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# THESIS

SIMTBED a Graphical Test Bed for Analyzing and Reporting the Results of a Statistical Simulation Experiment

by

Hans-Walter Drueg

September 1983

Thesis Advisor:

P.A.W. Lewis

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Naval Postgraduate School Monterey, California 93943				
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SIMTBED a Graphical Test Bed for Analyzing and Reporting the Results of a Statistical Simulation Experiment

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Hans-Walter Drueg Major, German Air Force Ing.(grad.), Hochschule der Bundeswehr Muenchen, 1974

Submitted in partial fulfillment of the requirements for the degree of

MASTER OF SCIENCE IN OPERATIONS RESEARCH

from the

NAVAL POSTGRADUATE SCHOOL September 1983

Jans. Lotter Author: Approved by: Thesis Advisor Second Reader Chairman, Department of **Operations** Research K.T. Dean of Information and Policy Sciences

# ABSTRACT

A graphical test bed in which the results of a simulation experiment can be reported and analyzed is described. The test bed is based on the regression adjusted graphics and estimation methodology developed by Heidelberger and Lewis [Ref. 1] for regenerative simulation. From the graphics and associated numerics, the experimenter can summarize and see simultaneously relative properties, such as bias, normality and standard deviation, of several estimators of a characteristic of a population for up to 8 sample sizes. The evolution of these properties with sample size is also displayed. The graphics is supported on a line printer to make it and the program portable. The technique is illustrated by examples concerning the effects of changes in data distribution on the behavior of the lag one serial correlation coefficient, the estimation of the shape parameter of Gamma random variables and a comparison of different methods (jackknife, bootstrap) for estimating the standard error of an estimator.

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#### ACKNOWLEDGEMENTS

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I wish to acknowledge three people who contributed to my thesis research. First is Professor P.A.W. Lewis who was my thesis advisor. His time and his advice was always available. His support contributed a great deal to the increase of my knowledge and the completion of this the 's for which I am grateful.

Second I would like to thank Professor E.J. Orav wh was always available to answer questions and to discuss unsolved problems. His advice was especially valuable to me in running and interpreting the output of the example program runs.

Third, but not last, I wish to thank L. Uribe who had always time and patience to discuss programming problems. He contributed the "SIMTB3" FORTRAN program which is part of this thesis.

# I. SYNOPSIS

#### SIMTBED

THE PROGRAM:

Portable FORTRAN program using printer plot graphics

(3 different program versions)

Program will run on:

IBM

VAX

IBM PC

etc.

ca. 900 lines of FORTRAN Code

Memory requirements:

SIMTB1 1 M Bytes

SIMTB2 1 M Bytes

SIMTB3 0.5 M Bytes

(may slightly differ with different type of estimator functions and subsample sizes)

**PURPOSES:** 

- To explore the distribution of a statistical estimator
- To see how that distribution changes with sample size
- To compare that distribution with the distribution of competing estimators

THE USER SUPPLIES:

A. Optional Parameters:

NE(1),NE(2),...,NE(8) = Subsample Sizes (maximum is 8)
The estimator is computed based on NE(i) data points
N = Total Number of simulated data points per

replication

At Subsample Size NE(i), there are [N/NE(i)] independent values of the estimator

M = Number of Replications When all replications have been run, there are M\* [N/NE(i)] independent values of the estimator at each NE(i)

D = Degree of Regression (maximum D = 3)

L = Number of Subsample Sizes (maximum L = 8) GRAPHICS and SCALING options

B. Data:

A total of M\*N simulated data values are needed. In SIMTBl and SIMTB2 the same data is used at each subsample size (NE(i)). In SIMTB3 new data is always generated.

C. Estimators:

Up to 3 FORTRAN functions (i.e. Estimators) are needed. They must accept as inputs a data subsample and the size of that subsample. They must return one value of the estimator for that subsample.

SIMTBED PRODUCES:

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- A one page graphical output (box plots) at each subsample size
- Numerical Summaries at each subsample size (mean,
   Std. Dev., Std. Dev. of the mean, skewness, kurtosis)

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 Regressions to quantify changes in the mean and variance as subsample size changes

#### II. INTRODUCTION

SIMTBED, with the different versions (SIMTB1, SIMTB2 and SIMTB3) is a graphical display program. The program is based on the program RAGE [Ref. 2]. It is used, with simulated data, on a digital computer. The program can be used to examine statistical estimators of different type, or properties of a single estimator under different distributional assumptions. The distribution of the estimator can be explored for given sample sizes and the properties can be compared for different sample sizes. The estimation conditions are controlled by the experimenter. It is also possible to examine the effects of changes in the underlying distribution of the data.

When the program SIMTB1 or SIMTB2 is used with simulated data, the data is assumed to be independent and identically distributed (iid). This iid data can be sectioned into M independent blocks of specified sample size N. The sample of size N, will be sectioned into smaller subsample of size NE(k). The estimates are then calculated from this subsample of size NE(k).

One salient feature of the program versions SIMTB1 and SIMTB2 is that they use the same batch of simulated random variables to explore the properties of all the estimators at the various subsample sizes. This is done for economy

and could be important on slow computers; the price paid is that the regression analysis provided by SIMTB1 and SIMTB2 of its graphical output is performed on correlated samples.

The version SIMTB3 uses one dimensional data and does not have this repetition feature. New data is used for each calculation of each estimator at each subsample size. The data is generated when the estimator function is called and only the needed batch of the exact subsample size is generated. This technique reduces the memory requirements.

Moreover all data sets are uncorrelated and a much more precise correlation can be performed if required. But this technique increases the computer time.

To use the program it is necessary only to define the optional parameters (see Section IV), supply the simulated random variables or a batch of data points, and provide the FORTRAN functions for the calculation of the estimators which are of interest. The program itself will subdivide the input data and feed the data properly into the functions, scale the graphic display, produce boxplots and summary statistics. A regression will be computed for the mean and variance of each estimator based on inverse subsample size. The result of the regression is displayed graphically and numerically.

The program is written in ANSI Standard FORTRAN (X3.9-1966) and extensively tested on an IBM 3033 computer using FORTRAN IV (H Extended) or FORTRAN IV (G1) compilers. The

program SIMTBED (all versions) provides all subroutines used inside the program. Besides the estimator functions, the user has to provide NO additional subroutines via packages like IMSL. The program should be totally portable; it has been tested under FORTRAN 77 on a VAX 11/780. The only limitation is the available memory.

# III. GENERAL IDEA AND DATA STRUCTURE OF THE PROGRAM

The main purpose of SIMTBED, with the different versions, is to explore the distributional behavior of estimators and show their properties in a graphical and numerical display. All versions use the same ideas, they only differ in the type of data and the way the data is used inside the program.



Figure 1. Sectioning of the Data into M\*N Sections

To study the behavior of an estimator the experimenter usually uses well known simulated data. Thus if one is interested in exploring the behavior of estimates of the shape parameter in a Gamma population, one generates Gamma variates from a random number generator package (e.g., IMSL subroutine Chap. G). This batch of simulated data is processed by SIMTBED in the following way.

The data batch is first divided into M independent blocks. Each block contains N data points. So the starting data batch has to consist of M\*N data points (see Figure 1).

All blocks are divided into subsamples of size  $n_i$ . The actual subsample size  $n_i$  is an element of the subsample size array NE. This array can store up to 8 different values. Then the estimator is calculated for each subsample of size  $n_i$ . The estimator function will be calculated  $(\lfloor N/n_i \rfloor)$ \*M times. This total population of estimates is used to evaluate the summary statistics for the estimate and construct the corresponding box plot. If NE contains another element, the blocks are divided into the new subsample  $n_{i+1}$  size and all calculations are done again.

In addition to the summary statistics and the box plots (see e.g., Figure 3a), a regression on the averages and on the variance is computed, following the methodology of regression adjusted estimate (RARE) developed by Heidelberger and Lewis [Ref. 1].

The RARE estimate is the regression coefficient  $\alpha_0$ . It is the asymptotic estimate of the expected value of the parameter. The unbiased RAGE estimate of the average of the parameter is determined by the regression formula:

$$E(\theta(n_i)) = \alpha_0 + \alpha_1 \frac{1}{n_i} + \alpha_2 \frac{1}{n_i^2} + \dots + \alpha_D \frac{1}{n_i^D}$$

where D is an input parameter.

The asymptotic RARE estimate is printed as a dashed line in the graph.

The unbiased RAGE estimate of the variance of the estimator is given by the formula:

$$s^{2}(n_{i}) = \beta_{1} \frac{1}{n_{i}} + \beta_{2} \frac{1}{(n_{i})^{1.5}} + \beta_{3} \frac{1}{(n_{i})^{2}} + \cdots$$

The regression calculations of the average are done for each block separately. The result are M sets of regression coefficients. The finally printed regression coefficients are the averages of the M replications (see Figure 2). From the set of coefficients the variance and the standard deviation of the regression coefficients is calculated.

The regression on the variance is done once, using all (M\*N) data points.



Figure 2. Structure of the Regression Coefficients

#### IV. ARGUMENTS OF THE PROGRAMS SIMTBL AND SIMTB2

All versions of SIMTBED have in general the same argument list. SIMTB2 (a version for multivariate random variables) has two additional arguments. All arguments will be described in detail and all restrictions or limitations will be discussed. In Section V, detailed examples of setups for SIMTB1 and SIMTB2 are given. A. X--DATA ARRAY

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The array X is the input data array. X is single precision REAL\*4, and is generally simulated data e.g., in Section VII, independent Gamma variates.

In SIMTB1 the dimension of the array X must not exceed 50,000.

In SIMTB2 the input data is multivariate and consequently the array X has two dimensions. The size of the dimensions is not directly limited by the program. The space must be provided by the calling program and is passed as an argument (see IR and IRK). The memory requirements increase rapidly as the dimensions of X increase.

B. N--SAMPLE SIZE

The sample size N is the number of data points per section of input data X. N is an INTEGER. Depending on the precision of the simulation that is required, the sample size N can vary from 1 to 50,000.

In SIMTB2 N is the number of multivariate data points per section. M (the number of replications) times N must not exceed IR, the row dimension of X.

If M times N exceeds 50,000 an error message will be printed and the execution will be terminated. If the product M times N exceeds the total number of data points provided by the user, NO error message will signal the user error and the result of the execution is not predictable.

# C. M--NUMBER OF REPLICATIONS

The number of replications M of the array X is an INTEGER. M determines the number of sections, into which the data set X is divided. So M\*N is the dimension of X in SIMTB1. The parameter M also determines the number of regressions on the mean values that will be run to find the regression coefficients in the regression on the mean. If M is 1 only one regression will be done and no variance and standard deviation of the regression coefficients can be calculated.

# D. NE--SUBSAMPLE SIZE ARRAY

The argument NE is an INTEGER array, containing up to 8 subsample sizes. These are the subsample sizes at which the properties of the estimator are to be investigated. NE must always contain 8 elements. If less than 8 subsample sizes are used, the array must be filled up with dummy values. The estimator is calculated for each subsample

individually. The used values of NE (not the dummy values)
have to be ordered from the smallest to the largest
(NE(1) < NE(2) < NE(3) < ...).</pre>

The program can only handle up to a total number of 12,500 estimates. This limit is caused by storage limitations and can be expanded for larger computers. The smallest subsample size NE(1) produces the most estimates and if this case exceeds 12,500 the execution will be terminated and an error message will be printed.

In SIMTB2 all values of NE have to be less than 5,000.

# E. L--NUMBER OF SUBSAMPLE SIZES (BOX PLOTS)

The number of box plots L in the graphical output (the number of subsamples at which the estimator is examined), is an INTEGER with values from 1 to 8. The value of L determines how many elements of the array NE the program will use (e.g., L = 2, the program uses only NE(1) and NE(2) for the calculations). L determines the number of box plots and the number of corresponding summary statistics in the output. If L is out of range the program will terminate execution and print an error message.

For L = 1 no regression is possible. No regression output will be printed.

#### F. D--DEGREE OF REGRESSION

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The degree of regression on the mean D, is an INTEGER with values from 1 to 3. The chosen degree refers to the

number of coefficients calculated and printed for the regression equations. Experience has shown that D = 3 is preferable (higher values cause severe numerical problems in the regression computations).

If D exceeds the value of L-1, the program reduces D to this number, regardless of the value chosen by the user.

#### G. RG--REDUCED GRAPHICS

The argument RG is an INTEGER with value:

0 = off ==> full graphics

1 = set ==> reduced graphics

In the reduced graphics case the vertical scale of the graph is reduced by eliminating the outliers. Only the number of cutliers is counted and the number is printed. This enables the user to see the body of the boxplot in more detail.

#### H. SEI--SCALING ESTIMATORS INDIVIDUALLY

The argument SEI is an INTEGER with value:

0 = off ==> common scaling

l = set ==> individual scaling.

For SEI = 0 all printed graphs (max. 3 per program run) are scaled to the same range. This makes the comparison of the different graphs easier. The value SEI = 1 causes the program to scale each graph individually.

The argument SEI works in combination with the arguments RG and SVS. The combination of these three arguments make it possible to fit the printed graphs to the needs of the user.

I. SVS--SETTING THE VERTICAL SCALE

The argument SVS is an INTEGER with value:

0 = off ==> automatic scaling

l = set ==> scaling by the user.

SVS = 0 causes the program to calculate the scale of the graphic printout. The final graphic display is influenced by the chosen values of RG and SEI. The values of YMIN and YMAX are ignored by the program.

For SVS = 1 the user must provide the scaling. The graphics are vertically scaled to a given minimum value (YMIN) and maximum value (YMIN and YMAX). The arguments of RG and SEI are ignored. Only the numbers of outliers outside the display are printed for each box plot.

# J. YMIN--MINIMUM VALUE OF THE VERTICAL SCALE

The scaling parameter YMIN is data type REAL\*4. It is the lower limit of the vertical scale. It affects the scaling only in combination with SVS = 1. If the chosen value is so large that the value YMIN lies inside the body of the box plot, an error occurs and the program ends with an abnormal ending.

#### K. YMAX--MAXIMUM VALUE OF THE VERTICAL SCALE

The scaling parameter YMAX is data type REAL\*4. It is the upper limit of the vertical scale. The scaling is only effected if SVS has value 1. If the value of YMAX is too small and it lies inside the body of the box plot, the program comes to an abnormal ending.

YMIN and YMAX in combination with SVS = 1 should only be used for well known graphic ouptut. With this option, it is possible to scale the output of different program runs to a common scale. In particular if more than 3 estimators have to be estimated and compared, so that a common scale is needed, this option may be used.

## L. NEST--NUMBER OF ESTIMATORS

The parameter NEST is an INTEGER with the value 1, 2 or 3. The value of NEST determines the number of different one-page graphic displays the program produces with one call from the calling program. Usually the value of NEST is equal to the number of different estimators used in the program.

In SIMTB2 the same estimator may be used with different (e.g., normal, exponential etc.) distributed data sets.

#### M. EST1, EST2, EST3--ESTIMATOR FUNCTIONS

These 3 parameters are data type REAL\*4 and are used to pass the EXTERNAL function names to the program. An external declared function is a function which computes the value of an estimator. This function may call other routines, but the final value of the estimator must be passed over this function name.

For SIMTBL each function must have the two arguments X and NEK (e.g., FUNCTION VARIANCE (X,NEK)). X is the data array and NEK is the number of data elements in X.

SIMTB2 needs for each function four arguments X, NEK, IDR, IRK (e.g., FUNCTION CORRELATION (X,NEK,IDR,IRK)). X is a two dimensional data array and NEK is the subsample size, for which the function is evaluated. IDR and IRK are the dimensions of the array X.

If the user wants to use less than 3 estimator functions, he must use dummy arguments and choose the correct value of NEST. The easiest way to do this is to use a function of a previous used estimator again (for details of the programming see Section V).

# N. TTL1, TTL2, TTL3--DESCRIPTION OF THE ESTIMATORS

These arrays are used to pass titles from the calling program to SIMTB. Each title has to be 120 characters long (15 fields, each 8 characters wide). The title is printed below the output of the corresponding function.

If the user uses less than 3 functions and titles, he has to use dummy arguments (for details see Section V).

If the titles are not in the correct format, corresponding to the FORMAT statement the program will not execute properly.

#### O. IR, IRK--DIMENSIONS OF THE ARRAY X

These arguments are used ONLY in SIMTB2. IR (row dimension) and IRK (column dimension) are INTEGERS and have to match the dimension of X in the calling program.

If the dimensions don't match, NO error message will be produced and the output is unpredictable. The error may not be obvious, and the ouput may look reasonable.

# V. DUMMY EXAMPLES OF IMPLEMENTING SIMTB AND SIMTB2 INTO A DRIVER-PROGRAM

The following examples show how the programs SIMTB1 or SIMTB2 can be implemented into a FORTRAN driver-program. The only purpose of the examples is to clarify the FORTRAN implementation, to avoid programming errors by the user. Additional comment lines are added to the program examples.

In the first example SIMTB1 is used to compare two different estimators (VAR and UNBVAR) of the variance of a normal sample. The sample may be generated with a random number generator (e.g., LLRANDOMII).

In the second example SIMTB2 is used to compare the distribution of two estimators. The estimators are the covariance (COV) and the correlation coefficient (CORR) of a bivariate standard normal sample.

```
A. EXAMPLE 1 USING SIMTB1
```

MAIN

C EXAMPLE of SIMTB1 Calling program, it has not to be the MAIN program REAL\*4 X(50000), YMIN, YMAX, VAR, UNBVAR REAL\*8 T1(15), T2(15), T3(15) INTEGER N, M, NE(8), L, D, RG, SEI, SVS, NEST C

DATA N /2500/

DATA M / 20/

DATA NE /10,20,25,50,100,0,0,0/

C Array NE must have 8 elements, if only 5 are used, add

C dummy variables and set L = 5

```
DATA L
                  5/
             /
     DATA RG /
                 0/
     DATA SEI / 0/
     DATA SVS / 0/
    DATA NEST/ 2/
    DATA T1 /'ESTIMATE','OF THE V','ARIANCE','USING ',
    +'VAR=(1/N)', '*SUM(X(I',')-XBAR)*', '*2 ',7*' '/
    DATA T2 /'ESTIMATE', 'OF THE V', 'ARIANCE ', 'USING ',
    +'VAR=(1/(1','-N))*SUM','(X(I)-XB','AR)**2 ',7*' '/
C All 15 fields (each 8 characters) have to be
С
  initialized
С
    EXTERNAL VAR, UNBVAR
С
C Generate M*N independent Normal (0,1) Random numbers
  and store into X
С
С
    CALL SIMTB1(X,N,M,NE,L,D,RG,SEI,SVS,YMIN,YMAX,NEST
                ,VAR,T1,UNBVAR,T2,VAR,T1)
  EST3=VAR and TTL3=Tl used as dummy variables
С
С
     STOP
     END
```

С FUNCTION VAR (X, NEK) C Function to calculate the Variance. C All calculations inside the function should be done in C DOUBLE PRECISION С REAL\*4 X(N), VAR REAL\*8 SUM, XBAR, DVAR С SUM=0.0D0 DO 10 I=1,N SUM=SUM+DBLE(X(I)) 10 CONTINUE XBAR=SUM/FLOAT(N) SUM=0.0D0 DO 20 I=1,N SUM=SUM+((DBLE(X(I)))-XBAR)\*\*220 CONTINUE DVAR=SUM/FLOAT(N) VAR=SNGL(DVAR) С RETURN END FUNCTION UNBVAR (X,NEK) C Function to calculate the Variance. C All calculations inside the function should be done in C DOUBLE PRECISION

С

REAL\*4 X(N), UNBVAR REAL\*8 SUM, XBAR, DUNVAR

#### С

SUM=0.0D0

DO 10 I=1,N

SUM=SUM+DBLE(X(I))

10 CONTINUE

XBAR=SUM/FLOAT(N)

SUM=0.0D0

DO 20 I=1,N

SUM=SUM+((DBLE(X(I)))~XBAR) \*\*2

Let a La La La La La

20 CONTINUE

DUNVAR=SUM/FLOAT(N)

UNBVAR=SNGL (DUNVAR)

С

RETURN

END

B. EXAMPLE 2 USING SIMTB2

MAIN

C EXAMPLE of SIMTB2 Calling program, it has not to be the MAIN program REAL\*4 X(25000,2), YMIN, YMAX, COV, CORR REAL\*8 T1(15), T2(15), T3(15) INTEGER N, M, NE(8), L, D, RG, SEI, SVS, NEST, IR,

IRK

С

- DATA N /2500/ DATA M / 10/ DATA IR /25000/ DATA IRK / 2/
- C IR and IRK must be equal to the dimensions of X

DATA NE /10,20,25,50,83,100,125,250/

DATA L / 8/

DATA RG / 0/

DATA SEI / 0/

DATA SVS / 1/

DATA YMIN/ 0.0/

DATA YMAX/ 1.0/

DATA NEST/ 2/

DATA T1 /'ESTIMATE','OF THE C','OVARIANC','E

+11\*' '/

DATA T2 /'ESTIMATE','OF THE C','ORRELAT1','ON COEFF',

+'ICIENT ','10\*' '/

C All 15 fields (each 8 characters) have to be

C initialized

С

EXTERNAL COV, CORR

С

C Generate M\*N pairs of independent random bivariate
C numbers, each pair being independent N(0,1) random

С variables and store into X С CALL SIMTB2 (X,N,M,NE,L,D,RG,SEI,SVS,YMIN,YMAX,NEXT ,COV,T1,CORR,T2,COV,T1,IR,IRK) С EST3=COV and TTL3=Tl used as dummy variables С STOP END С С FUNCTION COV (X, NEK, IDR, IRK) Function to calculate the Covariance. С All calculations inside the function should be done in С С DOUBLE PRECISION С REAL\*4 X(IDR, IRK), COV REAL\*8 SUM1, SUM2, SUM3, XBAR1, XBAR2, EX1X2, DCOV С SUM1=0.0D0 SUM2=0.0D0 SUM3=0.0D0 DO 10 I=1,N SUM1=SUM1+DBLE(X(I,1)) SUM2=SUM2+DBLE(X(I,2))SUM3=SUM3+DBLE(X(I,1)\*X(I,2)) 10 CONTINUE XBAR1=SUM1/FLOAT(N)
```
XBAR2=SUM2/FLOAT(N)
     EX1X2=SUM3/FLOAT(N)
     DCOV=EX1X2-(XBAR1*XBAR2)
     COV=SNGL(DCOV)
С
     RETURN
     END
С
     FUNCTION CORR (X, NEK, IDR, IRK)
C Function to calculate the Correlation coefficient
C All calculations inside the function should be done in
C DOUBLE PRECISION
С
     REAL*4 X(IDR, IRK), CORR
     REAL*8 SUM1, SUM2, SUM3, XBAR1, XBAR2, EX1X2, VAR1, VAR2,
            COV, DCORR
С
     SUM1=0.0D0
     SUM2=0.0D0
     SUM3=0.0D0
```

DO 10 I=1,N

```
SUM1=SUM1+DBLE(X(I,1))
```

```
SUM2=SUM2+DBLE(X(I,2))
```

```
SUM3=SUM3+DBLE(X(I,1)*X(I,2))
```

10 CONTINUE

XBAR1=SUM1/FLOAT(N)

XBAR2-SUM2/FLOAT(N)

EX1X2=SUM3/FLOAT(N)

SUM1=0.0D0

SUM2=0.0D0

DO 20 I=1,N

SUM1=SUM1+DBLE(X(I,1)\*\*2)

SUM2=SUM2+DBLE(X(I,2)\*\*2)

20 CONTINUE

VARl=(SUM1/FLOAT(N))-(XBAR1\*\*2) VAR2=(SUM2/FLOAT(N))-(XBAR2\*\*2) COV=EX1X2-(XBAR1\*XBAR2) DCORR=COV/((VAR1\*VAR2)\*\*0.5) CORR=SNGL(DCORR)

С

RETURN

END

# VI. STUDY OF THE BEHAVIOR OF SERIAL CORRELATION ESTIMATES FOR DIFFERENT DISTRIBUTIONS

#### A. CALCULATION OF THE FIRST SERIAL CORRELATION COEFFICIENT

It is known that for an independent sample from a population with finite variance, the distribution of the serial correlation coefficient (Anderson and Walker, 1964) [Ref. 3] is asymptotically Normal with mean zero and variances 1/n, where n is the sample size. If the population is i.i.d Normal then the bias is exactly -1/n. Since those asymptotic properties are frequently used as approximations in tests of significance, it is important to know how valid the approximation would be in small samples from a variety of distributions. We will look at that question in the next two sections and then go on to consider two alternative measures of correlation, Fisher's z-transform and the 2-fold jackknifed estimate of the correlation. Their ability to reduce bias and/or induce Normality will be examined against other changes in the distribution of the estimators, particularly variance inflation. A simulation study, without graphics, of some of these problems was conducted by Cox (1966) [Ref. 4].

#### B. SIMTBL OUTPUT FOR SERIAL CORRELATION

Figure 3(a) shows the simulated distribution and sample properties of the serial correlation coefficient estimate

$$r_{n} = \frac{\prod_{j=1}^{n-1} (x_{j} - \overline{x}_{1}) (x_{j+1} - \overline{x}_{n})}{(n-1) \sum_{j=1}^{n} (x_{j} - \overline{x}_{0})^{2}},$$

where:

$$\overline{x}_0 = \sum_{j=1}^n \frac{x_j}{n},$$

$$\overline{X}_{1} = \sum_{j=1}^{n-1} X_{j}/(n-1)$$
, and

$$\bar{x}_{n} = \sum_{j=2}^{n} x_{j}/(n-1)$$

for various sub-sample sizes  $n = n_i$ . This definition matches that used by Anderson and Walker (1964). We consider first subsamples of size  $n_1 = 10$ , and then of size  $n_2 = 20$ ,  $n_3 = 30$ ,  $n_4 = 40$ ,  $n_5 = 50$ ,  $n_6 = 75$ ,  $n_7 = 100$  and  $n_8 = 150$ , successively. For each subsample size the input sample of N = 5000 simulated Normal (0,1) random variables is divided into as many full subsamples of size  $n_i$  as possible, and the serial correlation is computed for each of the  $[N/n_i]$  subsamples of size  $n_i$ . The entire procedure is then replicated M = 10 times, each time with a new simulated sample of N = 5000 Normal (0,1) variables.

After all M replications have been run, all the estimates of serial correlation for each subsample size are grouped together and their simulated distribution is presented via a boxplot and summary statistics. The boxplot follows the standards discussed in Mosteller and Tukey (1977) [Ref. 5] with the median denoted by a + within the box, the mean by a \* within the box, the outliers by 0's, and the far outliers by \*'s beyond the whiskers. The summary statistics include the sample mean, sample standard deviation, estimated standard deviation of the sample mean (i.e., sample standard deviation/ $sqrt(M[N/n_{i}])$ , sample skewness and sample kurtosis of the correlation estimates.

Looking at the output, the first (leftmost) boxplot in the graph in Figure 3(a) shows the distribution of

(# Replications) × 
$$\begin{bmatrix} \frac{(\text{Simulation})}{(\text{Sample Size})} \\ \frac{(\text{Subsample})}{(\text{Size})} \\ = 10 \times \begin{bmatrix} \frac{5000}{10} \end{bmatrix} \\ = 10 \times 500 = 5000 \end{bmatrix}$$

estimates of serial correlation from independent subsamples of size  $n_1 = 10$ . Summary statistics for the boxplot can be found below the graph in the column labeled "Subsample Size 10," so that the average serial correlation is -.1074, and the estimated standard deviation is .2996. The estimated standard deviation of the serial correlation estimate is .2996/ $\sqrt{(5000)} = .00424$ . Recall that this refers to correlation estimates based on subsamples of size 10.

Since the X-axis of the graph represents subsample size, the last (rightmost) boxplot shows the distribution of a de la caracteria de la c

$$10 \times \left[\frac{5000}{150}\right] = 10 \times 33 = 330$$

estimates of serial correlation from independent subsamples of size  $n_8 = 150$ . Although the 330 estimates are independent of each other, they are not independent of the 5000 estimates that comprise the first boxplot since the same data (divided and processed in different ways) was used for both. Summary statistics show that the average correlation has dropped to -.007372, indicating the fall off in bias, and the standard deviation has dropped to .07822, indicating the greater accuracy with which the correlation can be estimated when 150 points, rather than 10, are available.

In order to quantify the changes that are occurring in the mean and variance of the distribution of the estimator as subsample size changes, SIMTBl performs two types of regressions. The first regression is on the averages and is done after each replication, using the average serial correlation for that replication,  $\overline{r}_{n_i}$ , as the dependent variable. Inverse powers of the subsample size serve as the independent variables. For Figure 3(a) the degree of the regression was chosen to be D = 3 so, for each replication, the equations we attempt to fit by least squares are:

$$\overline{r}_{n_{i}} = a_{0} + \frac{a_{1}}{n_{i}} + \frac{a_{2}}{n_{i}^{2}} + \frac{a_{3}}{n_{i}^{3}}$$
 for  $i = 1, 2, ..., 8$ .

This form anticipates the general asymptotic expansion

$$E(\hat{\Theta}(n)) = \Theta + \frac{\alpha_1}{n} + \frac{\alpha_2}{n^2} + \frac{\alpha_3}{n^3} + \dots$$

which holds true in the current situation with  $\Theta = 0$  and (in the Normal case)  $\alpha = -1$  (see Cramer (1948) for general results of this type) [Ref. 6].

Values of  $a_0$ ,  $a_1$ ,  $a_2$ , and  $a_3$  are calculated after each replication, averaged across the M replications to get  $\overline{a}_0$ ,  $\overline{a}_1$ ,  $\overline{a}_2$ , and  $\overline{a}_3$ , and then the averages are reported below the summary statistics on the line "Mean of Regression on Averages--Coefficients." We find that  $\overline{a}_0 = -.000272$  and  $\overline{a}_1 = -1.03074$ , both close to their theoretical counterparts.

Because we have 10 replications and therefore 10 independent values of each of  $a_0$ ,  $a_1$ ,  $a_2$ , and  $a_3$ , we can also estimate the variances and standard deviations of  $a_0$ ,  $a_1$ ,  $a_2$ , and  $a_3$  across replications. These values are presented on the two lines immediately below the coefficients. For instance, the estimated s.d. of the estimate  $\overline{a}_0 = -.000272$  of  $a_0$  is .003892.

The regression line for the mean value of the estimator is presented visually in the graph as a dotted curve. The estimated asymptote (i.e.,  $\overline{a}_0$ ) is printed with a dashed line wherever it does not coincide with the regression line. Bias, therefore, can be viewed as the difference between those two lines.

The second regression referred to above is done after all replications have been run and the variances of the estimators

at each subsample size have been calculated. (Note that the standard deviations, not the variances, are presented in the summary statistics.) It should be recalled from previous discussion that these variances, as well as all measures in the summary statistics, are based on the grouping together of the serial correlations <u>from all replications</u>, at each subsample size. This is in contrast to the procedure for the regression on the means, where average correlations are computed for each subsample size <u>for each replication</u>. In the case of the variances, we have 8 equations:

$$\hat{var}(r_{n_{i}}) = \frac{b_{0}}{n_{i}} + \frac{b_{1}}{n_{i}^{3/2}} + \frac{b_{2}}{n_{i}^{2}} + \frac{b_{3}}{n_{i}^{5/2}}, \quad i = 1, 2, \dots, 8,$$

which we fit by least squares in order to estimate the coefficient  $\beta_0$ ,  $\beta_1$ ,  $\beta_2$ , and  $\beta_3$  in the presumed asymptotic expansion

$$\operatorname{Var}(\hat{\Theta}(n)) = \frac{\beta_0}{n} + \frac{\beta_1}{n^{3/2}} + \frac{\beta_2}{n^2} + \frac{\beta_3}{n^{5/2}} + \dots$$

This expansion holds for the variance of the estimated serial correlation coefficient for independent data. Usually it will be  $\beta_0$  in which we are most interested since  $\beta_0$  is used in computing asymptotic relative efficiencies of estimators. For independent data with finite variance, we know that  $\beta_0 = 1$ . The computed values of  $b_0$ ,  $b_1$ ,  $b_2$ , and  $b_3$ , are presented on the line labeled 'Regression on Variance--- Coefficients'. Notice that  $b_0 = .7438$  is close to the theoretical value of 1.

The final two numbers on Figure 3(a), YMIN and YMAX, simply show the scale of the vertical axis. Because the SIMTB1 program option to put Figures 3(a), 3(b) and 3(c) on the same scale was in effect, it may be that no boxplot in a given Figure (e.g., Figure 3(b)) requires the full range of Y-values.

In order to produce Figure 3(b), the Normal (0,1) data that went into Figure 1(a) was squared to create longer tailed  $\chi^2(1)$  random variables. The output is entirely analogous to that for Figure 3(a). Similarly, for Figure 1(c), the Normal (0,1) data was exponentiated in order to create Lognormal (0,1) data and to produce analogous graphical output. The indication is that the distribution of the sample serial correlation is robust with respect to the population distribution.

The features of the SIMTB1 output will become clearer when they are associated with the various properties of the correlation estimator. First, however, a few technical comments concerning the regressions are necessary.

# C. SOME COMMENTS ON THE REGRESSIONS

Two types of problems, numerical and statistical, can occur when attempting to fit the two sets of regression equations presented in Section VI.B.

First, there is the question of numerical stability when the independent variables, {1,  $n_i^{-1}$ ,  $n_i^{-2}$ ,  $n_i^{-3}$ } or { $n_i^{-1}$ ,  $n_i^{-3/2}$ ,  $n_i^{-2}$ ,  $n_i^{-5/2}$ } decrease geometrically. If we

attempt to form  $X^{T}X$ , where X is the respective design matrix and  $X^{T}$  is the transpose of X, we get values that range from 8 (assuming 8 subsample sizes) to  $\sum_{i=1}^{8} n_{i}^{-6}$  for the regression on the means, and  $\sum_{i=1}^{7} n_{i}^{-2}$  to  $\sum_{i=1}^{7} n_{i}^{-5}$  for the regression on the variances. Experience has shown that attempts to solve systems with such extremes in the  $X^{T}X$  matrix produce erroneous results. Instead, SIMTBl scales the design matrices by multiplying each column of X by  $Max(n_{i})$  raised to the proper power so that no entry becomes too small. The standard Choleski decomposition is then used to fit the equations, and the coefficients are properly rescaled before they are reported. This procedure produces numerically reliable results.

The second problem concerns the breakdown of statistical assumptions in our regression models. It has already been pointed out in Section VI.B that the two sets of dependent variables:

(1) the  $\overline{\Theta}(n_i)$  when considering the regression on the means;

(2) the s<sup>2</sup>(n<sub>i</sub>) = 
$$\begin{bmatrix} M \\ j \\ j \\ j \\ j \\ 1 \end{bmatrix} = \begin{bmatrix} \hat{\Theta}_{j}(n_{i}) - \overline{\Theta}(n_{i}) \end{bmatrix}^{2} \\ \frac{M \begin{bmatrix} N/n_{i} \end{bmatrix}}{M \begin{bmatrix} N/n_{i} \end{bmatrix}}$$

when considering the regression on the variances, are not independent over i since all are based on the same simulated data. The extent of the dependence is demonstrated by the correlation matrix in Table 1. Entries in that table show the estimated correlation between  $s^2(n_i)$  and  $s^2(n_j)$  for

ENTRIES IN THE TABLE ARE THE ESTIMATED CORRELATIONS
BETWEEN THE ESTIMATED VARIANCES OF THE r_ AT
DIFFERENT SUBSAMPLE SIZES:
$CORR(s^{2}(r), s^{2}(r))$ for $i = 1,, 8, i = 1,, 8$

	TAB	LE	1
--	-----	----	---

	1	Ŧ	2	3	4	5	6	1	8	
j										
1		1.00	.49	.46	26	.18	17	.14	.01	
2		.49	1.00	.40	.55	.11	.38	.38	03	
3		.46	.40	1.00	.23	.23	.44	.21	. 29	
4		26	.55	.23	1.00	.42	.86	.57	.35	
5		.18	.11	.23	. 42	1.00	.71	.43	.59	
6		17	.38	.44	.86	.71	1.00	.45	.53	
7		.14	.38	.21	.57	.43	.45	1.00	.72	
8		.01	03	.29	.35	.59	.53	.72	1.00	

Recall that  $r_n$  is the estimated serial correlation for a simulated Normal (0,1) subsample of size n. Also, the estimated correlations shown above were computed using 10 values (replications) of  $s^2(r_n)$  and  $s^2(r_n)$  for each i and  $r_i$  j.

all i and j, where the estimation was done by repeating the SIMTBl experiment with 10 different batches of 50,000 simulated random variables. Since only 10 values went into each correlation calculation, the table is only accurate to within approximately  $\pm 2/\sqrt{10} = .632$ . We see some indication of positive correlation, especially when i and j are close, but the lack of independence is not severe enough to hurt the regression results for either the estimated means or variances significantly.

A second assumption, implicit in any ~egression, is that the dependent variables have equal variances. This condition holds true for the means, which can be shown to satisfy

$$Var(\overline{\Theta}(n_i)) = \frac{M}{N}$$

independently of i. The estimated variances, however, are not equivalent and, if we assume the  $\hat{\Theta}_{j}(n_{i})$  to be approximately Normally distributed so that

$$\begin{array}{c} M \begin{bmatrix} N/n_{i} \\ \sum \\ j=1 \end{array} \right) \left( \hat{\Theta}_{j}(n_{i}) - \overline{\Theta}(n_{i}) \right)^{2}$$

is approximately proportional to a  $\chi^2_{M} [N/n] - 1$  random variable, we can compute

$$\operatorname{Var}(s^{2}(n_{i})) \stackrel{\sim}{=} \frac{2}{\operatorname{MNn}_{i} - n_{i}^{2}}$$

To correct this problem, SIMTBl scales the  $s^2(n_i)$  by  $\sqrt{n_i}$  so that

$$\operatorname{Var}(\sqrt{n_{i}} s^{2}(n_{i})) = \frac{2}{MN - n_{i}} = \frac{2}{MN}$$

since MN >>  $n_i$ . The design matrix is scaled accordingly and the values  $b_0$ ,  $b_1$ ,  $b_2$ , and  $b_3$  discussed in Section VI.B. are reported.

Table 2 shows the effects of the rescaling by presenting first the estimated variances of the  $s^2(n_i)$ , where the estimation is done by repeating SIMTB1 for 10 batches of 50,000 simulated data points. These estimated variances decrease as  $n_i$  increases, closely paralleling the second line of Table 2 which has the approximate theoretical values (i.e.,  $2/(MNn_i - n_i^2))$ . The final line of Table 2 shows the estimated variances of the rescaled  $s^2(n_i)$ , i.e., the  $\sqrt{n_i} s^2(n_i)$ , which, as expected and hoped, show a more constant variance with i.

Although future versions of SIMTB1 will include more sophisticated regression routines and the ability to generate independent samples at each subsample size, the SIMTB1 is quick, usable, and accurate for most situations.

# D. INTERPRETING THE SERIAL CORRELATION RESULTS

Returning to Figure 3(a) which shows the simulated distribution of the serial correlation coefficient from independent, Normal (0,1) data, the following comments summarize the most striking features:

### TABLE 2

A COMPARISON OF THE ESTIMATED VARIANCE OF  $s^2(r_n)$ WITH THE APPROXIMATE THEORETICAL VARIANCE OF  $n_i$  $s^2(r_n)$  AND WITH THE APPROXIMATELY EQUIVARIANT SCALED i VERSIONS,  $n_i^{-5} s^2(r_n)$ .

All entries have been multiplied by 10<sup>5</sup>.

 $n_i = 10 \ 20 \ 30 \ 40 \ 50 \ 75 \ 100 \ 150$  $\hat{var}(s^2(r_{n_i})) \ .177 \ .150 \ .204 \ .079 \ .047 \ .031 \ .049 \ .022$ 

Approx. Theoretical Var( $s^2(r_n)$ ) .400 .200 .133 .100 .080 .053 .040 .027

 $\hat{var}(n_i^{-.5} s^2(r_{n_i}))$  1.77 2.99 6.12 3.18 2.33 2.33 4.88 3.35

The estimated variances of  $s^2(r_n)$  and  $\sqrt{n_i} s^2(r_n)$  were calculated using 10 independent replications of  $s^2(r_n)$ .

(a) The boxplots appear very symmetric at all subsample sizes with nearly equal numbers of outliers at either tail and with mean and median coincidental. This observation is confirmed by the estimates of skewness in the summary statistics. Kurtosis is mildly negative at small subsample sizes but, overall, asymptotic Normality seems to take hold rather quickly.

(b) The average serial correlation is negative for small subsam-les. This is demonstrated by the dotted regression curve which starts at approximately -.10 and levels off near 0 for subsamples greater than about 85. The dashed asymptote of -.000272 is very close to the theoretical value of 0, and the mean values in the summary table closely reflect the bias of -1/n.

(c) The standard deviations of the simulated distributions are very close to the asymptotic values of  $n_i^{-0.5}$ , although the lead coefficient in the regression on the variances,  $b_0 = .743756$ , is not as close to the theoretical value of 1 as we would hope. When SIMTB1 is repeated 10 times with 10 different batches of simualted data, we find an average value for  $b_0$  to be 1.0604, with a standard deviation for  $b_0$  of .307. The estimation procedure for  $b_0$ , therefore, remains valid, but the estimate itself is highly variable.

The agreement between the simulated and the theoretical, asymptotic values of the bias and variances was discovered previously by Cox (1966). SIMTB1 has now allowed us to

automatically look at a broader range of subsample sizes and to see, through boxplots and estima es of skewness and kurtosis, a fuller picture of any changes in the distribution of the estimator. We can be satisfied that estimates of serial correlation do behave approximately as Normal (-1/n, 1/n) rangome variables when the underlying data is Normal (0,1).

If the lead terms in the expansions of the mean and variance of the estimated correlation coefficient (i.e.,  $a_0$ ,  $a_1$ , and  $b_0$ ) had been unknown, we would also have a fairly good idea now of what they were.

When the underlying data is  $\chi_1^2$ , Figure 3(b) confirms Cox's observation that the bias is relatively uneffected but, for small subsamples, the standard deviation is smaller than the expected  $n^{-1/2}$ . Unlike Figure 3(a), there is a pronounced skewness in the boxplots in Figure 3(b) with many more outliers at the positive end, and with the mean higher than the median at the first four subsample sizes. The problem of suppressed variance seems cured at  $n_7 = 100$  and  $n_8 = 150$ , but the skewness remains and could cause problems in tests of significance.

Figure 3(c), which is based on an underlying batch of simulated Lognormal (0,1) data, shows a slight exaggeration of the effects in Figure 3(b). The standard deviation is more suppressed and does not attain the theoretical level by  $n_8 = 150$ . The positive skewness is more pronounced and kurtosis does not approach the theoretical value of 0.

Overall, the effects of long-tailed data on the distribution of the serial correlation coefficient can be summarized as follows:

- Bias is not significantly effected and remains at approximately -1/n.
- (ii) The variance of the distribution of the serial correlation coefficient is reduced by longertailed data.
- (iii) Positive skewness is created in the distribution.
- (iv) Kurtosis may become positive at larger subsample sizes.
- (v) For long-tailed data (i.e., Lognormal), a subsample size of 150 is not large enough to insure asymptotic Normality.

E. SIMTBL OUTPUT FOR THE Z-TRANSFORM OF THE CORRELATION Fisher's z-transform of the estimated correlated coefficient is defined by:

$$Z_n = \frac{1}{2} \log \frac{1 + r_n}{1 - r_n}$$
,

where  $r_n$  is the estimated serial correlation presented in Section VI.B. The transformation is intended to make the distribution of the  $Z_n$  more Normal than that of the  $r_n$ . When the same SIMTBl experiment described in Section VI.B. is run using  $Z_n$  as the estimator instead of  $r_n$ , we get the results shown in Figures 4(a), 4(b) and 4(c). It should be noted that the scale of the boxplots here has been forced to be approximately comparable to the scale for the boxplots in Section VI.B. This is done by suppressing outliers that are more than 1.5 interquartile distances beyond the quartiles of the boxplot. If we had allowed the data to scale the boxplots, we would have seen a much wider range on the vertical axis because the  $Z_n$  are not restricted to the limits of -1 to +1 and because there is one far outlier at -3.8. In this type of "reduced graphics," we still see the number of outliers that fall beyond the allowable range through the numbers at the ends of the boxplots, but we do not see their actual locations.

Figure 4(a) shows the distribution of the z-transformed correlation coefficients when the underlying data is simulated, Normal (0,1). At each subsample size, the mean and standard deviation are close to the theoretical  $n^{-1}$  and  $n^{-1/2}$  respectively. The skewness and kurtosis at subsample size  $n_1 = 10$  are far from the theoretical Normal distribution values of 0 and 0, reflecting partly the one far outlier at -3.8 and partly the negative skew in the remainder of the  $2n_1$ 's. For other subsample sizes, there is no strong evidence to contradict the assumption of approximate Normality.

The relationship between Figure 4(b) and 4(a) is similar to that between 3(b) and 3(a). Figure 4(b), which is based on simulated  $\chi_1^2$  data, shows (a) bias that is the same as for the transformed correlations based on Normal data, (b) slightly suppressed variances, particularly at small subsample sizes and (c) positive skewness which persists at large subsample sizes. In addition, there are signs of positive kurtosis at small subsample sizes.

Figure 4(c) is based on Lognormal (0,1) data and shows high values of skewness and kurtosis at almost all subsample sizes. Approximate Normality seems an unwarranted assumption. In fact, the kurtosis is converging very slowly to its asymptotic value of 0.

In general, using the z-transform does not help with Normality assumptions, especially when dealing with longtailed distributions.

F. SIMTB1 OUTPUT FOR THE 2-FOLD JACKKNIFE OF THE CORRELATION

The final Figures, 5(a), 5(b) and 5(c), deal with the 2fold jackknife estimate of correlation. Again, the figures are reduced graphics with scaling comparable to that of the boxplots of Sections VI.D and VI.E. To define the estimator, we start with a given subsample of size n, compute the serial correlation for the first  $\lfloor n/2 \rfloor$  points and call it  $r_1(n/2)$ , compute the serial correlation for the second  $\lfloor n/2 \rfloor$  points and call it  $r_2(n/2)$  and compute the serial correlation for the entire subsample of n points and call it  $r_0(n)$ . Each computation follows the formula in Section VI.B. The three estimators are then combined to form two pseudo-values,

 $r_1^{*}(n) = 2r_0(n) - r_1(n/2)$ 

and

$$r_2^*(n) = 2r_0(n) - r_2(n/2)$$
,

and the final jackknife estimator for that subsample is defined as

$$\tilde{r}(n) = \frac{r_1 * n + r_2 * (n)}{2}$$

Although a jackknife estimator may have many favorable properties, we are concerned here primarily with its ability to remove bias, hopefully without inflating the variances of the estimator and/or inducing nonnormality.

Figure 3(a), based on simulated Normal (0,1) data, shows nearly complete removal of bias, even at small subsample sizes. The cost of the bias reduction is reflected in an increase of nearly 50% in the standard deviation of the correlation estimate for subsample size 10, and lesser relative increases at larger subsample sizes. There is also an indication of a positive skew for small subsample sizes, and the problem that the jackknife estimator need not fall into the -1 to +1 range which is desirable for a correlation coefficient estimate.

When using simulated  $\chi_1^2$  data as in Figure 5(b), or simulated Lognormal (0,1) data as in Figure 5(c), there is again no problem with bias. Variance inflation, though it exists

at small subsample sizes, is not as large as when Normal (0,1) data is used. The distributions of the jackknifed correlations show very pronounced positive skews, however, as well as positive kurtosis. These two problems are worse for the longer-tailed Lognormal data.

Overall, the jackknife estimator is very successful at removing bias but the costs include variance inflation, which can be severe at small subsample sizes, plus increased positive skewness and kurtosis when the estimates are based on data from longer-tailed distributions.

#### G. COMPARISON OF THE THREE ESTIMATES OF CORRELATION

For Normal (0,1) data, the distribution of the usual correlation coefficient displayed in Figure 3(a) behaves very much as theoretical asymptotic calculations would predict, even at small subsample sizes. This makes it possible to correct for bias in the estimator and to perform tests of significance. Use of Fisher's z-transform, as illustrated in Figure 4(a) does not seem necessary since it does not significantly improve the approximate Normality of the estimator. The jackknife estimator in Figure 5(a) may be valuable if a direct, unbiased estimator is needed but the inflated variance of the jackknife estimator may limit the usefulness of the estimate as well as make any tests of significance too conservative.

When the underlying data comes from a longer-tailed distribution, the usual correlation coefficient in Figures 3(b)

and 3(c) retains a predictable bias term, although the variance of its distribution is slightly depressed and the skewness and kurtosis becomes positive, even for subsamples as large as 150. This means that it is still possible to estimate the correlation accurately, but tests of significance fall on shakey assumptions of Normality. The z-transform in Figures 4(b) and 4(c) does little to firm up those assumptions and, in some cases, makes the situation worse. As in the case of Normal data, the 2-fold jackknifed correlation in Figures 5(b) and 5(c) is bias-free but follows a fairly non-Normal distribution which would invalidate significance testing.

All of the preceding observations and conclusions flow immediately from the nine figures presented so far. Further studies could easily be done through SIMTBl, looking at larger subsample sizes, correlated data, and alternative marginal distributions. For demonstration purposes, though, it is better to proceed to our second application.

# VII. STUDY OF PROBLEMS OF ESTIMATING SHAPE PARAMETERS FOR HIGHLY SKEWED DISTRIBUTIONS

A. ESTIMATING THE SHAPE PARAMETER FOR A GAMMA DISTRIBUTION

As a second application of SIMTB1, we will consider a problem which has received much less statistical attention; asymptotic results are summarized in Cox and Lewis (1966, Ch. 2) [Ref. 7] and Johnson and Kotz (1970, Ch. 17) [Ref. 8]. We want to estimate the shape parameter, K, for a Gamma distribution, where the Gamma density is given by

$$(\frac{K}{u})^{K} \frac{x^{K-1}}{\Gamma(x)} e^{-Kx/u} \qquad x > 0; \quad K > 0; \quad \mu > 0$$

$$f(x) = 0 \qquad x < 0$$

Notice that the mean of this distribution is u, not K/u as in some differently parameterized versions of the Gamma density. For the data that will be simulated for use in SIMTB1 we will use K = 5 and u = 1 and K = 0.25 and  $\mu$  = 1. The closer the mean of our estimate is to 5 or 0.25, the better (in terms of bias) is our estimation procedure. Other factors such as the variance and Normality of the estimator will of course also have influence in the determination of a preferred estimator.

Section VII.B will compare the commonly used maximum likelihood estimator to the competing method of moments

estimator. Both procedures result in asymptotically Normal estimators (Cramer, 1948) but the m.l.e. is usually preferred because of its favorable asymptotic relative efficiency (Cox and Lewis, 1966) [Ref. 7]. Through SIMTBL, though, we will see that for small subsamples the estimated variances of the two estimators of K are not as far apart as asymptotic results lead us to believe. In addition, the bias that appears in both estimators is smaller for the moment estimator.

In Section VII.C. we will use a four-fold jackknife of both the m.l.e. and moments estimators to successfully remove the bias. What is remarkable is that, unlike the jackknifing of the serial correlation, there is little or no cost in terms of variance inflation and nonnormality for the jackknifed moment estimator. When K = .25, we will see in Section VII.D. that the jackknifed m.l.e. dominates the other three estimators at all subsample sizes when considering the mean, variance, and Normality of the estimator.

### B. MAXIMUM LIKELIHOOD AND MOMENT ESTIMATORS OF K

Figure 6(a) is very similar in format to the figures that have already been presented for the correlation example except that:

(1) The estimator whose distribution is being displayed is the maximum likelihood estimator of K, the shape parameter of a Gamma(5) population. We denote the estimator, computed from a simulated subsample of size n, by  $\hat{K}(n)$  and define it

to be the solution of the equation:

$$n[\log \hat{K}(n) - \Psi(\hat{K}(n))] = n \log \sum_{i=1}^{n} X_i/n - \sum_{i=1}^{n} \log x_i,$$

where the X<sub>i</sub> are the simulated Gamma(5) random variables and  $\Psi(\cdot)$  is the digamma function (Cox and Lewis, 1966).

(2) The eight subsample sizes which we will be looking at are  $n_1 = 33$ ,  $n_2 = 50$ ,  $n_3 = 71$ ,  $n_4 = 100$ ,  $n_5 = 125$ ,  $n_6 = 166$ ,  $n_7 = 250$  and  $n_8 = 500$ . We will not see as much detail at small subsample sizes but we will see some of the asymptotic (n = 500) effects coming in.

(3) At each subsample size we will work with  $M^* = 20$ independent replications of  $N^* = 2500$  simulated Gamma(5) random variables, instead of the M = 10 replications of N = 5000 variables used previously. The total number of independent simulated random variables across replications remain constant at the program maximum of 50,000. Hence, the boxplot at subsample size 50 in Figure 6(a) represents the distribution of  $M^*[N^*/50] = 1000$  estimates of  $\hat{K}(50)$  just as the boxplot at subsample size 50 in Figure 3(a) represents the distribution of M[N/50] = 1000 estimates of r(n). As long as the product,  $M \times N$ , remains constant, the only effect that changing the number of replications has, up to rounding in  $[N/n_i]$ , is to change the results in the regression on the averages. By using  $M^* = 20$  and  $N^* = 2500$ , SIMTB1 reports regression coefficients averaged over 20 replications, but,

within each replication, the dependent variables are averages over just  $|2500/n_i|$  values of the estimator.

(4) The boxplots are presented using the reduced graphics option. In this option any extreme outliers (i.e., those beyond 1.5 interquartile distances) are included as a count at the tail of each boxplot. This option was chosen in order to give more graphical weight to the body of the distributions and the fall-off in the bias. Limited printer resolution makes it impossible to show details in the body and the tails of the distributions if there are many straggling outliers. In the case of very extreme outliers, no detail would be seen in the body of the boxplot without the reduced graphics option.

Figure 6(b) looks at the distribution of the moment estimator of K, the shape parameter of a Gamma (K) population:

$$\widetilde{K}(n) = (n-1) \overline{X}^2 / \sum_{i=1}^n (X_i - \overline{X})^2$$

where  $\overline{X} = \sum_{i=1}^{n} X_i/n$ , n is the subsample size, and the  $X_i$ are the simulated Gamma(5) random variables. The SIMTB1 options and parameters mentioned in (2), (3) and (4) preceding are also in effect here.

The two Figures, 6(a) and 6(b), show a very pronounced bias in both estimation procedures, although the moment estimator is slightly closer to the unbiased value of 5. As expected, the standard deviation of the m.l.e. is lower than that of the moment estimator although the relative

difference at small subsample sizes, for instance 1.448 versus 1.482 at  $n_1 = 33$ , may not outweight the increase in bias with the m.l.e. At larger subsample sizes, the relative difference is close to the theoretical asymptotic relative efficiency of .78 (i.e., .91 at  $n_7 = 250$ ).

Both estimators also show distributions with positive skewness and kurtosis that decrease to the asymptotic 0 levels as subsample size increases. The asymptotics appear to take hold more quickly for the moment estimator than for the m.l.e.

In summary, SIMTBl shows that the m.l.e. is indeed better than the moment estimator in terms of variance, but not as good for small sample sizes as asymptotic results would lead us to believe. In the other areas of bias and asymptotic Normality, the moment estimator would have to be preferred.

# C. 4-FOLD JACKKNIFED ESTIMATORS OF K

Figures 6(c) and 6(d) show the distributions of the 4-fold jackknife m.l.e. of K and 4-fold jackknifed moment estimator of K, respectively. A 4-fold jackknife estimator is similar to the 2-fold jackknife estimator described in Section VI.F. except that there are 4 pseudo-values that come out of dividing each subsample into fourths. More details can be found in Mosteller and Tukey (1977) [Ref. 6].

The purpose of the jackknife is to remove the conspicuous bias observed in Figures 6(a) and 6(b). This goal is seen to be accomplished in Figure 6(c) and 6(d) and we can also note

smaller values of skewness and kurtosis, indicating a quicker approach to asymptotic Normality. The skewness and kurtosis of the jackknifed moment estimator are the lowest, at small subsample sizes, among all estimators. The variance of the jackknifed moment estimator is also only slightly inflated, as is the variance of the jackknifed m.l.e.

All told, the jackknifed moment estimator, because of its lack of bias, small variance, and low skewness and kurtosis, would be the method of choice if estimation of K or significance testing was the goal.

D. RESULTS FOR K = 0.25

In Figures 7(a), 7(b), 7(c) and 7(d) we show similar results to those discussed above for the case K = 5.0, but using K = 0.25. The fact (Cox and Lewis, 1966, Ch. 3) [Ref. 7] that the m.l.e. estimate is much more efficient than the moment estimate is graphically illustrated. What is new is the effect of jackknifing: bias is reduced without the sacrifice of variance inflation or nonnormality.

Further comparisons and interpretations are similar to those done for the case K = 5.0, and are left to the reader.

E. CONCLUSIONS

Simply by providing SIMTB1 with the desired estimators, we have been able (a) to explore in depth the effects of changes in data distribution and of different estimation procedures on the calculation of the serial correlation

coefficient, and (b) to compare four different ways to estimate the shape parameter in a highly skewed Gamma population.

The graphics and numerical output combine to let us see and quantify distributional changes that occur as subsample size grows. We can see bias fall away, variance shrink, and skewness disappear as the estimator approaches asymptotic Normality. Terms in the asymptotic expansion of the mean and variance of the estimator are automatically calculated and can be used to compare different estimators.

# VIII. COMPARISON OF DIFFERENT METHODS FOR ESTIMATING THE VARIABILITY OF THE STANDARD DEVIATION OF CORRELATION ESTIMATES

#### A. INTRODUCTION

Bradley Efron and Gail Gong (1982) review in their article, "A Leisurely Look at the Bootstrap, the Jackknife, and Cross-Validation" [Ref. 9] different methods for estimating statistical error of parameter estimates. They discuss in particular the problem of estimating the error of a statistical estimator with the example of the estimates of the standard error for the correlation coefficient of a bivariate normal distribution. They compared the standard deviation estimates of different methods using 200 simulations at one fixed sample size of 14.

SIMTB2 was used to explore the distributions of the estimates they used in their article. The bootstrap, the jackknife, the infinitesimal jackknife (delta method) and the normal theory are the methods for which the distributions were explored. The estimation methods will not be explained in detail (see Efron and Gong in The American Statistician, Feb. 1983, Vol. 37, No. 1), only the setup of SIMTB2 and the output will be discussed.

#### B. SETUP OF SIMTB2 AND THE ESTIMATOR FUNCTIONS

The bivariate normal distributed input data with known correlation 0.5 was generated with an IMSL random number

generator (GGNSM). 14,000 bivariate data points were generated and then sectioned into 10 blocks, each having 1,400 points (M = 10, N = 1400). The subsample sizes (NE(k)) used are 10, 14, 20, 28, 35, 40, 70 and 100. Only subsample size 14 was used by Efron and Gong.

The program had to be run with 5 different standard deviation estimator functions. SIMTB2, as the other versions, can only handle up to 3 estimator functions in one program run. To make the given outputs comparable the fixed scale option (SVS = 1, YMIN = 0.0 and YMAX = 0.7) was chosen.

The bootstrap estimate of standard deviation was done with 2 different numbers of bootstrap replications (B = 128, B = 512). So for the subsample size of 14, the bootstrap procedure with B bootstrap replications in itself was done (1400/14 = 100; 100\*10 = 1000) 1,000 times.

The jackknife function followed the standard jackknife procedure and used the jackknife formula for the standard deviation:

$$s_{jack} = \left[\frac{n-1}{n} \sum_{i=1}^{n} (\overline{X}_{(i)} - \overline{X}_{(\cdot)})^2\right]^{1/2}$$

with

$$\hat{\Theta}_{(j)} = \hat{\Theta}(\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_{i-1}, \mathbf{x}_{i+1}, \dots, \mathbf{x}_n) \text{ for } \overline{\mathbf{X}}_{(i)}$$

and

$$\hat{\Theta}_{(\cdot)} = \frac{1}{n} \sum_{i=1}^{n} \hat{\Theta}_{(i)}$$
 for  $\overline{X}_{(\cdot)}$ 

The delta method (infinitesimal jackknife) function calculated the estimate with the formula:

$$\mathbf{s}_{\text{Delta}} = \{ \frac{\hat{\rho}^2}{4n} [ \frac{\hat{\mu}_{40}}{\hat{\mu}_{20}^2} + \frac{\hat{\mu}_{04}}{\hat{\mu}_{02}^2} + \frac{2\hat{\mu}_{22}}{\hat{\mu}_{20}\hat{\mu}_{02}} + \frac{4\hat{\mu}_{22}}{\hat{\mu}_{20}^2} - \frac{4\hat{\mu}_{31}}{\hat{\mu}_{11}\hat{\mu}_{02}} - \frac{4\hat{\mu}_{13}}{\hat{\mu}_{11}\hat{\mu}_{02}} ] \}^{1/2}$$

with

$$\hat{\mu}_{gh} = \frac{1}{n} \sum_{i=1}^{n} (Y_i - \overline{Y})^g (Z_i - \overline{Z})^h$$

and

 $X_i = (Y_i, Z_i)$ 

In doing the actual calculations for the delta method, for small subsample sizes  $(10, 14, \ldots, 40)$  the value of the variance becomes negative. A negative variance can not be interpreted with much meaning. The number of negative values goes down (from 305 for NE(1) = 10 to 18 for NE(6) = 40) with increasing subsample size. Most of the negative values are small. To solve the programming problem (square root of a negative number) the function sets this negative value to 0.0D0.

For the normal theory estimate, instead of carrying out a bootstrap, an approximation formula was used. It is the

same formula the article uses for the comparison.

$$S_{norm} = \frac{(1 - \hat{\rho}^2)}{\sqrt{(n-3)}}$$

See Efron and Gong for details.

#### C. INTERPRETING THE SIMTB2 OUTPUT

The output of the program runs is provided as Figures 6, 7, 8, 9 and 10. A comparison of the numerical output (subsample size 14) with the results is done in Table 3.

The bootstrap procedure (Figures 8 and 9) was done with 2 different numbers of bootstrap replications (B = 128and B = 512). Both distributions for the standard deviation (S.D.) look very similar. Both are positively skewed with some outliers at the right tail. In both cases the outliers are in the same range. As the boxplots and the summary statistics show, the increase of the number of bootstrap replications (B) does not result in a large improvement in the performance of the estimation function.

The jackknife estimate (Figure 10) has a positively skewed distribution with outliers. The distribution of the jackknife estimate looks very similar to the distribution of the bootstrap estimates. For small subsample sizes the bootstrap distribution has more outliers. Overall the performance of the jackknife procedure is as good as the bootstrap, but the jackknife needs less computer time.

TABLE 3

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ESTIMATES OF THE STANDARD DEVIATION FOR THE CORRELATION COEFFICIENT FOR A BIVARIATE NORMAL WITH TRUE CORRELATION  $\rho = .5$ 

	Summary (Efron	Statisti & Gong (1	c 200 7 982))	rials	Summary SIMTB2	Statisti (M = 10, 1	c = 1000 N = 140	Trials 0, NE(k) = 14	<u> </u>
	Ave	s.D.	CA	MSE	Ave	s.D.	cv	<b>MSE</b>	
Bootstrap B = 128	.206	.066	.32	0.062	.212	0.059	.28	0.059	
Bootstrap B = 512	.206	.063	.31	0.064	.212	0.058	.27	0.058	
Jackknife	.223	.085	.38	0.085	.226	0.086	.38	0.086	
Delta Method	.125	.058	.33	0.022	.157*	0.096*	.61*	0.074*	
Normal Theory	.217	.056	.26	0.056	.217*	0.055	.25	0.055	
True Value	.218								

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negative values set to 0.0 ×

The distribution of the estimates produced by the delta method (Figure 11) is negatively skewed and has nearly no outliers. But in calculating the estimates the problem of negative values for the variance came up. For some subsamples, the final estimate (the standard deviation) could not be calculated, since the corresponding value of the variance was negative. In these cases, the standard deviation was set to 0.0. This procedure influences the distribution and the summary statistics. The influence is more important for small subsample sizes than for larger ones. So the graphical and numerical output should be seen with this fact in mind.

The normal theory function (Figure 12) produces estimates with a negatively skewed distribution but only a few outliers and the distribution is tailed to the left. The tail of the distribution is in the opposite direction of all other distributions. For the estimate of the standard deviation for the correlation coefficient the result of the normal theory is close to the true result. This may not be valid for other estimators.

In addition to the comparisons Efron and Gong did, with SIMTB2 it is easy to investigate how the sample size will influence the estimate of the standard deviation of the correlation coefficient. In Table 4 the methods are compared for a subsample size of 10 and 100. With increasing subsample size the quality of the estimate should improve, but the

TABLE 4

FOR THE CORRELATION WITH TRUE CORRELATION SIMTB2(M = 10,N = 1400) ESTIMATOR OF THE STANDARD DEVIATION COEFFICIENT FROM A BIVARIATE NORMAL  $\rho = 0.5$  AT DIFFERENT SAMPLE SIZES.

	Sub	1400 Tria	als ze 10		Sut	140 Tri. sample S.	als ize 100	
	AVE	s.D.	c.v.	<b>MSE</b>	AVE	s.D.	c.v.	<b>MSE</b>
Bootstrap 3 = 128	0.26	0.083	0.32	0.083	0.087	0.0076	0.088	0.013
Bootstrap B = 512	0.26	0.082	0.32	0.082	0.087	0.0077	0.088	0.014
Jackknife	0.28	0.13	0.46	0.13	0.076	0.011	0.14	0.011
Delta Method	0.18*	0.12*	0.64*	0.148*	0.071*	0.016*	0.22*	0.016
Normal Theory	0.027	0.082	0.31	0.082	0.076	0.0076	0.1	0.008
<b>True Value</b>	0.267				0.0753			

\*
negative values for Variance set to 0.0
improvement may be different for the different methods of estimation. By making the subsample size 10 times larger, with the SIMTB2-side effect of reducing the total number of calculated estimates, the bootstrap improves less than the jackknife, delta method and normal theory.

## IX. FINAL CONCLUSIONS

SIMTBED with the different versions can be used on digital computers of different size (mainframe to micro) and type. The limitations in using the program are given more by hardware constraints like memory size and computer time than by the program itself.

The FORTRAN program is completely portable, changes in the code, may only be necessary to adapt the program to special restrictions given by a special type of hardware. This may occur in using micro computers more often than with mainframe computers. Up to now all versions of code are written for the more normal standard computer environment and do not need special equipment (color printer, etc.). Additionally hardware dependent features like color output can improve the graphics of the program.

SIMTBED makes it easy to evaluate the result of statistical experiments. The combination of graphics and numerical summaries for different sample sizes make it easy to judge the distributional behavior of a statistical estimator. The result can be seen without additional computations in the graphic outputs. Comparing only the boxplots it is possible to judge the influence of subsample size on the variability of an estimator.

Besides for research the program can be used in showing students the distributional behavior of different estimators in a pictorial way. It is easy to compare the different behavior of similar estimators (e.g., biased vs. unbiased estimator of the variance) for different sample sizes.

The easy use and the fast visual impression of the distributional behavior of an estimator, given by the graphic output is one of the advantages in using SIMTBED. Besides this fast first visual impression all necessary and needed numerics are given for further and deeper investigations.





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Coefficient for a Lognormal (0,1) Sample

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4-Fold Jackknifed Maximum Likelihood Estimate of the Shape Parameter of the Gamma Distribution (k = 0.25)Figure 7c.



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## 4 APPENDIX

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## (VERSION 1) PROGRAM LISTING SIMTBL

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SAMI CTS GTS JUNN NUNN NUNN NUNN TO GENERATE REGRESSION ADJUSTED ESTIMATES AND BCX OF ESTIMATES OF AN INPUT RAW DATA SERIES X CONTAIN (REFLICATIONS) OP N VALUES EACH. UP TO 3 ESTIMATI FUNCTIONS CAN BE USED. THE GRAPHS CAN ALL BE OF 7 SCALE OR SCALED INDIVIDUALLY. PARAM FTFRS 10 **NFSCETDTTON** FUFFCSB

(L)

M	REAL+4 ARRAY CONTAINING DATA. A PAXIMUM OF 50,000 DATA ELEMENTS CAN BE STORED IN X.
N	NUBERR OF CATA ELEMENTS PER SECTION (N IS SAMPLE SIZE). N CANNOT EXCEED 50,000 AND M*N MUST NCT EXCEED 50,000.
8	NUMEER OF SECTIONS (REPLICATIONS). M CANNOT EXCEED 100 AND M+N MUST NOT EXCEED 50,000.
di N	INTEGER ARRAY OF SIZE & CONTAINING SUESAMPLE SIZES FOR N. THE VALUES OF NE MUST BE PROM SMALLEST TO LARGEST. NO ELEMENT OF THE ARRAY NE CAN BE GREATER THAN N. M* (N/NE(1)) MUST NOT EXCEED 12,500.
П	NUMEER OF SUBSAMPLE SIZES FROM NE (C) THAT WILL BE USED TO
	IT IS ALSO THE NUMBER OF BOXPLOTS THAT WILL BE FRODUCED.
Ð	DEGREE OF REGRESSION FOR MEAN AND VARIANCE REGRESSIONS. D WILL BE REDUCED BY RAGE IF THE SAMPLE IS NOT LARGE ENCUGH. D MUST BE 1,2 OR 3. D=0 WILL IGNORE REGRESSIONS.
	*** SCALING *** SCALING IS ACCOMPLISHED BY TAKING THE SMALLEST AND THE LARGEST ESTIMATE VALUES FROM ALL ESTIMATING FUNCTIONS
	THE SEI PARAMETER ALLOWS THE USER TO SCALE THE GRAPHS CF EACH ESTIMATOR INDIVIDUALLY OR TO SCALE THE GRAPHS
	THE SAME SCALE. SCALING ALL TO THE SAME SCALE IS Accomplished by taking the minimum and maximum estimate from at the pertmators hered by in screamery site
	TICAL SCALE TO: THE UPPER QUARTILE USER TO RRECUCE THE VER- TICAL SCALE TO: THE UPPER QUARTILE LISTANCE + 1.5 TIMES INTERQUARTILE DISTANCE AS THE MAX VALUE AND THE LOWER

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MICROCOPY RESOLUTION TEST CHART NATIONAL BUREAU OF STANDARDS-1963-A

THE FROM ZE. ED Ci M # ATOR. ESS CAL ш ΕY HONE H \*\*\* HX ·H HE 0 HHH CUARTILE - 1.5 TIMES THE INTERQUARTILE DI STANCE AS MIN VALUE. THE INTERQUARTILE DI STANCE IS COMFUTED TET SAMPLE OF ESTIMATES FROM THE NE(1) SUBSAMFLE SI IF THERE ARE NO ESTIMATES FROM THE NE(1) SUBSAMFLE SI VALUES THEN THE SCALE IS TO THE FIRST VALUE WITHIN. TF THER E ARE AND THE NUMBER PRINTED AT THESE MIN AND MAN ARE COUNTED AND THE NUMBER PRINTED AT THE ENDS OF T ECX PLOTS. PARAMET ALLOWS THE USER TO SET THE VERTI SCALE. WHEN THE VERTICAL SCALE IS SET THE SET PARAFI IS TGNO RED AND THE VERTICAL SCALE IS SET THE SET PARAFI ( N) WI POINT RAGE) T THA UNIT BE Ē \*\* ທີ່ສີ H CALCULATE E PI 11 ŝ Ω ► TH EACH ESTIMATOR (EST 2, 3). N BE USED TO DESCRIEE EACH EST IECLARED AS REAL + 8 (15) ARRAYS TOF THE CALLING FRCGRAM RAGE. LE AS AN ARGUMENT THERE MUST CTERS BETWEEN APOSTFOPHES. AP ID YMAX. S V S SEI SV ŧ NDIVIDUALL ALLY. \* \* \* \* \* \* \* \* \* \* \* \* PNAME (X, CFDATA CGRAM (RA ES MUST BE C.C. 5 HEN EN 121 121 (LL) (CL) THE VERTICAL SCALE OF THI S VERTICAL SCALE TC UPPEI INTERQUARTILE LISTANCE. H 3 VERTICAL SCAL 3 H ILL 10 ER USER IDU COLATE THE ESTIMATOR FUNCTIONS THAT WI COLATE THE STATISTICAL PARAMETER. I SEQUENCE ON EACH FUNCTION IS: CALL S THE DATA ARRAY AND N IS THE NUMBER THE DATA ARRAY AND N IS THE NUMBER THEY ARE USED IN THE CALLING FRO ORDER THEY ARE USED. DUMMY VARIABLES SD USED RAFHS ÷ ΕY ΒY \* ٠ X DATA. НЦ SET OH # S ÷ TECALI - v ÷ RSH \* \* SCALE. SCALE. STHAT WI MATO GRAE AM WILL CALCULA' SETS VERTICAL S' \* \* STI BS # # VERTICAL VERTICAL CIATED WIT ACTERS CAN AOST BE DE A ARGUMENT CHARAC ATORS AMETER 2 OR 3 101 REDUCE T GRAPHICS .E + (-) ESTIMAT # # ESTINI AL PARI ¥ \* 90 101 111 111 LE DGR . 0F **184** TIES ASS 120 CHA 106 TITLE 106 AS 16 PASS 16 PASS 16 NIMUM OF REDU OUAR 1 UMBER OF STATISTICA IEST MUST VALUI SCAL PB( US) VA LUE # \*\*\*\* EI=0 0=0 GH 0-30 0 RT INCON HARAH >> HI # à a ഗഗ SS えいえ 4 \* E CT3 Y HAX NEST 11L1 11L2 11L2 **NIHX** SVS SEI RG \* -•

Series.

BE HGW EACH GRAPH IS TO BE SCALED.
EC. 1) GC TC 50
EC. 1) GC TO 75
EC. 1) GO TO 75
ALL ESTIMATORS TO THE SAME SCALE OF ESTIMATOF W/WIDEST PTS. H NE, L, D, RG, S EI, SVS, YMIN, YMAX, NEST, EST 1, [12500] 5], TTL3 (15) VS, SH 10 09 IF (NEST.EQ. 1.0R.NEST.EQ.2.0R.NEST.EQ.3) HRITE (6,106) IF (N. LE.5600) GO TO 2 HRITE (6,105) IF (M.GE.1.AKD N TE 100. EH=WE(1) HW = H+N LT=L-1 IF(LT EQ, 0) DO 11 F=1,1 I = 1+1 TE (N. GE. 1. AND. M. LE. 100) GO TO ESTE (6, 104) GO TO 4 80 5 F (L. GE. 1. AND. L. LE.8) FITE (6, 103) EST= ( (N/NE (1)) GO TO ELE. 12500 GO TO E16, 109) 10 TEL LES ഗ 9 09 K=N/NE (L) IF (K.GE.1) GO TO 6 WRITE (6,107) TEST= { (N/NE (11) EST= (6, 10 €) TO EST.NE.0) = THIK = THAN = THAN = THAN EST.EC. ET.EC. ET.EC. +TTL1 EST2 +TTL1 EST2 REAL X (500CC REAL+8 TTL1 INTEGER NE (9 INTEGER D, 1, GRAPH ALL 

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PAIR\*\*\* ULH PAIR VECTOR WIDEST WIDEST NI KEEP KEEP SCALE FIND VERTICAL SCALE FOR 3RD ESTIMATOR. K IF(NEST II 3) GO TO 10 CALL SECEST(X N BNE(IK) EST X Y FO IF(RG EQ 1) CALL DELETO(Y KP, YMAX, YMIN) IF(TMIN II, ULH (2) ULH (2) = MIN IF(TMIN GT. ULH (4) ULH (4) = TMAX, YMIN) IF(TMUE RETURN CALCULATED SCALE TO CALLER YMIN=ULH (2) TEAX=ULH (4) CAL SCALE FCR 1ST ESTIMATOR. T (X NL MNE (IK) F EST 1 Y KP) C ALL DELETO (F KP, FMX, YMIN) C ALL MAXMIN Y KP, YMX, YMIN) T. ULH (2) ULH (2) = FMIN T. ULH (4) ULH (4) = TMAX FIND VERTICAL SCALE FCR 2ND ESTIMATOR. IF (MEST IT 2) GO TO 10 CALL SECEST (X N H NE(IK) EST2 Y K P) IF (RG EQ 1) CALL DELETO (Y KP, YMAX, YMIN) IF (YMIN II CALL MAXMIN (Y KP, YMAX, YMIN) IF (YMIN II ULH (2) ULH (2) = MIN IF (YMAX .GT. ULH (4) ULH (4) = YMAX DC 10 FIND DC 10 FIND DC 10 CALL VERTIC CALL VERTIC VERTIC VERTIC VERTIC VERTIC VERTIC VERTIC VERTIC 50 2

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0 3, \*\*\*\*) 500, \*\*\*\*) fn Order of '/ ment' scaling'/ Le.') 102 FCEMAT (1%, FSTIMATOR: '15A8) 103 FCEMAT (1%, VERTICAL SCALE: YMIN =' F10.4' (15K' YMAX = ' F10.4') 104 FCEMAT (\*\*\*\* ERROR...L MUST BE AN INTEGER EFTWEEN 1 AND 100. \*\*\* 105 FCEMAT (\*\*\*\* ERROR...M\*MUST BE AN INTEGER FETWEEN 1 AND 100. \*\*\* 106 FCEMAT (\*\*\*\* ERROR...M\*MUST BE AN INTEGER FETWEEN 1 AND 100. \*\*\* 107 FORMAT (\*\*\*\* ERROR...M\*MUST BE 3 OR LESS. \*\*\*\*) 107 FORMAT (\*\*\*\* ERROR...N/NE(L) MUST BE 1 OR GREATER TO COMPUTE', 108 FCEMAT (\*\*\*\* ERROR...N/NE(L) MUST BE 1 OR GREATER TO COMPUTE', 108 FCEMAT (\*\*\*\* ERROR...N/NE(L) MUST BE 1 OR GREATER TO COMPUTE', 108 FCEMAT (\*\*\*\* ERROR...N/NE(L) MUST BE 1 OR GREATER TO COMPUTE', 108 FCEMAT (\*\*\*\* ERROR...N/NE(L) MUST BE 1 OR GREATER TO COMPUTE', 109 FCEMAT (\*\*\*\* ERROR...N/NE(L) MUST BE 1 OR GREATER TO COMPUTE', 100 FCEMAT (\*\*\*\* ERROR...N/NE(L) MUST BE LESS THEN'N OR ECUAL TO 3 108 FCEMAT (\*\*\*\* ERROR...N/NE(1) MUST BE LESS THEN'N OR ECUAL TO 3 108 FCEMAT (\*\*\*\* ERROR...N/NE(1) MUST BE LESS THEN'N OR ECUAL TO 3 108 FCEMAT (\*\*\*\* ERROR...N/NE(1) MUST BE LESS THEN'N OR ECUAL TO 500. \*\*\*\*) 110 FCCMAT (\*\*\*\* WAN ING...N'NE(1) MUST BE LESS THEN'N OR ECUAL TO 500. \*\*\*\*) 110 FCCMAT (\*\*\*\* WAN ING...N'NE(1) MUST BE LESS THEN'N OR ECUAL TO 500. \*\*\*\*) 110 FCCMAT (\*\*\*\* WAN ING...N'NE(1) MUST BE LESS THEN'N OR ECUAL TO 500. \*\*\*\*) 110 FCCMAT (\*\*\*\* WAN ING...N'NE(1) IS NOT SMALLEST ELEMENT SCALE.') GRAFH **GRAFH DND** QN KP, YAAX, YHIN) KP, YAAX, YHIN) ~ (N I W FIND VERTICAL SCALE FOR 3RD ESTIMATOR A IF (S V S: EQ. 1) GO TO 78 CALL SFCEST (X N M NE 1), EST3 Y K P, MAX, MIN) IF (RG NE 1) CALL MAXHIN (Y, KP, YMAX, YHIN) UIH(2) =YMIN UIH(2) CAL SCALE FOR 3RD ESTIMATOR A T (X N M NE (1) CST3 Y KP, MIN) CALL HAXMIN (Y, KP, YMAX, YMIN) FIND VERTICAL SCALE FOR 2ND ESTIMATOR CALL SECEST (X NG NE (1), EST2 YKP) IF (RG E0.1) CALL DELETO (Y, KP, YMAX, YMI) IF (RG WD 1) CALL MAXHIN (Y, KP, YMAX, YMI) UIH(2) =YMIM UIH(4) =YMAX CALL PAST (X M EST2 NE, L, RG, D, ULH, Y) WRITE (6, 107) TTL2 IF (NEST . L1. 3) GO TO 80 LE FOR 2ND ESTIMATOR NE(1) EST2 Y KP) DELETO(Y KP, MAX, Y HII HAXHIN (Y, KP, Y MAX, Y HII S CALL SECEST (X M. M.E.(1), EST1, Y.KP) IF (RG. EQ. 1) CALL DELETO (Y, KP, YHAX, YHI IF (RG. WE. 1) CALL MAXHIN (Y, KP, YHAX, YHI UIH(2) = THI UIH(4) = THI UIH(2) = THI UIH(4) = THI UIH(2) = THI UIH(4) = THI UIH(2) = THI UIH(4) = THI UIH(4) = THI UIH(2) = THI UIH(2) = THI UIH(4) = THI UIH(2) = THI UIH(4) = THI 2 2 ETU RN ND 75 78 80

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, ET (8) CRDER  $\begin{array}{c} \textbf{M}^{\#} \textbf{M} \quad \textbf{M} \text{UST} \quad \textbf{EB} \quad <= 50000) \\ \textbf{S} \quad \textbf{OF} \quad \textbf{W} \quad \textbf{VALUES} \quad \textbf{EACH} \\ \textbf{1} \quad \textbf{AND} \quad \textbf{0}) \\ \textbf{T} \quad \textbf{BE} \quad \textbf{IN} \quad \textbf{ASCENDING} \quad \textbf{CRDE} \\ \textbf{3} \quad \textbf{S} \quad <= \ \textbf{L} - \ \textbf{1} \end{array}$ HER CALC. FUNCTION \*\*\*\*\*\*\*\*\* NO. OF EEPLICATIONS (NUST BE <= 100) NUMBER CF VALUES IN EACH REPLICATION (N+W MUST BE USERS VECTOR WITH M CONSECUTIVE BATCHES OF W VALUE NO. OF SECTION SIZES (MUST BE BETWEEN 1 AND 8) ARRAY WITH THE L SUBSAMPLE SIZES (MUST BE 1N ASCE = DEGREE OF THE REGRESSION (MUST BE <= 3 & <= L-1 ) = XHIN, YMIN XM AX YMAX IN USER UNITS ONLY UIH(2) AND ULH(4) NEED TO BE PASSED. CTHERS SUEROUTINE ERST(X N, M EST NE, L, RG, UD, ULH, Y) REGRESSION ADJUSTED ESTIMATE CALCULATES ESTIMATES FROM USER DATA USING MEST" FICTS EASIC OR RETRENCHED GRAPH ON LINE PRINTER USER WRITTEN ESTIMATING FUNCTION. FUNCTION NAME (X, N) IS A VECTOR WITH N ENTRIES \*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\* # NAME OF USE USAGE: WHERE X IS \*\*\* \*\*\*\* ٠ \*\* Ħ \*\*\*\*\* ุ่ม แส้ EST 846 ÷ 000 U C

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-UIH(1) + (DLH(3) - DLH(1) / (ULH(3) - ULH(1)) + DLH(1) + 5
LAST+4 LOCX(K) = LAST+4
                                                                                                                                                                                                    REPLICATIONS
                                                                                                                                                                                                      *
                                                                                                                                           DC 80 K=1, I

REK=NB(K)

FNEK=NB(K)

ENTIONS (K)

SECTION FUTE ESTIMATORS FOR SIZE K

CALL SECEST(XNN M. RNEK EST Y.KP)

AVERAGE ESTIMATES OF SIZE NE(K) FOR EACH OF

KP=0

C_10 I=1.M
4 FLOT (I J) = BLK
3 CCWTINUE
SET HORIZONTAL XHIN, XHAX
0IH(1) = 7*KE(1)
0IH(3) =1, 2*WE(L)
SET SCALE
CALL SCALE (UIH, DLH)
CALL SCALE (UIH, DLH)
CALL SCALE (UIH, DLH)
CC HPUTE LOCATION CF EOXPLOTS ALONG X-AXIS
LAST=-1
DC 5 K=1.1
                                                                                                                                                                                                                  E K)
NE (K)
(F)
(F)
                                                                                                         IP(LOCX (N) =
IP(LOCX (N) =
IP(LOCX (N) =
IAST=100
CC WT IN UE
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*KP+3.)/(KP-1.)*(KP-2.)*(KP-3.))
(KP-1.)*(KP+KF-3.)/(KF*(KP-2.)*(KP-3))
- 3.
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              CAN
                                                                                                                                                                                            KF /( (KP-1.) * (KP-2.))
** 3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            PLOTING
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      /FLOA T (M)
0 T0 54
)-M*BA(I)**2)/(M*(M-1.))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              OR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         IF (D1. LT. 2) GO TO 113
DC 92 K=1 b
DO 47 J=1 L
CCMTINUE
CALL REEG (FA.RT.BT.L.D1.IX1.IX2)
E 1 CML REEG (FA.RT.BT.L.D1.IX1.IX2)
D 1 2 3 KT=2 L
D 2 3 KT=2 L
D 2 5 CMTINUE
CCMTINUE
CCMTINUE
                                                                                                                                                                                                                                                                                                                                ÎSCHU (YAR TVAR) - 3
= TDV
= STDV
= STDV/SQRT (FLOAT (KP))
= SKEU
= VAR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       IF D1.IT.2 THEN NO REGRESSIONS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     OVEE
SAMFLE SIZE 1
UTATION.
70 7
                                                                                                                                                                                                                                                                                (KP-2.) +
VAR+3. +
+ VAR)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         D0 94 I=1.C1
FA(I) =0.
C0 95 J=1.H
BA [I] =0.
C0 11 = BA (I) + B(I,J) **2
C0 11 = BA (I) + B(I,J) **2
FA(I) = BA (I) / FLOA T(M)
IF(M : EQ. {) CO TO 54
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   AVERAGE REGRESSION CCEFF.
                                                                                                             (0- j
                                                                                                                                                                                                                                                                         AR# (K
                                                                                                        (SUA3) + (SUA4) + (SU
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ŝ VICE SPACE TO USER SPACE \* (ULH(3)-ULH(1)) ( (ULH(3)-DLH(1)) + ULH(1) \* (AIUE PROM X AND THE REGRESSION COPFFICIENTS. + VARIANCE SCALE ASYMFTOTE, EETAO, AND PLOT ACROSS FLCT. J= (BA (1) - UIH(2)) \* (DLH(4) - DLH(2)) / (ULH(4) - UIH(2)) + DLH(2) IF (J LT 1 00R. J .GT. 50) GO TO 117 DC 120 I=3 / IHIDTH IF (PLOT (I,J) .EQ. ELK) PLOT (I,J) = DASH CCWTINUE DL H (2) MAP THE Y VALUE FROM USER SPACE TO DEVICE SPACE J=(UY-ULH (2)) \* (DIH (4) - DLH (2)) / (ULH (4) - ULH (2)) + IF(J LT 1 0R J GT 50) GO TO 98 IF(PLOT (1,J) .EQ. BIK) PLOT (1,J) = DOT CCWTINUE HITH **PROM EACH SEGMENT** 17 K=H+ (N/NE (I))
17=L
D1=D1
DC 111 I=1.L
IT = [T-1]
IT = [T-1]
IT = [N/NE (LT)]
IT = [N/NE (LT)]
IT = [T-1]
IT = [T-1 & ASYMPTOTE **BEGRESSION LINE REGRESSION CN VARIANCES** CC 98 I=3 INIDTH MAP I PROB DEVICE SFA UX=(I-DLH(1)) \* (ULH(3) COMPUTE THE Y VAIUE P UY=BA(1) CC 99 J=1, F UY=UY+BA(J+1)/UX++J CONTINUE 94 CCNTINE (I) \*\*.5 **ESTABLISH** FLOT 85 120 117 1112 **4** 8 11 66 JUUU UU 000U UU UU

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+ ULH(2) (6,156) L8=8 (6,156) (NE(I),I=1,L8) (6,157) LABEL(1) (STAT(K,1),K=1L8) TO INSURE SAMPLE SIZE IS LARGE ENOUGH TC COMPUTE STICS EFFORE ATTEMPTING TO PRINT STATS. 13 HRITE (6, 102) HRITE (6, 101) DC 90 J=1, 50 DC 90 J=1, 50 HRITE (6, 101) HRITE (6, 101) HRITE (6, 103) YLABEI, (PLOT (I, K), 1= 1, IWIDTH) ES CCHTINUE DC 115 I=1, 122 DC 115 I=1, 122 DC 115 I=1, 122 (STAT (K, 2), K=1, L1) (STAT (K, 3), K=1, L1) 15 CC WTINUE FLOT (I 2) = BLK FLOT (LOCX (J) , 1) = CBAR IX = NE(J) IX = LOCX (J) , 1) = CBAR IX = LOCX (J) I TIT (1, 2) = BLK I=1 IT = M4 (K/NE(L1)) (K1.6E.2) G0 T0 11 = L1-1 I CCNTINUE GC TO 14 HEITE (6,157) LABEL (2); (5 HEITE (6,157) LABEL (3); (5 LT = L1 DC 22 I=1,IT 130 11.0 115 22 06 5 ŝ =

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00 FCRHAT (91, 122 (1-1), 1-1)

12 FCRHAT (91, 122 (1-1), 1-1)

12 FCRHAT (91, 122 (1-1), 1-1)

15 FCRHAT (92 (1-1), 1-1)

15 FCRHAT (106 13.6)

12 FCRHAT (106 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               .FFICIENTS: 4620.6)
.6X,4620.6)
.6X,4620.6)
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ELOT (122,50), DASH, CBAR, CROSS, CSTR, CC, NUM (10)
IFLAG
/--/, CBAR/'!'/, CSTR/'*'/, CROSS/'+'/, CO/'0'/
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         tEBROUTINE EOXPRT (Y, NY, IX, PLOT, RG)
FEPABES BCXPLOT FACM VECTOR Y (IN 2-D ARRAY PLOT)
EAL Y (NY), ULH (4), DLH (4)
NTEGER RG
NTEGER*2 ELOT (122,50), DASH, CBAR, CROSS, CSTR, CC, NUM (
CGICAL*1 IFLAG
CGICAL*1 IFLAG

      156
      LABB1(5), (STAT(K,5),K=1,L1)

      151
      (BA(I), I=1,D1)

      256
      fouture

      153
      (BV(I), I=1,D1)

      256
      fouture

      153
      (BV(I), I=1,D1)

      153
      (BV(I), I=1,D1)

      153
      (BV(I), I=1,D1)

      153
      (V(I), I=1,D1)

GC TO 14
HRITE (6, 158) LABEL(4), (STAT(K,4),K=1,L1)
LT = L1
DC 33 I=1,II
                                                                                                                                    13
                                                                                     f [1
f [b/H = (L 1) ]
c = .4) g c 10
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FRINTEC. NUMEER ))=(( AND THE TO 5 FOINTS JUST SHOW THE POINTS PLOT (1 FALLS OUTSIDE WINDOW LT.1) GO TO 0 OUTSIDE WINDOW GO TO 30 J)=CSTR TO BE COUNTED C IF (NY .GE . 9) GO TO 5 U EEN LESS THAN 9 FOINTS JUST SHOW T J= (Y(I) \* YEIN) \*VSCALE + 1. C IGNORE \* AIUE IF IT FALLS OUTSIDE W . LT. XLOW) ARE **\* VSCALE+1** CALE+1. PLCAT(NY) IN-YHIN) #VSCALE+ HEAN) =CSTR 1) =DASH =DASH =DASH 33 =DASH 33 =DASH 50 TLIERS G0 TC55 #VS CAL \*VSCAL IF IT AN ЦĢ SUNO **64 64** N# 0 1001 (N I • 50= 2 U H. ----• 0 + NUE NE = S 0 EU HS Ņ 355 21 5 CHHHHHOHO ŬNĂ **UNERO** سميت HAHAHOOAA 88 20 8 S

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ENDS UP WITH HI-CRCSS POINTER (LAST FOINT LE XHI) XHI) IHX=J XHI - AND Y (I) - LE.CHI) PLOT (IX, J) =CO CHI) FLCT (IX, J) =CSTR X HI) UF WITH HI-CROSS POINTER (LAST FOINT LE IHX=J .AND.Y(I).LE.CHI) PLOT(IX,J)=CO TO INTERQUANTILE + (-) INTERQUARTILE CISTANCE. OW) PLOT(IX,J)=CC TO 26 1ST POINT GE XLCW) R. Y(I).IT. XLOW) GO TO 25 LOW-CROSS POINTER (1ST POINT GE XLCW) • BOX NUME É OF OUTLIERS UNLESS K=1,2 - YMIN) \*VSCALE EOVE AND BELOW THE EO.C) GO TO 22 MPRT(IX,J,IK, FLOT) 10 S MIN) + VSCALE ĊĔĂR 3, IHX =CBAR ENDS XHI) د د AG=. TRU SCALE 11 ບິດ H 30 52 25 26 0 1 22

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                                                                                                                                               NO
                                                                                                                                                                                      NUMPRT PLOTS THE NUMBER IK IN THE 2-D ARRAY PLOT CENTERED
THE PLOT(IX,J) POSITION.
IX = COLUEN OF MATRIX PLOT WHERE NUMBER IS TO BE PRINTED.
J = ROW OF MATRIX WHERE MUMBER IS TO BE PRINTED.
IK = NUMBER TO BE PRINTED
FLOT = 2-D ARRAY WHERE NUMBER IS TO BE PLOTED.
                                                                                                                                                                                                                                                   NUH (10) (ELCT (122 50) 5. .6. .7. .8. .9./
10) 60 TO 1
100) 60 TO 2
1000 60 TO 2
1000 60 TO 3
                                                                                                                                                                                                                                                                                                                                                                     00+10000-11000+1000-1100+100-110+10)
= NU A(11+1)
                                                                                                                                                                                                                                                                                                                                                          C-11000+1000-I100+100)/10
                                                                                                                                                                                                                                                                                                                / = NUM(I 10000+1)
-I10000*10000/11000
| = NUM(I 10000+1)
I10000*10000-I1000*1000)/100
= NUM(I 1000+1)
10000410006-11000*1000-I 100*

                                                                                                                                                                       SUBROUTINE NUMPRT (IX, J, IK, PLOT)
                                                                                 EEAL*8 TO REAL*4
=1IX2
}=SNGL(E(J))
CCNTINGE
CCNTINGE
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MATHUI
CHOLES
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DO 15 Ja
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RETURNS MAN AND MIN'VÁIUES'OF VECTOR Y OF LENGTH

REAL Y (N)

YMAX=Y (1)

YMIN=Y (1)

DC 605 J=1 N

DC 605 J=1 N

IF(Y (J) . LÍ. YMIN) YMIN=Y (J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   NEK
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           SUBROUTINE SECEST (X & H, NEK, EST, Y, KF)
FEAL X (5000C) Y (12500)
COMPUTE ESTIMATES "EST" FOR SECTION LENGTH
NEK=N/NEK
KF=0
DC 10 I=1, M
(IX-1) = NUM(I10+1)
(IX-1) = NUM(I10+1)
(IX-115+10)
(IX-115+10)
(I+11)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             , NEK)
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ELCT (11, J)
SC TO 22J
FLOT (11, J)
BETURN
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\*\*\*\* \* CUARTILE + (-) FOINT WITHIN , XTY (4) , BHAT (4) , WY (4) × NI CHOLES (XTX, XTY BHAT, N) 4), SUM, LT (4,4), XTX (4,4) VALUES .GT. YMAX) YMAX=Y(J) 25 FUNCTION PCTL(Y N P) CCMPUTES P FEACENTILE OF REAL T(N) R=F\*PLCAT(N) R=F\*PLCAT(N) I=MLXO(INT(5), 1) I=MLXO(INT(5), 1) I=MLNO(INT(5), 1) R=F-INT(R) R=F-INT(R) PCTL=Y(I)+F\*(Y(J)-Y(I)) END 90 SUBROUTINE REAL+8 L 4 REAL+4 B 4 4 CCNTINUE RETURN ENC \*\*\* \*\* \* \* \* SAAH 605 23 ບບັບ U υυυ U U

\*\*\*\*\*\*\*\*\*\*\*\* \*\*\*\*\*\*\*\*\*\*\*\*\* \*\*\*\*\*\*\*\* \* \*\*\*\*\*\*\*\*\*\* 2 HY (1) = XTY (1)/L (1, 1) DO (1) = XTY (1)/L (1, 1) SUM=0 OFC DO 600 0 = 1, II SUM=0 OFC SUM=SUM+ (WY (J) +L (I, J) ) CONTINUE HY (I) = (XTY (I) - SUM)/L (I, I) ÖĞĪTHH DECOMPOSITION ) =DSQET(XTX(1,1)) D\_K=2,N IT + BHAT = WY. 000 C. 000 CDO EHAT 0 \* \* • 700 ###U 600

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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    XT + X = XRES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 XTX
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BEAL+8 Y (8),XT (4,8),X (8,4), XTY (4),SUM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          30

CCNTINUE

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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          H
BHAT (N) = WY (N) / LT (N, N)
DC 000 II = 4, N
I = N - II + 1
SUM = 0.0 CC
D0 750 J=I, N
CONTINUE
BHAT(I) = (WY (I) - SUM) / LT (I, J))
CCNTINUE
BHAT(I) = (WY (I) - SUM) / LT (I, I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              MATRIX BUITIPLICATICN XT * Y
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              MATRIX MULTIPLICATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           DO 20 I=1 EANSPOSE IN LT
DO 20 I=1 E
DO 10 J=1 N
XT (J I)=X(I,J)
CCNTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ***
                                                                                                                                                                                                                                                                                                                                                                      DC 950 I=1 4
B [1]=SNGI (BHAT (I) )
CCNTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        XT + X = XRES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        BETURN
End
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INPLACE SORT USING SHELL ALGORITHM *********
REAL Y (N) 1EMP
INTEGEN GAE
ICGICAL EXCH
 ***********************
                                                                    ************************
                                                                                                                                                                                                                                                                                                                                 (I).GT.Y (KK))) GO TO 100
                                                                                                                                                                                                                                                                                                                                                     JÕ CONTINUE
CONTINUE
CONTINUE
CONTINUE
GÅP=(GÅF/2)
GC TO 5
CCNTINUE
                                                                                                                                                                                                                                                                         500
                                                                                    CC 50 I=1 M
SUM=0.0FC
D0 40 J=1 M
CONTINUE
CONTINUE
CCNTINUE
RETURN
END
                                                                                                                                                                                                                                                                        60 TO
                                                                                                                                                                                                                                                                GAP= (M/2)

IF (.NCT. (GAP.NE.0)) (

EXCH=TRUE.

EXCH=TRUE.

N=N-GAP

N=N-GAP

N=N-GAP

N=1.4

KK=I+GAP

IP (.NCT. (Y(I).G7)
                     -1, N
, I) = X (I , J)
                                                                  xT + Y = xTY
* BUILD XT
DC 20 I=158
DO 10 5=
CONTINUE
CCNTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                   FETURN
END
                                      C****
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## APPENDIX B

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## SIMTB2 (VERSION 2) PROGRAM LISTING

## SIMTE2 PROGRAM LISTING

TO GENERATE REGRESSION ADJUSTED ESTIMATES AND BCX PLCTS OF ESTIMATES OF AN INPUT RAW DATA SERIES X CONTAING M (REFLICATIONS) OF N VALUES EACH. UP TO 3 ESTIMATING FUNCTIONS CAN BE USED. THE GRAPHS CAN ALL RE OF THE SAME SCALE OR SCALED INDIVIDUALLY.	ICN OF PARAMETERS	REMI#4 ARRAY CONTAINING DATA. A MAXIMUM OF 50,000 DATA ELEMENTS CAN BE STORED IN X.	NUMEER OP DATA ELEMENTS PER SECTION (N IS SAMPLE SIZE). N CANNOT EXCEED 50,000 AND M*N MUST NOT EXCEED 50,000.	NUMBER OF SECTIONS (REPLICATIONS). M CANNOT EXCEED 100 AND M*N MUST NOT EXCEED 50,000.	INTEGER ARRAY OF SIZE 8 CONTAINING SUBSAMPLE SIZES FCR N. The Values of Ne Must be from Smallest to largest. No element of the Array Ne Can be greater than N. M*(N/NE(1)) MUST NOT EXCEED 12,500.	NUMEER OP SUBSAMPLE SIZES PROM NE(8) THAT WILL BE USED TO Section No.	IT IS ALSC THE NUMBER OF BOXPLOTS THAT WILL BE FRODUCED.	DEGREE OF REGRESSION FOR MEAN AND VARIANCE REGRESSIONS. D will be reduced by rage if the sample is not large encugh. D must be 1,2 or 3. D=0 will ignore regressions.	*** SCALING *** SCALING IS ACCOMPLISHED BY TAKING THE SMAILEST AND THE IARGEST ESTIMATE VALUES FROM ALL ESTIMATING FUNCTIONS	THE SEI PARAMETER ALLOWS THE USER TO SCALE THE GRAPH CF EACH ESTIMATOR INDIVIDUALLY OF TC SCALE THEM ALL TO	TEE SAME SCALE. SCALING ALL TO THE SAME SCALE IS Accomplished by taking the minimum and maximum estimat From All tee estimators using ne(1) subsample size.	THE RG FARAMETER ALLOWS THE USER TO RREDUCE THE VER- TICAL SCALE TO: THE UPPER QUARTILE LISTANCE + 1.5 TIMES INTERQUARTILE DISTANCE AS THE MAX VALUE AND THE LOWER
FUFFCSE	DESCEIPTIC	X	Z	Ð	H N	Г		Ð				

 $\alpha >$ × HE BOI ۲D 101~ ല ×£ ATOI ESS 년 전 문 AT A H . L \* -HE 22EHH # 0 TH EACH ESTIMATOR (EST 1, 2, 3), A IN BE USED TO DESCRIEE EACH ESTIM ECLARED AS REAL+8 (15) ARRAY S UNLI IT OF THE CALLING FRGGRAM RAGE. LE AS AN ARGUMENT THERE MUST BE CTERS BETWEEN APCSTROPHES. MES THE INTERQUARTILE DI STANCE AS INTERQUARTILE DISTANCE IS COMFUTED IMATES FROM THE NE (1) SUBSAMFLE SI ISTIMATES OUTSIDE THESE MIN AND MAN CALE IS TO THE FIRST VALUE WITHIN MATES OUTSIDE THESE IIMITS THEN TH HE NUMBER PRINTED AT THE ENDS OF ERT ARA BZ S APHS. E ŧ S=1 LUN LUN ω**ι** 46 LLY. Ħ CALCULAT α DATA P DATA P I RAGI SEI >0 SA SV MAX. Z 4 E E DUA S D WHEN ч<u>н</u> EN 83 **HUN** NDIVII ALLY. . R TO SET SET THE BECCMES **HH** TO YHIN AND A AD \* SGRI SGRI H ILL 10 C UPE ER AATOR FUNCTIONS THAT WIL TISTICAL PARAMETER. JACH FUNCTION IS: CALL F IY AND N IS THE NUMBER O LRED IN THE CALLING FROG C USED. DUMMY VARIABLES S THAN 3 ESTIMATORS. 24 USE US 1 HB USED AFIIS THE VERTICAL SCALE S VERTICAL SCALE TO INTERQUARTILE DIS \* BΥ 8 шолн ⋗ E USI CALI ß <u>م</u> A B EB AT WILL BE ROM X DATA ឝ £4 SE. ผมด 201 S ALLOWS THE ATICAL SCAL VERTICAL S RS<sup>1</sup> PHS ERTICAL SCAL SCALE. . MATOF μı SCAL F.B. H-CAL ES BSH н. Же VERTICAL Ô. GUARTILE - 1.5 TIME THE SAMPLE OF ESTIN IF THERE ARE NO ESTIN VALUES THEN THE SOL ARE COUNTED AND THE ECX PLOTS PARAMET SCALE. WHEN THE VEB IS IGNOFED AND THE VEB OF THE ESTIMATO LATE THE ESTIMATO SEQUENCE ON EACO THE DATA ARRAY I MUST BE DECLAREI RDER THEY ARE UG THERE ARE LESS ଳଘ୍ରଷ MO ഗപ HADZHA SSOCIATED WI ABACTERS CA LE MUST BE D S AN ARGUMEN S ING THE TIT OF 120 CHARA EARANET I PHICS (-) VERTI( E ESTINAT N WILLI ED + CGRAI ER SI OF 84 U H EDUCE OULCE AL BE LON OF \* 144 SC**N** ASS ASS щS പ Ð AUH VALUI AL US IIO 45 CALCULA CALCULA CALLULA CALL SE CALL SE THEY THEY THEY THEY THEY THEY THEY CACE 120 CACE 120 CASSED CASSED MEER ATIST Ă œ O > 91 GĦ 0-LOH Ë Ца ...... DHA ΞH ΰU >> HONASS ZUZ 24 24 ທທ ທທ 1111 1112 1113 ST2 ST2 ST2 NIW X X H AX NEST SVS EI BG S ри ни ри • .

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IL, D, RG, SEI, SVS, YHIN, YHAX, NEST, ESTI, 2500) TL3 (15) 10 00 SCALED. IF (NEST. EQ. 1.0R.NEST.EQ.2.0R.NEST.EQ.3) INTE (6,106) ESTE (M. IF F.... F(LT.EQ.0) GO TO 13 C 11 I=1,1 I = 1+1 IF(NE(I).GT.NE(I1)) WRITE(6,110) NTINUE ST=0 BE m 10 60 T0 4 (L.G.P.1.AND.L.LE.8) GO TO ST={6,103) EACH GRAPH IS 60 TC 50 60 TO 75 E. 1 AND. M.L E. 100) 6, 104) GO TO 80 ~ E (NN. LE. 5CC00) GO TO RITE (6,105) EST= (6,105) GO TO S ٥ TESTE (6, 106) TESTE (6, 106) TESTE (6, 106) TESTE (6, 107) TESTE (6, 107) TESTE (6, 105) TESTE SUBROUTIN ATTLI, EST2 REAL X (IR REAL X (IR REAL 40 TT IXTEGER W INTEGER D \* STE ST -

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PAIR\*\*\* PAIR \* \* \* ULH \*\*\*\*\*\*\*\*\*\* VECTOR WIDEST WIDEST NI KEEP KEEP IRK) IRK) RK) FIND VERTICAL SCALE FOR 3RD ESTIMATOR. IF(NEST IT 3) GO TO 10 CALL SECEST(X N M N F(IK) FST3 Y K Y MAX, YMIN) IF(RG.EO.1) CALL MAXMIN(Y, KP, YMAX, YMIN) IF(RMIN IT ULH (4) ULH (2) = YMIN IP(YMAX GT. ULH (4) ULH (4) = YMAX, YMIN) RETURN CALCULATED SCALE TO CALLER YMAX=ULH (2) YMAX=ULH (2) YAIN YAIN YAIN . azz TOR **2ND ESTIMATOR** FICAL SCALE FOR 2ND ESTIMATO 17.2) GO TO 10 SST (X N H NE (IK) 1) CALL DELETO(F, KP, YMAK, YM 1) CALL MAXMIN (Y, KP, YMAX, YM 11. ULH (2) ULH (2) = YMIN 61. ULH (4) ULH (4) = YMAX \*\*\*\*\*\*\*\*\*\* **Z**2> EST 1 Y КР. ҮМ КР. ҮМ (2) = УМЛ (4) = УМЛ ŝ MLE FOR 15 MNE(IK) beleto(f MAXMIN(Y (2)) ULH(( \*\*\*\*\* ALL ALL ULH ULH \*\*\*\*\* DIH(2) =1.E30 DC H(4) =1.E30 FIND VERTICAL CALL SECEST(X IF(RG.EQ.1) C IF(RG.NE.1) C IF(RG.NE.1) C IF(YAIN . 11. C . RTI FIND VEB ALL EST ALL EST ALL EST FRG EQ FRG NIN \* HHUHHHH 50 2

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ΗJ EH --**GR** GRI FIND VERTICAL SCALE FOR 1ST ESTIMATOR AND GR CALL SECEST(X, N, M, NE(1), EST1, Y, KP, IR, IRK) IF RG. FO. 1) CALL EELFTO(Y, KP, YMAX, YMIN) IF RG. WE 1) CALL EAXMIN(Y, KP, YMAX, YMIN) UIH(2) =YMIM UIH(4) =YMAX CALL PAST(N, M, EST1, NE, L, RG, D, ULH, Y, IR, IRK) WEITE(6, 101) ULH(2), ULH(4) WEITE(6, 102) TTL IF (WEST . 11. 2) GC TC 80 , IRK) , IRK) RK) FIND VERTICAL SCALE FOR 2ND ESTIMATOR AND CALL SECEST (X NLM NE (1), EST2 Y KP, IR, IRK) IF (RG EQ 1) CALL DELETD (Y, KP, YMAX, Y HIN) IF (RG NE 1) CALL MAXMIN (Y, KP, YMAX, Y HIN) UIH(2) =YMIN UIH(4) =YMAX CALL PRST (X M, EST2 NE, L, RG, D, ULH, Y, IR, II WRITE (6, 102) TTL2 IF (NEST . L1. 3) GO TO 80 FIND VERTICAL SCALE FOR 3RD ESTIMATOR AND IF (SVS.EQ.1) GO TO 78 CALL SECEST (X N.M. NE (1), EST3 Y KP IR, IR, I IF (RG.EQ.1) CALL DELETD (Y, KP, YMAX, YMIN) IF (RG.NE.1) CALL MAXMIN (Y, KP, YMAX, YMIN) ULH(2) = YMIN ULH(2) = YMIN 01H(4) = YMAX 01H(2) = YMIN 01H(2) = YMIN 01H(2) = YMIN 01H(2) = YMIN 01H(2) = YMAX 01H(4) = QN X 24 A LE FOR 1ST ES A NE (1), EST 1, Y ÉEL FTO (Y, KP, Y EAXAIN (Y, KP, Y 78 UU UU υ

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9 ORDER \* íد) E. 10. OF EFPLICATIONS (MUST BE <= 100) 10 MBER CF VALUES IN EACH REPLICATION (M\*N MUST FE <= 10000) 15 ERS VECTOR WITH M CONSECUTIVE BATCHES OF N VALUES EACH 15 ERS VECTOR WITH M CONSECUTIVE BATCHES OF N VALUES EACH 10. OF SECTION SIZES (MUST FE BETWEEN 1 AND 8) ARRAT WITH THE I SUBSAMPLE SIZES (MUST FE IN ASCENDING ORD DEGREE OF THE REGRESSION (MUST BE <= 3 E <= 1) XMIN, YMIN XMAX YMAX IN USER UNITS ONLY ULH(2) AND ULH(4) NEED TO BE PASSED. OTHERS CALC. HER (4), BS (4), RT (8) DLH/1.1.1.122.50:/ CBAR/1.1.1 DOT/1.1. BLK/1.HEAN, STD', STD MEAN', SKEWNESS', KURTOSIS'/ FUNCTIO JTH, UD, D, LT, CT, RG, RNEK BLK, DA SH, CSTR, NUH (10), DOT ) (b) (b) S AND VAFIANCE ERST(X & W, M EST ME, I, RG, UD, ULH, Y, IR, IEK) ACJUST ED FSTIMATE ESTIMATES PROM USER DATA USING "EST" PU C OR RETRENCHED GRAFH ON LINE PRINTER b, D1\_IWIDTH, UD D4 LT CT, RG R b) CBAR BLK, DASH CSTR, NUH( (4), DLH(4) Y (12500) T (86) VT (8) 4, LABEL (5) 4, LABEL (5) 4, B(4, 100), V (4), BA (4), BV (4 R WBITTEN ESTIMATING FUNCTION. FUNCTION NAME (X,N) A VECTOR-WITH N ENTRIES **AVERAGES** E ATA DLH/!. !. '22: 50: / CBAR/ DATA BLK/. 'DASH'. STD', STD HEA DEBLN0 (3, UC, L-1) IX1=8 IX2=4 MAEH\*N FIDTH= IFIX(DLH(3)) FIDTH= IFIX(DLH( **LIMENSION NE(L) INTEGER NB (E)** LOC X (8), D **INTEGER+2** FLOF (12250), **REAL #4** X (15, INK), ULH (4) **REAL #4** RH (8, 100), STAT (8) **REAL #4** RA (8, 4), RV (8, 4), \*\*\* USE IS ø \* \*\* NAME CF USAGE: UHERE X S C BROUTINE B E G R E S S I ON C A L C U L A T E S F I C T S E A S I C EST 86 E4 J ပ υ 

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-UIH(1) * (DLH(3) -DLH(1)) / (ULH(3) -ULH(1)) +DLH(1)+.5
LAST+4 LOCX {K} = LAST+4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              M REPLICATIONS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              0F
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IRIRK)
FOR EACH
                                                                                                                                    CCWTIMUE
SET HORTZONTAL XMIN, XMAX
UIH(1) = 7*NE(1)
UIH(3) =1,2*NE(1)
SET SCALE
CALL SCALE
CALL SCALE (ULH,DLH)
CCHPUTE LOCATION CF EOXPLOTS ALONG X-AXIS
LAST=-1
DO 5 K=1,L
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    DC 80 K=1 (K)

FNEK=NE(K)

FNEK=NE(K)

ENEK=NE(K)

SECTICN & COMPUTE ESTIMATORS FOR SI

CALL SECEST(X NN M. RNEK EST Y, KP IR

AVERAGE ESTIMATES OF SIZE NE(K) FOR

RH (K I) = 4

RH (K I) = 4

RH (K I) = 5

RH (K, I) + Y (KF)

DO 10 I = 1

RH (K I) = 5

RH (K, I) + Y (KF)

CONTINUE

RH (K, I) + Y (KF)

CONTINUE

RH (K, I) - Y (KF)

CONTINUE

CO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            NE(K) = N/NE(K)
10C X (K) = (KE)
1F(LOCX (K) . I
LAST=LOCX (K) . I
C NT IN UE
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P-2.) * (KP-3.))
(KP* (KP-2.) * (KP-3))
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                                                                                                                                                                                                                                                                                                                                                                                                      DONE
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                                                   FCR
                                                                                                                                                                                                             (KP-1.) * (KP
(KP+KE-3.)/(
                                                                                                                                                                                                                                                                                                                                                                                                      PLOTING CAN
                                                                                                                                                          * (KP-2.))
                                                   LARGE ENOUGH

      ENTSOME SAMFIE
      SIZE IS LANGE

      TT:2)
      GO TO 7

      M2:2)
      (KP - 1.0)

      SNG1
      (SUM3)
      * KP / (KP - 1.)

      M2:2)
      SNG1
      (SUM3)
      * KP / (KP - 1.)

      M2:2)
      SNG1
      (SUM3)
      * KP / (KP - 2.)

      SNG1
      (SUM4)
      (KP - 2.)
      * (KP + 3.)

      M2:2)
      SNG1
      (SUM4)
      * (KP - 2.)

      M3:2
      SNG1
      (VAR
      * VAR)
      - 3.

      M3:2
      SNG1
      (VAR
      * VAR)
      - 3.

      M3:2
      STDV
      SOR4
      (VAR
      * VAR)
      - 3.

      M3:2
      STDV
      SOR4
      (KP)
      - 3.
      .

      M4:2
      SCRUA
      VAR
      - 3.
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      .

      M3:2
      STDV
      SOR4
      - 1.0)
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      M3:2
      STDV
      VAR
      - 1.0)
      .
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      .

      M4:2
      STDV
      VAR
      - 1.
                                                                                                                                                                                                                                                                                                                                                                                                                                    IF (D1. LT. 2) GO TO 113
DC 92 K=1 2
DO 47 J=1 L
CCNTINUE
CALL REG (EA, RT, BT, L, D1, IX1, IX2)
CALL REG (EA, RT, BT, L, D1, IX1, IX2)
Dd 23 KT=2 (1
B (KT K) = ET (KT) *NE (L) ** (KT-1)
2 CCNTINUE
                                                                                                                                                                                                                                                                                                                                                                                                      OR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    E
                                                                                                                                                                                                                                                                                                                                                                                                     REGRESSIONS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   OVER
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   AVERAGE REGRESSION CCEFF.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           **2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  D0 94 I=1,D1
EA(I) =0.
C0 95 J=1,F
EA(I) =BA(I) +B(I,J) *
EV(I) =BV(I) +B(I,J) *
CONTINCE
EA(I) =BA(I) +B(I,J) *
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             {] $0 T0 54
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DEV
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SUNU = SUNU
CCNTINUE
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MOMENT
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                                                CHECK
FACH
IF (K)
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A REAL PROPERTY AND A REAL

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VICE SPACE TO USER SPACE
+ (UIH (3) - ULH (1) / (DLH (3) - DLH (1) + ULH (1)
VALUE PROM X AND THE REGRESSICN COEPPICIENTS.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       A VARIANCE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                + ELH (2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     SCALE ASYMFTOTE, EETAO, AND PLOT ACROSS PLOT.

J= (BA () - UIH(2)) * (DIH(4) - DLH(2)) / (ULH(4) - ULH(2))

IF (J LT: 1.0R, J.GT. 50) GO TO 117

DC 120 I=3, INIDTH

IF (PLCT (I.J) .EQ. BIK) PLOT (I.J) = DASH

CCMTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          HIIM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       BEGRESSION CN VARIANCES FROM EACH SEGMENT
                                                                                                                                      ASYMPTOTE
EV(I) = (BV (I) - M*BA(I) **2) / (M* (M-1.)

ES(I) = BV (I) **.5

CCNTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 V(I) *NE (L) ** (FLOAT (I) /2.)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          1 CCNTINUE

2 IF (TT.LT.DT) DT=LT

1 P (DT.LT.2) GO TO 113

PC 48 J=1 1

PC 48 J=1 
                                                                                                                                         ట
                                                                                                                                         ESTABLISH FEGRESSION LINE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 112
                                                                                                                                                                             DC 98 I=3 IKIDTH
MAP I FROE DEVICE SPA
UX= (I-DLH (1)) * (UIH (3)
COM PUTE TEE Y VALUE P
UY=BA (1)
COM FLUE A (3+1) /U X** J
COM TINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   0
F
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  111 I=1,I
IP(K.GE.2) GO 1
LT=LT-1
K=M*(N/WE(LT))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        HAP THE Y VALUE

J= (UY-ULH (2)) * (D

IF (J .LT 1 . 0R

IF (PLOT (I.J) .EQ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  K = M + (N/N E (I))

L T = L

E T = D 1

E T = D 1

E T = 1, I

L T = I T - 1, I

L T = I T - 1, I

K = M + (N/N E (I))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             CCNTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              98
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ULH(2)
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LARGE ENOUGH IC COMPUTE
PRINT STATS.
                                                                                                                                                                                                     GO TO 85
{ # (ULH (4) - ULH (2) ) / (DLH (4) - DLH (2) )
ABEL, (FLOT (I, K), ]= {, IHILTH)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    (STAT (K, 2), K=1, L1)
(STAT (K, 3), K=1, L1)
         [1] I=1,L8)

L(1) (STAT (K, 1)

AMELE SIZE IS,LA

ATTERETING TO P
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      JRE AT.
JRE AT.
LI (K1, GE.2) GO TO 11
*1 CCNTINUE
11 WRITE (6, 157) LABF
IT = L1
11 WRITE (6, 157) LABF
IT = L1
DC 22 I=1
DC 22 I=1
       *** *****
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          EEFORE AN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CCALL NUCCCALL
HRITTE (CCALL NUCCCALL NUCCCALL
HRITTE (CCALL NUCCCALL NU
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FIOT
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4 G20.6
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                                                                                                                                                                           IC TENTS: '
3X 4620.6)
1,4620.6)
                                                                                                                                                                                                                                                                                                          ELOT (122,50), DASH, CEAR, CROSS, CSTR, CC, NUM (10)
LFLAG
                                                                                                                                                                                                                                                                                   SUEROUTINE EOXPRT (Y NY, IX, PLOT, RG)
PREPARES BCXPLOT FKCM, VECTOR Y (IN 2-D ARRAY PLOT)
FEAL Y (NY), GLH (4), DLH (4)
INTEGEA RG
INTEGER*2 FLOT (122,50), DASH, CEAR, CROSS, CSTR, CC, NUM (
ICGICAL*1 IFLAG
                                                                                                                                                                           AVERAGES - CCE
COEFFICIENTS:
COEFFICIENTS:
                                                                                                                                                                                                                      X COEFL
                                                                     GO TO 444
(BA [ ], [=1,D1)
(BA [ ], I=1,D1)
(BV [ ], I=1,D1)
(BS [ ] , I=1,D1]
                (6,158) LABEL (4), (STAT (K,4),K=1,L1)
                                                                                                                                                                                                                          DN ON VARIANCE -
ITZE (N): 15,20X
EGRESSION (D): ',
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DF REGRESSION -
F REGRESSION -
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                                                                                                                                                       , 122A1, 1
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                                                                                                                     I=1, DT)
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                                                                                                                                                                      E-4) GC TO
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PRINTEC. NUM EER Tehn 9 FOINTS JUST SHOW THE POINTS T HE ANC 88 20 a رى

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(IHX (IHX LE ы Г nEXT\_LINE ENDS UP WITH HI-CROSS POINTER (LAST FOINT
IP (Y []) .LE.XHI) IHX=J
IF (Y []) .GT.XHI .AND.Y(I) .LE.CHI) PLOT (IX,J) =CO
IP (Y []) .GT.CHI) .ELOT(IX,J) =CSTR
CCNTINUE
GC TO 56 NEXT LINE ENDS UP WITH HI-CROSS POINTER (LAST FOINT IF(Y (I).LE.XHI) IHX=J IF(Y (I).GT.XHI).AND.Y(I).LE.CHTN NOT CCNTINUE NCE. IF/L/L/GF.CLOW AND.Y(I).LT.XLOW) PLOT(IX,J)=CO THIS IS THE LOW-CRCSS FOINTER (IST POINT GE XICU) FLAG=.TRUE. IX\*J LINE ENDS TO TO XLCW) Total DISTA INTERQUARTILE Ó BOX UNLESS IF K. EQ. 2 I N=I II IF K. EQ. 2 J= (CHI-YHIN) \*VSCALE IF J. GT.50 J=50 IF (IK.EQ.0) GO TO 22 CALL NUMPRT (IX,J, IK, FLOT) CCNTINUE THE (-)+ EELOW T.CHI) III=III+ C.OR. J.LT.1 F.CLOW AND.Y(I .CR. Y(I).IT.XL EE LOW-CROSS PO NUMBER OF OUTLIERS K=1,2 TO INTERQUARTILE **\*VSCALE+** + BARS AFOVE AND E 2 I=ILX,IQ1 T (IX,I)=CBAR INUE H-YMIN) + VSCALE CLON. HI, EQI=1 FILL B CC 32 FLOT CC NTIN DC 33 SCALE 56 55 Ē 0e 22 32 25 26 JUUU ပပ

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CIM (IX1)

DIM (IX2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           *
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) XTX (4 4 4 ) XTY (4 )
EAL+8 *$**$**********
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      *****
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           (3) -DLH (2) / (ULH (3) - ULH (2)
(4) -DLH (2) / (ULH (4) - ULH (2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                YS, BS, M, N, IX1, IX 2)
Y=X+B
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         D IN AN ARRA
AN ARRAY OF
AN ARRAY OF
Y(IX2,IX2)
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FCEUST REGRESSION ON Y=X4BS,M,N,IX

Y=H-VECTOR CONTAINED IN AN ARRAY O

B=N-VECTOR CONTAINED IN AN ARRAY O

B=N-VECTOR CONTAINED IN AN ARRAY O

WY=WCFK ARRAY OF DIM(IX2,IX2)

WY=WCFK ARRAY OF DIM(IX1,IX2)

WY=WCFK ARRAY CF DIM(IX1,IX2)

WY=WCFK ARRAY CF DIM(IX1,IX2)

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WY=WCFK ARRAY CF DIM(IX2)

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r(IX<sup>+</sup>1J) = NUM(I10+1)

r(IX<sup>+</sup>1J) = NUM(I10+1)

r(IX<sup>+</sup>2,J) = NUM(I10+1)

r(IX<sup>+</sup>2,J) = NUM(I1+1)
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THE PLOT(IX,J) POSITION.
IX = CCLUMN'OP MATRIX PLOT WHERE NUMBER IS TO BE
J = ROW OP MATRIX WHERE MUMBER IS TO BE PRINTED.
IK = NUMBEF TO BE PRINTED
FLOT = 2-D ARRAY WHERE NUMBER IS TO BE PLOTED.
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"'SECOND DIMENSION OF ARRAY XW DCES NOT MATCH"
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LATA IRK2/ 3/
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REAL X (IR, IFK) , Y ( 12500), XW (5000, 3)
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KP=KE+1
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E SCALES THE GRAPH TO UPPER (LOWER)
INTEROU ARTILE DISTANCE OR TO FIRST
ITS IF NC FOINTS EXIST OUTSIDE.
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RFTURNS MAX AND MIN (Y, WAIUES, OF VECTOR Y OF

YMAX=Y ()

YMIN=Y ()

YMIN=Y ()

CC 605 J=1 N

CC 605 J=1 N

CC 605 J=1 N

FT (Y (J) . G1. YMIN) YMIN=Y (J)

FT (Y (J) . G1. YMAX) YMAX=Y (J)

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, XTY (4) , EHAT (4) , WY (4)
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ELA T [1] = 0.CDO
CC 5d J = 1.N
CC 10 If [ J] = 0.CDO
CC 11 [ J] = 0.CDO
CC NT I NUE
DC 500 J = 1.KK
DC 500 J = 1.KK
DC 200 J = 1.KK
JJ = J - 1
DC 200 J = 1.KK
JJ = 1.CO
DC 140 E = 1 JJ
CONTINUE
CONTINU
                                                                                                                                                                                                                                                                                                   FCTL (Z, KP...25)

PCTL (Z, KP...25)

PCTL (Z, KP...25)

2.5*P22-1.5*P75

2.5*P25-1.5*P75

1.5*F25

1.5*F25-1.5*F25

1.5*F25

1.5*F255

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                                                                                                                                                                                                                                                                                                                                                                                                                        SUEROUTINE MATSO (X, XRES, M, N)
REAL+8 X (8,4), XT (4,8, XRES (4,4), SUM
                                                                         2
                                                                                                                                                                                                                                                                                                                                                                                                      ×
                                                                                                                                                                                                  -
                                                                                    WY (J) = XTY (J) L (1, 1)

DO (J) = XTY (J) L (1, 1)

II = I - 1

SUM=0.0 LC

DO 600 -= 1 II

CONTINUE

WY (I) = (XTY (I) - SUM) /L (I, I)

CCNTINUE
                                                                                                                                                                                                                                                                                                                                                                                                    TX
                                                                         PART 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                      \begin{array}{c} \text{EUILD} & \textbf{X} - \textbf{T} \text{ EAN SPOSE IN LT} \\ \text{DC} & 20 & \textbf{I} = \begin{array}{c} \textbf{X} & \textbf{Y} \\ \textbf{D} & \textbf{10} & \begin{array}{c} \textbf{S} & \textbf{z} \\ \textbf{J} & \textbf{z} \\ \textbf{X} & \textbf{I} \\ \textbf{J} & \textbf{I} \end{array} \right) = \textbf{X} (\textbf{I}, \textbf{J}) \\ \text{CCNTINUE} \end{array}
                                                                                                                                                                                                                                                                                                                                                                                                   MATRIX BULTIPLICATION
L I
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B (I)=SNGI (BHAT (I) )
CCNTINUE
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N I
                               I (J, I)
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DC 540 T
DC 530 T
TT I
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                                                                          = XTY
                                                                                   SUEROUTINE MATMUL ( X,Y,XTY,M,N )
REAL+8 Y (8) ,XT (4,8) ,X(8,4) ,XTY (4) ,SUM
                                J= SOM + (XT (I,K) * X (K,J)
                                                                                                                                                                                                          SUBEROUTINE SORT (Y,N)
INFLACE SORT USING SHELL ALGORITHM
REAL Y (N),TEMP
INTEGER GAF
ICGICAL EXCE
                                                                          X + TX
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                                                                         MATRIX PULTIPLICATION
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CONFINUE
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     XRES
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CONTINUE
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               DO 20 I=1 1
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10 IF (.WOT.(GAP.WE. 0)) GO TO 500
10 EXCH=.TRUE.
 K=N-GAP
 K=T-GAP
 K=I-GAP
 KK=I+GAP
 KK] F (AB)
 KK=I+GAP
 KK] = 1.K
 KK]
 KK = I+GAP
 KK] = 1.K
 KK]
 KK = I+GAP
 KK] = 1.K
 KK]
 IO
 IP (.WOT.(FK) = 1.K)) GO TO 100
 IP (.WOT.(FK) = 1.K)
 CONTINUE
 IO
 CONTINUE
 CONTINUE

J.

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APPENDIX C

SIMTB3 (VERSION 3) PROGRAM LISTING

SINTE3 FROGRAM LISTING

CF EACH ESTIMATOR INDIVIDUALLY CR TC SCALE THEM ALL TO THE SAME SCALE. SCALING THE MININUM AND MAXIMUM ESTIMATE ACCOMPLISHED BY TAKING THE MININUM AND MAXIMUM ESTIMATE THE BG FARANETER ALLOWS THE USER TO RRFCUCE THE YER-TICAL SCALE TO: THE UPPER QUARTILE USER TO RRFCUCE THE YER-TICALS AND THE DISTANCE AS THE USER TO RRFCUCE THE YER-INTERQUARTILE - 1.5 TIMATE ALLOWS THE MAXIMUM AND THE FOR SAMPLE TICALS THE POINT THE DISTANCE AS THE DISTANCE AS THE THE SAMPLE - 1.5 TIMATES THE NATHER DISTANCE AS THE THE SAMPLE OF ESTIMATES FROM THE NEALL SUBSAMPLE SIZE IF THER ARE NO ESTIMATES FROM THE NEALLS UND MAX VALUES THEN THE SCALE IS TO THE FIRST VALUE WITHIN. THE FARE ARE NOUNTED AT THE FIRST VALUE WITHIN. THE THER E ARE NUMBER PRINTED AT THE ENDS OF THE ECX PLOTS. THE SVS PARAMET ALLOWS THE USER TO SET THE YEAR AND YAX. IS TGNO RED AND THE VERTICAL SCALE IS SET THE YEAR AND WAX. ERTED ×a (e.) ATOI S. HHN O INSI <2 E HS. E SVS= <u>Ge</u>3 E EACH ESTI . БD CALCULAT INDIVIDUALLY DUALLY. ZA AP S V S SCALE. N AND YMAX. U1 • 124 HAN T E E D HEN HEN ш Ш шщ FNAN OF I CGRAN THE VERTICAL SCALE OF TH S VERTICAL SCALE TC UPPE INTERQUARTILE DISTANCE. 3 з **H TLL** 0 L ER HE ESTIMATOR FUNCTIONS THAT WIL THE STATISTICAL PARAMETER. NCE ON EACH FUNCTION IS: CAIL F ATA ARRAY AND N IS THE NUMBER O BE DECLARED IN THE CALLING FRGG THEY ARE USED. DUMMY VARIABIES ARE LESS THAN 3 ESTIMATORS. E LEI œ SEI CAL SCALE VERTICAL SU EC DIVI TOR 9 0S) ΕY ВΥ A D T A UN SE ЕJ STIA НЗ W X DA S RS • PH S S E E E SÇALE. STIMATOR SS GRAP SCALE ΞS RS THAT W TER FROM υÞ а ы Ω. RTICAL VERTICAL 32 CALE EST VERTICAL T N N REDUCE T GRAPHICS LE + (-) SETS VEB RAMETE , 2 OR жU BD нш NN M E 1 4H 90 NAMES OF THE CAICULATE THE CAIL SEQUENCE X IS THE DATA THE AUST BE THE ORDER THE HEN THER AR NO NCT E REDUCE G UARTILI PROGRI USER OF SOC: NOT ы ца П щ TIC I UST LUE VALU -SH ous ΞŪ MPER PIIST SI MU TIES 120 VA **D**MO H H H H EI=0 EI=1 0-GH # # 30 HO HO >> Ĥ DHM ທິທ ົດທ = ZNZ à a NIN EAX ST3 ST3 ST3 112 NEST SNS EIS

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SUPROUTINE SIMTB3 (ISEED1, ISEED2, ISEED3, Y N, NE, LD, RG, SET, SVS, +YHIN, YHAX, KEST, GEND1, EST1, TTL1, GEND2, EST2, TTL2, GEND3, EST3, TTL3) 5) ARRAYS UNLESS BY VALUE THERE APOSTROPHES. 2 **1** AL+8(15 TITLE FINEEN ပ္ပ NEST.EQ.3) MDST BE DECLARED AS REI VAIUE (WHEN PASSING THE MINIMUM OF 120 CHARS. BI SCALED. BE 2 (15) TT L3 (15) .0R. 0£ 2 ' IF (N EST. EQ.1 . OR. NEST. EQ.2 .' TEST= {6.106}. IF (M GE.1 . ANC. M.LE.100) GO TO IF (M GE.1 . ANC. M.LE.100) GO TO IF (M GE.1 . AND. L.LE.8) GO TO 4 IF (LEST= {6.163}. IF (D LE.3) GO TO 5 'RITE {6.166}. 3 SI ະວິ Q TO 50 80 10 I 15 200 00) (15 CT 12 CT 12 CT 15 CT 50 13 00 ±00 ..... 60 T0 PASSED BY Passed by Must be a 00 U00 BNU \*\*\*\*\*\*\*\* 2 HCE () AE. rE.3) 60 ,101, . FQ. 0) G - E 3 0 - 1 - E 3 0 REAL ULH(4) REAL+0 TTL INTEGER NE INTEGER D, I ലല N CE 25 m N N A1 ഷഗഗ DETEI DETEI エピー HHES OFH H \*\*\*\* U U m Ś Ś U  $\sim$ 3

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F W/WIDEST PTS. PAT B\*\*\*\* \*\*\*\* ULH PAII VECTOR STI MATOR **WILDEST** WILLEST GV) (GEND1, I SEED1, N, M, EST1, NE, I, RG, L, ULH,Y 01) ULH 2), ULA (4) 02) TTL 3 , Y, KE) , Y, K F) z Y,KP) ----KEEP KEEP SCALE +GRAPH ALL FSTIMATORS TO THE SAME SCALE OF +GRAPH ALL FSTIMATORS TO THE SAME SCALE OF UIH(4) =-1.F30 ISEED=ISEEC1 FIND VERTICAL SCALE FCR 1ST ESTIMATOR. CALL SECEST (GEND 1 ISEED, N. M. N. F(IK), FST1, Y IF(RG. B0.1) CALL DELETO(Y, KP, YMAX, YMIN) IF(YMIN 11, ULH (4)) ULH(2) = YMAX, YMIN) IF(YMAX GT. ULH (4)) ULH(4) = YMAX. • XX, THIN XX, THIN XX, YHIN (GEND 2, I SEED, N, M, NE (IK), EST 2 CALL DELETO(Y, KP, YMAX, YMIN) CALL MAXMIN(Y, KP, YMAX, YMIN) ULH  $\{2, \}$  ULH  $\{2, \}$  = YMIN ULH  $\{4, \}$  = YMAX . ESTIMATOR. FIXED VERTICAL MATOR USED. ESTIMATOR Y MAN Y MAN MIN MAN CALLER FIND VERTICAL SCAIE FCR 3RD ESTI IF (NEST LIT. 3) GO TO 40 ISEED=ISEEC3 DC 30 IK=1 CALL SECEST (GEND 3 ISEED, N, M, NE, CALL SECEST (GEND 3 ISEED, N, M, NE, IF (NG NE 1) CALL MAXMIN (Y, KP, YM, IF (YM IN - 11, ULH (2)) ULH (2) = YMI IF (YM IN - 11, ULH (2)) ULH (4) = YMI IF (YM IN CALCULATED SCALE TO CALLE O CCNTINUE Y MX = ULH (2) Y MX = ULH (2) SCALE FOR 2ND USING BOXFLOTS U PCF EACH FIND VERTICAL ISEED=ISEET2 CALL SECTAL CALL SECTAL IF RG. ED. 11 IF RG. NE. 1) CONTINUE IF VMIN . 11 CONTINUE FFOCESS BO CNE CALL P CCNT INUE CALL PRST WFITE (6, 10 WRITE (6, 10 10 20 30 50 40

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TEL( PEST, IT, 2) GC TO 80 CALL PRST(6E ND2, ISEED2, NGM, EST2, NE, L, RG, D, ULH, Y, GV) IF (NEST, IT, 3) GO TO 80 CALL PEST(6E ND3, ISEED3, NGM, EST3, NE, L, RG, D, ULH, Y, GV) URITE (6, 102) ULH(2), ULH(4) CALL PEST(6, 102) TTL3 CC TO 80 GC TO 80 GC TO 80 GC TO 80 CC TO 80 T. 2) GC TO 80 EWD2, ISEED2 N, M, EST2, NE, L, RG, D, ULH,Y,GV) ULH 2), ULH (4) TTL2 TTL2 TTL2 GMD 3) GO TO 80 EWD 3) ISEED3 N, EST3, NE, L, RG, D, ULH,Y,GV) ULA 2), ULH (4) TTL3 , GV) (V) FIND VERTICAL SCALE FCR 2ND ESTIMATOR AND GRAFH. ISEED=ISEE[2 CALL SECEST (GEND2 LISEED, N, M NE(1), EST2, Y, KP) IF (RG. EQ. 1) CALL FELETO (Y, KP, YMAX, YMIN) ULH(2) =YMIN ULH(2) =YMIN ULH(2) =YMIN ULH(2) =YMIN ULH(2) =YMIN ULH(2) =YMIN ULH(2) ULH(2), ULH(4) WRITE (6, 101) ULH(2), ULH(4) WRITE (6, 101) ULH(2), ULH(4) WRITE (6, 102) IF (NEST . L1.3) GC TO 80 SEED3, N, M, EST3, NE, L, RG, D, UIH, Y 2), ULH (4) H GRA , Y, KP) AND KP.YMAX,YMIN) (P.YMAX,YMIN) ESTIMATOR FCR 3RD 78 DELETO (Y, KP MAXMIN (Y, KP SCAIE GO TO (GEND3 CALL N CALL N END3 IS ULH (2 FIND VERTICAL ISEED=ISEEC3 CALL SECEST(GE TF RG. E0.11 CAL UIH(2) =YMIN WRITE (6, 101) WRITE (6, 101) U 78 35

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\*\*\*\*\* LING. • HERE ORDE \*\* • = 50000) EACH 122) GV YMAX= 'G10.4) YMAX= 'G مكرا •# 8 \* \* +\*N MUST PE <= 500 OF N VALUES EACH AND 8) EF IN ASCENDING E = L-1 ) S \*\*\* . ပပ AL Z SETT C D'A'HIN' FUNCTIO DOT 61 • ID IN D, LT, CT, RG, RNEK SH, CSTR, NUM(10) , I, RG, UD DATA USING "EST" H ON LINE PRINTER NERATE THE DATA FUNCTION 0< ы С Ш • OF REPLICATIONS (MUST BE <= 100) IMBER CF VALUES IN EACH REPLICATION ERS VECTOR WITH M CONSECUTIVE BATCH.S RRAY WITH THE L SUBSAMPLE SIZES (MUST RRAY WITH THE L SUBSAMPLE SIZES (MUST FGREE OF THE REGRESSION (MUST BE <= 3 MULY ULH(2) AND ULH(4) NEED TO BE PASSE MULY ULH(2) AND ULH(4) NEED TO BE PASSE RIN YMIN XMAX THED ON LAST PLOT TC SUEROUTINE ERST(GENCAT, ISEED, N, M, EST, NE, REGRESSION ADJUSTED ESTIMATE CALCULATES ESTIMATES FROM USER DATA USIN FLCTS EASIC OR RETRENCHED GRAPH ON LINE GENDAT = SUEROUTINE NAME TO GENERATE THI **NTRIE**: R WRITTEN ESTIMATING FUNCTION NAME (X, N) A VECTOR-WITH N ENTRI D1, INIDTH, UD, D CBAR, BLK, DA S (20000), GV (2) (8,6), VT (8) **A** • -00 NB (E) IOC X (8), D 2 FIOT (122,50), 14 (4), DLH (4), Y 4 (6,100), STA f (8) GENLAT USE \*\*\*\*\*\*\*\* FOR S н NAME CF USAGE: WHERE X SEED PCCRMAT (11, PCCRM TNC RI CNUE R#NI R#2 ULF Ħ DIMENS] INTEGEI INTEGEI REAL \*4 RETURN<sup>-</sup> ENC CC NTIN U EITE S EE D Ħ ΗS لىن 000000 80 \* 0 2 æ 2 0ä

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SUM2,SUM3,SUM4,LABEL {5} BA (6,4) ,RV (8,4) ,B(4, 100) ,V (4) ,BA (4) ,EV (4) ,BS (4) ,RT (8) ,ET (8) ഗ  $= \{DLH(3) - DLH(1) / (ULH(3) - ULH(1)) + DLH(1) + LOCX \{K\} = LAST+4$ M REPLICATIONS L. 1. 122. 50 CBAR/ 1. SOTAL' 1. VOTAL' 1. VARTOSIS'/ CHEAN', STD', STD MEAN', SKEWNESS', KURTOSIS'/ E.I-1) AVERAGES AND VARIANCES DC 80 K=1,1 NEK=NB(K) FNEK=NB(K) SECTION & COMPUTE ESTIMATORS FOR SIZE K CALL SECEST (GENDAT, ISEED, N, M, RNEK, EST Y, KF) AVERAGE ESTIMATES OF SIZE NE(K) FOR EACH OF CCNTINUE SET HOKIZONTAL XMIN, XMAX UIH(1) = 7\*KE(1) UIH(3) =1.2\*WE(1) SET SCALE CALL SCALE (UIH,DLH) CCMPUTE LOCATION CF BOXFLOTS ALONG X-AXIS LAST=-1 DC 5 K=1,L EGRESSION MATRICES FOR NE (L) / FLOAT (NE (K) ) =1\*\* ([FLOAT (J])/2.0) -UIH(1) LAST+4 **ARRAY** ]22 |)=ELK 10 I=1, M + CCNTINUE CONTINUE CONTINUE CONTINUE CONTINUE DC 3 DIH/1 T= PLOAT RA /K ELOT I ELOT I CUTINU R E AL # 8 R E AL # 4 0 86 E4 ŝ

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P-2.)\*KP+3.)/((KP-1.)\*(KE-2.)\*(KF-3.)) R\*3.\*(KP-1.)\*(KP+KE-3.)/(KP\*(KP-2.)\*(KE-3)) VAR) - 3. DONE FOR D1.IT.2 THEN NO REGRESSIONS OR PLOTING CAN BE KE /( (KP-1.) \* (KP-2.)) \*\* 3 LARGE ENOUGH EOTPET (Y, KP, LOCX (K), PLOT, RG) K GT 8) GO TC 80 UTE HEAN AND MCHENT ESTIMATES = STDV = STDV/SQRT (FLOAT (KP)) = SKEW = CKURT = VAR IS RH (K I) = G. EO 15 J= 1, NBK KP=KP+1 GV (1) = A HAX1 (GV (1), Y (KP) GV (2) = A HAX1 (GV (1), Y (KP) CONTINUE FH (K, I) = FH (K, I) + Y (KP) CONTINUE FH (K, I) = FE (K, I) / FLOAT (NBK) CCNTI NUE CALL. BOXPFT (Y, KP, LOCX (K), PLOT CALL. BOXPFT (Y, KP, LOCX (Y), PLOT CALL. BOXPFT (Y, KP, LOCX SAMPLE SIZE UTATION. 0 2 2 2 1.0) SUM 4) \* (KP - VAR 4 VAR + / (VAF \* 1. (SUM 3) \* K (SUM 3) \* K (SUM 3) \* K (100 9 XMEAN=0. TO 180 IM 1=1, KP XMEAN=XMEAN=KEAN+Y(IM1) XMEAN=XMEAN=KEAN/FLOAT(KP) SUM2 = 0.6C0 SUM3 = 0.6C0 SUM3 = 0.6C0 SUM3 = 0.6C0 SUM4 = 1111 SUM2 = Y(1111) SUM3 = SUM2 + DEV \* D SUM3 = SUM2 + DEV \* D d L XSCH4 XSCH4 1 = XHEAN CTDV 50 # X MEAN X MEAN X MEAN EECI ACH TATS STATS STATS STATS STATS STATS CCNTI SU H KUR TAT KEN N DS AR ρ., ЧI 80 180 190 2 ധ m

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COEFFICIENTS.
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   CLH (2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           DLH(2)
                                                                                                                                                CALC.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     +
                                                                                                                                                                                                                                                                                                                                                                                                                                                                          MAP THE Y VALUE FRCM USER SPACE TO DEVICE SPACE

J= (UY-ULH (2)) * (DLH (4) - DLH (2)) / (ULH (4) - ULH (2)) +

IP(J .LT. 1. OR. J .GT. 50) GO TO 98

IP(PLOT (1,J) .EC. ELK) PLOT (1,J) = EOT

CCNTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       SCALE ASYMFTOTE, BETAO AND PLOT ACROSS PLOT.
J= (BA (1) - UIH(2)) * (DIH(4) - DLH(2)) / (ULH(4) - ULH(2))
                                                                                                                                                ω
                                                                                                                                                                                                                                                                                                                                                                     R SPACE
(DLH (3) - DLH (1))
THE REGRESSIDN
                                                                                                                                               REFLICATIONS
                                                                                                                                                                                    CC 95 J=1, M
BA (I) = BA (I) + B (I, J) ++2
EV (I) = BV (I) + B (I, J) ++2
CONTINUE
IF (I) = BA (I) / FLOA I (A)
IF (I) = BA (I) / FLOA I (A)
FV (I) = BV (I) - M + B A (I) ++2) / (M + (M - 1.))
BV (I) = BV (I) ++5
34 CCNTINUE
                                                                                                                                                                                                                                                                                                                                  A SYMPTOTE
    IF (D1.LT.2) GO TO 113
DC 92 K=1 2
EC 47 J=1,I
BT (J)=RH (J,K)
CCHTINUE
CALL RREG (FA, RT, BT, I, D1, IX1, IX2)
EALL RREG (FA, RT, BT, I, D1, IX1, IX2)
E(XT K)=Ef(KT) + NE(I) + (KT-1)
2 CCNTINUE
                                                                                                                                                                                                                                                                                                                                                              TH
VICE SEACE TO USER
* ULH(3) - ULH(1) ) / (1
* VALUE PROM X AND
                                                                                                                                                   z
                                                                                                                                                   OVEF
                                                                                                                                                                                                                                                                                                                                     ω
                                                                                                                                                                                                                                                                                                                                    ESTABLISH REGRESSION LINE
                                                                                                                                                  AVERAGE REGRESSION CCEFF.
                                                                                                                                                                                                                                                                                                                                                   CC 98 I=3 IMIDTH
MAP I FROE DEVICE SFA
UX= (I-DLH (1)) * (ULH (3)
COM PUTE THE Y VAIUE F1
UY=BA (1)
CO 99 J=1, C
UY=UY+BA (J+1)/UX**J
CONTINUE
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                                                                                                                                                                              1=1
                                                                                                                                                                       D0 94
EN(I)
EV
1
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+ ULH(2)
                                       VARIANCE
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                                       REGRESSION CN VARIANCES PROM EACH SEGMENT WITH
IF (J . IT. 1.0R. J .GT. 50) GO TO 117

CC 120 I=3, IWIDTH

IF(PLCT (I,J) .EQ. BIK) PLOT (I,J)=DASH

CC WTINUE
50) GO TO 117
                                                                                                                                                      CALL REG (FV, VT, V, LT, DT, IX1, IX2)
DC 77 I=1, ET
V(I) = V(I) *NE (L) ** (FLOAT(I) /2.)
CC NTINUE
                                                                                                                    T. D1) DT=LT
T.2) G0 T0 113
=151AT(J,6)*(WE(J)**0.5)
                                                                                     GO TO 112
                                                                                                                                                                                                                                                                                                                                               r (LŎĊX (J), 1) = CEAR
NE (J)
LOĊX (J)
                                                                                               LT=LT-1

LT=LT-1

CCMTINUE

IF(LT-LT-D1) DT=LT

IF(DT-LT-D1) DT=LT

DC 48 _=1

VT (J) = STAT(J,6)

CCNTINUE

CALL RRG(FV,VT,V,
                                                                             (X:GE.2)
                                                      K=## (N/NE(I))
I1=L
E1=D1
D0 111 I=1"I
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COMPUTE
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7 LABEL(1) (STAT(K, 1) K=1 L8)

NEURE SAMELE SIZE IS LARGE ENOUGH TC

EEPORE ATTEMETING TO PRINT STATS.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ) LABEL (5), (STAT (K, 5), K=1,L1)

GO TO 444, I=1,D1)

, (BA (I), I=1,D1)

, (BV (I), I=1,D1)

, (BY (I), I=1,D1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      TNUE
0 14
16,156) LABEI (4), (STAT (K,4),K=1,L1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                              6,157) LABEL (2), (STAT (K,2), K=1,L1)
6,157) LABEL (3), (STAT (K,3), K=1,L1)
                                                    (PLOT (I,1), I=1, IWIDTH)
PLOT (I,2), I=1, IWIDTH)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               C C MLL NUM PET (IX, 2, IK, PLOT)
WEITE (6, 104) (PLOT (I, 2), I= 1
WEITE (6, 104) (PLOT (I, 2), I= 1
LG=L
IF (L8 .GT .E) L8= 8
WEITE (6, 146) (NE(I), I= 1, L8)
WEITE (5, 146) (NE(I), I= 1, L8) (NE(I),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               122 (1-1) , + 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               I=1, DT)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         <sup>4</sup> <sup>IT</sup>
<sup>4</sup> <sup>(K/NE</sup> (L1)
<sup>6</sup> <sup>5</sup> <sup>-</sup> <sup>3</sup>) <sup>60</sup> <sup>T0</sup> <sup>12</sup>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           13
                                                                                                                                                                                                                                                                                                                                4 [N/NE(L1) )
4 [N/NE(L1) )
6 [-2] 6 C 10 11
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f (N/NE(L 1))
GE-4) GC TO
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SUESAMPLE')

SIZE '8 (18,6X),/)

A6 8614.4)

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HEFN LESS THAN 9 POINTS JUST SHOW THE POINTS
DC 8 I=1 NY
J={Y (I) -YMIN) *VSCALE + 1
J={Y (I) -YMIN) *VSCALE + 1
IGNORE VAICE IF IT FAILS OUTSIDE WINDOW
IF(J.GT.50 OR. J.LT.1) GO TO 8
IF(J.GT.50 OR. J.LT.1) GO TO 8
LICT (IX, J) =CO
SUM=SUM+f(I)
SUM=SUM+f(I)
B0 08 I=1 NY
SUM=SUM+f(I)
B0 08 I=1 NY
SUM=SUM+f(I)
B0 08 I=1 NY
SUM=SUM+f(I)
CCNTINUE
SUM=SUM+f(I)
B0 6C TO 99
SUM=SUM+f(I)
FILATEF
SUM=SCATEF
FILATEF
FILAT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          Telot (122, 50), DASH, CBAR, CROSS, CSTR, CC, NUM (10)
IFIAG
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      PLOT)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             STEROUTINE EOXPRT (Y, NY, IX, PLOT, RG)
PREPARES BCXFLOT FRCH VECTOR Y (IN 2-D ARRAY
12241, 11)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            FFAL Y (NY) , ULH (4) , DLH (4)
INTEGEARC
INTEGER*2 FIOT (122,50), D
LCGICAI*1 IFIAG
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TO BE COUNTED AND THE NUMBER FRINTED. E WITH HI-CROSS POINTER (LAST FOINT LE XHI) IHX=J INTERQUARTILE CISTANCE. XLCW) (I).LT.XLOW) PLOT (IX.J)=CO XLOW) GO TO 25 POINTER (1ST POINT GE XLCW) PLOT (IX, J) = COOUTSIDE WINDOW GO TO 30 J)=CSTR FLCT (IX, J) = CSTRINTERQUARTILE + (-) ARE . MIN) + VSCALE+1 +III=III L E + = DA SH = DA SH = DA SH = DA SH DUTL I ERS 30 T 0 55 **\*VSCALE+** - CROSS CAL IQ3 =CBAR =CBAR SV# \*\* 5 ENDS CHI) 50 LAG=.TR LINE J • ទួ 200 THOM 5 -iH GC TO I HI= 2 NOUN I=2 SCALE III=0 DC 31 DC 31 IF (Y H 3 20 30 S 25

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(IHX) а ГЕ (LAST FOINT CLOW . AND.Y(I) GO TO 31 CLOW . AND.Y(I) . LT.XLOW) PLOT(IX,J)=CO CR. Y(I).IT.XLOW) GO TO 26 E LOW-CROSS POINTER (1ST POINT GE XLCW) PLOT (IX, J) = CO IFLEFIAG CR. Y(I).IT.XLOW.GOTO'26 THIS IS TEF LOW-CROSS POINTER (1ST POINT IFLAG=.TRLE. IIX=J NEXT LINE ENDS UF WITH HI-CROSS POINTER IF(Y(I).LF.XHI) IHX=J IF(Y(I).CF.XHI).AND.Y(I).LE.CHI) PLOT(IX CCWTINUE BOX 0 NUMBEE OF OUTLIERS UNLESS K=1,2 IK=III J= (CHI-YMIN) \*VSCALE ) J=50 C) GO TO 22 T (IX,J, IK, FLOT) FELOW THE FLILL BARS REOVE AND FELOW E CC 32 I=IL X, IO FLOT (IX, I) =CBAR FLOT (IX, I) =CBAR 3 I=IQ 3, IHX FLOT (IX, ILX) =CBAR FLOT (IX, IHX) =CROSS FLOT (IX, IQ) =DASH FLOT (IX, IQ) =CROSS FLOT (IX, IQ) =CSIR SUB=CONTINUE SUB=SUB/FLCAT(NY) FLOT (IX, IQ) =CSIR FLOT (IX, IQ) =CROSS FLOT (IX, BARS AFOVE AND F T(IX,I)=CBAR INUE H-XHIN) + ASCALE PHHER ER FILL DC 3 C++++ **...**, 56 56 40 22 32 EE 26

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\*\*\*\*\*\*\*\*\*\*\*\*\*\*\* NO ED PRINTED. CENTER 3 ΒE PLOT 10 ARRAY IS WHERE NUMBER BS (4) B (4) XTX (4,4), XTY (4) REAL\*8 \*\*\*\*\* 2 - D 

 XMAX=ULH { 3 XMIN=ULH { 2 YMAX=ULH { 4 YMAX=ULH { 4 YMAX=ULH { 4 YSCALE= { DLH { 4} -DLH { 2} } / (ULH { 4} -ULH { 1} ) YSCALE= { DLH { 4} -DLH { 2} } / (ULH { 4} -ULH { 2} )

 IN THE \*\*\* NUMPRT PLOIS THE NUMFER IK TEE PLOT(IX,J) POSITION. IX = COLUMN'OF MATRIX PLOT FEAL\*8 TO REAL\*4 1=1 IX2 1=5NGL(E(J)) KTY B, N) XS (8 4) [ (8 4 ] 6 AL \*4 16 \*\*\*\*\*\*\* MATSO MATMUI CHOLES CONTINU' CCNVEFT DO 15 CALL • • C + + + + \*\*\*\* 1 \*\* ÷ ₽ ∪ 10 15 00000000000  $\mathbf{u}\mathbf{u}\mathbf{u}$ C 0000

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NEM (10) (ELOT (122,50) 5, '6', '7', '8', '9'/ 10) 60 10 1 100) 60 10 2 1000 60 10 3 1000 60 10 4 K/10000 60 10 4 | # (I 10+1) 0000-I1000+1000-I100+100-I 10+10) | # (I 1+1) X WHERE MUMBER IS TO BE PRINTED. E PRINTED WHERE NUMBER IS TO BE PLOTED. -2 53 = NUM (110000+1) (1 K-11000 6410000) /1000 (1 K-110000 +10000+1) (1 K-110000 +10000-11000+1000) /100 J) = NUM (1100+1) (K-110000410000-11000+1000) /100 (1 1.3) = NUM (110+1) SUBROUTINE SECEST (GENDAT, IX, N, M, NEK, EST, Y, KP) FIGT [ 1 x - 2 ] = NUM [ 1 10000 + 1 ] 00 FIGT [ 1 x - 1 ] = NUM [ 1 10000 + 1 ] 00 + 1000 - 1 100 FIGT [ 1 x - 1 ] = NUM [ 1 1000 + 1 ] 00 + 1000 - 1 100 FIGT [ 1 x + 1 ] = NUM [ 1 100 + 1 ] 00 + 1000 - 1 100 FIGT [ 1 x + 2 ] = NUM [ 1 10 + 1 ] FIGT [ 1 x + 2 ] = NUM [ 1 100 + 1 ] 00 + 1000 - 1 100 FIGT [ 1 x + 2 ] = NUM [ 1 10 + 1 ] FIGT [ 1 x + 2 ] = NUM [ 1 100 + 1 ] 00 + 1000 - 1 100 FIGT [ 1 x + 2 ] = NUM [ 1 100 + 1 ] FIGT [ 1 x + 2 ] = NUM [ 1 100 + 1 ] FIGT [ 1 x + 1 ] = NUM [ 1 0 + 1 ] FIGT [ 1 x + 1 ] = NUM [ 1 100 + 1 ] FIGT [ 1 x + 1 ] = NUM [ 1 0 + 1 ] FIGT [ 1 x + 1 ] = NUM [ 1 0 + 1 ] FIGT [ 1 x + 1 ] = NUM [ 1 0 + 1 ] FIGT [ 1 x + 1 ] = NUM [ 1 0 + 1 ] FIGT [ 1 x + 1 ] = NUM [ 1 0 + 1 ] FIGT [ 1 x + 1 ] = NUM [ 1 0 + 1 ] FIGT [ 1 x + 1 ] = NUM [ 1 0 + 1 ] FIGT [ 1 x + 1 ] = NUM [ 1 0 + 1 ] FIGT [ 1 x + 1 ] = NUM [ I 1CO+100-I10+1) I 1CO+100-I10+10) ,J) = NUM(I1+1) = NUM(I10+1) (+10) :\*10) :\*10) :\*10)  $\begin{array}{l} FIOT (1 X + 1, J) = NU H (1 + 1) \\ GC TO = IX / 10 \\ FIOT (1 X - 1) \\ I = IX / 10 \\ FIOT (1 X - 1) \\ FIOT (1 X - 1) \\ FIOT (1 X J) = NU H (1 + 1) \\ GC TO \\ 22 \\ FIOT (1 X, J) = NU H (I + 1) \\ FIOT (1 X, J) = NU (I + 1) \\ FIOT (1 X, J) = NU (I + 1) \\ FIOT (1 X, J) = NU (I$ J = ROW OF FATRIX IK = NUMBEF TO BE FLOT = 2-D ARRAY W TEGER\* HHHHO XXXXO 22

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C BEAL Y (N)

FALL Y (N)

Y MAX = Y (N)

FOUR WORLES OF VECTOR Y OF LENGTH N

FOUR (N)

FOUR WORLES OF VECTOR Y OF LENGTH N

FOUR (N)

FOUR WORLES OF VECTOR Y OF LENGTH N

FOUR WORLES OF VECTOR Y
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ***************
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                                                                            SECTION LENGTH NEK
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         (LOWER)
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SCALES THE GRAPH, TO UPPER
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             PCTL(YENTILEOF NALUES
PEERCENTILEOF N VALUES
LATA IS ALREADY SORTED
                                                                            FOR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          SCET (Y, N)
BEAL X (2000), Y (1)
INTEGER IX
CCHPUTE ESTIMATES "EST" I
RE=0
DC 10 I=1 F NBK
KP=K F+1 NBK
KP=K F+1 NBK
KP=K F+1 (IX X, NEK)
COLTINUE
CCNTINUE
BETURN
FHC
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    FUNCTICN PCTL(Y, N, P, IC)
CC HPUTES P FERCENTIFE OF
WFEN IC=1 LATA IS ALREAD)
REAL Y(N)
REAL Y(N)
REPARCAT(N+1)
IF (IC .NE'1)
IF (IC .NE'1)
I = MINO (I N'1 (5) , 1)
J = MINO (I N'1 (5) , 1)
J = MINO (I N'1 (5) , 1)
B = B - INT (R)
FETURN
FETURN
END
                                                                            HESTU
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       SUBROUTINE
SUBROUTINE
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a R. Katalan and K. Caratan K. K. Caratan (K. K. Caratan) and the state of the state of the state of the state of the

NI HLIN SUBROUTINE CHOLES (XTX,XTY BHAT,N) BEAL+8 L (4,4),SUM,LT(4,4),ÍTX(4,4),XTY(4),BHAT(4),WY(4) REAL+4 B (4) INTEGER P FOINT ARTILE DISTANCE OR TO FIRST C FCINTS EXIST OUTSIDE. \*\*\*\*\*\* Finite Fin Y KP ... 25.0) Y KP ... 25.0) Z L 1.54 E 50.1 Z L 1.54 E 55 7 L 1.54 E 25 7 L 1.55 E 2 ES INTEROU A INTE IP NC KP)\_\_\_\_ 

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                                                                                                                                                                                                                                                                                                                    = XRES
                                                                                                                                                                                                                                                                                                                                                              ** *** * * * * *
                                                                                                                                                                                                                                                                                                                                    SUEROUTINE MATSO (X XEES, M, N)
REAL+8 I (8,4), XI (4,8), XRES (4,4), SUM
                                                          2
                                                                                                                                                                                                                                                                                                                    X * X
                                                                                                                                                              * IT * EHAT = WY ****
EHAT (N) = WY !N / LT (N, N)
DC 800 II = 2, N
I = N - II + 1
SUM = 0.0 CC
D0 750 0 EC
D0 750 0 EC
D0 750 0 EC
D0 750 0 EC
BHAT(I) = (WY (I) - SUM) / LT (I, J) )
CCNTINUE
                                                                                              II=I-1
SUM=0.0EC
DO 600 J=1,II
SUM=SUM+(WY (J) *L (I,J))
CONTINUE
WY (I) = (XTY (I) - SUM)/L (I,I)
CCNTINUE
                                                          PART
                                                                                                                                                                                                                                                                                                                                                             EUILD X-TEANSPOSE IN LT
                                                                                                                                                                                                                                                                                                                    MATRIX MULTIPLICATION
E I
                                                                                                                                                                                                                                                          DC 950 I=1 4
B (I)=SNGI (BHAT (I) )
CCNTINUE
                                                            XC,
                                                                                                                                                                                                                                                                                                                                                                             H H
                  () = I (J, I)
 ECSE
BUILC L-TRA
DC 540 I
CO 530
IT (I
530 CONTINUE
540 CC WTINUE
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END
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USING SHELL ALGORITHM ********
W,TEMP
                                                                                  XTX
                                                                                                 NUS,
                                                                                    N
                                       UM+(XT(I,K) *X(K,J))
NUE
                                                                                          X + X
                                                                                                                                      _ = XTY ****
DC 50 I=1 K
SUM=0.6 CC
DO 40 J=1 M
CONTINUE
CONTINUE
CCNTINUE
EETURN
CCNTINUE
EEU
END
                                                    = SUM
                                                                                 MATRIX FULTIPLICATION
                                                                                                                    DC 20 I=1 E
DO 10 5=1 N
XT (J I) = X (I , J)
CCNTINUE
CCNTINUE
                                                    (r'1)
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XRES
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INFLACE SORT US
REAL Y(N),
INTEGER GAF
ICGICAL EXCH
                                              CCNTINUE
CCNTINUE
EETURN
END
                      BUILD XT
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## LIST OF REFERENCES

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