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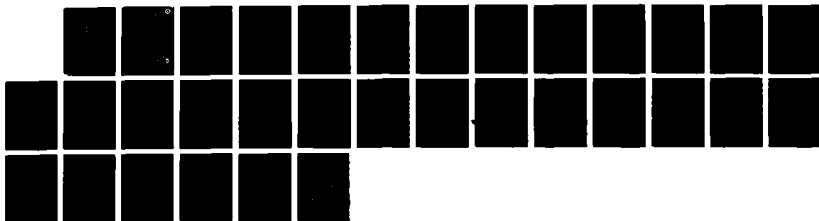
SELF-CONSISTENT FIELD MODEL FOR THE COMPLEX CAVITY
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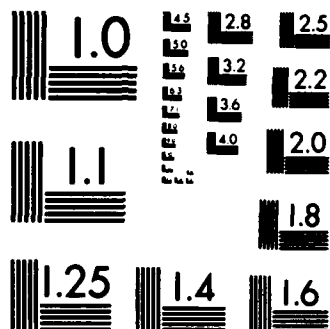
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Self-Consistent Field Model for the Complex Cavity Gyrotron

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September 17, 1987

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<p>Mode competition in gyrotrons with highly overmoded cavities can degrade efficiency and output mode purity. One approach to mode selection which has been demonstrated experimentally involves a sudden change in the cavity radius. Cavities with this feature are called "complex-" or "step-cavities". This paper presents a theoretical model for the step-cavity gyrotron. The model applied to steady state operation. The axial variation of the cavity RF fields is determined self-consistently with the electron beam motion by integration of the wave equation simultaneously with the nonlinear electron equations of motion. The model accounts for mode conversion effects at the step as well as beam loading effects such cavity Q modification and frequency pulling. The model is applied to the analysis of a TE_{01}/TE_{04} complex cavity gyrotron.</p>				
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SELF-CONSISTENT FIELD MODEL FOR THE COMPLEX CAVITY GYROTRON

I. INTRODUCTION

The gyrotron oscillator is currently under development as a high average power, efficient millimeter wave source. The gyrotron derives much of its high power capability from the ability to operate stably in a single mode of an over-moded resonator. However, as the trend toward higher output power leads to increasingly over-moded cavities, the mode density increases and mode competition can occur. This effect can seriously degrade the efficiency of operation and is undesirable for other reasons as well. For example, the plasma heating application for magnetic fusion involves highly mode and frequency specific transmission systems for the output power. Thus mode selection techniques for gyrotron cavities are of considerable interest, particularly with respect to different transverse modes. One method which has been successfully demonstrated in several devices involves a sudden change or step in the cavity wall radius. The "complex-cavity" or "step-cavity" concept was first demonstrated in a TE_{01}/TE_{04} configuration by Carmel et al (1983), and has been incorporated in a 60 GHz TE_{01}/TE_{02} device (Felch et al 1984) and in a 140 GHz TE_{02}/TE_{03} device developed by Varian. The 60 GHz Varian device produces 200 kW of cw power and it and the 140 GHz gyrotron currently under development represent the current state-of-the-art of high average power gyrotrons in the U.S.

The essential idea of the complex cavity approach is that a particular pair of modes having the same azimuthal index m can be tightly coupled to form a high Q mode of the complete cavity. In the step cavity configuration

(Carmel et al 1983) mode coupling occurs at a sudden change in the cavity wall radius. The cavity is designed such that the local waveguide modes of this mode pair are simultaneously near cut-off in the two cylindrical sections of the cavity at the desired operating frequency. Mode pairs with a different mode index m' will not be simultaneously resonant in the cavity sections and will form modes of the complete cavity which are less favorable for gyrotron operation. Such modes may have a shorter effective interaction length, a lower Q factor, or lower inter-mode conversion efficiency at the step. These effects usually lead to higher starting currents. The success of this approach depends on several factors including mode density, fabrication tolerances, and mode conversion at the cavity step. As the mode density increases, more than one mode pair can become simultaneously resonant. Step-cavity gyrotrons are more sensitive to machining tolerances than conventional gyromonotrons because of the bimodal resonance condition. Finally, conversion into unwanted modes at the step can degrade the mode purity and Q factor of the device. Clearly, theoretical models are needed which can investigate and quantify these effects.

In this paper a theoretical model of the step-cavity gyrotron is presented. The model is based on a Self-Consistent Field theory for low Q gyromonotrons developed previously (Fliflet et al. 1982). This theory treats steady-state operation in a single cavity mode. The axial variation of the cavity RF fields is determined self-consistently with the electron beam motion by integrating the wave equation simultaneously with the electron equations of motion. The theory accounts for important aspects of gyrotron operation such as modification of the cavity Q and resonant frequency by beam loading. These effects are omitted when cold cavity eigenmodes are used to describe the RF

field distribution during operation. Calculations for step-cavity gyrotrons have to date been based on the use of cold cavity eigenmodes and it is of interest to explore beam loading effects for such devices.

In this paper, the SCF approach for gyromonotrons is extended to account for a sudden change or step in the cavity diameter. In addition to the beam loading effects noted for gyromonotrons, the method predicts the mode conversion efficiency at the step. Mode conversion at the step is calculated by the field matching technique of Masterman and Clarricoats (1971). To obtain a computationally tractable model suitable for use in design studies, the following simplifications are introduced: (1) The beam is assumed to interact with just one TE_{mn} waveguide mode in each cavity section. The modes in the two sections will differ only in radial index. (2) Non-resonant modes which may be excited at the step are assumed to propagate out of the cavity without reflection by the cavity structure. This is consistent with the fact that such modes are not close to cutoff and will be weakly affected by changes in the cavity wall radius. With these assumptions, SCF calculations for the step-cavity gyrotron are not significantly more involved than for conventional gyromonotrons. These assumptions appear to be consistent with the step cavity concept, but their validity must ultimately be tested by comparison with experiment or with more general calculations.

The method has been applied to the analysis of a TE_{01}/TE_{04} step cavity configuration similar to the NRL experiment (Carmel et al 1983). The results indicate that the selectivity of the cavity for the $m=0$ mode is enhanced compared to a conventional TE_{04} gyromonotron. The $TE_{01} - TE_{04}$ mode conversion efficiency at the cavity step can be high (95%) which allows good output mode

purity. The selectivity of the cavity is optimum when the $m=2$ competing mode is not cut-off in the input section since in this case the Q factor for this mode is degraded by diffraction losses at the input. This effect was exploited in the NRL experiment and probably contributed significantly to the stability of the device. The effect of having the $m=2$ mode cut-off in the input section was investigated.

The remainder of this paper consists of three sections. Section II contains an outline of the self-consistent field theory and describes the present application of Masterman and Clarricoat's field matching technique for waveguide discontinuities. Section III presents the results of calculations, and Section IV contains discussion of results and our conclusions. Except as noted, MKS units are used throughout.

II. THEORETICAL MODEL

A. Self-Consistent Field Equations

The electron beam - rf field dynamics are treated according to a system of coupled, non-linear, ordinary differential equations derived previously (Fliflet et al 1982). The electrons follow helical trajectories due to a strong applied axial magnetic field which may be weakly tapered and experience perturbing rf fields. Space-charge effects are neglected. On either side of the cavity step, the beam is assumed to interact with a single TE circular waveguide mode of the form:

$$\vec{E}_t = \text{Re}\{C_{mn}[k_{mn}J'_m(k_{mn}r)\hat{\theta} + imJ_m(k_{mn}r)\hat{r}/r]f(z)\exp[i(\omega t - m\theta)]\} \quad (1)$$

where ω is the wave frequency, J_m is a Bessel function of the first kind, the prime denotes differentiation, and $k_{mn} = x_{mn}/r_w$ is the transverse wave number. The normalization constant is given by

$$C_{mn} = [\sqrt{\pi(x_{mn}^2 - m^2)} J_m(x_{mn})]^{-1} \quad (2)$$

where x_{mn} is the n th zero of J'_m and r_w is the radius of the cavity wall which is assumed to be weakly irregular except at the step. The axial dependence of the rf fields in the resonator is given by the complex profile function

$$f(z) = f(z)\exp[-i\phi(z)] \quad (3)$$

It is convenient to use the normalized momentum variable

$$\vec{u} = \gamma \vec{v} \quad (4)$$

where \vec{v} is the electron velocity and γ is the relativistic factor given by:

$$\gamma = [1 + u^2/c^2]^{1/2} \quad (5)$$

and c is the speed of light. To obtain a slow time scale formulation the transverse momentum is expressed in terms of magnitude and phase variables u_t and Λ according to

$$u_x + iu_y = iu_t \exp[i(\omega t/s - \Lambda)] \quad (6)$$

where s is the harmonic number. Consider the case of an annular electron beam propagating in a circular waveguide structure. Neglecting the interaction with the rf magnetic field components and considering the interaction with a single harmonic of the cyclotron frequency, the equations for steady-state operation are given by:

$$\frac{du_t}{dz} = -\frac{\gamma \eta C_{mn} J_{m-s}(k_{mn} R_0)}{u_z} \frac{\partial J_s(k_{mn} r_L)}{\partial r_L} \text{Re}\{f \exp(is\Lambda)\} + \frac{u_t}{2B_z} \frac{dB_z}{dz} \quad (7a)$$

$$\frac{d\Lambda}{dz} = -\frac{\gamma \eta C_{mn} J_{m-s}(k_{mn} R_0)}{u_z u_t} \frac{s J_s(k_{mn} r_L)}{r_L} \text{Re}\{if \exp(is\Lambda)\} + \frac{\gamma}{u_z} (\omega/s - \Omega_z/\gamma) \quad (7b)$$

$$\frac{du_z}{dz} = -\frac{u_t^2}{2u_z B_z} \frac{dB_z}{dz} \quad (7c)$$

$$\left[\frac{d^2}{dz^2} + (\omega/c)^2 - k_{mn}^2 \right] f =$$

$$-2i\mu\omega I_0 C_{mn} J_{m-s}(k_{mn} R_0) \frac{1}{2\pi} \int_0^{2\pi} d\Lambda \frac{u_t}{u_z} \frac{\partial J_s(k_{mn} r_L)}{\partial r_L} \exp(-is\Lambda) \quad (7d)$$

where z is the axial spatial coordinate, $\eta=e/m$ is the charge to rest mass ratio for an electron, and R_0 is the guiding center radius for a thin annular beam. The local non-relativistic cyclotron frequency is given by

$$\Omega_z = \eta B_z \quad (8)$$

and the axial magnetic field is assumed to be constant within the electron

beam. The Larmor radius $r_L = u_t/\Omega_z$. The first three equations are derived from the Lorentz force equation, and the last equation is derived from Maxwell's equations. In Eq.(7d) I_0 is the beam current and Λ_0 is the electron phase entering the interaction region. Eqs.(7a-d) are solved subject to appropriate boundary conditions as discussed below.

It is readily verified that the total power flowing in the beam and interacting mode is conserved by Eqs.(7a-d).

B. Field Matching Procedure at Cavity Step

A computer oriented field matching technique due to Masterman and Clarricoats (1971) is used to treat mode conversion at the cavity step. The present application involves the junction of two coaxial circular waveguides. The discontinuity plane aperture cross section is equal to the smaller waveguide cross section. In this method the rf fields in the discontinuity plane are expressed in terms of transverse vector functions. For a TE mode the transverse electric and magnetic fields in waveguide I are in general given by

$$\vec{E}_t = \sum_m (a_{im} + a_{rm}) \vec{e}_m \quad (9a)$$

$$\vec{H}_t = \sum_m (a_{im} - a_{rm}) \vec{h}_m \quad (9b)$$

where the transverse vector functions are given by

$$\vec{e} = z \times \vec{\nabla}_t \psi \quad (10a)$$

$$\vec{h} = - \vec{\nabla}_t \psi \quad (10b)$$

The scalar function ψ satisfies the wave equation

$$(\nabla_t^2 + k_t^2) \psi = 0 \quad (11)$$

and the boundary condition

$$\frac{\partial \psi}{\partial r} = 0 \quad (12)$$

at the waveguide wall. For a circular waveguide, the scalar function is given by

$$\psi = C_{mn} J_m(k_{t1} r) e^{-im\theta} \quad (13)$$

where $k_{t1} = x_{mn1}/r_{w1}$. The vector functions \vec{e} and \vec{h} satisfy the orthonormality condition

$$\int_s \vec{e}_i \times \vec{h}_j \cdot d\vec{s} = \delta_{ij} \quad (14)$$

where $\delta_{ij} = 0$ if $i \neq j$ or 1 if $i = j$. The coefficient a_{im} is the amplitude of a mode incident to the discontinuity plane, a_{rm} is the amplitude of a mode reflected from the plane. Both propagating and evanescent modes should be included. Similarly, in waveguide II the fields are given by

$$\vec{E}_t' = \sum_n (a_{in}' + a_{rn}') \vec{e}_n' \quad (15a)$$

$$\vec{H}_t' = \sum_n (a_{rn}' - a_{in}') \vec{h}_n' \quad (15b)$$

where \vec{e}_n' and \vec{h}_n' are vector functions for waveguide II. To proceed, the infinite series representations of the transverse fields are truncated after a finite number of terms, say, p modes in waveguide I and p' modes in waveguide II. The transverse electric and magnetic fields must be continuous across the aperture. This condition and the orthogonality of the vector functions leads to a set of linear equations for the mode amplitudes:

$$a_{in}' + a_{rn}' = R_{nm}(a_{im} + a_{rm}) \quad (16a)$$

$$S_{mn}(a_{rn}' + a_{in}') = a_{im} + a_{rm} \quad (16b)$$

where the summation over repeated indicies is understood and R_{nm} and S_{mn} are given by

$$R_{nm} = \frac{\int_S \vec{e}_m \times \vec{h}_n' \cdot d\vec{s}}{\int_S \vec{e}_n' \times \vec{h}_n' \cdot d\vec{s}} \quad (17a)$$

$$S_{nm} = \frac{\int_S \vec{e}_m \times \vec{h}_n' \cdot d\vec{s}}{\int_S \vec{e}_m \times \vec{h}_m \cdot d\vec{s}} \quad (17b)$$

For circular waveguides, R_{nm} and S_{nm} involve integrals of Bessel functions. Closed form expressions for these integrals can be obtained (Gradshteyn and

Ryzhik 1965). In the present application, waveguide I corresponds to the cavity section for which the mode M is nearly cutoff and interacts with the beam; and waveguide II corresponds to the cavity section for which the mode N is nearly cutoff and interacts with the beam. Except for the step, the cavity consists of a slightly irregular waveguide structure which has little effect on modes which are far from cutoff. It is therefore assumed that any non-resonant propagating modes excited by mode conversion at the step will simply propagate out of the system without reflection at the cavity input or output sections. Therefore, the incident mode amplitudes are all zero except for a_{im} and a'_{in} .

In the present model, the boundary conditions on the mode M are applied at the cavity input and the self-consistent field equations are integrated up to the cavity step. Only the beam interactions with the mode M are included. This integration determines the values of a_{im} and a_{rm} since the interaction with both forward and backward waves has been included. To continue the integration of the field equations beyond the step, it is necessary to calculate the amplitude coefficients a'_{im} and a'_{rm} . The non-zero value of a'_{in} results from the interaction with the beam as well as from reflection from the cavity output structure. These coefficients as well as the amplitudes of other modes excited at the step are obtained as follows: Eliminating the coefficients a'_{rm} from Eqs.(18a,b) leads to

$$2S_{mn}a'_{in} = (S_{mn}R'_{n,m} - \delta_{m,m'})a_{im} + (S_{mn}R'_{n,m} + \delta_{m,m'})a_{rm} \quad (20)$$

Using the facts that $a_{im} = 0$, $m=M$, and $a_{in} = 0$, $n=N$, Eq.(20) can be rewritten in the form

$$\begin{aligned}
& (-S_{mn} R_{n'm'} + \delta_{m,m'}) a_{rm'} + 2S_{mN} a'_{iN} \\
& = (S_{mn} - \delta_{m,M}) a_{iM} + (S_{mn} R_{n'M} + \delta_{m,n}) a_{rM}
\end{aligned} \tag{21}$$

Eq.(21) consists of p inhomogeneous linear equations for p unknowns and can be solved using standard matrix methods. The unknowns are the $p-1$ amplitudes a_{rm} , $m=M$, and a'_{iN} . The remaining p' coefficients a_{rn} are then given by

$$a'_{rn} = R_{nm} (a_{im} + a_{rm}) - a'_{in} \tag{22}$$

To summarize, the self-consistent field approach for step-cavity gyrotrons involves integrating Eqs.(7a-d) for the mode M up to the step, applying the field matching procedure to obtain the amplitudes of modes excited by mode conversion at the step, and then integrating Eqs.(7a-d) for mode N to the cavity output region. The desired solutions are those for which the mode N satisfies outgoing wave boundary conditions at the cavity output, i.e.,

$$df_N/dz = -ik_z f_N \tag{23}$$

where k_z is the axial wavenumber in the output waveguide. Within the assumptions of the model, the boundary conditions for the other modes are automatically satisfied by the matching procedure.

Since f_N is complex, Eq.(23) represents two conditions. Thus the solution of the self-consistent field equations for the step-cavity

configuration - as for the gyromonotron - constitutes a two dimensional eigenvalue problem. If the mode M has the form of a growing evanescent wave in the cavity input section, then for fixed beam, magnetic field, and resonator parameters the eigenfunctions correspond to discrete pairs of values for $f_M(z_0)$ and ω . These are not known a priori and must be found by a search procedure.

III. CALCULATIONS AND RESULTS

Calculations have been carried out for a TE_{01}/TE_{04} step cavity configuration. The cavity design is shown in Figure 1. The principal competing mode pair is the TE_{21}/TE_{24} combination. The beam voltage was taken to be 70 kV and a beam pitch ratio of $\alpha = v_t/v_z = 1.5$ was used. The cavity dimensions correspond to operation at approximately 35 GHz. A step-cavity design of this type was successfully demonstrated experimentally by Carmel et al (1982) at NRL. The cavity is designed such that for the M=0 case, the resonant mode is close to cut-off in both cavity sections, whereas for the M=2 case, the resonant frequency is considerably above cut-off in the smaller cavity section. The beam drift tube of the experimental cavity was not cut-off to the TE_{21} mode which leads to diffraction losses at the input and degradation of the Q-factor for the M=2 mode. This effect is readily achieved in cavities with the smaller section resonant for the TE_{01} mode since TE_{01} and TE_{21} cut-off radii differ significantly. It is more difficult to achieve in cavities where the smaller section supports a higher order TE_{0n} mode because for $n > 1$ there is much less difference in the cut-off radii for $m=0$ and $m=2$ modes.

The convergence of the field matching procedure at the step was checked by varying the number of modes retained in the expansions on each side of the step. As discussed by Masterman and Clarricoats the number of modes retained on each side should be approximately equal to the ratio of the corresponding waveguide radii. Adequate convergence was obtained using four modes on the TE_{01} side and sixteen modes on the TE_{04} side.

The axial profile of the RF field corresponding to the $M=0$ mode is shown in Figure 2 for typical current and magnetic field parameters. The local efficiency as a function of cavity position is also shown.

Figure 3 shows the numerically computed oscillation threshold currents for the lowest order $M=0$ and $M=2$ modes as a function of magnetic field. The optimum efficiency operating points are also indicated. The $m=2$ calculations assume the mode is cut-off at the cavity input and thus are relevant to higher order mode configurations such as TE_{03}/TE_{04} , etc. The threshold current curves are shifted by about 600 Gauss. This shift is much greater than that of the corresponding threshold current curves for the TE_{04} and TE_{24} modes in a gyromonotron. Unlike the gyromonotron (Carmel et al 1982), the optimum operating point of the step cavity $M=0$ mode is outside the $M=2$ threshold current curve. Thus competition between $M=0$ and $M=2$ modes should be significantly reduced. Note, however, that the minimum starting current of the $M=2$ mode is not much higher than that of the $M=0$ mode in the configuration analyzed. Even though the TE_{21} mode is not close to cut-off in the smaller cavity section, it is trapped by coupling to the TE_{42} mode and has significant interactions with the beam.

Figure 4 shows the efficiency vs. beam current for several values of magnetic field for the $M=0$ mode. The maximum calculated efficiency is about 43%. This is somewhat less than can be achieved in a well designed gyromonotron ($\approx 50\%$) for $\alpha = 1.5$ and could probably be improved by further cavity optimization.

Mode purity is an important issue for step-type cavities since conversion of operating modes into unwanted modes can occur at the step. This effect can also reduce the cavity Q-factor. The calculated mode purity at optimum efficiency is about 95%, thus mode conversion effects due to the step are small in the present design.

IV. CONCLUSIONS

The self-consistent field approach for gyromonotrons has been extended to the analysis of step cavity configurations. The approach allows the numerical calculation of the large signal efficiency, oscillation threshold currents, loaded Q factor, and mode conversion effects at the step. The method of calculation is relatively efficient - the computational effort is not greatly increased over the gyromonotron case - thus the method is suitable for use in design optimization studies of step cavity devices.

The approach has been applied to the investigation of the lowest order $M=0$ and $M=2$ modes of a configuration designed for TE_{01}/TE_{04} operation. The magnetic fields values for optimum efficiency operation are found to be more separated than in a gyromonotron, thus the competition between these modes

should be reduced. However, the minimum starting currents for the M=0 and M=2 modes are found to be comparable in the case that the TE_{21} mode is cut-off in the electron beam drift tube. It is concluded that a sufficiently large amplitude TE_{21} mode can contribute significantly to beam bunching even when not close to the cut-off condition. This can occur in step-cavity configurations when the lower order competing mode (TE_{21}) is cut-off at the cavity input and tightly coupled to the higher order mode (TE_{24}). Selectivity against the M=2 mode is considerably enhanced when the TE_{21} mode is not cut-off in the beam drift tube since in this case the overall cavity Q factor for the M=2 mode is significantly reduced and, furthermore, the TE_{21} mode does not achieve a large amplitude from being trapped. It is argued that this should be a general feature of step cavity designs. To our knowledge this effect has not been pointed out before.

The calculations show that conversion into unwanted modes at the step is small under optimum efficiency operating conditions, of order 95%.

V. ACKNOWLEDGEMENTS

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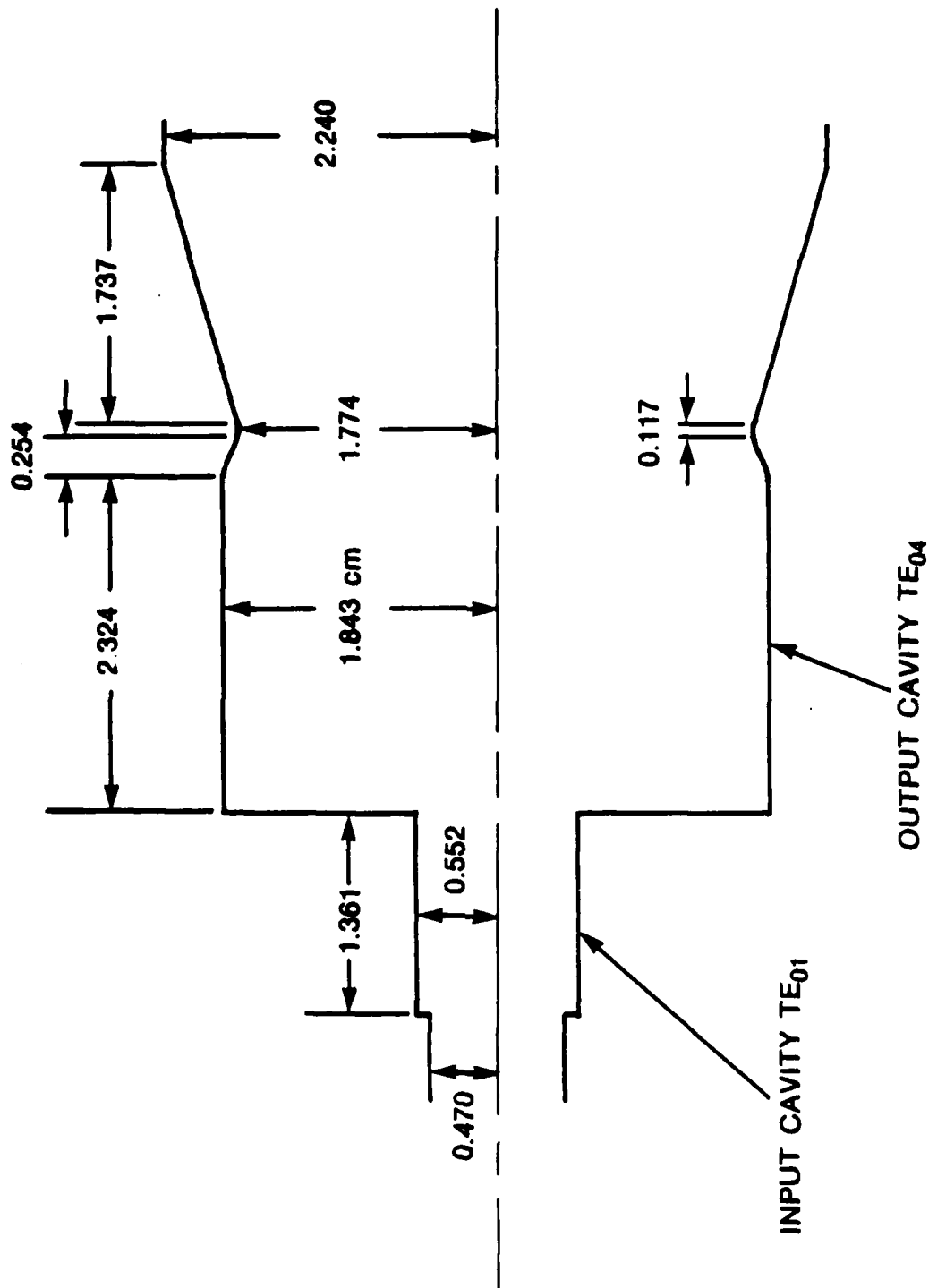


Figure 1. 35 GHz TE_{01}/TE_{04} step-cavity design used in calculations.

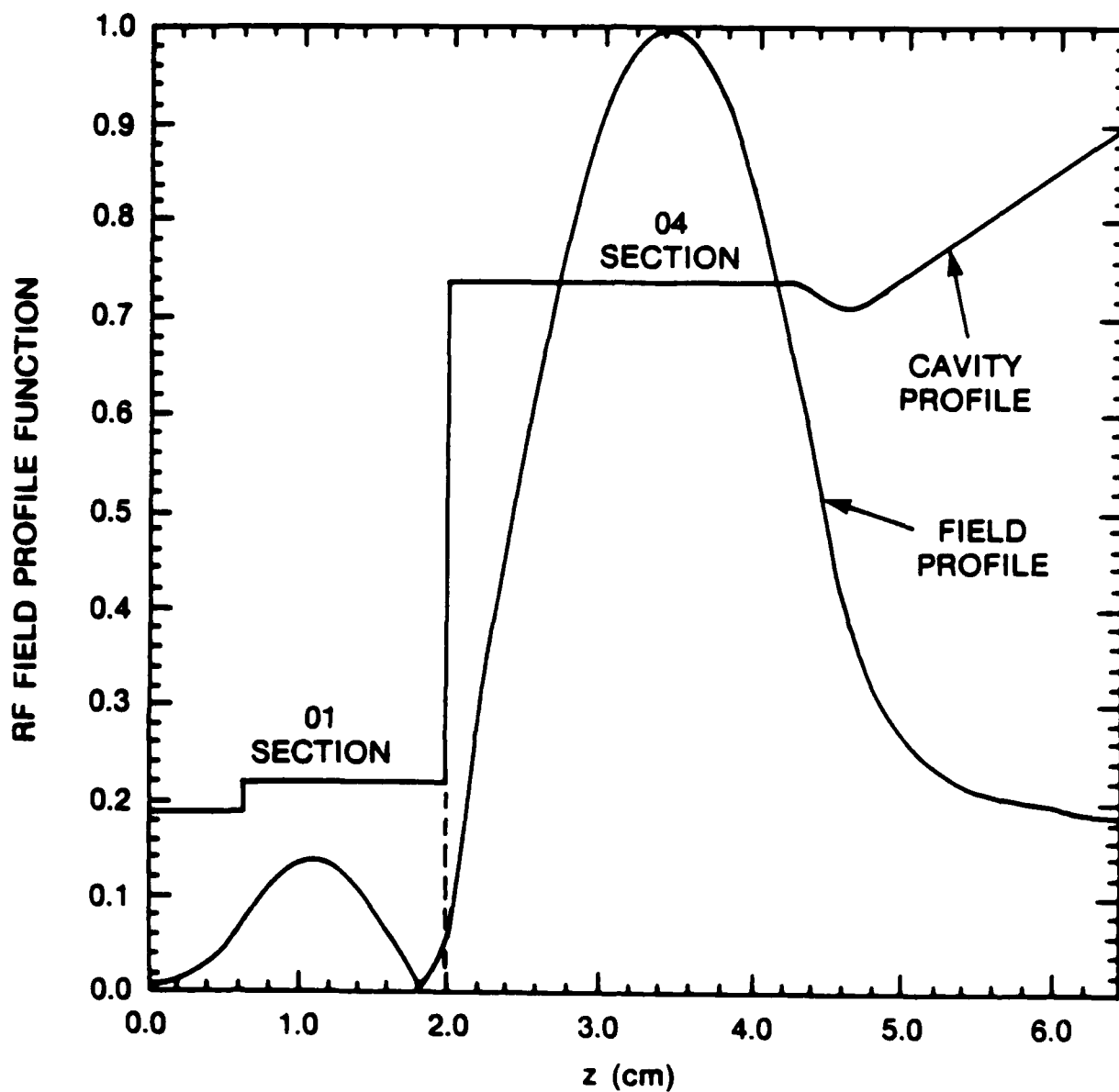


Figure 2. Axial RF field profile for $M=0$ mode corresponding to optimum efficiency conditions.

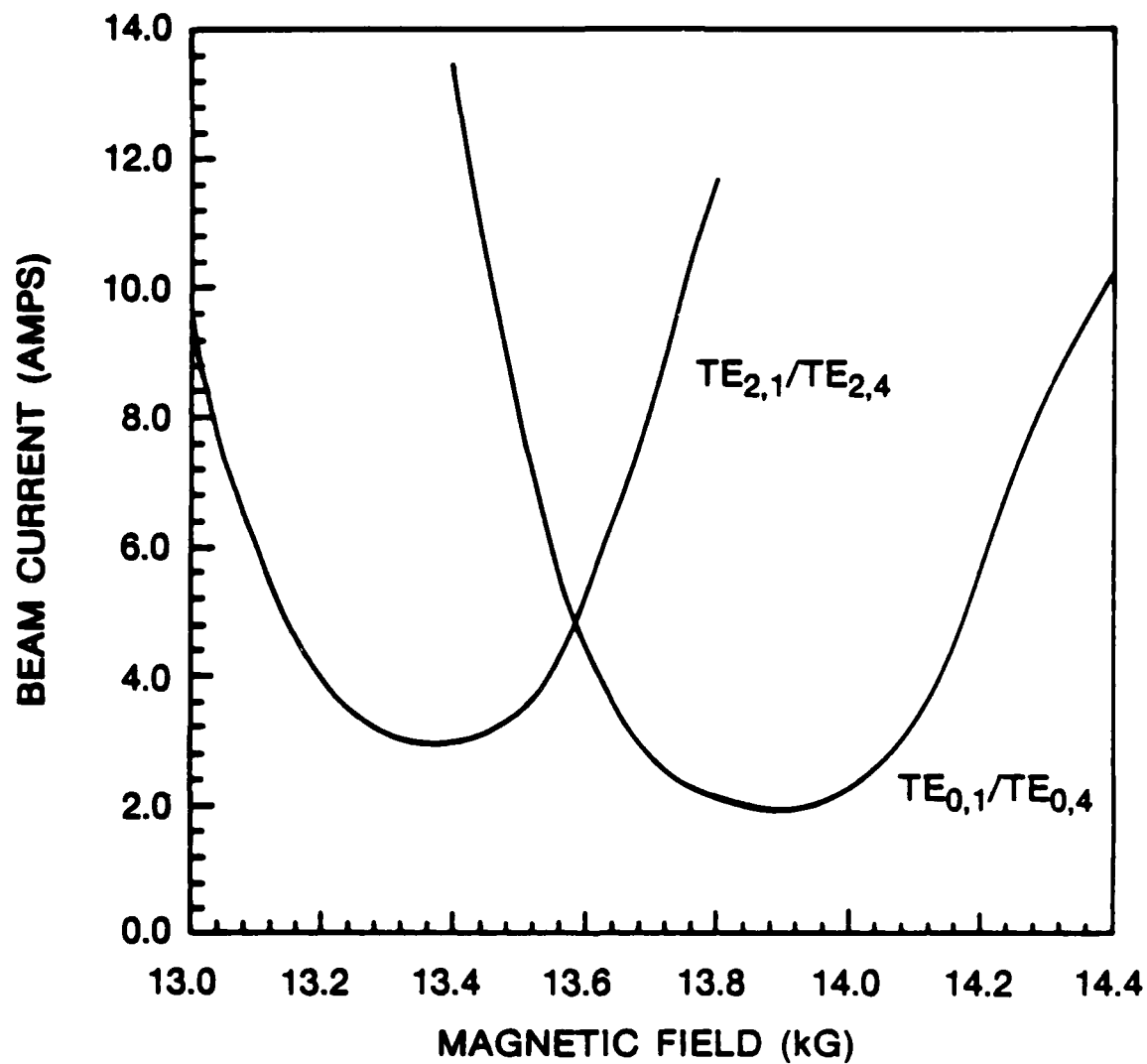


Figure 3. Oscillation threshold currents for for lowest order M=0 and M=2 modes as a function of magnetic field.

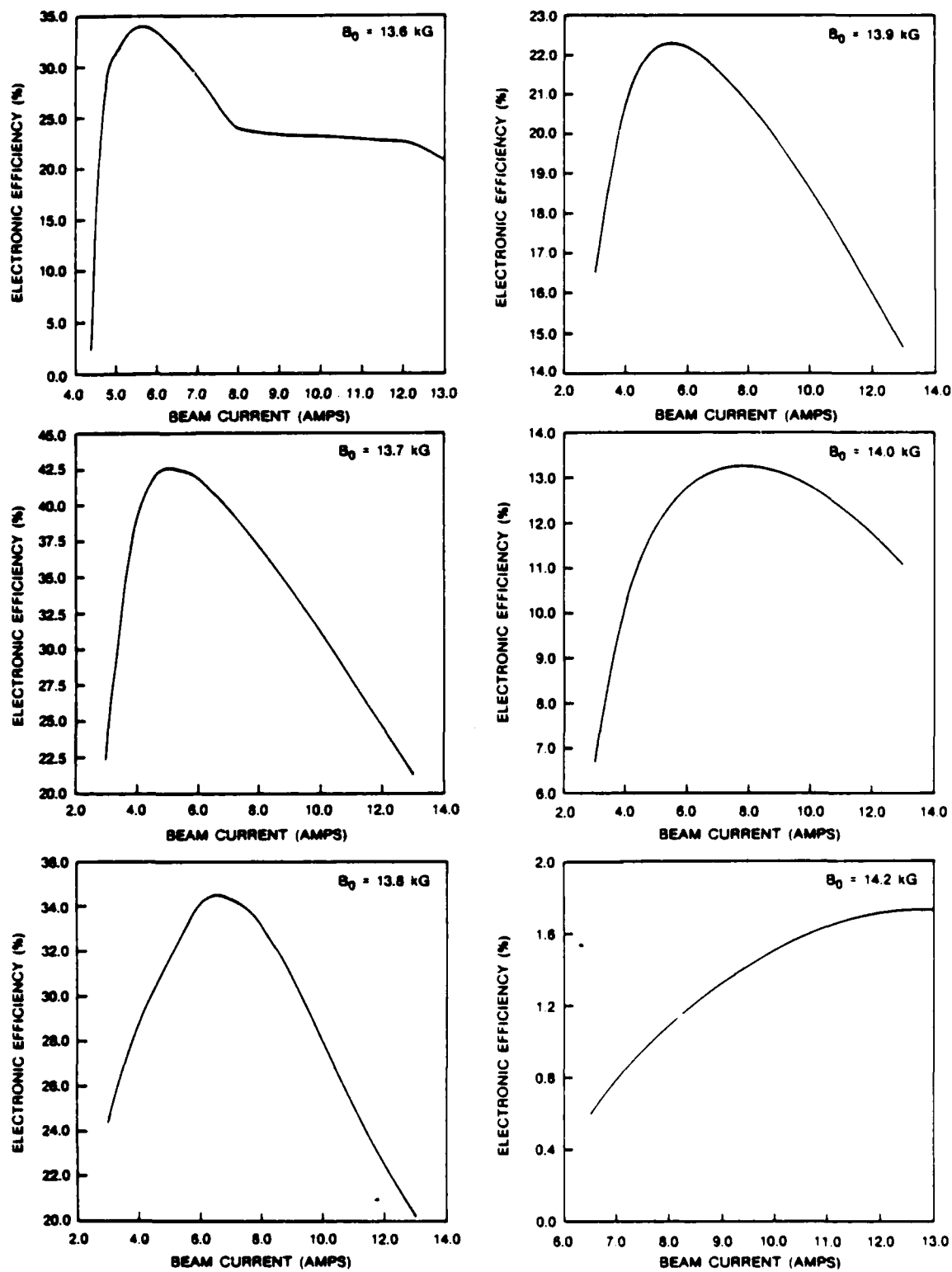


Figure 4. Nonlinear efficiency vs. beam current for the lowest order $M=0$ mode at several values of magnetic field.

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