

NAVAL POSTGRADUATE SCHOOL Monterey, California



TIME DEVELOPMENT OF CERENKOV RADIATION

Fred R. Buskirk and John R. Neighbours

May 1984

Technical Report

071

Approved for public release; distribution unlimited

Prepared for: Naval Sea Systems Command WASHINGTON, DC 20362

ITIC FILE COPY

NAVAL POSTGRADUATE SCHOOL Monterey, California

Commodore R. H. Shumaker Superintendent

David Schrady Provost

The work reported herein was supported by the Naval Sea Systems Command,

Reproduction of all or part of this report is authorized.

This report was prepared by:

Buskirk R. Professor of Physics

R. Neighbours

Professor of Physics

Reviewed by:

1

Released by:

G. E. Schacher, Chairman Department of Physics

Dyer

Dean of Science and Engineering

	REPORT DOCUMENTATION PAGE	
AEPORT NUMBER	2. GOVT ACCESSION NO.	3. RECIPIENT'S CATALOG NUMBER
NPS-61-84-006	10 113226	
. TITLE (and Subsiste)	VID/IAI IV FS	S. TYPE OF REPORT & PERIOD COVERED
Time Development of Cerenko	v	Mechanical Poport
Radiation		Technical Report
		6. PERFORMING ORG. REPORT NUMBER
		S. CONTRACT OR GRANT NUMBER(s)
Fred R. Buskirk		
John R. Neighbours		
D. PERFORMING ORGANIZATION NAME AND ADDRI Namal Doctoraduate School	E 3 \$	AREA & WORK UNIT NUMBERS
Monterey, California 93943		62768N
Monterey, currornia seste		N000248 WR10821
1. CONTROLLING OFFICE NAME AND ADDRESS		12. REPORT DATE
Naval Sea Systems Command		May 1984
PMS405		13. NUMBER OF PAGES
A MONITORING AGENCY NAME & ADDRESS/// diffe	rent trem Controlling Office)	18. SECURITY CLASS. (of this report)
	• • • •	
		Unclassified
		ISA. DECLASSIFICATION/DOWNGRADING
7. DISTRIBUTION STATEMENT (of the obstract enter	rod in Block 20, il dillorant fra	n Report)
7. DISTRIBUTION STATEMENT (of the abotract enter	rod in Block 20, il dillorani fra	n Roport)
7. DISTRIBUTION STATEMENT (of the obstract onto 8. SUPPLEMENTARY NOTES	rod in Block 20, il dillorant fra	n Report)
7. DISTRIBUTION STATEMENT (of the obstract onto	rod in Block 20, il dillorani tra	n Report)
7. DISTRIBUTION STATEMENT (of the obstract onto 8. SUPPLEMENTARY NOTES 9. KEY WORDS (Continue on reverse side if necessor)	rod in Block 20, il dillorani fra y and identify by block mambar)	n Report)
7. DISTRIBUTION STATEMENT (of the obstract enter 8. SUPPLEMENTARY NOTES 9. KEY WORDS (Continue on reverse side if necessary Cerenkov Radiation Polativistic clostron beam	red in Block 20, il dillerent fre y and identify by block number)	n Report)
7. DISTRIBUTION STATEMENT (of the obstract onto 8. SUPPLEMENTARY NOTES 9. KEY WORDS (Continue on reverse side if necessary Cerenkov Radiation Relativistic electron beam Radiation Field	rod in Block 20, il dillorent tru y end identify by block number) S	n Report)
7. DISTRIBUTION STATEMENT (of the obstract onto 8. SUPPLEMENTARY NOTES 9. KEY WORDS (Continue on reverse side if necessory Cerenkov Radiation Relativistic electron beam Radiation Field	rod in Block 20, if different free y and identify by block number) S	n Report)
7. DISTRIBUTION STATEMENT (of the obstract enter 8. SUPPLEMENTARY NOTES 9. KEY WORDS (Continue on reverse side if necessor) Cerenkov Radiation Relativistic electron beam Radiation Field	red in Block 20, il dillorent fre y and identify by block number) S	n Report)
7. DISTRIBUTION STATEMENT (of the obstract onto 8. SUPPLEMENTARY NOTES 9. KEY WORDS (Continue on reverse side if necessory Cerenkov Radiation Relativistic electron beam Radiation Field 0. ABSTRACT (Continue on reverse side if necessory	rod in Block 20, il dillorent tru y and identify by block number) S and identify by block number)	n Report)
7. DISTRIBUTION STATEMENT (of the obelifact enter 8. SUPPLEMENTARY NOTES 9. KEY WORDS (Continue on reverse olde if necessary Cerenkov Radiation Relativistic electron beam Radiation Field 9. ABSTRACT (Continue on reverse olde if necessary See attached	rod in Block 20, if different free y and identify by block mathem) S	n Report)
7. DISTRIBUTION STATEMENT (of the obstract enter 8. SUPPLEMENTARY NOTES 9. KEY WORDS (Continue on reverse side if necessory Cerenkov Radiation Relativistic electron beam Radiation Field 0. ABSTRACT (Continue on reverse side if necessory See attached	red in Block 20, il dillorani tru y and identify by block number) S and identify by block number)	n Report)
7. DISTRIBUTION STATEMENT (of the obstract enter 8. SUPPLEMENTARY NOTES 9. KEY WORDS (Continue on reverse side if necessor) Cerenkov Radiation Relativistic electron beam Radiation Field 9. ABSTRACT (Continue on reverse side if necessor) See attached	rod in Block 20, il dillorant tru y and identify by block number) S	n Report)
7. DISTRIBUTION STATEMENT (of the obeliact enter 8. SUPPLEMENTARY NOTES 9. KEY WORDS (Continue on reverse elde if necessor) Cerenkov Radiation Relativistic electron beam Radiation Field 9. ABSTRACT (Continue en reverse elde if necessor) See attached	rod in Block 20, il dillorent tru y and identify by block number) S and identify by block number)	n Report)
7. DISTRIBUTION STATEMENT (of the obelifact enter 8. SUPPLEMENTARY NOTES 9. KEY WORDS (Continue on reverse olde if necessory Cerenkov Radiation Relativistic electron beam Radiation Field 9. ABSTRACT (Continue on reverse olde if necessory See attached	rod in Block 20, if different free y and identify by block mathem) S	n Report)
2. DISTRIBUTION STATEMENT (of the obstract enter 3. SUPPLEMENTARY NOTES 3. KEY WORDS (Continue on reverse side if necessory Cerenkov Radiation Relativistic electron beam Radiation Field 3. ABSTRACT (Continue on reverse side if necessory See attached	rod in Block 20, il dillorant tru y and identify by block number) S and identify by block number)	n Report)
7. DISTRIBUTION STATEMENT (of the obelifact enter 8. SUPPLEMENTARY NOTES 9. KEY WORDS (Continue on reverse elde if necessary Cerenkov Radiation Relativistic electron beam Radiation Field 0. ADSTRACT (Continue on reverse elde if necessary See attached 0. ADSTRACT (Continue on reverse elde if necessary See attached	rod in Block 20, il dillorent ine y and identify by block mathem) S and identify by block mathem)	n Report)

de.

C

Ŕ

r

SECURITY CLASSIFICATION OF THIS PASE (ſ

t

(

TIME DEVELOPMENT OF CERENKOV RADIATION

Fred R. Buskirk John R. Neighbours

Physics Department Naval Postgraduate School Monterey, California 93943

ABSTRACT

Most developments of Cerenkov Radiation are in terms of the Fourier components of the fields and power emitted by a single electron. When many electrons in a compact bunch are emitted from an accelerator, the bunch radiates coherently and at a lower frequency than for a single electron. The theory for the time structure of the fields arising from a charge bunch is developed, and it is shown that the source of the radiation is di/dt. Present detector technology should be able to resolve these fields. \leq

Accession For	l
NTIS GRA&I DTIC TAB Utennounced I Justification	
By Distribution/	
Availability Codes	
Avail and/or Dist Special	

TIME DEVELOPMENT OF CERENKOV RADIATION

INTRODUCTION

Cerenkov radiation, produced by a charge or group of charges, moving faster than the speed of electromagnetic radiation in a medium, has been investigated, starting with the experiments of Cerenkov¹ in 1934 and the explanation by Frank and Tamm² in 1937. Since power radiated by a single charged particle is proportional to the frequency, most of the research effort has been devoted to the relatively intense optical radiation which is favored over the microwave region by a factor of about 10⁴. The optical results^{3,4} are given in terms of the Fourier components of the fields and the radiated power.

In our previous work^{5,6} it was noted that microwave radiation can be significant because all the electrons in an accelerator bunch (about 10⁹) radiate coherently; an effect which more than offsets the single particle increase in radiated power with frequency. For an electron beam generated by a traveling wave Linac and passing through air, it was shown that the various harmonics of the basic frequency up to about the tenth are emitted. (In the case of an L or S band Linac, these correspond to 10 GHz and 30 GHz respectively.)

The time structure of Cerenkov radiation fields in the optical and even in the higher frequency microwave regions is difficult to observe because the detectors register power. One of the few

treatments of the time dependence, by Tamm⁷ in 1939, showed that the optical radiation by an electron is singular on the Cerenkov front. Here we consider the time structure of fields generated when electron bunches radiate coherently; in a development which complements the frequency domain analysis of our earlier work ^{5,6}.

The fields should be observable for beams from induction accelerators which produce bunches much longer than those produced by S or L band Linacs.

MAGNETIC RADIATION FIELD

ł

The purpose of this paper is to present a development of the time dependence of the electric field generated by the Cerenkov mechanism. The method is first to determine the potentials from the moving charge distribution, and subsequently to obtain the fields (in cgs units) from the potentials by

$$\vec{B} = \nabla \times \vec{A} \tag{1}$$

$$\vec{E} = -\nabla \hat{v} - \frac{1}{c_0} \frac{\partial \vec{A}}{\partial t}$$
(2)

We assume a charge density function ρ_v and a current density $\dot{J}_v = \rho_v \dot{v}/c_0$ with the velocity \dot{v} in the plus z direction. The charge and current are assumed to be concentrated along the z axis such that

$$\rho_{r}(\vec{r}, t) = \rho(z, t) \, \delta(x) \, \delta(y) \tag{3}$$

and the charge is assumed to move with no change in shape so that the z and t dependence of the charge is

$$\rho(z,t) = \rho_{o}(z-vt) \tag{4}$$

Note that ρ_v and j_v represent the usual charge and current densities, while ρ and ρ_o throughout this paper are charge per unit length. The velocity of light is c and c_o in the medium and free space, respectively.

The potentials are found by taking the usual retarded solutions to the wave equations; which become under the assumption of a line distribution of charge (3),

$$\varphi(\mathbf{\dot{r}}, t) = \varepsilon^{-1} \int \mathbb{R}^{-1} \rho(\mathbf{\dot{r}}', t') dz'$$
(5)

$$\vec{A}(\vec{r},t) = \frac{\vec{v}}{c_0} \int R^{-1} \rho(r',t') dz'$$
 (6)

where $\vec{R} = \vec{r} - \vec{r}'$ and t' is the retarded time

$$t' = t - |\vec{r} - \vec{r}'|/c$$

Now (4), the assumption of rigid motion of the charge distribution, can be incorporated into the potentials, and a new variable u(z') = z' - vt' can be introduced so that the potentials (5) and (6) become

$$\Phi(\vec{r}, t) = \epsilon^{-1} \int R^{-1} \rho(u) dz'$$
(8)

$$\vec{A}(\vec{r},t) = \frac{\vec{v}}{c_0} \int R^{-1} \rho_0(u) dz!$$
 (9)

Also, since the charge is confined to the z' axis, the new variable u(z') can be written more explicitly.

$$u(z') = z' - vt + \frac{v}{c} [x^2 + y^2 + (z - z')^2]^{1/2}$$
 (10)

The magnetic field \vec{B} may be calculated from (1) and since \vec{A} has only a z-component, \vec{B} has only the x and y components, $B_x = \frac{\partial}{\partial y} A_z$ and $B_y = -\frac{\partial}{\partial x} A_z$. Carrying out the differentiation for the x component gives

$$B_{\mathbf{x}} = \frac{\mathbf{v}}{\mathbf{c}_{0}} \int \frac{\partial}{\partial \mathbf{y}} \mathbf{R}^{-1} \rho_{0}(\mathbf{u}) d\mathbf{z}'$$

$$+ \frac{\mathbf{v}}{\mathbf{c}_{0}} \int \mathbf{R}^{-1} \frac{\partial}{\partial \mathbf{y}} \rho_{0}(\mathbf{u}) d\mathbf{z}'$$
(11)

For radiation, the first integral, falling off as R^{-2} at large distances, will be neglected and only the second term will be considered further. From (10), it is seen that u is a function of x and y so that the second integral can be written

$$B_{\mathbf{x}} = \frac{\mathbf{v}^2}{cc_0} \int \frac{\mathbf{y}}{\mathbf{R}^2} \rho_0'(\mathbf{u}) d\mathbf{z}' \qquad (12)$$

where $\rho_0'(u)$ is the derivative of ρ_0 with respect to its argument u. The corresponding expression for B_y has y replaced by (-x). These two components can be combined to give the total magnetic radiation field \vec{B} . In the cylindrical coordinates, (s, 9, z) where s is the radius vector $s = (x^2 + y^2)^{1/2}$, \vec{B} is tangential (i.e. in the $\hat{\theta}$ direction) with a magnitude given by

$$B = \frac{v^2}{cc_0} \int \frac{s}{R^2} \rho_0'(u) dz' \qquad (13)$$

TIME DEVELOPMENT

In order to evaluate (13) for B, it is necessary to consider the dependence of u on z' as given in (10). In the u-z' plane, the first two terms are a straight line with unit slope and an intercept which changes with time, while the third term is a hyperbola opening in the +u direction with asymptotic slopes of $\pm \frac{v}{c}$. The sum of these two curves is u(z'). In the Cerenkov case with v > c, the result is a curve whose ends both point upward as shown in Fig. 1. As time increases, the entire curve will translate downward to smaller u values as a result of the negative second term in (10).

Only changing currents (those with a non zero ρ_0 ' will contribute to the magnetic radiation field (13). To proceed and demonstrate the method, a ramp-front current pulse is chosen as a simple example. Assuming that the front end of a current pulse increases linearly up to a constant value, the derivative $\rho_0'(u)$ will be a constant valued square pulse of magnitude ρ_m' as is also shown in Fig. 1. The corresponding negative $\rho_0'(u)$ pulse occurring at the tail of a current pulse is not shown and its effect is considered separately.

For large negative times, the u(z') curve (a) is completely above the pulse-like non zero portion of the $\rho_0'(u)$ curve so that the contribution in (13) to B from $\rho_0'(u)$ is zero and therefore, B is zero. As time increases, the u(z') curve moves downward until the B pulse begins when u(z') is tangent (curve b) to the upper portion of the $\rho_0'(u)$ pulse. The value

of the integral in (13) increases as u(z) continues its constant downward motion with increasing time until u(z')becomes tangent (curve 3) with the lower part of the $\rho_0'(u)$ pulse. At this time the non zero part of the integral has the largest extent -from z_1 to z_2 . At later times, the integral breaks into two regions of the z' axis and if $\rho_0'(u)$ is constant, t e value of the integral decreases with increasing time because the extent of the integral in the two regions continues to decrease as a result of the upward turn of u(z').

This calculation may be carried further to determine the time structure (shape) of the resulting B pulse. Although the expression (13) for B can be integrated directly in the case where the slope $\rho_0'(u)$ is constant, it is instructive be carry out the calculation by developing u in a power series Denoting z_0' as the value of z' at which u(z') has zero slope, the values of z_0' , $u(z_0')$ and the second derivative are

$$z_{o}' = -s \left(\frac{v^{2}}{c^{2}} - 1\right)^{-1/2}$$
 (14)

$$u(z_{o}') = s\left(\frac{v^{2}}{c^{2}}-1\right)^{-1/2} - \dot{v}t$$
 (15)

$$\frac{\partial^2 u}{\partial z'^2} \Big|_{z_0} = \frac{1}{s} \frac{c^2}{v^2} \left(\frac{v^2}{c^2} - 1 \right)^{3/2} \equiv 2 A \qquad (16)$$

so that u can be expressed as a power series about the minimum

$$u = u(z_0') + A(z' - z_0')^2$$
(17)

The limits z_1' and z_2' can be written in terms of the minimum value as $z'_2 = z_0' + \Delta z$ and $z_1' = z_0' - \Delta z'$ where $\Delta z'$ is the value of $z'-z_0'$ such that the difference $u(z') - u(z_0') = a$, the width of the current derivative pulse v_0' . Then from (17), $a = A(\Delta z')^2$ or

$$\Delta z' = (a/A)^{1/2}$$
(18)

Using this value, the maximum magnetic radiation field for the rising front of the magnetic field pulse is easily evaluated from (13) under the assumption that s and R are slowly varying to give

$$B_{max} = \frac{v^2}{cc_o} \frac{s}{R^2} \rho_m' 2\left(\frac{a}{A}\right)^{-1/2}$$
(19)

Values of B for the rise up to the peak value given above are found by the same process but using appropriately smaller values of $\Delta z'$. The result is that the integral (and therefore B) increases as $t^{1/2}$ after the onset of the pulse. After the maximum magnetic field is reached, the integral splits into two parts. If the expression on the right side of (19) is called I(a), the value of B at later times becomes

$$B = I(a' + a) - I(a') .$$
 (20)

where a' is the distance by which the minimum in u(z') is below the lower step of the ρ_0 ' pulse in Fig. 1. The first term in (20) increases slowly with a', but the second term decreases as $(a')^{1/2}$ leading to the sharp fall off of the magnetic field after the maximum as shown in Fig. 2.

A complete current pulse may be considered as a linear rise, followed by a constant current, and then a linear decrease. The latter part gives rise to a negative $\rho'(u)$ and a reversed magnetic field pulse so that the magnetic field for a complete current pulse has the double peaked structure shown in Fig. 2.

ELECTRIC RADIATION FIELD

In a manner similar to the derivation of (13), the electric radiation field may be found from (2), (8), and (9). The details are omitted, but the result is

$$\vec{E} = -\frac{v}{c_o} \int \left(\frac{\vec{R} c}{R c_o} - \frac{\vec{v}}{c_o}\right) \frac{1}{R} \rho_o'(u) dz' \qquad (21)$$

The direction of \vec{E} may be determined from the following considerations. If \vec{R} is assumed approximately constant and denoted by \vec{R}_{m} in the region which contributes most strongly to the integral, then

$$\vec{E} \cdot \frac{\vec{R}}{R} = \vec{E} \cdot \frac{\vec{R}}{R_m} = I \left(1 - \frac{\nabla}{c} \cos\theta\right)$$
(22)

where I represents the integral in (21) without the factor in parenthesis and θ is the angle between \mathbf{R}_{m} and the z axis. But the value of \mathbf{R}_{m} in the region which contributes to the integral is found by evaluating the general expression (21) at $\mathbf{z}' = \mathbf{z}_{0}'$. To simplify the expression, let the observer be at $\mathbf{z} = \mathbf{0}$ and also assume that the ρ_{0}' pulse is centered near $\mathbf{u} = \mathbf{0}$. Then $\mathbf{R}_{m} = (\mathbf{s}^{2} + \mathbf{z}'^{2})^{1/2}$ may be evaluated using (14) to give

$$R_{m} = s\left(1 - \frac{c^{2}}{v^{2}}\right)^{-1/2}$$
(23)

If the usual Cerenkov angle is defined as $\cos \theta_{\rm C} = \frac{\rm C}{\rm v} + \frac{\rm R}{\rm m}$ can be written as

$$R_{m} = \frac{s}{\sin \theta_{C}}$$
(24)

From (22) it is apparent that \vec{E} is perpendicular to \vec{R}_{m} when $\vartheta = \vartheta_{C}$ and (24) shows that \vec{R}_{m} is the value of \vec{R} at the Cerenkov angle ϑ_{C} . Thus, the electric field from the front of the pulse (i.e., $z' = z_{m}$) is transverse to \vec{R}_{m} .

The situation is clarified in Fig. 3. The charge, traveling from left to right, emits a signal from A, which travels to the the observer at O, traversing a distance R_m . The observer is at z = o and a distance s from the path. The field \vec{E} is perpendicular to \vec{R}_m . The signal was emitted from A at an earlier time t' in order to arrive at O at the time t, with $c(t-t') = R_m$. By the time the signal reaches O, the particle is at B, with D = v(t-t'). Then $R_m/D = c/v = \cos\theta_c$ as expected. D is the path length from A to B.

From Fig. 3, one should also note that the field is transverse to \vec{R}_m , which points from the earlier (retarded time) position of the particle, and is radial relative to the present position of the particle. The former condition holds for typical dipole radiation, while the latter condition holds for the Lienard-Wiechart field for a particle moving with v < c. The Lienard-Wiechart fields fall off as the inverse square of the distance, and do not represent radiation. In contrast, the

fields discussed here fall off more slowly than R^{-1} and represent radiation; and the total radiated power is discussed in the next section.

RADIATED POWER

The energy radiated may be found by calculating the Povnting vector and integrating over a surface. If the surface is a cylinder centered on the z axis, the fields at a given time have a pattern independent of angle and a z dependence as shown in the top curve of Fig. 2. The Povnting vector is, of course, along \vec{R}_m , and the outward component may be integrated over the cylinder to give the total power radiated. As a crude estimate for the integral, replace the field by the peak field (19) and let the spatial width of the pulse be a. The radiated power is then

$$P(approx) = \frac{R}{c^2} v I_o^2 \sin^2\theta_c$$
(25)

in cqs units. In the mks system, the square bracket is replaced by $2\mu_0/\pi$.

In the earlier calculations,^{5,6} the fields and power were expressed in terms of Fourier amplitudes. If the same current pulse is assumed, P_{ω} has frequency components up to the value of ω such that the wave length of the radiation is equal to the pulse length. If it is assumed that P_{ω} rises linearly up to this frequency and suddenly drops, the total power radiated becomes (in Mks units)

$$[P_{\omega} = \frac{\pi}{2} \mu_{0} v I_{0}^{2} \sin^{2}\theta_{c}$$
 (26)

Equations (25) and (26) are both rough estimates and the point is that the similarity of the results is asserted to be confirmation that the calculations in this paper represent the Cerenkov radiation, here expressed in terms of time dependence of the fields.

DISCUSSION

In preceding sections, the time structure of the electric and magnetic radiation fields was developed. Only the far fields were retained and in the development leading to the B field (13), and the E field (21), only the assumption of a rigid charge confined to a line was introduced. It is seen from these equations that the time derivative of the current is the source function.

The simple model chosen to demonstrate the method of developing the time structures was that of a uniform charge distribution with uniformly varying front and rear sections. This model gives the square pulse charge derivative of height p'_m shown in Fig. 1 which is easy to use in evaluating the integral (13). Similar remarks hold for the power series expansion of u(z') which is an increasingly better approximation as the time during which the current is changing, decreases. Current variations other than linear may be readily incorporated within the framework given. Also it should be noted that in all cases the variation of R^{-2} in (13) which was assumed constant in the example will tend to sharpen both the leading and trailing edges of a field pulse.

In the evaluation of the time structure of the fields, the peak field arose when the integral (13) had the most widely spaced limits; a situation which occurs because u(z') has a negative slope for sufficiently negative values of (z' - z) as

shown at the left side of Fig. 1. In the non-Cerenkov case $(\frac{v}{c} < 1)$ this situation does not arise since then the slope of the u(z') function always has the same sign. In this case (i.e. v < c) the u(z') curve bends downward instead of upward for large negative values of (z' - z) and the only contribution to the integral (13) is from small regions of z'.

These results show how the time structure of Cerenkov radiation arises from the time rate of change of the charge distribution in an electron bunch. Present technology is such that this structure is not observable in the Cerenkov radiation from S or L band Linacs because of their relatively high fundamental frequency. However, induction accelerators with their longer electron bunch structure should produce Cerenkov signals in air for energies greater than about 25 Mev, which should be observable.

The extension of this method of calculation of the fields for both Cerenkov and sub-Cerenkov charge velocities is easily made for cases for which the charge derivative $\rho'(u)$ is not constant. A detailed report is under preparation.

Finally, we note that although the results of other workers 4,7 often have singularities in the radiated power at the Cerenkov angle, the present results and our previous ones 5,6 show that the radiated power is finite whether calculated in the frequency or time domain. Also it should be noted that causality is satisfied because the fields are zero at times earlier than the leading edge of the pulse shown in Fig. 2.

This work was supported by the U.S. Naval Postgraduate School Foundation Research Program and the Naval Surface Weapon Center, White Oak, Maryland.

L

REFERENCES

1.	P. Cerenkov, Dokl. Akad. Nauk. SSSR 2 451 (1934).
2.	I. M. Frank and I. Tamm, Dokl. Akad. Nauk. SSSR 14 107
	(1937).
3.	J. V. Jelley, "Cerenkov Radiation and Its Applications"
	(Pergamon, London, 1958).
4.	V. P. Zrelov, "Cerenkov Radiation in High Energy Physics",
	(Atomizdat, Moscow, (1968); translation: Israel Program
	for Scientific Translations, Jerusalem, (1970)).
5.	F. R. Buskirk and J. R. Neighbours, Phys. Rev. <u>A 28</u> ,
	1531 (1983).
6.	J. R. Neighbours and F. R. Buskirk (To be published in
	Phys. Rev. <u>A 29</u> , June (1984).
7.	I. Tamm, J. Phys SSSR <u>1</u> 439 (1939).

ł

1

FIGURE CAPTIONS

- Figure 1. The function u = z' vt', defined in the text is plotted for increasing times t_1 , t_2 , t_3 at the point of observation. The corresponding current derivative profile, on the right, is a function of u only and remains fixed in time. The field signal pulse starts at t_1 , and reaches a maximum at t_3 .
- Figure 2. The electric field pulse generated by the beam current profile, shown in the lower curve.
- Figure 3. Geometrical relations for the Cerenkov pulse. The source (ρ_0') at A emits a signal at an early time giving the \vec{E} field at the observer 9; when the field reaches the observer, the particle is at B.



Figure 1.







DISTRIBUTION LIST

1 Office of Naval Research CDR R. Swafford 800 N. Quincy Street Arlington, VA 22217 1 Office of Naval Research CDR James Offutt 1030 East Green Street Pasadena, CA 91106 2 Library Code 0142 Naval Postgraduate School Monterey, CA 93943 2 Office of Researach Administration Code 012A Naval Postgraduate School Monterey, CA 93943 20 F. R. Buskirk & J. R. Neighbours Naval Postgraduate School Physics Department, Code 61 Monterey, CA 93943 1 Dr. Thomas Starke M4, M.S. P942 Los Alamos National Laboratory Los Alamos, NM 87545 1 MAJ E. W. Pogue M4, M.S. P942 Los Alamos National Laboratory Los Alamos, NM 87545 1 Dr. Charles Bowman D442 Los Alamos National Laboratory Los Alamos, NM 87545 1 Dr. Thomas Fessenden L-436 Lawrence Livermore National Laboratory Box 808 Livermore, CA 94550

Dr. Richard Briggs L-321 Lawrence Livermore National Laboratory Box 808 Livermore, CA 94550 2

3

1

1

1

2

2

Dr. C. M. Huddleston R-401 Naval Surface Weapons Center White Oak Silver Spring, MD 20910

CAPT R. L. Topping PMS 405 Strategic Systems Project Office Naval Sea Systems Command Washington, D.C. 20376

ľ.

þ

Dr. David Merritt PMS 405 Strategic Systems Project Office Naval Sea Systems Command Washington, D.C. 20376

CDR William Bassett PMS 405 Strategic Systems Project Office Naval Sea Systems Command Washington, D.C. 20376

Director, Defense Advanced Research Project Agency ATTN: LCOL Richard A. Gullickson 1400 Wilson Blvd. Arlington, VA 22209

Defense Technical Information Center Cameron Station Alexandria, Virginia 22314