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ADVISORY GROUP FOR AEROSPACE RESEARCH AND DEVELOPMENT

(ORGANISATION DU TRAITE DE L'ATLANTIQUE NORD)

AGARD Report No. 723

Addendum 1

AIRCRAFT DRAG PREDICTION AND REDUCTION

Computational Drag Analyses and Minimization; Mission Impossible?

by

J.W.Slooff National Aerospace Laboratory (NLR) Amsterdam, The Netherlands



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PREFACE

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With diminishing world fuel supplies, and a global increase in fuel price over the last ten years, the reduction of aircraft drag has become a technology of major importance to aircraft manufacturers. Likewise, advances in test and evaluation techniques have facilitated the accurate evaluation of drag and led to concurrent developments in drag prediction methods. A noteworthy development is the use of a number of novel flow control methods which, through either passive or active interaction with the flow physics, can lead to substantial drag reductions.

This special course covers some of the more recent progress in drag reduction, measurement and prediction. The topics presented discuss the different sources and contributions to aircraft drag with particular emphasis on those areas in which significant new developments have taken place.

The course begins with a general review of drag reduction technology. Then the possibility of reduction of skin friction through control of laminar flow is discussed, with design aspects of laminar flow control hardware included. The other possibility of skin friction reduction through modification of the structure of the turbulence in the boundary layer is also discussed.

Methods for predicting and reducing the drag of external stores, of nacelles, of fuselage protuberances, and of fuselage afterbodies are then presented.

Transonic drag rise, the prediction of viscous and wave drag by a method matching inviscid flow calculations and boundary layer integral calculations, and the reduction of transonic drag through boundary layer control are also discussed.

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COMPUTATIONAL DRAG ANALYSES AND MINIMIZATION; MISSION IMPOSSIBLE? by J.W. Slooff National Aerospace Laboratory (NLR) Amsterdam, The Netherlands

SUMMARY

A discussion is given of the possibilities and problems associated with drag prediction, analysis and minimization by means of computational fluid dynamics (CFD) techniques based on inviscid and viscous-inviscid interaction flow models.

Attention is paid to

- classical and computational means of distinguishing between various drag components

- how to obtain values of drag components from currently available CFD codes and the problem of accuracy - examples of computational drag diagnostics

computational drag minimization

- computational drag minimization The discussion is limited, in essence, to sub/transonic transport (wing) aerodynamics, but should, at least partly, also be applicable to sub/transonic serodynamics of fighter sircraft.

INTRODUCTION 1

> The accurate prediction of aircraft aerodynamic drag is a generally recognized and respected problem. So is the accurate measurement of drag in the wind tunnel that, eventually, forms the basis for full scale drag prediction.

In the past 15 years Computational Fluid Dynamics (CFD) has emerged as an additional and complementary tool for aerodynamic design and analysis. The purpose of this lecture is to review and comment on its role as a drag prediction and analysis tool.

The aerodynamic design process of sircraft is characterized by a sequence of design and analysis cycles. In each cycle a (further) reduction of drag will, generally, be one, but not the only objective. Identification of the source of an unacceptably or undesirably high drag level or drag variation with lift or Mach number is a prerequisite for a successful drag reduction program. Identification of drag sources may follow different approaches. The classical or phenomenological one is based on the availability of overall force (wind tunnel) data only. In combination with simple, semi-empirical theory. CFD, as we shall see later, offers possibilities for a more physically/analytically oriented approach in which the various contributions to drag are distinguished by the underlying physical mechanisms rather than by the observed aerodynamic force variation phenomena. The main part of this lecture is directed towards the question of how the various components of drag, that can be destinguished, are modelled by, and can be obtained from the currently available CFD codes. As will be illustrated through examples, accuracy, in this context, is a crucial issue.

will be illustrated through examples, accuracy, in this context, is a crucial issue. It will also be demonstrated that, in spite of its current shortcomings, CFD is a powerful tool for drag diagnostics. The final part of the lecture contains a discussion on computational drag minimization.

2 DRAG ANALYSIS, INTRODUCTORY REMARKS

There are various possible ways of distinguishing between different components of aerodynamic drag,

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 according to the type of force acting on the body, i.e. pressure or friction drag (Fig. 1)
 according to the physical mechanisms that are responsible for drag, i.e. friction, causing "viscous" drag, vortex shedding, responsible for induced drag, and shock wave formation, causing wave drag

(Fig. 2). Viscous drag manifests itself partly as friction drag and partly as pressure drag. The other two as pressure drag only. Neither of the two classifications given above is fully manageable in a situation in which only total force data are available, such as in routine (balance) measurements in a wind tunnel. For which only total force data are available, such as in routine (saiance) measurements in a wind tunnel. For this reason the classical approach to drag analyses is based on the observation of characteristic features in the variation of drag with, e.g., lift and Mach number. We may call this the phenomenological approach distinction is usually made between - (subsonic) minimum drag; C min

- (subsonic) drag-due-to-lift; CDI.
- compressibility drag; ^{AC}D compr
- trim drag; AC_Dtrim

"trim
- miscellaneous drag (due to excressenses, etc); &C_D misc

In other words, the total drag is written as

+ AC_Dtrim + AC_Dmisc $C_{D_{tot}} = C_{D_{min}} + C_{D_{L}} + \Delta C_{D_{compt}}$

(1)

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or a similar expression.

The (subsonic) minimum drag (Fig. 3) and drag-due-to-lift (Fig. 4) are usually defined at some suitable subcritical free stream Mach number such as M = 0.5 or 0.6. Compressibility drag is defined on the same

basis (Fig. 5). As defined above, C_D contains most of the "viscous drag" and some induced drag. However, a distinc-min

tion between the two can usually not be made unless datailed knowledge about the span loading of the wing is available. In preliminary design studies C______ is usually estimated by means of the classical "form min"

factor" methods that, e.g. can be found in Hoerner's Book "Fluid Dynamic Drag", USAF DATCOM and the ESDU data sheets.

The (subsonic) drag due to lift contains most if not all of the induced drag, some viscous drag and, possibly, some wave drag at the higher lift values. It is usually estimated or fitted by means of the classical induced drag formula

[C_L-C_L(C_D)]²)]# с_{р,} = -(2) TÁR

the "Oswald" factor "e" accounting for the deviation of the spanwise load distribution from the elliptical one and for the variation of the viscous drag with lift. Compressibility drag (Fig. 5) contains most if not all of the wave drag, the increase of viscous drag

with Mach number and possibly some induced drag due to changes in span loading with Mach number. A general theoretical basis (apart from CFD means) for the prediction of wave drag does not exist.

Trim drag contains the induced drag increment of wing plus tail due to tail load plus some viecous drag and wave drag. The latter two because the wing, at least for conventional configurations, has to operate at a higher lift coefficient than untrimmed due to the negative tail load. The classical or phenomenological approach, as mentioned, leads to a manageable way of distinguishing

between drag components in case only overall force data are available. A disadvantage 1a, however, that it often remains difficult, if not impossible, to point-out the precise source of an undesirable drag 'surprise". The reason being that these classically distinguished drag components do not reflect one single but, in fact, several physical mechanisms. In this respect an analytical approach to drag snalysis, that distinguishes between the three major physical mechanisms, i.e. friction (viscosity), vortex shedding and shock wave formation, has certain advantages. As we shall see, CPD methods may serve such purpose.

CLASSIFICATION OF CFD METHODS WITH RESPECT TO DRAG PREDICTION POTENTIAL ٦

Prior to going into the details of the possibilities and limitations of computational drag determina-tion it is useful to summarize briefly which drag phenomena are modelled by the mathematical/physical models underlying the currently available CFD codes. Figs. 6 and 7 may serve this purpose. Figure 6 presents the hierarchy of mathematical/physical flow models of interest for applied CFD purposes. Reynolds averaged Navier-Stokes methods can provide both friction drag and pressure drag and, at least in principle, contain all information to distinguish between viscous drag, induced drag and wave least in principle, contain all information to distinguish between viscous drag, induced drag add wave drag. However, because of the very large computational effort required, such methods are not (wit) general-ly available in the applied computational environment, at least for problems involving three dimensions. For this reason we will not pay any further attention to Navier-Stokes methods in this lecture note. On the next level (somal modeling) we must distinguish between inviscid flow and viscous flow (boundary layer) methods. The mutual interaction between the invincid and viscous parts of the flow field

is modelled through an interaction law describing the coupling between the two zones at a suitably chosen boundary.

The boundary layer methods model viscous drag only, subject to the boundary conditions provided by the external inviscid flow through the interaction law.

Three further levels of modelling with decreasing physical significance can be distinguished for invis-cid flow. Methods based on the Euler equations model both induced drag and wave drag. So do methods based on the full potential equation for compressible flow, but as far as wave drag is concerned, in an approximate sense only. The approximation involved implies a limitation to weak or at most moderately strong shocks with a maximum normal Mach number of about 1.3. This, however, is acceptable for many Strong should with a maximum hormar facts number of about 1.3. Into, novel, is accurate for any practical purposes. Figure 8, taken from ref. 1, provides an impression of the accuracy of the potential flow model in relation to the Buler model for a shock Mach number of about 1.3. Linear potential flow methods, such as panel methods, model induced drag only (plus a part of the wave drag in case of linearized supersonic flow).

DETERMINATION OF DRAG FROM CFD CODES

Generally speaking there are two different ways of obtaining drag values from CFD code application. One is the direct integration of pressure and friction forces. We will call this the <u>near-field</u> approach. The other is based on application of the momentum theorem to a control volume enclosing the configuration. We will call this the far-field approach.

4.1 "Near-field" assessment; pressure and friction drag

The accurate determination of <u>pressure drag</u> from wind tunnel pressure measurements is a well respected problem. The following examples illustrate that the problem is of comparable magnitude in CFD; at least in three dimensions, and if one does not have access to a sufficiently fast computer with sufficiently large

Proof a stock for the presence of the pressure drag dependence on mesh d neity for a 2D lifting airfoil with a strong shock wave as calculated with a "state of the art" Euler code employing an O-type mesh (N being the number of mesh points). The results indicate that, for the particular case considered, a 196 x 36 mesh suffices to obtain a pressure drag coefficient value accurate to 1 "count" (10"). (The latter value seems to be widely accepted as a "target" accuracy for drag measurement in wind-tunnel testing). Similar results for a shock-free supercritical sirfoil as obtains with two different Euler codes (of which one with several different distribution of mesh points) and a full potential code are presented in figure 10. All these codes use O-type meshes but with different distributions of mesh points. The message of figure 10 is that the sensitivity of the results for mesh density depende strongly on the distribution of mesh points.

the distribution of mesh points. For Euler code 1 this sensitivity is clearly unacceptably high for the

particular type of mesh used. For Euler code 2 it is seen to vary strongly with the distribution of mesh points. For the full potential code a 192x96 mesh is required for a 1 count accuracy.

It can be concluded from figures 9 and 10 that, with a suitable distribution of mesh points, a 200x50 to 200x100 mesh will generally be sufficient to obtain pressure drag values for 2D airfoils that are, numerically, accurate to 1 count. For the currently available general purpose type of main frame computer this is certainly feasible.

An aspect that may also affect the accuracy of CFD pressure drag prediction is mash extent. The point An appet that may also allet the seturacy of the pressure drag, as computed with a finite volume is illustrated by figure 11 *). Shown is the depence of the pressure drag, as computed with a finite volume type Eular code, on the distance from the airfoil at which the far field boundary condition (in this case free stream plus asymptotic far-field vortex term) is prescribed. The particular case requires a mesh ex-tent of about 100 chords for a 1 count accuracy! (This value would be reduced if a more accurate asymptotic

far field boundary condition is used). A 3D sxample of pressure drag dependence on mesh density is presented in figure 12. The case considered is an application of a modified FLO22 code (Ref. 3) to a transport type wing with transonic flow. About 400 relaxation iterations were performed on each fine mesh plus successive mesh refinement. The figure illu-

relaxation iterations were performed on each fine mesh plus successive mesh refinement. The figure illu-strates that, for the particular C-type mesh utilized in these calculations, something of the order of 540 k mesh points are required for a (numerical) accuracy of 1 count if the calculations are performed for a given lift. The situation is distressingly worse if the calculations are performed for a given angle of attack. Examples such as that of figure 12 serve to illustrate the point that the accurate determination of inviscid pressure drag for 3D wings is currently (almost) impossible in an engineering environment. The general experience is that this applies to finite difference/finite volume type field methods as well as "panel" methods. However, as we shall see later, this does not necessarily mean, that CFD, even now, cannot play a useful role in drag nradicing/antives. play a useful role in drag prediction/analyses studies.

The problem of the accurate prediction of the <u>friction drag</u> by means of boundary layer codes is of a somewhat different nature. Unlike the (current) situation with inviscid flow methods, numerical accuracy (truncation errors) is not the major source of concern in boundary layer calculations, the computational requirements being relatively modest. In boundary layer computations the "absolute" accuracy associated with the particular choice of mathematical/physical model is of greater importance. The most important factors involved are: - type of method ("integral" of "field" method)

- transition and turbulence models

- type of interaction law used ("weak" or "strong")

 type of interaction and used (then to fitting)
 type of flow (attached or separated)
 Examples of skin friction prediction, for low speed flows, are presented in figures 13, 14. In one
 case (Eppler airfoil) the agreement between measured and calculated skin-friction distribution is seen to
 be quite good. In the other case (upper surface of the main airfoil of a high-lift configuration) there is substantial disagreement between theory (4 different methods) and experiment, the reason of which is not clear. These examples illustrate that the accurate prediction of skin friction may not (yet) be taken for granted.

It is the author's general impression that the "absolute" errors involved in friction drag prediction may be as large as 5 to 15 counts for attached flows and possibly larger for separated flows. This, how-ever, does not exclude the possibility to obtain meaningful predictions of friction drag for similar types of flow on similar configuration on an increment/decrement basis.

4.2 "Far-field assessment (momentum theorem)

Expressions for the drag acting on a body can also be derived by applying the momentum theorem to a control volume enclosing the body. In the following we will do so first for the case of purely inviscid flow and subsequently for inviscid flows with "viscous" interactions and boundary layer/wake flows ("zonal modelling")

4.2.1 Inviscid flow, general expressions

Consider a control volume of the type as indicated (for a half wing) in figure 15. In the far-field Consider a control volume of the type as indicated (for a half wing) in figure 15. In the far-field (s) the volume is bounded by a plane normal to the x-axis far upstream of the wing, a similar plane (far) downstream and planes parellel to the x-z and x-y planes, respectively, each at a large distance from the wing. In the mear-field the volume is bounded by the body (wing) surface (S₀) and (both sides of) the shock-wave (S₁₀) and vortex sheet (S₁) surfaces. The reasons for excluding the vortex sheet from the control volume is in the fact that the Matter must be bounded by a single closed surface. Hence a cut must be introduced between S₁ and S₍₀₎. The vortex sheet is a natural, and, as we shall see later, scenatizes necessary choice for such a cut. The reason for excluding the shock surface will become apparent shortly. Application of the conservation law for momentum to the control volume of figure 15 leads to the integral expression

$$\iint_{\mathbf{r}} [\mathbf{p} \mathbf{n}_{\mathbf{x}} + (\mathbf{p} \mathbf{\hat{q}} \cdot \mathbf{\hat{n}})\mathbf{u}] d\mathbf{s} = 0$$

where

Sec.5

$$S = S_B + S_{aback} + S_{wake} + S_{(w)}$$

.

p is the (local) static pressure, \bar{q} is the total velocity vector, ρ is the density, \bar{n} is the unit outward normal to the control volume (hence pointing inside S_{g} , S_{shock} and S_{wake}) and u is the component in the free-stream (x-) direction of \bar{q} .

*) Figs. 9, 10 and 11 have been derived from data contained by reference 2.

(3)

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Splitting-off the body pressure integral from eq. (3) leads to the following relation for the pressure drag

$$D_{p} = \iint_{S_{B}} p n_{x} d S =$$

$$= - \iint_{S \leftarrow S_{B}} [p n_{x} + (p \bar{q}.\bar{n}) u] dS - \oiint_{B} (p \bar{q}.\bar{n}) u d S$$

$$= - \iint_{S \leftarrow B} [p n_{1,x} + (p \bar{q}.\bar{n}_{1}) u]^{\frac{1}{2}} d S +$$

$$S_{abock}$$

$$= - \iint_{S \leftarrow B} [p n_{1,x} + (p \bar{q}.\bar{n}_{1}) u]^{\frac{1}{2}} d S +$$

$$= - \iint_{S \leftarrow B} [p n_{1,x} + (p \bar{q}.\bar{n}_{1}) u]^{\frac{1}{2}} d S +$$

$$= - \iint_{S \leftarrow B} [p n_{x} + (p \bar{q}.\bar{n}) u] d S +$$

$$= - \iint_{S \leftarrow B} [p n_{x} + (p \bar{q}.\bar{n}) u] d S +$$

$$= - \iint_{S \leftarrow B} [p n_{x} + (p \bar{q}.\bar{n}) u] d S +$$

$$= - \iint_{S \leftarrow B} [p n_{x} + (p \bar{q}.\bar{n}) u] d S +$$

denotes a jump of the particular quantity across the particular surface of discontinuity. Here [Note that, in the case of zero normal mass flux on the body and vortex sheet, which we will consider first, both I, and the second part of I, are zero. Note also that eq. (5) is equally valid in "full potential" flow and "Euler" flow. However, the various terms distinguished in eq. (5) have different meanings in these two flow models.

(5)

two flow models. In the (time-dependent) <u>Euler codes</u> that are currently available, momentum, as well as mass and energy, are conserved in the whole of the flow field, including shocks and vortex sheets. The latter two are captured as narrow regions with high velocity gradient rather than discontinuities as a result of the numerical and artificial dissipation associated with the discretization schemes that are being used. Within these layers momentum is conserved to the (numerical) accuracy implied by these schemes. It follows that in the Euler flow model the integrals I, and I, of eq. (5), assuming vanishing truncation errors, are identi-cal to zero. As already mentioned, the fourth integral (I₄) is also zero in case of zero normal velocity on S₂. Hence, the remaining term I₂, i.e. in the far-field integral, contains both the wave drag and the induced drag. induced drag.

In (conservative) potential flow models mass as well as energy (and entropy) are conserved across shock waves, (or rather the shock layers that result from the numerical schemes), but momentum normal to the shock is not. The latter, in fact, is the very mechanism for the production of wave drag in potential flow models, as described by Steger and Baldwin, Ref. 6 (see also Van der Vooren and Slooff, Ref. 7). It also constitutes the reason for excluding the shock surface from the momentum control volume. In spite of the non-physical nature of this seemingly strange mechanism, potential flow methods generate useful numbers of "wave drag" as long as the component of the local Mach number normal to the shock does not exceed a value of say, 1.3. The point was already illustrated by figure 8.

value of say, 1.3. The point was already illustrated by figure 8. From the discussion just given it follows, that in the potential flow model, the integral I in eq. (5) is different from zero and represents (an approximation to) the wave drag. The far-field integral I, now contains the induced drag only. The integral I, as mentioned, is zero in case of zero normal mass flux on S. Remains to discuss the "wake" integral I, for the potential flow case. In the currently available potential flow codes' it is general practica to model the vortex sheet as a (curved) plane of discontinuity, coinciding with a plane of the computational mesh, that carries a jump in potential. The jump in potential is taken to be constant along the mesh lines in this plane which coincide, approximately, with the free stream direction. In addition the difference formulae utilized on both sides of this "vortex sheet" are chosen such that there is continuity of normal mass flux across the "vortex sheet". An implication of this is, that the "flux" term of momentum is continuous across the vortex sheet discontinuity by identical to zero in potential flow calculations with a priori selected fixed position of the vortex sheet. The author is not aware of any numerical assessment of this term, which, indeed, is generally neglected. term, which, indeed, is generally neglected.

4.2.2 The evaluation of wave drag and induced drag from potential flow codes

In the preceeding paragraph we have seen that, in potential flow, the <u>wave drag</u> can be determined, at least in principle, by integrating the jump in momentum across the shoc surface(s), (term I, of eq. (5)). In practice it appears that the accurate determination of the wave drag along these lines poses several difficulties

First of all, as noted before, shocks are smeared by numerical capturing schemes. This problem can be overcome by enlarging the contour of integration to ensure that the shock is completely enveloped and calculating the loss of momentum within this contour. Figure 16 shows permissible contours of integration.

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The major problem associated with calculating the wave drag along these lines is the accurate numerical evaluation of the integral. It has been found (Yu, et.al., Ref. 8) that very fine meshes are required to perform the integration with acceptable accuracy and that the relaxation process for solving the flow equations must be continued to iteration levels that are far beyond those of current engineering practice. The reason for the latter is in the fact that any mass flux residual (source of sink like) acts as a spurious drag of thrust source. This must either be avoided by a large number of iterations or be corrected for, see reference 8. Making use of the mass conservation law applied to the contour $S_{\rm shock}$ (Fig. 16)*), i.e.

 $- \oint_{S=hock} \rho \, \bar{q} \cdot \bar{n} \, dS = R_{shock} \tag{6}$

where $R_{\rm shock}$ represents the sum of the residual sources in the flow field within S shock, the integral I of eq. (5) can be written as

$$I_{I} = - \oint [p n_{x} + (u - u_{u}) \rho \bar{q} \cdot \bar{n}] dS + u_{w} R_{shock}$$

$$S_{shock}$$
(7)

With the second term of (7) representing the drag or thrust associated with any residual sources within S shock' the first term represents the wave drag. I.e.:

$$D_{\text{wave}} = - \iint_{\mathbf{x}} [p n_{\mathbf{x}} + (u - u_{\mathbf{w}}) \rho \bar{q} \cdot \bar{n}] dS = I_{1}^{*}$$
(8)

The problem of accuracy is illustrated by figure 17 which was taken from reference 8. For a transport type of wing-body configuration with a mesh which is typical for current engineering practice, the calculated wave drag varies between 34 and 59 drag counts, depending on the integration contour selected. Evidently much finer grids (possibly of the order of (.5 to 1) x 10 gridpoints) are required to calculate the wave drag in this way with acceptable accuracy.

An interesting alternative way of evaluating the wave drag from potential flow codes has been proposed by Garabedian et.al., Ref. 9. They have shown that the integration of the artificial viscosity term over the supersonic part of the flow field provides a measure of the wave drag.

As discussed in section 4.2.1 the <u>induced drag</u> in potential flow is represented by the term I_3 of eq. (5). In analogy with the shock integral I_1 , the term I_3 can be rewritten as

$$I_{3} = - \oiint [p n_{x} + (u-u_{x}) \rho \bar{q}.\bar{n}] dS + u_{x} [\oiint \rho \bar{q}.\bar{n} dS - R_{(\omega)}]$$

$$S_{(\omega)} \qquad S_{B}^{+S} wake \qquad (9)$$

with R (...) defined by

$$\oint_{S_{(m)}} (p \bar{q}.\bar{n}) dS + \oint_{B} p \bar{q}.\bar{n} dS = R_{(m)}$$
(10)
$$S_{(m)} \qquad S_{B}^{+S} wake$$

With the second term of eq. (9) again representing the drag acting on intentional and/or spurious sources, (within $S_{(m)}$), the induced drag is given by

$$D_{i} = - \oiint [p n_{x} + (u - u_{n}) \rho \bar{q}, \bar{n}] dS = I_{3}^{\prime}$$

$$S_{(n)}$$
(11)

In finite volume type of potential flow codes this integral can be evaluated on suitably chosen grid boundary planes. The experience appears to be (Ref. 8) that this can be done with acceptable numerical accuracy.

An alternative is to let the boundary surface $S_{(\infty)}$ of eq. (11) go to infinity in which case the integral reduces to the "Trafftz-plane" (x=+ ∞) integral:

$$D_{i} = - \iint_{x \to \infty} [(p - p_{\omega}) + (u - u_{\omega}) \rho u] dS$$
(12)

Assuming small perturbations in the "Trefftz-plane", eq. (12) may be further simplified to the classical result (see figure 18)

$$D_{1} = \int \left[\left[\bullet \right] \right] \cdot \overline{q} \cdot \overline{n}_{vake} dt$$

$$S_{under} \cap x = 0$$
(13)

For details of the derivation and approximations involved see e.g. Lock, Ref. 10. Note that eq. (13) can be used to calculate the drag from finite difference/finite volume type of calculations as well as from linear, panel type methods.

While the small perturbation assumptions on which eq. (13) is based are violated for high lift and low aspect ratio, and possibly at the (tip) edge of the vortex sheat in any case, the general experience (including the author's) is, that it leads to induced drag values of acceptable accuracy in many if not most practical cases.

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*) Note the positive direction of the normals on S shock and S t

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4.2.3 The evaluation of drag from Euler codes

As discussed in section 4.2.1 the integral I_3 of eq. (5), or eq. (9), contains both the wave drag and the induced drag in "Euler flow", (as well as the drag associated with any spurious or real mass sources inside the flow field). Reportedly (Ref. 8), the numerical evaluation of the far field integral in Euler codes can be performed with acceptable accuracy in 2D, but not in 3D. The main problems seem to be in-appropriate (far-field) boundary conditions, at least for this purpose, and lack of resolution due to the relatively small number of mesh points that can be afforded in engineering applications.

Splitting the total inviscid trag from the far-field integral into wave drag and induced drag parts is not a trivial matter. As discussed by Lock (Ref. 10) it can be done only under certain simplifying assump-tions. To the author's knowledge it has not (yet) been attempted in actual 3D Euler applications. In the latter the problem is further exhanced by the fact that vortex sheets are captured as shear layers rather than discontinuities. Further exploration of the possibilities along these lines deserves attention.

A separate evaluation of the wave drag is possible by considering the entropy production of shock waves, or, rather, the entropy produced within a contour enveloping the numerically smeared shock layers (Fig.

For this purpose use can be made of an expression originally derived by Oswatitach (Ref. 11)

 $D_{wave} = \frac{T_{w}}{q_{w}} \int (\tilde{s} - \tilde{s}_{w}) \rho \bar{q} \cdot \bar{n} ds$ shock (14)

(S denoting entropy and T the freestream temperature). or variants thereof (see also Ref. 10). The experience appears to be (Ref. 8) that eq. (14) can be evaluated with acceptable accuracy in 2D but not (yet) in 3D. The main problems being spurious entropy production (dissipation) associated with the numerical schemes, in particular near the flow boundaries, and lack of resolution (mesh points). Summarizing the discussion on Euler codes we may conclude that the problem of determining drag with

acceptable accuracy is even more severe than for potential flow codes. In particular if distinction between wave drag and induced drag is the objective.

4.2.4 Zonal modelling

Assessing the various components of drag becomes more complicated when the effects of viscosity in the flow field are taken into account by matching the outer inviscid part of the flow field with the (inner) viscous or boundary layer part through an appropriate interaction law (zonal modelling). It appears, see Lighthill, Ref. 12, that there are several alternative ways for matching. However, the most convenient, and indeed most commonly adopted possibility, is to simulate the displacement effect of the boundary layer and wake on the outer inviscid flow through imposing a "transpiration mass flux" boundary condition on the body surface and wake centerline or vortex sheet. In the "weak" interaction formulation, which is applicable to attached flows only, the transpiration mass flux at the body surface and on the vortex sheet in the invis-cid flow, and the tangential mass flux at the edge of the boundary layer in the boundary layer flow, are cia flow, and the tangential mass flux at the edge of the boundary layer in the boundary layer flow, are chosen such that the normal and tangential mass flux components in both the inviscid and boundary layer flow match at the location S_{\pm} , figure 20, of the edg of the boundary layer and wake. In the "strong" interaction formulation, which is (also) applicable to separated flows, the sequence of "inviscid" and "viscous" calculations (interaction law) is chosen differently for reasons of computational stability and efficiency, with, however, the same objective of matching the inviscid and boundary layer flow at the edge of the hundary layer (are a constant).

efficiency, with, however, the same objective of matching the inviscid and boundary layer flow at the edge of the boundary layer (see, e.g. Refs. 13, 14). With zonal modeling in the sense described above, we have, in the inviscid part of the flow problem, apart from the actual inviscid flow outside the surface S_{dge} , an "equivalent" inviscid flow inside of S_{dge} . In the real v' < cous flow, the region within S_{dge} is of course, occupied by the boundary layer and wate. In case the boundary layer and wake flow are modelied by the "classical" boundary layer equations there are no pressure gradients across the boundary layer and wake. However, triple deck theory for turbu-lent boundary layers (for a survey see, e.g. Ref. 14) teaches that normal pressure gradients are not negli-gible near the trailing edge, near separation lines and where shock waves intersect the boundary layer. The formulations given below are chosen such that they also cover the case with normal pressure gradients in the viscous flow.

With the purpose of relating "edge" and body/wake quantities we will now apply the momentum theorem first to the equivalent inviacid flow within S $_{edge}$ (Fig. 20). It reads

Note that, for the same reasons as discussed in sections 4.2.1 and 4.2.2 we have excluded the shock(s) from the area of integration.

Distinguishing the various parts of the area of integration eq. (15) can be written as

$$\begin{array}{c} \begin{array}{c} & & & \\ & & & \\ & \\ & & \\$$

With the abbreviations introduced above, eq. (16) can be rewritten as

$$D_{p_{eq.inv}} - \delta I_{1,inv} - I_2 - I_4 + \iint_{\rho uu d S} = D_{p_{edge}} + I_{4,edge}$$
(17)
$$\delta S_{(\infty)}$$

or, making use of eq. (5), (D of eq. (16), (17), being identical to D of eq. (5)), $p_{eq.inv}$

$$I_1 - \delta I_{1,inv} + I_3 + \iint_{\delta S_{(\infty)}} \rho uu d S = D_{p_{edge}} + I_{4,edge}$$
(18)

Eq. (18) relates the "far-field" and "edge" quantities of the "outer" inviscid flow.

We now apply the momentum theorem to the viscous flow within S $_{edge}$ (Fig. 21). This gives

$$\int_{B} \int_{B} \int_{$$

In eq. (19) $\tau_{\rm v}$ represents the x-component of the frictional force, capital U the x-component of the total velocity in the viscous flow. The total drag D on the body can be written as tot.

$$D_{tot.} = \oint_{B} \left[p n_x + \tau_x \right] dS = D_p + D_p$$
(20)

or, using eq. (19)

٠,

$$D_{tot.} = \iint_{S_{B}} (\rho \ \bar{q}.\bar{n}) \ U \ d \ S + \int_{S_{B}} \int_{$$

Note that in the case with normal pressure gradients the pressure drag in the viscous flow, D , is not identical to the pressure drag in the equivalent inviscid flow D P_{visc} $P_{eq.inv}$ Note further that without mass transfer ($\rho \ \bar{q} . \bar{n} = 0$), and/or zero slip (U = 0), the first term of eq. (21) is zero.

^{*)} As discussed in section 4.2.2 the smearing of shock waves by numerical schemes requires the jump integral δI_1 , like I_1 itself, to be replaced by a (closed) contour integral.

Since $\tau = 0$ at the edge of the viscous region, and far downstream, and with the abbreviations intro-duced above, π (see also eq. (16)), eq. (21) can be rewritten as

$$D_{tot.} = \delta I_{1,visc} + D_{p_{edge}} + I_{4,edge} - \iint_{\delta(=)} \rho UU d S$$
(22)

or, using eq. (18)

$$D_{tot.} = I_1 - \delta_* I_{1,inv} + \delta I_{1,visc} + I_3 + \iint_{\delta S_{(m)}} [\rho_{inv} uu - \rho UU] d S$$
(23)

expansions. In actual numerical calculations the shock, as mentioned before, is smeared over several meshe and both "shock correction" terms are usually ignored. Returning to the expression (23) for the total drag we will now try to distinguish further between wave drag, vortex (or induced) drag, and viscous (boundary layer) drag and drag due to possible spurious residual sources within the flow field. For this purpose we first rewrite eq. (23) by introducing the ex-pressions (7), (8) for I_1 , the corresponding expressions for $\delta I_{1,inv}$, and (9) for I_3 , giving

$$D_{tot} = I_{1}^{i} - \delta I_{1,inv}^{i} + \delta I_{1,visc} + u_{\omega} (R_{shock} - \delta R_{shock})$$

$$- \iint_{S_{(\omega)}} [p n_{\chi} + (u - u_{\omega}) (\rho \bar{q})_{inv} \cdot \bar{n}] d S - u_{\omega} R_{(\omega)} +$$

$$+ u_{\omega} \iint_{S_{B}^{AS} wake} (\rho \bar{q})_{inv} \cdot \bar{n} d S + \iint_{\delta S_{(\omega)}} [\rho_{inv} uu - \rho UU] d S \qquad (24)$$

From the matching requirement that the mass fluxes outside the boundary layer and wake are equal in inviscid and viscous flow it follows that

$$\oint_{S(=)} (\rho \ \bar{q})_{inv} \cdot \bar{n} dS - \iint_{\delta S(w)} \rho_{inv} u dS = \oint_{S(=)} (\rho \ \bar{q})_{visc} \cdot \bar{n} dS - \iint_{\delta S(w)} \rho U dS$$
(25)

or, since, (eq. (10)),

also that

With (27), the expression (24) for the total drag finally takes the form

 $D_{tot.} = I_1' - \delta I_{1,inv}' + \delta I_{1,visc} + u_{\omega} (R_{shock} - \delta R_{shock}) +$

$$- \iint_{S_{(m)}} [p n_{x} + (u-u_{n})(p \bar{q})_{inv} \cdot \bar{n}] d S +$$

$$+ \iint_{\delta S_{(m)}} [u-u_{n})(p_{inv} u - p U) d S +$$

$$+ \iint_{\delta S_{(m)}} [u-U) p U d S$$

(28)

As before, we will consider the meaning of the various terms in eq. (28), in particular for the situation that the downstream boundary $(\delta)S_{(m)}$ of the control volume tends to infinity.

It follows from the preceding discussions that in case the outer inviscid flow is modelled by the <u>potential</u> equation the wave drag is modelled by the terms $I_1^{-\delta}I_{1,ny}^{+} + \delta I_{1,visc}$ and the induced drag by the term $I_1^{-\delta}$. Considering the term I_1 is may be noted that in two-dimensional flow $\delta u^{-\omega}$, so that I_e^{+0} . In three dimensions with lift this is not exactly the case because of the flow perturbations induced by the trailing vortices. However, as indicated, a.o. by Lock (Ref. 10), the magnitude of the factor $(u-u_n)$, is generally negligible, except, perhaps for high lift and small aspect ratio. It is further noted, that the factor $(\rho_{inv} u-\rho U)$, when integrated over δS_{inv} , is of the order of the displacement volume of the wake. Hence I_{inv} if all probability, can be asfely neglected in most practical cases. The term I_6 , obviously, represents the viscous drag. We will return to this term in section 4.2.5.

In case the outer inviscid flow is modelled by means of the <u>Euler</u> equations we have, as mentioned before, $I_1 - \delta I_1$, $+ \delta I_1$, $+ \delta I_1$, - 0, while I_1 contains both the induced drag and the wave drag of the equi-valent inviscid¹Tlow. While³ $I_1 + 0$ for potential flow, at least in two dimensions, it is, in general, $\neq 0$ in case of Euler flow because $u \neq u_0$ in the wake of shock waves. Hence, I_s , like the term(s) δI_1 in potential flow, can be considered as a (viscous) correction to the inviscid wave'drag. It takes account of the fact that the wave drag associated with those parts of the shock waves of the equivalent inviscid flow within S_1 should be subtracted from the total "inviscid" wave drag. The author is not aware of any quantitative of dimensical assessment of this term. The term I_s again models the viscous drag. It should be noted that if the downstream end of the control volume is taken at a finite distance from the configuration it is no longer possible to identify the warious drag sources (induced/vortex, wave, viscous drag) directly and uniquely with the terms of e. (28).

viscous drag) directly and uniquely with the terms of eq. (28).

4.2.5 Viscous drag

As mentioned above, the viscous or boundary layer drag is represented by the term I_{c} of eq. (28), or

$$D_{visc} = \iint_{\delta S} (u-U) \rho U d S (= I_6)$$
⁽²⁹⁾

Evaluation of eq. (29) requires, in the general case, a method for the calculation of three-dimensional wakes. The problem is, however, that, even for planar, i.e. non-rolling-up wakes such methods are not generally available.

Limiting the discussions to wings, the approximate procedure that is usually followed to circumvent this problem is to compute the boundary layer, and, if possible, the wake, up to the trailing edge or some finite distance downstream of the trailing edge and to extrapolate the development of the viscous wake to downstream infinity.

For this purpose, eq. (29) is replaced by

$$D_{visc} = \rho_{\omega} u_{\omega}^{2} \int_{-\theta_{\omega}} (y') \, dy'$$

$$S_{wake} \prod x^{-i\omega}$$
(30)

where

 $\theta_{\omega}(\mathbf{y}') = \int_{1}^{+\infty} \left(\frac{\mathbf{u}}{\mathbf{u}_{\omega}} - \frac{\mathbf{U}}{\mathbf{u}_{\omega}}\right) \frac{\rho \mathbf{U}}{\rho_{\omega} \mathbf{u}_{\omega}} dz'$ (31)

is the (local) momentum thickness at downstream infinity. (y',z') are coordinates along and normal to the wake in the plane $x^{\mu+\omega}$. Note that the expressions (30), (31) are applicable only in the case of planar, i.e. wing-like wakes.

In two-dimensional flow, the classical Squire and Young method (Ref. 15) or variants thereof are usually applied to relate θ_{α} to the momentum thickness $\theta(\mathbf{x})$ calculated by means of a boundary layer/wake method at some finite distance from the trailing edge. Under the assumption that the shape function H varies linearly with ln U , (U being the velocity at the edge of the boundary layer), the Squire and Young method leads to the expression (in "boundary layer" notation)

$$\theta_{m} = \theta(\mathbf{x}) \begin{bmatrix} \frac{T_{0}(\mathbf{x})}{T_{0}(\mathbf{x})} \end{bmatrix} \begin{bmatrix} \frac{1}{\gamma-1} & 2 + \frac{H(\mathbf{x}) + H(\mathbf{x})}{2} \\ \begin{bmatrix} U_{0}(\mathbf{x}) \\ U_{0}(\mathbf{x}) \end{bmatrix} \end{bmatrix}$$
(32)

The procedure used for 3-D wings is generally similar to the one described above. In this case $\theta(x)$ is

The procedure used for 3-5 wings is generally similar to the one described above. In this case $\sigma(\mathbf{x})$ usually taken as θ_{m} at the trailing edge and some extended form of the Squire and Young method, derived for infinite yawed wings, is used at each span station to relate θ_{m} to θ_{m} (see e.g. Lock, Ref. 10). It is appropriate at this point to stress the point that the basic assumptions underlying the Squire and Young method are not valid in case of (highly) asymetric vakes (aft-loaded airfoils), wakes in (strong) pressure gradients and highly three-dimensional wakes. In such conditions methods of the type (strong) pressure gradients and highly three-d sketched above should be applied with caution.

Figures 22, 23 illustrate results of an application of the procedure to a 3D transport type wing and a comparison with experimental (wake rake) data (Ref. 16). A fully three-di encional boundary layer code was used to calculate θ upto the trailing edge.

Figure 23 illustrates that even for a relatively simple case as that of figure 22 the difference between calculated and measured viscous drag may be substantial. Although there are numerous potential sources of error in, at least, the computational methods and procedures involved, the precise origin of such discrepancies is by no means clear.

An example of viscous drag prediction for a fairly complicated 2D case (airfoil with flap at low speed, from Ref. 17) is reproduced in figure 24. The figure serves the purpose of illustrating that turbu-lence modelling is of crucial importance for wakes in strong longitudinal pressure gradients such as occur in the main wake of flapped airfoils.

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4.3 Cross-checking near-field and far-field values

In view of the inaccuracies and uncertainties discussed and illustrated above, it is advisable to compute the different components of drag in as many ways as possible and compare the results (vis. figure 25). Differences between drag component values computed in different ways may provide an indication of the error levels that are possibly involved.

On the inviscid side, an obvious check is to compare the integrated (near-field) pressure drag against the sum of the induced drag and wave drag as obtained from the (far-field) momentum considerations. Eq. (5)

represents the basic equation for such a check. In case of <u>potential flow</u> it may be more convenient to rewrite eq. (5) in terms of the expression (7), (8) and (9)-(13) for the (corrected) wave drag and induced drag. This yields

$$D_{p_{eq.inv}} = I_1' + u_m R_{abock} + I_3' + u_m \left[\iint_{S_B + S_{wake}} \rho \bar{q} \cdot \bar{n} d S - R_{(m)} \right] - \iint_{S_B + S_{wake}} \left[p n_{1x} \right]_2^1 d S - \iint_{S_B + S_{wake}} (\rho \bar{q} \cdot \bar{n}) u d S$$
(33)

 $D_{Peq.inv} = D_{wave} + D_i + \bigoplus_{s=s}^{0^n} (u_w - u) \rho \bar{q} \cdot \bar{n} d s + S_{B+S}^{s} wake$ $- \iint_{\mathbf{p}} \left[p n_{\mathbf{I}\mathbf{x}} \right]_{2}^{1} d S - u_{\omega} \left[R_{(\omega)} - R_{shock} \right]$ (34)

with D given by eq. (8) and D, by eq. (11), (12) or (13). The third term on the right hand side of eq. (34), is non-zero in case of surface (and wake) "transpiration" only. It can be interpreted as the pressure drag (of the equivalent, inviscid flow) induced by the viscous displacement effect (D_{rac}) . The fourth term, D , represents the effect of a pressure jump across the inviscid wake discontinuity Pwake

(vortex sheet). It is zero in case of a fully relaxed vortex sheet and vanishing viscous wake thickness or viscous wakes with zero normal pressure gradients (see also section 4.2.1). The terms R, and R, re-present the effect of possible residual sources inside the flow field (section 4.2.2). They are, of course,

zero in case of a fully converged solution. In case the inviscid flow is modelled by the <u>Euler</u> equations it follows, from the discussion of sections 4.2.1 through 4.2.3, that the corresponding expression is

$$D_{\text{peq.inv}} = I_3^{*} + \iint_{S_B^{+S_{\text{wake}}}} (u_{\underline{u}} - u) \rho \bar{q}.\bar{n} d s + \\ - \iint_{S_{\text{wake}}} D_{\text{pwake}} - \\ - \iint_{S_{\text{wake}}} \left[p n_{1x} \right]_2^1 d s - u_{\underline{u}} R_{(\underline{u})}$$
(35)

with I_3^* (eq. (11)) containing both the wave drag and the induced drag.

With 1; (eq. (1)) containing both the wave arag and the induced arag. In viscous flow a similar check can, of course be performed by computing the total drag by integrating the surface pressure and skin friction, eq. (20), as well as by eq. (28). An additional checking possibility is obtained by eliminating I'₃ from eqs. (28) and (33), (34),

leading to the general expression,

$$D_{P_{visc}} + D_{F} + \delta I_{1,inv} - \delta I_{1,visc} + u_{\omega} \delta R_{shock} - I_{5} - I_{6} = D_{P_{eq,inv}} - D_{\delta^{*}} - D_{vake} + u_{\omega} R_{(\omega)}$$
(37)

In case of potential outer flow we have $I_{s} \rightarrow 0$, at least in two dimensional flow (cf. section 4.2.4). In case of "Euler" outer flow this reduces to

$$D_{p} + D_{p} - I_{5} - I_{6} = D_{p} - D_{6*} - D_{p} + u_{m} R_{(m)}$$
visc eq.inv vake (38)

Note that, in the absence of shock waves, with zero normal pressure gradients across boundary layer and wake, and with zero mass flux residual, eqs. (37), (38) reduce further to

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or

$$I_6 (=D_{visc}) - D_F = D_{\delta s}$$

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expressing that the total viscous drag minus the friction drag equals (should equal), the pressure drag due viscous effects.

4.4 Engineering approach to computational drag analysis

In the preceeding sections we have seen that we are still far from a situation in which we can compute drag with acceptable absolute accuracy. An additional problem is that the majority of the available inviscid flow codes provide values for integrated pressure drag only, so that a division into wave drag and

inviscid flow codes provide values for integrated pressure drag only, so that a division into wave drag and induced drag is not readily svailable. In spite of this situation it has proven to be possible to devise engineering procedures for deter-mining drag from CFD codes with usable accuracy; at least in applications where drag <u>increments</u>, due to (small) changes in flow conditions or geometry, rather than absolute accuracy is the subject of interest. Examples of such procedures may be found in a.o. Refs. 3 and 18. In Ref. 3 the induced drag of a wing-body configuration is calculated from Trefftz-plane considera-tions, utilizing the spanwise distribution of circulation obtained from a potential flow code and assuming that there is no workied in order the badd

that there is no vorticity shed from the body.

that there is no vorticity shed from the body. The following procedure is used to obtain an estimate for the wave drag. First, the total inviscid drag of the wing as determined from integrated pressures is compared with the induced drag of the wing for a number of subcritical flow conditions. Assuming that the induced drag is determined with sufficient accuracy this comparison yields a correction ΔC_D for the pressure drag which is expressed as a function of p

wing lift and Mach number as follows,

$$\Delta C_{D_{p}} = C_{0} + C_{2} (C_{L \text{wing}} + C_{1})^{2} + C_{3} H_{2}^{2} + C_{4} (1 - H_{2}^{2})^{-b_{2}} + C_{5} H_{2}^{2} C_{L}^{2}$$
(40)

The quadratic C₁-term in (40) is suggested by the fact that the induced drag (and hence, in subcritical flow, also the pressure drag) is a quadratic function of the lift; one would expect the error in this to be proportional to the level of the induced drag. The terms with H_{a}^{b} and $(1 - H_{a}^{2})^{-2}$ are suggested by the Rayleigh-Janzen H_{a}^{2} -expansion theory and Prandtl-Glauert theory, respectively. The cross-term $H_{a}^{2}C_{a}^{2}$ is merely empirical.

The constants C_0 to C_s are determined by equating the corrected pressure drag and the far-field induced drag for six subcritical flow conditions involving three different C_s -values and three Mach numbers. The experience is that in this way the corrected pressure drag in the whole subcritical flow regime can be determined with an accuracy of a few drag counts. With the constants C_0 to C_s known the correction formula (40) is also used to correct the pressure drag in supercritical flow conditions. For supercritical flow conditions the wave drag is then determined by subtracting the induced drag of the wing from the converted experience drag of the wing from the corrected pressure drag, 1.e.

$$C_{D_{wave}} = C_{D} + \Delta C_{D} (M_{w}, C_{L}) - C_{D}.$$
(41)

Note that the procedure assumes that wave drag is generated by the wing only. An alternative for the "pressure drag error extrapolation" technique described above may be to use a mesh density extrapolation procedure of the type illustrated by figure 12. The pressure drag error extrapolation procedure of Ref. 3 forms part of a fairly complex system of computer programs for the prediction of the aerodynamic characteristics of wing-body configuration in transonic flow (Fig. 26). In this system wing viscous drag is computed by a fully 3D finite difference type of boundary layer code in combination with an extended form of the Squire and Young method (section 4.2.5). Figure 27 provides comparisons of measured and computed drag for a narrow-body transport configuration, ob-tained through the system of figure 26, illustrating the usefulness of the drag prediction procedure. Note that the variation of drag with lift and Mach number is predicted reasonably well as long as the flow is attached; even the absolute drag level is fairly close if the computed wing drag is added to the (viscous) drag of the body alone as measured in the wind tunnel. Further examples may be found in ref. 3. The pressure drag extrapolation technique may also be used wing section vise to obtain estimates for

The pressure drag extrapolation technique may also be used wing section wise to obtain estimates for the distribution of wave drag along the span of the wing. Additional information provided by the system of figure 26 contains boundary layer and wing section viscous drag quantities (Fig. 28) and, of course, detailed pressure distributions.

5. COMPUTATIONAL DRAG MINIMIZATION

The past decade has seen repeated efforts, some (partly) succesful, others less so, to directly ine past decade has seen repeated erforts, some (partiy) successing, others less so, to directly address the problem of drag minimization by combining computer codes for aerodynamic (drag) analyses (flow solvers) with numerical optimization algorithms. The objective being that the optimization algorithm con-trols variations of a number of independent variables, such as parameters defining the geometry, with the purpose of finding the particular combination of parameters that, subject to given constraints, leads to a minimal drag. In this process, the function of the flow solver is to provide drag values for each combina-tion of values of the independent variables that is considered to be feasib e and "interesting" by the optimization algorithm.

Generally speaking computational (or numerical) drag minimization requires - a choice of object function (in this case the drag, but other choices are possible)

- a flow solver (aerodynamic analysis code) - a choice of independent variables

a choice of constraint functions defining that part of the solution space that is considered to be feasible from the engineering or another (e.g. numerical) point of view

- an optimization algorithm.

With respect to the choice of independent variables one may distinguish two different approaches. One, and indeed the most common choice is to use parameters defining the geometry as the independent variables. This requires a direct or analyses type of flow solver only. The approach is generally referred to as direct

direct numerical optimization. While applications of the direct numerical optimization approach have seen the use of various aero-dynamic codes, the feasible directions/gradient optimization algorithm CONMIN/COPES, developed by Vanderplaats (Ref. 19) seems to be used almost exclusively, in particular in combination with transonic flow codes.

The approach, pioneered by Hicks et al (Ref. 20) ows its existence entirely to the availability of large and fast computer systems. Because of the excessively large computational requirements, at least in 3D, the approach is sometimes referred to as "design by brute force". Nevertheless it holds great potential for the future. A reappraisal of the technique has been given by Hicks (Ref. 21). Several chastening experiences are also reported in Ref. 28. A generalized flow diagram of the numerical optimization technique is presented in figure 29. The

A generalized flow diagram of the numerical optimization technique is presented in figure 29. The process is initiated by the choice of an aerodynamic object function F that is to be minimized (in this case the drag) a number of quantities to be constrained G, and a set of design variables. The constraints can be of aerodynamic of geometric nature; e.g. C_1 and/or t/c greater than a specified value. The design variables are generally taken to be the coefficients A_1 of a number of shape functions

 $z = z_0 + \sum_{i=1}^n A_i f_i$ (42)

describing (modifications to) the starting wing geometry. The process begins by perturbing, in sequence, each of the shape function coefficients A. The result-ing n shapes are analyzed by means of the aerodynamic program (determination of F and G_j 's) and the deri-vatives $\frac{\partial F}{\partial A_1}$, $\frac{\partial G_1}{\partial A_1}$, or rather the difference quotients $\frac{\Delta F}{\Delta A_1} = \frac{\Delta G_1}{\Delta A_1}$ are determined. The next step is the formation, by the optimization program, of the gradient ∇F and the determination of the direction of steepest descent of F. in the n-dimensional space formed by the basis vectors A. while satisfying the constraints. The optimization program then executes a number (typically 3) of steps in this direction, with another aerodynamic analyzia performed at each step. until either a constraint is met or F attains a constraints, ine optimization program time accures a pumpt in the constraints in our of a status a mother accodynamic analysis performed at each step, until either a constraint is met or F attains a minimum. In the first case, or when the minimum of F is lower than the previous minimum, the process is repeated; new gradients are determined, etc. When the latest minimum or F is equal to or higher than the previous one the process is terminated.

The optimization process described above requires typically 10 complete cycles or, in other words, 10(n+3) analysis calculations (Ref. 19). This immediately illustrates the weakes, point of the numerical optimization approach. In order to keep the computational effort required within reasonable bounds one has to put severe limitations on the number n of design variables, in particular in 3D flow. The problem is enhanced by the fact that for acceptable convergence of the optimization process it is necessary to avoid "numerical noise" in the partial derivates of the object function (Refs. 23, 24). This requires that the "numerical noise in the partial derivates of the object function (kers. 25, 24). This requires that the relaxation process in each analysis calculation must be continued until the residual has reached a level beyond that which is often customary in "normal" analysis calculations. It also appears to exclude the use of analysis codes with simple boundary layer corrections (Ref. 21). The reason for the latter is that the airfoil aerodynamic quantities do not vary consistently enough when boundary layer and potential flow are coupled in the weak interaction sense.

One way to reduce the number of analysis calculations required in 3D applications is to evolve the design variables in a series of steps (Ref. 26). For example by first designing the upper surface, section by section, going from root to tip and then the lower surface. Clearly it is also important to select a starting geometry having aerodynamic characteristics which are already close to the target. This asks for an information system/data base approach. With previous experience stored in the data base, the latter can be searched for the most suitable starting solution. As described in Ref. 19 the data base, the latter can also be used to speed-up the convergence of numerical optimization by at least a factor two. With the results of <u>all</u> preceding geometry perturbations stored it is possible to construct higher partial derivatives of the object function and utilise higher order gradient methods. With the severe limitations on n, the choice of the shape functions is of utmost importance. The

with the severe indications on n, the choice of the snape functions is of utmost importance. The choice should be directed towards describing a sufficiently wide class of practical solutions. While simple polynomial expressions were used in early applications (Refs. 20, 22) of the numerical optimization con-cept, a more sophisticated class of shape functions describing more local geometry modifications was used in later applications. (Refs. 23, 24, 25). However, as discussed in Ref. 26, there is a need for still better shape functions with even more localized curvature variations. In fact it can be argued that while the shape functions is a sufficient of the schedule of the schedule of the functions of the schedule of the functions of the schedule of the schedule of the schedule of the functions of the schedule of the schedule of the schedule of the schedule of the functions of the schedule of the functions of the schedule of the schedule of the schedule of the functions of the schedule of

better shape functions with even more localized curvature variations. In fact it can be argued that while curvature based shape functions are suitable for areas with subcritical flow, slope based shape functions might be more appropriate in areas with locally supersonic flow. An interesting choice for the shape functions is discussed by Aidala et.al. (Ref. 29). They consider shape functions generated by means of feeding certain pressure distribution modifications into an inverse program. The result is a set of design shapes that are (almost) orthogonal in an aerodynamic sense, that is, affect only one specific pressure distribution characteristic and no other ones. While the choice of the design variables is of great practical significance, the precise choice of the other of the design variables is of great practical significance.

object function, in conjunction with the choice of the serodynamic and geometric constraints, is of both more fundamental and practical interest. In two-dimensional transonic applications (Refs. 19, 20, 22, 23) more fundamental and practical interest. In two-dimensional transonic applications (Refs. 19, 20, 22, 23) it has been customary to minimize the wave drag subject to constraints on, e.g., airfoil thickness or volume, lift and/or pitching moment. Although it is clear that constraints are necessary in a meaningful drag minimization problem it is by no means clear how exactly the problem should be formulated in order to guarantee a unique solution. The problem is illustrated by figure 30, taken from Ref. 19. Shown are the results of two drag minimization runs with identical free stream conditions and identical constraints on lift and airfoil volume. Only the starting solutions differ. As illustrated by the figure the two resulting airfoils are totally different in shape. Clearly the problem, as formulated, has more than one, local minisum and neither of the two necessarily represents the absolute minisum. An interesting discussion on criteris for suitable serodynamic object functions can be found in Ref. 29.

Figure 30, the second airfoil in particular, also illustrates another potential problem of direct (inviscid) wave drag minimization. In the absence of (direct) control over the pressure distribution the solution may acquire unrealistically high pressure gradients, such as near the upper surface trailing edge. A strong point of the numerical optimization approach is the possibility of selecting object functions and constraints suitable for sultipoint designs. An example of a two-point design applications the design of airfoils with low drag creep can be found in Ref. 23. Low speed airfoil design applications are considered in Refs. 27. On It is also primely provide the design of a subscience of the second surface of a subscience of the second surface of a surface considered in Refs. 27, 30. It is also entirely possible to consider, e.g. transonic drag minimization

and low-speed stall requirements simultaneously. While the direct minimisation of drag is feasible in two dimensions, it is hardly so, at present, in the case of three-dimensional wings. Several unsuccessful attempts in this direction can be found in the literature, (Refs. 24, 25, 26). The main reason for this failure is the lack of accuracy in the determina-tion of the drag with the currently available 3D codes and the limited number of mesh points (Chapter 4). Another problem would seem to be that the problem of uniqueness in three dimensions is even more severe than in two dimensions. The accuracy problem may be overcome when more efficient algorithms and/or more computer power (vector/parallel machines) allows the number of mesh points to be increased. The uniqueness problem would probably require the introduction of more constraints or more sophisticated object functions.

Summarizing the discussion on direct numerical optimization, it may be said that the potential possibilities of the approach are enormous with, at present, unique capabilities such as multi-point and con strained design. However, the approach is also unique in terms of required computer resources. Substantial improvements in both flow optimization code algorithms and/or computer efficiency, relative to current eral standards, are required before numerical optimization in 3D wing design can be used on a routine bases.

An alternative possibility for computational drag minimization is to use serodynamic (load and pressure distribution) rather than geometric shape functions as independent variables. In this approach an pressure distribution) rather than geometric shape functions as independent variables. In this approach an optimization algorithm is used to optimize the pressure distribution, s.g. with the objective to winnize the drag. Using the latest available estimate of the geometry this can be done relatively cheap through an induced drag (Treffix plane) and a boundary layer code. While this approach implies direct control over induced drag and viscous drag it does not so with respect to wave drag. However, wave drag may be controlled indirectly by imposing constraints on the minimum pressure or maximum upper surface Mach number. With the target C -distribution established the new geometry can be determined by means of an inverse code. Subsequently the Sif-design characteristics can be determined by means of an inverse code. is repeated when the new geometry differs significantly from the previous one or when a geometry or off-design constraint is met. In the latter cases (new) constraints will have to be imposed on the values of the parameters describing the pressure distribution. A flow chart of the process, which is called inverse parameters describing the pressure distribution. A flow chart of the procedure, which is called <u>inverse</u> <u>numerical optimisation</u>, (Ref. 31), is given by figure 31.

An example of a method which fits into the framework of inverse numerical optimization is one for determining the spanwise loadings for minimum induced drag on lifting parts of multiple, non-planar config-urations (Ref. 32). The program utilizes constrained optimization techniques and panel method "technology" in the Treffts-plane. It is capable of dealing with pitching moment (trimmed situation) and bending m constraints.

The input required by the program is summarized in figure 32. It comprises general geometric config-uration data, position of the center of gravity, required (trimmed) lift coefficient, wing, body and tail pitching moment and drag data.

A typical example of the capabilities of the program is presented in figure 33. Figure 33a illustrates the type of configuration considered, with various vertical positions of the horizontal tail. Optimum spanwise load distributions for a high and a low positioned horizontal tail for a given wing-

optimum spanules load distributions for a high and a low positioned horizontal tail for a given wing-body pitching moment and 30 % MG c.g. location are compared in figure 33b. It illustrates the point that optimal wing design cannot be achieved without taking account of the tail configuration. Minimum induced drag span loads for two different levels of wing-body pitching moment for a low tail configuration are compared in figure 33c. Figures 33d and e illustrice the point that the minimum trimmed induced drag of high tail configurations is much more sensitive to variations in wing-body pitching moment and c.g. positions than that of low tail configurations. This, however, does not necessarily imply that a low tail configuration is to be preferred; there may be other design criteris that dominate this choice. that a

In conclusion, figure 33f presents the optimum span load for a configuration which utilizes "active" loading of nacelle/pylon and flap rail fairings. In the particular example a 1.5 % reduction of the minimum trimmed induced drag can be realized by "active" rather than "passive" (streamline) shaping of pylons and flap rail fairings.

The program has been exten nded recently with an airfoil characteristics data base allowing e.g. the optimization of the spanwise distribution of wing section lift and pitching moment for minimum induced plus airfoil viscous drag for a given spanwise distribution of airfoil thickness.

Programs such as just described can be very helpful in the conceptual and preliminary design of mini-mum drag sircraft. They are also used for creating the starting point for the specification of "target" pressure distributions in the detailed aerodynamic design of wings by means of inverse methods

Chordwise pressure distributions leading, approximately, to minimum viscous drag can, in principle, be determined by combining an optimization algorithm with a boundary layer code. Possibilities along these lines are currently being explored at NLR using a program system called CADOS (Ref. 33). The program uses basic "serodynamic" as well as spline-type pressure distribution shape functions (Fig. 34) and can handle laminar as well as turbulent flows. It can address problems like the determination of the pressure distri-

Imminar as well as turbulent flows. It can address problems like the determination of the pressure distri-bution that, subject to constraints on, e.g. lift, pitching moment coefficient and average pressure level (airfoil thickness) leads to minimum viscous drag. A simple, exploratory example of application is presented in figure 35. The figure shows the results of pressure distribution modifications to a basic pressure distribution by means of spline-type shape func-tions with the objective to minimize the drag. The boundary layer was not allowed to separate. Although the mobile formation of the state of th problem, as formulated, is not necessarily a sensible one, it illustrates the basic idea of the approach. In the particular case the answer is, obviously, determined to a large extent by the constraints implied by the basic and spline shape functions. Other choices for these will lead to a different answer. The approach is currently being explored further.

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It is the suthor's opinion that the inverse numerical optimization approach is worthy of further investigation; not in the least because the computational effort required is much smaller than that of direct numerical optimization.

CONCLUDING REMARKS 6

An overview has been presented of the possibilities and problems associated with the prediction, analysis and minimization of drag using CFD methods. The discussion is limited to sub/transomic inviscid (potential and Euler) flow models, boundary layer and wake methods and methods employing viscous-inviscid interactions.

From the discussion it is concluded that the absolute accuracy of the computational determination of subsonic aircraft (wing) drag is, currently, of the order of 10 to 30 "counts" at best. The main problems seem to be

- lack of resolution due to the limited number of mesh-points and lack of convergence due to the limited number of iterations or time steps that can be run on the computer systems that are currently available in most engineering environments (particular important for wave drag and, but possibly to a lesser extent, for induced drag)

- spurious entropy production in Euler codes as a result of insufficiently accurate implementation of boundary conditions

- lack of (appropriate) methods and turbulence models for the computation of wakes in pressure gradient and dary layers with complex interaction phenomena. bouz

An additional problem of the majority of the available inviscid flow codes is that they provide values for integrated pressure drag only so that a division into wave drag and induced drag is not readily avail-

for integrated pressure drag only so that a division into wave drag and induced drag is not readily avail-able. In spite of this situation it has proved possible to devise engineering procedures for determining drag increments for (closely) similar flow conditions or configurations with usable accuracy. Closely related to the problems mentioned above is the fact that configuration optimization for drag reduction by means of <u>direct numerical optimization</u> techniques is hardly feasible in current engineering environments, at least for three-dimensional problems. An alternative might be to use numerical optimiza-tion for designing minimum drag "target" pressure distributions and to use inverse methods to find the corresponding geometry (<u>inverse numerical optimization</u>).

Summarising, it may be stated the <u>accurate</u> numerical determination and minimization of drag is currently almost "mission impossible", at least for three-dimensional flow. However, there are exciting prospects for the future, not in the least because of the continuing rapid advancements in computer technology.

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• USUALLY ESTIMATED BY MEANS OF FORM FACTOR METHODS

 $C_{D_{min}} = C_{F}(1 + k t/c + ...) \cdot \frac{S_{wet}}{S_{ref}}$

Fig. 3 Definition of "(subsonic) minimum drag"



- (REYNOLDS AVERAGED) NAVIER STOKES METHODS
 - CAN PROVIDE FRICTION DRAG AND PRESSURE DRAG
 - CONTAIN ALL INFORMATION NECESSARY TO DISTINGUISH
 - BETWEEN VISCOUS DRAG, INDUCED DRAG AND WAVE DRAG GENERALLY NOT YET AVAILABLE IN INDUSTRIAL ENVIRONMENT

INVISCID METHODS

MODEL PRESSURE DRAG ONLY

	INDUCED DRAG	WAVE DRAG
EULER	x	x
FULL POTENTIAL	x	x*)
LINEARIZED POTENTIAL	x	- 1

*) APPROXIMATIVE, ACCEPTABLY ACCURATE FOR Mn < 1.3 ?

- BOUNDARY LAYER AND WAKE METHODS
 - FRICTION DRAG (BOUNDARY LAYER)
 - TOTAL VISCOUS DRAG (WAKE)
- Fig. 7 Drag (component) prediction capability potential of various CFD models

Fig. 6 Hierarchy of mathematical/physical CFD flow models



Fig. 8 Comparison of Euler (FL052S) and full potential (FL036) solutions (Ref. 1)

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Fig. 23 Comparison of experimental (wake rake) and calculated viscous drag distribution for transport type wing





Fig. 25 Chart of relations between drag components



Fig. 26 Schematic of NLR XFL022 system for the analysis of wing-fuselage configurations in transonic flow



Fig. 27 NLR XFL022 drag analyses fo narrow-body transport configuration







Fig. 28 NLR XFL022 wing-fuselage transonic analysis system: examples of standard graphics output

Fig. 29 Flow chart of direct numerical optimisation















Fig. 31 Scheme for inverse numerical optimisation (conjectural)











Fig. 33 Examples of trimmed induced drag minimization studies

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