| AD-A101 422 | ARMY Shad Apr Etl- | ENGIN ED REL: 81 C (| EER TOP Lef Ima : Taylo | OGRAPHI Ges for R | C LABS | FORT B Graphic | ELVOIR APPLIC | VA ATIONS | (1) | F/G NL | 6/2 | |
|--------------------------|-----------------------------|----------------------------|-------------------------------|-------------------------|--------|-------------------|------------------|--------------|-----|-----------|-----|--|
| 1 or 3 AD(1422 | C | | | | | | | | | | | |
| | | | | | | | | | | | | |
| | | | | | | | | | | | | |
| | | | | | | | | | | | | |
| | | | | | | | | | | | | |
| | | | | | | | | | | | | |
| | | | | | | | | | | | | |
| | | | | | | | | | | | | |

ETL-0259

5-

AD A101422

Shaded relief images for cartographic applications

Cyrus C. Taylor

APRIL 1981

FILE COPY

S DTIC S ELECT JUL 1 6 19 H

LEVELT

EU.S. ARMY CORPS OF ENGINEERS ENGINEER TOPOGRAPHIC LABORATORIES FORT BELVOIR, VIRGINIA 22060

APPROVED FOR PUBLIC RELEASE; DISTRIBUTION UNLIMITED

Destroy this report when no longer needed. Do not return it to the originator.

and the second secon

The findings in this report are not to be construed as an official Department of the Army position unless so designated by other authorized documents.

The citation in this report of trade names of commercially available products does not constitute official endorsement or approval of the use of such products.

| | AENTATION PAGE | READ INSTRUCTIONS BEFORE COMPLETING FORM |
|--|---|---|
| T. REPORT NUMBER | 2. GOVT ACCESSI | ON NO. 3. RECIPIENT'S CATALOG NUMBER |
| EIL-209 | /I_0-/T | 5 TYPE OF REPORT & REPORT OF |
| SHADED RELIEF IMAGES FO | OR IONS | 9 Research Note |
| 7. AUTHOR(a) | <u> </u> | 8. CONTRACT OR GRANT NUMBER(.) |
| CYRUS C. TAYLOR | | |
| 9. PERFORMING ORGANIZATION NAME U.S. Army Engineer Topograph Fort Belvoir, VA 22060 | e AND ADDRESS nic Laboratories | 10. PROGRAM ELEMENT, PROJECT, TAS AREA & WORK UNIT NUMBERS |
| 11. CONTROLLING OFFICE NAME AND | ADDRESS | 12. REPORT DATE |
| U.S. Army Engineer Topograph | nic Laboratories / | //)Apr |
| Fort Belvoir, VA 22060 | (| 193 |
| 14. MONITORING AGENCY NAME & AD | DRESS(II different from Controlling O | ffice) 15. SECURITY CLASS. (of this report) |
| | | Unclassified |
| | | SCHEDULE |
| The DISTRIBUTION STATEMENT (of the | | |
| | | |
| 18. SUPPLEMENTARY NOTES | | |
| 18. SUPPLEMENTARY NOTES 19. KEY WORDS (Continue on reverse etd Atmospheric Haze | te it necessary and identity by block Perspective Projection | number) Variable Sun Angle |
| SUPPLEMENTARY NOTES KEY WORDS (Continue on reverse sid Atmospheric Haze Gray-Shade Image Image Formation Light Scattering | te it necessary and identify by block Perspective Projection Photometry Polynomial Data Base Relief Contours | number) Variable Sun Angle |
| 18. SUPPLEMENTARY NOTES 19. KEY WORDS (Continue on reverse side Atmospheric Haze Gray-Shade Image Image Formation Light Scattering Orthonormal Projection | te it necessary and identity by block Perspective Projection Photometry Polynomial Data Base Relief Contours Shaded Relief | number) Variable Sun Angle |
| 18. SUPPLEMENTARY NOTES 19. KEY WORDS (Continue on reverse side Atmospheric Haze Gray-Shade Image Image Formation Light Scattering Orthonormal Projection 20. ABSTRACT (Continue on reverse side The computer generation of sha geometric theory of image for discussion of the image simula graphic Laboratories (ETL). S blems, such as variable sun a discussed. The successful impl marizing details of the theory listings of the ETL software. | te it necessary and identify by block Perspective Projection Photometry Polynomial Data Base Relief Contours Shaded Relief If necessary and identify by block n aded relief images for cartogy mation is presented in some ation algorithms developed ieveral algorithms devised to angle, haze simulation, and lementation of these algorit are included, as are a Softwa | variable Sun Angle Variable Sun Angle raphic applications is analyzed. The detail, and is used to motivate the at the U.S. Army Engineer Topo- o address specific cartographic pro- relief contour algorithms, are also hms is described. Appendixes sum- re User's Guide, sample images, and |

しままくしょう

1. a to 1.

The work described in this report was performed in the Automated Cartography Branch, Mapping Developments Division, U.S. Army Engineer Topographic Lab-

PREFACE oratories by Mr. Cyrus C. Taylor. His training and technical guidance were provided by Mr. James R. Jancaitis, Project Engineer.

The study was done during the summers of 1978 and 1979 under the supervision of Mr. W. Howard Carr, Chief, Automated Cartography Branch; Mr. Eugene P. Griffin, Chief, Mapping Developments Division; and Mr. Howard O. McComas, Director, Topographic Development Laboratory.

This work was supported by the Defense Mapping Agency under the research and development sub-task entitled "Advanced SACARTS Software," 64701B/4303.

COL Daniel L. Lycan, CE was Commander and Director and Mr. Robert P. Macchia was Technical Director of the Engineer Topographic Laboratories during the study and report preparation.

1

| Acces | ssion For | _ | | | | |
|-------------|------------|-------|--|--|--|--|
| MILS | GRHAI | | | | | |
| DITE | TAB | | | | | |
| Unannounced | | | | | | |
| Just: | lfication_ | | | | | |
| | | | | | | |
| B; | | | | | | |
| Dist | ibuticn/ | | | | | |
| Ava | ilability | Codes | | | | |
| | Avai1 and | /or | | | | |
| Dist | Special | . { | | | | |
| Λ | | | | | | |
| H | | | | | | |
| | | 1 | | | | |

CONTENTS

ļ

A Construction of the second second

| | TITLE | PAGE |
|------|--|------|
| PRE | FACE | 1 |
| ILLU | 4 | |
| ТАВ | LES | 7 |
| I. | INTRODUCTION | 8 |
| II. | THEORY | 9 |
| | A. The Geometry of Image Formation | 12 |
| | 1. Orthonormal Projections | 12 |
| | 2. Perspective Projection | 14 |
| | B. Photometric Variables | 20 |
| | C. Light-Scattering | 26 |
| | 1. Lambert's Law | 27 |
| | 2. The Lommel-Seeliger Law | 30 |
| | D. Image Photometry | 33 |
| III. | ALGORITHMS | 39 |
| | A. Definition of Global Variables | 43 |
| | B. Visibility Algorithms | 43 |
| | 1. Assumption | 43 |
| | 2. Algorithmic Solutions | 43 |
| | C. Slope Determination | 54 |
| | 1. Normal to a Surface | 54 |
| | 2. Calculation of Angles to a Normal | 59 |
| | D. Density Computions | 62 |
| | 1. Definition and Calculation of Vectors of | |
| | Observation and Illumination | 62 |
| | 2. Image Illumination Calculation | 65 |
| | E. Graphic Production | 67 |
| | F. Special Purpose Algorithms | 69 |
| | 1. Variable Sun Angle Algorithms | 69 |
| | 2. Relief Contours | 74 |
| | 3. Simulation of Atmospheric Haze | 75 |
| IV. | IMPLEMENTATION AND RESULTS | 78 |
| | A. Perspective Shaded Relief Algorithms | 78 |
| | B. Orthonormal Shaded Relief Algorithms | 80 |

B. Orthonormal Shaded Relief Algorithms

CONTENTS (Continued)

-

| | TITLE | PAGE |
|---------|---------------------------------------|------|
| V. | DISCUSSION | 82 |
| VI. | CONCLUSIONS | 82 |
| APPF | ENDIX A | 86 |
| • • • • | 1. Theoretical Details | 86 |
| | 2 The Lommel-Seeliger Law | 92 |
| | 3. Image Element Illumination | 95 |
| APP | ENDIX B | 98 |
| | 1. Software Guide | 98 |
| | 2. Perspective Routines | 98 |
| | 3. Orthonormal Shaded Relief Routines | 111 |
| APP | ENDIX C | 116 |
| APP | ENDIX D | 138 |

ILLUSTRATIONS

| FIGURE | TITLE | PAGE |
|--------|---|------|
| 1 | Orthonormal Projection | 13 |
| 2 | Perspective View | 15 |
| 3 | Perspective View (With Emphasis on Perpendicular Porjection Plane). | 16 |
| 4 | Perspective View (With Emphasis on Oblique Projecting Plane). | 17 |
| 5 | The Y Coordinate Determination in Perspective View | 18 |
| 6 | The X Coordinate Determination in Perspective View. | 19 |
| 7 | Luminous Intensity | 25 |
| 8 | Illumination | 25 |
| 9 | Measurement of Luminous Flux | 29 |
| 10 | Geometry of Image Formation | 35 |
| 11 | Acceptable Elements of a Raster Pixel (Any Point in Hatched Area). | 45 |
| 12 | Radials in the Perspective Image | 46 |
| 13 | A Radial Terrain Profile With Sample Points Projected. | 48 |
| 14 | Concave Radial Profile | 51 |
| 15 | Convex Radial Profile | 53 |
| 16 | Biased Use of Elevation Data Points | 57 |

2010

ILLUSTRATIONS (Continued)

and the second second

| FIGURE | TITLE | PAGE |
|--------|--|------|
| 17 | Unbiased Use of Elevation Data | 57 |
| 18 | Angles to a Normal | 60 |
| 19 | Definition of Solar Vector | 63 |
| 20 | Definition of V | 64 |
| 21 | Sun Azimuth Importance | 70 |
| 22 | Variation of Solar Azimuth | 70 |
| 23 | Variation of Solar Azimuth | 72 |
| A1 | Definition of Variables for Lambert and Lommel-Seeliger Derivation | 90 |
| C1 | Nominal Perspective View: Cache, OK | 117 |
| C2 | Telescopic Perspective View: Cache, OK | 118 |
| C3 | Perspective View: Cache, OK | 119 |
| C4 | Telescopic Perspective View: Cache, OK | 120 |
| C5 | Wide Angle View: Cache, OK | 121 |
| C6 | Fisheye View: Cache, OK | 122 |
| C7 | Perspective View. High Sun: Cache, OK | 123 |
| C8 | Perspective View. Low Sun: Cache, OK | 124 |
| С9 | Perspective View. NW Sun: Cache, OK | 125 |
| C10 | Perspective View With Haze: Cache, OK | 126 |

ILLUSTRATIONS (Continued)

÷,

| FIGURE | TITLE | PAGE | |
|--------|--|------|--|
| C11 | Perspective View With 1/64 Resolution: Cache, OK | 127 | |
| C12 | Perspective View (N): Cache, OK | 128 | |
| C13 | Perspective View: Elk Mountain | 129 | |
| C14 | Perspective View: Elk Mountain With Haze | 130 | |
| C15 | Perspective View With Ridge Enhancement: Cache, OK | 131 | |
| C16 | Orthonormal Shaded Relief: Cache, OK | 132 | |
| C17 | Orthonormal Shaded Relief: Cache, OK | 133 | |
| C18 | Orthonormal Shaded Relief Image With Variable Sun Azimuth Merged With SIMCON Contours (20-meters Interval) | 134 | |
| C19 | Relief Contours: Cache, OK | 135 | |
| C20 | Relief Contours: Cache, OK | 136 | |
| C21 | Orthonormal View: Cache, OK | 137 | |

6

and the second second

TABLES

| NUMBER | TITLE | PAGE |
|--------|---|------|
| 1 | Line Printer Density Table | 68 |
| 2 | SHDPER.FTN | 83 |
| 3 | ALSLP.FTN | 84 |
| 4 | Outline of GRNDPT Source Code Function | 84 |
| 5 | The Angular Width of the Image as a Function of DIS | 85 |
| 6 | SSLPLP.FTN | 85 |

SHADED RELIEF IMAGES FOR CARTOGRAPHIC APPLICATIONS

It is the task of the carte rapher to display spatially distributed data in the most cost-effective and easily perceived manner available. Since the uses to which the data will be applied are varied, the optimum way of

I. INTRODUCTION displaying the data will also vary. This report examines a variety of related means of displaying one type of data, terrain elevation, for which versatile and efficient software has been produced at the Automated Cartography Branch, U.S. Army Engineer Topograbic Laboratories (ETL).

The problem of presenting terrain relief is not new. The history of cartography has been a progression from crude symbols representing mountains, to hachures, and then to the familiar contour lines as a means of portraying the surface of the earth.¹ With clear advantages owing to the presence of quantitative elevation information and the ease of registration with non-hypsometric information, the contour map has become the standard cartographic product depicting terrain relief. Nevertheless, terrain form is often difficult to perceive quickly and accurately in a representation limited to contours. Consequently, it is often desirable to supplement the contours with additional terrain representations.² Additionally, contour maps are not ideal for all users of cartographic products. With the advent of high speed digital computers and the creation of comprehensive digital terrain models, a variety of inexpensive cartographic products can be created for special applications, such as flight simulations or cut and fill studies.

The research described in this report approaches these problems from the standpoint of the qualitative representation of terrain based on the generation of idealized images. Two major types of products are investigated: (1) the analytic creation of shaded relief overlays for contour maps, and (2) the production of synthetic photographs. Both products exploit the variation of brightness between different areas of terrain owing to varying inclinations of the source of illumination. Since the resulting cartographic products are dependent on very few variables, it should be easy to train people to use efficiently the wealth of qualitative information present in these products.

and the second second

¹A. Robinson, R. Sale, and J. Morrison. *Elements of Cartography*, Fourth Ed., Wiley, 1978, pp. 15-31.

²J. Deates. Cartographic Design and Production, Longman, 1973, p. 73.

This report systematically examines the problems associated with the creation of shaded relief overlays, synthetic photographs, relief contours, and related products. The theories of forming images by optical systems and of light scattering from solid surfaces are examined first. Constraints on the implementation of the results of the theory imposed by available equipment are discussed next. The algorithms developed at ETL to produce shaded relief cartographic products are then described, with emphasis on the versatility provided by the polynomial terrain data base that is used as the basis of the ETL software. Finally, the report examines the results of the implementation of these algorithms on the ETL-PDP-11/45.

As outlined in the introduction of this report, the goal of the work described herein is to develop algorithms to produce terrain representations with significant qualitative informational content. As with most cartographic **II. THEORY** products, these terrain representations are visual representations. which are used because it is easier to interpret spatial data presented in a visual form. These qualitative representations are more or less highly specialized shaded relief images of the terrain. In this manner, information regarding landform can be quickly retrieved from the image on the basis of the continuous tone image and implicit lighting directions and surface characteristics.

In this section, the physical processes that we seek to simulate are examined. First, an analysis of the theoretical basis of the problem is essential. Although the basic theory is not new, a source that contains all aspects of the basic theory is needed.

At the outset, it is important to note the level at which we seek to understand the processes of image formation. We are interested only in the basic aspects of image formation, such as can be treated by means of classical physical quantities and by means of simple geometric optics. We are not interested in the more detailed understanding afforded by the use of electromagnetic theory, nor are we interested in the chemical details of image formation in real imaging systems such as the retina or photographic film. Thus, we will not consider diffraction and interference or quantum effects. This hardly seems a restriction for our purposes, since these effects are only important at a much smaller scale than we are concerned with.

We will divide the problem into conceptually and physically independent subproblems and will discuss briefly the solution of each. There are four intermediate problems that must be solved if we are to simulate shaded relief images of the terrain. These problems are

- 1. The description of the lighting source illuminating the terrain.
- 2. The interaction of the incident light with the surface of the terrain.
- 3. The propagation of the light from the terrain to the particular (idealized) imaging system.
- 4. The recording of the important properties of the reflected light in some permanent image.

The first and third problems deal only with the direction of the propagation of the light; consequently, we do not need to consider the intensity of the light rays with which we are dealing.

The first problem is only implicitly dealt with in this section of the report, since, as we shall see, it is sufficient to define the direction and intensity of the illuminating light locally; i.e. at each point of the surface which we are imaging. Throughout much of this report, we shall assume a uniform direction and intensity of illumination across the entire area imaged.

The third problem is explicitly considered in some detail, since it is important to understand the various types of idealized images that we shall simulate. Two image types will be examined, the orthonormal and perspective projections. The orthonormal projection must be understood if shaded relief overlays are to be produced, for example, contour maps. Perspective projections are the mathematical idealization of the familiar types of imaging, such as vision and photography. These two projection types are sufficient to produce a variety of cartographic products. A third projection type which is also of cartographic interest is the oblique projection. This type has been discussed in a previous report.³

In the two remaining problems, the interaction of light with the terrain surface and with a recording medium, one must consider the intensity of light as well as the

³C. Taylor. Parallel Profile Plots for Visual Terrain Display, U.S. Army (ngineer Topographic Laboratories, Fort Belvoir, Virginia, 17L-0115, September 1977, AD-A051 483, pp. 8-11.

direction in which the light is propagating. We must therefore use some of the elements of photometry, which has developed the concepts necessary to discuss these problems mathematically. Since the reader may not be familiar with the basic concepts of photometry, a brief discussion of the elementary photometric variables is included. This will enable the two remaining problems to be examined.

The description of the second problem, the interaction of light with the surface of the earth, takes the form of a light-scattering "law." Such a law is a mathematical relationship between the brightness of the surface and a function of the relative positions of the observer and the source of illumination. It is important to note that we know of no law that accurately describes the interaction of light with all types of terrain under all lighting conditions, nor do we want such law for our purposes. Any such law would be very complex, since we would have to treat such variables as terrain composition. More importantly, such a law would be extremely difficult to interpret. Instead, we seek a light-scattering law that provides a good qualitative representation of the form of the terrain. In this report, two such laws are described. The two were selected for their simplicity of mathematical form, physical basis, and extensive empirical justification.⁴ Although this description of the interaction of light with the terrain is not unique or in any sense the best, the two laws are representative and can be quickly understood.

The last problem is that of recording in a permanent image the important properties of the light reflected from terrain. The solution is a function relating the brightness of a given surface point with the illumination of the corresponding point of the image. For the case of the perspective projection, we derive an exact solution. This solution simulates such photographic phenomena as vignetting. Such effects are perceptually objectionable for our purposes since qualitative analysis of the image becomes more complex. Thus, we shall simplify our formulas by using reasonable approximations. The result will be readily amenable to algorithmic implementation and will be suitable for the simulation of both perspective and orthonormal shaded relief images.

Thus, in this section, the theoretical basis for the production of shaded relief images of the terrain is developed. This problem is divided into four independent subproblems. A theoretical solution is developed for each. Since the subproblems are independent, this approach results in an algorithmic solution to the problem of shaded relief images that is readily amendable to computer implementation.

⁴B Horn. *Hill Shading and the Reflectance Map in Image Understanding in Proceedings*, Ed. by L. Baumann, Science Applications, Inc., Report SA1-80--895, 1979, pp. 79--120.

A. THE GEOMETRY OF IMAGE FORMATION. The first problem to be addressed is that of the geometry of image formation for the imaging systems of interest. This problem is treated first since it is the means of correlating points of the terrain with points of the image. Its solution plays a central role in any algorithms developed for shaded relief images. The process of image formation is, as noted before, best treated in terms of geometric optics. In such an approach, the formulation of the problems is in terms of projective geometry. Thus, the solutions derived below will be projection equations defining the geometry of image formation for the types of images of interest.

Two types of projections to generate images are considered here: orthonormal projections and perspective projections. These two projections were chosen as being of primary cartographic interest at the present time. The orthonormal projection of gray shade information may be used as a contour map overlay, enabling a quick analysis of terrain form by aiding the task of interpreting contour lines. Perspective projections of gray shade data will be valuable wherever a relistic portrayal of the terrain, as seen from a given point, is called for.

1. Orthonormal Projections. An orthonormal projection may be defined as the projection from an object onto a projection plane parallel to the base of the object, using projectors that are uniformly perpendicular to the projection plane. (see figure 1). Thus, the projection equations will define a transformation from a three-dimensional space to a two-dimensional plane. Accordingly, a three-dimensional cartesian coordinate system (x, y, z) can be introduced that will be used to define the position of points of the object, and a two-dimensional (x', y') cartesian coordinate system can be used in the projection plane. For simplicity, let the x', x and the y', y axes be parallel. Then, the projection equations are simply

$$\mathbf{X}' = \mathbf{X} \tag{1}$$

$$\mathbf{Y}' = \mathbf{Y} \tag{2}$$

Note that the z-coordinate (elevation) drops out of the projection equations. Equations (1) and (2) apply only to maps created at a 1:1 scale. To allow for other map scales, a parameter, α , is introduced, such that for an $-\alpha$:1 map,

$$\mathbf{X}' = \mathbf{1}/\boldsymbol{\alpha} \mathbf{X} \tag{3}$$

$$Y' = 1/\alpha Y$$
 (4)



It should be noted that the earth's surface cannot be depicted in an orthonormal projection where the projection plane is everywhere perpendicular to the earth's surface, since a sphere is a nondevelopable surface. All standard topographic maps are projections in which this problem is minimized, and it is assumed that the data base for preparing orthonormal shaded relief projections has been transformed in this manner.

2. Perspective Projection. A perspective projection is a projection of an object onto an image plane, characterized by nonparallel projectors that converge to a point behind the image plane (see figure 2). We are concerned with the particular case in which the image plane is parallel to the plane defined by the Z-and X-Axes of some coordinate system associated with the object. This is not a limitation on the generality of the transformation equations that will be derived; a suitable rotation of the coordinate system of the object will enable any perspective view to be produced.

We begin our derivation of the projection equations by defining the relevant parameters (see figures 2 through 6), assuming the usual right-handed orthogonal (X, Y, Z) coordinate system associated with the object. The origin of this coordinate system is at some point Q. At a point X = 0, $Y = \ell$; Z = 0, a projection plane (PP) parallel to the XZ - Z plane of the coordinate system intersects the Y axis. The point F, located a distance h above the origin of the coordinate system plays a role analagous to that of the pinhole in a pinhole camera: all rays from the object will be assumed to converge to it. Two vertical planes, P and S, are used; P is perpendicular to the projection plane pp, and S is located at an angles to it. Both planes contain points Q and F. Finally, an image coordinate system (X', Y') is used in the projection plane, PP. This coordinate system has its origin at the point Q' with the X' axis parallel to the X axis, and the Y' axis parallel to the Z axis. The coordinates of Q' in terms of the (X, Y, Z) coordinate system are

$$X(Q') = X_{o}$$
(5)

$$Y(Q') = \ell \tag{6}$$

$$Z(Q') = Z$$
(7)

Consider first the X coordinate of some point of the object, Q, with coordinates (X, Y, Z). This point will be contained in some vertical plane S, inclined at an angle $\theta = \tan (x/y)$ to the vertical plane P (see figure 5). The projection of this point is seen to be

$$X' = \ell (x/y) - X_{o}$$
(8)



FIGURE 2. Perspective View.



FIGURE 3. Perspective View (With Emphasis on Perpendicular Projecting Plane).



È

, C

C. Tax

FIGURE 4. Perspective view (With Emphasis on Oblique Projecting Plane).





Now, determine the Y' coordinate. Examine the vertical plane S, containing the point Q being projected and the focal point F (see figure 6). Again, simple geometry determines the transformed coordinate. As shown in figure 6, the radial variable $r = \sqrt{(X^2 + Y^2)}$ and the distance $\ell' = \ell/\cos\theta$, which is the distance from the line F - Q along the plane S to the plane PP, as introduced. The coordinate Y' is thus

$$\mathbf{Y} = (\mathbf{Z} - \mathbf{h}) \, \boldsymbol{\ell} \, / \mathbf{r} + \mathbf{h} - \mathbf{Z}_{\mu} \tag{9}$$

Equations 8 and 9 are the basic transformation equations. As with the orthonormal projection, some scale factors may be desirable. Here, two such scale factors will prove valuable: an image scaling factor β , and a vertical exaggeration γ . Equation 8 and 9 thus become

$$\mathbf{X}' = -\mathbf{X}_{\mathbf{y}} + \beta \ell \, \left(\mathbf{x} / \mathbf{y} \right) \tag{10}$$

$$Y' = Y_0 + \beta (\ell/\cos\theta) \quad (h - \gamma Z)/r \tag{11}$$

where we let $Y_o = h - Z_o$.

A COMPANY A DESCRIPTION OF A DESCRIPTION

Equations 10 and 11 are the defining equations for a perspective projection. A generalization of these equations, incorporating a projection plane at an oblique angle to the vertical axis of the object coordinate system, is possible. Such a generalization is of little interest for most proposed applications, and, in any case, can be easily accomplished by an appropriate rotation of the object coordinate system.



FIGURE 6. The X Coordinate Determination in Perspective View.

B. PHOTOMETRIC VARIABLES. In defining the fundamental photometric variables, the ones of greatest importance in the rest of the report are brightness, illumination, and luminous intensity. Although the variables represent concepts that are quite similar to the colloquial meanings of the terms, a detailed understanding of the terms is needed. In defining the terms, it is assumed that the concept of energy transport by electromagnetic radiation is well understood. This concept, together with elementary geometric considerations, will be used to define the needed variables.

It should be noted that the discussion of the elementary photometric concepts is given to provide a background adequate for the analysis of terrain brightness and image illumination. In this introduction, the concepts are developed in a logical and concise manner, but the approach is not intended to be detailed or exhaustive. The reader interested in a more detailed treatment is referred to texts such as Walsh.⁵

Photometry is the branch of optics concerned with the measurement of light. Although it is not, strictly speaking, a part of geometric optics, many practical applications are such that the geometric approximation is reasonable. The present work is such an application. Hence, we shall adopt the geometrical model of light by which light is regarded as the flow of luminous energy along geometric rays.⁶ This flow is subject to the geometric law of conservation of energy, which requires that the energy transmitted in unit time across a section of a bundle of rays is constant. This definition will be used implicity. Consider the radiant energy emerging from a portion of some surface, Σ . This surface may be fictitious, the surface of a self-radiating (primary) source, or it may be an illuminated surface of a solid (a secondary source).

The time-averaged transfer of energy by a ray of light is defined by a vector

$$S = \frac{C}{4\pi} \vec{E} \times \vec{H}$$
(12)

⁵J. Walsh, *Photometry*, Third Ed., Dover, 1958.

⁶M. Born and E. Wolf. Principles of Optics, 1 ourth Ed., Pergammon Press, 1970, pp. 115–116.

Where the Gaussian notation has been used, C is the speed of light, \vec{E} is the electric field vector, and \vec{H} is the magnetic vector of the electromagnetic wave.⁷ It is sufficient to note that the vector \vec{S} , known as *Poyntings* vector, defines the direction of and represents the amount of energy that crosses a unit area perpendicular to the direction in which the ray is traveling per unit time.

Therefore, \vec{S} may be interpreted as the density and direction of energy flow in a beam of electromagnetic radiation. The quantity with which we are primarily concerned at this point is the total energy per second that crosses a given surface. This quantity is known as the *flux* of radiant energy (i.e., the total energy rer second) crossing the surface. The flux is defined by

$$F = \int_{\text{surface}} \langle \vec{S} \rangle + n \, dA$$
 (13)

where \hat{n} is the outward unit normal to the surface, dA is an infinitesimal area element of the surface, and $\langle \vec{S} \rangle$ is the time average of the *Poyntings* vector.⁸ It will be recalled that the dot product of two vectors is

$$\vec{A} \cdot \vec{B} = |\vec{A}| |\vec{B}| \cos\theta$$
(14)

where θ is the angle between the two vectors. Thus, substituting equation (14) in equation (13), we find that

$$F = \int_{\text{surface}} |\mathbf{s}| |\hat{\mathbf{n}}| \cos\theta \, d\mathbf{A}$$
(15)

or, since the normal vector was defined as the unit normal vector, $|\hat{n}| = 1$, and

$$F = \int_{\text{surface}} IS \int_{\text{cos}\theta} dA$$
(16)

⁷M. Born and F. Wolf. *Principles of Optics*, Fourth Ed., Pergammon Press, 1970, pp. 115–116.

⁸R. Longhurst. Geometrical and Physical Optics, Second Ed., Longmann, Green and Co., 1967, p. 434.

The above discussion assumes that the light with which we are concerned is traveling in a single, specific direction and that it has no divergence. However, this is an ideal situation, which does not exist in physical reality. Instead, the light traversing our surface will be composed of one or more rays of light occupying an infinitesimal solid angle. In general, for any direction defined by the polar angles (α, β) , there will be defined some differential *Poynting* vector (differential because it occupies a differential solid angle). Thus, in general, we have the differential *Poynting* vector in any given direction (α, β) , defined by an arbitrary function B (α, β) , such that

$$d\overline{S}(\alpha,\beta) + B(\alpha,\beta) d\Omega$$
(17)

where we assume that B (α , β) has a unique, (time-averaged) value for all (α , β).

To determine the flux of radiant energy across a differential element of our surface, one must integrate over all possible infinitestimal cones of light. Thus, one integrates with respect to the differential *Poynting* vectors, or equivalently, with respect to the differential solid angle. For the differential flux across a differential surface element with unit normal \hat{n} ,

$$dF = \int_{\alpha,\beta} d\vec{S} (\alpha, \beta) + \hat{n} dA$$
$$= \int_{\alpha,\beta} B (\alpha, \beta) \cos\theta (\alpha, \beta) d\Omega dA$$
(18)

where the dependence of θ on α and β has been explicitly noted.

The determination of the total flux of radiant energy across our surface requires integration over the differential surface element. It should be obvious that our differential *Poynting* function S (α , β) will also, in general, be a function of position. Thus, the total flux across some surface A with local coordinates (ξ , η), and polar angles (α , β) will be

$$F = \int_{\xi,\eta} F(\xi,\eta) dA$$

=
$$\int_{\xi,\eta} \int_{\alpha,\beta} B(\alpha,\beta;\xi,\eta) \cos\theta(\alpha,\beta;\xi,\eta) d\Omega dA \qquad (19)$$

Note the generalization that has been made. Since the differential flux incident on our surface will, in general, vary from point to point, so will the defining, function B. Similarly, since our surface may be curved, the value of the angle θ between the normal to the surface and some vector defined by the polar angles (α , β) will also be a function of position. This additional functional dependence has been made explicit in equations (20) and (21), with the two types of dependence differentiated by semicolons.

Let us now interpret these mathematical results in terms of photometrically defined variables. The only variable entering into the mathematical definition of the flux that is arbitrary is B (α , β). This variable is the photometric brightness,⁹ which is the photometric quantity that will be of concern throughout the rest of this report. It is analagous to the familiar concept of brightness, differing from it only in that (1) the efficiency of the human eye is a function of the intensity of the incident light, and (2) the efficiency of the human eye is a function of the frequency of the light.

Brightness is the most important photometric variable for our purposes, since it is independent of distance. Qualitatively, this can be seen by considering a luminous surface element $d\Sigma$ at a distance $|\vec{\tau}|$ from the surface element of a photodetector, da. We know from elementary physics that the flux upon the detector area element obeys the inverse square law. Noting that the solid angle subtended by the surface element also obeys the inverse square law and applying the differential form of equation (19), one can see that brightness is independent of the distance of the observer:

$$B = dF/(dA \cos\theta \ d\Omega)$$
(20)

Explicity writing the inverse square dependence of dF as

$$dF = dF_0 / |\vec{r}|^2$$
(21)

and of $d\Omega$ as

$$d\Omega_0 = d\Omega_0 |\vec{\tau}|^2$$
(22)

⁹R. Longhurst. Geometrical and Physical Optics, Second Ed., Longmann, Green and Co., 1967, p. 434.

where we have assumed all other quantities held constant, one can substitute into (20) and see that

$$\mathbf{B} = \mathrm{d}\mathbf{F}_{\mathrm{o}}/(\mathrm{d}\mathbf{A}\,\cos\theta\,\mathrm{d}\Omega_{\mathrm{o}}) \tag{23}$$

thus demonstrating the truth of our claim that brightness is independent of distance.

After having defined flux and photometric brightness, two other photometric quantities can be defined that will prove useful. Rewriting equation (20), we have the basic photometric equation of

$$\mathbf{IF} = \mathbf{B} \mathbf{d} \mathbf{A} \, \cos\!\theta \, \mathbf{d} \mathbf{\Omega} \tag{24}$$

where the quantities are as defined above.

Consider a small luminous surface element, dA, as shown in figure 7. This luminous surface does not necessarily radiate equally in all directions. To define the intensity of the element's radiation in a given direction, we define *luminous intensity*, 1, as the flux emitted per unit solid angle in a given direction.¹⁰ Mathematically, this is written as

$$dI = dF/d\Omega = B \cos\theta dA$$
(25)

where d1 is the differential luminous intensity of the surface element in a direction inclined at an angle θ to the normal to the surface element.

Now consider another surface element, dA, which is illuminated: i.e. there is a nonzero flux of radiation upon the surface (see figure 8). Then the incident flux per unit area upon the surface element is defined as the *illumination* of the element dA.¹¹ Thus, if we consider the illumination of the surface element by a source of illumination positioned at an angle θ to the normal to the surface element, the differential illumination, dI, of the surface element may be written as

$$dE = dF/dA = B\cos\theta \,d\Omega \tag{26}$$

These definitions complete the introduction to the basic photometric variables and will suffice for the succeeding discussions of light scattering by surfaces and of image photometry.

¹¹Ibid.

ľ

¹⁰M. Born and L. Wolt. *Principles of Optics*, Fourth Ed., Pergammon Press, 1970, p. 182.



A CONTRACTOR OF A CONTRACT





FIGURE 8. Illumination.

C. LIGHT-SCATTERING. The description of the scattering of light by a terrain surface is a central component of the theory of shaded relief images. It was shown previously that photometry provides the appropriate language for this description. Within the context of this language, one variable, surface brightness, was shown to embody all information of interest concerning light emerging from any surface. The discussion of photometry, however, left "brightness" as an abstract and arbitrary function. Thus, the meaning of "brightness" must be defined as it relates to light-scattering by surfaces. This is done by examining the two specific light-scattering functions selected for use in the ETL software.

The light-scattering function chosen is really the heart of any synthetic image. This formula determines how the terrain model is shaded. This shading of the terrain model is, in turn, the principal guide to the form of the terrain available to a viewer of a synthetic image. Such an observer will interpret the image on the basis of a number of poorly defined preconceptions based on years of visual experience. Thus, the light-scattering function chosen will, in a poorly understood manner, define the apparent relief of any synthetic image generated.

Two criteria were used to select the two light-scattering functions used at ETL:

1. Simplicity of mathematical form.

ļ.

2. Extensive empirical justification.

The first is essential if the chosen law is to be used in efficient software to generate shaded relief images. The second requires an extensive collection of familiar physical objects that are well described by the chosen functions. Any such formula should therefore satisfy the preconceptions of an observer interpreting the resulting image.

From the criteria, a deficiency exists in understanding the scattering of light: empirical results can rarely be expressed in terms of simple functions: however, theoretical formulate rarely provide a good description of actual surfaces. The two lightscattering functions chosen by ETL are complementary attempts to meet both criteria. Thus, Lambert's law accurately describes the light-scattering behaviour of many common surfaces, and it can be simply expressed. However, no entirely satisfactory derivation of it has yet been found. The Lommel-Seeliger law, on the other hand, was first derived from theoretical considerations. It is thus of simple mathematical form, but it is not broadly applicable. Empirical justification of both laws is presented below and discussion of the theory of each is included in appendix 1. The discussion below presents both Lambert's law and the Lommel-Seeliger law as functions describing the brightness of a terrain surface element. These functions depend on the relative orientation of the surface element to the source of illumination, and in the case of the Lommel-Seeliger law, upon the inclination of the surface to the observer. To use this formulation, one needs only to calculate the flux on a photosensitive surface. These results can then be qualitatively interpreted, emphasizing the characteristic properties of each.

1. Lambert's Law. The first of the light-scattering functions chosen for implementation in the ETL software was Lambert's law. Lambert's law describes the interaction of light with a surface that, by definition, is perfectly diffuse. In contrast with a perfectly reflecting surface, which is infinitely bright in the direction of reflection and totally dark elsewhere, a perfectly diffuse surface is equally bright, regardless of the direction from which it is viewed. However, this brightness is not independent of the source of illumination. This follows from the requirement that no more light can be reflected from a surface than is incident on it. Since the flux on a surface element will decline as the cosine of the angle i between the direction of propagation of the incident light and the normal to the surface, Lambert's law may thus be written¹²

$$\mathbf{B} = \mathbf{B}_{0} \cos i \tag{27}$$

The B_0 term is the maximum brightness of the surface and will depend upon the total reflectivity of the terrain and upon the illumination of the surface.

¹²J. Walsh. Photometry, Third Ed., Dover, 1958, p. 137.

Many natural surfaces, which are of cartographic interest, obey Lambert's law to a high degree of accuracy. The surface of any body composed of discrete particles that are translucent will obey Lambert's law to a good approximation.^{1,3} Thus, the law accurately describes the light-scattering properties of natural surfaces such as snow, sand, pumice, hoarfrost, and some vegetation. Lambert's law also accurately describes the diffusing properties of a surface that is rough or corrugated and that is composed of discrete low-albedo particles, each of which scatters light equally in all directions.^{1,4} Most rocks can be accurately modeled as such, and Lambert's law is thus applicable to them. This extensive collection of natural materials obeying Lambert's law suggests that, in addition to serving as a theoretical photometric standard, the law may also serve as a natural standard for diffuse surfaces for most people.

The two models given above for surfaces obeying Lambert's law are empirical in nature and cannot be justified in a rigorous theoretical manner.¹⁵ This is not a significant drawback for cartographic purposes, since Lambert's law is both empirical in nature and a simple mathematical form. However, the lack of theoretical justification does indicate a deficiency in the current understanding of the scattering of light. Appendix 1 includes, in a discussion parallel to the derivation of the Lommel-Seeliger law, a brief mathematical discussion of the first model of Lambert's law, indicating the deficiency of this model.

Applying Lambert's law to calculations of flux is straightforward, but illustrates several features of interest. The features can be demonstrated by examining a simple device for measuring the flux from a surface. The device consists of a photosensitive surface of area **a**, which through the use of apertures or some other system, has a light acceptance cone subtending a solid angle of $d\omega$ (see figure 9). This photodetector is situated a distance z above a surface obeying Lambert's law, and the detector acceptance cone is inclined at an angle θ to the normal to the surface. Consequently, the distance from the surface area within the detector acceptance cone to the detector is $r = z \sec \theta$. The surface element within the detector acceptance cone is thus of area

$$dA = r^2 d\omega / \cos\theta$$
(28)

14_{Ibid.}, p. 4553.

¹³B. Hapke and H. Van Horn, J. Geophys. Res., 68(1963), p. 4552.

¹⁸P. Beckmann. Scattering of Light by Rough Surface in Progress in Optics, N. VI, 1 d, by 1, Wolf, North-Holland, 1967, p. 57.



From the surface, the photodetector subtends a solid angle of

$$d\Omega = a/r^2 \tag{29}$$

If one uses the basic photometric identity, equation (24), the flux upon the detector is equal to the fraction of the light from each point of the surface that falls upon the detector $(d\Omega)$, times the effective area of the surface element $(dA \cos\theta)$, times the brightness of the surface:

$$F = B dA \cos\theta d\Omega$$

= $B_0 \cos\theta (r^2 d\omega / \cos\theta) \cos\theta (a/r^2)$
= $B_0 \cos\theta d\omega$ (30)

Several implications of this equation should be noted. First, if one assumes that the surface is uniform and of infinite extent, the flux upon the detector is independent of the viewing angle θ . Second, if one makes the same assumptions, the flux is independent of distance. The first of these is of greater general significance, since for surface elements of apparent area $dA = dA_o/\cos\theta$, it is also true. As the observer moves farther away, the flux will decline as $1/r^2$, but the independence of observation angle is still true. This property is discussed in the section on image photometry.

The implications of this discussion for the generation of synthetic images is clear. Slopes facing the source of illumination will be bright, slopes facing away will be dark, and flat areas or slopes parallel to the source of illumination will be neutral. The precise nature of the shading should resemble that of actual terrain.

2. The Lommel-Seeliger Law. The second light-scattering function chosen for implementation in the ETL software was the Lommel-Seeliger law. Theoretical in origin, the function is based on a simplified model of a low-albedo scattering body. A slightly more general treatment leads to a widely applicable light-scattering function, which, however, cannot be evaluated in closed form in terms of known functions.¹⁶ The simpler form of the Lommel-Seeliger law thus provides clear advantages for any simulation and, as discussed below, provides an approximate description of the light-scattering properties of a variety of natural surfaces. The principle feature of the Lommel-Seeliger law that differentiates it from Lambert's law is the dependence on viewing angle. This dependence is expressed in the Lommel-Seeliger law:¹⁷

$$\mathbf{B} = \mathbf{B}_{o} / (1 + \cos\theta / \cos i) \tag{31}$$

114.4

where B_0 , *i*, and θ are as defined in the description of Lambert's law.

As noted, the Lommel-Seeliger law is derived from a simple model of low albedo objects (see appendix 1). The principle criticism that this model is open to is that it neglects the porous structure of many such natural bodies.¹⁸ This neglect means that the pronounced backscatter common to many real low-albedo scatterers is not modeled by the Lommel-Seeliger law. It should be noted that the degree of this backscatter is an independent parameter in the detailed model. Thus, the Lommel-Seeliger law may be considered as the limit of a more general model as the porous structure of that model is reduced to insignificance. An additional parameter in both the simplified and general models should be noted: the scattering law of the individual particles composing the body is also an integral part of the general law. This additional term is relatively insignificant, however, since both models are rather insensitive to the term's precise form, for moderate valves of the illumination and viewing angles.¹⁹

Empirical justification of the Lommel-Seeliger law is essential if the second criteria for its selection is to be met. Just as the general model of low-albedo scattering bodies includes a parameter governing the significance of the porous structure, physical scatterers seem to embody such a parameter.²⁰ Thus, the significance

¹⁶B. Hapke. J. Geophys. Res., 68(1963), p. 4575.

17 Ibid., p. 4573.

¹⁸Ibid., p. 4573.

¹⁹Ibid., p. 4577.

²⁰B. Hapke and H. Van Horn. J. Geophys. Res. 68(1963), p. 4552.

of the backscatter is highly variable, ranging from a sharp peak for some vegetation, rocks, and the moon to broad, nearly insignificant peaks for other materials. Since in any application, the form of the light-scattering law of the particles of which the body is composed must be somewhat arbitrarily chosen, as does the structure parameter, there is at present no good empirical reason for not choosing the limiting case of the Lommel-Seeliger law. Since it is simple, the Lommel-Seeliger law was chosen for use at ETL, as well as for at least one previous study.²¹

The application of the Lommel-Seeliger formula for terrain brightness is quite similar to that for Lambert's law. If we model the same device introduced in the discussion of Lambert's law, the determination of the total flux incident upon a photodetector of area **a** is straightforward (see figure 9). Situated **a** distance **r** from the surface, with a detector acceptance cone subtending a solid angle $d\omega$ at an angle θ to the normal to the surface, the detector will accept light from a differential area of $dA = r^2 d\omega / \cos\theta$. Since the detector subtends solid angle of $d\Omega = a/r^2$ at the surface, the total flux on the detector is

$$F = B d\Omega \cos\theta dA \tag{32}$$

B is a function of i and θ , as defined above. Hence,

$$= \frac{B_o}{1 + \cos\theta/\cos i} \cos\theta \, dA \, d\Omega$$

$$\frac{B_o \, d\omega \, a}{1 + \cos\theta/\cos i}$$
(33)

This result is substantially different from the corresponding result for Lambert's law. It is dependent on both the angle of illumination and the angle of observation. The formula does meet the elementary esthetic criteria mentioned in the discussion of Lamber's law: slopes facing away from the source of illumination are dark, and slopes facing the source of illumination are bright. The dependence on θ is less intuitive, since the brightness of the terrain reaches a minimum for an orthonormal view, and a maximum for high ($\theta \simeq 90^{\circ}$) values of θ , all else held constant. This can be readily understood within the context of the model from which the Lommel-Seeliger law is derived, and accurately describes the behavior of many physical objects. Thus, any discussion of the ease of interpretation of an image generated using the Lommel-Seeliger law (or any other must be based on such images, and not on the relative complexity of the light-scattering law.

²¹R. Batson, K. Edwards, and E. Eliason. J. Res. U.S. Geol. Surv., 3(1975), p. 401.
D. IMAGE PHOTOMETRY. The remaining theoretical problem to be addressed is that of recording, in a permanent image, the important properties of the light reflected by the terrain. There are two aspects of this problem. First, what quantity should be used to define the light reflected by the terrain? Second, what quantity is a real recording medium, such as photographic film or the human eye, sensitive to? The solution to the problem will be a mathematical formula relating these two quantities for a particular imaging system.

We saw in our discussion of photometry that the brightness, B, of a surface is a quantity that is independent of distance. All other basic photometric variables, such as flux, luminous intensity, and illumination, can be expressed in terms of the brightness and the variables that describe the geometry of a particular situation. Further, light-scattering laws that define the interaction of the terrain surface with the incident light may easily be cast in a form defining the brightness of the terrain. Thus, the brightness will be used as the basic quantity defining the important properties of the interaction of light with the terrain surface.

The other basic quantity to which a recording medium is sensitive to can be chosen from the photographic theory. The density of a photographic image is, in general, a complicated function of the illumination as a function of time.²² In normal photochemical reactions at light levels, such as those which we seek to simulate, the amount of product per unit area that is formed is directly proportional to the product of the illumination of the area and the time of illumination.²³ By assuming a unit time for all exposures, we may therefore use the illumination of a given point of an image as the important property of the light incident on that point.

First, the problem for the case of perspective imaging systems, such as a camera, will be discussed. The formula derived is more exact than is desirable for our purposes. Consequently, several approximations will be introduced that are reasonable for the cases of interest. The approximations will be used for both the perspective and orthonormal projections.

The second se

²²J. Walsh. Photemetry, Third Ed., Dover, 1958, p. 435.

²³H. Baines. The Photographic Process in Photography for the Scientist, Ed. by C. Engel, Academic Press, 1968, p. 7.

As before, the variables must be defined (see figure 10). An imaging system, such as a camera, is composed of a lens of aperture a with a light-sensitive surface parallel to the lens a distance \mathbf{r}_0 behind it. This system is imaging a luminous surface dS located a distance \mathbf{r} from the center of the lens, at an angle θ to the central axis of the optical system. The normal to the luminous surface $\hat{\mathbf{n}}$ is oriented at an angle φ to the ray connecting dS to the center of the camera lens (assuming $\hat{\mathbf{n}}$ to be coplanar with \mathbf{r} for simplicity).

The flux emitted by the luminous surface into a solid angle $d\omega$, oriented at an angle φ to the normal to the surface, is given by

$$dF = \beta \cos\varphi \, d\omega \, dS \tag{34}$$

Now, for the case of the camera-object system described above,

$$d\omega = \frac{da\cos\theta}{r^2}$$
(35)

and hence,

$$dF = \frac{\beta \cos\varphi \, dS \, da \cos\theta}{r^2} \tag{36}$$

Integrating over the area of the camera lens, we thus see that the total flux incident upon the camera lens is given by

$$F = \frac{\beta \cos\varphi \, dS \, a \, \cos\theta}{r^2} \tag{37}$$

If we assume that all the light incident on the lens from the surface element dS passing through the lens is concentrated upon the corresponding image element dS! and that a factor of $(1 - \gamma)$ of the incident flux is scattered or absorbed during passage through the lens, then the illumination of the image element is given by

$$F = \frac{dS}{dS'} \frac{dF}{dS} (1 - \gamma)$$
(38)



The factor of dS/dS' must now be evaluated. Our surface element dS is positioned such that the unit normal may be characterized by a polar angle α and an azimuthal angle β . Similarly the ray will be defined that connects the center of the camera lens to dS by a polar angle δ and an azimuthal angle γ . First, determine the angle θ that the radial vector makes with the central axis of the optical system. Since the radial vector is treated as a unit vector, the x-component of the vector is

$$r_{x} = \cos\delta \cos\gamma \tag{39}$$

Noting the definition of θ , one can see that it is defined by

$$\theta = \cos^{-1} (\mathbf{r}_{x}/\mathbf{r}) = \cos^{-1} (\cos\delta \, \cos\gamma) \tag{40}$$

Now, in an ideal imaging system, linear features of an object parallel to the image plane are transformed onto linear features in the image plane by a factor of proportionality known as the lateral magnification, M^{24} Area elements are similarly transformed by a factor of M^2 . As defined, $M = dS_o/dS'$ is inversely proportional to the radius r. Features oriented to dS_o , as dS is in the figure, will be transformed as their projection onto dS_o , which is equal to the dot product of the respective normals. Thus

$$dS_{\alpha} = \hat{\pi} (dS_{\alpha}) \cdot \hat{\pi} (dS) dS$$

= (-1, 0, 0) \cdot (\frac{1}{c}\cos\alpha \cos\alpha \sin\alpha) dS (41)
= \cos\alpha \cos\alpha dS

Hence,

$$dS/dS = dS/dS_{0} - dS_{0}/dS$$
$$= \frac{1}{\cos\alpha \cos\beta} - \frac{1}{M^{2}}$$
$$= \frac{r^{2}}{M_{0}^{2}} - \frac{1}{\cos\alpha \cos\beta}$$
(42)

²⁴G. Franke. *Physical Optics in Photography*, Focal Press, 1966, p. 12.

where M_o is the magnification for some nominal distance r_o . Substituting (42) into (39) and (40). One has the illumination on dS^t as

$$E = \frac{r^2}{M_o^2 \cos\alpha \cos\beta} - \frac{a\beta \cos\varphi \cos\theta}{r^2} - (1-\gamma)dS$$

$$= \frac{\alpha\beta \cos\varphi \cos\theta dS}{M_o^2 \cos\alpha \cos\beta} - (1-\gamma)$$
(43)

Equation 46 is the rigorous formula for the perspective projection. Note that the illumination falls off rapidly as θ increases. In fact, since the other variables are not independent of θ , the actual dependence, holding all else constant, goes as $\cos^4 \theta$.²⁵ This effect is known as vignetting and results in a bright central image, which darkens rapidly towards the edges. As such, the effect is undersirable. Hence, several approximations shall be considered to eliminate this effect.

First, since

$$\cos\varphi = \hat{n} \cdot r$$
 (44)

one may write

i,

$$\cos\varphi = \cos\alpha \cos\beta \cos\gamma \cos\delta$$
$$-\cos\alpha \cos\beta \cos\delta \sin\gamma \qquad (45)$$
$$-\sin\alpha \sin\delta$$

For small γ and δ , such as is the case near the center of the image, $\cos\gamma \simeq \cos\delta \simeq 1$ and $\sin\gamma \simeq \sin\delta \simeq 0$. Substituting for this case,

$$E \simeq \frac{a \beta \cos \alpha \cos \beta \cos \theta}{M_{0}^{2} \cos \alpha \cos \beta} dS (1 - \gamma)$$
 46)

²⁵R. Longhurst. Geometrical and Physical Optics, Second Ed., Longmann, Green and Co., 1967, p. 412

Since for small γ and δ , θ is also small, we have

$$E \simeq \frac{q a \beta dS}{M_o^2}$$
(47)

where we have let

$$\gamma = 0 \tag{48}$$

The result, which is a reasonable approximation for the central region of a perspective view, is independent of \mathbf{r} and is independent of any of the defining angles. Since the limiting case of the approximations used corresponds to the orthonormal view, the result is also valid for the orthonormal projection of gray shade data. Thus, for both projections of interest in this report, a formula now exists that relates the brightness of a surface element to the illumination of the corresponding point of the image. Since the illumination defines the density of an actual image, recording the illumination as a function of position stores the important information of the image needed for simulation. In the previous section of this report, the theoretical basis was examined of the creation of shaded relief images for cartographic applications. This theoretical basis was divided into four independent components, each of

III. ALGORITHMS which was examined in detail. Now, the task of assembling

the components of the theory within a unified algorithm for the generation of shaded relief images, must be undertaken. The algorithms must be understood before use of the software developed in undertaken, which is essential before any major modifications of the software created are attempted.

First, some notes should be made regarding the nature of the model embodied in the algorithms described below. In nature, the process of image formation may be described as a continous process, at least at the level at which we seek to simulate it. Every visible point on the object contributes light to a single point on the image plane. Mathematically, this process could be defined by a function, a 1:1 mapping of visible points on the object onto the points of the image plane. The image function will be determined by the geometry of the imaging system, the geometric model of light, and the geometries of the object and image spaces. The continuous nature of the process is clearly defined. Although discontinuties may exist in the visible object space of the perspective projection, as when a valley dips out of sight, every point contributing to the image has another such point infinitesimally far away from it. Correspondingly, the image plane is the basis for a continuous image. Thus, no inherently discrete aspects to the process of image formation exists.

This continuity is to be contrasted with the inherently discrete nature of any digital simulation. The image plane in such a simulation of the imaging process must be modeled as an array of discrete pixels, each of which can assume one of a set of discrete brightness levels. This discrete nature of the image space means that an inverse function mapping the image space into the object space is needed, at least implicitly. Such a function cannot, in general, be analytically determined for the perspective projection because of the complicated nature of the phenomena being modeled. The inverse function must therefore be algorithmically determined by a series of successive approximations for each pixel of the image. Similar approximations must be developed for each element for the theory embodied in the model.

The guiding principles in the development of the algorithms for the generation of shaded relief images must, for our purposes, be efficient and versatile when implemented in the form of computer software. Since each calculation involved in an algorithm takes a finite amount of time, severe constraints are placed on the form of any algorithm developed, and hence on the nature of the approximate solutions used. Thus, these constraints help to determine the specific content of any algorithms developed.

The discussion of the algorithms embodying the various aspects of the theory proceeds in a manner reflecting the role of each algorithm within the ETL software. The structure of this software for perspective and orthonormal images is quite similar. As can be seen, there are four major computational components of the software, each embodying a corresponding theoretical component. Thus, there are four conceptual divisions to the unified algorithms developed.

These parameters are determined once for each image, and they define the particular characteristics of the shaded relief image to be generated. The following four components must be sequentially done for each element of the image:

- 1. Define global image parameters (observer position, imaging system characteristics, vector of illumination).
- 2. Correlate image/object.

- 3. Determine local surface orientation.
- 4. Compute surface brightness/image density.

Since the coded digital image must be output in some graphic format, the fifth component is:

5. Image generation.

The discussion of the first point is essentially limited to a brief treatment of the mathematical definition of the vectors of illumination and observation. The vectors are necessary, since together with the orientation of a local surface element, they may be used to define the brightness of that surface element by means of Lambert's law or the Lommel-Seeliger law. Thus, vectors define the manner in which the illumination of the terrain is simulated, knowledge of which is crucial to interprete accurately the image produced. Other global variables that must be defined, such as the focal length of a perspective imaging system, should require no detailed explanation.

Having specified the global variables defining the image to be produced, one can generate a simulated image by performing a series of local calculations for each element of the image. Once a given image element (pixel) is specified, some point must be determined on the surface of the terrain whose projection lies within the pixel. Since an analytic solution to this problem is not available for the perspective case, an algorithm yielding an approximate solution is discussed. This algorithm exploits the projection of a radial elevation profile that lies on a vertical line in the image plane. By sampling the elevation profile corresponding to a given column of pixels, a point on the terrain with the required characteristics can be found by a process of successive approximations. Elevation data points may be readily accessed as needed, a minor problem when the polynomial data base is used. The situation is much simpler in the case of the orthonormal projection, since projection equations (3) and (4) may easily be inverted.

Having found a point on the surface of the terrain corresponding to a given pixel, one may use the point as a representation sample of the pixel. After having found a representation point, the orientation of the surface at the chosen point must be determined. This orientation may be defined by the vector normal to the surface at the point of interest. The determination of the normal is discussed for two types of terrain elevation data bases. (1) uniformly gridded data, and (2) the polynomial terrain data base. Gridded data yields an approximate solution, and the polynomial terrain data base yields an analytic solution.

All that remains at this point is to use a given light-scattering law and the results of the above calculations to determine the illumination of the pixel of interest. Since most commercially available gray shade output devices require input data specifying the density of a photographic image and not the illumination, this conversion is discussed, as implemented in the ETL software.

Once the shaded relief image has been generated and coded in the form of image density values, it must be output to some device capable of producing the graphic product. Three such output devices are available at ETL: (1) an electron beam recorder (EBR) for very high resolution, near-continuous tone images; (2) a line printer for the generation of proofing images; and (3) a Versatec plotter, which is used to generage moderate in resolution halftone images. The requirements of each device are discussed, and the specific algorithms developed to meet these requirements are outlined.

At the end of this section, several algorithms are discussed that are devised to meet specific cartographic problems. These algorithms enable a variable (i.e. nonglobal) sun angle to be used to generate perspective or orthonormal images, the simulation of atmospheric haze in perspective views, and the orthonormal relief contour images. The variable sun angle algorithm was introduced to accent terrain features that would otherwise wash out because of poor orientation relative to a given source of illumination. This is accomplished by locally varying the azimuth of the source of illumination around a principle source, a common cartographic technique. The result is an enhanced representation of terrain form.^{26,27} Atmospheric haze is simulated by a simple model designed to provide additional distance clues to the viewer of a shaded relief perspective image. Finally, a simple algorithm enabling the production of relief contours is discussed. Based on a cartographic product first developed by Kitiro Tanaka,²⁸ one can combine the resulting image of the quantitative information of contours with a striking visual representation of terrain form. These special purpose algorithms substantially enhance the versatility of the ETL software.

The implementation of the theoretical results of the last section are discussed in a set of algorithms for the computer-generated shaded relief images. Corresponding to each part of the theoretical solution to the problem of shaded relief images is an algorithm embodying that solution, typically in an approximate manner. One section, defining the parameters of the image to be produced, is executed once for any image; the other component algorithms are executed sequentially for each image element. Although these algorithms were developed with the intention of efficiently using the polynomial terrain data base, they are generally applicable to any digital terrain model. Thus, the algorithms serve as the basis for versatile and efficient software to generate a variety of shaded relief terrain images.

²⁶P. Yoeli. "Die richtung des licht bei analytischen," Kartographiche Nachrieten Guetersloh 17(1967), pp. 537-544.

²⁷K. Brassel. "A Model for Automatic Hill Shading," Am. Cart. 1(1974), pp. 15-27.

²⁸K. Tanaka. "The Orthographic Relief Method of Representing Topography on Maps," Geogr. Rev. 40(1950), pp. 444-456.

A. DEFINITION OF GLOBAL VARIABLES. Most calculations made in generating a shaded relief image are local in nature. The calculations for a given pixel are independent of the calculations for any other pixel and are independent of any terrain except that which is projected into the pixel of interest. Certain parameters are global in nature and must be defined if the image generated is to appear coherent to a viewer. These parameters govern those aspects of the image that are invariant across it, and they define the characteristics of the imaging system, such as focal length and field of view, the location and direction of view of the imaging system, and the position of the source of illumination.

In discussing the local algorithms below, each of these parameters is treated as a constant, which it is for a given image. The mathematical details of each parameter are introduced as it seems convenient, since any formal discussion at this point would be largely unmotivated. None of the parameters are complicated so that at this point no more is required than to call attention to the role they play in unifying the local calculations.

B. VISIBILITY ALGORITHMS.

1. Assumption. As noted, the visibility problem is one of areas. Thus, visibile areas of an object corresponding to the area of a given pixel are sought. The solution to the visibility problem that is used at ETL is based on the observation that any visible point with a projection lying within a given image pixel may be used to approximate the characteristics of that pixel. In essence, this means that the plane tangent to the topographic surface at any such visible point may be used to model the surface over the visible region of the object corresponding to the given pixel (see appendix A). Although this may prove somewhat arbitrary, as when terrain dips out of view and then reappears, any refinement of the assumption will require global knowledge of the object. As a practical matter, for images of sufficiently high resolution, the assumption is quite reasonable.

2. Algorithmic Solutions. Having made the assumption, one reduces the visibility problem to determining a point (X, Y) on the terrain surface z(x, y), subject to the requirement that the projection of this point, (X', Y'), lies within an image pixel defined by image coordinates $(x \pm \Delta x, y \pm \Delta y)$. As noted in the introduction, two cases are of interest, the perspective and orthonormal projections.

a. Orthonormal Projection. The orthonormal projection of a terrain surface z(x, y) is defined by the orthonormal projection equations (3) and (4). Since z is a function of (x, y) and since the projection equations are independent of z, there is no visibility problem for the case of the orthonormal projection. One, and only one, point of the surface is projected onto a given point of the image. Given the (X', Y') coordinates of a pixel of interest and the scale factor defining the projection, by inverting the projection equations, a point on the surface is defined that meets the acceptance criteria. This point is given by

$$X = \alpha X' \tag{49}$$

$$Y = \alpha Y' \tag{50}$$

Thus, for the case of the orthonormal projection of a terrain data base, the problem of finding points on the surface that may be used to define an image is relatively simple. Once such a point is found corresponding to a given image element, processing proceeds as outlined below.

b. Perspective Projection. The perspective projection of a topographic surface z(x, y) is defined by the perspective projection equations (10) and (11). These projection equations are not independent of z, and portions of the terrain surface may be obscured by other areas of the surface. The first observation precludes a simple analytic object/image correlation algorithm, such as is available with the orthonormal projection, since inversion of the perspective equations requires knowledge of the surface z(x, y). The second observation indicates that not any point with a projection lying within a given pixel is acceptable, for it may be obscured by terrain in the foreground. Thus, in considering whether or not a given point is acceptable, some knowledge of the terrain between i and the observer is required.

Since an analytic solution to the visibility problem is not possible, the ETL software addresses this problem algorithmically. This algorithm is an iterative procedure for finding a visible point on the terrain surface with a projection lying within specified bounds of a given point on the image. This is illustrated in figure 11. In this figure, any surface point within the hatched region is acceptable, in that

1. It will be visible.

2. Its projection lies within a tolerance Δy of the prescribed point YS.





This example will be used to examine the details of the algorithm used in the ETL software. The algorithm is implemented in the FORTRAN subroutine GRNDPT, to which the reader is referred (see appendix B). Note that the algorithm described is not restricted to the perspective projection. All that is required for its use with another projection is the substitution of the appropriate projection equation.

The analysis of the algorithm proceeds from the projection equa-

tions

$$X = X_{o} + \beta \ell (X/y)$$
(51)

$$Y = Y_{o} + \beta (\frac{v}{\cos\theta}) (h - \gamma Z) /r$$
 (52)

where the variables are as defined before. Recalling that the visibility problem has been simplified to one requiring only the determination of a visible point corresponding to a given pixel, the visibility problem can be solved by sampling the terrain along a radial. Since equation (10) can be rewritten as

$$X = -X_{o} + \beta \ell \cot\theta$$
 (53)

and since θ is a constant for a radial elevation profile, the x coordinate will also be constant for the projection of a radial profile. This will correspond to a column of pixels for most raster display devices. Thus, a single radial profile of elevation data may be used to determine the visible portions of the terrain for an entire column of pixels. (see figure 3).

To illustrate the features of the algorithm, consider a general example. The image to be generated is to be composed on m x (2n + 1) pixels, where **m** is the number of pixels per column and the columns of pixels are numbered from -**n** to +**n** as illustrated in figure 12. A visible pixel that will be projected into the jth pixel (from the bottom of the image) of the kth column (-**n** $\leq k \leq n$) is sought. The first task, which is not executed unless the column of pixels is being considered for the first time, is the sampling of the terrain along a radial. This is accomplished by filling some array, say **Y**, with **p** successive elevation data values, Y(R₁, θ_K), such that

$$Y(R_{I}, \theta_{K}) = Y(X_{IK}, Y_{IK})$$
(54)



FIGURE 12. Radials in the Perspective Image.

Where

$$X_{1K} = R_1 \cos\theta_K \tag{55}$$

$$Y_{1K} = R_1 \sin \theta_K$$
 (56)

$$\mathbf{R}_{\mathbf{I}} = (\mathbf{I} - \mathbf{I}) \ \Delta \mathbf{R} \tag{57}$$

$$\theta_{\rm K} = \tan^{-1} \left({\rm K} \, \Delta {\rm Y} \, / \varrho \right) \tag{58}$$

$$1 \leqslant 1 \leqslant P \tag{59}$$

Here, y' is the incremental distance between pixel centers, f is the focal length of the imaging system, and r is the elevation sample interval. Note that

$$\Delta \mathbf{R} = \mathbf{r}_{max} / (\mathbf{P} - 1) \tag{60}$$

where \mathbf{r}_{\max} is the maximum radius of interest and $\Delta \mathbf{R}$ should be chosen such that the radial increment is less than one-half the wavelength of the highest frequency terrain feature of significance in the data base. A radial profile such as this, serving as a local terrain model, is illustrated in figure 13.

The visibility problem is solved implicity by processing from the bottom of a given column of pixels upward and outward along the radial elevation profile (see figure 13). The first time that the projection of two consecutive elevation data points bracket the center of a given pixel of interest, then terrain lying between those two data points will be projected onto the pixel. This search procedure, isolating a visible portion of the terrain bracketing the pixel of interest, is the first component of the correlation algorithm. The second component is a recursive procedure for isolating a point of the terrain just identified that will be projected with arbitrary accuracy onto the center of the pixel of interest. This is done by

- 1. Approximating the terrain by a linear model.
- 2. Solving for the point of the linear model that will be projected onto the center of the pixel.
- 3. Accessing the actual elevation data value at the predicted point.
- 4. Checking the projection of the actual point against the required tolerance and iterating the procedure again, if necessary.



۲

1.1

FIGURE 13. A Radial Terrain Profile With Sample Points Projected.

The first time that the correlation subroutine is called for a given column \mathbf{I} , the counter governing the progression through the elevation radial is set to unity.

1 = 1

The elevation values of the first and second entries of the elevation profile are retained in variables Z1 and Z2, since they will be needed in the second component of the correlation algorithm. The array positions are replaced with the image \mathbf{Y}^{\prime} coordinates of their projections (actually, $\mathbf{Y}(1)$ is replaced with a large negative number since the actual projection is -100). This is illustrated by the following code:

> Z1 = Y(1)Z2 = Y(2)Y(1) = -100Y(2) = PROJ(Y(2))

where PROJ(Y(2)) symbolizes the operation

ſ

$$PROJ(Y(2)) = Y_{o} + \beta \left(\frac{\gamma}{\cos \theta_{K}} \right) \left(h - \gamma Y(2) \right) / r$$
(61)

the test of the first component of the algorithm is next executed. If the center of the current pixel of interest, YS = j x y, is less than Y (2), then the correlation logic described below is executed. If not, I is incremented, Z1 and Z2 are updated, Y(I + 1) is transformed, and the search procedure continues. If YS lies between Y (I) and Y (I + 1), then the search ends and the correlation logic described below is executed. If the current points don't bracket YS, then I is incremented again, unless the end of the elevation profile has been reached. In this case, a flag is set specifying that the rest of the current column of pixels should be imaged as 'sky', since no terrain within r_{max} will have a projection onto the current point or onto any higher pixel in the current column.

The qualitative description given above of the first component of the correlation algorithm may be symbolically coded as follows:

- 10 I = I + 1 IF (I.NE.P) GO TO 70 NFLAG = 1 RETURN
- 70 Z1 = Z2 Z2 = Y(I + 1) Y(I + 1) = PROJ(Y(I + 1))IF (Y(I + 1).GE.YS.AND.Y(I).LE.YS) Go to 20 GO TO 10



Assume that the above code has been successfully executed and that two points of a radial elevation profile have been found with projections bracketing the Y' value of the current pixel of interest. The remaining component of the algorithm needs to be executed, that is to find the coordinates of a point along the profile with a projection lying within the specified tolerance. TOL, of the pixel center YS. The iterative procedure for this will now be examined.

The iterative procedure used to find a terrain point between the known array positions Y(1) and Y(1 + 1) satisfying the tolerance criteria is based on two observations:

ſ

- 1. The terrain between the I^{th} and the $I + 1^{st}$ elevation data values Z1 and Z2 will be monotone (increasing or decreasing) if the resolution **r** is adequate.
- 2. An analytic solution to the problem of finding the point corresponding to YS exists for the case that the terrain is linear.

In the first observation, it is implied that a series of linear approximations to the terrain between the two data points will converge to a solution. In the second observation, a quick, analytic method is presented for predicting the position of a data point that will map onto YS, based on the linear approximations. By then accessing the predicted data points and evaluating the projection of the actual point in terms of the tolerance criteria, an easily developed iterative procedure will yield a suitable point.

The key to this portion of the algorithm is the ability to determine a point on a linear surface, the perspective projection of which will fall onto a predetermined point on the image plane. The X' coordinate of the point has already been determined from the radial profiles. Thus, the Y' coordinate is of concern. As above, let the Y' coordinate of the screen point of interest take the value YS. If, as shown in figure 14, it is known that two elevation points, ZU and ZL, are visible at distances from the observer of RL and RU, respectively, then the terrain between the two points may be modeled by the linear function

$$Z(R) = \frac{(ZU - ZL)}{(RU - RL)} (R - RL) + ZL$$
(62)



FIGURE 14. Concave Radial Profile.

After substituting this into the Y' equation of the perspective projection and solving for the R such that the projection of Z(R) is equal to YS, it is seen that

Carrier and the second second

in the

$$R = \frac{-hf + (ZL)\beta\gamma - [(ZU - ZL)(\beta\gamma (RL)/\Delta]}{[YS - Y\phi]\cos\theta - [(ZU - ZL)(\beta\gamma /\Delta]}$$
(63)

This predicted radius is then used to access the actual elevation at that point. The elevation is then projected, and if within the tolerance criteria, is a suitable point. This logic may be symbolically coded as

XI = XO + R*COS(THETA) YI = YO + R*SIN(THETA) CALL ALT(XI, YI, Z) YTRY = PROJ(Z) YERR = YTRY - YSIF(ABS(YERR).LE.TOL)) GO TO 30

where ALT is a FORTRAN-callable subroutine that will return elevation values (z) at specified points (x, y).

Two cases exist if the projection of the predicted point is outside of the tolerance bounds. These, corresponding to locally convex and concave terrain, respectively, are illustrated in figures 14 and 15.

Consider the concave case first. In this case, YERR = YTRY - YS is less than zero; the convex case corresponds to a positive value of YERR.

IF(YERR.GT.0) GO TO 40

This situation is illustrated in figure 14. It is clear that a new, more accurate linear approximation to the terrain may be achieved by substituting the value of z derived from the first prediction for the value of ZL, and correspondingly replacing the value of RL with the predicted radius.

$$ZP = ZU - Z$$

$$ZL = Z$$

$$RL = R$$

$$DELTA = RU - RL$$

$$GO TO 50$$

The program will then predict a new radius, as outlined above, and in successive approximations, will approximate the desired point with an arbitrary degree of accuracy.

The convex case is similarly simple (see figure 15). In this case, the upper point and radius are modified before proceeding to the next iteration of the algorithm. In a manner similar to that of the concave case, the logic may be symbolized by

$$ZP = Z - ZL$$

$$ZU = Z$$

$$RU = R$$

$$DELTA = RU - RL$$

$$GO TO 50$$



FIGURE 15. Convex Radial Profile.

Similar, successively more accurate approximations to the desired point will be made until a satisfactory point is found, i.e. until the projection of a predicted point lies within the tolerance interval of the point YS.

Once a satisfactory point is found, control returns to the main routine. To reduce redundant operation of the correlation routine, NFLAG, (the 'sky' flag noted above) one can pass the pointers to position in the elevation array and the last two elevation values to the main routine. Further, with the polynomial terrain data base, the orientation of the terrain may be determined at the same time that the predicted points are tested against the tolerance criteria. Consequently, the slope parameters described below are also passed to the main routine.

C. SLOPE DETERMINATION. In this section, the problem of determining the parameters necessary to calculate the brightness of the surface at an arbitrary point on that surface will be discussed. In particular, the brightness of the surface at points as determined by the algorithms of the previous section will be calculated. The actual calculation of the brightness of the terrain at our point of interest will not be discussed because it is conceptually and algorithmically better treated with the calculation of pixel density in the next section. From the previous algorithms, at a given point, the brightness of terrain obeying Lambert's law is a function of the cosine of the angle θ between the normal to the surface and the vector defining the incident radiation. Similarly, everything being equal, the brightness of terrain obeying the Lommel-Seeliger law is a function of $\cos\theta$, and the cosine of the angle *i* between the normal to the surface and the vector from the point under consideration to the observer. Thus, in this section the algorithmic determination of the normal to a surface for both discrete and polynomial terrain data bases will be discussed. In addition, the calculation of the cosine of the angle between this vector and some arbitrary vector as defined by a polar angle α and an azimuthal angle β will be presented.

1. Normal to a Surface. Having found a point on the surface of the terrain with a corresponding projection within the pixel of interest on the image plane, one's next task is to determine the orientation of the surface at that point. The most convenient way to define the orientation is by a unit vector that is normal to the surface at that point.

A two-dimensional surface can be defined by the equation

$$Z = Z(u, v) \tag{64}$$

where \mathbf{u} and \mathbf{v} are arbitrary curvilinear coordinates on the surface of the terrain. The normal-to-a-surface at a point is defined by the cross product of any two district vectors tangent to the surface at that point. This is clear since the vector defined by the cross product of two vectors is perpendicular to both of them. Two such vectors are defined by the partial derivatives of the function with respect to the two variables. Thus, the normal vector (not a unit vector) is given by

$$\vec{r} = \frac{\partial \vec{f}}{\partial u} X \frac{\partial \vec{f}}{\partial v}$$
 (65)

Generalized curvilinear coordinates are of little interest because most topographic data bases are defined by the usual orthogonal cartesian coordinate system. However, two algorithms are of interest at this point: (1) the generation of normals from a discrete elevation data base, and (2) the generation of normals directly from the coefficients of a polynomial terrain data base. Algorithms of both types were implemented in the FTL software.

a. Discrete Data Bases. First, consider an elevation data base composed of discrete elevation data points. No particular format will be assumed for these data points (see Yoeli*). Thus, the points may be found at the intersection of some orthogonal grid, maybe randomly distributed, or maybe composed of points selected on the basis of arbitrary criteria. Having dealt with the general case, one can simplify the results for the case of data points found at the nodes of a uniform orthogonal grid.

Let us consider three data points θ (x, y, z), a (x, y, z), and b (x, y, z), surrounding the point **P** at which we seek to find the normal. These three points define the local surface at this point. The boundaries of the surface can be defined by two vectors \vec{a} and \vec{b} , respectively, correcting the points ϵa and b to θ . Algebraically, these vectors are defined by

 $\vec{a} = a(x, y, z) - \theta(x, y, z)$ (66)

$$\vec{a} = (a_x - \theta_x, a_y - \theta_y, a_z - \theta_z)$$
(67)

and

$$\mathbf{b} = \mathbf{b}(\mathbf{x}, \mathbf{y}, \mathbf{z}) - \boldsymbol{\theta}(\mathbf{x}, \mathbf{y}, \mathbf{z})$$
(6.3)

$$\overline{\mathbf{b}} = (\mathbf{b}_{x} - \theta_{x}, \mathbf{b}_{y} - \theta_{y}, \mathbf{b}_{z} - \theta_{z})$$
 (6.)

Since the vectors \vec{a} and \vec{b} define the local boundaries of the surface around **P**, and are thus coplanar and hence tangent to the surface, then the (non-unit) normal vector at **P** is given by $\vec{n} = \vec{a} \times \vec{b}$ with components

$$\mathbf{n}_{\mathbf{x}} = \mathbf{a}_{\mathbf{y}} \mathbf{b}_{\mathbf{z}} - \mathbf{a}_{\mathbf{z}} \mathbf{b}_{\mathbf{y}} \tag{70}$$

$$\mathbf{n}_{\mathbf{y}} = \mathbf{a}_{\mathbf{z}} \mathbf{b}_{\mathbf{y}} - \mathbf{a}_{\mathbf{x}} \mathbf{b}_{\mathbf{z}} \tag{71}$$

$$\mathbf{n}_{\mathbf{z}} = \mathbf{a}_{\mathbf{x}} \mathbf{b}_{\mathbf{y}} - \mathbf{a}_{\mathbf{y}} \mathbf{b}_{\mathbf{x}}$$
(72)

*See footnote 26.

The length of $|\vec{n}|$ of \vec{n} is given by $\sqrt{(n_x^2 + n_y^2 + n_z^2)}$, and hence, \hat{n} , the unit normal vector is given by

$$\mathbf{n} = \mathbf{n}/\mathbf{n} \tag{73}$$

If the data base is composed of elevation data points found at the intersections of lines parallel to the X- and Y- axis and is uniformly spaced, then a simplification in the formula is possible, resulting in reduced computation times. If a lies on a vertical plane parallel to that defined by the Z- and X- axis and **b** lies on a vertical plane parallel to the Z- and Y- axes, then \vec{a} is given by $(a_x, 0, a_z)$ and \vec{b} is given by $(0, b_y, b_z)$. Thus, the normal vector is given by

$$\mathbf{n}_{\mathbf{x}} = -\mathbf{a}_{\mathbf{z}} \mathbf{b}_{\mathbf{y}} \tag{74}$$

$$\mathbf{n}_{\mathbf{v}} = -\mathbf{a}_{\mathbf{x}} \mathbf{b}_{\mathbf{z}} \tag{75}$$

$$\mathbf{n}_{\mathbf{z}} = \mathbf{a}_{\mathbf{x}} \mathbf{b}_{\mathbf{y}} \tag{76}$$

As a result, reductions will occur in the computations necessary to compute the cosine of the angle between a normal vector and any other vector.

The above formulas are somewhat arbitrary, because the information content of the data base is not used in an unbiased manner. Thus, if a pixel center is taken to coincide with a given point of a regular grid data base, the four nearest points are all equidistant and, hence, are of equal information content. The above equations use only two of these four points and, hence, are biased (see figure 16).

The easiest way of removing this bias is by shifting the pixel center to the center of one square of the grid of the data base and then using the mean of the slopes determined along the sides of the square. Hence, the Z -components of equations (66) and (67) may be re-defined as

$$a_{2} = 1/2 (Z_{2} - Z_{1} + Z_{4} - Z_{3})$$
 (77)

$$b_2 = 1/2 (Z_3 - Z_1 + Z_4 - Z_2)$$
 (78)

where the Z_i are as defined in figure 17. These formulas have been implemented in the ETL software.



FIGURE 16. Biased Use of Elevation Data Points.

Second Second States



FIGURE 17. Unbiased Use of Elevation Data.

b. Polynomial Data Bases. The problem of analytically determining the normal to a topographic surface at a point will be discussed for a terrain modeled by a polynomial data base of the type developed for ETL.²⁹

The elevations are defined as a function of position

$$Z(X, Y) = \sum_{i=1}^{4} Z_i(X, Y) W_i(X, Y)$$
(79)

where the $Z_i(X, Y)$ are the four partially overlapping polynomial functions locally defining the terrain around the point P(X, Y), and the $W_i(X, Y)$ are the four corresponding weight functions used to define the terrain in the overlap area.

The normal to the surface at the point P(X, Y) can be defined in terms of the two partial derivations, $\partial Z/\partial X$ and $\partial Z/\partial Y$, as outlined above. From straightforward applications,

$$\partial Z_{\partial X} = \sum_{i=1}^{4} (\partial Z_i(X, Y) / \partial X W_i(X, Y) + \partial W_i(X, Y) / \partial X Z_i(X, Y))$$
(80)

$$\partial Z/\partial Y = \sum_{i=1}^{4} (\partial Z_i(X, Y)/\partial Y W_i(X, Y) + \partial W_i(X, Y)/\partial Y Z_i(X, Y))$$
(81)

To use equations (80) and (81), one must have a vector representation in a form analagous to the vectors defined for the discrete data base. The best concept of this is to consider these tangent vectors as defining a plane tangent to the topographic surface at the point of interest. If \vec{a} describes $\partial Z/\partial X$ and \vec{b} describes $\partial Z/\partial Y$, then the vectors \vec{a} and \vec{b} can be defined by

$$\vec{a} = (1, 0, \frac{\partial Z}{\partial X}) \tag{82}$$

$$\vec{\mathbf{b}} = (0, 1, \frac{\partial Z}{\partial Y}) \tag{83}$$

²⁹J. Jancaitis and J. Junkins. *Mathematical Techniques for Automated Cartography*, U.S. Army Engineer Topographic Laboratories. Fort Belvoir, Virginia, UTL-CR-73-4, February 1973, AD-758–300,

remembering that \vec{a} and \vec{b} lie in vertical planes parallel to the X- and Y-axes, respectively. The normal, \vec{n} , is defined as above with

$$n_{x} = -\frac{\partial Z}{\partial X}$$
(84)

$$n_v = -\frac{\partial Z}{\partial Y}$$
(85)

$$n_z = 1$$
 (86)

$$n = n/|n| = n/\sqrt{(n_x^2 + n_y^2 + n_z^2)}$$
 (87)

2. Calculation Of Angles To A Normal. Next will be discussed the problem of determining the angle *i* between \vec{n} , the normal vector to our topographic surface at a point P, and determining some vector \vec{S} , with component S_x , S_y , and S_z . We shall define \vec{S} in terms of a polar angle φ , and an azimuthal angle θ (see figure 18). Then

$$S_x = \sin\varphi \,\cos\theta$$
 (88)

$$S_v = \sin\varphi \sin\theta$$
 (89)

$$S_z = \cos\varphi \tag{90}$$

Note: As defined, $\mathbf{\vec{S}}$ is a unit vector.

As noted above, our interest actually lies in the cosine of the angle between these two vectors. If the scalar product of two vectors is defined, then

$$\vec{S} \cdot \vec{n} = |\vec{s}| |\vec{n}| \cos i = S_x n_x + S_y n_y + S_z n_z$$
 (91)

where *i* is the angle between the two vectors. If \vec{S} is normalized, then, by equations (58) to (60)

$$\cos i = \vec{S} \cdot \vec{n} / (|\vec{s}| |\vec{n}|) \tag{92}$$

$$\cos i = S_x (a_y b_z - a_z b_z) + S_{\partial} (a_z b_x - a_x b_y) + S_z (a_x b_y - a_y b_x) / (a_y b_z - a_z b_y)^2 + (a_z b_x - a_x b_y)^2 + (a_x b_y - a_y b_x)^2$$
(93)





If, as outlined above, \vec{a} and \vec{b} fall into vertical planes parallel to the X- and Y-axes, respectively, then this formula is

$$\cos i = \frac{-S_x a_z b_y - S_y a_x b_z + S_z a_x b_y}{\sqrt{\{(a_z b_y)^2 + (a_x b_z)^2 + (a_x b_y)^2\}}}$$
(94)

where $a_y = 0$ and $b_x = 0$ for this case.

Further, if the components of the normal vector are calculated from the polynomial data base as in equations (84) and (85), then

$$\cos i = \frac{-S_x \frac{\partial Z}{\partial X} - S_y \frac{\partial Z}{\partial Y} + S_z}{\sqrt{(\partial Z/\partial X)^2 + (\partial Z/\partial Y)^2 + 1}}$$
(95)

It will be recalled that the Lommel-Seeliger law uses the viewing angle n_z , which is the angle between the normal to the surface and the unit ray \vec{V} to the observer, as well as the angle of illumination *i* between the unit ray \vec{V} to the sun \vec{S} and the normal to the surface. The general case follows equation (93) with the components of \vec{V} , replacing those of \vec{S} , and ϵ replaced *i*. Similar substitutions are held for equations (94) and (95). For the orthonormal view, equations (94) and (95) become

$$\cos i = \sqrt{\frac{V_z a_x b_y}{\sqrt{\left\{a_z^2 b_y^2 + a_y^2 b_z^2 + a_x^2 b_y^2\right\}}}}$$
(96)

and

ſ

$$\cos i = \sqrt{\frac{V_z}{(\partial Z/\partial X)^2 + (\partial Z/\partial Y)^2 + 1}}$$
(97)

where V_z is the Z-component of the unit ray from the point of interest to the observer.

D. DENSITY COMPUTATIONS. The current problem is to calculate the illumination of a pixel of the image plane, for either perspective or orthonormal projection of terrain obeying either Lambert's or the Lommel-Seeliger brightness law, for a given direction of illumination and a given observer location.

The position of a point on the terrain corresponding to the current pixel that we are processing and the normal to the surface at that point have already been determined. First, computation of lighting and viewing vectors as used in the ETL software will be defined. The vectors are then applied to the computation of the illumination of our pixel. Next, the density concept used the concept of density to define the properties of the pixel that was used to define the image produced on an output device will be introduced.

1. Definition and Calculation of Vectors of Observation and Illumination. First, the vector of illumination that describes the position of the sun relative to the terrain of interest will be defined. Algorithmically, the normal vector is needed in terms of its X-, Y-, and Z-components, in the (X, Y, Z) coordinate system of the object. An angular definition is sometimes easier to understand, specifying an altitude φ and an azimuth θ for the sun. Fortunately, a simple transformation is possible (see figure 19). The ETL data bases, as well as most others, can locally define the Y-coordinate of the terrain as pointing due north and the X-coordinate as pointing due east. Aeronautical convention fixes azimuth such that 0° is due north, or parallel to the Y-axis, and 90° is due east, or parallel to the X-axis. Altitude is defined such that 0° is parallel to the surface, and 90° points towards the zenith. Thus, if \vec{S} represents the vector pointing towards the sun, the transformation is

$$S_{x} = \cos\varphi \, \cos\theta' \tag{98}$$

$$S_{v} = \cos\varphi \, \sin\theta' \tag{99}$$

$$S_z = \sin\varphi \tag{100}$$

where we introduce the variable $\theta' = 90^\circ - \theta$.

Next, consider the definition of the unit vector of observation, $\vec{\mathbf{V}}$, pointing from the point of the surface that we are considering to the instrument of observation. This vector is important only for the Lommel-Seeliger law; it does not



FIGURE 19. Definition of Solar Vector.

have a role in the brightness of a surface as described by Lambert's law. Further, for the case of an orthonormal image of terrain obeying the Lommel-Seeliger law, this vector is always vertical, in accordance with the definition of an orthonormal image.

All that needs to be considered then is the calculation of $\vec{\mathbf{V}}$ for a perspective view, and this need only be done when a Lommel-Seeliger image is to be created. Consider a perspective image geometry as illustrated in figure 20. The focal point **P** is defined at some distance Z_0 above a point **Q** of the terrain. A vertical plane corresponding to the *i*th column of pixels is defined by requiring that it be a vertical plane containing \vec{PQ} and that it be positioned at an angle θ to the northerly vertical plane. From equation (58), θ can be defined in terms of a principle viewing direction θ_p specified by the user, and an angle θ_i relative to the principle direction. (figure 20). Thus,

$$\theta = \theta_{\rm p} + \theta_i \tag{101}$$

$$\theta_{\rm p}$$
 + tan⁻¹ $\left(\frac{i\Delta X}{\varphi}\right)$ (102)



FIGURE 20. Definition of V.

where $\triangle X$ is the incremental distance between columns of pixels on the image plane, *i* defines the current column of interest, and **f** is the distance between **P** and the image plane along the principle viewing direction.

Assume that point T (r, θ , Z) of the terrain is found, corresponding to the pixel of interest, where θ is as above, r is the distance from O to the projection of T onto the horizontal plane containing O, and Z is the elevation of T above this plane. Then the angle of altitude φ is defined by

$$\varphi = \tan^{-1} \left(\frac{Z_0 - Z}{r} \right)$$
(103)

Thus, the components of the perspective viewing vector $\vec{\mathbf{V}}$ for a given pixel of the perspective projection as defined in terms of previously determined quantities is

$$V_{x} = -\cos\varphi \sin\theta \tag{104}$$

$$V_{x} = -\cos\varphi \, \cos\theta \tag{105}$$

$$V_{\mu} = -\sin\varphi \tag{106}$$

Thus, the parameters necessary to compute the image illumination for the cases that are being considered have been defined.

2. Image Illumination Calculation. To calculate image illumination, one must use the light-scattering laws previously reviewed. In the ETL Software, the user may specify that the brightness of the terrain is to be modeled by either the Lommel-Seeliger law, $B = Eo b \sum (\alpha)/1 + \cos\theta/\cos i$, or by Lambert's law, $B = Eo \cos i$, where the variables are defined in appendix A.

First, normalize Eo; it is not a user defined parameter. Second, assume in the case of the Lommel-Seeliger law that $b\Sigma(\alpha)$ is constant for all α and that this factor drops out. Thus, in essence the light-scattering law is reduced to

$$3 = [1 + \cos\theta / \cos i]^{-1}$$
(107)

for the Lommel-Seeliger law and to

$$B = \cos i \tag{108}$$

for Lambert's law.

As mentioned in section II, D, the concern is with the illumination of an image element in an optical system, not with the brightness of the illuminating point as observed at the optical system. As approximated within the ETL Software, the relationship is one of proportion.

$$\langle E \rangle = \alpha B \tag{109}$$

where $\langle E \rangle$ is the illumination of our pixel, and **B** is the brightness of some point of the image found by the object-image correlation algorithm (see section III, **A**). The calculation for **B** is dependent only on the relevant angles, which are found by evaluating the slope at the object point by means of the appropriate algorithm (see section III, **B**), the position of the observer (for the Lommel-Seeliger case) based on equations (104) to (106), and the position of the sun as defined by equations (98) to (100). The angles are then used to determine the cosines of the relevant angles by the appropriate formula of the sequence (91) to (97). The cosines are then used to determine the brightness by which the illumination of the pixel is approximated (after normalization).

However, the quantity that is to be used to define the image to be produced is not illumination, rather it is the density of the image. Before specifying the relationship, the meaning of density must be explained.

Consider a piece of photographic film, with illumination Eo, normal to the surface of the film. Let us assume that the film has been exposed and developed and, hence, that some light will be absorbed. The change in illumination across an infinitesimal layer of the fill will be

$$dE = -bE dt$$
(110)

where **b** is the fraction of the light absorbed in passing a unit thickness, **E** is the illumination of the upper surface of the infinitesimal layer, and dt is the thickness of the layer. Integrating, we find that the illumination of the far side will be

$$E = Eoe^{-bt}$$
(111)

where t is the thickness of the film. If the film is designed for viewing from the front, then assuming that all light is reflected at the bottom of the film, it undergoes similar absorbtion in the second pass through the film and obeys Lambert's law upon striking the upper surface (as in a matte print). The brightness of the film will be given by

$$B = Eoe^{-2bt}$$
(112)

In any case, convention defines the image, not by the brightness or intensity, but by the density. The density, D, is proportional to the exponent of equations (111) or (112). Consider (111) and let

$$D' = \ln (E/E_0) = \ln (e^{-bt}) = -bt$$
 (113)

This is not the usual density, which is conventionally defined in terms of the \log_{10} and must be positive. The relation is given by

$$D = \log (Eo/E) = \log_{10} e^{+bt} = \alpha bt = \alpha 2D'$$
 (114)

where $\alpha = 1/\ln_{10}$. The term Eo/E is known as the opacity.

Since the intensity Eo in the ETL algorithm is normalized, the density D is defined as

$$D = \log_{10} (1/E)$$
(115)

where E is calculated as outlined above. Output devices have between 12 and 256 different discrete density values available, with the values linearly positioned between some minimum and maximum density values. Consequently, a density scaling factor is used in the ETL algorithms to take advantage of the latitude in densities offered by the output devices, storing each density value to an 8-bit byte.

Thus the analysis of the basic algorithms of the ETL shaded relief software is completed.

F. **GRAPHIC PRODUCTION.** The basic algorithms governing the pixelby-pixel generation of the shaded relief images have been described. The result of these algorithms, for a given pixel, is a number. The process of converting this number into a pixel of corresponding density at a given position relative to the other p(y) of the image remains to be discussed.

Three types of devices are available at FTL to generate gray-shade images: (1) line printers for low resolution "proofing" plots, (2) a VERSATEC raster plotter to generate moderate resolution digital half-tone images, and (3) an Electron Beam Recorder (EBR) to generate high resolution near-continuous tone images. The first two output devices require special algorithms to generate shaded relief images, and the third device directly accepts a file containing sequential rows. Since the software to generate line printer or VERSATEC graphics requires sequential processing similar to that of the EBR and since it may be derived to output a given image to any or all output devices, the product of the ETL shaded relief software is a disk file contouring the coded density data. Both tiles store -7 bits of data (densities $0-12^{-7}$) in 8-bit bytes. Each record represents one column of pixel, and successive records represent successive columns. For compability with the disk access routine DSKTRN used at ETL, the image files generated are of uniform size, 2048 bytes by 2048 records for the file LPPERDAT generated by the shaded perspective routine SHDPER, and 1024 bytes by 1024 records for the orthonormal shaded relief routine SSLPLP.

The line printer routine used was devised by P. Yoeli and uses multiple stikings to generate varying densities.^{3,4} The look-up table used for this algorithm is shown in table 1. The VI RSATEC halftoning software creates a digital halftone pattern, characterized by 33 halftone dots per inch.^{3,1} Using the EBR is described in the literature.^{3,2}

Since all the algorithms used are described in available literature, no additional discussion is necessary. It is clear, though, that the file generated by the FTL software can be used by any gray-shade graphics generation device with minimal trouble

³⁰P. Yoelf, "The mechanization of Analytic Hill Shading," Carto, J. (1967).

³¹R. Rosenthal. Private Communication. U.S. Army Engineer Topographic Laboratories, Fort Belvoir, Virginia, 3 July 1979.

³²Operation and Maintenance Manual for Cartosraphic FBR System, Image Graphics, Inc., under contract Ne-DAAG-53-75-(C-0221, 1976, pp.67-72,

TABLE 1. Line Printer Density Table.

| CHARACTERS | | | DENSITY |
|--------------|--------------|--------------|---------|
| 1st Printing | 2nd Printing | 3rd Printing | |
| | | | 0.00 |
| • | | | 0.07 |
| - | | | 0.10 |
| 1 | | | 0.12 |
| / | | | 0.15 |
| V | | | 0.19 |
| # | | | 0.22 |
| (.1 | | | 0.26 |
| U | r. | | 0.30 |
| А | / | | 0.35 |
| А | V | | 0.40 |
| А | (a. | | 0.46 |
| А | V | 1 | 0.52 |
| А | U | 4 | 0.60 |
| А | (a) | W | 0.70 |

ł.

Î
F. SPECIAL PURPOSE ALGORITHMS. As noted in the introduction to this section, a number of special-purpose algorithms devised to address specific cartographic problems have been implemented in the ETL shaded relief software. The algorithms enable the solar azimuth to be varied, thus enhancing the impression of terrain relief and delineating the ridge lines.^{3 3} Producing "relief contours" enables atmospheric haze to be simulated, thus providing the option of simulating an additional qualitative distance cue in the perspective images.

1. Variable Sun Angle Algorithms. A problem occurs when a single source of illumination is used to delineate similar terrain features in different orientations. This is as much a problem for aerial photography as it is for artifically generated orthonormal or perspective images. First, the problem will be analyzed, then the various alleviating procedures developed by cartographers in the past will be considered. Finally, the adaptations of procedures implemented in the ETL software, will be examined.

فاستعمله

The problems inherent in using a single source of illumination may be seen in figure 21, which depicts an idealized ridge illuminated by side lighting. The ridge slop facing the sun is illuminated, and the far slope is in shadow. The form of the terrain is clear to an observer if he is aware of the direction of illumination. Now consider a situation such as in figure 21(b), in which the illumination is parallel to the ridge line. In such a case, both sides of the ridge are equally bright, and no information as to the terrain form is available to the observer. It is clear that in an area with varied topography and illuminated by a single source of light, the form of the terrain is poorly delineated, with some features exaggerated and some washed out.

As noted in the introduction, the problems associated with depicting terrain form are not new. For sometime, cartographers have been manually shading contour maps to improve interpretation of the terrain features. A simple solution might be in the careful choice of the direction of lighting, thus optimizing the delineation of the terrain. However, a problem exists that prohibits such a solution. This is the problem of interpretation, which requires a near-intuitive knowledge of

³³P. Yoeli. "Die richtung des licht bei analytischen," Kartographische Nachrieten Guetersloh 17(1967), pp. 537-544.









light direction. Shaded relief images are usually treated as though lighting is from the top or upper left. Because of this treatment, cartographers usually use north-west lighting when producing shaded relief overlays for contour maps, thus preventing the choice of the lighting direction.

To overcome the problem, cartographers have developed the procedures of implicity varying the direction of the lighting to emphasize all major terrain features. The variation in lighting direction is around a principal direction defining northwest heating. Although cartographers manually prepare shaded relief overlays of contour maps, substantial progress has been made in automating the process. Although quite sophisticated, the present algorithms are largely experimental.³⁴ The algorithms used at 1.11 are relatively simple, created largely to demonstrate the capability.

Fig. FTL software is based on the variation of the azimuthal component of the illumination vector. Thus, the vertical component will not be considered in this discussion. North-west lighting will be used throughout, and algorithm will be based on the local orientation of the surface, as defined by the normal vector $\hat{\mathbf{n}}$. The azimuth of $\hat{\mathbf{n}}$ will be φ_{n} .

First, let us consider the case of ridges parallel to the principal direction of light **S** (see figure 23). The normals to the two faces of the ridge lie roughly in the second and fourth quadrants of the Cartesian plane. This is the case where the greatest variation will probably be needed, as this is an example in which the ridge would be washed out. Fo guide our development of an algorithm, we note that as the ridge is rotated from an orientation parallel to the Y-axis to an orientation parallel to the X-axis, take **b** gradually dims and face **a** gradually brightens. A corresponding change will be unif the illumination vector **S** is changed from a position parallel to the X-axis to a position parallel to the Y-axis. Thus, for normals in the second quadrant the "Twashout" effect can be prevented by defining the light vector components S_x , S_y by

$$(S_x = -1, S_y = 0) = 0 \le \varphi_p \le 45^\circ$$
 (110)

$$(S_{s} = 0, S_{c} = 1)$$
 $45^{2} - \varphi_{n}^{2} = 90^{2}$ (11^{-1})

³⁴K. Brassel - "A Model for Automatic Hill Shading," Am. Cart., 1(1974), pp. 15–27.



E

FIGURE 23. Variation of Solar Azimuth.

and by

$$(S_x = -1, S_y = 0)$$
 for $180^\circ < \varphi_n \le 225^\circ$ (118)

$$(S_x = 0, S_y = 1)$$
 for $225^\circ < \varphi_n < 270^\circ$ (119)

for normals in the fourth quadrant.

For areas in between, one would like a smooth transition between the two lighting vectors used in equations (116 - 119). This can be defined by the first quadrant

$$(S_x = -\cos\varphi_n, S_y = \sin\varphi_n) \quad 90^\circ < \varphi_n \le 180^\circ$$
 (120)

and for the second quadrant

$$(S_x = \cos\varphi_n, S_y = \sin\varphi_n) 270^\circ < \varphi_n \leq 360^\circ$$
 (121)

In practice, one would like more control over the variation in lighting direction. The ETL software enables the user to input the angular variation $Z\theta$ desired. The above formulas are altered accordingly. Thus, instead of the orthongonal lighting directions specified by equations (116 - 119),

$$[S_{x} = -\cos(135^{\circ} + \theta), S_{y} = \sin(135^{\circ} + \theta)], 325^{\circ} + \theta < \varphi_{n} \le 145^{\circ} (122)$$
$$[S_{x} = -\cos(135^{\circ} + \theta), S_{y} = \sin(135^{\circ} - \theta)], 145^{\circ} < \varphi_{n} \le 135^{\circ} - \theta (123)$$
$$[S_{x} = -\cos(135^{\circ} + \theta), S_{y} = \sin(135^{\circ} + \theta)], 135^{\circ} + \theta < \varphi_{n} \le 225^{\circ} (124)$$

and

k

ł

the second s

and the second second

$$[\mathbf{S}_{\mathbf{x}} = -\cos(135^\circ - \theta), \ \mathbf{S}_{\mathbf{y}} = \sin(135^\circ - \theta)], \ 225^\circ < \varphi_{\mathbf{n}} \le 325^\circ - \theta \quad (125)$$

Formulas (120 and 121) are unaltered, except that the ranges are modified in accordance with equation (122 - 125).

Determining the local illumination vector straight forward, and it calculated immediately after the normals are determined, as outlined. The local illumination vector is then used to determine the illumination of the local surface area and hence, the density of the image. 2. Relief Contours. Several attempts have been made to combine directly the quantitative properties of contours with the qualitative advantages offered by shaded relief images by creating an image of a contour terrace model. These attempts implicitly involve creating a "layer-cake" model of the terrain, with the elevation discontinuities corresponding to contour lines. This model is then illuminated, and shadows are east by the tier structure, which is then photographed. In practice, actual models are rarely created. Instead, an ingenious manual method developed by Kitiro Tanaka is used.^{3.5} Working from a contour map, one can trace the contours away from the assumed source of light, keeping the nib parallel to the light source. Thus, a variable width contour line results. For complete representation, a gray background is used, and contours facing the light are similarly inked in white. The result is a striking, if costly, representation of the terrain.

An alternative method of creating a map with the visual impact similar to that of Tanaka's method can be created using the software developed at ETL. The method uses the main orthonormal shaded relief routine, SSLPLP, but calculates slopes in a slightly different manner. Briefly, the relief contour option of program SSLPLP involves creating a square grid of quantized elevation data. The quantization interval is a user input parameter and corresponds to the contour interval of the image. The quantized elevation values are then used to calculate slope for each pixel center. The slopes are used to calculate image densities at each pixel position as in the usual method for creating a shaded relief overlay.

The calculation of the slopes is straightforward. Each pixel has a uniform size and is assumed to be square. Elevation data values are generated at the ground locations corresponding to the four corners of the pixel. Letting Z_{u1} be the Z-value of the upper left corner of the pixel. Z_{ur} be the elevation value of the upper right corner, and Z_{ii} and Z_{1r} be the corresponding lower elevation values, we have

$$\Delta \mathbf{Z} : \Delta \mathbf{X} = \frac{1}{2} \left(\mathbf{Z}_{ur} - \mathbf{Z}_{u1} + \mathbf{Z}_{lr} - \mathbf{Z}_{ii} \right) / \Delta \mathbf{X}$$
(126)

$$\Delta \mathbf{Z}_{1} \Delta \mathbf{Y} = -\frac{1}{2} \left(\mathbf{Z}_{u1} - \mathbf{Z}_{u1} + \mathbf{Z}_{u2} - \mathbf{Z}_{l2} \right) \Delta \mathbf{Y}$$
(127)

where $\triangle X = \triangle Y = \text{pixel size}$.

³⁵K. Linaka — The Orthographic Relief Method of Representing Topography on Maps," *Geogr. Rev.*, 40(1950), pp. 444-456.

Since elevation values are quantized, unless a corresponding contour line passes through a given pixel, all elevations for that pixel will thus be assigned the neutral background density corresponding to flat terrain. If a single contour line passes through a pixel, then the mean plane fit to the four points corresponding to the pixel can assume any of 24 different orientations. Since the resolution of the image created is variable, more than one contour line may pass through a pixel. Thus the number of orientations is correspondingly increased.

It should be noted that ca is point of a contour line will be assigned to some pixel and that the width of the contour line cannot be less than the size of the pixel. To maximize contrast, the ETL software alters the vertical exaggeration such that illumination of slopes facing the source of illumination is maximized. Since contour lines parallel to the direction of illumination will be of low contrast relative to the background, it is usually convenient to utilize the variable sun angle algorithm described in this report.

3. Simulation of Atmospheric Haze. A simple model to simulate one aspect of atmospheric haze has recently been proposed.³⁶ This model treats only the attenuation properties of such haze, predicting for uniform haze an exponential decay of the apparent luminous intensity of a surface element with increasing distance. This is certainly one aspect of such haze, but only in the case of highly absorbent haze (such as, perhaps, industrial smog) or when the haze is not actually imaged but shades the ground as do clouds. The most important prediction of this model is that, for thick haze, distant objects will appear very dark. This is not the case with most actual haze. Consider a moderately thick ground fog. Distant "objects" in such a fog approach a uniform, non-zero brightness. To model more accurately the effects of such haze, ETL personnel have developed a new model of atmospheric haze.

and a survey of a

³⁶W. Dungan, Jr. "A Terrain and Cloud Computer Image Generating Model," *Computer Graphics*, 13(1979), No. 2, p. 143.

Careful consideration of the physics of light scattering results in a more appropriate (though still approximate) model of haze. Consider a thin slice of the atmosphere of thickness dr, measured along a radial to an observer. Fog or haze in this atmospheric section can be modeled as a collection of small randomly distributed particles with a cross section σ , and brightness b, with a density of n such particles per unit volume. The attenuation of a light beam traversing this section of the atmosphere along the radial to the observer will be

$$dE = -En\sigma dr \tag{128}$$

where E is the luminous intensity of the beam.

If the sun or other source of illumination shines upon the slice, then there will be an additional term to the expression for the attenuation of a beam traversing the ground haze. This term, expressing the fraction of the incident sunlight that is scattered into the beam, will be proprotional to $bE_sn\sigma$, where E_s is the luminous intensity of the source of illumination. Detailed analysis of the situation requires that the scattering be calculated in terms of illumination of an imaging element, considering the area of the light sensitive element, the size of the light acceptance cone of it, and the distance of a given scattering section of the atmosphere from the element. However, the net result of these considerations is a constant factor. It is thus convenient to lump this constant together with the brightness, b, in a new constant, C.

The differential equation governing the propagation of light through a ground fog, along a path roughly parallel to the surface of the earth is

$$dE = (-En\sigma + CEn\sigma) dr$$
(129)

Integration yields the solution

$$E(\mathbf{r}) = \exp(-\mathbf{r}\mathbf{n}\sigma) \left[CE_{s} \left\{ \exp(\mathbf{r}\mathbf{n}\sigma) \right\} + \mathbf{K} \right]$$
(130)

where \mathbf{K} is a constant of integration. Two boundary conditions must be satisfied by this constant of integration if the result is to be physically meaningful. These boundary conditions are

- 1. $E(r) \rightarrow E_0$ as $n\sigma \rightarrow 0$, where E_0 is the brightness of some object in the distance; and
- 2. $E(r) \rightarrow CE_s$ as $n\sigma \rightarrow \infty$ or as $r \rightarrow \infty$.

The first of these conditions corresponds to the physical situation of clean air, in which distant objects should be unobscured. The second boundary condition requires that the model of haze results in a uniform, finite brightness as the thickness of the haze increases. Both of these boundary conditions are satisfied by choosing

$$K = E_0 - CE_s$$
(131)

Thus, the model of haze implemented at ETL takes the form

$$E(r) = CE_s + (E_{\alpha} - CE_s) \exp(-rn\sigma)$$
(132)

By applying the Tyndall effect to this formula, the effect of atmospheric haze on the appearance of distant objects can be simulated. The Tyndall effect notes that very small objects, such as suspended dust, will scatter blue light much more than they will red. Thus, red light will pass through such a medium without appreciable change in intensity, and most blue light will be scattered. In color-shaded relief displays, the bluish-purple cast of distant mountains may be simulated by generating unattenuated shaded relief images for all colors, except blue or purple. In these image components, the above model for haze will be used. The result should be a moderately bright, relatively uniform, bluish tint of low contrast over distant objects.

From the above model of atmospheric haze, the effects of such haze can be more accurately predicted than with previous models. Although only slightly more complicated in form, this model should provide much more qualitative information to the viewer of a shaded relief image. As such, the model should ease the problem of interpreting such images. In particular, the bluish-purple cast of distant mountains can be accurately modeled, thus providing subtle distance clues otherwise unavailable. This will enable the accurate generation of color-shaded relief images. The algorithms discussed in this report have been coded in two FORTRAN routines. One set of routines, named SSLPLP, generates orthonormal shaded relief

IV. IMPLEMENTATION AND RESULTS

images; and the other, named SHDPER, generates perspective shaded relief images. To test the algorithms and software that have been developed, the two routines use an elevation/slope computation sub-

routine. ALSEP, that is "hardwired" to a polynomial terrain data base of Cache. Okla. In this section, the results of these tests are discussed.

A. PERSPECTIVE SHADED RELIEF ALGORITHMS. In this section, the results will be described of the implementation of the true-perspective algorithms in the shaded relief routines SHDPER. Running on a PDP-11/45 minicomputer, one can create a shaded relief perspective image SHDPER in a multi-user environment in approximately 5 milliseconds per pixel of clock time. The image is subject to enormous variation, dependent on viewing parameters, machine utilization, and control parameters. The user of the SHDPER routines can

- 1. Specify viewer location.
- 2. Specify imaging geometry.
- 3. Specify image resolution.
- 4. Specify the terrain viewed.
- 5. Specify a vertical exaggeration.
- 6. Define the position of the sun.
- 7. Enable local variation solar azimuth within user specified boundaries.
- 8. Choose between the Lommel-Seeliger law and Lambert's law to define terrain brightness.
- 9. Define the density scaling.
- 10. Specify program control parameters affecting processing efficiency.
- 11. Simulate the effects of atmospheric haze.

The program generates

- 1. Diagnostic output.
- 2. A DSKTRN-callable disk file of coded pixel densities.
- 3. Low resolution line printer plots.

Sample outputs demonstrating these capabilities are shown in figures C1 through C15. These images are each composed of 700,000 pixel (700 pixels by 1000 columns). The disk files containing the image density data were processed using ETL-modified VFRSAPLOT Software. To prevent the generation of overly dark, estimated by displeasing, halftone images, only $\frac{1}{2}$ of the available density latitude of the VERSAPLOT software has been used. This was done at the expense of some loss of tone continuity.

The images contained in appendix C are largely self-explanatory. The first image may be considered standard. In succeeding images, the effect of varying a single parameter at a time is demonstrated. The effect of changing the observer's altitude, the focal length of the imagery system, solar elevation, and solar azimuth are successive displayed. The effects of a very light ground haze are next portrayed. In figure C11, the effects of degrading resolution and displayed, which is a 128 by 179 pixel image that has been magnified by bilinear interpolation. Figures C12 and C13 are views of two different areas using the same image parameters that were used for the first image. Figure C14 is a view of the same area seen in the preceeding one, but this image is degraded by a moderate haze. The final image, figure C15, shows the parameters of the first image, but with the local variation of solar azimuth to enhance terrain features. No perspective image was included that illustrated the Lommel-Seeliger law. No satisfactory parameters have been found for such an image.

No attempt was made in coding to optimize the speed and efficiency of SHDPER. Tests on the ETL PDP-11/45, using the parameters of figure C1, indicate that approximately 4.8 milliseconds of clock time are required to process each pixel. This value may be strongly influenced by the parameters governing image generation. In particular, the dependence of execution time upon the sampling density has been investigated for the first image. The relationship is roughly linear, and, for a D (depth of view) of 7.4 map sheet inches (18.8 cm), the total execution time for this image may be estimated by

$$T (clockminutes) = 40 + .031 NPTS$$
 (133)

where NPTS is the number of sample elevation data points generated along the radial elevation profile. This formula should not be considered to be generally applicable, and may not be valid for NPTS ≤ 200 .

79

B. ORTHONORMAL SHADED RELIEF ALGORITHMS. In this section, the implementation of the orthonormal shaded relief in the program SSLPLP is discussed. From these routines, an orthonormal shaded relief image is produced that is defined by various input paramters from a polynomial terrain model. When the routines are run on the ETL PDP-11/45 computer, one can produce an image in approximately 3.3 milliseconds per pixel. However, the image is subject to variations as noted in the introduction to the SHDPER routines.

The user of the SSLPLP routines can

7

- 1. Specify the area to imaged.
- 2. Specify the resolution of the image.
- 3. Specify the vertical scaling factor for the terrain.
- 4. Specify the shading law to be used to model the terrain.
- 5. Specify the position of the "sun".
- 6. Define a variation in solar position to highlight terrain features.

From the routines one can generate

- 1. Diagnostic output.
- 2. A DSKTRN Callable disk file of coded pixel densities,
- 3. Low resolution line printer plots.

For sample outputs demonstrating these capabilities, see figures C10 through C21. As with the perspective images, the examples were generated from disk files containing coded image density data by the ETL-modified VERSAPLOT software. The exception of figure C20 must be noted, since this image was generated by means of a half-tone argorithm developed by R. Rosenthal of ETL.³⁷

C. P. 2010 Construction, J. S. Anny Engineer Topographic Laboratories, Fort Belvoir, Virginia,

The orthonormal images contained in figures C10 through C22 should be easy to interpret. Figure C16, which might be considered a "standard." is an orthonormal view of much of the terrain seen in the first perspective image (the perspective view is from the left of the orthonormal image, looking across the orthonormal view): the image contours 600 by 900 pixels. The second orthonormal image uses the same variation of solar azimuth used in the corresponding perspective view (figure C15). Figure C18 is the same image, upon which contour lines generated by the program SIMCON³⁸ have been overlaid by ETL-developed software.³⁹ The next two images illustrate the relief contour option of SSLPLP, with and without local variation of solar azimuth (figures C19 and C20). These two figures display a portion of the area of the previous orthonormal images. The final orthonormal image illustrates the use of the Lommel–Seeliger law (figure C21). The image is dark and of very low contrast.

As with the perspective software, no attempt was made in coding to optimize the speed and efficiency of SSLPLP. From test runs, the execution time is approximately 3.3 milliseconds per pixel for images some 540,000 pixels. This time shouldn't vary appreciably with any variation of parameters, but no extensive tests of this have been made.*

^{*}The algorithms decribed in this report have been substantially improved since the first draft of this report. A modified GRNDP1 routine has reduced execution times to an average of 40 percent of the above figures. A further modification, exploiting the redundant processing of previous approaches, has reduced execution times by an additional factor DF \simeq 2.5.

³⁸J. Jancaitis, Modeling and Contouring Surfaces Subject to Constraints, University of Virginia, U.S. Army Engineer Topographic Laboratories, Fort Belvoir, Virginia, ETL-CR-74-19, January 1975, AD-A010 406, pp. 163-165.

³⁹R. Rosenthal. User's Guide to MERGF. U.S. Army Engineer Topographic Laboratories, Fort Belvoir, Virginia, to be published.

The problems associated with generating shaded relief images have been systemtically investigated. Also, the theory of the formation of gray shade images by optical

V. DISCUSSION see

systems have been investigated, as has the theory of the scattering of light by solid surfaces with mathematical models having been successfully developed. The theoretical

conclusions of this investigation have been used to develop a series of algorithms for the efficient generation of a wide variety of shaded relief images. Special algorithms designed to address the specific cartographic problems of enhancing terrain features, modeling haze, and generating relief contours have also been developed. These algorithms have been implemented in two sets of FORTRAN routines: SHDPER, to generate shaded perspective images; and SSLPLP, to generate orthonormal shaded relief images and relief contours. These programs have been tested using a polynomial terrain data base of the Cache, Okla. The images that have been generated demonstrate the feasibility, economy, and promise that shaded relief images hold for future cartographic applications and for tailored specific user need (see tables 2 - 6).

It is concluded that:

VI. CONCLUSIONS

1. This effort has resulted in versatile and efficient shaded relief software that can now serve as the basis for future studies into terrain data user special requirements and needs. 2. More work is needed

in two main areas, improved presentation and product use studies. 3. The improved presentation should include color CRT and incorporate non-hypsometric terrain data.

TABLE 2. SHDPER FTN

Function/Source Code Correlation

| Description of Program Function | Compilation Lin | e Number |
|---|---------------------|----------|
| Overhead | 1 - 2 | 6 |
| Interactive Parameter Entry | 27 - 4 | 2 |
| Parameter Computation | 45 - 8 | 4 |
| Loop Over Columns of Image | 85 - 1 | 53 |
| Calculation of Radial Profile (CALL P | ΓS) 86 - 9 | 9 |
| Calculation of Densities of Current Column of Pixels | 100 - 1 | 45 |
| Determination (CALL GRNDP1, CALI Object/Image Point Correlation/Slop | LALT) De 110 - 1 | 15 |
| Density Computation | 116 - 1 | 45 |
| Write to Disk File | 146 - 1 | 53 |
| Write to Line Printer (If appropriate) | 154 - 1 | 62 |
| Overhead | 163 - 1 | 7 7 |

4

1 1

Èi

All and are about the second second

TABLE 3. ALSLP.FTN

والمتحافة والمعادية والتعريق والمتكادر

Function/Source Code Correlation

| | 1 vuilloci |
|--------|---|
| 1 – 1 | 3 |
| 14 - 3 | 32 |
| 33 - 5 | 53 |
| 54 – 6 | 57 |
| 68 - 7 | '6 |
| 77 – 8 | 33 |
| 84 - 9 | 2 |
| 92 - 9 | 98 |
| 00 - 1 | 11 |
| | 1 - 1 $14 - 3$ $33 - 5$ $54 - 6$ $68 - 7$ $77 - 8$ $84 - 9$ $92 - 9$ $00 - 1$ |

TABLE 4. Outline of GRNDPT Source Code Function

| Function | Compilation Line Numbers |
|--|--------------------------|
| Initilize Flags, Overhead | 1 - 13 |
| $Y(1) < Y_s (Y(1 + 1))?$ | 14 - 23 |
| Calculate 1st iteration parameters | 24 - 40 |
| Calculate projection of algorithmically determined point | 41 - 44 |
| Set parameters for next iteration, if needed | 45 - 59 |
| Return | 62 - 63 |

| | TABLE | 5. | The Angula as a H | nr Widt Functio | th of the on of DI | e Image S | |
|---------|-------|----|----------------------|--------------------|-----------------------|--------------|-------|
| DIS (") | | | | Total | Angular | Width of | Image |
| 4. | | | | | | 122° | |
| 6. | | | | | | 101° | |
| 8. | | | | | | 84° | |
| 10. | | | | | | 72 | |
| 12. | | | | | | 62° | |
| 14. | | | | | | 55° | |
| 16. | | | | | | 49° | |
| 18. | | | | | | 44° | |
| 20. | | | | | | 40° | |
| 24. | | | | | | 34° | |
| 30. | | | | | | 27° | |

TABLE 6. SSLPLP.FTN

Function/Source Code Correlation

ومراجع والمراجع

| Description of Function | Compilation Line Number |
|---|-------------------------|
| Overhead | 1 - 25 |
| Interactive Parameter Entry | 26 - 55 |
| Parameter Computation | 56 - 97 |
| Loop Over Rows of Image | 98 - 148 |
| Calculation of Slopes for row (CALL SLPS |) 101 - 110 |
| Calculation of Densities: Lambert's Law | 105 - 120 |
| Calculation of Densities: Lommel-Seeliger | Law 122 - 139 |
| Write Densities to Disk File | 144 - 147 |
| Write to Line Printer (If appropriate) (CALL LP) | 149 - 158 |
| Overhead | 159 - 169 |

1. Theoretical Details. Lambert's law is a scattering law that is an idealization of empirical evidence. As noted in this report, no good derviation of Lambert's law

APPENDIX A. has two components, just as Lambert's law may be thought of as having two com-

ponents:

- 1. The brightness of a surface obeying Lambert's law is independent of the direction of view.
- 2. The brightness of such a surface is proportional to the cosine of the angle between the vector of illumination and the normal to the surface.

The first component of Lambert's law accurately describes the functional dependence of brightness of self-luminous objects as well as that of some reflecting bodies. Consequently, the derivation given below first postulates a model for the microscopic structure of a self-luminous medium, and then shows that the surface of a body described by this model will be of constant brightness, regardless of the orientation of the surface to an observer.

The derivation of the second component of Lambert's law is not satisfactory. In essence, this portion of the derivation is an attempt to justify the third assumption given below about self-luminous bodies for illuminated reflecting bodies. This attempt is not successful in a rigorous mathematical sense, but is included for completeness of this appendix. It must be noted that this attempt is the author's: better "derivations" may exist, but they are not known to the author at the time of writing.

First, the variables involved in the derivation will be defined. As can be seen in figure A1, the system modeled might be used to measure the brightness of the surface **S**. These measurements would be based on the determination of the total flux of radiant energy incident upon the light-sensitive area, φ , of a photodetector. This detector has a light acceptance cone of width dw, the center of which is inclined at an angle θ to the normal to the surface **S**. The distance of the detector from the surface is **R**, measured along a ray within the detector acceptance cone, and the corresponding distance to some volume element dV is **r**, located a distance $z = (\mathbf{r} - \mathbf{R})\cos\theta$ below the surface.



A derivation such as this must be motivated by empirical evidence. If selfluminous bodies obey the first aspect of Lambert's law, then the body with surface S will be first modeled as a homogeneous, self-luminous medium. These assumptions can be easily modified to treat non-radiant bodies that are accurately modeled by Lambert's law, as will be discussed. The medium presently being considered is characterized by three features:

- 1. Each infinitesimal volume element radiates equally in all directions.
- 2. A ray of light has a mean free path of length before being absorbed or re-scattered, and thus lost to a given beam.
- 3. All volume elements are equally luminous, with luminosity per volume \mathbf{I}_{α} .

It is a well known result of statistical mechanics that a beam of light characterized by flux \mathbf{F} will, in such a medium, be attenuated by a factor of \mathbf{dF} in traversing a distance \mathbf{dx} , such that

$$dF = -F(1/\tau) \, dx \tag{134}$$

Thus, a beam of initial intensity \mathbf{F}_0 will be of intensity $\mathbf{F}(\mathbf{x})$ after traversing a distance \mathbf{x} , such that

$$\Gamma = \int_{0}^{x} dF = F_{0} e^{x/\tau}$$
(135)

Consider now a volume element a distance z beneath the surface. A light riv emitted from this element towards the detector will traverse a path of length $x = (r - R) - z \sec\theta$ before emerging from the surface. Now, $F_{\sigma} = I_{\sigma} - dV d\Omega$, where in this case, I_{σ} is the luminosity per unit volume, dV is the differential volume element, and $d\Omega$ is the solid angle subtended by the detector at the volume element. Hence, the differential flux incident upon the detector from this volume element will be

$$d\mathbf{F} = \mathbf{I} \cdot d\mathbf{V} \, d\Omega \, e^{i(\tau - \mathbf{R})} \, \boldsymbol{\tau}$$
(136)

To find the total flux of radiant energy upon the detector, one must integrate all the volume elements within the detector acceptance cone dW. Hence,

$$F = dF = \int_{r=R}^{\infty} I_{o} e^{-(r-R)/\tau} dV d\Omega$$
(137)

Now, $d\Omega = a/r^2$, and $dV = r^2 dW dr$. Hence,

$$F = \int_{r=R}^{\infty} I_{0} (a/r^{2})r^{2} dW e^{-(\tau - R)/\tau} dr$$
$$= \int_{r=R}^{\infty} I_{0} a dW e^{-(\tau - R)/\tau} dr$$
$$= I_{0} a dW \tau \qquad (138)$$

Thus, the flux received by a detector is independent of the inclination of the detector to the surface (i.e. independent of θ), if all else is held constant. The apparent surface is a function of angle

$$d\mathbf{A} = -\mathbf{R}^2 \, d\mathbf{W}(\cos(\theta)) \tag{139}$$

The solid angle that the light subtends is approximately constant:

$$\mathrm{d}\Omega = a_0 \mathrm{r}^2 \simeq a_0 \mathrm{R}^2 \tag{140}$$

This is a valid approximation, if $|\mathbf{R}| \gg \tau$, since all light emerging from the surface effectively emerged from a radius $|\mathbf{r}| \leq (\mathbf{R} + 10\gamma) \approx |\mathbf{R}|$. This follows from the exponential decay of the emerging flux: less than $|1\rangle$ of the emerging light traverses a distance of more than -10τ . Having made this approximation, one can keep the brightness of the surface constant:

$$B = \frac{F}{dA \cos\theta \ d\Omega}$$

= $F[[R^2 (dW \cos\theta) \cos\theta (a R^2)]]$
= $F[(a dW)]$
= $I_0 \tau$ (14)

)

The brightness of a surface obeying lambert's law is defined as being independent of the direction from which it is viewed, which is the case of the surface of the body just modeled. The first aspect of Lambert's law has thus been derived from microscopic considerations for a self-luminous body, in a form relating the brightness of the surface of the body to the flux incident upon a photodetector.

To complete a derivation of Lambert's law, one must justify the third assumption tion for reflecting bodies. This can only be done by making an additional assumption about the microscopic structure of such bodies. In particular, reflecting bodies that obey Lambert's law are composed of miscroscopic particles, each of which is

1. Non-absorbing.

2. Defuses light uniformly in all directions.

It must be shown that these assumptions lead to the following conclusions: In a semi-infinite body which may be modeled by these assumptions, (1) the intensity of the light with the body is everywhere constant, and (2) the intensity of the light is proportional to the cosine of the angle incidence of the incoming light.

First, examine a differential volume element dV a depth Z below the surface (see figure A1). By showing that the net flux upon this volume element is independent of Z, one assumption can be justified. Considerations of flux out (which, since no absorbtion is assumed, must equal flux in), will define the value of the constant.

The flux upon the volume element can be defined as an integral with two components; the flux of the incident light reaching volume element from the surface, and the flux scattered from the rest of the body. This incident light is assured to be of intensity \mathbf{E}_{α} above the surface and incident at an angle to the normal to the surface. By analysis similar to that above, the fraction of the incident light reaching $d\mathbf{V}$ will be

$$E_{Lonto} = \pi E_0 \Delta^2 e^{-Z \sec i/\tau}$$
(142)

where it has been assumed that the volume element is spherical and has a radius $\triangle (dV - 4\pi/3) \triangle^3$: $dA = \pi \triangle^2$). Of this, a fraction $\triangle/3\tau$ will be scattered. Thus, F_{out} of this fraction is

$$E_{1 \text{ out}} = \frac{\pi}{3\tau} E_0 \Delta^3 e^{-Z \sec(t)\tau}$$
(143)

The contribution from scattered light from the rest of the body must now be considered. Here the differential contribution for a volume element $d\mathbf{V}^t$ of luminous intensity \mathbf{I}_0 (assured constant, we must find \mathbf{I}_0 in terms of \mathbf{E}_0 and *i*) at a distance **r** will be

$$dF_{2 \text{ out}} = I_0 \frac{\pi \Delta^2}{r^2} e^{r/\tau} dV^{\tau}$$
(144)

where $\pi \Delta^2/r$ represents the solid angle subtended by dV at α . As above, a fraction of $\Delta/3\tau$ of this flux will be scattered. Flus,

$$dF_{out} = I_o \frac{\pi \Delta^3}{3\tau r^2} = e^{-t/\tau} dV^t$$
(145)

This must be integrated over the volume of the body. Since the surface deliniates the body, the limits of integration are:

$$F_{2,\text{out}} = \int_{\tau=0}^{\infty} \int_{-\varphi=0}^{2\pi} \int_{0}^{0} \frac{1}{\tau_{2}} \int_{0}^{0} \frac{\pi \Delta^{3}}{3\tau^{2}\tau} e^{\tau/\tau} dV'$$

+
$$\int_{0}^{2} \frac{8\pi \varphi}{2\tau} \int_{0}^{2\pi} \int_{0}^{\pi/2} \frac{\pi}{\tau_{2}} \int_{0}^{\pi/2} \frac{\pi \Delta^{3}}{3\tau^{2}\tau} e^{\tau/\tau} dV' (14\pi)$$

where, in spherical polar coordinates,

$$dV' = r^2 \sin\theta \, dr \, d\theta \, d\varphi \tag{14.1}$$

The first term can be readily integrated by standard techniques. The second cannot ite evaluated in closed form; hence, approximations must be resorted to if it is to be evaluated. This alone precludes the success of the approach, since in the absence of a closed form representation, it cannot be shown that the result will contain a term negating the Z dependence of F_1 . Strict limits can be placed on the Z dependence of F_1 , but these are not adsequate. They are inconsistent with the assumptions necessary for the derivation of the first. "aspect" of Lambert's law. Consequently, this "derivation" must be considered unsuccessful.

2. The Lommel-Seeliger Law. The Lommel-Seeliger law is a scattering law derived from realistic physical assumptions about the microscopic structure of a scattering medium. From this law, accurate predictions can be made about the light-scattering behavior of many natural surfaces. In particular, a scattering surface is assumed to be apparent and that it is actually the surface of a material body composed of many small, uniform scattering bodies. It is also assumed that the interaction of light with the body is amenable to statistical analysis.

The present derivation of the Lommel-Seeliger law is an extension of the treatment given by Hapke.⁴⁰ Since the derivation assumptions about the nature of the scattering body are. Explicit, the approach is representative of a large class of similar theoretical laws and is included as a detailed examination of one of these laws. As noted in the beginning of this section, the Lommel-Seeliger law was selected for the simplicity of its final mathamatical form and theoretical basis and for its ability to predict accurately the light-scattering properties of a variety of surfaces.

The following variables are used in the discussion that follows (see figure A1).

Definition of Variables

| n | = | mean number of scattering objects per unit volume: |
|------------------|---|--|
| σ | = | average cross section of a scattering object; |
| γ | = | mean free path of a beam of light rays in the medium. We shall assume that $\gamma = 1/n\sigma$ is always a good approximation. |
| b | = | total reflectivity of a scattering object. Hence, $(1 - b)$ is equivalent to the fraction of light incident on a scattering object which is absorbed. |
| i | = | the angle of the incident light with respect to the normal to the apparent surface: |
| α | = | angle between the rays of incidence and reflection: |
| θ | = | angle of the ray reflected towards the detector with the normal to the apparent surface; |
| dΩ | = | solid angle subtended by the detector at the surface: |
| a | | light-sensitive area of the detector: |
| R | = | distance of the detector from the apparent surface, measured along the path of the reflected ray $(d\Omega \approx a/R^2)$; |
| dW | = | solid angle of the acceptance cone of the detector; |
| \mathbf{E}_{0} | = | incident intensity (flux of radiant energy per unit area normal to the direction of incidence); and |
| Σ(α) | = | scattering law of an individual object. Of the light reflected, $\Sigma(\alpha)$ is that fraction of the incident light from a unit solid angle about the source reflected into the unit solid angle about the direction of observation. $\Sigma(\alpha)$ is normalized so that $\int_{4\pi} \Sigma(\alpha) d\Omega = 1$. |

⁴⁰B. Hapke, J. Geophys. Res. 68(1963), p. 4575.

Consider the fraction of radiation incident upon the apparent surface reaching a volume element $dV = r^2 dW$ at some distance $Z = (r - R) \cos\theta$ below the apparent surface. If the radiation is incident at an angle *i* to the normal to the apparent surface, then the distance traversed by the ray will be

$$Z' = Z/\cos i = Z \operatorname{Sec} i \tag{148}$$

The fractional change in the flux incident upon an infinitesimal volume element of the scattering material of thickness dZ' (measured along the path of the incident ray), owing to scattering or absorption within the differential volume element, will be

$$dE = -E' n\sigma dZ'$$
(149)

Hence,

$$E(Z') = E_0 e^{-n\sigma Z'}$$
(150)

and

$$E(Z) = E_0 e^{-n\sigma Z - Seci} = E_0 e^{-(Z - Seci)/\tau}$$
(151)

The light reaching the detector is the light within the detector acceptance cone, dW. This light may be interpreted as being reflected from the apparent surface area $dA = R^2 dW/\cos\theta$.

Consider the volume element dV a distance Z below the apparent surface. As above, the light intensity at the dV will be

$$E(Z) = E_{o} e^{(Z - Seci)/\tau}$$
(152)

Now, determine the differential flux incident upon the detector owing to scattering within this volume element. First, not all light incident upon the volume element will be reflected. Instead, only the light incident upon the surface area $dS = n\sigma dV$ of the scatterers within the volume will be available for reflection. Of this, only a fraction **b** will be reflected. The detector is located at an angle α to the radiation incident on the scatters; $\Sigma(\alpha)$ of the total reflected radiation will fall within a unit solid angle around the detector. However, the detector doesn't subtend a unit solid angle. It subtends a fraction $d\Omega = a/r^2$ of a unit solid angle. The product of these factors represents the flux incident upon the detector:

| AD-A1 | 101 422 | ARMY SHAD APR | ENGINE ED RELI 81 C C | ER TOP | OGRAPHI Ges for R | C LABS | FORT B GRAPHIC | ELVOIR APPLIC | VA ATIONS | . (U) | F/6 | 8/2 | |
|-----------------------|------------|---------------------|-----------------------------|----------|-------------------------|--------|-------------------|------------------|--------------|-------|--------|--------|--|
| UNCL/ | 2 3 | ETL- | 0259 | | | | | | | | NL. | | |
| | ADC1437 | | | | | | | | | | | | |
| | | | | | | | | | | | | - 1 | |
| t | | | | 朔 | ţ. | | | <u> </u> | | | メ 語 | | |
| 5). . x | | | | | | | | | | | | | |
| | | | | | | | | | | | | | |
| | | | | | | | | | | | | | |
| | | | | | | | | | | | | | |
| | | | | | | | | | | | | | |

$$dF = e_0 \left(\frac{\alpha}{r^2} \right) + b \sum \left(\alpha \right) n\sigma e^{i\left(\frac{z}{2} - S e c_i \right) - \tau} dV$$
(153)

Assume that the light reflected towards the detector will be further attenuated by a factor of $\exp[(-Z \operatorname{Sec}\theta) \gamma]$ before emerging from the apparent surface, since it must again pass through the scattering body. Hence, the flux of radiant energy reflected from the volume element dV and emerging from the surface will be the product of equation (173) and the new attenuation factor. Thus,

$$dV = V_{0} (a_{1}r^{2}) b \sum(\alpha) n\sigma e^{i(Z/Sect)\tau} e^{i(Z/Sec\theta)^{2}\tau} dV$$
$$= V_{0} n\sigma a b \sum(\alpha) exp[-(r-R)(1 + \cos\theta/\cos i)^{2}\tau] dr dW (154)$$
$$w = Z = (r - R) cs\theta \text{ and } dV = r^{2} dW dr has have used.$$

where the identities $Z = (r - R)\cos\theta$ and $dV = r^2 dW dr$ has been used.

Thus, the total flux of radiant energy falling upon the detector within the detector acceptance cone dW will be found by integrating the differential flux from each $dV = r^2 dW dr$ within the acceptance cone dW; i.e. by integrating over all r greater than R:

$$\mathbf{F} = \int_{|\mathbf{r}| = |\mathbf{R}|}^{\mathbf{r}} d\mathbf{F}$$

$$= \int_{|\mathbf{r}| = |\mathbf{R}|}^{\mathbf{r}} \mathbf{F}_{\alpha} |\mathbf{n}\sigma| a\mathbf{b} |\sum(\alpha) |d\mathbf{W}| e^{\frac{1}{2}(|\mathbf{r}| = |\mathbf{R}|)|(1 + \cos\theta/\cos i)/\tau|} |d\mathbf{r}|$$

$$= (\frac{\tau}{1 + \cos\theta/\cos i}) |(\mathbf{I}_{\alpha} |\mathbf{n}\sigma| a| \mathbf{b} |\sum(\alpha) |d\mathbf{W}|)$$

$$\approx -\frac{\mathbf{F}_{\alpha} |\mathbf{a}| \mathbf{b} |\sum(\alpha) |d\mathbf{W}|}{1 + \cos\theta/\cos i}$$
(155)

As mentioned before, this report is not interested in the total incident flux in photometric applications, such as photometry, but is interested in the photometric brightness. Recalling the basic photometric identity and invoking the geometric law of conservation of energy, one has

- 04

$$B = F'(dA \cos\theta \ d\Omega)$$

= $F/[dA \cos\theta \ (a/R^2)]$
= $\frac{E_0}{a} \frac{a}{b} \sum_{i}(\alpha) \ dW}{1 + \cos\theta/\cos i} = \frac{R^2}{a} = \frac{1}{-dA \cos\theta}$
= $\frac{E_0}{1 + \cos\theta/\cos i} = \frac{dA \cos\theta}{R^2} = \frac{R^2}{a} = \frac{1}{-dA \cos\theta}$
= $\frac{E_0}{1 + \cos\theta/\cos i} = \frac{E_0}{R^2} (\alpha)$ (156)

This is the form of the Lommel-Seeliger scattering law of interest to us.

3. Image Element Illumination. Let us repeat the problem addressed by this report: that is the determination of the densities of each of an array of image elements of a clearly defined optical system for the specified lighting conditions of a given terrain model.

The first problem to be considered is what each image element is to represent. Ideally: each element will reproduce the average illumination of that image element. Mathematically, this is a continuous process, defined by the integral of the illumination at each point of the image element, divided by the finite area of this element. Thus, the average illumination is given by

Į

$$< F > = \frac{\int dF}{A}$$
 (157)

where \mathbf{A} is the area of the image element, and \mathbf{dF} is the illumination of a differential image area element. $\mathbf{dS'}$. Recalling equation (41) and remembering that there is a 1:1 mapping of the differential surface area of the object into the corresponding element $\mathbf{dS'}$, one sees that equation (43) can be written as

$$\langle E \rangle \approx \frac{\int\limits_{S'} \frac{a B \cos\theta \cos\theta dS}{Mo^2 \cos\alpha \cos\beta}}{+A}$$
 (158)

where S^{i} is the corresponding area of the object.

It is this continuous integral that we must approximate by a discrete sum. If we let E_i represent the illumination of the *i*th point of the image element under consideration, then

$$\langle E \rangle \approx \frac{\sum_{i=1}^{n} E_{i}}{n}$$
 (159)

If the *i*th point of the image element is defined in terms of a local (x, y) coordinate system by $(X_i \ Y_i)$, and the corresponding point of the objects surface by (η_i, ξ_i) in terms of some (η, ξ) coordinate system on the surface of the object, then $B = B(\eta, \xi)$ and particular points can be defined as B_i . Similarly, θ and φ can be labeled by θ_i and φ_i . Then

$$\langle E \rangle \approx \frac{\sum_{i=1}^{n} \frac{B_i a \cos \varphi_i \cos \theta_i}{Mo^2 \cos \alpha \cos \theta}}{n}$$
 (160)

For realistic imaging systems, one may assume that θ will not vary appreciably over the image element. A more dubious assumption, although well-justified for image elements of sufficiently small areas, is that \mathbf{B}_i and φ_i will also vary by a negligible amount over the area of interest. Thus, we have

$$\langle E \rangle \approx \frac{a B_i \cos \varphi_i \cos \theta_i}{Mo^2 \cos \alpha \cos \beta}$$
 (161)

for some typical \mathbf{B}_i and corresponding θ_i and φ_i within the area of interest. Ideally, this point should be at or near the center of our image element, but in light of the approximations introduced thus far, this is not essential.

Finally, the approximation is introduced so that the field of view of the imaging system is small, and that for all elements of the image, θ_i XO. However, it is an approximation only for the perspective projection; it is exact for the orthonormal projection. Having introduced this approximation and noting that

$$\cos\varphi \approx \cos\alpha \cos\beta$$
 (162)

one has the formula for the "average" illumination $\langle E_j \rangle$ of the jth area element of the image, which contains a typical point with a corresponding point on the surface of the object characterized by a brightness B_i .

$$\langle E_j \rangle = \frac{a B_j}{Mo^2} = \alpha B_j$$
 (163)

This approximation is introduced for two reasons. First, the number of calculations will be significantly reduced that need to be made to determine the densities of a synthetic gray shade perspective image. Second, the final perspective should be composed of image elements with densities that are well defined functions of the terrain and lighting and that are not dependent on the arbitrary viewing parameter. In essence, the approximations introduced remove the vignetting effects that the rigorous equation accurately models. These effects would probably detract from the qualitative appearance of the image.

Same Same

1. Software Guide. This appendix is a user's guide to the ETL shaded relief software developed during the course of the work described in this report.

APPENDIX B.

The software was developed in FORTRAN on a PDP-11/45 minicomputer under an RSX-11/D operating system. The software is currently running on the ETL PDP-11/45 under

an RSX-11/M operating system. Familiarity with the body of this report is desirable before reading this appendix, and limited familiarity with FORTRAN and the RSX-11/M operating system is assumed.

This appendix present the information necessary to use the three sets of routines developed. First, the perspective shaded relief routine SHDPER.TSK procedures that are necessary to create the executable file from the FORTRAN source files will be examined, explaining the input parameters and detailing the format of the polynomial elevation data base, the output line printer graphic, and the coded-density disk file. The orthonormal shaded relief routine, SSLPLP.TSK will be examined. Finally, the program PDSKTP will be reviewed. The program reads the coded density data from the disk file created by either SSLPLP or a SHDPER and writes the data to a nine-track tape to generate high resolution images, using either the DICOMED or EBR gray shade recording devices available at ETL.

2. Perspective Routines. In this section, the use of the true-perspective shaded relief routines SHDPER will be described. Running on a PDP--11/45 mini-computer. SHDPER can created a shaded relief perspective image in a multi-user invironment in a time on the order of 5 milliseconds per pixel real time. This figure is subject to enormous variation, dependent on viewing parameters, machine use, and control parameters. The user of the SHDPER routines can

- 1. Specify viewer location.
- 2. Specify imaging geometry.
- 3. Specify image resolution,
- **4.** Specify the terrain viewed.
- 5. Specify a vertical exaggeration.
- 6. Define the position of the sun.
- 7. Enable a variable sun position within userspecified boundaries.
- 8. Choose between the Lommel-Seeliger law and Lambert's law to define terrain brightness.
- **9**. Define the density scaling.
- **10.** Specify program control parameters affecting processing efficiency.
- 11. Simulate the effects of atmospheric haze.

The program generates

- 1. Diagnostic output.
- 2. A DSKTRN-callable disk file of coded pixel densities.
 - 3. Low resolution line printer plots.

a. Building the Task: SHDPER.TSK. In this section, the procedures are examined for creating the file SHDPER.TSK to be executed on an RSX-11/M operating system. The user should know how to create files of the source code, as listed in appendix B, as well as the FORTRAN-callable I/O routine DSKTRN.

(1) FORTRAN Source Code File. In this section, the FORTRAN source code files needed to create the task SHDPER. TSK are examined. First, the algorithmic function of each of these files will be reviewed, and where appropriate, sufficient information for specific minor modifications will be presented.

(a) SHDPER.FTN. The program SHDPER.FTN is the main routine of the shaded perspective routines. An understanding of the basic structure of the program can be quickly gained by examining the listing and comparing it with the functional outline of the FORTRAN code presented in table 2.

There are two modifications of the file that the users might wish to make: (1) to alter the size of the maximum image that can be produced, and (2) to change the disk file created to another device.

To make the first modification, let M represent the desired maximum number of pixels per column of the image, and let N represent the maximum number of columns of pixels in the image. Thus, M' and N' are the corresponding least multiple of 256 greater than or equal to M/2 and N, respectively. Hence, the byte anag SHADE should be re-deminsioned

LOGICAL*1 SHADE (M)

and the two calls to DSKFIL should be altered as

100 CALL DSKFIL (2, -1,' DB:, LPPER.DAT', DUM, M, N)

CALL DSKFIL (2, -2,' DB1:, LPPER.DAT', DUM, M, N)

The dimensions of the Y-array may be altered with that of SHADE. The disk file name, or the device it is to be written on, can be enanged by altering the appropriate strings within the apostraphes of the two calls to DSKFIL. (b) PTS. FTN. The PTS.FTN file contains the subroutine PTS, which determines the coordinates at which elevation data points are to be accessed. The subroutine is compatible with the SHDPER calling routine and the altitude- and slope-computing subroutine ALT found in file ALSLP.FTN. Because it is simple, no outline of function will be given here.

The calling statement is

CALL PTS (X1, Y1, X2, Y2, NPTS, B, DLN, IASCD)

where

| (X1, Y1) | are the mapsheet coordinates of the observer's location |
|--------------|--|
| (X2, Y2) | are the coordinates of the other end point of the radial |
| | of interest. |
| NPTS | is the number of elevation data points to be generated |
| | along this profile and returned to the calling routine. |
| В | is the array in which the elevation data points are to |
| | be stored. |
| DLN IASCD | is, effectively, a dummy parameter for this application. should be set to 0 to minimize execution time. |
| - | |

One COMMON block should be defined in the calling routine (as it is in SHDPER):

COMMON/BOUNDS/XMAXB./YMAXB. XMINB. YMINB, ELEVB

where

and the second second

| (XMINB, | YMINB) | are the mapsheet coordinates of the origin of the |
|---------|--------|---|
| _ | | area modeled by the polynomial terrain data base. |
| (XMAXB. | YMAXB) | are the maximum mapsheet coordinates of the area |
| | | modeled by the polynomial data base. |
| | ELEVB | is the minimum elevation of the polynomial data |
| | | base. |

These variables are appropriately defined in the overhead portion of SHDPER. FTN.

(c) ALSLP.FTN. This file contains subroutine ALT. This subroutine accepts the X and Y mapsheet coordinates of the current point of interest and an integer flag IASCD. When IASCD = 0, only the elevation of the point of interest will be returned. When IASCD is set to 1 in the calling routine, both elevation and the partial derivatives $(\partial Z/\partial X \text{ and } \partial Z/\partial Y)$ at the point of interest will be returned.

The subroutine uses a polynomial terrain data base and currently is structured to read the coefficients of the upper one--third the Cache, Okla mapsheet into the arrays COEF1 (90, 40) and COEF2 (90, 40, 3). By bringing these coefficients into core, execution time is considerably reduced.

With this implementation, only data for points within the region modeled by the coefficients brought into core can be evaluated. The subroutine avoids inadvertent attempts to access non-modeled terrain areas by checking to see that the point of interest is within the region modeled. Points outside of this region will have their z values set to a nominal elevation, and the partial derivatives will be set to 0.

In table 3, the correlation is outlined between the function and the FORTRAN compilation line numbers used in the listing in appendix **B**.

The calling statement is

CALL ALT (X, Y, Z, SN, AZ, BZ, IASCD)

where

| (X, Y) | are the coordinates of the point of interest. |
|--------|---|
| L | will be the elevation of that data point. |
| SN | is a dummy parameter. |
| AZ, BZ | are respectively $\partial Z/\partial X$ and $\partial Z/\partial Y$; IASCD should |
| | not be equal to zero if AZ and BZ are desired. |

Two COMMON Blocks must be defined in the main routine.

COMMON/BOUNDS/XMAXB, YMAXB, YMINB, ELEVB

as in

ALSLP, FTN and COMMON/NEW'MRDR

where MRDR should be next to 1 in the main routine.

(d) GRNDPT.FTN. This file contains the image-object point correlation subroutine GRNDPT. The subroutine accepts the number of the current pixel of interest in the column of pixels being processed at the time of the call to the subroutine. On the basis of an array of elevation data points along the radial corresponding to the current column of pixels and the parameters defining the perspective view being generated, the subroutine finds a point along the radial, whose projection lies within a specified distance of the center of the pixel of interest.

The algorithm used (described in section IV, A) is iterative and makes several assumptions about the nature of the terrain modeled. Foremost among these is the assumption of continuity, which is violated at the "edge" of the area modeled by the coefficients in core. Hence, those views of the terrain in which the "cliff" would be visible are not amenable to analysis by the SP (or other) interative routine. The subroutine GRNDPT detects this condition, issues diagnostic error messages, and sets NFLAG to 10, which halts the execution of SHDPER.

In table 4, the correlation is outlined between the function of the source code and the line numbers of the FORTRAN compilation of GRNDPT in appendix C. In the table the notation found in section IV, A, is used.

The calling statement is

GRNDPT (J. Y. NFLAG, XI, YI, I. YMAX, IASCD, AZ, BZ, Z)

The argument and return values are as follows:

- J is the index of the pixel for which we are seeking a corresponding point on the ground. J runs from 1 at the bottom of the screen to NPIX at the top, where NPIX is the number of pixels in each column.
 Y is the array containing the screen Y-values of the
- projections of the points comprising the radial of
elevation data.NFLAGis a flag returned by
gRNDPT to the calling routine.
- NFLAG is 1, if a successful correlation has been made, and it is set to 10 if an error condition has been detected.
- (XI, YI) are the coordinates of the point on the ground whose projection lies within the pixel of interest.
 - **I** is an index pointing to the last **Y** array position with a value less than the last pixel center.
- YMAX is the maximum Y value in the Y array in the range Y(1) to Y(1). Any Y array value greater than YMAX is assumed to be visible.
- **IASCD** is the flag directing ALT to perform either altitude and slope, or just altitude computations. It should be set to 0 before calling GRNDPT.

Two COMMON Blocks must be defined in the calling routine:

COMMON/AARGH/Y, YO, THETAP, D. NPTS, DX, H.

YSF, I. SCL. TOL. THETA, YIST

and

COMMON/HGRAA/Z1, Z2, CSTP. SSTP. CST. SST

where

THE PROPERTY OF A

F.E.

| X, Y0 | are the SHDPER user specified "coordinates of position" (see SHDPER input Parameters below). |
|------------|---|
| ТНЕТАР | is the absolute azimuth in radians (aeronautical convention) of the current radial. |
| THETA | is the azimuth, in radians (aeronautical con- vention) relative to the principal direction of view. |
| YIST | is the elevation of the point (X, Y0). |
| DX | is the increment between pixel centers (De- fined as 14.5/(number of radials in SHDPER). |
| Н | is the elevation of the observer above ground level (in meters). |
| VSF | is the vertical scaling factor. |
| TOL | is the user specified tolerance. |
| SCL | is the ratio of inches on the image plane to meters on the ground |
| D,DIS,NPTS | are as specified in SHDPER Input Parameters. |

(e) SXSY.FTN. This file contains the variable sun angle subroutine SXSY. The subroutine varies the azimuthal position of the sun to highlight terrain features, within user-specified tolerances. Since the subroutine is well documented internally with respect to the functions outlined in section III, F, no table of source code function is given.

The calling sequence is

CALL SXSY (SX, SY, AZ, BZ)
SX, SY will be the X- and Y-- components of the illumination vector to be used for the current pixel.

AZ, BZ are the partial derivations $\partial Z/\partial X$ and $\partial Z/\partial Y$. defining the normal at the point of the surface of interest.

One COMMON Block must be defined:

COMMON/SEXY/DELTAG, COSEL, IVSUN, ANG, C1, C2, S1, S2

where DELTAG should be set to 1.

| COSEL | is the cosine of the elevation of the sun. | | |
|-------|--|--|--|
| IVSUN | is a flag specifying that the sun angle is to be | | |
| | varied (IVSUN = 1) or is not to be varied | | |
| | (IVSUN = 0). | | |

(f) LPPER.DAT. The file LPPER.FTN contains the line printer output algorithm LP. The subroutine accepts a byte array of arbitrary length and outputs the coded gray shade information of the first 100 array positions. The image format is summarized in section III, E of this report. Each byte should contain a value between 0 and 128. The correlation between density and input value can be found by examining the listing of LPPER.FTN and correlating it with table 1.

The calling statement is

CALL LPER (SHADE)

where SHADE is a byte (LOGICAL * 1) array of arbitrary length.

| ANG | is the angle of view (in radians, following the |
|----------------|--|
| | mathematical convention). |
| C1, C2, S1, S2 | are the values of S_x in equations (108, 109) |
| | and the values of S_v in equations (108, 109). |

104

where

.....

(g) LPPER.FTN. This file contains the line printer output subroutine LP. The subroutine is a straightforward implement of the Yoeli density table found in table 1. The calling statement is

CALL LP (SHADE)

where SHADE is a byte array containing the coded image densities.

(2) Compilation and Task Building. Before the SHDPER shaded relief perspective routines can be run, the source code files must be compiled, and the object files created by compilation must be combined into an executable file by the task builder.

Compilation is straightforward. If the user is logged on to the system, then the Main Console Routine (MCR) will issue a prompt:

MCR >

The user should then enter

FOR object file name, LP: = source file name, [CR]

If no line printer listing of the compilation is desired, the "LP:" may be deleted. An example of this process is

MCR > FOR SHDPER, LP: = SHDPER [CR]

The output file containing the object code will be placed, by default, in the file SHDPER.OBJ.

It should be noted that all of this assumes that the User Identification Code (UIC) of the user is that whose library contains the needed source code files as outlined in this appendix. If not, recourse to the RSX-11/M manuals should be made. In any case, all source code files should be compiled.

At this point, the executable task SHDPER.TSK can be built. This is done by using the indirect file SHDPER.TKB, (listed in this appendix). After the last source file has been compiled, one enters, in response to the MCR prompt

MCR > TKB SHDPER [CR]

This assumes that the FORTRAN --callable data access routine is stored under the UIC (300, 300). If this is not the case, then the command file SHDPER.CMD should be appropriately modified by the user. If the user is unsure as to how to do this, he should review the RSX-11/M operator's manuals. It is also possible that the user may desire alternative device assignments. These may be altered by changing the command file before task building or at the time of the running of the program (see the following section). In table 5, a summary of device assignments and program characteristics is shown.

b. Running SHDPER.TSK. Before discussing input parameters, it is appropriate to discuss the commands involved in initiating the execution of the SHDPER routine, as well as possible error conditions that might occur. Two procedures are available for initiating the execution of the task. Both assume that the task file SHDPER.TSK has been created, that the user is privileged (i.e. has logged on to a privileged UIC and has SET his UIC to that containing the task file), that the data base CACHE1.DAT exists on DB0: (and is unlocked), and that both disk drives (DB0: and DB1:) have been properly mounted.

The first means of initiating execution is, in fact, a subset of the second. In response to an MCR prompt, the user enters

MCR > RUN_SHDPER_[CR]

Execution should now commence, as outlined in the next section. It is possible, however, for error messages to occur as a result of any of several faulty conditions. The most frequent is related to the files. Either the input data file or the output data file may be locked. It is possible to check this (as well as correct it) by means of the Peripheral Interchange Program (PIP). In response to an MCR prompt, the user should enter

MCR > PIP:CACHE | 1 | DAT, DB1: = LPPER.DAT | UN |

If the files are not locked, PIP will respond with a message to that effect. If this is the case with both files, check to make sure that the files exist on the appropriate devices and are of the right dimensions. If they don't exist, PIP will respond with a message to that effect after the above command. If the files were locked, then no message will be issued; an MCR prompt will be issued, and the user should again attempt to run SHDPER. It should be noted that the active task created by the RUN command, as used above, will be named by the name of the terminal from which the task is excuted. Thus, if the user initiated operation on TTO:, then to abort the task during execution, the user must first bring up MCR by entering a < Control > [CR] command and then entering, in response to the MCR prompt

MCR > ABO TTO [CR]

Alternatively, the task can be INSTALLED before running, and an alternative name given to the active task. In response to an MCR prompt, the user enters

$MCR > INS SHDPER/TASK = SHDPER \{CR\}$

In this example, the task SHDPER is installed under the name of SHDPER. Any other name (6 characters) could be substituted for the second occurrence of "SHDPER". Having installed the task, one may alter the running priority by using the ALT command, or logical unit numbers can be reassigned to other physical devices by means of the REA command. See the RSX-11/M Operating Procedures Manual for details. The installed task is then run as above. The task should be removed after execution by the REM command:

MCR > REM SHDPER [CR]

c. Input Parameters. It is now assumed that the program is executing properly. In this section, the prompts issued by the program in sequential order will be reviewed, and the meaning of each of the input parameters will be explained. All RFAD statements in the program SHDPER.FTN are list directed. Thus, no attention needs to be paid to considerations of format.

Once the program has begun successful execution, it will issue a prompt

ENTER COORDINATES OF POSITION

The user should enter the X and Y mapsheet coordinate (X, Y, 0) of the position from which he wishes to create a perspective image. These coordinates do not have to be within the area modeled by the coefficients in core, but if this is not the case, care should be taken to avoid circumstances such as those described in the discussion of the subroutine GRNDPT in A.L.d. An example of an entry in response to this prompt is

7, 0, 14. [CR]

The shaded perspective routine will now issue another prompt:

ENTER ALTITUDE, AZIMUTH, # RADIALS, PTS/RADIAL,

DIS, # PIX/COLUMN, D

The first value entered should be the altitude in feet of the observer above ground level at the coordinates just entered. This defines the program variable HT. Low values for the altitude (0 to 1000 feet) will result in images with most of the image portraying terrain in the foreground; higher altitudes (1000 - 10.000 feet) will result in substantial coverage of distant objects.

The azimuth to be entered (AZ1), will specify the direction in which the imaging system will face. The program accepts any value for this parameter. It assumes that the value entered will be in degrees and will follow the aeronautical convention, such that 0° implies facing North, 90° implies facing East, etc.

The number of radial entered (NRAPS) specifies the number of columns in the resulting image. The actual number of columns in the image created will be (because of the algorithm used)

#Columns = 2 times INT(#radials specified/2) + 1

The number of columns are important in determining the vertical dimensions of the image. The software assumes a 14.5-inch-wide display screen, and a nominal spacing between pixels of DX = 14.5/(#columns-1). This **DX**, when mutiplied by the number of pixel per column, yields the effective vertical dimension of the image. The number of radials must be less than or equal to 1023, and the value entered should be positive.

The number of points per radial entered (NPTS) will determine the number of elevation data points to be generated along each radial profile. The NPTS number should greatly affect the time of execution; however, no study has been done of the actual impact of the value on execution time. It should be greater than 10 times the parameter D (see below) and must be less than 1024.

The distance of the image plane from the focal point is defined by DIS. Since the width of the image plane is internally fixed at 14.5 inch, the parameter also defines the angular width of the image. In table 5, a brief list of total angular widths are presented for various values of this parameter. Values of DIS below 10 result in fish-eyed views of the terrain, and values of DIS above 20 have narrow fields of view and are telescopic in nature. The number of pixels per column (NPIX) defines the height of the image, as noted above. This number must be less than 100 if line printer output is desired, and it must be less than 1024.

Finally, the mapsheet length of the radial of elevation data points generated is defined by D. Thus, only terrain within a radius D of the position of the observer will be imaged. Although D may assume any value, the value chosen should reflect the size of the area modeled.

The values for these seven parameters should be entered sequentially, seperate⁴ by commas. For example, one might enter

5000., 0., 200., 10., 100., 10., 100., 9.6 [CR]

The program will next issue the prompt

ENTER VERTICAL SCALING FACTOR, TOLERANCE

The first parameter to be entered, the vertical scaling factor VSF, is the vertical exaggeration to be applied to the terrain. It corresponds to the γ of equation (9) and should take a value between 1 and 5, although any value is acceptable.

The second parameter to be defined, the tolerance TOL, is defined in section III. B. There is no mathematically valid reason for defining TOL less than 0.5. Significantly greater values may under some circumstances result in images of ragged appearance. Thus, 0.5 is the suggested value.

One might enter the following in response to the prompt being considered

3, 0.5

The next prompt asks the user to

ENTER 0 FOR LAMBERTS LAW, 1 FOR

LOMMEL-SEELIGER LAW; DENSITY SCALING FACTOR, ATNTN COEF

The first entry requested defines the light-scattering law to be used in subsequent processing and sets a flag (LAW) in accordance with the entry.

The density scaling factor DSCL defines the factor by which the normalized densities that are calculated by the program are to be multiplied before packing each in an 8-bit byte. Any positive value is acceptable. For the upper one-

third of the CACHE, Okla. mapsheet as modeled at ETL, with the sun at altitude of 45° , with Lambert's law and with a vertical scaling factor of three, a good value is 200. A wide latitude is available, and it will be needed for various images. Thus, it is always a good idea to "proof" a proposed image with a line printer plot before generating a high resolution image.

The next input requested defines the attenuation coefficient. This parameter effectively enables the user to define the amount of haze present over the terrain viewed. Since haze is assumed to be of constant density, the contribution of the haze to image illumination increases roughly exponentially with distance. This parameter should be about half the value of **D**. An entry of 0, results in no haze,

A typical entry in response to this prompt might be

0. 200., 0. [CR]

The final input parameter prompt of SHDPSR asks the user to

ENTER ELEVATION, AZIMUTH OF SUN,

VARIATION OF SOLAR AZIMUTH.

This prompt enables the user to define the illumination of the terrain.

The first two inputs requested define the (principal) position of the sun. The first value requested, the elevation of the sum (ELEV1), is the altitude of the sun relative to a flat base plane. The parameter can assume values between 0° and 90° , such that zero degrees defines the sun to be on the horizon and 90° defines the sun to be directly overhead.

The second input parameter defines the azimuth of the vertical plane in which the elevation of the sun is measured. Any positive value is acceptable. The program assumes that the input will be in degrees and that the user will follow aeronautical conventions. Thus, an entry of 0 would define the sun as due north; and entry of 90 would define it as due east.

The third parameter enables the user to vary the sun angle, as outlined in section III, F of this report. The input requested is the variation in solar azimuth to be used in the algorithm, which defines variable RVIEW1. The program assumes an input in degrees, with any value between 0 and 90 being acceptable. Any value below 1° results in no variation of solar azimuth and values of 90° enables variation through one quadrant. At the present time, no detailed guidance can be given to the user with regards to the selection of these parameters. Optimum values are highly dependent on terrain, as well as on the other image parameters. A typical entry might be

45., 300., 0. [CR]

After processing the image that the user has just defined, the user will be required to

ENTER 1 FOR ANOTHER IMAGE

An entry of 1 enables the user to redefine parameters as outlined above. Any other entry halts execution.

3. Orthonormal Shaded Relief Routines. In this section the orthonormal shaded relief routines SSLPLP will be described. The routines produce an orthonormal shaded relief image defined by various input parameters from a polynomial terrain model. When being run on the ETL PDP-11/45 computer, the routines can produce an image in approximately 3 milliseconds per pixel, subject to variations as noted in the introduction to the SHDPER routines.

The user of the SSLPLP routines can

- 1. Specify the area to be imaged.
- 2. Specify the resolution of the image.
- 3. Specify the vertical scaling factor for the terrain.
- 4. Specify the shading law to be used to model the terrain.
- 5. Specify the position of the "sun".
- 6. Define a variation in solar position to highlight terrain features.

The routines generate

- 1. Diagnostic output.
- 2. A DSKTRN-Callable disk file of coded pixel densities.
- 3. Low resolution line printer plots.

a. Building the Task: SSLPLP.TSK. In this section, the procedures for creating the file SSLPLP.TSK are reviewed. It is assumed that the user has already created files of the source code (as listed in appendix B) as well as the FORTRAN callable disk 1/0 routine DSKTRN.

(1) FORTRAN Source Code Files. Before describing the actual procedure to create the SSLPLP task file, the function of each of the FORTRAN source files will be reviewed. Since most of the files have already been described in the SHDPER portion of this appendix, the previous discussion will not be repeated, only referenced.

(a) SSLPLP.FTN. This is the main routine of the orthonormal imaging routines. An understanding of the basic structure of the program can be quickly gained by comparing the listing of SSLPLP.FTN with the functional outline of the FORTRAN code presented in table 6.

SLPS.FTN. This file contains the source code for the subroutine SLPS, which generates an array of x and y slopes at equally spaced points along a profile of the terrain. The subroutine is called by

CALL SLPS (S1, Y1, X2, Y2, NPTS, AZA, BZA, DLN)

where

| (X1, Y1) | are the mapsheet coordi | nates of the first point |
|----------|-------------------------|--------------------------|
| | of the profile. | |
| | | |

- (X2, Y2) are the mapsheet coordinates of the last point of the profile.
- **NPTS** is the number of points along the profile at which the slopes are to be evaluated.
- AZA is the array that will be filled with the x-slopes $\partial Z/\partial X$.
- **BZA** is the array that will be filled with the y-slopes $\frac{\partial Z}{\partial Y}$.
- **DLN** is the distance in mapsheet inches between successive points along the profile. It is computed within SLPS.

One COMMON Block must be defined in the calling routine:

COMMON/BOUNDS/XMAXB, YMAXB, XMNB, YMINB, FLEVB

The common variables must be defined in the calling routine.

They are:

| XMAXB, YMAXB | The mapsheet coordinates of the upper right corner of the area modeled by the polynomial data base |
|--------------|--|
| XMINB, YMINB | The mapsheet coordinates of the lower left corner of the area modeled by the |
| ELEVB | The minimum elevation in meters of the area modeled. |

フィンキャー・ナ

The subroutine is very similar to the SHDPER subroutine PTS in structure.

(b) ALSLP.FTN, LPPER.FTN, SXSY.FTN. The files ALSLP. FTN, LPPER.FTN, and SXSY.FTN contain the remaining subroutines called by SSLPLP.FTN. All have been described in this appendix.

(2) Task Building. Before the SSLPLP orthonormal shaded relief routines can be run, the source code must be compiled, and the object files created by the compiler must be combined into an executable task file by the task builder. Source files should be compiled as outlined in this appendix.

When the source files have been appropriately compiled, the task file can be created. This is done by entering

MCR > TKB (a SSLPLP [CR]

As with SHDPER, the indirect command file SSLPLP.CMD assumes that the FORTRAN--callable disk 1/0 routine DSKTRN is stored in the UIC [300, 300]. If this is not the case, appropriate changes should be made in the command file.

b. Running SSLPLP.TSK. Execution of the program should begin. If an error condition occurs, it can be corrected as outlined in the discussion of the initiation of SHDPER in this appendix.

The prompts issued by the program will be reviewed in sequential order, and the meaning of each of the input parameters will be detailed. As with SHDPFR, all RFAD statements in SSLPLP are list directed, and no attention needs to be paid to the format of the input parameters.

Once the program has begun successful execution, it will issue the

prompt

and the second second

ENTER MAPSHEET COORDINATES OF LOWER

LEFT-HAND AREA OF INTEREST

The user should enter the X and Y mapsheet coordinates of the lower left corner (north-up) of the area of interest. This point does not have to be within the area modeled by the coefficients in core, though the unmodeled area will appear as a featureless plane. An entry in response to this prompt might be

5., 15. [CR]

The program will next prompt the user to

ENTER HEIGHT AND WIDTH OF AREA OF INTEREST

Height is the y-extent of the rectangular region to be modeled, and width is the corresponding x-extent. Both are measured in terms of mapsheet inches. A user might enter

4., 4. [CR]

The program next asks the user to

ENTER # PIXELS/HORIZONTAL LINE

The SSLPLP calculates one profile of elevation data points at a time. Each profile has a constant Y-coordinate, with successive profiles running from the upper (greater Y) boundary of the rectangle to the lower boundary. This prompt is asking the user to define the number of pixels in each of the profiles, which defines the pixel size and, thus, the number of profiles. It should be noted that a value of NPIX (the number of pixels per profile) of 100 or less results in the immediate production of line printer output, as well as of the disk file. Values greater than 100 will create only a disk file. A typical entry might be

100 [CR]

The program next asks the user to

ENTER VERTICAL SCALING FACTOR

The number entered will be used to scale the Z-coordinate of the 'terrain, resulting in an appearance of greater relief. Values between 1 and 10 are reasonable, although the values of other parameters will have an impact on the appearance of the final image. No absolute guidance can be given. This and other parameters must be optimized together, not one at a time. A typical entry might be

3. [CR]

The user next determines the light-scattering law that he will use to model the reflectance of the terrain. The user is asked to

ENTER FOR LAMBERTS LAW, 1 FOR THE LOMMEL-SEELIGER LAW

The prompt is self explanatory.

The final image defining prompt asks the user to

ENTER ANGLE OF ELEVATION OF LIGHT.

DIRECTION OF LIGHT, AZIMUTHAL VARIATION

This prompt plays precisely the same function that the corresponding prompt plays in the SHDPER routines. The user is referred to that section for more information about this prompt.

At this point, the program executes, and the user is asked, upon completion of the image just specified, to respond to

ANOTHER IMAGE: ENTER #1

The user should enter

1. [CR]

in order to continue execution. Any other entry will halt execution.

APPENDIX C.

Ì





۱

| |-|-

A start the start

è

ļ



H = 5500

Ĺ





the filt in

ł

;

Sal Destauration

FIGURE C4. Telescopic Perspective View: Cache, OK.

IJIS = 30.









FIGURE CS. Perspective View 1 ow Sun Cache, OK.

ţ

11. AW - (30, 45)







k

(Magnified With Bilinear Interpolation)

FIGURE CTE. Perspective View With 1 64 Resolution Cache, OK.

NPIX = 128NRAD = 179









1

FIGURE C15. Perspective View With Ridge Enhancement: Cache, OK.

10° SUN ANGLE VARIATION



FIGURE C16. Orthonormal Shaded Relief: Cache, OK.





FIGURE C18. Orthonormal Shaded Relief Image With Variable Sun Azimuth Merged With SIMCON Contours. (20-meters Interval)







APPENDIX D.

SHDPER/PR:0/FP/CP/NOTR=SHDPER,[300,J00]DSK1RN SXSY,LPPER,ALSLP PTS,RGSTR,GFNDP1 / UNITS=21 ASG=DB2:6,11:5,TI:7 ASG=DB0:14,DB0:13 ASG=DB2:12 //

139
| FORTRAN Shdper.F | IV Tn | -PLUS | V02-51E /TR:BLOCKS/WR | 13:21: | 37 | 21-APR-81 | PAGE 1 |
|--|--------------------|--|--|---|--|--|--|
| | 00000 | THIS P 9-TRA Conta Spect Based | ROGRAM WILL PROD CK ODD-PARITY MA INING THE CODED IVE VIEW OF THE O ON USER SPECIFI | UCE AN GNETIC DENSIT CACHE ED INP | EBR-C TAPE ILS OF Map Sh UT Par | OMPATIBLE File A Per- Eet, Ameters. | |
| | 0000000 | | PROGRAM BY CYRUS Automated Cartogi Usaetl, fort bel 18 July 1978 | C. TA Raphy I Vuir, | YLUR Branch Va | | |
| 0001 0002 0003 0004 0005 0006 | L | | LOGICAL*1 SHADE(DIMENSION Y(2048 DIMENSIUN ATIM(2 CUMMON /BOUNDS/X COMMON /REG/NRD1 COMMON /NEW/MRDR | 2048)) MAXB,YI ,NRD2,I | MAXB,X NRD3,N | MINB,YMINB, RD4,NRG1,NR | ELEVB G2,DXX |
| 0007 0008 | C C | 1 Fullum Fur ne | COMMON /SEXY/DEL COMMON /AARGH/X, SCL,TOL,DELR,DIS ING CUMMON ADDED W GRNDPT ROUTINE | TAG,CU YO,THE ,THETA 16 AU . C. T. | SEL,IV TAP,D, ,Y1ST G 79 AYLOR | SUN,ANG,C1, NP1S,DX,H,V | C2,51,52 SF, |
| 0009 | с | | CUMMON /HGRAA/Z1 | , Z2, CS | tp,sst | p,CST,SST | |
| 0010 | | 1 | DATA XMAXB/17.69 YMINB/.17717/,EL 1PAR/0/.1DEN/0/. | 6/,XM11 EVB/39 ICTL/1 | NB/.17 0./,10 28/.KO | 717/,YMAXB/ NIT/0/,KUDE UNT/128/ | 21.59/, /-1/,MODE/0/, |
| 0011 | | 1 | DATA PI/3.141592 | 6536/, | SCL/.0 | 007874016/ | |
| 0012 | 0000 | 1 | DATA IIMG/0/, IPF OPEN(UNIT=4, NAME 'DIRECI', READUNL OPEN(UNIT=9, NAME ACCESS='DIRECT', | ST/0/, = 'PL3D: Y,SHAR: = 'FORO READON: | IRFST/ EM.DAT ED,ASS 05.DAT LY,SHA | 0/ ',TYPE='OLD UCIATEVARIA ',TYPE='OLD RED,ASSUCIA | ',ACCESS= BLE=IV) ', TEVARIABLE=IW) |
| | | 1 | CALL TAPTRN(IUNI SHADE, MODE, IDONE IF(TERR.EQ.0)GO wRITE(5,1)IERR FORMAT(' TAPTRN | T,KUDE) TO 100 ERROR: | ,KOUNI ,13) | ,IER,NTRAN, | IPOS,ISTAT, |
| 0013 | L | 100 | CALL DSKF1L(4,-1 ,1FLAG,1ERR) | ,'DB0' | ,'САСН | E1.DAT',DUM | ,1024,100 |
| 0014 0015 0016 0017 | | 2 | IF(IERR.EQ.0)GU WRIIE(7,2)IERR,I FURMAT(' UPEN FA STOP | FLAG ILURE | DBUTCA | CHE1 ',213) | |
| | C C C C C C | 101 1 3 | CALL DSKFIL(3,-1 IFLAG,IERR) IF(IERR.LQ.0)GU WRITE(5,3)ILRR,I FURMAT(' UPEN FA STUP | ,'DBO' TO 102 Flag Ilure | ,'CACH DB01CA | E2.DAT',DUM CHE2 ',213) | ,1024,122, |
| 0018 0019 | - | 102 | KUUNT=8*IPAR+1DE CALL DSKFIL(2,-1 | N+ICTL ,'DB2' | ,'LPPE | R.DAT',DUM, | 1024,2043, |

| FORTRA | N IV-PLUS | V02-51E /TR:BLOCKS/wR | 13:21:37 | 21-APR-81 | PAGE 2 |
|----------|-----------|--------------------------------------|---|--------------------|-------------|
| 0.001.21 | •••• | | | | |
| | 1 | IFLAG, IERR) | | | |
| 0020 | | IF(IERR,EQ.0)G |) TO 114 | | |
| 0021 | | WRITE(7,115)1EF | RR,IFLAG | | |
| 0022 | 115 | FORMAT(1X, DB2: | LEPER OPEN | FAILURE',213) | |
| 0023 | | SIUP | | | |
| 0024 | 114 | CONTINUE | | | |
| 0025 | 127 | FORMAT(1X,2A4) | | | |
| | С | CALL TAPTRN(IUN | IT,6,KOUNT, | IERR, NTRAN, IPUS, | ISTAT, |
| | C 1 | SHADE, MODE, 100M | (E) | | |
| | С | IF(IERR.EQ.0)G |) TU 10 3 | | |
| | C | WRITE(5,1)IERR | | | |
| | С | STUP | | | |
| | C | | | | |
| 0026 | 103 | WRITE(7,4) | | | |
| 0027 | 4 | FORMAT(" ENTER | COURDINATES | OF PUSITION!) | |
| 0028 | | READ(5,*)X,Y0 | | | |
| 0025 | | WRITE(7,5) | | | |
| 0030 | 5 | FORMAT(ENTER | ALTITUDE, AZ | IMUTH, #RADIALS, P | TS/RADIAL", |
| | 1 | /, DIS, #PIX/C | OLUMN,D') | | |
| 0031 | | READ(5,*)HT,AZI | ,NRADS,NPTS | ,DIS,NPIX,D | |
| 0032 | | WRITE(7,6) | | | |
| 0033 | 6 | FORMAT(' ENTER | VERTICAL', | | |
| | 1 | SCALING FACTO | DR, TULERANC | E') | |
| 0034 | | READ(5,*), VSF, 1 | LOL | | |
| 0035 | _ | WRITE(7,7) | | | |
| 0036 | · · . | FURMAT(ENTER | O FUR LAMBE | RIS LAW, 1 FUR L | UMMEL- // |
| | 1 | SEELIGER LA | N; DENSITY S | CALING FACTUR;A1 | NTN CUEFY |
| 0037 | | READ(5, +)LAW, D | SCL,AININ1 | | |
| 0038 | • | WRITE(7,8) | | | |
| 0039 | 8 | FURMAIL ENIER | ELEVALION,A | ZIMUTH OF SUN; , | /, |
| 0040 | 1 | DEADLE +VET1 A | LUN UF SULAR | -) | |
| 0040 | C FOLLO | KEAD(SJY]EDIJAN Wing 2 tings de | CODE ADDED | 1 AUC 70 BY | |
| | | WING 3 DINES OF | CODE ADDED | I AUG 79 DI | |
| | C CONAL | SHULL DOUGESSEL | C FTC | 7 IA | |
| 0041 | C DIAR | 0HUI PROCESSEI WOITER(7 1951 | 10, EIC. | | |
| 0041 | 125 | - WRIIC(//120/ - FORMAT(18. (FNT) | |) | |
| 0042 | 125 | PEAD(5.*)YESET | | , | |
| 0045 | | CALL TIME (ATIM) | n | | |
| 0045 | | WRITE(7,127)(A) | , EIM(IJKL).1J | KL=1.2) | |
| 0045 | | IVSUN=0 | | | |
| 0047 | | IF(RVIEW1.LT.1. |)GO TO 104 | | |
| 0048 | | TVSUN=1 | ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,, | | |
| 0049 | 104 | AN=90AN1 | | | |
| 0050 | ••• | IF(NRADS.GE.10) | 24)GU TO 126 | | |
| 0051 | | 1PFST=1024+(11) | 4G-(2*(1IMG/ | 2))) | |
| 0052 | | IRFST=1024+(11) | 1G/2) | | |
| 0053 | 126 | CONTINUE | | | |
| 0054 | | AZA=(PI/2.)-(A | Z1*PI)/180. | | |
| 0055 | | RVIEW=RVIEW1/30 | 50. | | |
| 0056 | | RVIEw=(P1-2.*R) | /1Ew)/2. | | |
| 0057 | | EL=(EL1*PI)/180 |). | | |
| 0058 | | AN=(AN*PI)/180. | • | | |
| 0059 | | ANG=((135.*PI)/ | (180.)-AN | | |
| 0060 | | DX=14./FLOAT(NE | RADS-1) | | |
| | C FULLO | WING LINE ADDED | 1 AUG 79 BY | C. TAYLOR | |
| | | | | | |

| FURTRAN | IV-PLUS | V02-51E | 13:21:37 | 21-APR-81 | PAGE 3 |
|----------|----------|---------------------------------------|---------------------|---------------------|----------------------------------|
| SHUPER . | FIN | /IR:BLUCKS/WK | | | |
| 0061 | | OFST=YFSET/DX | | | |
| 0062 | | DXX=DX | | | |
| 0063 | | MRAD=NRADS/2 | | | |
| 0064 | | H=HT+12./50000. | | • | |
| 0065 | | SZ=SIN(EL) | | | |
| 0066 | | SY=SIN(AN)*COS(| SL) | • | |
| 0067 | | SX=CUS(AN)*CUS(E | rr) | • | |
| 0068 | | COSEL=COS(EL) | | | |
| 0069 | | DELR=D/FLOAT(NP) | (S-1) | | |
| 0070 | | DELTA=D/FLUAT(NE | | | |
| 0071 | | DELTAG=(DELTA#50 | 0000.)*(2.54/ | 100.) | |
| 0072 | | DELTAP=(DELTA/() | (5.E-4)+100. | ,/2.54)*9.)) | |
| 0073 | | CI=CUS(=RVIEw+() | 5. + P1/4.JJ | | |
| 0074 | | SI=SIN(RVIEW+() | , + E 1 / 4 . J J | | |
| 0075 | | SZ=SIN(RVIEW=(P) | ./4.JJ | | |
| 0078 | | | ~1/4.]] | | |
| 0077 | | ATNTN-ATNTN1 | 6 | | |
| 0078 | | AININ-AININI ITET+0 | | | |
| 0079 | | CALL INCETD | | | |
| 0081 | | WRITE(6.10)Y.YO | HT.471.VSF 1 | .A ATNTN1 | |
| 0082 | 10 | FORMAT($^{\prime}$ X Y=($^{\prime}$ | 289.4.1) HT= | | 4. ' VSF='. |
| 0002 | 1 | F9.4. LAw= .15 | ATNTN1=1.FF | (-5) | |
| 0083 | - | WRITE(6.11)NRADS | S.NPTS.NPIX.N | RDR.TOL.RVIEW1 | |
| 0084 | 11 | FORMAT(NRADS= | .I5. NPTS= | .15.' NPIX=', 15 | .' MRDR='.15.' |
| | 1 | TUL=', F9.4, 'RVII | Cw≓',F8.3) | ,,, , | / |
| 0085 | - | WRITE(6,12)EL1, | N1, DSCL, IVSL | JN.D.DIS | |
| 0086 | 12 | FORMAT(' EL, AN= | ',2F9.4,') D | SCL=',F9.4,' 1VS | UN=', 15 |
| | 1 | , D= ,F9.4, DI | S=',F9.4,/) | ••••• | • |
| | C DO LOC | JP OVER THE RADIA | LS | | |
| | С | | | | |
| 0087 | | DU 105 NRAD=MRAL |),-MRAD,-1 | | |
| | С | | | | |
| | CFIRST | PT OF RADIAL IS | X,Y; LAST PC | INT FOUND BY | |
| | C TRIGO | JNUMETRIC CUNSIDE | RATIONS, NOT | E THAT IN THIS P | RUGRAM |
| | C RADIA | ALS ARE SEPERATEI | BY A CUNSTA | ANT DISPLACEMENT | D b b c c c c c c c c c c |
| | | AT THE IMAGE PLA | ANE, KATHER T | THAN BY A CUNSTAN | T ANGLE |
| | | N THE TERTRUNIA P | PERSPECTIVE P | COTINES. | |
| | C MULTER | JLE THACE FILES A | AUST DEAD DDE | VIOUS IMAGE | |
| | C IF THE | PREVIOUS IMAGE | IS TO BE PRE | SERVED. | |
| | C FOLLO | NING 8 LINES ADDE | O C. TAYLOR | 10 AUG 79 | |
| 0088 | | MRCNT=MRAD=NRAD | +1+IREST | | |
| 0089 | | lF(IIMG.E0.0)GO | TO 128 | | |
| 0090 | | CALL DSKIRN(2.1 | IERR, MRCNT, N | RES, SHADE, 0, IDON | E) |
| 0091 | | IF(IERR.LU.0)GU | TU 128 | | |
| 0092 | | WRITE(7,118)IER | R, INRAD, MRAD, | MRCNT | |
| 0093 | | STOP | | | |
| 0094 | 128 | CONTINUE | | | |
| | C END OF | F ADDITION 10 AUG | 5 79 CCT | | |
| 0095 | | THETA=ATAN((NRAI | D*UX)/DIS) | | |
| 0096 | | IASCD=0 | | | |
| 0097 | | THETAP=AZA+THE1 | A | | |
| 0098 | | CST=COS(THETA) | | | |
| 0099 | | SST=SIN(THETA) | | | |
| 0100 | | CSTP=COS(THETAP) | | | |

| FURTRAN SHDPER.F | 1 V T N | I-PLUS | V02-51E /TR:BLOCKS/wR | 13:21:37 | 21-APK-81 | PAGE | 4 |
|--------------------------------------|------------|------------------|--|-------------------------|------------------------|------|---|
| 0101 0102 0103 0104 0105 | | | SSTP=SIN(THETAP) XEND=D*(CSTP) XEND=X+XEND YEND=Y0+D*(SSTP) CALL PTS(X.Y0.XF |) (nd.yend.npts | S.Y.DLN. LASCD) | | |
| 0100 | C C | FOLLUW New Gr | ING LINE ADDED H NDPT ROUTINE. C. | OR COMPATIBI | LITY WITH AUG 1979. | | |
| 0106 | | | IASCD=1 | | | | |
| | С | FULLUW | ING COMMENTS ARE | E NO LOIGER A | PPROPRIATE. | | |
| | Ċ | THESE | CUMPUTATIONS ARE | E NOW DONE IN | I GROUND | | |
| | C | CORKET | ATION ROUTINE. | C. TAILUR 16 | AUG /9. | | |
| | C C | | MKTIC(0)13)(1(1(| 5F),IGF=1,NP1 | .57 | | |
| | c | N.CIW H | AVE THE RADIAL P | REPRESENTED P | A PROFILE OF | | |
| | č | LLEVA | TION DATA PTS. | WE NEXT TRAN | SFORM THESE TO | | |
| | ē | SCREE | N COURDINATES, S | O THAT WE MA | Y CUMPARE PIXEL | | |
| | С | Y-VAL | UES WITH PROJECT | TED GROUND P1 | S, EVENTUALLY | | |
| | С | INTER | PULATING TO FIND | GROUND POSI | TIONS CORRESPONDING | | |
| | C C | TO PI | XEL POSITIONS. | | | | |
| | С | FOLLUN | ING 3 LINES CUMM | MENTED COUT F | OR NEW | | |
| | С | GRNPDT | ROUTINE, 16 AUG | 5 1979. C. TA | YLUR | | |
| | D | | DU 106 IPI=NPTS, | 2,-1 | | | |
| | D | | YS=H+(Y(1)-Y(IP)) | [))*VSF*SCL | | | |
| | υ | 106 | Y(IPT)=7YS*D18 | 5/((1PT+1)*DE | LR*CST) | | |
| 0107 | <i>.</i> . | 10110- | 11S1=1(1) | በሮሴ ለሀጥ ፋሬ እ፤ | | | |
| | L D | FULLUW | Y(1) = -100. | LED OUT 16 AL | 16 / 9. CCI. | | |
| | C | TUL CI | | - NO - NEEN CC | NUEDARD MOREEN | | |
| | c | | HRENI KADIAL HAG | IVED THE DIVE | T. DOSTITIONS OF | | |
| | č | THE S | CREEN. DETERMINI | ING CORRESPON | DING GROUND | | |
| | ĉ | POST | IONS. IF ANY. AN | ND CUMPUTE IN | AGE DENSITY AT | | |
| | ē | Thuse | POINTS. | | | | |
| | С | | | | | | |
| 0108 | | | NFLAG=0 | | | | |
| 0109 | | | YMAX=0. | | | | |
| 0110 | | | I=1 | | | | |
| | C. | | WRITE(6,13)(Y(10 | GF),1GF=1,NP1 | (5) | | |
| 0111 | 1 | 3 | FURMAT(IO(IX,IO) | 10.4,/),//) | | | |
| 0112 | ~ | 6 f i 1 f i 14 | DU 107 JEL,NPIX | 1 AUC 29 C TA | VEND | | |
| (11) 2 | C | FOLLOW | ING LINE ADDED (IFCT IF OFSI)CO | FO 108 | ILOR. | | |
| 0115 | c | FOLLOW | EINC LINE COMMENT | 10 100 TFD DUT FOR N | FW CRNPT | | |
| | c | ROUTIN | E 17 ANG 79. C. | TAYLOR. | | | |
| | ũ | 1.00110 | IASCD=0 | | | | |
| 0114 | • | | CALL GRNDP1(J.Y. | NFLAG.X1.Y1. | I,YMAX, IASCD | | |
| | | 1 | ,AZ, BZ, Z, 115T) | | | | |
| | С | | 1F(J.NE.10.AND. | J.NE.11)GO 10 | 0 112 | | |
| | C | | wRI1E(5,15)X,Y0, | ,X1,Y1 | | | |
| | C 1 | 5 | FORMAT(GRNDPT | VALUES: 4F1 | .0.4) | | |
| | CI | 12 | CUNTINUE | | 5 X 17 1 194 . A 17 17 | | |
| 0115 | | | IF (NELAG.NE.O.AN | ND.NELAG.NE.1 | UJGU TU 108 | | |
| | U. | L (11.1.00 | IF (NELAG.EQ.10) | JU TU 111 | | | |
| | C C | FULLUW | ING DINE COMMETE | | 141109 | | |
| | C. | MUG (9 | TOR NEW GRNDP1 | NUUIINE. L. | THING | | |

| FORTRAN | IV-PLUS | V02-51E | 13:21:37 | 21-APR-81 | PAGE 5 |
|---------|--------------|----------------------------------|-------------------|-----------------|----------------------|
| SHUPER. | r t in | /IK:BLUCKS/WR | | | |
| | υ | IASCU=1 | | | |
| | C FOLLO | WING LINE SUPERF | LUOUS WITH | NEW GRNPDT | |
| | C ROU11 | NE. 16 AUG 79. C | . TAYLOK | | |
| 0116 | 0 1 (A) 1 A) | CALL ALT(XI,YI, | Z,SN,AZ,BZ, | IASCD) | NUC 10 |
| | C FOLTO | NING IWU LINES C | UMMENTED UU | I C. TAYLUR IO | AUG 79 |
| | C | NGI=NC N71=N7 | | | |
| 0117 | C | AZ=AZ#VSF#DELTA | P | | |
| 0118 | | BZ=BZ*VSF*DELTA | P | | |
| 0119 | | CALL SXSY(SX, SY | ,AZ,BZ) | | |
| 0120 | | BEG=-SX*AZ*DEL1 | AG=SY+BZ+DE | LTAG+DELSQR*SZ | |
| 0121 | | DISI=SQRT((AZ+D |)ELTAG) **2+(1 | BZ*DELTAG)**2+(| (DELSQR**2)) |
| 0122 | | COSI=BEG/DISI | | | |
| 0123 | | IF(COSI.LT.1.E- | •6)CUSI=.000 | 001 | |
| 0124 | | IF (LAW, EQ.1)GO | 10 109 | | |
| 0125 | c | - SHAD-CUSI - WRITE(5 1121071 | 871.A7 H7 | USE DELTAD SY . | SY SZ DELTAR OFLITAG |
| 0126 | 113 | FORMAT(2(1),6F1 | 0.5./).//) | | |
| | C THIS I | LINE ADDED IN NE | W FUG FCTR (| CALCS | |
| | C 24 AU | G 79 C. TAYLOR | | | |
| 0127 | | IF(ABS(ATNTN).L | T.1.E-3)GO | IO 138 | |
| 0128 | 109 | CONTINUE | | | |
| | C | | | | |
| | CLUMME | L SELLIGER NUL P | IS LASI AS I | W NURMAL VIEW. | • |
| 0129 | C | R1P=SORT((X1=X) | **2+(Y1=Y0) | **21 | |
| 0130 | | YS = H + (Y(1) - Z) + V | SF*SCL | - / | |
| 0131 | | RER=SQRT(RIP**2 | !+¥S**2) | | |
| | C FULLU | WING LINE ADDED | FOR SMOG FA | CTOR | |
| | C C. TA | YLOR 24 AUG 79 | | | |
| 0132 | | IF (DAW, NE.1) GU | J TU 110 | | |
| 0133 | | AUPHA=(AIAN(IS/ | (RIPJ) (1.0HA) | | |
| 0135 | | VY=(SIN(THETAP) |) #(COSTALPH | A)) | |
| 0136 | | VZ=SIN(ALPHA) | , | | |
| 0137 | | COSE=((-DELTAG | (AZ¥VX+BZ¥V | Y)+VZ*DELSOR))/ | DIS1 |
| 0138 | | SHAD=1./(1.+(CC | DSE/COSI)) | | |
| 0139 | | IF(SHAD.LT.1.E. | 6)SHAD=0.00 | 0001 | |
| 0140 | | IF (ABS (ATNTN), I | T.1.E-3)GO | TO 138 | |
| 0141 | 110 | | Г. М. (Т. М.) | | |
| 0142 | | SHAD=1 +(SHAD=1 | TATA) TATA) | P) | |
| 0143 | 1 18 | SHAD=(ALOG10(1) | (SHAD))*DSC | L | |
| 0145 | 130 | 1F(SHAD_LT.1.)S | SHAD=1. | | |
| 0146 | | IF(SHAD.GT.127. |)SHAD=127. | | |
| 0147 | | SHADE(J+1PFST)= | SHAD | | |
| 0148 | | GO TO 107 | | | |
| 0149 | 108 | SHADE(J+1PFST)= | •0. | | |
| 0150 | 107 | CUNTINUE | | | |
| | | HTDHT DOARLER | | | |
| | C | | | | |
| | ē | | | | |
| | С | | | | |
| | C FOLLU | WING 2 LINES MUL | FD 10 AUG | 79 C. TAYLOR | |
| 0151 | | NROD=MRCNT-IRFS | δĽ | | |

;

| FURTRAN IV-PLUS SHDPER.FTN | V02-51E 13 /TR:BLOCKS/WR | 3:21:37 | 21-APR-81 | PAGE 6 |
|---|---|--|---|--------|
| 0152 0153 0154 0155 0156 118 C C 14 0157 C C | CALL RGSTR(NROD,SF CALL DSKTRN(2,2,IE IF(IERR.EQ.0)GG TC wRITE(7,118)IERR,M FORMAT(1X,'DSKTRN wRITE(5,14)NRAD,MF FORMAT(' NRAD=',3I STOP | HADE) ERR,MRCNT,NI J 105 WRAD,MRAD,MJ FAILURE',1 RAD,MRCNT [6] | RES,SHADE,0,IDONE) RCNT 3,316) | |
| C 0158 105 0159 0160 C FOLLON C IMAGE 0161 0162 | CONTINUE IF(NPIX.GT.100)GO DO 116 NRAD=1,(2*M ING LINE ADDED 10 PROCESSING. C. TAY NROD=NRAD+IRFST CALL DSKTRN(2,1,IE | TO 136 MRAD+1) AUG 79 FOR YLOR ERR,NROD,NR | MULTIPLE ES,SHADE,0,IDONE) | |
| 0163 0164 0165 C NUTE : C CURRE(0166 120 0167 116 | IF(lERR.EQ.0)GO TO WRITE(7,118)IERR STOP CHAT PROGRAM IS NOT CTLY PRINT MULTIPLE CALL LP(SHADE) CONTINUE | D 120 FIIIIIIII E IMAGÈ FIL | MODIFIED TO Es un lpo: | |
| 0168 136 C BECAU C IMAG C LOF C C C C C C C C C C C C C C C C C C C | CONTINUE SE OF EBR SUFTWARE LS BY 5 RECORDS OF AFTER ALL IMAGES | PROBLEMS, BALNKS, W1 | SEPERATE TH AN | |
| 0169 111 C C UNCUM C MULT C NEXT | CUNTINUE 4 LINES COMMENTED MENTED C. TAYLOR, W IPLE IMAGES TO BE (3 LINES ADDED SAN | OUT R. ROS WITH MODS T Generated O Me time C. | ENTHAL 6/79 O Allow Vernight Taylor 9 Aug 79 | |
| 0170 0171 0172 0173 0174 139 | ILMG=IIMG+1 CALL TIME(ATIM) wRITE(7,127)(AFIM) wRITE(7,139)ITST FORMAT(1X, *#ALT CA | (IJKL),IJKL Alls from G | =1,2) RNDPT=',18) | |
| 0175 0176 0177 9 0178 0179 | IF(11MG.GT.3)GO TU WRITE(7,9) FURMAT(* ENTER 1 F READ(5,*)1ANS IF(IANS.EQ.1)GU TO | J 137 For Andther D 103 | 1MAGE") | |
| 0180 137 0181 | CONTINUE CALL DSKFIL(2,-2, | 'DB2','LPPE | R.DAT',DUM,1024,204 | 3, |

| FURTRAN | IV-PLUS | V02-51E | 13:21:37 | 21-APR-81 | PAGE |
|------------|---------|----------------|----------------|--------------------|---------|
| SHDPER.FTN | | /TR:BLOCKS/WR | | | |
| | 1 | IFLAG, IERK) | | | |
| 0182 | | CALL DSKFIL(4, | -2, 'DB0', 'CA | CHE1.DAT', DUM, 10 | 24,100, |
| | 1 | IFLAG, IERR) | | | |
| | С | CALL DSKFIL(3, | -2, 'DB0', 'CA | CHE2.DAT', DUM, 10 | 24,122, |
| | C 1 | IFLAG, IERR) | | | |
| | С | | | | |
| | С | CLOSE(UN1T=4,D | ISPOSE='SAVE | *) | |
| | С | CLOSE(UNIT=9,D | ISPOSE='SAVE | •) | |
| | С | | | | |
| | С | | | | |
| | С | | | | |
| | С | | | | |
| | С | | | | |
| | C | | | | |
| | С | | | | |
| 0183 | | STOP | | | |
| 0184 | | END | | | |
| | | | | | |

and the second second

| LUNTRAN | lv-PLUS | 402-516 | | 13:21:31 | 21-APH-81 |
|---------|---------|---------|--------|----------|---------------|
| SHUPER. | t TN | /TR:BLO | CKS/#R | | |
| PRUGRAM | SECTION | 5 | | | |
| NUMBER | NAME | 512 | £ | A 1 | IRIBUIES |
| 1 | SCODE1 | 005036 | 1295 | Re | , L, CUN, LCL |
| 2 | SPDATA | 000126 | 43 | Rø | ,D,CUN,LCL |
| 3 | SIDATA | 001574 | 446 | RW | ,D,CUN,LCL |
| 4 | SVARS | 024366 | 5243 | Rie | ,D,CUN,LCL |
| 5 | STEMPS | 000012 | 5 | K n | , U, CUN, LCL |
| 0 | BUUNDS | 000024 | 10 | K# | , D, UVR, GBL |
| 1 | REG | 000020 | H | нw | ,D,OVK,GBL |
| 8 | NEW | 000002 | 1 | Ra | , D, UVR, GBL |
| У | SEXY | 000036 | 15 | Re | , U, UVR, GBL |
| 10 | AAKUN | 000066 | 27 | K W | ,D,UVR,GBL |
| 11 | HGRAA | 000030 | 12 | 8. | . D. UVR. GBL |

VARIABLES

and the second second

| NAME | TYPE | AUDRESS | NAME | 1146 | ADDELSS | NAME | 1126 | ADURESS | NAME | LINE | ADDRESS | NAME | TYPŁ | ADDRESS |
|----------|-------|-----------|--------|-------|-----------|--------|-------------|-----------|------------|-------|-----------|--------|------|-----------|
| ALPHA | n#4 | 4-024332 | AN | K#4 | 4-024120 | ANG | ⊨ +4 | 9-000012 | AN1 | H+4 | 4-024102 | ATHIN | H+4 | 4-024176 |
| AININI | H#4 | 4-024012 | AZ | K#4 | 4+024250 | AZA | ++4 | 4-024124 | AZ1 | ƙ#4 | 4-024054 | 686 | H+4 | 4-024276 |
| ыZ | H#4 | 4-024262 | COSE | R#4 | 4-024352 | CUSEL | R#4 | 9-000004 | CUSI | ¥*4 | 4-024306 | CST | K*4 | 11-000020 |
| COLF | K#4 | 11-000010 | CI | K+4 | 9-000016 | C2 | K#4 | 9-000022 | υ | H#4 | 10-000014 | DELF | 8+4 | 10-000046 |
| ULLSUR | F+4 | 4-024172 | DELTA | R+4 | 4-024162 | DELTAG | R#4 | 9-000000 | DELTAP | k#4 | 4-024166 | 015 | R#4 | 10-000052 |
| uist | H#4 | 4-024302 | DLN | R#4 | 4-024230 | DSCL | K*4 | 4-024000 | DUM | R+4 | 4-024040 | DX | R*4 | 10-000022 |
| 0.4.4 | H#4 | 7-000014 | EL. | H+4 | 4-024134 | ELEVE | ĸ≉4 | 5-000020 | LL1 | R+4 | 4-024070 | FCTH | H#4 | 4-024356 |
| rí | 6.04 | 10-000026 | нĩ | 6.4.4 | 4-024050 | 1 | 1+2 | 4-024242 | IAND | 1+2 | 4-024304 | IASCD | 1+2 | 4-024216 |
| ICTL. | 1+2 | 4-024022 | 1 DE N | 1+2 | 4-024020 | IDONE | 1+2 | 4-024212 | 1 E R K | 1+2 | 4-024046 | IFLAG | 1+2 | 4-024044 |
| LING | 1+2 | 4-024032 | LJKL | 1+2 | 4-024110 | INFAD | 1+2 | 4-024214 | IPAH | 1+2 | 4-024016 | 1PF ST | 1+2 | 4-024034 |
| TREST | 1+2 | 4-0/4036 | 1151 | 1+2 | 4-024202 | 10011 | 1+2 | 4-024010 | IVSUN | 1+2 | 9-000010 | Ĵ | 1#2 | 4-024244 |
| KLIDE | 1+2 | 4-024012 | KUUNT | 1+2 | 1-024024 | LAw | 1+2 | 4-624064 | MODE | 1 * 2 | 4+024014 | MRAD | 1#2 | 4-024144 |
| SHONT | 1+2 | 4-024206 | мнин | 3+2 | 8-0000000 | NFLAG | 1+2 | 4-024234 | NPIX | 1+2 | 4-024062 | NP1S | 1+2 | 10+060020 |
| aRAU | 1+2 | 4=024204 | NRAUS | 1+2 | 4-024000 | NRDI | 1+2 | 7-000000 | | 1+2 | 7-000002 | 6+L3 | 1+2 | 7-000004 |
| NEUA | 142 | 7-000005 | NRES | 1+2 | 4-024210 | NHGI | 1+2 | 7-000010 | NHG2 | 1+2 | 7-000012 | NEUL | 1+2 | 4=024362 |
| (Real | H#4 | 4-024140 | PI | 844 | 4+4/4026 | H1P | R+4 | 4-024316 | RRH | 8+4 | 4-024326 | RVIEN | R#4 | 4-024130 |
| HVIEWI | H # 4 | 4=024106 | SCL | R#4 | 10-000036 | SHAD | H+4 | 4-024312 | SN | H+4 | 4-924272 | 551 | 8*4 | 11-000024 |
| Safe | 8+4 | 11-000014 | SX | 8+4 | 4-024156 | SY | H+4 | 4-024152 | 52 | 8*4 | 4-024146 | 51 | H+4 | 9-000026 |
| <u>.</u> | | 9+000012 | LHETA | | 10-000056 | THEIAP | н#4 | 10-000010 | Tut. | H#4 | 10-000042 | Vot | 444 | 10-000032 |
| | 8.4.4 | 4+11/4336 | 110.00 | H#4 | 1-024442 | */ | H # 4 | 4=0/4340 | | | 10-000000 | XENL | 8*4 | 4-024220 |
| | | 4 024350 | ***** | 444 | 5-000000 | IMINH | | 5-000010 | YEND | 8.84 | 4=024224 | YESET | 4+4 | 4-0/4112 |
| - 21 | 1.84 | 4-024240 | 20000 | | 4-024236 | VNAXB | | 5-000004 | CRINH | H . A | 6-000014 | YS | 8.84 | 4+024122 |
| | | 10=000004 | 1151 | L 8 4 | 10=000062 | 7 | 6.94 | 4=024266 | 2.1 | | 11-000000 | 72 | | 11-000004 |
| 10 | | 10-000004 | 1131 | 6 ° N | 10-000002 | - | | | | | | | | |

APRAIS

| NAME | 1166 | ADDRESS | 512 | Ł | DIMENSIONS |
|--------|------|----------|--------|------|------------|
| ALIM | H#4 | 4-024000 | 000010 | 4 | (2) |
| SIGAUE | L+1 | 4-000000 | 004000 | 1024 | (2046) |
| 3 | H+4 | 4-004000 | 020000 | 4090 | (2048) |

LABELS

PAGE 8

FURTRAN 17-FLUS 702-51E 13:21:37 21-APK-81 Shufek.fln /IR:DUUKS/AK

PAGE Y

| LAULL | ALLFESS | LABEL | AUDRESS | LABEL | AUCHESS | LADEL | AUURESS | LABEL | ALDHES | s | |
|---------|----------------|------------|-----------|------------|----------|---------|--------------|-------|--------|-------|-------|
| 2. | 3-000000 | 4. | 3-000104 | 5 * | 3-000140 | ь. | 3-000252 | 1. | 3-0003 | 32 | |
| ۰. | 3-006412 | ч' | 3-001202 | 10* | 3-000020 | 11' | 3-300720 | 12. | 3-6010 | 22 | |
| 131 | ** | 100 | ** | 102 | 1-000112 | 103 | 1-000236 | 104 | 1-0010 | 102 | |
| 105 | 1-004342 | 107 | 1-004164 | 108 | 1-004142 | 109 | 1-003402 | 119 | 1-0037 | 56 | |
| 111 | ** | 113* | | 114 | 1-000230 | 115* | 3-000040 | 110 | | | |
| 110' | 3-001114 | 120 | 1-004520 | 1251 | 3-000570 | 120 | 1-001102 | 127" | 3-0000 | 70 | |
| 120 | 1-002544 | 130 | 1-004552 | 137 | 1-005002 | 138 | 1-004034 | 134, | 3-0011 | 44 | |
| runctio | NS ANL SUBROUT | INES REFER | INCED | | | | | | | | |
| ALT | USEFIL DOKT | R + GRNDPT | IPUSTR LP | 815 | RGSTH SA | SY TIME | SALGIO SAIAN | \$CU5 | SEXP | \$51% | SSURT |

IUTAL SPACE ALLUCATED = 033602 7105

,LP.LS(=5#0PEK

A STREET, STREE

and and an an

| FURTRAN SXSY.FTI | lv-PLUS V | V02-51E /TR:BLOCKS/WR | 13:23: | 08 2 | 1-APR-81 | PAG |
|--------------------------------------|--|---|--|--|---|------------------------|
| | C THIS C C 'SUN C CHEA' C REFERI C UF TH C (UNP) | SUBROUTINE IS D • TO STRENGTHEN TED BY PRUGHAMS ENCE: P. YOELI, HE ANALYTICAL H UBLISHED?-AUTO | ESIGNED THE DET SHADE.F SUME R HILL SADI CARTO FI | TU VARY All IN TN AND Emarks NG PROJ Les) | THE AZIMUTH O Shaded Relief Shadep.FTN. On The Complet ECT' | F THE Images Ion |
| | 2 C C C C C C C C | PROGRAM BY CYR Automafed Cari Usaefl, forf b 11 July 1978 | US C, IA Ugraphy Selvuir, | YLÖR BRANCH VA | | |
| 0001 0002 0003 0004 | ſ | SUBROUTINE SXS Commun /Sexy/d Real*4 nx,ny IF(IVSUN.EQ.0) | GO TU 11 | AZ,8Z) SEL,1VS 0 | UN,ANG,C1,C2,S | 1,82 |
| 0005 0006 0007 0008 0009 | | NX=-AZ*DELTAG NY=-BZ*DELTAG DISFI=SQRT((NX IF(DISFI.LT.I. CO=NX/DISFI | .**2)+(NY .E=6)GU T | **2)) 0 110 | | |
| 0010 0011 0012 | C IN EF C RUIA C THAT | SO=NY/DISF1 C=CO*COS(ANG)+ S=SO*COS(ANG)+ FECT, DUR X-Y C TED THRUUGH AN THE ANGULAR CO | SO*SIN(A CO*SIN(A DURDINAT ANGLE UF DURDINATE | NG) NG) E SYSTE ANG RA SYSTEM | M HAS BEEN DIANS. NOTE USED IN THIS | |
| | C RUUT C AEROI C TRAD C UUR C SX AI C TU TI C SECTOI | INE AND IN SHAD NAUTICAL ANGULA ITIUNAL ALGEBRA X-I CUURDINATE ND SY MUSI BE H HE MAIN ROUTINE R I CASE | DE OR SHA IR CUORDI AIC CUORD SYSTEM H RUTATED B | DLP IS NATE SY INATE S AS BEEN ACK BEF | NOT THE SIEM, BUT THE YSTEM, SINCE ROTATED, URE RETURNING | |
| 0013 | | IF(C.GT.(C1). | UR .S.LT | .(S1))G | O TO 10 | |
| 0015 | | SY=-S*CUSEL | | | | |
| 0016 | | GU TU 100 | | | | |
| | C SECTU | R III CASE | 1314 et 25.00 | (| 0 TO 30 | |
| 0018 | 10 | IF(C.L1.(C2). | UK .S.GT | .(S2))G | 0 10 20 | |
| 0010 | | SY=S*COSFL | | | | |
| 0020 | | GU TU 100 | | | | |
| 0020 | C SECTU | H 11 CASE: 2 SU | BCASES | | | |
| 0021 | 20 1 | IF((C.LT.0.AND .0R.(S.LT.0.A | .S.LT.0) | .OR.(C. (2))GO | L1.0.AND.S.LT. TU 30 | 51) |
| 0022 | | 1F(C.GT.(0.707 | 11))GU TU | 25 | | |
| 0023 | | SX=0. | | | | |
| 0024 | | SY=-CUSEL | | | | |
| 0025 | 0.5 | GU TU 100 | | | | |
| 0026 | 25 | SX=CUSEL | | | | |
| 0027 | | 51=V. Gu TO 100 | | | | |
| 0020 | C SECTO | K IV CASE: 2 SI | BCASES | | | |
| | C DECIU | | | | | |

ti di sino

PAGE 1

| FORTRAN SXSY.FIN | IV-PLUS | V02-51E /TR:BLUCKS/WR | 13:23:08 | 21-APR-81 |
|---------------------|---------|--------------------------|--------------|-------------------|
| 0029 | 30 | IF(C.LT.(-0.7071 |))GU TU 35 | |
| 0030 | | SX=0. | | |
| 0031 | | SY=-CUSEL | | |
| 0032 | | GO TO 100 | | |
| 0033 | 35 | SX=CUSEL | | |
| 0034 | | SY=0. | | |
| 0035 | 100 | CUNTINUE | | |
| | C WE MU | IST NOW ROTATE OU | R LOCAL X-Y | COURDINATE |
| | C SYSTE | M BACK, SO THAT | SX AND SY WI | ILL BE CONSISTANT |
| | C WITH | THE MAIN ROUTINE | S. | |
| 0036 | | Y=SY*CUS(ANG)~SX | (*SIN(ANG) | |
| 0037 | | X=SX*COS(ANG)+SY | *SIN(ANG) | |
| 0038 | | SX=-X | | |
| 0039 | | SY=-Y | | |
| C040 | 110 CC | DNTINUE | | |
| 0041 | | RETURN | | |
| 0042 | | END | | |

PAGE 2

2421-514 /141860682/84 2421-514 /141860682/84

PRUGRAM SECTIONS

| NUMBER | NAME | 5128 | | ATTHIBUTES |
|--------|----------------------------|----------------------------|----------------|---|
| 1 2 | SCUDE 1 SFDATA SVAKO | 001000 000014 000044 | 250 6 18 | HN, 1, CUN, LCL RN, D, CUN, LCL RN, D, CON, LCL |
| 5 | STEMPS SEX1 | 000004 | 2 15 | Rw,D,CÚN,LCL Rw,D,LYF,GBL |

ENIHI PUINTS NAME TIPE AUURESS NAME TYPE AUURESS NAME TYPE AUURESS NAME IYPE AUORESS NAME TYPE ADURESS SASI 1-0000000

PAGE 3

VARIABLES

ITPE ADDRESS NAME TIPE ALDRESS NAME TYPE ADURESS NAME TYPE ADDRESS NAME TYPE ACCRESS NAME C K*4 Deliag R*4 S K*4 S2 K*4 4-060624 6-000006 4-000030 6-000032 COSEL R#4 DISF1 R#4 SX ##4 X R#4 6-000004 4-000010 F-000002* 4-000040 ANU H+4 CO H+4 1v5UN 1+2 SI H+4 Y H+4 µ+4 µ+4 µ+4 H+4 F=000010# 6=000022 4=000004 6=000026 6=000012 AZ 4=000014 C1 6=000010 NA F=000004* Su 4=000034 F-000006* H2 5-000016 C2 4-000000 N1 4-000020 S1 K*4 8*4 H*4 K*4

LABELS

| LADEL | AUDKESS | LAULL | AUDRESS | LABEL | AUUKESS | LABEL | ADDRESS | LABEL | AUCHESS |
|-------|----------------------|-----------|----------------------|-------|----------|-------|----------|-------|----------|
| 10 | 1-000320 1-000660 | 20 110 | 1-000412 1-000776 | 25 | 1-000542 | 30 | 1-000570 | 35 | 1-000634 |

FUNCTIONS AND SUBBOUTINES REFERENCED SCUS SSIN SSURT

IUTAL SPACE ALLUCATED = 001122 297

, LP. LST=SX5Y

م. م. 1993، Alexandria (1995) متحافظ الم الحالية (1995) من 1995) ما يا 1995 م

| FURTRAN LPPER.E | 4 IV Ftn | -PLUS | VU2-51E /fr:blucks/wr | 13:23:37 | 21-APR-81 | PAGE 1 |
|--------------------|-------------|----------------|--|---|--------------|----------------|
| | c c | FILE | NAME - LPPER.FI | [N | | |
| 3001 | - | | SUBROUTINE LP(: | SHADE) | | |
| 200 2 | | | LOGICAL*1 SHADE | -(1),CHAR(12) | | |
| 2003 | | | LOGICAL*1 PRNT | (100) | | |
| 0004 | | 1 | DATA CHAR/ . | · · · , · - · , · 1 · 4 · , · w · / | *, */*, *V*, | ***, *@*, *U*, |
| | C | | WRITE(5,51)(SHA | ADE(M),M=1,32 |) | |
| 2005 | 5 | 1 | FURMAT(1x, 3203, | ,/) | | |
|)00b | | | DU 10 I=1,3 | | | |
| 2007 | | | DU 50 K=1,100 | | | |
| 2008 | | | IF(SHADE,K),LT, | v_{\bullet})SHADE(K)= | 127. | |
| 1009 | | > /s | PRNT(K)=CHAR(1) |) | | |
| 3010 | | 50 | CUNTINUE | | | |
| 1011 | | | DU 20 J=1,100 | 6 1 10 10 10 10 10 10 10 10 10 10 10 10 10 | | |
| 1012 | | | IF (SHADE (J).GI | | | |
| 1013 | | | IF(I.WE.I)GU IU | J 20 | | |
| 1014 | | | CD TO 20 |) | | |
| 1015 | | 21 | TECSHADECTS CT | 9) CO TO 22 | | |
| 010 | | 21 | TECT NE INCO TO | | | |
| 1018 | | | DBNT(.1)=CHAR(2) | | | |
| 2019 | | | | , | | |
| 1020 | | 22 | IF(SHADE(J).GT. | 14)GO TO 43 | | |
| 1021 | | | IF(1, NE, 1)GU T |) 20 | | |
| 1022 | | | PRNT(J)=CHAR(J) |) | | |
| 1023 | | | GU TU 20 | | | |
| 1024 | 4 | ٤ | IF(SHADE(J).GT. | 15)GU TU 23 | | |
| 1025 | | | IF(1.NE.1)GO TU |) 20 | | |
| 1026 | | | PRNT(J)=CHAR(4) |) | | |
| 1027 | | | GU TU 20 | | | |
| 1028 | | 23 | IF(SHADE(J).GT. | 19)GU TU 24 | | |
| 1029 | | | 1F(1.NE.1)GU TU | J 20 | | |
| 1030 | | | PRNT(J)=CHAR(5) |) | | |
| 1631 | | | GO 10 20 | | | |
| 032 | | 24 | IF(SHADE(J).GT. | 24)GU TU 25 | | |
| 680 | | | IF(1.NE.1)GU TC | 20 | | |
| 034 | | | PRNT(J)=CHAR(6) |) | | |
| 035 | | 61 E | GU TU ZU | 20200 7 . 20 | | |
| 050 | | 20 | IF (SHADE(J).GI | 28360 10 20 | | |
| 1120 | | | | | | |
| 0.30 | | | $-\frac{1}{2} - \frac{1}{2} - 1$ |) | | |
| 040 | | 26 | IF(SHADECH) GE | 11100 10 21 | | |
| 040 | | 20 | $IF(I_NF_1)GO$ | 1 20 | | |
| 04/ | | | PRN1(J)=CHAR(8 |) | | |
| 043 | | | GO TO 20 | • | | |
| 044 | | 21 | IF (SHADE(J).GE | .38)GU TU 28 | | |
| 045 | | | IF(1.EQ.3)G0 TO | 20 | | |
| 046 | | | IF(1.EV.1)PRNT | $(\mathbf{J}) = CHAR(9)$ | | |
| 047 | | | IF(I.EQ.2)PRNT | (J)=CHAR(2) | | |
| 048 | | | GU TO 20 | · · · · · · · · · · · · · · · · · · · | | |
| 049 | | 28 | IF(SHADE(J).GT.4 | 44)GU TU 29 | | |
| 050 | | | IF(1.EQ.3)GU TO | ע נ | | |
| 051 | | | IF(I.EQ.1)PRNT | (J)=CHAR(10) | | |
| 052 | | | 11(1.EQ.2)PRNT | (J)=CHAK(5) | | |
| | | | | | | |

| URIRAN | IV-PLUS | V02-51E | 13:23:37 | 21-APR |
|--------------|---------|----------------------|------------------------|--------|
| PPER.F | TN | /TR:BLUCKS/WR | | |
| 0 5 3 | | () D () () () | | |
| 053 | 26 | GU IU ZU | n | |
| 054 | 29 | IF (SHADE (J).G | 1.51360 10 3 | 0 |
| 055 | | 1F(1.EQ.3)GU | 10 20 | |
| 050 | | IF(I.EQ.I)PRN | 1(J) = CHAR(10) |) |
| 057 | | IF(1.EQ.2)PRW | I(J) = CHAR(5) | |
| 058 | | GO IU 20 | | |
| 059 | 30 | IF(SHADE(J).G | T.58)GO TU 3. | 1 |
| 060 | | 1F(1.EQ.3)GU | 10 20 | |
| u61 | | IF(I.EQ.1)PRN | 1(J) = CHAR(10) |) |
| 062 | | IF(I.EQ.2)PHN | T(J) = CHAR(8) | |
| 60U | | GU TÚ 20 | | |
| 064 | 31 | IF(SHADE(J).G | T.66)GO IÙ 3 | 2 |
| 065 | | 1F(1.EQ.3)PRN | T(J)=CHAR(4) | |
| 066 | | IF(1.EQ.1)PRN | T(J)=CHAR(6) | |
| 067 | | IF(I.EQ.2)PRN | $\Gamma(J) = CHAR(10)$ |) |
| 008 | | GO TO 20 | | |
| 069 | 32 | IF(SHADE(J).G | T.76)GU TU 3. | 3 |
| U70 | | PRNT(J)=CHAR(| 11) | |
| 071 | | IF(I.EQ.1)PKN | T(J) = CHAR(10) |) |
| 072 | | 1F(1.E0.2)PRN | T(J) = CHAR(9) | |
| 073 | | GO TO 20 | | |
| 074 | 33 | PRNT(J)=CHAR(| 12) | |
| 075 | | IF(I.EU.I)PRN | r(J)=CHAR(10 |) |
| 076 | | IF(I.EO.2)PRN | T(J) = CHAR(5) | • |
| 077 | 20 | CONTINUE | | |
| 078 | | WRITE(6,500)(| PRNT(L).L=1. | 100) |
| 079 | 500 | FORMAT(+ + . 1) | .100A1) | |
| 080 | 10 | CONTINUE | ,, | |
| 081 | | wRITE(5.501) | | |
| 082 | 501 | FORMAT(1X) | | |
| 083 | ~~* | RETURN | | |
| 084 | | FND | | |
| V U T | | U U | | |

1

Su ieun i

-81

| SSCH "F | 1V-F1. 1N | LS FU2-51E /INIBLO | (*=) | 13:53 | : 5/ 21- | APH = 0] | | PAGE 3 | | | | | | |
|-----------------------|---------------------------|-----------------------------------|----------------------------|---------------------------|-------------------------------|-------------------------------|----------------------|-------------------------|------------------------|------------------------------|----------------------------------|------------------------|------------------------------|----------------------------------|
| RUGKAM | SECTI | LNS | | | | | | | | | | | | |
| UMBER | HAME | 512 | c. | | AllFley | 1123 | | | | | | | | |
| 1 3 4 | SCULE SILAT SVAHD | 1 001704 A 000024 000170 | 48∡ 10 60 | | HA,1,CL HA,D,CC HA,D,CC | IN, LCL IN, LCL IN, LCL | | | | | | | | |
| N1K1 P | J1N15 | | | | | | | | | | | | | |
| NAME | 11FF | ADURESS | NAME | LIPE | AULRESS | NAME | 1 Y P E | ADDRESS | NAME | TYPE | ADDRESS | NAME | TIPE | ADURESS |
| LP | | 1-000000 | | | | | | | | | | | | |
| AFIADL | LD | | | | | | | | | | | | | |
| NAME | LINE. | AUUKESS | NAME | 1186 | ADURESS | NANE | TYPE | ADDRESS | NAME | TIPE | ADURESS | NAME | IYPE | ADUPESS |
| ı | 1+2 | 4-000160 | J | 1+2 | 4-000164 | К | 1+2 | 4-000102 | L | 1+2 | 4-000166 | | | |
| KKA\$5 | | | | | | | | | | | | | | |
| NAME | 1146 | ALLRESS | 512 | E. | DIMENSI | UNS | | | | | | | | |
| CHAN PRNT SHAUL | L+1 L+1 L+1 | 4+000000 4-000014 F-000002* | 000014 000144 000001 | 0 0 0 | (12) (100) (1) | | | | | | | | | |
| ABELS | | | | | | | | | | | | | | |
| LADEL | AUUF | 200 | LADEL | AUUK | LSS | LABEL | ADDH | (Eas | LABEL | ADDH | LSS | LADEL | AUUR | LSS |
| 43 54 70 | * 1-00 1-00 1-00 | * 0475 1102 0345 | 20 25 30 50 | 1-00 1-00 1-00 + | 1534 0552 1174 | 21 20 31 51 | 1-00 1-00 1-00 | 00216 00626 01266 | 22 27 32 500* | 1-00 1-00 1-00 3-00 | 10272 10702 11366 10000 | 23 28 33 501* | 1-00 1-00 1-00 3-00 | 00422 01002 01460 00010 |

LP.651=LFPEF

and the second second

| URTRAN | IV-FLUS TN | V02-51E /TR:BLUCKS/WR | 13:24:20 | 21-APR-81 | PAGE |
|--------|---------------------------------|---|--|---------------------------------------|------|
| | C C C | THIS SUBROUTINE A POINTON THE CA The Z value at 1 | ACCEPIS THE ICHE MAP SHEI THAT PUINT | X,Y COORDINATES OF ET, AND RETURNS | |
| | C8***** | ****** | ********* | ****** | |
| | C | 6000/00#1 | | ο. D | |
| | c | COMPUTER SCIENCE | SPECIALIST | JR (TRAINEE) | |
| | c | AUTO-CARIU BR | | | |
| | c | TDL, USAETL | | | |
| | С | FORI BELVUIR, VA | l | | |
| | C | 23 AUG 1977 | | | |
| | - L - C * * * * * * * | * * * * * * * * * * * * * * * * * * | ********** | ***** | |
| | C | | | | |
| 1001 | | SUBROUTINE ALICA | ,Y,Z,SN,AZ,I | BZ, IASCD) | |
| 1002 | | INTEGER COEF1 | | | |
| 1003 | | LUGICAL*1 CUEF2 | | 512) COEF2(00 40 2) | |
| 1004 | | DIMENSION COLFIC | (90,40),60F(; 1).FTT2(4).F | 113(4), FITA(4) | |
| 1005 | | CUMMUN /BUUNDS/X | MAXB.YMAXB. | XMINE, YMINE, ELEVE | |
| 1007 | | CUMMUN /NEW/MRDH | { | • - • • | |
| 1008 | | IF(X.UT.XMAXB .A | ND. Y.LT.YM | AXB | |
| | 1 | .AND. X.GT.XMINE | S .AND. Y.GI | YMINB)GO TU 2077 | |
|)009 | | Z=ELEVB | | | |
| 1010 | | A2=V. H7=0 | | | |
|)012 | | RETURN | | | |
| 013 | 2077 | CONTINUE | | | |
|)014 | | DATA IFIRST/0/ | | | |
|)015 | | IF(IFIRSI.GI.U) | GO IO 111 | | |
| 0016 | | IFIRST=1 | | | |
|)018 | | JSAVE=0 | | | |
|)019 | | BURDER=((5.E-4)) | 100./2.54)* | в. | |
|)020 | | FIT=(BURDER/8.) | +9. | - | |
|)021 | | DU 112 K=1,90 | | | |
|)022 | | CALL DSKIRN(4,1, | IERR,K, NRES | , BUF, 0, IDONE) | |
| 1023 | | IF(IERR.GI.0) G(| 10 9999 | | |
| 1024 | | $1 = 4 \neq (1 = 1) + 6 + 3/8$ | | | |
|)025 | | CUEF1(K,J)=BUF(I | .) | | |
| 1027 | | CUEF2(K,J,1)=BUB | ·(L+1) | | |
| 0028 | | CUEF2(K,J,Z)=BUE | ·(L+2) | | |
| 1029 | | COEF2(K,J,3)=BUR | ·(L+3) | | |
| 010 | 114 | CUNTINUE | | | |
| 1031 | 112 | CUNITINUE | | | |
| 1032 | * * * | J=INT((X-BURDER) | ZE11)+1 | | |
|)034 | | 1=1NF((Y-HURDER) |)/F1T)+1 | | |
| 1035 | | J1=J+1 | | | |
| JU30 | | IMUD=1-82 | | | |
| 1031 | | IF(I.LQ.ISAVE.AN | NU.J.LU.JSAV | E) GU TU 80 | |
| 1038 | | - IF(FCP 903 700 1 | 11 0005 7 TO 3338 | | |
|)U4U | | IN=(1MOD=1)+4 | | | |
| | | | | | |

l.

- 45

| FURIRAN IV-PLUS | V02-51E | 13:24:20 | 21-APR-81 | PAGE 2 |
|------------------|--|-------------------------|---|--------|
| ALSLP.FIN | /TR:BLUCKS/WR | | | |
| | | | | |
| 0041 | FIT1(1) = CUEF1(J) | (IMUD) | | |
| 042 | FIT2(1)=COEF1(J) | (IMUD+1) | | |
| 0043 | F113(1)=C0EF1(J1 | ,1MOD) | | |
| 0044 | FIT4(1)=CUEF1(J1 | ,1MOD+1) | | |
| 045 | DO 15 1P=2,4 | | | |
| 0046 | 11≈IB+IP | | | |
| 2047 | 12=18+4+18 | | | |
| 048 | FIT1(IP)=CUEF2(J | 1,1MGU,1P-1) | | |
|)049 | F1T2(1P)=COEF2(J) |],1MUD+1 ,1P• | -1) | |
| 0050 | F113(1P)=CUEF2(J | 11,1MUD,12+1) |) | |
| 0051 | FIT4(IP) = CUEF2(U) | 11,1MUD+1,1P• | -1) | |
| 052 75 | CUNTINUE | | | |
| 3053 80 | CONTINUE | | | |
| 0054 | XC = FLOAT(J=1) * FI | T+BORDER | | |
| 0055 | XL = (X - XC) / F I T | | | |
| 0056 | YC = FLUAr(1-1) + F1 | I+BURDER | | |
| 1057 | XP=(X-XC)\FIL | | | |
| 2028 | xLC=XL-1. | | | |
| 0059 | YLC=YL-1. | | | |
| 3060 | 21 = F1 f1 (1) + F1 f1 (1) | (2) + XL + (FI) | (1(3) + FIT1(4) + XL) + | ΥL |
| 0061 | Z2=F1T2(1)+F112(| .2)*XL + (FI1 | [2(3)+F1T2(4)*XL) * | YLC |
| 0062 | Z3 = F1T3(1) + F1T3(1) | (2) + XLC + (F) | 113(3) + F1T3(4) + XLC | * YL |
| 6000 | 24 = FII4(1) + FII4(1) | .2)*XLC + (E] | $[14(3) + FIT4(4) + \lambda LC]$ | * 71°C |
| 0064 | XL2=ABS(XL++(MRL)) | DR+1)) | | |
| 0005 | XLC2=ABS(XLC++(M | (RUR+1)) | | |
| 0066 | IL2=ABS(IL++(MRL | (R+1)) | | |
| 0067 | YLC2=ABS(YLC*+(P | RDR+IJJ | | |
| 0068 | IF (IASCD.EQ.0)GU | | | |
| 0069 | | | | |
| 0070 | AZZ=F112(2)+F112 | (4)+YLC | | |
| | A23 = F113(2) + F113 |)(4)+1L (\\\+V!) | | |
| 0072 | A24=F114(2)+F114 | | | |
| 0073 | B21=F111(3)+F111 | . (4) * 80 | | |
| 0074 | B42=F112(3)+F112 | ((4)*AL)//)*\// | | |
| 0075 | $D_{4} = F_{1} = (3) + F_{1} $ | | | |
| 0070 200 | | F(4)*X5C | | |
| 0077 200 aa79 | CONTINUE | | | |
| 0078 | | | | |
| | 10C10C | C++))*(*)(C) | | |
| 0000 | | (+3+))*(1DC4 | | |
| 0001 | |)*(Y)CO#(| (-2.++10+3.)) (-2.+V1(+3.)) | |
| | | -3.))*(VI.2*(| $ \begin{array}{c} 2 \\ 2 \\ 3 \\ 3 \\ 3 \\ 3 \\ 3 \\ 3 \\ 3 \\ 3 \\$ | |
| 0000 | H = (X D Z + (-Z + X D + (-Z + X D + (-Z | 1 TA 245 | 2.41543.33 | |
| 0085 | A(w) = 6 + x (C + 1) | - X (C) * (V) C) A | K(=2 #V(C+3 1) | |
| 0085 | $\Delta D M I = 0 \cdot A D C \cdot (I)$ | - XUCJ (IDC2 - | / (-2+710(+3+)) / *Y (+2)} | |
| 0080 | $AD_{2} = b + b + b + (1 + 2)$ | | | |
| 0088 | $\Delta U_A A = 0$, $* X I_A (1 + x)$ | (1.1#(YL.2#(=?) | · * * 1. + 3 .) } | |
| 0089 | HDW1=0, *YLC*(1) | | + = 2 = + X L C + 3 =)) | |
| 0090 | HDw2=6.*+L+(1.=Y | (L)*(XLC2*(=) | 2.*XLC+3.)) | |
| 0091 | BD23=+5, *Y1C+(); | -YLC)*(X1.2*) | (=2, *XL+3,)) | |
| 0092 | DDw4=0.*1L*(L.=Y | (1) + (1) + (-2) | + | |
| 0091 | AZ=Z1+ADa1+Z2+A | N2+23+Δ1)w ++2 | (4*ADw4 | |
| 0094 | AZ=AZ+AZ1*W1+AZ2 | ********** | AZ4*W4 | |
| 0095 | BZ=Z1+BDw1+Z2+BE | W2+23*HIL 3+5 | .4+BDw4 | |
| 0096 | HZ=HZ+HZ1+H1+H23 | *********** | 5%4*w4 | |
| | | | | |

| FORTRAN | IV-PL | US V02-51E | 13:24:20 | 21-APR-81 | PAGE 3 |
|---------|-------|-------------------|----------------|-------------------|-------------------|
| ALSLP.F | TH | /TR:BLOCKS/WH | 4 | | |
| U097 | 205 | Z=Z1*W1+Z2*W2+ | 23**3+24**4 | | |
| 0098 | 210 | CONTINUE | | | |
| | c | WRITE(6,101)/ | Z.BZ.21.22.23 | .Z4.W1.W2.W3,W4, | ADW1,ADW2, |
| | č | 1 . ADW3 . ADW4 E | BDW1.BDW2.BDW3 | .BDw4.AZ1.AZ2.AZ | 3, AZ4, BZ1, BZ2, |
| | č | 1 623.624 | | | |
| 0099 | 101 | FORMAT(1X.2F9 | .4.2X.2(4F9.4 | .2X)./.2(1X.3(4F | 9.4.2%)./).//) |
| 0100 | 100 | FURMAT(1X,15) | 15,2F10.3,F10 | .3./) | |
| 0101 | | JSAVE=J | | | |
| 0102 | | ISAVE=1 | | | |
| 0103 | | IUSVE=10N1T | | | |
| 0104 | | RETURN | | | |
| 0105 | 9999 | WRITE(5,9999) | DIERR | | |
| 0106 | 99991 | FURMAT(11/0 | FAILURE ON DB | 1: - IERR = ', 13 |) |
| 0107 | | SIOP | | - · · · · | - |
| 0108 | 9998 | 2=310. | | | |
| 0109 | | RETURN | | | |
| 0110 | | END | | | |

| FURIRA: Alsept | 14-660 18 | 5 VU2+511 /161866 | : JCK3/AM | [3:24 | :20 21+4 | 422-01 | | PAGE 4 | | | | | | |
|--|--|---|--|--|---|--|---|---|--|---|--|--|---------------------------------------|--|
| PRUGRAM | SECTIO | 145 | | | | | | | | | | | | |
| зимыен | NANE | 817 | ZE | | ATTELEU | lES | | | | | | | | |
| 1 2 4 5 7 | SCUDEI SPDATA SIDAIA SVAFS SIEMFS HUUNUS NEM | 003074 000024 000066 047504 000022 000022 000022 | /98 13 27 10146 9 10 1 | | Kw, 1, CUM Pw, D, CUM Rw, D, CUM Hw, L, CUM Hw, L, CUM Hw, L, CUM Hw, L, CUM | V, LCL V, LCL V, LCL V, LCL V, LCL V, LCL V, GBL | | | | | | | | |
| ENIKI P | UINIS | | | | | | | | | | | | | |
| HAME | 1186 | Aburess | NAME | 1186 | AUDRESS | NAME | 1185 | ALUFESS | LAFE | 1112 | AUDRESS | NAME | LIFE | AUUHESS |
| ALI | | 1-000000 | | | | | | | | | | | | |
| VAR LABL | LS. | | | | | | | | | | | | | |
| HAME | Liter. | AUDRESS | NARE | 1110 | AUGHESS | NAME | 1316 | AUUNE.55 | 6A* E | 1145 | ADDFESS | HAME | 1112 | ADURESS |
| AUW1 Ad1 BUW2 Bd3 F11 IEFK IUN[1 JSAVE MPES A4 ALC2 IC IMAAD 23 | *************************************** | $\begin{array}{c} \mathbf{u} = (\mathbf{u} + 7 + 3) \\ \mathbf{u} = (\mathbf{u} + 7 + 3) \\$ | AUA2 AC2 bLA3 DC4 1 le3ve J1 an A 1 an A 1 L 1 MIND C4 | ныны тарааныны мын жаларарарарарар жарарарарарарар | $\begin{array}{c} 4 - 04/450 \\ 4 - 047470 \\ 4 - 047470 \\ 4 - 047470 \\ 4 - 04750 \\ 4 - 04750 \\ 4 - 04750 \\ 4 - 04750 \\ 1 - 000002 \\ 1 - 04750 \\ 4 - 047334 \\ 4 - 047334 \\ \end{array}$ | ADad AZJ BDA4 BZJ IASCU IMUU II MUU II A A A A A A A A A A A A Z Z | 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | 4-047444 4-047370 4-047474 4-047410 f-00010* 4-047250 4-047230 4-047230 4-047230 4-047240 4-047214 t-000000* | AL#4 AZ4 BGPDER BZ4 Ih 12 L 22 X X X X X X X X X X X X X X X Z 2 X X X Z 2 X | ИМИМЫТТТТНЫМИ ++++++++++++++++++++++++++++++++++++ | 4 - 047454 4 - 047374 4 - 047326 4 - 047226 4 - 047414 4 - 047262 4 - 047262 4 - 047262 4 - 047262 4 - 047250 4 - 047424 4 - 047320 | A2 bUw1 H2 LLEVB LLONE J MRUP +3 ALC Y YL2 22 | H H H H H H H H H H H H H H H H H H H | F=000012* 4=04760 6=000026 4=047242 4=047242 4=047242 4=047242 4=047240 4=047350 4=047350 4=047350 |
| AFFAIS | | | | | | | | | | | | | | |
| NAME | I 1 FE | AUUPESS | 512 | Ł | LINENSI | UNS | | | | | | | | |
| 80F Cuefi Cuefi Fili Fili Fili Fili | H#4 1+2 1+4 H#4 H#4 H#4 | 4-043120 4-000000 4-016040 4-047120 4-047140 4-047140 4-047200 | 004000 016040 025060 000020 000020 000020 000020 000020 | 1024 3000 5400 8 8 8 | (512) (90,40) (90,40) (4) (4) (4) (4) | ;; | | | | | | | | |

LABELS

ļ

Marine Street

¥

LABEL ADURESS

LADEL ALDRESS

LABEL ADDRESS

LAUEL ADURESS

LABEL ADDRESS

and a state of the second state

FUNIKAN IV-PLUS VUZ-517 13124120 21-MPF-B1 PAGE 5 ALSEPTIN /IFIDUUCFS/AF 75 ** 80 1-001102 100' ** 101' ** 111 112 ** 114 ** 200 1-001774 205 1-052700 210 2077 1-000124 9998 1-003052 99999 1-003600 99991' 3-000000

1-000444

FUNCIIUNS AND SUBRUULINES REFERENCED

USPIRA

ľ

į.

1

: E

•

H

i

ţ

IGIAU SPACE ALLUCAILU = 052762 11001 , LP.LSI=ALSLE

| FURTRAN PTS.FTN | IV-PLUS | V02-51E /TR:BLOCKS/WR | 13:25:08 | 21-APR-81 | PAGE |
|--------------------|---------|---|-----------------|----------------------|------|
| | | | | | |
| | С | THIS SUBROUTINE | CALCULATES 1 | THE X,Y POSITIONS OF | |
| | С | ALL POINTS ALON | G A LOS PROF | ILE AT WHICH THE | |
| | С | ELEVATION IS TO | BE CALCULATI | ED | |
| | C | | | | |
| | C***** | ************** | ********** | *********** | |
| | C | DOCOMMENT OVDI | | | |
| | C | PRUGRAM BI CIRU | 5 C, TAYLUR | | |
| | C | | | | |
| | C | AUIU-CARIU BR | | | |
| | C | TOL UNSETI | | | |
| | Č | 10L,0ASE1E | | | |
| | C | 23 AUG 1977 | | V 1979 | |
| | C | TN OPARD TO BE | COMPATIBLE 1 | 1 1979 WITH DUAL | |
| | C | ALTIPUDE/SLOPE | COMPATIBLE | ATTH DORD | |
| | C | SUBRODTINE ALS | LP.FTN. TO B | F USED | |
| | č | BY SHADED RELU | FF PERSPECTI | VF SFTWR. | |
| | č | C. C. TAYLOB | | | |
| | c | | | | |
| | Č***** | *********** | ********** | ************** | |
| | с | | | | |
| | С | | | | |
| 0001 | | SUBROUTINE PTS(| X1,Y1,X2,Y2, | NPTS, B, DLN, IASCD) | |
| 0002 | | DIMENSION B(1) | | | |
| 0003 | | COMMON /BOUNDS/ | XMAXB,YMAXB, | XMINB,YMINB,ELEVB | |
| 0004 | | FNPTS1=FLUAT(NP | TS=1) | | |
| 0005 | | DLN=(SQRT((X2-X)) | 1)**2+(Y2=Y1 |)**2))/FNPTS1 | |
| 0000 | | DX = (X2 - X1)/FNPT | 51 | | |
| 0007 | | DY=(Y2-Y1)/FNPT | 51 | | |
| 0008 | | SN=DY/DLN | | | |
| 0009 | | DO 100 1=1,NPTS | | | |
| 0010 | | FIM1=FLUAT(1=1) | | | |
| 0011 | | X=X1+F1M1+DX | | | |
| 0012 | | | | 1 V () | |
| 0013 | | IF(X.LT.XMAXB . | AND. Y.LT.IM. | AXB | |
| | 1 | AND. A.GI.AMIN | B .ANU. I.GT | .IMINB) GU IU SU | |
| 0014 | | D(1)=ELEVD CO TO 100 | | | |
| 0015 | 50 | | SN N7 67 140 | CD.) | |
| | 30 | - UKUU KUI(A,I,4) - 4(I)=7 | SN/ #6, D6, 1AS | | |
| | 100 | | | | |
| 0010 | 100 | DETIEN | | | |
| 0019 | | L P P P P P P P P P P P P P P P P P P P | | | |
| 0020 | | | | | |

| FURIMA. FIS.FI. | 14-rL | uS vu2⇒51E V[H:#LUK | :+s/at | 13:25 | 108 21-4 | APH = 81 | | PAGE 2 | | | | | | |
|---------------------------------|--|--|------------------------------|-------------------------------------|---|---|--------------------------|---|----------------------|--------------------------|--|-------------------------------|--------------------------|---|
| PRUGRAM | SECT | LNS | | | | | | | | | | | | |
| NUMBER | GAPE. | SLit | : | | AIlkibu | 125 | | | | | | | | |
| ן 1 2 2 | SCLEF SIDAI SVARD SIEMF. DUDNE | 1 000456 A 000032 000052 S 00002 S 000024 | 151 13 21 1 10 | | ни, I, COI <i>Rи, D, CON</i> Rи, D, CON Rи, D, CON Fи, D, CVE | V,LCL V,LCL V,LCL V,LCL P,GBL | | | | | | | | |
| CHIRI P | uihi | | | | | | | | | | | | | |
| NAME | ITPE | ALUKESS | NAME | LIPE | ADDRESS | NAME | TIPE | AUDFESS | NAME | TTPE | ADDRESS | NAME | TYPE | ADUHESS |
| 110 | | 1-00-0000 | | | | | | | | | | | | |
| AMIABL | tə | | | | | | | | | | | | | |
| NAME | 1362 | ALOPESS | NAME | 1 I PE | ADDFESS | NAME | TIPE | AUDFESS | NAME | IYPE | ADDRESS | HAME | TTPE | ALDRESS |
| AL ELEVB NPIS X1 T1 | м#4 Т#5 М#4 М#4 М#4 | 4-030042 6-000020 F-000024 F-000024 F-000024 | 52 F1M1 SN X2 12 | ⊢♥4 ;+♥4 ;+♥4 ;;♥4 ;;♥4 | 4-000040 4-000022 4-000014 F=000000 F=600010* | DLN FNPTSI X Y C | 944 944 944 944 | F+000010* 4-000000 4-000020 4-000032 4-000032 | UX XMAXB YMAXB | H#4 I#2 R#4 £#4 | 4-000004 4-000020 6-000000 6-000004 | UY IASCU Xminb Yminb | H#4 1#2 R#4 R#4 | 4-060016 F-000020* 6-000016 6-060014 |
| AKKAYS | | | | | | | | | | | | • | | |
| NAME | 1:1PE | ALUHESS | 512 | Ł | DIMENSI | UNS | | | | | | | | |
| в | H+4 | F-000014* | 020024 | 4 | (1) | | | | | | | | | |
| LADELS | | | | | | | | | | | | | | |
| LABEL | ADDH | 155 | LABEL | ADDF | ESS | LABEL | ADDH | 655 | LABEL | ADDF | LSS | LABEL | ADDR | E 5 5 |
| 50 | 1-60 | 6356 | 160 | 1-00 | 10432 | | | | | | | | | |
| FUNCILU | NS ANU | SUBROUFIN | ES REFER | ENCED | | | | | | | | | | |
| ALI | SSUR | 1 | | | | | | | | | | | | |
| TUTAL S | FACE A | LLUCATED * | 000610 | 196 | | | | | | | | | | |

.LP.LST=PTS

.

| FORTRAN | IV-PLUS | V02-51E 1 | 3:25:26 | 21-APR-81 |
|----------|---------|--------------------|---------------|---------------------|
| RGSTR.FT | N | TR:BLUCKS/WR | | |
| 0001 | | SUBROUTINE RGSTR | NRAD, SHADE) | |
| 0002 | | LOGICAL*1 SHADE(1 | .) | |
| 6003 | | CUMMON /REG/NRD1, | NRD2, NRD3, N | RD4, NRG1, NRG2, DX |
| 0004 | | IF (NRAD.LE.NRD2.A | ND.NRAD.GE. | NRD1)GU TU 10 |
| 0005 | | IF(NRAD.LE.NRD4.A | ND.NRAD.GE. | NRD3)GO TO 20 |
| 0006 | | GO TO 100 | | |
| 0007 | 10 | IF(NRAD.NE.NRD1)G | O TO 11 | |
| 0008 | | DO 12 J=NRG1,NRG2 | } | |
| 0009 | 12 | SHADE(J)=127 | | |
| U010 | 11 | SHADE(NRG2)=127 | | |
| 0011 | | GU TO 100 | | |
| 0012 | 20 | IF(NRAD.NE.NRD4)G | 0 TO 21 | |
| 0013 | | DO 22 J=NRG1,NRG2 | <u>}</u> | |
| 0014 | 22 | SHADE(J) = 127 | | |
| 0015 | 21 | SHADE(NRG2)=127 | | |
| 0016 | | GU 10 100 | | |
| 0017 | | ENTRY IRGSTR | | |
| 0018 | | NRD4=INT(13./DX+0 | •5) | |
| 0019 | | NRD3=INT(12.5/DX+ | 0.5) | |
| 0020 | | NRD1=INT(1./DX+0. | 5) | |
| 0021 | | NRD2=INT(1.5/DX+0 | .5) | |
| 0022 | | NRG1=1NF(8.5/DX+0 | .5) | |
| 0023 | | NRG2=1NT(9./DX+0. | 5) | |
| 0024 | 100 | RETURN | | |
| 0025 | | END | | |

1 -

1

1

PAGE 1

| FORTRAN RGSTR.F: | EN 18-171 | /TR:BLUG | CK5/WK | 13:25 | :26 21- | APK=81 | | PAGE 2 | | | | | | |
|-----------------------|--|--|-------------------------|--------------|---|--|------------|-----------------------|--------------|------------|----------------------|-------|------|----------|
| PROGRAM | SECTIO | INS | | | | | | | | | | | | |
| NUMBER | NAME | SIZ | E | | ALTRIBU | ILS | | | | | | | | |
| 1 3 4 5 6 | SCUDEI SIDAII SVAKS STEMP: REG | 000462 000012 000002 000002 000002 | 153 5 1 1 8 | | Rw,1,00 Rw,D,00 Rw,D,00 Rw,D,00 Rw,D,00 | DN,LCL DN,LCL DN,LCL DN,LCL DN,LCL (R,GBL | | | | | | | | |
| ENTRY P | INTS | | | | | | | | | | | | | |
| NAME | TYPE | ADDRESS | NAME | LADE | ADDRESS | NAME | TYPE | ADDRESS | NAME | TYPE | ADDRESS | NAME | TYPE | ADDRESS |
| IRGSTR | | 1-000272 | KGSIR | | 1-000000 | | | | | | | | | |
| VARIABL | ES. | | | | | | | | | | | | | |
| NAME | TYPE | AUDRESS | NAME | TYPE | ADDRESS | NAME | TYPE | AUDRESS | NAME | TIPE | ADURESS | NAME | TYPE | AUUHESS |
| DX NRD3 | 143 H44 | 6-000014 6-000004 | NKD4 | 1+2 1+2 | 4-000000 6-000006 | NHAL NHG1 | 1#2 1#2 | F-000002* 6-000010 | NKU1 NKG2 | 1+2 1+2 | 6-000000 6-000012 | NRD2 | 1+2 | 6-000002 |
| ARRAYS | | | | | | | | | | | | | | |
| NAME | TYPE | AUDRESS | 512 | Ł | DIMENSI | UNS | | | | | | | | |
| SHAUL | L+3 | F=000004* | 000001 | U | (1) | | | | | | | | | |
| LABELS | | | | | | | | | | | | | | |
| LASEL | ADDE | 55 | LABEL | ADDR | ESS | LABEL | AUDH | (ESS | LABEL | ADDH | LSS | LABEL | ADUR | 1255 |
| 10 22 | 1-000 | 0052 | 11 100 | 1-00 1-00 | 0142 U432 | 12 | • | • | 20 | 1-00 | 0166 | 21 | 1-00 | 10240 |

TUTAL SPACE ALLUCATED = 000520 108 ,LP.LST=KGS1K

. 4

ľ

1

Ε

| FORIRAN GRNDPT.H | IV-PLUS TN | VU2-51E /1R:BLOCKS/wR | 13:25:59 | 21-APK-81 | 1 |
|---------------------|---------------|-----------------------------|--|-----------------------|-----|
| 0001 | | SUBROUTINE GRND | PT(J,Y,NFLAG | ,X1,YI,1 | |
| | i | ,YMAX, IASCD, AZ, | BZ,Z,11ST) | | |
| | C THIS : | SUBROUTINE IS DE | SIGNED AS A | MURE | |
| | C EFFIC. | IENT IMAGE/UBJEC | 1 CORRELATIO | N ROUTINE | |
| | C THAN | THE URIGINAL GRN | DPT.FTN OF A | UG 78. | |
| | C SEE " | COMPUTER GENERAL | IUN OF SHADE | D RELIEF IMAGES | |
| | C FOR C | ARTUGRAPHIC APPL | ICATIONS" FO | ĸ | |
| | C DOCUM | ENTATION. ALGOR | ITHM AND ROU | TINE | |
| | C BY C. | TAYLOR, 10 AUG | 79 | | |
| 0002 | | COMMON ZAARGHZX | , YU, THETAP, D | NPIS, DX, | |
| | 1 | H, VSF, SCL, TOL, D | ELR, DIS, THEI | A,YIST | |
| 0003 | | CUMMON /HGRAA/2 | 1,22,CSTP,SS | 1P,CST,SST | |
| 0004 | | DIMENSION Y(1) | | | |
| 0005 | | IF (NELAG.EQ.I)G | 6 TO 30 | | |
| 0006 | | | N 4 . | | |
| 0007 | | $\frac{1}{2}$ | 10 | | |
| 0008 | | 21+I(I) 20-V(0) | | | |
| 0010 | | x(1) = -100 | | | |
| 0011 | | Y(2) = H - (Y(2) - Y) | ST)*VSF*SCL | | |
| 0012 | | Y(2) = 7 - (Y(2) + 0) | IS)/(DELK*CS | 1) | |
| 0013 | 10 | CUNTINUE | | | |
| 0014 | | IF (YS.GE.Y(1).A | ND.YS.LE.Y(1 | +1))GU TO 20 | |
| 0015 | | 1=1+1 | | | |
| 0016 | | IF(I.NE.NPIS)GU | TU 70 | | |
| 0017 | | NFLAG=1 | | | |
| 0018 | | GU 10 30 | | | |
| 0019 | 70 | 21=22 | | | |
| 0020 | | $Z_{Z=Y(1+1)}$ | 1. 11. N. 11. 11. 11. 11. 11. 11. 11. 11 | | |
| 0021 | | | 211+A26+2CP | ATT (1 1 ± 1 5 1 5 ± | |
| 0022 | 1 | - I(I+I)=/.=(I(I+ - (ST) | 1)+013)/(FD0 | AI(I)+ULLR+ | |
| 0024 | * | | | | |
| 0025 | 20 | | | | |
| 0025 | | 20=22 | | | |
| 0026 | | 2L=21 | | | |
| 0027 | | A=VSF*SCL | | | |
| 0028 | | ZP=ZU-ZL | | | |
| 0029 | | R=FLUA1(1+1)*0E | LH. | | |
| 0030 | | DELIA=DELF | | | |
| 0031 | | нг=н Н | | | |
| 0032 | | RU=R+DELK | | | |
| 0033 | | 1THIN=0 | | | |
| 0034 | 50 | CUNTINUE | | | |
| | C FULLU | WING LINE COMMEN | TED UUT AFTE | F DE= | |
| | C BUGGI | NG. 17 AUG 79. C | • IAILUR Arid Deiger | 20 21 21 CST | |
| 0025 | 100 | WRITE(0,100)1,0 | ()UEUR,VEUIN) (10 5) | LF,LD,L0,C01 | |
| 0035 | 100 | ANEME(-H+D)Se(Y | 1ST=7L)+A+D] | S=7P+A+RL+DIS/DELT | A) |
| 0017 | | 0EN=(YS+7_)*CST | -2E*A*D15/DF | LIA | - • |
| 0038 | | RAD=ANUM/DEN | | | |
| 0039 | | 11410=11410+1 | | | |
| 0040 | | IF(ITRIN.EQ.25) | GU IU 60 | | |
| 0041 | | XI=X+HAD*CSIP | | | |
| 0042 | | 11=10+KAL*S512 | | | |
| U043 | | 1151=1181+1 | | | |

.

k -

PAGE 1

| FORTRAN | IV-FLUS | VU2-51E | 13:25:59 | 21-APR-01 | PAGE 2 |
|-------------|----------|--------------------|--------------------|-----------|--------|
| GRNUPT.F | TN | /IR:BLUCKS/wR | | | |
| 0044 | | CALL ALT(X1,Y1, | , 2, SN, A2, 62, 1 | (ASCD) | |
| 0045 | | YIRY=H-(Z-YIST) | +VSF+SCL | | |
| 0046 | | YIRY=7(YIRY+D | DIS)/(RAU*CST | [] | |
| 0047 | | YERR=YTRY=YS | | | |
| 0048 | | IF (ABS (YERR) .LT | [.(IUL*DX))G | Ŭ TU 30 | |
| | C TWO PO | DSSIBILITIES:COM | NCAVE AND CUN | VVE.X | |
| 0049 | | IF(YERR.GT.0)GU | J TU 40 | | |
| 0050 | | ZP=2U-2 | | | |
| 0051 | | 21=2 | | | |
| U052 | | RL=RAD | | | |
| 0053 | | DELTA=RU-RL | | | |
| 0054 | | RL=RAD | | | |
| 0055 | | GU TO 50 | | | |
| 0056 | 40 | ZP=Z-ZL | | | |
| 0057 | | 20=Z | | | |
| 0058 | | RU=RAD | | | |
| 0059 | | DELTA=RU-KL | | | |
| 0060 | | GU TU 50 | | | |
| 0061 | 60 | CUNTINUE | | | |
| 0062 | 30 | CUNTINUE | | | |
| 0063 | | RETURN | | | |
| 0064 | | END | | | |
| | | | | | |

Martiner

ليعتاقهم والأستينية

All and the second s

ſ

| FURIRAN IV-PLUS GRNDPI.FIN | VU2-51E /TR:BLUCKS/#R | 13:25:59 | 21-APR-81 | P/ |
|-------------------------------|--------------------------|----------|-----------|----|
| PROGRAM SECTION | 5 | | | |
| | 0175 | | | |

PAGE 3

| | | • | | |
|-------|---------|--------|-----|-----------------|
| UMBER | NAME | SIZ | E | ATTRIBUTES |
| 1 | \$CUDE1 | 001412 | 189 | KH, L, CUN, LCL |
| 3 | SIDATA | 000032 | 13 | RW, D, CON, LCL |
| 4 | SVARS | 000076 | 31 | Re.D.CON.LCL |
| 6 | AARGH | 000066 | 27 | RW, D, OVR, GBL |
| 7 | HGRAA | 000030 | 12 | Rw, D, UVR, GBL |
| | | | | |

ENTRY POINTS

•

J ----

NAME TYPE AUDRESS NAME TYPE ADDRESS Grndpt 1-000000

VARIABLES

| NAME | TYPE | ADDRESS | NAME | LAbe | ADDRESS | NAME | TYPŁ | ADDRESS | NAME | TYPE | ADDRESS | NAME | TYPE | ADDRESS |
|-------|------|-----------|------|------|-----------|------|------|-----------|-------|------|-----------|--------|------|----------|
| A | H#4 | 4-000014 | ANUM | H#4 | 4-000046 | AZ | R#4 | F-000022+ | 82 | K#4 | F=000024= | CST | H+4 | 7-000020 |
| CSTP | R#4 | 7-000010 | D | H+4 | b-000014 | DELR | R#4 | 6-000046 | DELTA | R#4 | 4-000030 | DEN | R#4 | 4-000052 |
| UIS | R+4 | 6-000052 | UX. | K#4 | 6-000022 | н | 8*4 | 6-000026 | 1 | 1+2 | F-000014* | IASCU | 1+2 | F-000020 |
| ITRIN | 1+2 | 4-000044 | ITST | 1+2 | F-000030* | J | 1+2 | F-0000024 | NFLAG | 1*2 | F-000006* | NPTS | 1#2 | 6-000020 |
| R | R#4 | 4-000024 | RAD | R#4 | 4-000050 | RL | H+4 | 4-000034 | RU | R#4 | 4-000040 | SCL | R#4 | 6-000036 |
| SN | H44 | 4-000062 | SST | H#4 | 7-000024 | SSTP | R#4 | 7-000014 | THETA | R#4 | 6-000056 | THETAP | 8*4 | 6-000010 |
| TOL | H#4 | 6-000042 | ¥ 5F | 14+4 | b-000032 | x | 6.44 | 6-000000 | XI | K+4 | F-000010* | TERR | R#4 | 4-000072 |
| 11 | H+4 | F=000012* | YMAX | 844 | F-000016+ | YS | 4*4 | 4-000000 | THY | R*4 | 4-000066 | 10 | R#4 | 6-000004 |
| TIST | H+4 | b=000062 | Z | R+4 | F=000026* | ZL. | R#4 | 4-000010 | ZP | 8*4 | 4-000020 | ZU | R#4 | 4-000004 |
| Z1 | H#4 | 7-000000 | Z2 | k#4 | 7-000004 | | | | | | | | - | |

AFRAYS

| NAME | TYPE | ADDRESS | SIZE | | DIMENSIONS |
|------|------|-----------|--------|---|------------|
| ۲ | K=4 | +-000004+ | 000004 | 2 | (1) |

LABELS

| LAULL | ADURESS | LABEL | AUDRESS | LABEL | ADURESS | LABEL | AUDRESS | LABEL | ADDRESS |
|----------|----------------------|----------|----------------------|-------|----------------|-------|----------|-------|----------|
| 10 60 | 1-000232 1-001402 | 20 70 | 1-000504 1-000332 | 100° | ** 1-001410 | 46 | 1-001322 | 50 | 1-000626 |

FUNCTIONS AND SUBRUUTINES REFERENCED

ALT

TUIAL SPACE ALLOCATED = 001660 472

FORTRAN IV-PLUS V02-51E 13:25:59 21-APR-81 GRNDPT.FTN /TR:BLOCKS/WR

, LP.LST=GRNDPT

والمقودين ويهدوها ساليها

في المحمد المربية الم

SSLPLP/PR:0/FP/CP/NOTR=SSLPLP,[300,300]DSKTRN SLPS,ALSLP,LPPER,SXSY,QUAN1,RCSLP / UNITS=21 ASG=T1:1,T1:6 ASG=T1:8 ASG=DB0:14,DB2:12 //

ŝ

| FORTRAN SSLPLP.F | 1 V 7 N | -PLUS | V02-51E /TR:BLOG | CKS/WR | 13:2 | 7:02 | 21-APR+ | 91 | PAGE | 1 |
|---------------------|------------|-----------------|----------------------|------------------------|--------------|--------------------|---|--------------|------|---|
| | C C | THIS P MAGNE | ROGRAM V TIC TAPE | NILL PROP E FILE CO | | AN OUTI NING TI | PUT 9 TRAG | CK | | |
| | č | DENSI | TIES OF | AN URTH | UNORM | AL IMA | GE OF A U | SER- | | |
| | Ĉ | SELEC | TED ARE | A UF THE | CACH | E, OK I | MAP SHEET | • | | |
| | С | THE U | SER MAY | SELECT I | BETWE | EN TWO | FORMULA I | FOR | | |
| | С | THE D | ETERMIN | ATION OF | THE | GRAY SI | HADES, SPI | ECIFY | | |
| | С | THE P | OSITIUN | UF THE | SUN, | THE PI | KEL DENSI | ΓΥ, | | |
| | С | AND A | VERTICA | AL SCALI | NG FA | CTUR. | | | | |
| | C | | | | | | | | | |
| | C 4 | ***** | ****** | ******* | * * * * * | ***** | ******** | **** | | |
| | C | nnoar | | | | | | | | |
| | c | | AM BI CI | IRUS IAI Procesee | V LDA | NC H | | | | |
| | č | FNCIN | FFD TOD | CRAPHIC | | aven - | | | | |
| | č | FURT | BELVOIR | . VA | UNDU | | | | | |
| | č | 27 JU | NE 1978 | , ,,, | | | | | | |
| | č | | | | | | | | | |
| | Ē | ***** | ****** | ****** | **** | ***** | ******** | **** | | |
| | С | DIMENS | ION THE | TWU ARA | YS TH | AT WIL | L | | | |
| | С | CUNTA | IN THE L | DATA PTS | FOR | TWO SU | CCESIVE | | | |
| | С | ELEVA | TION PRO | FILES. | THES | E WILL | BE | | | |
| | С | USED | TO DETER | RMINE TH | E LUC | AL SLU | PE OF | | | |
| | C | THE T | ERRAIN, | wHICH, | TOGET | HOR WI | TH OTHER | | | |
| | C | USER | DETERMIN | NED FACI | UKS, | DETERM. | INES | | | |
| 0001 | C | Inc 1 | NIENSII. DIMENSII | I UP INE | REFL 074) | 87X(10) | 51681. 24) | | | |
| 0001 | c | | THE BY | LE VEBVA | CUN1 | AINING | 29) Thf | | | |
| | c | DEL LICE | TY INFO | RMATION: | | ARRAY | WILL BE | | | |
| | č | - WK1TI | EN TO T | APE. | | | | | | |
| | ē | *FULLC | WING ST | ATEMENT | ADDED | R. RO. | SENTHAL 2 | /13/79 | | |
| 0002 | | | DIMENSI | DN IPYTE | S(10) | | | | | |
| | С | FULLUW | LING LIN | E ADDED | FOR 1 | IME ST. | ATEMENT | | | |
| | С | C. IAi | LUR. 26 | AUG 197 | 9 | | | | | |
| 6000 | | | DIMENSI | ON ALIMO | 2) | | | | | |
| 0004 | | | LUGICAL | *1 SHADE | (1024 | | | | | |
| 0005 | | | CUMMUN . | BUUNDS/ | | COSEL | , AMIND, IM | IND, ELEVD | | |
| 0000 | | | CUMMON . | / SEAI/DE | LIAG, | CUSEL | TAPON' WIG | ,(1,(2,51,52 | | |
| 0007 | | | | | г Чр./.Х | MINH | 17727. YMA | X8/21 59/ | | |
| 0000 | | | UATA YM | INB/.177 | 2/.EL | EVBZ31 | 0./.IUNIT | /0/.KUDE/=1/ | | |
| 0010 | | | DATA MUI | DE/U/, IP | AR/U/ | , IDEN/ | 0/.1CTL/1 | 28/ | | |
| 0011 | | | DATA KO | UNT/128/ | | • | • • • • • • | - | | |
| 0012 | | | IERR=0 | | | | | | | |
| 0013 | | | MRDR=1 | | | | | | | |
| 0014 | | | ¥I=3.14 | 159 | | | | | | |
| | С | WE HA | VE NUW | INITIALI | ZED I | APIRN I | FUR LUN1 | | | |
| | C | NOW N | E WILL C | JPEN THE | DISK | FILES | | DUM 1024 | | |
| 0015 | | | CALL DSI | NF15(4/* | I, DE | 50°, 'CA | CHEI.DAT. | ,DUM,1024 | | |
| | c | 1 | TODEN CIN | LAG, LERR Trai tvd | ノ トーナハ1 | | | | | |
| | c | 1 | RECURDS | 178=443. | SHARF | D.ASSO | CIAIEVARI | ARLF=IV) | , | |
| 0016 | C | 4 | IF(IERR | .LU.U)GU | 10 6 |) | ~ • · · · · · · · · · · · · · · · · · · | | | |
| | с | ALL WH | TIE STA | TEMENTS | MUUIF | 1LD 10 | | | | |
| | Ċ | WRITE | TO UNII | 1; 1.E. | , ALL | STATE | MENTS | | | |
| | С | 'WFITE | (5, CH | ANGED TU | WRII | ε(1, . | • • | | | |
| | C | CHANGE | S MADE (| IU ALLOW | DELA | AFD RU | NNING | | | |
| | | | | | | | | | | |

ſ

| FURTRAN | IV-PLUS | V02-51E | 13:27:02 | 21-APR-81 | PAGE 2 |
|----------|----------|-------------------------------------|-----------------------------|-------------------|-----------------|
| SSLPLP.F | TN | /TR:BLOCKS/WR | | | |
| | C OF SC | FTWARE, C. TAYL | OR. 26 AUG | 1979 | |
| 0017 | | WRITE(1,104) [EH | R,IFLAG | | |
| 0018 | 104 | FORMAT(" OPEN F | AILURE ON I | DB1:CACHE1.DAT' | ,213) |
| 0019 | | STOP | | | |
| | C6 | CONTINUE | | | |
| 0020 | 6 | CALL DSKF1L(2, | 1, DB0, St | DRLF.DAT',DUM,51 | 12, |
| | 1 | 1024, IFLAG, IERF | | | |
| | C | OPEN(UNIT=9,NAM | E= FUR005.1 | DAT', TIPE='ULD', | ACCESS= |
| | C 1 | *DIRECI*, READUR | LI, RECURDS | L2E=400, | |
| 0001 | C I | SHARED, ASSUCIAL | EVARIADUE=1 | [W] | |
| 0021 | | | , 10 1 | | |
| 0022 | 107 | WRITE(1/10/)IC | NN NATURE ON B | 981+SD81.F DAT! | (3) |
| 0023 | 107 | STOP | ATBOKE ON I | DI.OUKUPORT // | |
| 0024 | 7 | CONTINUE | | | |
| 0023 | C NUL SI | T PARITY AND DE | NSITY OF TA | APE | |
| | C NUW DE | FINE PARAMETERS | 5 | | |
| | C *NEXT | 7 LINES ADDED H | . ROSENTHAL | 2/13/79 | |
| 0026 | | WRITE(1,*)' ENT | ER DEVICE | AND FILE NAME: | "DDN:FILE.EXT" |
| 0027 | | wRITE(1,*)" TO | INPUT FROM | TERMINAL ENTER | ''Tl:''' |
| | C NEXT : | TWO READ STATEM | ENTS ALTEREI | D TO READ FROM | |
| | C UNIT | 4 IN ORDER TU AI | LOW DELAYER |) RUNS | |
| 0028 | | READ(8,5555)IB | (TES | | |
| 0029 | 5555 | FURMAT(10A2) | | | - |
| 0030 | | wRITE(1,*) ' NU! | ABER OF CHAI | RS IN FILE NAME | • |
| 0031 | | READ(8,*)NBYTE | | | |
| 0032 | 0 | CALL ASSIGN (4) | IBXIES, NBY | [20] | |
| | C PHOND | J COMMENIS ENII 1 Indite Ade Min | LKED K. KUSI Ledim inite | A 2/13/17 | |
| | C PROMP | DARAMETERS MAY | NOW BE REAL | TEROM DISK FIL | ES |
| | C CHANG | ES MADE TO "REAL |)(5,+)' NOW | 'READ(4,*) | |
| EEOU | 20 | CONTINUE | | | |
| 0034 | | WRITE(1,100) | | | |
| 0035 | 100 | FORMAT(1X, "ENT | ER MAPSHEET | COORDINATES OF | LOWER LEFT-HAND |
| | 1 | *,/,1X,* AREA | OF INTERES | 1') | |
| 0036 | | READ(4,*)XLL,Y | հն | | |
| 0037 | | wRITE(1,101) | | | |
| 0038 | 101 | FORMAT(1X, 'ENT | ER HEIGHT A | NO WIDTH OF ARE | A OF INTEREST J |
| 0039 | | READ(4,*)H,W | 131.351523 A.M | CTOUSTNO DUNCT | ON TO WE DEED! |
| 0040 | 130 | FURMALL ENTER | UKDER UF WI | EIGHIING FUNCII | UN TO BE USED J |
| 0041 | | - WRLIGLI/104) - SUUMATRILY (NT) | | | 6° * 1 |
| 0042 | 102 | DEADLA + NDIX | CR # FIALDO | THORIZONING DIM | 2) |
| 0043 | | WRTTE(1.103) | | | |
| 0045 | 103 | FURMAT(1X. 'ENT | ER VERTICAL | SCALING FACTUR | ') |
| 0045 | 100 | READ(4.*)VSF | | | • |
| 0041 | | WRITE(1,106) | | | |
| 0048 | 100 | FURMAT(1X, 'ENT | ER O FOR LA | MBERTS LAW, ',/, | 1X, |
| | 1 | 1 FOR THE LOM | MEL-SEELIGE | R LAW") | |
| 0049 | | READ(4,*)LAw | | | |
| 0050 | | WRITE(1,105) | | | |
| 0051 | 105 | FORMAI(" ENTER | ANGLE OF E | LEVATION OF LIG | HI, T, Z, T |
| | 1 | DIRECTION OF L | IGHT (O=FRU | W N'AA LKAW F). | . / . |
| | 1 | - AZIMUTHAL VA | KIATIUN"J | | |
| 0052 | | KEAU(4,*JE61,A | MT ¹ KATEMI | | |
| 0023 | | MKLIC(1/131) | | | |

ŀ

| FORTRAN SSLPLP. | IV-PLUS FTN | V02-51E /[R:BLOCKS/WR | 13:27:02 | 21-APR-81 | PAGE 3 |
|--------------------|----------------|---|-----------------|-----------------|--|
| 0054 | 131 | FORMAT(1X, 'RELI | EF CONTOURS | Y=1./.CONTOUR | |
| | 1 | INTERVAL (M)") | | • | |
| 0055 | | READ(4,*)IRELCN | ,ICON | | |
| 0056 | | IVSUN=0 | | | |
| | C FULLO | WING 3 LINES ADD | ED FOR DCMN1 | IN PURPOSES | |
| | C C. TA | YLOR, 26 AUG 197 | 9 | | |
| 0057 | | CALL TIME(ATIM) | | | |
| 0058 | | WRITE(1,134)(AT | IM(IJKL),IJI | (L=1,2) | |
| 0059 | 134 | FORMAT(1X,2A4) | | | |
| 0050 | | IF(RVIEWI.GT.I. | JIVSUN=1 | | |
| 0051 | | ANI=ADS(ANI) | | | |
| 0062 | | AN=90.=ANI FI=(FI1+2 14150 | 1/100 | | |
| 0063 | | $\Delta N = (\Delta N \pm 2 - 1 A + 5 Q)$ | /180 | | |
| 0065 | | ANG=((135.*3.14 | 159)/180.)=/ |) N | |
| 0066 | | RVIEW=RVIEW1*PI | /360. | | |
| 0067 | | RVIEw=(P1=2.*RV | IEw)/2. | | |
| •••• | C NOW DI | EFINE PARAMETER- | DEPENDANT VI | RIABLES | |
| 0068 | • • • • • | DELTA=W/FLOAT(N | PIX) | | |
| 0069 | | CNVRT=0.0007874 | 016 | | |
| 0070 | | CNVRT=1./CNVRT | | | |
| 0071 | | IF(IRELCN.EQ.1) | VSF=TAN(EL) | FCNVRT#(DELTA/I | CON) * VSF |
| 0072 | | DELTAP=DELTA/((| (5.E+4)+100 | /2.54)*9.} | |
| 0073 | | DELTAG=(DELTA*5 | 0000.)*(2.54 | 1/100.) | |
| 0074 | | NPTS=NPIX+1 | | | |
| 0075 | | XEND=XLL+W | | | |
| 00/6 | - | LSTRW=H/DELTA | | | |
| | C +FOFF | UWING LINE INSER | TED R. RUSEI | VIHAL 16-FEB-79 | |
| 0077 | | NUMRWS=LSTRW+I | n | | |
| 3078 | | | 2 | | |
| 5079 | C HOW P | RECISE ARE THE F | OLLOWING? | | |
| 1080 | | C1=COS(-RVIFW+3 | .*PI/4.) | | |
| 2081 | | C2=COS(=RVIEw+P | 1/4.) | | |
| 2082 | | S1=SIN(RVIEW+3. | *P1/4.) | | |
| 2083 | | S2=SIN(RVIEW-PI | /4.) | | |
| 2084 | | SY=COS(EL) +SIN(| AN) | | |
| 2085 | | SX=COS(EL)+COS(| AN) | | |
| 3086 | | SZ=SIN(EL) | | | |
| 2087 | | COSEL=COS(EL) | | | |
| | C ESTAB | LISH DENSITY SCA | LING FACTOR | | |
| | C ASS | UME DMAX=127 COR | RESPONDS TO | | |
| | C 10 | DENSITY OF 2.3 | | | |
| 2000 | C | DSCL=12/./2.3 | | | |
| 1088 | | WKITE(1,111) | DSCI (66 3) | • • | |
| 1083 | 111 | FURMALL' ENIER | DOCT (22.5) | , | |
| 1090 | 115 | FODMAT(+ FNTED | 1 TO DUMP FI | FVATIONS | |
| 1092 | 115 | WRIPE(6.112)XLC | YUL-H.W | | |
| 2093 | 112 | FORMAT(1XLL.YL | L=('.E7.3.' | E7.3. ').r | (************************************* |
|)094 | | WRITE(6.113)NPI | X, VSF, LAW, MI | RDR | |
|)095 | 113 | FORMAT(' NPIX=' | ,13,' VSF=' | F7.3 JAX=" | ., 'MRDR= ',13) |
| 2096 | | WRITE(6,114)EL1 | ,AN1,USCL,R | IEW1, NUMEWS | |
| 2097 | 114 | FURMAT(' EL=',F | 7.3, AN=', F | 8.3,'DSCL=',F7. | 3, 'RVIEW=', |
| | | 1F8.2, NUMBER U | F RUWS=",14 | ,//) | - |
| | C #ABUV | E 3 LINES, ADDIT | ION TO WRITH | E STATEMENT ADD | ED R. ROSENTHAL |

| FURTRAN SSLPLP.F | IV-PLUS TN | V02-51E /TR:BLOCKS/WR | 13:27:02 | 21-APR-81 | PAGE |
|---------------------|---------------|---------------------------------|-----------------------|-----------------------|---------|
| | / ESTABL | | | | |
| 1000 | C LOINDE | DD 1000 IBDw+0 I | CTDE | | |
| 1038 | | VCUD-VCUD-DELTA | 191KM | | |
| 1099 | | ICUR=ICUR+DELTA | | | |
| 0100 | | IF (IRELCN.EQ.I)G | 10 TU 132 | | |
| 0101 | | CALL SLPS(XLL,YC | UR, XEND, YCUR | ,NPIX,AZA,BZA,DLN) | |
| 0102 | | GU TO 133 | | | |
| 0103 | 132 | CALL RCSLP(XLL,Y | CUR, XEND, YCU | R,NPIX,AZA,6ZA | |
| | 1 | ,DLN, ICON, DELTAP | ·) | | |
| 0104 | 133 | CONTINUE | | | |
| 0105 | | IF(LAW.EV.1)GU T | 0 11 | | |
| 0106 | | DO 13 1P1X=1,NPI | X | | |
|)107 | | AZ=AZA(IP1X)*DEL | TAP | | |
| 0108 | | BZ=BZA(IPIX)*DEL | TAP | | |
| 0109 | | AZ=AZ*VSF | | | |
| 1110 | | 82=82*VSF | | | |
|)111 | | CALL SXSY(SX.SY. | AZ . 821 | | |
| 1112 | | $BFG = +SX + \Delta 7 + DFL TA$ | G-SYXDELTAGE | 87+061.508+57 | |
| 1112 | | DIS-SOPT((A7*DE) | .TAC1**2+(DEL | TAC+271++2+(DF1 SOP++ | 211 |
| 1113 | | CUST-HECKDIS | 1 KG) + + 2 + (DE L | ING+D2J++2+(DELSQK++ | . 4 3 3 |
| /114 | CODACIT | COST-BEG/DIS | 00000000000 | 1-100061 | |
| | C UPACII | 1-1/10, DENSIII-L | TO HE CHANCE | 1=100051 | |
| | C NOIE:D | LACOCI LE LAVE | TU DE UNANGE | D | |
| 115 | | | JCUSI=.00001 | | |
| 116 | | SHAD=ALUG10(1./C | 051) | | |
| 11/ | | SHAD=SHAD+USCL | - | | |
| 118 | | IF (SHAD.GT.127.) | SHAD=127. | | |
| 119 | | SHADE(IPIX)=SHAD |) | | |
| 120 | 13 | CUNTINUE | | | |
| 121 | | GO TU 1500 | | | |
| | C NUW DE | AL WITH THE LUMM | EL SEELIGER | CASE | |
| 122 | 11 | CUNIINUE | | | |
| | C | DIFFERENTIATE BE | IWEEN EVEN A | ND UDD ROWS | |
| 123 | | DU 19 1PIX=1,NP1 | Χ | | |
| 124 | | AZ=AZA(1PIX)*DEL | TAP | | |
| 125 | | BZ=BZA(IPIX)*OEL | TAP | | |
| 120 | | AZ=AZ+VSF | | | |
| +127 | | BZ=BZ*VSF | | | |
| 128 | | CALL SXSY(SX.SY. | AZ, BZ) | | |
| 129 | | BEG=DELTAG*(-SX* | AZ=SY*HZ)+DE | LSOR*SZ | |
| -1.40 | | DIS=SORT((AZ*DEL | (TAG) * * 2 + (BZ * | DELTAG) ##2+(DELSOR## | (2)) |
| 1131 | | CUSE=DELSORZDIS | | | - / / |
| 1112 | | COS1=BEGZD15 | | | |
| 1144 | | LECCUST LT 1. F=5 | ACASI= 00001 | | |
| 1 1 4 4 | | SHAD=1 / (1 + (COS)) | (COSI)) | | |
| .132 | | | | | |
| .132 | | TERESAN IT A YES | | | |
| 130 | | IF (SHAD. CI. 1) | AU-U. | | |
| 137 | | IF (SHAD.GI.12/.) | SHAD=127. | | |
| 138 | | SHADELIPIXJESHAD |) | | |
| 133 | 19 | CUNTINUE | | | |
| 140 | 1500 | CUNTINUE | | | |
| | C NUW WH | ITE II UUT TO DI | .SK | | |
| 141 | | JRUW=IRUW+1 | | | |
| 142 | | CALL DSKTRN(2,2, | IERE, JRUW, NE | ES, SHADE, | |
| | 1 | 0, LDUNE) | | | |
| 143 | | IF (IERR.EQ.0)GU | TU 15 | | |
| 144 | | wRITE(1,108)1EFF | ι | | |
| 145 | 108 | FURMAIL' DSKIRN | FAILURE: 1.13 | . J | |

| UKTRAN SLPLP. | IV-PLUS FTN | VU2-51E /TR:BLUCKS/wR | 13:27:02 | 21-APR-81 | PAGE 5 |
|------------------|----------------|--------------------------|---------------------|------------------|---------|
| 140 | | STOP | | | |
| 147 | 15 | CONTINUE | | | |
| 148 | 1000 | CONTINUE | | | |
| | C WRITE | AN END OF FILE | MARKER | | |
| 149 | | IF (NPIX.GI.100 |))GU TU 1501 | | |
| 150 | | DO 1502 JFIL=1, | JRUW | | |
| 151 | | CALL DSKTRN(2,1 | , IERR, JFIL.N | RES, SHADE. | |
| | 1 | 0,IDONE) | | | |
| 152 | | IF(IERR.EQ.0)GC |) TÚ 16 | | |
| 153 | | wRITE(1,108)1EF | R | | |
| 154 | | STUP | | | |
| 155 | * • | CONTINUE | | | |
| 156 | | CALL LP(SHADE) | | | |
| 157 | 1502 | CONTINUE | | | |
| 158 | 1501 | CUNTINUE | | | |
| 159 | | CALL TIME(ATIM) |) | | |
| 100 | | wRITE(1,134)(A1 | Marting (IJKL), IJK | L=1,2) | |
| 161 | | wRITE(1,109) | | | |
| 162 | 109 | FORMAT(ANOTHE | R IMAGE:ENTE | R 1') | |
| 163 | | READ(4,110)IANS | 5 | | |
| 104 | 110 | FORMAT(I4) | | | |
| 105 | | IF (IANS.EQ.1)GC |) TU 20 | | |
| 166 | | CALL USKFIL(4,- | 2, 'DEU', 'CAC | HE1.DAT', DUM, 1 | 024,100 |
| | 1 | ,IFLAG,IERR) | | | |
| 167 | | CALL DSKF1L(2,- | 2, DE0 , SDR | LF.DAT', DUM, 51 | 2,1024 |
| | 1 | ,1FLAG,1ERR) | | | |
| 108 | | STOP | | | |
| 169 | | END | | | |

| 1 | SCODE | 1 004104 | 1082 | | R#,1,00 | N, 5C6 | | | | | | | | |
|--------|-------|----------|--------|------|----------|--------|------|----------|--------------|-------|----------|--------|------|----------|
| 4 | SPDAT | A 000306 | 99 | | RW,D,CU | N,LCL | | | | | | | | |
| 3 | SIDAT | A 001574 | 440 | | RW,D,CO | NICL | | | | | | | | |
| • | SVARD | 022312 | 4109 | | RW,U,CU | N,LCL | | | | | | | | |
| 5 | STEMP | 5 000014 | .0 | | RW,D,CU | N,LCL | | | | | | | | |
| 6 | BOUND | 5 000024 | 10 | | Rw,D,OV | R,GBL | | | | | | | | |
| 1 | SEXY | 000036 | 15 | | Rw,D,OV | R,GBL | | | | | | | | |
| 8 | NEW | 000002 | 1 | | RW,D,OV | R,GBL | | | | | | | | |
| ARIABL | ŁS | | | | | | | | | | | | | |
| NAME | TTPE | ADDRESS | NAME | IXPE | ADDRESS | NAME | TYPE | ADDRESS | NAME | 1 YPE | ADDRESS | NAME | TYPE | ADDRESS |
| AN | 8+4 | 4-022142 | ANG | R#4 | 7-000012 | AN1 | R#4 | 4-022124 | AZ | R#4 | 4-022244 | BEG | R*4 | 4-022254 |
| BZ | R#4 | 4-022250 | CNVRT | R#4 | 4-022162 | COSE | R#4 | 4-022274 | COSEL | k#4 | 7-000004 | COSI | R*4 | 4-022264 |
| C1 | R+4 | 7-000016 | C 2 | R#4 | 7-000022 | DELSOR | R#4 | 4-022204 | DELTA | R#4 | 4-022156 | DELTAG | R*4 | 7-000000 |
| DELTAP | K*4 | 4-022166 | 015 | k#4 | 4-022260 | DLN | R#4 | 4-022236 | DSCL | 2*4 | 4-022230 | DUM | R#4 | 4-022060 |
| EL. | H+4 | 4-022146 | ELEVH | R+4 | 6-000020 | EL1 | R#4 | 4-022120 | н | H#4 | 4-022100 | 1ANS | 1+2 | 4-022310 |
| ICUN | 142 | 4-022136 | ICTL | 1#2 | 4-022046 | IDEN | 1+2 | 4-022044 | IDONE | 1#2 | 4+022304 | IERR | 1+2 | 4-022052 |
| 1FLAG | 1+2 | 4-022064 | 13KL | 1+2 | 4-022140 | 1PAR | 1*2 | 4-022042 | IPIX | 1+2 | 4-022242 | IRELCH | 1*2 | 4-022134 |
| IKOM | 1+2 | 4-022234 | IUNIT | 1+2 | 4-022034 | IVSUN | 1#2 | 7-000010 | J11L | 1*2 | 4-022306 | JROW | 1+2 | 4-022300 |
| KODE | 1+2 | 4-022036 | KOUNT | 1#2 | 4-022050 | LAW | 1+2 | 4-022116 | LSTHW | 1+2 | 4-022200 | NODE | 1*2 | 4-022040 |
| MRDR | 1+2 | 8-000000 | NBYTES | 1+2 | 4-022066 | NPIX | 1+2 | 4=022110 | NPTS | 1+2 | 4-022172 | NRES | 1*2 | 4-022302 |
| NUMR#S | 1+2 | 4+022202 | PI | R#4 | 4-022054 | RVIEW | R#4 | 4=022152 | RVIEW1 | R#4 | 4-022130 | SHAD | R*4 | 4-022270 |
| SA | K#4 | 4-022220 | SY | R#4 | 4-022214 | 5Z | R+4 | 4-022224 | S 1 | R#4 | 7-000026 | \$2 | K#4 | 7-000032 |
| VSF | H+4 | 4-022112 | in | R#4 | 4-022104 | XEND | R#4 | 4-022174 | XLL | R#4 | 4-022070 | XMAXB | R#4 | 6-000000 |
| XMINB | H#4 | 6-000010 | YCUR | R#4 | 4-022210 | YLL | 8#4 | 4-022074 | YMAXB | K*4 | 6-000004 | YMINB | R#4 | 6-000014 |
| | | | | | | | | | | | | | | |
| ANNAYS | | | | | | | | | | | | | | |

| | TYDE | ADDRESS | \$17 | | DIMENSION | | |
|---------|------|----------|--------|------|-----------|--|--|
| MARE | 1165 | AUDACOD | | | 010200100 | | |
| ATIM | H#4 | 4-020024 | 000010 | 4 | (2) | | |
| AZA | 894 | 4-000000 | 010000 | 2048 | (1024) | | |
| BZA | R#4 | 4-010000 | 010000 | 2049 | (1024) | | |
| IBITES. | 1+2 | 4-020000 | 000024 | 10 | (10) | | |
| SHADE | 1.41 | 4=020034 | 002000 | 612 | (1024) | | |

URINAN IV-PLUS VO2-51E SLPLP.FTN /IR:BLUCKS/#R

512E

RUGHAM SECTIONS

UMBER NAME

ABELS

| LABEL | ADDRESS | LABEL | ADDRESS | LABEL | ADDRESS | LABEL | ADDRESS | LABEL | ADDRESS |
|-------|----------|-------|----------|-------|----------|-------|----------|--------|----------|
| 6 | 1-000136 | 7 | 1-000220 | 11 | 1-003060 | 13 | ** | 15 | 1-003560 |
| 16 | 1-003714 | 19 | ** | 20 | 1-000406 | 100* | 3-000116 | 101* | 3-000230 |
| 102* | 3-000306 | 103* | 3-000350 | 104* | 3-000000 | 105* | 3-000510 | 106* | 3-000412 |
| 107* | 3-000046 | 108. | 3-001212 | 109* | 3-001240 | 110' | 3-001272 | 111' | 3-000750 |
| 112' | 3-000776 | 113* | 3-001046 | 114" | 3-001116 | 1151 | ** | 1 30 * | ** |
| 131' | 3-000662 | 132 | 1-002462 | 133 | 1-002500 | 134* | 3-000742 | 1000 | |
| 1500 | 1-003464 | 1501 | 1-003746 | 1502 | ** | 5555' | 3-000112 | | |

13:2/:02 21-APR-61

ATIRIBUTES

PAGE 6

きちょう

and the second sec

. ţ

-

きつうざき

FURTHAN IV-PLUS VU2+SIE 13:27:UZ 21-APR-81 PAGE 7 SSLPLP.FTN /IN:BLUCNS/NM

FUNCTIONS AND SUBROUTINES REFERENCED

ADDIGN UDATEL UDATER LP ROOLP DERD DADY TIME SALGIU SCUD SDIN SSURT STAN

. . .

EDIAL SPACE ALLUCATED = 030704 - 6368 ,LP,LST=SSLFLF
| FURTRAN SLPS.FTM | IV-PLUS | V02-51E /TR:BLOCKS/wR | 13:28:00 | 21-APK-81 | PAGE | 1 |
|---------------------|-------------|--|---|--|------|---|
| | C C C | THIS SUBROUTINE ALL POINTS ALGNO ELEVATION IS TO | CALCULATES T S A LOS PROFI BE CALCULATE | THE X,Y POSITIONS OF LE AT WHICH THE D | | |
| | C****** | | ****** | ****** | | |
| | C++++++ | ***** | | ***** | | |
| | C C | PROGRAM BY CYRUS | C. TAYLOR | | | |
| | č | AUTO-CARIO BR | | | | |
| | C | TDL.USAETL | | | | |
| | č | TDL.UASETL | | | | |
| | č | 23 AUG 1977 | | | | |
| | č | | | | | |
| | C***** | ************** | ********* | ****** | | |
| | с | | | | | |
| | С | | | | | |
| 0001 | | SUBROUTINE SLPS | Χ1,Υ1,λ2,Υ2, | NPTS,AZA,BZA,DLN) | | |
| 0002 | | DIMENSION AZA(1) | ,BZA(1) | | | |
| 0003 | | COMMON /BOUNDS/) | (MAXB,YMAXB,X | MINB,YMINB,ELEVB | | |
| 0004 | | FNPTS1=FLOAT(NPT | (S=1) | | | |
| 0005 | | DLN=(SQR1((X2-X) |)**2+(Y2=Y1) | **2))/ENPTS1 | | |
| 0006 | | DX=(X2-X1)/FNPTS | 51 | | | |
| 0007 | | DY=(Y2-Y1)/FNPTS | 51 | | | |
| 0008 | | SN=DY/DLN | | | | |
| 0009 | | DU 100 1=1,NPTS | | | | |
| 0010 | | FIM1=FLCAT(1-1) | | | | |
| 0011 | | X=X1+FIM1*DX | | | | |
| 0012 | | Y=Y1+F1M1*DY | | | | |
| 0013 | | TE(X.FL'XWAXR " | AND. Y.LT.YMA | XB | | |
| | 1 | .AND. X.GT.XM1NE | AND. Y.GT. | YMINB) GU TO 50 | | |
| 0014 | | AZA(1)=0. | | | | |
| 0015 | | BZA(1)=0. | | | | |
| 0016 | | GU TU 100 | | | | |
| 0017 | 50 | CALL ALT(X, Y, Z, S | SN, AZ, BZ, 1) | | | |
| 0018 | | AZA(1) = AZ | | | | |
| 0019 | | BZA(I)=BZ | | | | |
| 0020 | 100 | CONTINUE | | | | |
| 0021 | | RETURN | | | | |
| 0022 | | END | | | | |

FURTNAN IV-FLUG 102-51E 13:20:00 21-Afr-61 FAGF 2 SLPS.FEN /IN:NLUCKS/KR

PRUGRAM SECTIONS

| NUMBER | NAME | SIZE | | AIJFIPUILS |
|--------|--------|--------|-----|-----------------|
| 1 | SCODE1 | 000512 | 105 | Hm,1,CUN,LCL |
| 2 | SPDA1A | 000004 | 2 | AN, D, CUN, LCL |
| ف | SILATA | 000044 | 18 | KH, L, CUN, LCL |
| 4 | SVARS | 000052 | 21 | RW, D, CON, LCL |
| > | STEMPS | ບບປມປ2 | 1 | Fe, D, CUN, LUL |
| b | BUUNDS | 100024 | 10 | rn, L, Uir, Urr |

ENTRY PUINTS

NAME 11FE AUDRESS NAME TIPE AUDRESS NAME TIPE AUDRESS NAME TIPE OPESS NAME TIPE AUDRESS SEMS 1-0000000

ź

ARIABLES

 NAME
 Tipe
 ALUPESS
 NAME
 NAME

APPAID

NAME TIPE AUGHESS STREE STREESTLAS

ΑΖΑ ΗΦΑ ΓΗΟΣΟΓΙΑΦΟΣΟΟΦΑ 2 (1) ΒΖΑ ΕΦΑ Ε=00001ΒΦ συσστά 2 (1)

APELS

¥

- ARBEL ALLEROU - LARBEL ALLERIA - LALER - LARBEL ALLERIA - LARBEL ALLERIA - 57 - 1-12240 - 1 - 122400

n oligina Ascintentino Esteriori. All'Esteri

| FORTRAN Alslp.F1 | IV-PLUS [n | V02-51E /TR:BLOCKS/WR | 13:28:21 | 21-APR-81 | PAGE 1 |
|---------------------|---------------|---|--|---|--------|
| | C C C | THIS SUBROUTINE A POINTON THE CA THE Z VALUE AT 1 | ACCEPTS THE Ache Map Shei That Point | X,Y COORDINATES OF ET, AND RETURNS | |
| | C8***** | ************* | *********** | *********** | |
| | c | | | | |
| | C | SUBROUTINE BY CY | RUS C. TAYL | DR | |
| | С | COMPUTER SCIENCE | E SPECIALIST | (TRAINEE) | |
| | С | AUTO-CARTU BR | | | |
| | C | TDL, USAETL | | | |
| | C | FURT BELVUIR, VI | • | | |
| | C C | 23 AUG 19// | | | |
| | C****** | **** | ********** | ****** | |
| | c | | | • | |
| 0001 | | SUBROUTINE ALT(| X,Y,Z,SN,AZ, | BZ, IASCD) | |
| 0002 | | INTEGER COEF1 | | | |
| 0003 | | LOGICAL#1 COEF2 | | | |
| 0004 | | DIMENSION COEFI | (90,40),BUF(| 512),COEF2(90,40,3) | |
| 0005 | | DIMENSION FITI(| 4),F1T2(4),F | ITJ(4),FIT4(4) MALA MATNE ETEND | |
| 0006 | | COMMON /NEW/MEDI | ММАХ⊡;ІМАХ⊡; . 0 | AMIND, IMINO, CLEAD | |
| 0007 | | TECX.LT.XMAXB | AND. Y.LT.YM | AXR | |
| 0000 | 1 | .AND. X.GT.XMIN | B AND Y.GT | .YMINB)GO TO 2077 | |
| 0009 | - | Z=ELEVB | | • | |
| 0010 | | AZ=0. | | | |
| 0011 | | ВZ=0. | | | |
| 0012 | | RETURN | | | |
| 0013 | 2077 | CUNTINUE DATA LEIRET(A/ | | | |
| 0014 | | DATA TETESTAN | CO TO 111 | | |
| 0015 | | IFIRST=1 | 00 10 111 | | |
| 0017 | | ISAVE=0 | | | |
| 0018 | | JSAVE=0 | | | |
| 0019 | | BURDER=((5.E=4) | *100./2.54)* | 8. | |
| 0020 | | FIT=(BORDER/8.) | * 9, | | |
| 0021 | | DO 112 K=1,90 | | | |
| 0022 | | CALL DSKIRN(4,1 | ILERR, K, NRES | ,BUF, 0, IDUNE) | |
| 0023 | | $1112 \times 101 \times 101$ | 0 10 9999 | | |
| 0024 | | L=4*(J=1)+b+328 | | | |
| 0026 | | COEF1(K,J)=BUF(| L) | | |
| 0021 | | COEF2(K,J,1)=BU | F(6+1) | | |
| 0028 | | CUEF2(K,J,2)=BU | +(L+2) | | |
| 0029 | | COFE5(K'')'=RO | E(L+3) | | |
| 0630 | 114 | CUNTINUE | | | |
| 0031 | 112 | CONTINUE | | | |
| 0032 | | J=INT((X=BURDER |)/F(T)+1 | | |
| 0034 | | I=INT((Y-BORDER |)/F1T)+1 | | |
| 0035 | | J1=J+1 | | | |
| 0036 | | 1MOD=1-82 | | | |
| 0037 | | IF(I.EQ.ISAVE.A | ND.J.LU.JSAV | E) GU TO 80 | |
| 0038 | | IF(IMOD.LT.1) G | U TU 9998 | | |
| 0039 | | 1F(J.GT.90) GU | TU 9998 | | |
| 0040 | | 1D=(1MUD=1)+4 | | | |

ľ

| FORTRAN IV-PLUS | V02-51E | 13:28:21 | 21-APR-81 | PAGE 2 |
|-----------------|--|--------------------------------------|--|--------|
| ALSLP.FTN | /TR:BLOCKS/WR | | | |
| | | | | |
| 0041 | FIT1(1)=CUEF1(J | IMOD) | | |
| 0042 | FIT2(1) = COEF1(J) | ,IMOD+1) | | |
| 0043 | FIT3(1) = CUEF1(J) | (,IMOD) | | |
| 0044 | F1T4(1) = COEF1(J) | L,IMUD+1) | | |
| 0045 | DO 75 1P=2,4 | | | |
| 0046 | I1=1B+1P | | | |
| 0047 | 12=1B+4+1P | | | |
| 0048 | FIT1(IP) = COEF2(C) | J, IMOD, IP-1) | | |
| 0049 | F1T2(IP) = COEF2(| J,IMOD+1 ,IP- | •1) | |
| 0050 | FIT3(IP) = CUEF2(C | J1,IMUD,IP=1) | | |
| 0051 | FIT4(IP)=CUEF2(| J1,IMOD+1,IP= | •1) | |
| 0052 75 | CUNTINUE | | | |
| 0053 80 | CUNTINUE | | | |
| 0054 | | LT+BURDER | | |
| 0055 | | LEADOOLO | | |
| 0056 | | II+BUKDER | | |
| 0057 | | | | |
| 0058 | | | | |
| 0059 | 160-16-1. | ())#¥I ▲ (ETT | | VI |
| 0050 | 21-5111(1)+5110 | (2)*X0 + (EII (2)*X1 + (EII | []]]]]]]]]]]]]]]]]]]]]]]]]]]]]]]]]]]] | |
| 0001 | 22-0112(1)+0112(| (2)*X0 * (E11 (2)*YLC + (E1 | T2(2)+F112(4)+KUJ + | |
| 0053 | 23 = (113(1) + (113)) | (2)*XLC + (FI (2)*XLC + (FI | 112(3)+F113(4)+X6C) | * ¥1C |
| 0064 | $XL2=\Delta RS(XLA*(MR))$ | (2)*XDC + (14)R41)) | | • 150 |
| 0065 | XLC2=AHS(XLC++(HC | ARDR+111 | | |
| 0000 | YL2=ABS(YL++(MRI | R+111 | | |
| 0067 | YLC2=ABS(YLC++() | ARDR+1)) | | |
| 0068 | IF (IASCO_FO_O)G | 1 1 3 200 | | |
| 0069 | $AZ_1 = FIT_1(2) + FIT_1$ | L(4) #YL | | |
| 0070 | AZ2=F1T2(2)+F1T2 | (4) * YLC | | |
| 0071 | AZ3=FIT3(2)+FIT | 3(4)*1L | | |
| 0072 | AZ4 = FIT4(2) + FIT4 | I(4) #YLC | | |
| 0073 | BZ1=FIT1(3)+F1T1 | l(4)*XL | | |
| 0074 | BZ2=F1T2(3)+F112 | 2(4)*XL | | |
| 0075 | BZ3=F113(3)+F113 | 3(4)*XLC | | |
| 0076 | BZ4=FIT4(3)+F1T4 | 1(4)*XLC | | |
| 0077 200 | CUNTINUE | | | |
| 0078 | XLC=+XLC | | | |
| 0079 | YLC=-YLC | | | |
| 0080 | w1=(XLC2+(-2.+xl | JC+3.))*(YLC2 | 2 +(- 2.+YLC+3.)) | |
| 0081 | w2=(XLC2*(-2.*XL | JC+3.))*(XL2* | *(-2.*XL+3.)) | |
| 0082 | w3=(XL2*(-2.*XL4 | +3 .)) *(YLC2*(| -2.*YLC+3.)) | |
| 0083 | w4=(XL2*(-2.*XL4 | 3.))*(YL2*(- | ·2•+XT+3•)) | |
| 0084 | IF(IASCD.EQ.0)G | 10 205 | | |
| 0085 | ADW1 = -6. * XLC * (1.) | -XLC) + (YLC2+ | (=2.*YLC+3.)) | |
| 0086 | ADW3=6.*XL+(1) | (L)*(YLC2*(=2 | 2. #XLC+3.)) | |
| | AUWZ=+6.+XLC+(1. | .→XUCJ∓(¥U2+(/!>+/V!?+/ | .+&.+XL+3.)] .+VI | |
| 0000 | - HOW1===4 +XLF(I.=/ | 、UJTLIUZTLTZ。 v/Cltt/v/clt | | |
| 0090 | - DURI=-D。FILLF()。 - ADW2=6 まや(ま/1> | | · (~ Z • 7 AUC 7 3 • J J) * X C + 2 •) } | |
| 0090 | | いしょうしんれん ビスレーズ | | |
| 0097 | |) = x ロビリマしスロビマし (1.) 本(X1.) 本(=つ | .=&+TAWTJ+JJ #X1.42 }} | |
| 0093 | $AZ = 7.1 + ADw1 + 7.2 + \Delta\Gamma$ | 、シッ・ミスシェアしてど。) ルンチズイキムi) m マムグ | (4+Δ1)w4 | |
| 0094 | AZ=AZ+AZ1+w1+AZ | 2*w2+A2.3*w3+A | 12.4 * w 4 | |
| 0095 | BZ=Z1*BDw1+Z2*BI |)w2+Z3+HDw3+7 | 4+BDw4 | |
| 0096 | BZ=BZ+BZ1*w1+BZ2 | 2*+2+823*+3+E | 524*w4 | |

| FURIRAN ALSLP.FI | 1V-PL In | ιUS | V02-51E /TR:BLOCKS/wR | 13:20 | :21 | 21-APR-81 | PAGE | ٤ |
|---------------------|-------------|-----|--------------------------|------------|---------|---------------|----------------------|-------|
| | | | | | | | | |
| 0097 | 205 | | Z=Z1*W1+Z2*W2+ | 23*w3+24 | *w4 | | | |
| 0098 | 210 | | CONTINUE | | | | | |
| | С | | wKITE(6,101)A | Z, BZ, Z1, | 22,23, | 24, w1, W2, W | 3,w4,ADW1,ADW2, | |
| | С | 1 | , ADW3, ADW4,, B | Dw1,BDw2 | , BDW3, | BDw4, AZ1, A | 22, A23, AZ4, BZ1, B | 22. |
| | С | 1 | 823,624 | | | | • • • • • • • • • | • • • |
| 0099 | 101 | | FORMAT(1X,2F9 | .4,2X,2(| 4F9.4. | 2X),/,2(1X | ,3(4F9,4,2X),/), | 11) |
| 0100 | 100 | | FORMAT(1X, 15, | 15,2110. | 3.F10. | 3,/) | | |
| 0101 | | | JSAVE=J | • | | , . | | |
| 0102 | | | ISAVE=1 | | | | | |
| 0103 | | | IUSVE=IUNIT | | | | | |
| 0104 | | | RETURN | | | | | |
| 0105 | 9999 | | wRITE(5,99991 |) LERR | | | | |
| 0100 | 99991 | | FURMAT('11/0 | FAILURE | UN DB1 | : - IERR = | (51, | |
| 0107 | | | STUP | | | | • - • • | |
| 0108 | 9998 | | Z=310. | | | | | |
| 0109 | | | RETURN | | | | | |
| 0110 | | | END | | | | | |

| ALSUP.F | 14-511 14-511 | /1Himro 2 A05-21F | CKS/WH | 13:20 | 21 21-2 | A6K-81 | | PAGE 4 | | | | | | |
|-------------|------------------|----------------------|-----------------|------------------|-----------------|------------|--------------|------------------|--------|---------------|----------|------------|-------------|---|
| PRUGRAM | SECTION | NS | | | | | | | | | | | | |
| NUMBER | NAME | 512 | r | | Alifibul | LS | | | | | | | | |
| 1 | SCUDET | 003074 | 798 | | nn,1,Cul | LCL | | | | | | | | |
| 2 | SPDATA | 000024 | 10 | | PA, D.CUN | LCL | | | | | | | | |
| 3 | SIDATA | 000066 | 21 | | FN,L,CUN | ,LCL | | | | | | | | |
| | SVAFS CTL HUS | 04/504 | 10140 | | RW, D, CUP | | | | | | | | | |
| 5 | ALC: NEW | | | | HW, D, COP | CHI CHI | | | | | | | | |
| , | Ntw | 000002 | ĩ | | + n , L , U V H | GBL | | | | | | | | |
| тлікі Б | UINIS | | | | | | | | | | | | | |
| NAME | 11FE | AUDRESS | NAME. | hee | AULPESS | NAME | 11Pt | AUURESS | | 11PE | AUDERL | v : | Lief. | 601 m 200 |
| ALI | | 1-090000 | | | | | | | | | | | | |
| .AFIABL | ŁS | | | | | | | | | | | | | |
| NAME | 1166 | AULINESS | 1.442 | LTPL. | HULFEJA | NAME | liet | ALLAEDD | 1446 | lter | AUJHESU | 5 | : : PE | ALUPEDO |
| AUMI | F # 4 | 4-047440 | ALINZ | H+4 | 4-047450 | ALAS | + * 4 | 4-047444 | AUni | H+4 | 4-0474-4 | 42 | r * 4 | F-VUUU12 |
| AZ1 | ⊬≉4 | 4-047300 | ALL | н+4 | 4-647364 | AZJ | H 4 4 | 4-047370 | A.2.4 | ⊦+4 | 4-04/374 | PUNI | H#4 | 4- 41400 |
| HCn2 | 844 | 4-047464 | 1-1 + 3 | P+4 | 4-34747 | OLAY | 1+4 | ≠ =∪47474 | 114.80 | | 4-247220 | Pe | ⊢ •4 | F=102014 |
| 041 | H#4 | 4-047400 | ter | H#4 | 4-047464 | e | ⊢+4 | 4-04/41. | 664 | H # 4 | 447414 | LLEVE | F # 4 | 6-,00020 |
| F 1 1 | m # 4 | 4-047232 | i | 1 * 2 | 4-14:52 | よんろじい | 1 * 2 | 1-000016+ | Dr. | 1+2 | 4-04-260 | ILUNE | 1*4 | . 4 47244 |
| LEAK | 1+2 | 4-047240 | 11151 | 140 | 4-047226 | IMUD | 1+2 | 4-047256 | 15 | T+5 | 4-047262 | ISAVE | 1+2 | 4-047222 |
| IUNII | 1.4.2 | 4-047502 | 103+2 | 1.4 | 4-047500 | 11 | 192 | 4-047264 | 12 | 1+2 | 4-04/200 | <u>.</u> | 1+2 | 4-047240 |
| JSAVE | 1.4 | 4-04/224 | 31 | 1+2 | 4-04/254 | · . | 1 4 4 | 4-04/236 | L | 1.4.4 | 4-04/250 | MADE | 1.1 | 1-000000 |
| NRES . | | 4 - 0 4 7 2 4 2 | 23 | | F=000010+ | | P • • | 4-04/420 | • 2 | | 4-04/424 | * 3 | | 4-24/452 |
| | H 4 4 | 4-047474 | | H • • | F= 00002+ | AC | F • • | 4-04/2/0 | A.5. | | 4-04-214 | | | 4 * - 4 - 32 - |
| ALC 2 | 10 1 10 | 4-047300 | AL.2 | | 4-047340 | | | 1-14731 | A 1 1 | 17 4 4 | 4-043010 | | | F = 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 |
| 1 | | 4-047300 5-000000 | IL. | 10 1 1 10 1 1 | 4-04/304 | , Le | | | 71 | | 4-047354 | 7.7 | | 4-047355 |
| 23 | 694 | 4-047330 | 24 | H • • | 4-01-334 | ~ | | 1-000000 | 21 | | 4-04/320 | | | 4-047324 |
| 4- # A 1 3 | | | | | | | | | | | | | | |
| NA32 | 1 1 1 1 | ALCHESS | 01Z | L. | LIMENSI | JN 2 | | | | | | | | |
| e 1 | F 9 4 | 4-043120 | 004170 | 1924 | (512) | | | | | | | | | |
| in si i € 1 | 1.4.2 | ▲●し · いしりい | 1.0.40 | 30.00 | (90.40) | | | | | | | | | |
| COEF 2 | L. • . | 4-16940 | V23:00 | 5401 | (96,46,2 | 3 J | | | | | | | | |
| 1114 | F # 4 | 4-04/120 | けいいによう | b | (4) | | | | | | | | | |
| t i i Z | F # 4 | 3-047140 | JULICE | ÷ | (4) | | | | | | | | | |
| 1113 | | 4-011160 | uuuu∠u | 6 | (4) | | | | | | | | | |
| -114 | r.#4 | 4-)4/200 | 0000 2 0 | н | (4) | | | | | | | | | |
| LABELS | | | | | | | | | | | | | | |

LABEL ALUMESS LABEL ADDRESS LABEL ADDRESS LABEL ADDRESS LABEL ADDRESS

Sec. Sec.

.

| FORTRAN | 14-5702 A05-2 14-5702 A05-2 | 1€ LUCKS∕wR | 13:20:21 | 21-APH-81 | PAGE | 5 | | | |
|-------------------|--------------------------------|-------------------|----------------------------|---------------------|----------------------------|-----------------------|----------------------------|------------|----------|
| 75 112 2077 | ** ** 1+0.0124 | 80 114 9998 | 1-001102 ** 1-003052 | 100° 200 9999 | ** 1-001774 1-003006 | 101° 205 99991° | ** 1-002700 3-000000 | 111 210 | 1-000444 |
| FUNCTIO | INS AND SUBROUT | INES REFE | RENCED | | | | | | |
| DSKTRN | I | | | | | | | | |
| TOTAL S | SPACE ALLOCATED | = 052762 | 11001 | | | | | | |

, LP.LST=ALSLP

| FORTRAN LPPER.F: | IV-PLUS [n | V02-51E /TR:BLOCKS/WR | 13:29:05 | 21-APR-81 | PAGE 1 |
|---------------------|---------------|--|-------------------------|----------------|---------------|
| | C FILE | NAME - LPPER.FT | N | | |
| 0001 | • | SUBROUTINE LP(S | HADE) | | |
| 0002 | | LOGICAL*1 SHADE | (1),CHAR(12) | | |
| 0003 | | LOGICAL*1 PRNT(| 100) | | |
| 0004 | 1 | DATA CHAR/ ', | '.', '-', '1 4','W'/ | •, •/•, •\•, • | **, '@*, 'U*, |
| | С | WRITE(5,51)(SHA | DE(M),M=1,32 |) | |
| 0005 | 51 | FURMAT(1X,3203, | /) | | |
| 0006 | | DU 10 I=1,3 | | | |
| 0007 | | DO 50 K=1,100 | | | |
| 0008 | | IF(SHADE(K).LT. | 0.)SHADE(K) = | 127. | |
| 0009 | | PRNT(K)=CHAR(1) | | | |
| 0010 | 50 | CONTINUE | | | |
| 0011 | | DO 20 J=1,100 | | | |
| 0012 | | IF(SHADE(J).GT. | 6)GO TO 21 | | |
| 0013 | | IF(I.NE.1)GO TO | 20 | | |
| 0014 | | PRNT(J)=CHAR(1) | | | |
| 0015 | | GO TO 20 | | | |
| 0016 | 21 | IF(SHADE(J).GT. | 9)GO TO 22 | | |
| 0017 | | IF(I.NE.1)GO TO | 20 | | |
| 0018 | | PRNT(J)=CHAR(2) | | | |
| 0019 | • | GU TU 20 | | | |
| 0020 | 22 | IF (SHADE (J), GT. | 13)GU TU 43 | | |
| 0021 | | IF(I.NE.I)GU TU | 20 | | |
| 0022 | | PRNT(J)=CHAR(3) | | | |
| 0023 | | | 16100 00 00 | | |
| 0024 | 43 | IF (SHADE (J).GI. | 15/60 10 23 | | |
| 0025 | | DUNT(1)=(UAD(A) | 20 | | |
| 0020 | | CO TO 20 | | | |
| 0027 | 2.3 | IE(SHADE(1) CT | 19100 TO 24 | | |
| 0028 | 23 | 16(1 NE 1)CO 10 | 19700 10 24 | | |
| 0029 | | DUNT(1)=CHAB(5) | 20 | | |
| 0030 | | $\frac{1}{2} \frac{1}{2} \frac{1}$ | | | |
| 0032 | 24 | TE(SHADE(.1) GT. | 24 YG0 TO 25 | | |
| 0032 | 44 | IF(I_NF.1)G0 T0 | | | |
| 0034 | | PRNT(J)=CHAR(6) | | | |
| 0015 | | GO TO 20 | | | |
| 0036 | 25 | LE(SHADE(J)_GT. | 28)GU TO 26 | | |
| 0037 | 2 4 | IF(I_NE_1)GU TO | 20 | | |
| 0038 | | PRNT(J) = CHAR(7) | | | |
| 0039 | | GO TO 20 | | | |
| 0040 | 26 | IF(SHADE(J).GT. | 33)GO TO 27 | | |
| 0041 | | IF(1.NE.1)GU TO | 20 | | |
| 0042 | | PRNT(J)=CHAR(8) | | | |
| 0043 | | GU TU 20 | | | |
| 0044 | 27 | IF(SHADE(J).GT. | 38)GU TU 28 | | |
| 0045 | | IF(1.EQ.3)G0 TO | 20 | | |
| 0046 | | IF(I.EQ.1)PRNT(| J)=CHAR(9) | | |
| 0047 | | IF(I.EQ.2)PRNT(| J)=CHAR(2) | | |
| 0048 | | GO TU 20 | | | |
| 0049 | 28 | IF(SHADE(J)_GT_4 | 4)GO TO 29 | | |
| 0050 | | IF(1.EQ.3)GU TU | 20 | | |
| 0051 | | IF(I.EQ.1)PRNT(| J)=CHAR(10) | | |
| | | | | | |

| FORTRAN LPPER.F | IV-PLUS FN | V02-51E /TR:bLOCKS/w | 13:29:05 VR | 21-APR-81 | PAGE 2 |
|--------------------|---------------|-------------------------|---|-----------|--------|
| 0051 | | GU FO 20 | | | |
| 0054 | 29 | IF(SHADE(J). | GF.51)60 TO 30 | | |
| 0055 | | IF(1.E0.3)G |) TU 20 | | |
| 0056 | | 1F(1.E0.1)PF | RNT(J)=ChAR(10) | | |
| 0057 | | 1F(1.LU.2)PH | RNI(J)=CHAR(5) | | |
| 0058 | | GU TU 20 | | | |
| 0059 | 30 | IF(SHADE(J). | GT.58)GO TO 31 | | |
| 0060 | | 1F(1.E0.3)G0 | 10 20 | | |
| 0061 | | IF(1.E0.1)PF | RNT(J)=CHAR(10) | | |
| 0062 | | 1F(1.E0.2)PF | (NT(J)=CHAR(8) | | |
| 0063 | | GU TU 20 | | | |
| 0064 | 31 | IF(SHADE(J). | GI.66)GU TU 32 | | |
| 0065 | | IF(1.EQ.3)PF | NT(J)=CHAR(4) | | |
| 0066 | | IF(I.EQ.1)PF | NT(J)=CHAR(6) | | |
| 0067 | | IF(1.EQ.2)PH | RN1(J)=CHAR(10) | | |
| 0068 | | GU TU 20 | | | |
| 0069 | 32 | IF(SHADE(J). | GT./0)GU TU 33 | | |
| 0070 | | PRNT(J)=CHAH | <(11) | | |
| 0071 | | IF(1.EQ.1)PH | RNT(J)=CHAR(10) | | |
| 0072 | | 1F(I.EQ.2)PH | <nt(j)=char(9)< td=""><td></td><td></td></nt(j)=char(9)<> | | |
| 0073 | | GO TU 20 | | | |
| 0074 | 33 | PRN1(J)=CHAH | <(12) | | |
| 0075 | | 1F(1.EQ.1)PF | RNI(J)=CHAR(10) | | |
| 0076 | | 1F(I.EQ.2)PH | NT(J)=CHAR(5) | | |
| 0077 | 20 | CUNTINUE | | | |
| 0078 | | WRITE(6,500) | (PRNT(L), L=1, 1) | 00) | |
| 0079 | 500 | FURMAT("+",1 | (X,1U0A1) | | |
| 0080 | 10 | CONTINUE | | | |
| 0081 | | wRITE(6,501) |) | | |
| 0082 | 501 | FURMAT(1X) | | | |
| 0083 | | RETURN | | | |
| 0084 | | END | | | |
| | | | | | |

Transfer Strategy

| rukikak Leftek.t | 13-FEU 10 | a vuz=blr. Vikipin | 12168 | 13429 | -1- 21- | Ar:=01 | | PAUL 3 | | | | | | |
|-----------------------|-----------------------------|-----------------------------------|----------------------------|----------------------|-------------------------------|----------------|----------------------|--------------|-----------------------|------------------------------|---------------------------------|------------------------|----------------------|---------------------------------|
| PRUGHAN | SECTIO | 1.5 | | | | | | | | | | | | |
| NUMBER | NAME | 512 | t. | | Alibleu | ita | | | | | | | | |
| 1 3 4 | SCUDE I S ILATA SVARS | 001704 000024 000170 | 482 10 80 | | 4x,1,00 km,1,00 km,1,00 | N,LCL N,LCL | | | | | | | | |
| ENIRI P | UINIS | | | | | | | | | | | | | |
| NAME | 1:FE | AUURESS | NAME | 11PE | ALGHESS | AME | 1166 | nLükess | 5.44E | LIPL | ADDFESS | 5 A#1 | LYPE | ALUMEAS |
| LP | | 1-000000 | | | | | | | | | | | | |
| fafladl | E.S | | | | | | | | | | | | | |
| NAME | i tłe | ALUHEDS | NAME | TIPE | AUDRESS | NAME | 1112 | AULTEUS | • A M E | LIPE | A1 4880 | NAME | TIPE | ADUMESS |
| 1 | 1+2 | 4-060160 | J | 1+2 | 4+000104 | N | 1+2 | 4-60.102 | - | 1+2 | 4-110156 | | | |
| ARKAIS | | | | | | | | | | | | | | |
| NAME | 1125 | ALDHESS | 512 | .Ł | LIMENSI | L:+S | | | | | | | | |
| CHAR Prnt Shaue | L+1 L+1 L+1 | 4+000000 4-000014 F=000902* | 000014 000144 000001 | ع برو 0 | (12) (100) (1) | | | | | | | | | |
| LABELS | | | | | | | | | | | | | | |
| LABEL | ALLER | 55 | LAPEL | ni ch | tus | LArti | ALL+ | ·Lob | LACEL | 4 . D H | 1225 | aper l | A | 102 |
| 10 24 29 43 | 1-000 1-00 1-00 | 475 1102 1340 | 20 25 30 50 | 1-00 1-00 1-00 | 01534 00552 01174 | 21 20 31 | 1-00 1-00 1-00 | 1200 1200 | 22 27 32 500 | 1-00 1-00 1-00 3-00 | 10272 10702 1366 19044 | 23 20 33 501* | 1-01 1-01 1-01 | .0422 21002 21463 2013 |

٩.

TUTAL SPACE ALLOCATED = 002120 552 ,LP.LST=LPFEP

• • • •

| FORTRAN SXSY.FTN | IV-PLUS | V02-51E /TR:BLOCKS/WR | 13:29:38 | 21-APR-81 | PAGE | 1 |
|------------------|--|--|--|---|---------|---|
| | C THIS S C 'SUN' C CREAT C REFERE C OF TH C (UNPL | UBROUTINE IS DES TO STRENGTHEN S TED BY PROGRAMS S NCE: P. YUELI, HE ANALYTICAL HII IBLISHED?-AUTO CA | SIGNED TO VAN THE DETAIL IN SHADE.FTN ANN 'SOME REMARKS LL SADING PR(ARTO FILES) | RY THE AZIMUTH OF TH Shaded Relief Image Shadlp.ftn. S on the completion DJECT' | e Es | |
| Ċ | 2 | PROGRAM BY CYRUS | 5 C. TAYLOR | | | |
| (| - | AUTOMATED CARTO | GRAPHY BRANCH | 4 | | |
| (| | USAETL, FURT BEI | LVUIR, VA | | | |
| | - | 11 JULI 1978 | | | | |
| | | | | | | |
| 0001 | | SUBROUTINE SXSY | (SX,SY,AZ,BZ) | | | |
| 0002 | | COMMON /SEXY/DEI | LTAG, CUSEL, I | SUN, ANG, C1, C2, S1, S2 | | |
| 0003 | | REALTA NX,NY | 3 70 110 | | | |
| (| 2 | 11 (14000.52.0)00 | | | | |
| 0005 | - | NX=-AZ*DELTAG | | | | |
| 0006 | | NY=-BZ*DELTAG | | | | |
| 0007 | | DISFI=SQRT((NX** | *2)+(NY**2)) | | | |
| 0008 | | IF (DISFI,LT,1,E. | -6)GU TU 110 | | | |
| 0009 | | SU=NX/DISFI | | | | |
| 0011 | | C=C0+COS(ANG)-S(|)*SIN(ANG) | | | |
| 0012 | | S=S0*CUS(ANG)+CO |)*SIN(ANG) | | | |
| (| C IN EFF | ECT, OUR X-Y COU | ORDINATE SYST | EM HAS BEEN | | |
| (| C RUTAI | ED THROUGH AN AN | NGLE UF ANG F | ADIANS. NUIE | | |
| C | C THAT | THE ANGULAR COUP | ND SUNDED I | M USED IN THIS | | |
| | , RUUII 7 AFRON | INE AND IN SHADE | COOPDINATE S | NUI INE VSTEM BUT THE | | |
| | TRADI | TIONAL ALGEBRAIC | COURDINATE | SYSTEM, SINCE | | |
| Ċ | UUK X | -Y COURDINATE SY | STEM HAS BEE | IN RUTATED, | | |
| (| SX AN | ID SY MUST BE RUT | TATED BACK BE | FORE RETURNING | | |
| (| C TÚ 11 | E MAIN ROUTINE. | | | | |
| (| SECTOR | LI CASE | | | | |
| 0013 | | IF(C.GI.(CI). UP SX==C*COSFL | <.5.LT.(51) | | | |
| 0015 | | SY=-S+CUSEL | | | | |
| 0016 | | GU TU 100 | | | | |
| (| SECTOR | III CASE | | | | |
| 001/ | 10 | IF(C.LT.(C2). 06 | <.s.GT.(S2) | GU 10 20 | | |
| 0018 | | SX=C*COSEL | | | | |
| 0019 | | SI = S + CUSEL | | | | |
| 0020 | SECTOR | TI CASE: 2 SUBC | CASES | | | |
| 0021 | 20 | IF((C.LT.O.AND.S | 5.LT.0).UR.((| LT.O.AND.S.LT.S1) | | |
| | 1 | .OR.(S.LT.O.ANL | D.C.LT.C2))G | 0 10 30 | | |
| 0022 | | IF(C.GT.(0.7071) |))GU TU 25 | | | |
| 0023 | | SX=0. | | | | |
| 0024 | | 51=-CUSEL 60 Til 100 | | | | |
| 0025 | 25 | SX=CUSEL | | | | |
| 0027 | | SY=0. | | | | |
| 0028 | | GU TU 100 | | | | |
| (| C SECTOR | (IV CASE: 2 SUBC | CASES | | | |

| FURTRAN SXSY,FT | IV-PLUS N | V02-51E /Tr:Blucks/Wr | 13:29:38 | 21-APR-81 | PAGE |
|--------------------|--------------|--------------------------|--------------|-------------------|------|
| 0029 | 30 | 1F(C.LT.(~0.707 | 1))60 70 35 | | |
| 0030 | | SX=0. | 17700 10 35 | | |
| 0031 | | SY=-CUSEL | | | |
| 0032 | | GO TO 100 | | | |
| 6600 | 35 | SX=CUSEL | | | |
| 0034 | | SY=0. | | | |
| 0035 | 100 | CUNTINUE | | | |
| | C WE ML | JST NOW ROTATE O | UR LOCAL X-Y | COUPDINATE | |
| | C SYSTE | M BACK, SO THAT | SX AND SV | TLL BE CONSTSTANT | |
| | C WITH | THE MAIN ROUTIN | ES. | THE BE CONSISTANT | |
| 0036 | | Y=SY+CUS(ANG)-S | X#STN(ANG) | | |
| 0037 | | X=SX*CUS(ANG)+S | Y*SIN(ANG) | | |
| 8600 | | SX=-X | | | |
| 0039 | | SY=-Y | | | |
| 0040 | 110 CC | NTINUE | | | |
| 0041 | | RETURN | | | |
| 0042 | | END | | | |

| FORTRAN SASI.F1 | 1V-PLUS N | /18:512 | INS/AR | 13:29: | 38 21- | AF*=81 | | PAGE 3 | | |
|--------------------|--------------|----------|--------|--------|---------|--------|------|---------|------|------|
| PRUGRAM | SECTION | 15 | | | | | | | | |
| NUMBER | NAME | 517 | | | A11+160 | 165 | | | | |
| 1 | SCUDE1 | 001000 | 250 | | Ke,1,Cu | N, LCI | | | | |
| 2 | SPDATA | 000014 | 6 | | RW,D,CL | N.LCL | | | | |
| 4 | SVARS | 000044 | 16 | | KW,L,CL | N, LCL | | | | |
| 5 | STEMPS | 000004 | 4 | | HNILLO | NILCL | | | | |
| e | SEXI | 000036 | 15 | | ₽m,L,Cv | P,GBL | | | | |
| ENTRY P | CINIS | | | | | | | | | |
| NAME | TYPE A | UDRESS | NAME | IIPL | AUURESS | NAME | 1166 | AUURESS | NAME | LYPE |
| 5151 | i | 1-600000 | | | | | | | | |

VAHIADLES

| NAME | TIFE | ALLHESS | MANE | TYPE | ALLFESS | NAME | TYFE. | AUDRESS | NAME | TYPE | AUDRESS | ħA¥E | TYFF | ALUFESS |
|-------------------------------|-------------------|--|----------------------|--------------------------|--|----------------------|--------------------------|---|-------------------|--------------------------|--|---------------------------|--------------------------|---|
| ANU CU 1750N St T | H+4 1+2 K+4 | 8-000012 4-000014 5-00110 10 1-0000034 | A2 C1 NX SU | 944 944 944 944 | r-000000 6-000016 4-000000 4-000020 | 22 C2 NI 51 | 1*4 1*4 1*4 1*4 | f=00001c+ 6=000022 4=000004 6=000026 | L LELTAG SZ | 644 644 644 644 | 4-000024 6-000000 4-000030 6-000032 | Cusel LISEI Sx X | r#4 F#4 F#4 F#4 | c=360004 4+860010 F=600002≉ 4=660040 |

LADELS

| LABEL | AUDEESS | LABEL | ADDRESS | LABEI | AULKESS | LABEL | ADDPESS | LANTL | AUCHEUS |
|-----------|----------------------|----------|----------|-------|----------|-------|----------|-------|----------|
| 10 100 | 1-000320 1-000880 | , 110 | 1-000412 | 25 | 1-600542 | 30 | 1-000570 | 15 | 1-20.034 |

FUNCTIONS AND SUBMOUTINES REFERENCED

\$Cup \$216 \$00F1

TUTAL SPACE ALLUCATES = 001122 - 297 , Lr. Lof=SXS)

ADDRESS NAME TYPE ADDRESS

| FORTRAN IV-FLUS QUANT.FTN | V02-51E /TR:BLOCKS/WR | 13:37:21 | 21-APR-E. | PAGE 1 |
|------------------------------|---|-------------------------|-----------|--------|
| 0001 0002 0003 0003 | SUBROUTINE QUANT Z=FLOAT(ICON*(IN RETURN END | (2,1CUN) 1(2/CON))) | | |

*



FUKTRAN 1V-PLUS V02-51E 13137121 21-APR-81 QUANT_FTN /TNIBLOCKS/WK PAGE 2 PROGRAM SECTIONS NUNBER NAME ATTRIBUTES SIZE SCODE1 000054 22 SVARS 000004 2 RW,1,CON,LCL RW,D,CON,LCL 1 ENTRY PUINTS NAME TYPE ADDRESS QUANT 1-000000 VARIABLES NAME TYPE ADDRESS CON R+4 4-000000 ICON 1+2 F-000004+ Z R#4 F-000002+ TOTAL SPACE ALLUCATED = 000060 24 , LP. LST=QUANT

......

| FORTRAN RCSLP.F | 1 1 N | v-PLUS | V02-51E /TR:BLUCKS/ | 1 WK | 3:30:0 | 3 21 | -APK-81 | | PAGE | 1 |
|--|-------------|---------------------------|---|--|---|--|---|-------------------|--------|------|
| 0001 | c | 1 | SUBROUTINE BZA,DLN,IC | RCSLP(UN,DEL | XLL,YC Tap) | UR,XEND | ,Y,NP1X,A | ZA, | | |
| | | THIS THE A F Rel | SUBROUTINE C. Elevation V. Ine grid, in IEF contour | ALCULA ALUES, ORDER REPRES | TES AL AND C TO SI Entati | TITUDES Alculai Mulail On of Ti | , QUANTIZ Es slopes Tanaka's Errain. | ES Over | | |
| | | THIS : WIT POL | SUBROUTINE I H Edges Para Ynomial Terr | S REST Llel T Ain Mu | RICTED O THE DEL | COORDIN COORDIN | TANGULAR A'IE AXES | KEGIONS OF THE | | |
| | | PRUGRI | AM BY CYRUS Autu-C Usaetl Furt b 11 Jun | TAYLOR Arto B Elvoir E 1979 | R. , VA | | | | | |
| 0002 0003 0004 0005 0006 0007 0008 0009 0010 | • | | DIMENSIUN A COMMON /bOU FNPTS1=FLOA DLN=(SQR1((DY=(YEND-YC SN=DY/DLN IASCD=0 DX=(XEND-XL DX2=DX/2. | ZA(1), NDS/XM T(NPIX XEND-X UR)/FN L)/FNP | BZA(1) AXB,YM (-1) LL)**2 PTS1 TS1 | ,ELVES(AXB,XMI +(YCUR- | 2,2) NB,YMINB, YEND)**2) | ELEVB)/FNPTS1 | | |
| 0011 0012 0013 0014 | C C C | NOTE ' For | X1=XLL-DX2 X2=XLL+DX2 Y1=YCUR-DX2 Y2=YCUR+DX2 IHAT WE ASSU ALL CALLS F | ME THA Rom SS | T YCUR LPLP. | =YEND, | AS WILL B | E THE CAS | E | |
| 0015 0016 0017 0018 0019 0020 0021 0022 | - | | CALL ALT(X1 CALL QUANT(ELVES(1,1)= CALL ALT(X2 CALL QUANT(ELVES(2,1)= CALL ALT(X1 CALL QUANT(| ,Y1,Z, 2,ICON 2 ,Y1,Z, 2,ICON 2 ,Y2,Z, 2,ICON | SN,AZ,) SN,AZ,) SN,AZ,) | BZ,IASCI BZ,IASCI BZ,IASCI | (U) (U) | | | |
| 0023 0024 0025 0025 0026 0027 0028 0029 0030 | | | ELVES(1,2)= CALL ALT(X2 CALL QUANT(ELVES(2,2)= DO 100 1=1, IF(I.EQ.2*(AZ=0.5*((EL AZ=AZ/DELTA | 2 ,Y2,Z, 2,ICON 2 NPIX 1/2)JG VES(2, P | SN,AZ,) 0 tu 1 1)-elv | BZ,IASC 01 ES(1,1) | U))+(elves(| 2,2)-ELVE | S(1,2 | 2222 |
| 0032 0033 0034 0035 0036 | | | BZ=0.5+((EL BZ=BZ/JELTA BZA(1)=B2 X1=X1+DX CALL ALT(X1 | VES(1, P | 2)-ELV SN,AZ- | ES(1,1) BZ,1ASC |)+(ELVES(D) | 2,2)-ELVE | \$(2,1 |))) |

ĺ.

ŝ,

| FORTRAN IV-PL RCSLP.FIN | US VU2-51L / IR:BLUCKS/WR | 13:30:03 | 21-APR-81 | PAGE 3 | 2 |
|---|--|--|---|------------------------|---|
| 0037 0038 0039 0040 0041 0042 0043 0044 0045 0046 0047 0048 0049 0050 0051 0052 0053 0054 0055 0056 | CALL QUANI(2,10 ELVES(1,1)=Z CALL ALT(X1,Y2, CALL QUANT(2,10 ELVES(1,2)=Z GO TO 100 AZ=0.5*(ELVES(1 AZ=A2/DELTAP AZA(1)=AZ BZ=0.5*(ELVES(1 BZ=B2/DELTAP BZA(1)=BZ X1=X1+DX CALL ALT(X1,Y1) CALL ALT(X1,Y1) CALL QUANI(2,10 ELVES(2,1)=Z CALL ALT(X1,Y2) CALL QUANT(2,10) ELVES(2,2)=Z | CUN) ,Z.SN,AZ,BZ,IA CUN) 1,1)-ELVES(2,3 1,2)-ELVES(1,3 ,Z.SN,AZ,BZ,IA CUN) ,Z.SN,AZ,BZ,IA CUN) | ASCD) 1)+ELVES(1,2)-ELV 1)+ELVES(2,2)-ELV ASCD) ASCD) | VES(2,2)) VES(2,1)) | |
| 0057 0058 | RETURN END | | | | |

ALC: N

| FORTRA RCSLP. | AN IV-PLOS FIN | VU2-511 | CKS/#k | 13:30:03 | 51-95H-81 | PAGE | F |
|------------------|-------------------|---------|--------|----------|-----------|------|---|
| PROGRA | M SECTION | s | | | | | |
| NUMBER | NAME | 5121 | • | ATT | (PICJIES | | |
| 1 | SCUDEI | 001400 | 384 | Hw, | I,CON,LCL | | |
| 3 | SIDAIA | 000132 | 45 | K., | D,CUN,LCL | | |
| 4 | SVANS | 000110 | 36 | Kw, | D.CUN.LCL | | |
| 5 | SILMPS | 000006 | ذ | Re. | U.CON.LCL | | |
| b | BOUNDS | 000024 | 16 | Fe, | L,UYK,GBL | | |
| ENIRY | POINTS | | | | | | |

NAME TYPE AUDRESS NAME TYPE AUDRESS NAME TYPE ADDRESS NAME TYPE ADDRESS NAME TYPE ADDRESS RCSLP 1-000000

VARIABLES

| NAME | TYPE | ADDRESS | NAME | TYPE | ADDRESS | NAME | 11PE | ADDRESS | NAME | TYPE | ADDRESS | NAME | TYPE | ADDRESS |
|-------|------|-----------|-------|------|-----------|--------|------|-----------|--------|------|-----------|-------|------|-----------|
| AZ | ¥#4 | 4-000076 | 64 | H+4 | 4-000102 | DELIAP | F+4 | 1-000024- | LLN | H+4 | F-000020+ | DX | R=4 | 4-000042 |
| DX2 | R#4 | 4-000045 | DY | H#4 | 4-000030 | ELEVE | k#4 | 6-000020 | FNPTS1 | R*4 | 4-000020 | 1 | 1+2 | 4-000106 |
| LASCU | 1+2 | 4+000040 | 1CUN | 1+2 | 1-0000224 | NPIX | 1+2 | F=000012+ | SN | 8+4 | 4-000034 | XEND | R#4 | F-000006+ |
| XLL | H*4 | F-000002* | XMAXB | K+4 | 6-000000 | AMINE | ##4 | 6+000010 | X1 | R#4 | 4-000052 | X2 | R#4 | 4-000056 |
| ¥ | H#4 | F=000010* | YCUR | 644 | F=000604+ | YEND | 144 | 4-600024 | YMAXH | R#4 | 6-000004 | YMINB | R#4 | 6+000014 |
| ¥ 1 | H#4 | 4-000062 | 12 | H#4 | 4-000066 | Z | R#4 | 4-000072 | | | | | | |

ARRAYS

| NAME | TYPE | ADDRESS | \$12E | | DIMENSIONS |
|-------|-------|------------|--------|---|------------|
| AZA | ¥*4 | ++000014+ | 006604 | 2 | (1) |
| BZA | R#4 | F=0000616* | 000004 | 2 | (1) |
| LLVES | F * 4 | 4-000000 | 000020 | 6 | (2,2) |

LABELS

| LAULL | AUDRESS | LABEL | ADDRESS | LABEL | ADDRESS | LAHEL | AUDRESS | LABEL | ADDRESS |
|-------|----------|-------|----------|-------|---------|-------|---------|-------|---------|
| 100 | 1-001350 | 101 | 1+001052 | | | | | | |

FUNCTIONS AND SUBHOULINES HEREMORD

ALI QUANI SSURI

TUTAL SPACE ALLOCATED = 001674 476 ,LP,LST=RCSLP

