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THE AXISYMMETRIC INSTABILITY OF A SELF-PINCHED BEAM WITH A ROUNDED RADIAL DENSITY PROFILE

BY H. C. CHEN, H. S. UHM

RESEARCH AND TECHNOLOGY DEPARTMENT

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The plasma return current significantly modifies the growth rate of the instability such that the ratio of plasma to beam current $(-I_p/I_b = f R_p^2/R_b^2)$ largely determines the stability character of the beam. Furthermore, for the same fractional current neutralization f, the modes are highly unstable for smaller ratio of plasma to beam radius R_p/R_b . As comparing to the resistive hose instability, the growth rates for hollowing mode could be larger than

those of hose mode, while the sausage mode is much stabler than the hose mode. Stability properties are illustrated in detail for various system parameters.



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FOREWORD

The axisymmetric perturbations (sausage and hollowing modes) of an intense relativistic self-pinched electron beam propagating in a resistive plasma background are studied, especially for a beam with rounded radial density profile. The Bennett profiles are assumed for both the equilibrium beam current $J_b(r) = J_b(0) (1 + r^2/R_b^2)^{-2}$ and plasma return current $J_p(r) = -f J_b(0) (1 + r^2/R_p^2)^{-2}$, where R_b and R_p are the characteristic radii of the beam and plasma return currents respectively. It is further assumed that the electric conductivity $\sigma(r)$ of the plasma channel is proportional to the return current. For a paraxial electron beam with complete space-charge neutralization by the ambient plasma, the axisymmetric modes can be destabilized by the phase lag between the magnetic field and beam current, even without the plasma return current.

The plasma return current significantly modifies the growth rate of the instability such that the ratio of plasma to beam current $(-I_p/I_b = f R_p^2/R_b^2)$ largely determines the stability character of the beam. Furthermore, for the same fractional current neutralization f, the modes are highly unstable for smaller ratio of plasma to beam radius R_p/R_b . As comparing to the resistive hose instability, the growth rates for hollowing mode could be larger than those of hose mode, while the sausage mode is much stabler than the hose mode. Stability properties are illustrated in detail for various system parameters.

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I. Introduction

There has been considerable interest in recent years in the propagation of high-energy self-pinched relativistic electron beam in the highly resistive plasma medium. Naturally, the equilibrium and stability properties of the electron beam become one of the important subjects under investigation. The resistive hose instability appears to be the most serious magnetohydrodynamic instability for a beam in a resistive plasma channel and has been studied extensively by many authors.¹⁻³ Nevertheless, the axisymmetric oscillations could expell the beam from its channel and plague early beam propagation.⁴ It is the purpose of this paper to examine the importance of the axisymmetric modes in comparison with the hose mode. The axisymmetric perturbations of an intense self-pinched relativistic electron beam propagating in the plasma background have been studied previously by many workers both analytically^{5,6} and numerically.^{7,8} Recently Uhm and Lampe developed a self-consistent theory^{1,9} to derive the dispersion relation for a flat-topped radial density profile electron beam. This paper is an improved version of the previous study, including the influence of the rounded beam density profile on the axisymmetric modes. It has been understood that the flat-topped electron beam has the feature of unbounded linear growth rate for axisymmetric oscillations because all the beam electrons are assumed to have the same natural oscillation frequency which resonants with the wave. As we know in the real world, the beam contains electrons of all energies from the smallest up to the maximum possible energy which is equal to the kinetic energy of the accelerated electron. The electrons at different energy level oscillates with different frequencies and radii, thus the unharmonic beam electrons at different radial position exhibit different betatron frequency and resonant locally with the waves. Electrons with an excess of energy will move with

a greater radius and electrons with less energy oscillates around smaller radius. Therefore, each electron automatically chooses the appropriate phase necessary for their interaction with perturbed waves. This phase mixing is a damping mochanism for oscillation which prevents perturbation from growing to infinity.

From the thermal equilibrium calculations of the intense relativistic electron beam, it was found that the radial density profile for a nonrotating electron beam has the familiar Bennett equilibrium as derived originally by Bennett.¹⁰ For the choice of the thermal distribution function, the beam temperature profile and the axial velocity profile are uniform in the radial direction.¹¹ For the matter of practical interest, we assume the beam flow is paraxial, such that all the beam particles have nearly the same axial velocity, and the transverse energy is much smaller than that in the axial direction. For the type of beam we consider here, the equilibrium beam current can very well be represented by the Bennett profile

$$J_{b}(\mathbf{r}) = J_{b}(0)/(1 + r^{2}/R_{b}^{2})^{2}$$
(1)

where $R_{\rm h}$ is the characteristic beam radius.

The resistive plasma background responds the beam current with a plasma return current which strongly influences the stability behavior of the beam. A small transverse displacement of the beam can separate the beam from the return current which eventually causes the instability. For simplicity we assume the plasma background supplies enough ions to neutralize the beam electrons completely. Although the radial profile of the return current is determined by the electrical conductivity $\sigma(r)$ which relies heavily on the properties of the ambient plasma and experimental condition, for the time

being, it is assumed throughout this paper that the equilibrium plasma return current $J_p(r)$ and electrical conductivity $\sigma(r)$ have also the Bennett profile like

$$J_{p}(r) = -f J_{b}(0)/(1 + r^{2}/R_{p}^{2})^{2}$$
(2)

and

$$\sigma(\mathbf{r}) = \sigma(0) / (1 + r^2 / R_p^2)^2$$
(3)

where the characteristic beam radius R_p can be greater or smaller than R_b depending on the nature of the background plasma such as the ambient pressure and other physical properties. f is the ratio of beam current to plasma current at the beam axis

$$f = -J_{p}(0)/J_{b}(0)$$
 (4)

If the above mentioned equilibrium current configurations are used, then the effective current neutralization would be determined by the ratio of plasma to beam current which has the value

$$f_{eff} \equiv -I_p / I_b = f R_p^2 / R_b^2$$
(5)

The influence of the steady return current on the axisymmetric perturbations depends largely on the extent of plasma current profile overlapped with the beam current. By varying R_b and R_p , the effective current neutralization not only denotes the measure of roundness of the beam but also represents the degree of

overlap between beam and plasma current profiles. It is an important parameter used later to describe the effect of the current profiles on the instability.

In the sections which follow, the equilibrium properties of a self-pinched electron beam with a steady plasma return current are discussed in Section II, the necessary condition for radial confinement of the electron beam is anined. The standard linearized Vlasov-Maxwell treatments are summarized in Sec TIII. An integro-differential eigenvalue equation is obtained for the general ··~ded beam case, making use of the energy group model. The most important source term, namely the perturbed beam current for the rounded beam is also derived. For the purpose of comparison to the previous results, an integral form of an approximate dispersion relation is obtained for the general rounded beam. For the special case where the electrical conductivity, the beam and plasma return currents all have the Bennett profile, numerical results are obtained for various system parameters such as f, $R_{\rm p}$ and $R_{\rm b}$. Stability properties for the sausage and hollowing modes are illustrated and discussed in great detail. Finally, the growth rates of the axisymmetric modes are compared to those of the hose instability and the conclusions are drawn in Section IV.

II. Equilibrium state

Let us consider the steady state of an infinitely long intense relativistic self-pinched electron beam propagating in a resistive background plasma. The beam dynamic properties are described by the Vlasov-Maxwell Theory. In the following analysis, the cylindrical polar coordinates (r, θ, z) are used with the z-axis along the axis of symmetry. In steady state $(\partial/\partial t = 0)$ all the beam equilibrium quantities are assumed to be azimuthally symmetric $(\partial/\partial \theta = 0)$ and infinitely long and uniform in the axial direction $(\partial/\partial z = 0)$. The beam with net current I is assumed to satisfy the following relationship¹²

$$I/I_{2} = v/\gamma = I/17000 \beta \gamma <<1$$
 (6)

where v is Budker's parameter representing the number of electrons per classical electron radius length of the beam, $V_b = \beta c$ is the characteristic beam electron axial velocity, γ is the relativistic factor of the beam particle and I_a is the Alfven-Lawson limiting current. The beam electrons motion can be taken to be paraxial ($P_z^2 >> P_r^2 + p_{\theta}^2$) where P_i denotes the three components of the canonical angular momentum in i direction respectively. The axial velocity is very large compared to the transverse velocity and is considered to be a constant. In this regime, the equilibrium properties of an electron beam can be described by a velocity distribution function of the form

$$\mathbf{f}_{\mathbf{b}} = \mathbf{F} \left(\mathbf{H} - \gamma_{\mathbf{0}} \mathbf{mc}^2 \right) \delta \left(\mathbf{P}_{\mathbf{z}} - \mathbf{P}_{\mathbf{b}} \right)$$
(7)

where H is the total energy, P_z is the axial canonical momentum. The single

particle constants of motions in the equilibrium fields are given by

$$H = (m^{2}c^{4} + c^{2}p^{2})^{\frac{1}{2}}$$

$$P_{7} = p_{7} - e A_{7} (r)/c$$

where $\gamma_b \equiv (1 - \beta^2)^{-l_2}$ and $\beta \equiv v_b/c$ are the standard relativistic quantities, m and v_b are the rest mass and the velocity of the beam electron, c is the velocity of light in vacuum, γ_0 and P_b are constants, $A_z(r)$ is the axial component of vector potential for the equilibrium azimuthal self-magnetic field. There is no externally applied magnetic field in the self-pinched beam case so that $P_{\theta} = 0$. As a result, we can assume that f_b is not a function of P_{θ} as shown in (7). For the nonrotating beam, the vector potential A (r) has only the axial component $A_z(r)$ which can be determined self-consistently from the z component of the Ampere's law

$$\frac{1}{r}\frac{\partial}{\partial r}(rB_{e}) = -4\pi e\beta \left[n_{b}(r) - n_{p}(r)\right]$$
(8)

where $n_b(r)$ is the radial number density distribution of the electron beam, $n_p(r)$ is not the actual number density but related to the plasma return current by $J_p(r) = -e\beta c n_p(r)$. and by definition

$$B_{\theta} = -\partial A_{z}(r) / \partial r$$
(9)

where in deriving Eq. (8) the paraxial beam approximation has been used. All the electrons have the same axial velocity $V_z = \beta c$ and the transverse velocity of the beam electron is small compared with the axial velocity. Eq. (8) can

be used to calculate equilibrium azimuthal self-magnetic field self-consistently for any net current in the system. The relationship can be further related to the squared betatron frequency as

$$= (4\pi e^2 \beta^2 / \gamma_b m r^2) \int_0^r d\vec{r} \cdot \vec{r} \left[n_b(\vec{r}) - n_p(\vec{r}) \right]$$
(10)

where $\underset{\beta}{\omega}$ is the usual betatron frequency which characterizes the electron oscillations.

If the beam and plasma return currents have the assumed Bennett profile as in Eqs. (1) and (2), then Eq. (10) gives the value after integration

$$\omega_{\beta}^{2}(\mathbf{r}) = 0.5 \omega_{pb}^{2} \beta_{b}^{2} \left[1/(1+r^{2}/R_{b}^{2}) - f/(1+r^{2}/R_{p}^{2}) \right]$$
(11)

where $\omega_{pb} \equiv (4\pi n_b(0)e^2/\gamma_b m)^{\frac{1}{2}}$ is the beam plasma frequency at axis. It is important to point out that ω_{β} is a function of r except in the special case of a flat-topped beam which has the constant value; i.e.,

$$\omega_{\beta}^{2} = 0.5 \ \omega_{pb}^{2} \beta_{b}^{2} \ (1-f)$$
(12)

This is the most important distinction between the rounded and flat-topped beams, which gives, by no surprise, two complete different pictures in the linear perturbation analysis. In short, the growth rate for axisymmetric perturbations goes to infinity as $\Omega \neq \omega_{\beta}$ for the flat-topped beam, because the pinch force is harmonic. All the beam electrons are able to resonate with the wave at the same frequency. On the other hand, because the pinch

force is anharmonic for the rounded beam, the electrons have a wide variety of betatron frequencies which could damp the oscillation by phase mixing mechanism. It could have only radially localized wave-particle resonance, so that the growth rate is finite, which will become more obvious later.

As a matter of fact, if the squared betatron frequency is negative at certain radius r, then the equilibrium fails, and the beam is blown apart. Therefore, the radial confinement for the equilibrium state requires at least $\omega_{\beta}^2(\mathbf{r}) > 0$ for any radius r inside the beam. This assures that the magnetic focussing force is pinching the beam; otherwise, the beam will be hollowing out and eventually will become an annular beam. Since we have assumed in the beginning that the equilibrium beam current has the Bennett profile, the minimum requirement for such equilibrium profile to exist needs $\omega_{\beta}^2(\mathbf{r}) > 0$, which leads to

$$f < (1 + r^2/R_p^2)/(1 + r^2/R_b^2)$$
 (13)

For the case of $R_b > R_p$, the fractional current neutralization f is bounded by

$$f < 1$$
 , $R_{p} < R_{b}$, (14)

so that the beam current $J_b(r)$ is peaked on axis. However, if $R_b < R_p$, we obtain from Eq. (13) that

$$f < (R_b/R_p)^2$$
, $R_b < R_p$, (15)

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which is equivalent to $f_{eff} < 1$. Note that in the limit where $R_b = R_p$, both Eqs. (14) and (15) yield the same condition, namely f < 1, which also applies to the flat-topped beam case.

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Next let us consider an electron beam with a "loss-cone" distribution function

$$f_{b} = (n_{b}/2\pi\gamma_{b}m) \delta (H - \gamma_{0}mc^{2}) \delta (P_{z} - P_{b}).$$
(16)

Integration of (16) in the <u>P</u> space, according to definition, leads to a density distribution with flat-topped radial profile

$$n_{b}(r) = \begin{cases} n_{b} & \text{for } 0 \leq r < R_{b} \\ 0 & \text{for } R_{b} < r \end{cases}$$
(17)

where $n_b(r)$ is the equilibrium beam density profile and R_b is defined as the effective beam radius such that the number of electrons per unit length of the beam has

$$N_{b} = 2\pi \int_{0}^{\infty} d\mathbf{r} \, \mathbf{r} \, n_{b}(\mathbf{r}) = \pi \, R_{b}^{2} n_{b}$$
(18)

Note that the beam with flat-topped or Bennett profiles carry essentially the same amount of total current, which is very important when we compare the growth rates in both cases later on.

In the energy group model a beam has been subdivided into groups of particles with the same value of energy. By use of Eq. (7) the beam current

profile can be expressed by definition as

$$J_{b}(\mathbf{r}) = 2\pi\gamma_{b} me\beta c \int_{\phi_{0}}^{\infty} dU F (U + \gamma_{b} mc^{2})$$
(19)

where $U \equiv H - \gamma_b mc^2$ is the effective transverse energy and $\Phi_0(\mathbf{r}) \equiv e\beta A_z(\mathbf{r})$, which appeares in the lower limit of integration, is the minimum possible value of U necessary for an electron at r. Thus, the beam can be considered as a superposition of many components with different transverse energy

$$J_{b}(r) = \int_{0}^{\infty} dU F (U + \gamma_{b} mc^{2}) J_{0}(r, U)$$
(20)

where each component has the equilibrium current density profile like

$$J_{0}(\mathbf{r}, \mathbf{U}) = \begin{cases} -2\pi\gamma_{b} \operatorname{mesc} & \mathbf{r} < \mathbf{R} (\mathbf{U}) \\ 0 & \mathbf{r} > \mathbf{R} (\mathbf{U}) \end{cases}$$
(21)

where R(U) is the maximum radius for an electron with energy U.

III. Stability Analysis

A. Linear Perturbations

In this section, we use the linearized Vlasov-Maxwell equations to investigate the axisymmetric perturbations (m = 0) where m is the azimuthal harmonic number. We follow a normal mode approach by assuming that all the axisymmetric perturbed quantities vary with z and t according to

$$\delta\Phi(\underline{\mathbf{x}},\mathbf{t}) = \delta\Phi(\mathbf{r}) \exp\left[-j(\omega\tau + \Omega z/v_z)\right]$$
(22)

where the oscillating angular frequency ω is assumed to be complex with $Im(\omega) > 0$. The variables τ and Ω are defined by

$$\tau \equiv t - z/v_{\tau}$$

and $\Omega \equiv \omega - kv_{\tau}$.

Where z and t are the axial position and time in the laboratory frame, k is the axial wavenumber. Since all the beam electrons have nearly the same axial velocity for the paraxial beam we consider here, it is more convenient to use z and T as independent variables than the normal use of z and t. Thus Ω is the Doppler-shifted eigenfrequency seen by a beam electron, $V_{\rm b}$ T is a measure of the distance of a particular segment from the head of the beam. If each beam segment is taken to oscillate at a fixed real frequency Ω then the solution for complex ω can be solved mathematically from the dispersion relation. Physically Im(ω) represents the growth rate of the wave as we move backward from the head of the beam.

After Fourier decomposing the Maxwell equations, it is straightforward to show that for the case of long wave length (k $R_b << 1$) and low frequency ($\omega R_b << c$) regime the eigenvalue equation for the perturbed field $\delta\phi$ has the form

$$\frac{1}{r} \frac{\partial}{\partial r} r \frac{\partial}{\partial r} \delta \phi + \frac{4\pi \sigma \omega i}{c^2} \delta \phi = -\frac{4\pi}{c} \delta J_b(r)$$
(23)

where σ is the electrical conductivity of the plasma channel and the Vlasov perturbed beam current contribution $\delta J_{h}(\mathbf{r})$ is defined as

$$\delta J_{b}(\mathbf{r}) = -\mathbf{e} \int v_{z} \, \delta \mathbf{f}_{b}(\mathbf{r}, \underline{p}) \, d\underline{p} \, . \tag{24}$$

where $\delta f_b(r, \underline{p})$ is to be calculated from the integration of the linearized Vlasov equation. According to the energy group model in Eq. (20) one can express the perturbed beam current as

$$\delta J_{b}(\mathbf{r}) = \int_{0}^{\infty} dU F(U + \gamma_{b} mc^{2}) \delta J_{0}(\mathbf{r}, U). \qquad (25)$$

By use of Eq. (19) one can derive the following relationship

$$Fd\Phi_{0}(R)/dR = (1/2\pi\gamma_{h}me\beta c) \partial J_{h}(R)/\partial R$$
(26)

Substituting Eq. (26) into Eq. (25) for change of variables, one can finally write down the perturbed beam current below

$$\delta J_{b}(\mathbf{r}) = (1/2\pi\gamma_{b} \mathrm{me\betac}) \int_{\mathbf{r}}^{\infty} d\mathbf{R} \frac{dJ_{b}(\mathbf{R})}{d\mathbf{R}} \delta J_{0}(\mathbf{r},\mathbf{R})$$
(27)

If the plasma is a perfect conductor with infinite conductivity, all the beam particles which initially lie on a magnetic field line should continue to do so, and when they move the field must in some sense be carried along by the conductor. This is what Alfven¹³ expressed dramatically by saying that the field and fluid were "frozen together". On the contrary, if the plasma resistivity is significant, there is a phase lag between the beam oscillations and the magnetic restoring force. This magnetic decay force prevents the field line from following the beam oscillation which causes the instability to grow. This driving force is well represented by the second term of Eq. (23). The plasma return current influences the structure of the equilibrium beam current and vise versa which will be discussed in a separate paper later on. What we concern here is both currents with different radial profile strongly effect the perturbed beam current which in turn goes to Eq. (23) to determine the perturbed field. This is a major driving force for the axisymmetric perturbations. We will concentrate to derive the most important quantity, namely the perturbed beam current for the rounded beam.

Recall that for the loss-cone distribution as in Eq. (16) the corresponding beam density profile is known to be flat-topped as shown in Eq. (17). To solve the linearized Vlasov equation for the perturbed distribution function $\delta f_b(\underline{x},\underline{p},t)$, one can do the orbit integration along the unperturbed particle orbits, using the method of characteristic. From this standard Vlasov analysis and using a variational approximation method, an approximate dispersion relation can be obtained with the help of the trial eigenfunction of the form

$$\delta \phi_{n}(\mathbf{r}) = \sum_{j=0}^{n} A_{j}(\mathbf{r}/R_{b})^{2j} \qquad 0 \le \mathbf{r} \le R_{b}$$
 (28)

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where n is the radial mode number. We will mainly be interested in the lower order number modes, namely n = 1 and 2 which are believed to be the most important perturbations. For $\bar{n} = 1$ which is identified as sausage mode, the eigenfunction has the simple form

$$\delta \phi_{1}(\mathbf{r}) = \begin{cases} A_{0}(1 - \mathbf{r}^{2}/R_{b}^{2}) & 0 \le \mathbf{r} < R_{b} \\ 0 & R_{b} \le \mathbf{r} \end{cases}$$
(29)

which is a self-consistent solution to Eq. (23). The perturbed beam current density as defined in Eq. (24) can be integrated with the help of eigenfunction (29). This standard procedure but tedious operation gives the final result for the axial component of the perturbed current density like

$$\delta \mathcal{L}_{b}(\mathbf{r}) = \frac{c\beta^{2}}{4\pi} \frac{1}{\mathbf{r}} \frac{\partial}{\partial \mathbf{r}} \left(\mathbf{r} \frac{\omega_{pb}^{2}(\mathbf{r})}{\Omega^{2} - \omega_{B}^{2}} \frac{\partial}{\partial \mathbf{r}} \delta \phi(\mathbf{r}) \right)$$
(30)

as given in Eq. (32) of reference 5, where the plasma frequency $\omega_{pb}(r)$ is defined for the flat-topped beam by

$$\omega_{\rm pb}^2(\mathbf{r}) = \begin{cases} 4\pi n_{\rm b}(0) e^2 / \gamma_{\rm b} m & 0 < \mathbf{r} < R_{\rm b} \\ 0 & R_{\rm b} < \mathbf{r} \end{cases}$$
(31)

Similarly, let us consider next the radial mode number n = 2 which is known as hollowing mode. The name "hollowing" comes because the perturbation can indeed reduce the beam density on axis, leading to a hollow beam profile. The eigenfunction for n = 2 has been given by
$$\delta \phi_2(\mathbf{r}) = \begin{cases} A_0 (1 - 4r^2/R_b^2 + 3r^4/R_b^4) & 0 \le \mathbf{r} \le R_b \\ 0 & R_b < \mathbf{r} \end{cases}$$
(32)

After some tedious algebraic manipulations as demonstrated in reference (5), the z component of the perturbed current density finally becomes

$$\delta J_{b}(\mathbf{r}) = \frac{c\beta^{2}}{4\pi} \frac{1}{\mathbf{r}} \frac{\partial}{\partial \mathbf{r}} \left(\mathbf{r} \frac{\partial \delta \phi}{\partial \mathbf{r}} \frac{\omega_{pb}^{2}(\mathbf{r})}{\Omega^{2} - \omega_{\beta}^{2}} \left(1 + \frac{18 \omega_{\beta}^{2}}{\Omega^{2} - 4\omega_{\beta}^{2}} \right) \right)$$
(33)

Eqs. (30) and (33) display explicitly the intrinsic singularity at $\Omega^2 = \omega_\beta^2$ for wave-particle resonance. Moreover, it is further noticed that the hollowing mode has another singularity at second harmonic betatron frequency too; i.e., $\Omega^2 = 4\omega_\beta^2$. For the same token, one can expect more singularities at higher harmonic frequencies for higher order modes. Since ω_β is single-valued for the flat-topped beam, every electron can be in resonance at the same frequency and there is no limitation for the instability to grow. Therefore, it is almost impossible for a flat-topped beam to propagate in any medium. Fortunately as we shall see later because the beam is rounded, the nature is not going to be so cruel to allow the instability to grow indefinitely.

For the obvious reason, we are going to consider the importance of the influence of rounded radial density profile on axisymmetric perturbations. As we mentioned earlier, the betatron frequency is a function of radius r as long as the beam profile is rounded. It is very common to have energy spread for a high energy beam even right after coming out of the accelerator. In nature, it always represents an oscillation in energy about the equilibrium value. As long as the energy exceeds the equilibrium energy, the electron will travel

in orbit of larger radii, conversely, it will have smaller orbit at lower energy. The electrons reside on each infinitesmal Δr can have approximately constant ω_{β} with which they resonate locally. Therefore, it is quite reasonable to extend from the previous results for the flat-topped beam profile to include the rounded beam profile effect. To investigate the sausage and hollowing modes for the rounded beam, we have to derive first the perturbed beam current and the associated eigenfunction for each mode which are described below separately.

1. Sausage mode (n = 1)

It is evident that a beam with rounded radial density profile can be subdivided into groups of particles with the same value of energy, and in addition, it can also be sliced into components with different radii. As pointed out in Eq. (30), each energy group designated by R gives its perturbed axial current density for the n = 1 sausage mode

$$\delta J_{0}(\mathbf{r},\mathbf{R}) = 2\pi e^{2} c\beta^{2} \frac{1}{\mathbf{r}} \frac{\partial}{\partial \mathbf{r}} \left| \mathbf{r} \frac{\partial \delta \phi}{\partial \mathbf{r}} - \frac{dJ_{b}(\mathbf{R})/d\mathbf{R}}{\Omega^{2} - \omega_{B}^{2}(\mathbf{R})} \right|$$
(34)

where $\delta J_0(r,R)$ should be a continuous function on $0 \leq r \leq R$ and vanish smoothly at r = 0. Substituting Eq. (34) into Eq. (27) for summing up each individual component of the perturbed beam current, we have finally the result for the axial perturbed beam current like

$$\delta J_{b}(r) = \frac{e\beta}{\gamma m} \frac{1}{r} \frac{\partial}{\partial r} \left(r \int_{T}^{\infty} dR \frac{dJ_{b}(R)/dR}{\Omega^{2} - \omega_{\beta}^{2}} \frac{\partial \delta \phi}{\partial r} \right)$$
(35)

The corresponding eigenfunction is given by

$$\delta \phi_1(\mathbf{r}) = \int_{\mathbf{r}}^{\infty} d\mathbf{R} \, A_0 \, (1 - \mathbf{r}^2 / \mathbf{R}^2) \, d\mathbf{J}_b(\mathbf{R}) / d\mathbf{R}$$
(36)

Note that the intrinsic singularity at $\Omega = \omega_{\beta}$ in Eq. (30) for the flat-topped case has been replaced by the integration over R space which eventually gives a logarithmic singularity. Because of this, the growth rate is no longer unbounded as in the flat-topped case. The natural oscillation frequency ω_{β} varies for different electrons at different radius r, so that there is no single frequency Ω for which the entire beam electrons can resonate with the wave.

2. Hollowing mode (n = 2)

Accordingly, after considering the n = 1 sausage mode, likewise we can easily derive, based on the same theory, the perturbed current density and corresponding trial eigenfunction for the n = 2 hollowing mode. By use of Eqs. (32) and (33), one can obtain the perturbed beam current which has the axial component

$$\delta J_{b}(\mathbf{r}) = \frac{e\beta}{\gamma m} \frac{1}{r} \frac{\partial}{\partial r} \left\{ r \int_{\mathbf{r}}^{\infty} d\mathbf{R} \frac{dJ_{b}(\mathbf{R})/d\mathbf{R}}{\Omega^{2} - \omega_{\beta}^{2}} \left(1 + \frac{18\omega_{\beta}^{2}}{\Omega^{2} - 4\omega_{\beta}^{2}}\right) \frac{\partial}{\partial r} \frac{\delta}{\mathbf{r}}^{\frac{1}{2}} \right\}$$
(37)

and the corresponding eigenfunction for n = 2 becomes

$$\delta \phi_2(\mathbf{r}) = \int_{\mathbf{r}}^{\infty} d\mathbf{R} A_0(1 - 4\mathbf{r}^2/\mathbf{R}^2 + 3\mathbf{r}^4/\mathbf{R}^4) dJ_b(\mathbf{R})/d\mathbf{R}$$
(38)

Obviously, if the beam current $J_b(R)$ is a step function, then the above derived results for the rounded beam go back to that for the flat-topped beam case.

B. Dispersion relation

The derived eigenvalue equation (23) along with the perturbed beam current (35) or (37) constitute the main result for axisymmetric perturbations

which can be summarized in the general form

$$\frac{1}{r}\frac{d}{dr}\left[r\frac{d}{dr}\delta\phi(\mathbf{r})\Gamma_{j}(\mathbf{r})\right] + \frac{4\pi}{c^{2}}\sigma(\mathbf{r})\omega i\delta\phi(\mathbf{r}) = 0$$
(39)

where j = 1 or 2 representing sausage and hollowing mode respectively, so that the function $\Gamma_{i}(r)$ are defined by

$$\Gamma_{1}(\mathbf{r}) = 1 + \frac{4\pi e\beta}{\gamma m c} \int_{\mathbf{r}}^{\infty} d\mathbf{R} \frac{dJ_{b}(\mathbf{R})/d\mathbf{R}}{\Omega^{2} - \omega_{\beta}^{2}(\mathbf{R})}$$
(40)

and

$$\Gamma_{2}(\mathbf{r}) = 1 + \frac{4\pi e\beta}{\gamma m c} \int_{\mathbf{r}}^{\infty} d\mathbf{R} \frac{dJ_{b}(\mathbf{R})/d\mathbf{R}}{\Omega^{2} - \omega_{\beta}^{2}(\mathbf{R})} (1 + \frac{18\omega_{\beta}^{2}(\mathbf{R})}{\Omega^{2} - 4\omega_{\beta}^{2}(\mathbf{R})})$$
(41)

It is worth while to point out that the eigenvalue problem represented by Eq. (39) is independent of $\sigma(0)$, $J_b(0)$ and β which enables us to use them as a normalization factor for ω and Ω later in expressing the dispersion relationship. Therefore, the dispersion relation can be expressed quite generally as a functional relationship between $\Omega^2/\omega_{pb}^2\beta^2$ and $\omega\tau_d$ where the magnetic decay time for the perturbed current is defined by $\tau_d \equiv \pi\sigma(0)R_b^2/2c^2$. For any rounded beam, Eq. (39) along with (40) or (41) can be used to investigate the influence of the magnetic decay time and the plasma return current on axisymmetric instabilities.

Ironically, Eq. (39) is a standard eigenvalue problem which can be solved numerically. However, the method we adapted here enables us to

study certain specific cases which exhibit explicitly more physics. The dispersion relation that determines the complex eigenfrequency ω can be obtained easily by multiplying Eq. (39) by r $\delta \phi(\mathbf{r})$ on both sides and integrating over r from 0 to ∞ . This operation gives the following result

$$\int_{0}^{\infty} d\mathbf{r} \mathbf{r} \left[d\delta\phi(\mathbf{r})/d\mathbf{r} \right]^{2} \Gamma_{j}(\mathbf{r}) = \frac{4\pi\omega i}{c^{2}} \int_{0}^{\infty} d\mathbf{r} \mathbf{r} \sigma(\mathbf{r}) \left[\delta\phi(\mathbf{r}) \right]^{2}$$
(42)

The dependence of stability properties on the form of the conductivity profile is of considerable interest. Since the right hand side of Eq. (42) is not a function of Ω , the electrical conductivity σ (r) only serves as a weighted function in determining the value of ω . In other words, the results become free of restriction to beams propagating in a medium with any fixed conductivity profile. For any growing wave, broadening the conductivity channel ($R_p > R_b$) will reduce ω and has a stabilizing effect. A narrow profile for $\sigma(r) = (R_p < R_b)$ can substantially enhance the growth rate. However, the equilibrium conductivity $\sigma(r)$ in reality is a response to beam current and ambient plasma according to experimental condition and must be allowed to change with respect to time and space. We will examine this important property in the near future; Eq. (42) can be solved numerically to determine the stability properties for various system parameters of our interest. However, if the beam current is a step function as in the flat-topped beam case, Eq. (42) could lead to the following analytical results. Substituting Eqs. (36) and (40) into Eq. (42), the dispersion

relation for the m = 1 (sausage mode) becomes the simple form

$$\frac{4}{3} i\omega\tau_{d} = \frac{\Omega^{2} - \omega_{pb}^{2}\beta_{b}^{2}(1 - 2f)}{\Omega^{2} - 2\omega_{pb}^{2}\beta_{b}^{2}(1 - f)}$$
(43)

Similarly, by use of Eqs. (38), (41) and (42), the dispersion relation for the n = 2 (hollowing mode) becomes

$$\frac{4}{15} i\omega\tau_{d} = 1 + \frac{\omega_{pb}^{2}\beta_{b}^{2}}{\Omega^{2} - 2\omega_{pb}^{2}\beta_{b}^{2}(1-f)} \left[1 + \frac{9\omega_{pb}^{2}\beta_{b}^{2}(1-f)}{\Omega^{2} - 8\omega_{pb}^{2}\beta_{b}^{2}(1-f)} \right]$$
(44)

Since the right hand side of Eqs. (43) and (44) are real always, we can expect Re (ω) = 0 all the time. So the instabilities for the flat-topped beam are purely growing modes.

C. Numerical results

In the dispersion relations (42), we fix the real frequency Ω and solve for the complex ω numerically for various system parameters to determine the wave properties. The radial dependence of the equilibrium beam current, steady plasma current and conductivity of plasma channel are all assumed to have the similar Bennett profile, but different radii are allowed in general to express the complexity of the nature. In the following, the sausage and hollowing modes will be investigated separately for various system parameters such as f, R_b and R_p. The dispersion relation will be expressed as a functional relationship between $\Omega^2/\omega_{pb}^2\beta_b^2$ and $\omega\tau_d$. The results between rounded and flat-topped beams will be compared with physical interpretation.

1. Sausage mode (n = 1)

Let us start considering the n = 1 sausage mode in the simplest case where $R_p = R_b$; i.e., the beam and plasma return currents have the same Bennett profiles of equal radii so that $f = J_p(r)/J_b(r)$ is constant everywhere for any radius r. According to Eq. (36), if the beam current $J_b(R)$ has the Bennett profile as expressed in Eq. (1), then $\delta\phi_1(r)$ can be integrated easily to obtain

$$\delta\phi_{1}(\mathbf{r}) = \frac{\mathbf{r}^{2}}{\mathbf{R}_{b}^{2}} \left\{ (1 + \mathbf{R}_{b}^{2}/\mathbf{r}^{2})/2 - \ln(1 + \mathbf{R}_{b}^{2}/\mathbf{r}^{2}) - 0.5/(1 + \mathbf{R}_{b}^{2}/\mathbf{r}^{2}) \right\}$$
(45)

which has the peak value at r = 0 and decreases monotonically + 0 zero at $r = \infty$. Furthermore, the eigenfunction $\partial_{\phi_1}(r)$ and its first derivative with respect to r (i.e., $\partial_{\phi_1}/\partial r$) are independent of Ω and f, so that the LHS of dispersion relation (42) decides the stability criteria (stable or unstable) and the RHS determines the strength of the instability. Using Eqs. (1) and (11), Eq. (40) can be integrated to give the following analytical form

$$\Gamma_{1}(\mathbf{r}) = 1 - \left\{ \frac{1}{1 + \frac{\mathbf{r}^{2}}{R_{b}^{2}} + \frac{\Omega^{2}}{\omega_{pb}^{2}\beta_{b}^{2}(1-f)}} \ln \left[1 - \frac{2(1-f)\omega_{pb}^{2}\beta_{b}^{2}}{(1+\frac{\mathbf{r}^{2}}{R_{b}^{2}})\Omega^{2}} \right] \right\} (1-f)^{-1} \quad (46)$$

Note that $\Gamma_1(\mathbf{r})$ is complex with the definition for the complex logarithm

$$\ln Z \equiv \ln r + i\theta \tag{47}$$

where $z \equiv x + iy$ and $r = (x^2 + y^2)^{1/2}$, $\theta = \tan^{-1}(y/x)$. It becomes apparent that the intrinsic singularity appears in Eq. (30) has been replaced by the logarithmic singularity as explicitly shown in Eq. (46) as we mentioned

before; for any fixed Ω and f, the pole for logarithmic singularity can be located from the limit lim ln(z) which gives $z \rightarrow 0$

$$R_{S}^{2} = R_{b}^{2} \left[\frac{2(1 - f)\omega_{pb}^{2} \beta_{b}^{2}}{\Omega^{2}} - 1 \right]$$
(48)

It is because $\delta \phi_1(\mathbf{r})$ obtained in (45) is a strong monotone decreasing function, with respect to increasing r, the integrant in the LHS of Eq. (42) is almost zero near the logarithmic singularity R_s . In this regard, the perturbation is contributed essentially from the integration interval between 0 and R_s . Otherwise the LHS of Eq. (42) could approach infinity which gives the unbounded growth rate.

The results of solving Eqs. (42) and (43) give the unstable regions as shown in Fig. 1 for different values of f and Ω . The dashed and solid lines are for the flat-topped and rounded beams respectively. As Eq. (43) indicated, the unstable region for the flat-topped beam is bounded by two straight lines in the f - Ω space. The value of f is restricted but taken from -1 to 1 which covers completely the possible magnitude and direction of the plasma return current in our case. The fact is for a single pulse electron beam, the plasma return current is known to be flowing in the direction opposite to the beam current. However, the situation is not always so simple. For example, as in the case where the beam is a continuous pulse train, the intermission between the pulse can cause the plasma return current going in the opposite direction before the second pulse arrives. Anyway, the unstable region for the rounded beam has been greatly reduced towards smaller Ω in the upper half of f space. It is interesting to observe that the instability exists even when $\Omega = 0$ for both beams. For $\Omega = 0$, Eq. (46) can be simplified to give

$$\Gamma_{1}(\mathbf{r}) = 1 - (1 + \mathbf{r}^{2}/R_{b}^{2})^{-1} (1 - \mathbf{f})^{-1}$$
(49)

The real frequency $\operatorname{Re}(\omega) = 0$ for the rounded beam also indicating that the perturbations are purely growing modes, which can only be driven unstable by certain amount of plasma return current, i.e., $f \neq 0$. As f increases, the rounded beam becomes unstable first at f = 0.2 approximately while the flattopped beam remains stable until about f = 0.5. The growth rates $\operatorname{Im}(\omega\tau_d)$ for both beams are plotted against f in Figure 2 when $\Omega = 0$. The growth rates are approaching infinity in the limit of f = 1 as one can expect. Because the plasma return current cancels the beam current completely and the self-magnetic pinched force no longer exists.

If $\Omega \neq 0$, the growth rates versus Ω^2 for the flat-topped beam are shown in Figure 3 for various values of fractional current neutralization f. The growth rates could go to infinity no matter what value of f is chosen because of the singularities which appear explicitly in Eq. (43). Again, the results of $\text{Re}(\omega)$ are always zero indicating that the perturbation are purely growing modes. As to the results for rounded beam, the $\text{Im}(\omega\tau_d)$ and $\text{Re}(\omega\tau_d)$ for various f are shown versus Ω^2 in Figure 4(a) and (b) respectively. The growth rate is very small when f = 0 where the sausage mode is driven by magnetic decay force alone. For larger f, the growth rate increases dramatically which indicates the strong influence of the plasma return current on the instability. In comparison, the rounded beam does not have the feature of unbounded linear growth rate as in the case for the flat-topped beam. This is an important quantity for the rounded beam which is in favor of the beam propagation. As we know, if the beam is rounded, then the betatron frequency for each electron is not unique. A wave with a given real frequency Ω is resonant with portion of the beam electrons only, but not

all of them, and the resonant electrons tend to be localized in particular radial ranges of the beam; the oscillation frequency $\text{Re}(\omega)$ as shown in Figure 4(b) increases linearly with respect to Ω^2 . The reason of being that is very simple. As one can see in Eq. (42) the $\text{Re}(\omega)$ comes from $\text{Im}(\Gamma_1(\mathbf{r}))$, and the imaginary part of $\Gamma_1(\mathbf{r})$ is contributed only from the pole at $\Omega = \omega_\beta$ according to Eq. (40) if the path of integration is chosen along the Re(R) axis. By Cauchy's theorem a contour can be deformed without crossing the singularity and then applying the theorem of residues for evaluating the definite integral in Eq. (40), which gives eventually the same unique value of πi . More specifically, the last term in Eq. (46) has a logarithmic singularity from which a value of πi is obtained according to Eq. (47). Clearly, the term is linearly proportional to Ω^2 .

The electrical conductivity of the plasma channel is a rather complicated quantity characterized by a radial profile $\sigma(\mathbf{r})$ which determines the radial distribution of the plasma return current. For simplicity, the electrical conductivity $\sigma(\mathbf{r})$ and the plasma return current $J_p(\mathbf{r})$ are assumed to be steady and have the Bennett profiles of equal radii; usually the plasma return current flows at larger radius than the beam current at lower pressure because electric breakdown considerably spreads the conductivity channel. On the contrary, the higher pressure forces the plasma return current concentrating towards the beam axis. Therefore, without loss of generality, it is our interest to consider these two extreme cases where $R_p \neq R_b$, i.e., the plasma return current $J_p(\mathbf{r})$ and beam current $J_b(\mathbf{r})$ have the same Bennett profiles but different radii. When we do this, it is important to remember that the

restriction on fractional current neutralization f as shown in Eq. (13) has to be enforced so that the equilibrium beam profile may exist. Furthermore, under the condition of $R_p \neq R_b$, it is more convenient to use the effective current neutralization f_{eff} as defined in Eq. (5) instead of f.

First, let us consider the case of $R_n > R_b$. Figure (5) demonstrates the change of unstable region in the Ω - f_{eff} space due to different ratio of R_{p}/R_{b} . As $f_{eff} = 0$, the unstable regions in Ω domain are identical because there is no plasma return current so that the ratio of $R_{\rm p}/R_{\rm b}$ is irrelevant. The electrical conductivity $\sigma(r)$ serves as a weighting function in determining the growth rate of instability. For $f_{eff} \neq 0$, the instability growth region shrinks in the Ω space but extends towards higher negative \mathbf{f}_{eff} region as the ratio of R_p/R_b increases. If $f_{eff} < 0$, the expanded plasma return current flows in the same direction as the beam current does, which is contrary to the concept used in the center-core transmission line where both currents flow in the directions opposite to each other. No wonder it is more unstable for larger ratio of R_p/R_b ; as far as the growth rate is concerned, Figure (6) shows the solution (ωt_d) versus Ω^2 for various f_{eff} when $R_p = 2 R_b$. The growth rates $Im(\omega \tau_d)$ increases as f_{eff} increases. Obviously, the growth rates and the magnetic decay force $\text{Re}(\omega\tau_d)$ are smaller when comparing to those in Figure (4) where $R_p = R_b$, which indicates that the increase of plasma current radius aids stability for $f_{eff} > 1$.

Now let us consider the other extreme case where $R_p < R_b$, the results for the unstable regions in $\Omega - f_{eff}$ space are shown in Figure (7) for different ratio of R_p/R_b . The current neutralization f or effective current neutralization f_{eff} has to be restricted according to Eq. (14) as a minimum requirement for the radial confinement of the Bennett

beam. As a result, there is a forbidden region for each case in Figure (7) which fulfills the inequality $f_{eff} < (R_p/R_b)^2$ in f_{eff} domain; e.g., $f_{eff} > .25$ when $R_p = 0.5 R_b$.

As the plasma channel is narrower than the beam current, the unstable region increases in Ω space for $f_{eff} > 0$ but remains very stable for $f_{eff} < 0$. As $f_{eff} < 0$, the self-magnetic pinched force has been enhanced somewhat by the plasma return current which flows in the same direction as the beam current so that the beam is very stable. The growth rates for $R_p = 0.5 R_b$ are shown in Figure (8) versus Ω^2 for different f_{eff} . The value of f_{eff} is chosen only from 0 to 0.2 which corresponds that f increases from 0 to 0.8 because of the restriction of Eq. (14). The growth rate can be very large even for small value of f_{eff} . Finally, let us summarize the sausage mode calculations by presenting the criteria for non-oscillatory growth region in the $f_{eff} - R_p/R_b$ space which is shown in Figure (9). It is a purely growing mode where $\Omega = 0$ and $Re(\omega) = 0$. As one can see, the sausage mode of this kind can only be excited when $f_{eff} > 0$.

2. Hollowing mode

Next to the sausage mode, we want to consider and therefore do the similar calculations for the hollowing mode (n = 2). For the simplest case where $R_p = R_b$, the eigenfunction (38) has the form after integration

$$\delta\phi_2(r) = \delta\phi_1(r) - 1.5(r/R_b)^4 \left\{ 0.75 + 0.25 x^2 - 1.5 x + 1.5 \ln x + 0.5/x \right\}$$
(50)

where $\delta \phi_1(\mathbf{r})$ is equivalent to that shown in Eq. (45) and $X \equiv 1 + R_b^2/r^2$ for simplification. $\delta \phi_2(\mathbf{r})$ is also a monotone decreasing function which vanishes as $\mathbf{r} \neq \infty$. Likewise the expression for $\Gamma_2(\mathbf{r})$ in Eq. (41) can be integrated to give

$$\Gamma_{2}(\mathbf{r}) = \Gamma_{1}(\mathbf{r}) + \frac{9}{4} \frac{\Omega^{2}}{\omega_{pb}^{2}\beta_{b}^{2}(1-\mathbf{f})^{2}} \left\{ \frac{\omega_{pb}^{2}\beta_{b}^{2}(1-\mathbf{f})}{2\Omega^{2}} - \frac{5}{16} \ln x \right\}$$

+
$$\frac{1}{3}$$
 ln $\left[X - \frac{2\omega_{pb}^{2}\beta_{b}^{2}(1-f)}{\Omega^{2}} \right] - \frac{1}{48} \ln \left[X - \frac{8\omega_{pb}^{2}\beta_{b}^{2}(1-f)}{\Omega^{2}} \right] \right\}$ (51)

where $\Gamma_1(r)$ denotes the same expression as in Eq. (46) and $X = 1 + (R_p/r)^2$ also for simplification. As one can see in Eq. (51), the last two terms contain two logarithmic singularities which have been formed due to the two intrinsic singularities in Eq. (41). Substituting Eqs. (50) and (51) into Eq. (42), we solve the dispersion relation numerically for various system parameters. The results for the unstable regions in the Ω - f space are illustrated in Fig. (10) for the flat-topped (dashed line) and rounded beam (solid line) respectively. Note that the unstable region for the flat-topped beam is greatly reduced by the influence of the rounded beam profile. From Eq. (44) the growth rates for the flat-topped beam can be obtained easily and shown in Fig. (11) for various value of current neutralization f. Correspondingly, the $Im(\omega\tau_d)$ and $Re(\omega\tau_d)$ for the rounded beam are plotted against Ω^2 for various f in Fig. (12). As one can immediately see, the unbounded linear growth rates of the flat-topped beam are replaced by the finite growth rates of the rounded beam. For the rounded beam, both $I_{m}(\omega\tau_{d})$ and $\text{Re}(\omega\tau_d)$ increases as f increases. Note that the growth rate is very large even when f = 0, the hollowing mode is driven unstable by the magnetic
decay force along. It is further noticed that the peaks of the growth rates can be found near the dashed line as shown in Fig. (10) where the growth rates for the flat-topped beam become infinity.

Now, we are ready to make a comparison between the sausage and hollowing mode perturbations for the rounded beam. The growth rates as shown in Fig. (12) for the hollowing mode are generally larger than that of the sausage mode in Fig. (4). Fow example, when f = 0, the growth rate for the hollowing mode is at least an order of 2 larger than the n = 1 sausage mode. It concludes that the magnetic decay force plays an important role in exciting the hollowing mode. As f increases, the ratio of the growth rate between the two modes reduces gradually but still remains a factor of 10 approximately when f = 0.8. As f < 0, the plasma return current has the stabilizing effect on both modes, because it introduces additional self-magnetic pinched force for the beam. The sausage modes are very stable but not for the hollowing modes because the growth rates are very large even when f = 0, it certainly needs more plasma return current flowing in the same direction to stabilize the beam. Generally speaking, because of the huge growth rate of the hollowing mode, it seems unlikely to have any sausage mode oscillations or enough time for them to grow before the hollowing mode totally destroys the beam. Now, if one looks closely in Figs. (4) and (12) again, one can find another big difference between the results for the sausage and hollowing modes. Namely the maximum growth rate for various f occurs near small value of Ω for the sausage mode but span to very large values of Ω except for those with high current neutralization for the hollowing mode. Recall that the perturbation we are interested is in the low frequency regime. The theory derived here is not necessarily correct for high frequency perturbation. The beam electrons at various energy level oscillate with various betatron frequency at different radius. From Eq. (11), the betatron frequency $\omega_{\beta}(\mathbf{r})$ has the maximum value $\omega_{\beta}(0)$ at the beam axis and

decreases outwards outwards radially. Because of the natural oscillation of the electrons, it is likely that the waves are excited primarily in the frequency range of $0 < \Omega < \omega_{o}(0)$. In this respect, although the growth rates of the hollowing mode are very large in general, one has to be very careful about the location of Ω where the peaks of growth rates occur. One could argue that it is almost impossible to have waves excited with very large frequency Ω (e.g. $\Omega > \omega_{\rho}(0)$) unless the perturbation is imposed externally. In Fig. (12) the maximum growth rate occurs near the region where $\Omega > \omega_{\beta}(0)$ which is not likely to happen in the nature. Nevertheless, the maximum growth rate for f > 0.5 can be found in the region of Ω satisfying $\Omega < \omega_g(0)$. It indicates the possible excitation of the hollowing mode naturally when the current neutralization is high. There has been some evidence from numerical simulation results.⁸ For example, there is no sausage mode oscillation which has even been observed experimentally for a self-pinched electron beam propagating in the plasma. In addition, numerical simulation has indicated that the electron beam becomes hollow if the current neutralization exceeds 0.5 or so.

It is straight forward to extend the calculation of hollowing mode to consider the case where $R_p \neq R_b$, namely the beam and plasma return currents have the similar Bennett profiles but unequal radii. First, for the case $R_p > R_b$, Fig. (13) illustrates the various growth regions in the $\Omega - f_{eff}$ space for different ratio of R_p/R_b . The beam seems more stable as the ratio R_p/R_b increases, because the unstable region in Ω space have been greatly reduced and concentrated towards higher Ω domain. The growth rates versus Ω^2 for $R_p = 2R_b$ are shown in Fig. (14) for various f_{eff} . One can see clearly that the growth rates are not a strong function of f_{eff} any more. The reason is very simple, the hollowing mode perturbation is highly unstable at f = 0 where the instability is driven simply by the magnetic decay force.

The plasma return current tries to change the situation. However, under the condition of $R_{p} > R_{b}$, the amount of plasma return current overlapped with the beam remains almost unchanged even for very large ratio of R_p/R_b . On the other hand, for the second case where $R_{p} < R_{b}$, the unstable region for the hollowing mode perturbation as shown in Fig. (15) expands very much in Ω space as the ratio of R_p/R_b decreases first (e.g., $R_p = 0.5 R_b$), but shrinks back for further decrease of R_p/R_b , a forbidden region in the feff domain is drawn in Fig. (15) where the equilibrium Bennett beam fails to exist. The growth rates for $R_p = 0.5 R_b$ are plotted in Fig. (16) against Ω^2 for various f_{eff}. It is very clear that as f_{eff} increases the growth rate increases and can go to infinity (e.g., $f_{eff} > 0.15$ or f > 0.6equivalently). For higher f_{eff} , this is a very unstable situation for the beam because of the hollowing mode oscillations. Once the self-magnetic pinched force is reduced near the axis by the presence of the plasma return current, it is not difficult to understand why the beam electrons on the beam axis can easily be expelled by the highly concentrating return current. As long as the hollowing mode exists, the beam is going to become annular eventually and expand continuously.

IV. Conclusions

The equilibrium and stability of an intense relativistic self-pinched electron beam propagating in a resistive plasma channel has been studied by the Vlasov-Maxwell Theory. For the thermal equilibrium distribution function, the steady and equilibrium electron beam without plasma return current has the familiar Bennett radial density profile. When the plasma return current is unavoidable in the system, the minimum requirement for the radial confinement of the electron beam has been derived to restrict the degree of current neutralization. An analytical theory of the axisymmetric perturbations including the sausage (n = 1) and hollowing (n = 2) modes has been derived for an electron beam with rounded radial current profile. Complete space-charge neutralization.

In this paper, we have considered in particular a wave with real frequency Ω and Im(ω) > 0 which has a certain wave amplitude at the beam head and grows spatially backward along the beam. It is essentially a convective instability. A numerical calculation has been made for the special case where the equilibrium radial distribution of the beam and plasma return current, as well as electrical conductivity of the plasma channel, have similar Bennett profiles but different radii is also allowed. The results for axisymmetric perturbations have shown that the important system parameters such as the effective current neutralization, the radial profile of electrical conductivity of plasma channel, beam and plasma return current are very sensitive in determining the stability behavior of an electron beam. First, the results for the rounded beam have been compared to that of the flat-topped beam. Generally speaking, there is no linear bound on wave growth for the flat-topped beam. For the rounded beam, the finite growth rates for the hollowing mode are much larger than that of the sausage

mode. In practice, it has been concluded that the naturally excited hollowing mode oscillation is more likely to happen when the current neutralization exceeds about 0.5.

It has been shown from the calculations the high-frequency hollowing mode perturbations (i.e., $\Omega^2/\omega_{pb}^2 \beta_b^2 \approx 2$) can be driven unstable by the magnetic decay force alone where the phase lag between the transverse displacement of the beam and the magnetic field drives the instability. The naturally occurring plasma return current can flow either in the same or in the opposite direction as that of the beam current. The one flows in the same direction introduces additional self-magnetic pinched force which intends to stabilize the beam. On the contrary, the one in the opposite direction reduces the pinched force and thus enhances the perturbations. As $R_p < R_b$ where a narrow conducting channel confines the plasma return current, the highly concentrating return current on beam axis is very dangerous for hollowing and destroying the beam.

Finally, it is of importance to compare the growth rates of the axisymmetric modes to those of the hose instability. Generally, the growth rates for the sausage mode are much smaller than that of the hose modes as obtained from Figure 5 of Reference 2. This may well explain why the sausage mode oscillation has not been found experimentally or in numerical simulation. It is simply because of the domination of the hose mode, the beam could be expelled from its channel even before the sausage mode starts to grow. However, the maximum growth rates for the hollowing mode are larger in most cases or at least comparable to those of the hose mode which addresses very clearly the importance of the hollowing mode oscillation in the beam propagation.

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FIGURE 3. THE GROWTH RATE OF THE SAUSAGE MODE VERSUS Ω^2 FOR VARIOUS f FOR THE FLAT-TOPPED BEAM

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FIGURE 5. THE UNSTABLE REGION OF THE SAUSAGE MODE OF THE BENNETT BEAM IN THE $f_{eff} = \Omega$.SPACE FOR $R_p/R_b \neq 2$, 4, 6 RESPECTIVELY



FIGURE 6. GROWTH RATE Im(ω) AND REAL EIGENFREQUENCY R_e(ω) VERSUS Ω^2 FOR THE SAUSAGE MODE OF A BENNETT BEAM WITH R_p = 2 R_b FOR VARIOUS f_{eff}



FIGURE 7. THE UNSTABLE REGION OF THE SAUSAGE MODE OF THE BENNETT BEAM IN THE $f_{eff} - \Omega$ SPACE FOR $R_p/R_b \neq 0.9$, 0.5, AND 0.1, RESPECTIVELY



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FIGURE 8. GROWTH RATE Im(ω) AND REAL EIGENFREQUENCY R_e (ω) VERSUS Ω^2 FOR THE SAUSAGE MODE OF A BENNETT BEAM WITH R_p = 0.5 R_b FOR VARIOUS f_{eff}











FIGURE 11. THE GROWTH RATE OF THE HOLLOWING MODE VERSUS Ω^{2} FOR VARIOUS f FOR THE FLAT-TOPPED BEAM

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FIGURE 12. GROWTH RATE Im(ω) AND REAL EIGENFREQUENCY R_B(ω) VERSUS Ω^2 FOR THE HOLLOWING MODE OF A BENNETT BEAM WITH R_p = R_b FOR VARIOUS f

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FIGURE 13. THE UNSTABLE REGION OF THE HOLLOWING MODE OF THE BENNETT BEAM IN THE $f_{eff} - \Omega$ SPACE FOR R_p/R_b = 1.1, 2, 4, RESPECTIVELY





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FIGURE 15. THE UNSTABLE REGION OF THE HOLLOWING MODE OF THE BENNETT BEAM IN THE $f_{eff} - \Omega$ SPACE FOR R_p/R_b = 0.9, 0.5, 0.1, RESPECTIVELY





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