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# COMPUTER CONTROL AND ACTIVATION OF SIX-DEGREE-OF-FREEDOM SIMULATOR

EDWARD G. DAVIES RICHARD CHOU JOHN STONE KACHEUNG TSUI MAURICE Z. DARWISH WILLIAM REISENER FRANKLIN RESEARCH CENTER TWENTIETH AND PARKWAY PHILADELPHIA, PA 19103

> D. E. FRERICKS R. J. RADKIEWICZ PROJECT ENGINEERS ARRADCOM

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Following the acquisition of a passive ware Simulation Section, Rock Island Ar Research Center was contracted to desig tions for conversion from a passive to outlines and details the design philoso	nulti-degree-of-freedom simulator by th senal, Rock Island, IL, the Franklin n and to make the necessary modifica- an activated simulator. This report phy used for providing programmable
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motions, vibrations, and spring rates required for activating the passive simulator. This report also documents the changes required in the hydraulic power supply, the mechanical changes to the yaw and pitch gimbals, and the electronic changes to the spring rate controller.

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#### INTRODUCTION

The development phase, as recorded in this report, involved several areas of mutually dependent effort.

1. Calculations were made to determine the various mechanical design parameters and requirements.

2. Considerable effort was made to locate suitable commercial equipment to satisfy the design requirements. Negotiations were carried on with at least three potential suppliers of major components such as hydraulic pumps, motor and controls, servo valves, actuators, etc.

3. Mechanical layouts were made using the selected commercial equipment.

4. Servo analyses were made to verify that selected equipment would perform as required, and that it operated in a stable manner.

5. Hydraulic schematics were developed for the various systems.

6. Standard servo configurations were developed for control of the pitch and yaw circuits including features to insure safe, smooth start-up and fail-safe operation.

7. An extensive study was conducted on the analog and digital computer of the Franklin Institute Research Laboratories to verify the proposed spring rate and damping ratio control system. The design of the actual equipment was then developed.

8. A preliminary design was performed for the three vibration systems. The tail rotor vibrator and the auxiliary device vibrator units have reasonable design parameters. Since the main rotor vibrator unit is considerably more difficult because of the large mass to be moved, a compromise solution is presented.

Each of these phases, including mathematical support, is discussed in this report.

#### MATHEMATICAL MODEL

Discussion

The purpose of the following derivation is to provide the input data necessary to program the servo systems to:

1. Provide specified spring rates as measured at the platform,

2. Eliminate the effects of gravity, due to the finite spring rate of the triogonal actuators, as a result of variations in the geometry, and

3. Derive the input signals necessary to produce the desired yaw and pitch motion. In addition, a simplified analysis of the system dynamics was presented, to assess the importance of cross-coupling effects among the various servo systems.

The basic analysis has been separated into the following two major sections: (1) Calculation of the mean values, and (2) Calculation of linear derivatives for the combat vehicle. The system dynamics is also presented. A system of linear coefficients was selected to avoid continuous real-time calculation of all the variables, which would require excessive computing time and facilities. By linearizing the solution about the mean values, the time varying components can be derived from the input time functions by means of linear calculations. This greatly reduces the on-line computing facilities required. The mean values and linear derivatives can be computed off-line, and need be modified only if the basic geometry is changed, i.e., location of weapon, type of vehicle, etc.

The analysis was developed in general terms for each of the specified geometries to expand its use. In many cases, many of the parameters will be zero, and the actual calculations can be simplified. The equations were written in terms of state variables to simplify the notation. In most cases, these vectors consist of the six components of velocity or position necessary to specify the state of a particular element in the system--weapon, aircraft, triogonal system, etc. The basic approach was to develop the equations necessary to relate forces and moments in one coordinate system to those in another and to relate the velocities (linear and angular) of one system to another.

The concept of impedance was introduced to describe the relationship between the forces and moments and the resultant velocities. With this method, the weapon impedance can be found in terms of the output impedance of the triogonal actuators. For a desired set of spring constants at the platform, the corresponding spring constants of the actuators are then found.

An important requirement for the system is the elimination of gravitational extensions of the triogonal actuators from their desired neutral position. This is particularly important when the gimbal angles are changed, resulting in a reorientation of the gravity vector for the triogonal system. Before firing, in some cases, it will be necessary to adjust the gimbal angles manually to aim the weapon. For this, a continuous calculation of the gravitational loading must be performed. Since relatively large angular excursions may be required, a linearized approach will not give sufficient accuracy. The fixed coefficients involved in the calculation can be derived prior to the run, once the relationship among vehicle, triogonal system, and gimbal system is established. During a firing run, this same calculation can be used to correct for the time-varying inputs to the gimbal system. In addition, linearized corrections will be made to correct for variations in the triogonal actuator lengths due to yaw variations of the triogonal geometry when used with the combat vehicle.

A description of the vehicle dynamics has also been included, primarily to examine some of the cross-coupling effects. Prior calculations have described the servo systems and the effects of the geometry on them. This has been primarily a description of the output impedance of the support system for the vehicle. To complete the description of the entire system, it is necessary to add the equations to this, describing those elements external to the support system; i.e., the vehicle dynamics. By combining all these equations, an analytic solution for the system response was obtained. However, this requires the solution of six simultaneous nonlinear differential equations, which would have to be done with the aid of a computer. Even without deriving the overall system response, it is possible to estimate the coupling effects due to the external systems. For this purpose, equations have been derived which describe the servo output quantities (gimbal and triogonal forces and tail boom velocities) in terms of the input quantities (gimbal and triogonal velocities, tail boom forces, and weapon forces). To simplify the results, the mass of the support equipment has been neglected. This will produce an additional inertia load on the servo systems, but because the vehicle mass will be considerably larger, this simplification is justified for estimating purposes.

The cross-coupling terms result from two effects: (1) The inertia terms (acceleration and gyroscopic forces) are due to the mass of the vehicle, and (2) There are direct coupling terms due to the geometry. In this latter class are those between the tail boom and triogonal servos and among individual actuators in the triogonal system. These expressions have been presented in general terms, and the direct coupling terms were evaluated for a particular case. The inertia terms were not evaluated, since this requires a knowledge of the system velocities, which must be obtained from the solution to the system response discussed previously. The inertia effects are most significant for highly underdamped systems, and the energy stored within the system can build up to large values during firing due to inappropriate choices of firing rate and resonant frequencies. Generally, however, it is reasonable to assume the steady state values, due to the direct coupling terms, are representative of the forces and deflections that will be experienced. The passive system mathematical model makes use of the formula derived in the aircraft neutral position and the aircraft linear coefficients as a basis for the development of a computer program for use in operation of the simulator as a passive system. This program accepts as input the desired stiffness in six degrees-of-freedom and prints out corresponding actuator stiffness, accumulator precharge pressure and the top and bottom actuator pressures.

#### Computer Requirements

Many quantities must be calculated, both in preparing for and during an experimental run. These calculations are usually done off-line before the run on a linearized basis because of the excessive time and the computer facilities required to make continuous real time calculations.

Initially, the mean values of all quantities will be found and stored. Then linear coefficients will be developed to compute real time variations from the means during the run. Since the angular variations will generally be quite small (up to 10 degrees), this method will give reasonable accuracy, and the computational noise generated by this technique will be considerably less than the continuous calculation of total values.

3

A computer program has been prepared to calculate manual input values of effective mass, spring constant, and actuator lengths for quasi-static operation. In addition, the program can be used in a dynamic situation when the simulator is pitching and yawing. All calculations are based on derivations in the following sections and the computer program is described in detail in appendix A.

Primarily because of the complexity required to make pitch angle corrections to the actuator spring constant, all calculatuions will be performed digitally. The large number of coefficients required to be input to analog circuitry for this calculation would require an excessive number of D/A converters and storage elements. The complete calculation of spring constants, on an analog basis, could be performed, using prewired patch boards, selected for the particular choice of axes for which spring constants are specified. However, the resulting accuracy would be poor, due to the large number of multiplications required.

#### Neutral Position

Two modes of operation are planned using the aircraft fuselage: (1) A fixed weapon emplacement where the gimbal angles will be fixed to train the weapon on target, and (2) A movable weapon turret with varied gimbal angles with the weapon tracking system used to maintain the weapon on target.

In both cases, it is desired to maintain the triogonal system at or near its neutral position (except for reaction to weapon forces) and to maintain a constant platform impedance. In either case only the mean value calculations are required, since the geometry between the triogonal system and the vehicle is not varied with time.

For the combat vehicle, an additional pitch actuator has been added between the triogonal platform and the vehicle CM. This will supply the necessary dynamic pitch motion, while the triogonal system will supply the yaw motion. The gimbal system will be locked in place at the desired position. The mean triogonal position will again be the neutral position (all actuators equal length). Since, in this case, the geometry between the triogonal system and the vehicle does change with time, both the mean values and the linearized deviations from the mean are required.

#### Triogonal Actuator Lengths

The mean actuator lengths are determined so that a prescribed linear and angular displacement exists between the gimbal and the aircraft platform mounting plates. This displacement is defined by the vector distance from the origin of the gimbal coordinate system to the origin of the platform coordinate system, as measured in the platform system, and the relative Euler angles required to transform the gimbal system into the platform system. In general, yaw, pitch, and roll will be the rotation order for right-handed systems. The exception is the gimbal system which will operate in the reverse order of pitch and yaw because of the way it is constructed. The x-axis (roll) is defined in the forward direction, the y-axis (pitch) in the starboard lateral direction, and the z-axis (yaw) in the downward vertical direction.

Displacements defined by the vector are

$$\mathbf{x}_{1} = \begin{pmatrix} \mathbf{x} \\ \mathbf{y} \\ \mathbf{z} \end{pmatrix}$$
(1)

and the Euler angles by

$$\mathbf{x}_{3} = \begin{pmatrix} \phi \\ \theta \\ \psi \end{pmatrix}$$
(2)

The angular velocities of a point from one system to another are given

$$\dot{\mathbf{x}}_2 = \begin{pmatrix} \mathbf{p} \\ \mathbf{q} \\ \mathbf{r} \end{pmatrix} = \mathbf{G} (\mathbf{x}_3) \dot{\mathbf{x}}_3$$
(3)

where

by

$$G'(\mathbf{x}_{3}) = \begin{bmatrix} 1 & 0 & -\sin\theta \\ 0 & \cos\phi & \sin\phi & \cos\theta \\ 0 & -\sin\phi & \cos\phi & \cos\theta \end{bmatrix}$$
(4)

for all except the gimbal system. For this

$$G'(\mathbf{x}_{3G}) = \begin{bmatrix} \cos\theta_{G} \cos\psi_{G} & \sin\psi_{G} & 0\\ -\cos\theta_{G} \sin\psi_{G} & \cos\psi_{G} & 0\\ \sin\theta_{G} & 0 & 1 \end{bmatrix}$$
(5)

The displacement of the origins of two systems are defined as measured in the second system, into which the first is transformed. For instance, a point in the gimbal system can be transformed into the platform system through the equation

$$x_{1p} = E(x_{3p}) x_{1G} - r_p$$
 (6)

where the angular transformation

$$E(x_{3}) = E_{3}(\phi) E_{2}(\theta) E_{1}(\psi)$$
(7)

and

$$E_{1}(\psi) = \begin{bmatrix} \cos\psi & \sin\psi & 0 \\ -\sin\psi & \cos\psi & 0 \\ 0 & 0 & 1 \end{bmatrix}$$
(8)  

$$E_{2}(\theta) = \begin{bmatrix} \cos\theta & 0 & -\sin\theta \\ 0 & 1 & 0 \\ \sin\theta & 0 & \cos\theta \end{bmatrix}$$
(9)  

$$E_{3}(\phi) = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos\phi & \sin\phi \\ 0 & -\sin\phi & \cos\phi \end{bmatrix}$$
(10)

The displacement,  ${\bf r}_{\rm p},$  is the vector from the origin of the gimbal system to the origin of the platform system and measured there.

The location of the pivot points for the n-th actuator (n=lto6) is given in the gimbal system by

$$b_{n} = \begin{pmatrix} b \\ x \\ b \\ y \\ b \\ z \\ n \end{pmatrix}$$
(11)

The other end of the n-th actuator is located in the platform system at the point

$$a_{n} = \begin{pmatrix} a_{x} \\ a_{y} \\ a_{z} \end{pmatrix}_{n}$$
(12)

It then follows that the vector length of the n-th actuator in the platform system is given by

$$l_{n} = r_{p} + a_{n} - E(x_{3p}) b_{n}$$
 (13)

If we define

$$\mathbf{c}_{n} = \mathbf{E}(\mathbf{x}_{3p}) \mathbf{b}_{n} \tag{14}$$

then

$$l_n = r_p + a_n - c_n \tag{15}$$

The scalar length is found by premultiplying this by its transpose

$$(l_{0})_{n} = (l_{n_{t}} \cdot l_{n})^{1/2}$$
 (16)

These are the desired extended lengths (under gravitational load) for each of the actuators.

#### Direction Cosines of Actuators

The direction cosines of the actuators in the platform system are given simply by

$$\begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}_{n} = \frac{1}{(k_{o})}_{n} \qquad (17)$$

Velocity and Force Transformations

The scalar actuator velocities are determined from the relative velocity of the platform system to the gimbal system by first finding the vector velocities. For the n-th actuator, the vector velocity, in gimbal coordinate is

$$\dot{k}_{G} = x_{1G} + E(x_{3p}) \cdot a_{n}$$
 (18)

where

 $x_{1G} = E(x_{3p}) r$  is the location of the origin of the platform system in gimbal coordinates. But

$$\tilde{E}(x_{3p}) = E(x_{3p}) W(x_{2p})$$
 (19)

where

$$W(x_{1}) = \begin{bmatrix} 0 & -z & y \\ z & 0 & -x \\ -y & x & 0 \end{bmatrix}$$
(20)

so that

$$\dot{a}_{G} = \dot{x}_{1G} + E(x_{3p}) W(\dot{x}_{2p})a_{n}$$
 (21)

This is also equal to

$$\dot{a}_{G} = \dot{x}_{1G} + E(x_{3p}) W(-a) \dot{x}_{2p}$$
 (22)

Relative to the gimbal system, the linear velocity of the platform system in platform coordinates is

$$\dot{x}_{1p} = E(x_{3p}) \dot{x}_{1G}$$
 (23)

Then, the actuator velocity in platform coordinates is

$$\hat{a}_{p} = \hat{x}_{1p} - W(a) \hat{x}_{2p}$$
(24)

The scalar actuator velocity is found by projecting this along the actuator

$$\dot{k}_{n} = \begin{pmatrix} \alpha_{n} \\ \beta_{n} \\ \gamma_{n} \\ t \end{pmatrix}, \quad \dot{k}_{p} = \begin{bmatrix} \alpha \\ \beta \\ \gamma \\ t \end{bmatrix} - \begin{bmatrix} \alpha \\ \beta \\ \gamma \\ T \end{bmatrix} \\ t \end{bmatrix}_{t} W(a)_{n} \begin{pmatrix} \dot{x}_{1} \\ -\frac{1}{\dot{x}_{2}} \end{pmatrix}_{p}$$
(25)

If we let

$$\begin{pmatrix} \lambda \\ \mu \\ \nu \end{pmatrix} = W(a) \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}$$
(26)

This becomes

$$\dot{a}_{n} = \left[ \begin{array}{ccc} \alpha_{n} & \beta_{n} & \gamma_{n} & \lambda_{n} & \mu_{n} & \nu_{n} \\ \hline \alpha_{n} & \alpha_{n} & \alpha_{n} & \alpha_{n} & \alpha_{n} \end{array} \right] \left( \begin{array}{c} \dot{x}_{1} \\ \dot{x}_{2} \end{array} \right)_{p}$$
(27)

The column matrix of scalar actuator velocities is then

$$\dot{\lambda} = F\left(\frac{\dot{x}_1}{\dot{x}_2}\right)_p$$

(28)

where

$$\mathbf{F}^{\dagger} = \begin{bmatrix} \alpha_{1} & \beta_{1} & \gamma_{1} & \lambda_{1} & \mu_{1} & \nu_{1} \\ \alpha_{2} & \beta_{2} & \gamma_{2} & \lambda_{2} & \mu_{2} & \nu_{2} \\ \vdots & \vdots & \vdots & \vdots \\ \vdots & \vdots & \vdots & \vdots \\ \alpha_{6} & \vdots & \vdots & \ddots & \ddots & \nu_{6} \end{bmatrix}$$
(29)

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Since the actuator pivots have no angular restraint, the force exerted on the platform by the actuator is directed along the actuator. If the scalar force in the n-th actuator is  $f_n$ , the forces and moments produced by the n-th actuator about the platform system are

$$f_{p} = \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix} f_{n}$$
(30)  
$$m_{p} = W(a) f_{p} = W(a) \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix} f_{n}$$
(31)

(31)

or

$$\begin{pmatrix} f \\ p \\ m \\ p \end{pmatrix}_{n} = \begin{bmatrix} \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix} \\ \hline W(a) \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix} \end{bmatrix} f_{n}$$
(32)

The sum of the forces and moments of all six actuators is then

$$\begin{pmatrix} -\frac{f}{m} \end{pmatrix} = F_{t} \cdot f_{l}$$
(33)

where  $\boldsymbol{f}_{\boldsymbol{\ell}}$  is the column matrix of all actuator scalar forces.

The velocity and force transformations for the rectilinear systems can be derived as follows: A point in the platform system is transformed into the aircraft system by

$$x_{1a} = E (x_{3a}) x_{1p} - ra$$
 (34)

The linear velocity of the origin of the aircraft system, if there is no relative motion between the platform and the aircraft systems, is equal to the velocity of the origin of the platform system plus the rotational components of the  $r_a$  vector. The velocity of the platform system in aircraft coordinates is

$$(x_{1p})_a = E(x_{3a}) x_{1p}$$
 (35)

while the angular velocity of the platform system in aircraft coordinates is

$$(\mathbf{x}_{2p})_a = \mathbf{E}(\mathbf{x}_{3a}) \mathbf{x}_{2p}$$
 (36)

Thus, the linear velocity of the aircraft system is

$$\dot{x}_{1a} = E(x_{3a}) \dot{x}_{1p} - W(r_a) E(x_{3a}) \dot{x}_{2p}$$
 (37)

Then, if

$$\begin{pmatrix} \dot{x_1} \\ -\dot{x_2} \\ a \end{pmatrix} = H (x_{3a}, r_a) \begin{pmatrix} \dot{x_1} \\ -\dot{x_2} \\ \dot{x_2} \end{pmatrix} p$$
(38)

The velocity transformation is

$$H(x_{3a},r_{a}) = \begin{bmatrix} E(x_{3a}) & -W(r_{a}) & E(x_{3a}) \\ ---- & --- \\ 0 & ---- \\ 0 & E(x_{3a}) \end{bmatrix}$$
(39)

Forces and moments exerted on the platform system are transformed to the aircraft system by

$$f_a = E(x_{3a}) f_p$$
(40)

$$m_a = E(x_{3a}) m_p - W(r_a) \cdot E(x_{3a}) f_p$$
 (41)

Thus

$$\left(\frac{f}{m}\right)_{a} = \left[\begin{array}{c} E(x_{3a}) & | & 0\\ \hline -W(r_{a}) & E(x_{3a}) & | & -E(x_{3a}) \\ \hline -W(r_{a}) & E(x_{3a}) & | & E(x_{3a}) \\ \end{array}\right] \left(\frac{f}{m}\right)_{p}$$
(42)

or

$$\begin{pmatrix} f \\ -\frac{f}{m} \end{pmatrix}_{a} = H_{t}'(x_{3a}, r_{a}) \begin{pmatrix} f \\ -\frac{f}{m} \end{pmatrix}_{p}$$
(43)

The force transformation is the inverse transpose of the velocity transformation.

Impedance Transformations

The impedance of a system is defined as the transformation which produces the system velocities in response to impressed forces and moments. Thus, in general

$$\begin{pmatrix} \dot{x}_1 \\ -\dot{x}_2 \end{pmatrix} = z \begin{pmatrix} f \\ -\dot{m} \end{pmatrix}$$
(44)

With this definition, the impedance in the platform coordinate system produced by the triogonal actuator impedances is given by

$$\begin{pmatrix} \mathbf{\dot{x}}_{1p} \\ \mathbf{\ddot{x}}_{2p} \end{pmatrix} = \mathbf{\ddot{z}}_{p} \begin{pmatrix} \mathbf{f} \\ -\mathbf{m} \end{pmatrix}_{p}$$
(45)

The impedance matrix describing the actuators is

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$$\dot{\ell} = Z_{\ell} \cdot f_{\ell}$$
 (46)

where i and f are the scalar lengths and forces in the actuators. If the impedance is to appear as a spring system

$$\mathbf{z}_{\mathbf{y}} = \mathbf{S} \begin{bmatrix} 1/k_{|1} & 0 & \cdot & \cdot & 0 \\ 0 & 1/k_{2} & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ 0 & 0 & \cdot & \cdot & 1/k_{6} \end{bmatrix} = \mathbf{S} \mathbf{L}_{\mathbf{y}}$$
(47)

then this diagonal matrix uses the diagonal elements as the reciprocals of the spring constants of each actuator. It is also convenient to define a column matrix as

$$\begin{pmatrix} 1 \\ k \end{pmatrix}_{\ell} = \begin{bmatrix} 1/k_1 \\ 1/k_2 \\ \vdots \\ 1/k_6 \end{bmatrix}$$
(48)

Since

$$\begin{pmatrix} f \\ -m \end{pmatrix}_{p} = F_{t} f_{\ell}$$
(49)

$$\vec{F} \left( -\frac{\vec{x}_1}{\vec{x}_2} \right)_p = \vec{k}$$
(50)

the platform impedance is given by

$$Z_{p} = FZ_{\ell}F_{t}$$
(51)

Similarly the impedance of the aircraft system is

$$Z_{a} = H(x_{3a}, r_{a}) Z_{p} H_{t}(x_{3a}, r_{a})$$
 (52)

Actuator Spring Constants

Since the actuator spring constant matrix is diagonal, it is completely determined by specifying six spring constants on the weapons system. These can be the principal (diagonal) constants, or a combination of diagonal and mutual constants. The unspecified elements in the impedance matrix will also be completely determined by the choice of the first six. The only exception to these restrictions is when the diagonal elements are specified, the system in which the specified constants and platform system form a symmetrical geometry, and the triogonal system is in its neutral position. In this case, some of the matrices in the solution become singular, and the solution can only be obtained by specifying a fewer number of spring constants and by imposing arbitrary symmetry conditions on the triogonal system.

The impedance description of the system is preferable to an admittance description for the following reasons: (1) The system disturbance is a force. The response of the system to this force is described by the impedance rather than the admittance, and (2) Since only six of the 36 total elements of the impedance (or admittance) matrix at the weapon system can be specified, it is necessary to accept whatever mutual coupling results from this choice. Under these conditions, the diagonal elements of the impedance matrix cannot be made equal to the reciprocals of the diagonal elements of the admittance matrix, and the motion resulting from a specified input force will not be equal to the desired response, if admittance elements are specified. Instead, this will determine what forces and moments must be applied about all three axes to produce this response along a single axis.

To develop a general solution which can be applied to either the aircraft or combat vehicle configuration, it is assumed that in addition to the gimbal and platform systems described earlier, pitch and vehicle systems will be defined by

$$x_{1H} = E(x_{3H}) x_{1D} - r_{H}$$
(53)

$$x_{1V} = E(x_{3V}) x_{1H} - r_V$$
 (54)

Since the pitch system is restricted to motion about only the pitch axis, it is convenient to orient this system parallel to the platform system in its neutral position. Then

$$E(x_{3H}) = \begin{bmatrix} \cos \theta_{H} & 0 & -\sin \theta_{H} \\ 0 & 1 & 0 \\ \sin \theta_{H} & 0 & \cos \theta_{H} \end{bmatrix}$$
(55)

For the aircraft, the pitch angle,  $\theta_H$ , is fixed, and the displacement,  $r_H$ , is zero. For the combat vehicle,  $\theta_H$ , varies with time, and the displacement,  $r_H$ , as measured in the platform system is constant and contains only a z component.

$$\mathbf{E}'(\mathbf{x}_{3H}) \mathbf{r}_{H} = \begin{pmatrix} \mathbf{0} \\ \mathbf{0} \\ \mathbf{z}_{H} \end{pmatrix}$$
(56)

The vehicle Euler angles,  $x_{3v}$ , will normally be zero; that is, the vehicle axes will be parallel to the pitch system axes.

The impedance at the platform,

$$Z_{p} = F Z_{\ell} F_{t}$$
(57)

can be transformed to the pitch system coordinates by

$$Z_{\rm H} = H(x_{\rm 3H}, r_{\rm H}) F Z_{\rm l} F_{\rm t} H_{\rm t} (x_{\rm 3H}, r_{\rm H})$$
(58)

For the aircraft, the impedance will be defined along the platform axes; for the combat vehicle, it will be defined along the pitch system axes. In either case, it is assumed that only principal elements of the impedance matrix will be specified. If we define

A = F for the aircraft, or

 $A = H(x_{3H}, r_H) F$ 

for the combat vehicle, then we can write

$$Z_{p} = A Z_{l} A_{t}$$
(59)

for either configuration. Now, since Z must be diagonal, it follows that the principal elements of  $\rm Z_p$  are given by

$$\left(\frac{1}{k}\right)_{p} = \begin{bmatrix} a_{11}^{2} & a_{12}^{2} & \cdots & a_{16}^{2} \\ a_{21}^{2} & a_{22}^{2} & \cdots & \vdots \\ \vdots & & & \ddots & \vdots \\ \vdots & & & & \vdots \\ a_{61}^{2} & \cdots & a_{66}^{2} \end{bmatrix} \quad \left(\frac{1}{k}\right)_{g}$$

where

$$\left(\frac{1}{k}\right)_{p} = \begin{bmatrix} 1/k_{x} \\ 1/k_{y} \\ 1/k_{z} \\ 1/k_{\theta} \\ 1/k_{\theta} \\ 1/k_{\psi} \end{bmatrix}$$
 (61)

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(60)

and

$$\begin{pmatrix} \frac{1}{k} \\ \frac{1}{k} \\ \frac{1}{k} \\ \frac{1}{k_{2}} \\ \frac{1}{k_{3}} \\ \frac{1}{k_{4}} \\ \frac{1}{k_{5}} \\ \frac{1}{k_{6}} \end{bmatrix}$$
 (62)

If we define

$$K = \begin{bmatrix} a_{11}^{2} & \cdots & a_{16}^{2} \\ \vdots & & \vdots \\ \vdots & & \vdots \\ a_{61}^{2} & \cdots & a_{66}^{2} \end{bmatrix}$$
(63)

in which the elements are equal to the square of the corresponding elements of the A matrix

$$k_{mn} = a_{mn}^2$$
(64)

then

$$\left(\frac{1}{k}\right)_{p} = K \left(\frac{1}{k}\right)_{k}$$
(65)

The actuator spring constants cannot be found simply by inverting the K matrix due to the symmetry of the triogonal system. As a result, the F matrix has a rank of only three, thereby limiting the number of specified spring constants to three. It is necessary to choose arbitrary relationships among the actuator spring constants to reduce the set of six equations to three, before the resulting matrix can be inverted.

In the neutral position, the triogonal system is symmetrical about three vertical planes, spaced 120° apart in yaw. The definition of the actuator numbering system is shown in figure 1. The platform attachment points are defined for actuator 1, while the gimbal attachment points are defined for actuator 3. If we define the 120° yaw transformation by

$$\mathbf{E} = \begin{bmatrix} \cos \psi & \sin \psi & 0 \\ -\sin \psi & \cos \psi & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{pmatrix} -\frac{1}{2} & \frac{1}{2} & \sqrt{3} & 0 \\ -\frac{1}{2} & \sqrt{3} & -\frac{1}{2} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{pmatrix} -\frac{1}{2} & \sqrt{3} & -\frac{1}{2} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$
(66)

and the x-z plane image transformation by

$$R = \begin{bmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$
(67)

then, because of the symmetry, the following relations are obtained:

$$\begin{array}{c} a_{4} = Ra_{1} \\ a_{2} = E'a_{4} \\ a_{5} = Ra_{2} = Ea_{1} \\ a_{3} = E'a_{1} \\ a_{6} = Ra_{3} = Ea_{4} \end{array}$$

$$(68)$$

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The moment arms appearing in the triogonal transformation are given by

$$\begin{array}{c} W(a_{3}) \&_{3} = W(E^{a}_{1}) \&_{3} = E^{W}(a_{1}) \&_{1} \\ W(a_{5}) \&_{5} = W(Ea_{1}) \&_{5} = E W(a_{1}) \&_{1} \\ W(a_{2}) \&_{2} = W(E^{a}_{4}) \&_{2} = E^{W}(a_{4}) \&_{4} \\ W(a_{6}) \&_{6} = W(Ea_{4}) \&_{6} = E W(a_{4}) \&_{4} \\ W(a_{4}) \&_{4} = W(Ra_{1}) R\&_{1} = -RW(a_{1}) \&_{1} \end{array}$$

$$(70)$$

Thus

$$\ell_{1} = \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}_{1}$$
(71)

$$\lambda_{2} = \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}_{2} = E^{\prime}R \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}_{1} = \begin{bmatrix} -\frac{1}{2}\alpha + \frac{1}{2}\sqrt{3}\beta \\ \frac{1}{2}\sqrt{3}\alpha + \frac{1}{2}\beta \\ \gamma \end{bmatrix}$$
(72)

$$\mathfrak{A}_{3} = \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}_{3}^{\alpha} = \mathbf{E}^{\prime} \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}_{1}^{\alpha} = \begin{bmatrix} -\frac{1}{2} \alpha - \frac{1}{2} \sqrt{3} \beta \\ \frac{1}{2} \sqrt{3} \alpha - \frac{1}{2} \beta \\ \gamma \end{bmatrix}$$
(73)

$$\ell_{4} = \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}_{4} = \mathbb{R} \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}_{1} = \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}$$
(74)

$$k_{5} = \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}_{5} = \mathbf{E} \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}_{1} = \begin{bmatrix} -\frac{1}{2} \alpha + \frac{1}{2} \sqrt{3} \beta \\ -\frac{1}{2} \sqrt{3} \alpha - \frac{1}{2} \beta \\ \gamma \end{bmatrix}$$
(75)  
$$k_{6} = \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}_{6} = \mathbf{ER} \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}_{1} = \begin{bmatrix} -\frac{1}{2} \alpha - \frac{1}{2} \sqrt{3} \beta \\ -\frac{1}{2} \sqrt{3} \alpha + \frac{1}{2} \beta \\ \gamma \end{bmatrix}$$
(76)

and

$$\begin{pmatrix} \lambda \\ \mu \\ \nu \end{pmatrix}_{2} = - E^{*}R \begin{pmatrix} \lambda \\ \mu \\ \nu \end{pmatrix}_{1} = \begin{bmatrix} \frac{1}{2} \lambda - \frac{1}{2} \sqrt{3} \mu \\ -\frac{1}{2} \sqrt{3} \lambda - \frac{1}{2} \mu \\ -\nu \end{bmatrix}$$
(77)
$$\begin{pmatrix} \lambda \\ \mu \\ \nu \end{pmatrix}_{3} = E^{*} \begin{pmatrix} \lambda \\ \mu \\ \nu \end{pmatrix}_{1} = \begin{bmatrix} -\frac{1}{2} \lambda - \frac{1}{2} \sqrt{3} \mu \\ \frac{1}{2} \sqrt{3} \lambda - \frac{1}{2} \mu \\ \nu \end{bmatrix}$$
(78)

$$\begin{pmatrix} \lambda \\ \mu \\ \nu \end{pmatrix}_{4}^{\lambda} = -R \begin{pmatrix} \lambda \\ \mu \\ \nu \end{pmatrix}_{1}^{\lambda} = \begin{pmatrix} -\lambda \\ \mu \\ -\nu \end{pmatrix}$$
(78) (78) (78)

$$\begin{pmatrix} \lambda \\ \mu \\ \nu \end{pmatrix}_{5} = E \begin{pmatrix} \lambda \\ \mu \\ \nu \end{pmatrix}_{1} = \begin{bmatrix} -\frac{1}{2} \lambda + \frac{1}{2} \sqrt{3} \mu \\ -\frac{1}{2} \sqrt{3} \lambda - \frac{1}{2} \mu \\ \nu \end{bmatrix}$$
(80)

$$\begin{pmatrix} \lambda \\ \mu \\ \nu \end{pmatrix}_{6}^{2} = -ER \begin{pmatrix} \lambda \\ \mu \\ \nu \end{pmatrix}_{1}^{2} = \begin{bmatrix} \frac{1}{2} \lambda + \frac{1}{2} \sqrt{3} \mu \\ \frac{1}{2} \sqrt{3} \lambda - \frac{1}{2} \mu \\ -\nu \end{bmatrix}$$
(81)

Then, the triogonal transformation and its inverse are given by

$$\mathbf{F}^{\prime} = \begin{bmatrix} \alpha & | \beta & | \gamma & | \lambda & | \mu & | \nu \\ -\frac{1}{2} (\alpha - \sqrt{3}\beta) & | \frac{1}{2} (\sqrt{3}\alpha + \beta) & | \gamma & | \frac{1}{2} (\lambda - \sqrt{3}\mu) & | -\frac{1}{2} (\sqrt{3}\lambda + \mu) & | -\nu \\ | & | & | & | & | & | \\ -\frac{1}{2} (\alpha + \sqrt{3}\beta) & | \frac{1}{2} (\sqrt{3}\alpha - \beta) & | \gamma & | -\frac{1}{2} (\lambda + \sqrt{3}\mu) & | \frac{1}{2} (\sqrt{3}\lambda - \mu) & | \nu \\ -\frac{1}{2} (\alpha - \sqrt{3}\beta) & | -\frac{1}{2} (\sqrt{3}\alpha + \beta) & | \gamma & | -\frac{1}{2} (\lambda - \sqrt{3}\mu) & | -\frac{1}{2} (\sqrt{3}\lambda + \mu) & | \nu \\ -\frac{1}{2} (\alpha - \sqrt{3}\beta) & | -\frac{1}{2} (\sqrt{3}\alpha + \beta) & | \gamma & | -\frac{1}{2} (\lambda - \sqrt{3}\mu) & | -\frac{1}{2} (\sqrt{3}\lambda + \mu) & | \nu \\ -\frac{1}{2} (\alpha + \sqrt{3}\beta) & | -\frac{1}{2} (\sqrt{3}\alpha - \beta) & | \gamma & | -\frac{1}{2} (\lambda - \sqrt{3}\mu) & | -\frac{1}{2} (\sqrt{3}\lambda - \mu) & | -\nu \\ -\frac{1}{2} (\alpha + \sqrt{3}\beta) & | -\frac{1}{2} (\sqrt{3}\alpha - \beta) & | 2\lambda & | -(\lambda - \sqrt{3}\mu) & | -(\lambda + \sqrt{3}\mu) \\ -\frac{1}{2} (\alpha + \sqrt{3}\beta) & | -\frac{1}{2} (\sqrt{3}\alpha - \beta) & | 2\lambda & | -(\lambda - \sqrt{3}\mu) & | -(\lambda + \sqrt{3}\mu) \\ 2\mu & | (\sqrt{3}\lambda + \mu) & | (\sqrt{3}\lambda - \mu) & | -2\mu & | -(\sqrt{3}\lambda + \mu) & | -\nu \\ 2\mu & | (\sqrt{3}\lambda + \mu) & | (\sqrt{3}\lambda - \mu) & | -2\mu & | -(\sqrt{3}\lambda + \mu) & | -(\sqrt{3}\lambda - \mu) \\ -\nu & | & -\nu & | & -\nu & | -\nu & | -\nu \\ 2\alpha & | (\alpha - \sqrt{3}\beta) & | -(\alpha + \sqrt{3}\beta) & | -2\alpha & | -(\alpha - \sqrt{3}\beta) & | (\alpha + \sqrt{3}\beta) \\ 2\beta & | -(\sqrt{3}\alpha + \beta) & | (\sqrt{3}\alpha - \beta) & | 2\beta & | -(\sqrt{3}\alpha + \beta) & | (\sqrt{3}\alpha - \beta) \\ -\gamma & | & -\gamma & | & \gamma & | -\gamma & | & \gamma \\ | & | & -\gamma & | & \gamma & | & -\gamma & | & \gamma \\ \end{bmatrix}$$
(83)

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If we let

$$F = \begin{bmatrix} F_{11} & F_{12} \\ F_{21} & F_{22} \end{bmatrix}$$
(84)

it is seen that

$$F_{12} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{bmatrix} F_{11} = RF_{11}$$
(85)  
$$F_{22} = -\begin{bmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{bmatrix} F_{21} = -RF_{21}$$
(86)

Since, when specifying the principal elements of the impedance matrix, the spring constant matrix, K, is obtained by squaring the elements of the F matrix, it follows that

$$K = \begin{bmatrix} K_{11} & K_{11} \\ - & - & - \\ K_{21} & K_{21} \end{bmatrix}$$
(87)

Since the last three columns of K are equal to the first three, its rank is three, and only three of the desired spring constants can be specified.

$$\begin{pmatrix} \frac{1}{k} \\ p \end{pmatrix}_{p} = \kappa \begin{pmatrix} \frac{1}{k} \\ \end{pmatrix}_{g}$$

$$\begin{bmatrix} 1/k_{x} \\ 1/k_{y} \\ 1/k_{z} \\ 1/k_{\phi} \\ 1/k_{\phi} \\ 1/k_{\phi} \\ 1/k_{\psi} \end{bmatrix} = \begin{bmatrix} \kappa_{11} \\ -- \\ \kappa_{21} \\$$

Thus, the sum of the reciprocal spring constants for symmetrical actuators can be found from the three specified spring constants at the platform axes. It would be logical to retain the symmetry about the x-z plane by making  $k_1 = k_4$ ,  $k_2 = k_5$ , and  $k_3 = k_6$ , but this is not necessary. By doing this, several of the cross coupling terms can be made zero.

Examination of the six rows of the 6 x 3 matrix shows that the 3 x 3 matrices,  $K_{11}$  and  $K_{21}$ , are both singular. Thus, the three specified spring constants must be a combination of linear and angular constants. Any three of the six rows can be chosen, which do not result in a singular matrix. The only pairs that cannot be chosen are the z and  $\psi$  constants, the x and y constants when combined with either the z or  $\psi$  constant. The possible combinations are listed below.

x, θ, z
φ, y, ψ
x, θ, ψ
φ, y, z
x, φ, z
x, φ, ζ
y, θ, z
y, θ, ζ
y, θ, ψ
x, y, φ
x, y, θ
x, φ, θ
y, φ, θ

Of these, it is presumed that one of the desired constants will be  ${\bf k}_{{\bf x}}.$  This reduces the list to

x, θ, z
x, θ, ψ
x, φ, z
x, φ, ψ
x, y, φ
x, y, θ
x, φ, θ

The first two of these are orthogonal, the others lie in either the x-z or x-y plane. The first two have been evaluated. They are as follows. If we let

$$\begin{bmatrix} 1/k_{x} \\ 1/k_{\theta} \\ 1/k_{z} \end{bmatrix} = K_{1} \begin{bmatrix} 1/k_{1} + 1/k_{4} \\ 1/k_{2} + 1/k_{5} \\ 1/k_{3} + 1/k_{6} \end{bmatrix}$$
(90)

and

$$\begin{bmatrix} 1/k_{x} \\ 1/k_{\theta} \\ 1/k_{\psi} \end{bmatrix} = K_{2} \begin{bmatrix} 1/k_{1} + 1/k_{4} \\ 1/k_{2} + 1/k_{5} \\ 1/k_{3} + 1/k_{6} \end{bmatrix}$$
(91)

then

$$K_{1} = \frac{1}{36(\gamma\nu)^{2}} \begin{bmatrix} 4\lambda^{2} & (\lambda - \sqrt{3}\mu)^{2} & (\lambda + \sqrt{3}\mu)^{2} \\ 4\beta^{2} & (\sqrt{3}\alpha + \beta)^{2} & (\sqrt{3}\alpha - \beta)^{2} \\ \nu^{2} & \nu^{2} & \nu^{2} \end{bmatrix}$$
(92)

and

$$K_{2} = \frac{1}{36(\gamma\nu)^{2}} \begin{bmatrix} 4\lambda^{2} & (\lambda - \sqrt{3}\mu)^{2} & (\lambda + (\sqrt{3}\mu)^{2} \\ 4\beta^{2} & (\sqrt{3}\alpha + \beta)^{2} & (\sqrt{3}\alpha - \beta)^{2} \\ \gamma^{2} & \gamma^{2} & \gamma^{2} \end{bmatrix}$$
(93)

The inverse of  $K_1$  is

$$K_{1} = \frac{3\gamma\nu}{(\alpha\mu-\beta\lambda)} \begin{bmatrix} 4\alpha\beta & 4\lambda\mu & \frac{4\gamma(3\alpha\mu+\beta\lambda)}{\nu} \\ (\sqrt{3}\alpha+\beta)(\alpha-\sqrt{3}\beta) & (\sqrt{3}\lambda+\mu)(\lambda-\sqrt{3}\mu) & \frac{4\gamma[\sqrt{3}(\alpha\lambda-\beta\mu) - 2\beta\lambda]}{\nu} \\ -(\sqrt{3}\alpha-\beta)(\alpha+\sqrt{3}\beta) & -(\sqrt{3}\lambda-\mu)(\lambda+\sqrt{3}\mu) & -\frac{4\gamma[\sqrt{3}(\alpha\lambda-\beta\mu) + \beta\lambda]}{\nu} \end{bmatrix}$$
(94)  

$$K_{2} \text{ is identical, except that } \gamma \text{ is replaced by } \nu \text{ and } \nu \text{ by } \gamma.$$

The above relations provide the necessary equations to determine the neutral spring constants when employing the aircraft configuration. For the combat vehicle, the attachment point is further extended along the platform z-axis, and the attachment coordinate system is rotated through a pitch angle,  $\theta_{\rm H}$ . The extension along the z-axis does not alter any of the general conclusions that have been made; there is already an extension of 10 inches below the pivot point

plane for the aircraft attachment platform. Thus, neglecting the pitch angle, the rank of the K matrix is still three. Of course, the numerical values are affected by the extension. These can be corrected by assuming a new value of a, the platform pivot location, which will affect the values of  $\lambda$ ,  $\mu$ , and  $\nu$ , or the F matrix can be premultiplied by the quantity

$$\begin{bmatrix} 1 & -W(E'_{H}r_{H}) \\ 0 & 1 \\ 0 & 1 \end{bmatrix}$$
(95)

 ${\tt E'r}$  is the displacement of the pitch system origin from the platform system origin measured in platform coordinates, and is given by

$$\mathbf{E}_{\mathbf{H}} \cdot \mathbf{r}_{\mathbf{H}} = \begin{bmatrix} \mathbf{0} \\ \mathbf{0} \\ \mathbf{z}_{\mathbf{H}} \end{bmatrix}$$
(96)

Thus

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$$-W (E_{\rm H}' r_{\rm H}) = z_{\rm H} \begin{bmatrix} 0 & 1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$
(97)

Premultiplying the F matrix by this quantity is equivalent to modifying the pivot location point.

To include the pitch angle, the A matrix is formed by multiplying by the angular conversion matrix.

$$A = \begin{bmatrix} E_{H} & | & 0 \\ 0 & | & E_{H} \\ | & | & \end{bmatrix} \begin{bmatrix} 1 & | & -W(E_{H} \cdot r_{H}) \\ 0 & | & 1 \\ 0 & | & 1 \end{bmatrix} F$$
(98)

If we assume that the z extension to the pitch system origin is included in the definition of F, then

$$A = \begin{bmatrix} E_{H} & F_{11} & | & E_{H} & F_{12} \\ \hline E_{H} & F_{21} & | & E_{H} & F_{22} \end{bmatrix}$$
(99)

Since the relations between  ${\rm F}_{11}$  and  ${\rm F}_{12},$  and between  ${\rm F}_{21}$  and  ${\rm F}_{22}$  still hold

$$F_{12} = RF_{11}$$
 (100)

$$F_{22} = -RF_{21}$$
(101)

and, since

$$E_{\rm H}R = RE_{\rm H} \tag{102}$$

for pitch motion, it follows that

$$A = \begin{bmatrix} A_{11} & | & RA_{11} \\ \hline A_{21} & | & -RA_{21} \end{bmatrix}$$
(103)

The K matrix is again formed by squaring the elements of the A matrix, so that its rank is still three. The last three columns of the A matrix are the same as the first three, except for sign, which disappears when the elements are squared. Thus, as long as the origin of the attachment system to the vehicle lies on the z-axis of the platform system, and the roll and yaw angles of the attachment system relative to the triogonal system are zero, only three principal elements can be specified.

If we assume that

$$\mathbf{k}_1 = \mathbf{k}_4 \tag{104}$$

$$k_2 = k_5 \tag{105}$$

and

$$k_3 = k_6$$
 (106)

then

$$\begin{bmatrix} 1/k_{x} \\ 1/k_{\theta} \\ 1/k_{z} \end{bmatrix} = 2K_{1} \begin{bmatrix} 1/k_{1} \\ 1/k_{2} \\ 1/k_{3} \end{bmatrix}$$
(107)
Similar expressions hold for other choices of specified constants. Then

 $\begin{bmatrix} \frac{1}{k_1} \\ \frac{1}{k_2} \\ \frac{1}{k_3} \end{bmatrix} = \begin{bmatrix} \frac{1}{k_4} \\ \frac{1}{k_5} \\ \frac{1}{k_6} \end{bmatrix} = \frac{1}{2} K_1 \begin{bmatrix} 1/k_x \\ 1/k_\theta \\ 1/k_z \end{bmatrix}$ 

(108)

These equations can now be used to determine the actuator spring constants. It may still be necessary to restrict the choice of specified constants to obtain physically realizable results.

Actuator Gravitational Forces

To find the actuator unextended lengths, it is necessary to subtract from the values found in equations 1-16, the deflection due to supporting the weight of the aircraft The gravitational force is exerted in the earth axes zdirection at the origin of the aircraft coordinates. This must be resolved into the platform system to find the actuator forces.

The vehicle axes are tied to the earth axes through the gimbal coordinate system. The relationship between the earth and the gimbal systems will be defined as

$$x_{1G} = E(x_{3G}) x_{1E} - r_G$$
 (109)

Because of the physical construction of the gimbal system, it is appropriate to define the gimbal Euler angles in the reverse order as

$$E(x_{3G}) = E_1(\psi_G) \cdot E_2(\theta_G)$$
(110)

 $x_{3C}$  then defines the gimbal angles directly and

$$E(x_{3G}) = \begin{bmatrix} (\cos\psi_{G} \cdot \cos\theta_{G}) & \sin\psi_{G} & (-\cos\psi_{G} \cdot \sin\theta_{G}) \\ (-\sin\psi_{G} \cdot \cos\theta_{G}) & \cos\theta_{G} & (\sin\psi_{G} \cdot \sin\theta_{G}) \\ \sin\theta_{G} & 0 & \cos\theta_{G} \end{bmatrix}$$
(111)

The gravitational force in the vehicle system is then equal to

$$g_v = E(x_{3v}) E(x_{3H}) E(x_{3p}) E(x_{3G}) g_e$$
 (112)

where

$$g_{e} = g \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$$
(113)

This is transformed into forces and moments about the platform axes equal to

$$\mathbf{g}_{\mathbf{p}} = \mathbf{H}_{\mathbf{t}} \left( \mathbf{x}_{3\mathrm{H}}, \mathbf{r}_{\mathrm{H}} \right) \mathbf{H}_{\mathbf{t}} \left( \mathbf{x}_{3\mathrm{v}}, \mathbf{r}_{\mathrm{v}} \right) \begin{pmatrix} \mathbf{g}_{\mathrm{v}} \\ --\\ \mathbf{0} \end{pmatrix}$$
(114)

Finally, resolved along the actuators, the forces in the actuators are

$$f_{\ell} = mF_{t}H_{t} (x_{3H}, r_{H}) H_{t} (x_{3v}, r_{v}) \begin{pmatrix} g_{v} \\ - \\ 0 \end{pmatrix}$$
(115)

The actuator extensions are then

$$\Delta \ell = L_{\ell} f_{\ell}$$
(116)

The actuator extensions can also be expressed as

$$\Delta \ell = \left[f_{\ell}\right] \left(\frac{1}{k}\right)_{\ell} \tag{117}$$

where  $[f_{\ell}]$  is the diagonal matrix formed from the column matrix,  $f_{\ell}$ . If we assume

 $E(x_{3v}) = 1$  (118)

$$E(x_{3p}) = 1$$
 (119)

$$\mathbf{E}^{\prime} (\mathbf{x}_{3H}) \mathbf{r}_{H} = \begin{bmatrix} \mathbf{0} \\ \mathbf{0} \\ \mathbf{z}_{H} \end{bmatrix}$$
(120)

$$\mathbf{r}_{\mathbf{v}} = \begin{bmatrix} \mathbf{x}_{\mathbf{v}} \\ \mathbf{y}_{\mathbf{v}} \\ \mathbf{z}_{\mathbf{v}} \end{bmatrix}$$
(121)

and making use of the relation

 $E^{W}(\mathbf{r}) = W(E^{r})$ (122)

the above equations reduce to

$$g_{p} = \left[ \frac{1}{W \left\{ E_{H} - (r_{H} + r_{V}) \right\}} \right] g_{G}$$
(123)

where

$$g_{G} = g \begin{bmatrix} -\cos\psi_{G} & \sin\theta_{G} \\ \sin\psi_{G} & \sin\theta_{G} \\ \cos\theta_{G} \end{bmatrix}$$
(124)

If we let

$$\mathbf{r} = \mathbf{E}_{\mathbf{H}} \left( \mathbf{r}_{\mathbf{H}} + \mathbf{r}_{\mathbf{v}} \right) \tag{125}$$

then

$$\mathbf{r} = \begin{bmatrix} \mathbf{x}_{\mathbf{v}} \cos \theta_{\mathbf{H}} + \mathbf{z}_{\mathbf{v}} \sin \theta_{\mathbf{H}} \\ \mathbf{y}_{\mathbf{v}} \\ \mathbf{z}_{\mathbf{H}} - \mathbf{x}_{\mathbf{v}} \sin \theta_{\mathbf{H}} + \mathbf{z}_{\mathbf{v}} \cos^{\prime} \theta_{\mathbf{H}} \end{bmatrix}$$
(126)

Thus, it is necessary to resolve the gimbal and pitch angles into sine and cosine components and to perform the indicated multiplications to find the gravitational forces and moments about the platform axes. These can then be summed, using the coefficients given by the elements of the F matrix to find the actuator forces, and then divided by the spring constants to find the actuator extensions.

In the calculation of the displacement, r, an arbitrary value of the pitch angle,  $\theta_{\rm H}$ , has been assumed. This calculation can be made in real time to account for the instantaneous pitch angle of the combat vehicle. It still remains to be determined if the instantaneous pitch angle can be used for the calculation of spring constants, since real time matrix inversion may be required. Possibly, for the combat vehicle, spring constants will be calculated for zero pitch angle and variations from these values will be calculated in real time on a linearized basis. To be consistent, the gravitational forces will also be calculated for zero pitch angle, and the variations again calculated on a linearized basis about this point. The displacement then becomes simply

$$\mathbf{r} = \begin{bmatrix} \mathbf{x}_{\mathbf{v}} \\ \mathbf{y}_{\mathbf{v}} \\ \mathbf{z}_{\mathbf{v}} + \mathbf{z}_{\mathrm{H}} \end{bmatrix}$$
(127)

For the aircraft, spring constants are to be specified at the platform system, which does not contain the fixed pitch angle built into the aircraft. In this case, the pitch angle will be included in the calculation of gravitational forces, since it does not vary with time.

Actuator Mass Loads

To improve the performance of the adaptive loops used to program the actuator spring constants, it is desirable to input the effective mass loads on each of the actuators. These loads are found from the linearized equations of the aircraft motion.

Since the x-z plane in the aircraft system will normally be a plane of symmetry, the cross moments of inertia to the y-axis will be zero. The inertia matrix, under these conditions, simplifies to

$$\mathbf{J} = \begin{bmatrix} \mathbf{J}_{\mathbf{x}\mathbf{x}} & \mathbf{0} & \mathbf{J}_{\mathbf{x}\mathbf{z}} \\ \mathbf{0} & \mathbf{J}_{\mathbf{y}\mathbf{y}} & \mathbf{0} \\ \mathbf{J}_{\mathbf{x}\mathbf{z}} & \mathbf{0} & \mathbf{J}_{\mathbf{z}\mathbf{z}} \end{bmatrix}$$
(128)

The mass matrix is defined as

$$\mathbf{m} = \begin{bmatrix} \mathbf{m} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{m} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \mathbf{m} \end{bmatrix}$$
(129)

The moments of inertia should be the effective moments, including the effects of the tail boom simulator and the stability augmentation system if used for the aircraft.

The vehicle motion is defined by summing external forces and moments and equating these to the rates of momentum change by

$$f_{v} = m \left\{ \ddot{x}_{1} + W (\dot{x}_{2}) \dot{x}_{1} - E (x_{3}) g_{e} \right\}$$
(130)

$$(m)_{v} = J x_{2} + W (x_{2}) J x_{2}$$
 (131)

$$\dot{x}_3 = G(x_3) \dot{x}_2$$
 (132)

where the Euler angles and velocities are referenced to the earth system.

By the use of the following transformations,

$$\begin{pmatrix} f \\ -- \\ m \end{pmatrix}_{v} = H_{t}'(x_{3v}, r_{v}) H_{t}'(x_{3H}, r_{H}) \begin{pmatrix} f \\ -- \\ m \end{pmatrix}_{p}$$
(133)

$$f_{l} = F_{t} \left(\frac{f}{m}\right)_{p}$$
(134)

$$\left(\frac{\dot{\mathbf{x}}_{1}}{\dot{\mathbf{x}}_{2}}\right)_{p} = H^{\prime}(\mathbf{x}_{3H}, \mathbf{r}_{H}) H^{\prime}(\mathbf{x}_{3v}, \mathbf{r}_{v}) \left(\frac{\dot{\mathbf{x}}_{1}}{\dot{\mathbf{x}}_{2}}\right)_{v}$$
(135)

and

$$\dot{i} = F\left(\frac{\dot{x}_1}{\dot{x}_2}\right)_p \tag{136}$$

the actuator forces are given by

$$f_{\ell} = \left\{ F_{t} H_{H_{t}} H_{v_{t}} m_{v} H_{v} H_{H} F \right\} \ddot{\iota} + F_{t} H_{H_{t}} H_{v_{t}} m_{v} \frac{\partial}{\partial t} \left\{ H_{v} H_{H} F \right\} \dot{\iota} + F_{t} H_{H_{t}} H_{v_{t}} m_{v} \frac{\partial}{\partial t} \left\{ H_{v} H_{H} F \right\} \dot{\iota} + F_{t} H_{H_{t}} H_{v_{t}} \left[ \frac{W(\dot{x}_{2}) | 0}{\cdot 0} + \frac{W(\dot{x}_{2})}{|W(\dot{x}_{2})} \right] m_{v} H_{v} H_{H} F \dot{\iota} \\ - F_{t} H_{H_{t}} H_{v_{t}} \left[ \frac{E(x_{3})g_{e}}{0} \right]$$
(137)

Thus, the effective mass loads, for small signals, are given by the diagonal elements of

$$m_{\ell} = F_{t} H_{H_{t}} V_{t} W_{t} H_{H} F$$
(138)

where

$$\mathbf{m}_{\mathbf{v}} = \begin{bmatrix} \mathbf{m} & | & \mathbf{0} \\ - & | - \\ \mathbf{0} & | & \mathbf{J} \end{bmatrix}$$
(139)

For

$$E(x_{3v}) = 1$$
 (140)

and

$$\mathbf{r} = \mathbf{E}_{\mathrm{H}}^{\prime} \left( \mathbf{r}_{\mathrm{H}}^{\prime} + \mathbf{r}_{\mathrm{v}}^{\prime} \right) = \begin{pmatrix} \mathbf{x} \\ \mathbf{0} \\ \mathbf{z} \end{pmatrix}$$
(141)

this reduces to

$$(m_{\ell})_{11} = \left\{ F_{11}_{t} + F_{21}_{t} W (r) \right\} m \left\{ F_{11} - W (r) F_{21} \right\} + F_{21}_{t} \left\{ E_{H} J E_{H} \right\} F_{21}$$
(142)

$$(m_{\ell})_{12} = \left\{ F_{11}_{t} + F_{21}_{t} W (r) \right\} \stackrel{\text{m}}{=} R \left\{ F_{11} - W (r) F_{21} \right\}$$
$$- F_{21}_{t} \left\{ E_{H}^{\prime} J E_{H} R \right\} F_{21}$$
(143)

$$(m_{\ell})_{22} = (m_{\ell})_{11}$$
 (144)

$$(m_{\ell})_{21} = (m_{\ell})_{12}$$
 (145)

These results are valid if the vehicle center of mass lies in the x-z plane of the triogonal system.

The mass load of the actuator system upon itself must then be added to the mass load of the vehicle. The effective mass of the actuators is derived in appendix B. These values are then used in the computer program to calculate the mass constants for each actuator setting of the simulator.

Tail Boom Actuator Force Command

The tail boom actuator must provide a moment about the aircraft CG equivalent to that normally present due to the tail boom inertia. If the inertia is to be increased by an amount,  $\Delta J_{\tau}$ , a moment equal to

 $m = \Delta J_{z} \psi$ (146)

must be applied. The force applied by the tail boom actuator is then

$$f_{TB} = \frac{\Delta J}{r_{TB}} \ddot{\psi}$$
(147)

where  $r_{TR}$  is the moment arm of the actuator.

Linear Coefficients

#### Linearization of Equations

For the combat vehicle, the relationship between the triogonal system and the vehicle center of mass varies with time due to the yaw angle input to the triogonal system and the pitch angle variations introduced between the platform and vehicle. For this reason, the adaptive servo inputs (spring constant, and unloaded extension) must be varied in real time. This is not necessary for the aircraft. Initially, variations will be investigated on a linearized basis, because of the relatively small angles involved.

#### Incremental Gravitational Loading

The gravitational vector, at the vehicle center of mass, in vehicle coordinates is

$$g_v = E(x_{3v}) E(x_{3H}) E(x_{3p}) E(x_{3G}) g_e$$
 (148)

where

$$g_{e} = g\begin{pmatrix} 0\\0\\1 \end{pmatrix}$$
(149)

The forces provided by the actuators to support the vehicle are then

$$f_{\ell} = mF_{t}H_{t}(x_{3H})H_{t}(x_{3v}) \left(-\frac{g_{v}}{0}\right)$$
(150)

Since the effects of gimbal angle variations are included in the calculation of  $g_v$ , linearization is only required for the triogonal yaw angle,  $\psi_p$ , and the pitch angle,  $\theta_{\rm H}$ . The time derivative of the actuator forces, neglecting gimbal angle effects, is then

$$\dot{f}_{\ell} = \dot{m}F_{t}H_{Ht}H_{Vt} \left(\frac{g_{v}}{-\frac{v}{0}}\right) + mF_{t}H_{Ht}H_{vt}\left(\frac{g_{v}}{-\frac{v}{0}}\right) + mF_{t}H_{t}H_{vt}H_{vt}\left(\frac{g_{v}}{-\frac{v}{0}}\right)$$

$$+ mF_{t}H_{Ht}H_{vt} \left(\frac{g_{v}}{-\frac{v}{0}}\right)$$
(151)

where

$$\dot{\mathbf{g}}_{\mathbf{v}} = \mathbf{E}_{\mathbf{v}} \dot{\mathbf{E}}_{\mathbf{H}} \mathbf{E}_{\mathbf{p}} \mathbf{E}_{\mathbf{G}} \mathbf{g}_{\mathbf{e}} + \mathbf{E}_{\mathbf{v}} \mathbf{E}_{\mathbf{H}} \dot{\mathbf{E}}_{\mathbf{p}} \mathbf{G}_{\mathbf{g}} \mathbf{g}_{\mathbf{e}}$$
(152)

$$\dot{\mathbf{F}}_{\mathbf{t}} = \left(\frac{\partial \mathbf{F}_{\mathbf{t}}}{\partial \psi_{\mathbf{p}}}\right) \dot{\psi}_{\mathbf{p}}$$
(153)

$$\dot{\mathbf{H}}_{\mathrm{Ht}} = \left(\frac{\partial \mathbf{H}_{\mathrm{Ht}}}{\partial_{\theta \mathrm{H}}}\right) \dot{\boldsymbol{\theta}}_{\mathrm{H}} = \mathbf{H}_{\mathrm{Ht}} \begin{bmatrix} \mathbf{w} \begin{pmatrix} \mathbf{0} \\ \mathbf{1} \\ \mathbf{0} \end{pmatrix} \Big|_{\mathrm{H}} & \mathbf{0} \\ - \frac{\mathbf{0}}{\mathbf{0}} \Big|_{\mathrm{H}} & \mathbf{w} \begin{pmatrix} \mathbf{0} \\ \mathbf{1} \\ \mathbf{0} \end{pmatrix} \end{bmatrix} \dot{\boldsymbol{\theta}}_{\mathrm{H}}$$

$$(154)$$

$$\dot{\mathbf{E}}_{\mathrm{H}} = -\mathbf{W}(\dot{\mathbf{x}}_{2\mathrm{H}})\mathbf{E}_{\mathrm{H}} = -\mathbf{W}\begin{pmatrix}\mathbf{0}\\\mathbf{1}\\\mathbf{0}\end{pmatrix}\mathbf{E}_{\mathrm{H}}\dot{\mathbf{\theta}}_{\mathrm{H}}$$
(155)

$$\dot{\mathbf{E}}_{\mathbf{p}} = -\mathbf{W}(\dot{\mathbf{x}}_{2\mathbf{p}})\mathbf{E}_{\mathbf{p}} = -\mathbf{W}\begin{pmatrix}\mathbf{0}\\\mathbf{1}\\\mathbf{0}\end{pmatrix}\mathbf{E}_{\mathbf{p}}\dot{\Psi}_{\mathbf{p}}$$
(156)

Since the linearization is performed about the neutral position, then

$$E_{\rm p} = E_{\rm H} = 1$$
 (157)

Also, for convenience, the neutral pitch angle will be chosen so that the pitch system axes are parallel to the vehicle axes. Then

$$E_v = 1$$
 (158)

and

$$\dot{\mathbf{g}}_{\mathbf{v}} = -\mathbf{W} \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} \mathbf{g}_{\mathbf{G}} \dot{\boldsymbol{\theta}}_{\mathbf{H}}^{-\mathbf{W}} \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \mathbf{g}_{\mathbf{G}} \dot{\boldsymbol{\psi}}_{\mathbf{P}}$$

$$\dot{\mathbf{H}}_{\mathbf{H}t} = \begin{bmatrix} -\frac{1}{\mathbf{u}} - \frac{1}{\mathbf{u}} - \frac{0}{\mathbf{u}} - 1 \end{bmatrix} \begin{bmatrix} \mathbf{w} \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} & \mathbf{0} \\ -\frac{1}{\mathbf{u}} \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} \end{bmatrix} \dot{\boldsymbol{\theta}}_{\mathbf{H}}$$

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The derivative of the forces is then

$$\dot{f}_{\mathcal{L}} = m \left( \frac{\partial F_{t}}{\partial \psi p} \right) \left[ \frac{-1}{W(r_{H} + r_{v})} \right] g_{G} \dot{\psi}_{p} + mF_{t} \left[ -\frac{0}{W(0)} \right] g_{G} \dot{\theta}_{H} + mF_{t} \left[ \frac{-1}{W(0)} \right]$$

The gravitational components in the gimbal system,  ${\rm g}_{\rm G},$  and the components referred to the platform

$$g_{p} = \begin{bmatrix} - & -1 & - \\ W(r_{H} + r_{v}) \end{bmatrix} g_{G}$$
(162)

have been calculated for the static forces, f. Thus, it is only necessary to sum these with the proper scale factors as determined by the elements of F and  $\frac{\partial F}{\partial \Psi_{\rm P}}$  to find the coefficients which, when multiplied by the yaw and pitch angle variations, will give the variations in actuator forces.

The derivative of the triogonal transformation is obtained from the derivative of its inverse

$$\frac{\partial \mathbf{F}}{\partial \psi_{\mathbf{p}}} = -\mathbf{F} \left( \begin{array}{c} \frac{\partial \mathbf{F'}}{\partial \psi_{\mathbf{p}}} \end{array} \right) \mathbf{F}$$
(163)

It cannot be obtained directly, since an explicit expression for F, except in the neutral position, is too cumbersome. Since the n-th column of  $F_t$ ' is equal to

$$(\mathbf{F}_{t}')_{n} = \begin{bmatrix} \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}_{n} \\ \hline W(a_{n}) & \begin{pmatrix} \alpha \\ \gamma \end{pmatrix}_{n} \end{bmatrix}$$
(164)

and the derivative of the direction cosines is

$$\begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}_{\mathbf{n}} = -W^2 \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}_{\mathbf{n}} \quad \frac{\dot{\ell}}{n} \\ \frac{n}{\ell} \\ (165)$$

the derivative of the n-th column of  ${\rm F_t}'$  is

$$(\dot{F}_{t}')_{n} = -\frac{1}{lo} \begin{bmatrix} w^{2} \begin{pmatrix} \alpha \\ \beta \end{pmatrix}_{n} \dot{l}_{n} \\ - - \gamma \end{pmatrix}_{n} \frac{\dot{l}_{n}}{2} \\ W(a_{n}) W^{2} \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}_{n} \dot{l}_{n} \end{bmatrix}$$
(166)

The velocity,  $\dot{l}_n$ , is the vector velocity of the n-th actuator, so

$$\dot{\boldsymbol{x}}_{n} = \dot{\boldsymbol{x}}_{1p} - W(\boldsymbol{a}_{n})\dot{\boldsymbol{x}}_{2p} = \begin{bmatrix} 1 & | & -W(\boldsymbol{a}_{n}) \\ | & | & -W(\boldsymbol{a}_{n}) \end{bmatrix} \begin{pmatrix} \dot{\boldsymbol{x}}_{1p} \\ - \dot{\boldsymbol{x}}_{2p} \end{pmatrix}$$
(167)

Thus

$$(\mathbf{F}_{t}')_{n} = -\frac{1}{\ell_{0}} \begin{bmatrix} \mathbf{w}^{2} \begin{pmatrix} \alpha \\ \beta \\ \mathbf{y} \end{pmatrix} & | -\mathbf{w}^{2} \begin{pmatrix} \alpha \\ \beta \\ \mathbf{y} \end{pmatrix} \\ \mathbf{w}(\mathbf{a}_{n}) \mathbf{w}^{2} \begin{pmatrix} \alpha \\ \beta \\ \mathbf{y} \end{pmatrix} \\ \mathbf{w}(\mathbf{a}_{n}) \mathbf{w}^{2} \begin{pmatrix} \alpha \\ \beta \\ \mathbf{y} \end{pmatrix} \\ \mathbf{w}(\mathbf{a}_{n}) \mathbf{w}^{2} \begin{pmatrix} \alpha \\ \beta \\ \mathbf{y} \end{pmatrix} \\ \mathbf{w}(\mathbf{a}_{n}) \mathbf{w}^{2} \begin{pmatrix} \alpha \\ \beta \\ \mathbf{y} \end{pmatrix} \\ \mathbf{w}(\mathbf{a}_{n}) \mathbf{w}^{2} \begin{pmatrix} \alpha \\ \beta \\ \mathbf{y} \end{pmatrix} \\ \mathbf{w}(\mathbf{a}_{n}) \mathbf{w}^{2} \begin{pmatrix} \alpha \\ \beta \\ \mathbf{y} \end{pmatrix} \\ \mathbf{w}(\mathbf{a}_{n}) \end{bmatrix} \begin{bmatrix} \cdot \\ \cdot \\ \cdot \\ \cdot \\ \cdot \\ 2 \end{bmatrix} \\ \mathbf{w}$$
(168)

The direction cosines of the six actuators, in the neutral position, are given in terms of those for actuator number one by equations 71 thru 76.

After evaluating the submatrices of  $(\mathbf{F}_{t})_{n}$  we find

$$\frac{\partial (\mathbf{F}_{t}')_{2}}{\partial \left(-\frac{\mathbf{x}_{1}}{\mathbf{x}_{2}}\right)_{p}} = \begin{bmatrix} \underline{\mathbf{E}' \mathbf{R}} \mid \underline{\mathbf{0}}_{\mathbf{-}\mathbf{E' R}} \end{bmatrix} \frac{\partial (\mathbf{F}_{t}')_{1}}{\partial \left(-\frac{\mathbf{x}_{1}}{\mathbf{x}_{2}}\right)_{p}} \begin{bmatrix} \underline{\mathbf{RE}}_{\mathbf{-}} \mid \underline{\mathbf{0}}_{\mathbf{-}\mathbf{RE}} \end{bmatrix}$$
(169)

$$\frac{\partial (\mathbf{F}_{t}')}{\partial \left(\frac{x_{1}}{x_{2}}\right)_{p}} = \begin{bmatrix} -\mathbf{E}_{t}' \mid \mathbf{0} \\ \mathbf{0} \mid \mathbf{E}' \end{bmatrix} \frac{\partial (\mathbf{F}_{t}')}{\partial \left(\frac{x_{1}}{x_{2}}\right)_{p}} \begin{bmatrix} -\mathbf{E}_{t} \mid \mathbf{0} \\ \mathbf{0} \mid \mathbf{E} \end{bmatrix}$$
(170)

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$$\frac{\partial (\mathbf{F}_{t}')_{4}}{\left(\frac{\mathbf{x}_{1}}{\mathbf{x}_{2}}\right)_{p}} = \begin{bmatrix} \mathbf{R} & | & \mathbf{0} \\ \mathbf{0} & | & -\mathbf{R} \end{bmatrix} \frac{\partial (\mathbf{F}_{t}')_{1}}{\partial \left(\frac{\mathbf{x}_{1}}{\mathbf{x}_{2}}\right)_{p}} \begin{bmatrix} \mathbf{R} & | & \mathbf{0} \\ \mathbf{0} & | & -\mathbf{R} \end{bmatrix}$$
(171)

$$\frac{\partial (\mathbf{F}_{t}')_{5}}{\left(-\frac{\mathbf{x}_{1}}{2}\right)_{p}} = \begin{bmatrix} \mathbf{E}_{t} & \mathbf{0}_{t} \\ \mathbf{0}_{t} & \mathbf{E}_{t} \end{bmatrix} \cdot \frac{\partial (\mathbf{F}_{t}')_{1}}{\partial \left(-\frac{\mathbf{x}_{1}}{\mathbf{x}_{2}}\right)_{p}} \begin{bmatrix} \mathbf{E}_{t}' & \mathbf{0}_{t} \\ \mathbf{0}_{t} & \mathbf{E}_{t}' \end{bmatrix}$$
(172)

$$\frac{\partial (\mathbf{F}_{t}')_{6}}{\partial \left(-\frac{\mathbf{x}_{1}}{\mathbf{x}_{2}}\right)_{p}} = \begin{bmatrix} \mathbf{E}\mathbf{R} \mid \mathbf{0} \\ \mathbf{0} \mid -\mathbf{E}\mathbf{R} \end{bmatrix} \frac{\partial (\mathbf{F}_{t}')_{1}}{\partial \left(-\frac{\mathbf{x}_{1}}{\mathbf{x}_{2}}\right)_{p}} \begin{bmatrix} \mathbf{E}\mathbf{E}' \mid \mathbf{0} \\ \mathbf{0} \mid -\mathbf{R}\mathbf{E}' \end{bmatrix}$$
(173)

For pure yaw motion

$$\mathbf{x}_{lp} = 0 \tag{174}$$

and

$$\dot{\mathbf{x}}_{2\mathbf{p}} = \dot{\psi}_{\mathbf{p}} \begin{pmatrix} \mathbf{0} \\ \mathbf{0} \\ \mathbf{1} \end{pmatrix}$$
(175)

Since

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$$E\begin{pmatrix} 0\\0\\1 \end{pmatrix} = \begin{pmatrix} 0\\0\\1 \end{pmatrix}$$
(176)

$$\mathbf{R}\begin{pmatrix}\mathbf{0}\\\mathbf{1}\end{pmatrix} = \begin{pmatrix}\mathbf{0}\\\mathbf{0}\\\mathbf{1}\end{pmatrix} \tag{177}$$

the post multipliers can be dropped. Then, if we let

$$\frac{\partial (\mathbf{F}_{t}')_{1}}{\partial \psi_{p}} = \begin{vmatrix} \delta_{1} \\ \delta_{2} \\ \delta_{3} \\ \delta_{4} \\ \delta_{5} \\ \delta_{6} \end{vmatrix}$$

(178)

the derivative of F' with respect to platform yaw is

$$\begin{pmatrix} \frac{\partial F_{t}}{\partial \psi_{p}} \end{pmatrix}_{11} = \begin{bmatrix} \delta_{1} & \frac{1}{2}(\delta_{1} - \sqrt{3}\delta_{2}) & -\frac{1}{2}(\delta_{1} + \sqrt{3}\delta_{2}) \\ \delta_{2} & -\frac{1}{2}(\sqrt{3}\delta_{1} + \delta_{2}) & \frac{1}{2}(\sqrt{3}\delta_{1} - \delta_{2}) \\ \delta_{3} & -\delta_{3} & \delta_{3} \end{bmatrix}$$
(179)

$$\begin{pmatrix} \frac{\partial \mathbf{F}_{t}}{\partial \psi_{p}} \end{pmatrix}_{12} = \begin{bmatrix} -\delta_{1} & -1/2(\delta_{1} - \sqrt{3}\delta_{2}) & 1/2(\delta_{1} + \sqrt{3}\delta_{2}) \\ \delta_{2} & -1/2(\sqrt{3}\delta_{1} + \delta_{2}) & 1/2(\sqrt{3}\delta_{1} - \delta_{2}) \\ -\delta_{3} & \delta_{3} & -\delta_{3} \end{bmatrix}$$
(180)

$$\begin{pmatrix} \frac{\partial F_{t}}{\partial \psi_{p}} \end{pmatrix}_{21} = \begin{bmatrix} \delta_{4} & -1/2(\delta_{4} - \sqrt{3}\delta_{5}) & -1/2(\delta_{4} + \sqrt{3}\delta_{5}) \\ \delta_{5} & 1/2(\sqrt{3}\delta_{4} + \delta_{5}) & 1/2(\sqrt{3}\delta_{4} - \delta_{5}) \\ \delta_{6} & \delta_{6} & \delta_{6} \end{bmatrix}$$
(181)

$$\left(\frac{\Im F_{t}}{\Im \psi_{p}}\right)_{22} = \begin{bmatrix} \delta_{4} & -1/2(\delta_{4} - \sqrt{3}\delta_{5}) & -1/2(\delta_{4} + \sqrt{3}\delta_{5}) \\ -\delta_{5} & -1/2(\sqrt{3}\delta_{4} + \delta_{5}) & -1/2(\sqrt{3}\delta_{4} - \delta_{5}) \\ \delta_{6} & \delta_{6} & \delta_{6} \end{bmatrix}$$
(182)

thus

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$$\left(\frac{\partial \mathbf{F}_{t}}{\partial \psi_{p}}\right) = \begin{bmatrix} \mathbf{G}_{11t} & | & -\mathbf{RG}_{11t} \\ -\mathbf{G}_{12t} & | & -\mathbf{RG}_{12t} \end{bmatrix}$$
(183)

and

$$\begin{pmatrix} \frac{\partial \mathbf{F}'}{\partial \psi_{\mathbf{p}}} \end{pmatrix} = \begin{bmatrix} \mathbf{G}_{11} & \mathbf{G}_{12} \\ -\mathbf{G}_{11}\mathbf{R} & \mathbf{G}_{12}\mathbf{R} \end{bmatrix}$$
(184)

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The elements of this matrix are found from

$$\begin{pmatrix} \delta_{1} \\ \delta_{2} \\ \delta_{3} \end{pmatrix} = \frac{1}{\ell_{0}} \quad W^{2} \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix} W(a) \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$$
(185)

and

$$\begin{pmatrix} \delta_4 \\ \delta_5 \\ \delta_6 \end{pmatrix} = W(a) \begin{pmatrix} \delta_1 \\ \delta_2 \\ \delta_3 \end{pmatrix}$$
(186)

Thus

$$\begin{pmatrix} \delta_{1} \\ \delta_{2} \\ \delta_{3} \end{pmatrix} = \frac{1}{l_{0}} \begin{bmatrix} -a_{x}(\alpha\beta) - a_{y}(\beta^{2} + \gamma^{2}) \\ a_{x}(\alpha^{2} + \gamma^{2}) + a_{y}(\alpha\beta) \\ -a_{x}(\beta\gamma) + a_{y}(\alpha\gamma) \end{bmatrix}$$
(187)

$$\begin{pmatrix} \delta_4 \\ \delta_5 \\ \delta_6 \end{pmatrix} = \begin{bmatrix} a_y \delta_3 - a_z \delta_2 \\ a_z \delta_1 - a_x \delta_3 \\ a_x \delta_2 - a_y \delta_1 \end{bmatrix}$$
(188)

To find the derivative of the F matrix, it is now necessary to pre- and postmultiply this by F. If we let

$$G = \frac{\partial F'}{\partial \psi_{\rm p}}$$
(189)

then

$$\frac{\partial F}{\partial \psi_{\rm p}} = -FGF \tag{190}$$

The intermediate product, GF, is given by

$$J = GF = \begin{bmatrix} J_{11} & J_{12} \\ -J_{12} & -J_{11} \end{bmatrix}$$
(191)

where

$$J_{11} = \begin{bmatrix} .j_{11} & j_{12} & 0 \\ -j_{12} & -j_{11} & j_{23} \\ 0 & -j_{23} & j_{11} \end{bmatrix}$$
(192)

and

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$$J_{12} = \begin{bmatrix} -j_{23} & 0 & j_{16} \\ 0 & -j_{16} & 0 \\ j_{16} & 0 & j_{12} \end{bmatrix}$$
(193)

$$j_{11} = -\frac{3}{6\gamma\nu} \left[ a_{y}\gamma\delta_{1} - a_{x}\gamma\delta_{2} + (a_{y}\alpha - a_{x}\beta)\delta_{3} \right]$$
(194)

$$\mathbf{j}_{12} = -\frac{1}{6\gamma\nu} \left[ -(2a_y + \sqrt{3}a_x)\gamma\delta_1 + \sqrt{3}a_y\gamma\delta_2 + + \left\{ (2a_y + \sqrt{3}a_x)\alpha - \sqrt{3}a_y\beta\}\delta_3 \right]$$
(195)

$$\mathbf{j}_{23} = \frac{1}{6\gamma\nu} \left[ a_{y}\gamma\delta_{1} + 3a_{x}\gamma\delta_{2} - (a_{y}\alpha + 3a_{x}\beta)\delta_{3} \right]$$
(196)

$$j_{16} = -\frac{1}{6\gamma\nu} \left[ -(2a_{y} - \sqrt{3} a_{x})\gamma\delta_{1} - \sqrt{3}a_{y}\gamma\delta_{2} + \left\{ (2a_{y} - \sqrt{3}a_{x})\alpha + \sqrt{3}a_{y}\beta\}\delta_{3} \right]$$
(197)

The derivative of F is then

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$$\mathbf{P} = \frac{\partial \mathbf{F}}{\partial \psi_{\mathbf{p}}} = -\begin{bmatrix} \mathbf{F}_{11} & | & \mathbf{RF}_{11} \\ \mathbf{F}_{21} & | & -\mathbf{RF}_{21} \end{bmatrix} \begin{bmatrix} \mathbf{J}_{11} & | & \mathbf{J}_{12} \\ -\mathbf{J}_{12} & | & -\mathbf{J}_{11} \end{bmatrix}$$
(198)

or

$$P = \begin{bmatrix} P_{11} & -RP_{11} \\ \overline{P}_{21} & -P_{21} \end{bmatrix}$$
(199)

where

$$P_{11} = -(F_{11}J_{11} - RF_{11}J_{12})$$
(200)

and

$$P_{21} = -(F_{21}J_{11} + RF_{21}J_{12})$$
(201)

These expressions can be evaluated using equations (67), (83) and (191) to give the components of P.

# Incremental Changes in Spring Constants

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Because of the symmetry of the triogonal system, it was necessary to assume an arbitrary relationship between symmetrical actuators. For convenience, they were made equal. It will also be convenient to retain this relationship for deviations from the neutral position, resulting from yaw and pitch angle inputs. If we let the three specified spring constants be

$$\left(\frac{1}{k}\right)_{\mathrm{H}} = \begin{pmatrix} 1/k_{\mathrm{x}} \\ 1/k_{\mathrm{\theta}} \\ 1/k_{\mathrm{z}} \end{pmatrix}_{\mathrm{H}}$$
 (202)

as measured in the pitch system, and the resultant three actuator spring constants be

$$\left(\frac{1}{k}\right)_{g} = \begin{pmatrix} 1/k_{1} \\ 1/k_{2} \\ 1/k_{3} \end{pmatrix}$$
(203)

then, for this choice of specified constants

. . .

$$\left(\frac{1}{k}\right)_{\ell} = 1/2 \ \kappa_{l}' \ \left(\frac{1}{k}\right)_{H}$$
(204)

Similar expressions are obtained for other choices of specified constants. Since the specification is assumed to be along the pitch system axes, which are fixed to the vehicle, the instantaneous pitch angle, as well as the triogonal yaw angle affects the actuator constants. The pitch angle transformation does not appear explicitly in the definition of  $K_1$  since to do so might require real time inversion of this matrix. Instead, the neutral value of pitch angle has been assumed to be zero, for which the pitch system axes are parallel to the platform axes. To differentiate the above equation, the effect of pitch angle must be included. To do this, we can generalize the definition of the matrix K to include the pitch system transformation. With K given by equation 63

$$A = H_{\rm H} \cdot F \tag{205}$$

It then follows that

$$\frac{\partial K}{\partial \theta_{\rm H}} = 2 \begin{bmatrix} a_{11} \frac{\partial a_{11}}{\partial \theta {\rm H}} & \cdots & a_{16} \frac{\partial a_{16}}{\partial \theta_{\rm H}} \\ \vdots & & \vdots \\ \vdots & & \vdots \\ a_{61} \frac{\partial a_{61}}{\partial \theta_{\rm H}} & \cdots & a_{66} \frac{\partial a_{66}}{\partial \theta_{\rm H}} \end{bmatrix}$$
(206)

and

and

$$\frac{\partial K}{\partial \theta_{p}} = 2 \begin{bmatrix} a_{11} & \frac{\partial a_{11}}{\partial \psi_{p}} & \cdots & a_{16} & \frac{\partial a_{16}}{\partial \psi_{p}} \\ \vdots & & \vdots & \vdots \\ a_{61} & \frac{\partial a_{61}}{\partial \psi_{p}} & \cdots & a_{66} & \frac{\partial a_{66}}{\partial \psi_{p}} \end{bmatrix}$$

(207)

where

$$\frac{\partial A}{\partial \theta_{H}} = \frac{\partial H_{H}}{\partial \theta_{H}} \quad F = - \begin{bmatrix} W \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} & 0 \\ - & 0 \end{pmatrix} A \\ 0 & W \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} \end{bmatrix} A$$
(208)

and

$$\frac{\partial A}{\partial \psi}_{p} = H_{H} \frac{\partial F}{\partial \psi}_{p} = H_{H} \begin{bmatrix} \frac{P_{11}}{P_{21}} & | & -R^{P_{11}}\\ -R^{P_{11}} & | & -R^{P_{11}}\\ -R^{P_{11}} & | & -R^{P_{11}}\\ -R^{P_{11}} & | & -R^{P_{11}}\\ \end{array}$$
(209)

For variations in the pitch angle, we then have

$$\frac{\partial K}{\partial \theta_{\rm H}} = 2 \begin{bmatrix} -a_{11}a_{31} - a_{12}a_{32} & -a_{13}a_{33} \\ 0 & 0 & 0 \\ \frac{a_{11}a_{31}}{31} & a_{12}a_{32} & a_{13}a_{33} \\ -a_{41}a_{61} - a_{42}a_{62} & -a_{43}a_{63} \\ 0 & 0 & 0 \\ a_{41}a_{61} & a_{42}a_{62} & a_{43}a_{63} \\ -a_{41}a_{61} & a_{42}a_{62} & a_{43}a_{63} \\ 0 & 0 & 0 \\ -a_{41}a_{61} & a_{42}a_{62} & a_{43}a_{63} \\$$

The variation of the diagonal elements of the spring constant matrix as measured in the pitch system, due to pitch angle changes, is

$$\frac{\partial}{\partial \theta_{\rm H}} \left(\frac{1}{\rm k}\right)_{\rm H} = \frac{\partial K}{\partial \theta_{\rm H}} \left(\frac{1}{\rm k}\right)_{\rm \ell} + K \frac{\partial}{\partial \theta_{\rm H}} \left(\frac{1}{\rm k}\right)_{\rm \ell}$$
(211)

Since the last three columns of both K and  $\frac{\partial K}{\partial \theta}$  are equal to the first three columns, and the spring constants of the symmetrical actuators have been chosen equal, it follows that, for the three specified spring constants

$$\frac{\partial}{\partial \theta_{\rm H}} \left(\frac{1}{\rm k}\right)_{\rm H} = 2 \frac{\partial K_{\rm I}}{\partial \theta_{\rm H}} \left(\frac{1}{\rm k}\right)_{\rm g} + 2K_{\rm I} \frac{\partial}{\partial \theta_{\rm H}} \left(\frac{1}{\rm k}\right)_{\rm g}$$
(212)

If these three spring constants are to remain invariant with changes in pitch angle

$$\frac{\partial}{\partial \theta_{\rm H}} \left(\frac{1}{\rm k}\right)_{\rm g} = - \kappa_{\rm l}' \frac{\partial \kappa_{\rm l}}{\partial \theta_{\rm H}} \left(\frac{1}{\rm k}\right)_{\rm g}$$
(213)

For variations of the yaw angle

$$\frac{\partial \Lambda}{\partial \psi_{p}} = H_{H} \left[ \frac{P_{11}}{P_{21}} - \frac{|-RP_{11}|}{|-RP_{21}|} \right]$$
(214)

and

$$A = H_{H} \left[ \frac{F_{11}}{F_{21}} - \frac{|RF_{11}|}{|-RF_{21}|} \right]$$
(215)

Then

$$\frac{\partial K}{\partial \psi_{p}} = \begin{bmatrix} \frac{\partial K_{11}}{\partial \psi_{p}} & | & - & \frac{\partial K_{11}}{\partial \psi_{p}} \\ \frac{\partial F_{21}}{\partial K_{21}} & | & - & \frac{\partial F_{21}}{\partial K_{21}} \\ \frac{\partial F_{21}}{\partial \psi_{p}} & | & - & \frac{\partial F_{21}}{\partial \psi_{p}} \end{bmatrix}$$
(216)

Again

$$\frac{\partial}{\partial \Psi_{\mathbf{p}}} \left(\frac{1}{\mathbf{k}}\right)_{\mathbf{H}} = \frac{\partial K}{\partial \Psi_{\mathbf{p}}} \left(\frac{1}{\mathbf{k}}\right)_{\mathbf{g}} + K \frac{\partial}{\partial \Psi_{\mathbf{p}}} \left(\frac{1}{\mathbf{k}}\right)_{\mathbf{g}}$$
(217)

Since the last three columns of  $\frac{\partial K}{\partial \psi}_p$  are the negative of the first three, and the spring constants of symmetrical actuators have been chosen equal

$$\frac{\partial K}{\partial \psi_{p}} \left(\frac{1}{k}\right)_{k} = 0$$
(218)

It then follows for the three specified spring constants

$$\frac{\partial}{\partial \psi_{\mathbf{p}}} \left(\frac{1}{\mathbf{k}}\right)_{\mathbf{H}} = 2K_{\mathbf{1}} \frac{\partial}{\partial \psi_{\mathbf{p}}} \left(\frac{1}{\mathbf{k}}\right)_{\mathbf{g}}$$
(219)

If these are to remain invariant with changes in yaw angle, the changes in actuator spring constants are zero

$$\frac{\partial}{\partial \psi_{\mathbf{p}}} \left(\frac{1}{\mathbf{k}}\right)_{\boldsymbol{\ell}} = 0 \tag{220}$$

#### Incremental Actuator Extensions

After calculating the change in gravitational force and the change in spring constant, the change in actuator extension is found from

$$\delta(\Delta \ell) = L_{\ell} \delta(f_{\ell}) + [f_{\ell}]\delta\left(\frac{1}{k}\right)_{\ell}$$
(221)

or, for the n-th actuator

$$\delta (\Delta k)_{n} = \left(\frac{1}{k_{n}}\right) \delta(f_{n}) + f_{n} \delta\left(\frac{1}{k_{n}}\right)$$
(222)

This calculation must be made in real time since the variations of actuator force and spring constant are functions of time.

In addition, the actuator lengths must be changed to produce the yaw motion. From equation 16, the squared lengths of the actuators are

$$\left(\ell_{o}\right)_{n}^{2} = \ell_{n_{t}}\ell_{n}$$
(223)

where  $\ensuremath{\substack{k\\n}}$  is the vector actuator length

$$\ell_{n} = r_{p} + a_{n} - E(x_{3p})b_{n}$$
(224)

For yaw motion

$$E(x_{3p}) = \begin{bmatrix} \cos\psi_{p} & \sin\psi_{p} & 0 \\ -\sin\psi_{p} & \cos\psi_{p} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$
(225)

Then

$$\ell_{n} = \begin{pmatrix} 0 \\ 0 \\ z_{p} \end{pmatrix} + \begin{pmatrix} a \\ a^{x} \\ y \\ a^{z} \\ n \end{pmatrix} - \begin{bmatrix} b_{x} \cos \psi + b_{y} \sin \psi \\ -b_{x} \sin \psi + b_{y} \cos \psi \\ b_{x} & p & y & p \\ b_{z} & 0 & 0 \end{bmatrix} n$$
(226)

The squared length is

$$l_{n}^{2} = \{a_{x} - b_{x}\cos\psi_{p} - b_{y}\sin\psi_{p}\}_{n}^{2} + \{a_{y} + b_{x}\sin\psi_{p} - b_{y}\cos\psi_{p}\}_{n}^{2} + \{z_{p} + a_{z} - b_{z}\}^{2}$$
(227)

By expanding  $\sin \psi_{D}$  and  $\cos t \psi_{D}$ , the change in length is found to be

$$\delta \ell_{n} = \ell_{0} \{ C_{1} \psi_{p} - 1/2 (C_{1}^{2} - C_{2}) \psi_{p}^{2} + \frac{C_{1}}{6} (3C_{1}^{2} - 3C_{2} - 1) \psi_{p}^{3} + \dots \}$$
(228)

where

$$C_{1} = \frac{1}{lo^{2}} \left( a_{y} b_{x} - a_{x} b_{y} \right)$$
(229)

$$C_{2} = \frac{1}{lo^{2}} \left( a_{x} b_{x} + a_{y} b_{y} \right)$$
(230)

The first two terms will provide an accuracy of about 0.1% for angles up to 3.5 degrees. The third term increases this to 0.001%. Only two values need be calculated, since all odd numbered actuators and all even numbered actuators change by the same amount.

Exact Calculations of Pitch Angle Effects

The relatively large values of  $K_1' \quad \frac{\partial K_1}{\partial \theta_H}$  obtained when evaluated numerically indicate that linearization about zero pitch angle will introduce considerable error for angles up to 15 degrees. Therefore, the effects of pitch angle

will be calculated using the exact relationships. Linearization will still be used for yaw angle changes; however, this will be calculated for the instantaneous value of pitch angle. This is possible since the yaw angle inputs will be considerably smaller (less than 3.5 degrees).

To develop the equations for an exact solution, it is assumed that the matrix, F, includes the z-displacement to the origin of the pitch system. Then, the matrix, A, is given by

$$A = \begin{bmatrix} \frac{E_{H}}{0} & 0 \\ 0 & E_{H} \end{bmatrix} \begin{bmatrix} \frac{F_{11}}{1} & \frac{RF_{11}}{1} \\ F_{21} & RF_{21} \end{bmatrix}$$
(231)

But, since

 $E_{\rm H}R = RE_{\rm H} \tag{232}$ 

for pitch angle inputs

$$A = \begin{bmatrix} (E_{H}F_{11}) & | & R(E_{H}F_{11}) \\ (E_{H}F_{21}) & | & -R(E_{H}F_{21}) \end{bmatrix}$$
(233)

Thus

$$A_{11} = \begin{bmatrix} (f_{11}^{\cos\theta} - f_{31}^{\sin\theta}) & (f_{12}^{\cos\theta} - f_{32}^{\sin\theta}) & (f_{13}^{\cos\theta} - f_{33}^{\sin\theta}) \\ f_{21} & f_{22} & f_{23} \\ (f_{31}^{\cos\theta} + f_{11}^{\sin\theta}) & (f_{32}^{\cos\theta} + f_{12}^{\sin\theta}) & (f_{33}^{\cos\theta} + f_{13}^{\sin\theta}) \end{bmatrix}$$
(234)

and

$$A_{21} = \begin{bmatrix} (f_{41}^{\cos\theta} - f_{61}^{\sin\theta}) & (f_{42}^{\cos\theta} - f_{62}^{\sin\theta}) & (f_{43}^{\cos\theta} - f_{63}^{\sin\theta}) \\ f_{51} & f_{52} & f_{53} \\ (f_{61}^{\cos\theta} + f_{41}^{\sin\theta}) & (f_{62}^{\cos\theta} + f_{42}^{\sin\theta}) & (f_{63}^{\cos\theta} + f_{43}^{\sin\theta}) \end{bmatrix}$$
(235)

The matrix, K, is found by squaring each of these elements. Thus, the submatrix,  $K_1$ , is equal to

$$K_{1} = \begin{bmatrix} (f_{11}\cos\theta - f_{31}\sin\theta)^{2} & (f_{12}\cos\theta - f_{32}\sin\theta)^{2} & (f_{13}\cos\theta - f_{33}\sin\theta)^{2} \\ f_{51}^{2} & f_{52}^{2} & f_{53}^{2} \\ (f_{31}\cos\theta + f_{11}\sin\theta)^{2} & (f_{32}\cos\theta + f_{12}\sin\theta)^{2} & (f_{33}\cos\theta + f_{13}\sin\theta)^{2} \end{bmatrix} (236)$$

This can be inverted by evaluating the cofactors. If we let

$$K_{10} = \begin{bmatrix} f_{11}^{2} & f_{12}^{2} & f_{13}^{2} \\ f_{51}^{2} & f_{52}^{2} & f_{53}^{2} \\ f_{31}^{2} & f_{32}^{2} & f_{33}^{2} \end{bmatrix}$$
(237)

1.

and

$$\begin{aligned} |\kappa_{20}| &= f_{51}^{2} \left[ f_{13}f_{33}(f_{12}^{2} + f_{32}^{2}) - f_{12}f_{32}(f_{13}^{2} + f_{33}^{2}) \right] \\ &+ f_{52}^{2} \left[ f_{11}f_{31}(f_{13}^{2} + f_{33}^{2}) - f_{13}f_{33}(f_{11}^{2} + f_{31}^{2}) \right] \\ &+ f_{53}^{2} \left[ f_{12}f_{32}(f_{11}^{2} + f_{31}^{2}) - f_{11}f_{31}(f_{12}^{2} + f_{32}^{2}) \right] \end{aligned}$$
(238)

then, the determinant of  $\boldsymbol{K}_l$  is

$$|K_1| = |K_{10}| \cos 2\theta + |K_{20}| \sin 2\theta$$
 (239)

The cofactors of  $K_1$  are  $(K_1)_{mn}$  and the cofactors of  $K_{10}$  are  $(K_{10})_{mn}$ . Then, since

$$\left(\frac{1}{k}\right)_{\ell} = 1/2 \quad K' \left(\frac{1}{k}\right)_{\mathrm{H}}$$
(240)

the actuator spring constants can be found from the inverse of  $\ensuremath{\kappa_1}$ 

$$K_{1}' = K_{10}' \left\{ \cos^{2}\theta - \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix} \sin^{2}\theta \right\} + K_{30}'\sin^{2}\theta$$
(241)

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where

$$K_{10}' = \frac{1}{|K_1|} \begin{bmatrix} (K_{10})_{11} & (K_{10})_{21} & (K_{10})_{31} \\ (K_{10})_{12} & (K_{10})_{22} & (K_{10})_{32} \\ (K_{10})_{13} & (K_{10})_{23} & (K_{10})_{33} \end{bmatrix}$$
(242)  
$$K_{30}' = \frac{1}{|K_1|} \begin{bmatrix} (K_{20})_{11} & -(K_{20})_{21} & (K_{20})_{11} \\ (K_{20})_{12} & -(K_{20})_{22} & (K_{20})_{12} \\ (K_{20})_{13} & -(K_{20})_{23} & (K_{20})_{13} \end{bmatrix}$$
(243)

$$\kappa_{20} = f_{51}^{2} (\kappa_{20})_{21} + f_{52}^{2} (\kappa_{20})_{22} + f_{53}^{2} (\kappa_{20})_{23}$$
(244)

Similar expressions can be found for other choices of specified spring constants. In general, each of the cofactors and the determinant of the resulting matrix,  $K_n$ , will be of the form

$$(K_{n})_{pq} = C_{1} \cos^{4} \theta_{H} + C_{2} \cos^{3} \theta_{H} \sin^{2} \theta_{H} + C_{4} \cos^{2} \theta_{H} \sin^{2} \theta_{H} + C_{4} \cos^{2} \theta_{H} \sin^{3} \theta_{H} + C_{5} \sin^{4} \theta_{H}$$

$$(245)$$

or

$$(K_n)_{pq} = C_1 \cos^2 \theta_H + C_2 \cos \theta_H \sin \theta_H + C_3 \sin^2 \theta_H$$
(246)

The derivative of A with respect t  $_{0} \psi_{p}$  is now

$$\frac{\partial A}{\partial \psi_{p}} = \begin{bmatrix} E_{H} & 0 \\ 0 & E_{H} \end{bmatrix} \frac{\partial F}{\partial \psi_{p}} = \begin{bmatrix} (E_{H}P_{11}) & -R(E_{H}P_{11}) \\ (E_{H}P_{21}) & R(E_{H}P_{21}) \end{bmatrix}$$
(247)

The derivative of K is then

$$\frac{\partial K}{\partial \psi_{p}} = \begin{bmatrix} \frac{\partial K_{11}}{\partial \psi_{p}} & -\frac{\partial K_{11}}{\partial \psi_{p}} \\ \frac{\partial K_{21}}{\partial \psi_{p}} & -\frac{\partial K_{21}}{\partial \psi_{p}} \\ \frac{\partial K_{21}}{\partial \psi_{p}} & -\frac{\partial K_{21}}{\partial \psi_{p}} \end{bmatrix}$$
(248)

as before. Thus

$$\frac{\partial}{\partial \psi} \left(\frac{1}{k}\right)_{\ell} = 0$$
(249)

The gravitational loading can be found as a function of time from

$$\mathbf{f}_{\ell} = \mathbf{m}\mathbf{F}_{t} \left[ \frac{1}{\mathbf{W}(\mathbf{E}_{H} \cdot \mathbf{r}_{v})} - \right] \mathbf{g}_{G}$$
(250)

where  $\boldsymbol{g}_{\boldsymbol{G}}$  is given by equation (124) and

$$E_{H v}^{\prime} = \begin{bmatrix} x_{v} \cos \theta_{H} - z_{v} \sin \theta_{H} \\ y_{v} \\ z_{v} \cos \theta_{H} + x_{v} \sin \theta_{H} \end{bmatrix}$$
(251)

Thus, the gravitational moments are now

$$\begin{pmatrix} \mathbf{g}_{\phi} \\ \mathbf{g}_{\theta} \\ \mathbf{g}_{\psi} \end{pmatrix} = \begin{bmatrix} \mathbf{Y}_{\mathbf{v}} \mathbf{g}_{\mathbf{z}} - (\mathbf{z}_{\mathbf{v}} \cos\theta_{\mathbf{H}} + \mathbf{x}_{\mathbf{v}} \sin\theta_{\mathbf{H}}) \mathbf{g}_{\mathbf{y}} \\ (\mathbf{z}_{\mathbf{v}} \cos\theta_{\mathbf{H}} + \mathbf{x}_{\mathbf{v}} \sin\theta_{\mathbf{H}}) \mathbf{g}_{\mathbf{y}} - (\mathbf{x}_{\mathbf{v}} \cos\theta_{\mathbf{H}} - \mathbf{z}_{\mathbf{v}} \sin\theta_{\mathbf{H}}) \mathbf{g}_{\mathbf{z}} \\ (\mathbf{x}_{\mathbf{v}} \cos\theta_{\mathbf{H}} - \mathbf{z}_{\mathbf{v}} \sin\theta_{\mathbf{H}}) \mathbf{g}_{\mathbf{y}} - \mathbf{y}_{\mathbf{v}} \mathbf{g}_{\mathbf{x}} \end{bmatrix}$$
(252)

and, as before

$$f_{g} = mF_{t} \begin{bmatrix} g_{x} \\ g_{y} \\ g_{z} \\ g_{\phi} \\ g_{\theta} \\ g_{\psi} \end{bmatrix}$$
(253)

The change in gravitational loading due to yaw angle is obtained by replacing  $r_v$  in the earlier equations by  $E_H^{\,\prime}r_v^{\,}$ . If  $r_H^{\,}$  is included in the definition of F

$$\frac{\partial f_{g}}{\partial \psi_{p}} = m \left( \frac{\partial F_{t}}{\partial \psi_{p}} \right) \left[ \frac{1}{W(E_{H}'r_{v})} \right] g_{G}$$
$$- mF_{t} \left[ \frac{-\frac{1}{W(E_{H}'r_{v})}}{W(E_{H}'r_{v})} \right] W \left( \begin{array}{c} 0 \\ 0 \\ 1 \end{array} \right) g_{G}$$
(254)

$$\frac{\partial f_{\ell}}{\partial \psi_{p}} = m \left( \frac{\partial F_{t}}{\partial \psi_{p}} \right) \left[ \begin{array}{c} g_{x} \\ g_{y} \\ g_{z} \\ g_{\theta} \\ g_{\theta} \\ g_{\psi} \end{array} \right] +$$

$$- mF_{t} \left[ \begin{array}{c} -g_{y} \\ g_{x} \\ 0 \\ -(z_{v}\cos\theta_{H} + x_{v}\sin\theta_{H})g_{x} \\ -(z_{v}\cos\theta_{H} + x_{v}\sin\theta_{H})g_{y} \\ y_{v}g_{y} + (x_{v}\cos\theta_{H} - z_{v}\sin\theta_{H})g_{x} \\ \end{bmatrix} \right]$$

(255)

The rest of the calculations remain as before.

Summary of Calculations

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## Mean Values

Spring Constants (Off-line). Three spring constants are to be specified either in the platform system (aircraft) or pitch system (combat vehicle). The corresponding rows of the 6 x 3 matrix

$$\begin{bmatrix} -\frac{K}{K_{21}} \end{bmatrix} = \frac{1}{36(\gamma\nu)^{2}} \begin{bmatrix} 4\lambda^{2} (\lambda - \sqrt{3}\mu)^{2} (\lambda + \sqrt{3}\mu)^{2} \\ 4\mu^{2} (\sqrt{3}\lambda + \mu)^{2} (\sqrt{3}\lambda - \mu)^{2} \\ \frac{\nu^{2}}{4\alpha^{2}} - \frac{\nu^{2}}{(\alpha - \sqrt{3}\beta)^{2}} - \frac{\nu^{2}}{(\alpha + \sqrt{3}\beta)^{2}} \\ 4\beta^{2} (\sqrt{3}\alpha + \beta)^{2} (\sqrt{3}\alpha - \beta)^{2} \\ \gamma^{2} \gamma^{2} \gamma^{2} \gamma^{2} \gamma^{2} \end{bmatrix}$$
(256)

or

are then selected to form the  $3 \times 3$  spring constant matrix. For instance if  $k_x$ ,  $k_\theta$ , and  $k_z$  are specified, this matrix is equal to

$$K_{1} = \frac{1}{36(\gamma\nu)^{2}} \begin{bmatrix} 4\lambda^{2} & (\lambda - \sqrt{3}\mu)^{2} & (\lambda + \sqrt{3}\mu)^{2} \\ 4\beta^{2} & (\sqrt{3}\alpha + \beta)^{2} & (\sqrt{3}\alpha - \beta)^{2} \\ \nu^{2} & \nu^{2} & \nu^{2} \end{bmatrix}$$
(257)

The actuator spring constants are then found by inverting this matrix. For this case

$$K_{1}' = \frac{3\gamma\nu}{(\alpha\mu - \beta\lambda)} \begin{bmatrix} 4\alpha\beta & 4\lambda\mu & \frac{4\gamma(3\alpha\mu + \beta\lambda)}{\nu} \\ (\sqrt{3}\alpha + \beta)(\alpha - \sqrt{3}\beta) & (\sqrt{3}\lambda + \mu)(\lambda - \sqrt{3}\mu) & \frac{4\gamma[\sqrt{3}(\alpha\nu - \beta\mu) - 2\beta\lambda]}{\nu} \\ -(\sqrt{3}\alpha - \beta)(\alpha + \sqrt{3}\beta) & -(\sqrt{3}\lambda - \mu)(\lambda + \sqrt{3}\mu) - \frac{4\gamma[\sqrt{3}(\alpha\nu - \beta\mu) + 2\beta\lambda]}{\nu} \end{bmatrix} (258)$$

and the actuator spring constants are equal to

$$\begin{pmatrix} \frac{1}{k_1} \\ \frac{1}{k_2} \\ \frac{1}{k_3} \end{pmatrix} = \begin{pmatrix} \frac{1}{k_4} \\ \frac{1}{k_5} \\ \frac{1}{k_6} \end{pmatrix} = \frac{1}{2} K_1' \begin{pmatrix} \frac{1}{k_x} \\ \frac{1}{k_{\theta}} \\ \frac{1}{k_z} \end{pmatrix}$$

For the combat vehicle, a real time calculation of the spring constants, is required to include the effects of the instantaneous pitch angle. This involves determining the coefficients, in the cofactors of  $K_n$ , of the cosine and sine terms, for the particular choice of spring constants. In the most general case, the spring constant of actuator one is given by

$$\frac{1}{k_{1}} = \frac{1}{2|K_{n}|} \{ (K_{n})_{11} (\frac{1}{k_{u}}) + (K_{n})_{21} (\frac{1}{k})_{v} + (K_{n})_{31} (\frac{1}{k})_{w} \}$$
(260)

where u, v, and w are the specified axes. Each of the cofactors contains terms of the form

(259)

$$(K_{n})_{11} = C_{11} \cos^{4} \theta_{H} + C_{12} \cos^{3} \theta_{H} \sin \theta_{H} + C_{13} \cos^{2} \theta_{H} \sin^{2} \theta_{H} + C_{14} \cos^{2} \theta_{H} \sin^{3} \theta_{H} + C_{15} \sin^{4} \theta_{H}$$
(261)

Thus, for the desired specified constants, it is necessary to find the coefficients

$$d_{11} = C_{11}(\frac{1}{k_u}) + C_{21}(\frac{1}{k_v}) + C_{31}(\frac{1}{k_w})$$
(262)

$$d_{12} = C_{12}(\frac{1}{k_u}) + C_{22}(\frac{1}{k_v}) + C_{32}(\frac{1}{k_w})$$
(263)

$$d_{13} = C_{13}(\frac{1}{k_u}) + C_{23}(\frac{1}{k_v}) + C_{33}(\frac{1}{k_w})$$
(264)

$$d_{14} = C_{14}(\frac{1}{k_u}) + C_{24}(\frac{1}{k_v}) + C_{34}(\frac{1}{k_w})$$
(265)

$$d_{15} = C_{15}(\frac{1}{k_{u}}) + C_{25}(\frac{1}{k_{v}}) + C_{35}(\frac{1}{k_{w}})$$
(266)

then

$$\frac{1}{k_{1}} = \frac{1}{2|K_{n}|} \{ d_{11}\cos^{4}\theta_{H} + d_{12}\cos^{3}\theta_{H}\sin\theta_{H} + d_{13}\cos^{2}\theta_{H}\sin^{2}\theta_{H} + d_{14}\cos\theta_{H}\sin^{3}\theta_{H} + d_{15}\sin^{4}\theta_{H} \}$$
(267)

The determinant,  $|K_n|$ , is also a function of the angle,  $\theta_H$ , but the coefficients do not depend on the values of the specified constants. This evaluation must be made for all three actuator spring constants. The coefficients,  $C_{mn}$ , depend only on the choice of axes for which spring constants are specified. These need be caluclated only once for each choice of axes (of which there are 13 possible combinations, 7 of which include the x-axis).

This method of calculation eliminates the necessity of real time matrix inversion, and will give greater accuracy.

Actuator Forces (On-line). The gravity vector must first be resolved along the gimbal system axes, so

$$g_{G} = g \begin{bmatrix} -\cos\psi_{G} \sin\theta_{G} \\ \sin\psi_{G} \sin\theta_{G} \\ \cos\theta_{G} \end{bmatrix} = \begin{pmatrix} g_{x} \\ g_{y} \\ g_{z} \end{pmatrix}$$
(268)

Then, the gravitational moments about the platform system are calculated, and

$$W(\mathbf{r})g_{\mathbf{G}} = \begin{bmatrix} yg_{\mathbf{z}} - zg_{\mathbf{y}} \\ zg_{\mathbf{x}} - xg_{\mathbf{z}} \\ xg_{\mathbf{y}} - yg_{\mathbf{x}} \end{bmatrix} = \begin{pmatrix} g_{\phi} \\ g_{\theta} \\ g_{\psi} \end{pmatrix}$$
(269)

where

$$\mathbf{r} = \begin{pmatrix} \mathbf{x} \\ \mathbf{y} \\ \mathbf{z} \end{pmatrix} = \begin{bmatrix} \mathbf{x} \\ \mathbf{y} \\ \mathbf{y} \\ \mathbf{y} \\ \mathbf{z} \\ \mathbf{y} + \mathbf{z} \\ \mathbf{H} \end{bmatrix}$$
(270)

is the displacement of the center of mass of the aircraft from the origin of the platform system in platform coordinates, and

$$\mathbf{r} = \begin{pmatrix} \mathbf{x} \\ \mathbf{y} \\ \mathbf{z} \end{pmatrix} = \begin{bmatrix} \mathbf{x}_{\mathbf{v}} \cos\theta_{\mathrm{H}} - \mathbf{z}_{\mathbf{v}} \sin\theta_{\mathrm{H}} \\ \mathbf{y}_{\mathbf{v}} \\ \mathbf{z}_{\mathbf{v}} \cos\theta_{\mathrm{H}} + \mathbf{x}_{\mathbf{v}} \sin\theta_{\mathrm{H}} \\ \end{bmatrix}$$
(271)

is the displacement of the center of mass of the combat vehicle from the origin of the pitch system in platform coordinates. These components are then summed, after multiplying by the proper gain factors (elements of F matrix) to give the actuator forces,

$$\mathbf{f}_{\mathfrak{L}} = \begin{bmatrix} \mathbf{f}_{1} \\ \mathbf{f}_{2} \\ \mathbf{f}_{3} \\ \mathbf{f}_{4} \\ \mathbf{f}_{5} \\ \mathbf{f}_{6} \end{bmatrix} = \mathbf{mF}_{\mathsf{t}} \begin{bmatrix} \mathbf{g}_{\mathsf{x}} \\ \mathbf{g}_{\mathsf{y}} \\ \mathbf{g}_{z} \\ \mathbf{g}_{\phi} \\ \mathbf{g}_{\phi} \\ \mathbf{g}_{\theta} \\ \mathbf{g}_{\psi} \end{bmatrix}$$

(272)

Actuator Extensions (On-line). The actuator extensions are found simply by dividing each actuator force by the corresponding actuator spring constant, thus

$$(\Delta k)_{n} = \frac{f_{n}}{k_{n}} \text{ for } n = 1 \text{ to } 6.$$
(273)

Effective Mass Loads (Off-line). The mass load matrix is given by

$$m_{\chi} = F_{t} \begin{bmatrix} 1 & \downarrow & 0 \\ W(r) & \downarrow & 1 \end{bmatrix} \begin{bmatrix} m & \downarrow & 0 \\ 0 & \downarrow & J \end{bmatrix} \begin{bmatrix} 1 & \downarrow & -W(r) \\ 0 & \downarrow & I \end{bmatrix} F$$
(274)

where r is again the displacement of the center of mass from the platform origin, in platform coordinates. This is a straightforward matrix multiplication involving the location of the center of mass and the values of mass and moments of inertia. The result is a 6 x 6 matrix, containing the principal and crosscoupling mass terms. Since the model is a single DOF system, the mutual terms cannot be included. Either the principal terms or a combination of principal and mutual terms will be used for the inputs to the model. This choice will depend on experimental results.

Pitch Angle Effects (On-line)

This calculation is not required for the aircraft, as long as the displacement, r, is measured in the platform system. For the combat vehicle, the effect on gravitational forces was explained previously.

Spring Constants. For the actuator spring constants, it is necessary to evaluate the functions

$$2 |K_{m}| \frac{1}{k_{n}} = \begin{cases} \frac{d_{n1} \cos^{4} \theta_{H} + d_{n2} \cos^{3} \theta_{H} \sin \theta_{H} + d_{n3} \cos^{2} \theta_{H} \sin^{2} \theta_{H}}{+ d_{n4} \cos \theta_{H} \sin^{3} \theta_{H} + d_{n5} \sin^{4} \theta_{H}} \end{cases}$$
(275)

for n = 1 to 6

$$|K_{\rm m}| = d_{\rm ol} \cos^4 \theta_{\rm H} + d_{\rm o2} \cos^3 \theta_{\rm H} \sin \theta_{\rm H} + d_{\rm o3} \cos^2 \theta_{\rm H} \sin^2 \theta_{\rm H} + d_{\rm o4} \cos^2 \theta_{\rm H} \sin^2 \theta_{\rm H} + d_{\rm o5} \sin^4 \theta_{\rm H}$$

$$(276)$$

The coefficients, d<sub>pg</sub>, are found off-line as explained earlier.

Effective Mass Load. No correction will be made to the effective mass load, due to pitch or yaw angle variations. These corrections would be small (maybe 10%) and, since there is already some uncertainty in the best value of mass to use in the model, it is not worthwhile.

Triogonal Yaw Angle Increment (On-line)

Again, no correction is required for the aircraft. For the combat vehicle, corrections will be made to the actuator extensions.

Spring Constant Coefficients (Off-line). The derivative of the spring constants with respect to yaw angle were found to be zero, if symmetrical actuator spring constants are made equal. Thus, no correction is required.

Actuator Forces (On-line). These coefficients are functions of the gimbal angle and must be calculated in real time. They are given by

$$\frac{\partial f_{g}}{\partial \psi_{p}} = m \left( \frac{\partial F_{t}}{\partial \psi_{p}} \right) \left[ \frac{1}{\bar{W}(\bar{r})} \right] g_{G} - mF_{t} \left[ \frac{1}{\bar{W}(\bar{r})} \right] W \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} g_{G}$$
(277)

Since

$$W \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} g_{G} = \begin{pmatrix} -g_{y} \\ g_{x} \\ 0 \end{pmatrix}, \qquad (278)$$

$$W(\mathbf{r}) \quad W\begin{pmatrix} 0\\0\\1 \end{pmatrix} g_{G} = \begin{bmatrix} -zg_{x}\\-zg_{y}\\(xg_{x} + yg_{y}) \end{bmatrix}$$
(279)

These, plus the previously calculated values of the gravitational forces and moments, are summed according to the elements of the matrix F and its  $\psi$  - derivative to give the coefficients. The changes in actuator forces are then equal to

$$\delta \mathbf{f}_{\mathbf{n}} = \begin{pmatrix} \frac{\partial \mathbf{f}_{\mathbf{n}}}{\partial \psi_{\mathbf{p}}} \end{pmatrix} \psi_{\mathbf{p}}$$
(280)

For these calculations, the displacement, r, is equal to

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$$\mathbf{r} = \mathbf{E}_{\mathbf{H}}'\mathbf{r}_{\mathbf{V}} \tag{281}$$

as given in equation (251). Thus

$$W(\mathbf{r})W\begin{pmatrix}0\\0\\1\end{pmatrix}g_{G} = \begin{bmatrix} -(\frac{z}{v}\cos\theta_{H} + \mathbf{x}_{v}\sin\theta_{H})g_{x}\\ -(\frac{z}{v}\cos\theta_{H} + \mathbf{x}_{v}\sin\theta_{H})g_{y}\\ \mathbf{y}_{v}g_{y} + (\mathbf{x}_{v}\cos\theta_{H} - z_{v}\sin\theta_{H})g_{x} \end{bmatrix}$$
(282)

Actuator Extensions (On-line)

The actuator extensions for the combat vehicle are equal to those necessary to produce the desired yaw motion plus the gravitational extensions. The yaw inputs are

$$\delta(\Delta \ell)_{n} = \ell_{0} \{ \pm C_{1} \psi_{p} - 1/2 \ (C_{1}^{2} - C_{2}) \psi_{p}^{2} \}$$
(283)

The plus sign is used for odd numbered actuators, and the minus sign for even numbered actuators, where  $C_1$  and  $C_2$  are evaluated for actuator number one. The gravitational extensions are found by dividing the total gravitational force (results of both on-line actuator forces) by the spring constants.

$$(\Delta \ell)_{n} = \frac{\left[ f_{n} + \left( \frac{\partial f_{n}}{\partial \psi_{p}} \right) \psi_{p} \right]}{k_{n}} + \delta (\Delta \ell)_{n}$$
(284)

Evaluation of Matrices

### Calculation of Linear Coefficients

For both the off-line and on-line calculations, it is necessary to evaluate the elements of the matrices associated with the triogonal and pitch system transformations. The general configuration for the triogonal system has been presented in figure 1. The dimensions, in inches, for this are as follows:

$$a_{1} = \begin{bmatrix} 18\sqrt{3} \\ 3.0 \\ -10.0 \end{bmatrix}$$
(285)

$$\mathbf{b}_{1} = \begin{bmatrix} 13.5 \sqrt{3} \\ 31.5 \\ 9.875 \end{bmatrix}$$
(286)

$$\mathbf{r}_{\mathbf{p}} = \begin{bmatrix} \mathbf{0} \\ \mathbf{55.875} \end{bmatrix}$$
(287)

$$\ell_{1} = \begin{bmatrix} 4.5\sqrt{3} \\ -28.5 \\ 36.0 \end{bmatrix}$$
(288)

$$\ell_0 = 3\sqrt{241}$$
 (289)

For the turret adapter, whose center of rotation is 60 inches below the actuator neutral position

$$\mathbf{r}_{\mathbf{H}} = \begin{pmatrix} \mathbf{0} \\ \mathbf{0} \\ \mathbf{50.0} \end{pmatrix} \tag{290}$$

Then, the direction cosines are

$$\begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}_{1} = \frac{1}{\sqrt{241}} \begin{bmatrix} 1.5\sqrt{3} \\ -9.5 \\ 12.0 \end{bmatrix}$$
(291)

The actuator moment arms are obtained using equation (26) and are

$$\begin{pmatrix} \lambda \\ \mu \\ \nu \end{pmatrix}_{1} = \frac{1}{\sqrt{241}} \begin{bmatrix} -59.0 \\ -231\sqrt{3} \\ -175.5\sqrt{3} \end{bmatrix}$$
(292)

Then, from equation (83) the submatrices of the triogonal transformation are

$$F_{11} = \begin{bmatrix} -118 & -634 & 752 \\ -462\sqrt{3} & -290\sqrt{3} & 172\sqrt{3} \\ 175.5\sqrt{3} & 175.5\sqrt{3} & 175.5\sqrt{3} \end{bmatrix} \frac{\sqrt{241}}{12,636\sqrt{3}}$$
(293)

and

1

$$\mathbf{F}_{21} = \begin{bmatrix} 3\sqrt{3} & 11\sqrt{3} & 8\sqrt{3} \\ -19 & 5 & 14 \\ -12 & 12 & -12 \end{bmatrix} \qquad \frac{\sqrt{241}}{12,636\sqrt{3}}$$
(294)

The  $\psi_p$  - derivatives of the first column of  $F_t'$  are

$$\begin{pmatrix} \delta_1 \\ \delta_2 \\ \delta_3 \end{pmatrix} = \frac{1}{(241)} \begin{bmatrix} 22.25 \\ 890.25\sqrt{3} \\ 702\sqrt{3} \end{bmatrix}$$
(295)

and

$$\begin{pmatrix} \delta_4 \\ \delta_5 \\ \delta_6 \end{pmatrix} = \frac{1}{(241)^{3/2}} \begin{bmatrix} 11,008.5\sqrt{3} \\ -38,130.5\sqrt{3} \\ 48,006.75 \end{bmatrix}$$
(296)

The elements of the matrix

$$J = \left(\frac{\partial F'}{\partial \psi_{p}}\right) F$$
(297)

are

$$j_{11} = -\frac{11,471\sqrt{3}}{169,182}$$
(298)

$$j_{12} = \frac{38\sqrt{3}}{1053}$$
(299)

$$j_{23} = -\frac{323\sqrt{3}}{1053}$$
(300)

$$j_{16} = -\frac{34\sqrt{3}}{1053}$$
(301)

The submatrices of the  $\psi_p$  - derivative of F are

$$P_{11} = \begin{bmatrix} -.11223802 & -.25050026 & -.13826223 \\ .22445212 & -.015025086 & -.20942704 \\ .14129392 & -.14129392 & .14129392 \end{bmatrix}$$
(302)

$$P_{21} = \begin{bmatrix} -.013097284 & -.77950916 & .79260644 \\ -.90766138 & -.46517327 & .44248811 \\ .35786481 & .35786481 & .35786481 \end{bmatrix} 10^{-2}$$
(303)

For the combat vehicle, using  $A = H(\chi_{3H}, r_{H})F$  and equations (85) and (86), then

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$$\mathbf{A} = \begin{bmatrix} \frac{\{\mathbf{F}_{11} - \mathbf{W}(\mathbf{r}_{H})\mathbf{F}_{21}\}}{\mathbf{F}_{21}} & \mathbf{R}\{\mathbf{F}_{11} + \mathbf{W}(\mathbf{r}_{H})\mathbf{F}_{21}\}}{\mathbf{F}_{21}} \\ \mathbf{F}_{21} & \mathbf{F}_{21} \end{bmatrix}$$
(304)

$$W(r_{\rm H})F_{21} = \frac{\sqrt{241}}{12,636\sqrt{3}} \begin{bmatrix} 950 & -250 & -700\\ 150\sqrt{3} & 550\sqrt{3} & 400\sqrt{3}\\ 0 & 0 & 0 \end{bmatrix}$$
(305)

Then

$$A_{11} = \frac{\sqrt{241}}{12,636\sqrt{3}} \begin{bmatrix} -1068 & -384 & 1452 \\ -612\sqrt{3} & -840\sqrt{3} & -228\sqrt{3} \\ 175.5\sqrt{3} & 175.5\sqrt{3} & 175.5\sqrt{3} \end{bmatrix}$$
(306)

$$A_{21} = \frac{\sqrt{241}}{12,636\sqrt{3}} \begin{bmatrix} 3\sqrt{3} & 11\sqrt{3} & 8\sqrt{3} \\ -19 & 5 & 14 \\ -12 & 12 & -12 \end{bmatrix} = F_{21}$$
(307)

Then

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$$\left(\frac{\partial A}{\partial \theta_{\rm H}}\right)_{11} = \frac{\sqrt{241}}{12,636\sqrt{3}} \begin{bmatrix} -175.5\sqrt{3} & -175.5\sqrt{3} & -175.5\sqrt{3} \\ 0 & 0 & 0 \\ -1068 & -384 & 1452 \end{bmatrix}$$
(308)  
$$\left(\frac{\partial A}{\partial \theta_{\rm H}}\right)_{21} = \frac{\sqrt{241}}{12,636\sqrt{3}} \begin{bmatrix} 12 & -12 & 12 \\ 0 & 0 & 0 \\ 3\sqrt{3} & 11\sqrt{3} & 8\sqrt{3} \end{bmatrix}$$
(309)

$$\left(\frac{\partial K}{\partial \theta}_{H}\right)_{11} = \frac{241\sqrt{3}}{(6318)^{2}} \begin{bmatrix} 31,239 & 11,232 & -42,471 \\ 0 & 0 & 0 \\ -31,239 & -11,232 & 42,471 \end{bmatrix}$$
(310)

$$\left(\frac{\partial K}{\partial \theta_{\rm H}}\right)_{21} = \frac{241\sqrt{3}}{(6318)^2} \begin{bmatrix} 6 & 22 & 16\\ 0 & 0 & 0\\ -6 & -22 & -16 \end{bmatrix}$$
(311)

Also

$$\begin{pmatrix} \frac{\partial A}{\partial \psi_{p}} \end{pmatrix} = \begin{bmatrix} -\frac{\{P_{11} - W(r_{H})P_{21}\}}{P_{21}} & -R\{P_{11} - W(r_{H})P_{21}\} \\ P_{21} & P_{21} \end{bmatrix}$$
(312)

$$W(r_{\rm H})P_{21} = \frac{1}{\sqrt{241}} \begin{bmatrix} \frac{59,350}{8,424} & \frac{91,250}{25,272} & -\frac{86,800}{25,272} \\ \frac{4450\sqrt{3}}{75,816} & -\frac{264,850\sqrt{3}}{75,816} & \frac{269,300\sqrt{3}}{75,816} \\ 0 & 0 & 0 \end{bmatrix}$$
(313)

and

$$\left(\frac{\partial A}{\partial \psi_{p}}\right)_{11} = \frac{1}{\sqrt{241}} \begin{bmatrix} -\frac{6169}{702} & -\frac{7897}{1053} & \frac{2413}{2106} \\ \frac{13,081\sqrt{3}}{6318} & \frac{21,220\sqrt{3}}{6318} & -\frac{34,301\sqrt{3}}{6318} \\ \frac{64,009\sqrt{3}}{50,544} & -\frac{64,009\sqrt{3}}{50,544} & \frac{64,009\sqrt{3}}{50,544} \end{bmatrix}$$
(314)

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and

$$\left(\frac{\partial A}{\partial \psi_{\rm P}}\right)_{21} = \begin{bmatrix} -.013097284 & -.77950916 & .79260644 \\ -.90766138 & -.46517327 & .44248811 \\ .35786481 & .35786481 & .35786481 \end{bmatrix} 10^{-2}$$
(315)

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Then

$$\left(\frac{\partial K}{\partial \psi_{p}}\right)_{11} = \frac{1}{2106\sqrt{3}} \begin{bmatrix} \frac{1,098,082}{351} & \frac{1,010,816}{1053} & \frac{656,546}{1053} \\ -\frac{1,334,262}{351} & -\frac{2,970,800}{351} & \frac{1,303,438}{351} \\ \frac{64,009}{96} & -\frac{64,009}{96} & \frac{64,009}{96} \end{bmatrix}$$
(316)

$$\left(\frac{\partial K}{\partial \psi_{\rm p}}\right)_{21} = \frac{1}{6318\sqrt{3}} \begin{bmatrix} -\frac{89}{8424} & -\frac{58,267}{25,272} & \frac{5386}{3159} \\ \frac{22,553}{8424} & -\frac{9125}{25,272} & \frac{3038}{3159} \\ -2/3 & +2/3 & -2/3 \end{bmatrix}$$
(317)

$$K_{1} \left( \frac{\partial K_{1}}{\partial \theta_{H}} \right) = \frac{\sqrt{3}}{3,369,600} \begin{bmatrix} -9,065,807 & -3,259,616 & 12,325,423 \\ -24,416,705 & -8,779,040 & 33,195,745 \\ 19,812,112 & 7,123,456 & -26,935,568 \end{bmatrix}$$
(318)

The relatively large values in this matrix indicate that the original intention of linearizing the results for pitch variations about zero pitch angle might introduce serious errors. This led to the decision to calculate exact values for pitch angle inputs.

#### Off-Line Calculations for Aircraft

The previous evaluations of the direction cosines, moment arms, and matrix F are valid for the aircraft since they are referenced to the platform. The derivatives are not required for the aircraft configuration. The additional matrices necessary for the off-line calculations are

$$K_{1}' = \frac{9477}{800(241)} \begin{bmatrix} -57 & 54,516 & \frac{81,856}{351} \\ -55 & -183,860 & \frac{255,040}{351} \\ 112 & 129,344 & -\frac{183,296}{351} \end{bmatrix}$$
(319)

Thus

$$\begin{pmatrix} \frac{1}{k_1} \\ \frac{1}{k_2} \\ \frac{1}{k_3} \end{pmatrix} = \begin{pmatrix} \frac{1}{k_4} \\ \frac{1}{k_5} \\ \frac{1}{k_6} \end{pmatrix} = \begin{bmatrix} -1.4009050 & 1339.8551 \\ -1.3517505 & -4518.7790 & 17.85809 \\ 2.7526555 & 3178.9239 & -12.834522 \end{bmatrix} \begin{pmatrix} \frac{1}{k_x} \\ \frac{1}{k_\theta} \\ \frac{1}{k_z} \end{pmatrix}$$
(320)

The scale factors for summing gravitational components are given by equations (293) and (294).

Then
The mass loads will depend on the aircraft. For the AH-1G, we have the following values:

$$E_{H}'r_{v} = \begin{pmatrix} 0 \\ 0 \\ 37.455 \end{pmatrix}$$
(321)  
m = 24.61 lb sec<sup>2</sup>/in  
 $J_{x} = 30,360 \text{ in lb sec}^{2}$   
 $J_{y} = 140,592 \text{ in lb sec}^{2}$   
 $J_{z} = 121,968 \text{ in lb sec}^{2}$   
 $\theta_{H} = -20 \text{ degrees}$ 
(322)

Then

$$E_{H}'JE_{H} = \begin{bmatrix} -41,076 & 0 & -29,442 \\ 0 & 140,592 & 0 \\ -29,442 & 0 & 111,252 \end{bmatrix}$$
(323)

and

$$F_{11} - W(r)F_{21} = \begin{bmatrix} -.58847849 & -.3168681 & .90534657 \\ -.70564594 & -.86246023 & -.1568143 \\ .21561352 & .21561352 & .21561352 \end{bmatrix} (324)$$

The mass load submatrices are

$$(m_{g})_{11} = (m_{g})_{22} = \begin{bmatrix} 57.921932 & 10.439513 & -15.125035 \\ 10.439513 & 32.477998 & 0.6833395 \\ -15.125035 & 0.6833395 & 52.739365 \end{bmatrix}$$
 ib sec<sup>2</sup>/in (325)

$$(m_{\ell})_{12} = (m_{\ell})_{21} = \begin{bmatrix} 12.482499 & -12.412995 & -46.441314 \\ -12.412995 & -21.711075 & -2.6121869 \\ -46.441314 & -2.6121869 & 17.620422 \end{bmatrix}$$
 1b sec<sup>2</sup>/in  
(326)

60

The principal mass loads are then

$$\begin{pmatrix} m_1 \\ m_2 \\ m_3 \end{pmatrix} = \begin{pmatrix} m_4 \\ m_5 \\ m_6 \end{pmatrix} = \begin{bmatrix} 57.921932 \\ 32.477998 \\ 52.739365 \end{bmatrix}$$
 1b sec<sup>2</sup>/in (327)

The cross-mass terms have been calculated in case other than the principal values are used.

Off-Line Calculations for Combat Vehicle

The previously calculated values of  $A_{11}$  and  $A_{21}$  are valid for F, for which the displacement of the pitch system origin from the platform system origin is included. The values are given by equations (306) and (307). Thus, the equivalent moment arms at the neutral pitch system are given by substituting  $a_z = -60$  in equation (285)

$$\begin{pmatrix} \lambda \\ \mu \\ \nu \end{pmatrix} = \frac{1}{\sqrt{241}} \begin{bmatrix} -534 \\ -306\sqrt{3} \\ -175.5\sqrt{3} \end{bmatrix}$$
(328)

From equations (237), (306) and (307),  $K_{10}$  is

$$K_{10} = \frac{(241)}{3(12,636)^2} \begin{bmatrix} 1,140,624 & 147,456 & 2,108,304 \\ 361 & 25 & 196 \\ 92,400.75 & 92,400.75 & 92,400.75 \end{bmatrix}$$
(329)

The determinant of  $K_{10}$  is then

$$|K_{10}| = \frac{(241)^3(41,925)}{4(12636)^4}$$
(330)

Then, the inverse of  $K_{10}$  is given by

$$(K_{10}')_{o} = \frac{27}{259,075} \begin{bmatrix} -6,669 & 76,473,072 & -10,048 \\ -6,435 & -37,739,520 & 226,880 \\ 13,104 & -38,733,552 & -10,432 \end{bmatrix}$$
(331)

We identify

$$(K_{30}^{-})_{0} = \frac{K_{30}^{-}}{|K_{10}|}$$
(332)

Then from equation (243)

$$(K_{30}')_{0} = \begin{bmatrix} 1.4917264 & -14.360606.10^{4} & 1.4917264 \\ -9.807656 & 5.5365515.10^{4} & -9.807656 \\ -1.4965399 & .29057202.10^{4} & -1.49653399 \end{bmatrix}$$
(333)

and the actuator spring constants are

$$\kappa_{1}' = \frac{(\kappa_{10}')_{0} \{\cos^{2}\theta_{H} - \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix} \sin^{2}\theta_{H} \} + (\kappa_{30}')_{0} \sin^{2}\theta_{H}}{\{\cos^{2}\theta_{H} + \left|\frac{\kappa_{20}}{\kappa_{10}}\right| \sin^{2}\theta_{H} \}}$$
(334)

These equations are valid until

$$\tan 2\theta_{\rm H} = - \frac{|{}^{\rm K}10|}{|{}^{\rm K}20|} = + .52214737$$
(335)

or

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$$\theta_{\rm H} = + 13.8 \text{ degrees} \tag{336}$$

This is adequate to meet the 15 degree requirement.

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The coefficients which are to be calculated off-line are

$$C_{10} = 1$$
 (337)

$$\frac{C_{20}}{C_{10}} = \left|\frac{K_{20}}{K_{10}}\right| = 1.9151681$$
(338)

$$\begin{pmatrix} c_{11} \\ c_{12} \\ c_{13} \end{pmatrix} = (K_{10}')_{0} \begin{pmatrix} 1/k_{x} \\ 1/k_{\theta} \\ 1/k_{z} \end{pmatrix}$$

$$(339)$$

$$\begin{pmatrix} c_{21} \\ c_{22} \\ c_{23} \end{pmatrix} = (K_{10}')_{0} \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix} \begin{pmatrix} 1/k_{x} \\ 1/k_{\theta} \\ 1/k_{z} \end{pmatrix}$$
(340)

$$\begin{pmatrix} c_{31} \\ c_{32} \\ c_{33} \end{pmatrix} = (K_{30}')_{o} \begin{pmatrix} 1/k_{x} \\ 1/k_{\theta} \\ 1/k_{z} \end{pmatrix}$$

$$(341)$$

The gravitational loading and actuator extensions require no off-line calculations, other than the fixed values of F and  $\partial F / \partial \psi$ . The location of the vehicle CM and the weight must be input to complete these calculations. The actuator mass loading will be calculated in a manner similar to that for the aircraft, except that the mean value of pitch angle will be included. No correction will be made for variations in pitch and yaw angles. This again is a straightforward matrix multiplication using the input data describing the location of the CM and the mass and moments of inertia.

The final summary of the calculations required for the aircraft and combat vehicle configurations are then as follows:

# Aircraft

Input

Specified spring constants and axes -

 $k_u, k_v, k_w$ 

Spring constants matrix -

$$\begin{bmatrix} \frac{K_{11}}{K_{21}} \end{bmatrix} = \frac{(241)}{(12,636)^2(3)} \begin{bmatrix} 13,924 & 401,956 & 565,504 \\ 640,322 & 252,300 & 88,752 \\ 92,400.75 & 92,400.75 & 92,400.75 \\ 27 & 363 & 192 \\ 361 & 25 & 196 \\ 144 & 144 & 144 \end{bmatrix}$$
(342)

Select rows u, v, and w to form  ${\rm K}_{\rm m}$  Input  ${\rm K}_{\rm m}^{\star}$ 

Calculate

$$\left(\frac{1}{k}\right)_{\varrho} = \begin{bmatrix} 1/k_1 \\ 1/k_2 \\ 1/k_3 \end{bmatrix} = \begin{bmatrix} 1/k_4 \\ 1/k_5 \\ 1/k_6 \end{bmatrix} = \frac{1}{2} K_{m'} \begin{bmatrix} 1/k_u \\ 1/k_v \\ 1/k_w \end{bmatrix}$$
(343)

Test

$$k_n \ge k_{min} \qquad n = 1 \text{ to } 3$$
$$k_n \le k_{max} \qquad n = 1 \text{ to } 3$$

Input

Mass - m

Moments of Inertia -

$$\mathbf{r} = \mathbf{E}_{\mathrm{H}}'(\mathbf{r}_{\mathrm{H}} + \mathbf{r}_{\mathrm{v}}) = \begin{pmatrix} \mathbf{x} \\ \mathbf{y} \\ \mathbf{z} \end{pmatrix}$$
(344)

Pitch Angle -  $\theta_{\rm H}$ 

# Calculate

Mass loads -

where

$$\begin{bmatrix} F_{11} \\ F_{21} \end{bmatrix} = \frac{\sqrt{241}}{(12,636)\sqrt{3}} \begin{bmatrix} -118 & -634 & 752 \\ -462\sqrt{3} & -290\sqrt{3} & 172\sqrt{3} \\ \frac{175.5\sqrt{3}}{3\sqrt{3}} & \frac{175.5\sqrt{3}}{11\sqrt{3}} & \frac{175.5\sqrt{3}}{8\sqrt{3}} \\ -19 & 5 & 14 \\ -12 & 12 & -12 \end{bmatrix}$$
(346)

Input

Gimbal Angles - (On-line)  $\psi_{G}, \theta_{G}$ 

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Calculate (On-line)

$$g_{G} = \begin{pmatrix} g_{x} \\ g_{y} \\ g_{z} \end{pmatrix} = g \begin{bmatrix} -\cos\psi_{G} \sin\theta_{G} \\ \sin\psi_{G} \sin\theta_{G} \\ \cos\theta_{G} \end{bmatrix}$$
(347)

$$\mathbf{m}_{\mathbf{G}} = \begin{pmatrix} \mathbf{g}_{\phi} \\ \mathbf{g}_{\theta} \\ \mathbf{g}_{\psi} \end{pmatrix} = \begin{bmatrix} \mathbf{y}\mathbf{g}_{\mathbf{z}} - \mathbf{z}\mathbf{g}_{\mathbf{y}} \\ \mathbf{z}\mathbf{g}_{\mathbf{x}} - \mathbf{x}\mathbf{g}_{\mathbf{z}} \\ \mathbf{x}\mathbf{g}_{\mathbf{y}} - \mathbf{y}\mathbf{g}_{\mathbf{x}} \end{bmatrix}$$
(348)

$$f_{\mathfrak{g}} = \begin{bmatrix} f_{1} \\ f_{2} \\ f_{3} \\ f_{4} \\ f_{5} \\ f_{6} \end{bmatrix} = m \begin{bmatrix} F_{11t} \\ F_{11t}^{R} \\ F_{-F_{21t}^{R}} \end{bmatrix} \begin{pmatrix} g_{G} \\ \overline{m}_{G} \end{pmatrix}$$
(349)

$$(\Delta \ell)_{n} = \frac{f}{k_{n}} \qquad n = 1 \text{ to } 6 \qquad (350)$$

Combat Vehicle

Input

Specified spring constants and axes -

 $k_u$ ,  $k_v$ , and  $k_w$ 

Spring constant coefficients -

$$(C_q)_{mn}$$
 q = 1 to 5  
m = 1 to 3  
n = 1 to 3

Calculate

$$d_{mn} = (C_n)_{1m} (\frac{1}{k_u}) + (C_n)_{2m} (\frac{1}{k_v}) + (C_n)_{3m} (\frac{1}{k_w})$$

$$n = 1 \text{ to } 5$$

$$m = 1 \text{ to } 3$$
(351)

Input

```
Pitch Angle - (On-line)
\theta_{\rm H}
C_{\rm mo} m = 1 to 5
```

Calculate

$$|\kappa| = \{C_{10} \cos^{4} \theta_{H} + C_{20} \cos^{3} \theta_{H} \sin \theta_{H} + C_{30} \cos^{2} \theta_{H} \sin^{2} \theta_{H} + C_{40} \cos \theta_{H} \sin^{3} \theta_{H} + C_{50} \sin^{4} \theta_{H}\}$$
(352)

$$\frac{1}{k_{n}} = \frac{1}{2|K|} \{ d_{n1} \cos^{4} \theta_{H} + d_{n2} \cos^{3} \theta_{H} \sin \theta_{H} + d_{n3} \cos^{2} \theta_{H} \sin^{2} \theta_{H} + d_{n4} \cos \theta_{H} \sin^{3} \theta_{H} + d_{n5} \sin^{4} \theta_{H} \}$$

$$+ d_{n5} \sin^{4} \theta_{H} \}$$

$$n = 1 \text{ to } 3$$
(353)

(354)

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$$k_{n+3} = k_n$$

Test

 $k_{n} \ge k_{min} \qquad n = 1 \text{ to } 3$  $k_{n} \le k_{max} \qquad n = 1 \text{ to } 3$ 

Input

Mass - m

Moments of Inertia -

$$J_{xx}$$
,  $J_{yy}$ ,  $J_{zz}$ ,  $J_{xy}$ ,  $J_{xz}$ ,  $J_{yz}$ 

Displacement of CM

$$\mathbf{r}_{\mathbf{v}} = \begin{pmatrix} \mathbf{x}_{\mathbf{v}} \\ \mathbf{y}_{\mathbf{v}} \\ \mathbf{z}_{\mathbf{v}} \end{pmatrix}$$

Mean pitch angle -  $\theta_{Ho}$ 

Calculate

$$\mathbf{r}_{o} = \begin{bmatrix} \mathbf{x}_{v} \cos\theta_{Ho} + \mathbf{z}_{v} \sin\theta_{Ho} \\ \mathbf{y}_{v} \\ \mathbf{z}_{v} \cos\theta_{Ho} - \mathbf{x}_{v} \sin\theta_{Ho} \end{bmatrix} = \begin{pmatrix} \mathbf{x}_{o} \\ \mathbf{y}_{o} \\ \mathbf{z}_{o} \end{pmatrix}$$
(355)

$$m_{\chi} = \begin{bmatrix} F_{11t} & | & F_{21t} \\ F_{11t} & | & -F_{21t} & \\ \end{bmatrix} \begin{bmatrix} 1 \\ W(r_{o}) & | & 1 \end{bmatrix} \begin{bmatrix} -m \\ 0 & | & -W_{Ho} \end{bmatrix} \times \begin{bmatrix} 1 \\ W(r_{o}) & | & 1 \end{bmatrix} \begin{bmatrix} F_{11} & | & RF_{Ho} \\ F_{21} & | & -RF_{21} \end{bmatrix}$$
(356)

where

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$$\begin{bmatrix} F_{11} \\ F_{21} \end{bmatrix} = \begin{bmatrix} -1068 & -384 & 1452 \\ -612\sqrt{31} & -840\sqrt{3} & -228\sqrt{3} \\ 175.5\sqrt{3} & 175.5\sqrt{3} & 175.5\sqrt{3} \\ 3\sqrt{3} & 11\sqrt{3} & 8\sqrt{3} \\ -19 & 5 & 14 \\ -12 & 12 & -12 \end{bmatrix} \frac{\sqrt{241}}{(12,636)\sqrt{3}}$$
(357)

Input

θ<sub>G</sub>, ψ<sub>G</sub>

Triogonal Yaw Angle - (On-line)

Ψp

Calculate (On-line)

$$\mathbf{r} = \begin{pmatrix} \mathbf{x} \\ \mathbf{y} \\ \mathbf{z} \end{pmatrix} = \begin{bmatrix} \mathbf{x} \\ \mathbf{v} \\ \mathbf{v} \\ \mathbf{y} \\ \mathbf{v} \\ \mathbf{z} \\ \mathbf{v} \\ \mathbf$$

$$\mathbf{g}_{\mathbf{G}} = \begin{pmatrix} \mathbf{g}_{\mathbf{x}} \\ \mathbf{g}_{\mathbf{y}} \\ \mathbf{g}_{\mathbf{z}} \end{pmatrix} = \mathbf{g} \begin{bmatrix} -\cos\psi_{\mathbf{G}}\sin\theta_{\mathbf{G}} \\ \sin\psi_{\mathbf{G}}\sin\theta_{\mathbf{G}} \\ \cos\theta_{\mathbf{G}} \end{bmatrix}$$
(359)

$$\mathbf{m}_{\mathbf{G}} = \begin{pmatrix} \mathbf{g}_{\phi} \\ \mathbf{g}_{\theta} \\ \mathbf{g}_{\psi} \end{pmatrix} = \begin{bmatrix} \mathbf{y}\mathbf{g}_{\mathbf{z}} - \mathbf{z}\mathbf{g}_{\mathbf{y}} \\ \mathbf{z}\mathbf{g}_{\mathbf{x}} - \mathbf{x}\mathbf{g}_{\mathbf{z}} \\ \mathbf{x}\mathbf{g}_{\mathbf{y}} - \mathbf{y}\mathbf{g}_{\mathbf{x}} \end{bmatrix}$$
(360)

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$$\frac{\partial f_{\ell}}{\partial \psi_{p}} = m \left( \frac{\partial F_{t}}{\partial \psi_{p}} \right) \left( \frac{g_{C}}{m_{C}} \right) +$$

$$+ m \left[ \frac{F_{11t}}{F_{11t}} + \frac{F_{21t}}{F_{11t}} - F_{21t} R \right] \left[ \frac{g_{y}}{-g_{x}} - \frac{g_{y}}{-g_{y}} -$$

Where

$$\frac{\partial \mathbf{F}_{t}}{\partial \psi_{p}} = \begin{bmatrix} \mathbf{P}_{11t} & \mathbf{P}_{21t} \\ -\mathbf{P}_{11t}^{R} & \mathbf{P}_{21t}^{R} \end{bmatrix}$$
(362)

$$\begin{bmatrix} P_{11} \\ P_{21} \end{bmatrix} = \begin{bmatrix} -1, 332, 504 & -1, 137, 168 & 195, 336 \\ 313, 944\sqrt{3} & 509, 280\sqrt{3} & -823, 224\sqrt{3} \\ \underline{192, 027\sqrt{3}} & -192, 027\sqrt{3} & 192, 027\sqrt{3} \\ -178\sqrt{3} & -10, 594\sqrt{3} & 10, 722\sqrt{3} \\ -21, 366 & -10, 950 & 10, 416 \\ 8, 424 & 8, 424 & 8, 424 \\ x & \underline{1} \\ 151, 632\sqrt{241} \end{bmatrix}$$
(363)

$$\mathbf{f}_{\boldsymbol{\ell}} = \mathbf{m} \left[ \frac{\mathbf{F}_{11t}}{\mathbf{F}_{11t}} \frac{|}{|} \frac{\mathbf{F}_{21t}}{-\mathbf{F}_{21t}} \right] \left( \frac{\mathbf{g}_{\mathbf{C}}}{\mathbf{m}_{\mathbf{G}}} \right) + \psi_{\mathbf{p}} \left( \frac{\partial \mathbf{f}_{\boldsymbol{\ell}}}{\partial \psi_{\mathbf{p}}} \right)$$
(364)

$$(\Delta \ell)_{n} = \frac{f}{k}_{n} \qquad n = 1 \text{ to } 6 \qquad (365)$$

Table of Symbols

$$\begin{aligned} \mathbf{x}_1 &= \begin{pmatrix} \mathbf{x} \\ \mathbf{y} \\ \mathbf{z} \end{pmatrix} & \text{linear position vector} \\ \mathbf{x}_3 &= \begin{pmatrix} \phi \\ \theta \\ \psi \end{pmatrix} & \text{angular position vector} \begin{pmatrix} \text{relative} \\ \text{Euler angles} \end{pmatrix} \\ \dot{\mathbf{x}}_2 &= \begin{pmatrix} \mathbf{p} \\ \mathbf{q} \\ \mathbf{r} \end{pmatrix} & \text{angular velocity vector} \end{aligned}$$

x = displacement in direction of x-axis

y = displacement in direction of y-axis

z = displacement in direction of z-axis

- $\phi$  = roll angle
- $\theta$  = pitch angle
- $\psi$  = yaw angle
- p = roll velocity
- q = pitch velocity
- r = yaw velocity

$$\begin{aligned} \mathbf{x}_{2} &= \mathbf{C}^{\circ} \left( \mathbf{x}_{3} \right) \mathbf{x}_{3} \\ \mathbf{G}^{\circ} \left( \mathbf{x}_{3} \right) = \begin{bmatrix} 1 & 0 & -\sin \theta \\ 0 & \cos \phi & \sin \phi & \cos \theta \\ 0 & -\sin \phi & \cos \phi & \cos \theta \end{bmatrix} \\ \mathbf{G} &= & \text{subscript denoting gimbal system} \\ \mathbf{p} &= & \text{subscript denoting platform system} \\ \mathbf{k} &= & \text{subscript denoting actuator number} \\ \mathbf{a} &= & \text{subscript denoting aircraft system} \\ \mathbf{H} &= & \text{subscript denoting pitch actuator system} \\ \mathbf{W} &= & \text{subscript denoting tail-boom system, relative} \\ \mathbf{v} &= & \text{subscript denoting tail-boom system, relative} \\ \text{to aircraft system} \\ \mathbf{TB} &= & \text{subscript denoting tail-boom system, relative} \\ \mathbf{t} &= & \text{subscript denoting transpose} \\ \mathbf{t} &= & \text{subscript denoting transpose} \\ \mathbf{E}_{1}(\psi) &= \begin{bmatrix} \cos \psi & \sin \psi & 0 \\ -\sin \psi & \cos \psi & 0 \\ 0 & 0 & 1 \end{bmatrix} \\ &= & \text{pitch transformation} \\ \frac{1}{\sin \theta} & 0 & \cos \theta \end{bmatrix} = \text{pitch transformation} \\ \mathbf{E}_{3}(\phi) &= \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \phi & \sin \phi \\ 0 & -\sin \phi & \cos \phi \end{bmatrix} \\ &= & \text{roll transformation} \\ \frac{1}{\text{matrix}} \end{aligned}$$

 $E(x_3) = E_3(\phi)E_2(\theta)E_1(\psi) = angular transformation matrix$ 

$$b = \begin{pmatrix} b_x \\ b_y \\ b_z \end{pmatrix} = \text{location of upper end of actuator}$$

$$a = \begin{pmatrix} a_x \\ a_y \\ a_z \end{pmatrix} = 1 \text{ ocation of lower end of actuator}$$

$$\mathbf{r} = \begin{pmatrix} \mathbf{r} \\ \mathbf{x} \\ \mathbf{r} \\ \mathbf{y} \\ \mathbf{r} \\ \mathbf{z} \end{pmatrix} = \begin{array}{c} \text{vector displacement of origin of one} \\ \text{coordinate system from origin of another} \\ \text{coordinate system} \end{array}$$

$$\ell_{p} = \begin{pmatrix} \ell_{x} \\ \ell_{y} \\ \ell_{z} \end{pmatrix} = \text{vector length of actuator}$$

l = scalar length of actuator

 $l_i$  = unextended scalar length of actuator

$$\alpha = \frac{l_x}{l} = x - \text{direction cosine of actuator}$$

$$\beta = \frac{x_y}{k} = y - \text{direction cosine of actuator}$$

$$\gamma = \frac{l}{l} = z - \text{direction cosine of actuator}$$

$$W(x_1) = \begin{bmatrix} 0 & -z & y \\ z & 0 & -x \\ -y & x & 0 \end{bmatrix} = rotational matrix$$

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$$\begin{pmatrix} \dot{x}_{1} \\ -\frac{1}{x}_{2} \end{pmatrix} = \begin{pmatrix} \dot{x} \\ \dot{y} \\ \dot{z} \\ p \\ q \\ r \end{pmatrix} = \text{ velocity matrix}$$

$$\left(-\frac{f}{m}-\right) = \begin{pmatrix} f_{x} \\ f_{y} \\ f_{z} \\ m_{\phi} \\ m_{\theta} \\ m_{\psi} \end{pmatrix} = \text{force matrix}$$

$$\begin{pmatrix} \dot{x}_1 \\ - \dot{x}_2 \\ \dot{x}_2 \end{pmatrix}_p = F \hat{l} = triogonal velocity transformation$$

$$\begin{pmatrix} \lambda \\ \mu \\ \nu \end{pmatrix} = W(a) \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix} = \text{ actuator moment arms}$$

$$f_{pn} = \begin{pmatrix} f_x \\ f_y \\ f_z \\ f_z \end{pmatrix} = \text{vector actuator force (n-th actuator)}$$

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 $f_n = scalor actuator force (n-th actuator)$ 

$$f_{\ell} = \begin{pmatrix} f_1 \\ f_2 \\ f_3 \\ f_4 \\ f_5 \\ f_6 \end{pmatrix} = \text{ scalar actuator force matrix}$$

$$\begin{bmatrix} \mathbf{f}_{1} & 0 & \cdot & 0 \\ 0 & \mathbf{f}_{2} & \cdot & \cdot \\ \cdot & & \cdot & \cdot \\ 0 & 0 & \cdot & \mathbf{f}_{6} \end{bmatrix}$$

= diagonal actuator force matrix

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$$H(x_{3},r) = \begin{bmatrix} E(x_{3}) & -W(r) & E(x_{3}) \\ - & - & - & - & - & - \\ 0 & E(x_{3}) \end{bmatrix} = \text{rectilinear velocity} \text{transformation matrix}$$

$$\begin{pmatrix} \dot{x}_1 \\ \dot{x}_2 \end{pmatrix}$$
 = Z  $\begin{pmatrix} -\frac{f}{m} \end{pmatrix}$  = generalized impedance matrix

$$k_n$$
 = spring constant of n-th actuator

$$\begin{pmatrix} \frac{1}{k} \\ \frac{1}{k} \end{pmatrix}_{l} = \begin{bmatrix} \frac{1/k_{1}}{1/k_{2}} \\ \vdots \\ \vdots \\ \frac{1/k_{6}}{1/k_{6}} \end{bmatrix} = \text{actuator spring constant matrix}$$

$$\begin{split} \mathbf{L}_{\underline{k}} &= \begin{bmatrix} 1/k_1 & 0 & \cdots & 0 \\ 0 & 1/k_2 & \cdots & \vdots \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \cdots & 1/k_{\underline{6}} \end{bmatrix} = & \text{diagonal actuator spring constant matrix} \\ \begin{pmatrix} \frac{1}{k} \end{pmatrix}_{p} &= \begin{bmatrix} 1/k_{\mathbf{x}} \\ 1/k_{\mathbf{y}} \\ 1/k_{\mathbf{y}} \\ 1/k_{\mathbf{y}} \\ 1/k_{\mathbf{y}} \\ 1/k_{\mathbf{y}} \\ 1/k_{\mathbf{y}} \end{bmatrix} = & \text{platform spring constant matrix} \\ \begin{pmatrix} \frac{1}{k} \end{pmatrix}_{p} &= K\left(\frac{1}{k}\right)_{\underline{k}} &= & \text{spring constant transformation} \\ \frac{1}{k} \end{pmatrix}_{p} &= K\left(\frac{1}{k}\right)_{\underline{k}} &= & \text{spring constant transformation} \\ \begin{bmatrix} a_{11}^{2} & a_{12}^{2} & \cdots & a_{16}^{2} \\ a_{21}^{2} & a_{22}^{2} & \cdots \\ \vdots & \vdots & \vdots \\ a_{61}^{2} & \cdots & a_{66}^{2} \end{bmatrix} \\ A &= & H(\mathbf{x}_{3\mathbf{v}, \mathbf{r}_{\mathbf{v}}})H(\mathbf{x}_{3\mathbf{H}, \mathbf{r}_{\mathbf{H}}})F \\ &= & \text{velocity transformation from triogonal system to} \\ \mathbf{g} &= & \text{gravitational constant = 386 in/sec}^{2} \\ \mathbf{g}_{e} &= \begin{pmatrix} 0 \\ 0 \\ g \end{pmatrix} &= & \text{gravitational vector in earth coordinates.} \end{split}$$

$$\Delta l = \begin{pmatrix} \Delta l \\ \Delta l \\ 2 \\ \vdots \\ \vdots \\ \Delta l \\ 6 \end{pmatrix} = \text{actuator extension due to gravity}$$

m = mass of vehicle

$$J = \begin{bmatrix} J_{xx} & J_{xy} & J_{xz} \\ J_{xy} & J_{yy} & J_{yz} \\ J_{xz} & J_{yz} & J_{zz} \end{bmatrix} = moment of inertia matrix of vehicle$$

$$m = \begin{bmatrix} m & 0 & 0 \\ 0 & m & 0 \\ 0 & 0 & m \end{bmatrix} = mass matrix of vehicle$$

$$\mathbf{m}_{\mathbf{v}} = \begin{bmatrix} \mathbf{m} & \mathbf{0} \\ -\mathbf{-} - \mathbf{l} - \mathbf{-} \\ \mathbf{0} & \mathbf{J} \end{bmatrix} = \text{ inertia matrix of vehicle}$$

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 $m_{\ell}$  = effective inertia matrix seen by actuators

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Identities

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$$E'(x_{3}) = E_{t}(x_{3})$$
  

$$\dot{E}(x_{3}) = -W(\dot{x}_{2})E(x_{3})$$
  

$$\dot{E}'(x_{3}) = E'(x_{3})W(\dot{x}_{2})$$
  

$$E(x_{3})W(r)E'(x_{3}) = W(E(x_{3})r)$$
  

$$W_{t}(r) = -W(r)$$



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System Dynamics

## Aircraft

Aircraft Acceleration. The external forces and moments acting on the aircraft produce accelerations as follows:

$$\left(\frac{f}{m}\right)_{a} = \frac{\partial}{\partial t} \left\{ \begin{cases} m_{a} \left(\frac{x_{1}}{x_{2}}\right)_{a} \end{cases} -m_{a} \left[\frac{E(x_{3}) g_{e}}{-\frac{3}{0} - \frac{3}{0}}\right] \right\}$$
(366)

Where the aircraft velocities are measured in the aircraft coordinate system, relative to earth. After carrying out the differentiation, this is equivalent to

$$\begin{pmatrix} \underline{f} \\ \underline{m} \end{pmatrix}_{a} = m_{a} \begin{pmatrix} \dot{\mathbf{x}} \\ -\frac{1}{\mathbf{x}_{2}} \\ a \end{pmatrix}_{a} + \begin{bmatrix} \underline{W}(\dot{\mathbf{x}}_{2a}) & \mathbf{0} \\ -\overline{W}(\dot{\mathbf{x}}_{2a}) \end{bmatrix} m_{a} \begin{pmatrix} \dot{\mathbf{x}}_{1} \\ -\frac{1}{\mathbf{x}_{2}} \\ a \end{bmatrix} - m_{a} \begin{bmatrix} \underline{E}(\mathbf{x}_{3}) & \underline{g}_{e} \\ 0 \end{bmatrix}$$
(367)

The external forces acting on the aircraft and through the triogonal system, the tail boom forces, and the weapon forces are

$$\left(-\frac{f}{m}\right)_{a} = \left\{ \left(\frac{f}{m}\right)_{p} + \left(\frac{f}{m}\right)_{TB} + \left(\frac{f}{m}\right)_{w} \right\}_{a}$$
(368)

If the tail boom forces are applied to the aircraft about a coordinate system (fixed to the aircraft) defined by

$$x_{1B} = E(x_{3B}) x_{1a} - r_B$$
 (369)

the tail boom forces, referred to the aircraft c.g., are

$$\left(\frac{f}{m}\right)_{a,B} = H_t \left(x_{3B}, r_B\right) \left(\frac{f}{m}\right)_B$$
(370)

The velocities are related by

$$\begin{pmatrix} \dot{\mathbf{x}}_{1} \\ \bar{\mathbf{x}}_{2} \end{pmatrix}_{B} = H(\mathbf{x}_{3B}, \mathbf{r}_{B}) \begin{pmatrix} \dot{\mathbf{x}}_{1} \\ \bar{\mathbf{x}}_{2} \end{pmatrix}_{a}$$
(371)

The forces exerted by the platform on the aircraft, referred to the aircraft  $c \cdot g \cdot$ , are

$$\left(\frac{f}{m}\right)_{a,p} = H_{t} \left(x_{3a}, r_{a}\right) \left(\frac{f}{m}\right)_{p}$$
(372)

The weapon forces, referred to the aircraft c.g., are

$$\begin{pmatrix} \underline{f} \\ \underline{m} \end{pmatrix}_{a,w} = H_t (x_{3T}, r_T) H_t (x_{3w}, r_w) (\frac{f}{\underline{m}})$$

$$w \qquad (373)$$

Thus, the external forces acting on the aircraft are

$$\left(\frac{f}{m}\right)_{a} = H_{t}^{\prime}(x_{3a}, r_{a}) \left(\frac{f}{m}\right)_{p} + H_{t}^{\prime}(x_{3B}, r_{B}) \left(\frac{f}{m}\right)_{B}$$

$$+ H_{t}^{\prime}(x_{3T}, r_{T}) H_{t}^{\prime}(x_{3w}, r_{w}) \left(\frac{f}{m}\right)_{w}$$

$$(374)$$

These, plus the gravitational force, must be equal to the rate of change of momentum as given before.

The velocity of the aircraft is equal to the relative velocity between the platform and gimbal systems plus the velocity of the gimbal system all referenced to the aircraft coordinate system. The platform velocity is

$$\begin{pmatrix} \dot{\mathbf{x}}_{1} \\ \dot{\mathbf{x}}_{2} \end{pmatrix}_{\mathbf{p}} = H(\mathbf{x}_{3\mathbf{p}}, \mathbf{r}_{\mathbf{p}}) \begin{pmatrix} \dot{\mathbf{x}}_{1} \\ \dot{\mathbf{x}}_{2} \end{pmatrix}_{\mathbf{G}} + \begin{pmatrix} \dot{\mathbf{x}}_{1} \\ \dot{\mathbf{x}}_{2} \end{pmatrix}_{\mathbf{p}/\mathbf{G}}$$
(375)

where

 $\begin{pmatrix} x_1 \\ \hline x_2 \\ y/g \end{pmatrix}$  is the platform velocity, relative to the gimbal system.

That is

$$\begin{pmatrix} \dot{\mathbf{x}}_{1} \\ \ddot{\mathbf{x}}_{2} \end{pmatrix}_{\mathbf{p}/\mathbf{G}} = \mathbf{F} \cdot \dot{\mathbf{g}}$$
(376)

Referred to the aircraft c.g., this is

$$\begin{pmatrix} \dot{\mathbf{x}}_{1} \\ \dot{\bar{\mathbf{x}}}_{2} \end{pmatrix}_{a} = H(\mathbf{x}_{3a}, \mathbf{r}_{a}) \left\{ H(\mathbf{x}_{3p}, \mathbf{r}_{p}) \begin{pmatrix} \dot{\mathbf{x}}_{1} \\ \dot{\mathbf{x}}_{2} \end{pmatrix}_{G} + F \cdot \hat{\mathbf{y}} \right\}$$
(377)

The reaction force of the tail boom actuator is applied to the gimbal system through the transformation linking the tail boom system to the gimbal system. Since

$$x_{1B} = E(x_{3B}) x_{1a} - r_B$$
 (378)

$$x_{1a} = E(x_{3a}) x_{1p} - r_a$$
 (379)

$$x_{1p} = E(x_{3p}) x_{1G} - r_p$$
 (380)

it follows that

$$\mathbf{x}_{1B} = E(\mathbf{x}_{3B}) E(\mathbf{x}_{3a}) E(\mathbf{x}_{3p}) \cdot \mathbf{x}_{1G}$$
  
-  $\left\{ E(\mathbf{x}_{3B}) E(\mathbf{x}_{3a}) \mathbf{r}_{p} + E(\mathbf{x}_{3B}) \mathbf{r}_{a} + \mathbf{r}_{B} \right\}$  (381)

Thus

$$E(x_{3TB}) = E(x_{3B}) E(x_{3a}) E(x_{3p})$$
 (382)

and

$$r_{TB} = \left\{ E(x_{3B}) E(x_{3a}) r_{p} + E(x_{3B}) r_{a} + r_{B} \right\}$$
 (383)

The forces applied to the gimbal system, by the tail boom actuator are then

$$\left(\frac{f}{m}\right)_{G,TB} = H_t(x_{3TB}, r_{TB}) \quad \left(\frac{f}{m}\right)_B$$
(384)

The total force applied to (and supplied by) the gimbal system is then

$$\begin{pmatrix} \underline{f} \\ \underline{m} \end{pmatrix}_{G} = H_{t} (\mathbf{x}_{3TB}, \mathbf{r}_{TB}) \left( \frac{\underline{f}}{\underline{m}} \right)_{B} + H_{t} (\mathbf{x}_{3p}, \mathbf{r}_{p}) \left( \frac{\underline{f}}{\underline{m}} \right)_{p}$$
(385)

But, since

$$\left(\frac{f}{m}\right)_{p} = F_{t} \cdot f_{\ell}$$
(386)

This is equal to

$$\left(\frac{f}{m}\right)_{G} = H_{t} \left(x_{3TB}, r_{TB}\right) \left(\frac{f}{m}\right)_{B} + H_{t} \left(x_{3p}, r_{p}\right) f_{t} f_{\ell}$$
(387)

The final relationship required is that for the tail boom force. It is assumed that this is applied along the aircraft y axis, through the origin of the tail boom system. Then

$$\left(\frac{f}{m}\right)_{TB} = \begin{bmatrix} 0\\f_{y}\\0\\0\\0\\0\end{bmatrix}_{TB}$$
(388)

Also, the force is proportioned to the aircraft yaw acceleration

$$\begin{pmatrix} \mathbf{f}_{\mathbf{y}} \end{pmatrix}_{\mathbf{TB}} = - \frac{\Delta \mathbf{J}_{\mathbf{z}}}{(\mathbf{r}_{\mathbf{TB}})} \left[ \begin{array}{c} \mathbf{0} \\ \mathbf{0} \\ \mathbf{0} \\ \mathbf{0} \\ \mathbf{1} \end{array} \right]_{\mathbf{t}} \left[ \begin{array}{c} \frac{\partial}{\partial \mathbf{t}} & \left( \frac{\mathbf{x}_{1}}{\mathbf{x}_{2}} \right) \\ \frac{\partial}{\partial \mathbf{t}} & \left( \frac{\mathbf{x}_{1}}{\mathbf{x}_{2}} \right) \\ \mathbf{t} \end{array} \right]$$

$$(389)$$

This can be evaluated as

$$(\mathbf{f}_{\mathbf{y}})_{\mathbf{TB}} = -\frac{\Delta \mathbf{J}_{\mathbf{z}}}{(\mathbf{r}_{\mathbf{TB}})_{\mathbf{x}}} \begin{bmatrix} \mathbf{\dot{r}} + \mathbf{p}\mathbf{\dot{y}} - \mathbf{q} \mathbf{\dot{x}} \\ \mathbf{\dot{r}} + \mathbf{p}\mathbf{\dot{y}} - \mathbf{q} \mathbf{\dot{x}} \end{bmatrix}_{\mathbf{a}}$$
(390)

where

$$\dot{x}_{2a} = \begin{pmatrix} p \\ q \\ r \end{pmatrix}$$
(391)

Interaction of systems. The gimbal, triogonal, and tail boom systems are interconnected through the dynamics of the system. The mutual coupling terms can be derived by writing the expression for the output values in terms of the input values. That is

$$\left[\left(\frac{f}{m}\right)_{G}, f_{\chi}\right] = f\left[\left(\frac{\dot{x}_{1}}{\dot{x}_{2}}\right)_{G}, \dot{\chi}, \left(-\frac{f}{m}\right)_{W}, \left(-\frac{f}{m}\right)_{TB}, g\right]$$
(392)

By combining the equations listed previously, the output quantities are the gimbal forces,

$$\begin{pmatrix} \underline{f} \\ \underline{m} \end{pmatrix}_{G} = H_{P_{t}} H_{a_{t}} \frac{\partial}{\partial t} \left\{ m_{a} H_{a} H_{p} \left( \frac{\dot{x}_{1}}{\dot{x}_{2}} \right)_{G} \right\}$$

$$+ H_{P_{t}} H_{a_{t}} \frac{\partial}{\partial t} \left\{ m_{a} H_{a} F \dot{z} \right\}$$

$$- H_{P_{t}} H_{a_{t}} H_{T_{t}} H_{w_{t}} \left( \frac{f}{m} \right)_{w}$$

$$- H_{P_{t}} H_{a_{t}} m_{a} \left[ \frac{E(x_{3})}{0} \frac{g_{e}}{-0} \right]$$

$$(393)$$

the actuator forces,

$$f_{\chi} = F_{t} H_{a_{t}} \frac{\theta}{\partial t} \left\{ m_{a} H_{a} H_{p} \left( -\frac{\dot{x}_{1}}{\dot{x}_{2}} \right)_{G} \right\}$$

$$+ F_{t} H_{a_{t}} \frac{\partial}{\partial t} \left\{ m_{a} H_{a} F \dot{x} \right\}$$

$$- F_{t} H_{a_{t}} H_{B_{t}} \left( \frac{f}{m} \right)_{TB}$$

$$- F_{t} H_{a_{t}} H_{T_{t}} H_{w_{t}} \left( -\frac{f}{m} \right)_{w}$$

$$- F_{t} H_{a_{t}} m_{a} \left[ -\frac{F(x_{3})}{0} - \frac{g_{e}}{0} \right] \qquad (394)$$

and the tail boom actuator velocity

$$\begin{pmatrix} \mathbf{x}_{1} \\ \mathbf{x}_{2} \end{pmatrix}_{B,a/G} = \mathbf{H}_{B}\mathbf{H}_{a}\mathbf{F}\mathbf{L}$$
(395)

The values of inertia used in the matrix,  $m_a$ , in these equations are the actual values, since the inertia augmentation loop has not been closed. The tail boom force is given by

$$\begin{pmatrix} -\frac{f}{m} \end{pmatrix}_{TB} = -\frac{\Delta J}{(r_{TB})_{x}} \begin{bmatrix} 0\\0\\0\\0\\1 \end{bmatrix}_{t} \frac{\partial}{\partial t} \begin{pmatrix} \mathbf{x}_{1}\\\mathbf{x}_{2} \end{pmatrix}_{a}$$

$$(396)$$

The aircraft velocities,  $\begin{pmatrix} \cdot \\ x_1 \\ - \cdot \\ x_2 \end{pmatrix}_a$ , must be determined from the total system

response, not just the external system, as represented by the dynamic equations which makes it necessary to add the feedback loops and actuator output impedances. For the triogonal actuators, this includes the spring rate simulation  $L_g$ , and for the tail boom actuator, the aircraft yaw acceleration feedback as previously stated. For all actuators, it includes the compressibility and leakage components of the output impedance.

The first two terms of the force equations for the gimbal and triogonal systems represent the inertia effect of the load (acceleration and gyroscopic effects). The third term of the triogonal force equation is the inertia augmentation force, and since it is derived from the aircraft acceleration, it can be lumped into the inertia term by modifying the yaw moment of inertia. The last two terms of each give the response to the weapon and gravitational force inputs, respectively.

The tail boom actuator velocity is determined entirely by the motion of the triogonal system, since it is the only movable link coupling the two ends of the tail boom actuator.

Evaluation of the cross-coupling terms among the gimbal, triogonal, and tail boom systems can be accomplished by performing the indicated differentation of the momentum terms. Because of the highly nonlinear nature of the solution, the values will depend on the instantaneous velocities of the various parts of the system. The derivatives of the impedance transformation matrices have been evaluated for determining the linear coefficients, so that these can be used directly for numerical evaluation of the cross-coupling terms.

If it is assumed that the mass and aircraft transformation matrices are invariant, the two time derivatives are equal to

$$\frac{\partial}{\partial \mathbf{r}} \left\{ \begin{array}{c} \mathbf{m}_{H} \mathbf{H}_{\mathbf{a}} \mathbf{m}_{\mathbf{a}} \mathbf{p} \begin{pmatrix} \mathbf{x}_{1} \\ -\mathbf{x}_{2} \end{pmatrix}_{\mathbf{G}} \right\}$$

$$= \frac{\mathbf{m}_{H} \mathbf{H}_{\mathbf{a}} \mathbf{m}_{\mathbf{a}} \mathbf{p} \left\{ \begin{pmatrix} \mathbf{x}_{1} \\ -\mathbf{x}_{2} \end{pmatrix}_{\mathbf{G}} + \begin{bmatrix} \mathbf{W}(\mathbf{x}_{2G}) & \mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} & \mathbf{H}_{\mathbf{G}} \end{bmatrix} \begin{pmatrix} \mathbf{x}_{1} \\ -\mathbf{H}_{\mathbf{G}} & \mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} & \mathbf{H}_{\mathbf{G}} \end{bmatrix} \left\{ \begin{pmatrix} \mathbf{x}_{1} \\ -\mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} \end{pmatrix}_{\mathbf{G}} + \begin{bmatrix} \mathbf{W}(\mathbf{x}_{2G}) & \mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} & \mathbf{H}_{\mathbf{G}} \end{bmatrix} \begin{pmatrix} \mathbf{x}_{1} \\ -\mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} \end{pmatrix}_{\mathbf{G}} + \begin{bmatrix} \mathbf{W}(\mathbf{x}_{2G}) & \mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} & \mathbf{H}_{\mathbf{G}} \end{bmatrix} \begin{bmatrix} \mathbf{W}(\mathbf{x}_{2D}) & \mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} & \mathbf{H}_{\mathbf{G}} \end{bmatrix} \begin{bmatrix} \mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} \end{bmatrix} \\ -\mathbf{H}_{\mathbf{G}} & \mathbf{H}_{\mathbf{G}} \end{bmatrix} \begin{bmatrix} \mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} \end{bmatrix} \begin{bmatrix} \mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} \end{bmatrix} \begin{bmatrix} \mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} \end{bmatrix} \end{bmatrix} \begin{bmatrix} \mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} \end{bmatrix} \\ -\mathbf{H}_{\mathbf{G}} \end{bmatrix} \begin{bmatrix} \mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} \end{bmatrix} \begin{bmatrix} \mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} \end{bmatrix} \\ -\mathbf{H}_{\mathbf{G}} \end{bmatrix} \end{bmatrix} \begin{bmatrix} \mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} \end{bmatrix} \\ -\mathbf{H}_{\mathbf{G}} \end{bmatrix} \\ -\mathbf{H}_{\mathbf{G}} \end{bmatrix} \begin{bmatrix} \mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} \end{bmatrix} \\ -\mathbf{H}_{\mathbf{G}} \end{bmatrix} \end{bmatrix} \begin{bmatrix} \mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} \\ -\mathbf{H}_{\mathbf{G}} \end{bmatrix} \\ -\mathbf$$

(397)

Since

$$E'(x_3) W(r) E(x_3) = W (E'r),$$
 (398)

the last term can be simplified somewhat and

$$\frac{\partial}{\partial t} \left\{ \begin{bmatrix} m & H & Fl \\ a & a \end{bmatrix}^{\bullet} = \begin{bmatrix} m & H \\ a & a \end{bmatrix} \left\{ \begin{bmatrix} \bullet & \bullet \\ F & l \end{bmatrix} + F & l \end{bmatrix} \right\}$$
$$= \begin{bmatrix} m & H & Fl \\ a & a \end{bmatrix} \left\{ \begin{bmatrix} \bullet & \bullet \\ l & - \end{bmatrix} + F' & Fl \end{bmatrix}$$
(399)

The matrix of scalar actuator velocities can be differentiated directly since they are scalar quantities. The derivative of the transformation, F', was derived earlier in terms of the vector actuator velocities. The n-th row of this matrix is

$$(\mathbf{F}')_{\mathbf{n}} = \begin{bmatrix} \begin{pmatrix} \mathbf{\ell} \\ p\mathbf{n} \\ \mathbf{\ell} \\ \mathbf{0}\mathbf{n} \end{bmatrix} \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}_{\mathbf{n}} \begin{bmatrix} \mathbf{\ell} \\ \beta \\ \mathbf{\ell} \\ \mathbf{0}\mathbf{n} \end{bmatrix} \mathbf{W}^{2} \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}_{\mathbf{n}} \mathbf{W}^{2} \begin{pmatrix} \alpha \\ \beta \end{pmatrix}_{\mathbf{n}$$

where the scaler velocity of the n-th actuator is given by equation (25).

To derive cross-coupling terms as functions of the scalar velocities, the vector velocity must be expressed as a function of the scalar velocity. For the n-th actuator, this is

$$\begin{pmatrix} \bullet \\ \mu \\ p \end{pmatrix}_{\mathbf{n}} = \begin{bmatrix} \mathbf{1} \\ \mathbf{1} \\ \mathbf{1} \\ \mathbf{0} \end{bmatrix} \mathbf{F} \cdot \mathbf{k}$$
(401)

or

$$\begin{pmatrix} \mathbf{i}_{\mathbf{p}} \\ \mathbf{n}_{\mathbf{t}} \end{pmatrix} = \begin{pmatrix} \mathbf{i}_{\mathbf{t}} \\ \mathbf{k}_{\mathbf{t}} \\ \mathbf{k}_{\mathbf{t}} \end{pmatrix} \begin{bmatrix} \mathbf{i}_{\mathbf{t}} \\ \mathbf{i}_{\mathbf{t}} \\ \mathbf{n} \end{bmatrix}$$
(402)

Thus, the n-th row of F' is equal to

$$(\mathbf{F}^{*})_{\mathbf{n}} = \left[ -\frac{\hat{\boldsymbol{\lambda}}_{\mathbf{t}}}{\hat{\boldsymbol{\lambda}}_{\mathbf{on}}} \mathbf{F}_{\mathbf{t}} \left[ \overline{\boldsymbol{W}} \left( \overline{\mathbf{a}}_{\mathbf{n}}^{\mathsf{T}} \right] \mathbf{W}^{2} \begin{pmatrix} \boldsymbol{\alpha} \\ \boldsymbol{\beta} \\ \boldsymbol{\gamma} \end{pmatrix}_{\mathbf{n}} \right| \frac{\hat{\boldsymbol{\lambda}}_{\mathbf{t}}}{\hat{\boldsymbol{\lambda}}_{\mathbf{on}}} \mathbf{F}_{\mathbf{t}} \left[ \overline{\boldsymbol{W}} \left( \overline{\mathbf{a}}_{\mathbf{n}}^{\mathsf{T}} \right) - \right] \mathbf{W}^{2} \begin{pmatrix} \boldsymbol{\alpha} \\ \boldsymbol{\beta} \\ \boldsymbol{\gamma} \end{pmatrix}_{\mathbf{n}} \mathbf{W} \left( \mathbf{a}_{\mathbf{n}} \right) \right]$$
(403)

Since  $F_t$  must be evaluated numerically by finding the inverse of F', this expression cannot be reduced any further. For a given geometry, the triogonal system and its cross coupling terms can be evaluated numerically. The result will be a 6 x 6 matrix of coefficients, postmultiplied by the scalar actuator velocity matrix.

All cross-coupling terms between the gimbal and triogonal systems result from the inertia and gyroscopic effects. Between the triogonal and tail boom systems, there is a direct transfer of forces given by

$$\frac{\partial f_{\ell}}{\partial \left(\frac{f}{m}\right)_{W}} = -F_{t}H_{a}H_{t}T_{t}W_{t}$$
(404)

and a direct transfer of velocities given by

$$\frac{\partial \begin{pmatrix} \mathbf{x}_{1} \\ \mathbf{x}_{2} \end{pmatrix}}{\partial \mathbf{k}} = \mathbf{H}_{\mathbf{B}}\mathbf{H}_{\mathbf{a}}\mathbf{F}$$
(405)

Again, the matrices F and  $F_t$  must be evaluated numerically.

Combat Vehicle

The dynamics of the combat vehicle are similar to that for the aircraft, except that the tail boom actuator is not used, and an additional pitch actuator system is placed between the platform system and the vehicle system. Reaction forces of the pitch system are applied to the triogonal system (platform).

Vehicle Geometry. The external forces applied to the vehicle are now given by

 $\left( \frac{f}{m} \right)_{V} = \left\{ \left( \frac{f}{m} \right)_{H} + \left( \frac{f}{m} \right)_{W} \right\}_{V}$ (406)

and consist only of those forces transmitted from the pitch actuator and the weapon systems.

The weapon forces, referred to the vehicle, are now

$$\left(\frac{f}{m}\right)_{V,W} = H_{t}\left(X_{3T}, r_{T}\right) H_{t}\left(X_{3W}, r_{W}\right) \left(\frac{f}{m}\right)_{W}$$
(407)

and the pitch system forces, referred to the vehicle are

$$\left(\frac{f}{m}\right)_{V,H} = H_{t} \left(X_{3V}, r_{V}\right) \left(\frac{f}{m}\right)_{H}$$
(408)

The actuator forces are now

$$\mathbf{f}_{\ell} = \mathbf{F}_{t} \mathbf{H}_{t} \left( \mathbf{X}_{3H}, \mathbf{r}_{H} \right) \left( \frac{\mathbf{f}}{\mathbf{m}} \right)_{H}$$
(409)

The velocity of the platform is again equal to the relative velocity of the platform to the gimbal system plus the velocity of the gimbal system, referenced to the platform system coordinates.

$$\begin{pmatrix} \dot{\tilde{x}}_{1} \\ \bar{\tilde{x}}_{2} \end{pmatrix}_{P} = \left\{ \begin{pmatrix} \dot{\tilde{x}}_{1} \\ -\bar{\tilde{x}}_{2} \end{pmatrix}_{G} + \begin{pmatrix} \dot{\tilde{x}}_{1} \\ -\bar{\tilde{x}}_{2} \end{pmatrix}_{P/G} \right\}_{P}$$
(410)

The pitch system velocity is equal to the velocity of the platform plus the velocity of the pitch system relative to the platform, referenced to the pitch system coordinates.



Thus, the velocity of the pitch system is

$$\begin{pmatrix} \dot{\tilde{x}}_{1} \\ \dot{\tilde{x}}_{2} \end{pmatrix}_{H} = H_{H} \left\{ \begin{pmatrix} \dot{\tilde{x}}_{1} \\ \dot{\tilde{x}}_{2} \end{pmatrix}_{G} + F_{\ell} \right\} \quad \begin{pmatrix} \dot{\tilde{x}}_{1} \\ \dot{\tilde{x}}_{2} \end{pmatrix}_{H/G}$$
(412)

Finally, the velocity of the vehicle is

$$\begin{pmatrix} \mathbf{x}_{1} \\ \mathbf{x}_{2} \\ \mathbf{v} \end{pmatrix}_{\mathbf{V}} = H_{\mathbf{V}} \begin{pmatrix} \mathbf{x}_{1} \\ \mathbf{x}_{2} \end{pmatrix}_{\mathbf{H}}$$
(413)

The gravitational force applied at the vehicle CM is again equal to

$$\left(\frac{f}{m}\right)_{g} = m_{V} \left[\frac{E(X_{3})}{0} - \frac{0}{E(X_{3})}\right] \left[\frac{0}{0}\right]_{g} = m_{V} \left[\frac{E(X_{3})g}{0}\right]$$

$$\left(\frac{E(X_{3})g}{0}\right]$$

$$(414)$$

where

$$E(X_3) = E(X_{3V}) E(X_{3H}) E(X_{3P}) E(X_{3G})$$
 (415)

defines the Euler angles of the vehicle, referenced to earth.

Interaction of Systems. The output functions are now the gimbal, pitch, and triogonal system forces. Inputs are gimbal, triogonal, and pitch system velocities and weapon forces. The output functions are given by

Pitch actuator forces

$$\begin{pmatrix} \underline{f} \\ \overline{m} \end{pmatrix}_{H} = H_{V_{t}} \frac{\partial}{\partial t} \begin{cases} m_{V}H_{V}\begin{pmatrix} \underline{x}_{1} \\ \underline{x}_{2} \end{pmatrix}_{H/P} \\ + H_{V_{t}} \frac{\partial}{\partial t} \begin{cases} m_{V}H_{V}H_{H}H_{P}\begin{pmatrix} \underline{x}_{1} \\ \underline{x}_{2} \end{pmatrix}_{H/P} \\ + H_{V_{t}} \frac{\partial}{\partial t} \begin{cases} m_{V}H_{V}H_{H}H_{P}\begin{pmatrix} \underline{x}_{1} \\ \underline{x}_{2} \end{pmatrix}_{G} \\ + H_{V_{t}} \frac{\partial}{\partial t} \begin{cases} m_{V}H_{V}H_{H}H_{P} \begin{pmatrix} \underline{x}_{1} \\ \underline{x}_{2} \end{pmatrix}_{G} \\ + H_{V_{t}} \frac{\partial}{\partial t} \begin{cases} m_{V}H_{V}H_{H}H_{P} \begin{pmatrix} \underline{x}_{1} \\ \underline{x}_{2} \end{pmatrix}_{G} \\ - H_{V_{t}} H_{T_{t}} H_{W_{t}} \begin{pmatrix} \underline{f} \\ \underline{m} \end{pmatrix}_{W} \\ - H_{V_{t}} m_{V} \begin{bmatrix} E(X_{3})g_{e} \\ - 0 \end{bmatrix} \end{bmatrix}$$

(416)

Triogonal actuator forces

$$\mathbf{f}_{\ell} = \mathbf{F}_{\mathbf{t}} \mathbf{H}_{\mathbf{H}_{\mathbf{t}}} \left(\frac{\mathbf{f}}{\mathbf{m}}\right)_{\mathbf{H}}$$
(417)

Gimbal forces

$$\left(\frac{f}{m}\right)_{G} = H_{P_{t}} H_{H_{t}} \left(\frac{f}{m}\right)_{H}$$
(418)

Since all systems are cascaded, they must supply the same forces transformed through the geometry. Again, all coupling terms are the result of inertia and gyroscopic effects except the weapon and gravitational forces. In the derivatives of the momentum, the variables are the pitch system,  $H_{\rm H}$ , the platform system,  $H_{\rm p}$ , the triogonal system, F, and the input velocities,

$$\left(\frac{\dot{x}_1}{\dot{x}_2}\right)_{H/P}$$
,  $\left(\frac{\dot{x}_1}{\dot{x}_2}\right)_G$ , and  $\dot{i}$ . The derivative of  $\dot{i}$  is again  $\frac{\partial}{\partial t}$   $\dot{i} = \dot{i}$ , while the

derivatives of the gimbal and pitch system velocities are

$$\frac{\partial}{\partial t} \left( \frac{\dot{x}_1}{\dot{x}_2} \right)_{G} = \left( \frac{\ddot{x}_1}{\ddot{x}_2} \right)_{G} + \left[ \frac{W(\dot{x}_{2G})}{0} \right]_{W} \left( \frac{\dot{x}_{2G}}{\dot{x}_{2G}} \right] \left( \frac{\dot{x}_1}{\ddot{x}_2} \right)_{G}$$
(419)

and

-

.

$$\frac{\partial}{\partial t} \begin{pmatrix} \dot{\mathbf{x}}_{1} \\ \bar{\mathbf{x}}_{2} \end{pmatrix}_{H/P} = \begin{pmatrix} \overset{\bullet}{\mathbf{x}}_{1} \\ \vdots \\ \dot{\mathbf{x}}_{2} \end{pmatrix}_{H/P} + \begin{bmatrix} \overset{\bullet}{\mathbf{w}} (\dot{\mathbf{x}}_{2_{H/P}}) \\ \vdots \\ 0 \end{bmatrix} \begin{bmatrix} \overset{\bullet}{\mathbf{w}} (\dot{\mathbf{x}}_{2_{H/P}}) \\ \vdots \\ w (\dot{\mathbf{x}}_{2_{H/P}}) \end{bmatrix} \begin{pmatrix} \overset{\bullet}{\mathbf{x}}_{1} \\ \vdots \\ \mathbf{x}_{2} \end{pmatrix}_{H/P}$$
(420)

Again, the derivatives of the transformations are

$$H'H = -\left[\frac{E'}{0} \mid \frac{0}{E'}\right] \left[\frac{W(X_2)}{0} \mid \frac{W(r)}{W(X_2)}\right] \left[\frac{E}{0} \mid \frac{1}{E}\right]$$
$$= -\left[\frac{W(E'X_2)}{0} \mid \frac{W(E'r)}{W(E'X_2)}\right]$$
(421)

The momentum derivatives then become

$$\frac{\partial}{\partial t} \left\{ m_{V} H_{V} \left( \frac{\dot{x}_{1}}{\dot{x}_{2}} \right)_{H/P} \right\} = m_{V} H_{V} \left\{ \left( \frac{\ddot{x}_{1}}{\dot{x}_{2}} \right)_{H/P} + \left[ \frac{W(\dot{x}_{2})}{-\frac{H/P}{0}} \right] \left( \frac{U(\dot{x}_{2})}{-\frac{H/P}{0}} \right) \left( \frac{U(\dot{x}_{2})}{-\frac{H/P}{0}} \right) \left( \frac{U(\dot{x}_{2})}{-\frac{H/P}{0}} \right) \right\}$$
(422)

.

$$\frac{\partial}{\partial t} \left\{ {}^{m} \mathbf{v}^{H} \mathbf{v}^{H} \mathbf{H}^{H} \mathbf{P} \left( \begin{array}{c} \dot{\mathbf{x}}_{1} \\ \dot{\mathbf{x}}_{2} \\ \end{array} \right)_{G} \right\} = \\ = {}^{m} \mathbf{v}^{H} \mathbf{v}^{H} \mathbf{H}^{H} \mathbf{P} \left\{ \left( \begin{array}{c} \dot{\mathbf{x}}_{1} \\ \dot{\mathbf{x}}_{2} \\ \end{array} \right)_{G} + \left[ \begin{array}{c} \frac{\mathbf{w}(\dot{\mathbf{x}}_{2G})}{\mathbf{v}} - \mathbf{v}_{1} \\ \frac{\mathbf{w}(\dot{\mathbf{x}}_{2G})}{\mathbf{v}} - \mathbf{v}_{1} \\ \end{array} \right]_{G} + \left[ \begin{array}{c} \frac{\mathbf{w}(\dot{\mathbf{x}}_{2})}{\mathbf{v}(\dot{\mathbf{x}}_{2})} + \left[ \begin{array}{c} \frac{\mathbf{w}(\dot{\mathbf{x}}_{2G})}{\mathbf{v}(\dot{\mathbf{x}}_{2G})} - \mathbf{v}_{1} \\ \frac{\mathbf{w}(\dot{\mathbf{x}}_{2G})}{\mathbf{v}(\dot{\mathbf{x}}_{2G})} \right] \\ - \left[ \begin{array}{c} \frac{\mathbf{w}(\mathbf{x}_{2})}{\mathbf{v}(\dot{\mathbf{x}}_{2})} - \mathbf{v}_{1} \\ \frac{\mathbf{w}(\mathbf{x}_{2})}{\mathbf{v}(\mathbf{x}_{2})} \\ \frac{\mathbf{w}(\mathbf{x}_{2G})}{\mathbf{v}(\dot{\mathbf{x}}_{2})} \\ \frac{\mathbf{w}(\mathbf{x}_{2G})}{\mathbf{v}(\dot{\mathbf{x}}_{2})} \\ \frac{\mathbf{w}(\mathbf{x}_{2G})}{\mathbf{v}(\mathbf{x}_{2})} \\ \frac{\mathbf{w}(\mathbf{x}_{2G})}{\mathbf{v}(\mathbf{x}_{2})} \\ \frac{\mathbf{w}(\mathbf{x}_{2})}{\mathbf{v}(\mathbf{x}_{2})} \\ \frac{\mathbf{w}(\mathbf{x}_{2})}{\mathbf{w}(\mathbf{x}_{2})} \\ \frac{\mathbf{w}(\mathbf{x}_{2})}{\mathbf{w}(\mathbf{x}_{2})}{\mathbf{w}(\mathbf{x$$

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and

$$\frac{\partial}{\partial t} \left( {}^{m}_{V} H_{V} H_{H} F^{2} \right) =$$

$$= {}^{m}_{V} H_{V} H_{H} F \left\{ {}^{\bullet}_{\mathcal{X}} - F' \left[ \frac{W(E_{H}' X_{2})}{0} + \frac{1}{1} \frac{W(E_{H}' r_{H})}{W(E_{H}' X_{2})} \right] F^{\bullet}_{\mathcal{X}} - \left( {}^{\bullet}_{F} F \right) {}^{\bullet}_{\mathcal{X}} \right\}$$

$$(424)$$

Again, a numerical evaluation is the only practical way to determine the value of these cross-coupled terms, since they involve the matrix, F.

Passive System Mathematical Model

Purpose

The primary purpose of the mathematical model is to determine the upper and lower cylinder pressures of the triogonal actuator to produce the desired spring rate. The computer program STIFF 2 (app C) generates the required cylinder pressures as well as the actuator forces and stiffnesses for the specified gimbal rotation (pitch and yaw) because of the acting weight, the applied load and the system stiffness required.

The work detailed earlier in this report represents that portion of the analysis used in the passive system as detailed for computer programming.

Technical Approach

The following notations are used in this technical discussion:

- F = Force applied to system
- K = System stiffness
- D = System deflection
- f = Actuator force
- k = Actuator stiffness
- d = Actuator displacement
- A = Force transformation matrix
- B = Displacement transformation matrix
- $A^{T}$  = Matrix A transposed
- $B^{-1}$  = Matrix B inverted

Having specified the desired system stiffness (K) at the center (B) of the mounting platform, the actuator stiffnessess (k) can be derived as follows:

F_ =	K	Ď
f =	k	d ~
£ =	A	F~
d =	В	D

Substituting equations (427) and (428) in equation (425) we get

$$A F_{\sim} = k B D_{\sim}$$
  

$$F_{\sim} = A^{-1} k B D_{\sim}$$
(429)

From equations (425) and (429) we conclude that

$$K = A^{-1} k B \tag{430}$$

but

$$A^{-1} = B^{T} (app D)$$
(431)

$$\cdot \cdot K = B^{\mathrm{T}} k B \tag{432}$$

also

$$k = A K A^{T}$$
(433)

where  $B^{-1} = A^T$  (app D).

By defining the system stiffness (K) at the center (B) of the mounting platform, the actuator stiffnesses (k) can be determined using equation (433). Similarly, the system stiffness (K) can be determined from equation (432), when the actuator stiffnesses are known. The above necessitates defining either of the matrices A or B, which can be obtained from the next three paragraphs.

# Derivation of the Transformation Matrix $(B)^{T}$

The triogonal actuators represent a statically determinate system. This property makes it possible to obtain the transformation matrix (B), which is determined from the following six equations of equilibrium of forces:

$$F_{\mathbf{x}} = a_{\mathbf{x}_{1}} f_{1} + a_{\mathbf{x}_{2}} f_{2} + \dots + a_{\mathbf{x}_{6}} f_{6}$$

$$F_{\mathbf{y}} = a_{\mathbf{y}_{1}} f_{1} + a_{\mathbf{y}_{2}} f_{2} + \dots + a_{\mathbf{y}_{6}} f_{6}$$

$$F_{\mathbf{z}} = a_{\mathbf{z}_{1}} f_{1} + a_{\mathbf{z}_{2}} f_{2} + \dots + a_{\mathbf{z}_{6}} f_{6}$$

$$M_{\mathbf{x}} = f_{1}(\mathbf{y}_{1} \cdot \mathbf{a}_{\mathbf{z}_{1}} - \mathbf{z}_{1} \cdot \mathbf{a}_{\mathbf{y}_{1}}) + \dots + f_{6}(\mathbf{y}_{6} \cdot \mathbf{a}_{\mathbf{z}_{6}} - \mathbf{z}_{6} \cdot \mathbf{a}_{\mathbf{y}_{6}})$$

$$M_{\mathbf{y}} = f_{1}(\mathbf{z}_{1} \cdot \mathbf{a}_{\mathbf{x}_{1}} - \mathbf{x}_{1} \cdot \mathbf{a}_{\mathbf{z}_{1}}) + \dots + f_{6}(\mathbf{z}_{6} \cdot \mathbf{a}_{\mathbf{x}_{6}} - \mathbf{x}_{6} \cdot \mathbf{a}_{\mathbf{z}_{6}})$$

$$M_{\mathbf{z}} = f_{1}(\mathbf{x}_{1} \cdot \mathbf{a}_{\mathbf{y}_{1}} - \mathbf{y}_{1} \cdot \mathbf{a}_{\mathbf{x}_{1}}) + \dots + f_{6}(\mathbf{x}_{6} \cdot \mathbf{a}_{\mathbf{y}_{6}} - \mathbf{y}_{6} \cdot \mathbf{a}_{\mathbf{x}_{6}})$$

$$(434)$$

Where  $F_X$ ,  $F_Y$ ,  $F_Z$ ,  $M_X$ ,  $M_Y$ , and  $M_Z$  are the applied loads and moments to the system in the coordinate system, directions X, Y and Z,  $f_1$ -- $f_6$  are the forces in the actuators 1 through 6,  $a_{x1}$  is the direction cosine of actuator 1 in the X direction, etc., x, y, and z are the distances from the corresponding pivot point of the actuator to the system axes on the mounting platform in the x, y, and z directions, respectively.

The above six equations can be represented in a matrix form as follows:

$$\mathbf{F} = \mathbf{B}^{\mathrm{T}} \quad \mathbf{f}_{\mathcal{I}} \tag{435}$$

Method of Analysis

Having defined the external system loads (or recoil load) and the stiffness desired in the load direction, the actuator stiffnesses can then be calculated as follows:

1. Determine the displacements and rotations of the center (B) of the mounting platform, knowing the system load (F) and flexibility  $(K^{-1})$  at center (B)  $D = K^{-1} F$ 

2. Obtain the actuator displacement (d)  $d = B^T D$ 

- 3. Determine the actuator forces due to the system load (F)  $f_{\sim l} = A F_{\sim r}$
- 4. Determine the actuator forces due to the static load (P)  $f_{\gamma 2} = A P_{\gamma 2}$
- 5. Calculate the actuator stiffnesses  $k = f_{1} / d_{2}$

6. Knowing the effective areas (A) of the actuator, we calculate the pressure drop ( $\Delta p$ ) across the actuator pistons  $\Delta p = f_{2} / A_{0}$ 

7. Calculate the top and bottom pressures in the actuators

$$P_{t} = k \sqrt{2Ao} - \Delta p/2$$
$$P_{b} = k \sqrt{2Ao} - \Delta p/2$$

where V = volume of the accumulator.

Capabilities of the Computer Program STIFF 2

#### Output Generated.

1. Actuator forces due to the static load (weight)

2. Actuator forces and displacements due to external load (recoil load)

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3. Actuator stiffnesses due to the external load

4. Actuator pressures in the top and bottom cylinders due to all the applied loads

5. Top and bottom accumulator precharge pressure is generated when using oil in the actuators, and actuator precharge pressure is generated when using nitrogen

Possible Loading Conditions. This computer program is written flexibly to handle various loading conditions. Some examples are as follows:

1. For the stiffness required at the center of the mounting platform, the information given in the previous section is generated for the applied loads and the required system stiffness which are specified at the center of the mounting platform and in the direction of the platform axes.

2. For the stiffness required at the c.g. location of the vehicle, the same information given previously is generated when the applied loads and the required system stiffness are specified at the c.g. of the vehicle in the direction of the vehicle axes.

3. For the stiffness required at the weapon pivot, the recoil load and the required system stiffness are specified along the axis of the weapon, as well as the acting weight at the c.g. of the vehicle. The information generated is given in the previous section. The axis of the weapon is defined as the direction from the weapon pivot point to a specific target position.

The results are also produced by including the pitch and yaw motions of the gimbal system, while the stiffness required at the c.g. of the vehicle and at the weapon pivot are for the active system.

Input Data Required. The input data needed to use the computer program is explained as follows:

1. The mounting angle theta is between the vehicle longitudinal axis  $(X_n)$  and the mounting platform axis  $(X_n)$ .

2. The acting weights are the weight of the platform, part of the actuator weights, and the payload.

3. Location of the c.g. of the acting weights are derived from the gimbal axes  $(X, Y \text{ and } Z)_{C}$ .

4. Location of weapon mounting point is derived from the c.g. location of the acting weights.

5. Location of the target is to be derived from the earth axes (X, Y and Z)<sub>C</sub>.

6. Pitch and yaw angles of the gimbal

7. Damping media are used in the actuators to get a spring constant. Either oil for the higher spring rates and damping, or nitrogen for the lower spring rates and damping can be used.

8. As detailed previously, three locations for the system stiffness are possible.

9. The system stiffness is specified in any one or all of the system directions for translation and rotation. Forces are also specified where the stiffness is given. If the system stiffness is found at the weapon mounting point, only the stiffness and force along the weapon axis are specified.

# List of Constants Used in STIFF 2.

1. Coordinates of the pivot centers of actuators at yaw gimbal (XG (I), I = 1, 6)

2. Coordinates of the pivot centers of moving platform (XP(I), I = 1, 6)

3. Effective area of actuator piston (AP =  $21.205 \text{ in.}^2$ )

4. Total volume of accumulator plus actuator fully extended ( $V_0 = 421 \text{ in.}^3$ )

5. Effective volume of the actuator and the maximum and minimum actuator stiffness is shown in table 1.

The STIFF 2 input map is shown in table 2.

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## MAIN HYDRAULIC POWER UNIT

## Priority

Design and part selection for the hydraulic power unit was given first priority since this is a long lead time item. Further urgency is given to this unit since the Government is required to provide a suitable room in which the unit can be installed. The physical arrangement and clearance dimensions for such a room, to house the equipment described in this report, is shown on drawing D-2637.<sup>1</sup>

### Flow Requirements

The basic criteria for specifying this power unit is the total flow required to drive the various subsystems at their maximum performance velocities. These velocities (or rpm) are derived elsewhere in this report and are used here to predict the maximum required flow rate. Flow rate for a given actuator velocity can be obtained from the formula

$$Q_{valve}(gpm) = \frac{Velocity "/sec x piston area sq in x 60 sec/min}{231}$$
(436)

Then for pitch

$$Q_V = \frac{25.74 \times 50.265 \times 60}{231} = 336 \text{ gpm}$$
(437)

This will be the flow required on the larger area of the piston and through the servovalve. Considering that this pitch motion is a simple harmonic motion, the actual pumping capacity can be reduced by providing appropriate accumulators on the line. The use of accumulators will reduce the actual pump flow to

$$Q_{\text{pump}}(\text{gpm}) = \frac{2 \times Q_{\text{valve}}}{\pi} \text{ or}$$
$$= \frac{2 \times 336}{\pi} = 214 \text{ gpm}$$
(438)

The flow for yaw will be calculated in a somewhat different manner since a piston type hydraulic motor is involved rather than a hydraulic cylinder.

<sup>&</sup>lt;sup>1</sup>Drawings cited throughout this report are on file at the Ware Simulation Center, Rock Island Arsenal, Rock Island, IL, and are available for reference.

In the piston type, the motor flow is dependent on the motor displacement, maximum motor rpm, and volumetric efficiency of the motor, or

$$Q_{v}(gpm) = \frac{q^{"'}rev x rpm}{231^{"'}gal} x e$$
 (439)

where

P

= motor displacement/rev = 2310 in<sup>3</sup>/rev (taken from Haggulund's catalog motor model 8385)

e = volumetric efficiency = .8 (from catalog)  

$$Q_v(gpm) = \frac{2310 \times 3.15}{231 \times .8} = 39.37$$
(440)

This will be the maximum flow required at the motor and through the servovalve. The use of appropriate accumulators on the line will reduce the actual pump flow to

$$Q_p(gpm) = \frac{2 \times 39.37}{\pi} = 25 gpm [from equation (438)]$$
 (441)

The flow requirements for the 6-DOF suspension when using it as a spring rate device are fully developed later in this report. The flow entered in table 3 is based on the availability of the 480-gpm pump unit when simultaneous maximum performance of all units is required. Limitations of various factors which influence the actual flow rate will be explained later.

The flow for the tail boom simulator is calculated for a hydraulic cylinder from equation (436) or

$$Q_{v} = \frac{10.2^{\text{in/sec}} \times 1.6567^{\text{sq in}} \times 60^{\text{sec/min}}}{231^{\text{cu in/gal}}} = 4.4 \text{ gpm}$$
(442)

This will be the maximum flow required at the cylinder and through the servovalve. The use of accumulators on this line is not appropriate, so the pump flow requirement will also be 4.4 gpm.

Similarly the flow for the combat vehicle pitch is

$$Q_{v} = \frac{64.4^{\text{in/sec}} \times 7.568^{\text{sq in}} \times 60^{\text{sec/min}}}{231^{\text{cu in/gal}}} = 127 \text{ gpm}$$
(443)

maximum flow at the cylinder and through the servovalve. The use of appropriate accumulators on the line will reduce the actual pump flow to

$$Q_{p}(gpm) = \frac{2 \times 127}{\pi} = 81 gpm$$
 (444)
Again, the flow for the combat vehicle yaw, is

$$Q_{v} = \frac{22.5^{\text{in/sec}} \times 10.652^{\text{sq} \text{ in}} \times 60^{\text{sec/min}}}{231^{\text{cu} \text{ in/gal}}} = 62.25 \text{ gpm}$$
(445)

maximum flow at each of six cylinders and through each of six servovalves. Since all six actuators must be moving simultaneously, the total flow requirement will be 6 x 62.25 gpm or 373.5 gpm. The use of accumulators will reduce the actual pump flow to

$$Q_p(gpm) = \frac{2 \times 373.5}{\pi} = 238 gpm$$
 (446)

Three vibration systems are provided, two small units to simulate miscellaneous vibrations and one large unit to simulate rotor vibrations as discussed in detail later in this report.

The cylinder for the small units has an effective area of .283 sq in., and its piston moves at a maximum velocity of 31.4 in./sec, thus from equation (436).

$$Q_{v} = \frac{31.4 \text{ in/sec } x \cdot .283 \text{ sq in } x \cdot 60 \text{ sec/min}}{231 \text{ cu in/ gal}} = 2.31 \text{ gpm}$$
(447)

The cylinder for the large unit has an effective area of 1.89 sq in., and its piston moves at a maximum velocity of 47.3 in./sec, thus from equation (436)

$$Q_{v} = \frac{47.3^{in/sec} \times 1.89^{sq} \text{ in } \times 60^{sec/min}}{231^{cu} \text{ in/gal}} = 23.2 \text{ gpm}$$
(448)

Thus the total valve flow is

$$2 \times 2.31 + 23.2 = 27.8 \text{ gpm}$$
 (449)

The use of appropriate accumulators on the line will reduce the actual pump flow to

$$Q_{p}(gpm) = \frac{2 \times 27.8}{\pi} = 18 gpm$$
 (450)

From the above equation, the oil pump flow will be required for maximum performance of the various motions as shown in table 3.

Accumulator sizing is explained in appendix E, and accumulators for servosystems are given in table 4. Component Selection

Six potential suppliers were contacted for equipment recommendations, pricing, and delivery schedules. Of these only one, Airline Hydraulics Corporation, a distributor of Vicker's, Inc., equipment, has produced an acceptable proposal. On this basis, we have continued to negotiate with them.

Our design incorporates two power units, each with a rated flow of 120 gpm at 3000 psi, or a total pump flow of 240 gpm. From the information in table 3, it is apparent that this flow is adequate for the highest performance of any system operating alone. Combinations of simultaneous motions are possible at lower performance levels. These maximum performance levels can be determined by use of the various performance graphs included later in this report.

A block diagram of the overall hydraulic system (including the power units) is shown in figure 2. The schematic arrangement of the unit, as it is being developed, is shown on drawing C-2624 with its list of materials on drawing B-2631. A common 600 gallon-capacity tank will be provided to serve the total hydraulic system (both present and future equipment). Also, common pressure and return manifolds will be provided to serve both the present and future hydraulic equipment. As noted above, two identical 120 gpm-pump units will be furnished now with provisions for adding two additional, identical units in the future.

The selected Vickers, Inc., variable delivery, pressure compensated, axial piston pumps, Model PVA-120, requires that its suction inlet be pressurized to 100 psi to provide maximum life and efficiency and the quietest operation. This inlet pressure will be supplied to each main pump by its own auxiliary centrifugal pump rated at 200 gpm and 125-psi pressure. This pump will have its own motor rated at

H.P. = 
$$\frac{F1ow^{\text{gpm}} \times Pressure^{psi}}{1714} = \frac{1}{efficiency}$$
  
=  $\frac{200 \text{ gpm} \times 125 \text{ psi}}{1714} \times \frac{1}{73\%} = 20 \text{ H.P.}$  (451)

Output of this pump will be fed through full flow  $10\,\mu$  pressure filters and then to the suction inlet of its main pump. A pressure relief valve is provided in this line to protect against excessive pressure and to proportion the auxiliary pump flow to the suction requirements of the main pump. A pressure switch is provided in this line to interlock main pump motor starter to line pressure so that the main pump cannot be started unless suction pressure is available. An electric switch on the filters signals the operator control panel to indicate condition (cleanliness) of the filters.

Each main pump is rated for 120 gpm, 3000 psi at 1200 rpm and will have its own motor rated at

H.P. = 
$$\frac{120^{\text{gpm}} \times 3000^{\text{psi}}}{1714} \times \frac{1}{94\%} = 224$$
 H.P. [from equation (451)] (452)

The nearest standard motor of 250 HP will be provided. The motor will be wound as a part winding start motor to reduce the inrush current to 65% of normal inrush (for across-the-line starting). Suitable part winding starting equipment will be provided in the unit control center (units 1M and 2M).

The output of this pump will be fed to the pressure distribution manifold with the aid of the following devices: (1) a pressure relief value to protect against excessive pressure, (2) a check value to prevent pressure interaction between the pumps connected to the distribution manifold, and (3) a pressure guage for convenience in adjusting pump pressure and relief value settings.

Oil returning from the various operating systems will be collected in a common return manifold. From this manifold, it will be circulated through the cooling coils and returned to the common supply tank. Suitable valving, controls, and sensors are provided to maintain the set operating temperature of the oil.

To prevent surges and the possibility of cavitation of the hydraulic fluid on the return side of the servovalves, the return manifold is pressurized to 75 psi by a check valve set for this pressure. Accumulators are provided on both the pressure and return manifolds to smooth the flow of oil. Calculations for sizing these accumulators are given in appendix E.

## Cooling System

Some means must be provided for dissipating the heat produced by extended high performance operation of the hydraulic equipment. Since cooling water is not available at the installation, we have investigated the possibility of using oil-to-air cooling equipment. We have pursued this with several manufacturers. The best proposal was received from DeAnnuntis and Associates, Inc., representing the Trane Co. Two systems were proposed, one for a 95°F ambient air temperature and one for 105°F. Pertinent data from DeAnnuntis is given in appendix E.

# Control Center

Closely associated with the hydraulic power unit is the electric control center. We are planning to furnish a unit type control center which will provide for distribution of the electric power. This control center, to be installed in the pump room, will have the starters for the main pump motors, the auxiliary pump motors, and the cooling fan motors. Empty plug-in spaces will be provided for later installation of starting equipment for the future pump units. The physical layout of the pump unit, the individual compartment diagrams, and the overall schematic for the system, are shown in appendix E. Starters for the main pump motors are mounted in compartments 1M and 2M. They are connected as two winding motors to provide reduced starting current and consequent lower line currents (dwg A-2639, app E). Provisions are made for starting and stopping these motors at the control center or at the control console (see dwg 2CD-127). An interlock is provided to prevent operation of these motors until adequate suction pressure is available. Circuit breakers and overload relays are provided to protect the motors and line equipment from excess current demands or short circuits. Provision is made in each of these compartments for connecting three size 500-MCM power leads provided by the Government from their 440 V, three phase, 60-Hz supply. Compartments 5M and 6M are reserved for future addition of identical starting equipment.

Starters for the auxiliary pump motors are mounted in compartments 3B and 3D. These units are plug-in devices which connect to the rear mounted bus bar system. They are connected as across-the-line starters (dwg A-2640, app E). Provisions are made for starting and stopping these motors at the control center or at the control console (dwg 2CD-127). Circuit breakers and overload relays are provided to protect the motors and line equipment from excess current demands or short circuits. Compartments 3F and 3H are reserved for future addition of identical starting equipment.

Compartment 3K is empty and will not be used.

Compartment 3M contains a relay panel with the contactor (CR) for energizing the 110 V circuits, a relay (AR) which controls the oil cooler fan motors and fuses for the various remote equipment lines (dwg A-2641, app E).

Starters for the oil cooler fan motors are mounted in compartments 4B and 4D. These units are plug-in devices which connect to the rear mounted bus bar system. They are connected as across-the-line starters (dwg A-2642, app E). These motors cannot be started manually but are connected to run automatically when the main pumps are running and the tank oil temperature reaches  $130^{\circ}$ F. Circuit breakers and overload relays are provided to protect the motors and line equipment from excess current demands or short circuits. Provision is made in compartment 4B for connecting three size 2 AWG power leads provided by the Government from their 440 V, three phase, 60-Hz supply. Compartments 4F and 4H are reserved for future identical starting equipment.

Compartment 4K is empty and will not be used.

Compartment 4M contains a transformer panel to supply the 110 V needed by the entire system (dwg A-2643, app E). This unit is a plug-in device which connects to the rear mounted bus bar system. A 5KVA transformer is connected across two phases of the 440 V supply through contacts of relays 1MCR and 2MCR. The coils of these relays are connected across different phases of the supply line. This arrangement provides a simple means of phase failure protection to the entire system. Failure of any 440 V phase drops out the appropriate relay opening the 440 V connection to the transformer and interrupting the 110 V output. Without this 110 V output all the motor starter relays drop out stopping the motors. Relay (CR) also drops out thus shutting off all power to the electronic circuits including the servo systems.

The power control console (dwg 2CD-127) contains indicator lights to show:

- Main pump motors--RUN, and STOP
- Auxiliary pump motors--RUN, and STOP
- Hydraulic oil--TEMP LOW, TEMP OK, and TEMP HIGH
- Hydraulic oil--LEVEL LOW, LEVEL OK, and LEVEL HIGH
- FILTERS DIRTY, FILTERS OK

# MAIN PITCH SYSTEM

Main Pitch Actuator

Our investigation of the main pitch gimbal actuation system indicates that the required performance can be achieved with the existing mechanical system and hydraulic actuator.

Design calculations have been made to determine pertinent design values for various parameters of the main pitch drive system (app F). The calculations were made for both the AH-1G and the AAH helicopter. The moment of inertia calculations include the additional 3000 1b weight of the new yaw drive motor. The hydraulic force required to move the maximum load at the specified acceleration is 57,436 1b (AAH Helicopter). The existing actuator system provides 108,000 1b. The existing structure was designed to withstand this hydraulic load.

The existing hydraulic piping and control wiring must be completely changed to accommodate the new high flow servosystem. The hydraulic schematic of the new piping is shown on dwg A-2627, appendix F, and the physical layout is shown on drawing J-2603.

To meet the valve-flow requirement of 336 gpm, we propose to use a Moog 79-400 valve with a 73-233 Electro-Hydraulic Servo Valve as the pilot stage (Pc no. J-2603-9). This valve combination is rated 400 gpm at 1000 psi pressure drop. After investigating several other commercially available valves (Sanders Associates and MTS, Inc.) and our own design, the use of the Moog valve proved to be the most cost effective approach. Technical data on the Moog valve is given in appendix F.

System Analysis

A block diagram has been generated for the servo control systems to be incorporated in the design of the Helicopter Fuselage Mount Simulator. The general form for this block diagram is shown in figure 3 in which the main pitch control system is described. The general form for the transfer characteristics of these systems is shown in figure 4.

Main Pitch Actuator

The Main Pitch Actuator Feedback Control system transfer characteristic has been developed based on the general form shown in figure 4. A frequency response analysis was performed to determine open loop gain versus system stability for payload ranges varying from the AAH helicopter fuselage to the AH-1G helicopter fuselage. Specific values of constants shown in figure 4 for the main pitch actuator control system are listed in table 5.

As a guideline for setting a mimimum open-loop gain constant to resist a firing load of 9000 lb, so that the maximum position error will be well within  $\pm 2^{\circ}$ , an estimate of the maximum required open-loop gain constant of the main pitch actuator control system was made by the following equation derived in appendix G:<sup>2</sup>

 $\kappa > \frac{T_d^C}{r^2 A^2(\theta_d)_{ss}}$ 

(453)

<sup>&</sup>lt;sup>2</sup>This equation was derived under the assumptions of: (1) The actuator-load damping would mainly depend on the viscous damping, (2) the actuator-load structural stiffness is at least five times higher than the actuator hydraulic stiffness (app H).

#### where

K = main pitch control system open-loop gain constant n sec<sup>-1</sup>.

It is shown in appendix G that the required minimum open-loop gain constant was 4.1/sec.

To perform the frequency analysis, the transfer function of each system component must first be determined. When we consider that our primary interests in the analysis lie in the frequency range from d.c. to 100 Hz, the system components which will contribute significant dynamic characteristics to the open-loop response are the hydraulic valve and the actuator.

A Moog three stage, 4 way, hydraulic, flow-control valve has been selected for the main pitch actuator. A typical model of this valve rated 400 gpm at 1000 psi valve drop was tested by Moog with spool displacement feedback to provide excellent valve closed-loop frequency response flat from d.c. to 100 Hz. The phase response was measured and found to have phase shift of  $-8^{\circ}$  at 10 Hz,  $-45^{\circ}$ at 67 Hz and  $-90^{\circ}$  at 120 Hz.

The other component block to be considered in the frequency analysis is the pitch actuator and load dynamics. Its transfer function was found to have a second order time-lag characteristic equation between valve flow and actuator The natural frequency of this quadratic was calculated to be 3.63 Hz velocity. for the AAH fuselage payload and 5 Hz for the AH-1G fuselage payload. The damping factor of the quadratic was derived in terms of actuator viscous friction, valve leakage and load inertia. At this time, there is no information on the actuator viscous damping. It is very difficult either to calculate or to test the actuator-plus-load running friction, although we know that the actuator-load running friction is not equal to zero. By neglecting the viscous term in the derived transfer function, the damping factor due only to valve leakage and load inertia was calculated to be 0.04 for the AAH load and 0.03 for the AH-1G load. In the final system design, the actuator-load damping factor will be larger than 0.03 because of the actuator viscous friction. If the overall damping is below a selected nominal value of 0.3 (assumed), a means to increase the actuator damping such as an external leakage bypass across the acuator must be implemented. It is safe to assume, for the purpose of performing the frequency analysis, that the actuator transfer function is a quadratic having a damping factor of 0.3 for the worst case.

With the hydraulic valve minor loop characteristics obtained from the manufacturer (table 6) and the actuator dynamics, as discussed in the previous paragraphs, two frequency responses were calculated for the main pitch position control system under two different loading conditions, that is, with the AAH or the AH-1G fuselage as payloads. The open loop transfer characteristic for the AAH fuselage payload described in the block diagram of figure 5 is plotted in figure 6 where a Kv in excess of 5.25 per second is provided and phase and amplitude margins are well within the required design specification when a simple lag/lead network is placed in the forward open loop characteristic.

In each of the systems we have designed for a phase margin greater than  $40^{\circ}$  where phase margin is defined as "the angle by which the phase of the open loop

ratio of a stable system differs from 180° at gain crossover" (from Chestnut and Mazer, Vol. 1, pg 341).<sup>3</sup> A phase margin of 40° will produce a closed loop peak of +3.3 db while a phase margin of 30°, as referenced in the contract, would cause a +6 db peak in the closed loop characteristic which we would not consider as being a good design. A similar transfer characteristic is also plotted in figure 6 for the AH-1G payload described in the block diagram of figure 7.

The closed loop transfer characteristic for both the AAH and AH-1G payload are shown in figure 8 where the computed system bandwidth is approximately 10 times the specified bandwidth for the helicopter load.

Included in the plot of the closed loop characteristic of figure 8 is the maximum velocity that the system can achieve. This shows that a peak amplitude of  $\pm 28^{\circ}$  can be obtained from D.C. to 0.13 Hz while at the specified frequency bandwidth of 0.3 Hz a peak amplitude of  $\pm 11.9^{\circ}$  can be achieved before velocity limiting is reached. The frequency response test must be performed at an amplitude of 1° not to exceed velocity limitations when operating out to 20 Hz. Figure 9 shows the operating limits imposed on the system by the physical parameters of the system. The chart indicates that the required operation of  $10^{\circ}$  amplitude at 0.3 Hz will be met. At higher frequencies, the performance is flow limited out to about 4 Hz. Beyond this frequency, the performance is acceleration (force) limited. The acceleration limit shown on the chart is based on conditions with the AH-IG fuselage mounted on the simulator and the gun firing. The acceleration limits will be different for other conditions.

Pitch Actuator Control System Circuit Diagram

The circuit schematic of the main pitch control system has been completed. This design includes nonlinear gain compensation for unequal piston area. It also includes automatic error zeroing for start-up, reduced loop gain for smooth start-up, and error and full gain monitoring to control firing.

#### MAIN YAW SYSTEM

Main Yaw Actuator

The required yaw torque in the activated system is much higher than in the original system since the hydro/mechanical brake is no longer available for hold-ing the load under firing conditions.

Design calculations were made to determine pertinent design values for various parameters of the main yaw drive system (app I). Also, calculations were

<sup>&</sup>lt;sup>3</sup>Harold Chestnut and Robert W. Mazer, <u>Servomechanics and Regulating System</u> <u>Design</u>, second edition, Library of Congress 59-9339, John Wiley and Sons, New York, February, 1961.

made for both the AH-IG and the AAH helicopter. The moment of inertia calculations include the additional 3000 lb weight of the new yaw drive motor. The torque required to move the maximum load at the specified acceleration is 62,967 ft lb (AAH helicopter). The existing hydraulic motor, rated at 10,400 ft lb torque, is not adequate for the new requirements. See appendix I for detailed descriptions of several Hagglund motors.

To provide this larger torque capacity, it is necessary to replace the existing rotary torque actuator with one of larger capacity. The use of a larger capacity rotary torque actuator of the type currently mounted on the yaw gimbal (Ohio Oscillator Co. Model H-250) was ivestigated. Also, a similar rotary actuator made by Flo-Torq was investigated. In both cases, our required torque is higher than available in the normal production models made by these companies. Furthermore, they depend on rather large pitch spur gears to transmit torque. This gearing introduces an intolerable backlash of about 1/2 degree. Both these suppliers have declined to quote on furnishing nonstandard units.

We propose to use a Hagglund Model 8385 hydraulic motor for this application. The mounting arrangement of this motor on the yaw gimbal is shown on drawing D-2604. This motor has a rated capacity of 83,160 ft 1b at 3000 psi at speeds from zero to 16 rpm. An additional advantage accrues from the use of this motor since its construction eliminates the need for rotary hydraulic joints in the pipelines leading to the valve or motor ports. This unit is available in Hagglund's U. S. stock for prompt delivery.

The existing hydraulic piping and control wiring must be completely changed to accommodate the new high flow servo system. The hydraulic schematic of the new piping is shown on dwg A-2630 (app I).

To meet the valve flow requirement of 40 gpm, we propose to use a Moog 79-060 valve with a 73-232 electro-hydraulic servovalve as a pilot stage (pc. D-2604-6). This valve is rated 60 gpm at 1000 psi pressure drop and is the same valve to be used on the 6-DOF actuators. This 60-gpm valve is proposed because a suitable 40-gpm valve is not available. Duplicating the 6-DOF valving results in a small initial cost saving and saves on the requirements for maintenance parts.

We have investigated several other commercially available valves (Sanders Associates and MTS, Inc.) as well as our own design and have concluded that the use of the Moog valve is the most cost effective approach.

The existing hydro-mechanical brake system will be retained as a safety back up when the yaw servo is not energized. Its torque rating of 300,000 ft 1b is more than adequate to resist any contemplated loading. The existing structural members were designed for a maximum loading torque of 252,000 ft 1b and are more than adequate for the contemplated servo actuation.

The sections of this report covering the 6-DOF system and the combat-vehicle turret adapter will show that a torque of 196,650 ft lb is required to yaw the combat vehicle turret under specified conditions. As noted earlier, this main yaw system can provide only 83,160 ft lb of torque so it will not be used for high performance yawing of the combat-vehicle turret. The solution to this situation is discussed later in this report.

#### System Analysis

The main yaw control system was determined in a preliminary analysis. This is a standard position type of control servo where shaft angle is fed back to compare with the input command of angular position. The block diagram for this system is shown in figure 10.

The equations of system dynamics have been developed and are shown in figure 11. The specific values of constants shown in this figure for the main yaw control system are listed in table 7. The block labeled Hydraulic Valve Minor Loop Response is representative of the servovalve and spool valve general form that is shown in figure 4.

The open loop frequency response for the main yaw control system has been designed for a  $K_V$  of 6.3/sec. In appendix G, it is shown that  $K_V > 1.25/sec$  to satisfy positional accuracy during disturbing forces. The open loop response with a  $K_V$  in excess of the design value, as recorded in the block diagrams of figures 12 and 13, is plotted in figure 14 for both the AAH and AH-1G payload. The servo valve minor loop characteristics used in this analysis were obtained from the manufacturer and are listed in table 8.

The calculated open loop response recorded in figure 14 shows that the phase margin for the AAH helicopter fuselage is  $57^{\circ}$  and amplitude margin is -6.5 db while the same compensation will give a  $64^{\circ}$  phase margin and -7 db amplitude margin for the AH-1G fuselage all of which are within the specifications required.

The calculated closed loop response as recorded in figure 15 shows that a peak of  $\pm 1.5$  db appears around 0.15 Hz. The characteristic remains within  $\pm 1.5$  db over the range of d.c. to 0.33 Hz for the AAH payload and d.c. to 0.25 for the AH-1G. These are very close to the required bandwidth of 0.3 Hz and would be difficult to improve upon since the natural frequency of both systems is relatively low. This can be more accurately determined once the hardware is assembled and tested. Some improvement may now be achieved by adjustment of compensation networks.

Included in the plot of the closed loop characteristic of figure 15 is the maximum velocity that the system can achieve. This shows that a peak amplitude of  $\pm 75^{\circ}$  can be obtained from d.c. to 0.07 Hz, while at the specified frequency bandwidth of 0.3 Hz, a peak amplitude of 17.5° can be achieved before velocity limiting is reached. The frequency response test must be performed at an amplitude of less than 3.5° not to exceed velocity limitations when operating out to 20 Hz.

The operating limits imposed on the system by its physical parameters is shown in figure 16. The chart indicates that the required operation of  $10^{\circ}$  amplitude at 0.3 Hz will be met, but at higher frequencies the performance is flow limited to about 0.75 Hz. Beyond this frequency, the performance is acceleration (force) limited. The acceleration limit shown on the chart is based on conditions wth the AH-1G fuselage mounted on the simulator and the gun firing. The acceleration limits will be different for other conditions. Two lines are shown for velocity limits. One shows the limits at 40-gpm oil flow which is the volume assigned to this unit to meet the specified performance. The other line shows the limits at 60-gpm oil flow which is the valve capability and could be met when other systems are not demanding their full quota of oil.

System Circuit Diagram

The overall configuration of the main yaw system has been generated and card slots provided for the required electronics components to be mounted in the control console. All wiring details for this system have been completed.

#### TRIOGONAL SUSPENSION SYSTEM

6-DOF Suspension

The activation of the 6-DOF suspension is primarily a function of the control system. A complete analysis of the control system is given later in this report.

Two mechanical changes are required to make the suspension responsive to the control system. To bring the flow rate at maximum velocity within the flow capabilities of the hydraulic pump unit, we will insert a sleeve (dwg B-2616) and new piston (dwg B-2615) into the existing six actuators.

As an alternative, consideration was given to replacing the existing actuators with similar actuators having the required smaller bores. This approach was abandoned because of:

- Significant changes in mounting dimensions requiring design and production of several adapter pieces
- Smaller oil passages leading to high flow velocities and pressure drops
- No significant savings in machine down time
- Higher basic cost--\$360 each actuator for new sleeve and piston compared to \$650 for each new actuator plus the additional costs of the required adapters

The other change involves the addition of an electrohydraulic servovalve to control the flow. The selection of this valve, as for the other systems, depends on the required flow rate through the valve which then depends on the maximum velocity and area of the actuator piston.

# 6-DOF Springs

When used in the spring rate mode, the force and displacement to the payload can be expressed by the pressure and flow supplied to the support system as follows:

$$P = P_0 \sin \omega t$$
$$q = q_0 \cos \omega t$$

where

P = Instantaneous system pressure

 $P_0$  = Peak system pressure

q = Instantaneous system flow

q<sub>0</sub> = Peak system flow

Using the following equations, solve for flow

$$F X = \frac{P_o q_o}{\omega}$$
 (454)

$$\omega = \sqrt{\frac{K}{M}}$$
(455)

$$K = \frac{F}{K}$$
(456)

where

F = Applied force
X = Displacement
K = System spring rate
M = System mass

Then

$$q_{o} = \frac{F\left(\frac{F}{K}\right)\sqrt{\frac{K}{M}}}{P_{o}} = \frac{F^{2}\sqrt{\frac{K}{M}}}{KP_{o}}$$
(457)

or

$$\frac{F^2}{\sqrt{K}} = \Pr_{o} \sqrt{M} \times q_{o}$$
(458)

In equation (458), the actual flow in the system depends on four variables which may change from one test setup to another. Plotting these values is a convenient way to show their relationship, and to do this the following conditions were set up for the AH-1G aircraft system:

Suspended weight of the system is 12,000 lb, then

$$M = \frac{12000}{386.4} = 31 \frac{\# \sec^2 / in}{459}$$

Actuator pressure is

$$P_{a} = \frac{12000 \text{ lbs (.21561)}}{10.64 \text{ sq in}} = 243.2 \text{ psi}$$
(460)

$$\therefore \frac{F^2}{\sqrt{K}} = (243.2) \sqrt{31} q_0 = 1354 q_0$$
(461)

Since the servovalves were selected on the basis of turnet yaw capability and can pass a rated flow of 60 gpm each, this value (60 x 6 = 360 gpm) was assigned to  $q_0$  and a plot made of "F" vs "K" to define the maximum operating limits of this system (fig. 17).

In the combat vehicle system, a suspended weight of 13,000 lb was used so that

$$M = \frac{13000}{386.4} = 33.64 \tag{462}$$

$$P_{\rm T} = \frac{13000 \ x \ (.21561)}{10.64} = 263.4 \tag{463}$$

$$\frac{F^2}{\sqrt{K}} = 263.4 \sqrt{33.64} q_0 = 1528 q_0$$
(464)

The plot made of "F" vs"K" for  $q_0 = 360$  gpm defines the operating limits of this system when full valve flow is available. Another plot was made with  $q_0 = 49.2$  gpm to define the operating limits of this system when available flow is curtailed due to maximum simultaneous operation of the combat vehicle yaw motion.

## 6-DOF Yaw

The 6-DOF actuators will also be used to provide high performance yaw motion to the combat vehicle turrets. This application is discussed later in this report, where justification for use of a 60-gpm servovalve is presented. This servovalve will be a Moog 79-060 valve with a 73-232 electrohydraulic servovalve as the pilot stage as previously described in this report.

## 6-DOF Piping

The hydraulic schematic of the proposed piping is shown in figure 18. A new physical arrangement of the piping on the actuators is being worked out in conjunction with an overall pitch/yaw gimbal piping arrangement. A major part of this effort involves the use of rotary hydraulic joints to bring oil pressure onto the gimbals and to take off the return flow.

Two critical rotary transition points exist; one is at the main pitch gimbal axis, and the other is at the main yaw axis. A maximum flow of 269 gpm is required onto the yaw gimbal to supply the 6-DOF actuators when they are being used to provide yaw and spring motion to the combat vehicle turret. This flow must be brought from the stationary structure onto the movable pitch gimbal and then onto the movable yaw gimbal. The use of hose in this application does not appear practical:

- The required 2 1/2 in. I.D. x 3000 psi rated hose is not really flexible enough to accommodate the degree of gimbal rotation required
- The minimum bend radious of 36 in. would require a hose loop of at least 6 feet diameter between the structure and the pitch gimbal and between the pitch gimbal and the yaw gimbal
- The two hoses required (supply and return lines) at each of these places would be unsightly

We investigated commercially available joints made by Chickson and Barco. The available joints of the required capacity are not suitable for this application for the following reasons:

- Physical size too large for available space
- No pilot or mounting arrangements are provided so that complicated brackets would be required to support the joints and to provide concentricity with the gimbal axis
- Position of the pipe ports leads to a poor arrangement of our connecting pipes
- Any cost saving over special joints is doubtful

The design of a rotary joint suitable for use on both the pitch axis and the yaw axis of the simulator is shown in drawing D-2614. This joint contains passages for both the supply oil at 3000 psi and the return oil at 100 psi. Note that the high pressure passage is inside the low pressure passage so that any leakage of high pressure oil will flow into the return line. This joint also provides a pilot and mounting holes for easy attachment to the simulator.

#### 6-DOF Position Indication

The present limit switches mounted on each actuator and now used to control position indicating lights will be reconnected to provide shut-off signals if maximum excursion of the actuator is approached. Full range continous position indication will be provided electronically and indicated by calibrated meters at the control console. Exact position of each of the six actuators will be indicated at all times.

# Study of Spring/Damping Simulator

During the development of the system design, considerable effort has been expended to determine the best design for the spring/damping simulator. This study has mainly been performed on an analog computer available in the FIRL Labs for this type of design optimization. The basic concept has been reduced to practice in actual hardware (FIRL property; not purchased on the project), and portions of the test results are included in this report. The fabrication and tests to verify the concept were not charged to the project. The block diagram for the system to verify the concept is shown in figure 19. Data obtained from closed-loop tests were transferred back through a Nicholas chart to provide the The open-loop gain was then set for the desired open-loop characteristic. closed-loop damping, the results of which are recorded in figure 20. The system operated at a supply pressure of 1000 psi and supported a load of 200 lb. The hardware is shown in the photograph included as figure 21 where the load is resting on a support beam with the actuator close to fully extended. One of the pressure transducers is visible while the second is hidden by the upper framework. The overall sketch for the test stand is shown in figure 22. A long lever arm is used to lift the 200-1b weight from the load supporting actuator. Rapid upward motion of the lever arm located on the opposite side of the fulcrum from the load causes a force step input to the servoactuator.

Referring back again to figure 20, the recorded actuator position, shows an overdamped characteristic when a step input of position command is electronically injected into the system. One of the theories to be proved was the ability to change the system characteristic by the insertion of a lag network in the forward loop of the electronic amplifier system used to sum the position input command and feedback position and to drive the servovalve. The data obtained from tests provided an open-loop characteristic recorded in figure 23 as described by three test points. Two lag network designs were tried in which one had a break fre-The closed-loop theoretical requency of 0.7 cps, and the other at 1.0 cps. sponse for the break located at 0.7 cps is recorded in figure 24 in which both the frequency and step responses are recorded. This network was connected into the forward loop of the test system, and the step response for this hardware system is shown in figure 25. The underdamped characteristic is in quite good agreement with the theoretical response recorded in figure 24. It is quite evident that the overdamped system of figure 20 could then be easily controlled to have a predicted underdamped characteristic as recorded in figure 25. Since the

deflection of the actuator used to simulate a spring must be a function of applied force to the spring, tests were performed to verify the previously established characteristic as a change of force function on the actuator. The overdamped system of figure 20 is recorded in figure 26 for the condition of lifting the 200-1b weight and then letting it suddenly hang from the actuator, thus producing a step change in force. The response characteristic shows static change in actuator position as the weight is lifted and, on application of the weight, an overdamped response of change in position is recorded. The underdamped system is shown in figure 27, thus further verifying the system concept.

System Analysis

Up to this report period, the system analysis of the triogonal actuator control systems has been performed in the following four areas:

- 1. Stability analysis of one basic triogonal actuator <u>position</u> servo at maximum specified spring-rate condition
- 2. Development of the spring-rate adaptive control system block diagram for actuator pressure sensing
- 3. The closed-loop performance of the preliminary design, adaptive spring-rate control system due to a step force input
- 4. Frequency response analysis of the linearized adaptive spring-rate control system at four different spring rates.

Detailed discussions on these four analyses are reported in the following paragraphs.

Position Servo Analysis

It is essential to examine and design each of the triogonal actuator position servos properly so that they will be stable and can be controlled by the model following adaptive-control system at maximum specified sring-rate conditions. The basic triogonal actuator position servosystem, as shown in the system block diagram in figure 28 contains:

- A position input summing amplifier
- A gain control multiplier
- A phase control multiplier
- A minor-loop input amplifier
- A servovalve drive amplifier

- A three-stage, four-way flow control servovalve
- A valve spool displacement feedback LVDT
- The triogonal actuator with external bypass
- The actuator position feedback LVDT

The combined frequency response of the servovalve minor-loop components was provided by the servovalve manufacturer, since we considered purchasing a complete valve package with spool displacement LVDT feedback. The manufacturer's test data on one of the selected 60-gpm valve (Moog 79-060) is recorded in table 9.

The linearized actuator transfer function between valve flow and actuator velocity was derived as a quadratic with a natural frequency of

$$f = \frac{1}{2\pi} \sqrt{\frac{2 K_{HA}}{M}} \text{ (with actuator bypass)}$$
(465)

where

 $K_{HA}$  = Actuator hydraulic stiffness

M = Mass of actuator piston and load

The damping ratio is mainly dependent on the actuator bypass leakage flow which was designed (app H) to have a nominal value of 5.3 gpm at 1000 psi pressure drop.

The expression for the actuator damping ratio  $\xi$ , is

$$\zeta = \frac{1}{4} \sqrt{\frac{2^{-K} HA}{M}} \left( \frac{A^2}{K_{HA}C} + \frac{CM}{A^2} \right)$$
(466)

where

A = Effective area of piston of one side

C = Leakage coefficient of the bypass

When we consider the values of these parametes for the payload of the AAH helicopter fuselage (heaviest one) as follows:

$$K_{HA} = \frac{2B (A_{S} + A_{L})}{L}$$

$$B = 200,000 \text{ psi}$$

$$A_{S} = A_{L} = 10.652 \text{ in}^{2}$$

$$L = 9 \text{ in}$$

$$K_{HA} = 945,000 \text{ lb per in}$$

$$M = \frac{(16,000 + 2500 + 1500)(.21561)(3)}{368} = 33.5 \frac{1b - \sec^{2}}{\text{ in}} \text{ (worst case)}$$

$$C = \frac{5.8 \text{ gpm}}{1000 \text{ psi}} = 2.23 \times 10^{-2} \text{ cis/psi}$$

the calculated natural frequency, f, and damping ratio,  $\xi$ , for the actuator transfer function are

 $\xi = 0.7$ 

The open-loop gain constant required for the highest specified springrate was calculated (app H) as 36. Using an open-loop gain constant of 45 and the dynamic characteristics of the valve and actuator as stated above and plotted in figure 29, a closed-loop frequency response for the triogonal position servo was calculated and plotted as shown in figure 30. The graph obviously shows that the position loop is very stable even at the condition of simulating a maximum spring-rate of 250,000 lb/in. where a phase margin of 65° and amplitude margin of -12 db are observed in figure 29.

Adaptive Control System Block Diagram

In the proposed model following spring rate adaptive-control system, the system concept was derived to account for the sensing of the spring force applied to the spring model and the actual load mass. However, in real practice, the only force or pressure which can be easily measured will be the force or pressure developed across the actuator.

Referring to the system block diagram in figure 31, it can be shown that the force signal at  $F_3$  will be the applied force, F, if the transfer function of  $F_3/F_2$  is

$$\frac{F_3}{F_2} = \frac{1}{G_1 G_x}$$
(467)

where

- $G_1$  = Transfer function between servo output position, X, and force developed at  $F_2$ .
- G<sub>x</sub> = Closed-loop transfer function between applied force and servo output displacement, X.

(468)

Since

$$G_{x} = \frac{\frac{1}{MS^{2} + DS}}{\frac{1}{1 + \frac{G_{1}}{MS^{2} + DS}}}$$

with

- M = Effective actuator load mass
- D = Effective actuator load damping coefficient
- S = Laplace transform operator

$$G_1 G_x = \frac{G_1}{MS^2 + DS + G_1}$$
 (469)

or

$$\frac{F_3}{F_2} = \frac{MS^2 + DS + G_1}{G_1}$$
(470)

The above equation indicates the simulation of a second order leading network in order to obtain the equivalent forcing function of F at  $F_3$ . One of the methods employed at the present time is to obtain an approximate leading transfer function of  $F_3/F_2$  with a second order lag at frequencies 22 times above the break frequency of  $\sqrt{G_1/M}$  which is

$$\frac{F_3}{F_2} = \frac{MS^2 + DS + G_1}{G_1 (MS^2 + DS + 500 G_1)}$$
(471)

The new system block diagram of the adaptive spring-rate control system is shown in figure 32. This has been proven successful in the computer analysis described later. Adaptive Spring-Rate Control System with Step Force Inputs

To verify the revised system block diagram and its controllability in spring-rate and damping, an analog computer simulation of the adaptive control system was performed. A spring-mass model identical to the model in the adaptive control loop was simulated so that the performance of the adaptive spring system could be compared to this external simple spring model. Recording of the simulation was made on strip chart channels as follows:

Channel 1 - System error, X-Xc

- 2 Actuator displacement, X
- 3 Adaptive loop spring model displacement, Xc
- 4 External Spring model displacement, Xm
- 5 Input signal (either force input or spring rate input to both spring models)

The simulation showed that high open-loop gain with lead compensation is required in the adaptive loop to provide fast response at maximum specified spring-rate and a low damping condition.

The test was performed by applying a small step force input superimposed on a static force applied to the actuator and to the external spring model. Eight recordings were made on four different spring-rates and two dampng ratio settings. These recordings are listed in table 10, with the results shown in figures 33 to 40.

When we compare the steady-state displacements of the actuator to those of the external model, we conclude that the control of spring-rate by the adaptive system is excellent. When we compare the transient portion of these recorded displacements, the control of the damping is cosidered good.

Effect of Variation in Damping in Hydraulic Actuator

A nominal or design value of damping will be selected for the actuators used in the triogonal system. A computer study was made to determine the effect on the spring rate simulation if the damping value in the actual hardware varied from the nominal. Referring to figure 32 the value of D in the force compensation network was held constant at the nominal value. All other values of D that are representative of the hardware were changed simultaneously from a nominal damping factor of 0.7 to 0.5 and 2.1. The theoretical force response of the actuator is shown in figure 41 for a step change in flow input where the damping factor is 0.5. In figure 42 the damping was changed to 0.7 and the force response has less overshoot. The heavily damped characteristic is shown in figure 43 where the damping factor is 2.1. The theoretical effect on the adaptive spring rate control system was studied for the spring rate of 130,000 lb/in. with two selected system damping ratios. A damping ratio of 0.376 is recorded in figure 44. It is shown that the actuator displacement characteristic is not greatly affected by a change in damping factor of 0.5 to 2.1. The damping ratio for the system was then selected as 1.24 and the results for damping factor changes from 0.5 to 2.1 are shown in figure 45. The actuator displacement is quite similar for the factor of 0.5 and 0.7. When the damping factor was moved to 2.1, one portion of the characteristic exhibited a higher frequency discontinuity in the overdamped rsponse. This much change in damping factor may be too extreme since it reflects a 300% increase over the nominal. A more realistic variation would be 30% for which the effect would be negligible. These effects can only be made firm once the hardware has been assembled and tests performed to verify the theoretical analysis.

# Adaptive Spring-Rate Control System-Dynamic Studies

To see the stability and dynamic performance of the adaptive spring-rate control system over the range of the spring-rate control from 1000 lb/in. to 100,000 lb/in., three step responses were recorded from the analog computer simulation of the spring-rate control system. These responses were measured for a step change in spring-rate from a selected level setting for the adaptive spring model under a constant load force. Because of the constant load force, the model and the actuator displacement will change when the spring-rate changes. By comparing the actuator displacement to an external spring-mass model displacement, the dynamic performance of the adaptive control system can be realized.

The strip-chart recordings of the displacement responses of the actuator and model at 1000 lb/in. spring-rate with a step change of 100 lb/in. is shown in figure 46.

The recording for the case of 10,000 lb/in. spring rate with a step change of 1000 lb/in. is shown in figure 47.

The recording for the case of 100,000 lb/in. spring-rate with a step change of 20,000 lb/in. is shown in figure 48.

Other constant parameter values used in this simulation are as follows:

Effective actuator load mass =  $4.33 \text{ lb-sec}^2/\text{in}$ .

Static load force = 2000 1b - 3000 1b

Actuator bypass leakage flow = 30 gpm at 1000 psi load pressure

Spring model damping factor = 0.35

During this study, it was found that a previously selected leakage flow of six gpm produced too great a damping coefficient for the lowest spring rate of 1000 lb/in. Since damping is a function of actuator velocity, and increased damping can be achieved by velocity feedback, a study was made to determine the effect of positive velocity feedback for the purpose of decreasing the damping coefficient. This is effective, but to reach the damping factor of 0.5 as recorded in figure 39, leakage had to be increased to 30 gpm at 1000 psi load pressure. However, a more normal static load condition would require

Total load	=	16,000	1b
Actuator load	=	2,667	1b
Maximum actuator load	=	5,334	1b_
Piston area	=	10,652	in <sup>2</sup>
Differential pressure	=	501	psi
Flow	=	21	gpm

~v

Revised Adaptive Spring-Rate Control System Block Diagram

The linearized transfer function of a hydraulic actuator between input flow, Q, and the actuator velocity, sX, has been derived in app H as the following quadratic function:

$$\frac{sX}{Q} = \frac{1/A}{\frac{M}{K_{HA}}s^2 + \left(\frac{D_a}{K_{HA}} + \frac{MC}{A^2}\right)s + 1 + \frac{D_aC}{A^2}}$$
(472)

The transfer function between the force,  $F_2$ , developed by the actuator and the actuator velocity can be expressed as

$$\frac{\mathrm{sX}}{\mathrm{F}_2} = \frac{1}{\mathrm{Ms} + \mathrm{D}_a} \tag{473}$$

From the above two equations, the transfer function between flow and force developed can be obtained by

$$\frac{F_2}{Q} = \frac{\frac{SA}{Q}}{\frac{SX}{F_2}} = \frac{\frac{(M_S + D_B)}{M_B + D_B} (1/A)}{\frac{M}{K_{HA}} + \frac{S^2}{K_{HA}} + \frac{MC}{A^2} + \frac{S + 1}{A^2} + \frac{D_B C}{A^2}}$$
(474)

Based on the above three actuator transfer functions, the system block diagram of the adaptive spring-rate control system was developed as shown in figure 32. However, equation (473) is correct only when there is no external input forces so the force developed,  $F_2$ , is for accelerating the load mass, M, and for overcoming the viscous damping force,  $D_a$ SX. When there is an external force, F, input to the actuator system, equation (473), should be modified as

$$\Sigma F = F_2 - F = M s^2 X + D_a s X$$
(475)

Equation (474) should then be modified in relation to equation (475). Instead of combining equations (472) and (475) to get the transfer between Q and  $F_2$ , the

actuator transfer function block diagram has been separated into three transfer blocks and a summing junction expressed by the equations

$$Q_{I} = A sX$$
(476)

$$Q_{v} - Q_{L} = Q_{cL}$$
(477)

$$Q_{\text{cL}} = \frac{A}{K_{\text{HA}}} sF_2 + \frac{C}{A} F_2$$
(478)

where

- $Q_{T}$  = Actuator velocity flow
- Q. = Servovalve output flow
- $Q_{cL}$  = Actuator compressibility and leakage flow

Subsequently, the force detection circuit in the adaptive loop (described earlier in this report) should be modified due to the change in  $G_1$  which is the transfer function between the servo output position, X, and the force developed at  $F_2$ . In simulating an actuator spring-rate of less than or equal to 100,000 lb/in., the force detection circuit transfer function of  $1/G_1G_x$  was derived to have a simple expression as follows:

$$\frac{1}{G_1 G_x} = \frac{M}{K_H} s^2 + \frac{MC}{A^2} s + 1 \qquad (for K \le 100,000)$$
(479)

With this transfer function and the revised actuator transfer function block diagram arrangement, a revised system block of the adaptive spring-rate control system was developed. The block diagram in figure 49 is to replace the one pre-viously derived as shown in figure 32.

Numerous analog computer runs from the revised adaptive control system were made to study its simulated performance. From the computer results, no change was observed in capability to obtain 1000 lb/in. spring-rate to greater than 100,000 lb/in. with good accuracy and excellent stability. Some very minor improvement was observed in the dynamic response at the 1000 lb/in. spring rate. The apparent leakage flow is the limiting factor of good transient response at the low spring-rate setting. A computer study on higher leakage bypass flow was made and is discussed in the next paragraphs.

System Response Curves Measured from the Computer Simulated Adaptive Control System at Larger Actuator Bypass Opening

The stiffness of a position-controlled hydraulic actuator servo system can be related mathematically to the system open loop-gain constant, K<sub>1</sub>, the

actuator piston area, A, and the actuator bypass leakage coefficient, C, as follows:

$$\frac{F}{X} = \frac{K_{y}A^{2}}{C} \left(1 + \frac{Da C}{A^{2}}\right)$$
(480)

where

F = Applied force

X = Actuator displacement

D<sub>2</sub> = Actuator viscous damping coefficient

From the above equation, many values of C can be used for a given spring stiffness as long as  $K_v$  changes with it (app H). However, the speed of the actuator displacement response due to a step change in force input is proportional to the servo open loop-gain constant,  $K_v$ . Although the adaptive controller may force the actuator servo to produce a displacement response similar to that of the model, the position servo loop should have a loop gain high enough or approximately equivalent to that required to produce the appropriate response time or damping of the actuator response. This means that for a higher position gain constant,  $K_v$ , at low spring-rate simulation, a higher leakage bypass is needed. The approximate value of the leakage coefficient, C, of the actuator bypass for a certain desirable damping was derived in the revised appendix H with a mathematical expression as follows:

$$C = \frac{A^2}{D} = \frac{A^2}{2\zeta\sqrt{KM}}$$
 (approximately) (481)

where

A	=	Actuator effective area
D	=	Adaptive model damping coefficient
K	=	Simulated spring-rate
ζ	=	Spring-mass damping factor
М	=	Effective mass of the actuator load

The value of C used in the previous design for a spring-rate higher than 60,000 lb/in. to a maximum of 200,000 lb/in. was 5.3 gpm per 1000 psi load pressure or more realistically 0.80 gpm per 150 psi. Later it was found that the leakage flow should be at least 21 gpm at 501 psi for a spring-rate of 1000 lb/in. which again is more realistically expressed as 6.3 gpm per 150 psi. To have a good model following-transient response for spring-rates between 300 to 30,000 lb/in., it was found that the leakage bypass should be opened more. In a recent analog computer study, excellent response curves were generated for low spring-rate simulations when the leakage coefficient of the bypass was set for 30 gpm per 150 psi load pressure. These curves are displayed in figures 50 to 58. The other major parameter values used in this computer simulation (fig. 49) were as follows:

 $= 2.63 \text{ lb-sec}^2/\text{in}$ М .77 cis/psi С = 10.652 sq. in Α 21 lb-sec/in (assumed) Da .945x10<sup>6</sup> lb/in К<sub>н</sub> k<sub>1</sub> = 10,000 ≒ .1 sec k, == 515 rad/sec ω, = .6 ζır

In equation (481), the value of C can be determined for a selected range of spring rates, K, and an average value of actuator load mass, M, from the two extremes in loading due to changes in actuator orientation. If necessary, a compromise can be made between the bypass leakage coefficient and the actuator piston area, A, to reduce the bypass flow rate.

Because of a substantial increase in bypass flow required for the low spring rate low-damping simulation, the leakage flow can no longer be negligible in equations (454) and (458) and in figure 19, and it should be modified to include a constant leakage flow for a nonfiring constant load mass. Based on the bypass leakage used in the computer simulation, the leakage flow per actuator is approximately one third of the maximum servovalve output flow at 150 psi load pressure and the maximum load pressure will be limited to approximately 500 psi, which is higher than the required actuator pressure of 243.2 psi calculated for the AH-IG fuselage system as described earlier in this report. In the combat vehicle system, the total flow requirement for maximum specified simulated velocity was calculated to be 62.3 gpm per actuator (app J), and the maximum actuator pressure required to develop the maximum acceleration was approximately 1520 psi which could not be reached if the computer simulation bypass is used. So either a higher flow-rate servovalve should be used for each of the 6-DOF actuators or a compromise in design of the actuator piston area and bypass as discussed in the previous paragraph will be needed for the combat vehicle motion When a 60 gpm-servovalve design is used for the 6-DOF actuatorsystem. suspension system, the lowest obtainable spring-rate with good system response for maximum combat vehicle yaw motion is predicted approximately at 20,000 The leakage bypass should then be set at 7 gpm per 150 psi actuator 1b/in. pressure for the combat vehicle. Spring-rate lower than 20,000 1b/in. can be achieved at a reduced performance on combat vehicle yaw motion with a larger actuator leakage bypass.

Mechanical Suspension

The purpose of the tail rotor simulator is to introduce the loads and forces into the cut-off frame of the helicopter that would normally appear there in a flying helicopter when the various weapons are fired. To accomplish this, a controllable force should be applied in the proper direction and magnitude to the end bulkhead of the cut-off helicopter. Two main objectives are to be met by the simulator: (1) The moment of inertia of the actual tail boom is to be simulated, and (2) the counter-recoil forces normally supplied by the tail rotor through pilot or stability augmentation system control are to be provided when firing the weapons.

It is difficult to reproduce the exact weight, c.g., and mass moment of inertia simultaneously unless the original geometry and mass distribution is preserved. However, the <u>effect</u> of the tail boom moment of inertia can be simulated if an external force is applied so that the firing load imparts the same acceleration to the cut-off helicopter as it would give to the full length helicopter. By including the effect of the stability augmentation system in this force calculation, this acceleration will be further tailored to simulate both the moment of inertia and the tail rotor thrust effect encountered during firing of the weapon.

This tail rotor simulator is an entirely new system developed for this specific application. Design calculations were made to determine pertinent design values for various parameters of this system. These values are tabulated in drawing A-2634, appendix K.

The physical arrangement of the structure required to support the force producing actuator is shown on drawing D-2606.4 The design of the upper support link has been changed to a fabricated pipe arch to permit its mounting to the underside of the yaw gimbal to straddle actuators number 2 and 3 to accommodate the mounting position of the AH-1G helicopter. This attachment point allows the tail rotor simulator and the aircraft to move as a unit when the main pitch and This main support linkage is designed as a pin jointed yaw angles are changed. "dog-leg" with spherical bearings to relieve the local moment loads. This allows the helicopter section to move freely in the fore and aft direction, in the vertical direction, and in pitch. The attachment of the hydraulic actuator to the support link is made through a universal joint which gives the helicopter freedom to roll (dwg D-2645). Pure lateral freedom is provided through the actuator when no yaw restraining signals are present. The actuator will produce a controlled yaw motion and the structure is designed to resist the applied moments and forces.

<sup>&</sup>lt;sup>4</sup>Drawings cited throughout this report are on file at the Ware Simulation Center, Rock Island Arsenal, Rock Island, IL.

The actuator is controlled by the servo system to produce the proper simulation forces. The hydraulic schematic is shown in drawing A-2635, appendix K. To meet the valve flow requirement of 4.4 gpm, we propose to use a standard commercial Moog valve model 73-233 rated 10 gpm at 1000 psi pressure drop.

System Analysis

The physical concept for the system analysis is shown in figure 59 where the various elements are denoted by

 $I_{ad}$  - Yaw moment of inertia of the mounting adapter  $I_f$  - Yaw moment of inertia of the fuselage  $K_F$  - Fuselage stiffness  $K_{SP}$  - Spring rate of 6-DOF

An assumption has been made that the stiffness of the support links and joints is much greater than either  $K_F$  or  $K_{SP}$ . A four-way servovalve is used to control pressure difference and flow in the piston and the bypass C.

From the physical layout, a block diagram has been developed as shown in figure 60.

The tail boom control system is designed to provide force control over a frequency range of approximately 0.005 Hz to 70 Hz. In any force system, provision must be made to maintain a steady state position so that the moving system does not change position due to unbalanced forces acting on the device. This was accomplished by providing a D.C. or static position feedback that automatically reduces in gain as the frequency of motion increases. Conversely, the force feedback system must have little or no D.C. gain but must be of constant gain over a selected frequency spectrum. The concept has been developed in which each system has been analyzed separately. The position servo is shown in the block diagram of figure 61 while the force servo is shown in the block diagram of fig-As noted in the plot of frequency response, figure 63, the force servo ure 62. is relatively flat from 0.005 Hz to 70 Hz while the position servo falls off in amplitude very rapidly above 0.001 Hz and remains at least -10 db below the D.C. nominal at any frequency above 0.01 Hz. The large negative and positive peaks in the position system are due to system dynamics that appear in the feedback path of the position system. These are not of importance since over the majority of the frequency range the position gain is 1/10 of the force gain thus insuring force control.

#### COMBAT VEHICLE SYSTEM

Mechanical Suspension

This overall simulator was designed as a variable flexibility, or variable damping ratio device for testing interactions between aircraft and weapon systems. A useful extension of this application is for testing interactions between combat vehicles and weapon systems. Because of the differences in mounting requirements and performance characteristics, some new adapters and operating equipment are required to take advantage of this extended usefulness.

The general arrangement of such a combat vehicle suspension system is shown on drawing D-2609. Design calculations were made to determine pertinent design values for various parameters of the system. These values for pitch motion are listed in drawing A-2633, appendix J.

The adapter consists of a turret mounting plate and tube which is adjustable in the vertical direction. The tube is mounted in a roll gimbal ring, then mounted on a pitch gimbal ring through trunnions and self aligning ball-joint bearings (Torrington 35SF14). The pitch gimbal and the self aligning ball-joint bearings are mounted on the suspension ring through trunnions.

The main suspension ring is designed to be attached directly to the clevis brackets of the 6-DOF suspension system rather than to the existing aircraft mounting platform. This provides a greater available clearance to the floor and helps to keep the total moving weight down.

The connection between the tube and the roll gimbal is a pair of taper wedge friction clamps designed to resist the torsional and thrust loads applied to it while permitting infinite axial adjustment of the turret and the pitch axis within the 24-inch range provided.

The combat vehicle system is provided with its own actuator to produce desired pitch displacements. The actuator is controlled by the servosystem. The hydraulic schematic is shown in drawing A-2636, appendix J. To meet the valve flow requirement of 126.6 gpm, we propose to use a Moog 79-200 valve with a 73-233 electro-hydraulic servovalve as the pilot stage. This valve combination is rated 200 gpm at 1000 psi pressure drop. We have investigated several other commercially available valves (Sanders Associates and MTS, Inc.) including our own design and have concluded that the use of the Moog valve is the most cost effective approach.

This actuator/valve combination is also required to provide for variable spring rates in pitch. As noted previously, a valve flow of 126.6 gpm is required to provide maximum pitch displacement performance. With a 200-gpm valve, an additional flow of 73.4 gpm can be accommodated to provide spring characteristics. By using the formulae developed earlier in this report, the following is concluded:

Suspended weight of combat vehicle is 13,000 lb.

$$M = \frac{13000}{386.4} = 33.64 \tag{482}$$

$$P_{t} = \frac{6076^{\#}(\text{actuator load})}{7.568^{"2}(\text{actuator area})} = 803 \text{ psi}$$
(483)

$$\frac{F^2}{\sqrt{K}} = 803 \sqrt{33.64} q_0 = 4657.4 q_0$$
(484)

The plot of "F" vs "K" for  $q_0 = 73$  gpm is shown in figure 64 to define the operating limits of this system for the specified conditions when simultaneously pitching at maximum performance. Note that the spring system is not flow limited at any combination of firing forces and spring rates within the system operating range.

As was mentioned earlier in this report, the main yaw system does not have the performance capabilities required to meet the maximum performance specified for combat vehicle yaw motion. A solution to this problem is available with the existing equipment. The triogonal actuator suspension system is very efficient in the yaw mode and can be programmed to provide the high frequency yaw motion to the turret while retaining its effectiveness as a spring simulator. When using this yaw mode, the existing hydraulic brake will be applied to the main yaw system effectively eliminating it from the movable systems.

Calculated pertinent parameters for combat vehicle yaw drive are tabulated as input to the SDFS computer program and shown in appendix J. Tabulations of the parameters associated with the main yaw drive for full combat vehicle performance are also shown in appendix J.

The output of this program is summarized in appendix J and confirms that the altered 6-DOF actuators are adequate to provide the maximum yaw performance as specified for the combat vehicle. To meet the valve flow requirement of 62.3 gpm, a Moog 79-060 valve will be used with a 73-232 electrohydraulic servovalve as a pilot stage. This valve is rated 60 gpm at 1000 psi pressure drop and is the same valve used on the main yaw drive. It is fully described earlier in this report. This valve will have a flow rate of 70.5 gpm at the minimum pressure drop of 1380 psi needed to provide maximum yaw performance as shown in the calculations given in appendix J. This then provides a valve flow of 8.2 gpm to be used in providing the spring rate operation. The plot of "F" vs "K" for  $q_s = 49.2$  gpm, shown in figure 19 of this report, defines the operating limits of this system when maximum performance operation of the combat vehicle is combined with spring rate requirements.

System Analysis

The combat vehicle system is controlled in pitch by the turret pitch control system. Since the main pitch control could not satisfy the velocity requirements for the combat vehicle, a smaller actuator has been provided that can achieve the amplitude and frequency requirements. This system will also provide a spring rate characteristic similar in design to each of the 6-DOF actuators. The block diagram for the Turret Pitch Position Servo System is shown in figure 65 and the transfer characteristic is recorded in figure 66. The characteristics for the servovalve were obtained from the manufacturer and are tabulated in table 12 for the band of frequencies that are pertinent to the servo system design. The open loop frequency response is shown in figure 67 for a  $K_v$  of 70 per second and a compensation network with a lag at 0.4 Hz and a lead at 0.8 Hz. The amplitude margin is -9.5 db and phase margin is 65 degrees. The closed loop response is shown in figure 68 indicating a well damped system with a bandwidth of 13 Hz (-3 db pt). Once the actual hardware system confirms these characteristics, the open loop gain can be raised by +3 db.

The spring rate control system will be similar in design to each of the 6-DOF spring rate actuators. The maximum stiffness will be determined by the amount of open loop,  $K_v$ , that can be put into the system.

The operating limits imposed on the turret pitch system by physical parameters of the system are shown in figure 69. These limits were calculated based on the data given previously. The chart indicates that the required operation of 3° amplitude at 3.5 Hz will be met. The acceleration limit shown on the chart is based on the MICV-65 turret mounted on the simulator and the gun firing.

Operating limits for the main yaw drive system are shown in figures 16 and 70. The specified operating point for the combat vehicle falls outside the achievable capabilities of the yaw system.

The operating limits for the combat vehicle using the 6-DOF actuators to provide yaw is shown in figure 71. The specified operating point in yaw can be achieved using the actuators as described earlier in this report.

# VIBRATION SYSTEMS

Introduction

Three vibrational systems will be supplied to provide environmental vibrations normally caused by parts of the system not included in the simulation. These are the main rotor, the tail rotor, and one auxiliary rotor (undesignated source). These components normally exert forces on the aircraft fuselage due to vibration of their masses. The vibrational systems will provide equivalent forces. Each vibration system will generate the desired force by vibrating a mass at the proper amplitude and frequency. A force will thus be exerted on the aircraft equal to the reaction force

f = mx

where x is the acceleration of the mass, m. The mass and acceleration values will be chosen to match the forces normally produced by the actual components. Each system will be a hydraulic servo system (single axis) which can be attached to the airframe at the desired location.

The servo systems will be excited by tape recordings, made under operational conditions, of the acceleration of the components being simulated by other inputs. The desired force is this acceleration multiplied by the mass of the component.

A preliminary investigation was made to determine if this approach was feasible and to evaluate some of the major requirements. Two basic designs were examined: (1) A relatively small system suitable for the tail-rotor and auxiliary vibrators, and (2) a much larger one suitable for the main rotor. A design for the combat vehicle was not evaluated because the 40,000 lb peak force requirement does not appear practical.

#### Main Rotor System

Vibration specifications for the main rotor give a double amplitude of 0.4 in. between 5 and 10 Hz, 2 g from 10 to 28 Hz, 0.05 in. double amplitude from 28 to 44 Hz, and 5 g from 44 to 5000 Hz. The weight of the main rotor system is 942.3 lb. Thus, the required force varies from a minimum of 480 lb at 5 Hz to a maximum of 4700 lb between 44 and 5000 Hz. To avoid adding excessive weight to the helicopter fuselage, the mass of the vibration system should be kept to a minimum, but this requires a relatively large displacement for the servo system. As a compromise, a vibrating weight of 250 lb was selected for the study. The required peak-to-peak amplitude of vibration is then 1.506 in.

Design Limitations

The output force is limited by several factors in different parts of the frequency range which are shown in figure 72. At low frequencies, the maximum amplitude of the vibrating mass produces a limit which varies as the square of the frequency. The values given will match the low-frequency requirements or the main rotor. In the mid-frequency range the output force will be limited by the supply pressure of 3000 PSI. The actuator area must be chosen large enough to provide the maximum required force. At high frequencies, the force is limited by a combination of saturation of the servovalve amplifier, the servovalve coil time constant, the servovalve spool resonance, and the flow capability of the servovalve. In this region, the limiting force varies inversely as the fourth power of frequency.

Design Parameters

The design parameters for this study were determined as follows:  $mg = 250 \ 1b$   $\mathbf{x}_{0} = \left(\frac{M_{a}}{M}\right) \quad \mathbf{y}_{0} = \frac{942.3}{250} \quad (0.2) = 0.753 \ \text{inch}$ (485)  $\mathbf{A} = \frac{f_{max}}{P_{max}} = \frac{4700}{2500} = 1.89 \ \text{in}^{2}$  $\mathbf{q}_{n} = 76 \ \text{in}^{3}/\text{sec} \ (20 \ \text{gpm valve})$  (486)

The 20 gpm valve provides a flow of

$$q_o = \sqrt{3} q_v = 132 \text{ in}^3/\text{sec } (23000 \text{ psi})$$
 (487)

The high frequency limit is then given by

$$\frac{f_{max}}{E_{v}} = \frac{q_{o}A\omega_{\gamma}}{Ri_{o}TC} \cdot \frac{1}{4}$$
(488)

where

$$\omega_{\gamma} = 628 \text{ rad/sec (valve spool resonance)}$$

$$T = 4.5 \text{ ms (valve coil time constant)}$$

$$i_{o} = 10 \text{ M}_{a} \qquad (valve rated current)$$

$$R = 500 \text{ ohm (valve coil resistance)}$$

$$C_{c} = 1.4210^{-5} \text{ in}^{5}/\text{lb (compliance)}$$

$$E_{v} = 10 \text{ volt (amplifier saturation voltage)}$$

Then, the maximum force is

$$f_{max} = \frac{1.97 \, 10^{12}}{f} \tag{489}$$

where f is the frequency in Hz. The maximum frequency at which full output (4700 lb) can be obtained is then

 $f_{max} = 138$  Hz

Tail Rotor System

The vibration specifications for the tail rotor are assumed to be identical to those for the main rotor. The parameters specified in the proposal have been used for the feasibility analysis. These are

$$m_g = 12.5 \text{ lb}$$
  
 $x_o = 0.5 \text{ in.}$   
A = 0.283 in.<sup>2</sup>

The peak velocity is then

$$\dot{\mathbf{x}}_{\max} = 62.8(0.5) = 31.4 \text{ in/sec}$$
 (490)

and the peak flow is

$$q_{max} = Ax_{max} = 8.80 \text{ in}^{3}/\text{sec} = 2.31 \text{ gpm}$$
 (491)

A 4 gpm (1000 psi) valve was chosen, for which the spool resonant frequency is

$$\omega_{\rm V} = 2 \Pi(220) = 1380 \text{ rad/sec}$$
 (492)

The valve coil time constant is again

 $T = 4.5 \cdot 10^{-3}$  sec

so that the maximum available force at high frequencies is now

$$f_{max} = \frac{2.16.10^{12}}{\frac{4}{10}}$$
(493)

The highest frequency at which the required force of 154 lb can be produced is then

$$f_{max} = 340 \text{ Hz}$$
 (494)

## Stability Analyses

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The response of the vibration servos will be affected by the impedance of the airframe at the mounting location, but it is reasonable to assume that over the range of frequencies for which the servo is designed to operate, the airframe will look like a pure mass, the value of which is much greater than that of the vibration system. The equivalent circuit for the vibration system is shown in figure 73. The feedback signal for the servo system is derived from a force transducer located between the actuator cylinder and the mounting frame. The loop gain for this system is given by

$$K_{oL} = \frac{M^{1}K_{c}K_{e}K_{i}K_{a}}{K_{x}} \cdot \frac{S^{2}}{\left(1 + \frac{A_{s}}{K_{q}K_{x}} \left[1 + SM^{1} \frac{g_{v} + S_{c}}{A^{2}}\right]\right)}$$
(495)

where

$$\begin{split} \textbf{M}^{1} &= \textbf{M} \underset{a}{\textbf{M}} \text{ is the equivalent mass of the system} \\ \hline (\textbf{M} \underset{a}{\textbf{M}}) \\ \textbf{M} &= \textbf{the mass of the vibrator} \\ \textbf{M}_{a} &= \textbf{the mass of the airframe} \\ \textbf{K}_{i} &= \textbf{the current gain of the servovalve amplifier} \\ \textbf{K}_{c} &= \textbf{the gain of the compensation network} \\ \textbf{K}_{E} &= \textbf{the gain of the error amplifier} \\ \textbf{A} &= \textbf{the piston area} \\ \textbf{X}_{o} &= \textbf{the half stroke} \\ \textbf{K}_{q} &= \frac{\left(\frac{\partial_{q}}{\partial_{1}}\right)\textbf{P}_{s}}{\left[1+2\zeta_{\gamma}\left(\frac{\textbf{S}}{\omega_{\gamma}}\right)+\left(\frac{\textbf{S}}{\omega_{\gamma}}\right)^{2}\right]} \\ \textbf{q}_{v} &= \textbf{the leakage flow constant} \\ \textbf{C}_{c} &= \textbf{the compliance of the trapped fluid} \\ \textbf{K}_{x} &= \frac{\textbf{K}_{xo}}{-(1+\textbf{T}_{x}\textbf{S})} \\ \textbf{T}_{x} &= \textbf{the IVDT time constant} \\ \textbf{K}_{a} &= \frac{\textbf{K}_{ao}}{-(1+\textbf{T}_{a}\textbf{S})} \\ \textbf{T}_{a} &= \textbf{the force transducer gain} \\ \textbf{T}_{a} &= \textbf{the two spool resonant frequency} \\ \textbf{\zeta}_{v} &= \textbf{the valve spool damping factor} \\ \left(\frac{\partial_{q}}{\partial_{1}}\right)_{\textbf{P}_{s}} \\ = \frac{\textbf{q}_{o}}{\textbf{i}_{o}} \\ = \textbf{low frequency valve gain at zero load pressure} \end{split}$$

Excluding the compensation network, this is proportional to the square of the frequency at low frequencies and inversely proportional to the cube of frequency at high frequencies. Furthermore, for low values of leakage, a large resonant peak may result from the load resonant frequency, but this can be reduced by the proper choice of actuator position feedback.

If the proper frequency dependence of the various gain factors appearing in the expression for loop gain are inserted, the denominator polynomial, excluding the compensation network, becomes

$$P(S) = 1 + \frac{A_{S}}{K_{xo}\left(\frac{\partial q}{\partial 1}\right)} \left[ 1 + \frac{SM\left(q\gamma + SC_{c}\right)}{A^{2}} \right] \left[ 1 + 2\zeta\left(\frac{S}{\omega_{\gamma}}\right)^{+}\left(\frac{S}{\omega_{\gamma}}\right)^{2} \right] (1+T_{x}S)$$

$$(496)$$

It is desired to select a value for the position transducer gain,  $K_{x0}$ , that will result in a reasonable degree of damping for the roots of this polynomial. Also, it is desirable to retain as low a value of leakage,  $q_v$ , as possible, unless suitable damping cannot be obtained without adding additional leakage. This has been possible, and the leakage constant has been assumed equal to zero.

For this value, the roots of the denominator polynomial occur at frequencies of

$$f_{x} = \begin{cases} 8.8 \angle \pm 17.2^{\circ} \\ 73.5 \angle \pm 74.8^{\circ} \\ 92.4 \angle \pm 87.6^{\circ} \end{cases}$$
 Hz (497)

The last two are underdamped more than desired but should cause no problem since they occur in the middle of the response band.

Main Rotor

For the main rotor vibrator, the following parameters have been chosen:

Mg = 250 lb (M=0.648 lb sec<sup>2</sup>/in)  
A = 1.89 in<sup>2</sup>  

$$X_{o} = 0.756$$
 in  
 $\left(\frac{\partial q}{\partial i}\right)_{P_{\gamma}} = 3000$   
= 13.2 in<sup>3</sup>/Ma sec (Moog 35S-020)

$$f_{\gamma} = 100 \text{ Hz}$$

$$C_{c} = 1.429 \cdot 10^{-5} \text{ in}^{5}/1b$$

$$g_{\gamma} = 0$$

$$T_{x} = 1.59 \cdot 10^{-3} \text{sec} (f_{x} = 100 \text{ Hz})$$

With these values, the load resonance will be reasonably well damped by choosing a position feedback gain equal to

$$K_{\rm x0} = 29.6 \, \text{Ma/in}$$
 (498)

This results in a resonance peak of about 11 db at 82.8 Hz in the loop gain.

To stabilize the loop, a compensation network equal to

$$K_{c} = \frac{7.76 (1+1.924 \cdot 10^{-3} s)^{4}}{(1+0.318s) (1+7.31 \cdot 10^{-3} s) (1+.0531 \cdot 10^{-3} s)^{2}}$$
(499)

is used. This results in a closed loop bandwidth extending from 3 Hz to 500 Hz. These curves are shown in figure 74.

Tail Rotor

For the tail rotor vibrator, the parameters are as follows:

$$M_{g} = 12.5 \text{ lb } (M = .0324 \text{ lb sec}^{2}/\text{in})$$

$$A = 0.283 \text{ in}^{2}$$

$$X_{o} = 0.5 \text{ in}$$

$$\left(\frac{\partial_{q}}{\partial_{i}}\right)_{P_{\gamma}} = 3000$$

$$f_{\gamma} = 220 \text{ Hz}$$

$$C_{c} = 1.905 \cdot 10^{-6} \text{ in}^{5}/\text{lb sec}$$

$$q_{\gamma} = 0$$

$$T_{x} = 1.59 \cdot 10^{-3} \text{ sec}$$

For these values, the position feedback gain has been made equal to  $K_{xo} = 46.4 \text{ Ma/in}$  (500)
This gives denominator roots at frequencies of

1

$$f_{x} = \begin{cases} 106.4 \neq 61.9^{\circ} \\ 149.5 \neq 82.4^{\circ} \\ 208.7 \neq 62.2^{\circ} \end{cases}$$
 Hz (501)

The compensation network in this case has been chosen to be

$$K_{c} = \frac{12.12 (1+1.065 \cdot 10^{-3} \text{s})^{3} (1+0.763 \cdot 10^{-3} \text{s})^{2}}{(1+.3188) (1+3.58 \cdot 10^{-3} \text{s})^{2} (1+.053 \cdot 10^{-3} \text{s})^{2}}$$
(502)

This again results in a closed loop bandwidth from 3 Hz to 500 Hz. These curves are shown in figure 75.

#### Final Designs

The final designs for the main rotor and tail rotor systems are shown in figures 76 and 77. The auxiliary system will be identical to the tail rotor system. Compensation has been added in the force feedback loop to correct for the high frequency response of the force transducers, and extend the bandwidth out to the predicted 500 Hz.

#### SYSTEM AND SUBSYSTEM ELECTRONIC POWER CONTROLS

The control of power supplies needed for all of the servosystems is shown in the schematic diagram of 26D-108. The power supplies, with the exception of the 5 V-regulated supply, will all be located in cabinet 3. The 5-V supply is located in cabinet 1 so that it will have short lead lengths to the computer interface logic circuits. The power to the supplies is controlled by a line contactor that is operated by a key switch (dwg A-2626, app E). Each supply will have an indicator type of fuse to protect the supply on the 120 V, 60 Hz power side. The power supply indicator lights are all 28-V lamps that are controlled through transistors with the exception of the 28-V supply, thus permitting use of one type of lamp and lamp housings that look uniform. The power supply leads to the servo systems have been divided to prevent coupling between systems where relatively long supply leads are necessary. The return for the 28-V unregulated supply is separate from the regulated supplies used for signal circuits, thus decreasing the chance of noise. The return for the -84-V supply used for the feedback circuits is connected to the signal common at each control location, thus making the common junction as close as possible to the input of the summing amplifier. An interlock circuit is provided to connect power to either the tail boom servo or the turret servo since both systems never operate simultaneously. Power select switches are also supplied for the vibration servos. These are independent of each other and can be selected in any desired combination. Panel lights indicate which system is powered.

#### SYSTEM START UP AND FAIL-SAFE INTERLOCKS

#### Start Up and Fail-Safe System

The preliminary design has been completed for the limit circuits so that electronic limit of command signals will be provided and followed up by limit switch circuits. The electronic position limit is provided to prevent the system from reaching the limit switch. Since start-up system has been designed so that the actuators must be within the operating range located between the limit switches, the servo system error must be below a specified amount and all power supplies must be on. To prevent undesirable motions in the actuators at turn-on caused by pressure build-up in the system, an automatic gain control has been designed. At turn-on, the gain is in the order of 1/10 the normal gain, thus decreasing system bandwidth which then limits velocity. During a nominal 5second period, the gain will rise smoothly to the normal set value.

#### Firing Interlock

The circuit schematic diagram (dwg 26D-109) for the fail-safe firing interlock has been completed. The visual indicator with engraved notation of "Standby to Fire" is designed to operate through the interlock of

- 1. Emergency pushbutton.
- 2. Main pump control relay contacts.
- 3. Gun aiming position sensor.
- 4. Servo system "full gain" relay contacts.
- 5. Servo system hydraulic control relay contacts.

When all subsystems are activated, thus closing the firing control relay, the "Gun on Target" and "Standby to Fire" indicator lights will be on. The firing can then be initiated by closing the firing circuit through a manually operated pushbutton in series with the firing relay contacts.

The panel layout for the firing interlock system has been completed and is shown in drawing 26D-127.

#### ELECTRONIC WIRING AND PACKAGING

#### Wiring

Preliminary circuit board wiring design was done for the pitch and yaw servo system. The computer interface circuit boards are under consideration. A total of 76 cards or 60% of the buffering and logics boards will be purchased items from the Digital Equipment Corporation. Most of the internal wiring diagrams of the control consoles have been completed. Wiring of the three control panels and one relay panel are also completed for construction.

#### Packaging

The latest estimate is that three 52 inch height-control consoles will be needed to house all of the electronics, power supplies, pump motor controls, and indicators. A total of 14 card racks will be needed to hold the boards. The tentative arrangement of the control consoles are

#### Control console 1

Pitch servo card rack Yaw servo card rack Computer interface card racks Turret pitch system card rack Tail boom control system card rack Terminal panel Control panel

#### Control console 2

Six triogonal actuator card racks Terminal panel Control panel

#### Control console 3

Vibration system card racks Relay panel Circuit breaker D.C. power supply Terminal panel Control panel

Main pump motor "Start/Stop" pushbuttons Auxiliary pump motor "Start/Stop" pushbuttons Indicating lights Main terminal board for incoming wire connections

The packaging for the card racks is shown in the drawing 26D-130. The control panel for the pitch, yaw, triogonal actuator, turret and tail boom systems is shown in drawings 26D-121 and 26D-124.

#### Conclusions

A design has been completed for an activated 6-DOF simulator. The simulator was designed to mount portions of vehicles and withstand the force of small arms and automatic cannons firing from these vehicles. This design includes: (1) A complete mathematical model of the simulator, (2) design and sizing of the required hydraulic and electrical controls, (3) design of an active pitch and yaw system for the simulator, (4) modeling and fabrication of the spring rate and damping controls for the triogonal actuator system, (5) design of a tail rotor simulator to be added to helicopter fuselages suspended from the 6-DOF simulator, (6) design of a combat vehicle adapter for suspending small turrets (less than 65-inch ring) from the simulator, and (7) design of vibration systems to simulate various field environments such as rotor beat or over-the-road motion.

Limits on the capabilities of the simulator are established throughout this design report. In some complex cases, such as the spring rates achievable by the simulator with systems of different inertias mounted to the simulator, definitive limits could not be defined. However, a computer program has been written based on the math model developed earlier in this report that will solve for the spring rate limitations.

This design indicates that the passive 6-DOF simulator can be modified to provide a tool for testing weapon systems under realistic conditions. A spring rate and damping ratio can be set into the simulator so that mounted vehicles will respond to weapon firings in a manner duplicating that encountered in the field. In addition, vibrations may be propagated through mounted systems with a spectrum similar to that measured in these vehicles under field conditions.

The activated 6-DOF simulator can then provide an effective laboratory setting for testing weapon systems under controlled, repeatable conditions. Types of tests that can be performed with the simulator include research and development testing prior to field testing to remove initial design deficiencies, initial production testing of weapons under controlled mounting and vibration conditions, product improvement testing to compare system changes fairly and accurately, and system identification testing to establish causes of weapon system failures correctly and to develop accurate models of these systems.

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### Table 1. Actuator variations

	Effective volume of the actuator	Actuator stiffness (1b/in.)
Damping media	(in. <sup>3</sup> )	<u>Maximum Minimum</u>
011	117.5	23,000 800
Nitrogen	326.0	5,000 300

### Table 2. STIFF 2 program input map

Card no.	Variable	Description	Format
$\begin{pmatrix} 1\\2\\3 \end{pmatrix}$	TITLE	For title and other information	10A6 10A6 10A6
4	THETA	Mounting angle of vehicle with platform (pitch), degrees (if THETA is greater than 99 END)	E10.0
5	W	Weight of platform, part of actuator and payload, pound	
	XW(1) I=1,3	Location of c.g. of weight with respect to center of gimbal (X,Y, and Z) inch	4E10.0
6	XGUN(1) I=1,3	Location of weapon mounting point to c.g. of weight (X,Y and Z) inch	3E10.0
7	TRGT(1) I-1,3	Location of target with respect to earth axes	3E10.0
8	RY RZ	Pitch angle of gimbal, degrees Yaw angle of gimbal, degrees	2E10.0
9	Media	Damping media, input $\begin{cases} 1 & \text{for oil} \\ \text{or} \\ 2 & \text{for nitrogen} \end{cases}$	12
10	LOC	Location where the system stiffness is specified	12
		LOC = 1 Stiffness given at center of the mounting platform, in the direction of the platform axes	

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Table 2. (cont)

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Card no.	Variable	Description	Format
		LOC = 2 Stiffness given at the c.g. location of the vehicle and in the direction of the vehicle axes <sup>*</sup>	
		LOC = 3 Stiffness given at the weapon pivot point in the direction of the weapon axes	
11	SK(I)	System stiffness required	6E10.0
	I <b>-</b> 1,6	(Note: If LOC = 3, SK(1) only is specified which is the stiffness along the weapon axis.)	
12	SF(I)	System force, which is the force applied in the direction in which the system stiffness SK is specified	6E10.0
		(Note: If LOC = 3, SF(1) is the recoil load of the weapon.)	

Return to card 4.

\*LOC 2 and 3 are intended to be used in the active system; this portion is not finalized.

### Table 3. Pump oil flow (gpm) required for various motions at maximum performance

Motion	Aircraft	Combat vehicle
Main pitch	214	
Main yaw 6-DOF springs	25 218 <sup>a</sup>	<u></u> 31b
Tail boom	5	
Turret pitch		81 gpm-pitch + 46 gpm spring
Turret yaw (6 DOF)		238
Vibrators	18	18
Total gpm for simultaneous maxi- mum performance	480	414

<sup>a</sup>Based on 480 gpm power unit. Performance limited to maximum flow rate of 269 gpm at the pump.

<sup>b</sup>Based on simultaneous maximum yaw performance. Performance limited to maximum flow rate of 269 gpm at the pump.

	Subsystem	Frequency (Hz)	Q <sub>V</sub> (gpm)	V <sub>x</sub> (gal.)	(gal.)	Accumulator provided (gal.)
1	Main pitch	0.3	336	1.76	37.0	40.0
2	Main yaw	0.3	40	0.21	4•4	5.0
3	6-DOF spring	1.0 <sup>a</sup>	360	0.566	11.89	12.0
4	Turret pitch	3.5	127	0.057	1.2	5.0
5	Turret yaw (6-DOF)	3.5	374	0.168	3.5	12.0
6	Tail boom	0.3	5 <sup>b</sup>	0	0	0
7	Shakers	10.0	28	0.0004	0.1	0.25

#### Table 4. Accumulators for servo systems

<sup>a</sup>Based on AH-1G aircraft with 1200 #/in. spring rate.

<sup>b</sup>Full flow provided by pump.

## Table 5. List of parameter values for calculating the main pitch control system frequency responses

Parameter	Symbol	Value	Unit
Effective actuator piston area	A	37.7	sq in.
Input summing amplifier gain	<sup>b</sup> 1	1	volt/volt
Foward compensation amplifier gain	b <sub>2</sub>	•9	volt/volt
Amplifier gain (adjustable)	b <sub>3</sub>	1.1	volt/volt
Hydraulic valve spool displacement feedback gain	b <sub>5</sub>	10	volts/in.
Pitch gimbal position feedback gain	<sup>b</sup> 6	0.6	volts/deg
Leakage coefficient of the spool valve	c <sub>2</sub>	$2.54 \times 10^{-2}$	cis/psi
Actuator-load viscous damping coefficient	D	$\leq 2 \times 10^7 *$	lb-insec
Total mass moment of inertia (with AAH payload)	J (AAH)	82,522	1b-insec <sup>2</sup>
Total mass moment of inertia (with AH-1G payload)	J (AH-1G)	43,430	lb-insec <sup>2</sup>
Spool valve flow gain	Кз	6170	cis/in.
Stiffness of actuator rod attachment joints	К <sub>А</sub>	2,500,000*	lb/in.
Actuator hydraulic stiffness	К <sub>НА</sub>	104,500	lb/in.
Effective radius of pitch angular rotation	r	78	in.
Valve spool displacement LVDT time constant	Т	•0016	seconds
Angle between actuator axis and tangent of pitching arc	$\theta_{\mathbf{T}}$	33° (max.)	degree
Assumed damping factor of the actuator and load	۲ <sub>А</sub>	•3*	
Forward compensation network		.053 s + 1 .106 s + 1	

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<sup>\*</sup>Assumed values

Table 6.	Servovalve	characteristics	of	main	pitch	ı control	system
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	Transfer	function
Frequency	Magnitude	Phase
(Hz)	(dB)	(degrees)
1.00E-01	0.00E.01	-1.5
3.00E-01	0.00E-01	-2.0
5.00E-01	0.00E-01	-3.0
7.00E-01	0.00E-01	-3.5
9.00E-01	0.00E-01	-3.7
1.00E+00	0.00E-01	-3.9
1.50E+00	0.00E-01	-4.3
2.00E+00	0.00E-01	-4.5
3.00E+00	0.00E-01	-5.0
3.10E+00	0.00E-01	-5.1
3.20E+00	0.00E-01	-5.1
3.30E+00	0.00E-01	-5.2
3.40E+00	0.00E-01	-5.2
3.50E+00	0.00E-01	-5.3
3.60E+00	0.00E-01	-5.3
3.70E+00	0.00E-01	-5.4
3.80E+00	0.00E-01	-5.4
3.90E+00	0.00E-01	-5.5
4.00E+00	0.00E-01	-5.5
5.00E+00	0.00E-01	-6.0
8.00E+00	0.00E-01	-6.5
1.00E+01	0.00E-01	-7.0
1.50E+01	0.00E-01	-11.5

# Table 7. List of parameter values used for calculating the main yaw control system frequency responses

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Parameter	Symbol	Value	Unit
Design system open-loop gain constant	G open	6.3	per sec
Forward path amplifier gain	<sup>b</sup> 1 <sup>b</sup> 2 <sup>b</sup> 3	1.1	volt/volt
Yaw gimbal position feedback gain	<b>Ե</b> 6	•4	volts/deg
Leakage coefficient of valve and motor	С	•0231	cis/psi
Hydraulic motor displacement	d <sub>m</sub>	368	cu in./rad
Motor-load viscous damping coefficient	D <sub>m</sub>	< <u>48,000</u>	lb-ft-sec
Total mass moment of inertia (with AAH payload)	J <sub>M</sub> (AAH)	47,545	1b-ft-sec <sup>2</sup>
Total mass moment of inertia (with AH-1G payload)	J <sub>M</sub> (AH-1G)	16,105	lb-ft-sec <sup>2</sup>
Motor hydraulic stiffness	K <sub>HM</sub>	$1.232 \times 10^6$	lb-ft/rad
Spool valve flow gain	K3	924	cis/in.
Compensation lead time constants	т <sub>1</sub> , т <sub>2</sub>	.795, 5.46	sec
Compensation lag time constants	т <sub>3</sub> , т <sub>4</sub>	1.59, 15.9	sec
Forward compensation	$\frac{(T_1)}{(T_3)}$	s + 1) (T <sub>2</sub> s + s + 1) (T <sub>4</sub> s +	1)

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Table 8.	Servoval	ve c	haracteri	stics	of	main	yaw	control	sy	yste	m
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	Transfer	function
Frequency	Magnitude	Phase
(Hz)	(dB)	(degrees)
1.00E+00	0.00E-01	-3.0
3.00E+00	0.00E-01	-4.0
5.00E+00	0.00E-01	-4.5
8.00E+00	0.00E-01	-5.0
1.00E+01	0.00E-01	-5.0
1.50E+01	0.00E-01	-8.0
2.00E+01	0.00E-01	-10.0
2.50E+01	0.00E-01	-13.0
3.00E+01	0.00E-01	-17.5
4.00E+01	0.00E-01	-28.0
7.00E+01	7.00E-01	-61.0

Table 9. Manufacturer's test data

Frequency (Hz)	Amplitude ratio (dB)	Phase-shift (degrees)
10	0	5
20	0	-10
40	0	-28
70	+0.7 (peak)	-61
82	0	-90
100	-1.5	-134

Table 10. Recordings on four spring-rates and two damping ratio settings

Static force	Spring-rate	
(1b)	<u>(1b/in.)</u>	Damping ratio
30,000	200 000	0.3
30,000	200,000	1.0
20,000	130,000	0.376
20,000	130,000	1.24
10,000	60,000	0.55
10,000	60,000	1.8
1,000	1,000	0.5
1,000	1,000	1.0

	Transfer function		
Frequency	Magnitude	Phase	
(Hz)	(dB)	(degrees)	
1 000+00		• •	
1 505+00	0.00E-01	-3.0	
1.302700	0.00E-01	-3.0	
2.00E+00	0.00E-01	-4.0	
3.00E+00	0.00E-01	-5.0	
5.00E+00	0.00E-01	-5.5	
7.00E+00	0.00E - 01	-6.0	
1.00E+01	0.00E-01	-7.0	
1.50E+01	-5.00E-02	-10.0	
2.00E+01	-2.00E-01	-13.0	
3.00E+01	-4.00E-01	-20.0	
4.00E+01	-5.00E-01	-25.0	
5.00E+01	-8.00E-01	-32.0	
6.00E+01	-1.30E+00	-40.0	
7.00E+01	-2.10E+00	-47.0	
8.00E+01	-2.80E+00	-55.0	
9.00E+01	-3.70E+00	-61.0	
1.00E+02	-4.50E+00	-68.0	
1.30E+02	-6.50E+00	-92.0	
1.50E+02	-7.60E+00	-107.0	
2.00E+02	-9.40E+00	-140.0	

Table 11. Moog servovalve 73-233 manufacturer's data

Table 12. Servovalve characteristics for turret control system

_	Transfer	function
Frequency	Magnitude	Phase
(Hz)	(dB)	(degrees)
5.00E+00	0.00E-01	-10.0
7.50E+00	0.00E-01	-11.0
1.00E+01	0.00E-01	-12.0
1.50E+01	2.00E-01	-16.0
2.00E+01	4.50E-01	-26.0
3.00E+01	-7.50E-01	-45.0
4.00E+01	-3.00E+00	-64.0
5.00E+01	-5.20E+00	-87.0
7.00E+01	-1.00E+01	-135.0



Figure 1. Triogonal system



Figure 2. Block diagram overall hydraulic system

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--- = MAIN HYDR. LINES

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Figure 3. Main pitch-actuator feedback control system block diagram







Figure 5. Main pitch control system AAH payload







Figure 7. Main pitch control system AH-1G payload







Figure 9. Main pitch operating limits



Figure 10. Main yaw feedback control system block diagram

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Figure 11. Transfer function block diagram of the main yaw feedback control system



Figure 12. Main yaw control system AAH payload





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Figure 16. Main yaw operating limits (AH-1G aircraft)



Figure 17. 6-DOF system spring rate (1b)







Figure 19. Control circuit to verify spring rate and damping control







Figure 21. Spring and damping test set-up



Figure 22. Test stand
















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Figure 33. Position response of the simulated adaptive spring-rate control system with step force input; K = 200,000  $\frac{1b}{in}$ ,  $\zeta = 0.3$ 



Figure 34. Position response of the simulated adaptive spring-rate control system with step force input;  $K = 200,000 \frac{1b}{in}, \zeta = 1.0$ 



Figure 35. Position response of the simulated adaptive spring-rate control system with step force input; K = 130,000  $\frac{1b}{in}$ ,  $\zeta$  = 0.376



Figure 36. Position response of the simulated adaptive spring-rate control system with step force input;  $K = 130,000 \frac{10}{10}$ ,  $\zeta = 1.24$ 



Figure 37. Position response of the simulated adaptive spring-rate control system with step force input;  $K = 60,000 \frac{1b}{in}, \zeta = 0.55$ 



Figure 38. Position response of the simulated adaptive spring-rate control system with step force input;  $K = 60,000 \frac{1b}{in}, \zeta = 1.8$ 



Figure 39. Position response of the simulated adaptive spring-rate control system with step force input;  $K = 1000 \frac{1b}{1n}$ ,  $\zeta = 0.5$ 



Figure 40. Position response of the simulated adaptive spring-rate control system with step force input; K = 1000  $\frac{1b}{1n}$ , 1.0











Figure 43. Theoretical force response of the actuator with 2.1 damping factor



Figure 44. Effects of actuator damping coefficient on the position response of the simulated adaptive spring-rate control system with a step force input;  $K = 130,000 \frac{1b}{1n}, \zeta = 0.376$ 



Figure 45. Effects of actuator damping coefficient on the position response of the simulated adaptive spring-rate control system with a step force input; K = 130,000  $\frac{1b}{in}$ ,  $\zeta = 1.24$ 



Figure 46. Analog computer simulation of the adaptive spring-rate control system with input =  $1000 \pm 50 \frac{10}{in}$ .



Figure 47. Analog computer simulation of the adaptive spring-rate control system with input = 10,000 ± 500  $\frac{16}{in}$ .



Figure 48. Analog computer simulation of the adaptive spring-rate control system with input = 90,000  $\pm$  10,000  $\frac{16}{10}$ .



Figure 49. Revised system block diagram of the adaptive spring-rate control system



Figure 50. Position response of the adaptive spring-rate control system with step force input; K = 300  $\frac{10}{10}$ ,  $\zeta$  = 0.468



Figure 51. Position response of the adaptive spring-rate control system with step force input; K =  $300 \frac{1h}{1n}$ ,  $\zeta = 1.4$ 



Figure 52. Position response of the adaptive spring-rate control system with step force input;  $K = 1000 \frac{1h}{1n}$ ,  $\zeta = 0.384$ 







Figure 54. Position response of the adaptive spring-rate control system with step force input; K =  $3000 \frac{1b}{in}$ ,  $\zeta = 0.444$ 







Figure 56. Position response of the adaptive spring-rate control system with step force input;  $K = 10,000 \frac{\text{Ib}}{\text{in.}}, \zeta = 0.487$ 



Figure 57. Position response of the adaptive spring-rate control system with step force input;  $K = 10,000 \frac{\text{Ib}}{\text{in}}, \zeta = 0.81$ 



Figure 58. Position response of the adaptive spring-rate control system with step force input;  $K = 30,000 \frac{1b}{in}, \zeta = 0.468$ 







Figure 60. Tail-boom control system block diagram

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Figure 61. Block diagram for position servo tail-boom control



Figure 62. Block diagram for force servo tail-boom control











Figure 65. - Turret pitch actuator position servo system block diagram



Figure 66. Turret pitch position control system

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Figure 69. Pitch drive operating limits combat vehicle



Figure 70. Main yaw drive operating limits combat vehicle



Figure 71. 6-DOF yaw drive operating limits combat vehicle



Figure 72. Output force limits (main rotor)



Figure 73. Vibrator-equivalent circuit















Figure 77. Vibrator servo system (TR)

APPENDIX A COMPUTER CONTROL OF 6-DOF SIMULATOR AND COMPUTER PROGRAM Computer Control of 6-DOF Simulator

Introduction

The digital computer (Nova 2/10) performs two functions in the control of the 6-DOF Simulator: (1) It calculates manual input values of effective mass, spring constant, and actuator lengths off-line. These can then be used for static operation. (2) It calculates the same quantities and inputs the results directly to the servo systems via the D/A converters. These are periodically updated to reflect changes in the gimbal pitch and yaw angles and in the pitch angle of the combat vehicle adapter.

The entire program is resident in core. Specific sections are addressed by appropiate inputs at the teletype keyboard. The off-line results are output to the teletype printer. The program sections are:

- 1. Load mass matrix
- 2. Spring constants
- 3. Elastance matrix at input system
- 4. Actuator static forces and lengths
- 5. On-line program

The sections must be addressed in order; however, any previously executed section can be readdressed. Succeeding sections must then again be taken in order. Addressing is accomplished by typing the above code number, following the query "\*".

28	TYPE " <15> "
	ACCEPT "*",Q
	IF (0-1) 28,231,29
29	IF (Q-QØ-1) 231,231,232
232	IF (Q-6) 28,231,28
231	GOTO (2,30,80,90,200) Q

Actuator Mass Load Matrix

The mass load is calculated from the equation developed in the Math Model earlier in this report.

$$M_{\rm P} = F_{\rm t} H_{\rm t} M H F \tag{A-1}$$

in which F is the triogonal transformation (from actuators to platform axes), H is the rectilinear transformation of the platform axes to the component axes, and M is the mass matrix along the component axes about its CM. Since M is defined about the CM, the two off-diagonal  $3 \times 3$  submatrices are zero. The diagonal submatrices are

$$M_{11} = \begin{bmatrix} m & 0 & 0 \\ 0 & m & 0 \\ 0 & 0 & m \end{bmatrix}$$
(A-2)

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$$M_{22} = \begin{bmatrix} J_{xx} & J_{xy} & J_{xz} \\ J_{xy} & J_{y} & J_{zz} \\ J_{xz} & J_{yz} & J_{zz} \end{bmatrix}$$

The equation, (A-1), is evaluated for each of the distinct components of the system, i.e., actuators, platform, platform adapter, and vehicle, and the results are added to give the total mass load. Since the triogonal transformation is common to all components, the summation is performed in the platform coordinate system and then transformed to the actuators. The value due to the actuators remains fixed since the actuators are never changed, and this data is stored permanently in the program (array AM).

DATA AM/1.900. 5,3\*0.,.7996739,2\*0.,1.90045,0.,-.7996739, 1 4\*0.,1.658009,4\*0.,-.7996739,0.,813.2535,2\*0.,.7996739, 2 3\*0.,813.2535,6\*0.,1750.554/

Similarly, since the triogonal system is assumed to be always in its neutral position, the transformation, F, remains constant and is stored as the array, F.

DATA F/5.107058E-2,-.530741,.2156135,3.685701E-3, 1 -1.347696E-2,-8.511763E-3,-.4851705,-.2211421,.2156135, 2 1.351424E-2,3.546568E-3,8.511763E-3,.4340999,.3095989, 3 .2156135,9.828537E-3,9.93039E-3,-8.511763E-3, 4 5.107058E-2,.530741,.2156135,-3.685701E-3,-1.347696E-2, 5 8.511763E-3,-.4851705,.2211421,.2156135,-1.351424E-2, 6 3.546568E-3,-8.511763E-3,.4340999,-.3095989,.2156135, 7 -9.828537E-3,9.93039E-3,8.511763E-3/

The rectilinear transformations, H, for each o the three load compnents, i.e., platform, platform adapter, and vehicle, are developed by the program from the locations of the centers of mass and the Euler angles of the corresponding coordinate systems. These are shown as

 $H = \begin{bmatrix} E(x_3) & -W(r) & E(x_3) \\ 0 & E(x_3) \end{bmatrix}$ (A-4)

The matrix, E, is the angular transformation of the Euler angles

$$\mathbf{x}_{3} = \begin{pmatrix} \phi \\ \theta \\ \psi \end{pmatrix} \tag{A-5}$$

(A-3)

and W is the rotational matrix of the distance to the center of mass

$$\mathbf{r} = \begin{pmatrix} \mathbf{x} \\ \mathbf{y} \\ \mathbf{z} \end{pmatrix} \tag{A-6}$$

given by

$$W(r) = \begin{pmatrix} 0 & -z & y \\ z & 0 & -x \\ -y & x & 0 \end{pmatrix}$$
(A-7)

The elements of the angular transformation are

e <sub>11</sub> = 0	cos 0	cos ψ	- · · · <b>)</b>
e <sub>21</sub> = 1	sin φ	sin θ	$\cos \psi - \cos \phi \sin \psi$
e <sub>31</sub> = 0	cos φ	$\sin \theta$	$\cos \psi + \sin \phi \sin \psi$
<sup>e</sup> 12 <sup>= 0</sup>	cos O	$\sin\psi$	in the second
e <sub>22</sub> = 0	cos φ	cos ψ	+ sin $\phi$ sin $\theta$ sin $\psi$
e <sub>32</sub> = 0	cos ¢	$\sin \theta$	$\sin\psi - \sin\phi \cos\psi$
e <sub>13</sub> = .	- sin	θ	
e <sub>23</sub> = 1	sin_¢	cos θ	1111117 
<sup>e</sup> 33 <sup>= 0</sup>	cosφ	cos θ	

These two transformations are returned by the subroutines ROT (W, X, Q) and ANGLE (E, X, Q), respectively. The value of the integer, Q, specifies the column of the array, X, from which values for r and  $x_3$  are taken. The rectilinear transformation, H, is returned by the subroutine TRANS (C, E, W, Q). The result is the array, C. The integer, Q, now either specifies the order of multiplication of W and E, depending on whether r is measured in the original system or the transformed system, or it specifies that r is equal to zero.

(A-8)

Initially, the configuration data is requested by the program. Development of the mass load proceeds as follows:

> 2 WRITE (10,4) 4 FORMAT (15HØCONFIGURATION //) ACCEPT "LOCATION OF CM <15>"," PLATFORM: <15>", 1 (X(R,1),R=1,3)," PLATFORM ADAPTER: <15>",(X(R,2),R=1,3), 2 " VEHICLE: <15>", (X(R,3), R=1,3), "PLATFORM ADAPTER <15>", 3 " LOCATION OF VEHICLE INTERFACE: <15>",(X(R,7),R=1,3), EULER ANGLES: <15>", (X(R,7),R=4,6), "WEIGHTS <15>", 4 " PLATFORM: ",WGT(1)," PLATFORM ADAPTER: ",WGT(2), 5 " 6 " VEHICLE: ",WGT(3), "MOMENTS OF INERTIA <15>", 7 " PLATFORM: <15>", (MOI(R,1),R=1,6), 8 " PLATFORM ADAPTER: <15>", (MOI(R,2), R=1,6), 9 '' VEHICLE: <15>", (MOI(R,3), R=1,6)

•

First, the locations of the centers of mass of the platform, platform adapter, and vehicle are inputed. These are typed in the order x, y, z, separated by commas and terminated with a carriage return ( $\checkmark$ ). The values for the platform and platform adapter are measured, in inches, from the origin of the platform coordinate system (in the plane of the lower pivot points of the actuators) to the appropriate CM, in the platform system. The location of the vehicle CM is measured from the origin of the platform adapter/vehicle interface, in the vehicle coordinate system. For the AH-1G, this origin is 10 inches below the origin of the platform system, along the z-azis. In this case

$$r_{v} = \begin{pmatrix} 12.8104 \\ 0 \\ 35.1962 \end{pmatrix}$$
(A-9)

Next the platform adapter/vehicle interface data are requested. This consists of the location of the origin, which, as stated for the AH-1G is

$$\mathbf{r}_{\mathbf{I}} = \begin{pmatrix} \mathbf{0} \\ \mathbf{0} \\ \mathbf{10} \end{pmatrix} \tag{A-10}$$

and the Euler angles (which rotate the platform axes into the vehicle axes). For the AH-IG, the vehicle system is pitched 20 degrees below the platform system, so that

$$\mathbf{x}_{3\mathbf{v}} = \begin{pmatrix} \mathbf{0} \\ -2\mathbf{0} \\ \mathbf{0} \end{pmatrix} \tag{A-11}$$

The third block of data requested consists of the weights of the platform, platform adapter, and vehicle (in pounds). For the AH-1G, these are 800, 1700 and 9500 lb, respectively.

Finally, the moments of inertia of platform, platform adapter, and vehicle are requested. These are typed in the order  $J_{xx}$ ,  $J_{yy}$ ,  $J_{zz}$ ,  $J_{xy}$ ,  $J_{xz}$ ,  $J_{yz}$ .

They are measured in units of in.  $lb \sec^2$ . The subroutine INERTIA (J, MOI, Q) forms the full 3 x 3 matrix (equation 3) from these values. The integer, Q, specifies the column of the array, MOI, from which values are taken.

With this data, the calculation can proceed. The mass matrix, M, is initialed to the values for the actuators.

D0 6 R=1.6 D0 6 S=1.6 M(R.S)=AM(R.S) CONTINUE

The derivation of these values is given in appendix B.

Next, the H transformation from interface to vehicle is formed.

CALL ROT(W,X,3) CALL ANGLE(E,X,7) CALL TRANS(C,E,W,1)

This returns the array

6

$$C = \begin{bmatrix} E(x_{3v}) & -W(r_{v}) & E(x_{3v}) \\ - & -V & -V & -3v \\ 0 & E(x_{3v}) \end{bmatrix}$$
(A-12)

Then the transformation from platform to interface is formed.

CALL ROT(W,X,7) CALL UNIT(E) CALL TRANS(D,E,W,1)

This returns the array

$$\mathbf{D} = \begin{bmatrix} 1 & -W(\mathbf{r}_{\mathbf{I}}) \\ - & -W(\mathbf{r}_{\mathbf{I}}) \\ 0 & 1 \end{bmatrix}$$
(A-13)

The complete transformation is then formed by multiplying the two.

CALL MULT(C, D, H, 6)

Since

$$E(x_3) W(r) = W [E(x_3)r] E(x_3)$$
 (A-14)

this returns the array

$$H = \begin{bmatrix} E(x_3) & i & -W[E(x_3) & r_1 + r_v] & E(x_{3v}) \\ 0 & i & E(x_{3v}) \end{bmatrix}$$
(A-15)

which is the rectilinear transformation from platform to vehicle.

The integer, Q, is set to 3, upon entering the loop beginning with statement 11, which then returns the inertia matrix for the vehicle. The mass matrix (6 x 6) is then formed, referred to vehicle axes.

Q=3 11 CALL INERTIA(J,MOI,Q) CALL ZERO(C,6) DO 14 R=1,3 DO 14 S=1,3 C(R+3,S+3)=J(P,S) IF (R-S) 14,12,14 12 C(R,S)=WGT(Q)/386.063 14 CONTINUE

This is then transformed to the platform axes by forming the product

 $M = H_{t}CH$ (A-16)

and adding this value to the previous value of M.

CALL MULT(C,H,H1,6) CALL TRNSP(C,H,6) CALL MULT(C,H1,H,6) DO 16 R=1,6 DO 16 S=1,6 M(R,S)=M(R,S)+H(R,S) 16 CONTINUE

The integer, Q, is now decremented by one, giving a new value of 2, and the program advances to statement 17. This returns the transformation from platform to the CM of the platform adapter.

> Q=Q-1 IF (Q) 21,21,17 17 CALL ROT(W,X,Q) CALL UNIT(E) CALL TRANS(H,E,W,1)

The program now loops back to statement 11

GOTO 11

and forms the mass matrix for the platform adapter. This is transformed to the platform axes and again added to the previous values. Once more the integer, Q, is decremented, this time to a value of one, and the procedure is repeated for the platform. The mass load matrix now contains the contributions from all four basic components of the system, actuators, vehicle, platform adapter, and platform. However, it is still referred to the platform coordinate system. By decrementing the value of Q once more (to a value of zero), the program advances to statement 21. This premultiplies it by F, in order to refer the values to the triogonal system.

21 CALL TRNSP(C,F,6) CALL MULT(C,M,H,6) CALL MULT(H,F,M,6)

To preserve symmetry in the calculations, the actuators were numbered so that 4, 5 and 6 are mirror images of 1, 2 and 3 in the X-Z plane. The physical actuators are numbered clockwise, with number 1 located in the positive Y direction. The array ACTN, also stored in common, is used to rearrange the matrix M into the matrix H1.

DATA ACTN/2,3,6,5,4,1/

DO 23 R=1.6 DO 23 S=1.6 H1(R.S)=M(ACTN(R).ACTN(S)) 23 CONTINUE

This matrix is then typed, in the order corresponding to the physical numbering system, and control of the program is returned to the operator.

WRITE (10,24)((H1(R,S),S=1,6)R=1,6)
24 FORMAT (40H0ACTUATOR LOAD MASS MATRIX (LE-SEC+2/IN) //
1 (6F10.4))
Q0=1
G0T0 28

Spring Constants

The second part of the program calculates the values of actuator spring constant, off-line. This generally follows the development of the math model as described earlier in this report. However, no restriction is placed on the location and orientation of the axes for which values are specified, except that they form a nonsingular set. Three values must be specified, which are the reciprocals of the principal elastances along three axes chosen from the lists of the spring constants of the math model as described earlier in this report. Their order of input depends on which value is most critical, since the values are subject to the physical limitations of the actuators and servo systems.

The initial part of this section determines the minimum and maximum values of spring constant possible for each of the actuators, based on the load mass determined in section 1. The maximum value is the smaller of 200,000 lb/in.

or  $\omega^2 M$ , where

$$\omega = 2\pi (10) = 62.8 \text{ rad/sec}$$
(A-17)

and M is the principal load mass element for that actuator. The minimum value is the larger of 250 lb/in. or  $\omega^2 M/1500$ .

D0 `35 R=1,6 K(R+15)=3947.842\*M(R,R) K(R+9)=K(R+15)/1500 IF (K(R+15)-2.0E5) 33,33,32 32 K(R+15)=2.0E5 33 IF (K(R+9)-250.) 34,35,35 34 K(R+9)=250. 35 CONTINUE

In addition, it has been assumed that the symmetry about the X-Z plane is preserved for spring constants, that is

$$k_{N+3} = k_N \tag{A-18}$$

Thus, the smaller maximum and larger minimum are chosen for each pair of actuators.

> DO 39 R=1,3 IF (K(R+15)-K(R+18)) 37,37,36 K(R+15)=K(R+18) 37 IF (K(R+9)-K(R+12)) 38,39,39 38 K(R+9)=K(R+12) 39 CONTINUE

The location and orientation of the coordinate system for which spring constants are to be specified ("Input System") is then requested.

ACCEPT "ORIGIN OF INPUT SYSTEM: ",(X(R,4),R=1,3), 1 "EULER ANGLES OF INPUT SYSTEM: ",(X(R,4),R=4,6)

These are typed in as measured in the vehicle system, using the origin of the interface as reference. For instance, if the CM of the aircraft is chosen, and values are specified along the aircraft axes, the following would be typed for the AH-1G

ORIGIN OF INPUT SYSTEM: 12.8104, 0., 35.1962

EULER ANGLES OF INPUT SYSTEM: 0., 0., 0.

Next, the matrix, A, is formed, which is the transformation from the input system to the triogonal system as previously described.

$$A = H(x_{31}, r_1) F$$
 (A-19)

CALL ANGLE(E,X,4) CALL ROT(W,X,4) CALL TRANS(C,E,W,2) CALL ANGLE(E,X,7) CALL ROT(W,X,7) CALL TRANS(D,E,W,2) CALL MULT(C,D,H,6) CALL MULT(H,F,A,6)

This is calculated by multiplying the transformation from interface to input system by that from platform to interface, and then multiplying the result by the triogonal transformation (actuator to platform). The index 2 is used in both calls to TRANS, since the distances in both cases are measured in the original system (not the one resulting from rotation by the Euler angles).

In order to continue, it is now necessary to specify which axes are to be chosen for the input values of spring constant. These are typed in the order of importance (U, V, W) with the code

x = 1 y = 2 z = 3  $\phi = 4 \text{ (roll)}$   $\theta = 5 \text{ (pitch)}$   $\psi = 6 \text{ (yaw)}$ 42 FORMAT (12HØINPUT AXES= ,Z) READ (11) N(1),N(2),N(3)

For instance, if the axes are x,  $\theta$ , and z, the following would be typed:

## INPUT AXES = 1, 5, 3 $\rightarrow$

The 3 x 3 matrix, G, is now formed which relates the actuator spring constants to the specified spring constants.

D0 43 R=1,3 D0 43 S=1,3 G(R,S)=A(N(R),S)\*A(N(R),S)+A(N(R),S+3)\*A(N(R),S+3) 43 CONTINUE

This calculation deviates slightly from that given in the math model, since the restriction on the location of the input coordinate system has been removed. The A matrix, in the general case, will not necessarily exhibit the symmetry specified in the math model. The inverse of this matrix is then returned by calling the subroutine INV.

The variable, GO, is the determinant, |G|. From the inverse, I, it is possible to calculate the actuator elastances directly from the specified elastances.

$$\begin{pmatrix} e_1 \\ e_2 \\ e_3 \end{pmatrix} = I \begin{pmatrix} e_u \\ e_v \\ e_w \end{pmatrix}$$
(A-20)

The input elastances,  $e_u$ ,  $e_v$  and  $e_w$ , must be chosen to give physically realizable values fo the actuators. The major portion of this part of the program is used for determining the limits on the input values which correspond to the limits previously imposed on the actuator values. For the specification of  $e_v$ , the most important of the three input values, the equations relating actuator values to input values are used.

$$\begin{pmatrix} e_{u} \\ e_{v} \\ e_{w} \end{pmatrix} = G \begin{pmatrix} e_{1} \\ e_{2} \\ e_{3} \end{pmatrix}$$
(A-21)

)

Since the elements of the matrix, G, are obtained by summing squares of the elements of the matrix, A, they must be positive. It then follows that the maximum and minimum values of input values are obtained by substituting maximum and minimum actuator values if there are no other restrictions. For the initial input specification

$$e_u = g_{11} e_1 + g_{12} e_2 + g_{13} e_3$$
 (A-22)

Thus the minimum and maximum limits on the equivalent spring constant are

$$K(7) = 1/(G(1,1)/K(10)+G(1,2)/K(11)+G(1,3)/K(12))$$
  
$$K(8) = 1/(G(1,1)/K(16)+G(1,2)/K(17)+G(1,3)/K(18))$$

These values are typed out with the appropriate dimensions, depending upon wheth- er  $k_u$  is a linear or angular constant, and an input value is requested.

IF (N(1)-3) 44,44,45
44 TYPE K(8)," >KU> ",K(7)," LB/IN"
GOTO 46
45 TYPE K(8)," >KU> ",K(7)," IN-LB/RAD"
46 ACCEPT "KU= ",K(9)

The operator then selects a value within these limits and types it.

With this value of  $e_u$  and the actuator limiting values, it is now possible to find the limits on  $e_v\,.$  From equation 20

$$e_{1} = i_{11} e_{u} + i_{12} e_{v} + i_{13} e_{w}$$

$$e_{2} = i_{21} e_{u} + i_{22} e_{v} + i_{23} e_{w}$$

$$e_{3} = i_{31} e_{u} + i_{32} e_{v} + i_{33} e_{w}$$
(A-23)

or, by solving for e<sub>w</sub>,

$$e_{w} = \frac{1}{i_{13}} (e_{1} - i_{11} e_{\mu}) - \frac{i_{12}}{i_{13}} e_{v}$$

$$e_{w} = \frac{1}{i_{23}} (e_{2} - i_{21} e_{\mu}) - \frac{i_{22}}{i_{23}} e_{v}$$

$$e_{w} = \frac{1}{i_{33}} (e_{3} - i_{31} e_{\mu}) - \frac{i_{32}}{i_{33}} e_{v}$$
(A-24)

For the maximum and minimum limits of  $e_1$ ,  $e_2$  and  $e_3$ , and the specified value of  $e_u$ , these provide six curves relating  $e_w$  to  $e_v$ . The intersections of these curves determine the limits of  $e_v$ .

Initially, the slopes of the curves are determined, B(R,1). If the coefficient of  $e_1$ ,  $e_2$ , or  $e_3$  is positive, the corresponding terms, B(R,2) and B(R,3) are determined from the miminum and maximum values of the actuator spring constant, respectively. If negative, they are interchanged.

D0 49 R=1,3 B(R,1)=-I(R,2)/I(R,3) IF (I(R,3)) 48,47,47 47 B(R,2)=1/(K(R+9)\*I(R,3)) B(R,3)=1/(K(R+15)\*I(R,3)) GOTO 49 48 B(R,2)=1/(K(R+15)\*I(R,3)) B(R,3)=1/(K(R+9)\*I(R,3)) 49 CONTINUE

These would be the intercepts on the w-axis if  $e_v$  were zero. To develop the equations necessary to determine the limits, it is necessary to rearrange the three equations, (A-24), in order of decreasing slopes. A typical result is shown in figure A-1. These are labeled  $e_{w1}$ ,  $e_{w2}$  and  $e_{w3}$ , respectively. The superscripts, + and -, are used to designate the maximum and minimum values of



Figure A-1. Equation (A-24)

each of the three equations. Thus, the actual value must lie between the two curves for each equation.

In the illustration, the values of  $e_v$  and  $e_w$  must lie in the shaded area to be within the limits of all three equations. Thus, since  $e_v$  is the next value to be specified, it must be between the values determined by intersections 1 and 4. The minimum is the largest of the three labeled 1, 2, and 3. These are the intersections of maximum value of the curve with the largest slope (1+) and the minimum values of the other two (2- and 3-), and the intersection of the maximum value of the curve with the intermediate slope (2+) and the minimum value of the curve with the minimum slope (3-). These are numbered as follows:

Intersection	Curves
1	2+, 3-
2	1+, 2-
3	1+, 3-

Similarly, the three intersections which determine the maximum value of e, are numbered as follows:

Intersection	Curves	
4	2+, 1-	
5	3+, 2-	
6	3+, 1-	

These six intersections comprise all of those possible between the maximum value of one curve and the minimum value of another.

Since B(R,2) and B(R,3) have been defined such that B(R,2) corresponds to the minimum and B(R,3) the maximum elastance curve, regardles of the sign of I(R,3), these intersections are found as follows: To avoid confusion, the equations will be rewritten with the symbols used in the program. For R = 1, 2, and 3

$$e_{wr}^{+} = B(R,3) - \frac{I(R,1)}{I(R,3)} e_{u} - \frac{I(R,2)}{I(R,3)} e_{v}$$

$$e_{wr}^{-} = B(R,2) - \frac{I(R,1)}{I(R,3)} e_{u} - \frac{I(R,2)}{I(R,3)} e_{v}$$
(A-25)

The six intersections are then

.

1. 
$$e_{v} [I(2,2)I(3,3) - I(2,3)I(3,2)]$$
  
=  $e_{u} [I(2,3)I(3,1) - I(2,1)I(3,3)] +$   
+  $I(2,3)I(3,3) [B(2,3) - B(3,2)]$   
2.  $e_{v} [I(1,3)I(3,2) - I(1,2)I(3,3)]$   
=  $e_{u} [I(1,1)I(3,3) - I(1,3)I(3,1)] +$   
+  $I(3,3)I(1,3) [B(3,2) - B(1,3)]$   
3.  $e_{v} [I(1,2)I(2,3) - I(1,3)I(2,2)]$   
=  $e_{u} [I(1,3)I(2,1) - I(1,1)I(2,3)] +$   
+  $I(1,3)I(2,3) [B(1,3) - B(2,2)]$   
4.  $e_{v} [I(2,2)I(3,3) - I(2,3)I(3,2)]$   
=  $e_{u} [I(2,3)I(3,1) - I(2,1)I(3,3)] +$   
+  $I(2,3)I(3,3) [B(2,2) - B(3,3)]$ 

(A-26)

\*

.

...

.

-

5. 
$$e_{v}[I(1,3)I(3,2) - I(1,2)I(3,3)]$$
  
=  $e_{u}[I(1,1)I(3,3) - I(1,3)I(3,1)] +$   
+  $I(3,3)I(1,3) [B(3,3) - B(1,2)]$ 

6. 
$$e_{v}[I(1,2)I(2,3) - I(1,3)I(2,2)]$$
  
=  $e_{u}(I(1,3)I(2,1) - I(1,1)I(2,3)] +$   
+  $I(1,3)I(2,3) [B(1,2) - B(2,3)]$ 
(A-26)

By introducing the cofactors of the matrix, I, these can be rewritten as

$$G(1,1)e_{v} = B(1,4) + G(2,1)e_{u}$$

$$G(1,2)e_{v} = B(2,4) + G(2,2)e_{u}$$

$$G(1,3)e_{v} = B(3,4) + G(2,3)e_{u}$$

$$G(1,1)e_{v} = B(1,5) + G(2,1)e_{u}$$

$$G(1,2)e_{v} = B(2,5) + G(2,2)e_{u}$$

$$G(1,3)e_{v} = B(3,5) + G(2,3)e_{u}$$

(A-27)

The program next calculates the six intercepts

B(1,4)=G0\*I(2,3)\*I(3,3)\*(B(2,3)-B(3,2)) B(2,4)=G0\*I(3,3)\*I(1,3)\*(B(3,2)-B(1,3)) B(3,4)=G0\*I(1,3)\*I(2,3)\*(B(1,3)-B(2,2)) B(1,5)=G0\*I(2,3)\*I(3,3)\*(B(2,2)-B(3,3)) B(2,5)=G0\*I(3,3)\*I(1,3)\*(B(3,3)-B(1,2)) B(3,5)=G0\*I(1,3)\*I(2,3)\*(B(1,2)-B(2,3)) The six values of  $e_v$  from these equations, for the specified value of  $e_u$ , are now calculated and assigned to the array, L. These values are repeated for L(7) through L(12) for later calculations (statement 61).

To separate these values of  $e_u$  into those representing maximum and minimum limits, it is necessary to determine the order of magnitude of the slopes. Six cases are possible, defined by assigning a value to the variable, Q, as follows:

<u>Q</u>			<u>Order</u>		
0	B(1,1)	≥	B(2,1)	≥	B(3,1)
1	B(1,1)	≥	~B(3,1)	>	B(2,1)
2	B(3,1)	>	B(1,1)	≽	B(2,1)
3	B(3,1)	>	B(2,1)	>	B(1,1)
4	B(2,1)	≥	B(3,1)	>	B(1,1)
5	. B(2,1)	>	B(1,1)	≥	B(3,1)

	IF (B(1,1)-B(2,1)) 56.51.51
.51	IF $(B(1,1)-B(3,1))$ 55,52,52
52	IF $(B(2,1)-B(3,1)) = 54,53,52$
53	Q=0
	GOTO 61
54	Q=1
-	GOTO 61
55	Q=2
	GOTO 61
56	IF (B(2,1)-B(3,1)) 60.57.57
57 ·	IF $(B(1,1)-B(3,1))$ 59.58.58
58	Q=5
	GOTO 61
59	Q=4
	G0T0 61
60	Q= 3

The values of  $e_{11}$  corresponding to maximum limits of  $e_{11}$  are then L(1 + Q), L(2 + Q), and L(3 + Q). Those corresponding to minimum limits are L(4 + Q), L(5 + Q), and L(6 + Q). The smallest of the maximum and the largest of the minimum are found by using the Fortran functions, AMIN1 and AMAX1.

61 D0 62 R=1,6 K(R+21)=L(R+Q)
62 CONTINUE K(7)=1/AMIN1(K(22),K(23),K(24)) K(6)=1/AMAX1(K(25),K(26),K(27))

The limits of  $k_v$  are then typed and a value requested.

	IF (N(2)-3)	63,63,64	
63	TYPE K(8),"	>KV> ",K(7),"	LB/IN"
	GOTO 65		
64	TYPE K(8),"	>KV> ",K(7),"	IN-LB/RAD"
65	ACCEPT "KV=	",K(1Ø)	

The operator then types his choice.

Now, given the values of  $k_u$  and  $k_v$ , three values of the maximum and minimum limits for  $k_w$  can be found directly from the equations, (A-25). The smallest maximum and largest minimum are again selected by the Fortran routines AMIN1 and AMAX1.

D0 66 R=1,3 K(R+21)=B(R,2)-I(R,1)/(I(R,3)\*K(9))+B(R,1)/K(10) K(R+24)=K(R+21)+B(R,3)-B(R,2) 66 CONTINUE K(7)=1/AMIN1(K(22),K(23),K(24)) K(8)=1/AMAX1(K(25),K(26),K(27))

The limits for  $k_w$  are then typed, and an input value is requested.

	IF (N(3)-3)	67,67,68	
67	TYPE K(8),"	>KW> ",K(7),"	LB/IN"
	GOTO 69		
68	TYPE K(8),"	>KW> ",K(7),"	IN-LB/RAD"
69	ACCEPT "KW=	">KCID	

This choice is then typed by the operator.

7Ø

The actuator spring constants are now calculated from the three input values and equations, (A-20).

D0 70 R=1,3 SK(R)=1/(I(R,1)/K(9)+I(R,2)/K(10)+I(R,3)/K(11)) SK(R+3)=SK(R) CONTINUE

These values are then typed by the printer, and control is again transferred to the operator.

	WRITE (10,71)			
71	FORMAT (17HØSPRING CONSTAN	ITS //)		
	WRITE (10,72) SK(2), SK(3),	SK(6)	1 m	
72	FORMAT (" K1="F10.2" K2= WRITE (10.73) SK(5),SK(4),	="FIؕ2"	K3="F10.2"	LB/IN")
73	FORMAT (" K4="F10•2" K5= Q0=2 GOTO 28	="F10.2"	K6="F10.2"	LB/IN")

Elastance at Input Coordinate System

The first section of part 3 of the program calculates the full 6 x 6 matrix of elastance values as measured at the input system. As previously described from the Math Model, the impedance (elastance) of the input system is given by

 $Z = AZ_{\rho}A_{+}$ (A-28)

The impedance of the actuators is a diagonal matrix of the individual actuator elastances. The program calculates the input elastance as follows, after which it types the values and returns control to the operator.

8Ø	WRITE (10,81)
81	FORMAT (19H0ELASTANCE AT INPUT //)
	DO 82 R=1.6
	DO 82 S=1.6
	$H(R,S)=\emptyset$ .
	DO 82 P=1.6
	H(R,S)=H(R,S)+A(R,P)*A(S,P)/SK(P)
82	CONTINUE
	WRITE (10,83)((H(R,S),S=1,6)R=1,6)
83	FORMAT (6E12.6)
	QØ= 3
	GOTO 28

Actuator Static Forces and Lengths

The next section, statements 90 to 98 and 207 to 226, calculates the actuator forces due to gravity and the resultant extensions due to the finite spring constants. These extensions are inputed (manually) to the servo systems to return the triogonal system to neutral. This same calculation is used as part of the on-line program (in which the results are inputed to the servo systems automatically) and will be discussed later in detail. Statements 90 to 98 serve to input data required for the off-line calculation and to type out the results. On entering this section, the gimbal pitch and yaw angles are requested.

90 TYPE " <15> " ACCEPT "GIMBAL PITCH ANGLE: ",X(5,5), 1 "GIMBAL YAW ANGLE: ",X(6,5)
These are typed by the operator, converted to radians, and assigned to the variables A2 and A1. The integer, Q0, is assigned the value 4 to identify the offline calculation, and N(4) is assigned the value zero to signify that the platform adapter pitch angle is fixed.

> QØ=4 N(4)=Ø A2=DTR\*X(5,5) A1=DTR\*X(6,5) GOTO 207

## PARAMETER DTR=.1745329E-1

On completing the calculations, the program returns to statement 92, types out the results, and returns control to the operator.

92	WRITE (10,93)	
93	FORMAT (23HØACTUATOR STATIC FORCES //)	· ·
	WRITE (10,94) ACTF(2), ACTF(3), ACTF(6)	
94	FORMAT (" F1="F9.2" F2="F9.2" F3="F9.2"	LB")
•	WRITE (10,95) ACTF(5), ACTF(4), ACTF(1)	
95	FORMAT (" F4="F9.2" F5="F9.2" F6="F9.2"	LB")
	WRITE (10,96)	
96	FORMAT (17HØACTUATOR LENGTHS //)	
	WRITE (10,97) LGTH(2),LGTH(3),LGTH(6)	
97	FORMAT (" L1="F8.6" L2="F8.6" L3="F8.6"	IN")
	WRITE (10,98) LGTH(5),LGTH(4),LGTH(1)	
98	FORMAT (" L4="F8.6" L5="F8.6" L6="F8.6"	IN")
	GOTO 28	

On-Line Program

The remainder of part 3 of the program performs the on-line calculations. On entering this section at statement 200, the operator is queried as to whether the platform adapter pitch angle is fixed or variable.

> 200 WRITE (10,201) 201 FORMAT (16H0ON-LINE PROGRAM //) Q0=5 ACCEPT "PITCH ANGLE FIXED (0) OR VARIABLE (1) ?",N(4)

This is the angle between the platform and the vehicle (platform adapter pitch angle), not the gimbal pitch angle. It will normally be fixed for the helicopter and variable for the combat vehicle. The operator responds with either a zero or one. If zero (fixed angle), the program jumps to statement 206. If one (variable angle), it calculates portions of the matrix, A, not involving the platform adapter pitch angle.

Starting with statement 202, the transformation from input system to platform system is formed. This is the same calculation as in part 2 of the program.

IF (N(4)) 206,206,202 202 CALL ANGLE(E,X,4) CALL ROT(W,X,4) CALL TRANS(C,E,W,2)

The next four statements define the angular transformation for the roll and pitch angles of the vehicle. This is expanded to the  $6 \times 6$  angular transformation

(A-29)

 $D = \begin{bmatrix} E & i & 0 \\ 0 & i & E \end{bmatrix}$  X(4,8) = X(4,7) X(5,8) = X(5,7)  $X(6,8) = \emptyset.$ CALL ANGLE(E,X,8) CALL TRANS(D, E,W,3)

The matrices C and D are then multiplied, to produce the matrix, H.

CALL MULT (C, D, H, 6)

The angular transformation for the vehicle yaw angle is next formed.

X(4,8)=Ø. X(5,8)=Ø. X(6,8)=X(6,7) CALL ANGLE(E,X,8)

This is combined with the rotational matrix for the interface location to form the partial transformation, C, which in turn is postmultiplied by the triogonal transformation.

> CALL ROT(W,X,7) CALL TRANS(C,E,W,2) CALL MULT(C,F,H1,6)

At this point, statement 206, the program is resumed for fixed as well as variable pitch angle. The three time variable angles, gimbal pitch and yaw, and platform adapter pitch, are next read in by the A/D converter.

206	DO 208 R:	=0,2	
A	LDA	Ø,T.+2,3	JR
A	DOAS	Ø,ADCV	
A	SKPDN	ADCV	
A	JMP	• <del>-</del> 1	
A	DIC	ØJADCV	
A	STA	Ø, T. + 1, 3	;5
	ANG(R+1):	= S	
208	CONTINUE		

The DO-loop sequentially sets R equal to 0, 1, and 2. These values are loaded into the A register of the A/D converter (channel number), and the conversion is started. The program waits until the done flag is set, when the converted value is loaded into accumulator zero. This is then temporarily stored in the runtime

stack at the location allocated for the variable, S. Finally, it is assigned to the appropriate element of the array, ANG.

The gimbal pitch and yaw angles are next converted to radians. These are scaled for full scale values of  $\pm$  50° in pitch and  $\pm$  75° in yaw. Calculation of the gravitational forces follows the development of the Math Model. The basic equation relating the actuator force to the various components which comprise the load is

$$\mathbf{f}_{\ell} = \mathbf{m} \mathbf{F}_{t} \mathbf{H}_{t} (\mathbf{x}_{3}, \mathbf{r}) \left( -\frac{\mathbf{g}_{v}}{\mathbf{0}} - \right)$$
 (A-30)

where  $H(x_3, r)$  is the transformation from the platform system to the CM of the particular component, F is the triogonal transformation, and  $g_v$  is the gravitational vector at the CM of the component. It is given by

$$g_v = E(x_3) E(x_{3G}) g_e$$
 (A-31)

where  $\mathbf{x}_{3G}$  is the set of gimbal Euler angles and  $\mathbf{g}_{e}$  is the earth's gravitational vector.

$$g_{e} = \begin{pmatrix} 0\\0\\g \end{pmatrix}$$
(A-32)

The gravitational vector referred to the gimbal system is

$$g_{G} = E(x_{3G}) g_{e} = g \begin{bmatrix} -\cos \psi_{G} \sin \theta_{G} \\ \sin \psi_{G} \sin \theta_{G} \\ \cos \theta_{G} \end{bmatrix}$$
(A-33)

Since the rectilinear transformation is given by

$$H(x_3, r) = \left[\frac{E(x_3)}{0} + \frac{1}{1} - \frac{W(r) E(x_3)}{E(x_3)}\right]$$
(A-34)

its transpose is

$$H_{t}(x_{3}, r) = \begin{bmatrix} E'(x_{3}) & 0 \\ -E'(x_{3})W(r) & E'(x_{3}) \end{bmatrix}$$
(A-35)

Equation 30 can then be simplified to

$$f_{g} = mF_{t} \left[ \frac{1}{E'(x_{3})} \frac{1}{W(r)} \frac{1}{E(x_{3})} \frac{1}{V(r)} \frac{1}{E(x_{3})} \frac{1}{V(r)} \frac{1}{E(x_{3})} \frac{1}{V(r)} \frac{1}{E(r)} \right] \left( \frac{g_{G}}{0} \right)$$
(A-36)

or

$$f_{\ell} = mF_{t} \begin{bmatrix} \frac{1}{W[E'(x_{3})r]} \end{bmatrix} g_{G}$$
(A-37)

as measured in the platform system, the forces and moments are

$$f_{p} = m \left[ \frac{1}{W[E'(x_{3}) r]} \right] g_{G}$$
(A-38)

Thus, the three forces are simply

$$\begin{pmatrix} f_{x} \\ f_{y} \\ f_{z} \end{pmatrix} = mg_{G}$$
(A-39)

and the moments are

$$\begin{pmatrix} m_{\phi} \\ m_{\theta} \\ m_{\psi} \end{pmatrix} = mW [E'(x_3) r] g_G$$
(A-40)

The gimbal gravitational unit vector is calculated first. This is assigned to the first three elements of the second row of the matrix, B.

A2=ANG(1)/2346.835 A1=ANG(2)/1564.557 207 CA1=COS(A1) SA1=SIN(A1) SA2=SIN(A2) B(2,1)=-CA1\*SA2 B(2,2)=SA1\*SA2 B(2,3)=COS(A2)

At this point, the program jumps to statement 219 if the pitch angle is fixed; otherwise, it continues with statement 211. Statements 211 to 219 complete

the calculation of the A matrix, using the variable pitch angle, ANG(3). New values of actuator spring constant are then calculated to reflect the change in pitch angle.

The platform adapter pitch angle, as measured by the A/D converter is first converted to degrees. Full scale represents  $\pm$  15 degrees. The angular transformation for this value is then formed and the full 6 x 6 angular transformation is generated.

IF (N(4)) 219,219,211 211 A3=ANG(3)/136.5333 X(5,8)=A3 X(6,8)=Ø. CALL ANGLE(E,X,8) CALL TRANS(C,E,W,3)

This is then postmultiplied by the matrix, Hl, and premultiplied by the matrix, H, to form the matrix A which is used for time varying pitch angles. The corresponding G matrix and its inverse are then also calculated.

CALL MULT(C,H1,D,6) CALL MULT(H,D,A,6) D0 213 R=1,3 D0 213 S=1,3 G(R,S)=A(N(R),S)\*A(N(R),S)+A(N(R),S+3)\*A(N(R),S+3) 213 CONTINUE CALL INV(I,G,GØ)

The new values of actuator spring constant are calculated from this matrix, I, and the previously inputed spring constants for the input system. If the variable pitch angle forces the actuator spring constants to exceed their physical limits, they are modified to these values.

> D0 214 R=1.3 SK(R) = 1/(I(R, 1)/K(9) + I(R, 2)/K(10) + I(R, 3)/K(11))214 CONTINUE D0 250 R=1,3 IF (SK(R)-K(R+15)) 216,216,215 215 SK(R) = K(R+15)216 IF (SK(R)-K(R+9)) 217,218,218 217 SK(R) = K(R+9)218 SK(R+3)=SK(R)250 CONTINUE

At this point, the measured platform adapter pitch angle is added to the fixed value previously typed in during part 1. This allows for any initial pitch angle between the vehicle coordinate system and the platform system, when the platform adapter pitch angle, as measured by the A/D converter, is zero. This initial value must be inputed in part 1 before going to the on-line program, in response to the query: "Platform Adapter Euler Angles." If the pitch angle is fixed, statement 219 selects only the fixed value from part 1.

A2=X(5,7)+A3 GOTO 220 219 A2=X(5,7)

From this point on, the program continues for both fixed and variable pitch angles. For fixed angles, it uses the values of actuator spring constant calculated in part 2.

The transpose of the angular transformation from platform to interface

220 X(4,8)=X(4,7) X(5,8)=A2 X(6,8)=X(6,7) CALL ANGLE(E,X,8)

is postmultiplied by the distance from the interface origin to the vehicle CM, and the result added to the distance from the platform to the interface.

CALL DIST(E,X(1,3),X(2,3),X(3,3),X(1,8),X(2,8),X(3,8)) D0 221 R=1,3 X(R,8)=X(R,8)+X(R,7) 221 CONTINUE

This gives the distance from the platform to the vehicle CM in platform coordinates which is shown as

 $r = E' (x_{3y}) r_y + r_T$ 

(A-41)

The rotational matrix of this is then formed.

CALL ROT(W.X.8)

When multiplied by the gimbal gravitational vector and the weight of the vehicle, this will give the platform moments due to the vehicle. Multiplying the gimbal gravitational vector by the weight of the vehicle gives the platform forces. These forces and moments are stored in the array, PLF.

	DO 233 R=1.6
	$PLF(R) = \emptyset$ .
233	CONTINUE
	Q=3
223	CALL DIST(-W,B(2,1),B(2,2),B(2,3),B(2,4),B(2,5),B(2,6))
	DO 222 R=1.6
	PLF(R) = PLF(R) + B(2,R) * WGT(Q)
222	CONTINUE

The integer, Q, equal to 3 identifies the vehicle in the above equations. It is now decremented by one to the value 2, and the rotational matrix for the platform adapter is formed.

Q=Q-1 IF (Q) 224,235,234 234 CALL ROT(W,Y,Q) GOTO 223 The program then loops back to statement 223. This causes the contribution of the platform adapter to be added to the platform forces and moments. The integer, Q, is again decremented by one to the value one (signifying the platform) and the program loops once more. This adds the contribution of the platform.

At this point, Q is decremented to zero, and the program jumps to statement 235. This adds the contribution of the actuators, decrements the value of Q to minus one and jumps to statement 224.

> 235 X(1,8)=0. X(2,8)=0. X(3,8)=ALOC CALL ROT(W,X,8) WGT(0)=AWGT GOTO 223

> > DATA AWGT, ALOC/529.2845, -13.22399/

The platform forces and moments are now multiplied by the triogonal transformation to give the actuator forces.

> 224 D0 226 R=1,6 ACTF(R)=Ø. D0 255 S=1,6 ACTF(R)=ACTF(R)+F(S,R)\*PLF(S) 255 CONTINUE

These are divided by the actuator spring constants to give the actuator extensions.

> LGTH(R)=ACTF(R)/SK(R) 226 CONTINUE

At this point, if the variable, QO, is equal to 4, which signifies the off-line calculation, the program returns to statement 92. Otherwise it continues. To output the data in the order in which the actuators are pysically numbered, the index, R, is equated sequentially to the values stored in the array ACTN.

IF (Q0-4) 256,92,256 256 D0 246 S=1,6 R=ACTN(S)

The range of the spring constants is now determined. If it is equal to or greater than 10,000 lb/in., the program jumps to statement 228; otherwise, the value is scaled for a full scale value of 10,000 and stored in the array, IVAL. The corresponding bit of the variable, RANGE, is cleared, to indicate that this value is measured with the low range. If the spring constant is greater than 10,000, it is scaled for a full scale value of 200,000 lb/in., and the corresponding bit of RANGE is set to one.

•	IF (SK(R)-10000.) 227,228,228
227	IVAL(R+1)=.4096*SK(R)
**	CALL ICLR(RANGE,S)
	GOTO 229
228	IVAL(R+1) = .02048 * SK(R)
	CALL ISET (RANGE, S)

The six least significant bits of the variable, RANGE, are used to indicate range values. The first, bit 15, applies to actuator number one. The sixth, bit 10, applies to actuator number 6.

As a precaution against exceeding the D/A input range due to converting from real to integer values, the integer result is checked against the full scale input values.

229 IF (IVAL(R+1)-7777K) 240,240,230 230 IVAL(R+1)=7777K

The actuator lengths are then scaled to a full scale value of  $\pm$  5 inches, and again, the integer values limited to the full scale input values.

240	$IVAL(R+7) = -409 \cdot 6 * LGTH(R)$
	IF (IVAL(R+7)-3777K) 242,242,241
241	IVAL(R+7) = 3777K
242	IF (IVAL(R+7)-174000K) 243,244,244
243	IVAL(R+7)=174000K

Next, the mass load inputs to the servos are calculated, scaled to a full scale value of 1.5 lb  $\sec^2/in$ , and limited to the maximum permissible value.

244	IVAL(R+13)=-3072/M(R,R)	
	IF (IVAL(R+13)-174000K)	245,246,246
245	IVAL (R+13)=174000K	
246	CONTINUE	

After all six spring constant ranges have been established in the DO-loop terminated by statement 246, the variable, RANGE, is stored in the first element of IVAL.

## IVAL(1)=RANGE

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The 19 values in the array, IVAL, are then outputed to the D/A converter, using the integer S (for which the location in the run-time stack is known) as temporary storage, both for the subaddress and for the data. Initially, the D/A sub-address is loaded into the D/A "A" register.

DO 249 R=1,19 S=IADDR(R) A DOA Ø,65

DATA IADDR/21K, 224K, 22K, 222K, 24K, 223K, 23K, 227K, 25K, 225K, 1 27K, 226K, 26K, 232K, 30K, 230K, 32K, 231K, 31K/

.

DIOS SLOT NO.	FUNCTION
5	RANGE
11B .	k <sub>6</sub>
7A	, k <sub>1</sub>
7B	· k <sub>2</sub>
11A	k <sub>5</sub>
9B	k4
<b>9</b> A	k <sub>3</sub>
17B	l
13A	۹. ۱
13B	£
17A	. 2 <u>5</u>
15B	L.
15A	L L
23B	<sup>m</sup> 6
19A	m <sub>1</sub>
19B	m <sub>2</sub>
23A	m <sub>s</sub>
21B	m <sup>w</sup> .
21A	. <sup>m</sup> a
•	<b>J</b>

Physically, the D/A outputs are arranged in the same order as the actuators are numbered. The data is updated in the order in which calculations are performed (symmetrical system).

Next the data is loaded into the D/A "B" register.

S=IVAL(R) A DOB Ø,65 249 CONTINUE

•

The Fortran compiler automatically loads the value of S into accumulator zero before storing it in the run-time stack when executing the instructions

$$S = IADDR(R)$$

and

$$S = IVAL(R)$$

Thus, there is no need to load accumulator zero with these values again, before outputing it to the D/A converter (device code 65).

This completes the on-line routine, except to loop back to the beginning (statement 206) to start another cycle. The escape routine

Α	. SKP DN	TTI
Α	JMP	LOOP
Α	NIOC	TTI
	GOTO 28	

allows the operator to break the loop and regain control, by stiking any key on the teletype. This sets the "done" flag causing the program to jump to statement 28, after clearing the teletype. If the "done" flag has not been set, the program jumps to the label "LOOP", which returns the program to statement 206.

> A LOOP: GOTO 206 END

COMPUTER PROGRAM FOR CONTROL OF 6-DOF SIMULATOR REPORT C3703, August, 1976

С

MAIN PROGRAM - 6 DOF SIMULATOR (RIA) - PART 1 PARAMETER DTR=-1745329E-1 COMMON/FXV/F(6,6), AM(6,6), AWGT, ALOC, IADDR(19), ACTN(6) DIMENSION A(6,6), ACTF(6), B(3,6), C(6,6), D(6,6), 1 = (3, 3), G(3, 3), H(6, 6), H1(6, 6), H2(3, 3), I(3, 3), IVAL(19),2 J(3,3),K(27),L(12),LGTH(6),M(6,6),M0I(6,3),N(4), 3 PLF(6), ANG(3), SK(6), W(3,3), WGT(0:3), X(6,8) INTEGER ANG, Q, QØ, P, P, S, ACTN, RANGE REAL I.J.K.L.LGTH.M.MOI EXTERNAL MULT, ROT, ANGLE, INERTIA, INV, DIST, ISET, ICLR, 1 TRANS, TRNSP, ZERO, UNIT DATA F/5.107058E-2,-.530741,.2156135,3.685701E-3, 1 -1.347696E-2,-8.511763E-3,-.4851705,-.2211421,.2156135, 2 1·351424E-2, 3·546568E-3, 8·511763E-3, ·4340999, ·3095989, **3** • 2156135, 9 • 828537E-3, 9 • 93Ø39E-3, -8 • 511763E-3, 4 5·107058E-2,·530741,·2156135,-3·685701E-3,-1·347696E-2, 5 8.511763E-3, -. 4851705, . 2211421, . 2156135, -1. 351424E-2, 6 3·546568E-3,-8·511763E-3, 4340999,-·3095989, 2156135, 7 -9.828537E-3,9.93039E-3,8.511763E-3/ DATA AM/1.90045,3\*0.,.7996739,2\*0.,1.90045,0.,-.7996739, 1 4\*0+,1+658009,4\*0+,-+7996739,0+,813+2535,2\*0+,7996739, 2 3\*0+,813+2535,6\*0+,1750+554/ DATA AWGT, ALOC/529.2845, -13.22399/ DATA IADDR/21K, 224K, 22K, 222K, 24K, 223K, 23K, 227K, 25K, 225K, 1 27K, 226K, 26K, 232K, 30K, 230K, 32K, 231K, 31K/ DATA ACTN/2,3,6,5,4,1/ TYPE " SIX DOF SIMULATOR <15> " 28 TYPE " <15> " ACCEPT "\*",0 IF (Q-1) 28,231,29 29 IF (Q-Q0-1) 231,231,232 232 IF (0-6) 28,231,28 231 GOTO (2,30,80,90,200) Q 2 WRITE (10,4) 4 FORMAT (15HØCONFIGURATION //) ACCEPT "LOCATION OF CM <15>"," PLATFORM: <15>", 1 (X(R,1),R=1,3)," PLATFORM ADAPTER: <15>",(X(R,2),R=1,3), 2 " VEHICLE: <15>", (X(R,3), R=1,3), "PLATFORM ADAPTER <15>", 3 " LOCATION OF VEHICLE INTERFACE: <15>", (X(R,7), R=1,3), 4 \*\* EULER ANGLES: <15>", (X(R,7),R=4,6), "WEIGHTS <15>", 5 " PLATFORM: ", WGT(1)," PLATFORM ADAPTER: ", WGT(2), 6 '' VEHICLE: ", WGT(3), "MOMENTS OF INERTIA <15>", 7 " PLATFORM: <15>", (MOI(R,1),R=1,6), 8 " PLATFORM ADAPTER: <15>", (MOI(R,2), R=1,6),

9 " VEHICLE: <15>", (MOI(R,3),R=1,6)

	D0 6 R=1,6
	D0 6 S=1,6
	M(R,S) = AM(R,S)
6	CONTINUE
	CALL ROT(W,X,3)
	CALL ANGLE(E,X,7)
	CALL TRANS(C, E, W, 1)
	CALL ROT (W, X, 7)
	CALL UNIT(E)
	CALL TRANS(D, E, W, 1)
	CALL MULT(C,D,H,6)
	Q=3
11	CALL INERTIA(J,MOI,Q)
	CALL ZERO(C,6)
	DO 14 R=1.3
	DO 14 S=1.3
	C(R+3,S+3)=J(R,S)
	IF (R-S) 14,12,14
12	C(R,S)=WGT(Q)/386.063
14	CONTINUE
	CALL MULT(C, H, H1, 6)
	CALL TRNSP(C,H,6)
	CALL MULT(C,H1,H,6)
	DO 16 R=1.6
	D0 16 S = 1.6
	M(R, S) = M(R, S) + H(R, S)
16	CONTINUE
	$\mathbf{Q} = \mathbf{Q} - 1$
-	IF (Q) 21,21,17
17	CALL ROT(W,X,Q)
	CALL UNIT(E)
	CALL TRANS(H, E, W, 1)
	GOTO 11
21	CALL TRNSP(C,F,6)
	CALL MULT(C,M,H,6)
	CALL MULT(H, F, M, 6)
	DO 23 R=1.6
	D0 23 $S=1.6$
	H1(R,S)=M(ACTN(R),ACTN(S))
23	CONTINUE
_	WRITE $(10,24)((H1(R,S),S=1,6)R=1,6)$
24	FORMAT (40H0ACTUATOR LOAD MASS MATRIX (LB-SEC+2/IN) //
	1 (6F10.4))
	$Q\emptyset = I$
	GOTO 28

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C	MAIN PROGRAM - PART 2
ЗØ	TYPE " <15> "
	DO 35 R=1.6
	K(R+15)=3947.842*M(R.R)
	K(P+Q) = K(P+15) / 1500
	IE (V(D+1E)=0, arc) 22, 22, 20
20	IF (N(N+15)=2+025) 33333332
32	K(R+15)=2.0E5
33	IF (K(R+9)-250.) 34,35,35
34	K(R+9)=250.
35	CONTINUE
	DO 39 R=1,3
	IF (K(R+15)-K(E+18)) 37,37,36
36	K(R+15) = K(R+18)
37	IF (K(R+Q) - K(R+12)) 38.30.30
28	V(P+0) - V(P+10)
20	
39	CONTINUE
	ACCEPT "ORIGIN OF INPUT SYSTEM: ", $(X(R, 4), R=1, 3)$ ,
	I "EULER ANGLES OF INPUT SYSTEM: ",(X(R,4),R=4,6)
	CALL ANGLE(E,X,4)
	CALL ROT(W,X,4)
	CALL TRANS(C, E, W, 2)
	CALL ANGLE(E,X,7)
	CALL ROT(W,X,7)
	CALL TRANS(D, F, U, 2)
	CALL MULT(C, D, H, 6)
40	WRITE (10)42)
42	FORMAT (12HOINPUT AXES= >Z)
	$= \operatorname{READ} (11) \operatorname{N}(1) \operatorname{N}(2) \operatorname{N}(3)$
	D0 43 R=1.3
•	D0 43 S=1.3
	G(R,S)=A(N(R),S)*A(N(R),S)+A(N(R),S+3)*A(N(R),S+3)
43	CONTINUE
-	CALL INV(I,G,GØ)
	K(7) = 1/(G(1,1)/K(10) + G(1,2)/K(11) + G(1,3)/K(12))
	K(8) = 1/(G(1,1)/K(16)+G(1,2)/K(17)+G(1,2)/K(12))
	IF (N(1)-3) hh.hh.h5
4/1	$TVDE K(2) \cdot V = V(2) + V(2) + V(2)$
	COLD WE SUCH SUCH SUCH SUCH SUCH SUCH SUCH SUCH
4 E	
45	TYPE K(8);" > KU> ";K(7);" IN-LB/RAD"
40	ACCEPT " $KU=$ " $K(9)$
	D0 49 R=1.3
	$B(R_{J}) = -I(R_{J}2)/I(R_{J}3)$
	IF (I(R,3)) 48,47,47
47	B(R,2)=1/(K(R+9)*I(R,3))
. :	B(R,3)=1/(K(R+15)*I(R,3))
	GOTO 49
48	$B(R_2)=1/(K(R+15)*I(R_2))$
	B(B,3) = 1/(K(B+0) + 1(B,2))
49	CONTINUE
-17	
	B(0, 4) = C(0+1)(2+3) + 1(3+3) + (B(2+3) - B(3+2))
	B(2) = GU + 1(3) + 1(1) + 3) + (B(3) + 2) - B(1) + 3)
	B(3,4)=G0*I(1,3)*I(2,3)*(B(1,3)-B(2,2))
	B(1,5)=G0*I(2,3)*I(3,3)*(B(2,2)-B(3,3))
	·B(2,5)=GØ*I(3,3)*I(1,3)*(B(3,3)-B(1,2))
	B(3,5)=G0*I(1,3)*I(2,3)*(B(1,2)-B(2,3))

•

	D0 50 R=1.3
	D0 50 S = 1.2
	L(R+3*(S-1)) = (B(R,S+3)+G(2,R)/K(9))/G(1,R)
	1(R+3*(S+1))=1(R+3*(S-1))
ea	CONTINUE
90	LUNIINUL 10 (D(1 1)-D(0 1)) E6 E1 E1
	IF (B(1)1)-B(2)1)) 50/51/51
51	IF (B(1,1)-B(3,1)) 55,52,52
52	IF $(B(2,1)-B(3,1))$ 54,53,53
53 -	Q=Ø
	GOTO 61
54	Q=1
	GOTO 61
55	Q=2
	G0T0 61
56	IF $(B(2,1)-B(3,1)) = 60,57,57$
57	IF (B(1,1)-B(3,1)) 59.58.58
57	0-5
50	
50	
59	
	GOTO 61
60	Q=3
61	D0 62 $R=1.6$
	K(R+21)=L(R+Q)
62	CONTINUE
	K(7)=1/AMIN1(K(22),K(23),K(24))
	K(8)=1/AMAX1(K(25),K(26),K(27))
	IF $(N(2)-3)$ 63,63,64
63	TYPE $K(8)$ , ">KV> ", $K(7)$ ," LB/IN"
Ū,	6070 65
64	TYPE $K(8)$ , "> $KU$ > ", $K(7)$ ," IN-1.B/RAD"
65	$ACCEPT "KU = " \cdot K(10)$
05	$\frac{1}{100} \frac{1}{100} \frac{1}$
	V(D+01) = D(D-0) = T(D-1)/(T(D-2)+V(0)) + D(D-1)/V(10)
	$K(R_{1}/2I) = D(R_{2}/2) = I(R_{2}/2) + D(R_{2}/2) + D($
	K(R+24) = K(R+21) + B(R+3) - B(R+2)
66	
	K(7) = 17 AMIN 1 (K(22)) K(23) K(24))
	K(8) = 1/AMAX1(K(25)) K(26) K(27))
	IF $(N(3)-3) = 67, 67, 68$
67	TYPE K(8)," > KW> ", K(7)," LB/IN"
	GOTO 69
68	TYPE K(8)," >KW> ",K(7)," IN-LB/RAD"
69	ACCEPT "KW= ",K(11)
	DO 70 R=1.3
	SK(R)=1/(I(R,1)/K(9)+I(R,2)/K(10)+I(R,3)/K(11))
	SK(R+3)=SK(R)
70	CONTINUE
	WRITE (10.71)
71	FORMAT (17H0SPRING CONSTANTS //)
11	$\frac{1}{10} \frac{1}{10} \frac$
70	
12	FURMALL ALE FID-2: $KZ="FID-2"$ $KJ="FID-2"$ LB/IN")
<b>a</b> 0	WRITE (10)737 SK(5)/SK(4)/SK(1)
73	FURMAT (" K4="F10.2" K5="F10.2" K6="F10.2" LB/IN")
	Q0=2
	GOTO 28

C	MAIN PROGRAM - PART 3	
8Ø	WRITE (10,81)	
81	FORMAT (19HØELASTANCE AT INPUT //)	٠
	DO 82 R=1.6	
•	D0 82 S=1.6	
	H(R,S)=0	
1	$D0 \ B2 \ P=1 = 6$	
1	H(R,S)=H(R,S)+A(R,P)*A(S,P)/SK(P)	
82	CONTINUE	
	WRITE (10,83)((H(R,S),S=1,6)R=1,6)	
83	FORMAT (6E12.6)	
	Q0=3	
	GOTO 28	
90	TYPE " <15> "	
	AUGEPT "GIMBAL PITCH ANGLE: JA(5)5/3	
	I "GIMBAL YAW ANGLE: JA(0)57	
	Q = 4	
	N(4)=0	
	AZ = DTR + A(5) + 5	
	$\mathbf{A1} = \mathbf{D1} \mathbf{K} + \mathbf{X} \mathbf{(0)} 57$	
00	1010207	
92	FORMAT (23HØACTHATOR STATIC FORCES //)	
	MRITE (10.94) ACTE(2), ACTE(3), ACTE(6)	
0/1	FORMAT (" FI="F9.2" F2="F9.2" F3="F9.2"	LB")
	WRITE $(10,95)$ ACTF $(5)$ , ACTF $(4)$ , ACTF $(1)$	
95	FORMAT (" F4="F9.2" F5="F9.2" F6="F9.2"	LB")
20	WRITE (10,96)	
96	FORMAT (17HØACTUATOR LENGTHS //)	
	WRITE (10,97) LGTH(2), LGTH(3), LGTH(6)	
97	FORMAT (" L1="F8.6" L2="F8.6" L3="F8.6"	IN")
	WRITE (10,98) LGTH(5),LGTH(4),LGTH(1)	
98	FORMAT (" L4="F8.6" L5="F8.6" L6="F8.6"	IN")
*	GOTO 28	
200	WRITE (10,201)	
201	FORMAT (16HØON-LINE PROGRAM //)	
	QØ=5	
	ACCEPT "PITCH ANGLE FIXED (Ø) OR VARIABLE (1	) ?",N(4)
_	IF (N(4)) 206,206,202	
202	CALL ANGLE(E, X, 4)	
	CALL ROT(W,X,4)	
	CALL TRANS( $C_{1}E_{2}V_{2}$ )	
	X(4,8) = X(4,7)	
	X(5,8)=X(5,7)	
	X(6,8)=0.	
	CALL ANGLE(E, X, 8)	
	CALL TRANS (D) E) W3 3)	
	CALL MULT(C, D, H, 6)	
	X(4,8)=0.	
· .		
	$A \setminus O \setminus O = A \setminus O \setminus I$	
•	CALL BOT (U.Y.7)	- *
	CALL RUISWAAAAA $(A = 1)$	
т.;	CALL MILT(C, $F$ , $H$ ) $A$	<u> </u>

206	DO 208 R=	=Ø,2							•
A	LDA	Ø, T. +2, 3		;;	2				
А	DOAS	Ø, ADCV							
A	SKPDN	ADCV							
A	JMP	• - 1							
A	DIC	Ø, ADCV							
Δ	STA	Ø.T.+1.3			2				
л	ANG (P+1)-	- 6							
049	CONTINUE	- 5							
200		10046 805							
	AZ=ANG(1)	72346+835							
	Al=ANG(2)	)/1564.557							
207	CAI = COS(4)	A1)		60 K.u.					
	SAI=SIN(A	A1)							
•	SA2=SIN(A	A2)							
	B(2,1)=-(	CA1*SA2							
	B(2,2)=SA	A1*SA2							
	B(2,3)=C(	DS(A2)							
	IF (N(4))	) 219,219,2	211						
211	A3=ANG(3)	)/136.5333							
	X(5,8) = A(3)	3		-					
	X(6,8) = 0			*					
•	CALL ANGI	F(F, X, R)					-	a	
	CALL TRAN			54 - 45					
	CALL MULT	T(C.W1.D.6)		1			~		
	CALL MUL								
	DO OLO D								
	D0 213 R=	= 1 - 3			•				
•	DU 213 5=			<b>.</b>				in the second	
o o	G(R,S)=A	(N(R),S)*A	N(R)	ر+(S د "	ACNCR	<b>)</b>	3)*A(N	I(R), S	+3)
213	CONTINUE			-					
	CALL INV	(I,G,GØ)				**		•	
-	DO 214 R=	=1=3							
-	-SK(R)=1/0	(I(R, D)/K(9))	))+I(	R,2)	/K(1Ø	)+I(F	\$•3)/¥	$\langle (11) \rangle$	
214	CONTINUE								
	DO 250 R=	=1=3					<b>-</b> .		
	IF (SK(R)	)-K(R+15))	216,	216,	215				
215	SK(R) = K(R)	R+15)							
216	IF (SK(R)	)-K(R+9)) 2	217,2	18,2	18				
217	SK(R) = K(R)	R+9)		•					
218	SK(R+3)=9	SK(R)							
250	CONTINUE								
	A2=X(5,7)	)+A3						•	
	GOTO 220				199				
219	A2=X(5.7)	۱.			·				
2200	X(h, g) = X	(1,7)							
660									
		$\sim$							
	X(5)8)=A	2							
	X(6,8)=X	2 (6,7)							
	X(5,8)=X X(6,8)=X CALL ANGI	2 (6,7) LE(E,X,8)							
	X(5,8)=A X(6,8)=X CALL ANG CALL DIS	2 (6,7) LE(E,X,8) T(E,X(1,3),	X(2,	3)•X	(3,3)	د1) X د	8),x(8)	(2,8);	X(3,8))
	X(5,8)=A X(6,8)=X CALL ANGI CALL DIS DO 221 R	2 (6,7) LE(E,X,8) T(E,X(1,3), =1,3	X(2,	3)•X	(3,3)	د1) X د	8),X(	(2,8),	X (3, 8) )
-	X(5,8)=A X(6,8)=X CALL ANGI CALL DIS D0 221 R X(R,8)=X	2 (6,7) LE(E,X,8) T(E,X(1,3), =1,3 (R,8)+X(R,7)	X(2,	3)•X	(3,3)	د1) X د	8), X	(2,8);	X(3,8))
221	X(5,8)=A X(6,8)=X CALL ANGI CALL DIS DO 221 R= X(R,8)=X CONTINUE	2 (6,7) LE(E,X,8) T(E,X(1,3), =1,3 (R,8)+X(R,7	X(2,	3)•X	(3,3)	•X(1•	8),X(	(2,8),	X(3,8))

×#

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•	DO 233 R=1,6
	PLF(R)=0.
233	CONTINUE
	0=3
202	CALL DIST(-W, B(2, 1), B(2, 2), B(2, 3), B(2, 4), B(2, 5), B(2, 4)
220	$\frac{1}{2} \frac{1}{2} \frac{1}$
	PLF(R)=PLF(R)+B(2,R)*WGT(Q)
222	CONTINUE
	Q = Q - 1
	IF (Q) 224,235,234
234	CALL ROT(W,X,Q)
	GOTO 223
235	X(1, B) = 0
200	
	X(3,8)=ALOC
	CALL ROT(W,X,8)
	WGT(Ø)=AWGT
	GOTO 223
224	DO 226 R=1.6
	ACTF(R)=0.
	D0.255.5=1.6
	$\Delta(TF(D) - \Delta(TF(D) + F(C, D) + D) F(C))$
ÓFE	
235	
	LGTH(R)=ACTF(R)/SK(R)
226	CONTINUE
	IF (Q0-4) 256,92,256
256	DO 246 S=1,6
	R=ACTN(S)
	IF (SK(R)-10000.) 227,228,228
227	IVAL(R+1) = -4096 + SK(R)
-	CALL ICLE (BANGE S)
~ .	COTO 200
009	
220	CALLATIZ-+02040+SA(R)
000	CALL ISET (RANGESS)
229	IF (IVAL(R+1)-7777K) 240,240,230
230	IVAL(R+1)=7777K
24Ø	IVAL(R+7)=-409.6*LGTH(R)
	IF (IVAL(R+7)-3777K) 242,242,241
241	IVAL(R+7)=3777K
242	IF (IVAL(R+7)-174000K) 243,244,244
243	IVAL (R+7)=174000K
244	$V(A_1, (B+1,3)) = -3072 (M(B, P))$
	IF (IUA) (P+12) = 1740000 A O A O A O A O A O A O A O A O A O
0/15	11 + (1) + (2) + (3) - (7) + (2) +
245	IVAL(R+13)=1/4000K
246	CONTINUE
	IVAL(I)=RANGE
	D0 249 R=1,19
•	S=IADDR(R)
A	DOA Ø,65
	S=IVAL(R)
A	D0B 0,65
249	CONTINUE
Δ	
A	
А	NIUC TTI
	GOTO 28
A L00	P:
	GOTO 206
	END.

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SUBROUTINE TRANS(C, E, W, Q) DIMENSION C(6,6), E(3,3), V(3,3), H(3,3) INTEGER Q.R.S EXTERNAL MULT, ZERO GOTO (1,2,3) Q CALL MULT (W. E. H. 3) 1 GOTO 4 2 CALL MULT (E, W, H, 3) GOTO 4 CALL ZERO(H,3) 3 4 DO 5 R=1.3 DO 5 S=1,3 C(R,S) = E(R,S)C(R+3,S)=Ø. C(R, S+3) = -H(R, S)C(R+3,S+3) = E(R,S)5 CONTINUE RETURN END SUBROUTINE TRNSP(C, D, Q) INTEGER Q.R.S DIMENSION C(Q,Q),D(Q,Q) DO 1 S=1.Q C(R.C) 2.5.5 C(R,S)=D(S,R)· 1 CONTINUE RETURN END SUBROUTINE ZERO(E,Q) INTEGER Q.R.S DIMENSION E(Q,Q) DO 1 R=1.Q DO 1 S=1.Q E(R,S)=0. CONTINUE 1 RETURN END SUBROUTINE MULT(C1, D1, H5,Q) INTEGER P.Q.R.S DIMENSION Cl(Q,Q), Dl(Q,Q), H5(Q,Q)DO 1 R=1.Q DO 1 S=1.Q  $H5(R,S)=\emptyset$ . DO 1 P=1,Q H5(R,S)=H5(R,S)+C1(R,P)\*D1(P,S)1 CONTINUE RETURN EIJD 👘

```
SUBROUTINE ROT(W,X,Q)
    INTEGER Q
   DIMENSION W(3,3),X(6,8)
   V(1→1)=Ø+
   W(2,1)=X(3,0)
   W(3,1) = -X(2,0)
   W(1,2) = -X(3,0)
   W(2,2)=0.
   W(3,2) = X(1,0)
   V(1,3) = X(2,0)
   W(2,3) = -X(1,Q)
    w(3,3) = 0.
   RETURN
    END
    SUBROUTINE INERTIA(J, MOI, Q)
    INTEGER Q
    DIMENSION J(3,3), MOI(6,3)
   J(1, 1) = MOI(1, 0)
    J(2,1) = MOI(4,Q)
    J(3, 1) = MOI(5, Q)
    J(1,2) = MOI(4,Q)
    J(2,2) = MOI(2,0)
    J(3,2) = MOI(6,0)
   (J(1,3)=MOI(5,Q)
    J(2,3) = MOI(6,0)
    J(3,3) = MOI(3,Q)
   RETURN
   END
   SUBROUTINE INV(1,G,G2)
    INTEGER R.S
    REAL I
   DIMENSION I(3,3), G(3,3), H(6,6)
   DO 1 R=1.3
   DO 1 S=1.3
    H(R,S)=G(R,S)
    H(R+3,S)=G(R,S)
    H(R_{3}S+3)=G(R_{3}S)
    H(R+3, S+3) = G(R, S)
    CONTINUE
    DO 2 R=1.3
    DO 2 S=1.3
    I(4-S,4-R)=H(2*R-1,2*S-1)*H(2*R,2*S)-H(2*R-1,2*S)*H(2*R,2*S-1)
2
    CONTINUE
    G2=I(1,1)*G(1,1)+I(2,1)*G(1,2)+I(3,1)*G(1,3)
    DO 3 R=1.3
    DO 3 S=1.3
    I(R,S) = I(R,S)/G2
3
   -CONTINUE
   RETURN
    END
```

```
SUBPOUTINE DIST(E1,X1,Y1,Z1,X0,Y0,Z0)
DIMENSION E1(3,3)
X = E_1(1, 1) * X_1 + E_1(2, 1) * Y_1 + E_1(3, 1) * Z_1
YØ=E1(1,2)*X1+E1(2,2)*Y1+E1(3,2)*Z1
ZØ = E1(1,3) * X1 + E1(2,3) * Y1 + E1(3,3) * Z1
RETURN
END
SUBROUTINE ANGLE(E,X,Q)
INTEGER Q
DIMENSION E(3,3),X(6,8)
DTR=1.745329E-2
PHI=DTR*X(4,Q)
THETA=DTR*X(5,Q)
PSI=DTR*X(6,Q)
SPHI=SIN(PHI)
CPHI=COS(PHI)
STHETA=SIN(THETA)
CTHETA=COS(THETA)
SPSI=SIN(PSI)
CPSI=COS(PSI)
E(1,1)=CTHETA*CPSI
E(2,1)=SPHI*STHETA*CPSI-CPH1*SPSI
E(3,1)=CPHI*STHETA*CPSI+SPHI*SPSI
E(1,2)=CTHETA*SPSI
E(2,2)=CPHI*CPSI+SPHI*STHETA*SPSI
E(3,2)=CPHI*STHETA*SPSI-SPHI*CPSI
E(1,3) = -STHETA
E(2,3)=SPHI*CTHETA
E(3,3)=CPHI*CTHETA
RETURN
END
SUBROUTINE UNIT(E)
INTEGER R
DIMENSION E(3,3)
EXTERNAL ZERO
CALL ZERO(E,3)
DO 1 R=1.3
E(R,R)=1.
CONTINUE
RETURN
```

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END
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APPENDIX B 6-DOF MATH MODEL ACTUATOR LOAD MASS DUE TO ACTUATORS

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## EFFECTIVE MASS OF ACUTATORS

Because of the motion of the platform, the actuators experience not only motion in their axial direction, but also motion in the transverse direction and rotation about the upper pivot point. Since they have finite mass and moments of inertia, this motion requires forces to be exerted by the platform on the actuators. Since each actuator can provide only axial forces, the nonaxial forces must be provided by the other five actuators.

To derive an expression for the mass load of the actuator system upon itself, it is necessary to first determine the actuator motion in terms of the platform motion. This then determines the forces exerted on each actuator which can then be translated into the platform coordinate system and summed for all six actuators. Then by transforming the impedance of the platform into the triogonal coordinate system, the equivalent mass load on each actuator can be found.

To determine the forces exerted on the individual actuator, it is necessary to determine the linear and angular velocities. For this purpose, a coordinate system will be affixed to each actuator with the x axis along the actuator axis. An angular transformation will be defined,  $E(x_3)$ , which rotates the platform axes into each of these systems. Then, since the projection of a unit vector along the actuator into the platform system must yield the direction cosines, we have

$$\begin{pmatrix} 1\\0\\0 \end{pmatrix} = E(x_3)\delta$$
(B-1)

or

$$S = E'(x_3) \begin{pmatrix} 1\\0\\0 \end{pmatrix}$$
(B-2)

where the direction cosines are

$$\delta = \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}$$
(B-3)

For the conventional order of rotation, the angular transformation is

$$E'(x_3) = E'_1(\psi) E'_2(\theta) E'_3(\phi)$$
 (B-4)

It then follows that the direction cosines are equal to

$$\delta = \begin{bmatrix} \cos \psi \cos \theta \\ \sin \psi \cos \theta \\ -\sin \theta \end{bmatrix}$$
(B-5)

These equations can be solved for the pitch and yaw angles to give

$$\sin \theta = -\gamma$$

$$\cos \theta = \sqrt{1 - \gamma^{2}}$$

$$\sin \psi = \beta / \sqrt{1 - \gamma^{2}}$$

$$\cos \psi = \alpha / \sqrt{1 - \gamma^{2}}$$
(B-6)

By differentiating these, we have

$$\dot{\theta} = -\dot{\gamma}/\sqrt{1 - \gamma^2}$$
  
$$\dot{\psi} = (\alpha \dot{\beta} - \beta \dot{\alpha})/(1 - \gamma^2)$$
(B-7)

The angular velocities of the actuator are

$$x_2 = G'(x_3) x_3$$
 (B-8)

or

$$x_3 = G(x_3) x_2^{(B-9)}$$

where

$$G(x_3) = \begin{bmatrix} 1 & \sin \phi \tan \theta & \cos \phi \tan \theta \\ 0 & \cos \phi & -\sin \phi \\ 0 & \sin \phi \sec \theta & \cos \phi \sec \theta \end{bmatrix}$$
(B-10)

Since the actuators are mounted to the gimbal system and platform by means of ball joints, no axial torque can be applied to either the cylinder or piston. Then the roll velocity is zero which is shown as

$$\mathbf{p} = \mathbf{0} \tag{B-11}$$

The time derivatives of the Euler Angles are then

$$\begin{aligned} \phi &= q \sin \phi \tan \theta + r \cos \phi \tan \theta \\ \theta &= q \cos \phi - r \sin \phi \\ \psi &= (q \sin \phi + r \cos \phi) \sec \theta \end{aligned}$$
 (B-12)

Thus

$$\phi = \psi \sin \theta = -\gamma \psi \tag{B-13}$$

The actuator angular velocities are then

$$\mathbf{x}_{2} = \frac{1}{\sqrt{1 - \gamma^{2}}} \begin{bmatrix} 0 \\ -\gamma \cos \phi + (\alpha \beta - \beta \alpha) \sin \phi \\ (\alpha \beta - \beta \alpha) \cos \phi + \gamma \sin \phi \end{bmatrix}$$
(B-14)

The choice of roll angle is arbitrary. Normally, it should be chosen so that the y and z axes are principal axes of the actuator. For an axially symmetric actuator, any value can be used. If we choose  $\phi = 0$ , then

$$\mathbf{x}_{2} = \frac{1}{\sqrt{1 - \gamma^{2}}} = \begin{bmatrix} 0 \\ -\gamma \\ (\alpha\beta - \beta\alpha) \end{bmatrix}$$
(B-15)

The actuator consists of two parts which move relative to each other, the cylinder and the piston. The axial velocity of the cylinder is zero, while that of the piston is equal to the scalar velocity of the actuator. The angular velocities of both are equal. To find the forces exerted by the platform on the actuator, we can isolate the two parts as shown in figure B-1. If we sum forces and moments about the CM of each, we have (for a linearized analysis):

$$f_{ax} + f_{cx} = M_{a}x_{a}$$

$$f_{ay} + f_{cy} = M_{a}y_{a}$$

$$f_{az} + f_{cz} = M_{a}z_{a}$$

$$0 = J_{ax}p$$
(B-16)

$$f_{cz}(l_{o} - d_{c} - d_{a}) - f_{az}(d_{a}) + M_{cy} = J_{ay} \dot{q}$$

$$f_{ay}(d_{a}) - f_{cy}(l_{o} - d_{c} - d_{a}) + M_{cz} = J_{az}\dot{r}$$

$$f_{bx} - f_{cx} = M_{b} \dot{v}_{b}$$

$$f_{by} - f_{cy} = M_{b} \dot{v}_{b}$$

$$f_{bz} - f_{cz} = M_{b} \dot{z}_{b}$$

$$0 = J_{bx}\dot{p}$$

$$(B-16)$$

$$cont$$

$$f_{bz}(d_{b}) + f_{cz}(d_{c} - d_{b}) - M_{cy} = J_{by}\dot{q}$$

$$-f_{cy}(d_{c} - d_{b}) - f_{by}(d_{b}) - M_{cz} = J_{bz}\dot{r}$$

The linear velocities are given in terms of the velocity of the platform pivot point by

$$\mathbf{x}_{a} = \mathbf{x}$$

$$\mathbf{y}_{a} = \left(\frac{\boldsymbol{\ell}_{o} - \boldsymbol{d}_{a}}{\boldsymbol{\ell}_{o}}\right) \quad \mathbf{y}$$

$$\mathbf{z}_{a} = \left(\frac{\boldsymbol{\ell}_{o} - \boldsymbol{d}_{a}}{\boldsymbol{\ell}_{o}}\right) \quad \mathbf{z}$$

$$\mathbf{x}_{b} = 0$$

$$\mathbf{y}_{b} = \left(\frac{\boldsymbol{\ell}_{o}}{\boldsymbol{\ell}_{o}}\right) \quad \mathbf{y}$$

$$\mathbf{z}_{b} = \left(\frac{\boldsymbol{d}_{b}}{\boldsymbol{\ell}_{o}}\right) \quad \mathbf{z}$$

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(B-17)



Figure B-1. Actuator dynamics

By solving these equations for the forces exerted by the platform on the actuator, we have

$$f_{ax} = M_{a} x$$

$$f_{ay} = M_{y} + \frac{J_{z}}{\lambda_{o}} r$$

$$f_{az} = M_{z} - \frac{J_{y}}{\lambda_{o}} q$$
(B-18)

where

$$M = M_{a} \left( \frac{l_{o} - d_{a}}{l_{o}} \right)^{2} + M_{b} \left( \frac{d_{b}}{l_{o}} \right)^{2}$$

$$J_{y} = (J_{ay} + J_{by})$$

$$J_{z} = (J_{az} + J_{bz})$$
(B-19)

Thus, the actuator forces are

$$f_{a} = \begin{bmatrix} m_{a} & 0 & 0 \\ 0 & m & 0 \\ 0 & 0 & m \end{bmatrix} \stackrel{\bullet}{\underset{1}{x_{1}}} + \frac{J}{\ell_{o}} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & -1 & 0 \end{bmatrix} \stackrel{\bullet}{\underset{2}{x_{2}}}$$
(B-20)

where it has been assumed

$$J_{y} = J_{z}$$
(B-21)

These forces are still expressed in the actuator coordinate system. In the plat-form system, they are

 $f_p = E'(x_3) f_a$  (B-22)

If the forces are translated to the origin of the platform system, the moments required to compensate for the translation are

$$M_{p} = W(a) f_{p}$$
(B-23)

The total forces and moments are the sums of these for all six actuators.

The accelerations,  $x_1$  and  $x_2$  are still expressed in the actuator coordinate system. The angular velocities were found to be

The rate of change of direction cosines is

$$\delta = -W^2 (\delta) \frac{\lambda}{\lambda_0}$$
(B-25)

Thus

The linear velocities are given in terms of the vector actuator velocity by

$$\mathbf{x}_{1} = \mathbf{E}(\mathbf{x}_{3}) \overset{\flat}{\mathbf{p}} \tag{B-27}$$

But the vector actuator velocity is related to the platform velocity by

$$\ell_{p} = \chi_{1p} - W(a) \chi_{2p}$$
 (B-28)

Thus

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$$x_1 = E(x_3) \left\{ \begin{array}{c} \bullet \\ x_{1p} - W(a) \\ \end{array} \right\}$$
(B-29)

For small (linearized) motions, the accelerations are related in the same manner as the velocities. Thus, by combining the above relationships, the platform forces and moments are related to the platform accelerations by

$$\left(\frac{f}{m}\right)_{p} = \sum_{n=1}^{6} \left[ \frac{m_{An}}{W_{(an)}m_{An}} + \frac{m_{An}}{W_{(an)}} + \frac{m_{An}}{W_{(an)}} + \frac{W_{(an)}}{W_{(an)}} + \frac{W_{(an)}}{W_{(an$$

-1.44

where, for each actuator

$$\begin{split} \mathbf{m}_{A} &= \mathbf{E}^{*}(\mathbf{x}_{3}) \left\{ \begin{bmatrix} \mathbf{m}_{a} & 0 & 0 \\ 0 & \mathbf{m} & 0 \\ 0 & 0 & \mathbf{m} \end{bmatrix} \mathbf{E}(\mathbf{x}_{3}) + \\ &- \frac{\mathbf{J}}{\ell_{o}^{2}} \cdot \frac{1}{\sqrt{1 - \gamma^{2}}} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & -1 & 0 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & -1 \\ -\beta & \alpha & 0 \end{bmatrix} \mathbf{W}^{2}(\delta) \right\} \\ \mathbf{E}(\mathbf{x}_{3}') &= \frac{1}{\sqrt{1 - \gamma^{2}}} \begin{bmatrix} \alpha \sqrt{1 - \gamma^{2}} + \beta \sqrt{1 - \gamma^{2}} &+ \gamma \sqrt{1 - \gamma^{2}} \\ -\beta & \alpha & 0 \\ -\alpha \gamma & -\beta \gamma & (1 - \gamma^{2}) \end{bmatrix} \\ \mathbf{W}^{2}(\delta) &= \begin{bmatrix} (\alpha^{2} - 1) & \alpha\beta & \alpha\gamma \\ \alpha\beta & (\beta^{2} - 1) & \beta\gamma \\ \alpha\gamma & \beta\gamma & (\gamma^{2} - 1) \end{bmatrix} \end{split}$$

(B-31)

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Thus

$$m_{A} = (m_{a} - m) \{1 + W^{2}(\delta)\} + m +$$

$$- \frac{J}{\ell_{o}^{2}} \frac{E'(x_{3})}{\sqrt{1 - \gamma^{2}}} \begin{bmatrix} 0 & 0 & 0 \\ -\beta & \alpha & 0 \\ 0 & 0 & 1 \end{bmatrix} W^{2}(\delta)$$
(B-32)

This reduces to

$$m_{A} = m + (m_{a} - m) \{1 + W^{2}(\delta)\} + -\frac{J}{\ell_{o}^{2}(1 - \gamma^{2})} \begin{bmatrix} \beta^{2} & \alpha\beta & \alpha\gamma \\ -\alpha\beta & \alpha^{2} & \beta\gamma \\ 0 & 0 & (1 - \gamma^{2}) \end{bmatrix} W^{2}(\delta)$$
(B-33)

which further reduces to

$$m_{A} = m + (m_{a} - m) \{1 + W^{2}(\delta)\} - \frac{J}{\ell_{o}^{2}} W^{2}(\delta)$$
  
(B-34)

After collecting terms, we have

$$m_{A} = m_{a} + \{m_{a} - m_{-} - \frac{J}{\ell_{o}^{2}}\} W^{2} (\delta)$$
(B-35)

The four submatrices of the mass matrix can then be found by summing

$$W^{2}(\delta)$$
,  $W(a) W^{2}(\delta)$ , and  $W(a) W^{2}(\delta) W(a)$  (B-36)

over the six actuators. These values are

$$\sum_{n=1}^{6} W^{2}(\delta_{n}) = -3 \begin{bmatrix} (1+\gamma^{2}) & 0 & 0 \\ 0 & (1+\gamma^{2}) & 0 \\ 0 & 0 & 2(1-\gamma^{2}) \end{bmatrix}$$

$$\sum_{n=1}^{6} W(a_n) W^2(\delta_n) = 3 \left\{ a_z (1 + \gamma^2) + \gamma (\alpha a_x + \beta a_y) \right\} \begin{bmatrix} 0 & 1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$\sum_{n=1}^{6} W(a_n) W^2(\delta_n) W(a_n) = 3 \begin{bmatrix} a_{11} & 0 & 0 \\ 0 & a_{11} & 0 \\ 0 & 0 & a_{33} \end{bmatrix}$$
(B-37)

where

$$a_{11} = a_{x}^{2}(1 - \gamma^{2}) + a_{y}^{2}(1 - \gamma^{2}) + a_{z}^{2}(1 + \gamma^{2}) + 2\gamma a_{z}(\alpha a_{x} + \beta a_{y})$$

$$a_{33} = 2 \left\{ a_{x}^{2}(1 - \beta^{2}) + a_{y}^{2}(1 - \alpha^{2}) + 2\alpha\beta a_{x}^{a}a_{y} \right\}$$
(B-38)

At the platform pivot plane, these evaluate to

$$\begin{split} \sum_{n=1}^{6} W^{2}(\delta_{n}) &= -\frac{3}{241} \begin{bmatrix} 385 & 0 & 0 \\ 0 & 385 & 0 \\ 0 & 0 & 194 \end{bmatrix} \\ &= \begin{bmatrix} -4.792531 & 0 & 0 \\ 0 & -4.7925311 & 0 \\ 0 & 0 & -2.4149378 \end{bmatrix} \\ \\ \sum_{n=1}^{6} W(a_{n}) W^{2}(\delta_{n}) &= \frac{1890}{241} \begin{bmatrix} 0 & +1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \\ &= \begin{bmatrix} -7.8423237 & 0 \\ 0 & 0 & 0 \end{bmatrix} \\ \\ \sum_{n=1}^{6} W(a_{n}) W^{2}(\delta_{n}) W(a_{n}) &= \frac{1}{241} \begin{bmatrix} 285471 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \\ &= \begin{bmatrix} 1184.5270 & 0 \\ 0 & 0 & 3585.5664 \end{bmatrix} (B-39) \end{split}$$

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$$\sum_{n=1}^{6} W(a_n) = 0$$
  
$$-\sum_{n=1}^{6} W^2(a_n) = \begin{bmatrix} 2943 & 0 & 0\\ 0 & 2943 & 0\\ 0 & 0 & 5886 \end{bmatrix} in^2$$
  
(B-40)

The neutral geometry of the RIA 6-DOF actuator is shown in figure B-2. In addition, two accumulators are attached to each cylinder. The calculated values for the piston and cylinder are then

$$M_{a} = .2352934 \text{ lb sec}^{2}/\text{in.}$$

$$d_{a} = 17.242 \text{ in.}$$

$$J_{ay} = J_{az} = 29.82127 \text{ in. lb sec}^{2}$$

$$M_{b} = 1.0168095 \text{ lb sec}^{2}/\text{in.}$$

$$d_{b} = 20.2079 \text{ in.}$$

$$J_{by} = 79.6253 \text{ in. lb sec}^{2}$$

$$J_{bz} = 88.49286 \text{ in. lb sec}^{2}$$

Since the orientation of the accumulators on the cylinders has not been specified, an average value of 84.0586 in. lb sec<sup>2</sup> will be used for both  $J_{by}$  and  $J_{bz}$ . Then the total transverse inertia is

$$J = J_a + J_b = 113.8799$$
 in. 1b sec<sup>2</sup>

The transverse mass is

$$M = 0.284759 \ 1b \ \sec^2/in. \tag{B-41}$$

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Then, for

$$l_o = 46.572524$$
 in  
 $(m_a - m - \frac{J}{l_o^2}) = -.101969$  lb sec<sup>2</sup>/in.  
(B-42)

Also



Figure B-2. Actuator neutral position

The load mass submatrices (as measured in the platform system) are then

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$$M_{11} = \begin{bmatrix} 1.900450 & 0 & 0 \\ 0 & 1.900450 & 0 \\ 0 & 0 & 1.658009 \end{bmatrix} \text{ lb sec}^2/\text{in.}$$

$$M_{12} = M_{21_{t}} = \begin{bmatrix} 0 & .7996739 & 0 \\ -.7996739 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \text{ lb sec}^2$$

$$M_{22} = \begin{bmatrix} 813.2535 & 0 & 0 \\ 0 & 8132535 & 0 \\ 0 & 0 & 1750.554 \end{bmatrix} \text{ in. lb sec}^2 \qquad (B-43)$$

APPENDIX C LISTING OF COMPUTER PROGRAM STIFF 2

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## LISTING OF COMPUTER PROGRAM "STIFF 2"

1*	DIMENSION TITLE(30), AD(6), AAK(6,6), AF(6), AK(6), AT(6,6), A(6,6),
2*	1AK1(6,6),B(6,6),C(3),C1(3),DX(6,6),DP(6),F(3),FA(6),F1(6),PR(6),
3*	2PTOP(6), PBOT(6), R1T(3,3), R1T2(3,3), R1T3(3,3), R0T2(3,3), R0T3(3,3),
4*	3ROT(3,3),SD(6),SE(6),SL(6),SK(6,6),SK1(6,6),SSK(6,6),SX(3,6),IRGT(
5*	43), XP(3,6), XG(3,6), XP1(3,6), XGUN(3), XGUN1(3), XW(3), XW1(3), SKO(6,6)
6*	5,XTRGT(3),DT(3),R6T(6,6),R5K(6,6),SK01(6,6),R5TT(6,6),S1K0(6,6)
7*	6,5F0(6),SF01(6),R0TT(6,6),R0TT1(6,6), PRT(6),PRB(6)
8*	7, SFC(6), R6T1(6,6), SD1(6)
9*	17=0
10*	READ (5,14) TITLE
11*	14 FORMAT (10A6)
12*	C CONSTANTS
13*	PI=3.141592654
14*	RAD=PI/180.
15*	C COORDINATES OF PIVOT CENTERS AT PITCH GIMBAL (DIRECTION, JOINT)
16*	X6 (1:1) = 15.5885
17*	XG(1,2) = -38.9711
18*	XG(1:3) = -38.9711
19*	X6(1)4) = 15.5885
20*	XG(1,5) = 23.3827
21*	$XG(1+6) = 23 \cdot 3827$
22*	XG(2,1) = 36.0
23*	XG(2) = -4.5
24*	XG(2*3) = -4*5
25*	XG (2+4) =-36+0
26*	XG (2,5) =-31.5
27*	XG(2,6) = 31.5
28*	C COORDINATES OF PIVOT CENTERS AT MOUNTING PLATFORM
29*	XP(1,1) = -12,9903
30*	XP (1+2) =-18+1865
31*	$XP(1+3) = -18 \cdot 1865$
32*	XP (1+4) =-12.9903
33*	XP(1,5) = 31.1769
34*	XP(1,6) = 31.1769
35*	XP(2,1) = 28.5
36*	XP(2,2) = 25.5
37*	XP (2+3) =-25+5
38*	xP(2,4) = -28.5
39*	XP(2,5) = -3.0

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<pre>414 DD 1 1=1r0 424 XG (371) = 9:375 437 1 XP (371) = 9:375 437 0 P (371) = 0:0 437 0 P (371) = 0:0 438 0 P (371) = 0:0 538 D (371) = 20 (371) 538 D (371) = 20 (371) = 20 (371) 539 D (371) = 20 (37</pre>	40*			XP(2,n) = 3.0
42*         XG (3*1) = 9.375           43*         XP (3*1) = 45.375           44*         C         AP = 21.205           46*         C         VO = TOTAL VOLUME (ACCUMULATOR* ACTUATOR FULLY EXTENDED)           47*         VO = 421.           46*         C C = CONDENTATE OF CENTER OF PLATFORM           47*         VO = 421.           46*         C C = CONDENTATE OF CENTER OF PLATFORM           50*         C(1) = 0.0           51*         C(2) = 0.0           52*         DO 3 1=1.6           53*         DO 3 1=1.6           54*         3 \$X(1,0)=X6 (1,0)+XP (1,0)           55*         DO 3 1=1.6           54*         3 \$X(1,0)=X6 (1,0)+XP (1,0)           55*         DO 3 1=1.6           56*         SL(1) = 0.0           57*         C ACULATE ACTUATOR LENGTH           56*         SL(1) = SAT(5L(1))           57*         C ALCULATE DIRECTON: COSINES           58*         DO 4 1=1.6           59*         S (1) = SA(31)/SL(1)           50*         DO 4 (1,0) = X(2,0)+(XP (1,0)-C (1) )-DX(1,0)+(XP (2,0)-C (2) )           50*         DO 4 (3,0)-C (3) )           60*         DO 2 (3,0)           60*         DO	41*			$DO \ 1 \ I=1, D$
43*         1 XP (3,1) = 0.5,75           44*         C AP = 24.205           45*         C VO = TOTAL VOLUME (ACCUMULATOR* ACTUATOR FULLY EXTENDED)           47*         VU = 421.           47*         C C CORDINATE OF CENTER OF PLATFORM           52*         D C 3 1=1/3           54*         D 3 1=1/3           55*         D J 1=1/6           56*         S L(1) = 5L(1)+S(J(T))+*2           67*         C CALCULATE DIRECTICS COSINES           62*         DO 0 L=1/6           55*         D 2 4 1=1/6           54*         D C 3 J=1/4           66*         D X(4+J)= D X(1+J)/X(P (1+J)-C (1) J+D X(1+J)+(XP (3+J)-C (3) J)           67*         D X(4+J)= D X(2+J)+(XP (1+J)-C (1) J+D X(1+J)+(XP (2+J)-C (2) J)           66*         D X(4+J)= D X(2+J)+(XP (1+J)-C (1) J+D X(1+J)+(XP (2+J)-C (2) J)           66	42*			XG(3,T) = 9.375
44*         C         AP = 2FFECTIVE ARE, OF ACTUATOR PISTON, IN2           45*         AP = 2FFECTIVE ARE, OF ACTUATOR PISTON, IN2           46*         C         V0 = TOTAL VOLUME (ACCUMULATOR* ACTUATOR FULLY EXTENDED)           47*         V0 = 421.           46*         C         C = CUDRDIATE OF CENTER OF PLATFORM           47*         V0 = 421.           46*         C         C = CUDRDIATE OF CENTER OF PLATFORM           47*         V0 = 421.         O.0           57*         D 0 3 I=173         D           58*         D 0 3 J=176         D           57*         D 0 4 I=176         D           58*         D 0 4 I=173         D           69*         S L(1) = SAT(ISL)1/3L(1)         AI           61*         D 0 7 J=173         D         G           64*         6 AC(J)I = SA(J)I/SL(1)         AI         AI           65*         D 7 J=173         AI         AI         AI           64*         A C ALQATE DRECTOR: COSINES         AI         AI         AI         AI         AI<	43*		1	XP (3,1) =45.875
45*         AP = 24.200           47*         C         V0 = TOTAL VOLUME (ACCUMULATOR* ACTUATOR FULLY EXTENDED)           47*         C         CCUDEDILATE OF CENTER OF PLATFORM           49*         C         CCUDEDILATE OF CENTER OF PLATFORM           49*         C         CCUDEDILATE OF CENTER OF PLATFORM           49*         CCUDEDILATE OF CENTER OF PLATFORM           49*         CCUDEDILATE OF CENTER OF PLATFORM           49*         CCUDEDILATE OF CENTER OF PLATFORM           52*         D0 3 JEIA           53*         D0 4 JEIA           54*         JSK(I)JEXCUDEDILATORY           55*         D0 4 JEIA           56*         SL(I) = 50.0175X(J/I)**2           60*         GSL(I) = SQRITSL(I)           61*         CCLCULATE DIRECTION COSINES           62*         D0 6 JEIA           64*         GOX(J) = SX(J/I)/XL(I)           65*         DX(1+J) = ZX(J/I)/XL(I)           65*         DX(2+J) = XX(J/J)/XL(I)           66*         DX(1+J) = ZX(J/I)/XL(I)           67*         DX(3+J) = ZX(J/J)/XL(I)           68*         DO & JEIA           69*         DO & ZIAIA           60*         DY (1+J) = ZX(J/J)/XL(I)           64* </th <th>44*</th> <th>C</th> <th>AP</th> <th>= EFFECTIVE AREA OF ACTUATOR PISTON, IN2</th>	44*	C	AP	= EFFECTIVE AREA OF ACTUATOR PISTON, IN2
46*         C         VU         = TOTAL         VOLUME LACCUMULATOR+ ACTUATOR FULLY EXTENDED)           47*         VU         = 41.           46*         C         C         C         COURTAL FOR CENTER OF PLATFORM           46*         C         C         C         C         C         C         C           51*         C(2)         = 0.0         State         C         C(2)         = 0.0           51*         C         C(2)         = XP(3,1)         Example         Do         State           52*         D0         J=r.6         State         State </th <th>45*</th> <th></th> <th>•</th> <th>AP = 21.205</th>	45*		•	AP = 21.205
47*       VU = 421.         49*       C = CounCharte OF CeNTER OF PLATFORM         49*       C (1) = 0.0         51*       C(3) = xP(3;1)         52*       D0 3 1=1:6         53*       C0 3 1=1:6         54*       S X(1,J)=-X0 (1,J)+XP (1,J)         55*       D0 4 1=1:6         56*       SL(1) = 0.0         57*       C ALCULATE ACTUATOR LENGTH         56*       SL(1) = SL(1)+SX(J,T)**2         60*       4 SL(1) = SQX(1)SL(1)         58*       D0 5 J=1:3         59*       S SL(1) = SX(J,1)/SL(1)         61*       C CALCULATE DIRCETS: COSINES         62*       D0 6 J=1:3         64*       6 DX(J,1)= DX(3,J)*(XP (2:J)=C (2) )=DX(2:J)*(XP (3:J)=C (3) )         65*       DX(4:J)= DX(3:J)*(XP (1:J)=C (1) )=DX(1:J)*(XP (3:J)=C (3) )         67*       CX(G,J)==DX(2:J)*(XP (1:J)=C (1) )=DX(1:J)*(XP (2:J)=C (2) )         68*       D0 (2:3)=1:6         70*       D (2:3)=1:1:6         71*       B(J,J) = DX(1:J)         72*       D (2:4)=1:1:0         73*       CALL MATINGA*(L):6         74*       D (2:4)=1:1:0         74*       D (2:4)=1:1:1:1:1:0         75*       D0 2:4 =1:1:0 </th <th>46*</th> <th>C</th> <th>VO</th> <th>= TOTAL VOLUME (ACCUMULATOR + ACTUATOR FULLY FXTENDED)</th>	46*	C	VO	= TOTAL VOLUME (ACCUMULATOR + ACTUATOR FULLY FXTENDED)
4.6#         C         C C= COURDINATE OF CENTER OF PLATFORM           494         C(1) = 0.0         50.4         C(2) = 0.0           51.4         C(2) = 0.0         51.4         C(3) = XP(3r1)           52.4         D0 3 1=1/3         53.5         53.4         D0 3 1=1/3           53.4         D0 3 1=1/3         53.4         D0 3 1=1/3           54.4         J SA(1/J)=-XU(I/J)+XP (I/J)         55.4         D0 4 1=1/6           55.4         D0 4 1=1/6         54.1         54.1         54.1           54.7         C CALCULATE ACTUATOR LENGTH         57.4         C CALCULATE DIRECTIO: COSINES           54.7         D0 6 1=1/6         53.4         D0 6 .5 1=1.3           54.4         D 0 (1-J) = SQ(1/J)/SL(1)         56.4         D0 (1-J) = SQ(1/J)/SL(1)           55.4         D 0 / J =1/6         53.4         D0 / J =1/6         53.4           54.4         D 0 (2-J) = X(2/J)+X(P (1/J)-C (1) )+DX(1/J)+X(P (3/J)-C (3) )         64.4         6 DX(4/J) = DX(3/J)+X(P (1/J)-C (1) )+DX(1/J)+X(P (3/J)-C (3) )           57.4         D 0/J 23 =1/6         D 0/J 23 =1/6         D 0/J 23 =1/6           57.4         D 0/J 23 =1/6         D 0/J 23 =1/6         D 0/J 23 =1/6           78.4 <thd 0="" 2="" 2<="" j="" th=""><th>47*</th><th></th><th>-</th><th><math display="block">V = 421 \cdot</math></th></thd>	47*		-	$V = 421 \cdot$
$\begin{array}{llllllllllllllllllllllllllllllllllll$	48*	C	C=	CUORDINATE OF CENTER OF PLATFORM
50* $C(2) = 0.0$ 51* $C(3) = XP(3,1)$ 52* D0 3 I=1+3 53* D0 3 J=1+6 54* J SX(1,1)=-XG (I,J)+XP (I,J) 55* D0 4 I=1+6 55* C CALCULATE ACTUATOR LEMETH 57* C CALCULATE INFACTOR LEMETH 58* D0 5 J=1+3 59* 5 SL(1) = SL(1)+SX(J,1)**2 60* 4 SL(1) = SQR(1SL(1)) 61* C CALCULATE DIRECTION COSINES 62* D0 6 J=1+6 63* D0 6 J=1+3 64* 6 DX(J+1) = SX(J+1)/SL(1) 65* D0 7 J=1+6 56* DX(4+J)= DX(3+J)*(XP (2,J)+C (2) )+CX(2+J)*(XP (3,J)+C (3) ) 64* 7 DX(4+J)= DX(3+J)*(XP (1,J)+C (1) )+DX(1+J)*(XP (3,J)+C (3) ) 64* 7 DX(4+J)= DX(3+J)*(XP (1+J)+C (1) )+DX(1+J)*(XP (3,J)+C (3) ) 64* 7 DX(4+J)= DX(2+J)*(XP (1+J)+C (1) )+DX(1+J)*(XP (2,J)+C (2) ) 65* D0 2 J=1+6 70* D0 23 J=1+6 71* E(J+1) = DX(1+J) 72* 23 A(1+J) = DX(1+J) 73* C ALL MATIN(A+IJ+6) 74* D0 24 J=1+a 75* D0 24 J=1+a 76* 24 AT(1+J) = A(J+1) 77* C THETA = MOUNTING ANGLE OF VEHICLE WITH FLATFORM, DEG- 76* 15 FORMAT(1H1+, CASE+13+10A6/X+10A6//10A6// ) 64* C N= WEIGHT OF PLATFORM, PART OF ACTUATORS AND +AYLOAD, L0 64* C N= WEIGHT OF PLATFORM, PART OF ACTUATORS AND +AYLOAD, L0 64* C N= WEIGHT OF PLATFORM, PART OF ACTUATORS AND +AYLOAD, L0 64* C X= C AL CASTION OF WEIGHT W.R.T. CENTER OF DITCH GIMBAL 77* READ(5+2) W, XA (1)+1=3,3) 64* C T(GT = POSITION OF WEIGHT W.R.T. CENTER OF PITCH GIMBAL 78* READ(5+2) W, XA (1)+1=1+3] 79* C THETA = MOUNTING POINT W.R.T. CENTER OF PITCH GIMBAL 77* READ(5+2) W, XA (1)+1=1+3] 78* C T(GT = POSITION OF WEIGHT W.R.T. CENTER OF PITCH GIMBAL 78* READ(5+2) W, XA (1)+1=1+3] 79* C T(GT = POSITION OF WEIGHT W.R.T. CENTER OF PITCH GIMBAL 78* READ(5+2) W, YA (2) = R+1+4 79* READ(5+2) W, YA (2) = R+1+4 79* READ(5+2) W, YA (2) = R+1+4 79* READ(5+2) TO TO F WEIGHT W.R.T. CENTER OF PITCH GIMBAL 79* READ(5+2) W, YA (2) = R+1+4+AD 74* READ (5+2) TICH ATHETA + MOUNTING POINT W.R.T. CENTER OF PITCH GIMBAL 75* READ(5+2) W, YA (2) = R+1+4+AD 75* READ(5+2) RA (ABAL PITCH AND YAM 75* READ(5+2) RA (ABAL PITCH	49*			C(1) = 0.0
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	50*			C(2) = 0.0
92*       D0 3 J=1:6 $93*$ D0 3 J=1:6 $94*$ J SX(1,J)=-XG (1,J)*XP (1,J) $95*$ D0 4 1=1:6 $95*$ D0 4 1=1:6 $95*$ SL(1) = 0.0 $97*$ C CALCULATE ACTUATOR LEMETH $95*$ SL(1) =SL(1)+SL(0,1)**2 $60*$ 4 SL(1) =SL(1)*COSINES $62*$ D0 6 J=1:6 $63*$ D0 6 J=1:7 $64*$ 6 DX(J+1)= SX(J+1)/SL(1) $64*$ G DX(J+1)= SX(J+1)/SL(1) $64*$ DX(J+1)= SX(J+1)/SL(1) $64*$ DX(J+1)= DX(1,J)*(XP (2,J)-C (2) )-CX(2,J)*(XP (3,J)-C (3) ) $64*$ DX(J+1)= DX(1,J)*(XP (1,J)-C (1) )+DX(1,J)*(XP (3,J)-C (3) ) $64*$ DX(J+1)= DX(1,J)*(XP (1,J)-C (1) )+DX(1,J)*(XP (2,J)-C (2) ) $64*$ DX(J+1)= DX(1,J) $72*$ DX (J+1)= DX(1,J) $72*$ CALL MATIN(A, L, L6) $74*$ D0 24 J=1:6 $75*$ D0 24 J=1:6 $75*$ D0 24 J=1:6 $74*$ D0 24 J=1:6 $75*$ D0 24 J=1:6 $75*$ D0 24 J=1:6 $75*$ <	51*			C(3) = XP(3,1)
53* D0 3 J=16 54* S 5X(I,J)=-XG (I,J)+XP (I,J) 55* D0 4 1=176 56* SL(I) = 0.0 57* C CALCULATE ACTUATOR LEMETH 58* D0 5 J=173 59* 5 SL(I) =5L(I)+5X(J,I)**2 60* 4 SL(I) =5GRT(SL(I)) 61* C CALCULATE DIRECTON COSINES 62* D0 6 J=176 63* D0 6 J=176 64* 6 DX(J,I)= 5X(J,I)*(XP (2,J)=C (2) )=DX(2,J)*(XP (3,J)=C (3) ) 67* DX(3,J)=DX(3,J)*(XP (1,J)=C (1) )+DX(1,J)*(XP (3,J)=C (3) ) 67* DX(3,J)=DX(3,J)*(XP (1,J)=C (1) )+DX(1,J)*(XP (3,J)=C (3) ) 67* DX(3,J)=DX(3,J)*(XP (1,J)=C (1) )+DX(1,J)*(XP (2,J)=C (2) ) 69* D0 23 J=16 70* D0 23 J=16 71* B(J,I) = DX(I+J) 72* 23 A(I,J) = DX(I+J) 74* D0 24 J=16 75* CALL MATIN(A*LD)6 74* D0 24 J=16 76* 24 AT(I,J) = A(J,I) 77* C THETA = MOUNTI, C ANGLE OF VEHICLE WITH PLATFORM, DE6. 78* 1000 READ(5,2) THETA 79* I [=11+1 60* IF(THETA.GT.99.) 60 TO 9999 81* WHITE(DJS) II,TITLE 62* 15 FORMAT(IH1* CASE*,I3,1006/3X,1006//1006//) 63* C W= WEIGHT OF PLATFORM, PART OF ACTUATORS AND PATLOD, LD 64* C XWE C.G. LOCATION OF WEIGHT W.R.T. CENTER OF DIMMAL , IN. 65* READ(5,2) W(Xn(I),I1=1,3) 66* C THETA = POSITION OF WEIGHT W.R.T. CENTER OF PITCH GIMSAL 77* C ALL 5,21 (XGL,(I),I1=1,3) 78* CALCUS21 W(Xn(I),I=1,3) 79* C READ(5,21 (THCT(I),I=1,3) 70* C RY AND RZ ARE THE GIMBAL PITCH AND YAW 77* C RATA SEAR THE GIMBAL PITCH AND YAW 78* READ(5,21 (THCT(I),I=1,3) 79* C RY AND RZ ARE THE GIMBAL PITCH AND YAW 79* READ(5,21 (THCT(I),I=1,3) 70* C RY AND RZ ARE THE GIMBAL PITCH AND YAW 70* READ (5,21 (THCT(I),I=1,3) 70* C RY AND RZ ARE THE GIMBAL PITCH AND YAW 70* READ (5,21 (THET IA, THE A 70* RADY = RY*HAD 70* RADZ = RZ*RAD	52*	anterproper specific de la construction de la construction de la construction de la construction de la constru	a allali och roch an andrahen	D0 3 I=1,3
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	53*			NO 3 J=1.6
55* DJ 4 1=1/6 56* SL(1) = 0.0 57* C CALCULATE ACTUATOR LENGTH 58* DJ 5 J=1/3 59* 5 SL(1) =SL(1)+SX(J,1)**2 60* 4 SL(1) =SQRT(SL(1)) 61* C CALCULATE DIRECTION COSINES 62* DJ 6 J=1/6 63* DJ 7 J=1/6 65* DJ 7 J=1/6 65* DJ 7 J=1/6 65* DJ 7 J=1/6 65* DJ 7 J=1/6 66* T DX(3/J)=SX(J/1)/SL(1) 65* DJ 7 J=1/6 66* T DX(3/J)=DX(3/J)*(XP (2/J)=C (2) )=DX(2/J)*(XP (3/J)=C (3) ) 67* DX(3/J)=DX(3/J)*(XP (1/J)=C (1) )=DX(1/J)*(XP (3/J)=C (3) ) 67* DX(3/J)=DX(2/J)*(XP (1/J)=C (1) )=DX(1/J)*(XP (2/J)=C (2) ) 68* 7 DX(6/J)=DX(2/J)*(XP (1/J)=C (1) )=DX(1/J)*(XP (2/J)=C (2) ) 69* DJ 23 J=1/6 70* DJ 23 J=1/6 71* B(J,1) = DX(1/J) 72* CALL MATIN(A/IJ/6) 74* DJ 24 J=1/6 75* CALL MATIN(A/IJ/6) 75* CALL MATIN(A/IJ/6) 75* C THETA = MOUNTLG ANGLE OF VEHICLE WITH PLATFORM, DE6. 76* 24 AT(1/J) = A(J/T) 77* C THETA = MOUNTLG ANGLE OF VEHICLE WITH PLATFORM, DE6. 76* IGO REAG(5/2) THETA 79* J[=17+1] 60* IF(THETA/GT-99.) 60 TO 9999 61* WRITE(G/IS) JI,JITLE 62* C K= C.G. LOCATION OF WEIGHT W.R.T. CENTER OF GIMBAL , IN. 65* REAG(5/2) W, (Xe(1)/I=1/3) 66* C XGUN = POSITION OF WARGHT W.R.T. CENTER OF FITCH GIMBAL 67* READ(5/2) W, (Xe(1)/I=1/3) 68* C TKOT = POSITION OF WARGT W.R.T. CENTER OF PITCH GIMBAL 69* READ(5/2) W, NZ 69* READ(5/2) KY/NZ 62* 2 FORMAT(E10/I)=1/7 62* C THOT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL 69* READ(5/2) KY/NZ 62* 2 FORMAT(E10/I)=1/7 62* C TKOT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL 69* READ(5/2) KY/NZ 62* 2 FORMAT(E10/I)=1/7 62* C TKOT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL 69* READ(5/2) KY/NZ 62* 2 FORMAT(E10/I)=1/7 63* C RY AD Z ARE THE GIMBAL PITCH AND YAW 64* RADY = RY*RAD 65* RAUZ = RZ*RAD	54*		3	$SX(I,J) = -X_G (I,J) + XP (I,J)$
56*       SL(1) = 0.0         57*       C CALCULATE ACTUATOR LENGTH         58*       D0 5 J=13         59*       S.L(1) = SQL(1)+SX(J,1)**2         60*       4 SL(1) = SQL(1): COSIMES         62*       D0 6 J=1.6         63*       D0 6 J=1.6         64*       6 0X(J,1)= SX(J,1)/SL(1)         65*       D0 7 J=1.6         66*       DX(4+J)= DX(3,J)*(XP (2,J)-C (2) )+DX(1,J)*(XP (3,J)-C (3) )         67*       DX(5,J)=-DX(2,J)*(XP (1,J)-C (1) )+DX(1,J)*(XP (3,J)-C (3) )         68*       7 DX(5,J)=-DX(2,J)*(XP (1,J)-C (1) )+DX(1,J)*(XP (2,J)-C (2) )         69*       D0 23 J=1.6         70*       D0 23 J=1.6         71*       DU(23 J=1.6         72*       23 A(1,J) = DX(1,J)         73*       CALL MATN(A: LD=6)         74*       D0 24 J=1.6         75*       D0 24 J=1.6         75*       D0 24 J=1.6         74*       1000 READ(5.2) THET.         75*       D0 24 J=1.6         74*       1000 READ(5.2) THET.         75*       D0 24 J=1.6         74*       1000 READ(5.2) THET.         75*       D0 24 J=1.6         75*       D0 24 J=1.6         76*       <	55*		-	$D_{2} + 1 = 1.6$
57*       C CALCULATE ACTUATOR LENGTH         56*       D0 5 J=13         59*       5 SL(I) =SL(I)+SX(J,I)**2         60*       4 SL(I) =SGRT(SL(I))         61*       C CALCULATE DIRECTION COSINES         62*       D0 6 J=13         63*       D0 7 J=16         65*       D0 7 J=16         66*       PX(J,I)=SX(J,I)/SL(I)         67*       DX(5,J)=DX(3,J)*(XP (2,J)=C (2) )=DX(2,J)*(XP (3,J)=C (3) )         67*       DX(5,J)=DX(3,J)*(XP (1,J)=C (1) )+DX(1,J)*(XP (2,J)=C (2) )         68*       T DX(5,J)=DX(2,J)*(XP (1,J)=C (1) )+DX(1,J)*(XP (2,J)=C (2) )         69*       D0 23 J=1.6         70*       D0 23 J=1.6         70*       D0 24 J=1.0         73*       CALCU MATIN(K:L)         74*       D0 24 J=1.0         75*       D0 24 J=1.0         76*       24 AT(1,J) = A(J,I)         77*       C THETA = MOUNTING ANGLE OF VEHICLE WITH FLATFORM, DEG.         75*       D0 24 J=1.0         76*       24 AT(1,J) = A(J,I)         77*       C THETA = MOUNTING ANGLE OF VEHICLE WITH FLATFORM, DEG.         78*       C HACTO, FLETA         79*       IT=174         60*       IF(THETA.6T.99.) 60 TO 9999         <	56*			$S_{L}(1) = 0.0$
58* D0 5 J=1:3 59* 5 SL(1) =SL(1)+SX(J,I)**2 60* 4 SL(1) =SQT(SL(1)) 61* C CALCULATE DIRECTIO: COSINES 62* D0 6 J=1:6 63* D0 6 J=1:3 64* 6 DX(J:I) = SX(J:I)/SL(I) 65* D7 J=1:6 65* DX(4:J) = DX(3:J)*(XP (2:J)-C (2))-DX(2:J)*(XP (3:J)-C (3)) 67* DX(5:J)=-DX(3:J)*(XP (1:J)-C (1))+DX(1:J)*(XP (3:J)-C (3)) 68* 7 DX(5:J)=-DX(2:J)*(XP (1:J)-C (1))+DX(1:J)*(XP (2:J)-C (2)) 69* D0 23 J=1:6 70* D0 23 J=1:6 71* B(J:I) = DX(I:J) 73* CALL MATIN(A:IJ:6) 74* D0 24 J=1:6 75* D0 24 J=1:6 76* 24 AT(1:J) = A(J:I) 77* C THETA = MOUNTING ANGLE OF VEHICLE WITH FLATFORM, DEG. 76* 1000 READ(5:2) THETA 79* I I=11*1. 60* IF(ITHETA:6I:99.) GO TO 9999 61* WRITE(G:15) II:TITLE 62* D5 FURMAT(1HI: C:SE':13:10A6/0X:10A6//10A6//) 83* C w= WEIGHT OF PLATFORM, PART OF ACTUATORS AND PAYLOAD, LD 84* C Xw= C:G. LCCATION OF WEIGHT W:R.T. CENTER OF DIMBAL , IN: 85* READ(5:2) W(Xa(1):1:1:3) 66* C XGUM = POSITION OF WEAPON MOUNTING POINT W:R.T. C.G. CF WEIGHT 67* READ(5:2) (TROT(1):1:1:3) 68* C WA NEZ ARE THE GIMBAL PITCH AND YAW 91* READ(5:2) (TROT(1):1:1:3) 69* C RY AND RZ ARE THE GIMBAL PITCH AND YAW 91* READ(5:2) (X:META 92* 2 FORMAT(6HI: A:META 94* RADY = RY*ARD 95* RTHETA RY*ARD 95* RTHETA XEARD 95* RTHETA XEARD 95* RTHETA XEARD 95* RTHETA XEARD 95* RTHETA XEARD	57*	С	CAL	CULATE ACTUATOR LENGTH
59*       5 SL(1) = SL(1) + SL(J, 1) * 2         60*       4 SL(1) = SQRT(SL(1))         61*       C CALCULATE DIRECTION COSIMES         62*       D0 6 J=1.6         63*       D0 7 J=1.6         64*       6 0 A(J, 1) = SX(J, 1)/SL(1)         65*       D0 7 J=1.6         66*       DX(4, J) = DX(3, J)*(XP (2, J)=C (2) )=DX(2, J)*(XP (3, J)=C (3) )         67*       DX(5, J)=DX(3, J)*(XP (1, J)=C (1) )+DX(1, J)*(XP (3, J)=C (3) )         68*       7 DX(2, J)=DX(2, J)*(XP (1, J)=C (1) )+DX(1, J)*(XP (2, J)=C (2) )         69*       D0 23 J=1.6         70*       D0 23 J=1.6         71*       B(J, 1) = DX(1, J)         72*       23 A(1, J) = DX(1, J)         73*       CAL(MATIN(A, FUR6)         74*       D0 24 J=1.6         75*       D0 24 J=1.6         76*       24 AT(1, J) = A(J, 1)         77*       C THETA = MOUNTLAG ANGLE OF VEHICLE WITH FLATFORM, DEG.         78*       IO0 24 J=1.6         78*       IO0 24 J=1.6         79*       I(=IT+1)         60*       IF(THETA.6T.99.) 60 TO 9999         81*       WRITE(G,15) II.TITLE         82*       15 FORMAT(H11* CALTOR M PARTOF ACTUNTORS AND PAYLOAD, LD         84*	58*	an an agu tha san a straight 2017	an in the second second second	00.5  J=1.3
60* 4 SL(1) =SQRT(SL(1)) 61* C CALCULATE DIRECTION: COSINES 62* D0 6 J=1.3 64* 6 DA(J+I)= SX(J+1)/SL(I) 65* D0 7 J=1.6 66* DX(4+J)= DX(3+J)*(XP (2+J)-C (2) )-DX(2+J)*(XP (3+J)-C (3) ) 67* CX(5+J)=-DX(3+J)*(XP (1+J)-C (1) )+DX(1+J)*(XP (3+J)-C (3) ) 68* 7 DX(5+J)=DX(2+J)*(XP (1+J)-C (1) )+DX(1+J)*(XP (2+J)-C (2) ) 69* D0 23 J=1.6 70* D0 23 J=1.6 71* E(J+I) = DA(1+J) 73* CALL MATIN(A+IJ+6) 74* D0 24 J=1.6 76* 24 AT(1+J) = A(J+I) 77* C THETA = MOUNTING ANGLE OF VEHICLE WITH FLATFORM, DEG. 76* 1000 READ(5+2) THETA 79* If(THETA-GT-99+) GO TO 9999 81* WRITE(5+13) ILTITLE 62* T5 FORMAT(1H)+ CASE*13*10A6/8X*10A6//10A6//) 83* C W= WEIGHT OF PLATFORM, PART OF ACTUATORS AND PAYLOAD, LD 84* C XWE C+G. LOCATION OF WEIGHT W+R+T. CENTER OF GAMBAL + IN- 85* READ(5+2) W+(XA(1)+I=1+3) 86* C XGUM = POSITION OF TARGET W-R-T. CENTER OF PITCH GIMBAL 89* READ(5+2) KTHE THE GIMBAL PITCH AND YAW 91* READ (5+2) KTHE GIMBAL PITCH AND YAW 91* READ (5+2) KTHE THE A 94* RADY = RY*RAD 95* RTHETA FARAD 96* RADY = RY*RAD	59*		5	SL(I) = SL(I) + SX(J,I) * * 2
61* C CALCULATE DIRECTION COSINES 62* D0 6 J=1+6 63* D0 7 J=1,6 65* D0 7 J=1,6 66* DX(4,J)= DX(3,J)*(XP (2,J)-C (2) )-DX(2,J)*(XP (3,J)-C (3) ) 67* DX(5,J)=DX(3,J)*(XP (1,J)-C (1) )+DX(1,J)*(XP (3,J)-C (3) ) 68* 7 DX(2,J)=DX(2,J)*(XP (1,J)-C (1) )+DX(1,J)*(XP (2,J)-C (2) ) 69* D0 23 J=1+6 70* D0 23 J=1+6 70* D0 23 J=1+6 71* E(J,I) = DX(1,J) 72* 23 A(1,J) = DX(1,J) 73* CALL MATIN(A,IJ,6) 74* D0 24 J=1,0 75* D0 24 J=1,0 75* 24 A(1,J) = A(J,I) 77* C THETA = MOUNTING ANGLE OF VEHICLE WITH PLATFORM, DEG. 76* 1000 READ(5,2) THETA 79* I[f=17+1 60* IF(THETA.6F.99.) 60 TO 9999 81* WRITE(0,IS) IJ,IIILE 82* 15 FORMAT(H1+* CASE*,I3,I0A6/3X*10A6//10A6// ) 83* C W= WEIGHT OF PLATFORM, PART OF ACTUATORS AND PAYLOAD, LB 84* C XWE CG. LOCATION OF WEIGHT W.R.T. CENTER OF GIMBAL , IN. 85* READ(5,2) W,(Xa(1),I=1,3) 66* C XGUM = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL / IN. 85* READ(5,2) W,(Xa(1),I=1,3) 66* C XGUM = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL 90* C RY AND RZ ARE THE GIMBAL PITCH AND YAW 81* READ(5,2) W,(Xa(1),I=1,3) 84* C TRGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL 92* 2 FORMAT(GELO.0) 93* READ(5,2) KY,KZ 94* C RY AND RZ ARE THE GIMBAL PITCH AND YAW 94* READ(5,2) KY,KZ 95* RTINCTA =THEITA*,KAD 95* RTINCTA =THEITA*,KAD 96* RAUZ = RZ*,RAD	60*		4	SL(I) =SORT(SL(I))
62* D0 6 I=1+6 63* D0 6 J=1+3 64* 6 DX(J+J) = SX(J+I)/SL(I) 65* D0 7 J=1,6 66* DX(4+J) = DX(3+J)*(XP (2+J)-C (2) )+DX(1+J)*(XP (3+J)-C (3) ) 67* DX(3+J) = DX(2+J)*(XP (1+J)-C (1) )+DX(1+J)*(XP (2+J)-C (2) ) 68* 7 DX(3+J) = DX(2+J)*(XP (1+J)-C (1) )+DX(1+J)*(XP (2+J)-C (2) ) 69* D6 23 J=1+6 70* D0 23 J=1+6 71* B(J+I) = DX(1+J) 73* CALL MATIR(A+IJ+6) 74* D0 24 J=1+0 75* D0 24 J=1+0 76* 24 AT(I+J) = A(J+I) 77* C THETA = MOUNTING ANGLE OF VEHICLE WITH FLATFORM, DEG. 76* 1000 READ(5+2) THETA 79* IF(IHETA+GT-99+) 60 TO 9999 81* WRITE(0+15) II,TITLE 82* 15 FORMAT(1H1+' CASE'+I3+10A6/8X+10A6//10A6// ) 83* C W= WEIGHT OF PLATFORM, PART OF ACTUATORS AND PAYLOAD+ L8 84* C XWE C.6. LCCATION OF WEIGHT W.R.T. CENTER OF GIMSAL , IN. 85* READ(5+2) W(Xn(1)+I=1+3) 66* C XGUN = POSITION OF WEIGHT W.R.T. CENTER OF FITCH GIMSAL 84* C TKGT = POSITION OF TARGET W.R.T. CENTER OF FITCH GIMSAL 84* C TKGT = POSITION OF TARGET W.R.T. CENTER OF FITCH GIMSAL 84* C TKGT = POSITION OF TARGET W.R.T. CENTER OF FITCH GIMSAL 84* C TKGT = POSITION OF TARGET W.R.T. CENTER OF FITCH GIMSAL 84* C TKGT = POSITION OF TARGET W.R.T. CENTER OF FITCH GIMSAL 84* C TKGT = POSITION OF TARGET W.R.T. CENTER OF FITCH GIMSAL 84* C READ(5+2) (XGU,(1)+I=1+3) 86* C RY AND RZ ARE THE GIMBAL PITCH AND YAW 81* READ(5+2) (XGU,(1)+I=1+3) 84* C RY AND RZ ARE THE GIMBAL PITCH AND YAW 81* READ (5+2) (XGU,(1)+I=1+3) 90* C RY AND RZ ARE THE GIMBAL PITCH AND YAW 91* READ (5+2) (XGU,(1)+I=1+3) 92* 2 FORMAT(6E10-0) 93* RY = RY+THETA 94* RADY = RY+RAD 95* RTNETA = THETATAFAD	61*	C	CAL	CULATE DIRECTION COSTNES
63*       00 6 J=1,3         64*       6 DX(J+I)= SX(J+I)/SL(I)         65*       00 7 J=1,6         66*       0X(4+J)= DX(3+J)*(XP (2+J)=C (2) )=0X(2+J)*(XP (3+J)=C (3) )         67*       0X(5+J)=-DX(3+J)*(XP (1+J)=C (1) )+DX(1+J)*(XP (3+J)=C (3) )         68*       7 0X(4+J)= DX(2+J)*(XP (1+J)=C (1) )+DX(1+J)*(XP (2+J)=C (2) )         69*       00 23 J=1+6         71*       B(J+I)= DX(1+J)         72*       23 A(1+J)= DX(1+J)         73*       CALL MATIN(A+IJ+6)         74*       D0 24 J=1+0         75*       D0 24 J=1+0         76*       24 AT(1+J)= A(J+I)         77*       C THETA = MOUNTING ANGLE OF VEHICLE WITH FLATFORM* DEG.         78*       1000 READ(5+2) THETA         79*       I1=IT+1         60*       IF(THETA+GF+99+) GO TO 9999         81*       C W= WEIGHT OF PLATFORM* PRT OF ACTUATORS AND PAYLOAD* LB         82*       15 FORMAT(1H1* CASE**13*10/6/8X*10A6//10A6// )         83*       C W= WEIGHT OF PLATFORM* PRT OF ACTUATORS AND PAYLOAD* LB         84*       C Xwe C-G* LOCATION OF WEIGHT W.R.T. CENTER OF GIMBAL , IN.         85*       C XGUN = POSITION OF WEAPON MOUNTING POINT W.R.T. C.G. CF WEIGHT         67*       READ(5+2) (XGUL(1)*I=1+3)         86*       C TKGT =	62*	-		D0 6 I=1/6
64* 6 DA(J,I)= SX(J,I)/SL(I) 65* D0 7 J1,6 65* DX(4,J)= DX(3,J)*(XP (2,J)-C (2) )-DX(2,J)*(XP (3,J)-C (3) ) 67* DX(5,J)=-DX(3,J)*(XP (1,J)-C (1) )+DX(1,J)*(XP (3,J)-C (3) ) 68* 7 DX(5,J)=DX(2,J)*(XP (1,J)-C (1) )-DX(1,J)*(XP (2,J)-C (2) ) 69* D0 23 J=1.6 70* D0 23 J=1.6 71* B(J,I) = DX(I,J) 73* CALL MATIN(A,ID,6) 74* D0 24 J=1.6 76* 24 AT(1,J) = A(J,I) 76* C THETA = MOUNTING ANGLE OF VEHICLE WITH FLATFORM, DEG. 76* 1000 READ(5,2) THETA 79* I(-1,T+1) 60* IF(THETA.GT.99.) GO TO 9999 81* WRITE(G,15) II.TITLE 82* 15 FUNMAT(1H1,* CASE*, I3/10/6/8X,10A6//10A6// ) 84* C Xw= C.G. LOCATION OF WEIGHT W.R.T. CENTER OF GIMBAL , IN. 85* READ(5,2) (TAGT (1),I=1,3) 86* C XuU = POSITION OF WEAPON MOUNTING POINT W.R.T. C.G. CF WEIGHT 67* READ(5,2) (TAGT (1),I=1,3) 84* C Xw= C.G. LOCATION OF TARGET W.R.T. CENTER OF PITCH GIMBAL 84* C Xw= C.G. UCATION OF TARGET W.R.T. CENTER OF PITCH GIMBAL 84* C Xw= C.G. UCATION OF TARGET W.R.T. CENTER OF PITCH GIMBAL 84* C Xw= CAG (5,2) (XGU(1),I=1,3) 85* C TRGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL 84* C Xw= CAU(5,2) (TRGT (1),I=1,3) 85* C TRGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL 84* C READ(5,2) (TRGT (1),I=1,3) 85* C TRGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL 85* READ(5,2) (TRGT (1),I=1,3) 86* C RY AND RZ ARE THE GIMBAL PITCH AND YAW 81* READ (5,2) (TRGT (1),I=1,3) 95* C RY AND RZ ARE THE GIMBAL PITCH AND YAW 81* READ (5,2) (TRGT HETA.RAD 95* RTHETA THETA.RAD 95* RTHETA THETA.RAD 95* RTHETA THETA.RAD 95* RTHETA THETA.RAD	63*			DO 6 J=1.3
65*       D0 7 J=1,6         66*       DX(4,J)= DX(3,J)*(XP (2,J)=C (2) )=DX(2,J)*(XP (3,J)=C (3) )         67*       DX(5,J)=-DX(3,J)*(XP (1,J)=C (1) )=DX(1,J)*(XP (3,J)=C (3) )         68*       7 DX(5,J)=DX(2,J)*(XP (1,J)=C (1) )=DX(1,J)*(XP (2,J)=C (2) )         69*       D0 23 J=1;6         70*       D0 23 J=1;6         71*       B(J,I) = DX(1,J)         73*       CALL MATIN(A,IJ;6)         74*       D0 24 J=1;6         75*       C0 24 J=1;6         75*       D0 24 J=1;6         76*       100 READ(5;2) THETA         79*       IT=1T+1         60*       IF (THETA-GT-99*) 60 TO 9999         81*       WRITE(G:15) II;TITLE         62*       IS FORMAT(1H1*)* CASE*; I3:10A6/8X*10A6//10A6//*)         63*       C W= WEIGHT OF PLATFORM, PART OF ACTUATORS AND FAYLOAD, LB         84*       C X= C.6. LOCATION OF WEIGHT W.R.T. CENTER OF GIMBAL , IN.         85*       READ(5;2) (RG(1); I=1;3)         86*       C XuUM = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         87*       READ(5;2) (RG(1); I=1;3)         88*       C TKGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         89*       READ(5;2) (RG(1); I=1;3)         90*       C RY AND RZ ARE THE GIMBAL PITCH AND YAW	64*		6	$D_{\lambda}(J,I) = S_{\lambda}(J,I)/SL(I)$
56*       DX(4,J)= DX(3,J)*(XP (2,J)-C (2) )-DX(2,J)*(XP (3,J)-C (3) )         67*       DX(5,J)=-DX(3,J)*(XP (1,J)-C (1) )-DX(1,J)*(XP (3,J)-C (3) )         68*       7 DX(5,J)=DX(2,J)*(XP (1,J)-C (1) )-DX(1,J)*(XP (2,J)-C (2) )         69*       D0 23 J=1;6         70*       D0 23 J=1;6         71*       B(J,I) = DX(1,J)         72*       23 A(1,J) = DX(1,J)         73*       CALL MATIN(A,IJ,6)         74*       D0 24 J=1;0         76*       24 J=1;0         78*       If(I+I)         79*       If(I+I)         79*       If(I+I)         79*       If(I+I)         79*       If(I+I)         70*       C WEIGHI OF PLATFORM, PART OF ACTUATORS AND PAYLOAD, LB         82*       15 FORMAT(1H1,* CASE', I3,10A6/8X,10A6//10A6// )         83*       C W= LIGHI OF PLATFORM, PART OF ACTUATORS AND PAYLOAD, LB         84*       C Xw= C.6. LOCATION OF WEIGHT W.R.T. CENTER OF GIMBAL , IN.         85*       READ(5,2) (XGU,(1),I=1,3)         86*       C XGUN = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         87*       REA	65*		0	D0 7 J=1,6
67*       DX(5,J)=-DX(3,J)*(XP (1,J)-C (1) )+DX(1,J)*(XP (3,J)-C (3) )         68*       7 DX(6,J)= DX(2,J)*(XP (1,J)-C (1) )-DX(1,J)*(XP (2,J)-C (2) )         69*       D0 23 J=1;6         70*       D0 23 J=1;6         71*       E(J,1)= DX(1,J)         72*       23 A(1,J)= DX(1,J)         73*       CALL MATIN(A, IJ;6)         74*       D0 24 J=1;6         75*       D0 24 J=1;6         76*       24 AT(1,J) = A(J,T)         77*       C THETA = MOUNTA;6 ANGLE OF VEHICLE WITH FLATFORM, DEG.         78*       1000 READ(5,2) THETA         79*       If=IT+1         60*       IF(THETA.6f.99.) GO TO 9999         81*       WRITE(G,15) II.FITHE         62*       15 FORMAT(1H1.* CASE*, I3*10/6/8X*1046//1046// )         63*       C W= WEIGHT OF PLATFORM, PART OF ACTUATORS AND PAYLOAD, LB         84*       C Xw= C.6. LOCATION OF WEIGHT W.R.T. CENTER OF GIMBAL / IN.         85*       READ(5,2) W(Xa(1), 1=1,3)         86*       C XGUN = POSITION OF WEAPON MOUNTING POINT W.R.T. C.6. CF WEIGHT         87*       READ(5,2) (TRGT(1), 1=1,3)         80*       C TKGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         89*       READ(5,2) (TRGT(1), 1=1,3)         90*       C TKGT = POSITION OF TARG	66*			DX(4,J) = DX(3,J) * (XP(2,J) - C(2)) - DX(2,J) * (XP(3,J) - C(3))
68*       7 DX(5,J) = DX(2,J)*(XP (1,J)-C (1) )-DX(1,J)*(XP (2,J)-C (2) )         69*       D0.23 I=1;6         70*       D0.23 J=1;6         71*       B(J,I) = DX(1;J)         73*       CALL MATIN(A;LJ;6)         74*       D0.24 J=1;6         75*       D0.24 J=1;6         76*       24 AT(1;J) = A(J;I)         77*       C         78*       ID00 READ(5;2) THETA         79*       IT=1;t+1         60*       IF(THETA:GE:99.) GO TO 9999         61*       WRITE(G:15) IT,TITLE         62*       15 FORMAT(1H1;* C:SE*; IS;10A6/8X;10A6//10A6// )         83*       C         84*       C Xwc G:6. LCCATION OF WEAPON MCUNTING POINT W:R.T. C.G. CF WEIGHT         65*       READ(5;2) w; (Xn(1); I=1;3)         66*       C XGUN = POSITION OF WEAPON MCUNTING POINT W:R.T. C.G. CF WEIGHT         67*       READ(5;2) (TRGT(1); I=1;3)         90*       C TY GGT = POSITION OF TARGET W:R.T. CENTER OF PITCH GIMBAL         89*       READ(5;2) (XGUL)(I); I=1;3)         90*       C TRGT = POSITIO	67*			DX((5,J) = -DX((3,J)) * (XP((1,J)) - C((1))) + DX((1,J)) * (XP((3,J)) - C((3)))
69*       D0 23 J=1:6         70*       D0 23 J=1:6         71*       B(J,I) = DX(I,J)         72*       23 A(I,J) = DX(I,J)         73*       CALL MATIN(A,IJ,6)         74*       D0 24 J=1:0         75*       D0 24 J=1:0         76*       24 AT(I,J) = A(J,I)         77*       C THETA = MOUNTING ANGLE OF VEHICLE WITH PLATFORM, DEG.         76*       1000 READ(5:2) THETA         79*       If=IT+1         60*       IF(THETA:6F:99:) GO TO 9999         81*       WRITE(6:15) II.TITILE         82*       15 FORMAT(1H1: CASE':13:10A6/8X:10A6//10A6//)         83*       C W= WRITE(0:15) U.I.TITILE         82*       15 FORMAT(1H1: CASE':13:10A6/8X:10A6//10A6//)         83*       C W= WRITE(0:15) U.I.TITILE         82*       15 FORMAT(1H1: CASE':13:10A6/8X:10A6//10A6//)         83*       C W= WRITE(0:10:10) F WEIGHT W.R.T. CENTER OF GIMBAL , IN.         85*       READ(5:2) W:(Xa(1):1:=1:3)         86*       C TKGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         89*       READ(5:2) (IRGT(I):1=1:3)         90*       C RY AND RZ ARE THE GIMBAL PITCH AND YAW         91*       READ (5:2) RY:NZ         92*       2 FORMAT(6E10:0)	68*		7	DX(b,J) = DX(2,J) * (XP(1,J) - C(1)) - DX(1,J) * (XP(2,J) - C(2))
70*       D0 23 J=1:6         71* $B(J,I) = DA(I,J)$ 72*       23 A(I,J) = DA(I,J)         73*       CALL MATIN(A:LJ,G)         74*       D0 24 J=1:0         75*       D0 24 J=1:0         76*       24 AT(I,J) = A(J,I)         77*       C       THETA = MOUNTING ANGLE OF VEHICLE WITH PLATFORM, DEG.         78*       1000 READ(5,2) THETA         79*       IT=IT+1         60*       IF(HETA.GI.99.) GO TO 9999         81*       WRITE(0,15) II.JIILE         82*       15 FORMAT(1H1,* CASE*I3.10/6/8X.10A6//10A6//)         83*       C W= ULGHT OF PLATFORM, PART OF ACTUATORS AND PAYLOAD, LB         84*       C Xw= C.G. LOCATION OF WEIGHT W.R.T. CENTER OF GIMBAL , IN.         85*       READ(5,2) W.(X_R(1).1=1.3)         86*       C XGUN = POSITION OF WEAPON MOUNTING POINT W.R.T. C.G. CF WEIGHT         67*       READ(5,2) (IRGT(1).I=1.3)         88*       C TRGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         89*       READ(5,2) (IRGT(1).I=1.3)         90*       C RY AND RZ ARE THE GIMBAL PITCH AND YAW         81*       READ (5,2) RY.RZ         92*       2 FORMAT(6E10.0)         93*       RY = RY+HHETA         94*       RADY =	69*			DU 23 I=1+6
71*       B(J,I) = DX(I,J)         72*       23 A(I,J) = DX(I,J)         73*       CALL MATIN(A,IJ,6)         74*       D0 24 J=1.0         75*       D0 24 J=1.0         76*       24 AT(I,J) = A(J,I)         77*       C THETA = MOUNTING ANGLE OF VEHICLE WITH PLATFORM, DEG.         78*       1000 READ(5,2) THETA         79*       If=IT+1         60*       IF(THETA.GT.99.) GO TO 9999         81*       WRITE(G,15) II,TITLE         82*       15 FORMAT (IH1.* CASE*,13,10A6/8X,10A6//10A6// )         83*       C W= WEIGHT OF PLATFORM, PART OF ACTUATORS AND PAYLOAD, LB         84*       C Xw= C.G. LCCATION OF WEIGHT W.R.T. CENTER OF GIMBAL , IN.         85*       READ(5,2) w,(Xa(1),I=1,3)         86*       C XGUN = POSITION OF WEAPON MOUNTING POINT W.R.T. C.G. CF WEIGHT         87*       READ(5,2) (XGU.4(1),I=1,3)         88*       C TRGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         89*       READ(5,2) (TRGT(I),I=1,3)         88*       C TRGT = POSITION OF TARGET PITCH AND YAW         91*       READ(5,2) (TRGT(I),I=1,3)         89*       READ(5,2) RY.KZ         92*       2 FORMAT(6E10.0)         93*       RY = RY*RAD         94*       RADY =	70*			DU 23 J=1,6
72*       23 A(I,J) = D/(I,J)         75*       CALL MATIN(A,IJ,6)         74*       D0 24 J=1,0         75*       C0 24 J=1,0         76*       24 AT(I,J) = A(J,I)         77*       C THETA = MOUNTING ANGLE OF VEHICLE WITH PLATFORM, DEG.         76*       1000 READ(5,2) THETA         79*       If=IT+1         60*       IF(THETA.GT.99.) GO TO 9999         81*       WRITE(0,15) II,TITLE         82*       C W= WEIGHT OF PLATFORM, PART OF ACTUATORS AND PAYLOAD, LB         84*       C Xw= C.G. LOCATION OF WEIGHT W.R.T. CENTER OF GIMBAL , IN.         85*       RCAD(5,2) w(X_R(1),I=1,3)         86*       C XGUN = POSITION OF WEIGHT W.R.T. CENTER OF PITCH GIMBAL         87*       READ(5,2) (XGUA(I),I=1,3)         88*       C TRGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         89*       READ(5,2) (TRGT(I),I=1,3)         80*       C TRGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         89*       READ(5,2) (TRGT(I),I=1,3)         90*       C RY AND RZ ARE THE GIMBAL PITCH AND YAW         91*       READ (5,2) RY,RZ         92*       2 FORMAT(6E10.0)         93*       RY = RY+RAD         95*       RIMETA =THETA*RAD         96*       RAUZ	71*			$B(J,I) = D_{X}(I,J)$
73*       CALL MATIN(A, LD, 6)         74*       DD 24 i=1;o         75*       DD 24 j=1;o         76*       24 AT(1,J) = A(J,I)         77*       C THETA = MOUNTING ANGLE OF VEHICLE WITH PLATFORM, DEG.         78*       1000 READ(5,2) THETA         79*       IT=IT+1         60*       IF(THETA.GT.99.) GO TO 9999         81*       WRITE(o,15) II,TITLE         82*       15 FORMAT(1H1,* CASE*, I3, 10A6/8X, 10A6//10A6// )         83*       C W= WEIGHT OF PLATFORM, PART OF ACTUATORS AND PAYLOAD, LB         84*       C Xw= C.G. LOCATION OF WEIGHT W.R.T. CENTER OF GIMBAL , IN.         85*       READ(5,2) W, (X_A(1), I=1,3)         86*       C XGUN = POSITION OF WEAPON MOUNTING POINT W.R.T. C.G. CF WEIGHT         87*       READ(5,2) (IRGT(1), I=1,3)         88*       C TRGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         89*       READ(5,2) (IRGT(1), I=1,3)         90*       C RY AND RZ ARE THE GIMBAL PITCH AND YAW         91*       READ (5,2) RY, NZ         92*       2 FORMAT(6E10.0)         93*       RY = RY+HETA         94*       RADU = RY*RAD         95*       RTHETA =THETA*RAD         96*       RAUZ =RZ*RAD	72*		23	$A(I,J) = D_A(I,J)$
74*       D0 24 j=1;0         75*       D0 24 j=1;0         76*       24 AT(I;J) = A(J;T)         77*       C THETA = MOUNTL;6 ANGLE OF VEHICLE WITH PLATFORM, DEG.         78*       1000 READ(5;2) THETA         79*       If=IT+1         60*       IF(THETA:6T:99*) GO TO 9999         61*       WRITE(0;15) II;TITLE         82*       15 FORMAT(1H1*, CASE*;13*10A6/8X*10A6//10A6//)         83*       C w= wEIGHT OF PLATFORM, PART OF ACTUATORS AND PAYLOAD, LB         84*       C Xw= C.G. LOCATION OF WEIGHT W.R.T. CENTER OF GIMBAL , IN.         85*       READ(5;2) w;(Xr,(1)*1=1;3)         86*       C XuGU = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         89*       READ(5;2) (XGU_4(I)*1=1;3)         88*       C TRGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         89*       READ(5;2) (XGU_4(I)*1=1;3)         89*       READ(5;2) (TRGT(I)*1=1;3)         90*       C RY AND RZ ARE THE GIMBAL PITCH AND YAW         91*       READ (5;2) RY:RZ         92*       2 FORMAT(6E10:0)         93*       RY = RY+THETA         94*       RADY = RY*RAD         95*       RTHETA =THETA*RAD         96*       RAUZ =RZ*RAD	73*		-	CALL MATIN(A, IU, 6)
75*         D0         24         J=1:0           76*         24         AT(I,J) = A(J,I)         77*         C         THETA = MOUNTING ANGLE OF VEHICLE WITH PLATFORM, DEG.           76*         1000 READ(5,2) THETA         1000 READ(5,2) THETA         79*         1f=1T+1           60*         IF(THETA.GT.99.) GO TO 9999         81*         WRITE(0,15) II.JITLE         82*           82*         15 FORMAT(1H1,* CASE*,13:10/6/8X:10A6//10A6// )         83*         C         WE           83*         C         W= LGHT OF PLATFORM, PART OF ACTUATORS AND PAYLOAD, LB         84*         C           84*         C         Xw= C.6. LOCATION OF WEIGHT W.R.T. CENTER OF GIMBAL , IN.         85*           85*         READ(5,2) W; (Xn(1), I=1,3)         86*         C         TRGT = POSITION OF WEAPON MOUNTING POINT W.R.T. C.G. CF WEIGHT           87*         READ(5,2) (XGU.(I), I=1,3)         88*         C         TRGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL           89*         READ(5,2) (TRGT(I), I=1,3)         90*         C         RY AND RZ ARE THE GIMBAL PITCH AND YAW           90*         C         RY AND RZ ARE THE GIMBAL PITCH AND YAW         81*         READ (5,2) RY.NZ           92*         2 FORMAT(6E10.0)         93*         RY = RY+THETA           94* <t< th=""><th>74*</th><th></th><th></th><th>DU 24 1=1,0</th></t<>	74*			DU 24 1=1,0
76*       24 AT(I,J) = A(J,T)         77*       C THETA = MOUNTING ANGLE OF VEHICLE WITH PLATFORM, DEG.         78*       1000 READ(5,2) THETA         79*       IT=IT+1         50*       IF(THETA.6T.99.) GO TO 9999         81*       WRITE(0,15) II,TITLE         82*       15 FORMAT(1H1,* CASE*,13,10A6/8X,10A6//10A6//)         83*       C W= WEIGHT OF PLATFORM, PART OF ACTUATORS AND PAYLOAD, LB         84*       C Xw= C.G. LOCATION OF WEIGHT W.R.T. CENTER OF GIMBAL , IN.         85*       READ(5,2) W, (Xnc(1), I=1,3)         66*       C XGUN = POSITION OF WEAPON MOUNTING POINT W.R.T. C.G. CF WEIGHT         67*       READ(5,2) (XGU.(I), I=1,3)         88*       C TRGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         89*       READ(5,2) (TRGT(I), I=1,3)         90*       C RY AND RZ ARE THE GIMBAL PITCH AND YAW         91*       READ (5,2) (TRGT(I), I=1,3)         90*       C RY AND RZ ARE THE GIMBAL PITCH AND YAW         91*       READ (5,2) RY, RZ         92*       2 FORMAT(6E10.0)         93*       RY = RY+THETA         94*       RADY = RY*RAD         95*       RTHETA.=THETA*RAD         96*       RADZ =RZ*RAD	75*			DO 24 J=1.0
77*       C       THETA = MOUNTING ANGLE OF VEHICLE WITH PLATFORM, DEG.         76*       1000 READ(5,2) THETA         79*       IT=IT+1         60*       IF(THETA.GF.99.) GO TO 9999         81*       WRITE(0.15) IT.TITLE         82*       15 FORMAT(1H1,* CASE*, I3, 10A6/8X, 10A6//10A6//)         83*       C         84*       C XW= C.G. LCCATION OF WEIGHT W.R.T. CENTER OF GIMBAL , IN.         85*       READ(5,2) W, (XR(1), I=1,3)         86*       C XGUN = POSITION OF WEIGHT W.R.T. CENTER OF FITCH GIMBAL         87*       READ(5,2) (XGU.(I), I=1,3)         88*       C TRGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         89*       READ(5,2) (TRGT(I), I=1,3)         90*       C RY AND RZ ARE THE GIMBAL PITCH AND YAW         91*       READ (5,2) RY, NZ         92*       2 FORMAT(6E10.0)         93*       RY = RY+THETA         94*       RADY = RY*RAD         95*       RTHETA =THETA*RAD         96*       RAUZ =RZ*RAD	76*		24	AT(I,J) = A(J,I)
76*       1000 READ(5,2) THETA         79*       I[=IT+1         60*       IF(THETA.GT.99.) GO TO 9999         81*       WRITE(6,15) II.TITLE         82*       15 FORMAT(1H1,* CASE*,13,10A6/8X,10A6//10A6//)         83*       C W= WEIGHT OF PLATFORM, PART OF ACTUATORS AND PAYLOAD, LB         84*       C Xw= C.G. LOCATION OF WEIGHT W.R.T. CENTER OF GIMBAL , IN.         85*       READ(5,2) W,(XR(1),I=1,3)         86*       C XGUN = POSITION OF WEAPON MOUNTING POINT W.R.T. C.G. CF WEIGHT         67*       READ(5,2) (XGUA(I),I=1,3)         88*       C TRGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         89*       READ(5,2) (TRGT(I),I=1,3)         90*       C RY AND RZ ARE THE GIMBAL PITCH AND YAW         91*       READ (5,2) RY:NZ         92*       2 FORMAT(6E10.0)         93*       RY = RY+THETA         94*       RADY = RY*RAD         95*       RTHETA*RAD         96*       RADZ =RZ*RAD	77*	C	TH	ETA = MOUNTING ANGLE OF VEHICLE WITH PLATFORM, DEG.
79*       IT=IT+1         60*       IF(THETA.GT.99.) GO TO 9999         81*       WRITE(0,15) IT.TITLE         82*       15 FORMAT(1H1,* CASE*, I3,10A6/8X,10A6//10A6//)         83*       C W= WEIGHT OF PLATFORM, PART OF ACTUATORS AND PAYLOAD, LB         84*       C Xw= C.G. LCCATION OF WEIGHT W.R.T. CENTER OF GIMBAL , IN.         85*       READ(5,2) W, (XR(1), I=1,3)         86*       C XGUN = POSITION OF WEAPON MOUNTING POINT W.R.T. C.G. CF WEIGHT         67*       READ(5,2) (XGU.(I), I=1,3)         88*       C TRGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         89*       READ(5,2) (TRGT(I), I=1,3)         90*       C RY AND RZ ARE THE GIMBAL PITCH AND YAW         91*       REAU (5,2) RY, NZ         92*       2 FORMAT(6E10.0)         93*       RY = RY+THETA         94*       RADY = RY*RAD         95*       RTHEJA =THETA*RAD         96*       RAUZ =RZ*RAD	78*		1000	READ(5,2) THETA
60*       IF(THETA.GT.99.) GO TO 9999         81*       WRITE(6,15) II,TITLE         82*       15 FORMAT(1H1,* CASE*,13,10A6/8X,10A6//10A6//)         83*       C w= WEIGHT OF PLATFORM, PART OF ACTUATORS AND PAYLOAD, L8         84*       C Xw= C.G. LOCATION OF WEIGHT W.R.T. CENTER OF GIMBAL , IN.         85*       READ(5,2) W, (Xn(1), I=1,3)         86*       C XGUN = POSITION OF WEAPON MOUNTING POINT W.R.T. C.G. CF WEIGHT         87*       READ(5,2) (XGUA(1), I=1,3)         88*       C TKGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         89*       READ(5,2) (TRGT(1), I=1,3)         90*       C RY AND RZ ARE THE GIMBAL PITCH AND YAW         91*       READ (5,2) RY.NZ         92*       2 FORMAT(6E10.0)         93*       RY = RY+THETA         94*       RADY = RY*RAD         95*       RTHETA =THETA*RAD         96*       RAUZ =RZ*RAD	79*			_I(=1T+1
81*       WRITE(6,15) IT,TITLE         82*       15 FORMAT(1H1,* CASE*,13,10A6/8X,10A6//10A6//)         83*       C W= WEIGHT OF PLATFORM, PART OF ACTUATORS AND PAYLOAD, LB         84*       C Xw= C.G. LOCATION OF WEIGHT W.R.T. CENTER OF GIMBAL , IN.         85*       READ(5,2) W,(Xm(1),I=1,3)         86*       C XGUN = POSITION OF WEAPON MOUNTING POINT W.R.T. C.G. CF WEIGHT         87*       READ(5,2) (XGUA(1),I=1,3)         88*       C TRGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         89*       READ(5,2) (TRGT(I),I=1,3)         90*       C RY AND RZ ARE THE GIMBAL PITCH AND YAW         91*       READ (5,2) RY,RZ         92*       2 FORMAT(6E10.0)         93*       RY = RY+THETA         94*       RADY = RY*RAD         95*       RTHETA =THETA*RAD         96*       RAUZ =RZ*RAD	60*			IF(THETA.GT.99.) GO TO 9999
82*       15 FORMAT(1H1,* CASE*,13,10A6/8X,10A6//10A6//)         83*       C       W= WEIGHT OF PLATFORM, PART OF ACTUATORS AND PAYLOAD; LB         84*       C       Xw= C.G. LOCATION OF WEIGHT W.R.T. CENTER OF GIMBAL ; IN.         85*       RCAD(5;2) W; (Xm(1);1=1;3)         86*       C       XGUN = POSITION OF WEAPON MOUNTING POINT W.R.T. C.G. CF WEIGHT         87*       READ(5;2) (XGUM(1);1=1;3)         88*       C       TRGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         89*       READ(5;2) (TRGT(1);1=1;3)         90*       C       RY AND RZ ARE THE GIMBAL PITCH AND YAW         91*       READ (5;2) RY:RZ         92*       2 FORMAT(6E10:0)         93*       RY = RY*RAD         94*       RADY = RY*RAD         95*       RTHEIA =THETA*RAD         96*       RAUZ =RZ*RAD	81*			WRITE(0,15) IT, TITLE
83*       C       W= WEIGHL OF PLATFORM, PART OF ACTUATORS AND PAYLOAD, L8         84*       C       Xw= C.G. LOCATION OF WEIGHT W.R.T. CENTER OF GIMBAL , IN.         85*       READ(5,2) W, (Xn(1), I=1,3)         86*       C       XGUN = POSITION OF WEAPON MOUNTING POINT W.R.T. C.G. CF WEIGHT         67*       READ(5,2) (XGUn(1), I=1,3)         88*       C       TRGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         89*       READ(5,2) (TRGT(1), I=1,3)         90*       C       RY AND RZ ARE THE GIMBAL PITCH AND YAW         91*       REAU (5,2) RY.RZ         92*       2 FORMAT(6E10.0)         93*       RY = RY+THETA         94*       RADY = RY*RAD         95*       RTHETA =THETA*RAD         96*       RAUZ =RZ*RAD	82*		15	FORMAT(1H1+' CASE'+13+10A6/8X+10A6//10A6//)
84*       C       Xw= C.G. LOCATION OF WEIGHT W.R.T. CENTER OF GIMBAL , IN.         85*       READ(5,2) W,(Xk(1),I=1,3)         86*       C       XGUN = POSITION OF WEAPON MOUNTING POINT W.R.T. C.G. CF WEIGHT         87*       READ(5,2) (XGUn(1),I=1,3)         88*       C       TRGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         89*       READ(5,2) (TRGT(1),I=1,3)         90*       C       RY AND RZ ARE THE GIMBAL PITCH AND YAW         91*       READ (5,2) RY,RZ         92*       2 FORMAT(6E10.0)         93*       RY = RY+THETA         94*       RADY = RY*RAD         95*       RTHETA =THETA*RAD         96*       RAUZ =RZ*RAD	83*		W=	WEIGHT OF PLATFORM, PART OF ACTUATORS AND PAYLOAD, LB
65*       READ(5+2) W+(Xn(1)+I=1+3)         66*       C XGUN = POSITION OF WEAPON MOUNTING POINT W+R+T. C.G. CF WEIGHT         67*       READ(5+2) (XGUn(1)+I=1+3)         88*       C TRGT = POSITION OF TARGET W+R+T. CENTER OF PITCH GIMBAL         89*       READ(5+2) (TRGT(1)+I=1+3)         90*       C RY AND RZ ARE THE GIMBAL PITCH AND YAW         91*       READ (5+2) RY+RZ         92*       2 FORMAT(6E10+0)         93*       RY = RY+THETA         94*       RADY = RY*RAD         95*       RTHETA =THETA*RAD         96*       RADZ =RZ*RAD	84*	C	Xiv	= C.G. LOCATION OF WEIGHT W.R.T. CENTER OF GIMBAL , IN.
66*       C XGUN = POSITION OF WEAPON MOUNTING POINT W.R.T. C.G. CF WEIGHT         67*       REAU(5;2) (XGU.(I),I=1;3)         88*       C TRGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         89*       READ(5;2) (TRGT(I);I=1;3)         90*       C RY AND RZ ARE THE GIMBAL PITCH AND YAW         91*       REAU (5;2) RY:RZ         92*       2 FORMAT(6E10:0)         93*       RY = RY+THETA         94*       RADY = RY*RAD         95*       RTHEIA =THETA*RAD         96*       RAUZ =RZ*RAD	85*			$READ(5/2) w (X_{n}(1) / 1=1/3)$
87*       READ(5+2) (XGU_4(1)+I=1.3)         88*       C       TRGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         89*       READ(5+2) (TRGT(1)+I=1.3)         90*       C       RY AND RZ ARE THE GIMBAL PITCH AND YAW         91*       READ (5,2) RY.RZ         92*       2 FORMAT(6E10.0)         93*       RY = RY+THETA         94*       RADY = RY*RAD         95*       RTHEIA =THETA*RAD         96*       RAUZ =RZ*RAD	66*	C	XG	UN = POSITION OF WEAPON MOUNTING POINT W.R.T. C.G. CF WEIGHT
88*       C       TRGT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL         89*       READ(5+2) (TRGT(I)+I=1+3)         90*       C       RY AND RZ ARE THE GIMBAL PITCH AND YAW         91*       READ (5+2) RY+RZ         92*       2 FORMAT(6E10+0)         93*       RY = RY+THETA         94*       RADY = RY*RAD         95*       RTHETA =THETA*RAD         96*       RAUZ =RZ*RAD	8/*			$REAU(5i2) (XGU_{i}(I), I=1,3)$
89*       READ(5+2) (TRGT(I)+I=1+3)         90*       C       RY AND RZ ARE THE GIMBAL PITCH AND YAW         91*       READ (5+2) RY+RZ         92*       2 FORMAT(6E10+0)         93*       RY = RY+THETA         94*       RADY = RY*RAD         95*       RTHETA =THETA*RAD         96*       RAUZ =RZ*RAD	*88	C	TR	GT = POSITION OF TARGET W.R.T. CENTER OF PITCH GIMBAL
90*CRYANDRZARETHEGIMBALPITCHANDYAW91*READ(5,2)RY:RZ92*2FORMAT(6E10.0)93*RY = RY+THETA94*RADY = RY*RAD95*RTHETA =THETA*RAD96*RADZ =RZ*RAD	89*			READ(5:2) (TRGT(1):1=1:3)
91*     READ (5,2) RY:RZ       92*     2 FORMAT(6E10.0)       93*     RY = RY+THETA       94*     RADY = RY*RAD       95*     RTHETA =THETA*RAD       96*     RAUZ =RZ*RAD	90*	C	RY	AND RZ ARE THE GIMBAL PITCH AND YAW
92*     2 FORMAT(GE10.0)       93*     RY = RY+THETA       94*     RADY = RY*RAD       95*     RTHETA =THETA*RAD       96*     RAUZ =RZ*RAD	51*			KEAD (5/2) RY/RZ
Y2*         RY = RY+1HE LA           94*         RADY = RY*RAD           95*         RTHETA =THETA*RAD           96*         RADZ =RZ*RAD	92*		2	FURMAT(GELU-U)
94* RAUT = RT*RAU 95* RTHETA = THETA*RAD 96* RAUZ = RZ*RAD	¥3*	****		KI = KI + I + I A
96* RAUZ =RZ*RAD	94*			
	90*			<u> NINE JA ITE JA本KAU</u> DN1-2
	ンロギ			

97*	CALL RT2(ROT2/RADY)
98*	CALL R13 (ROT3/RADZ)
99*	CALL MATMAT (ROT3, KOT2, ROT, 3, 3)
00*	CALL MATMAT (RUT IXP IXP11613)
01*	CALL MATVEC(ROT, C, C1, 3)
02*	WRITELUISI) W
03*	81 FORMAT(9X, 'ACTING WEIGHT ='+F16.1, 'LBS'//)
04*	WRITE(6,26)
05*	26 FORMAT(9X'COORDINATES, INCH '7X'X', 11X'Y', 11X'Z'/)
06*	WRITE(6,29) ((XW(I), I=1,3), (XGUN(I), I=1,3), (TRGT(I), I=1,3))
07*	29 FORMAT(9X'C.G. OF WEIGHT '3F12.3/9X'WEAPON MOUNTING POINT'
08*	1 3F12+3/9X+'TARGET ' 3F12+3/)
09*	C MEDIA 1 = OIL
10*	C MEDIA 2 = NITROGEN
11*	READ(5,22) MEDIA
12*	22 FORMAT(12)
13*	WRITE(6,96) THETA
14*	96 FORMATIZ 74X MOUNTING ANGLE OF VEHICLE WITH PLATFORMA DEG.
15*	1 F10.2)
16*	WRITE (6180) RYIRZ
17*	80 FORMAT(//9X'GIMBAL ROTATION/ DEG. //
18*	
19*	
20*	C = EFFECTIVE VOLUME OF ALLOMOLATORY IND
21*	$1F(MEDIA \cdot EQ \cdot I) = GO(10) = 200$
22 <b>*</b>	$A = 2000 \bullet$
23*	
<u>297</u>	
264	$\frac{90}{200} = \frac{10}{200} = \frac{23000}{200}$
27+	$\Delta K_{M} M = 20000$
28*	V = 117.5
29*	201 CONTINUE
.30*	C AKMAX, AKMIN = ACTUATOR STIFFNESS MAX. AND MIN. RESP.
.31*	IF (MEDIA.EQ.1) WRITE (6,82) V, AKMAX, AKMIN
.32*	IF (MEDIA . EQ. 2) WRITE (6, 182) V, AKMAX, AKMIN
.33*	82 FURMAT( /3X'DAMPING MEDIA OIL '//
.34*	1 <u>3X'EFFECTIVE VOLUME OF ACCUMULATOR = 'F10.1,' IN3 '/</u>
.35*	2 3X'MAXIMUM ACTUATOR STIFFNESS = 'F10.1,' LB/IN'/
136*	3 3X'MINIMUM ACTUATOR STIFFNESS = 'F10.1.' LB/IN'/)
.37*	182 FORMAT(///3X'DAMPING MEDIA NITROGEN'//
138*	1 <u>3X'EFFECTIVE VOLUME OF ACCUMULATOR = 'F10.1.' IN3</u>
.39*	2 3X MAXIMUM ACTUATOR STIFFNESS = 'F10.1,' LB/IN'
140*	3 3X'MINIMUM ACTUATOR STIFFNESS = 'F10.1,' LB/1N'//
141*	999 FORMAT(2X///)
142*	99 FORMAT(/16/)
.43*	C CALCULATE FORCE AND MOMENT COMPONENTS
.44*	$p_0 = 8$ $1 = 1 \cdot 3$
.45*	8 F(1) = 0.0
.46*	$F(3) \equiv N$
14/*	RADIT = -RADT
148*	$\frac{RAU12}{CAUL} = \frac{1}{RAU4}$
149*	
151-	$\frac{UALL KIJ(KIJ)KAUIZ}{CALL MATMAT(DIT3,DIT,3,3)}$
101*	
1574	CALL MAIVEC (GOT. YW. YWI.3)
1004	

154*	CALL MATVEC(ROT, XGUN, XGUN1, 3)
155*	F1(4) = F(3)*(XW1(2) - C1(2)) - F(2)*(XW1(3) - C1(3))
156*	F1(5) = F(1)*(Xw1(3) - C1(3)) - F(3)*(Xw1(1) - C1(1))
157*	F1(6) = F(2)*(XW1(1) - C1(1)) - F(1)*(XW1(2) - C1(2))
:58*	C FAEACTUATOR FORCE I B
59*	100 FORMAT(6F15.6)
60*	
61*	
62*	
674	
1004	
.04 <b>*</b>	SF0(1)=0.0
.05*	SEC(1)=0.0
.66*	D0 52 J=1+6
.67*	RUTT(1,J)=0,0
-68*	ROIT1(I,J)=0.0
.69*	SKO(I,J) = 0.0
.70*	-SK(I,J) = 0.0
.71*	AK1(I,J) = 0.0
72*	$52 \text{ SK}(1, \omega) = 0.0$
73*	$D_{0}$ 112 $I=1\cdot 3$
74*	
75*	
76+	
77+	
70.0	
78*	112  ROT(1+3) = RT(1,3)
19*	C LOC = CODE FOR LOCATION OF DESIRED STIFFNESS
80*	C 1. AT MIG. PLATFORM, 2. AT C.G. OF VEHICLE, 3. AT WEAPON MTG. PT.
81*	READ(5,22) LOC
82*	C SK = STIFFNESS REQUIRED IN WEAPON COORDINATE SYSTEM
83*	67  READ  (5,2) (SK(1,1),1=1,6)
84*	IF(LOC+LT+3) G0 T0 70 +
85*	DO 45 I=1,3
86*	45 XTRGT(I)=TRGT(I)-(XGUN1(I)+XW1(I))
87*	STRGT=0.0
88*	D0 46 1=1,3
89*	46 STRGT=STRGT+XTRGT(T)**2
90*	STRGT_SORT (STRGT)
91*	
92*	
03+	$\begin{array}{c} 0 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\$
0/1+	$T_{1} = 3n \sqrt{1/1} = 3n \sqrt{1/1} + 1/(1/1) + 1/4$
277	
06 +	
90*	READ(5)2) RECOL
9/*	
98*	75 SFO1(I)=RECOLE*DT(I)
99*	CALL MATVEC (ROTT: SF01: SF0: 6)
00*	WRITE(6,103) RECOIL
01*	103 FORMAT(/3X, 'RECOIL LOAD =', F10.1,' LBS!//)
02*	WRITE(6,66)
03*	66 FORMAT(14X, 'REQUIRED STIFFNESS AT WEAPON MOUNTING POINT'/)
04*	C TRANSFER WEAPON STIFFNESS TO PLATFORM SYSTEM
05*	X1 = XGUN(1) + XW(1) - C(1)
06*	Y1=xGUN(2)+XW(2) -C(2)
07*	Z1=XGUN(3)+XW(3) -C(3)
08*	$CALL R6T2(R6T \cdot 0 \cdot X1 \cdot Y1 \cdot Z1)$
()9×	D0 121 T=1.6
10*	$D(121) J = 1 \cdot 6$
¥07	
	11

11*	121 R6TT(I,J)=R6T(J,I)
12*	CALL_MATMAT(R61,SK0,RSK,6,6)
13*	CALL MATMAT(RSK+R6TT+SK01+6+6)
14*	CALL MATVEC(R6T, SF0, SF, 6)
15*	D0 27 I=1+6
16*	D0_27_J=1+6
17*	IF (SK01(I,J).LT. 1.0) GO TO 27
18*	IF(SF(I).LT. 1.0) GO TO 27
19*	SK1(1/J) = 1./SK01(1/J)
20*	27 CONTINUE
21*	$\frac{60}{10} \frac{10}{71}$
22*	$\frac{C}{20} = EXTERNAL FORLES$
204	$\frac{10}{10} \frac{10}{10} 10$
25*	DO 123 T=1.6
201	103 CE(1) = CEO(1)
207	122 WRITE(6.72)
28*	72  FORMAT(/144) = YTERMAL LOADS ()
29*	WRITE(6, 94) (SEO(T), I=1.6)
30*	94 FORMAT( 31x1x1+12X1Y1+12X171//4X1FORCE+ 18. 1+3F12-1/
31*	1 4X MOMENTE IN 1 B. 1.3F12.1/)
32*	IF(1,0C,FQ,1) GO TO 74
33*	$IF(10C \cdot FQ \cdot 2)$ WRITE(6,65)
34*	65 FORMAT(14X, 'REQUIRED STIFFNESS AT C.G. OF VEHICLE !/)
35*	GO TO 97
36*	74 WRITE(6,64)
37*	64 FORMAT(14X, 'REQUIRED STIFFNESS AT MOUNTING PLATFORM '/)
38*	DO 150 I=1,6
39*	150 SKO(I,I)=SK(I,I)
40*	GO TO 28
:41*	97 RTHETA = $-RTHETA$
:42*	$\chi_1 = \chi_{\chi_1}(1) - c_1(1)$
:43*	Y1 = XW1(2) - C1(2)
44*	$Z1 = X_{N}1(3) - C1(3)$
45*	CALL RGT2(RGT, RTHETA, X1, Y1, Z1)
246*	CALL MATVEC (R61, SF0, SF, 6)
247*	$DO \ 300 \ I=1/6$
:48*	1 + (SK(1) + (-1) +
249*	SUI(1/=SFO(1//SK(1/1)
15U*	
101*	
1574	CALL MATVEC(DET1, CD1, CD, C)
100+ 154*	$WRITE(6.13)(CD(1) \cdot 1 - 1 \cdot 6)$
155*	CO TO 373
156*	28 DO 21 J=1.6
157*	D0 21 J=1+6
158*	21  SKO1(1.1) = SKO(1.1)
159×	31 DO 73 I=1+6
260*	D0 73 J=1.6
261*	IF (SK01(I,J).LT. 1.0) GO TO 73
262*	$SK1(I_{J}) = 1./SK01(I_{J})$
263*	73 CONTINUE
264*	373 CONTINUE
265*	71 WRITE(6,104)(SK(I,I),I=1,6)
266*	104 FORMAT( 31x'x', 12x'Y', 12x'Z'//4x'TRANSLATION, LB/IN', 3F12.1/
267*	1 4X'ROTATION, IN.LB/RAD', 3F12.1/)

268*	20 FORMAT(6F12.1/)
269*	IF(LOC.EQ.2) GO TO 245
270*	CALL MATVEC(SK1,SF,SD,6)
271*	C TRANSFORMATION OF FORCES TO CENTER OF GIMBAL
:72*	245 D0 42 I=1+0
:73*	42 SFC(I)=SF(I)+F1(I)
274*	SFC(4)=SFC(4)-SFC(2)*C(3)
275*	SFC(5)=SFC(5)+SEC(1)*C(3)
276*	SFC(6) = SFC(6)
:77*	WRITE(6,124)
:78*	124 FORMAT(/14X'FORCES AT PITCH GIMBAL IN ITS COORDINATE SYSTEM!/)
:79*	WRITE(6,94) (SEC(I), I=1,6)
180*	CALL MATVEC(B,SD,AD,6)
101*	CALL MATVEC (A: SF; AF; 6)
102*	
:03*	AK(1) = AF(1) / AD(1)
184*	50  AK1(1,1)=1.7 AK(1)
100×	CALL MAIMAI(AI)AKI)AAK)616)
1007	CALL MAIMAI(AAKIA ISSKI6)6)
101+	
180¥	$\frac{1}{77} = \frac{1}{77} = \frac{1}{10} \frac{1}{10} \frac{1}{10} \frac{1}{100} = \frac{1}{100} \frac{1}{100} = \frac{1}{100} \frac{1}{100} \frac{1}{100} \frac{1}{100} = \frac{1}{100} \frac$
90 <b>x</b>	11. UVINE TOUT ACTUATOR FORCES AND DISPLACEMENTS DUE TO 77 8X ACTUATOR
91*	$\frac{1}{1} + \frac{1}{1} + \frac{1}$
92*	$\frac{75}{75} = \frac{75}{75} = 75$
93*	$\begin{array}{c} \text{D0}  \text{G}  IIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIII$
94*	9  DP(1) = FA(1)/AP
95*	C = AK = ACTUATOR STIFFNESS I B/TH
96*	102 FURMAT(3E15.6)
97*	C CHECK IF ACTUATOR STIFFNESS IS WITHIN RANGE
98*	DU 10 I=1,3
99*	IF (AK(I).GT.AKMIN)GO TO 11
00*	WRITE (6,13) AK(I), AKMIN
01*	GU TO 10
02*	13 FORMAT(6F15.4)
03*	11 IF (AK(I), LT, AKMAX) GO TO 10
04*	WRITE (6,13) AK(I), AKMAX
05*	10 CONTINUE
05*	C CALCULATE ACTUATOR PRESSURES
0.0 *	
00*	$\frac{P_{10}P_{11}-(AK(1)*V/(2**AP**2))-0*5*0P(1)}{10}$
10*	$\frac{1}{10000000000000000000000000000000000$
11*	107 FORMAT (//1984 ACTUATOD STIEFNESS AND ODESCUDECT/
12*	107 TORMAT 17/10A ACIDATOR STIFFNESS AND PRESSURES!
13*	2STIFFNESS TOP PRESSURE BOT, DESSURE 1/21Y 11 9/TNL.10V
14*	2'PST' 14X'PST'/)
15*	WRITE(6,101) (1,AK(1),PTOP(1),PBOT(1),I=1,6)
16*	101 FORMAT(9X, 11, 3F17.1)
17*	C PR = PRECHARGE PRESSURE, PSI (FOR NITROGEN ONLY)
18*	IF (MEDIA.EQ.1) GO TO 203
19*	D0 205 I=1+6
20*	205 PR(I) = PTOP(I) * V/VO
21*	WRITE(6,202)
22*	202 FORMAT(//24X'ACTUATOR PRECHARGE'/24X'
<u>&lt;3</u> *	1 //19X'ACTUATOR '7X'PRECHARGE (PSI)'/ )
24*	D0 206 I=1+6

25*		IF(FA(I).LT. 0.0) GO TO 207
26*		WRITE(6,209) I, PR(I)
27*	209	FORMAT(20X,11,1 (TOP)',F17.1)
28*		GO TO 206
29*	207	WRITE(6/208) I, PR(I)
30*	208	FORMAT(20X+11+ (BOTTOM)++F14.1)
31*	206	CONTINUE
32*		GO TO 230
33*	203	D0 250 I=1+6
34*		PRI(I)=PTOP(I)*V/235.
35*	250	PRB(I)=PBOT(I)*V/235.
36*		WRITE(6,222)
37*	222-	FORMAT(//24X'ACCUMULATOR PRECHARGE'/24X'
38*	1	//15X'NO.', 8X'TOP', 10X'BOTTOM'/)
39*		WRITE(6,290)(1,PRT(1),PRB(1),I=1,6)
40*	290	FORMAT (16X, 11, 2F14, 1)
41*	230	WRITE(6,530)
42*	530	FORMAT(//1H1//)
43*		WRITE(6,531)
44*	531	FORMAT(/ 20X RESULTANT FLEXIBILITY AT THE REQUIRED LOCATION //
45*		WRITE(6,511) ((SSK(I,J),J=1,6),I=1,6)
46*	511	FORMAT( 2X+6E12+67)
47*		CALL MATIN(SSK+ID+6)
48*		WRITE(6,210)
49*	210	FORMAT(/ 20X RESULTANT STIFFNESS AT THE REQUIRED LOCATION //)
50*		WRITE(6,211) ((SSK(I,J),J=1,6),I=1,6)
51*	211	FORMAT( 2X+6F12+1/)
52*		GO TO 1000
53*	9999	STOP
54*		END
	-	
*		

R6T3 3/12/74-13:	04:10 (,0)	
INE R6T3	ENTRY POINT 000103	
USED: CODE	(1) 000124; DATA(0) 000026; BLANK_COMMON(2) 000000	
L REFERENCE	S (BLOCK+ NAME)	
COS SIN NERR35		
ASSIGNMENT	(BLOCK, TYPE, RELATIVE LOCATION, NAME)	
000017 105 000004 INS	G <u>0001 000020 110G 0001 000043 123G 0001 000044</u> P\$ 0000 I 000001 J	1266
1*	SUBROUTINE R6T3 (R0T2,Q,X,Y,Z)	
2*	DIMENSION ROT2(6,6)	
<u>3</u> ≭ 4∗	$DU \ 1 \ J=1/6$	
_5*	1 ROT2(I,J)=0.0	
6 <b>*</b>	ROT2(1,1)=COS(Q)	
	R012(1/3)-31N(0) R012(2,2)=1.0	
9*	ROT2(3,1) = -SIN(Q)	
10*	ROT2(3,3)=COS(Q)	
10*	D0 2 1-1+3	
13*	$2 \text{ ROT}_2(1+3, J+3) = \text{ ROT}_2(1, J)$	
14*	ROT2(1,5)=-Z	
15*	ROT2(1;6) = Y	
10 <del>*</del> 1 <b>7</b> *	ROT2(2)4)= 2 ROT2(2)6)==X	
18*	ROT2(3,4) = -Y	
19*	ROT2(3,5) = X	
20*		
) OF COMPIL	ATION: NO LIAGNOSTICS.	
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		e
		1
and space in a solub distant space of conversion of the start of the start		1

>

13/06/74-16	2 5:28:25 (+0)	
INE R6T2	ENTRY POINT 000103	
USED: COL	DE(1) 000124; DATA(0) 000026; BLANK COMMON(2) 000000	
	CES (BLOCK + NAME)	
COS		
SIN NERR3\$		
	AT (BLUCK, TYPE, RELATIVE LOCATION, MAME)	
000017 10 000004 10	056 0001 000020 1106 0001 000043 1236 000 NJP5 0000 I 000601 J	1 000044 1266
	SUB-OUTINE ROT2 (ROT2 + Q+X+Y+7)	
1* 2*	SULKOUTINE R6T2(BOT2,Q,X,Y,Z) DIMENSION R0T2(6,6)	
1* 2* 3*	SULMOUTINE R6T2(R0T2,Q,X,Y,Z) DIMENSION R0T2(6,6) D0 1 I=1,6	
1* 2* 3* 4*	SULAOUTINE R6T2(R0T2,Q,X,Y,Z) DIMENSION R0T2(6,6) D0 1 I=1,6 D0 1 J=1,6	
1* 2* 3* 4* 5*	SULROUTINE R6T2(R0T2,Q,X,Y,Z) DIMENSION R0T2(6,6) D0 1 I=1,6 D0 1 J=1,6 1 R0T2(I,J)=0.0	
1* 2* 3* 4* 5*	SULKOUTINE R6T2(R0T2,Q,X,Y,Z) DIMENSION R0T2(6,6) D0 1 I=1,6 D0 1 J=1,6 1 R0T2(I,J)=0.0 R0T2(1,1)=C0S(Q)	
1* 2* 3* 4* 5* 6* 7*	SULKOUTINE R6T2(R0T2,Q,X,Y,Z) DIMENSION R0T2(6,6) D0 1 I=1,6 D0 1 J=1,6 1 R0T2(I,J)=0.0 R0T2(1,1)=C0S(Q) R0T2(1,3)=SIN(Q)	
1* 2* 3* 4* 5* 6* 7* 8*	SULKOUTINE R6T2(R0T2,Q,X,Y,Z) DIMENSION R0T2(6,6) D0 1 I=1,6 D0 1 J=1,6 1 R0T2(I,J)=0.0 R0T2(1,1)=C0S(Q) R0T2(1,3)=SIN(Q) R0T2(2,2)=1.0 P0T2(2,2)=1.0	· · · · · · · · · · · · · · · · · · ·
1* 2* 3* 4* 5* 6* 7* 8* 9*	SULKOUTINE R6T2(R0T2,Q,X,Y,Z) DIMENSION R0T2(6,6) D0 1 I=1,6 D0 1 J=1,6 1 R0T2(I,J)=0.0 R0T2(1,1)=C0S(Q) R0T2(1,3)=SIN(Q) R0T2(2,2)=1.0 R0T2(3,1)=-SIN(Q) R0T2(3,1)=-SIN(Q)	
1* 2* 3* 4* 5* 6* 7* 8* 9* 10*	SULROUTINE R6T2(R0T2,Q,X,Y,Z) DIMENSION R0T2(6,6) D0 1 I=1,6 D0 1 J=1,6 1 R0T2(I,J)=0.0 R0T2(1,1)=COS(Q) R0T2(1,3)=SIN(Q) R0T2(2,2)=1.0 R0T2(3,1)=-SIN(Q) R0T2(3,3)=COS(Q) P0 2 (1=1,4)	· · · · · · · · · · · · · · · · · · ·
1* 2* 3* 4* 5* 6* 7* 8* 9* 10* 11*	SULKOUTINE R6T2(R0T2,Q,X,Y,Z) DIMENSION R0T2(6,6) D0 1 I=1,6 D0 1 J=1,6 1 R0T2(I,J)=0.0 R0T2(1,1)=COS(Q) R0T2(1,3)=SIN(Q) R0T2(2,2)=1.0 R0T2(3,1)=-SIN(Q) R0T2(3,3)=COS(Q) D0 2 I=1,3 D0 2 I=1,3	
1* 2* 3* 4* 5* 6* 7* 8* 9* 10* 11* 12* 13*	SULROUTINE R6T2(R0T2,Q,X,Y,Z) DIMENSION R0T2(6,6) D0 1 I=1,6 D0 1 J=1,6 1 R0T2(I,J)=0.0 R0T2(1,1)=COS(Q) R0T2(1,3)=SIN(Q) R0T2(2,2)=1.0 R0T2(3,1)==SIN(Q) R0T2(3,3)=COS(Q) D0 2 I=1,3 D0 2 J=1,3 2 R0T2(I+3,1+3) = R0T2(I+1)	
1* 2* 3* 4* 5* 6* 7* 8* 9* 10* 11* 12* 13*	SULROUTINE R6T2(R0T2,Q,X,Y,Z) DIMENSION R0T2(6,6) D0 1 I=1,6 D0 1 J=1,6 1 R0T2(I,J)=0.0 R0T2(1,1)=COS(Q) R0T2(1,3)=SIN(Q) R0T2(2,2)=1.0 R0T2(2,2)=1.0 R0T2(3,1)==SIN(Q) R0T2(3,3)=COS(Q) D0 2 I=1,3 D0 2 J=1,3 2 R0T2(I+3,J+3) = R0T2(I,J) P0T2(H,2)=-7	· · · · · · · · · · · · · · · · · · ·
1* 2* 3* 4* 5* 6* 7* 8* 9* 10* 12* 13* 14* 15*	SUDROUTINE R6T2(R0T2,Q,X,Y,Z) DIMENSION R0T2(6,6) D0 1 I=1,6 D0 1 J=1,6 1 R0T2(I,J)=0.0 R0T2(1,1)=C0S(Q) R0T2(1,3)=SIN(Q) R0T2(2,2)=1.0 R0T2(2,2)=1.0 R0T2(3,1)=-SIN(Q) R0T2(3,3)=C0S(Q) D0 2 I=1,3 2 R0T2(I+3,J+3) = R0T2(I,J) R0T2(4,2)=-2 R0(2(4,3)= Y	· · · · · · · · · · · · · · · · · · ·
1* 2* 3* 4* 5* 6* 7* 8* 9* 10* <u>11*</u> 12* 13* 14* 15* 16*	SULROUTINE R6T2(R0T2,Q,X,Y,Z) DIMENSION R0T2(6,6) D0 1 I=1,6 1 R0T2(I,J)=0.0 R0T2(1,1)=COS(Q) R0T2(1,3)=SIN(Q) R0T2(2,2)=1.0 R0T2(3,1)==SIN(Q) R0T2(3,3)=COS(Q) D0 2 I=1,3 2 R0T2(I+3,J+3) = R0T2(I,J) R0T2(4,2)=-Z R0(2(4,3)= Y R0T2(5,1)= Z	· · · · · · · · · · · · · · · · · · ·
$ \begin{array}{c} 1*\\ 2*\\ 3*\\ 4*\\ 5*\\ 6*\\ 7*\\ 8*\\ 9*\\ 10*\\ 11*\\ 12*\\ 13*\\ 14*\\ 15*\\ 16*\\ 17*\\ \end{array} $	SUL: (OUTINE R6T2(ROT2,Q,X,Y,Z) DIMENSION ROT2(6,6) DO 1 J=1,6 1 ROT2(I,J)=0.0 ROT2(1,1)=COS(Q) ROT2(1,3)=SIN(Q) ROT2(2,2)=1.0 ROT2(3,1)=-SIN(Q) ROT2(3,3)=COS(Q) DO 2 J=1,3 2 ROT2(I+3,J+3) = ROT2(I,J) ROT2(4,2)=-Z ROT2(5,1)= Z ROT2(5,3)=-X	
$ \begin{array}{c} 1*\\ 2*\\ 3*\\ 4*\\ 5*\\ 6*\\ 7*\\ 8*\\ 9*\\ 10*\\ 11*\\ 12*\\ 13*\\ 14*\\ 15*\\ 16*\\ 17*\\ 18*\\ \end{array} $	SULHOUTINE R6T2(R0T2,Q,X,Y,Z) DIMENSION R0T2(6,6) DO 1 I=1,6 DO 1 J=1,6 1 R0T2(I,J)=0.0 R0T2(I,J)=COS(Q) R0T2(1,3)=SIN(Q) R0T2(2,2)=1.0 R0T2(3,1)==SIN(Q) R0T2(3,3)=COS(Q) DO 2 I=1,3 DO 2 J=1,3 2 R0T2(I+3,J+3) = R0T2(I,J) R0T2(4,2)=-2 R0T2(5,1)= Z R0T2(5,3)=-X R0T2(6,1)=-Y	
1* 2* 3* 4* 5* 6* 7* 8* 9* 10* 11* 12* 13* 14* 15* 16* 17* 18* 19*	SULHOUTINE R6T2(R0T2, $q, X, Y, Z$ ) DIMENSION R0T2(6,6) DO 1 I=1,6 DO 1 J=1,6 1 R0T2(I,J)=0.0 R0T2(I,J)=COS( $q$ ) R0T2(1,3)=SIN( $q$ ) R0T2(2,2)=1.0 R0T2(3,1)==SIN( $q$ ) R0T2(3,3)=COS( $q$ ) D0 2 I=1,3 D6 2 J=1,3 2 R0T2(I+3,J+3) = R0T2(I,J) R0T2(4,2)==Z R0T2(5,1)= Z R0T2(6,1)==Y R0T2(6,1)==Y R0T2(6,2)= X	
1* 2* 3* 4* 5* 6* 7* 8* 9* 10* 11* 12* 13* 14* 15* 16* 17* 18* 19* 20*	SULROUTINE R6T2(R0T2,Q,X,Y,Z) DIMENSION R0T2(6,6) D0 1 I=1,6 D0 1 J=1,6 1 R0T2(I,J)=0.0 R0T2(I,J)=COS(Q) R0T2(I,J)=SIN(Q) R0T2(2,2)=1.0 R0T2(3,1)=-SIN(Q) R0T2(3,3)=COS(Q) D0 2 I=1,3 2 R0T2(I+3,J+3) = R0T2(I,J) R0T2(4,2)=-Z R0T2(5,1)= Z R0T2(5,1)= Z R0T2(6,1)=-Y R012(6,2)= X R6TURN	
1* 2* 3* 4* 5* 6* 7* 8* 9* 10* 11* 12* 13* 14* 15* 16* 17* 18* 19* 20* 21*	SULMOUTINE R6T2(R0T2,Q,X,Y,Z) DIMENSION R0T2(6,6) D0 1 I=1,6 1 R0T2(1,J)=0.0 R0T2(1,J)=COS(Q) R0T2(1,3)=SIN(Q) R0T2(2,2)=1.0 R0T2(3,1)==SIN(Q) R0T2(3,3)=COS(Q) D0 2 J=1,3 2 R0T2(1+3,J+3) = R0T2(I,J) R0T2(4,2)==Z R0T2(5,1)= Z R0T2(5,3)==X R0T2(6,2)= X RETURN FND	

#### •MATIN:•MATIN 3/06/74-16:28:26 (,0)

### INE MATIN ENTRY POINT 000341

USED: CODE(1) 000361; DATA(0) 000070; BLANK COMMON(2) 000000

L REFERENCES (BLOCK . NAME)

NERR35

ASSIGNMENT (BLOCK, TYPE, RELATIVE LOCATION, NAME)

000062 1	00L 0001	. 00006	5 105L	0001	000015	107G	0001	000021	114G
0000042 1	256 0001	00011	3 1526	0001	000155	1630	0001	000163	170G
000235 2	076 0001	00026	2 217G	0001	000304	231G	0001	000133	310L
000300 7	101 0001	00031	7 7151	0001	000312	720L	0001	000321	740L
000022 0	ETERM 0000	T 00002	4 1	0000	I 000032	ICOLUM.	0000 I	000000	INDEX
000031 1	ROW 000(	T 00002	3 J	0000	I 000032	JCOLUM	0000 I	000031	JROW
000026	0000	T 00003	0 1 1	0000	R 000027	PIVOT	0000 R	000033	SWAP
OCCCED E			diama di seconda di se						

1*	nnon, a ar annahad ddy 114.00 ATE 1000 BAS	SUBROUTINE MATIN(Z, ID, N)	
2*	С	MATRIX INVERSION ONLY	00001:
3*	С		00001:
4*		DIMENSION INDEX( 6.3), Z(N,N)	
5*		EQUIVALENCE (IROW, JROW), (ICOLUM, JCOLUM), (AMAX, T, SWAP)	00001:
6*	°C		00001
7*	C	INITIALIZATION	00001:
8*	Ċ		00001
9*		DETERM=1.0	
10*		D0 20 J=1 (N	00001
11*	20	INDEX(J,3) = 0	00001
12*		D0 550 I=1,N	00001
13*	С		00001
14*	Č	SEARCH FOR PIVOT ELEMENT	00001
15*	C		00001
16*	-	AMAX=0.0	
17*		DO 105 J=1,N	00001
18*		IF (INDEX(J, 3). EQ.1) GO TO 105	00001
19*	and a character solution is a second second second	DO 100 $K=1$ , N	00001
20*		IF (INDEX(K,3)-1) 80, 100, 715	00001
21*	8(	IF(AMAX, GE, ABS(Z(J,K)))GO TO 100	
22*	-	IRO%=J	00001
23*		ICOLUM=K	00001
24*		AMAX = ABS(Z(J,K))	
25*	10	CONTINUE	00001
26*	10	5 CONTINUE	00001
27*		INDEX(ICOLUM, 3) = INDEX(ICOLUM, 3) +1	00001
28*		INDEX(I,1)=IROW	00001
29*		INJEX(1,2)=ICOLUM	00001

	and the second se		
30*	С		00001
31*	<u> </u>	INTERCHANGE ROWS TO PUT PIVOT ELEMENT ON DIAGONAL	00001
32*	С		00001
33*		IF (IROW.EQ.ICOLUMIGO_IO_310	00001
34*			00001
<u>35</u> *			00001
30*		SWAP=2(1ROW) L	00001
304	21		00001
30*	c 20	JU ZYICOLUMILI-SVAP	00001
40*	C	DIVIDE DIVOT ROW BY DIVOT ELEMENT	00001
404 41×	č	DIVIDE FIVOT ROW BY FIVOT ELEMENT	00001
42*	<u> </u>		00001
424	~~~		00001
44*	y.		
45*			00001
46*	31		00001
47*	<u> </u>		00001
48*	<u>c</u>	REDUCE NON-RIVOT ROWS	00001
49*	č		00001
50*	. <u> </u>	DQ 550 L1=1.N	00001
51*			00001
52*			00001
53*			30001
54*			00001
55*	4	50 Z(L1,L) = Z(L1,L) - Z(ICOLUM,L) * T	00001
56*	5	50 CONTINUE	00001:
57*	C		00001
58*	С	INTERCHANGE COLUMNS	00001:
59*	<u> </u>		00001
60*		DO 710 I=1,N	00001.
61*		L=N+1-1	00001
62*		IF(INDEX(L,1).EQ.INDEX(L,2))G0 TO 710	00001
03*		JROW=INDEX(L,1)	00001:
64*		JCOLUM=INDEX(L+2)	00001
65*	· · · · · · · · · · · · · · · · · · ·	DO 705 K=1,::	00001
66*		SWAP=Z(K+JROW)	00001
67*		Z(K, JROW) = Z(K, JCOLUM)	00001
68*		Z(K, JCOLUM)=SWAP	00001
69*		D5 CONTINUE	00001
70*	7	10 CONTINUE	00001
71*		$\sim$ D0 730 K = 1 N	00001
72*		IF(INDEX(K,3).EQ.1)60 TO 720	00001
.73*_		6070715	00001
74*	7	20 CONTINUE	00001.
75*		SU CONTINUE	00001
76*		10 = 1	00001
1/*		<u>60 10 /40</u>	00001
78*	7	15 1D =2	00001
(9*	l		
80*	C	LAST CARD OF PROGRAM	00001
81×		END	

OF COMPILATION:

ч.

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NO DIAGNOSTICS.

291

#### •MATMAT •• MATMAT 3/06/74-16:28:28 (,0)

INE MATMAT ENTRY POINT 000112

USED: CODE(1) 000132; DATA(0) 000042; BLANK COMMON(2) 000000

L REFERENCES (BLOCK, NAME)

NERR3\$

ASSIGNMENT (BLOCK, TYPE, RELATIVE LOCATION, NAME)

000043 1056	0001	000046 110G	0001	000050 114G	<u>0000 I 00000 I</u>
000001 J	0000 I	0000 <b>02</b> K			

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-10

1*	SUBROUTINE MATMAT(A,B,C,M,N)
2*	DIMENSION A(N+N)+B(N+M)+C(N+M)
3*	DO 1 I=1.N
4*	DO 1 J=1.M
5*	C(I,J) = 0.0
6*	DO 1 K=1+N
7*	C(I,J) = C(I,J) + A(I,K) * B(K,J)
8*	RETURN
9*	END

) OF COMPILATION: NO DIAGNOSTICS.

	· · · · · · · · · · · · · · · · · · ·	and a second sec		states a substance of the state of the state of the state		contraction a survey of the second second and the second	a subsequences and a subsequence of the subsection of the subsecti	
					and the second s	the second state of the second state of the second state and the second state of the s		
A new particular state distance and a state of the state	and a start of the	and the second sec	at a substantial and the second second second					
	and the second se				Contraction of the local division of the loc			
				and the strength of the streng	the second s	and the second s	and an over reduced and the state of the sta	
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					and a second			
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•RT2••RT2 03/06/74-16:28:29 (+0)

TINE RT2 ENTRY POINT 000033

USED: CODE(1) 000042; DATA(0) 000012; BLANK COMMON(2) 000000

L REFERENCES (BLOCK . NAME)

COS SIN NERR35

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ASSIGNMENT (BLOCK, TYPE, RELATIVE LOCATION, NAME)

000001 INJP\$

1*	SUBROUTINE RT2(ROT2,Q)	
2*	DIMENSION ROT2(3,3)	
3*	ROT2(1,1) = COS(Q)	1
4*	$ROT_2(1,2) = 0$ .	
5*	ROT2(1,3) = SIN(Q)	
6*	ROT2(2,1) = 0.	
7*	ROT2(2,2) = 1.	/
8*	R0T2(2,3) = 0.	
9*	ROT2(3,1) = -SIN(Q)	
10*	ROT2(3,2) = 0.	
11*	ROT2(3,3) = COS(Q)	
12*	RETURN	
13*	END	
·		
OF COMP	ILATION: NO DIAGNOSTICS.	

.RT3RT3		
3/06/74-16	(28:30 (r.u)	
INE RT3	ENTRY POINT 000033	
USED: COD	E(1)_000042; DATA(0)_000012; BLANK_COMMON(2)_000000	
L REFERENC	ES (BLOCK, NAME)	
COS		
SIN		
NERR3\$		
ASSIGNMEN	I (BLOCK) ITPE, RELATIVE LOCATION, NAME,	
000001 IN	JP\$	
ana antara any sina di dependenti i di ana dia da mana ana an		
1*	SUBROUTINE RT3(ROT3,R)	
2*	$\frac{\text{DIMENSION ROIS(3:3)}}{\text{DOT3(1:1)} = \text{COC}(0)}$	
3*	RO(3(1)1) = COS(R)	
<u> </u>	R(1,3,1,2) = -311(1)	
5* 4*	PO(3(2,1) = 0)	
7*	POT3(2,2) = COS(R)	
9. <b>*</b>	R013(2,3) = 0.	
9*	Rot3(3,1) = 0.	
10*	ROT3(3,2) = 0.	
11*	R0T3(3,3) = 1.	
12*	RETURN	
13*	END	
OF COMPIL	LATION: NO DIAGNOSTICS.	
nyang kandulan salah katalah kang pang sama pang sama salah kang kang kang kang sa		
	1	
1		

FINE MATVEC	ENTRY POINT 000062	``		
LUSED: CODI	E(1) 000077; DATA(0) 000025; BLANK COMMON(2) 00000	]		
L REFERENC	ES (BLOCK / NAME)			
NERR3\$				
ASSIGNMEN	T (BLOCK, TYPE, RELATIVE LOCATION, NAME)			
5 ASSIGNMEN	T (BLOCK, TYPE, RELATIVE LOCATION, NAME) 56 0001 000031 1116 0000 I 000000 I	0000	000003	INJP
5_ASSIGNMEN 000025_10	T (BLOCK, TYPE, RELATIVE LOCATION, NAME) 56 0001 000031 1116 0000 I 000000 I	0000	000003	INJP
- ASSIGNMEN 000025 10	T (BLOCK, TYPE, RELATIVE LOCATION, NAME) 56 0001 000031 1116 0000 I 000000 I SUBROUTINE MATVEC(A,B,C,N)	0000	000003	INJP
- ASSIGNMEN 000025 10 1* 2*	T (BLOCK, TYPE, RELATIVE LOCATION, NAME) 56 0001 000031 1116 0000 I 000000 I SUBROUTINE MATVEC(A,B,C,N) DIMENSION A(N,N),B(N),C(N)	0000	000003	INJP
- ASSIGNMEN 000025_10 1* 2* 3*	T (BLOCK, TYPE, RELATIVE LOCATION, NAME) 56 0001 000031 1116 0000 I 000000 I SUBROUTINE MATVEC(A,B,C,N) DIMENSION A(N,N),B(N),C(N) DO 1 I = 1,N	<b>0</b> 000	000003	INJP
- ASSIGNMEN 000025 10 1* 2* 3* 4*	T (BLOCK, TYPE, RELATIVE LOCATION, NAME) 56 0001 000031 1116 0000 I 000000 I SUBROUTINE MATVEC(A,B,C,N) DIMENSION A(N,N),B(N),C(N) D0 1 I = 1,N C(I) = 0,		000003	INJP
- ASSIGNMEN 000025 10 1* 2* 3* 4* 5*	T (BLOCK, TYPE, RELATIVE LOCATION, NAME) 56 0001 000031 1116 0000 I 000000 I SUBROUTINE MATVEC(A, B, C, N) DIMENSION A(N, N), B(N), C(N) D0 1 I = 1, N C(I) = 0, D0 1 J = 1, N	0000	000003	INJP1
E_ASSIGNMEN 	T (BLOCK, TYPE, RELATIVE LOCATION, NAME) 56 0001 000031 1116 0000 I 000000 I SUBROUTINE MATVEC(A,B,C,N) DIMENSIGN A(N,N),B(N),C(N) D0 1 I = 1,N C(I) = 0, D0 1 J = 1,N 1 C(I) = C(I) + A(I,J)*B(J)	0000	000003	INJP

) OF COMPILATION: NO DIAGNOSTICS.

1.			6- D 0	E STM		
2.	an an ann an ann ann ann ann ann ann an	WALL TO THE REPORT OF A MARKET MALE AND A	*****	****	*****	elegation in the state of
3.	VEN				1000150	
4.	0.	alan baharan dan series di seria di se	- <b></b>	**************************************		
5.	3000.0	0.0	0.0	45.875		
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12.	1000.					a
13.	0.0					
14.	3000.0	0.0	0.0	45.875		
.15.	1000.					
16.	0.0	0.0	0.0			
17.	0.0	0.0				
18.	2				· · · · · · · · · · · · · · · · · · ·	
19.				Philippediate attended to a state to content on these sta-	-	··· ··· ··· ··· ··· ···
20.	0.0	0.0	3585+2	l.		W, F
.21.	0.0		1000.			1
22.	. 0.					
23	3000.0	0.0	0.0	45.875		
24•	ە0	0.0	0.0			
.25.	1000.	0.0	0.		and we have a state of the set of	
26.	0.0	0.0				
27.	2					- Vala
28.	1					I M F
29.	1207.5	Biological de les este en este en el desenant, es es este en el		erikan likele oon ontoonaan aaken ardaan adaan di aa ar oon oon aanaa ar	1758500.	T.
30.	1000.				1000.	¥ <sub>w</sub>

CASE	1		6- D *****	0 F *****	S I M ******	U L A ****	T 0 ★≭≭≭≭	P
V	EHICLE	•••• Ati	16	HELICO	PTER			
artis fana ann addith far gen praeme. Mad	ACTING WEIGHT				30	00.0	LBS	
	COORDINATES,	INCH	n a 🔹 a 🖉 an se an annaigh agus a m	-X		¥		Z
~	C C OF WEIGH	17		. 000		. 000		45.875
	WEAPON MOUNT	NG POINT	nij maritikiskiska prisi Andrewski Sandari (1998)	.000		.000		.000
	TARGET		10	00.000				_50.000
MOU	NTING ANGLE OF	VEHICLE W	ITH P	LATEOR	HAP DEG.	····•	•••	•00
	GIMBAL ROTATI	ON, DEG.						
	PITCH Yaw	•00 ( •00	INCL.	MOUNT	ING ANG	i <u>LE)</u>		
DAMP	ING_MED1A		EN					
EFFE	CTIVE VOLUME OF	- ACCUMULA	TOR		326.0	1N3		
MAXI	MUM ACTUATOR S	TIFFNESS			5000.0	LB/I	11	
MINI	MUM ACTUATOR S	FIFFNESS			300.0	LB/I	N	A. Management of the state of t
	EXTERN	AL LOADS		مەرەپىيە يەتەت يەرەپىيە تەرەپىيەر بەرەپىيەر يەرەپىيەر يەرەپىيەر يەرەپىيەر يەرەپىيەر يەرەپىيەر يەرەپىيەر يەرەپى				
and provide stress of the statement			X		Y		Z	
FOR	CE, LB.	100	0.0		• 0		• 0	
MOM	EMT. IN.LE.		•0	na naya, w a pamalana na katalaka ang katala ang	• 0	1922 - 1974 I VIII I	• 0	-
-	REQUIRE	D STIFFNES	S_AT_	MOUNT	ING PLAT	FORM		
ana an ann a sciùi dan dan			Х		Y		Ζ.	9000 18 900 - 10 - 10 - 10 - 10 - 10 - 10 - 10
TRA	NSLATION, LB/I	N 120	7.5		• 0		• 0	
ROT	TATION, IN. LB/RA	D ·	• 0		• 0		• 0	

CASE 1

### 

### VEHICLE ..... AH 16 HELICOPTER

		ACTUATOR FORCE	ES AND DISPLACEMENTS	SIDUE TO
	ACTUATUR	WEIGHTILB	RECOIL LOAD.LE.	DIPL. (RECOIL LD.), IN
/	1	646•8 646•8	-485.2	50819 .30959
	- 3 4 5 6	646+8 646+8 646+3 646+8	434.1 -485.2 51.1 51.1	•36959 -•50219 •13860 •13860
		ACTUATOR STIP	FENESS AND PRESSURES	
	ACTUATOR	STIFFNESS LEVIN	TOP PRESSURE PSI	BOT. PRESSURE PSI

		a na manana m		
1	954.7	330.5	361.3	alex a specific and a strong larger and the strong st
2	1174.5	410.5	441.0	
ĩ	1174.5	410.5	441.0	
4	954.7	33u•3	361.3	
5	368•5	118.3	148.2	
		118.3	14R.8	

# ACCUMULATOR PRECHARGE

re ben konstanten alteren samata antara antar antar antar an 🗞 a bataria fater val menur materi — abata ur antar	ACCUNULATOR	PLECHARGE (PSI	)	
	1 (TUP)	256.2		
	2 (TÚP)	317.9		
	3 (TOP)	317.9		
	4 (TJP)	256.2		
	5 (TOP)	91.6		
	6 (TOP)	91.6		

### RESULTANT STIFFMESS AT CENTER OF PLATFORM

ن .	0	0	0	<b>-</b> .0	1207.5
-17930+4	• Û	13058.6	0	803.1	0
U	26613.2	0	2934.8	<b>-</b> •0	0
-116455.2	• 9	1843334.9	<b>-</b> .J	13058.6	-•0
•1	1084776.9	• 0	26615.2	• Û	0
1915275.2	• 1	-116455.2	0	-17930-4	• 0

ASE 2	6- D *****	6- D O F S I M U L A T O R ******************************				
VEHICLE	AH 1G	HELICO	PTER			
ACTING WEIGHT			30	00.0	LBS	
COORDINATES INCH	ageny agences, a summaria association is also and for the first to the	X	1	Y		Z
- C.G. OF WEIGHT		.000		- 000		45.875
WEAPON MOUNTING PO TARGET	INT C10	00.000 .000	$\bigcirc$	000		•000
MOUNTING ANGLE OF VEHIC	LE WITH P	LATEOR	M. DEG.			•00
GIMBAL ROTATION D	EG.				,	
PITCH .0 Yaw .0	0 (INCL. 0	MOUNT	ING_ANG	LE)		
DAMPING MEDIA NI	TROGEN					
EFFECTIVE VOLUME OF ACCU	MULATOR	<b>=</b>	326.0	IN3.		
MAXIMUM ACTUATOR STIFFNE MINIMUM ACTUATOR STIFFNE	SS SS	☴	5000.0 300.0	L3/I L8/I	V N	
EXTERNAL LOA	DS					
	X		Y		Z	
FORCE, LB.	• 0		• 0	10	00.0	
FORCE, LB. MOMEMT, IN.LB.	• 0		• 0	10	0	
FORCE, LB. MOMEMT, IN.LB. REQUIRED STIF	.0 .0 FNESS_AT	MOUNTI	•0 •0 NG PLAT	10 FORM	•0	
FORCE, LB. MOMEMI, IN.LB. REQUIRED STIF	•0 •0 FNESS_AT X	MOUNTI	•0 •0 NG_PLAT Y	10 FORM	0 2_	
FORCE, LB. MOMEMI, IN.LB. REQUIRED STIF	.0 .0 FNESS_AT X0	MOUNTI	•0 •0 .NG_PLAT Y0	10 FORM 35	2 85.2	

		· · · · · · · · · · · ·	0- U U *******	F 5 I M U <u>********</u> *	L A T O R	and a second and the second and a second and the se
VE	ICLE	•••••••	16 HEL	ICOPTER		
						ar a sea an ann an an an an ann ann ann ann an
	na mananan a shipping yang dalak sa shipping yan dalak ka ka sana ya	ACTUATOR FORC	ES AND D	ISPLACEMENTS	DUE TO	
β	CTUATOR	WEIGHT,LB	RECOI	L LOAD, LB.	DIPL. (RECOI	L LD.),IN
	1	646 • 8		215.6	•21	561
	.3	646.8				561
	4	646.8		215.6	•21	561
	5	646.8		215.6		561
	6	646.8		215.6	•21	561 561
50		ACTUATOR STI	FFNESS AI	ND PRESSURES		
	CTUATOR		Ta			n water constituting grap (2 (2 + ) decomposition of a distance
·	CIURIUR-	LB/IN	L01	PSI	BOT PRESS	URE
a dalaman menye nagar, dalaman dalar yang menye nagaran	1	1000.0		347.3	377.8	
	2	1000.0		347.3	377.8	
	3	1000.0	3	347.3	377.8	
	4	1000.0		347.3	377.8	
	5	1000.0	3	347.3	377.8	
	6	1000.0	9 	347.3	377.8	
<ul> <li>(1) (1)(1)</li> <li>(2) (2)(1)(1)</li> <li>(3) (2)(1)(1)(1)(1)(1)(1)(1)(1)(1)(1)(1)(1)(1)</li></ul>		ACCUMUL	ATOR PREC	HARGE		
	ny na sa an	ACCUMULATOR	PRE	CHARGE (PSI	)	
W. S. THERE AND ADDRESS AND ADDRESS AD	<ol> <li>Militade de comme a type — a space</li> </ol>	1 (TUP)		268.9		
		2 (TOP)		268.9		
		3(TOP)		268.9		
		4 (TOP)		268.9	and the second	na an an an Anna an Anna an Anna an Anna an an Anna Ann
		5 (TOP)		268.9		
		6 (TOP)		268.9		-
	antigenetics i det mannenskelse dig Valder i den er an man anne a	RESULTANT S	TIFFNESS	AT CENTER O	F PLATFORM	****
. 1	207.5	0	0	0	-7842.5	and and a standard to an appropriate that which a standard a standard and a
·	0	1207.5	•0	7842.7	• 0	-,
	-•0	0	3585.2	0	•0	•
	0	7842.7	0	1758542.3	• 0	-1.
-7	842.5	• 0 -	•0	• 0	1758533.9	•
	-	and a second sec		and the second state of the second		· · · · · · · · · · · · · · · · · · ·

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VEHICLE	••• Ari 1G	HELICOPIE	<b>?</b>	
ACTING WEIGHT	and an and the South Southers of Southers of Southers of Southers and the	=	3000.0	LBS
	- ** •			-
COORDINATES, IN	CH	- X	1	
C.G. OF WEIGHT	and second states of the state	.000	.000	45.875
WEAPON MOUNTING	POINT	.000	.000	•000 •000
TARGET	-	1000.000		
			-	
	นากระบาน	PLATEORM.	DEG.	
	Le SEGe			
GINBAL ROTATION			a m	
		. MOUNTIN	ANGLE)	
and an an and a state of the st	and a state of the second state of the			
YAW	• 00			
YAW	• 00		((	
YAW	• 00			
YAW	• JO • _NETROGEN			
YAW	•00 •_NETROGEN-	2 =3	26.0 1113	
YAW AMPING_MEDIA FFECTIVE VOLUME OF AXIMUM ACTUATOR STI	•00 •_NLTROGEN_ ACCUMULATOF FFNESS	x =3 = 50	26.0 IN3 00.0 LB/	IN
YAW AMPING_MEDIA FFECTIVE VOLUME OF AXIMUM ACTUATOR STI INIMUM ACTUATOR STI	•00 •_NLTROGEN- ACCUMULATOF FFNESS FFNESS	2 =3 = 50 =3	26.0 IN3 00.0 LB/ 00.0 L3/	IN IN
YAW AMPING_MEDIA FFECTIVE VOLUME OF AXIMUM ACTUATOR STI INIMUM ACTUATOR STI	•00 • INLTROGEN ACCUMULATOR FENESS FENESS	2 =3 =50 =3	26.0 IN3 00.0 L8/ 00.0 L3/	IN IN
YAW AMPING_MEDIA FFECTIVE VOLUME OF AXIMUM ACTUATOR STI INIMUM ACTUATOR STI EXTERNAL	•00 •_NETROGEN ACCUMULATOR FENESS FENESS LOADS	<pre></pre>	26.0 1N3 00.0 LB/ 00.0 L3/	IN IN 
YAW AMPING_MEDIA FFECTIVE VOLUME OF AXIMUM ACTUATOR STI INIMUM ACTUATOR STI EXTERNAL	•00 • INLTROGEN ACCUMULATOR FFNESS FFNESS LOADS X	2 =3 =50 =3	26.0 IN3 00.0 LB/ 00.0 L3/	IN IN Z
YAW AMPING_MEDIA FFECTIVE VOLUME OF AXIMUM ACTUATOR STI INIMUM ACTUATOR STI EXTERNAL FORCE, LB.	.00 .INLTROGEN ACCUMULATOR FFNESS FFNESS LOADS X 1000.	x = -3 = 50 = 3	26.0 IN3 00.0 LB/ 00.0 L3/ Y	IN IN Z •0
YAW AMPING_MEDIA FFECTIVE VOLUME OF AXIMUM ACTUATOR STI INIMUM ACTUATOR STI EXTERNAL FORCE, LB. MOMEMT,_IN.LB.	• JO • INLTROGEN ACCUMULATOR FFNESS FFNESS LOADS X 1000.1	x = -3 = 50 = 3	26.0 IN3 00.0 L9/ 00.0 L3/ Y .0	IN IN Z • 0 • 0
YAW AMPING_MEDIA FFECTIVE VOLUME OF AXIMUM ACTUATOR STI INIMUM ACTUATOR STI EXTERNAL FORCE: LB. MOMEMT. IN.LB. REQUIRED	• JO • INLEROGEN ACCUMULATOR FFNESS FFNESS LOADS X 1000. STIFFNESS	2 = _3 = 50 = 3 01000 AT MOUNTING	26.0 IN3 00.0 LB/ 00.0 L3/ Y .0 .0 .0	IN IN Z .0 .0
YAW AMPING_MEDIA FFECTIVE VOLUME OF AXIMUM ACTUATOR STI INIMUM ACTUATOR STI EXTERNAL FORCE, LB. MOMEMT,_IN.LB. REQUIRED	• JO • INLTROGEN ACCUMULATOR FFNESS FFNESS LOADS X 1000.1 STIFFNESS X	2 = 3 = 50 = 3 0 1000 AT MOUNTING	26.0 IN3 00.0 LB/ 00.0 L3/ Y .0 .0 .0 .0 .0 .0 .0 .0 .0 .0 .0 .0 .0	IN IN Z .0 .0
YAW AMPING_MEDIA FFECTIVE VOLUME OF AXIMUM ACTUATOR STI INIMUM ACTUATOR STI EXTERNAL FORCE: LB. MOMEMT,_IN.LB. REQUIRED	• JO • INLEROGEN ACCUMULATOR FFNESS FFNESS LOADS X 1000 • STIFFNESS X	R = 3 = 50 = 3 0 1000 ΔΓ ΜΟυΝΤΙΝ3	26.0 IN3 00.0 L3/ 00.0 L3/ Y .0 .0 .0 .0 .0 .0 .0 .0 .0 .0 .0	IN IN Z .0 .0 .0 .0

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CASE	3	6- D O F S I M U L A T O R *******************					
v	EHICLE			AH 1G_HEL	ICOPTER	4	
	nanatara ng mang mangan kanatara anananan akan an	ACTU	JATOR FO	RCES AND E	ISPLACEMENT	S DUE TO	
	ACTUATOR	WE	IGHT,LB	RECOL	L LOAD, LB.	DIPL. (RECOI	L LD.),IN
	1 2		646•8		-481.6 444.0	50	248
	3		646 • d	in any contrast survey dia in some of the state of the st	444.3		759
			646.8		481 6	- 50	109
	5	•	646.8		37.6	.12	489
· · · · · · · · · · · · · · · · · · ·	6		646•8		376	•12	489
		ACT	UATOR S	TIFFNESS A	ND PRESSURE	S	
	ACTUATOR	ST	IFFN⊂SS B∕In	- TC	P PRESSURE PSI	BOT+PRESS PSI	URE
Malgare de La grapo recons alla Malanda de Very de la	1		958•5		332.2	362.7	
	2	1	176.0		411.0	441.5	
	3	1	176.0		411.0	441.5	
			958.5	where we determined and the second	332.2	362.7	
	5		301.0		93.9	124.4	
r Ten Anton Balaggin Alma, gigay w		and the second sec	301 • 0	ter starrenspannen, v. read dates	93,9	124.4	na filma line inter ar an an ann an
			ACCUM	LATOR PRE	CHARGE		· · · ·
		ACC	UMULATO	۲	ECHARGE (PS	i.)	
		- 1	(TOP)		257.2		
		2	(TOP)		318.3		
		- 3	(TOP)		318.3		-
		4	(TOP)		257.2		
	an and manipulation interaction of particular having a	5 6	(TOP)	nen 1	72.7		
		RE	SULTANT	STIFFNESS	AT CENTER O	F PLATFORM	· · · · · · · ·
	1207.1	9 MA &	0	-20.1		515.5	• (
	0	7	53.4	0	13248.6	• 0	-19596.6
	-20.1		0	2910.4	0	29222.1	-•(
	-•0	132	48.6	0	1847402.1	• 0	-108162.0
	515.5		• 0	29222.1	• 0	1007732.1	• 1
	• 0	-195	96.6	-•0	-108162.7	•1	1567540.6
-	1.1						

## INPUT DATA

3.	VEHICLE AH 1G HELICOPTER					
4.	20.					
5.	9500.0	0 • Ú	0.0	93.33		
6.	0.0	0.0	0.0			
7.	1000.	0.0	0.			
8.	0.0	0.0				
9.	1					
10.	1					
11.	10000.		30000.		15000000.	
	T0000		<u><u><u></u><u></u><u><u></u><u></u><u></u><u><u></u><u></u><u></u><u><u></u><u></u><u></u><u></u><u></u><u></u><u></u><u></u><u></u></u></u></u></u></u>		statistic disease where the second	
12.	-8457.		-3078.		-401327.	
12. 13. 4E: 0.0	-8457. 100. 922 SECONDS.		-3078.		-401327.	
12. 13. E: 0.0	-8457. 100. 922_SECONDS.	•	-3078.		-401327.	
12. 13. 4E: 0.0	-8457. 100. 922_SECONDS.	•	-3078.		-401327.	

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VEHICLE	AH 1G	HELICOPTER		
ACTING WEIGHT			9500.0 L	LBS
COORDINATES, INCH		X	Y	ΖΖ
C.G. OF WEIGHT		• 0 0 0	.000	93.3
WEAPON MOUNTING PO	DINT	.000	•000	• 0
TARGEL	1	000.000		• 0
MOUNTING ANGLE OF VEHIC	LE VITH I	PLATFORM, D	<u> </u>	
GIMBAL ROTATION,	JEG.			
PITCH 20.1	JO (INCL	• MOUNTING	ANGLE)	
IAW •	00		_	
DAMPING MEDIA	IL UMULATOR ESS ESS	= <u>117</u> = 23000 = 800	.5 IN3 .0 LB/IN .0 LB/IN	
DAMPING MEDIA	IL UMULATOR ESS ESS ADS	= <u>117</u> = 23000 = 800	.5 IN3 •0 LB/IN •0 LB/IN	
DAMPING MEDIAO EFFECTIVE VOLUME OF ACCO MAXIMUM ACTUATOR STIFFN MINIMUM ACTUATOR STIFFN EXTERNAL LO	IL UMULATOR ESS ESS ADS X	= 117 = 23000 = 800	.5 IN3 .0 LB/IN .0 LB/IN	2
DAMPING MEDIA	IL UMULATOR ESS ESS ADS X -8457.0	= <u>117</u> = 23000 = 800 Y	.5 IN3 •0 LB/IN •0 LB/IN	Z '8•0
DAMPING MEDIA	IL UMULATOR ESS ESS ADS X -8457.0 .0	= 117 = 23000 = 800 Y -401327.0	.5 IN3 .0 LB/IN .0 LB/IN -307	Z 2.0 •0
DAMPING MEDIAO EFFECTIVE VOLUME OF ACCO MAXIMUM ACTUATOR STIFFN MINIMUM ACTUATOR STIFFN EXTERNAL LO FORCE, LB. MOMEMT, IN.LB. REQUIRED STI	IL UMULATOR ESS ADS X -8457.0 0 FENESS AT	= 117 = 23000 = 800 Y Y -401327.0 HOUNTING F	.5 IN3 .0 LB/IN .0 LB/IN -307	Z 2.8.0 .0
DAMPING MEDIA	IL UMULATOR ESS ESS ADS X -8457.0 .0 FFNESS AT X	= 117 = 23000 = 800 Y Y -401327.0 MOUNTING F	.5 IN3 .0 LB/IN .0 LB/IN -307	Z 8.0 .0 Z
DAMPING MEDIA	IL UMULATOR ESS ESS ADS X -8457.0 0 FFNESS AT X 10000.0 0	= 117 = 23000 = 800 Y Y -401327.0 MOUNTING P Y .0 15000000.0	.5 IN3 .0 LB/IN .0 LB/IN -307 PLATFORM 3000	Z 8.0 .0 Z .0.0 .0
DAMPING MEDIA	IL UMULATOR ESS ESS ADS X -8457.0 .0 FFNESS AT X 10000.0 .0 TCH_GIMBA	= 117 = 23000 = 800 Y Y -401327.0 MOUNTING F Y 15000000.0	.5 IN3 .0 LB/IN .0 LB/IN -307 	Z 8.0 .0 Z 0.0 .0 SYSTEM
DAMPING MEDIA	IL UMULATOR ESS ESS ADS X -8457.0 0 FFNESS AT X 10000.0 0 TCH_GIMBA X	= 117 = 23000 = 800 Y Y -401327.0 MOUNTING F Y 15000000.0 L IN ITS CO Y	.5 IN3 .0 LB/IN .0 LB/IN -307 	Z 8.0 .0 Z 0.0 .0 SYSTEM Z
DAMPING MEDIA	IL UMULATOR ESS ESS ADS X -8457.0 .0 FENESS AT X 10000.0 .0 TCH_GIMBA X -11706.2	= 117 = 23000 = 300 Y Y -401327.0 MOUNTING F Y 15000000.0 L IN ITS CO Y	.5 IN3 .0 LB/IN .0 LB/IN -307 -3	Z 8.0 .0 Z 0.0 .0 SYSTEM Z

# VEHICLE ..... AH 1G HELICOPTER

CASE 1

# ACTUATOR FORCES AND DISPLACEMENTS DUE TO

ACTUATOR	WEIGHT, LB	RECOIL LOAD.LB.	DIPL.(RECOIL LD.), IN
1	2954.4	2016.1	.17099
2	-1016.8	-8320.2	
3	-1016+8	-8320.2	83285
4	2954.4	2016.1	•17099
5	3836•9	4313.1	• 42394
6	3636.9	4313.1	.42394
	ACTUATOR 1 2 3 4 5 6	ACTUATOR WEIGHT,LB 1 2954.4 2 -1016.8 3 -1016.8 4 2954.4 5 3836.9 6 3836.9	ACTUATOR         WEIGHT,LB         RECOIL LOAD,LB.           1         2954.4         2016.1           2         -1016.8         -8320.2           3         -1016.6         -8320.2           4         2954.4         2016.1           5         3836.9         4313.1           6         3836.9         4313.1

# ACTUATOR STIFFNESS AND PRESSURES

 ACTUATOR	SJIFFNESS LB/IN	TOP_PRESSURE PSI	BOT PRESSURE PSI	-
 1	11790.7	1470.9	1610.2	
2	9990.0	1329.2	1281.3	
 3	9990.0	1329.2	1281.3	
4	11790.7	1470.9	1610.2	
 5	10173.9	1238.8	1419.8	
6	10173.9	1238.8	1419.8	

ACCUMULATOR	PRECHARGE

		7.00	DOTTOM	
			<u>BUITOM</u>	
	1	735.4	805.1	
angegen mennen. V men undragt higherig en genera a namen datae en mennen i	2	664+6	640.6	
	3	064.6	640.6	and they appear to a first an administration for the second
anny per anderer and a second se	4	735.4	805.1	
	5	619.4	709.9	
	6	619•4	709.9	

RESULTA	NI FLEXIBILI	IY AT THE RE	QUIRED LOCA	ION
•000000	.315871-05	.228706-13	•435845-06	439648-1
•828593 <b>-</b> 04	170530-11	282288-06	.426326-13	.412051-0
170530-11	.263319-04	.399680-13	128639-07	•159872 <del>-</del> 1
282288-06	.435207-13	.529893-07	333067-15	340362-0
.355271-13	128639-07	277556-15	•575809-07	.111022-1
.412051-07	.159872-13	340362-08	•000000	•410364-0
RESULTA	NT STIFFNESS	AT THE REQU	JIRED LOCATIO	DN
0	-1660.8	0	-102018.7	
12293.7	• 0	65045.4	0	-6949.
• 0	38186.4	0	21101.7	
65045.4	0	19316977.2	1	1536864.
0	21101.7	.1	18143777.5	<u> </u>
-6949.3	0	1536864.1	1	24503048.
	gen de 2 generation announces, a semanante annot fantera announce a constituir de <b>1999 de 1999 de 1999</b>	ana an		
1999 - Antonio Antonio A	ananaganah - alah a sanak - 490 cd (r - 49 kalp ugla-alahapat a tan ay ang ang ang a			1998 198 54 54 51 51 51 5 5 5 5 5 5 5 5 5 5 5 5
ann a na me ne ann an ann aitean bhairean airean	anaganggata kasaman an a ny amin' ana			
wan an a	ndy and many a second of the state of the st			a alanahai ali i internitian lina at internet
anna an				
	RESULTA .000000 .828593-04 170530-11 282288-06 .355271-13 .412051-07 RESULTA 0 12293.7 .0 65045.4 0 -6949.3	RESULTANT FLEXIBILI         .000000       .315871-05         .628593-04      170530-11        170530-11       .263319-04        282288-06       .435207-13         .355271-13      128639-07         .412051-07       .159872-13         RESULTANT       STIFFNESS        0       -1660.8         12293.7       .0         .0       38186.4         65045.4      0        0       21101.7         -6949.3      0	RESULTANT FLEXIBILITY AT THE RE         .000000       .315871-05       .228706-13         .828593-04      170530-11      282288-06        170530-11       .263319-04       .399680-13        282288-06       .435207-13       .529893-07         .355271-13      128639-07      277556-15         .412051-07       .159872-13      340362-08         RESULTANT STIFFNESS AT THE REQU      0       -1660.8        0       -1660.8      0         12293.7       .0       65045.4         .0       38186.4      0         65045.4      0       19316977.2        0       21101.7       .1         -6949.3      0       1536864.1	RESULTANT FLEXIBILITY AT THE REQUIRED LOCAT         .000000       .315871-05       .228706-13       .435845-06         .828593-04      170530-11      282288-06       .426326-13        170530-11       .263319-04       .399680-13      128639-07        282288-06       .435207-13       .529893-07      333067-15         .355271-13      128639-07      277556-15       .575809-07         .412051-07       .159872-13      340362-08       .000000         RESULTANT STIFFNESS AT THE REQUIRED LOCATIG      0       -102018.7         .0       .12293.7       .0       65045.4      0         .0       .38186.4      0       21101.7         .0       .21101.7       .1       18143777.5        6949.3      0       1536864.1      1

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APPENDIX D USE OF PIPDYNE COMPUTER PROGRAM TO VERIFY THAT  $A^T = B^{-1}$  AND  $B^T = A^{-1}$ 

Summary

The relationship between the system stiffness and the actuator stiffnesses of the mathematical model is

$$K = A^{-1} k B \tag{D-1}$$

or

$$K = B^T k B \tag{D-2}$$

where

$$B^{T} = A^{-1}$$
 (D-3)

The following analysis is given to verify that  $A^{T} = B^{-1}$  and  $B^{T} = A^{-1}$ .

Test Model

The triogonal actuator system, which is composed of six actuators elements 1 through 6 is shown in figure D-1. A joint is located at each end of the actuators; the top joints 8 through 13 are the boundary joints. Joints 1 through 7 are located on the mounting platform, of which joint 1 is used to introduce the loads to the system. Elements 6 through 18 represent the mounting platform which interconnects joints 1 through 7 to form a rigid structure.

Use of Computer Program

A computer program to solve a three-dimensional frame structure may be used. Here, FIRL computer program called PIPDYN is used.

Input Data Required

1. Joint Coordinates

The coordinates of joints 1 through 13 are given in the X, Y, Z system shown on figure D-1.

2. Material Properties

The material used is steel, for which

Youngs Modulus =  $30 \times 10^6$  psi, and

Poisson's Ratio = 0.3

#### 3. Member Properties

The members representing the mounting platform (7 through 18) are assumed to be of solid circular cross section of 10 in diameter.

Members 1 through 6 representing the actuators are assumed to have the same stiffnesses (k) of 10,000 lb/in. each and are represented by a solid circular cross section.

The following approach is used to obtain the diameter of members representing the actuators.

$$k = \frac{AE}{L}$$
(D-4)  

$$\therefore A = \frac{kL}{E}$$

$$d = \sqrt{\frac{4A}{\pi}} = \sqrt{\frac{4kL}{\pi E}}$$
(D-5)

where

K = actuator stiffness = 10,000 lb/in. L = actuator length = 46.57 in. E = Youngs modulus = 30 x  $10^6$  psi

### Therefore

The diameter (d) of the member = 0.1406 in.

4. Releases

The following constraints are imposed on the test model in order to represent the actual triogonal system.

The joint located at the top end of each actuator (boundary joints) is released in rotation about the three system axes. The joint located at the bottom of each actuator is released in rotation about two of the system axes, the third rotation is constrained to avoid singularity.

5. Loading

Two loading conditions are imposed on the system and are applied at joint (1).

Loading (1) - Forces

A unit force = 10,000 lb is applied in each direction of the system axes X, Y and Z. Similarly a unit moment = 10,000 in./lb is applied about each direction of the system axes X, Y and Z.

A total of 6 loads are applied at joint 1.

Loading (2) - Displacements

A unit displacement = 1.0 in. is applied in each direction of the system axes X, Y and Z. Similarly, a unit rotation = 1.0 radian is applied about each direction of the system axes X, Y and Z.

A total of 6 loads are applied at joint 1. Note that joint 1 is completely constrained from translation and rotation except in that direction in which a translation or a rotation loading is applied.

Computer Results

The computer results are given in attachment (2).

The two loading cases are designated by:

Loading 1 - Force transformation, and

Loading 2 - Displacement transformation

Extraction of Results for Computer Output

Three sets of results are extracted from the computer output to verify the three following relations.

Force Displacement for the Triogonal System

Equation (425) of the mathematical model given earlier in this report is

(D-6)

 $\mathbf{F} = \mathbf{K} \mathbf{D}$ 

The computer output listed in table D-1 determines matrix K which is given in table D-2. This matrix is obtained by getting the displacements and rotations of joint 1 in each of the system coordinate directions due to the applied loading 1.

Actuator System, Force Transformation Matrix

Equation (427) of the mathematical model given earlier in this report is

$$f_{\sim} = A F_{\sim}$$
 (D-7)

Matrix  $A^{T}$  is given in table D-3, which is obtained from the computer output, loading 1, which is the actuator force (along its local axis - F2, at end 2) with a sign reversed to represent the actuator force component in the direction of the applied load.

Actuator System, Displacement Transformation Matrix

Equation (428) of the mathematical model given earlier in this report is

 $\mathbf{d} = \mathbf{B} \mathbf{D} \tag{D-8}$ 

Matrix  $B^T$  is given in table D-4 which is obtained from the computer output, loading 2, which is the actuator displacement (along its local axis - X2, at end 2) with a sign reversed to represent the actuator component in the direction of the applied displacement.

#### Conclusions

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The following results can be concluded, simply by inspection of matrices A and  $B^{-1}$  (tables D-3 and D-6) and matrices B and  $A^{-1}$  (tables D-4 and D-5), that

$$A^{T} = B^{-1}$$
 (D-9)

and

$$B^{\mathrm{T}} = A^{-1} \tag{D-10}$$

Also by comparing matrix  $(A^{-1} \times B)$  table D-7 and the stiffness matrix (K) (table D-2), we can justify equation D-1 given in the summary of this appendix, which is applied for the stiffness of equal actuators.



# Figure D-1. Test model, triogonal actuator system (plan)

# Table D-1. System flexibility matrix\*

.00000	.00380	.00000	.00000	.00000	.85320
00000	.00000	00380	.00000	.85320	.00000
.00000	.00000	.00000	.27976	.00000	.00000
.00000	.00000	•00059	.00000	00380	.00000
.00000	<b>.</b> 00059	.00000	.00000	.00000	•00380
•00044	•00000	•00000	.00000	00000	.00000

\*Ref. computer results, attachment 2 - loading 1

Table D-2. System stiffness matrix (K)

1.20682	.00000	00000	.00000	-7.80397	•00000
•00000	1.20682	.00000	7.80405	.00000	.00001
00000	•00000	3.57445	•00000	00010	.00000
.00000	7.80405	.000001751	<b>.9</b> 0138	.00000	•00005
-7.80398	•00000	00010	.000001751	<b>.8947</b> 0	.00000
.00000	.00001	.00000	.00005	•0000022 <b>9</b> 4	•29361

lable D-3. Actuator system, force transformation matrix (A	Actuator system, force transformation matrix (A	(A) <sup>T</sup> ;
--	---	--------------------

.05107	.05107	48517	.43410	.43410	48517
53074	•53074	•22114	30960	•30960	22114
.21561	.21561	•21561	.21561	•21561	•21561
.00369	00369	01351	00983	.00983	.01351
01348	01348	•00355	.00993	.00993	.00355
00851	.00851	00851	.00851	00851	.00851

\*Ref computer results attachment 2 - loading 1

Table D-4. Actuator system, displacement transformation matrix (B)<sup>T</sup>\*

.16682	.16682	61322	•44641	.44641	61322
•61178	.61178	.16142	•45036	45036	16142
•77074	.77074	•77074	•77074	.77074	.77074
2.31516	-2.31516	-21.95092	-19.63575	19.63575	21.95092
-24.01006	-24.01006	10.00000	14.01000	14.01000	10.00000
-19.52951	19.52951	-19.52949	19.52950	19.52950	19.52949

\*Ref. computer results attachment 2 - loading 2

Table D-5.  $A^{-1}$  matrix

.16722	.16722	61359	•44636	•44636	61359
61194	•611 <b>9</b> 4	.16098	45096	•45096	16098
•77300	.77300	.77300	.77300	.77300	.77300
2.31930	-2.31930	22.03258	-19.71328	19.71328	22.03258
-24.09446	-24.09446	10.03938	14.05508	14.05508	10.03938
-19.58389	19.58389	-19.59343	19.57708	-19.57708	19.59343

Table D-6.  $B^{-1}$  matrix

.05119	.05119	48537	•43418	.43418	48537
53090	•530 <b>9</b> 0	.22112	30979	.30979	22112
•21624	•21624	•21624	.21624	•21624	.21624
.00369	00369	01356	00987	.00987	.01356
01353	01353	.00357	.00996	.00996	.00357
00853	.00853	00853	.00853	00853	.00853

Table D-7.  $A^{-1} \times B$  matrix (equivalent to  $B^T \times B$ )

00000	-7.79466	00000	00000	.00000	1.20684
.00002	00000	7.80899	.00000	1.20690	00000
.00000	00009	.00000	3.57469	.00000	00000
00049	.00000	.18031	.000011752	7.80515	00000
.00003	.62956	000001751	.00001	.00000	-7.80288
.88837	•000022294	•68668	00000	.00305	.00000

### APPENDIX E MAIN HYDRAULIC POWER UNIT

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4.

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Adiabatic condition:

$$V_{1} = \frac{V_{s}(P_{1}/P_{1})^{1/n}}{1 - (P_{s}/P_{s})^{1/n}}$$

Where:

- V<sub>1</sub> = Size of accumulator necessary, cu. in. This is the maximum volume occupied by the gas at precharge pressure.
- V. = Volume of fluid discharged from accumulator, cu. in. It is the additional volume of fluid demanded by the system.
- $P_1 = Gas precharge of accumulator, psi. This pressure must$

be less than or equal to minimum system pressure (P<sub>s</sub>).

- $P_{z} = Maximum system design operating pressure, psi.$
- V<sub>s</sub> = Compressed volume of gas at maximum system pressure, cu. in.
- $P_s =$  Minimum system pressure at which the additional volume of fluid is needed, psi.
- V. = The expanded volume of gas at minimum system pressure, cu. in.



$$Q_{v} = ReQ'O \quad \forall ALVE \quad FLOW \quad (""'_{SEC})$$

$$Q_{p} = Pump \quad FLOW \quad P_{ROVIDED} = \frac{2Q_{v}}{\pi} \quad (""'_{SEC})$$

$$\therefore \quad V_{\pi} = \frac{Q_{v} - Q_{p}}{FREQUENCY} = (Q_{v} - \frac{2Q}{\pi})/f = \frac{.3634}{f} \frac{Q_{v}}{f} \quad (IN^{3})$$

$$Let : \quad P_{i} = 1.500 \quad PSI \quad P_{2} = 3.000 \quad PSI \quad f \quad \frac{P_{3}}{F_{2}} = .9$$

$$\therefore \quad P_{3} = 2.700 \quad PSI \quad \frac{P_{3}}{P_{i}} = \frac{2700}{1500} = 1.8$$

$$n = 1.4 \quad (FOR \quad N_{2}) \quad \frac{1}{n} = .714$$

$$V_{1} = \frac{V_{x}(1.8)^{114}}{1-(.9)^{.714}} = \frac{1.5217 V_{x}}{.0725} = 21 V_{x} = \frac{7.6314 Q_{y}}{f} (10^{3})$$

 $C_{ONVERT} TO GALLONS:$   $V_{1} = 21V_{2} = \frac{(21)(.3634)Q_{V} \frac{60}{231}(GPM)}{f(G0)(CPM)} = \frac{.033Q_{V}}{f}(GAL)$
ACCUMULATOR - AT POWER UNIT :-

## SIZING - FOR LINE SHOCK DAMPENER ONLY:-

 $V = \left(\frac{W}{2\pi}v^{*}\right) \left(\frac{n-1}{P}\right)$  $\begin{bmatrix} \frac{12}{\left[\frac{P_2}{P_1}\right]^{\prime}} \begin{bmatrix} n-1\\ n \end{bmatrix} = 1 \end{bmatrix}$   $P_2 = Maximum shock pressure, psi.$  W = Total weight of fluid in the pipe line, lb

Where: V =Required accumulator capacity, cu. in.

g = Acceleration due to gravity,32.2 ft/sec<sup>\*</sup>.

n = 1.4 for nitrogen.

v = Flow velocity, ft/sec.

 $P_1 =$ System pressure at normal flow rate, psi.

P1 = 3000 PSI Pz= 1.5 (P1) = 0.500 PSI V = 20 FT/SEC. (240 GPM IN 3.85 IN PIPE) W = Y.A.L = 53 (#) × 3.85 (A) × 70 = 100 #  $V = \left[\frac{100}{20}(20)^{2}\right] \left[\frac{.4}{3000}\right] \left[\frac{.12}{(15)^{.285}}\right] = 8.(10^{3})$ FOR PUMP PULSATION DAMPENER:-PERMISSIBLE FLUCTUATION = + 5% OF 3000 PSI  $V_{i} = \frac{(6(DISPL)(1.05)^{.714}}{1 - (.95)^{.714}}, \quad DISPL = \frac{240 \times 231}{1200 \, RFm} = 46.2 \, (10)^{3}$ : V, = 27.72 (1.036) = 800 (1N3)

ACCUMULATOR SIZE = BOB = 3.5 GAL (MIN.) NEARELT STOCK SIZE : 5 GAL.

DEANNUNTIS & ASSOCIATES, INC. CONSULTING ENGINEERS

WESTERN SAVINGS BANK BUILDING + PHILADELPHIA, PA. 19107

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REGISTERED PROFESSIONAL ENGINEERS PENNYPACKER 5-7814

WILLIAM J. DEANNUNTIS, P. E.

#### FLUID COOLER REQUIREMENTS

THE FRANKLIN INSTITUTE 20th and Cherry Streets Philadelphia, Pa.

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		. 1
CONDITIONS*	CASE I	CASE II
Ambient Air Temp.	95.0°F.	105.0°F.
GPM of Oil	250	250
Entering Oil Temp.	130.00°F.	130.00°F.
Leaving Oil Temp.	116.35°F.	116.35°F.
MBH	687.0	687.0
Elevation	1000 Ft.	1000 Ft.

\*Conditions: Cool 250 GPM of MIL-O-5606 fluid from 130°F. to a minimum of 116.35°F. at 95°F. ambient air (Case I) and 105°F. (Case II). The fluid shall be pumped from a 600-gallon tank at atmospheric pressure.

## DEANNUNTIS & Associates, Inc.

CONSULTING ENGINEERS

WESTERN SAVINGS BANK BUILDING + PHILADELPHIA, PA. 19107

REGISTERED PROFESSIONAL ENGINEERS PENNYPACKER 5-7814 WILLIAM J. DEANNUNTIS, P. E.

#### FLUID COOLER SELECTION

#### THE FRANKLIN INSTITUTE 20th and Cherry Streets Philadelphia, Pa.

EQUIP. SELECTION	CASE I	CASE II
Trane Model No.	GC08-B2-14.5-5	GC08-B2-21-5
Velocity (FPS) Std: Coil Face Vel.(FPM)	. 70 500	73 550
Oil Press. Drop (PSI)	3	4
Velocity (FPS) BHP (Per Fan)	2.23 5 (Approx)	$\begin{array}{c} 2.23 \\ 12 (Approx) \end{array}$
R.P.M.	550	.670
Fans	(2) 60" Dia.	(2) 60" Dia.
Coil Face Area	116 Ft. <sup>2</sup>	$168 \text{ Ft.}^2$
Fin Series (Fins/Ft.)	S-16 (108)	S-16 (108)
Tubes	5/8" Dia. x 0.024"	5/8" Dia.x 0.024"
Heeden Turc	Copper	Copper
Arrangement	HR No. 4	HR No. 4
Mean T.D. (°F.)	21.7	14.5
Fan Motors	4 Row - 2 Pass (2) 7% H P ·	4 Row - 2 Pass (2) 15 н р
Coils	(4) 24" x 174"	(4) 24" x 252"

Includes: Base unit, Drive Arrangement No. 4, 4 Coils 24" x Length, 4 Row, 2 Pass HR Coils, Adjustable Pitch Fans, Fan Guards and Orifices, Motors TEFC Type, Single Speed 1800 RPM, Belts & Sheaves.

NOTE: OPTIONAL EQUIP.: MOTORIZED DAMPERS, CAPACITY CONTROLS, CATWALK, LADDER, FAN GUARDS.





Drawing B-2638. Arrangement - unit control center



Drawing A-2639







Drawing A-2640



Drawing A-2640. Auxiliary pump starter - unit 3B (unit 3D)



Drawing A-2641. Relay panel - unit 3M



Drawing A-2641. Relay panel - unit 3M



Drawing A-2642. Motor starter - unit 4B (unit 4D)





Drawing A-2626. Electrical schematic controls - modified helicopter fuselage mount simulator







Drawing A-2626



Drawing A-2626





X22 V ХII OFF REMOTE LOCAL LOCAL. LOCAL START STOP 15 A 311 35 037 36 132 Ð. FUSE 2M2, REMOTE 42 REMOTE START PRESS, STOP 2011 SWITCH 39 0 0 0 (AUX. PUNP 2M1, 36 2012 OUTLET) 2063 "EMERG." TIMED 2TD 40 INTERLOCK CLOSING. 2014 35 2M22  $2MI_{z}$ STOP (LOCAL) 31 43 STOP (REMOTE) 2M13 RUN (LOCAL) 31 RUN (REMOTE) MAIN PUMP MOTOR No.2 250 IP - 1200 RPM REFERENCE DWG. No. A-2639 1 X II X2.



Drawing A-2626



Drawing A-2626



LOCAL OFF REMOTE XII ×22 ¥ LOCAL LOCAL START STOP 10 A 105 104 107 101 104 103 010 0 FUSE REMOTE REMOTE START STOP. 0 109 010 0 -0 6MI, 6011 6012 106 105 GMI 108 GMI2 STOP (LOCAL) 102 101 STOP (REMOTE) 6 Ml3 110 RUN (LOCAL) 101 RUN (REMOTE) AUX. PUMP MOTOR No.6 20 HP - 1800 RPM REFERENCE DWG. No. A-26.40 VX II X22

Drawing A-2626



Drawing A-2626



Drawing A-2626



Drawing A-2626

#### APPENDIX F MAIN PITCH SYSTEM

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TITLE ACTIVATION OF G-DOF SIMULATOR					
MAIN PITCH		DRIVE SYSTEM: AH-IG			
P.	ARAMETER		REFERENCE	DESIGN VALUE	υνιτ
M. OF	ASS MOMENT INERTIA	Ζ	AH-IG	43,430 *	[B-FT-56C <sup>2</sup>
Un	IBALANCE	Tm	37,520 × 2,284' × COS 45'	6.0,606 *	LB-FT
Fil	EING TORQUE	Tfr	9000 # x 11'	99,000	LB-FT
M,	AX. AMPLITUDE	X	EXISTING	+ 45 - 10	DEGREE
NON	AMPLITUDE	X	Spec.	10	DEGREE
101	FREQUENCY	f	SPEC.	.3	Hē
412	. VELOCITY	X	(217)°(f)(X)/360	.33	R'AD/ SEC
PE	Accel.	ż	2π(f)(x)	.62	RADÍSEL 2
00	ARM	R	EXISTING	6.5'	FT.
4"6	STROKE	2	EXISTING	72"	1N.
×	REQ'D TORQUE	T	1.5(1×+ Tm + Tfr)	279,800	LB-FT
ORE	HVD. FORCE	FH	T= 43,046.	108,000 * AVAILABLE	LB.
8 2	PISTON	As	$> \frac{F_H}{3,000} = 14.56$	37.7 AVAILABLE	1112
<u>()</u>	AREA	A.		50.265	/ N <sup>2</sup>
704	PISTON SPEED	V	12R(X)	25.74	IN/SEC
Lu7	VALVE FLOW	Q.	AL(V)(60) 231	336	GPM
Ac	PUMP FLOW	Qp	$> \frac{z}{\tau_{i}} Q_{v}$	214	GPM
	HYDRAULIC STIFFNESS	KH	2×10 <sup>5</sup> 2(As+AL) R <sup>2</sup>	247 × 106	LB-FT/ RAD.
ESTIMATED NATURAL FREQ. Jn 21 VIZI 11. Hz					
Form 207	104 671 <b>* 5EE DI</b> SH	WG A-2 EET 2.	351	Drawing No. A-26 Sheet 1 of 4	28

<sup>'</sup>351

Drawing No. A-2628 Sheet 1 of 4

ltem	Weight (1b)	C.G. Offset R(ft)	$\frac{WR^2}{g}$ (1b-ft-sec <sup>2</sup> )	l <sub>o</sub> (1b-ft- sec <sup>2</sup> )
Pitch & Yaw Gimbals Ass'y.	20,000	0	0.	9,500
(6) Suspension Actuators	2,520	2.5	490	87
Mounting Adaptor	2,500	4.0 *	1,242	324
AH-1G Helicoptor	9,500	7.78	17,857	13,401
YAW DRIVE MOTOR ASSY	3000	-1.5	211	318
			·	
Total .	-37,520	2.284	19,800	23,630
Mass Moment of Inertia	43,	430		

Estimated Mass Moment of Inertia About Main Pitch (Y) Axis.

 $C. G. = \frac{(2520)(2.5) + (2500)(4) + (9500)(7.78) - (3000)(1.5)}{37,520} = 2,284'$ 

MAX. UNBALANCE TORQUE (Tm) :-

$$T_{m} = (37520) (2.284) (\cos 45^{\circ}) = 60,606 (47-16)$$

$$F_{H}(AVAIL) = (A_{S} \times 3000 \text{ PSI}) - (A_{L} \times 100 \text{ PSI}) = (37.7 \times 3000) - (50.265 \times 100)$$

$$= 113,100 - 5026.5 = 108,000 \text{ Br.}$$

$$Drawing No. A-2628$$
Sheet 2 of 4

"orm 207 10M 6-71

MAIN PITCH		DRIVE SYSTEM: AAH			
Ŧ	PARAMETER		REFERENCE	DESIGN VALUE	UNIT
М. 07	ASS MOMENT E INERTIA	I	AAH HELICOPTER	<b>82,</b> 498 . <sup>A</sup>	LB-FT-S
Ur	NBALANCE	Tm	(44,020) (3,096) Cos 45°	96,365	LB-F
Fi	EING TORQUE	Tfr	9000 # x 11'	99,000 .	LB-FT
М.	AX. AMPLITUDE	×	EXISTING ACTUATOR	+ 45°	DEGRE
NOL	AMPLITUDE	X	SPEC.	10°	DEGRE
NO7	FREQUENCY	f	SPEC.	.3	Ha
¥ K	· VELOCITY	Ż	$(2\pi)^{2}(f)(x)/_{360}$	.33	RAD/SE
d'	. Accel.	ż	$2\pi(f)(\dot{x})$	.62	RAD/SEC
0	ARM	R	EXISTENA	6.5'	FT.
K0	STROKE	Ż	EXISTING	72"	IN.
x 4	REQ'D TORQUE	T	1.5(IX+ Tm + Tfr)	369,770	iB-FT
386	HYD. FORCE	FH	T = 56 888 R = 56 888	10 <b>B,000 *</b> Available	LB.
2	PISTON	As	> FH = 19.15 3000 REG.B.	37.7 AVAILABLE	INZ
	AREA	A.		50,265	INZ
1704	PISTON SPEED	V	12R(X)	25.74	IN/SE
7UX	VALVE FLOW	$Q_{*}$	<u>A1(V)(60)</u> 231	336	GPN
NC	PUMP FLOW	Q <sub>p</sub>	$> \frac{2}{\pi} Q_V$	214	GPN
	HYDRAULIC STIFFNESS	KH	2×10 <sup>5</sup> 2(As+AL) R <sup>2</sup>	247 × 106	LB-FT/
E 147	ESTIMATED WRAL FREQ.	fn	$\frac{1}{2\pi}\sqrt{\frac{k_{H}}{1.2}}$	7.95	Hz

-

ltem	Weight (1b)	Ċ.G. Offset R(ft)	$\frac{WR^2}{g} \frac{(1b-ft-sec^2)}{sec^2}$	l <sub>o</sub> (1b-ft- sec <sup>2</sup> )
Pitch & Yaw Gimbals Ass'y.	20,000	0	0	9,500
(6) Suspension Actuators	2,520	2.5	490	87
Mounting Adaptor	2,500	4.0	1,242	324
AAH Helicoptor	16,000	7.78 *	30,076	40,250
YAW DRIVE MOTOR ASSY	3,000	-1.5	211	318
-	<b>ب</b>		• •	
Total .	44,020	3,096	32019	50,479
Mass Moment of Inertia	82,	<i>498</i>		

Estimated Mass Moment of Inertia About Main Pitch (Y) Axis.

 $C. G. = \frac{(2520)(2.5) + (2500)(4) + (16000)(7.78) - (3000)(1.5)}{44020} = 3.006$ 

Tm = (44020)(3.096)(cos 45)= 96365 (FT-16)

\* ASSUMED SAME AS AH-IG HELICOPTOR, ACTUAL C.G. OFF.SET DEPEND UPON DETAILED DESIGN OF SUSPENSION ADAPTOR FOR THE PARTICULAR AIRCRAFT.

> Drawing No. A-2628 Sheet 4 of 4



Form 207 10M 6-71

Drawing No. A-2627

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# Moog 79 Series-400 GPM High Flow Servovalves

Moog 79 Series — 400 GPM Servovalves control position, velocity or force of massive machine elements, with fast response at high flows. They are 3-stage servovalves using standard 2-stage Moog industrial valves for pilot operation. Operating in conjunction with an electronic position feedback loop, the pilot valve controls position of the 3rd stage spool, which in turn meters the high output flow.

Because of the high position loop gain around the 3rd stage, hysteresis and threshold properties meet or exceed the specifications of the best 2-stage servovalves. Application areas include automatic gage control for steel mills, vibration testing or large equipment, position control on huge machinery, or wherever precise control is required in the range of 0 to 600 HP.

A single servoamplifier can be used to provide closed loop operation for the third stage spool position and the required amplification and electronicmixing functions for the outer or major loops. Moog Series 82 Servocontrollers are highly recommended for this purpose.



SCHEMATIC DIAGRAM 79 SERIES 3 STAGE SERVOVALVE WITH ELECTRICAL FEEDBACK

### The following options are available:

- Choice of Moog Series 73, 74 or 76 Servovalve for pilot operation with flow rates for optimum performance in the particular application.
- Choice of LVDT or DCDT spool position feedback transducer.
- Provision for mounting auxiliary spool position transducer for monitoring.
- Provision for operating the pilot valve from a separate hydraulic power source.

#### **General Characteristics**

Contraction of the local data and the local data an	
Flow Rating	400 gpm at 1000 psi valve drop
Operating Pressure	300 to 3000 psi
Inlet proof pressure	4500 psi
Return proof pressure	3000 psi
Fluid	Petroleum base hydraulic fluid Others on special order
Filtration	10 microns recommended
Internal leakage at null	less than 2% of rated flow
External leakage	none
Pressure gain at null	Greater than 30% supply pressure for 1% input
Weight	157 lbs.
Null Shift*	less than 1% for 80% to 110% supply pressure variation 0% to 20% back pressure variation 100°F temperature change
Hysteresis*	less than 1%
Threshold*	less than 0.5%

\*Values for third stage spool position loop gain of 250 sec



25

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50

# % RATED SPOOL STROKE

......

75

100

125





357

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APPENDIX G DETERMINATION OF SERVO OPEN-LOOP GAIN REQUIRED FOR RESISTING LOAD DISTURBANCES

\*

When we consider an angular position feedback control system with a simple block diagram as shown in figures G-1 and G-2, the output position error,  $\theta_d$ , caused by a disturbing torque,  $T_d$ , can be obtained from the closed-loop transfer function of figure G-2 as follows:

$$\frac{\Theta_{d}}{T_{d}} = \frac{G_{2}}{1 + G_{1}G_{2}}$$
(G-1)

where

•1 <sup>2</sup> 1

 $G_1$  = transfer function between output position and torque developed

 $G_2$  = transfer function between load torque and output position

For the case of an electrohydraulic actuator system,  $G_1$  and  $G_2$  can be derived from a typical position control system block diagram shown in figure G-3. When we combine the two feedback branches, with  $\theta_{in} = 0$ , the transfer function of  $G_1$  is

$$\mathbf{G}_{1} = \frac{\mathbf{r}}{\frac{A}{K_{H}}\mathbf{S} + \frac{C}{A}} \begin{bmatrix} \frac{\mathbf{K}_{1}\mathbf{K}_{2}}{\frac{\mathbf{s}}{\omega^{2}} + \frac{2\phi}{\omega}\mathbf{S} + 1} + \mathbf{r}\mathbf{A}\mathbf{S} \end{bmatrix}$$
(G-2)

$$G_2 = \frac{1}{JS^2 + DS}$$
(G-3)

where

- A = effective actuator piston area
- C = leakage coefficient of the actuator and servovalve spool
- D = actuator-load viscous damping coefficient

J = total load mass moment of inertia

 $K_{\rm H}$  = actuator hydraulic stiffness

 $K_1$  = amplifier scale factor in ma per radian

 $K_2$  = servovalve gain constant in cis per ma

r = effective radius of angular motion

S = Laplace transform operator

- $\phi$  = servovalve transfer function damping factor
- $\omega$  = servovalve transfer function natural frequency



Figure G-1. Angular position control feedback servo system



Figure G-2. Closed-loop transfer function



Figure G-3. Position control system

The closed-loop transfer function of position due to a disturbing torque,  ${\rm T}_{\rm d},$  is therefore

$$\frac{\theta_{d}}{T_{d}} = \frac{\left(\frac{A}{K_{H}}S + \frac{C}{A}\right)\left(\frac{S^{2}}{\omega^{2}} + \frac{2\phi}{\omega}S + 1\right)}{\left(JS^{2} + DS\right)\left(\frac{A}{K_{H}}S + \frac{C}{A}\right)\left(\frac{S^{2}}{\omega^{2}} + \frac{2\phi}{\omega}S + 1\right) + r^{2}AS\left(\frac{S^{2}}{\omega^{2}} + \frac{2\phi}{\omega}S + 1\right) + rK_{1}K_{2}}$$
(G-4)

When applying the final value theorem to determine the steady-state error in position,  $\begin{pmatrix} \theta_d \\ SS \end{pmatrix}$ , due to a step disturbing torque,  $T_d$ , the steady-state error is

$$\left( \Theta_{d} \right)_{SS} = \lim_{S \to 0} S \left( \frac{\Theta_{d}}{T_{d}} \right) \left( \frac{T_{d}}{S} \right) = \frac{T_{d} c}{rAK_{1}K_{2}}$$

$$(G-5)$$

To express the steady-state error in terms of the servo system open-loop gain constant,  $K_1K_2$  in the above expression can be substituted by  $K_0$  which is derived from figure G-3 as follows:

Since

 $K_{o}$  = open-loop gain constant

$$= \frac{K_1 K_2}{rA \left(1 + \frac{DC}{r^2 A^2}\right)}$$
(G-6)

thus

$$rAK_{1}K_{2} = r^{2}A^{2}\left(1 + \frac{DC}{r^{2}A^{2}}\right)K_{0}$$
 (G-7)

or

$$\left(\theta_{d}\right)_{SS} = \frac{T_{d}C}{r^{2}A^{2}\left(1 + \frac{DC}{r^{2}A^{2}}\right)K_{o}}$$
(G-8)

or

$$K_{o} = \frac{T_{d} C}{r^{2} A^{2} \left(1 + \frac{DC}{r^{2} A^{2}}\right) \left(\theta_{d}\right)_{SS}}$$
(G-9)

For a specified value of step disturbing torque,  $T_{\rm d}$ , and an acceptable position error,  $\theta_{\rm d}$ , the required servo system open-loop gain constant,  $K_{\rm o}$ , to resist the disturbing torque is

$$\kappa_{o} > \frac{T_{d} C}{r^{2} A^{2} (\theta_{d})_{SS}}$$
(G-10)

since

$$\frac{T_{d}C}{r^{2}A^{2}(\theta_{d})_{SS}} > \frac{T_{d}C}{r^{2}A^{2}\left(1 + \frac{DC}{r^{2}A^{2}}\right)(\theta_{d})_{SS}}$$
(G-11)

Calculation of the Main Pitch Control System Open-Loop Gain

For a maximum firing torque of 99,000 ft-lb as calculated in appendix F of this report, the required servo open-loop constant,  $K_v$ , to resist this disturbing torque for a position error of 1 degree or less is

$$K_{v} = \frac{(99,000)(12)C}{r^{2} A^{2} (1/57.3)}$$
(G-12)

where

- C = assumed to have a leakage coefficient equivalent to a damping factor of 0.8 for the actuator
  - = 0.508 cis/psi
- A = 37.7 sq in.
- r = 78 in
- $K_v = 4.1/sec$

The value of  $K_v$  used in the system design is 7 which is larger than the required loop gain calculated above.

Calculation of the Main Yaw Control System Open-Loop Gain

The required open-loop gain constant for the Main Yaw control system was calculated with the following parameter values:

 $T_{d} = 10,625 \text{ ft-1b (app I)}$  C = 0.0231 cis/psi (table 7)  $dm = 368 \text{ in.}^{3}/\text{rad}$   $(\theta_{d})_{ss} = \frac{1}{57.3} \text{ radian}$   $K_{v} = \frac{(10,625) (12) (.0231) (57.3)}{(368) (368)}$  = 1.25 1/sec

(G-13)

The value of  $\rm K_v$  used in the system design is 6.3 which is much greater than the required value of  $\rm K_v$  calculated above.

APPENDIX H CALCULATION OF THE REQUIRED OPEN-LOOP GAIN AND BYPASS LEAKAGE COEFFICIENT OF THE TRIOGONAL ACTUATOR SERVO SYSTEM The steady-state error in position due to a constant, frequency independent disturbing force in a position control servo system can be derived as

$$X_{d \text{ static}} = \frac{F_{d}}{DK_{v}}$$
(H-1)

where

 $X_d$  = position error due to disturbance  $F_d$  = disturbing force

D = damping coefficient of the actuator-load

The damping coefficient D in equation (H-1) can be derived from the characteristic equation of the hydraulic valve-actuator-load transfer function. The transfer function was developed in a previous analysis in a form of

$$\frac{X}{Q_2} = \frac{1}{As[(\frac{1}{K_{HA}} + \frac{1}{K_A}) MS^2 + (\frac{MC_2}{A^2} + \frac{D}{K_A})s + 1 + \frac{DC}{A^2}]}$$
(H-2)

where

- X = actuator displacement
- $Q_2$  = actuator input flow rate
- A = effective piston area

 $K_{HA}$  = actuator hydraulic stiffness

 $K_A$  = actuator attachment joints and structural stiffness

C = leakage coefficient of the hydraulic valve and actuator bypass

s = Laplace transform operator

If D is mainly due to the actuator bypass leakage flow, it would have a value approximately equal to  $D = \frac{A^2}{C}$ 

The last term in equation (H-2) will be equal to one such as

$$\frac{DC}{A^2} = \frac{A^2}{C} \times \frac{C}{A^2} = 1$$
(H-3)

The second order function in the denominator of (H-2) can then be solved for the damping ratio,  $\zeta$ , and the natural frequency,  $\omega_n$ . Since  $K_A >> K_{HA}$ , the terms in  $K_A$  may be ignored. Then

$$\omega_{n} = \sqrt{\frac{2K_{HA}}{M}}$$
(H-4)

and

$$\frac{2\zeta}{\omega}_{n} = \frac{1}{2} \left( \frac{M}{D} + \frac{D}{K_{HA}} \right)$$
(H-5)

Using (H-4), equation (H-5) can be solved for D.

$$D = \sqrt{2\kappa_{\text{HA}}^{M}} \left[\zeta \pm \sqrt{\zeta^{2} - \frac{1}{2}}\right]$$
(H-6)

The design values of  ${\rm K}_{\rm HA},$  M, A,  ${\rm F}_{\rm d}/{\rm X}_{\rm d}$  for each 6-DOF actuator are

$$K_{HA} = 0.945 \times 10^{6} \text{ lb/in.}$$
  
 $M = 33.5 \text{ lb-sec}^{2}/\text{in.}$   
 $A = 20.652 \text{ in.}^{2}$   
 $\frac{F_{d}}{X_{d}} = K_{ACT} = 2 \times 10^{5} \text{lb/sec}$ 

Therefore, the bypass leakage coefficient C can be determined from equations (H-3) and (H-6).

$$C = \frac{A^2}{\sqrt{2K_{HA}^M} \left[\zeta \pm \sqrt{\zeta^2 - \frac{1}{2}}\right]}$$
(H-7)

For  $\zeta = 0.707$  and the values given above

$$C = 2.04 \text{ X } 10^{-2} \text{cis/psi} = \frac{5.30 \text{ gpm}}{1000 \text{ psi}}$$
(H-8)

The required servo-open loop gain  ${\rm K}_{\rm V}$  in equation (H-1) is given by

$$K_{\rm V} = \frac{F_{\rm d}}{DX_{\rm d}} \tag{H-9}$$

From equation (H-6) and the design values

$$K_{\rm V} = 36$$
 (H-10)

Revision

Equation (H-1) was derived assuming no disturbing force applied to the actuator. For the 6-DOF simulator a disturbing force (gun-firing) will be present. The following derivation was developed to further clarify equation (H-1).

When we consider a position feedback control system with a simple block diagram as shown in figures H-1 and H-2, the output position, X, due to a disturbing impact load force, F, can be obtained from the closed-loop transfer function of figure H-2 as follows:

$$\frac{X}{F} = \frac{G_2}{1 + G_1 G_2} \tag{H-11}$$

where

Í.

 $G_1$  = transfer function between output position and force developed  $G_2$  = transfer function between load force and output position

For the case of an electrohydraulic actuator system,  $G_1$  and  $G_2$  can be derived from a typical position control system block diagram shown in figure H-3. When we combine the two feedback branches, with  $X_{in.} = 0$ , the transfer function of  $G_1$  is

$$G_{1}(s) = \frac{1}{\frac{A}{K_{HA}}s + \frac{C}{A}} = \frac{\frac{K_{1}K_{2}}{\frac{S^{2}}{\omega} + \frac{2\zeta}{\omega}s + 1} + As$$
 (H-12)

and

$$G_2(s) = \frac{1}{Ms^2 + Ds}$$
 (H-13)

where

A = effective actuator piston area

C = leakage coefficient of the actuator and servovalve

D = actuator--load viscous damping coefficient (e.g., piston, joints and load frictions, load damper, and windage friction, etc.)

M = total moving load mass



Figure H-1. Block diagram of the position feedback control system, view 1



Figure H-2. Block diagram of the position feedback control system, view 2



Figure H-3. Block diagram of an electrohydraulic actuator position servo

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 $K_{HA}$  = actuator hydraulic stiffness

 $K_1$  = amplifier scaling factor in ma per inch

 $K_2$  = servovalve gain constant in cis per ma

- s = Laplace transform operator
- $\zeta$  = servovalve transfer function damping factor
- $\omega$  = servovalve transfer function natural frequency

The closed-loop transfer function of position due to a disturbing force F is, therefore

$$\frac{X_{d}}{F} = \frac{(\frac{A}{K_{H}}s + \frac{C}{A})(\frac{S}{\omega} + \frac{2\zeta}{\omega}s + 1)}{(Ms^{2} + Ds)(\frac{A}{K_{H}}s + \frac{C}{A})(\frac{S^{2}}{\omega} + \frac{2\zeta}{\omega}s + 1) + As(\frac{S^{2}}{\omega} + \frac{2\zeta}{\omega}s + 1) + K_{1}K_{2}}$$
(H-14)

When applying the final value theorm to determine the steady-state error in position  $(X)_{ss}$  due to a step disturbing force F, the steady-state error is

$$(X)_{ss} = \lim_{s \to 0} s \left(\frac{X_d}{F}\right) \left(\frac{F}{s}\right) = \frac{FC}{AK_1 K_2}$$
(H-15)

To express the steady-state error in terms of the servo system open-loop gain constant,  $K_V$ , the parameters  $K_1$  and  $K_2$  in equatin (H-5) can be related to  $K_V$ , from figure 3, as follows:

$$K_{v} = \frac{K_{1}K_{2}}{A(1 + \frac{DC}{A^{2}})}$$
(H-16)

Substituting equation (H-16) into (H-15) gives

$$(x)_{ss} = \frac{FC}{A^2 K_V (1 + \frac{DC}{A^2})}$$
(H-17)

The required servo system open-loop gain constant to resist a specified maximum disturbing force F for an acceptable steady-state position error  $(X)_{ss}$  is

$$K_{V} = \frac{FC}{A^{2}(1 + \frac{DC}{A^{2}}(X)_{ss})}$$
(H-18)

For  $D = A^2/C$  equation (H-18) becomes

$$K_{V} = \frac{F}{2DX_{SS}}$$
(H-19)

This is a lower bound on equation (H-19) and, therefore, equation (H-9) merely provided a larger gain than required for the open-loop gain.

APPENDIX I MAIN YAW SYSTEM

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MAIN YAW		Drive Syst	ЕМ:-		
·PARAMETER	· -	REFERENCE	DESIGA	I VALUE	Un
MASS MOMENT OF INERTIA	I	AAH AIRCRAFT AH-1G AIRCRAFT	47.6	25 * 18 * *	1B-F
UNBALANCE	·Tm	<u>ААН -</u> Днід-	800	00 * 50 **	L
FIRING TORQUE	T <sub>fr</sub>	3000 # × 42.5	10,62	25. *	LB
MAX. AMPLITUDE	×	SPEC.	±7	5	De
ROL AMPLITUDE	X	SPEC.	± /	0	De
FREQUENCY	f	SPEC.	. 5	3	• 4
Y VELOCITY	×	(2π)*(f)(x)/360	:3	3	ZAC
d' Accel.	Ä	2n(f)(x)	. 6	62 ,	RA
REQ'D TORQUE	7	1.5 (IX+Tm+T++)	AAH 7. AHS 4.	1,636	LB
MAX. RPM	ω	× ( <sup>60</sup> /2π)	3.1.	5	R
NAX. TORQUE	Tmax	<u>3080</u> × 3000 × (e) EFF: 9 100	83,10	AVAILABLE	LB
ON MOTOR FLOW	8	CATALOG	2310	2.	R
VALVE FLOW	Q,	$\frac{8\omega}{231(e)} = 40_{REQ'D.}$	6	ORATED	GI
PUMP FLOW	Qp.	$\frac{2}{\pi}Qv$	25	5	GF
HYDRAULIC STIFFNESS	KH	DWG. A-2629 SEE SH. 2 OF 4	1,23.	2×106	63-4
ESTIMATED		1 Fri	AAH	.74	
LOGANICAL	fn	27 1.2 1			Н
r countre y		•	AH-1G	1.27	

TITLE MAIN YAW DRIVE

 $\frac{E57}{H} \frac{H}{PAULIC} \frac{571FFNESS}{S71FFNESS} \frac{OF}{DRIVE} \frac{MOTOR}{MOTOR}$   $\frac{HAGGLUNDS}{MODEL} \frac{MODEL}{MOTOR} \frac{MOTOR}{MOTOR} = \frac{100}{100} \frac{100}{100} = \frac{100}{100$ 

ESTIMATO	od Mass	MOMENT	OF	INERTIA
ABOUT	HEUCOPT	or YAN	(2)	Axis:-

ІТЕМ	Weiaнт (16.)	C.G. OFFSET R (FT.)	<u>W</u> 2 <sup>2</sup> <u>9</u> (16-FT-	Io SEC <sup>2</sup> )
YAW GIMBAL	7,500	0	0	1900
YAN DRIVE MOTOR	3,000	0	0	435
(6) SUSPENSION ACTUATORS	2,520	0	0	580
MOUNTING ADAPTORS	2500	. 0	0	185
HELICOPTOR AAH	16,000	.5	125	4400
TOTAL	31,520		125	47,500
-	· · ·		476	.25

UNBALANCE MOMENT (Tm) = 16000 # x. 5 = 8000 (F7-16).

FIRING TORQUE (Tfr)= 3000 # x 42.5 (FT-16) MAK.

Drawing No. A-2629 Sheet 3 of 4

form 20 10M 6-71

TITLE YAW DRIVE

ESTIMATED MASS MOMENT OF INERTIA ABOUT HEUCOPTOR YAW (2) AXIS:-

ІТЕМ	Weiaнт (16.)	C.G. OFFSET R (FT.)	<u>WR</u> <sup>2</sup> <u>9</u> (16-FT-	I.0 56C²J
YAW GIMBAL	7,500	0	0.	1900
YAW DRIVE MOTOR	3,000	. 0	0	435
(6) SUSPENSION ACTUATORS	2,520	0	0	580
MOUNTING ADAPTORS	2,500	0	0	185
HELICOPTOR AH-1G	9,500	1.19	<u>.</u> 118	12,260
TOTAL			418	15360
	e		157	18 <sub>.</sub>

UNBALANCE MOMENT (Tm) = 9500 \* × 1.19 = 11305 (FT-16)

FIRING TORQUE (Tfr)= 3000 # \* 42.5" =10,625 (27-16) MAX.

Drawing No. A-2629 Sheet 4 of 4

Form 207 10M 6-71

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#### OPERATING PRINCIPLES

The pistons (1) are contained in a stationary cylinder housing (2) and are connected to rollers (3) which bear on the cam ring (4). The rotary valve (5) distributes oil from the inlet (A) to each cylinder in sequence. The oil pressure displaces the pistons outward, forcing the rollers against the cam ring, causing it and the outer casing of the motor to rotate. Fixed side guides (6) absorb reaction forces on the rollers, thus unloading the pistons from any side (tangential) forces. Oil escapes from the motor through outlet (C). An even number of opposed pistons assures hydraulic balance and unloads the main bearing from any piston forces.



#### OUTSTANDING FEATURES

# FULL RATED STARTING TORQUE

- CONSTANT TORQUE 0 TO FULL RPM
- LOW SPEED CONTROL
   UNDER 1 RPM AT FULL TORQUE
- INSTANT REVERSING
- TWO SPEED RANGES
- INTEGRAL CONTROL VALVES
- INTEGRAL HYDRAULIC BRAKES
- FREE WHEELING

### MOTOR CHARACTERISTICS

			NORMAL SP	EED RANGE	-	IIIGHE	R SPEED R	ANGE
MOTOR TYPE	WEIGHT	GALS. DIL PER REV.	CU. IN. PER/REV.	TORQUE FT, LB. 100 PSI	RPM	GALS. Oil Per Rev.	TORQUE FT. LB. 100 PSI	RPM
1155	216	.22	50.8	69	0.300			
2150	728	.62	143.2	190	0-100	.31	95	0-120
2165	728	1.05	242.5	321	0-60	.52	160	0.110
3160	639	.90	207.9	273	0-200	.45	136	0.200
4150	958	1.24	286.4	380	0-115	.62	190	0.115
4160	958	1.80	415.8	545	0-80	.90	272	0.80
4170	958	2.44	563.6	743	<b>0</b> .65	1.22	372	0 65
6170	1365	2.92	674.5	890	0.55	1.46	445	0-55
6185	1435	4.32	997.9	1315	0-36	2.16	657	0.36
8285	3080	8.64	1996.0	2630	0-16	4.32	1315	0.32
8385	3080	10.00	2310.0	3080	0.16	5.00	1540	0.32

Note: Maximum pressures. Types 1155 and 3160 — 5000 PSI. Types 2150 and 4150 — 3500 PSI. Type 4160 — 3250 PSI. All others — 3000 PSI.



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## PERFORMANCE CHARACTERISTICS







LEAD COMPENSATION

119-27 5:

APPENDIX J COMBAT VEHICLE SYSTEM

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	TITLE ACTIVA	TION	OF G-DOF S	SIMULATOR	
-	TANK PITCH	/	DRIVE SYST	EM :	
F.	ARAMETER		REFERENCE	DESIGN VALUE	UNIT
M. OF	ASS MOMENT INERTIA	Ι	MICV 65 + 10%	2,000	LB-FT-SEC <sup>2</sup>
Un	IBALANCE	Tm	6076(1)(SIN 15°)	1573	LB-FT
FIA	EING TORQUE	Tfr	3000 × 3'	9,000	' LB-FT
M.	ax. Amplitude	×		± 15°	DEGREE
NON	AMPLITUDE	X	Spec.	3.0	Degree
MOT	FREQUENCY	f	SPEC.	3.5	Ha
AK	. VELOCITY	Ż	$(2\pi)^{2}(f)(\chi)/_{360}$	1.15	RAO/SEC
Pe	Accel.	κ.	271(f)(x)	25,32	RAD/SEL 2
00	ARM	R	56"	4.67	FT.
2"	STROKE	- 2	2(51N 15°)(56)= 29"	30"	1N.
12 ×	REGO TORQUE	Τ.	1.5 (IX + Tm + Tfr)	91,820	LB-FT
SKE	HYD. FORCE	FH	$\frac{T}{R} = 19676_{REQD}$	21,947 AVAIL	LB.
<i>₫</i> 'B.	PISTON	As	$> \frac{F_H}{3000} = 6.56$	7.568 AVAIL	1 N <sup>2</sup>
	AREA	A.	= 'As	7.568	/ N <sup>2</sup>
1701	PISTON SPEED	V	12 R(X)	64.4	IN/SEL
Tur.	VALVE FLOW	Qr	$\frac{A_{L}(V)(60)}{231}$	126.6	GPM
Ac	PUMP FLOW	Q <sub>p</sub>	$> \frac{2}{\pi} Q_{V}$	81	GPM
	HYDRAULIC STIFFNESS	KH	2×10 <sup>5</sup> 2(As+AL) 4/12 R <sup>2</sup>	53.35 × 106	LB-FT/ . RAD.
E NAT	URAL FREQ.	Fn	$\frac{1}{2\pi}\sqrt{\frac{k_{H}}{1.2}}$	23.7	Hz

Form 207 1014 6-71

Drawing No. A-2633

ltem	Weight (1b)	C.G. Offset R(ft)	$\frac{WR^2}{g} (1b-ft-sec^2)$	l (lb-ft- sec <sup>2</sup> )
(Pitch & Roll Gimbal)	4,000	0	0 ·	465
Tank Coupla (MICV65 + 10%)	6,076	11	189	1,155
Support TUBE	1120	Ľ	35	521
			*	
				1
Total	10,076		380	1,620
Mass Moment of Inertia	(lb-ft-sec <sup>2</sup> )		2,0	000

σ

## Estimated Mass Moment of Inertia About Tank Pitch Axis

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Form 207 10M 6-71

Drawing No. A-2636

# Moog 79 Series-200 GPM High Flow Servovalves

Moog 79 Series — 200 GPM Servovalves control position, velocity or force of massive machine elements, with fast response at high flows. They are 3-stage servovalves using standard 2-stage Moog industrial valves for pilot operation. Operating in conjunction with an electronic position feedback loop, the pilot valve controls position of the 3rd stage spool, which in turn meters the high output flow.

Because of the high position loop gain around the 3rd stage, hysteresis and threshold properties meet or exceed the specifications of the best 2-stage servovalves. The excellent dynamic response of the 79 Series — 200 GPM servovalves makes them well suited for structural or fatigue testing applications where high frequency and full amplitude output are required.

A single servoamplifier can be used to provide closed loop operation for the third stage spool position and the required amplification and electronic mixing functions for the outer or major loops. Moog Series 82 Servocontrollers are highly recommended for this purpose.

Moog 79 Series — 200 GPM Servovalves are available in two configurations: Standard and High Response. In the Standard configuration, pilot valve flow operates on the full area of the third stage spool. In the High Response configuration, pistons of smaller area are incorporated on the ends of the third stage spool to optimize response as a function of pilot valve flow.



The following options are available in both configurations:

- Choice of Moog Series 73, 74 or 76 Servovalve for pilot operation with flow rates for optimum performance in the particular application.
- Choice of LVDT or DCDT spool position feedback transducer.
- Provision for mounting auxiliary spool positions transducer for monitoring.
- Provision for operating the pilot valve from a separate hydraulic power source.



#### **General Characteristics**

Flow Rating	200 gpm at 1000 psi valve drop
Operating Pressure	300 to 3000 psi
Inlet proof pressure	4500 psi
Return proof pressure	3000 psi
Fluid	Petroleum base hydraulic fluid Others on special order
Filtration	10 microns recommended
Internal leakage at null	less than 2% of rated flow
External leakage	none
Pressure gain at null	Greater than 30% supply pressure for 1% input
Weight	47 lbs.
Null Shift*	less than 1% for 80% to 110% supply pressure variation 0% to 20% back pressure variation 100°F temperature change
Hysteresis*	less than 1%
Threshold*	less than 0.5%
An address of the second s	

\*Values for third stage spool position loop gain of 250 sec





# SYSTEM RESPONSE



TITLE 6-DOF FOR TANK YAW DRIVE

Suspended W4: = 13,000 (14.)  
MASS MOMENT OF INERTIA 
$$(I_2) = 30,000 (16 - 10 - 56c^{*})$$
  
REQU Acceleration  $(\ddot{\psi}) = 25.32 (\frac{PAO}{56c^{*}})$   
FIRING LOAD: 3000 (16) AT 3' ARM  
 $F_X = 3000 (16)$   
 $M_2 = 108,000 (17 - 16)$   
TORQUE  $(T) = I_2 \ddot{\psi} + M_2 = 867,600 (17 - 16)$   
EQUIV.  $\ddot{\psi}$  FOR SAME  $I_2 (\ddot{\psi}_i)$ :  
 $\dot{\psi}_i = \frac{T}{I_2} = \frac{867600}{86000} = 28.92 (\frac{PAO}{56c^{*}}) \frac{5AY 29}{54Y 29}$   
Assumue (2) Concentrated W4: AT  $\pm X''$  (6500 + 64.)  
 $I_2 = (2) (\frac{6500}{9}) (X^2) = 30,000 (16 - 10 - 56c^{*})$   
 $X = \sqrt{\frac{30,000 + 9}{(2)(6500)}} = 29.86'' (\frac{5AY 30''}{54Y 30'})$   
Acceleration IN X-AXIS DUE TO FIRING: --  
 $F = M\dot{X} = 3000$  #  
 $\dot{X} = \frac{3000 + 9}{13,000 *} = .23g = 89.17 (\frac{10}{56c^{*}}) \frac{5AY 90}{54Y 90}$ 

Form 207 10M 1-73

TITLE 6-DOF FOR TANK VAN DRIVE

INPUT OF SOFS PROGRAM :-

	LUMPED	WEIGHT		
NO.	<u>×</u>	Y	7	w+ (16)
1	+ 30"	0	+36"	6,500
2	- 30"	0	+36	6,500

PLATFORM I	DISPLACE	MENT	
	×	Y	Z
TRANSLATION (IN.)	0	0	0
ROTATION (DEGREE)	0	0	3.0

AcceleRATIONS A	LTING ON	W4.	
	×	Y	2
TRANSLATION ("/SEC")	90.	0	0
ROTATION (RAO/SEC2)	. 0	0	29.

"SDFS" 6 - D.O.F. FOR TANK YAW DRIVE . . . . . . COORDINATES OF FIXED FRAME ACTUATOR X (IN.) Y\_ (IN.)\_ Z (IN.) 1 15.58846 36.00000 -36.00000 2 -38.97114 4.50000 -36.00000 3 -38.97114 -4,50000 -36,00000 4 15.58846 -36.00000 -36.00000 5 23.38269 -31.50000 -36.00000 6 23.38269 31.50000 -36.00000 COORDINATES OF MOVING FRAME X (IN.) ACTUATOR Y (IN.) Z (IN.) 1 -12.99038 2 -18.18653 25.50000 .00000 3 -18.18653 -25.50000 .00000 4 -12.99038 -28.50000 .00000 5 31.17691 -3.00000 .00000 6 31.17691 3.00000 .00000 ..... COORDINATES OF LUMPED WEIGHTS NO. X (IN.) Y (IN.) \_ Z (IN.) WEIGHT (LBS) 1 ... 30.00000 +00000 .36.00000 2 -30.00000 •00000 36.00000 6500.00000 397

	PLATFORM_DIS	PLACEMENT		
TRANSLATI Rotation	ON (IN.) (DEG.)	XY •000 •0 •0000	Z 00 •000 00 •000	
C	OORDINATES OF	MOVING FRAM	ME	
ACTUATOR	X (IN.)	Y (IN+)	Z (IN•)	ACTUATOR LENGTH
1	-12.99038	28.50000	.00000	46.57252
2	-18.18653	25.50000	.00000	46.57252
3	-18.18653	-25.50000	.00000	46.57252
. 4 K	-12.99038	-28.50000	•00000	46.57252
5	31 17(01	~3.00000	•00000	46.57252
			•.00000	46.57252
ACCEL LINEAR ANGULAR (	(IN/SEC2) RAD/SEC2)	NG ON WEIGH X Y •00 •00	Z 00 00 00 00	• • •• ••• ••••••
ACTU	ATOR FORCES	· • • • • • • • •		•
ACTU	ATOR FORCES	5)		•
ACTU ACTUATOR	ATOR FORCES FORCE (LB	s) 4		•
ACTU ACTUATOR	ATOR FORCES FORCE(LB 	S) 44	· · · · · · · · · · · · · · · · · · ·	•
ACTU ACTUATOR 1 2 3	ATOR FORCES FORCE(LB 	S) 4 4 4	·····	•
ACTU ACTUATOR 1 2 3 4 5	ATOR FORCES FORCE(LB -28030+0 -28030+0 -28030+0 -28030+0	S) 4 4 4 4		•
ACTU ACTUATOR 2 3 4 5 6	ATOR FORCES FORCE(LB 	S) 4 4 4 4 4 4	······	•
ACTU ACTUATOR 1 2 3 4 5 6	ATOR FORCES FORCE(LB -28030+0 -28030+0 -28030+0 -28030+0 -28030+0 -28030+0	S) 4 4 4 4 4 4 4 4		•
ACTU ACTUATOR 1 2 3 4 5 6 COMP	ATOR FORCES FORCE(LB 28030+0 28030+0 28030+0 28030+0 28030+0 28030+0 0NENTS OF FOR	S) 4 4 4 4 4 4 4 5 5 5 5 7 7 7 7 7 7 7 7 7		•
ACTU ACTUATOR 1 2 3 4 5 6 COMP 1	ATOR FORCES FORCE(LB .28030+0 .28030+0 .28030+0 .28030+0 .28030+0 .28030+0 .28030+0 .28030+0 .28030+0	S) 4 4 4 4 4 4 5 5 5 3 9+03	•21667+04	
ACTU ACTUATOR 1 2 3 4 5 6 COMP 1 2	ATOR FORCES FORCE(LB .28030+0 .28030+0 .28030+0 .28030+0 .28030+0 .28030+0 .28030+0 .28030+0 .28030+0 .28030+0 .28030+0	S) 4 4 4 4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5	•21667+04 •21667+04	
ACTU ACTUATOR 1 2 3 4 5 6 COMP 1 2 3	ATOR FORCES FORCE(LB 28030+0 28030+0 28030+0 28030+0 28030+0 28030+0 28030+0 28030+0 12509+04 12509+04 2209+04	S) 4 4 4 4 4 4 CES •45139+03 •12639+04 •12639+04	•21667+04 •21667+04 •21667+04 •21667+04	
ACTU ACTUATOR 1 2 3 4 5 6 COMP 1 2 3 4 4	ATOR FORCES FORCE (LB .28030+0 .2	S) 4 4 4 4 4 4 CES • 45139+03 • 12639+04 • 12639+04 • 12639+04 • 45139+03	•21667+04 •21667+04 •21667+04 •21667+04 •21667+04	
ACTU ACTUATOR 1 2 3 4 5 6 COMP 1 2 3 4 5	ATOR FORCES FORCE(LB .28030+0 .28	S) 4 4 4 4 4 4 CES • 45139+03 • 12639+04 • 12639+04 • 12639+04 • 12639+04 • 1253+04	•21667+04 •21667+04 •21667+04 •21667+04 •21667+04 •21667+04	
ACTU ACTUATOR 1 2 3 4 5 6 COMP 1 2 3 4 5 6	ATOR FORCES FORCE(LB .28030+0 .2809+04 .46910+03 .46910+0400+040+0400+040+040+040+040+040+040	S) 4 4 4 4 4 4 4 4 5 12639+03 •12639+04 •12639+04 •12639+04 •17153+04 •17153+04	•21667+04 •21667+04 •21667+04 •21667+04 •21667+04 •21667+04 •21667+04	
FOI	R TANK YAW DE	IVE		
--	---	---	--	---
	COORDINATES C	E FIXED FRAM	<u>الا</u>	
ACTUATOR	X (IN.)	Y (IN.)	Z.(IN.)	
1	15,58846	36.00000	-36,00000	
2	-38.97114	4.50000	-36.00000	
33	-38.97114	-4.50000	-36.00000	
4	15.58846	-36.00000	-36.00000	
	23.38269	-31.50000	-36.00000	
6	23.38269	31.50000	-36.00000	
(	COORDINATES C	E MOVING ERA	ME	
ACTUATOR	X (IN+).	Y (IN.)	Z (IN.)	•
1	-12-99030	28.50000		
2	-18.18653	25.50000		1. The set of the s
3	-18.18653	-25.50000	•00000	
4	-12.99038	-28.50000	• [10000	
5	31.17691	-3.00000	.00000	
6	31.17691	3.00000	•00000	
				······································
. 16	COURDINATES	OF LUMPED	EIGHTS	
NV •	X (IN•)		2 (IN+)	WEIGHT (LBS)
1	30.00000	•00000	36.00000	6500.00000
۷	-30.00000	•00000	36.00000	. 6500.00000
	an a			
	an a		a Marcela di Amerikany di persong pangan dan kalanya dagi ki di seja dan yang ka	
	· · · · · · · · · · · · · · · · · · ·	na manda mana ka kana ka kana ina ang kana kana ka mana kana kana kana kana k		
an a				
	An ar anna an a	, ,		

la angelaki na ani ange panyan iking kina anger ip tampa sa ip	PLAIEORN_D	ISPLACEMENT.		
TRANSLATI ROTATION	ON (IN.) (DEG.)	X Y •000 •0 •000 •0	2 00 •000 00 •000	· · · · · · · · · · · · · · · · · · ·
C	OORDINATES (	DF MOVING FRA	ME	
ACTUATOR	X (IN.)	Y (IN+)	Z (IN.)	ACTUATOR LENGTH
1	-12.99038	28.50000	•00000	46.57252
2	-18.18653	25.50000	,00000	46,57252
3	-18.18653	-25.50000	•00000	46.57252 .
4	-12.99038	-28.50000	•00000	46.57252
5	31.17691	-3.00000	•00000	46.57252
<b>.</b> 0	51.17691	3.00000	• • • • • • • • • • • • • • • • • • • •	46+57252
ACCEL	ERATIONS ACT	TING ON WEIGH	τς	
	-			
TNEAD	(TN/CECO)	X T	<u> </u>	
ANGULAR (	RAD/SEC2)	•00	• 00 • 00 _	
	JATOR FORCES			
		2	,	
ACTUATOR	FORCE	_BS)	· · · · · · · · · · · · · · · · · · ·	
	FORCE (1	-BS)		
ACTUATOR	FORCE (1 .17205- .51999-	-BS) +04 +04		
ACTUATOR	FORCE (1 •17205 •51999 •51999	-BS) +04 +04 +04		
ACTUATOR 12 4 4	FORCE (1 •17205 •51999 •51999 •17205 •17205	-BS) +04 +04 +04 +J4	· · · · · · · · · · · · · · · · · · ·	
ACTUATOR 12 3 4 5 6	FORCE (1 • 17205 • 51999 • 51999 • 17205 • 14885 • 14885	-BS) +04 +04 +04 +J4 +J4 +04		
ACTUATOR 12 3 4 5 6	FORCE (1 •17205 •51999 •51999 •17205 •14885 •14885	-BS) +04 +04 +04 +J4 +J4 +04 +04		
ACTUATOR 1 2 3 4 5 6 CON-F	FORCE (1 .17205- .51999- .51999- .17205- .14885- .14885- .14885- PONENTS OF FO	-BS) +04 +04 +04 +J4 +04 +04 +04		
ACTUATOR 1 2 3 4 5 6 CONF	FORCE (1 .17205- .51999- .51999- .17205- .14885- .1485-	-BS) +04 +04 +04 +04 +04 +04 +04 +04 -04 -027707+03	•13299+04	
ACTUATOR 1 2 3 4 5 6 COMF 1 2	FORCE (1 .17205- .51999- .51999- .17205- .14885- .1485-	-BS) +04 +04 +04 +04 +04 +04 +04 +04 -0707+03 -23447+04	•13299+04 •40194+04	
ACTUATOR 1 2 3 4 5 6 COMF 1 3 3	FORCE (1 .17205- .51999- .51999- .17205- .14885- .14885- .14885- PONEINTS OF FO 10558+04 .23206+04 .23206+04	-BS) +04 +04 +04 +04 +04 +04 +04 +04 -27707+03 -23447+04 23447+04	•13299+04 •40194+04 •40194+04	
ACTUATOR 2 3 4 5 6 COMF 2 3 4	FORCE (1 .17205- .51999- .51999- .17205- .14885- .1485-	-BS) +04 +04 +04 +04 +04 +04 +04 +04 +04 -27707+03 -23447+04 -27707+03	•13299+04 •40194+04 •40194+04 •13299+04	
ACTUATOR 1 2 3 4 5 6 COMF 1 2 3 4 5	FORCE (1 .17205- .51999- .51999- .17205- .14885- .1485-	-BS) +04 +04 +04 +04 +04 +04 +04 +04 +04 +04	•13299+04 •40194+04 •40194+04 •13299+04 •11506+04	
ACTUATOR 1 2 3 4 5 6 COMF 1 2 3 4 5 6	FORCE (1 .17205- .51999- .51999- .17205- .14885- .14885- .14885- PONEINTS OF FO 10558+04 .23206+04 .23206+04 10558+04 .24912+03 .24912+03	-BS) +04 +04 +04 +04 +04 +04 +04 +04 +04 +04	•13299+04 •40194+04 •40194+04 •13299+04 •11506+04 •11506+04	

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C	OORDINATES_0	F FIXED ERA	ME	,
ACTUATOR	X (IN•)	Y.(IN.)	Z_(IN.)	· · · · · · · · · · · · · · · · · · ·
1	15.58846	36.00000	-36.00000	
2	-38.97114	4.50000	-36.00000	· · · · · · · · · · · · · · · · · · ·
3	-38.97114	-4.50000	-36.00000	
4	15.58846	-36.00000	-36.00000	
5	23.38269	-31,50000	-36.00000	
6	23.38269	31.50000	-36.00000	
C	OORDINATES_D	E MOVING ER	AME	•
ACTUATOR	X (IN.)	Y (IN.)	Z (IN•.)	
1	-12.00430	28.50000	00000	
2	-18,195030	25,50000		and the supersystem to an address of the supersystem and and the supersystem and and the supersystem of the
3	-18,18653	-25 50000	•00000	
4	-12.09034	-28.50000		
5	31,17601	-20,00000	•00000	
6	31,17691	3.00000	•00000	
	COORDINATES_	OF LUMPED	NEIGHTS	
NO •	X (IN.).	Y (IN+)		WEIGHT (LBS
1 2	30.00000	•00000	36.00000	6500.00000
		· · ·	• • • • • • • •	
••• •• • •				
			• • • • • • • • • • • • • • • • • • •	•
		·		
		*		
		•		

TRANSLATION ROTATION	PLATEORM_DI	SPLACEME	NT		
TRANSLATION ROTATION	J (TNL)				· · · · · · · · · · · · · · · · · · ·
ROTATION	* * #14# /	X	Y _ •00	2 0 • 000	
	(DEG.)	•000	•00	0 3.000	
CO	DRDINATES O	F MOVING	FRAM	Ē	
ACTUATOR	X (IN.)	Y (I	N•)	Z (IN.)	ACTUATOR LENGTH
1	-14.46415	27.78	108	.00000	47.60998
	-19.49618	24.51	324	• 00000	45.56099
3	-16.82704	-26.41	686	•00000	47.60998
. 4 . r	-11.48100	-29.14	081	•00000	45.56099
5	31.29120	-1.36	421	•00000	47.60998
6	30.97718	4•62	756	•00000	45.56099
ACCELER	RATIONS ACT	ING ON W	EIGHT	5	
TNEAD ()		X	Ŷ	Z	
ANGILAD (D)	D/SECSI	• 00	• • •		
ACTUATOR	FORCE(L	BS)			
. 1	.13748+	05	•		
2	76717+	<u>04</u>	******		
3	•13748+	05	•		
4	76717+	04		•••••••••	
5	•13748+	05			
6	76717+	04			
COMPO	ENTS OF FU	RCES			
1	86778+04	23732+	04	•10395+05	
2 -	32793+04	33699+	04 -	•60618+04	
3	63942+04	63286+	04	.10395+05	
4	45580+04	11550+	04 -	•60618+04	
5	22836+04	.87018+	04	.10395+05	
6 -,	12788+04	•45249+	04 -	•60618+04	
		•	***		
				, <u>an ha an an Anna an</u>	

TITLE 6-DOF FOR TANK YAW SUMMARY : "SDFS" OUTPUT ACTUATOR LENGTH: (MAX) = 47.60998" (MIN.) = 45.56099 Double Ampliquoe: (al) = 2.04899" ACTUATOR FORCE : - (ACTUATOR NO. 3 IS THE MAX.) Fa (MAX.) = 13,784 + 5,200 - 2,803 = 16,181 (16) MAX. ACTUATOR WORKING PRESSURE: Pa = 16.181 = 1520 (PSI), AP = 2900-1520=1380(PSI) SERVOVALVE RATED 60 GPM AT 1000 PSi IS CAPABLE OF DELIVERING QUE 60 / AP = 70.5 GPM (AT OP = 1380) MAX. PISTON SPEED (X) = WX  $\dot{X} = (3.5)(2\pi)(\frac{2.04899}{2}) = 22.53$  "/sec. REQ'D VALVE FLOW (Qo) FOR YAW DRIVE: Qo = (22.53) (10.64) 60 = 62.3 GPM. AVAILABLE VALVE FLOW FOR 6. DOF SPRING SYSTEM :-Q= 6 (Qv - Qo) = 6 × 8.2 = 49.2 GPM

Form 207 10M 1-73

TITLE ACTIVATION OF 6-DOF SIMULATOR

PERFORMACE LIMITS OF TURRET YAW BY USING MAIN YAW DRIVE :-

1. DEIVE MOTOR

208	MAX. TORQUE	Тмах	<u>3080</u> × 3000 × (e) EFF: 9 100	83,160	LB-FT
1011	MOTOR FLOW	8	CATALOG	2310.	IN 3 REV.
V.E.	VALVE FLOW	Q.	$\frac{8 \omega}{23 H(2)} = 40 (=.9)$	60	GPM
1201	PUMP FLOW	Q.p	$\frac{2}{\pi}Qv$	26	GPM
1	HYORAULIC STIFFNESS	KH	5EE DWG. NO. A-2629, SHEET 2.	1.232×10 <sup>6</sup>	LB-FT/ RAD.

3. MAX. Acceleration(x):  $1.5(I_2 + T_m + T_{4r}) = 83160(LB-FT)$   $T_m = 0$ ,  $T_{4r} = 9000(LB-FT)$   $\dot{x} = \left(\frac{83160}{1.5} - 9000\right)/5415 = 8.576(RA0/SEC^2)$ 4. MAX. Velocity(x) := For 60 GPM Value Flow  $-\frac{8}{231(.9)} = 60 GPM$ ,  $W = \frac{60(251)(.9)}{2310} = 5.4(RPM)$ ,  $\dot{x} = \frac{5.4(2\pi)}{60} = .56(\frac{RA0}{SEC})$ 5. ESTMATED MATURAL FREQUENCY  $(f_n) := f_n = \frac{1}{2\pi}\sqrt{\frac{KH}{12T}} = \frac{1}{2\pi}\sqrt{\frac{1.232 \times 10^6}{5.64(51)}} = 2.19 Ha$ 

Form 207 10M 1-73

Drawing No. A-2661

APPENDIX K TAIL ROTOR SIMULATOR

4

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TITLE ACTIVATION OF G-DOF SIMULATOR							
-	TAIL ROTOR		DRIVE SYSTEM:				
F	PARAMETER	-	REFERENCE	DESIGN VALUE	UNIT		
M	ASS MOMENT E INGRIA	I	AH-161	15,670	LB-FT-SEC <sup>2</sup>		
U	NBALANCE	Tm		0	LB.FT		
FI.	RING TORQUE	T <sub>fr</sub>	3000 × 1.5'	4500	2B-FT		
M	AX. AMPLITUDE	$\times$		± 3°	DEGREE		
NON	AMPLITUDE-	X	SPEC.	± 3° .	DEGREE		
MO7	FREQUENCY	f	SPEC.	.3	Ha		
X	VELOCITY	Ż	$(2\pi)^{*}(f)(\chi)/360$	•1	RAD/SEC		
P.	. Accel.	ÿ	$2\pi(f)(\dot{x})$	. 19	RADI ISEC2		
2	ARM	R	(STA. 302")	8.5'	· FT.		
"Ko	STROKE	.4	(2x) (2#) 12 360 x 12=10.7	$11(\pm 5\frac{1}{2})$	1 N.		
x/s	REQ'D TORQUE	T	1.5 (IX + Tm + Tfr)	11,216	1B-FT		
ORE	HYD. FORCE	FH	$\frac{T}{R} = 1320$ $\frac{T}{REQ'D}$	4970. AVAIL.	LB.		
0,0	PISTON	As	> FH 3000 = 46 REQID	1.6567. EVAIL	INZ		
6/	AREA	A.	= As	1.6567	/ N <sup>2</sup>		
170,	PISTON SPEED	V	12R(X)	10.2	IN/BEC		
YUZ:	VALVE FLOW	$Q_{r}$	$\frac{A_{1}(V)(Go)}{231} = 4.4$	Морц 73-233 (10 GPM)	GPNI		
Ac	PUMP FLOW	Qp.	> Z QV ACCUMULATOR USED	4.4	GPM		
	HYDRAULIC STIFFNESS	K.H	2×10 <sup>5</sup> 2(As+AL) 2 <sup>2</sup>	104.5×106	LB-FT/ RAD.		
E NAT	STIMATED WRAL FREQ.	Fn	$\frac{1}{2\pi}\sqrt{\frac{K_{H}}{1.2 I}}$	11.86	Hz		

Form 207 10Ni 6-71

Drawing No. A-2634

TITLE TAIL ROTOR SIMULATOR

	LOCATIONS (IN.)				MOMENT	FORCE
	57A.	W. L	X	2	(87-16)	(16)
C. G.	200	69.7	0	0	0	
TAIL ROTOR	520.67	118.3	320.67	48.6	28,700	1,074
SIMULATOR	302.	85.16	102.	15.46	28,700	3,370

AH- 1G HEUCOPTOR

FIRING LOAD = 3000 # (MAX.) AT 18" SIMULATOR REACTION =  $\frac{3000 \times 18}{102}$  = 530 # TOTAL MOMENT OF INERTIA (II) = 15,670 (16.FT. SEC<sup>2</sup>) SECTION ON SIMULATOR (I2) = 5,000 (16.FT. SEC<sup>2</sup>)

Simulator FORCE =  $\frac{\dot{\psi}(I_1 - I_2)}{8.51}$  where  $\dot{\psi} = .62(\frac{RAP}{SEC^2})$ =  $\frac{.62(10,670)}{8.5} = 800 \, \text{f}$ 

Form 207 10M 1-73

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Form 207 10M 6-71

# MOOG SERIES 73 SERVOVALVE

The 73 Series Servovalve is a high pr formance, two-stage design that cover the ran e of rated flows from 1 to 15 gpm et (200 pr (4 to 58 lit min at 70 bars). The radius have a large field replaceable fill profirst stage flow that insures lor trouble-free operation.

The output stage is a closed atter, four-way, sliding spool. The pilot stage is symmetrical double-nozzle and flapper, i five, by a double air gap, dry torque motor. I schan tal feedback of spool position i provic to by a simple cantilever spring. The value lesign is simple and rugged for dependent on glife operation. A large capacity, field replaceable filter gives added protection of first stage flow.

The spool and sleeve assembly floats on o-rings in an aluminum alloy body. This isolates the spool from side loading that could be imposed by mounting the valve on a slightly uneven manifold. A convenient null adjustment is provided by an eccentric pin that locates the sleeve. The pilot stage is built-up as a separate subassembly that can be removed without upsetting careful spacing of the torque motor parts.

Several 73 Series models are available from stock. A variety of options can be supplied on special order.



In a conventional closed-loop position control system, valve flow is applied to a hydraulic piston which drives the load. Load position is measured electrically and fed back for comparison with a signal representing the desired position. The resulting error signal is amplified, providing current input to the valve to control flow.



### OPERATION

Moog Series 73 Servovalves use an electrical torque motor, a double-nozzle pilot stage, and a slidingspool second stage. Electrical current in the torque motor gives proportional displacement of the second stage spool; hence, proportional flow to the load.

### TORQUE MOTOR

The torque motor includes coils, polepieces, magnets, and an armature. The armature is supported for limited pivotal movement by a flexure tube. The flexure tube also provides a fluid seal between the hydraulic and electromagnetic portions of the valve.

#### PILOT STAGE

The flapper attaches to the center of the armature and extends down, inside the flexure tube. A nozzle is located on each side of the flapper so that flapper motion varies the nozzle openings. Pressurized hydraulic fluid is supplied to each nozzle through a filter and inlet orifice. Differential pressures caused by flapper movement between the nozzles are applied to the ends of the valve spool.

### **DESIGN FEATURES\***

rugged aluminum alloy body

- o-ring floated, center pinned bushing with convenient null adjust
- field replaceable 20 micron filter for pilot flow
- dry torque motor in sealed compartment
- frictionless, flexure tube supported armature-flapper
- modular torque motor and pilot stage assembly
- balanced, double coil, double air gap torque motor
- mechanical feedback with simple cantilever spring
- spool-bushing diametral tolerances held within 10 microinches (¼ micron)
- motor coils protected during thermal and vibration extremes by resilient potting

optional fifth port for separate pilot supply

\*Design features of the Series 73 Servovalve are covered by U.S. Patents 3,023,782 and 3,228,423 together with corresponding patents in several foreign countries.

#### VALVE SPOOL

The 4-way valve spool controls flow from the supply to either control port (C1 or C2). Simultaneously, the other control port is opened to fluid return. The spool fits in a sleeve that contains openings which are uncovered by spool motion to meter flow to the load. Various valve rated flows are provided by sizing these openings in the sleeve. Spool motion deflects a cantilever feedback wire that applies torque to the armature-flapper.

### **OPERATION**

Electrical current in the torque motor coils causes either clockwise or counter-clockwise torque on the armature. This torque displaces the flapper between the two nozzles. The differential nozzle flow moves the spool to either the right or left. The spool continues to move until the feedback torque counteracts the electromagnetic torque. At this point the armature/flapper is returned to center, so the spool stops and remains displaced until the electrical input changes to a new level. Therefore, valve spool position is proportional to the electrical signal. The actual flow from the valve to the load will depend upon the supply and load pressures as described on page 3 under Rated Flow.



### TERMINOLOGY

See Moog Technical Bulletin No. 117 for a complete discussion of servovalve terminology and test techniques.

### ELECTRICAL

INPUT CURRENT The electrical current to the valve which commands control flow, expressed in milliamperes (ma).

RATED CURRENT The specified input current of either polarity to produce rated flow, expressed in milliamperes (ma). Rated current is specified for a porticular coll consection (onferential, series or parallel colls) and does not include null bias current.

QUIESCENT CURRENT A dc current that is present in each valve coil when using a differential coil connection. The polarity of the current in the two coils is reversed so that no signal input exists.

COLL IMPEDANCE The complex ratio of coil voltage to coil current. Coil impedance will vary with signal frequency, amplitude, and other operating conditions, but can be approximated by the dc coil resistance (ohms) and the apparent coil inductance (henrys) measured at a signal frequency.

DITHER An ac signal sometimes superimposed on the servovalve input to improve system resolution. Dither is expressed by the dither frequency (Hz) and the peak-to-peak dither current amplitude (ma).

### HYDRAULIC

CONTROL FLOW The flow through the valve control ports to the load, expressed in in<sup>3</sup>/sec (cis), or gal/min (gpm), or lit/min (lpm).

RATED FLOW The specified control flow corresponding to rated current and given supply and load pressure conditions. Rated flow is normally specified as the no-load flow and is expressed in cis, or gpm, or lpm.

FLOW GAIN The nominal relationship of control flow to input current, expressed as cis/ma, or gpm /ma, or lpm/ma.

NO-LOAD FLOW The control flow with zero load pressure drop, expressed in cis, or gpm, or lpm.

INTERNAL LEAKAGE The total internal valve flow from pressure to return with zero control flow (usually measured with control ports blocked), expressed in cis, or gpm, or lpm. Leakage flow will vary with input current, generally being a maximum at the valve null (called NULL LEAKAGE).

LOAD PRESSURE DROP The differential pressure between the control ports (that is, across the load actuator), expressed in lbs/in<sup>2</sup> (psi), or bars. VALVE PRESSURE DROP The sum of the differential pressures across the control orifices of the servovalve spool, expressed in psi or bars. Valve pressure drop will equal the supply pressure, minus the return pressure, minus the load pressure drop  $[P_V = (P_S - P_R) - P_L]$ .

### PERFORMANCE

LINEARITY The maximum deviation of control flow from the best straight line of flow gain. Expressed as percent of rated current.

SYMMETRY The degree of equality between the flow gain of one polarity and that of reversed polarity, measured as the difference in flow gain for each polarity and expressed as percent of the greater.

HYSTERESIS The difference in valve input currents required to produce the same valve output as the valve is slowly cycled between plus and minus rated current. Expressed as percent of rated current.

THRESHOLD The increment of input current required to produce a change in valve output. Valve threshold is usually measured as the current increment required to change from an increasing output to a decreasing output. Expressed as percent of rated current.

LAP In a sliding spool valve, the relative axial position relationship between the fixed and movable flow-metering edges with the spool at null. Lap is measured as the total separation at zero flow of straight line extensions of the nearly straight portions of the flow curve, drawn separately for each polarity. Expressed as percent of rated current.

**PRESSURE GAIN** The change of load pressure drop with input current and zero control flow (control ports blocked). Expressed as the nominal psi/ma or bars/ma throughout the range of load pressure between  $\pm$  40% supply pressure.

NULL The condition where the valve supplies zero control flow at zero load pressure drop.

NULL BIAS The input current required to bring the valve to null, excluding the effects of valve hysteresis. Expressed as percent of rated current.

NULL SHIFT The change in null bias resulting from changes in operating conditions or environment. Expressed as percent of rated current.

FREQUENCY RESPONSE The relationship of no-load control flow to input current when the current is made to vary sinusoidally at constant amplitude over a range of frequencies. Frequency response is expressed by the amplitude ratio (in decibels, or db), and phase angle (in degrees), over a specific frequency range.

		English	Metric	Conversion*
	fluid flow	in³/sec (cis)	lit/min (lpm)	1 lpm/cis
UNITS		gal/min (gpm)		3.8 lpm/gpm
	fluid pressure	lbs/in² (psi)	bars	0.07 bars/psi
Recommended English and Metric	dimensions	inch (in)	millimeters (mm)	25 mm/in
(SI) units for expressing servo-	weight	pounds (:b)	kilogram (kg)	0.45 kg/lb
following:	force	pounds (ib)	deka Newtons (daN)	0.45 daN/lb
	torque	in-ibs	deka Newton meters (daNm)	0.011 daNm/in-lb
	temperature	degrees Fahrenheit (*F)	degrees Celsius (°C)	•C = 5/9 (•F −32)

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## HYDRAULIC CHARACTERISTICS

Unless specified otherwise, all performance parameters are given for valve operation on Mobil DTE-24 fluid at 100°F (38°C).





FIGURE 2 - CHANGE IN CONTROL FLOW WITH CURRENT AND LOAD PRESSURE **FLUID SUPPLY** Series 73 Servovalves are intended to operate with constant supply pressure.

Supply Pressure	
minimum maximum standard maximum special order	200 psi (14 bars) 3000 psi (210 bars) 5000 psi (350 bars)
Proof Pressure	
at pressure port at return port	150% supply 100% supply
Fluid*	petroleum base hydraulic fluids 60 to 450 SSU at 100°F (38°C)
Supply filtration required	10u nominal (25u absolute) or better recommended
Operating temperature	
minimum	– 40°F (– 40°C)
maximum unless limited by fluid	+ 275°F (+ 135°C)
	Supply Pressure minimum maximum standard maximum special order Proof Pressure at pressure port at return port Fluid* Supply filtration required Operating temperature minimum maximum unless limited by fluid

\*Buna N seals are standard; Viton A and EPR available on special order.

**RATED FLOW** Flow specified below is the full valve control flow with either  $\pm 100\%$  electrical input when operating with supply and load pressure conditions that give 1000 psi (70 bars) valve drop. Control flow will saturate in higher flow models due to pressure drop in internal passages.

Five valve models are available from stock:

Valve Model	Flow with 1000 psi (70 bars) Supply Rated Flow Internal Leakage
73-100	1 gpm (3.8 lit/min) < 0.17 gpm (0.66 lit/min)
73-101	2½ gpm (9.5 lit/min) < 0.22 gpm (0.83 lit/min)
73-102	5 gpm (19 lit/min) < 0.35 gpm (1.32 lit/min)
73-103	10 gpm (38 lit/min) < 0.35 gpm (1.32 lit/min)
73-104	15 gpm (57 lit/min) < 0.35 gpm (1.32 lit/min)

Rated flow for other valve pressure drop conditions is given in Figure 1. Flow with various combinations of supply pressure and load pressure drop can be determined by calculating the valve pressure drop.

$$\begin{array}{l} \mathsf{P_v} = (\mathsf{P_s} - \mathsf{P_R}) - \mathsf{P_L} \\ \mathsf{P_v} = \text{valve pressure drop} \\ \mathsf{P_s} = \text{supply pressure} \\ \mathsf{P_R} = \text{return pressure} \\ \mathsf{P_L} = \text{load pressure drop} \end{array}$$

FLOW-LOAD CHARACTERISTICS Control flow to the load will change with load pressure drop and electrical input as shown in Figure 2. These characteristics follow closely the theoretical square-root relationship for sharp-edged orifices, which is

$$Q_{L} = K \ i \sqrt{P_{v}}$$

$$Q_{L} = \text{control flow}$$

$$K = \text{valve sizing constant}$$

$$i = \text{input current}$$

$$P_{v} = \text{valve pressure drop}$$

# PERFORMANCE CHARACTERISTICS

FIGURE 3 NO-LOAD FLOW GAIN TOLERANCES

FLOW GAIN The no-load flow characteristics of a Series 73 servovalve can be plotted to show flow gain, symmetry, and linearity. Typical limits (excluding hysteresis effects) are shown in Figure 3.

**LINEARITY** The nonlinearity of control flow to input current will be most severe in the null region due to variations in the spool null cut. With standard production tolerances valve flow gain about null (within  $\pm 5\%$  of rated current input) may range from 50 to 200% of the normal flow gain.

### **RATED FLOW TOLERANCE**

$\pm 10\%$
< 10%
< 3%
$< \frac{1}{2}\%$

### SPOOL DRIVING FORCES

The maximum hydraulic force available to drive the secondstage spool will depend upon the supply pressure, and the hydraulic amplifier pressure gradient. The normal first-stage configuration for a Series 73 Servovalve will produce a spool driving force gradient which exceeds 1 lb/% (0.4 daN/%) input current with a 3000 psi (210 bars) supply. This gradient will be reduced about 30% when operating on a 1000 psi (70 bars) supply. The maximum spool driving force with 3000 psi (210 bars) supply is 150 pounds (67 daN).

STICS :UAless specified otherwise, all performance parameters are given for valve operation on Mobil DTE-24 fluid at 100°F (38°C).

**PRESSURE GAIN** The blocked load differential pressure will change rapidly from one limit to the other as input current causes the valve spool to traverse the null region. Normally the pressure gain at null for Series 73 Servovalves exceeds 30% of supply pressure for 1% of rated current and can be as high as 80%.

### NULL

MILL CHIET

externally adjustable

NULL SHIFT		
With Temperature	100°F variation (56°C)	<±4%
With Acceleration	to 10 g	<± 2%
With Supply Pressure	80% to 110% nominal	<± 2%
With Quiescent Current	50% to 100% rated current	<± 2%
With Back Pressure	0% to 20% of supply	<± 2%

**FREQUENCY RESPONSE** Typical response characteristics for Series 73 servovalves are shown in Figures 4 and 5. Servovalve frequency response will vary with signal amplitude, supply pressure, temperature, and internal valve design parameters. The variation in response with supply pressure, as expressed by the change in frequency of the 90° phase point, is given in Figure 6.

**STEP RESPONSE** Typical transient response of 73 Series servovalves is given in Figure 7. The straight-line portion of the response represents saturation flow from the pilot stage which will increase with higher supply pressures.



## ELECTRICAL CHARACTERISTICS

### **RATED CURRENT & COIL RESISTANCE**

A variety of coils are available for 73 Series servovalves, so there is a wide choice of rated current. See Table I. It is possible to derate a coil to give a lower rated current than listed, thus rated current may be 8 ma differential for a 1000 ohm/coil valve.

Also, 73 Series valves can be supplied with internal resistors to give higher resistance for a given rated current. Thus 670 ohm resistors with 130 ohm coils will give 30 ma rated differential current with 800 ohm/coil.

### Table II. Standard Coil Connections

Alternate Connections and Polarities Can Be Supplied

### Table I. Available Coils for 73 Series Servovalves

Nominal	Recommended Rated Current — ma		
Per Coil At 70°F (21°C) Ohms	Differential, Parallel, or Single Coll Configuration	Series Coils	Approx. Inductance Per Coil® Henries
22	200	100	0.10
40	50	25	0.15
80	40	20	0.30
130	30	15	0.55
200	20	10	0.80
500	15	7.5	2.2
1000	10	5	4.5
1500	8	4	6.5

\*Approximate inductance at 50 Hz; servovalve pressurized; total coil inductance will be approximately three times value given.

COIL CONFIGURATION	DIFFERENTIAL COILS	SERIES COILS	PARALLEL COILS	SINGLE COILS
TORQUE MOTOR COILS			<u>(000</u> )	
PIGTAIL COLORS	grn red blu	grn red	grn red	grn red yei blu
INPUT CURRENT FOR FLOW OUT CONTROL PORT C1	for A+, when current A to $B < A$ to C; for A-, when current B to $A > C$ to A; for series coils use B+ C	with B+, A-	with B+, A	with B+, A- or D+, C; for differential coils tie A to D; for series coils tie A to D; for parallel coils tie A to C and B to D.

**COIL CONNECTIONS** The two coils of the **73** Series servovalve may be connected in several different ways as shown in Table II. Usually a four-pin connector (that mates with an MS3106-14S-2S) is supplied, although MS connectors with fewer pins, or Bendix Pigmy connectors, or pigtails are also available.

SERVOAMPLIFIER The servovalve responds to input current, so a servoamplifier that has high internal impedance (as obtained with current feedback) should be used. This will reduce the effects of coil inductance and will minimize changes due to coil resistance variations.

QUIESCENT CURRENT If used, it is recommended that quiescent current not exceed 100% rated current.

**DITHER** A small amplitude dither signal may be used to improve system performance. If used it is recommended that dither frequency be 200 to 400 Hz and less than 20% rated current amplitude.

**COIL IMPEDANCE** The resistance and inductance of standard coils are given in Table I. The two coils in each servovalve are wound for equal turns with a normal production tolerance on coil resistance of  $\pm 12\%$ . Copper magnet wire is used, so the coil resistance will vary significantly with temperature. The effects of coil resistance changes can be essentially eliminated through use of a current feedback servoamplifier having high output impedance.

Inductance is determined under pressurized operating conditions and is greatly influenced by back emf's of the torque motor. These effects vary with most operating conditions, and vary greatly with signal frequencies above 100 Hz. The apparent coil inductance values given are determined at 50 Hz. If the valve coils are connected in series, mutual inductance will cause the total inductance to be approximately three times the inductance per coil.

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