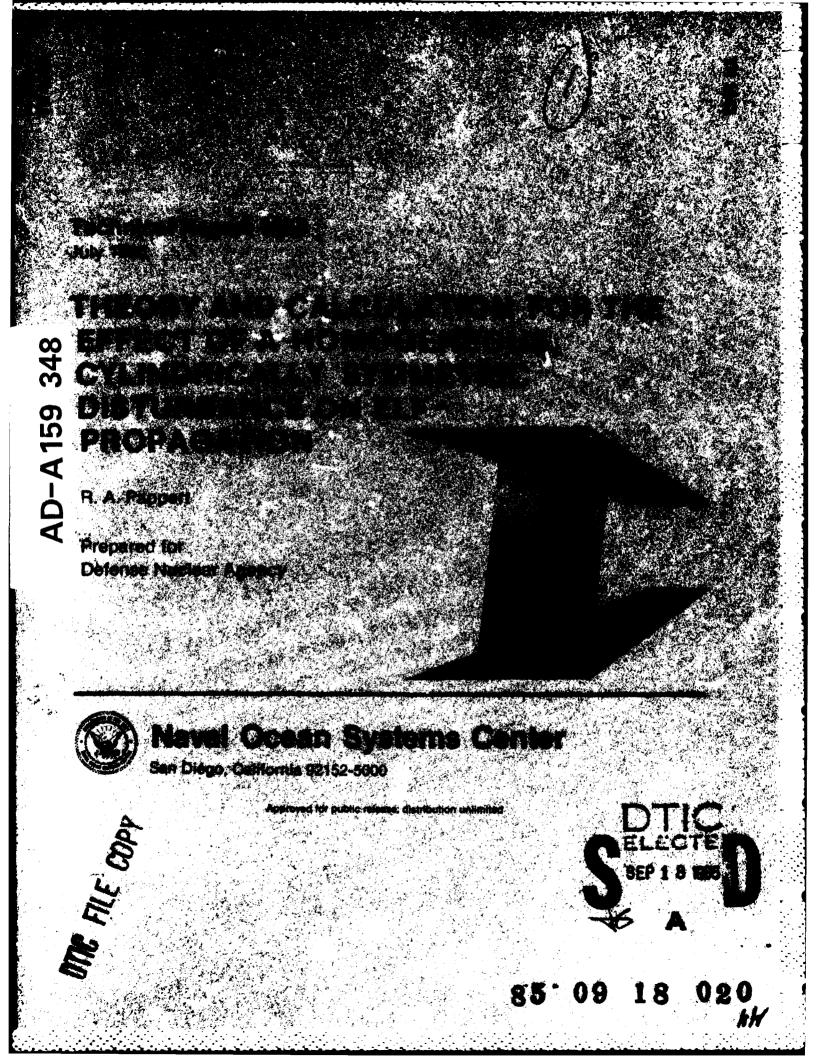


MICROCOPY RESOLUTION TEST CHART NATIONAL BUREAU OF STANDARDS - 1963 - A

1. The sec.





NAVAL OCEAN SYSTEMS CENTER SAN DIEGO, CA 92152

# F. M. PESTORIUS, CAPT, USN

R.M. HILLYER Technical Director

### ADMINISTRATIVE INFORMATION

This work, sponsored by the Defense Nuclear Agency, was performed during the period December 1984 through July 1985.

Released by J.A. Ferguson, Head Modeling Branch Under authority of J.H. Richter, Head Ocean and Atmospheric Sciences Division

#### ACKNOWLEDGEMENTS

The author wishes to express his gratitude to Ms. L.R. Hitney for valuable assistance with the computer program implementation of the formulas in Section II.

AS

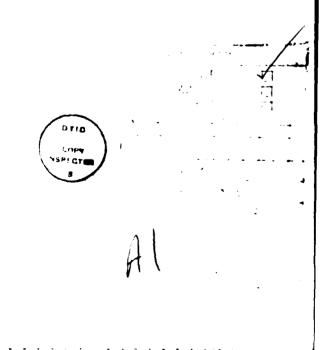
ţ

CURITY CLASSIFICATION OF THIS PAGE	A	DA 1	59348		<u> </u>	· · · · _ · ·	
	R	EPORT DOCU	MENTATION PA	GE			
18 REPORT SECURITY CLASSIFICATION UNCLASSIFIED			16 RESTRICTIVE MARKINGS				
SECURITY CLASSIFICATION AUTHORITY			3 DISTRIBUTION/AVAILABILITY OF REPORT				
DECLASSIFICATION/DOWNGRADING SCHED			Approved for publi	c release; distributio	on unlimited.		
						- 14 - 14 - 14 - 14 - 14 - 14 - 14 - 14	
PERFORMING ORGANIZATION REPORT NUMB	IEN(S)		5 MONITORING ORGANIZA	TION REPORT NUMBER(S)			
OSC TR 1043		60 OFFICE SYMBOL	78 NAME OF MONITORING	ORCANIZATION			
		(if applicable)		ONGANZATION		SEP 1 8 10	
aval Ocean Systems Center		l	7b ADDRESS (City, State an	d ZIP Codei	None V		
ADDRESS (CH), SHEEP NO LA COMP					C		
an Diego, CA 92152-5000					```	v A	
NAME OF FUNDING SPONSORING ORGANIZ	ATION	8b OFFICE SYMBOL (if applicable)	9 PROCUREMENT INSTRUM	MENT IDENTIFICATION NUM	BER		
efense Nuclear Agency							
ADDRESS (City, State and ZIP Code)		<b>.</b>	10 SOURCE OF FUNDING N PROGRAM ELEMENT NO	PROJECT NO	TASK NO Agency A ccession		
			Phogham Element no	PROJECT NO		Accession	
ashington, DC 20350			62715H	99QMXBB		DN651 524	
3. TYPE OF REPORT 136 TIME COVERED Research FROM Dec 84 to Jul 85				14 DATE OF REPORT (Year Month, Day) July 1985 62			
SUPPLEMENTARY NOTATION							
COSATI CODES		18 SUBJECT TERMS (Cont	inue on reverse if necessary and ide	ntify by block number)			
FIELD GROUP SUB-GROUP		ELF VLF	lonospheric propagation Propagation modeling				
		Earth ion	nosphere waveguide				
ABSTRACT (Continue on reverse if necessary							
A simple surface propage equency (ELF) propagation. Th de component of a horizontal di in contain a substantial mixture of lows for broadside excitation as omogeneous, cylindrically symm atching equations at the bounda tantamount to simply matching rpe environment indicate substar	ough often ade pole. That exc of TE compone well as a syster etric disturban- ry of the distur the ground ver	quate, one shortcomi itation can be quite si ent. In this study a be natic allowance for he ce centered over the t bance are developed tical electric and azim	gnificant in a sporadic-E ginning is made on ELF- ight gain effects. The de ransmitter. The method by evaluating height gain juthal magnetic fields at	lure to allow for ex- environment, when propagation model evelopment is for a utilizes normal-mo- integrals, and it is s- the boundary. Res	citation by th i the modal po- development flat earth with de decomposi- shown that th	e broad- blarization which r a laterally tion. is method	
			21 ABSTRACT SECURITY	CLASSIFICATION			
DISTRIBUTION AVAILABILITY OF ABSTRACT				ED			

# CONTENTS

I	Introduction	ן
II	Model and Theory	3
111	Results	16
IV	Summary	23
۷	References	25
	Figures	29

i



Page

# I. INTRODUCTION

Since an ELF signal from a remote transmitter is received over a range of azimuth angles, lateral ionospheric gradients produced by sporadic-E layering or nuclear depressions can produce significant effects on propagation in the lower ELF band. This is because the Fresnel zone size can be comparable to the transverse dimensions over which the disturbed ionosphere changes Although a number of workers have addressed the question of significantly. propagation in waveguide environments which vary both along and transverse to the path of propagation [Wait, 1964; Greifinger and Greifinger, 1977; Field and Joiner, 1979, 1982; Pappert, 1980, 1985; Ferguson, Hitney and Pappert, 1982; Shellman, 1983], no formulation exists which can fully account for the propagation effects produced by a localized disturbance with simultaneous allowance for vertical inhomogeneity, and anisotropy in a spherical geometry. Thus, it has been common practice to estimate the effects produced by localized ionospheric disturbances by using a simple surface propagation model introduced by Wait and more fully developed by the Greifingers and Field. The theory is predicated on the assumption that the field can be separated into lateral and height-dependent factors, and the model has been used to estimate the behavior of the lateral factor. Excitation factor and height gain effects are generally ignored. When applying the method to nocturnal environments, additional assumptions are made. Among these is the omission of the TE component of the modal polarization. This omission is well justified in the ambient case. However, it is known that under sporadic-E layering, considerable mixing between TE and TM waves can occur. When the surface propagation model is applied to nocturnal sporadic-E environments, this TE component is neglected.

In this study a start is made on ELF propagation model development which allows for the inclusion of excitation-factor and height gain effects along with allowance for the TE component. The development is for a flat earth with a homogeneous, cylindrically symmetric disturbance centered over the transmitter (see Figure 1). The method can be extended to more complicated geometries by methods discussed by the Greifingers and recently implemented by Pappert [1985] for surface model calculations. The development utilizes normal-mode decomposition (only the single non-evanescent mode which propagates at ELF has been used for the calculations), and the normal mode parameters are taken to be independent of the direction or azimuth of propagation. A method akin to mode conversion has been used to develop the matching equations at the boundary,  $r_0$ , of the disturbance. This method is shown to be tantamount to simply matching the ground vertical electric and azimuthal magnetic fields at  $r_0$ . Results indicate substantial departures from the surface propagation model and WKB predictions.

Essential theoretical background is given in Section II. Azimuthal dependence as well as other features of the modes are discussed in Section III along with the final field results. Conclusions and recommendations are summarized in Section IV.

# II. MODEL AND THEORY

The problem is illustrated in Figure 1, where a horizontal electric dipole (current moment Idl) is shown within the earth-ionosphere waveguide and beneath the center of a large cylindrically symmetric patch of sporadic-E. The vertical composition of the nighttime ambient electron and ion profiles with and without the sporadic-E layer is shown in Figure 2. The ground is taken to be homogeneous, with conductivity  $\sigma_g$  and permittivity  $\varepsilon_g$ . A crucial assumption, discussed more fully in Section III, is that the propagation is independent of its azimuth. The electric, É, and magnetic, Å, fields excited by the horizontal dipole can be derived from two scalar potentials V and W [Wait, 1963], where V is identified with quasi TM excitation and W with quasi TE excitation. Total field components within the guide are given by [Webber and Peden, 1971].

$$H_{z} = \left(\frac{\partial^{2}}{\partial z^{2}} + k^{2}\right)W , \quad E_{z} = \left(\frac{\partial^{2}}{\partial z^{2}} + k^{2}\right)V \quad (1-a)$$

$$H_{\phi} = -j\omega\varepsilon_{0} \frac{\partial V}{\partial r} + \frac{1}{r} \frac{\partial^{2} W}{\partial z \partial \phi} , \quad E_{\phi} = j\omega\mu_{0} \frac{\partial W}{\partial r} + \frac{1}{r} \frac{\partial^{2} V}{\partial r \partial \phi}$$
(1-b)

$$H_{r} = \frac{\partial^{2} W}{\partial z \partial r} + \frac{j \omega \varepsilon_{o}}{r} \frac{\partial V}{\partial \phi}, \quad E_{r} = \frac{\partial^{2} V}{\partial z \partial r} - \frac{j \omega \mu_{o}}{r} \frac{\partial W}{\partial \phi}$$
(1-c)

where  $\omega$ ,  $\mu_0$ ,  $\varepsilon_0$  and k are angular frequency, free space permeability, free space permittivity and free space wavenumber, respectively. A time dependence  $\exp(j\omega t)$  is assumed and  $j = \sqrt{-1}$ .

Free space field components,  $E_z^p$ , and,  $H_z^p$ , generated by the horizontal electric dipole are:

$$E_{z}^{p} = \pm \frac{Mk^{3}}{2} \cos\phi \int_{\Gamma} S^{2}CH_{1}^{(2)}(kSr)exp(-jkC|z-z_{0}|)d\theta \qquad (2)$$

$$\pi H_z^p = \frac{Mk^3}{2} \sin\phi \int_{\Gamma} S^2 H_1^{(2)}(kSr) \exp(-jkC|z-z_0|) d\theta$$
(3)

where

$$M = Idl/(4\pi j\omega\epsilon_0) , S = sin\Theta , C = cos\Theta , \eta = \sqrt{\frac{\mu_0}{\epsilon_0}}$$
(4)

Gamma,  $\Gamma$ , is the contour with lower endpoint  $-\pi/2 - j\infty$  and upper endpoint  $\pi/2 + j\infty$ .  $H_1^{(2)}$  is the Hankel function of order 1 of the second kind. The plus sign in Eq. (2) applies when  $z > z_0$  and the minus sign when  $z < z_0$ , where  $z_0$  is the transmitter height (see Figure 1).

To the primary field components represented by Eqs. (2) and (3) must be added the field components associated with the boundary reflections or, equivalently, the image fields. Let R be the plane wave reflection matrix, referenced to ground level, associated with reflections from structure above  $z_0$  and  $\bar{R}$  the corresponding reflection matrix associated with reflections from structure below  $z_0$ . In terms of the elements defined by Budden [1961], the reflection matrices associated with the z field components are:

$$\mathbf{R} = \begin{pmatrix} \mathbf{I}^{\mathbf{R}} & \mathbf{I} & -\mathbf{I}^{\mathbf{R}} \\ -\mathbf{I}^{\mathbf{R}} & \mathbf{I}^{\mathbf{R}} \\ \mathbf{I}^{\mathbf{R}} & \mathbf{I}^{\mathbf{R}} \end{pmatrix}, \quad \mathbf{\tilde{R}} = \begin{pmatrix} \mathbf{I}^{\mathbf{R}} & \mathbf{0} \\ \mathbf{0} & \mathbf{I}^{\mathbf{\tilde{R}}} \\ \mathbf{I}^{\mathbf{R}} \end{pmatrix}$$
(5)

The notation I denotes vertical polarization, and the notation  $\perp$  denotes horizontal polarization. The first subscript refers to the polarization of the electric field of the upgoing wave while the second subscript refers to the corresponding polarization of the downcoming wave. Following Pappert [1968], the total z field components within the guide may be written as

$$\begin{cases} E_{TH_{z}} \\ H_{z} \end{cases} = \frac{Mk^{3}}{2} \left[ \cos \phi \int S^{2}CH_{1}^{(2)}(kSr) \left( e^{-jkCz} + Re^{jkCz} \right) F\left( e^{jkCz} - \bar{R}e^{-jkCz} o \right) \left( \frac{1}{0} \right) d\theta \right]$$

$$+ \sin \phi \int S^{2}H_{1}^{(2)}(kSr) \left( e^{-jkCz} + Re^{jkCz} \right) F\left( e^{jkCz} o + \bar{R}e^{-jkCz} o \right) \left( \frac{0}{1} \right) d\theta$$

$$(6)$$

where

$$F = (1 - R\bar{R})^{-1}$$
<sup>(7)</sup>

By carrying out the matrix operations indicated in Eqs. (6) and (7) and evaluating the integral by means of residue theory [Budden, 1962] one obtains

$$E_{z} = \pi j M k^{3} cos \phi \sum_{m} \left[ \frac{S^{2} CH_{1}^{(2)} (kSr) (1 - \Gamma_{L} R_{\perp} \overline{R}_{\perp}) (e^{jkCz} + \pi_{R} e^{-jkCz}) (e^{jkCz} o - \pi_{R} e^{-jkCz} o)}{\pi^{R}} \right]_{m} de^{-jkCz} de^{jkCz} de^{jkC$$

Here m is a mode index (only one non-evanescent mode exists in the ELF band) and the modal function is

$$\Delta = (1 - R_{\parallel}, \bar{R}_{\parallel})(1 - R_{\perp}, \bar{R}_{\perp}) - \bar{R}_{\perp}, \bar{R}_{\parallel}, R_{\parallel}, R_{\perp}$$
(10)

The modal equation  $\Delta = 0$  has also been used in arriving at Eqs. (8) and (9).

From Eqs. (1-a) the total potentials V and W within the guide are

$$V = \pi j M k \sum_{m} \left\{ \frac{H_{1}^{(2)}(kSr)(e^{jkCz} + R_{m}\bar{R}_{m} e^{-jkCz})}{\partial \Delta / \partial \Theta} \left[ \frac{(1 - R_{\perp} \bar{R}_{\perp})C(e^{jkCz} - R_{m}\bar{R}_{m} e^{-jkCz})}{R_{m}\bar{R}_{m}} \cos \phi - R_{m}R_{m}(e^{jkCz} + R_{\perp}\bar{R}_{\perp} e^{-jkCz} + R_{\perp}\bar{R}_{\perp} e^{-jkCz} - R_{m}\bar{R}_{\perp} e^{-jkCz} - R_{$$

$$\pi \mathbf{W} = -\pi \mathbf{j} \mathbf{M} \mathbf{k} \sum_{\mathbf{M}} \left\{ \frac{\mathbf{H}_{1}^{(2)}(\mathbf{k} \mathbf{S} \mathbf{r}) \left( e^{\mathbf{j} \mathbf{k} \mathbf{C} \mathbf{z}} + \mathbf{1} \overline{\mathbf{R}}_{\perp} e^{-\mathbf{j} \mathbf{k} \mathbf{C} \mathbf{z}} \right)}{\partial \Delta / \partial \Theta} \left[ \mathbf{R}_{\perp} \mathbf{C} \left( e^{-\mathbf{j} \mathbf{k} \mathbf{C} \mathbf{z}} \mathbf{o} - \mathbf{R}_{\parallel} \mathbf{R}_{\parallel} e^{-\mathbf{j} \mathbf{k} \mathbf{C} \mathbf{z}} \mathbf{o} \right) \cos \phi - \frac{(1 - \mathbf{R}_{\parallel} \mathbf{R}_{\parallel}) \left( e^{\mathbf{j} \mathbf{k} \mathbf{C} \mathbf{z}} \mathbf{o} + \mathbf{1} \overline{\mathbf{R}}_{\perp} e^{-\mathbf{j} \mathbf{k} \mathbf{C} \mathbf{z}} \mathbf{o} \right)}{\mathbf{1} \overline{\mathbf{R}}_{\perp}} \sin \phi \right] \right\} \mathbf{m}$$

$$(12)$$

Equations (11) and (12) may be conveniently written as

$$V = -\pi jMk \sum_{m} \{\lambda H_{1}^{(2)}(kSr)h_{y}(z) [e_{x}(z_{0})\cos\phi + \alpha e_{y}(z_{0})\sin\phi]\}_{m}$$
(13)

$$\pi M = \pi j M k \sum_{m} \{\lambda H_{1}^{(2)}(kSr) e_{y}(z) [e_{x}(z_{0}) \cos \phi + \alpha e_{y}(z_{0}) \sin \phi]\}_{m}$$
(14)

where

$$\lambda = \frac{\left(1 - \frac{1}{1}R_{\perp} - \frac{1}{1}R_{\perp}\right)\left(1 + \frac{1}{1}R_{\parallel}\right)^{2}}{\frac{1}{1}R_{\parallel} - \left(\frac{\partial\Delta}{\partial\Theta}\right)}, \quad \alpha = \frac{1}{1}\frac{R_{\parallel}}{\frac{1}{1}R_{\perp}}$$
(15)

and the modal height gains  $\mathbf{h}_{\mathbf{y}}$  and  $\mathbf{e}_{\mathbf{y}}$  are defined by

$$h_{y}(z) = \frac{e^{jkCz_{+}}\bar{R}_{\parallel} e^{-jkCz}}{1 + \bar{R}_{\parallel}}, \quad e_{y}(z) = f \frac{e^{jkCz_{+}}\bar{R}_{\perp}e^{-jkCz}}{1 + \bar{R}_{\perp}}$$
(16)

All other height gains are given by Maxwell's equations subject to y invariance and an exp(-jkSx) dependence. The other height gains are (note that h is defined as n times the magnetic intensity).

$$e_{x} = -\frac{1}{jk} \frac{\partial h_{y}}{\partial z} = -C \frac{e^{jkCz} - \|\overline{R}\|}{1 + \|\overline{R}\|} e^{-jkCz}, \quad h_{x} = \frac{1}{jk} \frac{\partial e_{y}}{\partial z} = fC \frac{e^{jkCz} - [\overline{R}] e^{-jkCz}}{1 + [\overline{R}]}$$
(17)  
$$e_{z} = \frac{h_{y}}{(jkexp(-jkSx))} \frac{\partial}{\partial x} [exp(-jkSx)] = -Sh_{y}, \quad h_{z} = -\frac{e_{y}}{(jkexp(-jkSx))} \frac{\partial}{\partial x} [exp(-jkSx)] = Se_{y}$$
(18)

Because of the assumed propagation isotropy in azimuth, the height gains are independent of the azimuth angle  $\phi$ . In Eqs. (16) and (17), f is the modal polarization ratio given by

$$f = \frac{e_{y}(z=0)}{h_{y}(z=0)} = \frac{(1+\bar{R}_{\perp})(1-\bar{R}_{\parallel},\bar{R}_{\parallel})}{(1+\bar{R}_{\parallel})\bar{L}R_{\parallel},\bar{R}_{\perp}} = \frac{(1+\bar{R}_{\perp})}{(1+\bar{R}_{\parallel})} \frac{\bar{R}_{\perp},\bar{R}_{\parallel}}{1-\bar{L}R_{\perp},\bar{R}_{\perp}}$$
(19)

Thus far the discussion has been restricted to the region within the guide. The modal height gains, however, have meaning both within and wihout the guide (e.g., within the ionosphere) and are calculable by means of numerical integration of Maxwell's equations [Pitteway, 1965; Smith, 1970]. Therefore, with the understanding that  $h_y$ ,  $e_y$ , etc., represent these general height gain functions, the field components deduced from V and W by means of Eqs. (1) can be continued into the ionosphere.

In anticipation of solving the problem posed in Fig. 1 by satisfying continuity requirements at the boundary  $r=r_0$ , the superscript p will be used to denote values in the perturbed region, and the superscript u will be used to denote values in the unperturbed region. To the primary fields in the perturbed region must be added the secondary fields. The crucial assumption is now made that these secondary fields generated by the discontinuity at  $r = r_0$  may be described in terms of a normal-mode expansion so that the secondary potentials take the form

$$V_{s} = \sum_{m} \{ J_{1}(kS^{p}r)h_{y}^{p}(z)(x_{1}\cos\phi + x_{2}\sin\phi) \}_{m}$$
(20)

$$m_{s}^{\mu} = -\sum_{m} \{J_{1}(kS^{p}r)e_{y}^{p}(z) (x_{1}\cos\phi + x_{2}\sin\phi)\}_{m}$$
(21)

where  $J_1$  is the Bessel function of the first kind of order one and guarantees that the secondary fields are finite at the origin. It is likewise assumed that the potentials in the unperturbed region can be written in terms of a normal-mode expansion so that

$$V_{e} = \sum_{m} \{H_{1}^{(2)}(kS^{u}r)h_{y}^{u}(z)(x_{3}\cos\phi + x_{4}\sin\phi)\}_{m}$$

$$mW_{e} = -\sum_{m} \{H_{1}^{(2)}(kS^{u}r)e_{y}^{u}(z)(x_{3}\cos\phi + x_{4}\sin\phi)\}_{m}$$
(22)
(23)

Matching the tangential components of the fields at  $r = r_0$  yields

$$j \pi Mk^{3} \sum_{m} \left\{ \lambda^{p} S^{p} [e_{x}^{p}(z_{0}) \cos \phi + \alpha^{p} e_{y}^{p}(z_{0}) \sin \phi] \left[ \begin{array}{c} jH_{1}^{(2)'}(kS^{p}r_{0})e_{y}^{p}(z) \\ H_{1}^{(2)'}(kS^{p}r_{0})e_{z}^{p}(z) \\ jH_{1}^{(2)'}(kS^{p}r_{0})h_{y}^{p}(z) \\ H_{1}^{(2)'}(kS^{p}r_{0})h_{z}^{p}(z) \end{array} \right. \right. \right.$$

$$+ j \lambda^{p} S^{p} \frac{H_{1}^{(2)}(kS^{p}r_{0})}{kS^{p}r_{0}} \left[ -e_{x}^{p}(z_{0}) \sin \phi + \alpha^{p} e_{y}^{p}(z_{0}) \cos \phi \right] \left[ \begin{array}{c} e_{x}^{p}(z) \\ h_{x}^{p}(z) \\ 0 \\ h_{x}^{p}(z) \\ 0 \end{array} \right] \right\}$$

$$- k^{2} \sum_{m} \left\{ S^{p}(x_{1} \cos \phi + x_{2} \sin \phi) \left[ \begin{array}{c} jJ_{1}^{'}(kS^{p}r_{0})e_{y}^{p}(z) \\ J_{1}(kS^{p}r_{0})h_{y}^{p}(z) \\ J_{1}(kS^{p}r_{0})h_{y}^{p}(z) \\ J_{1}(kS^{p}r_{0})h_{z}^{p}(z) \end{array} \right] \right\}$$

#### IV SUMMARY

In this report, a development to allow for the inclusion of excitation factor and height gain effects on ELF propagation in a laterally inhomogeneous guide has been started. The development is for a flat earth geometry and the simple environment of Figure 1. Several crucial assumptions have been made. First, it has been assumed that the perturbing environment is homogeneous as well as cylindrically symmetric. Second, it has been assumed that the primary fields, as well as secondary fields generated by the boundary at  $r = r_0$ , are described by normal modes, and only the consequences of the single nonevanescent mode have been investigated. Third, the normal-mode parameters have been taken to be independent of the direction or azimuth of propagation.

A method akin to mode conversion, termed in this study the SMA (for Single Mode Analysis) method, has been used for establishing the boundary equations at  $r = r_0$ . As in mode conversion analysis, the SMA method involves numerical integration of height gain functions. It has been shown that the SMA method is tantamount to matching H<sub> $\phi$ </sub> and E<sub>z</sub> at  $r = r_0$  at the ground. This is a significant result because it implies the reasonableness of a generalized surface propagation model which allows in a systematic way for excitation factor and height gain effects as well as broadside excitation.

It has been found that excitation factor and height gain effects can be quite significant for sporadic-E environments conforming to the geometry of Figure 1. In particular, broadside excitation, because of the sizable TE contamination of the modal polarization, can be very substantial. TE contamination would also be expected to play a role were the disturbance to fall over the receiver rather than over the transmitter.

23

PREVIOUS PAGE

IS BLANK

the dominating terms of Eqs. (29) through (32) involve integrals of products of  $e_z$  and  $h_y$  terms. These terms are nearly constant and of order unity below about 73 km (see Figures 29 and 30), where most of the contribution to the integrals comes from. The integrals involving the products of TE components would generally be much smaller, as Figures 29 and 30 show. At any rate, it is a fact that simply matching the  $H_{\phi}$  and  $E_z$  components at  $r = r_0$  at the ground is for all practical purposes equivalent to the height gain integration method (the SMA method) used in Section TI to develop the results. This is made clear in Figures 31 through 34, which show a worst-case comparison between SMA results and "Field Matching" results (i.e., results obtained by demanding continuity of  $H_{\phi}$  and  $E_z$  at the ground at  $r = r_0$ ). The differences are indeed very slight. This is a significant result because it implies the reasonableness of a generalized surface propagation model which allows in a systematic way for excitation factor and height gain effects as well as broadside excitation.

A disquieting though not surprising feature of the analysis is that the TE components are not continuous at  $r = r_0$ . This would be expected for the  $E_{\phi}$  and  $H_z$  components since, as Figures 29 and 30 show,  $e_y$  and  $h_z$  vary substantially across the guide. However, the  $h_x$  component is quite substantial and reasonably stable across the guide. But as Figure 35 (a representative example) shows, the  $H_r$  component experiences a large discontinuity at  $r = r_0$  at the ground. This is not surprising because, as we have just seen, the SMA method is equivalent to matching only the  $H_{\phi}$  and  $E_z$  components at  $r = r_0$  at the ground. It is not clear what the resolution to this dilemma is. Perhaps inclusion of evanescent modes would improve the agreement for continuity of  $H_r$  without destroying the  $H_{\phi}$  and  $E_z$  continuity. However, no efforts along those lines have been attempted in the current study.

close to broadside, excitation variation for the unperturbed guide is close to the surface model result; however, the perturbed guide's normalized source height gain variation shows marked departure from the surface model result. This is because of the large TE admixture to the modal polarization in the perturbed region. Whereas for the unperturbed guide  $|e_{X}^{U}(o)| >> |e_{Y}^{U}(o)|$ , the situation for the perturbed guide is that  $|e_{Y}^{p}(o)|$  is somewhat greater than  $|e_{X}^{p}(o)|$ , and that results in the interference null in Figure 16 occurring at  $\approx 36^{\circ}$  and for the region  $\phi < 0$  being essentially a region of constructive interference.

المستقد الاستعادي المراجب المراجب والمنافسة فالمستخدم المراجب والمراجب والمراجب المراجب المراجب المراجب المراج المستقد المستقد المستقد المراجب والمنافس المراجب والمنافس من المراجب والمراجب والمراجب المراجب المراجب والمراجب

Figures 17 and 18 show results for the amplitude radios  $|H_{\phi}/H_{\phi}^{u}|$  and  $|E_{z}/E_{z}^{u}|$  at the ground for crossed dipole sources which are out of phase by 90°. Shown are SMA, WKB and surface propagation model results. Again the SMA results are very nearly continuous at  $r = r_{0}$  while the WKB results manifest sizable discontinuities there. Exterior to the disturbance, the SMA and surface propagation model results are in reasonable agreement. Interior to the disturbance, the SMA results for  $H_{\phi}$  differ significantly from the surface propagation model results while the interior results for  $E_{z}$  for the two models are in reasonable agreement.

Figures 19 through 28 show SMA and WKB phase results for  $H_{\phi}$  and  $E_z$  for the cases for which amplitude results have been given previously. The significant features are the near continuity of the phase of  $H_{\phi}$  and  $E_z$  at  $r = r_0$ for the SMA method and the large discontinuity exhibited there by the WKB results. The near continuity of the amplitudes and phases at  $r = r_0$  means that the height gain integration method used in Section II to develop the results is tantamount to simply matching  $H_{\phi}$  and  $E_z$  components at  $r = r_0$  at the ground. The latter method involves no height gain integrations such as used in the method of Section II. It is suspected that the reason for this is that

iii) SMA results show significant departures from both the surface propagation model and the WKB results.

iv) At short ranges the SMA and WKB results generally show good agreement.

v) In contrast to the surface propagation model results, the SMA results show a marked angular (i.e.,  $\phi$ ) dependence.

Result (i) above is due in large measure to the large discrepancy between the perturbed ( $\theta^p$  = 57.16° - 65.03°j) and unperturbed ( $\theta^u$  = 84.48° - 34.12°j) eigenangles as well as the difference between the perturbed  $[e_v^p(o) = (5.78)$ 6.77j)x10<sup>-4</sup>] and unperturbed  $[e_y^u(o) = (5.25-2.21j)x10^{-5}]$  field components and the difference between the excitation factors (  $\lambda^p$  = 2.32 - 4.99j and  $\lambda^u$  = -  $4.32 \times 10^{-2}$  - 7.42j). In connection with (ii) above, it is pointed out that continuity of the field components  ${\rm H}_{\rm d}$  and  ${\rm E}_{\rm Z}$  is not obviously forced by the matching method of Section II. Departures mentioned in (iii) point out clearly the significance of height gain and excitation factor effects ignored in the surface propagation model. Observation (iv) is explained by the fact that the secondary fields [which depend upon  $J_1(kS^{Pr})$  and  $J_1(kS^{Pr})$ ] for are small compared with the primary fields which depend |kSPr|<<1 upon  $H_1^{(2)}(kS^{p}r)$  and  $H_1^{(2)'}(kS^{p}r)$ . Figure 16 illustrates the source of the angular dependence mentioned in (v). Shown is the normalized source height gain  $(e_x(o)\cos\phi + e_y(o)\sin\phi)/e_x(o)$  in dB for both the perturbed "p" and unperturbed "u" quantities versus azimuth. Shown also is the  $20\log_{10} |\cos\phi|$ variation predicted by the surface propagation model (which assumes only excitation from the end-on component of the source dipole). Except for angles

vertical component of the geomagnetic field for high latitudes. Azimuthal invariance is strictly valid for a dip angle of 90°.

All remaining figures in this study are for 75 Hz, and for a vertical geomagnetic field (i.e., dip of 90°) of strength .41 x sin(77°) gauss. The ground conductivity has been taken to be  $10^{-2}$  siemens/m and the dielectric constant 15. The lower conductivity of about 2.8 x  $10^{-4}$  siemens/m at the transmitter be included simply multiplying the height can by gains  $e_x^p(p)$  and  $e_v^p(o)$  by  $\sqrt{10^{-2}/2.8 \times 10^{-4}} = 5.98$  (or 15.5 dB). However, the factor is of no consequence in the present study, where either amplitude ratios or phase differences are plotted. Finally, the radius of the disturbance has been taken to be 500 km.

Figures 8 through 15 show results for the amplitude ratios  $|H_{\phi}/H_{\phi}^{u}|$  and  $|E_{z}/E_{z}^{u}|$  at the ground for an electric dipole source at the ground oriented in the x direction (see Figure 1). Figures 8 and 9 are for broadside launch (i.e.,  $\phi = \pm 90^{\circ}$ ), Figures 10 and 11 are for  $\phi = 45^{\circ}$ , Figures 12 and 13 are for end-on launch (i.e.,  $\phi = 0^{\circ}$ ), and Figures 14 and 15 are for  $\phi = -45^{\circ}$ . Results of the present study are labeled SMA for Single Mode Analysis. Shown also on Figures 10 through 15 are WKB results and results of the surface propagation model, which neglects excitation factor and height gain effects (Pappert, 1985). The surface propagation results are  $\phi$  independent. There are several observations that can be made from these figures.

i) WKB results generally show a sizable discontinuity at  $r = r_0$ .

ii) SMA results are very nearly continuous at r = r though range derivatives are discontinuous.

ELF propagation in the ambient guide can be taken to be independent of azimuth.

Figure 5 shows that the azimuthal deviation from the average attenuation rate for the disturbed profile (i.e., ambient plus sporadic-E) is less than 10%. The large difference between the mean attenuation rates for the two dips shown on Figure 5 results from the critical role which the vertical component of the geomagnetic field plays in determining the attenuation rate. This is discussed in the work of Pappert and Moler [1978]. Possible contributions of this effect to azimuthal variations as well as azimuthal dependence due to possible lateral inhomogneity of the layer are ignored in this study. Finally, Figure 6 shows that the azimuthal deviation from the average normalized phase velocity for the disturbed profile is also less than 10%. Thus, though the evidence for assuming azimuthally independent propagation in this instance is not as formidable as in the case of the ambient profile, the azimuthal variations for constant dip angle are still sufficiently small to make reasonable, at least as a first approximation, the assumption of azimuthal invariance. The assumption is, of course, most reasonable when applied to effects caused by natural or artificial ionospheric depressions and has served as the basis for the theoretical development of Section II.

Figure 7 shows attenuation rate as a function of frequency for the ambient nighttime profile and the ambient plus sporadic-E profile. Two curves for the disturbed environment are shown. The solid curve is for a dip angle of 77°, a geomagnetic field strength of 0.41 gauss, a ground conductivity of  $10^{-2}$  siemens/m and dielectric constant of 15. The dashed curve is for a dip of 90° and a geomagnetic field strength of 0.41 x sin(77°) gauss (i.e., the radial component of the geomagnetic field used for the solid curve). The near coincidence of the two curves demonstrates the controlling feature of the

# III. RESULTS

In a previous study [Pappert and Moler, 1978] full-wave outputs for an ambient nighttime profile disturbed by a sporadic-E layer (see Figure 2) have been analyzed with respect to ionospheric absorption and reflection features at lower ELF. In that work it was shown that an order-of-magnitude enhancement in the attenuation rate due to the sporadic-E layering was a distinct possibility (see also Figures 3, 5 and 7 herein). In this section, features of the propagation associated with the simple sporadic-E environment of Figures 1 and 2 will be explored by implementation of theory developed in Section II.

Figures 3 through 6 show the behavior of the attenuation rate and phase velocity (normalized to the free space speed of light) at 75 Hz as a function of azimuth of propagation relative to magnetic north for dip angles of 60° and 75°. A conductivity of  $\sigma = 10^{-2}$  siemens/m, dielectric constant of 15, and geomagnetic field strength of 0.41 gauss have been used for the calculations. Figure 3 indicates mid and northerly latitude ambient attenuation rates of slightly greater than 0.8 dB/Mm. This is somewhat lower than the WTF measurements, which estimate a nighttime mid-latitude value of 1.0 dB/Mm. This comparison could be indicative of a deficiency in the ionospheric model, although other models also generally yield lower attenuation rates than those suggested by WTF measurements. Most measurements of ELF nocturnal fades have been made for paths for which the dip angle is 5°60°. The curves of Figure 3 indicate an azimuthal variation in attenuation rate of less than 0.03 dB/Mm. Similarly, Figure 4 shows the difference in the normalized phase velocity for the east to west and west to east directions is less than 1%. Thus, for paths of concern in this study,

$$+ \lambda_{m}^{P} S_{m}^{p} \frac{H_{1}^{(2)}(kS_{m}^{p}r)}{kS_{m}^{p}r} H_{1}^{(2)'}(kS_{m}^{p}r)h_{ym}^{p}(z) [e_{xm}^{p}(z_{0})\cos\phi + \alpha_{m}^{p}e_{ym}^{p}(z_{0})\sin\phi] + \lambda_{m}^{P} S_{m}^{p} \frac{H_{1}^{(2)}(kS_{m}^{p}r)}{kS_{m}^{p}r} h_{xm}^{p}(z) [-e_{xm}^{p}(z_{0})\sin\phi + \alpha_{m}^{p}e_{ym}^{p}(z_{0})\cos\phi] , r < r_{0} = -\pi M k^{3} \sum_{m} \left\{ \sqrt{\lambda_{m}^{p}\lambda_{m}^{u}} \bar{S}_{m} H_{1}^{(2)'}(k\bar{S}_{m}r)h_{ym}^{u}(z) [e_{xm}^{p}(z_{0})\cos\phi + \alpha_{m}^{p}e_{ym}^{p}(z_{0})\sin\phi] + \sqrt{\lambda_{m}^{p}\lambda_{m}^{u}} \bar{S}_{m} \frac{H_{1}^{(2)}(k\bar{S}_{m}r)}{k\bar{S}_{m}r} h_{xm}^{u}(z) [-e_{xm}^{p}(z_{0})\sin\phi + \alpha_{m}^{p}e_{ym}^{p}(z_{0})\cos\phi] \right\} , r > r_{0}$$

$$\pi H_{r}^{W} = -\pi M k_{m}^{3} \sum_{m} \left\{ \lambda_{m}^{p} S_{m}^{p} H_{1}^{(2)'}(kS_{m}^{p}r)h_{xm}^{p}(z) \left[ e_{x}^{p}(z_{0})\cos\phi + \alpha_{m}^{p} e_{ym}^{p}(z_{0})\sin\phi \right] \right\} - \lambda_{m}^{p} S_{m}^{p} \frac{H_{1}^{(2)}(kS_{m}^{p}r)}{kS_{m}^{p}r} h_{ym}^{p}(z) \left[ -e_{xm}^{p}(z_{0})\cos\phi + \alpha_{m}^{p} e_{ym}^{p}(z_{0})\sin\phi \right] \right\} , r < r_{o}$$

$$= -\pi M k_{m}^{3} \sum_{m} \left\{ \sqrt{\lambda_{m}^{p} \lambda_{m}^{u}} \tilde{S}_{m} H_{1}^{(2)'}(k\bar{S}_{m}r)h_{xm}^{u}(z) \left[ e_{xm}^{p}(z_{0})\cos\phi + \alpha_{m}^{p} e_{ym}^{p}(z_{0})\sin\phi \right] \right\} , r > r_{o}$$

$$= -\sqrt{\lambda_{m}^{p} \lambda_{m}^{u}} \tilde{S}_{m} \frac{H_{1}^{(2)}(k\bar{S}_{m}r)}{k\bar{S}_{m}r} h_{ym}^{u}(z) \left[ -e_{xm}^{p}(z_{0})\cos\phi + \alpha_{m}^{p} e_{ym}^{p}(z_{0})\sin\phi \right] \right\} , r > r_{o}$$

$$(41)$$

where

1

$$\bar{S}_{m} = \frac{S_{m}^{p}r_{o} + S_{m}^{u}(r-r_{o})}{r}$$
,  $r>r_{o}$  (42)

Results based on Eqs. (33) through (41) are given in the following section.

$$E_{z}^{u} = j \pi M k_{m}^{3} \sum_{m} \lambda_{m}^{u} S_{m}^{u} H_{1}^{(2)} (k S_{m}^{u} r) e_{zm}^{u} (z) [e_{xm}^{u} (z_{o}) \cos \phi + \alpha_{m}^{u} e_{ym}^{u} (z_{o}) \sin \phi]$$
(36)

$$\pi H^{u}_{\phi} = -\pi M K^{3} \sum_{m} \left\{ \lambda^{u}_{m} S^{u}_{m} H^{(2)}_{1}(k S^{u}_{m} r) h^{u}_{ym}(z) \left[ e^{u}_{xm}(z_{o}) \cos \phi + \alpha^{u}_{m} e^{u}_{ym}(z_{o}) \sin \phi \right] \right\}$$

$$+\lambda_{m}^{u}S_{m}^{u}\frac{H_{1}^{(2)}(kS_{m}^{u}r)}{kS_{m}^{u}r}h_{\chi m}^{u}(z)\left[-e_{\chi m}^{u}(z_{o})\sin\phi + \alpha_{m}^{u}e_{\chi m}^{u}(z_{o})\cos\phi\right]\right\}$$
(37)

$$\pi H_r^u = -\pi M k_m^3 \sum_{m} \left\{ \lambda_m^u S_m^u H_1^{(2)'}(k S_m^u r) h_{Xm}^u(z) \left[ e_{Xm}^u(z_0) \cos \phi + \alpha_m^u e_{Ym}^u(z_0) \sin \phi \right] \right\}$$

$$-\lambda_{m}^{u}S_{m}^{u}\frac{H_{1}^{(2)}(kS_{m}^{u}r)}{kS_{m}^{u}r}h_{ym}^{u}(z)\left[-e_{xm}^{u}(z_{0})\sin\phi + \alpha_{m}^{u}e_{ym}^{u}(z_{0})\cos\phi\right]\right\}$$
(38)

As a matter of interest, comparisons will also be made in the following section with the so-called WKB result [Bickel et al., 1970] which involves the geometric mean of the excitation factor at the terminals of the path and the average of the propagation constant over the path. The WKB formulas for the field as implemented in the present study are as follows:

$$E_{z}^{W} = j\pi Mk_{m}^{3} \sum_{m} \lambda_{m}^{p} S_{m}^{p} H_{1}^{(2)}(kS_{m}^{p}r)e_{zm}^{p}(z) [e_{xm}^{p}(z_{o})\cos\phi + \alpha_{m}^{p}e_{ym}^{p}(z_{o})\sin\phi] , r < r_{o}$$

$$= j\pi Mk_{m}^{3} \sum_{m} \sqrt{\lambda_{m}^{p} \lambda_{m}^{u}} S_{m}^{u} H_{1}^{(2)}(k\overline{S}_{m}r)e_{zm}^{u}(z) [e_{xm}^{p}(z_{o})\cos\phi + \alpha_{m}^{p}e_{ym}^{p}(z_{o})\sin\phi] , r > r_{o}$$
(39)

$$\left. \begin{array}{l} \left. \left. H_{\varphi}^{p} = -\pi kk^{3} \sum_{m} \left[ \lambda_{m}^{p} \sum_{m}^{p} h_{zm}^{(2)} (kS_{m}^{p}r) h_{ym}^{p}(z) \left[ e_{xm}^{p}(z_{0}) \cos\phi + a_{m}^{p} e_{ym}^{p}(z_{0}) \sin\phi \right] \right] \right. \\ \left. \left. + \lambda_{m}^{p} S_{m}^{h_{z}^{(2)}} (kS_{m}^{p}r) h_{xm}^{p}(z) \left[ -e_{xm}^{p}(z_{0}) \sin\phi + a_{m}^{p} e_{ym}^{p}(z_{0}) \cos\phi \right] \right] \right. \\ \left. \left. - jk^{2} \sum_{m} \left[ S_{m}^{p} J_{1}^{1} (kS_{m}^{p}r) h_{ym}^{p}(z) \left[ x_{1m} \cos\phi + x_{2m} \sin\phi \right] \right] \right. \\ \left. \left. + S_{m}^{p} \frac{J_{1}^{1} (kS_{m}^{p}r)}{kS_{m}^{p}r} h_{xm}^{p}(z) \left[ -x_{1m} \sin\phi + x_{2m} \cos\phi \right] \right] \right. \\ \left. \left. r < r_{0} \right] \right. \\ \left. \left. \left. - jk^{2} \sum_{m} \left[ S_{m}^{u} J_{1}^{(2)} (kS_{m}^{u}r) h_{ym}^{u}(z) \left[ x_{3m} \cos\phi + x_{4m} \sin\phi \right] \right] \right] \right. \\ \left. \left. r < r_{0} \right] \right] \right. \\ \left. \left. \left. + S_{m}^{u} \frac{J_{1}^{(k}(kS_{m}^{u}r)}{kS_{m}^{u}r} h_{xm}^{u}(z) \left[ -x_{3m} \sin\phi + x_{4m} \cos\phi \right] \right] \right. \\ \left. \left. r > r_{0} \right] \right] \right. \\ \left. \left. \left. + S_{m}^{u} \frac{J_{1}^{(2)} (kS_{m}^{u}r)}{kS_{m}^{u}r} h_{xm}^{u}(z) \left[ -x_{3m} \sin\phi + x_{4m} \cos\phi \right] \right] \right. \\ \left. \left. r > r_{0} \right] \right] \right] \right. \\ \left. \left. \left. + S_{m}^{u} \frac{J_{1}^{(2)} (kS_{m}^{p}r)}{kS_{m}^{p}r} h_{xm}^{p}(z) \left[ -e_{xm}^{p}(z_{0}) \cos\phi + a_{m}^{p} e_{ym}^{p}(z_{0}) \sin\phi \right] \right] \right] \right] \right] \right. \\ \left. \left. \left. + S_{m}^{u} \frac{J_{1}^{(k}(kS_{m}^{p}r)}{kS_{m}^{m}r} h_{xm}^{p}(z) \left[ -e_{xm}^{p}(z_{0}) \sin\phi + a_{m}^{p} e_{ym}^{p}(z_{0}) \cos\phi \right] \right] \right\} \right] \right] \right\}$$

$$\left. \left. \left. \left. \left. \left. - \lambda_{m}^{k} S_{m}^{p} h_{xm}^{p}(z) \left[ -e_{xm}^{p}(z_{0}) \sin\phi + a_{m}^{p} e_{ym}^{p}(z_{0}) \cos\phi \right] \right] \right\} \right] \right\} \right] \right\}$$

$$\left. \left. \left. \left. \left. \left. - \lambda_{m}^{k} S_{m}^{p} h_{xm}^{p}(z) \left[ -x_{1m} \sin\phi + x_{2m} \cos\phi \right] \right] \right] \right\} \right] \right\} \right\} \right\}$$

$$\left. \left. \left. \left. \left. \left. \left. r < r_{0} \right\} \right] \right\} \right\} \right] \left. \left. \left. r < r_{0} \right\} \right] \right\} \right] \left. \left. r < r_{0} \right\} \right] \right\} \right\}$$

$$\left. \left. \left. \left. \left. \left. - \left[ S_{m}^{u} \frac{J_{1}^{(2)} (kS_{m}^{u}r) h_{xm}^{u}(z) \left[ x_{3m} \cos\phi + x_{4m} \sin\phi \right] \right] \right] \right\} \right] \right\} \right\} \right\} \right\} \left. \left. r < r_{0} \right\} \right\}$$

Since ratios of the perturbed to unperturbed fields are the quantities displayed in the following section, for convenience the unperturbed fields are listed below

$$\sum_{m} \left( s_{m}^{p} Q_{nm}^{up} x_{1m} + j s_{m}^{p} \frac{J_{1}(k s_{m}^{p} r_{o})}{k s_{m}^{p} r_{o}} R_{nm}^{up} x_{2m} - s_{m}^{u} T_{nm}^{uu} x_{3m} - j s_{m}^{u} \frac{H_{1}^{(2)}(k s_{m}^{u} r_{o})}{k s_{m}^{u} r_{o}} U_{nm}^{uu} x_{4m} \right)$$

$$= j\pi M k \sum_{m} \left\{ \lambda_{m}^{p} S_{m}^{p} \left[ e_{xm}^{p} (z_{o}) P_{nm}^{up} + j \alpha_{m}^{p} e_{ym}^{p} (z_{o}) \frac{1}{k S_{m}^{p} r_{o}} R_{nm}^{up} \right] \right\}$$
(30)

$$\sum_{m} \left[ -j S_{m}^{p} \frac{J_{1}(k S_{m}^{p} r_{o})}{k S_{m}^{p} r_{o}} R_{nm}^{pp} x_{1m}^{} + S_{m}^{p} Q_{nm}^{pp} x_{2m}^{} + j S_{m}^{u} \frac{H_{1}^{(2)}(k S_{m}^{u} r_{o})}{k S_{m}^{u} r_{o}} U_{nm}^{pu} x_{3m}^{} - S_{in}^{u} T_{nm}^{pu} x_{4m}^{} \right]$$

$$= j\pi Mk \sum_{m} \left\{ \lambda_{m}^{p} S_{m}^{p} \left[ \alpha_{m}^{p} e_{ym}^{p}(z_{o}) P_{nm}^{pp} - j e_{xm}^{p}(z_{o}) \frac{H_{1}^{(2)}(kS_{m}^{p}r_{o})}{kS_{m}^{p}r_{o}} R_{nm}^{pp} \right] \right\}$$
(31)

$$\sum_{m} \left[ -j S_{in}^{p} \frac{J_{1}(kS_{m}^{p}r_{o})}{kS_{m}^{p}r_{o}} R_{nm}^{up} x_{1m}^{u} + S_{in}^{p} Q_{nm}^{up} x_{2m}^{u} + j S_{m}^{u} \frac{H_{1}^{(2)}(kS_{m}^{u}r_{o})}{kS_{m}^{u}r_{o}} U_{nm}^{uu} x_{3m}^{u} - S_{in}^{u} T_{nm}^{uu} x_{4m}^{u} \right]$$

$$= j_{\pi}Mk\sum_{m}\left\{\lambda_{m}^{p}S_{m}^{p}\left[\alpha_{m}^{p}e_{ym}^{p}(z_{o})P_{nm}^{up}-je_{xm}^{p}(z_{o})\frac{H_{1}^{(2)}(kS_{m}^{p}r_{o})}{kS_{m}^{p}r_{o}}R_{nm}^{up}\right]\right\}$$
(32)

Equations (29) through (32) determine  $(x_1, x_2, x_3, x_4)_m$  and in terms of these quantities the field components discussed in the following section are developed from Eqs. (1), (13), (14) and (20) through (23). They are

$$E_{z}^{p} = j \pi M k_{m}^{3} \sum_{m} \lambda_{m}^{p} S_{m}^{p} H_{1}^{(2)} (k S_{m}^{p} r) e_{zm}^{p} (z) [e_{xm}^{p} (z_{0}) \cos \phi + \alpha_{m}^{p} e_{ym}^{p} (z_{0}) \sin \phi] \\ -k_{m}^{2} \sum_{m}^{N} S_{m}^{p} I_{1} (k S_{m}^{p} r) e_{zm}^{p} (z) [x_{1m} \cos \phi + x_{2m} \sin \phi] , r < r_{0}$$

$$= -k_{m}^{2} \sum_{m}^{N} H_{1}^{(2)} (k S_{m}^{u} r) e_{zm}^{u} (z) [x_{3m} \cos \phi + x_{4m} \sin \phi] , r > r_{0}$$

$$(33)$$

$$P_{nm}^{pp} = \int_{-\infty}^{\infty} [a_{n}^{p}(-)]^{\dagger} P_{m} dz , \quad Q_{nm}^{pp} = \int_{-\infty}^{\infty} [a_{n}^{p}(-)]^{\dagger} Q_{m} dz , \quad R_{nm}^{pp} = \int_{-\infty}^{\infty} [a_{n}^{p}(-)]^{\dagger} R_{m} dz ,$$

$$T_{nm}^{pu} = \int_{-\infty}^{\infty} [a_{n}^{p}(-)]^{\dagger} T_{m} dz , \quad U_{nm}^{pu} = \int_{-\infty}^{\infty} [a_{n}^{p}(-)]^{\dagger} U_{m} dz ,$$

$$P_{nm}^{up} = \int_{-\infty}^{\infty} [a_{n}^{u}(+)]^{\dagger} P_{m} dz , \quad Q_{nm}^{up} = \int_{-\infty}^{\infty} [a_{n}^{u}(+)]^{\dagger} Q_{m} dz , \quad R_{nm}^{up} = \int_{-\infty}^{\infty} [a_{n}^{u}(+)]^{\dagger} R_{m} dz ,$$

$$T_{nm}^{uu} = \int_{-\infty}^{\infty} [a_{n}^{u}(+)]^{\dagger} T_{m} dz , \quad U_{nm}^{uu} = \int_{-\infty}^{\infty} [a_{n}^{u}(+)]^{\dagger} U_{m} dz$$
(28)

In Eq. (28) the dagger sign, t, indicates the adjoint (i.e., the complex conjugate transpose).

To generate the field matching equations, first multiply Eq. (24) through by  $\cos \phi$  and integrate  $\phi$  from 0 to  $2\pi$ . Next multiply through by  $[q_n^p(-)]^{\dagger}$  and integrate over z. If N is the total number of modes used, this generates one equation for the 4 x N unknowns  $(x_1, x_2, x_3, x_4)_m$ , where m takes on the values 1 through N. Next multiply the equation obtained from the  $\phi$  integration by  $(q_n^u(+))^{\dagger}$  and integrate over z. This generates a second equation. By extracting the sin $\phi$  terms, two more equations are generated in a similar fashion. Performing these operations for n = 1 through N generates the requisite 4 x N equations. The equations are (here the mode indices are included explicitly):

$$\sum_{m} \left[ s_{m}^{p} Q_{nm}^{pp} x_{1m} + j s_{m}^{p} \frac{J_{1}(k s_{m}^{p} r_{o})}{k s_{m}^{p} r_{o}} R_{nm}^{pp} x_{2m} - s_{m}^{u} T_{nm}^{pu} x_{3m} - j s_{m}^{u} \frac{H_{1}^{(2)}(k s_{m}^{u} r_{o})}{k s_{m}^{u} r_{o}} U_{nm}^{pu} x_{4m} \right]$$

$$= j \pi M k \sum_{m} \left\{ \chi_{m}^{p} s_{m}^{p} \left[ e_{xm}^{p}(z_{o})^{p} r_{nm}^{pp} + j \alpha_{m}^{p} e_{ym}^{p}(z_{o}) \frac{H_{1}^{(2)}(k s_{m}^{p} r_{o})}{k s_{m}^{p} r_{o}} R_{nm}^{pp} \right] \right\}$$
(29)

As discussed by Pappert and Smith [1972], there exists height gains

$$q_{m}^{p}(-) = \begin{pmatrix} w_{1}^{p}(z) \\ w_{2}^{p}(z) \\ w_{3}^{p}(z) \\ w_{4}^{p}(z) \\ w_{4}^{p}(z) \\ m \end{pmatrix}_{m} q_{m}^{u}(+) = \begin{pmatrix} w_{1}^{u}(z) \\ w_{2}^{u}(z) \\ w_{3}^{u}(z) \\ w_{4}^{u}(z) \\ w_{4}^{u}(z) \\ m \end{pmatrix}_{m}$$
(26)

associated with an adjoint guide for which the inner products  $[q_n^p(-), f_m^p(-)]$ and  $[q_n^u(+), f_m^u(+)]$  are zero when  $m \neq n$ . The matching equations will be developed by a method somewhat akin to the treatment of mode conversion in the VLF band [Pappert and Snyder, 1972], although it is by no means clear in the present case that it is an optimum or preferred procedure. As will be seen later, the method does have the convenient consequence that it is essentially equivalent to simply matching H<sub> $\phi$ </sub> and E<sub>Z</sub> at  $r = r_0$  at the ground. As a preliminary to developing the matching equations, the following definitions will be useful:

$$P_{m} = \begin{bmatrix} jH_{1}^{(2)'}(kS^{p}r_{o})e_{y}^{p}(z) \\ H_{1}^{(2)}(kS^{p}r_{o})e_{z}^{p}(z) \\ jH_{1}^{(2)'}(kS^{p}r_{o})h_{y}^{p}(z) \\ H_{1}^{(2)}(kS^{p}r_{o})h_{z}^{p}(z) \end{bmatrix}_{m}, \quad Q_{m} = \begin{bmatrix} jJ_{1}^{'}(kS^{p}r_{o})e_{y}^{p}(z) \\ J_{1}^{'}(kS^{p}r_{o})e_{z}^{p}(z) \\ jJ_{1}^{'}(kS^{p}r_{o})h_{y}^{p}(z) \\ J_{1}^{'}(kS^{p}r_{o})h_{z}^{p}(z) \end{bmatrix}_{m}, \quad R_{m} = \begin{bmatrix} e_{x}^{p}(z) \\ 0 \\ h_{x}^{p}(z) \\ J_{1}^{'}(kS^{p}r_{o})h_{z}^{p}(z) \end{bmatrix}_{m}$$

$$T_{m} = \begin{bmatrix} jH_{1}^{(2)'}(kS^{u}r_{o})e_{y}^{u}(z) \\ H_{1}^{(2)}(kS^{u}r_{o})e_{z}^{u}(z) \\ jH_{1}^{(2)'}(kS^{u}r_{o})h_{y}^{u}(z) \\ H_{1}^{(2)}(kS^{u}r_{o})h_{z}^{u}(z) \end{bmatrix}_{m} = \begin{bmatrix} e_{x}^{u}(z) \\ 0 \\ h_{x}^{u}(z) \\ 0 \\ 0 \end{bmatrix}_{m}$$

(27)

$$+jS^{p}\frac{J_{1}(kS^{p}r_{0})}{kS^{p}r_{0}}(-x_{1}\sin\phi + x_{2}\cos\phi)\begin{bmatrix}e_{x}^{p}(z)\\0\\h_{x}^{p}(z)\\0\end{bmatrix}\Big]_{m}$$

$$= -k^{2}\sum_{m}\left\{S^{u}(x_{3}\cos\phi + x_{4}\sin\phi)\begin{bmatrix}jH_{1}^{(2)'}(kS^{u}r_{0})e_{y}^{u}(z)\\H_{1}^{(2)}(kS^{u}r_{0})e_{z}^{u}(z)\\jH_{1}^{(2)'}(kS^{u}r_{0})h_{y}^{u}(z)\\H_{1}^{(2)}(kS^{u}r_{0})h_{z}^{u}(z)\end{bmatrix}$$

$$+ jS^{u}\frac{H_{1}^{(2)}(kS^{u}r_{0})}{kS^{u}r_{0}}(-x_{3}\sin\phi + x_{4}\cos\phi)\begin{bmatrix}e_{x}^{u}(z)\\0\\h_{x}^{u}(z)\\0\end{bmatrix}\Big]_{m}$$
(24)

In Eq. (24) the top element of the column vector is  $E_{\phi}$ , the second  $E_z$ , the third  $\pi_{\phi}$ , and the last is  $\pi_z$ . The left-hand side of the equation gives the fields associated with the perturbed region at  $r = r_0$  and the right-hand side gives the fields associated with the unperturbed region at  $r = r_0$ .

With a finite number of modes (and in the present case only one nonevanescent mode exists) it is impossible to satisfy Eq. (24) for all z. Thus, the continuity will be developed only approximately following a prescription suggested by asymptotic considerations when  $|kS^{p}r_{0}|>>1$  and  $|kS^{u}r_{0}|>>1$ . In that instance the leading terms of the forward (+) and backward (-) propagating waves associated with Eq. (24) becomes a product of radial functions and the column vectors

$$f_{m}^{p}(\pm) = \begin{bmatrix} \pm e_{y}^{p}(z) \\ e_{z}^{p}(z) \\ \pm h_{y}^{p}(z) \\ h_{z}^{p}(z) \end{bmatrix}_{in}, f_{m}^{u}(\pm) = \begin{bmatrix} e_{y}^{u}(z) \\ e_{z}^{u}(z) \\ h_{y}^{u}(z) \\ h_{y}^{u}(z) \\ h_{z}^{u}(z) \end{bmatrix}_{m}$$
(25)

A disquieting feature of the analysis is that the TE components, and in particular the H<sub>r</sub> component, are not continuous at  $r = r_0$ . This is not terribly surprising because, as just mentioned, the method used to obtain the boundary equations is equivalent to matching only the H<sub> $\phi$ </sub> and E<sub>Z</sub> components at  $r = r_0$  at the ground. Perhaps inclusion of evanescent modes would improve continuity of H<sub>r</sub> without destroying the H<sub> $\phi$ </sub> and E<sub>Z</sub> continuity. However, no effort along those lines has been attempted in the current study.

Several possible extensions of the present effort are:

i) Examine effects of non-evanescent modes on continuity of major field components.

ii) Extend analysis to allow for general location of the disturbance relative to the transmitter.

iii) Extend analysis to allow for radial and/or azimuthal variations.

iv) Include the effect of earth curvature.

v) Extend the analysis to elliptically symmetric disturbances.

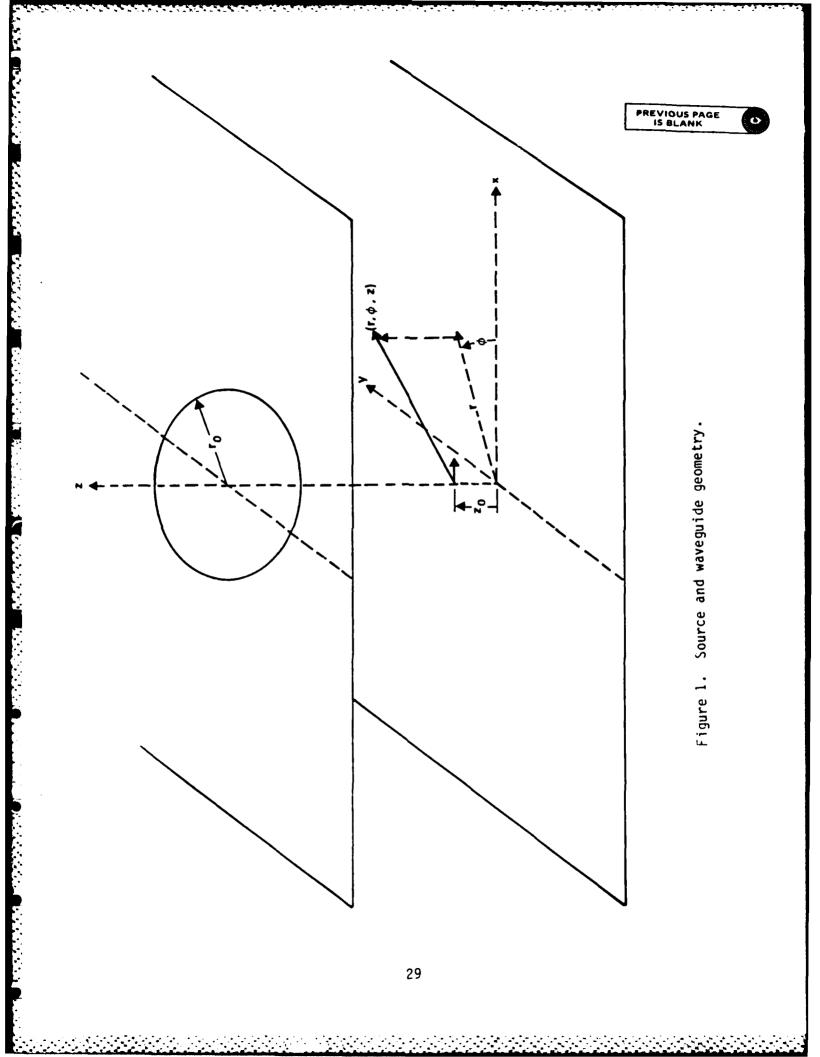
## REFERENCES

- Bickel, J.E., J.A. Ferguson, and G.V. Stanley, "Experimental observation of magnetic field effects on VLF propagation at night," <u>Radio Sci</u>., 5(1), 19-25, 1970.
- Budden, K.G., <u>Radio waves in the Ionosphere</u>, (Cambridge Univ. Press, Cambridge), 1961.
- Budden, K.G., "The influence of the earth's magnetic field on radio propagation by waveguide modes," <u>Proc. Roy. Soc.</u> (London), Ser. A265 (1323), 538-553, 1962.
- Ferguson, J.A., L.R. Hitney and R.A. Pappert, A Program to Compute Vertical Electric ELF Fields in a Laterally Inhomogeneous Earth Ionosphere Waveguide, NOSC TR 851, prepared for the Def. Nucl. Agency, 62 pp, Dec 1982.
- Field, E.C. and R.G. Joiner, "An integral equation approach to long wave propagation in a non stratified earth ionosphere waveguide," <u>Radio Sci.</u>, 14(6), 1057-1068, 1979.
- Field, E.C. and R.G. Joiner, "Effects of lateral ionospheric gradients on ELF propagation," Radio Sci., 17(3), 693-700, 1982.
- Greifinger, C. and P. Greifinger, Effects of a Cylindrically Symmetric Ionospheric Disturbance on ELF Propagation in the Earth Ionosphere Waveguide, Def. Nucl. Agency Rep. DNA 4399T, 40 pp., R & D Associates, Marina del Rey, Calif., June 1977.

- Pappert, R.A., On the Problem of Horizontal Dipole Excitation of the Earth-Ionosphere Waveguide. Interim report No. 724 prepared by the Naval Electronics Laboratory Center (now NOSC) for the Defense Atomic Support Agency (now DNA), March 1968.
- Pappert, R.A. and R.R. Smith, "Orthogonality of VLF height gains in the earth ionosphere waveguide," Radio Sci., 7(2), 275-278, 1972.
- Pappert, R.A. and F.P. Snyder, "Some results of a mode conversion program for VLF," Radio Sci., 7(10), 913-923, 1972.
- Pappert, R.A. and W.F. Moler, "A theoretical study of ELF normal mode reflection and absorption produced by nighttime ionospheres," <u>J. Atmos.</u> Terr. Phys., 40(9), 1031-1045, 1978.
- Pappert, R.A., "Effects of a large patch of sporadic-E on nighttime propagation at lower ELF," J. Atmos. Terr. Phys., 42(5), 417-425, 1980.
- Pappert, R.A., "Calculated effects of traveling sporadic-E on nocturnal ELF propagation. Comparison with measurement," <u>Radio Sci</u>., 20(2), 229-246, 1985.
- Pitteway, M.L.V., "The numerical calculation of wave-fields, reflection coefficients and polarizations for long radio waves in the lower ionosphere." I, Phil. Trans. Roy. Soc. (London), Ser. A257 (1079), 219-241, 1965.

Shellman, C.H., Propagation of ELF Waves in the Spherical Earth-Ionosphere Waveguide with Transverse and Longitudinal Variation of Properties, NOSC TD 607, prepared for the Def. Nucl. Agency, 194 pp., June 1983.

- Smith, R.R., A Program to Compute Ionospheric Height Gain Functions and Field Strengths. Interim Report No. 711 prepared by the Naval Electronics Laboratory Center (now NOSC) for the Defense Atomic Support Agency (now DNA), December 1970.
- Wait, J.R., "The mode theory of VLF radio propagation for a spherical earth and a concentric anisotropic ionosphere," <u>Can. J. Phys.</u>, 41(2), 299-315, 1963.
- Wait, J.R., "On phase changes in very-low frequency propagation induced by an ionospheric depression of finite extent," <u>J. Geophys. Res.</u>, 59(3), 441-445, 1964.
- Webber, G.E. and I.C. Peden, "VLF fields of a horizontal dipole below the polar anisotropic ionosphere," <u>IEEE Transactions on Antennas and</u> Propagation, AP-19(4), 523-529, 1971.



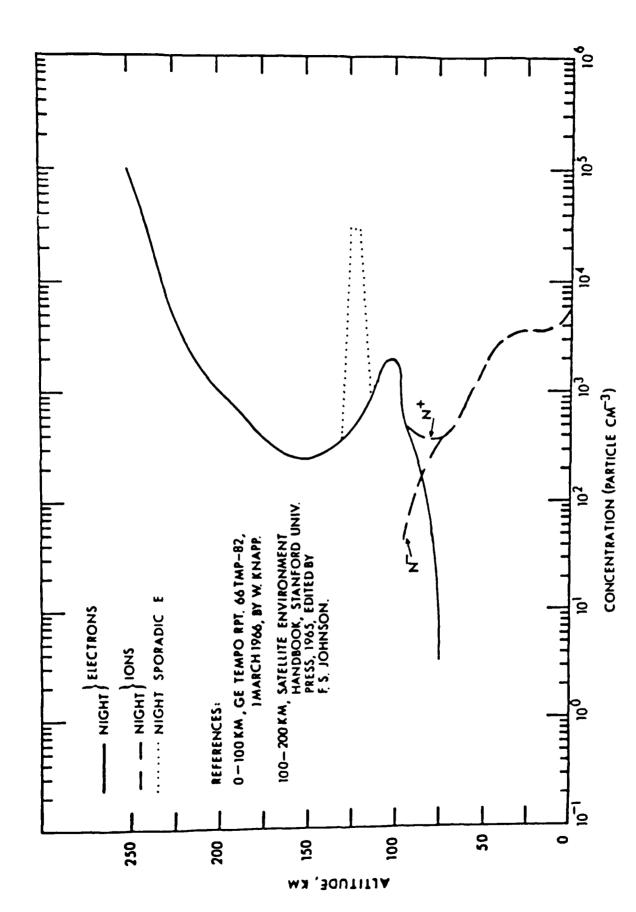
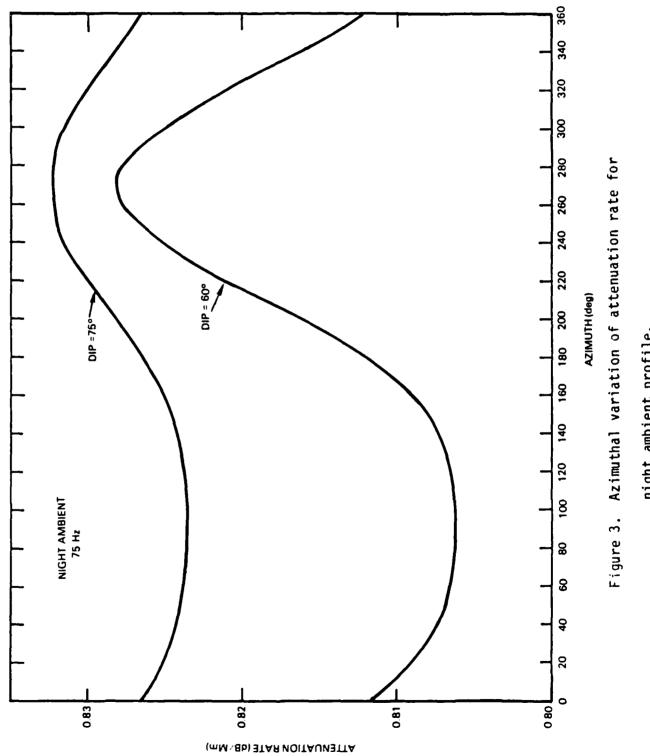
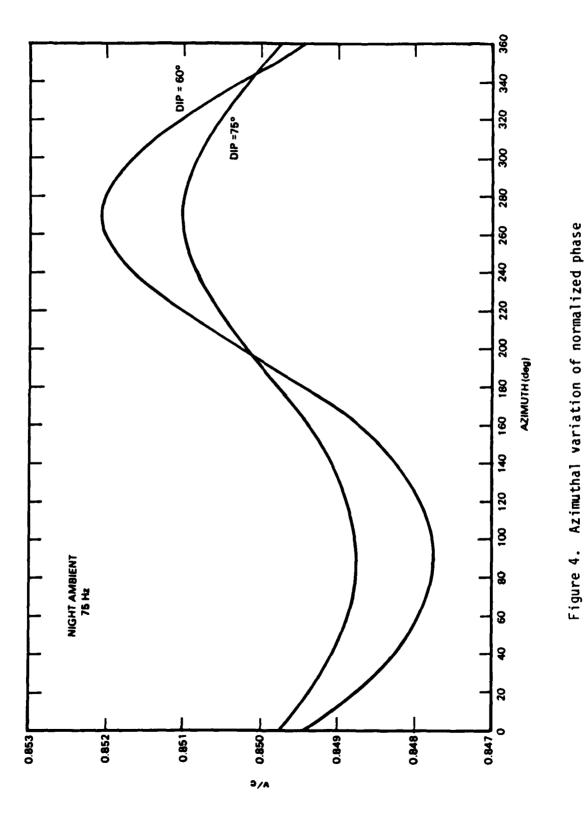


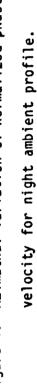
Figure 2. Night ambient and sporadic E profiles.

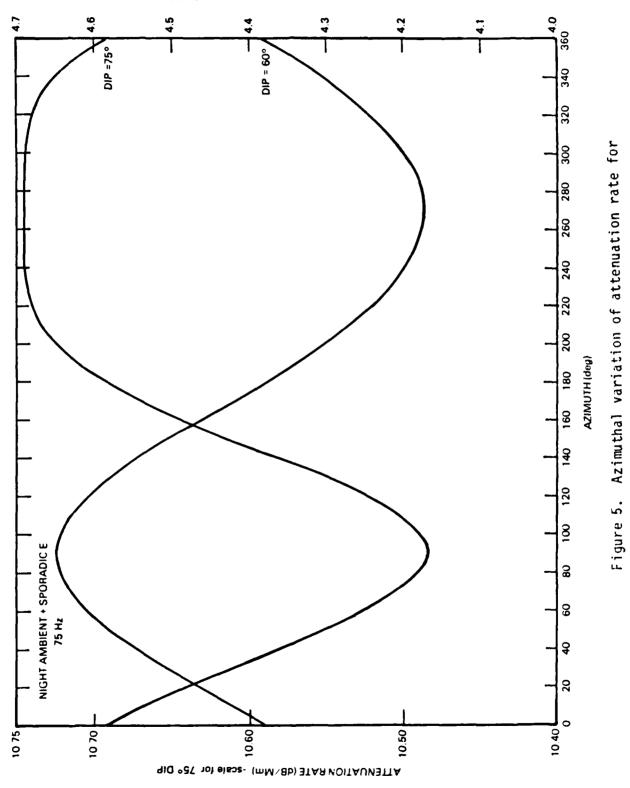


ſ

night ambient profile.



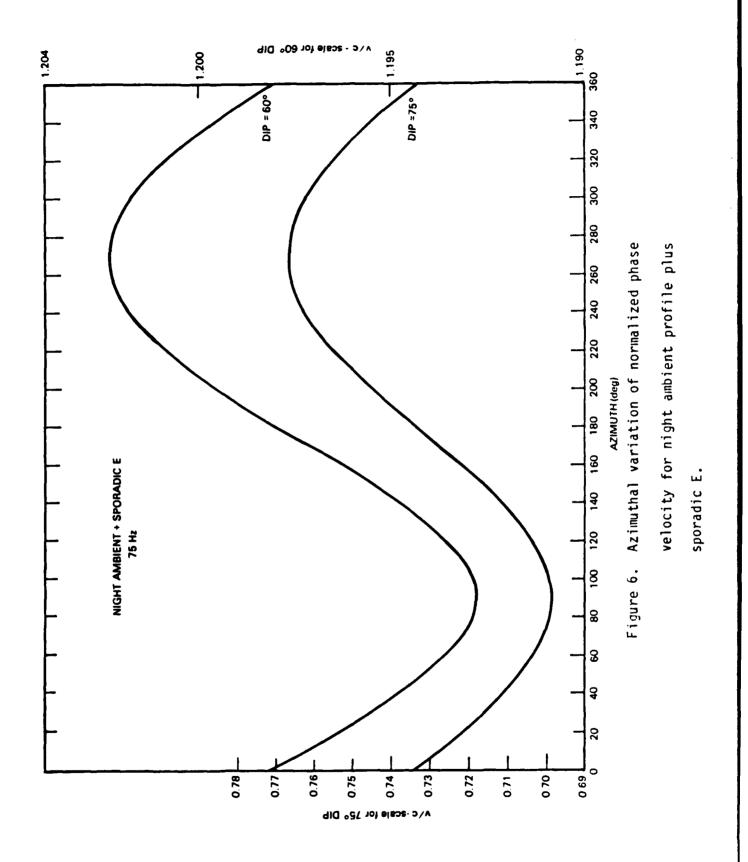




night ambient profile plus sporadic E.

•

ATTENUATION RATE (d8/Mm)-scale for 60°



وأنعفك

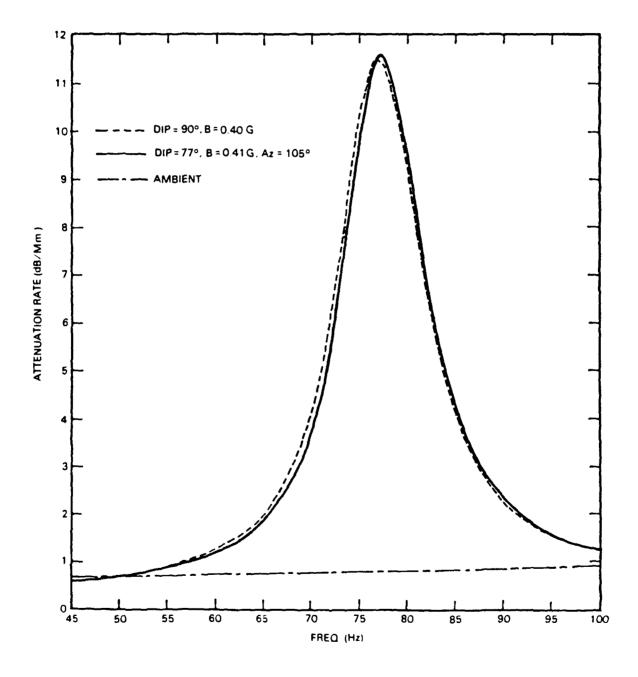
 

Figure 7. Attenuation rate vs. frequency.

٠.

.-

. . . . . . . .

. . . .

*.*...

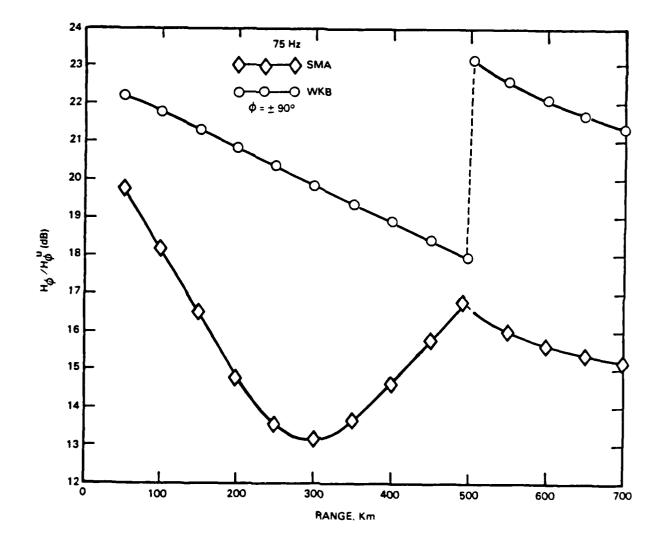
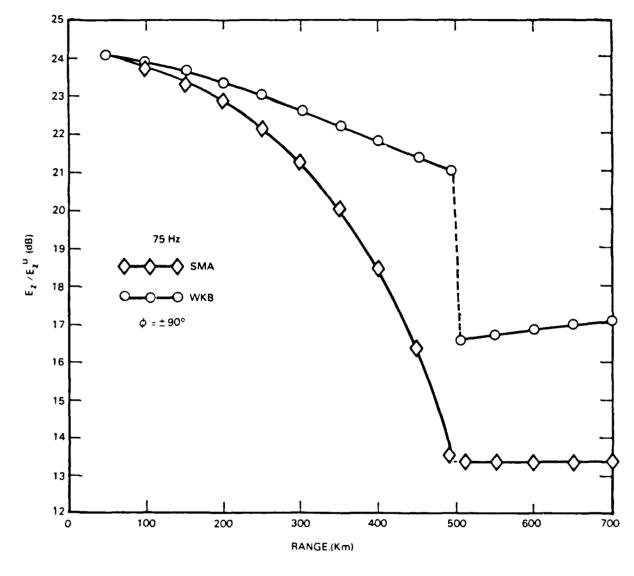
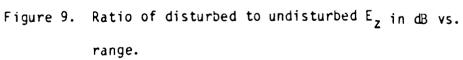


Figure 8. Ratio of disturbed to undisturbed H  $_{\varphi}$  in dB vs. range.





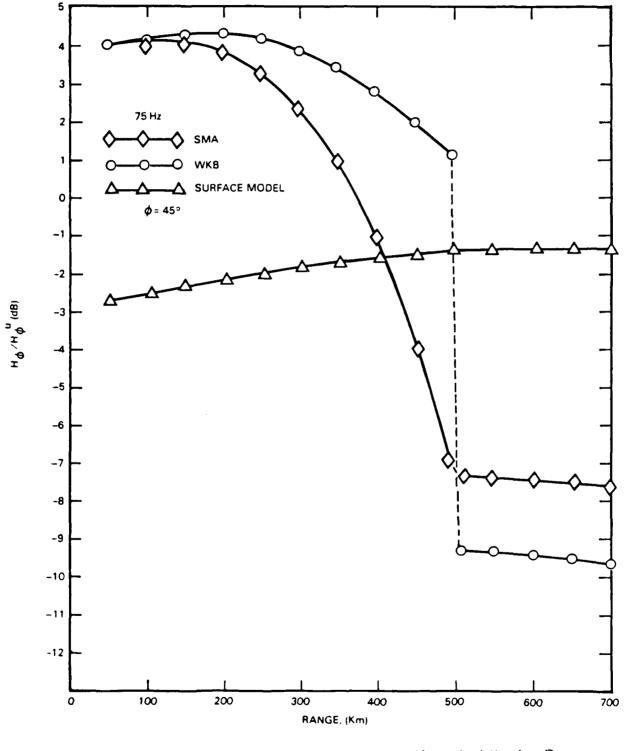


Figure 10. Ratio of disturbed to undisturbed H  $_{\varphi}$  in dB vs.

. . . . . . . . . . . .

range.

•

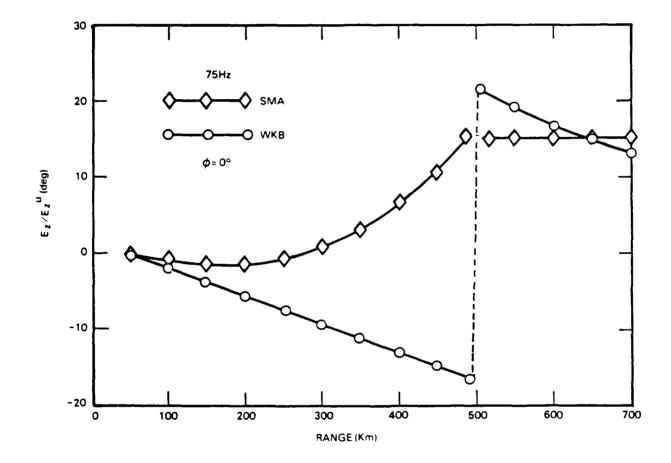


Figure 24. Disturbed and undisturbed phase difference for  $E_z$  vs. range.

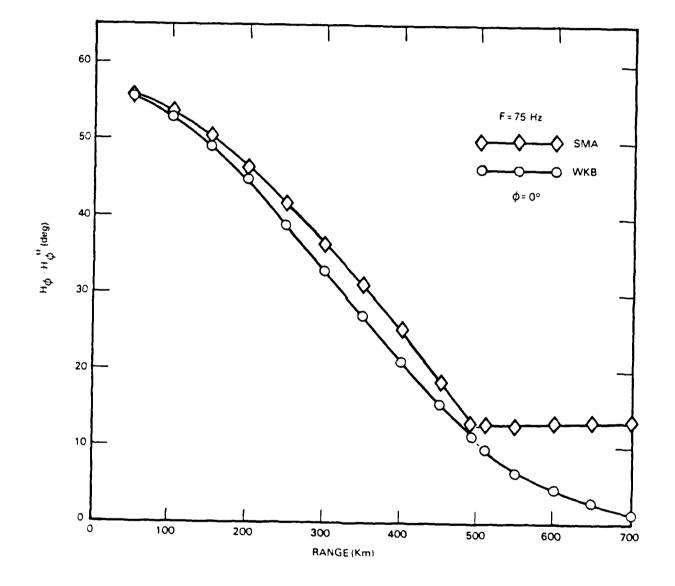
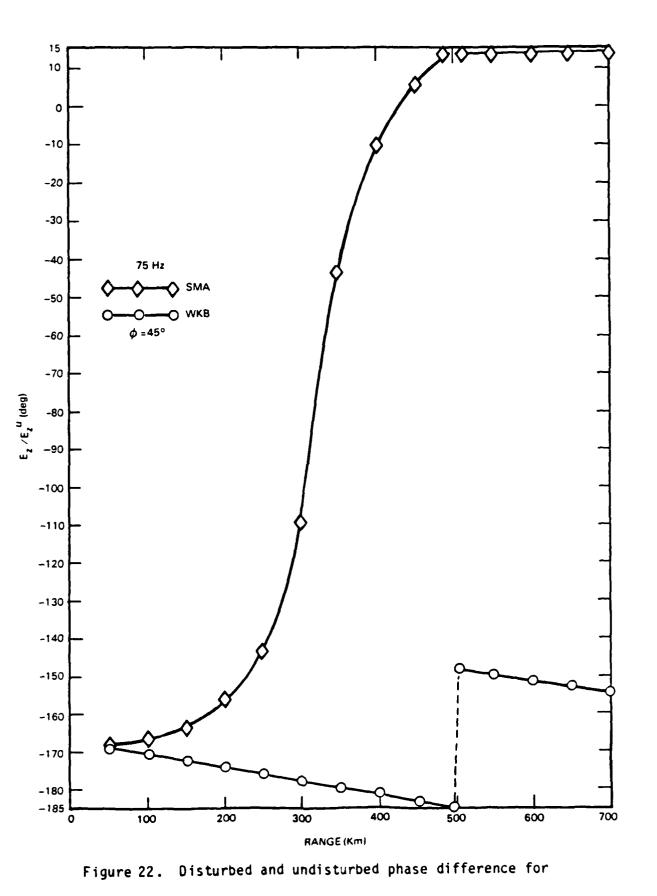


Figure 23. Disturbed and undisturbed phase difference for H  $_{\phi}$  vs. range.

٠.



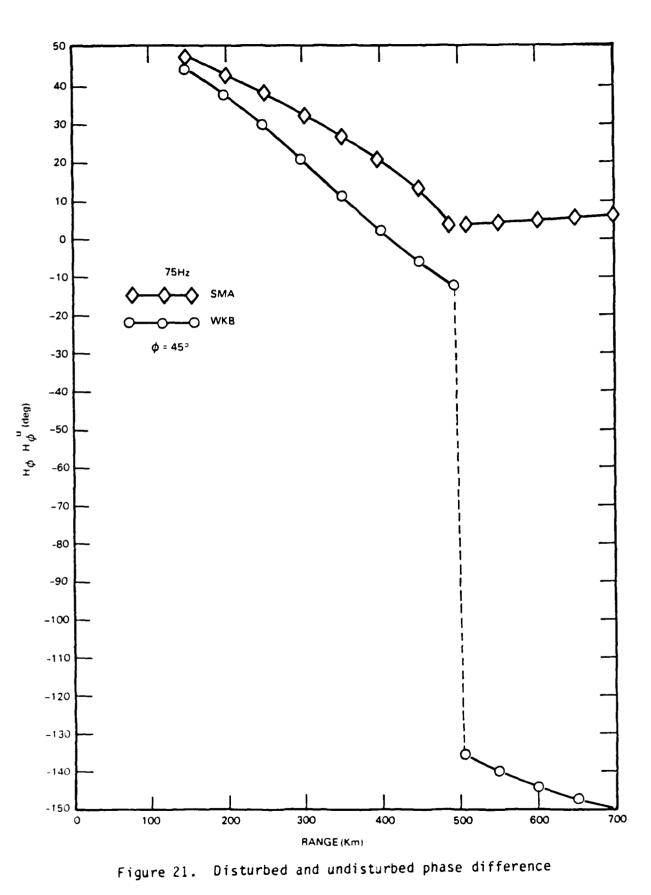
E<sub>z</sub> vs. range.

.

1.1.1

· · · ·

· .•



for  ${\rm H}_{\varphi}$  vs. range.

.

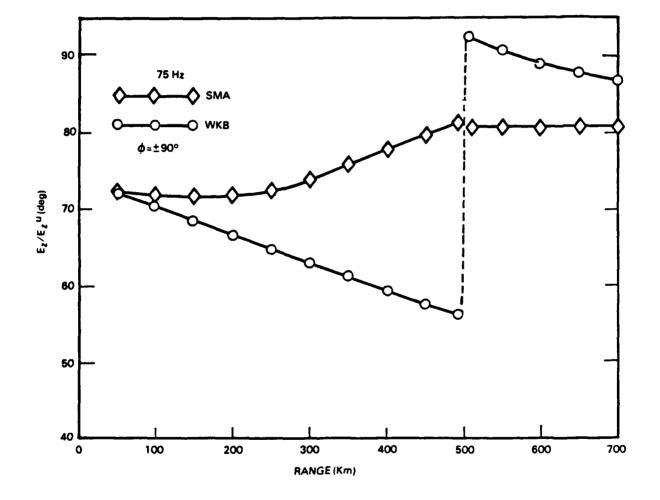


Figure 20. Disturbed and undisturbed phase difference for  $E_z$  vs. range.

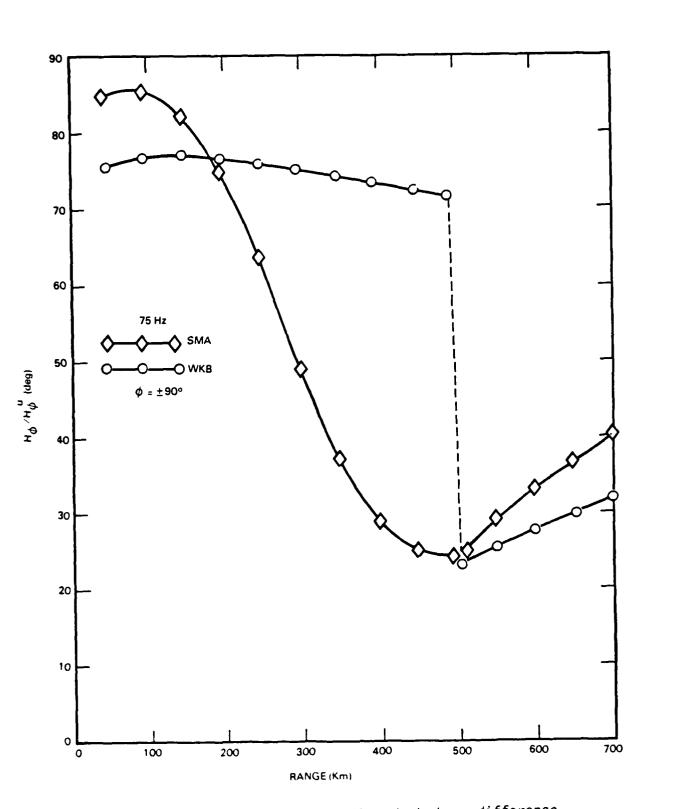
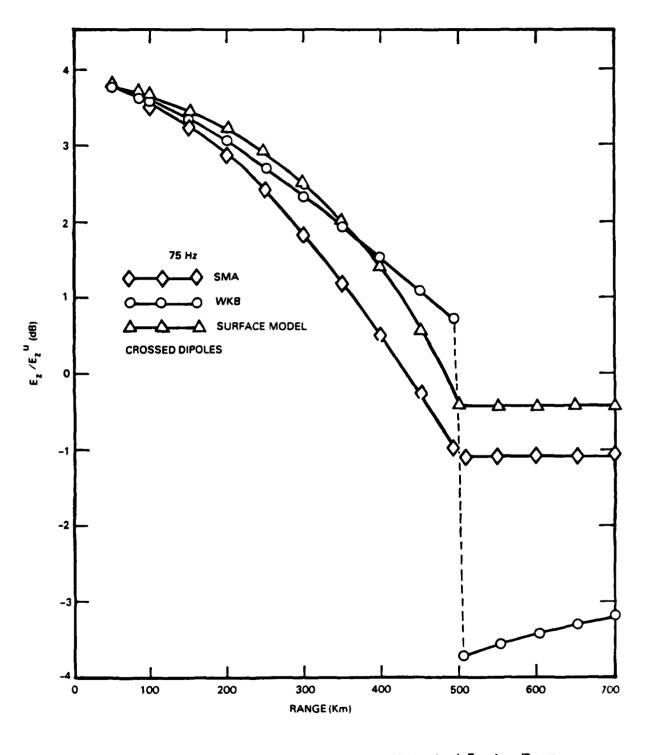


Figure 19. Disturbed and undisturbed phase difference

for  ${\rm H}_{\phi}$  vs. range.



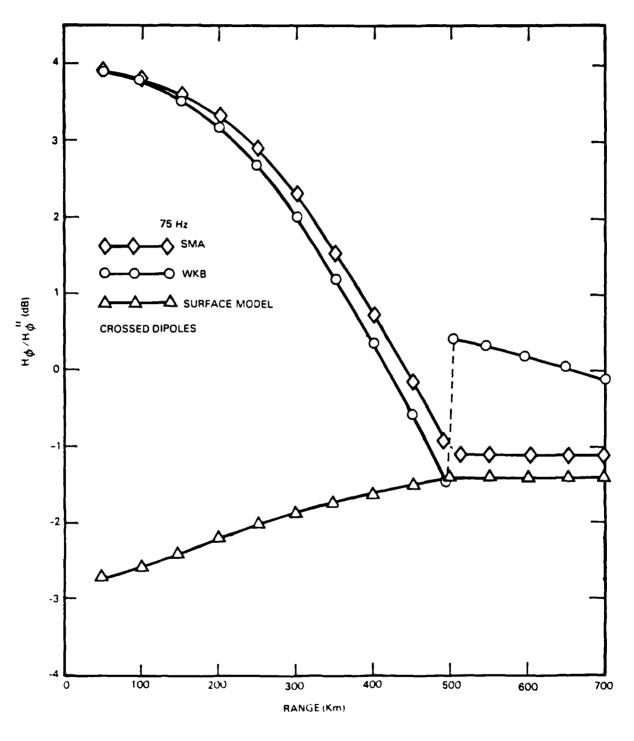
.1

. . .

••••

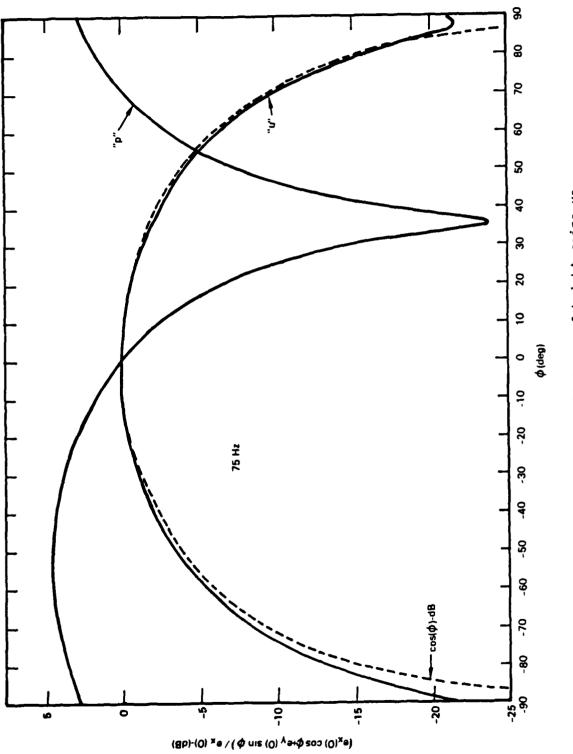
F

Figure 18. Ratio of disturbed to undisturbed E<sub>z</sub> in dB vs. range.



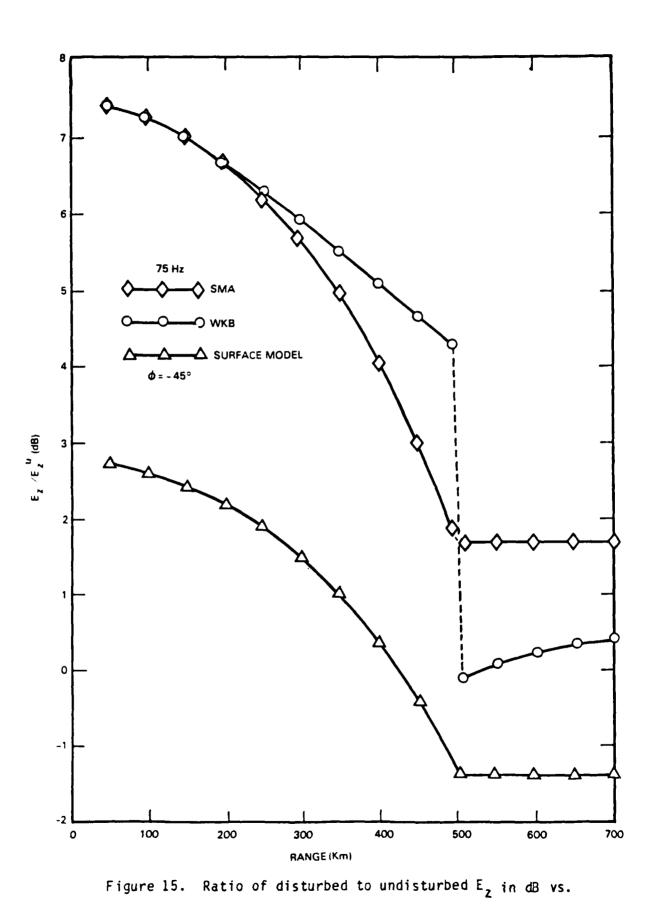
¥

Figure 17. Ratio of disturbed to undisturbed H  $_{\phi}$  in dB vs. range.





azimuth.



range.

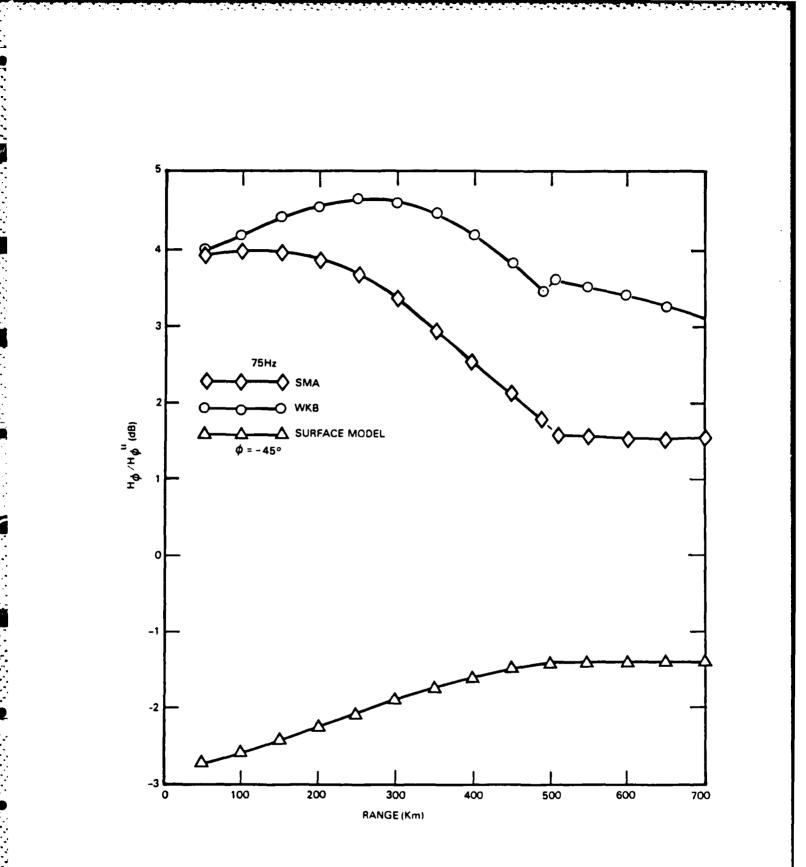
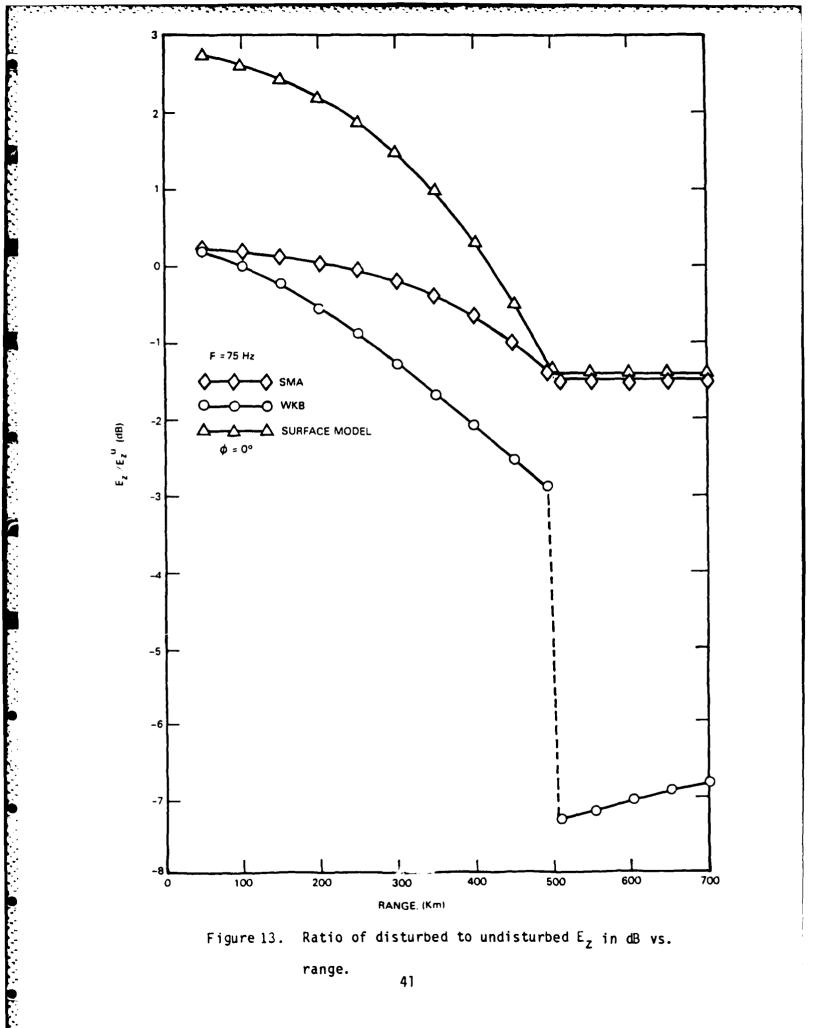


Figure 14. Ratio of disturbed to undisturbed H  $_{\phi}$  in dB vs. range.



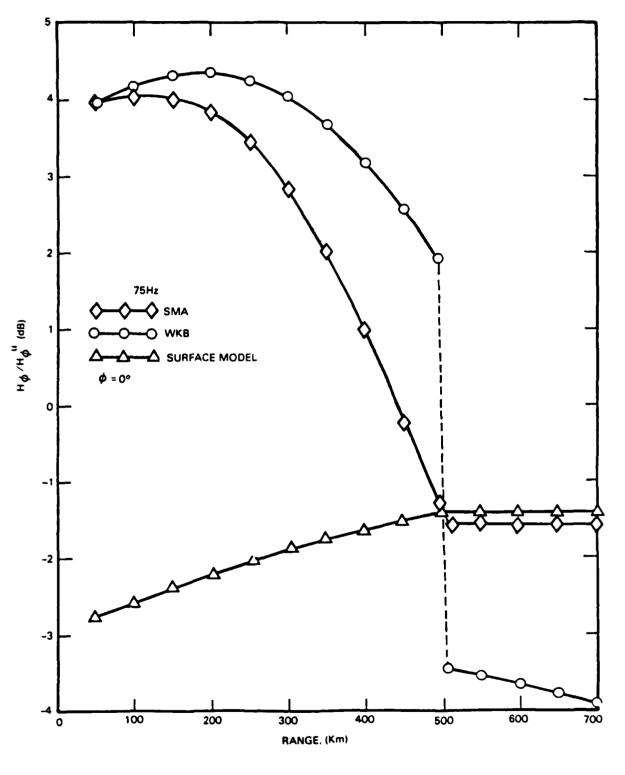


Figure 12. Ratio of disturbed to undisturbed H  $_{\phi}$  in dB vs. range.

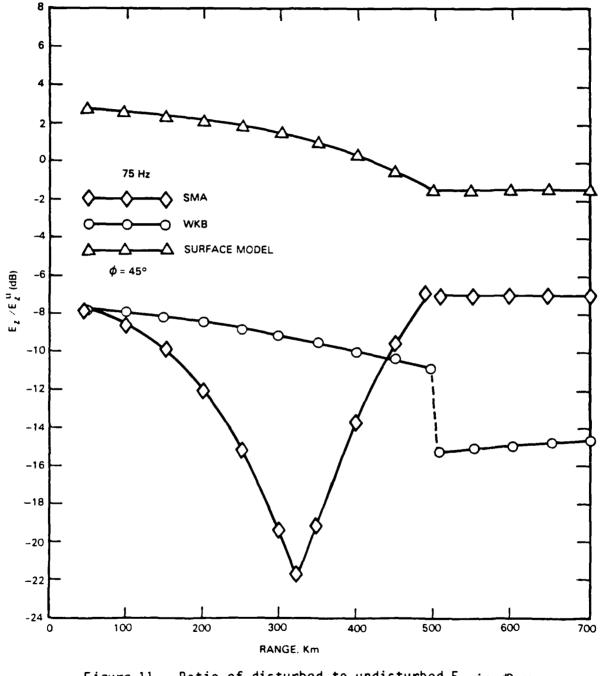


Figure 11. Ratio of disturbed to undisturbed  $E_z$  in dB vs.

range.

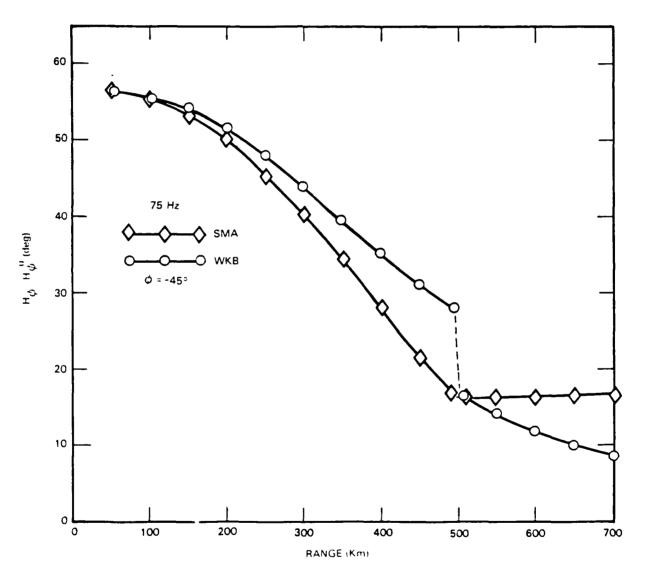


Figure 25. Disturbed and undisturbed phase difference for  ${\rm H}_{\varphi}$  vs. range.

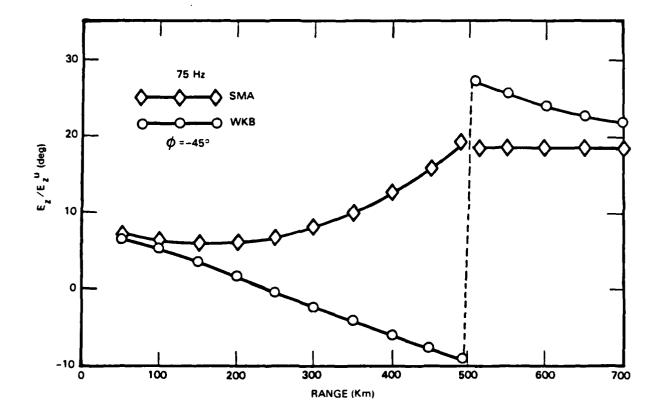


Figure 26. Disturbed and undisturbed phase difference for  $E_z$  vs. range.

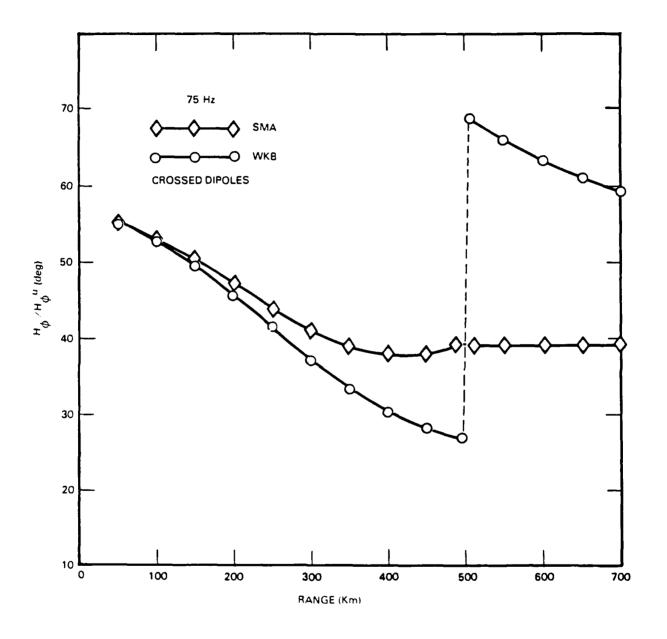


Figure 27. Disturbed and undisturbed phase difference for  $H_{\phi}$  vs. range.

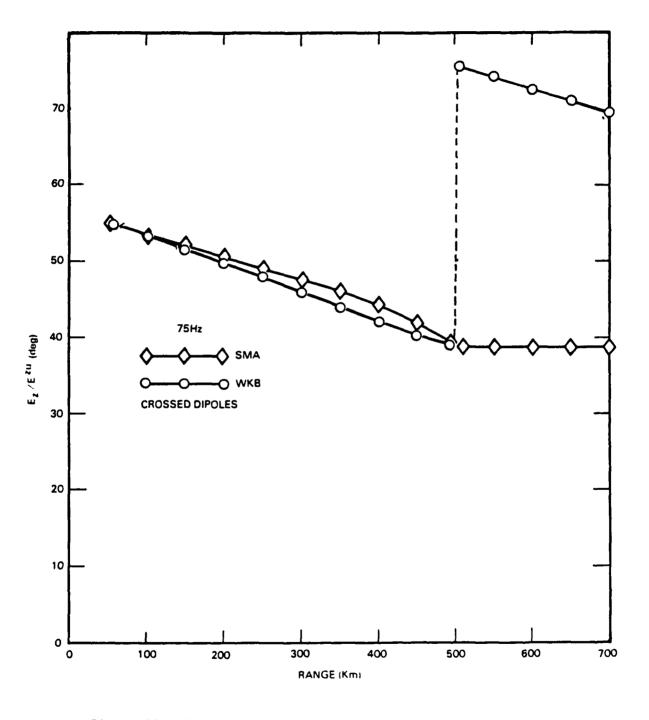


Figure 28. Disturbed and undisturbed phase difference for

E<sub>z</sub> vs. range.

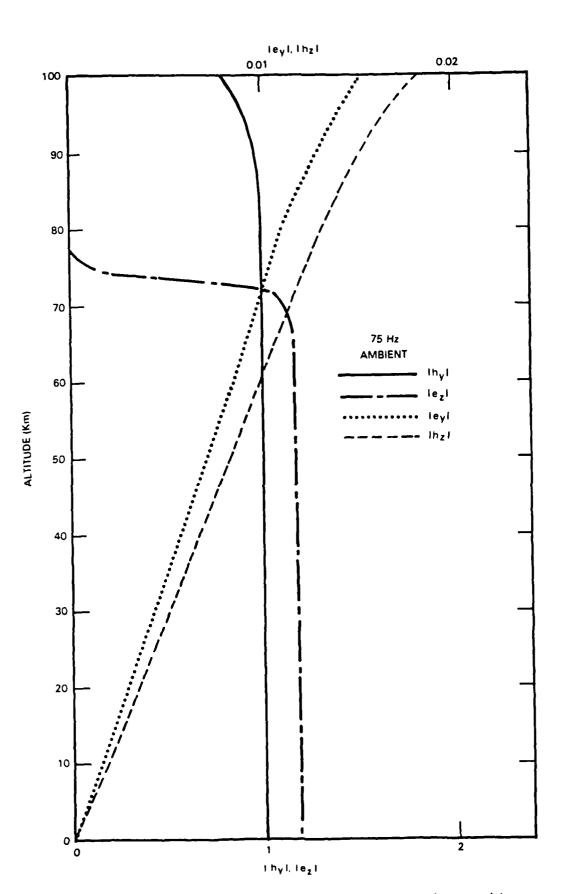


Figure 29. Height gain behavior for ambient guide.

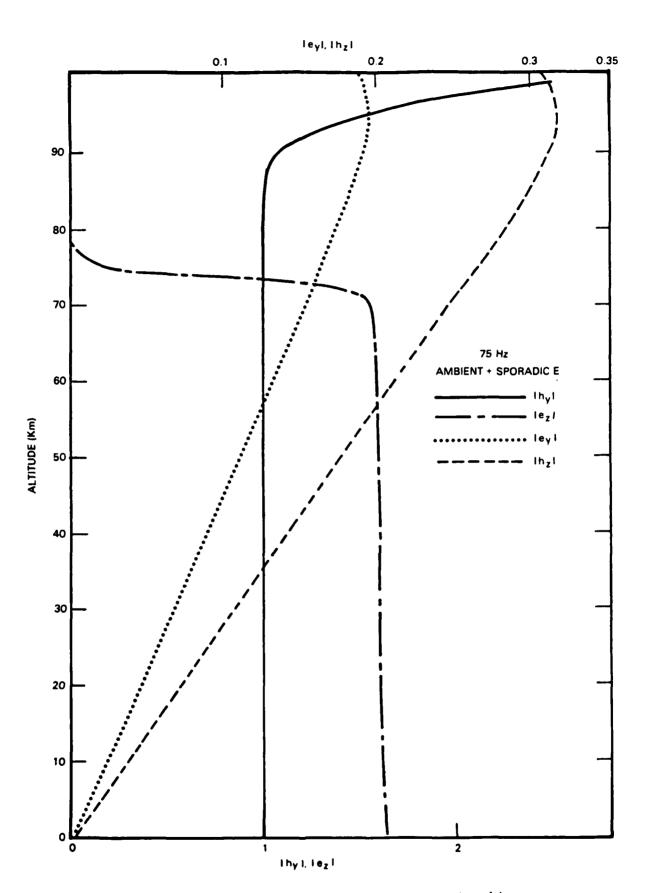
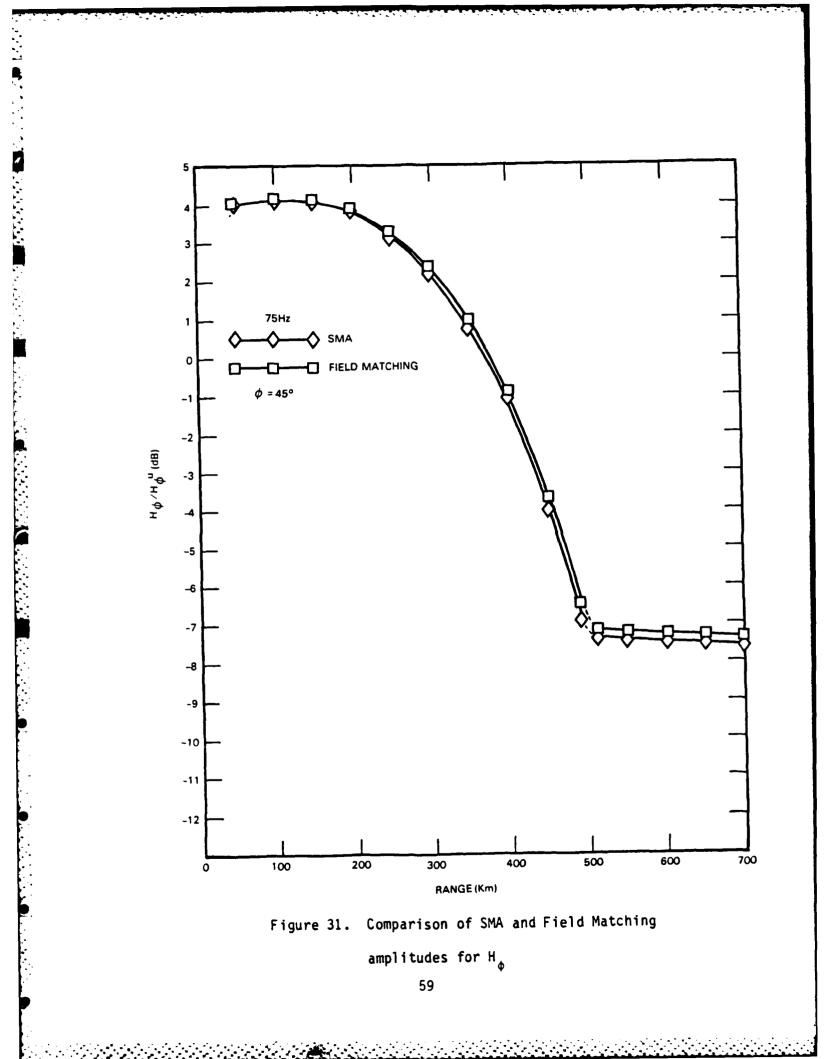
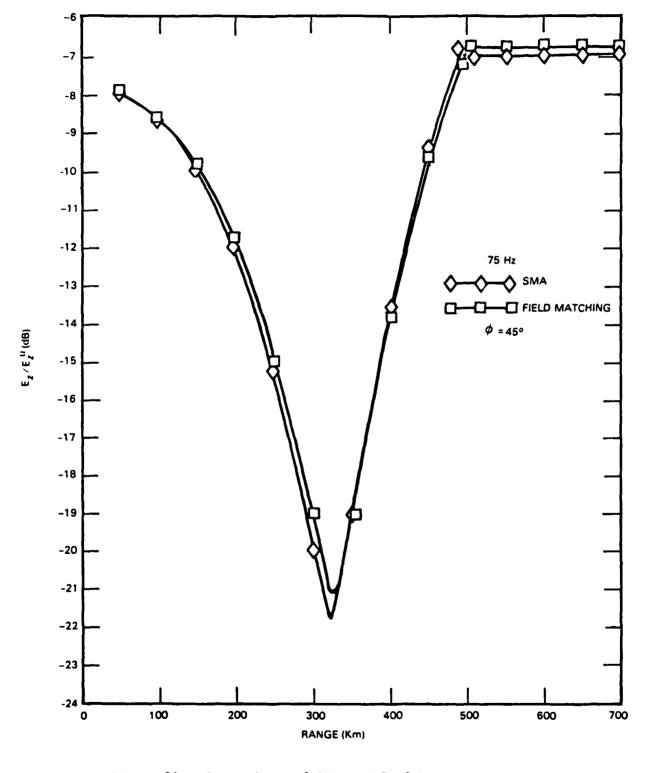


Figure 30. Height gain behavior for perturbed guide.







for Ez.

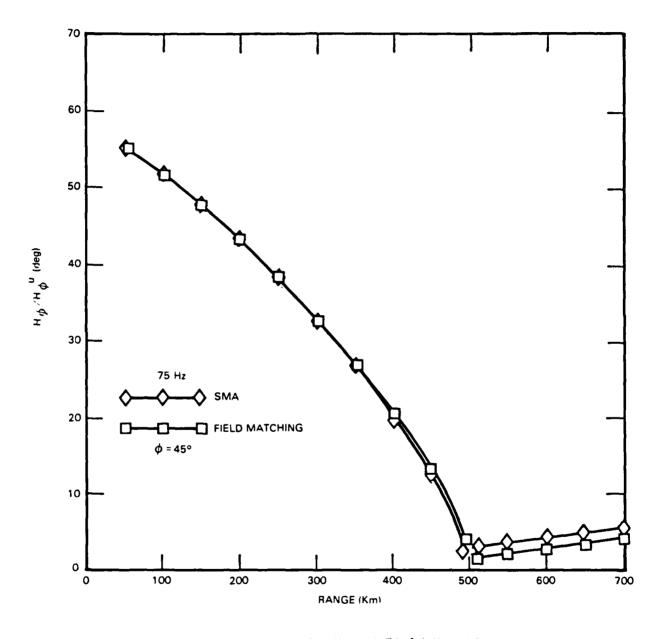


Figure 33. Comparison of SMA and Field Matching phases for  ${\rm H}_{\phi}$ 



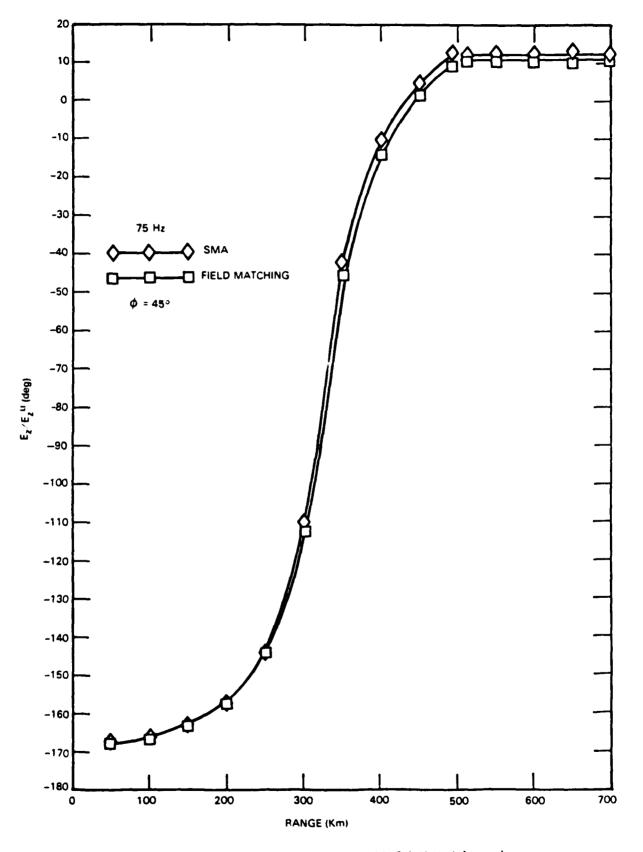


Figure 34. Comparison of SMA and Field Matching phases

for Ez.

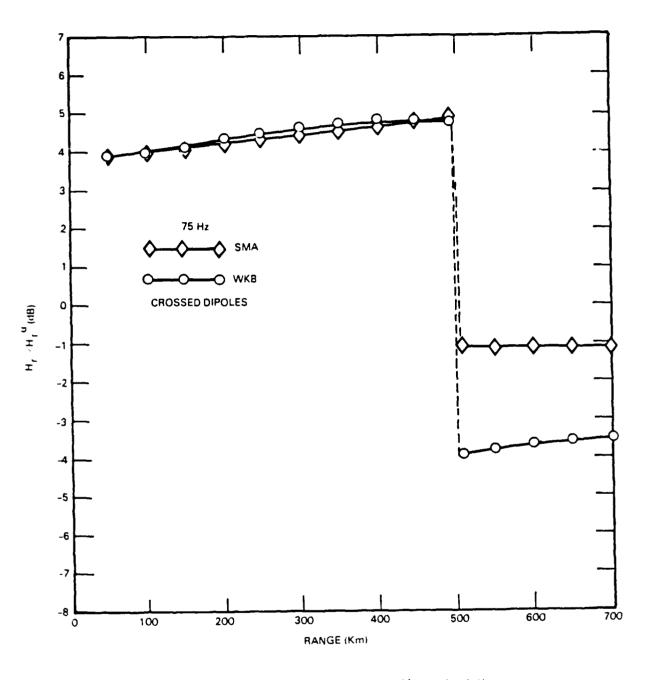


Figure 35. Ratio of disturbed to undisturbed  $H_r$  in dB vs. range.

## DISTRIBUTION LIST

DEPARTMENT OF DEFENSE DEPUTY UNDER SECRETARY OF DEFENSE CMD, CONT, COMM & INTELL DEPARTMENT OF DEFENSE WASHINGTON, DC 20301

DIRECTOR COMMAND CONTROL TECHNICAL CENTER 11440 ISAAC NEWTON SQUARE, N RESTON, VA 22091 C-650

DIRECTOR COMMAND CONTROL TECHNICAL CENTER ROOM ME682, THE PENTAGON WASHINGTON, DC 20301 C-312

DIRECTOR DEFENSE ADVANCED RESEARCH PROJECT AGENCY 1440 WILSON BLVD ARLINGTON, VA 22209 NUCLEAR MONITORING RSCH STRATEGIC TECH OFFICE

DEFENSE COMMUNICATION ENGINEERING CENTER 1860 WIEHLE AVENUE RESTON, VA 22090 CODE R220 (M HOROWITZ) CODE R410 CODE R103

DIRECTOR DEFENSE COMMUNICATIONS AGENCY WASHINGTON, DC 20305 CODE 810 CODE 480 CODE 101B

DEFENSE COMMUNICATIONS AGENCY WWMCCS SYSTEM ENGINEERING ORG WASHINGTON, DC 20305 RL CRAWFORD

DEFENSE TECHNICAL INFORMATION CENTER CAMERON STATION ALEXANDRIA, VA 22314

DIRECTOR DEFENSE INTELLIGENCE AGENCY WASHINGTON, DC 20301 DIAST-5 DB4C (EDWARD O'FARRELL)

DIRECTOR DEFENSE NUCLEAR AGENCY WASHINGTON, DC 20305 DDST TITL TECH LIBRARY RAAE STVL DIRECTOR JOINT STRAT TGT PLANNING STAFF JCS OFFUTT AFB OMAHA, NB 68113 JPST COMMANDER FIELD COMMAND DEFENSE NUCLEAR AGENCY KIRKTLAND AFB, NM 87115 FCPR DIRECTOR INTERSERVICE NUCLEAR WEAPONS SCHOOL KIRTLAND AFB, NM 87115 DOCUMENT CONTROL CHIEF LIVERMORE DIVISION FLD COMMAND DNA LAWRENCE LIVERMORE LABORATORY PO BOX 808 LIVERMORE, CA 94550 FCPRL DIRECTOR NATIONAL SECURITY AGENCY FT GEORGE G MEADE, MD 20755 W65 OLIVER H BARTLETT W32 TECHNICAL LIBRARY JOHN SKILLMAN R52 OJCS/J-3 THE PENTAGON WASHINGTON, DC 20301 OPERATIONS (WWMCCS EVAL OFF, MR TOMA) OJCS/J-5 THE PENTAGON WASHINGTON, DC 20301 PLANS & POLICY (NUCLEAR DIVISION) UNDER SECRY OF DEFENSE FOR RESEARCH AND ENGINEERING DEPARTMENT OF DEFENSE WASHINGTON, DC 20301 S&SS (OS) AGE

DEPARTMENT OF THE ARMY COMMANDER/DIRECTOR ATMOSPHERIC SCIENCES LABORATORY US ARMY ELECTRONICS COMMAND WHITE SANDS MISSILE RANGE, NM 88002 DELAS-AE-M (FE NILES)

COMMANDER HARRY DIAMOND LABORATORIES 2800 POWDER MILL RD ADELPHI, MD 20783 DELHD-NP (FN WIMENITZ) MILDRED H WEINER DRXDO-II

COMMANDER US ARMY FOREIGN SCIENCE & TECH CENTER 220 7TH STREET, NE CHARLOTTESVILLE, VA 22901 R JONES PA CROWLEY

COMMANDER US ARMY NUCLEAR AGENCY 7500 BACKLICK ROAD BUILDING 2073 SPRINGFIELD, VA 22150 MONA-WE (J BERBERET)

CHIEF US ARMY RESEARCH OFFICE PO BOX 12211 TRIANGEL PARK, NC 27709 DRXRD-ZC

DEPARTMENT OF THE NAVY CHIEF OF NAVAL OPERATIONS NAVY DEPARTMENT WASHINGTON, DC 20350 OP 941 OP 604C3 OP 943 OP 981

CHIEF OF NAVAL RESEARCH NAVY DEPARTMENT ARLINGTON, VA 22217 CODE 402 CODE 420 CODE 421 CODE 461 CODE 464

COMMANDING OFFICER NAVAL INTELLIGENCE SUPPORT CENTER 4301 SUITLAND RD BLDG 5 WASHINGTON, DC 20390 OFFICER-IN-CHARGE WHITE OAK LABORATORY NAVAL SURFACE WEAPONS CENTER SILVER SPRING, MD 20910 CODE WA501 NAVY NUC PRGMS OFF CODE WX21 TECH LIBRARY

COMMANDER NAVAL TELECOMMUNICATIONS COMMAND NAVTELCOM HEADQUARTERS 4401 MASSACHUSETTS AVE, NW WASHINGTON, DC 20390 CODE 24C

COMMANDING OFFICER NAVY UNDERWATER SOUND LABORATORY FORT TRUMBULL NEW LONDON, CT 06320 PETER BANNISTER DA MILLER

DIRECTOR STRATEGIC SYSTEMS PROJECT OFFICE NAVY DEPARTMENT WASHINGTON, DC 20376 N141

DEPARTMENT OF THE AIR FORCE COMMANDER ADC/DC

ENT AFB, CO 80912 DC (MR LONG)

COMMANDER ADCOM/XPD ENT AFB, CO 80912 XPQDQ XP

AF GEOPHYSICS LABORATORY, AFSC HASCOM AFB, MA 01731 CRU (S HOROWITZ)

AF WEAPONS LABORATORY, AFSC KIRTLAND AFB, NM 87117 SUL (2) DYC

COMMANDER ROME AIR DEVELOPMENT CENTER, AFSC GRIFFISS AFB, NY 13440 EMTLD DOC LIBRARY

COMMANDER ROME AIR DEVELOPMENT CENTER, AFSC HANSCOM AFB, MA 01731 EEP JOHN RASMUSSEN

والمحالية والمحالية

COMMANDER IN CHIEF STRATEGIC AIR COMMAND OFFUTT AFB, NB 68113 NRT XPFS

LAWRENCE LIVERMORE NATIONAL LABORATORY PO BOX 808 LIVERMORE, CA 94550 TECH INFO DEPT L-3

LOS ALAMOS NATIONAL SCIENTIFIC LABORATORY PO BOX 1663 LOS ALAMOS, NM 87545 DOC CON FOR TF TASCHEK DOC CON FOR D R WESTERVELT DOC CON FOR PW KEATON

SANDIA LABORATORY LIVERMORE NATIONAL LABORATORY PO BOX 969 LIVERMORE, CA 94550 DOC CON FOR BE MURPHEY DOC CON FOR TB COOK ORG 8000

SANDIA NATIONAL LABORATORY PO BOX 5800 A'.BUQUERQUE, NM 87115 DOC CON FOR SPACE PROJ DIV DOC CON FOR AD THORNBROUGH DOC CON FOR 3141 SANDIA RPT COLL

OTHER GOVERNMENT DEPARTMENT OF COMMERCE NATIONAL BUREAU OF STANDARDS WASHINGTON, DC 20234 RAYMOND T MOORE

DEPARTMENT OF COMMERCE OFFICE OF TELECOMMUNICATIONS INSTITUTE FOR TELECOM SCIENCE BOULDER, CO 80302 WILLIAM F UTLAUT LA BERRY A GLENN JEAN

DEPARTMENT OF DEFENSE CONTRACTORS AEROSPACE CORPORATION PO BOX 92957 LOS ANGELES, CA 90009 IRVING M GARFUNKEL

ANALYTICAL SYSTEMS ENGINEERING CORP 5 OLD CONCORD RD BURLINGTON, MA 01803 RADIO SCIENCES THE BOEING COMPANY PO BOX 3707 SEATTLE, WA 98124 GLENN A HALL JF KENNEY

ESL, INC 495 JAVA DRIVE SUNNYVALE, CA 94086 JAMES MARSHALL

GENERAL ELECTRIC COMPANY SPACE DIVISION VALLEY FORGE SPACE CENTER GODDARD BLVD KING OF PRUSSIA PO BOX 8555 PHILADELPHIA, PA 19101 SPACE SCIENCE LAB (MH BORTNER)

KAMAN TEMPO 816 STATE STREET PO DRAWER QQ SANTA BARBARA, CA 93102 B GAMBILL DASIAC WARREN S KNAPP

GTE SYLVANIA, INC ELECTRONICS SYSTEMS GRP EASTERN DIVISION 77 A STREET NEEDHAM, MA 02194 MARSHAL CROSS

ITT RESEARCH INSTITUTE 10 WEST 35TH STREET CHICAGO, IL 60616 TECHNICAL LIBRARY

UNIVERSITY OF ILLINOIS DEPARTMENT OF ELECTRICAL ENGINEERING URBANA, IL 61803 AERONOMY LABORATORY

JOHNS HOPKINS UNIVERSITY APPLIED PHYSICS LABORATORY JOHNS HOPKINS ROAD LAUREL, MD 20810 J NEWLAND PT KOMISKE

LOCKHEED MISSILE & SPACE CO, INC. 3251 HANOVER STREET PALO ALTO, CA 94304 EE GAINES WL IMHOF D/52-12 JB REAGAN D652-12 RG JOHNSON D/52-12

MASSACHUSETTS INSTITUTE OF TECHNOLOGY LINCOLN LABORATORY PO BOX 73 LEXINGTON, MA 02173 DM TOWLE

MISSION RESEARCH CORPORATION 735 STATE STREET SANTA BARBARA, CA 93101 R HENDRICK F FAJEN

MITRE CORPORATION PO BOX 209 BEDFORD, MA 01730 G HARDING

PACIFIC-SIERRA RESEARCH CORP 1456 CLOVERFIELD BLVD SANTA MONICA, CA 90404 EC FIELD, JR

PENNSYLVANIA STATE UNIVERSITY IONOSPHERIC RESEARCH LABORATORY 318 ELECTRICAL ENGINEERING EAST UNIVERSITY PARK, PA 16802 IONOSPHERIC RSCH LAB

R&D ASSOCIATES PO BOX 9695 MARINA DEL REY, CA 90291 FORREST GILMORE WILLIAM J KARZAS PHYLLIS GREIFINGER CARL GREIFINGER HA ORY BRYAN GABBARD RP TURCO SAUL ALTSCHULER RAND CORPORATION 1700 MAIN STREET SANTA MONICA, CA 90406 TECHNICAL LIBRARY CULLEN CRAIN

SRI INTERNATIONAL 333 RAVENSWOOD AVENUE MENLO PARK, CA 94025 DONALD NEILSON GEORGE CARPENTER WG CHETNUT JR PETERSON GARY PRICE

STANFORD UNIVERSITY RADIO SCIENCE LABORATORY STANFORD, CA 94305 RA HELLIWELL FRASER SMITH J KATSURFRAKIS

CALIFORNIA INSTITUTE OF TECHNOLOGY JET PROPULSION LABORATORY 4800 OAK GROVE DRIVE PASADENA, CA 91103 ERNEST K SMITH

.....

## END

## FILMED

11-85

DTIC