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INFORMATION CONTENT AND SENSITIVITY OF MATRIX ELEMENTS TO
STRUCTURAL CHANGES IN COMPLEX SCATTERING SYSTEM

by

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questions about:

- a. the information content in the various matrix elements,
- b. their response to large and small changes in particle property,
- c. their specificity to a particular parameter change,
- d. the information density per scattering angle interval,
- e. ways to quantify changes,

still needed careful study. The research was an optical study of fundamental systems theoretically solvable and experimentally obtainable. The things learned from this study and described in this report will give insight to the matrix element data obtained from complex scattering systems.

Preface

The work described in this report was authorized under Contract No. DAAK 11-80-Q-0106. This work was started in September 1980 and completed in September 1982.

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CONTENTS

I. STATEMENT OF THE PROBLEM AND RESEARCH ACTIVITIES..... 4

II. THE RESULTS..... 6

 A. Response of S_{ij} to Change in Particle Size..... 6

 B. Arc Length as a Probe for Change..... 12

 C. Fourier Transforms as a Probe for Change..... 14

 D. Information Contained in Forward and Backscatterer.. 15

 E. Average, Mean or Effective Refractive Index..... 18

 F. Stokes Vectors, Mueller Matrices and Polarized
 Scattered Light..... 18

III. FINAL COMMENTS..... 18

APPENDICES

 A. Colloquia, Seminars and Conferences..... 19

 B. Papers..... 20



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INFORMATION CONTENT AND SENSITIVITY OF MATRIX ELEMENTS TO
STRUCTURAL CHANGES IN COMPLEX SCATTERING SYSTEMS

I. STATEMENT OF THE PROBLEM AND RESEARCH ACTIVITIES

This research was carried out to investigate the basic problems that are central to understanding light scattered from complex systems. Simple systems refer to those spherical, elliptical and cylindrical geometries that are directly amenable to theory. Computer programs can calculate every property of these systems and can evaluate the data extracted from experimental systems. Theoretical results are known to the accuracy of the fundamental optical and electrical constants, and experimental data can be achieved to arbitrary high degree of accuracy. Laboratory devices work under ideal conditions whereas diagnostic equipment for field work is limited by (short) measurement time, angular resolution, spatial resolution, angular view (θ -scan) and time for data analysis of complex curves to get the desired information.

One problem concerns how much scattering data is needed, how good it must be and how well it describes the scatterer (or scattering system) in a practical way. Another problem concerns how much information is contained in the various light scattering matrix elements and whether changes in the signals can be related to changes in particular optical or geometrical properties. The statement of these problems and the experimental attack on them are summarized in six research objectives listed below:

A. Measure the matrix elements S_{ij} for perfect scattering systems and preparations of exactly known mixtures of perfect

systems. Determine which matrix elements more accurately describe the system and signify a change.

B. Procure and prepare perfect scattering systems and exactly known mixtures of perfect systems.

C. Apply Fourier transforms, curve length, method of moments, area ratios, inflection points, polynomial fits, etc. to light scattering data to elucidate and quantify small changes in the data that arise from small changes in the system.

D. Investigate the role of "average, mean or effective" refractive index as it pertains to a complex scattering system and determine if it is a relevant optical constant for describing the system.

E. Investigate how much data is necessary to uniquely determine the optical properties of a scattering system. Data acquisition can be limited to finite angular resolution, limited-scan, noise and imperfect optical elements. Determine what compromises and shortcuts can be taken.

F. Prepare a tutorial report discussing the two common systems for treating the Stoke's vector $V = (I, Q, U, V)$ and $V = (I_e, I_r, I_q, I_v)$, the elements of the scattering matrix in each system and the relationship between these matrices and the experimental measurements actually made.

All research objectives have been met. Some results have been published, some are submitted for publication and some are in final stages of preparation (See Appendix B). The rest of this final report will discuss some of our most important results and show some of the data that will ultimately appear in

published papers.

II. THE RESULTS

We have procured and prepared perfect scattering systems and mixtures of perfect systems. These are perfect spheres (purchased from Duke Chemical Company), perfect fibers (fabricated in our laboratory), polydispersed irregular particle systems (purchased from Duke Chemical or fabricated by us), and perturbed fibers (fabricated by us). In all cases we have attempted to document the optical, electrical and geometrical properties of the particle or particle system to make the experimental data useful for theorists. This satisfies research objective B.

We have measured and calculated the matrix elements S_{ij} for perfect scattering systems and preparations of exactly known mixtures. The data were used to determine which matrix elements were needed to characterize the system and which ones were most sensitive to system changes. This satisfies research objective A. The net result is an experimental and theoretical data bank which can be manipulated and studied to examine how geometrical, optical and electrical constants contribute to the various S_{ij} light scattering curves.

The experimental and theoretical results of our studies of the above mentioned data bank and its manipulation are vast and are still being analyzed. Some results are discussed below.

A. Response of S_{ij} to Change in Particle Size.

Figures 1 through 5, which demonstrate how certain matrix elements change with particle size, is pertinent to research objective C.

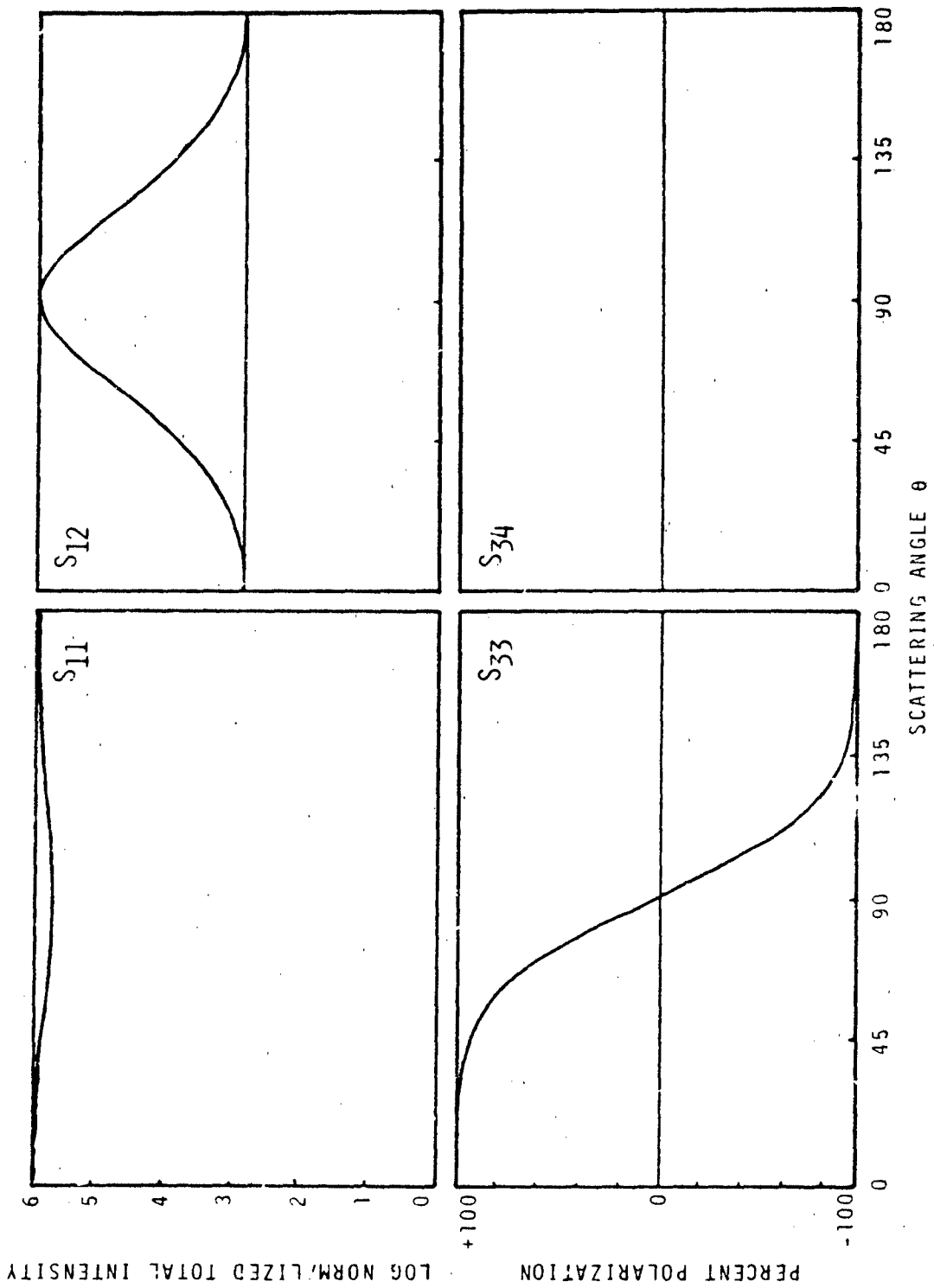


Figure 1. The Four Non-Zero Light Scattering Matrix Elements for 0.075 Micron Spheres Showing Their Response to a One Percent Increase in Radius (Solid Line) and Their Difference $\Delta S_{ij} = S_{ij}^1 - S_{ij}^0$ (Dotted Line) $\lambda = 4416\text{\AA}$ $n_1 = 1.10$ $n_2 = 0$.

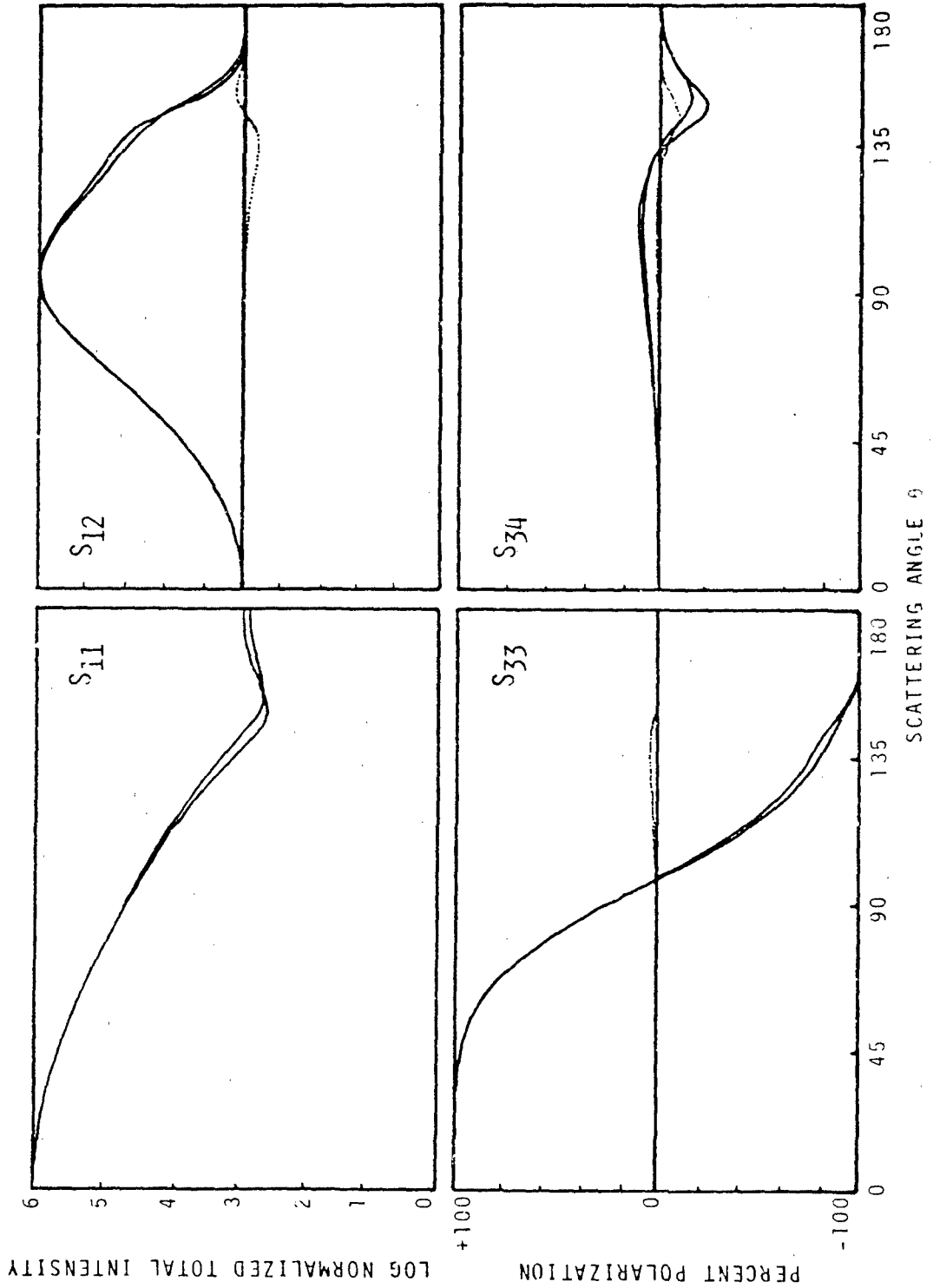


Figure 2. The Four Non-Zero Light Scattering Matrix Elements for 0.15 Micron Spheres Showing Their Response to a One Percent Increase in Radius (Solid Line) and Their Difference $\Delta = S_{ij}^L - S_{ij}$ (Dotted Line) $\cdot 4416\lambda \ n_1 = 1.0 \ n_2 = 0$.

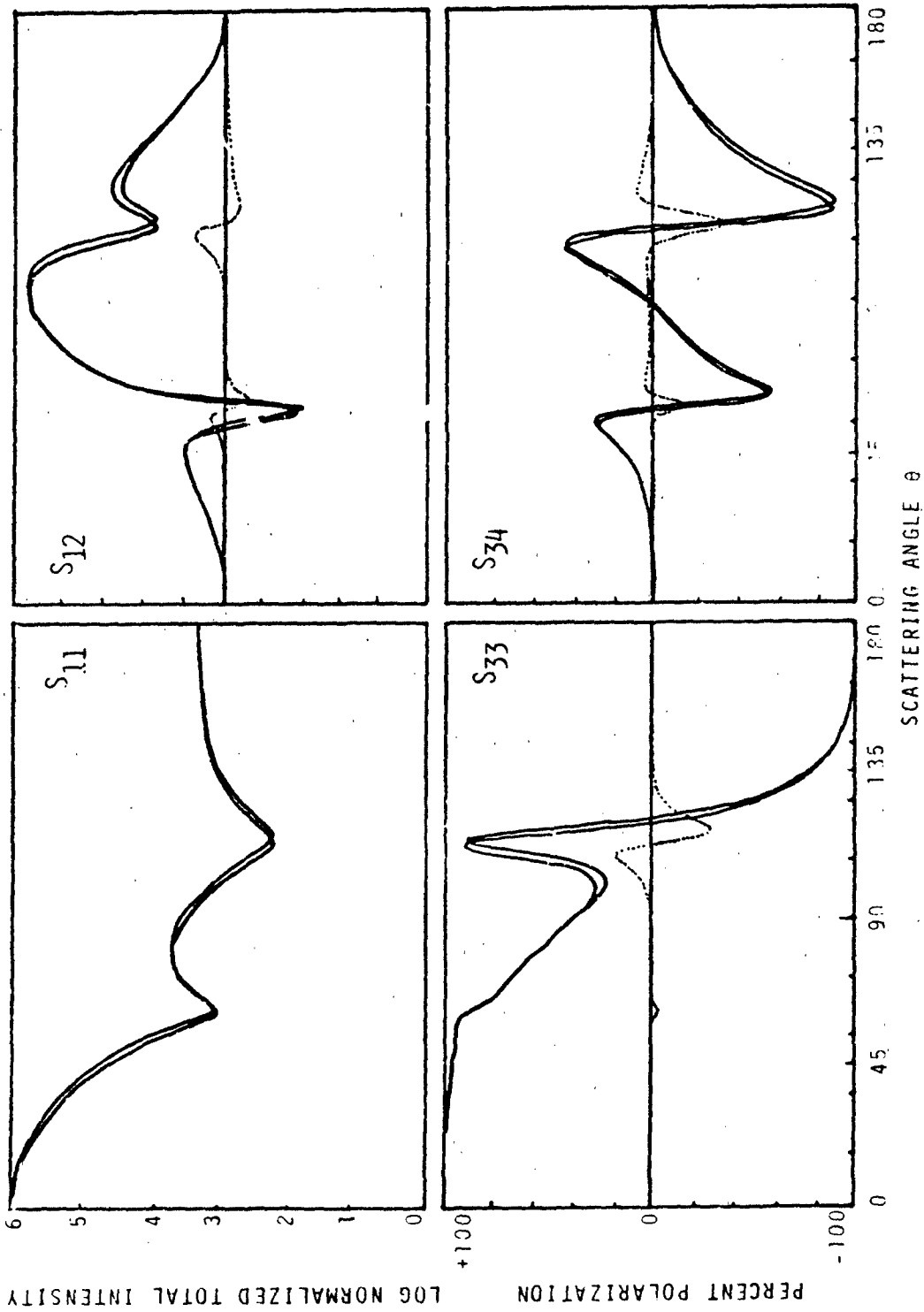


Figure 3. The Four Non-Zero Light Scattering Matrix Elements for 0.3 Micron Spheres Showing Their Response to a One Percent Increase in Radius (Solid Line) and Their Difference $\Delta = S_{ij}^L - S_{ij}^S$ (Dotted Line) $\lambda = 4416\text{\AA}$ $n_1 = 1.10$ $n_2 = 0$.

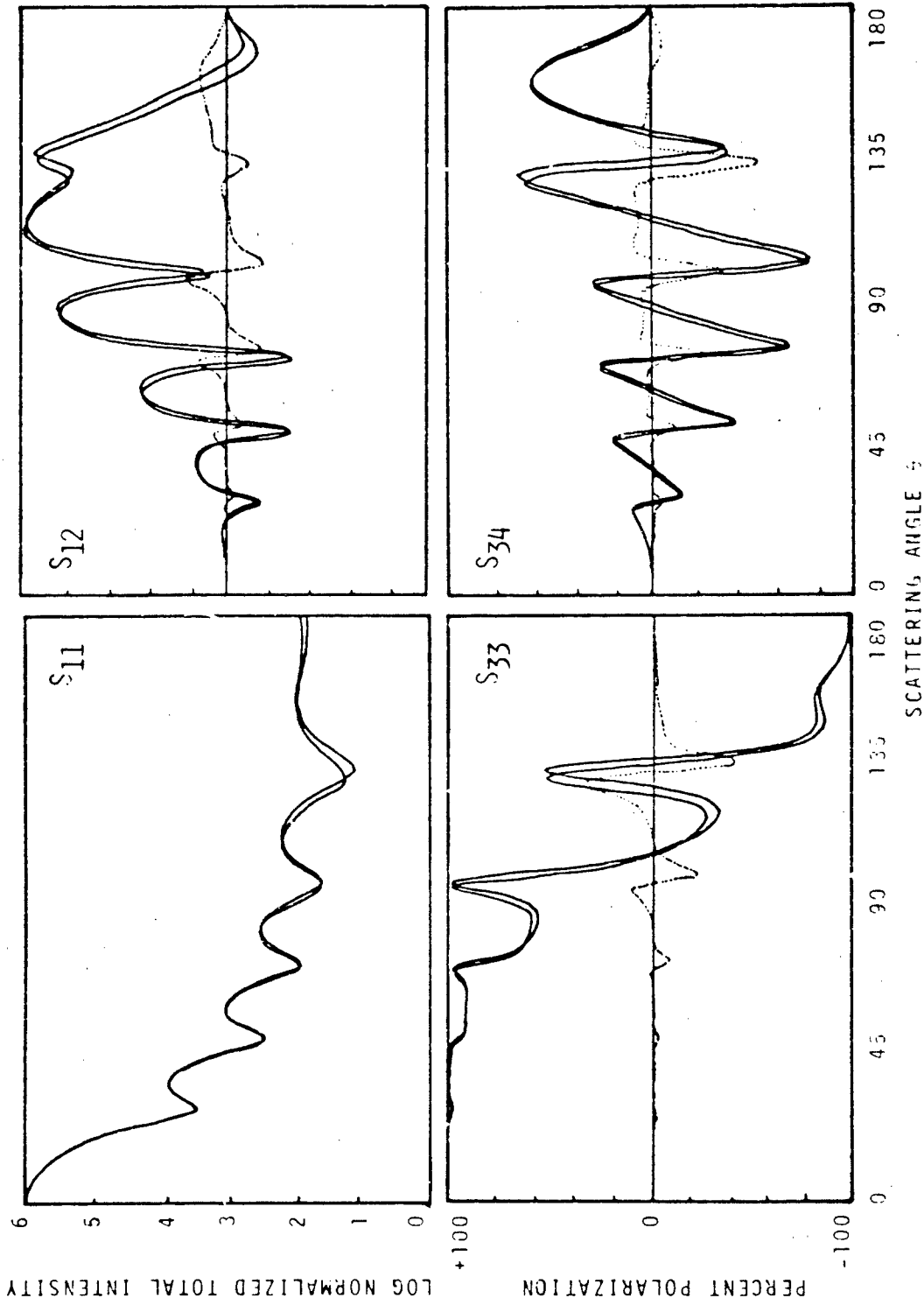


Figure 4. The Four Non-Zero Light Scattering Matrix Elements for 0.6 Micron Spheres Showing Their Responses to a One Percent Increase in Radius (Solid Line) and Their Difference $S_{ij}^R - S_{ij}^S$ (Dotted Line) 4416\AA $n_1 = 1.10$ $n_2 = 0$.

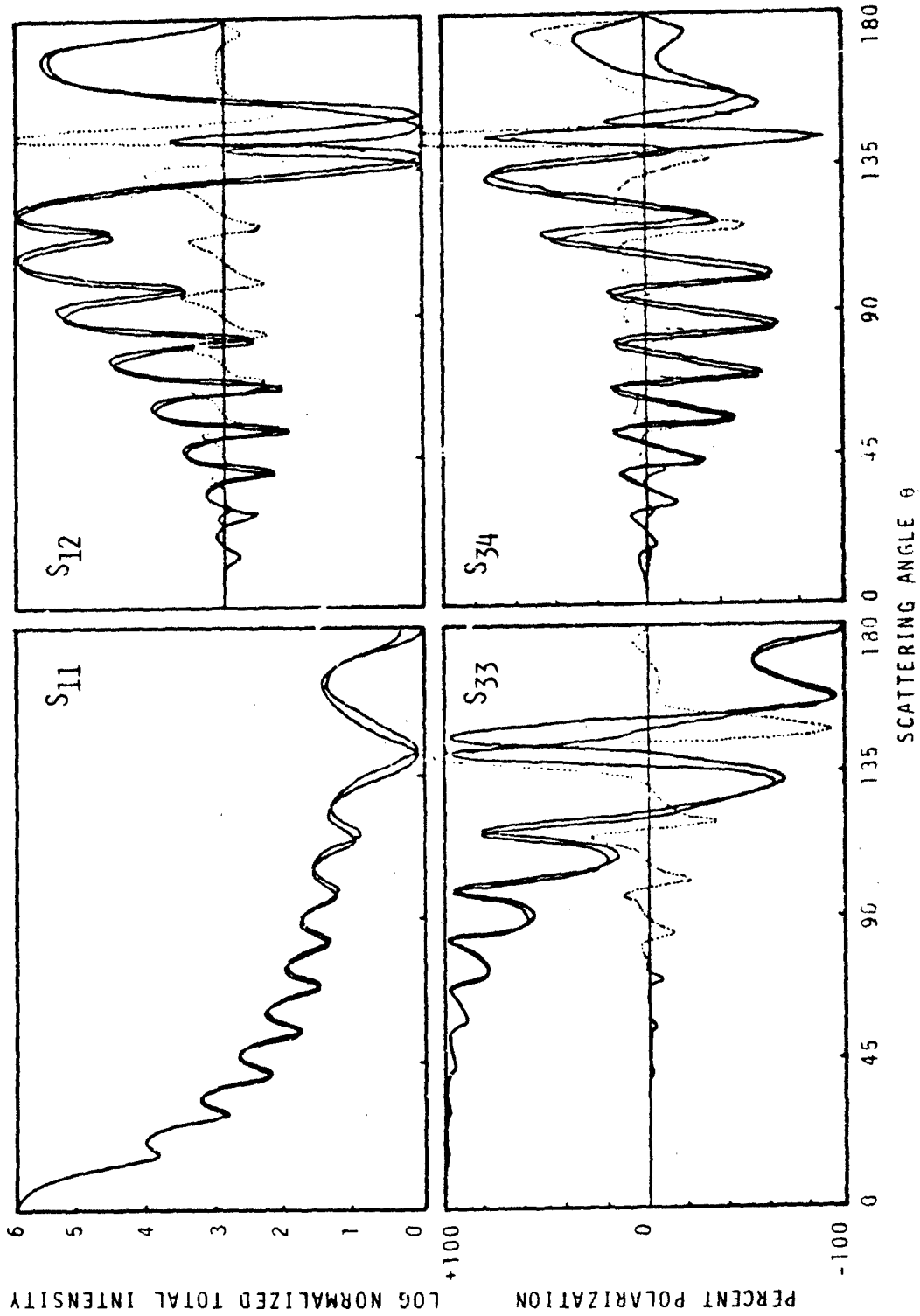


Figure 5. The Four Non-Zero Light Scattering Matrix Elements for 1.00 Micron Spheres Showing Their Response to a One Percent Increase in Radius (Solid Line) and Their Difference : = $S_{ij}^L - S_{ij}^S$ (Dotted Line) . 4416A $n_1 = 1.10$ $n_2 = 0$.

1. Response to large size change.

Figure 1 shows the four non-zero matrix elements for a very small Rayleigh sphere ($r = 0.075\mu$). It can be solved exactly using the approximation that $r \ll \lambda$ yielding the three functions $\sin^2\theta$, $\cos\theta$ and zero for the matrix elements S_{12} , S_{33} and S_{34} respectively. Scanning each particular matrix element from Figure 1 to Figure 5 shows how each matrix element changes with increasing sphere radius. Increasing the radius approximately a factor of 2 going from Figure 1 to 5 causes all matrix elements to develop high frequency phase information. Each matrix element will be discussed individually.

Matrix element S_{11}

This matrix element represents the total intensity of light scattered by the particle. Unpolarized light illuminates the scatterer, and the total scattered intensity is measured. The vertical scale is logarithmic, the curve has been normalized to maximum intensity at $\theta = 0$. As the particle increases size, S_{11} oscillates with increasing frequency. We also note that the ratio light scattered forward, ($\theta = 0$) to back ($\theta = 180^\circ$) increases. Larger particles scatter more light in the forward direction. For the particle studied here the ratio changes by 3 orders of magnitude. While this is generally true for low index particles, the ratio decreases as n_1 increases.

Matrix element S_{12}

This matrix element represents the extent to which the particle can distinguish between horizontally and vertically polarized light. If both were treated equally by the particle

S_{12} would be zero. As r increases, the initially smooth \sin^2 curve becomes distorted in the back scatter region, and finally develops oscillations about zero as large as +100%.

Matrix element S_{33}

This matrix element represents the extent to which the particle can distinguish between $+45^\circ$ and -45° polarization. If both were treated equally S_{33} would be zero. As r increases, the initially smooth \cos curve becomes distorted and like S_{12} develops oscillations that can vary rapidly between +100%.

Matrix element S_{34}

This matrix element represents the extent to which the particle can distinguish between left-hand and right-hand circular polarization when illuminated with $+45^\circ$ or -45° linear polarization. If all combinations were treated equally S_{34} would be zero. As r increases, the initially zero S_{34} signal becomes non-zero and like the other S_{ij} , develops oscillations of increasing frequency and amplitude.

We can make the following observations about how the matrix elements respond to a large change in spherical particle size:

- a. All matrix elements develop structure as the particle size increases. Quantifying the structure makes it possible to relate structure to particle size in some cases. For example in Figures 1-5 the number of maxima (or minima) in any matrix element curve is equal to the size of the particle in microns to within 10%. However, this is a special case and the results are fortuitously accurate for this combination of n_1 , n_2 and r .
- b. Large particles scatter more light into all angles than small particles. For the particles discussed here there is a 10^6

intensity difference between the small and large particle scattering efficiency.

c. The ratio (forward scatter:back scatter) increases as the particle size increases. This is generally true for low refractive index n_1 . However as n_1 increases the ratio decreases for constant r . Increasing absorption however increases the ratio by removing more light from the backscatter.

d. Regardless of particle size, refractive index or absorption the following bounds govern all S_{ij} for spheres.

S_{11} initially decreases as θ increases from zero,

S_{12} is always zero at $\theta = 0$ and $\theta = 180^\circ$,

S_{33} is always +100% at $\theta = 0$ and -100% at $\theta = 180^\circ$,

S_{34} is always zero at $\theta = 0^\circ$ and $\theta = 180^\circ$

and zero everywhere for "very small" particles.

These bounds are obeyed even by mixtures of perfect spheres polydispersed in n_1 , n_2 and r . Fibers obey only the bound on S_{11} and the bound that S_{34} is zero everywhere for "very small" fiber radii.

e. Some special comments about S_{34}

The matrix element S_{34} has distinguished itself as a particularly important signature and sensitive probe of scattering systems. Our initial experiments many years ago with biophysical particles would have ended without success if S_{34} did not uniquely survive to distinguish different polydispersed biological particle systems. It is unfortunate that S_{34} is not as experimentally accessible as the matrix elements S_{11} and S_{12} which are responsible for most of the information obtained from

remote scattering systems. S_{34} is first a true indicator of "large particles" becoming non-zero as particle size goes from small to large (Rayleigh to Mie). For the system discussed here, S_{34} already shows a non-zero signal for $r = 0.15\mu$, 10.4416μ ($n_1 = 1.10$). Experimentally S_{34} is a powerful probe since large amplification of an initially zero S_{34} signal can yield a "full scale" reading for an arbitrarily small change in the signal. Thus the smallest deviation from zero will appear directly. This technique does not work for S_{12} and S_{33} which already have values of ± 100 for small particles. For these elements, a small change must occur on an already large (full scale) signal. We have experimentally and theoretically investigated the ability of S_{12} and S_{33} to respond to a small increase in r by subtracting from them the "Rayleigh component", $S_{12} = \sin^2 \theta$ and $S_{33} = \cos^2 \theta$. The result, when amplified, can display approximately the same sensitivity as S_{34} . However, since noiseless signals do not occur experimentally, subtraction does not yield the same accuracy achieved from measuring S_{34} directly.

2. Response of S_{ij} to Small Size Change (Difference Curves).

Figures 1 through 5 which show the matrix elements for the five sphere sizes $r = 0.075, 0.15, 0.30, 0.60$ and 1.0 microns also show the matrix element signals that occur when the initial size is changed by a small value of 1%. Both matrix element curves are indicated by solid lines, and their difference $S_{ij}^L - S_{ij}^S$ is shown as a dotted line. We observe the following:

a. Figure 1. A 1% change in radius of a 0.075μ (Rayleigh) particle is not detected graphically at this level of sensi-

vity. The actual numbers used to plot the curves show differences less than 0.1%, within the noise of most experiments.

b. Figure 2. A 1% radius change in a 0.15μ particle changes all matrix elements. In addition, the difference occurs in the back scatter ($\theta > 90^\circ$). S_{34} shows the largest difference, but is in competition with S_{12} .

c. Figure 3. For larger particles ($r = 0.3\mu$) changes occur both in forward and back scatter but are larger in the back scatter. Again S_{34} is most sensitive.

d. Figure 4. A 1% change in even larger particles ($r = 0.6\mu$) cause changes throughout the entire θ -range. Differences are larger in the back scatter and S_{34} is most sensitive.

e. Figure 5. For our largest particles ($r = 1.0\mu$), amplitude shifts caused by 1% size changes cause extremely large difference signals. Note that all difference curves go off the scale, $(S_{ij}^L - S_{ij}^S) > S_{ij}(\max) = 100\%$ in the back scatter. S_{34} is most sensitive and the most sensitive region is $135^\circ \leq \theta \leq 160^\circ$.

f. General Conclusions.

Small changes (1%) in the radii of very small particles are not detected by any of the S_{ij} . Differences increase as particle size increases and appear in all S_{ij} . S_{34} is the most sensitive, giving the largest difference. All differences are larger in the back scatter. Phase shifts are not as dramatic as amplitude shifts. This is demonstrated by S_{34} in its response to a 1% change in a 1.0μ particle at $\theta = 145^\circ$ (Figure 5).

All experimental and theoretical results discussed here are for perfect single spheres and fibers. Their implications become

very important for complex scattering systems such as mixtures of polydispersed perfect spheres, irregular single particles or mixtures of irregular particles. The bounds on S_{ij} at $\theta = 0^\circ$, 90° and 180° discussed earlier will be violated on departure from sphericity.

B. Arc Length as a Probe For Change.

Scanning each particular matrix element from Figures 1 through 5 shows how each matrix element responds to an increasing sphere radius. The most obvious change in all signals is the increasing frequency and amplitude of the oscillations. This feature manifests itself as a change in arc length. We studied the arc length of each S_{ij} as a function of particle radius and obtained Figures 6 and 7.

The arc length is simply the geometrical length of the curve in arbitrary units. A straight horizontal line for all S_{ij} is assigned an arc length of 180 (for 180°). For S_{12} , S_{33} and S_{34} a straight horizontal line starting at $\theta = 0$, $\pi = 0\%$ going to $\theta = 0$, $\pi = 100\%$; to $\theta = 180^\circ$, $\pi = 100\%$; and then to $\theta = 180^\circ$, $\pi = 0\%$ has an arc length of $(100 + 180 + 100) = 380$ units. The same geometrical value occurs for the normalized S_{11} curves. Arc length becomes valuable when different curves or families of curves are compared.

Figure 6 shows two useful results:

1. Arc lengths of S_{12} , S_{33} and S_{34} increase more or less monotonically with increasing radius.
2. The arc lengths of S_{11} oscillate wildly and are not monotonic.

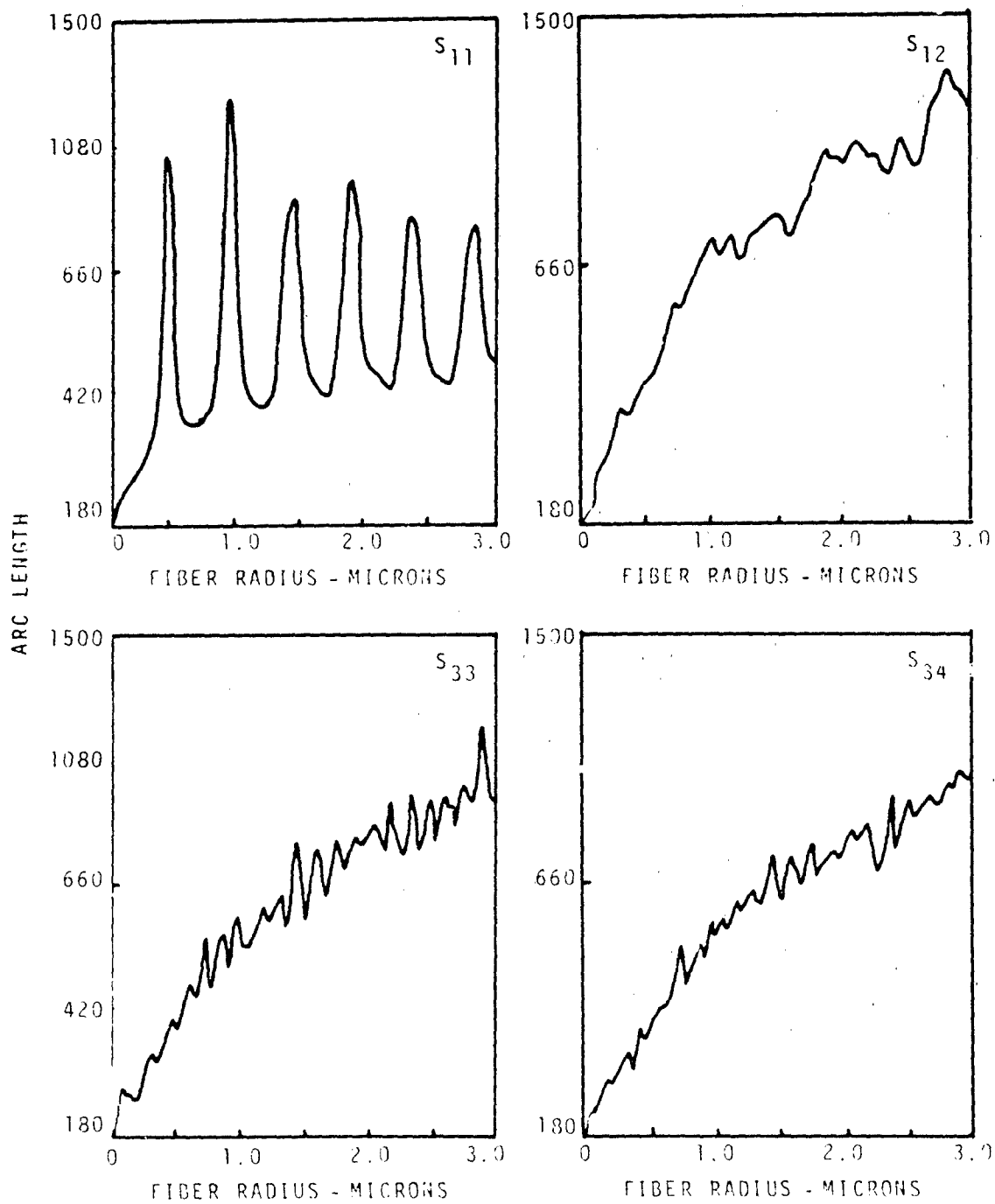


Figure 6. The Arc Length of Four Matrix Elements as a Function of Fiber Radius for $n_1 = 1.4662$, $n_2 = 0.0$ and $\lambda = 0.4416$ Microns.

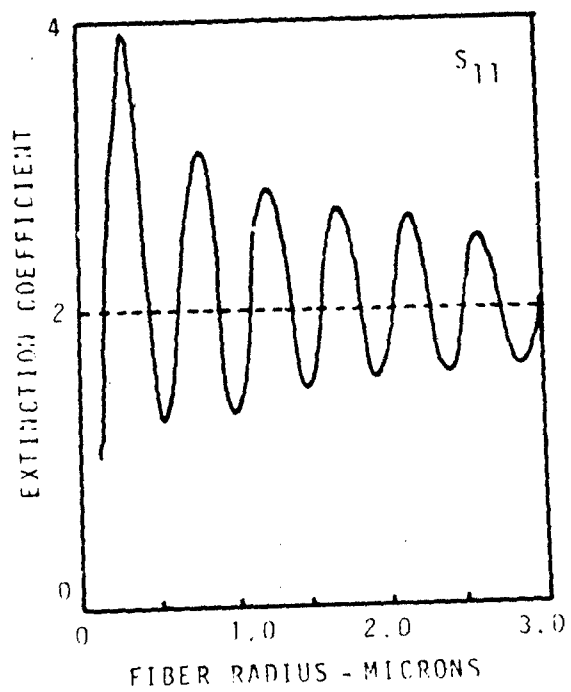
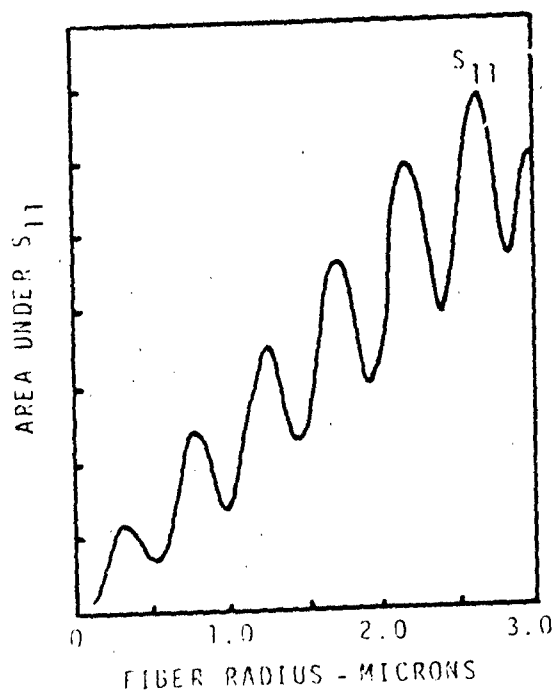
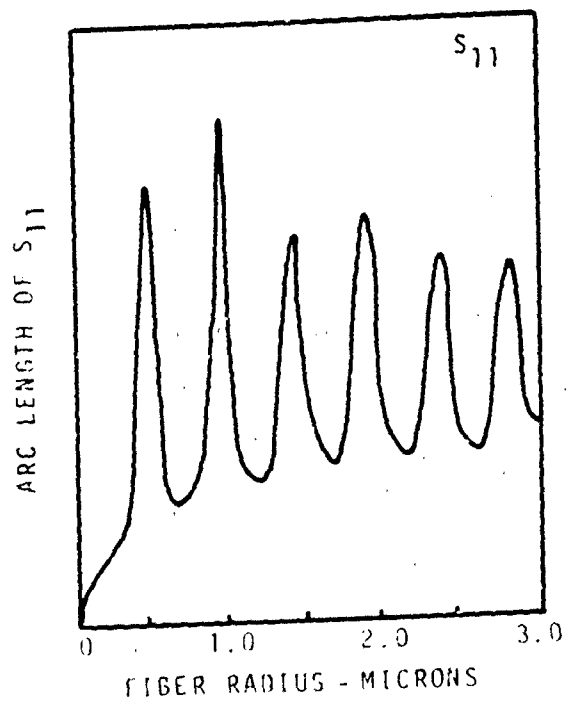


Figure 7. The Arc Length, Area Under the Curve and Extinction Coefficient Determined from S_{11} as a Function of Fiber Radius for $n_1 = 1.4662$, $n_2 = 0.0$ and $\lambda = 0.4416$ Microns.

The arc length of S_{11} is not an accurate probe for changing particle size. For a particular radii (close to $r = 1.0 \mu$) the arc length could decrease by more than a factor of 3 for a 30% increase or decrease in size. The other S_{ij} possess some structure but give more accurate results. The relationship between radius r and arc length AL of S_{33} and S_{34} is given by

$$r(\text{microns}) = \sqrt{\frac{AL-180}{113.2}}$$

Note that for larger particles ($r > 1.5 \mu$) the AL of S_{12} is larger than that of S_{33} and S_{34} . For smaller particles ($r < 1.0 \mu$) the relationship is

$$r(\text{microns}) = \frac{(AL-180)}{45}$$

Although it is well-known that certain features of S_{ij} curves change with particle property, previously, only limited attention has been given to quantifying the change as we are doing here. These observations are important for monitoring changes that occur in system parameters during time resolved or biological experiments, for example, where often the exact optical properties are not as important as knowing what changed and by how much.

Further study of S_{11} arc length led to some interesting results. We noticed that the arc length oscillations in S_{11} are similar to the well-known cross section oscillations that occur as a function of particle radius. More fundamental than the arc length however is the area under S_{11} which represents the total energy scattered by the particle. This line of reasoning led to

Figure 7 which shows how the arc length compares to the area under S_{11} which when multiplied by $\frac{4}{3}\pi r^3$ yields the well-known extinction coefficient as a function of r . Therefore arc length of S_{11} has a behavior similar to the fundamental particle property--the extinction cross section. The other S_{ij} arc lengths are not fundamental but useful nevertheless as probes for changes in particle parameters.

Results of similar arc length data as a function of n_1 and n_2 will be published.

C. Fourier Transforms as a Probe For Change.

The increasing oscillatory structure on S_{ij} curves resulting from increasing radius has been shown in Figures 1-5. The S_{ij} curves are expansions of integral order Bessel functions whose amplitudes are varied by harmonic functions. Our studies of the Fourier transforms of the S_{ij} give additional information about the scatterer and the relative sensitivity of various S_{ij} to particle parameter change. Figures 8, 9 and 10 show the FT three sets of particles respectively: $r = 0.25\mu$ and 0.30μ ; $r = 0.55\mu$ and 0.60μ ; and $r = 2.5\mu$ and 2.6μ . We observe the following:

1. Increasing particle size introduces more oscillatory structure (higher frequency components) on all S_{ij} .
2. S_{11} has a low frequency continuum lacking significant monochromatic features.
3. S_{33} is only slightly better than S_{11} possessing a low frequency continuum (initially it is $\cos^2 \theta$) and a few quantized frequency components for larger particles.
4. S_{12} and S_{34} are very competitive. They both display

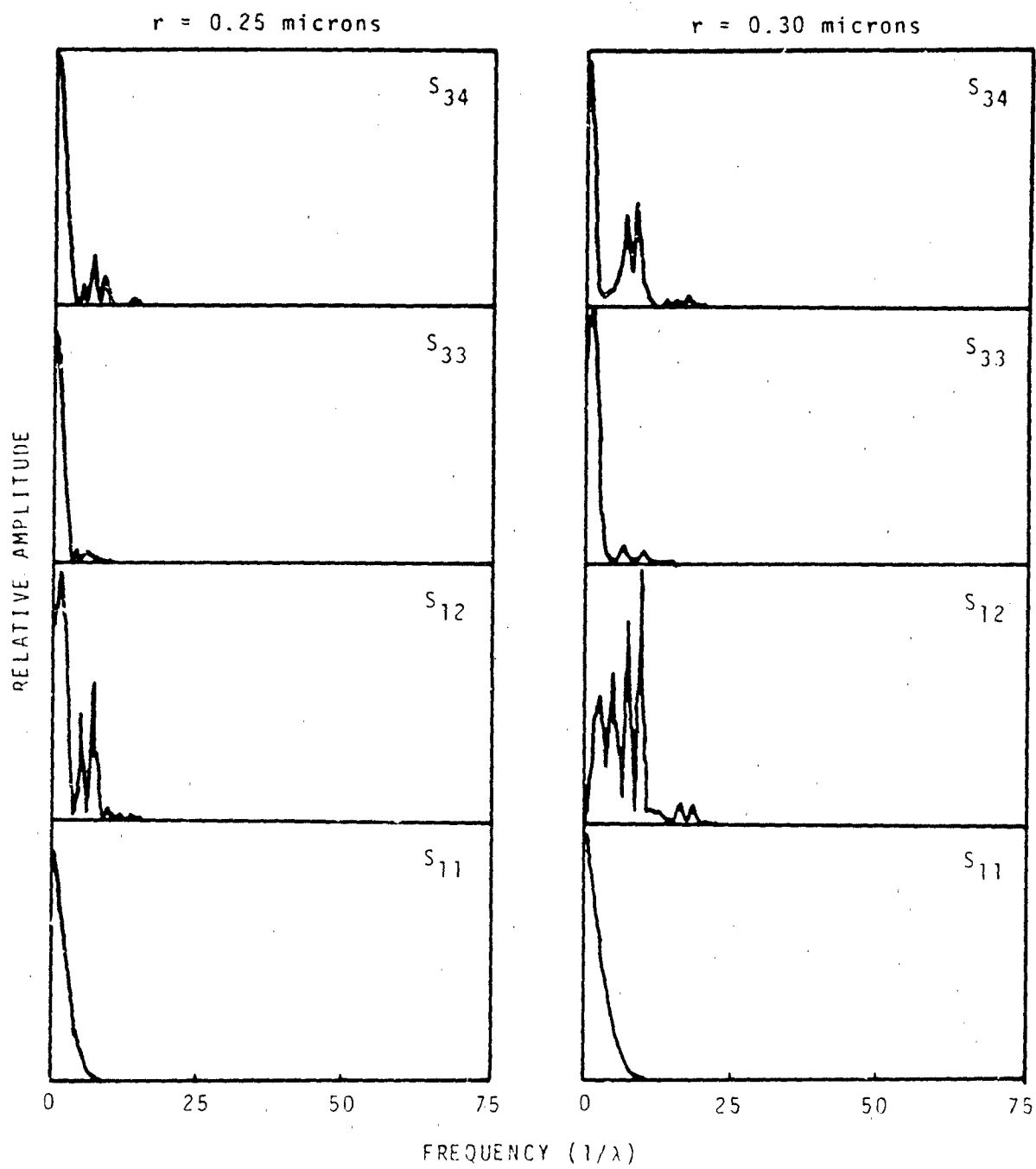


Figure 8. Amplitude-Frequency Distributions of Four Non-Zero Fiber Matrix Elements and Their Response to a Small Change in the Radius of a 0.25 Micron Fiber. $\lambda 4416\text{\AA}$ $n_1 = 1.466$ $n_2 = 0$.

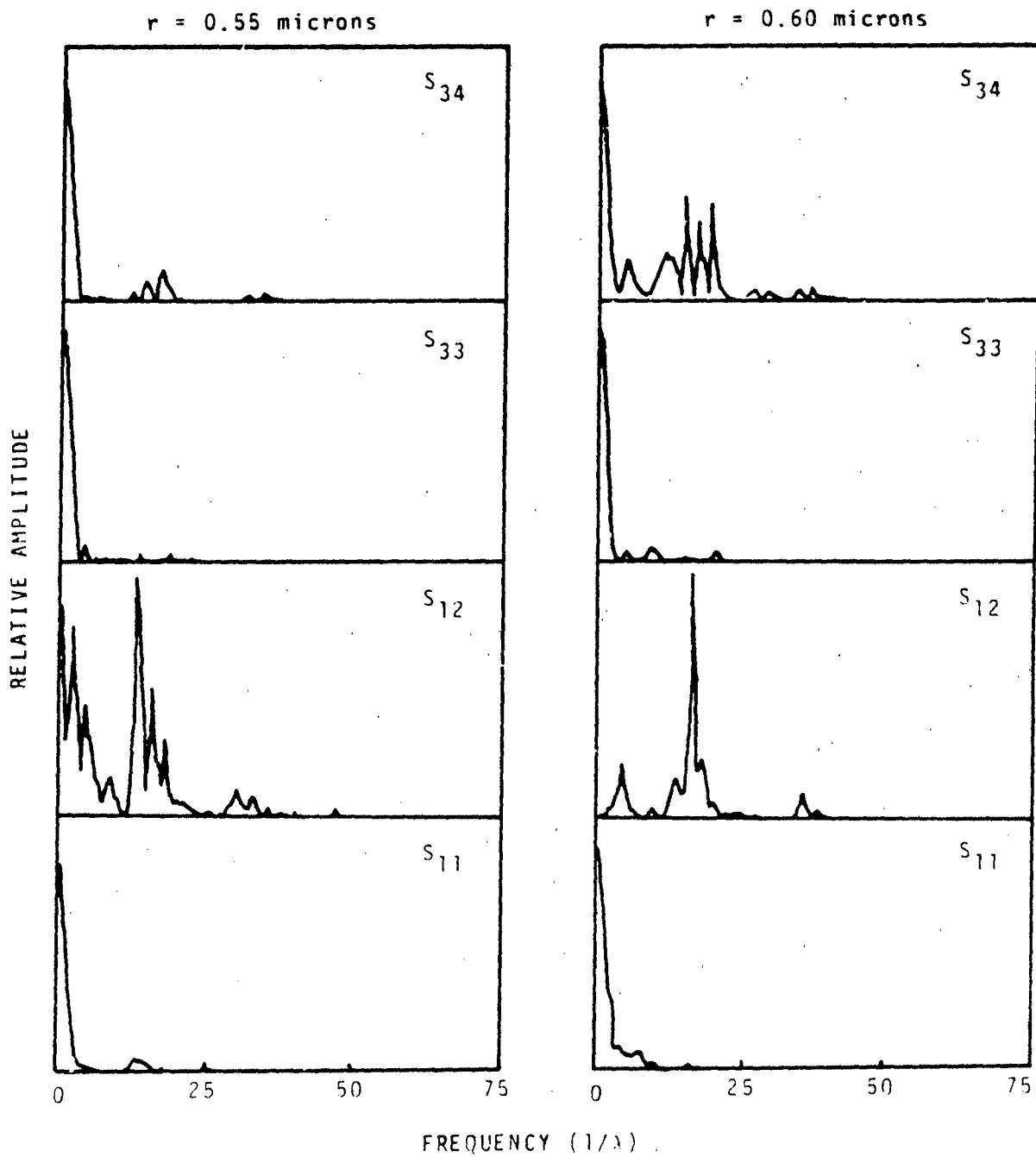


Figure 9. Amplitude-Frequency Distributions of Four Non-Zero Fiber Matrix Elements and Their Response to a Small Change in the Radius of a 0.55 Micron Fiber. 4416A $n_1 = 1.466$ $n_2 = 0$.

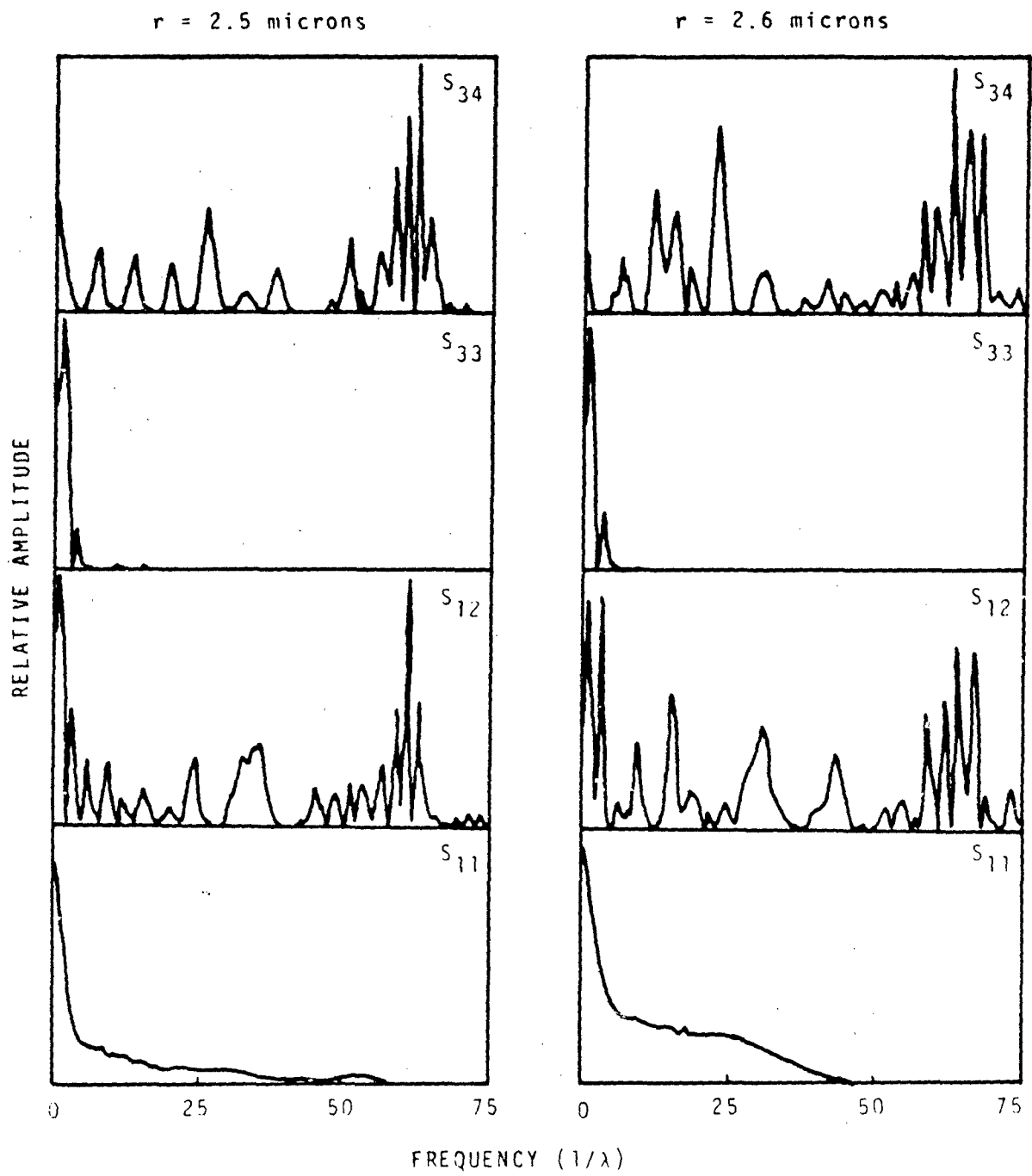


Figure 10. Amplitude-Frequency Distributions of Four Non-Zero Fiber Matrix Elements and Their Response to a Small Change in the Radius of a 2.5 Micron Fiber. $\lambda 4416\text{\AA}$ $n_1 = 1.466$ $n_2 = 0$.

extensive quantized frequency information for the same size particle and also compete as a detector of small size change. However S_{34} might be more reliable since the number of components increase as r increases whereas the number of components in S_{12} remain constant or change only slightly. When components and amplitudes are taken into account, S_{12} and S_{34} are comparable and serve well as signatures and indicators of change. S_{12} is more readily accessible to remote sensing experiments since it couples unpolarized (total intensity) incident on the scatterer with horizontally polarized scattered light.

It is interesting to observe the relative efficiency of representing the S_{ij} in terms of Bessel functions as compared to Fourier transforms - both of which make a complete mathematical set. To generate a particular set of S_{ij} requires about twice to three times as many Fourier coefficients as Bessel coefficients. This is due to the natural cylindrical geometry of the scattering system which lends itself directly to Bessel's equation and a Bessel function solution.

D. Information Contained in Forward and Back Scatter

We investigated the amount of information contained in the forward scattered and back scattered light into small $\Delta\theta$ near $\theta = 0$ and $\theta = 180^\circ$, respectively. This satisfies objective E. Many ground based remote sensing experiments have access only to back scatter information from light scattered back to the laser site. Figure 11 shows the intensities of forward ($\theta = 0^\circ$) and back scattered ($\theta = 180^\circ$) light as a function of sphere radius for spheres with various optical constants. Figure 11 can be studied in several ways.

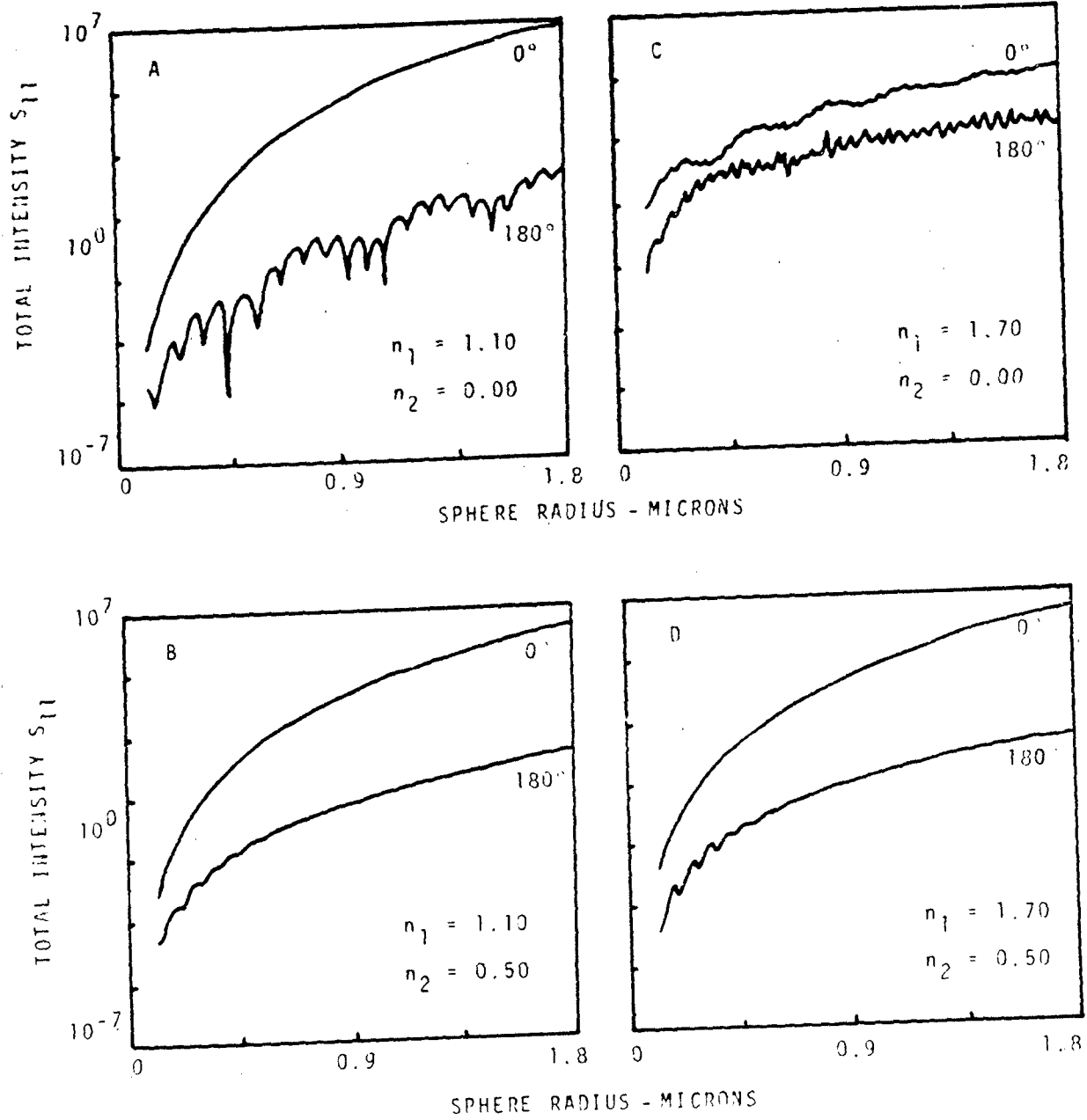


Figure 11. Forward Scatter ($\theta = 0$) and Back Scatter ($\theta = 180^\circ$) Efficiencies as a Function of Sphere Radius and Optical Constants.

Change n_1 from 1.1 to 1.7 with $n_2 = 0$ go from A to C.

Change n_1 from 1.1 to 1.7 with $n_2 = 0.5$ go from B to D.

Change n_2 from 0 to 0.5 with $n_1 = 1.1$ go from A to B.

Change n_2 from 0 to 0.5 with $n_1 = 1.7$ go from C to D.

a. Figure 11-A. The forward scatter ($\theta = 0$) from particles of small n_1 ($n_1 = 1.1$) and n_2 ($n_2 = 0.0$) increases smoothly and monotonically over 10 orders of magnitude for a one order of magnitude increase in radius. This says that one 1.5μ particle scatters, in the forward direction, as much light as 10^{10} 0.15μ particles. This is an effective way to hide particles or particle information.

The back scatter ($\theta = 180^\circ$) increases also, but only by 7 orders of magnitude. In addition it is not monotonic. For example, increasing or decreasing the size of a 0.45μ particle increases the scattered intensity by 3 orders of magnitude making the back scatter intensity information non-unique to particle size. Back scatter measurements are very sensitive to particle change, but not good indicators of particle size. They are good probes but not good signatures.

b. Figure 11-B. Absorption ($n_2 = 0.5$) destroys virtually all structure in the back scatter. Both forward and back scatter curves are essentially monotonic. However, the intensity ratio: forward to back scatter, remains about the same as that for particles with zero absorption ($n_2 = 0$) shown in Fig. A.

c. Figure 11-C. The intensity of both forward and back scattered light from large index particles ($n_1 = 1.7$) with no absorption ($n_2 = 0$) oscillates with increasing particle size.

3The forward scatter oscillations are larger, the back scatter oscillations are smaller for larger n_1 . In addition, the ratio of forward to back scatter remains essentially constant ($\sim 10^2$), independent of particle size.

d. Figure 11-D. Scattering from high index ($n_1 = 1.7$) and high absorption ($n_2 = 0.5$) spheres displays oscillations in the back scatter only for smaller particles ($r < 0.7\mu$).

e. General Conclusions

Low refractive index spheres scatter light in the forward direction with an intensity that increases smoothly and monotonically with increasing particle size - essentially independent of the amount of absorption. Absorption destroys oscillation in both the forward and back scatter - essentially independent of the value of n_1 .

Back scatter information is a sensitive probe for change but not a unique indicator of size. Back scatter information that does not oscillate with wavelength must come from particles with large absorption (assuming that n_2 stays large over the θ -range). Conversely substantial θ -dependent oscillation in the back scatter must be caused by low absorption and low index particles. In general, there is more information in back scatter than in forward scatter - which is fortunate for many ground based remote sensing experiments.

All observations discussed above are valid for single spheres or monodispersed sphere systems. Polydispersity and/or systems of irregular particles will destroy phase-amplitude information. Exactly what information remains is the subject of our present research.

E. Average, mean or effective refractive index

This study satisfies research objective D and has been published in Aerosol Science and Technology 1:329-335(1982).

F. Stokes Vectors, Mueller Matrices and polarized light scattering

This study satisfies research objective F. A paper has been submitted to the American Journal of Physics.

III. FINAL COMMENTS

This final report describes the main thrust of our research and a number of experimental results from which conclusions were drawn to make our point concerning the information contained in the matrix elements. At best, significant trends can be established. To investigate all combinations of r , n_1 and n_2 would yield an infinitely large data bank too unwieldy to analyze. We attempted to limit our particles into regions: size-large, medium, small; refractive index and absorption-high, medium, low and chose carefully combinations that will establish a trend or generate an exception. This approach has been productive and has given good insight to the information contained in light scattering data.

APPENDIX A

COLLOQUIA, SEMINARS AND CONFERENCES

- Conferences:
1. CSL on light scattering, Aberdeen, Maryland, June 15-17, 1981.
 2. Conference on Aerosol Science, Santa Monica, California, February 20-23, 1982.
- Colloquia:
1. Optical Sciences Department, University of Arizona, Spring 1982.
 2. SERI, Golden, Colorado, Summer 1981.
 3. Physics Department, University of Lund, Lund, Sweden, Summer 1982.
 4. Physics Department, University of Arizona, Fall 1982.
- Seminars:
1. SERI, Golden, Colorado, Summer 1981.
 2. Physics Department, University of Lund, Lund, Sweden, Summer 1982.

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APPENDIX B

PAPERS

1. "Masking of Information in Light Scattering Signals from Complex Scatterers", William S. Bickel, Hashim A. Yousif and Wilbur M. Bailey, *Aerosol Science and Technology* 1:329-335 (1982).
2. "Light Scattering from Fibers - an Extension of a Single Slit Diffraction Experiment", Wolfgang Gilliar and William S. Bickel, submitted to *Am. J. of Physics*.
3. "The Physical and Optical Properties of Agglomerated Gold Films Optical Scattering from Surfaces", Richard Zito, William S. Bickel and Wilbur M. Bailey, submitted to *Applied Optics*.
4. "Stokes Vectors, Mueller Matrices and Polarized Scattered Light", William S. Bickel and Wilbur M. Bailey, submitted to *Am. J. Physics*.
5. "Light Diffraction Studies of Single Muscle Fiber as a Function of Fiber Rotation", Wolfgang Gilliar and William S. Bickel, accepted by *Biophysical Journal*.
6. "Light Scattering from Geometrically Perturbed Thin Fiber," William S. Bickel and Gordon Videen, to be submitted to *App. Optics*.
7. "Information Content in LS Signals from Mixtures, Polydispersed and Multiple Scattering System", William S. Bickel, Wilbur M. Bailey and Hashim A. Yousif, to be submitted to *Applied Optics*.

8. "Sensitivity of LS Matrix Elements to Small Changes in Structural and Optical Constants of Perfect Scatterers", William S. Bickel, W. M. Bailey and H. A. Yousif, to be submitted to Aerosol Science and Technology.

9. "Scattering Corrections to ORD and CD Measurements", William S. Bickel, to be submitted to App. Optics.

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