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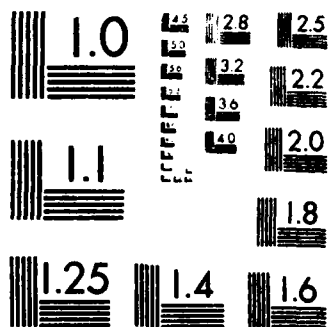
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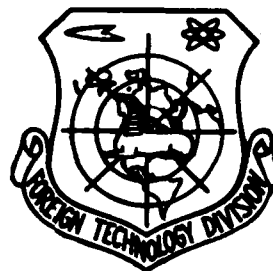
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THE PROXIMITY EFFECTS OF SUPERCONDUCTING
MULTILAYER FILM

by

C. Xueyu and Y. Daole



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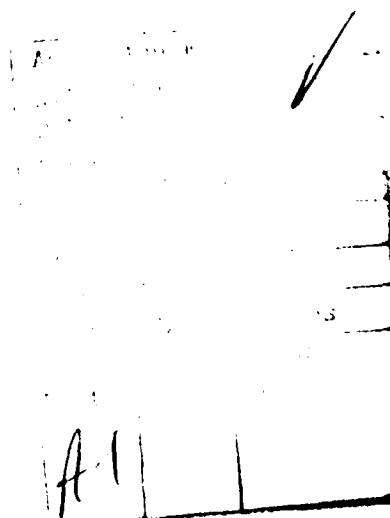
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THE PROXIMITY EFFECTS OF SUPERCONDUCTING MULTILAYER FILM

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Abstract

This paper considers the proximity effects of superconducting multilayer films composed of different metals. Using the Silvert and Cooper method, the relationship between the critical temperature of a superconducting multilayer film with strong heterogeneity and its geometric structure is given under the Cooper limit.

By using modern material preparation techniques such as sputtering, evaporation, epitaxy etc., based on some peoples' designs of atomic scales, we synthesized various previously non-existent new types of materials and studied their structures and properties. This has been an important trend in solid physics in recent years. For example, besides semiconductor materials, there have also been reports recently of making new materials with "multilayered ultrathin common lattice structures" (LUCS) from niobium and copper possessing different properties [1].

When compared with large pieces of homogeneous specimens, multilayered thin film systems have two new factors which should be considered. One is the appearance of many heterogeneous interfaces. See Reference [2] for an analytical discussion of them. The second factor is the proximity effects caused by the many heterogeneous layers being periodically adjacent to each other and the superconducting electron pairs possessing non-localization. This paper makes a preliminary investigation of this problem. We began from a simplified model under

heterogeneous interface conditions, used the GLAG theory and gave the general relationship between the multilayered film's critical temperature and geometric factors.

We conceived that the multilayered film was composed from two types of pure superconducting materials, S_1 and S_2 , and their thicknesses were separately d_1 and d_2 . In order to simplify the problem and outstanding focal points, we assumed that the property difference concentrations of the two types of materials were reflected on their electro-acoustic coupling constant (NV), separately $(NV)_1$ and $(NV)_2$. The other properties were the same.

We used the Silvert and Cooper method to calculate the proximity effects [3].

The virtual time, Fourier transformation, Green's function and abnormal Green's function of the superconductor satisfy the following formulas in the T_c area:

$$G_a(r, r') = G^{(0)}(r - r') - \int dr_1 dr_2 G^{(0)}(r, r_1) \Delta(r_1) G^{(0)}(r_1, r_2) \Delta^*(r_2) G_a(r_2, r'), \quad (1)$$

$$F_a(r, r') = \int dr_1 G_a(r, r_1) \Delta(r_1) G^{(0)}(r_1, r'), \quad (2)$$

In the formula, G_ω and F_ω are separately the completely normal and abnormal functions, $G_\omega^{(0)}$ is the zero order Green function and $\Delta(r)$ is the energy gap function which changes with the space. They should satisfy the following self-consistent conditions:

$$\Delta(r) = V(r) \cdot F(r, r), \quad (3)$$

In the formula $F(r, r) = k_B T \sum F_a(r, r)$ and k_B is the Boltzmann

constant. In the T_c vicinity, $\Delta(r)$ is a small quantity and G_ω and F_ω rely on the expansion in powers of Δ :

$$G_\omega(r, r') = \sum_{m=0}^{\infty} G_\omega^{(m)}(r, r'), \quad (4)$$

$$G_\omega^{(m)}(r, r') = - \int dr_1 dr_2 G_\omega^{(0)}(r, r_1) \Delta(r_1) G_\omega^{(0)}(r_2, r_1) \cdot \Delta(r_2) G_\omega^{(m-1)}(r_2, r'), \quad (5)$$

$$F_\omega(r, r') = \sum_{m=1}^{\infty} F_\omega^{(m)}(r, r'), \quad (6)$$

$$F_\omega^{(m)}(r, r') = \int dr_1 G_\omega^{(m-1)}(r_1, r) \Delta(r_1) G_\omega^{(0)}(r', r_1). \quad (7)$$

By separately substituting formulas (5) and (7) into formulas (4) and (6), we can test and verify this.

We can see from the above expansion formulas that $F_\omega^{(m)}$ is the $2m-1$ times homogeneous function of Δ . In later calculations, we only keep the first order terms of Δ and in this way formula (3) changes to

$$\Delta(r) = V(r) k_B T \sum_n \int dr_1 G_\omega^{(0)}(r - r_1) \Delta(r_1) G_\omega^{(0)}(r - r_1), \quad (8)$$

In the formula

$$\omega = (2n + 1)\pi k_B T \quad n = 0, \pm 1, \pm 2, \dots$$

The zero order Green function is known

$$G_\omega^{(0)} = \left(- \frac{m}{2\pi |r - r'|} \right) \exp \left[i k |r - r'| \operatorname{sgn} \omega - \frac{|\omega| |r - r'|}{v} \right]. \quad (9)$$

We substitute formula (9) into formula (8)

$$\Delta(r) = V(r) \int dr_1 F^{(0)}(r - r_1) \Delta(r_1), \quad (10)$$

In the formula

$$F^{(0)} = k_B T \sum_n \left(\frac{m}{2\pi |r - r'|} \right)^2 \exp \left[- \frac{2|\omega| |r - r'|}{v} \right]. \quad (11)$$

By assuming each layer of the multilayered film is parallel to the xy plane, we can first carry out metric integration of formula (1) and obtain

$$\Delta(z) = V(z)N_z \frac{1}{v_1} k_B T \sum_{\omega} \int \Delta(z') E_1 \left(\frac{2\omega(z-z')}{v_1} \right) dz', \quad (12)$$

In the formula, N_z is the fixed region density of the z area and E_1 is the improper index integral, defined as

$$E_1(u) = \int_1^{\infty} \frac{dt}{t} \exp[-ut]. \quad (13)$$

For convenience of calculations, we make the following stipulations: each layer's coordinates of S_1 are $kd < z < (k+a)d$; each layer's coordinates of S_2 are $(k+a)d < z < (k+1)d$, $k=0, \pm 1, \pm 2, \dots$; $d=d_1+d_2$; $a=d_1/d$; $\mu = (VN)_2/(VN)_1$.

Each layer of superconducting multilayer films is relatively thin. When we consider the so-called Cooper limit, that is, the thickness of each layer is smaller than the coherent length of a corresponding material, at this time, the energy gap function of each level is approximately a constant, separately taken as Δ_1 and Δ_2 . Further, disregarding the macroscopic boundary of the superconductor, we consider the layer number of multilayer film to be infinite.

By letting z_1 and z_2 separately be the two points in the S_1 and S_2 layers and using formula (12) for the two points, we can obtain two linear unrelated equations:

$$\Delta_1 = (NV)_{11}\Delta_1 + (NV)_{12}\Delta_2, \quad (14)$$

$$\Delta_2 = \mu(NV)_{21}\Delta_1 + \mu(NV)_{22}\Delta_2, \quad (15)$$

In the formula, f_{ij} is determined by the precise positions of z_1 and z_2 . By taking z_1 and z_2 in each period k , we can obtain

these two equations. However, because of the translational symmetry of the system, if there is only the equations between z_1 and z_2 , then they are linear and unrelated and do not lose generality. Taking z_1 and z_2 in the period of $k=0$, f_{ij} can be written in the following form:

$$\begin{aligned} f_{11} &= \frac{\pi k_B T}{v_f} \sum_{\omega} \sum_k \int_{k-d}^{(k+\omega)d} E_1\left(\frac{|z_1 - z'|}{l_0}\right) dz', \\ f_{12} &= \frac{\pi k_B T}{v_f} \sum_{\omega} \sum_k \int_{(k+\omega)d}^{(k+1)d} E_1\left(\frac{|z_1 - z'|}{l_0}\right) dz', \\ f_{21} &= \frac{\pi k_B T}{v_f} \sum_{\omega} \sum_k \int_{k-d}^{(k+\omega)d} E_1\left(\frac{|z_2 - z'|}{l_0}\right) dz', \\ f_{22} &= \frac{\pi k_B T}{v_f} \sum_{\omega} \sum_k \int_{(k+\omega)d}^{(k+1)d} E_1\left(\frac{|z_2 - z'|}{l_0}\right) dz', \\ l_0 &= v_f / 2 |\omega|. \end{aligned} \quad (16)$$

The set of equations (14) and (15) have non-zero solution conditions and the coefficient determinate is zero:

$$[(VN)f_{11} - 1] \cdot [\mu(VN)f_{22} - 1] = \mu(VN)f_{12} \cdot f_{21}. \quad (17)$$

We can find the relationship of T_c and d , a , μ and $(VN)_1$ from formula (17). Under common conditions, we can only use the numerical solution method to solve formula (17) yet under strong heterogeneous conditions wherein $\mu \rightarrow 0$, we can obtain an approximate analytical result. At this time, formula (17) changes to

$$f_{11} = \frac{1}{(NV)_1}. \quad (18)$$

After completing the integration of z'

$$\begin{aligned} f_{11} &= (\pi k_B T) \sum_{\omega} \frac{1}{2|\omega|} \left\{ \sum_{k=-1}^{\infty} \int_1^{\infty} \frac{dt}{t^2} \exp\left[-\frac{z_1 t}{l_0}\right] \right. \\ &\quad \times \left[\exp\left(\frac{k+a}{l_0} dt\right) - \exp\left(\frac{k}{l_0} dt\right) \right] + \sum_{k=1}^{\infty} \int_1^{\infty} \frac{dt}{t^2} \exp\left[\frac{z_1 t}{l_0}\right] \\ &\quad \times \left[\exp\left(-\frac{d}{l_0} dt\right) - \exp\left(-\frac{k+a}{l_0} dt\right) \right] + \int_1^{\infty} \frac{dt}{t^2} \left[1 - \exp\left(-\frac{ad - z_1}{l_0} t\right) \right] \right\}. \quad (19) \end{aligned}$$

Under the sign of integration, the summation of k is

$$f_{11} = (\pi k_B T) \sum_{\omega} \frac{1}{|\omega|} \left\{ 1 + \frac{1}{2} \int_1^{\infty} \frac{dt}{t^2} \frac{1 - \exp\left(-\frac{adt}{l_{\omega}}\right)}{1 - \exp\left(-\frac{dt}{l_{\omega}}\right)} \right. \\ \times \exp\left(-\frac{dt}{l_{\omega}}\right) \left[\exp\left(\frac{z_1 t}{l_{\omega}}\right) + \exp\left(\frac{ad - z_1 t}{l_{\omega}}\right) \right] \\ \left. - \frac{1}{2} \int_1^{\infty} \frac{dt}{t^2} \left[\exp\left(-\frac{z_1 t}{l_{\omega}}\right) + \exp\left(-\frac{ad - z_1 t}{l_{\omega}}\right) \right] \right\}. \quad (20)$$

We then find the mean of z_1 in $[0, ad]$

$$\langle f_{11} \rangle = (\pi k_B T) \sum_{\omega} \frac{1}{|\omega|} \left\{ 1 - \frac{l_{\omega}}{ad} \int_1^{\infty} \frac{dt}{t^2} \right. \\ \times \frac{\left[1 - \exp\left(-\frac{adt}{l_{\omega}}\right) \right] \left[1 - \exp\left(-\frac{1-a}{l_{\omega}} dt\right) \right]}{1 - \exp\left(-\frac{dt}{l_{\omega}}\right)} \left. \right\}. \quad (21)$$

We will first analyze several types of limit situations below.

When $a=1$, that is, a homogeneous superconductor wherein the entire multilayer film is S_1 material, the second term in the curly brackets in formula (21) is zero and formula (21) changes to

$$\langle f_{11} \rangle = (\pi k_B T) \sum_{\omega} \frac{1}{|\omega|}. \quad (22)$$

Based on de Gennes' transformation [4]:

$$(\pi k_B T) \sum_{\omega} \frac{1}{|\omega|} \rightarrow \ln \frac{1.14 \omega_D}{T_c}. \quad (23)$$

Formula (18) then changes into the T_c formula of the BCS theory

$$T_c = 1.14 \omega_D \exp\left(-\frac{1}{N V}\right), \quad (24)$$

In the formula, ω_D is the Debye frequency.

When $a=0$, the entire multilayered film is normal metal S_2 , the term within the curly brackets of formula (21) is zero and from formulas (14) and (15), $\Delta_1 = \Delta_2 = 0$ which is the expected result.

When each layer is very thin and $d \rightarrow 0$, the system approaches being a homogeneous system, the factor in the curly brackets of formula (21) $\rightarrow a$ and the T_c formula changes to

$$T_c = 1.14\omega_D \exp\left(-\frac{1}{aNV}\right). \quad (25)$$

This shows that the system is equivalent to a homogeneous superconductor with an equivalent coupling constant of (aNV) .

Under common conditions, by introducing a parameter $l\omega_0$, formula (21) changes to

$$(\pi k_B T) \sum_{\omega} \frac{1}{|\omega|} \{1 - \gamma\} = \langle f_n \rangle, \quad (26)$$

$$\gamma = \frac{l\omega_0}{ad} \int_0^{\infty} \frac{dt}{t^3} \frac{\left[1 - \exp\left(-\frac{adt}{l\omega_0}\right)\right] \left[1 - \exp\left(-\frac{1-a}{l\omega_0} dt\right)\right]}{1 - \exp\left(-\frac{dt}{l\omega_0}\right)}, \quad (27)$$

In the formulas, the selection of $l\omega_0$ should cause formula (26) to be equal to formula (21). In this way, the T_c formula can be written as

$$T_c = 1.14\omega_D \exp\left[-\frac{1}{(NV)_1(1-\gamma)}\right]. \quad (28)$$

By dividing formula (28) with $T_0 = 1.14\omega_D \exp\left[-\frac{1}{(NV)_1}\right]$, we obtain

$$\frac{T_c}{T_0} = \exp\left[-\frac{1}{(NV)_1} \cdot \frac{\gamma}{1-\gamma}\right]. \quad (29)$$

Using copper and niobium multilayered film as examples, Fig. 1 shows the relationship of $T_c/T_0 \sim a$ and $x(x=d/l_{\omega 0})$ as well as the $(NV)_1 \approx 0.3$ of the niobium.

When the curves in Fig. 1 are in $x \rightarrow \infty$, they all tend to approach 1. The curve corresponding to $a=0.2$ crosses with the longitudinal axis at 0.04 but this is not drawn in the figure.

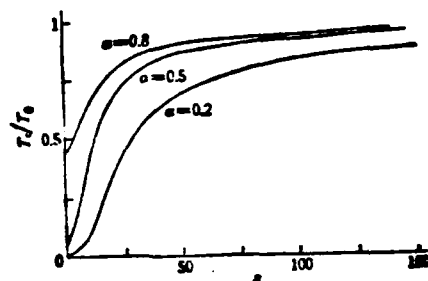


Fig. 1

In the above calculations we did not consider the special effects of the heterogeneous interfaces and therefore the results are basically the same as those of the common and simple S-N proximity effects. The T_c value of the entire multilayer film system is between the large material T_c values of the two types of metal. Therefore, if we find in the tests that the T_c value of the superconducting multilayer film has certain differences, for example, higher or lower than the large material T_c of each constituent element, then this is direct evidence of the influence of heterogeneous interfaces on the structures of the electrons.

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