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# **Radiation Transport in a Nitrogen Plasma General Formalism and 1-Dimensional Model**

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# **RADIATION TRANSPORT IN A NITROGEN PLASMA GENERAL FORMALISM AND 1-DIMENSIONAL MODEL**

# I. INTRODUCTION

An energetic electron beam propagating through air dissociates and ionizes  $N_2$  and  $O_2$  leaving behind a hot plasma composed primarily of N,  $N^+$ ,  $N^{++}$ , O, O<sup>+</sup>, and O<sup>++</sup>. Emissions from this plasma cool the heated channel as well as provide diagnostic information. To properly describe the evolution of the channel under nonequilibrium conditions one must solve, simultaneously, the time-dependent rate equations which provide the population densities of all bound and continuum states involved in the radiative and collisional processes and the corresponding radiative transfer equations which account for the effect of the important emissions on the plasma. In this paper we show the effect of radiation transport on the cooling of a nitrogen plasma. The nitrogen plasma consists of N,  $N^+$ , and  $N^{++}$ , each of which exists in various excited states as well as ground states. The radiation transport is treated as 1dimensional.

Depending on the nature of the specific problem, there are many approaches to solving the radiative transfer equation<sup>1</sup>. For example, geometry, time-dependence, radiation characteristics (line versus continuum radiation, single lines versus many lines, etc.), optical thickness, inclusion of scattering, and the thermodynamic state of the gas all play a role in determining the best approach and corresponding set of approximations. For instance, rarely is an exact solution attempted for geometries other than planar<sup>2</sup>. In many cases decomposition of the radiative transfer equation into a set of moment equations with corresponding restrictions on the angular dependence of the <u>Manuscript approved September 3, 1986</u>.

intensity<sup>3</sup> has proven to be a useful procedure. Kulander<sup>4</sup> used such an approach to investigate radiative transfer in a high-temperature nonequilibrium nitrogen plasma confined to a planar geometry. For radiative transfer in optically thick regions, i.e. regions which are large compared to the optical depth of the radiation, the diffusion approximation method, as developed in neutron transport theory<sup>2</sup>, may be applicable. Comparisons between moment method, diffusion method, and exact (or nearly exact) results have been made for model problems<sup>6</sup>. Multi-frequency grouping methods are often applied when it is necessary to transport many frequencies and possible to define groups of frequencies within which the absorption coefficients are similiar. Average radiative transfer quantities are then calculated'. Combinations of the above approaches may be undertaken as well<sup>8</sup>. One method that has seen extended use is the escape probability formalism, as based on the approach first introduced by Holstein<sup>9</sup>. This method has been used for a variety of problems<sup>10,11</sup>.

The approach presented in this paper derives from the escape probability formalism. Spectral line transfer is emphasized. The basic assumption of the theory, therefore, is the absence of correlation between the frequencies of emitted and absorbed photons in the sequential process. This is rigorously satisfied when the line broadening is determined by impact mechanisms as opposed to the Doppler effect. Rather than attempting to solve the transfer equation frequency-by-frequency over a line-width, an effective probability is derived for the propagation of any photon whose origin is a single transition. This approach allows for the treatment of many lines and accounts for the phenomenon that photons emitted from line wings have longer absorption lengths than those emitted near line center. It also provides for a description of such well-known radiative transfer effects as channel cooling due to radiative emission, diffusion of radiation energy, and photo-pumping, i.e. photoabsorption leading to an enhanced production of electrons, ions, and excited atoms/ions. The method is valid for nonequilibrium conditions and when expected reduces to equilibrium results.

The details of the above approach and its relationship to solving the chemistry rate equations are discussed in section II. Specifics of the model, in particular, line profile, geometry, plasma composition, and temperature and energy equations are presented in section III. Numerical results for two models with specific initial conditions given and discussed in section IV. Concluding remarks are reserved for section V.

#### II. GENERAL FORMALISM

#### Population Dynamics Α.

dt

The coupled rate equations which describe the evolution of the nitrogen plasma include the following collisional and radiative processes: electron impact excitation and deexcitation of N and  $N^+$ , electron impact ionization of N and  $N^+$ , three-body recombination of  $N^+$  and  $N^{++}$ , radiative recombination of  $N^+$  and  $N^{++}$ , spontaneous emission, stimulated emission, and absorption for N and  $N^+$ . The rate equation for  $N_m^{z-1}(r,t)$ , i.e. the population density of the (z-1) ion (or neutral if z=1) in the electronic state whose index is m, is

 $dN^{z-1}$  $(\mathbf{r}, \mathbf{t}) = Ne \begin{bmatrix} \Sigma & N_1^{z-1} & X_{1m}^{z-1} & - & N_m^{z-1} & \Sigma & Y_{m1}^{z-1} \\ 1 < m-1 & & 1 < m-1 \end{bmatrix}$ + Ne  $\begin{bmatrix} \Sigma & N_n^{z-1} & Y_{nm}^{z-1} - N_m^{z-1} & \Sigma & X_{mn}^{z-1} \\ n > m+1 & n > m+1 & mn \end{bmatrix}$ + Ne  $\begin{bmatrix} Ne & \sum N_n^z & \alpha_{3,nm}^{z-1} \\ n & n & n \end{bmatrix}$  +  $\sum N_n^z & \alpha_{r,nm}^{z-1} \end{bmatrix}$ - Ne  $\begin{bmatrix} Ne N_m^{z-1} & \alpha_{3,m1}^{z-2} + N_m^{z-1} & \alpha_{r,m1}^{z-2} \end{bmatrix}$ - Ne  $N_m^{z-1} \sum_{n=1}^{z} S_{mn}^{z-1}$  + Ne  $\sum_{l=1}^{z} N_{l}^{z-2} S_{lm}^{z-2}$ +  $\sum_{\substack{n \geq m+1}} N_m^{z-1} A_{mn}^{z-1} - N_m^{z-1} \sum_{\substack{l \leq m-1}} A_{ml}^{z-1}$ +  $\sum_{\substack{l \leq m-1}} N_l^{z-1} 4\pi B_{lm}^{z-1} \left[ \int_{\Delta v_{-1}} J_v \phi_v dv \right]$  $- N_{m}^{z-1} \sum_{1 \leq m-1} 4\pi B_{m1}^{z-1} \left[ \int_{\Delta v_{m1}} J_{v} X_{v} dv \right]$  $- N_{m}^{z-1} \sum_{n \ge m+1}^{z} 4\pi B_{mn}^{z-1} \left[ \int_{\Delta v_{nm}}^{J} J_{v} \phi_{v} dv \right]$  $+ \sum_{\substack{n>m+1}} N_n^{z-1} 4\pi B_{nm}^{z-1} \left[ \int_{\Delta v_{nm}} J_v X_v dv \right] .$ 

(1)

In Eq. (1) all atom, ion, and electric population densities are implicit functions of r and t. The rate coefficients for excitation, de-excitation, ionization, three-body recombination, radiative recombination, and spontaneous emission are designated by X, Y, S,  $\alpha_2$ ,  $\alpha_r$ , and A, respectively. Subscripts refer to the states involved in the particular transition while superscripts identify the ion stage. For example,  $x_{lm}^{z-1}$  is the rate coefficient for collisional excitation of ions with net charge z-1 to an electronic state m from state 1. The effects of radiation transport on individual species are contained in the last four terms which account for stimulated emission and photoabsorption. These terms depend on the normalized frequency profiles for absorption and emission,  $\phi_{\chi}$  and  $\chi_{\chi}$ , the appropriate Einstein B-coefficient, the linewidths  $\Delta v$ , and the mean angle-averaged intensity,  $J_{y}(r,t)$ . The mean intensity J, is obtained by solving the radiative transfer equation for frequency v; this is discussed in detail later below.

The radiation terms in Eq. (1) are simplified by assuming the emission and absorption profiles are identical. Using the standard relations between the Einstein coefficients Eq. (1) becomes

 $\frac{dN_{m}^{z-1}}{dt}(r,t) = \text{ collisional terms + spontaneous emission}$   $+ \sum_{\substack{l \leq m-1 \\ l \leq m-1}} \frac{c^{2}}{2h\nu_{ml}^{3}} \left[ \int_{\Delta\nu_{ml}} J_{\nu} \phi_{\nu} d\nu \right] N_{m}^{z-1} A_{ml}^{z-1} \left[ \frac{g_{m}^{z-1}}{g_{l}^{z-1}} \frac{N_{l}^{z-1}}{N_{m}^{z-1}} - 1 \right]$   $- \sum_{\substack{n \geq m+1 \\ n \geq m+1}} \frac{c^{2}}{2h\nu_{nm}^{3}} \left[ \int_{\Delta\nu_{nm}} J_{\nu} \phi_{\nu} d\nu \right] N_{n}^{z-1} A_{nm}^{z-1} \left[ \frac{g_{n}^{z-1}}{g_{m}^{z-1}} \frac{N_{m}^{z-1}}{N_{n}^{z-1}} - 1 \right] . (2)$ 

Stimulated emission is now treated as a modification to absorption.

If, in Eq. (2), a "gross re-absorption factor" is defined for each transition line as

$$1 - \Lambda_{ml}^{z-1} = \frac{c^2}{2h\nu_{ml}^3} \left[ \int_{\Delta\nu_{ml}} J_{\nu} \phi_{\nu} d\nu \right] \left[ \frac{g_m^{z-1}}{g_1^{z-1}} \frac{N_1^{z-1}}{N_m^{z-1}} - 1 \right]$$
(3)

then the rate equation becomes

 $\frac{dN_{m}^{z-1}}{dt} (r,t) = \text{ collisional terms + spontaneous emission}$  $+ \sum_{\substack{l \le m-1 \\ l \le m-1}} N_{m}^{z-1} (1 - \Lambda_{ml}^{z-1}) A_{ml}^{z-1}$  $- \sum_{\substack{n \ge m+1}} N_{n}^{z-1} (1 - \Lambda_{nm}^{z-1}) A_{nm}^{z-1} .$ (4)

Optically thick and thin results are frequently obtained by treating the set of  $\{\Lambda\}$  as constants with values ranging between 0 and 1. In this manner the radiative transfer equation need not be solved and limiting population densities are obtained 12-16.

B. Radiative Transfer Equation
 The radiative transfer equation in its simplest form is

$$\frac{dI}{ds} = -\kappa'_{v}I_{v} + j_{v} \qquad (5)$$

Here,  $\kappa'_{v}$  is the absorption coefficient (corrected for stimulated emission) at frequency v,  $j_{v}$  the emission coefficient for the radiation,  $I_{v}$  the intensity, and s defines a ray through the medium. The general non steadystate solution to Eq. (5) is written in integral form as

$$I_{v}(\mathbf{r}, t, \Theta, \Psi) = \int_{s_{0}}^{s} ds' j_{v}(s', t') e^{-\int_{s}^{s} \kappa_{v}'(s'', t'') ds''} .$$
 (6)

In Eq. (6) t' = t-(s-s')/c, t'' = t-(s-s'')/c, and  $j_v$  ds' is the amount of radiation born at s',t' on ray ds' in a direction  $\Theta, \Psi$ . Multiplying by the exponential gives the fraction of radiation that arrives at s,t. The coordinate system is shown in Fig. 1. In this study continuum absorption and emission are neglected. The emission coefficient for a specific transition line  $v_{m1}$  is

$$j_{v} = \frac{hv_{m1}}{4\pi} A_{m1}^{z-1} \phi_{v} N_{m}^{z-1}$$
(7)

The absorption coefficient for the same transition is

$$\kappa_{v}' = \kappa_{v} \left[ 1 - \frac{g_{1}^{z-1} N_{m}^{z-1}}{g_{m}^{z-1} N_{1}^{z-1}} \right]$$
(8)

where

$$\zeta_{v} = \frac{\lambda_{ml}^{2}}{8\pi} \frac{g_{m}^{z-1}}{g_{l}^{z-1}} N_{l}^{z-1} A_{ml}^{z-1} \phi_{v} \qquad (9)$$

The statistical weights for the upper and lower states are  $g_m^{z-1}$  and  $g_1^{z-1}$ .

It is the mean intensity  $J_{\nu}(\mathbf{r},t)$  that enters into Eq. (2) and determines the effect of radiation transport on the individual population densities. Letting  $\rho = |\mathbf{r} - \mathbf{r'}|$ , defining the volume element  $dV = d\mathbf{r'} = {\rho'}^2 \sin \Theta \, d\Theta \, d\Psi \, d\rho'$ , and averaging over  $\Theta, \Psi$  the mean intensity is

$$\frac{hv_{m1}}{4\pi} A_{m1}^{z-1} \phi_{v} \int_{0}^{\rho_{m}} \frac{N_{m}^{z-1}(r',t')}{4\pi \rho'^{2}} e^{-\int_{0}^{\rho'} \kappa_{v}'(r'',t'') d\rho''}$$
(10)

where  $t' = t - \rho'/c$  and  $t'' = t - \rho''/c$ . Eq. (10) gives the angle-averaged solution to the radiative transfer equation for a specific frequency v.

C. Population Dynamics Plus Radiative Transfer The rate equations may be rewritten in simpler form as

 $\frac{dN_m^{z-1}}{dt}$  (r,t) = collisional terms + spontaneous emission dt

 $+ \sum_{\substack{l \le m-1 \\ l \le m-1}} R_{ml}^{z-1} A_{ml}^{z-1} - \sum_{\substack{n \ge m+1 \\ n \ge m+1}} R_{nm}^{z-1} A_{nm}^{z-1}$ (11)

where the set {R} is defined by comparison with Eq. (2). Substituting Eq. (10) into the absorption term, noting that  $\kappa'_{\nu}$  is given by Eq. (8), and interchanging the  $\nu$  and r' integrations results in

$$R_{ml}^{z-1}(r,t) = \int dr' N_{m}^{z-1}(r',t') G_{ml}(r',t';r,t) . \qquad (12)$$

 $G_{m1}$  is the probability that a photon emitted at r',t' is absorbed in a volume element dr at r,t and is given as

$$G_{ml}(r',t',r,t) = \frac{1}{4\pi |r-r'|^2} \int_{\Delta v_{ml}}^{dv \phi_v} \kappa'_v(r,t) e^{-\int_0^{\rho'} d\rho'' \kappa'_v(r'',t'')} . (13)$$

The discretized version of Eqs. (11) - (13) forms the basis for the "escape-probability formalism" discussed previously.

It is useful to compare  $G_{ml}$  to  $T_{ml}(\rho';t)$ , i.e. the probability a photon travels a distance  $\rho'$  without being absorbed, defined as

$$T_{ml}(\rho';t) = \int_{\Delta v_{ml}}^{d_v \phi_v} e^{-\int_0^{\rho'} d\rho'' \kappa'_v(r'',t-\rho''/c)} . \quad (14)$$

Specifically, if  $\kappa'_{v}(\mathbf{r},t) = \kappa'_{v}(\mathbf{r}',t')$  then the following relation holds,

$$G_{ml}(r',t';r,t) = \frac{-1}{4\pi \rho'^2} \quad \frac{\partial}{\partial \rho} T_{ml}(\rho';t) \quad . \tag{15}$$

Physically, the requirement is that over the mean free path of an emitted photon the absorption coefficient does not change much, i.e. the number of absorbers encountered during transit remains nearly constant.  $T_{ml}(\rho';t)$  can be written as

$$T_{ml}(\rho',t) = \int_{\Delta v_{ml}}^{dv} \phi_{v} e^{-\kappa_{v}'(r,t)\rho'}$$
(16)

Eq. (16) was initially introduced by Holstein $^9$  and evaluated for various line profiles.

The problem is now reduced to the following steps: (1) For the transitions included in the model choose an appropriate line shape and evaluate Eq. (16) either exactly or approximately. (2) For the desired geometry obtain the set {G} from Eq. (15). (3) Use these to evaluate the absorption terms in Eq. (12). (4) Solve the rate equations. The procedure must be done self-consistently since  $\kappa_v$ ' depends on the solution to the rate equations. III. MODEL

### A. Nitrogen Plasma

Our interest is in studying radiative transfer in a hot channel, in particular, for electron temperatures of 1.0 - 3.0 eV. In this temperature range the constituents are primarily atomic or ionic. We have included in the calculations the lowest 13 levels of N, the lowest 17 levels of N<sup>+</sup>, and 2 representative levels of N<sup>++</sup>. Details of the model have been presented elsewhere<sup>13,14</sup>. All bound-bound radiative transitions allowed by this energy scheme are included and form the basis for the line radiation discussed previously. In this manner the dominant uv and visible spectral lines are transferred.

#### B. $T(\rho)$

The absorption coefficients, defined in Eqs. (8) and (9), depend on the line shape,  $\phi_{v}$ . We have assumed this line shape is given by a Lorentzian, i.e.

$$\phi_{v,ml} = \frac{1}{\pi} \frac{\Delta v}{(v - v_{ml})^2 + (\Delta v)^2}$$
 (17)

The line width is  $\Delta v$ . In the temperature and electron density regimes of interest, Ne = [ $10^{16} - 10^{19}$  cm<sup>-3</sup>], Doppler and Stark broadening are the two dominant mechanisms. The Lorentz profile, Eq. (17), is characteristic of the Stark broadening, where isolated spectral lines of atoms in dense plasmas are broadened by electron impact<sup>17</sup>. However, in our computations we consider the effects of both Doppler and Stark broadening whose actual line shape should be a Voight profile. In the computations described below, we calculate the line broadening of both as a function of frequency, electron temperature, and electron density and choose  $\Delta v$  to be the greater of the two. The Stark effect generally dominates. Additional details have been presented elsewhere<sup>18</sup>. For the Lorentzian line shape Holstein $^9$  obtained the asymptotic functional form of Eq. (16) as

$$T_{ml}(\rho) = \frac{1}{(\pi \kappa_{ml} \rho)^{1/2}} \qquad \kappa_{ml} \rho >> 1$$
 (18)

 $\kappa_{ml}$  is the absorption coefficient at line center. The exact integration of T( $\rho$ ) is shown in Fig. 2 along with two empirical approximations. For  $x = \kappa_{ml} \rho$  the dotted line corresponds to

$$T_{ml}(\rho) = e^{-x} + \frac{\left[1 - e^{-.8x^{3/2}}\right]}{(\pi x)^{1/2}}$$
(19)

while the dashed line corresponds to

$$T_{ml}(p) = 1 - x/3 \qquad x \le 1$$
  
= (2/3) x<sup>-1/2</sup> x \ge 1. (20)

Eq. (20) is used in this study.

C. Geometry and G<sub>m1</sub>

The results discussed in section IV are for a geometry where radiation is assumed to flow in only two directions, but along one dimension, i.e. r = r. The plasma is contained within a finite region,  $-L \leq r \leq L$ , so in addition to transfer, energy is radiated beyond the boundary. For this geometry the  $4\pi \rho'^2$  factor in Eq. (15) is excluded.

When evaluating Eq. (12) care must be taken to properly consider three possible cases which depend on the absorption length at line center,  $\kappa_{ml}$ , and the distance to the boundary edge, L. The radiation may be thick in both directions,  $L-r \ge 1/\kappa_{ml}$  and  $L+r \ge 1/\kappa_{ml}$ . It may be thin in both directions,  $L-r \le 1/\kappa_{ml}$  and  $L+r \le 1/\kappa_{ml}$ , or thick in one direction and thin in the other,  $L+x \ge 1/\kappa_{ml}$  and

 $L-x \ge 1/\kappa_{ml}$ . Symmetry considerations enable us to reduce computations to the half space r = [0,L]. A typical absorption term for the case where the line is thick in each direction is

$$R_{ml}^{z-1}(r,t) = \frac{\kappa_{ml}}{6} \int_{0}^{1/\kappa_{ml}} d\rho N_{m}^{z-1}(\rho,t)$$

+ 
$$\frac{1}{6 \kappa_{ml}^{1/2}} \int_{1/\kappa_{ml}}^{\rho_{m}} d\rho \frac{N_{m}^{z-1}(\rho,t)}{\rho^{3/2}}$$

+ contribution from the left . (21)

Note that  $\kappa_{ml} = \kappa_{ml}(r,t)$  and  $\rho_m = L-r$ . Similiar results are obtained for the other cases.

# D. Temperature Equation

As radiation is transferred from one local region within the plasma to another, cooling or heating may take place. As radiation escapes the plasma entirely, a net cooling occurs. To model this phenomenon the relevant temperatures, generally, electron and gas, must be monitored. For hot channels created by intense electron beams the plasma electron temperature and the gas kinetic temperature frequently reach an identical value, afterwhich the subsequent evolution is well described by a single temperature. In the present model it is assumed that for a given set of initial conditions the plasma is characterized by a single temperature, i.e. T(r,t) = Te(r,t) = Tg(r,t). The time evolution of T(r,t) is obtained from the energy conservation equation,

$$\frac{3}{2} T(r,t) \left( Ne(r,t) + Ng(r,t) \right) = E_{p}(r,0) + E_{g}(r,0) + E_{c}(r,0) - E_{c}(r,t) - E_{c}(r,t) .$$
(22)

Here,  $E_p(r,0)$ ,  $E_g(r,0)$ , and  $E_c(r,0)$  are the plasma, gas kinetic, and chemical energies at t = 0 for point r, respectively. Ne(r,t) and Ng(r,t) are the electron and total gas particle densities at time t and point r.  $E_c(r,t)$ is the chemical energy at time t and Erad(r,t) is the amount of energy radiated from (or to if Erad < 0) point r at time t. Erad(r,t) is obtained by solving the following equation,

$$\frac{d}{dt} \operatorname{Erad}(r,t) = \sum_{\substack{m,l,z}} \left[ \begin{array}{c} R_{ml}^{z-1}(r,t) - N_{ml}^{z-1}(r,t) \end{array} \right] A_{ml}^{z-1} h v_{ml}$$

+ continuum radiation . (23)

Continuum radiation results from free-free and free-bound (radiative recombination) transitions. In this model radiation from free-free transitions is neglected, uv radiation from all 2-body recombination events is assumed to be optically thick while visible radiation from these events is optically thin. Eqs. (11), (22), and (23) are the essence of the model. The detailed radiative transfer is contained in Eqs. (11) and (23). Eq.(22) insures energy conservation.

#### IV. NUMERICAL RESULTS

Numerical integration of Eqs. (11) and (23) is accomplished by using CHEMEQ, a routine designed to solve stiff ordinary differential equations<sup>19</sup>. Symmetry enables us to carry out the integration over half the grid, i.e. [0,L]. In this section the following initial conditions are assumed: The size of the region is 1 cm, i.e. L = .5 cm. Initial population densities are distributed uniformly across the grid [0,L]. The values are N(1)+N(2)+N(3) = $3.715 \times 10^{19} \text{ cm}^{-3}$ , Ne = N<sup>+</sup>(1)+N<sup>+</sup>(2)+N<sup>+</sup>(3) = 5.0 × 10^{16} \text{ cm}^{-3}. and all others are set to 0.0 (actually,  $1 \times 10^4$  cm<sup>-3</sup>). The specific ground N and  $N^+$  states are populated according to statistical weights. Two initial temperature profiles are assumed. The first is a uniform distribution; Te = 3.0 eV for  $0.0 \le r \le .5$  cm. The second is non-uniform; Te = 3.0 eV for  $0.0 \le r \le .2$  cm and decreases linearly to a value of 1.5 eV at r = .5 cm. Setting the initial population densities and temperatures is equivalent to setting the initial plasma electron, gas kinetic, and chemical energy distributions.

Eqs. (11) and (23) are integrated until an equilibrium is nearly established. During the integration the radiation terms, for example, Eq. (21), are updated using the solutions to the rate equations. Initially this is done every  $10^{-10}$  sec and relaxed to  $10^{-7}$  sec at longer times. Figs. 3a - 10a correspond to the uniform temperature distribution results, while Figs. 3b - 10b are for the nonuniform case.

# A. Rate Equation Results

Figs. 3 and 4 show radiative transfer and cooling as evidenced by the evolution of T(r,t) up to  $t = 10^{-5}$  sec for r = 0.0, 0.25, and 0.5 cm. For both cases the species rapidly approach a local equilibrium while the energy in the system readjusts. This occurs because the initial conditions correspond to a nonequilibrium situation. The initial relaxation takes approximately 10 ns during which time radiative transfer has not begun to play a significant role. For the uniform case cooling is nearly constant

across the grid for 10  $\mu$ sec. The outer boundary does show a lower temperature than the interior, particularly for 5 - 8  $\mu$ sec. This is due to more energy loss. The non-uniform case shows the center cooling more rapidly than the boundary region. Even at 10  $\mu$ sec a temperature gradient remains.

Fig. 5 shows the time evolution of the electron density for both cases. While the electron density was initially constant across the grid for the uniform case the extra energy lost from the boundary lead to a decrease in temperature, mentioned above, which in turn lead to a lower Ne at the edge. By contrast Ne at the boundary for the nonuniform case decreases only slightly from its maximum while the interior values decrease more rapidly, reflecting the behavior of T(r,t).

# B. Energy Loss Results

The time histories of the energy profiles for r = 0.0and 0.5 cm are presented in Figs. 6 and 7. In all cases the amount of chemical energy exceeds the gas kinetic energy which is greater than the plasma electron energy. Figs. 6a and 7a show the extent to which more energy is radiated from the boundary than from the center. Since there was less energy at the grid edge than at the center for the nonuniform case, the opposite situation is seen in Figs. 6b and 7b. In terms of energetics these figures show that the time scale for radiative transfer to contribute significant energy loss is on the order of microseconds. The radiative energy loss values, Erad(r,t), for r = 0.0, 0.25, and 0.5 cm are show in Fig. 8. By 10 µsec these terms have nearly saturated as have the energy values.

Throughout the integration the photon energy that is created, re-absorbed, and radiated from the system is monitored. One quantity of interest is the radiated energy flux for each line,  $Q_{ml}$ , given in units of  $eV-cm^{-2}-sec^{-1}$ . The flux radiating from one side is calculated according to

$$Q_{ml}^{z-1} = \int_{0}^{R} dr \ N_{m}^{z-1}(r,t) \ A_{ml}^{z-1} \ hv_{ml} \left[ 1 - \frac{R_{ml}^{z-1}(r,t)}{N_{m}^{z-1}(r,t)} \right] \quad .$$
 (24)

Table 1 shows the flux values for the major contributing lines as a function of time. The surge in emitted radiation at 1 ns corresponds to the rapid population of exited N and N<sup>+</sup> states during the initial energy redistribution period. Subsequent time behavior shows a slowing down of the cooling rate as radiation energy is lost from the system. Generally, the energy loss is dominated by emissions from the nitrogen uv lines. The N<sup>+</sup> uv lines and N optical lines also contribute to the energy loss, though to a lesser degree; their contribution is not shown. The effect of the N<sup>+</sup> visible lines is negligible. This is consistent with the corresponding temperature values.

### TABLE 1

Time	Transition Line (Å)					Total
	1493.3	1134.6	1199.9	1743.6	1243.3	•
100 ps	7.8×10 <sup>17</sup>	1.0×10 <sup>17</sup>	2.2×10 <sup>17</sup>	3.9×10 <sup>17</sup>	2.3×10 <sup>17</sup>	1.9×10 <sup>18</sup>
l ns	8.0×10 <sup>23</sup>	6.3×10 <sup>23</sup>	5.7×10 <sup>23</sup>	4.6×10 <sup>23</sup>	1.7×10 <sup>23</sup>	2.8×10 <sup>24</sup>
10 ns	4.4×10 <sup>23</sup>	3.6×10 <sup>23</sup>	3.4×10 <sup>23</sup>	2.6×10 <sup>23</sup>	2.1×10 <sup>23</sup>	2.0×10 <sup>24</sup>
100 ns	3.9×10 <sup>23</sup>	3.6×10 <sup>23</sup>	2.9×10 <sup>23</sup>	2.3×10 <sup>23</sup>	2.0×10 <sup>23</sup>	1.9×10 <sup>24</sup>
1 µs	3.4×10 <sup>23</sup>	2.9×10 <sup>23</sup>	2.5×10 <sup>23</sup>	2.0×10 <sup>23</sup>	1.7×10 <sup>23</sup>	1.6×10 <sup>24</sup>
10 µs	9.2×10 <sup>22</sup>	6.7×10 <sup>22</sup>	6.4×10 <sup>22</sup>	6.2×10 <sup>22</sup>	3.5×10 <sup>22</sup>	3.9×10 <sup>23</sup>

Radiated Energy Flux  $(eV-cm^{-2}-sec^{-1})$ 

C. Line Results

It is convenient to define a line-integrated mean intensity,  $\mathbf{J}_{m1}^{z-1},$  as

$$J_{ml}^{z-1}(r,t) = \int_{\Delta v_{ml}} J_{v}^{z-1} \phi_{v} dv . \qquad (25)$$

In terms of the appropriate absorption term and population densities it follows that

$$J_{ml}^{z-1}(r,t) = \frac{2hv_{ml}^{3}}{c^{2}} \frac{R_{ml}^{z-1}(r,t)}{N_{m}^{z-1}(r,t)} \left[ \frac{g_{m}^{z-1} N_{l}^{z-1}(r,t)}{g_{l}^{z-1} N_{m}^{z-1}(r,t)} - 1 \right]^{-1} . (26)$$

Figs. 9 - 10 show the line integrated mean intensities for 2 transition lines (1199.9 Å, and 8211.8 Å) at different times (10 ns, 100 ns, 1 $\mu$ s, and 10 $\mu$ s). The distribution of radiation for these lines is, therefore, monitored as a function of time and space. The results are consistent with the associated temperature profiles. As expected the line intensities for the uniform case show much less variation over the grid than the non-uniform case, particularly at early times. As radiation transfer occurs energy diffuses outward. Fig. 9b, in particular, shows the extent to which the line intensity in the central region decreases compared to the outer region as a function of time.

# D. Discussion

Diffusion and cooling are two aspects of the radiative transfer process. When energy is distributed uniformly across a confined region it is seen that the outer boundary cools more rapidly than the interior, thus establishing a temperature (or energy) gradient which drives subsequent transfer and net cooling. Radiative transfer initiated by the existence of a temperature gradient behaves differently. In this case energy diffuses outward from the outset and the hotter inner region cools more rapidly than the cooler outer region. Using the model described previously the above numerical results for the given set of initial conditions demonstrate that the radiative transfer time is on the order of microseconds. This can be understood within the context of the following simple picture:

If radiative transfer is considered to be a sequence of photon emissions and absorptions it should be possible to estimate bounds on the time required for radiation to diffuse from the center of a region to a boundary. For a specific transition line,  $m \rightarrow 1$ , the diffusion time may be estimated as

$$t_{ml} = \frac{L}{x_{ml}} \frac{1}{A_{ml}}$$
(27)

= 
$$1/A_{ml}^{\star}$$
 (28)

where L is the distance to the boundary (.5 cm in this study) and  $x_{ml}$  is the "mean free path". This definition corresponds to the following picture: After a photon travels a distance  $x_{ml}$  it is absorbed and re-emitted in  $1/A_{ml}$ (seconds). It continues on in this manner until reaching the boundary. In Eq. (28) the effective emission coefficient is defined as  $A_{ml}^{\star} = A_{ml}/\tau_{ml}$  where  $\tau_{ml}$  is the optical depth.

Within the context of our radiative transfer model, the definition of  $x_{ml}$  is not obvious. The simplest choice is to define  $x_{ml}$  as the inverse of the absorption coefficient at line center,  $x_{ml} = 1/\kappa_{ml}$ . This puts the emphasis for radiative transfer on photons that are emitted directly at the center of the frequency profile. The probability that a photon travels this far without being absorbed, as given by Eq. (20), is 0.67. In the simple diffusion picture it is assumed that the photon is then absorbed. This gives an upper bound on the diffusion time scale. For comparison,  $x_{ml}$  is defined as the distance at which  $\Gamma_{ml}(\rho) = 0.05$ . In this manner absorption is guaranteed after the photon has

travelled  $x_{ml} = 177.8/\kappa_{ml}$ . The later definition places more emphasis for radiative transfer on photons emitted from the line wings since these are the photons that contribute to the asymptotic behavior of  $T_{ml}(\rho)$ . This gives a lower bound for the onset of radiative transfer.

Table 2 shows a comparison of these diffusion times for the top 12 lines contributing to radiation, as determined by  $Q_{ml}$  at t = 10 ns. The diffusion time using  $x_{ml} = 1/\kappa_{ml}$  is denoted as  $t_{ml}^1$  and  $t_{ml}^{wing}$  is the estimate for the larger value of  $x_{ml}$ . These estimates are in fact consistent with the results presented in Figs. 3 - 10.

# TABLE 2

Diffusion Time Estimates (sec)						
Wavelength (Å)	$\kappa_{1m}^{r=0}(cm^{-1})$	t <sup>l</sup> ml	t <sup>wing</sup> ml			
1402 2	7 2.103	6 610-6	2 7.10-8			
1493.3	7.3×10	0.0×10	3.7×10			
1134.6	4.6×10 <sup>-</sup>	4.3×10 -	2.4×10			
1199.9	2.3×10 <sup>4</sup>	4.9×10 <sup>-5</sup>	$2.8 \times 10^{-7}$			
1743.6	2.2×10 <sup>3</sup>	5.5×10 <sup>-6</sup>	3.1×10 <sup>-8</sup>			
1243.3	7.7×10 <sup>3</sup>	8.4×10 <sup>-6</sup>	4.7×10 <sup>-8</sup>			
1085.1	7.5×10 <sup>3</sup>	6.6×10 <sup>-6</sup>	3.7×10 <sup>-8</sup>			
1411.9	4.9×10 <sup>2</sup>	4.9×10 <sup>-6</sup>	2.7×10 <sup>-8</sup>			
8617.5	7.0×10 <sup>1</sup>	$1.2 \times 10^{-6}$	6.6×10 <sup>-9</sup>			
916.3	9.3×10 <sup>3</sup>	2.6×10 <sup>-6</sup>	1.5×10 <sup>-8</sup>			
8617.5	1.6×10 <sup>1</sup>	$2.6 \times 10^{-7}$	1.5×10 <sup>-9</sup>			
7452.2	1.3×10 <sup>1</sup>	$2.1 \times 10^{-7}$	1.2×10 <sup>-9</sup>			
9395.3	2.3×10 <sup>1</sup>	5.7×10 <sup>-7</sup>	3.2×10 <sup>-9</sup>			

# V. CONCLUDING REMARKS

A radiative tranport model has been developed which emphasizes the transfer of line radiation in a hot nitrogen plasma. The radiative transfer equations are solved selfconsistently with the corresponding time-dependent chemistry equations. This approach allows for the transfer of many lines and does not require a state of LTE to exist. Numerical results for two simple test cases show the utility of the model in describing radiative transfer effects. A following report will present the results of using this model to account for radiation transport in the realistic description of a plasma generated by an intense electron beam.





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Fig. 2  $T(x=\kappa_{ml}\rho)$ . Exact integration is solid line. Eq. (19) is dashed line. Eq. (20) is dotted line.











1.11.12





51. S



Same as Fig. 9 for 8211.8 Å. 10 Fig.

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