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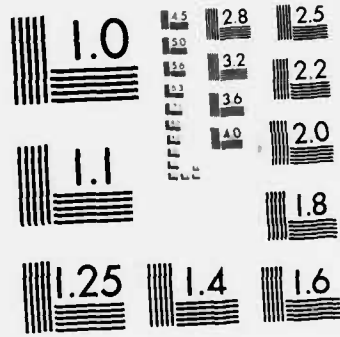
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CALCULATION OF WAVE PACKET TRAJECTORIES AND WAVE HEIGHTS FOR VARIABLE WATER DEPTHS AND CURRENTS

BY J. ERNEST BREEDING, JR.
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FINAL
TECHNICAL REPORT NO. JEB-11
DEPARTMENT OF OCEANOGRAPHY AND OCEAN ENGINEERING
FLORIDA INSTITUTE OF TECHNOLOGY

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September, 1982

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ABSTRACT

The theory and numerical methods are presented for determining the paths and wave heights of gravity water wave packets. Both variable water depths and currents are considered. The wave height is computed accounting for the effects of shoaling, refraction, and energy dissipation. A ray curvature expression is used to determine the wave packet trajectories where the speed of the packet is given by $G = (d\omega/dk) \cos \phi$. The symbol ω denotes the angular frequency, k is the wave number, and ϕ is the difference between the direction of the wave packet and the direction of the wavelets within the packet. The wavelet direction is determined at each point of the wave packet trajectory. The wave packet and ray directions differ when there are currents. The calculations for variations in water depth are greatly simplified by choosing a coordinate system at each ray point in which one axis is aligned parallel with the direction of the gradient of the water depth. In a similar fashion, the calculations involving variations in current are simplified by choosing a coordinate system at each ray point in which an axis is taken parallel with the direction of the gradient of the current magnitude. Example printouts and plots are presented to illustrate the wave prediction method.

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CHAPTER I

It has been shown by Breeding (1978, 1981) that a wave packet refracts according to Snell's law with the geometric group velocity G where

$$G = (\partial\omega / \partial k) \cos \phi \quad (1-1)$$

The symbol ω denotes the angular frequency and k is the wave number. The angle ϕ is the difference between the direction of the wave packet and the direction of the wavelets within the packet. The wavelet direction at each point of the wave packet trajectory is determined by Snell's law with phase velocity.

In this work a numerical method is presented for determining the rays of gravity water wave packets. Further, a procedure is developed for computing the wave heights along the paths accounting for the effects of shoaling, refraction, and energy dissipation. Both a variable water depth and current are considered.

There are a number of papers in which numerical methods are presented for calculating and plotting the trajectories of monochromatic rays. Skovgaard, et al (1975) summarize a number of these methods and present one of their own. The numerical methods for calculating and plotting rays which are presented in this work are based on the Wilson (1966) program. However, extensive modifications of the Wilson program were required in order to compute the path of a wave packet. Wilson did not consider wave heights.

In Chapter II equations defining the trajectories of wave packets in a current are presented. An expression is derived for the ray curvature of a wave packet. The Doppler shift in the frequency of the waves due to a current is considered. Properties of the packet ray curvature are discussed for the particular case of parallel water depth contours and no currents. The methods used in computing the wavelet direction are described. The numerical procedure for locating each ray point is discussed. Rules for dealing with reflection points due to water depth variations, which occur when the ray curvature becomes infinite, are established. The condition for the total reflection of waves due to a current is presented.

The shoaling, refraction, and friction coefficients used to compute the wave heights are described. The ray separation equation is discussed. An analytical solution to the equation is presented for the case of parallel wave speed contours. In the program a numerical method is used to solve the ray separation equation. This method is discussed, and the procedure for dealing with reflection points is described. The method for locating caustics and focal points is explained. Near a caustic an approximate solution of the ray separation equation is used in the calculations. This solution is presented. There is a discussion of the wave breaking criterion.

The variations due to water depth and currents are considered separately. The partial derivatives of the wave speeds are related to the corresponding water depth derivatives. The calculations are greatly simplified by making them in a $x'y'$ -coordinate system which is chosen so that at each ray point

the positive x' -axis is in the direction of the gradient of the water depth. As a result, the first partial derivatives of the water depth and wave speeds with respect to y' -vanish. Further, there is a simplification in the second partial derivatives involving y' . In a similar manner, a $x''y''$ -coordinate system is used to determine the partial derivatives of the wave speeds and to relate them to the variations in a current. The positive x'' -axis is taken in the direction of the gradient of the current speed. This results in a simplification of all the derivatives involving y'' . The chapter concludes with a summary of the basic equations.

Chapter III contains details of the computer program and a program listing. The program listing contains many comments to explain the operation of the program.

Chapter IV contains details on how to prepare the water depth and current grids. The way to prepare a computer run is explained, and the printed output is described. Both the printout and plots are illustrated. Included are the results for sample data which are provided so that a user can test the program.

The principal notation used in the report is presented following the references.

CHAPTER II THEORY

2.1 Trajectories of Gravity Water Wave Packets. In this section a method is presented for determining the surface trajectories of gravity water wave packets considering both a variable water depth and a variable current.

a. Ray paths

Arthur (1950) considered the trajectories of monochromatic waves in a current. His method is easily extended to determine the trajectories of wave packets in a current. The ray paths are defined by

$$\frac{dx}{dt} = u_x + G \cos \theta \quad (2-1)$$

$$\frac{dy}{dt} = u_y + G \sin \theta \quad (2-2)$$

where x, y are the Cartesian coordinates, t is time, and θ is the direction of the wave packet with respect to the positive x -axis. The x - and y -components of the horizontal component of the current velocity are denoted by u_x and u_y where u is the current speed. The geometric group speed of the wave^xpacket^y relative to the current is G . The ray direction ρ is defined by

$$\tan \rho = \frac{u_y + G \sin \theta}{u_x + G \cos \theta} \quad (2-3)$$

b. Ray curvature for wave packets

The ray curvature κ_v of a ray moving with phase speed v over a variable bottom topography was derived by Munk and Arthur (1952) and Arthur, et al (1952) as

$$\kappa_v = \frac{d\gamma}{ds_v} = \frac{1}{v} \left(\sin \gamma \frac{\partial v}{\partial x} - \cos \gamma \frac{\partial v}{\partial y} \right) \quad (2-4)$$

where γ is the direction of the monochromatic wave with respect to the positive x-axis and s_γ is the arc length along the ray.

The ray curvature κ_G for the trajectory of a wave packet for a variable bottom topography is given by

$$\kappa_G = \frac{d\theta}{ds_G} = \frac{1}{G} \left(\sin \theta \frac{\partial G}{\partial x} - \cos \theta \frac{\partial G}{\partial y} \right) \quad (2-5)$$

where ds_G is an element of arc length along the ray.

The ray curvature expressions are readily extended to include variable currents. For monochromatic rays (Arthur, 1950)

$$\kappa_v = \frac{1}{v + u_k} \left[\sin \gamma \left(\frac{\partial v}{\partial x} + \frac{\partial u_k}{\partial x} \right) - \cos \gamma \left(\frac{\partial v}{\partial y} + \frac{\partial u_k}{\partial y} \right) \right] \quad (2-6)$$

$$u_k = \hat{e}_k \cdot \vec{u} \quad (2-7)$$

where \hat{e}_k is a unit vector in the direction of γ , u_k is the component of the current in the direction of γ , and v is the phase speed relative to the current. For wave packets

$$\kappa_G = \frac{1}{G + u_m} \left[\sin \theta \left(\frac{\partial G}{\partial x} + \frac{\partial u_m}{\partial x} \right) - \cos \theta \left(\frac{\partial G}{\partial y} + \frac{\partial u_m}{\partial y} \right) \right] \quad (2-8)$$

$$u_m = \hat{e}_m \cdot \vec{u} \quad (2-9)$$

where \hat{e}_m is a unit vector in the direction of θ and u_m is the component of the current in the direction of θ .

The geometric group speed is defined (Breeding, 1978)

$$G = U \cos \phi \quad (2-10)$$

where

$$U = \frac{d\omega}{dk} \quad (2-11)$$

$$\phi = \theta - \gamma \quad (2-12)$$

and U is the conventional (collinear) group speed. The angular frequency $\omega = 2\pi f$, $f = 1/T$ is the frequency, and T is the wave period. These quantities are all defined relative to the current where

$$\omega = \omega_g - \vec{k} \cdot \vec{u} \quad (2-13)$$

and ω_g is the angular frequency in a fixed coordinate system relative to the water bottom. The wave number $k = 2\pi/\lambda$ and λ is the wavelength.

The first partial derivatives of G are determined using Equation (2-10).

$$\frac{\partial G}{\partial X} = \frac{\partial U}{\partial X} \cos \phi - U \sin \phi \frac{\partial \phi}{\partial X} \quad (2-14)$$

$$\frac{\partial G}{\partial Y} = \frac{\partial U}{\partial Y} \cos \phi - U \sin \phi \frac{\partial \phi}{\partial Y} \quad (2-15)$$

Through the use of Equation (2-8) the spatial derivatives of θ are taken to be

$$\frac{\partial \theta}{\partial X} = \frac{\tan \theta}{G + u_m} \left(\frac{\partial G}{\partial X} + \frac{\partial u_m}{\partial X} \right) \quad (2-16)$$

$$\frac{\partial \theta}{\partial Y} = \frac{-\cot \theta}{G + u_m} \left(\frac{\partial G}{\partial Y} + \frac{\partial u_m}{\partial Y} \right) \quad (2-17)$$

In like manner, from Equation (2-6) it is found that

$$\frac{\partial Y}{\partial X} = \frac{\tan Y}{v + u_x} \left(\frac{\partial v}{\partial X} + \frac{\partial u_x}{\partial X} \right) \quad (2-18)$$

$$\frac{\partial Y}{\partial y} = \frac{-\cot Y}{v + u_x} \left(\frac{\partial v}{\partial y} + \frac{\partial u_x}{\partial y} \right) \quad (2-19)$$

When Equations (2-16) and (2-18) are substituted into Equation (2-14) and the terms are rearranged, it is found that

$$\frac{\partial G}{\partial X} = \left(1 + \frac{U \sin \phi \tan \theta}{G + u_m} \right)^{-1} \left\{ \frac{\partial U}{\partial X} \cos \phi + U \sin \phi \left[\frac{\tan Y}{v + u_x} \left(\frac{\partial v}{\partial X} + \frac{\partial u_x}{\partial X} \right) - \frac{\tan \theta}{G + u_m} \frac{\partial u_m}{\partial X} \right] \right\} \quad (2-20)$$

The substitution of Equations (2-17) and (2-19) into Equation (2-15) leads to

$$\frac{\partial G}{\partial y} = \left(1 - \frac{U \sin \phi \cot \theta}{G + u_m} \right)^{-1} \left\{ \frac{\partial U}{\partial y} \cos \phi + U \sin \phi \left[\frac{\cot \theta}{G + u_m} \frac{\partial u_m}{\partial y} - \frac{\cot Y}{v + u_x} \left(\frac{\partial v}{\partial y} + \frac{\partial u_x}{\partial y} \right) \right] \right\} \quad (2-21)$$

In the event there are no currents Equations (2-20) and (2-21) reduce to

$$\frac{\partial G}{\partial X} = \frac{\frac{\partial U}{\partial X} \cos \phi + \frac{U}{v} \sin \phi \tan Y \frac{\partial v}{\partial X}}{1 + \tan \phi \tan \theta}, \quad u = 0 \quad (2-22)$$

$$\frac{\partial G}{\partial y} = \frac{\frac{\partial U}{\partial y} \cos \phi - \frac{U}{v} \sin \phi \cot Y \frac{\partial v}{\partial y}}{1 - \tan \phi \cot \theta}, \quad u = 0 \quad (2-23)$$

In the computations it is convenient to separate out the variations due to water depth and the variations in frequency due to a variable current. As a result, if only one of the types of variation is being considered the equations associated with the other type of variation can be ignored. The

ray curvature for the wave packet is expressed as

$$K_G = \frac{1}{G + u_m} \left[\left\{ \sin \theta \frac{\partial G}{\partial X} - \cos \theta \frac{\partial G}{\partial Y} \right\}_h + \left\{ \sin \theta \left(\frac{\partial G}{\partial X} + \frac{\partial u_m}{\partial X} \right) - \cos \theta \left(\frac{\partial G}{\partial Y} + \frac{\partial u_m}{\partial Y} \right) \right\}_w \right] \quad (2-24)$$

where the subscript h denotes terms in which a variation in water depth is considered, and the subscript w refers to terms in which changes in current are accounted for.

Since the wave packet and the ray travel with different velocities, the incremental distances by which they advance for a given time interval are different. The wave packet incremental distance must extend to the same wave speed contour reached by the ray. This is illustrated in Figure (2-1) where the wave speed contours are assumed to be locally parallel. From the figure, it is seen that

$$ds_G = \frac{\cos \rho}{\cos \theta} ds_{ray} \quad (2-25)$$

c. Properties of the wave packet ray curvature

The ray curvature of a wave packet has been examined (Breeding, 1981) for the case of parallel water depth contours and no currents. If the water depth contours are parallel to the y-axis the packet ray curvature becomes

$$K_G = \frac{\frac{1}{U} \frac{\partial U}{\partial X} + \frac{\tan \phi \tan \gamma}{v} \frac{\partial v}{\partial X}}{\cos \theta + \tan \phi \sec \theta} \quad (2-26)$$

From this expression it is found that refraction causes a wave packet trajectory to become directed either parallel or perpendicular to the water depth contours. In either case the packet ray curvature will vanish. For wave packets propagating toward deep water, if the initial direction exceeds a critical angle total reflection occurs. At the reflection point the wavelet direction becomes parallel to the wave speed contours, the wave packet direction becomes perpendicular to the contours, the geometric group velocity goes to zero, and the packet ray curvature becomes infinite.

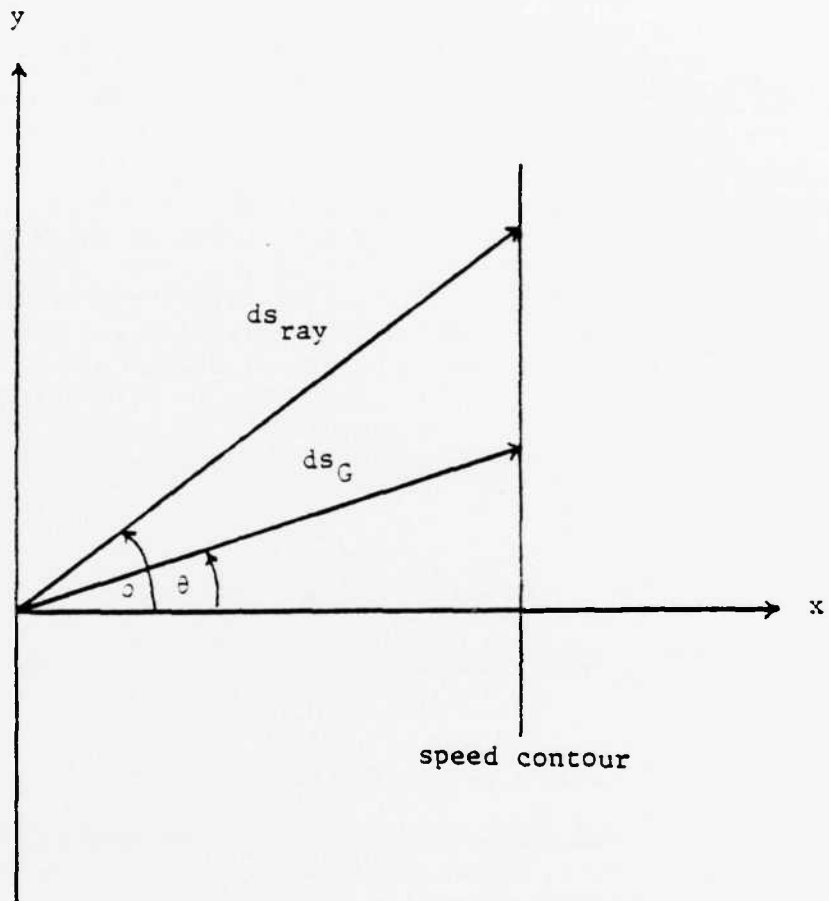


Figure (2-1). RELATIONSHIP BETWEEN THE RAY AND WAVE PACKET INCREMENTAL DISTANCES

d. Wavelet direction

Both the wave packet and wavelet directions must be computed in determining each point of a ray path. When variations occur in both the water depth and a current the change in the wavelet direction is computed using the wavelet ray curvature expression. It is found that the change in wavelet direction is given by

$$\Delta\gamma = \left[\left\{ \cos \rho \left(\tan \gamma \frac{\partial v}{\partial x} - \frac{\partial v}{\partial y} \right) \right\}_h + \left\{ \cos \rho \left(\tan \gamma \left(\frac{\partial v}{\partial x} + \frac{\partial u_x}{\partial x} \right) - \left(\frac{\partial v}{\partial y} + \frac{\partial u_y}{\partial y} \right) \right) \right\}_w \right] \frac{G_R \Delta t}{v + u_x} \quad (2-27)$$

where G_R is the ray speed and Δt is the time step interval between ray points. The variations due to water depth and current are considered separately. In Equation (2-27) the difference in the incremental distances which rays and wavelets advance for a given Δt has been taken into account.

The wavelet direction can be calculated using Snell's law with phase velocity. This approach has been found to be both more accurate and to require fewer calculations in locating the next ray point than when the ray curvature expression is used to compute the wavelet direction. Accordingly, if variations are to be considered only in the water depth or a current, but not both, Snell's law is used to compute the wavelet direction.

In order to use Snell's law, the incident wavelet angle is defined with respect to the normal to the wave speed contours which is extended in the direction of increasing wave speed. The wave speed contours are assumed to be locally parallel about the ray point. In the computations a number of rules are employed where the subscripts n and $(n+1)$ refer to consecutive points of a ray and n is a positive integer. The first step, if necessary, is to successively add or subtract 360° from the incident wavelet angle until it is within the range $0 \leq \gamma_n < 360^\circ$. Then when Snell's law is given by

$$\gamma_{n+1}^* = \arcsin \left(\frac{v_{n+1}}{v_n} \sin \gamma_n \right) \quad (2-28)$$

where $-90^\circ \leq \gamma_{n+1}^* \leq 90^\circ$, the angle γ_{n+1} is defined by the following scheme.

$$\gamma_{n+1} = \begin{cases} \gamma_{n+1}^* , & \gamma_n \leq 90^\circ \\ 180^\circ - \gamma_{n+1}^* , & 90^\circ < \gamma_n \leq 270^\circ \\ 360^\circ + \gamma_{n+1}^* , & \gamma_n > 270^\circ \end{cases} \quad (2-29)$$

e. Determining the path

Successive points of a ray are found by iteration using the ray curvature expression for a wave packet. The wavelet direction is determined at each point along the ray. The coordinates of each ray point are defined by

$$X_{m+1} = X_m + \Delta X \quad (2-30)$$

$$Y_{m+1} = Y_m + \Delta Y \quad (2-31)$$

where

$$\Delta X = (G \cos \bar{\theta} + u \cos \epsilon) \frac{\Delta t}{GRID} \quad (2-32)$$

$$\Delta Y = (G \sin \bar{\theta} + u \sin \epsilon) \frac{\Delta t}{GRID} \quad (2-33)$$

and where ϵ is the direction of the current with respect to the positive x-axis. Further

$$\bar{\theta} = \frac{1}{2} (\theta_m + \theta_{m+1}) \quad (2-34)$$

$$\theta_{m+1} = \theta_m + \Delta \theta \quad (2-35)$$

$$\Delta \theta = \frac{1}{2} [(K_G)_m + (K_G)_{m+1}] D_m. \quad (2-36)$$

$$D_m = \frac{G_r(\Delta t)}{GRID} \quad (2-37)$$

where D_m is the incremental distance in grid units between the points n and $(n \pm 1)$ of a ray, GRID is the grid unit distance in units consistent with G , and Δt is the time step.

f. Reflection points for water depths

Reflection points due to variations in water depth require special consideration. The waves are assumed to reflect if any of three criteria are satisfied. The first test for reflection is based on Snell's law with phase velocity. Reflection occurs if

$$\left| \frac{v_{m+1}}{v_m} \sin \gamma \right| > 1 \quad (2-38)$$

The wavelet angle is defined with respect to the normal to the wave speed contour which is extended in the direction of increasing water depth.

As a reflection point is approached the ray curvature changes so quickly that calculations of the ray curvature by iteration may cease to converge. If convergence fails reflection is assumed if the following conditions are met.

$$\frac{v_{m+1}}{v_m} > 1 \quad (2-39)$$

$$|\tan \gamma| > \tan 80^\circ$$

The first condition requires that the phase speed increases between the last two ray points, and the second condition requires that the wavelet direction be consistent with total reflection.

A third criterion is used to specify reflection points in order to maintain accuracy in calculating the ray trajectory. Very near a reflection point, due to the rapidly changing ray curvature, the estimates of ray points can become erratic. Therefore, reflection is assumed if the following conditions are met

$$\frac{v_{m+1}}{v_m} > 1$$

$$|\tan \gamma| > \tan 89.5^\circ \quad (2-40)$$

$$|\tan \theta| < \tan 75^\circ$$

When a reflection point is determined on the basis of either the second or third criterion, it is advisable to examine the printout to determine if the ray particulars are consistent with total reflection. The values of the packet ray curvature, the wavelet direction, the packet direction, and the geometric group velocity should exhibit the behavior described in Section (2.1), c.

When a reflection occurs there is an option either to halt the ray trajectory or to continue it as a reflection. When the reflection option is chosen, the reflection angles (defined with respect to the normal to the water depth contour) are determined by the relations

$$\gamma_r = -\gamma_i + 180^\circ \quad (2-41)$$

$$\theta_r = -\theta_i + 180^\circ \quad (2-42)$$

$$\rho_r = -\rho_i + 180^\circ \quad (2-43)$$

The subscript r denotes the reflection angles, and the subscript i signifies the angles at the last ray point reached prior to where the reflection criterion is satisfied.

The ray curvature calculations are more likely to converge and the accuracy of the path is increased if there is a restriction on how much the ray direction can change between successive ray points. Accordingly, if γ is within 10° of a direction for which the ray curvature is infinite, and θ is within 75° of being perpendicular to the water depth contour, the time step between ray points is successively halved, as necessary, until $|\Delta\theta|$ is less than 1° . In the event it is necessary to reduce the time step to less than 0.5 seconds the ray is stopped.

g. Total reflection for currents

Total reflection due to variations in a current is determined on the basis of Snell's law for the wavelets. Reflection occurs if

$$\left| \frac{(V + u_x)_{m+1} \sin \gamma}{(V + u_x)_m} \right| > 1 \quad (2-44)$$

where the wavelet angle is defined with respect to the normal to the wave speed contour which is extended in the direction of increasing current speed.

2.2 Wave Height Calculations. Modification of the wave height due to refraction, shoaling, and energy dissipation is considered. The wave height H increases when adjacent rays converge and it decreases when the rays diverge; this effect is accounted for by the refraction coefficient K_R . The shoaling coefficient K_S accounts for the change in H due to the variation in the propagation speed of the wave packet. The loss in energy due to wave motion at the sea bottom is determined by the friction coefficient K_F .

a. Without energy dissipation

The average rate of energy transmission F can be defined

$$F = E l G_T \quad (2-45)$$

where $G_T = G + u_m$, E is the energy per unit area, and l is the perpendicular distance between rays. Note that G_T is the speed of the advected group front. The energy is assumed to be conserved along the ray. Therefore

$$F_{j+1} = F_j \quad (2-46)$$

where j and $(j + 1)$ denote consecutive ray points. It is further assumed that E is proportional to H^2 . Accordingly, it follows from Equations (2-45) and (2-46) that

$$H_{j+1} = (K_S)_{j+1} (K_R)_{j+1} H_j \quad (2-47)$$

where $(K_S)_{j+1}$ and $(K_R)_{j+1}$ are the shoaling and refraction coefficients, respectively, between points j and $(j + 1)$.

$$(K_S)_{j+1} = \left(\frac{(G_T)_j}{(G_T)_{j+1}} \right)^{\frac{1}{2}} \quad (2-48)$$

$$(K_R)_{j+1} = \left(\frac{l_j}{l_{j+1}} \right)^{\frac{1}{2}} \quad (2-49)$$

If H_0 is the initial wave height, then the wave height at the n-th point is

$$H_m = K_S K_R H_0 \quad (2-50)$$

where

$$K_S = (K_S)_1 (K_S)_2 \cdots (K_S)_m = \left(\frac{(G_T)_0}{(G_T)_m} \right)^{\frac{1}{2}} \quad (2-51)$$

$$K_R = (K_R)_1 (K_R)_2 \cdots (K_R)_m = \left(\frac{l_0}{l_m} \right)^{\frac{1}{2}} \quad (2-52)$$

b. With energy dissipation

To account for energy losses, Equation (2-46) can be restated

$$F_{j+1} = (K_F)_{j+1}^2 F_j \quad (2-53)$$

where $(K_F)_{j+1}$ is the friction coefficient between the points j and $(j + 1)$. As a result, the relationship between the wave heights at consecutive ray points can be expressed by

$$H_{j+1} = (K_S)_{j+1} (K_R)_{j+1} (K_F)_{j+1} H_j \quad (2-54)$$

In terms of the initial wave height, the wave height at the n-th point is given by

$$H_m = K_S K_R K_F H_0 \quad (2-55)$$

where

$$K_F = (K_F)_1 (K_F)_2 \cdots (K_F)_M = (K_F)_M (K_F)_M \quad (2-56)$$

2.3 Refraction Coefficient. In computing K_R it is convenient to define

$$\beta = \frac{l_m}{l_0} \quad (2-57)$$

where β is called the ray separation factor. Equation (2-52) for the refraction coefficient becomes

$$K_R = |\beta|^{-\frac{1}{2}} \quad (2-58)$$

a. Ray separation equation

In considering the refraction of monochromatic waves, Munk and Arthur (1952) have shown that β can be determined from a second-order differential equation called the ray separation equation. The equation can be stated

$$\frac{d^2 \beta}{dt^2} + p \frac{d\beta}{dt} + q\beta = 0 \quad (2-59)$$

where t is time. For monochromatic waves with no currents

$$p = -2 \left(\cos \gamma \frac{\partial \psi}{\partial x} + \sin \gamma \frac{\partial \psi}{\partial y} \right) \quad (2-60)$$

$$q = v \left(\sin^2 \gamma \frac{\partial^2 v}{\partial x^2} - 2 \sin \gamma \cos \gamma \frac{\partial^2 v}{\partial x \partial y} + \cos^2 \gamma \frac{\partial^2 v}{\partial y^2} \right) \quad (2-61)$$

For a wave packet trajectory with currents

$$p = -2 \left[\cos \theta \left(\frac{\partial G}{\partial x} + \frac{\partial u_m}{\partial x} \right) + \sin \theta \left(\frac{\partial G}{\partial y} + \frac{\partial u_m}{\partial y} \right) \right] \quad (2-62)$$

$$q = G_T \left[\sin^2 \theta \left(\frac{\partial^2 G}{\partial x^2} + \frac{\partial^2 u_m}{\partial x^2} \right) - 2 \sin \theta \cos \theta \left(\frac{\partial^2 G}{\partial x \partial y} + \frac{\partial^2 u_m}{\partial x \partial y} \right) + \cos^2 \theta \left(\frac{\partial^2 G}{\partial y^2} + \frac{\partial^2 u_m}{\partial y^2} \right) \right] \quad (2-63)$$

As in the case of computing the ray curvature (Section (2.1), b), it is convenient to separate out the variations due to water depth and a current.

$$p = -2 \left[\left\{ \cos \theta \frac{\partial G}{\partial x} + \sin \theta \frac{\partial G}{\partial y} \right\}_h + \left\{ \cos \theta \left(\frac{\partial G}{\partial x} + \frac{\partial u_m}{\partial x} \right) + \sin \theta \left(\frac{\partial G}{\partial y} + \frac{\partial u_m}{\partial y} \right) \right\}_w \right] \quad (2-64)$$

$$q = G_T \left[\left\{ \sin^2 \theta \frac{\partial^2 G}{\partial x^2} - 2 \sin \theta \cos \theta \frac{\partial^2 G}{\partial x \partial y} + \cos^2 \theta \frac{\partial^2 G}{\partial y^2} \right\}_h + \left\{ \sin^2 \theta \left(\frac{\partial^2 G}{\partial x^2} + \frac{\partial^2 u_m}{\partial x^2} \right) - 2 \sin \theta \cos \theta \left(\frac{\partial^2 G}{\partial x \partial y} + \frac{\partial^2 u_m}{\partial x \partial y} \right) + \cos^2 \theta \left(\frac{\partial^2 G}{\partial y^2} + \frac{\partial^2 u_m}{\partial y^2} \right) \right\}_w \right] \quad (2-65)$$

b. Solution for parallel water depth contours

There is a simple solution to Equations (2-59), (2-62), and (2-63) when the water depth contours and current contours are mutually parallel. Then, when the xy-coordinate system is chosen with the x-axis perpendicular to the contours, it can be shown that

$$\beta = \frac{\cos \theta_n}{\cos \theta_0} \quad (2-66)$$

where the subscript 0 denotes the initial value and the subscript n depicts the value at the n-th ray point. The time derivative of Equation (2-66) can be expressed

$$\frac{\partial \beta}{\partial t} = -\beta \sin \theta \tan \theta \left(\frac{\partial G}{\partial X} + \frac{\partial u_m}{\partial X} \right) \quad (2-67)$$

c. Numerical solutions of the ray separation equation

Several numerical methods can be used to solve the ray separation equation. An easy to use fourth order finite difference solution to Equation (2-59) is the Fox method (Salvadori and Baron, 1961). However, this method has the disadvantage that the time step must be constant between successive ray points. When p and q do not change much between ray points, the general solution of a homogeneous second-order differential equation with constant coefficients (Wylie, 1951) can be used to solve the ray separation equation. This solution has 3 cases depending on the value of $(p^2 - 4q)$. The value of β at each new ray point is found using the values of p and q at the last point. There is usually little difference between the results obtained by this method and the Fox method.

A numerical method which does not require a constant time step and which better accounts for the variation of p and q along a ray is the Runge-Kutta method. This method is stable. It is also self-starting, i.e., values at the previous point are used to find values at the next point (Romanelli, 1960). For these reasons, the Runge-Kutta method was selected for the solution of the ray separation equation.

In order to use the Runge-Kutta method, Equation (2-59) is reduced to a system of first-order equations.

$$\frac{\partial \beta}{\partial t} = u_N \quad (2-68)$$

$$\frac{du_N}{dt} = -(p u_N + q \beta) \quad (2-69)$$

Both fourth and fifth order solutions of 3 are obtained. The initial conditions are the values of β and $d\beta/dt$ at the first ray point. The latter is estimated using Equation (2-67). The solutions require the values of (p_n, q_n) at the n -th ray point and the values (p_{n+1}, q_{n+1}) at the $(n+1)$ -th ray point. Further, the values of (p_1, q_1) , (p_2, q_2) , (p_3, q_3) , (p_4, q_4) , and (p_5, q_5) are needed along the ray at points intermediate to the ray points. They are determined, respectively, at time intervals of $(\Delta t)/3$, $(\Delta t)/4$, $0.45573725(\Delta t)$, $2(\Delta t)/3$, and $0.8(\Delta t)$ beyond the n -th ray point where Δt is the time step in the calculations.

A fourth order Runge-Kutta method with a minimum truncation error bound is given by Ralston (1962). The solution for the ray separation equation becomes

$$\begin{aligned} \beta_{m+1} = & \beta_m + 0.17476028 K_1 - 0.55148066 K_2 \\ & + 1.20553560 K_3 + 0.17118478 K_4 \end{aligned} \quad (2-70)$$

$$\begin{aligned} \left(\frac{d\beta}{dt}\right)_{m+1} = & \left(\frac{d\beta}{dt}\right)_m + 0.17476028 L_1 - 0.55148066 L_2 \\ & + 1.20553560 L_3 + 0.17118478 L_4 \end{aligned} \quad (2-71)$$

where

$$K_1 = (\Delta t) \left(\frac{d\beta}{dt}\right)_m \quad (2-72)$$

$$L_1 = -(\Delta t) \left[p_m \left(\frac{d\beta}{dt}\right)_m + q_m \beta_m \right] \quad (2-73)$$

$$K_2 = (\Delta t) \left[\left(\frac{d\beta}{dt}\right)_m + 0.4 L_1 \right] \quad (2-74)$$

$$L_2 = -(\Delta t) \left[p_2 \left(\left(\frac{d\beta}{dt}\right)_m + 0.4 L_1 \right) + q_2 (\beta_m + 0.4 K_1) \right] \quad (2-75)$$

$$K_3 = (\Delta t) \left[\left(\frac{d\beta}{dt} \right)_m + 0.29697761 L_1 + 0.15875964 L_2 \right] \quad (2-76)$$

$$L_3 = -(\Delta t) \left[p_3 \left(\left(\frac{d\beta}{dt} \right)_m + 0.29697761 L_1 + 0.15875964 L_2 \right) + q_3 (\beta_m + 0.29697761 K_1 + 0.15875964 K_2) \right] \quad (2-77)$$

$$K_4 = (\Delta t) \left[\left(\frac{d\beta}{dt} \right)_m + 0.21810040 L_1 - 3.05096516 L_2 + 3.83286476 L_3 \right] \quad (2-78)$$

$$L_4 = -(\Delta t) \left[p_{m+1} \left(\left(\frac{d\beta}{dt} \right)_m + 0.21810040 L_1 - 3.05096516 L_2 + 3.83286476 L_3 \right) + q_{m+1} (\beta_m + 0.21810040 K_1 - 3.05096516 K_2 + 3.83286476 K_3) \right] \quad (2-79)$$

A disadvantage of the Runge-Kutta method is that there is no simple means for estimating the truncation error (Milne, 1953). One procedure for controlling the error is to compute both fourth and fifth order solutions of β and to adjust the time step so that the two estimates differ by less than an arbitrary amount.

A fifth order Runge-Kutta method is given by Milne (1953). The fifth order solutions for β and $d\beta/dt$ are

$$\beta_{m+1}^{(5)} = \beta_m + \frac{1}{192} (23K_1 + 125K_6 - 81K_8 + 125K_9) \quad (2-80)$$

$$\left(\frac{d\beta}{dt} \right)_{m+1}^{(5)} = \left(\frac{d\beta}{dt} \right)_m + \frac{1}{192} (23L_1 + 125L_6 - 81L_8 + 125L_9) \quad (2-81)$$

where

$$K_5 = (\Delta t) \left[\left(\frac{\partial \beta}{\partial t} \right)_m + \frac{L_1}{3} \right] \quad (2-82)$$

$$L_5 = -(\Delta t) \left[p_1 \left(\left(\frac{\partial \beta}{\partial t} \right)_m + \frac{L_1}{3} \right) + q_1 \left(\beta_m + \frac{K_1}{3} \right) \right] \quad (2-83)$$

$$K_6 = (\Delta t) \left[\left(\frac{\partial \beta}{\partial t} \right)_m + \frac{6L_5 + 4L_1}{25} \right] \quad (2-84)$$

$$L_6 = -(\Delta t) \left[p_2 \left(\left(\frac{\partial \beta}{\partial t} \right)_m + \frac{6L_5 + 4L_1}{25} \right) + q_2 \left(\beta_m + \frac{6K_5 + 4K_1}{25} \right) \right] \quad (2-85)$$

$$K_7 = (\Delta t) \left[\left(\frac{\partial \beta}{\partial t} \right)_m + \frac{15L_6 - 12L_5 + L_1}{4} \right] \quad (2-86)$$

$$L_7 = -(\Delta t) \left[p_{m+1} \left(\left(\frac{\partial \beta}{\partial t} \right)_m + \frac{15L_6 - 12L_5 + L_1}{4} \right) + q_{m+1} \left(\beta_m + \frac{15K_6 - 12K_5 + K_1}{4} \right) \right] \quad (2-87)$$

$$K_8 = (\Delta t) \left[\left(\frac{\partial \beta}{\partial t} \right)_m + \frac{8L_7 - 50L_6 + 90L_5 + 6L_1}{81} \right] \quad (2-88)$$

$$L_8 = -(\Delta t) \left[p_4 \left(\left(\frac{\partial \beta}{\partial t} \right)_m + \frac{8L_7 - 50L_6 + 90L_5 + 6L_1}{81} \right) + q_4 \left(\beta_m + \frac{8K_7 - 50K_6 + 90K_5 + 6K_1}{81} \right) \right] \quad (2-89)$$

$$K_9 = (\Delta t) \left[\left(\frac{\partial \beta}{\partial t} \right)_m + \frac{8L_7 + 10L_6 + 36L_5 + 6L_1}{75} \right] \quad (2-90)$$

$$L_q = -(\Delta t) \left[p_5 \left(\left(\frac{d\beta}{dt} \right)_m + \frac{8L_7 + 10L_6 + 36L_5 + 6L_1}{75} \right) + q_5 \left(\beta_m + \frac{8K_7 + 10K_6 + 36K_5 + 6K_1}{75} \right) \right] \quad (2-91)$$

The difference between the fourth and fifth order solutions of β and $d\beta/dt$ are

$$\epsilon_\beta = \beta_{m+1} - \beta_m \quad (5) \quad (2-92)$$

$$\epsilon_{\beta t} = \left(\frac{d\beta}{dt} \right)_{m+1} - \left(\frac{d\beta}{dt} \right)_m \quad (5) \quad (2-93)$$

In the calculations, with the exception of when near reflection points, both $|\epsilon_\beta|$ and $|\epsilon_{\beta t}|$ are monitored. If either is greater than or equal to an arbitrary constant (determined as an input parameter) the time step is halved, the corresponding $(n+1)$ -th ray point is found, and the β and $d\beta/dt$ calculations are repeated. This process continues, as necessary, until both $|\epsilon_\beta|$ and $|\epsilon_{\beta t}|$ are less than the arbitrary constant. If the time step is reduced to less than 0.5 seconds the ray is stopped.

d. Reflection points

The numerical solutions of the ray separation equation have not proved satisfactory when leaving a reflection point. This is possibly due to the rapid changes in p which becomes infinite at the reflection point. However, as the reflection point is approached the value of β approaches a constant. Therefore, if the reflection option is chosen, the value of β is held constant in the calculations if the wavelet direction is within 10° of being parallel to the water depth contours. After passing the reflection point, Equation (2-67) is used to estimate $d\beta/dt$ for restarting the Runge-Kutta calculations. If the reflection option is not chosen the calculations of β continue up to the reflection point. As a result, by choosing this option it is possible to determine the value of β at a reflection point.

e. Caustics and focal points

The value of β is monitored along a ray. If the value of β becomes less than 0.0001 (K_R greater than 100) it is assumed that a focal point or caustic has been located. In this case the ray is stopped.

Near a caustic the ray separation equation is given approximately by

$$\frac{d^2\beta}{dt^2} + q\beta = 0 \quad (2-94)$$

In order to improve calculations near a caustic, if variations are considered in only water depth or currents, but not both, Equation (2-94) is used in computing β . For negative values of q the solution to this equation is

$$\beta = e^{-\sqrt{|q|} t} \quad (2-95)$$

and

$$\frac{d\beta}{dt} = -\sqrt{|q|} \beta \quad (2-96)$$

If the packet direction is within 5° of being parallel to the wave speed contours Equation (2-96) is used to evaluate $d\beta/dt$.

Very small or large values of K_R should be viewed with caution. The values may be incorrect due to numerical inaccuracies in the calculations. This can be checked by examining the behavior of adjacent rays on a plot. For large K_R values the rays should converge closely and for small values of K_R the rays should widely diverge. It is probably best to view K_R values less than 0.2 and greater than 5 in a qualitative sense.

2.4 Friction Coefficient. Energy dissipation of the waves due to bottom friction is considered. The friction coefficient is determined using a method based on the theory of Putnam and Johnson (1949) and Bretschneider and Reid (1954). Other energy dissipation methods can be substituted if desired.

In this work the friction factor c_f is defined following Jonsson (1966)

$$\tau = \frac{1}{2} c_f \rho_f u_M^2 \quad (2-97)$$

where τ is the tangential stress per unit area at the bottom, ρ_f is the density of the fluid, and u_M is the maximum velocity of the fluid at the bottom. The definition for τ given by Putnam and Johnson (1949) does not contain the factor $\frac{1}{2}$. When Equation (2-97) is used the friction coefficient becomes

$$K_F = \frac{(K_F)_m}{F (K_F)_m (\Delta s_G)_{m+1} + 1} \quad (2-98)$$

where $(K_F)_m$ is defined by Equation (2-56), $(\Delta s_G)_{n+1}$ is the incremental distance between the ray points n and $(n+1)$, and

$$F = \left(\frac{8\pi^2}{3g} \right) \left(\frac{c_f H_o}{U_o} \right) \left(\frac{K_s}{T \sinh kh} \right)^3 \quad (2-99)$$

2.5 Wave Breaking Criterion. In the program there is an option to determine if the waves break. When this option is chosen, the waves are assumed to break when the following relation is satisfied.

$$\frac{H}{\lambda} > \frac{1}{7} \tanh kh \quad (2-100)$$

2.6 Spatial Derivatives of G, U, v, and h for Water Depths. In this section relations are presented for connecting the partial derivatives of G, U, v, and the water depth h. Only variations in water depth are considered. A current is assumed to be either constant or not to exist. The spatial derivatives are determined in a coordinate system where the first order y-partial derivatives vanish and the second order y-derivatives are reduced to simplified expressions. As a result, there is a reduction in the number of calculations which would otherwise be required.

a. Determination of h and its partial derivatives

For each ray point the water depth h is interpolated from a quadratic surface equation which is fitted to the water depths at 12 grid points as illustrated in Figure (2-2). The use of a quadratic surface makes it possible to evaluate second derivatives which are required in calculating the wave height. The surface is approximated by the general quadratic equation (Dobson, 1967)

$$h = E_1 + E_2 x + E_3 y + E_4 x^2 + E_5 xy + E_6 y^2 \quad (2-101)$$

where the coefficients E are determined by fitting the equation by the method of least squares to the 12 water depth values. The partial derivatives of h are readily determined from Equation (2-101).

$$\frac{\partial h}{\partial x} = E_2 + 2E_4 x + E_5 y \quad (2-102)$$

$$\frac{\partial h}{\partial y} = E_3 + E_5 x + 2E_6 y \quad (2-103)$$

$$\frac{\partial^2 h}{\partial x^2} = 2E_4 \quad (2-104)$$

$$\frac{\partial^2 h}{\partial x \partial y} = E_5 \quad (2-105)$$

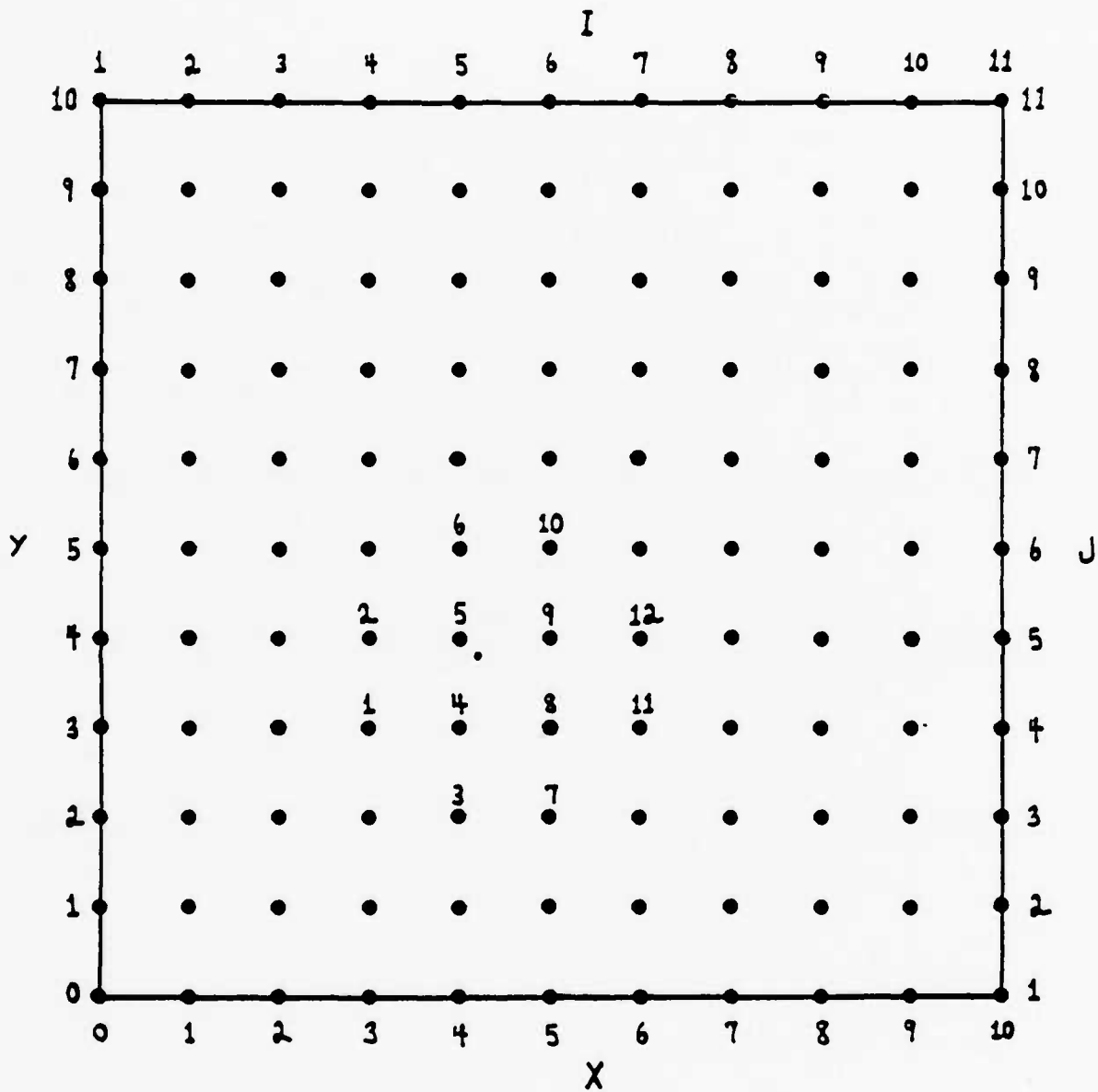


Figure (2-2). SELECTION OF WATER DEPTHS ABOUT
RAY POINT $(X,Y) = (4.2, 3.8)$

$$\frac{\partial^2 h}{\partial y^2} = 2E_6 \quad (2-106)$$

b. Rotation of axes to make computations

At each point of a wave packet trajectory the calculations are made in a $x'y'$ -coordinate system where the x' -axis is taken in the direction of the gradient of the water depth. The particulars of a trajectory are tabulated in a xy -coordinate system which retains a fixed orientation with respect to the water depth grid. The relationships between these coordinate systems and a specific ray point for a set of nonparallel water depth contours are shown in Figure (2-3). Equations relating these coordinate systems are given by

$$x' = x \cos \alpha + y \sin \alpha \quad (2-107)$$

$$y' = -x \sin \alpha + y \cos \alpha \quad (2-108)$$

$$\tan \alpha = \frac{\partial h}{\partial y} / \frac{\partial h}{\partial x} \quad (2-109)$$

where α is the angle by which the x' -axis is rotated with respect to the x -axis and h is the water depth. Note that

$$\rho' = \rho - \alpha \quad (2-110)$$

$$\theta' = \theta - \alpha \quad (2-111)$$

$$\gamma' = \gamma - \alpha \quad (2-112)$$

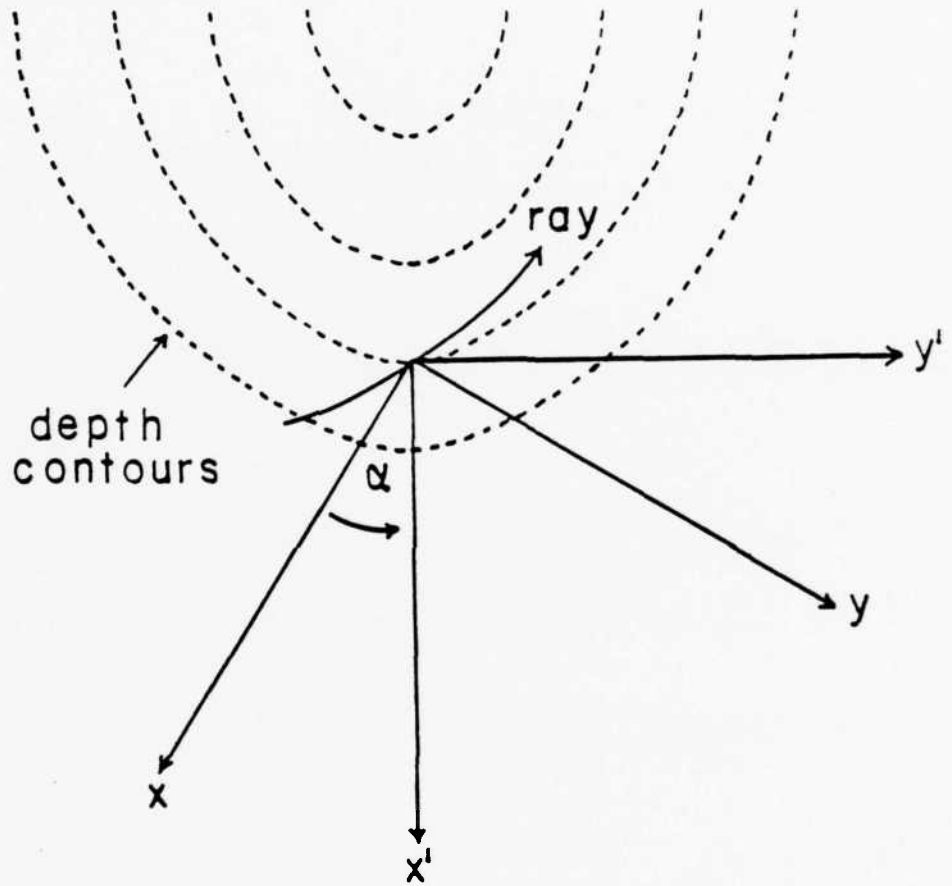


Figure (2-3). RELATIONSHIPS BETWEEN THE COORDINATE SYSTEMS AND THE WATER DEPTH CONTOURS

The partial derivatives of h in the $x'y'$ -coordinate system with respect to the partial derivatives of h in the xy -coordinate system are given by

$$\frac{\partial h}{\partial x'} = \frac{\partial h}{\partial x} \cos \alpha + \frac{\partial h}{\partial y} \sin \alpha \quad (2-113)$$

$$\frac{\partial h}{\partial y'} = -\frac{\partial h}{\partial x} \sin \alpha + \frac{\partial h}{\partial y} \cos \alpha = 0 \quad (2-114)$$

$$\frac{\partial^2 h}{(\partial x')^2} = \frac{\partial^2 h}{\partial x^2} \cos^2 \alpha + 2 \frac{\partial^2 h}{\partial x \partial y} \sin \alpha \cos \alpha + \frac{\partial^2 h}{\partial y^2} \sin^2 \alpha \quad (2-115)$$

$$\frac{\partial^2 h}{(\partial y')^2} = \frac{\partial^2 h}{\partial x^2} \sin^2 \alpha - 2 \frac{\partial^2 h}{\partial x \partial y} \sin \alpha \cos \alpha + \frac{\partial^2 h}{\partial y^2} \cos^2 \alpha \quad (2-116)$$

$$\frac{\partial^2 h}{\partial x' \partial y'} = \left(\frac{\partial^2 h}{\partial y^2} - \frac{\partial^2 h}{\partial x^2} \right) \sin \alpha \cos \alpha + \frac{\partial^2 h}{\partial x \partial y} (\cos^2 \alpha - \sin^2 \alpha) \quad (2-117)$$

c. Derivatives of v

As a convenience in the computations, the spatial derivatives of v are expressed in terms of the spatial derivatives of h . For linear theory (Lamb, 1932) the phase speed of a gravity water wave can be defined

$$v = \frac{g}{\omega} \tanh \frac{\omega h}{v} \quad (2-118)$$

where g is the acceleration due to gravity. The first partial derivatives of v in the $x'y'$ -coordinate system are given by (Wilson, 1966; Dobson, 1967; Breeding, 1972)

$$\frac{\partial v}{\partial x'} = W \frac{\partial h}{\partial x'} \quad (2-119)$$

$$\frac{\partial v}{\partial y'} = W \frac{\partial h}{\partial y'} = 0 \quad (2-120)$$

where

$$W = \frac{g v (1 - a^2 v^2)}{v^2 + g h (1 - a^2 v^2)} \quad (2-121)$$

$$a = \frac{c}{g} \quad (2-122)$$

The second partial derivatives of v are defined by

$$\frac{\partial^2 v}{(\partial x')^2} = W \left[\frac{\partial^2 h}{(\partial x')^2} + \gamma_h \left(\frac{\partial h}{\partial x'} \right)^2 \right] \quad (2-123)$$

$$\frac{\partial^2 v}{(\partial y')^2} = W \frac{\partial^2 h}{(\partial y')^2} \quad (2-124)$$

$$\frac{\partial^2 v}{\partial x' \partial y'} = W \frac{\partial^2 h}{\partial x' \partial y'} \quad (2-125)$$

where

$$\frac{y}{h} = - \frac{2g v^2}{[v^2 + gh(1 - \alpha^2 v^2)]^2} \quad (2-126)$$

d. Derivatives of U

For linear wave theory the collinear group speed of a gravity water wave can be defined

$$U = \frac{1}{2} \left(1 + \frac{I}{\sinh I} \right) v \quad (2-127)$$

where

$$I = \frac{2\omega h}{v} \quad (2-128)$$

The first partial derivatives of U in the x'y'-coordinate system are given by

$$\frac{\partial U}{\partial x'} = \frac{U}{v} \frac{\partial v}{\partial x'} + \eta \Phi \Psi_x \quad (2-129)$$

$$\frac{\partial U}{\partial y'} = \frac{U}{v} \frac{\partial v}{\partial y'} + \eta \Phi \Psi_y = 0 \quad (2-130)$$

where

$$\eta = \frac{U}{v} - \frac{1}{2} \quad (2-131)$$

$$\Phi = [1 - (I^2 + 4\eta^2)^{\frac{1}{2}}] \quad (2-132)$$

$$\psi_x = \frac{v}{h} \frac{\partial h}{\partial x'} - \frac{\partial v}{\partial x'} \quad (2-133)$$

$$\psi_y = \frac{v}{h} \frac{\partial h}{\partial y'} - \frac{\partial v}{\partial y'} = 0 \quad (2-134)$$

The second partial derivatives of U are given by

$$\frac{\partial^2 U}{(\partial x')^2} = \frac{U}{v} \frac{\partial^2 v}{(\partial x')^2} + \frac{\partial \eta}{\partial x'} \left(\frac{\partial v}{\partial x'} + \Phi \psi_x \right) + \eta \left(\psi_x \frac{\partial \Phi}{\partial x'} + \Phi \frac{\partial \psi_x}{\partial x'} \right) \quad (2-135)$$

$$\frac{\partial^2 U}{(\partial y')^2} = \frac{U}{v} \frac{\partial^2 v}{(\partial y')^2} + \eta \Phi \frac{\partial \psi_x}{\partial y'} \quad (2-136)$$

$$\frac{\partial^2 U}{\partial x' \partial y'} = \frac{U}{v} \frac{\partial^2 v}{\partial x' \partial y'} + \eta \Phi \frac{\partial \psi_x}{\partial y'} \quad (2-137)$$

where

$$\frac{\partial \eta}{\partial x'} = \frac{1}{v} \left(\frac{\partial U}{\partial x'} - \frac{U}{v} \frac{\partial v}{\partial x'} \right) \quad (2-138)$$

$$\frac{\partial \Phi}{\partial x'} = - \frac{\frac{I^2 \psi_x}{v} + 4\eta \frac{\partial \eta}{\partial x'}}{(I^2 + 4\eta^2)^{\frac{1}{2}}} \quad (2-139)$$

$$\frac{\partial \psi_x}{\partial x'} = \frac{1}{h} \left(v \frac{\partial^2 h}{(\partial x')^2} - \psi_x \frac{\partial h}{\partial x'} \right) - \frac{\partial^2 v}{(\partial x')^2} \quad (2-140)$$

$$\frac{\partial \psi_x}{\partial y'} = \frac{v}{h} \frac{\partial^2 h}{(\partial y')^2} - \frac{\partial^2 v}{(\partial y')^2} \quad (2-141)$$

$$\frac{\partial \psi_x}{\partial y'} = \frac{v}{h} \frac{\partial^2 h}{\partial x' \partial y'} - \frac{\partial^2 v}{\partial x' \partial y'} \quad (2-142)$$

e. Derivatives of G

The first partial derivatives of G were derived in Section (2.1), b as Equations (2-22) and (2-23). In the x'y'-coordinate system these derivatives become

$$\frac{\partial G}{\partial x'} = \frac{\frac{\partial U}{\partial x'} \cos \phi + \frac{U}{v} \sin \phi \tan \gamma' \frac{\partial v}{\partial x'}}{1 + \tan \phi \tan \theta'} \quad (2-143)$$

$$\frac{\partial G}{\partial y'} = 0 \quad (2-144)$$

The second partial derivatives of G can be expressed by

$$\begin{aligned} \frac{\partial^2 G}{(\partial x')^2} = & \frac{1}{1 + \tan \phi \tan \theta'} \left[\frac{\partial^2 U}{(\partial x')^2} \cos \phi - \frac{\partial \phi}{\partial x'} \left(2 \frac{\partial U}{\partial x'} \sin \phi + G \frac{\partial \phi}{\partial x'} \right) \right. \\ & \left. - U \sin \phi \left\{ \tan \theta' \left(\frac{\partial \theta'}{\partial x'} \right)^2 - \tan \gamma' \left[\frac{1}{v} \frac{\partial^2 v}{(\partial x')^2} + \left(\frac{\partial \gamma'}{\partial x'} \right)^2 \right] \right\} \right] \end{aligned} \quad (2-145)$$

$$\frac{\partial^2 G}{(\partial y')^2} = \frac{\frac{\partial^2 U}{(\partial y')^2} \cos \phi - \frac{U}{v} \sin \phi \cot \gamma' \frac{\partial^2 v}{(\partial y')^2}}{1 - \tan \phi \cot \theta'} \quad (2-146)$$

$$\frac{\partial^2 G}{\partial x' \partial y'} = \frac{\frac{\partial^2 U}{\partial x' \partial y'} \cos \phi + \frac{U}{v} \sin \phi \tan \gamma' \frac{\partial^2 v}{\partial x' \partial y'}}{1 + \tan \phi \tan \theta'} \quad (2-147)$$

where

$$\frac{\partial \phi}{\partial x'} = \frac{\partial \theta'}{\partial x'} - \frac{\partial \gamma'}{\partial x'} \quad (2-148)$$

$$\frac{\partial \theta'}{\partial x'} = \frac{\tan \theta'}{G} \frac{\partial G}{\partial x'} \quad (2-149)$$

$$\frac{\partial \gamma'}{\partial x'} = \frac{\tan \gamma'}{v} \frac{\partial v}{\partial x'} \quad (2-150)$$

2.7 Spatial Derivatives of G , U , v , ω , u , and ε for Currents. In this section relations are presented for connecting the partial derivatives of G , U , v , ω , and a current of magnitude u and direction ε . The water depth is assumed to be constant. The spatial derivatives are determined in a coordinate system where the y -derivatives are reduced to simplified expressions. This results in a corresponding reduction in the number of computations.

a. Determination of u , ε , and their partial derivatives

For each ray point the current components u_x and u_y are interpolated from quadratic surface equations which are fitted to their respective current component values at 12 grid points as described for water depths in Section (2.6), a. The resulting quadratic equations are

$$u_x = E_{x1} + E_{x2} X + E_{x3} Y + E_{x4} X^2 + E_{x5} XY + E_{x6} Y^2 \quad (2-151)$$

$$u_y = E_{y1} + E_{y2} X + E_{y3} Y + E_{y4} X^2 + E_{y5} XY + E_{y6} Y^2 \quad (2-152)$$

The magnitude of the current is given by

$$u = (u_x^2 + u_y^2)^{\frac{1}{2}} \quad (2-153)$$

and the current direction is defined by

$$\tan \epsilon = \frac{u_y}{u_x} \quad (2-154)$$

The partial derivatives of u_x and u_y are found from Equations (2-151) and (2-152).

$$\frac{\partial u_x}{\partial X} = E_{x2} + 2E_{x4}X + E_{x5}Y \quad (2-155)$$

$$\frac{\partial u_x}{\partial Y} = E_{x3} + E_{x5}X + 2E_{x6}Y \quad (2-156)$$

$$\frac{\partial^2 u_x}{\partial X^2} = 2E_{x4} \quad (2-157)$$

$$\frac{\partial^2 u_x}{\partial X \partial Y} = E_{x5} \quad (2-158)$$

$$\frac{\partial^2 u_x}{\partial Y^2} = 2E_{x6} \quad (2-159)$$

$$\frac{\partial u_y}{\partial X} = E_{y2} + 2E_{y4}X + E_{y5}Y \quad (2-160)$$

$$\frac{\partial u_y}{\partial y} = E_{y3} + E_{y5}x + 2E_{y6}y \quad (2-161)$$

$$\frac{\partial^2 u_y}{\partial x^2} = 2E_{y4} \quad (2-162)$$

$$\frac{\partial^2 u_y}{\partial x \partial y} = E_{y5} \quad (2-163)$$

$$\frac{\partial^2 u_y}{\partial y^2} = 2E_{y6} \quad (2-164)$$

The partial derivatives of u are found to be given by

$$\frac{\partial u}{\partial x} = \frac{1}{u} \left(u_x \frac{\partial u_x}{\partial x} + u_y \frac{\partial u_y}{\partial x} \right) \quad (2-165)$$

$$\frac{\partial u}{\partial y} = \frac{1}{u} \left(u_x \frac{\partial u_x}{\partial y} + u_y \frac{\partial u_y}{\partial y} \right) \quad (2-166)$$

$$\frac{\partial^2 u}{\partial x^2} = \frac{1}{u} \left[u_x \frac{\partial^2 u_x}{\partial x^2} + \left(\frac{\partial u_x}{\partial x} \right)^2 + u_y \frac{\partial^2 u_y}{\partial x^2} + \left(\frac{\partial u_y}{\partial x} \right)^2 - \left(\frac{\partial u}{\partial x} \right)^2 \right] \quad (2-167)$$

$$\frac{\partial^2 u}{\partial x \partial y} = \frac{1}{u} \left[u_x \frac{\partial^2 u_x}{\partial x \partial y} + \frac{\partial u_x}{\partial x} \frac{\partial u_x}{\partial y} + u_y \frac{\partial^2 u_y}{\partial x \partial y} + \frac{\partial u_y}{\partial x} \frac{\partial u_y}{\partial y} - \frac{\partial u}{\partial x} \frac{\partial u}{\partial y} \right] \quad (2-168)$$

$$\frac{\partial^2 u}{\partial y^2} = \frac{1}{u} \left[u_x \frac{\partial^2 u_x}{\partial y^2} + \left(\frac{\partial u_x}{\partial y} \right)^2 + u_y \frac{\partial^2 u_y}{\partial y^2} + \left(\frac{\partial u_y}{\partial y} \right)^2 - \left(\frac{\partial u}{\partial y} \right)^2 \right] \quad (2-169)$$

The partial derivatives of ε are determined to be

$$\frac{\partial \varepsilon}{\partial x} = \frac{1}{u^2} \left(u_x \frac{\partial u_y}{\partial x} - u_y \frac{\partial u_x}{\partial x} \right) \quad (2-170)$$

$$\frac{\partial \varepsilon}{\partial y} = \frac{1}{u^2} \left(u_x \frac{\partial u_y}{\partial y} - u_y \frac{\partial u_x}{\partial y} \right) \quad (2-171)$$

$$\frac{\partial^2 \varepsilon}{\partial x^2} = \frac{1}{u} \left[\frac{1}{u} \left(u_x \frac{\partial^2 u_y}{\partial x^2} - u_y \frac{\partial^2 u_x}{\partial x^2} \right) - 2 \frac{\partial \varepsilon}{\partial x} \frac{\partial u}{\partial x} \right] \quad (2-172)$$

$$\begin{aligned} \frac{\partial^2 \varepsilon}{\partial x \partial y} = \frac{1}{u} \left[\frac{1}{u} \left(\frac{\partial u_x}{\partial x} \frac{\partial u_y}{\partial y} + u_x \frac{\partial^2 u_y}{\partial x \partial y} - \frac{\partial u_y}{\partial x} \frac{\partial u_x}{\partial y} - u_y \frac{\partial^2 u_x}{\partial x \partial y} \right) \right. \\ \left. - 2 \frac{\partial \varepsilon}{\partial y} \frac{\partial u}{\partial x} \right] \quad (2-173) \end{aligned}$$

$$\frac{\partial^2 \epsilon}{\partial y^2} = \frac{1}{u} \left[\frac{1}{u} \left(u_x \frac{\partial^2 u_y}{\partial y^2} - u_y \frac{\partial^2 u_x}{\partial y^2} \right) - 2 \frac{\partial \epsilon}{\partial y} \frac{\partial u}{\partial y} \right] \quad (2-174)$$

b. Rotation of axes to make computations

Following the procedure described in Section (2.6), b for water depths, the calculations are made in a $x''y''$ -coordinate system where the x'' -axis is taken in the direction of the gradient of the current speed. The ray particulars are tabulated in the xy -coordinate system which is fixed with respect to the current grids. The equations which relate these coordinate systems are expressed by

$$x'' = x \cos \alpha_c + y \sin \alpha_c \quad (2-175)$$

$$y'' = -x \sin \alpha_c + y \cos \alpha_c \quad (2-176)$$

$$\tan \alpha_c = \frac{\partial u}{\partial y} / \frac{\partial u}{\partial x} \quad (2-177)$$

where α_c is the angle by which the x'' -axis is rotated with respect to the x -axis. ^c Further

$$\rho'' = \rho - \alpha_c \quad (2-178)$$

$$\theta'' = \theta - \alpha_c \quad (2-179)$$

$$y'' = Y - \alpha_c \quad (2-180)$$

The partial derivatives of u in the $x''y''$ -coordinate system with respect to the partial derivatives of u in the xy -coordinate system are given by

$$\frac{\partial u}{\partial x''} = \frac{\partial u}{\partial x} \cos \alpha_c + \frac{\partial u}{\partial y} \sin \alpha_c \quad (2-181)$$

$$\frac{\partial u}{\partial y''} = -\frac{\partial u}{\partial x} \sin \alpha_c + \frac{\partial u}{\partial y} \cos \alpha_c = 0 \quad (2-182)$$

$$\frac{\partial^2 u}{(\partial x'')^2} = \frac{\partial^2 u}{\partial x^2} \cos^2 \alpha_c + 2 \frac{\partial^2 u}{\partial x \partial y} \sin \alpha_c \cos \alpha_c + \frac{\partial^2 u}{\partial y^2} \sin^2 \alpha_c \quad (2-183)$$

$$\frac{\partial^2 u}{(\partial y'')^2} = \frac{\partial^2 u}{\partial x^2} \sin^2 \alpha_c - 2 \frac{\partial^2 u}{\partial x \partial y} \sin \alpha_c \cos \alpha_c + \frac{\partial^2 u}{\partial y^2} \cos^2 \alpha_c \quad (2-184)$$

$$\frac{\partial^2 u}{\partial x'' \partial y''} = \left(\frac{\partial^2 u}{\partial y^2} - \frac{\partial^2 u}{\partial x^2} \right) \sin \alpha_c \cos \alpha_c + \frac{\partial^2 u}{\partial x \partial y} (\cos^2 \alpha_c - \sin^2 \alpha_c) \quad (2-185)$$

The relations connecting the partial derivatives of ϵ between the two coordinate systems are given by

$$\frac{\partial \epsilon''}{\partial x''} = \frac{\partial \epsilon}{\partial x} \cos \alpha_c + \frac{\partial \epsilon}{\partial y} \sin \alpha_c \quad (2-186)$$

$$\frac{\partial \epsilon''}{\partial y''} = - \frac{\partial \epsilon}{\partial x} \sin \alpha_c + \frac{\partial \epsilon}{\partial y} \cos \alpha_c \quad (2-187)$$

$$\frac{\partial^2 \epsilon''}{(\partial x'')^2} = \frac{\partial^2 \epsilon}{\partial x^2} \cos^2 \alpha_c + 2 \frac{\partial^2 \epsilon}{\partial x \partial y} \sin \alpha_c \cos \alpha_c + \frac{\partial^2 \epsilon}{\partial y^2} \sin^2 \alpha_c \quad (2-188)$$

$$\frac{\partial^2 \epsilon''}{(\partial y'')^2} = \frac{\partial^2 \epsilon}{\partial x^2} \sin^2 \alpha_c - 2 \frac{\partial^2 \epsilon}{\partial x \partial y} \sin \alpha_c \cos \alpha_c + \frac{\partial^2 \epsilon}{\partial y^2} \cos^2 \alpha_c \quad (2-189)$$

$$\frac{\partial^2 \epsilon''}{\partial x'' \partial y''} = \left(\frac{\partial^2 \epsilon}{\partial y^2} - \frac{\partial^2 \epsilon}{\partial x^2} \right) \sin \alpha_c \cos \alpha_c + \frac{\partial^2 \epsilon}{\partial x \partial y} (\cos^2 \alpha_c - \sin^2 \alpha_c) \quad (2-190)$$

c. Derivatives of ω , v , and u_k

In Section (2.6), c the derivatives of v are expressed directly in terms of the corresponding derivatives of water depth. In considering currents the derivatives of v are related to derivatives in ω . For the first x'' -derivatives it is found that

$$\frac{\partial \omega}{\partial x''} = - \left\{ 1 - \frac{k M_a W_\omega}{1 + M_a} + \frac{u_a}{v} (1 - k W_\omega) \right\}^{-1} \left[\frac{k}{(1 + M_a)} \left[\frac{\partial u}{\partial x''} \cos(\gamma'' - \epsilon'') \right. \right. \quad (2-191)$$

$$\left. \left. + u \sin(\gamma'' - \epsilon'') \frac{\partial \epsilon''}{\partial x''} \right] \right]$$

$$\frac{\partial u_a}{\partial x''} = - \frac{M_a}{1 + M_a} \frac{\partial v}{\partial x''} + \frac{1}{1 + M_a} \left[\frac{\partial u}{\partial x''} \cos(\gamma'' - \epsilon'') + u \sin(\gamma'' - \epsilon'') \frac{\partial \epsilon''}{\partial x''} \right] \quad (2-192)$$

$$\frac{\partial v}{\partial x''} = W_{\omega} \frac{\partial \omega}{\partial x''} \quad (2-193)$$

where

$$W_{\omega} = \frac{hg v (1 - a^2 v^2) - v^3}{\omega [v^2 + gh (1 - a^2 v^2)]} \quad (2-194)$$

$$a = \frac{\omega}{g} \quad (2-195)$$

$$M_{\xi} = \frac{u \sin(\gamma'' - \epsilon'') \tan \gamma''}{v + u_{\xi}} \quad (2-196)$$

$$u_{\xi} = u \cos(\gamma'' - \epsilon'') \quad (2-197)$$

The first y'' -derivatives can be expressed

$$\frac{\partial \omega}{\partial y''} = - \left\{ 1 + \frac{h M_{\xi} W_{\omega}}{1 - M_{\xi}} + \frac{u_{\xi}}{v} (1 - h W_{\omega}) \right\}^{-1} \left(\frac{h}{1 - M_{\xi}} \right) u \sin(\gamma'' - \epsilon'') \frac{\partial \epsilon''}{\partial y''} \quad (2-198)$$

$$\frac{\partial u_{\xi}}{\partial y''} = \frac{M_{\xi}}{1 - M_{\xi}} \frac{\partial v}{\partial y''} + \frac{1}{1 - M_{\xi}} u \sin(\gamma'' - \epsilon'') \frac{\partial \epsilon''}{\partial y''} \quad (2-199)$$

$$\frac{\partial v}{\partial y''} = W_{\omega} \frac{\partial \omega}{\partial y''} \quad (2-200)$$

where

$$M_2 = \frac{u \sin(\gamma'' - \epsilon'') \cot \gamma''}{v + u_2} \quad (2-201)$$

The second x'' -derivatives are determined to be

$$\begin{aligned} \frac{\partial^2 \omega}{(\partial x'')^2} = & \left(1 - \frac{h M_2 W_\omega}{1 + M_2} + \frac{u_2 (1 - h W_\omega)}{v} \right)^{-1} \left[\frac{h M_2 \gamma_\omega}{1 + M_2} \left(\frac{\partial \omega}{\partial x''} \right)^2 - h u_2 \right. \\ & \left. - 2 \frac{\partial h}{\partial x''} \frac{\partial u_2}{\partial x''} + \frac{u_2}{v} \frac{\partial \omega}{\partial x''} \left(\frac{1 - h W_\omega}{v} \frac{\partial v}{\partial x''} + h \gamma_\omega \frac{\partial \omega}{\partial x''} + W_\omega \frac{\partial h}{\partial x''} \right) \right] \end{aligned} \quad (2-202)$$

$$\frac{\partial^2 u_2}{(\partial x'')^2} = - \frac{M_2}{1 + M_2} \frac{\partial^2 v}{(\partial x'')^2} + u_2 \quad (2-203)$$

$$\frac{\partial^2 v}{(\partial x'')^2} = W_\omega \frac{\partial^2 \omega}{(\partial x'')^2} + \gamma_\omega \left(\frac{\partial \omega}{\partial x''} \right)^2 \quad (2-204)$$

where

$$\begin{aligned} \gamma_\omega = & \frac{2v}{v^2 + g h (1 - a^2 v^2)} \left[\left(\frac{v}{\omega} \right)^2 + h (1 - a^2 v^2) \left\{ (g - h \omega^2) \left(\frac{W_\omega}{v} \right)^2 \right. \right. \\ & \left. \left. + 2 h \omega \left(\frac{W_\omega}{v} \right) - \frac{1}{a \omega} - h \right\} \right] \end{aligned} \quad (2-205)$$

$$\begin{aligned}
 u_2 = \frac{1}{1+M_2} & \left[\frac{\partial^2 u}{(\partial X'')^2} \cos(\gamma'' - \epsilon'') - 2 \frac{\partial u}{\partial X''} \sin(\gamma'' - \epsilon'') \left(\frac{\partial \gamma''}{\partial X''} - \frac{\partial \epsilon''}{\partial X''} \right) \right. \\
 & - u \cos(\gamma'' - \epsilon'') \left(\frac{\partial \gamma''}{\partial X''} - \frac{\partial \epsilon''}{\partial X''} \right)^2 + u \sin(\gamma'' - \epsilon'') \left\{ -\tan \gamma'' \left(\frac{\partial \gamma''}{\partial X''} \right)^2 \right. \\
 & \left. \left. + \frac{\partial^2 \epsilon''}{(\partial X'')^2} \right\} \right] \quad (2-206)
 \end{aligned}$$

$$\frac{\partial \gamma''}{\partial X''} = \frac{\tan \gamma''}{v + u_2} \left(\frac{\partial v}{\partial X''} + \frac{\partial u_2}{\partial X''} \right) \quad (2-207)$$

$$\frac{\partial h}{\partial X''} = \frac{1 - h W_\omega}{v} \frac{\partial \omega}{\partial X''} \quad (2-208)$$

The second derivatives with respect to y'' become

$$\begin{aligned}
 \frac{\partial^2 \omega}{(\partial y'')^2} = & \left(1 + \frac{h M_2 W_\omega}{1 - M_2} + \frac{u_2 (1 - h W_\omega)}{v} \right)^{-1} \left[-\frac{h M_2 \gamma_\omega}{1 - M_2} \left(\frac{\partial \omega}{\partial y''} \right)^2 - h u_3 \right. \\
 & \left. - 2 \frac{\partial h}{\partial y''} \frac{\partial u_2}{\partial y''} + \frac{u_2}{v} \frac{\partial \omega}{\partial y''} \left(\frac{1 - h W_\omega}{v} \frac{\partial v}{\partial y''} + h \gamma_\omega \frac{\partial \omega}{\partial y''} + W_\omega \frac{\partial h}{\partial y''} \right) \right] \quad (2-209)
 \end{aligned}$$

$$\frac{\partial^2 u_2}{(\partial y'')^2} = \frac{M_2}{1 - M_2} \frac{\partial^2 v}{(\partial y'')^2} + u_3 \quad (2-210)$$

$$\frac{\partial^2 v}{(\partial y'')^2} = W_\omega \frac{\partial^2 \omega}{(\partial y'')^2} + \gamma_\omega \left(\frac{\partial \omega}{\partial y''} \right)^2 \quad (2-211)$$

where

$$u_3 = \frac{1}{1-M_R} \left[\frac{\partial^2 u}{(\partial y''')^2} \cos(\gamma'' - \epsilon'') - u \cos(\gamma'' - \epsilon'') \left(\frac{\partial \gamma''}{\partial y''} - \frac{\partial \epsilon''}{\partial y''} \right)^2 \right. \\ \left. + u \sin(\gamma'' - \epsilon'') \left\{ \cot \gamma'' \left(\frac{\partial \gamma''}{\partial y''} \right)^2 + \frac{\partial^2 \epsilon''}{(\partial y''')^2} \right\} \right] \quad (2-212)$$

$$\frac{\partial \gamma''}{\partial y''} = - \frac{\cot \gamma''}{v + u_2} \left(\frac{\partial v}{\partial y''} + \frac{\partial u_2}{\partial y''} \right) \quad (2-213)$$

$$\frac{\partial h}{\partial y''} = \frac{1 - h W_\omega}{v} \frac{\partial \omega}{\partial y''} \quad (2-214)$$

The mixed derivatives can be stated as

$$\frac{\partial^2 \omega}{\partial x'' \partial y''} = \left(1 - \frac{h M_R W_\omega}{1 + M_R} + \frac{u_2 (1 - h W_\omega)}{v} \right)^{-1} \left[\frac{h M_R \gamma_\omega}{1 + M_R} \frac{\partial \omega}{\partial x''} \frac{\partial \omega}{\partial y''} \right. \\ \left. - h u_4 - \frac{\partial h}{\partial y''} \frac{\partial u_2}{\partial x''} - \frac{\partial u_2}{\partial y''} \frac{\partial h}{\partial x''} + \frac{u_2}{v} \frac{\partial \omega}{\partial x''} \left(\frac{1 - h W_\omega}{v} \frac{\partial v}{\partial y''} \right. \right. \\ \left. \left. + h \gamma_\omega \frac{\partial \omega}{\partial y''} + W_\omega \frac{\partial h}{\partial y''} \right) \right] \quad (2-215)$$

$$\frac{\partial^2 u_2}{\partial x'' \partial y''} = - \frac{M_R}{1 + M_R} \frac{\partial^2 v}{\partial x'' \partial y''} + u_4 \quad (2-216)$$

$$\frac{\partial^2 v}{\partial x'' \partial y''} = W_\omega \frac{\partial^2 \omega}{\partial x'' \partial y''} + \gamma_\omega \frac{\partial \omega}{\partial x''} \frac{\partial \omega}{\partial y''} \quad (2-217)$$

where

$$\begin{aligned}
 u_4 = & \frac{1}{1+M_g} \left[\frac{\partial^2 u}{\partial x'' \partial y''} \cos(\gamma'' - \epsilon'') - \frac{\partial u}{\partial x''} \sin(\gamma'' - \epsilon'') \left(\frac{\partial \gamma''}{\partial y''} - \frac{\partial \epsilon''}{\partial y''} \right) \right. \\
 & - u \cos(\gamma'' - \epsilon'') \left(\frac{\partial \gamma''}{\partial x''} - \frac{\partial \epsilon''}{\partial x''} \right) \left(\frac{\partial \gamma''}{\partial y''} - \frac{\partial \epsilon''}{\partial y''} \right) \\
 & \left. + u \sin(\gamma'' - \epsilon'') \left\{ -(\cot \gamma'' + 2 \tan \gamma'') \frac{\partial \gamma''}{\partial x''} \frac{\partial \gamma''}{\partial y''} + \frac{\partial^2 \epsilon''}{\partial x'' \partial y''} \right\} \right]
 \end{aligned} \tag{2-218}$$

d. Derivatives of U

The spatial derivatives of U due to variations in a current are similar to the derivatives presented in Section (2.6), d for variations in U due to changes in water depth. The first derivatives are seen to be

$$\frac{\partial U}{\partial x''} = \frac{U}{v} \frac{\partial v}{\partial x''} + \eta \Phi \Delta_x \tag{2-219}$$

$$\frac{\partial U}{\partial y''} = \frac{U}{v} \frac{\partial v}{\partial y''} + \eta \Phi \Delta_y \tag{2-220}$$

where

$$\eta = \frac{U}{v} - \frac{1}{2} \tag{2-221}$$

$$\Phi = \left[1 - (I^2 + 4\eta^2)^{\frac{1}{2}} \right] \tag{2-222}$$

$$I = \frac{2\omega h}{v} \tag{2-223}$$

$$\Delta_x = \frac{v}{\omega} \frac{\partial \omega}{\partial x''} - \frac{\partial v}{\partial x''} \tag{2-224}$$

$$\Delta_{\psi} = \frac{\nu}{\omega} \frac{\partial \omega}{\partial \psi''} - \frac{\partial \nu}{\partial \psi''} \quad (2-225)$$

Note that η , Φ , and I are defined the same as in Section (2.6), d.
The second spatial derivatives of U are given by

$$\frac{\partial^2 U}{(\partial x''^2)^2} = \frac{U}{\nu} \frac{\partial^2 \nu}{(\partial x''^2)^2} + \frac{\partial \eta}{\partial x''} \left(\frac{\partial \nu}{\partial x''} + \Phi \Delta_x \right) + \eta \left(\Delta_x \frac{\partial \Phi}{\partial x''} + \Phi \frac{\partial \Delta_x}{\partial x''} \right) \quad (2-226)$$

$$\frac{\partial^2 U}{(\partial \psi''^2)^2} = \frac{U}{\nu} \frac{\partial^2 \nu}{(\partial \psi''^2)^2} + \frac{\partial \eta}{\partial \psi''} \left(\frac{\partial \nu}{\partial \psi''} + \Phi \Delta_{\psi} \right) + \eta \left(\Delta_{\psi} \frac{\partial \Phi}{\partial \psi''} + \Phi \frac{\partial \Delta_{\psi}}{\partial \psi''} \right) \quad (2-227)$$

$$\frac{\partial^2 U}{\partial x'' \partial \psi''} = \frac{U}{\nu} \frac{\partial^2 \nu}{\partial x'' \partial \psi''} + \frac{\partial \eta}{\partial \psi''} \left(\frac{\partial \nu}{\partial x''} + \Phi \Delta_x \right) + \eta \left(\Delta_x \frac{\partial \Phi}{\partial \psi''} + \Phi \frac{\partial \Delta_x}{\partial \psi''} \right) \quad (2-228)$$

where

$$\frac{\partial \eta}{\partial x''} = \frac{1}{\nu} \left(\frac{\partial U}{\partial x''} - \frac{U}{\nu} \frac{\partial \nu}{\partial x''} \right) \quad (2-229)$$

$$\frac{\partial \Phi}{\partial x''} = - \frac{\frac{I^2 \Delta_x}{\nu} + 4 \eta \frac{\partial \eta}{\partial x''}}{(I^2 + 4 \eta^2)^{\frac{1}{2}}} \quad (2-230)$$

$$\frac{\partial \Delta_x}{\partial x''} = \frac{1}{\omega} \left(\nu \frac{\partial^2 \omega}{(\partial x''^2)^2} - \Delta_x \frac{\partial \omega}{\partial x''} \right) - \frac{\partial^2 \nu}{(\partial x''^2)^2} \quad (2-231)$$

$$\frac{\partial \eta}{\partial \psi''} = \frac{1}{v} \left(\frac{\partial U}{\partial \psi''} - \frac{U}{v} \frac{\partial v}{\partial \psi''} \right) \quad (2-232)$$

$$\frac{\partial \Phi}{\partial \psi''} = - \frac{\frac{I^2 \Delta \psi}{v} + 4\eta \frac{\partial \eta}{\partial \psi''}}{(I^2 + 4\eta^2)^{\frac{1}{2}}} \quad (2-233)$$

$$\frac{\partial \Delta \psi}{\partial \psi''} = \frac{1}{\omega} \left(v \frac{\partial^2 \omega}{(\partial \psi'')^2} - \Delta \psi \frac{\partial \omega}{\partial \psi''} \right) - \frac{\partial^2 v}{(\partial \psi'')^2} \quad (2-234)$$

$$\frac{\partial \Delta x}{\partial \psi''} = \frac{1}{\omega} \left(v \frac{\partial^2 \omega}{\partial x'' \partial \psi''} - \Delta \psi \frac{\partial \omega}{\partial x''} \right) - \frac{\partial^2 v}{\partial x'' \partial \psi''} \quad (2-235)$$

e. Derivatives of G and u_m

The first partial derivatives of G are considered in Section (2.1), b. It is necessary to consider the derivatives of G and u_m together. For the first x'' -derivatives it is found that

$$\frac{\partial u_m}{\partial x''} = - \frac{M}{1+M} \frac{\partial G}{\partial x''} + \frac{1}{1+M} \left[\frac{\partial u}{\partial x''} \cos(\theta'' - \epsilon'') + u \sin(\theta'' - \epsilon'') \frac{\partial \epsilon''}{\partial x''} \right] \quad (2-236)$$

$$\begin{aligned} \frac{\partial G}{\partial x''} = & \left(1 + \frac{N_\theta}{1+M} \right)^{-1} \left[\frac{\partial U}{\partial x''} \cos \phi - \frac{N_\theta}{1+M} \left\{ \frac{\partial u}{\partial x''} \cos(\theta'' - \epsilon'') \right. \right. \\ & \left. \left. + u \sin(\theta'' - \epsilon'') \frac{\partial \epsilon''}{\partial x''} \right\} + N_\gamma \left(\frac{\partial v}{\partial x''} + \frac{\partial u_\gamma}{\partial x''} \right) \right] \quad (2-237) \end{aligned}$$

where

$$M = \frac{u \sin(\theta'' - \epsilon'') \tan \theta''}{G + u_m} \quad (2-238)$$

$$N_\theta = \frac{U \sin \phi \tan \theta''}{G + u_m} \quad (2-239)$$

$$N_\gamma = \frac{U \sin \phi \tan \gamma''}{v + u_p} \quad (2-240)$$

$$u_m = u \cos(\theta'' - \epsilon'') \quad (2-241)$$

The y'' -derivatives can be stated as

$$\frac{\partial u_m}{\partial y''} = \frac{M_\gamma}{1 - M_\gamma} \frac{\partial G}{\partial y''} + \frac{1}{1 - M_\gamma} \left[u \sin(\theta'' - \epsilon'') \frac{\partial \epsilon''}{\partial y''} \right] \quad (2-242)$$

$$\begin{aligned} \frac{\partial G}{\partial y''} = & \left(1 - \frac{J_\theta}{1 - M_\gamma} \right)^{-1} \left[\frac{\partial U}{\partial y''} \cos \phi + \frac{J_\theta}{1 - M_\gamma} \left\{ u \sin(\theta'' - \epsilon'') \frac{\partial \epsilon''}{\partial y''} \right\} \right. \\ & \left. - J_\gamma \left(\frac{\partial v}{\partial y''} + \frac{\partial u_p}{\partial y''} \right) \right] \quad (2-243) \end{aligned}$$

where

$$M_y = \frac{u \sin(\theta'' - \epsilon'') \cot \theta''}{G + u_m} \quad (2-244)$$

$$J_\theta = \frac{U \sin \phi \cot \theta''}{G + u_m} \quad (2-245)$$

$$J_\gamma = \frac{U \sin \phi \cot \gamma''}{v + u_g} \quad (2-246)$$

The second x'' -derivatives are determined to be

$$\frac{\partial^2 u_m}{(\partial x'')^2} = - \frac{M}{1+M} \frac{\partial^2 G}{(\partial x'')^2} + G_2 \quad (2-247)$$

$$\begin{aligned} \frac{\partial^2 G}{(\partial x'')^2} = & \left(1 + \frac{N_\theta}{1+M}\right)^{-1} \left[\frac{\partial^2 U}{(\partial x'')^2} \cos \phi - \frac{\partial \phi}{\partial x''} \left(2 \frac{\partial U}{\partial x''} \sin \phi \right. \right. \\ & \left. \left. + G \frac{\partial \phi}{\partial x''} \right) - N_\theta G_2 - U \sin \phi \tan \theta'' \left(\frac{\partial \theta''}{\partial x''} \right)^2 \right. \\ & \left. + N_\gamma \left(\frac{\partial^2 v}{(\partial x'')^2} + \frac{\partial^2 u_g}{(\partial x'')^2} \right) + U \sin \phi \tan \gamma'' \left(\frac{\partial \gamma''}{\partial x''} \right)^2 \right] \quad (2-248) \end{aligned}$$

where

$$G_2 = \frac{1}{1+M} \left[\frac{\partial^2 u}{(\partial X''')^2} \cos(\theta'' - \epsilon'') - 2 \frac{\partial u}{\partial X''} \sin(\theta'' - \epsilon'') \left(\frac{\partial \theta''}{\partial X''} - \frac{\partial \epsilon''}{\partial X''} \right) \right. \\ \left. - u \cos(\theta'' - \epsilon'') \left(\frac{\partial \theta''}{\partial X''} - \frac{\partial \epsilon''}{\partial X''} \right)^2 + u \sin(\theta'' - \epsilon'') \left\{ -\tan \theta'' \left(\frac{\partial \theta''}{\partial X''} \right)^2 \right. \right. \\ \left. \left. + \frac{\partial^2 \epsilon''}{(\partial X''')^2} \right\} \right] \quad (2-249)$$

$$\frac{\partial \theta''}{\partial X''} = \frac{\tan \theta''}{G + u_m} \left(\frac{\partial G}{\partial X''} + \frac{\partial u_m}{\partial X''} \right) \quad (2-250)$$

$$\frac{\partial \phi}{\partial X''} = \frac{\partial \theta''}{\partial X''} - \frac{\partial \gamma''}{\partial X''} \quad (2-251)$$

The second derivatives with respect to y'' are

$$\frac{\partial^2 u_m}{(\partial y''')^2} = \frac{M_\gamma}{1-M_\gamma} \frac{\partial^2 G}{(\partial y''')^2} + G_3 \quad (2-252)$$

$$\frac{\partial^2 G}{(\partial y''')^2} = \left(1 - \frac{J_\theta}{1-M_\gamma} \right)^{-1} \left[\frac{\partial^2 U}{(\partial y''')^2} \cos \phi - \frac{\partial \phi}{\partial y''} \left(2 \frac{\partial U}{\partial y''} \sin \phi \right. \right. \\ \left. \left. + G \frac{\partial \phi}{\partial y''} \right) + J_\theta G_3 + U \sin \phi \cot \theta'' \left(\frac{\partial \theta''}{\partial y''} \right)^2 \right. \\ \left. - J_\gamma \left(\frac{\partial^2 v}{(\partial y''')^2} + \frac{\partial^2 u_\gamma}{(\partial y''')^2} \right) - U \sin \phi \cot \gamma'' \left(\frac{\partial \gamma''}{\partial y''} \right)^2 \right] \quad (2-253)$$

where

$$G_3 = \frac{1}{1 - M_y} \left[\frac{\partial^2 u}{(\partial y'')^2} \cos(\theta'' - \epsilon'') - u \cos(\theta'' - \epsilon'') \left(\frac{\partial \theta''}{\partial y''} - \frac{\partial \epsilon''}{\partial y''} \right)^2 \right. \\ \left. + u \sin(\theta'' - \epsilon'') \left\{ \cot \theta'' \left(\frac{\partial \theta''}{\partial y''} \right)^2 + \frac{\partial \epsilon''}{(\partial y'')^2} \right\} \right] \quad (2-254)$$

$$\frac{\partial \theta''}{\partial y''} = - \frac{\cot \theta''}{G + u_m} \left(\frac{\partial G}{\partial y''} + \frac{\partial u_m}{\partial y''} \right) \quad (2-255)$$

$$\frac{\partial \phi}{\partial y''} = \frac{\partial \theta''}{\partial y''} - \frac{\partial \gamma''}{\partial y''} \quad (2-256)$$

The mixed derivatives can be stated as

$$\frac{\partial^2 u_m}{\partial x'' \partial y''} = - \frac{M_{xy}}{1 + M_{xy}} \frac{\partial^2 G}{\partial x'' \partial y''} + G_4 \quad (2-257)$$

$$\frac{\partial^2 G}{\partial x'' \partial y''} = \left(1 + \frac{N_\theta}{1 + M_{xy}} \right)^{-1} \left[\frac{\partial^2 U}{\partial x'' \partial y''} \cos \phi - \frac{\partial \phi}{\partial y''} \left(\frac{\partial U}{\partial x''} \sin \phi \right. \right. \\ \left. \left. + G \frac{\partial \phi}{\partial x''} \right) - \frac{\partial U}{\partial y''} \sin \phi \frac{\partial \phi}{\partial x''} - N_\theta G_4 - U \sin \phi \frac{\partial \theta''}{\partial x''} \frac{\partial \theta''}{\partial y''} (\cot \theta'' \right. \\ \left. + 2 \tan \theta'' \right) + N_\gamma \left(\frac{\partial^2 v}{\partial x'' \partial y''} + \frac{\partial^2 u_z}{\partial x'' \partial y''} \right) \\ \left. + U \sin \phi \frac{\partial \gamma''}{\partial x''} \frac{\partial \gamma''}{\partial y''} (\cot \gamma'' + 2 \tan \gamma'') \right] \quad (2-258)$$

where

$$G_4 = \frac{1}{1 + M_{xy}} \left[\frac{\partial^2 u}{\partial x'' \partial y''} \cos(\theta'' - \epsilon'') - \left(\frac{\partial \theta''}{\partial y''} - \frac{\partial \epsilon''}{\partial y''} \right) \left\{ \frac{\partial u}{\partial x''} \sin(\theta'' - \epsilon'') \right. \right. \\ \left. \left. + u \cos(\theta'' - \epsilon'') \left(\frac{\partial \theta''}{\partial x''} - \frac{\partial \epsilon''}{\partial x''} \right) \right\} \right] \quad (2-259)$$

$$+ u \cos(\theta'' - \epsilon'') \left\{ - \frac{\partial \theta''}{\partial x''} \frac{\partial \theta''}{\partial y''} (\cot \theta'' + 2 \tan \theta'') + \frac{\partial^2 \epsilon''}{\partial x'' \partial y''} \right\} \quad (2-260)$$

$$M_{xy} = \frac{u \cos(\theta'' - \epsilon'') \tan \theta''}{G + u_m}$$

2.8 Summary of Basic Equations. In the $x'y'$ - and $x''y''$ -coordinate systems, Equation (2-24) for the ray curvature of the wave packet becomes

$$K_G = \frac{1}{G + u_m} \left[\left\{ \sin \theta' \frac{\partial G}{\partial x'} \right\}_r - \left\{ \sin \theta'' \left(\frac{\partial G}{\partial x''} + \frac{\partial u_m}{\partial x''} \right) \right. \right. \\ \left. \left. - \cos \theta'' \left(\frac{\partial G}{\partial y''} + \frac{\partial u_m}{\partial y''} \right) \right\}_\omega \right] \quad (2-261)$$

Equation (2-25), which defines the ratio of the incremental distances of the wave packets and rays, is applied separately to the calculations accounting for water depth and current variations.

Equation (2-27) for the change in wavelet direction becomes

$$\Delta \gamma = \left[\left\{ \cos \rho' \tan \gamma' \frac{\partial v}{\partial x'} \right\}_r + \left\{ \cos \rho'' \left(\tan \gamma'' \left(\frac{\partial v}{\partial x''} + \frac{\partial u_g}{\partial x''} \right) \right. \right. \right. \\ \left. \left. \left. - \left(\frac{\partial v}{\partial y''} + \frac{\partial u_g}{\partial y''} \right) \right) \right\}_\omega \right] \frac{G_r \Delta t}{v + u_g} \quad (2-262)$$

When the wavelet direction is computed using Snell's law, the $x'y'$ -coordinate system is the natural system to use for variations in water depth, and the $x''y''$ -coordinate system is used for changes due to currents. Snell's law is stated in Equations (2-28) and (2-29). The Doppler shifted frequency, due to a current, is defined by Equation (2-13).

The wave height is given by Equation (2-54). The shoaling coefficient is defined by Equation (2-51), whereas the friction coefficient is defined by Equations (2-98), (2-99), and (2-56). The refraction coefficient is

determined as a function of β using Equation (2-58). The ray separation factor β is determined by solving Equation (2-59) where

$$p = -2 \left[\left\{ \cos \theta' \frac{\partial G}{\partial x'} \right\}_h + \left\{ \cos \theta'' \left(\frac{\partial G}{\partial x''} + \frac{\partial u_m}{\partial x''} \right) + \sin \theta'' \left(\frac{\partial G}{\partial y''} + \frac{\partial u_m}{\partial y''} \right) \right\}_w \right] \quad (2-263)$$

$$q = G_T \left[\left\{ \sin^2 \theta' \frac{\partial^2 G}{(\partial x')^2} - 2 \sin \theta' \cos \theta' \frac{\partial^2 G}{\partial x' \partial y'} + \cos^2 \theta' \frac{\partial^2 G}{(\partial y')^2} \right\}_h \right. \\ \left. + \left\{ \sin^2 \theta'' \left(\frac{\partial^2 G}{(\partial x'')^2} + \frac{\partial^2 u_m}{(\partial x'')^2} \right) - 2 \sin \theta'' \cos \theta'' \left(\frac{\partial^2 G}{\partial x'' \partial y''} + \frac{\partial^2 u_m}{\partial x'' \partial y''} \right) \right. \right. \\ \left. \left. + \cos^2 \theta'' \left(\frac{\partial^2 G}{(\partial y'')^2} + \frac{\partial^2 u_m}{(\partial y'')^2} \right) \right\}_w \right] \quad (2-264)$$

In the $x'y'$ -coordinate system $\partial h / \partial y' = 0$. As a result the first partial derivatives of the wave speeds with respect to y' vanish, and there is a simplification in the second derivatives involving y' . In the $x''y''$ -coordinate system $\partial u / \partial y'' = 0$. This results in a simplification of all the derivatives involving y'' . However, the first partial derivatives of the speeds do not vanish unless $\partial \epsilon' / \partial y'' = 0$.

CHAPTER III THE COMPUTER PROGRAM

3.1 Introduction to the Computer Program. Including the arrays the computer program requires approximately 580,000 bytes of storage. Of this amount, the arrays CMAT, CURX, CURY, AX, and AY occupy about 187,000 bytes of storage.

The input and output directions of the wave packets, wavelets, and currents are defined as the directions from which the waves and currents come with respect to true north. Before making calculations these angles are transformed using the following relationships

$$\theta_C = \text{CNVRS}A - \theta_N + 180 \quad (3-1)$$

$$\gamma_C = \text{CNVRS}A - \gamma_N + 180 \quad (3-2)$$

$$\varepsilon_C = \text{CNVRS}A - \varepsilon_N + 180 \quad (3-3)$$

where the subscript C refers to the calculation coordinate system, the subscript N denotes the true north coordinate system, and CNVRS A is the direction of the positive x-axis of the grids with respect to true north. The angles are in degrees.

The program listing contains information on the input and output devices used in running the program. All the input and output parameters are defined. A description is given of the subroutine structure. Notes are provided on the plotting software which is used. The use of double precision in the calculations is discussed. Numerous comments are included to explain the operation of the program.

3.2 Listing of the Computer Program.

001 PROGRAM WAUPAK
002 C
003 C THIS IS A PROGRAM FOR CALCULATING AND PLOTTING THE PATHS OF SURFACE
004 C GRAVITY WATER WAVE PACKETS AND FOR CALCULATING THE WAVE HEIGHTS ALONG
005 C THESE PATHS CONSIDERING WATER DEPTHS AND CURRENTS. THE EFFECTS OF
006 C SHOALING, REFRACTION, AND ENERGY DISSIPATION ARE ACCOUNTED FOR.
007 C
008 C THE PROGRAM WAS COMPLETED SEPTEMBER 1982 UNDER A CONTRACT WITH THE
009 C COASTAL SCIENCES PROGRAM, OFFICE OF NAVAL RESEARCH. THE PROGRAM WAS
010 C PREPARED BY
011 C
012 C J. ERNEST BREEDING, JR
013 C SHELLEY KAY HORTON
014 C DEPARTMENT OF OCEANOGRAPHY AND OCEAN ENGINEERING
015 C
016 C MICHAEL C. NEWELL
017 C INTERACTIVE COMPUTING FACILITY
018 C
019 C FLORIDA INSTITUTE OF TECHNOLOGY
020 C MELBOURNE, FL 32901
021 C USA
022 C
023 C THIS PROGRAM IS BASED ON A PROGRAM FOR COMPUTING THE PATHS OF MONOCHROMATIC
024 C RAYS DUE TO VARIATIONS IN WATER DEPTH BY
025 C
026 C W. STANLEY WILSON, 'A METHOD FOR CALCULATING AND PLOTTING SURFACE
027 C WAVE RAYS,' TECHNICAL MEMORANDUM NO. 17, COASTAL ENGINEERING
028 C RESEARCH CENTER, 57 PP. (1966) (AD-636-771).
029 C
030 C WITH THE EXCEPTION OF THE PLOTTING SUBROUTINES, THE WILSON PROGRAM WAS
031 C EXTENSIVELY MODIFIED IN ORDER TO COMPUTE THE PATH OF A WAVE PACKET AND
032 C TO COMPUTE THE WAVE HEIGHT.
033 C
034 C COPIES OF THIS PROGRAM MAY BE OBTAINED ON 9-TRACK, 800 OR 1600 BPI ASCII
035 C ENCODED TAPES BY SENDING A BLANK TAPE TO THE AUTHORS.
036 C
037 C
038 C I/O UNIT NUMBERS
039 C
040 C UNIT 1 CONTROL DATA FILE (INPUT)
041 C
042 C UNIT 2 WATER DEPTH GRID FILE (INPUT)
043 C
044 C UNIT 3 CURRENT SPEED GRID FILE (INPUT)
045 C
046 C UNIT 5 TERMINAL INPUT (USED ONLY BY SUBROUTINE IOSET)
047 C
048 C UNIT 6 PRINT FILE (OUTPUT)

049 C
050 C UNIT 9 PLOT FILE (OUTPUT)
051 C
052 C INPUT PARAMETERS
053 C
054 C A IS THE INITIAL DIRECTION FROM WHICH THE WAVE PACKET
055 C COMES WITH RESPECT TO TRUE NORTH.
056 C
057 C AKRTOL DETERMINES THE ACCURACY IN CALCULATING THE REFRACTION
058 C COEFFICIENT.
059 C
060 C AV IS THE INITIAL DIRECTION FROM WHICH THE WAVELETS COME
061 C WITH RESPECT TO TRUE NORTH.
062 C
063 C CCON IS A FACTOR TO CONVERT THE CURRENTS IN CURX AND CURY TO
064 C FEET/SECOND OR METERS/SECOND.
065 C
066 C CF IS THE FRICTION FACTOR FOR THE FRICTION COEFFICIENT.
067 C
068 C CIN IF CIN IS NOT ZERO IT IS THE TRAVEL TIME IN SECONDS
069 C BETWEEN SUCCESSIVE TICK MARKS ON A RAY.
070 C
071 C CHAT IS THE WATER DEPTH GRID.
072 C
073 C CNURSA IS THE DIRECTION OF THE POSITIVE X-AXIS OF THE WATER
074 C DEPTH AND CURRENT GRIDS WITH RESPECT TO TRUE NORTH.
075 C
076 C CONTURC SPECIFIES THE SOUNDING CURRENTS IN FEET/SECOND OR
077 C METERS/SECOND.
078 C
079 C CONTURD SPECIFIES THE SOUNDING DEPTHS IN FEET OR METERS.
080 C
081 C CURX IS THE X-COMPONENT CURRENT GRID.
082 C
083 C CURY IS THE Y-COMPONENT CURRENT GRID.
084 C
085 C DATE1,
086 C DATE2 DEFINE THE YEAR, MONTH, AND DAY.
087 C
088 C DCON IS A FACTOR TO CONVERT THE WATER DEPTHS IN CHAT
089 C TO FEET OR METERS.
090 C
091 C DELTAT IS THE TIME STEP IN SECONDS.
092 C
093 C DEP IS THE WATER DEPTH IN FEET OR METERS IF THERE IS
094 C NO WATER DEPTH GRID.
095 C
096 C DIR IS A COMPUTER RUN IDENTIFIER.
097 C
098 C GRID IS THE NUMBER OF FEET OR METERS PER GRID UNIT.
099 C
100 C HGTZ IS THE INITIAL WAVE HEIGHT IN FEET OR METERS.
101 C

102 C HT IS THE HEIGHT OF THE PLOT IN INCHES OR CENTIMETERS.
103 C
104 C MM IS THE MAXIMUM X FOR THE WATER DEPTH AND CURRENT
105 C GRIDS.
106 C
107 C MOE IS THE UNITS SPECIFIER
108 C = 0 => ENGLISH UNITS
109 C = 1 => METRIC UNITS
110 C
111 C MXPLOT IS THE NUMBER OF PLOTS OR COMPUTER RUNS.
112 C
113 C NAX IS THE PLOT AXES CALIBRATE FLAG
114 C = 0 => DO NOT CALIBRATE AXES
115 C = 1 => CALIBRATE AXES
116 C
117 C NC IS THE CURRENT GRID FLAG
118 C = 0 => THERE IS NO CURRENT GRID
119 C = 1 => THERE IS A CURRENT GRID
120 C
121 C NCC IF NONZERO, IT IS THE NUMBER OF SOUNDING CURRENT
122 C VALUES FOR A PLOT.
123 C
124 C NCO IF NONZERO, IT IS THE NUMBER OF SOUNDING WATER DEPTH
125 C VALUES FOR A PLOT.
126 C
127 C ND IS THE WATER DEPTH GRID FLAG
128 C = 0 => THERE IS NO WATER DEPTH GRID
129 C = 1 => THERE IS A WATER DEPTH GRID
130 C
131 C NFAN IS THE RAY NUMBER FLAG
132 C = 0 => RAYS ARE NUMBERED AT THEIR INITIAL POINTS
133 C = 1 => RAYS ARE NUMBERED AT THEIR TERMINAL POINTS
134 C
135 C NN IS THE MAXIMUM Y FOR THE WATER DEPTH AND CURRENT
136 C GRIDS.
137 C
138 C NNSKIP IS THE AMOUNT ADDED TO THE Y-COLUMN IN SELECTING THE
139 C NEXT COLUMN FOR LOCATING SOUNDING VALUES.
140 C
141 C NOR IS THE NUMBER OF RAYS FOR A GIVEN RUN.
142 C
143 C NPT IS THE FLAG FOR OPTIONAL RAY OUTPUT
144 C = 0 => OPTIONAL RAY PARTICULARS ARE NOT PRINTED
145 C = 1 => OPTIONAL RAY PARTICULARS ARE PRINTED
146 C
147 C NROPT IS THE REFLECTION POINT CONTINUATION FLAG
148 C = 0 => RAY IS NOT CONTINUED BEYOND REFLECTION POINT
149 C = 1 => RAY IS CONTINUED BEYOND REFLECTION POINT
150 C
151 C NSH IS THE SHORELINE FLAG
152 C = 0 => SHORELINE IS NOT DRAWN
153 C = 1 => SHORELINE IS DRAWN
154 C

155 C NSK DETERMINES THE FREQUENCY OF PRINTED OUTPUT. OUTPUT
 156 C OCCURS FOR THOSE VALUES OF MAX WHICH ARE AN INTEGRAL
 157 C MULTIPLE OF NSK.
 158 C
 159 C NWBRK IS THE WAVE BREAK TEST FLAG
 160 C = 0 => WAVE BREAK TEST IS MADE
 161 C = 1 => WAVE BREAK TEST IS NOT MADE
 162 C
 163 C NXCHAT IS THE GRID READ FLAG
 164 C = 0 => READ NEW GRID(S)
 165 C = 1 => USE GRID(S) FROM PREVIOUS PLOT
 166 C
 167 C PROJECT IS A COMPUTER RUN IDENTIFIER.
 168 C
 169 C TT IS THE INPUT WAVELET PERIOD IN SECONDS.
 170 C
 171 C X,Y ARE THE INITIAL RAY COORDINATES.
 172 C
 173 C Z IS THE CURRENT SPEED IN FEET/SECOND OR METERS/
 174 C SECOND IF THERE ARE NO CURRENT GRIDS.
 175 C
 176 C ZD IS THE INITIAL DIRECTION FROM WHICH THE CURRENT COMES
 177 C WITH RESPECT TO TRUE NORTH IF THERE ARE NO CURRENT
 178 C GRIDS.
 179 C
 180 C OUTPUT RAY PARTICULARS
 181 C
 182 C CUR:DI IS THE DIRECTION FROM WHICH THE CURRENT COMES WITH
 183 C RESPECT TO TRUE NORTH.
 184 C
 185 C CUR:SP IS THE CURRENT SPEED IN FEET/SECOND OR METERS/SECOND.
 186 C
 187 C DEPTH IS THE WATER DEPTH IN FEET OR METERS.
 188 C
 189 C G=U *
 190 C COS(PACK-WAVE) IS THE GEOMETRIC GROUP SPEED IN FEET/SECOND
 191 C OR METERS/SECOND RELATIVE TO THE CURRENT.
 192 C
 193 C GR IS THE RAY SPEED IN FEET/SECOND OR METERS/SECOND.
 194 C
 195 C HGT IS THE WAVE HEIGHT IN FEET OR METERS.
 196 C
 197 C KF IS THE FRICTION COEFFICIENT.
 198 C
 199 C KR IS THE REFRACTION COEFFICIENT.
 200 C
 201 C KS IS THE SHOALING COEFFICIENT.
 202 C
 203 C MAX IS AN INDEX TO NUMBER POINTS ALONG A RAY.
 204 C
 205 C PACK IS THE DIRECTION FROM WHICH THE WAVE PACKET COMES WITH
 206 C RESPECT TO TRUE NORTH.
 207 C

208 C PERIOD IS THE WAVELET PERIOD IN SECONDS RELATIVE TO THE
209 C CURRENT.
210 C
211 C RAY IS THE DIRECTION FROM WHICH THE RAY COMES WITH RESPECT
212 C TO TRUE NORTH.
213 C
214 C WAVE IS THE DIRECTION FROM WHICH THE WAVELETS (IN A PACKET)
215 C COME WITH RESPECT TO TRUE NORTH.
216 C
217 C X,Y ARE THE COORDINATES OF A RAY POINT.
218 C
219 C ADDITIONAL OUTPUT IF NPT IS NOT ZERO
220 C
221 C BETA IS THE RAY SEPARATION FACTOR.
222 C
223 C BRK UP IS THE TYPE OF TIME STEP BREAKUP IF ONE OCCURS. IF THE
224 C BREAKUP OCCURS IN ORDER TO MAINTAIN ACCURACY IN THE
225 C REFRACTION CALCULATIONS, 'BETA' APPEARS IN THE
226 C PRINTOUT. IF A TIME STEP BREAKUP IS REQUIRED TO KEEP
227 C THE CHANGE IN 'PACK' TO LESS THAN ONE DEGREE BETWEEN
228 C SUCCESSIVE RAY POINTS NEAR A REFLECTION POINT,
229 C 'REFLECT' APPEARS IN THE PRINTOUT.
230 C
231 C CURVATURE IS THE RAY CURVATURE OF THE PACKET IN RADIANS/GRID
232 C UNIT.
233 C
234 C DBETA/DT IS THE TIME DERIVATIVE OF BETA.
235 C
236 C GT IS THE SPEED OF THE ADVECTED GROUP FRONT IN
237 C FEET/SECOND OR METERS/SECOND RELATIVE TO THE
238 C CURRENT.
239 C
240 C NO IS THE NUMBER OF INTERVALS THE INPUT TIME STEP IS
241 C DIVIDED INTO.
242 C
243 C PCT:CX IS THE MAXIMUM PERCENTAGE DIFFERENCE FOR THE X-
244 C COMPONENT CURRENT GRID. SEE EXPLANATION TO PCT:D.
245 C
246 C PCT:CY IS THE MAXIMUM PERCENTAGE DIFFERENCE FOR THE Y-
247 C COMPONENT CURRENT GRID. SEE EXPLANATION TO PCT:D.
248 C
249 C PCT:D IS THE MAXIMUM OF THE PERCENTAGE DIFFERENCES AT THE 4
250 C GRID POINTS CLOSEST TO THE RAY POINT OF THE SURFACE
251 C FIT DERIVED WATER DEPTH RELATIVE TO THE ACTUAL DEPTH.
252 C
253 C ROTAT:C IS THE ANGLE OF THE ROTATED XY-SYSTEM (WHERE THE Y-
254 C DERIVATIVES ARE SIMPLIFIED) RELATIVE TO THE CURRENT
255 C GRID XY-SYSTEM.
256 C
257 C ROTAT:D IS THE ANGLE OF THE ROTATED XY-SYSTEM (WHERE THE FIRST
258 C Y-DERIVATIVES VANISH) RELATIVE TO THE WATER DEPTH
259 C GRID XY-SYSTEM.
260 C

261 C	U	IS THE CONVENTIONAL GROUP SPEED IN FEET/SECOND OR METERS/SECOND RELATIVE TO THE CURRENT.
262 C		
263 C		
264 C	V	IS THE PHASE SPEED IN FEET/SECOND OR METERS/SECOND RELATIVE TO THE CURRENT.
265 C		
266 C		
267 C	VT	IS THE SPEED OF THE ADVECTED WAVELET FRONT IN FEET/SECOND OR METERS/SECOND RELATIVE TO THE CURRENT.
268 C		
269 C		
270 C		

271 C
272 C SUBROUTINE STRUCTURE

273 C			
274 C	WAUPAK		MAINLINE PROGRAM
275 C			
276 C		IOSET	SET UP I/O UNITS
277 C			
278 C		NUMCON	PLOT SOUNDING DEPTHS
279 C		NUMBER	CALCOMP ROUTINE TO PLOT NUMBERS
280 C		PLOT	CALCOMP ROUTINE TO PLOT SYMBOLS
281 C			
282 C		NUMCON2	PLOT CURRENT SPEED CONTURS
283 C		NUMBER	CALCOMP ROUTINE TO PLOT NUMBERS
284 C		PLOT	CALCOMP ROUTINE TO PLOT POINTS
285 C			
286 C		PLOT	CALCOMP ROUTINE TO PLOT POINTS
287 C			
288 C		PLOTS	CALCOMP ROUTINE TO INITIALIZE PLOTTER
289 C			
290 C		PRTPRM	PRINT OUT INPUT PARAMETERS
291 C			
292 C		RAYN	CONTROL RAY CALCULATIONS AND PRINTOUT
293 C		ANGCON	CONVERT ANGLES FOR PRINTOUT
294 C		DRAW	DRAW A RAY PATH AND TICK MARKS
295 C		NUMBER	CALCOMP ROUTINE TO DRAW NUMBERS
296 C		PLOT	CALCOMP ROUTINE TO PLOT POINTS
297 C		HEIGHT	COMPUTE WAVE HEIGHT
298 C		MOVE	MOVE PACKET ALONG PATH
299 C		ANGCON	CONVERT ANGLES FOR PRINTOUT
300 C		HEIGHT	COMPUTE WAVE HEIGHT
301 C		PAGCOL	PRINT PAGE AND COLUMN HEADINGS
302 C		SURFCE	COMPUTE WAVE PARTICULARS
303 C		VELCTY	COMPUTE WAVE SPEEDS
304 C		PAGCOL	PRINT PAGE AND COLUMN HEADINGS
305 C		PCD	COMPUTE PERCENT DIFFERENCES
306 C		STORE	STORE DATA ON CURRENT POINT
307 C		SURFCE	COMPUTE WAVE PARTICULARS
308 C		VELCTY	COMPUTE WAVE SPEEDS
309 C			
310 C		SHORE	PLOT IN THE SHORELINE IF REQUIRED

311 C	PLOT	CALCOMP ROUTINE TO PLOT POINTS
312 C		
313 C	TITLE	TITLE AND BORDER THE PLOT
314 C	AXIS2	PLOT AXES
315 C	NUMBER	CALCOMP ROUTINE TO PLOT NUMBERS
316 C	PLOT	CALCOMP ROUTINE TO PLOT POINTS
317 C	SYMBOL	CALCOMP ROUTINE TO PLOT SYMBOLS
318 C	NUMBER	CALCOMP ROUTINE TO PLOT NUMBERS
319 C	PLOT	CALCOMP ROUTINE TO PLOT POINTS
320 C	SYMBOL	CALCOMP ROUTINE TO PLOT SYMBOLS

321 C
322 C NOTES
323 C

324 C THIS PROGRAM USES THE CALCOMP HCBS (HOST COMPUTER BASIC SOFTWARE) TO
325 C PERFORM ALL PLOTTING. USERS SHOULD NOTE THAT THIS SOFTWARE VARIES
326 C SLIGHTLY FROM VERSION TO VERSION; IN ADDITION, MANY SITES HAVE
327 C MODIFIED THIS PACKAGE LOCALLY TO SUIT PARTICULAR NEEDS.

328 C
329 C DOUBLE PRECISION HAS BEEN USED IN THIS PROGRAM TO OBTAIN REQUIRED
330 C ACCURACY ON THE VAX 11/780 AND IBM 370 COMPUTERS. USERS OF CDC CYBER
331 C COMPUTERS AND THE LIKE, WHICH USE EXTENDED PRECISION BY DEFAULT,
332 C SHOULD NOT REQUIRE DOUBLE PRECISION.

333 C
334 C THIS PROGRAM HAS BEEN EXTENSIVELY MODIFIED ON A VAX 11/780 USING A
335 C FORTRAN 77 COMPILER. EVERY EFFORT HAS BEEN MADE TO USE ANSI 1966
336 C STANDARD FORTRAN CONSTRUCTS. THE ONLY VAX SPECIFIC SUBROUTINE
337 C IS 'IOSET'; SEE THE COMMENTS IN THAT ROUTINE FOR MORE SPECIFICS.
338 C

339 IMPLICIT REAL*8 (A-H,O-Z)

340 C
341 DIMENSION CONTURD(9),CONTURC(9),EM(6,12),S(6,6)
342 DIMENSION C(12),CX(12),CY(12),E(6),EX(6),EY(6)

343 C
344 C VARIOUS GRIDS NEEDED FOR VARIOUS ROUTINES

345 C
346 COMMON /GRDCOM/ CHAT(120,120), CURX(120,120), CURY(120,120),
347 1 CURR(120,120), AX(4500), AY(4500)

348 C
349 C COMMON BLOCK PRTCOM IS USED BY SUBROUTINE PRTPRM

350 C
351 COMMON /PRTCOM/ HT, MXPLOT, NOR, NPT, NAX, NSH, NCO, NCC, NXCHAT,
352 1 MM, NN, NNSKIP

353 C
354 C MAICOM IS USED BY ALL ROUTINES

355 C
356 COMMON /MAICOM/ ALFA, AMM, ANN, CF, CIN, CNVRS, CONTURD, DATE1, DATE2,
357 1 DCON, DELTAT, DIR, DY, EM, GRID, HGTZ, AKRTOL, PROJECT,
358 2 S, SDLTAT, NSK, TT, NWBRK, NBRKUP, NFAN, NFLAGR,
359 3 NOLINE, IFLG, MOE, NFLECT, NFRACT, NRFLBU, NRFRBU, NROPT

360 C


```

361 C          RAYCOM IS USED BY ALL ROUTINES REQUIRING RAY DATA
362 C
363 COMMON /RAYCOM/ BDZ,C,CX,CY,D,DELA,DEP,DGDX,DHDX,E,EX,EY,G,GZERO,
364 1          HGT,AKFC,AKR,AKS,POT,PREV,P1,P2,P3,P4,P5,QOT,Q1,
365 2          Q2,Q3,Q4,Q5,PU,SVU,PDEP,SPREV,GTZERO,
366 3          PALFA,SVAV,PG,U,V,IHGT,
367 4          NTOREF,INUM,MAXQ,NUMT,NOREF
368 C
369 C          SRFCOM IS USED BY ALL ROUTINES PERFORMING SURFACE FUNCTIONS
370 C
371 COMMON /SRFCOM/ ND,NC,CCON,TTT,ARRAY,GR,GT,SARAY,PZ,PZD,
372 1          CALFA,PCALFA,PARAY,PREVT,SPREVT,VT,SVT,ASV,
373 2          Z,ZD,BZ,KMAX,PX,PY,PTTT,PANGLE,PGR,PPCTD,PPCTCX,
374 3          PPCTCY,PGT,SVBZ,SVBDZ,KNUMT,KRFLBU,KRFRBU,CDGDX,
375 4          UMX,AGR,PGAM,PBZ,PBDZ,PFK,PV,PVT
376 C
377 C          NUMCOM IS USED BY NUMCON
378 C
379 COMMON /NUMCOM/ CONTURC
380 C
381 C          SET UP THE INPUT FILES AND INITIALIZE THE CALCOMP PLOTTER
382 C
383 CALL IOSET
384 CALL PLOTS(0.0,0.0,9)
385 C
386 C          DEFINE SOME CONSTANTS
387 C
388 MMAX=4500
389 LI=50
390 C
391 C          READ THE FIRST CONTROL CARD
392 C
393 READ (1,3) MXPLOT,PROJECT,DATE1,DATE2,DIR
394 C
395 C          LOOP OVER THE PLOT SETS
396 C
397 DO 399 NPLOT=1,MXPLOT
398 READ (1,4) NOR,NPT,NSK,HT,CIN,NAX,NSH,NCO,NCC,MNSKIP,NXCHAT,MOE
399 READ (1,5) MM,NN,CNURSA,GRID,DCON,DEP,ND,CCON,Z,ZD,NC
400 C
401 C          THE INPUT DIRECTIONS ARE TRANSFORMED TO THE COMPUTATIONAL
402 C          COORDINATES AND TO RADIANS
403 C
404 ZD=CNURSA-ZD+180.D0
405 ZD=ZD*1.74532925D-2
406 C
407 C          SELECT ACCELERATION DUE TO GRAVITY
408 C
409 IF (MOE .EQ. 0) GO TO 23
410 AGR=9.8D0
411 C
412 C          CONVERT TO ENGLISH UNITS FOR PLOT CALCULATIONS
413 C

```

```

414      HT=HT/2.54D0
415      GRIDPLT=GRID/0.3048D0
416      GO TO 22
417 23    AGR=32.2D0
418      GRIDPLT=GRID
419 C
420 C          CONVERT CIN FROM SECONDS TO HOURS
421 C
422 22    CIN=CIN/3600.D0
423      AMM=MM-1.D0
424      ANN=NN-1.D0
425      DY=ANN/HT
426      SCLI=GRIDPLT*DY*12.
427      CALL TITLE (NPLOT,MAX,SCLI,HT)
428 C
429 C          READ THE WATER DEPTH GRID, IF ANY
430 C
431      IF (ND .EQ. 0) GO TO 25
432      IF (NXCHAT .NE. 0) GO TO 3939
433      READ (2,11) ((CHAT(J,I),I=1,MM),J=1,NN)
434 C
435 C          READ THE CONTURD CARD IF ANY, THEN PLOT SOUNDING DEPTH
436 C          CONTOURS REQUESTED
437 C
438 3939  IF (NCO .LE. 0) GO TO 493
439      READ (1,495) (CONTURD(I),I=1,NCO)
440      CALL NUMCON
441 C
442 C          PLOT THE SHORELINE IF REQUESTED
443 C
444 493  IF (NSH .EQ. 0) GO TO 393
445      CALL SHORE
446 C
447 C          READ THE CURRENT GRID, IF ANY
448 C
449 393  IF (NC .EQ. 0) GO TO 3937
450 25  IF (NXCHAT .NE. 0) GO TO 3949
451      READ(3,11) ((CURY(J,I),I=1,MM),J=1,NN)
452      READ(3,11) ((CURX(J,I),I=1,MM),J=1,NN)
453 C
454 C          COMPUTE MAGNITUDE OF CURRENT
455 C
456      DO 50 J=1,NN
457          DO 51 I=1,MM
458              CURR(J,I)=DSQRT(CURX(J,I)**2+CURY(J,I)**2)
459 51      CONTINUE
460 50      CONTINUE
461 C
462 C          READ THE CONTURC CARD IF ANY, THEN PLOT CURRENT
463 C          PROFILES REQUESTED
464 C
465 3949  IF (NCC .LE. 0) GO TO 3937
466      READ(1,495) (CONTURC(I),I=1,NCC)

```

```
467      CALL NUMCON2
468 C
469 C          PRINT SYSTEM PARTICULARS
470 C
471 3937     CALL PRTPRM(NPLOT)
472 C
473 C          LOOP OVER THE RAYS OF THIS SET
474 C
475     DO 15 N=1,NOR
476         READ(1,6) DELTAT,TT,X,Y,A,AV,HGTZ,CF,AKRTOL,NROPT,NWBRK,NFAN
477 C
478 C          SET AND/OR COMPUTE INITIAL VALUES
479 C
480         TTT=TT
481         SDLTAT=DELTAT
482         A=CNVRS-A+180.D0
483         A=A*1.74532925D-2
484         AV=CNVRS-AV+180.D0
485         AV=AV*1.74532925D-2
486         MAXQ=1
487         NOLINE=0
488         NBRKUP=0
489         NFLECT=0
490         NRFLBU=0
491         NFRACT=0
492         NRFRBU=0
493         NFLAGR=0
494         IFLG=0
495         ALFA=0.0D0
496         CALFA=0.D0
497         SVAU=AV
498         ASV=A
499         ARAY=A
500 C
501 C          PERFORM CALCULATIONS FOR THIS RAY
502 C
503         CALL RAYN(X,Y,A,NPLOT,N,MKAX,LI,AV)
504 15     CONTINUE
505 C
506 C          RE-ORIGIN THE PLOTTER FOR THIS PLOT
507 C
508         CALL PLOT (-3.,-.4,-3)
509 C
510 C          THEN CONTINUE WITH THE NEXT PLOT
511 C
512 399     CONTINUE
513 C
514 C          CLOSE OUT THE PLOTTER, THEN WRITE TERMINATION RECORD AND END
515 C
516         CALL PLOT(0,0,999)
517         WRITE (6,999*)
518         CALL EXIT
519 C
```

```

520 C          FORMAT SECTION
521 C
522 3          FORMAT(I2,1X,3(A6,1X),A6)
523 4          FORMAT(3(2X,I3),5X,2(F8.3,2X),7(2X,I3))
524 5          FORMAT(2(2X,I3),1X,F7.3,2(1X,F9.3),1X,F7.2,1X,I3,1X,F9.5,1X,
525 1          F7.2,1X,F6.2,1X,I3)
526 6          FORMAT(7(F6.2,2X),2(F6.4,2X),3(I1,1X))
527 11         FORMAT(16F5.0)
528 495        FORMAT(9F8.2)
529 9999       FORMAT(1H1,17H THIS IS THE END.)
530           END

```

```

001          SUBROUTINE TITLE (NPLOT,NAX,SCLI,HT)

```

```

002 C

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003 C          PURPOSE

```

```

004 C

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005 C          THIS SUBROUTINE LABELS THE PLOT AND ADDS THE STRAIGHT LINE
006 C          BORDERS.

```

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007 C

```

```

008 C          SUBROUTINES REQUIRED

```

```

009 C

```

```

010 C          AXIS2          SUBROUTINE FOR DRAWING AXES
011 C          SYMBOL         CALCOMP ROUTINE FOR DRAWING VARIOUS SYMBOLS
012 C          NUMBER        CALCOMP ROUTINE FOR DRAWING NUMBERS
013 C          PLOT          CALCOMP ROUTINE FOR DRAWING POINTS AND LINES
014 C

```

```

015          IMPLICIT REAL*8 (A-H,O-Z)

```

```

016          DIMENSION CONTURD(9),EM(6,12),S(6,6)

```

```

017          COMMON /MAICOM/ ALFA,AMM,ANN,CF,CIN,CNURSA,CONTURD,DATE1,DATE2,

```

```

018 1          DCON,DELTAT,DIR,DY,EM,GRID,HGTZ,AKRTOL,PROJECT,

```

```

019 2          S,SDLTAT,NSK,TT,NWBRK,NBRKUP,NFAN,NFLAGR,

```

```

020 3          NOLINE,IFLG,MOE,NFLECT,NFRACT,NRFLBU,NRFRBU,NROPT

```

```

021 C

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```

022 C          MOVE THE PLOT AXIS, AND DEFINE SOME CONSTANTS

```

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023 C

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```

024          CALL PLOT(3.,0.4,3)

```

```

025          RT=AMM/DY

```

```

026          XNPLOT=NPLOT

```

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027 C

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028 C          DRAW IN THE PLOT TITLE LABELS

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029 C

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```

030          CALL SYMBOL(1.25,0.4,.2,17HPROJ. NO.          ,90.,17)

```

```

031          CALL SYMBOL(1.25,2.4,.2,PROJECT,90.,6)

```

```

032          CALL SYMBOL(1.25,4.0,.2,DATE1,90.,6)

```

```

033          CALL SYMBOL(1.25,5.2,.2,DATE2,90.,2)

```

```

034          CALL SYMBOL(1.50,0.4,.2,23HSCL = 1/          , CIN =,90.,23)

```

```

035          CALL NUMBER(1.50,2.0,.2,SCLI,90.,-1)

```

```

036          CALL NUMBER(1.50,5.2,.2,CIN*3600.,90.,-1)

```

```

037          CALL SYMBOL(1.75,0.4,.2,19H PLOT NO.          , DIR. =,90.,19)

```

```

038          CALL NUMBER(1.75,2.2,.2,XNPLOT,90.,-1)

```

```

039          CALL SYMBOL(1.75,4.4,.2,DIR,90.,6)

```

```

040 C
041 C           CHECK AXIS TYPE
042 C
043           IF (NAX .NE. 0) GO TO 705
044 C
045 C           DRAW STRAIGHT-LINE BORDERS FOR THE PLOT
046 C
047           CALL PLOT(3.,0.4,3)
048           CALL PLOT(3.,HT+.4,2)
049           GO TO 706
050 C
051 C           DRAW FULL LABELED AXES
052 C
053 705       CALL AXIS2(3.,0.4,1HY,1,HT,90.,0.,DY)
054           CALL AXIS2(3.,.4,1HX,-1,RT,0.,0.,DY)
055           CALL PLOT(3.,HT+.4,3)
056 C
057 C           DRAW IN OUTER BOX LIMITS
058 C
059 706       CALL PLOT(RT+3.,HT+.4,2)
060           CALL PLOT(RT+3.,.4,2)
061 C
062 C           THEN RE-ORIGIN IN CORRECT POSITION
063 C
064           IF (NAX .EQ. 0) CALL PLOT(3.,0.4,2)
065           CALL PLOT(3.,0.4,-3)
066           YHT=HT
067           RETURN
068           END

```

```

001       SUBROUTINE AXIS2(X,Y,BCD,NC,SIZE,THETA,YMIN,DY)
002 C
003 C           PURPOSE
004 C
005 C           THIS ROUTINE DRAWS, CALIBRATES, AND LABELS THE AXES
006 C           FOR THE PLOT.
007 C
008 C           SUBROUTINES REQUIRED
009 C
010 C           NUMBER           CALCOMP ROUTINE FOR PLOTTING NUMBERS
011 C           PLOT             CALCOMP ROUTINE FOR MOVING THE PEN
012 C           SYMBOL           CALCOMP ROUTINE FOR PLOTTING SYMBOLS
013 C
014       IMPLICIT REAL*8 (A-H,O-Z)
015 C
016 C           INITIALIZE VARIOUS CONSTANTS
017 C
018       BIGN=1.0D0
019 C
020 C           IF THERE ARE NO CHARACTERS FOR THE AXIS, THERE IS NO NEED
021 C           TO RE-ORIGIN

```

```

022 C
023     IF (NC .GE. 0) GO TO 2
024     BIGN=-1.0D0
025 2   NAC=IABS(NC)
026     TH=THETA*1.74532925D-2
027     N=DY*SIZE+0.5D0
028     CTH=DCOS(TH)
029     STH=DSIN(TH)
030     TN=N
031     XB=X
032     YB=Y
033     XA=X-0.1D0*BIGN*STH
034     YA=Y+0.1D0*BIGN*CTH
035 C
036 C           DRAW AXIS WITH CALIBRATED TICK MARKS
037 C
038     CALL PLOT(XA,YA,3)
039     DO 20 I=1,N
040         CALL PLOT(XB,YB,2)
041         XC=XB+CTH/DY
042         YC=YB+STH/DY
043         CALL PLOT(XC,YC,2)
044         XA=XA+CTH/DY
045         YA=YA+STH/DY
046         CALL PLOT(XA,YA,2)
047         XB=XC
048         YB=YC
049 20    CONTINUE
050     IBSV=YMIN+TN
051     XA=XB-(.20D0*BIGN-.05D0)*STH-.02857D0*CTH
052     YA=YB+(.20D0*BIGN-.05D0)*CTH-.02857D0*STH
053     N=N+1
054 C
055 C           NUMBER THE ORIGIN AND EVERY TENTH TICK MARK
056 C
057     DO 30 I=1,N
058         IF (MOD(IBSV,10).EQ. 0)
059 1       CALL NUMBER(XA,YA,.1,FLOAT(IBSV),THETA,-1)
060         IBSV=IBSV-1
061         XA=XA-CTH/DY
062         YA=YA-STH/DY
063 30    CONTINUE
064 C
065 C           LABEL THE AXIS
066 C
067     TNC=NAC+7
068     XA=X+(SIZE/2.0-.06*TNC)*CTH-(-.07+BIGN*.36)*STH
069     YA=Y+(SIZE/2.0-.06*TNC)*STH+(-.07+BIGN*.36)*CTH
070     CALL SYMBOL(XA,YA,.14,BCD,THETA,NAC)
071     RETURN
072     END

```

```

001      SUBROUTINE NUMCON
002 C
003 C          PURPOSE
004 C
005 C          THIS ROUTINE LOCATES AND DRAWS IN THE SPECIFIED SOUNDING
006 C          DEPTHS.
007 C
008 C          SUBROUTINES REQUIRED
009 C
010 C              NUMBER          CALCOMP ROUTINE TO DRAW NUMBERS
011 C              PLOT            CALCOMP ROUTINE TO MOVE THE PEN
012 C
013      IMPLICIT REAL*8 (A-H,O-Z)
014 C
015      DIMENSION CONTURD(9),EM(6,12),S(6,6)
016 C
017      COMMON /MAICOM/ ALFA,AMM,ANN,CF,CIN,CNURSA,CONTURD,DATE1,DATE2,
018 1          DCON,DELTAT,DIR,DY,EM,GRID,HGTZ,AKRTOL,PROJECT,
019 2          S,SDLTAT,NSK,TT,NWBRK,NBRKUP,NFAN,NFLAGR,
020 3          NOLINE,IFLG,MOE,NFLECT,NFRACT,NRFLBU,NRFRBU,NROPT
021 C
022      COMMON /GRDCOM/ CHAT(120,120), CURX(120,120), CURY(120,120),
023 1          CURR(120,120), AX(4500), AY(4500)
024 C
025      COMMON /PRTCOM/ HT,MXPLOT,NOR,NPT,NAX,NSH,NCO,NCC,NXCHAT,
026 1          MM,NN,NNSKIP
027 C
028 C          DEFINE SOME USEFUL CONSTANTS
029 C
030      MOD=NN-1
031      MODD=MM-1
032 C
033 C          SELECT Y-COLUMN STARTING WITH THE SECOND Y-COLUMN
034 C
035      DO 5000 J=2, MOD, NNSKIP
036          YJ=J-1
037          KKK=1
038 C
039 C          SELECT SOUNDING DEPTH
040 C
041      DO 8000 KC=1,NCO
042          KWIT=0
043          NDIF=3
044          I=MM-1
045 C
046 C          SEARCH COLUMN FOR THE GIVEN SOUNDING DEPTH BEGINNING ONE
047 C          GRID UNIT FROM THE END OF THE COLUMN
048 C
049      DO 1011 II=1,MODD
050          XI=I-1
051          IL=I+1
052          XL=IL-1
053 C

```

```

054 C          CHECK FOR CONTOUR REACHING THE SHORELINE
055 C
056           IF (KWIT .GT. 0) GO TO 8000
057           IF (CHAT(J,I) .GT. 0) GO TO 20
058           KWIT=1
059 C
060 C          LOCATE OURSELVES WITH RESPECT TO THE CONTOUR
061 C
062 20         IF (CHAT(J,I)*DCON-CONTURD(KC)) 12,11,13
063 C
064 C          THE CONTOUR FELL ON A GRID POINT
065 C
066 11         AX(KKK)=XI
067           AY(KKK)=CONTURD(KC)
068           KKK=KKK+1
069           NDIF=3
070           GO TO 1010
071 C
072 C          WE HAVE NOT YET REACHED THE PROPER REGION
073 C
074 12         GO TO (14,77,14),NDIF
075 14         NDIF=1
076           GO TO 1010
077 13         GO TO (77,15,15),NDIF
078 15         NDIF=2
079           GO TO 1010
080 C
081 C          THE CONTOUR IS WITHIN THIS GRID ELEMENT.  LINEARLY
082 C          INTERPOLATE FOR THE SOUNDING DEPTH
083 C
084 77         SLPX=(DCON*(CHAT(J,IL)-CHAT(J,I)))/(XL-XI)
085           XP=(CONTURD(KC)-DCON*CHAT(J,I))/SLPX+XI
086           AX(KKK)=XP
087           AY(KKK)=CONTURD(KC)
088           KKK=KKK+1
089           GO TO (81,82),NDIF
090 81         NDIF=2
091           GO TO 1010
092 82         NDIF=1
093 1010        I = I - 1
094 1011        CONTINUE
095 8000        CONTINUE
096 C
097 C          DRAW OUT SOUNDING DEPTHS FOR EACH SELECTED Y-COLUMN
098 C
099           KKK=KKK-1
100           IF (KKK-1) 5000,668,670
101 670        KKL=KKK-1
102           DO 998 IA=1,KKL
103             IAD=IA+1
104           DO 997 IB=IAD,KKK
105             IF (AX(IA) .LE. AX(IB)) GO TO 997
106           XMIN=AX(IA)

```



```

107          AX(IA)=AX(IB)
108          AX(IB)=XMIN
109          XMIN=AY(IA)
110          AY(IA)=AY(IB)
111          AY(IB)=XMIN
112 997      CONTINUE
113 998      CONTINUE
114 668      IF (MOD(J,2) .NE. 0) GO TO 104
115          KONE=KKK
116          KADD=-1
117          LAST=1
118          GO TO 105
119 104      KONE=1
120          KADD=1
121          LAST=KKK
122 C
123 C          NUMBER THE CONTOUR
124 C
125 105      CALL NUMBER(AX(KONE)/DY,YJ/DY,0.10,AY(KONE),0.0,-1)
126          CALL SYMBOL(999.0,999.0,0.10,'D',0.0,1)
127          IF (KONE .EQ. LAST) GO TO 5000
128          KONE=KONE+KADD
129          GO TO 105
130 5000     CONTINUE
131 C
132 C          RE-ORIGIN THE PLOTTER AND EXIT
133 C
134          CALL PLOT(0.,0.,-3)
135          RETURN
136          END

```

```

001      SUBROUTINE NUMCON2
002 C
003 C          PURPOSE
004 C
005 C          THIS ROUTINE LOCATES AND DRAWS IN THE CURRENT SPEED
006 C          CONTOURS.
007 C
008 C          SUBROUTINES REQUIRED
009 C
010 C          NUMBER          CALCOMP ROUTINE FOR PLOTTING NUMBERS
011 C          PLOT            CALCOMP ROUTINE FOR MOVING THE PEN
012 C
013 C
014      IMPLICIT REAL*8 (A-H,O-Z)
015 C
016      DIMENSION CONTURD(9),CONTURC(9),EM(6,12),S(6,6),C(12),CX(12)
017      DIMENSION CY(12),E(6),EX(6),EY(6)
018 C
019      COMMON /GRDCOM/ CHAT(120,120), CURX(120,120), CURY(120,120),
020      1          CURR(120,120), AX(4500), AY(4500)

```

```

021 C
022     COMMON /PRTCOM/ HT,MXPLOT,NOR,NPT,NAX,NSH,NCO,NCC,NXCMAT,
023     1             MM,NN,NNSKIP
024 C
025     COMMON /HAICOM/ ALFA,AMM,ANN,CF,CIN,CNVRSA,CONTURD,DATE1,DATE2,
026     1             DCON,DELTAT,DIR,DY,EM,GRID,HGTZ,AKRTOL,PROJCT,
027     2             S,SDLTAT,NSK,TT,NWBRK,NBRKUP,NFAN,NFLAGR,
028     3             NOLINE,IFLG:MOE,NFLECT,NFRACT,NRFLBU,NRFRBU,NROPT
029 C
030     COMMON /RAYCOM/ BDZ,C,CX,CY,D,DELA,DEP,DGDY,DHDX,E,EX,EY,G,GZERO,
031     1             HGT,AKFC,AKR,AKS,POT,PREV,P1,P2,P3,P4,P5,QOT,Q1,
032     2             Q2,Q3,Q4,Q5,PU,SUV,PDEP,SPREV,GTZERO,
033     3             PALFA,SVAU,PG,U,V,IHGT,
034     4             NTOREF,INUM,MAXQ,NUMT,NOREF
035 C
036     COMMON /SRFCOM/ ND,NC,CCON,TTT,ARAY,GR,GT,SARAY,PZ,PZD,
037     1             CALFA,PCALFA,PARAY,PREVT,SPREVT,VT,SVT,ASU,
038     2             Z,ZD,BZ,KMAX,PX,PY,PTTT,PANGLE,PGR,PPCTD,PPCTCX,
039     3             PPCTCY,PGT,SUBZ,SUBDZ,KNUMT,KRFLBU,KRFRBU,CDGDY,
040     4             UMX,AGR,PGAM,PBZ,PBDZ,PFK,PV,PVT
041 C
042     COMMON /NUMCOM/ CONTURC
043 C
044 C             DEFINE SOME USEFUL CONSTANTS
045 C
046     NOD=NN-1
047     MODD=MM-1
048 C
049 C             SELECT Y-COLUMN STARTING WITH THE FOURTH Y-COLUMN
050 C
051     DO 5000 J=4, NOD, NNSKIP
052         YJ=J-1
053         KKK=1
054 C
055 C             SELECT CURRENT SPEED CONTOUR
056 C
057     DO 8000 KC=1,NCC
058         NDIF=3
059         I=MM-1
060 C
061 C             SEARCH COLUMN FOR THE GIVEN CURRENT SPEED CONTOUR BEGINNING
062 C             ONE GRID UNIT FROM THE END OF THE COLUMN
063 C
064     DO 1011 II=1,MODD
065         XI=I-1
066         IL=I+1
067         XL=IL-1
068 C
069 C             FIGURE OUT WHERE WE ARE IN RESPECT TO THE CONTOUR
070 C             LINE
071 C
072     20         IF (CURR(J,I)*CCON-CONTURC(KC)) 12,11,13
073 C

```

```

074 C          THE CONTOUR FELL ON A GRID POINT
075 C
076 11          AX(KKK)=XI
077            AY(KKK)=CONTURC(KC)
078            KKK=KKK+1
079            NDIF=3
080            GO TO 1010
081 12          GO TO (14,77,14),NDIF
082 14          NDIF=1
083            GO TO 1010
084 13          GO TO (77,15,15),NDIF
085 15          NDIF=2
086            GO TO 1010
087 C
088 C          THE CONTOUR FELL WITHIN THE CURRENT GRID ELEMENT.
089 C          LINEARLY INTERPOLATE FOR THE CURRENT SPEED CONTOUR
090 C
091 77          SLPX=(CCON*(CURR(J,IL)-CURR(J,I)))/(XL-XI)
092            XP=(CONTURC(KC)-CCON*CURR(J,I))/SLPX+XI
093            AX(KKK)=XP
094            AY(KKK)=CONTURC(KC)
095            KKK=KKK+1
096            GO TO (81,82),NDIF
097 81          NDIF=2
098            GO TO 1010
099 82          NDIF=1
100 1010        I=I-1
101 1011        CONTINUE
102 8000        CONTINUE
103 C
104 C          DRAW THE SPEED CONTOURS FOR EACH OF THE SELECTED Y-COLUMNS
105 C
106            KKK=KKK-1
107            IF (KKK-1) 5000,668,670
108 670        KKL=KKK-1
109            DO 998 IA=1,KKL
110              IAD=IA+1
111              DO 997 IB=IAD,KKK
112                IF (AX(IA) .LE. AX(IB)) GO TO 997
113                XMIN=AX(IA)
114                AX(IA)=AX(IB)
115                AX(IB)=XMIN
116                XMIN=AY(IA)
117                AY(IA)=AY(IB)
118                AY(IB)=XMIN
119 997          CONTINUE
120 998          CONTINUE
121 668          IF (MOD(J,2) .NE. 0) GO TO 104
122            KONE=KKK
123            KADD=-1
124            LAST=1
125            GO TO 105
126 104        KONE=1

```

```

127      KADD=1
128      LAST=KKK
129 C
130 C          NUMBER THE CONTOUR
131 C
132 105     CALL NUMBER(AX(KONE)/DY,YJ/DY,0.10,AY(KONE),0.0,2)
133     CALL SYMBOL(999.0,999.0,0.10,'C',0.0,1)
134     IF (KONE .EQ. LAST) GO TO 5000
135     KONE=KONE+KADD
136     GO TO 105
137 5000    CONTINUE
138 C
139 C          RESET THE PLOTTER ORIGIN AND EXIT
140 C
141     CALL PLOT(0.,0.,-3)
142     RETURN
143     END

```

```

001      SUBROUTINE SHORE
002 C
003 C          PURPOSE
004 C
005 C          THIS ROUTINE IS CALLED TO DRAW IN THE SHORELINE.
006 C
007 C          SUBROUTINES REQUIRED
008 C
009 C          PLOT          CALCOMP ROUTINE TO MOVE THE PEN
010 C
011     IMPLICIT REAL*8 (A-H,O-Z)
012 C
013     DIMENSION CONTURD(9),EM(6,12),S(6,6)
014 C
015     COMMON /GRDCOM/ CHAT(120,120), CURX(120,120), CURY(120,120),
016 1          CURR(120,120), AX(4500), AY(4500)
017 C
018     COMMON /PRTCOM/ HT,MXPLOT,NOR,NPT,NAX,NSH,NCO,NCC,NXCHAT,
019 1          MM,NN,MNSKIP
020 C
021     COMMON /MAICOM/ ALFA,AMM,ANN,CF,CIN,CNURSA,CONTURD,DATE1,DATE2,
022 1          DCON,DELTAT,DIR,DY,EM,GRID,HGTZ,AKRTOL,PROJECT,
023 2          S,SDLTAT,NSK,TT,NWBRK,NBRKUP,NFAN,NFLAGR,
024 3          NOLINE,IFLG,MOE,NFLECT,NFRACT,NRFLBU,NRFRBU,NROPT
025 C
026 C          INLINE FUNCTION TO LINEARLY INTERPOLATE OVER 2 POINTS
027 C
028     PONT(X1,X2,D1,D2)=X1-D1*((X1-X2)/(D1-D2))
029     IC=3
030 C
031 C          SELECT Y-COLUMN
032 C
033     DO 1 J=1,NN

```

```

034      YJ=J-1
035      JL=J-1
036      YL=JL-1
037      I=MM
038 C
039 C          SEARCH COLUMN FOR ZERO WATER DEPTH STARTING WITH MAXIMUM X
040 C
041      DO 3 II=1,MM
042          XI=I-1
043          IL=I+1
044          XL=IL-1
045 C
046 C          FIND OURSELVES WITH RESPECT TO THE SHORELINE
047 C          (CHAT < 0 => POINT IS ON LAND)
048 C
049      IF (CHAT(J,I)) 100,200,300
050 C
051 C          WE ARE ON LAND
052 C
053 100      IF (IC .GT. 2) GO TO 102
054 C
055 C          INTERPOLATE FOR ZERO WATER DEPTH
056 C
057 101      XP=PONT(XI,XL,CHAT(J,I),CHAT(J,IL))
058          CALL PLOT(XP/DY,YJ/DY,IC)
059          IC=2
060          GO TO 1
061 102      IF (J .LE. 1) GO TO 101
062          YP=PONT(YJ,YL,CHAT(J,1),CHAT(JL,1))
063          CALL PLOT (0.0,YP/DY,IC)
064          IC=2
065          XP=PONT(XI,XL,CHAT(J,I),CHAT(J,IL))
066          CALL PLOT(XP/DY,YJ/DY,IC)
067          GO TO 1
068 C
069 C          WE ARE EXACTLY ON THE SHORELINE
070 C
071 200      IF (II .NE. MM) GO TO 201
072          CALL PLOT(XI/DY,YJ/DY,IC)
073          IF (IC .GT. 2) GO TO 204
074          IC=3
075          GO TO 1
076 204      IC=2
077          GO TO 1
078 201      IF (IC .LE. 2) GO TO 207
079          IF (J .LE. 1) GO TO 207
080          YP=PONT(YJ,YL,CHAT(J,1),CHAT(JL,1))
081          CALL PLOT (0.0,YP/DY,IC)
082          IC=2
083 207      CALL PLOT(XI/DY,YJ/DY,IC)
084          IC=2
085          GO TO 1
086 C

```

```

087 C           WE ARE STILL OFF SHORE; KEEP LOOKING FOR LAND
088 C
089 300        IF (II .NE. MM) GO TO 2
090           IF (IC .GT. 2) GO TO 1
091           YP=PONT(YJ,YL,CHAT(J,1),CHAT(JL,1))
092           CALL PLOT (0.0,YP/DY,IC)
093           IC=3
094           GO TO 1
095 2          I=I-1
096 3          CONTINUE
097 1          CONTINUE
098 C
099 C           RE-ORIGIN THE PLOTTER AND EXIT
100 C
101           CALL PLOT(0.,0.,-3)
102           RETURN
103           END

```

```

001           SUBROUTINE RAYN(X,Y,A,NPLOT,N,MMAX,LI,AV)

```

```

002 C

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```

003 C           PURPOSE

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004 C

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005 C

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006 C

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007 C

```

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008 C

```

```

009 C

```

```

SUBROUTINES REQUIRED

```

```

010 C

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```

011 C

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```

012 C

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013 C

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014 C

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015 C

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016 C

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017 C

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018 C

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019 C

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020

```

```

IMPLICIT REAL*8 (A-H,O-Z)

```

```

021 C

```

```

022

```

```

DIMENSION CONTURD(9),EM(6,12),S(6,6)

```

```

023

```

```

DIMENSION C(12),CX(12),CY(12),E(6),EX(6),EY(6)

```

```

024 C

```

```

025

```

```

COMMON /GRDCOM/ CHAT(120,120), CURX(120,120), CURY(120,120),

```

```

026

```

```

1 CURR(120,120), AX(4500), AY(4500)

```

```

027 C

```

```

028

```

```

COMMON /PRTCOM/ HT,MXPLOT,NOR,NPT,NAX,NSH,NCO,NCC,NXCHAT,

```

```

029

```

```

1 MM,NN,NNSKIP

```

```

030 C

```

```

031

```

```

COMMON /MAICOM/ ALFA,AMH,ANN,CF,CIN,CHURSA,CONTURD,DATE1,DATE2,

```

```

032

```

```

1 DCON,DELTAT,DIR,DY,EM,GRID,HGTZ,AKRTOL,PROJECT,

```

```

034      3          NOLINE,IFLG,MOE,NFLECT,NFRACT,NRFLBU,NRFRBU,NROPT
035 C
036      COMMON /RAYCOM/ BDZ,C,CX,CY,D,DELA,DEP,DGDX,IHDX,E,EX,EY,G,GZERO,
037      1          HGT,AKFC,AKR,AKS,POT,PREV,P1,P2,P3,P4,P5,QOT,Q1,
038      2          Q2,Q3,Q4,Q5,PU,SVV,PDEP,SPREV,GTZERO,
039      3          PALFA,SVAU,PG,U,V,IHGT,
040      4          NTOREF,INUM,MAXQ,NUMT,NOREF
041 C
042      COMMON /SRFCOM/ ND,NC,CCON,TTT,ARAY,GR,GT,SARAY,PZ,PZD,
043      1          CALFA,PCALFA,PARAY,PREVT,SPREVT,VT,SVT,ASU,
044      2          Z,ZD,BZ,KMAX,PX,PY,PTTT,PANGLE,PGR,PPCTD,PPCTCX,
045      3          PPCTCY,PGT,SVBZ,SVBDZ,KNUMT,KRFLBU,KRFRBU,CDGDX,
046      4          UMX,AGR,PGAM,PBZ,PBDZ,PFK,PV,PVT
047 C
048 C          SET INITIAL VALUES FOR THIS RAY
049 C
050      NDP=1
051      NFK=1
052      NGO=1
053      KREST=0
054      KCIN=0
055      NOREF=0
056      BZ=1.D0
057      BDZ=0.D0
058      IHGT=1
059 C
060 C          CALL SURFCE, MOVE, AND HEIGHT TO DETERMINE VALUES AT
061 C          THE FIRST RAY POINT
062 C
063      CALL SURFCE(X,Y,A,FK,NFK,NDP,IWAVIT,AV)
064      IHGT=0
065 C
066 C          SET INITIAL VALUES FOR THIS RAY
067 C
068      INUM=0
069      PALFA=ALFA
070      SVV=V
071      PREV=SVV
072      SVT=VT
073      GZERO=G
074      GTZERO=GT
075      TIMEQ=0.
076 C
077 C          COMPUTE VALUES AT THE INITIAL RAY POINT
078 C
079      CALL MOVE(X,Y,A,FK,NGO,MIT,NFK,NDP,AV,LI)
080      CALL HEIGHT(X,Y,A,FK,NGO,MIT,NFK,NDP,AV)
081      GO TO 160
082 C
083 C          CHECK FOR AX, AY ARRAY LIMITS EXCEEDED
084 C
085      3      MAXQ=1+MAXQ
086      IF (MAXQ+KCIN .LT. MMAX) GO TO 399

```

```
087      WRITE (6,401)
088      GO TO 190
089  399  SAVEGR=GR
090 C
091 C          DETERMINE NEXT RAY POINT
092 C
093      CALL MOVE(X,Y,A,FK,NGO,MIT,NFK,NDP,AV,LI)
094      IF (NDP .EQ. 1) GO TO 396
095 C
096 C          RAY REACHED SHORE
097 C
098  402  WRITE (6,403)
099      MAXQ=MAXQ-1
100      GO TO 190
101 C
102 C          CHECK RETURNED STATUS
103 C
104  396  GO TO (397,397,404,514,515,1900,516,528),MIT
105 C
106 C          PACKET CURVATURE ITERATION NOT CONVERGING
107 C
108  404  WRITE (6,405)
109      GO TO 571
110 C
111 C          A CAUSTIC OR FOCAL POINT ENCOUNTERED
112 C
113  514  WRITE (6,504)
114      GO TO 571
115 C
116 C          THE WAVE BROKE
117 C
118  515  WRITE (6,505)
119      GO TO 571
120 C
121 C          SOME SORT OF REFLECTION HANGUP ENCOUNTERED
122 C
123  516  WRITE (6,517)
124      GO TO 571
125 C
126 C          BREAKUP TIME STEP WAS LESS THAN 0.5 SECONDS
127 C
128  528  WRITE (6,529)
129  571  MAXQ=MAXQ-1
130      GO TO 190
131 C
132 C          COMPUTE TRAVEL TIME ALONG THE RAY
133 C
134  397  TIMEQ=TIMEQ+(D*GRID/(1800.*(GR+SAVEGR)))
135  160  IF (ND .NE. 0) CALL PCD(C,E,PCTD)
136      IF (NC .EQ. 0) GO TO 614
137      CALL PCD(CX,EX,PCTCX)
138      CALL PCD(CY,EY,PCTCY)
139  614  IF (MAXQ .EQ. 1 .OR. MOD(MAXQ,NSK) .EQ. 0) GO TO 3041
```



```

140      GO TO 161
141 C
142 C          WRITE RAY PARTICULARS FOR SELECTED RAY POINTS
143 C
144 3041  ANGLE=A
145      CALL ANGCON(ANGLE,CNURSA)
146      GAM=AV
147      CALL ANGCON(GAM,CNURSA)
148      ARAY1=ARAY
149      CALL ANGCON(ARAY1,CNURSA)
150      ZDP=ZD
151      CALL ANGCON(ZDP,CNURSA)
152      IF (MOD(NOLINE,LI) .EQ. 0) CALL PAGCOL(NPLOT,N)
153      NOLINE=NOLINE+1
154      WRITE (6,612) (MAXQ,X,Y,DEP,Z,ZDP,TTT,ARAY1,
155 1      ANGLE,GAM,G,GR,HGT,AKS,AKFC,AKR)
156      IF (NPT .EQ. 0) GO TO 161
157      ALFAP=ALFA/1.74532925D-2
158      CALFAP=CALFA/1.74532925D-2
159      IF (MOD(NOLINE,LI) .EQ. 0) CALL PAGCOL(NPLOT,N)
160      NOLINE=NOLINE+1
161      WRITE(6,615) ALFAP,PCTD,CALFAP,PCTCX,PCTCY,GT,
162 1      U,V,VT,BZ,BDZ,NUMT,FK
163      IF (NUMT .LE. 1) GO TO 161
164      IF (NRFLBU .EQ. 0) GO TO 616
165      WRITE(6,617)
166 616  IF (NRFRBU .EQ. 0) GO TO 161
167      WRITE(6,618)
168 C
169 C          SAVE PRINTOUT VALUES
170 C
171 161  KRFLBU=NRFLBU
172      KRFRBU=NRFRBU
173      NRFLBU=0
174      NRFRBU=0
175      KMAX=MAXQ
176      PX=X
177      PY=Y
178      PDEP=DEP
179      PZ=Z
180      PZD=ZD
181      PTTT=TTT
182      PARAY=ARAY
183      PANGLE=A
184      PGAM=AV
185      PGR=GR
186      PG=G
187      PHGT=HGT
188      PKS=AKS
189      PKFC=AKFC
190      PKR=AKR
191      PALFA=ALFA
192      IF (NPT .EQ. 0) GO TO 613

```

```

193      PPCTD=PCTD
194      PCALFA=CALFA
195      PPCTCX=PCTCX
196      PPCTCY=PCTCY
197      PGT=GT
198      PU=U
199      PV=V
200      PVT=VT
201      PBZ=BZ
202      PBDZ=BDZ
203      KNUMT=NUMT
204      PFK=FK
205 C
206 C          STORE THE CURRENT RAY POSITION FOR LATER PLOTTING
207 C
208 613      CALL STORE(X,Y,A,KMAX,TIMEQ,KCIN,KREST)
209          IF (MIT .EQ. 1) GO TO 10
210          IF (MOD(NOLINE,LI) .EQ. 0) CALL PAGCOL(NPLOT,N)
211          NOLINE=NOLINE+1
212 C
213 C          PACKET CURVATURE WAS AVERAGED
214 C
215          WRITE (6,9) MAXQ
216 10      IF (MAXQ .GT. 1) GO TO 13
217          GO TO (3,402),NDP
218 13      IF (NGO .EQ. 1) GO TO 3
219 C
220 C          RAY REACHED GRID BOUNDRY
221 C
222          WRITE (6,407)
223 190     IF (MAXQ .LE. 1 .OR. MOD(MAXQ,NSK) .EQ. 0) GO TO 1900
224 C
225 C          WRITE RAY PARTICULARS FOR THE LAST POINT
226 C
227          CALL ANGCON (PANGLE,CNVRSA)
228          CALL ANGCON (PGAM,CNVRSA)
229          CALL ANGCON (PARAY,CNVRSA)
230          CALL ANGCON (PZD,CNVRSA)
231          IF (MOD(NOLINE,LI) .EQ. 0) CALL PAGCOL(NPLOT,N)
232          NOLINE=NOLINE+1
233          WRITE (6,612) KMAX,PX,PY,PDEP,PZ,PZD,PTTT,PARAY,PANGLE,PGAM,PG,
234 1          PGR,PHGT,PKS,PKFC,PKR
235          IF (NPT .EQ. 0) GO TO 1900
236          PALFA=PALFA/1.74532925D-2
237          PCALFA=PCALFA/1.74532925D-2
238          IF (MOD(NOLINE,LI) .EQ. 0) CALL PAGCOL(NPLOT,N)
239          WRITE(6,615) (PALFA,PPCTD,PCALFA,PPCTCX,PPCTCY,PGT,
240 1          PU,PV,PVT,PBZ,PBDZ,KNUMT,PFK)
241          IF (KNUMT .LE. 1) GO TO 1900
242          IF (KRFLBU .EQ. 0) GO TO 619
243          WRITE(6,617)
244 619     IF (KRFRBU .EQ. 0) GO TO 1900
245          WRITE(6,618)

```

```

246 C
247 C           DRAW THE RAY PATH
248 C
249 1900 CALL DRAW(N,KMAX,KCIN,KREST)
250 RETURN
251 401 FORMAT(80X,35HDIMENSION OF OUTPUT-ARRAYS EXCEEDED)
252 403 FORMAT(80X,17HRAY REACHED SHORE)
253 405 FORMAT(80X,41HPACKET CURVATURE ITERATION NOT CONVERGING)
254 504 FORMAT(80X,22HCAUSTIC OR FOCAL POINT)
255 505 FORMAT(80X,11HWAVE BREAKS)
256 517 FORMAT(80X,18HREFLECTION HANG-UP)
257 529 FORMAT(80X,38HBREAKUP TIME STEP LESS THAN 0.5 SECOND)
258 612 FORMAT(1X,I5,2F8.2,2(F9.2,F9.4),3F8.2,2F7.2,4F9.4)
259 615 FORMAT(2X,0PF9.2,F8.2,0PF9.2,2F8.2,4F7.2,F8.4,1X,1PE10.3,9X,I5,
260 1 1X,1PE10.3)
261 617 FORMAT(1H+,93X,7HREFLECT)
262 618 FORMAT(1H+,96X,4HBETA)
263 9 FORMAT(80X,4HMAX=,I4,27H, PACKET CURVATURE AVERAGED)
264 407 FORMAT(80X,25HRAY REACHED GRID BOUNDARY)
265 END

```

```

266 SUBROUTINE ANGCON(ANG,CNURSA)
267 C
268 C PURPOSE
269 C
270 C THIS ROUTINE DEFINES ANGLES WITH RESPECT TO TRUE NORTH
271 C AND PLACES THEM IN THE RANGE 0 TO 360 DEGREES FOR PRINTOUT.
272 C
273 C SUBROUTINES REQUIRED
274 C
275 C NONE
276 C
277 C IMPLICIT REAL*8 (A-H,O-Z)
278 C
279 C CONVERT THE ANGLE
280 C
281 C ANG=ANG/1.74532925D-2
282 C ANG=CNURSA-ANG+180.DO
283 C
284 C FORCE IT INTO 0 -> 360 DEGREES
285 C
286 51 IF (ANG .GE. 0.DO) GO TO 50
287 C ANG=ANG+360.DO
288 C GO TO 51
289 50 IF (ANG .LT. 360.DO) GO TO 52
290 C ANG=ANG-360.DO
291 C GO TO 50
292 C
293 C THEN EXIT
294 C
295 52 RETURN

```

```

296      END

297      SUBROUTINE PAGCOL(NPLOT,N)
298 C
299 C      PURPOSE
300 C
301 C          THIS ROUTINE PRINTS THE PAGE AND COLUMN HEADINGS AT THE
302 C          TOP OF A NEW PAGE.
303 C
304 C      SUBROUTINES REQUIRED
305 C
306 C          NONE
307 C
308      IMPLICIT REAL*8 (A-H,O-Z)
309 C
310      DIMENSION CONTURD(9),EM(6,12),S(6,6),C(12),CX(12),CY(12)
311      DIMENSION E(6),EX(6),EY(6)
312 C
313      COMMON /PRTCOM/ HT,MXPLOT,NOR,NPT,NAX,NSH,NCO,NCC,NXCMAT,
314      1                MM,NN,NNSKIP
315      COMMON /MAICOM/ ALFA,AMM,ANN,CF,CIN,CNURSA,CONTURD,DATE1,DATE2,
316      1                DCON,DELTAT,DIR,DY,EM,GRID,HGTZ,AKRTOL,PROJECT,
317      2                S,SDLTAT,NSK,TT,NWBRK,NBRKUP,NFAN,NFLAGR,
318      3                NOLINE,IPLG,MOE,NFLECT,NFRACT,NRFLBU,NRFRBU,NROPT
319      COMMON /RAYCOM/ BDZ,C,CX,CY,D,DELA,DEP,DGDY,DHDX,E,EX,EY,G,GZERO,
320      1                HGT,AKFC,AKR,AKS,POT,PREV,P1,P2,P3,P4,P5,QOT,Q1,
321      2                Q2,Q3,Q4,Q5,PU,SUV,PDEP,SPREV,GTZERO,
322      3                PALFA,SVAV,PG,U,V,IHGT,
323      4                NTOREF,INUM,MAXQ,NUMT,NOREF
324 C
325 C          WRITE OUT THE HEADINGS
326 C
327      WRITE (6,7) (PROJECT,DATE1,DATE2,NPLOT,TT,N,DELTAT,CF,AKRTOL)
328 C
329 C          CHECK FOR SECOND LINE OF PAGE HEADINGS
330 C
331      IF (MAXQ .NE. 1) GO TO 453
332 C
333 C          CHECK FOR METRIC <--> ENGLISH UNITS
334 C
335      IF (MOE .NE. 0) GO TO 465
336      WRITE (6,470)
337      GO TO 453
338 465      WRITE (6,471)
339 C
340 C          PRINT OUT COLUMN HEADINGS
341 C
342 453      WRITE (6,150)
343 C
344 C          CHECK FOR USER-REQUESTED EXPANDED PRINTOUT
345 C

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```

346     IF (NPT .EQ. 0) GO TO 160
347     WRITE(6,155)
348 C
349 C           DOUBLE SPACE THEN EXIT
350 C
351 160    WRITE (6,165)
352     RETURN
353 C
354 C           FORMAT SECTION
355 C
356 7      FORMAT (1H1,12HPROJECT NO. ,A6,1H,,2X,2A6,1H,,5X,8HPLUT NO.,I3,
357 1      1H,,1X,7HPERIOD=,F5.1,4HSEC.,1H,,1X,7HRAY NO.,I3,1H,,
358 2      1X,7HDELTAT=,F6.2,1H,,1X,3HCF=,F8.6,1H,,1X,
359 3      6HKRTOL=,F8.6,/)
360 150    FORMAT (1X,3HMAX,2X,1HX,7X,1HY,7X,5HDEPTH,4X,
361 1      6HCUR:SP,3X,6HCUR:DI,3X,6HPERIOD,3X,
362 2      3HRAY,5X,4HPACK,4X,4HWAVE,4X,1HG,6X,2HGR,5X,3HHGT,6X,2HKS,7X,
363 3      2HKF,7X,2HKR)
364 155    FORMAT (2X,7HROTAT:D,2X,5HPCT:D,3X,7HROTAT:C,2X,
365 1      6HPCT:CX,2X,6HPCT:CY,2X,2HGT,5X,1HU,6X,1HV,
366 2      6X,2HVT,5X,4HBETA,4X,8HDBETA/DT,3X,
367 3      6HBRK UP,3X,2HND,3X,9HCURVATURE)
368 165    FORMAT (1H0)
369 470    FORMAT(1X,51HTHE OUTPUT IS IN ENGLISH UNITS.  DEPTH,HGT(FEET).
370 1      28HG,GR,GT,U,V,VT(FEET/SECOND),,/)
371 471    FORMAT(1X,51HTHE OUTPUT IS IN METRIC UNITS.  DEPTH,HGT(METER).
372 1      29HG,GR,GT,U,V,VT(METER/SECOND),,/)
373     END

```

```

001     SUBROUTINE MOVE(X,Y,A,FK,NGO,MIT,NFK,NDP,AV,LI)
002 C
003 C           PURPOSE
004 C
005 C           THIS SUBROUTINE COMPUTES THE PATH OF THE WAVE PACKET.  TESTS
006 C           ARE MADE TO LOCATE A REFLECTION POINT AND, IF DESIRED, THE
007 C           RAY PATH IS CONTINUED BEYOND THE REFLECTION POINT.
008 C
009 C           SUBROUTINES REQUIRED
010 C
011 C           SURFCE          ROUTINE TO COMPUTE WAVE PARTICULARS
012 C           ANGCON          ROUTINE TO CONVERT ANGLES FOR PRINTOUT
013 C           PAGCOL          ROUTINE TO PRINT PAGE AND COLUMN HEADINGS
014 C           HEIGHT          ROUTINE TO COMPUTE WAVE HEIGHT
015 C
016     IMPLICIT REAL*8 (A-H,O-Z)
017 C
018     DIMENSION CONTURD(9),EM(6,12),S(6,6)
019     DIMENSION C(12),CX(12),CY(12),E(6),EX(6),EY(6)
020 C
021     COMMON /GRDCOM/ CHAT(120,120), CURX(120,120), CURY(120,120),
022 1      CURR(120,120), AX(4500), AY(4500)

```

```

023     COMMON /PRTCOM/ HT, MXPLOT, NOR, NPT, NAX, NSH, NCO, NCC, NXCHAT,
024     1     MM, NN, NNSKIP
025     COMMON /MAICOM/ ALFA, AMM, ANN, CF, CIN, CNVRS, CONTURD, DATE1, DATE2,
026     1     DCON, DELTAT, DIR, DY, EM, GRID, HGTZ, AKRTOL, PROJET,
027     2     S, SDLTAT, NSK, TT, NWBRK, NBRKUP, NFAN, NFLAGR,
028     3     NOLINE, IFLG, MOE, NFLECT, NFRACT, NRFLBU, NRFRBU, NROPT
029     COMMON /RAYCOM/ BDZ, C, CX, CY, D, DELA, DEP, DGD, DHD, E, EX, EY, G, GZERO,
030     1     HGT, AKFC, AKR, AKS, POT, PREV, P1, P2, P3, P4, P5, QOT, Q1,
031     2     Q2, Q3, Q4, Q5, PU, SVV, PDEP, SPREV, GTZERO,
032     3     PALFA, SVAV, PG, U, V, IHGT,
033     4     NTOREF, INUM, MAXQ, NUMT, NOREF
034     COMMON /SRFCOM/ ND, NC, CCON, TTT, ARAY, GR, GT, SARAY, PZ, PZD,
035     1     CALFA, PCALFA, PARAY, PREVT, SPREVT, VT, SVT, ASV,
036     2     Z, ZD, BZ, KMAX, PX, PY, PTTT, PANGLE, PGR, PPCTD, PFCTCX,
037     3     PPCTCY, PGT, SVBZ, SVBDZ, KNUMT, KRFLBU, KRFRBU, CDGD,
038     4     UMX, AGR, PGAM, PBZ, PBDZ, PFK, PV, PVT
039 C
040 C     INITIALIZE QUANTITIES
041 C
042     AAV=AV
043     IWAUIT=1
044     IF (ND .EQ. 1 .AND. NC .EQ. 1) IWAUIT=0
045     NUMT=1
046     MIT=1
047     NOREF=0
048 C
049 C     SAVE VALUES IN CASE OF BREAKUP OF TIME STEP INTEVAL
050 C
051     SVGR=GR
052     SVGT=GT
053     SVA=A
054     SVAAV=AAV
055     SVTTT=TTT
056     SVX=X
057     SVY=Y
058     IF (MAXQ .NE. 2) GO TO 3033
059     SVFKB=FK
060     GO TO 203
061 3033 SVFKB=FKBAR
062     SAVFK=FK
063 203  IF (MAXQ-2) 38,102,81
064 102  FKBAR=FK
065 C
066 C     *****
067 C     *****
068 C     **                                     **
069 C     ** BEGIN ITERATION SEGMENT **
070 C     **                                     **
071 C     *****
072 C     *****
073 C
074 C     ITERATE TO FIND VALUES FOR THE NEXT POINT
075 C

```

```

076 81      DO 20 IT=1,50
077 C
078 C          COMPUTE THE INCREMENTAL DISTANCE TO THE NEXT RAY POINT
079 C
080          D=(GR*DELTAT)/GRID
081 39      DELA=FKBAR*D
082          AA=A+DELA
083          ABAR=A+0.5*DELA
084          IF (NC .EQ. 1 .OR. DABS(Z) .GT. 1.D-6) GO TO 206
085 C
086 C          COMPUTE COMPONENT INCREMENTAL DISTANCES WHEN THERE IS
087 C          NO CURRENT
088 C
089          DELX=D*DCOS(ABAR)
090          DELY=D*DSIN(ABAR)
091          ARAY=AA
092          GO TO 75
093 C
094 C          COMPUTE INCREMENTAL DISTANCES WHEN THERE IS A CURRENT
095 C
096 206      DELX=(G*DCOS(ABAR)+Z*DCOS(ZD))*DELTAT/GRID
097          DELY=(G*DSIN(ABAR)+Z*DSIN(ZD))*DELTAT/GRID
098          ARAY=ATAN2(DELY,DELX)
099 C
100 C          DETERMINE THE LOCATION OF THE NEXT POINT
101 C
102 75      XX=X+DELX
103          YY=Y+DELY
104          CALL SURFCE(XX,YY,AA,FKK,NFK,NDP,IWAUIT,AAV)
105          AVP=AAV-ALFA
106          IF (NTOREF .EQ. 0) GO TO 86
107 C
108 C          REFLECTION HAS BEEN DETERMINED ON THE BASIS OF SNELL'S
109 C          LAW WITH PHASE VELOCITY
110 C
111          NREF=1
112          GO TO 13
113 C
114 C          DETERMINE IF THE PHASE SPEED IS INCREASING OR DECREASING
115 C
116 86      DUD=SVV/PREV
117          GO TO (101,6,38,38,38,38,38,38),MIT
118 101      IF (NDP .EQ. 2) GO TO 38
119          FKBAR=0.5*(FK+FKK)
120          IF (IT .NE. 49) GO TO 88
121          SVFK=FKBAR
122 88      IF (IT-48) 5,37,9
123 37      FKKPP=FKBAR
124 5       IF (MAXQ .GT. 2) GO TO 9
125          IF (IT .LE. 1) GO TO 21
126 C
127 C          TEST FOR CONVERGENCE OF THE RAY CURVATURE CALCULATIONS
128 C

```

```

129 9      IF (DABS(FKKP-FKBAR) .LE. 0.00009D0/D .AND.
130      1      IWAUIT .EQ. 1 ) GO TO 6
131 21      FKKP = FKBAR
132 20      CONTINUE
133 C
134 C      *****
135 C      *****
136 C      ** **
137 C      ** END ITERATION SEGMENT **
138 C      ** **
139 C      *****
140 C      *****
141 C
142 C      DETERMINE IF THE RAY CURVATURE IS CONVERGING TO TWO VALUES
143 C
144      IF (DABS(FKKPP-FKBAR) .LE. 0.00009D0/D .AND. IWAUIT .EQ. 1)
145      1      GO TO 18
146      IF (ND .EQ. 0) GO TO 161
147 C
148 C      DETERMINE IF CONVERGENCE FAILED DUE TO A REFLECTION POINT
149 C
150      IF (DUD .GT. 1.0 .AND. DABS(DTAN(AVP)) .GT. 5.6712818D0) GO TO 91
151 161      MIT=3
152      GO TO 38
153 C
154 C      REFLECTION IS ASSUMED IF THE PHASE SPEED IS INCREASING AND
155 C      THE WAVELET DIRECTION IS WITHIN 10 DEGREES OF BEING PARALLEL
156 C      TO THE WATER DEPTH CONTOUR
157 C
158 91      NREF=2
159      GO TO 13
160 18      FKBAR=.5*(FKBAR+SVFK)
161      MIT=2
162      GO TO 39
163 6      IF (ND .EQ. 0) GO TO 92
164 C
165 C      CHECK TO SEE IF WE ARE TOO CLOSE TO A REFLECTION POINT
166 C
167      IF (DUD .LE. 1.0 .OR.
168      1      DABS(DTAN(AVP)) .LE. 114.588650D0 .OR.
169      2      DABS(DTAN(A-ALFA)) .GE. 3.7320508D0) GO TO 92
170 C
171 C      REFLECTION IS ASSUMED IF THE PHASE SPEED IS INCREASING,
172 C      THE WAVELET DIRECTION IS WITHIN 0.5 DEGREES OF BEING
173 C      PARALLEL TO THE WATER DEPTH CONTOUR, AND THE WAVE PACKET
174 C      DIRECTION IS WITHIN 75 DEGREES OF BEING PERPENDICULAR TO
175 C      THE WATER DEPTH CONTOUR
176 C
177      NREF=3
178 C
179 C      *****
180 C      *****
181 C      ** **

```



```

182 C          ** BEGIN REFLECTION SEGMENT **
183 C          **
184 C          ****
185 C          ****
186 C
187 13  NOREF=NOREF+1
188 C
189 C          TEST FOR REFLECTION HANG-UP
190 C
191 C          IF (NOREF .LT. 2) GO TO 305
192 C
193 C          MORE THAN ONE REFLECTION HAS OCCURED AT THE SAME POINT
194 C
195 C          MIT=7
196 C          GO TO 38
197 C
198 C          RECOVER SAVED VALUES FOR PREVIOUS POINT AND SET QUANTITIES
199 C
200 305  DELTAT=SDLTAT
201 C          A=PANGLE
202 C          ASV=A
203 C          SVAU=PGAM
204 C          ALFA=PALFA
205 C          X=PX
206 C          Y=PY
207 C          NUMT=1
208 C          IFLG=0
209 C          INUM=0
210 C          NBRKUP=0
211 C          NFLECT=0
212 C          NRFLBU=0
213 C          NFRACT=0
214 C          NRFRBU=0
215 C          IF (MAXQ .LE. 1 .OR. MOD(MAXQ,NSK) .EQ. 0) GO TO 1900
216 C
217 C          RAY PARTICULARS NEED TO BE WRITTEN FOR THE REFLECTION POINT
218 C
219 C          CALL ANGCON (PANGLE,CNVRSA)
220 C          CALL ANGCON (PGAM,CNVRSA)
221 C          CALL ANGCON (PARAY,CNVRSA)
222 C          CALL ANGCON (PZD,CNVRSA)
223 C          IF (MOD(NOLINE,LI) .EQ. 0) CALL PAGCOL(NPLOT,N)
224 C          NOLINE=NOLINE+1
225 C          WRITE (6,612) KHAX,PX,PY,PDEP,PZ,PZD,PTTT,
226 1          PARAY,PANGLE,PGAM,PG,PGR,HGT,AKS,AKFC,AKR
227 C          IF (NPT .EQ. 0) GO TO 1900
228 C          WALFA=PALFA/1.74532925D-2
229 C          WCALFA=PCALFA/1.74532925D-2
230 C          IF (MOD(NOLINE,LI) .EQ. 0) CALL PAGCOL(NPLOT,N)
231 C          NOLINE=NOLINE+1
232 C          WRITE(6,615) WALFA,PPCTD,WCALFA,PPCTCX,PPCTCY,PGT,
233 1          PU,PV,PVT,PRZ,PBDZ,KNUMT,PEK
234 C          IF (KNUMT .LE. 1) GO TO 1900

```

```

235     IF (KRFLBU .EQ. 0) GO TO 619
236     WRITE(6,617)
237 619   IF (KRFRBU .EQ. 0) GO TO 1900
238     WRITE(6,618)
239 1900  IF (MOD(NOLINE,LI) .EQ. 0) CALL PAGCOL(NPLOT,N)
240 C
241 C           WRITE OUT TYPE OF REFLECTION
242 C
243 3044  GO TO (97,98,99),NREF
244 97    WRITE (6,152) (KMAX)
245     GO TO 300
246 98    WRITE (6,153) (KMAX)
247     GO TO 300
248 99    WRITE (6,154) (KMAX)
249 300   NOLINE=NOLINE+1
250 14    IF (NROPT .NE. 0) GO TO 301
251 C
252 C           RAY IS NOT CONTINUED
253 C
254     MIT=6
255     GO TO 38
256 301   NTOREF=0
257 C
258 C           COMPUTE REFLECTION ANGLES
259 C
260     SVAU=2.*ALFA-SVAU+3.141592654D0
261     A=2.*ALFA-A+3.141592654D0
262     ARAY=2.*ALFA-ARAY+3.141592654D0
263     AV=SVAU
264     AAV=SVAU
265     IHGT=1
266     CALL SURFCE(X,Y,A,FK,NFK,NDP,IWAVIT,SVAU,CMAT,CURX,CURY,AX,AY)
267     IHGT=0
268 C
269 C           SET QUANTITIES FOR REFLECTION POINT
270 C
271     SVU=V
272     PREV=SVU
273     SVT=VT
274     BDZ=-BDZ
275     PATI=POT
276     QATI=QOT
277     NFLAGR=1
278     GO TO 102
279 C
280 C           *****
281 C           *****
282 C           **                               **
283 C           **   END REFLECTION SEGMENT   **
284 C           **                               **
285 C           *****
286 C           *****
287 C

```

AD-A134 879

CALCULATION OF WAVE PACKET TRAJECTORIES AND WAVE
HEIGHTS FOR VARIABLE WAT. (U) FLORIDA INST OF TECH
MELBOURNE DEPT OF OCEANOGRAPHY AND OCEAN.

2/2

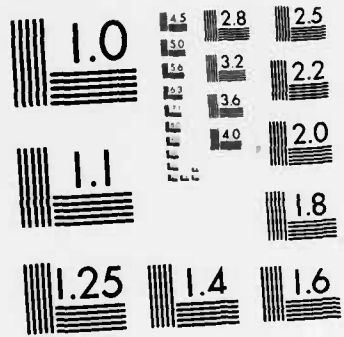
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F/G 8/3

NL





MICROCOPY RESOLUTION TEST CHART
NATIONAL BUREAU OF STANDARDS-1963-A

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288 C          DETERMINE IF POINT IS TOO CLOSE TO A GRID BOUNDARY
289 C
290 92      IF ((XX-1.5)*((AMM-1.5)-XX) .GE. 0.0 .AND.
291      1      (YY-1.5)*((ANN-1.5)-YY) .GE. 0.0) GO TO 309
292          HGO=2
293 C
294 C          UPDATE QUANTITIES AND SAVE VALUES IN CASE OF BREAKUP OF THE
295 C          TIME STEP INTERVAL
296 C
297 309      XS=XX
298          YS=YY
299          SVAV=AAV
300          IF (ND .EQ. 1 .AND. NC .EQ. 1) IWAVIT=0
301          ASV=A
302          SPREV=PREV
303          PREV=SVV
304          SVV=V
305          SPREVT=PREVT
306          PREVT=SVT
307          SVT=VT
308          IF (NC .EQ. 0 .AND. DABS(Z) .LT. 1,D-6) ARAY=AA
309          AAA=.5*(AA+A)
310          A=AA
311          AAAV=.5*(AAV+AV)
312          AV=AAV
313          FK=FKK
314          IF (NFLECT .EQ. 1) GO TO 40
315 C
316 C          COMPUTE P AND Q FOR THE INTERMEDIATE POINTS
317 C
318          XX=X+(1.0D0/3.0D0)*DELX*(DABS(DCOS(AAA)))
319          YY=Y+(1.0D0/3.0D0)*DELY*(DABS(DSIN(AAA)))
320          INGT=1
321          CALL SURFCE(XX,YY,AAA,FKK,NFK,NDP,IWAVIT,AAAV)
322          P1=POT
323          Q1=QOT
324          XX=X+.4*DELX*(DABS(DCOS(AAA)))
325          YY=Y+.4*DELY*(DABS(DSIN(AAA)))
326          CALL SURFCE(XX,YY,AAA,FKK,NFK,NDP,IWAVIT,AAAV)
327          P2=POT
328          Q2=QOT
329          XX=X+.45573725D0*DELX*(DABS(DCOS(AAA)))
330          YY=Y+.45573725D0*DELY*(DABS(DSIN(AAA)))
331          CALL SURFCE(XX,YY,AAA,FKK,NFK,NDP,IWAVIT,AAAV)
332          P3=POT
333          Q3=QOT
334          XX=X+(2.0D0/3.0D0)*DELX*(DABS(DCOS(AAA)))
335          YY=Y+(2.0D0/3.0D0)*DELY*(DABS(DSIN(AAA)))
336          CALL SURFCE(XX,YY,AAA,FKK,NFK,NDP,IWAVIT,AAAV)
337          P4=POT
338          Q4=QOT
339          XX=X+.8*DELX*(DABS(DCOS(AAA)))
340          YY=Y+.8*DELY*(DABS(DSIN(AAA)))

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```

341 CALL SURFCE (XX,YY,AAA,FKK,NFK,NDP,IWAVIT,AAAV)
342 P5=POT
343 Q5=QOT
344 CALL SURFCE (XS,YS,AA,FKK,NFK,NDP,IWAVIT,AAV)
345 IHGT=0
346 40 X=XS
347 Y=YS
348 CALL HEIGHT(X,Y,A,FK,NGO,MIT,NFK,NDP,AV)
349 IF (NBRKUP .EQ. 0) GO TO 38
350 C
351 C RECOVER SAVED VALUES BECAUSE OF THE BREAKUP OF THE TIME
352 C STEP INTERVAL
353 C
354 IF (IFLG .NE. 0) GO TO 203
355 GR=SVGR
356 GT=SVGT
357 SVV=PREV
358 PREV=SPREV
359 SVT=PREVT
360 PREVT=SPREVT
361 A=SVA
362 AAV=SVA AV
363 AV=SVA AV
364 SVA AV=SVA AV
365 IF (MAXQ .NE. 2) GO TO 311
366 FK=SVFKB
367 GO TO 312
368 311 FKBAR=SVFKB
369 FK=SAVFK
370 312 TTT=SVTTT
371 X=SVX
372 Y=SVY
373 GO TO 203
374 38 RETURN
375 C
376 C FORMAT SECTION
377 C
378 152 FORMAT(1X,5HMAX =,I4,1H,,5X,
379 1 43HREFLECTION: SNELLS LAW WITH PHASE VELOCITY)
380 153 FORMAT(1X,5HMAX =,I4,1H,,5X,13HREFLECTION:
381 1 41HPACKET CURVATURE ITERATION NOT CONVERGING)
382 154 FORMAT(1X,5HMAX =,I4,1H,,5X,34HREFLECTION: NEAR REFLECTION POINT)
383 612 FORMAT (1X,I5,2F8.2,2(F9.2,F9.4),3F8.2,2F7.2,4F9.4)
384 615 FORMAT(2X,0PF9.2,F8.2,0PF9.2,2F8.2,4F7.2,F8.4,1X,1PE10.3,9X,I5,
385 1 1X,1PE10.3)
386 617 FORMAT(1H+,93X,7HREFLECT)
387 618 FORMAT(1H+,96X,4HBETA)
388 END

001 SUBROUTINE HEIGHT(X,Y,A,FK,NGO,MIT,NFK,NDP,AV)
002 C

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```

003 C      PURPOSE
004 C
005 C      THIS ROUTINE COMPUTES THE WAVE HEIGHT.  IF NECESSARY,
006 C      THE TIME STEP IS SUCCESSIVELY HALVED TO MAINTAIN THE DESIRED
007 C      ACCURACY IN COMPUTING THE REFRACTION COEFFICIENT, OR THE
008 C      RAY PATH NEAR A REFLECTION POINT.
009 C
010 C      SUBROUTINES REQUIRED
011 C
012 C      NONE
013 C
014 C      IMPLICIT REAL*8 (A-H,O-Z)
015 C
016 C      DIMENSION CONTURD(9),EM(6,12),S(6,6)
017 C      DIMENSION C(12),CX(12),CY(12),E(6),EX(6),EY(6)
018 C
019 C      COMMON /MAICOM/ ALFA,AMM,ANN,CF,CIN,CNURSA,CONTURD,DATE1,DATE2,
020 C      1 DCON,DELTAT,DIR,DY,EM,GRID,HGTZ,AKRTOL,PROJECT,
021 C      2 S,SDLTAT,NSK,TT,NWBRK,NBRKUP,NFAN,NFLAGR,
022 C      3 NOLINE,IFLG,MOE,NFLECT,NFRACT,NRFLBU,NRFRBU,NROPT
023 C      COMMON /RAYCOM/ BDZ,C,CX,CY,D,DELA,DEP,DGDX,DHDX,E,EX,EY,G,GZERO,
024 C      1 HGT,AKFC,AKR,AKS,POT,PREV,P1,P2,P3,P4,P5,QUT,Q1,
025 C      2 Q2,Q3,Q4,Q5,PU,SUV,PDEP,SPREV,GTZERO,
026 C      3 PALFA,SVAV,PG,U,V,IHGT,
027 C      4 NTOREF,INUM,MAXQ,NUMT,NOREF
028 C      COMMON /SRFCOM/ ND,NC,CCON,TTT,ARAY,GR,GT,SARAY,PZ,PZD,
029 C      1 CALFA,PCALFA,PARAY,PREVT,SPREVT,VT,SVT,ASV,
030 C      2 Z,ZD,BZ,KMAX,PX,PY,PTTT,PANGLE,PGR,PPCTD,PPCTCX,
031 C      3 PPCTCY,PGT,SVBZ,SVBDZ,KNUMT,KRFLBU,KRFRBU,CDGDX,
032 C      4 UMX,AGR,PGAM,PBZ,PBDZ,PFK,PV,PVT
033 C
034 C      IF (MAXQ .GT. 1) GO TO 2
035 C
036 C      COMPUTE OR SET QUANTITIES
037 C
038 C      PATI=POT
039 C      QATI=QOT
040 C      BZTOL=AKRTOL**2
041 C      APQ=1.D-12
042 C      IBDZ=0
043 C      AKF=1.D0
044 C      AKR=1.D0
045 C      AKS=1.D0
046 C      HGT=HGTZ*AKS*AKF*AKR
047 C      AKFC=AKF
048 C      FRICTC=26.318945D0/AGR
049 C      GO TO 38
050 C
051 C      COMPUTE SHOALING COEFFICIENT
052 C
053 C      2 AKS=DSQRT(DABS(GTZERO/GT))
054 C
055 C      COMPUTE FRICTION COEFFICIENT

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056 C
057     SKH=6.283185308D0*DEP/(V*TTT)
058     IF (NFK .EQ. 2) GO TO 35
059     AKF = 1.0D0
060     GO TO 36
061 35     AKF=1./(AKFC*FRICTC*CF*HGTZ*D*GRID/((TTT**3)*GTZERO))*
062     1     (2.*AKS/(DEXP(SKH)-DEXP(-SKH)))*3+1.)
063 36     AKFC=AKFC*AKF
064 C
065 C             SAVE VALUES IN CASE OF THE BREAKUP OF THE TIME STEP INTERVAL
066 C
067     SBZ=BZ
068     SBDZ=BDZ
069 C
070 C             SET NROPT TO ZERO SO THAT A RAY IS NOT CONTINUED BEYOND A
071 C             SECOND REFLECTION POINT
072 C
073     IF (NFLAGR .NE. 0) NROPT=0
074     IF (NFK .EQ. 1) GO TO 30
075     IF (NFRACT .NE. 0) GO TO 33
076     IF (NFLECT .EQ. 0) GO TO 207
077     IF (NROPT .EQ. 0 .AND. NFLAGR .EQ. 0) GO TO 33
078     GO TO 202
079 207     IF (DABS(DTAN(AU-ALFA)) .LE. 5.671282D0 .OR.
080     1     DABS(DTAN(A-ALFA)) .GE. 3.7320508D0) GO TO 201
081 C
082 C             IF THE WAVELET DIRECTION IS WITHIN 10 DEGREES OF BEING
083 C             PARALLEL TO THE WATER DEPTH CONTOUR AND THE WAVE PACKET
084 C             DIRECTION IS WITHIN 75 DEGREES OF BEING PERPENDICULAR TO
085 C             THE WATER DEPTH CONTOUR, THE RAY IS ASSUMED TO BE NEAR
086 C             A REFLECTION POINT
087 C
088     NFLECT=1
089     NRFLBU=1
090     IF (NROPT .EQ. 0 .AND. NFLAGR .EQ. 0) GO TO 33
091     IF (NFLAGR .NE. 0) IBDZ=1
092     GO TO 202
093 201     IF (IBDZ .EQ. 0) GO TO 33
094     IBDZ=0
095 C
096 C             COMPUTE D(BETA)/DT ANALYTICALLY TO START THE RUNGE KUTTA
097 C             CALCULATIONS AFTER THE REFLECTION POINT
098 C
099     BDZ=-(BZ*DSIN(A-ALFA)*DTAN(A-ALFA)*DGDY/GRID)
100     IF (NC .EQ. 0) GO TO 205
101     BDZC=-(BZ*DSIN(A-CALFA)*DTAN(A-CALFA)*((CDGDY+UMX)/GRID))
102     BDZ=BDZ+BDZC
103 205     SBDZ=BDZ
104 C
105 C             DETERMINE IF THE WATER DEPTH IS NEARLY CONSTANT
106 C
107 33     IF (DABS(DHDY/GRID) .GT. .00001D0) GO TO 32
108 30     IF (DABS(Z) .GT. 1.D-6) GO TO 32

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109 C
110 C           IN DEEP WATER OR WATER OF CONSTANT DEPTH, IF THERE IS NO
111 C           CURRENT BETA DOES NOT CHANGE
112 C
113           EBZ=0.00
114           EBDZ=0.00
115           GO TO 71
116 C
117 C           DETERMINE IF P OR Q VALUES ARE NOT ZERO
118 C
119 32          IF (DABS(PATI) .GT. APQ .AND. DABS(P3) .GT. APQ
120             1 .AND. DABS(POT) .GT. APQ) GO TO 320
121           IF (DABS(QATI) .GT. APQ .AND. DABS(Q3) .GT. APQ
122             1 .AND. DABS(QOT) .GT. APQ) GO TO 320
123           GO TO 71
124 C
125 C           COMPUTE BETA AND D(BETA)/DT USING THE RUNGE KUTTA METHOD
126 C
127 320        AK1=DELTAT*BDZ
128           AL1=-DELTAT*(PATI*BDZ+QATI*BZ)
129           AK2=DELTAT*(BDZ+.4*AL1)
130           AL2=-DELTAT*(P2*(BDZ+0.4*AL1)+Q2*(BZ+0.4*AK1))
131           AK3=DELTAT*(BDZ+2.9697761D-1*AL1+1.5875964D-1*AL2)
132           AL3=-DELTAT*(P3*(BDZ+2.9697761D-1*AL1+1.5875964D-1*AL2)+Q3*(BZ+
133             1 2.9697761D-1*AK1+1.5875964D-1*AK2))
134           AK4=DELTAT*(BDZ+2.1810040D-1*AL1-3.05096516D0*AL2+3.83286476D0
135             1 *AL3)
136           AL4=-DELTAT*(POT*(BDZ+2.1810040D-1*AL1-3.05096516D0*AL2
137             1 +3.83286476D0*AL3)
138             2 +QOT*(BZ+2.1810040D-1*AK1-3.05096516D0*AK2+3.83286476D0*AK3))
139           AK5=DELTAT*(BDZ+AL1/3.)
140           AL5=-DELTAT*(P1*(BDZ+AL1/3.)+Q1*(BZ+AK1/3.))
141           AK6=DELTAT*(BDZ+(6.*AL5+4.*AL1)/25.)
142           AL6=-DELTAT*(P2*(BDZ+(6.*AL5+4.*AL1)/25.)+Q2*(BZ+(6.*AK5+4.*AK1)
143             1 /25.))
144           AK7=DELTAT*(BDZ+(15.*AL6-12.*AL5+AL1)/4.)
145           AL7=-DELTAT*(POT*(BDZ+(15.*AL6-12.*AL5+AL1)/4.)+QUT*(BZ+(15.*AK6
146             1 -12.*AK5+AK1)/4.))
147           AK8=DELTAT*(BDZ+(8.*AL7-50.*AL6+90.*AL5+6.*AL1)/81.)
148           AL8=-DELTAT*(P4*(BDZ+(8.*AL7-50.*AL6+90.*AL5+6.*AL1)/81.)+Q4*(BZ+
149             1 (8.*AK7-50.*AK6+90.*AK5+6.*AK1)/81.))
150           AK9=DELTAT*(BDZ+(8.*AL7+10.*AL6+36.*AL5+6.*AL1)/75.)
151           AL9=-DELTAT*(P5*(BDZ+(8.*AL7+10.*AL6+36.*AL5+6.*AL1)/75.)+Q5*(BZ+
152             1 (8.*AK7+10.*AK6+36.*AK5+6.*AK1)/75.))
153           BZ5=BZ+(1.0D0/192.0D0)*(23.*AK1+125.*AK6-81.*AK8+125.*AK9)
154           BDZ5=BDZ+(1.0D0/192.0D0)*(23.*AL1+125.*AL6-81.*AL8+125.*AL9)
155           BDZ=BDZ+0.17476028D0*AL1-0.55148066D0*AL2+1.20553560D0*AL3+
156             1 0.17118478D0*AL4
157           BZ=BZ+0.17476028D0*AK1-0.55148066D0*AK2+1.20553560D0*AK3+
158             1 0.17118478D0*AK4
159           IF (NC .EQ. 0 .AND. ND .EQ. 1 .AND.
160             1 DABS(DTAN(A-ALFA)) .GE. 11.43D0) GO TO 802
161           IF (ND .EQ. 0 .AND. NC .EQ. 1 .AND.

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162      1   DABS(DTAN(A-CALFA)) .GE. 11.43D0) GO TO 802
163      GO TO 801
164 C
165 C           COMPUTE D(BETA)/DT ANALYTICALLY NEAR A CAUSTIC
166 C
167 802   BDZ=-(DSQRT(DABS(QOT)))*SBZ
168      BZ5=BZ
169      BDZ5=BDZ
170 C
171 C           COMPUTE DIFFERENCE BETWEEN 4TH AND 5TH ORDER SOLUTIONS AS
172 C           AN ACCURACY TEST
173 C
174 801   EBZ=BZ-BZ5
175      EBDZ=BDZ-BDZ5
176 C
177 C           COMPUTE REFRACTION COEFFICIENT
178 C
179 71   AKR=1./(DSQRT(DABS(BZ)))
180      IF (NFLECT .EQ. 0) GO TO 401
181 202   IF (IFLG .NE. 0) GO TO 55
182 C
183 C           NEAR A REFLECTION POINT LIMIT THE CHANGE IN THE PACKET
184 C           DIRECTION
185 C
186      IF (DABS(DELA) .LT. 1.74532925D-2) GO TO 22
187      GO TO 58
188 401   IF (IFLG .NE. 0) GO TO 55
189 C
190 C           REQUIRE THAT THE BETA CALCULATION HAS THE DESIRED ACCURACY
191 C
192      IF (DABS(EBZ) .GE. BZTOL .OR. DABS(EBDZ) .GE. BZTOL) GO TO 21
193 22   IF (NUMT .LE. 1) GO TO 4
194      IFLG=1
195      GO TO 55
196 21   NFRACT=1
197      NRFRBU=1
198 C
199 C           IF THE DESIRED ACCURACY IS NOT REACHED, BREAK UP THE TIME
200 C           STEP INTERVAL AND RESUME CALCULATIONS
201 C
202 58   DELTAT=.5*DELTAT
203      IF (DELTAT .GE. 0.5) GO TO 81
204      MIT=8
205      NBRKUP=0
206      GO TO 38
207 81   NBRKUP=1
208 C
209 C           DOUBLE THE NUMBER OF INTERVALS THE TIME STEP IS DIVIDED INTO
210 C           AND RECOVER SAVED VALUES
211 C
212      NUMT=2*NUMT
213      BZ=SBZ
214      BDZ=SBZ

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215      AKFC=AKFC/AKF
216      GO TO 38
217 55    INUM=INUM+1
218 C
219 C      DETERMINE IF THE PROPER NUMBER OF POINTS FOR THE BREAKUP OF
220 C      THE TIME STEP HAVE BEEN COMPUTED
221 C
222      IF (INUM .LT. NUMT) GO TO 64
223 C
224 C      RESUME CALCULATIONS WITH THE ORIGINAL TIME STEP
225 C
226      IFLG=0
227      INUM=0
228      DELTAT=SDLTAT
229      NBRKUP=0
230      GO TO 4
231 C
232 C      UPDATE P AND Q VALUES
233 C
234 64    PATI=POT
235      QATI=QOT
236 C
237 C      TEST FOR FOCAL POINT OR CAUSTIC
238 C
239      IF (BZ .GT. 0.0001D0) GO TO 67
240 68    MIT=4
241      NBRKUP=0
242      GO TO 38
243 67    NBRKUP=1
244      GO TO 38
245 4     IF (BZ .LE. 0.0001D0) GO TO 68
246 C
247 C      UPDATE P AND Q VALUES
248 C
249      PATI=POT
250      QATI=QOT
251      NFRACT=0
252      NFLECT=0
253 C
254 C      COMPUTE WAVE HEIGHT
255 C
256      HGT=HGTZ*AKS*AKFC*AKR
257      IF (NWBK .EQ. 0) GO TO 38
258 C
259 C      TEST FOR WAVE BREAK
260 C
261      IF (HGT/(V*TT) .LE. (1./7.)*DTANH(SKH)) GO TO 38
262      MIT=5
263 38    RETURN
264      END
```

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001 SUBROUTINE SURFCE(X,Y,A,FK,NFK,NDP,IWAVIT,AV)
002 C
003 C PURPOSE
004 C
005 C THIS ROUTINE COMPUTES THE WATER DEPTH, CURRENT MAGNITUDE,
006 C CURRENT DIRECTION, ROTATION ANGLES, WAVELET DIRECTION,
007 C PROPAGATION VELOCITIES, COEFFICIENTS OF THE RAY SEPARATION
008 C EQUATION (P AND Q), THE PACKET RAY CURVATURE, AND THE INITIAL
009 C VALUES OF D(BETA)/DT.
010 C
011 C SUBROUTINES REQUIRED
012 C
013 C VELCTY ROUTINE TO COMPUTE WAVE SPEEDS
014 C
015 C IMPLICIT REAL*8 (A-H,O-Z)
016 C
017 C DIMENSION CONTURD(9),EM(6,12),S(6,6)
018 C DIMENSION C(12),CX(12),CY(12),E(6),EX(6),EY(6)
019 C DIMENSION YVW(6)
020 C
021 C COMMON /GRDCOM/ CHAT(120,120), CURX(120,120), CURY(120,120),
022 C 1 CURR(120,120), AX(4500), AY(4500)
023 C COMMON /PRTCOM/ HT,MXPLOT,NUR,NPT,NAX,NSH,NCO,NCC,NXCHAT,
024 C 1 MM,NN,NNSKIP
025 C COMMON /MAICOM/ ALFA,AMM,ANN,CF,CIN,CNURSA,CONTURD,DATE1,DATE2,
026 C 1 DCON,DELTAT,DIR,DY,EM,GRID,HGTZ,AKRTOL,PROJECT,
027 C 2 S,SDLTAT,NSK,TT,NWBRK,NBRKUP,NFAN,NFLAGR,
028 C 3 NOLINE,IFLG,MOE,NFLECT,NFRACT,NRFLBU,NRFRBU,NROPT
029 C COMMON /RAYCOM/ BDZ,C,CX,CY,D,DELA,DEP,DGDX,DHDX,E,EX,EY,G,GZERO,
030 C 1 HGT,AKFC,AKR,AKS,POT,PREV,P1,P2,P3,P4,P5,QOT,Q1,
031 C 2 Q2,Q3,Q4,Q5,PU,SUV,PDEF,SPREV,GTZERO,
032 C 3 PALFA,SVAV,PG,U,V,IHGT,
033 C 4 NTOREF,INUM,MAXQ,NUMT,NOREF
034 C COMMON /SRFCOM/ ND,NC,CCON,TTT,ARAY,GR,GT,SARAY,PZ,PZD,
035 C 1 CALFA,PCALFA,PARAY,PREVT,SPREVT,UT,SVT,ASV,
036 C 2 Z,ZD,BZ,KMAX,PX,PY,PTTT,PANGLE,PGR,PPCTD,PPCTCX,
037 C 3 PPCTCY,PGT,SVBZ,SVBDZ,KNUMT,KRFLBU,KRFRBU,CDGDX,
038 C 4 UMX,AGR,PGAM,PBZ,PRDZ,PFK,PV,PVT
039 C
040 C DATA IN THE S AND EM ARRAYS ARE USED IN FITTING QUADRATIC
041 C SURFACES FOR WATER DEPTHS AND CURRENTS
042 C
043 C DATA S/
044 C 1 2.2248800,-1.5968900,-1.5968900, 0.2500, 0.4736842, 0.2500,
045 C 2 -1.5968900, 1.6895930, 1.0361840,-0.3750,-0.3157895,-0.1875,
046 C 3 -1.5968900, 1.0361840, 1.6895930,-0.1875,-0.3157895,-0.3750,
047 C 4 0.2500000,-0.3750000,-0.1875000, 0.1250, 0.0000000, 0.0625,
048 C 5 0.4736842,-0.3157895,-0.3157895, 0.0000, 0.2105263, 0.0000,
049 C 6 0.2500000,-0.1875000,-0.3750000, 0.0625, 0.0000000, 0.1250/
050 C DATA EM/1.,0.,1.,0.,0.,1.,1.,0.,2.,0.,0.,4.,
051 C 1 1.,1.,0.,1.,0.,0.,1.,1.,1.,1.,1.,1.,
052 C 2 1.,1.,2.,1.,2.,4.,1.,1.,3.,1.,3.,9.,
053 C 3 1.,2.,0.,4.,0.,0.,1.,2.,1.,4.,2.,1.,

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054      4      1.,2.,2.,4.,4.,4.,1.,2.,3.,4.,6.,9.,
055      5      1.,3.,1.,9.,3.,1.,1.,3.,2.,9.,6.,4./
056 C
057      IF (MAXQ .GT. 1) GO TO 201
058      IF (ND .EQ. 1) GO TO 573
059 C
060 C      IF THERE IS NO WATER DEPTH GRID, THE RAY CURVATURE, P, AND Q
061 C      DUE TO DEPTH VARIATIONS ARE SET EQUAL TO ZERO
062 C
063      FKAD=0.DO
064      POTD=0.DO
065      QOTD=0.DO
066 573     IF (NC .EQ. 1) GO TO 574
067 C
068 C      IF THERE IS NO CURRENT GRID, THE RAY CURAVATURE P AND Q DUE
069 C      TO CURRENT VARIATIONS ARE SET EQUAL TO ZERO
070 C
071      FKAC=0.DO
072      POTC=0.DO
073      QOTC=0.DO
074 574     IDBDT=0
075      IONCE=1
076 C
077 C      *****
078 C      *****
079 C      ***** BEGIN SURFACE FITTING SEGMENT *****
080 C      *****
081 C      *****
082 C
083 201     I=X
084         J=Y
085         FI=I
086         FJ=J
087         FIC=I
088         FJC=J
089         XL=X+1.-FI
090         YL=Y+1.-FJ
091         IF (ND .EQ. 0) GO TO 324
092         IF (MAXQ .LE. 1) GO TO 1
093         IF (ZI .NE. FI) GO TO 1
094         IF (ZJ .EQ. FJ) GO TO 3
095 1       ZI=FI
096         ZJ=FJ
097 C
098 C      SELECT 12 DEPTHS FROM THE GRID ABOUT THE RAY POINT
099 C
100         C(1)=CHAT(J+1,I)
101         C(2)=CHAT(J+2,I)
102         C(3)=CHAT(J,I+1)
103         C(4)=CHAT(J+1,I+1)
104         C(5)=CHAT(J+2,I+1)
105         C(6)=CHAT(J+3,I+1)
106         C(7)=CHAT(J,I+2)

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107      C(8)=CMAT(J+1,I+2)
108      C(9)=CMAT(J+2,I+2)
109      C(10)=CMAT(J+3,I+2)
110      C(11)=CMAT(J+1,I+3)
111      C(12)=CMAT(J+2,I+3)
112 C
113 C          FIT QUADRATIC SURFACE TO THE 12 DEPTHS.  AT SUCCESSIVE RAY
114 C          POINTS A NEW QUADRATIC SURFACE IS DETERMINED ONLY IF THERE
115 C          IS A CHANGE IN ANY OF THE 12 WATER DEPTH GRID VALUES
116 C
117      DO 319 II=1,6
118          YVW(II)=0.
119          DO 318 L=1,12
120              YVW(II)=YVW(II)+C(L)*EM(II,L)
121 318      CONTINUE
122 319      CONTINUE
123      DO 321 II=1,6
124          E(II)=0.
125          DO 320 JJ=1,6
126              E(II)=E(II)+S(JJ,II)*YVW(JJ)
127 320      CONTINUE
128 321      CONTINUE
129 C
130 C          COMPUTE INTERPOLATED WATER DEPTH
131 C
132 3      DEP=(E(1)+E(2)*XL+E(3)*YL+E(4)*XL**2+E(5)*XL*YL+E(6)*YL**2)*DCON
133 C
134 C          COMPUTE PARTIAL DERIVATIVES OF WATER DEPTH IN FIXED XY-
135 C          SYSTEM
136 C
137      HX=(E(2)+2.*E(4)*XL+E(5)*YL)*DCON
138      HY=(E(3)+E(5)*XL+E(6)*2.*YL)*DCON
139      DHDXM=DSQRT((HX*HX)+(HY*HY))
140 C
141 C          IF THERE IS A VARIATION IN WATER DEPTH COMPUTE THE ROTATION
142 C          ANGLE
143 C
144      IF (DABS(DHDXM/GRID) .GT. 0.00001) ALFA=DATAN2(HY,HX)
145      COSALF=DCOS(ALFA)
146      SINALF=DSIN(ALFA)
147 C
148 C          COMPUTE PARTIAL DERIVATIVE OF WATER DEPTH IN ROTATED XY-
149 C          SYSTEM
150 C
151      DHDX=HX*COSALF+HY*SINALF
152      IF (IHGT .EQ. 0) GO TO 572
153 C
154 C          COMPUTE SECOND PARTIAL DERIVATIVES OF WATER DEPTH IN FIXED
155 C          XY-SYSTEM
156 C
157      HXX=2.*E(4)*DCON
158      HYY=2.*E(6)*DCON
159      HXY=E(5)*DCON

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160 C
161 C           COMPUTE SECOND PARTIAL DERIVATIVES OF WATER DEPTH IN
162 C           ROTATED XY-SYSTEM
163 C
164           HDER1=2.*SINALF*COSALF*HXY
165           DHDXX=(COSALF**2)*HXX+HDER1+(SINALF**2)*HYY
166           DHDYY=(SINALF**2)*HXX-HDER1+(COSALF**2)*HYY
167           DHDXY=(SINALF*COSALF)*(HYY-HXX)+((COSALF**2)-(SINALF**2))*HXY
168 C
169 C           IF THE WATER DEPTH IS GREATER THAN 0, THE CALCULATIONS
170 C           ARE CONTINUED
171 C
172 572       IF (DEP .GT. 0.) GO TO 324
173           NDP=2
174           GO TO 403
175 C
176 C           COMPUTE DEEP WATER WAVELENGTH
177 C
178 324       WL=AGR*(TTT**2)/6.283185308D0
179           IF (DEP/WL .GT. .64) GO TO 322
180           NFK=2
181           GO TO 50
182 C
183 C           IN DEEP WATER SET NFK = 1
184 C
185 322       NFK=1
186 50        IF (NC .EQ. 0) GO TO 323
187           IK=0
188           IF (MAXQ .LE. 1) GO TO 52
189           IF (ZIC .NE. FIC) GO TO 71
190           IF (ZJC .EQ. FJC) GO TO 53
191 71        IK=1
192 52        ZIC=FIC
193           ZJC=FJC
194 C
195 C           SELECT 12 CURRENT SPEEDS FROM X-COMPONENT GRID ABOUT THE RAY
196 C           POINT
197 C
198           CX(1)=CURX(J+1,I)
199           CX(2)=CURX(J+2,I)
200           CX(3)=CURX(J,I+1)
201           CX(4)=CURX(J+1,I+1)
202           CX(5)=CURX(J+2,I+1)
203           CX(6)=CURX(J+3,I+1)
204           CX(7)=CURX(J,I+2)
205           CX(8)=CURX(J+1,I+2)
206           CX(9)=CURX(J+2,I+2)
207           CX(10)=CURX(J+3,I+2)
208           CX(11)=CURX(J+1,I+3)
209           CX(12)=CURX(J+2,I+3)
210 C
211 C           DETERMINE IF THE X-COMPONENT CURRENT VALUES ARE EQUAL
212 C           AT THE FOUR NEAREST GRID POINTS

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213 C
214 IF (DABS(CX(5)-CX(8)) .GT. 0.000001D0) GO TO 551
215 IF (DABS(CX(4)-CX(9)) .GT. 0.000001D0) GO TO 551
216 IF (DABS(CX(5)-CX(9)) .GT. 0.000001D0) GO TO 551
217 IF (MAXQ .LE. 1 .OR. IK .EQ. 1) GO TO 562
218 53 IF (IZX .EQ. 1) GO TO 561
219 C
220 C IF THE FOUR GRID POINT VALUES ARE EQUAL THE COMPONENT CURRENT
221 C AND ITS DERIVATIVES ARE SET EQUAL TO ZERO
222 C
223 562 ZX=0.D0
224 ZXX=0.D0
225 ZXY=0.D0
226 ZXXX=0.D0
227 ZXYX=0.D0
228 ZXXY=0.D0
229 IZX=0
230 GO TO 557
231 C
232 C FIT QUADRATIC SURFACE TO THE 12 CURRENT SPEED VALUES FOR THE
233 C X-COMPONENT. AT SUCCESSIVE RAY POINTS A NEW QUADRATIC
234 C SURFACE IS DETERMINED ONLY IF THERE IS A CHANGE IN ANY OF THE
235 C 12 CURRENT SPEED GRID VALUES
236 C
237 551 DO 54 II=1,6
238 YVW(II)=0.0D0
239 DO 80 L=1,12
240 YVW(II)=YVW(II)+CX(L)*EM(II,L)
241 80 CONTINUE
242 54 CONTINUE
243 DO 81 II=1,6
244 EX(II)=0.0D0
245 DO 55 JJ=1,6
246 EX(II)=EX(II)+S(JJ,II)*YVW(JJ)
247 55 CONTINUE
248 81 CONTINUE
249 C
250 C COMPUTE INTERPOLATED X-COMPONENT CURRENT
251 C
252 561 ZX=(EX(1)+EX(2)*XL+EX(3)*YL+EX(4)*XL**2+EX(5)*XL*YL+
253 1 EX(6)*YL**2)*CCON
254 C
255 C COMPUTE PARTIAL DERIVATIVES OF X-COMPONENT CURRENT IN
256 C FIXED XY-SYSTEM
257 C
258 ZXX=(EX(2)+2.D0*EX(4)*XL+EX(5)*YL)*CCON
259 ZXY=(EX(3)+EX(5)*XL+EX(6)*2.D0*YL)*CCON
260 ZXXX=2.D0*EX(4)*CCON
261 ZXYX=2.D0*EX(6)*CCON
262 ZXXY=EX(5)*CCON
263 IZX=1
264 IDBDT=1
265 557 IF (MAXQ .LE. 1) GO TO 72

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266      IF (IK .EQ. 0) GO TO 56
267 C
268 C          SELECT 12 CURRENT SPEEDS FROM Y-COMPONENT GRID ABOUT THE
269 C          RAY POINT
270 C
271 72      CY(1)=CURY(J+1,I)
272      CY(2)=CURY(J+2,I)
273      CY(3)=CURY(J,I+1)
274      CY(4)=CURY(J+1,I+1)
275      CY(5)=CURY(J+2,I+1)
276      CY(6)=CURY(J+3,I+1)
277      CY(7)=CURY(J,I+2)
278      CY(8)=CURY(J+1,I+2)
279      CY(9)=CURY(J+2,I+2)
280      CY(10)=CURY(J+3,I+2)
281      CY(11)=CURY(J+1,I+3)
282      CY(12)=CURY(J+2,I+3)
283 C
284 C          DETERMINE IF THE Y-COMPONENT CURRENT VALUES ARE EQUAL
285 C          AT THE FOUR NEAREST GRID POINTS
286 C
287      IF (DABS(CY(5)-CY(8)) .GT. 0.000001D0) GO TO 552
288      IF (DABS(CY(4)-CY(9)) .GT. 0.000001D0) GO TO 552
289      IF (DABS(CY(5)-CY(9)) .GT. 0.000001D0) GO TO 552
290      IF (MAXQ .LE. 1 .OR. IK .EQ. 1) GO TO 564
291 56      IF (IZY .EQ. 1) GO TO 563
292 C
293 C          IF THE FOUR GRID POINT VALUES ARE EQUAL THE COMPONENT CURRENT
294 C          AND ITS DERIVATIVES ARE SET EQUAL TO ZERO
295 C
296 564      ZY=0.D0
297      ZYX=0.D0
298      ZYY=0.D0
299      ZYXX=0.D0
300      ZYYY=0.D0
301      ZYXY=0.D0
302      IZY=0
303      GO TO 553
304 C
305 C          FIT QUADRATIC SURFACE TO THE 12 CURRENT SPEED VALUES FOR
306 C          THE Y-COMPONENT, AT SUCCESSIVE RAY POINTS A NEW QUADRATIC
307 C          SURFACE IS DETERMINED ONLY IF THERE IS A CHANGE IN ANY OF
308 C          THE 12 CURRENT SPEED GRID VALUES
309 C
310 552      DO 57 II=1,6
311          YVW(II)=0.D0
312          DO 82 L=1,12
313              YVW(II)=YVW(II)+CY(L)*EM(II,L)
314 82      CONTINUE
315 57      CONTINUE
316      DO 59 II=1,6
317          EY(II)=0.D0
318      DO 58 JJ=1,6

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319             EY(II)=EY(II)+S(JJ,II)*YVW(JJ)
320 58         CONTINUE
321 59         CONTINUE
322 C
323 C             COMPUTE INTERPOLATED Y-COMPONENT CURRENT
324 C
325 563        ZY=(EY(1)+EY(2)*XL+EY(3)*YL+EY(4)*XL**2+EY(5)*XL*YL+
326 1          EY(6)*YL**2)*CCON
327 C
328 C             COMPUTE PARTIAL DERIVATIVES OF Y-COMPONENT CURRENT IN
329 C             FIXED XY-SYSTEM
330 C
331             ZYX=(EY(2)+2.DO*EY(4)*XL+EY(5)*YL)*CCON
332             ZYY=(EY(3)+EY(5)*XL+EY(6)*2.DO*YL)*CCON
333             ZYXX=2.DO*EY(4)*CCON
334             ZYYY=2.DO*EY(6)*CCON
335             ZYXY=EY(5)*CCON
336             IZY=1
337             IDBDT=1
338 C
339 C             DETERMINE CURRENT SPEED MAGNITUDE
340 C
341 553        Z=DSQRT((ZX**2)+(ZY**2))
342             IF (DABS(Z) .GT. 0.000001D0) GO TO 213
343 C
344 C             IF THE CURRENT SPEED IS NEAR ZERO THE CURRENT DERIVATIVES
345 C             IN THE ROTATED XY-SYSTEM ARE SET EQUAL TO ZERO
346 C
347             DZDX=0.DO
348             DZDXX=0.DO
349             DZDYY=0.DO
350             DZDXY=0.DO
351             DZDDX=0.DO
352             DZDDY=0.DO
353             DZDDXX=0.DO
354             DZDDYY=0.DO
355             DZDDXY=0.DO
356             GO TO 323
357 C
358 C             COMPUTE FIRST PARTIAL DERIVATIVES OF CURRENT SPEED IN
359 C             FIXED XY-SYSTEM
360 C
361 213        ZTX=(ZX*ZXX+ZY*ZYX)/Z
362             ZTY=(ZX*ZXY+ZY*ZYY)/Z
363             DZDXM=DSQRT((ZTX*ZTX)+(ZTY*ZTY))
364 C
365 C             IF THERE IS A VARIATION IN CURRENT COMPUTE THE ROTATION ANGLE
366 C
367             IF (DABS(DZDXM/GRID) .GT. 0.00001) CALFA=DATAN2(ZTY,ZTX)
368             SICALF=DSIN(CALFA)
369             COCALF=DCOS(CALFA)
370 C
371 C             COMPUTE FIRST PARTIAL DERIVATIVE OF CURRENT SPEED IN

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372 C          ROTATED XY-SYSTEM
373 C
374 C          DZDX=ZTX*COCALF+ZTY*SICALF
375 C
376 C          COMPUTE CURRENT DIRECTION
377 C
378 C          ZD=DATAN2(ZY,ZX)
379 C
380 C          COMPUTE FIRST PARTIAL DERIVATIVES OF CURRENT DIRECTION IN
381 C          FIXED XY-SYSTEM
382 C
383 C          ZDX=(ZX*ZYX-ZY*ZXX)/(Z**2)
384 C          ZDY=(ZX*ZYY-ZY*ZXY)/(Z**2)
385 C
386 C          COMPUTE FIRST PARTIAL DERIVATIVES OF CURRENT DIRECTION IN
387 C          ROTATED XY-SYSTEM
388 C
389 C          DZDDX=COCALF*ZDX+SICALF*ZDY
390 C          DZDDY=-SICALF*ZDX+COCALF*ZDY
391 C          IF (IHGT .EQ. 0) GO TO 323
392 C
393 C          COMPUTE SECOND PARTIAL DERIVATIVES OF CURRENT SPEED IN FIXED
394 C          XY-SYSTEM
395 C
396 C          ZTXX=(ZX*ZXXX+ZXX*ZXX+ZY*ZYXX+ZYX*ZYX-ZTX*ZTX)/Z
397 C          ZTXY=(ZX*ZXXY+ZXX*ZXY+ZY*ZYXY+ZYX*ZYY-ZTX*ZTY)/Z
398 C          ZTTY=(ZX*ZXY+ZXY*ZXY+ZY*ZYYY+ZYY*ZYY-ZTY*ZTY)/Z
399 C
400 C          COMPUTE SECOND PARTIAL DERIVATIVES OF CURRENT SPEED IN ROTATED
401 C          XY-SYSTEM
402 C
403 C          ZDER1=2.*SICALF*COCALF*ZTXY
404 C          DZDXX=(COCALF**2)*ZTXX+ZDER1+(SICALF**2)*ZTTY
405 C          DZDYY=(SICALF**2)*ZTXX-ZDER1+(COCALF**2)*ZTTY
406 C          DZDXY=(SICALF*COCALF)*(ZTTY-ZTXX)+((COCALF**2)-(SICALF**2))*ZTXY
407 C
408 C          COMPUTE SECOND PARTIAL DERIVATIVES OF CURRENT DIRECTION IN
409 C          FIXED XY-SYSTEM
410 C
411 C          ZDXX=(((ZX*ZYXX-ZY*ZXXX)/Z)-2.DO*ZDX*ZTX)/Z
412 C          ZDYY=(((ZX*ZYYY-ZY*ZXY)/Z)-2.DO*ZDY*ZTY)/Z
413 C          ZDXY=(((ZXX*ZYY+ZXY*ZYXY-ZYX*ZXY-ZY*ZXXY)/Z)-2.DO*ZDY*ZTX)/Z
414 C
415 C          COMPUTE SECOND PARTIAL DERIVATIVES OF CURRENT DIRECTION IN
416 C          ROTATED XY-SYSTEM
417 C
418 C          ZDDER1=2.*SICALF*COCALF*ZDXY
419 C          DZDDXX=(COCALF**2)*ZDXX+ZDDER1+(SICALF**2)*ZDYY
420 C          DZDDYY=(SICALF**2)*ZDXX-ZDDER1+(COCALF**2)*ZDYY
421 C          DZDDXY=(SICALF*COCALF)*(ZDYY-ZDXX)+((COCALF**2)-(SICALF**2))*ZDXY
422 C
423 C          *****
424 C          *****

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425 C          ***** END OF SURFACE FITTING SEGMENT *****
426 C          *****
427 C          *****
428 C
429 C
430 C          COMPUTE VELOCITIES AND DOPPLER SHIFTED WAVE PERIOD
431 C
432 323 DD 60 IT=1,50
433          TTO=TTT
434          CALL VELCTY(V,TTT,MAXQ,DEP,NFK,U,NC,AGR)
435          TTT=TT*(1.D0+Z*DCOS(AV-ZD)/V)
436          IF (DABS((TTO-TTT)/TTT) .LE. 0.000001D0) GO TO 61
437 60 CONTINUE
438 61 IF (IHGT .NE. 0) GO TO 12
439 C
440 C          *****
441 C          *****
442 C          ***** BEGIN WAVELET COMPUTATION SEGMENT *****
443 C          *****
444 C          *****
445 C
446          IF (ND .EQ. 1 .AND. NC .EQ. 1) GO TO 570
447          IF (ND .EQ. 0) GO TO 26
448 C
449 C          COMPUTE WAVELET DIRECTION IN ROTATED XY-SYSTEM USING SNELL'S
450 C          LAW FOR WATER DEPTHS
451 C
452          GP=SVAV-ALFA
453 14 IF (DABS(GP) .LE. 6.283185308D0) GO TO 13
454          IF (GP) 16,13,17
455 16 GP=GP+6.283185308D0
456          GO TO 14
457 17 GP=GP-6.283185308D0
458          GO TO 14
459 13 ARG1=V*DSIN(GP)/SVV
460 C
461 C          TEST FOR TOTAL REFLECTION OF THE WAVELETS
462 C
463          IF (DABS(ARG1) .LE. 1.D0) GO TO 18
464          NTOREF=1
465          GO TO 403
466 18 NTOREF=0
467          GPT=DASIN(ARG1)
468          IF (DABS(GP) .LE. 4.71238898038D0) GO TO 20
469          AVP=6.283185308D0+GPT
470          GO TO 22
471 20 IF (DABS(GP) .LE. 1.5707963268D0) GO TO 23
472          AVP=3.141592654D0-GPT
473          GO TO 22
474 23 AVP=GPT
475 22 AV=AVP+ALFA
476          IF (NC .EQ. 0) GO TO 12
477 C

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478 C          COMPUTE WAVELET DIRECTION IN ROTATED XY-SYSTEM USING SNELL'S LAW F
479 C
480 26      GPC=SVAV-CALFA
481 114     IF (DABS(GPC) .LE. 6.283185308D0) GO TO 113
482        IF (GPC) 116,113,117
483 116     GPC=GPC+6.283185308D0
484        GO TO 114
485 117     GPC=GPC-6.283185308D0
486        GO TO 114
487 113     DO 122 ITT=1,50
488        AVPSAV=AVP
489 C
490 C          COMPUTE PHASE VELOCITY AND DOPPLER SHIFTED WAVE PERIOD
491 C
492        DO 255 IT=1,50
493        TTO=TTT
494        CALL VELCTY(V,TTT,MAXQ,DEP,NFK,U,NC,AGR)
495        TTT=TT*(1.D0+Z*DCOS(AV-ZD)/V)
496        IF (DABS((TTO-TTT)/TTT) .LE. 0.000001D0) GO TO 254
497 255     CONTINUE
498 254     VT=V+Z*DCOS(AV-ZD)
499        ARG1C=VT*DSIN(GPC)/SVT
500 C
501 C          TEST FOR TOTAL REFLECTION OF THE WAVELETS
502 C
503        IF (DABS(ARG1C) .LE. 1.D0) GO TO 118
504        NTOREF=1
505        GO TO 403
506 118     NTOREF=0
507        GPCT=DASIN(ARG1C)
508        IF (DABS(GPC) .LE. 4.71238898038D0) GO TO 120
509        AVP=6.283185308D0+GPCT
510        GO TO 115
511 120     IF (DABS(GPC) .LE. 1.5707963268D0) GO TO 123
512        AVP=3.141592654D0-GPCT
513        GO TO 115
514 123     AVP=GPCT
515 115     AV=AVP+CALFA
516        IF (ITT .LE. 1) GO TO 122
517        IF (DABS((AVPSAV-AVP)/AVP) .LE. 0.000001D0) GO TO 12
518 122     CONTINUE
519        GO TO 12
520 C
521 C          COMPUTE WAVELET DIRECTION IN ROTATED XY-SYSTEMS USING RAY
522 C          CURVATURE EXPRESSION FOR WATER DEPTHS AND CURRENTS
523 C
524 570     IF (MAXQ .EQ. 1) GO TO 12
525        NTOREF=0
526        DELAVS=DELAV
527        DELAV=((DTAN(SVAV-ALFA)*DCOS(ARAY-ALFA)*DVDX)+
528 1        DCOS(ARAY-CALFA)*(DTAN(SVAV-CALFA)*(CDVDX+UKX)-
529 2        (CDVDY+UKY)))*(GR/VT)*(DELTAT/GRID)
530        DELAVB=0.5D0*(DELAVS+DELAV)

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531      IF (DABS(DELAUB-DELAUS) .LE. 0.000009D0) IWAUIT=1
532      AV=SVAV+DELAUB
533 C
534 C      *****
535 C      *****
536 C      ***** END OF WAVELET COMPUTATION SEGMENT *****
537 C      *****
538 C      *****
539 C
540 12    PHI=A-AV
541      COSPHI=DCOS(PHI)
542      SINPHI=DSIN(PHI)
543      TANPHI=DTAN(PHI)
544 C
545 C      COMPUTE GEOMETRIC GROUP VELOCITY
546 C
547      G=U*DCOS(PHI)
548      AVMZD=AV-ZD
549      SIAVMZ=DSIN(AVMZD)
550      COAVMZ=DCOS(AVMZD)
551 C
552 C      COMPUTE VELOCITY OF ADVECTED WAVELET FRONT IN CURRENT
553 C
554      VT=V+Z*COAVMZ
555      AMZD=A-ZD
556      SIAMZD=DSIN(AMZD)
557      COAMZD=DCOS(AMZD)
558 C
559 C      COMPUTE RAY VELOCITY IN CURRENT
560 C
561      GR=(G**2+Z**2+2*Z*G*COAMZD)**.5
562 C
563 C      COMPUTE VELOCITY OF ADVECTED GROUP FRONT IN CURRENT
564 C
565      GT=G+Z*COAMZD
566 C
567 C      *****
568 C      *****
569 C      ***** BEGIN CURVATURE, P AND Q SEGMENT *****
570 C      *****
571 C      *****
572 C
573 C
574 C
575 C      COMPUTE ANGULAR FREQUENCY
576 C
577      OMEGA=2.D0*3.141592654D0/TTT
578      A2V2=1.0-((OMEGA*V/AGR)**2)
579      WHAQ=(V**2)+AGR*DEP*A2V2
580      OI=2.0*OMEGA*DEP/V
581      UVRA=U/V
582      UD1=UVRA-0.5
583      UD2=(1.0-DSQRT((OI**2)+4.0*(UD1**2)))

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584      IF (ND .EQ. 0) GO TO 251
585      IF (NFK .EQ. 2) GO TO 402
586 C
587 C          IN DEEP WATER THE GEOMETRIC GROUP VELOCITY DERIVATIVE, RAY
588 C          CURVATURE, P, AND Q FOR WATER DEPTHS ARE SET EQUAL TO ZERO
589 C
590      DVDX=0.00
591      DGDY=0.00
592      FKAD=0.00
593      POTD=0.00
594      QOTD=0.00
595      GO TO 575
596 402      W=AGR*V*A2V2/WHAO
597 C
598 C          COMPUTE THE FIRST DERIVATIVE OF THE PHASE VELOCITY FOR
599 C          WATER DEPTHS
600 C
601      DVDX=W*DHDY
602      AVMAL=AV-ALFA
603      TANAVM=DTAN(AVMAL)
604      COSAVM=DCOS(AVMAL)
605      AMALFA=A-ALFA
606      TANAMA=DTAN(AMALFA)
607      COSAMA=DCOS(AMALFA)
608      SINAMA=DSIN(AMALFA)
609      UD3X=(V/DEP)*DHDY-DVDX
610 C
611 C          COMPUTE FIRST DERIVATIVE OF CONVENTIONAL GROUP VELOCITY FOR
612 C          WATER DEPTHS
613 C
614      DUDX=UVRA*DVDX+UD1*UD2*UD3X
615      RHO=1.00/(1.00+TANPHI*TANAMA)
616      SIGMA=U*SINPHI*TANAVM/V
617 C
618 C          COMPUTE FIRST DERIVATIVE OF GEOMETRIC GROUP VELOCITY FOR
619 C          WATER DEPTHS
620 C
621      DGDY=RHO*(DUDX*COSPHI+SIGMA*DVDX)
622 C
623 C          COMPUTE PACKET RAY CURVATURE FOR WATER DEPTHS IN ROTATED
624 C          XY-SYSTEM
625 C
626      DSRAD=DCOS(ARAY-ALFA)/COSAMA
627      FKAD=SINAMA*DGDY*DSRAD
628      IF (IHGT .EQ. 0) GO TO 575
629 C
630 C          COMPUTE P FOR WATER DEPTHS IN ROTATED XY-SYSTEM
631 C
632      POTD=(-2.*COSAMA*DGDY)/GRID
633      DAVDX=TANAVM*DVDX/V
634      DADY=TANAMA*DGDY/G
635      DPHIDY=DADY-DAVDX
636      YH=-2.0*AGR*(V**2)/(WHAO**2)

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637 C
638 C           COMPUTE SECOND DERIVATIVES OF PHASE VELOCITY FOR WATER DEPTHS
639 C
640           DVDXX=W*(DHDXX+YH*(DHDXX**2))
641           DVDYY=W*DHDYY
642           DVDXY=W*DHDXY
643           UD4X=(DUDX-UVRA*DUDX)/V
644           UD5X=((V*DHDXX-UD3X*DHDX)/DEP)-DVDXX
645           UD6=-UD3X*((OI**2)*UD3X/V)+4.*UD1*UD4X
646           UD7=DSQRT((OI**2)+4.*(UD1**2))
647 C
648 C           COMPUTE SECOND DERIVATIVES OF CONVENTIONAL GROUP VELOCITY
649 C           FOR WATER DEPTHS
650 C
651           DUDXX=UVRA*DVDXX+UD4X*(DVDX+UD2*UD3X)+UD1*((UD6/UD7)+UD2*UD5X)
652           DUDYY=UVRA*DVDYY+UD1*UD2*((V/DEP)*DHDYY-DVDYY)
653           DUDXY=UVRA*DVDXY+UD1*UD2*((V/DEP)*DHDXY-DVDXY)
654 C
655 C           COMPUTE SECOND DERIVATIVES OF GEOMETRIC GROUP VELOCITY FOR
656 C           WATER DEPTHS
657 C
658           DGDXX=RHO*(DUDXX*COSPHI-DPHIDX*(2.*DUDX*SINPHI+G*DPHIDX)
659           1           -U*SINPHI*(TANAMA*(DADX**2)-TANAVM*((DVDX/V)+(DAVDX**2))))
660           IF (DABS(TANAMA) .GT. 0.08748866D0 .AND. DABS(TANAVM) .GT.
661           1           0.08748866D0) GO TO 35
662           ZETA=1.
663           XI=0.
664           GO TO 36
665 35          ZETA=1.0/(1.0-TANPHI/TANAMA)
666           XI=U*SINPHI/V*TANAVM
667 36          DGDYY=ZETA*(DUDYY*COSPHI-XI*DVDYY)
668           DGDXY=RHO*(DUDXY*COSPHI+SIGMA*DVDXY)
669 C
670 C           COMPUTE Q FOR WATER DEPTHS IN ROTATED XY-SYSTEM
671 C
672           QOTD=(G*((SINAMA**2)*DGDXX-2.*SINAMA*COSAMA*DGDXY+
673           1*(COSAMA**2)*DGDYY))/(GRID**2)
674 575        IF (NC .EQ. 0) GO TO 252
675 251        IF (NFK .EQ. 2) GO TO 203
676           WO=-V/OMEGA
677           GO TO 204
678 203        WO=(DEP*AGR*V*A2V2-(V**3))/(OMEGA*WHAO)
679 204        WAVNO=OMEGA/V
680           CTAVM=DTAN(AV-CALFA)
681 C
682 C           COMPUTE COMPONENT OF CURRENT NORMAL TO WAVELET FRONT
683 C
684           UK=Z*COAVMZ
685           RMKL1=Z*SIAVMZ/VT
686           RMK=RMKL1*CTAVM
687           RMK1=1.D0+RMK
688           RMKL2=UK*(1.D0-WAVNO*WO)/V
689           OD1=1.D0/(1.D0-(WAVNO*RMK*WO/RMK1)+RMKL2)

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690      OD2=DZDX*COAVMZ+Z*SIAVMZ*DZDDX
691      OMEGX=-OD1*(WAVNO/RMK1)*OD2
692      RMKY=RMKL1/CTAVM
693      RMKY1=1-RMKY
694      ODY1=1.00/(1.00-(WAVNO*RMKY*WO/RMKY1)+RMKL2)
695      ODY2=Z*SIAVMZ*DZDDY
696      OMEGY=-ODY1*(WAVNO/RMKY1)*ODY2
697 C
698 C          COMPUTE THE FIRST DERIVATIVES OF THE PHASE VELOCITY FOR
699 C          CURRENTS
700 C
701      CDVDX=WO*OMEGX
702      CDVDY=WO*OMEGY
703 C
704 C          COMPUTE FIRST DERIVATIVES OF CURRENT COMPONENT NORMAL TO
705 C          WAVELET FRONT
706 C
707      UKX=(-RMK*CDVDX+OD2)/RMK1
708      UKY=(RMKY*CDVDY+ODY2)/RMKY1
709      CAMALF=A-CALFA
710      CSAM=DSIN(CAMALF)
711      CCAH=DCOS(CAMALF)
712      CTAM=DTAN(CAMALF)
713      IF (MFK ,EQ, 2) GO TO 207
714 C
715 C          COMPUTE FIRST DERIVATIVES OF CONVENTIONAL GROUP VELOCITY FOR
716 C          CURRENTS IN DEEP WATER
717 C
718      CDUDX=CDVDX/2.
719      CDUDY=CDVDY/2.
720      GO TO 208
721 207      UDC1=(V/OMEGA)*OMEGX-CDVDX
722          UDCY1=(V/OMEGA)*OMEGY-CDVDY
723 C
724 C          COMPUTE FIRST DERIVATIVES OF CONVENTIONAL GROUP VELOCITY FOR
725 C          CURRENTS
726 C
727      CDUDX=UVRA*CDVDX+UD1*UD2*UDC1
728      CDUDY=UVRA*CDVDY+UD1*UD2*UDCY1
729 208      RMCOM=Z*SIAMZD/GT
730          RM=RMCOM*CTAM
731          RM1=1.00+RM
732          RNT=(U*SINPHI*CTAM)/GT
733          RNG=(U*SINPHI*CTAVM)/VT
734          GDC2=DZDX*COAMZD+Z*SIAMZD*DZDDX
735          GDC3=RNT/RM1
736          RMY=RMCOM/CTAM
737          RMY1=1.00-RMY
738          RNTY=(U*SINPHI)/(GT*CTAM)
739          RNGY=(U*SINPHI)/(VT*CTAVM)
740          GDCY2=Z*SIAMZD*DZDDY
741          GDCY3=RNTY/RMY1
742 C

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743 C          COMPUTE FIRST DERIVATIVES OF GEOMETRIC GROUP VELOCITY
744 C          FOR CURRENTS
745 C
746          CDGDX=(CDUDX*COSPFI-GDC3*GDC2+RNG*(CDVDX+UKX))/(1.D0+GDC3)
747          CDGDY=(CDUDY*COSPFI+GDCY3*GDCY2-RNGY*(CDVDY+UKY))/(1.D0-GDCY3)
748 C
749 C          COMPUTE FIRST DERIVATIVES OF CURRENT COMPONENT NORMAL TO
750 C          GROUP FRONT
751 C
752          UMX=(-RM*CDGDX+GDC2)/RM1
753          UMY=(RMY*CDGDY+GDCY2)/RMY1
754 C
755 C          COMPUTE PACKET RAY CURVATURE FOR CURRENTS IN ROTATED XY-SYSTEM
756 C
757          DSRAC=DCOS(ARAY-CALFA)/CCAM
758          FKAC=(CSAM*(CDGDX+UMX)-CCAM*(CDGDY+UMY))*DSRAC
759          IF (IHGT .EQ. 0) GO TO 252
760 C
761 C          COMPUTE P FOR CURRENTS IN ROTATED XY-SYSTEM
762 C
763          POTC=(-2.0*(CCAM*(CDGDX+UMX)+CSAM*(CDGDY+UMY))/GRID
764          IF (NFK .EQ. 2) GO TO 209
765          Y0=2.*V/(OMEGA**2)
766          GO TO 210
767 209        Y01=WO/V
768          Y02=(AGR-DEP*(OMEGA**2))*(Y01**2)+2.*DEP*OMEGA*Y01-
769          1      (AGR/(OMEGA**2))-DEP
770          Y0=(2.*V/WHAD)*(((V/OMEGA)**2)+DEP*A2V2*Y02)
771 210        CDAVDX=(CTAVM/VT)*(CDVDX+UKX)
772          GMZDX=CDAVDX-DZDDX
773          GMZDX2=(GMZDX**2)
774          OD3=(DZDXX*COAVMZ-2.D0*DZDX*SIAVMZ*GMZDX-Z*COAVMZ*GMZDX2+
775          1      Z*SIAVMZ*(-CTAVM*(CDAVDX**2)+DZDDXX))/RMK1
776          OD4=(1.D0-WAVNO*WO)/V
777          WAVNOX=OD4*OMEGX
778          OD5=1.D0/(1.D0-(WAVNO*RMK*WO/RMK1)+RMKL2)
779          OMEGX=OD5*((WAVNO*RMK*Y0/RMK1)*(OMEGX**2)-WAVNO*OD3-
780          1      2.D0*WAVNOX*UKX+(UK*OMEGX/V)*(OD4*CDVDX+
781          2      WAVNO*Y0*OMEGX+WO*WAVNOX))
782          CDAVDY=-((CDVDY+UKY)/(VT*CTAVM)
783          GMZDY=CDAVDY-DZDDY
784          GMZDY2=(GMZDY**2)
785          ODY3=(DZDYY*COAVMZ-Z*COAVMZ*GMZDY2+
786          1      Z*SIAVMZ*((CDAVDY**2)/CTAVM)+DZDDYY))/RMKY1
787          WAVNOY=OD4*OMEGY
788          ODY5=1.D0/(1.D0+(WAVNO*RMKY*WO/RMKY1)+RMKL2)
789          ODY6=(UK/V)*((OD4*CDVDY+WAVNO*Y0*OMEGY+WO*WAVNOY)
790          OMEGY=ODY5*((WAVNO*RMKY*Y0/RMKY1)*(OMEGY**2)-WAVNO*ODY3-
791          1      2.D0*WAVNOY*UKY+ODY6*OMEGY)
792          ODXY4=(DZDXY*COAVMZ-DZDX*SIAVMZ*GMZDY-Z*COAVMZ*GMZDX*GMZDY+
793          1      Z*SIAVMZ*(-((1.D0/CTAVM)+2.D0*CTAVM)*CDAVDX*CDAVDY+
794          2      DZDDXY))/RMK1
795          OMEGXY=OD5*((WAVNO*RMK*Y0/RMK1)*OMEGX*OMEGY-WAVNO*ODXY4-

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796      1      WAVNOY*UKX-WAVNOX*UKY+ODY6*OMEGX)
797 C
798 C      COMPUTE SECOND DERIVATIVES OF PHASE VELOCITY FOR CURRENTS
799 C
800      CDVDXX=WO*OMEGXX+YO*(OMEGX**2)
801      CDVDYY=WO*OMEGYY+YO*(OMEGY**2)
802      CDVDXY=WO*OMEGXY+YO*OMEGX*OMEGY
803 C
804 C      COMPUTE SECOND DERIVATIVES OF CURRENT COMPONENT NORMAL TO
805 C      WAVELET FRONT
806 C
807      UKXX=-(RMK*CDVDXX/RMK1)+OD3
808      UKYY=(RMKY*CDVDYY/RMKY1)+ODY3
809      UKXY=-(RMK*CDVDXY/RMK1)+ODXY4
810      IF (NFK .EQ. 2) GO TO 211
811 C
812 C      COMPUTE SECOND DERIVATIVES OF CONVENTIONAL GROUP VELOCITY FOR
813 C      CURRENTS IN DEEP WATER
814 C
815      CDUDXX=CDVDXX/2.
816      CDUDYY=CDVDYY/2.
817      CDUDXY=CDVDXY/2.
818      GO TO 212
819 211      UDC2=(CDUDX-UVRA*CDVDX)/V
820      UDC3=((V*OMEGXX-UDC1*OMEGX)/OMEGA)-CDVDXX
821      UDC4=-UDC1*((OI**2)*UDC1/V)+4.*UD1*UDC2)
822      UDC5=DSQRT((OI**2)+4.*(UD1**2))
823      UDCY2=(CDUDY-UVRA*CDVDY)/V
824      UDCY3=((V*OMEGYY-UDCY1*OMEGY)/OMEGA)-CDVDYY
825      UDCY4=((OI**2)*UDCY1/V)+4.*UD1*UDCY2
826      UDCXY3=((V*OMEGXY-UDCY1*OMEGX)/OMEGA)-CDVDXY
827 C
828 C      COMPUTE SECOND DERIVATIVES OF CONVENTIONAL GROUP VELOCITY FOR
829 C      CURRENTS
830 C
831      CDUDXX=UVRA*CDVDXX+UDC2*(CDVDX+UD2*UDC1)+
832      1      UD1*((UDC4/UDC5)+UD2*UDC3)
833      CDUDYY=UVRA*CDVDYY+UDCY2*(CDVDY+UD2*UDCY1)+
834      1      UD1*((-UDCY1*UDCY4/UDC5)+UD2*UDCY3)
835      CDUDXY=UVRA*CDVDXY+UDCY2*(CDVDX+UD2*UDC1)+
836      1      UD1*((-UDC1*UDCY4/UDC5)+UD2*UDCXY3)
837 212      CDADX=(CTAM/GT)*(CDGDX+UMX)
838      CDADY=-(CDGDY+UMY)/(CTAM*GT)
839      CDPHDX=CDADX-CDAVDX
840      CDPHDY=CDADY-CDAVDY
841      TMZDX=CDADX-DZDDX
842      TMZDX2=(TMZDX**2)
843      TMZDY=CDADY-DZDDY
844      TMZDY2=(TMZDY**2)
845      GDC4=(COAMZD*DZDXX-2.D0*DZDX*SIAMZD*TMZDX-Z*COAMZD*TMZDX2+
846      1      Z*SIAMZD*(-CTAM*(CDADX**2)+DZDDXX))/RM1
847      GDCY4=(COAMZD*DZDYY-Z*COAMZD*TMZDY2+
848      1      Z*SIAMZD*((CDADY**2)/CTAM)+DZDDYY))/RMY1

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849      RMY = Z*COAMZD*CTAM/GT
850      RMY1 = 1.00 + RMY
851      GDCXY4 = (COAMZD*DZDXY - TMZDY*(DZDX*SIAMZD + Z*COAMZD*TMZDX) +
852      1      Z*COAMZD*(-CDADX*CDADY*((1./CTAM)+2.*CTAM)+
853      2      DZDXY))/RMY1
854 C
855 C      COMPUTE SECOND DERIVATIVES OF GEOMETRIC GROUP VELOCITY FOR
856 C      CURRENTS
857 C
858      CDGDXX = (CDUDXX*COSPHI - CDPHDX*(2.00*CDUDX*SINPHI + G*CDPHDX) -
859      1      RNT*GDC4 - U*SINPHI*CTAM*(CDADX**2) + RNG*(CDVDXX + UKXX) +
860      2      U*SINPHI*CTAVM*(CDAVDX**2))/(1.00 + (RNT/RM1))
861      CDGDYY = (CDUDYY*COSPHI - CDPHDY*(2.00*CDUDY*SINPHI + G*CDPHDY) +
862      1      RNTY*GDCY4 + U*SINPHI*((CDADY**2)/CTAM) - RNGY*(CDVDYY +
863      2      UKYY) - U*SINPHI*((CDAVDY**2)/CTAVM))/(1.00 - GDCY3)
864      CDGDXY = (CDUDXY*COSPHI - CDPHDY*(CDUDX*SINPHI + G*CDPHDX) -
865      1      CDUDY*SINPHI*CDPHDX - RNT*GDCXY4 - U*SINPHI*CDADX*
866      2      CDADY*((1./CTAM)+2.*CTAM) + RNG*(CDVDXY + UKXY) +
867      3      U*SINPHI*CDAVDX*CDAVDY*((1./CTAVM)+2.*CTAVM))/
868      4      (1.00 + (RNT/RMY1))
869 C
870 C      COMPUTE SECOND DERIVATIVES OF CURRENT COMPONENT NORMAL TO
871 C      GROUP FRONT
872 C
873      UMXX = -(RM*CDGDXX/RM1) + GDC4
874      UMY = (RMY*CDGDYY/RMY1) + GDCY4
875      UMXY = -(RMY*CDGDXY/RMY1) + GDCXY4
876 C
877 C      COMPUTE Q FOR CURRENTS IN ROTATED XY-SYSTEM
878 C
879      QOTC = GT*((CSAM**2)*(CDGDXX + UMXX) - 2.*CSAM*CCAM*
880      1      (CDGDXY + UMXY) + (CCAM**2)*(CDGDYY + UMY))/(GRID**2)
881 C
882 C      COMPUTE PACKET RAY CURVATURE, P, AND Q FOR WATER DEPTHS AND
883 C      CURRENTS
884 C
885 252    FK = (FKAD + FKAC)/GT
886      POT = POTD + POTC
887      QOT = QOTD + QOTC
888 C
889 C      *****
890 C      *****
891 C      ***** END OF CURVATURE, P AND Q SEGMENT *****
892 C      *****
893 C      *****
894 C
895      IF (MAXQ .GT. 1) GO TO 405
896 C
897 C      COMPUTE INITIAL D(BETA)/DT FOR WATER DEPTHS
898 C
899      IF (ND .EQ. 1) BDZ = -TANAMA*SINAMA*DGDX/GRID
900 C
901 C      COMPUTE INITIAL CHANGE IN WAVELET DIRECTION FOR STARTING THE

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902 C           RAY CURVATURE CALCULATIONS OF THE WAVELET DIRECTION
903 C
904           IF (ND .EQ. 1 .AND. NC .EQ. 1) DELAV=
905 1           ((DTAN(SVAV-ALFA)*DCOS(ARAY-ALFA)*DUDX)+
906 2           DCOS(ARAY-CALFA)*(DTAN(SVAV-CALFA)*(CDUDX+UKX)-
907 3           (CDVDY+UKY)))*(GR/VT)*(DELTAT/GRID)
908 405        IF (MAXQ .EQ. MAXQSA) GO TO 403
909           MAXQSA=MAXQ
910           IF (IONCE .EQ. 0 .OR.
911 1           IDBDT .EQ. 0 .OR.
912 2           DABS(Z) .LE. 1.D-6) GO TO 403
913 C
914 C           COMPUT INITIAL D(BETA)/DT FOR CURRENTS
915 C
916           BDZA=-(BZ*CSAM*CTAM)*((CDGDX+UMX)/GRID)
917           BDZ=BDZ+BDZA
918           IONCE=0
919 403        RETURN
920           END

```

```

001          SUBROUTINE VELCTY(V,TT,MAXQ,DEP,NFK,U,NC,AGR)
002 C
003 C          PURPOSE
004 C
005 C          THIS ROUTINE COMPUTES THE PHASE VELOCITY AND COLINEAR
006 C          (CONVENTIONAL) GROUP VELOCITY.
007 C
008 C          SUBROUTINES REQUIRED
009 C
010 C          NONE
011 C
012          IMPLICIT REAL*8 (A-H,O-Z)
013 C
014          IF (MAXQ .GT. 1 .AND. NC .EQ. 0) GO TO 102
015          BAR=6.283185308D0/TT
016          CXXO=TT*AGR/6.283185308D0
017          CCC=CXXO
018          GO TO 103
019 102        CCC=XCXY
020 103        IF (NFK .EQ. 2) GO TO 105
021 C
022 C          PHASE VELOCITY IS EQUAL TO DEEP WATER VALUE
023 C
024          V=CXXO
025          GO TO 106
026 105        DO 1000 M=1,90
027 C
028 C          COMPUTE PHASE VELOCITY FOR WATER OF ARBITRARY DEPTH
029 C
030          V=CXXO*DTANH(BAR*DEP/CCC)
031          IF (DABS(V-CCC) .LT. .00005D0) GO TO 106

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```

032 1000 CCC=(V+CCC)/2.
033 106  XCY=V
034      BAR2=2.*BAR*DEP/V
035      IF (NFK .EQ. 2) GO TO 3036
036 C
037 C          COMPUTE DEEP WATER VALUE OF GROUP VELOCITY
038 C
039      U=.5*V
040      GO TO 107
041 C
042 C          COMPUTE GROUP VELOCITY FOR WATER OF ARBIRTRARY DEPTH
043 C
044 3036 U=.5*V*(1.+2.*BAR2/(DEXP(BAR2)-DEXP(-BAR2)))
045 107  RETURN
046      END

```

```

001      SUBROUTINE PCD(C,E,PCTDIF)
002 C
003 C          PURPOSE
004 C
005 C          THIS ROUTINE DETERMINES THE DIFFERENCE BETWEEN THE GRID
006 C          VALUE AND THE VALUE COMPUTED FROM THE 12-POINT SURFACE
007 C          FIT FOR THE 4 GRID POINTS CLOSEST TO THE RAY POINT.
008 C          THE MAXIMUM PERCENTAGE DIFFERENCE OF THE 4 GRID POINTS
009 C          IS DETERMINED.
010 C
011 C          SUBROUTINES REQUIRED
012 C
013 C          NONE
014 C
015      IMPLICIT REAL*8 (A-H,O-Z)
016 C
017      DIMENSION C(12),E(6)
018      IF (C(4)*C(5)*C(8)*C(9) .NE. 0.) GU TO 901
019 C
020 C          PCTDIF IS SET TO 999 IF THE PRODUCT OF THE FOUR GRID
021 C          VALUES IS ZERO
022 C
023      PCTDIF=999.
024      GO TO 902
025 901  P1=DABS((C(4)-(E(1)+E(2)+E(3)+E(4)+E(5)+E(6)))/C(4))
026      P2=DABS((C(5)-(E(1)+E(2)+2.*E(3)+E(4)+E(5)*2.+E(6)*4.))/C(5))
027      P3=DABS((C(8)-(E(1)+E(2)*2.+E(3)+E(4)*4.+E(5)*2.+E(6)))/C(8))
028      P4=DABS((C(9)-(E(1)+E(2)*2.+E(3)*2.+E(4)*4.+E(5)*4.+E(6)*4.))/
029      1  C(9))
030      PCTDIF=100.*DHAX1(P1,P2,P3,P4)
031 902  RETURN
032      END

```

```

001      SUBROUTINE STORE(X,Y,A,KMAX,TIMEQ,KCIN,KREST)
002 C
003 C      PURPOSE
004 C
005 C      IN THIS ROUTINE THE COORDINATES OF EACH RAY POINT ARE STORED.
006 C      IF DESIRED, THE LOCATIONS OF TICK MARKS AT EQUAL TIME
007 C      INTERVALS ALONG THE RAY ARE COMPUTED AND STORED.
008 C
009 C      SUBROUTINES REQUIRED
010 C
011 C      NONE
012 C
013      IMPLICIT REAL*8 (A-H,O-Z)
014 C
015      DIMENSION CONTURD(9),EM(6,12),S(6,6)
016      DIMENSION C(12),CX(12),CY(12),E(6),EX(6),EY(6)
017 C
018      COMMON /GRDCOM/ CHAT(120,120), CURX(120,120), CURY(120,120),
019      1      CURR(120,120), AX(4500), AY(4500)
020      COMMON /PRTCOM/ HT,MXPLOT,NOR,NPT,NAX,NSH,NCO,NCC,NXCHAT,
021      1      MM,NN,NNSKIP
022      COMMON /MAICOM/ ALFA,AMM,ANN,CF,CIN,CNURSA,CONTURD,DATE1,DATE2,
023      1      DCON,DELTAT,DIR,DY,EM,GRID,HGTZ,AKRTOL,PROJECT,
024      2      S,SDLTAT,NSK,TT,NWBRK,NBRKUP,NFAN,NFLAGR,
025      3      NOLINE,IFLG,MOE,NFLECT,NFRACT,NRFLBU,NRFRBU,NROPT
026      COMMON /RAYCOM/ BDZ,C,CX,CY,D,IELA,DEP,DGDY,DHDX,E,EX,EY,G,GZERO,
027      1      HGT,AKFC,AKR,AKS,POT,PREV,P1,P2,P3,P4,P5,QOT,Q1,
028      2      Q2,Q3,Q4,Q5,PU,SVV,PDEP,SPREV,GTZERO,
029      3      PALFA,SVAV,PG,U,V,IHGT,
030      4      NTOREF,INUM,MAXQ,NUMT,NOREF
031 C
032      IF (CIN .LE. 0) GO TO 403
033      IF (KMAX .GT. 1) GO TO 401
034      AT=0.
035 C
036 C      STORE POINT COORDINATES
037 C
038      403 KQ=KMAX+KCIN
039      AX(KQ)=X
040      AY(KQ)=Y
041      IF (CIN .LE. 0.) GO TO 205
042      402 ZA=A
043      SAVEGR=GR
044      GO TO 205
045      401 ET=TIMEQ-AT
046      IF (CIN-ET) 405,404,403
047 C
048 C      RAY POINT AND TICK MARK COINCIDE, STORE WITH NEGATIVE X
049 C
050      404 KQ=KMAX+KCIN
051      AX(KQ)=-X
052      AY(KQ)=Y
053      KREST=KREST+1

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```

054      AT=AT+CIN
055      GO TO 402
056 C
057 C          COMPUTE LOCATION OF TICK MARK AND STORE WITH NEGATIVE X
058 C
059 405  DSC=(ET-CIN)*(GR+SAVEGR)*3600.D0/(GRID*2.)
060      AA=(A+ZA)/2.
061      XM=DSC*DCOS(AA)
062      YM=DSC*DSIN(AA)
063      KQ=KMAX+KCIN
064      AX(KQ)=-X+XM
065      AY(KQ)=Y-YM
066      KREST=KREST+1
067      KCIN=KCIN+1
068      AT=AT+CIN
069      GO TO 401
070 C
071 C          THEN EXIT
072 C
073 205  RETURN
074      END

```

```

001      SUBROUTINE DRAW (N,KMAX,KCIN,KREST)
002 C
003 C          PURPOSE
004 C
005 C          THIS ROTUINE DRAWS AND NUMBERS THE RAYS.  IF DESIRED, TICK
006 C          MARKS ARE DRAWN AT EQUAL TIME INTERVALS.
007 C
008 C          SUBROUTINES CALLED
009 C
010 C          PLOT          CALCOMP ROUTINE TO MOVE THE PEN
011 C          NUMBER        CALCOMP ROUTINE TO DRAW A NUMBER AT A POINT
012 C
013      IMPLICIT REAL*8 (A-H,O-Z)
014 C
015      DIMENSION CONTURD(9),EM(6,12),S(6,6)
016      DIMENSION C(12),CX(12),CY(12),E(6),EX(6),EY(6)
017 C
018      COMMON /GRDCOM/  CHAT(120,120), CURX(120,120), CURY(120,120),
019 1          CURR(120,120), AX(4500), AY(4500)
020      COMMON /PRTCOM/  HT,MXPLOT,NOR,NPT,NAX,NSH,NCO,NCC,NXCMT,
021 1          MM,NN,NNSKIP
022      COMMON /MAICOM/  ALFA,AMM,ANN,CF,CIN,CNURSA,CONTURD,DATE1,DATE2,
023 1          DCON,DELTAT,DIR,DY,EM,GRID,HGTZ,AKRTOL,PROJCT,
024 2          S,SDLTAT,NSK,TT,NWBRK,NBRKUP,NFAN,NFLAGR,
025 3          NOLINE,IFLG,MOE,NFLECT,NFRACT,NRFLBU,NRFRBU,NROPT
026      COMMON /RAYCOM/  BDZ,C,CX,CY,D,DELA,DEP,DGDY,DHDX,E,EX,EY,G,GZERO,
027 1          HGT,AKFC,AKR,AKS,POT,PREV,P1,P2,P3,P4,P5,QOT,Q1,
028 2          Q2,Q3,Q4,Q5,PU,SUU,PDEP,SPREV,GTZERO,
029 3          PALFA,SAVU,PG,U,V,IHGT,

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030      4          NTOREF, INUM, MAXQ, NUMT, NOREF
031 C
032      XN=N
033      KMAX=KMAX+KCIN
034      IF (AX(KMAX) .GE. 0.) GO TO 601
035      AX(KMAX)=-AX(KMAX)
036      KREST=KREST-1
037 601 IF (MOD(N,2) .NE. 0) GO TO 104
038 C
039 C          BEGIN EVEN-NUMBERED RAY WITH THE TERMINAL POINT
040 C
041      KTWO=KMAX-1
042      KADD=-1
043      LAST=1
044      MC=KREST+1
045      IF (NFAN .EQ. 0) GO TO 201
046      CALL NUMBER (AX(KMAX)/DY,AY(KMAX)/DY,0.1,XN,0.0,-1)
047 201 CALL PLOT (AX(KMAX)/DY,AY(KMAX)/DY,3)
048      IF (KMAX .LE. 1) GO TO 106
049      GO TO 105
050 C
051 C          BEGIN ODD NUMBERED RAY WITH THE INITIAL POINT
052 C
053 104 KTWO=2
054      KADD=1
055      LAST=KMAX
056      MC=0
057      IF (NFAN .NE. 0) GO TO 111
058 C
059 C          NUMBER RAY AT THE INITIAL POINT
060 C
061      CALL NUMBER (AX(1)/DY,AY(1)/DY,0.1,XN,0.0,-1)
062 111 CALL PLOT (AX(1)/DY,AY(1)/DY,3)
063      IF (KMAX .LE. 1) GO TO 106
064 105 IF (CIN .LE. 0.) GO TO 300
065      IF (AX(KTWO) .LT. 0.) GO TO 302
066 C
067 C          DRAW SEGMENT OF RAY
068 C
069 300 CALL PLOT (AX(KTWO)/DY,AY(KTWO)/DY,2)
070      GO TO 303
071 302 AX(KTWO)=-AX(KTWO)
072      WI=.05
073      MC=MC+KADD
074      IF (MOD(MC,10) .NE..0) GO TO 500
075      WI=.10
076 500 XPN=AX(KTWO)/DY
077      YPN=AY(KTWO)/DY
078      KQ=KTWO-KADD
079 430 XPL=AX(KQ)/DY
080      YPL=AY(KQ)/DY
081      IF (DABS(XPN-XPL) .LT. .0005D0 .AND.
082 1     DABS(YPN-YPL) .LT. .0005D0) GO TO 410

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```

083      GO TO 420
084 C
085 C          POINTS ARE TOO CLOSE TOGETHER
086 C
087 410  KQ=KQ-KADD
088      GO TO 430
089 420  DSC=DSQRT((XPN-XPL)**2+(YPN-YPL)**2)
090 C
091 C          DRAW THE RAY
092 C
093      CALL PLOT(XPN,YPN,2)
094      XB=WI*(YPN-YPL)/DSC
095      YB=-WI*(XPN-XPL)/DSC
096 C
097 C          DRAW THE TICK MARK ON THE RAY
098 C
099      CALL PLOT (XPN+XB,YPN+YB,2)
100      CALL PLOT (XPN-XB,YPN-YB,2)
101      CALL PLOT (XPN,YPN,2)
102 303  IF (KTWO .EQ. LAST) GO TO 106
103      KTWO=KTWO+KADD
104      GO TO 105
105 106  IF (KADD .GE. 0) GO TO 108
106      IF (NFAN .NE. 0) GO TO 205
107      CALL NUMBER (AX(1)/DY,AY(1)/DY,0.1,XN,0.0,-1)
108      GO TO 205
109 108  IF (NFAN .EQ. 0) GO TO 205
110 C
111 C          NUMBER THE RAY AT THE TERMINAL POINT
112 C
113      CALL NUMBER (AX(KMAX)/DY,AY(KMAX)/DY,0.1,XN,0.0,-1)
114 205  RETURN
115      END

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116      SUBROUTINE IOSET
117 C
118 C          PURPOSE
119 C
120 C          THIS SUBROUTINE SETS UP THE I/O FILES FOR THE VARIOUS
121 C          WAVPAK ROUTINES. THE USER IS ASKED FOR EACH FILE NAME,
122 C          WHICH IS THEN OPENED AND MADE READY FOR I/O. THIS IS
123 C          THE ONLY TOTALLY VAX DEPENDENT SUBROUTINE, AND MAY BE
124 C          REPLACED BY THE APPROPRIATE JOB CONTROL LANGUAGE ASSIGNMENTS
125 C          FOR THE PARTICULAR MACHINE USED.
126 C
127 C          SUBROUTINES REQUIRED
128 C
129 C          NONE
130 C
131      CHARACTER*20 FILE_NAME
132 C

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```

133 C          FIRST, SET UP THE DATA INPUT FILE NAME
134 C
135          TYPE 100, '$ENTER THE CONTROL FILE NAME '
136          READ(5,100) FILE_NAME
137          CLOSE(UNIT=1)
138          OPEN(UNIT=1,NAME=FILE_NAME,TYPE='OLD',DEFAULTFILE=',CTL')
139 C
140 C          NOW THE WATER DEPTH GRID INPUT FILE
141 C
142          TYPE 100, '$ENTER WATER DEPTH GRID FILE NAME <NONE> '
143          READ(5,100) FILE_NAME
144          IF (FILE_NAME .EQ. ' ') GOTO 20
145          CLOSE(UNIT=2)
146          OPEN(UNIT=2,NAME=FILE_NAME,TYPE='OLD',DEFAULTFILE=',GRD')
147 C
148 C          NOW THE CURRENT SPEED INPUT FILE
149 C
150 20        CONTINUE
151          TYPE 100, '$ENTER CURRENT SPEED GRID FILE NAME <NONE> '
152          READ(5,100) FILE_NAME
153          IF (FILE_NAME .EQ. ' ') GOTO 30
154          CLOSE(UNIT=3)
155          OPEN(UNIT=3,NAME=FILE_NAME,TYPE='OLD',DEFAULTFILE=',GRD')
156 C
157 C          NOW THE OUTPUT FILE NAME
158 C
159 30        TYPE 100, '$ENTER THE OUTPUT FILE NAME '
160          READ(5,100) FILE_NAME
161          CLOSE(UNIT=6)
162          OPEN(UNIT=6,NAME=FILE_NAME,TYPE='NEW',DEFAULTFILE=',OUT')
163 C
164 C          NOW THE PLOT FILE NAME
165 C
166          TYPE 100, '$ENTER THE PLOT FILE NAME <NONE> '
167          READ(5,100) FILE_NAME
168          IF (FILE_NAME .NE. ' ') GOTO 10
169          CLOSE(UNIT=9)
170          OPEN(UNIT=9,NAME='NL:DUMMY.PLT',STATUS='NEW',
171             1  CARRIAGECONTROL='LIST')
172          RETURN
173 10        CLOSE(UNIT=9)
174          OPEN(UNIT=9,NAME=FILE_NAME,STATUS='NEW',CARRIAGECONTROL='LIST',
175             1  DEFAULTFILE=',PLT')
176          RETURN
177 100      FORMAT(A)
178          END

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001          SUBROUTINE PRTPRM(NPLOT)
002 C
003 C          PURPOSE
004 C

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005 C           THIS SUBROUTINE PRINTS THE PARAMETERS READ FROM THE
006 C           CONTROL FILE.  THE RAY PARAMETERS ARE NOT READ AT THIS
007 C           TIME.
008 C
009 C           SUBROUTINES REQUIRED
010 C
011 C           NONE
012 C
013 C           IMPLICIT REAL*8 (A-H,O-Z)
014 C
015 C           DIMENSION CONTURD(9),CONTURC(9),EM(6,12),S(6,6),CONTURC1(9)
016 C           DIMENSION C(12),E(6),EX(6),EY(6),CONTURD1(9),CX(12),CY(12)
017 C
018 C           COMMON /PRTCOM/ HT,MXPLOT,NOR,NPT,NAX,NSH,NCO,NCC,NXCHAT,
019 C           1             MM,NN,NNSKIP
020 C
021 C           COMMON /MAICOM/ ALFA,AMM,ANN,CF,CIN,CNURSA,CONTURD,DATE1,DATE2,
022 C           1             DCON,DELTAT,DIR,DY,EM,GRID,HGTZ,AKRTOL,PROJECT,
023 C           2             S,SDLTAT,NSK,TT,NWBRK,NBRKUP,NFAN,NFLAGR,
024 C           3             NOLINE,IFLG,MOE,NFLECT,NFRACT,NRFLBU,NRFRBU,NROPT
025 C
026 C           COMMON /RAYCOM/ BDZ,C,CX,CY,D,DELA,DEP,UGDX,DHDX,E,EX,EY,G,GZERO,
027 C           1             HGT,AKFC,AKR,AKS,POT,PREV,P1,P2,P3,P4,P5,QOT,Q1,
028 C           2             Q2,Q3,Q4,Q5,PU,SUU,PDEP,SPREV,GTZERO,
029 C           3             PALFA,SVAU,PG,U,V,IHGT,
030 C           4             NTOREF,INUM,MAXQ,NUMT,NOREF
031 C
032 C           COMMON /SRFCOM/ ND,NC,CCON,TTT,ARAY,GR,GT,SARAY,PZ,PZD,
033 C           1             CALFA,PCALFA,PARAY,PREVT,SPREVT,VT,SVT,ASV,
034 C           2             Z,ZD,BZ,KMAX,PX,PY,PTTT,PANGLE,PGR,PPCTD,PPCTCX,
035 C           3             PPCTCY,PGT,SVBZ,SVBDZ,KNUMT,KRFLBU,KRFRBU,CDGDX,
036 C           4             UMX,AGR,PGAM,PBZ,PRDZ,PFK,PV,PVT
037 C
038 C           COMMON/NUMCOM/CONTURC
039 C
040 C           SOME LOCAL THINGS
041 C
042 C           REAL*4 YES,NO,YESNO,INCH,CENTIM,INCH
043 C
044 C           DATA YES,NO,INCH,CENTIM/'YES ','NO ',' IN ',' CM '/
045 C
046 C           REAL*8 METRIC,ENGLIS,METENG,FEET,METERS,FETMET
047 C
048 C           DATA METRIC,ENGLIS,FEET,METERS/'METRIC ','ENGLISH ',' FEET ',
049 C           1             ' METERS '/
050 C
051 C           SET UP UNIT IDENTIFIERS.  DEFAULT IS ENGLISH
052 C
053 C           INCH = INCH
054 C           METENG = ENGLISH
055 C           FETMET = FEET
056 C           DCON1 = DCON
057 C           GRID1 = GRID

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058      CIN1 = CIN
059      IF (MOE .EQ. 0) GO TO 10
060 C
061 C          MOE <> 0 => UNITS ARE METRIC
062 C
063      INCH = CENTIM
064      METENG = METRIC
065      FETMET = METERS
066      DCON1=DCON*0.3048
067      GRID1=GRID*0.3048D0
068      CIN1=CIN*3600D0
069      IF (ND .EQ. 0) GO TO 20
070      DO 4000 I=1,NCO
071          CONTURD1(I)=CONTURD(I)/DCON
072 4000 CONTINUE
073 20      IF (NC .EQ. 0) GO TO 10
074      DO 3000 I=1,NCC
075          CONTURC1(I)=CONTURC(I)/CCON
076 3000 CONTINUE
077 C
078 C          FIRST SET OF DATA
079 C
080 10      WRITE(6,100) NPLOT,PROJCT,DATE1,DATE2,DIR,MXPLOT,METENG
081 C
082 C          THE MEANING OF NPT HAS BEEN CHANGED.
083 C
084 C
085 C          SECOND SET.  IF NPT = 0, THEN DON'T PRINT INTERMID. RAY DATA
086 C
087      YESNO = YES
088      IF (NPT .EQ. 0) YESNO = NO
089      WRITE(6,200) NOR,YESNO,NSK,CIN1,HT,INCH
090 C
091 C          THIRD SET.  MAX = 0 => NO CALIBRATE AXIS
092 C
093      YESNO = YES
094      IF (MAX .EQ. 0) YESNO = NO
095      WRITE(6,300) YESNO
096 C
097 C          FOURTH SET.  NSH = 0 => DON'T PLOT SHORELINE
098 C
099      YESNO = YES
100      IF (NSH .EQ. 0) YESNO = NO
101      WRITE(6,400) YESNO
102 C
103 C          FIFTH SET.
104 C
105      IF (ND .EQ. 0) GO TO 30
106      WRITE(6,500) NCO
107 30      IF (NC .EQ. 0) GO TO 40
108      WRITE(6,510) NCC
109 C
110 C          SIXTH SET.  IF NXCHAT = 0 THEN READ A NEW CMATRIX

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111 C
112 40  YESNO = NO
113     IF (NXCMAT .EQ. 0) YESNO = YES
114     WRITE(6,600) YESNO
115     IF (NXCMAT .EQ. 0) WRITE(6,610) MM,NN,GRID1,FETMET
116 C
117 C           SEVENTH SET.
118 C
119     WRITE(6,700) CNVRSR,DCON1,CCON,MNSKIP
120 C
121 C           EIGHTH SET
122 C
123     IF (ND .EQ. 0) WRITE(6,710) DEP
124     IF (ND .NE. 0) WRITE(6,720)
125     ZDPRIM = (CNVRSR + 180.0) - (ZD/1.74532925D-2)
126     IF (NC .EQ. 0) WRITE(6,730) Z,ZDPRIM
127     IF (NC .NE. 0) WRITE(6,740)
128 C
129 C           LAST SET -- CONTURS IF NEEDED
130 C
131     IF (NCC .NE. 0) WRITE(6,920) METENG,(CONTURC1(I),I=1,NCC)
132     IF (NCO .NE. 0) WRITE(6,930) METENG,(CONTURD1(I),I=1,NCO)
133 C
134 C           AND SPLIT BACK TO THE SALT MINES
135 C
136     RETURN
137 100  FORMAT('1WAVPAK -- WAVE PACKET TRAJECTORY ANALYSIS PROGRAM V2.0'//
138     1' SYSTEM PARAMTERS FOR PLOT NUMBER ',I2,':'//
139     2'     PROJECT NAME ..... ',A6/
140     3'     PROJECT DATE ..... ',2A6/
141     4'     PLOT IDENTIFICATION LABEL ..... ',A6/
142     5'     NUMBER OF RUNS TO BE MADE ..... ',I3//
143     6'     DATA UNITS ..... ',A8)
144 200  FORMAT('     NUMBER OF RAYS TO BE RUN ..... ',I3/
145     1'     PRINT INTERMEDIATE RAY RESULTS ..... ',A4/
146     2'     INTERMEDIATE RAY RESULT INTERVAL ..... ',I3/
147     3'     RAY TICK MARK SPACING ..... ',F8.3,' SEC'/
148     4'     PLOTTER Y-AXIS LENGTH ..... ',F8.3,A4)
149 300  FORMAT('     CALIBRATE AND LABEL AXES ..... ',A4)
150 400  FORMAT('     PLOT SHORELINE ..... ',A4)
151 500  FORMAT('     NUMBER OF SOUNDING DEPTHS ..... ',I3)
152 510  FORMAT('     NUMBER OF CURRENT SOUNDINGS..... ',I3)
153 600  FORMAT('     READ A NEW GRID ..... ',A4)
154 610  FORMAT('     GRID DIMENSIONS ..... ('
155     1'                                     ,I3,',' ,I3,')'//
156     2'     GRID SPACING ..... ',1PE10.3,A8)
157 700  FORMAT('     RAY CONVERSION ANGLE ..... ',F8.3/
158     1'     WATER DEPTH CONVERSION FACTOR..... ',1PE10.3/
159     2'     CURRENT SPEED CONVERSION FACTOR ..... ',1PE10.3/
160     3'     SOUNDING INCREMENT ..... ',I3)
161 710  FORMAT('     WATER DEPTH GRID SPECIFIED ..... NO'/
162     1'     WATER DEPTH CONSTANT ..... ',1PE10.3)
163 720  FORMAT('     WATER DEPTH GRID SPECIFIED ..... YES')

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164 730  FORMAT('      CURRENT GRID SPECIFIED ..... NO')
165      1'      INITIAL CURRENT SPEED ..... ',1PE10.3/
166      2'      INITIAL CURRENT DIRECTION ..... ',1PE10.3)
167 740  FORMAT('      CURRENT GRID SPECIFIED ..... YES')
168 920  FORMAT('OSOUNDING CURRENT SPEED (',A6,'): '//6X,9F10.2)
169 930  FORMAT('OSOUNDING WATER DEPTHS (',A6,'): '//6X,9F10.2)
170      END
```

CHAPTER IV USING THE COMPUTER PROGRAM

4.1 Preparation of the Water Depth Grid. Once a coastal area is selected for making wave forecasts a water depth grid must be prepared. Details with numerous illustrations for preparing water depth grids are given by Wilson (1966). It is necessary to obtain charts of the region of interest containing sufficiently detailed bathymetric information.

A water depth grid is rectangular in shape. The value of x varies between 0 and AMM while y varies from 0 to ANN . The values of AMM and ANN are defined by

$$AMM = MM - 1 \quad (4-1)$$

$$ANN = NN - 1 \quad (4-2)$$

where MM is the number of water depth values in a y -column and NN is the number of columns. The value of MM must be an integral multiple of 16. If another number is preferred the format statement in the computer program used to input the water depth values must be changed. The maximum values of MM and NN depend upon the storage capacity of the computer. In the computer program presented in this report the values of MM and NN are assumed not to exceed 120. If the grid requirements exceed the storage capacity of the computer the coastal region of interest can be divided into several overlapping grids.

The xy -coordinate system is right-handed with the x -axis usually extending seaward. The direction of the x -axis with respect to true north is defined as $CNVRSA$. The use of $CNVRSA$ makes it possible to define the input and output wave directions with respect to true north.

The distance between water depths in the x - or y -directions is a grid interval or grid unit and is denoted by $GRID$. This distance must be small enough for the water depth grid to describe adequately the bottom topography. If it is desirable for rays to start in deep water the grid must extend at least several grid units seaward of the deep water depth of the largest wave period of interest. In this report deep water is defined as any depth greater than $0.64 \lambda_d$ where λ_d is the deep water wavelength. This definition of deep water is chosen since the group speed is nearly invariant for greater water depths in the absence of currents.

To determine the location of the water depths to be read from a chart lines can be drawn on tracing paper parallel to the x - and y -axes of the grid and separated a distance equal to a grid unit. The tracing paper is placed on the chart and water depths are estimated for the points defined by the intersection of the grid lines. The water depths can be recorded in any system of units.

One of the program options is to have the shoreline drawn on a plot.

In order for the location of the shoreline to be computed it is necessary to determine negative values of water depths for at least two grid points landward of the shoreline. The negative values are determined by drawing the reflection of water depth contours on land with respect to the shoreline. Zero water depths can be used to fill out a column for grid points more than two grid units landward of the shore.

4.2 Preparation of the Current Grid. The current grid is prepared in a similar fashion to the water depth grid. The current grid contains both the x- and y-components of the current. The x-component current values follow the y-component values. The component values of the current can be either positive or negative, depending on the nature of the current. Both the x- and y-component values in the grid must have identical values of MM and NN. Any system of units can be used to record the current. As in the case of water depths, the grid unit spacing is denoted by GRID. If there is both a water depth grid and a current grid, the values of MM, NN, and GRID must be the same for both grids. It is not possible to determine a shoreline for a current.

4.3 Preparing a Computer Run. The way in which data is prepared for a computer run is illustrated on the coding form in Figure (4-1). Eight types of computer cards are used. The columns available for each parameter are outlined by rectangles. The positions of decimal points for real numbers are indicated. If there is no decimal point the number is an integer and is placed in the rectangle as far to the right as possible. The input parameters must appear on each card as shown, and the card types must be in the order indicated.

For the first type of computer card, MXPLOT is the number of runs for a given operation of the computer program. The PROJCT is a 6-character label of any combination of letters and numbers. The label can be used, for example, to indicate a project number. An alternative use is to identify which water depth grid is used for the run. It appears in both the printed output and on the plot. DATE1 and DATE2 are used to date the run. DATE1 can be used for the year and the month in the form ZZ/YY/. DATE2 can be used for the day in the form XX. The DIR is another 6-character label of any combination of letters and numbers. This label appears only on the plot. One possible label is WAVPAK, which can denote that wave packet trajectories are presented. If the rays have a common initial direction, DIR can be used to indicate that direction.

The number of rays for a given run, NOR, is input on the second type of computer card. The values of NPT and NSK determine the amount of printed output. If NPT is zero there is only one line of printout of the ray particulars for a given ray point. If NPT is not zero there are two lines of printout of the ray particulars (described in the next section). Printout occurs for the first ray point, those points which are an integral multiple of NSK, and the last point. The value of HT is the length of the y-axis of the plot in inches or centimeters. If CIN is not zero tick marks are placed on the rays at equal intervals of travel time given by the value of CIN in seconds. If no tick marks are desired CIN is zero.

The x- and y-axes of the plot will be calibrated and labeled if NAX is not zero. If NAX is zero the plot borders are drawn but the axes are not calibrated. The shoreline is drawn on the plot if NSH is not zero. If the shoreline is not desired NSH must be zero. In order to have a shoreline

there must be a water depth grid (CMAT). It must be prepared for a shoreline as described in Section (4.1). The number of sounding water depths for a plot is NCO. There cannot be more than 9 sounding depths, and they are input on the CONTURD computer card. If NCO is zero there are no sounding depths; in this case the CONTURD card must be removed from the input. In the same manner, NCC is the number of current speed contours for a plot. The contour values are input on the CONTURC card. Up to nine values can be placed on the card. If no current speed contours are desired the CONTURC card must not appear in the input and NCC must equal zero. The value of NNSKIP is the amount by which y is incremented in selecting columns for locating water depth and current speed contours. For example, if NNSKIP is 15 and NN is 64, sounding water depths are located for the 2, 17, 32, 47, and 62 y -columns. Current speed contours are located for the 4, 19, 34, and 51 y -columns.

If a water depth grid, a current grid, or both are to be read in the input for the computer run the value of NXCMAT is zero. If NXCMAT is not zero the grids for the previous run are used again. This situation can arise if MXPLOT is greater than one. If English units are to be used in the input and output MOE is zero. If MOE is not zero Metric units are used.

The third type of computer card contains the input dimensions for the water depth grid. A description of the quantities MM, NN, CNVRSR, and GRID are described in the previous sections of this chapter. The angle CNVRSR is given in degrees and GRID is given in feet or meters. The value of DCON is chosen so that the product of DCON and a water depth in CMAT yields a value with units of feet or meters.

A water depth value in feet or meters is read in the input as DEP. This value determines the water depth for a current grid if there is no water depth grid. If there is a water depth grid the value of DEP is replaced by values determined from the water depth grid. If a water depth grid is to be read in the input ND must equal one. Otherwise ND equals zero.

The value of CCON is chosen so that the product of CCON and a component current speed value in the current grid produces a value with units of feet/second or meters/second. A current speed magnitude can be input as Z and the current direction as ZD. These values represent a constant current to be used with a water depth grid provided there is no current grid. The values of Z and ZD are replaced with values determined from a current grid if one exists. If a current grid is to be read in the input NC must equal one. If NC equals zero no current grid is read.

The fourth type of computer card is used to input the water depth grid (CMAT). The units of CMAT determine the value of DCON. There are 16 water depths on each card. The water depths are entered column by column starting with the first column. There are NN columns. In each column the water depths are entered starting with the land values, if any, and proceeding seaward. There are MM values per column. The format for entering the water depths does not include numbers beyond the decimal points. Near shore it may be desirable to record water depths to the nearest tenth of a foot or meter. On some computer systems it is possible to enter data routinely in this form with the indicated format for CMAT being overridden. If such a capability is not available it may be desirable to alter the format statement for CMAT in WAVPAK.

If NCO is not zero the CONTURD computer card is used to input the sounding water depths in feet or meters. The number of sounding depths must agree with NCO which should not exceed 9. If NCO is zero the CONTURD card must be removed.

The current grid contains both CURX and CURY, and it appears as input on the sixth type of computer card. The CURY values precede the CURX values. The numbers are placed on the cards in the same manner as described for the CMAT cards.

The seventh type of computer card is CONTURC, and it contains the current speed contour values in feet/second or meters/second. The number of contour values must be equivalent to NCC. There cannot be more than 9 values. The CONTURC card must not appear in the input if NCC is zero.

The eighth type of computer card is used to input the particulars for each ray. There must be as many ray cards as declared in the input for NOR. The initial time step interval between ray points in seconds is DELTAT. The initial wave period in seconds is TT, and X, Y are the initial ray coordinates. The initial ray points should be at least two grid units from a grid boundary. The initial wave packet and wavelet directions are A and AV, respectively. The directions are in degrees and are the directions from which the waves come with respect to true north. The initial wave height in feet or meters is HGTZ.

The friction factor is CF. The value of AKRTOL determines the accuracy of the calculations of the refraction coefficient with the exception of near reflection points. As a general rule, if accuracy is required to the second decimal point AKRTOL is 0.01. If accuracy is desired to the third decimal point AKRTOL is 0.001.

To continue a ray beyond a reflection point NROPT is set unequal to zero. If NROPT is zero a ray is stopped at a reflection point. A test is made to determine if a wave breaks if NWBRK is not zero. If NWBRK is zero there is no test to determine if a wave breaks. If the ray is to be numbered at its terminal point NFAN is set unequal to zero. A group of rays should be numbered at their terminal points if they have a common origin. If NFAN is zero the ray is numbered at its initial point.

A sample of input data for a computer run with 6 rays is shown in Figure (4-2). Since the water depth contours are parallel, only one of the 64 columns of water depth values is shown in the rectangle labeled CMAT. The current speed contours also are parallel. The rectangle labeled CURY shows the current values for a column. The CURX values, which also must appear in the input, are all zero. Computer outputs for these data are presented in Section (4.6). Therefore, if desired, these input data can be used to check the computer program.

4.4 The Printed Output. At the beginning of each printout is a summary (Figure (4-4)) of the input information common to all the rays. The next thing that appears in the printout is the page heading. This contains the PROJCT, date, plot number, input wave period, ray number, input time step, friction factor, and AKRTOL. If at the first ray point this is followed by a statement denoting whether English or Metric units are used in the output. The column headings appear next in the output. Beyond the first point of a ray the page and column headings occur after every 50 lines of additional printout.

The column headings identify the ray particulars which appear in the output. They contain the ray point number MAX, the ray coordinates X, Y, and the water depth DEPTH in meters or feet. The current speed CUR:SP is in meters/second or feet/second, and the current direction CUR:DI is in degrees. The Doppler shifted wave period appears in the output as PERIOD. The ray, wave packet,

and wavelet directions are denoted, respectively, by RAY, PACK, and WAVE. These are the directions in degrees from which the waves come with respect to true north. The geometric group speed is given by G, and the ray speed is specified by GR. The units are in meters/second or feet/second. The wave height is HGT in meters or feet. The shoaling coefficient is identified by KS, and KF represents the friction coefficient. The refraction coefficient is defined by KR.

There is an additional line of printout if NPT is unequal to zero. This line contains fourteen ray particulars. The angle in degrees by which the x'y'-coordinate system (water depths) is rotated with respect to the positive x-axis for computations is given by ROTAT:D. An estimate of how well the computed water bottom surface fits the actual water depths is given by PCT:D (see page 59). The smaller the value the better the fit. The angle in degrees by which the x''y''-coordinate system (currents) is rotated with respect to the positive x-axis for computations is denoted by ROTAT:C. The quantities PCT:CX and PCT:CY are estimates of how well the surface fit derived x- and y-component current values, respectively, agree with the actual values (see page 59). The speed of the advected group front is GT, the conventional group speed is U, the phase speed is V, and the speed of the advected wavelet front is VT. These speeds have units of meters/second or feet/second. The ray separation factor is specified by BETA, and the time derivative of the ray separation factor is given by DBETA/DT. The type of time step breakup, should one occur, is shown as BRK UP. If the breakup is to maintain accuracy in the refraction calculations, BETA appears in the output. If the breakup is to keep the change in PACK to less than one degree between successive ray points near a reflection point, REFLECT appears in the printout. The number of intervals the input time step is divided into is denoted by NO. Finally, the wave packet ray curvature is given as CURVATURE in radians per grid unit.

The travel time along the wave packet trajectory does not appear in the output. However, it can be determined by subtracting one from MAX and multiplying the result by the input time step.

The ray particulars are printed out for the first ray point, those points which are an integral multiple of SK, and the last point. Printout occurs for a reflection point should one occur. Note that the number of ray points, NO, which occur when there is a breakup of the input time step interval is not counted in MAX. There is no printout for ray points which occur within a breakup.

A number of descriptive printouts appear with the ray particulars when certain types of calculations occur or when a ray terminates. If the packet ray curvature has not converged after fifty iterations the ray curvatures of the 48th and 50th iterations are compared to see if they are nearly the same. If so, the ray curvature is assumed to have converged to two values. This would happen if estimates of the new ray point alternate between two grid cells. For this situation, the average of the ray curvature averages for the 49th and 50th iterations is determined and is used to locate the next ray point. When this happens the following type of printout appears.

(1) MAX= 123, PACKET CURVATURE AVERAGED

If NSK > 1 this descriptive printout occurs even if there is no printed output of the ray particulars.

When there is a reflection one of three types of descriptive printouts occurs (Sections (2.1), f and g).

- (2) MAX= 123, REFLECTION: SNELLS LAW WITH PHASE VELOCITY
- (3) MAX= 123, REFLECTION: PACKET CURVATURE ITERATION NOT CONVERGING
- (4) MAX= 123, REFLECTION: NEAR REFLECTION POINT

The ray point where one of these three descriptive printouts occurs is the last ray point if NROPT = 0.

When a ray terminates one of the following descriptive printouts can appear in the output.

- (5) DIMENSION OF OUTPUT-ARRAYS EXCEEDED
- (6) RAY REACHED SHORE
- (7) RAY REACHED GRID BOUNDARY
- (8) PACKET CURVATURE ITERATION NOT CONVERGING
- (9) CAUSTIC OR FOCAL POINT
- (10) WAVE BREAKS
- (11) REFLECTION HAND-UP
- (12) BREAKUP TIME STEP LESS THAN 0.5 SECOND

Printout (5) occurs if the sum of the number of ray points and tick marks is equal to or greater than the array dimension MMAX. Printout (6) is obtained if the water depth becomes zero or negative. Printout (7) results if the ray point is within 1.5 grid units of a grid boundary. The conditions for a reflection point are not satisfied if Printout (8) occurs. Printout (9) is produced if the ray separation factor becomes less than 0.0001. The condition for Printout (10) is given in Section (2.5). Printout (11) is obtained if there are successive reflections at the same ray point. Printout (12) can occur if the calculation time step becomes too small in either calculating the ray path near a reflection point (Section (2.1), f) or in calculating the ray separation factor (Section (2.3), c).

4.5 The Plots. Each plot contains a label consisting of PROJECT, the date, the scale factor, the time in seconds between tick marks on a ray, if any, the plot number, and DIR. If NAX \neq 0 the axes of the plot are calibrated and labeled. If NSH \neq 0 the shoreline is drawn. Each ray is numbered. If FAN = 0 the number appears at the initial ray point, and if FAN \neq 0 the ray is numbered at its terminal point. If NCO \neq 0 sounding water depth values are labeled. A "D" appears after the number to indicate a water depth. If NCC \neq 0 current contour values are labeled. The number is followed by a "C" to signify a current value.

4.6 Examples of Computer Output. Several computer runs were made using the data presented in Figure (4-2). The six rays shown in the figure were

determined for the given water depth grid (CMAT). Each column of CMAT is the same as shown in Figure (4-2). A plot of the rays appears in Figure (4-3). Figure (4-4) shows a summary of the input parameters which are common to all the rays for this run. Figures (4-5) through (4-10) contain the printed output for the six rays. The examples illustrate rays beginning both at an intermediate water depth and in deep water. Three different wave periods are considered. The second ray undergoes a reflection (Section (2.1), f and Section (2.3), d). For the last two rays the friction factor is assumed to be zero. Tick marks and sounding water depths are shown on the plot.

The first and last rays for the data shown in Figure (4-2) were computed for the given current grid. Only the values for a column of CURY are shown. The CURX values are all zero. Figure (4-11) is a plot of the rays, and the printed output is presented in Figures (4-12) and (4-13).

For an additional comparison, the first and last rays in Figure (4-2) were computed for the given water depth and current grids. The resulting plot is seen in figure (4-14), and the listing of the rays is given in Figures (4-15) and (4-16).

In Figure (4-17) the period of the wave packet trajectories is 14.0 seconds and they begin in deep water. The water depth contours are sinusoidal with an amplitude of 5 kilometers and a wavelength of 20 kilometers. GRID has a value of 312.5 meters.

This example is quite interesting since there is decidedly more energy in the bay than at the headland. The opposite result would be expected for monochromatic trajectories. The refraction of wave packets could explain why there is more erosion in bays than at headlands for some coastlines. Figures (4-18) through (4-20) show the printed output for rays number 4, 8, and 16, respectively, of Figure (4-17). The computed refraction coefficients agree favorably with values estimated from the plot.

Figure (4-21) shows a portion of the Gulf of Mexico off the southwestern Florida coast. A water depth grid was prepared for this region with GRID = 14886.2 feet (4.537 km) and CNVRS = 180°. A ray plot for this region is shown in Figure (4-22). The first two rays start at an intermediate water depth, whereas the remaining rays begin in deep water. Figure (4-23) displays printed output for the first portion of ray number 1. Since the water depth contours are not parallel there is a variation in ROTAT:D.

Ray number 2 has a reflection. Figure (4-24) shows a listing of the ray particulars near the reflection point. The wave packet and wavelet angles in the xy - and $x'y'$ -coordinate systems are defined by Equations (3-1), (3-2), (2-111), and (2-112). At the reflection point the angles in the xy -coordinate system are $\theta_C = 275.22^\circ$ and $\gamma_C = 2.50^\circ$. In the $x'y'$ -coordinate system $\theta' = 2.21^\circ$ and $\gamma' = 89.49^\circ$.

Ray number 12 illustrates the importance of examining the ray particulars in the printout. Figure (4-26) shows the printed output for this ray. A message in the output states there is a reflection. However, a reflection is not likely since DEPTH, θ' , γ' , CURVATURE, and G do not exhibit the behavior characteristic of a reflection. At the ray point where the reflection is indicated $\theta' = 115.33^\circ$ and $\gamma' = 117.07^\circ$. This false reflection is the result of a large change in ROTAT:D between successive ray points. When this occurs the water depth grid is not sufficiently detailed to adequately represent the changing water depth contours.

Figure (4-25) is the printout for ray number 6 of Figure (4-22). This is an example of a ray which reached shore.

PROJ. NO. PAR 2 , 82/09/15
SCL = 1/310039 ; CIN = 300
PLOT NO. 1 , DIR. = WAVPAK

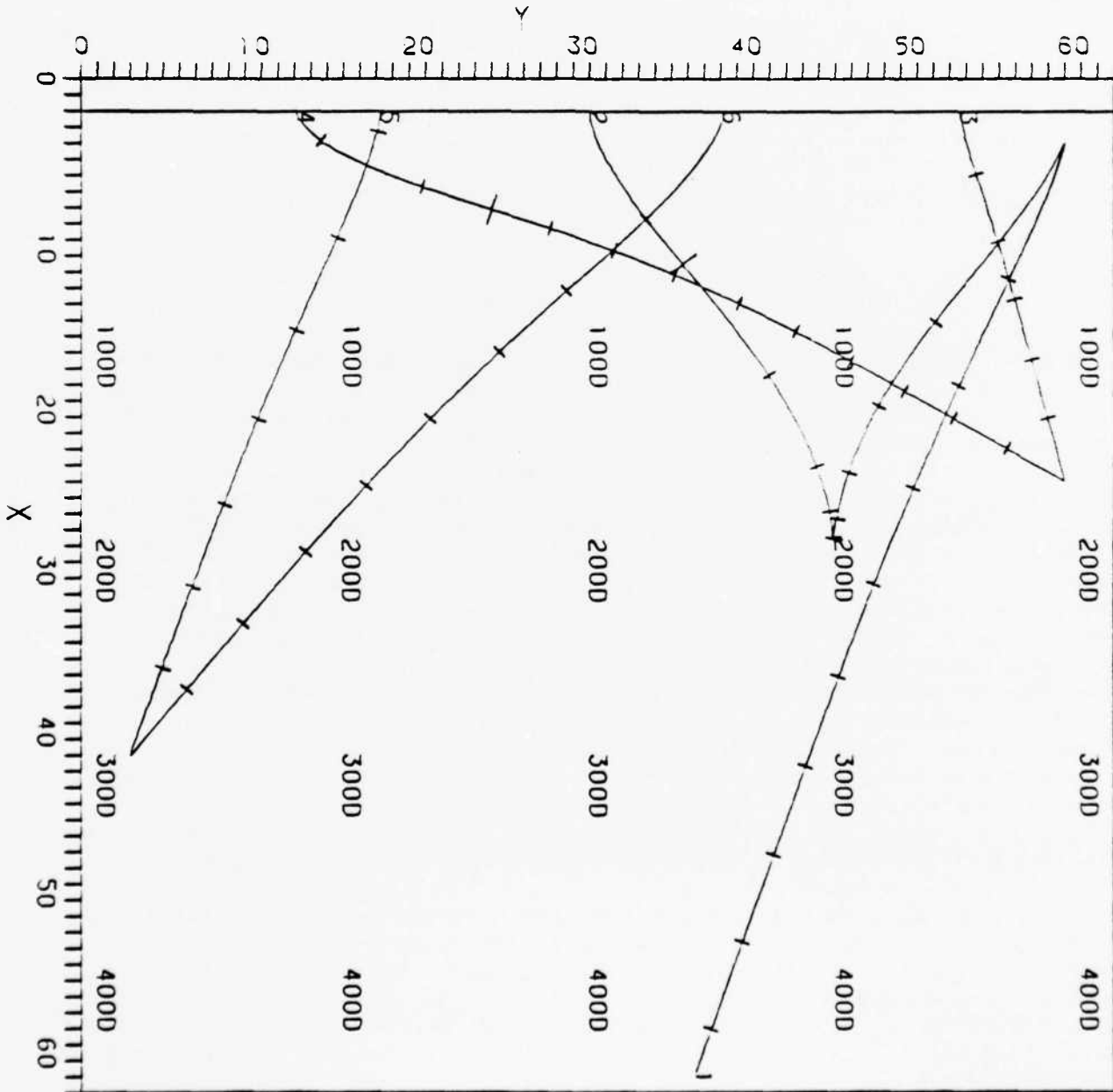


Figure (4-3). PLOT FOR SAMPLE INPUT DATA FOR WATER DEPTH GRID

WAVPAK -- WAVE PACKET TRAJECTORY ANALYSIS PROGRAM V2.0

SYSTEM PARAMETERS FOR PLOT NUMBER 1:

PROJECT NAME	PAR 2
PROJECT DATE	82/09/15
PLOT IDENTIFICATION LABEL	WAVPAK
NUMBER OF RUNS TO BE MADE	1
DATA UNITS	METRIC
NUMBER OF RAYS TO BE RUN	6
PRINT INTERMEDIATE RAY RESULTS	YES
INTERMEDIATE RAY RESULT INTERVAL	10
RAY TICK MARK SPACING	300.000 SEC
PLOTTER Y-AXIS LENGTH	6.000 IN
CALIBRATE AND LABEL AXES	YES
PLOT SHORELINE	YES
NUMBER OF SOUNDING DEPTHS	4
READ A NEW GRID	YES
GRID DIMENSIONS	(64, 64)
GRID SPACING	2.286E+02 METERS
RAY CONVERSION ANGLE	180.000
WATER DEPTH CONVERSION FACTOR.....	3.048E-01
CURRENT SPEED CONVERSION FACTOR	1.000E-02
SOUNDING INCREMENT	15
WATER DEPTH GRID SPECIFIED	YES
CURRENT GRID SPECIFIED	NO
INITIAL CURRENT SPEED	0.000E+00
INITIAL CURRENT DIRECTION	2.700E+02

SOUNDING WATER DEPTHS (METRIC):

100.00 200.00 300.00 400.00

Figure (4-4). SUMMARY OF INPUT PARAMETERS COMMON TO ALL RAYS

PROJECT NO. PAR 2 , 82/09/15 , PLOT NO. 1, PERIOD= 20.0SEC., RAY NO. 1, DELTAT= 25.00, CF=0.100000, KKTDL=0.001000
 THE OUTPUT IS IN METRIC UNITS. DEPTH:HGT(METER). G,GR:GT,U,V,VT(METER/SECOND).

MAX X ROTAT:D	Y PCT:D	DEPTH ROAT:C	CUR:SP FCT:CX	CUR:DI FCT:CY	PERIOD U	RAY V	PACK VT	WAVE BETA	G DBETA/DI	GR BRK UP	HGT NO	NS CURVATURE	KF	KR
1	4.00	60.00	15.00	0.0000	270.00	20.0000	15.00	15.00	15.00	11.24	11.24	3.0000	1.0000	1.0000
	0.00	0.01	0.00	0.00	11.24	11.24	11.82	11.82	1.0000	-2.198E-04		1	-5.478E-02	1.0000
10	8.10	58.54	45.73	0.0000	270.00	20.0000	22.67	22.67	25.33	16.72	16.72	2.2645	0.8197	0.9003
	0.00	0.01	0.00	0.00	16.72	16.74	19.54	19.54	0.9559	-1.452E-04	BETA	2	-1.631E-02	1.0228
20	13.55	56.07	66.63	0.0000	270.00	20.0000	25.20	25.20	33.03	18.47	18.47	2.1416	0.7800	0.8860
	-0.01	0.01	0.00	0.00	18.47	18.64	24.89	24.89	0.9374	-1.191E-05		1	-1.060E-03	1.0328
30	19.08	53.50	128.08	0.0000	270.00	20.0000	24.49	24.49	37.65	17.97	17.97	2.1559	0.7907	0.8225
	-0.01	0.01	0.00	0.00	17.97	18.46	27.89	27.89	0.9428	4.204E-05		1	4.101E-03	1.0299
40	24.40	51.15	168.02	0.0000	270.00	20.0000	22.95	22.95	40.23	16.90	16.90	2.2073	0.8154	0.8814
	-0.02	0.01	0.00	0.00	16.90	17.70	29.50	29.50	0.9540	4.292E-05		1	4.727E-03	1.0238
50	29.47	49.08	205.98	0.0000	270.00	20.0000	21.59	21.59	41.61	15.95	15.95	2.2599	0.8392	0.8810
	-0.02	0.01	0.00	0.00	15.95	16.98	30.33	30.33	0.9632	3.033E-05		1	3.748E-03	1.0189
60	34.32	47.21	242.37	0.0000	270.00	20.0000	20.63	20.63	42.33	15.29	15.29	2.3009	0.8572	0.8809
	-0.02	0.01	0.00	0.00	15.29	16.46	30.76	30.76	0.9693	1.903E-05		1	2.561E-03	1.0157
70	39.03	45.47	277.69	0.0000	270.00	20.0000	20.02	20.02	42.70	14.86	14.86	2.3290	0.8694	0.8808
	-0.03	0.01	0.00	0.00	14.86	16.11	30.97	30.97	0.9731	1.137E-05		1	1.619E-03	1.0137
80	43.65	43.81	312.33	0.0000	270.00	20.0000	19.65	19.65	42.88	14.61	14.61	2.3467	0.8770	0.8808
	-0.03	0.01	0.00	0.00	14.61	15.90	31.08	31.08	0.9753	6.630E-06		1	9.771E-04	1.0126
90	48.21	42.19	346.57	0.0000	270.00	20.0000	19.43	19.43	42.98	14.46	14.46	2.3575	0.8816	0.8808
	-0.03	0.01	0.00	0.00	14.46	15.77	31.14	31.14	0.9765	3.806E-06		1	5.725E-04	1.0119
100	52.74	40.60	380.55	0.0000	270.00	20.0000	19.30	19.30	43.03	14.37	14.37	2.3637	0.8843	0.8808
	-0.04	0.01	0.00	0.00	14.37	15.69	31.17	31.17	0.9773	2.160E-06		1	3.286E-04	1.0116
110	57.25	39.02	414.34	0.0000	270.00	20.0000	19.25	19.25	43.08	14.27	14.27	2.3717	0.8874	0.8808
	-0.04	0.01	0.00	0.00	14.27	15.60	31.19	31.19	0.9775	1.621E-06		1	0.000E+00	1.0114
120	61.74	37.45	448.01	0.0000	270.00	20.0000	19.25	19.25	43.08	14.27	14.27	2.3717	0.8874	0.8808
	-0.04	0.01	0.00	0.00	14.27	15.60	31.19	31.19	0.9775	1.621E-06		1	0.000E+00	1.0114

RAY REACHED GRID BOUNDARY

Figure (4-5). LISTING FOR RAY NUMBER 1 OF SAMPLE INPUT DATA FOR WATER DEPTH GRID

PROJECT NO. PAR 2 , 82/09/15 , PLOT NO. 1 , PERIOD= 20.0SEC., RAY NO. 2, DELTA I= 25.00, CF=0.100000, KRIDL=0.001000

THE OUTPUT IS IN METRIC UNITS. DEPTH:HGT(METER). G,GR:GT,U,V,VT(METER/SECOND).

MAX X ROTAT:D	Y FCT:D	DEPTH ROTAT:C	CUR:SP FCT:CX	CUR:DI FCT:CY	PERIOD U	RAY V	PACK VF	WAVE BETA	G DRETA/DT	GR BRK UP	HGT NO	KS CURVATURE	KF	KR
1	4.00	60.00	15.00	0.0000	270.00	20.0000	23.00	23.00	11.24	11.24	3.0000	1.0000	1.0000	1.0000
0.00	0.01	0.00	0.00	0.00	11.24	11.24	11.82	1.0000	-5.258E-04			-8.270E-02		
10	7.71	57.86	42.82	0.0000	270.00	20.0000	34.80	38.93	16.40	16.40	2.3481	0.8277	0.8277	0.8938
0.00	0.01	0.00	0.00	0.00	16.40	16.44	19.01	0.8932	-3.608E-04		BETA 2	-2.660E-02		
20	12.34	54.31	77.55	0.0000	270.00	20.0000	38.64	52.41	17.95	17.95	2.2551	0.7912	0.7912	1.0848
-0.01	0.01	0.00	0.00	0.00	17.95	18.48	23.97	0.8498	1.514E-05		BETA 2	9.041E-04		
30	16.94	50.80	112.05	0.0000	270.00	20.0000	34.99	62.93	16.48	16.48	2.2835	0.8257	0.8257	1.0589
-0.01	0.01	0.00	0.00	0.00	16.48	18.65	26.94	0.8919	2.866E-04			2.073E-02		
40	21.12	48.25	143.42	0.0000	270.00	20.0000	27.04	71.13	13.07	13.07	2.4518	0.9273	0.9273	1.0148
-0.01	0.01	0.00	0.00	0.00	13.07	18.19	28.63	0.9711	3.069E-04			3.534E-02		
50	24.47	46.83	168.51	0.0000	270.00	20.0000	18.70	77.32	9.21	9.21	2.8263	1.1043	1.1043	0.9834
-0.02	0.01	0.00	0.00	0.00	9.21	17.69	29.51	1.0340	1.915E-04			4.472E-02		
60	26.82	46.18	186.11	0.0000	270.00	20.0000	11.78	82.02	5.86	5.86	3.5051	1.3842	1.3842	0.9738
-0.02	0.01	0.00	0.00	0.00	5.86	17.34	29.96	1.0545	1.384E-04			5.663E-02		
70	28.23	45.96	196.68	0.0000	270.00	20.0000	6.17	85.80	3.09	3.09	4.8280	1.9080	1.9080	0.9738
-0.02	0.01	0.00	0.00	0.00	3.09	17.14	30.17	1.0545	1.384E-04			9.035E-02		
80	28.81	45.91	201.05	0.0000	270.00	20.0000	1.45	89.03	0.72	0.72	9.9758	3.9463	3.9463	0.9738
-0.02	0.01	0.00	0.00	0.00	0.72	17.07	30.25	1.0545	1.384E-04			3.515E-01		
81	28.83	45.91	201.18	0.0000	270.00	20.0000	1.02	89.32	0.51	0.51	11.9000	4.7083	4.7083	0.9738
-0.02	0.01	0.00	0.00	0.00	0.51	17.06	30.25	1.0545	1.384E-04			4.897E-01		
MAX = 81,														
90	28.24	45.87	196.80	0.0000	270.00	20.0000	173.82	94.19	3.08	3.08	4.8200	1.9086	1.9086	0.9738
-0.02	0.01	0.00	0.00	0.00	3.08	17.14	30.18	1.0545	-1.384E-04			9.312E-02		
100	26.69	45.61	185.19	0.0000	270.00	20.0000	167.61	98.30	6.13	6.13	3.4161	1.3537	1.3537	0.9738
-0.02	0.01	0.00	0.00	0.00	6.13	17.36	29.94	1.0545	-1.384E-04			5.649E-02		
110	24.12	44.85	165.87	0.0000	270.00	20.0000	160.03	103.38	9.75	9.75	2.7488	1.0732	1.0732	0.9892
-0.02	0.01	0.00	0.00	0.00	9.75	17.74	29.44	1.0219	-2.309E-04			4.420E-02		
120	20.53	43.21	138.98	0.0000	270.00	20.0000	151.16	110.02	13.76	13.76	2.4003	0.9036	0.9036	1.0274
-0.01	0.01	0.00	0.00	0.00	13.76	18.27	28.43	0.9474	-3.554E-04		BETA 2	3.368E-02		
130	16.18	40.37	106.32	0.0000	270.00	20.0000	143.44	118.72	16.98	16.98	2.2628	0.8134	0.8134	1.0789
-0.01	0.01	0.00	0.00	0.00	16.98	18.69	26.54	0.8591	-3.066E-04			1.742E-02		
140	11.54	36.70	71.56	0.0000	270.00	20.0000	140.96	129.68	17.95	17.95	2.2421	0.7911	0.7911	1.1076
-0.01	0.01	0.00	0.00	0.00	17.95	18.31	23.29	0.8152	-1.425E-05		BETA 2	-3.288E-03		
150	6.99	33.26	37.44	0.0000	270.00	20.0000	146.36	143.63	15.79	15.79	2.2682	0.8434	0.8434	1.0793
0.00	0.01	0.00	0.00	0.00	15.79	15.81	17.95	0.8584	3.531E-04		BETA 2	-3.330E-02		
160	3.23	31.29	9.26	0.0000	270.00	20.0000	161.43	161.95	9.09	9.09	2.2922	1.1119	1.1119	1.0152
0.00	0.01	0.00	0.00	0.00	9.09	9.09	9.38	0.9703	4.482E-04		BETA 4	-1.169E-01		
167	2.03	31.02	0.25	0.0000	270.00	20.0000	176.88	177.04	1.56	1.56	0.2098	2.6834	2.6834	0.9891
0.00	999.00	0.00	0.00	0.00	1.56	1.56	1.56	1.0222	9.070E-05		BETA 4	-8.165E-01		

Figure (4-6). LISTING FOR RAY NUMBER 2 OF SAMPLE INPUT DATA FOR WATER DEPTH GRID

PROJECT NO. FAR 2 , 82/09/15 , PLOT NO. 1, PERIOD= 12.0SEC., RAY NO. 3, DELTA I= 25.00, CF=0.100000, KRIDL=0.001000

THE OUTPUT IS IN METRIC UNITS. DEPTH,HGT(METER). G,GR,GT,U,V,VT(METER/SECOND).

MAX X ROTAT:D	Y FCT:D	DEPTH ROTAT:C	CUR:SF FCT:EX	CUR:DI FCT:CY	PERIOD U	RAY V	PACK VT	WAVE BETA	G DRETA/DI	GR BRK	HGT UF	NO	KS CURVATURE	KF	KR
1	25.00	60.00	172.49	0.0000	270.00	12.0000	165.00	165.00	9.36	9.36	9.36	3.0000	1.0000	1.0000	1.0000
-0.02	0.01	0.00	0.00	0.00	9.36	9.36	18.72	1.0000	0.000E+00				0.000E+00		
10	22.29	59.27	152.16	0.0000	270.00	12.0000	165.00	165.00	9.36	9.36	9.36	3.0000	1.0000	1.0000	1.0000
-0.01	0.01	0.00	0.00	0.00	9.36	9.36	18.72	1.0000	0.000E+00				0.000E+00		
20	19.26	58.46	129.47	0.0000	270.00	12.0000	164.94	165.02	9.44	9.44	9.44	2.9869	0.9956	1.0000	1.0000
-0.01	0.01	0.00	0.00	0.00	9.44	9.44	18.69	0.9999	-1.237E-06				7.935E-04		
30	16.21	57.63	106.55	0.0000	270.00	12.0000	164.71	165.08	9.59	9.59	9.59	2.9646	0.9878	0.9999	1.0004
-0.01	0.01	0.00	0.00	0.00	9.59	9.59	18.62	0.9991	-5.750E-06				2.073E-03		
40	13.07	56.76	83.04	0.0000	270.00	12.0000	164.12	165.27	9.96	9.96	9.96	2.9116	0.9693	0.9996	1.0017
-0.01	0.01	0.00	0.00	0.00	9.96	9.96	18.39	0.9966	-1.578E-05				4.620E-03		
50	9.78	55.79	58.33	0.0000	270.00	12.0000	162.95	165.92	10.68	10.68	10.68	2.8128	0.9362	0.9970	1.0045
-0.01	0.01	0.00	0.00	0.00	10.68	10.68	17.59	0.9910	-2.741E-05				6.760E-03		
60	6.28	54.68	32.08	0.0000	270.00	12.0000	162.18	167.97	11.14	11.14	11.14	2.7068	0.9165	0.9783	1.0064
0.00	0.01	0.00	0.00	0.00	11.14	11.20	15.08	0.9873	1.885E-05				-3.614E-03		
70	3.08	53.75	8.13	0.0000	270.00	12.0000	167.47	173.18	7.92	7.92	7.92	2.5113	1.0871	0.7750	0.9936
0.00	0.01	0.00	0.00	0.00	7.92	7.96	8.59	1.0130	1.833E-04			BETA 2	-7.620E-02		
76	2.07	53.59	0.52	0.0000	270.00	12.0000	176.51	178.22	2.24	2.24	2.24	0.4574	2.0445	0.0759	0.9822
0.00	999.00	0.00	0.00	0.00	2.24	2.24	2.25	1.0365	8.062E-05			BETA 4	-4.333E-01		

Figure (4-7). LISTING FOR RAY NUMBER 3 OF SAMPLE INPUT DATA FOR WATER DEPTH GRID

PROJECT NO. PAR 2 , 82/09/15 , FLOT NO. 1, PERIOD= 12.0SEC., RAY NO. 4, DELTAT= 25.00, CF=0.100000, KR10L=0.001000
 THE OUTPUT IS IN METRIC UNITS. DEPTH,HGT(METER). G*GR,GT,U,V,VT(METER/SECOND).

MAX X ROTAT:D	Y PCT:D	DEPTH ROTAT:C	CUR:SP PCT:CY	CUR:DI PCT:CY	PERIOD U	RAY V	BACK VT	WAVE RETA	G DBETA/DT	GR BKK UP	HGT NO	KS CURVATURE	KF	KR
1	25.00	60.00	172.49	0.0000	270.00	12.0000	120.00	120.00	120.00	9.36	9.36	3.0000	1.0000	1.0000
-0.02	0.01	0.00	0.00	0.00	9.36	9.36	18.72	18.72	1.0000	0.000E+00		1	0.000E+00	1.0000
10	23.60	57.57	161.96	0.0000	270.00	12.0000	120.00	120.00	120.00	9.36	9.36	3.0000	1.0000	1.0000
-0.02	0.01	0.00	0.00	0.00	9.36	9.36	18.72	18.72	1.0000	0.000E+00		1	0.000E+00	1.0000
20	22.04	54.87	150.27	0.0000	270.00	12.0000	120.00	120.00	120.00	9.36	9.36	3.0000	1.0000	1.0000
-0.01	0.01	0.00	0.00	0.00	9.36	9.36	18.72	18.72	1.0000	0.000E+00		1	0.000E+00	1.0000
30	20.47	52.16	138.55	0.0000	270.00	12.0000	119.88	119.88	120.08	9.41	9.41	2.9919	0.9971	1.0000
-0.01	0.01	0.00	0.00	0.00	9.41	9.41	18.70	18.70	0.9997	-7.194E-06		1	1.753E-03	1.0002
40	18.92	49.43	126.87	0.0000	270.00	12.0000	119.48	119.48	120.16	9.45	9.45	2.9928	0.9951	1.0000
-0.01	0.01	0.00	0.00	0.00	9.45	9.45	18.69	18.69	0.9949	-3.249E-05		1	2.904E-03	1.0025
50	17.38	46.67	115.32	0.0000	270.00	12.0000	118.82	118.82	120.31	9.51	9.51	3.0021	0.9918	1.0090
-0.01	0.01	0.00	0.00	0.00	9.51	9.52	18.66	18.66	0.9823	-7.114E-05		1	4.612E-03	1.0090
60	15.86	43.87	103.98	0.0000	270.00	12.0000	117.80	117.80	120.56	9.61	9.61	3.0245	0.9870	1.0216
-0.01	0.01	0.00	0.00	0.00	9.61	9.62	18.61	18.61	0.9581	-1.246E-04		1	6.874E-03	1.0430
70	14.40	41.00	92.97	0.0000	270.00	12.0000	116.32	116.32	121.01	9.74	9.74	3.0665	0.9804	1.0430
-0.01	0.01	0.00	0.00	0.00	9.74	9.77	18.52	18.52	0.9192	-1.870E-04		1	9.343E-03	1.0749
80	12.99	38.04	82.45	0.0000	270.00	12.0000	114.40	114.40	121.75	9.89	9.89	3.1332	0.9725	1.0749
-0.01	0.01	0.00	0.00	0.00	9.89	9.98	18.38	18.38	0.8654	-2.392E-04		1	1.119E-02	1.1161
90	11.68	34.99	72.58	0.0000	270.00	12.0000	112.22	112.22	122.85	10.06	10.06	3.2223	0.9646	1.1161
-0.01	0.01	0.00	0.00	0.00	10.06	10.23	18.16	18.16	0.8028	-2.530E-04		1	1.138E-02	1.1594
100	10.46	31.84	63.44	0.0000	270.00	12.0000	110.16	110.16	124.39	10.20	10.20	3.3157	0.9580	1.1594
-0.01	0.01	0.00	0.00	0.00	10.20	10.52	17.84	17.84	0.7439	-2.084E-04		1	9.429E-03	1.1922
110	9.33	28.62	54.95	0.0000	270.00	12.0000	108.66	108.66	126.40	10.29	10.29	3.3760	0.9535	1.1922
-0.01	0.01	0.00	0.00	0.00	10.29	10.81	17.40	17.40	0.7035	-1.050E-04		1	5.581E-03	1.1987
120	8.25	25.35	46.86	0.0000	270.00	12.0000	108.08	108.08	128.98	10.33	10.33	3.3553	0.9519	1.1987
0.00	0.01	0.00	0.00	0.00	10.33	11.05	16.80	16.80	0.6959	5.434E-05		1	9.545E-06	1.1646
130	7.17	22.09	38.75	0.0000	270.00	12.0000	108.83	108.83	132.32	10.28	10.28	3.2072	0.9540	1.1646
0.00	0.01	0.00	0.00	0.00	10.28	11.21	15.98	15.98	0.7372	2.945E-04		1	-8.27E-03	1.0796
140	6.00	18.89	30.02	0.0000	270.00	12.0000	111.69	111.69	136.98	10.09	10.09	2.8953	0.9632	1.0796
0.00	0.01	0.00	0.00	0.00	10.09	11.16	14.75	14.75	0.8579	7.182E-04	RETA	2	-2.348E-02	0.9379
150	4.63	15.92	19.73	0.0000	270.00	12.0000	119.07	119.07	144.28	9.49	9.49	2.3865	0.9931	0.9379
0.00	0.01	0.00	0.00	0.00	9.49	10.49	12.62	12.62	1.1369	1.648E-03	RETA	2	-6.291E-02	0.7492
160	2.93	13.65	6.96	0.0000	270.00	12.0000	139.30	139.30	158.31	7.08	7.08	1.5868	1.1501	0.7492
0.00	999.00	0.00	0.00	0.00	7.08	7.48	7.99	7.99	1.7814	3.644E-03	RETA	8	-2.521E-01	
RAY REACHED SHORE														
166	2.07	13.16	0.55	0.0000	270.00	12.0000	167.76	167.76	173.83	2.30	2.30	0.3445	2.0181	0.6594
0.00	999.00	0.00	0.00	0.00	2.30	2.31	2.32	2.32	2.3002	2.125E-03	RETA	16	-1.398E+00	

Figure (4-8). LISTING FOR RAY NUMBER 4 OF SAMPLE INPUT DATA FOR WATER DEPTH GRID

PROJECT NO. PAR 2 , 82/09/15 , PLOT NO. 1, PERIOD= 17.0SEC., RAY NO. 5, DELTAT= 25.00, CF=0.000000, KRIDL=0.001000

THE OUTPUT IS IN METRIC UNITS. DEPTH,HGT(METER). G,GR,GT,U,V,VI(METER/SECOND).

MAX X ROTAT:D	Y PCT:D	DEPTH ROTIAT:C	CUR:SF PCT:EX	CUR:DI PCT:CY	PERIOD GT	RAY U	PACK VT	WAVE BETA	G DRETA/DI	GR BRK UP	HGT NO	KS CURVATURE	KF	KR
1	42.00	3.00	299.99	0.0000	270.00	17.0000	200.00	200.00	200.00	13.26	13.26	3.0000	1.0000	1.0000
	-0.03	0.01	0.00	0.00	13.26	13.26	26.52	26.52	1.0000	0.000E+00		1	0.000E+00	
10	38.25	4.37	271.88	0.0000	270.00	17.0000	200.04	200.04	199.98	13.35	13.35	2.9901	0.9967	1.0000
	-0.03	0.01	0.00	0.00	13.35	13.35	26.49	26.49	1.0000	-7.740E-07		1	-3.987E-04	
20	34.06	5.90	240.45	0.0000	270.00	17.0000	200.18	200.18	199.95	13.44	13.44	2.9804	0.9932	1.0000
	-0.02	0.01	0.00	0.00	13.44	13.44	26.45	26.45	0.9995	-3.374E-06		1	-7.923E-04	
30	29.84	7.46	298.76	0.0000	270.00	17.0000	200.46	200.46	199.88	13.62	13.62	2.9622	0.9865	1.0000
	-0.02	0.01	0.00	0.00	13.62	13.62	26.36	26.36	0.9981	-8.249E-06		1	-1.499E-03	
40	25.54	9.08	176.54	0.0000	270.00	17.0000	200.97	200.97	199.72	13.96	13.96	2.9304	0.9744	1.0000
	-0.02	0.01	0.00	0.00	13.96	13.96	26.16	26.16	0.9951	-1.659E-05		1	-2.615E-03	
50	21.12	10.81	143.43	0.0000	270.00	17.0000	201.85	201.85	199.34	14.53	14.53	2.8807	0.9552	1.0000
	-0.01	0.01	0.00	0.00	14.53	14.53	25.68	25.68	0.9895	-2.803E-05		1	-3.921E-03	
60	16.54	12.71	109.03	0.0000	270.00	17.0000	203.05	203.05	198.49	15.29	15.29	2.8198	0.9312	1.0000
	-0.01	0.01	0.00	0.00	15.29	15.29	24.59	24.59	0.9815	-3.318E-05		1	-4.166E-03	
70	11.77	14.79	73.24	0.0000	270.00	17.0000	203.83	203.83	196.67	15.78	15.78	2.7831	0.9166	1.0000
	-0.01	0.01	0.00	0.00	15.78	15.78	22.24	22.24	0.9763	3.092E-06		1	9.816E-05	
80	7.07	16.80	38.01	0.0000	270.00	17.0000	201.87	201.87	193.12	14.55	14.55	2.8763	0.9545	1.0000
	0.00	0.01	0.00	0.00	14.55	14.72	17.59	17.59	0.9910	1.306E-04		1	1.665E-02	
90	3.26	18.09	9.43	0.0000	270.00	17.0000	193.21	193.21	186.97	8.95	8.95	3.5802	1.2174	1.0000
	0.00	0.01	0.00	0.00	8.95	9.00	9.40	9.40	1.0407	2.285E-04	RETA	2	7.792E-02	
97	2.04	18.28	0.28	0.0000	270.00	17.0000	182.41	182.41	181.23	1.66	1.66	8.2026	2.8266	1.0000
	0.00	999.00	0.00	0.00	0.00	1.66	1.66	1.66	1.0687	5.373E-05	BETA	4	5.573E-01	

Figure (4-9). LISTING FOR RAY NUMBER 5 OF SAMPLE INPUT DATA FOR WATER DEPTH GRID

PROJECT NO. PAR 2 , 82/09/15 , PLOT NO. 1, PERIOD= 17.0SEC., RAY NO. 6, DELTAT= 25.00, CF=0.000000, KRIDL=0.001000

THE OUTPUT IS IN METRIC UNITS. DEPTH:HGT(MEIER), G:GR:GT,U,V,VT(MEIER/SECOND).

MAX X ROTAT:D	Y FCT:D	DEPTH ROTAT:C	CUR:SF FCT:CK	CUR:DI FCT:CY	PERIOD U	RAY V	PACK VT	WAVE HETA	G DRETA/DUT	GR BRK UP	HGT NO	KS CURVATURE	KF	KR
1	42.00	3.00	299.99	0.0000	270.00	17.0000	220.00	220.00	220.00	13.26	3.0000	1.0000	1.0000	1.0000
	-0.03	0.01	0.00	0.00	13.26	13.26	26.52	1.0000	0.0000E+00			0.0000E+00		
10	38.95	5.56	277.08	0.0000	270.00	17.0000	220.06	220.06	219.96	13.34	2.9913	0.9971	1.0000	1.0000
	-0.03	0.01	0.00	0.00	13.34	13.34	26.49	0.9999	-2.050E-06			-6.658E-04		
20	35.54	8.44	251.55	0.0000	270.00	17.0000	220.28	220.28	219.91	13.40	2.9863	0.9947	1.0000	1.0007
	-0.02	0.01	0.00	0.00	13.40	13.40	26.47	0.9985	-9.637E-06			-1.169E-03		
30	32.13	11.35	225.97	0.0000	270.00	17.0000	220.67	220.67	219.83	13.51	2.9800	0.9907	1.0000	1.0027
	-0.02	0.01	0.00	0.00	13.51	13.51	26.42	0.9947	-2.232E-05			-1.986E-03		
40	28.71	14.32	200.32	0.0000	270.00	17.0000	221.32	221.32	219.66	13.69	2.9719	0.9841	1.0000	1.0067
	-0.02	0.01	0.00	0.00	13.69	13.70	26.32	0.9868	-4.227E-05			-3.213E-03		
50	25.27	17.39	174.56	0.0000	270.00	17.0000	222.35	222.35	219.32	13.98	2.9625	0.9740	1.0000	1.0139
	-0.02	0.01	0.00	0.00	13.98	13.99	26.14	0.9728	-7.034E-05			-4.809E-03		
60	21.83	20.61	148.68	0.0000	270.00	17.0000	223.85	223.85	218.68	14.38	2.9536	0.9602	1.0000	1.0253
	-0.02	0.01	0.00	0.00	14.38	14.44	25.78	0.9513	-1.014E-04			-6.346E-03		
70	18.37	24.04	122.76	0.0000	270.00	17.0000	225.71	225.71	217.52	14.86	2.9488	0.9446	1.0000	1.0406
	-0.01	0.01	0.00	0.00	14.86	15.01	25.12	0.9235	-1.155E-04			-6.715E-03		
80	14.91	27.70	96.84	0.0000	270.00	17.0000	227.38	227.38	215.53	15.27	2.9491	0.9317	1.0000	1.0551
	-0.01	0.01	0.00	0.00	15.27	15.61	23.97	0.8983	-7.246E-05			-4.173E-03		
90	11.47	31.48	71.01	0.0000	270.00	17.0000	227.64	227.64	212.29	15.34	2.9462	0.9297	1.0000	1.0563
	-0.01	0.01	0.00	0.00	15.34	15.90	22.03	0.8963	7.851E-05			3.457E-03		
100	8.02	35.11	45.19	0.0000	270.00	17.0000	224.51	224.51	207.16	14.55	2.9368	0.9545	1.0000	1.0256
	0.00	0.01	0.00	0.00	14.55	15.25	18.83	0.9507	3.874E-04			2.102E-02		
110	4.65	37.97	19.90	0.0000	270.00	17.0000	214.28	214.28	198.84	11.70	3.0401	1.0647	1.0000	0.9518
	0.00	0.01	0.00	0.00	11.70	12.13	13.32	1.1038	8.429E-04		RETA	7.151E-02		
120	2.20	39.15	1.51	0.0000	270.00	17.0000	190.52	190.52	185.34	3.80	4.8864	1.8686	1.0000	0.8717
	0.00	999.00	0.00	0.00	3.80	3.81	3.84	1.3161	5.403E-04		RETA	4.387E-01		
122	2.03	39.18	0.24	0.0000	270.00	17.0000	184.16	184.16	182.11	1.52	7.6709	2.9549	1.0000	0.8653
	0.00	999.00	0.00	0.00	1.52	1.52	1.52	1.3355	2.219E-04		RETA	1.146E+00		

Figure (4-10). LISTING FOR RAY NUMBER 6 OF SAMPLE INPUT DATA FOR WATER DEPTH GRID

PROJ. NO. PCURR , 82/09/15
 SCL = 1/310039 , CIN = 0
 PLOT NO. 1 , DIR. = WAVPAK

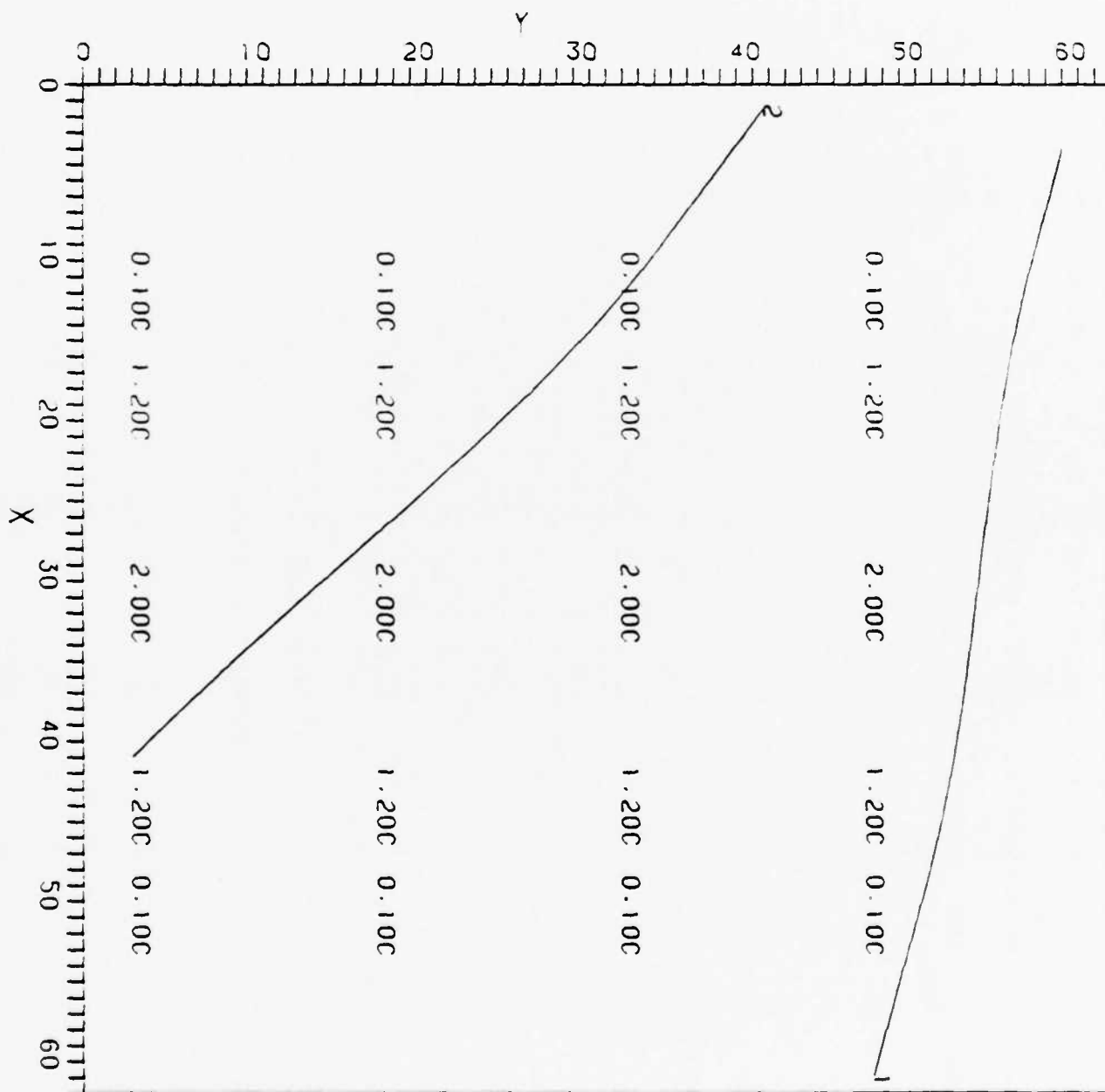


Figure (4-11). PLOT FOR SAMPLE INPUT DATA FOR CURRENT GRID

PROJECT NO. FCURR , 82/09/15 , PLOT NO. 1, PERIOD= 20.0SEC., RAY NO. 1, DELTAT= 25.00, CF=0.100000, KRTOL=0.001000

THE OUTPUT IS IN METRIC UNITS. DEPTH,HGT(METER). G*GR,GT,U,V,VT(METER/SECOND).

MAX X ROTAT:D	Y PCT:D	DEPTH ROTAT:C	CUR:SF PCT:CX	CUR:DI PCT:CY	PERIOD U	RAY V	FACK VT	WAVE BETA	G DBETA/DT	GR BRK UP	HGT NO	KS CURVATURE	KF	KR
1	4.00	60.00	500.00	0.0000	270.00	20.0000	15.00	15.00	15.00	15.60	3.0000	1.0000	1.0000	1.0000
0.00	0.00	0.00	999.00	999.00	15.60	15.60	31.19	31.19	1.0000	0.000E+00	1	0.000E+00	1.0000	1.0000
10	8.52	58.79	500.00	0.0000	270.00	20.0000	15.00	15.00	15.00	15.60	3.0000	1.0000	1.0000	1.0000
0.00	0.00	0.00	999.00	999.00	15.60	15.60	31.19	31.19	1.0000	0.000E+00	1	0.000E+00	1.0000	1.0000
20	13.53	57.53	500.00	0.6444	270.00	19.8936	12.77	14.77	14.84	15.51	3.0226	1.0080	1.0080	0.9995
0.00	0.00	0.00	999.00	0.01	15.35	15.51	31.03	30.86	1.0010	5.402E-06	1	1.045E-03	1.045E-03	0.9990
30	18.52	56.55	500.00	1.3414	270.00	19.7798	9.82	14.51	14.66	15.43	3.0469	1.0167	1.0167	1.0000
0.00	0.00	-0.01	999.00	0.01	15.09	15.43	30.85	30.51	1.0021	3.512E-06	1	7.150E-04	7.150E-04	0.9986
40	23.49	55.80	500.00	1.7883	270.00	19.7076	7.85	14.34	14.56	15.37	3.0625	1.0222	1.0222	1.0000
0.00	0.00	-0.02	999.00	0.01	14.93	15.37	30.74	30.29	1.0028	1.889E-06	1	3.996E-04	3.996E-04	0.9985
50	28.45	55.17	500.00	1.9880	270.00	19.6755	6.87	14.26	14.51	15.34	3.0694	1.0247	1.0247	1.0000
0.00	0.00	-0.09	999.00	0.01	14.85	15.34	30.69	30.19	1.0031	4.026E-07	1	9.377E-05	9.377E-05	0.9985
60	33.41	54.57	500.00	1.9417	270.00	19.6829	7.00	14.27	14.52	15.35	3.0678	1.0241	1.0241	1.0000
0.00	0.00	-0.17	999.00	0.01	14.87	15.35	30.70	30.21	1.0030	-8.447E-07	1	-2.095E-04	-2.095E-04	0.9987
70	38.37	53.91	500.00	1.6493	270.00	19.7300	8.12	14.37	14.59	15.39	3.0575	1.0205	1.0205	1.0000
0.00	0.00	-0.17	999.00	0.01	14.98	15.39	30.77	30.36	1.0026	-2.363E-06	1	-5.171E-04	-5.171E-04	0.9991
80	43.35	53.10	500.00	1.1089	270.00	19.8177	10.50	14.56	14.72	15.45	3.0386	1.0138	1.0138	1.0000
0.00	0.00	-0.17	999.00	0.01	15.18	15.45	30.91	30.63	1.0018	-4.057E-06	1	-8.351E-04	-8.351E-04	0.9997
90	48.35	52.05	500.00	0.3169	270.00	19.9476	13.36	14.84	14.92	15.56	3.0110	1.0039	1.0039	1.0000
0.00	0.00	-0.18	999.00	0.01	15.48	15.56	31.11	31.03	1.0006	-6.067E-06	1	-1.170E-03	-1.170E-03	0.9999
100	53.37	50.72	500.00	0.0000	270.00	20.0000	14.94	14.94	15.00	15.60	2.9998	1.0000	1.0000	1.0000
0.00	0.00	-0.18	999.00	999.00	15.60	15.60	31.19	31.19	1.0001	-3.845E-06	1	0.000E+00	0.000E+00	0.9999
110	58.39	49.38	500.00	0.0000	270.00	20.0000	14.94	14.94	15.00	15.60	2.9998	1.0000	1.0000	1.0000
0.00	0.00	-0.18	999.00	999.00	15.60	15.60	31.19	31.19	1.0001	-3.845E-06	1	0.000E+00	0.000E+00	0.9999
117	61.91	48.45	500.00	0.0000	270.00	20.0000	14.94	14.94	15.00	15.60	2.9998	1.0000	1.0000	1.0000
0.00	0.00	-0.18	999.00	999.00	15.60	15.60	31.19	31.19	1.0001	-3.845E-06	1	0.000E+00	0.000E+00	0.9999

Figure (4-12). LISTING FOR RAY NUMBER 1 OF SAMPLE INPUT DATA FOR CURRENT GRID

PROJECT NO. PCURR , 82/09/15 , PLOT NO. 1, PERIOD= 17.0SEC., RAY NO. 2, DELTAT= 25.00, CF=0.000000, KRTEL=0.001000

THE OUTPUT IS IN METRIC UNITS. DEPTH,HGT(METER). G,GR,GT,U,V,VT(METER/SECOND).

MAX X ROTAT:D	Y PCT:D	DEPTH ROTAT:C	CUR:SP PCT:CX	CUR:DI PCT:CY	GT	PERIOD U	RAY V	FACK VT	WAVE BETA	G URETA/DI	GR BKK UP	HGT NO	KS CURVATURE	KF	KR
1	42.00	3.00	500.00	1.2800	270.00	17.5121	220.00	220.00	220.00	220.00	13.66	14.51	3.0000	1.0000	1.0000
0.00	0.00	-179.99	999.00	0.01	14.48	13.66	27.31	28.14	1.0000	-8.827E-05			1	-5.447E-03	
10	38.88	6.11	500.00	1.6060	270.00	17.6475	225.69	221.16	220.75	13.76	14.87	2.9923	0.9885	1.0000	1.0091
0.00	0.00	-179.99	999.00	0.01	14.82	13.76	27.53	28.57	0.9821	-6.954E-05			1	-3.871E-03	
20	35.44	9.75	500.00	1.8520	270.00	17.7511	227.21	222.08	221.33	13.84	15.15	2.9876	0.9798	1.0000	1.0164
0.00	0.00	-179.98	999.00	0.01	15.08	13.84	27.69	28.91	0.9680	-4.271E-05			1	-2.403E-03	
30	32.02	13.51	500.00	1.9795	270.00	17.8052	228.02	222.58	221.64	13.88	15.29	2.9844	0.9753	1.0000	1.0200
0.00	0.00	-179.93	999.00	0.01	15.22	13.89	27.77	29.09	0.9611	-1.152E-05			1	-9.012E-04	
40	28.62	17.31	500.00	1.9904	270.00	17.8098	228.15	222.65	221.67	13.89	15.31	2.9813	0.9749	1.0000	1.0194
0.00	0.00	-0.11	999.00	0.01	15.24	13.89	27.78	29.10	0.9624	2.136E-05			1	6.116E-04	
50	25.21	21.08	500.00	1.8851	270.00	17.7651	227.61	222.27	221.42	13.85	15.18	2.9781	0.9786	1.0000	1.0144
0.00	0.00	-0.03	999.00	0.01	15.12	13.85	27.71	28.96	0.9717	5.302E-05			1	2.115E-03	
60	21.78	24.75	500.00	1.6621	270.00	17.6710	226.37	221.47	220.88	13.78	14.93	2.9764	0.9864	1.0000	1.0058
0.00	0.00	-0.02	999.00	0.01	14.88	13.78	27.56	28.65	0.9886	8.072E-05			1	3.586E-03	
70	18.32	28.25	500.00	1.3180	270.00	17.5278	224.41	220.28	220.09	13.67	14.56	2.9785	0.9986	1.0000	0.9943
0.00	0.00	-0.01	999.00	0.01	14.52	13.67	27.34	28.19	1.0116	1.022E-04			1	5.003E-03	
80	14.83	31.50	500.00	0.8488	270.00	17.3362	221.68	218.75	219.05	13.52	14.07	2.9877	1.0151	1.0000	0.9810
0.00	0.00	0.00	999.00	0.01	14.05	13.52	27.04	27.57	1.0390	1.162E-04			1	6.336E-03	
90	11.29	34.43	500.00	0.2501	270.00	17.0977	218.09	216.93	217.79	13.33	13.48	3.0069	1.0363	1.0000	0.9672
0.00	0.00	0.00	999.00	0.01	13.48	13.33	26.67	26.82	1.0690	1.224E-04			1	7.556E-03	
100	7.74	37.07	500.00	0.0000	270.00	17.0000	216.38	216.38	217.28	13.26	13.26	3.0211	1.0451	1.0000	0.9635
0.00	0.00	0.00	999.00	0.0000	13.26	13.26	26.52	26.52	1.0771	8.031E-05			1	0.000E+00	
110	4.18	39.69	500.00	0.0000	270.00	17.0000	216.38	216.38	217.28	13.26	13.26	3.0211	1.0451	1.0000	0.9635
0.00	0.00	0.00	999.00	0.0000	13.26	13.26	26.52	26.52	1.0771	8.031E-05			1	0.000E+00	
118	1.33	41.79	500.00	0.0000	270.00	17.0000	216.38	216.38	217.28	13.26	13.26	3.0211	1.0451	1.0000	0.9635
0.00	0.00	0.00	999.00	0.0000	13.26	13.26	26.52	26.52	1.0771	8.031E-05			1	0.000E+00	

Figure (4-13). LISTING FOR RAY NUMBER 2 OF SAMPLE INPUT DATA FOR CURRENT GRID

PROJ. NO. PDAC , 82/09/15
 SCL = 1/310039 ; CIN = 0
 PLOT NO. 1 , DIR. = WAVPAK

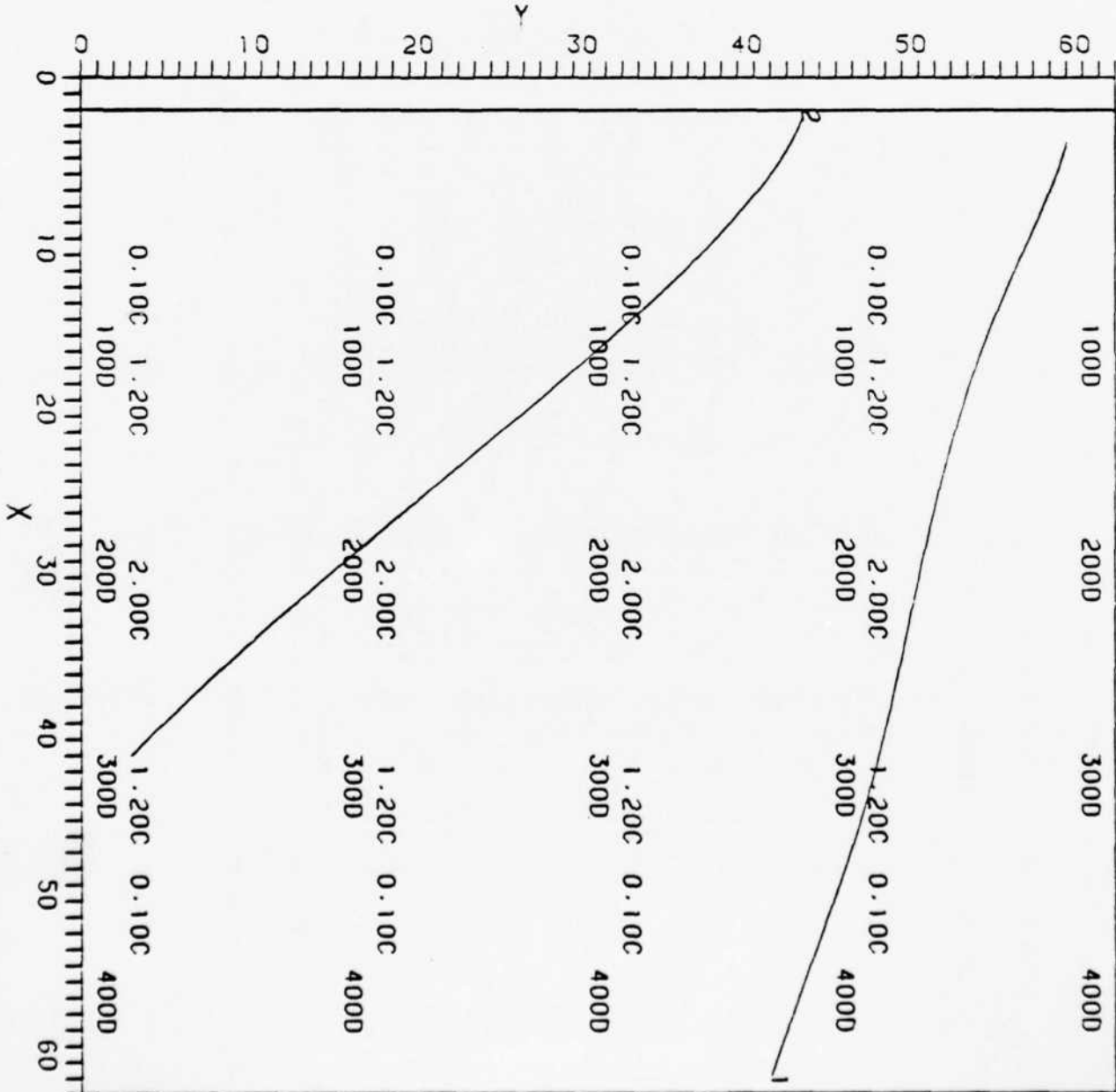


Figure (4-14). PLOT FOR SAMPLE INPUT DATA FOR WATER DEPTH AND CURRENT GRIDS

OBJECT NO. PDAC , 82/09/15 , FLOT NO. 1, PERIOD= 20.0SEC., RAY NO. 1, DELTAT= 25.00, CF=0.100000, KKTOL=0.001000
 DEPTH:PGT(U,V,VT)(METER/SECOND).

IX	X	Y	DEPTH	CUR:SF	CUR:DI	PERIOD	RAY	PACK	WAVE	G	GR	HGT	KS	KF	KR
NOIAT:D	FCI:D	ROIAT:C	ROIAT:C	FCI:GX	FCI:CY	U	U	VT	BETA	DBETA/DI	BRK UP	NO	CURVATURE	KF	KR
1	4.00	60.00	15.00	0.0000	270.00	20.0000	15.00	15.00	15.00	11.24	11.24	3.0000	1.0000	1.0000	1.0000
10	8.10	58.54	0.00	999.00	999.00	11.24	11.82	11.82	1.0000	-2.198E-04			-5.478E-02	0.8195	0.9003
20	13.54	56.17	0.00	999.00	999.00	16.73	22.55	22.68	0.9558	-1.458E-04	BETA	2.2639	-1.640E-02	0.8860	1.0303
30	19.01	54.11	127.56	1.3958	270.00	19.4280	24.78	24.44	0.9421	1.482E-05		2.1619	2.002E-03	0.8826	1.0252
40	24.21	52.56	166.55	1.8321	270.00	19.2553	27.44	26.66	0.9514	4.648E-05		2.2114	0.8147	0.8816	1.0197
50	29.13	51.38	203.46	1.9961	270.00	19.1905	28.70	27.63	0.9618	3.373E-05		2.2877	0.8483	0.8816	1.0197
60	33.87	50.36	239.04	1.9249	270.00	19.2179	29.30	28.12	0.9680	1.680E-05		2.3482	0.8738	0.8813	1.0164
70	38.52	49.37	273.88	1.6370	270.00	19.3308	30.37	29.67	0.9706	4.102E-06		2.3831	0.8881	0.8812	1.0151
80	43.12	48.26	308.37	1.1396	270.00	19.5294	30.86	29.59	0.9704	-5.142E-06		2.3956	0.8927	0.8812	1.0151
90	47.70	46.94	342.76	0.4329	270.00	19.8186	30.86	29.66	0.9681	-1.262E-05		2.3914	0.8901	0.8812	1.0163
100	52.30	45.36	377.21	0.0000	270.00	20.0000	30.86	30.58	0.9641	-1.957E-05		2.3748	0.8821	0.8812	1.0184
110	56.87	43.74	411.49	0.0000	270.00	20.0000	31.16	31.16	0.9598	-1.541E-05		2.3674	-1.684E-03	0.8812	1.0207
120	61.42	42.14	445.67	0.0000	270.00	20.0000	31.16	31.16	0.9574	-1.599E-05		2.3788	0.8774	0.8812	1.0220
121	61.88	41.98	449.08	0.0000	270.00	20.0000	31.19	31.19	0.9574	-1.599E-05	RAY REACHED GRID BOUNDARY	2.3788	0.8805	0.8812	1.0220
-0.05	0.01	-180.00	999.00	999.00	999.00	14.49	31.19	31.19	0.9574	-1.599E-05		2.3788	0.8805	0.8812	1.0220

Figure (4-15). LISTING FOR RAY NUMBER 1 OF SAMPLE INPUT DATA FOR WATER DEPTH AND CURRENT GRIDS

PROJECT NO. PDAC , 82/09/15 , FLOT NO. 1, PERIOD= 17.0SEC., RAY NO. 2, DELTAT= 25.00, CF=0.000000, KNTDL=0.001000
 THE OUTPUT IS IN METRIC UNITS. DEPTH:HGT(METER). G,GR,GT,U,V,VT(METER/SECOND).

MAX X	Y	DEPTH	CUR:SF	CUR:DI	PERIOD	RAY	PACK	WAVE	G	GR	HGT	KS	KF	KR
ROTAT:D	FCT:D	ROTAT:C	FCT:CX	FCT:CY	U	V	VT	RETA	DRETA/DT	BRK UP	NO	CURVATURE		
1	42.00	3.00	299.99	1.2800	270.00	17.5121	220.00	220.00	220.00	13.66	14.51	3.0000	1.0000	1.0000
-0.03	0.01	-179.99	999.00	0.01	14.48	13.66	27.31	28.14	1.0000	-8.827E-05		1	-5.447E-03	
10	38.86	6.14	276.42	1.6076	270.00	17.6486	225.90	221.35	220.71	13.89	15.00	2.9794	0.9839	1.0000
-0.03	0.01	-179.99	999.00	0.01	14.96	13.89	27.48	28.53	0.9816	-7.526E-05		1	-4.852E-03	
20	35.39	9.84	250.44	1.8544	270.00	17.7527	227.67	222.64	221.22	14.08	15.40	2.9674	0.9716	1.0000
-0.02	0.01	-179.98	999.00	0.01	15.34	14.09	27.60	28.82	0.9648	-5.851E-05		1	-3.987E-03	
30	31.95	13.72	224.59	1.9809	270.00	17.8065	228.90	223.73	221.37	14.29	15.73	2.9558	0.9615	1.0000
-0.02	0.01	-179.92	999.00	0.01	15.66	14.31	27.60	28.91	0.9523	-4.162E-05		1	-3.260E-03	
40	28.50	17.73	198.76	1.9887	270.00	17.8100	229.67	224.63	221.12	14.54	16.00	2.9432	0.9531	1.0000
-0.02	0.01	-0.10	999.00	0.01	15.94	14.57	27.45	28.75	0.9439	-2.612E-05		1	-2.651E-03	
50	25.04	21.84	172.80	1.8770	270.00	17.7628	229.99	225.36	220.38	14.84	16.23	2.9288	0.9462	1.0000
-0.02	0.01	-0.03	999.00	0.01	16.17	14.90	27.10	28.32	0.9393	-1.020E-05		1	-2.050E-03	
60	21.54	26.01	146.58	1.6425	270.00	17.6642	229.87	225.89	219.07	15.18	16.40	2.9121	0.9409	1.0000
-0.01	0.01	-0.01	999.00	0.01	16.36	15.29	26.50	27.53	0.9395	1.461E-05		1	-1.181E-03	
70	17.99	30.18	119.90	1.2784	270.00	17.5124	229.12	226.03	216.97	15.51	16.45	2.8914	0.9388	1.0000
-0.01	0.01	-0.01	999.00	0.01	16.43	15.70	25.50	26.27	0.9488	6.661E-05		1	5.361E-04	
80	14.35	34.25	92.64	0.7757	270.00	17.3070	227.33	225.35	213.86	15.71	16.27	2.8637	0.9437	1.0000
-0.01	0.01	0.00	999.00	0.01	16.26	16.03	23.93	24.36	0.9774	1.746E-04		1	4.310E-03	
90	10.63	38.04	64.69	0.1041	270.00	17.0405	223.25	222.93	209.33	15.46	15.53	2.8360	0.9656	1.0000
-0.01	0.01	0.00	999.00	999.00	15.53	15.90	21.41	21.46	1.0435	3.457E-04	REIA	8	1.147E-02	
100	6.89	41.29	36.66	0.0000	270.00	17.0000	218.50	218.30	203.10	14.09	14.09	2.8212	1.0137	1.0000
0.00	0.01	0.00	999.00	999.00	14.09	14.60	17.33	17.33	1.1620	6.639E-04	REIA	2	2.947E-02	
110	3.51	43.49	11.31	0.0000	270.00	17.0000	205.08	204.83	193.16	9.52	9.52	3.1535	1.2332	1.0000
0.00	0.01	0.00	999.00	999.00	9.52	9.72	10.25	10.25	1.3763	9.723E-04	REIA	4	1.123E-01	
118	2.04	43.96	0.28	0.0000	270.00	17.0000	184.40	184.22	181.85	RAY REACHED SHORE		7.1769	2.9495	1.0000
0.00	999.00	0.00	999.00	999.00	1.66	1.67	1.67	1.67	1.5201	2.373E-04	REIA	8	9.643E-01	

Figure (4-16). LISTING FOR RAY NUMBER 2 OF SAMPLE INPUT DATA FOR WATER DEPTH AND CURRENT GRIDS

PROJ. NO. SIN 3 , 82/09/15
SCL = 1/196850 ; CIN = 0
PLOT NO. 1 , DIR. = WAVPAK

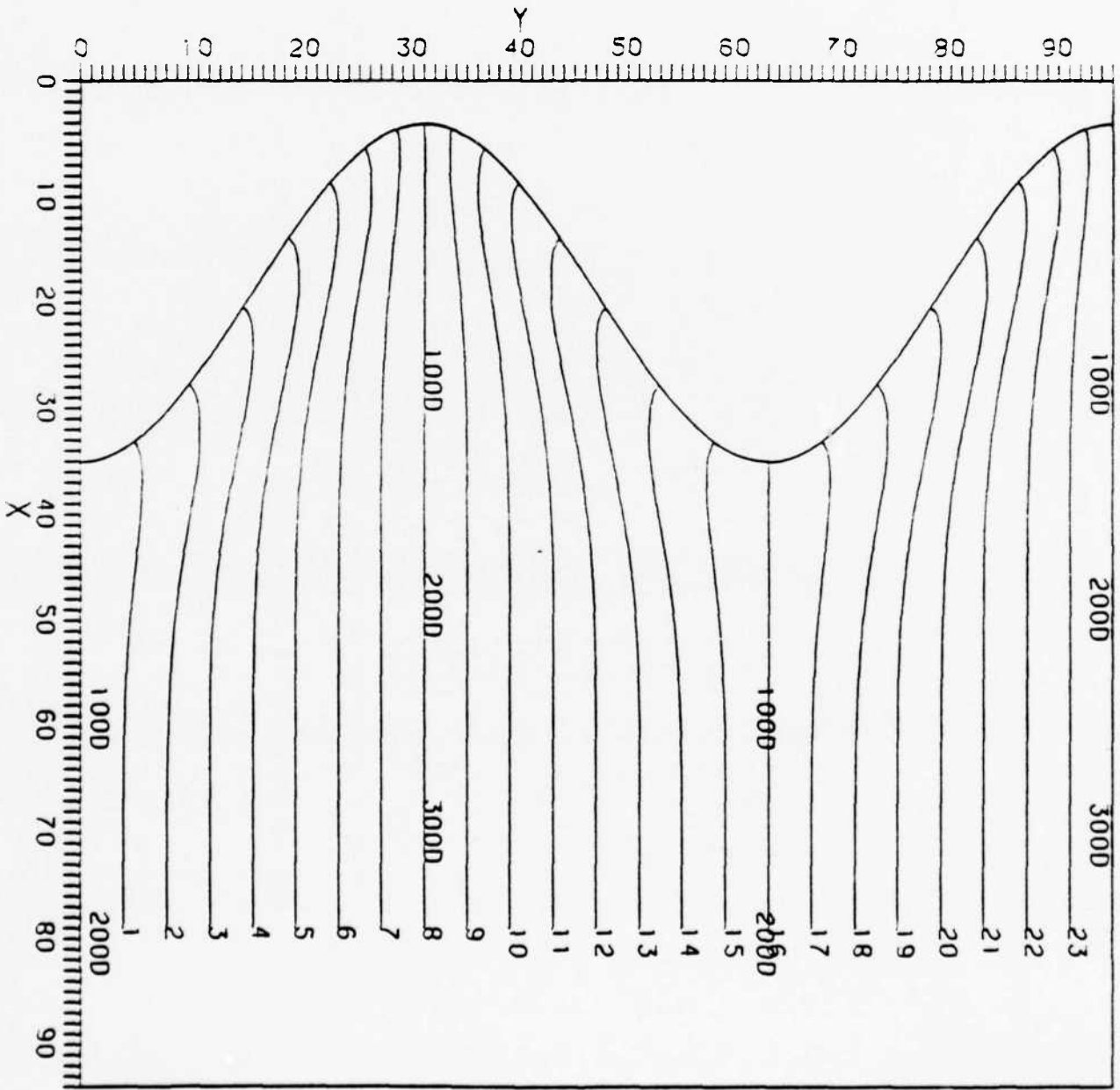


Figure (4-17). PLOT FOR SINUSOIDAL WATER DEPTH CONTOURS

PROJECT NO. SIN 3 , 82/09/15 , PLOT NO. 1, PERIOD= 14.0SEC., RAY NO. 4, DELTAT= 10.00, CF=0.000000, KNTOL=0.001000

THE OUTPUT IS IN METRIC UNITS. DEPTH,HGT(METER). G,GR,GT,U,V,VT(METER/SECOND).

MAX X ROTAT:D	Y FCT:D	DEPTH ROTAT:C	CUR:SF FCT:CX	CUR:DI FCT:CY	PERIOD U	RAY V	PACK VT	WAVE BETA	G DBETA/DI	GR BRK UP	HGT NO	KS CURVAIURE	KF	KR
1	80.00	16.00	281.26	0.0000	0.00	14.0000	180.00	180.00	180.00	10.92	10.92	1.0000	1.0000	1.0000
57.53	0.01	0.00	0.00	0.00	10.92	10.92	21.84	21.84	1.0000	0.000E+00	1.0000	1.0000	0.000E+00	1.0000
20	73.36	16.00	250.12	0.0000	0.00	14.0000	180.00	180.00	180.00	10.92	10.92	1.0000	1.0000	1.0000
57.51	0.02	0.00	0.00	0.00	10.92	10.92	21.84	21.84	1.0000	0.000E+00	1.0000	1.0000	0.000E+00	1.0000
40	66.37	16.00	217.39	0.0000	0.00	14.0000	180.00	180.00	180.00	10.92	10.92	1.0000	1.0000	1.0000
57.38	0.02	0.00	0.00	0.00	10.92	10.92	21.84	21.84	1.0000	0.000E+00	1.0000	1.0000	0.000E+00	1.0000
60	59.37	16.00	184.62	0.0000	0.00	14.0000	180.18	180.18	179.91	10.99	10.99	0.9971	0.9967	1.0000
57.54	0.03	0.00	0.00	0.00	10.99	10.99	21.81	21.81	0.9992	-2.660E-05	1.0005	1.0000	-1.664E-03	1.0102
80	52.30	16.08	152.05	0.0000	0.00	14.0000	181.31	181.31	179.66	11.13	11.13	1.0005	0.9904	1.0000
57.54	0.03	0.00	0.00	0.00	11.13	11.13	21.75	21.75	0.9799	-1.907E-04	1.0219	1.0000	-4.454E-03	1.0461
100	45.10	16.40	120.58	0.0000	0.00	14.0000	184.02	184.02	178.84	11.44	11.44	1.0219	0.9769	1.0000
57.50	0.02	0.00	0.00	0.00	11.44	11.49	21.55	21.55	0.9137	-4.834E-04	1.0740	1.0000	-8.902E-03	1.1202
120	37.68	17.19	91.63	0.0000	0.00	14.0000	188.30	188.30	176.66	11.88	11.88	1.0740	0.9588	1.0000
57.22	0.04	0.00	0.00	0.00	11.88	12.13	20.99	20.99	0.7970	-6.077E-04	1.1230	1.0000	-9.938E-03	1.1845
140	30.10	18.54	65.84	0.0000	0.00	14.0000	191.32	191.32	172.30	12.15	12.15	1.1230	0.9481	1.0000
56.75	0.03	0.00	0.00	0.00	12.15	12.85	19.75	19.75	0.7128	-1.185E-04	1.0655	1.0000	-2.182E-03	1.1108
160	22.50	19.97	40.21	0.0000	0.00	14.0000	188.44	188.44	164.33	11.87	11.87	1.0655	0.9593	1.0000
55.37	0.17	0.00	0.00	0.00	11.87	13.00	17.11	17.11	0.8105	1.362E-03	BETA 2	1.0000	1.979E-02	1.0000
180	15.73	19.98	8.55	0.0000	0.00	14.0000	161.87	161.87	144.09	7.98	7.98	0.9446	1.1698	1.0000
55.46	2.70	0.00	0.00	0.00	7.98	8.38	8.89	8.89	1.5337	6.978E-03	BETA 4	1.0000	2.179E-01	0.8075
1E7	14.75	19.44	0.20	0.0000	0.00	14.0000	130.35	130.35	127.26	1.40	1.40	1.9964	2.7917	1.0000
55.91	6.74	0.00	0.00	0.00	1.40	1.40	1.40	1.40	1.9554	2.248E-03	BETA 16	1.0000	2.248E+00	0.7151

Figure (4-18). LISTING FOR RAY NUMBER 4 IN FIGURE (4-17)

PROJECT NO. SIN 3 , 82/09/15 , PLOT NO. 1, PERIOD= 14.0SEC., RAY NO. 8, DELTAT= 10.00, CF=0.000000, KRIDL=0.001000
 THE OUTPUT IS IN METRIC UNITS. DEPTH,HGT(METER). G,GR,GT,U,V,VT(METER/SECOND).

MAX X ROIAT:D	Y FCT:D	DEPTH ROIAT:C	CUR:SF FCT:CX	CUR:DI FCT:CY	PERIOD U	RAY V	PACK VT	WAVE BETA	G DRETA/DI	GR BRK UP	HGT NO	KS CURVATURE	NF CURVATURE	KR
1	80.00	32.00	356.26	0.0000	0.00	14.0000	180.00	180.00	180.00	10.92	10.92	1.0000	1.0000	1.0000
	-0.20	0.01	0.00	0.00	10.92	10.92	21.84	21.84	1.0000	0.000E+00		1	0.000E+00	1.0000
20	73.36	32.00	325.12	0.0000	0.00	14.0000	180.00	180.00	180.00	10.92	10.92	1.0000	1.0000	1.0000
	-0.19	0.02	0.00	0.00	10.92	10.92	21.84	21.84	1.0000	0.000E+00		1	0.000E+00	1.0000
40	66.37	32.00	292.38	0.0000	0.00	14.0000	180.00	180.00	180.00	10.92	10.92	1.0000	1.0000	1.0000
	-0.13	0.02	0.00	0.00	10.92	10.92	21.84	21.84	1.0000	0.000E+00		1	0.000E+00	1.0000
60	59.39	32.00	259.61	0.0000	0.00	14.0000	180.00	180.00	180.00	10.92	10.92	1.0000	1.0000	1.0000
	-0.03	0.02	0.00	0.00	10.92	10.92	21.84	21.84	1.0000	0.000E+00		1	0.000E+00	1.0000
80	52.40	32.00	226.84	0.0000	0.00	14.0000	180.00	180.00	180.00	10.92	10.92	1.0000	1.0000	1.0000
	0.10	0.01	0.00	0.00	10.92	10.92	21.84	21.84	1.0000	0.000E+00		1	0.000E+00	1.0000
100	45.41	32.00	194.11	0.0000	0.00	14.0000	180.00	180.00	180.00	10.97	10.97	0.9976	0.9976	1.0000
	0.00	0.01	0.00	0.00	10.97	10.97	21.82	21.82	1.0000	0.000E+00		1	3.171E-08	1.0022
120	38.36	32.00	161.09	0.0000	0.00	14.0000	180.00	180.00	180.00	11.08	11.08	0.9949	0.9927	1.0000
	-0.08	0.02	0.00	0.00	11.08	11.08	21.78	21.78	0.9956	-5.364E-05		1	3.233E-06	1.0143
140	31.20	32.00	127.51	0.0000	0.00	14.0000	180.00	180.00	180.00	11.38	11.38	0.9934	0.9793	1.0000
	-0.04	0.03	0.00	0.00	11.38	11.38	21.62	21.62	0.9720	-2.088E-04		1	4.403E-06	1.0560
160	23.72	32.00	92.43	0.0000	0.00	14.0000	180.00	180.00	180.00	12.11	12.11	1.0029	0.9497	1.0000
	-0.06	0.04	0.00	0.00	12.11	12.11	21.01	21.01	0.8967	-5.881E-04		1	1.018E-05	1.1762
180	15.66	32.00	54.65	0.0000	0.00	14.0000	180.00	180.00	180.00	13.06	13.06	1.0754	0.9143	1.0000
	-0.03	0.07	0.00	0.00	13.06	13.06	18.83	18.83	0.7229	-1.106E-03		1	2.443E-06	1.3529
200	7.61	32.00	16.96	0.0000	0.00	14.0000	180.00	180.00	180.00	10.80	10.80	1.3603	1.0055	1.0000
	-0.11	0.15	0.00	0.00	10.80	10.80	12.14	12.14	0.5463	-2.375E-04		1	-1.623E-04	
MAX= 215, PACKET CURVATURE AVERAGED														
RAY REACHED SHORE														
217	4.04	32.00	0.18	0.0000	0.00	14.0000	180.08	180.08	180.13	1.33	1.33	3.6478	2.8642	1.0000
	-0.27	999.00	0.00	0.00	1.33	1.33	1.33	1.33	0.6165	3.320E-04		2	-4.338E-02	

Figure (4-19). LISTING FOR RAY NUMBER 8 IN FIGURE (4-17)

PROJECT NO. 8IN 3 , 82/09/13 , PLOT NO. 1, PERIOD= 14.0SEC., RAY NO. 16, DELTAT= 10.00, CF=0.000000, KRTEL=0.001000

THE OUTPUT IS IN METRIC UNITS. DEPTH,HGT(METER). G,GR,GT,U,V,VT(METER/SECOND).

MAX X ROTAT:D	Y PCT:D	DEPTH ROTAT:C	CUR:SF FCT:CX	CUR:DI FCT:CY	PERIOD U	RAY V	PACK VT	WAVE BETA	G DBETA/DT	GR BRK UP	HGT NO	KS CURVATURE	KF	KR
1	80.00	64.00	206.22	0.0000	0.00	14.0000	180.00	180.00	10.92	10.92	1.0000	1.0000	1.0000	1.0000
-0.21	0.01	0.00	0.00	0.00	10.92	10.92	21.84	21.84	1.0000	0.000E+00	1	0.000E+00	1.0000	1.0000
20	73.33	64.00	174.98	0.0000	0.00	14.0000	180.00	180.00	11.02	11.02	0.9948	0.9954	1.0000	0.9993
0.00	0.01	0.00	0.00	0.00	11.02	11.02	21.80	21.80	1.0013	2.501E-05	1	-1.397E-08	1.0000	0.9927
40	66.23	64.00	141.70	0.0000	0.00	14.0000	180.00	180.00	11.22	11.22	0.9793	0.9865	1.0000	0.9927
0.01	0.01	0.00	0.00	0.00	11.22	11.22	21.71	21.71	1.0147	1.273E-04	1	-3.150E-07	1.0000	0.9693
60	58.92	64.00	107.42	0.0000	0.00	14.0000	180.00	180.00	11.74	11.74	0.9348	0.9644	1.0000	0.9693
0.01	0.02	0.00	0.00	0.00	11.74	11.74	21.36	21.36	1.0643	4.143E-04	1	-7.121E-07	1.0000	0.9099
80	51.13	64.00	70.91	0.0000	0.00	14.0000	180.00	180.00	12.72	12.72	0.8432	0.9266	1.0000	0.9099
-0.06	0.06	0.00	0.00	0.00	12.72	12.72	20.08	20.08	1.2077	1.077E-03	1	1.218E-05	1.0000	0.8269
100	42.83	64.00	32.03	0.0000	0.00	14.0000	180.00	180.00	12.65	12.65	0.7683	0.9291	1.0000	0.8269
0.01	0.05	0.00	0.00	0.00	12.65	12.65	15.76	15.76	1.4624	9.981E-04	1	2.193E-06	1.0000	0.8684
120	36.54	64.00	2.53	0.0000	0.00	14.0000	180.03	180.03	4.85	4.85	1.3025	1.4998	1.0000	0.8684
0.00	999.00	0.00	0.00	0.00	4.85	4.85	4.94	4.94	1.3259	-1.861E-03	1	4.432E-04	1.0000	0.8684
125	36.02	64.00	0.11	0.0000	0.00	14.0000	180.03	180.03	1.05	1.05	2.8826	3.2314	1.0000	0.8921
-0.04	999.00	0.00	0.00	0.00	1.05	1.05	1.05	1.05	1.2566	-6.322E-04	2	-2.604E-03	1.0000	0.8921

Figure (4-20). LISTING FOR RAY NUMBER 16 IN FIGURE (4-17)

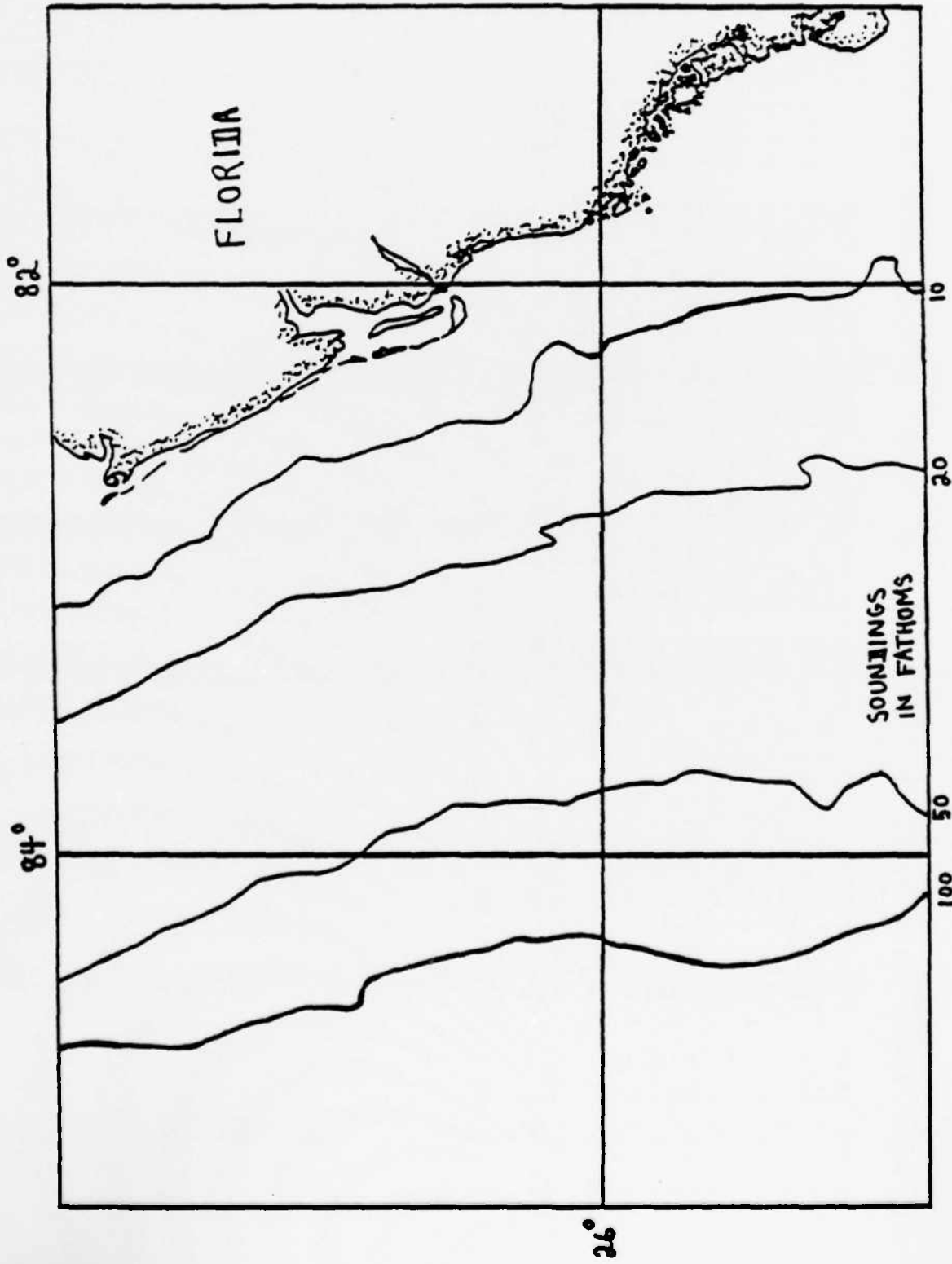


Figure (4-21). GULF OF MEXICO OFF THE SOUTHWESTERN FLORIDA COAST

PROJ. NO. GOM 3 , 82/09/15
SCL = 1/2649744 ; CIN = 0
PLOT NO. 1 , DIR. = WAVPAK

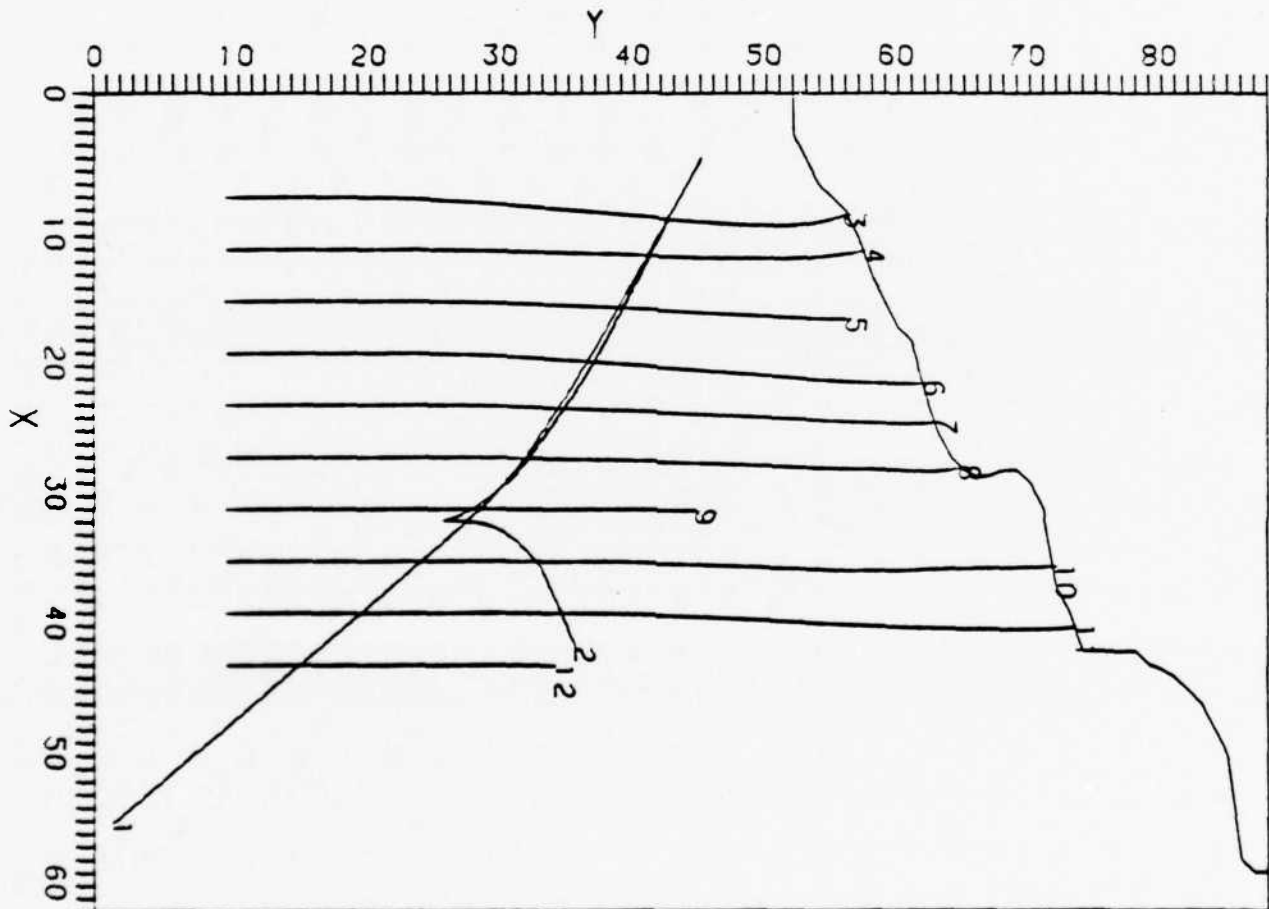


Figure (4-22). PLOT OF RAYS OFF THE SOUTHWESTERN FLORIDA COAST

THE OUTPUT IS IN ENGLISH UNITS. DEPTH,HGT(FEET). G,GR,GT,U,V,VI(FEET/SECOND).

MAX X ROTAT:D	Y FCT:D	DEPTH ROTAT:C	DEPTH FCT:C	CURISF FCT:CY	CUR:DI GT	PERIOD U	RAY V	PACK VT	WAVE BETA	G DRETA/DI	GR BRK UP	HGT UP	NO	KS CURVATURE	KF	KR
1	5.00	46.00	74.74	0.0000	270.00	12.0000	30.00	30.00	30.00	30.00	35.42	35.42	1.0000	1.0000	1.0000	1.0000
-74.29	11.91	0.00	0.00	0.00	0.00	35.42	43.83	43.83	1.0000	-4.694E-05			1	2.022E-02		
25	7.55	44.57	98.89	0.0000	270.00	12.0000	28.73	28.73	24.50	36.56	36.56		0.9862	0.9843	0.9983	1.0037
-62.56	4.82	0.00	0.00	0.00	0.00	36.56	48.50	48.50	0.9927	1.372E-05			1	2.641E-03		
50	10.26	43.10	116.75	0.0000	270.00	12.0000	28.62	28.62	23.09	36.72	36.72		0.9718	0.9822	0.9972	0.9922
-44.88	1.82	0.00	0.00	0.00	0.00	36.72	51.17	51.17	1.0159	2.018E-05			1	-1.622E-04		
75	12.96	41.62	135.50	0.0000	270.00	12.0000	28.73	28.73	22.02	36.48	36.48		0.9627	0.9854	0.9966	0.9802
-32.19	2.32	0.00	0.00	0.00	0.00	36.48	53.43	53.43	1.0407	1.871E-05			1	-1.242E-04		
100	15.63	40.15	147.78	0.0000	270.00	12.0000	28.97	28.97	21.33	36.15	36.15		0.9564	0.9898	0.9961	0.9699
-58.22	1.97	0.00	0.00	0.00	0.00	36.15	54.65	54.65	1.0629	2.003E-05			1	-3.163E-03		
125	18.25	38.68	164.91	0.0000	270.00	12.0000	29.58	29.58	20.13	35.52	35.52		0.9534	0.9987	0.9958	0.9587
-68.34	1.61	0.00	0.00	0.00	0.00	35.52	56.09	56.09	1.0879	1.716E-05			1	-5.144E-03		
150	20.81	37.21	181.92	0.0000	270.00	12.0000	30.44	30.44	18.98	34.75	34.75		0.9591	1.0096	0.9956	0.9542
-65.48	2.34	0.00	0.00	0.00	0.00	34.75	57.24	57.24	1.0983	-2.225E-06			1	-6.375E-03		
175	23.28	35.71	193.73	0.0000	270.00	12.0000	32.46	32.46	17.43	33.86	33.86		0.9734	1.0227	0.9954	0.9561
-81.77	0.54	0.00	0.00	0.00	0.00	33.86	57.90	57.90	1.0940	3.927E-06			1	-1.097E-02		
200	25.63	34.18	210.25	0.0000	270.00	12.0000	33.49	33.49	16.52	33.01	33.01		0.9856	1.0360	0.9953	0.9559
-64.23	1.06	0.00	0.00	0.00	0.00	33.01	58.68	58.68	1.0944	-3.582E-06			1	-5.104E-03		
225	27.90	32.63	228.96	0.0000	270.00	12.0000	35.38	35.38	15.57	31.90	31.90		0.9891	1.0537	0.9952	0.9432
-78.95	2.03	0.00	0.00	0.00	0.00	31.90	59.37	59.37	1.1241	5.742E-05			1	-2.039E-02		
250	29.94	31.06	269.76	0.0000	270.00	12.0000	40.14	40.14	13.25	29.26	29.26		0.9905	1.1003	0.9952	0.9045
-79.85	1.46	0.00	0.00	0.00	0.00	29.26	60.37	60.37	1.2222	7.219E-05			1	-3.524E-02		
275	31.68	29.49	325.17	0.0000	270.00	12.0000	44.18	44.18	11.63	26.81	26.81		1.0109	1.1495	0.9952	0.8837
-83.73	0.52	0.00	0.00	0.00	0.00	26.81	61.03	61.03	1.2806	2.343E-05			1	-2.706E-02		
300	33.20	27.93	373.55	0.0000	270.00	12.0000	47.07	47.07	10.81	25.24	25.24		1.0370	1.1846	0.9952	0.8796
-87.18	0.42	0.00	0.00	0.00	0.00	25.24	61.29	61.29	1.2924	-1.003E-06			1	-2.007E-02		
325	34.60	26.38	423.28	0.0000	270.00	12.0000	48.57	48.57	10.42	24.40	24.40		1.0579	1.2049	0.9952	0.8822
-82.61	0.56	0.00	0.00	0.00	0.00	24.40	61.41	61.41	1.2848	-9.049E-06			1	-7.437E-03		
350	35.93	24.85	483.22	0.0000	270.00	12.0000	49.21	49.21	10.08	23.85	23.85		1.0742	1.2187	0.9952	0.8857
-89.25	0.84	0.00	0.00	0.00	0.00	23.85	61.50	61.50	1.2746	-9.920E-06			1	0.000E+00		
375	37.24	23.34	534.64	0.0000	270.00	12.0000	49.21	49.21	10.08	23.85	23.85		1.0742	1.2187	0.9952	0.8857
-96.83	0.40	0.00	0.00	0.00	0.00	23.85	61.50	61.50	1.2746	-9.920E-06			1	0.000E+00		
400	38.55	21.82	566.18	0.0000	270.00	12.0000	49.21	49.21	10.08	23.85	23.85		1.0742	1.2187	0.9952	0.8857
-102.41	0.31	0.00	0.00	0.00	0.00	23.85	61.50	61.50	1.2746	-9.920E-06			1	0.000E+00		
425	39.85	20.30	609.05	0.0000	270.00	12.0000	49.21	49.21	10.08	23.85	23.85		1.0742	1.2187	0.9952	0.8857
-107.90	1.12	0.00	0.00	0.00	0.00	23.85	61.50	61.50	1.2746	-9.920E-06			1	0.000E+00		
450	41.16	18.79	647.32	0.0000	270.00	12.0000	49.21	49.21	10.08	23.85	23.85		1.0742	1.2187	0.9952	0.8857
-94.22	0.84	0.00	0.00	0.00	0.00	23.85	61.50	61.50	1.2746	-9.920E-06			1	0.000E+00		
475	42.47	17.27	694.47	0.0000	270.00	12.0000	49.21	49.21	10.08	23.85	23.85		1.0742	1.2187	0.9952	0.8857
-83.71	1.33	0.00	0.00	0.00	0.00	23.85	61.50	61.50	1.2746	-9.920E-06			1	0.000E+00		
500	43.78	15.76	698.65	0.0000	270.00	12.0000	49.21	49.21	10.08	23.85	23.85		1.0742	1.2187	0.9952	0.8857
-65.92	7.81	0.00	0.00	0.00	0.00	23.85	61.50	61.50	1.2746	-9.920E-06			1	0.000E+00		
525	45.09	14.24	1128.34	0.0000	270.00	12.0000	49.21	49.21	10.08	23.85	23.85		1.0742	1.2187	0.9952	0.8857
-74.69	5.06	0.00	0.00	0.00	0.00	23.85	61.50	61.50	1.2746	-9.920E-06			1	0.000E+00		
550	46.40	12.72	2130.94	0.0000	270.00	12.0000	49.21	49.21	10.08	23.85	23.85		1.0742	1.2187	0.9952	0.8857
-61.16	3.62	0.00	0.00	0.00	0.00	23.85	61.50	61.50	1.2746	-9.920E-06			1	0.000E+00		
575	47.70	11.21	3487.60	0.0000	270.00	12.0000	49.21	49.21	10.08	23.85	23.85		1.0742	1.2187	0.9952	0.8857
-50.50	0.82	0.00	0.00	0.00	0.00	23.85	61.50	61.50	1.2746	-9.920E-06			1	0.000E+00		
600	49.01	9.69	5199.19	0.0000	270.00	12.0000	49.21	49.21	10.08	23.85	23.85		1.0742	1.2187	0.9952	0.8857
-52.55	3.53	0.00	0.00	0.00	0.00	23.85	61.50	61.50	1.2746	-9.920E-06			1	0.000E+00		

Figure (4-23). PARTIAL LISTING FOR RAY NUMBER 1 IN FIGURE (4-22)

PROJECT NO. GOM 3 , 82/09/15 , PLOT NO. 1, PERIOD= 12.0SEC., KAY NO. 2, DELTAT= 50.00, CF=0.005000, KRIDL=0.001,000

THE OUTPUT IS IN ENGLISH UNITS. DEPTH,HGT(FEET). G,GR,GT,U,V,VT(FEET/SECOND).

MAX X ROTAT:D	Y PCT:D	DEPTH ROTAT:C	CUR:SP PCT:EX	CUR:DI PCT:CY	PERIOD GT	RAY V	PACK VT	WAVE BETA	G DRETA/DI	GR BRK UP	HGT NO	KS CURVATURE	KF	KR
1	5.00	46.00	74.74	0.0000	270.00	12.0000	28.00	28.00	28.00	35.42	35.42	1.0000	1.0000	1.0000
-74.29	11.91	0.00	0.00	0.00	35.42	35.42	43.83	43.83	1.0000	-5.211E-05	0.9878	1	2.094E-02	1.0048
25	7.60	44.67	98.35	0.0000	270.00	12.0000	26.66	26.66	21.95	36.52	36.52	0.9878	0.9848	1.0048
-63.41	4.82	0.00	0.00	0.00	36.52	36.52	48.41	48.41	0.9905	1.516E-05	0.9715	1	2.796E-03	0.9911
50	10.35	43.29	116.22	0.0000	270.00	12.0000	26.55	26.55	20.13	36.66	36.66	0.9715	0.9830	0.9911
-50.16	1.82	0.00	0.00	0.00	36.66	36.66	51.10	51.10	1.0181	2.530E-05	0.9608	1	-3.778E-04	0.9763
75	13.09	41.92	136.18	0.0000	270.00	12.0000	26.78	26.78	18.39	36.32	36.32	0.9608	0.9875	0.9763
-40.35	2.22	0.00	0.00	0.00	36.32	36.32	53.50	53.50	1.0492	2.020E-05	0.9539	1	-6.765E-04	0.9655
100	15.80	40.54	146.18	0.0000	270.00	12.0000	27.11	27.11	17.57	36.01	36.01	0.9539	0.9918	0.9655
-54.81	1.97	0.00	0.00	0.00	36.01	36.01	54.50	54.50	1.0727	1.973E-05	0.9521	1	-2.998E-03	0.9552
125	18.46	39.16	161.05	0.0000	270.00	12.0000	28.08	28.08	16.26	35.36	35.36	0.9521	1.0009	0.9552
-77.45	0.96	0.00	0.00	0.00	35.36	35.36	55.79	55.79	1.0960	1.679E-05	0.9679	1	-1.044E-02	0.9544
150	21.02	37.74	179.34	0.0000	270.00	12.0000	30.10	30.10	13.90	34.14	34.14	0.9679	1.0187	0.9544
-74.79	2.78	0.00	0.00	0.00	34.14	35.55	57.08	57.08	1.0978	-1.921E-05	0.9981	1	-1.572E-02	0.9667
175	23.41	36.27	188.97	0.0000	270.00	12.0000	33.17	33.17	12.36	32.92	32.92	0.9981	1.0372	0.9667
-84.75	2.60	0.00	0.00	0.00	32.92	35.22	57.65	57.65	1.0701	-2.584E-06	1.0190	1	-1.895E-02	0.9660
200	25.64	34.74	206.33	0.0000	270.00	12.0000	35.12	35.12	10.68	31.53	31.53	1.0190	1.0599	0.9660
-70.13	1.06	0.00	0.00	0.00	31.53	34.64	58.51	58.51	1.0715	-6.567E-06	1.0421	1	-1.084E-02	0.9713
225	27.76	33.22	220.64	0.0000	270.00	12.0000	36.58	36.58	9.69	30.48	30.48	1.0421	1.0781	0.9713
-68.83	1.97	0.00	0.00	0.00	30.48	34.17	59.08	59.08	1.0599	3.647E-06	1.0922	1	-1.424E-02	0.9453
250	29.63	31.68	251.56	0.0000	270.00	12.0000	44.45	44.45	6.63	26.27	26.27	1.0922	1.1611	0.9453
-83.57	1.46	0.00	0.00	0.00	26.27	33.26	59.99	59.99	1.1190	8.305E-05	1.1791	1	-9.005E-02	0.9172
275	30.93	30.20	302.28	0.0000	270.00	12.0000	52.15	52.15	3.46	21.22	21.22	1.1791	1.2919	0.9172
-81.88	1.06	0.00	0.00	0.00	21.22	32.15	60.83	60.83	1.1888	2.915E-05	1.3047	1	-6.368E-02	0.9152
300	31.84	28.88	344.19	0.0000	270.00	12.0000	58.42	58.42	1.56	17.26	17.26	1.3047	1.4327	0.9152
-83.66	0.24	0.00	0.00	0.00	17.26	31.57	61.16	61.16	1.1938	2.173E-05	1.4816	1	-6.265E-02	0.9152
325	32.47	27.75	380.20	0.0000	270.00	12.0000	64.77	64.77	0.12	13.38	13.38	1.4816	1.6269	0.9152
-86.58	0.40	0.00	0.00	0.00	13.38	31.26	61.31	61.31	1.1938	2.173E-05	1.9576	1	-1.381E-01	0.9152
350	32.79	26.91	403.51	0.0000	270.00	12.0000	74.64	74.64	358.90	7.67	7.67	1.9576	2.1495	0.9152
-87.65	0.79	0.00	0.00	0.00	7.67	31.12	61.37	61.37	1.1938	2.173E-05	3.6253	1	-4.632E-01	0.9152
375	32.86	26.55	414.57	0.0000	270.00	12.0000	83.62	83.62	357.75	2.24	2.24	3.6253	3.9807	0.9152
-87.08	0.79	0.00	0.00	0.00	2.24	31.07	61.39	61.39	1.1938	2.173E-05	4.4597	1	-3.931E-01	0.9152
383	32.87	26.50	416.13	0.0000	270.00	12.0000	84.78	84.78	357.50	1.48	1.48	4.4597	4.8969	0.9152
-86.99	0.79	0.00	0.00	0.00	1.48	31.06	61.40	61.40	1.1938	2.173E-05	3.4055	1	-4.182E-01	0.9152
MAX = 383	REFLECTION:	NEAR REFLECTION POINT												
400	32.87	26.61	412.49	0.0000	270.00	12.0000	270.74	270.74	356.06	2.53	2.53	3.4055	3.7395	0.9152
-87.23	0.79	0.00	0.00	0.00	2.53	31.07	61.39	61.39	1.1938	-2.173E-05	2.9232	1	-1.337E-01	0.9152
425	32.87	26.87	404.81	0.0000	270.00	12.0000	271.93	271.93	355.59	3.44	3.44	2.9232	3.2098	0.9152
-87.80	0.79	0.00	0.00	0.00	3.44	31.11	61.37	61.37	1.1938	-2.173E-05	2.6741	1	-4.956E-02	0.9152
450	32.89	27.18	397.39	0.0000	270.00	12.0000	272.82	272.82	355.24	4.11	4.11	2.6741	2.9364	0.9152
-87.94	0.40	0.00	0.00	0.00	4.11	31.15	61.36	61.36	1.1938	-2.173E-05	2.4925	1	-4.306E-02	0.9152
475	32.91	27.55	386.52	0.0000	270.00	12.0000	273.51	273.51	354.79	4.73	4.73	2.4925	2.7369	0.9152
-88.78	0.40	0.00	0.00	0.00	4.73	31.22	61.33	61.33	1.1938	-2.173E-05	2.3703	1	-2.378E-02	0.9152
500	32.93	27.97	374.03	0.0000	270.00	12.0000	273.97	273.97	354.35	5.23	5.23	2.3703	2.6027	0.9152
-89.71	0.40	0.00	0.00	0.00	5.23	31.30	61.29	61.29	1.1938	-2.173E-05	2.0435	1	-1.515E-02	0.9152
525	32.98	28.47	359.02	0.0000	270.00	12.0000	276.31	276.31	353.38	7.03	7.03	2.0435	2.2439	0.9152
-86.67	0.46	0.00	0.00	0.00	7.03	31.43	61.23	61.23	1.1938	-2.173E-05	1.6340	1	-1.081E-01	0.9152
550	33.09	29.20	338.41	0.0000	270.00	12.0000	282.14	282.14	351.79	11.00	11.00	1.6340	1.7943	0.9152
-85.72	0.61	0.00	0.00	0.00	11.00	31.64	61.13	61.13	1.1938	-2.173E-05	1.2674	1	-1.734E-01	0.9152
575	33.46	30.34	303.66	0.0000	270.00	12.0000	293.66	293.66	348.97	18.29	18.29	1.2674	1.3917	0.9152

Figure (4-24). PARTIAL LISTING FOR RAY NUMBER 2 IN FIGURE (4-22)

PROJECT NO. GOM 3 , 82/09/15 , PLOT NO. 1, PERIOD= 12.0SEC., RAY NO. 6, DELTAT= 50.00, CF=0.005000, KRTDL=0.001000
 THE OUTPUT IS IN ENGLISH UNITS. DEPTH*HGT(FEET). G,GR,GT,U,V,VT(FEET/SECOND).

MAX X ROTAT:D	Y FCT:D	DEPTH ROTAT:C	DEPTH FCT:CK	CUR:SP FCT:CK	CUR:DI FCT:CY	GT GT	PERIOD U	RAY V	PACK VT	WAVE BETA	G DBETA/DI	GR BRK UP	HGT NO	KS CURVATURE	KF NO	KR
1	20.00	10.00	877.93	0.0000	270.00	12.0000	270.00	270.00	270.00	270.00	30.75	30.75	1.0000	1.0000	1.0000	1.0000
-84.19	6.75		0.00	0.00	0.00	30.75	30.75	61.50	61.50	1.0000	0.000E+00	30.75	1.0000	0.000E+00	1.0000	1.0000
25	20.00	12.48	716.56	0.0000	270.00	12.0000	270.00	270.00	270.00	270.00	30.75	30.75	1.0000	1.0000	1.0000	1.0000
-70.57	0.35		0.00	0.00	0.00	30.75	30.75	61.50	61.50	1.0000	0.000E+00	30.75	1.0000	0.000E+00	1.0000	1.0000
50	20.00	15.06	579.74	0.0000	270.00	12.0000	270.00	270.00	270.00	270.00	30.75	30.75	1.0000	1.0000	1.0000	1.0000
-76.30	1.12		0.00	0.00	0.00	30.75	30.75	61.50	61.50	1.0000	0.000E+00	30.75	1.0000	0.000E+00	1.0000	1.0000
75	20.00	17.64	528.04	0.0000	270.00	12.0000	270.00	270.00	270.00	270.00	30.75	30.75	1.0000	1.0000	1.0000	1.0000
-52.97	0.52		0.00	0.00	0.00	30.75	30.75	61.50	61.50	1.0000	0.000E+00	30.75	1.0000	0.000E+00	1.0000	1.0000
100	20.00	20.23	464.00	0.0000	270.00	12.0000	270.01	270.01	270.01	269.98	30.90	30.90	0.9975	0.9975	1.0000	1.0000
-61.91	0.44		0.00	0.00	0.00	30.90	30.90	61.45	61.45	1.0000	-1.346E-07	31.15	0.9941	-1.036E-03	1.0000	1.0007
125	20.00	22.83	396.69	0.0000	270.00	12.0000	270.23	270.23	270.23	269.93	31.15	31.15	0.9941	0.9935	1.0000	1.0007
-61.50	0.53		0.00	0.00	0.00	31.15	31.15	61.36	61.36	0.9987	-1.763E-06	31.95	0.9834	-2.624E-03	1.0000	1.0024
150	20.03	25.47	314.40	0.0000	270.00	12.0000	270.99	270.99	270.99	269.72	31.95	31.95	0.9834	0.9810	1.0000	1.0024
-60.03	1.08		0.00	0.00	0.00	31.95	31.95	60.95	60.95	0.9953	-5.162E-06	32.78	0.9736	-7.984E-03	1.0000	1.0052
175	20.10	28.19	269.45	0.0000	270.00	12.0000	272.09	272.09	272.09	269.37	32.78	32.78	0.9736	0.9686	1.0000	1.0052
-57.22	0.92		0.00	0.00	0.00	32.78	32.81	60.36	60.36	0.9897	-1.269E-06	33.70	0.9611	-5.755E-03	1.0000	1.0062
200	20.23	30.98	233.19	0.0000	270.00	12.0000	272.96	272.96	272.96	268.98	33.70	33.70	0.9611	0.9552	1.0000	1.0062
-63.39	1.47		0.00	0.00	0.00	33.70	33.78	59.50	59.50	0.9877	-2.522E-07	34.66	0.9440	-6.217E-03	1.0000	1.0023
225	20.40	33.84	201.57	0.0000	270.00	12.0000	273.70	273.70	273.70	268.58	34.66	34.66	0.9440	0.9419	1.0000	1.0023
-74.82	1.72		0.00	0.00	0.00	34.66	34.80	58.29	58.29	0.9954	-6.760E-06	35.19	0.9338	-3.106E-03	1.0000	0.9993
250	20.60	36.77	183.75	0.0000	270.00	12.0000	274.28	274.28	274.28	268.11	35.19	35.19	0.9338	0.9347	1.0000	0.9993
-55.30	1.83		0.00	0.00	0.00	35.19	35.40	57.35	57.35	1.0014	-5.932E-07	35.97	0.9249	-3.340E-03	1.0000	1.0008
275	20.83	39.74	158.15	0.0000	270.00	12.0000	274.58	274.58	274.58	267.99	35.97	35.97	0.9249	0.9246	1.0000	1.0008
-94.56	1.96		0.00	0.00	0.00	35.97	36.20	55.56	55.56	0.9985	-6.272E-06	36.43	0.9226	-1.655E-06	1.0000	1.0051
300	21.08	42.77	138.94	0.0000	270.00	12.0000	274.61	274.61	274.61	268.10	36.43	36.43	0.9226	0.9187	1.0000	1.0051
-87.52	0.53		0.00	0.00	0.00	36.43	36.67	53.79	53.79	0.9898	-5.594E-06	36.69	0.9197	-3.778E-04	1.0000	1.0061
325	21.32	45.83	121.64	0.0000	270.00	12.0000	274.55	274.55	274.55	268.76	36.69	36.69	0.9197	0.9154	1.0000	1.0061
-109.23	1.13		0.00	0.00	0.00	36.69	36.88	51.81	51.81	0.9878	-1.236E-06	36.67	0.9184	3.220E-04	1.0000	1.0053
350	21.57	48.91	109.17	0.0000	270.00	12.0000	274.53	274.53	274.53	268.94	36.67	36.67	0.9184	0.9157	1.0000	1.0053
-90.55	0.57		0.00	0.00	0.00	36.67	36.85	50.10	50.10	0.9896	-1.272E-06	36.09	0.9279	1.108E-04	1.0000	1.0090
375	21.81	51.96	87.81	0.0000	270.00	12.0000	274.42	274.42	274.42	268.93	36.09	36.09	0.9279	0.9230	1.0000	1.0090
-71.53	3.28		0.00	0.00	0.00	36.09	36.26	46.53	46.53	0.9823	-1.764E-05	35.44	0.9391	2.299E-03	1.0000	1.0140
400	22.04	54.96	77.20	0.0000	270.00	12.0000	274.12	274.12	274.12	268.54	35.44	35.44	0.9391	0.9314	1.0000	1.0140
-66.53	6.55		0.00	0.00	0.00	35.44	35.61	44.37	44.37	0.9727	-7.376E-06	32.91	0.9640	7.729E-03	1.0000	1.0068
425	22.22	57.83	54.54	0.0000	270.00	12.0000	273.16	273.16	273.16	267.47	32.91	32.91	0.9640	0.9667	1.0000	1.0068
-87.72	1.68		0.00	0.00	0.00	32.91	33.07	38.65	38.65	0.9866	-8.963E-06	30.69	0.9855	1.790E-03	1.0000	1.0006
450	22.33	60.53	42.81	0.0000	270.00	12.0000	270.95	270.95	270.95	265.22	30.69	30.69	0.9855	0.9841	1.0000	1.0006
-68.96	8.76		0.00	0.00	0.00	30.69	30.85	34.86	34.86	0.9988	-4.989E-05	17.18	1.2562	1.854E-02	1.0000	0.9862
475	22.32	62.76	10.01	0.0000	270.00	12.0000	268.94	268.94	268.94	266.04	17.18	17.18	1.2562	1.3379	1.0000	0.9862
-88.34	999.00		0.00	0.00	0.00	17.18	17.20	17.70	17.70	1.0283	-1.453E-05	10.17	1.4843	1.343E-02	1.0000	0.9881
480	22.32	62.99	3.31	0.0000	270.00	12.0000	268.80	268.80	268.80	267.13	10.17	10.17	1.4843	1.7390	1.0000	0.9881
-88.73	999.00		0.00	0.00	0.00	10.17	10.17	10.27	10.27	1.0243	-1.559E-05	10.17	1.4843	5.251E-03	1.0000	0.9881

Figure (4-25). LISTING FOR RAY NUMBER 6 IN FIGURE (4-22)

PROJECT NO. GOM 3 , 82/09/15 , PLOT NO. 1, PERIOD= 12.0SEC., RAY NO. 12, DELTAT= 50.00, CF=0.005000, KRIDL=0.001000

THE OUTPUT IS IN ENGLISH UNITS, DEPTH,HGT(FEET), G,GR,GT,U,V,VI(FEET/SECOND).

MAX X ROTAT:D	Y PCT:D	DEPTH ROTAT:C	CUR:SF PCT:CX	CUR:DI PCT:CY	PERIOD U	RAY U	VI	PACK VI	WAVE BETA	G DBETA/DT	GR BRK UP	HGT NO	KS CURVATURE	KF	KR
1	44.00	10.00	3720.80	0.0000	270.00	12.0000	270.00	270.00	270.00	270.00	30.75	30.75	1.0000	1.0000	1.0000
-92.34	1.76	0.00	0.00	0.00	30.75	30.75	61.50	61.50	1.0000	0.000E+00	0.000E+00	0.000E+00	1.0000	1.0000	1.0000
25	44.00	12.48	1907.92	0.0000	270.00	12.0000	270.00	270.00	270.00	270.00	30.75	30.75	1.0000	1.0000	1.0000
-82.21	2.68	0.00	0.00	0.00	30.75	30.75	61.50	61.50	1.0000	0.000E+00	0.000E+00	0.000E+00	1.0000	1.0000	1.0000
50	44.00	15.06	818.87	0.0000	270.00	12.0000	270.00	270.00	270.00	270.00	30.75	30.75	1.0000	1.0000	1.0000
-73.19	6.49	0.00	0.00	0.00	30.75	30.75	61.50	61.50	1.0000	0.000E+00	0.000E+00	0.000E+00	1.0000	1.0000	1.0000
75	44.00	17.64	672.75	0.0000	270.00	12.0000	270.00	270.00	270.00	270.00	30.75	30.75	1.0000	1.0000	1.0000
-107.89	1.15	0.00	0.00	0.00	30.75	30.75	61.50	61.50	1.0000	0.000E+00	0.000E+00	0.000E+00	1.0000	1.0000	1.0000
100	44.00	20.22	561.81	0.0000	270.00	12.0000	270.00	270.00	270.00	270.00	30.75	30.75	1.0000	1.0000	1.0000
-106.21	1.12	0.00	0.00	0.00	30.75	30.75	61.50	61.50	1.0000	0.000E+00	0.000E+00	0.000E+00	1.0000	1.0000	1.0000
125	44.00	22.81	519.07	0.0000	270.00	12.0000	270.00	270.00	270.00	270.00	30.75	30.75	1.0000	1.0000	1.0000
-84.15	0.61	0.00	0.00	0.00	30.75	30.75	61.50	61.50	1.0000	0.000E+00	0.000E+00	0.000E+00	1.0000	1.0000	1.0000
150	44.00	25.39	471.15	0.0000	270.00	12.0000	270.00	270.00	270.00	269.99	30.89	30.89	0.9977	0.9977	1.0000
-80.10	0.16	0.00	0.00	0.00	30.89	30.89	61.46	61.46	1.0000	0.000E+00	0.000E+00	0.000E+00	1.0000	1.0000	1.0000
175	44.00	27.99	404.71	0.0000	270.00	12.0000	270.08	270.08	269.98	31.11	31.11	31.11	0.9943	0.9941	1.0000
-82.51	0.60	0.00	0.00	0.00	31.11	31.11	61.37	61.37	0.9997	-7.882E-07	-7.882E-07	-7.882E-07	1.0000	-6.285E-04	1.0000
200	44.01	30.62	330.16	0.0000	270.00	12.0000	270.23	270.23	269.94	31.74	31.74	31.74	0.9852	0.9843	1.0000
-80.20	0.76	0.00	0.00	0.00	31.74	31.74	61.07	61.07	0.9982	-1.291E-06	-1.291E-06	-1.291E-06	1.0000	-1.863E-03	1.0000
225	44.03	33.33	259.30	0.0000	270.00	12.0000	270.79	270.79	269.73	33.05	33.05	33.05	0.9637	0.9645	0.9992
-73.26	4.78	0.00	0.00	0.00	33.05	33.06	60.16	60.16	1.0016	4.581E-06	4.581E-06	4.581E-06	1.0000	-5.721E-03	1.0000
239	44.06	34.91	232.41	0.0000	270.00	12.0000	271.22	271.22	269.48	33.79	33.79	33.79	0.9526	0.9539	0.9986
-26.55	3.36	0.00	0.00	0.00	33.79	33.81	59.48	59.48	1.0028	-2.344E-06	-2.344E-06	-2.344E-06	1.0000	-2.214E-03	1.0000
MAX = 239.															
239	44.06	34.91	232.41	0.0000	10.14	12.0000	300.36	300.36	40.03	33.79	33.79	33.79	0.9526	0.9539	1.0000
-26.55	3.36	0.00	0.00	0.00	33.79	33.81	59.48	59.48	1.0028	-2.344E-06	-2.344E-06	-2.344E-06	1.0000	-2.214E-03	1.0000

REFLECTION HAND-UP

Figure (4-26). LISTING FOR RAY NUMBER 12 IN FIGURE (4-22)

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PRINCIPAL NOTATION

The principal symbols are defined. In defining derivatives the letters in parentheses are used to complete the symbols. The underlined letters denote the variables to which the derivatives are applied. The input and output parameters used in the computer program are defined on pages 56-60.

A	The program symbol for θ . In the input and output A is the direction in degrees from which the wave packet comes, with respect to true north. Internally in the program A is the direction in radians with which the wave packet moves with respect to the positive x-axis.
AA	The wave packet direction at the new ray point.
AAA, AA <u>A</u> V	The average of the values at the new and previous ray points, respectively, of the wave packet and wavelet directions.
ABAR	The average of the wave packet directions at the present and new points.
AGR	The program symbol for g .
AK(i)	The program symbol for K_i where $i = 1, 2, \dots, 9$.
AKFC	The program symbol for K_F .
AKR	The program symbol for K_R .
AKS	The program symbol for K_S .
AL(i)	The program symbol for L_i where $i = 1, 2, \dots, 9$.
ALFA	The program symbol for α .
AMM, ANN	The maximum values of x and y, respectively, for a water depth grid.
ARAY	The program symbol for ρ . The directions of ARAY are defined following the same conventions used in the definitions of A.
AV	The program symbol for γ . The directions of AV are defined following the same conventions used in the definitions of A.
AVP	The program symbol for γ' or γ'' .
AX, AY	The arrays used to store the locations of contour values, ray points, and tick marks.

BDZ The program symbol for $d\delta/dt$.

BDZ5 The fifth order Runge-Kutta solution of $d\delta/dt$.

BZ The program symbol for β .

BZTOL The limiting value for $|EBZ|$ and $|EBDZ|$ in the Runge-Kutta calculations of β and $d\delta/dt$. If $|EBZ|$ or $|EBDZ|$ exceeds or is equal to BZTOL the time step interval is halved.

BZ5 The fifth order Runge-Kutta solution of β .

C An array of 12 water depths from CMAT used to fit a quadratic surface in the vicinity of the ray point.

CALFA The program symbol for α_c .

CDAD_ (X,Y) The program symbols for derivatives of θ in the x"y"-coordinate system (currents).

CDAVD_ (X,Y) The program symbols for derivatives of η in the x"y"-coordinate system (currents).

CDGD_ (X,Y,XX,XY,YY) The program symbols for derivatives of G in the x"y"-coordinate system (currents).

CDPHD_ (X,Y) The program symbols for derivatives of ϕ in the x"y"-coordinate system (currents).

CDUD_ (X,Y,XX,XY,YY) The program symbols for derivatives of U in the x"y"-coordinate system (currents).

CDVD_ (X,Y,XX,XY,YY) The program symbols for derivatives of v in the x"y"-coordinate system (currents).

CF The program symbol for c_f .

CIN If CIN is not zero, its value is the travel time between tick marks along a ray. In the input CIN is in seconds, but for the calculations CIN is converted to hours. If CIN is zero there are no tick marks on a ray.

CMAT The water depth grid in a two dimensional array.

CNVRSA The direction of the positive x-axis of the water depth and current grids with respect to true north. The use of this conversion angle permits the wave and current directions to be defined with respect to true north in the input and output.

CONTURC An array containing the current profile values in feet/second or meters/second. There can be as many as 9 values.

CONTURD	An array containing the sounding water depths in feet or meters. There can be as many as 9 values.
CURR	The current magnitude in a two dimensional array.
CURX	The x-component current in a two dimensional array.
CURY	The y-component current in a two dimensional array.
CX	An array of 12 x-component current values from CURX used to fit a quadratic surface in the vicinity of the ray point.
CY	An array of 12 y-component current values from CURY used to fit a quadratic surface in the vicinity of the ray point.
c_f	The friction factor.
D	The program symbol for D_n .
<u>DADX</u>	The program symbol for the derivative of σ in the x'y'-coordinate system (water depths).
<u>DAVDX</u>	The program symbol for the derivative of γ in the x'y'-coordinate system (water depths).
DELA	The change in the wave packet direction from the present to the new ray point.
DELAV	The change in the wavelet direction from the present to the new ray point.
DELX, DELY	The change in the values from the present to the new ray points of the x and y coordinates, respectively.
DEP	The program symbol for h.
<u>DGD</u> _ _	(X,XX,XY,YY) The program symbols for derivatives of G in the x'y'-coordinate system (water depths).
<u>DHD</u> _ _	(X,XX,XY,YY) The program symbols for derivatives of h in the x'y'-coordinate system (water depths).
D_n	The incremental distance in grid units between ray points.
<u>DPHIDX</u>	The program symbol for the derivative of ϕ in the x'y'-coordinate system (water depths).
DUD	The ratio of the phase speed at the present ray point to the value at the previous ray point.

DUD_ _	(X,XX,XY,YY) The program symbols for derivatives of U in the x'y'-coordinate system (water depths).
DVD_ _	(X,XX,XY,YY) The program symbols for derivatives of v in the x'y'-coordinate system (water depths).
DY	The number of grid units per inch or centimeter for a particular plot.
DZDD_ _	(X,Y,XX,XY,YY) The program symbols for derivatives of ϵ in the x''y''-coordinate system (currents).
DZD_ _	(X,Y,XX,XY,YY) The program symbols for derivatives of u in the x''y''-coordinate system (currents)
E	An array of 6 coefficients of the quadratic surface equation which is fitted to the 12 water depths in the array C.
EBDZ	The program symbol for ϵ_{3t} .
EBZ	The program symbol for ϵ_3 .
EM	A two dimensional array of numbers used in computing the array E.
EX	An array of 6 coefficients of the quadratic surface equation which is fitted to the 12 x-component current values in the array CX.
EY	An array of 6 coefficients of the quadratic surface equation which is fitted to the 12 y-component current values in the array CY.
E	The wave energy per unit area.
\hat{e}_k	A unit vector in the direction of γ .
\hat{e}_m	A unit vector in the direction of θ .
FK	The program symbol for κ_G . It is measured in radians/grid unit.
FKAC	The program symbol for the packet ray curvature considering only variations due to currents.
FKAD	The program symbol for the packet ray curvature considering only variations due to water depths.
FKBAR	The average of the packet ray curvature at the present and new ray points.
FKK	The value of κ_G in radians/grid unit at the new ray point.

F	The average rate of energy transmission of the waves.
f	The frequency of the wave (1/T) relative to the current.
G	The geometric group speed.
GR	The program symbol for G_R .
G_R	The ray speed.
GRID	The number of feet or meters per grid unit for a particular water depth grid.
GT	The program symbol for G_T .
G_T	The speed of the advected group front in a current.
GTZERO	The value of G_T at the first ray point.
GZERO	The value of G at the first ray point.
g	The acceleration due to gravity.
H	The wave height.
HGT	The program symbol for H.
HGTZ	The initial value of H.
H _ _	(X,Y,XX,XY,YY) The program symbols for derivatives of h in the xy-coordinate system (water depths).
h	The water depth.
IBDZ	Is set equal to zero in HEIGHT at the beginning of a ray. If a reflected ray is continued beyond a reflection point, IBDZ is set equal to one in HEIGHT when the calculations of β and $d\beta/dt$ are to resume. As a result, $d\beta/dt$ is determined analytically to restart the Runge Kutta calculations.
IBBDT	Is set equal to zero in SURFCE at the beginning of a ray. When a ray enters a current IBDT is set equal to one in SURFCE. As a result, the initial value of $d\beta/dt$ for currents is determined analytically. This value is used in the Runge Kutta calculations of β and $d\beta/dt$.
IFLG	When IFLG is zero a check is made in HEIGHT to determine if there should be a breakup of the time step interval in order to maintain the desired accuracy in the calculations of either β or the ray path. If there is a division of the time step interval, IFLG is set equal to one once the time step interval is sufficiently reduced. When IFLG

- equals one further checks for a breakup of the time step interval are not made at new ray points until the breakup ends and calculations are resumed with the initial time step.
- IHGT If IHGT is set equal to zero the wavelet direction is determined in SURFCE. If IHGT is set equal to one the values of p and q are determined in SURFCE.
- INUM An index to count the ray points within the broken interval when there is a division of the initial time step interval.
- IONCE Is set equal to one in SURFCE at the beginning of a ray. IONCE is set equal to zero after the initial value of $d\beta/dt$ for currents is determined analytically in SURFCE. As a result, this calculation is not repeated for the ray.
- IWAVIT The flag IWAVIT is used when both water depth and current grids exist. Its purpose is to require accuracy in the calculation of the wavelet direction when iterating to a new ray point. At the beginning of the iteration process IWAVIT is set equal to zero. When successive wavelet estimates differ by less than a predetermined amount, IWAVIT is set equal to one. Iterations stop when both IWAVIT equals one and the ray curvature calculations have converged.
- KCIN The number of tick marks along a ray which do not coincide with ray points.
- K_F The friction coefficient.
- K_i Expressions used in the Runge-Kutta calculations of β and $d\beta/dt$ where $i = 1, 2, \dots, 9$.
- KMAX The same as MAX except in DRAW where it is the sum of MAX and KCIN.
- K_R The refraction coefficient.
- KREST The number of tick marks along a ray.
- K_S The shoaling coefficient.
- k The wave number $2\pi/\lambda$.
- LI The number of lines of printout between page and column headings.
- L_i Expressions used in the Runge-Kutta calculations of β and $d\beta/dt$ where $i = 1, 2, \dots, 9$.
- ℓ The perpendicular distance between rays.

MAXQ An index to number points along a ray at time intervals equal to the initial time step.

MIT If MIT is 1 the wave packet curvature approximations in MOVE converge to one value. If MIT is 2 the curvature approximations converge to two values. If the curvature approximations do not converge and there is no reflection MIT is 3. If MIT is 4 a caustic or focal point is computed in HEIGHT. MIT is 5 if it is determined in HEIGHT that the wave breaks. When there is a reflection but the ray is not continued MIT is 6. If MIT is 7 more than one reflection from the same point is determined in MOVE. If MIT is 8 the breakup time step determined in HEIGHT is less than 0.5 seconds.

MMAX The dimension of the AX and AY arrays.

N The ray number.

NBRKUP Is zero except during a breakup of the time step interval when the value is one. After returning to MOVE from HEIGHT, the value of NBRKUP determines where the program resumes.

NDP The water depth is determined in SURFCE. If the value is greater than 0, NDP is 1 (initialized in RAYN). If the water depth equals or is less than 0, NDP is 2.

NFK The value of NFK is determined in SURFCE. If the ratio of the water depth to the deep water wavelength is greater than 0.64, NFK is 1. Otherwise, NFK is 2.

NFLAGR Is set equal to zero in WAVPAK at the beginning of a ray. The value is changed to one in MOVE if there is a reflection and the ray is continued. If NFLAGR is one, in HEIGHT the value of NROPT is set equal to zero.

NFLECT In WAVPAK, NFLECT is set equal to zero at the beginning of a ray. In HEIGHT, NFLECT is set equal to one for those ray points where the conditions for being close to a reflection point are met.

NFRACT In WAVPAK, NFRAC T is set equal to zero at the beginning of a ray. In HEIGHT, NFRAC T is set equal to one for those ray points where there is a breakup of the time step interval due to insufficient accuracy in the Runge-Kutta calculations of β and $d\beta/dt$.

NGO The value of NGO is determined in MOVE. If a ray point lies within one and one half grid units of a grid boundary NGO is 2. Otherwise, NGO is 1. (Initialized in RAYN.)

NOLINE An index used to determine when to write page and column headings depending upon the number of lines of printout.

NOREF An index to count the number of reflections at a ray point.

NPLOT The plot number.

NREF The value of NREF is determined in MOVE and it denotes the kind of reflection. When there is reflection due to Snell's law with phase velocity NREF is 1. When reflection occurs because the packet curvature iteration is not converging NREF is 2. If there is reflection because the ray point is too near a reflection point NREF is 3.

NRFLBU In WAVPAK, NRFLBU is set equal to zero at the beginning of a ray. In HEIGHT, NRFLBU is set equal to one for those ray points where the conditions for being close to a reflection point are met. This causes the statement "REFLECT" to appear in the output.

NRFRBU In WAVPAK, NRFRBU is set equal to zero at the beginning of a ray. In HEIGHT, NRFRBU is set equal to one for those ray points where there is a breakup of the time step interval due to insufficient accuracy in the Runge-Kutta calculations of β and $d\beta/dt$. This causes the statement "BETA" to appear in the output.

NROPT The initial value of NROPT is determined in the input data. If NROPT is zero a ray is not continued beyond a reflection point. If NROPT is not zero a ray is continued beyond a reflection point. After a reflection NROPT is set equal to zero so that a ray is not continued beyond a second reflection point if one should exist.

NTOREF If there is total reflection due to the wavelets NTOREF is set equal to one. Otherwise, NTOREF is set equal to zero. The reflection test is made in SURFCE.

NUMT The number of divisions when there is a breakup of the initial time step interval.

n An index to number ray points.

OMEGA The program symbol for ω .

OMEG_ _ (X,Y,XX,XY,YY) The program symbols for derivatives of ω in the x"y"-coordinate system (currents).

PATI A program symbol for p. The value of p at the point prior to the new ray point.

PHI The program symbol for ϕ .

POT A program symbol for p. The value of p at the new ray point.

POTC	The program symbol for p at the new ray point considering only variations due to currents.
POTD	The program symbol for p at the new ray point considering only variations due to water depths.
PREV	The value of v at the previous ray point.
PREVT	The value of v_T at the previous ray point.
P(i)	Program symbols for p. The values of p at points intermediate to the new and previous ray points where $i = 1, 2, \dots, 5$.
P	A coefficient of the ray separation equation.
QATI	A program symbol for q. The value of q at the point prior to the new ray point.
QOT	A program symbol for q. The value of q at the new ray point.
QOTC	The program symbol for q at the new ray point considering only variations due to currents.
QOTD	The program symbol for q at the new ray point considering only variations due to water depths.
Q(i)	Program symbols for q. The values of q at points intermediate to the new and previous ray points where $i = 1, 2, \dots, 5$.
q	A coefficient of the ray separation equation.
RT	The length of the x-axis in inches or centimeters for a given plot.
S	A two dimensional array of numbers used in computing the arrays E, EX, and EY.
SCL	The scale of the plot.
S_G	The arc length of a wave packet trajectory.
s_{ray}	The arc length of a ray.
s_v	The arc length of a monochromatic ray.
T	The wave period relative to the current.
TIMEQ	The travel time along a ray.

TT	The program symbol for the input wave period.
TTT	The program symbol for the Doppler shifted wave period.
t	Time.
U	The conventional group speed $d\omega/dk$.
UK	The program symbol for u_k .
UK__	(X,Y,XX,XY,YY) The program symbols for derivatives of u_k in the x''y''-coordinate system (currents).
UM__	(X,Y,XX,XY,YY) The program symbols for derivatives of u_m in the x''y''-coordinate system (currents).
u	The speed of the current.
u_k	The component of the current in the direction of \hat{t} , i.e., perpendicular to the wavelet front.
u_m	The component of the current in the direction of \hat{n} , i.e., perpendicular to the group front.
V	The program symbol for v.
VT	The program symbol for v_T .
v	The phase speed of a monochromatic wave.
v_T	The speed of the advected wavelet front in a current.
WAVNO	The program symbol for k.
WAVNO__	(X,Y) The program symbols for derivatives of k in the x''y''-coordinate system (currents).
WL	The program symbol for the deep water value of λ .
X	The program symbol for x.
XX	The program symbol for x at the new ray point.
x	A Cartesian coordinate of the water depth grid.
x'	A Cartesian coordinate in a system chosen such that $\partial h/\partial y' = 0$.
x''	A Cartesian coordinate in a system chosen such that $\partial u/\partial y'' = 0$.
Y	The program symbol for y.

YVW	A one dimensional array used in computing the arrays E, EX, and EY.
YY	The program symbol for y at the new ray point.
y	A Cartesian coordinate of the water depth grid.
y'	A Cartesian coordinate in a system chosen such that $\partial h / \partial y' = 0$.
y''	A Cartesian coordinate in a system chosen such that $\partial u / \partial y'' = 0$.
Z	The program symbol for u.
ZD	The program symbol for ϵ .
ZD_ _	(X,Y,XX,XY,YY) The program symbols for derivatives of ϵ in the xy-coordinate system.
ZT_ _	(X,Y,XX,XY,YY) The program symbols for derivatives of u in the xy-coordinate system.
ZX	The program symbol for the x-component of the current in the xy-coordinate system.
ZX_ _	(X,Y,XX,XY,YY) The program symbols for derivatives of ZX in the xy-coordinate system.
ZY	The program symbol for the y-component of the current in the xy-coordinate system.
ZY_ _	(X,Y,XX,XY,YY) The program symbols for derivatives of ZY in the xy-coordinate system.
α	The angle the x'-axis is rotated with respect to the x-axis such that $\partial h / \partial y' = 0$.
α_c	The angle the x''-axis is rotated with respect to the x-axis such that $\partial u / \partial y'' = 0$.
β	The ray separation factor.
γ	The wavelet direction defined with respect to the positive x-axis.
Δt	The time step interval between ray points.
ϵ	The current direction with respect to the positive x-axis.
ϵ_β	The difference between the fourth and fifth order Runge-Kutta solutions of β .

ϵ_{3t}	The difference between the fourth and fifth order Runge-Kutta solutions of $d\beta/dt$.
$\hat{\theta}$	The wave packet direction defined with respect to the positive x-axis.
κ_G	The ray curvature of the wave packet.
κ_V	The ray curvature of a monochromatic wave.
λ	The wavelength.
π	3.1415927
ϕ	The ray direction defined with respect to the positive x-axis.
τ	The tangential stress per unit area at the bottom.
ψ	The angle $(\psi - \gamma)$.
ω	The radian frequency $(2\pi f)$ of the wave relative to the current.

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20. ABSTRACT (Continue on reverse side if necessary and identify by block number) The theory and numerical methods are presented for determining the paths and wave heights of gravity water wave packets. Both variable water depths and currents are considered. The wave height is computed accounting for the effects of shoaling, refraction, and energy dissipation. A ray curvature expression is used to determine the wave packet trajectories where the speed of the packet is given by $G = (d\omega/dk) \cos \alpha$. The symbol α denotes the angular		

frequency, k is the wave number, and ϕ is the difference between the direction of the wave packet and the direction of the wavelets within the packet. The wavelet direction is determined at each point of the wave packet trajectory. The wave packet and ray directions differ when there are currents. The calculations for variations in water depth are greatly simplified by choosing a coordinate system at each ray point in which one axis is aligned parallel with the direction of the gradient of the water depth. In a similar fashion, the calculations involving variations in current are simplified by choosing a coordinate system at each ray point in which an axis is taken parallel with the direction of the gradient of the current magnitude. Example printouts and plots are presented to illustrate the wave prediction method.

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END

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DTIC

D_n

The incremental distance in grid units between ray points.

DPHIDX

The program symbol for the derivative of ϕ in the x'y'-coordinate system (water depths).

DUD

The ratio of the phase speed at the present ray point to the value at the previous ray point.

FKAC The program symbol for the packet ray curvature considering only variations due to currents.

FKAD The program symbol for the packet ray curvature considering only variations due to water depths.

FKBAR The average of the packet ray curvature at the present and new ray points.

FKK The value of κ_G in radians/grid unit at the new ray point.

SURFACE. As a result, the initial value of dp/dt for currents is determined analytically. This value is used in the Runge Kutta calculations of β and $d\ell/dt$.

IPLG

When IPLG is zero a check is made in HEIGHT to determine if there should be a breakup of the time step interval in order to maintain the desired accuracy in the calculations of either β or the ray path. If there is a division of the time step interval, IPLG is set equal to one once the time step interval is sufficiently reduced. When IPLG

- k The wave number $2\pi/\lambda$.
- LI The number of lines of printout between page and column headings.
- L_i Expressions used in the Runge-Kutta calculations of β and $d\beta/dt$ where $i = 1, 2, \dots, 9$.
- ℓ The perpendicular distance between rays.

NGO

The value of NGO is determined in MOVE. If a ray point lies within one and one half grid units of a grid boundary NGO is 2. Otherwise, NGO is 1. (Initialized in RAYN.)

NOLINE

An index used to determine when to write page and column headings depending upon the number of lines of printout.

PATI

A program symbol for p. The value of p at the point prior to the new ray point.

PHI

The program symbol for ϕ .

POT

A program symbol for p. The value of p at the new ray point.