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a low loss guasioptical cavity for a two-stage free electron laser (FFL)

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Abstract

A quasiontical cavity consisting of a cylindrical, metallic, overmoded, TE_{01} wavequide between two spherical end mirrors will be used to contain long-wavelength (~ 1 mm) pump radiation in a two-stage FEL. The major loss mechanism is found to be mode conversion. Two different modified cavities are shown to suffer negligible mode conversion, and two more possible approaches, with low mode conversion and additional advantages, are discussed.

I. Introduction

In a two-stage FEL, intense first-stage radiation acts as a short spatial period (~ 1 mm) pump field to produce shorter wavelength second-stage output with relatively modest electron beam energy.¹ Significant gain can be achieved in the second stage only if the first stage radiation can build up to intensities of 10^7-10^8 W/cm². In order to accommodate these intensities and provide a region of uniform interaction between the 1-mm radiation and the electron beam, we propose a waveguide laser configuration Figure 1).



λ_{pump}= 1mm

λIR = 5.3μ

Figure 1. TP₀₁ cavity. The electron beam travels along the guide axis from right to left. The pump and infrared waves separate due to differential diffraction in the free-space regions.

We discuss general features of this configuration in Section II. In Section III the loss due to mode conversion is described and weighed against other loss mechanisms. Minimizing the losses helps achieve high intensity and increases the overall efficiency of the twostage laser. Mode conversion, which is the most significant loss, may be reduced by certain cavity modifications, which are described in Section IV. Other aspects of two-stage Entdesign are discussed in an accompanying article.²

II. General features of the TFOI cavity

A two-stage FFL cavity must provide interaction regions for both stages, suffer low pump losses, and transmit a fraction of the second-stage radiation. Both the first-stage and second-stage interactions take place in the wavequide where good overlap between the fields and the electron beam can be achieved. The electron beam passes through the second-stage interaction region with the low energy spread necessary for the interaction. Then it passes through the first-stage magnetostatic wiggler, acquiring a relatively large beam energy spread as described elsewhere in this volume.³

The cylindrical wavequide shown in Figure 1 supports the TE_{01} circular mode. The most important field component of this mode is the azimuthal electric field, E_{01} , which has an annular profile as shown in Figure 2. Revond the quide this annular mode diverges with a diffraction angle proportional to λ/a , where λ is the pump wavelength and a is the quide radius. The radial profile of E_{01} remains annular, and the magnitude of E_{01} near the cavity axis grows smaller. The infrared mode is also annular, but its diffraction angle, proportional to λ_{IR}/a , is much smaller than that of the pump field. Thus annular mirrors permit passage of the infrared mode on axis with low transmission of the 1-mm pump field. As λ/a increases, this mirror-hole loss decreases, but waveguide attenuation increases.



Figure 2. Mirror-hole diffraction losses are low due to annular field distribution.

Figure 3. TE₀₁ resistive losses are the lowest of any guided mode.

As Figure 3 shows, the π_{01} mode is the lowest loss mode in an overmoded ($\lambda << 2a$) circular wavequide. Conventional rectangular guide has no mode with comparable short-wavelength behavior. Thus the π_{01}^{π} circular mode offers the best combination of guided propagation and low loss. The π_{02}^{π} mode has a factor of four higher attenuation in the waveguide and higher transmission through the mirror holes. Figher-order π_{01}^{π} modes and all other modes suffer even higher losses.

The wall currents in π_{01}^{μ} wavequide are purely azimuthal. Thus, the quide may be segmented axially with little increase in wavequide attenuation. This permits the introduction of an axial electric field for gain optimization. It will also greatly increase the losses for non- π_{01}^{μ} modes.

TIT. Mode conversion

Mode conversion, also known as coupling loss, results from the failure of the reflected radiation to duplicate precisely the original $\frac{\pi E}{01}$ mode at the waveguide end. In our analysis, as in previous waveguide laser work, ⁴ the radiation propagating between the guide and the mirror is represented as a set of free-space modes, each with a spherical wave front, and the curvature of the spherical mirror is chosen to match these wave fronts. The appropriate modes are the Gauss-LaGuerre $\frac{\pi EM_p}{\pi} * modes$, for which the azimuthal electric field at the beam waist is given as

$$E_{\phi, p}(u) = \sqrt{\frac{2u}{\pi w_{o}^{2}}} L_{p}^{(1)}(u) \frac{1}{\sqrt{p+1}} e^{-u/2}, \qquad (1)$$

where $u=2r^2/w_0^2$. For convenience, we choose to locate the beam waist at the wavequide end. This condition, together with the matching of wave-front curvature to mirror curvature, determines the beam waist radius w_0 for the complete set of free-space modes. Different values of w_0 are associated with different mirror curvatures.

If the TE_{01} mode at the end of the wavequide is expressed as

$$E' = \sum_{p=0}^{n} C_{p} E_{\phi,p'}$$
(2)

then, after the trip to the mirror and back, we have

$$\mathcal{R}_{\phi} = \sum_{p=0}^{r} C_{p} \mathcal{R}_{\phi,p} \exp(2i\phi_{p}), \qquad (3)$$

where $\phi_p = 2p \tan^{-1} [L\lambda/\pi w_o^2]$, L is the guide-mirror separation, and λ is the pump wavelength. Throughout this paper the mirror diameter is assumed to be large enough to allow us to ignore the radiation lost around the edge. The reconstructed field \mathbb{R}'_{μ} will not, in general, be equal to \mathbb{R}_{μ} . This is because the free-space modes suffer a relative phase shift, $2\phi_p$, proportional to their mode number. (See, for example, Kogelnik and Li.⁵) The phase shifts are important because the amplitudes of high-order free-space modes are significant, as seen in Table 1.

When π_{ϕ}' is expanded in terms of $\pi_{E_{OI}}$ circular-wavequide modes, the fraction of power converted into non- $\pi_{E_{OI}}$ modes is found. This will be small if ϕ_{p} is close to px or 0. We will be concerned with the former condition, which can also be expressed as

 $L\lambda/\pi w_0^2 >> 1.$ ⁽⁴⁾

Larger quide-mirror separations lead to lower mode conversion. Smaller beam waists (maintaining a fixed ratio of beam waist radius to waveguide radius) also lead to lower mode conversion. Figure 4, which shows the power not in the TE_{01} mode after a single reflection for the case $w_0/a=0.3$, illustrates this behavior clearly. The value $w_0/a=0.3$ is chosen because it minimizes the mode conversion.

These mode conversion values match with results from a Fresnel-Huygens propagation code. The propagation code avoids a free-space mode field representation by calculating the far-field radiation pattern at the mirror directly from the TE_{D1} aperture distribution,

Table 1.	Free-Space	Mode	Coefficients	•

	w _o ⁄a = 0.300 Minimum mode conversion loss.		w _o ∕a ≠ 0.564 Maximum ^{TrEM} Ol*amplitude.		w _o /a = 0.675 Peak of TFM ₀₁₄ mode located at same radius as peak of TF ₀₁ mode.	
<u> </u>	מ	ط _ی	p	C _م	đ	c _م
	 0	0.6153#+00	0	0.98345+00	0	0.9447#+00
	1	5828F+00	1	63192-03	1	0.2947E+00
	2	0.44005+00	2	1583E+00	2	3544E-01
	3	26957+00	3	4704E-01	3	10528+00
	4	0.1139#+00	4	0.3764F-01 0.4585F-01	4	6372E-01
	5			0.15338-01	5 6	0218R-02
	5	0.2040 = 01	7	- 1291F-01	7	0.35458-01
	Ŕ	0.1125 = 01	Ŕ	2311E-D1	8	0.2427E-01
	9	13885-01	ğ	1673E-01	.9	0.6822E-02
	10	5760F-02	10	33687-02	10	8117E-02
	11	0.88756-02	11	0.80815-02	11	1630E-01

where the aperture is the open wavequide end. $\mathbb{R}_{\phi}^{\prime}$ is then given by the far-field pattern in the plane of the aperture due to the distribution on the mirror.

Guide-mirror separations larger than a few meters are inconvenient experimentally. Reducing the quide radius, a, reduces mode conversion but increases the resistive loss in the wavequide. Flectron beam optics also becomes more difficult with a smaller quide diameter. Since we wish to hold the total cavity losses below one percent and maintain a relativeley large quide diameter, we would like to reduce mode conversion substantially.



Piqure 4. Overmoding trades wavequide attenuation for mode conversion.

Figure 5. Mirror-hole diffraction is small for likely dimensions.

For example, with L=3m and a=1.2 cm, the total round-trip cavity losses are 1.8%. Of this total, 0.9% is due to mode conversion and 0.6% is due to resistive losses in the wavequide and at the end mirrors. Methods of reducing mode conversion to negligible levels are discussed in the next section. To reduce losses further the mirrors and wavequide could be cooled to reduce absorption.

What remains is the diffraction loss through the infrared output coupling hole. This loss depends on the guide radius as well as the guide-mirror separation, L, because for lowloss infrared transmission the hole radius is of the order of the guide radius. Figure 5 shows the dependence of this loss on cavity parameters. In the above example we have $L\lambda/a^2=20.8$, which for a symmetric cavity with holes in both mirrors implies a little over 0.3% contribution to the total losses. This loss can be reduced by increasing L.

IV. Improved cavity designs

Four different approaches are described for reducing mode conversion. The first two, involving modified reflectors, have already led to theoretically viable solutions, as will be shown. Work in progress on the horn and closed-cavity approaches is discussed. A less practical fifth approach, phase-conjugate reflection, is also mentioned.

Two-element reflectors

Mode matching with a single spherical reflector, as discussed in Section IVI, is imperfect unless the guide-mirror separation is \bullet or 0. At intermediate values of the separation, free-space modes with different radial mode numbers arrive back at the waveguide with relative phase shifts as discussed in the previous section, and imperfect reconstruction of the waveguide mode results. A two-element reflector (see Figure 6) provides an additional relative phase shift in the lens-mirror region which can be adjusted to make all round-trip relative phase shifts an integral multiple of 2π . A derivation of the condition which the reflector parameters must satisfy is outlined below.



Figure 6. Two-element reflector.

For convenience we define the Rayleigh range, $Z_0 = \pi w_0^2/\lambda$, where w_0 is again the beam radius at the waist. Let 7_{01} and 7_{02} be the Rayleigh ranges associated with the beam between the wavequide and the lens and the beam between the lens and the mirror, respectively. Distances L_1 , L_2 , focal lengths of lens f and mirror f_m , and lens-beam waist distance 7_2 are shown in Figure 6. The relative phase shifts between successive modes, and associated with the two beams as indicated in Figure 6, are given as follows:

$$\Psi_{1,f} = 2\pi a n (2\pi)^{1/2} (1)$$
(5b)

$$\Psi_{2,f} = 2 \tan \left[-\left(\left| \frac{\pi}{2} \right| - \frac{L_2}{\pi_0} \right) \right].$$
(5d)

The total relative phase shift between successive free-space modes propagating from the waveguide to the mirror is

$$\psi_{0} = (\psi_{1,f} - \psi_{1,i}) + (\psi_{2,f} - \psi_{2,i}). \tag{6}$$

Making use of relations between free-space beam parameters (see Reference 5) leads eventually to

$$\phi_{0} = 2 \tan^{-1} \left[\frac{fL_{1} + fL_{2} - L_{1}L_{2}}{z_{01}(f - L_{2})} \right].$$
(7)

Setting either the numerator or denominator equal to zero in the argument appearing in Foustion 7 gives the result that ϕ_0 is some multiple of x. Thus, the round trip relative phase shift for all free-space modes is an integral multiple of 2x.

We examine the latter case, $f=L_2$, and make the further simplification $L_1=L_2=f$. In this case we also find $7_{01}7_{02}=f^2$ and $7_2=L_2$. The result for 7_2 implies that the mirror is located at the second beam waist and, thus, will be flat $(f_m=e)$. With L_1 equal to L_2 , we can easily fold the optical system by replacing the lens with a reflector of focal length f and moving the flat to the end of the wavequide. Pique 7 indicates the ray paths in such a system and lists parameters associated with a 3m separation. Radiation reentering the waveguide directly from the curved mirror without reflecting off the plane mirror is not correctly conditioned for mode matching. However, the field is small near the axis for the TEM_p * modes so that this mismatch is insignificant for a 3m separation.



Figure 7. Folded two-element reflector with 3m separation.

Thus, without increasing the overall cavity length, mode conversion losses can be made negligible. In the 3m case this eliminates a 0.9% loss, while introducing a separationindependent 0.6% absorption loss due to the four additional reflections. Cooling would now be even more desirable. Total round-trip losses could be reduced from 1.5% to about 0.9% with liquid nitrogen or to about 0.3% with liquid helium.

Wave-front reflector

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Another approach to the reduction of mode conversion requires figuring of the mirror surface to match the incident wave front of the total field, given by the sum of the free-space modes. Such a mirror simultaneously reverses the propagation direction of the entire wave front, which then follows exactly in reverse the evolution undergone during propagation from the wavequide to the mirror. No phase conjugation occurs; only carefully controlled conventional reflection is required. In terms of free-space modes, one can say that the mirror reduces the optical path length for each higher-order mode by the amount required to compensate for the relative phase shifts by making use of each mode s unique transverse profile. Thus, the phase shifts vanish, and the returning radiation precisely duplicates the original TH_{01} mode.

The total electric field along a surface of uniform phase can be written

$$\mathbf{R}_{\phi} = \left[\sum_{p=0}^{\infty} C_{p} \frac{w_{0}}{w} L_{p}^{(1)}(u) e^{-u/2} \exp\left[-i(kz-\phi_{p}) - r^{2}(1/w^{2}+ik/2R)\right]\right]^{e^{i\omega t}},$$
(8)

where

$$\operatorname{Im} \left[\sum_{p=0}^{m} C_p L_p^{(1)}(u) \exp(i\phi_p) \right] = 0$$
(9)

with $\phi_p = 2p \tan^{-1}(7/7_0)$ and $u=2r^2/w^2$. The coefficients C_p include the normalization constants. Here, R is the radius of curvature of the wave fronts of the individual modes, and w is the beam radius at arbitrary 7. R and w are given as

$$R = \pi (1 + \pi_0^2 / \pi^2)$$
 (10a)

$$x^2 = x_0^2 (1 + \pi^2 / \pi_0^2).$$
(10b)

The condition imposed by Equation 9 determines Z(r) for an arbitrarily selected value of the overall phase at a fixed time. We generality is lost in making this selection. Equation 9 can be solved numerically for 2.

In order to be sure of achieving low mode conversion, we will need to evaluate the errors introduced by the paraxial approximation in each of the prospective cavity designs. For example, spherical mirrors might be replaced by parabolic mirrors. If non-paraxial corrections to the mirror figure are required, they could most easily be implemented as a modification to the wave-front reflector, since aspherizing is already necessary. No additional absorption losses would be incurred as with the two-element reflector.

Horns

An appealing solution to the mode conversion problem would be to convert the TP_{01} wavequide mode to the lowest order free-space mode with very little power in higher-order free-space modes. Welative phase shifts between modes would then have no significance. This approach would require specially designed horns on the ends of the wavequide. In addition to reducing mode conversion, such horns would radiate a cleaner far-field pattern than the open pipe, permitting a larger mirror-hole diameter and a smaller overall mirror diameter. Morne may also be the least expensive solution to implement. Morns are commonly designed with the goal of reducing the side lobes present in the radiation matterns of open-ended, single-mode waveguides. Side lobes imply the presence of high-order free-space modes. Thus our design criteria will be similar to those commonly used, but they will be more stringent.

The closest approach to the required horn design seems to be the aperture-matched horn reported by Burnside and Chuang.⁶ Flared surfaces attached to the end of a conventional horn have been found theoretically and experimentally to reduce side lobe power levels by roughly a factor of three below the already low levels present in the pattern produced by the unmodified horn (see Figure 8). The unmodified horn is similar to our open-ended waveguide in that a single mode is incident upon an aperture which has dimensions large compared to a wavelength. Thus, a flared surface may be able to reduce mode conversion.





Figure 8. (a) Aperture-matched horn (after Ref. 6, copyright 1982 IEEE).

The contours discussed in Reference 6 are probably not adequate for the performance we require. Ideally, a design procedure should be created in which an optimum or near-optimum contour is found as a function of the coupling between the TF_{01} wavequide mode and the TFM_{01*} free-space mode. Such a design procedure exists for the simpler problem of a

nonlinear taper, which couples the TF_{01} mode in circular waveguide to the same mode in a waveguide of different diameter by carefully controlling the TF_{02} power in the taper.⁷ Adaptation of this procedure to our problem must account for many unwanted modes rather than only one.

Closed cavity

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A different approach is to enclose completely eqi between the wavequide and the spherical mirror with a tapered wavequide as shown in Figure 9. If the maximum taper

angle, θ_0 , is no more than a few degrees, then only the lowest two cone modes are required to represent the field in the tapered region adequately.

(b)



Figure 9. (a) Closed cavity with a linear taper.



nonlinearly tapered section.

The TF cone modes are given by

$$E_{\phi,n}(\theta,R) = \int_{T}^{C} R_{\nu_{n}+1/2}^{(2)}(kR) \frac{d}{d\theta} \left[P_{\nu_{n}}(\cos\theta) \right], \qquad (11)$$

where n is the transverse mode number. Azimuthal symmetry is assumed. C is a constant, R is the distance from the cone's vertex, k is the free-space wavenumber and θ is the angle with respect to the cone's axis. $\mathbb{R}^{(2)}$ and P are, respectively, the Rankel function of the second kind and the resociated Legendre function. The order of each function is indicated by a subscript, which is positive but not, in general, an integer. The v_n (n=1,2,3 ...) are a discrete set of numbers which are found numerically by satisfying the condition

$$\mathbf{E}_{\phi,\mathbf{n}}(\theta_{\mathbf{C}'}\mathbf{R}) = 0, \tag{12}$$

The Theor cone modes are very similar to the "Ron circular-waveguide modes. Thus, the best cavity performance would be obtained by arranging for only the TR_{01} mode to be incident upon the mirror. As in the case of the lowest-order free-space mode, this permits a large mirror-hole diameter and relatively smaller overall mirror diameter. Good conversion to the TR_{01} cone mode could be achieved by the nonlinear section of the compound taper shown in Figure 9b. This could be designed according to the procedure given in Reference 7 with little modification.

The simpler case of a linear taper (Figure 9a) is examined briefly here. About one percent of the power is allowed to propagate in the TE_{02} cone mode and smaller fractions in higher-order modes. These fractions are found by expanding the incident TE_{01} circular-waveguide mode in terms of the functions given in Equation 11, accounting for the phase variation of the incident mode along a constant-phase spherical surface of the cone modes. As in the free-space case, E_{ϕ}' is evaluated including the relative phase shifts accumulated by the cone modes propagating to the mirror and back. The phase shifts are found by evaluating the Wankel function in Equation 11. Then E_{ϕ}' , in turn, is expanded in terms of TE_{on} circular-waveguide modes in order to determine the mode conversion.

Some results are displayed in Figure 10. The minima occur when the length of the taper is sufficient to introduce approximately 180° of relative phase shift between the first two cone modes. Arriving back at the waveguide, the TEO, cone mode converts into a TEO, circular mode and a smaller amplitude TF_{02} mode. The TF_{02} cone mode converts mostly to the TF_{02} circular mode. When the phase shift is 180° , these two πE_{02} waves approximately cancel, nearly eliminating the major contribution to mode conversion in the closed cavity. The relative phase shifts are smaller as the diameter increases. Thus, a greater length is required to accumulate the necessary 180° as Figure 10 shows.



Figure 10. (a) Closed-cavityomode conversion vs. linear taper length with $\theta_0 = 2^{-1}$.

The choice of taper angle involves a tradeoff between mode conversion and a reasonable taper length to reach the diameter required to couple out the infrared radiation. The power in higher-order cone modés increases quickly above $\theta=3^{\circ}$. The waveguide diameter can then be chosen to minimize the loss through the mirror hole (which again has roughly the same diameter as the waveguide) and the loss due to waveguide attenuation. Figure 11 shows the tradeoff associated with this choice,



Figure 11. In the closed cavity a tradeoff exists between mirror-hole loss and wavequide attenuation.

Phase-conjugate reflectors

Phase-conjugate reflectors have been considered for use as end mirrors.⁸ There would be no mode conversion with such reflectors. However, the efficiency of present phase conjugators is low by our standards, either through low reflectivity or large power requirements. Higher efficiency may result as researchers continue their efforts.

V. Conclusions

Mode conversion is identified as a major loss mechanism in a TP_{01} quasioptical cavity. Two possible cavity modifications are shown to eliminate mode conversion. These are the two-element reflector and the wave-front reflector. Two other approaches, the horn and the closed cavity may be able to reduce both mode conversion and mirror hole losses. The use of phase-conjugate reflectors depends on future demonstration of efficient operation.

IV. Acknowledgements

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