







TECHNICAL REPORT EL-81-6

THERMAL VEGETATION CANOPY MODEL STUDIES

Ь

J. A. Smith, K. J. Ranson, D. Nguyen

Department of Wood Science
College of Forestry and Natural Resources
Colorado State University
Fort Collins, Colo. 80523

and

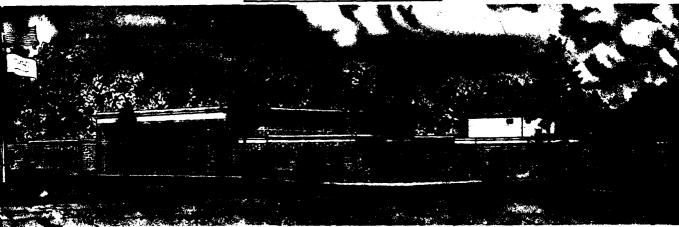
L. E. Link

U. S. Army Engineer Waterways Experiment Station P. O. Box 631, Vicksburg, Miss. 39180

> August 1981 Final Report

Approved For Public Release; Distribution Unlimited





Prepared for Headquarters, Department of the Army Washington, D. C. 20314

Under Project No. 4A762730AT42, Task A4, Work Unit 003 (Contract No. DACW 39-77-C-0073)

Monitored by Environmental Laboratory
U. S. Army Engineer Waterways Experiment Station
P. O. Box 63I, Vicksburg, Miss. 39180

811030037

FILE COPY



Destroy this report when no longer needed. Do not return it to the originator.

The findings in this report are not to be construed as an official Department of the Army position unless so designated by other authorized documents.

The contents of this report are not to be used for advertising, publication, or promotional purposes. Citation of trade names does not constitute an official endorsement or approval of the use of such commercial products.

Carry Might

Unclassified
SECURITY CLASSIFICATION OF THIS PAGE (When Date Entered)

REPORT DOCUMENTATION PAGE	READ INSTRUCTIONS BEFORE COMPLETING FORM
Technical Report EL 81-6: 22. GOVT ACCESSION AD -AL	
THERMAL VEGETATION CANOPY MODEL STUDIES	Final report . 11 77-
	6. PERFORMING ORG. REPORT NUMBER
J. A. Smith, K. J. Ranson, D. Nguyen, and L. E. Link	DACW 39-77-C-0073
Ollege of Forestry and Natural Resources, Colorado State University, Fort Collins, Colo. 805 and U. S. Army Engineer Waterways Experiment Sttion, P. O. Box 631, Vicksburg, Miss. 39180	23, Tank (A) Honk Uni+ 003
11. CONTROLLING OFFICE NAME AND ADDRESS Headquarters, Department of the Army Washington, D. C. 20314	August 1981 / 19. NUMBER OF PAGES 212
14. MONITORING AGENCY NAME & ADDRESS(If different from Controlling Off U. S. Army Engineer Waterways Experiment Statio Environmental Laboratory	Unclassified
P. O. Box 631, Vicksburg, Miss. 39180	15a, DECLASSIFICATION/DOWNGRADING SCHEDULE
Approved for public release; distribution unlim	•••
James A. /Smit K. Jon /Ranson Duong /Nguyen Lewis E. /Link	····:. h
Available from National Technical Information Sopringfield, Va. 22151.	ervice, 5285 Port Royal Road,
Terrain models (Continue on reverse side if necessary and identify by block of Computerized simulation Terrain models (An Infrared detectors Thermal measuremen Temperature Vegetation Terrain analysis	alytical) ts
This is the final report in a series. Over a concerned with developing comprehensive optobases, the development and evaluation of optical models, and the interpretation of these measure ports in this series have described optical and over a coniferous site (Pinus contorta) in Lead	verall objectives of this project cical and thermal signature data al and thermal canopy radiation ements. Previous technical re- d thermal measurements obtained

DD 1 JAN 73 1473 EDITION OF 1 NOV 65 IS OBSOLETE

Unclassified
SECURITY CLASSIFICATION OF THIS PAGE (When Date Entered)

SECURITY CLASSIFICATION OF THIS PAGE(When Data Entered)

ABSTRACT (Continued).

data set served as a test bed for the development and initial evaluation of first, individual components, that is, needle and leaves, thermal models, and then a composite canopy terrain model.

The objectives of the work reported in this study were to evaluate the thermal models developed under a wider range of meteorological conditions and for different vegetation types. In this regard, experiments were performed on a second coniferous site (Pseudotsuga manziesii) near Seattle, Washington, and a deciduous community (oak-hickory) at the Oak Ridge National Laboratory, Tennessee. As part of the evaluation procedure a complete sensitivity analysis was performed for the model. The second major objective of the study reported here was a restructuring of the mathematical model which enabled a factoring of the geometrical characterization of the canopy in terms of matrices which can be convolved with the energy process terms. The newly structured model more easily permits the precalculation of these important geometrical characteristics for a wide variety of terrain elements. Finally, two parameter estimation techniques are proposed for both the static, steady-state, thermal behavior of a canopy and the dynamic or time-dependent implementation.

Access	ion Fo	r		
NTIS	GRA&I		X	
DTIC ?				
Unannounced 🔲				
Justin	Picatio	n		
By Distr	i bution	./		
Availability Codes				
	Avail a	and/	or	
Dist	Spec	ial		
1		1		
14		,	46.00	



Unclassified

SECURITY CLASSIFICATION OF THIS PAGE(When Date Entered)

PREFACE

The research described in this report was conducted by personnel of the Department of Forest and Wood Sciences, College of Forestry and Natural Resources, Colorado State University (CSU) from 1 October 1978 to 1 February 1980 under contract No. DACH 39-77-C-0073 to the U.S. Army Engineer Waterways Experiment Station (WES). The study was done under Department of the Army Project No. 4A762730AT42, Task A4, Terrain/Operations Simulation, Work Unit 003, Electromagnetic Target Surround Characteristics in Natural Terrains.

Participating project personnel concerned with the tasks described in this report include Dr. James A. Smith, Principal Investigator; Mr. K. Jon Ranson, Research Associate; and Mr. Frank Croft, Graduate Research Assistant. In addition, very significant support was provided by Dr. Duong Nguyen of the Civil Engineering Department. Dr. Lee Balick, on assignment at the WES from CSU, was responsible for the technical review of the report and numerous suggestions that benefited the overall quality of this report.

Experimental data utilized in this study were obtained from a deciduous community at Oak Ridge National Laboratory in conjunction with Dr.

B. Hutchison of the Atmospheric Turbulence and Diffusion Laboratory of the National Oceanic and Atmospheric Administration. Similarly, measurements were obtained over a Douglas-fir community in cooperation with Dr.

Leo Fritschen of the University of Washington. Thermal imagery was obtained by the Oregon National Guard at the Washington site.

The study was conducted under the general supervision of Dr. John Harrison, Chief of the Environmental Laboratory (EL), and Mr. Bob Benn,

Chief of the Environmental Systems Division, EL. Dr. Lewis E. Link, Chief of the Environmental Constraints Group, EL, was Technical Monitor for the study.

Commanders and Directors of WES during the conduct of this study were COL. John L. Cannon, CE, and COL. Nelson P. Conover, CE. Technical Director was Mr. Fred R. Brown.

This report should be cited as follows:

Smith, J.A., Ranson, K.J., Nguyen, D., and Link, L.E. 1981. "Thermal Vegetation Canopy Model Studies," Technical Report EL-81-6, prepared by Colorado State University in collaboration with the Environmental Laboratory, Waterways Experiment Station, for the U.S. Army Engineer Waterways Experiment Station, CE, Vicksburg, Miss.

CONTENTS

			<u>Page</u>
PREFA	CE		1
PART	I:	INTRODUCTION	5
		Model Framework	5
		Sensitivity Analysis	8
		Experimental Validation	10
		Recommendations	10
PART	II:	NEW MODEL STRUCTURE	13
		Energy-Balance Framework	13
		Explicit Evaluation of the Jacobian	15
		Geometrical Factorization	16
		Sequence of Required Computer Runs	19
PART	III:	SENSITIVITY ANALYSIS	21
PART	IV:	MODEL VALIDATION EXPERIMENTS	24
		Experimental Design	24
		Site Descriptions	25
		Cedar River, Washington	26
		Walker Branch, Tennessee	27
		Modeling Input Data	28
		Foliage geometry	28
		Leaf area index	30
		Canopy density parameter	31
		Canopy optical parameters	31
		Shortwave absorption coefficients	32
		Stomatal resistance	33
		Emissivity and absorptivity	34

		Page
	Canopy Temperature Measurements	. 34
	Model Validation Results	. 36
	Douglas-fir canopy	. 36
	Oak-hickory canopy	. 37
	Summary	. 38
PART	V: RECOMMENDATIONS	39
	Model Improvements	39
	Parameter Estimation	41
	REFERENCES	. 44
	APPENDIX A: PROGRAM LISTINGS	. A1
	APPENDIX B: GEOMETRICAL MATRICES FOR THEORETICAL CANOPIES	.B1
	APPENDIX C: SENSITIVITY ANALYSIS RESULTS	. C1
	APPENDIX D: SUPPORTING VALIDATION DATA	. D1

THERMAL VEGETATION CANOPY MODEL STUDIES

PART I: INTRODUCTION

- 1. This technical report is the last of a series of reports prepared on scene radiation dynamics. Earlier volumes in this series have described the development of models for optical and thermal energy interactions with forest and grassland vegetation canopies. Extensive field measurement efforts done in cooperation with the U.S. Army Engineer Waterways Experiment Station (WES) have also been separately reported. This report describes further efforts in thermal model development, evaluation, and sensitivity analysis. Measurements obtained over a Douglas-fir (Pseudotsuga menziesii) experimental site near Seattle, Washington, and an oak-hickory, deciduous site near Oak Ridge National Laboratory, Tennessee, are included. At both sites intensive ground instrumentation was employed as well as thermal overflights provided by the Oregon National Guard and the Georgia National Guard, respectively. In addition, analyses have been performed with data from Zweibrücken Air Force Base in the Federal Republic of Germany.
- This introduction briefly summarizes the following topics which are explored more fully in the body of the report: (a) model framework,
 (b) sensitivity analysis, (c) experimental validation, and (d) recommendations.

Model Framework

3. The initial thermal canopy model utilized in this study is described in the report by Kimes, Smith, and Ranson (1979). The model is a plane-parallel abstraction of a vegetation canopy divided into three horizontal layers. Furthermore, steady-state conditions are assumed.

4. An energy-balance formulation of the model may be given in vector form by

$$\underline{F}(X,\underline{P},\underline{U}) = 0 \tag{1}$$

where:

 $\underline{F} = (F_1 \ F_2 \ F_3)$ is the energy-balance equation for layers 1, 2, and 3, considering the following energy components: longwave transfers, shortwave transfers, sensible heat, and evapotranspiration

 $\underline{X} = (X_1 \ X_2 \ X_3)^T$ is the average layer temperature vector for layers 1, 2, and 3

 $\underline{P} = (\varepsilon_i, i=1,2,3 \quad \alpha_i, i=1,2,3 \quad \varepsilon_g \quad R_1 \quad \underline{S} \quad \underline{A})$ is the parameter vector characterizing the canopy layers

 ϵ_i, α_i = emissivity and absorptivity of the vegetation layer

 ϵ_{a} , α_{a} = emissivity and absorptivity of the ground layer

 R_{1} = canopy stomatal resistance to water vapor diffusion

 \underline{S} = longwave flux transfer matrix calculated from geometrical properties of the canopy

 \underline{A} = shortwave flux absorption coefficient vector

 $\underline{U} = (T_a T_g WS RH SW)^T$ is the control or input vector

 $T_a = air temperature$

 $T_a = ground temperature$

WS = wind speed

RH = relative humidity

SW = shortwave flux

5. As part of the tasks of this project, \underline{F} was rewritten in the following form, which explicitly factors the geometrical properties of the canopy from the remaining energy terms:

$$\underline{F} = \frac{1}{2} \underline{\alpha} \underline{\sigma} \underline{B}(\underline{X})^{\mathsf{T}} \underline{S} + \underline{B}(\underline{X}) + \underline{A} + \underline{H}(\underline{X}) + \underline{LE}(\underline{X})$$
 (2)

where:

 σ = Stefan-Boltzmann constant

 \underline{B} = vector of longwave emission terms

H = vector of sensible heat

LE = vector of evapotranspiration term

The significance of this factorization is that a wide variety of abstract or canonical canopies may be characterized by precalculation of \underline{S} and \underline{A} matrices. These matrix tables may then be convolved with the appropriate meteorological driving variables to simulate diurnal behavior for a wide spectrum of scenaries. Five standard canopy structures of three different densities are given. These canopy structure combinations represent a spectrum of geometrical structure-indexed thermal variations. Other combinations may easily be calculated.

6. In addition a view factor matrix \underline{VF} is precalculated for each canopy characterization which is used to calculate thermal exitance \underline{W} as a function of view angle, Θ .

$$W(o) = VF(Layer, o) B^{T}$$
 (3)

where:

W = the predicted canopy exitance at view angle, o

- 7. Finally, a new solution of the energy-balance equation was formulated utilizing the knowledge of the \underline{F} function which permits an explicit evaluation of the Jacobian.
- 8. Specifically, a modified iterative Newton-Raphson technique is employed (Burden, Faires, and Reynolds 1978).
- 9. Given \underline{P} , \underline{U} for a given time period, $\underline{F}(\underline{X},\underline{P},\underline{U})$ becomes a function of \underline{X} only. Expanding about an initial guess, \underline{X}_0 , and employing a minimum squared error criteria yields

$$\delta \underline{X} = \underline{X} - \underline{X}_{0} = (J^{\mathsf{T}}J)^{-1}J^{\mathsf{T}} \left[-\underline{F}(\underline{X}_{0})\right] \tag{4}$$

where:

J = the Jacobian evaluated at $\underline{X} = \underline{X}_0$ and the n+1 iteration is given by

$$\frac{\chi}{2n+1} = \frac{\chi}{2n} + \delta \frac{\chi}{2} \tag{5}$$

Convergence usually occurs within a few iterations.

10. The initial guess is taken to be air temperature; thus, the solution approach may be interpreted as determining the modification to the air temperature profile which arises when a canopy is inserted into the volume space under consideration.

Sensitivity Analysis

- 11. A sensitivity analysis was performed on the following parameters and input variables:
 - $lpha_{f i}$ longwave absorptivity for vegetation layers 1, 2, and 3
 - $\epsilon_{\mbox{\scriptsize i}}$ longwave emissivity for layers 1, 2, and 3
 - $arepsilon_{oldsymbol{\sigma}}$ ground emissivity

 R_1 canopy stomatal resistance

 A_1 shortwave absorption in vegetation layers 1, 2, and 3

RH relative humidity

 T_{α} ground temperature

WS wind speed

T_a air temperature above the canopy

 ${\bf T}_{{\bf a}{\bf c}}$ air temperature within the canopy

Sensitivity analysis was not directly performed on the \underline{S} matrix nor on the view factor matrix. Rather, the above analyses were repeated for two different \underline{S} matrix configurations. One corresponded to the Douglas-fir canopy and the second to an oak-hickory canopy.

12. Sensitivity analysis (Tomovic 1963) involves the evaluation of the sensitivity matrix:

$$\left[\frac{\partial \overline{X}}{\partial \overline{P}}\right]_{X_0, P_0} = S_{XP} \tag{6}$$

where:

 \underline{X} = layer temperature vector

 \underline{P} = 16-component parameter/input vector

The analysis was performed in each case for x_0, p_0 corresponding to a daytime and nighttime representative set of conditions.

13. The first order perturbation of each of the 16 parameters was evaluated systematically, solving for the new equilibrium canopy temperature profile after each perturbation, i.e.,

$$\delta \underline{X} = S_{xp} \delta \underline{P} \tag{7}$$

The most sensitive parameter of the model was found to be the air temperature within the canopy. Next, dependence on canopy stomatal resistance was found to be highly nonlinear for the low values of R_{\parallel} . The dependence of canopy temperature on most other parameters was found to be highly linear.

Experimental Validation

14. Comparison of both daytime and nighttime measurements for the Doulgas-fir and oak-hickory canopies with simulation predictions were carried out. For both of the canopies, nighttime simulations deviated from measured values by 2° C or less. Daytime simulations underestimated measured Douglas-fir canopy temperatures by a maximum of 2° C; whereas, simulation of the lower canopy for oak-hickory overestimated temperatures by a maximum of 4° C. Deviation patterns could be explained in terms of macroscopic and variable environmental conditions.

Recommendations

- 15. Two broad categories of recommendations are made in the enclosed report. First, several suggestions are made relative to improvements that could be made in the thermal model itself. Secondly, some suggested approaches for estimating required parameters in the model from observed data are given.
- 16. Sensitivity analysis has indicated the importance of the air temperature within the canopy as an input to the model. Further, the validation experiments have indicated the importance of utilizing an appropriate wind speed measurement. Thus, it would appear to be appropriate

to review the various hypotheses concerning the variation in air temperature and wind speed with height. The model is easily modified to include a height dependence of these two variables; they are treated as constants simply because there is not a very strong rationale for choosing among the various options. In a similar vein, various authors' recommendations have been selected for analytic representations of the energy budget components. It may be useful to systematically evaluate several alternative formulations. Two further extensions to the physics of the model would include the incorporation of a ground temperature prediction module and the expansion of the steady-state formulation to a time-dependent process, that is, allowing for heat storage within the canopy.

- 17. Finally, further analysis of the structure of the geometrical matrices, that is, the \underline{S} , \underline{A} , and VF matrices, relative to the intrinsic canopy structure variables should be undertaken. Specifically, the possibility of further factoring these matrices in terms of their leaf area index dependence and their dependence upon leaf slope distribution should be investigated. It may be possible to treat the density, that is the leaf area index dependence, as a simple scaling influence on precalculated structural forms. If an analytic decomposition of these matrices in terms of these two influences is not possible, numerical approaches should be investigated. A faster, more tractable, calculation of the shortwave absorption coefficient should be given high priority.
- 18. Two approaches are recommended for parameter estimation analysis. The first method described is based on the Kalman filtering techniques. The linearization of the model in terms of a classic state-space framework is outlined. A Kalman filtering approach on a parameter vector or an

augmented state vector is described (Friedland 1972). A second approach to parameter estimation is suggested, which is based on the use of sensitivity functions (Durando and Leondes 1976). This approach also begins with a state-space formulation of the model but then proceeds to use the sensitivity functions to calculate an unknown parameter vector by minimizing the square of the error vector between predicted and measured response.

19. The appendixes of this report include the program listings for the thermal model, the sensitivity program, the geometrical preprocessing programs, SCALC, and the SRVC absorption model. Also included in the appendixes are the geometrical matrices for 15 abstract canopies, the sensitivity results, and supporting validation data.

PART II: NEW MODEL STRUCTURE

20. This part summarizes the updated formulation and solution approach to the basic thermal canopy model developed under previous efforts. The individual expressions for the component energy budget processes are summarized and explicit expressions for the elements of the Jacobian matrix are given. The geometrical factorization of the energy budget equation, particularly for the longwave flux transfers, is derived, and the sequence of computer programs required to develop a thermal simulation is described.

Energy-Balance Framework

- 21. The model is a plane-parallel abstraction of a vegetation canopy divided into three horizontal layers. Two additional source layers are given by the atmosphere above the canopy and by the underlying ground or understory layer. An energy-balance framework, assuming steady-state conditions, is formulated for each of the three vegetation layers (sinks) as a function of the five source layers. For this and subsequent sections Figure 1 may prove useful for conceptualizing the various energy flows. The sink or vegetation layers are represented by $i=1,2,3;\ j=1,2,3,4,5$ represents, respectively, the atmosphere, the three vegetation layers, and the ground source layers of energy flux. The combination of the i,j indices, thus represents a flow of energy from source layer j to sink layer i.
- 22. The vector expression for the energy-balance equations was given in the Part I, Equations 1 and 2 as:

$$F = \frac{1}{2} \alpha \sigma B(X)^{T}S + B(X) + A + H(X) + LE(X)$$

23. The vector equation may be expanded in long form and the explicit dependence on parameters or input variables indicated by

$$\frac{1}{2} \alpha_{1} \sigma \left[B(T_{a}) S_{11} + B(X_{1}) S_{12} + B(X_{2}) S_{13} + B(X_{3}) S_{14} + B(T_{g}) S_{15} \right] + A_{1} - \sigma B(X_{1}) + H(X_{1}; WS, T_{a}) + LE(X_{1}; WS, T_{a}, R_{1}, RH) = 0$$
(8)

where the explicit formulation for each energy budget component used in the model is given by

Longwave:
$$B(X_i) = \varepsilon_i (X_i + 273)^4$$
 (11)

$$B(T_a) = \varepsilon_a (T_a + 273)^4 \tag{12}$$

$$B(T_q) = \varepsilon_q (T_q + 273)^4 \tag{13}$$

Sensible Heat: $H(X_iWS,T_a) = (X_i-T_a) -0.698(20.4 + 0.2WS^{0.97})(14)$ Evapotranspiration:

LE(
$$X_i$$
; WS, T_a , R_l ,RH) = -697.75(-0.566 X_i + 597.3)

$$\times \frac{(5.234 e^{0.056715 \cdot X_i} -RH 5.234 e^{0.056715 \cdot T_a}) 10^{-6}}{R_l + 1/60 (0.04 + 1.27 WS^{-1/2})}$$
(15)

Shortwave absorption:
$$A_i = ABS(i) \cdot SW$$
 (16)

where:

$$\epsilon_{air} = 1 - 0.261 e^{-7.77} \cdot 10^{-4} T_a^2$$
 (17)

ABS(i) = shortwave absorption coefficients calculated by an optical absorption model which uses a Monte Carlo Technique to include multiple scattering effects (see Program SRVC in Appendix A)

14

Explicit Evaluation of the Jacobian

24. As indicated in Part I, the use of the iterative Newton-Raphson technique for solving the nonlinear thermal equations involves repeated evaluation of the expression

$$\delta \underline{X} = (J^{\mathsf{T}}J)^{-1} J^{\mathsf{T}} \left[-\underline{F}(X_{\mathsf{O}}) \right]$$
 (18)

where:

J = system Jacobian =
$$\left[\frac{\partial F}{\partial X}\right] X = X_0$$
 (19)

The Newton-Raphson method is employed because, in this case, there are relatively simple closed-form expressions for the elements of \underline{F} , and the Jacobian matrix can explicitly be evaluated. Specifically,

$$J = \begin{pmatrix} \frac{\partial F_1}{\partial X_1} & \frac{\partial F_2}{\partial X_1} & \frac{\partial F_3}{\partial X_1} \\ \frac{\partial F_1}{\partial X_2} & \frac{\partial F_2}{\partial X_2} & \frac{\partial F_3}{\partial X_2} \\ \frac{\partial F_1}{\partial X_3} & \frac{\partial F_2}{\partial X_3} & \frac{\partial F_3}{\partial X_3} \end{pmatrix}$$
(20)

The i,j component of \underline{J} is easily derived as

$$J_{ij} = 2 \alpha_{i} \epsilon_{j} S_{ij} \sigma(X_{j} + 273)^{3} + \delta_{ij} \{4\epsilon_{j} \sigma(X_{j} + 273)^{3} + 0.698 T_{a}\}$$

$$(20.4 + 0.2WS^{0.97}) + \frac{(697.75)(0.566)(5.234)(10^{-6})(e^{0.056715 X_{j}} - RH e^{0.056715 T_{a}})}{R_{l} + 1/60 (0.04 + 1.27 WS^{-0.5})} + \frac{-(697.75)(-0.566 X_{j} + 597.3)(5.234)(0.056715) 10^{-6} e^{0.056715 X_{j}}}{R_{l} + 1/60 (0.04 + 1.27 WS^{-0.5})}$$

$$(21)$$

where:

 δ_{ii} = Dirac delta function

25. Program TMODEL, which implements the equations, is given in Appendix A. Subroutine FEVAL evaluates the function and the Jacobian derivatives and calls upon Subroutine BFUNC which calculates the long-wave energy component and derivative; Subroutine QFUNC calculates the sensible heat component and derivative. It should also be noted that two different expressions for the convection coefficient arise, depending upon the ambient wind speed. Subroutine RFUNC calculates the evapotranspiration.

Geometrical Factorization

- 26. A significant simplification of the thermal model employed in this study was the factorization of the geometric-dependent terms from the energy-related terms for the longwave flux transfer processes. This factorization is made possible essentially because of the lack of multiple scattering in the thermal regime between canopy components whose emissivities (absorptivities) are assumed nearly unity and by the fact that the thermal properties on both sides of a canopy component are assumed equal. The significance of the factorization is not so much in the increased efficiency in model calculation as it is in permitting the possibility of precalculating these geometrical matrices, \underline{S} , for a wide variety of plant canopies. These precalculated matrices may then be convolved with the appropriate driving variables as required. Program SCALC (Appendix A) performs the actual calculations for given input of geometric measurements.
 - 27. The required input data for a three-layer canopy include

 f_{ik} = leaf slope distribution for layer i=1,2,3 and angle θ_k =5,15,...,85

16

 N_i = leaf area index LAI , for layer i

Appendix B presents the \underline{S} matrices calculated for five different theoretical canopies at three different LAI densities = 1, 4, and 7.

28. The five theoretical canopies are approximated by Verhoef and Bunnik (1975) as

Planopnile:
$$f_{ik} = \frac{2}{\pi} (1 + \cos 2 \Theta_k)$$

Erectophile:
$$f_{ik} = \frac{2}{\pi} (1 - \cos 2 \Theta_k)$$

Plagiophile:
$$f_{ik} = \frac{2}{\pi} (1 - \cos 4 \Theta_k)$$

Extremophile:
$$f_{ik} = \frac{2}{\pi} (1 + \cos 4 \Theta_k)$$

Uniform:
$$f_{ik} = \frac{2}{\pi}$$

where Θ_k is the leaf slope angle.

The elements of the \underline{S} matrix, itself, are given by

$$S_{ij} = \sum_{k=1}^{9} f_{ik} C_{ijk}$$
 (22)

where:

$$C_{ijk} = \int_{0}^{\pi/2} \int_{0}^{2\pi} |\hat{a} \cdot \hat{r}| CONT_{ijr} d\phi_{r} d\theta_{r}$$
 (23)

 \hat{a} is the orientation of the leaf at angle Θ_k ; and \hat{r} is the direction of the energy flux described by Θ_r , ϕ_r (i.e., \hat{r} = (sin Θ_r cos ϕ_r , sin Θ_r sin ϕ_r , cos Θ_r) (24)

The elements of CONT $_{ijr}$ represent the weighting coefficients which give the flux contributions from a source layer, j=1,2,3,4,5, to a sink vegetation canopy layer, i=1,2,3, from a particular source direction Θ_r , ϕ_r .

These elements for an arbitrary direction, \hat{r} , are given in Table 1. $P_{0}(i,r) \text{ is the probability of a gap in transversing layer } i \text{ at direction}$ r. It may approximated by

$$P_{o}(i,r) \stackrel{\Delta}{=} P_{o}(i,\Theta_{r}) = e^{-N(i)} g(i,\Theta_{r}) \sec \Theta_{r}$$
 (25)

where g(i,0_r) is the mean canopy layer projection in direction $\,\theta_r^{}$. Mean canopy projection is given by

$$g(i,\Theta_r) = \int_{-\infty}^{\pi/2} k(\Theta_r,\Theta_k) f_{ik} d\Theta_k$$
 (26)

where:

$$= 2/\pi \cos \theta_k \cos \theta_r , \theta_k \leq \pi/2 - \theta_r$$

$$= 4/\pi^2 \cos \theta_k \cos \theta_r (\phi_k - \pi/2 - \tan \phi_k) , \theta_k \geq \pi/2 - \theta_r$$

$$\phi_k = \cos^{-1} (-\cot \theta_k \cot \theta_r)$$

Program SCALC also calculates the view factor matrix for the canopy.

This matrix is used to determine the thermal flux contribution from each vegetation layer and the ground layer which is intercepted by a sensor viewing the canopy at a particular zenith angle. It is given by

$$W(i,\Theta_{r}) = \underline{VF}(i,\Theta_{r}) = [VF(1,r) \ VF(2,r) \ VF(3,r) \ VF(4,r)]^{T}$$

$$VF(1,\Theta_{r}) = 1 - P_{o}(1,r)$$

$$VF(2,\Theta_{r}) = P_{o}(1,r)[1 - P_{o}(2,r)]$$

$$VF(3,\Theta_{r}) = P_{o}(1,r) P_{o}(2,r)[1 - P_{o}(3,r)]$$

$$VF(4,\Theta_{r}) = P_{o}(1,r) P_{o}(2,r) P_{o}(3,r)$$

Sequence of Required Computer Runs

- 29. Appendix A contains a listing of all the computer programs utilized in this study. Three of these programs are directly concerned with thermal modeling or preprocessing steps that must be initiated before the thermal calculations may be made. In addition, program SENSIT has been included. This program performs the systematic and repetitive calculations necessary to complete the sensitivity calculations of many of the thermal model parameters.
- 30. The basic thermal model is program TMODEL. This program assumes that the geometrical characterization of the canopy has been performed and the appropriate S matrix, shortwave absorption vector, and view factor matrix have been calculated. The model then performs similar calculations at discrete time intervals, given the specification of the appropriate parameter (emission and absorption characteristics of the canopy elements and the ground, canopy stomatal resistance to water vapor diffusion). Furthermore, the input information must be provided at the discrete time intervals simulated. These data consist of the air temperature, the ground temperature, the wind speed, the relative humidity, and the shortwave flux. The basic philosophy of TMODEL is that for a given type or types of vegetation canopies, one would want to simulate a multitude of scenarios for their thermal behavior based on either ambient meteorological conditions or modifications to the thermal properties of the canopy or understory. Thus, it is usually required to calculate the geometrical characteristics of the canopy type only once and then perform multiple simulations of the canopy with TMODEL.
- 31. The calculations of the appropriate geometrical flux transfer matrices are done by Program SCALC and Program SRVC for absorption. For both of these programs, detailed canopy geometry information is required.

This includes the leaf area index for each layer, and the leaf slope distribution by layer. In addition, to calculate the shortwave absorption coefficients, average optical properties of the canopy elements are required. The SRVC absorption model is further described in a report by Kimes, Smith, and Ranson (1979).

- 32. The complete set of geometrical matrices have been calculated for the lodgepole pine canopy in Leadville, Colorado, studies under earlier WES sponsorship, the Douglas-fir canopy from the Cedar River Watershed, near Seattle, Washington, and the oak-hickory deciduous community at the Walker Branch Watershed at Oak Ridge National Laboratory in Tennessee. In addition, the geometrical characterization has been performed for 15 abstract canopies of varying densities and geometrices. These data are given in Appendix B.
- 33. In summary, given a specific canopy to be studied and for which detailed geometrical measurements have been obtained, Program SCALC and the SRVC absorption model are first used in a preprocessing manner to calculate the appropriate flux-transfer matrices. The data generated from these runs are then used in Program TMODEL. If there is no specific geometrical measurement available for canopies of interest, then one of the 15 theoretical canopies in Appendix B may be appropriate.
- 34. An example of a complete analysis for the validation experiments is given in Part IV.

PART III: SENSITIVITY ANALYSIS

35. The basic analytic model described in this report may be indicated by the form:

$$F(X,P,U) = 0$$

To simplify notation, \underline{U} will be considered to be an additional set of parameters augmenting the \underline{P} vector, and it will be written that:

$$\underline{F}(\underline{X},\underline{P}) = 0$$

Further, the solution to the system of equations for a specific parameter \underline{P}_0 will be indicated as $\underline{X}(\underline{P}_0)$.

- 36. Sensitivity analysis consists of determining the change in the solution to the model for a small change or perturbation in model parameters, i.e., $X(\underline{P}_0 + \Delta \underline{P})$.
 - 37. The sensitivity function $S_{\chi p}$ is defined (Tomovic 1963) as:

$$\lim_{\Delta \xrightarrow{P \to 0}} \frac{\underline{X}(\underline{P}_0 + \Delta \underline{P}) - \underline{X}(\underline{P}_0)}{\Delta P}$$

The sensitivity function may be evaluated analytically by differentiation of the system equations with respect to the parameters under consideration, yielding the following sensitivity equation:

$$\frac{\partial F}{\partial X} \frac{\partial X}{\partial P} + \frac{\partial F}{\partial P} = 0$$
or
$$S_{xp} \frac{\partial F}{\partial X} + \frac{\partial F}{\partial P} = 0$$
(27)

Alternatively, computer simulations may be employed in which the parameters are systematically and separately perturbed from nominal values and new canopy temperatures are determined.

- 38. As indicated in Part I, this latter approach was employed for this study. Program SENSIT was written to facilitate the calculation (Appendix A).
- 39. Program SENSIT requires environmental data and temperatures for each layer to initialize the analysis. In addition, geometrical factor matrices describing a particular canopy are required. The environmental data used was collected by WES personnel at Zweibrücken Air Force Base in West Germany on 4 October 1979. Data was selected at 0600 hours and 1100 hours to provide for nighttime (predawn) and daytime analysis. Initial state temperatures for each layer were determined from simulation results. The sensitivity analysis was performed for both the Douglas-fir and oakhickory canopies resulting in a total of four analyses. Table 2 lists the initial environmental parameters and initial temperatures for each sensitivity run. Graphical results of parameter changes versus predicted temperatures are found in Appendix C.
- 40. The daytime sensitivity analysis showed that the predicted canopy temperatures were most sensitive to the air temperature within the canopy. A 10 percent change in canopy air temperature resulted in nearly a 10 percent change in all layers for both types of canopies. Decreasing longwave absorption coefficients by 10 percent resulted in less than a 0.5°C change in predicted temperatures and showed a layer by layer dependence for both canopies and time periods. Predicted canopy temperatures showed minimal sensitivity to changes in air and ground temperatures as input to the model. Temperature predictions were nearly equally sensitive to the shortwave absorption in all three layers

for both canopies. Changing the canopy emissivity in the top layer for both canopies had little effect on predicted temperature for layer 1, but slightly increased sensitivity was noted for the two lower canopy layers. Decreasing ground emissivity from 1.0 to 0.9 increased predicted temperatures by less than 0.5°C. Changing relative humidity showed little effect on canopy temperatures with the daytime oak-hickory analysis exhibiting the greatest sensitivity. A linear relationship was noted between predicted canopy temperatures and the parameters discussed above. Only stomatal resistance and wind speed analyses showed nonlinear trends. Sensitivity plots of stomatal resistance for Douglas-fir and oak-hickory are shown in Figure 2. In both cases the plots are nonlinear above values of 0.08 min/cm. Other analyses not reported here showed a linear relationship for R greater than 0.08 min/cm to about 1.5 min/cm. Figure 3 shows plots of wind speed versus predicted temperature for Doulgasfir daytime and nighttime analyses. The daytime plot shows an increase in temperature with decreasing wind speed; but at night, temperatures decrease slightly with decreasing wind speed.

PART IV: MODEL VALIDATION EXPERIMENTS

41. As discussed earlier, the objective of the field experiments was to provide data sets from diverse targets and environmental conditions for validation of the Colorado State University (CSU) thermal canopy model. Two existing research sites were located through the efforts of WES personnel that proved to be ideal for the experiments. The Cedar River site was located in a Douglas-fir forest near Seattle, Washington. A second research site, the Nalker Branch Watershed, was typical of an Appalachian deciduous forest and was located near Oak Ridge, Tennessee. Both research sites were being used for ongoing research in forest meteorology and possessed extensive instrumentation and computerized data acquisition support. The principal scientist responsible for the development of the Cedar River site was Dr. Leo J. Fritschen of the College of Forest Resources, University of Washington, while Dr. Boyd A. Hutchison of the Atmospheric Turbulence and Diffusion Laboratory (ATDL), National Oceanic and Atmospheric Administration (NOAA) was responsible for the Walker Branch site. Further descriptions of these sites are given below.

Experimental Design

42. The model validation experiments were designed by CSU and WES personnel with cooperation from Drs. Fritschen and Hutchison. The goal was to provide appropriate input and validation data for the CSU canopy models. Input data included optical, thermal, and environmental parameters for two consecutive 24-hour periods of the targets. Validation

data consisted of foliage temperatures. In addition, thermal scanner imagery was to be obtained by local National Guard units at specified times throughout the measurement periods. Characterization of the foliage angle distributions of the canopies was also required. Input data requirements and methods are discussed in a later section.

43. WES personnel were responsible for overall mission coordination, thermal radiometric measurements of ground and canopy, air temperature measurements in the lower 1.5 m of the canopies, and arranging for National Guard thermal scanner overflights of the experimental sites. CSU personnel communicated requirements for micrometeorological data to Drs. Fritschen and Hutchison, obtained foliage geometry data from the sites, and performed necessary optical measurements required to run the canopy models. Groups headed by Drs. Fritschen and Hutchison provided site access, operated and maintained the data acquisition systems, and provided assistance for interpreting the micrometeorological data. In addition, Dr. L. W. Gay of the School of Renewable Natural Resources, Arizona University at Tucson participated in the Cedar River Douglas-fir experiment to test the use of direct beam depletion measurements for determining forest biomass.

Site Descriptions

44. Two established research sites were available for this study. A site near Seattle, Washington, developed and maintained by Dr. Leo Fritschen of the University of Washington, provided data for a stand of mature Douglas-fir. Dr. Boyd Hutchison of ATDL/NUAA made available an oak-hickory site near Oak Ridge, Tennessee and provided necessary

environmental data. A detailed description of these sites is provided below.

Cedar River, Washington

- 45. The Cedar River, Washington, study site is located on the Λ . E. Thompson Research Center at the western end of the Cedar River Watershed. The site lies in the Puget Sound Basin at the western foot of the Cascade Mountains 55 km southeast of Seattle, Washington, at $47^{\circ}23$ 'N and 121° 56'W. The elevation is approximately 215 m above mean sea level.
- 46. The area was logged prior to 1924 and subsequent fires resulted in a mosaic of different aged stands (Jensen, 1976). The most common community on the site is Douglas-fir (Pseudotsuga menziesii (Mirb.) Franco). This naturally regenerated stand was approximately 41 years old with an average tree spacing of 5.8m. There were 572 trees per hectare consisting mainly of Douglas-fir, a few hemlock, and maple (Figure 4). Ground cover consisted of fern, salal, huckleberry mosses, and litter (Figure 5). Bare soil areas were minimal and occurred only on roads and other localized disturbed areas. Soil at the site consisted of Barneston gravelly, loamy sand originating from glacial outwash.
- 47. The specific study site was located at a micrometeorological observatory maintained and operated by the University of Washington.

 Average height of the Douglas-fir stand was about 28 m with an average LAI of approximately 7.8. Located at this site was a 28-m-tall Douglas-fir tree contained in a lysimeter (Fritschen, Cox, and Kinerson, 1973). The site adjacent to this tree was instrumented to provide data for

evapotranspiration studies. These data included wet and dry bulb temperatures, soil temperatures, global shortwave radiation, precipitation, and wind speed and direction. In addition, needle surface temperatures were monitored at several points around the lysimeter tree near the top and center of the canopy. These data were recorded at selected time intervals by a computerized data acquisition system.

A 33-m walk-up tower was available adjacent to the lysimeter tree to provide access to needle temperature sensors and other measurement devices.

Walker Branch, Tennessee

- 48. The Walker Branch study site is located near the Walker Branch Watershed research facility on the U.S. Department of Energy Reservation near Oak Ridge, Tennessee, at 35°58'N and 84°15'W. An intensive forest meteorological research site operated by the ATDL of the NOAA was made available for this study. This research area is situated on a ridge top about 70 m above the valley floor at an elevation of 335 m above mean sea level.
- 49. The area is representative of an Appalachian deciduous forest (Hutchison, 1977). The species composition of the stand is dominated by various species of oak and hickory, including Quercus alba, Quercus prinus, Quercus velutina, Carya glabra and Carya ovata. Acer rubra (red maple), Prunus serotina (black cherry), Liriodendron tulipifera (yellow popular) are less frequently found. Common understory plants include Oxydendron arboreum (sour wood), Cornus florida (flowering dogwood) and Cercis canadensis (eastern redbud). The average height of the

codominant trees forming the canopy is about 21.5 m with lower limit of the live crown being 15 m above the ground. These heights vary greatly due to the uneven age of the stand (Figure 6). Basal area was approximately 26 m² ha⁻¹. The site appeared parklike due to a fire that occurred several years ago. Understory growth, however, is abundant. The ground is covered by an accumulation of litter (Figure 7) with bare soil occurring only in disturbed areas. In addition, fragmented, grey-colored rock covered the road surfaces. A metal track was in place beneath the stand to provide all-weather access for research vehicles. This track was covered with litter by ATDL personnel during the field experiments.

50. The site is extensively instrumented to record data pertinent to forest meteorology research as well as the thermal modeling studies. Hutchison (1977) gives a detailed description of the research facility.

Modeling Input Data

51. The data collected at the two sites included foliage and background optical parameters, geometry characterization measurements, and environmental measurements. This section describes the data required for the models and the techniques or sources used to acquire it. Listings of the data values are included in Appendix D.

Foliage geometry

52. The structure of a canopy defined by the foliage inclination angles and LAI is important for characterizing the interactions of radiation with the canopy. These inputs are required by the optical SRVC

model (Oliver and Smith 1974) to estimate the shortwave absorption of a canopy and by the thermal model to describe longwave energy exchanges inside and outside of the canopy.

- 53. The procedure for determining foliage geometry included acquiring high-contrast black-and-white slide photography of canopy silhouettes. These slides serve as input to a laser diffractometer which characterizes the frequency of occurrence of foliage angles in terms of the resulting diffraction pattern. The diffraction patterns are optically sampled, and the results are analyzed with a series of computer programs. See Kimes, Smith, and Ranson (1979) for a discussion of the theory and procedures.
- 54. The walk-up towers at both sites provided an excellent platform for acquiring slides of the canopies. For the purposes of the modeling, the canopies were partitioned into three layers of equal height. Photographs were taken for each layer from several directions from the tower. This provided a larger sample size and minimized effects of azimuthal asymmetry. Ideally, the photographs should be taken with a white backdrop placed behind the target to eliminate background trees and shadows. However, this was impractical for the canopies under study. As a result, the slides were manually interpreted to delineate branches of the desired tree in the photographs. This was done by projecting the slide on white paper and tracing the appropriate branches. Earlier work by Kimes, Smith, and Ranson (1979) showed that for complex canopies, such as conifers, two interpretations are required: one with all branches represented, and a separate tracing including only branches bearing foliage. High-contrast slides of these tracings were used as input to the laser diffractometer. The branch and foliage measurements were

combined later to provide the inclination angle distributions for each layer.

55. The calculated foliage angle distributions for a Douglas-fir canopy are shown in Figure 8. For comparison purposes, distributions of lodgepole pine (Pinus contorta) reported by Kimes, Ranson, Kirchner, and Smith (1978) are included. Figure 9 shows foliage angle distributions for oak-hickory. These data were derived from direct measurements provided by Dr. Hutchison. Laser diffraction results for oak-hickory were unavailable due to equipment problems. For comparison a one-layer distribution for Russian olive (Elaeagnus angustifolia) reported by Kimes, Smith, and Ranson (1979) is included.

Leaf area index

56. LAI is defined as the total one-sided leaf area occupying the horizontally projected area of the canopy. For example, an LAI of 5 indicates that five layers of leaves could be overlayed to completely fill an area equal to the canopy projection on the ground. LAI's for this study were determined from data provided by Drs. Fritschen and Hutchison. LAI's for the Douglas-fir canopy were derived from measurements reported by Kinerson and Fritschen (1971). In this report, graphs of canopy height $\underline{z}(\underline{m})$ versus surface area density $\underline{F}(\underline{z})$ (m^2 m^{-3}) for nine sample plots are given. Integrating $\underline{F}(\underline{z})$ over height gives the needle surface area index NSAI for a particular height increment dz. Data points were taken from the graphs and averaged for given heights to produce a single average surface density curve. This curve was partitioned into three layers of equal height and layer NSAI's determined

by Simpsons Rule (Figure 10). For our modeling purposes, LAI values were determined by dividing NSAI for each layer by two.

57. LAI for the oak-hickory canopy was determined from data provided by ATDL. These data consisted of a graph of cumulative LAI versus height and graph of LAI at given heights through the canopy. A smoothed version of the latter is presented as Figure 11.

Canopy density parameter

58. This parameter ranges from 0 to 1 and describes the spatial dispersion of foliage elements within a canopy. As values approach 1, gaps in the canopy are less frequent since the foliage is more regularly dispersed. This parameter is used in the equation to determine the probability of gaps occurring in a canopy layer. A value of 0.1 was chosen for all model runs. For a detailed discussion of spatial dispersion of canopies see deWit (1965).

Canopy optical param lers

- 59. The shortwave transmission and reflectance of foliage elements are required as inputs for estimating average absorption coefficients as discussed below. Canopy element transmission values were measured at the study sites, but reflectance values were derived from the published literature.
- 60. The procedure for determining transmission consisted of placing a needle or leaf over a narrow slit on a flat plate attached to a photodiode and recording a reading of the amount of light passing through the sample. Measurements were made in four wavelength bands—at $4.8\mu m$, $0.55\mu m$, $0.68\mu m$, and $0.80\mu m$. The transmission measurements were then

ratioed to the incoming spectral irradiance measured from a BaSo $_4$ standard reflectance panel. The measurement procedure was repeated for several foliage samples and the results averaged. Natural illumination was used for the Douglas-fir needles; however, because of rapidly changing irradiance conditions at the Walker Branch site, a bank of fluorescent tubes was used as the irradiance source. The transmission measurements were integrated over wavelength to estimate the average shortwave transmittance from 0.48 to $0.80\mu m$. This wavelength interval was assumed adequate.

- 61. Shortwave reflectance values for Douglas-fir were obtained from data presented by Jarvis, James, and Landsberg (1976). Curves for old and new Douglas-fir needles were digitized and averaged. The resulting curve was then integrated over the wavelength interval from $0.45\mu m$ to $1.2\mu m$ to obtain the average shortwave reflectance coefficient. The oakhickory canopy element reflectance was determined from data presented by Colwell (1969). Data for maple, oak, and yellow poplar were averaged and integrated over the wavelength interval $0.45\mu m$ to $1.2\mu m$.
- 62. In addition to foliage transmission and reflectance estimates, an average background reflectance was determined at both sites. Measurements were made of various surface covers such as litter, bare soil, and ground cover vegetation. The results were weighted according to visual estimates of occurrence and then averaged and integrated.

Shortwave absorption coefficients

63. The absorption of global shortwave radiation by canopy layers is an important component in the daytime energy budget. It is, however, difficult to directly measure and must be estimated with models. These

coefficients were approximated with the SRVC model modified for absorption (Kimes, Smith, and Berry, 1980). The procedure involved running model simulations with appropriate canopy layer geometry, LAI, and optical parameters for an average zenith sun angle of 45°. The resulting absorption values represent the proportion of shortwave absorption in each canopy layer. Since the thermal model requires absorption per unit leaf area, the simulated absorption coefficients were divided by the one-sided leaf area in a given layer.

Stomatal resistance

64. The resistance of the leaf to water vapor diffusion depends on many environmental factors. Leaf stomates open and close in response to microclimatic and soil conditions and regulate the cooling of the plant through evapotranspiration. Thus, stomatal resistance is important when considering energy budget analysis of plants. This parameter is difficult to measure, so for modeling purposes average values were used as constants. The value for Douglas-fir was set at 0.66 min/cm as an average value for coniferous forest (Kimes, Smith, and Ranson, 1979). Stomatal resistances were determined from data provided by Hutchison*. These data ranged from 0.04 to 0.07 min/cm for sun leaves. The upper value was selected for use in all deciduous canopy simulations.

^{*} Personal communication; B. A. Hutchison, Atmospheric Turbulence and Diffusion Laboratory, National Oceanic and Atmospheric Administration, Oak Ridge, Tennessee, 1979.

Emissivity and absorptivity

65. The ability of a canopy element to emit and absorb longwave radiation is expressed by the emissivity and absorptivity coefficients specified for each component in the canopy layers and for the ground layer. Available literature values or direct measurements could, consequently, be substituted. For all of the analyses reported here, the emissivity ε_i and absorptivity α_i are set equal to 1.0 for each of the three canopy layers. Emissivity of the ground ε_g was also set at 1.0. Emissivity of the air ε_a was calculated as a function of air temperature by the following function (Hudson, 1969):

$$\epsilon_a = 1.0 - 0.0261 e^{(-0.000777 T_a^2)}$$

Canopy Temperature Measurements

- 66. Since the purpose of the experiments was to collect data sets for validation of the thermal model, actual canopy foliage temperature measurements were required. The experiments were designed to provide measured canopy temperatures, as well as thermal scanner images of the sites.
- 67. The experimental setup at the Cedar River site included temperature measurements for a number of individual Douglas-fir needles. The temperature sensors were located around the lysimeter tree at average heights of 26 m and 20 m. The measurements at a given height were averaged to give an average layer measurement. The 26-m measurement was assumed to represent the average canopy temperature for layer 1. The 20-m measurement approximated layer 2, although its location was closer to the boundary between layer 1 and layer 2. These layer temperatures are plotted along with air temperature against time in Figure 12.

- 68. No individual leaf temperature measurements were available at the Walker Branch site, so a portable thermal radiometer* was used to monitor the canopy temperature throughout a 24-hour period. The procedure was to position the instrument upward from the ground at the canopy and slowly move it until the maximum temperature was recorded. This was done to minimize errors due to the presence of sky or clouds in the field of view. Figure 13 shows a plot of the canopy temperature with air temperature above the canopy and ground temperature against time.
- 69. In addition to the geometrical, optical, and thermal parameters discussed above, a set of dynamic variables characterizing the microclimate of the target is required to drive the thermal model. These parameters consist of air temperature above the canopy, ground surface temperature, wind speed at the top of the canopy, relative humidity, and global shortwave radiation.
- 70. Air temperature, ground temperature, and shortwave radiation are important components for energy exchange into and within the system; whereas wind speed and relative humidity are important for determining forced convection loss and evapotranspirative cooling of plants, respectively.
- 71. Environmental data were provided from the automated recording systems at the two sites. Air and ground temperatures and global shortwave radiation were measured directly. Relative humidity was determined from wet and dry bulb temperatures. All measurements were

^{*} Barnes Insta-Therm, Barnes Engineering Corporation.

either instantaneous or short time interval averages. Plots of the four environmental parameters are shown in Figure 14 for Cedar River and Figure 15 for Walker Branch.

Model Validation Results

72. The data collected for the coniferous Doulgas-fir and deciduous oak-hickory canopies provided a good means of testing the thermal model under these diverse conditions. Three-layer canopy temperature simulations were made over a 48-hour period with both data sets and the results were compared with measured temperatures.

Douglas-fir canopy

- 73. The thermal model was run with environmental data acquired over the 48-hour period of 4-5 August 1979. These data plus the required geometrical factor matrices which include the longwave exchange coefficients, the sensor view angle weighting factors, and average shortwave absorption coefficients are listed in Appendix D. The emissivities and thermal absorption coefficients for each layer were set to 1.0. The total canopy resistance to water vapor diffusion was input at 0.66 min/cm.
- 74. A plot of the simulated three-layer temperatures with measured air temperature is shown in Figure 16. The layer 1 simulated temperatures follow the trend of air temperature, but fall below during the night and are higher during the day. The layer 2 and layer 3 predictions are nearly equal to air temperature throughout the 48-hour period. Comparisons of measured and predicted needle temperatures for layers 1 and 2 are presented as Figures 17 and 18, respectively.

75. The layer 1 predicted temperatures vary from the measured temperature by a maximum of 3°C. These deviations were observed during the daytime hours under very hazy skies. Nighttime predictions deviated from measured by 2°C or less with the maximum deviations occurring under conditions of fog. This leads to the conclusion that the thermal model may be most valid for days with primarily direct solar radiation and clear nights where radiative cooling is occurring.

Oak-hickory canopy

- 76. Environmental data acquired at the Walker Branch site for the 48-hour period from 18-19 August 1979 were used to validate the thermal model for a deciduous oak-hickory canopy. Emissivities and thermal absorption coefficients for the three canopy layers were set to 1.0. Canopy resistance to water vapor diffusion was input as 0.07 min/cm and held constant. The input environmental and geometrical factor data for this canopy simulation are presented in Appendix D.
- 77. Figure 19 presents the three-layer canopy temperature predictions along with measured air temperature. Nighttime simulations were nearly equal to air temperature, but daytime predictions varied by a maximum of 2° C over air temperature.
- 78. Measured temperatures were compared to predicted results for layer 2 and are shown in Figure 20. The agreement between model and measured temperatures was quite good. The largest deviation (3° C) occurred in the afternoon; but morning and nighttime predictions varied by only 1° C or less.

Summary

79. The results of the model validation study indicate that the thermal canopy temperature model provided good estimates of actual temperatures for nighttime periods to within 2°C for both canopies studied. Daytime simulations generally underestimated measured temperatures for Douglas-fir and overestimated temperatures for cak-hickory. The results indicate that the model may not adequately account for energy transfers under foggy or very hazy conditions.

PART V: RECOMMENDATIONS

80. Two broad directions for further research and development are suggested in the paragraphs below. The first set of tasks represent logical extensions or improvements to the thermal model utilized in this study. Also, a not-quite-so-obvious extension to the calculation of the geometrically dependent flux transfer matrices is outlined. The second thrust recommended for further development is concerned with parameter estimation techniques which can be used to estimate model parameters, control (or input) variables, and elements of the state vector itself. Two techniques are described. The first technique based on sensitivity functions is appropriate for the steady-state version of the model. The second method, based on the Kalman filter, is more appropriate for dynamic representation of the thermal model.

Model Improvements

- 81. The most urgent need for model improvement is to evaluate different theories for the height dependence of air temperature within the canopy and of the vertical profile for wind speed. It is particularly appropriate to examine those techniques which would yield these temperature and wind profiles from a few limited measurements. The structure of the current thermal model can easily include vertical variations in the two parameters; they are held constant for the want of better knowledge and for simplicity.
- 82. The utility of the model could be extended if a ground temperature module was included. Particularly for this extension it may be appropriate to develop a time-dependent version of the model to include heat storage effects.

- 83. A useful exercise, but of lesser priority, would be to systematically examine the alternative formulations expressed by various authors for different components of the energy budget equation; that is, evapotranspiration, sensible heat, and so forth. There is no clear rationale for selecting one expression over another. However, the separate expressions can be programmed and sensitivity analysis performed on the individual expressions.
- 84. Finally, further analysis of the structure of the geometrical matrices should be carried out to determine if either an analytical decomposition of the matrices into a leaf density (leaf area index) component and leaf slope distributions can be constructed. If an analytical decomposition is not possible, then numerical interpolation techniques should be investigated.
- 85. As an example, consider the expressions for the view factor matrix $\underline{VF}(i,0)$ where Θ_r is the zenith view angle and i=1,2,3,4 corresponds to contributions from the three vegetation layers and the ground surface:

$$\underline{VF}(i,\Theta_r) = [VF(1,r) \ VF(2,r) \ VF(3,r) \ VF(4,r)]^T$$

$$VF(1,\Theta_r) = 1 - P_0(1,r)$$

$$VF(2,\Theta_r) = P_0(1,r) \ (1 - P_0(2,r)$$

$$VF(3,\Theta_r) = P_0(1,r) \ P_0(2,r) \ (1 - P_0(3,r))$$

$$VF(4,\Theta_r) = P_0(1,r) \ P_0(2,r) \ P_0(3,r)$$

where:

 $P_0(i,\Theta) = e^{-LAI} g(i,\Theta) \sec \Theta$ LAI (i) = the mean leaf area index for layer i

g(i,0) = the mean canopy projection of vegetation layer i in the direction θ , depending only on the leaf slope distributions for layer i

86. A direct factorization is not apparent. However, particularly for large LAI a Taylor series expansion would yield a more tractable form. Alternately, LAI could be varied between 0 and 10 and numerical tables generated.

Parameter Estimation

- 87. Two different approaches are suggested for estimation of parameters, control vector inputs, and/or selected components of the unknown state vector, that is the average canopy temperature for the three different layers. One approach is more applicable to the steady-state conditions; the second approach is more appropriate for the time-dependent version of the model. In each case it is assumed that selected measurements of canopy temperatures are available for some time periods and that some of the parameters and control vector components are also known. A typical scenario would be that the top layer canopy temperature is measured over a diurnal cycle and that all parameters and input components are known except for the <u>S</u> matrix, the longwave flux transfer matrix. It is then desired to estimate the <u>S</u> matrix which depends on the geometrical properties of the canopy and evaluate the fit on a second diurnal cycle. Other scenario examples can be envisioned. In this section, general development of the two-parameter estimation techniques are indicated.
- 88. First, consider the steady-state situation where the model is given by the following equation:

$$\underline{F}(\underline{X},\underline{P},\underline{U}) = 0$$

where the symbols have the same meaning as given earlier. For this situation the parameter estimation technique of nonlinear systems as described by Durando and Leondes (1976) is recommended. For simplicitity

the \underline{U} vector is appended to the \underline{P} vector and the equation is reexpressed as:

$$F(X,P) = 0$$

Further, it is assumed that observation variables are the canopy temperature variable, x , directly. Given a known measurement, $\underline{X}_0\underline{F}(\underline{X},\underline{P})$ becomes a function of \underline{P} only. Assume an initial estimate of $\underline{P},\underline{P}_0$. Then $\underline{F}(\underline{X},\underline{P})$ can be expanded about \underline{P}_0 :

$$\underline{F}(\underline{X},\underline{P}) - \underline{F}(\underline{X}_0,\underline{P}_0) = \frac{\partial \underline{F}}{\partial \underline{P}_{\underline{P}} = \underline{P}_0} (\underline{P} - \underline{P}_0) + \underline{\varepsilon}$$
 (28)

For the steady-state formulation $\underline{F}(\underline{X},\underline{P})=0$; ε is the error vector. Iteration is continued until convergence, i.e.,

$$\underline{P}_{n+1} = \underline{P}_n + \delta \underline{P} \tag{29}$$

- 89. If observations are available for more than one time interval, the optimal \underline{P} is chosen which minimizes the sum of $\varepsilon^{\mathsf{T}}\varepsilon$ over all time intervals. More general formulations of this approach, including the use of a variable increment step size, are given in the paper by Durando and Leondes.
- 90. The second technique proposed is applicable to the time-dependent formulation of the thermal model given:

$$M \frac{\partial \underline{X}}{\partial \underline{T}} = \underline{F}(\underline{X}, \underline{P}, \underline{U}, \underline{T})$$
 (30)

where:

M = specific heat capacity of the system

T = time

The general approach recommended here is the use of the Kalman filter after first linearizing the system. Specifically,

$$\underline{X} = \underline{A} \underline{X} + \underline{B} \underline{U} + \underline{W} \tag{31}$$

$$Z = H X + V \tag{32}$$

where $\underline{X} = \partial \underline{X}/\partial T$ represents the dynamical equations of the system, A and B are expansion matrices, and W represents the modeling error.

- 91. \underline{Z} is the observation vector, which now permits transformation on the state vector (canopy temperature), and \underline{V} is the observation noise.
- 92. Kalman filtering on the state vector or on the augmented state vector, that is, after appending \underline{P} or \underline{U} to \underline{X} , is then given by the standard expressions (Friedland 1972):

$$\hat{X}_n = \tilde{X}_n + K_n \left(Z_n - H \tilde{X}_n \right) \tag{33}$$

$$\tilde{\chi}_{n} = \Phi_{n-1} \hat{\chi}_{n-1} \tag{34}$$

where:

$$K_n = \tilde{P}_n H_n^T (H_n \tilde{P}_n H_n^T + V_n)^{-1}$$
 (35)

$$\tilde{P}_{n} = \Phi_{n-1} \hat{P}_{n-1} + B_{n-1} W_{n} B_{n-1}^{T}$$
 (36)

$$\hat{P}_{n} = (I - K_{n} H_{n}) \tilde{P}_{n}$$
 (37)

- Φ is the transition matrix for the system, n represents the discrete time interval, and \tilde{X} describes the model predictions.
- 93. An additional $\hat{\underline{X}}_0$, $\hat{\underline{P}}_0$ is required if many time intervals are available, e.g., a diurnal cycle; however, the final estimates are insensitive to these values.

REFERENCES

- Burden, R.L., J.D. Faires, and A.C. Reynolds. 1978. <u>Numerical Analysis</u>. Prindle, Weber, and Schmidt, Boston, Mass.
- Colwell, C.E. 1969. Seasonal change in foliar reflectance of five broadleaved forest species. Ph.D. Thesis, University of Michigan, Ann Arbor, 112 pp.
- deWit, C.T. 1965. Photosynthesis of Leaf Canopies. Agr. Res. Pap. 663, Wageningen, Netherlands. pp. 1-57.
- Durando, A. and C.T. Leondes. 1976. Parameter Estimation of Nonlinear, Time-Variant Systems by the Method of Sensitivity Functions. Compt. and Elect. Eng. 3:421-424.
- Friedland, B. 1972. A Review of Recursive Filtering Functions. Spring Joint Computer Conference.
- Fritschen, L.J., L. Cox, and R. Kinerson. 1973. A 28-meter Douglas-fir in a Weighting Lysimeter. Forest Sci. 19:256-261.
- Hudson, R.D., Jr. 1969. Infrared System Engineering, Wiley, New York.
- Hutchison, B.A. 1977. Atmospheric Turbulence and Diffusion Laboratory Deciduous Forest Meteorology Research Program, An. Overview. Atmospheric Turbulence and Diffusion Laboratory, National Oceanic and Atmospheric Administration, Cont. File 77/1. 11 pp.
- Jarvis, P.G., G.B. James, and J.J. Landsberg. 1976. Coniferous forest. in: <u>Vegetation and the Atmosphere</u>, Vol 2 (J.L. Monteith, ed.) Academic Press, New York, 439 pp.
- Jensen, E.C. 1976. The Crown Structure of a Single Codominant Douglasfir. Master's Thesis, University of Washington, Seattle, Wash. 83 pp.
- Kimes, D.S., K.J. Ranson, J.A. Kirchner, and J.A. Smith. 1978. Modeling Descriptors and Terrain Modules. Final Report under contract DACW 39-77-C-0073, Environmental Laboratory, U.S. Army Engineer Waterways Experiment Station, Vicksburg, Mississippi, 125 pp.
- Kimes, D.S., J.A. Smith, and J.K. Berry. 1980. Extension of the Optical Diffraction Analysis Technique for Estimating Forest Canopy Geometry. Aust. J. Bot. 27:575-588.
- Kimes. D.S., J.A. Smith, and K.J. Ranson. 1979. Terrain Feature Canopy Modeling. Final Report under U.S. Army Research Office Grant DAAG29-78-G-0045. Colorado State University, Fort Collins, Colo.

- Kinerson, R. Jr., and L.J. Fritschen. 1971. Modeling a Coniferous Forest Canopy. Agr. Meteor. 8:439-445.
- Oliver, R.E., and J.A. Smith. 1974. A Stochastic Canopy Model of Diurnal Reflectance. Final Report, U.S. Army Research Office, Durham, N.C. DAHCO4-74-6001. 82 pp.
- Tomovic, R. 1963. <u>Sensitivity Analysis of Dynamic Systems</u>. McGraw-Hill, New York.
- Verhoef, W., and N.J.J. Bunnik. 1975. A Model Study on the Relations Between Crop Characteristics and Canopy Spectral Reflectance. NIWARS publication No. 33, 3 Kanaalweg Delft, The Netherlands, 89 pp.

Expressions for contribution coefficients ${\tt CONT}_{ij\ell}$ for sink layer i, source component j, and leaf slope index r; $P_o(i,r) = probability of gap for layer i and leaf slope index <math>\ell$.

Source		Sink Layer	
Layer	-	2	м
-	p _o ⁴ (1,r)	P _o (1,r) P _o ^½ (2,r)	P ₀ (1,r) P ₀ (2,r) P ₀ ¹² (3,r)
8	2(1-P ₀ ³ 2(1,r))	$P_0^{\frac{1}{2}}(2,r) - P_0^{\frac{1}{2}}(2,r) P_0(1,r)$	$P_0^{\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ } P_0(2,r) P_0(1,r)$
m	$p_0^{\frac{1}{2}}(1,r) - p_0^{\frac{1}{2}}(1,r) p_0(2,r)$	$2(1 - P_0^{\frac{1}{2}}(2,r))$	p ₃ ² (3,r) - p ₃ ² (3,r) p ₀ (2,r)
•	p, 3 (1,r) p (2,r) - p, 3 (1,r) p (2,r) p (3,r)	Pot(2,r) - Pot(2,r) Po(3,r)	$2(1 - P_0^{\frac{k_2}{2}}(3,r))$
v	Po*(1,r) Po(2,r) Po(3,r)	Po ³ (2,r) Po(3,r)	p, ^k (3,r)

Table 2

<u>Initial environmental and initial temperature data used</u>
<u>for sensitivity analyses for the Douglas-fir and oak-hickory canopies</u>

	Environmental Data						
Time hours	A _T o <u>c</u>	G _T	WS cm/s	RH	SWR ₂		
0600	10.6	10.7	136.0	0.72	0.0		
1100	18.2	19.0	110.0	0.84	299.7		

<u>Initial Temperatures</u>, ^OC

	Time hours	Layer 1	Layer 2	Layer 3
Douglas-fir	0600	9.0	10.1	10.1
	1100	18.4	18.2	18.2
Oak-hickory	0600	10.1	10.5	10.5
	1100	18.8	18.5	18.2

•

SOURCE SINK VARIABLE VARIABLE SKY J=1 I-1 **VEGETATION LAYER ONE** J=2 I=2 **VEGETATION LAYER TWO** J=3 I=3 J=4 **VEGETATION LAYER THREE** J=5 GROUND LAYER

•

Figure 1. Diagram showing sink and source variable indices used in in the model energy flow formulations

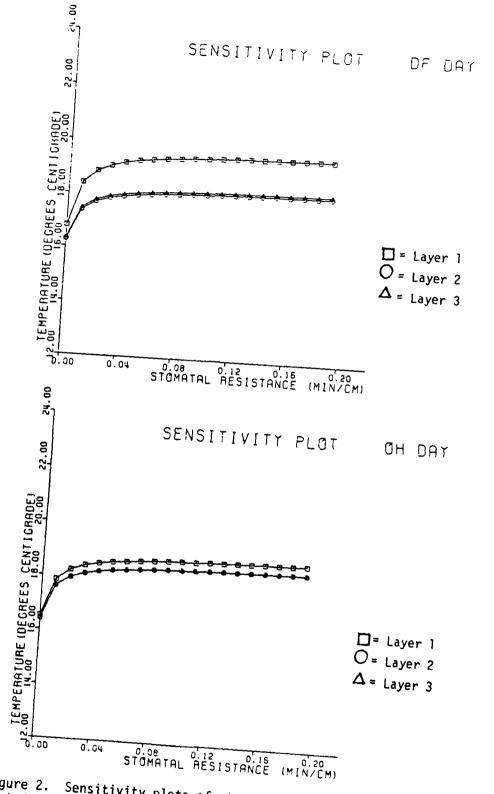


Figure 2. Sensitivity plots of stomatal resistance versus predicted canopy temperature for Douglas-fir (top) and Oak-hickory daytime analyses

1. 1. ...

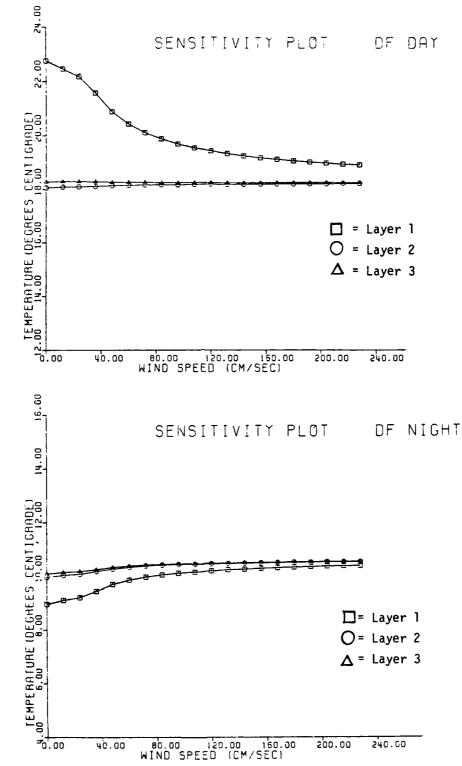


Figure 3. Sensitivity plots of wind speed versus predicted canopy temperature for Douglas-fir day and nighttime analyses

· . .

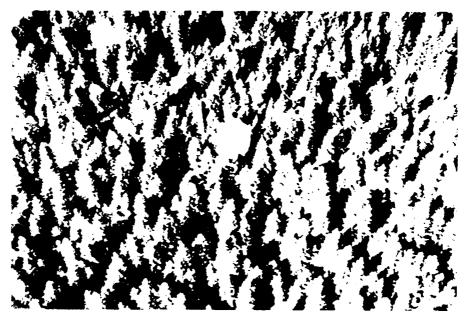


Figure 4. Aerial view of the Douglas-fir canopy at Cedar River, Washington, site; object in center of photograph is a greenhouse enclosure over the lysimeter tree; structure not in place at the time of the experiments (photo courtesy of Leo J. Fritschen)

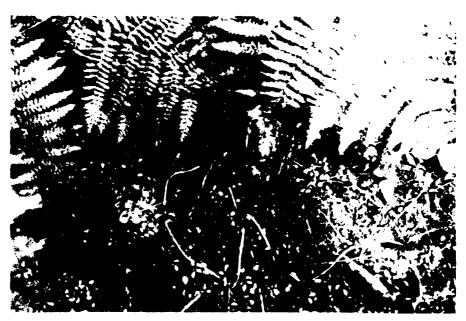


Figure 5. Typical ground cover at the Cedar River site

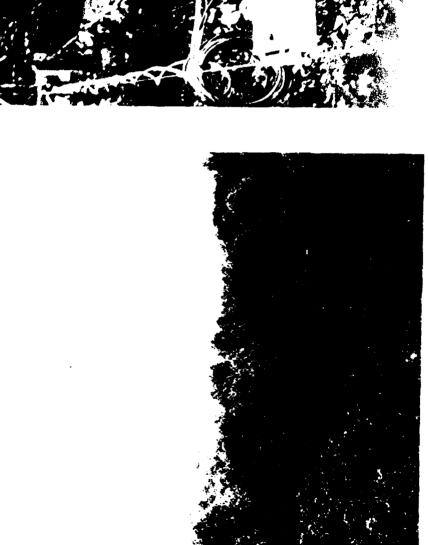
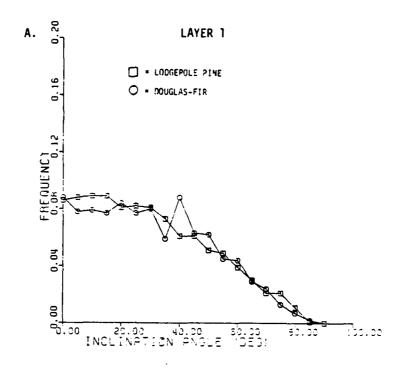


Figure 6. Oblique view of deciduous canopy at Walker Branch site showing height variations of tree crowns



Figure 7. Ground cover at Walker Branch site consisting primarily of litter and seedling trees; the cart (center) is mounted on a tram system and measured shortwave and photosynthetically active radiation at bottom of canopy



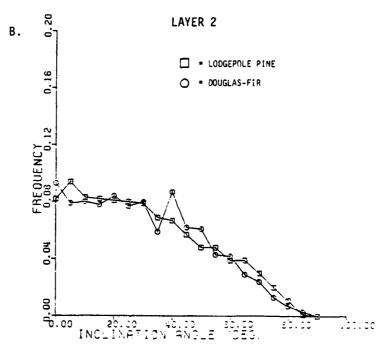


Figure 8. Comparative plots of foilage angle frequency for Douglas-fir and lodgepole pine. A) Layer 1, B) Layer 2 and C) Layer 3 (Continued)

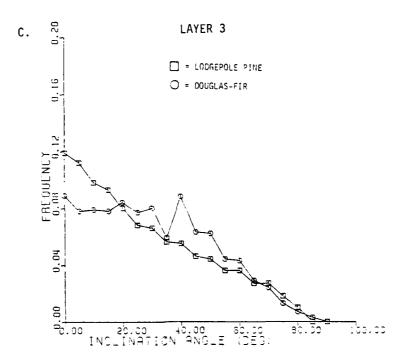


Figure 8. Concluded.

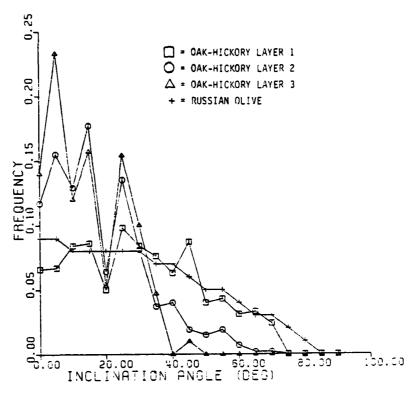


Figure 9. Foilage inclination angle frequency plots for the three layer oak-hickory canopy and a one-layer Russian olive canopy.

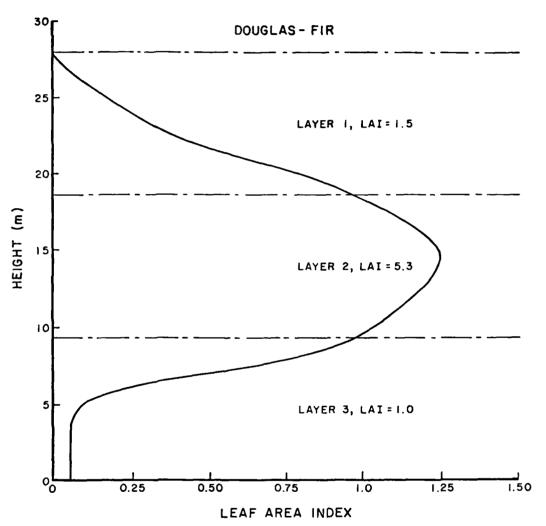


Figure 10. Leaf area index distribution for the Douglas-fir canopy

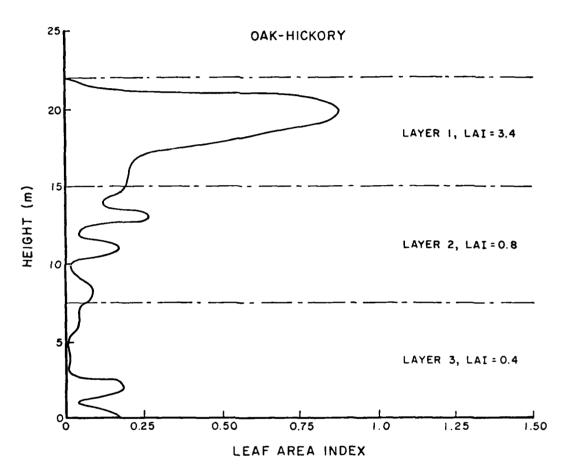


Figure 11. Leaf area index distribution for the oak-hickory canopy

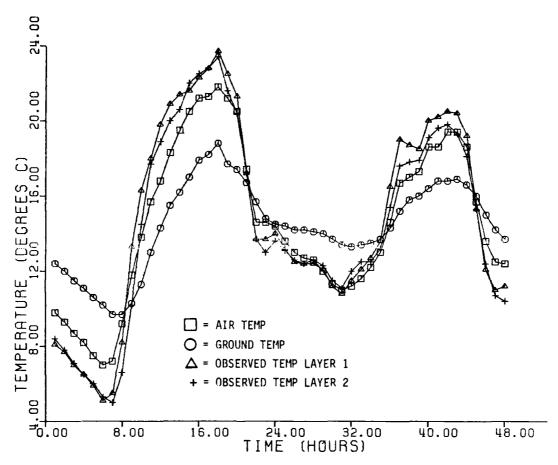


Figure 12. Measured average layer needle temperatures for Douglas-fir plotted with air and ground temperatures for a 48-hour period from August 4 to August 5, 1979; layer 1 and layer 2 needle temperatures measured at 26 m and 20 m respectively

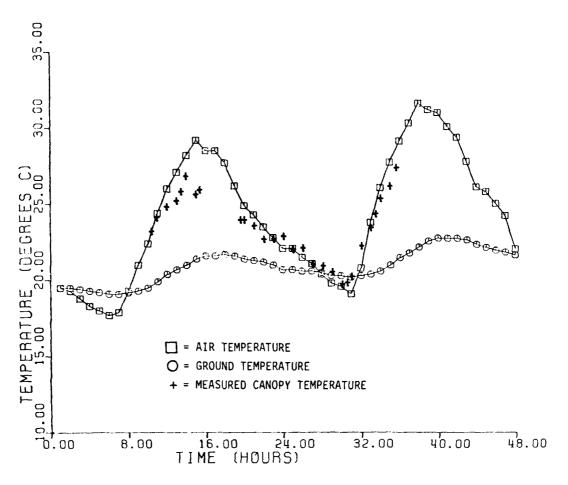


Figure 13. Measured average canopy temperature for oakhickory plotted with air and ground temperatures for a 48-hour period from August 18 to August 19, 1979; canopy temperatures measured intermittently from 1100 hours on August 18 to 1200 hours on August 19 with a hand-held thermal radiometer

1

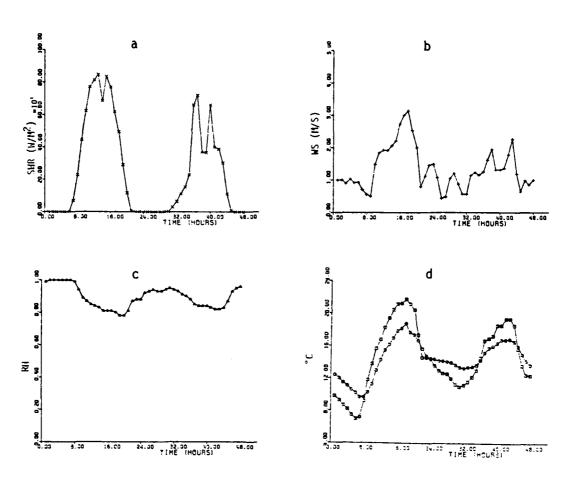


Figure 14. Plots of thermal model environmental input parameters for the Cedar River site from 0000 hr 4 August 1979 to 2400 hr 5 August 1979: a) Global shortwave radiation (SWR), b) Wind speed (WS), c) Relative humidity as estimated from wet and dry bulb temperatures, and d) air temperature () and ground temperature ()

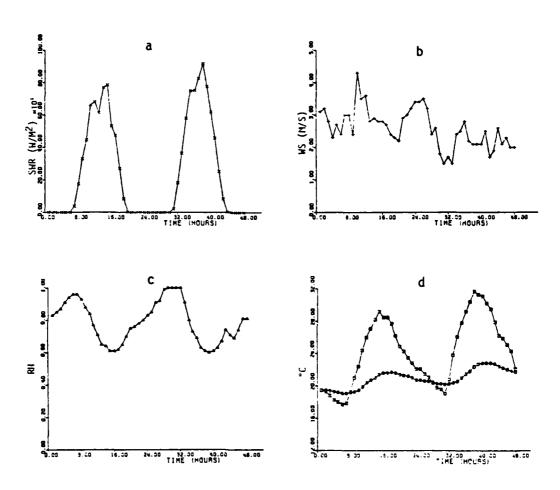


Figure 15. Plots of thermal model environmental input parameters for Walker Branch Site: a) Global shortwave radiation (SWR), b) Wind speed (WS), c) Relative humidity as estimated from wet and dry bulb temperatures, and d) air temperature () and ground temperature ()

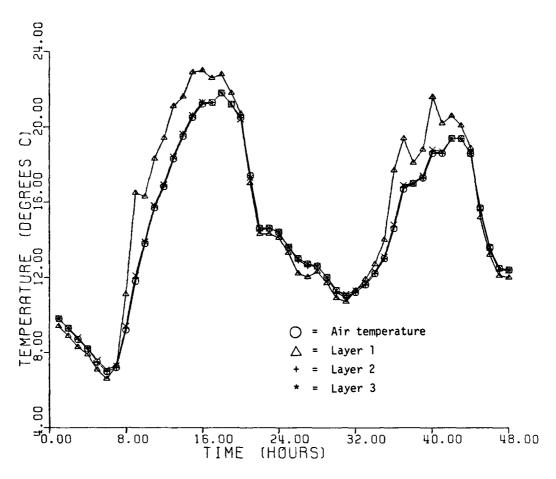


Figure 16. Simulation results for the three-layer Douglasfir canopy plotted with air temperature for the 48-hour time period from 4-5 August 1979

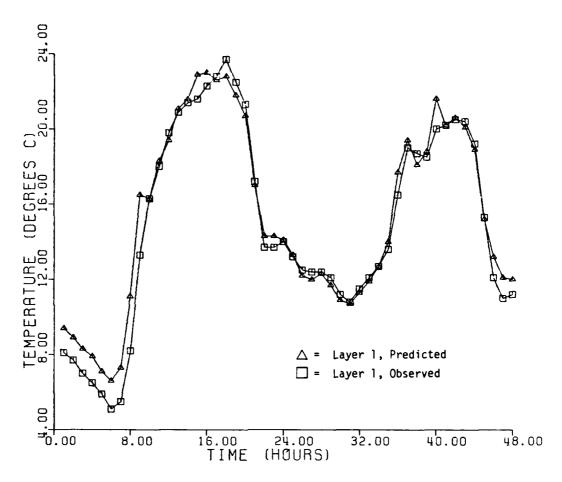


Figure 17. Layer 1 predicted temperatures plotted with average temperatures measured at the 26-m level in the Douglas-fir canopy

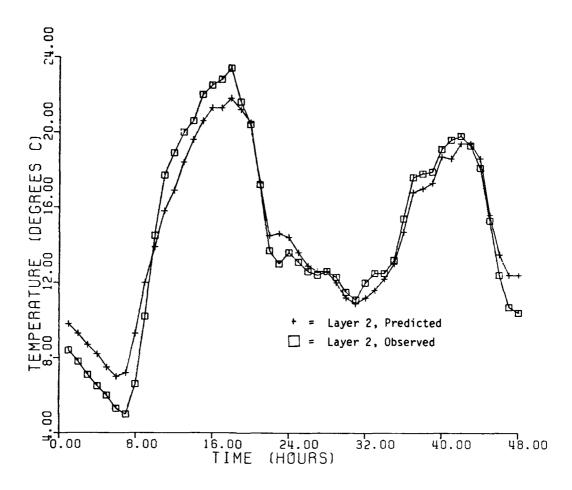


Figure 18. Layer 2 predicted temperature plotted with average temperatures measured at the 20-m level in the Douglas-fir canopy

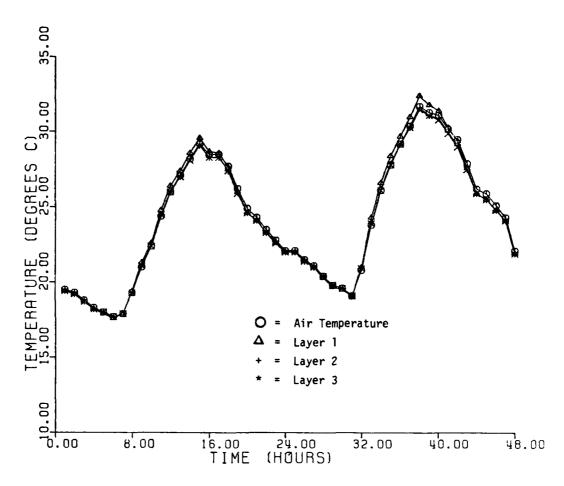


Figure 19. Simulation results for the three-layer oak-hickory canopy plotted with air temperatures for the 48-hour period from 18-19 August 1979

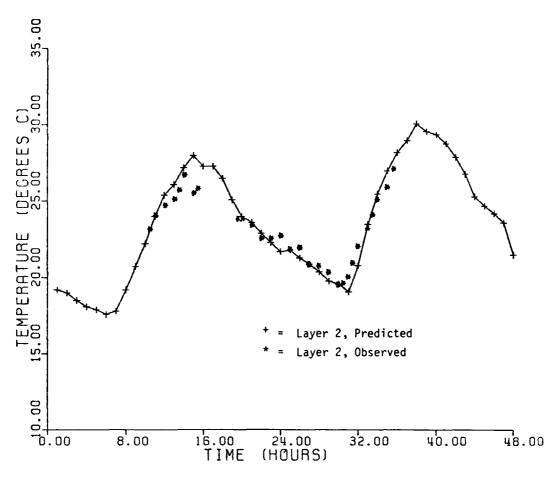


Figure 20. Layer 2 predicted temperature plotted with measured average temperature of oak-hickory canopy; measurements made with a thermal infrared radiometer

APPENDIX A: PROGRAM LISTINGS

TMODEL

```
PROGRAM THODEL1(INPUT,OUTPUT,TAPE5=INPUT,TAPE6=OUTPUT,
     1TAPE1, TAPE2, TAPE3)
COMMON/PARA1/SIG, STA(3), S(3,3), STG(3), X(3), A(3), U(4,9),
     1ALP(3), FHU, TA, TAC, TG, EPS(3), EPSTG, RH, RL
      COMMON/PARA2/BTA, BTG, BX(3), DBX(3), QX(3), DQX(3), RX(3), DRX(3)
      COMMON/ESTIM/FX(3),DFX(3,3)
      COMMON/SENSOR/ERT(9), ERTH(3), EX(9), EXH(3)
        DIMENSION DX(3), SABS(3)
C
C
                          TOL=.00001
      SIG=5.6686E-8 $
C
          READ CANOPY GEONETRY MATRICES
C
             FROM TAPE 2
C
C
C
      READ(2,203) TITLE1,TITLE2,TITLE3
      URITE(3,203)TITLE1,TITLE2,TITLE3
           READ W MATRIX: SENSOR VIEW ANGLE WEIGHTS
C
C
      DO 2001 N=1.4
        READ(2,202) (U(N,J),J=1,9)
 2001 CONTINUE
     -- READ S MATRIX: LW FLUX TRANSFERS
 C
 C
       DO 2000 I=1,3
       READ(2,202)STA(I),(S(I,J),J=1,3),STG(I)
 2000 CONTINUE
 C
           READ ABS: SW FLUX
 C
 C
       FORMAT(9F7.4)
 202
       READ(2,202) (SABS(N),N=1,3)
       FORMAT(1X,3A10)
 203
           DEFINE NOMINAL VALUES FOR MODEL PARAMAMETERS
 C1000 FORMAT(14,4F5.0,2X,F5.0)
 C1000 FORMAT(14,2F7.2,2F6.2,2X,F10.2)
       ALP(1)=1.0
        ALP(2)=1.0
        ALP(3)=1.0
        EPS(1)=1.0
        EPS(2)=1.0
        EPS(3)=1.0
        EPST6=1.0
```

```
C
C
          READ-IN THE NUMBER OF SINULATION PERIODS
C
      PRINT 201
  201 FORMAT(//, * ENTER THE NUMBER OF SINULATION PERIODS DESIRED*/)
      READ*, NSIN
        READ IN CANOPY RESISTANCE ---
      PRINT 219
  219 FORMAT(/, *ENTER THE CANOPY STOMATAL RESISTANCE FOR THIS RUM*/)
      READ*, RL
      WRITE(6,600)
  600 FORMAT(1H ,4HTIME,4X,3HSWR,15X,1HA,31X,1HB,31X,1HH,23X,2HLE)
      WRITE(6,602)
  602 FORHAT(1H ,17X,1H1,7X,1H2,7X,1H3,7X,1HA,7X,1H1,7X,1H2,7X,1H3,7X,
     .1H6,7X,1H1,7X,1H2,7X,1H3,7X,1H1,7X,1H2,7X,1H3)
         CONTINUE
      DO 100 NTIME=1,NSIM
      READ(1, *) ITINE, TA, TG, FNU, RH, GLB
C.... CONVERT FAU IN M/SEC TO CM/SEC....
      FNU = FNU+100.
      A(1)=GLB+SABS(1)
                              A(2)=GLB+SABS(2)
                                                   $A(3) = GLB*SABS(3)
      TAC=TA
      DO 90 I=1.3
90
      X(I)=TA
  50 CALL FEVAL
      DO 20 I=1.3
   20 FX(I) = -FX(J)
      CALL SOLVE(FX,3,DFX,3,DX)
      DO 30 I=1,3
   30 \times (I) = \times (I) + B \times (I)
      DO 40 I=1,3
      DEV=DX(I)
      IF(ABS(DEV) .GT. TOL) GO TO 50
   40 CONTINUE
       CALL WATTS
      URITE(3,80) ITIME, TA, TG, (ERTH(J), J=1,3)
   80 FORMAT(1H ,110,2F7.2,3F6.1)
   95 FORMAT(110,4F10.5)
      BTA=BTA+SIG $ BX(1)=BX(1)+SIG $BX(2)=BX(2)+SIG $ BX(3)=BX(3)+SIG
      BTG=BTG*SIG
С
      WRITE(6,604)ITIME,GLB,(A(I),I=1,3),BTA,(BX(I),I=1,3),BTG,(QX(I),
     .I=1,3),(RX(I),I=1,3)
  604 FORMAT(1H ,14,15F8.2)
  100 CONTINUE
      STOP
      END
      SUBROUTINE FEVAL
C
      CONHON/PARA1/SIG,STA(3),S(3,3),STG(3),X(3),A(3),U(4,9),
     1ALP(3), FMU, TA, TAC, TG, EPS(3), EPSTB, RH, RL
      COMMON/PARA2/BTA, BTG, BX(3), DBX(3), QX(3), DQX(3), RX(3), DRX(3)
```

```
COMMON/ESTIM/FX(3),DFX(3,3)
C
      CALL FBTA(TA, 3TA)
      CALL BRUNC(EPSTG, TG, BTG, DBTG)
      DO 10 I=1,3
      CALL Brunc(EPS(I),X(I),3X(I),DBX(I))
      CALL GFUNC(X(I), TAC, FNU, QX(I), DQX(I))
      CALL RFUNC(X(I), TAC, FNU, RL, RH, RX(I), DRX(I))
   10 CONTINUE
      DO 20 IL=1.3
   20 FX(IL)=0.5*ALP(IL)*SIG*(BTA*STA(IL)+3X(1)*S(IL,1)+BX(2)*
     15(IL,2)+BX(3)+S(IL,3)+BTG+STG(IL))+A(IL)-SIG+BX(IL)+QX(IL)
     2+RX(IL)
      DO 30 I=1,3
      DO 30 J=1,3
   30 DFX(I,J)=0.
      DO 40 IL=1,3
      DO 40 J=1.3
      IF(J.NE.IL) GO TO 35
      DFX(IL,J)=0.5+ALP(IL)+SIG+DBX(J)+S(IL,J)-SIG+DBX(IL)+DQX(IL)+
     1DRX(IL)
      GO TO 40
   35 DFX(IL.J)=0.5+ALP(IL)+SIG+DBX(J)+S(IL.J)
   40 CONTINUE
      RETURN
      END
      SUBROUTINE BFUNC(EPSI,XI,3XI,DBXI)
C
      BXI=EPSI+(XI+273.0) ** 4,
      DBXI=4. *EPSI * (XI+273.0) **3.
      RETURN
      END
      SUBROUTINE FBTA(TA,3TA)
C
      EPSTA=1.-0.261 * EXP(-7.77E-4 * TA * TA)
      CALL BFUNC(EPSTA, TA. BTA, DBTA)
      RETURN
      END
      SUBROUTINE OFUNC(XI, TAC, FNU, QXI, DQXI)
C
      IF(FMU.6T.30.) GO TO 10
      HC=0.69775*(20.4+0.2*FHU**0.97)
      GO TO 20
   10 HC=0.69775*(0.95*FHU**0.97)
   20 QXI=(XI-TAC) + (-HC)
```

```
DQXI=-HC
      RETURN
      END
      SUBROUTINE RFUNC(XI, TAC, FNU, RL, RH, RXI, DRXI)
C
      RNUN=FEX(XI) +1.0E-6-RH+FEX(TAC) +1.0E-6
      RDEN=RL+(1./60.)+(0.04+1.27+FMU++(-0.5))
      RXI1=-697.75*(-0.566*XI+597.3)
      RXI2=RNUM/RDEN
      RXI=RXI1*RXI2
      DRXI=697.75+0.566+RXI2+RXI1+(0.056715E-6+FEX(XI))/RBEN
      RETURN
      SUBROUTINE INVERSE(A, N, D)
C
C
          INVERT A 3*3 REAL MATRIX A WHOSE DETERMINANT IS D
C
          THE RESULT WILL BE STORED IN A
C
      DIMENSION A(3,3), 3(3,3)
C
      B=A(1,1)*A(2,2)*A(3,3)+A(1,2)*A(2,3)*A(3,1)+A(1,3)*A(2,1)*
     1A(3,2)-A(3,1)*A(2,2)*A(1,3)-A(1,1)*A(3,2)*A(2,3)-A(2,1)*
     2A(1,2)*A(3,3)
      B(1,1)=(A(2,2)*A(3,3)-A(2,3)*A(3,2))/D
      B(1,2)=-(A(2,1)*A(3,3)-A(2,3)*A(3,1))/B
      B(1,3)=(A(2,1)*A(3,2)-A(2,2)*A(3,1))/B
      B(2,1)=-(A(1,2)*A(3,3)-A(1,3)*A(3,2))/D
      B(2,2)=(A(1,1)*A(3,3)-A(1,3)*A(3,1))/D
      B(2,3)=-(A(1,1)*A(3,2)-A(1,2)*A(3,1))/D
      B(3,1)=(A(1,2)*A(2,3)-A(1,3)*A(2,2))/D
      B(3,2)=-(A(1,1)+A(2,3)-A(1,3)+A(2,1))/B
      B(3,3)=(A(1,1)*A(2,2)-A(1,2)*A(2,1))/B
      DO 10 I=1.3
      DO 10 J=1.3
   10 A(I,J)=B(I,J)
      RETURN
      END
      FUNCTION FEX(XI)
C
      XX=5.2342*EXP(0.056715*XI)
      FEX=XX
      RETURN
      SUBROUTINE SOLVE(Y,N,A,H,X)
C
```

```
C
      DIMENSION Y(N), A(N, N), X(N), ATA(N, N), ATY(N)
      DIMENSION Y(3), A(3,3), X(3), ATA(3,3), ATY(3)
C
      DO 10 I=1,H
      DO 10 J=1, M
      ATA(I,J)=0.
      DO 10 K=1,N
   10 ATA(I,J)=ATA(I,J)+A(K,I)#A(K,J)
      CALL INVERSE(ATA, M, D)
      DO 20 I=1,H
      ATY(I)=0.
      DO 20 J=1.N
   20 ATY(I)=ATY(I)+A(J,I)*Y(J)
      DO 30 I=1.N
      X(I)=0.
      DO 30 J=1.X
   30 \times (I) = X(I) + ATA(I, J) + ATY(J)
      RETURN
      END
      SUBROUTINE WATTS
      CONHON/PARA1/SIG, STA(3), S(3,3), STG(3), X(3), A(3), W(4,9),
     1ALP(3), FMU, TA, TAC, TG, EPS(3), EPSTG, RH, RL
      COMMON/SENSOR/ERT(9), ERTH(3), EX(9), EXH(3)
C
      DO 1 N=1,3
      EXH(N)=EPS(H)+SIG+(X(N)+273.)++4
      ERTH(N)=((EXH(N)/SIG)**0.25) - 273.
      CONTINUE
C
      DO 2 J=1,9
      EX(J)=SIG+EPS(1)+W(1,J)+(X(1)+273.)++4+
     1SIG+EPS(2)+W(2,J)+(X(2)+273.)++4+
     2SIG*EPS(3)*W(3,J)*(X(3)+273.)**4+
     3SIG*EPSTG*W(4,J)*(T6+273.)**4
      ERT(J)=((EX(J)/SIG)**0.25)-273.
2
      CONTINUE
      RETURN
      END
```

SCALC

```
PROGRAM SCALC(INPUT, DUTPUT, TAPE5=INPUT, TAPE6=OUTPUT, TAPE1, TAPE2,
     .TAPE3)
C...THIS PROGRAM IS EXTRACTED FROM THE TOSM MODEL BY KIMES TO
C...CALCULATE THE SENSOR VIEW WEIGHTING MATRIX W AND THE LONGWAVE
C...RADIATION EXCHANGE MATRIX S FOR A GIVEN CANOPY GEOMETRY.
C...REQUIRED INPUTS ARE LEAF INCLINATION ANGLE AND CORRESPONDING
C...FREQUENCY, CANOPY DENSITY (SLAI) AND LEAF AREA INDEX (FLAI)
C...FOR EACH OF THREE CANDPY LAYERS.
C
      COMMON /A/ WV,RH,RL,D(3)
      COMMON /B/ PGAP(3,9), PHIT(3,9), PGAP2(3,9), PHIT2(3,9), STEF
      COMMON/C/COSTA(9,9,18), EMISSV(4), ABSORB(3), ESKY, EGRD, SECTAR(9)
      COMMON/D/CONT(3,5,9),C(3,5,9), SUNT(3,9), KELV, GT, NUSIM, ITIME
      COMMON/E/AT, THETA(9), PHI(18), XLF(9), YLF(9), ZLF(9), XS(9,18)
      COMMON/F/YS(9,18),ZS(9), CEDTR, B, FREQB(9,3), WA(15),EPS
      COMMON/G/NSIG,N, ITHAX
      COHNON /H/ INDEX1.TITLE(8)
      COHKON /I/ X(3)
      COMMON /J/ THERM, THHLEX, CONVEC, TRANS
      COHHON/S/ ARSOL(3)
C...READ AND ASSIGN THE INPUT BATA
      NUSIM=-1
      INDEX1=0
   76 IF (INDEX1.EG.NUSIM) STOP
      CALL INPUTDA
      IF (INDEX1.GT.1) GO TO 95
C
  .. CALCULATE THE CANOPY GEOMETRY COEFFICIENTS
      CALL CANGEDH
      CALL WHAT (TITLE)
C...CALCULATE THE SIN THETA FACTORS FOR ALL SOURCE ANGLE-LEAF ANGLE
   PURMUTATIONS.
C
      CALL BEVANG
```

```
C...CALCULATE THE NORMALIZING FACTOR FOR THE RELATIVE SIZES OF SOURCE SECTORS
      CALL SECTOR
   95 CONTINUE
C...CALCULATE THE THERHAL RADIATION COEFFICIENTS
      CALL SETUP
C...CALCULATE THE AVERAGE LEAF TEMPERATURE WITHIN EACH LAYER.
C
C...DISPLAY THE OUTPUT
      CALL BUTDAT
      GO TO 76
      END
      SUBROUTINE INPUTDA
C
C...SUBROUTINE INPUTDA READS AND ASSIGNS THE INPUT DATA
C
C
      COMMON/GED/ PHIT1(3,9),FLAI(3,1),SLAI(3,1),AXLFA(19,3),AYLFA(19,3)
      COMMON /A/ UV,RH,RL,D(3)
      COHMON /B/ PGAP(3,9), PHIT(3,9), PGAP2(3,9), PHIT2(3,9), STEF
      COMMON/C/COSTA(9,9,18), EMISSV(4), ABSORB(3), ESKY, EGRD, SECTAR(9)
      COMMON/D/CONT(3,5,9),C(3,5,9), SUNT(3,9), KELV, GT, NUSIK, ITIME
      COMMON/E/AT, THETA(9), PHI(18), XLF(9), YLF(9), ZLF(9), XS(9,18)
      COMMON/F/YS(9,18),ZS(9), CEDTR, B, FREQD(9,3), WA(15),EFS
      COMMON/G/NSIG.N. ITHAX
      COMMON /H/ INDEX1, TITLE(8)
      COMMON /I/ X(3)
      COMMON /J/ THERM, THALEX, CONVEC, TRANS
      COMMON /N/ STOR(3)
      COMMON/S/ ABSOL(3)
£
C...TEST FOR THE SIMULATION NUMBER AND SKIP TO THE APPROPRIATE INPUT DATA
      IF (INDEX1.EQ.0) GO TO 99
      IF (INDEX1.EQ.NUSIN) STOP
   99 CONTINUE
C...ASSIGN THE STEFFAN BOLTZMANN CONSTANT WATTS/M**2*K**4
      STEF=5.6686E-8
```

```
C...ASSIGN THE CONVERSION FACTOR FOR KELVIN-DEGREES
      B = 273.0
C...READ THE AVERAGE THERMAL EMISSIVITY COEFFICIENTS FOR THE 3 VEGETAION LAYERS
     (1,2,3) AND THE GROUND(4).
      READ(1,199)(TITLE(N),N=1,8)
      IF(EDF(1).NE.O.)STOP
  199 FORMAT(8A10)
С
C
C
C...READ THE CANOPY GEOMETRY FREQUENCY DISTRIBUTIONS OF THE ELEMENTS
    IN LAYERS 1,2,3. AXLFA REPRESENTS THE INCLINATION ANGLES 0-90
    (5 DEGREE INTERVALS) AND AYLFA REPRESENTS THE CORRESPONDING
    FREQUENCY. SLAI AND FLAI ARE EACH LAYERS S PARAMETER AND LAI
    RESPECTIVELY.
C
C
      DO 190 I=1,3
      READ(1, *)(AXLFA(N, I), AYLFA(N, I), N=1, 19)
      READ(1,*)SLAI(I,1),FLAI(I,1)
  190 CONTINUE
  101 FORMAT (8F10.5)
      RETURN
      ENF
      SUBROUTINE OUTDAT
C...SUBROUTINE OUTPUT FORMATS THE DATA TO BE DISPLAYED.
C
      COMMON/SENS/ ELAYT(9), ELAYH(3), ERTT(9), ERTH(3)
      COMMON/GEO/ PHIT1(3,9), FLAI(3,1), SLAI(3,1), AXLFA(19,3), AYLFA(19,3)
      COMMON /A/ WV.RH.RL.D(3)
      CONMON /B/ PGAP(3,9), PHIT(3,9), PGAP2(3,9), PHIT2(3,9), STEF
      COMMON/C/COSTA(9,9,18), EMISSV(4), ABSORB(3), ESKY, EGRD, SECTAR(9)
      COMMON/D/CONT(3,5,9),C(3,5,9), SUMT(3,9), KELV, GT, NUSIM, ITIME
      COMMON/E/AT.THETA(9).PHI(18).XLF(9). YLF(9). ZLF(9). XS(9.18)
      COMMON/F/YS(9,18),ZS(9), CEDTR, B, FREQD(9,3) , WA(15),EPS
      COMMON/G/NSIG,N, ITHAX
      COMMON /H/ INDEX1.TITLE(8)
```

```
CONNON /I/ X(3)
      COMMON /J/ THERM, THMLEX, CONVEC, TRANS
      COMMON /K/ TT1(3).TT2(3),TT3(3),TT4(3)
      COHNON /N/ STOR(3)
      COMMON /L/ TEMP(3)
      COMMON/S/ ABSOL(3)
      DIMENSION S(3,5)
C
C...WRITE THE CALCULATED GEOMETRY FOR EACH LAYER
      DO 319 I=1,3
      WRITE(2,320) I
  320 FORMAT (///,* THE COMPONENT ANGLE COMPUTATIONS FOR LAYER *.11./)
      WRITE(2,321) FLAI(I,1), SLAI(I,1)
  321 FORMAT ( * LAI = *,F4.2,4X,* S= *,F4.2,/)
      URITE(2,322) (AXLFA(N,I),AYLFA(N,I),N=1,19)
  322 FORMAT( * XLFA, YLFA *,/,(2X,16F8.3))
      WRITE(2,323) (PGAP(I,M), N=1,9)
  323 FORMAT(//, * PGAP FOR 1-9 INCLINATION INTERVALS*, 9F8.3)
  319 CONTINUE
C...WRITE THE CALCULATED THERNAL CONTRIBUTIONS COEFFICIENTS
      WRITE(2,302)
  302 FORMAT(1X,/,* THE PROPORTION OF RADIANCE AREA CONTRIBUTED BY
     $4 SECTOR OF THE 9 BANDS(1-9) DIVIDED BY 18 (SECTORS) ARE=≠./)
      WRITE(2,303)(SECTAR(I),I=1,9)
  303 FORMAT(10X,9F10.5,//)
      WRITE(2,40)
  40 FORMAT (1X,//,* THE BAND-PGAP-PHIT-COEFFICIENTS FOR THE THERNAL RA
     +DIATION TRANSFERS ARE =*,/)
      DO 39 I=1,3
      URITE(2,41) I
   41 FORMAT (1X.* THE 9 BAND COEFFICIENTS TO LAYER *, 11, * ARE*)
      DO 39 J=1,5
      WRITE (2,42) J, (CONT(I, J, H), H=1,9)
   42 FORMAT(8X, * FROM LAYER*, 11, 2X, 9F6.4)
  39 CONTINUE
      WRITE(2,50)
  50 FORMAT (1x,///,* THE FINAL THERMAL RADIATION COEFFICIENTS ARE AS FOLLOWS
     +*,/)
      DO 49 MXX=1,3
      DO 49 NXX = 1.5
      S(MXX, NXX) = 0.0
```

```
49 CONTINUE
      DO 51 I=1,3
      WRITE(2,52) I
  52 FORMAT (1x, * THE THERNAL RADIATION CONTRIBUTION TO LAYER *, 11, * FO
     +R EACH OF THE 9 LEAF INCLINATIONS ARE*)
      DO 51 J=1,5
      WRITE (2,53) J, (C(I,J,N), H=1,9)
      DO 51 K=1.9
      S(I,J) = S(I,J)+C(I,J,K)*FREQD(K,I)
   53 FORMAT (8x,* FROM LAYER*, I1, 2x, 9E10.3)
   51 CONTINUE
      100 55 IXX = 1.3
      URITE(3,505)(S(IXX,JXX),JXX≈1,5)
      FORMAT(5F7.4)
      WRITE(6,503)(S(IXX,JXX),JXX=1,5)
  503 FORMAT(1H ,5F10.4)
  55 CONTINUE
      RETURN
      END
      SUBROUTINE SETUP
C
C...SUBROUTINE SETUP PRE-CALCULATES AND PRE-ARRANGES MANY OF THE THERMAL
   COEFFICIENTS NEEDED FOR THE FINAL ENERGY BUDGETS WHICH ARE PLACED INTO THE
    ZSYSTH ROUTINE.
C
C
      COMMON /A/ NV,RH,RL,D(3)
      COMMON /B/ PGAP(3,9), PHIT(3,9), PGAP2(3,9), PHIT2(3,9), STEF
      COMMON/C/COSTA(9,9,18), EMISSV(4), ABSORB(3), ESKY, EGRD, SECTAR(9)
      COMMON/D/CONT(3,5,9),C(3,5,9), SUKT(3,9), KELV, GT, NUSIK, ITIME
      COMMON/E/AT, THETA(9), PHI(18), XLF(9), YLF(9), ZLF(9), XS(9,18)
      COHHON/F/YS(9,18),ZS(9), CEDTR, B, FREQD(9,3), WA(15),EPS
      COMMON/G/NSIG.N. ITMAX
      COMMON /H/ INDEX1.TITLE(8)
C
C...FOR EACH LAYER CALCULATE THE BAND-PGAP-PHIT COEFFICIENTS NEEDED FOR EACH
    LAYERS THERNAL RADIATION CONTRIBUTION TO A SPECIFIC LAYER.
C
C
      DO 20 I=1,9
C
C
C...CONTRIBUTION COEFFICIENTS TO LAYER 1
```

```
C
C....FROM SKY
      CONT(1,1,1) = PGAP2(1,1)
C....FRON LAYER 1
      CONT(1,2,1)= 2.*PHIT2(1,1)
C....FROM LAYER 2
      CONT(1,3,1) = PGAP2(1,1) - PGAP2(1,1) + PGAP(2,1)
C
C....FROM LAYER 3
      CONT(1,4,I) = PGAP2(1,I) * PGAP(2,I) - PGAP2(1,I) * PGAP(2,I) * PGAP(3,I)
C
C....FRON GROUND
      CONT(1,5,I) = PGAP2(1,I) * PGAP(2,I) * PGAP(3,I)
C...CONTRIBUTION COEFFICIENTS TO LAYER 2
C....FROM SKY
      CONT(2,1,1)= PGAP(1,1)*PGAF2(2,1)
C....FRON LAYER 1
С
      CONT(2,2,1) = PGAP2(2,1)-PGAP2(2,1)*PGAP(1,1)
  ....FROM LAYER 2
      CONT(2,3,1)= 2.*PHIT2(2,1)
C....FROM LAYER 3
      CONT(2,4,1) = PGAP2(2,1)-PGAP2(2,1)+PGAP(3,1)
ε
C....FRON GROUND
      CONT(2,5,1) = PGAP2(2,1) * PGAP(3,1)
```

```
C
C...CONTRIBUTION COEFFICIENTS TO LAYER 3
C....FROM SKY
      CONT(3,1,1) = PGAP(1,1) + PGAP(2,1) + PGAP2(3,1)
C....FRON LAYER 1
      CONT(3,2,1) = PGAP2(3,1) + PGAP(2,1) - PGAP2(3,1) + PGAP(2,1) + PGAP(1,1)
C....FROM LAYER 2
      CONT(3,3,I) = PGAP2(3,I) - PGAP2(3,I) + PGAP(2,I)
C....FRON LAYER 3
      CBNT(3.4,1)= 2.*PHIT2(3,1)
C....FROM GROUND
      CONT(3,5,I) = PGAP2(3,I)
   20 CONTINUE
C...NOW FORK THE EQUATION COEFFICIENTS FOR THE CONTRIBUTED THERMAL RADIANT
    ENERGY TO EACH LAYER AND FOR EACH LEAF INCLINATION ANGLE WITHIN A LAYER.
C
      CALL SET03(C,3,5,9)
C...THERNAL RADIATION CONTRIBUTION TO LAYER N
      DO 30 N=1,3
C...FOR EACH LEAF INCLINATION ANGLE INTERVAL
      BO 30 I= 1,9
C...SUK EACH SECTORS RADIATION CONTRIBUTION (9 BANDS CONTAINING 18 SECTORS)
      DO 30 J=1,9
      DO 30 K=1,18
```

```
C...ABSORBED THERMAL RADIATION CONTRIBUTED BY SKY
C
     C(N,1,I) = C(N,1,I) + SECTAR(J) + CONT(N,1,J)
    +*COSTA(I,J,K)
C...ABSORBED THERMAL RADIATION CONTRIBUTED BY LAYER 1
      C(N,2,I) = C(N,2,I) + SECTAR(J)*CONT(N,2,J)
     +*COSTA(I.J.K)
C
C...ABSORBED THERMAL RADIATION CONTRIBUTED BY LAYER 2
      C(N,3,I) = C(N,3,I) + SECTAR(J) * CONT(N,3,J)
    +*COSTA(I,J,K)
C
C...ABSORBED THERNAL RADIATION CONTRIBUTED BY LAYER 3
      C(N,4,1) = C(N,4,1) + SECTAR(J) * CONT(N,4,J)
     +*COSTA(I,J,K)
C...ARSORBED THERMAL RADIATION CONTRIBUTED BY THE GROUND
      C(N,5,I) = C(N,5,I) + SECTAR(J)*CONT(N,5,J)
     +*COSTA(I,J,K)
   30 CONTINUE
      RETURN
      END
      SUBROUTINE DEVANG
C
C...SUBROUTINE DVANG CALCULATES THE COS(ANGLE) DEVIATION
    ANGLE OF ALL LEAF INCLINATIONS SOURCE ORIENTAIONS PERHUTATIONS. THE THEORY
C
    IS BASED ON THE EXISTENCE OF PLANE ELEMENTS AS USED IN THE SRVC MODEL.
C
C
C
      COMMON /A/ WV.RH.RL.D(3)
      COMMON /B/ PGAP(3,9), PHIT(3,9), PGAP2(3,9), PHIT2(3,9), STEF
      COMMON/C/COSTA(9,9,18), EMISSV(4), ABSORB(3), ESKY, EGRD, SECTAR(9)
      COMMON/B/CONT(3,5,9),C(3,5,9), SUNT(3,9), KELV, GT, NUSIH, ITIME
      COMMOR/E/AT, THETA(9), PHI(18), XLF(9), YLF(9), ZLF(9), XS(9,18)
      COMMON/F/YS(9,18),ZS(9), CEDTR, B, FREQD(9,3), WA(15),EPS
      COMMON/G/MSIG,N, ITHAX
      INTEGER SB,SS
      CEDTR= 0.017453293
```

```
C...CALCULATE INCLINATIN ANGLES IN RADIANS
      THETA(1)= 5. * CEDTR
      BC 10 I=1.8
      THETA(I+1)= THETA(I) + 10.0 + CEBTR
   10 CONTINUE
C...CALCULATE AZIMUTH ANGLES IN RADIANS
C
      PHI(1)= 10. *CEBTR
      DO 20 I=1,17
      PHI(I+1) = 20. *CEDTR+PHI(I)
   20 CONTINUE
C...CALCULATE ALL THE DIRECTION COSINES OF SOURCE SECTORS
C
      DO 40 I=1,9
      ZS(I)=SIN(THETA(I))
      DO 40 J=1,18
      XS(I,J)=COS(THETA(I))*COS(PHI(J))
      YS(I,J)= COS(THETA(I))*SIN(PHI(J))
   40 CONTINUE
C...CALCULATE THE DIRECTION COSINES FOR THE NORMAL VECTOR OF ALL PLANAR LEAF
C
    INCLINATION ANGLES ASSUMING THAT THE AZIMUTH ANGLE IS EQUAL TO ZERO DEGREES.
C
      BO 30 I= 1.9
      XLF(I)= -SIN(THETA(I))
      YLF(I) = 0.0
      ZLF(I) = COS(THETA(I))
   30 CONTINUE
C...CALCULATE THE ABSOLUTE VALUE OF THE DOT PRODUCTS OF ALL SOURCE-LEAF
    ANGLE PERMUTATIONS. THIS VALUE IS EQUAL TO THE COSINE FACTOR BESIRED.
C
      DO 50 LI=1,9
      DO 50 SB=1,9
      DO 50 SS= 1,18
      DOT= (XLF(LI) *XS(SB,SS)+YLF(LI) *YS(SB,SS)+ZLF(LI) *ZS(SB))
      COSTA(LI,SB,SS) = ABS (DOT)
   50 CONTINUE
      RETURN
      END
      SUPROUTINE CANGEON
```

```
C
C...SUBROUTINE CANGEON CALCULATES THE CANOPY GEONETRY COEFFICIENTS.
C...THE SUBROUTINE CANGEON CALLS SUBROUTINE SRUCHOD WHICH IS A MODIFIED
   PORTION OF THE SRVC MODEL THAT CALCULATES THE CANOPY GEOMETRY
    PARAMETERS.
C
C
      COHMON/GEO/ PHIT1(3,9),FLAI(3,1),SLAI(3,1),AXLFA(19,3),AYLFA(19,3)
      CONNON /A/ WV,RH,RL,D(3)
      COMMON /B/ PGAP(3,9), PHIT(3,9), PGAP2(3,9), PHIT2(3,9), STEF
      COMMON/C/COSTA(9,9,18), EMISSV(4), ABSORB(3), ESKY, EGRD, SECTAR(9)
      COHHON/U/CONT(3,5,9),C(3,5,9), SUHT(3,9), KELV, GT, NUSIH, ITIHE
      CDHMON/E/AT, THETA(9), PHI(18), XLF(9), YLF(9), ZLF(9), XS(9,18)
      COMMON/F/YS(9,18),ZS(9), CEDTR, B, FREQD(9,3) , WA(15),EPS
      COMMON/G/NSIG,N, ITMAX
      CALL SRVCHOD
      DO 10 I=1.3
      DO 10 M=1.9
C...TRANSFER IDENTICAL ARRAYS PHIT AND PHITI. PHIT CONTAINS THE
   PROBABILITY OF HIT COEFFICIENTS FOR EACH VIEW ANGLE AND LAYER
C
   PERMUTAION
C
     PHIT(I,K)=PHIT1(I,K)
C
C...CALCULATE THE PROBABILITY OF GAP (PGAP) FOR ALL PERHUTATIONS.
     PGAP(I.M)=1.-PHIT(I.M)
C...CALCULATE THE PROBABILITY OF GAP AND HIT FOR THE HALF LAYERS(PGAP2, PHIT2)
   FOR ALL PERHUTATIONS.
C
     PGAP2(I,K)= SQRT(PGAP(I,K))
     PHIT2(I.K)=1.-PGAP2(I.M)
   10 CONTINUE
C...OBTAIN THE FREQUENCY OF OCCURENCE (FREQD) OF ELEMENTS IN EACH OF THE
C... NINE INCLINATION INTERVALS FOR EACH LAYER.
     DO 15 J=1.3
     ABD=0.0
      DO 20 N=1,9
     FREQD(N,J) = AYLFA(2*N,J)
     ADD=ADD + FREQD(N.J)
```

```
20 CONTINUE
      DO 25 K=1,9
      FREQD(K, J)=FREQD(K, J)/ADD
   25 CONTINUE
   15 CONTINUE
      RETURN
      END
      SUBROUTINE SRVCHOD
C
C
C...SUBROUTINE SRVCHOD IS A MODIFIED VERSION OF A PORTION OF THE SRVC
C
   HODEL WHICH CALCUALTES THE GEOMETRIC PARAMETERS OF A CANOPY.
C
C
      COMMON/GEO/ PHIT1(3,9),FLAI(3,1),SLAI(3,1),AXLFA(19,3),AYLFA(19,3)
      DIMENSION NANGLE(3,3), FLA(3,3,10), THETA(10)
      DIMENSION PHIT(3,3,10), MTP(3), OPM(10), XK(9), XLFA(19)
      BIHENSION YLFA(19), DM(17), F(19), BP(9)
      REAL INCLF
C
C
C....GENERAL SIMULATION CONSTRAINTS
                                                                           SRVC
C
      CEPI02= 1.57079632
      CE2PI= 6.28318530
      CEIPI= 3.14159265
      CEDTR=.017453293
      CERTB= 57.2957795
      CEKTR= .00029088821
      NBANDS=9
      NNAT=1
      NLAY=3
                                                                           SRVC
      BANDW=90/NBANDS
C
C....PARAMETER INITIALIZATION AND CONVERSION
                                                                           SRVC
C
                                                                           SRVC
      MSOUR=NBANDS+1
      BANDU=BANDU+CEDTR
                                                                           SRVC
C
C....COEFFICIENTS FOR DIFFUSE RADIATION VECTORS
                                                                           SRVC
      ALPHA2=0.
                                                                           SRVC
      SINA2=0.
                                                                           SRVC
      DO 2 I=1.NBANDS
                                                                           SRVC
      SINA1=SINA2
                                                                           SRVC
```

```
SRVC
      ALPHA2=ALPHA2+BANDW
                                                                           SRVC
      SINA2=SIN(ALPHA2)
                                                                           SRVC
      XK(I)=SINA2+SINA2-SINA1+SINA1
    2 CONTINUE
                                                                           SRVC
C...SOURCE DIRECTION INCLINATION ANGLES
C
                                                                           SRVC
      TOTAL=0.
                                                                           SRVC
      THETA(1)=(BANDU/2.)-BANDU
                                                                           SRVC
      DO 3 I=1.NBANDS
      THETA(I+1)=THETA(I)+BANDU
                                                                           SRVC
    3 CONTINUE
C....CANOPY GEONETRY. EACH CANOPY LAYER IS COMPOSED OF ONE OPTICAL
                                                                           SRVC
C.... MATERIAL WHICH MAY BE SPECIFIED AND UNIQUE GEOMETRICAL PROPERTIES.
                                                                           SRVC
C....CANOPY GEOMETRIC PARAMETERS CONSIST OF (1)LEAF ANGLE FREQUENCY
C....DISTRIBUTION FUNCTION DENOTED BY XLFA AND YLFA (2)LEAF AREA INDEX
                                                                           SRVC
C.... DENOTED BY FLAI AND (3) CANOPY DENSITY DENOTED BY SLAI. XLFA (DEG) SRVC
C...AND YLFA HUST BE SPECIFIED AT AN ODD NUMBER (NANG) OF EVENLY SPACED SRVC
C....POINTS. FLAI IS NON-NEGATIVE AND SLAI RANGES BETWEEN O AND 1.
                                                                           SRVC
C
                                                                           SRVC
      DELF=10. *CEDTR
      DO 350 IL=1,NLAY
                                                                           SRVC
      NANG=19
C
C...ASSIGN THE NUMBER OF MATERIALS IN ANY GIVEN LAYER
      IhAT=1
                                                                           SRVD
      MTP(IL) = INAT
      INATT=INAT
      DO 351 J=1, IMAT1
      IMAT = J
      BO 41 MM=1, NANG
      XLFA(NN)=AXLFA(NM,IL)
      YLFA(NK)=AYLFA(NK.IL)
   41 CONTINUE
C
C....INTEGRATE AND NORMALIZE THE LEAF ANGLE FREQUENCY DISTRIBUTION
                                                                           SRVC
C....FUNCTION USING SIMPSONS RULE--THIS IS TEMPORARILY DENOTED BY F.
                                                                           SRVC
C....H-1 EQUALLY SPACED INTERVALS OF F ARE THEN DETERMINED AND DENOTED
                                                                           SRVC
C....BY FLA (M POINTS). THE TABLE FLA IS USED FOR RANDONLY SELECTING
                                                                           SRVC
C...LEAF INCLINATION ANGLES.
                                                                           SRVC
      DO 305 I=1, NANG
                                                                           SRVC
305
      XLFA(I)=XLFA(I) + CEDTR
                                                                           SRVC
```

```
M = ((NANG-1)/2) + 1
                                                                             SRVC
      NANGLE(IL, IMAT)=N
                                                                             SRVC
                                                                             SRVC
      CALL TBLR(N, XLFA, YLFA, BM, F)
                                                                             SRYC
      DO 310 IANG=1, M
                                                                             SRVC
  310 FLA(IL, IMAT, IANG) = DM(IANG)
C
C....NORMALIZE THE INPUT LEAF FREQUENCY DISTRIBUTION FUNCTION TO OBTAIN
                                                                             SRVC
C....A DENSITY FUNCTION F WHICH IS SPECIFIED AT M POINTS.
                                                                             SRVC
                                                                             SRVC
      FTOT=0.
                                                                             SRVC
      DO 311 I=1, NANG
                                                                             SRVC
 311 FTOT=FTOT+YLFA(I)
                                                                             SRVC
      DO 312 I=1,9
                                                                             SP.VC
  312 F(I)=(YLFA(2*I)+YLFA(2*I+1))/FTOT
      DO 315 I=1.NANG
                                                                             SRVC
315
      XLFA(I)=XLFA(I) + CERTD
                                                                             SRVC
                                                                             SRVC
      H=H-1
C
C....CALCULATE THE MEAN PROJECTION (OP) IN THE DIRECTION OF THE SOURCE
                                                                             SRVC
C... (THETA) OF ONE UNIT LEAF AREA WITH INCLINATION INCLF. THE LEAVES
                                                                             SRVC
C....AT THIS ANGLE ARE ASSUMED TO BE AZIMUTHALLY ISOTROPIC.
                                                                             SRVC
      BO 330 IANGLE=1, NSOUR
                                                                             SRVC
      INCLF=-5.*CEDTR
                                                                             SRVC
      DO 320 I=1,9
                                                                             SRVC
                                                                             SRVC
      INCLF = INCLF + DELF
  320 CALL COP(INCLF, THETA(IANGLE), OP(I), CEPIO2)
C....CALCULATE THE MEAN PROJECTION (OPH) IN THE DIRECTION OF THE SOURCE
                                                                             SRVC
C....(THETA) OF ONE UNIT LEAF AREA AVERAGED OVER THE CANDPY LEAF ANGLE
                                                                             SRVC
C....DENSITY FUNCTION F.
                                                                             SRVC
      CALL COPH(F, OP, OPH(IANGLE))
                                                                             SRVC
C
C....CALCULATE THE PROBABILITY OF A HIT (PHIT) FOR A LIGHT RAY WITH
                                                                             SRVC
C....SOURCE DIRECTION THETA.
                                                                             SRVC
C
      CALL PDENS(IL, IMAT. IANGLE, OPM (IANGLE). THETA. NANGLE. FLA. SLAI, FLAI,
     * PHIT)
 330 CONTINUE
                                                                             SRVC
 351 CONTINUE
 350 CONTINUE
                                                                             SRVC
       J=NHAT
```

DC 228 I=1,3

```
BO 228 M=1,9
      PHIT1(I, N) = PHIT(I, 1, N+1)
  228 CONTINUE
      RETURN
      END
                                                                           SRVC
      SUBROUTINE COP(ALPHA, BETA, OP, CEPIO2)
                                                                           COP
C
C....THIS PROGRAM CALCULATES THE MEAN PROJECTION OF A UNIT LEAF AREA IN
                                                                           COP
C....THE DIRECTION OF THE SOURCE. THE LEAF IS INCLINED AT AN ANGLE
                                                                           COP
C....ALPHA AND IS ASSUMED TO BE AZIMUTHALLY ISOTROPIC.
                                                                           COP
C
C
                                                                           COP
      DP=COS(ALPHA) +SIN(BETA)
                                                                           COP
      IF(ALPHA.LE.BETA) RETURN
C....THETAO IS THE LEAF AZIMUTH ANGLE AT WHICH OP BECOMES NEGATIVE AND
                                                                           COP
C....IS IN THE FIRST QUADRANT. THE FUNCTION OF IS SYMMETRIC AND HENCE
                                                                           COP
C....IS AVERAGED OVER LEAF AZIMUTH ANGLES OF O TO PI RADIANS.
                                                                           COP
                                                                           COP
      THETAO=ACOS(TAN(BETA)/TAN(ALPHA))
                                                                           COP
      TANTO=TAN(THETAO)
      OP=OP*(1.+(TANTG-THETAO)/CEPIO2)
                                                                           COP
                                                                           COF
      RETURN
      END
                                                                           COP
                                                                           COPK
      SUBROUTINE COPH(G,OP,OPH)
C
C....THIS PROGRAM CALCULATES THE MEAN PROJECTION OF A UNIT LEAF AREA IN COPP.
C....THE DIRECTION OF THE SOURCE (OPM) FOR THE SINULATED CANOPY. THE
                                                                           COPh
C...LEAVES OF THE CANOPY ARE ASSUMED TO BE AZIMUTHALLY ISOTROPIC. THE
                                                                          COPM
C....OP FUNCTION USED IN THE CALCULATION HAS BEEN PREVIOUSLY DETERMINED
                                                                           COPH
C....FOR A GIVEN SOURCE DIRECTION FOR LEAF INCLINATION ANGLES OF
                                                                           COPE
C....5, 15, ..., 85 DEGREES. G IS THE LEAF INCLINATION ANGLE DENSITY
                                                                           COPH
                                                                           COPH
C....FUNCTION.
                                                                           COPH
C
                                                                           COPM
      DIMENSION OP(9),G(9)
                                                                           COPM
      OPM=0.
                                                                           COPM
      DO 1 I=1,9
    1 OPH=OPM+OP(I)*G(I)
                                                                           COPM
      RETURN
                                                                           COPH
                                                                           COPK
      END
      SUBROUTINE PDENS(IL.HTYPE, IANGLE, OPH. THETA, NANGLE, FLA, SLAI, FLAI,
```

```
* PHIT)
C
C
   --THIS PROGRAM COMPUTES THE PROBABILITY THAT LIGHT AT INCIDENT ANGLE
                                                                            PDENS
C
     THETA(IANGLE) INTERACTS WITH MATERIAL TYPE MTYPE WITHIN CANOPY
                                                                            PDENS
C
     LAYER IL.
                                                                            PDENS
C
                                                                            PDENS
C
C
     INPUT
                                                                            PDENS
C
                                                                            PDENS
       IL
C
       HTYPE
                                                                            PDENS
C
       IANGLE
                                                                            PDENS
C
                                                                            PDENS
       MAO
ε
       SLAI
                                                                            PDENS
С
       FLAI
                                                                            PDENS
C
                                                                            PDENS
       THETA
C
                                                                            PDENS
     OUTPUT
C
                                                                            PDENS
       PHIT
C
                                                                            PDENS
C
      DIMENSION DUM(357), THETA(10)
      DIMENSION NANGLE(3,3),FLA(3,3,10),SLAI(3,3),FLAI(3,3),PHIT(3,3,10) PDENS
                                                                            PDENS
      ARG=1.-(SLAI(IL, MTYPE) * OPM/SIN(THETA(IANGLE)))
                                                                            PDENS
      IF (ARG.LE.O.) GO TO 1
      PG=ARG++(FLAI(IL, NTYPE)/SLAI(IL, NTYPE))
                                                                            PDERS
      GO TO 2
                                                                            PDENS
      P0 = 0.
                                                                            PDENS
1
      CONTINUE
                                                                            PDERS
      PHIT(IL, MTYPE, IANGLE)=1.-PO
                                                                            PDEKS
      RETURN
      END
                                                                            PDENS
      SUBROUTINE TBLR(N, X, Y, XX, Z)
                                                                            TBLR
C
                                                                            TBLR
C....THIS PROGRAM FINDS THE INTEGRAL Z(X) OF THE FUNCTION Y(X) FROM X(1) TBLR
C....TO X(2H-1) USING SIMPSONS RULE. THE INTEGRAL Z(X) IS NORMALIZED TO TBLR
C....1.0 AT X(2K-1). THE TABLE OF Z VERSUS X IS THEN INVERTED TO DETER- TBLR
C.... MINE X AS A FUNCTION OF Z AT M REGULARLY SPACED POINTS ALONG Z.
                                                                            TBLR
                                                                            TBLR
C
     INPUT VARIABLES
                                                                            TBLR
       M = DESIRED NUMBER OF REGULARLY SPACED POINTS ALONG Z
                                                                            TBLR
                                                                            TBLR
C
       X = SPECIFIED AT 2N-1 POINTS
       Y = SPECIFIED AT 2M-1 POINTS
                                                                            TBLR
C
     OUTPUT VARIABLES
                                                                            TBLR
```

```
C
       XX = THE TABLE OF X VALUES FOR M REGULARLY SPACED POINTS
                                                                            TBLR
C
                                                                            TBLR
            (H-1 INTERVALS) ALONG Z.
                                                                            TBLR
       Z = THE NORMALIZED INTEGRAL OF Y AT X(1), X(3), ..., X(2M-1).
                                                                            TBLR
                                                                            TBLR
      DIMENSION X(19), Y(19), Z(10), XI(10), XX(10)
C....SIMPSONS RULE INTEGRATION
                                                                            TBLR
10
      Z(1) = 0.0
                                                                            TBLR
      DX = X(2) - X(1)
                                                                            TBLR
20
                                                                            TBLR
      D0 50 J = 2, H
      J0 = 2*J - 3
                                                                            TBLR
30
      J1 = 2*J - 2
                                                                            TBLR
      J2 = 2*J - 1
                                                                            TBLR
                                                                            TBLR
40
      Z(J) = Z(J - 1) + DX + (Y(J0) + 4. + Y(J1) + Y(J2))/3.0
50
      XI(J) = X(J2)
                                                                            TBLR
      XI(1)=X(1)
                                                                            TBLR
                                                                            TBLR
C....NORMALIZE INTEGRAL Z(X)
                                                                            TBLR
60
      DO 70 J = 1.H
70
      Z(J) = Z(J)/Z(H)
                                                                            TBLR
C....FIND X AT M REGULARLY SPACED POINTS ALONG Z.
                                                                            TBLR
                                                                            TBLR
      XX(1) = X(1)
      EN = N - 1
                                                                            TRLR
      F = 1.0/EN
                                                                            TBLR
      JS=2
                                                                            TELR
      DO 120 K = 2,K
03
                                                                            TPLR
      ZT = K - 1
                                                                            TBLR
      ZT = ZT*F
                                                                            TBLR
90
      DO 110 J = JS, K
                                                                            TBLR
      IF(Z(J) - ZT) 110, 100, 100
                                                                            TBLR
      G = (ZT - Z(J - 1)) / (Z(J) - Z(J - 1))
                                                                            TBLR
      XX(K) = XI(J - 1) + G*(XI(J) - XI(J - 1))
                                                                            TBLR
      60 TO 115
                                                                            TBLR
110
      CONTINUE
                                                                            TBLR
115
      JS=J
                                                                            TBLR
120
      CONTINUE
                                                                            TBLR
      RETURN
                                                                            TBLR
      END
                                                                            TBLR
      SUBROUTINE SECTOR
C
```

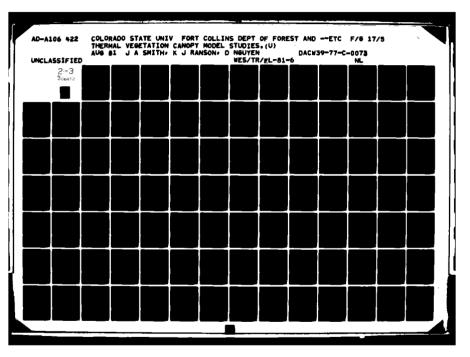
```
C...SUBROUTINE SECTOR CALCULATES THE NORMALIZING FACTORS WHICH ACCOUNT FOR THE A
C
    AREA OF EACH SOURCE SECTOR.
C
C
      COMMON /A/ WV,RH,RL,D(3)
      COMMON /B/ PGAP(3,9), PHIT(3,9), PGAP2(3,9), PHIT2(3,9), STEF
      COMMON/C/COSTA(9,9,18), EMISSV(4), ABSORB(3), ESKY, EGRD, SECTAR(9)
      COHMON/D/CONT(3,5,9),C(3,5,9), SUNT(3,9), KELV, GT, NUSIH, ITIME
      COMMON/E/AT, THETA(9), PHI(18), XLF(9), YLF(9), ZLF(9), XS(9,18)
      COMMON/F/YS(9,18),ZS(9), CEDTR, B, FREQD(9,3), WA(15),EPS
      COMMON/G/NSIG,N, ITMAX
      BANDU= 10. *CEDTR
       ALPHA2= 0.
      SINA2=0.
      DO 2 I=1.9
      SINA1=SINA2
      ALPHA2= ALPHA2 + BANDW
      SINA2= SIN (ALPHA2)
C
C... NOTE WE MUST DIVIDE BY SIN(THETA) SINCE WE ARE INTERESTED IN THE FLUX
     BEFORE IT HITS A HORIZONTAL PANAL.
C
C
      SECTAR(I) = (SINA2**2-SINA1**2)/(18.*SIN(THETA(I)))
    2 CONTINUE
      RETURN
      END
       SUBROUTINE SET02(A,I,J)
C
C
C...SUBROUTINE SETO2 SETS ALL ELEMENTS OF A 2-DIMENSIONAL ARRAY TO 0.0
C
       DIMENSION A(I,J)
      DO 10 K=1,I
      BO 10 L=1,J
      A(K,L) = 0.0
   10 CONTINUE
      RETURN
      END
      SUBROUTINE SETO3 (A,I,J,K)
C...SUBROUTINE SETO3 SETS ALL ELEMENTS OF A 3-DIMENSIONAL ARRAY TO 0.0
```

```
BIKENSION A(I,J,K)
      DO 10 L=1,I
      DO 10 M=1,J
      BO 10 N=1,K
      A(L, H, N) = 0.0
   10 CONTINUE
      RETURN
      END
      SUBROUTINE WHAT(TITLE)
      COMMON/B/ PGAP(3,9), PHIT(3,9), PGAP2(3,9), PHIT2(3,9), STEF
      DIMENSION W(4,9), TITLE(8)
Ç
    WHAT CALCULATES THE W HATRIX.
      D0 10 H = 1,9
      U(1,K) = PHIT(1,K)
      U(2, H) = PGAP(1, H) - PGAP(1, H) + PGAP(2, H)
      U(3, H) = PGAP(1, H) * PGAP(2, H) - PGAP(1, H) * PGAP(2, H) * PGAP(3, H)
      k(4,M) = PGAP(1,M)*PGAP(2,M)*PGAP(3,M)
   10 CONTINUE
      WRITE(6,199)(TITLE(N),N=1,8)
      WRITE(3,199)(TITLE(N),N=1,8)
  199 FORMAT(* THE W AND S MATRICES FOR */8410)
      WRITE(3,300)((W(M,N),N=1,9),H=1,4)
      URITE(6,300)((U(H,N),N=1,9),H=1,4)
  300 FORNAT(9F7.4)
      RETURN
      END
```

SENSIT

```
PROGRAM SENSIT(INPUT, OUTPUT, TAPE5=INPUT, TAPE6=OUTPUT, TAPE1, TAPE2)
      COMMON/PARA1/SIG, STA(3), S(3,3), STG(3), X(3), PARAM(16), A(3),
     1ALP(3), FNU, TA, TAC, TG, EPS(3), EPSTG, RH, RL
      COMMON/PARA2/BTA, BTG, BX(3), DBX(3), QX(3), DQX(3), RX(3), DRX(3)
      CONHON/ESTIN/FX(3), DFX(3,3)
      DIMENSION PAR(16), DSTEP(16), DP(16), DX(3), TEMP(3), XO(3), XX(3),
     1FSEN(3),PARMAX(16)
C
C
         DEFINE INPUT VARIABLES
      SIG=5.6686E-8
      STA(1)=0.6107
      STA(2)=0.1887
      STA(3)=0.0728
      STG(1)=0.0815
      STG(2)=0.2482
      STG(3)=0.7257
      S(1,1)=0.7715 $ S(1,2)=0.4769 $ S(1,3)=0.0523
                      $ 5(2,2)=1.1600 $
      S(2,1)=0.2277
                                            S(2,3)=0.1682
      S(3,1)=0.0830 $ S(3,2)=0.5698 $
                                            S(3,3)=0.5414
C
          DEFINE NOMINAL VALUES FOR HODEL PARAMETERS
      PAR(1)=ALP(1)=1.0
      PAR(2)=ALP(2)=1.0
      PAR(3)=ALP(3)=1.0
      PAR(4)=FHU=10.0
      PAR(5)=TA=14.6
      PAR(6)=TAC=14.6
      PAR(7)=TG=11.7
      PAR(8)=EPS(1)=1.0
      PAR(9)=EPS(2)=1.0
      PAR(10)=EPS(3)=1.0
      PAR(11) = EPSTG=1.0
      PAR(12)=RH=0.20
      PAR(13)=RL=0.66
      PAR(14)=A(1)=144.
      PAR(15)=A(2)=49.
      PAR(16)=A(3)=46.
C
C
          DEFINE INITIAL VALUES FOR STATE VARIABLES
      X0(1)=20.4
      X0(2)=16.6
```

```
XO(3)=16.3
C
          DEFINE UPPER BOUNDS FOR HODEL PARAMETERS
C
      PARMAX(1)=PARMAX(2)=PARMAX(3)=1.0
      PARMAX(8)=PARMAX(9)=PARMAX(10)=PARMAX(11)=1.0
      PARMAX(4)=20.0
      PARMAX(5)=PARMAX(6)=PARMAX(7)=30.0
      PARMAX(12)=0.50
      PARMAX(13)=1.20
      PARMAX(14)=150.0
      PARHAX(15)=PARHAX(16)=60.
C
C
          DEFINE STEP-SIZES OF MODEL PARAMETERS FOR SENSITIVITY ANALYSIS
C
      DSTEP(1)=DSTEP(2)=DSTEP(3)=DSTEP(3)=DSTEP(9)=DSTEP(10)=DSTEP(11)=
     1-0.005
       DSTEP(4)=-1.0
      DSTEP(5) = DSTEP(6) = DSTEP(7) = -1.0
      BSTEP(12)=-0.05
      DSTEP(13) = -0.05
      DSTEP(14)=-7.5
      DSTEP(15)=DSTEP(16)=-3.0
C
C
          START SENSITIVITY ANALYSIS
C
      TOL=0.0001
      DO 100 IP=1,16
      DO 92 I=1.16
   92 PARAM(I)=PAR(I)
      DO 94 I=1.3
      XX(I)=XO(I)
   94 X(I)=XO(I)
      DO 90 NTIME=1.20
      FACTOR=NTIME-1
      DP(IP)=FACTOR+DSTEP(IP)
      PARAH(IP)=PARHAX(IP)+DP(IP)
   50 CALL FEVAL
C
        URITE(6,1010).(FX(I),I=1,3)
C1010
          FORMAT(1H ,3F10.5)
      DO 20 I=1,3
   20 FX(I) = -FX(I)
      CALL SOLVE(FX,3,DFX,3,DX)
      DO 30 I=1,3
C
        URITE(6,1010) X(1),DX(1)
```



```
30 X(1)=X(1)+DX(1)
      DO 40 I=1,3
      DEV=BX(I)
      IF(ABS(DEV) .GT. TOL) 60 TO 50
      FSEN(I)=(X(I)-XX(I))/DSTEP(IP)
      XX(I) = X(I)
   (1)X=(1)9H2T 04
      URITE(1,90) (TEMP(I), I=1,3), PARAM(IP)
   80 FORMAT(3F10.5)
   90 CONTINUE
  100 CONTINUE
      ENDFILE 1
      REVIND 1
      STOP
      END
      SUBROUTINE FEVAL
C
      COMMON/PARA1/SIB,STA(3),S(3,3),STB(3),X(3),PARAM(16),A(3),
     1ALP(3), FHU, TA, TAC, TG, EPS(3), EPSTG, RH, RL
      COMMON/PARA2/BTA, BTG, BX(3), DBX(3), QX(3), DQX(3), RX(3), DRX(3)
      CONMON/ESTIM/FX(3),DFX(3,3)
C
      ALP(1)=PARAM(1)
      ALP(2)=PARAN(2)
      ALP(3)=PARAH(3)
      FHU=PARAH(4)
      TA=PARAM(5)
      TAC=PARAH(6)
      TG=PARAM(7)
      EPS(1)=PARAH(8)
      EPS(2)=PARAH(9)
      EPS(3)=PARAM(10)
      EPSTG=PARAH(11)
      RH=PARAM(12)
      RL=PARAM(13)
      A(1)=PARAM(14)
      A(2)=PARAM(15)
      A(3)=PARAH(16)
      CALL F3TA(TA,BTA)
      CALL BFUNC(EPSTG, TG, BTG, D3TG)
      DO 10 I=1,3
      CALL 3FUNC(EPS(I),X(I),3X(I),93X(I))
      CALL GFUNC(X(I), TAC, FNU, QX(I), DQX(I))
      CALL REUNC(X(I), TAC, FNU, RL, RN, RX(I), DRX(I))
  10 CONTINUS
```

```
BO 20 IL=1,3
   20 FX(IL)=0.5*ALP(IL)*SIG*(BTA*STA(IL)+BX(1)*S(IL,1)+BX(2)*
     1S(IL,2)+BX(3)+S(IL,3)+BTG+STG(IL))+A(IL)-SIG+BX(IL)+QX(IL)
     2+RX(IL)
      DO 30 I=1,3
      DO 30 J=1,3
   30 DFX(I,J)=0.
      DO 40 IL=1,3
      D0 40 J=1,3
      IF(J.NE.IL) GO TO 35
      DFX(IL,J)=0.5*ALP(IL)*SIG*DBX(J)*S(IL,J)-SIG*DBX(IL)*DQX(IL)*
     1DRX(IL)
      GO TO 40
   35 DFX(IL,J)=0.5+ALP(IL)+SIG+DBX(J)+S(IL,J)
   40 CONTINUE
      RETURN
      GKB
      SUBROUTINE BFUNC(EPSI, XI, BXI, DBXI)
C
      BXI=EPSI = (XI+273.0) * * 4.
      BBXI=4.*EPSI*(XI+273.0)**3.
      RETURN
      END
      SUBROUTINE FBTA(TA, 3TA)
C
      EPSTA=1.-0.261*EXP(-7.77E-4*TA*TA)
      CALL BFUNC(EPSTA, TA, BTA, BBTA)
      RETURN
      END
      SUBROUTINE QFUNC(X1, TAC, FHU, QX1, DQX1)
C
      IF(FMU.GT.30.) GO TO 10
      HC=0.69775*(20.4+0.2*FMU**.97)
      GO TO 20
   10 HC=0.69775*(0.95*FMU**.97)
   20 QXI=(XI-TAC)+HC+(-1.0)
      DQXI=HC*(-1.0)
      RETURN
      END
      SUBROUTINE RFUNC(XI, TAC, FMU, RL, RH, RXI, DRXI)
C
      RNUH=FEX(XI) *1.0E-6-RH*FEX(TAC) *1.0E-6
      RBEN=RL+(1./60.)*(0.04+1.27*FMU**(-0.5))
      RXI1=-697.75*(-0.566*XI+597.3)
      RXI2=RNUM/RDEN
      RXI=RXI1*RXI2
      DRXI=697.75+0.566+RXI2+RXI1*(0.056715E-6*FEX(XI))/RDEN
      RETURN
      END
```

```
SUBROUTINE INVERSE(A,N,D)
C
          INVERT A 3+3 REAL MATRIX A WHOSE DETERMINANT IS D
C
C
          THE RESULT WILL BE STORED IN A
C
      DIMENSION A(3,3),B(3,3)
C
      D=A(1,1)*A(2,2)*A(3,3)*A(1,2)*A(2,3)*A(3,1)*A(1,3)*A(2,1)*
     1A(3,2)-A(3,1)*A(2,2)*A(1,3)-A(1,1)*A(3,2)*A(2,3)-A(2,1)*
     2A(1,2)*A(3,3)
      B(1,1)=(A(2,2)+A(3,3)-A(2,3)+A(3,2))/D
      B(1,2)=-(A(2,1)+A(3,3)-A(2,3)+A(3,1))/D
      B(1,3)=(A(2,1)*A(3,2)-A(2,2)*A(3,1))/D
      B(2,1)=-(A(1,2)+A(3,3)-A(1,3)+A(3,2))/B
      B(2,2)=(A(1,1)*A(3,3)-A(1,3)*A(3,1))/B
      B(2,3)=-(A(1,1)*A(3,2)-A(1,2)*A(3,1))/D
      B(3,1)=(A(1,2)*A(2,3)~A(1,3)*A(2,2))/B
      B(3,2)=-(A(1,1)+A(2,3)-A(1,3)+A(2,1))/D
      B(3,3)=(A(1,1)*A(2,2)-A(1,2)*A(2,1))/B
      DO 10 I=1.3
      DO 10 J=1.3
   (L,I)B=(L,I)A 01
      RETURN
      END
      FUNCTION FEX(XI)
C
      XX=5.2342*EXP(0.056715*XI)
      FEX=XX
      RETURN
      END
      SUBROUTINE SOLVE(Y,N,A,H,X)
3
      DIHENSION Y(N), A(N,N), X(H), ATA(N,N), ATY(N)
      DIMENSION Y(3), A(3,3), X(3), ATA(3,3), ATY(3)
C
      DO 10 I=1,N
      DO 10 J=1,N
      0=(L,I)ATA
      DO 10 K=1,N
   10 ATA(I,J)=ATA(I,J)+A(K,I)+A(K,J)
      CALL INVERSE(ATA, N, D)
      DO 20 I=1, N
      ATY(I)=0.
      DO 20 J=1,N
   20 ATY(I)=ATY(I)+A(J,I)+Y(J)
```

DO 30 I=1, N
 X(I)=0.
 BO 30 J=1, N
30 X(I)=X(I)+ATA(I, J)+ATY(J)
 RETURN
END

SRVC

```
*BECK SRVC
      PROGRAM SRVC(INPUT, DUTPUT, TAPE&=OUTPUT, TAPE5=INPUT)
                                                                              SRVC
C.... SOLAR RADIATION - VEGETATION CANOPY REFLECTANCE HODEL
C.... THIS PROGRAM CALCULATES THE APPARENT DIRECTIONAL REFLECTANCE OF A
                                                                              SRVC
C.... VEGETATION CANOPY AS A FUNCTION OF CAMOPY GEOMETRY, LEAF REFLEC-
                                                                              SRVC
C.... TANCE AND TRANSHISSION, SOIL REFLECTANCE, AND CANOPY IRRADIANCE
                                                                              SRVC
                                                                              SRVC
C.... FOR A GIVEN SOLAR POSITION.
                                                                              SRVC
C.... R.E. OLIVER AND J.A. SHITH COLORADO STATE UNIVERSITY JUNE, 1974
                                                                              SRVC
                                                                              SRVC
                 .... COMMON BLOCKS AND REFERENCES .....
C.
C
                                                                              SRVC
C
     LABEL
               EXTERNAL REFERENCES
                                                                              SRVC
                                                                              SRVC
C
C
                BLOCK DATA, LAMBIN, SUN, ETHRES, LANGLE, MRM, SETZ, UTIL, SRVC
      C1
C
                                                                              SRVC
                                                                              SRVC
C
                                                                              SRVC
C
                LANBIN, PDENS, AND OPTICAL.
      C2
                                                                              SRVC
C
                                                                              SRVC
C
      64
                LANGLE, PDENS, AND PGAP.
                                                                              SRVC
C
£
                ETHRES, SETZ, AND LAMBIN.
                                                                              SRVC
      CA
                                                                              SRVC
C
C
                                                                              SRVC
      C8
                LANGLE.
                                                                              SRVC
C
C
                OPTICAL.
                                                                              SRVC
      LI
                                                                              SRVC
C
C
                                                                              SRVC
                PGAP AND LANBIN
      CHAT
C
                                                                              SRVC
C
      11
                LANGLE AND LAMBIN.
                                                                              SRVC
                                                                              SRVC
C
      COMMON/C1/DAY, YEAR, TIME, GLAT, GLONG, DEC, BANDW, NLAM, THETS1, THETS2,
                                                                              SRVC
                                                                              SRVC
     1NHAT, EXTRA(4), NOP, INIT, DUM1(13),
     2CEBTR, CERTD, CENTR, CEPIO2, CE1PI, CE2PI, BUN2(14),
                                                                              SRVC
     35INLAT, COSLAT, SINDEC, COSDEC, COSH, SINZ, COSZ, SINAZ, COSAZ, LXS, LYS, LZS SRVC
      COMMON/C2/CANRM(17), SKYIM(17), DIFIM(17), R(17), T(17), RG(17), XLAM(17
     1), SOURCE(10,17), THETA(10), ZENITH(10)
      COMMON/C4/MANGLE(3,3),FLA(3,3,10),SLAI(3,3),FLAI(3,3),PHIT(3,3,10) SRVC
      COMMON/C6/DR(4,10,17), UR(4,10,17), THRESD(10), IGOD(4,10), IGOU(4,10) SRVC
                                                                              SRVC
     1,THRESU(10)
      COMMON /KIM/ INL(3,3,2)
                                                                              SRVC
      COMMON/C8/SINL, COSL, SINP, COSP
      COMMON/L1/DATAID(7,9), XHU(17,9), C(17,17,9), NVEC(9)
                                                                              SRVC
      COMMON/CHAT/NTP(3), NLAY, OPH(10)
                                                                              SRVC
                                                                              SRVC
     A, ENDLC
      COMMON AVEC(17), XX(9), SXL, SYL, SZL, XLF, YLF, ZLF
                                                                              SRVC
```

```
1,XS(10,18),YS(10,18),ZS(10)
                                                                          SRVC
     A, ENDB3
                                                                          SRVC
      COMMON /AB3/TABSO(4,17)
C..... INTERNAL ARRAYS .....
                                                                          SRVC
      DIMENSION JOBID(8), VECT(17), SIG(17), V(17,17), COR(17,17)
                                                                          SRVC
      DIMENSION COV(10,17,17), COVN(17,17)
                                                                          SRVC
      DIMENSION XLFA(19), YLFA(19), DM(17), DM1(17), REFER(17)
                                                                          SRVC
      DINENSION RIT(10,17), RITBAR(10,17), RBAR(10,17)
                                                                          SRVC
      DIMENSION F(19), OP(9)
                                                                          SRVC
      INTEGER RORT
      REAL LXS, LYS, LZS, INCLF
                                                                          SRVC
      INTEGER DAY, YEAR, TH, TN, ZDEG
                                                                          SRVC
 8000 CONTINUE
      DO 10 I=1,10
      THETA(I)=0.
      ZENITH(I)=0.
     ZS(I)=0.
      THRESD(1)=0.
     OPM(1)=0.
     THRESU(I)=0.
     DO 10 J=1,18
  10 YS(I,J)=0.
     DO 4 K=1,17
     CANRH(K)=0.
     SKYIN(K)=0.
     DIFIN(K)=0.
     R(K)=0.
     T(K)=0.
     RG(K)=0.
     DM(K)=0.
     DM1(K)=0.
     SIG(K)=0.
     XLAM(K)=0.
     BO 4 I=1,10
     SOURCE(I,K)=0.
     RIT(I.K)=0.
     RITBAR(I,K)=0.
     RBAR(I,K)=0.
   4 CONTINUE
     DO 9 I=1,19
     F(1)=0.
     XLFA(I)=0.
   9 YLFA(1)=0.
     DO 12 I=1,9
     NVEC(I)=0.
```

```
OP(1)=0.
      XK(I)=0.
      DO 12 J=1,17
   12 XHU(J, I)=0.
      BO 7 I=1,3
      MTP(1)=0.
      90 7 J=1.3
      NANGLE(I,J)=0.
      SLAI(I,J)=0.
      FLAI(I,J)=0.
      DO 7 K=1,10
      FLA(I, J, K) = 0.
    7 PHIT(I,J,K)=0.
      DO 6 I=1,3
      30 6 J=1,3
      DO 6 K=1,2
    6 INL(I,J,K)=0.
C....PERIPHERAL CONTROLS
                                                                              SRVC
      IHIST = 0
                                                                              SRVC
      ISTOH = 1
                                                                              SRVC
      IFILE = 5
                                                                              SRVC
C....IFILE ASSIGNMENT COULD BE MADE THRU A READ STATEMENT.
                                                                              SRVC
      IF(EOF(5).NE.O.) STOP
      IF(IHIST.EQ.1) CALL FUN(-1.-1)
                                                                              SRVC
C....GENERAL SINULATION CONSTRAINTS
                                                                              SRVC
      READ(IFILE, 100) JOBID, DAY, YEAR, TH, TH, GLAT, GLONG, DEC, NBANDS,
                                                                              SRVC
                                                                              SRYC
     INLAH, MMAT, INIT, MSAMP, MTRIAL
      IF(EOF(5).NE.O.) STOP
                                                                              SRVC
                                                                              SRVC
      READ(IFILE, 102) NLAY
                                                                              SRVC
      BANDU=90/NBANDS
      URITE(6,200) JOBID, DAY, YEAR, TH, TN, GLAT, GLONG, DEC, BANDW, NLAH, HNAT,
                                                                             SRVC
                                                                              SRVC
     1INIT, NSAMP, MTRIAL, MLAY
      READ(IFILE, 101) THRESD $READ(IFILE, 101) THRESU
                                                                              SRVC
                                                                              SRVC
      URITE(4,221) THRESD, THRESU
C....PARAMETER INITIALIZATION AND CONVERSION
                                                                              SRVC
      DO 1073 J=1,4
      DO 1073 I=1, NLAM
      TABSO(J,I)=0.0
 1073 CONTINUE
                                                                              SRVC
      NSOUR=NBANDS+1
      HLAYP1=NLAY+1
                                                                              SRVC
      CALL RANSET(INIT)
                                                                              SRVC
                                                                              SRVC
      XT1=TH
                                                                              SRYC
      XT2=T5
      TIME=XT1+(XT2/60.)
                                                                              SRVC
```

GLAT=GLAT+CEDTR	SRVC
GLONG=GLONG+CEDTR	SRVC
DEC=DEC*CEDTR	SRVC
BANDU=BANBU+CEDTR	SRVC
CSUN POSITION PARAMETERS	SRVC
CALL SUN	SRVC
WRITE(6,222) LXS,LYS,LZS	SRVC
ZS(1) = LZS	SRVC
CCOEFFICIENTS FOR DIFFUSE RADIATION VECTORS	SRVC
CSENSOR/BAND AREA RATIO FOR ALL DIFFUSE BANDS	SRVC
ALPHA2=0.	SRVC
SINA2=0.	SRVC
DO 2 I=1,NBANDS	SRVC
SINA1=SINA2	SRVC
ALPHA2=ALPHA2+BANDU	SRVC
SINA2=ACFAR2+DARDW SINA2=SIN(ALPHA2)	SRVC
XX(I)=SINA2+SINA2-SINA1+SINA1	SRVC
2 CONTINUE	3446
• •••••	SRVC
URITE(6,208) (XK(I),I=1,NBANDS) CSOURCE DIRECTION INCLINATION ANGLES	SRVC
	SRVC
TOTAL=0.	
THETA(1)=(BANDU/2.)-BANDU	SRVC
DO 3 I=1, MBANDS	SRVC
THETA(I+1)=THETA(I)+BANDU	SRVC
3 CONTINUE	00110
THETA(1)=CEPIO2-ACOS(COSZ)	SRVC
CONS=LZS+TOTAL	SRVE
DO 50 I=1,10	SRVC
50 ZENITH(I)=CEPIO2-THETA(I)	SRVC
WRITE(6,223) THETA CDIRECTION COSINES OF AZIMUTHAL SECTORS IN THE DIFFUSE BANDS	SRVC
DE820=20.+CEDIR	SRVC
	SRVC
DO 60 JSOR=2, NSOUR	SRVC
ZS(JSOR)=SIN(THETA(JSOR))	SRVC
PHI=10.+CEDTR	SRVC
DO 60 IPHI=1,18	SRVC
XS(JSOR, IPHI) = COS(THETA(JSOR)) + COS(PHI)	SRVC
YS(JSOR, IPHI)=COS(THETA(JSOR))*SIN(PHI)	SRVC
60 PHI=PHI+DEG20	SRVC
CCANOPY GEOMETRY. EACH CANOPY LAYER IS COMPOSED OF ONE OPTICAL	SRVC
CMATERIAL WHICH MAY BE SPECIFIED AND UNIQUE GEOMETRICAL PROPERTIES.	••••
CCANOPY GEOMETRIC PARAMETERS CONSIST OF (1)LEAF ANGLE FREQUENCY	SRVC
CDISTRIBUTION FUNCTION DENOTED BY XLFA AND YLFA (2)LEAF AREA INDEX	SRVC
CDENOTED BY FLAI AND (3) CANOPY DENSITY DENOTED BY SLAI. XLFA (DEG)	SRVC
CAND YLFA HUST BE SPECIFIED AT AN ODD NUMBER (NANG) OF EVENLY SPACED	SRVC

```
C....POINTS. FLAI IS NON-HEGATIVE AND SLAI RANGES BETWEEN O AND 1.
                                                                             SRVC
                                                                             SRVC
      DELF=10. +CEDTR
      URITE(6,227)
                                                                             SRVC
                                                                             SRVC
      DO 350 IL=1, NLAY
                                                                             SRVC
      READ(IFILE, 102) NANG
C...READ IN THE NUMBER OF NATERIALS IN ANY GIVEN LAYER
      READ(IFILE, 102) INAT
                                                                             SRVC
      HTP(IL) = IMAT
                                                                             SRVC
      TAMI=!TAMI
      DO 351 J=1.IMAT1
      L = TAKI
                                                                             SRYC
      READ(IFILE, 101) (XLFA(I), YLFA(I), I=1, NANG)
                                                                             SRVC
      READ(IFILE.101) SLAI(IL.IMAT), FLAI(IL,IMAT)
C....INTEGRATE AND NORMALIZE THE LEAF ANGLE FREQUENCY DISTRIBUTION
                                                                             SRVC
C....FUNCTION USING SIMPSONS RULE--THIS IS TEMPORARILY DENOTED BY F.
                                                                             SRVC
C....N-1 EDUALLY SPACED INTERVALS OF F ARE THEN DETERMINED AND DENOTED
                                                                             SRYC
C....BY FLA (X POINTS). THE TABLE FLA IS USED FOR RANDOMLY SELECTING
                                                                             SRVC
C...LEAF INCLINATION ANGLES.
                                                                             SRVC
      DO 305 I=1, NANG
                                                                             SRVC
305
      XLFA(1)=XLFA(1) +CEDTR
                                                                             SRVC
                                                                             SRVC
      H=((NANG-1)/2)+1
      NANGLE(IL.IMAT)=M
                                                                             SRVC
      CALL TBLR(H, XLFA, YLFA, DM, F)
                                                                             SRVC
                                                                             SRVC
      WRITE(6,233) (F(I), I=1, H)
                                                                             SRVC
      DO 310 IANG=1, N
  310 FLA(IL, IMAT, IANG) = DM(IANG)
                                                                             SRVC
C....NORMALIZE THE INPUT LEAF FREQUENCY DISTRIBUTION FUNCTION TO OBTAIN
                                                                             SRVC
C....A DENSITY FUNCTION F WHICH IS SPECIFIED AT H POINTS.
                                                                             SRVC
      FTOT=0.
                                                                             SRVC
      DO 311 I=1, NANG
                                                                             SRVC
  311 FTOT=FTOT+YLFA(I)
                                                                             SRVC
                                                                             SRVC
      DO 312 I=1.9
  312 F(I)=(YLFA(2*I)+YLFA(2*I+1))/FTOT
                                                                             SRVC
      DO 315 I=1.NANG
                                                                             SRVC
                                                                             SRVC
315
      XLFA(I)=XLFA(I)+CERTD
      WRITE(6,230) IL, IMAT, NANG, (XLFA(I), YLFA(I), I=1, NANG)
                                                                             SRVC
                                                                             SRVC
      WRITE(6,231) NANGLE(IL, INAT)
      WRITE(6,232) (FLA(IL, IMAT, I), I=1, H)
                                                                             SRVC
      H=H-1
                                                                             SRVC
      WRITE(6,233) (F(I),I=1,N)
                                                                             SRVC
      URITE(6,207) FLAI(IL, INAT), SLAI(IL, INAT)
                                                                             SRVC
C....CALCULATE THE HEAN PROJECTION (OP) IN THE DIRECTION OF THE SOURCE
                                                                             SRVC
C...(THETA) OF DNE UNIT LEAF AREA WITH INCLINATION INCLF. THE LEAVES
                                                                             SRVC
C....AT THIS ANGLE ARE ASSUMED TO BE AZIMUTHALLY ISOTROPIC.
                                                                             SRVC
      DO 330 IANGLE=1.NSOUR
                                                                             SRVC
```

```
INCLF=-5. +CEDTR
                                                                             SRVC
      DO 320 1=1.9
                                                                             SRVC
      INCLF = INCLF + DELF
                                                                             SRVC
  320 CALL COP(INCLF, THETA(IANGLE), OP(I))
                                                                             SRVC
C....CALCULATE THE MEAN PROJECTION (OPN) IN THE DIRECTION OF THE SOURCE
                                                                             SRVC
C....(THETA) OF ONE UNIT LEAF AREA AVERAGED OVER THE CANOPY LEAF ANGLE
                                                                             SRVC
C.... DENSITY FUNCTION F.
                                                                             SRVC
      CALL COPM(F.OP.OPM(IANGLE))
                                                                             SRVC
C....CALCULATE THE PROBABILITY OF A HIT (PHIT) FOR A LIGHT RAY WITH
                                                                             SRYC
C....SOURCE DIRECTION THETA.
                                                                             SRVC
      CALL PDENS(IL, IHAT, IANGLE, DPH(IANGLE))
                                                                             SRVC
      WRITE(6,235) OP, OPH(IANGLE), PHIT(IL, IMAT, IANGLE)
                                                                             SRVC
  330 CONTINUE
                                                                             SRVC
  351 CONTINUE
  350 CONTINUE
                                                                             SRVC
      WRITE(6,228)
                                                                             SRVC
C.... REFLECTANCE AND TRANSMISSION VECTORS ARE READ FOR EACH CANOPY
                                                                             SRYC
C....CONSTITUENT. IN ADDITION REFLECTANCE VECTORS ARE READ FOR THE SOIL SRVC
C....BACKGROUND AND THE HEASURED CANOPY. THE HEAN VECTOR AND COVARIANCE SRVC
C....AND CORRELATION HATRICES ARE CALCULATED AS WELL AS THE SQUARE-ROOT SRVC
C.... MATRIX WHICH IS SUBSEQUENTLY USED FOR MULTIVARIATE NORMAL
                                                                             SRVC
C....STOCHASTIC VECTOR SAMPLING.
                                                                             SRVC
                                                                             SRVC
C.... WAVELENGTHS TO BE SIMULATED
                                                                             SRVC
      REAB(IFILE, 101) (XLAH(I), I=1, NLAH)
                                                                             SRVC
      URITE(6,201) (XLAH(I),I=1,NLAH)
                                                                             SRVC
C....CONSTITUENT OPTICAL VECTORS
                                                                             SRVC
C... READ NUMBER OF CONSTITUENT OPTICAL VECTORS WHICH EQUALS 2*HTYPE
    * NUMBER OF LAYERS
      READ (IFILE.105) NOP
 105 FORMAT (110)
      READ(IFILE, 104)(DATAID(I), I=1,7)
      WRITE(6,5) (DATAID(1),1=1,7)
      READ(IFILE, 101) (CANRH(J), J=1, NLAH)
      URITE(6,294)
      WRITE(6,203) (CANRM(J),J=1,NLAH)
      READ(IFILE, 101) (SKYIM(J), J=1, NLAM)
      WRITE(6,295)
      URITE(6,203) (SKYIM(J), J=1, NLAM)
      READ(IFILE, 101) (DIFIM(J), J=1, NLAH)
      URITE(6,296)
      WRITE(6,203) (DIFIM(J), J=1, NLAM)
      READ(IFILE, 101) (RG(J), J=1, NLAH)
      WRITE(6,297)
      WRITE(6,203) (RG(J),J=1.NLAH)
```

```
DO 11 NL=1, NOP
      READ(IFILE, 106) NULAY, MTYP, RORT, (DATAID(I), I=1,7)
      WRITE(6,202)(DATAID(I), I=1,7), NULAY, HTYP, RORT
      READ(IFILE, 101) (XMU(I, NL), I=1, NLAH)
      INL(NULAY, HTYP, RORT) = NL
      WRITE(6,204) (XMU(I,NL),I=1,NLAM)
                                                                           SRVC
   11 CONTINUE
      URITE (6,210)
                                                                           SRVC
                                BIG LOOP
                                                                          SRVC
                                                                           SRVC
      ISTOP=0
      DO 40 J=1.NLAN
      SOURCE(1,J)=(SKYIH(J)-DIFIH(J))/(SKYIH(J))
      DO 40 I=1, NBANDS
   40 SOURCE(I+1,J)=(DIFIH(J)+XK(I))/(SKYIH(J))
      URITE(6.209)
      DO 45 I=1, MSOUR
   45 WRITE(6,203) (SOURCE(I,J),J=1,NLAM)
      DO 7000 ISAMP=1.NSAMP
                                                                           SRVC
      DO 6000 ITRIAL=1.NTRIAL
                                                                           SRVC
C....COMPUTE PROPORTION OF IRRADIANCE WHICH IS DIRECT AND PROPORTION
                                                                           SRVC
C....WHICH IS DIFFUSE.
                                                                           SRVC
C....POPULATE FIRST (TOP) DOWN DWELL LAYER (DR) WITH INCIDENT DIRECT AND SRVC
C....DIFFUSE LIGHT. DOWN DWELL RADIATION FLUX (DR) IS INDEXED FROM 1 TO SRVC
C....NLAY IN A DOWN GOING SEQUENCE. UPWARD DWELL RADIATION FLUX (UR)
C....IS INDEXED FROM 1 TO NLAY+! IN UPWARD GOING SEQUENCE. THAT IS FOR
C....FOR UR, LAYER 1 IS THE LAYER IMMEDIATELY ABOVE THE BACKGROUND. THE SRVC
C....FLUX IN LAYER NLAY+1 IS THAT WHICH ESCAPES THE CANOPY AND TOBETHER SRVC
C....WITH THE INCIDENT FLUX DETERMINES THE CANOPY REFLECTANCE.
                                                                           SRVC
      BG 8 K=1.17
      DO 8 J=1,10
      DO 8 I=1,4
      UR(I,J,K)=0.
      DR(I,J,K)=0.
      IGOD(I,J)=0.
      IGOU(I.J)=0.
    8 CONTINUE
      DO 1003 J=1, NSOUR
                                                                           SRVC
                                                                           SRVC
      DO 1003 K=1.NLAM
                                                                           SRVC
 1003 DR(1,J,K)=SOURCE(J,K)
C....SET FLUX LEVEL INDICATORS (DOWNWARD)
                                                                           SRVC
                                                                           SRVC
      CALL ETHRES(NLAY, NSOUR, -1)
C.....FAST LOOP TRACES LIGHT ATTENUATION THROUGH CANOPY......
                                                                          SRVC
C....FLUX PASSING THROUGH LAYERS IN A DOWNWARD DIRECTION
                                                                           SRVC
                                                                           SRVC
2000 CONTINUE
                                                                           SRVC
      DO 2600 IL=1, NLAY
```

```
SRVC
      DO 2500 JSOR=1.NSOUR
C....CHECK FLUX LEVEL INDICATOR
                                                                              SRVC
      IF(IGOD(IL, JSOR) . EQ. 0.) GO TO 2500
                                                                              SRVC
                                                                              SRVC
C....DID LIGHT STRIKE LEAF
      CALL PGAP(IL, JSOR, -1, IHIT, HTYPE)
                                                                              SRVC
                                                                              SRVC
      IF(IHIT.EQ.0) G0 TO 2200
                                                                              SRVC
      DO 2100 IPHIP=1,18
                                                                              SRVC
C....DIRECTION COSINES OF SOURCE SECTOR (LVLH)
                                                                              SRVC
      SXL = XS(JSOR, IPHIP)
      SYL = YS(JSOR, IPHIP)
                                                                              SRVC
                                                                              SRVC
      SZL = ZS(JSOR)
                                                                              SRVC
      CALL LAMBIN(IL, JSOR, MIYPE, -1, MSOUR)
 2100 CONTINUE
                                                                              SRVC
                                                                              SRVC
      GO TO 2400
                                                                              SRVC
C....GAP ENCOUNTERED IN DOUNWARD PATH
                                                                              SRVC
 2200 DO 2250 KL=1.NLAN
                                                                              SRVC
 2250 DR(IL+1, JSOR, KL) = DR(IL+1, JSOR, KL) + DR(IL, JSOR, KL)
                                                                              SRVC
2400 CALL SETZ(IL, JSOR, -1)
                                                                              SRVC
2500 CONTINUE
                                                                              SRVC
      CALL ETHRES(NLAY, NSOUR, -1)
                                                                              SRYC
 2600 CONTINUE
C....BACKGROUND REACHED - REFLECTS LAMBERTIAN
                                                                              SRVC
                                                                              SRVC
      DO 3600 JSOR=1, MSOUR
                                                                              SRYC
      DO 3400 JJ=2. MSOUR
                                                                              SRVC
      IL = NLAY + 1
                                                                              SRVC
      DO 3400 KL=1,NLAM
      UR(1,JJ,KL)=UR(1,JJ,KL)+RG(KL)+DR(IL,JSOR,KL)+XK(JJ-1)
 3400 TABSO(4,KL)=TABSO(4,KL)+(1.-RG(KL))+DR(IL,JSOR,KL)+XK(JJ-1)
      CALL SETZ(NLAY+1, JSGR, -1)
                                                                              SRVC
                                                                              SRVC
 3600 CONTINUE
                                                                              SRUC
      CALL ETHRES(NLAY, NSOUR, +1)
C....FLUX PASSING THROUGH LAYERS IN AN UPWARD DIRECTION
                                                                              SRVC
      DO 4600 IL=1.NLAY
                                                                              SRVC
      DO 4500 JSOR=2, NSOUR
                                                                              SRVC
C....CHECK FLUX LEVEL INDICATOR
                                                                              SRVC
      IF(IGOU(IL, JSOR).EQ.0) GO TO 4500
                                                                              SRVC
C....DID LIGHT STRIKE LEAF
                                                                              SRVC
      CALL PGAP(IL, JSOR, +1, IHIT, MTYPE)
                                                                              SRVC
      IF(IHIT.EQ.0) GO TO 4200
                                                                              SRVC
                                                                              SRVC
      DO 4100 IPHIP=1,18
C....DIRECTION COSINES OF SOURCE SECTOR (LVLH)
                                                                              SRVC
                                                                              SRVC
      SXL = XS(JSOR, IPHIP)
                                                                              SRVC
      SYL = YS(JSOR, IPHIP)
                                                                              SRVC
      SZL = ZS(JSOR)
      CALL LANDTH(IL, JSOR, MTYPE, +1, NSOUR)
                                                                              SRVC
```

```
SRUC
 4100 CONTINUE
      GO TO 4400
                                                                             SRVC
C....GAP ENCOUNTERED IN UPWARD PATH
                                                                             SRVC
 4200 BO 4250 KL=1,NLAM
                                                                             SRVC
 4250 UR(IL+1, JSOR, KL) = UR(IL+1, JSOR, KL) + UR(IL, JSOR, KL)
                                                                             SRVC
 4400 CALL SETZ(IL, JSOR, +1)
                                                                             SRVC
4500 CONTINUE
                                                                             SRVC
      CALL ETHRES(NLAY, NSOUR, +1)
                                                                             SRVC
 4600 CONTINUE
                                                                             SRVC
                                                                             SRVC
      CALL ETHRES(NLAY, NSOUR, -1)
      CALL ETHRES(NLAY, NSOUR, +1)
                                                                             SRYC
C....RECYCLE THROUGH LAYERS UNTIL FLUX EXHAUSTED
                                                                             SRVC
                                                                             SRVC
      DO 5000 IL=1, NLAY
                                                                             SRVC
      DO 5000 JSOR=2, NSOUR
      IF (IGOU(IL.JSDR).NE.O) GO TO 2000
                                                                             SRYC
5000 CONTINUE
                                                                             SRVC
                                                                             SRVC
      DO 5001 IL=2,NLAYP1
                                                                             SRVC
      DO 5001 JSOR=1.NSOUR
                                                                             SRVC
      IF(IGOD(IL.JSOR).NE.O) SO TO 2000
 5001 CONTINUE
                                                                             SRVC
C....FLUX EXHAUSTED IN ALL SOURCES--COMPUTE REFLECTANCE FOR THIS TRIAL
                                                                             SRVC
                                                                             SRVC
      DO 5200 JSOR=2.NSOUR
      DO 5200 KL=1.NLAM
                                                                             SRVC
      RIT(JSOR, KL) = UR(NLAY+1, JSOR, KL)/XK(JSOR-1)
                                                                             SRVC
 5200 RITBAR(JSOR,KL)=RITBAR(JSOR,KL)+RIT(JSOR,KL)
      WRITE(5,283) ISAMP, ITRIAL
                                                                             SRVC
      DO 5300 JSOR=2.NSOUR
      ZDEG=105-10*JSDR
                                                                             SRVC
 5300 WRITE(6,284) ZDEG,(RIT(JSOR,KL),KL=1,NLAM)
                                                                             SRYC
 6000 CONTINUE
                                                                             SRVC
                                                                             SRVC
C....TRIALS COMPLETE FOR THIS SAMPLE POINT
                                                                             SRVC
      FTRIAL=NTRIAL
 6200 DO 6300 JSOR=2, NSOUR
                                                                             SRVC
                                                                             SRVC
      DO 6300 KL=1, NLAM
 6300 RITBAR(JSOR, KL)=RITBAR(JSOR, KL)/FTRIAL
                                                                             SRVC
      URITE(6,286) ISAMP
                                                                             SRVC
      DO 6400 JSOR=2.NSOUR
                                                                             SRVC
      ZDEG=105-10+JSOR
                                                                             SRVC
                                                                             SRVC
 6400 WRITE(6,284) ZDEG,(RITBAR(JSOR,KL),KL=1,NLAM)
      DO 6600 JSOR=2,NSOUR
                                                                             SRVC
                                                                             SRVC
      DO 6500 KL=1,NLAM
      RBAR(JSOR, KL)=RBAR(JSOR, KL)+RITBAR(JSOR, KL)
                                                                             SRVC
                                                                             SRVC
      DO 6500 KLL=1,NLAH
 4500 COV(JSOR,KL,KLL)=COV(JSOR,KL,KLL)+RITBAR(JSOR,KL)*RITBAR(JSOR,KLL) SRVC
                                                                             SRVC
      DO 6600 KL=1,NLAM
```

```
6600 RITBAR(JSOR,KL)=0.
                                                                           SRVC
      IF(ISTOP.EQ.1) GO TO 7100
                                                                           SRVC
7000 CONTINUE
                                                                           SRVC
      FSAMP=NSAMP
                                                                           SRVC
      GO TO 7150
                                                                           SRVC
 7100 FSAMP=ISAMP
                                                                           SRVC
C....ALL SAMPLE POINTS ESTIMATED
                                                                           SRVC
7150 DG 7200 JSOR=2,NSOUR
                                                                           SRVC
      DO 7200 KL=1, NLAM
                                                                           SRVC
7200 RBAR(JSOR, KL)=RBAR(JSOR, KL)/FSAMP
                                                                           SRVC
      DO 7900 JSOR=2.NSOUR
                                                                           SRVC
      ZDEG=105-10+JSOR
                                                                           SRVC
      IF(FSAMP.LE.1.) GO TO 7600
                                                                           SRVC
      BO 7400 I=1, NLAH
                                                                           SRVC
      DO 7300 J=1,NLAM
                                                                           SRVC
7300 COV(JSOR,I,J)=(COV(JSOR,I,J)-FSAMP*RBAR(JSOR,I)*RBAR(JSOR,J))
                                                                           SRVC
     1/(FSAMP-1.)
                                                                           SRVC
7400 SIG(I)=SQRT(COV(JSOR,I,I))
                                                                           SRVC
      DO 7500 I=1, NLAM
                                                                           SRVC
      DO 7500 J=1.NLAM
                                                                           SRVC
7500 COR(I,J)=COV(JSOR,I,J)/(SIG(I)+SIG(J))
                                                                           SRVC
7600 WRITE(6,287) ZDEG, (RBAR(JSOR, KL), KL=1, NLAM)
                                                                           SRVC
      WRITE(6,293) (SIG(KL),KL=1,NLAM)
      IF(FSAMP.LE.1.) GO TO 7900
                                                                           SRVC
      WRITE(6,288)
                                                                           SRVC
      DO 7700 I=1,NLAH
                                                                           SRVC
7700 WRITE(6,289) (COV(JSOR,I,J),J=1,NLAM)
                                                                           SRVC
      WRITE(6,291)
                                                                           SRVC
      DG 7800 I=1.NLAN
                                                                           SRVC
7800 WRITE(6,289) (COR(I,J),J=1,NLAM)
                                                                           SRVC
7900 CONTINUE
                                                                           SRYC
      DO 7213 IK=1.4
      DO 7213 KL=1,NLAM
      TABSO (IK, KL) = TABSO(IK, KL)/(FSAMP*FTRIAL)
7213 CONTINUE
      DO 7215 I=1.4
      JJ=1
      WRITE (6,7214) JJ.(TABSO(I.J),J=1,NLAH)
7214 FORMAT ( * THE LAYER IS+,12,* THE ABSORPTIONS ARE +,6(F8.5,1X))
7215 CONTINUE
      IF(IFILE.EQ.5) GO TO 8000
                                                                           SRVC
      STOP
                                                                           SRVC
        ................DATA FORMATS..............
                                                                        .. SRVC
 100 FORHAT(BA10,/,4X,I3,7X,I4,7X,2I2,6X,F6.2,7X,F7.2,5X,F7.2,8X,I2,/, SRVC
    15x,12,7x,11,7x,15,9x,15,8x,15)
                                                                           SRVC
```

```
SRVC
101 FORMAT(8F10.5)
102 FORMAT(110.7A10)
                                                                        SRVC
103 FORMAT(8E10.4)
                                                                        SRVC
104 FORMAT(7A10)
  5 FORMAT(#0#,7A10)
106 FGRMAT(311,7A10)
200 FORMAT(*1*,43X,*SOLAR RADIATION/VEGETATION CANOPY REFLECTANCE HODE SRVC
   1L*,//,64X,*INPUT DATA*,//,1X,8A10,/,
                                                                        SRVC
   2* JULIAN DAY *, I3, *, YEAR *, I4, *, TIME *, 212, * HOURS*, /,
                                                                        SRVC
   3* LATITUDE = *, F6.2, * DEGREES, LONGITUDE = *, F7.2, * DEGREES*,/,
                                                                        SRVC
   4* SOLAR DECLINATION = *,F6.2,* DEGREES*,/,
                                                                        SRVC
   5* BAND WIDTH OF DIFFUSE VECTORS = *,F5.1,* DEGREES*,/,
                                                                        SRUC
   6* NUMBER OF WAVELENGTH BANDS SIMULATED *,12,/,
                                                                        SRVC
   7* NUMBER OF CANOPY CONSTITUENTS *,11,/,
                                                                        SRVC
   9* K DIGIT ODD NO. TO INITIALIZE RANDON SEQUENCE = *,15,/,
                                                                        SRVC
                                                                        SRVC
   9 * NSAMP = +, 15,/,
   A* MTRIAL = *,15,/,
                                                                        SRVC
                                                                        SRVC
   B = NLAY = +, I1,
                                                                        SRVC
   C)
201 FORMAT( *ONAVELENGTHS SINULATED*, /, *0*, F7.4, 16F8.4)
                                                                        SRYC
202 FORMAT(*0*,7A10/* *,*NUMBER OF LAYERS = *,I1/* *,
   1*MATERIAL TYPE = *, I1/* *, *R OR T
203 FORMAT(* *,F7.4,16F8.4)
                                                                        SRVC
204 FORMAT(*0
                                                                        SRVC
                  MEAN*,/,8X,10E12_4)
205 FORMAT(*0
                  COVARIANCE MATRIX#)
                                                                        SRVC
206 FORMAT(*ORANDOM VECTOR GENERATED FROM THE *,7A10,/,(* *,10E12.4))
                                                                        SRVC
207 FORMAT(*OLAI = *,F4.2,4X,*S = *,F4.2)
                                                                        SRVC
208 FORMAT(*ODIFFUSE VECTOR COEFFICIENTS*,/,
                                                                        SRVC
   19(*
            K *)./.(9F8.4))
                                                                        SRVC
209 FORMAT(+01RRABIANCE SOURCE VECTORS+)
                                                                        SRVC
210 FORMAT(1H1)
                                                                        SRVC
211 FORMAT(*0
                  CORRELATION MATRIX+)
                                                                        SRVC
212 FORMAT(*ODM1 = *,9F8.4)
                                                                        SRVC
221 FORMAT(*OTHRESD = *,10F8.4/* THRESU = *,10F8.4)
                                                                        SRVC
222 FORMAT( + ODIRECTION COSINES OF SUN
                                           *,3F8.4)
                                                                        SRVC
223 FORMAT(*OTHETA =*,10F8.4)
                                                                        SRUC
227 FORMAT(///* *,25(1H.),2X,*CANOPY GEOMETRY*,2X,25(1H.)//)
                                                                        SRVC
228 FORMAT(/* *,25(1H.))
                                                                        SRVC
230 FORMAT( *OLEAF ANGLE COMPUTATIONS - IL = *, I1,
                                                                        SRVC
                                                                        SRVC
   SRVC
   1/,(2X,16F8.3))
231 FORMAT(*ONANGLE(IL, IMAT) = *,12)
                                                                        SRVC
232 FORMAT(*0
                 FLA =*,10F8.3)
                                                                        SRVC
233 FORMAT( +0
                 F = *, 10F8.3
                                                                        SRVC
235 FORMAT(+0
                 OP =+,9F8.3,3X,+OPM = +,F8.3,3X,+PHIT = +,F8.3)
                                                                        SRVC
```

```
SRVC
  251 FORMAT(8X,10E12.4)
                                                                              SRVC
  282 FORNAT( * OREFER = *,8E13.4)
  283 FORMAT( *OREFLECTANCE FOR SAMPLE*, 13, * TRIAL*, 13.5X.
                                                                              SRVC
     1*COMPUTATION TIME WAS*,F5.1,* SECONDS.*)
                                                                              SRVC
                                                                              SRVC
  284 FORNAT(* Z =*, I3, * DEG*, 3X, 10F7.3)
  285 FORMAT( *OCAUTION....SAMPLE *, I3, * CONTAINS ONLY *, I3, * TRIALS. *)
                                                                              SRVC
  286 FORMAT(*0*,75(1H.)/* HEAN REFLECTANCE FOR SAMPLE*,13)
                                                                              SRVC
  287 FORMAT(*OGRAND MEAN FOR Z =*, 13, * DEGREES.*, 3X, 10F7.3)
                                                                              SRVC
                  COVARIANCE HATRIX*)
                                                                              SRVC
  288 FORMAT(*0
  289 FORMAT(7X,10F12.8)
                                                                              SRVC
                                                                              SRVC
  291 FORMAT(#0
                   CORRELATION MATRIX+)
                                                                              SRVC
  292 FORMAT(1X,120(1H-))
  293 FORMAT( + OSTDEV +, 1X, 10F12.8)
  294 FORMAT( *OMEASURED REFLECTANCE *)
  295 FORMAT( *OGLOBAL IRRADIANCE *)
  296 FORMAT( *ODIFFUSE IRRADIANCE *)
  297 FORMAT( + OSOIL REFLECTANCE +)
                                                                              SRVC
      END
*DECK LAMBIN
                                                                              LAMBIN
      SUBROUTINE LAMBIN(IL, JSOR, MTYPE, IDIR, MSOUR)
C....FOR A GIVEN FLUX SOURCE THIS PROGRAM CALLS THE APPROPRIATE
                                                                              LAMBIN
C.....PROGRAMS TO DETERMINE LEAF ORIENTATION AND OPTICAL PROPERTIES
                                                                              LANBIN
C....AND UPDATES THE DIFFUSE SOURCES WITH SCATTERED FLUX.
                                                                              LANBIN
                                                                              LAMBIN
     SXL, SYL, SZL
                                                                              LAMBIN
     JSOR
     LXS, LYS, LZS
                                                                              LAMBIN
     IDIR
                                                                              LAMBTN
C
     NLAH
                                                                              LAMBIN
                                                                              LANBTH
C
     DR(I,J,K)
C
     UR(I,J,K)
                                                                              LAMBIN
C
     HTYPE
                                                                              LAMBIN
C
     IL
                                                                              LAMBIN
C
     NSOUR
                                                                              LANBIN
C
     R,T
C
     ZENITH
                                                                              LAMBIN
C
   OUTPUT VARIABLES
                                                                              LAMBIN
C
     DR(I,J,K)
                                                                              LAMBIN
C
     UR(I,J,K)
                                                                              LAMBIN
C
                                                                              LAMBIN
      COMMON BUMO(17), XK(9), SXL, SYL, SZL, XLF, YLF, ZLF
                                                                              LAMBIN
      COMMON/C1/DUM1(7), NLAM, DUM2(26), CE1PI, DUM3(24), LXS, LYS, LZS
                                                                              LAMBIN
      COMMON/C2/DUM4(51),R(17),T(17),RG(17),DUM5(197),ZENITH(10)
                                                                              LAMBIN
      COMMON/C6/DR(4,10,17),UR(4,10,17)
                                                                              LANBIN
      COMMON/CHAT/HTP(3), NLAY, OPH(10)
```

C

```
COMMON /AB3/TABSO(4,17)
      DIMENSION H(17).PTRP(2.17)
                                                                             LAMBIN
      REAL LXS, LYS, LZS
                                                                             LAMBIN
      DATA PI02/1.570796327/
C....SET DIRECTION COSINES OF SOURCE
                                                                             LAMBIN
      XL=SXL
                                                                             LAMBIN
      YL=SYL
                                                                             LAMBIN
                                                                             LAMBTN
      ZL=SZL
      IF(JSOR.NE.1) GO TO 100
                                                                             LAMBIN
      XL=LXS
                                                                             LAMBIN
      YL=LYS
                                                                             LAMBIN
                                                                             LAMBIN
      ZL=LZS
C....RANDOM LEAF ORIENTATION, DIRECTION COSINES OF NORMAL, AND
                                                                             LAHSTN
C...LEAF OPTICAL PROPERTIES
                                                                             LAMBTN
  100 IF(IDIR.EQ.-1) IXL=IL
                                                                             LAMBIN
      IF(IDIR.EG.1) IXL=NLAY-IL+1
                                                                             LAMBIN
      CALL LANGLE(IXL, NTYPE, THETAL, PHIL)
                                                                             LAMBIN
C....SET SIDE OF LEAF WHICH LIGHT STRIKES. ISIDE=1 (TOP), -1 (BOTTOM).
                                                                             LAMBIN
      ISIDE=-IDIR
                                                                             LANBIN
      BOT=XL*XLF+YL*YLF+ZL*ZLF
                                                                             LAMBTH
      IF(DOT.LT.O.) ISIDE=IDIR
                                                                             LAMBTN
      COSLS=ABS(DOT)
                                                                             LAMBTN
      IF(IDIR.EQ.1) GO TO 5
                                                                             LAMBIN
      DO 4 KL=1.NLAM
                                                                             LAMBIN
    4 H(KL)= DR(IL, JSOR, KL)/18.
                                                                             LAMBIN
      GD TO 9
                                                                             LANBIN
    5 DO 7 KL=1, NLAN
    7 H(KL)= UR(IL, JSOR, KL)/18.
    9 CONTINUE
                                                                             LANBIN
C...SET OPTICAL PROPERTIES FOR HTYPE, LAYER, REFLECT. AND TRANS.
C....UPDATE DIFFUSE SOURCES WITH SCATTERED RADIATION FLUX
                                                                             LAMBIN
      DO 50 JJSOR=2, MSOUR
                                                                             LAMBIN
      IF(ISIDE.EQ.-1) CALL BFLUX(THETAL, ZENITH(JJSOR), H, T, R, NLAM, PTRP)
                                                                             LAMBTH
      IF(ISIDE.EQ.1) CALL BFLUX(THETAL, ZENITH(JJSOR), H, R, T, NLAM, PTRP)
                                                                             LAMBIN
      DO 50 KL=1, NLAH
                                                                             LAMBTH
      IF(IDIR.EQ.1) GO TO 45
                                                                             LAMBIN
      DR(IL+1, JJSOR, KL) = DR(IL+1, JJSOR, KL)+PTRP(2, KL)
                                                                             LAMBIN
      UR(NLAY+2-IL, JJSOR, KL) = UR(NLAY+2-IL, JJSOR, KL)+PTRP(1, KL)
                                                                             LAMBIN
                                                                             LAMBIN
      GJ TO 50
   45 DR(NLAY+2-IL, JJSOR, KL)=DR(NLAY+2-IL, JJSOR, KL)+PTRP(2, KL)
                                                                             LAMBIN
      UR(IL+1, JJSOR, KL) = UR(IL+1, JJSOR, KL)+PTRP(1, KL)
                                                                             LAMBIN
   50 CONTINUE
                                                                             LANBIN
      DO 53 KL=1.NLAM
      TABSO(IL.KL)=H(KL) +(1.-(R(KL)+T(KL)))+TABSO(IL,KL)
   53 CONTINUE
```

RETURN End	LAMBTH Lambth
*DECK BFLUX	
SUBROUTINE BFLUX(TA,TRP,H,R,T,NLAM,PTRP)	BFLUX
CGIVEN THE IRRADIANCE H OF A LEAF INCLINED AT TA THIS PROGRAM	BFLUX
CDETERMINES THE FLUX REFLECTED AND TRANSMITTED INTO A SOURCE	BFLUX
CBAND WHOSE ZENITH ANGLE IS TRP.	BFLUX
DIMENSION PTRP(2,17),H(17),R(17),T(17)	BFLUX
BATA PI/3.141592654/,PI02/1.570796327/	BFLUX
F1(X,Y)=COS(TA)+(SIN(X)++2-SIN(Y)++2)	BFLUX
F2(X)=ACOS(-1/(TAN(TA)+TAN(X)))	BFLUX
F3(X,Y,Z)=2.*SIN(TA)*SIN(X)*(DEL+.25*(SIN(2.*Y)-SIN(2.*Z)))/P	
DEL=.087266463	BFLUX
T1=TRP-DEL	BFLUX
T2=TRP+BEL	BFLUX
IF(TA.LE.PID2-T2) GO TO 10	BFLUX
IF(TA.GE.PIO2-T1) GO TO 20	BFLUX
GO TO 30	BFLUX
CCASE 1	BFLUX
10 XF1=F1(T2,T1)	BFLUX
DO 15 KL=1,NLAM	BFLUX
PTRP(1,KL)=R(KL)+H(KL)+XF1	BFLUX
PTRP(2,KL)=T(KL)+H(KL)+XF1	BFLUX
15 CONTINUE Return	BFLUX 3FLUX
CCASE 2	
20 XF1=F1(T2,T1)	∌FLUX BFLUX
IF(TA.LE.1.5533) GO TO 21	BFLUX
PRP=PIO2	BFLUX
60 TO 22	BFLUX
21 PRP=F2(TRP)	BFLUX
22 XF3=F3(PRP,T1,T2)	BFLUX
DO 25 KL=1, NLAN	BFLUX
PTRP(1,KL)=H(KL)+(R(KL)+T(KL))+XF3+	BFLUX
1(R(KL)*H(KL)*PRP-T(KL)*H(KL)*PI+T(KL)*H(KL)*PRP)*XF1/PI	BFLUX
PTRP(2.KL)=H(KL)+(T(KL)+R(KL))+XF3+	BFLUX
1(T(KL)*H(KL)*PRP-R(KL)*H(KL)*PI+R(KL)*H(KL)*PRP)*XF1/PI	BFLUX
25 CONTINUE	BFLUX
RETURN	BFLUX
CCASE 3	BFLUX
30 TB=PIO2-TA	BFLUX
XF1=F1(TB,T1)	BFLUX
DO 35 KL=1,NLAM	BFLUX
PTRP(1,KL)=R(KL)+H(KL)+XF1	BFLUX
35 PTRP(2,KL)=T(KL)+H(KL)+XF1	BFLUX

```
BFLUX
      IF(TB+T2.LE.3.106) GO TO 36
                                                                             BFLUX
      PRP=PI02
      60 TO 37
                                                                             BFLUX
                                                                             BFLUX
   36 PRP=F2((TB+T2)/2.)
   37 XF1=F1(T2,TB)
                                                                             BFLUX
                                                                            BFLUX
      DEL=((TRP+TA)/2.)-.74176493
                                                                             BFLUX
      XF3=F3(PRP, TB, T2)
      DO 40 KL=1, NLAM
                                                                             BFLUX
      PTRP(1,KL)=PTRP(1,KL)+H(KL)+(R(KL)+T(KL))+XF3+
                                                                             BFLUX
     1(R(KL)*H(KL)*PRP-T(KL)*H(KL)*PI+T(KL)*H(KL)*PRP)*XF1/PI
                                                                             BFLUX
      PTRP(2,KL)=PTRP(2,KL)+H(KL)+(T(KL)+R(KL))+XF3+
                                                                             BFLUX
     1(T(XL)+H(KL)+PRP-R(KL)+H(KL)+PI+R(KL)+H(KL)+PRP)+XF1/PI
                                                                             BFLUX
                                                                             BFLUX
   40 CONTINUE
      RETURN
                                                                             BFLUX
                                                                             3FLUX
      ENB
*DECK LANGLE
      SUBROUTINE LANGLE(IL, NTYPE, THETAL, PHIL)
                                                                             LANGLE
C----THIS PROGRAM SELECTS A RANDOM LEAF INCLINATION (THETAL) AND AZIMUTH LANGLE
     (PHIL) AND THEN COMPUTES ITS DIRECTION COSINES XLF, YLF, AND ZLF.
                                                                             LANGLE
     THE INTERNEDIATE PARAMETERS SINL, COSL, SINP, AND COSP ARE ALSO
                                                                             LANGLE
     OUTPUT. RANDOM LEAF REFLECTANCE AND TRANSHITTANCE VECTORS ARE ALSO LANGLE
C
     SELECTED.
                                                                             LANGLE
                                                                             LANGLE
C
C
     INPUT
                                                                             LANGLE
                                                                             LANGLE
C
       IL
C
       HTYPE
                                                                             LANGLE
C
       NANGLE
                                                                             LANGLE
C
                                                                             LANGLE
     OUTPUT
       THETAL
C
                                                                             LANGLE
C
       PHIL
                                                                             LANGLE
C
                                                                            LANGLE
       XLF, YLF, ZLF
C
                                                                            LANGLE
       SINL, COSL, SINP, COSP
C
       R,T
                                                                            LANGLE
                                                                             LANGLE
      CONMON/C1/DUH2(31), CERTD, BUH7(3), CE2PI
      COMMON/C4/NANGLE(3,3),FLA(3,3,10),SLAI(3,3),FLAI(3,3),PHIT(3,3,10) LANGLE
                                                                             LANGLE
      COMMON/CB/SINL, COSL, SINP, COSP
                                                                             LANGLE
      COMMON DUN3(29), XLF, YLF, ZLF
      COHHON /KIH/ INL(3,3,2)
C---- DETERMINE RANDOM LEAF ORIENTATION.
                                                                             LANGLE
                                                                             LANGLE
      FM=MANGLE(IL, HTYPE)
                                                                             LANGLE
      XT=RANF(0.)
                                                                             LANGLE
      XI=1.+(FH-1.)+XT
                                                                             LANGLE
      IX=XI
                                                                             LANGLE
      1F(IX.EQ. NANGLE(IL.NTYPE)) IX=IX-1
```

```
IXP1=IX+1
                                                                           LANGLE
      THETAL=FLA(IL, MTYPE, IX)+.5*(FLA(IL, MTYPE, IXP1)-FLA(IL, MTYPE, IX))
                                                                           LANGLE
      PHIL=CE2PI * RANF(0.)
                                                                           LANGLE
C----THETAL. PHIL ARE LEAF INCLINATION AND AZIMUTH, RESPECTIVELY.
                                                                           LANGLE
      CONTINUE
                                                                           LANGLE
      SINL=SIN(THETAL)
                                                                           LANGLE
                                                                           LANGLE
      COSL=COS(THETAL)
      SINP=SIN(PHIL)
                                                                           LANGLE
                                                                           LANGLE
      COSP=COS(PHIL)
C----COMPUTE LEAF NORMAL DIRECTION COSINES
                                                                           LANGLE
      XLF=-SINL *COSP
                                                                           LANGLE
      YLF = - SINL + SINP
                                                                           LANGLE
                                                                           LANGLE
      ZLF=COSL
                                                                           LANGLE
C----SELECT RANDON LEAF REFLECTANCE AND TRANSMITTANCE VECTORS.
      CALL OPTICAL(XTYPE, IL)
                                                                           LANGLE
      RETURN
                                                                           LANGLE
      END
*DECK COP
                                                                           COP
      SUBROUTINE COP(ALPHA, BETA, OP)
                                                                           COP
C....THIS PROGRAM CALCULATES THE MEAN PROJECTION OF A UNIT LEAF AREA IN
                                                                           COP
C....THE DIRECTION OF THE SOURCE. THE LEAF IS INCLINED AT AN ANGLE
                                                                           COP
C....ALPHA AND IS ASSUMED TO BE AZIMUTHALLY ISOTROPIC. THE SOURCE
                                                                           COP
C....DIRECTION IS AT AN AZIMUTH OF ZERO AND AN INCLINATION OF BETA.
                                                                           COP
                                                                           COP
      COMMON/C1/DUH1(33), CEPIO2
                                                                           COP
      OP=COS(ALPHA) +SIN(BETA)
                                                                           COP
      IF(ALPHA.LE.BETA) RETURN
                                                                           COP
C....THETAO IS THE LEAF AZIMUTH ANGLE AT WHICH OP BECOMES NEGATIVE AND
                                                                           COP
C....IS IN THE FIRST QUADRANT. THE FUNCTION OP IS SYMMETRIC AND HENCE
                                                                           COP
C....IS AVERAGED OVER LEAF AZIMUTH ANGLES OF O TO PI RADIANS.
                                                                           COP
      THETAO=ACOS(TAN(BETA)/TAN(ALPHA))
                                                                           COP
      TANTO=TAN(THETAO)
                                                                           COP
      OP=OP+(1.+(TANTO-THETAO)/CEPIO2)
                                                                           COP
      RETURN
                                                                           COP
      END
                                                                           COP
*DECK COPM
      SUBROUTINE COPH(G.OP.OPH)
                                                                           COPH
C....THIS PROGRAM CALCULATES THE MEAN PROJECTION OF A UNIT LEAF AREA IN
                                                                           COPH
C....THE DIRECTION OF THE SOURCE (OPH) FOR THE SIMULATED CANOPY. THE
                                                                           COPM
C....LEAVES OF THE CANOPY ARE ASSUMED TO BE AZIMUTHALLY ISOTROPIC. THE
                                                                           COPH
C....OP FUNCTION USED IN THE CALCULATION HAS BEEN PREVIOUSLY DETERMINED
                                                                           COPM
C....FOR A GIVEN SOURCE BIRECTION FOR LEAF INCLINATION ANGLES OF
                                                                           COPM
C....5, 15, ..., 85 DEGREES. G IS THE LEAF INCLINATION ANGLE DENSITY
                                                                           COPH
C....FUNCTION.
                                                                           COPM
```

```
COPH
C
      DIMENSION OP(9),G(9)
                                                                             COPM
                                                                             COPH
      OPH=0.
                                                                             COPH
      DO 1 I=1,9
    1 OPM=OPM+OP(I)+G(I)
                                                                             COPH
                                                                              COPH
      RETURN
                                                                             COPM
      END
*DECK PDENS
      SUBROUTINE PDENS(IL, MTYPE, IANGLE, OPM)
                                                                             PDENS
C----THIS PROGRAM COMPUTES THE PROBABILITY THAT LIGHT AT INCIDENT ANGLE
                                                                             PDENS
     THETA(IANGLE) INTERACTS WITH MATERIAL TYPE HTYPE WITHIN CANOPY
C
                                                                             PDENS
C
     LAYER IL.
                                                                             PDENS
C
                                                                             PDENS
C
     INPUT
                                                                             PDENS
                                                                             PDENS
C
       IL
C
       MITTE
                                                                             PDENS
C
       IANGLE
                                                                             PDENS
                                                                             PDENS
C
       OPH
C
                                                                             PDENS
       SLAI
                                                                             PDENS
C
       FLAI
                                                                             PDENS
C
       THETA
C
     OUTPUT
                                                                             PDENS
                                                                             PBENS
C
       PHIT
C
                                                                             PDENS
      CONMON/C2/DUH(289), THETA(10)
      COMMON/C4/NANGLE(3,3),FLA(3,3,10),SLAI(3,3),FLAI(3,3),PHIT(3,3,10) PDENS
      ARG=1.-(SLAI(IL, NTYPE) *OPH/SIN(THETA(IANGLE)))
                                                                             PDENS
                                                                             PDENS
      IF (ARG.LE.O.) 60 TO 1
                                                                             PDENS
      PO=ARG++(FLAI(IL, MTYPE)/SLAI(IL, MTYPE))
      GO TO 2
                                                                             PDENS
      P0 = 0.
                                                                             PDENS
1
                                                                             PDENS
      WRITE(6,100) IANGLE
                                                                             PDENS
100
      FORMAT (1H0, * PO SET TO ZERO*, 15)
                                                                             PDENS
2
      CONTINUE
                                                                             PDENS
      PHIT(IL, HTYPE, IANGLE)=1.-PO
                                                                             PDENS
      RETURN
                                                                             PDENS
      END
*DECK PGAP
                                                                             PGAP
      SUBROUTINE PGAP(IL, IANGLE, IDIR, IHIT, NTYPE)
C----THIS PROGRAM DETERMINES IF AN INTERACTION IS BEING MADE IN LAYER IL PGAP
     AND SETS THE MATERIAL TYPE OF LAYER IL.
                                                                             PGAP
C
                                                                             PGAP
C
C
     INPUT
                                                                             PGAP
                                                                             PSAP
C
       IL
                                                                             PGAP
       IANGLE
C
```

```
PGAP
C
       IDIR
£
                                                                            PGAP
       NLAY
                                                                            PGAP
C
       MTP
C
       PHIT
                                                                            PBAP
C
     OUTPUT
                                                                            PGAP
C
                                                                            PGAP
       IHIT
C
                                                                            PGAP
       HTYPE
C
                                                                            PGAP
      COMMON/C4/NAMGLE(3,3),FLA(3,3,10),SLAI(3,3),FLAI(3,3),PHIT(3,3,10) PGAP
      COHHON/CHAT/HTP(3), NLAY
                                                                            PGAP
      REAL PHITN
                                                                            PGAP
      IF(IDIR.LT.O) GO TO 10
      ILAYER=NLAY+1-IL
                                                                            PGAP
      GO TO 20
                                                                            PGAP
   10 ILAYER=IL
                                                                            PGAP
C...MTP(ILAYER) GIVES THE LAST MTYPE WITHIN A LAYER WHICH CONTAINS THE COMBINED
    MTYPE DISTRIBUTION.
   20 HTYPE=HTP(ILAYER)
                                                                            PGAP
                                                                            PGAP
      IHIT=0
                                                                            PGAP
      TEST=RANF(0.)
                                                                            PGAP
      IF(PHIT(ILAYER, HTYPE, IANGLE).LT.TEST) GO TO 30
                                                                            PGAP
      IHIT=1
      IF (MTYPE.EQ.1) GO TO 30
C...A HIT HAS BEEN RECORDED - NOW WHAT BID IT HIT.
C...NORMALIZE THE 2 MATERIAL DISTIBUTION TO 1.0
      PHITN = PHIT(IL,1, IANGLE)/(PHIT(IL,1, IANGLE)+PHIT(IL,2, IANGLE))
      TEST = RANF(0.)
      IF (PHITH .LT.TEST) GO TO 40
      HTYPE = 1
      GO TO 30
   40 HTYPE = 2
                                                                            PGAP
   30 RETURN
      END
                                                                            PGAP
*DECK ETHRES
                                                                            ETHRES
      SUBROUTINE ETHRES(NLAY, NSOUR, IDIR)
C----THIS PROGRAM DETERMINES (FOR EACH LAYER AND FOR ALL LIGHT SOURCE
                                                                            ETHRES
     DIRECTIONS) IF THE SOURCE FLUX IS ABOVE THRESHOLD REDUIREMENTS IN
C
                                                                            ETHRES
C
     THE DIRECTION INDICATED BY IDIR. INDICATORS IGOD OR IGOU ARE SET
                                                                            ETHRES
C
     ACCORDINGLY.
                                                                            ETHRES
C
                                                                            ETHRES
C
     INPUT
                                                                            ETHRES
C
       NLAY
                                                                            ETHRES
C
       NSOUR
                                                                            ETHRES
C
       IDIR
                                                                            ETHRES
       NLAM
                                                                            ETHRES
```

```
C
       DR
                                                                             ETHRES
C
       UR
                                                                             ETHRES
C
       THRES
                                                                             ETHRES
C
     OUTPUT
                                                                             ETHRES
C
       IGOD
                                                                             ETHRES
C
       IGOU
                                                                             ETHRES
C
                                                                             ETHRES
                                                                             ETHRES
      COMMON/C1/DUMO(7), NLAH
      COMMON/C6/DR(4,10,17),UR(4,10,17),THRESD(10),IGOD(4,10),IGOU(4,10) ETHRES
     1,THRESU(10)
                                                                             ETHRES
C----BOUNUARD FLUX
                                                                             ETHRES
      IF(IDIR.6T.0) GO TO 10
                                                                             ETHRES
      NLAYER=NLAY+1
                                                                             ETHRES
      DO 2 I=1, NLAYER
                                                                             ETHRES
      DO 2 J=1, NSOUR
                                                                             ETHRES
                                                                             ETHRES
      IGOD(I.J)=0
      DO 1 K=1, NLAM
                                                                             ETHRES
                                                                             ETHRES
      IF(DR(I,J,K).LT.THRESD(J)) GO TO 1
                                                                             ETHRES
      IGOD(I,J)=1
                                                                             ETHRES
      60 TO 2
                                                                             ETHRES
    1 CONTINUE
    2 CONTINUE
                                                                             ETHRES
      RETURN
                                                                             ETHRES
                                                                             ETHRES
C----UPWARD FLUX
                                                                             ETHRES
10
      CONTINUE
      DO 4 I=1, NLAY
                                                                             ETHRES
      DO 4 J=2. NSOUR
                                                                             ETHRES
      IGOU(I,J)=0
                                                                             ETHRES
      DO 3 K=1, NLAM
                                                                             ETHRES
      IF(UR(I,J,K).LT.THRESU(J)) 60 TO 3
                                                                             ETHRES
      IGOU(I,J)=1
                                                                             ETHRES
      GO TO 4
                                                                             ETHRES
    3 CONTINUE
                                                                             ETHRES
    4 CONTINUE
                                                                             ETHRES
                                                                             ETHRES
      RETURN
                                                                             ETHRES
      END
*DECK SETZ
      SUBROUTINE SETZ(IL, IANGLE, IDIR)
                                                                             SETZ
C----THIS PROGRAM SETS THE FLUX (AND ITS APPROPRIATE INDICATORS) IN THE
                                                                             SETZ
     IDIR DIRECTION AT ANGLE THETA (IANGLE) IN LAYER IL TO ZERO.
                                                                             SETZ
C
C
                                                                             SETZ
C
     INPUT
                                                                             SETZ
C
                                                                             SETZ
       IL
                                                                             SETZ
C
       IANGLE
                                                                             SETZ
C
       IDIR
```

```
SET2
C
       NLAH
C
                                                                              SETZ
     CUTPUT
                                                                              SETZ
C
       DR
C
                                                                              SETZ
       UR
C
                                                                              SETZ
       IGOD
C
                                                                              SETZ
       IGOU
C
                                                                              SETZ
                                                                              SETZ
      COMMON/C1/BUN1(7), NLAM
                                                                              SETZ
      COMMON/C6/DR(4,10,17),UR(4,10,17),THRES(10),IGOB(4,10),IGOU(4,10)
      IF(IDIR.EQ.1) GO TO 10
                                                                              SETZ
C----DOWNWARD FLUX
                                                                              SETZ
                                                                              SETZ
      DO 1 K=1, NLAH
                                                                              SETZ
    1 DR(IL, IANGLE, K) = 0.
                                                                              SETZ
      IGOD(IL, IANGLE)=0
                                                                              SETZ
      RETURN
C----UPYARD FLUX
                                                                              SETZ
                                                                              SETZ
10
      CONTINUE
      DO 2 K=1, NLAN
                                                                              SETZ
    2 UR(IL, IANGLE, K)=0.
                                                                              SETZ
      IGOU(IL, IANGLE)=0
                                                                              SETZ
                                                                              SETZ
      RETURN
                                                                              SETZ
      END
*DECK OPTICAL
      SUBROUTINE OPTICAL (HTYPE, IL)
C----THIS PROGRAM SELECTS RANDOM LEAF REFLECTANCE AND TRANSMITTANCE
                                                                              OPTICAL
C
     VECTORS FOR NATERIAL TYPE HTYPE.
                                                                              OPTICAL
C
                                                                              OPTICAL
C
                                                                              OPTICAL
     INPUT
C
                                                                              OPTICAL
       MTYPE
C
       NVEC
                                                                              OPTICAL
C
                                                                              OPTICAL
       C
C
       UKX
                                                                              OPTICAL
C
     OUTPUT
                                                                              OPTICAL
C
       R.T
                                                                              OPTICAL
      COMMON/L1/DATAID(7,9),XNU(17,9),C(17,17,9),NVEC(9)
                                                                              OPTICAL
      COMMON/C2/CAMRH(17), SKYIH(17), DIFIH(17), R(17), T(17),
     1RG(17), XLAH(17), SOURCE(10,17), THETA(10)
      CONMON /KIH/ INL(3,3,2)
C... SELECT APPROPRIATE OPTICAL VECTOR GIVEN HTYPE, IL, AND R OR T VECTOR.
      I= INL(IL, HTYPE, 1)
      J=I+1
                                                                              OPTICAL
   11 CALL UTIL(XMU(1,I),R)
   13 CALL UTIL(XMU(1,J),T)
      RETURN
                                                                              OPTICAL
```

```
END
                                                                            OPTICAL
*DECK NRM
*DECK MATSOR
*DECK BLDATA
      BLOCK DATA
                                                                            BDAT
      CONMON/C1/DUN(30), CEDTR, CERTD, CENTR, CEPIO2, CE1PI, CE2PI
                                                                            TAGE
      DATA CEDTR, CERTB, CENTR/.017453293,57.2957795,.00029088821/
                                                                            BDAT
      DATA CEPIO2, CE1PI, CE2PI/1.57079632, 3.14159265, 6.28318530/
                                                                            BDAT
      END
                                                                            BDAT
*DECK TBLR
      SUBROUTINE TBLR(H, X, Y, XX, Z)
                                                                            TBLR
C
                                                                            TBLR
C....THIS PROGRAM FINDS THE INTEGRAL Z(X) OF THE FUNCTION Y(X) FROM X(1) TBLR
C....TO X(2H-1) USING SIMPSONS RULE THE INTEGRAL Z(X) IS NORMALIZED TO T3LR
C....1.0 AT X(2M-1). THE TABLE OF Z VERSUS X IS THEN INVERTED TO DETER- TBLR
C....MINE X AS A FUNCTION OF Z AT M REGULARLY SPACED POINTS ALONG Z.
                                                                            T3LR
C
     INPUT VARIABLES
                                                                            TBLR
C
       M = DESIRED NUMBER OF REGULARLY SPACED POINTS ALONG Z
                                                                            TBLR
                                                                            TBLR
       X = SPECIFIED AT 2M-1 POINTS
       Y = SPECIFIED AT 2N-1 POINTS
                                                                            TBLR
C
     OUTPUT VARIABLES
                                                                            TBLR
       XX = THE TABLE OF X VALUES FOR M REGULARLY SPACED POINTS
C
                                                                            TBLR
C
            (M-1 INTERVALS) ALONG Z.
                                                                            TBLR
C
         = THE NORMALIZED INTEGRAL OF Y AT X(1), X(3), ..., X(2M-1).
                                                                            TBLR
                                                                            TBLR
      DIMENSION X(19), Y(19), Z(10), XI(10), XX(10)
                                                                            TBLR
C....SIMPSONS RULE INTEGRATION
                                                                            TBLR
10
      Z(1) = 0.0
                                                                            TBLR
      DX = X(2) - X(1)
                                                                            TBLR
20
      D0 50 J = 2.M
                                                                            TBLR
      J0 = 2*J - 3
                                                                            TBLR
                                                                            TBLR
      J1 = 2*J - 2
30
      J2 = 2*J - 1
                                                                            TBLR
40
      Z(J) = Z(J - 1) + BX*(Y(J0) +4.*Y(J1) + Y(J2))/3.0
                                                                            TBLR
      XI(J) = X(J2)
50
                                                                            TBLR
      XI(1)=X(1)
                                                                            TBLR
C....NORMALIZE INTEGRAL Z(X)
                                                                            TBLR
60
      DO 70 J = 1,H
                                                                            TBLR
70
      Z(J) = Z(J)/Z(H)
                                                                            TBLR
C....FIND X AT M REGULARLY SPACED POINTS ALONG Z.
                                                                            TBLR
      XX(1) = X(1)
                                                                            TBLR
      EH = N - 1
                                                                            TBLR
      F = 1.0/EN
                                                                            TBLR
                                                                            TBLR
      JS=2
```

```
TBLR
80
      DO 120 K = 2,H
      ZT = K - 1
                                                                               TBLR
                                                                               TBLR
      ZT = ZT*F
                                                                               TBLR
90
      DO 110 J =JS.M
      IF(Z(J) - ZT) 110, 100, 100
                                                                               TBLR
100
                                                                               TBLR
      G = (ZT - Z(J - 1)) /(Z(J) - Z(J - 1))
      XX(K) = XI(J - 1) + G*(XI(J) - XI(J - 1))
                                                                               TBLR
      GO TD 115
                                                                               T3LR
      CONTINUE
                                                                               TBLR
110
                                                                               TBLR
115
      JS=J
                                                                               TBLR
120
      CONTINUE
                                                                               TBLR
      RETURN
      END
                                                                               TBLR
C
                                                                               SUN
      SUBROUTINE SUN
                                                                               SUN
C----THIS PROGRAM CALCULATES THE POSITION OF THE SUN
                                                                               SUN
C
     INPUT
                                                                               SUN
C
                                                                               SUN
       TIME
C
                                                                               SUN
       BLAT
C
                                                                               SUN
       DEC
C
     DUTPUT
                                                                               SUN
                                                                               SUN
C
       SINLAT, COSLAT
C
                                                                               SUN
       SINDEC, COSDEC
C
                                                                               SUN
       COSH
C
       SINZ, COSZ
                                                                               KUZ
C
       SINAZ, COSAZ
                                                                               SUN
C
                                                                               SUN
       LXS, LYS, LZS
C
                                                                               SUN
C
         TIME OF SIMULATION (HOURS)
                                                                               SUN
C
         GLAT IS SITE GEOGRAPHICAL LATITUDE
                                                                               SUN
C
         GLONG IS SITE LONGITUDE
                                                                               SUN
         DEC IS SOLAR DECLINATION
                                                                               SUN
         H IS SOLAR HOUR ANGLE
                                                                               SUN
         COSZ IS COSINE OF SOLAR ZENITH ANGLE
                                                                               SUN
C
         COSAZ IS COSINE OF SOLAR AZINUTH
                                                                               SUN
C
         LXS, LYS, LZS ARE SOLAR DIRECTION COSINES
                                                                               SUN
С
                                                                               SUN
                                                                               SUN
      COMMON/C1/DAY, YEAR, TIME, GLAT, GLONG, DEC, DUM(24),
                                                                               SUN
     1CEDTR, CERTD, CENTR, DUM2(17),
     2SINLAT, COSLAT, SINDEC, COSDEC, COSH, SINZ, COSZ, SINAZ, COSAZ, LXS, LYS, LZS SUN
                                                                               SUN
      REAL LXS.LYS.LZS
                                                                               SUN
      H=ABS(((12.-TIME)+15.)+CEDTR)
                                                                               SUN
      SINLAT=SIN(GLAT)
```

COSLAT=COS(GLAT)	SUN
SINDEC=SIN(DEC)	NUS
COSDEC=COS(DEC)	SUN
COSH=COS(H)	SUN
COSZ=SINLAT+SINBEC+COSLAT+COSDEC+COS	H SUN
SINZ=SQRT()COSZ+COSZ)	SUN
COSAZ=(SINDEC-SINLAT+COSZ)/(COSLAT+S	INZ) SUN
SINAZ=SURT(1COSAZ+COSAZ)	SUN
LXS=SINZ*COSAZ	SUN
LYS=SINZ+SINAZ	SUN
LZS=COSZ	SUN
RETURN	KUR
EXD	SUN
C	
SUBROUTINE UTIL(A,B)	UTIL
CSET VECTOR B = VECTOR A	UTIL
CONNON/C1/DUN(7), NLAH	UTIL
DIMENSION A(17), B(17)	UTIL
DO 1 I=1, NLAN	UTIL
1 B(I)=A(I)	UTIL
RETURN	UTIL
END	UTIL
C	
SUBROUTINE FUN(A,B)	FUN
RETURN	FUN
END	FUN

APPENDIX B: GEOMETRICAL MATRICES FOR THEORETICAL CANOPIES

Planophile Canopy Geometry

	PROSABI	LITY OF	OCCURRENCE
INCLINATION ANGLE	LAYER 1	LAYER	
0.0	.105	.105	.105
5.0	.104	.104	.104
10.0	.102	.102	.102
15.0	.098	.098	.098
20.0	.093	.093	.093
25.0	.086	.086	.086
30.0	.079	.079	.079
35.0	.071	.071	.071
40.0	.062	.062	.062
45.0	.053	.053	
50.0	.043	.043	
55.0	.035	.035	.035
60.0	.026	.026	
65.0	.019	.019	
70.0	.012	.012	
75.0	.007	.007	
80.0	.003	.003	
85.0	.001	.001	
90.0	0.000	0.000	

CANOPY GEOMETRY INPUT DATA FOR PLANOPHILE, LAI=1

LEAF AREA INDEX

LAYER 1 LAYER 2 LAYER 3

.25 .50 .25

CANOPY DENSITY PARAMETERS

LAYER 1 LAYER 2 LAYER 3

.10 .10 .10

GEONETRICAL VIEW ANGLE FACTOR MATRIX

				ZENITH	ANGLE				
	5.0	15.0	25.0	35.0	45.0	55.0	45.0	75.0	85.0
LAYER 1	.5606	.2652	.2094	.1913	.1846	.1820	.1812	.1810	.1810
LAYER 2	.3546	.3380	.2964	.2798	.2732	.2707	.2699	.2697	-2694
LAYER 3	.0476	.1052	.1035	.1012	.1001	.0996	.0995	.0994	.0994
GROUND	.0373	-2916	.3907	.4277	.4422	.4477	.4495	.4499	-4499

			FROM	ROM			
TO	SKY	LAYER 1	LAYER 2	LAYER 3	BROUND		
LAYER 1	.8695	-2540	.3385	.1087	.4222		
LAYER 2	.5973	.1663	.4657	. 1663	.5973		
LAYER 3	.4222	-1087	.3385	.2540	.8695		

CANOPY GEONETRY INPUT DATA FOR PLANOPHILE, LAI=4

LEAF AREA INDEX

LAYER 1 LAYER 2 LAYER 3

1.00 2.00 1.00

CANOPY BENSITY PARAMETERS

LAYER 1 LAYER 2 LAYER 3

.10 .10 .10

GEONETRICAL VIEW ANGLE FACTOR NATRIX

ZENITH ANGLE									
	5.0	15.0	25.0	35.0	45.0	55.0	65.0	75.0	85.0
LAYER 1	.9627	.7084	.6093	.5723	.5578	.5523	.5505	.5501	.5501
LAYER 2	.0372	.2668	.3311	.3495	.3557	.3579	.3587	.3588	.3589
LAYER 3	0.0000	.0176	.0363	.0448	.0482	.0495	.0500	.0501	.0501
BROUND	0.0000	.0072	.0233	.0335	.0382	.0402	.0408	.0410	-0410

OT	SKY	LAYER 1	FROM Layer 2	*****		
LAYER 1	.5973	.7983	.4944	.0588	.0441	
LAYER 2	.1578	.2196	1.2381	.2196	.1578	
LAYER 3	.0441	.0588	.4944	.7983	.5973	

CANOPY GEOMETRY INPUT DATA FOR PLANOPHILE, LAI=7

LEAF AREA INDEX

LAYER 1	LAYER 2	LAYER 3
4 75	7 54	4 35

CANOPY DENSITY PARAMETERS

LAYER 1	LAYER 2	LAYER 3
10	10	10

GEONETRICAL VIEW ANGLE FACTOR MATRIX

				LENIIN	WARRE				
	5.0	15.0	25.0	35.0	45.0	55.0	65.0	75.0	85.0
LAYER 1	.9968	.8843	.8069	.7738	.7602	.7550	.7533	.7529	.7528
LAYER 2	.0032	.1141	.1859	.2146	.2260	.2303	.2317	.2321	.2321
LAYER 3	0.0000	.0014	.0058	.0090	.0105	.0111	.0113	.0114	.0114
GROUND	0.0000	.0002	.0014	.0026	.0033	.0036	.0037	.0037	.0037

			FROM				
TO	SKY	LAYER 1	LAYER 2	LAYER 3	GROUND		
LAYER 1	.4222	1.1484	.4011	.0162	.0049		
LAYER 2	.0441	.1516	1.6014	.1516	.0441		
LAYER 3	.0049	.0162	.4011	1.1484	.4222		

Erectophile Canopy Geometry

	PROBABI	OCCURRENCE		
INCLINATION ANGLE	LAYER 1	LAYER	2 LAYER 3	
0.0	0.000	0.000	0.000	
5.0	.001	.001	.001	
10.0	.003	.003	.003	
15.0	.007	.007	.007	
20.0	.012	.012	.012	
25.0	.019	.019	.019	
30.0	.026	.026	.026	
35.0	.035	.035	.035	
40.0	.043	.043	.043	
45.0	.053	.053	.053	
50.0	.062	.062	.062	
55.0	.071	.071	.071	
60.0	.079	.079	.079	
65.0	.086	.084	.086	
70.0	.093	.093	.093	
<i>7</i> 5.0	.098	.098	.098	
80.0	.102	.102	.102	
85.0	.104	.104	.104	
90.0	.105	.105	.105	

CANOPY GEOMETRY INPUT DATA FOR ERECTOPHILE, LAI=1

LEAF AREA INDEX

LAYER 1 LAYER 2 LAYER 3

.25 .50 .25

CANOPY DENSITY PARAMETERS

LAYER 1 LAYER 2 LAYER 3

.10 .10 .10

GEONETRICAL VIEW ANGLE FACTOR MATRIX

ZENITH ANGLE									
	5.0	15.0	25.0	35.0	45.0	55.0	65.0	75.0	85.0
LAYER 1	.9056	. 4333	.2770	.2036	.1620	.1365	.1204	.1109	.1064
LAYER 2	.0936	.3847	.3451	.2912	.2495	.2196	.1991	.1863	.1801
LAYER 3	.0008	.0789	.1047	.1028	.0953	.0879	.0820	.0780	.0759
BROUND						.5561			

TO	SKY	LAYER 1	FROM Layer 2	LAYER 3	GROUND
LAYER 1	.7591	.4716	.3378	.0864	.3350
LAYER 2	.4764	.1540	.7292	.1540	.4764
LAYER 3	.3350	-0864	.3378	-4716	.7591

CANOPY GEOMETRY INPUT DATA FOR ERECTOPHILE, LAI=4

LEAF AREA INDEX

LAYER 1	LAYER 2	LAYER 3
1.00	2.00	1.00

CANOPY DENSITY PARAMETERS

LAYER 1	LAYER 2	LAYER 3
10	10	-10

GEOMETRICAL VIEW ANGLE FACTOR MATRIX

		ANGLE							
	5.0	15.0	25.0	35.0	45.0	55.0	65.0	75.0	85.0
LAYER 1	.9999	.8969	.7268	.5976	.5069	.4439	.4015	.3752	.3625
LAYER 2	-0001	.1020	.2528	.3372	.3732	.3841	.3841	.3809	.3784
LAYER 3	0.0000	.0010	.0148	.0389	8040.	.0763	.0861	.0915	.0939
GROUND	0.0000	.0001	.0056	.0262	.0591	.0956	.1283	.1524	.1652

			FROM		
10	SKY	LAYER 1	LAYER 2	LAYER 3	GROUND
LAYER 1	.4764	1.0372	.3794	.0467	.0502
LAYER 2	.1377	.1627	1.3891	.1627	.1377
LAYER 3	.0502	.0467	.3794	1.0372	.4764

CANOPY GEONETRY INPUT DATA FOR ERECTOPHILE, LAI=7

LEAF AREA INDEX

LAYER 1 LAYER 2 LAYER 3

1.75 3.50 1.75

CANOPY DENSITY PARAMETERS

LAYER 1 LAYER 2 LAYER 3

.10 .10 .10

GEONETRICAL VIEW ANGLE FACTOR MATRIX

ZENITH ANGLE									
	5.0	15.0	25.0	35.0	45.0	55.0	65.0	75.0	85.0
LAYER 1	1.0000	.9812	.8967	.7967	.7098	.6419	.5928	.5609	.5451
LAYER 2	0.0000	.0188	.1022	-1949	.2657	.3122	.3397	.3544	.3607
LAYER 3	0.0000	0.0000	.0010	.0067	.0173	.0295	.0400	.0475	.0513
BROUND	0.0000	0.0000	.0001	.0017	.0071	.0164	.0275	.0372	.0428

το	SKY	LAYER 1	FRON Layer 2	LAYER 3	GROUND
LAYER 1	.3350	1.3200	.3057	.0188	.0105
LAYER 2	.0502	.1151	1.6592	.1151	.0502
LAYER 3	.0105	-0188	.3057	1.3200	.3350

Plagiophile Canopy Geometry

	PROBABILITY OF OCCURRENCE				
INCLINATION ANGLE	LAYER 1	LAYER			
0.0	0.000	0.000	0.000		
5.0	.003	.003	.003		
10.0	.013	.013	.013		
15.0	.028	.028	.028		
20.0	.046	.046	.046		
25.0	.065	.065	.065		
	.083	.083	.083		
30.0	.098	.098	.098		
35.0	.108	.108	.108		
40.0	.111	.111	.111		
45.0		.108	.108		
50.0	.108	-	.078		
55.0	.098	.098	.083		
60.0	.083	.083			
65.0	.065	.065	.065		
70.0	.046	.046	.046		
75.0	.028	.028	.028		
80.0	.013	.013	.013		
85.0	.003	.003	.003		
90.0	0.000	0.000	0.000		

CANOPY GEOMETRY INPUT DATA FOR PLAGIOPHILE, LAI=1

LEAF AREA INDEX

LAYER 1 LAYER 2 LAYER 3

.25 .50 .25

CANOPY BENSITY PARAMETERS

LAYER 1 LAYER 2 LAYER 3

.10 .10 .10

GEONETRICAL VIEW ANGLE FACTOR MATRIX

				ZENITH	ANGLE				
	5.0	15.0	25.0	35.0	45.0	55.0	65.0	75.0	85.0
LAYER 1	.8005	.3622	.2461	.2003	.1801	-1716	.1684	.1676	.1676
LAYER 2				.2883					
LAYER 3	.0064	.0940	.1055	.1024	.0993	.0975	.0969	-0967	.0967
GROUND	.0016	. 1454	.3230	-4090	.451R	.4710	4782	4800	- 4802

TO	SKY	LAYER 1	FROM Layer 2	LAYER 3	GROUND
LAYER 1	-8124	.3680	.3525	.0976	.3622
LAYER 2	.5212	.1665	.6173	.1665	.5212
LAYER 3	.3622	.0976	.3525	.3680	.8124

CANOPY GEONETRY INPUT BATA FOR PLAGIOPHILE, LAI=4

LEAF AREA INDEX

LAYER 1	LAYER 2	LAYER 3
1.00	2.00	1.00

CANOPY DENSITY PARAMETERS

LAYER 1	LAYER 2	LAYER 3
10	10	10

GEONETRICAL VIEW ANGLE FACTOR MATRIX

				ZENITH	ANGLE				
	5.0	15.0	25.0	35.0	45.0	55.0	45.0	75.0	85.0
LAYER 1	.9984	.8346	.6770	.5910	.5482	- 5290	.5218	5200	.5198
LAYER 2	.0016	.1609	. 2893	.3406	. 350A	7445	7400	7404	
LAYER 3	0.0000	.0038	A228	-0404	AEA4	.3003	.3000		.3695
GROUND	0.0000	2000						.0575	.0575
UNUUND	0.000	.000/	.0109	.0280	.0417	.0492	.0523	.0531	.0532

TO	SKY	LAYER 1	FRON Layer 2	LAYER 3	GROUND
LAYER 1	.5212	.9503	.4337	.0491	.0384
LAYER 2	.1335	.1892	1.3425	.1892	.1335
LAYER 3	.0384	.0491	.4337	.9503	.5212

CANOPY GEONETRY INPUT BATA FOR PLAGIOPHILE, LAI=7

LEAF AREA INDEX

LAYER 1 LAYER 2 LAYER 3

1.75 3.50 1.75

CANOPY DENSITY PARAMETERS

LAYER 1 LAYER 2 LAYER 3

.10 .10 .10

GEONETRICAL VIEW ANGLE FACTOR MATRIX

	ZENITH ANGLE								
	5.0	15.0	25.0	35.0	45.0	55.0	65.0	75.0	85.0
LAYER 1	1.0000	.9571	.8616	.7908	.7510	.7322	.7250	.7232	.7230
LAYER 2	0.0000	.0428	.1357	.2000	.2335	-2486	.2542	.2556	.2557
LAYER 3	0.0000	.0001	.0023	.0072	.0116	.0141	.0151	.0153	.0154
GROUND	0.0000	0.000	.0004	0019	.0038	.0051	0057	0059	0059

TO	SKY	LAYER 1	FRON Layer 2	LAYER 3	GROUND
LAYER 1	.3622	1.2683	.3433	.0142	.0047
LAYER 2	.0384	.1271	1.6617	.1271	.0384
LAYER 3	-0047	.0142	.3433	1.2683	.3622

Extremophile Canopy Geometry

	PROBABILITY OF OCCURRENCE				
INCLINATION ANGLE	LAYER 1	LAYER	2 LAYER 3		
0.0	.100	.100	.100		
5.0	.097	.097	.097		
10.0	.088	.088	.088		
15.0	.075	.075	.075		
20.0	.059	.059	.059		
25.0	.041	.041	-041		
30.0	.025	.025	.025		
35.0	.012	.012	.012		
40.0	-003	.003	.003		
45.0	0.000	0.000	0.000		
50.0	.003	.003	.003		
55.0	.012	.012	.012		
60.0	.025	.025	.025		
65.0	.041	.041	-041		
70.0	-059	.059	.059		
75.0	.075	.075	.075		
80.0	.088	.088	.088		
85.0	.097	.097	.097		
90.0	.100	.100	.100		

CANOPY GEOMETRY INPUT DATA FOR EXTREMOPHILE, LAI=1

LEAF AREA INDEX

LAYER 1 LAYER 2 LAYER 3

.25 .50 .25

CANOPY DENSITY PARAMETERS

LAYER 1 LAYER 2 LAYER 3

.10 .10 .10

GEONETRICAL VIEW ANGLE FACTOR MATRIX

				TENTIH	RNGLE				
	5.0	15.0	25.0	35.0	45.0	55.0	65.0	75.0	85.0
LAYER 1	.7427	.3437	.2414	.1949	.1672	.1484	.1354	.1270	.1228
LAYER 2	.2403	.3736	.3221	.2832	.2552	.2340	.2183	.2077	.2023
LAYER 3	.0126	.0972	.1054	.1017	.0966	.0917	.0875	.0845	.0829
GROUND	.0044	.1855	.3311	.4202	.4811	.5259	.5588	.5808	.5920

TO	SKY	LAYER 1	FROM Layer 2	LAYER 3	GROUND
, ,	VN I	CHICK I	Enite 2	EHIEK U	
LAYER 1	.8350	.3202	.3383	.0971	.3995
LAYER 2	.5572	.1618	.5521	.1618	.5572
LAYER 3	.3995	.0971	.3383	.3202	.8350

CANOPY GEOMETRY INPUT DATA FOR EXTREMOPHILE, LAI=4

LEAF AREA INDEX

LAYER 1	LAYER 2	LAYER 3
1 00	2 00	1 00

CANOPY DENSITY PARAMETERS

LAYER 1	LAYER 2	LAYER 3
.10	.10	.10

GEONETRICAL VIEW ANGLE FACTOR MATRIX

	ZENITH ANGLE								
	5.0	15.0	25.0	35.0	45.0	55.0	65.0	75.0	85.0
LAYER 1	.9956	.8145	.6689	.5798	.5189	.4741	.4412	.4192	.4080
LAYER 2	.0044	.1792	.2948	.3460	.3697	.3804	.3843	.3849	.3845
LAYER 3	0.0000	.0052	.0243	.0430	.0578	.0690	.0770	.0821	.0846
GROUND	0.0000	.0012	.0120	.0312	.0536	.0765	.0975	.1138	.1228

TO	SKY	LAYER 1	FROM Layer 2	LAYER 3	GROUND
LAYER 1	.5572	.8756	.4436	.0576	.0561
LAYER 2	.1643	.1956	1.2704	.1956	.1643
LAYER 3	.0561	.0576	.4436	.8756	.5572

CANOPY GEOMETRY INPUT BATA FOR EXTREMOPHILE, LAI=7

LEAF AREA INDEX

LAYER 1	LAYER 2	LAYER 3
1 75	3 50	1 75

CANOPY DENSITY PARAMETERS

LAYER 1	LAYER 2	LAYER 3		
.10	.10	.10		

GEONETRICAL VIEW ANGLE FACTOR NATRIX

				ZENITH ANGLE					
	5.0	15.0	25.0	35.0	45.0	55.0	65.0	<i>7</i> 5.0	85.0
LAYER 1	.9999	.9482	.8544	.7821	.7236	.6768	.6404	.6152	.6020
LAYER 2	.0001	.0517	.1404	.2074	.2550	.2891	.3127	.3274	.3344
LAYER 3	0.0000	.0001	.0020	.0061	.0111	.0162	.0207	.0241	.0259
GROUND	0.0000	0.0000	.0010	.0044	.0103	.0179	.0262	.0334	.0376

			FROM			
TO	SKY	LAYER 1	LAYER 2	LAYER 3	GROUND	
LAYER 1	.3983	1.1936	.3674	.0149	.0160	
LAYER 2	.0558	.1427	1.5931	.1036	.0949	
LAYER 3	.0125	.0273	.5174	.8756	.5572	

Spherical Canopy Geometry

	PROBABI	OCCURRENCE	
INCLINATION ANGLE	LAYER 1	LAYER	2 LAYER 3
0.0	.056	.056	.056
5.0	.056	.056	.056
10.0	.056	.056	.056
15.0	.056	.056	.056
20.0	.056	.056	.056
25.0	.056	.056	.056
30.0	.056	.056	.056
35.0	.056	.056	.056
40.0	.056	.056	.056
45.0	.056	.056	.056
50.0	.056	.056	.056
55.0	.056	.056	.056
60.0	.056	.056	.056
65.0	.056	.056	.056
70.0	.056	.056	.056
75.0	.056	.056	.056
80.0	.056	.056	.056
85.0	.056	.056	.056
90.0	.056	.056	.056

CANOPY GEOMETRY INPUT DATA FOR SPHERICAL, LAI=1

LEAF AREA INDEX

LAYER 1	LAYER 2	LAYER 3
.25	.50	.25

CANOPY DENSITY PARAMETERS

LAYER 1	LAYER 2	LAYER 3
-10	.10	. 10

GEOHETRICAL VIEW ANGLE FACTOR MATRIX

				ZENITH	ZENITH ANGLE					
	5.0	15.0	25.0	35.0	45.0	55.0	65.0	75.0	85.0	
LAYER 1	.7712	.3525	.2437	.1975	.1733	.1594	.1511	.1464	.1442	
LAYER 2				.2856						
LAYER 3	.0092	.0957	.1054	.1021	.0979	.0947	.0924	.0911	.0904	
GROUND	.0027	.1758	.3273	.4148	.4670	.4992	.5192	.5309	.5364	

			FROM		
TO	SKY	LAYER 1	LAYER 2	LAYER 3	GROUND
LAYER 1	.8244	.3427	.3455	.0974	.3814
LAYER 2	.5398	-1643	.5832	.1643	.5398
LAYER 3	.3814	.0974	.3455	.3427	.8244

CANOPY GEONETRY INPUT DATA FOR SPHERICAL, LAI=4

LEAF AREA INDEX

LAYER 1 LAYER 2 LAYER 3

1.00 2.00 1.00

CANOPY DENSITY PARAMETERS

LAYER 1 LAYER 2 LAYER 3

.10 .10 .10

GEOMETRICAL VIEW ANGLE FACTOR MATRIX

	ZENITH ANGLE								
	5.0	15.0	25.0	35.0	45.0	55.0	65.0	75.0	85.0
LAYER 1	.9973	.8242	.6727	.5852	.5330	.5008	.4808	.4691	. 4636
LAYER 2	.0027	.1703	.2922	.3435	.3652	.3748	.3792	.3813	.3821
LAYER 3	0.0000	.0045	.0236	.0418	.0543	.0623	.0673	.0702	.0715
BROUND	0.0000	-0010	-0115	-0296	.0476	-0621	.0727	-0794	-0828

LONG WAVE TRANSFER MATRIX

	FROM								
TO	SKY	LAYER 1	LAYER 2	LAYER 3	GROUND				
LAYER 1	.5398	.9118	.4395	.0536	.0468				
LAYER 2	.1489	.1928	1.3079	.1928	.1489				
LAYER 3	.0468	.0536	.4395	.9118	.5398				

CANOPY GEOMETRY INPUT BATA FOR SPHERICAL, LAI=7

LEAF AREA INDEX

LAYER 1 LAYER 2 LAYER 3

1.75 3.50 1.75

CANOPY DENSITY PARAMETERS

LAYER 1 LAYER 2 LAYER 3

.10 .10 .10

GEONETRICAL VIEW ANGLE FACTOR MATRIX

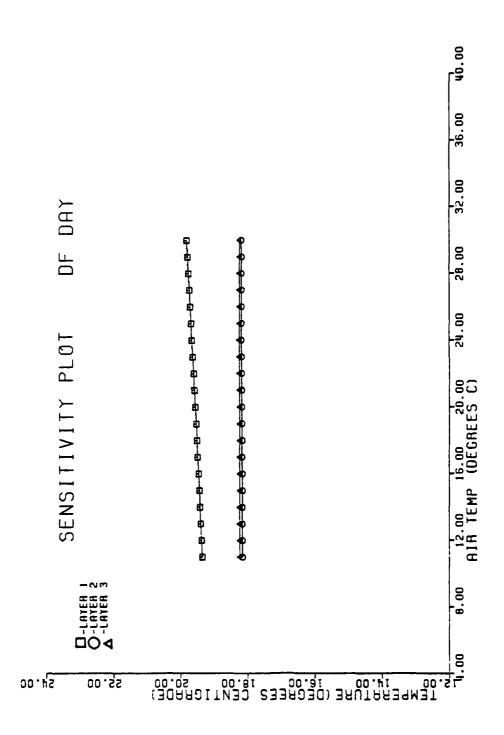
	ZENITH ANGLE								
	5.0	15.0	25.0	35.0	45.0	55.0	65.0	75.0	85.0
LAYER 1	1.0000	.9523	.8584	.7856	.7362	.7035	.6824	.6698	.6638
LAYER 2	0.0000	.0476	.1388	.2046	.2455	.2704	.2855	.2942	. 2982
LAYER 3	0.0000	.0001	.0024	.0077	.0135	.0183	.0219	.0241	.0252
BROUND	0.0000	0.0000	.0004	-0021	.0048	-0077	-0102	-0119	.0128

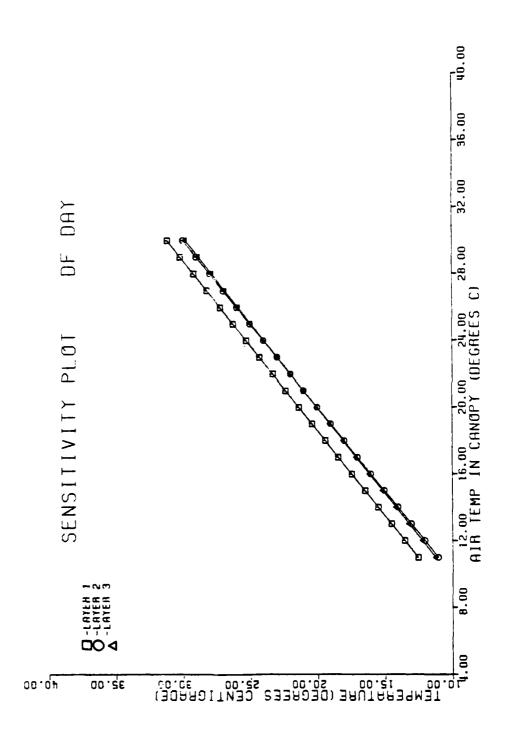
LONG WAVE TRANSFER MATRIX

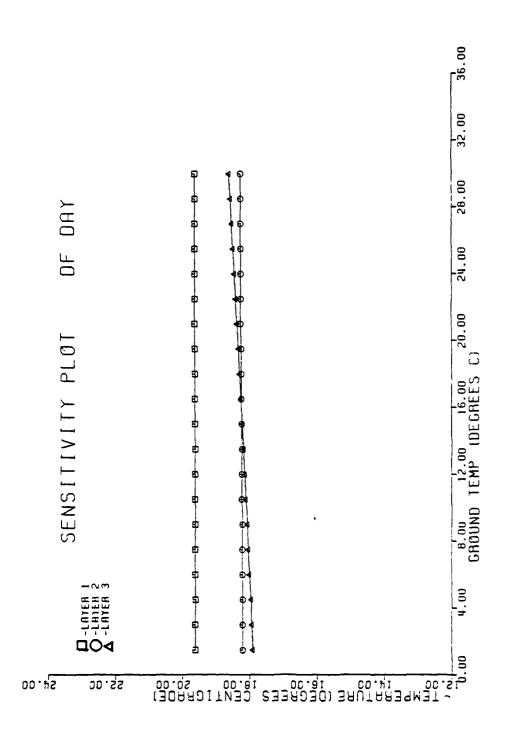
TO	SKY	LAYER 1	FROM Layer 2	LAYER 3	GROUND
LAYER 1	.3814	1.2286	.3570	.0175	.0069
LAYER 2	.0468	.1354	1.6271	.1354	.0468
LAYER 3	.0069	.0175	.3570	1.2286	.3814

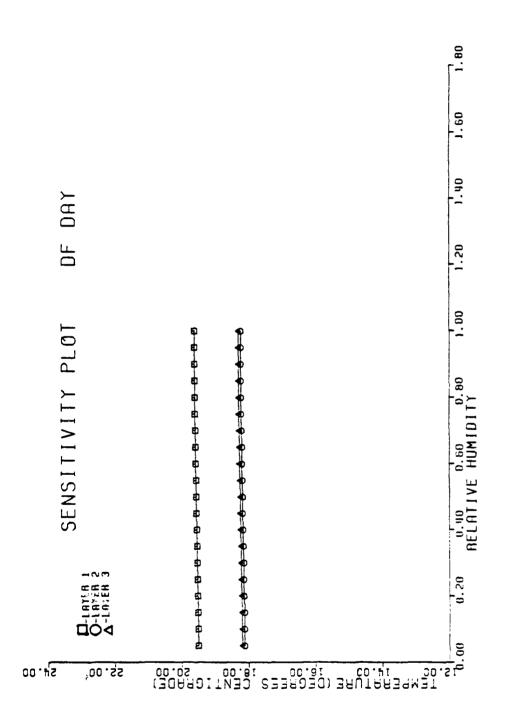
APPENDIX C: SENSITIVITY ANALYSIS RESULTS

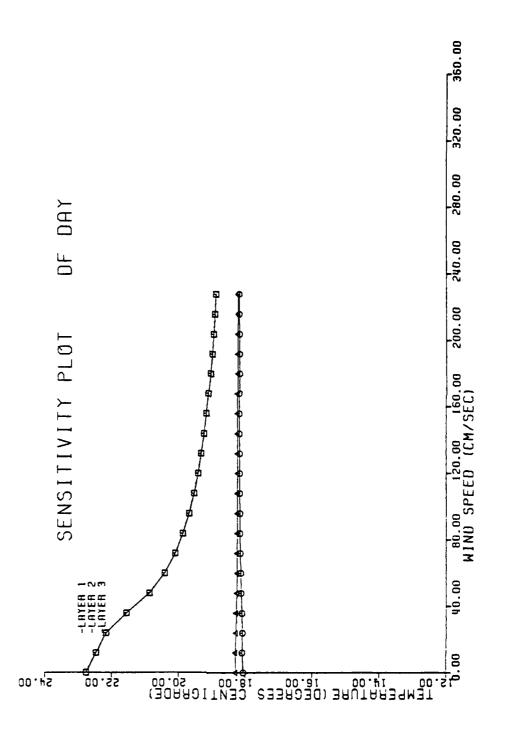
Douglas-Fir Daytime Sensitivity Plots

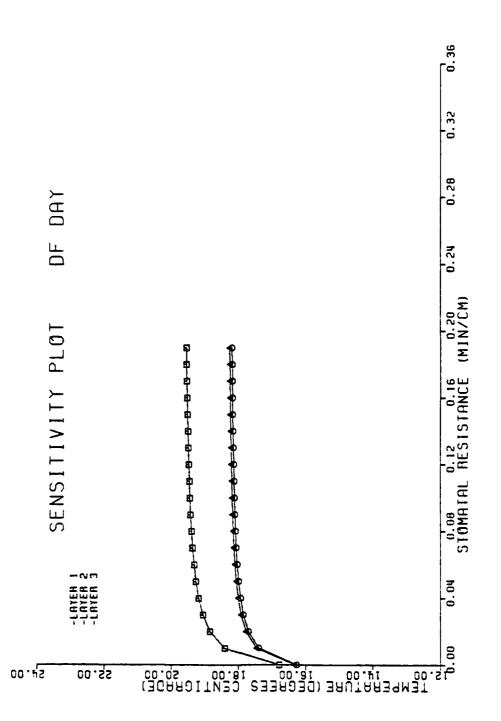


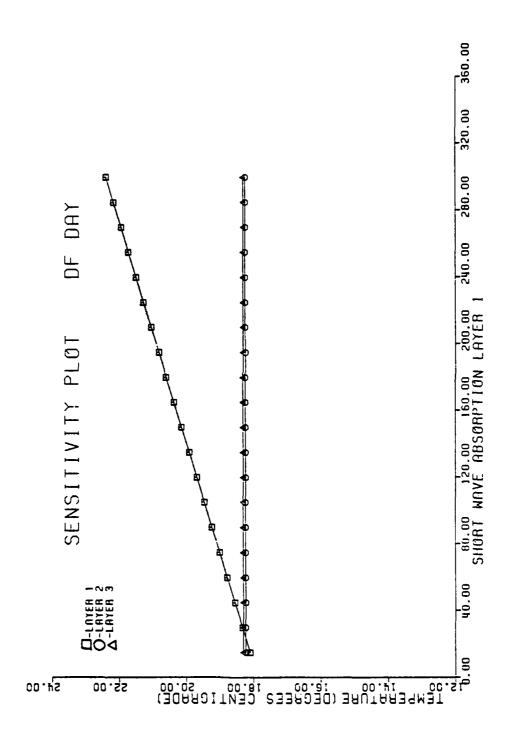


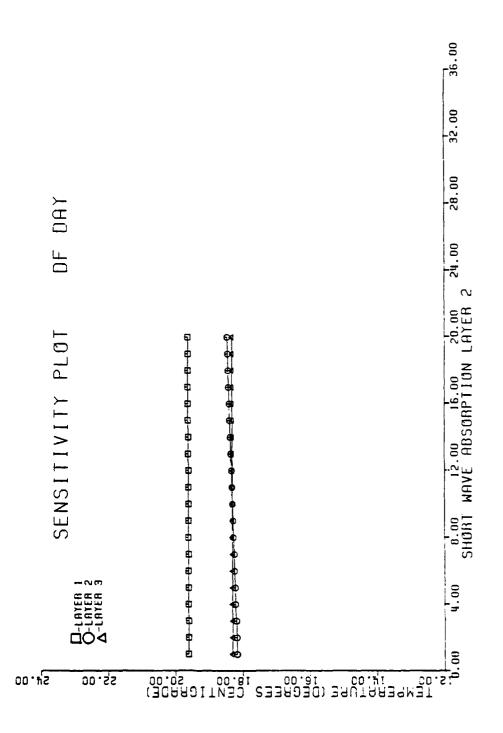


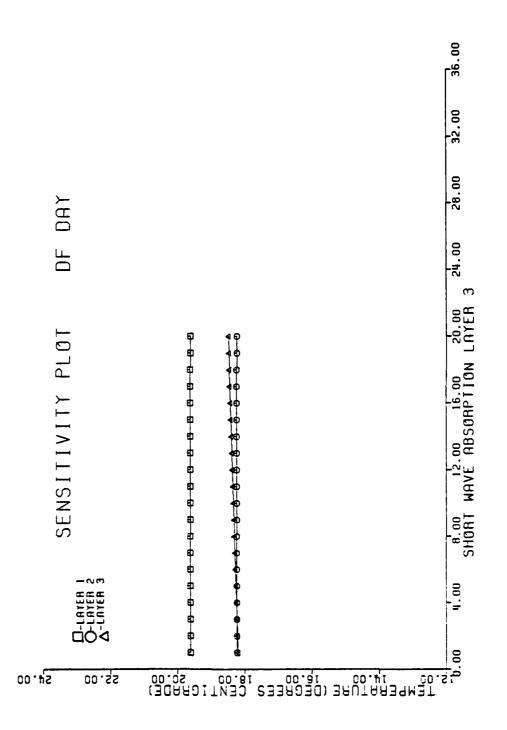


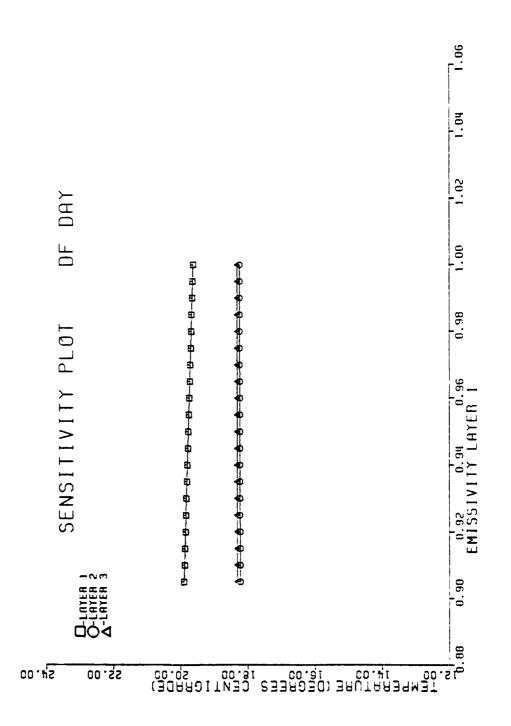


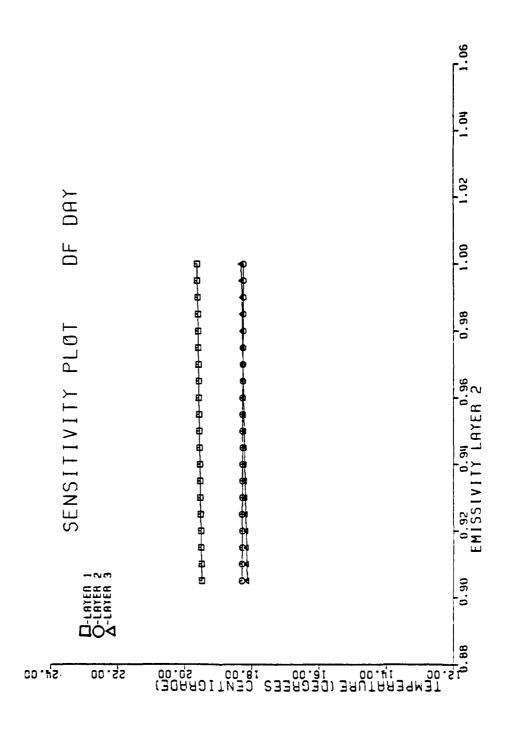


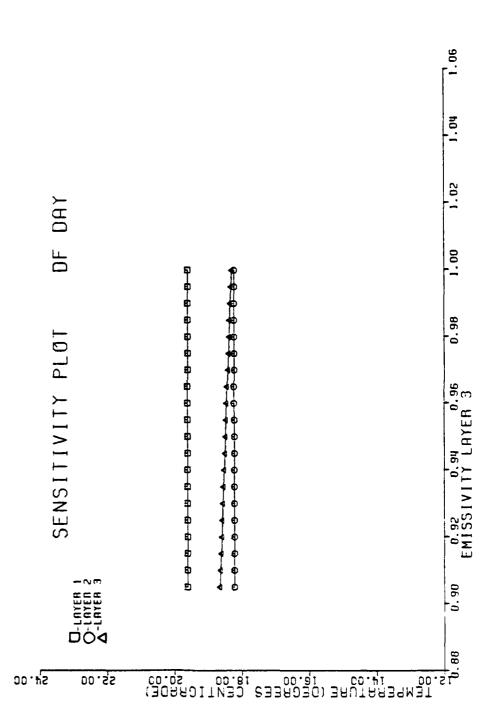


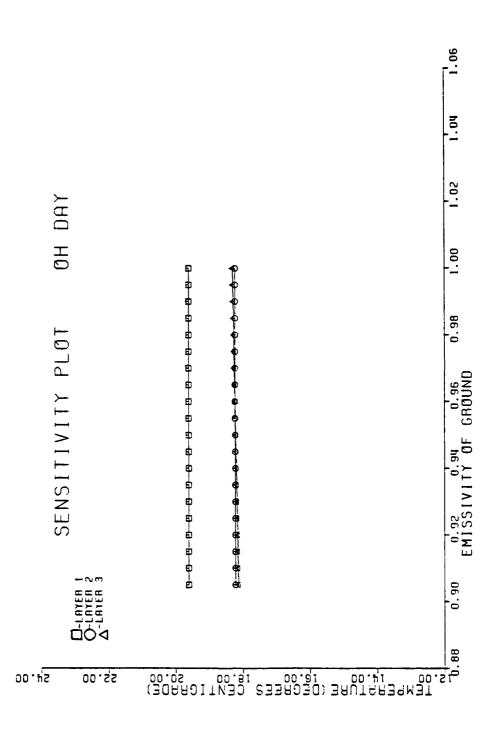


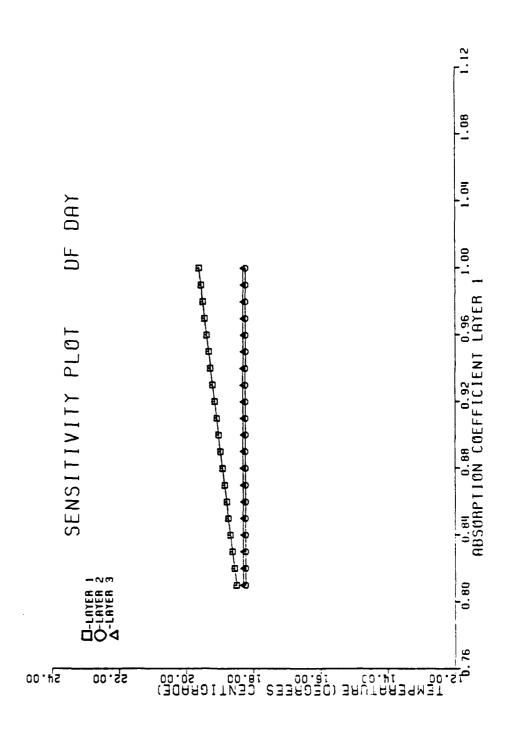


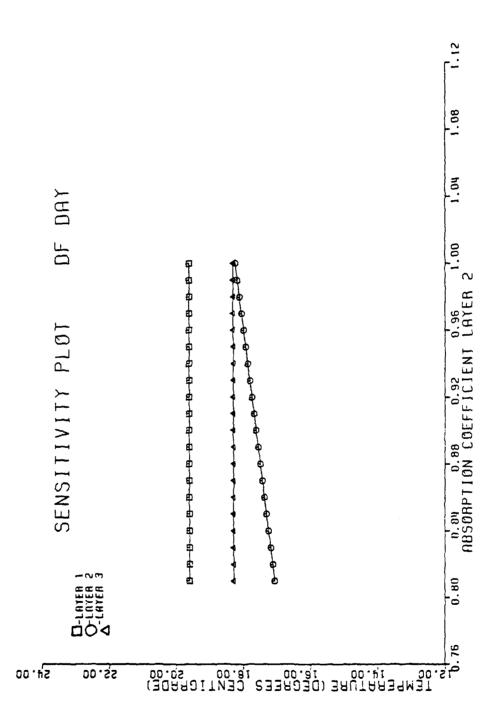


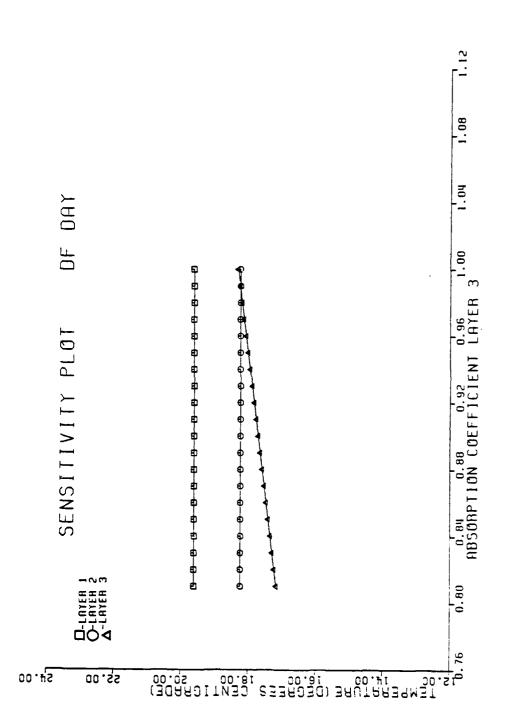




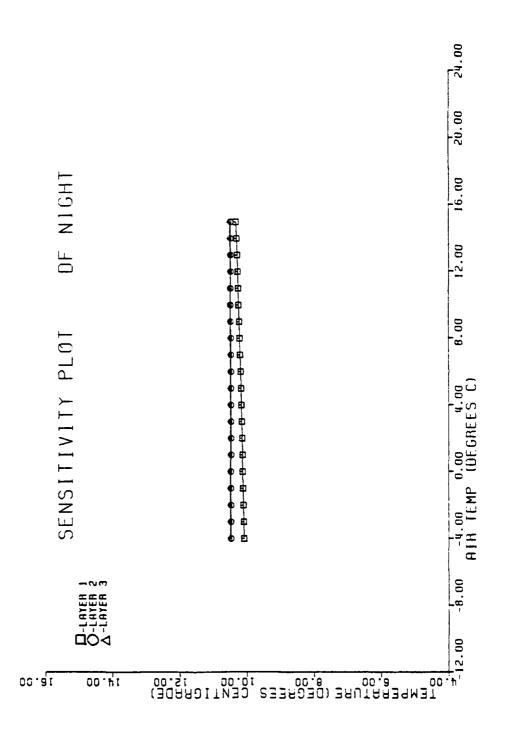


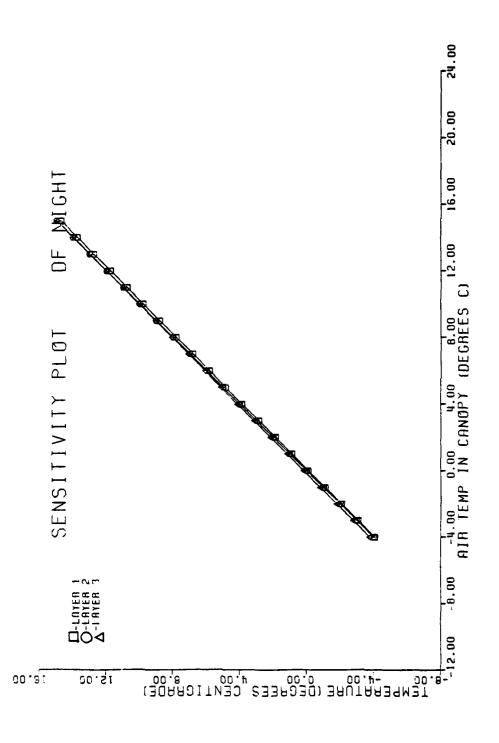


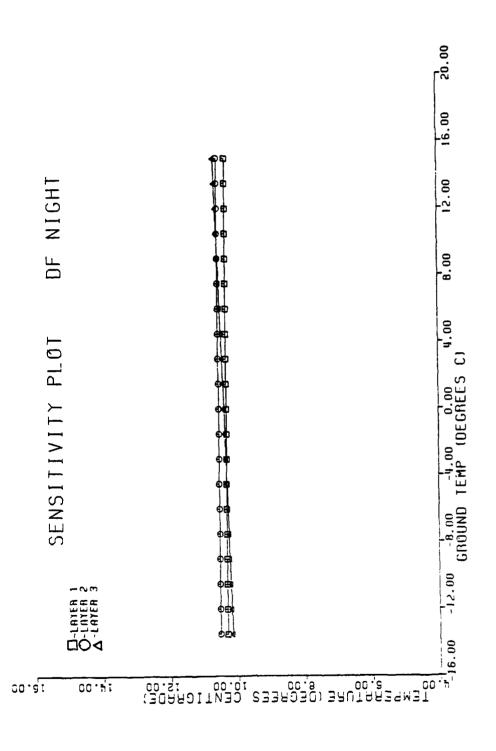




Douglas-Fir Nighttime Sensitivity Plots

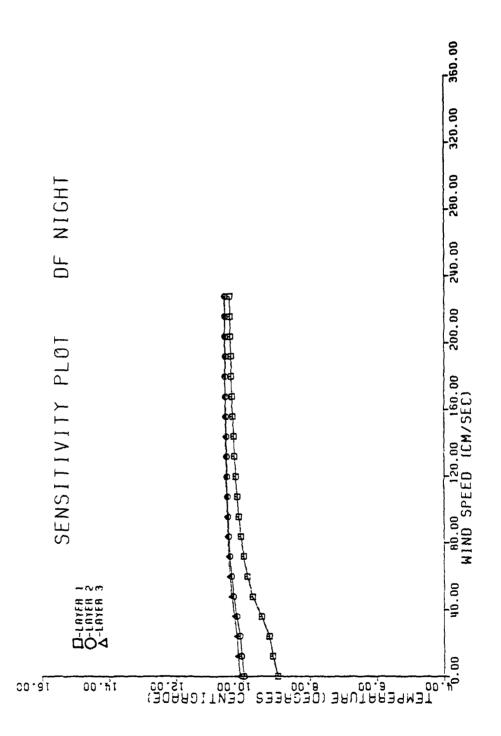


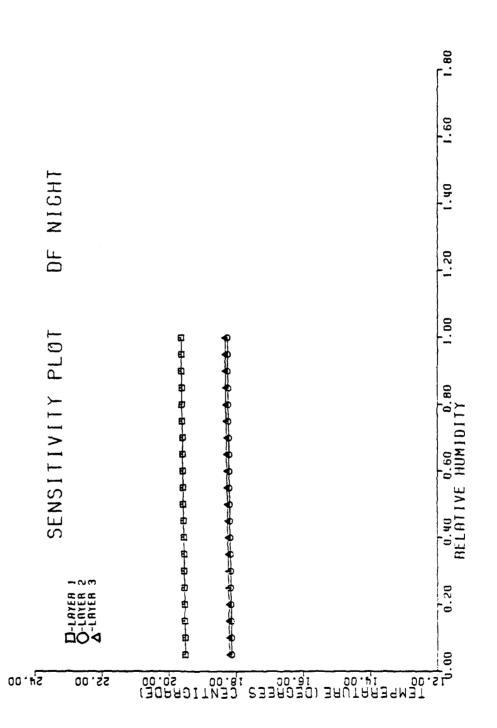


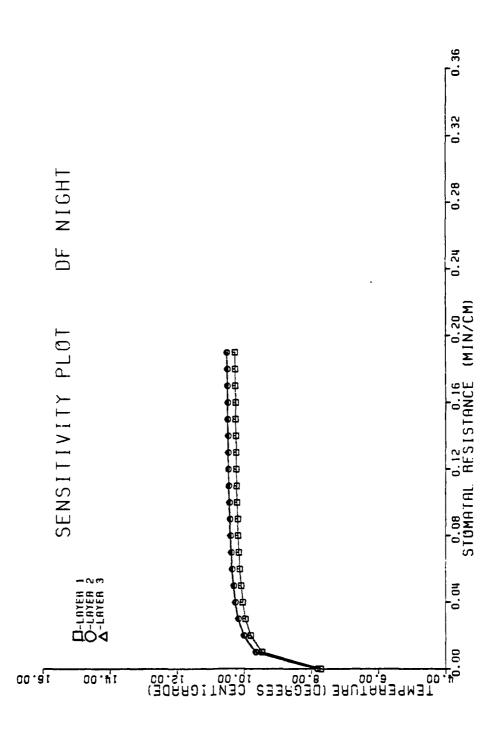


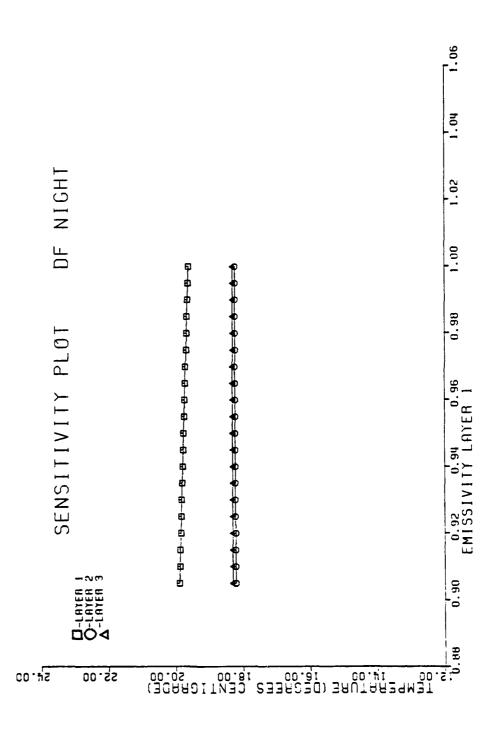
C22

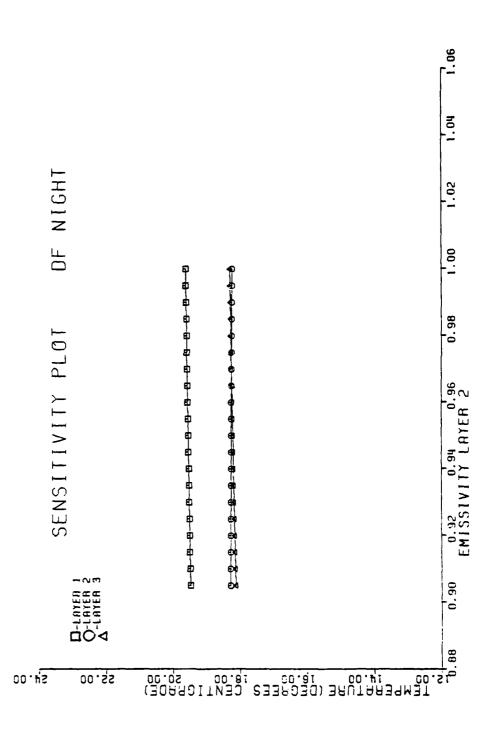
The second second

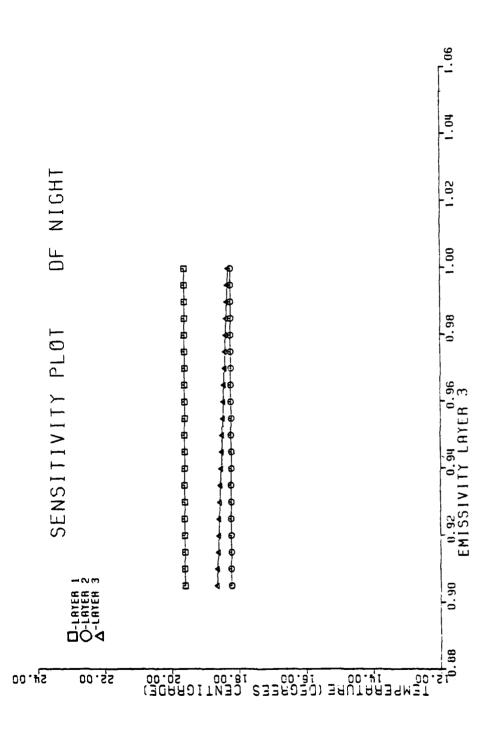


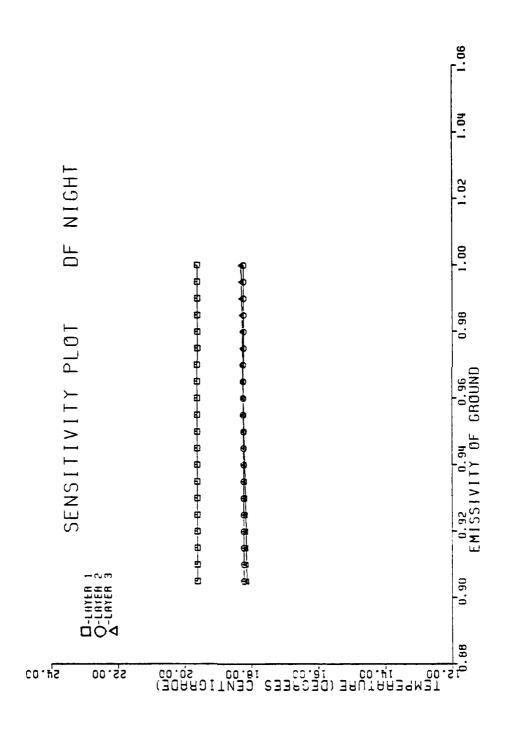


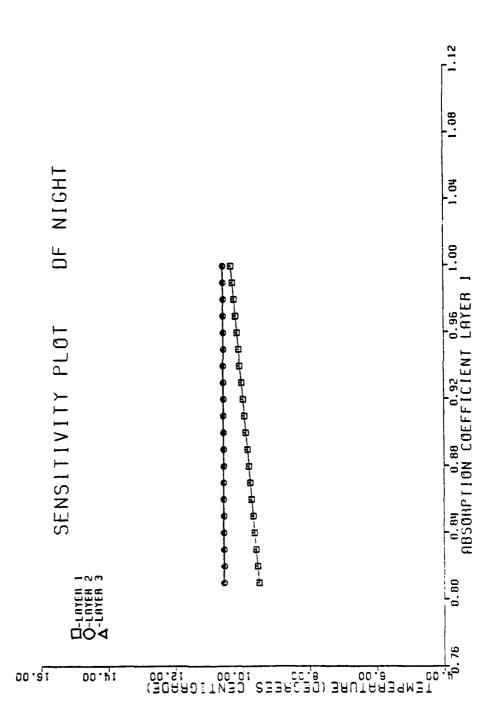


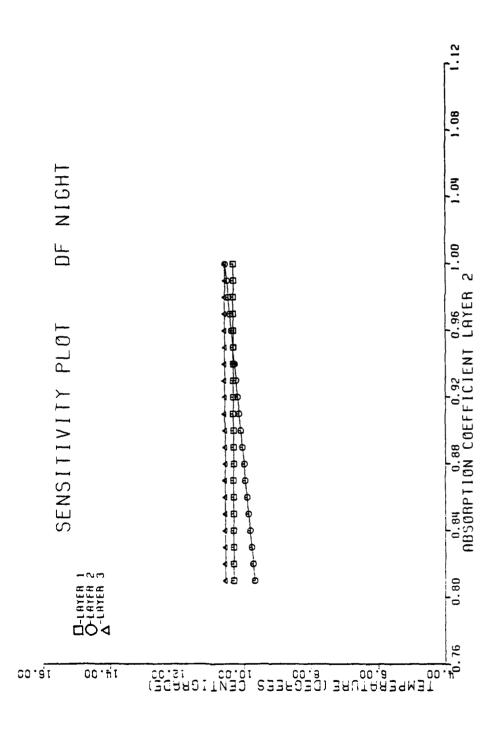




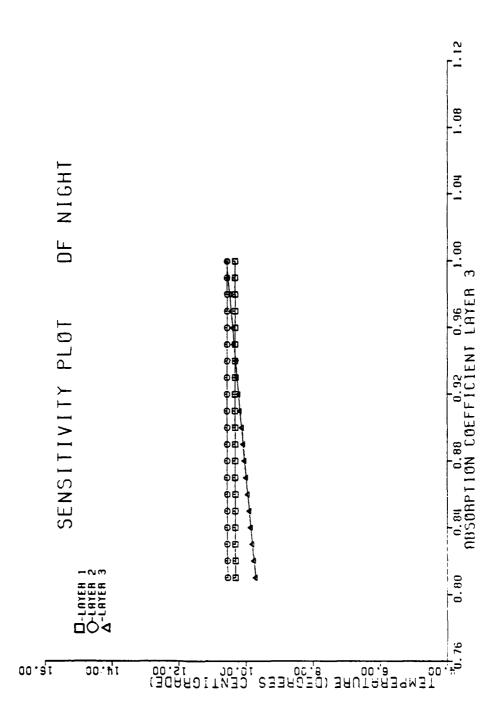




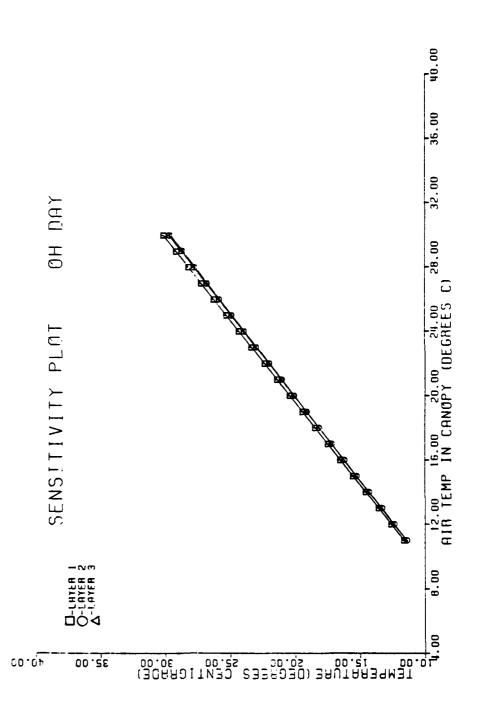


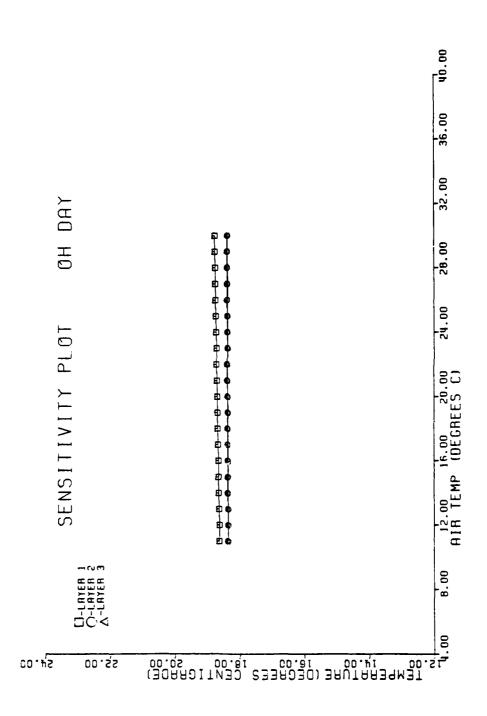


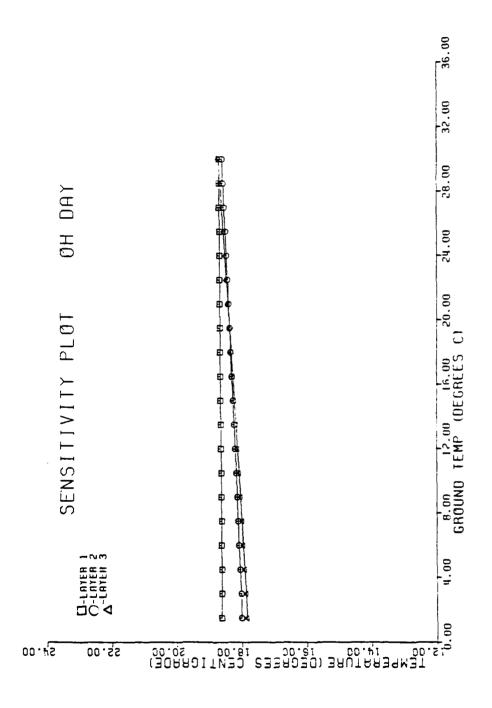
The state of the s

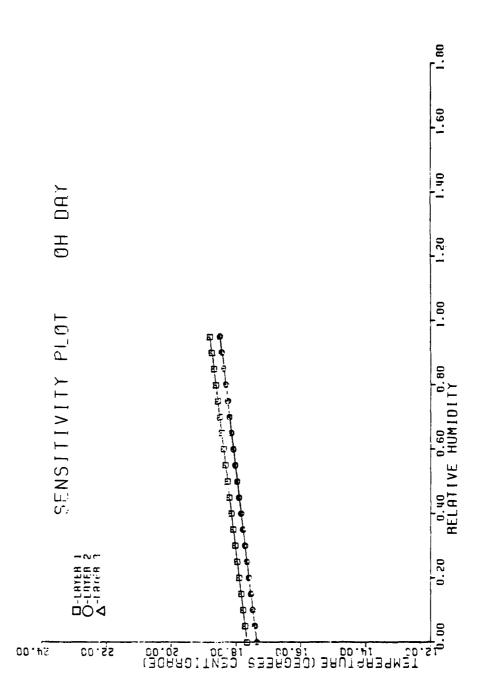


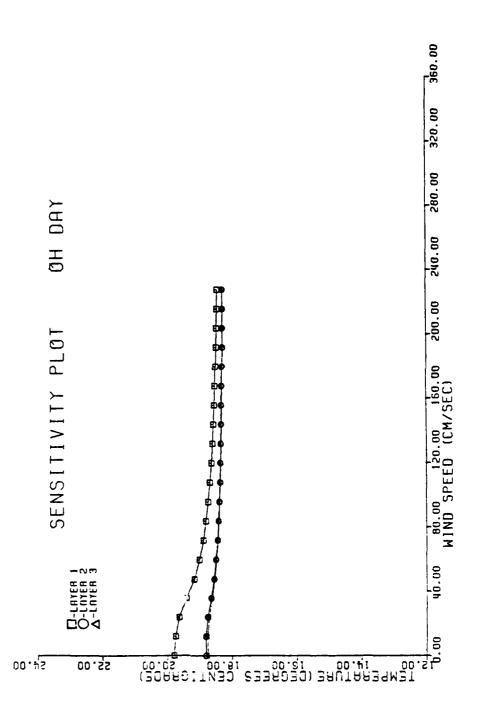
Oak-Hickory Daytime Sensitivity Plots

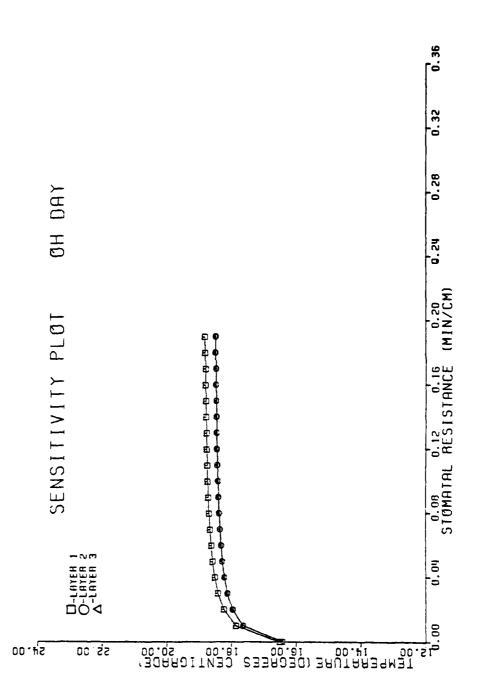




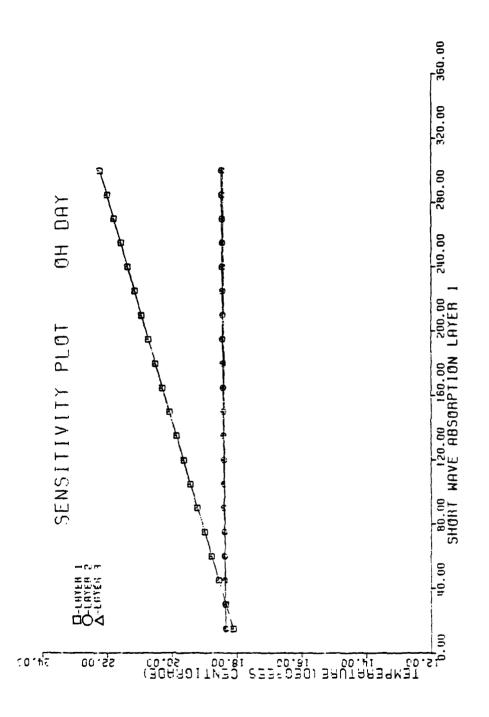


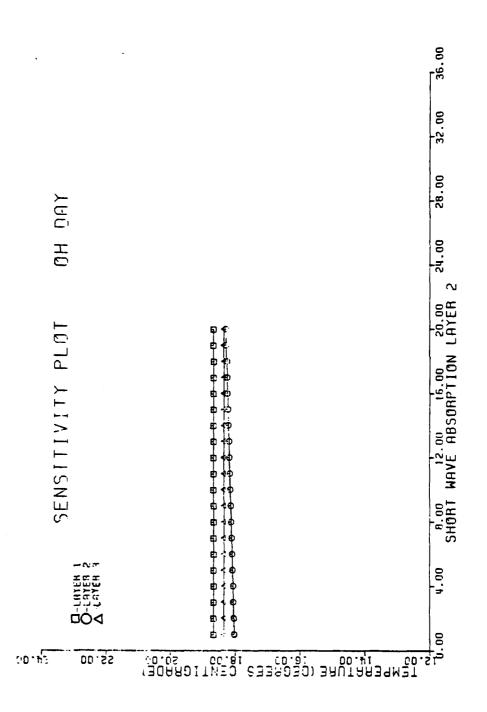


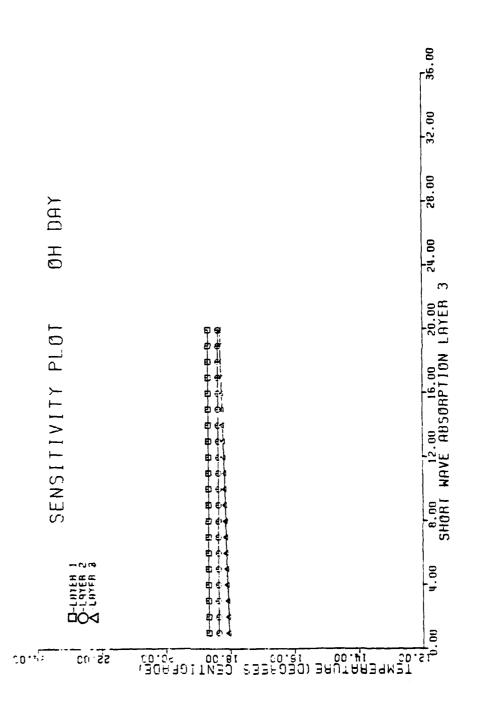


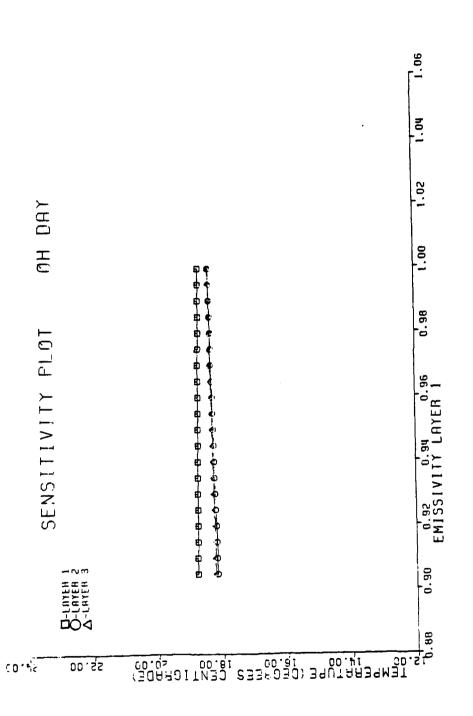


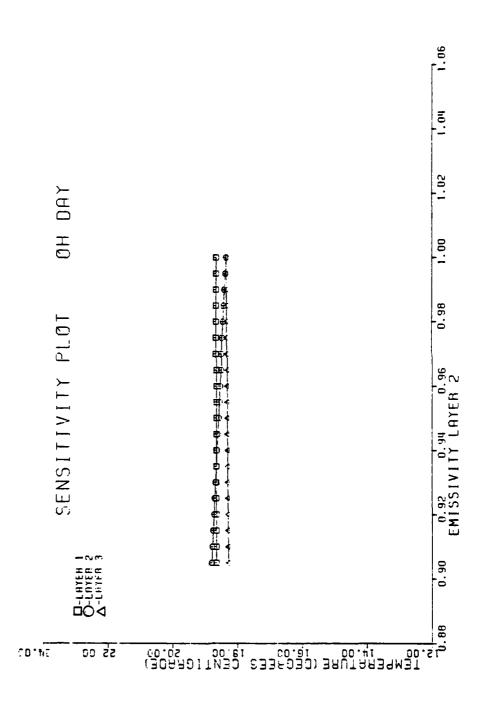
Con the

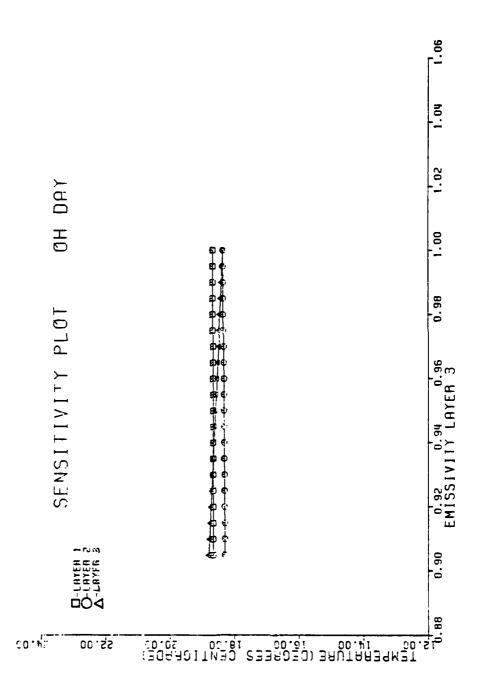


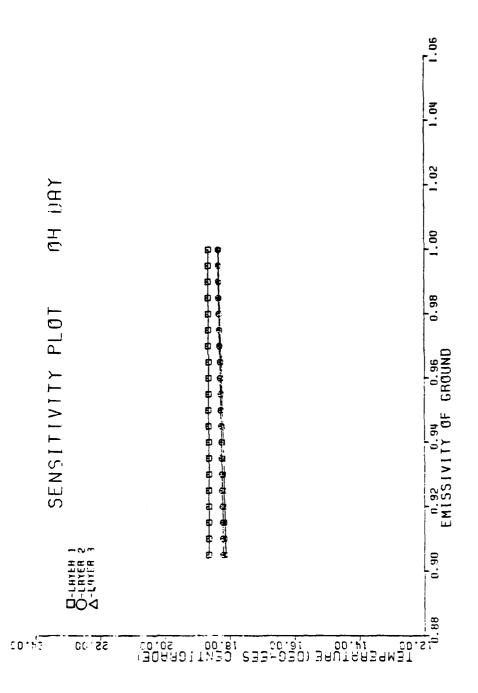


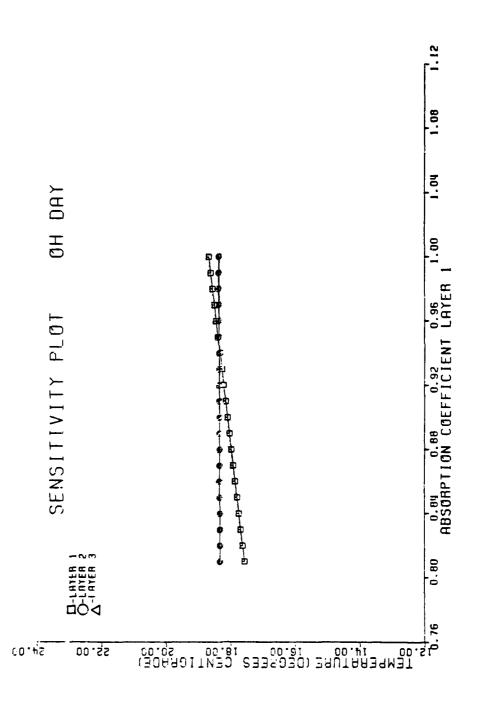




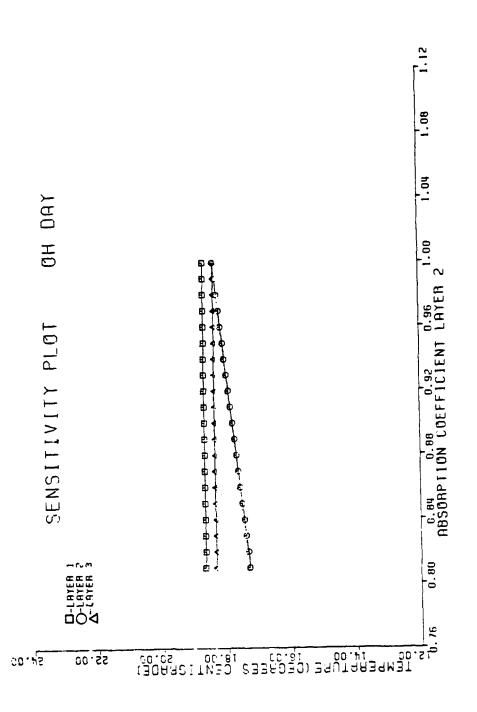


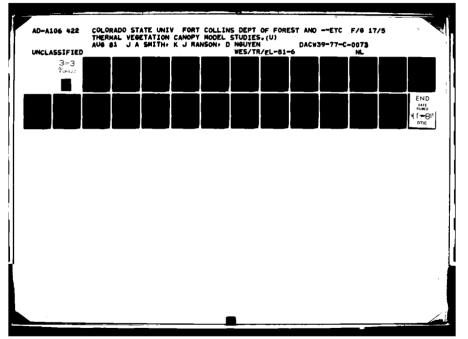


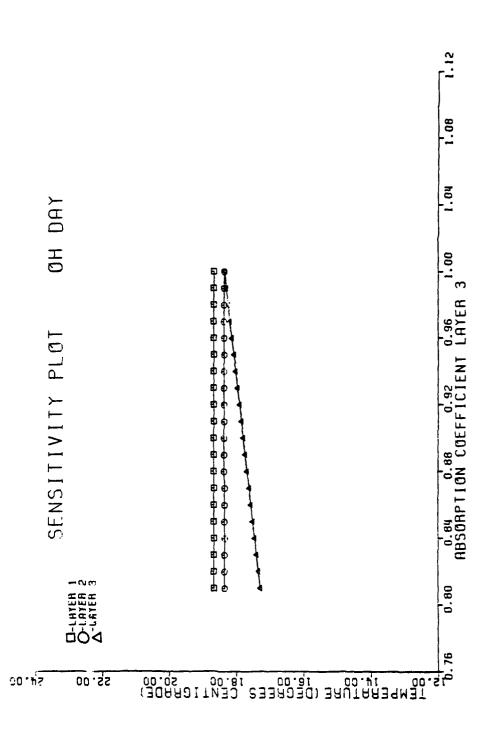




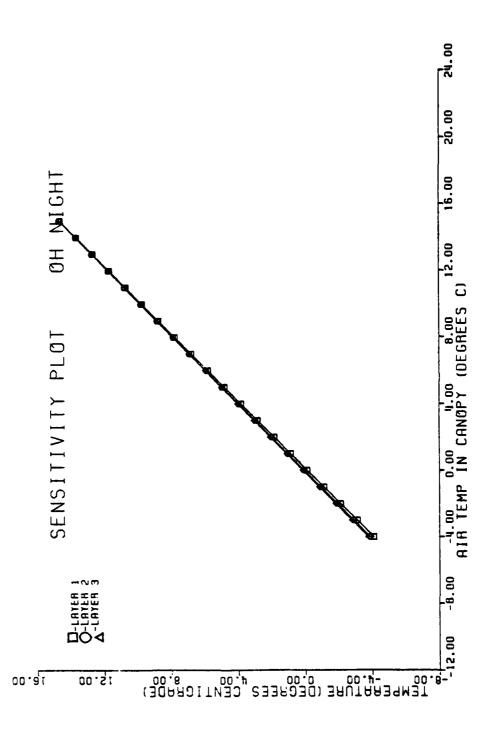
State of the state

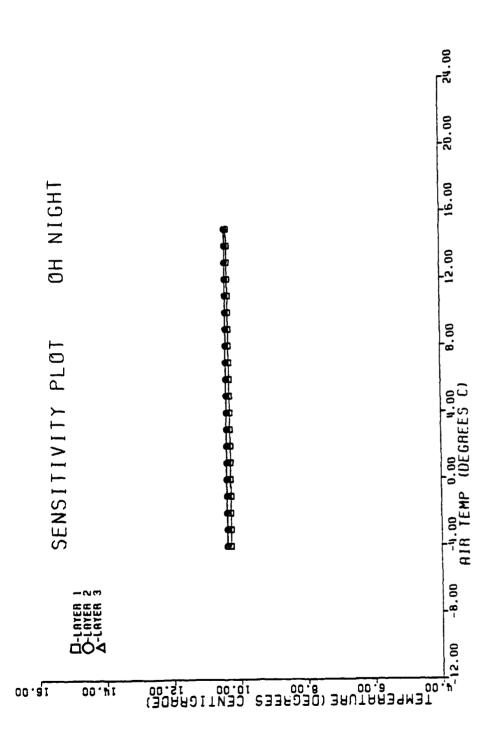


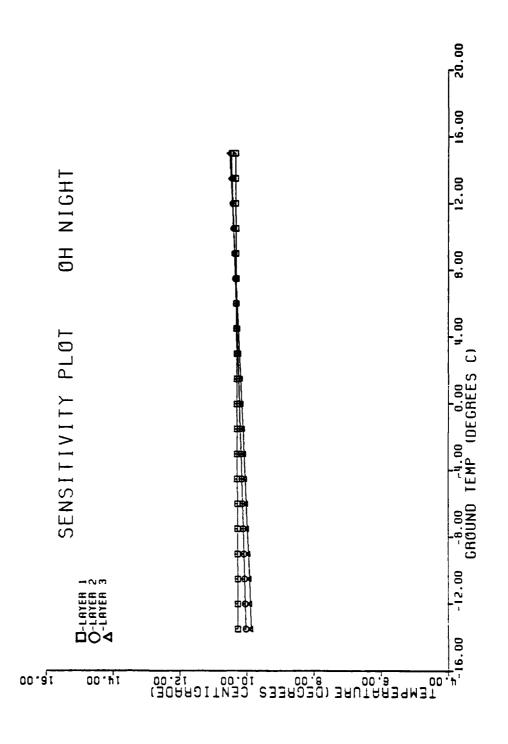


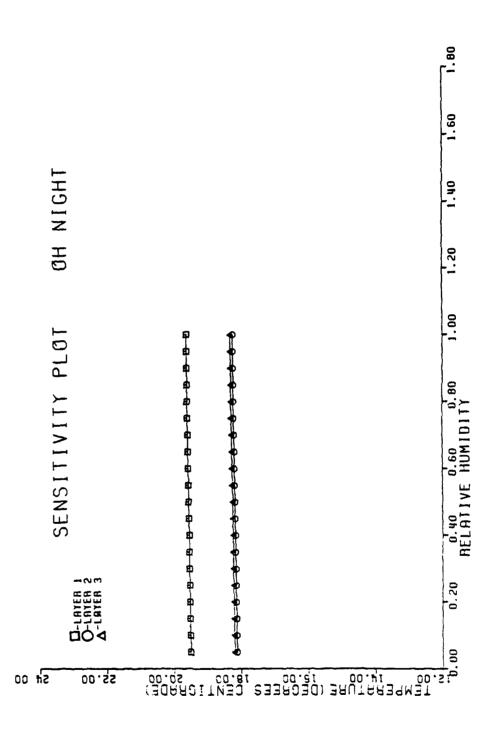


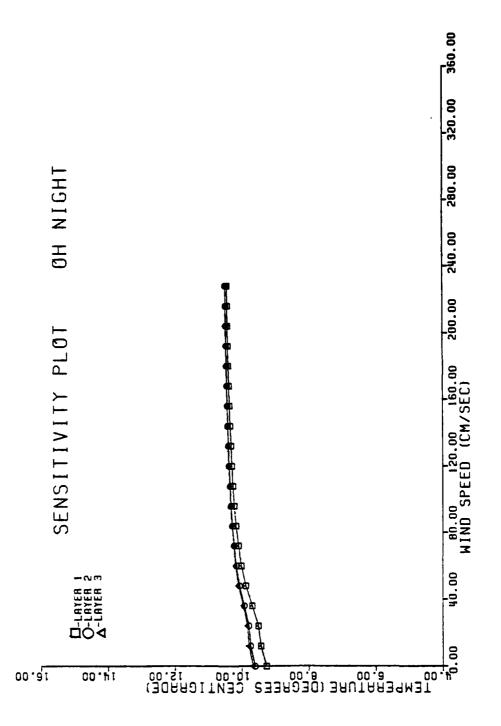
Oak-Hickory Nighttime Sensitivity Plots

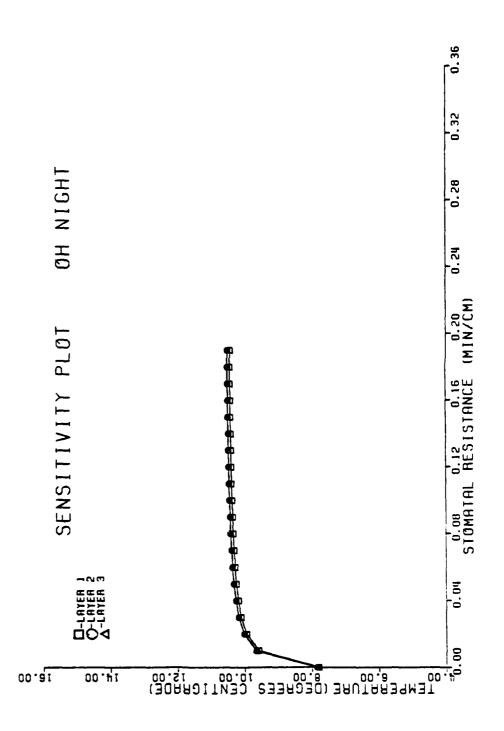


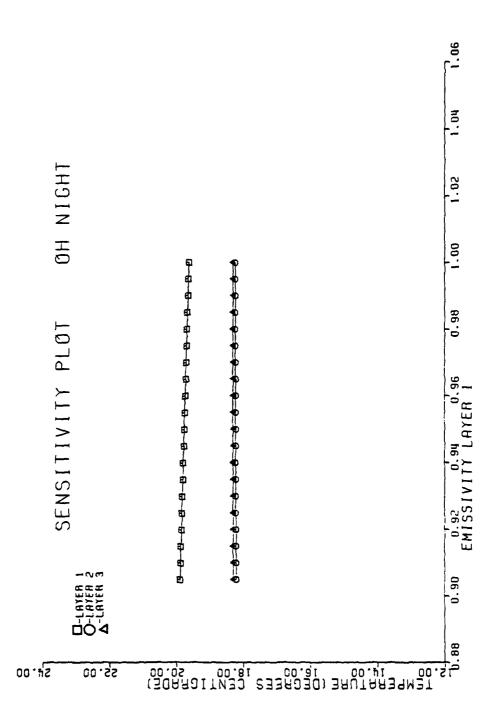


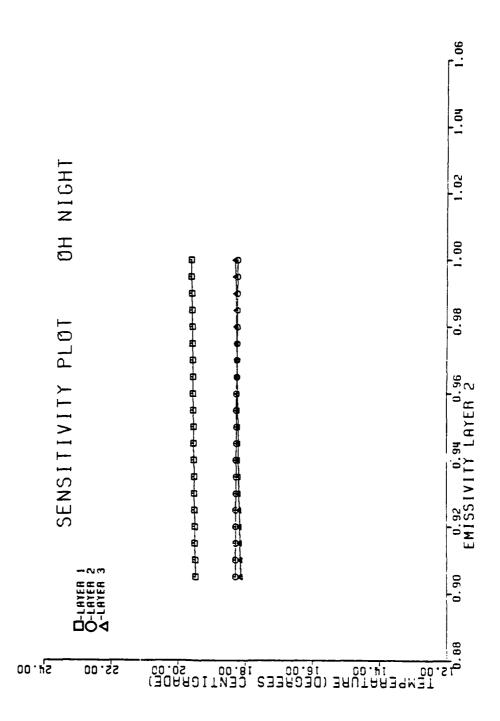


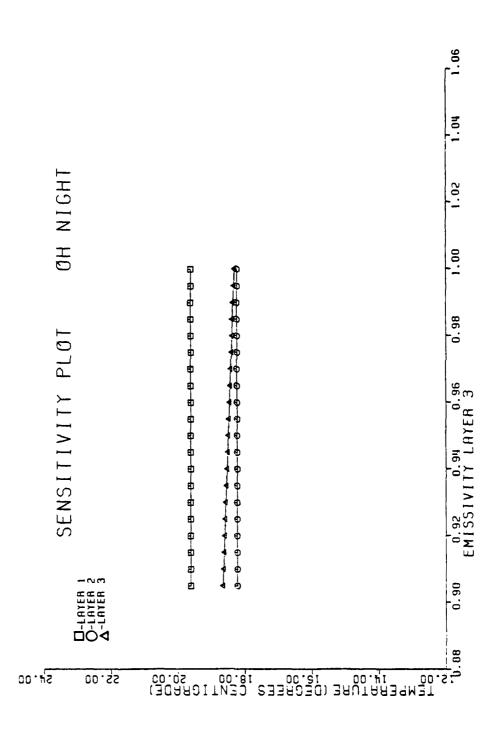


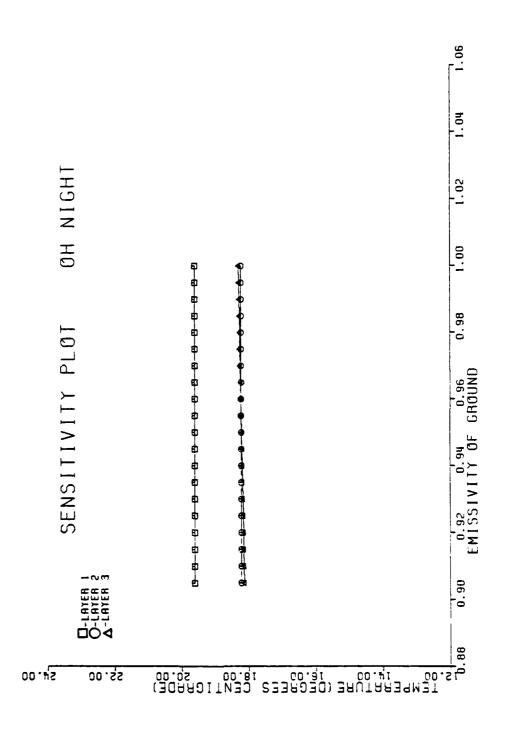


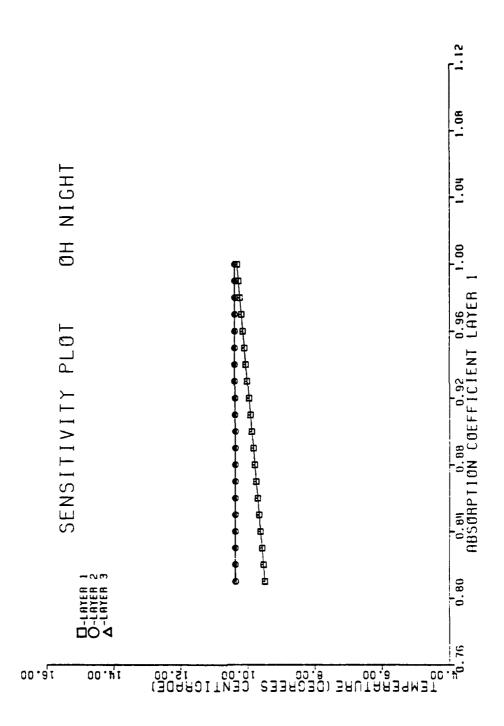


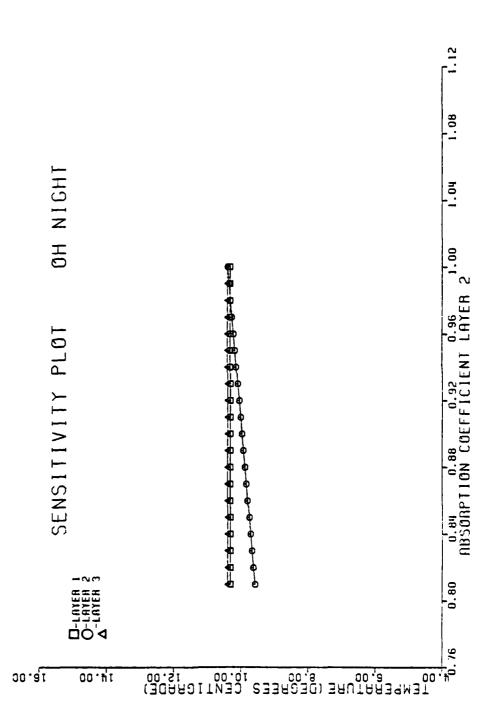


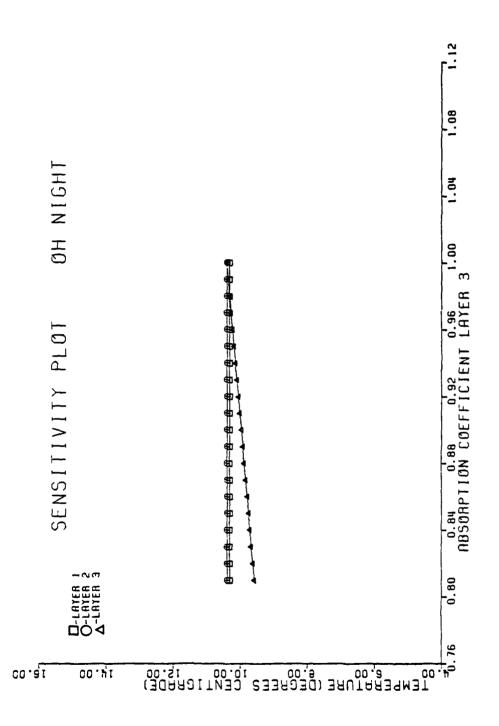












APPENDIX D: SUPPORTING VALIDATION DATA

Cedar River, Douglas-Fir

CANOPY GEOMETRY INPUT DATA FOR DOUGLAS-FIR

LEAF AREA INDEX

1.50 5.30 1.00

CANOPY DENSITY PARAMETERS

.10 .10 .10

FOLIAGE ANGLE DISTRIBUTION

	PROBABI	OCCURRENCE	
INCLINATION ANGLE	LAYER 1	LAYER	2 LAYER 3
0.0	.088	.093	.089
5.0	.078	.079	.078
10.0	.079	.080	.079
15.0	.077	.078	.078
20.0	.084	.084	.084
25.0	.077	.077	-077
30.0	.081	.080	.080
35.0	-059	.059	.059
40.0	.088	.087	.088
45.0	.063	.062	.068
50.0	.062	.061	.062
55.0	.045	.043	.044
60.0	.044	.042	.043
65.0	.029	.029	.029
70.0	.024	.024	.024
75.0	.013	.013	.013
80.0	.007	.007	-007
85.0	.003	.003	.003
90.0	0.000	0.000	0.000

THERNAL HODEL INPUT DATA FOR DOUGLAS-FIR

GEONETRICAL VIEW ANGLE FACTOR MATRIX

	ZENITH ANGLE								
	5.0	15.0	25.0	35.0	45.0	55.0	65.0	75.0	85.0
LAYER 1	.9974	.8703	.7697	.7214	.6994	.6900	.6865	.6856	. 6855
LAYER 2							.3079		
LAYER 3	.0000	-0001	.0009	.0018	.0025	.0028	.0029	.0029	.0029
GROUND	.0000	.0000	.0006	.0015	.0022	.0025	.0027	.0027	.0027

LONG WAVE TRANSFER MATRIX

			FROM		
TO	SKY	LAYER 1	LAYER 2	LAYER 3	GROUND
LAYER 1	.4599	1.0731	.4540	.0031	.0027
LAYER 2	.0267	.0661	1.8071	.0507	.0421
LAYER 3	.0022	.0052	.5887	.8008	.5960

AVERAGE SHORTWAVE ABSORPTION COEFFICIENTS

LAYER 1 LAYER 2 LAYER 3

.3890 .0190 .0280

STONATAL RESISTANCE

.66 (MIN/CM)

CEDAR RIVER, WASHINGTON 4 AUGUST 1979

TIME	AIR TEMP	GRND TEMP	UIND SPEED	REL HUN	GLOBAL SUR
(HOURS)	(DEG C)	(DEG C)	(M/SEC)		(U/H++2)
100	9.8	12.4	1.0	.99	0.00
200	9.3	12.0	1.0	1.00	0.00
300	8.7	11.5	.9	1.00	0.00
400	8.2	11.1	1.0	1.00	0.00
500	7.5	10.6	.9	1.00	0.00
600	7.0	10.2	. 9	1.00	1.80
700	7.2	9.7	.7	1.00	69.20
800	9.2	9.7	.6	.99	227.80
900	11.8	10.3	.5	.94	445.70
1000	13.8	11.3	1.5	.89	621.60
1100	15.7	13.0	1.8	.87	772.60
1200	16.8	14.3	1.9	.85	814.50
1300	18.3	15.5	1.9	.84	847.70
1400	19.5	16.2	2.1	.83	484.80
1500	20.5	17.0	2.2	.81	835.70
1600	21.2	17.9	2.7	.81	770.20
1700	21.3	18.2	3.0	.81	618.40
1800	21.8	18.8	3.1	.80	493.90
1900	21.2	17.7	2.5	.78	289.90
2000	29.5	17.4	2.0	.78	115.40
2100	17.4	16.7	.8	.81	7.50
2200	14.6	15.7	1.1	.87	0.00
2300	14.6	14.8	1.5	.88	0.00
2400	14.4	14.5	1.5	.88	0.00

CEDAR RIVER, WASHINGTON 5 AUGUST 1979

TIME	AIR TEMP	GRND TEMP	WIND SPEED	REL HUM	GLOBAL SUR
(HOURS)	(DEG C)	(DEG C)	(H/SEC)		(9/###2)
100	13.6	14.4	1.1	.92	0.00
200	13.0	14.2	. 4	.93	0.00
300	12.7	14.2	.5	.94	0.00
400	12.6	14.1	1.1	.93	0.00
50 0	12.0	14.0	1.2	.93	0.00
600	11.3	13.7	.9	.94	1.60
700	11.0	13.4	. 6	.95	30.40
800	11.2	13.3	.6	.94	64.50
900	11.6	13.4	1.2	.93	111.90
1000	12.2	13.5	1.2	.91	154.60
1100	13.0	13.7	1.2	.90	228.20
1200	14.6	14.3	1.3	.88	459.40
1300	16.7	15.2	1.6	.85	719.30
1400	17.0	15.8	2.0	.84	370.00
1500	17.3	16.0	1.3	.84	366.60
1600	18.6	16.4	1.3	.84	659.40
1700	18.6	16.8	1.4	.83	399.20
1800	19.4	16.8	1.8	.82	388.00
1900	19.4	16.9	2.3	.82	301.30
2000	18.6	16.6	1.2	.83	110.90
2100	15.7	16.0	.7	.87	9.20
2200	13.6	15.0	1.0	.93	0.00
2300	12.5	14.2	.9	.95	0.00
2400	12.4	13.7	1.0	.96	0.00

Walker Branch, Oak-Hickory

CANOPY GEOMETRY INPUT DATA FOR OAK HICKORY

LEAF AREA INDEX

1.40 .80 .40

CANOPY DENSITY PARAMETERS

.10 .10 .10

FOLIAGE ANGLE DISTRIBUTION

	PROBABI	LITY OF	OCCURRENCE
INCLINATION ANGLE	LAYER 1	LAYER	
0.0	.066	.117	.014
5.0	.067	.155	.233
10.0	.084	.129	.120
15.0	.086	.177	.157
20.0	.050	.064	.053
25.0	.098	.135	.154
30.0	.084	.081	.100
35.0	.076	.037	.047
40.0	.063	.040	0.000
	.087	.019	.010
45.0	.040	.015	
50.0	.043	.019	
55.0	.031	.007	
60.0	.033	.002	
65.0		.002	
70.0	.024	0.000	
75.0	0.000		1111
80.0	0.000	0.000	
85.0	0.000	0.000	
90.0	0.000	0.000	0.000

THERNAL MODEL INPUT DATA FOR OAK HICKORY

GEOMETRICAL VIEW ANGLE FACTOR HATRIX

	ZENITH ANGLE								
	5.0	15.0	25.0	35.0	45.0	55.0	65.0	75.0	85.0
LAYER 1	1.0000	.9947	.9774	.9642	.9573	.9545	.9536	.9536	.9536
LAYER 2	0.0000	.0018	.0068	.0105	.0124	.0131	.0134	.0134	.0134
LAYER 3	0.0000	.0011	.0047	.0075	.0090	.0096	.0098	.0098	.0098
GROUND	0.0000	.0023	.0110	.0178	.0213	.0227	.0232	.0232	.0232

LONG WAVE TRANSFER HATRIX

TO	SKY	LAYER 1	FROM Layer 2	LAYER 3	GROUND
LAYER 1	.1595	1.6741	.0470	.0338	.0788
LAYER 2	.0281	.7914	.3539	.2589	.5607
LAYER 3	.0201	.5442	.2574	.3496	.8217

AVERAGE SHORTWAVE ABSORPTION COEFFICIENTS

LAYER 1 LAYER 2 LAYER 3

.089 .042 .040

STOHATAL RESISTANCE

.07 (HIN/CH)

WALKER BRANCH, TENNESSEE 18 AUGUST 1979

TIME	AIR TEMP G	RND TEHP I	IND SPEED	REL HUM	GLOBAL SUR
(HOURS)	(DEG C)	(DEG C)	(M/SEC)		(W/H**2)
100	19.5	19.5	3.1	.83	0.00
200	19.3	19.5	3.2	.85	0.00
300	18.8	19.4	2.8	.87	0.00
400	18.3	19.3	2.3	.91	0.00
500	18.0	19.2	2.7	.94	0.00
900	17.7	19.1	2.4	.96	0.00
700	17.9	19.1	3.0	.96	38.20
800	19.3	19.2	3.0	.93	175.40
900	21.0	19.3	2.4	.88	329.90
1000	22.4	19.5	4.3	.84	445.70
1100	24.4	19.9	3.5	.77	661.90
1200	26.0	20.4	3.6	.71	681.10
1300	27.1	20.7	2.8	.65	614.00
1400	28.2	21.0	2.9	.64	770.10
1500	29.2	21.4	2.8	.61	787.00
1600	28.5	21.6	2.8	.61	531.70
1700	28.5	21.6	2.7	.62	474.00
1800	27.7	21.7	2.4	. 65	269.10
1900	26.2	21.6	2.3	.70	85.00
2000	24.9	21.4	2.2	.75	2.90
2100	24.3	21.3	2.9	.76	0.00
2200	23.5	21.2	3.0	.78	0.00
2300	22.8	21.0	3.2	.80	0.00
2400	22.1	20.7	3.4	.83	0.00

WALKER BRANCH, TENNESSEE 19 AUGUST 1979

TIME	AIR TEMP	GRND TEMP	WIND SPEED	REL HUK	
(HOURS)	(DEG C)	(DEG C)	(H/SEC)		(U/H**2)
		00.7		05	0.00
100	22.1	20.7	3.4	.85	
200	21.5	20.6	3.5	.91	0.00
300	21.1	20.6	3.2	.92	0.00
400	20.4	20.5	2.4	.99	0.00
500	19.8	20.3	2.6	1.00	0.00
600	19.6	20.3	1.8	1.00	0.00
700	19.1	20.2	1.5	1.00	22.80
800	20.8	20.3	1.7	1.00	182.80
900	23.8	20.4	1.5	.91	345.00
1000	26.1	20.6	2.4	.80	582.10
1100	27.8	21.0	2.5	.73	751.60
1200	29.2	21.5	2.8	.69	753.60
1300	30.4	21.8	2.2	.63	827.50
1400	31.7	22.2	2.1	.61	917.40
1500	31.3	22.6	2.1	.60	778.00
1600	31.1	22.8	2.1	.61	620.40
1700	30.2	22.8	2.5	.63	457.60
1800	29.5	22.8	1.7	. 67	251.70
1900	27.9	22.7	1.9	.74	81.40
		22.4	2.6	.71	2.60
2000	26.2				
2100	25.9	22.2	2.1	-69	0.00
2200	25.1	22.0	2.3	.74	0.00
2300	24.3	22.9	2.0	.81	0.00
2400	22.1	21.7	2.0	.81	0.00

In accordance with letter from DAEN-RDC, DAEN-ASI dated 22 July 1977, Subject: Facsimile Catalog Cards for Laboratory Technical Publications, a facsimile catalog card in Library of Congress MARC format is reproduced below.

Thermal vegetation canopy model studies: final report / by J.A. Smith ... [et al]. (Department of Wood Science, College of Forestry and Natural Resources, Colorado State University). -- Vicksburg, Miss.: U.S. Army Engineer Waterways Experiment Station; Springfield, Va.: available from NTIS, [1981].
213 p. in various pagings: ill.; 27 cm. -- (Technical report / U.S. Army Engineer Waterways Experiment Station; EL-81-6)
Cover title.
"August 1981."
"Prepared for Headquarters, Department of the Army, under Project No. 4A762730AT42, Task A4, Work Unit 003 (Contract No. DACW 39-77-C-0073)."
"Monitored by Environmental Laboratory, U.S. Army Engineer Waterways Experiment Station."
Bibliography: p. 44-45.

Thermal vegetation canopy model studies: ... 1981. (Card 2)

1. Computer simulation. 2. Infra-red detectors.
3. Remote sensing. 4. Thermal analysis. 5. Vegetation classification. I. Smith, J.A. II. Colorado State University. College of Forestry and Natural Resources. III. United States. Department of the Army. IV. U.S. Army Engineer Waterways Experiment Station. Environmental Laboratory. IV. Series: Technical report (U.S. Army Engineer Waterways Experiment Station); EL-81-6. TA7.W34 no.EL-81-6

/

1. 1.

