

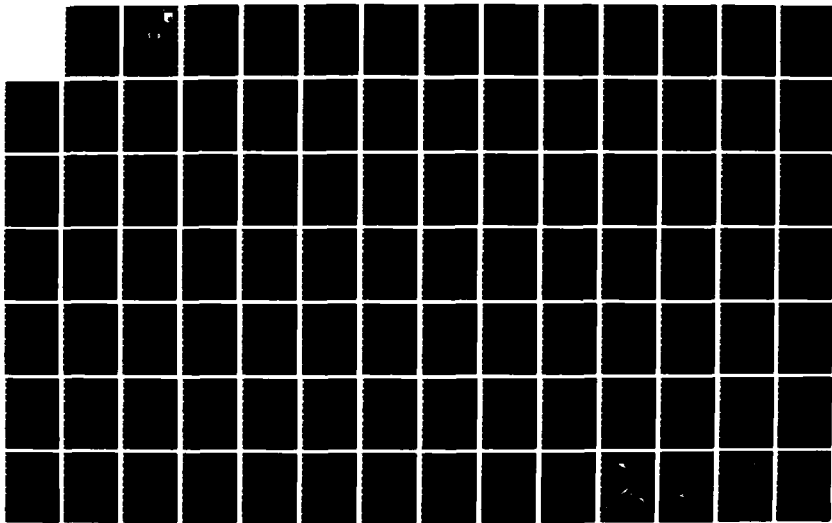
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VISCID/INVISCID SEPARATED FLOWS



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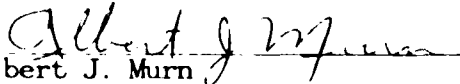
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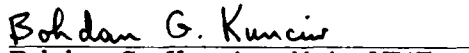
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This technical report has been reviewed and is approved for publication.


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FOREWORD

This report was prepared for the United States Air Force by the Douglas Aircraft Company, Long Beach, California, and the McDonnell Aircraft Company, St. Louis, Missouri in partial fulfillment of Contract Number F33615-83-C-3026. This report describes a method for calculating the flowfield about fighter aircraft geometries in the presence of flow separation, and includes comparisons with test data for three fighter configurations.

The contract was under the direction of Mr. Albert J. Murn of the Air Force Flight Dynamics Laboratory, Wright-Patterson Air Force Base, Ohio. His efforts and forbearance are gratefully acknowledged.



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SECTION I INTRODUCTION

In past years aircraft configuration design was accomplished mainly by wind tunnel testing while flow-calculation methods contributed little because they were limited to simple geometries and restricted in the physical processes that they represented. This virtually exclusive reliance on testing had disadvantages which led to less-than-optimum designs. Each potential configuration had to be fabricated as a wind tunnel model with corresponding expense and time delay and, if the tests suggested design changes, the process should have been repeated, though on occasions this could not be done because of the time and expense involved in an iteration cycle. Moreover, tests provide incomplete information in that, for example, static-measurements may be restricted to a small number of locations. Force and moment data are seldom explained in terms of flow phenomena and the extent of separated regions is usually not determined. Finally, there is the necessary scaling from model to full-scale vehicle which can be uncertain so that, for example, separation observed on a model may be different from that encountered in full scale.

Intensive efforts have been pursued for many years to help to overcome the limitations of calculation methods and to develop them to represent accurately the flows over airplane configurations. Regardless of the specific algorithm employed, the cost and especially the elapsed time required to develop a numerical representation of a given configuration is much less than that required for an experimental test. Once such a basic numerical model has been developed, many variations on the design can be investigated computationally and only the most promising selected for wind-tunnel testing. A flow computation method is required to represent the geometry of the airplane and the essential properties of the fluid and, to achieve the objective, limitations of calculation methods have been removed in recent years by the development of new and powerful calculation tools.

There are three possible approaches which can be used for the calculation of the viscous flow over an aircraft configuration. The first approach makes use of the Reynolds-averaged Navier-Stokes equations and various reduced forms including the so-called parabolized and thin-layer Navier-Stokes equations. Significant advances have been made in this area, for example, by Shang and

Scherr [1] who made the first attempt to numerically simulate the flowfield around a complete aircraft by solving the Navier-Stokes equations. To demonstrate the feasibility of their approach, they chose the hypersonic research aircraft X24C-10D for which a detailed experimental database exists. Using a mesh system around 5×10^5 nodes, they performed impressive calculations at an angle of attack of six degrees with a nominal Mach number of 5.95, and indicated areas where future research should concentrate to make this approach more efficient and practical.

The second and third approaches both make use of solutions of inviscid and viscous flow equations coupled by special procedures. The second approach is based on the two-dimensional method developed by Gilmer and Bristow [2] in which an empirical inviscid flow model is used to represent the effects of flow separation [2,3]. A direct boundary-layer calculation is employed up to the point of separation. Downstream of this point, a free surface is introduced to model the separated flow region. The shape and the length of the separation zone are computed by satisfying a constant pressure boundary condition on the surface and very good results have been obtained for airfoils at a wide range of angles of attack including stall.

The third approach, which is referred to as the interactive boundary-layer approach, uses special coupling techniques between inviscid and viscous flows and novel numerical procedures. The particular form developed by Cebeci et al. [4] is very general and allows any inviscid flow method to be coupled with solutions of the boundary-layer equations. For example, in its application to two-dimensional subsonic flows over airfoils, it employs Halsey's inviscid procedure [5] based on the conformal mapping and Fourier analysis techniques and computes the flow over the airfoil and wake. Successive viscous sweeps are performed, after each of which the external inviscid solution is recomputed, until a converged solution is obtained. The boundary-layer method, which is an inverse finite-difference scheme developed by Cebeci [6], uses an algebraic eddy-viscosity formulation due to Cebeci and Smith [7] and is able to compute flows with large regions of separation without numerical problems. In regions of reverse flow, it uses the FLARE approximation [8] in which the streamwise convective term is set equal to zero in the recirculating region. A detailed description of the method and of its application to a range of airfoils at angles of attack up to and including stall is provided in [4]. The results

presented in Section 3.1 show that this procedure has removed a major obstacle in that flows with large regions of separation can now be computed accurately.

A comparison between the interactive procedure [4] and a method based on the thin-Navier-Stokes equation has been reported in [9] for the NACA 0012 airfoil. This study demonstrated that the Navier-Stokes approach and the interactive boundary-layer approach gave comparable results up to the stall angle. However, the interactive boundary-layer approach required much less computing time.

The purpose of the present work is to develop a general method for computing three-dimensional flows on wings with leading- and trailing-edge separation. The second and third approaches, described above, have been critically examined to determine the extent to which they can fulfill this purpose. It was considered that the second approach should be more suited to large regions of trailing-edge separation whereas the third approach should be more appropriate for leading-edge separation bubbles. Extensive tests showed that the second approach failed to converge in those situations for which it was intended and, although it was satisfactory for flows with small trailing-edge separation, considerable effort may still be required to overcome its limitations. The third approach on the other hand, has proved to be able to represent leading- and trailing-edge separation without limitations, as discussed further in Section 3.0.

The remainder of this report has been arranged in five sections. In Section 2.0, the inviscid method is briefly described prior to more extensive descriptions of interactive boundary-layer methods based on strip theory and quasi-three-dimensional approximations. The viscous-flow equations, transformations and solution procedure have been described previously in [4] for two-dimensional flows and in [10] for quasi-three-dimensional flows. Results obtained with these procedures are presented in Section 3.0 for several configurations and the relative merits of the two interactive approaches are considered. The computer program, which embodies both methods is described in Section 4.0 and sample input data for the three contract test cases are presented in Section 5.0. The report ends with a summary of the more important conclusions in Section 6.0.

SECTION II

DESCRIPTION OF THE INTERACTIVE BOUNDARY-LAYER METHODS

The method described here combines inviscid flow and inverse boundary layer procedures in an interactive manner which permits the calculation of flows with leading and trailing-edge separation. According to this method, the inviscid method of Section 2.1 is used to compute the flow over the given configuration with a zero normal velocity boundary condition. The resulting pressure distribution serves as a boundary condition for the boundary layer method of Section 2.2 which computes all relevant boundary layer parameters, including a surface blowing distribution to simulate the displacement thickness effect. While the inviscid-flow calculations (see Section 2.1) are performed for the entire configuration, viscous flow calculations are presently restricted to the wing and make use of strip theory and quasi three dimensional approximations discussed in Section 2.2.

The viscous effects computed by the boundary-layer method are then used to determine a distribution of normal velocity on the surface. The inviscid flow method is used for a second time with this blowing velocity distribution as a boundary condition and the procedure is repeated until convergence.

2.1 Inviscid Flow Method

The inviscid flow method, which is the first-order surface-source panel method developed by Hess, is capable of computing flow about completely arbitrary configurations. Because of its robustness and its availability, it has been acquired by several dozen facilities around the country and applied not only to aircraft but also to ships, submarines, automobiles, buildings, and topographical features. The three-dimensional body is represented by a set of plane quadrilateral panels, as shown in Fig. 1*. A three-dimensional body consists of lifting and nonlifting portions. A lifting portion, such as a wing or pylon, is characterized by having a well-defined trailing edge, from which issues a trailing vortex wake and along which the Kutta condition is applied. Nonlifting portions of the body lack such trailing edges. Every panel has a constant value of source strength σ . Panels of lifting portions have, in addition, a quadratically varying doublet strength μ . Values of source

*Figures begin on page .

density on the panels are independent parameters available for satisfying the boundary condition. The chordwise dipole variation over the panels of a lifting strip (Fig. 1) is assumed in a form that leads to favorable numerics, so that the dipole strength is reduced to a single adjustable parameter - the circulation on that strip. Thus the set of independent dipole parameters equals the number of locations where the Kutta condition is enforced, i.e., at the trailing-edge segment of each strip.

The nature of the Kutta condition adopted by the many panel methods which are currently available varies greatly. The condition adopted by Hess [11] is the physically meaningful condition of equal upper and lower surface pressures at the trailing edge. All other methods make use of other derived conditions, e.g. a prescribed flow direction a short distance downstream, which do not guarantee a pressure match at the trailing edge. For instance, Margason et al. [12] showed that pressure mismatches of up to half of the freestream dynamic pressure could occur from such alternate forms of the Kutta condition. Figure 2, which is taken from [12] shows this clearly. Since we are interested in the computation of flows for which the behavior of the boundary layer at the trailing edge can have a significant effect on the overall flow solution, it is believed that the approach adopted here is more realistic.

The computational procedure is as follows. On each panel a control point is selected where the normal-velocity boundary condition is applied and where velocity and pressure are eventually calculated. Using the well-known point-source potential, the velocity induced by the source density on a panel at a point in space is

$$\vec{v}(\text{panel}) = \left[\iint_{\text{panel}} \text{grad}(1/r) dS \right] \sigma(\text{panel}) \quad (2.1)$$

where the constant value of σ has been taken outside the integral whose value therefore depends only on geometry. Suppose N panels are used to define the body, and let σ_j denote the value of source density on the j th panel.

The velocity induced by the j th panel at the control point of the i th panel is defined as $\vec{v}_{ij} \sigma_j$, where \vec{v}_{ij} is an integral of the form of Eq. (2.1). The integral may be carried out analytically. Explicit formulas are contained in [11], but they are too lengthy for inclusion here. The corresponding normal velocity at the i th control point is

$$A_{1j}\sigma_j = \vec{n}_1 \cdot \vec{V}_{1j}\sigma_j \quad (2.2)$$

where \vec{n}_1 is the unit normal vector to the i th panel. Applying the normal velocity boundary condition at all control points then yields the following set of linear algebraic equations:

$$\sum_{j=1}^N A_{1j}\sigma_j = -\vec{n}_1 \cdot \vec{V}_\infty \quad (2.3)$$

This is the numerical approximation of the integral equation that expresses the zero normal-velocity boundary condition. Once the σ_j have been determined, the disturbance velocities at the control points due to the body are given by

$$\vec{v}_1 = \sum_{j=1}^N \vec{V}_{1j}\sigma_j \quad i = 1, 2, \dots, N \quad (2.4)$$

While the addition of lift in two dimensions causes no significant increase in the complexity of the problem, the problem of three dimensional lifting flow is not only considerably more complicated than nonlifting flow but requires assumptions that are somewhat arbitrary [11]. The main features are illustrated in Fig. 1. As mentioned above, wings or other lifting portions of the configuration are characterized by having trailing edges from which issue trailing vortex wakes. So-called bound circulation is hypothesized to lie on or within the wing surface, with strength varying in both the chordwise direction and in the direction parallel to the trailing edge ("spanwise" in aerodynamic jargon). The variation of the bound circulation in the chordwise direction is predetermined, while the spanwise variation is adjusted to satisfy a condition of smooth flow off the entire trailing edge, and the trailing vorticity has constant strength in the stream direction and an initial strength at the trailing edge equal to the local "spanwise" derivative of bound circulation strength. The location of the wake once it leaves the trailing edge is initially unknown, which introduces a nonlinearity into the problem. It is customary simply to assume a wake location, because in most problems the calculated results are not sensitive to the details of the wake shape. However, the location can be determined by iterating the calculation if necessary.

With regard to computing effort and cost, the two principal tasks associated with this method are calculation of the N^2 velocities \vec{V}_{1j} and the

solution of the set of linear equations, Eq. (2.3). Other portions of the calculation require comparatively negligible computing efforts. In three dimensional applications rather large numbers of panels are employed. Panel numbers over 3000 are common. These are the number of unknowns actually solved for after all symmetries, etc., have been utilized. Accordingly, it is economically important that all possible efficiencies be employed in carrying out the two principal tasks. For the first task this is accomplished by using simple approximate expressions for V_{ij} when computing the influence of distant panels [13]. The second task is speeded up by the use of block iterative matrix solutions, as developed by Clark [14]. The source method lends itself particularly well to these efficiencies, without which no three dimensional method is practical.

In updating the external inviscid velocity to account for the boundary layer displacement effects, two approaches can be considered. The first, known as the displacement surface approach, involves modifying the geometry to account for the boundary layer displacement thickness. The second approach is to introduce a blowing velocity on the surface of the original body so that the dividing stream surface of the inviscid flow approximates the displacement thickness computed by the boundary-layer procedure. While both approaches have been applied in our studies, the first approach has been found to be less suitable because it involves the computation of the inviscid flow past a body with a finite opening at the trailing edge. For separated flow, the size of this open trailing edge can become significant and the computation of the inviscid flow past such a body is nonunique unless some additional conditions are imposed along this trailing-edge opening. By adopting the surface blowing approach, the equivalent trailing edge thickness of the dividing stream surface is controlled by the blowing velocity introduced on the wing surface in a physically realistic way without resorting to additional boundary conditions.

The blowing velocity computed by the boundary-layer procedure is applied on the wing surface. However, as pointed out above, the aim is to model the flow past the displacement surface. For flows involving large trailing-edge separation, it has been shown in [4] that it is important to both evaluate the external inviscid pressure distribution and apply the Kutta condition on the displacement surface. In the present method this is achieved by introducing additional off body points corresponding to each control point for which the

boundary layer distribution has been computed. These off body points are used both to compute the final pressure distribution and to apply the Kutta condition.

2.2 Interactive Viscous-Flow Method

An accurate prediction of the flowfield over a wing requires the calculation of flow on the surface and in the wake. The airfoil studies conducted in [4] indicate that the wake influence is negligible for airfoils at low angles of attack and that it is sufficient to calculate the flow on the airfoil only. In the case of the NACA 0012 airfoil, for example, the wake effect begins to become important for angles of incidence, α , greater than 10° , and is important at angles of incidence approaching stall, which for this airfoil is around 16° as shown in Fig. 3. The inclusion of the wake effect, which is not considered here, reduces the flow separation on the surface and allows the numerical calculations to be performed with less difficulty. In the present study, we investigate the ability of the interactive boundary-layer scheme to calculate flows with massive separation and perform calculations for configurations at high angles of attack, as discussed in Section 3.0.

2.2.1 Boundary-Layer Equations

The full three-dimensional boundary-layer equations and their boundary conditions may be written as the following nonorthogonal curvilinear coordinate system [10]:

Continuity Equation

$$\frac{\partial}{\partial x} (uh_2 \sin\theta) + \frac{\partial}{\partial z} (wh_1 \sin\theta) + \frac{\partial}{\partial y} (vh_1 h_2 \sin\theta) = 0 \quad (2.5a)$$

x-Momentum Equation

$$\begin{aligned} \frac{u}{h_1} \frac{\partial u}{\partial x} + \frac{w}{h_2} \frac{\partial u}{\partial z} + v \frac{\partial u}{\partial y} - \cot\theta K_1 u^2 + \csc\theta K_2 w^2 + K_{12} uw \\ = - \frac{\csc^2\theta}{\rho h_1} \frac{\partial p}{\partial x} + \frac{\cot\theta \csc\theta}{\rho h_2} \frac{\partial p}{\partial z} + \frac{\partial}{\partial y} (v \frac{\partial u}{\partial y} - \overline{u'v'}) \end{aligned} \quad (2.5b)$$

z-Momentum Equation

$$\begin{aligned} \frac{u}{h_1} \frac{\partial w}{\partial x} + \frac{w}{h_2} \frac{\partial w}{\partial z} + v \frac{\partial w}{\partial y} + \csc\theta K_1 u^2 - \cot\theta K_2 w^2 + K_{21} uw \\ = \frac{\cot\theta \csc\theta}{\rho h_1} \frac{\partial p}{\partial x} - \frac{\csc^2\theta}{\rho h_2} \frac{\partial p}{\partial z} + \frac{\partial}{\partial y} (v \frac{\partial w}{\partial y} - \overline{v'w'}) \end{aligned} \quad (2.5c)$$

$$y = 0: \quad u, v, w = 0 \quad (2.6a)$$

$$y = \delta: \quad u = u_e(x, z), \quad w = w_e(x, z) \quad (2.6b)$$

Here x, z denote the coordinate system on the surface of the body and y is the actual distance measured normal to the surface. The boundary-layer equations and boundary conditions for this system according to first-order boundary-layer theory are based on the assumption that the pressure is constant across the shear layer and stress gradients in directions parallel to the surface are negligible compared with those normal to the surface. In the above equations h_1 and h_2 denote the metric coefficients and θ denotes the angle between the coordinate lines and, as a result of first-order boundary-layer theory, they are functions of the surface coordinates x and z only. They can be obtained from the relations which define the three-dimensional body in the Cartesian coordinate system $\bar{x}, \bar{y}, \bar{z}$ by

$$F(\bar{x}, \bar{y}, \bar{z}) = 0 \quad (2.7)$$

and those that define the curvilinear coordinate system. Thus the metric coefficients and the angle between θ are given by

$$h_1^2 = \left(\frac{\partial \bar{x}}{\partial x}\right)^2 + \left(\frac{\partial \bar{y}}{\partial x}\right)^2 + \left(\frac{\partial \bar{z}}{\partial x}\right)^2 \quad (2.8a)$$

$$h_2^2 = \left(\frac{\partial \bar{x}}{\partial z}\right)^2 + \left(\frac{\partial \bar{y}}{\partial z}\right)^2 + \left(\frac{\partial \bar{z}}{\partial z}\right)^2 \quad (2.8b)$$

$$\cos\theta = \frac{(\partial \bar{x} / \partial x)(\partial \bar{x} / \partial z) + (\partial \bar{y} / \partial x)(\partial \bar{y} / \partial z) + (\partial \bar{z} / \partial x)(\partial \bar{z} / \partial z)}{h_1 h_2} \quad (2.9)$$

The parameters K_1 and K_2 are known as the geodesic curvatures of the curves $z = \text{constant}$ and $x = \text{constant}$, respectively, see Fig. 4, and are given by

$$K_1 = \frac{1}{h_1 h_2 \sin\theta} \left[\frac{\partial}{\partial x} (h_2 \cos\theta) - \frac{\partial h_1}{\partial z} \right] \quad (2.10a)$$

$$K_2 = \frac{1}{h_1 h_2 \sin\theta} \left[\frac{\partial}{\partial z} (h_1 \cos\theta) - \frac{\partial h_2}{\partial x} \right] \quad (2.10b)$$

The parameters K_{12} and K_{21} are defined by

$$K_{12} = \frac{1}{\sin\theta} \left[-K_1 - \frac{1}{h_1} \frac{\partial\theta}{\partial x} + \cos\theta \left(K_2 + \frac{1}{h_2} \frac{\partial\theta}{\partial z} \right) \right] \quad (2.11a)$$

$$K_{21} = \frac{1}{\sin\theta} \left[-K_2 - \frac{1}{h_2} \frac{\partial\theta}{\partial z} + \cos\theta \left(K_1 + \frac{1}{h_1} \frac{\partial\theta}{\partial x} \right) \right] \quad (2.11b)$$

The magnitude of the velocity vector u_t in the boundary layer is given by

$$u_t = (u^2 + w^2 + 2uw \cos\theta)^{1/2} \quad (2.12)$$

In the present study we use two reduced forms of the above boundary-layer equations. The first is referred to as the quasi-three-dimensional boundary-layer equations in which the flow variations with respect to z are neglected so that the equations become

$$\frac{\partial}{\partial x} (uh_2 \sin\theta) + \frac{\partial}{\partial y} (vh_1 h_2 \sin\theta) = 0 \quad (2.13a)$$

$$\frac{u}{h_1} \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} - K_1 u^2 \cot\theta + K_2 w^2 \csc\theta + K_{12} uw = - \frac{\csc^2\theta}{h_1 \rho} \frac{\partial p}{\partial x} + \frac{\partial}{\partial y} \left(v \frac{\partial u}{\partial y} - \overline{u'v'} \right) \quad (2.13b)$$

$$\frac{u}{h_1} \frac{\partial w}{\partial x} + v \frac{\partial w}{\partial y} + K_1 u^2 \csc\theta - K_2 w^2 \cot\theta + K_{21} uw = \frac{\csc\theta \cot\theta}{h_1 \rho} \frac{\partial p}{\partial x} + \frac{\partial}{\partial y} \left(v \frac{\partial w}{\partial y} - \overline{u'w'} \right) \quad (2.13c)$$

The second is referred to as the strip-theory approximation which essentially solves the well-known two-dimensional boundary-layer equations,

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 \quad (2.14)$$

$$u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = u_e \frac{du_e}{dx} + \frac{\partial}{\partial y} \left(v \frac{\partial u}{\partial y} - \overline{u'v'} \right) \quad (2.15)$$

In this approach, the streamwise external velocity u_e is replaced by the total velocity V defined by

$$V = (u_e^2 + w_e^2 + 2u_e w_e \cos\theta)^{1/2} \quad (2.16)$$

and is assigned to each spanwise strip.

2.2.2 Interactive Scheme

It is well known that the boundary-layer equations are singular at separation when solved for a prescribed external velocity distribution. They are not singular at separation, however, when the external velocity is computed as part of the solution by, for example, prescribing a displacement thickness: this is known as the inverse problem and leads to solution of the boundary-layer equations with separation.

For flows with separation, the presence of the upstream velocity component introduces a numerical instability into the solution of the boundary-layer equations. Over the years, several approaches have been proposed to overcome this problem. One popular approach, known as the FLARE approximation after the originators, Flugge-Lotz and Reynher [8], neglects the longitudinal convection terms $u(\partial u/\partial x)$ and $u(\partial w/\partial x)$ in the momentum equations (2.5). This approximation is satisfactory provided that the size of the separated region remains small. However, as the size of the recirculation region increases, this approximation becomes less accurate and requires the development of additional procedures to account for the neglected convective terms. One successful scheme, which has been applied to two-dimensional flows, is referred to as the DUIT procedure [15, 16] (Downstream, Upstream Iteration) and requires several sweeps through the recirculation region. With this scheme, the FLARE approach is used to compute a solution within the recirculation region, and then in successive sweeps the $u(\partial u/\partial x)$ term is progressively introduced until it is fully represented. Another successful approach developed by Cebeci [17] makes use of the unsteady boundary-layer equations in which the convective term is introduced into the equations progressively as a function of time. The present method uses only the FLARE approach for both 2-D and quasi-3-D flows, and does not consider the effect of the terms neglected due to this approximation.

In an interactive boundary-layer scheme, a link between a displacement thickness and external flow is provided, and two types of procedures have been developed for this purpose for two-dimensional flows. In the first approach

[18-22], the solutions of the boundary-layer equations are computed initially for a prescribed external velocity to obtain an estimate of the displacement thickness $\delta^*(x)$ distribution, and then in an inverse mode for a specified displacement-thickness distribution $\delta^*(x)$. If this initial calculation encounters separation, $\delta^*(x)$ is extrapolated to the trailing edge. The subsequent boundary-layer calculations are then performed in an inverse mode to compute the blowing velocity needed in the inviscid flow method. In general, this procedure leads to two external velocity distributions, $u_{ev}(x)$ derived from the inverse boundary-layer solution and $u_{e1}(x)$ derived from the updated approximation to the inviscid velocity past the body with viscous effects. A relaxation formula in the form

$$\delta^{*v+1}(x) = \delta^{*v}(x) \left[1 + \omega \left(\frac{u_{ev}(x)}{u_{e1}(x)} - 1 \right) \right], \quad v = 0, 1, 2, \dots \quad (2.17)$$

where ω denotes a relaxation parameter, is then introduced to define an updated displacement thickness distribution and to obtain new solutions of the boundary-layer equations and the inviscid flow equations so that the interactive procedure between inviscid and viscous flow solutions can be iterated until convergence is achieved.

The second approach [23], which is recommended on the grounds of generality and physical basis, treats the external velocity $u_e(x)$ and the displacement thickness $\delta^*(x)$ as unknown quantities. The boundary-layer equations are solved simultaneously in an inverse mode and with successive sweeps over the body surface. For each sweep, the external boundary condition is written as the sum of the inviscid velocity $u_e^0(x)$ over the body, and a perturbation velocity $\delta u_e(x)$, that is,

$$y = \delta, \quad u_e(x) = u_e^0(x) + \delta u_e(x) \quad (2.18)$$

The perturbation velocity δu_e is computed from a local approximation based on a thin airfoil theory in terms of the local blowing velocity, $d/d\sigma$ ($u_e \delta^*$), required to simulate the boundary layer thickness. The perturbation velocity is written as

$$\delta u_e(x) = \frac{1}{w} \int_{x_a}^{x_b} \frac{d}{d\sigma} (u_e \delta^*) \frac{d\sigma}{x - \sigma} \quad (2.19)$$

where the interaction region is confined to $[x_a, x_b]$. Introducing a discrete approximation for this integral enables the perturbation velocity to be expressed in terms of the geometric coefficients of the airfoil, as discussed in [4].

This two-dimensional interactive procedure has recently been extended under an AFOSR contract [10] to the quasi-three-dimensional equations referred previously. The relationship between displacement thickness and external velocity needed in the interactive calculations was obtained by generalizing the formulation used for two-dimensional flows. The irrotationality condition, which for an orthogonal system is

$$\frac{\partial}{\partial x} [h_2(w_e^o + \delta w_e)] = \left[\frac{\partial}{\partial z} h_1(u_e^o + \delta u_e) \right] \quad (2.20)$$

was used to provide a relationship between the two velocity components u_e and w_e and shows that the choice of computing the perturbation velocities due to viscous effects is not arbitrary. The assumption that $\delta u_e(x)$ is a function of x alone requires that

$$\frac{\partial}{\partial x} (\delta w_e) = 0$$

and that

$$w_e = w_e^o \quad (2.21)$$

In this way the edge boundary conditions for a quasi-three-dimensional boundary-layer flow with interaction are given by Eqs. (2.6) and (2.18).

2.2.3 Turbulence Model

The presence of Reynolds shear stress terms in the boundary-layer equations requires a turbulence model. The algebraic eddy-viscosity ϵ_m formulation of Cebeci and Smith [7] is used here. According to this formulation for two-dimensional wall boundary-layer flows, ϵ_m is defined by two separate formulas, given by

$$\epsilon_m = \begin{cases} \{0.4y[1 - \exp(-y/A)]\}^2 \left| \frac{\partial u}{\partial y} \right| \gamma_{tr} & 0 \leq y \leq y_c \end{cases} \quad (2.22a)$$

$$\epsilon_m = \begin{cases} \alpha \int_0^y (u_e - u) dy \left| \gamma_{tr} \gamma \right. & y_c \leq y \leq \delta \end{cases} \quad (2.22b)$$

where

$$A = 26\nu u_{\tau}^{-1}, \quad u_{\tau} = \left(\frac{\tau_{\theta}}{\rho}\right)^{1/2}$$

$$\tau_{\theta} = \nu \frac{\partial u}{\partial y}, \quad \gamma = \frac{1}{1 + 5.5(y/\delta)^6} \quad (2.23)$$

The condition used to define y_c is the continuity of the eddy viscosity; from the wall outward Eq. (2.22a) is applied until its value is equal to the one given by Eq. (2.22b).

In Eq. (2.22), γ_{tr} is an intermittency factor which accounts for the transitional region that exists between a laminar and turbulent flow. It is given by

$$\gamma_{tr} = 1 - \exp\left[-G(x - x_{tr}) \int_{x_{tr}}^x \frac{dx}{u_e}\right] \quad (2.24a)$$

Here x_{tr} is the location of the start of transition. The empirical factor G is

$$G = \frac{1}{1200} \frac{u_e^3}{\nu^2} R_{x_{tr}}^{-1.34} \quad (2.24b)$$

where the transition Reynolds number $R_{x_{tr}} = (u_e x_{tr}/\nu)$ and the transition location x_{tr} is either specified or calculated from the empirical formula of Michel [29]

$$R_{\theta_{tr}} = 1.174 R_{x_{tr}}^{0.46} \left(1 + \frac{22,400}{R_{x_{tr}}}\right) \quad (2.24c)$$

According to the Cebeci Smith model, the parameter α in Eq. (2.22b) is equal to 0.0168 for values of R_{θ} greater than 5000, and is given by the expression in [24] for R_{θ} less than 5000. Studies conducted by Head and his associates [25,26] the recent experimental data of Nakayama [27] and Simpson et al. [28] and the numerical studies of Carter [20] indicate that in flows with strong pressure gradient, the value of α should also be changed when $R_{\theta} > 5000$. Head and his associates recommend that α in Eq. (2.22b) be given by

$$\alpha = \alpha_{eq} F(r) \quad (2.25a)$$

where

$$\alpha_{eq} = 0.002094 + 0.02672[1 - \exp(-0.1163G)] \quad (2.25b)$$

$$G = 4.8285 (\Pi + 1.0717)^{1/2} + 1.8438 \quad (2.25c)$$

$$\Pi = \frac{\delta^*}{\tau_w} \frac{dp}{dx} \quad (2.25d)$$

$$F = \begin{cases} (5 - 4r)/(3 - 2r) & r < 1 \\ \frac{1}{2r - 1} & r \geq 1 \end{cases} \quad (2.25e)$$

$$\quad (2.25f)$$

In Eqs. (2.25e) and (2.25f), r represents the ratio of the local rate of growth of the boundary layer to the rate of growth of the corresponding equilibrium layer.

They also suggested that γ in Eq. (2.23) be replaced by

$$\gamma = \frac{2.0}{1 - \text{erf}[1/2(\gamma/\delta - \beta)]} \quad (2.25g)$$

where β is a function of shape factor H .

Simpson et al. [28] suggest that

$$\alpha = 0.0168/F^{2.5} \quad (2.26a)$$

Here F denotes the ratio of the product of the turbulent energy by normal stresses to that by shear stress evaluated at the location where shear stress is maximum, that is,

$$F = \left\{ \frac{\overline{u'^2} - \overline{v'^2}}{-\overline{u'v'}} \frac{\partial u}{\partial x} \right\} \frac{1}{(-\overline{u'v'})_{\max}} \quad (2.26b)$$

Before Eq. (2.26a) can be used in Eq. (2.26b), an additional relationship between $(\overline{u'^2} - \overline{v'^2})$ and $(-\overline{u'v'})$ at $(-\overline{u'v'})_{\max}$ is needed. Here we assume that the ratio in Eq. (2.26b),

$$\beta = \left\{ \frac{\overline{u'^2} - \overline{v'^2}}{-\overline{u'v'}} \right\} \frac{1}{(-\overline{u'v'})_{\max}} \quad (2.26c)$$

is a function of $R_T = \tau_w / (-\overline{u'v'})_{\max}$ which, according to the data of Nakayama [27], can be represented by

$$\beta = \frac{6}{1 + 2R_T(2 - R_T)} \quad (2.26d)$$

for $R_T < 1.0$. For $R_T \geq 1.0$, we take β to be

$$\beta = \frac{2R_T}{1 + R_T} \quad (2.26e)$$

Introducing the above relationships into the definition of F , we have the following expression for α , according to Eq. (2.26a),

$$\alpha = \frac{0.0168}{[1 - \beta(\partial u/\partial x)/(\partial u/\partial y)]^{2.5}} \quad (2.27)$$

where β is given by Eqs. (2.26d) and (2.26e). This expression is used here although further studies are clearly required to evaluate its range of validity. Work of this nature is in progress.

For three-dimensional flows, the above formulation was generalized as discussed in [16] and in the inner region ϵ_m is defined by

$$(\epsilon_m)_i = L^2 \left[\left(\frac{\partial u}{\partial y} \right)^2 + \left(\frac{\partial w}{\partial y} \right)^2 + 2 \left(\frac{\partial u}{\partial y} \right) \left(\frac{\partial w}{\partial y} \right) \cos\theta \right]^{1/2} \quad (2.28)$$

where

$$L = 0.4y[1 - \exp(-y/A)], \quad A = 26 \frac{\nu}{u_\tau}, \quad u_\tau = \left(\frac{\tau_{tw}}{\rho} \right)^{1/2} \quad (2.29)$$

$$\tau_{tw} = \mu \left[\left(\frac{\partial u}{\partial y} \right)_w^2 + \left(\frac{\partial w}{\partial y} \right)_w^2 + 2 \left(\frac{\partial u}{\partial y} \right)_w \left(\frac{\partial w}{\partial y} \right)_w \cos\theta \right]^{1/2}$$

In the outer region ϵ_m is defined by

$$(\epsilon_m)_o = \alpha \left| \int_0^\infty (u_{te} - u_t) dy \right| \quad (2.30)$$

and α is given by Eq. (2.27).

2.2.4 Transformed Equations

The equations of Section 2.2.1 may be solved in the forms presented or expressed in other forms which are more convenient for accurate solution. For two-dimensional flows, as in [4], we use the Falkner-Skan transformation in the early stages of the flow

$$\eta = \sqrt{u_e/vx} y, \quad \psi = \sqrt{u_e vx} f(x, \eta) \quad (2.31)$$

With primes denoting differentiation with respect to η and $b = 1 + \epsilon_m/v$, Eqs. (2.14) and (2.15) and their boundary conditions can be written in the form:

$$(bf'')' + \frac{m+1}{2} ff'' + m[1 - (f')^2] = x(f' \frac{\partial f'}{\partial x} - f'' \frac{\partial f}{\partial x}) \quad (2.32)$$

$$\eta = 0, \quad f = f' = 0 \quad (2.33a)$$

$$\eta = \eta_e, \quad f' = 1 \quad (2.33b)$$

Here ψ is the usual definition of the stream function that satisfies the continuity equation,

$$u = \frac{\partial \psi}{\partial y}, \quad v = -\frac{\partial \psi}{\partial x} \quad (2.34)$$

and m is a dimensionless pressure-gradient parameter,

$$m = \frac{x}{u_e} \frac{du_e}{dx} \quad (2.35)$$

This transformation provides the generation of initial conditions at the stagnation point of the airfoil and allows the calculations to be performed economically and accurately around the leading edge, where the governing equations are being solved for the prescribed external velocity distribution. For interactive boundary-layer calculations, where $u_e(x)$ is not known, a constant reference velocity u_0 is used in the transformation

$$Y = \sqrt{u_0/vx} y, \quad \Psi = \sqrt{u_0 vx} F(x, Y) \quad (2.36)$$

In terms of these new variables, Eqs. (2.14) and (2.15) and their boundary conditions can be written in the form:

$$(bF'')' + \frac{1}{2} FF'' + xe \frac{de}{dx} = x(F' \frac{\partial F'}{\partial x} - F'' \frac{\partial F}{\partial x}) \quad (2.37)$$

$$Y = 0, \quad F = F' = 0 \quad (2.38a)$$

$$Y = Y_e, \quad F' = e, \quad e - \dot{c}_{11} (Y_e e - F) = g_1 \quad (2.38b)$$

where

$$\dot{c}_{11} = c_{11} \sqrt{vx/u_0}, \quad e = \frac{u_e}{u_0}$$

Here the parameter g_1 , which results from the discrete approximation to Eq. (2.19) is given by

$$g_1 = \bar{u}_e^k + \sum_{j=1}^{i-1} c_{1j} (D_j - D_j^k) - c_{11} D_1^k \quad (2.39)$$

where

$$D = \sqrt{vx/u_0} (Y_e e - F_e)$$

For quasi-three-dimensional flows, we define

$$x = x, \quad d\eta = \left(\frac{u_0}{vs_1}\right)^{1/2} dy \quad (2.40)$$

Here u_0 is a reference velocity and s_1 denotes the length in the longitudinal direction measured from the initial line $x = x^*$. We again introduce the definition of stream function $\psi(x, y)$

$$uh_2 \sin\theta = \frac{\partial\psi}{\partial y}, \quad vh_1 h_2 \sin\theta = -\frac{\partial\psi}{\partial x} \quad (2.41)$$

so that with the definition of eddy viscosity, the quasi-three-dimensional boundary-layer equations given by Eq. (2.13) can be written as [10]

$$\begin{aligned} (bf'')' + m_1 f f'' + m_3 [(f')^2 - e^2] + m_5 (f'g' - \bar{w}_e e) + m_4 [(g')^2 - (\bar{w}_e)^2] \\ = m_9 (f' \frac{\partial f'}{\partial x} - e \frac{\partial e}{\partial x} - f'' \frac{\partial f}{\partial x}) \end{aligned} \quad (2.42)$$

$$\begin{aligned} (bg'')' + m_1 f g'' + m_6 [(g')^2 - \bar{w}_e^2] + m_7 [(f')^2 - e^2] + m_8 (f'g' - \bar{w}_e e) \\ = m_9 (f' \frac{\partial g'}{\partial x} - e \frac{\partial \bar{w}_e}{\partial x} - g'' \frac{\partial f}{\partial x}) \end{aligned} \quad (2.43)$$

where, with $f' = u/u_0$, $g' = w/u_0$, $\bar{w}_e = w_e/u_0$

$$\begin{aligned} m_1 &= \frac{\sqrt{s_1}}{h_1 h_2 \sin\theta} \frac{\partial}{\partial x} (\sqrt{s_1} h_2 \sin\theta), & m_3 &= K_1 s_1 \cot\theta \\ m_4 &= -K_2 s_1 \csc\theta, & m_5 &= -K_{12} s_1', & m_6 &= s_1 K_2 \cot\theta \\ m_7 &= -m_3, & m_8 &= -K_{21} s_1', & m_9 &= s_1/h_1 \end{aligned} \quad (2.44)$$

The boundary conditions become

$$\eta = 0, \quad f = f' = 0, \quad g = g' = 0 \quad (2.45a)$$

$$\eta = \eta_e, \quad f' = e(x), \quad g' = \bar{w}_e(x) = \bar{w}_e^0 \quad (2.45b)$$

$$e(x) = \bar{u}_e^0 + \frac{1}{\pi} \int_{x_a}^{x_b} \frac{d\Delta}{d\sigma} \frac{d\sigma}{x - \sigma}$$

where

$$\Delta = \frac{s_1}{\sqrt{R}} (\eta_e e - f_e), \quad R = \frac{u_0 s_1}{v} \quad (2.46)$$

2.2.5 Solution Procedure

The numerical solution of the system of equations given in the previous section is obtained with Keller's box method for the standard and interactive methods. This is an efficient, second-order finite-difference method extensively used by Cebeci and his associates for a wide range of flows, as discussed in Bradshaw et al. [16]. The description of the standard method is given in that reference as well as in Cebeci and Bradshaw [29]. The general features of the inverse method which makes use of the Mechul-function formulation are also described for two-dimensional flows in Bradshaw et al. [16] and in [10] for quasi-three-dimensional flows. As in previous two-dimensional studies the FLARE approximation in which the convective term $\partial F'/\partial x$ is set equal to zero in the recirculating region is employed, and no attempt was made to improve the accuracy of the solutions resulting from this approximation.

As in the solution of two-dimensional flows by Keller's method, we write Eq. (2.37) as a first-order system. For this purpose we let

$$F' = u \quad (2.47a)$$

$$u' = v \quad (2.47b)$$

and write Eq. (2.37) as

$$(bv)' + \frac{1}{2} Fv + xe \frac{de}{dx} = x(u \frac{\partial u}{\partial x} - v \frac{\partial F}{\partial x}) \quad (2.47c)$$

Since e is a function of x , only, we write

$$e' = 0 \quad (2.47d)$$

The boundary conditions for the system given by Eqs. (2.47) now can be written as

$$Y = 0, \quad P = 0, \quad u = 0 \quad (2.48a)$$

$$Y = Y_e, \quad u = e, \quad e - \dot{c}_{11} (Y_e e - P) = g_1 \quad (2.48b)$$

After the finite-difference approximations to Eqs. (2.47) and (2.48) are written, the resulting nonlinear algebraic system is linearized by Newton's method and the linear system is then solved by the block elimination method. For further details, see [29].

SECTION III RESULTS AND DISCUSSIONS

The interactive boundary-layer procedure described in the previous section has been applied to a number of test cases and the results will be presented here.

Section 3.1 presents the results obtained from the application of the two-dimensional strip theory approach to two wing alone configurations to verify the soundness of the interactive boundary layer technique. Section 3.2 will present the results obtained from the two-dimensional and the quasi-three dimensional methods for three wing-body fighter configurations.

3.1 Wing Alone Configurations

The first configuration considered is an RAE clean wing with a 28° sweep angle for which experimental data has been obtained by Lovell [30]. Figure 5 shows the computed lift curve up to 18° angle of attack. It can be seen that there is good agreement up to about 12° , beyond which the discrepancy increases. This disagreement at the higher angles of attack is due to the three dimensional nature of the flow, and due to the sensitivity of the flow to the transition location. This sensitivity is illustrated by Fig. 6 which shows the variation of the flow solution to the transition location at an angle of attack of 17.5° . Moving the transition location leads to a significant change in the lift separation location and displacement thickness, particularly near the wing tip. Figure 7 shows the results for $\alpha = 18.5^\circ$ with the computed transition location. As can be seen the separation location at this angle of attack occurs at about the midchord location. The size of the leading and trailing edge separation regions at $\alpha = 17.5^\circ$ can be seen from Fig. 8 in which the local skin friction is plotted.

Near the wing tip it can be seen that there is a small leading edge separation, shown by the region of negative skin friction, and that the trailing edge separation is occurring at about 65% local chord.

Figures 9-11 illustrate the results obtained for a NACA 0012 swept wing for which data was obtained by Yip and Shubert [31] for a range of angles of attack. Figure 9 shows the viscous and inviscid lift up to 21.18° from which the effects of the increasing flow separation at higher angles of attack can

clearly be seen. Figure 10 shows the computed and experimental pressure distributions for $\alpha = 19.35^\circ$ at two sections, 50% and 85% of semispan, both of which agree very well.

The importance of the transition location is illustrated by Figure 11 which shows the computed separation location, trailing-edge displacement thickness and lift distribution for $\alpha = 21.12^\circ$. Two curves are shown, the solid line was obtained with a computed transition location at about 3% chord on the upper surface. The dashed line was obtained by specifying a transition location closer to the leading edge attachment line on the lower surface. It can be seen that this small movement in the transition location moves the separation location forward from 60% chord to about 30% chord.

3.2 Application to Wing/Body Test Cases

Three wing/body test cases were identified for which there was experimental data available to evaluate the current procedure. The three cases are, an F-15 with a modified wing designed to investigate the role of a leading-edge laminar separation, an Advanced Navy Fighter configuration, and an unmodified F-15. The geometry and input data associated with these test cases is discussed in detail in Section 5 (Figs. 26-30).

The F-15 laminar bubble configuration has been run at a range of angles of attack using both the 2-D and the quasi 3-D boundary-layer procedures. Figure 12 shows the computed lift compared with the experimental data [32]. It can be seen that at lower angles of attack the 2-D and quasi 3-D approaches agree closely, while at higher angles of attack the quasi 3-D boundary layer procedure agrees better with the experimental data. At lower angles of attack both approaches over-predict the lift, possibly due to an inadequate modelling of the flow over the body.

Figure 13 shows an example of the computed and experimental pressure distributions for $\alpha = 10.75^\circ$ angle of attack at three stations across the span from close to the wing tip to close to the wing root. It can be seen that for this angle of attack there is very little difference between the 2-D and the quasi three dimensional boundary layer methods, and that both give a reasonable approximation to the measured pressures except close to the leading edge.

One further aspect of the present method which has been investigated concerns the use of a panel method for the calculation of compressible flow. A panel method is an incompressible solution procedure and so Mach number effects must be accounted for by means of a compressibility correction. In this case a Goethert correction is applied using the following procedure: the solution to the linearized potential flow equation

$$(1 - M_\infty^2) \frac{\partial^2 \phi}{\partial x^2} + \frac{\partial^2 \phi}{\partial y^2} + \frac{\partial^2 \phi}{\partial z^2} = 0 \quad (3.1)$$

is obtained, where ϕ is the perturbation in the potential due to the body. Provided that this perturbation velocity is small compared with the freestream velocity equation (3.1) provides a good approximation to the flow. This is true for the flow over thin wings. However, around the leading edge, or on any forward facing surface, this basic assumption is violated.

The compressibility correction for the initial velocity calculation is implemented here by first scaling the y and z coordinates by $\beta = \sqrt{1 - M_\infty^2}$. The incompressible flow is then computed about this equivalent body and the computed velocity components are divided by β^2 in the x-direction and β in the y- and z-directions.

For the subsequent updates to the inviscid velocity to account for the viscous effects the same procedure is adopted. However, this calculation involves two additional features over the initial inviscid calculation. The first is the introduction of the blowing velocity required to simulate the displacement thickness and the second is the introduction of off-body points at which the Kutta condition is to be applied and the final velocity computed. In applying the Mach number correction two additional assumptions are therefore necessary. The first is that the blowing velocity is predominantly in the y,z direction so that the blowing velocity applied on the "equivalent incompressible body" can be scaled by β . The second assumption is that the displacement effect of the boundary layer is also predominantly in the y,z direction. Therefore in defining the off-body point location in the transformed plane the displacement thickness is first scaled by β . Since both the displacement thickness and the blowing velocity are most significant near the trailing edge both of these assumptions are valid.

It should be pointed out that the interactive viscous calculation is performed entirely in the physical plane. The Mach number correction outlined above is used to provide the compressible external velocity distribution.

While the compressibility correction will provide a good approximation at lower angles of attack, it becomes less accurate at higher angles of attack when the flow can become supercritical and shock waves can form through the leading edge region. Figure 14 shows the inviscid computed pressure distribution at the mid-semispan location computed by the present panel method and by the transonic full-potential wing/body code developed by Chen et al. [33] at $\alpha = 6.84^\circ$, 10.75° and 12.95° for $M = 0.6$. At the lower angle of attack the two procedures agree well except close to the leading edge where the transonic code predicts a higher suction peak. However, at $\alpha = 12.95^\circ$ the transonic method predicts a shock wave and a larger difference in the pressure distribution through this region is predicted.

The second wing/body test case which has been considered is the Advanced Navy Fighter (ANF) for which experimental data is available [34]. This configuration was tested experimentally both with and without a canard. Figure 15 shows the computed and experimental lift distribution for this configuration without the canard and Figure 16 shows the viscous and inviscid pressure distribution compared with experimental data at $\alpha = 7.7^\circ$ across the span. It can be seen that there is good agreement. The only other pressure data for this particular configuration is for $\alpha = 22^\circ$ at which angle the data shows the presence of a shock wave near the leading edge suction peak. Due to the limitations of the compressibility correction outlined above this case has not been pursued. The effect of the canard is shown in Figure 17, in which the computed viscous lift distribution is shown with and without the canard. This case was run with the canard at zero deflection angle for which there was no experimental data, and the viscous effects were computed only on the main wing.

The final configuration which has been investigated is an unmodified F-15 wing/body for which experimental data was obtained by Anderson [35]. Figure 18 shows the computed and experimental lift curves from which it can be seen that there is good agreement up to 8.66° angle of attack. Figure 19 shows the computed pressure distribution for 8.66° which is in good agreement with the experimental data.

SECTION IV PROGRAM DESCRIPTION

The method developed here calculates the viscous flow over a lifting body through the use of an interactive boundary-layer technique in which a three-dimensional panel method is coupled with a finite-difference boundary-layer method. Two distinct boundary-layer procedures have been adopted, the first of which uses a two-dimensional strip theory approach while the second is a quasi-three-dimensional boundary-layer method.

The structure of the code is illustrated in Figure 20, which gives a schematic flow chart of the code. There are three major computational modules required, namely the inviscid panel method, the two-dimensional boundary-layer routines and the quasi-three-dimensional boundary-layer routines. The communication between the potential flow code and the boundary-layer routines is handled through the use of external disk storage.

For a given flow condition the inviscid solution is first computed and the pressure distribution over the wing is saved. If the 2-D boundary-layer mode is selected, this data is separated into strips, and an interactive boundary-layer calculation is performed independently for the upper and lower parts of each lifting strip using the method outlined in Section 2.2.5. Each of these boundary-layer calculations require a number of iterative sweeps over each surface in order to match the current external velocity distribution, given by Eqs. (2.18) and (2.19), with that computed by the boundary-layer equations, (2.47) and (2.48). Once these inner iterations have been completed and the corresponding displacement thickness and blowing velocity has been computed these data are transferred back to the inviscid flow code and the external velocity distribution is updated to incorporate the viscous effects. One complete iteration between the viscous and inviscid codes is referred to as a cycle. Several such cycles are usually performed in order to obtain a fully converged solution in which the computed viscous and inviscid solutions match one another. The precise number of cycles performed is governed either by an input parameter which specifies the maximum number of cycles, or else by a convergence check which is based on the maximum change in a displacement thickness parameter from one cycle to the next. Typically up to 5 cycles may be required for a fully converged solution.

A similar procedure is employed for the quasi-three-dimensional boundary layer method with interface routines handling the transfer of the data between the viscous and the inviscid codes. In this case the data required is more extensive than that required for the two-dimensional boundary layer calculation since surface coordinates and curvatures are required for the complete surface. Therefore, the interface program accesses the velocity data produced by the inviscid calculations, and computes a dividing line separating the upper and lower portions of the wing flowfield. For each surface, a boundary-layer grid is now defined and the geometric surface curvatures and the velocity components are interpolated onto the boundary layer grid. The quasi three-dimensional boundary layer procedure now iterates over each surface in a similar fashion to the two-dimensional approach in which the perturbed inviscid velocity is matched with that computed by the boundary layer equations, (2.42) - (2.46). The computed displacement thickness and blowing velocity is then transferred back to the potential flow code for the next viscous/inviscid cycle.

After a converged solution has been obtained for the first specified angle of attack, the process is repeated for the next angle of attack. However, rather than start the calculation using the purely inviscid potential flow solution, the blowing velocity and displacement thickness computed for the previous angle of attack are used for boundary conditions in the first inviscid flow solution. Therefore, when running multiple angles of attack, the angles should be specified in increasing order. In this way the number of cycles required for a converged solution is reduced, particularly at higher angles of attack when boundary-layer separation can lead to fairly large displacement thicknesses. To take further advantage of this fact, the program may be executed in a restart mode in which data stored by a previous run may be input as a starting solution for the next angle of attack to be computed. After each run, the following two datasets may therefore be saved for use in a subsequent run:

Unit #33 This stores the blowing velocity and the displacement thickness data.

and

Unit #47 This unit stores the geometric coefficients of the airfoil appearing in the interaction formula used in the quasi three-dimensional boundary layer method.

or

Unit #51 - This unit stores the geometric coefficients of the airfoil appearing in the interaction formula used in the two-dimensional boundary-layer method.

The user can therefore run a range of angles of attack either by specifying all of the angles of attack in one single run, or else as a series of separate runs which make use of the restart capability.

4.1 Input Data Description

4.1.1 Body Geometry

The input to this program consists of the coordinates of a number of points that define the surface of a three-dimensional configuration on which the flow is to be computed. For the purpose of organizing these points for computation, each point is assigned a pair of integers, m and n . These integers need not be input, but their use must be understood to insure the correctness of the input and to facilitate the interpretation of the output.

For each point, n identifies the "column" of points to which it belongs, while m identifies its position in the "column," i.e., the "row." The first point of a "column" always has $m = 1$. To insure that the program will compute outward normal vectors, the following condition must be satisfied by the input points. If an observer is located in the flow and is oriented so that locally he sees points on the surface with m values increasing upward, he must also see n values increasing toward the right. Examples of correct and incorrect input are shown in Figure 21. In this figure the flowfield lies above the paper, while the interior of the body lies below the paper. Occasionally, it happens that despite all care a body is input incorrectly. If the entire body is input incorrectly - not some sections correctly and some incorrectly - the difficulty can be remedied by changing the sign of one coordinate of all the input points. This trick will give an input body of the proper shape at perhaps a peculiar location. Otherwise, the input will have to be done over.

The body surface is divided into sections, which may be actual physical divisions or may be selected for convenience. A section is defined as consisting of a group of at least two n -lines. Within each section the n -lines

are input in order of increasing n . On each n -line the points are input in order of increasing m . All n -lines in a section must have the same number of points, but this may vary from section to section. The first n -line of the first section is $n = 1$. From then on the n -lines may be thought of as numbered consecutively through all sections, i.e., the numbering is not begun over at the beginning of each section. Panels will be formed that are associated with points on every n -line except those that are last in their respective sections. Points on these latter n -lines are used only to form panels associated with points on the next lowest n -lines.

To illustrate this procedure, consider the plan view of a body shown in Figure 22. This body has been divided into four sections, as shown in the figure. The first section contains four n -lines, $n = 1, 2, 3, 4$; the second, five n -lines, $n = 5, 6, 7, 8, 9$; the third three n -lines, $n = 10, 11, 12$; and the fourth three n -lines; $n = 13, 14, 15$. The number of points on each n -line are:

Section =	1	2	3	4
M =	4	7	4	2

Notice that the line $n = 4$ has only four points, the points $m = 1, 2, 3, 4$ and the m -grid of Section 1, which is listed in the figure along the $n = 1$ line. The lines $n = 4$ and $n = 5$ are physically identical. Some of the points on the two lines are physically identical but correspond to different values of m . This is of no consequence. In this scheme sections are completely independent. No elements are computed corresponding to points on lines $n = 4, 9, 12, 15$.

There is no restriction that the m and n lines of different sections have to be roughly parallel. The arrangement shown in Figure 23 is permissible.

As discussed in Section 2.1, the body is divided into lifting and nonlifting sections. The arrangement of the input requires that all lifting sections precede nonlifting sections with a one-point-per-card format of (3F10.5,2I1) with a maximum of 2000 panels and 100 strips defining the configuration. This data is input to the program through Unit #29. Also, since the boundary-layer calculations can be made for only one lifting section, this section must precede any other lifting sections. The two integers that follow each set of coordinates are the status flag and label flag, respectively, that is

STATUS FLAG	LABEL FLAG
2 - new section	1 - lifting body, or 0 - nonlifting body
1 - new N-line	(these flags are needed only when STATUS FLAG = 2)
0 - same N-line	
3 - end of input for the whole body	

4.1.2 Namelist Block Input

There are two namelist blocks that contain two groups of input data.

Namelist Name A:

This namelist block consists of all the control flags and flow conditions required to control the interactive viscous calculation.

<u>Variables</u>	<u>Remarks</u>
LIFT3D	Control flag for the execution of the potential-flow program. = 0 Skip the initial potential flow and execution will start with the boundary-layer code. = 1 Use the potential flow program for every cycle. (default is 1)
IBL3D	Control flag for executing a boundary-layer program. = 0 Use the two-dimensional boundary-layer program. = 1 Use the quasi-three-dimensional boundary-layer program. (default is 0)
KINKNO	Total number of "kink" stations input ("kink" station means a discontinuity in the planform of the first lifting section). (default is 0, maximum is 5)
MS	Station numbers where "kink" occurs in the planform. The order of these "kink" stations should be in the same order as the spanwise stations input to the Neumann program. They are also part of the input spanwise stations. (default is 0)
MLINE(i)	Number of defining chordwise points on each N-line of the i-th lifting section.
NLINE(i)	Number of defining spanwise points on each M-line of the i-th lifting section.
MAXCYC	Maximum number of interaction cycles. (default is 0)

<u>Variables</u>	<u>Remarks</u>
MAXANG	Number of angles of attack to be calculated. (default is 1, maximum is 10)
IPNTGM	Optional (debug) print flag for the interfacing program. = 0 No intermediate print. = 1 With intermediate print. (default is 0)
IPNTNU	Optional (debug) print flag for the potential flow program. = 0 No intermediate print. = 1 With intermediate print. (default is 0)
IPNTB3	Optional (debug) print flag for the quasi-three-dimensional boundary layer program. = 0 No intermediate print. = 1 With intermediate print. (default is 0)
DBMAX	Maximum difference in circulation values generated from potential flow solution for convergence. (default is 0.01)
ALPHAI	Input angles of attack values. Total number input = MAXANG. (default is 0.0)
AMACH	Input Mach number. (default is 0.0)

Namelist Name B:

Namelist B contains the geometric variables and control flags which pertain to the potential flow calculation.

<u>Variables</u>	<u>Remarks</u>
BOV2	The semi-span value of the lifting body. (default is 1.0)
IAUTOW	Automatic wake generation flag: = 1 Program generates bisector wake. = 2 Program generates flat wake, i.e. wake panel is parallel to the x-axis. = 0 User input wake panels. (default is 1)
IPCV	Chordwise vorticity flag. = 0 Constant vorticity used. = 1 Parabolic vorticity used. (default is 0)

VariablesRemarks

NOTE: This flag controls the form of the predetermined chordwise bound-vorticity variation discussed in Section 2.1. For wings with cusped or thin trailing edges, the constant variation may lead to unrealistic variations in the pressure close to the trailing edge. In such cases, the parabolic variation should be used. Otherwise the constant chordwise option should be used.

ITERAT

Matrix Solution flag.

= 0 (direct solution for 350 panels or less, otherwise use iterative solution).

= 1 Iterative solution.

= 2 Direct solution.

(default is 1)

Note: Iterative solution must be used when viscous calculations are made.

IVNSP

Nonuniform Flow/Specified Normal Velocity flag.

= 0 No nonuniform flow or blowing velocity.

= 1 Nonuniform Flow Specified. In the case onset flow velocity components at every control point must be input on Unit 33 in 3F10.6 card image format.

Otherwise velocity components are computed from freestream flow direction.

= 2 Nonzero normal velocity condition is specified on some section or sections. If this option is used, then Unit 33 must contain the following data:

1st record: "SECTION k"

Subsequent records: required normal velocity (FORMAT 1F10.6) with 1 record for each control point in the k-th section. These cards are repeated for each section for which nonzero boundary condition is satisfied.

NOTE: These options are only available for a purely inviscid calculation.

LIFSEC

Number of lifting sections input.

NOTE: Boundary-layer calculations can be made for the first lifting body only.

LINEAR

Spanwise vorticity flag.

= 0 Constant vorticity used.

= 1 Linear vorticity used. If selected, the variables, NLINEL and NLINEN must be input.

(default is 0)

NOTE: This flag controls the variation of spanwise vorticity across a given lifting strip. The level on each strip is determined by the Kutta condition as discussed in Section 2.1.

<u>Variables</u>	<u>Remarks</u>
NLINE1(i)	Condition for the first N-line of the i-th lifting section. = 1 The first N-line is the wing tip. = 4 The first N-line belongs to an extra strip or is next to a symmetry plane.
NLINEN(i)	Condition for the last N-line of the i-th lifting section. = 1 The last N-line is the wing tip. = 4 The last N-line belongs to an extra strip or next to a symmetry plane.
LIST	Geometry formation flag. = 0 Complete potential flow calculation modes. = 1 Calculation stop after geometry formation (default is 0)
NOFF	Off-body point flag. = 0 No off-body point input. = 1 Off-body point input. (default is 0) NOTE: Off-body points are points in the flow at which the velocity and pressure are to be computed. If this option is used, the off-body coordinates must be supplied on Unit 32 using 3F10.6 card image format.
NSYM1	First plane of symmetry flag. = 0 No symmetry. = 1 One plane of symmetry (about the x-z plane). (default is 1)
NSYM2	Second plane of symmetry flag. = 0 No second plane of symmetry used. = 1 Symmetry about the y-z plane (NSYM1 must also be = 1). (default is 0)
ORIGNX ORIGNY ORIGNZ	The x,y,z coordinates of the input moment origin (default is 0, 0, 0).
NSORCE(i)	Number of on-body panels per strip for the i-th lifting section.
NWAKE(i)	Total number of wake panels input for the i-th lifting section. (If IAUTOW \neq 0, NWAKE \equiv 1)
NSTRIP(i)	Total number of strips in the i-th lifting section.
IXFLAG(i)	Extra strip option input for the i-th lifting section. = 0 No extra strip. = 1 First strip is an extra strip. = 2 First and last strips are extra strips. = 3 Last strip is an extra strip.

VariablesRemarks

NOTE: An extra strip is a strip of panels on a lifting section which carries a vorticity distribution but on which no boundary conditions are satisfied. Such a strip is used for instance at an intersection between a wing and a fuselage in order to provide a more accurate carry-over of the wing lift across the fuselage. In this case the extra strip is internal to the fuselage, and it extends from the wing root to the fuselage centerline. Further details of the use of extra strips is discussed by Hess [36].

REFCHD Reference chord value. (This is needed for the calculation of the lift coefficient.)
(default is 1.0)

RFAREA Reference area value. (This is needed for the calculation of the lift coefficient.)
(default is 1.0)

4.1.3 Boundary-Layer Calculation Data Input

(a) Card number 1
Format (6F10.0)

<u>Card Column</u>	<u>Variables</u>	<u>Remarks</u>
1-10	RCx10 ⁻⁶	Reynolds number based on CREF.
11-20	CREF	Reference length. In the same physical units that are used for the input geometry. NOTE: This need not be the same value as REFCHD used above. CREF is only used to calculate the local Reynolds number in terms of the input coordinates. e.g. If the geometry is specified in inches, and the Reynolds number/ft is input, then CREF would be 12.
31-40	FRSTAT	= 1.0 Option for using a previous angle of attack solution as an initial estimate for the current angle of attack calculation. = 0.0 Option not used (or the initial run).
41-50	FPRNT	= 1.0 Detailed boundary-layer print. = 0.0 No boundary-layer print.

(b) Card Number 2
Format (6F10.0)

<u>Card Column</u>	<u>Variables</u>	<u>Remarks</u>
1-10	FNBLU	Number of boundary layer stations at which calculations are made on the upper surface of the first lifting body (max = 100).
11-20	PTRIU	Transition input flag = 0 Transition location specified across the span. See Cards 3 and 4. = 1 Transition calculated by the program at pressure peak. = 2 Transition calculated by the program using Michel's criteria.
21-30	FSWPU	Number of iteration sweeps to be made for the upper surface. (FSWPU = 10.0 is recommended)
31-40	FNTRU	Number of transition locations to be specified. (if PTRIU = 0)

(c) Card number 3 (needed only if PTRIU = 0).
Format (6F10.0)

<u>Card Column</u>	<u>Variables</u>	<u>Remarks</u>
1-10	YTRN	Spanwise location, in the input geometry system, where transition will be specified (this location does <u>not</u> have to correspond to the coordinates used to define the geometry).
11-20	YTRN+1	.
	.	.
51-60	YTRN+5	.

(Repeat this card if necessary until i = FNTRU.)

(d) Card number 4 (needed only if PTRIU = 0).
Format (6F10.0)

<u>Card Column</u>	<u>Variables</u>	<u>Remarks</u>
1-10	XCTRN	x/c chordwise location of specified transition.

11-20 XCTRN+1
 .
 .
51-60 XCTRN+5

(Repeat this card if necessary until 1 = FNTRU.)

The following cards, numbers 5, 6 and 7, have the same format as cards 2, 3 and 4 and the variables have the same meaning but correspond to the lower surface.

(e) Card number 5
Format (6F10.0)

Variables FNBL, PTRIL, PSWPL, FNTRL

PSWPL = 5.0 is recommended.

(f) Card number 6
Format (6F10.0)

Variable YTRN

(g) Card number 7
Format (6F10.0)

Variable XCTRN

Note that the chordwise location of specified transition must be preceded by a minus sign when it is being input on the airfoil lower surface.

The cards in this section, (a) through (g), are to be repeated for each angle of attack calculated.

4.2 Output Data Description

4.2.1 Summary

Potential Flow

The following data are printed for the potential flow calculation:

1. Input flags.

II. Panel formation.

III. Matrix solution (by iteration method).

IV. Solution summary. This includes:

lift coefficient, drag coefficient, pitch, roll, yaw and n values for each lifting and nonlifting section, plus the same set of data for the whole configuration.

V. Final cycle. For every panel, the following data are printed:

- . panel number
- . control point coordinates - x_o, y_o, z_o
- . inviscid velocities - v_x, v_y, v_z
- . inviscid total velocity V_T and viscous corrected pressure coefficient C_p
- . displacement thickness - DELS
- . shape factor - H
- . skin friction - CF.

4.2.2 Format

A test case consisting of one lifting and four nonlifting sections with a total of 221 panels, Figure 24, was created to present a sample of the program output, and a listing of this geometry (input through Unit #29) is presented in Table 1. Two angles of attack were calculated with the transition locations on the lifting section computed by the program. The namelist block input for this case is:

```
REPORT TEST CASE, TRANS. CALC., 2DSTRIP BL, M=0.8, ALPHAS
&A LIFT3D=1, IBL3D=0,
MAXCYC=2, NLINE=5, MLINE=21,
MAXANG=2, ALPHAI(1)=1.3, ALPHAI(2)=3.4,
AMACH=0.8, &END
&B BOV2=12.955, IAUTOW=2, NSYM1=1, LIFSEC=1, REFCHD=8.2912,
LINEAR=0, IXFLAG(1)=3, IPCV=1,
RFAREA=95.904, NSORCE=20, NSTRIP=4, NWAKE=1, &END
7.0      12.0      0.0      0.0
70.0     2.0      10.0
51.0     2.0      5.0
7.0      12.0     0.0      0.0
70.0     2.0      10.0
51.0     2.0      5.0
```

For conciseness, the output presented here will be the pertinent information for the first angle of attack only and is shown in Figure 25.

Table 1. Input geometry data for the sample test case.

x	y	z	x	y	z	x	y	z	x	y	z
20.320007	12.950000	5.689997221	22.049988	5.6999998	5.479327200	25.103775	0.0000000	0.0000000	0.985788300		
20.248184	12.950000	5.659527600	21.488954	5.6999998	5.458943400	26.737854	0.0000000	0.0000000	6.692972200		
20.039001	12.950000	5.642725900	21.298386	5.6999998	5.502729400	28.032578	0.0000000	0.0000000	6.438945900		
20.712478	12.950000	5.627047500	21.491623	5.6999998	5.590855800	28.858948	0.0000000	0.0000000	6.247252500		
20.301193	12.950000	5.604248100	22.046387	5.6999998	5.682218800	29.139999	0.0000000	0.0000000	6.169997200		
27.848038	12.950000	5.588881300	22.921051	5.6999998	5.774380700	1.4388998	0.0000000	0.0000000	6.159998820		
27.390981	12.950000	5.529536300	24.025009	5.6999998	5.855646100	1.4399998	0.0084315	0.161222700			
26.979998	12.950000	5.503880700	25.251343	5.6999998	5.891611400	1.4399998	0.0098637	0.180487200			
26.653732	12.950000	5.482185900	26.478824	5.6999998	5.850277900	1.4399998	0.0104338	0.167038800			
26.444412	12.950000	5.467838400	27.582291	5.6999998	5.778900300	1.4399998	0.0103374	0.151741000			
26.371002	12.950000	5.452908200	28.461888	5.6999998	5.728014000	1.4399998	0.0085511	0.149518000			
26.441805	12.950000	5.511909800	29.028505	5.6999998	5.690294300	1.4399998	0.0027379	0.150388700			
26.850253	12.950000	5.537014000	29.220001	5.6999998	5.688997200	1.4399998	0.0001927	0.149381600			
26.975800	12.950000	5.569729800	29.181774	1.6310434	5.688997210	1.4399998	0.0004819	0.145678500			
27.385544	12.950000	5.614847200	28.807547	1.6285334	5.653852200	1.4399998	0.0000000	0.139999400			
27.840240	12.950000	5.680013200	28.172808	1.6335869	5.600514400	3.0000000	0.1928958	6.888820300			
26.286280	12.950000	5.661705500	27.028528	1.6678520	5.521410000	3.0000000	0.3631767	6.787053600			
26.708923	12.950000	5.683177000	25.588823	1.7781889	5.490619700	3.0000000	0.4918574	6.816842100			
26.038898	12.950000	5.675870900	23.986252	1.8357840	5.538883900	3.0000000	0.5607882	6.237488700			
29.247543	12.950000	5.669478500	22.388957	1.9418851	5.619744300	3.0000000	0.4959082	6.053087200			
26.270004	9.3299999	5.689997210	20.848931	2.0539112	5.688937600	3.0000000	0.3600985	5.814361000			
26.137855	9.3299999	5.658048600	19.806320	2.1326818	5.759267800	3.0000000	0.1880037	5.618710300			
26.768011	9.3299999	5.606512100	19.071398	2.1750240	5.788211000	3.0000000	0.0000000	5.758899300			
27.409607	9.3299999	5.656803700	18.848488	2.2003370	5.877244000	6.8000004	0.0000000	6.000000010			
26.578278	9.3299999	5.522551500	19.087887	2.1932545	5.898942500	6.8000004	0.3757820	7.875558800			
25.743439	9.3299999	5.489906900	19.618451	2.1308517	6.136426900	6.8000004	0.9098854	7.281573300			
24.991823	9.3299999	5.443327900	22.402405	2.0328290	6.215392100	6.8000004	1.0701828	6.911097500			
24.394518	9.3299999	5.426845700	24.003601	1.8385239	6.225601200	6.8000004	1.1407099	6.512920000			
24.012182	9.3299999	5.395872800	25.601135	1.7748887	6.115730300	6.8000004	1.0307589	6.135311100			
23.886387	9.3299999	5.438118900	27.038820	1.6883813	5.961447700	6.8000004	0.7527732	5.845423700			
24.009415	9.3299999	5.507829700	28.180145	1.6218841	5.824855500	6.8000004	0.3938298	5.667017900			
24.391281	9.3299999	5.547428100	29.181484	1.6310434	5.869997200	6.8000004	0.0000000	5.578999900			
24.988847	9.3299999	5.597880300	29.139999	0.0000000	6.189997210	6.8000004	0.0000000	6.000000020			
25.734804	9.3299999	5.687744100	28.648022	0.0000000	6.188208100	6.8000004	0.3798224	7.883428700			
26.588884	9.3299999	5.750885900	28.003937	0.0000000	6.148680800	6.8000004	0.9006198	7.278782800			
27.400884	9.3299999	5.741801900	26.688950	0.0000000	6.150129300	6.8000004	1.0639114	6.909449800			
28.154190	9.3299999	5.711984800	25.034119	0.0000000	6.412736900	6.8000004	1.1430740	6.518009200			
28.753342	9.3299999	5.696475000	23.208055	0.0000000	6.925851000	6.8000004	1.0284891	6.137653400			
29.138046	9.3299999	5.680374100	21.384949	0.0000000	6.857525100	6.8000004	0.7542807	5.843463900			
29.220001	5.6999998	5.669997210	19.750841	0.0000000	7.150182700	6.8000004	0.3924263	5.672342300			
29.028016	5.6999998	5.651124000	17.620010	0.0000000	7.422036200	6.8000004	0.0000000	5.579999900			
28.488084	5.6999998	5.587138200	17.382259	0.0000000	7.553010000	9.0400000	0.0000000	9.399999610			
27.581843	5.6999998	5.509122800	17.644577	0.0000000	7.802229100	9.0400000	0.5151625	9.148937200			
26.488252	5.6999998	5.478988800	18.488088	0.0000000	7.556008300	9.0400000	0.7953402	8.648261200			
25.260284	5.6999998	5.480448800	19.603375	0.0000000	7.437680200	9.0400000	0.7559274	8.067444800			
24.033788	5.6999998	5.478083800	21.457535	0.0000000	7.253735500	9.0400000	1.1685621	7.872409100			
22.927994	5.6999998	5.478483300	23.288808	0.0000000	7.253735500						

Table 1. Continued

	X	Y	Z	X	Y	Z	X	Y	Z		
9	0400000	1.3772736	7.142297700	16	828384	2.2364789	6.462136300	35	999989	1.1518841	6.365452800
9	0400000	1.3486974	6.571766900	16	828660	2.1972888	5.958491100	35	999989	1.4077408	6.017142300
9	0400000	1.0454197	6.085439700	20	898888	0.0000000	6.928970310	35	999989	1.5362034	7.806899900
9	0400000	0.5897094	5.763486900	20	905899	0.5430155	6.889450100	35	999989	1.5333567	7.173847200
9	0400000	0.0000000	5.659998900	20	905583	1.0725965	6.772514300	35	999989	1.4977627	6.743378600
11	470000	0.0000000	5.439998610	20	903654	1.6052437	6.677392000	35	999989	1.3129398	6.353323000
11	470000	0.5272308	9.172778200	20	908998	2.0392651	6.391488100	13	239998	2.4958245	6.089388820
11	470000	0.7217981	8.626779800	20	896912	2.0498791	7.846530900	13	239998	1.6660210	5.995590200
11	470000	1.1584234	8.287037800	20	867115	2.0407467	7.302267100	13	239998	1.2355471	5.953220400
11	470000	1.4484529	7.763285800	20	864354	2.0329008	6.757774400	13	239998	0.6313735	5.758119700
11	470000	1.4618241	7.160081100	20	892029	2.0380592	6.213587800	13	240000	0.0000000	5.699997900
11	470000	1.4360714	6.551931400	23	898637	0.0000000	6.001497310	16	428421	2.3336649	5.938537610
11	470000	1.6433350	6.030721700	23	902847	0.5091249	6.985610500	16	428657	1.7531338	5.831500100
11	470000	0.8007850	5.783112500	23	901718	1.0143394	6.898937400	16	428345	1.1574640	5.760498500
11	470000	0.0000000	5.699998900	23	901588	1.0143394	6.898937400	16	428558	0.5921336	5.812080600
13	240000	0.0000000	9.159998610	23	892583	1.7295752	6.254428900	16	428741	0.0000000	5.531058400
13	240000	0.4588438	8.880802400	23	894165	1.8317899	7.755286200	16	428680	2.1972866	5.856490110
13	240000	0.9617893	8.596923800	23	885254	1.8213902	7.245484400	16	822535	1.7481203	5.812126400
13	240000	1.4048698	8.214414800	23	885834	1.8420534	6.735670100	16	829805	1.1604424	5.576710700
13	240000	1.5412628	7.633884400	23	893800	1.8425722	6.225877500	16	831253	0.5821130	5.486088600
13	240000	1.5878000	7.038956700	26	970062	0.0000000	6.950943910	16	831085	0.0000000	5.408371900
13	240000	1.4770479	6.451713600	26	974182	0.4979586	6.905910500	20	886703	2.0584173	5.698275810
13	240000	1.1558962	5.957092300	26	972397	0.9651402	6.728383100	20	879913	1.7316999	5.396406200
13	240000	0.5905445	5.769768800	26	965439	1.3427353	6.403904900	20	876480	1.1529741	5.371751800
13	240000	0.0000000	5.679999400	26	957245	1.5826340	7.965984300	20	861332	0.5750989	5.334608300
13	240000	0.0000000	5.180000320	26	959717	1.6738930	7.473424900	20	878632	0.0000000	5.280242900
13	239998	1.0979691	8.571403500	26	957230	1.6788139	6.973434400	23	872177	1.8409662	5.543289210
13	239998	1.5787401	8.185799600	26	959368	1.6910200	6.472663900	23	855942	1.4630432	5.435104400
13	239998	2.2372141	8.191214600	26	969788	1.6907854	5.971778900	23	855820	0.9678883	5.445723500
13	239998	2.7671642	7.936422300	26	432983	0.0000000	6.923634810	23	850540	0.4829558	5.552112600
13	239998	2.8483087	7.282396300	26	435516	0.5035268	6.639376400	23	849945	0.0000000	5.480190300
13	239998	2.8114081	6.634428000	26	433823	0.9718443	6.840609700	26	953262	1.8928741	5.520198910
13	239998	2.4954042	6.089308700	26	428285	1.3321495	6.262444000	26	940323	1.4043455	5.558598600
16	429108	0.0000000	6.939050710	26	423691	1.6277708	7.827078800	26	936279	0.9289543	5.688654400
16	428986	0.6114895	6.895422000	26	423798	1.6208820	6.810544000	26	933533	0.4746038	5.671554600
16	434341	1.6870451	6.361007700	26	428085	1.6278219	6.299811100	26	933487	0.0000000	5.606189700
16	428437	2.2952358	6.290433900	26	442827	1.6184028	6.7891695500	26	438095	1.6290388	5.623371110
16	432297	2.4785501	7.730808400	30	761002	0.0000000	6.918388410	26	421432	1.3282881	5.639211700
16	428482	2.4784088	7.118317600	30	761002	0.4970595	6.827903700	26	416948	0.6805089	5.775707200
16	425522	2.4915514	6.505980500	30	761002	0.9552400	6.622685400	26	416856	0.4509697	5.730981800
16	428421	2.3335943	5.936427200	30	781017	1.3085413	8.285527700	26	417343	0.0000000	5.657361100
16	830948	0.0000000	6.939308210	30	781017	1.5700121	7.634810900	30	773058	1.6295404	5.820005100
16	830780	0.6015922	8.857445700	30	781017	1.8472712	7.336636300	30	773058	0.8504359	5.897218800
16	829712	1.1878748	8.701623900	30	761002	1.8413708	6.833274800	30	773058	0.0000000	5.716688100
16	835739	1.7537479	8.524408400	30	781002	1.8388779	6.327983900	35	999989	1.3129187	6.353290810
16	825607	2.2591143	8.284925500	36	000000	0.0000000	5.622973300	35	999989	1.0792589	6.037482300
16	832809	2.2711515	7.675120400	35	999989	0.4266687	6.821846700	35	999989	0.7593449	5.810174900
16	830536	2.2706423	7.067988500	35	999989	0.8200570	8.642345400	35	999989	0.3885908	5.661399300
								38	000000	0.0000000	5.619998000

4.3 External Units

There are a total of 50 external units required although they are not simultaneously used. A list of the unit numbers and types follows:

1. Direct access data sets:

Unit #20 - 400 records, each 200 words long - potential flow velocity

Unit #61 - 3280 records, each 990 words long - used for quasi-3-D boundary-layer program

Unit #62 - 41 records, each 990 words long - used for quasi-3-D boundary-layer program

2. Sequential data sets: This includes units 3, 4, 5, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 38, 39, 40, 41, 42, 43, 44, 45, 56, 47, 51, 63, 64, 65, 66, 67.

Unit #29 is the geometry data set for the input body. These datasets are used both for the inviscid velocity calculation and for the communication between the viscous and the inviscid parts of the calculation.

3. Datasets required to be saved:

Unit #34 - This unit contains the inviscid velocities and control points.

Unit #33 - This unit contains the blowing velocities and the displacement thickness values for viscous/inviscid interactive runs.

Unit #51 - This unit contains some input data to the 2-D boundary-layer program.

Unit #47 - This unit contains the blowing velocities from the 3-D boundary-layer program.

4.4 CRAY JCL

An example of the JCL required for the execution of the program on CRAY using the two-dimensional strip theory boundary-layer procedure, follows. Example 1 is for an initial calculation with the appropriate data saved for

subsequent runs and example 2 shows how the previously saved data is used to make additional calculations.

Example 1

```
JOB,JN=XXXXX ,T=900,MFL=2000000.
ACCOUNT,US=XXXXXX ,UPW= XXXXX ,AC=XXXXXXXXX .
*
COPYF,I=$IN,O=INPUT. COPY INPUT FILE
REWIND,DN=INPUT.
*
COPYF,I=$IN,O=GEOM. COPY INPUT FILE
REWIND,DN=GEOM.
*
ACCESS,DN=KCMCAIR,PDN=KCMCAIRCRAV,ID=OBJLIB.
STATIC,LEVEL=NEW.
BUILD,I=0,L=0,OBL=KCMCAIR,B=0,NBL=MCARBIN,NODIR. CREATE SEQUENTIAL BIN
*
ASSIGN,DN=INPUT,A=FT05. ALLOCATE APPROPRIATE FILES
ASSIGN,DN=$OUT,A=FT06.
ASSIGN,DN=GEOM,A=FT29.
ASSIGN,DN=FILE34,A=FT34.
ASSIGN,DN=FILE33,A=FT33.
ASSIGN,DN=FILE51,A=FT51.
*
MODE,FI=DISABLE.
*
DEGLDR,CMD='BIN=MCARBIN'. LINK BINARIES
SABD. EXECUTE LOAD MODULE
*
SAVE,DN=FILE34,PDN=INVELNEW. SAVE OUTPUT DATASET FOR THE NEXT CAL.
SAVE,DN=FILE33,PDN=BLOW2DNEW.
SAVE,DN=FILE51,PDN=BL2DINPNEW.
*
EXIT.
/EOF
F15 WITH LAMINAR BUBBLE WING, MULTIPLE ALPHAS, M=0.6
 8A LIFT3D=1,IBL3D=0,MAXCYC=2,MLINE=51,NLINE=14,
  MAXANG=2,ALPHA(1)=6.95,ALPHA(2)=8.95,AMACH(1)=0.60,
  AMACH(2)=0.6,&END
 8B BOV2=13.008,IAUTOW=2,NSYM1=1,LIFSEC=1,NSTRIP=13,
  IXFLAG(1)=3,NSORCE=50,NWAKE=1,RFAREA=96.7,REFCHD=8.325,&END
 6.022 8.325 0.0 0.0
 61.0 2.0 10.0 0.0
 51.0 2.0 5.0 0.0
 6.022 8.325 1.0 0.0
 61.0 2.0 10.0 0.0
 51.0 2.0 5.0 0.0
/EOF
32.966003 13.008000 5.949856821
32.924698 13.008000 5.950995400
32.863266 13.008000 5.952991500
32.782425 13.008000 5.956209200
32.683380 13.008000 5.959699600
32.567581 13.008000 5.961723300
.
.
.
43.000000 1.3186102 5.600000400
43.000000 0.5522600 5.600000400
43.000000 0.1862400 5.600000400
43.000000 0.0000000 5.600000400
/EOF
```

} saved for future runs

} input data set

} geometry data set

Example 2

```
JOB, JN=XXXXXX , T=1200, MFL=2400000.
ACCOUNT, US=XXXXXX , UPW=XXXXXX , AC=XXXXXXXXXX
*
COPYF, I=$IN, O=INPUT. COPY INPUT FILE
REWIND, DN=INPUT.
*
COPYF, I=$IN, O=GEOM. COPY INPUT FILE
REWIND, DN=GEOM.
* ACCESS PERMANENT DATASETS
ACCESS, DN=KCMCAIR, PDN=KCMCAIRCRA, ID=OBJLIB.
ACCESS, DN=DUMMY34, PDN=INVELNEW.
ACCESS, DN=DUMMY33, PDN=BLOW2DNEW.
ACCESS, DN=DUMMY51, PDN=BL2DINPNEW.
* COPY DATASETS
* COPY FILE34
REWIND, DN=DUMMY34.
COPYR, I=DUMMY34, O=FILE34, NR.
REWIND, DN=FILE34.
* COPY FILE33
REWIND, DN=DUMMY33.
COPYR, I=DUMMY33, O=FILE33, NR.
REWIND, DN=FILE33.
* COPY FILE51
REWIND, DN=DUMMY51.
COPYR, I=DUMMY51, O=FILE51, NR.
REWIND, DN=FILE51.
*
STATIC, LEVEL=NEW.
BUILD, I=0, L=0, OBL=KCMCAIR, B=0, NBL=MCARBIN, NODIR. CREATE SEQUENTIAL BIN
*
ASSIGN, DN=INPUT, A=FT05. ALLOCATE APPROPRIATE FILES
ASSIGN, DN=$OUT, A=FT06.
ASSIGN, DN=GEOM, A=FT29.
ASSIGN, DN=FILE34, A=FT34.
ASSIGN, DN=FILE33, A=FT33.
ASSIGN, DN=FILE51, A=FT51.
*
MODE, FI=DISABLE.
*
SEGLDR, CMD='BIN=MCARBIN'. LINK BINARIES
$ABD. EXECUTE LOAD MODULE
*
SAVE, DN=FILE34, PDN=INVELNEW. SAVE OUTPUT DATASET FOR THE NEXT CAL.
SAVE, DN=FILE33, PDN=BLOW2DNEW.
SAVE, DN=FILE51, PDN=BL2DINPNEW.
*
EXIT.
/EOF
/15 WITH LAMINAR BUBBLE WING, MULTIPLE ALPHAS, M=0.6
&A LIFT3D=1, IBL3D=0, MAXCYC=2, MLINE=51, NLINE=14,
MAXANG=2, ALPHAI(1)=7.95, ALPHAI(2)=8.95, AMACH(1)=0.60,
AMACH(2)=0.6, &END
&B BOV2=13.008, IAUTOW=2, NSYM1=1, LIFSEC=1, NSTRIP=13,
IXFLAG(1)=3, NSORCE=50, NWAKE=1, RFAREA=96.7, REFCHD=8.325, &END
6.022 8.325 1.0 0.0
61.0 2.0 10.0 0.0
51.0 2.0 5.0 0.0
6.022 8.325 1.0 0.0
61.0 2.0 10.0 0.0
51.0 2.0 5.0 0.0
/EOF
32.966003 13.008000 5.949856821
32.924698 13.008000 5.950995400
32.863266 13.008000 5.952991500
32.782425 13.008000 5.956209200
.
.
.
43.000000 0.5522600 5.600000400
43.000000 0.1862400 5.600000400
43.000000 0.0000000 5.600000400
/EOF
```

} data from previous run

} saved for future runs

} input data set

} geometry data set

SECTION V
TEST CASES

Three test cases were investigated: (1) F-15 with laminar bubble wing, (2) Advanced Navy Fighter (ANF), and (3) unmodified F-15.

5.1 Test Case 1 - F-15 with Laminar Bubble Wing

The coordinates of the geometry for test case 1 are given in model scale (4.7%) in inches. 1084 panels defined this configuration with 600 of them describing the wing, as shown in Figure 26. All of the calculations use the symmetry option of the program so that the given number of panels are for only half the configuration.

Inviscid and viscous calculations for Case 1 were made to compare with test data [32] at a Mach number ≈ 0.6 , $Rc \approx 8.5 \times 10^6$ /ft and a range of angle of attack from 6.84° through 15.83° . Viscous solutions were calculated by both the two-dimensional strip theory boundary layer and the quasi-three-dimensional boundary-layer procedures, and the location of transition was calculated by the program using Michel's criterion.

The input required to execute the two-dimensional strip theory boundary-layer procedure for case 1 was:

1. A data set, Unit 29, Format (3F10.0, 2I1), containing the x,y,z coordinates of the geometry, and
2. A data set, Unit 5, containing the flags, geometry and flow parameters, and boundary-layer parameters.

```
F15 - LAMINAR BUBBLE WING, A=6.84, M=0.6, TRANS. CALC.  
&A LIFT3D=1, IBL3D=0, MAXCYC=2, MLINE=51, NLINE=14,  
  MAXANG=1, ALPHAI(1)=6.84, AMACH=0.60, &END  
&B BOY2=13.008, IAUTOW=2, NSYM1=1, LIFSEC=1, NSTRIP=13,  
  NSORCE=50, NWAKE=1, RFAREA=96.7, REFCHD=8.325, &END  
6.022      8.325      0.0      0.0  
81.0       2.0       10.0  
51.0       2.0       5.0
```

If more calculations are desired for additional, higher angles of attack, the results of the calculations of a lower angle of attack may be used for the initial guess for these calculations. The data saved on units 33 and 51 from

the first calculation is now used as input for the additional calculations and the namelist block input will appear as:

```

F15 WITH LAMINAR BUBBLE WING, MULTIPLE ALPHAS, M=0.6
&A LIFT3D=1, IBL3D=0, MAXCYC=2, MLINE=51, NLINE=14,
  MAXANG=2, ALPHAI(1)=10.75, ALPHAI(2)=12.95,
  AMACH=0.6, &END
&B BOV2=13.008, IAUTOW=2, NSYM1=1, LIFSEC=1, NSTRIP=13,
  NSORCE=50, NWAKE=1, RFAREA=96.7, REFCHD=8.325, &END
6.022      8.325      1.0      0.0
61.0       2.0       10.0
51.0       2.0       5.0
6.022      8.325      1.0      0.0
61.0       2.0       10.0
51.0       2.0       5.0

```

To execute the program using the quasi-three-dimensional boundary-layer procedure, the input is identical to that of the two-dimensional strip theory boundary-layer procedure with the exception of the following flags in Namelist A: IBL3D = 1, INTF = 1.

5.2 Test Case 2 - Advanced Navy Fighter (ANF)

Geometry data for the Advanced Navy Fighter consisted of 6% model scale coordinates given in inches. The configuration (Figure 27) was defined by approximately 1200 panels which provided for 360 panels to describe the wing and 192 panels to describe the canard. Since the boundary-layer effects can be calculated on only one lifting section, this configuration was first run without the canard (Figure 27a) and the results were compared with experiment (Figures 15 and 16). Calculations with the canard on (Figure 27b) were then made and the effect was compared with the canard off case (Figure 17).

Because the wing is mounted so low on the fuselage the wing extra strip would protrude through the fuselage if it were defined as a continuation of the wing to the centerline as is usually done. Therefore the extra strip was tilted "up" so that it fell completely inside the fuselage so as not to change the fuselage geometry. See Figure 28.

Calculations for test case 2 were made for $M = 0.5988$, $R_L = 7.0 \times 10^6 / \text{ft}$, $C_L = 0.45$ and $\alpha = 7.7182^\circ$ to compare pressure data given in Reference 34. Viscous solutions were obtained with the strip theory boundary-layer procedure being used to calculate the viscous effects. As in test case 1, the

transition location was calculated by the program using Michel's criterion.

The namelist block input for this case was:

```
ANF. NO CANARD., TRANS. CALC., 2DSTRIP BL, M=0.6
&A LIFT3D=0, IBL3D=0,
MAXCYC=2, NLINE=8, MLINE=51,
MAXANG=1, ALPHAI(1)=7.7182, AMACH=0.6, &END
&B BOY2=12.955, IAUTOW=2, NSYM1=1, LIFSEC=1, REFCHD=8.2912,
LINEAR=0, IXFLAG(1)=3, IPCV=1,
RFAREA=95.904, NSORCE=50, NSTRIP=7, NWAKE=1, &END
7.0      12.0      0.0      0.0
70.0     2.0      10.0
51.0     2.0      5.0
```

A series of calculations at various angles of attack were made to compare the calculated and experimental lift coefficients for the canard-off case. These calculations were repeated for the configuration with the canard to compare the calculated effect of the canard. The namelist block input for the configuration with canard for multiple angles of attack was:

```
ANF. CANARD., TRANS. CALC., 2DSTRIP BL, M=0.6, MULT. ALPHAS
&A LIFT3D=1, IBL3D=0,
MAXCYC=2, NLINE=8, MLINE=51,
MAXANG=6, ALPHAI(1)=1.3, ALPHAI(2)=3.4, ALPHAI(3)=4.7,
ALPHAI(4)=6.0, ALPHAI(5)=7.7182, ALPHAI(6)=9.2, AMACH=0.6, &END
&B BOY2=12.955, IAUTOW=2, NSYM1=1, LIFSEC=2, REFCHD=8.2912,
LINEAR=0, IXFLAG(1)=3, IXFLAG(2)=3, IPCV=1, RFAREA=95.904,
NSORCE(1)=50, NSORCE(2)=48, NSTRIP(1)=7, NSTRIP(2)=5, NWAKE(1)=1,
NWAKE(2)=1, &END
7.0      12.0      0.0      0.0
70.0     2.0      10.0
51.0     2.0      5.0
7.0      12.0      0.0      0.0
70.0     2.0      10.0
51.0     2.0      5.0
7.0      12.0      0.0      0.0
70.0     2.0      10.0
51.0     2.0      5.0
7.0      12.0      0.0      0.0
70.0     2.0      10.0
51.0     2.0      5.0
7.0      12.0      0.0      0.0
70.0     2.0      10.0
51.0     2.0      5.0
```

5.3 Test Case 3 - Unmodified F-15

The unmodified F-15 geometry coordinates were full scale in inches. This configuration [35] was defined by 981 panels, 450 of which described the wing (Fig. 29). The wing is mounted high on the fuselage and as in the case of the Advanced Navy fighter configuration, the extra strip had to be tilted, in this case "down", so as not to protrude through the top of the nacelle. Figure 30 shows the arrangement of the panels on the wing used in the calculations of

test case 3. The measured data was obtained with a sting-mounted fuselage/wing configuration which included the vertical tail. The computed results, however, were for a configuration without the vertical tail.

Viscous and inviscid calculations were made for this configuration to compare with experiment [35] at $M = 0.6$, $R_L/ft = 5.78 \times 10^6$ for a range of angle of attack, $2.21^\circ \leq \alpha \leq 8.66^\circ$. The two-dimensional strip theory boundary-layer procedure was used in the interaction calculation to compute the viscous results. The namelist block input for test case 3 follows:

```

NEW F15 CONFIGURATION, M=0.6, STRIP2D BL, TRANSITION INPUT
&A LIFT3D=1, IBL3D=0,
  MAXCYC=2, NLINE=11, MLINE=61,
  MAXANG=2, ALPHAI(1)=4.36, ALPHAI(2)=6.51,
  AMACH=0.6, KINKNO=1, MS=6, &END
&B BOY2=256.20, IAUTOW=2, NSYM1=1, LIFSEC=1,
  IXFLAG(1)=3, IPCV=1, REFCHD=191.23, RFAREA=43776., NSORCE=60,
  NSTRIP=10, NWAKE=1, &END
4.33      191.23      0.0      0.0
71.0      0.0      10.0      6.0
254.0     220.0     185.0     150.0     115.0     80.0
0.05      0.05      0.05      0.05      0.05      0.05
61.0      0.0      5.0      6.0
254.0     220.0     185.0     150.0     115.0     80.0
-0.05     -0.05     -0.05     -0.05     -0.05     -0.05
4.33      191.23      1.0      0.0
71.0      0.0      10.0      6.0
254.0     220.0     185.0     150.0     115.0     80.0
0.05      0.05      0.05      0.05      0.05      0.05
61.0      0.0      5.0      6.0
254.0     220.0     185.0     150.0     115.0     80.0
-0.05     -0.05     -0.05     -0.05     -0.05     -0.05

```

SECTION VI

CONCLUSIONS AND RECOMMENDATIONS

An interactive viscous/inviscid procedure has been developed for the computation of viscous flow over 3-D wing/body configurations. The method developed makes use of a three-dimensional surface-source panel method developed by Hess [11] and an inverse finite-difference boundary-layer procedure of [6].

Two alternative boundary-layer formulations have been considered, the first is a two-dimensional strip theory implementation [4] and the second [10] is a quasi-three-dimensional boundary-layer method. These procedures have been coupled with the external potential flow calculation via an interface routine which handles the necessary interpolation and transfer of data between the viscous and the inviscid parts of the calculation.

The present method is able to compute flows with both leading- and trailing-edge separations. In most of the cases considered here, the calculations were performed by computing transition by an empirical formula, which, at higher angles of attack, resulted in a separated region as much as 35% upstream of the trailing edge. However, at the conditions approaching stall, a small change in transition location led to regions of massive flow separation on the wing, which the present method handled without any numerical difficulties.

The studies conducted here indicate that at lower angles of attack there is very little difference between the results computed by either of the two boundary-layer procedures. However, at higher angles of attack, for which there are significant regions of flow separation, the quasi-three-dimensional boundary-layer procedure has been found to provide a useful improvement in the results when compared with the experimental data.

The inviscid method used here is general and can be applied to complex aircraft configurations. The viscous effects, however, are limited to the wing alone with some approximations. For example, the use of either two-dimensional strip theory or the quasi-three-dimensional boundary-layer approximation is satisfactory at low to medium angles of attack. At higher angles

of attack, the flow becomes "more" three dimensional and the calculations should use the complete equations. Furthermore, the effect of the viscous wakes neglected in the solution procedure also becomes important at higher angles of attack and needs to be included in the solution procedure.

The viscous capabilities of the present computer code can also be extended to the other components of the airplane configurations to include, for example, multiple lifting sections, as well as the fuselage and other nonlifting components.

SECTION VII

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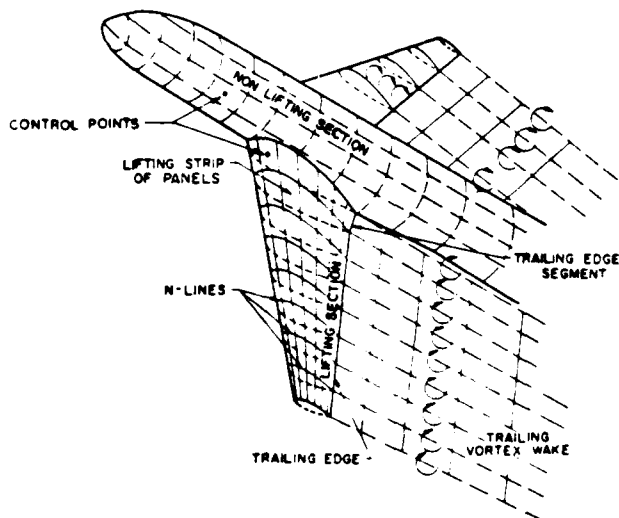


Figure 1. Wing/body configuration.

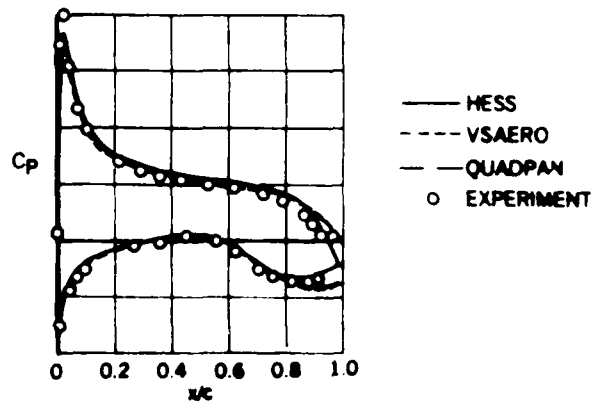


Figure 2. Effect of alternate Kutta conditions.

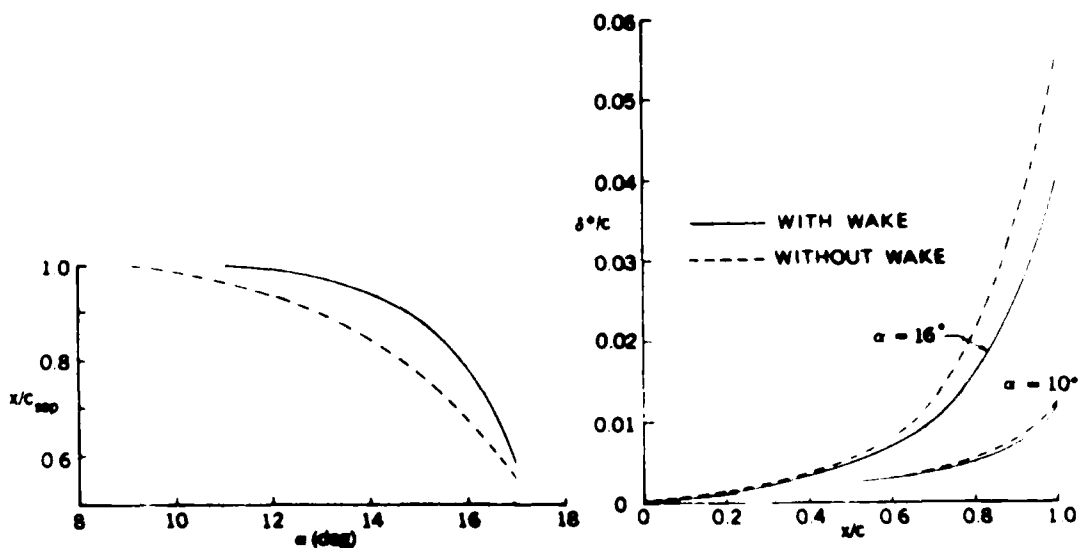


Figure 3. Effect of wake on the separation region and displacement thickness for the NACA 0012 airfoil, $R_c = 6.0 \times 10^6$.

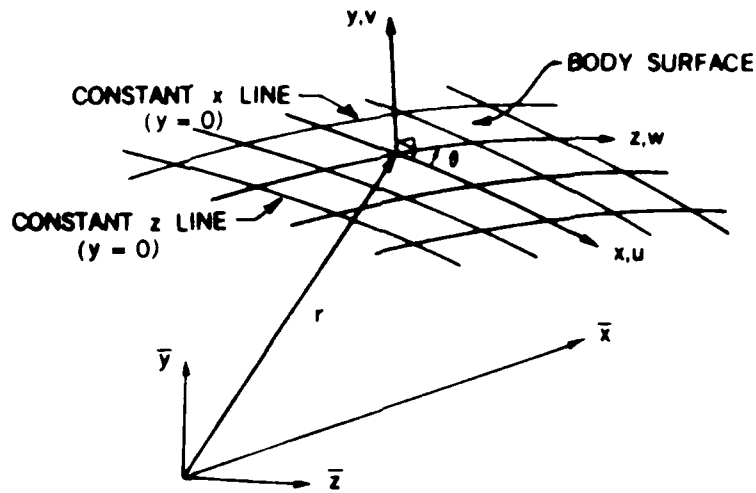


Figure 4. Notation for nonorthogonal curvilinear coordinate system on the body surface. Note that x and z are not orthogonal to each other but y is to x and z .

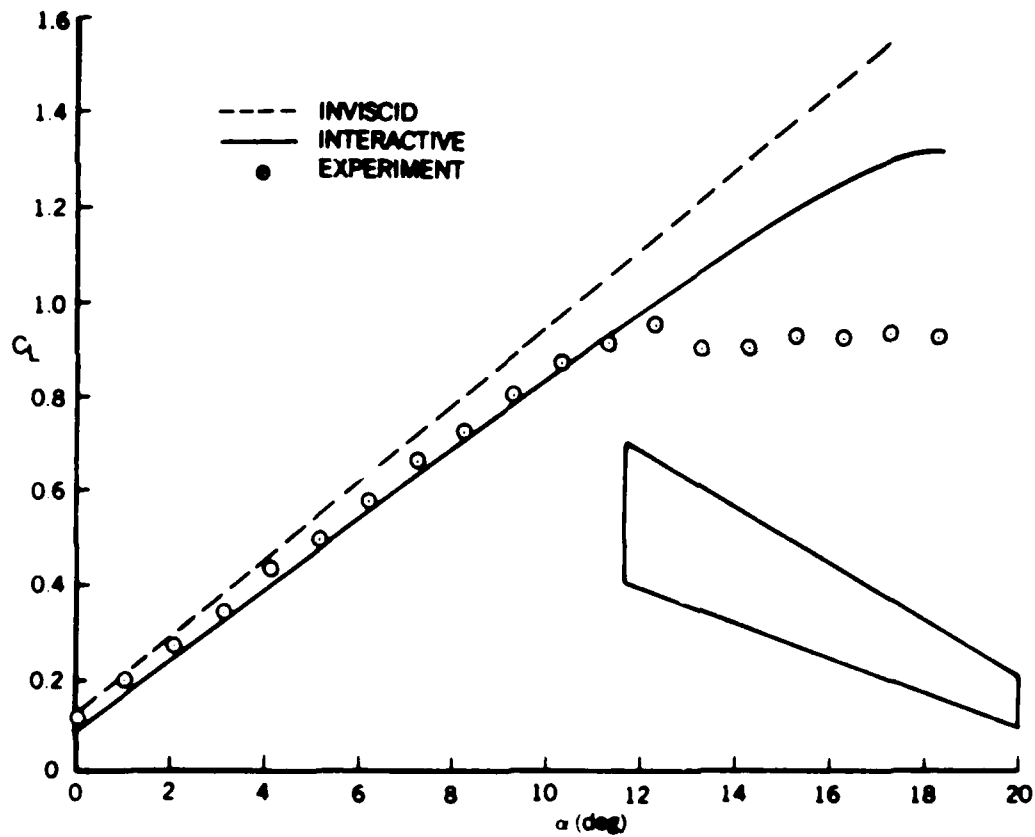


Figure 5. Comparison of computed and experimental lift curves for the RAE wing.

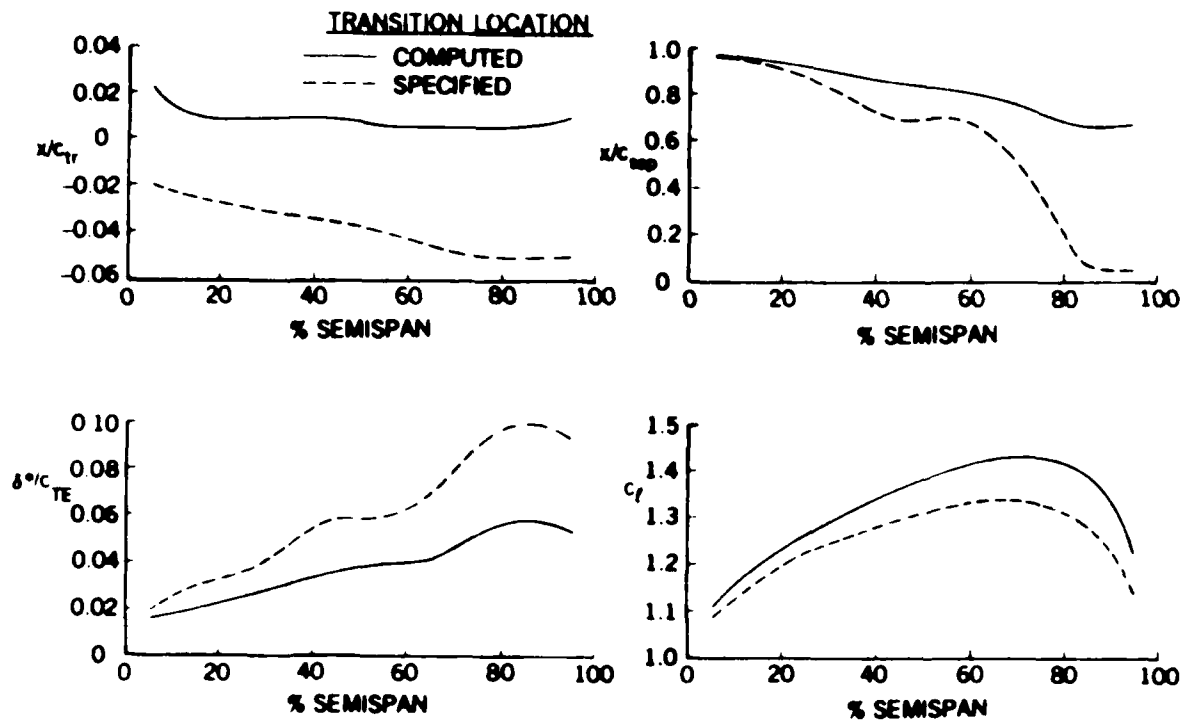


Figure 6. Effect of transition location on flow separation, displacement thickness and lift distribution for the RAE wing, $\alpha = 17.5^\circ$.

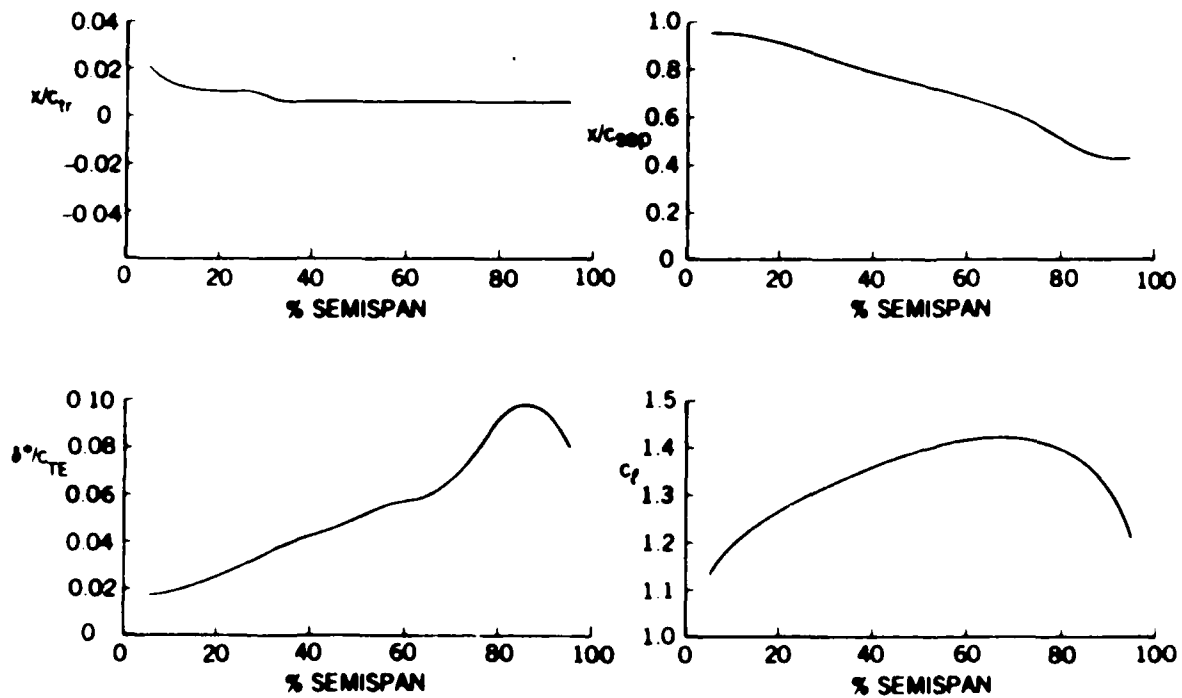


Figure 7. Computed transition location, flow separation, displacement thickness and lift distribution for the RAE wing, $\alpha = 18.5^\circ$.

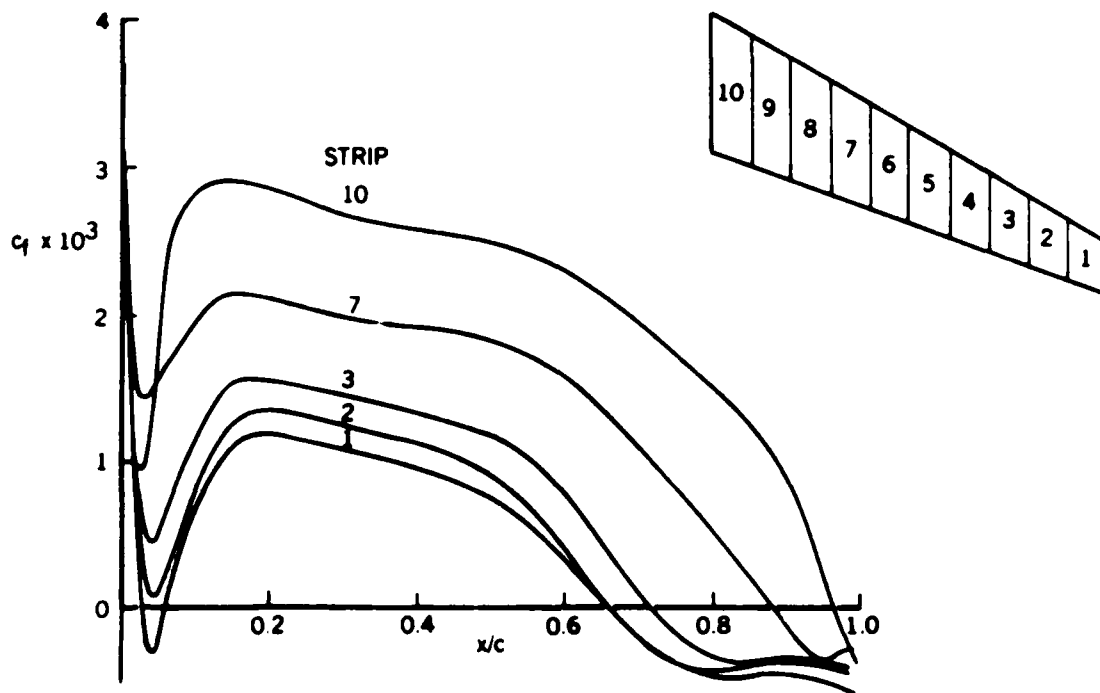


Figure 8. Leading and trailing edge separation location for the RAE wing, $\alpha = 17.5^\circ$.

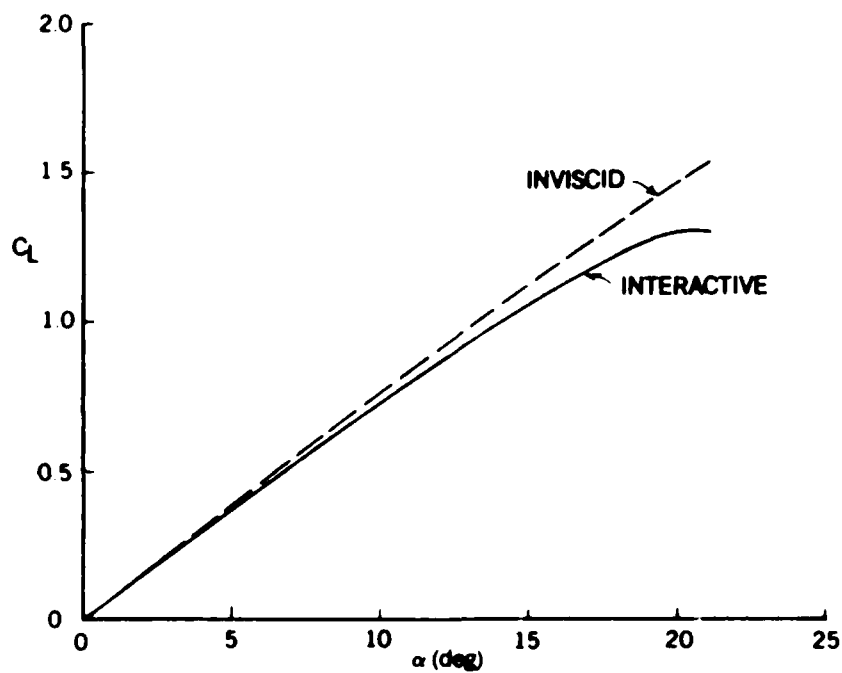


Figure 9. Computed viscous and inviscid lift curve for the NACA 0012 swept wing.

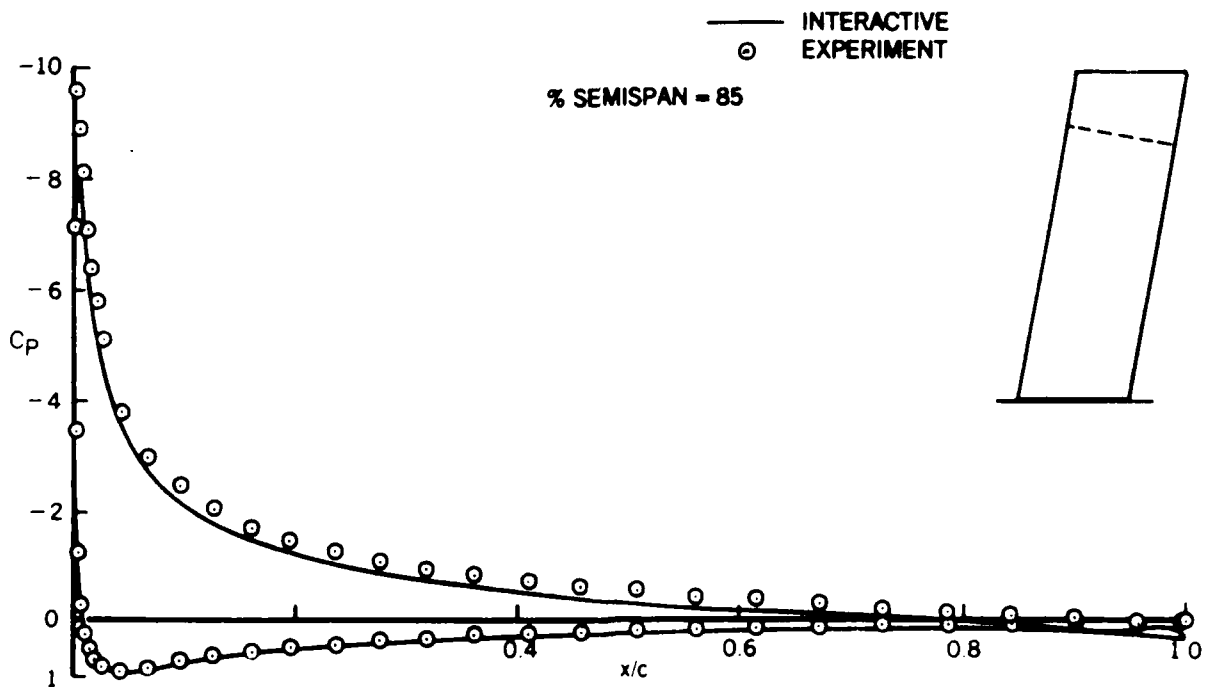
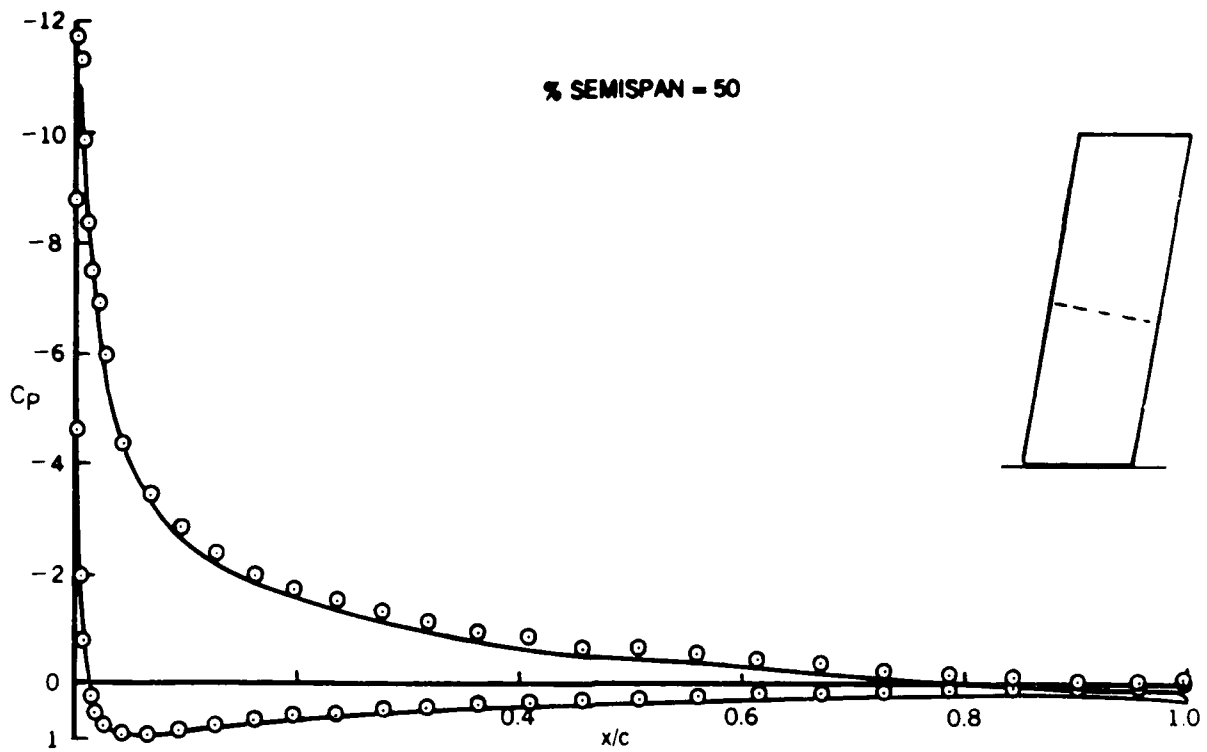


Figure 10. Comparison of calculated and experimental pressure distribution on the NACA 0012 swept wing, $\alpha = 19.35^\circ$.

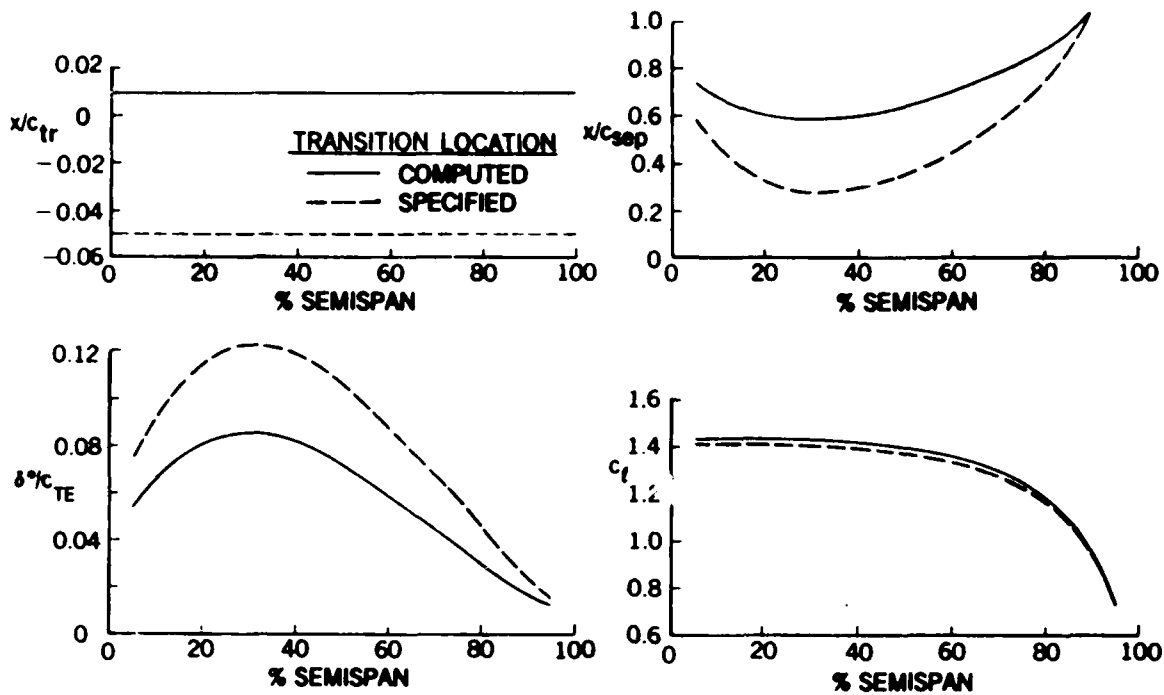


Figure 11. Effect of transition location on flow separation, displacement thickness and lift distribution for the NACA 0012 swept wing, $\alpha = 21.12^\circ$.

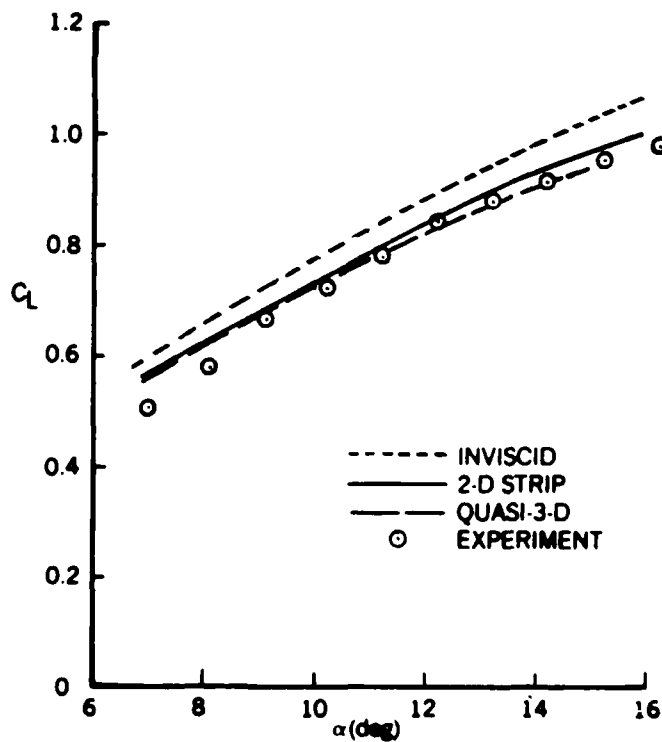


Figure 12. Comparison of 2-D strip theory and quasi-3-D methods for the F-15 fighter with laminar bubble wing.

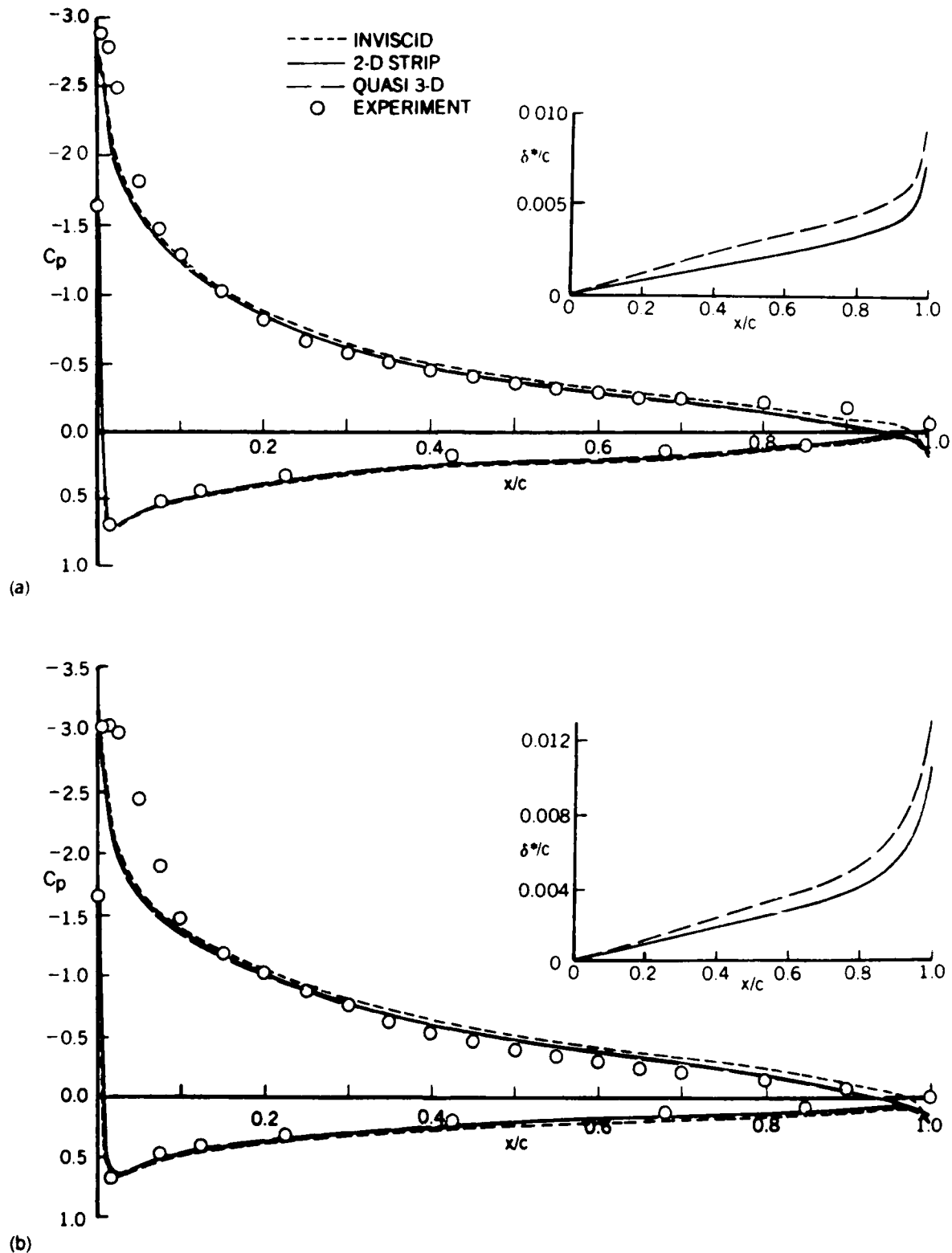


Figure 13. Comparison of the calculated and experimental pressure distribution for the F-15 with laminar bubble wing, $\alpha = 10.75^\circ$. Insert shows the chordwise variation of displacement thickness as calculated by the 2-D strip theory and the quasi-three-dimensional boundary-layer methods. (a) 38% semispan. (b) 58% semispan.

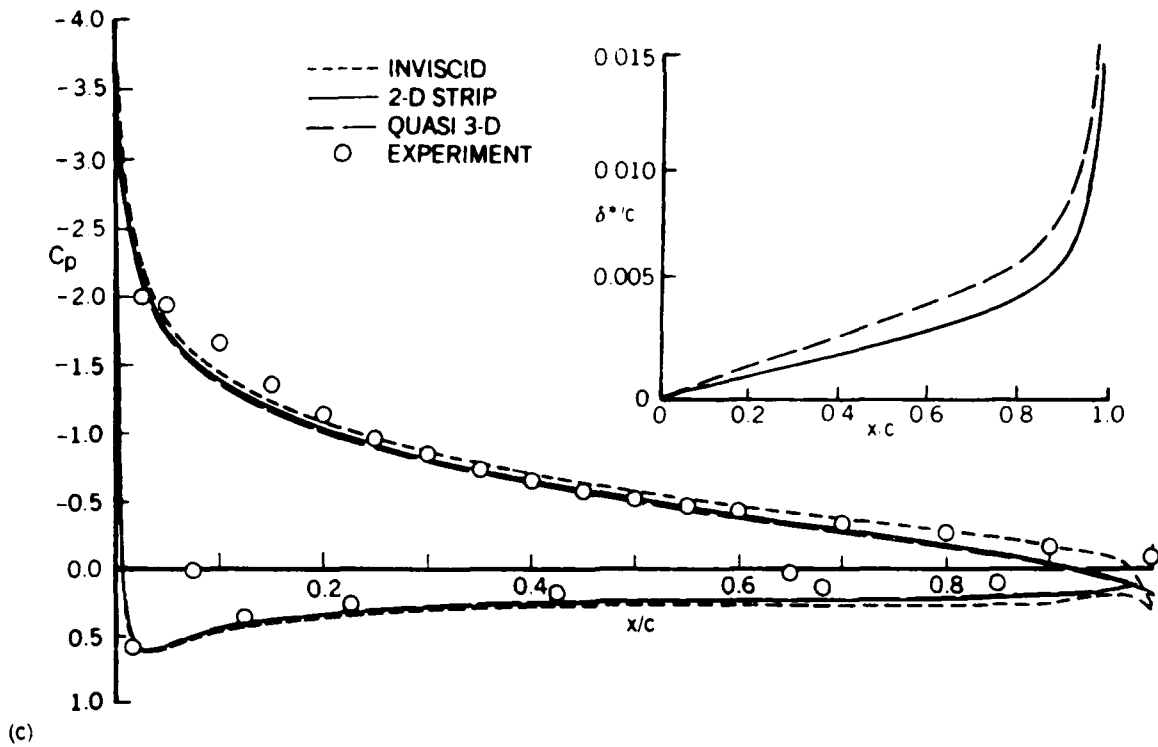


Figure 13. (Continued) (c) 88% semispan.

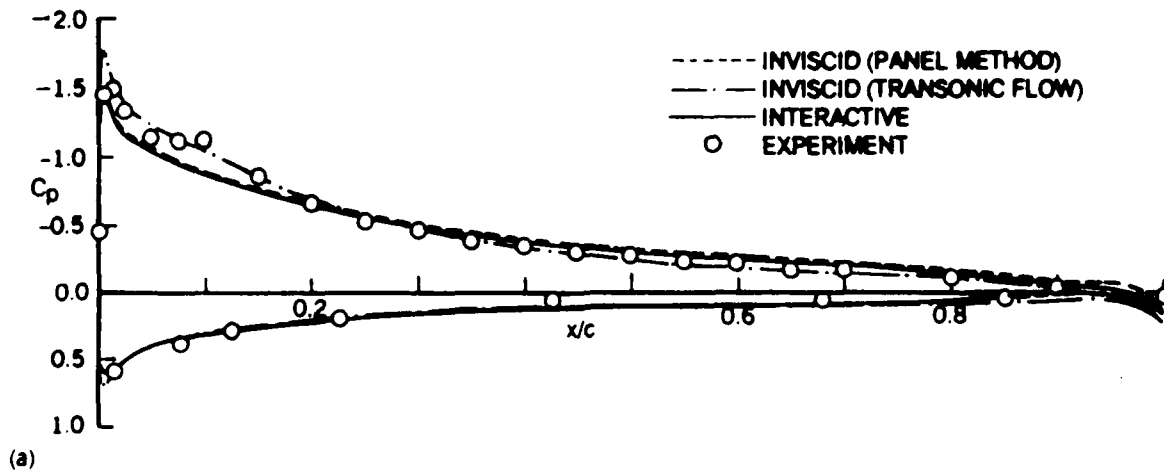


Figure 14. Comparison of the mid-semispan pressure distribution obtained by the panel method and the transonic flow method for the F-15 with laminar bubble wing, $M = 0.6$. (a) $\alpha = 6.84^\circ$.

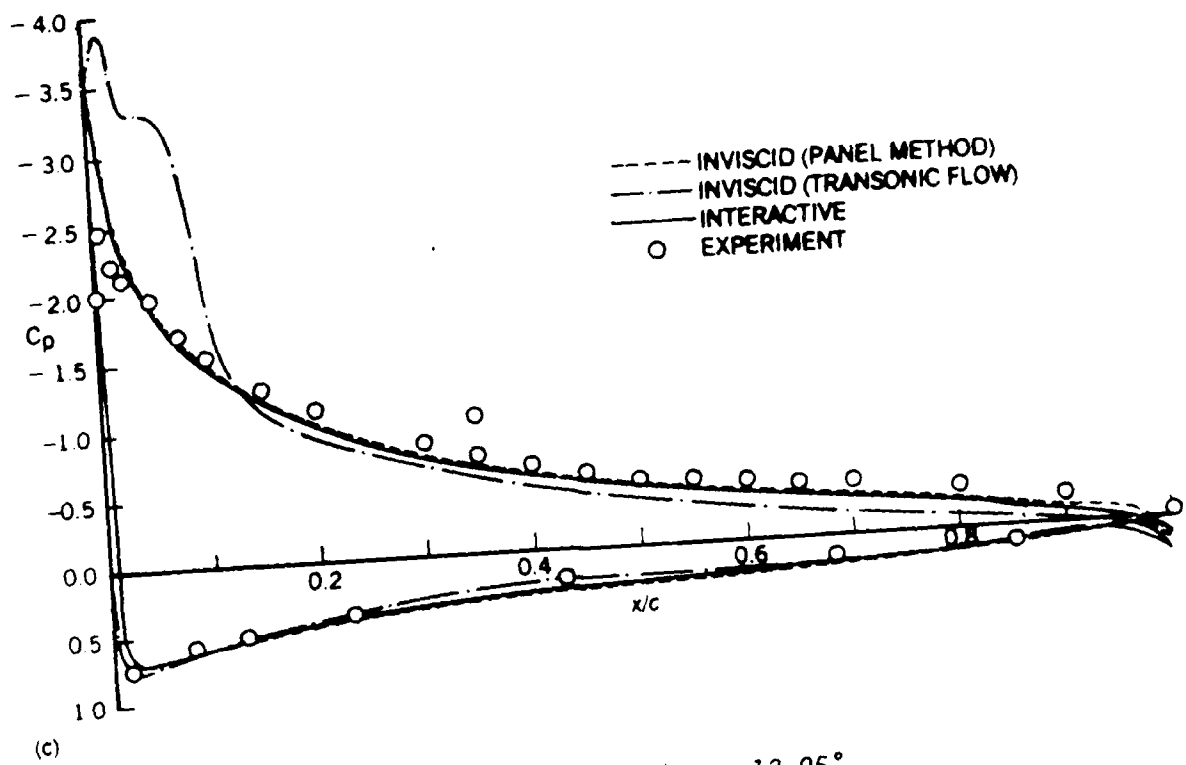
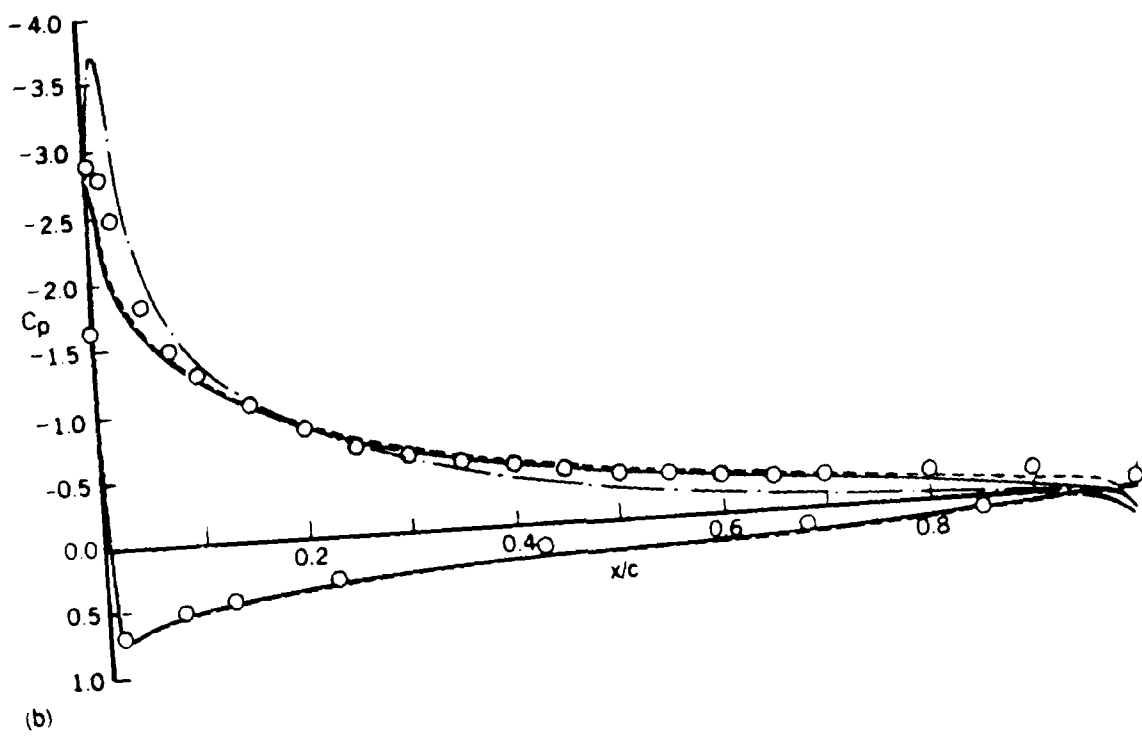


Figure 14. (Continued) (b) $\alpha = 10.75^\circ$. (c) $\alpha = 12.95^\circ$.

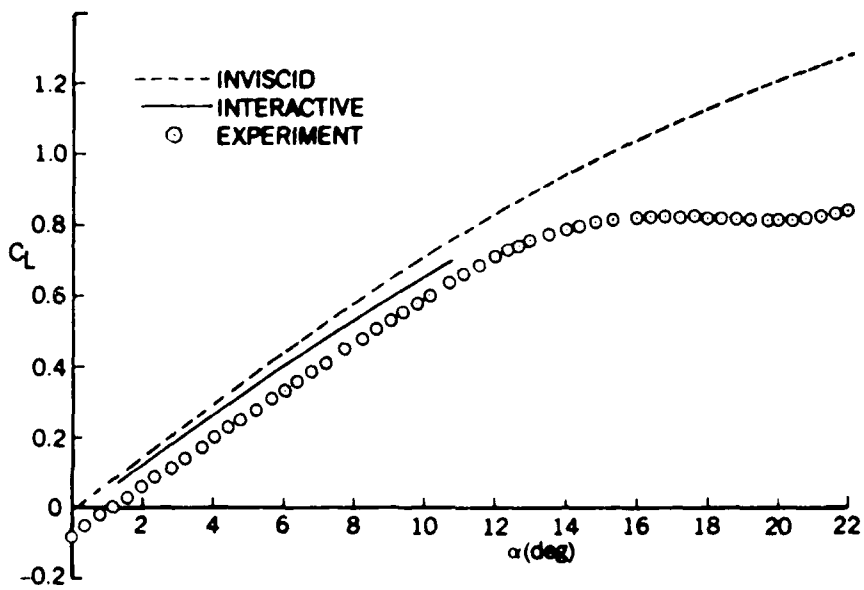
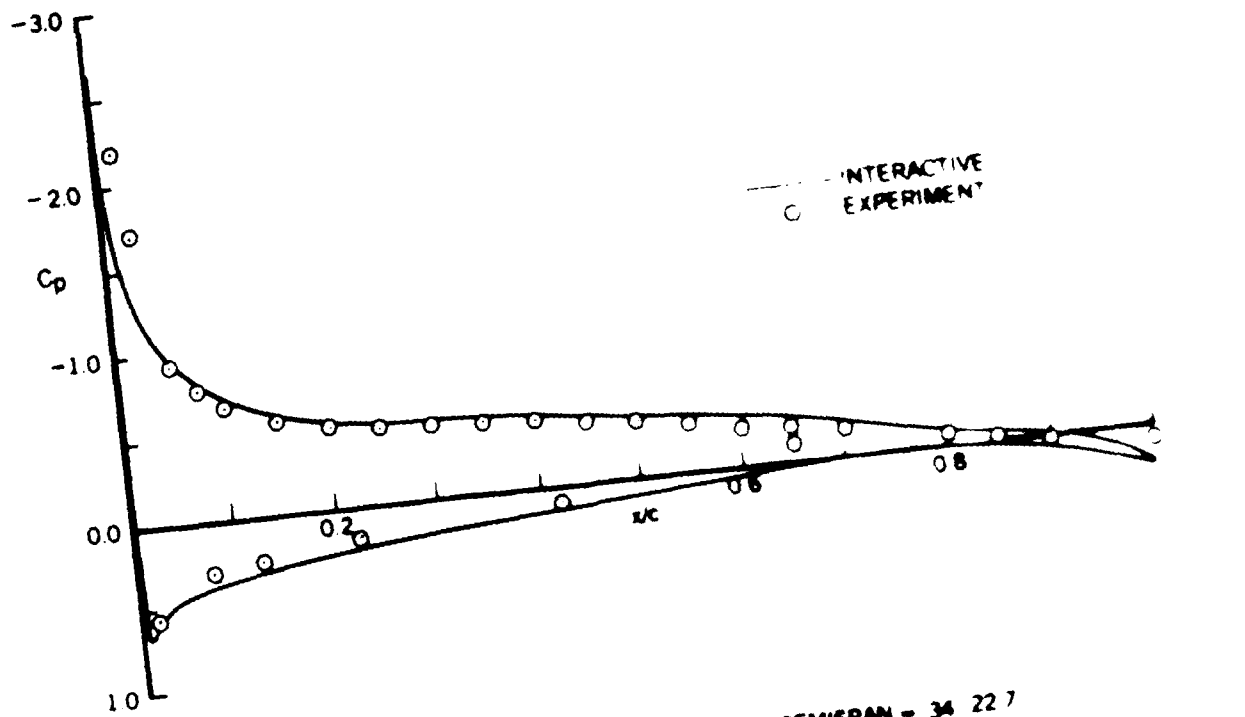
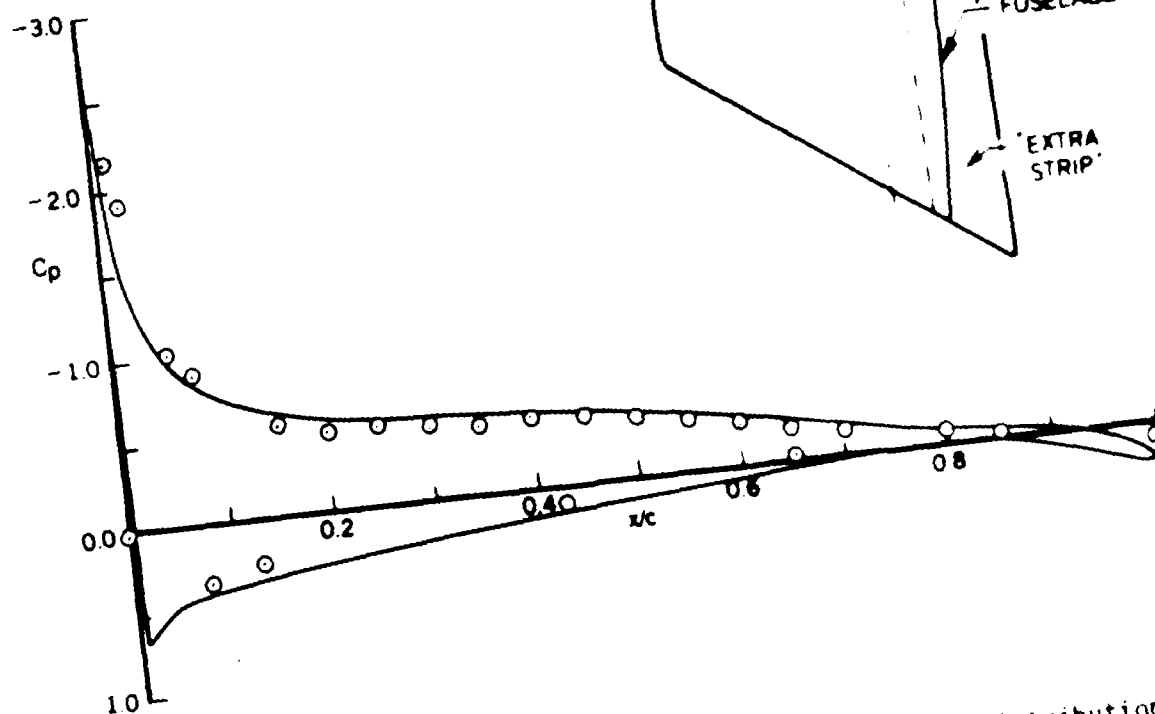
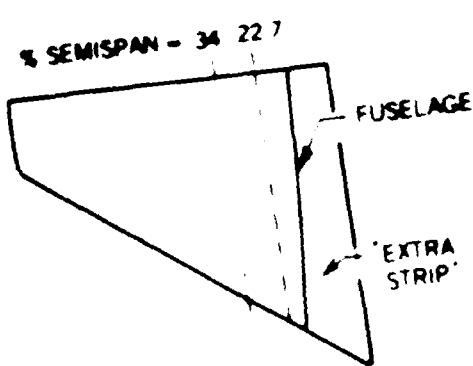


Figure 15. Comparison of computed and experimental lift curves for the ANF wing/body configuration.



(a)



(b)

Figure 16. Comparison of computed and experimental pressure distribution for ANF wing/body configuration, $\alpha = 7.7^\circ$, $M = 0.6$. (a) 22.7% semispan. (b) 34.5% semispan.

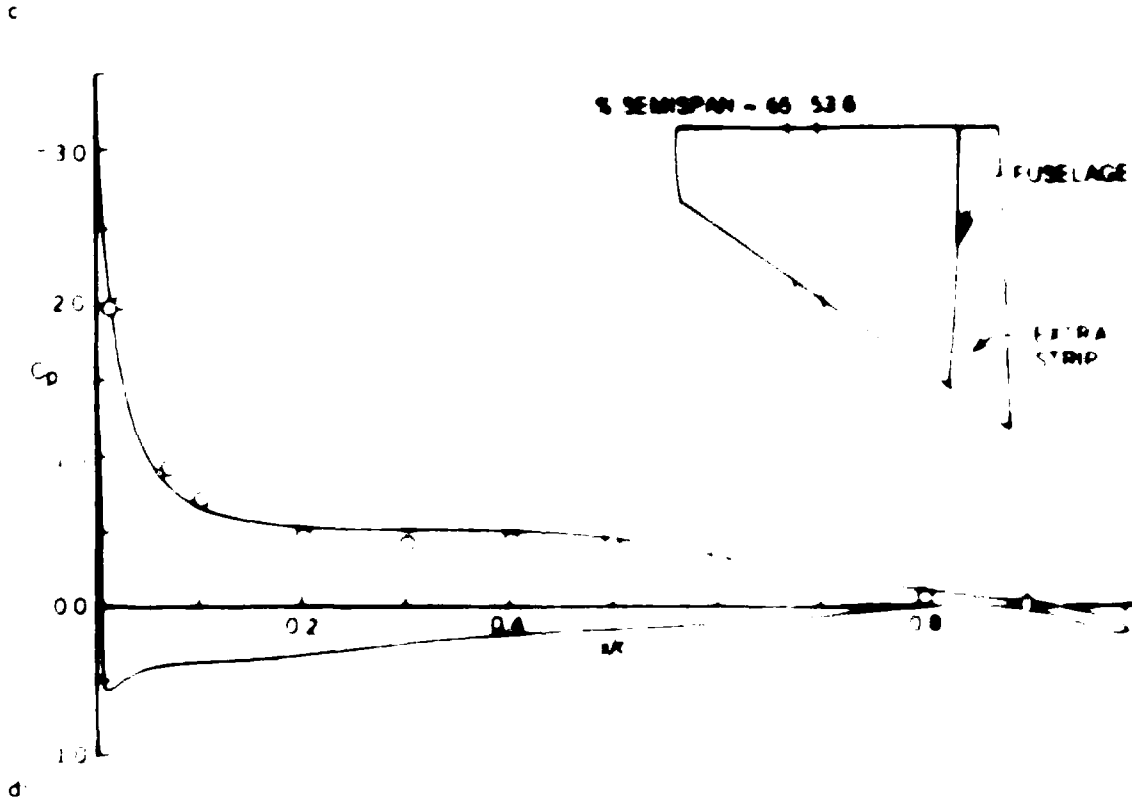
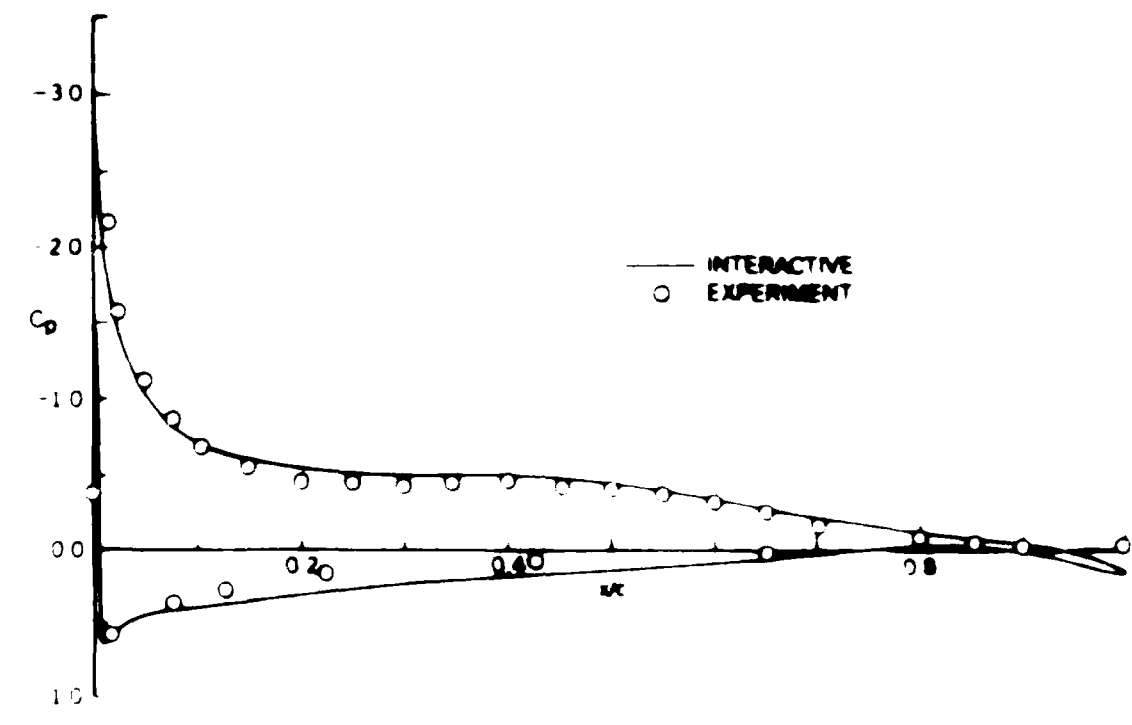


Figure 11. Comparison of lift and drag coefficients for a fuselage with a semi-span of 65.536.

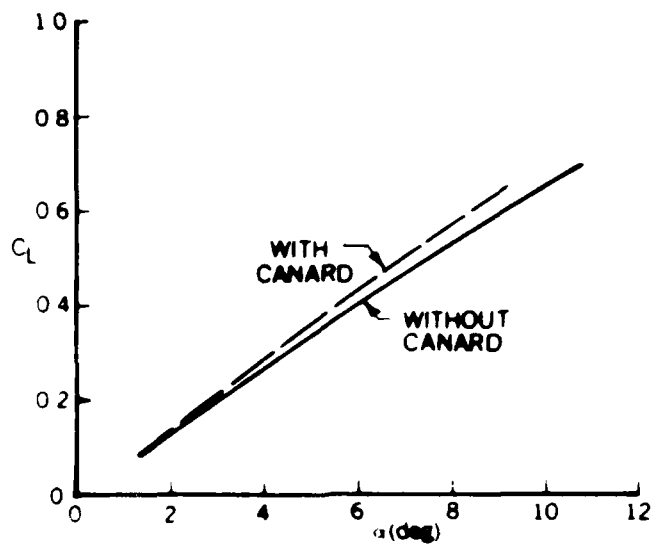


Figure 1. Effect of canard on the calculated lift curve of the ANF wing/body configuration, $M = 0.6$.

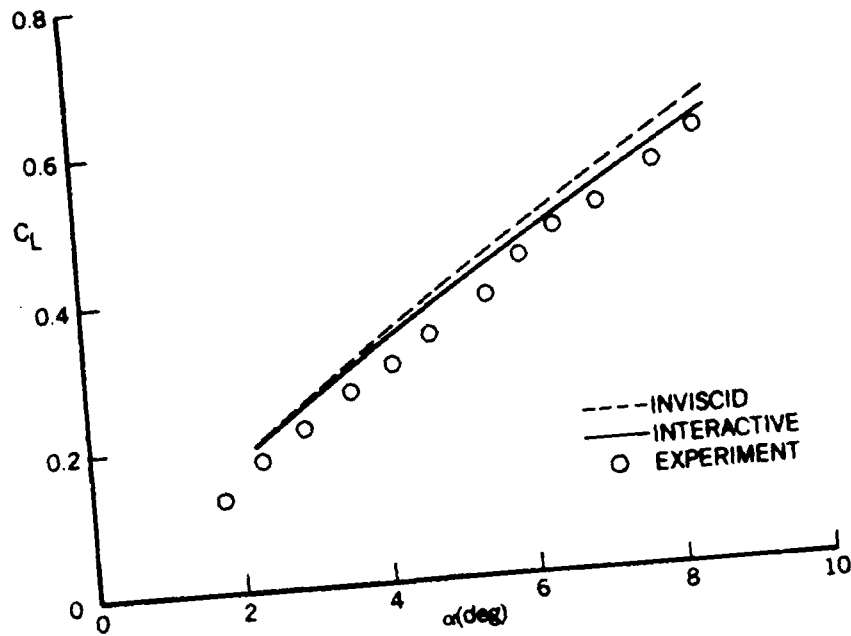


Figure 18. Comparison of computed and experimental lift curves for the unmodified F-15.

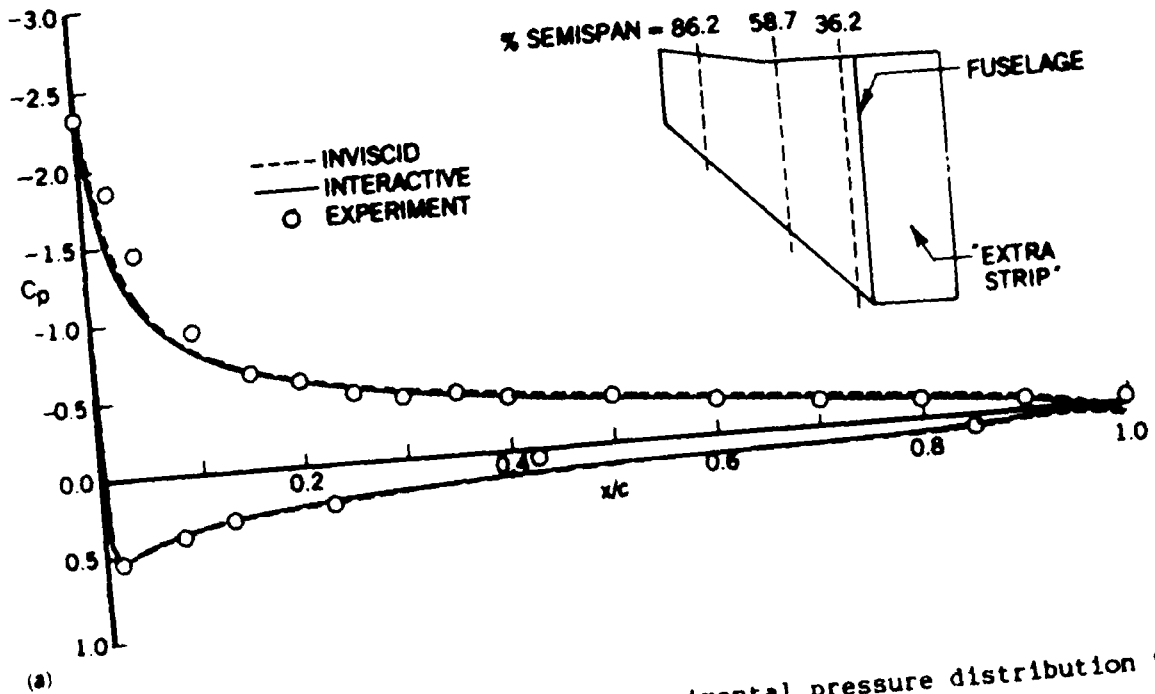


Figure 19. Comparison of computed and experimental pressure distribution for the unmodified F-15, $\alpha = 8.66^\circ$. (a) 36.2% semispan.

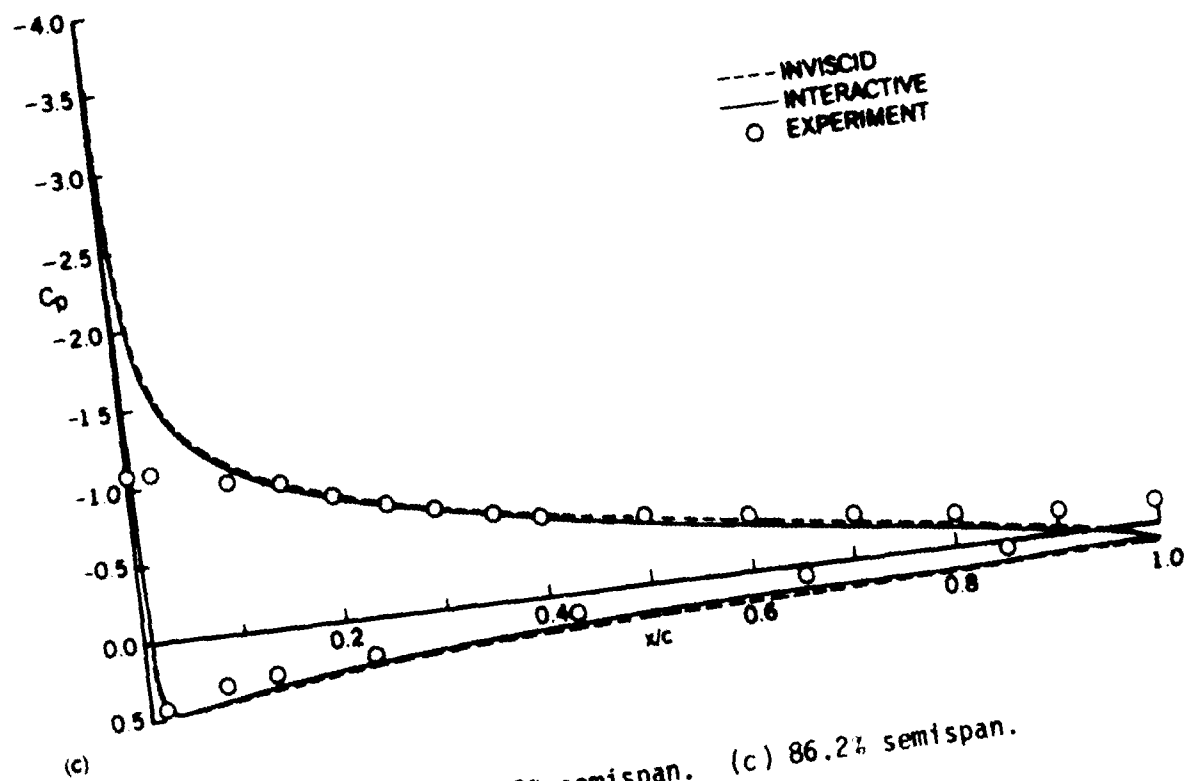
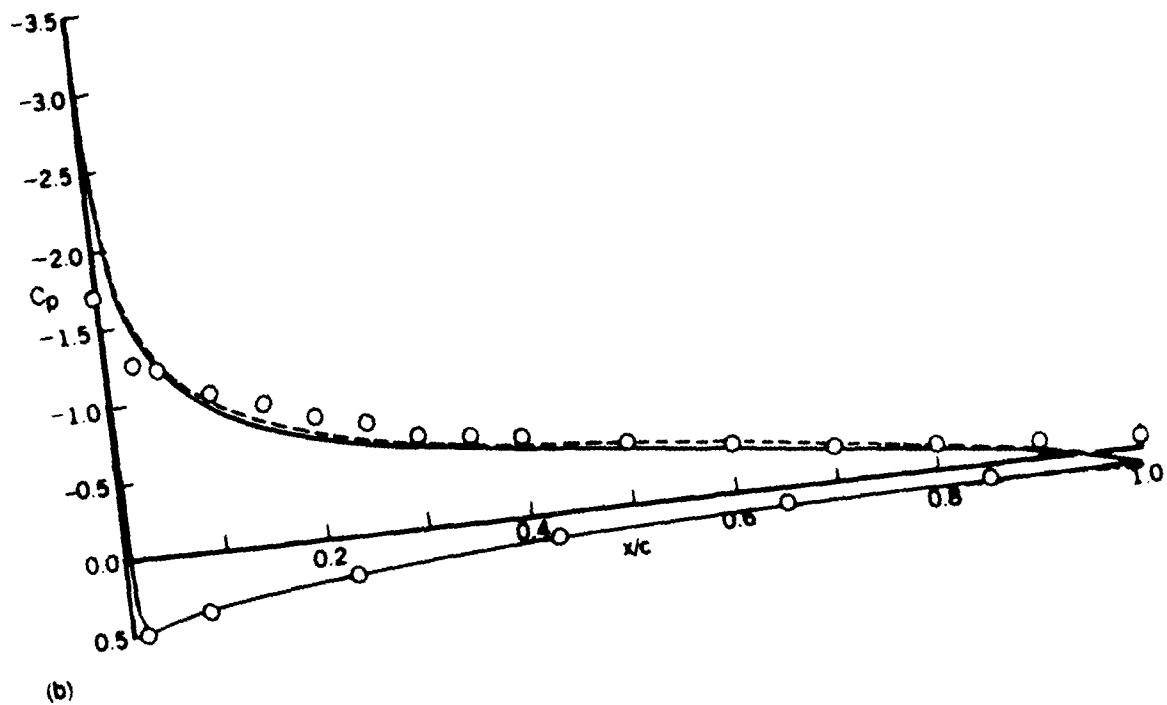


Figure 19. (Continued) (b) 58.7% semispan. (c) 86.2% semispan.

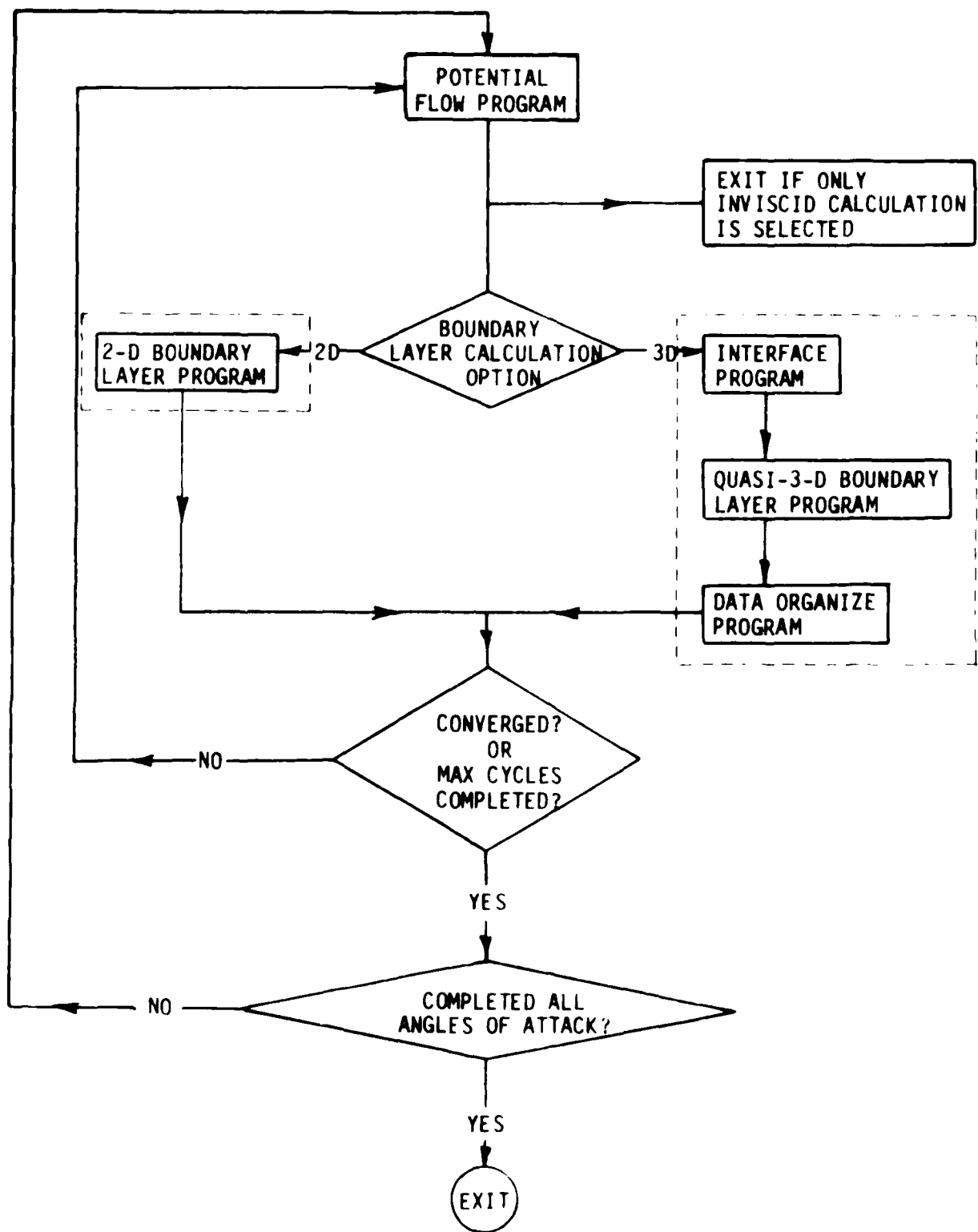


Figure 20. Flow structure of three-dimensional viscous/inviscid interaction program.

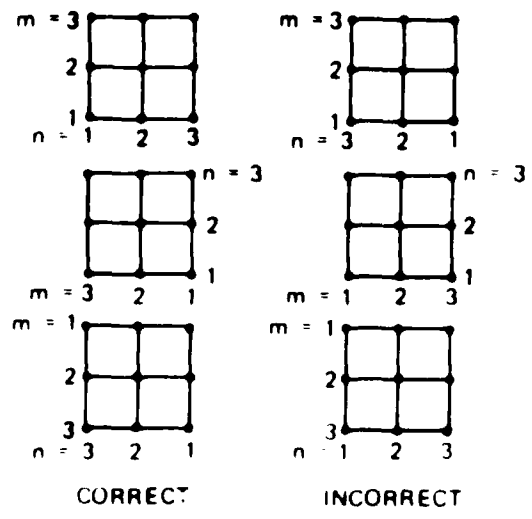


Figure 21. Examples of correct and incorrect input.

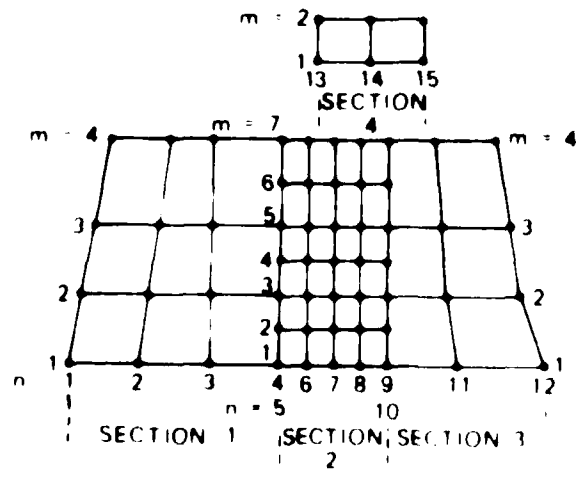


Figure 22. Plan view of the input points on a body divided into sections.

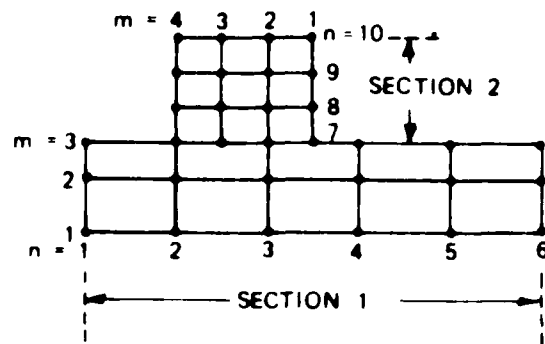


Figure 23. Another possible division into sections.

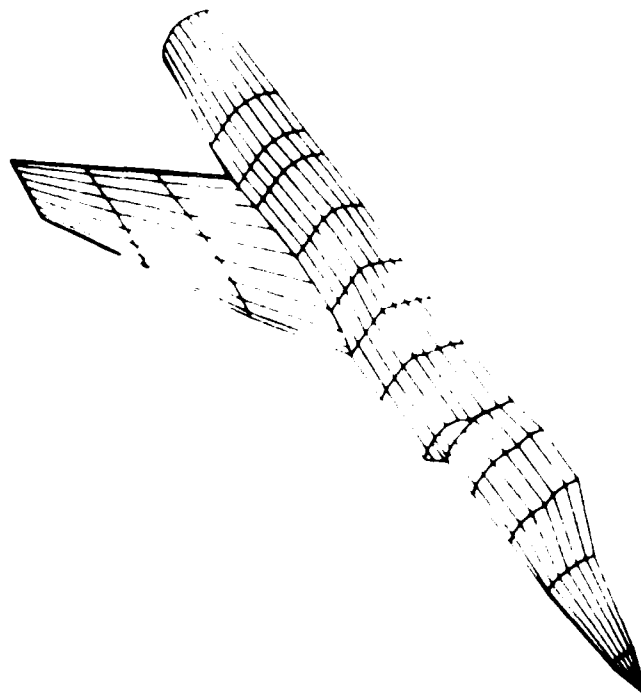


Figure 24. Arrangement of panels for the sample test case.

PAGE 1 3-D VISCOUS-INVISCID INTERACTIVE PROGRAM TUESDAY, APR 15, 1986
 CASE TITLE: REPORT TEST CASE, TRANS. CALC., ZDSTRIP BL, M=0.6, ALPHAS ALPHA = 1.30 MACH = 0.6000
 PAGE TITLE: USER INPUT DATA VISCOUS/INVISCID CYCLE NO. 0

CASE TITLE: REPORT TEST CASE, TRANS. CALC., ZDSTRIP BL, M=0.6, ALPHAS

NAMELIST "A" INPUT DATA :

IBL3D = 0 IPMTB3 = 0 IPMTGM = 0 IPNTNU = 0 KINKNO = 0
 LIFT3D = 1 MAXAMG = 2 MAXCYC = 2 MLINE = 21 NLINE = 5
 ALPHA = 1.300000
 AMACH = 0.600000

NAMELIST "B" INPUT DATA :

IAUTOM = 2 IPCV = 1 ITERAT = 1 IVNSP = 1 LIFSEC = 1
 LINEAR = 0 LIST = 0 MOFF = 0 NSYMI = 1 NSYMZ = 0
 IXPFLAG = 3 0
 MLINE1 = 0
 MLINE = 0
 MSTRIP = 4 0
 NSORCE = 20
 MMAKE = 1 0
 BOV2 = 12 955000 ORIGNX = 0.0 ORIGNY = 0.0 ORIONZ = 0.0
 REFCMD = 8.291200 RFAREA = 95.904007

BOUNDARY LAYER INPUT DATA :

BL2D = 0.000000 RC = 0.700000E+07 RSTART = 0.0 VGP = 1.125353
 ETAE = 8.000000 DETAI = 0.015775
 UPPER SURFACE DATA :
 NB = 70 ITR = 2 ISMP = 10 NTRM = 0
 LOWER SURFACE DATA :
 NB = 51 ITR = 2 ISMP = 5 NTRM = 0
 START COMPUTING ALPHA = 1.300

Figure 25. Output from the sample test case.

CASE TITLE: REPORT TEST CASE TRANS. CALC. 2DSTRIP BL. M=0.6, ALPHAS ALPHA = 1.50 MACH = 0.6000
PAGE TITLE: INPUT DATA VISCOUS/INVISCID CYCLE NO. 0

INPUT FLAGS

ICYCLE =	0
BOV2 =	12.95500
CIVAL =	0.0
HGND =	0.0
IAUTOM =	2
IBLFIT =	1
ICONV =	1
ICONT =	1
IOUT =	0
IPCV =	1
ITERAT =	1
KUTTA =	0
IWMSP =	0
LIFSEC =	1
LINEAR =	0
LIST =	0
MAXCYC =	2
MPR =	0
NLR =	0
NOFF =	0
NSYM1 =	1
NSYM2 =	0
ORIGNY =	0.0
ORIGNZ =	0.0
RFAREA =	95.90401
REFCHD =	8.29120
RMACH =	0.60000

RUN MODE = 0 (0=INITIAL RUN. 1=BLOWING RUN.)

NSORCE =	20
NWAKE =	1
NSTRIP =	4
IXFLAG =	3

INPUT UNIFORM ONSET FLOWS IN DEGS AND COMPONENTS

(1) DEG -- 1.29999 COMPONENTS -- 0.999743 0.0 0.022687

INPUT MACH NO. = 0.600000 BETA = 0.800000E+00

Figure 25. (Continued) Output from the sample case.

3-D VISCIOUS-INVISCID INTERACTIVE PROGRAM

REPORT TEST CASE, TRAN, CALC, ZDSTRIP, BL, M=0.6, ALPHAS = 1.30 MACH = 0.6000
 INPUT PANEL CORNER POINTS AND COMPUTED PANEL QUANTITIES VISCIOUS-INVISCID CYCLE NO. 0

PAGE	4	3-D VISCIOUS-INVISCID INTERACTIVE PROGRAM																
CASE TITLE	REPORT TEST CASE, TRAN, CALC, ZDSTRIP, BL, M=0.6, ALPHAS = 1.30 MACH = 0.6000																	
PAGE TITLE	INPUT PANEL CORNER POINTS AND COMPUTED PANEL QUANTITIES																	
PNL NO	IV	IU	X	Y	Z	XA	XB	XC	XD	YE	YF	ZB	NX	NY	NZ	AVERAGE PROJ. DIST	MAXIMUM DIAGONAL	PROJECTE AREA
44	6	28	46606	5.70000	5.58714	28.17281	1.63357	5.60051	0.09007	-0.00650	-0.99591	0.006654	4.155313	2.64594				
45	5	27	59184	5.70000	5.50912	27.02953	1.68795	5.52141	0.07733	-0.01136	-0.99694	0.005085	4.262078	4.10008				
46	4	25	48625	5.70000	5.47897	25.58682	1.77617	5.49062	0.07365	-0.00737	-0.99969	0.010056	4.406711	5.09187				
47	5	26	26028	5.70000	5.48045	23.98625	1.83578	5.53868	-0.01761	-0.00406	-0.99984	0.010056	4.602991	5.53808				
48	6	24	03377	5.70000	5.47608	22.38866	1.94199	5.61974	0.02774	-0.01585	-0.99949	0.019194	4.732355	5.46672				
49	7	22	92799	5.70000	5.47648	20.94963	2.03391	5.69694	-0.03193	-0.03350	-0.99893	0.017456	4.781501	4.82229				
50	8	22	04999	5.70000	5.47933	19.80632	2.13268	5.75927	0.03411	-0.04928	-0.99820	0.014556	4.749308	3.73834				
51	9	21	48695	5.70000	5.45894	18.07140	2.17502	5.78621	-0.00766	-0.08031	-0.99674	0.012314	4.625520	2.36084				
52	10	21	29839	5.70000	5.50273	18.84647	2.20004	5.87724	0.0168	-0.11448	-0.96651	0.007721	4.604711	4.80284				
53	11	21	49162	5.70000	5.59086	19.09769	2.19325	5.99694	-0.03898	0.36394	0.84585	0.000404	4.396436	0.93019				
54	12	22	04639	5.70000	5.69222	19.81845	2.13085	6.13643	-0.17003	0.22631	0.95910	0.001449	4.592165	2.42994				
55	13	22	92105	5.70000	5.77438	20.95973	2.03263	6.21539	-0.07081	0.16140	0.98434	0.009470	4.743588	3.81329				
56	14	24	02501	5.70000	5.85565	22.40240	1.92678	6.24798	-0.03891	0.12971	0.99079	0.018784	4.793959	4.88158				
57	15	25	25134	5.70000	5.89181	24.00360	1.83852	6.22560	-0.00188	0.09538	0.99544	0.012850	4.741836	5.48945				
58	16	26	47662	5.70000	5.85028	25.60114	1.77469	6.11573	0.05485	0.06174	0.99658	0.012906	4.601089	5.54991				
59	17	27	58229	5.70000	5.77590	27.03862	1.68438	5.96145	0.09048	0.04023	0.99509	0.013508	4.410319	5.10722				
60	18	28	46187	5.70000	5.72801	28.18015	1.62168	5.82466	0.09225	0.02518	0.99542	0.016280	4.265160	4.12953				
61	19	29	02650	5.70000	5.69029	28.91148	1.62589	5.71483	0.11308	0.00926	0.99354	0.013185	4.167491	2.66030				
62	20	29	22000	5.70000	5.67000	29.16177	1.63104	5.67000	0.14522	-0.00011	0.98940	0.004006	4.086027	0.91352				
63	21	29	41472	5.70000	5.67000	29.41631	1.63104	5.67000	0.0	0.0	1.00000	0.0	4.076810	0.91398				
64	1	29	16177	1.63104	5.67000	0.0	0.0	6.17000	0.03304	-0.29778	-0.95406	0.003971	1.734078	0.46668				
65	2	28	90755	5.65365	5.65365	28.84802	0.0	6.16821	0.04389	-0.31171	-0.94916	0.008309	1.926676	1.35720				
66	3	27	02953	5.60051	5.52141	28.00394	0.0	6.14668	0.02153	-0.32633	-0.94150	0.015783	2.275011	2.17747				
67	4	25	58682	1.77617	5.49062	25.03412	0.0	6.23597	-0.02688	-0.36258	-0.93156	0.017741	2.710762	2.90402				
68	5	23	98625	1.83578	5.53868	23.20605	0.0	6.41274	-0.06703	-0.38749	-0.91943	0.019998	3.111118	3.39134				
69	6	22	38866	1.94199	5.61974	21.38495	0.0	6.65753	-0.09914	-0.41166	-0.90593	0.020614	3.376589	3.62136				
70	7	20	94963	2.03391	5.69694	19.75064	0.0	6.92859	-0.11689	-0.44096	-0.88988	0.025054	3.530232	3.52737				
71	8	19	80632	2.13268	5.75927	18.45403	0.0	7.15018	-0.11683	-0.47512	-0.87213	0.020852	3.565797	2.99242				
72	9	19	07140	2.17502	5.78621	17.62001	0.0	7.28232	-0.10056	-0.50794	-0.85550	0.014675	3.414163	2.01416				
73	10	18	84647	2.20004	5.87724	17.36226	0.0	7.42204	-0.02297	-0.50845	-0.85203	0.004936	3.214189	0.64297				
74	11	19	09769	2.19325	5.99694	17.64458	0.0	7.55301	-0.30590	0.67700	0.66940	0.000658	3.138953	0.88292				
75	12	19	81845	2.13085	6.13643	18.68807	0.0	7.60223	-0.07191	0.60203	0.79523	0.010760	3.358908	2.18778				
76	13	20	95973	2.03263	6.21539	19.80338	0.0	7.55601	0.01107	0.55435	0.85174	0.016122	3.491758	3.67073				
77	14	22	40240	1.92678	6.24798	21.45753	0.0	7.43768	0.04143	0.52233	0.85174	0.016122	3.491758	3.67073				
78	15	24	00360	1.83852	6.22560	23.28661	0.0	7.25374	0.04493	0.48502	0.87209	0.020823	3.567968	3.74950				
79	16	25	60114	1.77469	6.11573	25.10378	0.0	6.98579	0.10709	0.43396	0.89455	0.022546	3.331994	3.47307				
80	17	27	03862	1.68638	5.96145	26.73785	0.0	6.92997	0.14367	0.38812	0.91034	0.015895	2.764696	2.94201				
81	18	28	18015	1.62168	5.82466	28.03258	0.0	6.43695	0.15806	0.35316	0.92211	0.015719	2.338412	2.19527				
82	19	28	91148	1.62589	5.71483	28.85895	0.0	6.24725	0.17824	0.31733	0.93142	0.014695	1.984590	1.35857				
83	20	29	16177	1.63104	5.67000	29.14000	0.0	6.24725	0.17824	0.31733	0.93142	0.014695	1.984590	1.35857				
84	21	29	41631	1.63104	5.67000	29.43172	0.0	6.17000	0.21157	0.29094	0.93305	0.006306	1.756554	0.46508				
85	1	1	44000	0.0	6.16000	3.00000	0.0	6.90000	0.0	0.29309	0.93608	0.0	1.728189	0.46594				
86	2	1	44000	0.00643	6.16123	3.00000	0.0	6.86682	-0.42309	0.14364	0.89466	0.001006	1.726101	0.17374				
87	3	1	44000	0.00968	6.16049	3.00000	0.0	6.76705	-0.41087	0.45684	0.78897	0.000447	1.722223	0.17160				
88	3	1	44000	0.01043	6.15704	3.00000	0.0	6.61642	-0.39078	0.70527	0.59152	0.000757	1.711767	0.17041				

Figure 25. (Continued) Output from the sample case.

CASE TITLE REPORT TEST CASE TRAMS, CALC, ZDSTRIP BL, M-O 6, ALPHAS ALPHA = 1.30 MACH = 0.6000
PAGE TITLE INPUT PANEL CORNER POINTS AND COMPUTED PANEL QUANTITIES VISCOUS/INVISCID CYCLE NO. 0

Table with columns: CNL NO, IV, IO, X, YA, Z, A, B, C, D, E, F, G, H, I, J, K, L, M, N, O, P, Q, R, S, T, U, V, W, X, Y, Z, AA, AB, AC, AD, AE, AF, AG, AH, AI, AJ, AK, AL, AM, AN, AO, AP, AQ, AR, AS, AT, AU, AV, AW, AX, AY, AZ, BA, BB, BC, BD, BE, BF, BG, BH, BI, BJ, BK, BL, BM, BN, BO, BP, BQ, BR, BS, BT, BU, BV, BW, BX, BY, BZ, CA, CB, CC, CD, CE, CF, CG, CH, CI, CJ, CK, CL, CM, CN, CO, CP, CQ, CR, CS, CT, CU, CV, CW, CX, CY, CZ, DA, DB, DC, DD, DE, DF, DG, DH, DI, DJ, DK, DL, DM, DN, DO, DP, DQ, DR, DS, DT, DU, DV, DW, DX, DY, DZ, EA, EB, EC, ED, EE, EF, EG, EH, EI, EJ, EK, EL, EM, EN, EO, EP, EQ, ER, ES, ET, EU, EV, EW, EX, EY, EZ, FA, FB, FC, FD, FE, FF, FG, FH, FI, FJ, FK, FL, FM, FN, FO, FP, FQ, FR, FS, FT, FU, FV, FW, FX, FY, FZ, GA, GB, GC, GD, GE, GF, GG, GH, GI, GJ, GK, GL, GM, GN, GO, GP, GQ, GR, GS, GT, GU, GV, GW, GX, GY, GZ, HA, HB, HC, HD, HE, HF, HG, HH, HI, HJ, HK, HL, HM, HN, HO, HP, HQ, HR, HS, HT, HU, HV, HW, HX, HY, HZ, IA, IB, IC, ID, IE, IF, IG, IH, II, IJ, IK, IL, IM, IN, IO, IP, IQ, IR, IS, IT, IU, IV, IW, IX, IY, IZ, JA, JB, JC, JD, JE, JF, JG, JH, JI, JJ, JK, JL, JM, JN, JO, JP, JQ, JR, JS, JT, JU, JV, JW, JX, JY, JZ, KA, KB, KC, KD, KE, KF, KG, KH, KI, KJ, KK, KL, KM, KN, KO, KP, KQ, KR, KS, KT, KU, KV, KW, KX, KY, KZ, LA, LB, LC, LD, LE, LF, LG, LH, LI, LJ, LK, LL, LM, LN, LO, LP, LQ, LR, LS, LT, LU, LV, LW, LX, LY, LZ, MA, MB, MC, MD, ME, MF, MG, MH, MI, MJ, MK, ML, MM, MN, MO, MP, MQ, MR, MS, MT, MU, MV, MW, MX, MY, MZ, NA, NB, NC, ND, NE, NF, NG, NH, NI, NJ, NK, NL, NM, NO, NP, NQ, NR, NS, NT, NU, NV, NW, NX, NY, NZ, OA, OB, OC, OD, OE, OF, OG, OH, OI, OJ, OK, OL, OM, ON, OO, OP, OQ, OR, OS, OT, OU, OV, OW, OX, OY, OZ, PA, PB, PC, PD, PE, PF, PG, PH, PI, PJ, PK, PL, PM, PN, PO, PP, PQ, PR, PS, PT, PU, PV, PW, PX, PY, PZ, QA, QB, QC, QD, QE, QF, QG, QH, QI, QJ, QK, QL, QM, QN, QO, QP, QQ, QR, QS, QT, QU, QV, QW, QX, QY, QZ, RA, RB, RC, RD, RE, RF, RG, RH, RI, RJ, RK, RL, RM, RN, RO, RP, RQ, RR, RS, RT, RU, RV, RW, RX, RY, RZ, SA, SB, SC, SD, SE, SF, SG, SH, SI, SJ, SK, SL, SM, SN, SO, SP, SQ, SR, SS, ST, SU, SV, SW, SX, SY, SZ, TA, TB, TC, TD, TE, TF, TG, TH, TI, TJ, TK, TL, TM, TN, TO, TP, TQ, TR, TS, TT, TU, TV, TW, TX, TY, TZ, UA, UB, UC, UD, UE, UF, UG, UH, UI, UJ, UK, UL, UM, UN, UO, UP, UQ, UR, US, UT, UV, UW, UX, UY, UZ, VA, VB, VC, VD, VE, VF, VG, VH, VI, VJ, VK, VL, VM, VN, VO, VP, VQ, VR, VS, VT, VU, VW, VX, VY, VZ, WA, WB, WC, WD, WE, WF, WG, WH, WI, WJ, WK, WL, WM, WN, WO, WP, WQ, WR, WS, WT, WU, WV, WW, WX, WY, WZ, XA, XB, XC, XD, XE, XF, XG, XH, XI, XJ, XK, XL, XM, XN, XO, XP, XQ, XR, XS, XT, XU, XV, XW, XX, XY, XZ, YA, YB, YC, YD, YE, YF, YG, YH, YI, YJ, YK, YL, YM, YN, YO, YP, YQ, YR, YS, YT, YU, YV, YW, YX, YZ, ZA, ZB, ZC, ZD, ZE, ZF, ZG, ZH, ZI, ZJ, ZK, ZL, ZM, ZN, ZO, ZP, ZQ, ZR, ZS, ZT, ZU, ZV, ZW, ZX, ZY, ZZ.

TUESDAY, APR 15, 1986

3-D VISCOUS INVISCID INTERACTIVE PROGRAM

REPORT: TEST CASE TRANS CALC 2DSTRIP BL, M=0.6, ALPHAS
INPUT PANEL: CORNER POINTS AND COMPUTED PANEL QUANTITIES

ALPHA = 1.50 MACH = 0.6000
VISCOSUS/INVISCID CYCLE NO. = 0

SEC	ID	IA	D E F I N I T I O N S												A V E R A G E		M A X I M U M		P R O J E C T E D	
			YA	ZA	XB	YB	ZB	NX	NY	NZ	PROJ. DIST	DIAGONAL	AREA	DIAGONAL	AREA					
186	1	25	89417	1.83177	7.75529	26.95972	1.67389	7.47342	0.06649	0.97928	0.19131	0.002345	3.165515	1.55137						
187	2	25	88525	1.82139	7.24348	26.95723	1.67881	6.97343	0.04836	0.99891	-0.00595	0.003384	3.164968	1.55282						
188	3	25	88583	1.84205	6.73567	26.95937	1.69102	6.47266	0.05053	0.99819	0.03260	0.002017	3.172443	1.55508						
189	4	25	89360	1.84257	6.22568	26.96979	1.69079	5.97178	0.04928	0.99878	0.00117	0.000152	3.180747	1.55568						
190	5	26	97006	0.0	8.95094	28.43298	0.0	8.92383	0.03150	0.12796	0.99128	0.009598	1.553557	0.73858						
191	6	26	97418	0.49796	8.90591	28.43552	0.50353	8.83938	0.04736	0.37291	0.92666	0.004812	1.557402	0.73767						
192	7	26	97240	0.96514	8.72838	28.43382	0.97184	8.64061	0.05335	0.67569	0.73249	0.009107	1.564400	0.73594						
193	8	26	96544	1.34274	8.40390	28.42628	1.33215	8.28244	0.05058	0.88395	0.46483	0.004036	1.581067	0.73987						
194	9	26	95724	1.58263	7.96596	28.42099	1.56277	7.82708	0.03764	0.98725	0.15467	0.007003	1.602433	0.73958						
195	10	26	95972	1.67389	7.47342	28.42369	1.62768	7.32153	0.03531	0.99937	-0.00194	0.002899	1.608027	0.74132						
196	11	26	95723	1.67881	6.97343	28.42380	1.62088	6.81034	0.04342	0.99887	0.01918	0.001340	1.618658	0.74270						
197	12	26	95937	1.69102	6.47266	28.42809	1.62782	6.29961	0.04546	0.99891	-0.01039	0.002722	1.634870	0.74231						
198	13	26	96979	1.69079	5.97178	28.44263	1.61640	5.78917	0.00382	0.17222	0.98505	0.001758	2.382419	1.18172						
199	14	28	43298	0.0	8.92383	30.76100	0.0	8.91839	0.00777	0.39569	0.91662	0.002484	2.382488	1.17569						
200	15	28	43552	0.50353	8.83938	30.76100	0.49706	8.62790	0.01138	0.70797	0.70615	0.001036	2.389291	1.17656						
201	16	28	43382	0.97184	8.64061	30.76100	0.95524	8.26269	0.00404	0.87428	0.48540	0.003718	2.394282	1.18474						
202	17	28	42628	1.33215	8.28244	30.76102	1.30854	8.26553	-0.00642	0.99006	0.14052	0.003398	2.393654	1.18289						
203	18	28	42099	1.56277	7.82708	30.76100	1.57001	7.83461	-0.00847	0.99889	-0.01250	0.002028	2.396280	1.18786						
204	19	28	42369	1.62768	7.32153	30.76102	1.64137	7.33864	-0.00680	0.99997	0.00435	0.002344	2.393211	1.18656						
205	20	28	42380	1.62088	6.81034	30.76100	1.63888	6.83327	-0.00493	0.99978	-0.02050	0.000513	2.381105	1.18128						
206	21	28	42809	1.62782	6.29961	30.76100	1.63888	6.32798	0.00440	0.16946	0.98553	0.002472	5.262889	2.45523						
207	22	28	44263	1.61640	5.78917	30.76100	1.62955	5.82798	0.00691	0.41152	0.91137	0.007556	5.269319	2.44759						
208	23	30	76100	0.0	8.91839	36.00000	0.0	8.89000	0.01054	0.67918	0.73390	0.011086	5.275148	2.44541						
209	24	30	76100	0.49706	8.83938	35.99997	0.42667	8.62165	0.01045	0.83307	0.55307	0.010256	5.282365	2.45018						
210	25	30	76100	0.95524	8.64235	35.99997	0.82006	8.36565	0.01592	0.97508	0.22131	0.017216	5.288132	2.45503						
211	26	30	76100	1.30854	8.26553	35.99997	1.15188	8.36565	0.02144	0.99573	-0.00932	0.000595	5.296791	2.45830						
212	27	30	76100	1.57001	7.83661	35.99997	1.40774	8.01714	0.02668	0.98882	-0.04065	0.00025	5.307860	2.45411						
213	28	30	76100	1.64727	7.33864	35.99997	1.53620	7.60670	0.06171	0.97541	-0.21158	0.048875	5.320848	2.40371						
214	29	30	76100	1.64137	6.83327	35.99997	1.53336	7.17385	0.00450	0.16378	-0.98562	0.005181	5.285070	1.95443						
215	30	30	76100	1.63888	6.32798	35.99998	1.49776	6.74338	-0.05030	0.07576	-0.99586	0.002861	5.273629	1.96647						
216	31	30	76100	1.62955	5.82797	35.99997	1.31294	6.35332	-0.04189	0.29804	-0.95363	0.003951	5.270663	1.95509						
217	32	13	24000	2.49562	6.08937	16.42842	2.33368	5.93854	-0.04803	0.11126	-0.99263	0.007266	3.2588414	1.96511						
218	33	13	24000	1.86802	5.99559	16.42966	2.33368	5.93854	-0.04156	0.16378	-0.98562	0.005181	3.285070	1.95443						
219	34	13	24000	1.23555	5.93222	16.42834	1.75313	5.83150	-0.05030	0.07576	-0.99586	0.002861	3.273629	1.96647						
220	35	13	24000	0.63137	5.75612	16.42856	1.15746	5.78050	-0.04189	0.29804	-0.95363	0.003951	3.270663	1.95509						
221	36	13	24000	0.0	5.70000	16.42874	0.0	5.53106	-0.04803	0.11126	-0.99263	0.007266	3.2588414	1.96511						
222	37	16	42842	2.33368	5.93854	18.82666	2.19727	5.85649	-0.04986	0.32227	-0.94533	0.042979	2.495832	1.30712						
223	38	16	42966	1.75313	5.83150	18.83253	1.74812	5.61213	-0.08748	0.07287	-0.99350	0.003692	2.485142	1.43054						
224	39	16	42834	1.15746	5.78050	18.82961	1.16044	5.57671	-0.08748	0.07287	-0.99350	0.003692	2.485142	1.43054						
225	40	16	42856	0.59213	5.61208	18.83125	0.58211	5.48809	-0.06611	0.21870	-0.97355	0.020159	2.488068	1.41081						
226	41	16	42874	0.0	5.53106	18.83109	0.0	5.40837	-0.05052	0.13545	-0.98950	0.000016	2.482788	1.42554						
227	42	18	82666	2.19727	5.85649	20.88670	2.05842	5.69828	-0.05260	0.57492	-0.81652	0.029500	2.155057	0.97577						
228	43	18	83253	1.74812	5.61213	20.87991	1.73170	5.59641	-0.05260	0.57492	-0.81652	0.029500	2.155057	0.97577						

Figure 25. (Continued) Output from the sample case.

PAGE 8		3-D VISCOUS-INVISCID INTERACTIVE PROGRAM													TUESDAY, APR 15, 1986						
CASE TITLE: REPORT TEST CASE, TRANS. CALC., ZDSRIP BL, M=0.6, ALPHAS															ALPHA = 1.30 MACH = 0.6000						
PAGE TITLE: INPUT PANEL CORNER POINTS AND COMPUTED PANEL QUANTITIES															VISCOUS/INVISCID CYCLE NO = 0						
PML NO.	IV	IU	X	E	I	K	Y A	Z A	X B	Y B	Z B	M X	N Y	O R	M A	L S	N Z	AVERAGE PROJ DIST	MAXIMUM DIAGONAL	PROJECTED AREA	
203	2		18.82961	1.16044	5.57671	20.87648	1.15297	5.37175	5.37175	0.10178	0.05172	-0.99346	0.002551	2.142354	1.20176						
204	3		18.83125	0.58211	5.48809	20.88133	0.57510	5.33481	5.33481	-0.06223	0.10709	-0.99030	0.012850	2.147258	1.19551						
205	4		18.83109	0.0	5.40837	20.87863	0.0	5.28024	5.28024	-0.06786	0.11517	-0.99103	0.005988	2.136645	1.19619						
206	4	1	20.88670	2.05842	5.69828	23.87218	1.84097	5.54329	5.54329	0.02409	0.50223	-0.86440	0.048341	3.039151	1.21816						
207	2		20.87648	1.15297	5.37175	23.85582	0.96787	5.44572	5.44572	0.01990	0.01300	-0.99972	0.008531	3.072762	1.59912						
208	3		20.88133	0.57510	5.33481	23.85054	0.48296	5.55211	5.55211	0.04577	-0.06515	-0.99482	0.037354	3.055228	1.54551						
209	4		20.87863	0.0	5.28024	23.84995	0.0	5.48019	5.48019	0.07140	0.11818	-0.99042	0.007054	3.027294	1.50661						
210	5	1	23.87218	1.84097	5.54329	26.95326	1.69297	5.52020	5.52020	0.01946	0.10326	-0.99446	0.034125	3.107005	1.03463						
211	2		23.85594	1.46304	5.43510	26.94032	1.40435	5.58660	5.58660	0.05373	-0.12344	-0.99090	0.025300	3.135004	1.50960						
212	3		23.85054	0.48296	5.55211	26.93353	0.47460	5.67155	5.67155	0.05420	0.11506	-0.99178	0.024805	3.125154	1.45931						
213	4		23.84995	0.0	5.48019	26.93349	0.0	5.60617	5.60617	0.05956	0.14100	-0.98910	0.001319	3.125757	1.40246						
214	6	1	26.95326	1.69297	5.52020	28.43810	1.62904	5.62337	5.62337	0.05714	0.09434	-0.99390	0.005036	3.517400	0.94017						
215	2		26.94032	1.40435	5.58660	28.42143	1.32829	5.63921	5.63921	0.05028	-0.25814	-0.96480	0.000149	3.501754	0.70817						
216	3		26.93353	0.47460	5.67155	28.41666	0.45097	5.73098	5.73098	0.05716	0.04499	-0.99726	0.012194	3.548078	0.65617						
217	4		26.93349	0.0	5.60617	28.41734	0.0	5.65738	5.65738	0.03603	0.14842	-0.98819	0.002911	3.557929	0.69417						
218	7	1	28.43810	1.62904	5.62337	30.77306	1.62954	5.82408	5.82408	0.07717	0.00943	-0.99697	0.009953	3.370031	0.76117						
219	2		28.42143	1.32829	5.63921	30.77306	1.28273	5.80082	5.80082	0.05394	0.25570	-0.96325	0.000745	3.413509	0.73149						
220	3		28.41666	0.45097	5.73098	30.77307	0.43325	5.78187	5.78187	0.03780	0.18562	-0.98189	0.017911	3.598204	1.01546						
221	4		28.41734	0.0	5.65738	30.77306	0.0	5.71667	5.71667	0.02367	0.15505	-0.98162	0.001305	3.592204	1.05464						
222	8	1	30.77306	1.62954	5.82408	35.99997	1.31292	6.35329	6.35329	0.08001	0.30243	-0.86813	0.077120	5.200120	1.16117						
223	2		30.77306	1.28273	5.80082	35.99997	1.07826	6.03748	6.03748	0.04001	0.08001	-0.96813	0.004521	5.253059	1.99517						
224	3		30.77307	0.43325	5.89722	35.99997	0.75934	5.81017	5.81017	0.03893	0.17143	-0.98301	0.006481	5.251007	2.16090						
225	4		30.77306	0.0	5.71667	36.00000	0.0	5.62000	5.62000	0.01795	0.15258	-0.98813	0.000641	5.247349	2.16813						

Figure 25. (Continued) Output from the simulation.

BASED UPON INPUT VALUES OF AREF, BOVZ, CREF, CYAM

TYPE	SEC	NV	CL	CD	CDF	CPITCH	CROLL	CYAM	ETA	SECTCL	SECTCD	ASTRIP	CIRCUITM
LIFT	1	1	0.0045	-0.0003	0.0006	-0.0155	-0.0024	-0.0014	0.8443	0.0284	-0.0018	15.0991	-0.0042
	2	2	0.0226	-0.0007	0.0020	-0.0700	-0.0075	-0.0042	0.5712	0.0096	-0.0028	24.1940	-0.0175
	3	3	0.0512	-0.0001	0.0064	-0.1443	-0.0185	-0.0113	0.2759	0.1303	-0.0002	35.5155	-0.0322
SECT. TOT:			0.0784	-0.0011	0.0090	-0.2297	-0.0284	-0.0170					
NLIF	2	1	-0.0008	0.0010	-0.0016	0.0010	0.0005	0.0003					
	2	2	-0.0029	0.0009	-0.0024	0.0026	0.0014	0.0010					
SECT. TOT:			-0.0037	0.0018	-0.0040	0.0035	0.0019	0.0013					
NLIF	3	1	-0.0019	-0.0000	0.0031	0.0019	-0.0048	-0.0032					
	2	2	0.0037	-0.0005	0.0092	-0.0051	-0.0112	-0.0074					
	3	3	0.0023	-0.0000	0.0042	-0.0034	-0.0061	-0.0040					
SECT. TOT:			0.0041	-0.0005	0.0184	-0.0067	-0.0222	-0.0167					
NLIF	4	1	0.0028	0.0001	0.0034	-0.0050	-0.0060	-0.0039					
	2	2	0.0019	0.0000	0.0011	-0.0041	-0.0023	-0.0015					
	3	3	0.0027	0.0007	0.0076	-0.0060	-0.0178	-0.0115					
	4	4	0.0064	0.0009	0.0131	-0.0166	-0.0350	-0.0227					
	5	5	0.0042	0.0007	0.0083	-0.0125	-0.0251	-0.0163					
	6	6	-0.0004	-0.0000	-0.0007	0.0012	0.0024	0.0016					
	7	7	-0.0011	-0.0000	-0.0037	0.0039	0.0133	0.0086					
	8	8	-0.0013	-0.0001	-0.0031	0.0050	0.0125	0.0081					
SECT. TOT:			0.0153	0.0023	0.0259	-0.0340	-0.0580	-0.0377					
NLIF	5	1	-0.0008	-0.0001	0.0001	0.0014	-0.0002	-0.0002					
	2	2	0.0011	0.0001	-0.0001	-0.0023	0.0002	0.0002					
	3	3	-0.0003	-0.0000	-0.0001	0.0007	0.0002	0.0001					
	4	4	-0.0015	0.0000	-0.0003	0.0041	0.0009	0.0006					
	5	5	-0.0024	0.0000	0.0000	0.0073	0.0000	-0.0000					
	6	6	0.0006	-0.0000	0.0000	-0.0019	-0.0000	-0.0001					
	7	7	0.0030	-0.0001	-0.0000	-0.0107	-0.0000	0.0000					
	8	8	0.0024	0.0000	-0.0007	-0.0096	0.0029	0.0019					
SECT. TOT:			0.0021	0.0000	-0.0011	-0.0110	0.0038	0.0025					
CONFIG. TOT:			0.0962	0.0026	0.0483	-0.2779	0.0058	0.0657					

Figure 25. (Continued) Output from the sample case.

CASE TITLE: REPORT TEST CASE, TRANS. CALC., 2DSTRIP BL, M=0.6, ALPHAS

PAGE TITLE: INPUT DATA

ALPHA = 1.30 MACH = 0.6000
VISCOUS/INVISCID CYCLE NO. 7

INPUT FLAGS

```

ICYCLE = 2
BOV2 = 12.95500
CIVAL = 0.0
HGND = 0.0
IAUTOM = 2
IBLFIT = 1
ICONT = 1
ICONV = 1
IOUT = 0
IPCV = 1
ITERAT = 1
KUTTA = 2
IVNSP = 3
LIFSEC = 1
LINEAR = 0
LIST = 0
MAXCYC = 2
MPR = 0
NLR = 0
NOFF = 0
NSYM1 = 1
NSYM2 = 0
ORIGNX = 0.0
ORIGNY = 0.0
ORIGNZ = 0.0
REFAREA = 95.90401
REFCHD = 8.29120
RMACH = 0.60000

```

RUN MODE = 1 (0=INITIAL RUN. 1=BLOWING RUN.)

```

NSORCE = 20
NMAKE = 1
NSTRIP = 4
IXFLAG = 3

```

OFF - BODY KUTA CONDITION HAS BEEN SELECTED...
 PRINTED CP DISTRIBUTION AND FORCE CALCULATION
 WILL USE OFF - BODY PRESSURES

INPUT UNIFORM ONSET FLOWS IN DEGS AND COMPONENTS

(1) DEG -- 1.299999 COMPONENTS -- 0.999743 0.0 0.022687

INPUT MACH NO. = 0.600000 BETA = 0.800000E+00

Figure 25. (Continued) Output from the sample case.

REPORT TEST CASE TRANS. CALC., 2DSTRIP BL, M=0.6, ALPHAS
FUNDAMENTAL FLOW SOLUTION

***** WARNING ***** PRINTED CP, VX, VY, VZ AND FORCES ARE COMPUTED AT OFF - BODY POINTS

PNL. SEC. NO.	SEC. TYPE	IV	IU	CONTROL POINTS			INCOMPRESSIBLE POTENTIAL FL. SOLUTN			VISCOUS FLOW SOLUTION				
				X	Y	Z	VX	VY	VZ	VT	CPVISC	DELS	H	CF
1	1	LIFT	1	29.24013	10.96359	5.66436	0.93231	-0.01307	0.08559	0.93632	0.12468	0.01364	1.44747	0.00215
2	2			29.03622	10.96347	5.64078	0.98662	-0.01499	0.10140	0.99193	0.01610	0.01122	1.40443	0.00254
3	3			28.64761	10.96357	5.60907	1.02211	-0.01426	0.05038	1.02345	-0.04725	0.00901	1.37516	0.00296
4	4			28.11116	10.96349	5.58675	1.01983	-0.01113	0.02401	1.02018	-0.04061	0.00763	1.37522	0.00314
5	5			27.48058	10.96352	5.56079	1.01973	-0.01228	0.04799	1.02094	-0.04215	0.00627	1.38920	0.00326
6	6			26.81805	10.96350	5.52009	1.03064	-0.01718	0.06576	1.03287	-0.06643	0.00467	1.40574	0.00350
7	7			26.18784	10.96351	5.48367	1.04009	-0.01847	0.03926	1.04099	-0.08304	0.00308	1.43536	0.00392
8	8			25.65141	10.96352	5.46120	1.02644	-0.01792	0.03486	1.02706	-0.05459	0.00160	1.45275	0.00413
9	9			25.26169	10.96329	5.44005	1.07117	-0.03579	0.07396	1.07432	-0.15203	0.00118	2.65748	0.00141
10	10			25.06764	10.97600	5.44348	1.10662	-0.04894	-0.32796	1.15523	-0.32460	0.00056	2.40618	0.00390
11	11			25.07443	10.96301	5.48399	0.77459	-0.01763	0.38051	0.87971	-0.23075	0.00046	2.46123	0.00507
12	12			25.25879	10.96352	5.52620	1.06502	-0.02358	0.11381	1.07135	-0.14583	0.00086	2.43471	0.00267
13	13			25.64748	10.96352	5.56395	1.02522	-0.00116	0.08888	1.03305	-0.06678	0.00154	2.54228	0.00128
14	14			26.18195	10.96349	5.62001	1.03308	-0.00266	0.11678	1.03966	-0.08031	0.00194	1.50915	0.00416
15	15			26.81053	10.96356	5.68236	1.07420	-0.01810	0.08719	1.07788	-0.15949	0.00342	1.41828	0.00382
16	16			27.47318	10.96352	5.71222	1.07533	-0.02718	0.09927	1.07571	-0.15494	0.00503	1.40258	0.00339
17	17			28.10471	10.96349	5.70677	1.03977	-0.02277	-0.02585	1.04034	-0.08171	0.00687	1.40091	0.00308
18	18			28.64288	10.96350	5.69308	1.01909	-0.01937	-0.02554	1.01960	-0.03944	0.00865	1.40263	0.00285
19	19			29.03436	10.96348	5.68132	0.99370	-0.01648	-0.03353	0.99440	-0.01118	0.01085	1.42634	0.00248
20	20			29.24001	10.96351	5.67272	0.95605	-0.01389	-0.03472	0.93679	-0.12377	0.01330	1.47251	0.00205
21	21	LIFT	2	29.16090	7.39987	5.66219	0.91564	-0.01339	0.07040	0.91844	-0.15867	0.02141	1.44938	0.00192
22	22			28.84059	7.39991	5.62529	0.96203	-0.01540	0.10577	0.96795	-0.06342	0.01746	1.40458	0.00224
23	23			28.23080	7.39988	5.56673	1.01934	-0.01629	0.07057	1.02191	-0.04413	0.01333	1.36412	0.00267
24	24			27.38876	7.39995	5.52633	1.03561	-0.01078	0.01658	1.03580	-0.07240	0.01075	1.35239	0.00292
25	25			26.39757	7.39989	5.50779	1.03201	-0.00625	0.00969	1.03207	-0.06479	0.00877	1.35971	0.00307
26	26			25.35545	7.39992	5.48668	1.02821	-0.00451	0.02158	1.02845	-0.05741	0.00675	1.37464	0.00325
27	27			24.36435	7.39990	5.46707	1.01886	-0.00109	0.00754	1.01889	-0.03800	0.00473	1.40066	0.00353
28	28			23.52112	7.39990	5.45788	1.00530	-0.01013	0.00161	1.00535	-0.01072	0.00266	1.45147	0.00410
29	29			22.90884	7.40013	5.44205	1.03720	-0.00732	0.05109	1.03849	-0.07790	0.01362	2.36798	0.00194
30	30			22.58910	7.39812	5.45092	1.00541	-0.01494	-0.27981	1.04373	-0.08866	0.0082	2.48810	0.00259
31	31			22.58403	7.39007	5.51242	0.84744	-0.13831	0.39963	0.94709	-0.10397	0.00061	2.51505	0.00348
32	32			22.90768	7.40009	5.58819	1.06614	-0.02158	0.15716	1.07788	-0.15948	0.01111	2.46504	0.00193
33	33			23.51645	7.39992	5.65806	1.06370	-0.02201	0.09246	1.06794	-0.13873	0.0161	1.68904	0.00320
34	34			24.35703	7.39992	5.73437	1.07019	-0.02539	0.09736	1.08088	-0.16577	0.03553	1.41164	0.00381
35	35			25.34647	7.39989	5.80141	1.10116	-0.03913	0.03167	1.10306	-0.21255	0.00570	1.38025	0.00334
36	36			26.38838	7.39989	5.81260	1.08644	-0.04081	-0.02645	1.08753	-0.17974	0.00823	1.37638	0.00299
37	37			27.37976	7.39992	5.77294	1.04551	-0.03223	-0.05783	1.04760	-0.09662	0.01117	1.38115	0.00273
38	38			28.24221	7.39990	5.72987	1.02087	-0.02363	-0.04470	1.02212	-0.04455	0.01394	1.38315	0.00256
39	39			28.83855	7.39993	5.69944	0.99281	-0.01870	-0.05043	0.99426	-0.01144	0.01786	1.41612	0.00216
40	40			29.16106	7.39991	5.67782	0.91634	-0.01499	-0.06952	0.91909	-0.15745	0.02341	1.49192	0.00159
41	41	LIFT	3	29.07686	3.57456	5.66122	0.90135	-0.00560	0.03300	0.90292	-0.18781	0.02719	1.45170	0.00180
42	42			28.63852	3.57524	5.62328	0.95113	-0.01021	0.07431	0.95409	-0.09044	0.02183	1.40367	0.00213
43	43			27.80554	3.59075	5.55483	1.00331	-0.01397	0.06878	1.00576	-0.01155	0.01639	1.36383	0.00254
44	44			26.65736	3.62799	5.50029	1.03838	-0.01597	0.01731	1.03865	-0.07823	0.01256	1.34654	0.00281
45	45			25.30577	3.66661	5.49795	1.03428	-0.01472	-0.04421	1.03467	-0.07010	0.00989	1.34876	0.00302
46	46			25.88484	3.70989	5.53098	1.01736	-0.01250	-0.03422	1.01801	-0.03623	0.00742	1.36786	0.00320
47	47			22.53481	3.76683	5.57135	1.00265	-0.00704	-0.03848	1.00341	-0.00683	0.00475	1.40352	0.00354

Figure 25. (Continued) Output from the sample case.

REPORT TEST CASE, TRANS. CALC., 2DSTRIP BL, M=0.6, ALPHAS ALPHA = 1.30 MACH = 0.6000
FUNDAMENTAL FLOW SOLUTION VISCOUS/INVISCID CYCLE NO. ?

***** WARNING ***** PRINTED CP, VX, VY, VZ AND FORCES ARE COMPUTED AT OFF - BODY POINTS

PNL NO.	SEC NO.	TYPE	IV	IU	X	Y	Z	VX	VY	VZ	FL SOLUTM	VT	CPVISC	DEL'S	M	CF
50	1	LIFT	3	8	21.38661	3.81661	5.60855	0.99272	-0.00028	-0.03998	0.99352	0.01293	0.00449	1.56006	0.00360	
51	9			9	20.55191	3.84817	5.62768	1.00214	-0.00469	-0.01359	1.00224	-0.00449	0.00131	2.46320	0.00174	
52	10			10	20.12907	3.87635	5.66301	0.83159	0.09117	-0.027961	0.88207	0.22642	0.00688	2.49230	0.00337	
53	11			11	20.12923	3.86983	5.75069	0.95051	0.07616	0.61043	1.03114	-0.07719	0.00089	2.42182	0.00257	
54	12			12	20.56233	3.85267	5.86353	1.08542	-0.04040	0.19328	1.10323	-0.21291	0.00153	2.48262	0.00130	
55	13			13	21.38992	3.81062	5.96442	1.10391	-0.06462	0.08515	1.10908	-0.22533	0.00220	1.49197	0.00388	
56	14			14	22.53728	3.75731	6.03259	1.10148	-0.06255	0.04788	1.10429	-0.21517	0.00501	1.60145	0.00337	
57	15			15	23.88872	3.70660	6.06332	1.10401	-0.06082	0.00550	1.10370	-0.21814	0.00790	1.36897	0.00306	
58	16			16	25.30960	3.66691	6.02750	1.08764	-0.05335	-0.05668	1.09042	-0.18582	0.01118	1.56281	0.00279	
59	17			17	26.65891	3.62719	5.93108	1.04836	-0.03743	-0.09349	1.05319	-0.10814	0.01507	1.36786	0.00257	
60	18			18	27.80655	3.58724	5.82587	1.01464	-0.02249	-0.09333	1.01897	-0.03817	0.01918	1.37711	0.00237	
61	19			19	28.64058	3.57153	5.74079	0.97141	-0.01339	-0.10459	0.97712	0.04542	0.02315	1.41573	0.00196	
62	20			20	29.07799	3.57391	5.68655	0.89678	-0.00720	-0.11344	0.90395	0.18590	0.03385	1.50455	0.00139	
85	1	MLIF	1	1	2.46411	0.06440	6.35111	0.75468	0.07703	0.38173	0.84923	0.28587	0.0	0.0	0.0	
86	2			2	2.47168	0.18659	6.59474	0.77080	0.22390	0.31014	0.86050	0.26566	0.0	0.0	0.0	
87	3			3	2.47205	0.28618	6.51136	0.79471	0.31750	0.19068	0.87677	0.23612	0.0	0.0	0.0	
88	4			4	2.46727	0.35007	6.39909	0.82226	0.05226	0.09527	0.89527	0.20205	0.0	0.0	0.0	
89	5			5	2.47436	0.37490	6.27388	0.85603	0.31877	-0.07974	0.91933	0.16153	0.0	0.0	0.0	
90	6			6	2.47711	0.35302	6.14681	0.88443	0.24658	-0.17317	0.93455	0.12844	0.0	0.0	0.0	
91	7			7	2.47280	0.28379	6.03986	0.91063	0.14755	-0.21602	0.94746	0.10325	0.0	0.0	0.0	
92	8			8	2.47440	0.18161	5.96121	0.92291	0.08655	-0.22223	0.95322	0.09211	0.0	0.0	0.0	
93	9			9	2.47641	0.06238	5.90800	0.92732	0.04277	-0.22565	0.95334	0.08800	0.0	0.0	0.0	
94	1	MLIF	2	1	5.00345	0.14725	7.47020	0.89886	0.08386	0.25269	0.93746	0.12248	0.0	0.0	0.0	
95	2			2	5.00385	0.41482	7.33160	0.92507	0.17022	0.15698	0.95361	0.09137	0.0	0.0	0.0	
96	3			3	5.00467	0.62980	7.11092	0.94500	0.18820	0.07900	0.96799	0.06569	0.0	0.0	0.0	
97	4			4	5.01137	0.78530	6.84464	0.95977	0.18308	0.01148	0.97714	0.04538	0.0	0.0	0.0	
98	5			5	5.00465	0.86400	6.54678	0.97014	0.16587	-0.04871	0.98543	0.02900	0.0	0.0	0.0	
99	6			6	5.00488	0.83868	6.24607	0.93182	0.10714	-0.10447	0.99514	0.00970	0.0	0.0	0.0	
100	7			7	5.00902	0.68681	5.98742	0.93554	0.03233	-0.10223	1.00129	-0.00259	0.0	0.0	0.0	
101	8			8	5.00489	0.44066	5.80510	0.99954	0.00351	-0.07620	1.00245	-0.00490	0.0	0.0	0.0	
102	9			9	5.00645	0.15131	5.69692	1.00081	-0.00223	-0.05834	1.00251	-0.00503	0.0	0.0	0.0	
103	1	MLIF	1	1	7.89182	0.22528	8.64750	0.82161	0.22572	0.39664	0.93985	0.11790	0.0	0.0	0.0	
104	2			2	7.88930	0.59265	8.35452	0.98438	0.33180	0.08057	1.04191	-0.08492	0.0	0.0	0.0	
105	3			3	7.89877	0.77934	7.92960	1.04804	0.08741	-0.04195	1.05251	-0.10674	0.0	0.0	0.0	
106	4			4	7.89551	0.97142	7.50561	1.00056	0.17571	0.04801	1.01815	-0.03650	0.0	0.0	0.0	
107	5			5	7.89360	1.19285	7.08127	1.02065	0.17370	-0.04643	1.03636	-0.07355	0.0	0.0	0.0	
108	6			6	7.89500	1.23320	6.60854	1.03699	0.06775	-0.10944	1.04494	-0.09115	0.0	0.0	0.0	
109	7			7	7.89226	1.05357	6.16956	1.03518	-0.02399	-0.06834	1.03771	-0.07632	0.0	0.0	0.0	
110	8			8	7.89304	0.69748	5.84617	1.02804	-0.03618	-0.01388	1.02877	-0.05806	0.0	0.0	0.0	
111	9			9	7.89288	0.24317	5.67151	1.02366	-0.01818	0.01985	1.02402	-0.04840	0.0	0.0	0.0	
112	1	MLIF	2	1	10.26125	0.20661	9.29051	1.07871	-0.02324	0.02212	1.07919	-0.16222	0.0	0.0	0.0	
113	2			2	10.25645	0.63987	8.89867	1.07430	-0.04798	0.07513	1.07846	-0.15943	0.0	0.0	0.0	
114	3			3	10.24283	0.85733	8.40572	1.06318	0.03595	0.1801	1.07032	-0.14368	0.0	0.0	0.0	
115	4			4	10.26551	1.13351	7.94864	1.03734	0.10870	-0.00160	1.04853	-0.09853	0.0	0.0	0.0	
116	5			5	10.26760	1.36949	7.43462	1.03834	0.08569	-0.09160	1.04187	-0.08484	0.0	0.0	0.0	
117	6			6	10.26759	1.41179	6.85602	1.03155	0.03951	-0.01427	1.03281	-0.06548	0.0	0.0	0.0	
118	7			7	10.26149	1.24667	6.30984	1.02184	0.03644	-0.02743	1.02286	-0.04604	0.0	0.0	0.0	

Figure 25. (Continued) Output from the sample case.

CASE TITLE: REPORT TEST CASE TRANS. CALC., 2DSTRIP BL, M=0.6, ALPHAS ALPHA = 1.30 MACH = 0.6000
PAGE TITLE: FUNDAMENTAL FLOW SOLUTION VISCOUS/INVISCID CYCLE NO 2

***** WARNING ***** PRINTED CP, VX, VY, VZ AND FORCES ARE COMPUTED AT OFF - BODY POINTS

Table with columns: PNL. SEC NO., TYPE, IV, IU, X, Y, Z, VX, VY, VZ, FL, SOLUTM, CPVISC, DELS, M, SOLUTION, CF. Rows are numbered 119 to 165 and include labels like '3 NLIF 2', '4 NLIF 1', etc.

Figure 25. (Continued) Output from the sample case.

ALPHA = 1.30 MACH = 0.6000
VISCOUS/INVISCID CYCLE NO. 2

CASE TITLE: REPORT TEST CASE, TRANS. CALC., 2D STRIP BL, M=0.6, ALPHAS
PAGE TITLE: FUNDAMENTAL FLOW SOLUTION

***** WARNING ***** PRINTED CP, VX, VY, VZ AND FORCES ARE COMPUTED AT OFF - BODY POINTS

PNL. NO.	SEC. NO.	TYPE	IV	IU	X	Y	Z	VX	VY	VZ	FL SOLUTM	VT	CPVISC	DELTA	FLOM	SOLUTION	CF
166	4	MLIF	5	5	25.42151	1.70469	7.86266	1.03962	-0.06153	-0.04600	1.04245	-0.08603	0.0	0.0	0.0	0.0	0.0
167	6		6	25.41881	1.75172	7.36230	7.36230	1.04612	-0.05009	-0.04329	1.04822	-0.09788	0.0	0.0	0.0	0.0	0.0
168	7		7	25.41711	1.75855	6.85720	6.85720	1.05115	-0.05059	-0.05659	1.05389	-0.10959	0.0	0.0	0.0	0.0	0.0
169	8		8	25.42238	1.76684	6.35180	6.35180	1.03797	-0.05059	-0.02418	1.03948	-0.07994	0.0	0.0	0.0	0.0	0.0
170	4	MLIF	6	1	27.70573	0.25036	8.90493	0.99409	0.09540	-0.03690	0.99479	-0.01040	0.0	0.0	0.0	0.0	0.0
171	2		2	27.70613	0.73465	8.77844	8.77844	0.99145	0.09236	-0.05632	0.99305	-0.01386	0.0	0.0	0.0	0.0	0.0
172	3		3	27.70192	1.15299	8.51363	8.51363	0.98821	-0.01439	-0.06350	0.99036	-0.01922	0.0	0.0	0.0	0.0	0.0
173	4		4	27.69508	1.45510	8.11951	8.11951	0.98601	-0.02706	-0.06094	0.98826	-0.02337	0.0	0.0	0.0	0.0	0.0
174	5		5	27.69247	1.61170	7.64675	7.64675	0.98503	-0.02921	-0.05920	0.98724	-0.02561	0.0	0.0	0.0	0.0	0.0
175	6		6	27.69366	1.65022	7.14936	7.14936	0.98444	-0.03510	-0.06313	0.98708	-0.02372	0.0	0.0	0.0	0.0	0.0
176	7		7	27.69446	1.65454	6.63872	6.63872	0.98637	-0.04194	-0.06506	0.98940	-0.02113	0.0	0.0	0.0	0.0	0.0
177	8		8	27.70216	1.65640	6.13291	6.13291	0.99925	-0.04588	-0.03929	1.00107	-0.00214	0.0	0.0	0.0	0.0	0.0
178	4	MLIF	7	1	29.59558	0.25010	8.87338	0.98785	0.09415	-0.00911	0.98790	-0.02409	0.0	0.0	0.0	0.0	0.0
179	2		2	29.59525	0.73196	8.73264	8.73264	0.98705	0.07711	-0.01605	0.98720	-0.02348	0.0	0.0	0.0	0.0	0.0
180	3		3	29.59332	1.14206	8.45273	8.45273	0.98534	-0.00386	-0.02437	0.98565	-0.02856	0.0	0.0	0.0	0.0	0.0
181	4		4	29.58984	1.44342	8.05233	8.05233	0.98261	-0.06497	-0.02531	0.98297	-0.03388	0.0	0.0	0.0	0.0	0.0
182	5		5	29.58868	1.60191	7.58049	7.58049	0.97873	-0.08081	-0.03563	0.97944	-0.04084	0.0	0.0	0.0	0.0	0.0
183	6		6	29.59019	1.63428	7.07597	7.07597	0.97395	-0.08783	-0.04399	0.97497	-0.04965	0.0	0.0	0.0	0.0	0.0
184	7		7	29.59125	1.63222	6.56790	6.56790	0.96798	-0.06886	-0.04924	0.96926	-0.06084	0.0	0.0	0.0	0.0	0.0
185	8		8	29.59599	1.62816	6.06016	6.06016	0.96105	-0.00350	-0.06822	0.96348	-0.07218	0.0	0.0	0.0	0.0	0.0
186	4	MLIF	8	1	33.31235	0.23139	8.82471	0.99270	0.00184	-0.00929	0.99275	-0.01446	0.0	0.0	0.0	0.0	0.0
187	2		2	33.31352	0.67604	8.72855	8.72855	0.99251	0.00325	-0.01355	0.99261	-0.01475	0.0	0.0	0.0	0.0	0.0
188	3		3	33.31471	1.06076	8.47324	8.47324	0.99208	-0.00092	-0.01968	0.99227	-0.01591	0.0	0.0	0.0	0.0	0.0
189	4		4	33.31329	1.36159	8.11887	8.11887	0.99159	-0.00071	-0.02439	0.99189	-0.01618	0.0	0.0	0.0	0.0	0.0
190	5		5	33.31270	1.54207	7.69636	7.69636	0.99085	-0.09076	-0.03303	0.99145	-0.01705	0.0	0.0	0.0	0.0	0.0
191	6		6	33.31296	1.59096	7.23419	7.23419	0.98980	-0.02157	-0.03272	0.99058	-0.01879	0.0	0.0	0.0	0.0	0.0
192	7		7	33.31207	1.57947	6.76468	6.76468	0.98902	-0.02776	-0.03493	0.99003	-0.01986	0.0	0.0	0.0	0.0	0.0
193	8		8	33.30974	1.52285	6.30544	6.30544	0.98450	-0.06499	-0.01540	0.98676	-0.02635	0.0	0.0	0.0	0.0	0.0
194	5	MLIF	1	14.81527	2.11342	5.96469	5.96469	1.00894	0.12577	-0.02604	1.01708	-0.03434	0.0	0.0	0.0	0.0	0.0
195	2		2	14.81896	1.50402	5.89102	5.89102	1.00106	0.05295	-0.05104	1.00375	-0.00752	0.0	0.0	0.0	0.0	0.0
196	3		3	14.81444	0.90450	5.77846	5.77846	0.99856	0.04162	-0.03541	1.00005	-0.00011	0.0	0.0	0.0	0.0	0.0
197	4		4	14.81868	0.30595	5.65037	5.65037	0.99545	0.01609	-0.05097	0.99688	-0.00623	0.0	0.0	0.0	0.0	0.0
198	5	MLIF	2	17.59962	2.00868	5.81144	5.81144	0.99139	0.18477	-0.00601	1.00847	-0.01659	0.0	0.0	0.0	0.0	0.0
199	2		2	17.62697	1.45485	5.70088	5.70088	0.97745	-0.07718	-0.08565	0.98423	-0.03137	0.0	0.0	0.0	0.0	0.0
200	3		3	17.62782	0.87312	5.61447	5.61447	0.98096	0.03946	-0.06274	0.98375	-0.03232	0.0	0.0	0.0	0.0	0.0
201	4		4	17.62646	0.29358	5.51007	5.51007	0.98284	0.03370	-0.05315	0.98437	-0.03109	0.0	0.0	0.0	0.0	0.0
202	5	MLIF	3	19.83246	1.93489	5.64308	5.64308	0.98520	0.07253	-0.01727	0.98801	-0.02388	0.0	0.0	0.0	0.0	0.0
203	2		2	19.85184	1.44836	5.48933	5.48933	0.99082	0.04634	-0.10395	0.99733	-0.00531	0.0	0.0	0.0	0.0	0.0
204	3		3	19.85289	0.86769	5.44299	5.44299	1.00256	0.01755	-0.08983	1.00673	-0.01368	0.0	0.0	0.0	0.0	0.0
205	4		4	19.85269	0.28941	5.37808	5.37808	1.01070	0.00839	-0.07250	1.01333	-0.02677	0.0	0.0	0.0	0.0	0.0
206	5	MLIF	4	22.34166	1.77620	5.51833	5.51833	0.96990	-0.04276	-0.00205	0.97085	-0.05774	0.0	0.0	0.0	0.0	0.0
207	2		2	22.32808	1.33181	5.41150	5.41150	1.01904	-0.03363	-0.01518	1.01971	-0.03966	0.0	0.0	0.0	0.0	0.0
208	3		3	22.32729	0.79658	5.42419	5.42419	1.02086	0.04388	-0.06328	1.02221	-0.04472	0.0	0.0	0.0	0.0	0.0
209	4		4	22.32355	0.26516	5.60852	5.60852	1.01996	-0.01835	-0.04628	1.02228	-0.04487	0.0	0.0	0.0	0.0	0.0
210	5	MLIF	5	25.32568	1.60299	5.51299	5.51299	1.03458	-0.03048	-0.01250	1.03511	-0.07099	0.0	0.0	0.0	0.0	0.0
211	2		2	25.39319	1.19109	5.52680	5.52680	1.01902	-0.02373	-0.05330	1.02068	-0.04164	0.0	0.0	0.0	0.0	0.0
212	3		3	25.37105	0.71381	5.58322	5.58322	1.01594	-0.00179	-0.05088	1.01721	-0.03462	0.0	0.0	0.0	0.0	0.0

Figure 25. (Continued) Output from the sample case.

CASE TITLE: REPORT TEST CASE, TRANS. CALC., 2DSTRIP BL, M=0.6, ALPHAS
 PAGE TITLE: FUNDAMENTAL FLOW SOLUTION
 ALPHA = 1.30 MACH = 0.6000
 VISCOUS/INVISCID CYCLE NO. 7

***** WARNING ***** PRINTED CP, VX, VY, VZ AND FORCES ARE COMPUTED AT OFF - BODY POINTS

PNL NO.	SEC NO.	TYPE	IV	IU	X	Y	Z	VX	VY	VZ	FL	VT	CPVISC	DELS	H	SOLUTION	CF
213	5	NLIF	5	4	25.38698	0.23939	5.57731	1.01413	-0.00103	0.03567	1.01476	0.01476	-0.02965	0.0	0.0	0.0	0.0
214	5	NLIF	6	1	27.69252	1.51353	5.58560	0.98902	0.03070	0.04963	0.99074	0.99074	0.01846	0.0	0.0	0.0	0.0
215				2	27.67360	1.13571	5.66022	0.98591	0.02010	0.04173	0.98700	0.98700	0.02589	0.0	0.0	0.0	0.0
216				3	27.66954	0.68392	5.71137	0.98876	0.00774	0.05273	0.99019	0.99019	0.01955	0.0	0.0	0.0	0.0
217				4	27.66939	0.23143	5.66630	0.99183	0.00289	0.03418	0.99243	0.99243	0.01511	0.0	0.0	0.0	0.0
218	5	NLIF	7	1	29.62930	1.46696	5.72402	0.95142	-0.05193	0.06995	0.95540	0.95540	0.08789	0.0	0.0	0.0	0.0
219				2	29.58521	1.08563	5.77759	0.95061	0.01215	0.06671	0.96183	0.96183	0.07540	0.0	0.0	0.0	0.0
220				3	29.59535	0.65382	5.79646	0.98842	0.00182	0.03352	0.96900	0.96900	0.06136	0.0	0.0	0.0	0.0
221				4	29.58678	0.22110	5.72153	0.97199	0.00262	0.01941	0.97219	0.97219	0.05511	0.0	0.0	0.0	0.0
222	5	NLIF	8	1	33.45131	1.32301	6.00874	0.97882	-0.03100	0.07828	0.98264	0.98264	0.03492	0.0	0.0	0.0	0.0
223				2	33.32368	0.99475	5.88553	0.98698	0.03491	0.02059	0.98781	0.98781	0.02428	0.0	0.0	0.0	0.0
224				3	33.34593	0.60794	5.79339	0.98681	0.02723	-0.00987	0.98723	0.98723	0.02542	0.0	0.0	0.0	0.0
225				4	33.33748	0.20518	5.70091	0.98630	0.01035	-0.02095	0.98658	0.98658	0.02671	0.0	0.0	0.0	0.0

Figure 25. (Continued) Output from the sample case.

CASE TITLE: REPORT TEST CASE, TRANS. CALC., 2DSTRIP BL, M=0.6, ALPHAS
 PAGE TITLE: INTEGRATED PRESSURES

ALPHA = 1.30 MACH = 0.6000
 VISCOUS/INVISCID CYCLE NO. 2

TYPE	SEC	NV	CL	CD	CSF	CPITCH	BOV2, CROLL	CREF	CYAW	ETA	SECTCL	SECTCD	ASTRIP	CIRCULTM
***** WARNING *****														
LIFT	1	1	0.0039	PRINTED	CP, VX, VY, VZ	AND FORCES	ARE	COMPUTED	AT	OFF	- BODY	POINTS		
	2	0.0207	-0.0002	-0.0005	-0.0135	-0.0022	-0.0013	0.8463	0.0246				15.0991	-0.0058
	3	0.0484	-0.0006	0.0019	-0.0037	-0.0070	-0.0040	0.5712	0.0820				28.1940	-0.0165
			-0.0001	0.0062	-0.1354	-0.0178	-0.0109	0.2759	0.1506				35.5155	-0.0310
SECT. TOT:		0.0729	-0.0010	0.0086	-0.2126	-0.0271	-0.0162							
MLIF	2	1	-0.0008	0.0010	-0.0016	0.0010	0.0005	0.0003						
	2	-0.0029	0.0009	-0.0024	0.0026	0.0015	0.0010							
SECT. TOT:		-0.0037	0.0018	-0.0040	0.0035	0.0019	0.0013							
MLIF	3	1	-0.0019	-0.0000	0.0051	0.0019	-0.0048	-0.0032						
	2	0.0037	-0.0005	0.0091	-0.0031	-0.0111	-0.0074	-0.0074						
	3	0.0023	-0.0000	0.0041	-0.0034	-0.0061	-0.0040	-0.0040						
SECT. TOT:		0.0041	-0.0005	0.0183	-0.0066	-0.0220	-0.0146							
MLIF	4	1	0.0027	0.0001	0.0033	-0.0048	-0.0058	-0.0038						
	2	0.0018	0.0000	0.0010	-0.0039	-0.0020	-0.0013	-0.0013						
	3	0.0026	0.0007	0.0073	-0.0037	-0.0171	-0.0111	-0.0111						
	4	0.0062	0.0009	0.0128	-0.0161	-0.0341	-0.0221	-0.0221						
	5	0.0041	0.0007	0.0080	-0.0121	-0.0244	-0.0158	-0.0158						
	6	-0.0004	-0.0001	-0.0008	0.0013	0.0028	0.0018	0.0018						
	7	-0.0011	-0.0000	-0.0035	0.0039	0.0126	0.0081	0.0126						
	8	-0.0012	-0.0001	-0.0029	0.0046	0.0115	0.0074	0.0115						
SECT. TOT:		0.0148	0.0022	0.0251	-0.0330	-0.0564	-0.0367							
MLIF	5	1	-0.0007	-0.0000	0.0001	0.0013	-0.0002	-0.0001						
	2	0.0012	0.0001	-0.0001	-0.0024	0.0005	0.0002	0.0002						
	3	-0.0002	-0.0000	-0.0001	0.0005	0.0002	0.0001	0.0001						
	4	-0.0015	0.0000	-0.0003	0.0041	0.0009	0.0006	0.0006						
	5	-0.0024	0.0000	0.0000	0.0074	0.0000	-0.0000	-0.0000						
	6	0.0005	-0.0000	0.0000	-0.0017	-0.0001	-0.0001	-0.0001						
	7	0.0027	-0.0001	-0.0000	-0.0099	-0.0000	0.0000	0.0000						
	8	0.0022	0.0000	-0.0007	-0.0089	0.0027	0.0017	0.0017						
SECT. TOT:		0.0018	0.0000	-0.0011	-0.0096	0.0037	0.0024							
CONFIG. TOT:		0.0899	0.0026	0.0469	-0.2583	0.0040	0.0639							

Figure 25. (Concluded) Output from the sample case.

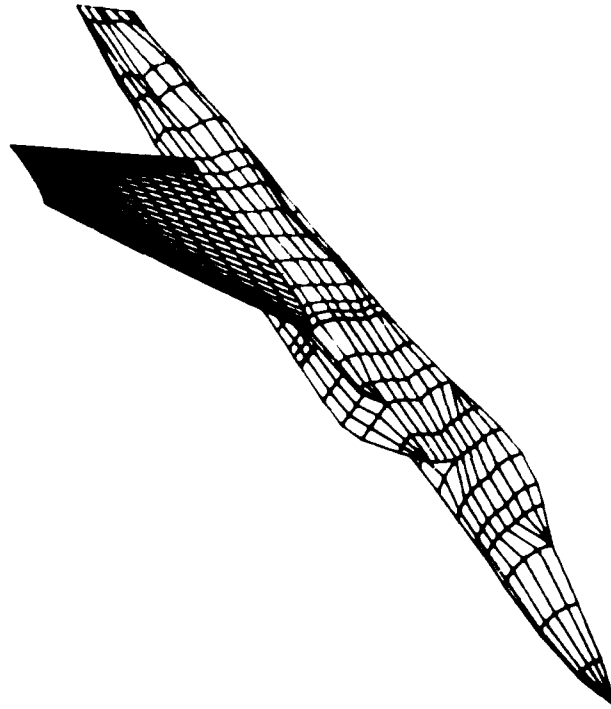


Figure 26. Panel arrangement for test case 1.

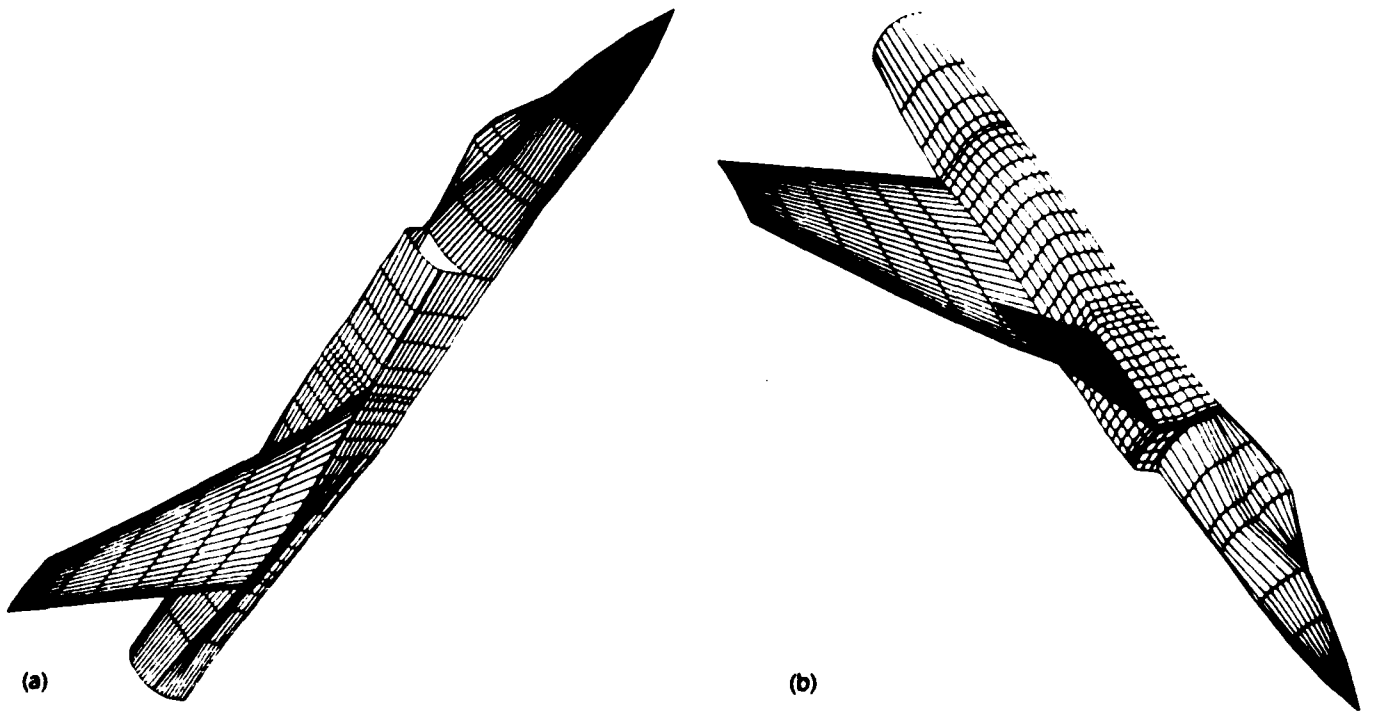


Figure 27. Panel arrangement for test case 2, (a) without canard, (b) with canard.

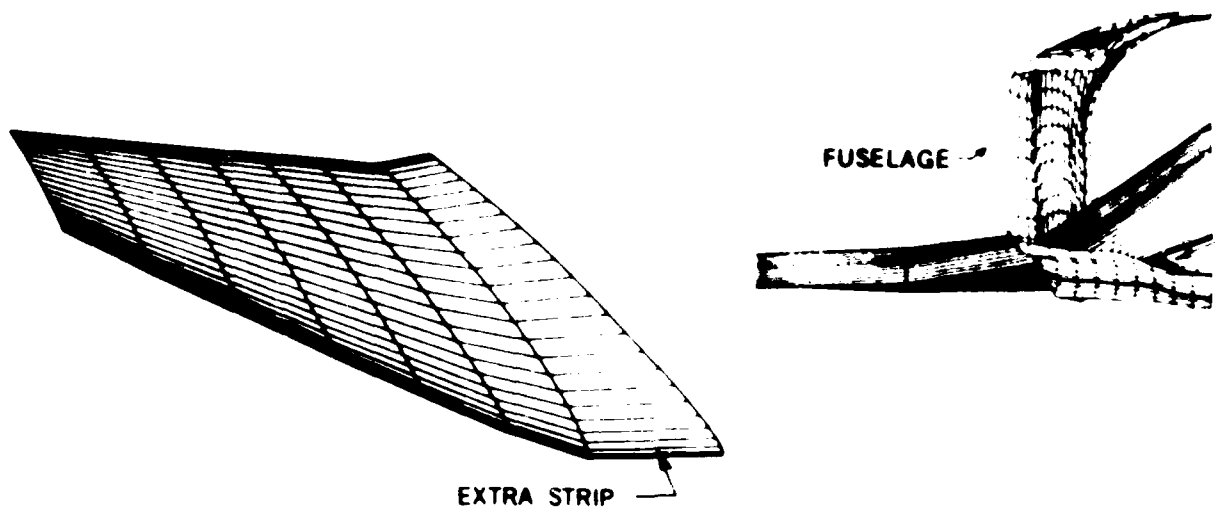


Figure 28. Panel arrangement of the wing for test case 2.

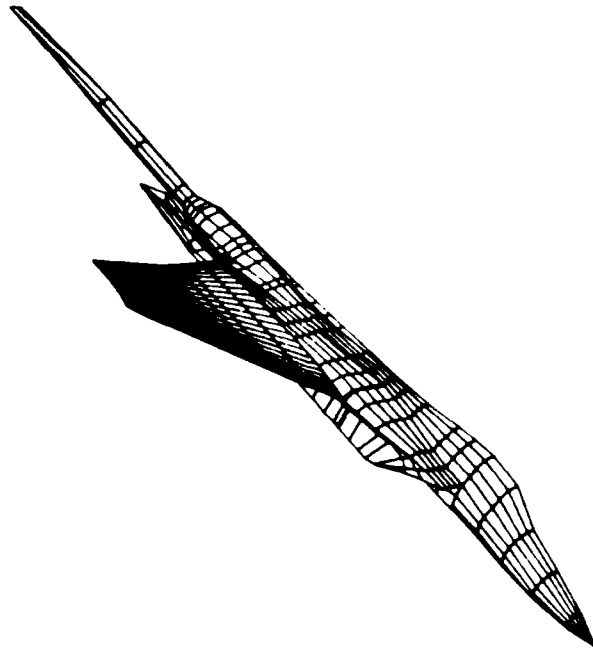


Figure 29. Panel arrangement for test case 3.

EXTRA STRIP

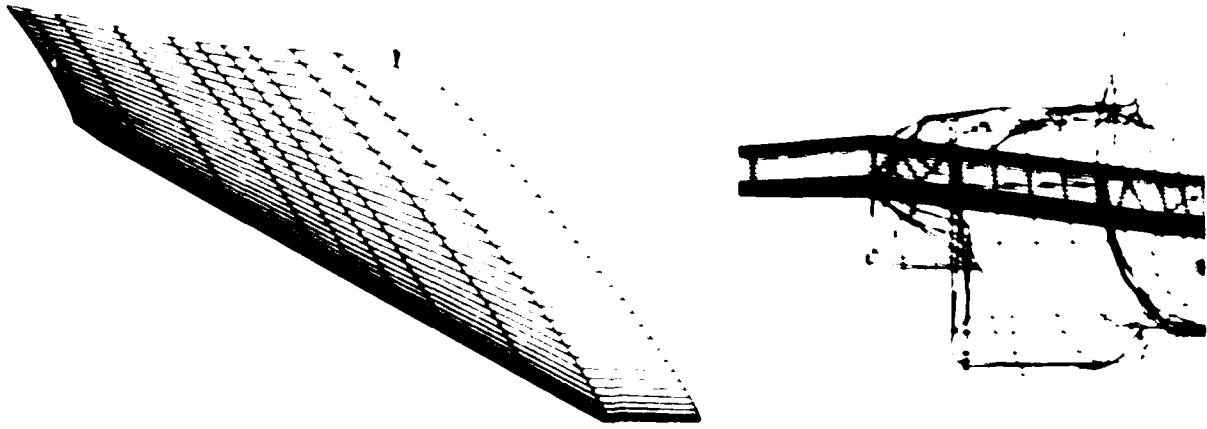


Figure 30. Panel arrangement of the wing for test case 3.

END

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