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ELECTROMAGNETIC BRAKING OF A
METALLIC PROJECTILE IN FLIGHT

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20. ABSTRACT *(Continue on reverse side if necessary and identify by block number)*

    A simple model for the electromagnetic deceleration of a moving metallic projectile is described. This model incorporates the influence of magnetic field parameters, time-dependent field diffusion, and device geometry to approximate the braking action. The model predicts that a viable experimental braking device can be designed.

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CONTENTS

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INTRODUCTION

It has long been known that solid objects (e.g. projectiles) can be acceler-
ated by electromagnetic (EM) forces (ref 1). Typically, currents are required to
flow either in the projectile or in an arc behind it. These currents can be
supplied through sliding contacts, induced during the acceleration process, or
pre-established (persistent) (ref 2).

Deceleration of a moving projectile is possible by operating an EM accelera-
tion system in the reverse mode. Such schemes involve a degree of flux compres-
sion such as that incorporated in the inverse railgun concept recently espoused
by Marshall (ref 3), which accomplishes projectile deceleration as a means of
transferring electrical energy to a separate load.

The subject of this report is the passive electromagnetic braking of a mov-
ing projectile where kinetic energy is directly converted into heat. The phenom-
enon has an intrinsic conceptual appeal, and potential applications include the
controlled "soft" catch of appropriately configured projectiles in flight.

A simple model was conceived to obtain some feeling for the magnitude of
parameters involved in the electromagnetic braking process and constraints im-
posed upon the design of a braking device. The model considers the motion of a
cylindrical, metallic projectile in an axial magnetic field uniformly distributed
in a space confined by a fixed, resistive, cylindrical liner which is coaxial
with the moving projectile.

Field compression in the gap between the moving projectile and the liner
causes θ-currents to rise along the projectile surface and the adjacent segment
of the liner surface by field diffusion in both conducting materials. These
currents give rise to resistive Joule heating caused by the time dependence of
field diffusion and the motion of the projectile. The induced currents, espe-
cially in the liner, show a nonuniform distribution in the relatively short time
interval during which the projectile moves along over its own length. The net
force resulting from the interacting current distributions on the projectile and
the adjacent liner segment is anticipated to be nonvanishing and will counteract
the projectile's motion. In this way, the projectile is losing its kinetic ener-
gy while at the same time, resistive Joule heating is generated in the projectile
and the liner.

MODELING OF BRAKING ACTION

The model described is illustrated in figure 1. A cylindrical metallic pro-
jectile with mass m_p, radius r_0, length L_p, conductivity σ_p, and permeability μ_p
moves with velocity v in an axial uniform magnetic field B_0. The space is con-
fined by a fixed resistive liner with inner and outer radii r_1 and r_2, respec-
tively, conductivity σ_L, and permeability μ_L (fig. 1).

1

The field is assumed to be compressed discontinuously in the gap between the projectile surface and the adjacent liner surface (radii r_o and r_1, respectively) at axial positions z_1 and z_2.

The motion of the projectile is hypothesized to be such that magnetic energy is conserved throughout the braking process. Neglecting mechanical work associated with nonaxial forces on components, conservation of energy gives

$$m_p v \frac{\delta v}{\delta t} = - \frac{\delta H}{\delta t} \tag{1}$$

where H is the resistive Joule heating generated in the projectile and the liner during braking.

The magnetic field in the gap between the projectile and the liner is of induction

$$B_z = B_o \left[\frac{r_1^2}{r_1^2 - r_o^2} \right] \tag{2}$$

for $r_o < r < r_1$ and $z_1 < z < z_2$.

It is assumed that B_z is a constant during the braking process and that its value is independent of the location on the surfaces of bordering projectile and liner.

For radial diffusion of the magnetic field in the liner segment adjacent to the moving projectile, the equation (ref 4)

$$\frac{\delta^2 B_z'}{\delta r^2} - \mu_L \, \sigma_L \, \frac{\delta B_z'}{\delta t} = 0 \tag{3}$$

where

$$B_z'(t = o) = o \text{ and } B_z' = B_z - B_o$$

is valid.

Equation 3 leads to

$$B_z' = B_z' (r_1) \left[1 - \frac{2}{\sqrt{\pi}} \int_o^{\sqrt{\frac{\mu_L \sigma_L}{4t}} \frac{(r-r_1)}{2}} e^{-\omega} \, d\omega \right] \tag{4}$$

The induced θ-currents in the liner are given by

$$J_L = -\frac{1}{\mu_L} \frac{\delta B_z'}{\delta r} \tag{5}$$

Equations 4 and 5 give;

$$J_L = \frac{B_z'(r_1)}{\mu_L} \sqrt{\frac{\mu_L \sigma_L}{\pi t}} \, e^{-\frac{\mu_L \sigma_L}{4t}(r-r_1)^2} \tag{6}$$

Similar results are obtained for the induced currents in the projectile where B_z is the magnetic field at the conductor surface. The heat generated per unit time, $\frac{\delta H}{\delta t}$, in the conducting surfaces of projectile and liner bordering the gap between them, is expressed by:

$$\frac{\delta H}{\delta t} = \int_{z_1}^{z_2} \left[\frac{2\pi r_1}{\sigma_L} \int_{r_1}^{\infty} J_L^2 \, dr' + \frac{2\pi r_o}{\sigma_p} \int_{-\infty}^{r_o} J_p^2 \, dr \right] dz \tag{7}$$

where J_L and J_p are the currents induced in the liner and projectile, respectively, and where $z_2 - z_1 = L_p$.

Equation 7 leads to

$$\frac{\delta H}{\delta t} = \frac{2\pi r_1}{\sigma_L} \left[\frac{B_z'(r_1)}{\mu_L} \right]^2 \int_{z_1}^{z_2} \sqrt{\frac{\mu_L \sigma_L}{2\pi t}} \, dz + \frac{2\pi r_o}{\sigma_p} \left[\frac{B_z(r_o)}{\mu_p} \right]^2 L_p \sqrt{\frac{\mu_p \sigma_p}{2\pi t}} \tag{8}$$

In performing the integration over z in equation 8, the time scale in the liner segment covered by the moving projectile is running from zero to L_p/v, while the time scale for the generation in the projectile is running from the beginning towards the end of the braking process (accumulation). The dynamics mentioned here cause the nonuniform distribution of θ-currents (eq 6) in the liner segment adjacent to the moving projectile and are the source for a net braking force on the projectile.

Combining equations 1 and 8 gives the analytical expression

$$m_p v \frac{\delta v}{\delta t} = -\left[\beta_L \, v^{1/2} + \beta_p \, t^{-1/2} \right] \tag{9}$$

describing the braking action in the chosen setup.

3

In equation 9, β_L and β_p are

$$\beta_L = \frac{2\pi r_1}{\sigma_L} \left[\frac{B_z'(r_1)}{\mu_L} \right]^2 \sqrt{\frac{2\mu_L \sigma_L L_p}{\pi}}$$

$$\beta_p = \frac{2\pi r_o}{\sigma_p} \left[\frac{B_z(r_o)}{\mu_p} \right]^2 L_p \sqrt{\frac{\mu_p \sigma_p}{2\pi}}$$

(10)

CALCULATED RESULTS

To obtain some feeling for the magnitude of parameters involved in electro-magnetic braking, an example involving the motion of a cylindrical steel projectile in an axial magnetic field in a space confined by a copper liner (fig. 1) is analyzed. Solving equation 9 numerically with a steel projectile mass m_p - 6 kg, length L_p = 0.508 m, radius r_o = 0.0508 m, μ_p = 2 x 10^{-4} Wb/A m, σ_p = 0.38 x 10^7 mho/m, and a copper liner with radius r_1 = 0.05334m, μ_L = 12.57 x 10^{-7} Wb/A m, and σ_L = 5.8 x 10^7 mho/m gives the data of table 1 when braking action starts at a projectile velocity v_o = 600 m/s.

The length, ΔL, and time, Δt, involved in braking the projectile to a final velocity of zero m/s and the overall heat generated in the liner, ΔH_L, and the projectile, ΔH_p, are given in table 1. ΔL and Δt are calculated with equation 9 (V,t - history), and ΔH_L and ΔH_p are calculated with equation 10.

Table 1. Electromagnetic braking action parameters for a steel projectile and copper liner

Magnetic field, B_0 (T)	Length, ΔL (m)	Time, Δt (s)	Liner heat, ΔH_L (J)	Projectile heat, ΔH_p (J)
1	12.9	34.5 x 10^{-3}	1.079 x 10^6	504
2	3.1	8.7 x 10^{-3}	1.079 x 10^6	1.01 x 10^3
3	1.4	3.9 x 10^{-3}	1.078 x 10^6	1.5 x 10^3

4

Keeping other parameters constant, the influence of gap-width $(r_1 - r_0)$ on braking length, ΔL, time, Δt, and heat generated in the projectile, ΔH_p, is shown in figures 2, 3, and 4, respectively.

If other materials for projectile and liner are considered (e.g., changing only μ and σ with respect to values mentioned above), substantial changes in braking length and time are calculated. If, for example, a tungsten projectile and copper liner are taken, braking lengths and times are reduced by a factor of about 2 to 3 and heat generated in the projectile is increased by a factor of about 1000. Taking a steel liner and a steel or tungsten projectile increases braking lengths to many tens of meters and times to many seconds.

Although not indicated here numerically, the influence of projectile mass on braking length and time appears to be almost proportional.

DISCUSSION

The model presented here contains a number of limitations. For instance, a practical device for electromagnetic braking of a metallic projectile would have a finite length. Braking the motion of the projectile on entering the magnetic field, present in the setup depicted in figure 1, is substantial and is not modeled here. During compression of the magnetic field in the gap between the moving projectile and the liner, the change in magnetic induction is continuous [not discontinuous as assumed here (fig. 1)] and slightly different at the front and the rear of the projectile. Although current distributions on liner and projectile surfaces will then be more complicated, as will force distributions, it is not anticipated that calculated results will change drastically (i.e., not more than a factor of two).

A more substantial limitation of the model is the assumption that B_z (magnetic induction) in the gap is a constant during braking. As a result of diffusion of the B-field in the projectile and adjacent liner surfaces, B_z on these surfaces will change not only in going from z_1 toward z_2 (fig. 1) but also during the whole braking process. Leakage of the compressed field from the gap causes less braking action than calculated. However, depending on the magnitude, the braking time, Δt, leakage will have a minor influence on calculated parameters when the associated skin depth $\left[\delta\left(\delta = \pi\Delta t/(\mu\sigma)\right)\right]$ is smaller than the gap width $(r_1 - r_0)$ considered. Application of the model presented here implies, therefore, that braking times in the order of a few milliseconds or less have to be considered. In addition, the effectiveness of the model may be further enhanced by restricting attention to ferromagnetic projectiles. Apart from the limitations mentioned above, the calculated results show that with realistic values for initial magnetic induction and gap width, metallic projectiles with a mass and initial velocity of interest can be decelerated over an acceptable length.

In designing a device, the mechanical strength constraints related to the construction of the projectile to be decelerated, the liner and the B-field generating coil have to be considered. In the gap between the moving projectile and

5

the adjacent liner segment, mechanical stresses on both materials can rise as high as 4 to 8 kbar with B_0 and $(r_1 - r_0)$ values of several tesla and mm, respectively. Temperature rises in the projectile and liner surface layers caused by resistive Joule heating are minor for the B_0 and $(r_1 - r_0)$ values.

CONCLUSIONS

Within the constraints of the model, calculated results showed that with values for the magnetic induction B_0 of several tesla and a gap width between projectile and liner of several mm's, a steel projectile with a mass of 6 kg and an initial velocity of 600 m/s can be slowed down to rest over a length of several meters without excessive stress-loading or heating of components.

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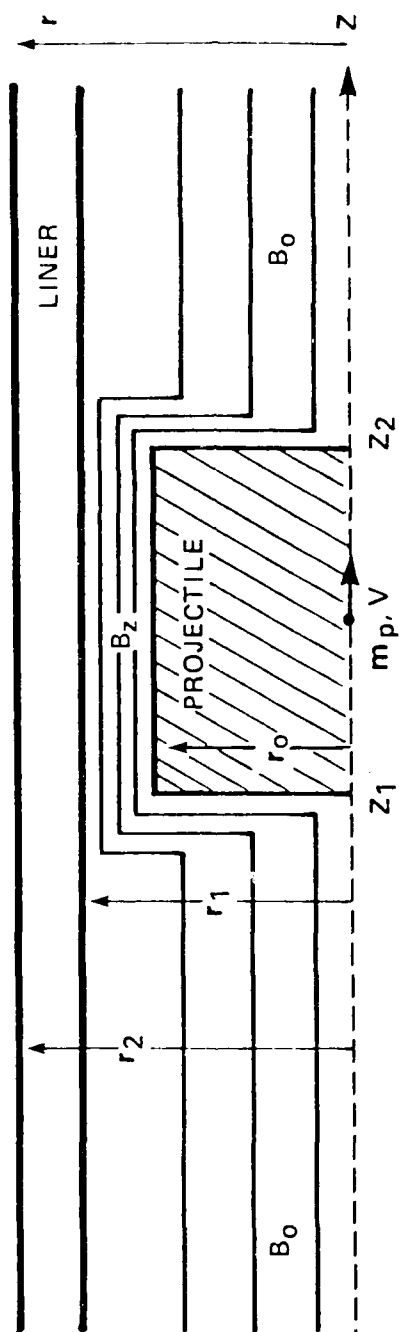
Figure 1. Magnetic field configuration around a metallic projectile moving in an axial field confined by a resistive liner (axis-symmetric part is shown)
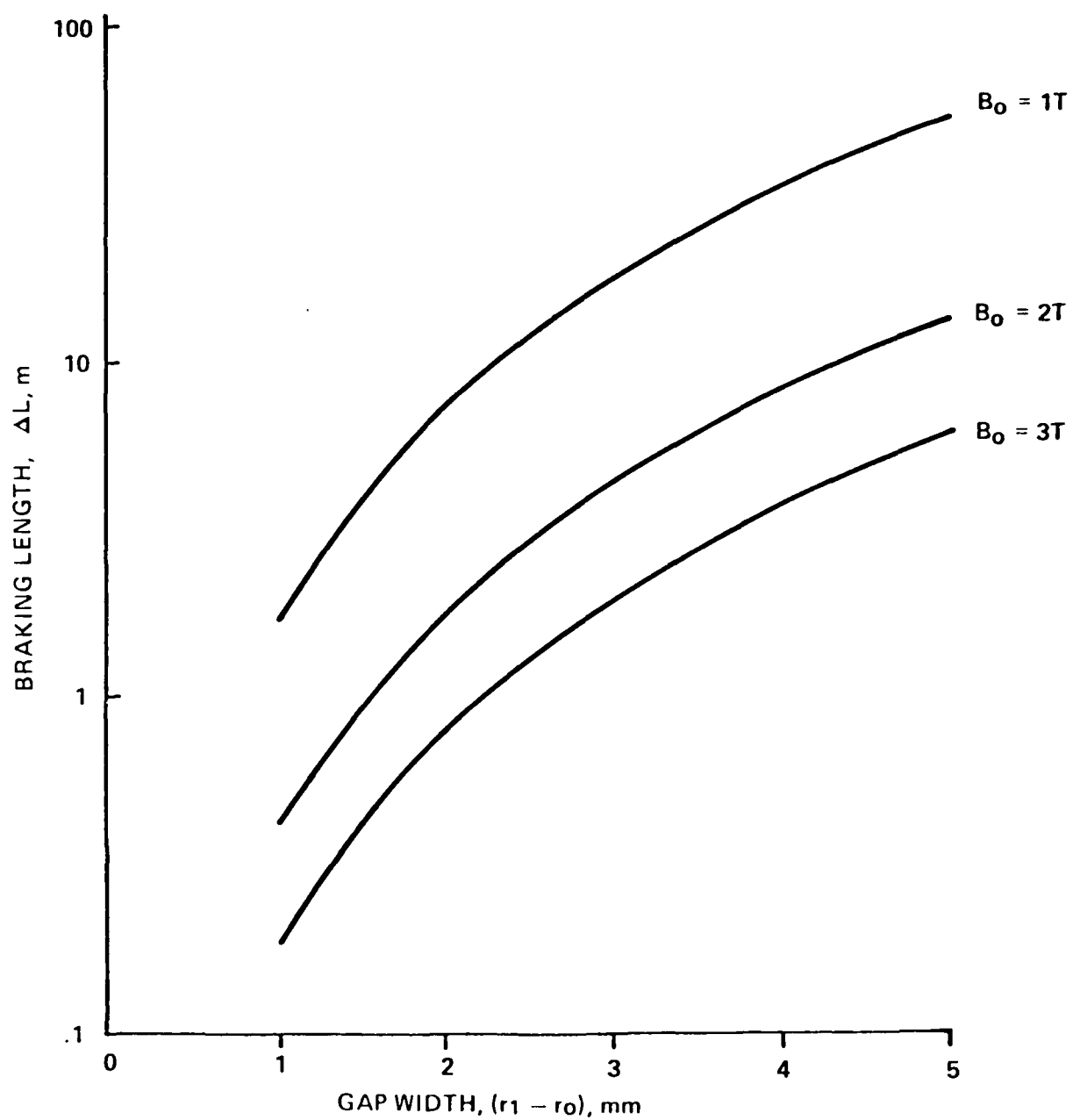
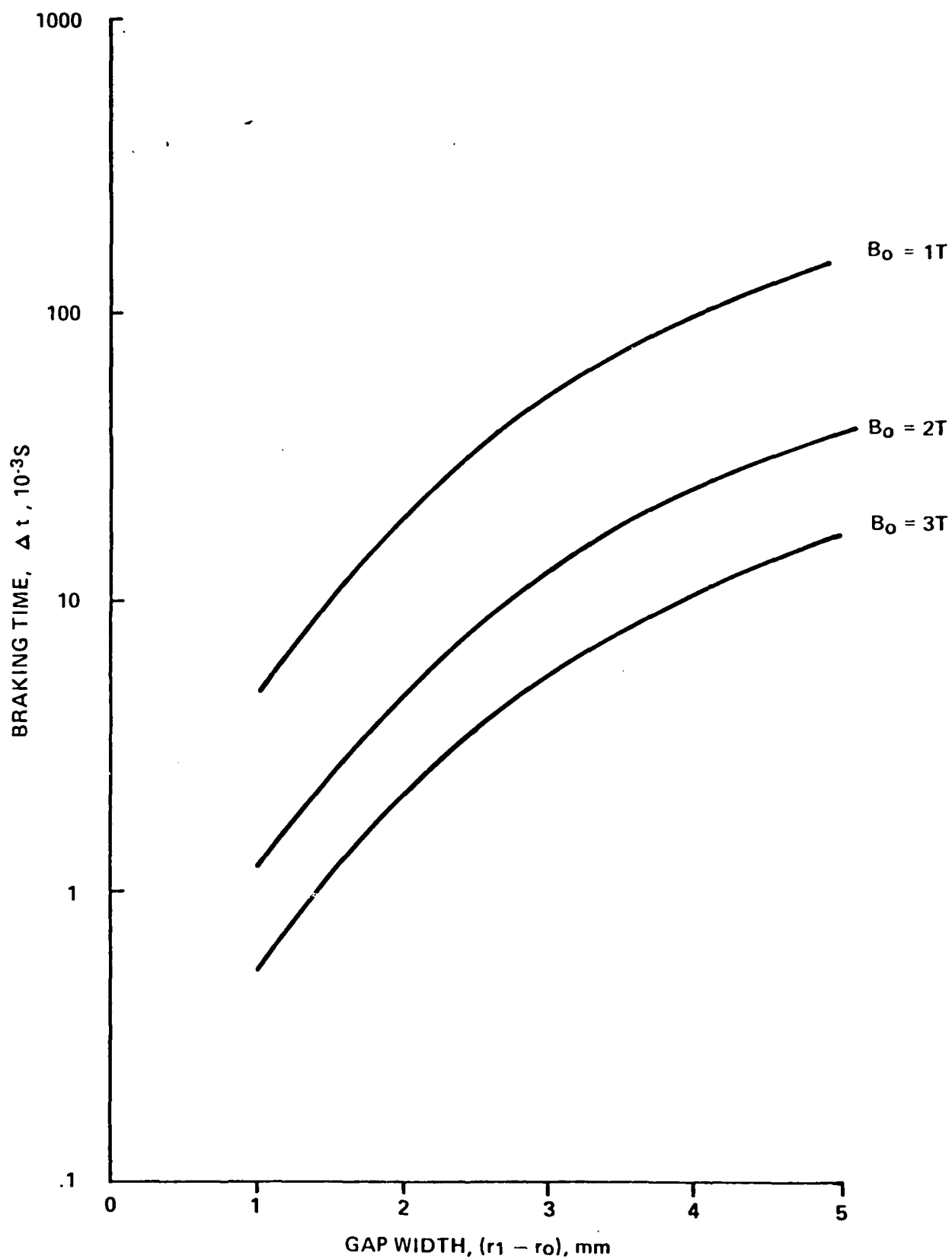Figure 2. Braking length ΔL as a function of gap-width for a steel projectile and copper liner, B_o = 1, 2, and 3T.

10

Figure 3. Braking time Δt as a function of gap-width for a steel projectile and copper liner, $B_o = 1$, 2, and 3T
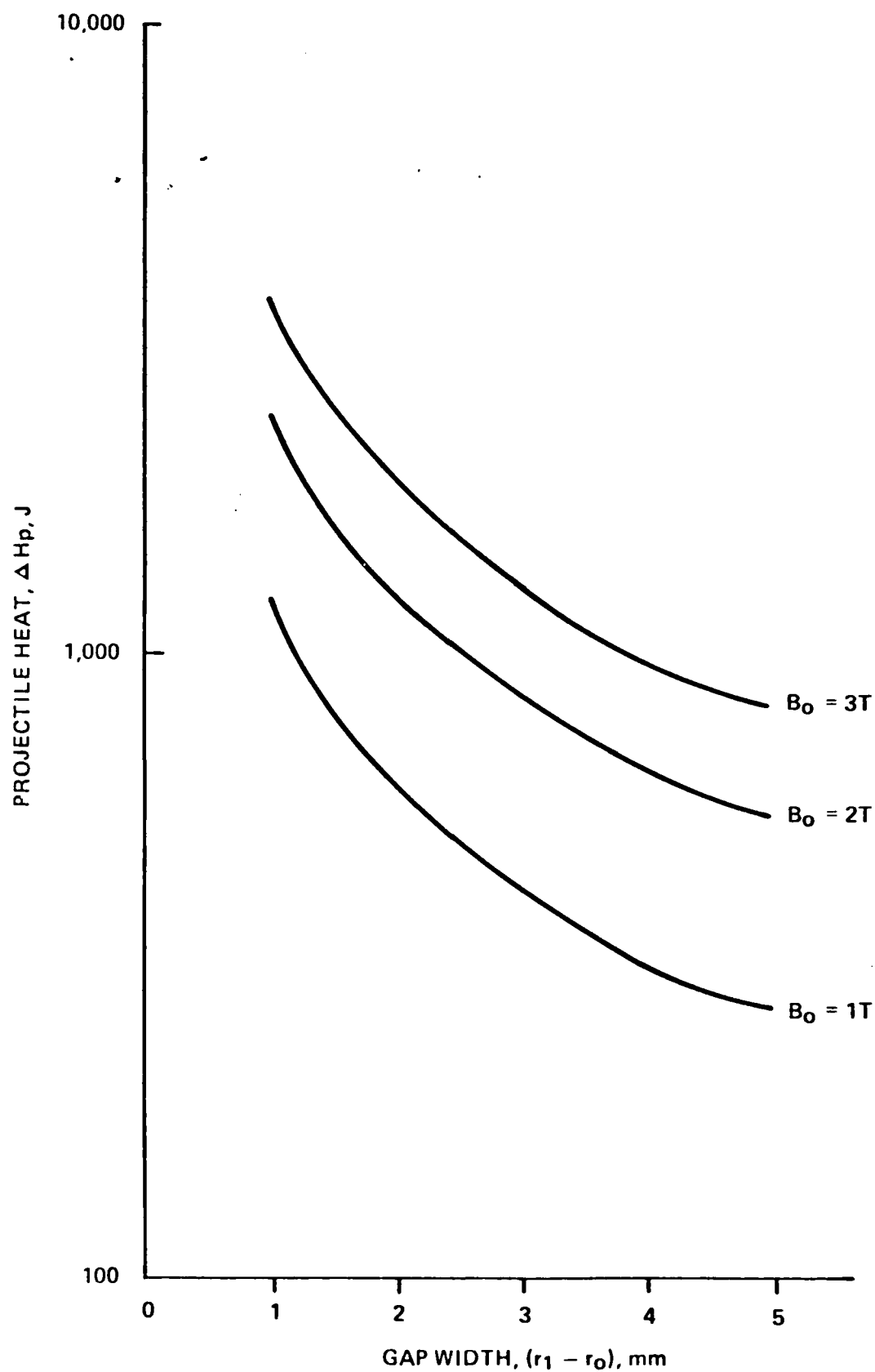
11

Figure 4. Projectile heat ΔH_p generated during braking as a function of gap-width for a steel projectile and copper liner, B_o = 1, 2, and 3T

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