

MICROCOPY RESOLUTION TEST CHART  
NATIONAL BUREAU OF STANDARDS 1963-A

3

MISCELLANEOUS PAPER SL-86-6



US Army Corps of Engineers

# STUDY OF STORED ENERGY SYSTEMS PROPOSED FOR TESTING A PRESSURE-REGULATING VALVE

by

James B. Cheek

Structures Laboratory

DEPARTMENT OF THE ARMY  
Waterways Experiment Station, Corps of Engineers  
PO Box 631, Vicksburg, Mississippi 39180-0631



AD-A170 390

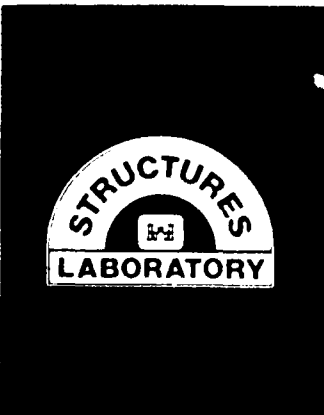
DTIC  
SELECTED  
JUL 31 1986  
S D



July 1986  
Final Report

Approved For Public Release Distribution Unlimited

DTIC FILE COPY



Defense Nuclear Agency  
Washington, DC 20305  
Work Unit 31588

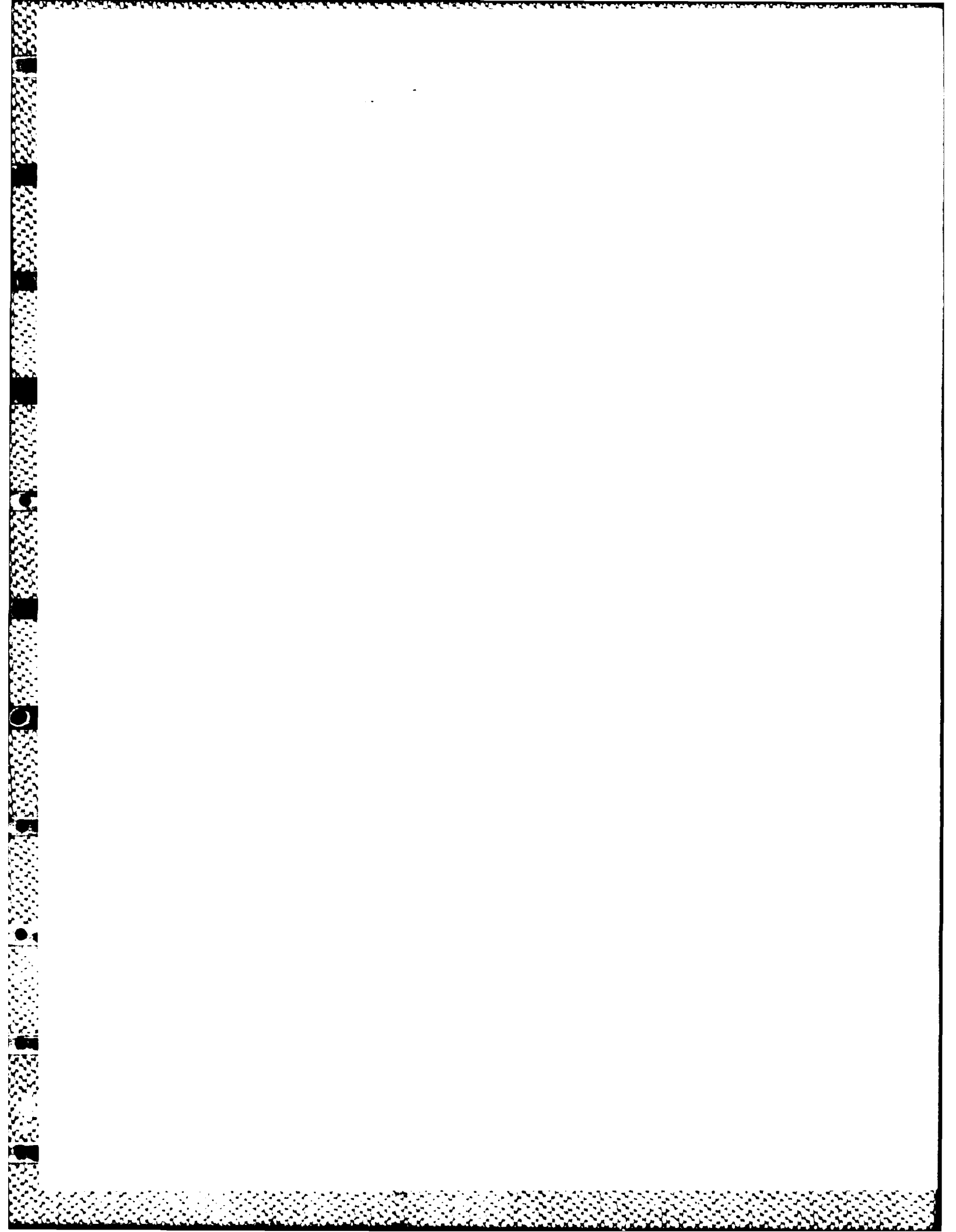
6 7 29

102

AD-A170390

SECURITY CLASSIFICATION OF THIS PAGE

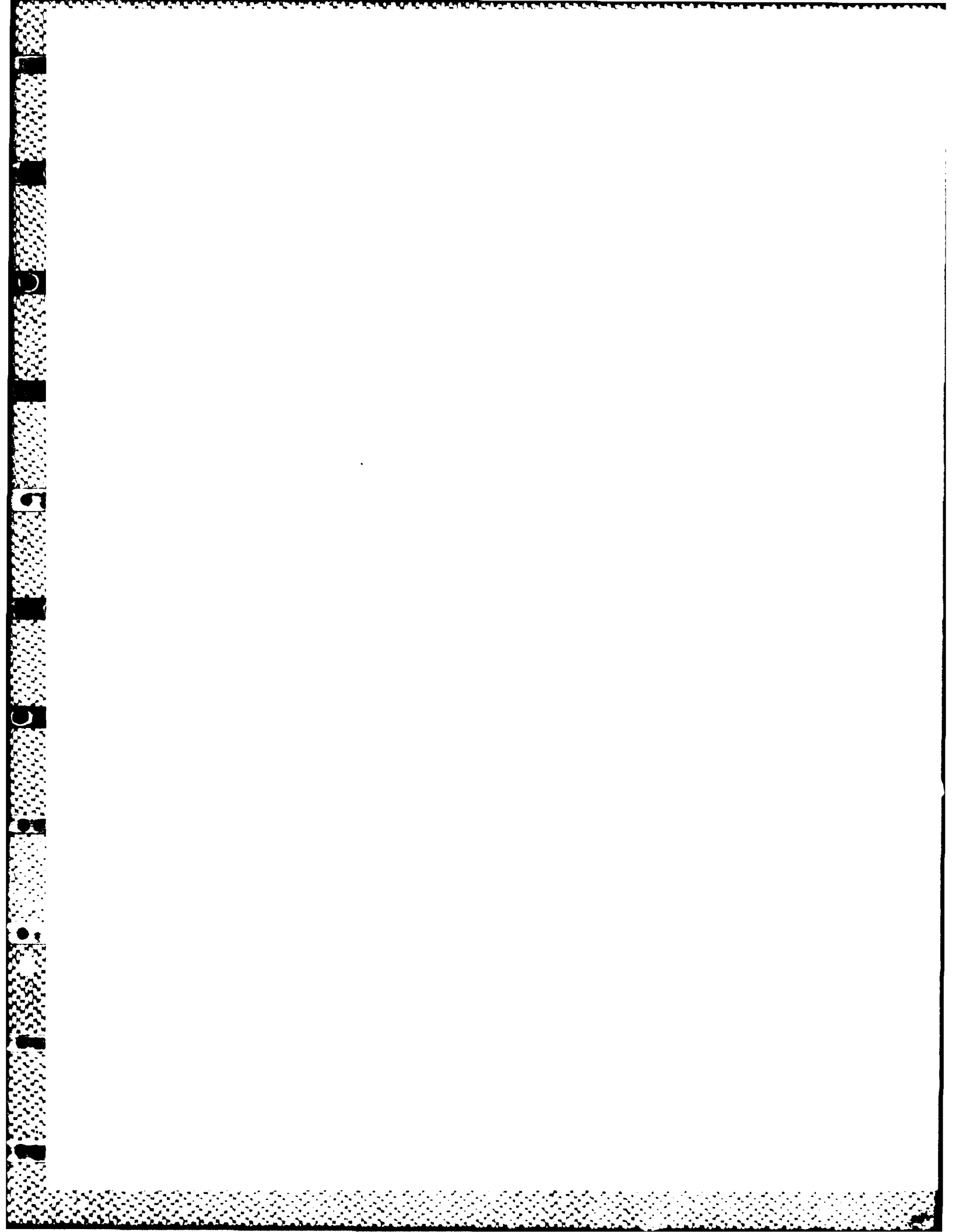
REPORT DOCUMENTATION PAGE				Form Approved OMB No 0704-0188 Exp Date Jun 30, 1986	
1a REPORT SECURITY CLASSIFICATION Unclassified		1b RESTRICTIVE MARKINGS			
2a SECURITY CLASSIFICATION AUTHORITY		3 DISTRIBUTION/AVAILABILITY OF REPORT			
2b DECLASSIFICATION/DOWNGRADING SCHEDULE		Approved for public release; distribution unlimited.			
4 PERFORMING ORGANIZATION REPORT NUMBER(S) Miscellaneous Paper SL-86-6		5 MONITORING ORGANIZATION REPORT NUMBER(S)			
6a. NAME OF PERFORMING ORGANIZATION USAEWES Structures Laboratory		6b. OFFICE SYMBOL (if applicable)	7a. NAME OF MONITORING ORGANIZATION		
6c. ADDRESS (City, State, and ZIP Code) PO Box 631 Vicksburg, MS 39180-0631		7b. ADDRESS (City, State, and ZIP Code)			
8a. NAME OF FUNDING/SPONSORING ORGANIZATION Defense Nuclear Agency		8b. OFFICE SYMBOL (if applicable)	9 PROCUREMENT INSTRUMENT IDENTIFICATION NUMBER		
8c. ADDRESS (City, State, and ZIP Code) Washington, DC 20305		10. SOURCE OF FUNDING NUMBERS			
		PROGRAM ELEMENT NO.	PROJECT NO	TASK NO	WORK UNIT ACCESSION NO 31588
11 TITLE (Include Security Classification) Study of Stored Energy Systems Proposed for Testing a Pressure-Regulating Valve					
12 PERSONAL AUTHOR(S) Cheek, James B.					
13a. TYPE OF REPORT Final report		13b. TIME COVERED FROM _____ TO _____	14 DATE OF REPORT (Year, Month, Day) July 1986		15 PAGE COUNT 48
16 SUPPLEMENTARY NOTATION Available from National Technical Information Service, 5285 Port Royal Road, Springfield, VA 22161.					
17. COSATI CODES		18. SUBJECT TERMS (Continue on reverse if necessary and identify by block number)			
FIELD	GROUP	SUB-GROUP	Drop testing Pumping		
			Dynamic analysis, rotational Shock isolation systems		
			Pressure-regulating valve Stored mechanical energy		
19 ABSTRACT (Continue on reverse if necessary and identify by block number) <p>Two systems using stored mechanical energy, rotational and translational (drop), were proposed for use in testing a high discharge, high-pressure-regulating valve. A computer-based dynamic analysis of those systems indicates the drop test system to be less costly, but near the practical limits of drop height and weight. The rotational system will exercise the valve for one-half of a pump cycle provided the pump begins at the start of a pump output cycle. The rotational system must be able to withstand very large forces. Neither system exercises the valve for enough time, but the rotational system appears to be capable of longer testing time.</p>					
20 DISTRIBUTION/AVAILABILITY OF ABSTRACT <input checked="" type="checkbox"/> UNCLASSIFIED/UNLIMITED <input type="checkbox"/> SAME AS RPT <input type="checkbox"/> DTIC USERS			21 ABSTRACT SECURITY CLASSIFICATION Unclassified		
22a NAME OF RESPONSIBLE INDIVIDUAL			22b TELEPHONE (Include Area Code)		22c OFFICE SYMBOL



CONVERSION FACTORS, NON-SI TO SI (METRIC)  
UNITS OF MEASUREMENT

Non-SI units of measurement used in this report can be converted to SI  
(metric) units as follows:

<u>Multiply</u>	<u>By</u>	<u>To Obtain</u>
degrees (angle)	0.01745329	radians
feet	0.3048	metres
foot-pounds (force)	1.355818	joules
gallons (US liquid)	3.785412	cubic decimetres
inches	2.54	centimetres
pounds (force) per square inch	6.894757	kilopascals
pounds (mass)	0.4535924	kilograms



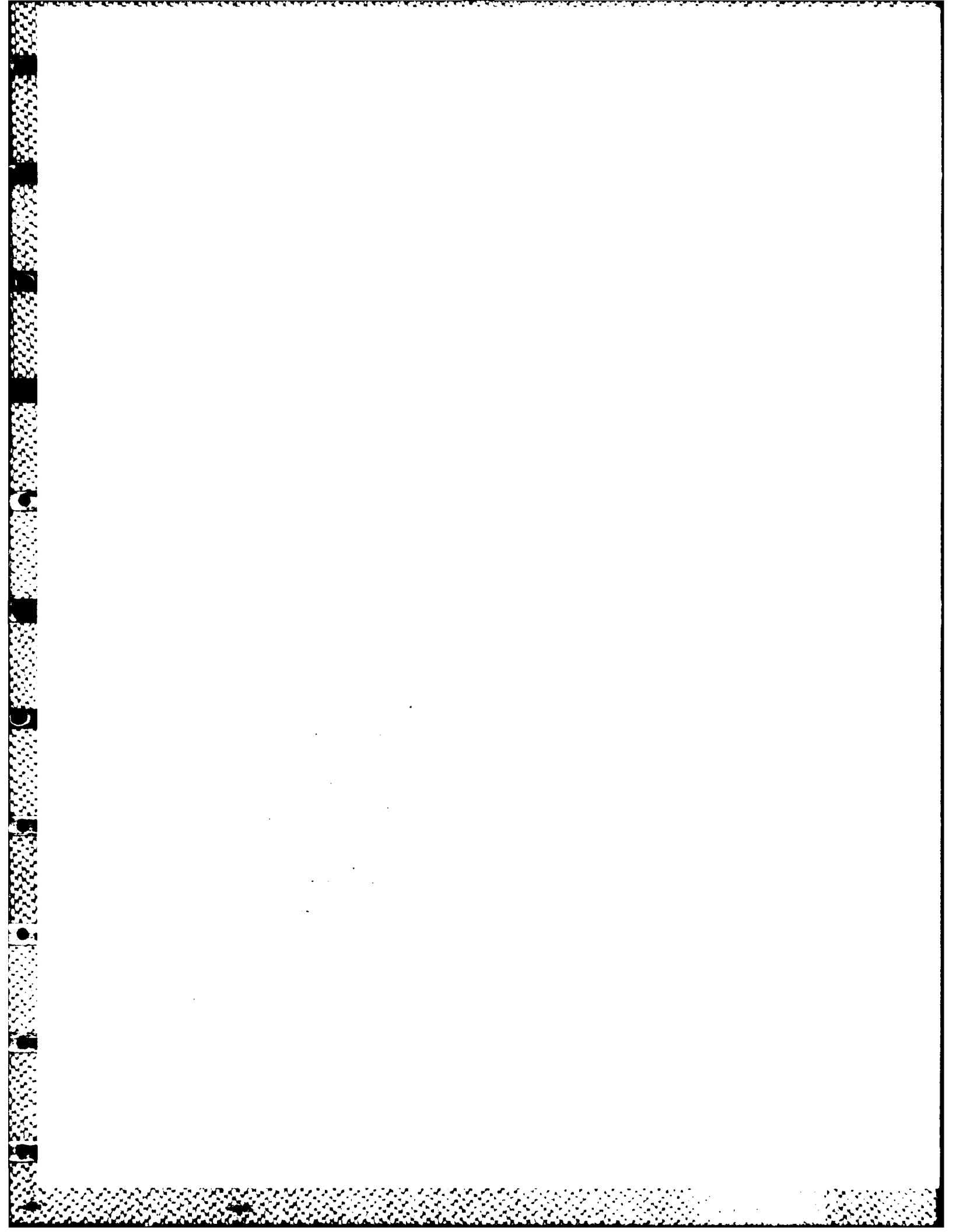
## SUMMARY

Two valve test systems were studied. They each use a stored energy approach; one is rotational, the other is translational (drop). An idealized dynamic analysis indicates the rotational system will generate peak forces and torques that will require a massive test fixture. The test fixture needs a thorough design and dynamic analysis to assure it will operate under such severe dynamic forces.

The drop test will almost equal the performance of the rotational system. It also appears to be less costly. However, it is near the practical limits of ball weight, drop height and available reaction structure.

Neither system produces the design discharge for enough time to evaluate the regulating valve's performance. Precise timing of the start of pumping in the rotational test is critical to attaining the desired discharges.





PREFACE

This study was conducted in January 1986, by personnel of the US Army Engineer Waterways Experiment Station (WES), under the sponsorship of the Defense Nuclear Agency (DNA) in support of the Silo Test Program-Shock Isolation Systems. The DNA project officer was Mr. James Cooper. Mr. Larry Selzer, Aerospace Corporation, proposed the concept as a means of evaluating a valve for a full-scale shock isolation system.

The investigation was conducted under the supervision of Messrs. Bryant Mather, Chief, Structures Laboratory (SL); James T. Ballard, Assistant Chief, SL; Dr. Jimmy P. Balsara, Chief, Structural Mechanics Division (SMD), SL; and Mr. Robert E. Walker, Project Manager, SMD. This report was prepared by Mr. James B. Cheek, SMD.

The Director of WES during the investigation and preparation of this report was COL Allen F. Grum. The Technical Director was Dr. Robert W. Whalin.

Accession For	
NTIS CRA&I	<input checked="" type="checkbox"/>
DTIC TAB	<input type="checkbox"/>
Unannounced	<input type="checkbox"/>
Justification	
By	
Distribution/	
Availability Codes	
Dist	Avail and/or Special
A-1	



## CONTENTS

	<u>Page</u>
SUMMARY.....	1
PREFACE.....	2
PART I: INTRODUCTION.....	4
PART II: IDEALIZED ANALYSIS, ROTATIONAL.....	4
Valve Specification.....	4
Test Fixture Data.....	4
Dynamic Analysis.....	5
PART III: IDEALIZED ANALYSIS, DROP TEST.....	6
Drop Test System.....	6
Dynamic Analysis, Drop.....	7
PART IV: CONCLUSIONS.....	8
APPENDIX A: ROTATIONAL TEST RESULTS.....	A1
APPENDIX B: ROTATIONAL TEST RESULTS, PUMP START AT ZERO DEGREES.....	B1
APPENDIX C: ROTATIONAL SYSTEM PROGRAM "JPUMP".....	C1
APPENDIX D: METHOD FOR CALCULATING SLOWDOWN OF FLYWHEEL.....	D1
Initial Conditions.....	D1
Calculating Procedure for Flywheel Slowdown.....	D2
Calculating Moment Applied to the Crankshaft.....	D3
APPENDIX E: ANALYSIS OF THE DROP TEST SYSTEM.....	E1
Output of the Drop Test Analysis Program "JPEND".....	E2
Listing of the Drop Test Analysis Program "JPEND".....	E3
Equation for Drop Height.....	E4
Equation for Total Discharge Time.....	E5

STUDY OF STORED ENERGY SYSTEMS  
PROPOSED FOR TESTING  
A PRESSURE REGULATING VALVE

PART I: INTRODUCTION

1. The analysis documented in this report was accomplished as part of a feasibility study to develop design requirements for a device proposed for testing a hydraulic pressure regulating valve. Because of the valve's high operating pressure and discharge, designing the test device presents many difficult analysis problems. This study looks at but one of those problems in a highly idealized fashion. Nevertheless, the analysis is useful in that it establishes the best performance attainable from a "perfect" system. That performance can be used to see how well it meets test system requirements. From that evaluation, decisions on any changes needed to a practical system can be made and more extensive engineering analysis can be conducted.

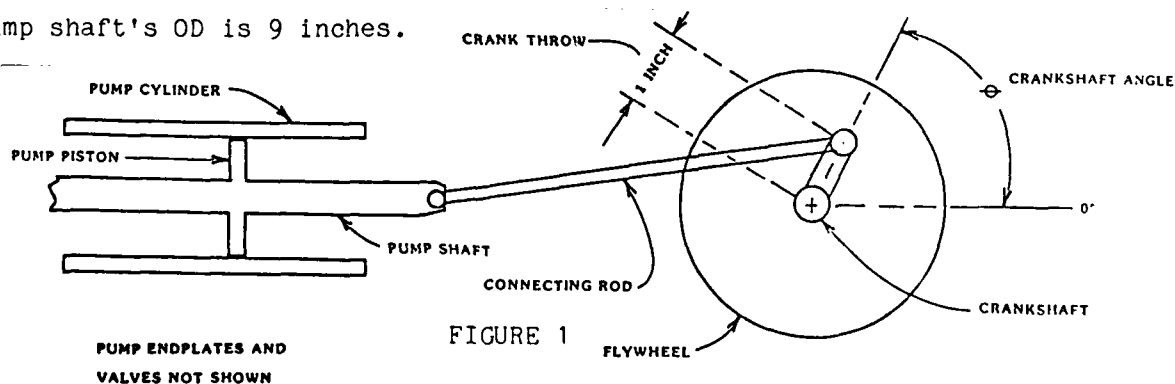
PART II: IDEALIZED ANALYSIS, ROTATIONAL

Valve Specification

2. The following analysis was done on a fixture proposed to test a regulating valve at a constant regulating pressure of 4,350 pounds per square inch (psi), at a design maximum flow of 26.4 gallons per second (gps).

Test Fixture Data

3. The Test Fixture consists of two, 30 inch diameter, solid disc flywheels weighting 1,000 pounds (lb). Each is connected to a crankshaft having a one-inch offset (throw) which is in turn linked by a connecting rod to a pump as shown in Figure 1 below. The pump cylinder's ID is 16 inches and the pump shaft's OD is 9 inches.



## Dynamic Analysis

4. The analysis is based on a perfect system (no mechanical or pumping loss). The results, presented in Appendix A, indicate the following:

- a. At 424 revolutions per minute (rpm), the pump will discharge 26.4 gpm, peak, provided the pumping starts when the crankshaft angle is 90°. The discharge will decline, as shown in Figure A2, to zero in 71 milliseconds (msec).
- b. Peak torque in the drive is near 50,000 foot-pounds (ft-lbs) (see Figures A1 and A3).
- c. The drive will slow from 424 rpm to zero rpm in 70° of crank rotation which is  $70.8^\circ/360^\circ = .197$  revolutions.
- d. The force required to operate the pump shaft is almost 600,000 lb at design pressure.
- e. Operating the system at 577 rpm and starting the test at zero degrees crankshaft angle produces the desired peak discharge and increases the time of regulated discharge (See Figure B7).

5. Appendix B, like Appendix A, graphs the test fixture performance. However, pumping starts at a crank angle of zero degrees. Peak pump output is only 16 gpm using 424 rpm as above (see Figures B1 and B2).

6. A second series of calculations was made keeping all conditions the same except the shaft speed which was changed to 577 rpm in order to raise the peak pump discharge to near the design specification (26.4 gpm). The results of those calculations are presented on Figures B7 through B12.

7. Those calculations indicate a longer discharge time at a higher discharge. However, the total discharge time of a single cycle system such as this is unlikely to be long enough to thoroughly exercise the test valve.

8. The computer program used for the rotational system analysis is presented in Appendix C.

9. Appendix D presents the calculations upon which the dynamic analysis is based. It also outlines the program logic used in modeling the slowdown of the drive system.

PART III. IDEALIZED ANALYSIS, DROP TEST

Drop Test System

10. For comparison purposes, a swinging ball test fixture was evaluated. The system consisted of a ball suspended by a sling from a fixed point. When directly below the suspension point, the ball will impact the piston of a hydraulic cylinder connected to the regulating valve. Energy is stored in the ball by raising it to height H as shown in Figure 2.

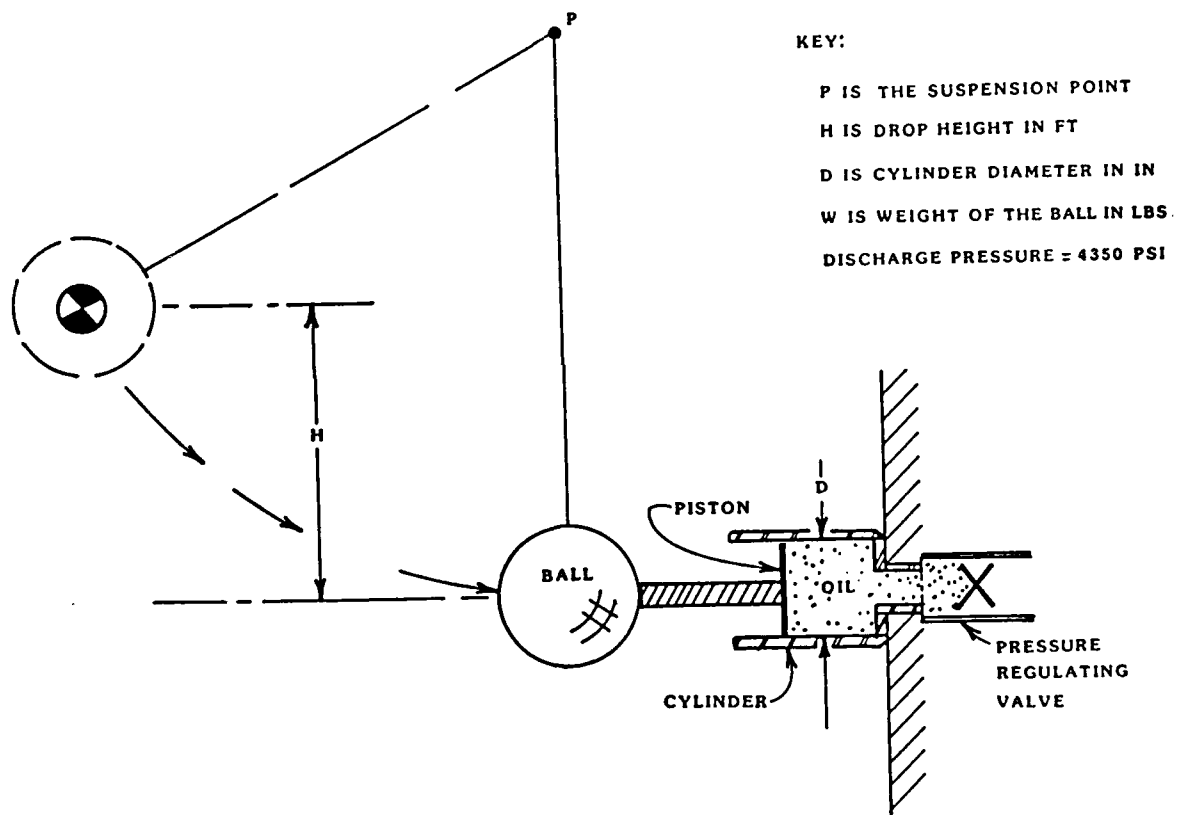


FIGURE 2

## Dynamic Analysis, Drop

11. The dynamic analysis calculations and the computer program, shown in Appendix E, are based on total transfer of momentum from the ball to the pump system, ie., the ball does not rebound. The results show the following:

- a. The drop height controls the peak flow rate. Consequently, for a given cylinder diameter, H is fixed in order to attain the valve's design flow.
- b. For a given cylinder diameter (thus drop height) increasing the weight of the ball increases the discharge time of the cylinder.
- c. A 3.5 inch diameter cylinder, a 43.1 foot drop height, and a 2,000 lb ball will produce the design peak flow followed by a linear decline to zero flow for 78 msec.
- d. Figure 3 is a composite plot showing the discharge versus time graphs of the best rotational test (from Figure B8) and the best drop test. This plot clearly shows the superior performance of the rotational system.
- e. Time-discharge graphs of other cylinder diameters and ball weights are shown in Figure E2.

```
PROGRAM ROSSCOBRA/JPLWP -- JAY CHEEK, SHD. SL. DES. 16 JAN 1986
PISTON DIAMETER = 16.00 IN
SHAFT DIAMETER = 8.00 IN
PUMP PRESSURE = 4350.00 PSI
FLYWHEEL DIAMETER = 30.00 IN
FLYWHEEL WEIGHT = 2000.00 LB
CRANK THROW = 1.00 IN
CONNECTING ROD LENGTH = 30.00 IN
INITIAL RPM = 577.00
CRANK ANGLE AT START = 0. DEG
```

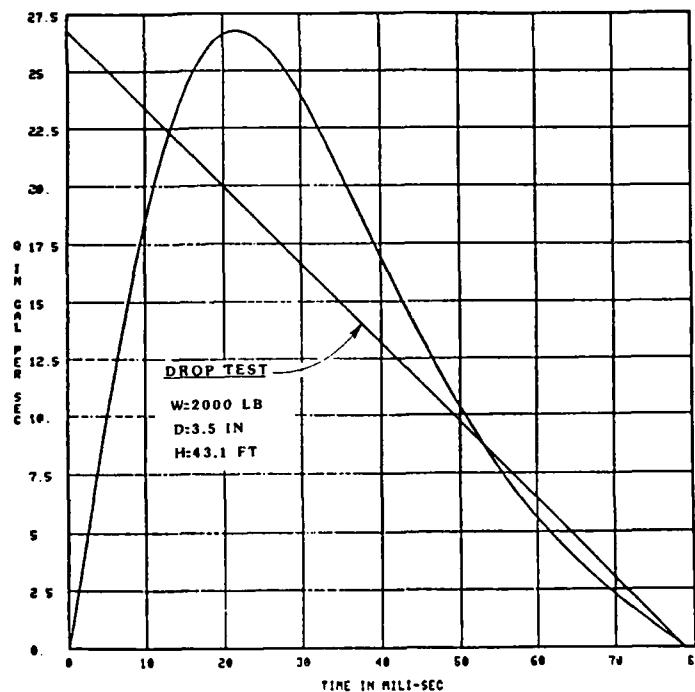


FIGURE 3

#### PART IV: CONCLUSIONS

12. The following conclusions are based on the idealized analysis of the two systems.

- a. Provided the initial rpm of the rotational test is increased from 424 to 577, the Drop Test will do an inferior job of exercising the regulating valve because of the Drop Test's linear decline in discharge. However, the drop test will cost less.
- b. The drop test is near the practical limits of ball weight and drop height. Going beyond the design discharge requires a four fold increase in drop height to double the peak discharge. Changing to a larger cylinder diameter increases discharge directly with the square of D, but decreases flow time with  $D^4$ .
- c. The very short test time of the rotating system produces extremely large forces in the bearings as well as other parts of the mechanism.
- d. The ability to increase rpm allows the rotational system to test at high discharges, provided the fixture can handle the peak forces. Consequently, it is more flexible.
- e. Precise timing for the start of the test is critical to getting meaningful results.
- f. Neither system provides enough time at high discharge to thoroughly test the regulator performance.



## APPENDIX A: ROTATIONAL TEST RESULTS

1. The figures presented in this appendix show the rotational testing system's performance at the design shaft speed of 424 rpm. Other analysis (not presented) showed that the design discharge (26.4 gpm) would be attained only when pumping action starts at a shaft angle of ninety degrees. This analysis shows the system's performance under those conditions.

2. Figure A1 provides a tabulation of various system parameters versus time. Figures A2 through A6 are plots of those same parameters versus time.

TEST START ANGLE, RPM =?

=90 424

N	T(SEC)	THETA	RPM	KE (FT-LB)	Q (GAL/SEC)	TORQ (FT-LB)
0	0.	90.00	424.0	47833.	26.49	-49824.
100	0.0044	100.71	380.6	38539.	23.51	-49259.
200	0.0089	110.28	338.3	30454.	20.06	-47276.
300	0.0133	118.74	298.2	23661.	16.60	-44384.
400	0.0178	126.18	260.9	18106.	13.42	-41007.
500	0.0222	132.66	226.6	13658.	10.65	-37467.
600	0.0266	138.27	195.3	10153.	8.33	-33988.
700	0.0311	143.09	167.1	7427.	6.43	-30721.
800	0.0355	147.19	141.5	5330.	4.92	-27754.
900	0.0400	150.64	118.4	3733.	3.74	-25134.
1000	0.0444	153.51	97.5	2529.	2.80	-22883.
1100	0.0488	155.85	78.3	1633.	2.07	-21004.
1200	0.0533	157.70	60.7	979.	1.48	-19492.
1300	0.0577	159.09	44.2	519.	1.01	-18338.
1400	0.0622	160.05	28.5	216.	0.63	-17531.
1500	0.0666	160.61	13.4	48.	0.29	-17064.

PUMPING ENDS AT 0.071 SEC.

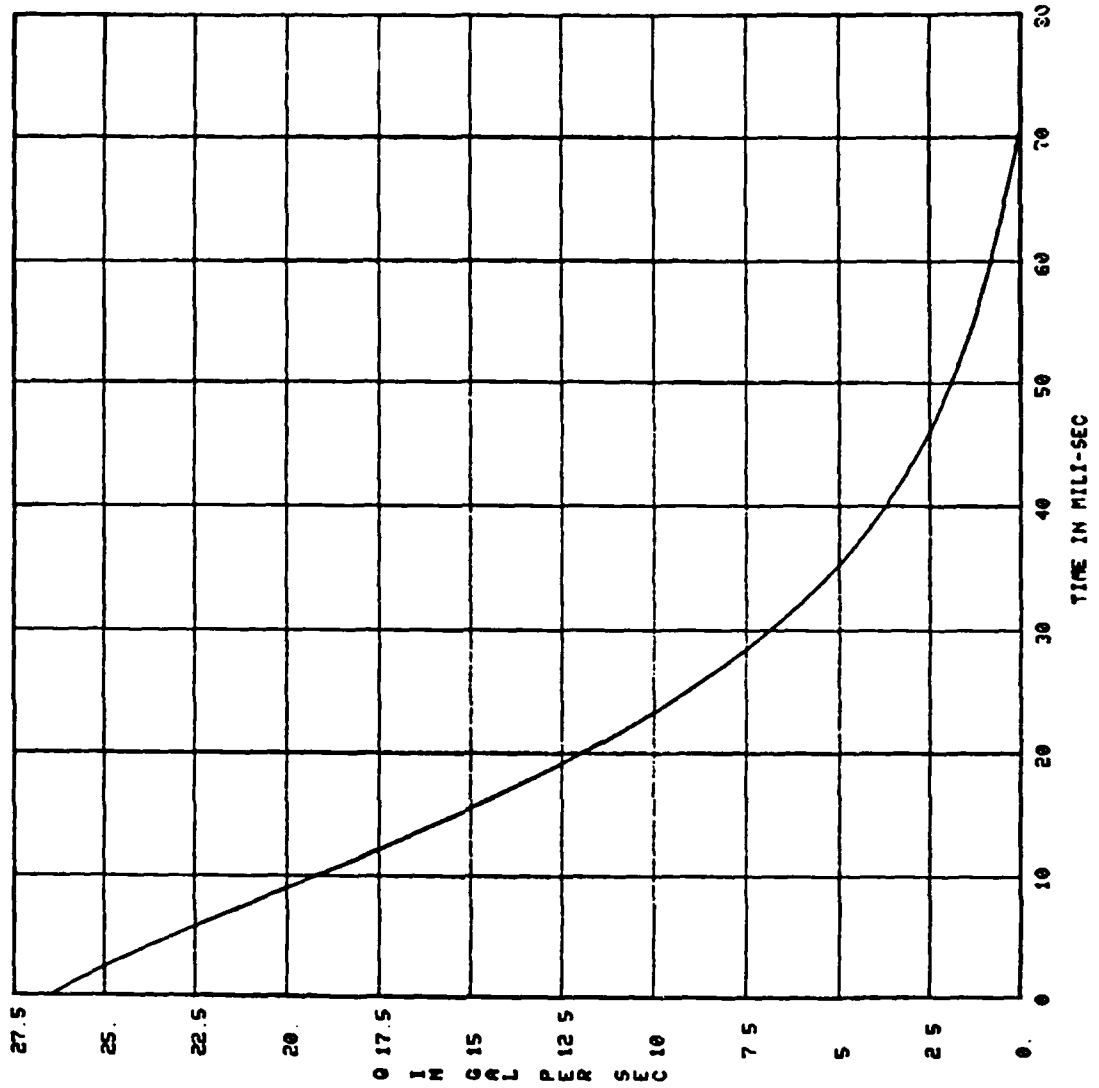
PUMP CUTOUT ANGLE = 70.8 DEGREES

NUMBER OF TIME STEPS = 1591

FIGURE A1

PROGRAM ROSSCOBRA/JUMP -- JAY CHEEK, SHD, SL, WES, 16 JAN 1986

PISTON DIAMETER = 16.00 IN  
 SHAFT DIAMETER = 9.00 IN  
 PUMP PRESSURE = 4350.00 PSI  
 FLYWHEEL DIAMETER = 30.00 IN  
 FLYWHEEL WEIGHT = 2000.00 LB  
 CRANK THROU = 1.00 IN  
 CONNECTING ROD LENGTH = 30.00 IN  
 INITIAL RPM = 424.00  
 CRANK ANGLE AT START = 90.00 DEG



0 17.5  
 I H  
 G 15  
 A L  
 P 12.5  
 R  
 S 10  
 C  
 7.5  
 5  
 2.5  
 0

FIGURE A2

PROGRAM ROSSOBRA/JUMP -- JAY CREEK. SMD. SL. UES. 16 JAN 1986

PISTON DIAMETER = 16.00 IN  
 SHAFT DIAMETER = 9.00 IN  
 PUMP PRESSURE = 4350.00 PSI  
 FLYWHEEL DIAMETER = 30.00 IN  
 FLYWHEEL WEIGHT = 2000.00 LB  
 CRANK THROW = 1.00 IN  
 CONNECTING ROD LENGTH = 30.00 IN  
 INITIAL RPM = 424.00  
 CRANK ANGLE AT START = 90.00 DEG

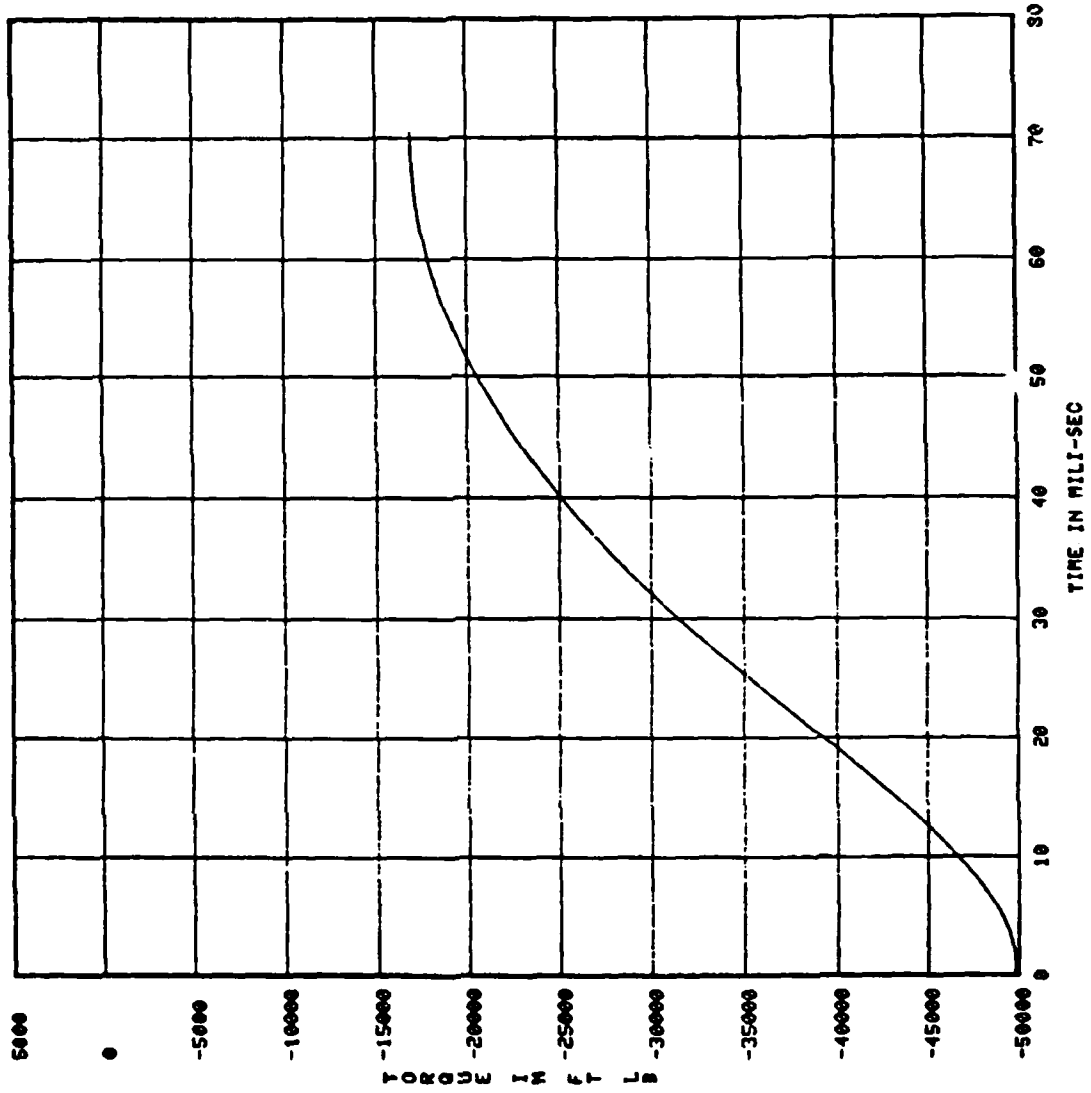


FIGURE A3

PROGRAM ROSSCORRA/JPLUMP -- JAY CHEIK. SHD. SL. LES. 16 JAN 1988

PISTON DIAMETER . 16.00 IN  
 SHAFT DIAMETER . 9.00 IN  
 PUMP PRESSURE . 4350.00 PSI  
 FLYWHEEL DIAMETER . 30.00 IN  
 FLYWHEEL WEIGHT . 2000.00 LB  
 CRANK THROU . 1.00 IN  
 CONNECTING ROD LENGTH . 30.00 IN  
 INITIAL RPM . 424.00  
 CRANK ANGLE AT START . 90.00 DEG

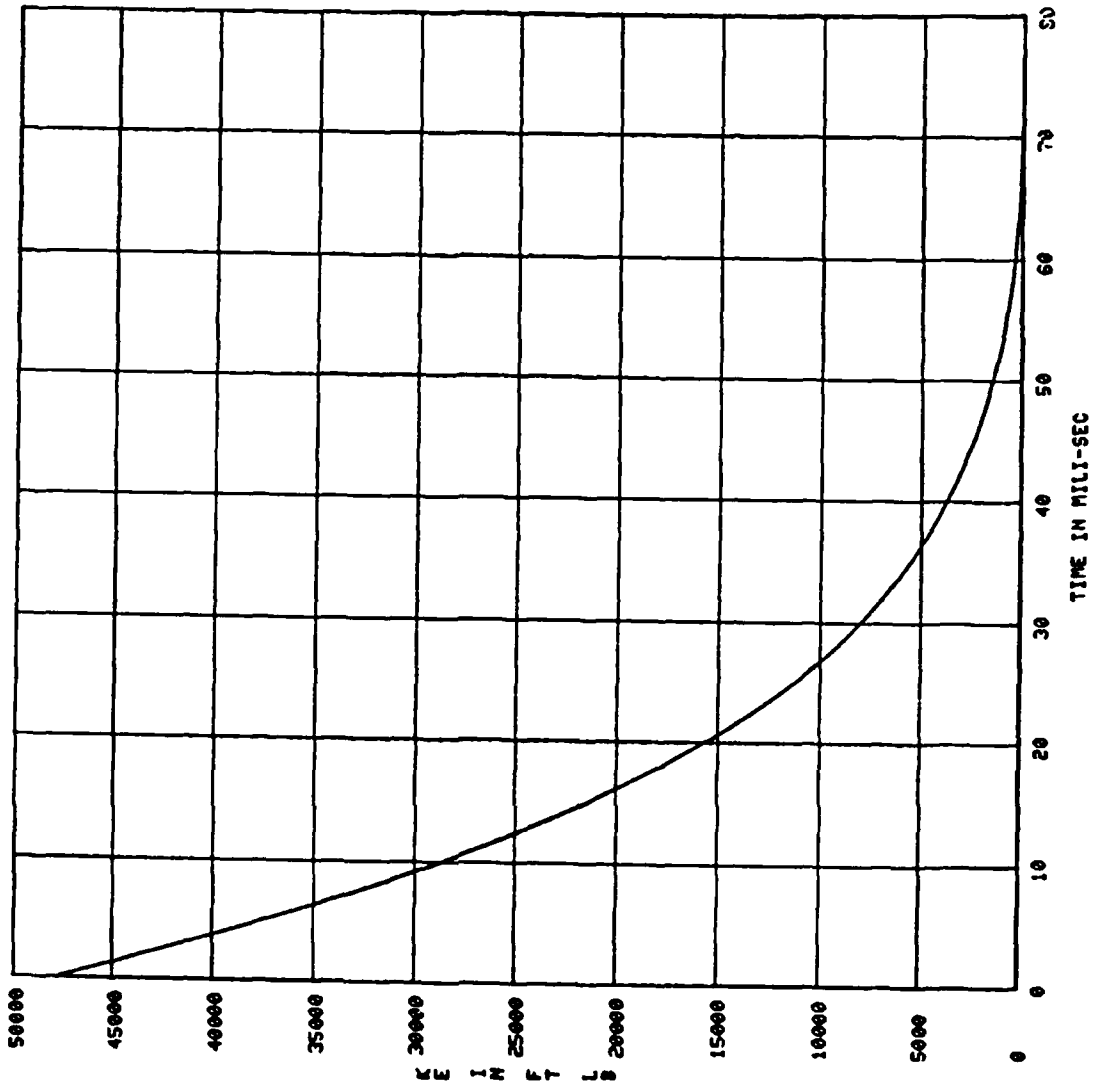


FIGURE A4

PROGRAM ROSSCORRA/JUMP -- JAY CHEEK. SHD. SL. LES. 16 JAN 1986

PISTON DIAMETER \* 16.00 IN  
SHAFT DIAMETER \* 9.00 IN  
PUMP PRESSURE \* 4360.00 PSI  
FLYWHEEL DIAMETER \* 30.00 IN  
FLYWHEEL WEIGHT \* 2000.00 LB  
CRANK THROW \* 1.00 IN  
CONNECTING ROD LENGTH \* 30.00 IN  
INITIAL RPM \* 424.00  
CRANK ANGLE AT START \* 90.00 DEG

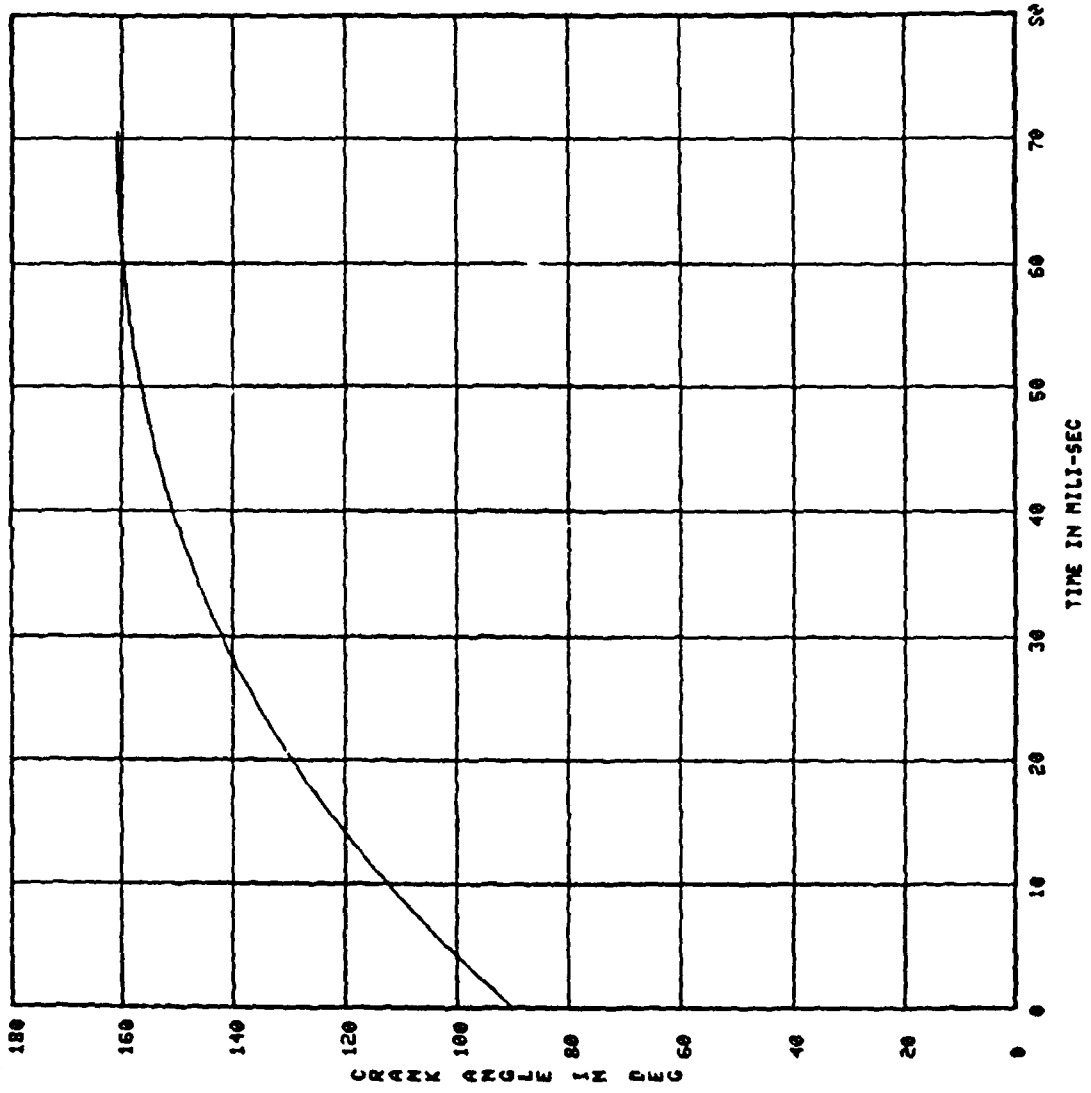


FIGURE A5

PROGRAM ROSSCORRA/JPLUMP -- JAY CHEEK. STD. SL. UES. 16 JAN 1988

PISTON DIAMETER - 16.00 IN  
SHAFT DIAMETER - 9.00 IN  
PUMP PRESSURE - 4350.00 PSI  
FLYWHEEL DIAMETER - 30.00 IN  
FLYWHEEL WEIGHT - 2000.00 LB  
CRANK THROU - 1.00 IN  
CONNECTING ROD LENGTH - 30.00 IN  
INITIAL RPM - 424.00  
CRANK ANGLE AT START - 90.00 DEG

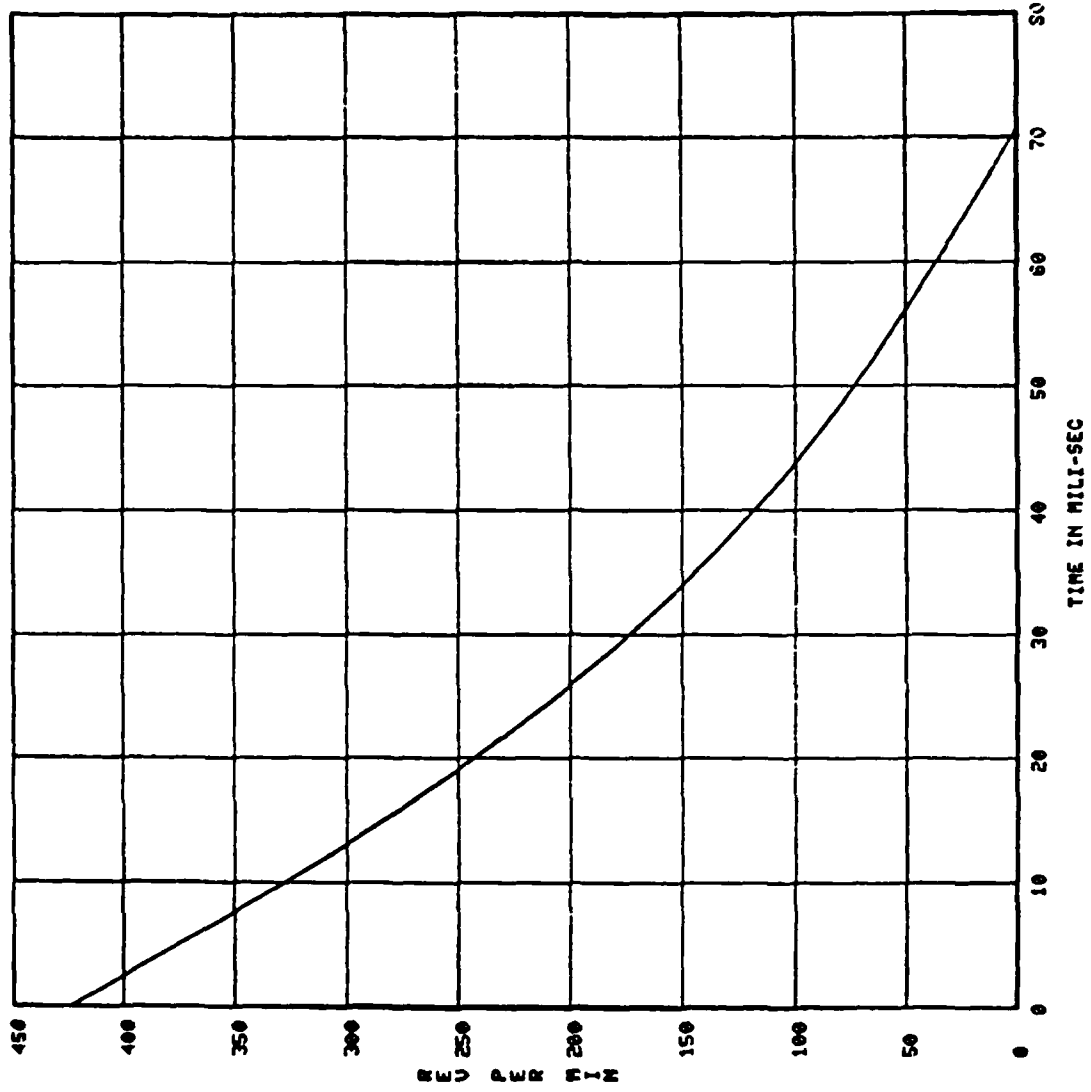


FIGURE A6

## APPENDIX B: ROTATIONAL TEST RESULTS, PUMP START AT ZERO DEGREES

1. The figures presented in this appendix show the rotational testing system's performance at two shaft speeds. Other analysis (not presented) shows that the design discharge (26.4 gpm) would be attained at the design rpm (424) only when pumping action started at a shaft angle of ninety degrees. However, at that point the piston and fluid are moving at the maximum velocity making pump starting very difficult under those conditions. This analysis shows two sets of results for starting the test at zero degrees.

2. Figure B1 provides a tabulation of various system parameters versus time. That output shows the peak discharge reduced to about 16 gpm when the shaft speed at pump start is 424 rpm. Figures B2 through B6 show plots of discharge and other system parameters versus time for the 424 rpm test.

3. Figures B7 and B8 show the peak system discharge to be at the design discharge when the shaft speed at pump start is increased to 577 rpm. Figures B9 through B12 show other system parameters versus time at 577 rpm.



TEST START ANGLE, RPM =?

=0 424

N	T (SEC)	THETA	RPM	KE (FT-LB)	Q (GAL/SEC)	TORQ (FT-LB)
0	0.	0.	424.0	47833.	0.03	0.
100	0.0044	11.26	419.9	46914.	4.93	-9410.
200	0.0089	22.30	407.8	44243.	9.35	-18323.
300	0.0133	32.92	388.2	40103.	12.79	-26317.
400	0.0178	42.92	362.2	34907.	15.02	-33101.
500	0.0222	52.16	330.8	29121.	15.98	-38542.
600	0.0266	60.50	295.3	23199.	15.78	-42654.
700	0.0311	67.86	256.7	17529.	14.66	-45569.
800	0.0355	74.15	216.0	12409.	12.85	-47493.
900	0.0400	79.34	173.9	8047.	10.61	-48662.
1000	0.0444	83.40	131.1	4572.	8.10	-49304.
1100	0.0488	86.31	87.9	2053.	5.46	-49614.
1200	0.0533	88.07	44.4	525.	2.77	-49739.
1300	0.0577	88.66	1.0	0.	0.06	-49771.

PUMPING ENDS AT 0.058 SEC.

PUMP CUTOUT ANGLE = 88.7 DEGREES

NUMBER OF TIME STEPS = 1303

FIGURE B1

PROGRAM ROSSOBRA-JPUMP -- JAY CHEEK. STD. SL. UES. 16 JAN 1986

PISTON DIAMETER = 16.00 IN  
 SHAFT DIAMETER = 9.00 IN  
 PUMP PRESSURE = 4350.00 PSI  
 FLYWHEEL DIAMETER = 30.00 IN  
 FLYWHEEL WEIGHT = 2000.00 LB  
 CRANK THROU = 1.00 IN  
 CONNECTING ROD LENGTH = 30.00 IN  
 INITIAL RPM = 424.00  
 CRANK ANGLE AT START = 0 DEG

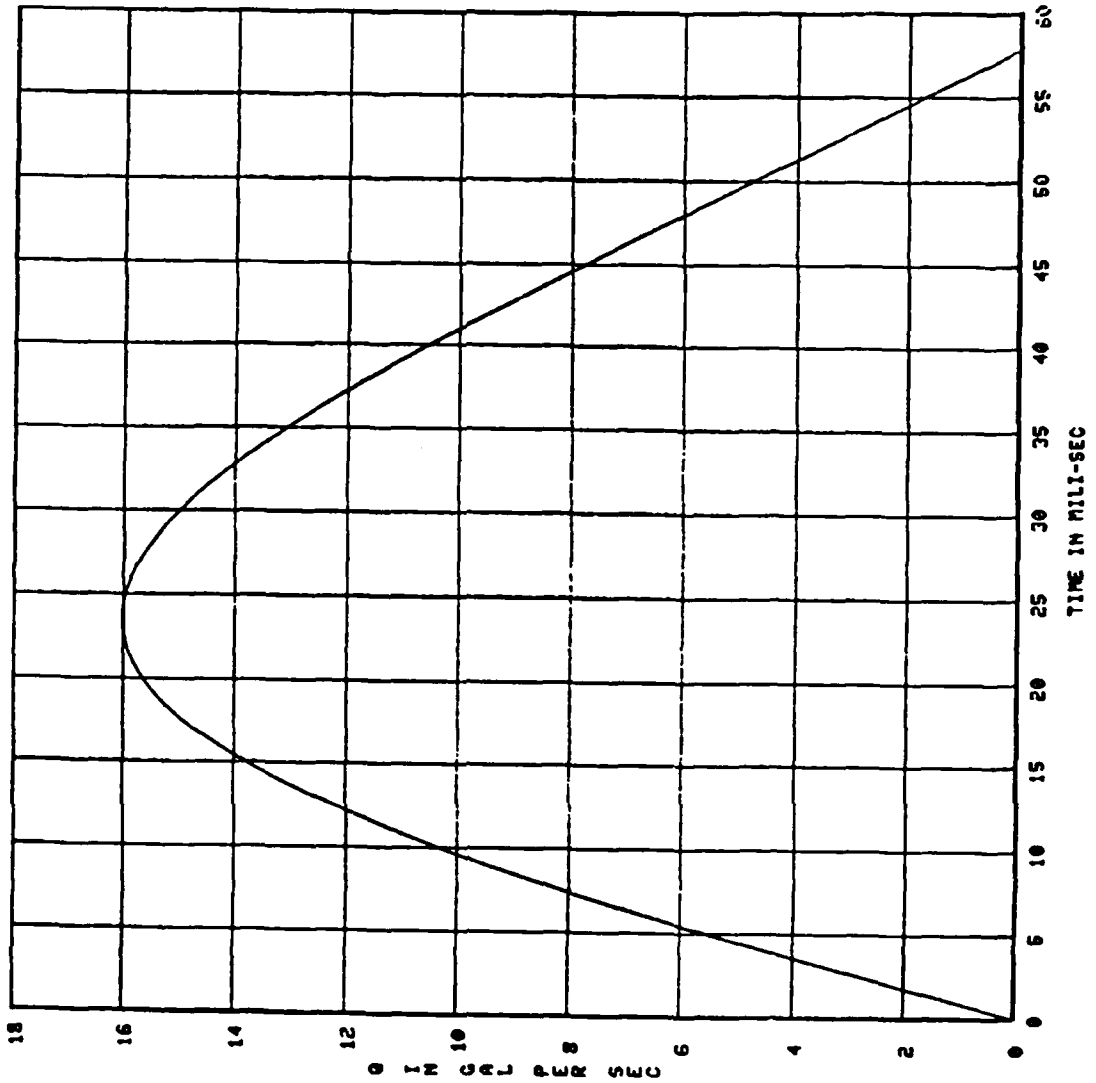


FIGURE B2

PROGRAM ROSSCOBRA/JUMP -- JAY CHEEK, SHD. SL. UES. 16 JAN 1986

PISTON DIAMETER = 16.00 IN  
 SHAFT DIAMETER = 9.00 IN  
 PUMP PRESSURE = 4350.00 PSI  
 FLYWHEEL DIAMETER = 30.00 IN  
 FLYWHEEL WEIGHT = 2000.00 LB  
 CRANK THROU = 1.00 IN  
 CONNECTING ROD LENGTH = 30.00 IN  
 INITIAL RPM = 424.00  
 CRANK ANGLE AT START = 0. DEG

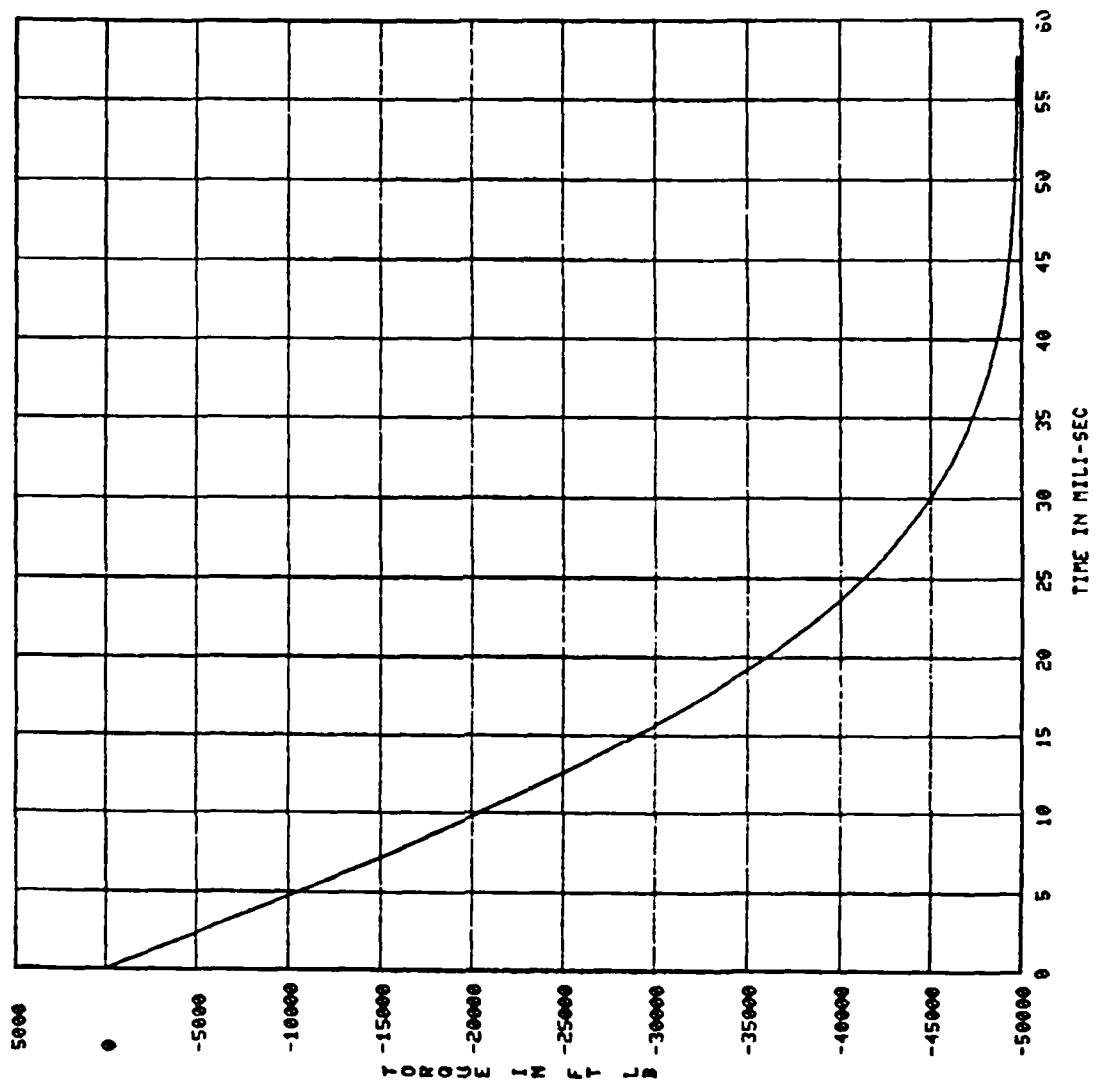


FIGURE B3

PROGRAM ROSSCOBRA/JPLUMP -- JAY CHEEK, SHD, SL, MES, 16 JAN 1986

PISTON DIAMETER = 16.00 IN  
SHAFT DIAMETER = 9.00 IN  
PUMP PRESSURE = 4350.00 PSI  
FLYWHEEL DIAMETER = 30.00 IN  
FLYWHEEL WEIGHT = 2000.00 LB  
CRANK THROW = 1.00 IN  
CONNECTING ROD LENGTH = 30.00 IN  
INITIAL RPM = 424.00  
CRANK ANGLE AT START = 0 DEG

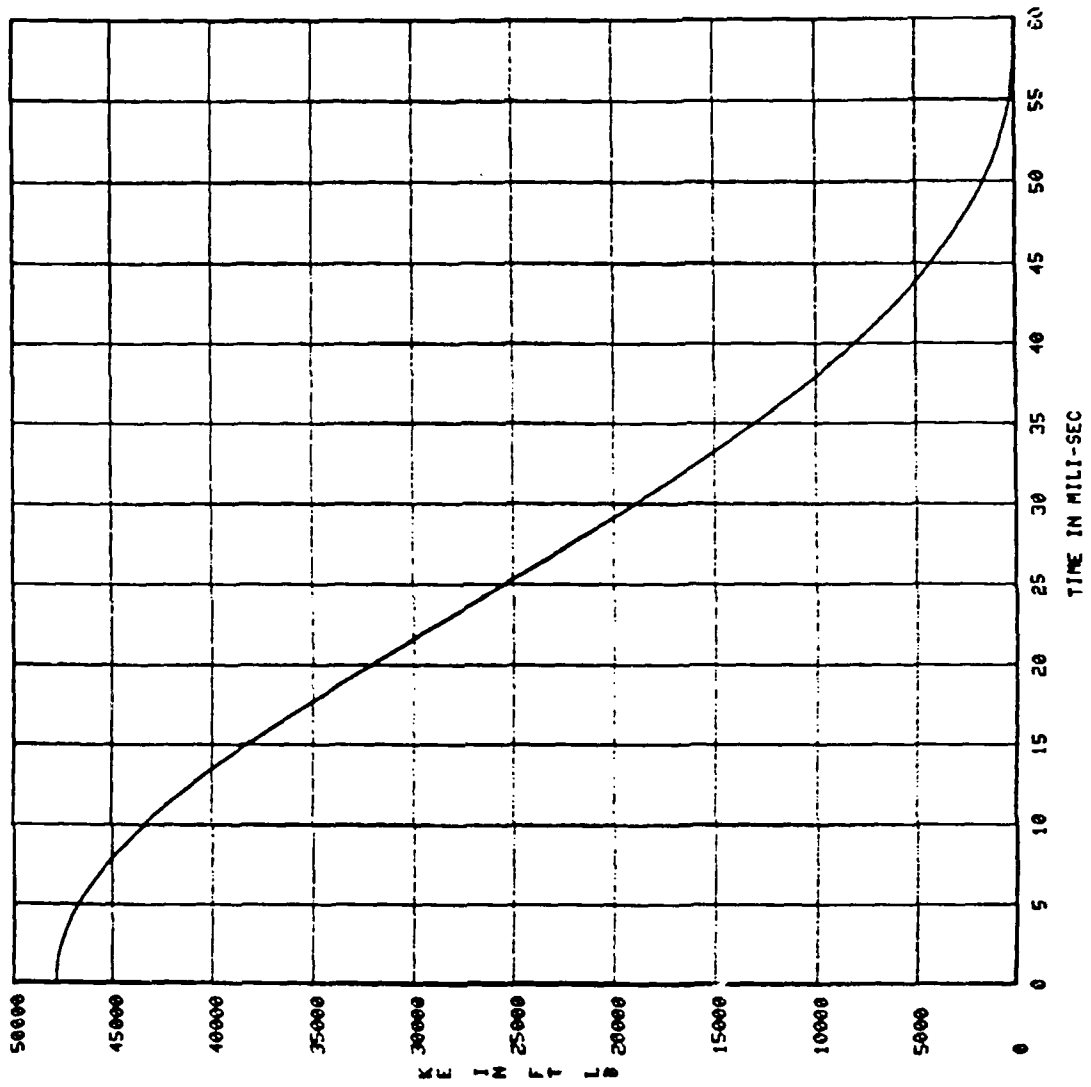


FIGURE B4

PROGRAM ROSSCOBRA/JUMP --- JAY CHEEK, SMD, SL, UES, 16 JAN 1986

PISTON DIAMETER - 16.00 IN  
SHAFT DIAMETER - 9.00 IN  
PUMP PRESSURE - 4350.00 PSI  
FLYWHEEL DIAMETER - 30.00 IN  
FLYWHEEL WEIGHT - 2000.00 LB  
CRANK THROU - 1.00 IN  
CONNECTING ROD LENGTH - 30.00 IN  
INITIAL RPM - 424.00  
CRANK ANGLE AT START - 0 DEG

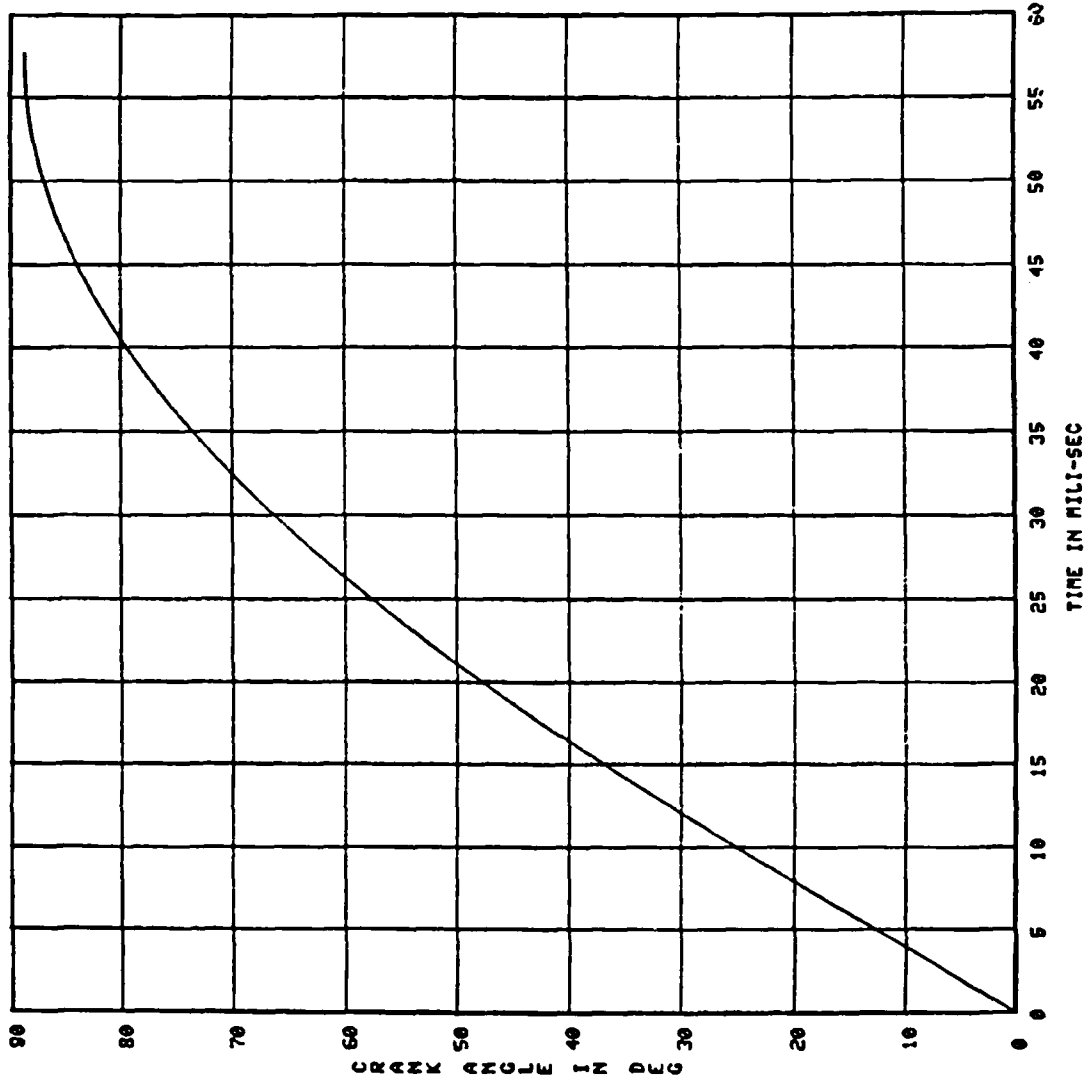


FIGURE B5

PROGRAM ROSSCOBRA/JPUMP -- JAY CHEEK. SNO. SL. UES. 16 JAN 1986

PISTON DIAMETER . 16.00 IN  
SHAFT DIAMETER . 9.00 IN  
PUMP PRESSURE . 4350.00 PSI  
FLYWHEEL DIAMETER . 30.00 IN  
FLYWHEEL HEIGHT . 2000.00 LB  
CRANK THROU . 1.00 IN  
CONNECTING ROD LENGTH . 30.00 IN  
INITIAL RPM . 424.00  
CRANK ANGLE AT START . 0. DEG

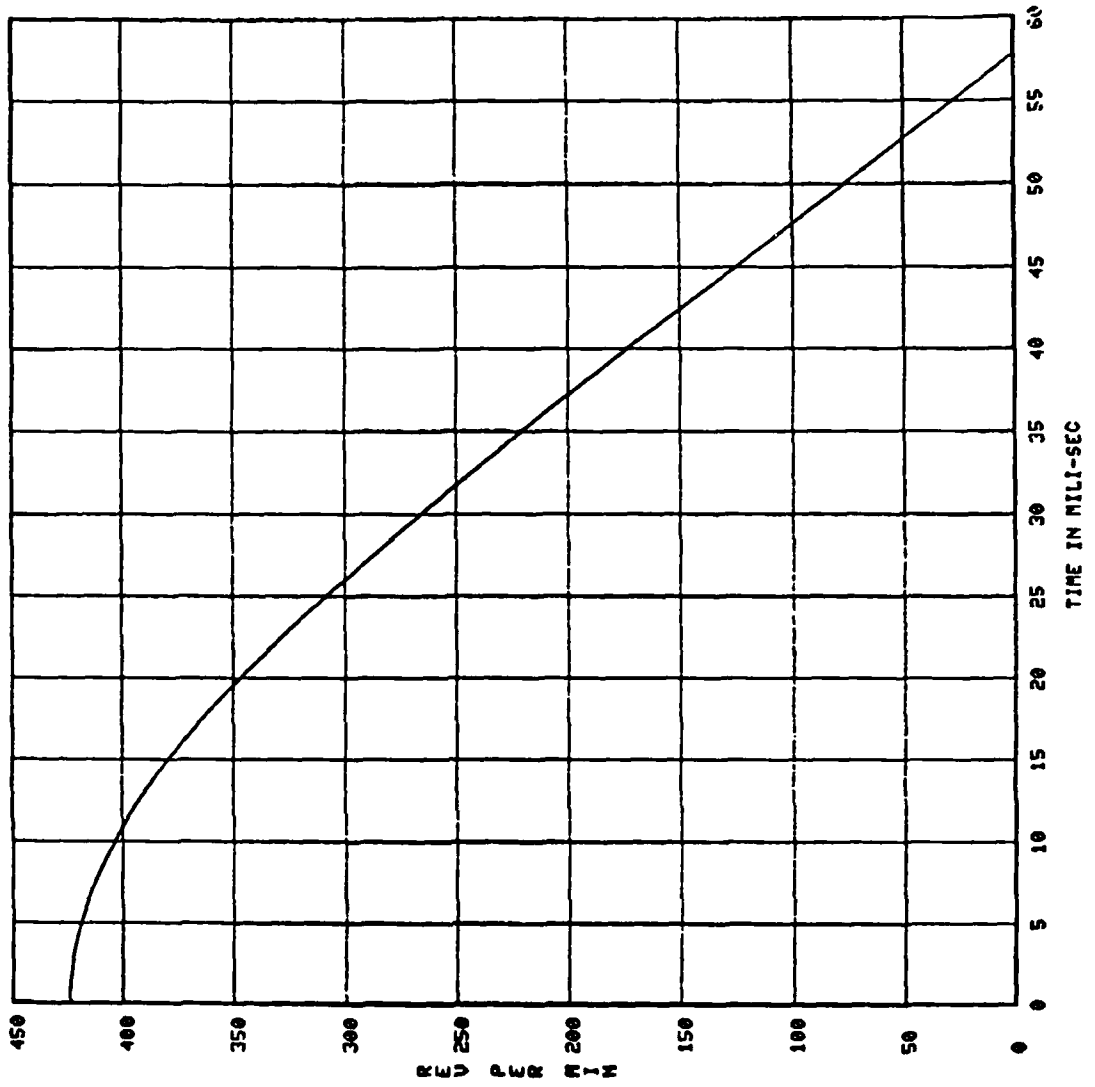


FIGURE B6

TEST START ANGLE, RPM =?

=0 577

N	T(SEC)	THETA	RPM	KE (FT-LB)	Q (GAL/SEC)	TORQ (FT-LB)
0	0.	0.	577.0	88582.	0.06	0.
100	0.0060	20.79	566.8	85472.	12.12	-17136.
200	0.0121	40.86	537.4	76851.	21.36	-31771.
300	0.0181	59.57	493.0	64679.	26.09	-42233.
400	0.0242	76.47	438.9	51265.	26.44	-48063.
500	0.0302	91.32	380.4	38501.	23.78	-49849.
600	0.0363	104.03	321.6	27511.	19.65	-48728.
700	0.0423	114.64	265.2	18707.	15.27	-45915.
800	0.0483	123.28	212.6	12025.	11.31	-42414.
900	0.0544	130.09	164.2	7177.	8.02	-38934.
1000	0.0604	135.22	119.8	3817.	5.40	-35925.
1100	0.0665	138.80	78.5	1639.	3.31	-33642.
1200	0.0725	140.92	39.4	413.	1.59	-32219.
1300	0.0786	141.66	1.5	1.	0.06	-31718.

PUMPING ENDS AT 0.079 SEC.

PUMP CUTOUT ANGLE = 141.7 DEGREES

NUMBER OF TIME STEPS = 1304

FIGURE B7

PROGRAM ROSSCORRA/JPLIMP -- JAY CHEEK. SMD. SL. UES. 16 JAN 1986

PISTON DIAMETER = 16.00 IN  
 SHAFI DIAMETER = 0.00 IN  
 PUMP PRESSURE = 4350.00 PSI  
 FLYWHEEL DIAMETER = 30.00 IN  
 FLYWHEEL WEIGHT = 2000.00 LB  
 CRANK THROU = 1.00 IN  
 CONNECTING ROD LENGTH = 30.00 IN  
 INITIAL RPM = 577.00  
 CRANK ANGLE AT START = 0. DEG

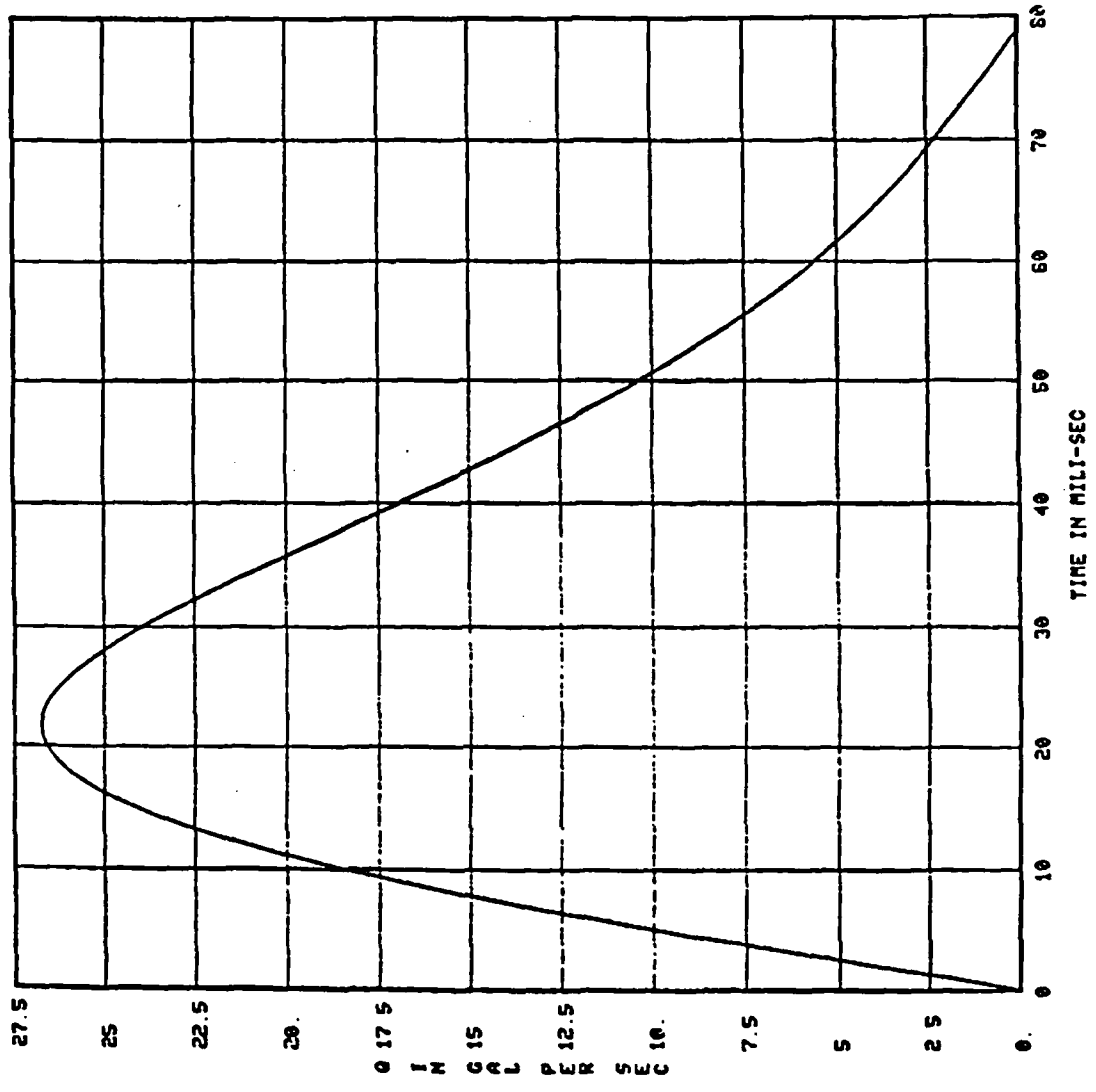


FIGURE B8



PROGRAM ROSSCOBRA/JUMP -- JAY CHEEK. SMD. SL. LES. 16 JAN 1986

PISTON DIAMETER = 16.00 IN  
 SHAFT DIAMETER = 9.00 IN  
 PUMP PRESSURE = 4350.00 PSI  
 FLYWHEEL DIAMETER = 30.00 IN  
 FLYWHEEL WEIGHT = 2000.00 LB  
 CRANK THROU = 1.00 IN  
 CONNECTING ROD LENGTH = 30.00 IN  
 INITIAL RPM = 577.00  
 CRANK ANGLE AT START = 0 DEG

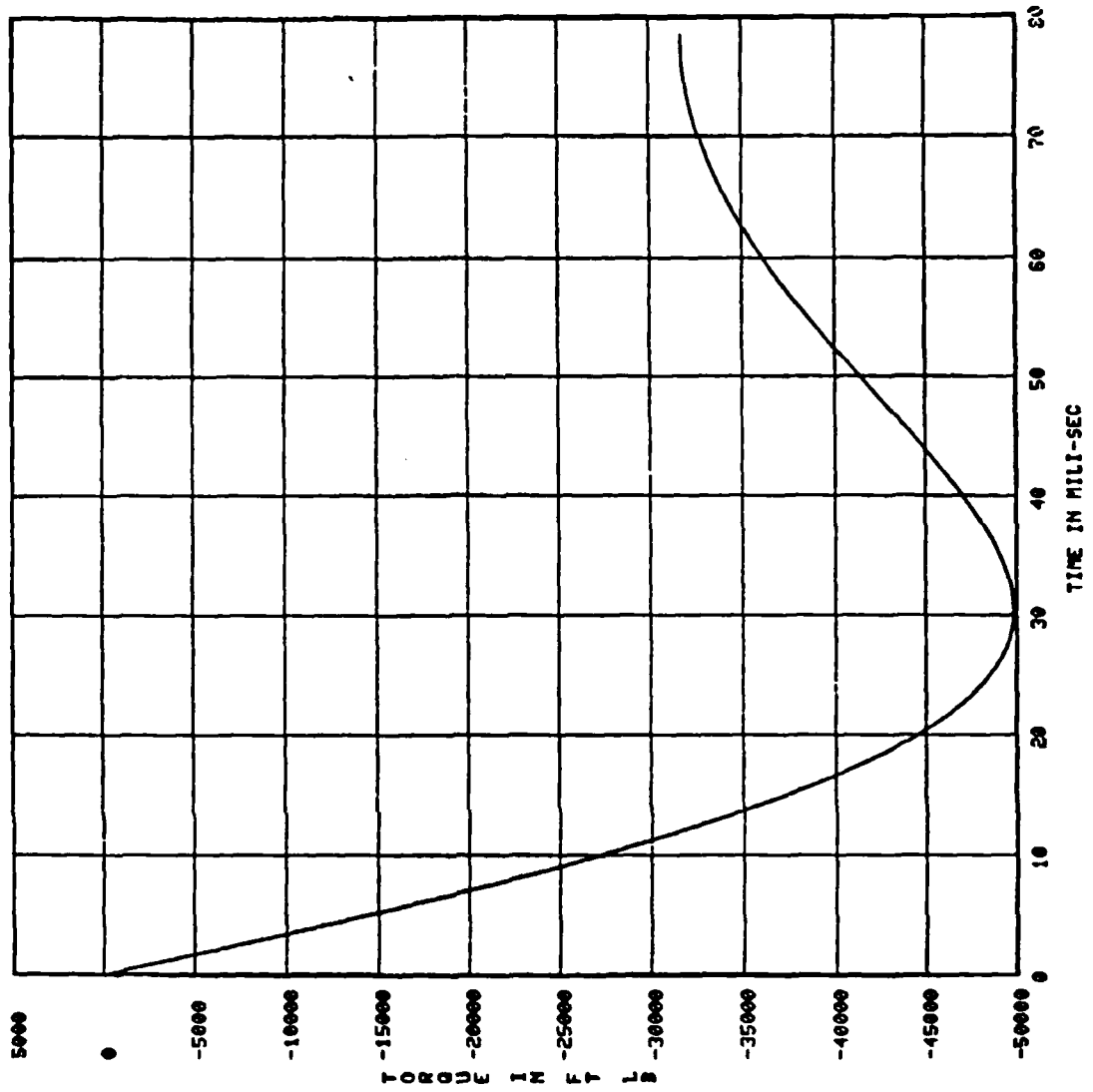


FIGURE B9

PROGRAM ROSSOBRA/JFURP --- JAY CHEEK. SHD. SL. LES. 16 JAN 1986

PISTON DIAMETER . 16.00 IN  
 SHAFT DIAMETER . 9.00 IN  
 PUMP PRESSURE . 4350.00 PSI  
 FLYWHEEL DIAMETER . 30.00 IN  
 FLYWHEEL WEIGHT . 2000.00 LB  
 CRANK THROW . 1.00 IN  
 CONNECTING ROD LENGTH . 30.00 IN  
 INITIAL RPM . 577.00  
 CRANK ANGLE AT START . 0. DEG

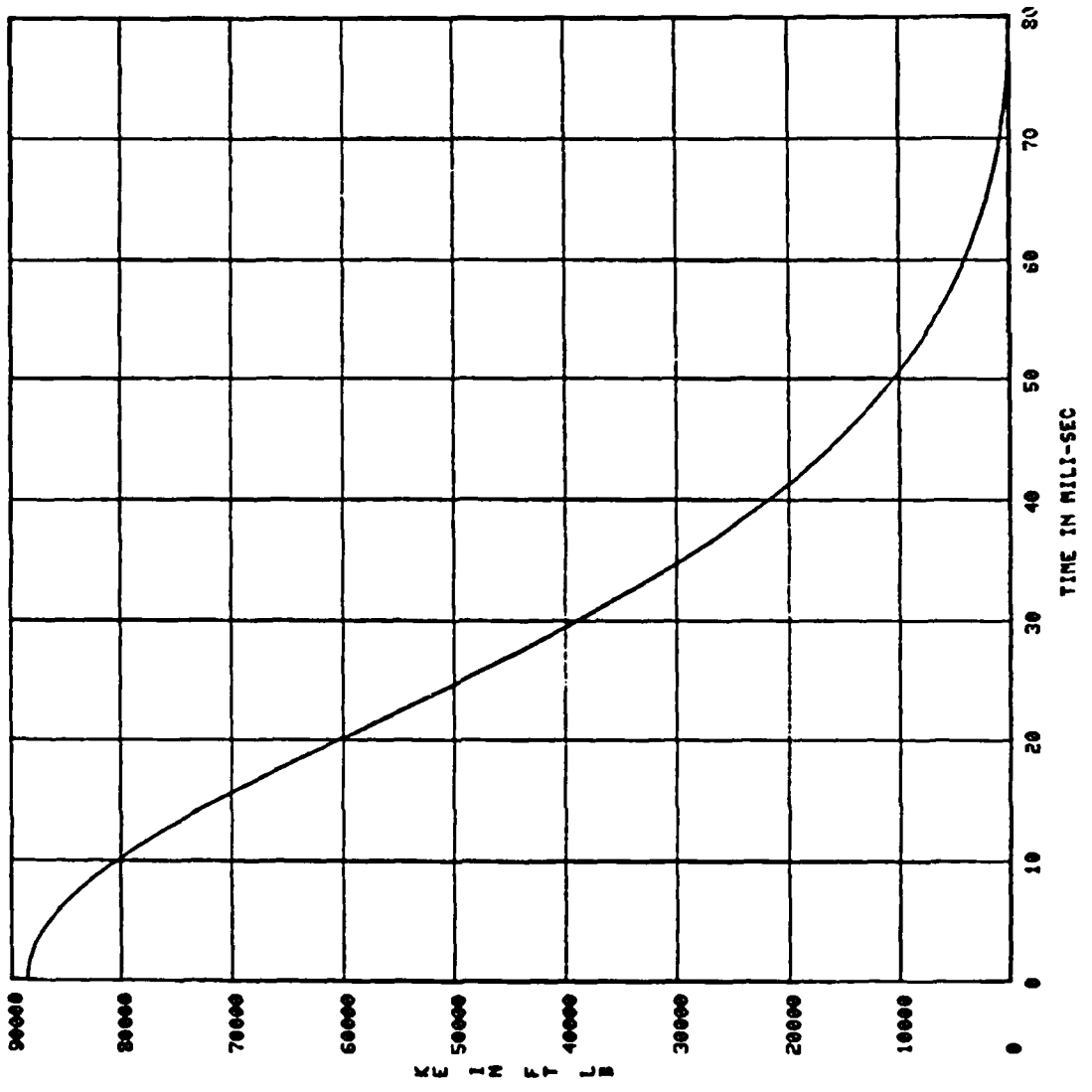


FIGURE B10

PROGRAM ROSSCORRA/JPLUMP --- JAY CHEEK. SRD. SL. LES. 16 JAN 1986

PISTON DIAMETER . 16.00 IN  
SHAFT DIAMETER . 9.00 IN  
PUMP PRESSURE . 4350.00 PSI  
FLYWHEEL DIAMETER . 30.00 IN  
FLYWHEEL WEIGHT . 2000.00 LB  
CRANK THROU . 1.00 IN  
CONNECTING ROD LENGTH . 30.00 IN  
INITIAL RPN . 577.00  
CRANK ANGLE AT START . 0. DEG

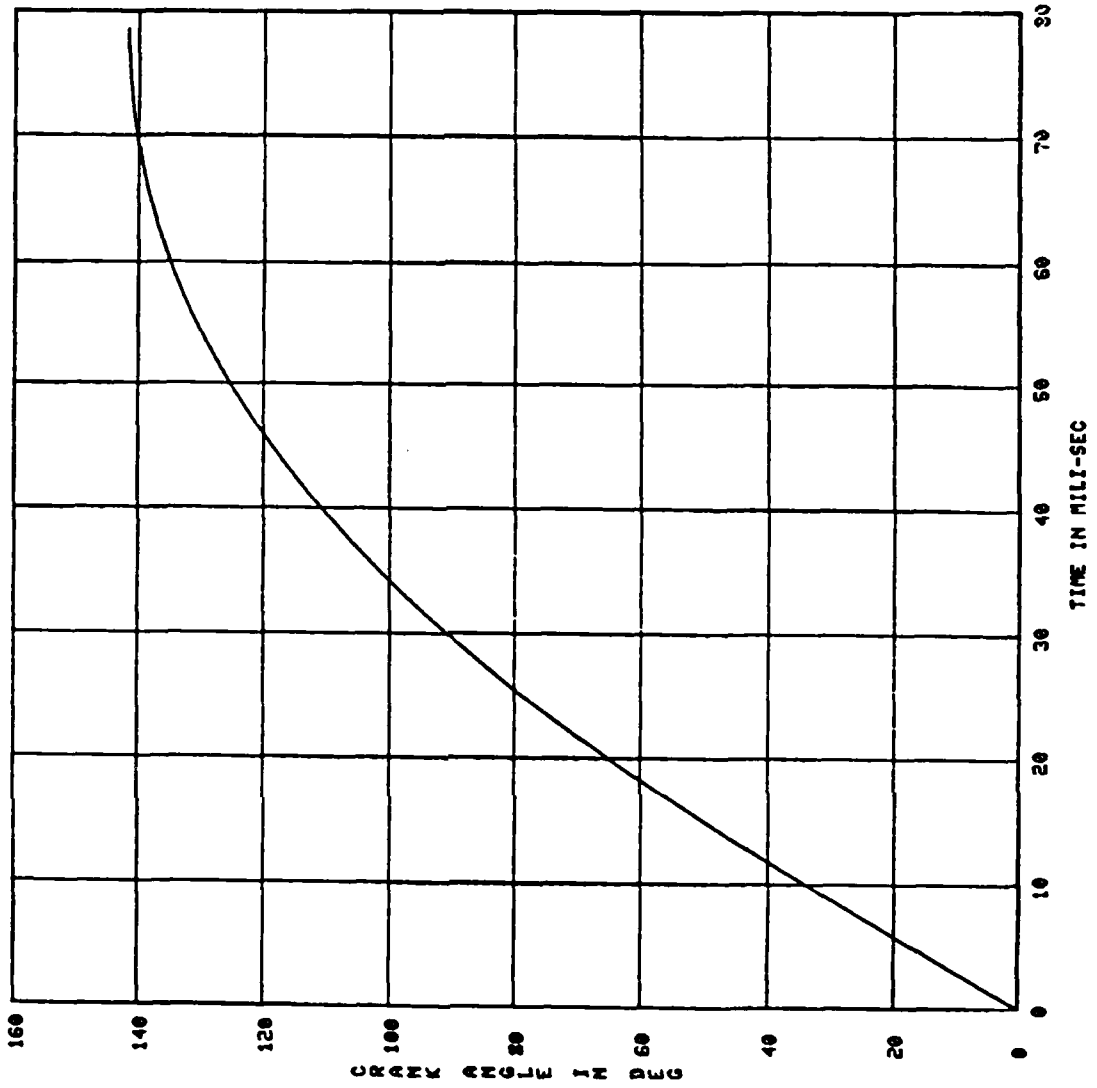


FIGURE B11

PROGRAM ROSSCORAJPLMP -- JAY CHEEK, SHD. SL. UES. 16 JAN 1986

PISTON DIAMETER = 16.00 IN  
 SHAFT DIAMETER = 9.00 IN  
 PUMP PRESSURE = 4350.00 PSI  
 FLYWHEEL DIAMETER = 30.00 IN  
 FLYWHEEL HEIGHT = 2000.00 LB  
 CRANK THROU = 1.00 IN  
 CONNECTING ROD LENGTH = 30.00 IN  
 INITIAL RPM = 577.00  
 CRANK ANGLE AT START = 0 DEG

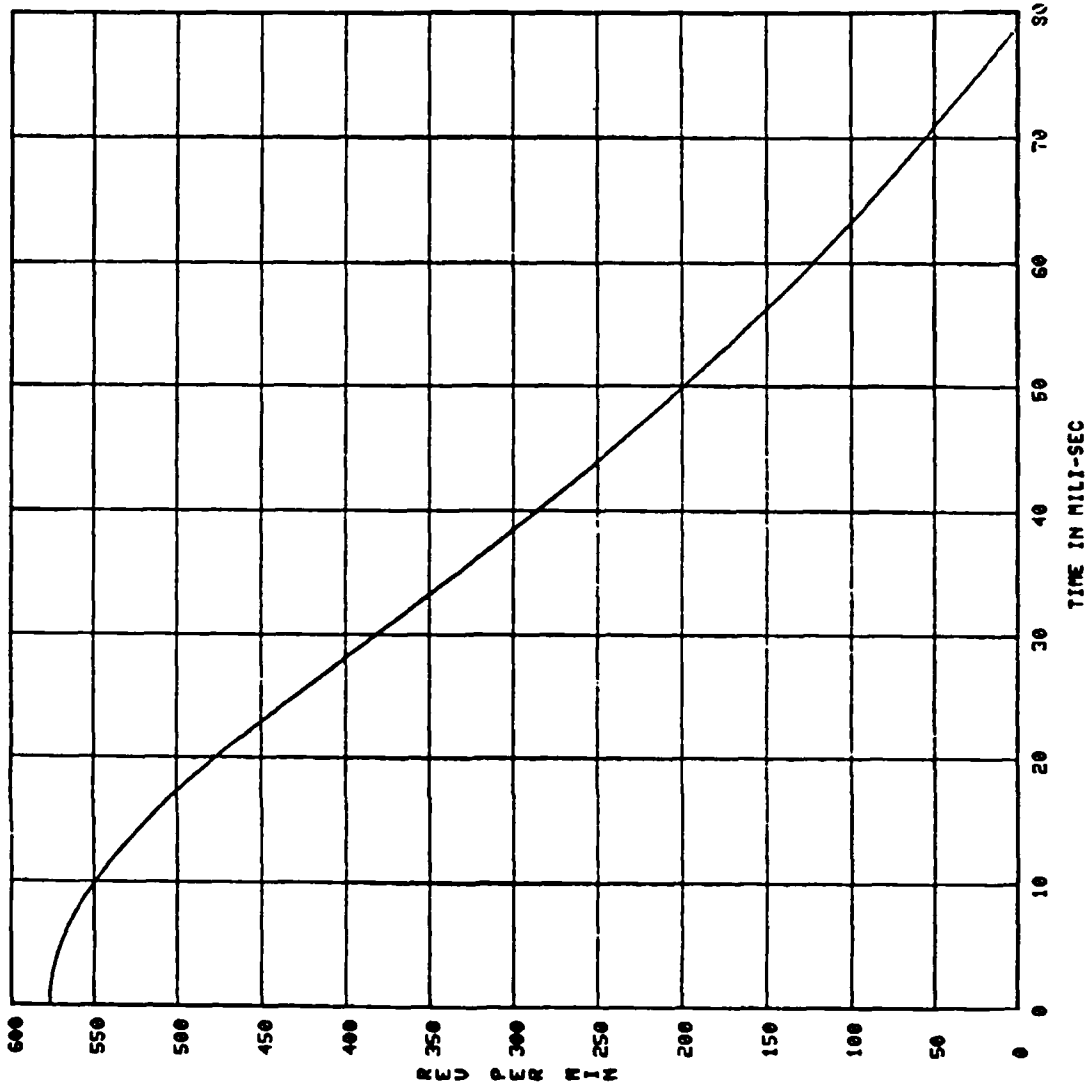


FIGURE B12

APPENDIX C: ROTATIONAL SYSTEM PROGRAM "JPUMP"

1. This appendix presents a listing of program JPUMP that was used for the idealized dynamic analysis of the rotational test system. This program produced the tabulations and plots presented in Appendixes A and B.

JFUMP

```
100#TITLE FILED IN ROSSCOBRA/JFUMP
200 PUMP RUN-TIME TEST PROGRAM
300 JAY CHEEK, SMD, SL, WES, 14 JAN 1986
400
500 DP PISTON DAMETER (IN.)
600 DS PUMP SHAFT DIAMETER(IN.)
700 AP EFFECTIVE AREA OF PISTON (FT**2)
800 SP STROKE OF THE PISTON (IN)
900 DF FLYWHEEL DIAMETER (IN.)
1000 WF FLYWHEEL WEIGHT (LBS.)
1100 PI 3.1415927
1200 DTR FACTOR TO CONVERT DEGREES TO RADIANS
1300 G 32.2
1400 P WORKING PRESSURE IN THE PUMP (P/IN**2)
1500 FM FLYWHEEL MASS
1600 RMI ROTATIONAL MOMENT OF THE FLYWHEEL
1700 RPM INITIAL REV. PER MIN. OF THE FLYWHEEL
1800 AVF CURRENT ANGULAR VELOCITY OF THE FLYWHEEL (RAD./SEC)
1900 AVFI INITIAL ANGULAR VELOCITY OF THE FLYWHEEL (RAD./SEC)
2000 EK KINETIC ENERGY OF THE FLYWHEEL
2100 THETA1 SHAFT ANGLE WHEN PUMPING TEST STARTS (DEG)
2200 THETA CURRENT SHAFT ANGLE DURING PUMP TEST
2300 ZMI INITIAL MOMENTUM OF THE FLYWHEEL
2400 ZM CURRENT MOMENTUM OF THE FLYWHEEL
2500 ZIMP TOTAL IMPULSE ON FLYWHEEL FROM PUMP ACTION
2600 TDEL TIME STEP(SEC)
2700 TI CURRENT TIME SINCE START OF THE TEST.
2800 CL CONNECTING ROD LENGTH.
2900 TOR TORQUE APPLIED DURING ONE TIME STEP
3000 ALPHA ANGULAR DECELERATION DURING ONE TIME STEP.
3100 Q DISCHARGE OF THE PUMP IN GAL/SEC.
3200 XF DIST. FROM CL OF CRANK TO PUMP AT STEP N
3300 XFL DIST. FROM CL OF CRANK TO PUMP AT STEP N-1
3400
3500
360 DIMENSION V(1500,6)
370 DATA PI/3.1415927/, G/32.2/, DP/16.0/, DS/9.0/,
380 & DTR/57.295780/, WF/1000.0/, SP/2.0/, P/4350.0/,
390 & DF/30.0/, CL/30.0/
4000
4100 PLOT SETUP
420 CALL USTART
430 CALL UPSET('SPEED', 120.)
440 CALL USET('SMALL')
450 CALL USET('XBOTHLABELS')
460 CALL USET('YBOTHLABELS')
470 CALL UERASE
480 CALL UHOME
490 CALL UALPHA
5000
```

JFUMP

```

510C GET INITIAL CONDITIONS
520 100 WRITE (6,110) ' TEST START ANGLE, RPM =?'
530 110 FORMAT (V)
540 READ (5,110) THETA1, RPM
550C PISTON AREA
560 AP = PI * (IP * IP - IS * IS) / 576.0
570C MASS OF THE TWO FLYWHEELS
580 FM = WF * 2.0 / G
590C ROTATIONAL MOMENT OF INERTIA
600 RMI = FM * DF * DF / 1152.0
610C INITIAL ANGULAR VELOCITY
620 AVFI = RPM * PI / 30.0
630C
640C CALC CONSTANTS FOR THE INTEGRATION LOOP.
650C CRANK ARM LENGTH IN FT
660 TH = SP / 24.0
670C SQUARE OF THE CONNECTING ROD LENGTH
680 CLS = CL * CL / 144.0
690C TIME STEP IN SEC.
700 TDEL = AVFI / 1000000.0
710C PUMP FORCE TIMES CRANK ARM LENGTH
720 FR = AP * P * TH * 144.0
730C STEP COUNTER
740 N = 0
750C INITIAL ANGULAR VELOCITY OF THE CRANKSHAFT (RADIAN/SEC)
760 AVF = AVFI
770C CRANKSHAFT ANGLE AT START OF PUMPING (0 DEG IS
780C TOP DEAD CENTER OF STROKE)
790 THETA = THETA1
800C NUMBER OF POINTS TO BE PLOTTED
810 NVP = 0
820C
830C HEADING.
840 WRITE (6,120)
850 120 FORMAT (' N T(SEC) THETA RPM KE (FT-LB) Q '
860 & ', '(GAL/SEC) TORQ (FT-LB)')
870C
880C START THE PUMP TEST LOOP
890C ELAPSED TIME IN SEC
900 130 TI = N * TDEL
910C CURRENT CRANKSHAFT ANGLE IN RADIAN
920 TR = THETA / DTR
930C KINETIC ENERGY IN FT LBS
940 EK = RMI * AVF * AVF / 2.0
950C TEST FOR SPECIAL CALCULATION FOR Q AT START
960 IF (N .NE. 0) GO TO 140
970C CALC PUMP POSITION JUST BEFORE THE FIRST STEP.
980 TRR = TR - AVF * TDEL
990 ST = SIN(TRR)
1000 TEMP1 = TH * COS(TRR)

```

## JPUMP

```

1010     TEMP2 = SQRT(CLS-(TH*ST)**2)
1020     XPL = TEMP2 - TEMP1
1030 140 ST = SIN(TR)
1040C   X COMPONENT OF THE CRANK ARM
1050     TEMP1 = TH * COS(TR)
1060C   PROJECTION OF CONN. ROD ON X AXIS
1070     TEMP2 = SQRT(CLS-(TH*ST)**2)
1080C   POSITION OF THE PUMP AT STEP N
1090     XP = TEMP2 - TEMP1
1100C   PUMP DISCHARGE DURING THIS STEP
1110     Q = ABS(XP-XPL) * AP * 7.5 / TDEL
1120     XPL = XP
1130C   SLOWDOWN TORQUE ON CRANK DUE TO PUMPING FORCE
1140     TOR = - ABS(FR*ST*(1.0-TEMP1/TEMP2))
1150C   ANGULAR DECELERATION
1160     ALPHA = TOR / RMI
1170     IF (MOD(N,100) .EQ. 0) WRITE (6,150) N, TI, THETA, AVF /
1180     &      2. / PI * 60, EK, Q, TOR
1190 150 FORMAT (1X, I4, F8.4, F8.2, F8.1, F10.0, F14.2, F14.0)
1200C
1210C   SAVE EVERY FIFTH POINT FOR PLOTTING
1220     IF (MOD(N,5) .NE. 0) GO TO 160
1230     NVP = NVP + 1
1240     V(NVP,1) = TI * 1000.0
1250     V(NVP,2) = Q
1260     V(NVP,3) = TOR
1270     V(NVP,4) = EK
1280     V(NVP,5) = THETA
1290     V(NVP,6) = AVF / 2.0 / PI * 60.0
1300C   NEW ANGULAR VELOCITY DUE TO SLOWDOWN TORQUE
1310 160 AVF = AVF + ALPHA * TDEL
1320C   COUNT STEP
1330     N = N + 1
1340C   STILL ROTATING?
1350     IF (AVF .LT. 0.0) GO TO 170
1360C   YES. ADVANCE TO NEXT CRANK ANGLE
1370     THETA = THETA + AVF * TDEL * DTR
1380     GO TO 130
1390C
1400C   DONE
1410 170 WRITE (6,180) TI, THETA - THETA1, N
1420 180 FORMAT ( ' PUMPING ENDS AT ', F10.3, ' SEC.' /
1430     &      ' PUMP CUTOUT ANGLE = ', F8.1, ' DEGREES' /
1440     &      ' NUMBER OF TIME STEPS = ', I5 // )
1450     CALL UPAUSE
1460C
1470C   PLOT THE CURVES
1480     CALL PLOTFU(V, NVP, DP, DS, P, DF, WF, SP, CL, RPM, THETA1)
1490     GO TO 100
1500     END

```



```

JPUMP
1510     SUBROUTINE PLOTPU(V, NV, DP, DS, P, DF, WF, SP, CL, RPM,
1520     &     THETA1)
1530C
1540C PLOT ANY OF THE 5 ARRAYS AS A FUNCTION OF TIME (ARRAY1).
1550C JAY CHEEK, SMD, SL, WES, 16 JAN 1986
1560C
1570     CHARACTER*20 T(20)
1580     DIMENSION V(1500,6)
1590     DATA T(1) // 'TIME IN MILI-SEC\ ' /, T(2)
1600     &     // 'Q IN GAL PER SEC\ ' /, T(3)
1610     &     // 'TORQUE IN FT LB\ ' /, T(4)
1620     &     // 'KE IN FT LB\ ' /, T(5)
1630     &     // 'CRANK ANGLE IN DEG\ ' /, T(6)
1640     &     // 'REV PER MIN\ ' /
1650C START PLOTTING
1660     FN = NV
1670     CALL UPSET('XLABEL', T(1))
1680     DO 120 I = 2, 6
1690C
1700C IS THIS GRAPH NEEDED?
1710     WRITE (6,100) T(I)
1720 100  FORMAT (' PLOT ', A20, '?')
1730     CALL IANSR(IST)
1740     IF (IST .EQ. 0) GO TO 120
1750C
1760C YES. DO IT.
1770     CALL UPSET('YLABEL', T(I))
1780     CALL UERASE
1790     CALL UDAREA(4.0, 14.0, 0.0, 10.0)
1800     CALL USET('GRIDAXIS')
1810     CALL UPLOT1(V(1, I), V(1, I), FN)
1820     CALL UHOME
1830     CALL UALPHA
1840     WRITE (6,110) DP, DS, P, DF, WF * 2.0, SP / 2.0, CL, RPM,
1850     &     THETA1
1860 110  FORMAT (' PROGRAM ROSSCOBRA/JPUMP -- JAY CHEEK, SMD, '
1870     &     , 'SL, WES, 16 JAN 1986' / ' PISTON DIAMETER =',
1880     &     F8.2, ' IN' / ' SHAFT DIAMETER =', F8.2, ' IN' /
1890     &     ' PUMP PRESSURE =', F8.2, ' PSI' /
1900     &     ' FLYWHEEL DIAMETER =', F8.2, ' IN' /
1910     &     ' FLYWHEEL WEIGHT =', F8.2, ' LB' /
1920     &     ' CRANK THROW =', F6.2, ' IN' / ' CONNECTING ROD LENGTH
1930     &     , F8.2, ' IN' / ' INITIAL RPM ='
1940     &     , F8.2 / ' CRANK ANGLE AT START =', F8.2, ' DEG')
1950     CALL UPAUSE
1960 120 CONTINUE
1970     RETURN
1980     END

```

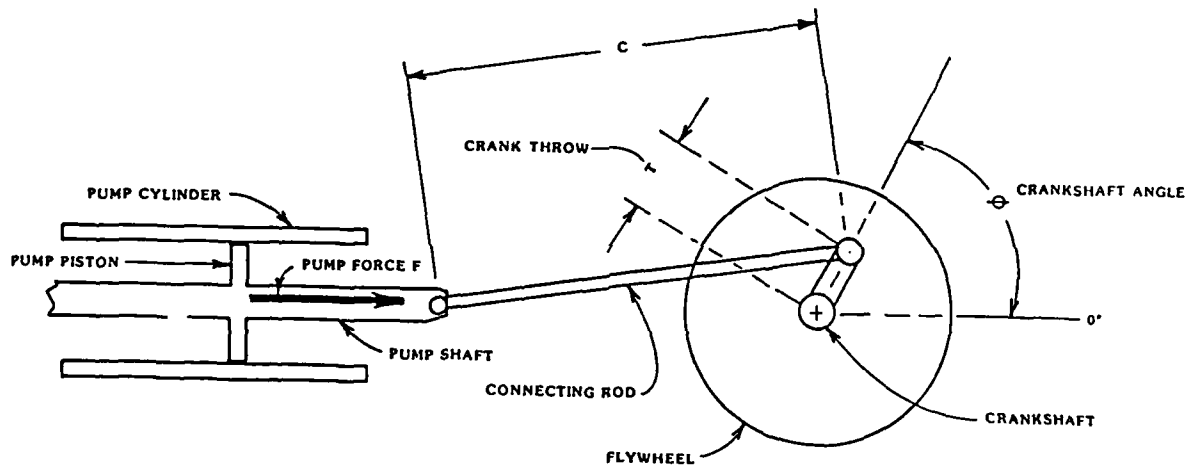
JPUMP

```
1990      SUBROUTINE IANSR(IWHAT)
2000C     SEE WHETHER THE USER GIVES A Y (OR A CARRIAGE RETURN)
2010C     FOR YES OR A N FOR NO TO A PREVIOUSLY ASKED QUESTION.
2020C
2030C     CODE FILED IN ROSSCOBRA/JHEST-S.
2040C     JAY CHEEK, SMD, SL, WES; DEC 1981
2050C
2060      DATA IBLK//      '//, IYES//Y      '//, NO//N      '//
2070     100 IWHAT = 0
2080      READ (5,110) II
2090     110 FORMAT (A4)
2100      IF (II .EQ. NO) RETURN
2110      IWHAT = 1
2120      IF (II .EQ. IYES) RETURN
2130      IF (II .EQ. IBLK) RETURN
2140      WRITE (6,120)
2150     120 FORMAT (' ERROR: ONLY Y OR RETURN (FOR YES) OR N (FOR
2160      &      , 'NO) ALLOWED, RETRY')
2170      GO TO 100
2180      END
```

APPENDIX D: METHOD FOR CALCULATING SLOWDOWN OF FLYWHEEL

Initial Conditions

1. As shown in Figure D1, a flywheel (solid disc) of weight  $W$  is rotating at an initial rpm. The flywheel diameter is  $D$ . The flywheel is connected to a crankshaft whose offset (throw) is  $T$ . A connecting rod of length  $C$  connects the crank to the pump that resists motion with a constant force  $F$ . That force is directed on a line from the crankshaft center-line through the center-line of the pump shaft.



Pump's End Plates and Valves not shown

Idealized Pump and Drive System

Figure D1

### Calculating Procedure For Flywheel Slowdown

2. The following steps are used to calculate the flywheel slowdown:

a. Calculate the Rotational Moment of Inertia (I).

$$I = \frac{W}{g} \left(\frac{D}{2}\right)^2 \frac{1}{2}$$

b. Calculate the Angular Velocity ( $\omega$ ).

$$\omega = 2\pi \frac{(\text{rpm})}{60}$$

and choose a small time step ( $\Delta t$ ) so that the wheel will rotate less than  $.1^\circ$  at the initial rpm during time  $\Delta t$ .

c. At each time Step  $i$ , Calculate:

1. The angle traversed ( $\Delta\theta$ ) during this time step (constant angular velocity ( $\omega$ ) is assumed).

$$\Delta\theta = \omega_i \Delta t$$

2. The current angular location ( $\theta$ ) of the crank.

$$\theta_i = \theta_{i-1} + \Delta\theta$$

3. The component of F, acting through the connecting rod that is perpendicular to the crank arm ( $F_M$ ).

4. The torque ( $\Gamma$ ) at angle  $\theta$ .

$$\Gamma = F_M r$$

5. The angular deceleration ( $\alpha$ ) produced by this constant torque.

$$\alpha = - \Gamma / I$$

6. The new angular velocity due to the slowdown torque from the pumping force.

$$\omega_i = \omega_{i-1} + \alpha \Delta t$$

7. Add 1 to i and repeat steps C1 through C7 until  $\omega_i \leq 0$ .
8. Done.

### Calculating Moment Applied To The Crankshaft

3. As illustrated in Figure D2: T is crankshaft throw, F is force to operate the pump, C is connecting rod length, E is the moment arm,  $\theta$  is crankshaft angle, and G is the force normal to E.

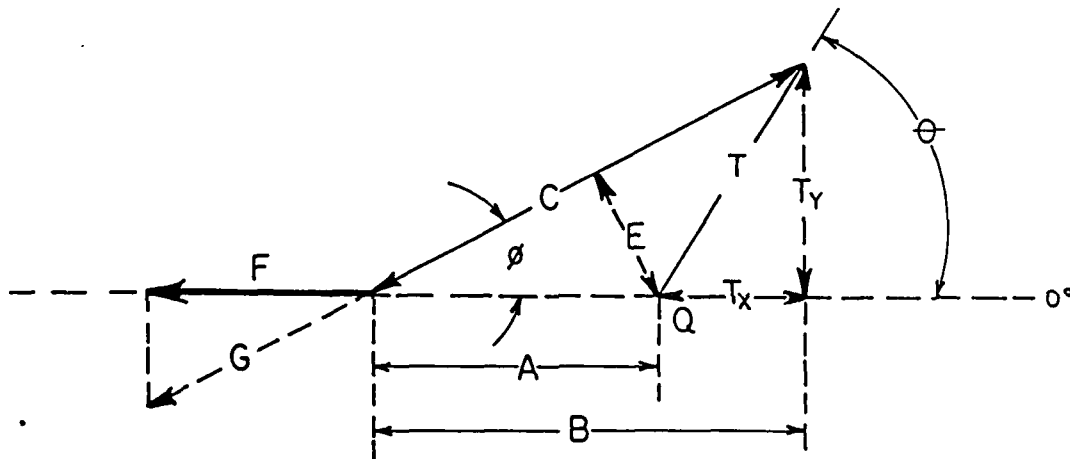


Figure D2

Calculating the Torque ( $\Gamma$ ) about point Q.

$$\begin{aligned} \Gamma &= G E & B &= (C^2 - T_y^2)^{1/2} & \sin \phi &= \frac{T_y}{C} = \frac{T \sin \theta}{C} \\ E &= A \sin \phi & T_y &= T \sin \theta & G &= \frac{F}{\cos \phi} \\ A &= B - T_x & T_x &= T \cos \theta & \cos \phi &= \frac{B}{C} \end{aligned}$$

$$\Gamma = \frac{F}{\frac{B}{C}} (B - T_x) \frac{T_y}{C} = F T_y \left(1 - \frac{T_x}{B}\right)$$

$$\Gamma = F T \sin \theta \left[ 1 - \frac{T \cos \theta}{(C^2 - T^2 \sin^2 \theta)^{1/2}} \right] \text{ for } C > T$$

## APPENDIX E: ANALYSIS OF THE DROP TEST SYSTEM

1. This appendix contains the output of the drop test analysis program, JPEND (Figure E1), the listing of the program (E3), and the development of the equations used (E4 and E5). The output is given for both 1,000 and 2,000 pound balls impacting on the pistons of various diameter cylinders. The drop height is paired with the cylinder diameter to produce the rated discharge peak of 26.4 gps. Discharge pressure is assumed to be constant at 4,350 psi. Note that an increase in ball weight, holding other parameters constant, serves to increase the test time (t) directly as the ratio of the new weight to the old

$$t_N = \frac{W_N}{W_O} t_O \quad \text{where subscripts O and N} \\ \text{refer to old and new values.}$$

Figure E2 gives the discharge versus time curves for several ball weight, cylinder diameter and drop height combinations.

Output of the Drop Test Analysis Program "JPEND"

DROP TEST OF VALVE  
 FOR BALL WEIGHT OF 1000. LB PEAK DISCHARGE OF 26.4 GAL / SEC  
 AND DISCHARGE PRESSURE OF 4350. PSI

CYLINDER DIAMETER (INCHES)	DROP HEIGHT (FEET)	RETARD FORCE (POUNDS)	IMPACT VELOCITY (FT / SEC)	DISCHARGE TIME (SECONDS)	KINETIC ENERGY (FT - LBS)
3.50	43.10	41852.	52.68	0.039	43101.
3.75	32.71	48044.	45.89	0.030	32706.
4.00	25.26	54664.	40.34	0.023	25265.
4.25	19.82	61710.	35.73	0.018	19824.
4.50	15.77	69184.	31.87	0.014	15773.
4.75	12.71	77084.	28.60	0.012	12705.
5.00	10.35	85412.	25.82	0.009	10348.

DROP TEST OF VALVE  
 FOR BALL WEIGHT OF 2000. LB PEAK DISCHARGE OF 26.4 GAL / SEC  
 AND DISCHARGE PRESSURE OF 4350. PSI

CYLINDER DIAMETER (INCHES)	DROP HEIGHT (FEET)	RETARD FORCE (POUNDS)	IMPACT VELOCITY (FT / SEC)	DISCHARGE TIME (SECONDS)	KINETIC ENERGY (FT - LBS)
3.50	43.10	41852.	52.68	0.078	86201.
3.75	32.71	48044.	45.89	0.059	65413.
4.00	25.26	54664.	40.34	0.046	50530.
4.25	19.82	61710.	35.73	0.036	39649.
4.50	15.77	69184.	31.87	0.029	31545.
4.75	12.71	77084.	28.60	0.023	25410.
5.00	10.35	85412.	25.82	0.019	20697.

FIGURE E2

Listing of the Drop Test Analysis Program "JPEND"

```
JPEND
100$TITLE FILED IN ROSSCOBRA/JPEND
200  CALC OF PENDULUM TEST OF VALVE PERFORMANCE.
300  JAY CHEEK SMD, SL, WES, 17 JAN 1986
400
50    DATA PI/3.1415926/, P/4350.0/, Q/26.4/
600
70    DO 130 J = 1, 2
800  WEIGHT OF BALL
90    WT = J * 1000.0
1000 DIAMETER OF HYDRAULIC CYLINDER (ONE STROKE PUMP)
110    D = 3.250
120    WRITE (6,100) WT, Q, P
130  100  FORMAT ( '//// '          DROP TEST OF VALVE' /
140    &    ' FOR BALL WEIGHT OF', F6.0,
150    &    ' LB   PEAK DISCHARGE OF', F5.1, ' GAL / SEC' /
160    &    ' AND DISCHARGE PRESSURE OF', F6.0, ' PSI' //
170    &    ' CYLINDER   DROP      RETARD      IMPACT   '
180    &    , 'DISCHARGE  KINETIC' /
190    &    ' DIAMETER   HEIGHT   FORCE      VELOCITY   TIME '
200    &    , ' ENERGY' /
210    &    ' (INCHES) (FEET)   (POUNDS) (FT / SEC) '
220    &    , '(SECONDS) (FT - LBS)')
2300
2400  CALC FOR SEVERAL CYL. DIAMETERS
250    DO 120 I = 1, 7
2600  DIAMETER
270    DI = D + I * .25
2800  PISTON (CYLINDER) AREA
290    A = PI * DI * DI / 4.0
3000  MASS OF THE BALL
310    ZMASS = WT / 32.2
3200  DROP HEIGHT TO PRODUCE PEAK DISCHARGE
330    H = 9.280 * Q * Q / DI ** 4
3400  IMPACT VELOCITY
350    V = SQRT(2.0*32.2*H)
3600  RETARDING FORCE OF THE CYLINDER
370    F = P * A
3800  TIME OF DISCHARGE
390    TI = ZMASS * V / F
4000  KINETIC ENERGY
410    EK = ZMASS * V * V / 2.0
4200
4300  RESULTS
440    WRITE (6,110) DI, H, F, V, TI, EK
450  110  FORMAT (1X, F7.2, F10.2, F12.0, F10.2, F10.3, F10.0)
460  120  CONTINUE
470  130  CONTINUE
480    STOP
490    END
```



Equation For Drop Height

2. Calculating combinations of cylinder diameter (D) and drop height (H) that yield a specific value of fluid discharge Q.

a. Impact velocity =  $U_I = (2gH)^{\frac{1}{2}}$

where U is in ft/sec

H is in ft

g is in ft/sec<sup>2</sup>

b. Discharge =  $Q = \frac{V}{\Delta t}$  where V is volume in ft<sup>3</sup>.

$$Q = \frac{V}{\Delta t} = \frac{A\Delta x}{\Delta t} = AU_I$$

where A is cylinder area =  $\frac{\pi}{4} D^2$

D is cylinder diameter in ft

c.  $H = \frac{Q_I^2}{2g \left(\frac{\pi}{4} D^2\right)^2} = \frac{Q_I^2}{1.234gD^4}$

where  $Q_I$  is discharge at impact, i.e., peak discharge.

d. Converting for Q in gps, and D in inches.

$$H = \frac{\left(\frac{Q_I}{7.5}\right)^2}{1.234 \left(\frac{D}{12}\right)^4 g} = \frac{9.280 Q_I^2}{D^4}$$

### Equation For Total Discharge Time

3. As shown on E4, Drop Weight (H) relates to Peak Discharge ( $Q_I$ ) and cylinder diameter (D) by:

$$H = \frac{9.280Q_I^2}{D^4} \quad \text{Where } Q \text{ is in gps, } D \text{ is in inches.}$$

Conservation of momentum gives  $MU_I = Ft$

Where t is the time in seconds that the constant force F exists, M is the ball mass, W is the ball weight and  $M = \frac{W}{g}$ .

$$F \text{ is the constant piston force} = \frac{\pi D^2 P}{4}$$

Where P is pressure in psi, F is in lbs.

$$U_I = \text{impact velocity} = (2gH)^{\frac{1}{2}}$$

Total discharge time (t) is

$$t = \frac{MU_I}{F} = \frac{\frac{W}{g} (2gH)^{\frac{1}{2}}}{\frac{\pi}{4} D^2 P} = \frac{\frac{W}{g} \left( 2g \frac{9.280Q_I^2}{D^4} \right)^{\frac{1}{2}}}{\frac{\pi}{4} D^2 P} = .9667 \frac{W Q_I}{P D^4}$$

Where: W is weight in lb, D is diameter in inches, Q is discharge in gps, P is pressure in psi, and t is time in sec.

For P = 4,350 psi,  $Q_I = 26.4$  gps

$$t = .005866 \frac{W}{D^4}$$

# DROP TEST OF PRESSURE REGULATING VALVE

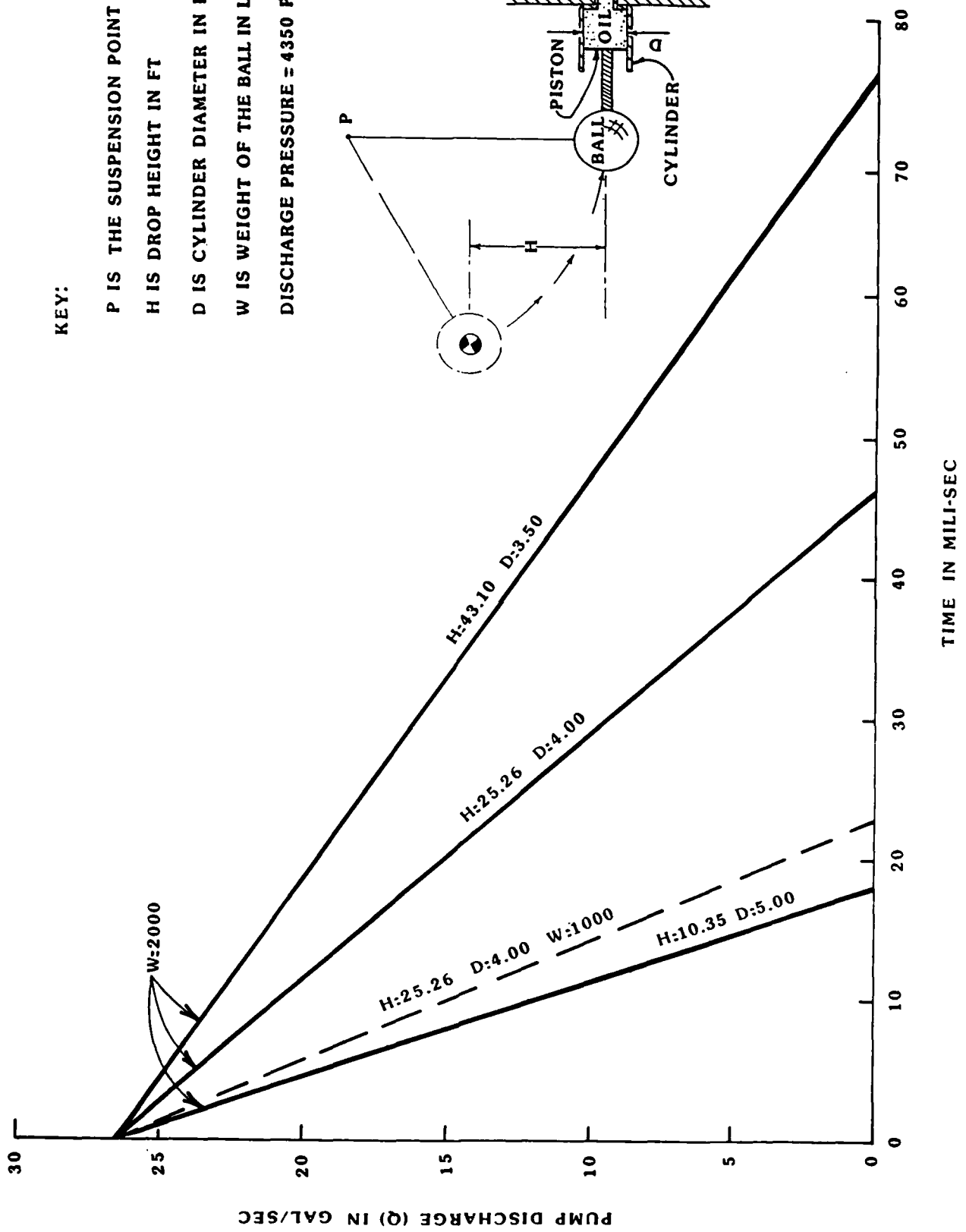


Figure E2

END

DITIC

8-86