



2

DTIC FILE COPY

NPS72-87-001CR

NAVAL POSTGRADUATE SCHOOL

Monterey, California

AD-A183 041



DTIC
SELECTED
AUG 0 8 1987
S
K E

CONTRACTOR REPORT

NUMERICAL COMPUTATION OF RING-SYMMETRIC
SPACECRAFT EXHAUST PLUMES

by

Joseph Falcovitz

January 1987

Approved for public release; distribution unlimited.

Prepared for: Strategic Defense Initiative Office
The Pentagon
Washington, DC 20301-7100

NAVAL POSTGRADUATE SCHOOL
Monterey, California

RADM R. C. Austin
Superintendent

D. A. Schrady
Provost

The work reported herein was performed for the Naval Postgraduate School by Dr. Joseph Falcovitz under contract N62271-86-M-0214. The work presented in this report is in support of "Rarefied Gas Dynamics of Laser Exhaust Plume" sponsored by the Strategic Defense Initiative Office/Directed Energy Office. This is a partial report for that contract. The work provides information concerning numerical computation of the flow in spacecraft exhaust plumes. The project at the Naval Postgraduate School is under the cognizance of Distinguished Professor A. E. Fuhs who is principal investigator.

Reproduction of all or part of this report is authorized.

Prepared by:

Joseph Falcovitz

DR. JOSEPH FALCOVITZ
Research Contractor

Reviewed by:

Allen E Fuhs

ALLEN E. FUHS
Distinguished Professor & Chairman
Space Systems Academic Group

Released by:

G. E. Schacher

G. E. SCHACHER
Dean of Science and Engineering

REPORT DOCUMENTATION PAGE

1a. REPORT SECURITY CLASSIFICATION UNCLASSIFIED		1b. RESTRICTIVE MARKINGS NONE	
2a. SECURITY CLASSIFICATION AUTHORITY		3. DISTRIBUTION/AVAILABILITY OF REPORT Approved for Public Release; Distribution Unlimited	
2b. DECLASSIFICATION/DOWNGRADING SCHEDULE			
4. PERFORMING ORGANIZATION REPORT NUMBER(S) NPS72-87-001CR		5. MONITORING ORGANIZATION REPORT NUMBER(S) NPS72-87-001CR	
6a. NAME OF PERFORMING ORGANIZATION JOSEPH FALCOVITZ	6b. OFFICE SYMBOL (If applicable) 72	7a. NAME OF MONITORING ORGANIZATION NAVAL POSTGRADUATE SCHOOL, CODE 72	
6c. ADDRESS (City, State, and ZIP Code) Research Contractor Naval Postgraduate School, Code 72 Monterey, CA 93943-5100		7b. ADDRESS (City, State, and ZIP Code) Space Systems Academic Group Monterey, CA 93943-5100	
8a. NAME OF FUNDING/SPONSORING ORGANIZATION Strategic Defense Initiative Office	8b. OFFICE SYMBOL (If applicable) SDIO/DEO	9. PROCUREMENT INSTRUMENT IDENTIFICATION NUMBER MIPR DGAA60045	
8c. ADDRESS (City, State, and ZIP Code) SDIO/DEO Washington, DC 20301-7100		10. SOURCE OF FUNDING NUMBERS	
		PROGRAM ELEMENT NO. PE63221	TASK NO.
		PROJECT NO. 	WORK UNIT ACCESSION NO.
11. TITLE (Include Security Classification) Numerical Computation of Ring-Symmetric Spacecraft Exhaust Plumes			
12. PERSONAL AUTHOR(S) JOSEPH FALCOVITZ			
13a. TYPE OF REPORT Contractor Report	13b. TIME COVERED FROM Jan 86 TO Aug 86	14. DATE OF REPORT (Year, Month, Day) January 1987	15. PAGE COUNT 54
16. SUPPLEMENTARY NOTATION			
17. COSATI CODES		18. SUBJECT TERMS (Continue on reverse if necessary and identify by block number)	
FIELD	GROUP	SUB-GROUP	
		Laser Exhaust, Exhaust Plume, Method, of Characteristics, Inverse Marching, Ring Plumes	
19. ABSTRACT (Continue on reverse if necessary and identify by block number)			
<p>This report supplements report NPS72-86-003CR, It provides further details about the code JET and the numerical schemes on which it is based: inverse marching characteristic and semi-inverse marching characteristic (SIMA) schemes. The computational procedure is described in some detail. The principles of operation of the code JET are outlined, including a glossary of all major arrays, variables and subroutines. Finally, the full listing of the JET code is reproduced.</p> <p style="text-align: center;">(Keywords)</p>			
20. DISTRIBUTION/AVAILABILITY OF ABSTRACT <input checked="" type="checkbox"/> UNCLASSIFIED/UNLIMITED <input type="checkbox"/> SAME AS RPT <input type="checkbox"/> DTIC USERS		21. ABSTRACT SECURITY CLASSIFICATION UNCLASSIFIED	
22a. NAME OF RESPONSIBLE INDIVIDUAL ALLEN E. FUHS, Distinguished Professor	22b. TELEPHONE (Include Area Code) (408)646-2948	22c. OFFICE SYMBOL 72	

ABSTRACT

This report supplements report NPS72-86-003CR. It provides further details about the code JET and the numerical schemes on which it is based: inverse marching characteristic and semi-inverse marching characteristic (SIMA) schemes. The computational procedure is described in some detail. The principles of operation of the code JET are outlined, including a glossary of all major arrays, variables and subroutines. Finally, the full listing of the JET code is reproduced.

ACKNOWLEDGEMENT

This work was conducted as part of a laser exhaust study under the cognizance of Distinguished Professor Allen E. Fuhs. I deeply appreciate and wish to thank Professor Fuhs for his continuous support and guidance.

Accession For	
DTIC TAB	<input checked="" type="checkbox"/>
Unannounced	<input type="checkbox"/>
Justification	
By	
Distribution/	
Availability Codes	
Avail and/or	
Dist	Special
A-1	



TABLE OF CONTENTS

1.	INTRODUCTION.....	1
2.	THE COMPUTATIONAL SCHEME.....	3
2.1	Riemann Invariants.....	3
2.2	The Integration Scheme for a New Grid Point.....	4
2.3	Boundary Conditions.....	5
2.4	Continuum Breakdown Surface.....	6
3.	THE JET CODE.....	7
3.1	Main Variables.....	7
3.2	Auxiliary Variables.....	8
3.3	Major Parameters.....	10
3.4	Description of JET subroutines.....	12
4.	THE JET CODE LISTING.....	20
5.	REFERENCES.....	45
6.	DISTRIBUTION LIST.....	46

NOMENCLATURE followed by units (if any) and CODE NOTATION (if any)

a	sound speed (m sec ⁻¹)
B	breakdown parameter [5,6,7]
C[±]	characteristic lines inclined at ($\theta \pm \mu$)
D	molecular diameter (hard spheres) (m)
M	Mach number
n	number density (molecules/m ³)
p	pressure (Pa)
S	coordinate along streamlines (m)
u	flow velocity (m/sec)
x	axial cartesian coordinate
y	radial cartesian coordinate
γ	specific-heat ratio (G)
η	length coordinate along fan characteristics (C⁺) (m)
θ	inclination of flow velocity vector
λ_0	mean free path at stagnation conditions (m)
μ	Mach angle ($\sin\mu = 1/M$) (MU)
v	Prandtl-Meyer function (NU)
ξ	length coordinate along transverse (C⁻) characteristic
σ	collision cross-section πD^2 (m ²) (SIGMA)
τ	molecular opacity (expected number of collisions by a fast invading molecule) (XI)
ϕ	collision frequency (sec ⁻¹)
ω	symmetry index (0 - planar flow, 1 - axisymmetric flow) (DELTA)
Γ	the fraction $[(\gamma + 1)/(\gamma - 1)]^{1/2}$
(v + θ)	Riemann invariant along C⁻ (RM)
(v - θ)	Riemann invariant along C⁺ (RP)

INDICES

()₀	a specific point in the CRW (x₀, y₀) (Also : stagnation conditions)
()₁	nozzle exit conditions
()_L	limiting CRW characteristic (p = 0)
()_f	final CRW characteristic (boundary of numerical integration)
()_c	corner of CRW

EMPTY PAGE

1. INTRODUCTION

In a recent report [1] a mixed numerical/analytical approach to the computation of a ring-symmetric spacecraft exhaust plume was presented. The numerical scheme had been implemented in a code named "JET" which is capable of generating whole-plume flow fields, while the analytic approximation is restricted to the ring-symmetric centered rarefaction waves (CRW) that flank the plume. The present report is intended to serve as a supplement to [1] in providing details on the computational scheme and the code JET.

The spacecraft exhaust flow (Fig. 1 of [1]) is idealized as a ring-symmetric steady isentropic expansion of an ideal gas. The nozzle lips are assumed sharp; the supersonic flow from the exit surface of the ring-nozzle is assumed uniform, and the background is considered to be perfect vacuum.

The standard scheme for computing such idealized ring-plumes is the classical (direct) method of characteristics [2]. At a preliminary phase of the present laser exhaust study, a code AXSYM [3] was written for computing ring-plumes using this method. A notorious shortcoming of the direct method of characteristics is that the solution grid is highly irregular, being formed by the (oblique) intersection of the C^+ and the C^- families of characteristic lines. We first encountered a difficulty with this grid while seeking a scheme for integrating the molecular opacity along a straight line [1]. This computation would have required rather complex coding for the geometry of intersection between a straight line and an irregular grid. It seemed preferable to opt for a computation scheme that would produce a more regular grid, even at the expense of some loss of accuracy. Such scheme is the inverse marching method of characteristics [4].

Generally the marching in this type of scheme is in the downstream direction, i.e., the y direction in our case. Grid points are located on a succession of constant- y rows, thereby introducing a measure of regularity in the solution grid. Just two rows have to be stored in the computer core memory - the "old" row and the "new" row, whereas in the direct method of characteristics whole grid-image matrices are required to reside simultaneously in core memory.

The first version of the JET code was based on the inverse marching scheme given by Zucrow and Hoffman (Section 12-5 in [4]), where the flow variables were the *two cartesian velocity components*. The computation seemed accurate everywhere, except within the centered rarefaction wave (CRW). In an attempt to replicate a planar CRW (Prandtl-Meyer flow), the numerical solution exhibited an

instability : Mach number increased along the (low pressure) boundary characteristic line, rather than remain constant.

A *qualitative* explanation for this instability is the following. Flow gradients in a CRW are inversely proportional to distance from the corner, so that the inverse marching scheme gives rise to an amplification of interpolation errors at every marching step, leading to an apparently divergent (unstable) numerical solution. Increasing the order of interpolation from linear to cubic did not eliminate the instability.

Looking for a scheme that would replicate a planar CRW accurately, we tried the modified marching idea as presented by Zucrow and Hoffman for 1-D time-dependent flows (Sections 19-6(a) and 19-6(j) of [4]). In this scheme new grid points are determined by forwardly extending a "primary" family of continuous characteristic lines from old grid points. The primary family in a CRW is the characteristics fanning out from the corner (we assume it is the C^+ family). By choosing this modified scheme, the interpolation for trace points obtained from reversely extended C^+ lines was eliminated. However, the corresponding interpolation for the transverse C^- characteristics remained, and with it the aforementioned instability.

In order to replicate a planar CRW, we had to replace the flow variables by the *Riemann invariants* ($v \pm \theta$). In a C^+ planar CRW, the Riemann invariant ($v + \theta$) is uniformly constant, so that the interpolation in ($v + \theta$) due to reversely extending C^- characteristics introduces no error at all. This scheme, which we named SIMA (Semi Inverse Marching Algorithm), was indeed verified to replicate a planar CRW exactly, when implemented in the code JET.

The plan of this report is the following. In Ch. 2 we supplement the description of the numerical scheme given in Ch. 2 of [1] , by adding more details on the computational procedure. A description of the code JET is given in Ch. 3, and the code listing is reproduced in Ch. 4.

Note on symmetry :

The code JET has two symmetry options. When DELTA = 1 a ring-symmetry is in effect; when DELTA = 0, a planar symmetry is in effect. An axisymmetric jet exiting in the y direction from the same nozzle aperture along the x axis can readily be computed by replacing all terms in the code that correspond to $\sin(\theta)/y$ in the compatibility equations (2.1-1), by $\cos(\theta)/x$. In that case the coding is virtually unchanged, and the only care that should be exercised is for the difference equations for new grid points on or near the y axis. Also, all reference to the analytic approximation of the ring-symmetric CRW [1] should be deleted in this case, as it is designed specifically for ring-symmetry.

2. THE COMPUTATIONAL SCHEME

A basic description of the semi inverse (SIMA) and inverse marching schemes was given in Ch. 2 of [1]. We supplement this description by specifying the slightly modified definition of Riemann invariants in the code, and by giving information about some ancillary computations.

2.1 Riemann Invariants

The compatibility equations whose integration constitutes the numerical solution to the governing equations [1] are expressed in terms of the Riemann invariants as follows :

$$\text{Along } C^+ \quad \dots \quad (v - \theta)_4 = (v - \theta)_2 + \omega \sin\mu_{24} \sin\theta_{24} \Delta\eta / y_{24} \quad (2.1-1)$$

$$\text{Along } C^- \quad \dots \quad (v + \theta)_4 = (v + \theta)_1 + \omega \sin\mu_{14} \sin\theta_{14} \Delta\xi / y_{14}$$

The Riemann invariants $(v \pm \theta)$ are modified for convenience, by adding a constant to both v and θ . The new definitions of $v(M)$ and θ are :

$$v(M) = -\Gamma \arctan(\Gamma q) + \arctan(q)$$

$$q = (M^2 - 1)^{-1/2} \quad (2.1-2)$$

$$\theta \rightarrow \theta - \theta_L$$

Thus, in a Prandtl-Meyer flow with entry Mach number of M_1 , the modified values of both $v(M)$ and θ vanish as $M \rightarrow \infty$. As a consequence, in a C^+ Prandtl-Meyer flow the modified invariant $(v + \theta)$ vanishes uniformly. In this modified form, the computation of M from $v(M)$ is readily done by performing standard Newton-Raphson iterations (in RFUNC), using the derivative :

$$v'(q) = -(\Gamma^2 - 1) [(1 + \Gamma^2 q^2)(1 + q^2)]^{-1} \quad (2.1-3)$$

2.2 The Integration Scheme for a New Grid Point

The integration scheme has been sketched in Ch. 2 of [1]. It is performed in INVMAR for inverse marching points or in SEMINV for semi-inverse marching (SIMA) points. The computational scheme is specified via the following seven-step procedure :

INVMAR (Inverse Marching)

- (a) Grid : At this stage the new grid point has already been defined.
- (b) Predictor : Flow variables are the interpolated (linear nearest-neighbor) value on the old row for a point having the new grid x coordinate (x_4).
- (c) Centered variables : Denote the Riemann invariants by

$$RM = (v + \theta) \tag{2.2-1}$$

$$RP = (v - \theta)$$

then centered values for segments (1,4) and (2,4) (using code notation) are :

$$RM_{14} = (RM_1 + RM_4)/2 \quad RP_{14} = (RP_1 + RP_4)/2 \tag{2.2-2}$$

$$RM_{24} = (RM_2 + RM_4)/2 \quad RP_{24} = (RP_2 + RP_4)/2$$

All other centered flow variables are computed from the centered Riemann invariants by calling RFUNC.

- (d) Inverse Extension : old trace points x_1, x_2 are evaluated from the geometrical relations

$$\text{Along } C^- \quad \dots \quad y_{\text{new}} - y_{\text{old}} = (x_4 - x_1) \tan(\theta_{14} - \mu_{14}) \tag{2.2-3}$$

$$\text{Along } C^+ \quad \dots \quad y_{\text{new}} - y_{\text{old}} = (x_4 - x_2) \tan(\theta_{24} + \mu_{24})$$

- (e) Interpolation : find Riemann invariants RM, RP at old trace points x_1 and x_2 through nearest-neighbor linear interpolation by calling INTERP.
- (f) Integration : Using the compatibility relations in finite-difference form (2.1-1) with segment-centered coefficients, compute iteration-updated values of Riemann invariants at new grid point.

- (g) Corrector : if values of Riemann invariants and old trace points x_1 , x_2 are not sufficiently convergent, resume the procedure at step (c) above.

SEMINV (Semi Inverse Marching - SIMA)

- (a) Grid : New grid point (x_4) is determined as part of the SIMA scheme at step (d) below.
- (b) Predictor : Flow variables are those of point (x_2, y_{old}).
- (c) Centered variables : Identical to step (c) above.
- (d) Semi-Inverse Extension : new grid point x_4 and old trace point x_1 are evaluated from the geometrical relations in Eq. (2.2-3) above.
- (e) Interpolation : find Riemann invariants RM, RP at old trace point x_1 through nearest-neighbor linear interpolation by calling INTERP.
- (f) Integration : Identical to step (f) above.
- (g) Corrector : Identical to step (g) above, except for replacing x_2 in the convergence test by x_4 .

2.3 Boundary Conditions

On the vacuum side the boundary conditions ($p=0$) can only be approximately implemented in a method of characteristics scheme. We do so by ending the computation on a certain "final" C^+ fan characteristic line that starts out with a sufficiently high Mach number M_f at the corner (typically $M_f=3.4$). The marching computation of new grid points on the boundary C^+ characteristic via the SIMA scheme is identical to that of C^+ characteristics within the ring-symmetric CRW. It is noted that under this boundary scheme some outflow takes place through the boundary characteristic line, so that the total mass flow through a row $y = y_{new}$ decreases slightly as y_{new} increases.

At the nozzle exit the boundary conditions are assumed to be uniform outflow in the radial (y) direction with Mach number M_1 . At the nozzle lip, the SIMA integration starts out from a presumed planar CRW (Prandtl-Meyer flow) at the corner (i.e., the associate CRW in the terminology of Ch. 3 in [1]).

At the plane of symmetry ($x=0$) the boundary condition is simply $\theta = \pi/2$. However, this condition is implemented indirectly, by assuming that the flow at virtual grid points with $x < 0$ is a mirror-image of the flow at the corresponding $x > 0$ points. The reason is that when a new grid point of $x_4 = 0$ or of x_4 sufficiently close to zero is considered for inverse-marching integration, the inversely extended trace point (x_1, y_{old}) can be at $x < 0$. Considering the subtraction of θ_L from θ as in Eq.(2.1-2), the reflection rules are :

$$RM \rightarrow RP + (\pi - 2\theta_L) \quad (2.3-1)$$

$$RP \rightarrow RM - (\pi - 2\theta_L)$$

where values on the left and right of the \rightarrow symbol correspond to values left and right of $x=0$. This boundary condition is implemented in INTERP.

2.4 Continuum Breakdown Surface

As an informative option, the code JET can compute (in PLUMES) points on a surface of continuum breakdown [5,6,7], which is defined as a line of constant B , where B is given by :

$$B = -(u/\varphi) \rho^{-1} (d\rho/dS) \quad (2.4-1)$$

$$\varphi = 4(\pi\gamma)^{-1/2} \sigma n a$$

When the standard isentropic relations for ρ and n in terms of M are substituted in (2.4-1), the flow speed is expressed as $u=Ma$ and the streamwise gradient of M is expressed in cartesian coordinates, we get :

$$B = \lambda_0 (\pi\gamma/8)^{1/2} M^2 \left[1 + ((\gamma-1)/2)M^2 \right]^{1/(\gamma-1)-1} \left[M_x \cos\theta + M_y \sin\theta \right] \quad (2.4-2)$$

$$\lambda_0 = (2^{1/2} \sigma n_0)^{-1}$$

Note that the sign of B has been chosen as positive for expansion flows. This definition is preferred to taking an absolute value of the flow gradient, since it assures proper interpolation of B even if its spatial distribution goes through $B=0$.

Due to the dependence of B on a spatial gradient, its numerical evaluation (see BREAK) is attributed to mid-grid points both in x and in y .

3. THE JET CODE

In this chapter we provide a concise description of the JET code according to its version at the time of the JET018 run. This description is intended as an aid in reading the code listing which is given in Ch. 4.

The plan of this chapter is as follows. Array variables that constitute the mainstay of the computational scheme are described in Section 3.1. Auxiliary array variables that are used primarily for processing the information generated by the numerical scheme, are described in Section 3.2, followed in Section 3.3 by a list of major parameters that control the computation (some of them also serve as run data). Finally, all subroutines are listed and described in Section 3.4.

3.1 Main Variables

The array variables used for the computational scheme are organized in two labeled COMMON groups. The first group /VECS/ is designed to hold two grid rows - the old row designated by suffix F and the new row designated by suffix N. The second group /CHARAC/ are characteristic-indexed arrays that hold information about continuous characteristic lines. This characteristic information is used in two ways : it is incorporated in the SIMA computational scheme for the CRW region, and it is used to store data for optional plotting of characteristic lines (see PLUMES and PRINT).

The basic organization is that the new arrays (suffix N) are those in which values are stored during the course of the marching computational procedure. At the end of each marching step, values are transferred from new arrays to old arrays (suffix F); this is done in MOVE. In the array listing below, we indicate in parenthesis the subroutine (or subroutines) in which that new array is defined.

/VECS/

XN(I)	x coordinate of grid point I. (GRIDN)
RMN(I)	modified Riemann invariant ($v + \theta$) at grid point I. (BEGIN, INVMAR, LOADC).
RPN(I)	modified Riemann invariant ($v - \theta$) at grid point I. (BEGIN, INVMAR, LOADC).
MN(I)	Mach number at grid point I (BEGIN, INVMAR, LOADC).
MUN(I)	Mach angle μ at grid point I. (BEGIN, INVMAR, LOADC).
TETAN(I)	true (unmodified) flow angle θ at grid point I. (BEGIN, INVMAR, LOADC).

BN(I) value of breakdown parameter **B** at point I-1/2 (and at half a marching step back in **y** as well). (BREAK).

XTEMP(I) used for auxiliary computation of I-1/2 grid points in PLUMES.

/CHARAC/

XCHARN(KC) **x** coordinate of point on characteristic line number KC. (BEGIN, SEMINV, PLUMES).

YCHARN(KC) **y** coordinate of point on characteristic line number KC. (BEGIN, SEMINV, PLUMES).

RMCARN(KC) modified Riemann invariant ($v + \theta$) of point on characteristic line number KC. (BEGIN, SEMINV).

RPCARN(KC) modified Riemann invariant ($v - \theta$) of point on characteristic line number KC. (BEGIN, SEMINV).

TCHARN(KC) true (unmodified) flow angle θ at point on characteristic line number KC. (BEGIN, SEMINV).

MUCARN(KC) Mach angle μ at point on characteristic line number KC. (BEGIN, SEMINV).

CSIGNN(KC) sign of characteristic line number KC. It has value 1 for C^+ and value -1 for C^- . Note that upon reflection of a C^+ line from the symmetry plane ($x=0$), the sign value is changed from 1 to -1. (BEGIN, SEMINV).

MCHARN(KC) Mach number at point on characteristic line number KC. (BEGIN, SEMINV).

MCHARI(KC) Mach number at Prandtl-Meyer's fan characteristic number KC at the corner. It is defined initially and is not changed during the run. (BEGIN).

3.2 Auxiliary Variables

In addition to the major arrays mentioned above, there are several groups of auxiliary arrays that do not affect the computational scheme, but are intended for informative processing of the results. These groups are /PLUME/, /IPLUME/, /THICKY/, /THICKX/, /GRP/. /PLUME/ is used to preserve points on special lines for later plotting (in a separate code). /THICKY/ and /THICKX/ are for storing values of radial (**y**) and lateral (**x**) molecular opacities. The group /GRP/ is used in conjunction with comparative computation of the ring-symmetric CRW flow according to the analytic approximation [1].

/PLUME/ (PLUMES, PRINT)

XPL(J,IPL) x coordinate at marching step J of special line number IPL.
YPL(J,IPL) y coordinate at marching step J of special line number IPL.

/IPLUME/ (PLUMES, PRINT)

KPL number of special lines computed in PLUMES.
ITYPL(IPL) index indicating the type of special line number IPL.

/THICKY/ (OPACY, PRINT)

XTH(J) x coordinate on boundary characteristic line at marching step J, from which radial opacity is integrated.
TH(J) radial opacity computed by y-integration from the boundary point defined by XTH(J) (up to current YN).

/THICKX/ (OPACX, PLUMES, PRINT)

YXI(JXI) y coordinate of printed row number JXI (the index JXI counts just rows that have been printed). The row to be printed next upon calling PRINT is the row having YF near YXI(JXI).
XI(I,JXI) lateral (x) molecular opacity [I] at point XF(I), for printed row JXI. It is obtained by numerically integrating the solution obtained from the JET computation (see OPACX).
XIPM(I,JXI) same as XI(I,JXI) except that the Prandtl-Meyer solution is used to estimate the flow at grid points XF(I).
XIGRP(I,JXI) same as above, except that the analytic approximation to a ring-symmetric CRW [I] is used to estimate the flow at grid points XF(I).
XIAPP(I,JXI) same as XIGRP(I,JXI) except that the numerical integration is replaced by an approximate closed-form expression [I].
XIF(I,JXI) stores grid points XF(I) of printed row JXI.

/GRP/ (PRINT, HMSET, MFUNC, HINTER, MATCH)

DMINV increment of inverse Mach number for array MHINV(I).
MHINV(I) inverse Mach number array (from 0 to 1/MEXIT), from which the H(M) function can be evaluated (HMSET).
HMOV(I) values of the H(M) function evaluated by numerical integration. It is used to compute this function by interpolation. (HMSET, HINTER).

3.3 Major Parameters

Parameters that define and control a particular run (such as the maximum y for the marching computation, the number of grid points on a row and many more) are defined in INIDAT. (The code JET has no input file and no READ statements). The major control parameters are grouped in /PAR/ (floating point) and in /IPAR/ (integers); thermodynamic data are grouped in /STAG/.

We indicate in the listing the subroutines in which the labeled COMMON group or a particular parameter is defined (or sometimes referred to).

/PAR/ (INIDAT)

MEXIT	nozzle exit Mach number (M_1).
MFIN	Mach number of the final (boundary) CRW characteristic at the corner (M_p).
YMAX	maximum value of y for the marching scheme. When YF.GE.YMAX the run is terminated.
DY0	initial marching step.
DY	current marching step.
DYNEXT	next marching step (YSTEP).
STAB	stability coefficient for marching step (STAB.LE.1). (See YSTEP).
DELTA	symmetry index. DELTA = 0 for plane symmetry; DELTA = 1 for ring-symmetry.
PSI1	angle of Prandtl-Meyer fan characteristic at exit conditions (measured from x axis).
PSIF	angle of final (boundary) Prandtl-Meyer fan characteristic.
SIGMA	collision cross-section (σ).
FRACG	the number of intervals initially allocated to the CRW fan is a FRACG fraction of the total number of intervals (KF0-1). (see BEGIN).
EPSIL	convergence parameter (small number). (INVMAR, SEMINV).
TETLIM	flow angle (from x axis) of the limiting ($p = 0$) velocity vector of the flow at the lip-centered Prandtl-Meyer fan.
TETSYM	PAI-2*TETLIM for reflection transformation (see INTERP).

/IPAR/ (INIDAT)

JMAX	maximum number of marching steps. If J.GE.JMAX run is terminated.
KF0	initial (and maximum) number of grid points in a row.
KF	current number of grid points in the old row.
KN	current number of grid points in the new row.

ITER0 maximum number of iterations for the integration of the compatibility relations (see INVMAR and SEMINV; also used in RFUNC, PLUMES).
IM, IP search indices for interpolation subroutine INTERP. (see INVMAR, SEMINV).
J current row index (also index of a marching step).
KF2 defined as $2 * KF$; not used in present version.
IDEL, JDEL increments for printing grid point I and row J (see PRINT).
JYXI number of rows to be printed in a run.
JXI index of printing row, to be printed next (see PRINT).
ILEAD index I at the first grid point on current new row, where the SIMA integration commences. Initially this point corresponds to the leading characteristic of the CRW. (see GRIDN, BEGIN).
ILEADF value of ILEAD for current old row.
KCLEAD index in the characteristic array for the characteristic line that corresponds to the new grid point $I = ILEAD$ (see GRIDN). Initially $KCLEAD = 1$.

/STAG/ (INIDAT)

RHO0, N0 stagnation density and number density.
P0, T0, A0 stagnation pressure, temperature and sound speed.
MDOT1 mass flow rate from ring-nozzle (only from the $x > 0$ half). (See PRINT).

/ICHA/ (BEGIN)

KCHARP number of C^+ characteristic lines for which data is stored (either for SIMA computation or for subsequent plotting).
KCHARM number of C^- characteristic lines for which data is stored (only for subsequent plotting).
KCHAR0 total number of characteristics for which data is stored, i.e., $KCHAR0 = KCHARP + KCHARM$.

3.4 Description of JET subroutines

MAIN PROGRAM

The main program performs two functions. The first section (up to statement 1) is the initial set up; it is performed just once. The second section is the marching loop with the step index J. This program can be read as a flow chart of the overall computational procedure.

INIDAT is for setting up run data. In BEGIN the initial conditions for the marching computation are set up. A single marching step is performed by calling MARCH, and the loading of new row vectors into old row vectors is done by calling MOVE. The call to YSTEP is for the first computed marching step. All remaining calls are for informative tasks (see HMSET, BREAK, OPACY, PLUMES, PRINT). Run is terminated when either YF.GE.YMAX or when J.GE.JMAX.

NOTE ON EXEC : The only special feature in the EXEC is retaining the output unit 7 file for optional post-plotting. The printed output (unit 6) is the system's standard (default).

INIDAT

Initial data definition and preliminary data computations. The data is defined by statements rather than by reading an input file. The meaning of major parameters was described in Section 3.3 above. User is invited to modify the data definitions, particularly of run-control parameters such as YMAX, JYXI and YXI(JXI) (for printing JYXI selected rows).

BEGIN

Here all initial values (prior to beginning of marching schemes integration) are loaded into all major computational arrays (Section 3.1). Also, values of the key integer parameters KCHARP, KCHARM, KCHAR0, ILEAD, KCLEAD and KF are defined.

In the first loop (loop 1) we define an initial family of C^+ characteristic lines for the lip-centered CRW, by storing the Mach number of the Prandtl-Meyer fan characteristics in the array

MCHARI(KC). Note that the fan characteristics are generated at equal RP intervals, since the flow variables are RM and RP. However, a different division might also be acceptable.

The next step is the definition of initial values for all characteristic arrays, first the C^+ arrays (loop 2), then the C^- arrays (loop 21). The C^- characteristic lines are needed just for informative output (post-plotting), so the present version contains just one C^- line. The user may modify that.

The remaining grid points (altogether KF0 grid points are initially available) are uniformly distributed across the nozzle opening, and the row arrays are loaded with the corresponding nozzle-exit flow variables (loop 3).

PRINT

The main task of this subroutine is the printing of flow variables at grid points of selected rows. The printing of a row is selected when YF is close to a predefined array YXI(JXI). Following the printing, JXI is updated by adding 1.

For comparison, additional flow variables are printed for each row. These are computed from the analytic approximation to a ring-symmetric CRW [1], by calling MATCH. Also, lateral molecular opacities of various kinds of approximation are computed by calling OPACX, and are printed for each grid point within the CRW.

Following the row printing (statement 120), arrays intended for post-processing (plotting of special lines) are printed and subsequently written on output unit 7. This is done once per run, just before run termination.

FIN

This subroutine is called when an error is encountered, in order to terminate the run. Note that the run is terminated by deliberately introducing an error of computing SQRT(-1), which is done in order to trigger the printing of calling sequences by the operating system.

MARCH

This subroutine performs a single marching step by calling the proper computational subroutines at an appropriate sequence. It can be read as a flow chart of the entire computational scheme. First the segment of the new row suitable for SIMA computation is calculated by calling SEMINV. Then new grid points for that part of the new row for which inverse marching integration is to be performed, are generated by calling GRIDN. The results of the SEMINV computation, which were stored in characteristic arrays, are now loaded into row arrays by calling LOADC. Finally, the computation of the new row is completed by calling INVMAR which computes the flow at the remaining grid points by the inverse marching scheme.

INVMAR

This is one of the two central subroutines for computing the flow at new grid points (the other is SEMINV). Here the inverse marching scheme is used. The computational procedure follows the seven-step description given in Section 2.2 above. Note that the initial value of the search indices IM and IP is not redefined at each call to INTERP, since it is assumed that IM and IP do not change much at consecutive calls to INTERP, so that search efficiency is enhanced by not starting the search from an arbitrary point (such as either end of the row).

SEMINV

This is the subroutine performing the SIMA scheme for computing the flow at new grid points located along continuous characteristic lines of the lip-centered CRW (at prescribed y-marching steps). The essence of the computational procedure of this subroutine was given as a seven-step description in Section 2.2. The same remark about IM given in the preceding INVMAR description applies here as well.

The main loop (100) is over all characteristic lines, including some C^- lines in addition to the C^+ lines. Thus, the array CSIGNF(KC) is used to get the appropriate expressions for either C^+ or C^- characteristics. It is noted that while normally the characteristic segments through points 1 and 2 are C^- and C^+ respectively, this is reversed when a C^- rather than a C^+ line is computed via the SIMA scheme. In this case, which is characterized by having CSIGNF(KC).LT.0, the Riemann

invariants integrated along segments (1,4) and (2,4) are interchanged. This is done in the few statements just preceding and following statement 21.

An additional capability of this subroutine is to treat a change of a C^+ characteristic line into a C^- line upon reflection from the symmetry plane ($x=0$). This is done by first computing a new grid point having $X4.LT.0$, and then changing its sign after setting $CSIGNN(KC) = -1$ (statements just preceding statement 30). It is also possible to skip the computation of a particular characteristic by setting $CSIGNN(KC)=0$. This feature is not exploited in the present version.

Finally, we note that not all characteristic lines computed here are part of the marching flow computation. Only those with indices KC between $KCLEAD$ and $KCHARP$ are. All other characteristic lines are computed just for informative purposes (post-plotting).

RFUNC

Here M , MU , $TETA$ are computed from the two Riemann invariants RM , RP . The computation of M is performed by a Newton-Raphson iteration using Equations (2.1-2) and (2.1-3) given in Section 2.1 above.

INTERP

This subroutine starts by finding through a search procedure the grid interval ($I, I+1$) that contains a given point X . Then the Riemann invariants are computed for this point by linear interpolation, and returned in RM , RP . Note that X may be negative, which accounts for the relatively elaborate search logic in the determination of I , and for the reflection transformation (as in Eq. (2.3-1) above) preceding the last two statements of the subroutine.

INTERX

This interpolation routine performs an inverse task to that of `INTERP`, in that it finds the point $X0$ that corresponds to a given linearly interpolated value of the flow variable $VAR0$. It is used in `PLUMES` to compute the location of a breakdown surface point on a new row of x -centered and y -centered grid points

BREAK

This subroutine computes the new breakdown parameter array $BN(I)$. The computation is based on the description given in Section 2.4 above.

OPACY

Here the radial (Y) molecular opacity array $TH(J)$ is computed. At each marching step J , a new boundary grid point $XTH(J)$ is added, then the radial opacities at all preceding boundary points are updated by adding the contribution of the gas layer between the current old and new rows. Note that since grid points on adjacent rows are not located on equal- X columns, this procedure requires X -interpolation by calling `INTERP`.

PLUMES

This is a user-defined subroutine, where up to 10 special lines can be computed and subsequently retained on output unit 7 for post-processing (plotting). The type of the line $ITYPL(IPL)$ and a parameter $VPL(IPL)$ that defines the line, are computed through user-inserted statements in the section preceding statement 2000. Then an additional point on the current new row is computed for each line type. The available types are clearly stated in comments. Note that characteristic lines have already been computed in `SEMINV` using the `SIMA` scheme, regardless of whether they are part of the solution grid to the flow field, or are just computed for informative purpose. It is the user's choice which of these lines (if any) are to be saved in the `/PLUME/` arrays for subsequent post-processing (plotting).

GRIDN

This subroutine computes the grid points in that segment of the new row for which the flow is computed by the inverse marching scheme (in `INVMAR`). Initially, this segment extends from $x=0$ to the new row grid point which lies on the leading characteristic of the lip-centered CRW. However, since the leading characteristic is reflected from the symmetry plane ($x=0$) at some point, this segment steadily shrinks in size as the marching proceeds. The remedy is to declare the next-to-the-

leading characteristic line ($KC = 2$) as the beginning of the segment for SIMA integration, by setting $KCLEAD = 2$. This process of increasing $KCLEAD$ is repeated whenever it is deemed necessary. The criterion in the present version for the minimal $KCLEAD$ is that the inverse-marching segment should be at least twice $DX1$ - the average CRW grid interval (loop 1, the two statements following $DX1 = \dots$). Also, $ILEAD$ is redefined for each row according to $XLEAD/DX1 + 2$ in order to achieve a row of relatively uniform grid intervals throughout. The result is that the number of grid points in a row is initially $KF0$, but eventually it decreases due to both increase of $KCLEAD$ and decrease of $ILEAD$.

YSTEP

In this subroutine the next marching step $DYNEXT$ is computed at the end of the current marching step. It is defined as the smallest step obtained by forward intersection of C^- and C^+ characteristics from adjacent grid points. Note that the actual value of $DYNEXT$ is reduced by a "stability" factor $STAB$, and that $\dot{D}Y$ is also limited by the growth-rate factor DDY and by $DYMAX$ (see MAIN PROGRAM).

MOVE

Here old row arrays (loop 1) and old characteristic arrays (loop 2) are loaded with values of flow variables from corresponding new arrays, in preparation for the next marching step. As a result of this organizational feature, informative computations (e.g. $BREAK$, $OPACY$) that require both new and old rows, have to be performed prior to calling $MOVE$.

OPACX

Here lateral (X) opacities that correspond to the number of expected collisions of a fast molecule invading the CRW in the $-X$ direction, are computed. All opacities, except $XIAPP(1)$, are computed by numerical integration. In loop 1 we compute the opacity contribution of the segment lying just outside the computational boundary characteristic ($MFIN$), assuming a Prandtl-Meyer flow. This additional opacity is denoted $XI0$. If the flow is ring-symmetric, $XI0$ is recalculated using the analytic approximation [1] to estimate the flow field at the fringes of the ring-symmetric CRW (see also the closed form expression for τ in [1]).

The computation of opacity arrays starts after statement 14. First, the opacity at each grid point is set to XI0. Thus, even though the numerical flow computation does not include the fluid outside the boundary characteristic line, the opacity integration includes an estimate of that "missing" part, i.e., of XI0. In typical case computations of a ring-symmetric CRW [1] we found that the maximum value of XI0 was about 0.16., which indicated that as far as interaction with invading ambient molecules is concerned, the approximation $MFIN = 34$ was a reasonable substitute for $MFIN = \infty$.

The next step is the computation by numerical integration of three approximations to the lateral opacity : XI(I,JXI), XIPM(I,JXI), XIGRP(I,JXI). (Note that when the flow is ring-symmetric, the approximation XIPM(I,JXI) obtained by assuming a Prandtl-Meyer flow is usually grossly exaggerated). The opacity XIGRP(I,JXI) is based on the analytic approximation to a ring-symmetric CRW [1] , and is reasonably close to XI(I,JXI) which is obtained from the numerical solution to the flow field. Finally, a simplified closed-form integration of lateral opacity [1] is computed as XIAPP(I,JXI) (loop 3). Thus, the quantitative difference between XI(I,JXI) and XIGRP(I,JXI) is an indication to the degree of accuracy achieved by the analytic approximation to a ring-symmetric CRW [1] , while the difference between XIGRP(I,JXI) and XIAPP(I,JXI) indicates the level of error introduced by the closed-form integration of lateral opacity [1] .

LOADC

Here flow variables of new grid points computed via the SIMA scheme (SEMINV) are loaded into new row arrays from corresponding characteristic arrays.

NUFUNC

This function computes the modified $v(M)$ value as given by Eq. (2.1-2). Note that presently $NU0 = 0$ (see INIDAT).

HMSET

This subroutine is called just once from the MAIN PROGRAM. Its task is to set up the arrays in /GRP/, so that the function $H(M)$ [1] can be evaluated by interpolation (in HINTER). There is also an informative printout of various derivatives (see Ch. 3 of [1]) generated in this subroutine.

MFUNC

This subroutine is called by HMSET in order to compute functions of Mach number that serve in the computation of $H(M)$. The output variable F is the integrand for the integration leading to $H(M)$.

HINTER

This subroutine computes $H(M)$ by linear interpolation in inverse Mach number, using the /GRP/ arrays computed in HMSET.

MATCH

This subroutine is called from PRINT to compute the Mach number according to the analytic approximation of a ring-symmetric CRW [1], for point $(YF, XF(I))$. $M0B$ is the associate Mach number $M(0, \beta)$, which is preserved in the array MCHARI(KC) for all CRW characteristics that are used in the SIMA computation. Hence the Mach number $M(\alpha, \beta)$, denoted by MAB can be computed directly from the analytic approximation [1] to the area function at $(YF, XF(I))$ by calling AREAF. Since typically $M(0, \beta)$ is not known, we also compute the Mach number via the inverse-problem procedure [1], denoting the resulting Mach numbers by suffix I: $M0BI$ for $M(0, \beta)$ and $MABI$ for $M(\alpha, \beta)$. The inverse-problem iterative procedure [1] is performed in loop 1, resulting in $M0BI$. From $M0BI$ the value of $MABI$ is computed through the area function approximation as for MAB above.

AREAF

This subroutine computes the Mach number M that corresponds to the area function F (Eq. (3.2-1) of [1]). The computation is done by Newton-Raphson iterations, and it has been found to converge when $M.GT.1$ (and when $M - 1$ is not much smaller than 1).

4. THE JET CODE LISTING

```

C#OPTIONS LIST
C JET018 JET0001
C "JET" A SEMI-INVERSE MARCHING CHARACTERISTICS METHOD FOR RING JETS. JET0002
C USING RIEMANN INVARIANTS RM=(NU+TETA), RP=(NU-TETA) AS FIELD JET0003
C VARIABLES. JET0004
  IMPLICIT REAL*8(A-H,L-Z,*) JET0005
  REAL*4 XPL,YPL JET0006
  COMMON /PLUME/XPL(1002,10),YPL(1002) JET0007
  COMMON /IPLUME/KPL,ITYPL(10) JET0008
  COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101), JET0009
1   TETA(101),BF(101), JET0010
2   XN(101),RMN(101),RPN(101),MN(101),MUN(101), JET0011
3   TETAN(101),BN(101),XTEMP(101) JET0012
  COMMON/THICKY/XTH(1002),TH(1002) JET0013
  REAL*4 YXI,XI,XIPM,XIGRP,XIAPP,XIF JET0014
  COMMON /THICKX/YXI(20),XI(101,20),XIPM(101,20),XIGRP(101,20) JET0015
1   ,XIAPP(101,20),XIF(101,20) JET0016
  COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15, JET0017
1   G16,G17,G18,G19,G20 JET0018
  COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT, JET0019
1   STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO, JET0020
2   TETSYM,TETLIM,DDY,DYMAX JET0021
  COMMON /STAG/RH00,NO,P0,T0,A0,MDOT1 JET0022
  COMMON /IPAR/JMAX,KFO,ITER0,KF,KN,IM,IP,J, JET0023
1   KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD JET0024
  COMMON /ROW/YF,YN,DXF,DXN JET0025
  COMMON /CHARAC/XCHARF(92),YCHARF(92),XCHARN(92),YCHARN(92), JET0026
1   RMCARF(92),RPCARF(92),RMCARN(92),RPCARN(92), JET0027
2   TCHARF(92),TCHARN(92),MUCARF(92),MUCARN(92), JET0028
3   CSIGNN(92),CSIGNF(92),MCHARN(92),MCHARF(92), JET0029
4   MCHARI(92) JET0030
  COMMON /ICHARA/KCHARP,KCHARM,KCHARO JET0031
  COMMON /GRP/DMINV,MHINV(101),HMV(101) JET0032
  COMMON /IGRP/KHM JET0033
C JET0034
101 PRINT 101 JET0035
  FORMAT('1') JET0036
  J=1 JET0037
  IF(J.EQ.1) STOP JET0038
  CALL INIDAT JET0039
  PRINT 101 JET0040
  CALL HMSET JET0041
  PRINT 101 JET0042
  CALL BEGIN JET0043
  CALL MARCH JET0044
  CALL OPACY JET0045
  CALL PLUMES JET0046
  CALL PRINT JET0047
  J=2 JET0048
  CALL PLUMES JET0049
  CALL MOVE JET0050
  CALL OPACY JET0051
  CALL PRINT JET0052
  CALL YSTEP JET0053
1 J=J+1 JET0054
C DY WAS DETERMINED BY THE PREVIOUS CALL TO GRIDN. JET0055
  DY=DMINI(DYNEXT,DY*DDY,DYMAX) JET0056
C INTEGRATE BY ONE Y-STEP JET0057
  CALL MARCH JET0058
C BREAKDOWN PARAMETER (BF(I)). JET0059
  CALL BREAK JET0060
C SPECIALLY DESIGNATED LINES (FOR PLOTTING). JET0061
  CALL PLUMES JET0062
C STORE NEW LINE (N) IN OLD LINE (F). JET0063
  CALL MOVE JET0064
C COMPUTE RADIAL MOLECULAR OPACITIES JET0065
  CALL OPACY JET0066
C Y-STEP IS VARIABLE, SO JMAX IS USED AS END-OF-RUN CRITERION. JET0067
  IF(YF.GE.YMAX) JMAX=J JET0068
C PRINT FIELD AT MOST RECENT Y. JET0069
  CALL PRINT JET0070
C NEXT Y-STEP. JET0071
  JET0072

```

	CALL YSTEP	JET0073
	IF(J.LT.JMAX) GO TO 1	JET0074
	STOP	JET0075
	END	JET0076
		<i>IN/DAT</i>
	SUBROUTINE INIDAT	JET0077
C	SUBROUTINE NUMBER 1	JET0078
	IMPLICIT REAL*8(A-H,L-Z,*)	JET0079
	COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),	JET0080
1	TETAF(101),BF(101),	JET0081
2	XN(101),RMN(101),RPN(101),MN(101),MUN(101),	JET0082
3	TETAN(101),BN(101),XTEMP(101)	JET0083
	COMMON/THICKY/XTH(1002),TH(1002)	JET0084
	REAL*4 YXI,XI,XIPM,XIGRP,XIAPP,XIF	JET0085
	COMMON /THICKX/YXI(20),XI(101,20),XIPM(101,20),XIGRP(101,20)	JET0086
1	,XIAPP(101,20),XIF(101,20)	JET0087
	COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,	JET0088
1	G16,G17,G18,G19,G20	JET0089
	COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,	JET0090
1	STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NU0,	JET0091
2	TETSYM,TETLIM,DDY,DYMAX	JET0092
	COMMON /STAG/RH00,NO,PO,TO,A0,MDOT1	JET0093
	COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J,	JET0094
1	KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD	JET0095
	COMMON /ROW/YF,YN,DXF,DXN	JET0096
C		JET0097
	PAI=4.D0*DATAN(1.D0)	JET0098
	PAI2=2.D0*DATAN(1.D0)	JET0099
	DEG=180.D0/PAI	JET0100
	AR=8.3143D3	JET0101
	AV=6.022D 26	JET0102
	AW=7.27D0	JET0103
	RH00=0.0075D0	JET0104
	TO=2300.D0	JET0105
	G=1.54D0	JET0106
	D=2.5D-10	JET0107
	MEXIT=4.D0	JET0108
	MFIN=34.D0	JET0109
	XC=0.5D0	JET0110
	YC=2.5D0	JET0111
C	DELTA=0 CORRESPONDS TO PLANE SYMMETRY	JET0112
C	DELTA=1 CORRESPONDS TO CYLINDRICAL SYMMETRY	JET0113
	DELTA=1.D0	JET0114
	FRACG=0.6D0	JET0115
	EPSIL=1.D-8	JET0116
	ITER0=20	JET0117
	KF0=101	JET0118
	JMAX=1001	JET0119
	STAB=0.50D0	JET0120
	DDY=1.05D0	JET0121
	DYMAX=0.5D0	JET0122
	YMAX=50.D0	JET0123
	DY0=YC/250.D0	JET0124
	IDEL=1	JET0125
	JDEL=1	JET0126
C	POINTS FOR PRINTING FLOW FIELD AT YF=YXI(JXI)	JET0127
	JXI=1	JET0128
	JYXI=11	JET0129
	DYXI=5.D0	JET0130
	YXI(1)=YC+0.5D0	JET0131
	YXI(2)=YXI(1)+2.D0	JET0132
	I0=2	JET0133
	DO 1 I=I0,JYXI	JET0134
	YXI(I)=YXI(I0)+DYXI*DFLOAT(I-I0)	JET0135
1	CONTINUE	JET0136
	IF(KF0.GT.101) CALL FIN(101)	JET0137
	IF(JMAX.GT.1001) CALL FIN(102)	JET0138
	IF(FRACG.GT.1.D0 .OR. FRACG.LT.0.) CALL FIN(103)	JET0139
	IF(JYXI.GT.20) CALL FIN(104)	JET0140
	IF(DELTA*(1.D0-DELTA).NE.0.) CALL FIN(105)	JET0141
	NO=RH00*AV/AW	JET0142
	A0=DSQRT(G*AR*TO/AW)	JET0143
	PO=AR*RH00*TO/AW	JET0144

```

SIGMA=PAI*D**2
LAMDA0=1.D0/(DSQRT(2.D0)*SIGMA*NO)
G1=(G-1.D0)/2.D0
G2=(G+1.D0)/(2.D0*(G-1.D0))
G3=G/2.D0
G4=(G+1.D0)/(G-1.D0)
G5=DSQRT((G+1.D0)/(G-1.D0))
G6=1.D0/(G-1.D0)
G7=2.D0/(G+1.D0)
G8=(0.5D0*(G+1.D0)**2/(G-1.D0))*((1.D0/(G+1.D0))*
1 ((G+1.D0)/(G-1.D0))*((G-1.D0)/(G+1.D0))
G9=(G+3.D0)/(2.D0*(G-1.D0))
G10=(7.D0-3.D0*G)/(2.D0*(G-1.D0))
G11=(2.D0/(G+1.D0))*((1.D0/(G-1.D0))
G12=DSQRT((G+1.D0)/(G-1.D0))-1.D0
G13=(2.D0-G)/(2.D0*(G-1.D0))
G14=G/(2.D0*(G-1.D0))
G15=(G+1.D0)/(3.D0-G)
G16=(G+1.D0)/4.D0
G20=LAMDA0*DSQRT(PAI*G/8.D0)
ZETA1=G5*DATAN(DSQRT(MEXIT**2-1.D0)/G5)
AMU1=DARSIN(1.D0/MEXIT)
PSI1=PAI2+AMU1
ZETA1=G5*DATAN(DSQRT(MFIN**2-1.D0)/G5)
PSIF=PSI1+ZETA1-ZETA1
NU0=0.
TETLIM=NUFUNC(MEXIT)+PAI2-NU0
PSILIM=TETLIM
TETSYM=PAI-2.D0*TETLIM
GOREM=1.D0+G1*MEXIT**2
RH01=RH00/GOREM**G6
V1=MEXIT*AO/DSQRT(GOREM)
P1=P0/GOREM*(G/(G-1.D0))
T1=T0/DSQRT(GOREM)
YYC=2.D0*PAI*YC
IF(DELTA.EQ.0.) YYC=1.D0
MDOT1=YYC*XC*RH01*V1
C
PRINT 21,AR,AV,AW,G,RH00,NO,P0,T0,A0,D
21 FORMAT(/1X,'THERMODYNAMIC DATA: '/
1 1X,'AR,AV,AW,G=',2X,2D14.5,2F9.3/
2 1X,'RH00,NO,P0,T0,A0,D=',6D13.5)
PRINT 22,XC,YC,MEXIT,RH01,P1,T1,V1,MDOT1,PSI1*DEG,PSIF*DEG,
1 PSILIM*DEG
22 FORMAT(/1X,'CORNER DATA: XC,YC=',2F9.2/
1 1X,'EXIT CONDITIONS: ',
2 2X,'MEXIT,RH01,P1,T1,V1,MDOT1=',F9.3,5D13.4/
3 1X,'CENTERED FAN LIMITS: ',
4 2X,'PSI1,PSIF,PSILIM=',3F10.3)
PRINT 23,DELTA,KF0,JMAX,ITER0,DY0,YMAX,STAB,DDY
23 FORMAT(/1X,'INTEGRATION DATA. SYMMETRY INDEX: DELTA=',F4.1/
1 1X,'NUMBER OF POINTS IN X AND Y DIRECTIONS: KF0,JMAX=',
2 2I5/
3 1X,'MAX. NUM. OF ITERATIONS ITER0=',I5/
5 1X,'INITIAL Y-STEP AND MAXIMUM Y: DY0,YMAX=',2D14.5/
6 1X,'Y-STEP STABILITY FACTORS STAB,DDY=',2F7.3)
RETURN
END
SUBROUTINE BEGIN
C SUBROUTINE NUMBER 2
IMPLICIT REAL*8(A-H,L-Z,$)
COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),
1 TETA1(101),BF(101),
2 XN(101),RMN(101),RPN(101),MN(101),MUN(101),
3 TETAN(101),BN(101),XTEMP(101)
COMMON/THICKY/XTH(1002),TH(1002)
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,
1 G16,G17,G18,G19,G20
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,
1 STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NU0,
2 TETSYM,TETLIM,DDY,DYMAX
COMMON /STAG/RH00,NO,P0,T0,A0,MDOT1
BEGIN

```



```

COMMON /IPAR/JMAX, KFO, ITERO, KF, KN, IM, IP, J, JET0217
1 KF2, IDEL, JDEL, JYXI, JXI, ILEAD, ILEADF, KCLEAD JET0218
COMMON /ROW/YF, YN, DXF, DXN JET0219
COMMON /CHARAC/XCHARF(92), YCHARF(92), XCHARN(92), YCHARN(92), JET0220
1 RMCARF(92), RPCARF(92), RMCARN(92), RPCARN(92), JET0221
2 TCHARF(92), TCHARN(92), MUCARF(92), MUCARN(92), JET0222
3 CSIGNN(92), CSIGNF(92), MCHARN(92), MCHARF(92), JET0223
4 MCHARI(92) JET0224
COMMON /ICHARA/KCHARP, KCHARM, KCHARO JET0225
C JET0226
C DEFINE INITIAL CHARACTERISTIC PARAMETERS. USE INTERPOLATION OF
C RIEMANN INVARIANT ACROSS THE FAN. JET0227
C JET0228
KCHARP=IDINT(FRACG*DFLOAT(KFO-1)+1.D-6)+1 JET0229
KCHARO=KCHARP+1 JET0230
KCHARM=KCHARO-KCHARP JET0231
IF(KCHARP.LT.2) CALL FIN(200) JET0232
IF(KCHARO.GT.92) CALL FIN(210) JET0233
IF(KCHARM.LT.1) CALL FIN(205) JET0234
NU1=NUFUNC(MEXIT) JET0235
RM1=NUO JET0236
TET1=RM1-NU1 JET0237
RPO=NU1-TET1 JET0238
NUFIN=NUFUNC(MFIN) JET0239
RPFIN=NUFIN-(RM1-NUFIN) JET0240
DRP=(RPFIN-RPO)/DFLOAT(KCHARP-1) JET0241
DO 1 KC=1, KCHARP JET0242
RP1=RPO+DRP*DFLOAT(KC-1) JET0243
CALL RFUNC(RM1, RP1, M1, MU1, TETA1) JET0244
MCHARI(KC)=M1 JET0245
1 CONTINUE JET0246
C DATA FOR C+ CHARACTERISTICS. JET0247
C THE RIEMANN INVARIANTS ARE DEFINED IN SUCH A WAY THAT BOTH VANISH AT
C INFINITE MACH NUMBER. JET0248
C JET0249
RM1=NUO JET0250
DO 2 KC=1, KCHARP JET0251
CSIGNF(KC)=1.D0 JET0252
XCHARF(KC)=XC JET0253
YCHARF(KC)=YC JET0254
IF(MCHARI(KC).EQ.0.) CALL FIN(231) JET0255
NU=NUFUNC(MCHARI(KC)) JET0256
TET=RM1-NU JET0257
RP1=NU-TET JET0258
CALL RFUNC(RM1, RP1, M1, MU1, TETA1) JET0259
MCHARF(KC)=M1 JET0260
MUCARF(KC)=MU1 JET0261
TCHARF(KC)=TETA1 JET0262
RMCARF(KC)=RM1 JET0263
RPCARF(KC)=RP1 JET0264
2 CONTINUE JET0265
C DATA FOR C- CHARACTERISTICS. JET0266
KC1=KCHARP+1 JET0267
XCHARF(KC1)=0.8D0*XC JET0268
DO 21 KC=KC1, KCHARO JET0269
CSIGNF(KC)=-1.D0 JET0270
MCHARI(KC)=MEXIT JET0271
MUCARF(KC)=DARSIN(1.D0/MCHARI(KC)) JET0272
TCHARF(KC)=PAI2 JET0273
YCHARF(KC)=YC JET0274
MCHARF(KC)=MEXIT JET0275
RMCARF(KC)=RM1 JET0276
RPCARF(KC)=NUFUNC(MEXIT)-(TCHARF(KC)-TETLIM) JET0277
21 CONTINUE JET0278
C DEFINE GRID AND INITIAL CONDITIONS AT EXIT PLANE. JET0279
KFAN=KCHARP-1 JET0280
ILEAD=KFO-KFAN JET0281
KCLEAD=1 JET0282
KF=KFO JET0283
KF2=2*KF JET0284
YF=YC JET0285
DO 3 I=1, KF JET0286
KC=KCLEAD+I-ILEAD JET0287
IF(KC.GT.KCHARP) CALL FIN(241) JET0288

```

```

IF(KC.GE.1) GO TO 31
XF(I)=DFLOAT(I-1)*XC/DFLOAT(ILEAD-1)
MF(I)=MEXIT
TETAF(I)=PAI2
GO TO 32
31 CONTINUE
XF(I)=XC
MF(I)=MCHARF(KC)
TETAF(I)=TCHARF(KC)
32 CONTINUE
RMF(I)=NUFUNC(MF(I))+(TETAF(I)-TETLIM)
RPF(I)=NUFUNC(MF(I))-(TETAF(I)-TETLIM)
MUF(I)=DARSIN(1.DO/MF(I))
BF(I)=0.
3 CONTINUE
DY=DYO
DO 4 KC=1,KCHARO
CSIGNN(KC)=CSIGNF(KC)
4 CONTINUE
DO 5 I=1,KN
BN(I)=0.
5 CONTINUE
RETURN
END
PRINT
SUBROUTINE PRINT
C SUBROUTINE NUMBER 3
IMPLICIT REAL*8(A-H,L-Z,*)
REAL*4 XPL,YPL
COMMON /PLUME/XPL(1002,10),YPL(1002)
COMMON /IPLUME/KPL,ITYPL(10)
COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),
1 TETAF(101),BF(101),
2 XN(101),RMN(101),RPN(101),MN(101),MUN(101),
3 TETAN(101),BN(101),XTEMP(101)
COMMON/THICKY/XTH(1002),TH(1002)
REAL*4 YXI,XI,XIPM,XIGRP,XIAPP,XIF
COMMON /THICKX/YXI(20),XI(101,20),XIPM(101,20),XIGRP(101,20)
1 ,XIAPP(101,20),XIF(101,20)
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,
1 G16,G17,G18,G19,G20
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DYO,DY,DYNEXT,
1 STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO,
2 TETSYM,TETLIM,DDY,DYMAX
COMMON /STAG/RHOO,NO,PO,TO,AO,MDOT1
COMMON /CHARAC/XCHARF(92),YCHARF(92),XCHARN(92),YCHARN(92),
1 RMCARF(92),RPCARF(92),RMCARN(92),RPCARN(92),
2 TCHARF(92),TCHARN(92),MUCARF(92),MUCARN(92),
3 CSIGNN(92),CSIGNF(92),MCHARN(92),MCHARF(92),
4 MCHARI(92)
COMMON /IPAR/JMAX,KFO,ITERO,KF,KN,IM,IP,J,
1 KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD
COMMON /ROW/YF,YN,DXF,DXN
C
SUM=0.
KF1=KF-1
DO 10 I=1,KF1
DX=XF(I+1)-XF(I)
GOREM=1.DO+G1*MF(I)**2
GOREM1=1.DO+G1*MF(I+1)**2
RATEM=RHOO*AO*MF(I)*DSIN(TETAF(I))/GOREM***(G6+0.5D0)
RATEP=RHOO*AO*MF(I+1)*DSIN(TETAF(I+1))/GOREM1***(G6+0.5D0)
SUM=SUM+DX*(RATEM+RATEP)/2.DO
10 CONTINUE
YYF=2.DO*PAI*YF
IF(DELTA.EQ.0.) YYF=1.DO
MDOTFR=YYF*SUM/MDOT1
PRINT 11, J,KCLEAD,KF,ILEAD,YF,DY,XF(KF),MF(KF),MDOTFR
11 FORMAT(1X,'J,KCLEAD,KF,ILEAD,YF,DY,XF(KF),MBOUND,MDOTR=',
1 4I5,5D12.4)
C
C PRINT FLOW FIELD AT Y=YF
C

```

```

IF(J.EQ.JMAX) JXI=MINO(JXI,JYXI)
IF(J.EQ.1 .OR. J.EQ.JMAX) GO TO 121
IF(JXI.GT.JYXI) GO TO 120
IF(YXI(JXI).GT.YF+0.5D0*DY) GO TO 120
121 CONTINUE
YXI(JXI)=YF
CALL OPACX
C COMPUTE MACH NUMBER FOR CYLINDRICAL EXPANSION MCYL.
F=(YF/YC)*(G7*(1.D0+G1*MEXIT**2))*G2/MEXIT
CALL AREA(F,MCYL)
PRINT 22,JXI,KCLEAD,ILEAD,KF,MCYL,YF
22 FORMAT(/1X,'PRINTING NUMBER JXI,KCLEAD,ILEAD,KF=',4I4,
1 5X,'MCYL,YF=',2D14.5/)
PRINT 1
1 FORMAT(/1X,' I ',' KC ',' XF(I) ',' TETAF(I) ',
1 MF(I) ', MAB ',
2 MABI ', MOBI ',
3 XI(I) ', XIGRP(I) ',
4 XIAPP(I) ', XIPM(I) '/')
IDEL1=IDEL
IF(J.EQ.1.OR.J.EQ.JMAX) IDEL1=1
DO 20 I=1,KF,IDEL1
KC=KCLEAD+(I-ILEAD)
IF(KC.LT.KCLEAD) KC=0
MOB=1.D10
MOBI=1.D10
MAB=1.D10
MABI=1.D10
MPM=MF(I)
IF(KC.EQ.0) GO TO 23
MOB=MCHARI(KC)
IF(J.EQ.1) GO TO 23
PSIPM=PAI2-DATAN((XF(I)-XC)/(YF-YC))
ZETA=PSI1+ZETA1-PSIPM
MPM=DSQRT((G5*DTAN(ZETA/G5))*2+1.D0)
CALL MATCH(I,MOB,MAB,MOBI,MABI)
23 CONTINUE
PRINT 21,I,KC,XF(I),TETAF(I)*DEG,MF(I),MAB,MABI,MOBI,
1 XI(I,JXI),XIGRP(I,JXI),XIAPP(I,JXI),XIPM(I,JXI)
21 FORMAT(1X,2I4,10D12.4)
20 CONTINUE
IF(J.EQ.1) GO TO 120
IF(J.EQ.JMAX) GO TO 120
JXI=JXI+1
120 CONTINUE
IF(J.LT.JMAX) GO TO 200
PRINT 101
101 FORMAT('1')
PRINT 102
102 FORMAT(1X,'RADIAL MOLECULAR THICKNESS J,XTH(J),TH(J)='/)
PRINT 202,(JJ,XTH(JJ),TH(JJ),JJ=1,JMAX)
202 FORMAT(/5(I5,D11.4,D10.3))
PRINT 101
PRINT 103,(IPL,ITYPL(IPL),IPL=1,KPL)
103 FORMAT(1X,'PLUME TYPES IPL,ITYPL(IPL)=' ,
1 2(/1X,5(5X,2I4)))
PRINT 104
104 FORMAT(1X,'PLUME POINTS J,YPL(J),XPL(J,1),XPL(J,2),...='/)
JDEL1=1
DO 203 JJ=1,JMAX,JDEL1
PRINT 204, JJ,YPL(JJ),(XPL(JJ,IPL),IPL=1,KPL)
204 FORMAT(1X,I5,2X,E12.4,10E11.3)
203 CONTINUE
C WRITE ON TAPE7 FOR SUBSEQUENT PLOTTING.
C NO MORE THAN 80 CHARACTERS PER LINE ON TAPE7.
WRITE(7,205) JMAX,KPL
205 FORMAT(8I10/8I10)
WRITE(7,205) (ITYPL(IPL),IPL=1,KPL)
DO 210 JJ=1,JMAX
WRITE(7,211) YPL(JJ),(XPL(JJ,IPL),IPL=1,KPL)
211 FORMAT(6E13.6/2X,6E13.6/2X,6E13.6/2X,6E13.6)
210 CONTINUE

```

JET0361
JET0362
JET0363
JET0364
JET0365
JET0366
JET0367
JET0368
JET0369
JET0370
JET0371
JET0372
JET0373
JET0374
JET0375
JET0376
JET0377
JET0378
JET0379
JET0380
JET0381
JET0382
JET0383
JET0384
JET0385
JET0386
JET0387
JET0388
JET0389
JET0390
JET0391
JET0392
JET0393
JET0394
JET0395
JET0396
JET0397
JET0398
JET0399
JET0400
JET0401
JET0402
JET0403
JET0404
JET0405
JET0406
JET0407
JET0408
JET0409
JET0410
JET0411
JET0412
JET0413
JET0414
JET0415
JET0416
JET0417
JET0418
JET0419
JET0420
JET0421
JET0422
JET0423
JET0424
JET0425
JET0426
JET0427
JET0428
JET0429
JET0430
JET0431
JET0432

C	WRITE LATERAL (X) OPACITIES	JET0433
	JXIO=JXI	JET0434
	WRITE(7,205) JXIO,KFO	JET0435
	PRINT 226, JXIO,KFO	JET0436
226	FORMAT(///1X,'LATERAL (X) OPACITIES JXIO,KFO=',2I8)	JET0437
	DO 220 JXI=1,JXIO	JET0438
	WRITE(7,221) JXI,YXI(JXI)	JET0439
221	FORMAT(I10,E13.6)	JET0440
	PRINT 227, JXI,YXI(JXI)	JET0441
227	FORMAT(//1X,'JXI,YXI(JXI)=' ,I8,E15.6/)	JET0442
	DO 225 I=1,KFO	JET0443
	WRITE(7,211) XIF(I,JXI),XI(I,JXI),XIPM(I,JXI),XIGRP(I,JXI),	JET0444
1	XIAPP(I,JXI)	JET0445
	PRINT 211, XIF(I,JXI),XI(I,JXI),XIPM(I,JXI),XIGRP(I,JXI),	JET0446
1	XIAPP(I,JXI)	JET0447
225	CONTINUE	JET0448
220	CONTINUE	JET0449
200	CONTINUE	JET0450
	RETURN	JET0451
	END	JET0452
	FIN	
	SUBROUTINE FIN(IFIN)	JET0453
C	SUBROUTINE NUMBER 4	JET0454
C	STOP WHEN ERROR IS DETECTED.	JET0455
	IMPLICIT REAL*8(A-H,L-Z,*)	JET0456
	PRINT 1,IFIN	JET0457
1	FORMAT(/1X,'FIN CODE IFIN=' ,I6/)	JET0458
C	INDUCE ERROR IN ORDER TO GENERATE TRACING OF CALLING SUBROUTINES.	JET0459
	X=-1.DO	JET0460
	Y=X+DSQRT(X)	JET0461
	IF(IFIN.LE.0) GO TO 100	JET0462
	STOP	JET0463
100	RETURN	JET0464
	END	JET0465
	MARCH	
	SUBROUTINE MARCH	JET0466
C	SUBROUTINE NUMBER 5	JET0467
	IMPLICIT REAL*8(A-H,L-Z,*)	JET0468
	COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),	JET0469
1	TETA(101),BF(101),	JET0470
2	XN(101),RMN(101),RPN(101),MN(101),MUN(101),	JET0471
3	TETAN(101),BN(101),XTEMP(101)	JET0472
	COMMON/THICKY/XTH(1002),TH(1002)	JET0473
	COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,	JET0474
1	G16,G17,G18,G19,G20	JET0475
	COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,	JET0476
1	STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO,	JET0477
2	TETSYM,TETLIM,DDY,DYMAX	JET0478
	COMMON /STAG/RH00,NO,PO,TO,A0,MDOT1	JET0479
	COMMON /IPAR/JMAX,KFO,ITERO,KF,KN,IM,IP,J,	JET0480
1	KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD	JET0481
	COMMON /ROW/YF,YN,DXF,DXN	JET0482
	COMMON /CHARAC/XCHARF(92),YCHARF(92),XCHARN(92),YCHARN(92),	JET0483
1	RMCARF(92),RPCARF(92),RMCARN(92),RPCARN(92),	JET0484
2	TCHARF(92),TCHARN(92),MUCARF(92),MUCARN(92),	JET0485
3	CSIGNN(92),CSIGNF(92),MCHARN(92),MCHARF(92),	JET0486
4	MCHARI(92)	JET0487
	COMMON /ICHARA/KCHARP,KCHARM,KCHARO	JET0488
C		JET0489
C	ADVANCE FLOW FIELD FROM YF TO YN	JET0490
	IM=KF	JET0491
	IP=KF	JET0492
	YN=YF+DY	JET0493
	KN=KFO	JET0494
C	SEMI-INVERSE INTEGRATION FOR FAN POINTS.	JET0495
	CALL SEMINV	JET0496
C	NEW GRID POINTS (JUST INVERSE MARCHING).	JET0497
	CALL GRIDN	JET0498
C	LOAD FLOW VARIABLES FROM SEMI-INVERSE INTEGRATION INTO VECTORS	JET0499
	CALL LOADC	JET0500
C	CHARACTERISTIC SCHEME INTEGRATION FOR INNER POINTS (INVERSE MARCH).	JET0501
	CALL INVMAR	JET0502
	RETURN	JET0503
	END	JET0504

```

SUBROUTINE INVMAR
C SUBROUTINE NUMBER 6
IMPLICIT REAL*8(A-H,L-Z,$)
COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),
1 TETAF(101),BF(101),
2 XN(101),RMN(101),RPN(101),MN(101),MUN(101),
3 TETAN(101),BN(101),XTEMP(101)
COMMON/THICKY/XTH(1002),TH(1002)
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,
1 G16,G17,G18,G19,G20
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,
1 STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO,
2 TETSYM,TETLIM,DDY,DYMAX
COMMON /STAG/RHOO,NO,PO,TO,AO,MDOT1
COMMON /IPAR/JMAX,KFO,ITERO,KF,KN,IM,IP,J,
1 KF2,IDEL,JDEL,JYXI,JXI,Ilead,Ileadf,KCLEAD
COMMON /ROW/YF,YN,DXF,DXN
C
C INTEGRATION WITH INVERSE CHARACTERISTICS FOR NEW POINT(X4,Y4).
C OLD POINTS ARE (X1,Y1),(X2,Y2).
C X1 IS OBTAINED BY INVERSE C- FROM X4
C X2 IS OBTAINED BY INVERSE C+ FROM X4
C NOTE THAT X1 MAY BE NEGATIVE (E. G. WHEN X4=0).
KN1=Ilead-1
IF(KN1.LE.0) CALL FIN(601)
DO 1000 I=1,KN1
I4=I
X4=XN(I)
Y4=YN
IF4=(IM+IP)/2
CALL INTERP(0,IF4,KF,X4,XF,RM4,RMF,RP4,RPF)
CALL RFUNC(RM4,RP4,M4,MU4,TETA4)
M14=M4
MU14=MU4
TETA14=TETA4
M24=M4
MU24=MU4
TETA24=TETA4
Y1=YF
Y2=YF
Y14=(Y1+Y4)/2.DO
Y24=(Y2+Y4)/2.DO
X1=1.D10
X2=1.D10
RM4=1.D10
RP4=1.D10
ITER=0
GO TO 2
C
C CORRECTOR
C
C 1 ITER=ITER+1
C AVERAGED PROPERTIES ON C-(14),C+(24) CHARACTERISTICS.
RM14=(RM1+RM4)/2.DO
RP14=(RP1+RP4)/2.DO
RM24=(RM2+RM4)/2.DO
RP24=(RP2+RP4)/2.DO
C M14,MU14,TETA14, M24,MU24,TETA24 AVERAGED ON C-,C+ CHARACTERISTICS.
CALL RFUNC(RM14,RP14,M14,MU14,TETA14)
CALL RFUNC(RM24,RP24,M24,MU24,TETA24)
2 CONTINUE
C NEW X1,X2
X10=X1
X20=X2
X1=X4-DY/DTAN(TETA14-MU14)
X2=X4-DY/DTAN(TETA24+MU24)
IF(X2.LT.0.) CALL FIN(670)
D14=DSQRT((X1-X4)**2+DY**2)
D24=DSQRT((X2-X4)**2+DY**2)
C INTERPOLATE OLD DISTRIBUTION FOR RM1,RP1, RM2,RP2 AT X1,X2.
CALL INTERP(0,IM,KF,X1,XF,RM1,RMF,RP1,RPF)
CALL INTERP(0,IP,KF,X2,XF,RM2,RMF,RP2,RPF)

```

```

JET0505
JET0506
JET0507
JET0508
JET0509
JET0510
JET0511
JET0512
JET0513
JET0514
JET0515
JET0516
JET0517
JET0518
JET0519
JET0520
JET0521
JET0522
JET0523
JET0524
JET0525
JET0526
JET0527
JET0528
JET0529
JET0530
JET0531
JET0532
JET0533
JET0534
JET0535
JET0536
JET0537
JET0538
JET0539
JET0540
JET0541
JET0542
JET0543
JET0544
JET0545
JET0546
JET0547
JET0548
JET0549
JET0550
JET0551
JET0552
JET0553
JET0554
JET0555
JET0556
JET0557
JET0558
JET0559
JET0560
JET0561
JET0562
JET0563
JET0564
JET0565
JET0566
JET0567
JET0568
JET0569
JET0570
JET0571
JET0572
JET0573
JET0574
JET0575
JET0576

```

```

C NO NEED FOR RE-AVERAGING SINCE IT INTRODUCES ONLY HIGHER ORDER JET0577
C CHANGES INTO THE ITERATION SCHEME. JET0578
C INTEGRATE THE CHARACTERISTIC EQUATIONS FOR RM4,RP4 AT X4,Y4. JET0579
  RM40=RM4 JET0580
  RP40=RP4 JET0581
  RM4=RM1+DELTA*DSIN(TETA14)*D14/(M14*Y14) JET0582
  RP4=RP2+DELTA*DSIN(TETA24)*D24/(M24*Y24) JET0583
C CONVERGENCE TEST JET0584
  EPS=(DABS(X1-X10)+DABS(X2-X20))/DY+DABS(RM4-RM40)+DABS(RP4-RP40) JET0585
  IF(ITER.GT.ITER0) GO TO 10 JET0586
  IF(EPS.GT.EPSIL) GO TO 1 JET0587
  RMN(I)=RM4 JET0588
  RPN(I)=RP4 JET0589
  CALL RFUNC(RM4,RP4,MN(I),MUN(I),TETAN(I)) JET0590
1000 CONTINUE JET0591
  RETURN JET0592
10 CONTINUE JET0593
  PRINT 11,I4,KN,IF4,IM,IP,KF,ITER,ITER0,EPS,EPSIL,X1,X2,X4,M14,M24 JET0594
11 FORMAT(1X,'SUBR. INVMAR. I4,KN,IF4,IM,IP,KF,ITER,ITER0=',8I5/ JET0595
1 1X,'EPS,EPSIL,X1,X2,X4,M14,M24=',7D14.6/) JET0596
  CALL FIN(611) JET0597
  RETURN JET0598
  END JET0599

```

SEMINV

```

SUBROUTINE SEMINV JET0600
C SUBROUTINE NUMBER 7 JET0601
  IMPLICIT REAL*8(A-H,L-Z,$) JET0602
  COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101), JET0603
1  TETA(101),BF(101), JET0604
2  XN(101),RMN(101),RPN(101),MN(101),MUN(101), JET0605
3  TETAN(101),BN(101),XTEMP(101) JET0606
  COMMON/THICKY/XTH(1002),TH(1002) JET0607
  COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15, JET0608
1  G16,G17,G18,G19,G20 JET0609
  COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT, JET0610
1  STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO, JET0611
2  TETSYM,TETLIM,DDY,DYMAX JET0612
  COMMON /STAG/RH00,NO,PO,TO,AO,MDOT1 JET0613
  COMMON /IPAR/JMAX,KFO,ITER0,KF,KN,IM,IP,J, JET0614
1  KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD JET0615
  COMMON /ROW/YF,YN,DXF,DXN JET0616
  COMMON /CHARAC/XCHARF(92),YCHARF(92),XCHARN(92),YCHARN(92), JET0617
1  RMCARF(92),RPCARF(92),RMCARN(92),RPCARN(92), JET0618
2  TCHARF(92),TCHARN(92),MUCARF(92),MUCARN(92), JET0619
3  CSIGNN(92),CSIGNF(92),MCHARN(92),MCHARF(92), JET0620
4  MCHARI(92) JET0621
  COMMON /ICHARA/KCHARP,KCHARM,KCHARO JET0622
C JET0623
C COMPUTE NEW POINT (X4,Y4), BY PASSING A C+ CHARACTERISTIC JET0624
C THROUGH OLD POINT (X2,Y2). BOTH POINTS ARE ON CHARACTERISTIC LINE JET0625
C NUMBER KC. JET0626
  IM=1 JET0627
  DO 100 KC=1,KCHARO JET0628
  IF(CSIGNN(KC).EQ.0.) GO TO 100 JET0629
C JET0630
C PREDICTOR JET0631
C JET0632
  Y1=YF JET0633
  Y2=YF JET0634
  Y4=YN JET0635
  Y14=(Y1+Y4)/2.DO JET0636
  Y24=(Y2+Y4)/2.DO JET0637
  X2=XCHARF(KC) JET0638
  RM2=RMCARF(KC) JET0639
  RP2=RPCARF(KC) JET0640
  M2=MCHARF(KC) JET0641
  MU2=MUCARF(KC) JET0642
  TETA2=TCHARF(KC) JET0643
  M14=M2 JET0644
  MU14=MU2 JET0645
  TETA14=TETA2 JET0646
  M24=M2 JET0647
  MU24=MU2 JET0648

```

```

TETA24=TETA2
X4=1.D10
X1=1.D10
RM4=1.D10
RP4=1.D10
ITER=0
GO TO 2
C
C CORRECTOR
C
1 ITER=ITER+1
C AVERAGED PROPERTIES ON C-(14),C+(24) CHARACTERISTICS.
RM14=(RM1+RM4)/2.D0
RP14=(RP1+RP4)/2.D0
RM24=(RM2+RM4)/2.D0
RP24=(RP2+RP4)/2.D0
C M14,MU14,TETA14, M24,MU24,TETA24 AVERAGED ON C-,C+ CHARACTERISTICS.
CALL RFUNC(RM14,RP14,M14,MU14,TETA14)
CALL RFUNC(RM24,RP24,M24,MU24,TETA24)
2 CONTINUE
C NEW X4,X1
X40=X4
X10=X1
X4=X2+DY/DTAN(TETA24+CSIGNF(KC)*MU24)
X1=X4-DY/DTAN(TETA14-CSIGNF(KC)*MU14)
D14=DSQRT((X1-X4)**2+DY**2)
D24=DSQRT((X2-X4)**2+DY**2)
C INTERPOLATE OLD DISTRIBUTION FOR RM1,RP1, AT X1.
CALL INTERP(0,IM,KF,X1,XF,RM1,RMF,RP1,RPF)
IF(J.GT.1) GO TO 22
IF(CSIGNF(KC).LT.0.) GO TO 22
RP1=RP2
22 CONTINUE
C NO NEED FOR RE-AVERAGING SINCE IT INTRODUCES ONLY HIGHER ORDER
C CHANGES INTO THE ITERATION SCHEME.
C INTEGRATE THE CHARACTERISTIC EQUATIONS FOR RM4,RP4 AT X4,Y4.
RM40=RM4
RP40=RP4
IF(CSIGNF(KC).LT.0.) GO TO 21
RM4=RM1+DELTA*DSIN(TETA14)*D14/(M14*Y14)
RP4=RP2+DELTA*DSIN(TETA24)*D24/(M24*Y24)
GO TO 20
21 CONTINUE
RM4=RM2+DELTA*DSIN(TETA24)*D24/(M24*Y24)
RP4=RP1+DELTA*DSIN(TETA14)*D14/(M14*Y14)
20 CONTINUE
C CONVERGENCE TEST
EPS=(DABS(X4-X40)+DABS(X1-X10))/DY+DABS(RM4-RM40)+DABS(RP4-RP40)
IF(ITER.GT.ITER0) GO TO 10
IF(EPS.GT.EPSIL) GO TO 1
CSIGNN(KC)=CSIGNF(KC)
IF(X4.GT.0.) GO TO 30
RMSAVE=RM4
RM4=RP4+TETSYM
RP4=RM4-TETSYM
CSIGNN(KC)=-1.D0
30 CONTINUE
RMCARN(KC)=RM4
RPCARN(KC)=RP4
CALL RFUNC(RM4,RP4,M4,MU4,TETA4)
TCHARN(KC)=TETA4
XCHARN(KC)=DABS(X4)
YCHARN(KC)=Y4
MUCARN(KC)=MU4
MCHARN(KC)=M4
100 CONTINUE
RETURN
10 CONTINUE
PRINT 11,KC,KCHAR0,IM,KF,ITER,ITER0,EPS,EPSIL,X1,X2,X4,M14,M24
11 FORMAT(1X,'SUBR. SEMINV. KC,KCHAR0,IM,KF,ITER,ITER0=',6I5/
1 1X,'EPS,EPSIL,X1,X2,X4,M14,M24=',7D14.6/)
CALL FIN(711)

```

JET0649
JET0650
JET0651
JET0652
JET0653
JET0654
JET0655
JET0656
JET0657
JET0658
JET0659
JET0660
JET0661
JET0662
JET0663
JET0664
JET0665
JET0666
JET0667
JET0668
JET0669
JET0670
JET0671
JET0672
JET0673
JET0674
JET0675
JET0676
JET0677
JET0678
JET0679
JET0680
JET0681
JET0682
JET0683
JET0684
JET0685
JET0686
JET0687
JET0688
JET0689
JET0690
JET0691
JET0692
JET0693
JET0694
JET0695
JET0696
JET0697
JET0698
JET0699
JET0700
JET0701
JET0702
JET0703
JET0704
JET0705
JET0706
JET0707
JET0708
JET0709
JET0710
JET0711
JET0712
JET0713
JET0714
JET0715
JET0716
JET0717
JET0718
JET0719
JET0720

	RETURN	RFUNC	JET0721
	END		JET0722
	SUBROUTINE RFUNC(RM,RP,M,MU,TETA)		JET0723
C	SUBROUTINE NUMBER 8		JET0724
	IMPLICIT REAL*8(A-H,L-Z,\$)		JET0725
	COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),		JET0726
1	TETAF(101),BF(101),		JET0727
2	XN(101),RMN(101),RPN(101),MN(101),MUN(101),		JET0728
3	TETAN(101),BN(101),XTEMP(101)		JET0729
	COMMON/THICKY/XTH(1002),TH(1002)		JET0730
	COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,		JET0731
1	G16,G17,G18,G19,G20		JET0732
	COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,		JET0733
1	STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO,		JET0734
2	TETSYM,TETLIM,DDY,DYMAX		JET0735
	COMMON /STAG/RH00,NO,PO,TO,AO,MDOT1		JET0736
	COMMON /IPAR/JMAX,KFO,ITERO,KF,KN,IM,IP,J,		JET0737
1	KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD		JET0738
	COMMON /ROW/YF,YN,DXF,DXN		JET0739
C	COMPUTE M,MU,TETA AT A POINT, AS FUNCTION OF RIEMANN INVAR. RM,RP.		JET0740
C	TETA=(RM-RP)/2.DO+TETLIM		JET0741
	NU=(RM+RP)/2.DO		JET0742
C	NU=NUO-(G5*ARCTAN(G5*Q)-ARCTAN(Q)), WHERE Q=(M**2-1)**(-1/2)		JET0743
C	FIND Q(NU), AND HENCE M(NU), THROUGH NEWTON RAPHSON ITERATIONS.		JET0744
	Q=-((NU-NUO)/(G4-1.DO))		JET0745
	IF(Q.LE.0.) CALL FIN(801)		JET0746
	ITER=0		JET0747
1	ITER=ITER+1		JET0748
	QF=Q		JET0749
	DNUDT=-((G4-1.DO)/((1.DO+G4*Q**2)*(1.DO+Q**2)))		JET0750
	DNU=NU-(NUO-(G5*DATAN(G5*Q)-DATAN(Q)))		JET0751
	Q=Q+DNU/DNUDT		JET0752
	IF(Q.LE.0.) CALL FIN(811)		JET0753
	EPS=DABS(Q-QF)/Q		JET0754
	IF(ITER.GT.ITERO) GO TO 10		JET0755
	IF(EPS.GT.EPSIL*1.D-3) GO TO 1		JET0756
	M=DSQRT(1.DO+1.DO/Q**2)		JET0757
	MU=DARSIN(1.DO/M)		JET0758
	RETURN		JET0759
10	CONTINUE		JET0760
	CALL FIN(810)		JET0761
	RETURN		JET0762
	END	INTERP	JET0763
	SUBROUTINE INTERP(JNEW,I,KGRID,X,XVEC,RM,RMVEC,RP,RPVEC)		JET0764
C	SUBROUTINE NUMBER 9		JET0765
	IMPLICIT REAL*8(A-H,L-Z,\$)		JET0766
	COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),		JET0767
1	TETAF(101),BF(101),		JET0768
2	XN(101),RMN(101),RPN(101),MN(101),MUN(101),		JET0769
3	TETAN(101),BN(101),XTEMP(101)		JET0770
	COMMON/THICKY/XTH(1002),TH(1002)		JET0771
	COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,		JET0772
1	G16,G17,G18,G19,G20		JET0773
	COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,		JET0774
1	STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO,		JET0775
2	TETSYM,TETLIM,DDY,DYMAX		JET0776
	COMMON /STAG/RH00,NO,PO,TO,AO,MDOT1		JET0777
	COMMON /IPAR/JMAX,KFO,ITERO,KF,KN,IM,IP,J,		JET0778
1	KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD		JET0779
	COMMON /ROW/YF,YN,DXF,DXN		JET0780
	DIMENSION XVEC(1),RMVEC(1),RPVEC(1)		JET0781
C	FIND I SUCH THAT XVEC(I).LE.X.AND.XVEC(I+1).GE.X		JET0782
C	FIND RM,RP BY LINEAR INTERPOLATION.		JET0783
C	NOTE THAT X MAY BE NEGATIVE.		JET0784
	IF(DABS(X).LE.XVEC(KGRID)) GO TO 901		JET0785
	PRINT 900,X,KGRID,XVEC(KGRID)		JET0786
	FORMAT(/1X,D15.7,I10,4X,D15.7/)	JET0789	JET0787
	CALL FIN(900)		JET0788
901	CONTINUE		JET0789
	KG2=2*KGRID		JET0790
			JET0791
			JET0792

	IO=MINO(I,KGRID-2)	JET0793
	ICOUNT=0	JET0794
1	I=IO	JET0795
	SIGN1=1.DO	JET0796
	IF(I.GE.1) GO TO 10	JET0797
	SIGN1=-1.DO	JET0798
	I=-I+2	JET0799
10	CONTINUE	JET0800
	IF(I.GT.KGRID) CALL FIN(901)	JET0801
	XX1=SIGN1*XVEC(I)	JET0802
	I1=I	JET0803
	IF(XX1.LE.X) GO TO 11	JET0804
	IO=IO-1	JET0805
	ICOUNT=ICOUNT+1	JET0806
	IF(ICOUNT.GT.KG2) CALL FIN(911)	JET0807
	GO TO 1	JET0808
11	CONTINUE	JET0809
	I=IO+1	JET0810
	SIGN2=1.DO	JET0811
	IF(I.GE.1) GO TO 12	JET0812
	SIGN2=-1.DO	JET0813
	I=-I+2	JET0814
12	CONTINUE	JET0815
	IF(I.GT.KGRID) CALL FIN(912)	JET0816
	XX2=SIGN2*XVEC(I)	JET0817
	I2=I	JET0818
	IF(XX2.GE.X) GO TO 13	JET0819
	IO=IO+1	JET0820
	ICOUNT=ICOUNT+1	JET0821
	IF(ICOUNT.GT.KG2) CALL FIN(913)	JET0822
	GO TO 1	JET0823
13	CONTINUE	JET0824
	F1=(XX2-X)/(XX2-XX1)	JET0825
	F2=1.DO-F1	JET0826
	IF(F1.LT.0.) CALL FIN(991)	JET0827
	IF(F2.LT.0.) CALL FIN(992)	JET0828
	RM1=RMF(I1)	JET0829
	RP1=RPF(I1)	JET0830
	RM2=RMF(I2)	JET0831
	RP2=RPF(I2)	JET0832
	IF(SIGN1.LT.0.) RM1=RPF(I1)+TETSYM	JET0833
	IF(SIGN1.LT.0.) RP1=RMF(I1)-TETSYM	JET0834
	IF(SIGN2.LT.0.) RM2=RPF(I2)+TETSYM	JET0835
	IF(SIGN2.LT.0.) RP2=RMF(I2)-TETSYM	JET0836
	RM=F1*RM1+F2*RM2	JET0837
	RP=F1*RP1+F2*RP2	JET0838
	RETURN	JET0839
	END	JET0840
INTERX		
	SUBROUTINE INTERX(JNEW,I1,VARO,VAR,KGRID,XO,XVEC)	JET0841
C	SUBROUTINE NUMBER 10	JET0842
	IMPLICIT REAL*8(A-H,L-Z,*)	JET0843
	COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),	JET0844
1	TETAF(101),BF(101),	JET0845
2	XN(101),RMN(101),RPN(101),MN(101),MUN(101),	JET0846
3	TETAN(101),BN(101),XTEMP(101)	JET0847
	COMMON/THICKY/XTH(1002),TH(1002)	JET0848
	COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,	JET0849
1	G16,G17,G18,G19,G20	JET0850
	COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,	JET0851
1	STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO,	JET0852
2	TETSYM,TETLIM,DDY,DYMAX	JET0853
	COMMON /STAG/RHOO,NO,PO,TO,AO,MDOT1	JET0854
	COMMON /IPAR/JMAX,KFO,ITERO,KF,KN,IM,IP,J,	JET0855
1	KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD	JET0856
	COMMON /ROW/YF,YN,DXF,DXN	JET0857
	DIMENSION VAR(1),XVEC(1)	JET0858
C	FIND XO AND I1 SUCH THAT XVEC(I1)<XO<XVEC(I1+1), AND XO CORRESPONDS	JET0859
C	TO THE LOCATION AT WHICH VARO IS A LINEAR INTERPOLATION OF VAR(I).	JET0860
	XO=1.D23	JET0861
	IFIRST=I1	JET0862
	IF(I1.GT.0) GO TO 10	JET0863
	IFIRST=KGRID-IABS(I1)+2	JET0864

```

10 CONTINUE JET0865
DO 1 II=IFIRST,KGRID JET0866
I=II JET0867
IF(I1.GT.0) GO TO 11 JET0868
I=KGRID-II+2 JET0869
11 CONTINUE JET0870
IF(I.LE.0) CALL FIN(1001) JET0871
IF(I.GT.KGRID) CALL FIN(1002) JET0872
IF(I.EQ.1) GO TO 1 JET0873
IF((VAR(I)-VAR0)*(VAR(I-1)-VAR0).GT.0.) GO TO 1 JET0874
IF(VAR(I).EQ.VAR(I-1)) GO TO 1 JET0875
F1=(VAR(I)-VAR0)/(VAR(I)-VAR(I-1)) JET0876
F2=1.DO-F1 JET0877
IF(F1.LT.0.) CALL FIN(1011) JET0878
IF(F2.LT.0.) CALL FIN(1012) JET0879
X0=F1*XVEC(I-1)+F2*XVEC(I) JET0880
I1=I-1 JET0881
GO TO 2 JET0882
1 CONTINUE JET0883
2 CONTINUE JET0884
RETURN JET0885
END JET0886

```

BREAK

```

SUBROUTINE BREAK JET0887
C SUBROUTINE NUMBER 11 JET0888
IMPLICIT REAL*8(A-H,L-Z,$) JET0889
REAL MB,MX,MY JET0890
COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101), JET0891
1 TETAF(101),BF(101), JET0892
2 XN(101),RMN(101),RPN(101),MN(101),MUN(101), JET0893
3 TETAN(101),BN(101),XTEMP(101) JET0894
COMMON/THICKY/XTH(1002),TH(1002) JET0895
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15, JET0896
1 G16,G17,G18,G19,G20 JET0897
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT, JET0898
1 STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO, JET0899
2 TETSYM,TETLIM,DDY,DYMAX JET0900
COMMON /STAG/RH00,NO,PO,TO,AO,MDOT1 JET0901
COMMON /IPAR/JMAX,KFO,ITERO,KF,KN,IM,IP,J, JET0902
1 KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD JET0903
COMMON /ROW/YF,YN,DXF,DXN JET0904
C COMPUTE THE BREAKDOWN PARAMETER AT (I-1/2,K-1/2). STORE IN BN(I). JET0905
YB=0.5D0*(YF+YN) JET0906
DYY=DY JET0907
IM=2 JET0908
DO 1 I=2,KN JET0909
X1=XN(I-1) JET0910
X2=XN(I) JET0911
DXX=X2-X1 JET0912
IF(X2.GT.XF(KF)) GO TO 2 JET0913
CALL INTERP(0,IM,KF,X1,XF,RM1,RMF,RP1,RPF) JET0915
CALL INTERP(0,IM,KF,X2,XF,RM2,RMF,RP2,RPF) JET0916
CALL RFUNC(RM1,RP1,M1,MU1,TETA1) JET0917
CALL RFUNC(RM2,RP2,M2,MU2,TETA2) JET0918
MX=0.5D0*((MN(I)-MN(I-1))+(M2-M1))/DXX JET0919
MY=0.5D0*((MN(I)-M2)+(MN(I-1)-M1))/DYY JET0920
MB=0.25D0*(MN(I-1)+MN(I)+M1+M2) JET0921
TETAB=0.25D0*(TETAN(I-1)+TETAN(I)+TETA1+TETA2) JET0922
GOREM=MB**2*(1.DO+G1*MB**2)**(G6-1.DO) JET0923
GRAD=MX*DCOS(TETAB)+MY*DSIN(TETAB) JET0924
B=G20*GOREM*GRAD JET0925
GO TO 3 JET0926
2 B=1.D22 JET0927
3 BN(I)=B JET0928
1 CONTINUE JET0929
BN(1)=BN(2) JET0930
RETURN JET0931
END JET0932

```

OPACY

```

SUBROUTINE OPACY JET0933
C SUBROUTINE NUMBER 12 JET0934
IMPLICIT REAL*8(A-H,L-Z,$) JET0935
COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101), JET0936

```

```

1          TETAF(101),BF(101), JET0937
2          XN(101),RMN(101),RPN(101),MN(101),MUN(101), JET0938
3          TETAN(101),BN(101),XTEMP(101) JET0939
COMMON/THICKY/XTH(1002),TH(1002) JET0940
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15, JET0941
1          G16,G17,G18,G19,G20 JET0942
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DYO,DY,DYNEXT, JET0943
1          STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO, JET0944
2          TETSYM,TETLIM,DDY,DYMAX JET0945
COMMON /STAG/RHOO,NO,PO,TO,AO,MDOT1 JET0946
COMMON /IPAR/JMAX,KFO,ITERO,KF,KN,IM,IP,J, JET0947
1          KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD JET0948
COMMON /ROW/YF,YN,DXF,DXN JET0949
C JET0950
C COMPUTE THE MOLECULAR THICKNESS AT END POINTS OF EACH ROW. JET0951
IM=2 JET0952
XTH(J)=XF(KF) JET0953
TH(J)=0. JET0954
DTHO=NO*SIGMA*DY JET0955
IF(J.EQ.1) GO TO 11 JET0956
J1=J-1 JET0957
DO 1 JJ=1,J1 JET0958
XX1=XTH(JJ) JET0959
CALL INTERP(0,IM,KF,XX1,XF,RM1,RMF,RP1,RPF) JET0960
CALL RFUNC(RM1,RP1,M1,MU1,TETA1) JET0961
GOREM=1.D0+G1*M1**2 JET0962
DTH=DTHO/GOREM**G6 JET0963
TH(JJ)=TH(JJ)+DTH JET0964
1 CONTINUE JET0965
11 CONTINUE JET0966
RETURN JET0967
END JET0968
SUBROUTINE PLUMES JET0969
C SUBROUTINE NUMBER 13 JET0970
IMPLICIT REAL*8(A-H,L-Z,$) JET0971
REAL*4 XPL,YPL JET0972
COMMON /PLUME/XPL(1002,10),YPL(1002) JET0973
COMMON /IPLUME/KPL,ITYPL(10) JET0974
DIMENSION VPL(92) JET0975
COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101), JET0976
1          TETAF(101),BF(101), JET0977
2          XN(101),RMN(101),RPN(101),MN(101),MUN(101), JET0978
3          TETAN(101),BN(101),XTEMP(101) JET0979
COMMON/THICKY/XTH(1002),TH(1002) JET0980
REAL*4 YXI,XI,XIPM,XIGRP,XIAPP,XIF JET0981
COMMON /THICKX/YXI(20),XI(101,20),XIPM(101,20),XIGRP(101,20) JET0982
1          ,XIAPP(101,20),XIF(101,20) JET0983
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15, JET0984
1          G16,G17,G18,G19,G20 JET0985
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DYO,DY,DYNEXT, JET0986
1          STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO, JET0987
2          TETSYM,TETLIM,DDY,DYMAX JET0988
COMMON /STAG/RHOO,NO,PO,TO,AO,MDOT1 JET0989
COMMON /IPAR/JMAX,KFO,ITERO,KF,KN,IM,IP,J, JET0990
1          KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD JET0991
COMMON /ROW/YF,YN,DXF,DXN JET0992
COMMON /CHARAC/XCHARF(92),YCHARF(92),XCHARN(92),YCHARN(92), JET0993
1          RMCARF(92),RPCARF(92),RMCARN(92),RPCARN(92), JET0994
2          TCHARF(92),TCHARN(92),MUCARF(92),MUCARN(92), JET0995
3          CSIGNN(92),CSIGNF(92),MCHARN(92),MCHARF(92), JET0996
4          MCHARI(92) JET0997
COMMON /ICHARA/KCHARP,KCHARM,KCHARO JET0998
C COMPUTE SPECIAL POINTS AT Y=YN, AND STORE THEM AS JET0999
C (XPL(J,IPL),YPL(J))=YN. JET1000
C J IS THE MARCHING INDEX OF YN. JET1001
C IPL=1,2,...,KPL IS THE "PLUME" INDEX. PRESENTLY KPL.LE.5 JET1002
C VPL(IPL) IS A VALUE DEFINING THE "PLUME" CURVE. JET1003
C ITYPL(IPL) IS THE TYPE OF CURVE. IT DEFINES CURVES AS FOLLOWS: JET1004
C ITYPL(IPL)=0 DO NOTHING JET1005
C ITYPL(IPL)=1 REAL PLUME. IT IS THE BREAKDOWN SURFACE, DEFINED JET1006
C BY A CONSTANT VALUE OF THE BREAKDOWN PARAMETER B. JET1007
C SET VPL(IPL)=B. JET1008

```

PLUMES

```

C ITYPL(IPL)=2 CONSTANT MACH-NUMBER LINE. VPL(IPL)=M. JET1009
C ITYPL(IPL)=3 A SINGLE STREAMLINE. VPL(IPL) IS SET TO THE EXIT JET1010
C X-COORDINATE OF THAT STREAMLINE. JET1011
C ITYPL(IPL)=4 A SINGLE C+ CHARACTERISTIC LINE STARTING AT THE CORNER. JET1012
C VPL(IPL) IS SET TO THE INDEX KC OF THAT CHARACTERISTIC JET1013
C LINE. JET1014
C ITYPL(IPL)=5 A CONSTANT LATERAL (X) OPACITY LINE. VPL(IPL) IS SET JET1015
C TO THE VALUE OF THE (CONSTANT) OPACITY. JET1016
C JET1017
C DEFINE ITYPL(IPL) AND VPL(IPL) JET1018
KPL=10 JET1019
IF(KPL.GT.10) CALL FIN(1301) JET1020
DO 2000 IPL=1,KPL JET1021
GO TO (2001,2002,2003,2004,2005,2006,2007,2008,2009,2010),IPL JET1022
2001 ITYPL(IPL)=4 JET1023
VPL(IPL)=1 JET1024
GO TO 2000 JET1025
2002 ITYPL(IPL)=4 JET1026
VPL(IPL)=KCHARP JET1027
GO TO 2000 JET1028
2003 ITYPL(IPL)=4 JET1029
VPL(IPL)=19 JET1030
GO TO 2000 JET1031
2004 ITYPL(IPL)=4 JET1032
VPL(IPL)=31 JET1033
GO TO 2000 JET1034
2005 ITYPL(IPL)=4 JET1035
VPL(IPL)=47 JET1036
GO TO 2000 JET1037
2006 ITYPL(IPL)=4 JET1038
VPL(IPL)=55 JET1039
GO TO 2000 JET1040
2007 ITYPL(IPL)=1 JET1041
VPL(IPL)=0.02D0 JET1042
GO TO 2000 JET1043
2008 ITYPL(IPL)=1 JET1044
VPL(IPL)=0.03D0 JET1045
GO TO 2000 JET1046
2009 ITYPL(IPL)=1 JET1047
VPL(IPL)=0.05D0 JET1048
GO TO 2000 JET1049
2010 ITYPL(IPL)=1 JET1050
VPL(IPL)=0.08D0 JET1051
GO TO 2000 JET1052
2000 CONTINUE JET1053
C COMPUTE "PLUME" POINTS AT Y=YN JET1054
DO 1000 IPL=1,KPL JET1055
ITYP=ITYPL(IPL) JET1056
IF(ITYP.EQ.0) GO TO 1000 JET1057
GO TO (1,2,3,4,5), ITP JET1058
1 CONTINUE JET1059
C BREAKDOWN SURFACE PLUME. JET1060
C NOTE THAT DUE TO DIFFERENCE-CENTERING OF GRADIENTS, THE ACCURATE JET1061
C Y-COORDINATE IS 0.5*(YF+YN), RATHER THAN YN. IT CAN BE ADJUSTED JET1062
C IN THE PLOTTING CODE. JET1063
BO=VPL(IPL) JET1064
XTEMP(1)=XN(1) JET1065
DO 11 I=2,KN JET1066
XTEMP(I)=0.5D0*(XN(I)+XN(I-1)) JET1067
11 CONTINUE JET1068
I=2 JET1069
CALL INTERX(1,I,BO,BN,KN,XBO,XTEMP) JET1070
XPL(J,IPL)=XBO JET1071
GO TO 1001 JET1072
2 CONTINUE JET1073
C FIND BY INTERPOLATION THE X-COORDINATE WHERE M=MPL. JET1074
IF(J.GT.1) GO TO 200 JET1075
XPL(J,IPL)=XC JET1076
GO TO 1001 JET1077
200 CONTINUE JET1078
MPL=VPL(IPL) JET1079
I=-KN JET1080

```

CALL INTERX(1,I,MPL,MN,KN,XM0,XN)	JET1081
XPL(J,IPL)=XM0	JET1082
GO TO 1001	JET1083
3 CONTINUE	JET1084
C STREAMLINE INTERPOLATION.	JET1085
IF(J.GT.1) GO TO 300	JET1086
XPL(J,IPL)=VPL(IPL)	JET1087
GO TO 1001	JET1088
300 CONTINUE	JET1089
XSF=XPL(J-1,IPL)	JET1090
ISF=2	JET1091
ISN=2	JET1092
CALL INTERP(0,ISF,KF,XSF,XF,RMSF,RMF,RPSF,RPF)	JET1093
CALL RFUNC(RMSF,RPSF,MSF,MUSF,TETASF)	JET1094
XSN=XSF+DY*DTAN(PIA2-TETASF)	JET1095
ITER=1	JET1096
301 ITER=ITER+1	JET1097
CALL INTERP(1,ISN,KN,XSN,XN,RMSN,RMN,RPSN,RPN)	JET1098
CALL RFUNC(RMSN,RPSN,MSN,MUSN,TETASN)	JET1099
TETA AV=0.5D0*(TETASF+TETASN)	JET1100
XSN=XSF+DY*DTAN(PIA2-TETA AV)	JET1101
IF(ITER.LT.ITER0+2) GO TO 301	JET1102
XPL(J,IPL)=XSN	JET1103
GO TO 1001	JET1104
4 CONTINUE	JET1105
C CHARACTERISTIC LINE.	JET1106
KC=IDINT(VPL(IPL)+1.D-5)	JET1107
IF(J.GT.1) GO TO 41	JET1108
XPL(J,IPL)=XCHARF(KC)	JET1109
GO TO 1001	JET1110
41 CONTINUE	JET1111
XPL(J,IPL)=XCHARN(KC)	JET1112
IF(CSIGNN(KC).EQ.0.) XPL(J,IPL)=1.E33	JET1113
GO TO 1001	JET1114
5 CONTINUE	JET1115
C CONSTANT LATERAL (X) OPACITY	JET1116
CALL OPACX	JET1117
XIC=VPL(IPL)	JET1118
DO 51 II=2,KF	JET1119
I1=KF-II+1	JET1120
I2=I1+1	JET1121
XI1=XI(I1,JXI)	JET1122
XI2=XI(I2,JXI)	JET1123
IF((XIC-XI1)*(XIC-XI2).GT.0.) GO TO 51	JET1124
F2=(XI2-XIC)/(XI2-XI1)	JET1125
F1=1.D0-F2	JET1126
IF(F1.LT.0.) CALL FIN(1351)	JET1127
IF(F2.LT.0.) CALL FIN(1352)	JET1128
XIFC=F2*XF(I1)+F1*XF(I2)	JET1129
GO TO 52	JET1130
51 CONTINUE	JET1131
XIFC=1.D30	JET1132
52 CONTINUE	JET1133
XPL(J,IPL)=XIFC	JET1134
GO TO 1001	JET1135
1001 CONTINUE	JET1136
IF(J.GT.1) GO TO 1002	JET1137
YPL(J)=YC	JET1138
GO TO 1000	JET1139
1002 CONTINUE	JET1140
YPL(J)=YN	JET1141
1000 CONTINUE	JET1142
RETURN	JET1143
END	JET1144
GRIDN	
<hr/>	
SUBROUTINE GRIDN	JET1145
C SUBROUTINE NUMBER 14	JET1146
IMPLICIT REAL*8(A-H,L-Z,*)	JET1147
REAL*4 XPL,YPL	JET1148
COMMON /PLUME/XPL(1002,10),YPL(1002)	JET1149
COMMON /IPLUME/KPL,ITYPL(10)	JET1150
COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),	JET1151
1 TETA F(101),BF(101),	JET1152

```

2          XN(101),RMN(101),RPN(101),MN(101),MUN(101),      JET1153
3          TETAN(101),BN(101),XTEMP(101)                    JET1154
COMMON/THICKY/XTH(1002),TH(1002)                            JET1155
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15, JET1156
1          G16,G17,G18,G19,G20                                JET1157
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT, JET1158
1          STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO,  JET1159
2          TETSYM,TETLIM,DDY,DYMAX                          JET1160
COMMON /STAG/RH00,NO,P0,T0,A0,MDOT1                         JET1161
COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J,                  JET1162
1          KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD       JET1163
COMMON /ROW/YF,YN,DXF,DXN                                    JET1164
COMMON /CHARAC/XCHARF(92),YCHARF(92),XCHARN(92),YCHARN(92),  JET1165
1          RMCARF(92),RPCARF(92),RMCARN(92),RPCARN(92),      JET1166
2          TCHARF(92),TCHARN(92),MUCARF(92),MUCARN(92),     JET1167
3          CSIGNN(92),CSIGNF(92),MCHARN(92),MCHARF(92),     JET1168
4          MCHARI(92)                                         JET1169
COMMON /ICHARA/KCHARP,KCHARM,KCHARO                         JET1170
C DIVIDE LINE Y=YN INTO KN-1 INTERVALS.                     JET1171
C THE X-GRID IS NON-UNIFORMLY DEFINED AS FOLLOWS:         JET1172
C (1) (XCHARN(I),YCHARN(I)), (XCHARF(I),YCHARF(I)), I=1,2,...,KCHARP, JET1173
C DENOTE NEW AND OLD (FORMER) CHARACTERISTIC (C+) POINTS. LET I=1 JET1174
C AND I=KCHARP CORRESPOND TO THE LEADING AND BOUNDARY     JET1175
C CHARACTERISTICS (C+).                                     JET1176
C (2) THE GRID CONSISTS OF TWO SEGMENTS. THE SO-CALLED FLAT SEGMENT JET1177
C IS BETWEEN X=0 AND X=XLEAD=XCHARN(KCLEAD). THE SECOND IS THE JET1178
C FAN SEGMENT. IT IS FROM XLEAD TO XBOUND=XCHARN(KCHARP). JET1179
C (3) THE FAN SEGMENT IS INITIALLY DIVIDED INTO FRACG*(KF0-1) INTERVALS JET1180
C DEFINED BY THE FAMILY OF C+ CHARACTERISTIC LINES MCHARI(1) TO JET1181
C MCHARI(KCHARP).                                         JET1182
C (4) THE FLAT SEGMENT IS DIVIDED INTO (1-FRACG)*(KF0-1) EQUAL JET1183
C INTERVALS, AS LONG AS THEY ARE NOT SMALLER THAN THE AVERAGE JET1184
C FAN INTERVAL. WHEN THEY ARE, THEIR NUMBER IS REDUCED, BUT NOT JET1185
C BELOW THREE.                                           JET1186
C (5) KCLEAD IS INITIALLY 1. IT IS UPDATED SO THAT THE FLAT SEGMENT JET1187
C IS AT LEAST TWICE THE AVERAGE FAN INTERVAL.           JET1188
C ILEADF=ILEAD                                             JET1189
C KCLEAD=0                                                 JET1190
C DO 1 KC=1,KCHARP                                         JET1191
C IF(CSIGNN(KC).LT.0.) GO TO 1                             JET1192
C KCLEAD=KC                                                JET1193
C KFAN=KCHARP-KCLEAD                                       JET1194
C XLEAD=XCHARN(KCLEAD)                                     JET1195
C XBOUND=XCHARN(KCHARP)                                    JET1196
C DX1=(XBOUND-XLEAD)/DFLOAT(KFAN)                         JET1197
C IF(XLEAD/DX1.GT.2.DO) GO TO 11                          JET1198
1 CONTINUE                                                JET1199
11 CONTINUE                                                JET1200
C IF(KCLEAD.EQ. 0) CALL FIN(1401)                          JET1201
C IF(KCLEAD.EQ.KCHARP) CALL FIN(1402)                    JET1202
C ILEAD=IDINT(XLEAD/DX1)+2                                 JET1203
C IF(ILEAD+KFAN.GT.KF0) ILEAD=KF0-KFAN                   JET1204
C ILEAD1=ILEAD-1                                           JET1205
C KN=ILEAD+KFAN                                            JET1206
C IF(KN.GT.KF0) CALL FIN(1411)                             JET1207
C DX=XLEAD/DFLOAT(ILEAD1)                                  JET1208
C XN(1)=0.                                                 JET1209
C DO 2 I=1,ILEAD1                                          JET1210
C XN(I)=XN(1)+DX*DFLOAT(I-1)                              JET1211
2 CONTINUE                                                JET1212
C DO 3 I=ILEAD,KN                                          JET1213
C XN(I)=XCHARN(KCLEAD+I-ILEAD)                            JET1214
3 CONTINUE                                                JET1215
C RETURN                                                    JET1216
C END                                                        JET1217
SUBROUTINE YSTEP                                           JET1218
C SUBROUTINE NUMBER 15                                     JET1219
C IMPLICIT REAL*8(A-H,L-Z,*)                              JET1220
C REAL*4 XPL,YPL                                          JET1221
C COMMON /PLUME/XPL(1002,10),YPL(1002)                   JET1222
C COMMON /IPLUME/KPL,ITYPL(10)                            JET1223
C COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101), JET1224

```

YSTEP

```

1          TETAF(101),BF(101),                      JET1225
2          XN(101),RMN(101),RPN(101),MN(101),MUN(101), JET1226
3          TETAN(101),BN(101),XTEMP(101)           JET1227
COMMON/THICKY/XTH(1002),TH(1002)                   JET1228
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15, JET1229
1          G16,G17,G18,G19,G20                      JET1230
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT, JET1231
1          STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NU0, JET1232
2          TETSYM,TETLIM,DDY,DYMAX                JET1233
COMMON /STAG/RH00,NO,PO,TO,A0,MDOT1              JET1234
COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J,       JET1235
1          KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD JET1236
COMMON /ROW/YF,YN,DXF,DXN                         JET1237
COMMON /CHARAC/XCHARF(92),YCHARF(92),XCHARN(92),YCHARN(92), JET1238
1          RMCARF(92),RPCARF(92),RMCARN(92),RPCARN(92), JET1239
2          TCHARF(92),TCHARN(92),MUCARF(92),MUCARN(92), JET1240
3          CSIGNN(92),CSIGNF(92),MCHARN(92),MCHARF(92), JET1241
4          MCHARI(92)                               JET1242
COMMON /ICHARA/KCHARP,KCHARM,KCHARO              JET1243
C COMPUTE NEXT Y-STEP.                            JET1244
C DYNEXT IS DEFINED AS THE MINIMAL "TRIANGULATION" Y-STEP DYT, OBTAINED JET1245
C BY FORWARD INTERSECTION OF C-,C+ CHARACTERISTICS FROM ADJACENT GRID JET1246
C POINTS X1,X2.                                   JET1247
  DYMIN=1.D40                                     JET1248
  DO 1 I=3,KF                                     JET1249
  X1=XF(I-1)                                       JET1250
  X2=XF(I)                                          JET1251
  DX=X2-X1                                         JET1252
  TP1=DTAN(TETAF(I-1)-MUF(I-1))                  JET1253
  TP2=DTAN(TETAF(I)+MUF(I))                      JET1254
  F1=-TP2/(TP1-TP2)                               JET1255
  IF(F1.LE.0.) PRINT 555,I,X1,X2,DX,TP1,TP2,F1   JET1256
555  FORMAT(/1X,'I,X1,X2,DX,TP1,TP2,F1=',I5,6D14.6/) JET1257
  IF(F1.LT.0.) CALL FIN(1501)                     JET1258
  DYT=F1*DX*TP1                                    JET1259
  IF(DYT.LE.0.) CALL FIN(1502)                    JET1260
  DYMIN=DMIN1(DYMIN,STAB*DYT)                     JET1261
1  CONTINUE                                       JET1262
  DYNEXT=DYMIN                                     JET1263
  RETURN                                           JET1264
  END                                             JET1265
SUBROUTINE MOVE
C SUBROUTINE NUMBER 16
  IMPLICIT REAL*8(A-H,L-Z,*)
  REAL*4 XPL,YPL
  COMMON /PLUME/XPL(1002,10),YPL(1002)
  COMMON /IPLUME/KPL,ITYPL(10)
  COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),
1          TETAF(101),BF(101),
2          XN(101),RMN(101),RPN(101),MN(101),MUN(101),
3          TETAN(101),BN(101),XTEMP(101)
COMMON/THICKY/XTH(1002),TH(1002)
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,
1          G16,G17,G18,G19,G20
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,
1          STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NU0,
2          TETSYM,TETLIM,DDY,DYMAX
COMMON /STAG/RH00,NO,PO,TO,A0,MDOT1
COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J,
1          KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD
COMMON /ROW/YF,YN,DXF,DXN
COMMON /CHARAC/XCHARF(92),YCHARF(92),XCHARN(92),YCHARN(92),
1          RMCARF(92),RPCARF(92),RMCARN(92),RPCARN(92),
2          TCHARF(92),TCHARN(92),MUCARF(92),MUCARN(92),
3          CSIGNN(92),CSIGNF(92),MCHARN(92),MCHARF(92),
4          MCHARI(92)
COMMON /ICHARA/KCHARP,KCHARM,KCHARO
C STORE NEW LINE (N) IN OLD LINE (F).
  KF=KN
  KF2=2*KF
  YF=YN
  DO 1 I=1,KN

```

MOVE

	XF(I)=XN(I)	JET1297
	RMF(I)=RMN(I)	JET1298
	RPF(I)=RPN(I)	JET1299
	MF(I)=MN(I)	JET1300
	MUF(I)=MUN(I)	JET1301
	TETAF(I)=TETAN(I)	JET1302
	BF(I)=BN(I)	JET1303
1	CONTINUE	JET1304
	DO 2 KC=1,KCHAR0	JET1305
	IF(CSIGNN(KC).EQ.0.) GO TO 2	JET1306
	XCHARF(KC)=XCHARN(KC)	JET1307
	YCHARF(KC)=YCHARN(KC)	JET1308
	RMCARF(KC)=RMCARN(KC)	JET1309
	RPCARF(KC)=RPCARN(KC)	JET1310
	TCHARF(KC)=TCHARN(KC)	JET1311
	MUCARF(KC)=MUCARN(KC)	JET1312
	MCHARF(KC)=MCHARN(KC)	JET1313
	CSIGNF(KC)=CSIGNN(KC)	JET1314
2	CONTINUE	JET1315
	RETURN	JET1316
	END	JET1317
	OPACX	
	SUBROUTINE OPACX	JET1318
C	SUBROUTINE NUMBER 17	JET1319
	IMPLICIT REAL*8(A-H,L-Z,*)	JET1320
	REAL*4 XPL,YPL	JET1321
	COMMON /PLUME/XPL(1002,10),YPL(1002)	JET1322
	COMMON /IPLUME/KPL,ITYPL(10)	JET1323
	COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),	JET1324
1	TETAF(101),BF(101),	JET1325
2	XN(101),RMN(101),RPN(101),MN(101),MUN(101),	JET1326
3	TETAN(101),BN(101),XTEMP(101)	JET1327
	COMMON/THICKY/XTH(1002),TH(1002)	JET1328
	REAL*4 YXI,XI,XIPM,XIGRP,XIAPP,XIF	JET1329
	COMMON /THICKX/YXI(20),XI(101,20),XIPM(101,20),XIGRP(101,20)	JET1330
1	,XIAPP(101,20),XIF(101,20)	JET1331
	COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,	JET1332
1	G16,G17,G18,G19,G20	JET1333
	COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,	JET1334
1	STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO,	JET1335
2	TETSYM,TETLIM,DDY,DYMAX	JET1336
	COMMON /STAG/RH00,NO,PO,TO,A0,MDOT1	JET1337
	COMMON /CHARAC/XCHARF(92),YCHARF(92),XCHARN(92),YCHARN(92),	JET1338
1	RMCARF(92),RPCARF(92),RMCARN(92),RPCARN(92),	JET1339
2	TCHARF(92),TCHARN(92),MUCARF(92),MUCARN(92),	JET1340
3	CSIGNN(92),CSIGNF(92),MCHARN(92),MCHARF(92),	JET1341
4	MCHARI(92)	JET1342
	COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J,	JET1343
1	KF2,IDEL,JDEL,JYXI,JXI,Ilead,Ileadf,KCLEAD	JET1344
	COMMON /ROW/YF,YN,DXF,DXN	JET1345
C	COMPUTE X-OPACITY.	JET1346
C	BEGIN FROM LIMITING CHARACTERISTIC OF AN ASSUMED P.M. FAN.	JET1347
C	XI0 -- THE THICKNESS BETWEEN THE LIMITING CHARACTERISTIC AND THE	JET1348
C	BOUNDARY CHARACTERISTIC OF THE NUMERICAL COMPUTATION.	JET1349
	DO 12 I=1,KF0	JET1350
	XIF(I,JXI)=XF(I)	JET1351
	XI(I,JXI)=0.	JET1352
	XIPM(I,JXI)=0.	JET1353
	XIGRP(I,JXI)=0.	JET1354
	XIAPP(I,JXI)=0.	JET1355
12	CONTINUE	JET1356
	IF(J.EQ.1) GO TO 1000	JET1357
	PSILIM=TETLIM	JET1358
	XLIM=XC+(YF-YC)/DTAN(PSILIM)	JET1359
	XBOUND=XF(KF)	JET1360
	KPM=10	JET1361
	DX=(XLIM-XBOUND)/DFLOAT(KPM)	JET1362
	SUM=0.	JET1363
	DO 1 I=1,KPM	JET1364
	X1=XBOUND+DFLOAT(I-1)*DX	JET1365
	X2=X1+DX	JET1366
	PS1=PAI2-DATAN((X1-XC)/(YF-YC))	JET1367
	PS2=PAI2-DATAN((X2-XC)/(YF-YC))	JET1368


```

Q1=(PS1-PSILIM)/G5
Q2=(PS2-PSILIM)/G5
IF(I.EQ.KPM) Q2=1.D-10
IF(Q2.LT.0.) CALL FIN(1701)
F1=G11*(DSIN(Q1))**(2.DO/(G-1.DO))
F2=G11*(DSIN(Q2))**(2.DO/(G-1.DO))
SUM=SUM+DX*(F1+F2)/2.DO
1 CONTINUE
XIO=SUM*(NO*SIGMA)
C RE-EVALUATE XIO FOR A RING-JET.
IF(Delta.EQ.0.) GO TO 14
M=MFIN
CALL MFUNC(M,F,ETA,TETA)
PSI=TETA+DARSIN(1.DO/M)
GOREM=1.DO+G1*M**2
GOR=M**2-1.DO
CALL HINTER(M,HM)
DELTOB=0.5DO*DSQRT(GOR)*(1.DO/(MEXIT*ETA)+DSIN(TETA)/M)/DSIN(PSI)
1 +G15*HM/2.DO
EVER=SIGMA*NO*YC/(M*DSIN(TETA)*DSIN(PSI)*GOREM**G6)
GGG=2.DO-DELTOB*(G+1.DO)/2.DO
IF(DABS(GGG).GT.1.D-10) GO TO 15
PRINT 16, DELTOB,G,GGG
16 FORMAT(/1X,'FROM OPACX. GGG NEARLY ZERO. EXPRESSION FOR XIO IS',
1 1X,'SINGULAR. DELTOB,G,GGG=',3D12.4/)
CALL FIN(1715)
15 CONTINUE
EVER=EVER/GGG
XIO=EVER*((YF/YC)**GGG-1.DO)/(YF/YC)
14 CONTINUE
XI(KF,JXI)=XIO
XIPM(KF,JXI)=XIO
XIGRP(KF,JXI)=XIO
KF1=KF-1
DO 2 II=1,KF1
I=KF-II+1
X1=XF(I)
X2=XF(I-1)
DX=X1-X2
F1=1.DO/(1.DO+G1*MF(I)**2)**G6
F2=1.DO/(1.DO+G1*MF(I-1)**2)**G6
DTNUM=(NO*SIGMA)*DX*(F1+F2)/2.DO
XI(I-1,JXI)=XI(I,JXI)+DTNUM
XIPM(I-1,JXI)=1.D24
XIGRP(I-1,JXI)=1.D24
PS1=PAI2-DATAN((X1-XC)/(YF-YC))
PS2=PAI2-DATAN((X2-XC)/(YF-YC))
IF(PS2.GT.PSI1) GO TO 2
Q1=(PS1-PSILIM)/G5
Q2=(PS2-PSILIM)/G5
IF(Q1.LT.0.) CALL FIN(1711)
F1=G11*(DSIN(Q1))**(2.DO/(G-1.DO))
F2=G11*(DSIN(Q2))**(2.DO/(G-1.DO))
DTPM=(NO*SIGMA)*DX*(F1+F2)/2.DO
XIPM(I-1,JXI)=XIPM(I,JXI)+DTPM
DIST1=DSQRT((X1-XC)**2+(YF-YC)**2)
DIST2=DSQRT((X2-XC)**2+(YF-YC)**2)
KC1=KCLEAD+I-ILEAD
KC2=KC1-1
IF(KC2.LT.KCLEAD) GO TO 21
M1=MCHARI(KC1)
M2=MCHARI(KC2)
CALL MATCH(I,M1,MG1,MOBI1,MABI1)
CALL MATCH(I-1,M2,MG2,MOBI2,MABI2)
F1=1.DO/(1.DO+G1*MG1**2)**G6
F2=1.DO/(1.DO+G1*MG2**2)**G6
DTGRP=(NO*SIGMA)*DX*(F1+F2)/2.DO
XIGRP(I-1,JXI)=XIGRP(I,JXI)+DTGRP
21 CONTINUE
2 CONTINUE
C APPROXIMATE THICKNESS XIAPP(I,JXI). BASED ON CLOSED-FORM INTEGRATION.
DO 3 I=1,KF

```

JET1369
JET1370
JET1371
JET1372
JET1373
JET1374
JET1375
JET1376
JET1377
JET1378
JET1379
JET1380
JET1381
JET1382
JET1383
JET1384
JET1385
JET1386
JET1387
JET1388
JET1389
JET1390
JET1391
JET1392
JET1393
JET1394
JET1395
JET1396
JET1397
JET1398
JET1399
JET1400
JET1401
JET1402
JET1403
JET1404
JET1405
JET1406
JET1407
JET1408
JET1409
JET1410
JET1411
JET1412
JET1413
JET1414
JET1415
JET1416
JET1417
JET1418
JET1419
JET1420
JET1421
JET1422
JET1423
JET1424
JET1425
JET1426
JET1427
JET1428
JET1429
JET1430
JET1431
JET1432
JET1433
JET1434
JET1435
JET1436
JET1437
JET1438
JET1439
JET1440

```

XIAPP(I, JXI)=1.D24
KC=KCLEAD+(I-I-ILEAD)
IF(Delta.EQ.0.) GO TO 3
IF(KC.LT.KCLEAD) GO TO 3
IF(XF(I).LT.XCHARF(1)) GO TO 3
M=MCHARI(KC)
CALL MFUNC(M, F, ETA, TETA)
PSI=TETA+DARSIN(1.D0/M)
GOREM=1.D0+G1*M**2
GOR=M**2-1.D0
CALL HINTER(M, HM)
DELTOB=0.5D0*DSQRT(GOR)*(1.D0/(MEXIT*ETA)+DSIN(TETA)/M)/DSIN(PSI)
1 +G15*HM/2.D0
EVER=SIGMA*NO*YC/(M*DSIN(TETA)*DSIN(PSI)*GOREM**G6)
GGG=2.D0-DELTOB*(G+1.D0)/2.D0
IF(DABS(GGG).GT.1.D-10) GO TO 25
PRINT 26, I, KC, M, DELTOB, G, GGG
26 FORMAT(/1X, 'FROM OPACX. GGG NEARLY ZERO. EXPRESSION FOR XI0 IS',
1 1X, 'SINGULAR. I, KC, M=', I5, D12.4/
2 1X, 'DELTOB, G, GGG=', 3D12.4/)
CALL FIN(1725)
25 CONTINUE
EVER=EVER/GGG
XIAPP(I, JXI)=EVER*((YF/YC)**GGG-1.D0)/(YF/YC)
3 CONTINUE
1000 CONTINUE
RETURN
END

```

LOADC

```

SUBROUTINE LOADC
C SUBROUTINE NUMBER 18
IMPLICIT REAL*8(A-H, L-Z, $)
REAL*4 XPL, YPL
COMMON /PLUME/XPL(1002, 10), YPL(1002)
COMMON /IPLUME/KPL, ITYPL(10)
COMMON /VECS/XF(101), RMF(101), RPF(101), MF(101), MUF(101),
1 TETA(101), BF(101),
2 XN(101), RMN(101), RPN(101), MN(101), MUN(101),
3 TETAN(101), BN(101), XTEMP(101)
COMMON/THICKY/XTH(1002), TH(1002)
REAL*4 YXI, XI, XIPM, XIGRP, XIAPP, XIF
COMMON /THICKX/YXI(20), XI(101, 20), XIPM(101, 20), XIGRP(101, 20)
1 , XIAPP(101, 20), XIF(101, 20)
COMMON /GAMA/G, G1, G2, G3, G4, G5, G6, G7, G8, G9, G10, G11, G12, G13, G14, G15,
1 G16, G17, G18, G19, G20
COMMON /PAR/PAI, PAI2, DEG, XC, YC, MEXIT, MFIN, YMAX, DY0, DY, DYNEXT,
1 STAB, DELTA, PSI1, PSIF, ZETA1, SIGMA, FRACG, EPSIL, NUO,
2 TETSYM, TETLIM, DDY, DYMAX
COMMON /STAG/RH00, NO, P0, T0, A0, MDOT1
COMMON /IPAR/JMAX, KFO, ITER0, KF, KN, IM, IP, J,
1 KF2, IDEL, JDEL, JYXI, JXI, ILEAD, ILEADF, KCLEAD
COMMON /ROW/YF, YN, DXF, DXN
COMMON /CHARAC/XCHARF(92), YCHARF(92), XCHARN(92), YCHARN(92),
1 RMCARF(92), RPCARF(92), RMCARN(92), RPCARN(92),
2 TCHARF(92), TCHARN(92), MUCARF(92), MUCARN(92),
3 CSIGNN(92), CSIGNF(92), MCHARN(92), MCHARF(92),
4 MCHARI(92)
COMMON /ICHARA/KCHARP, KCHARM, KCHARO
C LOAD FLOW VARIABLES OF GRID POINTS IN THE FAN SEGMENT FROM THE
C SEMI-INVERSE INTEGRATION (IN SUBR. SEMINV). NOTE THAT GRID POINTS
C XN(I) WERE ALREADY DETERMINED IN SUBR. GRIDN.
DO 1 I=ILEAD, KN
KC=KCLEAD+I-I-ILEAD
IF(KC.GT.KCHARP) CALL FIN(1801)
RMN(I)=RMCARN(KC)
RPN(I)=RPCARN(KC)
MN(I)=MCHARN(KC)
MUN(I)=MUCARN(KC)
TETAN(I)=TCHARN(KC)
1 CONTINUE
RETURN
END

```

NUFUNC

```

DOUBLE PRECISION FUNCTION NUFUNC(M)

```

```

C SUBROUTINE NUMBER 19
  IMPLICIT REAL*8(A-H,L-Z,*)
  REAL*4 XPL,YPL
  COMMON /PLUME/XPL(1002,10),YPL(1002)
  COMMON /IPLUME/KPL,ITYPL(10)
  COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),
1     TETAF(101),BF(101),
2     XN(101),RMN(101),RPN(101),MN(101),MUN(101),
3     TETAN(101),BN(101),XTEMP(101)
  COMMON/THICKY/XTH(1002),TH(1002)
  REAL*4 YXI,XI,XIPM,XIGRP,XIAPP,XIF
  COMMON /THICKX/YXI(20),XI(101,20),XIPM(101,20),XIGRP(101,20)
1     ,XIAPP(101,20),XIF(101,20)
  COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,
1     G16,G17,G18,G19,G20
  COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,
1     STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO,
2     TETSYM,TETLIM,DDY,DYMAX
  COMMON /STAG/RH00,NO,PO,TO,AO,MDOT1
  COMMON /IPAR/JMAX,KFO,ITERO,KF,KN,IM,IP,J,
1     KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD
  COMMON /ROW/YF,YN,DXF,DXN
  COMMON /CHARAC/XCHARF(92),YCHARF(92),XCHARN(92),YCHARN(92),
1     RMCARF(92),RPCARF(92),RMCARN(92),RPCARN(92),
2     TCHARF(92),TCHARN(92),MUCARF(92),MUCARN(92),
3     CSIGNN(92),CSIGNF(92),MCHARN(92),MCHARF(92),
4     MCHARI(92)
  COMMON /ICHARA/KCHARP,KCHARM,KCHARO
C COMPUTE NU AS FUNCTION OF MACH NUMBER M. NOTE THAT THE P.M.
C DEFINITION OF NU HAS BEEN MODIFIED BY ADDING A CONSTANT. THE USUAL
C CHOICE OF THE CONSTANT IS SUCH THAT NU=0 FOR INFINITE M.
  Q=1.DO/DSQRT(M**2-1.DO)
  NUFUNC=NUO-(G5*DATAN(G5*Q)-DATAN(Q))
  RETURN
  END

```

HMSET

```

SUBROUTINE HMSET
C SUBROUTINE NUMBER 20
  IMPLICIT REAL*8(A-H,L-Z,*)
  REAL*8 KAPA0B
  COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,
1     G16,G17,G18,G19,G20
  COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,
1     STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO,
2     TETSYM,TETLIM,DDY,DYMAX
  COMMON /IPAR/JMAX,KFO,ITERO,KF,KN,IM,IP,J,
1     KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD
  COMMON /GRP/DMINV,MHINV(101),HMOV(101)
  COMMON /IGRP/KHM
C A ROUTINE FOR THE C+ DERIVATIVE DUE TO RING SYMMETRY (GRP).
  KHM=51
  IF(KHM.GT.101) CALL FIN(2001)
  MINVO=1.DO/MEXIT
  DMINV=MINVO/DFLOAT(KHM-1)
  M=MEXIT
  SUM=0.
  KHM1=KHM-1
  DO 1 I=1,KHM1
  MF=M
  MHINV(I)=MINVO-DFLOAT(I-1)*DMINV
  M=1.DO/MHINV(I)
  DM=M-MF
  M1=M-DM
  M2=M-DM/2.DO
  M3=M
  CALL MFUNC(M1,F1,ETA1,TETA1)
  CALL MFUNC(M2,F2,ETA2,TETA2)
  CALL MFUNC(M3,F3,ETA3,TETA3)
  SUM=SUM+DM*(F1+4.DO*F2+F3)/6.DO
  ETA=ETA3
  TETA=TETA3
  PSI=TETA+DARSIN(1.DO/M)
  NGRM=((3.DO-G)/4.DO)*(M**2-1.DO)**0.75DO/

```

```

1      (DSIN(PSI)*(1.DO+G1*M**2)**G14) JET1585
HM=SUM*NORM JET1586
HNV(I)=HM JET1587
GOREM=1.DO+G1*M**2 JET1588
GOR=M**2-1.DO JET1589
DELTOB=0.5D0*DSQRT(GOR)*(1.DO/(MEXIT*ETA)+DSIN(TETA)/M)/DSIN(PSI) JET1590
1      +((G+1.DO)/(2.DO*(3.DO-G)))*HM JET1591
EPSIOB=DELTOB/DSQRT(GOR)-DSIN(TETA)/(M*DSIN(PSI)) JET1592
KAPAOB=1.DO JET1593
IF(DABS(PIA2-TETA).GT.1.D-6) JET1594
1KAPAOB=DTAN(TETA)*EPSIOB JET1595
LAMDOB=EPSIOB-DELTOB*GOREM/(GOR*DSQRT(GOR)) JET1596
PRINT 11,I,M,HM,TETA*DEG,PSI*DEG JET1597
11  FORMAT(1X,' I,M,HM,TETA,PSI=',I5,5D12.4) JET1598
PRINT 12,DELTOB,EPSIOB*DEG,KAPAOB*DEG,LAMDOB*DEG JET1599
12  FORMAT(1X,'DELTOB,EPSIOB,KAPAOB,LAMDOB=',5X,5D12.4) JET1600
1  CONTINUE JET1601
MHINV(KHM)=0. JET1602
HNV(KHM)=1.DO JET1603
RETURN JET1604
END JET1605
MFUNC
SUBROUTINE MFUNC(M,F,ETA,TETA) JET1606
C  SUBROUTINE NUMBER 21 JET1607
IMPLICIT REAL*8(A-H,L-Z,*) JET1608
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15, JET1609
1      G16,G17,G18,G19,G20 JET1610
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT, JET1611
1      STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO, JET1612
2      NUPT1,TETLIM JET1613
COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J, JET1614
1      KF2,IDEL,JDEL,JYXI,JXI,Ilead,Ileadf,KCLEAD JET1615
COMMON /GRP/DMINV,MHINV(101),HNV(101) JET1616
C  NU=NUFUNC(M) JET1617
TETA=NUFUNC(MEXIT)+PAI2-NU JET1618
GOREM=1.DO+G1*M**2 JET1619
GOR=M**2-1.DO JET1620
F=(M**2)*(GOREM**G13)*DSIN(TETA)/GOR**1.25D0 JET1621
GOREM1=1.DO+G1*MEXIT**2 JET1622
GOR1=MEXIT**2-1.DO JET1623
ETA=((GOREM/GOREM1)**G14)*((GOR1/GOR)**0.25D0) JET1624
RETURN JET1625
END JET1626
SUBROUTINE HINTER(M,H) JET1627
C  SUBROUTINE NUMBER 22 JET1628
IMPLICIT REAL*8(A-H,L-Z,*) JET1629
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15, JET1630
1      G16,G17,G18,G19,G20 JET1631
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT, JET1632
1      STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO, JET1633
2      TETSYM,TETLIM,DDY,DYMAX JET1634
COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J, JET1635
1      KF2,IDEL,JDEL,JYXI,JXI,Ilead,Ileadf,KCLEAD JET1636
COMMON /GRP/DMINV,MHINV(101),HNV(101) JET1637
COMMON /IGRP/KHM JET1638
C  COMPUTE H(M) BY INTERPOLATION JET1639
MINV=1.DO/M JET1640
I=KHM-IDINT(MINV/DMINV-1.D-9)-1 JET1641
IF(I.GE.1.AND.I.LT.KHM) GO TO 1 JET1642
PRINT 11,I,KHM,M,MEXIT JET1643
11  FORMAT(1X,'I,KHM,M,MEXIT=',2I5,2D14.6/) JET1644
CALL FIN(2201) JET1645
1  CONTINUE JET1646
F1=(MINV-MHINV(I+1))/DMINV JET1647
F2=1.DO-F1 JET1648
IF(F1.LT.-1.D-9) CALL FIN(2210) JET1649
IF(F2.LT.-1.D-9) CALL FIN(2211) JET1650
H=F1*HNV(I)+F2*HNV(I+1) JET1651
RETURN JET1652
END JET1653
SUBROUTINE MATCH(I,MOB,MAB,MOBI,MABI) JET1654
C  SUBROUTINE NUMBER 23 JET1655
JET1656

```

```

IMPLICIT REAL*8(A-H,L-Z,*)
COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),
1      TETAF(101),BF(101),
2      XN(101),RMN(101),RPN(101),MN(101),MUN(101),
3      TETAN(101),BN(101),XTEMP(101)
COMMON /ROW/YF,YN,DXF,DXN
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,
1      G16,G17,G18,G19,G20
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,
1      STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO,
2      TETSYM,TETLIM,DDY,DYMAX
COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J,
1      KF2,IDEL,JDEL,JYXI,JXI,Ilead,Ileadf,KCLEAD
COMMON /GRP/DMINV,MHINV(101),HMV(101)
COMMON /IGRP/KHM
C COMPUTE H(M) AND THE ALFA-DERIVATIVES
M=MOB
CALL MFUNC(M,F,ETA,TETA)
PSI=TETA+DARSIN(1.DO/M)
CALL HINTER(M,HM)
GOREM=1.DO+G1*M**2
GOR=M**2-1.DO
DELTOB=0.5D0*DSQRT(GOR)*(1.DO/(MEXIT*ETA)+DSIN(TETA)/M)/DSIN(PSI)
1 +G15*HM/2.DO
FOB=(G7*GOREM)**G2/M
FAB=FOB*(YF/YC)**DELTOB
CALL AREAAF(FAB,MAB)
C COMPUTE MABI FROM THE INVERSE PROBLEM SOLUTION
COTAV=(XF(I)-XC)/(YF-YC)
PSI0=PAI2-DATAN(COTAV)
EVY=YF*DLOG(YF/YC)/(YF-YC)-1.DO
PSIN=PSI0
DO 1 ITER=1,50
PSI=PSIN
M=DSQRT(1.DO+G4/DTAN((PSI-TETLIM)/G5)**2)
M=DMAX1(M,MEXIT)
CALL HINTER(M,HM)
CALL MFUNC(M,F,ETA,TETA)
GOREM=1.DO+G1*M**2
GOR=M**2-1.DO
DELTOB=0.5D0*DSQRT(GOR)*(1.DO/(MEXIT*ETA)+DSIN(TETA)/M)/DSIN(PSI)
1 +G15*HM/2.DO
EPSI0B=DELTOB/DSQRT(GOR)-DSIN(TETA)/(M*DSIN(PSI))
LAMDOB=EPSI0B-DELTOB*GOREM/(GOR*DSQRT(GOR))
COTN=COTAV+LAMDOB*EVY/DSIN(PSI)**2
PSIN=PAI2-DATAN(COTN)
DPSI=PSIN-PSI
IF(DABS(DPSI).LT.1.D-9) GO TO 11
1 CONTINUE
PRINT 12,I,ITER,PSI,PSIN,DPSI,M,XF(I),YF,XC,YC
12 FORMAT(/1X,'I,ITER,PSI,PSIN,DPSI,M,XF(I),YF,XC,YC='//
1 1X,2I4,8D11.3/)
CALL FIN(2301)
11 CONTINUE
C USING MOBI=M AS COMPUTED FROM THE INVERSE PROBLEM, FIND MABI.
MOBI=M
M=MOBI
CALL MFUNC(M,F,ETA,TETA)
PSI=TETA+DARSIN(1.DO/M)
CALL HINTER(M,HM)
GOREM=1.DO+G1*M**2
GOR=M**2-1.DO
DELTOB=0.5D0*DSQRT(GOR)*(1.DO/(MEXIT*ETA)+DSIN(TETA)/M)/DSIN(PSI)
1 +G15*HM/2.DO
FOB=(G7*GOREM)**G2/M
FAB=FOB*(YF/YC)**DELTOB
CALL AREAAF(FAB,MABI)
RETURN
END
SUBROUTINE AREAAF(F,M)
C SUBROUTINE NUMBER 24
IMPLICIT REAL*8(A-H,L-Z,*)

```

AREAAF

```

COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15, JET1729
1      G16,G17,G18,G19,G20 JET1730
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DYO,DY,DYNEXT, JET1731
1      STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO, JET1732
2      TETSYM,TETLIM,DDY,DYMAX JET1733
COMMON /IPAR/JMAX,KFO,ITERO,KF,KN,IM,IP,J, JET1734
1      KF2,IDEL,JDEL,JYXI,JXI,Ilead,ILEADF,KCLEAD JET1735
COMMON /GRP/DMINV,MHINV(101),HNV(101) JET1736
COMMON /IGRP/KHM JET1737
C COMPUTE MACH NUMBER M FROM AREA RATIO FUNCTION F JET1738
C  $F = ((2/(G+1)) * (1+(G-1)*M**2)) ** ((G+1)/(2*(G-1))) / M$  JET1739
C INITIAL GUESS IS MIN JET1740
E1=(F*MEXIT)**(1.D0/G2)/G7 JET1741
E2=(E1-1.D0)/G1 JET1742
E3=DMAX1(E2,MEXIT**2) JET1743
MIN=DSQRT(E3) JET1744
EMN=MIN JET1745
DO 1 I=1,100 JET1746
EMO=EMN JET1747
GOREM=1.D0+G1*EMO**2 JET1748
GOR=EMO**2-1.D0 JET1749
FO=(G7*GOREM)**G2/EMO JET1750
DF=FO-F JET1751
C PRINT 123,I,EMO,EMN,FO,F,DF,GOR,GOREM JET1752
C123 FORMAT(1X,'I,EMO,EMN,FO,F,DF,GOR,GOREM=',I5,7D12.4) JET1753
DFDM=FO*GOR/(EMO*GOREM) JET1754
DMN=DF/DFDM JET1755
EMN=EMO-DMN JET1756
EPSEM=DABS(DMN/EMN) JET1757
IF(EPSEM.LT.1.D-10) GO TO 11 JET1758
1 CONTINUE JET1759
CALL FIN(2401) JET1760
11 CONTINUE JET1761
M=EMN JET1762
RETURN JET1763
END JET1764

```

5. REFERENCES

- [1] Falcovitz, J., "Analytic and Numerical Computation of Ring-Symmetric Spacecraft Exhaust Plumes", Naval Postgraduate School, Monterey, CA, Report NPS72-86-003CR, December 1986.
- [2] Liepmann, H. W. and Roshko, A., *Elements of Gasdynamics*, John Wiley, New York, 1957.
- [3] Abramovich, S., "Gas Dynamics of Laser Exhaust External to Spacecraft", Naval Postgraduate School, Monterey, CA, Contractor Report NPS67-84-006CR, Nov. 1985.
- [4] Zucrow, M. J. and Hoffman, J. D., *Gas Dynamics*, John Wiley, New York, 1976.
- [5] Bird, G. A., *Molecular Gas Dynamics*, Clarendon Press, Oxford, 1976.
- [6] Bird, G. A., "Breakdown of Continuum Flow in Free Jets and Rocket Plumes", Proceedings of 12th Symposium on Rarefied Gas Dynamics. In Volume 74, *Progress in Astronautics and Aeronautics*, Part II, p.681, Sam S. Fisher, Editor. Published by AIAA, 1981.
- [7] Falcovitz, J., "A Breakdown Surface Model for Thermal Backscattering from the Exhaust Plume of a Space-Based HF Laser", Naval Postgraduate School, Monterey, CA, Report NPS67-86-002CR, June 1986.

6. DISTRIBUTION LIST

No. of Copies

- 1. Defense Technical Information Center
Cameron Station
Alexandria, VA 22314 2

- 2. Library, Code 0142
Naval Postgraduate School
Monterey, CA 93943-5100. 2

- 3. Department Chairman, Code 67
Department of Aeronautics
Naval Postgraduate School
Monterey, CA 93943-5100. 1

- 4. Distinguished Professor Allen E. Fuhs
Space Systems Academic Group, Code 72
Naval Postgraduate School
Monterey, CA 93943-5100. 5

- 5. Dr. Neil Griff
SDIO/DEO
Washington, DC 20301-7100. 3

- 6. Mr. Bruce Pierce
SDIO/DEO
Washington, DC 20301-7100. 1

- 7. Dr. Joseph Falcovitz
Code 72
Naval Postgraduate School
Monterey, CA 93943-5100. 5

- 8. Professor Max F. Platzer
 Department of Aeronautics, Code 67
 Naval Postgraduate School
 Monterey, CA 93943-5100. 1

- 9. Professor Oscar Biblarz
 Department of Aeronautics, Code 67
 Naval Postgraduate School
 Monterey, CA 93943-5100. 1

- 10. Professor David W. Netzer
 Department of Aeronautics, Code 67
 Naval Postgraduate School
 Monterey, CA 93943-5100. 1

- 11. Research Administration Office
 Code 012
 Naval Postgraduate School
 Monterey, CA 93943-5100. 1

- 12. Dr. P. Avizonis
 Air Force Weapons Laboratory
 Kirtland Air Force Base, NM 87117 1

- 13. Dr. John Lawless
 Space Power Inc.
 1977 Concourse Drive
 San Jose, CA 95131 1

- 14. Dr. Mark Thornton
 Boeing Aerospace Company
 Post Office Box 3999
 Seattle, WA 98124-2499 1

No. of Copies

- 15. LT. Mark Price
AFRPL
Edwards AFB, CA 93523 1

- 16. Mr. Arthur W. Rogers
Space Systems Division
Hughes Aircraft Co.
P. O. Box 92919, Los Angeles, CA 90009 1

- 17. LCOL Rick Babcock, USAF
Air Force Geophysical Laboratory
Hanscomb Field
Bedford, MA 01730 1

- 18. Dr. James Stark Draper
Aerodyne Research, Inc.
45 Manning Road
Billerica, MA 01821 1

END

9-87

Dtic