies which have been crudely estimated in this phenomenological discussion. The role of DNA excitations in biological processes may be important and weems likely to be, based on these simple estimates.

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## Figure Captions

- Figure 1. Dispersion relations for several optical bands in poly(dG).poly(dC). The frequency is in cm<sup>-1</sup> and the phase is the relative phase between neighbor unit cells. In terms of a wavevector q, this phase is qa where a is the lattice constant.
- Figure 2. Calculated change in frequency of selected zone center modes of poly(dG).poly(dC) as a function of temperature. For details see reference (14).
- Figure 3. The contribution to the fluctuation amplitude by individual vibrational bands for the hydrogen bond adjacent the major groove in poly(dG)·poly(dC). The three divisions are for the two base pairs adjoining a melted base pair on either side and for a base pair far away from the melted base pair. For the 95-100 cm<sup>-1</sup> band the highest division is for the (+1) base pair i.e. 3' + 5' direction in the G chain. The next highest is for the (-1) base pair i.e. on the other side of the melt. The lowest division is for the (\$\circ\$) base pair i.e. far away from the melt. See reference 11 for details.







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