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INDEPENDENT VARIABLES(U) IOWA UNIV IOWA CITY DEPT OF
STATISTICS AND ACTUARIAL SCIENCE G BRIL ET AL. JUL 82
TR-86 N00014-80-C-0321

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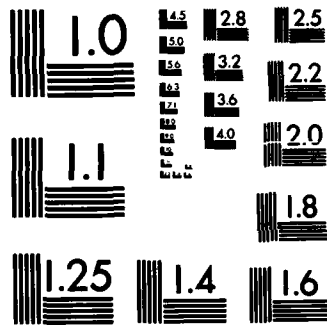
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A FORTRAN PROGRAM FOR ISOTONIC REGRESSION
IN TWO INDEPENDENT VARIABLES

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Technical Report No. 86

July, 1982

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This work was supported by ONR Contract N00014-80-C-0321.

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to program often lead to excessive computation time. Dykstra and Robertson (1982) give an algorithm for computing the least squares regression function which is increasing in each of several variables. This algorithm uses successive one-dimensional smoothings and is very efficient, relative to other available algorithms. A Fortran IV program to implement this algorithm for two independent variables is given below.

STRUCTURE

SUBROUTINE SMOOTH (NROW, NCOL, X, W, NCYCLE, G, ICYCLE, IFAULT)

Formal Parameters

NROW	Integer	input: the number of rows
NCOL	Integer	input: the number of columns
X	Real Array (NROW,NCOL)	input: the original values
W	Real Array (NROW,NCOL)	input: the original weights, all zero or positive
NCYCLE	Integer	input: the maximum number of cycles if the array does not converge
GCHECK	Real Array (NROW,NCOL)	workspace
WT	Real Array (NROW,NCOL)	workspace
G	Real Array (NROW,NCOL)	output: the smoothed values if con- vergence was attained, or the values after the maximum number of iterations
ICYCLE	Integer	output: the actual number of cycles the smoothing process required

IFault Integer output: a fault indicator, equal to

- 1 if convergence was not attained in the specified number of cycles
- 2 if any element of W is negative
- 3 if rows and/or columns exceed 20
- 4 if a zero weight was replaced by 0.00001
- 0 otherwise

Auxiliary Algorithm

SMOOTH uses the subroutine PAV (K,X,IORDER,W,FINALX) to apply the pool adjacent violators algorithm for the isotonic regression on rows and columns.

Constants

The constant EPS is used to determine if convergence has been attained. If each entry of the array after the current smoothing does not differ from the corresponding entry from the previous smoothing by more than EPS, the array is considered to be smoothed.

Restrictions

The X and W arrays cannot have more than 20 rows and/or columns. However, if one wished to smooth a larger array, the changes to the subroutine would be minimal.

The W array cannot contain any negative values. If zero values are encountered, they are replaced by 10^{-5} for the amalgamation.

Time and Accuracy

For the 9×9 array in Table 4 in Dykstra and Robertson (1982), convergence was attained in 47 iterations at a CPU time of .26 seconds.

The constant EPS specifies the change from one cycle to the next for convergence. It has been given an initial value of 10^{-5} ; however if greater or lesser accuracy is required, the value may be changed.

Related Algorithms

Cran (1980) gives an algorithm (AS 149) for amalgamation of the means in the case of simple ordering, which can be used as an alternative to SUBROUTINE PAV.

REFERENCES

- Dykstra, Richard L. and Robertson, Tim (1982). An algorithm for isotonic regression for two or more independent variables. Ann. Statist. 10 (to appear).
- Cran, G.W. (1980). Amalgamation of means in the case of simple ordering. Applied Statistics, 29, 209-211.
- Barlow, R.E., Bartholomew, D.J., Bremner, J.M. and Brunk, H.D. (1972). Statistical Inference Under Order Restrictions. John Wiley and Sons, New York.

```

C
C      DRIVER PROGRAM FOR SMOOTH SUBROUTINE.
C
DIMENSION X(20,20), WT(20,20), G(20,20)
READ( 5, 10 ) NROW, NCOL, NCYCLE
10  FORMAT( 2I2, I5 )
DO 30 I = 1, NROW
READ( 5, 20 ) ( X(I,J), J = 1, NCOL )
20  FORMAT( 10F8.4 )
30  CONTINUE
DO 40 I = 1, NROW
READ( 5, 20 ) ( WT(I,J), J = 1, NCOL )
40  CONTINUE
C
C      ECHO CHECK THE INPUT ARRAYS.
C
WRITE( 6, 50 )
50  FORMAT( 1H1 )
WRITE( 6, 60 )
60  FORMAT( 4X, 34HTHE ORIGINAL MATRIX TO BE SMOOTHED, // )
DO 80 I = 1, NROW
WRITE( 6, 70 ) ( X(I,J), J = 1, NCOL )
70  FORMAT( 4X, 10F12.6 )
80  CONTINUE
WRITE( 6, 90 )
90  FORMAT( ///4X, 28HTHE ASSOCIATED WEIGHT MATRIX, // )
DO 100 I = 1, NROW
WRITE( 6, 70 ) ( WT(I,J), J = 1, NCOL )
100 CONTINUE
C
C      SMOOTH THE X ARRAY.
C
CALL SMOOTH( NROW, NCOL, X, WT, NCYCLE, ICYCLE, IFAULT, G )
C
C      CHECK FOR FAULT ERRORS IN THE SUBROUTINE.
C
IF ( IFAULT .EQ. 2 ) GOTO 160
IF ( IFAULT .EQ. 3 ) GOTO 180
IF ( IFAULT .EQ. 4 ) WRITE( 6, 110 )
110 FORMAT( //4X, 31HZERO WEIGHTS HAVE BEEN REPLACED,/,
*4X, 24HBY 0.00001 FOR SMOOTHING )
C
C      OUTPUT THE SMOOTHED MATRIX.
C
WRITE( 6, 50 )
WRITE( 6, 120 ) ICYCLE
120 FORMAT( //4X, 35HTHE NUMBER OF CYCLES COMPLETED WAS, I5 )
IF ( IFAULT .EQ. 1 ) WRITE( 6, 130 )
130 FORMAT( 4X, 43HTHE ARRAY DID NOT CONVERGE IN THE SPECIFIED, )
*4X, 16HNUMBER OF CYCLES )
WRITE( 6, 140 )
140 FORMAT( //4X, 19HTHE SMOOTHED MATRIX, // )
DO 150 I = 1, NROW
WRITE( 6, 70 ) ( G(I,J), J = 1, NCOL )
150 CONTINUE
STOP
160 WRITE( 6, 170 )
170 FORMAT( //4X, 31HAT LEAST ONE WEIGHT IS NEGATIVE )
STOP
180 WRITE( 6, 190 )

```


190 FORMAT(//4X, 29HROWS AND/OR COLUMNS EXCEED 20)
STOP
END

SUBROUTINE SMOOTH(NROW, NCOL, X, W, Ncycle, G, ICycle, IFAULT)

SUBROUTINE TO ORDER A 2 DIMENSIONAL ARRAY USING
AN ALGORITHM OF DYKSTRA AND ROBERTSON(1982).
THE ORDERING IS DONE SO THAT THE REGRESSION
FUNCTION IS INCREASING IN EACH INDEPENDENT VARIABLE.

DIMENSION X(20,20), WT(20,20), G(20,20), C(20,20)
DIMENSION R(20,20), ROWS(20), COLS(20), WEIGHT(20)
DIMENSION ORDER(20), GCHECK(20,20), W(20,20)
DATA EPS/ 1.0E-06/

IFault = 0

CHECK THAT ROWS AND COLUMNS DO NOT EXCEED 20.

IF (NROW .GT. 20 .OR. NCOL .GT. 20) GOTO 120

CHECK THAT WEIGHTS ARE POSITIVE, OR ZERO.

DO 5 I = 1, NROW
DO 5 J = 1, NCOL
IF (W(I, J) .LT. 0.0) GOTO 110
WT(I,J) = W(I,J)
IF(WT(I,J) .GE. EPS) GOTO 5
WT(I,J) = 0.00001
IFault = 4
CONTINUE

INITIALIZE R AND C TO ZERO, AND SET UP WORKSPACE.

DO 20 I = 1, NROW
DO 10 J = 1, NCOL
G(I, J) = X(I, J)
GCHECK(I, J) = X(I, J)
C(I, J) = 0.0
R(I, J) = 0.0

CONTINUE

CONTINUE

INITIALIZE COUNTER FOR NUMBER OF CYCLES.

ICOUNT = 0

SMOOTH OVER ROWS.

JCOUNT = 0
DO 50 I = 1, NROW
DO 30 J = 1, NCOL
ROWS(J) = G(I, J) - R(I, J)
WEIGHT(J) = WT(I, J)
CONTINUE

CALL PAVE(NCOL, ROWS, 1, WEIGHT, ORDER)

KCOUNT = 0

DO 40 J = 1, NCOL
R(I, J) = ORDER(J) - ROWS(J)
G(I, J) = ORDER(J)
IF (ABS(G(I, J) - GCHECK(I, J)) .LT. EPS)
* KCOUNT = KCOUNT + 1
GCHECK(I, J) = G(I, J)

```

40 CONTINUE
C
C   DETERMINE IF THERE IS NO CHANGE IN THE ITH ROW
C   FROM THE PREVIOUS ITERATION.
C
IF ( KCOUNT .EQ. NCOL ) JCOUNT = JCOUNT + 1
50 CONTINUE
ICOUNT = ICOUNT + 1
IF ( ICOUNT .EQ. 1 ) GOTO 55
C
C   DETERMINE IF THERE HAS BEEN NO CHANGE IN ALL
C   ROWS FROM THE PREVIOUS ITERATION.
C
IF ( JCOUNT .EQ. NROW ) GOTO 90
C
C   SMOOTH OVER COLUMNS.
C
55 LCOUNT = 0
DO 80 J = 1, NCOL
DO 60 I = 1, NROW
COLS( I ) = G( I, J ) - C( I, J )
WEIGHT( I ) = WT( I, J )
60 CONTINUE
C
CALL PAV( NROW, COLS, 1, WEIGHT, ORDER )
C
MCOUNT = 0
DO 70 I = 1, NROW
C( I, J ) = ORDER( I ) - COLS( I )
G( I, J ) = ORDER( I )
IF ( ABS( G( I, J ) - GCHECK( I, J ) ) .LT. EPS )
* MCOUNT = MCOUNT + 1
GCHECK( I, J ) = G( I, J )
70 CONTINUE
C
C   DETERMINE IF THERE IS NO CHANGE IN THE ITH COLUMN
C   FROM THE PREVIOUS ITERATION.
C
IF ( MCOUNT .EQ. NROW ) LCOUNT = LCOUNT + 1
80 CONTINUE
ICOUNT = ICOUNT + 1
C
C   DETERMINE IF THERE HAS BEEN NO CHANGE IN ALL COLUMNS
C   FROM THE PREVIOUS ITERATION.
C
IF ( LCOUNT .EQ. NCOL ) GOTO 90
C
C   CHECK IF NUMBER OF CYCLES HAS BEEN REACHED.
C
IF ( NCYCLE .EQ. ICOUNT ) GOTO 100
GOTO 25
90 ICYCLE = ICOUNT
RETURN
100 ICYCLE = ICOUNT
IFAILT = 1
RETURN
110 IFAILT = 2
RETURN
120 IFAILT = 3

```

```

RETURN
END
SUBROUTINE PAV( K, X, IORDER, W, FINALX )

```

```

C
C
C      SUBROUTINE TO APPLY POOL ADJACENT VIOLATORS THEOREM.

```

```

DIMENSION FX(20), WT(20), PW(20), X(20), W(20), FINALX(20)
DIMENSION W1(20)
DATA EPS / 1.0E-06 /

```

```

C
C
C      SET UP WORKSPACE.

```

```

DO 10 I = 1, K
FX(I) = X(I)
IF( IORDER .EQ. 0 ) FX(I) = -FX(I)
WT(I) = W(I)
PW(I) = WT(I) * FX(I)
W1(I) = W(I)
10 CONTINUE
IBEL = K - 1
I = 0
30 I = I + 1
35 IF( I .GT. IBEL ) GOTO 50
I1 = I + 1

```

```

C
C
C      DETERMINE IF POOLING IS REQUIRED.

```

```

IF( ( FX(I) - FX(I1) ) .LE. EPS ) GOTO 30

```

```

C
C
C      POOL THE ADJACENT VALUES.

```

```

PW(I) = PW(I) + PW(I1)
W1(I) = W1(I) + W1(I1)
FX(I) = PW(I) / W1(I)
IP = I + 1
IF( IP .GT. IBEL ) GOTO 45
DO 40 J = IP, IBEL
J1 = J + 1
PW(J) = PW(J1)
W1(J) = W1(J1)
FX(J) = FX(J1)
40 CONTINUE
45 IBEL = IBEL - 1
GOTO 35
50 IBEL1 = IBEL
ICOUNT = 0
IF( IBEL1 .LE. 0 ) GOTO 70

```

```

C
C
C      DETERMINE IF ALL VALUES ARE ORDERED.

```

```

DO 60 L = 1, IBEL1
L1 = L + 1
IF( ( FX(L) - FX(L1) ) .LE. EPS ) ICOUNT = ICOUNT + 1
60 CONTINUE
IF( ICOUNT .NE. IBEL1 ) GOTO 20

```

```

C
C
C      RECOVER FINAL ORDERED VALUES.

```

```

70 FINALX(1) = FX(1)
I = 1

```

```
J = 1
L = 2
80 IF( L .GT. K ) GOTO 100
WEIGHT = WT(L) + WT(I)
IF( WEIGHT .GT. W1(J) ) GOTO 90
FINALX(L) = FX(J)
WT(I) = WT(I) + WT(L)
L = L + 1
GOTO 80
90 J1 = J + 1
FINALX(L) = FX(J1)
I = L
J = J + 1
L = L + 1
GOTO 80
100 IF( IORDER .EQ. 1 ) RETURN
DO 110 I = 1, K
FINALX(I) = -FINALX(I)
110 CONTINUE
RETURN
END
```

REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM
1. REPORT NUMBER 11	2. GOVT ACCESSION NO. AD-A213520	3. RECIPIENT'S CATALOG NUMBER
4. TITLE (and Subtitle) A Fortran Program for Isotonic Regression in Two Independent Variables.		5. TYPE OF REPORT & PERIOD COVERED Technical Report
		6. PERFORMING ORG. REPORT NUMBER
7. AUTHOR(s) Gordon Brill, Richard Dykstra, Carolyn Pillers, and Tim Robertson		8. CONTRACT OR GRANT NUMBER(s) N000-80-C-0321
9. PERFORMING ORGANIZATION NAME AND ADDRESS Department of Statistics and Actuarial Science The University of Iowa		10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS
11. CONTROLLING OFFICE NAME AND ADDRESS Office of Naval Research Department of the Navy Arlington, VA		12. REPORT DATE July 1981
		13. NUMBER OF PAGES 10
14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office)		15. SECURITY CLASS. (of this report) Unclassified
		15a. DECLASSIFICATION/DOWNGRADING SCHEDULE
16. DISTRIBUTION STATEMENT (of this Report) APPROVED FOR PUBLIC RELEASE: DISTRIBUTION UNLIMITED.		
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)		
18. SUPPLEMENTARY NOTES		
19. KEY WORDS (Continue on reverse side if necessary and identify by block number) Order restricted inference, isotonic regression.		
20. ABSTRACT (Continue on reverse side if necessary and identify by block number) A Fortran program to implement the algorithm developed by Dykstra and Robertson (Ann. Statist. (1982)) for computing the regression which is required to be increasing in each of two independent variables.		

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