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# Recombination and Ionization in a Nitrogen Plasma

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19 ABSTRACT (Continue on reverse if necessary and identify by block number) A collisional-radiative model for a nitrogen plasma ( $N$ , $N^+$ and $N^{++}$ ) has been developed. The results for an optically thin, and optically thick in uv lines, are presented. The approach taken in the model is to solve a time dependent set of rate equations for a large number of excited states of $N$ and $N^+$ for a wide range of $T_e$ and $N_e$ . The excited states of interest emit radiation in the ultraviolet, visible and infrared which could be used for air plasma channel diagnostics. The model delineates the regimes in $T_e$ and $N_e$ where the excited states are in LTE and when they deviate from LTE, and is developed as a building block for an extensive radiative transfer model for air.			
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## RECOMBINATION AND IONIZATION IN A NITROGEN PLASMA

### I. INTRODUCTION

When air is heated and is highly ionized, nitrogen and its ions become relatively abundant for electron temperatures of 1-3 e.v. Emissions from such air provide diagnostic information and play a role in cooling the heated channel. To describe such a channel one must therefore perform a radiative transfer calculation which requires a detailed knowledge of the air species including excited states. To provide this information, we develop as a first step, a collisional-radiative model for nitrogen and its ion.

It is well known that a recombining plasma is a source of radiation. The character of this radiation, line versus continuum emission and absorption or uv versus visible and infrared radiation, depends on detailed aspects of the plasma. In addition to species type important properties include electron density, electron temperature, and optical character (thin, thick, or optically thick in select spectral regions). To quantitatively describe the spectral character of radiation emitted from a plasma these properties must be incorporated in a model which accurately monitors the evolution of the plasma, determines the extent to which the plasma is or is not in equilibrium, and accounts for the radiative transfer accordingly. For example, in the simplest case of a plasma in local

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thermodynamic equilibrium (LTE) the radiative transfer equation may be solved assuming Planck's function correctly represents the source radiation [1]. A more complete description, however, requires coupling the radiative transfer equations to the rate equations which provide the population densities of all bound and continuum states involved in the radiative and collisional processes of the specific plasma. The work presented in this paper is the initial step in constructing such a model.

A collisional-radiative model developed by Bates et. al. [2] has provided the framework for studies which give the excited state populations and their deviation from LTE for hydrogen and hydrogenic ions. Their theory is statistical in nature and treats the problem in a simple and tractable way. Effective collisional-radiative recombination and ionization coefficients are defined and determined from a knowledge of the rate coefficients for collisional excitation and ionization and the spontaneous transition probabilities, for the case of an optically thin plasma. The influence of self-absorption is then demonstrated for the special cases of a hydrogen plasma optically thick for various optical transitions. Their approach is to solve a coupled set of rate equations for the steady state values of excited state densities at fixed electron densities and temperatures, thereby showing the extent to which the excited state populations deviate from Saha equilibrium.



The work of Bates et. al. has motivated others to study the effects of collisional and radiative processes in plasmas. Drawin [3] has used more recent cross section information and recalculated the collisional-radiative recombination and ionization coefficients for hydrogen and hydrogenic plasmas analogous to Bates et. al., but within the context of a more general formalism. Park [4] has used the method of Bates to compute spectral line intensities for specific non-equilibrium conditions in a collision-dominant nitrogen plasma. Kulander [5] has also studied the spectral properties of radiation emitted from a non-equilibrium nitrogen plasma as well as the deviation from Saha equilibrium of the excited and ionized states of an optically thin plasma.

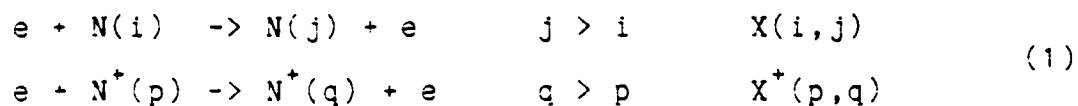
In the present work the focus is on an optically thin nitrogen plasma, however, unlike Bates and others we solve the time-dependent coupled rate equations explicitly, in a manner similar to the approach taken by Ali & Jones [6] to study recombination lasers in hydrogen and hydrogen like plasmas. The calculations are for a given electron temperature, but allow the electron density to evolve in time. As expected the population densities show an early transient behavior followed by a steady state, from which we calculate effective collisional-radiative recombination and ionization coefficients and compare the final state populations to those expected if Saha equilibrium conditions were satisfied. Our rate equations include the most

satisfied. Our rate equations include the most recent ionization, excitation, and recombination rate coefficients available, some of which are similar to those used by Drawin [3] and Bates [2], and some are based on experimental data. Finally, we consider the case of a nitrogen plasma optically thick in specific uv bound-bound spectral lines.

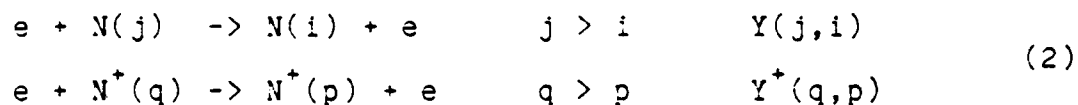
## II. COLLISIONAL AND RADIATIVE PROCESSES

The coupled rate equations which describe the evolution of the nitrogen plasma include the following collisional and radiative processes:

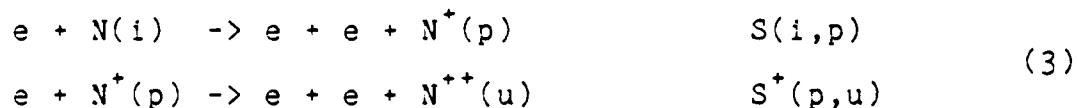
1. Collisional excitation - excitation of an upper electronic state by collisions of electrons with atoms (ions) in a lower state.



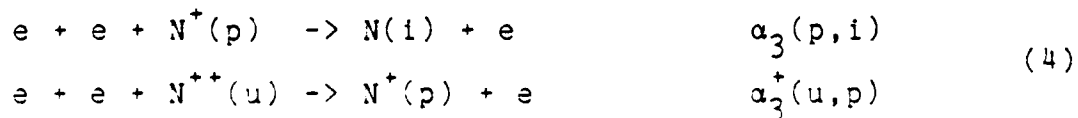
2. Collisional de-excitation - the inverse of 1.



3. Collisional ionization - ionization of atoms and ions



4. Three body recombination - the inverse of 3.



5. Radiative recombination.



6. Spontaneous emission.

$$\begin{array}{llll} N(j) \rightarrow N(i) + h\nu & j > i & A(j,i) & \\ N^+(q) \rightarrow N^+(p) + h\nu & q > p & A^+(q,p) & \end{array} \quad (6)$$

Since we are initially assuming a nitrogen plasma that is optically thin for all spectral regions photo-ionization and absorption have been excluded. These processes are accounted for most easily by describing photo-ionization as negative radiative recombination and absorption as negative spontaneous emission as was done by Drawin [3], and will be included in detail in a subsequent report.

### III. RATE EQUATIONS AND RATE COEFFICIENTS

#### A. Coupled rate equations

Let  $N^{z-1}(m)$  denote the population density of the  $(z-1)$ -th ion (or neutral if  $z=1$ ) in the electronic state whose index is  $m$ , where it is understood that the density depends on time. The rate equation describing the evolution of this state subject to the collisional and radiative processes outlined in the previous section is given by

$$\begin{aligned}
 \frac{dN}{dt} N^{z-1}(m) = & Ne \left[ \sum_{\ell \leq m-1} N^{z-1}(\ell) X^{z-1}(\ell, m) - N^{z-1}(m) \sum_{\ell \leq m-1} Y^{z-1}(m, \ell) \right] \\
 & + Ne \left[ \sum_{n \geq m-1} N^{z-1}(n) Y^{z-1}(n, m) - N^{z-1}(m) \sum_{n \geq m-1} X^{z-1}(m, n) \right] \\
 & + Ne \left[ Ne \sum_n N^z(n) \alpha_3^{z-1}(n, m) + \sum_n N^z(n) \alpha_R^{z-1}(n, m) \right] \\
 & - Ne N^{z-1}(m) \sum_n S^{z-1}(m, n) \tag{7} \\
 & - Ne \left[ Ne N^{z-1}(m) \sum_{\ell} \alpha_3^{z-2}(m, \ell) + N^{z-1}(m) \sum_{\ell} \alpha_R^{z-2}(m, \ell) \right] \\
 & + Ne \sum_{\ell} N^{z-2}(\ell) S^{z-2}(\ell, m) \\
 & + \sum_{n \geq m+1} N^{z-1}(n) A^{z-1}(n, m) - N^{z-1}(m) \sum_{\ell \leq m-1} N^{z-1}(\ell) A^{z-1}(\ell, m)
 \end{aligned}$$

where  $N_e$  is the electron density. The time history of all species is obtained by solving the set of equations constructed from equation (7) for all ions and neutrals in all states, whose indices are  $n$ ,  $l$ , and  $m$ .

### B. Energy Level Model

We have chosen to study the nitrogen plasma for electron temperatures in the range of 1.0 e.v. to 3.0 e.v.. In this temperature range the important radiation is produced by constituents which are atomic or ionic. In our calculation we have included the lowest thirteen (13) levels for N I, the lowest seventeen levels for N II, and two effective levels for N III. Details are presented in Tables I through III; this information can be found in Weise [7]. We note that this model includes as a subset the levels for N I and N II used in Kulander's studies [5], as well as most of the N III levels. While not as comprehensive in describing N I as Park [4], we account for N II and N III which he fails to do, since his interest is in a region of lower electron densities and higher temperatures.

Within this model the important bound-bound radiative transitions are listed in Table IV; each transition is described by its wavelength, the number given by Weise [7], spectral character, transition index ( for example,  $7+ - 1+$  denotes emission from the seventh to the first level in the ion N II ), and transition energy. This table shows, for instance, that the

visible radiation comes largely from transitions in the ion N II. Therefore, one would expect this radiation to be important once electron temperatures become sufficiently high that these upper levels of N II are accessed.

The important free-bound radiative transitions are listed in Table V. These include all transitions for the corresponding ions considered by Kulander [5b]. While there is a large amount of uv radiation the radiative recombination from  $N^+ \rightarrow N(i)$  where  $i \geq 7$  is a source of visible emission. This becomes the predominant source of visible radiation at lower electron densities and temperatures; such that the abundance of N II that is created resides in the ground state.

### C. Rate Coefficients

The rate coefficients for the collision and radiation processes outlined in section II. and used in the rate equations, i.e. equations (7) were obtained from several sources.

1. Transitions amongst the levels of the ground state configurations of nitrogen ( $^4S, ^2D, ^2P$ ) and nitrogen ion ( $^3P, ^1D, ^1S$ ) are optically forbidden. Electron impact excitation coefficients for the transitions in N I were obtained from reference [8]. Transitions among the metastable states in N II were accounted for using the analytic

expressions for the de-excitation rate coefficients given in reference [3]. The reverse rate coefficients were obtained from detailed balance.

2. Collisional excitation rates of transitions which are optically allowed, see Table IV, are obtained using the following simple formula [9]:

$$X(m,n) = \frac{4.3 \times 10^{-6} f(n,m) \exp \{-E(n,m)/T_e\}}{E(n,m) T_e^{1/2}} \Psi(n,m) \quad (8)$$

where  $E(n,m) = E(n) - E(m)$ ,  $m < n$ ,  $f(n,m)$  is the oscillator strength, and

$$\Psi(n,m) = 0.2 \text{ for ions} \quad (9)$$

$$\Psi(n,m) = \left(1.0 + \frac{E(n,m)}{T_e}\right)^{-1} \left\{ \left(20.0 + \frac{E(n,m)}{T_e}\right)^{-1} + \ln[1.25(1.0 + T_e/E(n,m))] \right\}$$

for neutrals

The de-excitation rates are calculated from detailed balance.

3. Collisional ionization from a specific level  $m$  to the appropriate level,  $n$ , of the next highest ion was obtained using the formula of Drawin [3],

$$S^{Z-1}(m,n) = 2.38 \times 10^{-8} \frac{E_H^2}{\Delta E} \frac{f(m)\xi(m)}{(T_e)^{1/2}} \Psi\left(\frac{\Delta E}{T_e}, 1\right) \quad (10)$$



where  $E_H$  is 13.59 e.v.,  $\xi(m)$  the number of equivalent electrons,  $\Delta E = E^Z(n) - E^{Z-1}(m)$ ,  $f(m)$  the oscillator strength, and  $z = 1$  for neutrals and  $> 1$  for ions.  $\Psi$  is given by

$$\Psi \left( \frac{\Delta E}{T_e}, 1 \right) = \int_{\Delta E/T_e}^{\infty} dx \left[ \frac{1 - \Delta E}{T_e} \right] \exp(-x) \ln \left[ \frac{1.253x}{\Delta E/T_e} \right] \quad (11)$$

where  $\beta = 1 + [(z-1)/(z+2)]$ . The oscillator strength was chosen so that rate coefficients given by equation (11) matched closely the ionization data in Table VIII of reference [10] which is based on experimental cross sections for the ionization of nitrogen; our choice was  $f(m) = 0.2$ . The rate coefficient for three-body recombination, obtained from detailed balance, is

$$\alpha_3^{z-1}(n,m) = 1.66 \times 10^{-22} \frac{g^{z-1}(m)}{g^z(n)} \frac{S^{z-1}(m,n)}{T_e^{3/2}} \exp \left( \frac{\Delta E}{T_e} \right) \quad (12)$$

where  $g^{z-1}(m)$  is the statistical weight of state  $m$  and  $g^z(n)$  is the weight of the ionic state.

4. The rate coefficients for radiative recombination were obtained using the approximate formula of Bates [2], e.g.

$$\alpha_R^{z-1}(p,i) = 5.2 \times 10^{-14} \exp \left( \frac{\Delta E}{T_e} \right) \left( \frac{\Delta E}{T_e} \right)^{3/2} E_1 \left( \frac{\Delta E}{T_e} \right) \quad (13)$$

Here  $E_1$  is the exponential integral

$$E_1 \left( \frac{\Delta E}{T_e} \right) = \int_1^{\infty} \frac{dx}{x} \exp \left( -\frac{\Delta E}{T_e} x \right) \quad (14)$$

For example, eq.(13) gives the rate coefficient for recombination of level  $p$  of  $N$  II to level  $i$  of  $N$  I, see II. 5., if  $z = 1$ .

5. Finally, the Einstein A coefficients for spontaneous emission were taken from Weise [7].

### D. Ionization Potential Reduction

The ionization energy of an isolated atom or ion is different from one immersed in a plasma [11] and must be corrected accordingly. The net ionization potential reduction is due to energy released upon placing an electron-ion pair in a plasma; one of the consequences is that electrons occupying states which in an isolated atom would be bound now become unbound should the corrected ionization potential be less than the energy of the state. Our rate equations have been modified to account for this high electron density (low electron temperature) phenomenon.

At each step in the numerical integration of the rate equations, eqs. (7), the electron density and temperature are noted and the ionization potential reduction,  $\Delta E_{\infty}^{z-1}$ , calculated according to

$$\Delta E_{\infty}^{z-1} = 1.93 \times 10^{-10} z \left( \frac{N_e}{T_e} \right)^{1/2} \quad (15)$$

where  $\Delta E_{\infty}^{z-1}$ , and  $T_e$  are in e.v. and  $N_e$  has units  $\#/cm^3$ . Reducing the ionization potential an amount determined by eq. (15) has the effect of modifying the collisional ionization rate coefficient, eq. (10), as follows:

$$S_c^{z-1}(m,n) = S^{z-1}(m,n) \times \exp\{\Delta E_{\infty}^{z-1}/T_e\} \quad (16)$$

For example, in the extreme case of low temperature,  $T_e = 1.0$  e.v., and high electron density,  $N_e = 10^{19}/cm^3$ , the ionization rate increases by 84% so its effect can be substantial.

## IV. NUMERICAL RESULTS

### A. Time-Dependent Population Densities

Figures (1)- (10) show representative results obtained by integrating equations (7). Numerical integration was accomplished by using CHEMEQ, a routine specifically designed to solve stiff ordinary differential equations [12]. The initial conditions for this set of figures are  $T_e = 2.0$  e.v.,  $N(1) = 4.0 \times 10^{13}/\text{cm}^3$ ,  $N_e = N^+(1) = 1.0 \times 10^{17}/\text{cm}^3$  (i.e. charge neutrality), with all other population densities being set equal to zero (actually  $1 \times 10^4/\text{cm}^3$ ). The general behavior of the time-dependent solutions is as expected - an early transient behavior followed by rapid relaxation to a steady state. The relaxation time is on the order of 15 - 22 nsec. Such rapid relaxation led Bates et. al. [2] to solve for the excited state population densities using a steady state approximation.

In Figure (1) the total population densities of the electrons, neutrals, and ions are presented. At  $T_e = 2.0$  e.v. the number of  $N^{++}$  ions is negligible, i.e. approximately three orders of magnitude less than the neutrals. Consequently, the total number of electrons nearly equals the total number of  $N^+$  ions which, in the steady state, exceeds the population of neutrals by a factor of three.

Examination of Figures (2) - (4) shows that most of the nitrogen population resides in the ground state and the metastable states, particularly the  $2D^0$  state. The levels which contribute to the emission of bound-bound uv radiation, N(4-6,13), are approximately equal in population to those which contribute to the emission of bound-bound ir radiation, N(8-12).

As in the case of N the ground and metastable states of  $N^+$  are the more heavily populated, see Figures (5) - (7). Unlike N only  $N^+(4)$  and  $N^+(5)$ , i.e. the first two excited states which emit bound-bound uv, are highly populated because of the low electron temperature. The rest of the uv and visible emitting levels are two orders of magnitude less than the N radiating levels. The population of the lower  $N^+$  levels is important for the emission of radiation resulting from radiative recombination, free-bound.

Figure (8) shows that the  $N^{++}$  ions that are created reside, as expected, predominately in the ground state.

While a direct comparison cannot be made with the results of Kulander [5a] our steady state populations are in qualitative agreement. The relative population of the major equilibrium species for  $N_e = 10^{16}/\text{cm}^3$  to  $10^{19}/\text{cm}^3$  and  $T_e = 1.0$  e.v. to 2.0 e.v. follows the trend obtained by Kulander. At  $T_e = 1.0$  e.v. N(1) is the major species for  $N_e = 10^{16}/\text{cm}^3$  to  $10^{19}/\text{cm}^3$  while at  $T_e = 2.0$  e.v.  $N^+(1)$  predominates. At  $T_e = 1.5$  e.v.

$N^+(1)$  is the major species at lower electron densities ( $10^{16}/\text{cm}^3 - 10^{18}/\text{cm}^3$ ) while  $N(1)$  is at higher density ( $10^{19}/\text{cm}^3$ ). Kulander also presents results on the distribution of population amongst species versus electron concentration. Again our results are in general agreement. Detailed aspects of our population distribution are discussed in section IV. C..

### B. Collisional-Radiative Recombination-Ionization Coefficients

Bates et. al. [2] have defined effective recombination and ionization coefficients which account for the net effect of collisional ionization, three-body recombination, and radiative recombination in a very simple way. These coefficients have been tabulated exclusively for hydrogen and hydrogenic ion plasmas, [2] and [3]. In this section we define the effective coefficients analogous to Bates et. al. and present results for our optically thin nitrogen plasma as well as the case where all bound-bound uv lines are assumed to be optically thick.

Denoting  $\alpha_{\text{CR}}^{\circ}$  and  $\alpha_{\text{CR}}^{+}$  as the effective recombination coefficients for  $N^+ \rightarrow N$  and  $N^{++} \rightarrow N^+$  and  $S_{\text{CR}}^{\circ}$  and  $S_{\text{CR}}^{+}$  as the effective ionization coefficients for the reverse processes the rate equations for  $N$ ,  $N^+$ ,  $N^{++}$ , and  $N_e$  may be written

$$\frac{dN}{dt} = N_e N^+ \alpha_{\text{CR}}^{\circ} - N_e N S_{\text{CR}}^{\circ}$$

$$\begin{aligned}
\frac{dN^+}{dt} &= -Ne N^+ \alpha_{CR}^0 + Ne N S_{CR}^0 + Ne N^{++} \alpha_{CR}^+ - Ne N^+ S_{CR}^+ \\
\frac{dN^{++}}{dt} &= Ne N^+ S_{CR}^+ - Ne N^{++} \alpha_{CR}^+ \\
\frac{dNe}{dt} &= Ne N S_{CR}^0 + Ne N^+ S_{CR}^+ - Ne N^+ \alpha_{CR}^0 - Ne N^{++} \alpha_{CR}^+
\end{aligned}
\tag{17}$$

Therefore, in terms of the detailed rate coefficients outlined in section II,  $\alpha_{CR}^0$ ,  $\alpha_{CR}^+$ ,  $S_{CR}^0$ , and  $S_{CR}^+$  are given by

$$\begin{aligned}
\alpha_{CR}^0 &= \{Ne \sum_{p,i} \alpha_3(p,i) N^+(p) + \sum_{p,i} \alpha_R(p,i) N^+(p)\} / N^+ \\
\alpha_{CR}^+ &= \{Ne \sum_{p,u} \alpha_3^+(u,p) N^{++}(u) + \sum_{p,i} \alpha_R^+(u,p) N^{++}(u)\} / N^{++} \\
S_{CR}^0 &= \{ \sum_{i,p} N(i) S(i,p) \} / N \\
S_{CR}^+ &= \{ \sum_{p,u} N^+(p) S^+(p,u) \} / N^+
\end{aligned}
\tag{18}$$

A quick check shows that these definitions satisfy the conditions for particle and charge conservation.

The coefficients defined in equations (17) and (18) are time-dependent, due to the time dependence of the contributing population densities; see Figs. (9) - (10). The steady state values are presented in Tables VI - IX as a function of the final electron density and electron temperature ( $T_e$  was fixed throughout the integration). Close examination of these results reveals the following: At high electron densities the effective recombination coefficient is linearly proportional to  $Ne$ . This is due to the dominance of three-body recombination over radiative (two-body) recombination in this regime,  $Ne \geq 10^{13}$  -

$10^{19}/\text{cm}^3$ . For lower electron densities the opposite is true and the effective coefficient approaches the two-body value. The collisional-radiative ionization coefficients show a rapid rise for low electron densities ( $N_e \leq 10^{16} - 10^{17}/\text{cm}^3$ ) and a much slower rise for higher densities ( $N_e \geq 10^{18}/\text{cm}^3$ ). This is in contrast to the behavior of the coefficients of Drawin and Bates which show a saturation at high  $N_e$ . The density dependence in  $S_{\text{CR}}^{\circ}$  and  $S_{\text{CR}}^{+}$  at high  $N_e$  in our calculation comes from the correction discussed in section III. D.. The level-specific collisional ionization coefficients depend on  $N_e$  and  $T_e$  in the manner of eq. (16); this carries through to the definition of  $S_{\text{CR}}^{\circ}$  and  $S_{\text{CR}}^{+}$  in eq. (18). Neither Drawin nor Bates included this correction.

The collisional-radiative coefficients in Tables VI and VIII can be loosely compared to the results of Bates et. al. [2] and Drawin [3]. While there is no a priori expectation that the results should be in strict agreement, to the extent that a nitrogen plasma differs from a hydrogenic plasma, many of the rate coefficients were obtained using similar (hydrogenic) expressions. However, it must be pointed out that the results of Bates et. al. and Drawin are not, themselves, in agreement. Specifically, the recombination coefficients of Bates et. al. exceed those of Drawin by up to a factor of four while the ionization coefficients are greater by an order of magnitude. At low electron densities,  $N_e \sim 10^{16}/\text{cm}^3$ , our recombination coefficients are generally a factor of one to four less than



those of Drawin and Bates et. al., depending on temperature. At higher Ne,  $\sim 10^{18}/\text{cm}^3$ , our recombination coefficients fall between their results. Our collisional-radiative ionization coefficients are in good agreement (factor of 1.0 - 2.0) with those of Drawin at low Ne,  $10^{16}/\text{cm}^3$  to  $10^{17}/\text{cm}^3$ . At higher Ne our coefficients exceed those of Drawin by up to a factor of ten. This difference is due primarily to the ionization potential reduction correction discussed above. As a reminder, the calculations of Bates and Drawin are for hydrogen where at higher electron densities the character of the ion does not change. In contrast, in nitrogen other stages of ionization arise.

In a subsequent report it will be shown that the absorption coefficient for our model nitrogen plasma is on the order of  $10^4/\text{cm}$  in the uv spectral regime. This corresponds to a mean free path of  $\sim 10^{-4}\text{cm}$ . In Tables X through XIII the collisional-radiative coefficients are presented for the case where all bound-bound uv lines are assumed to be completely reabsorbed. As expected, there is very little difference between the optically thin and optically thick recombination coefficients. For high electron densities,  $\geq 10^{18}/\text{cm}^3$ , where the plasma is collision-dominant (see the discussion in the next section), the ionization coefficients are comparable. However, for lower electron densities the optically thick ionization coefficients are much larger than the optically thin case, as great as a factor of ten.

### C. Saha Equilibrium

When collisional transition rates exceed the corresponding radiative transitions the plasma is said to be collision-dominated. It is then possible to specify the populations of the constituent species by using the Boltzmann-Saha equation at the local electron temperature [11]. The onset of Saha equilibrium depends on  $N_e$  and  $T_e$ ; for example, an optically thin nitrogen gas at  $T_e = 1.0$  e.v. becomes collision-dominant at  $N_e = 10^{13}/\text{cm}^3$  [5a].

One form of the Saha equation is, [11],

$$\frac{N_e N^Z(p)}{N^{Z-1}(i)} = \frac{2 g^Z(p)}{g^{Z-1}(i)} \left( \frac{mkT_e}{2\pi \hbar} \right)^{3/2} \exp\{-[E^Z(p) - E^{Z-1}(i)]/kT_e\} \quad (19)$$

We have used eq. (19), after correcting the exponential factor for the ionization potential reduction (see section III. D.), to compare the steady state population densities with those expected assuming a collision-dominant environment for a range of electron densities,  $N_e = [10^{16} - 10^{19}/\text{cm}^3]$ , and temperatures,  $T_e = [1.0 - 3.0$  e.v.]. The ratio of the level population to the Saha population may be defined as

$$\rho^{Z-1}(n) = N^{Z-1}(n)/N_s^{Z-1}(n) \quad (20)$$

where  $N_g^{Z-1}(n)$  is the solution to the corrected eq. (19). In Table XIV we present threshold values for Ne above which  $p^{Z-1}(n) = 1 \pm .15$  for the indicated levels, i.e. Saha equilibrium is achieved to within 15%. Column 1 requires this criteria to be satisfied for all N I and N II levels, column 2 restricts the criteria to excited states of N I (specifically,  $i = 7$  to 13), and column 3 to excited states of N II (i.e.  $p = 7$  to 17). The results show the following: First, for any given  $T_e$ , as the number of electrons increases equilibrium is achieved for excited N I states before excited N II states and, as expected, before the lower states. In addition to Ne the threshold values depend on  $T_e$ . As  $T_e$  increases more electrons are necessary to have a completely collision-dominant environment, i.e. complete LTE. For an optically thin nitrogen plasma a state of complete LTE exists if  $N_e \geq (2.2 - 5.0) \times 10^{18}/\text{cm}^3$  for  $T_e$  ranging from 1.0 to 3.0 e.v.. The criteria given by Griem [11] and others on the validity of LTE is that the electron deexcitation rate of the resonance line must exceed ten times the radiative decay, i.e. for the nitrogen atom one must have

$$Y(4,1) N_e \geq 10 A(4,1) \quad (21)$$

For  $T_e = 1.0$  e.v., Eq. (21) gives  $N_e \geq 2.3 \times 10^{18}/\text{cm}^3$  in our case. However, while radiative processes may be important to the lower levels the excited states of N I are still controlled by collisional processes for  $N_e \geq (5.7 - 2.1) \times 10^{17}/\text{cm}^3$  over the same temperature range. This quasi-stationary state exists for

electron densities four to twenty-five times less than is required for all states to be in LTE.

#### IV. CONCLUDING REMARKS

The recombination and ionization processes for an optically thin, homogeneous, charge neutral nitrogen plasma have been studied for electron densities between  $10^{16}/\text{cm}^3$  and  $10^{19}/\text{cm}^3$  and electron temperatures from 1.0 e.v. to 3.0 e.v.. Effective collisional-radiative recombination and ionization coefficients are calculated which describe the net recombination and ionization and may be used in sophisticated plasma chemistry simulation codes. The bound-bound and free-bound radiation has been characterized. It has been shown that for electron densities greater than  $\sim 10^{18}/\text{cm}^3$  a state of local thermodynamic equilibrium exists whereas excited states may be in equilibrium, collision-dominant, for electron densities as low as  $\sim 10^{17}/\text{cm}^3$ . This has implications for simplifying the description of radiative transfer in a plasma. For example, above  $N_e \sim 10^{18}/\text{cm}^3$  a transfer theory based on the assumption of LTE should be adequate while below  $N_e \sim 10^{17}/\text{cm}^3$  individual species must be considered in detail. In the intermediate regime hybrid theories should prove useful.

TABLE I  
Energy Levels for N I

Index	State	Configuration( $1s^2 2s^2$ )	Energy(e.v.)	Weight
1	$4S^0$	$2p^3$	0.0	4
2	$2D^0$	$2p^3$	2.38	10
3	$2P^0$	$2p^3$	3.58	6
4	$4P$	$2p^2(3P)3s$	10.33	12
5	$2P$	$2p^2(3P)3s$	10.69	6
6	$4P$	$2s2p^4$	10.93	12
7	$2S$	$2p^2(3P)3p$	11.60	2
8	$4D$	$2p^2(3P)3p$	11.76	20
9	$4P$	$2p^2(3P)3p$	11.85	12
10	$4S$	$2p^2(3P)3p$	12.00	4
11	$2D$	$2p^2(3P)3p$	12.01	10
12	$2P$	$2p^2(3P)3p$	12.13	6
13	$2D$	$2p^2(1D)3s$	12.36	10

TABLE II  
Energy Levels for N II

<u>Index</u>	<u>State</u>	<u>Configuration (<math>1s^2</math>)</u>	<u>Energy (e.v.)</u>	<u>Weight</u>
1	$3p$	$2s^2 2p^2$	0.01	9
2	$1D$	$2s^2 2p^2$	1.90	5
3	$1S$	$2s^2 2p^2$	4.05	1
4	$3D^0$	$2s 2p^3$	11.44	15
5	$3P^0$	$2s 2p^3$	13.54	9
6	$1D^0$	$2s 2p^3$	17.88	5
7	$3P^0$	$2s^2 2p(2p^0) 3s$	18.48	9
8	$1P^0$	$2s^2 2p(2p^0) 3s$	18.50	3
9	$3S^0$	$2s 2p^3$	19.24	3
10	$1P$	$2s^2 2p(2p^0) 3p$	20.41	3
11	$3D$	$2s^2 2p(2p^0) 3p$	20.66	15
12	$1P^0$	$2s 2p^3$	20.68	3
13	$3S$	$2s^2 2p(2p^0) 3p$	20.94	3
14	$3P$	$2s^2 2p(2p^0) 3p$	21.16	9
15	$1D$	$2s^2 2p(2p^0) 3p$	21.60	5
16	$1S$	$2s^2 2p(2p^0) 3p$	22.10	1
17	$3F^0$	$2s^2 2p(2p^0) 3d$	23.14	21

TABLE III  
Energy Levels for N III

<u>Index</u>	<u>State</u>	<u>Configuration (<math>1s^2</math>)</u>	<u>Energy (e.v.)</u>	<u>Weight</u>
1	$2P^0$	$2s^2 2p$	0.0	6
2	$4P^0$	$2s 2p^2$	7.1	12

TABLE IV  
Radiative Transitions (Bound - Bound)

<u>Wavelength(<math>\text{\AA}</math>)</u>	<u>#(Weise)</u>	<u>Spectrum</u>	<u>Index</u>	<u>Energy (e.v.)</u>
644.99	3	uv	9+ - 1+	19.23
660.28	5	uv	12+ - 2+	18.79
671.48	7	uv	7+ - 1+	18.48
745.84	6	uv	12+ - 3+	16.63
746.98	8	uv	8+ - 2+	16.60
775.96	4	uv	6+ - 2+	15.99
916.34	2	uv	5+ - 1+	13.54
1085.1	1	uv	4+ - 1+	11.43
1134.6	1	uv	4 - 1	10.93
1199.9	2	uv	6 - 1	10.34
1243.3	5	uv	13 - 2	9.98
1411.9	6	uv	13 - 3	8.79
1493.3	3	uv	5 - 2	8.31
1743.6	4	uv	5 - 3	7.12
3437.2	20	near uv	16+ - 8+	3.60
3995.0	19	vis	15+ - 8+	3.10
4623.2	17	vis	14+ - 7+	2.68
5028.8	16	vis	13+ - 7+	2.46
5679.4	15	vis	11+ - 7+	2.18
6482.1	18	vis	10+ - 8+	1.91
7452.2	23	vis	10 - 4	1.66
8211.8	22	ir	9 - 4	1.51
8617.5	25	ir	12 - 5	1.44
8691.6	21	ir	8 - 4	1.43
9395.3	24	ir	11 - 5	1.32
11602.0	7	ir	10 - 6	1.07

TABLE V  
Radiative Transitions (Free - Bound Thresholds)

<u>Wavelength(Å)</u>	<u>Spectrum</u>	<u>Index</u>	<u>Energy (e.v.)</u>
413.99	uv	1++ - 1+	29.59
447.58	uv	1++ - 2+	27.70
485.24	uv	1++ - 3+	25.55
490.82	uv	2++ - 4+	25.26
535.32	uv	2++ - 5+	23.16
658.77	uv	2++ - 6+	18.82
710.08	uv	2++ - 9+	17.46
773.91	uv	2++ - 12+	16.02
824.34	uv	4+ - 6	15.04
826.53	uv	3+ - 3	15.00
852.68	uv	1+ - 1	14.54
382.42	uv	2+ - 2	14.05
964.82	uv	2+ - 3	12.85
1019.57	uv	1+ - 2	12.16
1114.93	uv	1++ - 7+	11.15
1116.94	uv	1++ - 8+	11.10
1132.20	uv	1+ - 3	10.96
1349.08	uv	1++ - 10+	9.19
1386.80	uv	1++ - 11+	8.94
1431.64	uv	1++ - 13+	8.66
1468.96	uv	1++ - 14+	8.44
1549.75	uv	1++ - 15+	8.00
1653.07	uv	1++ - 16+	7.50
1919.20	uv	1++ - 17+	6.46
2944.89	uv	1+ - 4	4.21
3046.19	uv	2+ - 13	4.07
3220.26	uv	1+ - 5	3.85
4217.01	vis	1+ - 7	2.94
4459.71	vis	1+ - 8	2.78
4608.92	vis	1+ - 9	2.69
4881.10	vis	1+ - 10	2.54
4900.40	vis	1+ - 11	2.53
5144.40	vis	1+ - 12	2.41



TABLE VI  
 Collisional-Radiative Recombination Coefficients  
 Optically Thin (All Wavelengths)  
 Neutral

Te(e.v.)	1.0	1.5	2.0	2.5	3.0
Ne					
1.0E+16	2.5E-12	1.1E-12	8.4E-13	6.5E-13	4.6E-13
2.0	2.9	1.5	1.1E-12	8.2	5.4
3.0	3.3	1.8	1.3	1.0E-12	6.5
4.0	3.8	2.2	1.6	1.2	7.6
5.0	4.3	2.6	1.9	1.4	8.8
6.0	4.7	2.9	2.1	1.5	1.0E-12
7.0	5.2	3.3	2.4	1.7	1.1
8.0	5.6	3.7	2.6	1.9	1.2
9.0	6.1	4.0	2.9	2.0	1.3
1.0E+17	6.6	4.3	3.1	2.2	1.5
2.0	1.1E-11	7.4	5.6	3.9	2.6
3.0	1.7	1.1E-11	8.1	5.8	3.8
4.0	2.2	1.4	1.0E-11	7.5	5.0
5.0	2.7	1.7	1.3	9.4	6.3
6.0	3.2	2.0	1.5	1.1E-11	7.6
7.0	3.8	2.4	1.7	1.3	8.9
8.0	4.3	2.6	2.0	1.5	1.0E-11
9.0	4.8	3.0	2.2	1.7	1.1
1.0E+18	5.4	3.4	2.5	1.9	1.3
2.0	1.1E-10	6.8	4.8	3.8	2.7
3.0	1.6	1.0E-10	7.2	5.8	4.1
4.0	2.2	1.4	9.6	7.7	5.6
5.0	2.7	1.7	1.2E-10	9.6	7.0
6.0	3.3	2.1	1.5	1.1E-10	8.6
7.0	3.8	2.4	1.7	1.3	1.0E-10
8.0	4.4	2.8	2.0	1.5	1.2
9.0	4.9	3.2	2.2	1.7	1.3
1.0E+19	5.5	3.5	2.5	1.9	1.5

TABLE VII  
 Collisional-Radiative Recombination Coefficients  
 Optically Thin (All Wavelengths)

Te(e.v.) Ne	Ion				
	1.0	1.5	2.0	2.5	3.0
1.0E+15	3.6E-12	2.1E-12	1.7E-12	1.3E-12	9.7E-13
2.0	4.6	2.6	2.0	1.6	1.1E-12
3.0	5.3	3.1	2.4	1.8	1.3
4.0	5.9	3.6	2.8	2.1	1.4
5.0	6.4	4.1	3.1	2.3	1.6
6.0	6.9	4.6	3.5	2.5	1.7
7.0	7.4	5.0	3.8	2.8	1.9
8.0	8.0	5.5	4.2	3.0	2.0
9.0	8.5	6.0	4.5	3.2	2.2
1.0E+17	9.0	6.4	4.8	3.5	2.3
2.0	1.5E-11	1.0E-11	8.1	5.8	4.0
3.0	2.2	1.5	1.1E-11	8.1	5.8
4.0	2.9	1.9	1.5	1.1E-11	7.4
5.0	3.5	2.3	1.8	1.3	9.2
6.0	4.2	2.7	2.1	1.6	1.1E-11
7.0	4.9	3.2	2.4	1.9	1.3
8.0	5.5	3.6	2.8	2.1	1.5
9.0	6.2	4.0	3.1	2.4	1.7
1.0E+18	6.8	4.5	3.4	2.6	1.9
2.0	1.4E-10	8.9	6.4	5.2	3.9
3.0	2.1	1.3E-10	9.8	7.9	5.9
4.0	2.8	1.8	1.3E-10	1.1E-10	7.9
5.0	3.5	2.2	1.7	1.3	9.9
6.0	4.2	2.7	2.0	1.6	1.2E-10
7.0	4.9	3.1	2.3	1.8	1.4
8.0	5.5	3.6	2.7	2.1	1.6
9.0	6.2	4.0	3.0	2.3	1.8
1.0E+19	6.9	4.5	3.3	2.6	2.0

TABLE VIII

## Collisional-Radiative Recombination Coefficients

Optically Thin (All Wavelengths)

Neutral

Te(e.v.) Ne	1.0	1.5	2.0	2.5	3.0
1.0E+16	4.1E-14	4.0E-12	2.2E-11	2.2E-10	4.5E-10
2.0	5.4	5.8	7.0	2.8	6.0
3.0	6.4	7.6	8.8	3.5	7.4
4.0	7.2	9.2	1.0E-10	4.1	8.6
5.0	7.9	1.1E-11	1.2	4.6	9.8
6.0	8.6	1.2	1.3	5.1	1.1E-09
7.0	9.2	1.3	1.5	5.6	1.2
8.0	9.7	1.4	1.6	6.0	1.3
9.0	1.0E-13	1.5	1.7	6.4	1.4
1.0E+17	1.1	1.6	1.8	6.7	1.4
2.0	1.5	2.1	2.4	9.0	2.0
3.0	1.9	2.4	2.8	1.0E-09	2.3
4.0	2.1	2.7	3.0	1.1	2.5
5.0	2.3	2.9	3.2	1.2	2.7
6.0	2.5	3.1	3.3	1.3	2.9
7.0	2.6	3.2	3.4	1.3	3.0
8.0	2.7	3.3	3.5	1.4	3.1
9.0	2.8	3.4	3.6	1.4	3.1
1.0E+18	2.9	3.5	3.7	1.4	3.2
2.0	3.5	4.0	4.1	1.5	3.6
3.0	4.0	4.2	4.3	1.6	3.7
4.0	4.3	4.4	4.4	1.6	3.8
5.0	4.5	4.5	4.5	1.7	3.9
6.0	4.7	4.7	4.6	1.7	4.0
7.0	4.9	4.9	4.6	1.7	4.0
8.0	5.1	5.0	4.7	1.7	4.0
9.0	5.3	5.1	4.8	1.8	4.1
1.0E+19	5.5	5.2	4.8	1.8	4.1

TABLE IX

Collisional-Radiative Ionization Coefficients  
Optically Thin (All Wavelengths)

Te(e.v.) Ne	Ion				
	1.0	1.5	2.0	2.5	3.0
1.0E+16	2.9E-21	4.0E-17	5.8E-15	1.1E-13	8.4E-13
2.0	3.9	5.5	6.8	1.5	1.0E-12
3.0	4.9	7.2	1.0E-14	1.8	1.2
4.0	5.8	9.2	1.3	2.2	1.4
5.0	6.6	1.1E-16	1.5	2.6	1.6
6.0	7.4	1.3	1.8	3.0	1.8
7.0	8.1	1.5	2.0	3.4	2.1
8.0	8.8	1.6	2.2	3.7	2.3
9.0	9.5	1.8	2.4	4.1	2.5
1.0E+17	1.0E-20	1.9	2.6	4.4	2.7
2.0	1.7	3.0	4.3	7.4	4.6
3.0	2.2	3.9	5.6	1.0E-12	6.2
4.0	2.6	4.6	6.6	1.2	7.5
5.0	2.9	5.2	7.4	1.4	8.6
6.0	3.2	5.7	8.1	1.5	9.6
7.0	3.4	6.1	8.6	1.6	1.0E-11
8.0	3.6	6.4	9.2	1.7	1.1
9.0	3.8	6.8	9.6	1.8	1.2
1.0E+18	4.0	7.1	1.0E-13	1.9	1.2
2.0	5.4	9.1	1.2	2.4	1.6
3.0	6.5	1.0E-15	1.4	2.6	1.8
4.0	7.5	1.1	1.5	2.8	1.9
5.0	8.4	1.2	1.5	2.9	2.0
6.0	9.0	1.3	1.6	3.0	2.1
7.0	9.5	1.3	1.7	3.1	2.1
8.0	1.0E-19	1.4	1.7	3.2	2.2
9.0	1.1	1.4	1.8	3.3	2.2
1.0E+19	1.2	1.5	1.8	3.3	2.3

TABLE X

Collisional-Radiative Recombination Coefficients  
Optically Thick (All UV Bound-Bound Wavelengths)

Neutral

$T_e$ (e.v.) Ne	1.0	1.5	2.0	2.5	3.0
1.0E+16	2.6E-12	1.1E-12	8.2E-13	5.4E-13	4.8E-13
2.0	2.9	1.4	1.1E-12	6.7	5.8
3.0	3.3	1.8	1.3	8.0	7.0
4.0	3.8	2.2	1.6	9.4	8.2
5.0	4.3	2.6	1.8	1.1E-12	9.4
6.0	4.7	2.9	2.0	1.3	1.1E-12
7.0	5.1	3.3	2.3	1.4	1.2
8.0	5.6	3.7	2.5	1.6	1.3
9.0	6.1	4.0	2.8	1.8	1.4
1.0E+17	6.6	4.3	3.0	1.9	1.5
2.0	1.1E-11	7.4	5.6	3.6	2.7
3.0	1.7	1.1E-11	8.1	5.4	4.0
4.0	2.2	1.4	1.0E-11	7.3	5.2
5.0	2.7	1.7	1.3	9.1	6.5
6.0	3.2	2.0	1.5	1.1E-11	7.8
7.0	3.8	2.4	1.7	1.3	9.0
8.0	4.3	2.6	2.0	1.5	1.0E-11
9.0	4.8	3.0	2.2	1.7	1.1
1.0E+18	5.4	3.4	2.5	1.9	1.3
2.0	1.1E-10	6.8	4.8	3.8	2.7
3.0	1.6	1.0E-10	7.2	5.8	4.1
4.0	2.2	1.4	9.6	7.7	5.6
5.0	2.7	1.7	1.2E-10	9.6	7.0
6.0	3.3	2.1	1.5	1.1E-10	8.6
7.0	3.8	2.4	1.7	1.3	1.0E-10
8.0	4.4	2.8	2.0	1.5	1.2
9.0	4.9	3.2	2.2	1.7	1.3
1.0E+19	5.5	3.5	2.5	1.9	1.5

TABLE XI

## Collisional-Radiative Recombination Coefficients

Optically Thick (All Bound-Bound UV Wavelengths)

T <sub>e</sub> (e.v.) Ne	Ion				
	1.0	1.5	2.0	2.5	3.0
1.0E+16	4.4E-12	2.1E-12	1.7E-12	1.1E-12	1.0E-12
2.0	4.6	2.4	1.9	1.3	1.2
3.0	5.1	3.0	2.4	1.5	1.4
4.0	5.6	3.6	2.8	1.7	1.6
5.0	6.2	4.1	3.1	1.9	1.7
6.0	6.8	4.6	3.5	2.1	1.9
7.0	7.4	5.0	3.8	2.4	2.1
8.0	8.0	5.5	4.2	2.6	2.3
9.0	8.5	6.0	4.5	2.8	2.4
1.0E+17	9.0	6.4	4.8	3.0	2.6
2.0	1.5E-11	1.0E-11	8.1	6.3	5.7
3.0	2.2	1.5	1.1E-11	7.7	6.2
4.0	2.9	1.9	1.5	1.0E-11	8.0
5.0	3.5	2.3	1.8	1.3	9.6
6.0	4.2	2.7	2.1	1.6	1.1E-11
7.0	4.9	3.2	2.4	1.8	1.3
8.0	5.5	3.6	2.8	2.1	1.5
9.0	6.2	4.0	3.1	2.4	1.7
1.0E+18	6.8	4.5	3.4	2.6	1.9
2.0	1.4E-10	8.9	6.4	5.2	3.9
3.0	2.1	1.3E-10	9.8	7.9	5.9
4.0	2.8	1.8	1.3E-10	1.1E-10	7.9
5.0	3.5	2.2	1.7	1.3	9.9
6.0	4.2	2.7	2.0	1.6	1.2E-10
7.0	4.9	3.1	2.3	1.8	1.4
8.0	5.5	3.6	2.7	2.1	1.6
9.0	6.2	4.0	3.0	2.3	1.8
1.0E+19	6.9	4.5	3.3	2.6	2.0

TABLE XII

Collisional-Radiative Ionization Coefficients  
Optically Thick (All Bound-Bound UV Wavelengths)

Te(e.v.) Ne	Neutral				
	1.0	1.5	2.0	2.5	3.0
1.0E+16	3.6E-13	2.0E-11	1.6E-10	4.1E-10	1.0E-09
2.0	3.3	2.2	1.8	5.0	1.2
3.0	3.2	2.4	2.0	5.6	1.4
4.0	3.1	2.7	2.2	6.2	1.5
5.0	3.1	2.8	2.3	6.6	1.6
6.0	3.1	3.0	2.5	7.0	1.7
7.0	3.1	3.0	2.6	7.5	1.8
8.0	3.1	3.1	2.7	8.0	1.9
9.0	3.1	3.2	2.8	8.3	2.0
1.0E+17	3.1	3.2	2.9	8.7	2.0
2.0	3.1	3.4	3.4	1.1E-09	2.5
3.0	3.2	3.5	3.6	1.2	2.8
4.0	3.3	3.6	3.7	1.3	3.0
5.0	3.4	3.7	3.8	1.4	3.1
6.0	3.4	3.8	3.9	1.4	3.2
7.0	3.5	3.8	3.9	1.5	3.2
8.0	3.5	3.9	4.0	1.5	3.3
9.0	3.6	3.9	4.0	1.5	3.3
1.0E+18	3.6	4.0	4.0	1.5	3.4
2.0	4.0	4.3	4.2	1.6	3.6
3.0	4.3	4.5	4.4	1.7	3.8
4.0	4.5	4.6	4.5	1.7	3.9
5.0	4.7	4.7	4.6	1.7	4.0
6.0	4.9	4.9	4.7	1.7	4.1
7.0	5.1	5.0	4.8	1.8	4.1
8.0	5.3	5.1	4.8	1.8	4.1
9.0					
1.0E+19	5.6	5.3	4.9	1.8	4.2

TABLE XIII

Collisional-Radiative Ionization Coefficients  
Optically Thick (All Bound-Bound UV Wavelengths)

Te(e.v.) Ne	Ion				
	1.0	1.5	2.0	2.5	3.0
1.0E+16	4.0E-20	4.9E-16	6.8E-14	1.0E-12	6.7E-12
2.0	4.1	5.3	7.5	1.1	7.6
3.0	4.4	5.8	8.1	1.2	8.2
4.0	4.8	6.2	8.6	1.3	8.9
5.0	5.1	6.5	9.0	1.4	9.5
6.0	5.4	6.8	9.4	1.4	9.9
7.0	5.6	7.0	9.7	1.5	1.0E-11
8.0	5.9	7.1	9.9	1.6	1.1
9.0	6.1	7.2	1.0E-13	1.6	1.1
1.0E+17	6.4	7.3	1.0	1.7	1.1
2.0	8.4	7.8	1.1	2.0	1.4
3.0	1.0E-19	8.2	1.2	2.1	1.6
4.0	1.2	8.4	1.2	2.3	1.7
5.0	1.3	8.6	1.3	2.4	1.7
6.0	1.4	8.8	1.3	2.4	1.8
7.0	1.5	8.9	1.3	2.5	1.9
8.0	1.5	9.1	1.3	2.5	1.9
9.0	1.6	9.2	1.3	2.5	1.9
1.0E+18	1.7	9.4	1.3	2.6	2.0
2.0	2.1	1.0E-15	1.5	2.8	2.2
3.0	2.4	1.1	1.5	3.0	2.3
4.0	2.7	1.2	1.6	3.1	2.3
5.0	3.1	1.3	1.6	3.1	2.4
6.0	3.4	1.3	1.6	3.2	2.4
7.0	3.6	1.4	1.7	3.2	2.5
8.0	3.9	1.4	1.8	3.3	2.5
9.0	4.2	1.5	1.8	3.4	2.5
1.0E+19	4.5	1.5	1.8	3.4	2.5



TABLE XIV

Saha Threshold Values ( /cm<sup>3</sup> )

$T_e$ (e.v.)	All states	$N(i)$ ( $i \geq 7$ )	$N^+(p)$ ( $p \geq 7$ )
1.0	2.2E+18	4.5E+17	6.4E+17
1.5	2.5E+18	3.6E+17	6.8E+17
2.0	2.9E+18	3.0E+17	7.5E+17
2.5	3.4E+18	2.4E+17	7.8E+17
3.0	* 3.9E+18	* 2.0E+17	8.2E+17

\* Excluding N(13)

$N_0$ ,  $N^+$ ,  $N^{++}$ ,  $Ne$

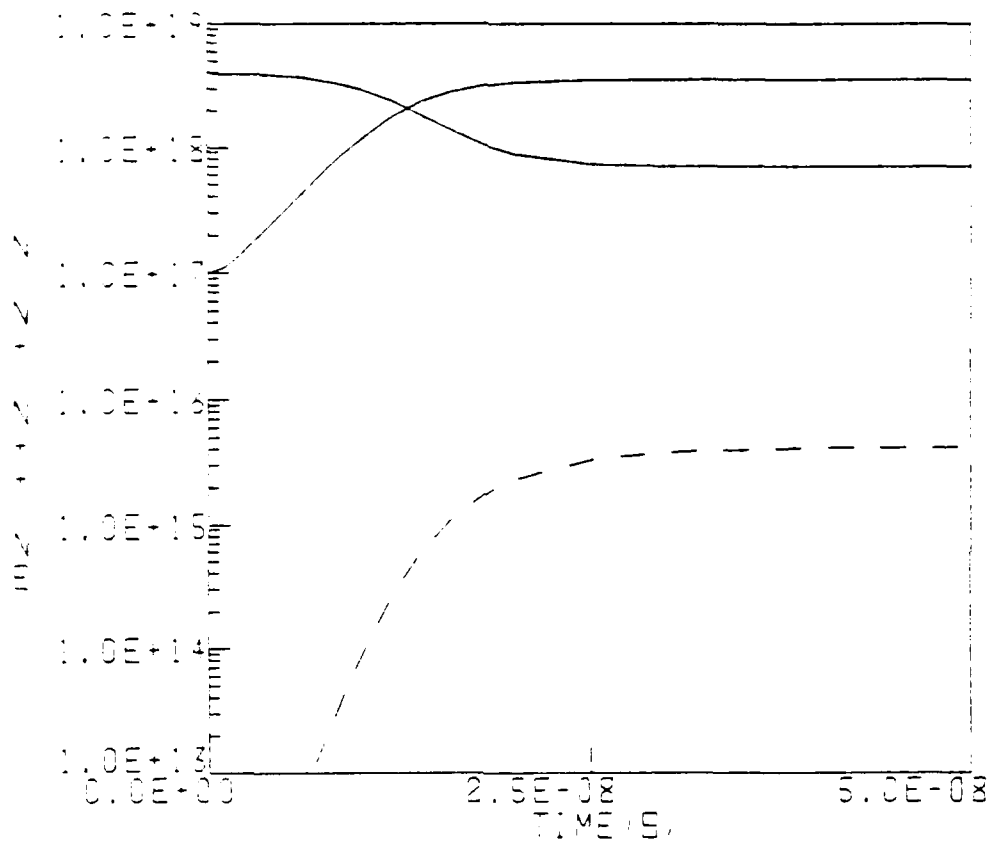


Figure 1.

Population densities for  $N$  (solid line, top at  $t=0$ ),  $N^+$  (solid line, bottom at  $t=0$ ),  $N^{++}$  (dashed line), and  $Ne$  (same as  $N^+$ ). All figures are for  $T_e=2.0$  e.v.

# N(1-3)

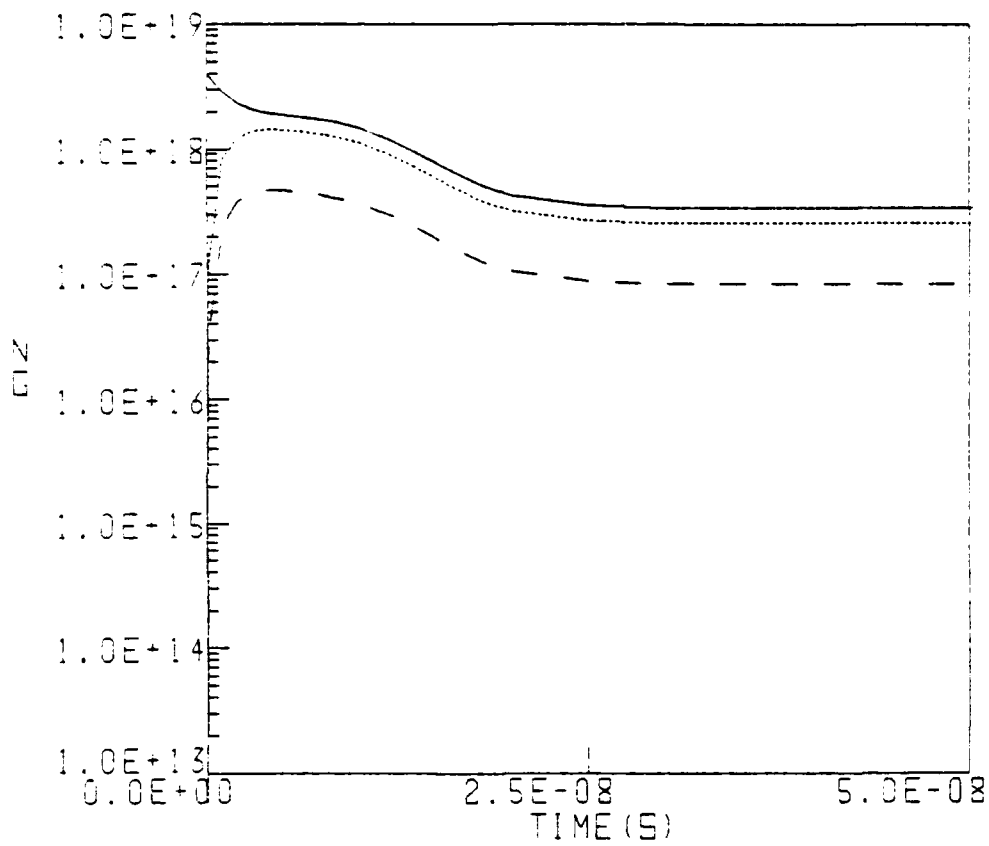


Figure 2.

Population densities for N(1), N(2), and N(3)  
(solid, dotted, and dashed lines, respectively).

N(4-6, 13) UV

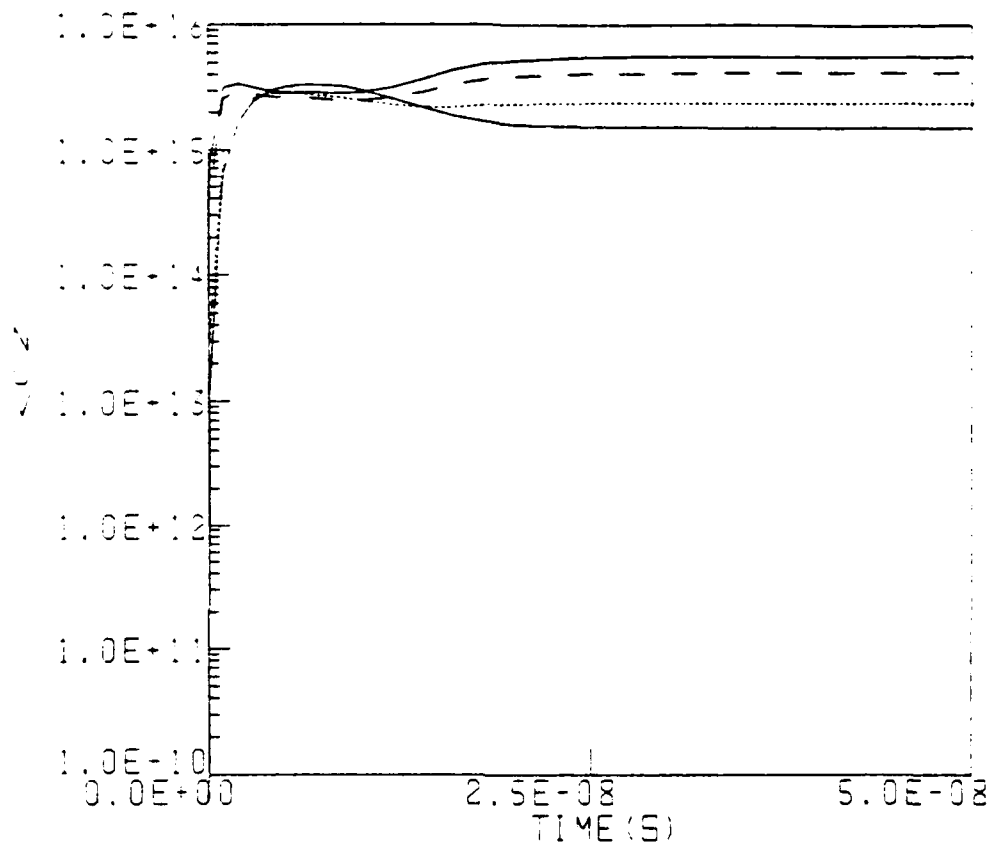


Figure 3.

Population densities for uv emitting N states;  
i.e. N(4) (solid line, top), N(5) (dotted line),  
N(6) (dashed line), and N(13) (solid line, bottom).

# N(8-12) IR

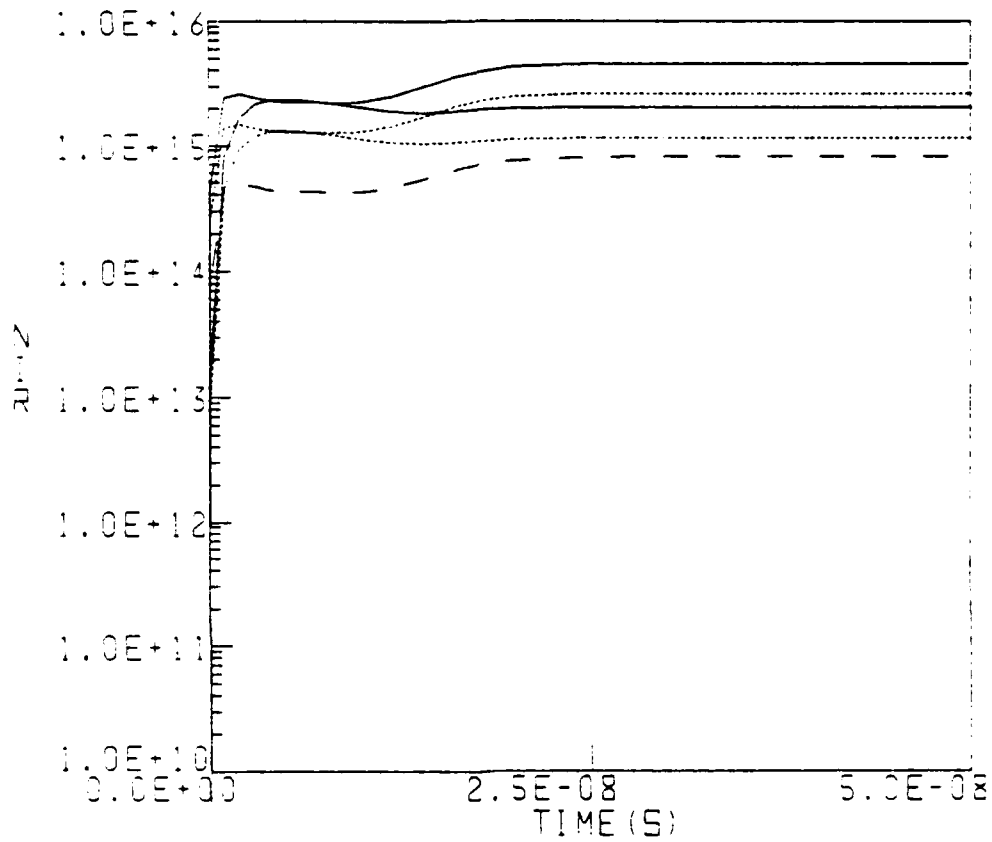


Figure 4.

Population densities for ir emitting N states;  
i.e. N(8) (solid line, top), N(9) (dotted line,  
top), N(10) (dashed line), N(11) (solid line,  
bottom), and N(12) (dotted line, bottom).

N<sup>+</sup> 1-3

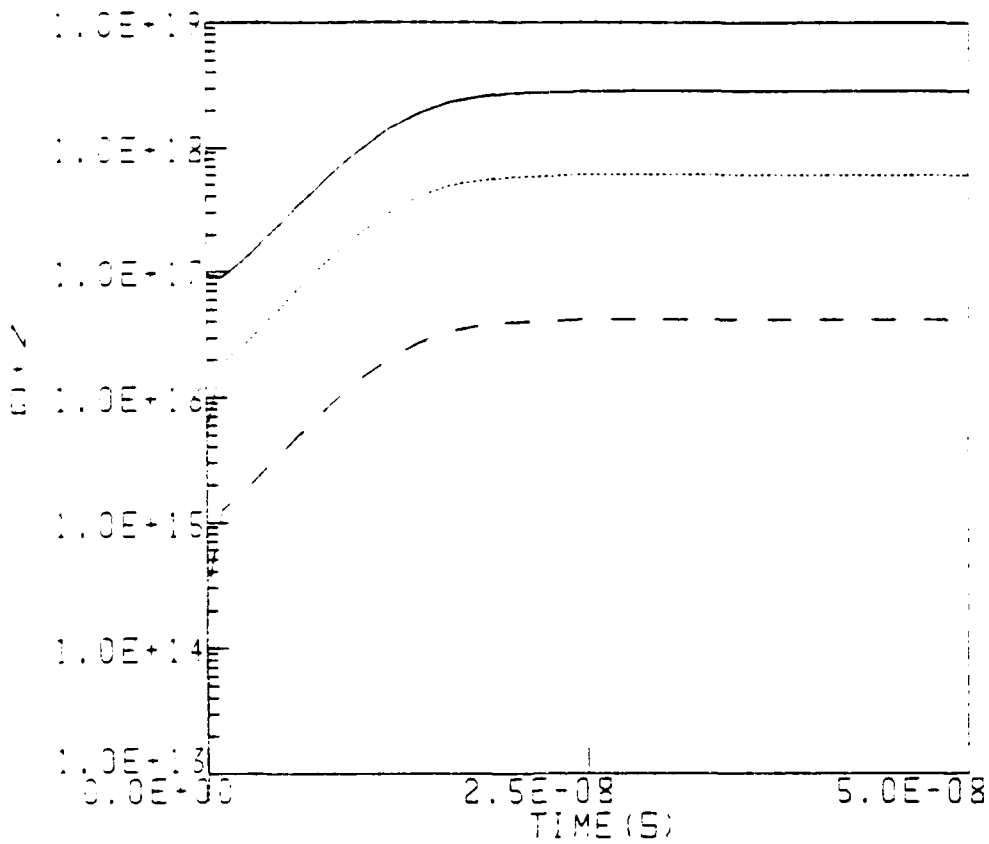


Figure 5.

Population densities for  $N^+$  ground configurations;  $N^+(1)$  (solid line),  $N^+(2)$  (dotted line), and  $N^+(3)$  (dashed line).

N-(4-9,12) UV

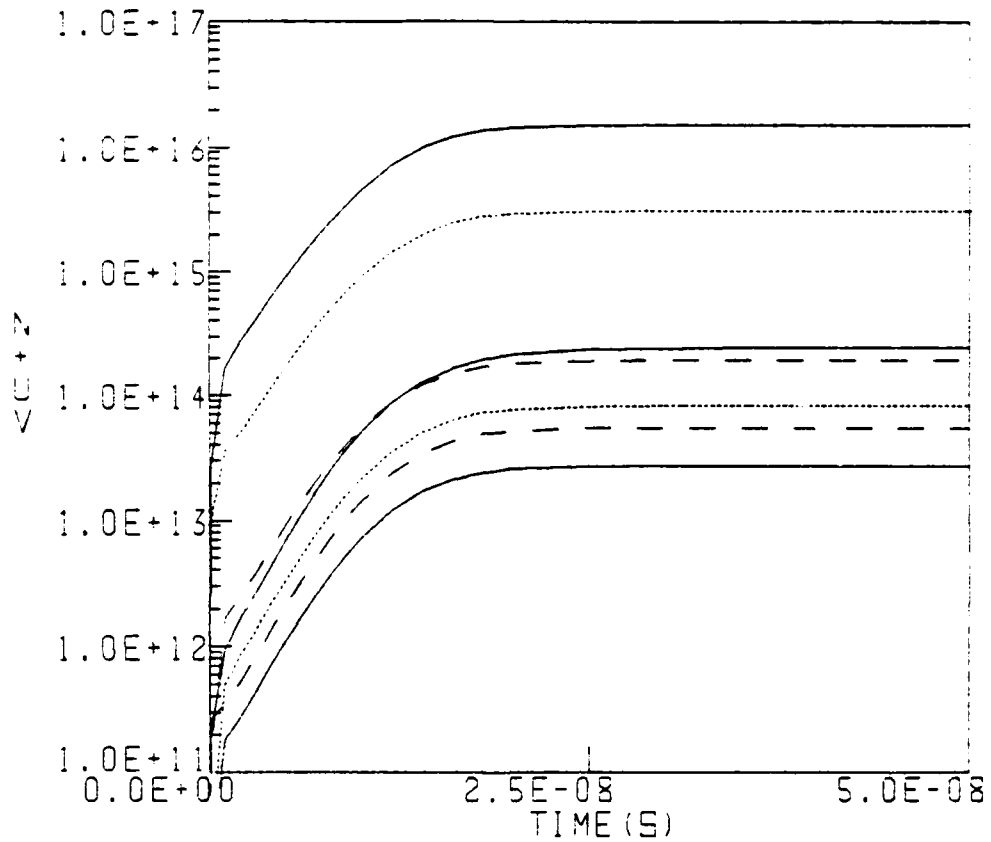


Figure 6.

Population densities for  $N^+$  uv emitting states;  $N^+(4)$  (solid line, top),  $N^+(5)$  (dotted line, top),  $N^+(6)$  (dashed line, top),  $N^+(7)$  (solid line, middle),  $N^+(8)$  (dotted line, bottom),  $N^+(9)$  (dashed line, bottom), and  $N^+(12)$  (solid line, bottom).

# N+(10-11, 13-17) VIS

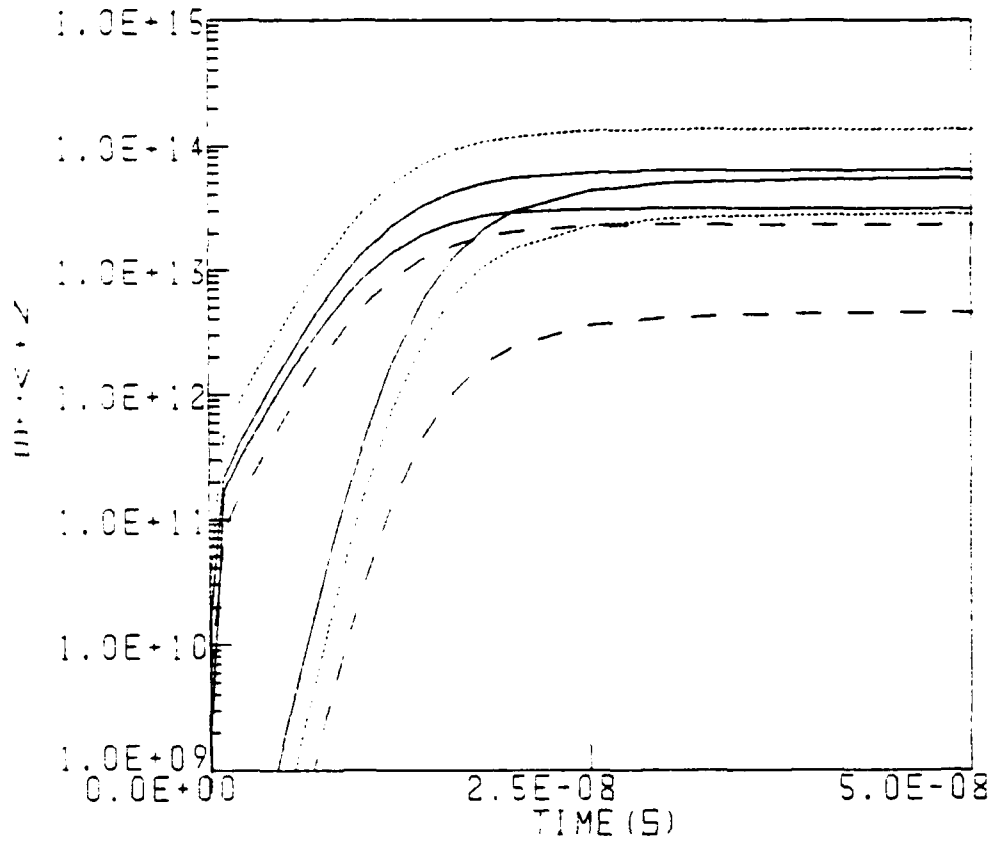


Figure 7.

Population densities for visible emitting  $N^+$  states; final order from top to bottom is  $N^+(11)$ ,  $N^+(10)$ ,  $N^+(17)$ ,  $N^+(14)$ ,  $N^+(15)$ ,  $N^+(13)$ , and  $N^+(16)$ .



# N<sup>++</sup> (1, 2)

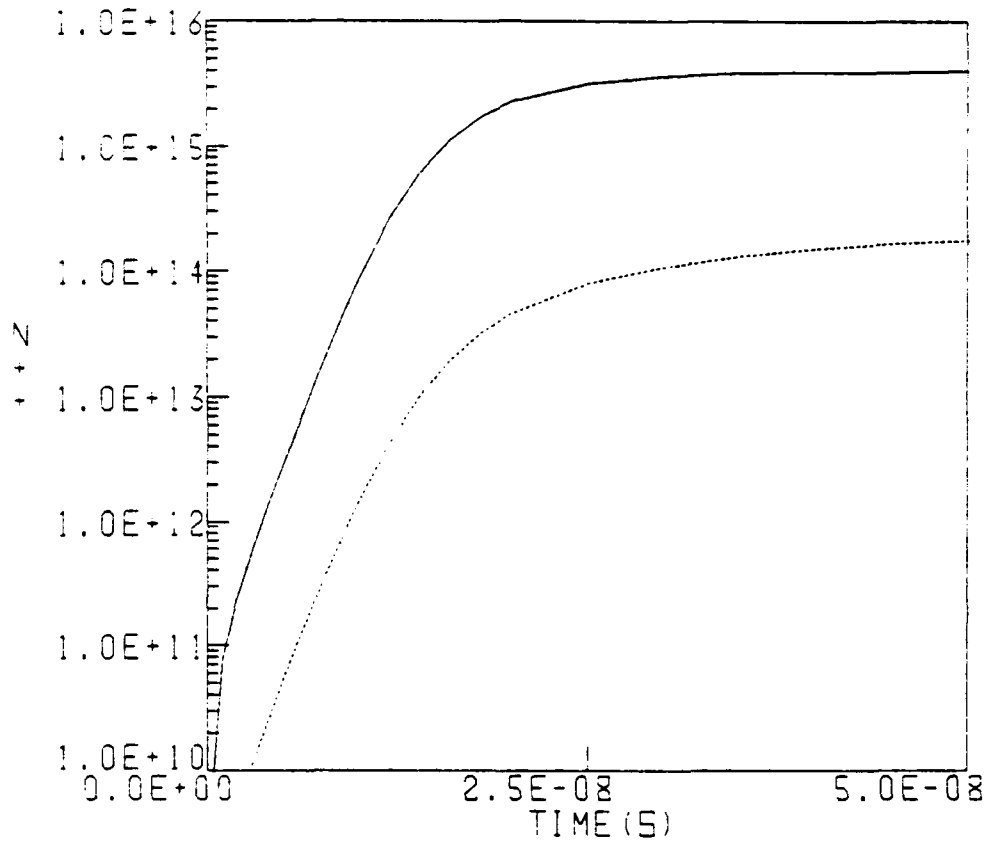


Figure 8.

Population densities for N<sup>++</sup> levels; N<sup>++</sup>(1) (solid line) and N<sup>++</sup>(2) (dotted line).

# CELL-RAD ALFA(0,+)

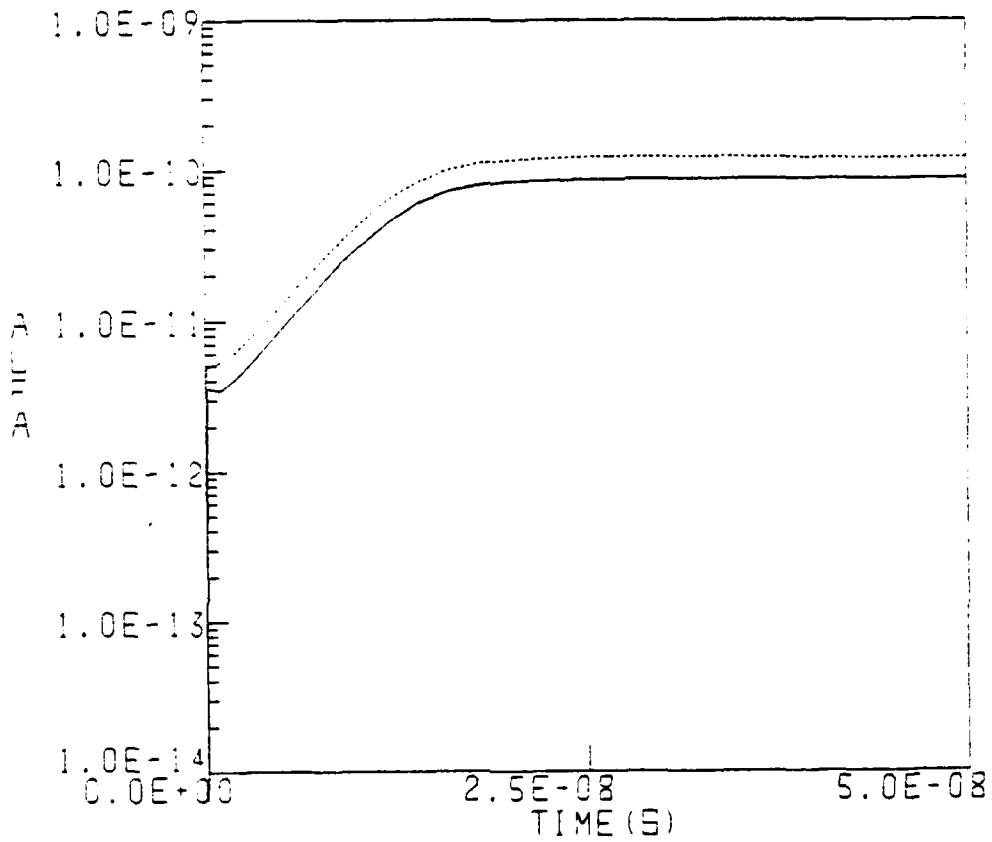


Figure 9.

Collisional-radiative recombination coefficients for optically thin neutral (solid line) and ion (dotted line) cases.

COLL-RAD 5 (0, +)

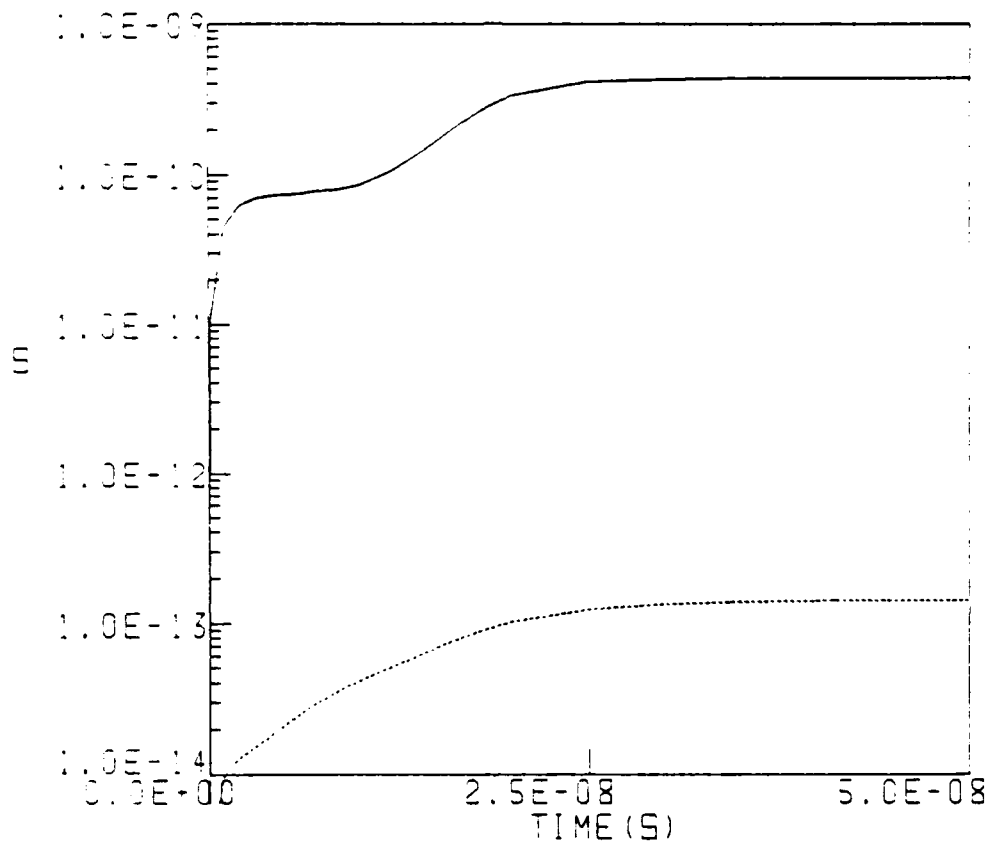


Figure 10.

Collisional-radiative ionization coefficients for the optically thin neutral (solid line) and ion (dotted line) cases.

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