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REDUCTION IN BANDWIDTH
BY USING VARIABLE LENGTH CODES

by

Serdar Akinsel

December 1985

Thesis Advisor:

R. W. Hamming

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Reduction in Bandwidth
by Using Variable Length Codes

by

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Lt. Jg., Turkish Navy
B.S., Turkish Naval Academy, 1979

Submitted in partial fulfillment of the
requirements for the degree of

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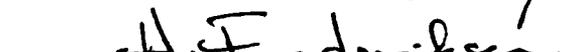
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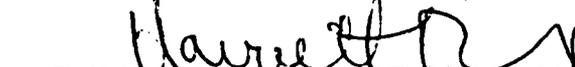
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ABSTRACT

A method of coding an ensemble of messages of a finite number of symbols is developed. Minimizing the average number of coding digits per message by using Huffman coding can result in a large variance. This is a problem because a large variance requires a large buffer and also creates more time delay during transmission and decoding respectively for on-line communication.

This research examines modified Huffman codes for the purpose of finding a way to reduce the variance. The effective parameters which give the lower variance modified Huffman codes are obtained. The buffer requirements and the reduction of the bandwidth to forward messages in an on-line communication is investigated. A possible design for a practical system is presented for using the modified Huffman codes.



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I. THE INTRODUCTION

The two main problems of representing the source alphabet symbols in terms of another system of symbols (the encoding process) are the following:

1. The altered symbols could be decoded incorrectly.
2. For the sake of efficiency the source symbols should be represented in a minimal form.

One coding process is to encode the source data into the binary digits (bits) which consists of 0's and 1's. Modern military communication systems are increasingly adopting the digital method of transmitting data. In addition to its simplicity part of the reason for the use of digital transmission is that it is more reliable than is analog transmission. Another reason that modern systems use digital methods is that integrated circuits are now very cheap and provide a powerful method for flexibly and reliably processing and transforming digital signals.

Dealing with digital transmission, shorter messages maximize the data transfer rate but also cause minimization of the redundancy of the source and hence vulnerability to errors. Variable length codes used to encode the source data drives the reduction in the source redundancy.

The Huffman code is clearly a variable length code. It takes advantage of the high frequency occurrence of some letters in the source alphabet by assigning them short bit sequences. On the other hand the low frequency occurrence of source symbols are assigned long bit sequences. [Ref. 1]

A. HUFFMAN CODING

Huffman encoding, devised by David A. Huffman, has the property of being a minimum redundancy encoding; that is, among all variable length binary encodings having the prefix property, that no complete symbol is the prefix of some

other symbol, this encoding has the lowest average number of binary digits used per letter of the original message, assuming that the message is made up of letters independently chosen, each with its probability given. [Ref. 2]

The underlying idea of the Huffman coding procedure is to repeatedly reduce a code to an equivalent problem with one less code symbol. In more detail, the two least probable symbols are merged into a single symbol whose probability is the sum of the two original probabilities and then this new symbol is inserted into its proper (ordered) position. As an example of Huffman encoding suppose we have a source alphabet of six symbols, with the given probabilities of occurrence. See (Table 1).

SYMBOL	PROBABILITIES
S1	0.4
S2	0.2
S3	0.2
S4	0.1
S5	0.05
S6	0.05

From Table 1 it can be observed that the sum of the probabilities is equal to one. If the symbols don't have the probabilities in decreasing order, they should be arranged in this way. The coding process can be done according to the following procedure.

To obtain the first reduction from the original n symbols to $n-1$ symbols combine the two least probable symbols of the source alphabet into a single symbol, whose probability is equal to the sum of the two corresponding probabilities. See (Figure 1.1).

Symbol	Prob.	Prob.
S1	0.4	0.4
S2	0.2	0.2
S3	0.2	0.2
S4	0.1	0.1
S5	0.05	0.1
S6	0.05	
	Original	First Reduction

Figure 1.1 The First Reduction.

The repetition of this reduction is to be continued until only two symbols remain. See (Figure 1.2). As in the original, in each reduction the probability summation equal to one is kept.

By giving the two symbols in the fourth reduction the values 0 and 1, and proceeding backwards to the left, the assignments for the original code words can be accomplished. Going backwards, one of these symbols has to be expanded into two symbols. By assigning a second digit 0 for one of them and 1 for the the other, this splitting process is continued until one comes back to the original symbols. Figure 1.3 shows the first three splitting processes and their respective assigned code words. The 0 and 1's in the parentheses are the assigned code words. The final code words for this example are given in Table 2.

Symbol	Prob.	Prob.	Prob.	Prob.	Prob.
S1	0.4	0.4	0.4	0.4	0.6
S2	0.2	0.2	0.2	0.4	0.4
S3	0.2	0.2	0.2	0.2	
S4	0.1	0.1	0.2		
S5	0.05	0.1			
S6	0.05				

|Original| First | Second | Third | Fourth
 | | Reduc. | Reduc. | Reduc. | Reduc.

Figure 1.2 The Reduction Process.

Symbol	Prob.	Prob.	Prob.
S1	0.4(1)	0.4(1)	0.6(0)
S2	0.2(01)	0.4(00)	0.4(1)
S3	0.2(000)	0.2(01)	
S4	0.2(001)		
S5			
S6			

| Third | Second | First
 | Splitting | Splitting | Splitting

Figure 1.3 The First Three Splitting Processes.

B. MODIFICATION OF HUFFMAN CODING

The procedure given in section A was accomplished by merging states at the bottom of the list of ordered probabilities. The code word lengths which were assigned to the symbols of the above example were (1,2,3,4,5,5) as shown in Table 2. The average code length is given by

$$L = 0.4(1) + 0.2(2) + 0.2(3) + 0.1(4) + 0.05(5) + 0.05(5)$$

$$L = 2.3$$

and the variance is given by

$$V = 0.4(1-2.3)^2 + 0.2(2-2.3)^2 + 0.2(3-2.3)^2 \\ + 0.1(4-2.3)^2 + 0.05(5-2.3)^2 + 0.05(5-2.3)^2 = 1.81$$

On the other hand, if the combined symbols are placed as high as possible in the list of ordered probabilities the code lengths obtained will be (2,2,2,3,4,4). For this second encoding the reductions are given in Figure 1.4. The first three splitting processes and final assignments of the source symbols are shown in Figure 1.5 and in Table 3 respectively.

The average code length is now given by

$$L = 0.4(2) + 0.2(2) + 0.2(2) + 0.1(3) + 0.05(4) + 0.05(4)$$

$$L = 2.3$$

and the variance is given by

$$V = 0.4(2-2.3)^2 + 0.2(2-2.3)^2 + 0.2(2-2.3)^2 \\ + 0.1(3-2.3)^2 + 0.05(4-2.3)^2 + 0.05(4-2.3)^2 = 0.41$$

Obviously the variability of the second assignment is lower than that of the first code. The result of moving merged symbols to high positions will result in the production of codes of lower variance. [Ref. 1: page 68]

To obtain codes of low variance as a modification of Huffman coding, three different parameters (N,K,E) are defined to describe the position where the combined symbol is to be placed. These three parameters, two of which were proposed in [Ref. 3], make use of what appears to be an optimal (in the sense minimizing variance) procedure of shifting the combined symbols higher than where they belong in the ordered probability listing. The definitions and examples of these parameters are given below.

TABLE 2
FINAL ASSIGNMENTS OF THE CODE WORDS

SYMBOL	CODE WORDS
S1	1
S2	01
S3	000
S4	0010
S5	00110
S6	00111

Symbol	Prob.	Prob.	Prob.	Prob.	Prob.
S1	0.4	0.4	0.4	0.4	0.6
S2	0.2	0.2	0.2	0.4	0.4
S3	0.2	0.2	0.2	0.2	
S4	0.1	0.1	0.2		
S5	0.05	0.1			
S6	0.05				

|Original| First | Second | Third | Fourth
 | | Reduc. | Reduc. | Reduc. | Reduc.

Figure 1.4 The Reduction Process for the Second Encoding.

1. The Parameter N

N is defined as an integer which is used to move the merged symbols to relatively higher positions than would be normally done. If N is set to 2, combined symbols are moved two positions higher than they would normally appear in the list of probabilities. Setting N equal to 0, the original

Symbol	Prob.	Prob.	Prob.
S1	0.4(00)	0.4(1)	0.6(0)
S2	0.2(01)	0.4(00)	0.4(1)
S3	0.2(10)	0.2(01)	
S4	0.2(11)		
S5			
S6			

Third Second First
 Splitting Splitting Splitting

Figure 1.5 Splitting Processes for the Second Encoding.

SYMBOL	CODE WORDS
S1	00
S2	10
S3	11
S4	011
S5	0100
S6	0101

Huffman encoding given in Table 1 can be obtained. Figure 1.6 demonstrates the first reduction of the modified Huffman coding for the example given in the previous section when N is set to 2. When the second reduction is performed the last symbols in the list are combined. In the example, the last two symbols of the first reduction (0.2 and 0.1) are

merged and the probability assigned to the combined symbol is 0.3. This merged new symbol is then placed at the top of the list.

Symbol	Prob.	Prob.
S1	0.4	0.4
S2	0.2	0.2
S3	0.2	0.1
S4	0.1	0.2
S5	0.05	0.1
S6	0.05	
	Original	First Reduction

Figure 1.6 Modified Huffman Coding for $N = 2$.

2. The Parameter K

The second parameter, K , is a number used to multiply the probability sum of each merged entry. This parameter generally causes the merged entry to appear in higher position than it would appear normally in the original Huffman coding. The original Huffman code is obtained by setting K to 1. Setting K equal to 3, for example, multiplies the probability of the combined entry by 3 and then puts it where it would normally appear. Of course now the probabilities no longer add to 1. The first reduction of the Huffman coding given in the previous section can be modified as shown in Figure 1.7.

3. The Parameter E

The third parameter, E , is a real number added to the sum of the probabilities of the merged entries. As far as the relative positions in the list of symbols are concerned, E has the same effect as K and N . The merged symbol is placed in the location where it would normally

Symbol	Prob.	Prob.
S1	0.4	0.4
S2	0.2	0.3
S3	0.2	0.2
S4	0.1	0.2
S5	0.05	0.1
S6	0.05	
	Original	First Reduction

Figure 1.7 Modified Huffman Coding for $K = 3$.

appear as if the result was the correct probability. Of course, again the probabilities do not sum to 1. The original Huffman coding is produced when E is set to 0. Figure 1.8 shows the first reduction of the modified Huffman coding for the example given in the previous section when E is set to 0.15.

Symbol	Prob.	Prob.
S1	0.4	0.4
S2	0.2	0.25
S3	0.2	0.2
S4	0.1	0.2
S5	0.05	0.1
S6	0.05	
	Original	First Reduction

Figure 1.8 Modified Huffman Coding for $E = 0.15$.

C. THE NORMALIZATION PROCESS

During the modification of the Huffman coding process, the requirement for the summation of the probabilities to be equal to one was not considered except for the parameter N. For the other two parameters (E,K) a probability sum equal to one can be retained by normalizing the list of ordered probabilities at each reduction stage during the modification process. To observe the effect of this normalization we first continue the reduction process and find the code words produced when the parameter E is set to 0.15 without normalizing. See (Figure 1.9). The splitting process and the final code words are given in Figure 1.10 and in Table 4, respectively.

On the other hand, if the normalization is applied at each reduction stage, the resulting reduction and splitting processes are as given in Figure 1.11 and Figure 1.12. Finally the code words after normalization are as shown in Table 5. The normalized probabilities at each reduction stage were obtained by dividing each probability by 1.15 (normalization parameter) for this particular example.

Table 4 and Table 5 emphasize that the same code words would be obtained either with or without normalization. The effect of normalization is only to decrease the probabilities at each reduction stage to a smaller number. But if the normalization parameter is a large number then the order of probabilities at reduction processes could be slightly different, resulting in slightly different code words. Clearly since the same code words are obtained there is no need to perform the work required for the normalization.

Symbol	Prob.	Prob.	Prob.	Prob.	Prob.
S1	0.4	0.4	0.45	0.6	1.0
S2	0.2	0.25	0.4	0.45	0.6
S3	0.2	0.2	0.25	0.4	
S4	0.1	0.2	0.2		
S5	0.05	0.1			
S6	0.05				
	Original	First	Second	Third	Fourth
		Reduc.	Reduc.	Reduc.	Reduc.

Figure 1.9 The Reduction Process when $E = 0.15$.

Symbol	Prob.	Prob.	Prob.	Prob.	Prob.
S1	0.4(01)	0.4(01)	0.45(00)	0.6(1)	1.0(0)
S2	0.2(11)	0.25(10)	0.4(01)	0.45(00)	0.6(1)
S3	0.2(000)	0.2(11)	0.25(10)	0.4(01)	
S4	0.1(001)	0.2(000)	0.2(11)		
S5	0.05(100)	0.1(001)			
S6	0.05(101)				
	Final	Fourth	Third	Second	First
	Split.	Split.	Split.	Split.	Split.

Figure 1.10 The Splitting Process when $E = 0.15$.

TABLE 4
THE FINAL CODE WORDS WHEN $E = 0.15$

SYMBOL	CODE WORDS
S1	01
S2	11
S3	000
S4	001
S5	100
S6	101

Symbol	Prob.	Norm.	Prob.	Norm.	Prob.	Norm.	Prob.	Norm.
S1	0.4	0.348	0.410	0.357	0.49	0.426	0.724	0.63
S2	0.2	0.217	0.348	0.303	0.357	0.310	0.426	0.37
S3	0.2	0.174	0.217	0.189	0.303	0.264		
S4	0.1	0.174	0.174	0.151				
S5	0.05	0.1	0.087					
S6	0.05							
Orig.	First Norm.	Second Norm.	Third Norm.	Fourth Norm.	Reduction	Reduction	Reduction	Reduction

Figure 1.11 The Normalized Reduction Process when E = 0.15.

Sym.	Prob.	Prob.	Prob.	Prob.	Prob.
S1	0.4(01)	0.348(01)	0.357(00)	0.426(1)	0.630(0)
S2	0.2(11)	0.217(10)	0.303(01)	0.310(00)	0.370(1)
S3	0.2(000)	0.174(11)	0.189(10)	0.264(01)	
S4	0.1(001)	0.174(000)	0.151(11)		
S5	0.05(100)	0.087(001)			
S6	0.05(101)				
	Final	Fourth	Third	Second	First
	Split	Split.	Split.	Split.	Split.

Figure 1.12 The Normalized Splitting Process ($E = 0.15$).

SYMBOL	CODE WORDS
S1	01
S2	11
S3	000
S4	001
S5	100
S6	101

II. MODIFICATION OF HUFFMAN CODING FOR A PARTICULAR ALPHABET

A. A PARTICULAR ALPHABET

Huffman coding produces the code with the minimum average code length. Here we propose to find a practical modified variable length code for the Turkish alphabet to minimize the average code length and also minimize the variance using techniques involving the parameters introduced in the previous chapter.

For the following two reasons the use of the Turkish alphabet was not possible:

1. The exact probabilities of the Turkish alphabet are not known.
2. Some of the letters in Turkish alphabet are not available on the keyboard.

Therefore, it was determined to use the same alphabet, given in [Ref. 3]. This alphabet consists of 47 characters with common usage letters, numbers (0-9) and special symbols for the use of the on-line communication.

Two Turkish magazine articles [Refs. 4,5] were used to obtain the approximate frequencies of occurrences of symbols of the Turkish alphabet. A Fortran language program and Statistical Analysis System (SAS) package program [Ref. 6], was executed to determine the probabilities as was done in [Ref. 3]. These magazine articles, the Fortran language program and SAS program appear in Appendix A.

Table 6 contains the data taken from the output of these programs. The characters with their probabilities in descending order are given in Table 7.

B. EXPERIMENTAL PARAMETER

The three different parameters N, K, E introduced in the first chapter were investigated with this particular alphabet to obtain lower variance codes than the original Huffman code. Because of the size of alphabet the modification process was not performed manually. A program written in a List programming language (LISP) was used, to produce the encoding. The output of the program gives the code words with their average lengths and the corresponding variances. This program is given in Appendix B [Refs. 7,8]. This program was run employing these three parameters N, K and E. The original Huffman coding can be obtained for this particular alphabet as before by setting parameters N and E to 0 and K to 1. According to the discussion in the previous chapter the normalization process was not considered necessary. These parameters were tested separately in order to find which parameter gives the best codes when each is used independently. The following three basic steps were performed.

- Step1. For parameter N, the program was executed 31 times. N was selected as each integer value from 0 to 30. While doing this the other two parameters, E and K, were fixed at 0 and at 1 respectively in order not to affect N.
- Step2. For parameter K the program was run 2072 times with K set equal to a sequence of rational numbers from 1. to 275. The average lengths and corresponding variances of the codes for each K were obtained. In this step parameters N and E were each set to zero for testing only the parameter K.
- Step3. For the parameter E the program was executed 2273 times with the values ranging from 0.0 to 0.3. The various values used yielded different codes with their mean times and variances. In order not to affect E, the other two parameters, N and K was set to 0 and to 1, respectively, while running the LISP program.

During the modification process applied to this particular alphabet, average code lengths and variances of the encoding for different values of the parameters were obtained. As far as unique mean times and variances are concerned, 24, 62, 251 unlike codes were obtained by the

choices for the parameters N, K and E respectively. For some values of the parameters, the resulting mean times and variances of the encoding are the same. Since the combined symbols were positioned as high as they could go in the reduction processes, the same mean times and variances were obtained after some certain values of the parameters. For example, for this particular alphabet for $N \geq 29$, $K \geq 272.84$ and $E \geq 0.264$, the same average code lengths and variances were obtained equal to 5.08843 and 0.08061 in each of the three different steps.

The preceding three steps also emphasize the fact that among all choices of the parameters, more codes are generated by using the third parameter E. Since this parameter E can be any real number, it can be adjusted so that the merged symbols do not move to higher positions in some of the reduction processes for some values of E but the merged symbols do move for some other values of E. On the other hand, by using some large values for N and K the merged symbols typically are brought to higher positions in the beginning of the reduction process. As more flexibility in the reduction processes is possible by the choice of values for E, more codes can be obtained using the parameter E, since the merged symbols do not always move to higher locations.

The different average lengths and variances, of the modified Huffman codes obtained with different parameter values of N, K, and E values are given in Tables 8, 9 and 10 respectively. The average length and variance obtained by setting N and E equal to 0, and K equal to 1, corresponds to the original Huffman code for this particular alphabet. The different values of the parameters given in these tables represent the minimum values for the given parameter which result in a given mean time and variance. For instance, all the codes using $E = 0.00011$ up to $E = 0.00033$ have the same average length and variance thus $E = 0.00011$ appears in

Table 10. To be able to determine a good experimental parameter, graphs which contain mean times on the horizontal axis and variances on the vertical axis were plotted for each parameter, separately. These graphs are shown in Figure 2.1, 2.2 and 2.3. The second and the third columns of Tables 8, 9 and 10 were used for the data in these figures. When these three graphs are compared with each other, the minimum variances for the corresponding average code lengths (dashed lines) were found for the codes due to the parameters N, K and E.

C. ASSIGNMENT OF THE CODES FOR THE PARAMETER E

According to the discussion in the previous section, E was chosen as a more robust parameter than the parameters N and K for modifying Huffman coding system, for the following two reasons:

1. E provides more unique codes than N and K.
2. E gives a lower bound as good as N and K on a mean time versus variance graph.

After the robust parameter E has been determined, the experimental codes can be found using this parameter. To find the experimental codes, the graph, shown in Figure 2.3, was used. Each point in the graph represents a unique, modified variable length code. The dashed line in the graph emphasizes the lower bound which met the minimum variance criteria. The boxes on this line were picked as the best experimental codes, for a given mean and variance. Table 11 shows the respective mean times and variances of the experimental codes extracted from Figure 2.3. It can be also noticed that the other codes that do not appear in Table 11 are those that appear above the dashed line.

The codes in Table 11, are listed with their mean times in increasing order but their variances in decreasing order. Despite having the minimum average length, the Huffman code has the largest variance. On the other hand, code M has a variance close to zero but has the largest mean time. For

the given alphabet it is possible to obtain a variance of zero by using a block code. A block code gives an average length of 6 with zero variance. Finally the code words belonging to the various codes in Table 11, are given in Table 12.

We graph in Figure 2.4 only the experimental codes from Table 11, that have minimum variance for a given mean time. The extreme points, the Huffman code (code A) and the block code, also appear in this figure. This figure emphasizes that a small increase in average length can cause a large reduction in variance.

When the Huffman code is utilized as the reference for computing the increments in average lengths and the decrements in variances of these modified codes, the gain in variance versus the loss in mean time can be plotted as a difference from the reference Huffman code. This graph is given in Figure 2.5. The data for this figure appears in Table 13. The line segments between code M and the block code and between Huffman code and code B are almost parallel to the horizontal and vertical axes respectively. These parallel segments in Figure 2.5 show that, a little gain in one variable can result in a significant loss in the other variable. The last two columns in Table 13 give the relative gain and loss between adjacent experimental codes.

The dashed line represents the curve for code F. The block code needs no buffer with this chosen output rate. Therefore, the plot belonging to the block code is a straight line. For convenience, to distinguish the plots from each other, they were moved to their input rates level. Then, for example, when the Huffman code needs to have a buffer length of 1 at the 21st character, its curve jumps from 4.30771 to 5.30771 and whenever there is no need for a buffer the curve remains at the 4.30771 level.

C. TRANSMISSION OF THE LONG MESSAGES

The use of the smaller capacity than the block code output rate causes a reduction in the bandwidth demands. As far as base performance is concerned, a 25% reduction in capacity means also a 25% saving in the bandwidth. Note in Table 14, a saving of 28.2%, greater than the 25% savings, is discussed. The Huffman code rate of 4.30771 which gives 28.2% reduction requires larger buffers. Except for the Huffman code, since it was used to send more than this rate can handle, the buffer sizes required continue to grow as the length of the messages increase. For this reason the bandwidth which saves 25% was determined as a best output rate (4.5 bits per unit time). The different buffer lengths for different lengths of messages are given in Table 16. The message lengths were arbitrarily selected by the author to also include the entire two magazine articles. The output rate was held fixed at 4.5 bits per unit time and the buffer lengths required were obtained by using the program in Appendix C. Table 16 shows the fact that when the input rates become larger than the output rate, the buffer sizes increase with longer messages.

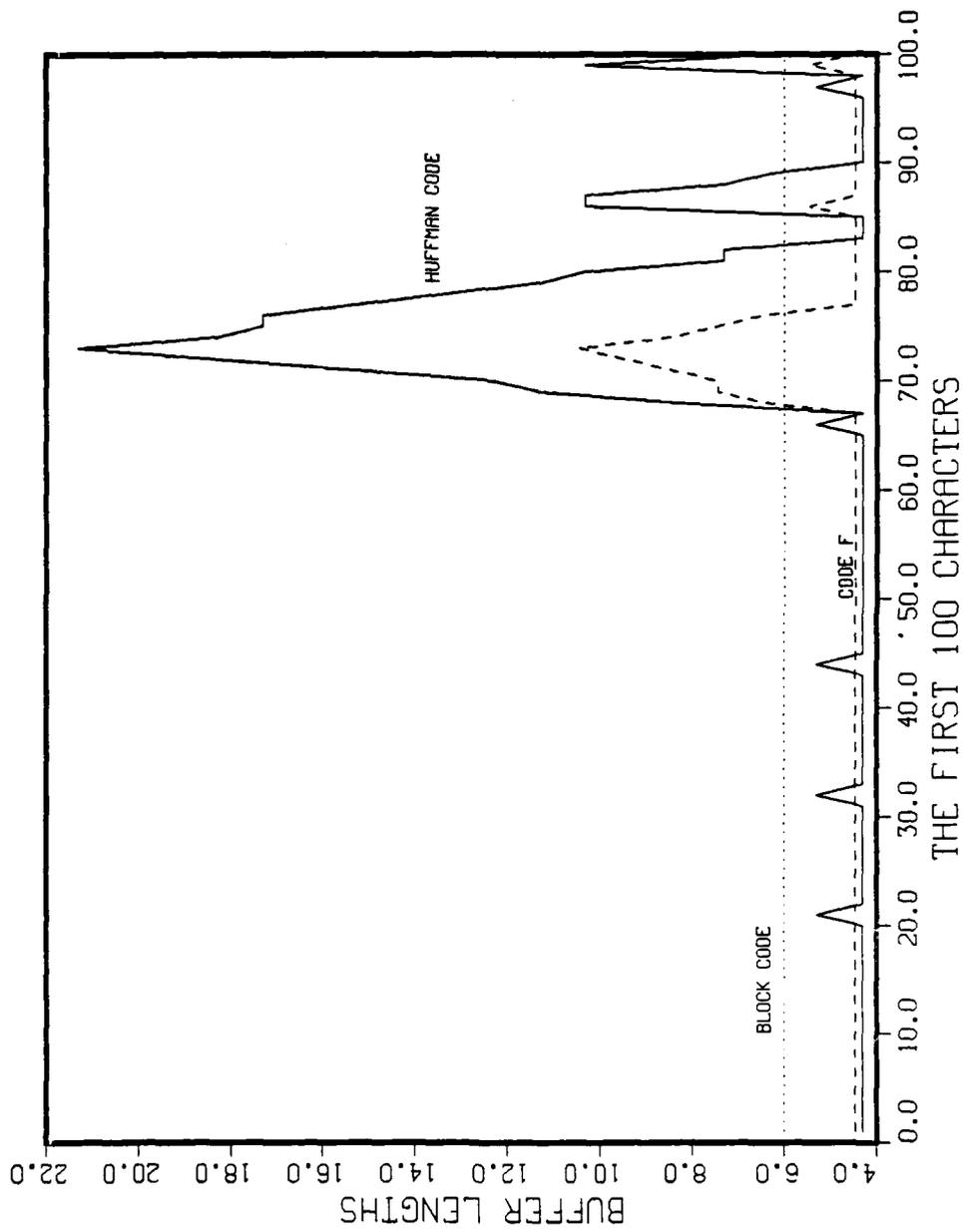


Figure 3.2 Change of Buffer Lengths for the First 100 Characters.

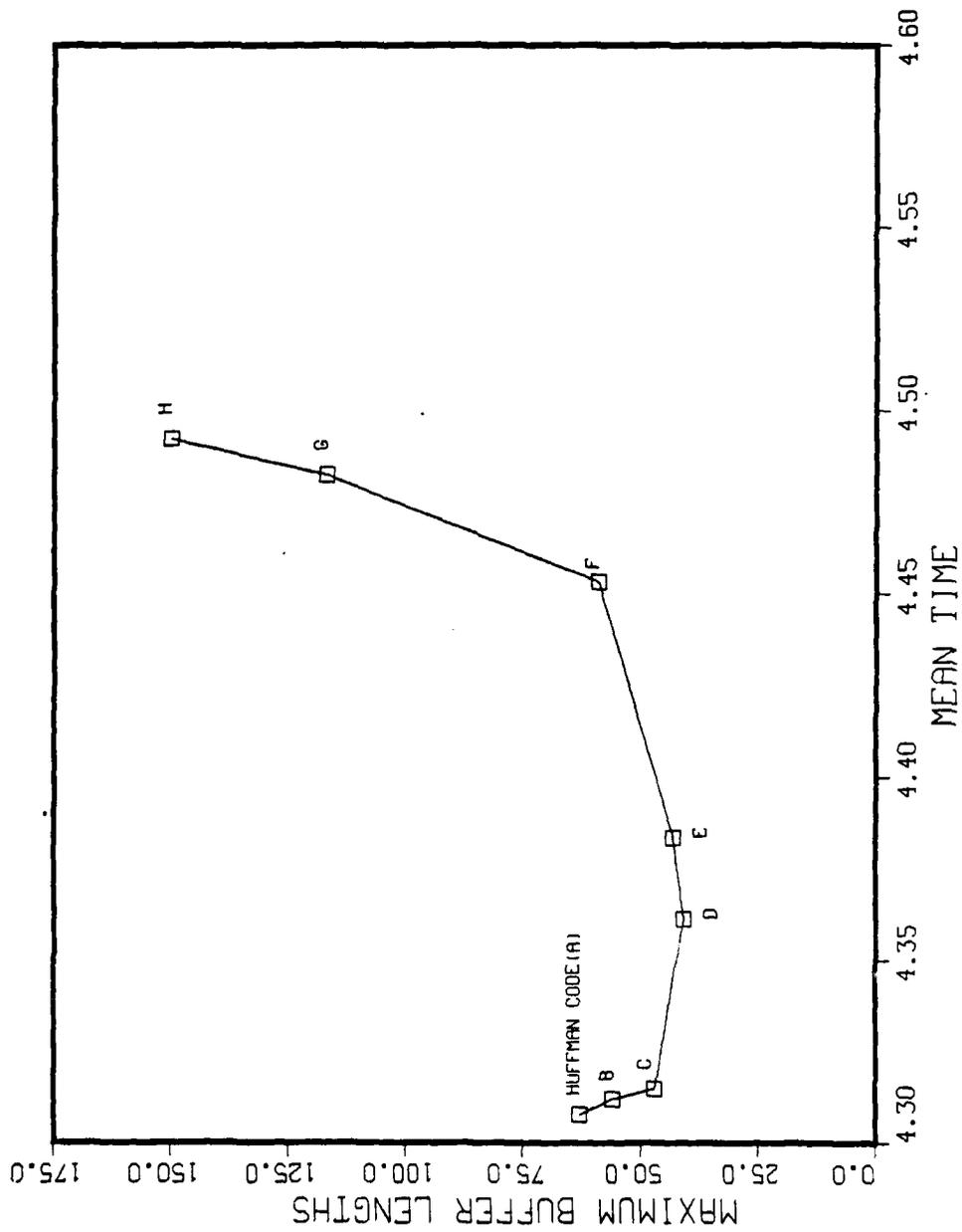


Figure 3.3 Maximum Buffer Lengths with Different Input Rates.

the discrimination of the transmitted message by an unintended recipient, the variable length code becomes more difficult to decrypt than the block code. Second, there is only so much bandwidth in the spectrum of available frequencies that passes through the earth's atmosphere, and already much of it is assigned to various uses. Therefore, the proposition of saving even 25% from the bandwidth can be observed as a valid estimated performance criteria.

Accordingly, these two important properties of the variable length codes carry an important role for military applications. However, the defect for that use is the time delay during the decoding of the received messages. In a critical case when transmitting an urgent short message the negative aspect of the time delay loses its importance, since the lengths of the buffer grow with the length of the messages. On the other hand, when longer messages are transmitted, considering both jamming avoidance and the time delay at the decoder, the bandwidth can be increased to higher rates to obtain smaller buffer lengths.

Definition of some other parameters, which would obtain better modified Huffman codes could result with a reduction of the lower bounds given in Figure 2.1, 2.2 and 2.3. Thus, with these coding systems, if done properly, more effective practical systems could be designed.

ALDILAR. GEMININ ILK TICARI YUKU OLAN ILETISIM UYDULARI 11 KASIM 1982 GUNU BASLAYAN BU SEFERDE BASARIYLA YORUNGEYE OTURTULDU. EGER BU UYDULAR YERDEN YORUNGEYE YERLESTIRILSEYDI, UYDU SAHIPLERI DAHA FAZLA PARA ODEMEK ZORUNDA KALACAKLARDI. BU SEYIRDE PERSONELI UZAY TUTTU. BU YUZDEN UZAYDA YURUYUS IZLENCESI BIR GUN ERTELENDI. ERTESI GUN ISE HER BIRI YARIM Milyar TL'NA MAL OLAN UZAY MELBUSATI ARIZALANDI. TUM UGRASLARA KARSIN ARIZALAR GIDERILEMEDIGI ICIN YURUYUSTEN VAZGECILDI. FAKAT BU COK ONEMLI BIR DENEYDI; CUNKI GELECEKTE UZAY LIMANI GIBI BUYUK YAPILAR INSA EDILIRKEN, BU TECHIZAT ILE ARAC DISI CALISMALAR YAPILACAK.

2. PROGRAMS

The two programs used to obtain the probabilities of the symbols in the magazine articles given above. A Fortran program creates a data set format which can be processed by a SAS program. The program which sets the logical record length of data file to 1, is given below.

```
//AKINSEL JOB (0936,5555), 'AKINSEL',CLASS=A
//*MAIN ORG=NPGVM1.0936P
// EXEC FORTVCG
//FORT.SYSIN DD*
C          THIS PROGRAM CONVERTS ONE LOGICAL RECORD OF
C          EIGHTY CHARACTERS TO EIGHTY
C          LOGICAL RECORDS OF ONE CHARACTER EACH.
C
C          UNIT 5: INPUT
C          UNIT 1: OUTPUT
C
          DIMENSION A(80)
          LINES =0
10 CONTINUE
          READ(5,20,END=100) A
20 FORMAT(80A1)
          LINES = LINES + 1
          DO 30 I=1,80
          WRITE(1,20) A(I)
30 CONTINUE
          GO TO 10
100 CONTINUE
          WRITE(6,110) LINES
110 FORMAT(1X,'NUMBER OF LINES READ: ',17)
          STOP
          END
/*
//GO.FT01F001 DD UNIT=3350,VOL=SER=MVS004,
```

```
DISP=(NEW,KEEP),  
//   DCB=(RECFM=FB,LRECL=,BLKSIZE=6000),  
//   SPACE=(TRK,(1,1)),DSN=S0936.LETTER  
//GO.SYSIN DD *  
    Insert text here. (Also,remove this line).  
/*  
//
```

The second program is executed to find the probability of each symbol in the alphabet. This SAS program is given below.

```
//AKINSEL JOB (0936,5555),'AKINSEL',CLASS=B
//*MAIN ORG=NPGVM1.0936P
// EXEC SAS
//TEXT DD UNIT=3350,VOL=SER=MVS004,DISP=SHR,
DSN=S0936.ALPHA1
//SYSIN DD *
OPTIONS LINESIZE = 80;
DATA TEXT;
    INFILE TEXT;
    INPUT @1 LETTER $CHAR1. ;
    IF LETTER EQ ' ' THEN DELETE;
PROC FREQ DATA=TEXT;
    TABLES LETTER;
/*
//
```

APPENDIX B

THE LISP PROGRAM OF CODING PROCESS

The Lisp program for finding the code words of the original Huffman and the modified Huffman codes is given below.

```
(defun huffman (P)
  (sortcar (assign (arrange (mapcar 'list P))) 'greaterp))

(defun arrange (Q)
  (cond ((null (cdr Q)) Q)
        (t (arrange (insert (list (add (caar Q) (caadr Q))
                                   (car Q) (cadr Q))
                             (caddr Q)) ) ) )

(defun insert (x Q)
  (cond ((null Q) (cons x Q))
        ((lessp (plus (times (car x) K) epsilon) (caar Q))
         (putin N x Q))
        (t (cons (car Q) (insert x (cdr Q)) ) ) )

(defun putin (n x L)
  (cond (( zerop n ) (cons x L))
        ((null L) (list x))
        (t (cons (car L) (putin (sub1 n) x (cdr L))))))

(defun assign (Q) (split nil (carQ)) )

(defun split (c L)
  (cond ((null (cdr L)) (list (list (car L) C)) )
        (t (append (split (cons 1 c) (cad1 L))
                    (split (cons 0 c) (caddr L)) ) ) )

(defun sortcode (L)
  (cond ((null L) nil)
        (t (inscode (caar L) (cadar L) (sortcode (cdr L)) ) ) )
```

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REDUCTION IN BANDWIDTH BY USING VARIABLE LENGTH CODES
(U) NAVAL POSTGRADUATE SCHOOL MONTEREY CA S AKINSEL
DEC 85

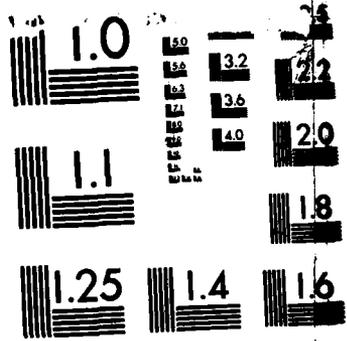
2/2

UNCLASSIFIED

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NL





MICROCOPY RESOLUTION TEST CHART
 NATIONAL BUREAU OF STANDARDS-1963-A

```

(defun inscode (p c L)
  (cond ((null L) (list (list p c)) )
        ((greaterp (length c) (length (cadar L)))
         (cons (list p (cadar L)) (inscode (caar L) c (cdr L)) ))
        (t (cons (list p c) L)) ))

(defun totlength (L)
  (cond ((null L) 0)
        (t (add (times (caar L) (length (cadar L)) )
                  (totlength (cdr L)) )) ))

(defun avglength (L)
  (quotient (times 1.0 (totlength L))
            (apply 'add (mapcar 'car L)) ))

(defun varlength (L)
  (quotient (times 1.0 (varlength2 L (avglength L)))
            (apply 'add (mapcar 'car L))))

(defun varlength2 (L mu)
  (cond ((null L) 0)
        (t (add (times (caar L)
                        (expt (difference (length (cadar L)) mu) 2))
                  (varlength2 (cdr L) mu))))))

(defun Zipf (n)
  (cond ((zerop n) nil)
        (t (cons (quotient 1.0 n) (Zipf (- n 1)) )) ))

(defun tryN (n e k)
  (set 'N n)
  (set 'epsilon e)
  (set 'K k)
  (set code (sortcode (huffman Turkish)) )
  (print (list 'N '= n 'epsilon '= e 'K '= k))
  (pp code)
  (print (list 'mean '= (avglength code))) (terpr)
  (print (list 'variance '= (varlength code))) (terpr))

```

```
(set 'Turkish
'(0.0 0.00006 0.00006 0.00017 0.00028 0.00034
  0.00039 0.00045 0.00045 0.00056 0.00061 0.00067
  0.00067 0.00073 0.00073 0.00084 0.00084 0.00089
  0.00112 0.00134 0.00162 0.00196 0.00358 0.00581
  0.00687 0.00872 0.00989 0.01017 0.01224 0.01637
  0.01883 0.02185 0.02660 0.02682 0.02945 0.03213
  0.03509 0.03861 0.03984 0.05130 0.05163 0.06085
  0.06611 0.07952 0.09427 0.10528 0.13339))
```

```
(set 'N 0)
(set 'epsilon 0)
(set 'K 1)
```

APPENDIX C
THE FORTRAN PROGRAM TO FIND THE MAXIMUM BUFFER LENGTHS

```
$JOB
C
C   ***   VARIABLE DEFINITIONS   ***
C
C   LENGTH = NUMBER OF BITS BELONGING TO EACH
C           CHARACTER AFTER CODING PROCESS
C   RATEI  = INPUT RATE (BITS PER UNIT TIME)
C   RATEO  = OUTPUT RATE (BITS PER UNIT TIME)
C   MAX    = MAXIMUM BUFFER LENGTH
C   BUF1(I) = BUFFER SIZE OF EACH CHARACTER
C   BUFFER = TEMPORARY VARIABLE
C   BUF2   = REAL PART OF THE BUFFER
C   A(I)   = ARRAY IN WHICH THE CHARACTERS ARE LISTED
C   N(I)   = ARRAY IN WHICH THE NUMBER OF CHARACTERS
C           ARE LISTED
C
C   ***   VARIABLE DECLARATIONS   ***
C
C   REAL BUFFER,LENGTH,RATEI,RATEO
C   CHARACTER*1 A(      )
C   INTEGER I,BUF1(      ),N(      ),MAX
C   (Insert the length of the messages inside
C    the parentheses given above.)
C
C   ***   BEGINNING OF THE PROGRAM   ***
C
C   READ(5,100) A
C   RATEI = (Insert the input rate.)
C   PRINT,'INPUT RATE IS = ',RATEI
C   PRINT,' '
```

```

RATEO = (Insert the output rate.)
PRINT,'OUTPUT RATE IS = ',RATEO
PRINT,' '
BUFFER = 0.0
DO 200 I = 1,(Insert the length of the message.)
    N(I) = I
200 CONTINUE
WRITE(6,300) 'BUFFER SIZE'
C (Insert the number of bits for each character
C after coding process next to the variable
C name 'LENGTH', given below.)
DO 400 I = 1,(insert the length of the message)
    IF (A(I).EQ.'/') THEN
        LENGTH =
    ELSE IF (A(I).EQ.'I') THEN
        LENGTH =
    ELSE IF (A(I).EQ.'A') THEN
        LENGTH =
    ELSE IF (A(I).EQ.'E') THEN
        LENGTH =
    ELSE IF (A(I).EQ.'N') THEN
        LENGTH =
    ELSE IF (A(I).EQ.'R') THEN
        LENGTH =
    ELSE IF (A(I).EQ.'U') THEN
        LENGTH =
    ELSE IF (A(I).EQ.'L') THEN
        LENGTH =
    ELSE IF (A(I).EQ.'S') THEN
        LENGTH =
    ELSE IF (A(I).EQ.'K') THEN
        LENGTH =
    ELSE IF (A(I).EQ.'D') THEN
        LENGTH =
    ELSE IF (A(I).EQ.'T') THEN

```

```

        LENGTH =
ELSE IF (A(I).EQ.'M') THEN
        LENGTH =
ELSE IF (A(I).EQ.'Y') THEN
        LENGTH =
ELSE IF (A(I).EQ.'O') THEN
        LENGTH =
ELSE IF (A(I).EQ.'G') THEN
        LENGTH =
ELSE IF (A(I).EQ.'B') THEN
        LENGTH =
ELSE IF (A(I).EQ.'C') THEN
        LENGTH =
ELSE IF (A(I).EQ.',') THEN
        LENGTH =
ELSE IF (A(I).EQ.'.') THEN
        LENGTH =
ELSE IF (A(I).EQ.'Z') THEN
        LENGTH =
ELSE IF (A(I).EQ.'V') THEN
        LENGTH =
ELSE IF (A(I).EQ.'P') THEN
        LENGTH =
ELSE IF (A(I).EQ.'H') THEN
        LENGTH =
ELSE IF (A(I).EQ.'F') THEN
        LENGTH =
ELSE IF (A(I).EQ.'O') THEN
        LENGTH =
ELSE IF (A(I).EQ.'') THEN
        LENGTH =
ELSE IF (A(I).EQ.'1') THEN
        LENGTH =
ELSE IF (A(I).EQ.'") THEN
        LENGTH =

```

```
ELSE IF (A(I).EQ.'2') THEN
    LENGTH =
ELSE IF (A(I).EQ.'') THEN
    LENGTH =
ELSE IF (A(I).EQ.'5') THEN
    LENGTH =
ELSE IF (A(I).EQ.'3') THEN
    LENGTH =
ELSE IF (A(I).EQ.'8') THEN
    LENGTH =
ELSE IF (A(I).EQ.'(') THEN
    LENGTH =
ELSE IF (A(I).EQ.'4') THEN
    LENGTH =
ELSE IF (A(I).EQ.';') THEN
    LENGTH =
ELSE IF (A(I).EQ.'9') THEN
    LENGTH =
ELSE IF (A(I).EQ.'J') THEN
    LENGTH =
ELSE IF (A(I).EQ.'6') THEN
    LENGTH =
ELSE IF (A(I).EQ.'W') THEN
    LENGTH =
ELSE IF (A(I).EQ.':') THEN
    LENGTH =
ELSE IF (A(I).EQ.'7') THEN
    LENGTH =
ELSE IF (A(I).EQ.'-') THEN
    LENGTH =
ELSE IF (A(I).EQ.'?') THEN
    LENGTH =
ELSE IF (A(I).EQ.'X') THEN
    LENGTH =
ELSE IF (A(I).EQ.'Q') THEN
```

```

        LENGTH =
        END IF
        BUFFER = BUFFER + LENGTH
        BUFFER = BUFFER - RATEO
        IF (BUFFER.LE.0.0) THEN
            BUFFER = 0.0
            BUF1(I) = BUFFER
        ELSE
            BUF2 = BUFFER - AINT(BUFFER)
            IF (BUF2.GT.0.0) THEN
                BUF1(I) = INT(BUFFER)
                BUF1(I) = BUF1(I) + 1
            ELSE
                BUF1(I) = INT(BUFFER)
            END IF
        END IF
400  CONTINUE
        MAX = 0
        DO 500 I = 1,(Insert the length of the message.)
            IF (MAX.LT.BUF1(I)) THEN
                MAX = BUF1(I)
            END IF
500  CONTINUE
        DO 600 I = 1,(Insert the length of the message.)
            WRITE(6,700) N(I),BUF1(I)
600  CONTINUE
100  FORMAT(73 A1)
700  FORMAT (I6,9X,I5)
300  FORMAT (9X,A12)
        STOP
        END
$ENTRY
C    (Insert the message itself below. Each line
C    should consist of 73 characters.)

```

APPENDIX D

FORTRAN PROGRAM TO FIND THE NUMBER OF OVERFLOWS

```
$JOB
C
C   ***   VARIABLE DEFINITIONS   ***
C
C   LENGTH = NUMBER OF BITS BELONGING TO EACH
C           CHARACTER AFTER ENCODING PROCESS
C   RATEI  = INPUT RATE (BITS PER UNIT TIME)
C   RATEO  = OUTPUT RATE (BITS PER UNIT TIME)
C   P      = NUMBER OF LOST CHARACTERS
C   R      = NUMBER OF TRANSMITTED CHARACTERS
C   DIFFER = DIFFERENCE BETWEEN LENGTH OF THE CHARACTER
C           AND OUTPUT RATE
C   BUFFER = PROVIDED BUFFER SIZE
C   A(I)   = ARRAY IN WHICH THE CHARACTERS ARE LISTED
C   DIFF1  = INTEGER PART OF DIFFER
C   DIFF2  = REAL PART OF DIFFER
C   FLOW   = DIFFERENCE BETWEEN BUFFER AND DIFF1
C
C   ***   VARIABLE DECLARATIONS   ***
C
C   REAL LENGTH,RATEI,RATEO,DIFFER,DIFF2
C   CHARACTER*1 A(      )
C   (Insert the length of the message inside the
C   parenthesis given above.)
C   INTEGER I,K,P,BUFFER,R,DIFF1,FLOW,T
C
C   ***   BEGINNING OF THE PROGRAM   ***
C
C   READ(5,100) A
C   DO 200 T =(      ,      )
```

C (Insert the smallest and the largest provided
C buffer size in the parenthesis above.)

BUFFER = T

P = 0

R = 0

DIFFER = 0.0

RATEI = (Insert the input rate.)

PRINT,'INPUT RATE IS = ',RATEI

PRINT,' '

RATEO = (Insert the output rate.)

PRINT,'OUTPUT RATE IS = ',RATEO

PRINT,' '

PRINT,'PROVIDED BUFFER IS = ',BUFFER

PRINT,' '

C (Insert the number of bits for each character
C after coding process next to the variable
C name 'LENGTH', given below.)

DO 300 I= 1,(Insert the length of the message.)

IF (A(I).EQ.'/') THEN

LENGTH =

ELSE IF (A(I).EQ.'I') THEN

LENGTH =

ELSE IF (A(I).EQ.'A') THEN

LENGTH =

ELSE IF (A(I).EQ.'E') THEN

LENGTH =

ELSE IF (A(I).EQ.'N') THEN

LENGTH =

ELSE IF (A(I).EQ.'R') THEN

LENGTH =

ELSE IF (A(I).EQ.'U') THEN

LENGTH =

ELSE IF (A(I).EQ.'L') THEN

LENGTH =

ELSE IF (A(I).EQ.'S') THEN

```
      LENGTH =
ELSE IF (A(I).EQ.'K') THEN
      LENGTH =
ELSE IF (A(I).EQ.'D') THEN
      LENGTH =
ELSE IF (A(I).EQ.'T') THEN
      LENGTH =
ELSE IF (A(I).EQ.'M') THEN
      LENGTH =
ELSE IF (A(I).EQ.'Y') THEN
      LENGTH =
ELSE IF (A(I).EQ.'O') THEN
      LENGTH =
ELSE IF (A(I).EQ.'G') THEN
      LENGTH =
ELSE IF (A(I).EQ.'B') THEN
      LENGTH =
ELSE IF (A(I).EQ.'C') THEN
      LENGTH =
ELSE IF (A(I).EQ.',') THEN
      LENGTH =
ELSE IF (A(I).EQ.'.') THEN
      LENGTH =
ELSE IF (A(I).EQ.'Z') THEN
      LENGTH =
ELSE IF (A(I).EQ.'V') THEN
      LENGTH =
ELSE IF (A(I).EQ.'P') THEN
      LENGTH =
ELSE IF (A(I).EQ.'H') THEN
      LENGTH =
ELSE IF (A(I).EQ.'F') THEN
      LENGTH =
ELSE IF (A(I).EQ.'O') THEN
      LENGTH =
```

```
ELSE IF (A(I).EQ.'') THEN
    LENGTH =
ELSE IF (A(I).EQ.'1') THEN
    LENGTH =
ELSE IF (A(I).EQ.'") THEN
    LENGTH =
ELSE IF (A(I).EQ.'2') THEN
    LENGTH =
ELSE IF (A(I).EQ.')') THEN
    LENGTH =
ELSE IF (A(I).EQ.'5') THEN
    LENGTH =
ELSE IF (A(I).EQ.'3') THEN
    LENGTH =
ELSE IF (A(I).EQ.'8') THEN
    LENGTH =
ELSE IF (A(I).EQ.'(') THEN
    LENGTH =
ELSE IF (A(I).EQ.'4') THEN
    LENGTH =
ELSE IF (A(I).EQ.';') THEN
    LENGTH =
ELSE IF (A(I).EQ.'9') THEN
    LENGTH =
ELSE IF (A(I).EQ.'J') THEN
    LENGTH =
ELSE IF (A(I).EQ.'6') THEN
    LENGTH =
ELSE IF (A(I).EQ.'W') THEN
    LENGTH =
ELSE IF (A(I).EQ.':') THEN
    LENGTH =
ELSE IF (A(I).EQ.'7') THEN
    LENGTH =
ELSE IF (A(I).EQ.'-') THEN
```

```

        LENGTH =
    ELSE IF (A(I).EQ.'?') THEN
        LENGTH =
    ELSE IF (A(I).EQ.'X') THEN
        LENGTH =
    ELSE IF (A(I).EQ.'Q') THEN
        LENGTH =
    END IF
    LENGTH = LENGTH + DIFFER
    DIFFER = LENGTH - RATEO
    IF (DIFFER.LE.0.0) THEN
        R = R + 1
        DIFFER = 0.0
    ELSE
        DIFF2 = DIFFER - AINT(DIFFER)
        IF (DIFF2.GT.0.0) THEN
            DIFF1 = INT(DIFFER)
            DIFF1 = DIFF1 + 1
        ELSE
            DIFF1 = INT(DIFFER)
        END IF
        FLOW = BUFFER - DIFF1
        IF (FLOW.LT.0)THEN
            P = P + 1
        ELSE
            R = R + 1
        END IF
    END IF
300 CONTINUE
    PRINT,'LOST CHARACTERS          ARE = ',P
    PRINT,'TRANSMITTED CHARACTERS ARE = ',R
    PRINT,' '
    PRINT,' '
    PRINT,' '
200 CONTINUE

```

100 FORMAT(73 A1)

STOP

END

\$ENTRY

C (Insert the message itself below. Each line

C should consist of 73 characters.)

LIST OF REFERENCES

1. Hamming, R.W., Coding and Information Theory, Prentice-Hall, Inc., 1980.
2. Huffman, D., "A Method for the Construction of Minimum Redundancy Codes", Proceedings of the Institute of Radio Engineers, Vol. 40, pp. 1098-1101, September 1952.
3. Kilic, Suha, Modification of Huffman Coding, Master's Thesis, Naval Postgraduate School, Monterey, CA., March 1985.
4. Stegers, Wolfgang, ceyiren Hataysal H. "Modern Gemilerin Garip Biçimleri", Bilim ve Teknik, Cilt 16, Sayı 191, Ekim 1983.
5. Dr. Derman I. Ethem, "Uzay Mekigi'nin Oykusunu", Bilim ve Teknik, Cilt 17, Sayı 194, Ocak 1984.
6. SAS Institute Inc. SAS User's Guide: Basics 1982 Edition, Cary NC: SAS Institute Inc., 1982.
7. Foderaro, John K., The Franz Lisp Manual, University of California, 1980.
8. Winston, Patrick Henry, Horn Berthold Klaus Paul, LISP, 1984.
9. Kleinrock, Leonard, Communication Nets, Dover Publications, Inc., 1972.
10. Kleinrock, Leonard, Queueing Systems, Volume II, Computer Applications, John Wiley & Sons, Inc., 1976.

BIBLIOGRAPHY

Allen, O. Arnold, Probability, Statistics, and Queueing Theory, with Computer Science Applications, Academic Press, 1978.

Riordan, John, Stochastic Service Systems, John Wiley & Sons, Inc., 1962.

Trivedi, S. Kishor, Probability & Statistics with Reliability Queueing, and Computer Science Applications, Prentice-Hall, Inc., 1982.

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