

AD-A142 274

RESEARCH ON NONLINEAR CONTROL THEORY (U) JOHNS HOPKINS  
UNIV BALTIMORE MD DEPT OF ELECTRICAL ENGINEERING AND  
COMPUTER SCIENCE W J RUGH MAR 84 AFOSR-TR-84-0460  
AFOSR-83-0079 F/G 5/8

NL

UNCLASSIFIED



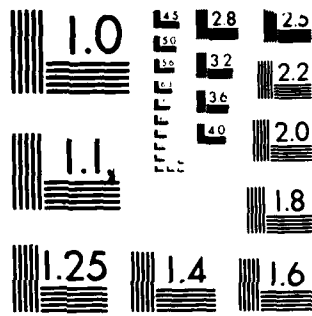
END

DATE

FILMED

7-84

DTIC



MICROCOPY RESOLUTION TEST CHART  
NATIONAL BUREAU OF STANDARDS 1963-A

AFOSR-TR- 84-0460

4

RESEARCH ON NONLINEAR CONTROL THEORY

AD-A142 274

Wilson J. Rugh  
Department of Electrical Engineering and Computer Science  
The Johns Hopkins University  
Baltimore, Maryland 21218

ANNUAL SCIENTIFIC REPORT

under

Grant Number AFOSR-83-0079

for the period

1 March 1983 through 29 February 1984

JUN 20 1984

ABSTRACT

This annual report briefly describes progress on research in non-linear control theory. Results reported include characterizations of the family of linearizations about constant operating points of non-linear systems described by transform-domain Volterra series, explicit formulas for the linearization of an interconnected system in terms of subsystem linearizations, and a characterization for linearization by feedback. Publications describing these results in detail are listed.

DTIC FILE COPY

Approved for public release:  
distribution unlimited.

84 06 19 038

## 1. RESEARCH OBJECTIVES AND STATUS

The objective of this research effort involves making use of recent developments in the representation and realization theories for nonlinear systems to address the problem of nonlinear feedback control. In particular, the objective is to characterize in explicit, input-output terms the relationships between open and closed-loop systems, and to use this characterization to develop more effective analysis and design techniques for nonlinear control systems.

Since the current, standard method for nonlinear system design is based on linearization of the nonlinear system equations, initial research toward the objective has focused on the relationship of a nonlinear system to its family of linearizations about a range of constant operating points. Using a transform-domain Volterra series representation for input-output behavior, a representation that appears to be suited to a wide range of flight control systems, explicit relationships have been developed for the parameterized transfer function that describes the family of linearizations. From these relationships, it is sometimes possible to describe simply the information about the nonlinear system embodied in the family of linearizations, or to see how certain structural characteristics of the nonlinear system can be ascertained from the form of the linearized transfer function. Also, it is easy to note various situations in which the linearization carries no useful information about the nonlinear system, so that design by linearization is doomed. For example, the linearization transfer function can be identically zero for non-trivial nonlinear systems. These results are reported in detail for discrete-time systems in [1], and for continuous-time systems in [2] and [3]. (These numbers refer to the publications listed in Section 2 of this report.)

A second step in the investigation was to develop the explicit relationship between the linearization of an interconnected nonlinear system and the subsystem linearizations, particularly for the feedback connection. While these relationships have been, in a vague sense, understood for some time, the explicit formulas obtained indicate more clearly the interaction between the operating point and the linearized system, i.e., how the linearized closed-loop system depends on the operating point. This is a key feature that limits the range of validity of a linearized design, since the linearization typically is accurate only in a neighborhood of a particular operating point. One interesting observation is that classical techniques of control system design that rely on the relationship between the linear open- and closed-loop systems must be used with great care in design-by-linearization settings. This is because the operating point value changes the relation of the open- and closed-loop systems. This work is reported in detail in [2].

The next step in this line of research is to use these results to propose better design methods than the standard design-by-linearization methods. To this end a promising method for extending the range of validity of linearized designs has been found, and this forms the basis for continuing work to be reported in due course.

AIR FORCE OFFICE OF SCIENTIFIC RESEARCH (AFSC)  
NOTICE OF TECHNICAL INFORMATION TO DTIC  
This report is available to the public and is  
approved for release under E.O. 1190-12.  
Distribution is unlimited.  
MATTHEW J. KERFER  
Chief, Technical Information Division

Another line of research has involved relating the ideas described above to recent results by G. Meyer, R. Su, and L. R. Hunt on linearization by feedback, and its application to flight control. In this approach nonlinear feedback can be used, in certain cases, to achieve a linear closed-loop system, so that further design can be performed using linear-system methods. A characterization for linearization by feedback in terms of transform-domain Volterra series representations has been obtained, and is reported in [4].

Finally, some effort has been devoted to developing a nonlinear-system simulation capability in anticipation of the need to evaluate and verify proposed design methods. In the course of this effort, results for a recently proposed nonlinear control scheme for flight control at high angles of attack were verified, and in part corrected.

## 2. PUBLICATIONS

[1] R. Lejeune and W. J. Rugh, "Linearization of Discrete-Time Polynomial Systems About Constant Operating Points," Proceedings of the 17th Annual Conference on Information Sciences and Systems, The Johns Hopkins University, Baltimore, MD, pp. 422-426, 1983.

[2] W. J. Rugh, "Linearization About Constant Operating Points: An Input-Output Viewpoint," Proceedings of the 22nd IEEE Conference on Decision and Control, San Antonio, TX, pp. 1165-1169, 1983.

[3] R. Lejeune and W. J. Rugh, "Linearization of Nonlinear Systems About Constant Operating Points," IEEE Transactions on Automatic Control, accepted for publication, 1984.

[4] W. J. Rugh, "An Input-Output Characterization for Linearization by Feedback," Systems and Control Letters, accepted for publication, 1984.

## 3. PERSONNEL

Principal Investigator:

Wilson J. Rugh

Research Assistants (Graduate Students):

Roland Lejeune; BS, Ecole Centrale des Arts et Metiers, Belgium, MS, University of Virginia

William Baumann; BS, Lehigh University, MS, MIT

## 4. INTERACTIONS

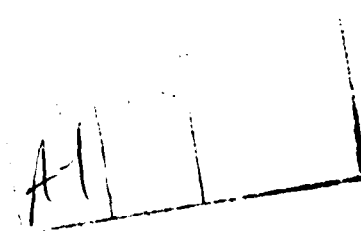
The publications in Section 2 were presented as follows.

[1] was presented at the Conference on Information Sciences and Systems, Baltimore, MD, on 24 March 1983.

[2] was presented as an invited paper at the IEEE Conference on Decision and Control, San Antonio, TX, on 15 December 1983.

[3] was presented at a research seminar in the Department of Electrical Engineering, University of Maryland, College Park, MD, on 8 March 1983.

[4] will be presented at the Conference on Information Sciences and Systems, Princeton, NJ, on 14 March 1984.



UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE

REPORT DOCUMENTATION PAGE

1a. REPORT SECURITY CLASSIFICATION UNCLASSIFIED		1d. RESTRICTIVE MARKINGS	
2a. SECURITY CLASSIFICATION AUTHORITY		3. DISTRIBUTION/AVAILABILITY OF REPORT Approved for public release; distribution unlimited.	
2b. DECLASSIFICATION/DOWNGRADING SCHEDULE			
4. PERFORMING ORGANIZATION REPORT NUMBER(S)		5. MONITORING ORGANIZATION REPORT NUMBER(S) <b>AFOSR-TR. 84-0460</b>	
6a. NAME OF PERFORMING ORGANIZATION Johns Hopkins University	6b. OFFICE SYMBOL (If applicable)	7a. NAME OF MONITORING ORGANIZATION Air Force Office of Scientific Research	
6c. ADDRESS (City, State and ZIP Code) Department of Electrical Engineering and Computer Science, Baltimore MD 21218		7b. ADDRESS (City, State and ZIP Code) Directorate of Mathematical & Information Sciences, Bolling AFB DC 20332	
8a. NAME OF FUNDING/SPONSORING ORGANIZATION AFOSR	8b. OFFICE SYMBOL (If applicable) NM	9. PROCUREMENT INSTRUMENT IDENTIFICATION NUMBER AFOSR-83-0079	
8c. ADDRESS (City, State and ZIP Code) Bolling AFB DC 20332		10. SOURCE OF FUNDING NOS.	
		PROGRAM ELEMENT NO. 61102F	TASK NO. A1
11. TITLE (Include Security Classification) RESEARCH ON NONLINEAR CONTROL THEORY		PROJECT NO. 2304	WORK UNIT NO.
12. PERSONAL AUTHOR(S) Wilson J. Rugh			
13a. TYPE OF REPORT Interim	13b. TIME COVERED FROM 1/3/83 TO 29/2/84	14. DATE OF REPORT (Yr., Mo., Day) MAR 1984	15. PAGE COUNT 4
16. SUPPLEMENTARY NOTATION			
17. COSATI CODES		18. SUBJECT TERMS (Continue on reverse if necessary and identify by block number)	
FIELD	GROUP	SUB GR	
		Control theory, nonlinear systems, Volterra series.	
19. ABSTRACT (Continue on reverse if necessary and identify by block number) This annual report briefly describes progress on research in nonlinear control theory. Results reported include characterizations of the family of linearizations about constant operating points of nonlinear systems described by transform-domain Volterra series, explicit formulas for the linearization of an interconnected system in terms of subsystem linearizations, and a characterization for linearization by feedback. Publications describing these results in detail are listed.			
20. DISTRIBUTION/AVAILABILITY OF ABSTRACT UNCLASSIFIED/UNLIMITED <input checked="" type="checkbox"/> SAME AS RPT. <input type="checkbox"/> DTIC USERS <input type="checkbox"/>		21. ABSTRACT SECURITY CLASSIFICATION UNCLASSIFIED	
22a. NAME OF RESPONSIBLE INDIVIDUAL Dr. John A. Burns		22b. TELEPHONE NUMBER (Include Area Code) (302) 767- 5028	22c. OFFICE SYMBOL NM

**DAT  
FILM**