

AD-A106 193

CENTER FOR NAVAL ANALYSES ALEXANDRIA VA INST OF NAVAL--ETC F/G 5/10  
A NOTE ON ESTIMATING CONTINUOUS TIME DECISION MODELS.(U)  
SEP 81 R P TROST, P LURIE, E BERGER

UNCLASSIFIED CNA-PP-320

NL

1 OF 1  
ADA  
36193

END  
DATE  
FILMED  
11-81  
DTIC

②

LEVEL II

PROFESSIONAL PAPER 320 / September 1981

AD A106193

# A NOTE ON ESTIMATING CONTINUOUS TIME DECISION MODELS

R. P. Trost  
Philip Lurie  
Edward Berger

DTIC  
ELECTE  
OCT 27 1981  
S B D

DTIC FILE COPY

DISTRIBUTION STATEMENT A  
Approved for public release;  
Distribution Unlimited



CENTER FOR NAVAL ANALYSES

81 10 22

PROFESSIONAL PAPER 320 / September 1981

**A NOTE ON ESTIMATING  
CONTINUOUS TIME  
DECISION MODELS.**

R. P. Trost  
Philip Lurie  
Edward Berger

10/21/81  
S. J. ...  
C. J. ...



*Institute of Naval Studies*

**CENTER FOR NAVAL ANALYSES**

2000 North Beauregard Street, Alexandria, Virginia 22311

41 2516

100

TABLE OF CONTENTS

	<u>Page</u>
Introduction.....	1
A source of bias: censored observations.....	2
A method for estimating continuous time models when the data are censored.....	4
Two empirical examples with censored observations.....	5
Duration of unemployment.....	6
Childspacing equation.....	9
Conclusions.....	14
References.....	15

<b>Accession For</b>	
NTIS GRA&I	<input checked="" type="checkbox"/>
DTIC TAB	<input type="checkbox"/>
Unannounced	<input type="checkbox"/>
Justification	
<b>PER LETTER</b>	
By _____	
Distribution/ _____	
Availability Codes	
Dist	Avail and/or Special
<b>A</b>	

A NOTE ON ESTIMATING CONTINUOUS  
TIME DECISION MODELS

by

R. P. Tost, Philip Lurie and Edward Berger\*

1. INTRODUCTION

Continuous time decision models have a long history in economics. In fact, the early work of Mincer [1962] implies that a woman's labor force participation decision is made with a continuous time horizon in mind. More recently, Mincer and Polacheck [1974 and 1978], Mincer and Ofek [1980], and Sandell and Shapiro [1978] analyze the length of time women remain out of the labor force. Sandell [1977] examines the determinants of the number of years women work after the birth of their first child, and in a stock adjustment model of fertility decisions, Hyman [1980] examines the length of time between births. There are also several studies that seem suited to continuous time analysis but are estimated with discrete time choice models. For example, Shapiro and Mott [1979] estimate a discrete time choice model of women's post child labor force participation rates. One could also analyze post child labor force participation, as Mincer and Polacheck [1974] do, by looking at a woman's interval of nonlabor force participation following the birth of a child.

All of the above studies choose (or imply) as the dependent variable of interest some measure of continuous time, whether it be in percentage terms or actual years. In some of these papers (e.g., Mincer and Polacheck [1974] and Hyman [1980]) this dependent variable is studied by looking at its mean

---

\* We would like to thank Robert Dorfman, Jacob Mincer and Solomon Polacheck for comments on earlier versions of this paper. Any remaining errors are our own responsibility.

value (actual or predicted) in various age and education subgroups. In other studies (e.g., Mincer and Ofek [1980] and Shapiro and Mott [1979]) the determinants of the dependent variable are estimated with regression analysis. While the estimation of continuous time models is a step in the right direction (away from discrete time choice models), the purpose of our note is to point out that the empirical results in these otherwise excellent theoretical papers may be biased. The source of this bias lies in the way censored observations are handled in the empirical analysis. The rest of the paper is divided into the following sections. In Section Two we discuss a potential source of bias in previous studies. In Section Three we propose an alternative method for estimating time decision models and in Section Four, we consider two different applications of this method. Section Five contains the conclusions.

## II. A SOURCE OF BIAS: CENSORED OBSERVATIONS

All the studies cited in the introduction derive and estimate life cycle decision models. One variable of interest in these papers is some sort of "length of time" variable. For example, Mincer and Polacheck [1974] study, among other things, the length of time women remain out of the labor force following the birth of the first child. Mincer and Ofek [1980] estimate the determinants of a woman's duration of unemployment. Hyman [1980] estimates a stock adjustment fertility model where one variable of interest is the length of time between children<sup>1</sup> (i.e., childspacing). The authors'

---

<sup>1</sup>Although Hyman's theoretical interest include the decision regarding the desired spacing between children, his actual empirical analysis only looks at the proportion of respondents who had one child during the following year, given that they desired to have one more child. However, child spacing in the usual meaning of the word is implied in his paper and is worth investigating.

justification for studying these dependent variables is well founded in economic theory, and we have no quarrel with their theoretical models. Our concern is with the empirical section and in particular with the manner in which censored observations are handled in the analysis. A simple example will demonstrate our point.

Suppose we want to estimate the average length of time women wait before returning to work following the birth of their first child. For simplicity, assume we have a sample of ten women who all gave birth on the same day. Let the observations  $y_i$  be:

1, 1, 2, 2, 3, 3, 4, 4, 5, 5

where  $y_i$  is the number of years elapsed before the women return to work.

If we analyze these data five years after the children are born, we can simply average the ten observations  $y_i$  to get an unbiased estimate of the mean.

Suppose, as is often the case with panel data, we do not have "completed" values of  $y_i$  for all the observations. This would be the case, for example, if we have data for only the first three years following the birth of these children. In this case we will have six observations where the length of time is observed (1,1,2,2,3,3) and four where the length of time is censored (the values 4, 4, 5, 5 which of course are unobserved) at 3 years. Here the term censored means that all we know is these four women wait at least three years before returning to work. If we simply average the six uncensored observations, we will underestimate the mean of  $y_i$ . Even if we include the censored observations and enter a value of "3" for them, we will still underestimate the mean value of  $y_i$ . These same problems exist if we wish to use regression analysis to measure the impact of an exogenous variable  $X_i$

on  $y_1$ , i.e., we will underestimate  $E(Y_1|X_1)$ . Despite these obvious biases, it is surprising that none of the previously cited papers discuss (or take account of) this "censored data" problem. As we show in the next section, there is a simple method for handling this problem, that to our knowledge has never been applied to economic data.

### III. A METHOD FOR ESTIMATING CONTINUOUS TIME MODELS WHEN THE DATA ARE CENSORED

The estimation of continuous time models have a long history in the biostatistical literature. They have been used extensively in the biomedical sciences in the general area of patient survival. Here the problem has been to estimate the probability that a patient survives beyond time  $T$ . A plot of these probabilities as a function of time, i.e.,

$$S(t) = P(T > t), \quad (1)$$

is called a "survival curve."

Kaplan and Meir [1958] were the first to derive a nonparametric maximum likelihood estimate of the true survival function in the presence of censoring. However, the Kaplan-Meir method only estimates "unadjusted" survival curves. That is, the survival curves are not adjusted for exogenous characteristics. It was not until 1972 that a nonparametric method became available for handling censored observations while adjusting for factors (i.e., exogenous variables) which may affect the probability of survival. This method was first proposed by Cox [1972] and is known as the Cox Regression model. The Cox model expresses a hazard function<sup>2</sup> as

---

<sup>2</sup>The hazard function  $h(t)$ , is defined as the conditional probability of a failure in the interval  $(t, t+dt)$ , given survival to time  $t$ . That is,

$$h(t)dt = P(t < T < t+dt | T > t).$$



$$h_z(t) = h_0(t)e^{\beta'Z},$$

where  $Z$  is a vector of exogenous variables,  $\beta$  is a vector of unknown coefficients and  $h_0(t)$  is assumed fixed and independent of  $Z$ , but otherwise completely unspecified. Note that  $h_0(t)$  corresponds to the hazard function for the situation when  $Z = 0$ . The survival function  $S_0(t)$  refers to the case where the exogenous variables  $Z = 0$  and is expressed as

$$S_0(t) = e^{-\int_0^t h_0(x) dx}.$$

Since the model assumes proportional hazards i.e., the hazard ratio for any two values of  $Z$  is independent of time, then

$$S_1(t) = (S_0(t))e^{\beta'Z_1},$$

where  $S_1(t)$  is the survival curve for an individual with exogenous variables  $Z_1$ . Cox [1972] shows how to estimate the vector  $\beta$  and the function  $h_0(t)$  with a maximum likelihood approach.

In the next section we demonstrate the usefulness of the Cox Regression technique by estimating an unemployment duration equation and a childspacing equation.

#### IV. TWO EMPIRICAL EXAMPLES WITH CENSORED OBSERVATIONS

In this section we demonstrate the feasibility of the Cox model with two empirical examples. The first application estimates an equation where the dependent variable is a woman's duration of unemployment following the birth of her first child. The second application concerns the length of time a family waits before having their first child.

#### A. Duration of Unemployment

As we noted earlier, many have studied the labor force participation decisions of women. Some, like Nelson [1977] and Heckman and Willis [1977] study it in the context of discrete time, while others like Mincer and Ofek [1980] analyze it in continuous time. In the present paper we show how the Cox regression model can be used to estimate the probability that a woman returns to work (following the birth of her first child) after one year, two years, three years, etc. This method takes account of the censored observations in the sample and will yield an unbiased estimate of the mean duration. We use the 1973 wave of the Parnes NLS data on young women to estimate the unemployment duration equation. Table 1 gives mean values for the six exogenous variables and the mean value of unemployment duration (the dependent variable). Note that by ignoring the fact that 79 of the duration observations are censored, one would underestimate the mean duration of unemployment for these women by 16 percent. A consistent estimate of mean duration is 3.25 and is easily calculated from  $E(T) = \int_0^{\infty} S(t)dt$ .

Table 2 gives the maximum likelihood estimates for the Cox model. To see how these coefficients are interpreted, recall that the Cox model expresses a "survival" curve as:

$$S(t) = (S_0(t)) \exp(B'X) \quad (2)$$

Consequently, a positive sign on the coefficient for exogenous variable Z means that as Z is larger, the women will decide to go back to work sooner. A negative sign means that as Z is larger, the women will wait longer before returning to work.

TABLE 1  
DEFINITION AND MEAN OF VARIABLES

<u>Variable</u>	<u>Mean</u>	<u>Definition</u>
Dependent variable	3.25*	Defined in table 2
EDUC	11.95	Wife's education
HUSINC	\$9274.55	Husband's income
DSMSA	.39	Dummy = 1 if in SMSA
DRACE	.245	Dummy = 1 if nonwhite
UNEMP	7.7	Unemployment rate of county
Age	19.54	Age of women when child was born

\*This mean takes account of the censored values. It is calculated as the area under the survival curve. If we calculate a simple mean of the 212 observations we get a value of 2.72. Hence, by ignoring the censoring problem we underestimate the duration of unemployment by 16 percent.

TABLE 2

## COEFFICIENT ESTIMATES IN THE COX REGRESSION MODEL

(Dependent Variable = Length of time to  
re-entering the labor force after having first child)

<u>Variable</u>	<u>Coefficient</u>	<u>Standard deviation</u>	<u><math>\chi^2_1</math>*</u>
EDUC	.1354	.0674	4.036
HUSINC	-.0000265	.0000206	1.654
DSMSA	.1326	.1878	.499
DRACE	.0586	.2092	.078
UNEMP	-.0127	.0155	.667
AGE	-.02195	.0465	.223

Log likelihood (all Betas = 0) = - 650.25

Log likelihood (all MLE) = - 647.09

Number of observations = 212

Number of censored values = 79

\*Using a significance level of .05, any  $\chi^2_1$  value greater than 3.84 is considered significant.

For the coefficients in Table 2 then, we see that as the woman's education increases, she will go back to work sooner. As her husband's income, her age or the unemployment rate increase however, she will wait longer before returning to work. The only significant coefficient at the .05 level is the education variable.

To see what effect education has on the time at which a woman returns to the labor force, recall that "survival" in our model means a woman did not go back to work by time  $t$ . Column 2 of Table 3 gives the survival probabilities for exogenous variables  $\bar{Z}_1 = (1) \text{ EDUC} = 12, (2) \text{ HUSING} = \$9200, (3) \text{ DSMSA} = 0, (4) \text{ DRACE} = 0, (5) \text{ UNEMP} = 77, \text{ and, } (6) \text{ AGE} = 19.5$ . Column 3 of Table 3 gives the survival probabilities for exogenous variables  $\bar{Z}_2$ , where  $\bar{Z}_2$  is the same as  $\bar{Z}_1$  except  $\text{EDUC} = 16$  rather than 12. Table 3 tells us that the probability of a woman with characteristics  $\bar{Z}_1$  of not going back to work within 2 years is .63. For a woman with characteristics  $\bar{Z}_2$ , this probability is .45.

#### B. Childspacing Equation

A second example that demonstrates the usefulness of the Cox technique in the estimation of economic decision equations is found in the work of Hyman [1980]. One variable of interest in Hyman's paper is childspacing, where he defines "childspacing" as the proportion of respondents who had one child during the following year, given that they desired to have one more child. In our paper we define childspacing as the length of time between children and estimate an equation where the dependent variable is the length of time women wait before having their first child. We again use the 1973 wave of the Parnes NLS data on young women. The dependent variable will be censored for those couples who did not have their first child by 1973. To handle this

TABLE 3

SURVIVAL\* PROBABILITIES EVALUATED AT  $\bar{z}_1$  AND  $\bar{z}_2$ 

<u>Time</u>	<u>Survival at <math>\bar{z}_1</math></u>	<u>Survival at <math>\bar{z}_2</math></u>
0	1.00	1.00
1	.75	.61
2	.63	.45
3	.51	.32
4	.44	.24
5	.38	.19
6	.34	.16
7	.29	.12

$\bar{z}_1$ : (1) EDUC = 12, (2) HUSINC = \$9200, (3) DSMSA = 0,  
 (4) DRACE = 0, (5) UNEMP = 77, and, (6) AGE = 19.5

$\bar{z}_2$ : Same as  $\bar{z}_1$ , except EDUC = 16.

\*Surviving to time t is defined as not returning to work by (i.e.,  
 to and including) time t.

censoring problem, the Cox regression model is a natural choice of estimation techniques and is the one we use. Table 4 gives the maximum likelihood estimates.

For the coefficients in Table 4 we see that as the wife's age, education, or IQ increases, or as husbands income goes up, the couple will wait longer before having the first child. Also, Table 1 tells us that couples who live in rural regions will wait longer than similar couples who live in urban areas before having the first child. However, the only significant coefficients are the education and income coefficients.

For this application "survival" means the family did not have a baby by any given time  $t$ . Column 2 of Table 5 gives the "survival" probabilities for exogenous variables  $\bar{z}_1$ : (1) Age = 20, (2) Dummy Rural = 0, (3) IQ = 100, (4) Educ. = 12, and, (5) Income = \$5,000. Column 2 tells us that probability of not have a child by two years is .425. A similar interpretation holds for the rest of column 2 in Table 5.

Column 3 of Table 5 gives the "survival" probabilities for exogenous variables  $\bar{z}_2$ :  $\bar{z}_2$  is the same as  $\bar{z}_1$ , except income = \$10,000 rather than \$5,000. Notice that the probabilities are uniformly (because of proportional hazard) higher for  $\bar{z}_2$ . This means that as income goes up (from \$5,000 to \$10,000), couples wait longer before having the first child. The probability of not having a child by any given year is greater for couples with husband's income of \$10,000 than it is for similar couples with husband's income of \$5,000. A similar interpretation holds for Column 4 of Table 5.

In this section we gave two examples of how the Cox model can be used to estimate economic time decision models. Our purpose in this empirical section was not to re-do previous studies, but to demonstrate the applicability and feasibility of the Cox regression technique. It is also hoped that we make others aware of the censored data problem in future analyses.

Table 4

Coefficient Estimates in the  
Cox Regression Model

(Dependent Variable = Number of Years\* Before  
Having First Child)

<u>Variable</u>	<u>Coefficient</u>	<u>Standard Deviation</u>	<u>X<sup>2</sup>**</u>
Age at marriage	-.000218	.0267	0.00
Dummy (=1 if Rural)	-.1072	.0873	1.51
IQ of Wife	-.0014	.0031	.21
Education of Wife	-.08899	.0308	8.37
Husband's Annual Income	-.000064	.000015	17.73

---

Log Likelihood (all Betas = 0) = -3692.19

Log Likelihood (at MLE) = -3671.59

Number of observations = 681

Number of couples having a child = 620

Number of censored values = 61

\* Since we only had annual data, our dependent variables took on discrete values 1, 2, 3, etc. Of course, the Cox model can easily handle a continuous dependent variable.

\*\* All X<sup>2</sup> are with 1 degree of freedom. Using a significance level of .05, any X<sup>2</sup> value greater than 3.84 is considered significant.



Table 5

Survival Probabilities Evaluated at  
 $\bar{z}_1$ ,  $\bar{z}_2$  and  $\bar{z}_3$

Time	Survival* at $\bar{z}_1$	Survival* at $\bar{z}_2$	Survival* at $\bar{z}_3$
0	1	1	1
1	.589	.681	.667
2	.425	.537	.519
3	.276	.393	.373
4	.194	.304	.285
5	.156	.260	.241
6	.119	.213	.196
7	.080	.160	.144
8	.073	.150	.135
9	.064	.136	.122
10	.044	.104	.091
11	.044	.104	.091

$\bar{z}_1$ : (1) Age = 20, (2) Dummy Rural = 0, (3) IQ = 100, (4) Education = 12,  
 (5) Husband's Annual Income = \$5,000.

$\bar{z}_2$ : Same as  $\bar{z}_1$ , except husbands annual income = \$10,000.

$\bar{z}_3$ : Same as  $\bar{z}_1$ , except Education = 15.

\*"Surviving" to time t is defined as not having a baby by (i.e., up to and including) time t.

## V. CONCLUSIONS

In this paper we pointed<sup>2</sup> out a potential source of bias in the estimation of continuous time decision equations. This bias will exist whenever there are censored observations in the data and estimation techniques such as least squares are used. To correct for this bias one has to use an estimation technique, such as the Cox regression model, which takes censored observations into account. We demonstrat<sup>3</sup>ed the usefulness of the Cox model by estimating an unemployment duration equation and a childspacing equation. We think that the Cox model performs adequately and yields reasonable estimates.

#### REFERENCES

- Cox, D. R., "Regression Models and Life Tables", Journal of the Royal Statistical Society, Series B, Vol. 34, 1972.
- Harry Diamond Laboratories, Technical Report HOL-TR-1707, "A Program for the Numerical Inversion of the Laplace Transform", by Arthur Hausner, August 1975.
- Hyman, J., "Estimation of Fertility Using a Stock-Adjustment Model", Review of Economics and Statistics, November, 1980.
- Mincer, J., "Labor Force Participation of Married Women", in Aspects of Labor Economics, edited by H. G. Lewis, New Jersey: Princeton University Press, 1962.
- Mincer, J. and H. Ofek, "Interrupted Work Careers", Working Paper No. 479, NBER, May 1980.
- Mincer, J. and S. Polachek, "Earnings of Women", J.P.E., Part 2, March/April 1974.
- Mincer, J. and S. Polachek, "Women's Earning Reexamined", Journal of Human Resources, Winter 1978.
- Nelson, F., "Censored Regression Models with Unobserved, Stochastic Censoring Thresholds", Journal of Econometrics, Nov. 1972.
- Sandell, S., "Attitudes Toward Market Work and the Effect of Wage Rates on Lifetime Labor Supply of Married Women", Journal of Human Resources, Summer, 1977.
- Sandell, S. and D. Shapiro, "The Theory of Human Capital and the Earnings of Women: A Reexamination of the Evidence", Journal of Human Resources, Winter, 1978.
- Shapiro, D. and F. Mott, "Labor Supply Behavior of Prospective and New Mothers", Demography, May, 1979.

ONA PROFESSIONAL PAPERS - 1978 TO PRESENT\*

- PP 211  
Mizrahi, Maurice M., "On Approximating the Circular Coverage Function," 14 pp., Feb 1978, AD A054 429
- PP 212  
Mangel, Marc, "On Singular Characteristic Initial Value Problems with Unique Solution," 20 pp., Jun 1978, AD A058 535
- PP 213  
Mangel, Marc, "Fluctuations in Systems with Multiple Steady States. Application to Lanchester Equations," 12 pp., Feb 78 (Presented at the First Annual Workshop on the Information Linkage Between Applied Mathematics and Industry, Naval PG School, Feb 23-25, 1978), AD A071 472
- PP 214  
Weinland, Robert G., "A Somewhat Different View of the Optimal Naval Posture," 37 pp., Jun 1978 (Presented at the 1976 Convention of the American Political Science Association (APSA/IUS Panel on "Changing Strategic Requirements and Military Posture"), Chicago, Ill., September 2, 1976), AD A056 228
- PP 215  
Colle, Russell C., "Comments on: Principles of Information Retrieval by Manfred Kochen," 10 pp., Mar 78 (Published as a Letter to the Editor, Journal of Documentation, Vol. 31, No. 4, pages 298-301), December 1975), AD A054 426
- PP 216  
Colle, Russell C., "Lotka's Frequency Distribution of Scientific Productivity," 18 pp., Feb 1978 (Published in the Journal of the American Society for Information Science, Vol. 28, No. 6, pp. 366-370, November 1977), AD A054 425
- PP 217  
Colle, Russell C., "Bibliometric Studies of Scientific Productivity," 17 pp., Mar 78 (Presented at the Annual meeting of the American Society for Information Science held in San Francisco, California, October 1976), AD A054 442
- PP 218 - Classified
- PP 219  
Huntzinger, R. LeVar, "Market Analysis with Rational Expectations: Theory and Estimation," 60 pp., Apr 78, AD A054 422
- PP 220  
Heurer, Donald E., "Diagonalization by Group Matrices," 26 pp., Apr 78, AD A054 443
- PP 221  
Weinland, Robert G., "Superpower Naval Diplomacy in the October 1973 Arab-Israeli War," 76 pp., Jun 1978 (Published in *Seapower in the Mediterranean: Political Utility and Military Constraints*, The Washington Papers No. 61, Beverly Hills and London: Sage Publications, 1979) AD A055 564
- PP 222  
Mizrahi, Maurice M., "Correspondence Rules and Path Integrals," 30 pp., Jun 1978 (Invited paper presented at the CNRS meeting on "Mathematical Problems in Feynman's Path Integrals," Marseille, France, May 22-26, 1978) (Published in Springer Verlag Lecture Notes in Physics, 106, (1979), 234-253) AD A055 536
- PP 223  
Mangel, Marc, "Stochastic Mechanics of Molecule Molecule Reactions," 21 pp., Jun 1978, AD A056 227
- PP 224  
Manger, Marc, "Aggregation, Bifurcation, and Extinction in Exploited Animal Populations," 48 pp., Mar 1978, AD A058 536  
\*Portions of this work were started at the Institute of Applied Mathematics and Statistics, University of British Columbia, Vancouver, B.C., Canada
- PP 225  
Mangel, Marc, "Oscillations, Fluctuations, and the Hopf Bifurcation," 43 pp., Jun 1978, AD A058 537  
\*Portions of this work were completed at the Institute of Applied Mathematics and Statistics, University of British Columbia, Vancouver, Canada.
- PP 226  
Reiston, J. M. and J. M. Mann, "Temperature and Current Dependence of Degradation in Red-Emitting GeP LEDs," 34 pp., Jun 1978 (Published in *Journal of Applied Physics*, 50, 3630, May 1979) AD A058 538  
\*Bell Telephone Laboratories, Inc.
- PP 227  
Mangel, Marc, "Uniform Treatment of Fluctuations at Critical Points," 30 pp., May 1978, AD A058 539
- PP 228  
Mangel, Marc, "Relaxation at Critical Points: Deterministic and Stochastic Theory," 54 pp., Jun 1978, AD A058 540
- PP 229  
Mangel, Marc, "Diffusion Theory of Reaction Rates, I: Formulation and Einstein-Smoluchowski Approximation," 50 pp., Jan 1978, AD A058 541
- PP 230  
Mangel, Marc, "Diffusion Theory of Reaction Rates, II: Ornstein-Uhlenbeck Approximation," 34 pp., Feb 1978, AD A058 542
- PP 231  
Wilson, Desmond P., Jr., "Naval Projection Forces: The Case for a Responsive NAF," Aug 1978, AD A054 543
- PP 232  
Jacobson, Louis, "Can Policy Changes Be Made Acceptable to Labor?" Aug 1978 (Submitted for publication in *Industrial and Labor Relations Review*), AD A061 528

\*ONA Professional Papers with an AD number may be obtained from the National Technical Information Service, U.S. Department of Commerce, Springfield, Virginia 22151. Other papers are available from the Management Information Office, Center for Naval Analysis, 2000 North Beauregard Street, Alexandria, Virginia 22311. An Index of Selected Publications is also available on request. The Index includes a Listing of Professional Papers; with abstracts; issued from 1969 to June 1981.

- PP 233  
Jacobson, Louis, "An Alternative Explanation of the Cyclical Pattern of Quits," 23 pp., Sep 1978
- PP 234 - Revised  
Jondrow, James and Levy, Robert A., "Does Federal Expenditure Displace State and Local Expenditure: The Case of Construction Grants," 25 pp., Oct 1979, AD A061 529
- PP 235  
Mizrahi, Maurice M., "The Semiclassical Expansion of the Anharmonic-Oscillator Propagator," 41 pp., Oct 1978 (Published in Journal of Mathematical Physics 20 (1979) pp. 844-855), AD A061 538
- PP 237  
Maurer, Donald, "A Matrix Criterion for Normal Integral Bases," 10 pp., Jan 1979 (Published in the Illinois Journal of Mathematics, Vol. 22 (1978), pp. 672-681)
- PP 238  
Utgoff, Kathleen Classen, "Unemployment Insurance and The Employment Rate," 20 pp., Oct 1978 (Presented at the Conference on Economic Indicators and Performance: The Current Dilemma Facing Government and Business Leaders, presented by Indiana University Graduate School of Business). AD A061 527
- PP 239  
Troost, R. P. and Warner, J. T., "The Effects of Military Occupational Training on Civilian Earnings: An Income Selectivity Approach," 38 pp., Nov 1979K, AD A077 831
- PP 240  
Powers, Bruce, "Goals of the Center for Naval Analyses," 13 pp., Dec 1978, AD A063 759
- PP 241  
Mangel, Marc, "Fluctuations at Chemical Instabilities," 24 pp., Dec 1978 (Published in Journal of Chemical Physics, Vol. 69, No. 6, Oct 15, 1978). AD A063 787
- PP 242  
Simpson, William R., "The Analysis of Dynamically Interactive Systems (Air Combat by the Numbers)," 160 pp., Dec 1978, AD A063 760
- PP 243  
Simpson, William R., "A Probabilistic Formulation of Murphy Dynamics as Applied to the Analysis of Operational Research Problems," 18 pp., Dec 1978, AD A063 761
- PP 244  
Sherman, Allan and Horowitz, Stanley A., "Maintenance Costs of Complex Equipment," 20 pp., Dec 1978 (Published By The American Society of Naval Engineers, Naval Engineers Journal, Vol. 91, No. 6, Dec 1979) AD A071 473
- PP 245  
Simpson, William R., "The Accelerometer Methods of Obtaining Aircraft Performance from Flight Test Data (Dynamic Performance Testing)," 403 pp., Jun 1979, AD A075 226
- PP 246  
Bredling, Frank, "Layoffs and Unemployment Insurance," 35 pp., Feb 1979 (Presented at the NBER Conference on "Low Income Labor Markets," Chicago, Jun 1978), AD A096 629
- PP 248  
Thomas, James A., Jr., "The Transport Properties of Dilute Gases in Applied Fields," 183 pp., Mar 1979, AD A096 464
- PP 249  
Glasser, Kenneth S., "A Secretary Problem with a Random Number of Choices," 23 pp., Mar 1979
- PP 250  
Mangel, Marc, "Modeling Fluctuations in Macroscopic Systems," 26 pp., Jun 1979
- PP 251  
Troost, Robert P., "The Estimation and Interpretation of Several Selectivity Models," 37 pp., Jun 1979, AD A075 941
- PP 252  
Nunn, Walter R., "Position Finding with Prior Knowledge of Covariance Parameters," 5 pp., Jun 1979 (Published in IEEE Transactions on Aerospace & Electronic Systems, Vol. AES-15, No. 3, Mar 1979)
- PP 253  
Glasser, Kenneth S., "The d-Choice Secretary Problem," 32 pp., Jun 1979, AD A075 225
- PP 254  
Mangel, Marc and Quanbeck, David B., "Integration of a Bivariate Normal Over an Offset Circle," 14 pp., Jun 1979, AD A096 471
- PP 255 - Classified, AD 8051 441L
- PP 256  
Maurer, Donald E., "Using Personnel Distribution Models," 27 pp., Feb 1980, AD A082 218
- PP 257  
Thaler, R., "Discounting and Fiscal Constraints: Why Discounting is Always Right," 10 pp., Aug 1979, AD A075 224
- PP 258  
Mangel, Marc S. and Thomas, James A., Jr., "Analytical Methods in Search Theory," 86 pp., Nov 1979, AD A077 832
- PP 259  
Glass, David V.; Hsu, Jh-Ching; Nunn, Walter R., and Perin, David A., "A Class of Commutative Markov Matrices," 17 pp., Nov 1979, AD A077 833
- PP 260  
Mangel, Marc S. and Cope, Davis K., "Detection Rate and Sweep Width in Visual Search," 14 pp., Nov 1979, AD A077 834
- PP 261  
Villa, Carlos L.; Zvijac, David J. and Ross, John, "Frank-Condon Theory of Chemical Dynamics. VI. Angular Distributions of Reaction Products," 14 pp., Nov 1979 (Reprinted from Journal Chemical Phys. 70(12), 15 Jun 1979), AD A076 287
- PP 262  
Peterson, Charles C., "Third World Military Elites in Soviet Perspective," 50 pp., Nov 1979, AD A077 835
- PP 263  
Robinson, Kathy I., "Using Commercial Tankers and Container-ships for Navy Underway Replenishment," 25 pp., Nov 1979, AD A077 836

- PP 264  
Weinland, Robert G., "The U.S. Navy in the Pacific: Past, Present, and Glimpses of the Future," 31 pp., Nov 1979 (Delivered at the International Symposium on the Sea, sponsored by the International Institute for Strategic Studies, The Brookings Institution and the Yonsei Shimun, Tokyo, 16-20 Oct 1978) AD A066 837
- PP 265  
Weinland, Robert G., "War and Peace in the North: Some Political Implications of the Changing Military Situation in Northern Europe," 18 pp., Nov 1979 (Prepared for presentation to the Conference of the Nordic Balance in Perspective: The Changing Military and Political Situation," Center for Strategic and International Studies, Georgetown University, Jun 15-16, 1978) AD A077 838
- PP 266  
Utgoff, Kathy Classen, and Brechling, Frank, "Taxes and Inflation," 25 pp., Nov 1979, AD A081 194
- PP 267  
Trost, Robert P., and Vogel, Robert C., "The Response of State Government Receipts to Economic Fluctuations and the Allocation of Counter-Cyclical Revenue Sharing Grants," 12 pp., Dec 1979 (Reprinted from the Review of Economics and Statistics, Vol. LXI, No. 3, August 1979)
- PP 268  
Thomson, James S., "Support Dependence and Inter-State Cooperation: The Case of Sub-Saharan Africa," 141 pp., Jan 1980, AD A081 193
- PP 269  
Weiss, Kenneth G., "The Soviet Involvement in the Ogaden War," 42 pp., Jan 1980 (Presented at the Southern Conference on Slavic Studies in October, 1979), AD A082 219
- PP 270  
Remnek, Richard, "Soviet Policy in the Horn of Africa: The Decision to Intervene," 52 pp., Jan 1980 (To be published in "The Soviet Union in the Third World: Success or Failure," ed. by Robert H. Donaldson, Westview Press, Boulder, Co., Summer 1980), AD A081 195
- PP 271  
McConnell, James, "Soviet and American Strategic Doctrines: One More Time," 43 pp., Jan 1980, AD A081 192
- PP 272  
Weiss, Kenneth G., "The Azores in Diplomacy and Strategy, 1940-1945," 46 pp., Mar 1980, AD A085 094
- PP 273  
Nakada, Michael K., "Labor Supply of Wives with Husbands Employed Either Full Time or Part Time," 39 pp., Mar 1980, AD A082 220
- PP 275  
Goldberg, Lawrence, "Recruiters Advertising and Navy Enlistments," 34 pp., Mar 1980, AD A082 221
- PP 276  
Goldberg, Lawrence, "Delaying an Overhaul and Ship's Equipment," 40 pp., May 1980, AD A085 095
- PP 277  
Mangel, Marc, "Small Fluctuations in Systems with Multiple Limit Cycles," 19 pp., Mar 1980 (Published in SIAM J. Appl. Math., Vol. 38, No. 1, Feb 1980) AD A086 229
- PP 278  
Mizrahi, Maurice, "A Targeting Problem: Exact vs. Expected-Value Approaches," 23 pp., Apr 1980, AD A085 096
- PP 279  
Walt, Stephen M., "Causal Inferences and the Use of Force: A Critique of Force Without War," 50 pp., May 1980, AD A085 097
- PP 280  
Goldberg, Lawrence, "Estimation of the Effects of A Ship's Steaming on the Failure Rate of Its Equipment: An Application of Econometric Analysis," 25 pp., Apr 1980, AD A085 098
- PP 281  
Mizrahi, Maurice M., "Comment on 'Discretization Problems of Functional Integrals in Phase Space'," 2 pp., May 1980, published in "Physical Review D", Vol. 22 (1980), AD A094 994
- PP 283  
Dismukes, Bradford, "Expected Demand for the U.S. Navy to Serve as An Instrument of U.S. Foreign Policy: Thinking About Political and Military Environmental Factors," 30 pp., Apr 1980, AD A085 099
- PP 284  
J. Kellison, W. Nunn, and U. Sumita, "The Laguerre Transform," 119 pp., May 1980, AD A085 100  
\*The Graduate School of Management, University of Rochester and the Center for Naval Analyses  
\*\*The Graduate School of Management, University of Rochester
- PP 285  
Remnek, Richard B., "Superpower Security Interests in the Indian Ocean Area," 26 pp., Jun 1980, AD A087 113
- PP 286  
Mizrahi, Maurice M., "On the WKB Approximation to the Propagator for Arbitrary Hamiltonians," 25 pp., Aug 1980 (Published in Journal of Math. Phys., 22(1) Jan 1981), AD A091 307
- PP 287  
Cope, Davis, "Limit Cycle Solutions of Reaction-Diffusion Equations," 35 pp., Jun 1980, AD A087 114
- PP 288  
Golman, Walter, "Don't Let Your Slides Flip You: A Painless Guide to Visuals That Really Aid," 28 pp., Oct 1980, AD A092 732
- PP 289  
Robinson, Jack, "Adequate Classification Guidance - A Solution and a Problem," 7 pp., Aug 1980, AD A091 212
- PP 290  
Watson, Gregory H., "Evaluation of Computer Software in an Operational Environment," 17 pp., Aug 1980, AD A091 213
- PP 291  
Maddala, G. S., and Trost, R. P., "Some Extensions of the Markov Process Model," 17 pp., Oct 1980, AD A091 946  
\*University of Florida
- PP 292  
Thomas, James A., Jr., "The Transport Properties of Binary Gas Mixtures in Applied Magnetic Fields," 10 pp., Sept 1980 (Published in Journal of Chemical Physics 72(10), 15 May 1980)

- PP 293  
Thomas, James A., Jr., "Evaluation of Kinetic Theory Collision Integrals Using the Generalized Phase Shift Approach," 12 pp., Sept 1980 (Printed in *Journal of Chemical Physics* 72(10), 15 May 1980)
- PP 294  
Roberts, Stephen S., "French Naval Policy Outside of Europe," 30 pp., Sept 1980 (Presented at the Conference of the Section on Military Studies, International Studies Association Kluweh Island, S.C.), AD A091 306
- PP 295  
Roberts, Stephen S., "An Indicator of Informal Empire: Patterns of U.S. Navy Cruising on Overseas Stations, 1869-1897," 40 pp., Sept 1980 (Presented at Fourth Naval History Symposium, US Naval Academy, 26 October 1979, AD A091 316)
- PP 296  
Dimukes, Bradford and Petersen, Charles C., "Maritime Factors Affecting Iberian Security," (Factores Maritimos Que Afectan La Seguridad Ibelca) 14 pp., Oct 1980, AD A092 733
- PP 297 - Classified
- PP 298  
Mizrahi, Maurice M., "A Markov Approach to Large Missile Attacks," 31 pp., Jan 1981, AD A096,159
- PP 299  
Jondrow, James M. and Levy, Robert A., "Wage Leadership in Construction, 19 pp., Jan 1981, AD A094 797
- PP 300  
Jondrow, James and Schmidt, Peter, "On the Estimation of Technical Inefficiency in the Stochastic Frontier Production Function Model," 11 pp., Jan 1981, AD A096 159  
"Michigan State University
- PP 301  
Jondrow, James M.; Levy, Robert A. and Hughes, Claire, "Technical Change and Employment in Steel, Autos, Aluminum, and Iron Ore, 17 pp., Mar 1981, AD A099 394
- PP 302  
Jondrow, James M. and Levy, Robert A., "The Effect of Imports on Employment Under Rational Expectations," 19 pp., Apr 1981, AD A099 392
- PP 303  
Thomason, James, "The Rarest Commodity in the Coming Resource Wars," 3 pp., Aug 1981 (Published in the *Washington Star*, April 13, 1981)
- PP 304  
Duffy, Michael K.; Greenwood, Michael J. and McDowell, John M., "A Cross-Sectional Model of Annual Interregional Migration and Employment Growth: Intertemporal Evidence of Structural Change, 1958-1975," 31 pp., Apr 1981, AD A099 393  
"University of Colorado  
"Arizona State University
- PP 305  
Nunn, Laura H., "An Introduction to the Literature of Search Theory," 32 pp., Jun 1981
- PP 306  
Anger, Thomas E., "What Good Are Warfare Models?" 7 pp., May 1981
- PP 307  
Thomason, James, "Dependence, Risk, and Vulnerability," 43 pp., Jun 1981
- PP 308  
Mizrahi, M.M., "Correspondence Rules and Path Integrals," Jul 1981. Published in *"Nuovo Cimento B"*, Vol. 61 (1981)
- PP 309  
Weinland, Robert G., "An (The?) Explanation of the Soviet Invasion of Afghanistan," 44 pp., May 1981
- PP 310  
Stanford, Janette M. and Tai Te Wu, "A Predictive Method for Determining Possible Three-dimensional Foldings of Immunoglobulin Backbones Around Antibody Combining Sites," 19 pp., Jun 1981 (Published in *J. theor. Biol.* (1981) 88, 421-439  
"Northwestern University, Evanston, IL
- PP 311  
Boves, Marianne, Brechling, Frank P. R., and Utgoff, Kathleen P. Classen, "An Evaluation of UI Funds," 13 pp., May 1981 (Published in *National Commission on Unemployment Compensation's Unemployment Compensation: Studies and Research, Volume 2, July 1980*)
- PP 312  
Jondrow, James; Boves, Marianne and Levy, Robert, "The Optimum Speed Limit," 23 pp., May 1981
- PP 313  
Roberts, Stephen S., "The U.S. Navy in the 1980s," 36 pp., Jul 1981
- PP 315  
Buck, Ralph V., Capt., "Le Catastrophe by any other name...", 4 pp., Jul 1981
- PP 316  
Roberts, Stephen S., "Western European and NATO Navies, 1980," 20 pp., Aug 1981
- PP 317  
Roberts, Stephen S., "Superpower Naval Crisis Management in the Mediterranean," 35 pp., Aug 1981
- PP 318  
Vago, Milan N., "Yugoslavia and the Soviet Policy of Force in the Mediterranean Since 1961," 187 pp., Aug 1981
- PP 319  
Smith, Michael W., "Anti-air Warfare Defense of Ships at Sea," 46 pp., Sep 1981 (This talk was delivered at the Naval Warfare System and Technology Conference of the American Institute of Aeronautics and Astronautics in Washington on December 12, 1980; in Boston on January 20, 1981; and in Los Angeles on June 12, 1981.)
- PP 320  
Trost, R.P.; Lurie, Phillip and Berger, Edward, "A Note on Estimating Continuous Time Decision Models," 15 pp., Sep 1981

