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INFLUENCE OF HULL FORM PARAMETERS ON ROLL MOTION(U)  
DAVID M TAYLOR NAVAL SHIP RESEARCH AND DEVELOPMENT  
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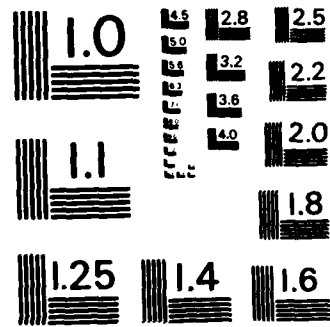
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# DAVID W. TAYLOR NAVAL SHIP RESEARCH AND DEVELOPMENT CENTER



Bethesda, Maryland 20084

AD-A159 804

## INFLUENCE OF HULL FORM PARAMETERS ON ROLL MOTION

by

David A. Walden

and

Paul J. Kopp

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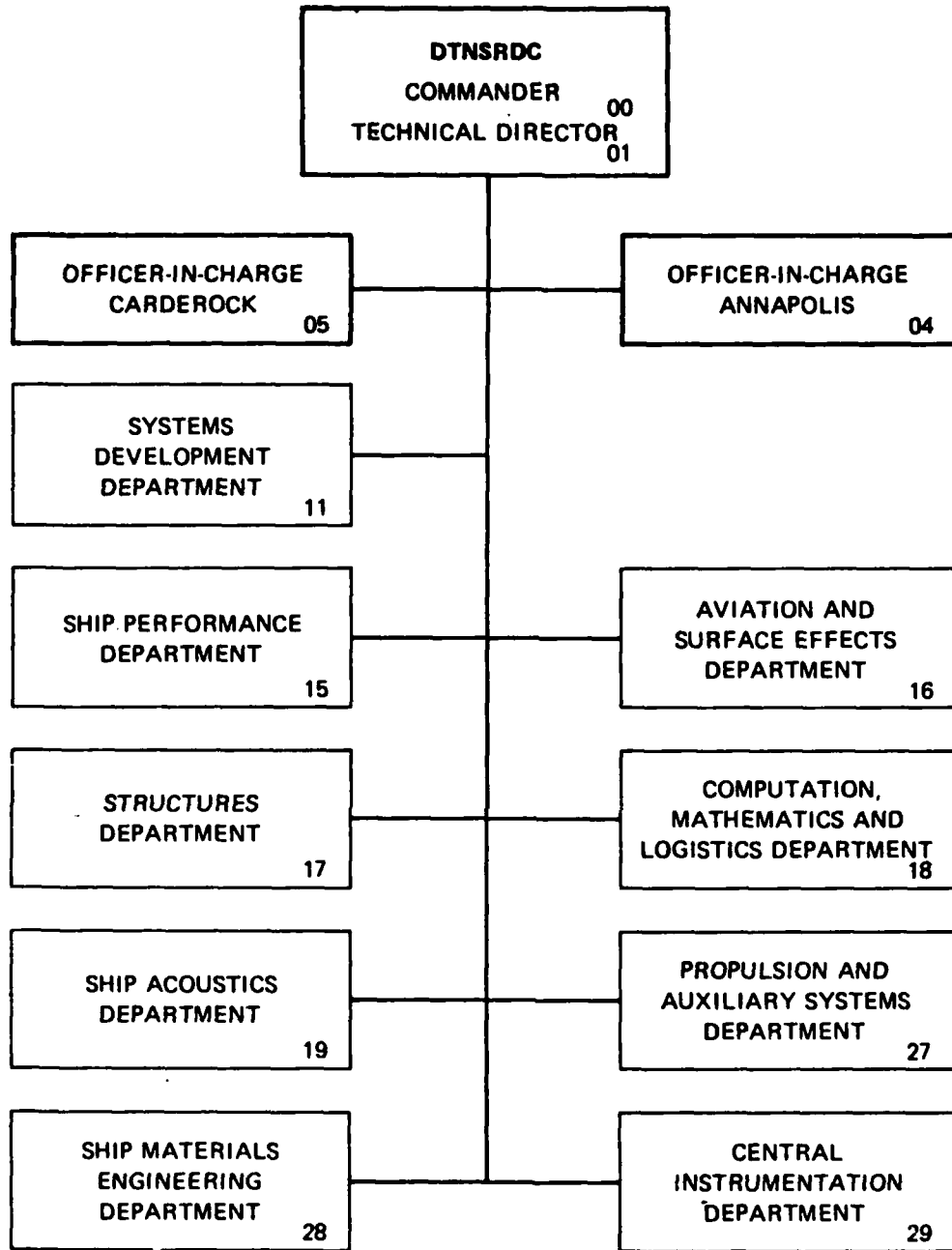
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INFLUENCE OF HULL FORM PARAMETERS ON ROLL MOTION

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NOTATION

L Length between perpendiculars  
 B Ship beam  
 C<sub>p</sub> Prismatic coefficient  
 C<sub>w</sub> Waterplane coefficient  
 C<sub>x</sub> Maximum section area coefficient  
 GM Metacentric height  
 KM Vertical location of metacenter above the baseline  
 LCF Longitudinal center of floatation expressed as percentage of L  
 aft of the forward perpendicular  
 p% p statistic (expected error, see page 3)  
 T Ship draft  
 VCG Vertical center of gravity  
 Δ Displacement

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## ABSTRACT

This report describes a statistical analysis of ship roll response as influenced by hull form parameters. A data base of 17 ships is described and regression analyses for the effect of hull form on roll angle are performed for three values of ship heading to wave direction and the maximum observed roll angle. Data for the ships that have antiroll fins are also presented.

## ADMINISTRATIVE INFORMATION

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## INTRODUCTION

The success of Bales<sup>1\*</sup> in quantifying the relation between hull form parameters and seakeeping performance in head seas has led to great interest in extending this work to oblique seas. The most important additional motion introduced by this extension is roll. The present work describes an investigation into the feasibility of developing seakeeping performance estimates based on hull form parameters for roll motion in a manner analogous to Bales' work for head seas.

## HULL FORM AND ROLL MOTION DATA BASE

In order to investigate the roll response of surface combatants, a data base of 17 ships was selected. These ships are frigates and destroyers and are a subset of ships used by Bales<sup>1</sup>. Seven of the 17 ships are equipped with antiroll fins and data is presented for these ships with and without antiroll fins.

The principal dimensions and hull form parameters are listed in Table 1.

## ROLL MOTION ANALYSIS

Ship motion calculations were carried out using the Navy's Standard Ship Motion Program (SMP81)<sup>2</sup> from which tabulated values of roll angles for long-crested seas were obtained. Roll angle data for ship headings to the wave direction of

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\*A complete listing of references is given on page 5.

60 (bow), 90 (beam), and 120 (quartering) degrees were extracted from the SMP81 output as well as the maximum observed roll angle.\* In all cases, a Bretschneider spectrum with a significant wave height of 3.5 meters and a ship speed of 30 knots was used. These are conditions in which frigates are expected to be fully operational. Table 2 contains a summary of the computed significant single amplitude roll angles.

To analyze the data, several regressions using ship characteristics and roll response were performed. These regressions were done using both multivariable stepwise and single independent variable regression methods.

In order to maintain statistical confidence in a regression with a relatively small sample size, a minimum number of independent variables should be used. To achieve this, two sets of regression calculations were performed. The first set of regressions uses a relatively large number of independent variables, while the second set of regressions use a much smaller number of variables.

Selection of the variables for the first set of regressions was based on an understanding of ship roll and previous analysis of the data used in this investigation. Ship motion theory indicates that the primary factors that determine roll response are functions of mass distribution (gyradius and the vertical center of mass), hydrodynamic damping (bilge keel area for example), and excitation force (governed by hull form, wave height and slope, and wave encounter frequency). One goal of the study was to determine if roll response could be predicted given the level of detail available at very early design stages. While vertical center of gravity and thus metacentric height is usually not available, it was decided to include metacentric height so that it would be possible to make a comparison of the regressions with and without the metacentric height included. Based on the regressions performed previously, the geometric variables that are considered to be of importance are ship length, beam, draft, prismatic coefficient, waterplane coefficient, and displacement.

The first set of regressions uses  $GM/B$ ,  $KM/B$ ,  $B/T$ ,  $C_p$ ,  $C_w$  and the squares of these variables. Additionally, displacement-length ratio and bilge keel area divided by length square are included. Table 3 shows the results of the single variable regressions for ship headings of 60, 90, and 120 degrees. Table 4 shows

---

\*The convention used in SMP81 is 0 degrees for head seas and 180 degrees for following seas.

the same regression results for the maximum observed roll angle. Results of the multivariable regression for the first selection of variables are not given because the number of variables used in the regression was close to the number of observations, leading to statistical uncertainty in the numeric results. The order in which variables were selected in each step of the regression was, however, used to determine the relative importance of each variable, since selection order is based on the sum of the squares reduced by the addition of a variable in the regression equation.

From the first set of regression results, the coefficient of determination for the single variable regressions and the order of selection for the multivariable regressions are used to reduce the number of variables. For the cases of ship headings of 60, 90, and 120 degrees, the variables that had the highest coefficient of determination and early selection were the same:  $GM/B$ ,  $(KM/B)^2$ ,  $(B/T)^2$ , and  $C_p$ . Plots of these coefficients versus roll angle at the three headings can be found in Figures 1 through 4. Figure 5 shows the cumulative proportion of the sum square reduced at each step in the multiple regression for beam seas. It can be seen that when  $GM/B$  is available, it gives the largest contribution. When  $GM/B$  is not used,  $(KM/B)^2$  gives the largest contribution, but the fit result is never as good as when  $GM/B$  is used. In the case of the maximum observed roll angle, a different set of variables was found to be significant, i.e.,  $(C_p)^2$ ,  $\Delta/(L/100)^3$ ,  $C_w^2$  and  $(B/T)^2$ . Figure 6 shows prismatic coefficient versus maximum expected roll angle. These two sets of variables then become the variables for the second set of regressions.

Tables 5 and 6 give the results for the second set of regressions. Table 5 gives the results for the multivariable regressions with and without  $GM/B$  for 60, 90, and 120 degree ship headings. Table 6 gives the results of the regression on the maximum observed roll angle. The coefficient of each variable in the regression equation is the slope of the regression plane in that dimension while the constant is the intercept of the regression plane with the roll angle axis. The standard deviation of the regression will give the range of error of the regression when multiplied by the square root of the number of independent variables. The  $p\%$  statistic is an indication of the expected error of the standard deviation as compared to the entire population and depends on the number of variables in the regression and the sample size<sup>3,4</sup>.

Table 7 shows the roll angles for the ships in the data base separated into groups of three GM/B ranges. The average roll angle for each range is plotted against ship heading in Figure 7. As the ship's heading goes from head to beam and then following seas, the influence of GM/B reverses. This can also be seen in the coefficients of the regression planes shown in Table 5. This agrees with trends shown by Schmitke<sup>5</sup>.

Figures 8 and 9 show the roll reduction obtained by using antiroll fins in beam seas and for the heading of maximum roll angle. The average reduction in roll is 64 percent for beam and 66 percent for the heading of maximum roll. Since the primary factors that control roll reduction with fins are the controller system and fin size, no correlation between hull form and roll reduction was observed.

Figure 10 shows the increase in operability for a destroyer hull form due to the addition of antiroll fins. Operability in this case is defined as the percentage of the time that the ship can operate in the winter North Atlantic without exceeding 8 degrees of roll, 3 degrees of pitch, 30 deck wetnesses per hour, 20 slams per hour, and 0.4g vertical acceleration at the bridge.

#### CONCLUSIONS

It has been shown that the dominant influence on roll response is metacentric height. This makes the estimation of roll response at very early design stages difficult since the location of the VCG is not available. Further, it is not possible to provide guidance on parameters other than GM because change in these parameters can have positive or negative influence on roll motion depending on the value of GM. Since it has been shown in a recent investigation for the Naval Studies Board, that adequately sized antiroll fins can reduce roll to the point where it is not the limiting motion, the recommended procedure for Navy combatants is to develop hull forms to reduce pitch and heave related responses and to provide adequate fins and bilge keels to reduce roll.

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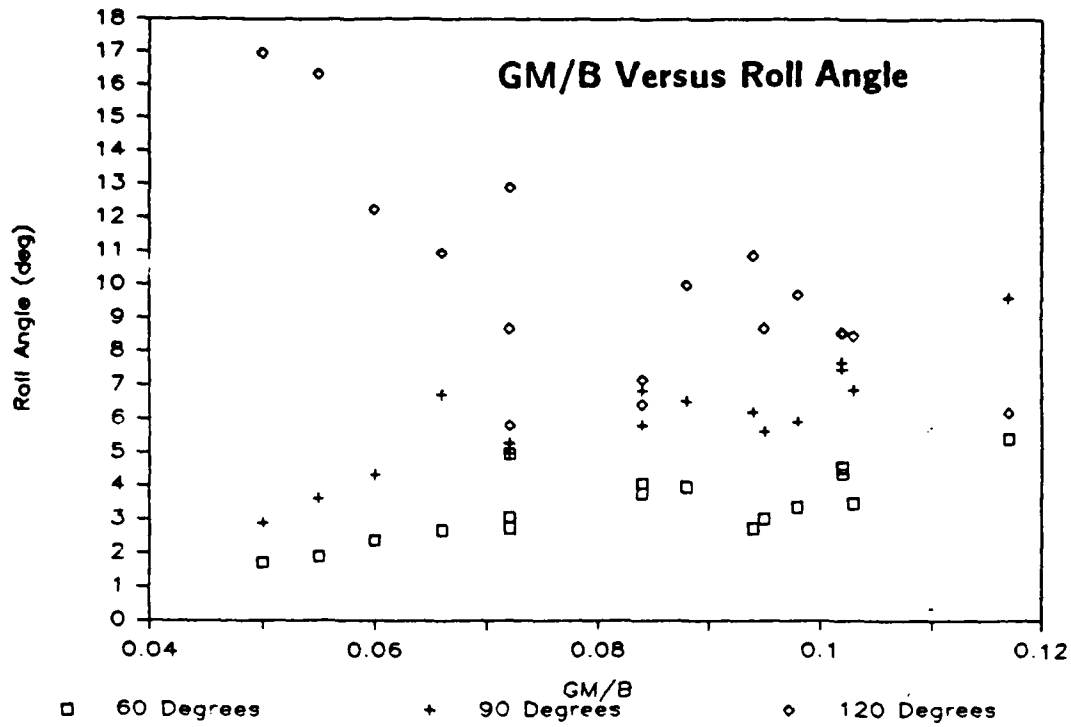


Figure 1 - GM/B versus Roll Angle

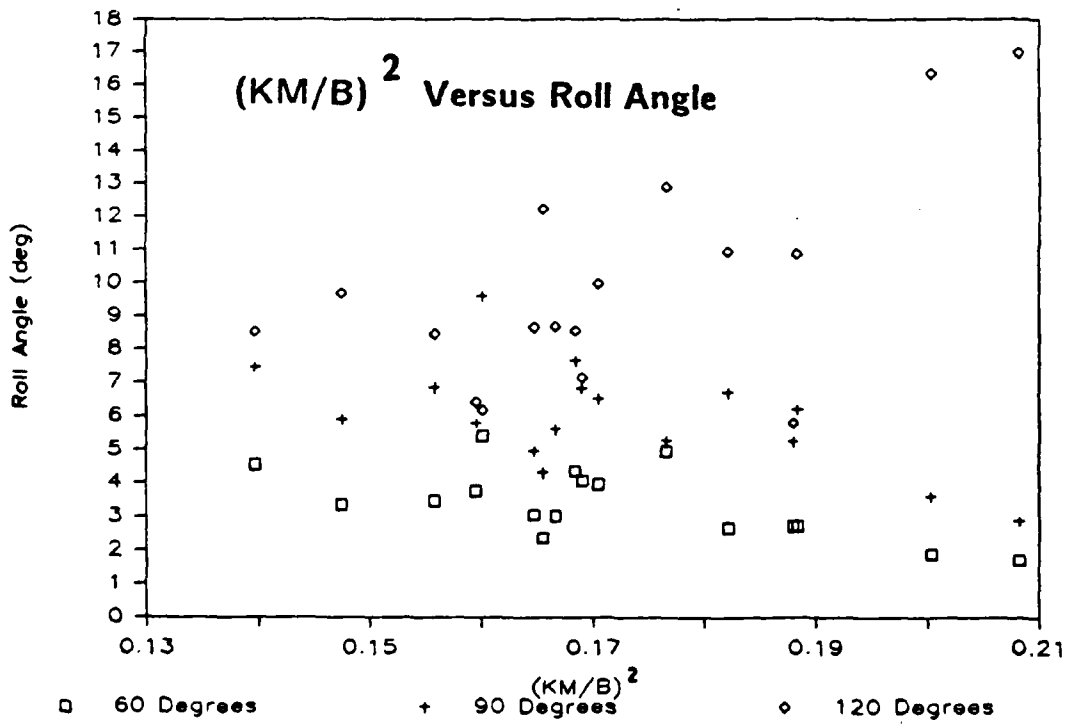


Figure 2 - (KM/B)<sup>2</sup> versus Roll Angle

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| GM/B= 0.05 - 0.08 |       |       |        |        |        |         |       |       |        | GM/B= 0.08 - 0.10 |        |         |       |       |        |       |        |  |  |
|-------------------|-------|-------|--------|--------|--------|---------|-------|-------|--------|-------------------|--------|---------|-------|-------|--------|-------|--------|--|--|
| GM/B              | R60   | R90   | R105   | R120   | ship # | GM/B    | R60   | R90   | RMAX   | R120              | ship # | GM/B    | R60   | R90   | RMAX   | R120  | ship # |  |  |
| 0.050             | 1.71  | 2.89  |        | 16.98  | 15     | 0.084   | 3.76  | 5.79  | 13.52  | 6.42              | 6      | 0.084   | 3.76  | 5.79  | 13.52  | 6.42  | 6      |  |  |
| 0.055             | 1.89  | 3.61  |        | 16.34  | 16     | 0.084   | 4.08  | 6.85  | 15.00  | 7.15              | 17     | 0.084   | 4.08  | 6.85  | 15.00  | 7.15  | 17     |  |  |
| 0.060             | 2.38  | 4.33  |        | 12.25  | 5      | 0.088   | 3.97  | 6.51  | 19.20  | 9.97              | 7      | 0.088   | 3.97  | 6.51  | 19.20  | 9.97  | 7      |  |  |
| 0.066             | 2.68  | 6.70  | 21.18  | 10.94  | 12     | 0.094   | 2.73  | 6.20  | 25.65  | 10.87             | 11     | 0.094   | 2.73  | 6.20  | 25.65  | 10.87 | 11     |  |  |
| 0.072             | 2.74  | 5.25  | 10.54  | 5.79   | 13     | 0.095   | 3.02  | 5.61  | 17.39  | 8.68              | 14     | 0.095   | 3.02  | 5.61  | 17.39  | 8.68  | 14     |  |  |
| 0.072             | 4.94  | 5.27  | 36.67  | 12.29  | 4      | 0.098   | 3.37  | 5.92  | 19.98  | 9.68              | 10     | 0.098   | 3.37  | 5.92  | 19.98  | 9.68  | 10     |  |  |
| 0.072             | 3.06  | 4.97  | 13.70  | 8.67   | 3      |         |       |       |        |                   |        |         |       |       |        |       |        |  |  |
| average           |       |       |        |        |        | average |       |       |        |                   |        | average |       |       |        |       |        |  |  |
| 0.064             | 2.771 | 4.717 | 20.523 | 11.894 |        | 0.091   | 3.488 | 6.147 | 18.457 | 8.795             |        | 0.091   | 3.488 | 6.147 | 18.457 | 8.795 |        |  |  |

| GM/B= 0.10 - 0.12 |       |       |        |       |        |         |       |       |        |       |        |
|-------------------|-------|-------|--------|-------|--------|---------|-------|-------|--------|-------|--------|
| GM/B              | R60   | R90   | RMAX   | R120  | ship # | GM/B    | R60   | R90   | RMAX   | R120  | ship # |
| 0.102             | 4.36  | 7.66  | 20.67  | 8.56  | 2      | 0.102   | 4.54  | 7.46  | 24.05  | 8.53  | 8      |
| 0.102             | 4.54  | 7.46  | 24.05  | 8.53  | 8      | 0.103   | 3.49  | 6.86  | 19.95  | 8.46  | 1      |
| 0.103             | 3.49  | 6.86  | 19.95  | 8.46  | 1      | 0.117   | 5.41  | 9.59  | 14.58  | 6.18  | 9      |
| 0.117             | 5.41  | 9.59  | 14.58  | 6.18  | 9      |         |       |       |        |       |        |
| average           |       |       |        |       |        | average |       |       |        |       |        |
| 0.106             | 4.450 | 7.893 | 19.813 | 7.933 |        | 0.106   | 4.450 | 7.893 | 19.813 | 7.933 |        |

TABLE 7 - ROLL SEPARATED BY GM/B RANGES AND HEADING



|                    |           |
|--------------------|-----------|
| Coefficients:      |           |
| Cp <sup>2</sup>    | 103.42720 |
| Disp-L             | -0.14628  |
| Cv <sup>2</sup>    | -59.94104 |
| (B/T) <sup>2</sup> | -0.61700  |
| Constant:          | 10.37530  |
| Cumulative Sum of  |           |
| Squares Reduced:   | 21%       |
| Standard           |           |
| Deviation:         | 5.63      |
| p%                 | 40%       |

TABLE 6 - MULTI-VARIABLE REGRESSION FOR MAXIMUM EXPECTED ROLL ANGLE

GM/B Included In Regression      GM/B Not Included In Regression      GM/B Included In Regression      GM/B Not Included In Regression

60 Degree Heading

Coefficients:  
 GM/B      28.61994  
 (GM/B)<sup>2</sup>    -16.69558  
 (B/T)<sup>2</sup>    -0.19731  
 Cp        -0.77042  
 Constant:    6.33871

Cumulative Sum of  
 Squares Reduced:    67%      53%  
 Standard Deviation:    0.58      0.69  
 p%                    40%      37%

90 Degree Heading

Coefficients:  
 GM/B      71.88931  
 (GM/B)<sup>2</sup>    -3.71507  
 (B/T)<sup>2</sup>    -0.22251  
 Cp        2.76008  
 Constant:    1.12526

Cumulative Sum of  
 Squares Reduced:    83%      46%  
 Standard Deviation:    0.64      1.14  
 p%                    40%      37%

GM/B Included In Regression      GM/B Not Included In Regression

120 Degree Heading

Coefficients:  
 GM/B      -76.95155  
 (GM/B)<sup>2</sup>    65.04913  
 (B/T)<sup>2</sup>    0.57719  
 Cp        -2.28124  
 Constant:    0.83420

Cumulative Sum of  
 Squares Reduced:    63%      53%  
 Standard Deviation:    1.90      2.15  
 p%                    40%      37%

Coefficients:  
 GM/B      120.01780  
 (GM/B)<sup>2</sup>    0.62976  
 Cp        3.30193  
 Constant:    -18.97141

Cumulative Sum of  
 Squares Reduced:    53%      46%  
 Standard Deviation:    2.15      1.14  
 p%                    37%      37%

TABLE 5 - MULTI-VARIABLE REGRESSIONS FOR 60, 90 AND 120 DEGREE HEADINGS

| Roll                  | GM/B    | (GM/B) <sup>2</sup> | KM/B    | (KM/B) <sup>2</sup> | B/T     | (B/T) <sup>2</sup> | AREA/L <sup>2</sup> | DISP-L  | Cp       | Cp <sup>2</sup> | Cw       | Cw <sup>2</sup> |
|-----------------------|---------|---------------------|---------|---------------------|---------|--------------------|---------------------|---------|----------|-----------------|----------|-----------------|
| 10.54                 | 0.0498  | 0.0025              | 0.3758  | 0.1397              | 2.5605  | 6.5560             | 0.0066              | 50.9415 | 0.5800   | 0.3364          | 0.7130   | 0.5084          |
| 36.67                 | 0.1172  | 0.0137              | 0.4563  | 0.2082              | 3.7318  | 13.9261            | 0.0138              | 77.7691 | 0.6700   | 0.4489          | 0.8150   | 0.6642          |
| 18.67                 | 0.0833  | 0.0073              | 0.4133  | 0.1712              | 3.1445  | 9.9713             | 0.0108              | 63.0614 | 0.6194   | 0.3844          | 0.7585   | 0.5761          |
| intercept             | 16.7046 | 16.8421             | 22.5628 | 20.5448             | 32.8230 | 26.0233            | 14.0995             | 4.2007  | -34.1712 | -7.2758         | -17.3188 | 0.8417          |
| slope                 | 47.5585 | 250.7170            | -9.4276 | -10.9692            | -4.5021 | -0.7378            | 421.4876            | 0.2294  | 85.3030  | 67.4908         | 47.4445  | 30.9389         |
| variance of x         | 0.0004  | 0.00001             | 0.0005  | 0.0003              | 0.0891  | 3.5172             | 0.000003            | 60.1752 | 0.0008   | 0.0012          | 0.0009   | 0.0021          |
| variance of y         | 38.60   |                     |         |                     |         |                    |                     |         |          |                 |          |                 |
| var of regression     | 40.1309 | 40.3470             | 40.9727 | 40.9754             | 39.0975 | 38.9820            | 40.4372             | 37.6518 | 35.1722  | 35.1934         | 38.8394  | 38.8459         |
| correlation coeff     | 0.1469  | 0.1277              | -0.0326 | -0.0315             | -0.2163 | -0.2227            | 0.1188              | 0.2864  | 0.3775   | 0.3768          | 0.2304   | 0.2300          |
| coef of determination | 0.0216  | 0.0163              | 0.0011  | 0.0010              | 0.0468  | 0.0496             | 0.0141              | 0.0820  | 0.1425   | 0.1420          | 0.0531   | 0.0529          |

Maximum Expected  
Roll Angle

TABLE 4 - LINEAR REGRESSIONS OF A SINGLE INDEPENDENT VARIABLE  
ON MAXIMUM EXPECTED ROLL ANGLE

| Roll                      | GM/B  | (GM/B) <sup>2</sup> | KM/B     | (KM/B) <sup>2</sup> | B/T      | (B/T) <sup>2</sup> | AREA/L <sup>2</sup> | DISP-L   | Cp       | Cp <sup>2</sup> | CW      | CW <sup>2</sup> |
|---------------------------|-------|---------------------|----------|---------------------|----------|--------------------|---------------------|----------|----------|-----------------|---------|-----------------|
| <b>60 Degree Heading</b>  |       |                     |          |                     |          |                    |                     |          |          |                 |         |                 |
| minimum                   | 1.71  | 0.0498              | 0.0025   | 0.3738              | 0.1397   | 2.5605             | 6.5560              | 50.9415  | 0.5800   | 0.3364          | 0.7130  | 0.5084          |
| maximum                   | 5.41  | 0.1172              | 0.0137   | 0.4563              | 0.2082   | 3.7318             | 13.9261             | 77.7691  | 0.6700   | 0.4489          | 0.8150  | 0.6642          |
| average                   | 3.42  | 0.0833              | 0.0073   | 0.4133              | 0.1712   | 3.1445             | 9.9713              | 63.0614  | 0.6194   | 0.3844          | 0.7585  | 0.5761          |
| intercept                 |       | 0.1591              | 1.7239   | 15.8288             | 9.6799   | 6.4341             | 5.0527              | 3.1384   | 8.4696   | 5.8005          | 6.8875  | 5.1646          |
| slope                     |       | 39.1361             | 233.0150 | -30.0261            | -36.5609 | -0.9587            | -0.1638             | -14.4390 | -8.1532  | -6.1946         | -4.5725 | -3.0291         |
| variance of x             |       | 0.0004              | 0.00001  | 0.0005              | 0.0003   | 0.0891             | 3.5172              | 0.000003 | 0.0008   | 0.0012          | 0.0009  | 0.0021          |
| variance of y             | 1.09  |                     |          |                     |          |                    |                     |          |          |                 |         |                 |
| var of regression         |       | 0.5555              | 0.5769   | 0.7139              | 0.7018   | 1.0679             | 1.0547              | 1.1543   | 1.1015   | 1.1059          | 1.1347  | 1.1341          |
| correlation coeff         |       | 0.7204              | 0.7074   | -0.6179             | -0.6263  | -0.2745            | -0.2946             | -0.0243  | -0.2150  | -0.2061         | -0.1323 | -0.1342         |
| coef of determination     |       | 0.5190              | 0.5005   | 0.3818              | 0.3923   | 0.0753             | 0.0868              | 0.0006   | 0.0011   | 0.0425          | 0.0175  | 0.0180          |
| <b>90 Degree Heading</b>  |       |                     |          |                     |          |                    |                     |          |          |                 |         |                 |
| minimum                   | 2.89  | 0.0498              | 0.0025   | 0.3738              | 0.1397   | 2.5605             | 6.5560              | 50.9415  | 0.5800   | 0.3364          | 0.7130  | 0.5084          |
| maximum                   | 9.59  | 0.1172              | 0.0137   | 0.4563              | 0.2082   | 3.7318             | 13.9261             | 77.7691  | 0.6700   | 0.4489          | 0.8150  | 0.6642          |
| average                   | 5.97  | 0.0833              | 0.0073   | 0.4133              | 0.1712   | 3.1445             | 9.9713              | 63.0614  | 0.6194   | 0.3844          | 0.7585  | 0.5761          |
| intercept                 |       | -0.0250             | 2.7980   | 24.1393             | 15.1473  | 9.7446             | 7.9828              | 5.9106   | 13.0987  | 9.3815          | 8.8877  | 7.4794          |
| slope                     |       | 71.9496             | 435.7637 | -43.9655            | -53.6017 | -1.2008            | -0.2020             | 5.3731   | -11.5107 | -8.8783         | -3.8484 | -2.6220         |
| variance of x             |       | 0.0004              | 0.00001  | 0.0005              | 0.0003   | 0.0891             | 3.5172              | 0.000003 | 0.0008   | 0.0012          | 0.0009  | 0.0021          |
| variance of y             | 2.53  |                     |          |                     |          |                    |                     |          |          |                 |         |                 |
| var of regression         |       | 0.6662              | 0.6708   | 1.7468              | 1.7184   | 2.5558             | 2.6922              | 2.6668   | 2.5859   | 2.5915          | 2.6780  | 2.6767          |
| correlation coeff         |       | 0.8675              | 0.8665   | -0.5926             | -0.6014  | -0.2252            | -0.2380             | 0.0059   | -0.1988  | -0.1935         | -0.0729 | -0.0761         |
| coef of determination     |       | 0.7526              | 0.7508   | 0.3512              | 0.3617   | 0.0507             | 0.0566              | .0000    | 0.0395   | 0.0374          | 0.0053  | 0.0058          |
| <b>120 Degree Heading</b> |       |                     |          |                     |          |                    |                     |          |          |                 |         |                 |
| minimum                   | 5.79  | 0.0498              | 0.0025   | 0.3738              | 0.1397   | 2.5605             | 6.5560              | 50.9415  | 0.5800   | 0.3364          | 0.7130  | 0.5084          |
| maximum                   | 16.98 | 0.1172              | 0.0137   | 0.4563              | 0.2082   | 3.7318             | 13.9261             | 77.7691  | 0.6700   | 0.4489          | 0.8150  | 0.6642          |
| average                   | 9.90  | 0.0833              | 0.0073   | 0.4133              | 0.1712   | 3.1445             | 9.9713              | 63.0614  | 0.6194   | 0.3844          | 0.7585  | 0.5761          |
| intercept                 |       | 19.5612             | 14.6844  | -28.8765            | -9.7912  | 0.5111             | 5.0343              | 5.3751   | -3.8082  | 3.4749          | -3.3072 | 3.4502          |
| slope                     |       | -115.916            | -656.876 | 95.8357             | 115.0225 | 2.9874             | 0.4884              | 418.0454 | 0.0990   | 16.7276         | 17.4192 | 11.2033         |
| variance of x             |       | 0.0004              | 0.00001  | 0.0005              | 0.0003   | 0.0891             | 3.5172              | 0.000003 | 0.0008   | 0.0012          | 0.0009  | 0.0021          |
| variance of y             | 10.46 |                     |          |                     |          |                    |                     |          |          |                 |         |                 |
| var of regression         |       | 5.8525              | 6.5180   | 6.8045              | 6.6269   | 10.2666            | 10.2199             | 10.5416  | 10.7178  | 10.7537         | 10.8180 | 10.8268         |
| correlation coeff         |       | -0.6880             | -0.6430  | 0.6226              | 0.6353   | 0.2757             | 0.2833              | 0.2264   | 0.1882   | 0.1794          | 0.1625  | 0.1600          |
| coef of determination     |       | 0.4733              | 0.4134   | 0.3876              | 0.4036   | 0.0760             | 0.0802              | 0.0513   | 0.0354   | 0.0322          | 0.0264  | 0.0256          |

TABLE 3 - LINEAR REGRESSIONS OF A SINGLE INDEPENDENT VARIABLE ON ROLL ANGLE AT 60, 90, AND 120 DEGREE HEADINGS

| Ship Number | Maximum Roll | Heading at Max | 60 Degree |         | 90 Degree |         | 120 Degree     |                | 90 Degree |  |
|-------------|--------------|----------------|-----------|---------|-----------|---------|----------------|----------------|-----------|--|
|             |              |                | Heading   | Heading | Heading   | Heading | Roll With Fine | Roll With Fine |           |  |
| 1           | 19.95        | 105            | 3.49      | 6.86    | 8.46      | 6.05    | 3.49           |                |           |  |
| 2           | 20.67        | 105            | 4.36      | 7.66    | 8.56      | 9.77    | 3.51           |                |           |  |
| 3           | 13.70        | 105            | 3.06      | 4.97    | 8.67      | 6.41    | 1.18           |                |           |  |
| 4           | 36.67        | 105            | 4.94      | 5.27    | 12.90     | 5.06    | 0.77           |                |           |  |
| 5           | 12.25        | 120            | 2.38      | 4.33    | 12.25     | 7.58    | 1.67           |                |           |  |
| 6           | 13.52        | 105            | 3.76      | 5.79    | 6.42      |         |                |                |           |  |
| 7           | 19.20        | 105            | 3.97      | 6.51    | 9.97      |         |                |                |           |  |
| 8           | 24.05        | 105            | 4.54      | 7.46    | 8.53      |         |                |                |           |  |
| 9           | 14.58        | 105            | 5.41      | 9.59    | 6.18      |         |                |                |           |  |
| 10          | 19.98        | 105            | 3.37      | 5.92    | 9.68      | 5.74    | 1.86           |                |           |  |
| 11          | 25.65        | 105            | 2.73      | 6.20    | 10.87     | 5.30    | 1.86           |                |           |  |
| 12          | 21.18        | 105            | 2.68      | 6.70    | 10.94     |         |                |                |           |  |
| 13          | 10.54        | 105            | 2.74      | 5.25    | 5.79      |         |                |                |           |  |
| 14          | 17.39        | 105            | 3.02      | 5.61    | 8.69      |         |                |                |           |  |
| 15          | 16.98        | 120            | 1.71      | 2.89    | 16.98     |         |                |                |           |  |
| 16          | 16.34        | 120            | 1.89      | 3.61    | 16.34     |         |                |                |           |  |
| 17          | 15.00        | 105            | 4.08      | 6.85    | 7.15      |         |                |                |           |  |
| average     | 18.67        |                | 3.42      | 5.97    | 9.90      |         |                |                |           |  |
| minimum     | 10.54        |                | 1.71      | 2.89    | 5.79      |         |                |                |           |  |
| maximum     | 36.67        |                | 5.41      | 9.59    | 16.98     |         |                |                |           |  |

TABLE 2 - SIGNIFICANT SINGLE AMPLITUDE ROLL ANGLE

| Ship Number     | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9     | 10     | 11     | 12     | 13     | 14     | 15     | 16     | 17     |
|-----------------|--------|--------|--------|--------|--------|--------|--------|--------|-------|--------|--------|--------|--------|--------|--------|--------|--------|
| L (m)           | 106.38 | 131.00 | 109.75 | 109.75 | 119.48 | 161.24 | 124.36 | 126.49 | 93.88 | 121.77 | 106.00 | 105.00 | 128.00 | 142.50 | 124.00 | 121.31 | 108.51 |
| B (m)           | 13.30  | 14.79  | 13.11  | 12.73  | 14.33  | 16.70  | 13.78  | 14.26  | 10.92 | 14.40  | 11.98  | 11.01  | 13.33  | 15.29  | 13.85  | 15.24  | 12.80  |
| T (m)           | 3.78   | 4.62   | 4.14   | 4.51   | 3.84   | 5.97   | 4.52   | 4.72   | 3.43  | 4.27   | 3.75   | 4.30   | 4.80   | 4.50   | 4.05   | 4.75   | 4.22   |
| Displ (cu. m)   | 2884   | 4352   | 2939   | 3502   | 3645   | 8004   | 3596   | 4257   | 1778  | 3406   | 2385   | 2761   | 4664   | 5024   | 3567   | 4710   | 2938   |
| Cv              | 0.75   | 0.75   | 0.72   | 0.80   | 0.75   | 0.74   | 0.73   | 0.74   | 0.77  | 0.71   | 0.78   | 0.81   | 0.82   | 0.75   | 0.75   | 0.79   | 0.75   |
| Cx              | 0.78   | 0.78   | 0.80   | 0.81   | 0.87   | 0.84   | 0.75   | 0.81   | 0.83  | 0.78   | 0.77   | 0.80   | 0.83   | 0.81   | 0.82   | 0.84   | 0.80   |
| Cp              | 0.63   | 0.61   | 0.60   | 0.67   | 0.62   | 0.58   | 0.60   | 0.60   | 0.59  | 0.60   | 0.63   | 0.67   | 0.67   | 0.62   | 0.61   | 0.62   | 0.61   |
| LCF (% L)       | 0.58   | 0.55   | 0.57   | 0.58   | 0.54   | 0.58   | 0.55   | 0.57   | 0.57  | 0.57   | 0.59   | 0.55   | 0.55   | 0.55   | 0.55   | 0.58   | 0.56   |
| DK AREA (sq. m) | 119    | 158    | 116    | 119    | 94     | 267    | 191    | 189    | 110   | 188    | 137    | 105    | 174    | 208    | 212    | 182    | 118    |
| AREA/L          | 1.12   | 1.21   | 1.06   | 1.08   | 0.79   | 1.66   | 1.54   | 1.49   | 1.17  | 1.54   | 1.29   | 1.00   | 1.36   | 1.46   | 1.71   | 1.50   | 1.09   |
| GM (m)          | 1.37   | 1.51   | 0.94   | 0.92   | 0.86   | 1.41   | 1.21   | 1.46   | 1.28  | 1.41   | 1.13   | 0.73   | 0.96   | 1.46   | 0.69   | 0.84   | 1.08   |
| GM/B            | 0.103  | 0.102  | 0.072  | 0.072  | 0.060  | 0.084  | 0.088  | 0.102  | 0.117 | 0.098  | 0.094  | 0.066  | 0.072  | 0.095  | 0.050  | 0.055  | 0.084  |
| KG (m)          | 5.25   | 6.07   | 5.32   | 5.35   | 5.85   | 6.67   | 5.69   | 5.33   | 4.37  | 5.53   | 5.20   | 4.70   | 5.78   | 6.24   | 6.32   | 6.82   | 5.26   |
| KG/B            | 0.395  | 0.410  | 0.406  | 0.420  | 0.407  | 0.399  | 0.413  | 0.374  | 0.400 | 0.384  | 0.434  | 0.427  | 0.434  | 0.408  | 0.456  | 0.448  | 0.411  |
| L/B             | 8.00   | 8.86   | 8.37   | 8.62   | 8.34   | 9.66   | 9.02   | 8.87   | 8.60  | 8.46   | 8.85   | 9.54   | 9.60   | 9.32   | 8.95   | 7.96   | 8.48   |
| B/T             | 3.52   | 3.20   | 3.17   | 2.82   | 3.73   | 2.80   | 3.05   | 3.02   | 3.18  | 3.37   | 3.19   | 2.56   | 2.78   | 3.40   | 3.42   | 3.21   | 3.83   |

TABLE 1 - HULL FORM CHARACTERISTICS

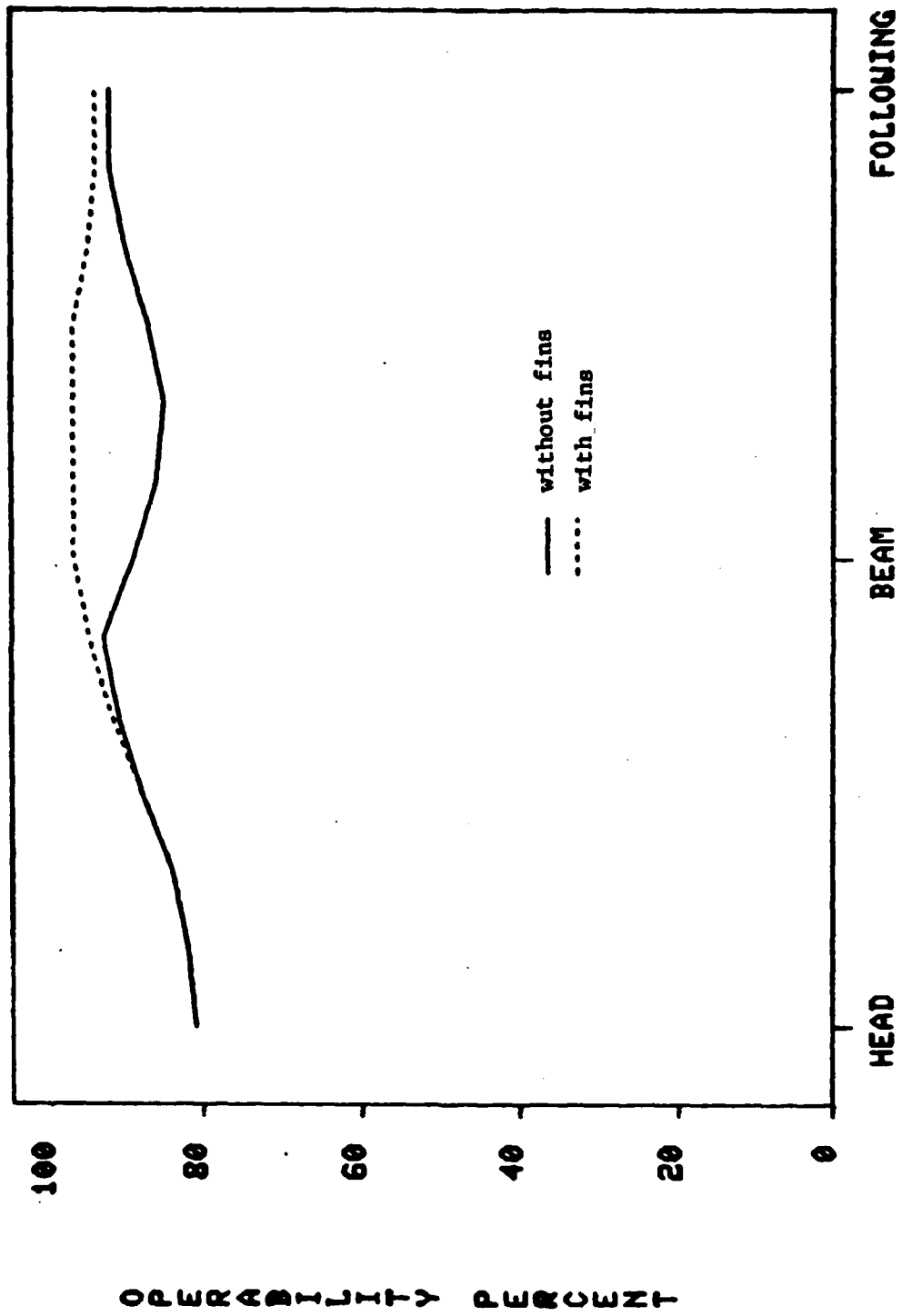


Figure 10 - Operability With and Without Anti-Roll Fins on a Destroyer Hull Form

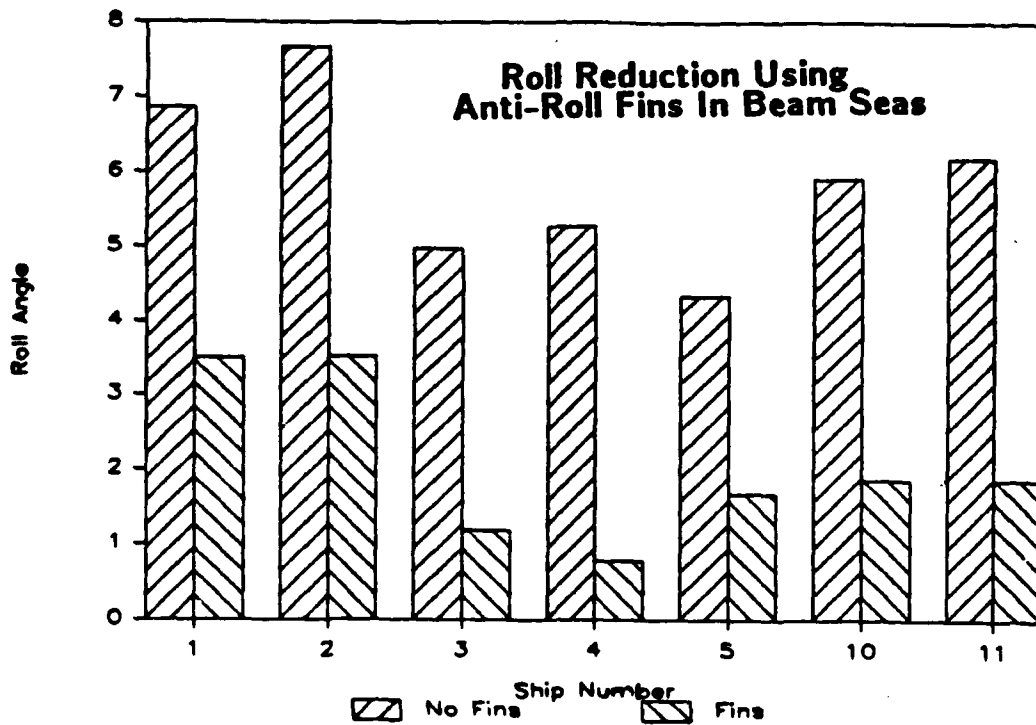


Figure 8 - Roll Reducting Using Anti-Roll Fins in Beam Seas

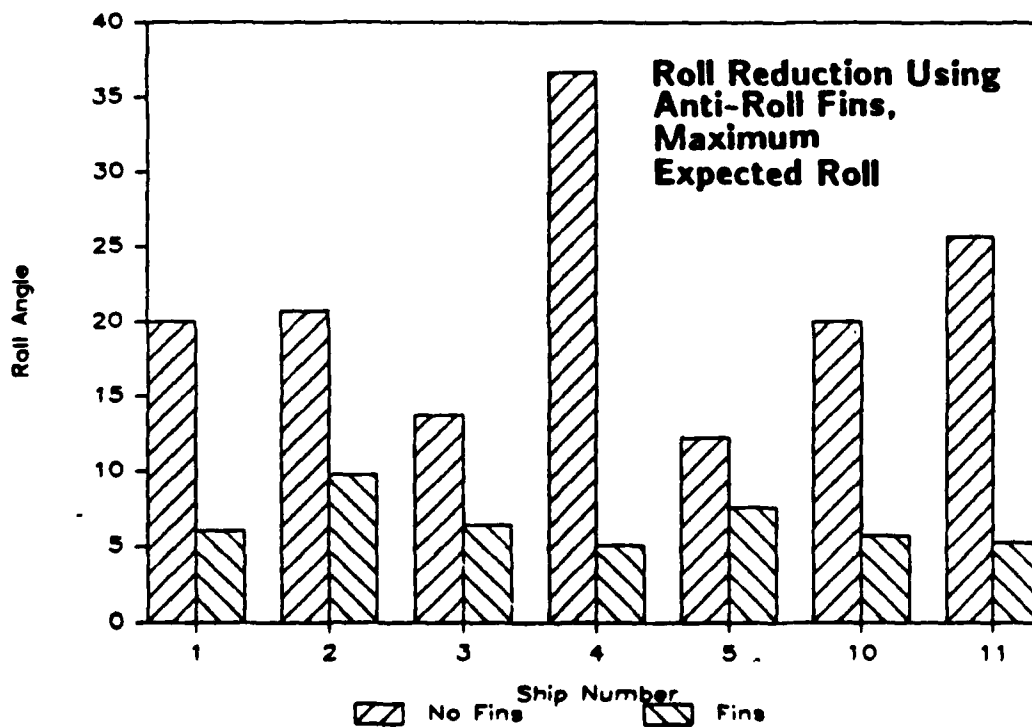


Figure 9 - Roll Reduction Using Anti-Roll Fins, Maximum Expected Roll



### Roll Variation With Heading And GM/B

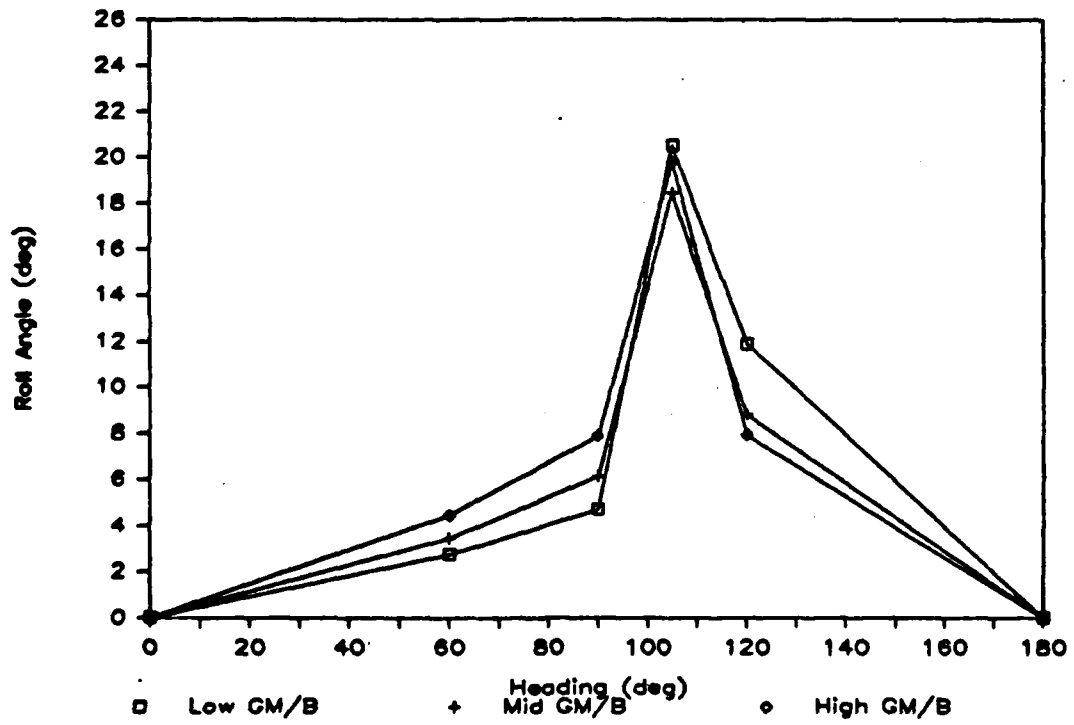


Figure 7 - Roll Variation with Heading and GM/B

### Prismatic Coefficient Versus Maximum Expected Roll

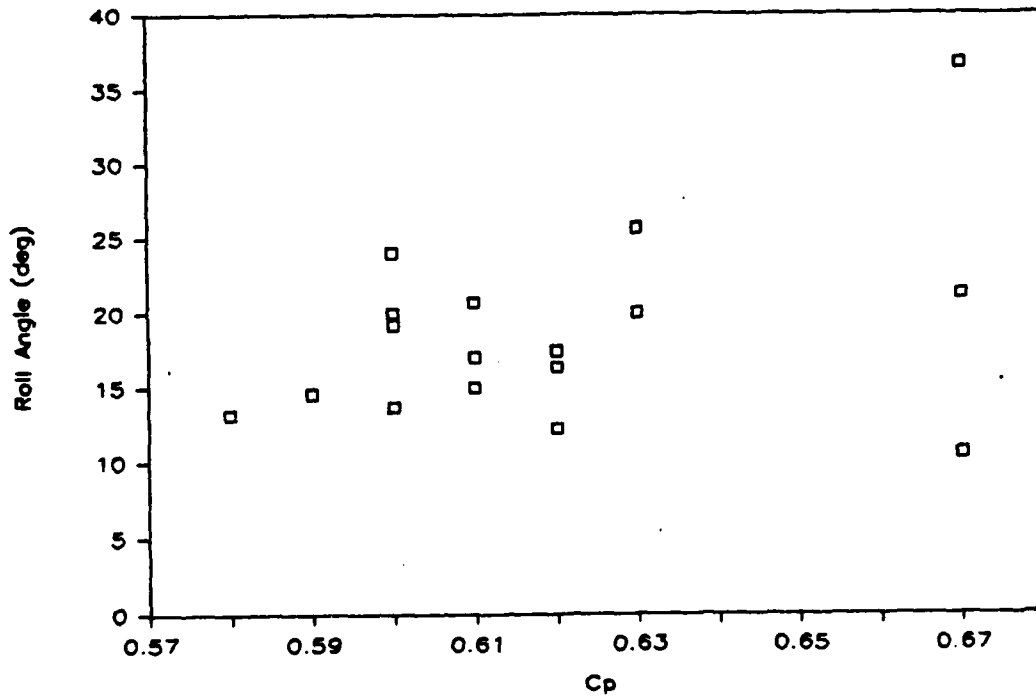


Figure 6 - Prismatic Coefficient versus Maximum Expected Roll

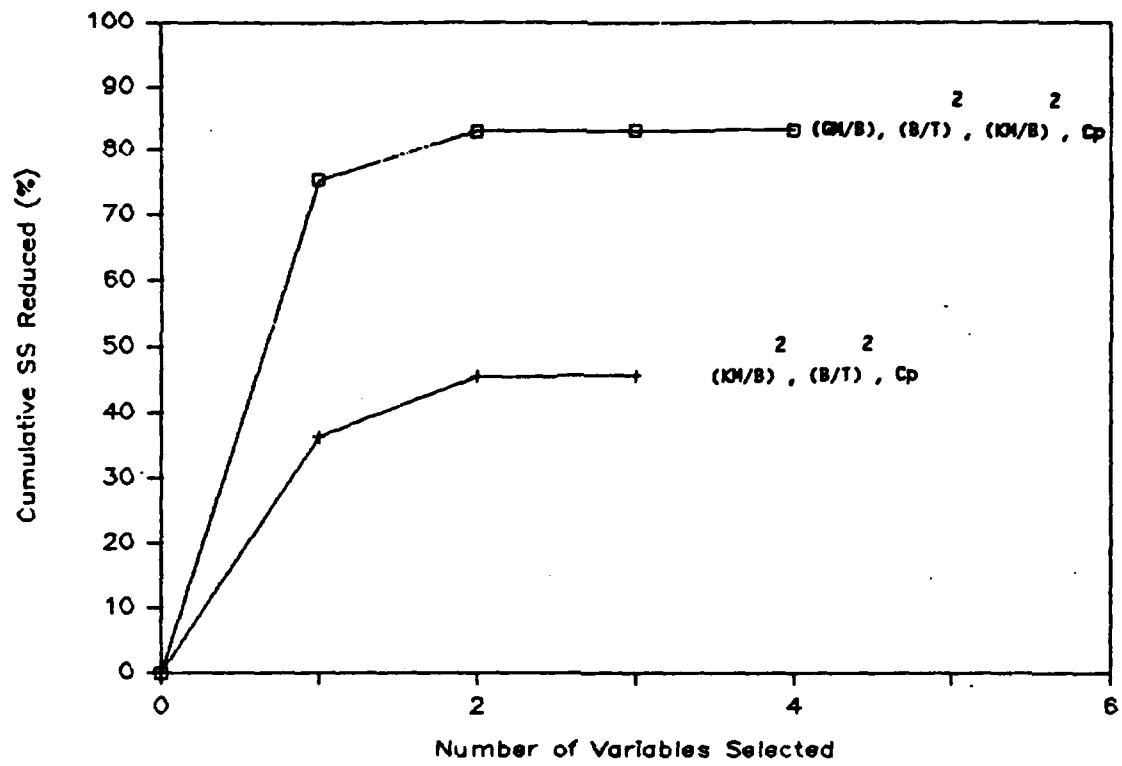


Figure 5 - Summary of Stepwise Regression for Beam Seas

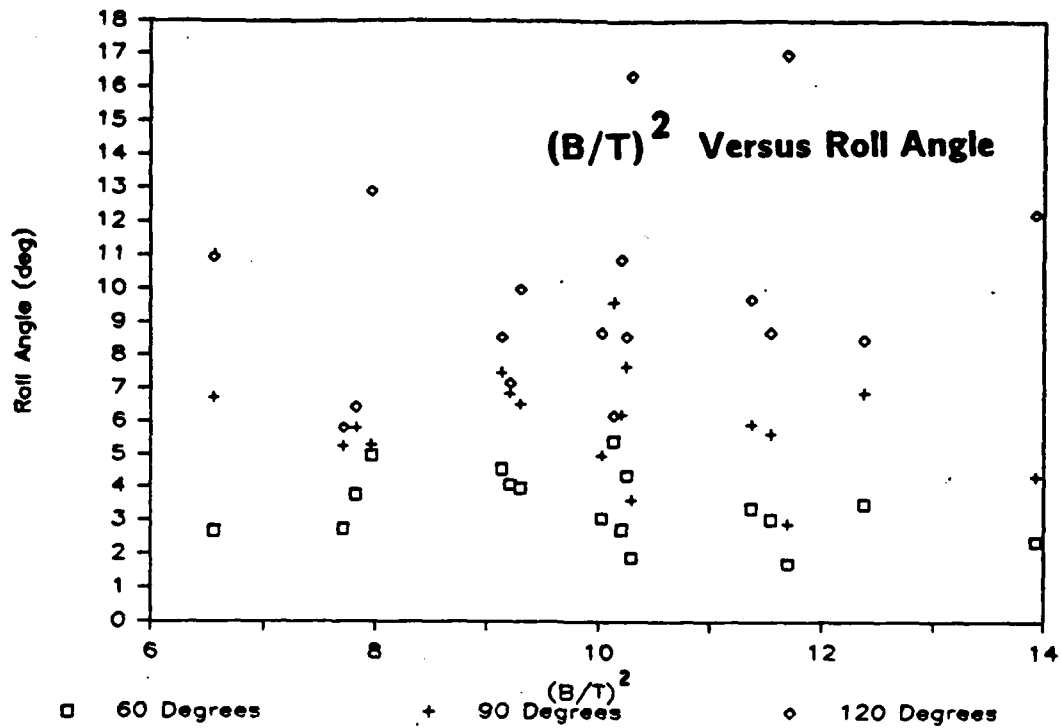


Figure 3 - (B/T)<sup>2</sup> versus Roll Angle

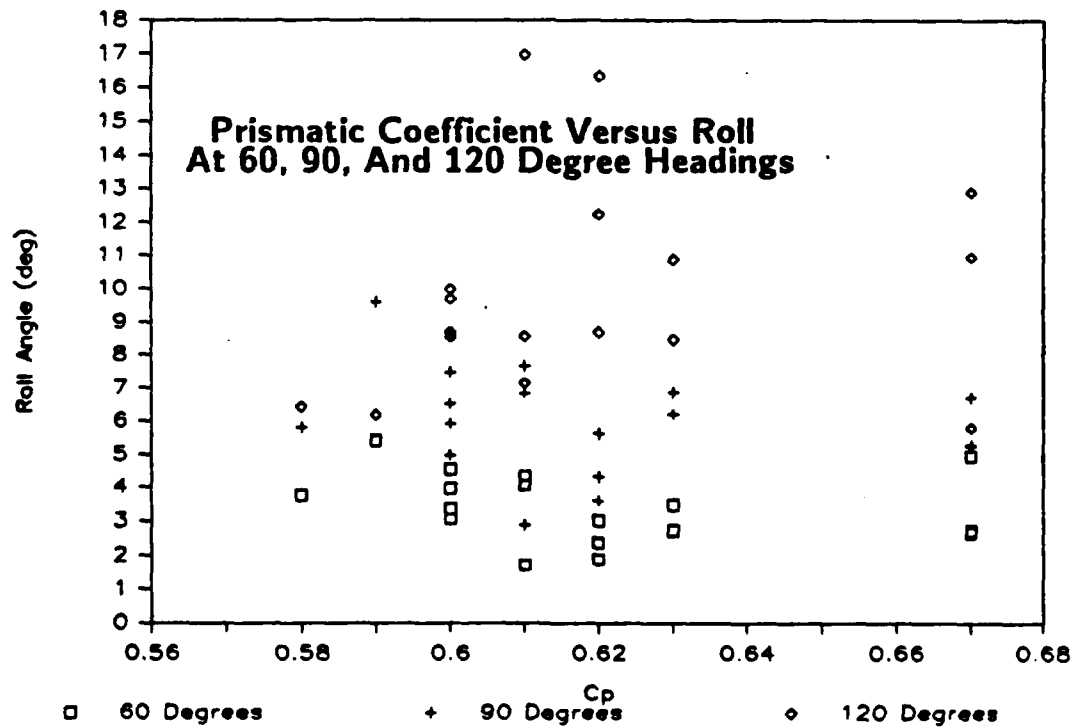


Figure 4 - Prismatic Coefficient versus Roll at 60, 90, and 120 Degree Headings

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