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OPTIMIZATION OF MULTI-ELEMENT AIRFOILS

K.P. Misegades



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20. Abstract A review of techniques aimed at maximizing C_l/C_d and C_d for multi-element airfoils showed the need for more exhaustive testing of possible configurations of flap deflection, slot geometry and airfoil angle of attack. For a typical 4-element airfoil, the number of possible configurations can easily be in the billions. A new technique, based on evolution strategy, has been developed for the problem of optimizing a multi-element airfoil with respect to its envelope of maximum C_l/C_d versus C_d . This technique was applied to an airfoil having a slotted leading edge flap and a double-slotted trailing edge flap using an existing computer program for 2D subsonic multi-element airfoils to provide values of aerodynamic coefficients. Although limitations of the program precluded the full determination of the envelope of C_l/C_d vs C_d , the problem of maximizing C_l/C_d for a minimum C_d constraint was solved. The result of testing approximately 400 configurations generated by the random mutation-natural selection procedure of evolution strategy was an 8-fold increase in C_l/C_d with a 12 % increase in C_d .		

Continued..

over the initial geometry. The conclusions reached from this work are 1) evolution strategy applied to the optimization of multi-element airfoils can yield substantial improvements in aerodynamic performance, 2) the number of configurations required to find the optimum can be reduced from the total number possible to a small fraction of the total with the same final result, 3) the inherent simplicity and speed of the technique developed lends itself well to further application in wind tunnels, 4) evolution theory appears to be the best choice for techniques aimed at the optimization of systems defined by a large number of degrees of freedom.

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This report has been reviewed by the EOARD Information Office and is releasable to the National Technical Information Service (NTIS). At NTIS it will be releasable to the general public, including foreign nations.

This technical report has been reviewed and is approved for publication.

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"But it can't fly, Newtons laws prove it!"

Th. von Karman, early 1900's

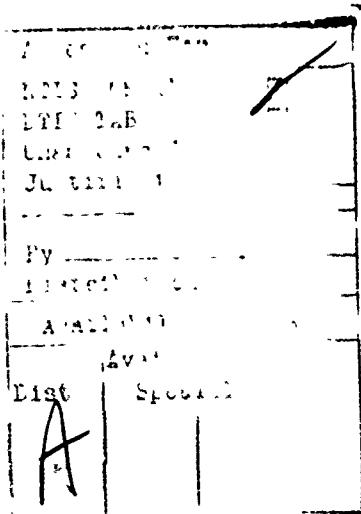


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1 INTRODUCTION

1.1 Multi-Element Airfoil Optimization

It is no secret today that competition among civilian and military aircraft manufacturers in the international marketplace is tough. This competition has demanded improved flight efficiency, and as a result a strong emphasis has been placed on design optimization with respect to take-off, cruise, and landing aerodynamic characteristics. Design considerations for take-off and landing aerodynamics are primarily directed towards the reduction of wing area, increase in maximum take-off weight, improved fuel efficiency, reduced field length requirements and lowered ground noise levels. The relative importance of the nondimensional coefficients of lift and drag, C_L and C_d respectively, for take-off and landing are shown in figure (1)¹.

Over the entire regime of flight, the performance at take-off, when aircraft weight and engine noise are at a maximum for the flight, is the most critical factor in the design of lifting surfaces. To achieve the maximum rate of angle of climb, thus reducing runway requirements and noise footprint, maximum C_L/C_d is desired for a given C_L . The envelope of values of maximum C_L/C_d versus C_L for the Boeing 727 wing, obtained from flight measurements, is given in figure (2), and is more or less similar to the envelope obtained for all other airfoils².

The complexity of multi-element airfoils, as seen in figure (2) and in more detail in figure (3A), has been dictated by the need for a smooth, and for high-speed transport aircraft shock-free airflow at cruise conditions, combined with the high-lift configurations required at take-off and landing^{2,3}. Although significant effort has been devoted to the study of advanced high-lift devices such as those employing blown flaps, jet flaps, boundary layer control or augmentor wings, it is reasonable to expect the continued use of mechanical devices for the next generation of civilian and military aircraft. Indeed, as shown in figure (4), values of $C_{L_{max}}$ for large, high-subsonic aircraft nearly doubled between 1950 and 1970 as a result of improved design of mechanical flap systems⁴. Once the choice of high-lift system and associated flap and airfoil geometries has been made, the relative positioning of the elements must be determined such that the obtainable values of C_L and C_L/C_d are sufficient to meet performance demands (or preflight promises!). The ideal set of configurations would be those that would result in the largest C_L/C_d -vs- C_L envelope. The number of all possible

configurations, however, is very large even for the typical case of an airfoil having a double-slotted trailing edge flap and a slotted leading edge flap, as depicted in figure (3B).

1.2 Empirical Methods

The most common means of determining the best airfoil-flap configurations involves many hours of wind tunnel testing for a representative set of variations of slot gap width and overlap, flap deflection and angle of attack. Optimum configurations are then made by adding to the main airfoil the leading and trailing edge devices, whose individual slot geometries have been optimized with respect to only one adjacent element. An example of this empirical method, reproduced from the work of Ljungstrom⁵, appears in figure (5). Although this empirical method can greatly improve the aerodynamic performance of a multi-element airfoil, there are two significant disadvantages that must be considered. First, the accuracy of an empirical method is dependent on a large number of test configurations; however, for even the most well-funded design relatively few different configurations are actually tested. For instance, for a 4-element airfoil, 500 test cases is only $5 \cdot 10^{-6}$ % of the number of possible cases, if each of the 10 degrees of freedom can be varied across 10 increments. Increasing the number of test cases comes at the expense of time and direct operating cost of wind tunnels. If wind tunnel time and cost trends increase at the rate depicted in figure (6), however, it is doubtful that empirical methods will produce better results than at the present time, when a great emphasis is being placed on improving high-lift device performance⁶. The second disadvantage of empirical methods is that by combining elements optimized with respect to only adjacent elements, the important viscous interaction between all elements is unaccounted for. This interaction, however, is strong and tests have shown that the combination of individually-optimized components rarely results in an optimum overall configuration⁵.

1.3 Self-Optimizing Airfoils

It would be desirable then to have a self-optimizing scheme, where the system seeks its own best configuration without the need for testing every possibility. Far from speculative, such schemes have been used with a good deal of success in several different problems where systems are described by several degrees of freedom and relative 'factors of fitness' result for each variation of parameters. One such application described by Levinsky⁷ attempted to

maximize C_L for a fixed maximum C_d and minimize C_d for a fixed minimum C_L for a flexible 2-dimensional airfoil mounted in a transonic intermittent wind tunnel. Results of this work, and results of further investigation of a 3-dimensional flexible airfoil⁸ in a transonic continuous wind tunnel are given in figures (7) and (8). In both cases, the hydraulically-actuated leading and trailing edges were modified automatically by on-line computers programmed with a gradient-strategy optimization scheme. This is described in section 2. The only human input was the factor of fitness to be maximized or minimized (C_L, C_d , or volume) and a constraint. Gradient strategy has also been used in the work of Hicks⁹, where 2-dimensional transonic airfoils were modified to improve C_L , C_d or maximize volume. Some of the more significant results of this work, performed numerically as opposed to the above mentioned wind tunnel work, are shown in figure (9). Although these examples have resulted in substantial improvements in airfoil performance, the application of their optimization methodology was found to be more cumbersome than the method described in this work. Existing optimization methods are compared below to a new scheme based on 'evolution strategy'. This scheme has been developed to determine the configurations of a 4-element airfoil giving maximum C_L/C_d for each value of C_L , where only the geometry of each element is known initially.

2 THEORY

2.1 Simple Optimization Problem-Existing Solution Methods

Consider the optimization problem faced by an experimentalist standing above a room in which there is a single geographical peak whose location with respect to a 2-dimensional coordinate system is to be determined. In this problem, the 'system', this being the human, has two degrees of freedom, his location with respect to the x-axis and the y-axis. At each x,y coordinate position, the value is determined of the geographical 'fitness factor', or the distance between the x-y plane and the surface below. The most rudimentary method to find the peak would be to make a number of random soundings in order to obtain a rough impression of the surface. In order to improve accuracy, the grid could be divided into a fine mesh and the height is then recorded at each mesh point. Although this scheme guarantees that all possible x,y combinations have been checked, the number of possible combinations increases with the square of the number of grid divisions and with a power equal to the number of degrees of freedom for higher order systems. Figure (10) depicts these 2 basic schemes along with two gradient-based strategies that were developed to converge to the peak with a reduced amount of effort¹⁰.

In the first of these two gradient-based strategies, known as the Gauss-Seidel Strategy, the experimentalist, trying to find the peak with the least amount of effort, simply proceeds in the direction of the steepest positive gradient, determined at the starting point, until the gradient becomes zero or negative. From this point, he turns in the direction of a new, locally-steepest gradient and continues in this new direction. This procedure is continued until the peak is found, that is, a position has been reached on the x-y plane where no positive gradients exist below. The second of these techniques, known as the 'general gradient strategy', is similar to the first except that at each step the magnitude of gradients in all directions is re-evaluated. Although the second scheme may result in the shorter total distance between the starting point and the peak with respect to the first scheme, it requires more work per step. Clearly, the use of either of the gradient strategies represents a substantial improvement over the inspection of every possible combination of the variable parameters. It is noted that in order to reduce the amount of effort involved in scheme B of figure (10), one is tempted to increase the grid spacing. The

danger of this, of course, is that there is a strong possibility that the peak will be completely missed; this is precisely the point mentioned previously related to optimizing airfoils by empirical methods. The danger of using gradient strategies in more complicated systems is that only a relative optimum may be reached, as the smaller of two peaks for the simple problem just described.

2.2 Simple Optimization Problem-Evolution Strategy Solution

A fifth, and relatively new optimization scheme that may further reduce the effort required to improve a system described by a number of degrees of freedom is based on 'evolution strategy'. 'Relatively' new is stressed, because the basis of this strategy is derived from the theories of natural selection first postulated by the 19th century biologist, Charles Darwin. As in biological systems, which in their simplest classifications can be grouped according to a number of parameters, such as size, number of appendages, means of reproduction or mobility, an engineering system survives if the combination of each of its defining parameters results in a 'beast' that is superior to all other combinations. Only recently has this concept been applied to realistic physical problems, the majority of the work to date being attributed to Professor Ingo Rechenberg, of the Technischen Universitat Berlin. In order to describe this scheme, we consider again the task of the experimentalist. Using evolution strategy, as depicted in figure (11A), a number of test points are selected randomly over a region near the starting point. The height is recorded at each point, then the experimentalist moves to the highest of these points. From there, the same number of new points are randomly chosen, and the procedure continues as before.

The distance from one 'high point' to each new point in a successive set is controlled by the previous distance, that is if a large step resulted in a larger height than a smaller step, all new points would be determined using steps approximately equal to the large step. This important factor of evolution strategy allows large steps to be taken early in the optimization process, and decreasing step size as the optimum position is approached. The inclusion of large mutation steps also prevents the convergence to local maxima, a problem associated with gradient strategies. In the case of a local maxima or small barrier in the optimization process, evolution strategy will jump ahead as the result of a large

mutation length.

2.3 Evolution Strategy Examples

Several examples of evolution strategy application are shown in figures (11) and (12)^{10,11}. As a simple verification test, figure (11B) depicts a segmented plate having 5 degrees of freedom that is mounted in a wind tunnel. The objective is to reduce the overall drag of the plate as measured by the momentum defect between the leading and the trailing edges. From the initial configuration, several new configurations, or cases, were created by random modifications of the angle of each segment with respect to an adjacent segment. After 140 cases, the segmented plate became nearly planar, the expected result. The important result is that 140 cases represents only $4.06 \cdot 10^{-5}\%$ of the total possible, 345 million.

The second example is an attempt to modify a system whose optimum configuration is unknown¹¹. In this case, shown in figure (12A), the objective was to maximize the efficiency of a two-phase supersonic nozzle constructed from a number of discs. The optimal configuration is radically different from conventional designs and verifies the ability of evolution strategy to converge to unknown solutions. It is also interesting to note that flow mixing regions seen in the figure have been previously suggested for improving nozzle efficiency.

The third example, that of reducing the head loss for a 90° bend of flexible tubing, also has an unpredictable result. As depicted in figure (12B) the final shape is a subtle change from the initial, a standard circular arc, but the result of 300 mutations is a halving of the head loss¹¹.

2.4 Selection of Optimization Method

The advantages of using evolution strategy over an exhaustive evaluation of every possible configuration are clear, except perhaps for the case of a system having only one degree of freedom. The advantages of evolution strategy over a 'strictly determined mathematical strategy', such as gradient methods, have been summarized by Rechenberg¹⁰:

1 When a large number of parameters are involved, the evolution strategy attains the desired result more rapidly than the more familiar strictly determined search strategies, assuming the size of the search steps to be the same in both cases. So far, this could only be proved for the case of an n-dimensional hyperplane rising in any arbitrary direction. A more general proof is being attempted.

2 Whereas the mathematical search strategies used so far

require very small steps (in the sense of the truncation of the Taylor series after the first term), the evolution method can and should operate also with much larger steps which exceed the linear region in the neighborhood. Taking larger steps signifies

- (a) in many situations a more rapid advance towards the desired aim, and
- (b) a shorter time to decide whether the step taken has been successful or not. (The change in the value of a function will generally be greater in the case of a large parameter change than in the case of a small change.)

3 A so-called "steady signal" in the measurement of the value of a function is a mathematical fiction. Disturbances are always present, which give rise to errors in measurement. The effectiveness of the strictly determined mathematical search strategies is markedly reduced by small errors of measurement. It is of the nature of the evolution method (as a stochastic search method) that small random errors of measurement cannot have a decisive influence on the development of the process.

4 There are cases in which the more familiar mathematical search strategies must reach deadlock. Such cases are frequently observed in physics; examples are hysteresis phenomena and locally limited extremal values. The evolution method can generally cope with such situations without difficulty.

5 The algorithm of the evolution strategy is extraordinarily simple. This implies that the effort required for an automation of the search process is relatively low.

Since the work associated with this report was strictly numerical, as opposed to experimental, the small error effect noted above related to the use of mathematical strategies could not have any significance; thus an argument could still be made in favor of gradient methods. Rechenberg, however, has found that a cross-over point exists at which search effort for improved configurations using evolution strategy is less than the effort required for gradient strategies⁹. This point is for systems having 5 or more degrees of freedom.

The system of interest in the work described here is a 4-element airfoil described by 10 parameters as shown in figure (13). Three pivot points describe the relative position of adjacent elements. The individual geometry of an element is given with respect to a local coordinate system with the origin on its leading edge. Pivot points 1 and 2 are fixed with respect to element 2 and are variable with respect to elements 1 and 3. Likewise, pivot point 3 is fixed with respect to element 3 and variable with respect to element 4. The two degrees of freedom for each of the pivot points plus the relative deflection between adjacent elements define 9 degrees of freedom. The 10th degree of freedom is the angle of

attack between the main airfoil and the freestream velocity vector.

As previously stated, the objective of this optimization is to obtain the best envelope of C_L/C_d -vs- C_L values. The fitness factor for this system is the magnitude of C_L/C_d for each value of C_L , which is equivalent to minimizing C_d for fixed C_L . This implies a series of individual optimizations over all desired values of C_L . The flexible nature of evolution strategy allows a two-step procedure, however. First C_L/C_d is maximized while maintaining C_L above the initial value; the limit of this maximization is a point on the envelope. The second step is then to move along this envelope with moderate mutation lengths, selecting those configurations having the best combination of C_L/C_d and C_L . It is because of this flexibility coupled with the abovementioned aspects of evolution strategy that this method was chosen over gradient strategies as a basis for multi-element airfoil optimization.

3 CALCULATION OF AERODYNAMIC COEFFICIENTS

3.1 Description of Program Theory and Use

Aerodynamic Coefficients are calculated by the program detailed in reference 13. This program is composed of the following task areas:

- A. Potential Flow Solution
- B. Ordinary Boundary Layer Solution
- C. Confluent Boundary Layer Solution
- D. Slot-Flow Analysis
- E. Combined Solution

The inviscid, potential flow solution makes use of the distributed vortex concept with the vortex singularity comprising the fundamental solution to the Laplace equation. Airfoils, arbitrarily arranged and composed of from one to four elements, have surfaces approximated by a closed polygon whose linear segments are represented by distributed singularities. Airfoil contours are limited to smooth, regular shapes with sharp or pointed trailing edges. The only restriction on the slot formed by two adjacent elements is that the magnitude of flap overlap must be greater than about 1% of the airfoil chord.

The ordinary boundary layer solution is comprised of mathematical models for laminar, transition, and turbulent boundary layers in subsonic flow. The laminar boundary layer model is based on the basic approach of Cohen and Reshotko modified to suit the needs of the program. Laminar stall criterion developed by the author of the program predicts the formation of short or long separation bubbles or bubble burst, a flow condition which causes the termination of further program execution. The transition model, evolving from the instability criteria of Schlichting and Ulrich, establishes limiting conditions for defining the position of transition on the airfoil. Two separate mathematical models for ordinary turbulent boundary layer development are used. The first, an approximate model developed by Goradia, is used in the initial iterative calculations. The second and more accurate model, based on the methods of Nash, determines the turbulent boundary layer in the final, viscous solution.

A significant feature of the program is the inclusion of a confluent boundary layer model that reflects the merging of an upper surface boundary layer with slot efflux. This model, developed from the experimental and analytical work of Goradia, accounts for the

highly complex viscous phenomena associated with slotted airfoils. Associated with the confluent boundary layer, a slot-flow model is defined for flow between slot regions.

The final viscous solution uses an iterative technique to combine the inviscid solution with the boundary layer calculations. The geometry of the 'equivalent airfoil', reflecting local boundary layer thicknesses, is successively defined over a variable number of iterations until pressure distributions have converged to a steady condition. As the work described in this report was more of a qualitative nature than quantitative, only one iteration between viscous and inviscid calculations is made, in the interest of reduced computation time. A comparison of predicted and experimental pressure coefficients using the program for a two-element airfoil appears in figure (15). A listing and description of program input is given in appendix (i) for the 4-element airfoil considered in this work.

4 OPTIMIZATION PROCEDURE

4.1 Geometry Modifications

The choice of evolution strategy required the preliminary development of the following:

- A. Scheme for Random Geometry Modifications
- B. Mutation Length Control
- C. Criterion for Convergence to Optimum
- D. Initial Airfoil Geometry

Of fundamental importance to the effectiveness of evolution strategy is the combination of large and small mutation lengths. If only small sizes are used, the number of improved cases will be high, but the rate of progress will be slow. On the other hand, if only large sizes are used, the optimum may be entirely skipped over. For this reason, new cases were divided into 3 groups, one having all mutation lengths of a base value, the second group having lengths of 50% of the base value, and the third group having lengths 150% of the base.

The control of the value of this base mutation length will be described below. For each new geometry, then, 18 new configurations are generated, divided into 3 groups of 6 cases each. The choice of 18 cases per set was somewhat arbitrary, but it was felt that this would be a good trade-off between effort and resulting improvement. As the optimization procedure was carried out, it was found that 18 cases was a safe choice, as the program used to determine C_l and C_d had certain limitations. In experiment, a smaller number of cases per set might be desirable.

All mutations were generated by a computer program, whose listing appears in appendix (ii) and is described by its logic diagram in figure (16A). The random choice required by this program is made using a random number generator that determines for each case which of the 10 parameters is to be modified, and in the event of a modification, whether the increment is positive or negative. As seen in figure (16C), two columns of mutation lengths are printed. The first gives the three lengths used to modify the x,y position of pivot points. These values represent a percentage of the range defined for each pivot point, as shown in figure (16B). The second column is degrees of mutation for flap deflection and angle of attack.

The Random number generator is a computer system function that returns an even distribution of real values in the range 0.0-1.0. A description of its algorithm is given in appendix (iii).

4.2 Mutation Length Control

As described above, three modification lengths are used for each new set of configurations. The control of the base, or middle length is critical, as rapid convergence to an optimum requires an expansion of mutation size far from the optimum and a compression close to it. In this optimization problem, the base length for a new set was controlled by the best case from the previous set. For instance, if case 1, a member of the third mutation length group, is the best in its set, its mutation length will be used as the base value for the next set. In this way, increasing lengths will be favored. On the other hand, if case 3 is the most improved, smaller lengths will be favored in the next set. Using this scheme, the optimization strategy self-adjusts to the distance from convergence.

4.3 Convergence Criterion

Concerning the question as to when convergence has been reached, a criterion is used that recognizes that mutation lengths will automatically compress as the point of convergence is approached. When the modification of an improved configuration fails to increase C_L/C_d for a minimum C_L , the airfoil has 'approximately converged'. For absolute convergence, an additional set of configurations is generated, based on the best case of the set that failed to improve over the point of approximate convergence. If again there is no improvement, convergence is said to exist.

The procedure proposed to determine the envelope of aerodynamic coefficients is comprised of the following two basic steps:

1. Maximize C_L/C_d while maintaining C_L greater than $C_{L\min}$, the value obtained from the initial geometry
 2. Move across the envelope from the maxima point found from step 1 to the maximum C_L limit, when flow separation occurs
- Results from this procedure are presented in section 5.

4.4 Initial Airfoil Geometry

The initial airfoil configuration was an arbitrary but realistic placement of elements so as to guarantee good flow conditions through the slots. The value of the 10th parameter, angle of attack, was determined from the polar shown in figure (14). An angle of 0.5° was used as it resulted in the maximum C_L/C_d . This initial configuration and angle of attack thus set the value of $C_{L\min}$ at 2.11. In all subsequent program calculations, mach number and Reynolds number, referenced to an airfoil chord of 350mm, were 0.125 and $1.26 \cdot 10^6$, respectively. Element profiles were

taken from reference 14, with appropriate modification to meet
the requirement of smooth contours.

5 RESULTS

5.1 First Three Configuration Sets

The first step of the optimization procedure, the maximization of C_l/C_d with the constraint of $C_{l\min}$, was started at the initial geometry. Figure (17) shows the scatter of data points for the first three sets (54 cases) of airfoil configurations. Some points have been omitted for clarity. Circled data points are best cases for each set; these cases serve as the bases for subsequent modifications. The automatic mutation length control reacts well in these first sets, far from the point of convergence, with an increase in base lengths between sets one and two and a constant base length between sets two and three. As expected, points scattered in the immediate vicinity of the initializing case were from the first mutation length group, and points scattered further away were from the second and third groups. As seen in figure (17), the ratio C_l/C_d appears more sensitive to airfoil modification than C_l . This effect continued for all other sets, with most points located in a narrow C_l band between 2.0 and 3.0 and a scatter of other points in a relatively low C_l/C_d - low C_l region. The tabulation of all configurations (37 sets, 656 cases) is given in Appendix (iv) together with initial and final configuration data.

5.2 Description of Complete Optimization

Figure (18) shows the result of continued maximization of C_l/C_d , plotting the best case for each of 37 sets. Up to set 11, mutation lengths generally expanded or remained constant. Sets 12-14, however, resulted in a compression of lengths, and convergence was thought to be imminent. Beyond set 14, lengths began to expand again until the base value stabilized at approximately 2% and 1° for pivot point location and deflection angles, respectively. This effect was considered to be a 'small barrier' in the optimization process, which the evolution strategy was able to step over with the larger of the three mutation lengths. A gradient strategy-based technique would have converged to such a barrier, or local maximum.

Beyond set 22, the accuracy of the aerodynamic coefficients became questionable, resulting in erratic behavior of the optimization process. When the process was continued without the $C_{l\min}$ constraint, large changes in C_l/C_d and C_l occurred for relatively small geometry modifications. As an attempt to return to smaller variations of coefficients, the process was restarted at set 24

with a forced reduction of step sizes, as shown by the dotted lines of figure (18). This resulted in sets 27 and 28 which again were characterized by large variations of coefficients for small modifications. This sequence of forced length compression and optimization restart was continued to the 37th, but by this point values of C_l/C_d were unrealistically high, even for the simplified two-dimensional airfoil model without induced drag or body interference effects. Indeed, during the process of optimization, numerous configurations resulted in unsuccessful program termination or extremely high values of C_l/C_d and in several cases, negative C_d . The reasons for this inaccuracy are thought to be one or a combination of the following:

- 1 Invalid geometry; i.e., overlap less than 1% of chord
- 2 Confluent boundary layer or slot flow model failures for small slot cross-sections
- 3 Inadequate verification of program by authors for 4-element airfoil configurations (note-the frequency and severity of inaccuracies were substantially less for the preliminary optimization of a 2-element airfoil)

In the further presentation of results, sets 21-22 are taken to be the approximate limit of data accuracy, although all points are shown.

C_l/C_d and C_l are shown with respect to set number in figure (19). The points again are from the best cases for each set. As seen in this figure, the result of 22 sets of configurations and 296 total cases, C_l/C_d has been increased from 4.28 to 36.6, a factor of 8.55. At the same time, C_l has been increased from 2.31 to 2.59, a result that evolved by favoring the configuration having the larger C_l when two or more had approximately the same C_l/C_d . Increasing C_l , however, was not the primary objective of the optimization.

Because of the limit of data accuracy, the optimization process was terminated at the 37th set, thus making it impossible to find the envelope of aerodynamic coefficients and thus carry out the second step of the proposed optimization.

5.3 Initial-Final Configuration Comparison

Figure (20) shows polars generated for the initial configuration and the configurations resulting from the process of C_l/C_d maximization. The resulting dramatic improvement in aerodynamic performance is apparent. During the process of optimization, a number of configurations produced values of C_l/C_d and C_l that when plotted fall to the right of the polar for maximized C_l/C_d . A polar

was generated from the point that was furthest to the right and is denoted as the 'optimized C_l configuration'. This configuration, it is interesting to note, was a member of the optimum C_l/C_d set, number 22. The dotted lines have been added to these polars to show the real flow behavior for multi-element airfoils such as shown in figure (2).

A comparison of initial and final configurations is given in figure (21). A noticeable effect of the optimization is the reduction of slot area and improved contour smoothness of the trailing edge flaps. Both of these effects have been shown experimentally to improve aerodynamic performance. The same changes did not occur for the leading edge flap. It was found that the multi-element airfoil program was very sensitive to reduction of slot area of the leading edge device when both trailing edge flaps were present. It is suspected that the reasons for this sensitivity are the same as those mentioned above.

A comparison between the optimum C_l/C_d configuration found using evolution strategy and that suggested by the empirical recommendations of reference 5 was attempted, but the slot geometries required were not capable of being modelled by the airfoil program. Any change from these recommendations so as to suit program input requirements would have resulted in a meaningless comparison.

CONCLUSIONS

Although the inaccuracy of the program used to determine aerodynamic coefficients precluded the full solution of the airfoil performance envelope, the problem of maximizing C_L/C_d was easily handled by the evolution strategy-based optimization technique. A review of existing techniques showed that evolution strategy is the best choice for systems described by 5 or more degrees of freedom, due to its relative incomplexity, flexibility to handle a wide variety of problems, and to the knowledge that the converged solution is an absolute optimum within the range of variation of these degrees of freedom.

The problem experienced with the use of the above-mentioned program reinforces the opinion that as of yet numerical solution methods are severely limited in their range of application to complex engineering systems, such as for a multi-element airfoil with its large number of configurations. The value of numerical methods, however, lies in their ability to provide preliminary results to be used as a starting point for further design refinement in the laboratory. Of course, as long as the limits of numerical methods are not exceeded, experimental optimization may be well predicted.

The next logical step related to the work described here is the application of evolution strategy to optimization in a wind tunnel. A setup is envisioned, similar to those of references 7 and 8, where modifications to the airfoil, analysis of aerodynamic coefficients, and optimization procedure are carried out by on-line computers. The importance of using the wind tunnel is that all configurations of an airfoil are capable of being tested, as opposed to computer model-imposed restrictions such as slot geometry and separation-free flow. An important note is that multi-element airfoils often are designed to perform with separated flow and negative overlap, two conditions that can not exist for the successful use of the program of reference 13.

The effect of increasing C_L/C_d through the modification of slot geometries while at the same time maintaining adequate C_L is best seen for the design trade-off between take-off and cruise flight. Increased C_L/C_d at take-off allows increased rate or angle of climb, decreased overall distance to reach a required screen height, increased take-off weight for the same runway requirement, or a combination of the three. An increase in C_L/C_d at take-off also has a strong influence on cruise flight efficiency through the reduction of the installed power needed for take-off.

By using an evolution-based strategy, the converged optimum is an 'absolute' optimum within the range of variations of the degrees of freedom of a particular system. The question of whether convergence has been obtained or not is thus eliminated; this was not the case for the design of the Boeing 737. This is seen in figure (4) by the 3 increments in $C_{l_{max}}$ for its high-lift devices. At each point, the design was probably considered to be an optimum!

Other areas of aerodynamic design that should lend themselves well to evolution-strategy optimization are the wing-fuselage junction, empennage, supercritical airfoils, engine nacelles, and fuselage rear up-sweep. These design areas are currently approached using procedures similar to those of flap design, the wind tunnel testing of a relatively small number of different configurations. Each of these problems is described by many degrees of freedom, a characteristic that has been shown to be well-suited to evolution strategy. The technique described in this work is by no means restricted to aerodynamic design, however. A wide range of applications can be imagined; the examples included in this report are only a few preliminary cases whose results show promise for this new technique to be used as a powerful tool in the design process.

One can consider the development of evolution strategy as a result of man learning from his observations of nature. Figure (22) depicts what might result if nature learns from the aerodynamic achievements of man.

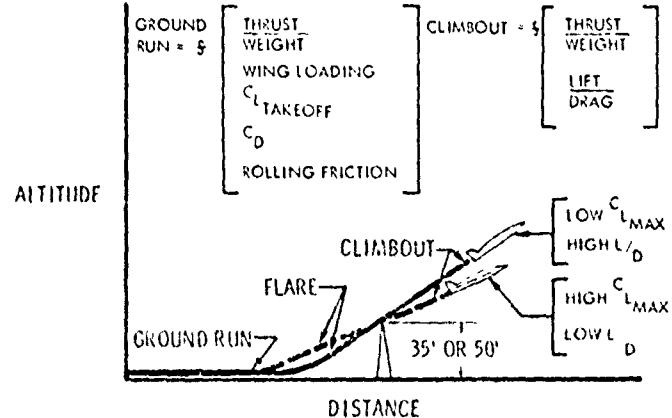
REFERENCES

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2. Steiner, J., et.al., "Case Study in Aircraft Design: The Boeing 727," AIAA Professional Study Series, Sept. 1978.
3. Bruner, G., "Le Boeing 747," DOC-AIR-ESPACE, No.112, Sept. 1968, pg. 7.
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5. Ljungström, B.J.G., "Experimental High Lift Optimization of Multiple Element Airfoils," Proceedings of the AGARD Conference on V/STOL Aerodynamics, AGARD-CP-143, Apr. 1974, pp. 13-1 - 13-16.
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10. Rechenberg, I., "Cybernetic Solution Path of an Experimental Problem," Royal Aircraft Establishment Library Translation No. 1122, Aug. 1965.

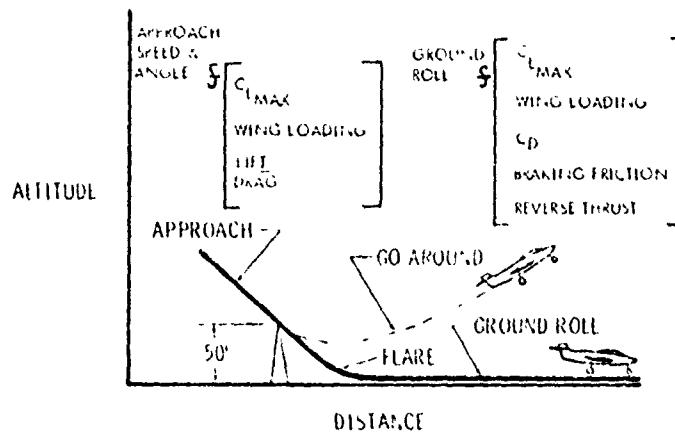
REFERENCES (cont'd)

11. Rechenberg, I., "Evolutionsstrategie, Optimierung Technischer Systeme nach Prinzipien der Biologischen Evolution," No. 15 of Problemata Series, Friedrich Frommann Verlag, Stuttgart-Bad Cannstatt, 1973.
12. Discussion between Professors I. Rechenberg and R. Stoff, Technischen Universitat Berlin, Feb. 1980.
13. Stevens, W., Goradia, S., and Braden, J., "Mathematical Model for Two-Dimensional Multi-Component Airfoils in Viscous Flow," Lockheed-Georgia Company, Marietta, Georgia, NASA CR-1843 and Supplement to NASA CR-1843, July 1971.
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TAKEOFF

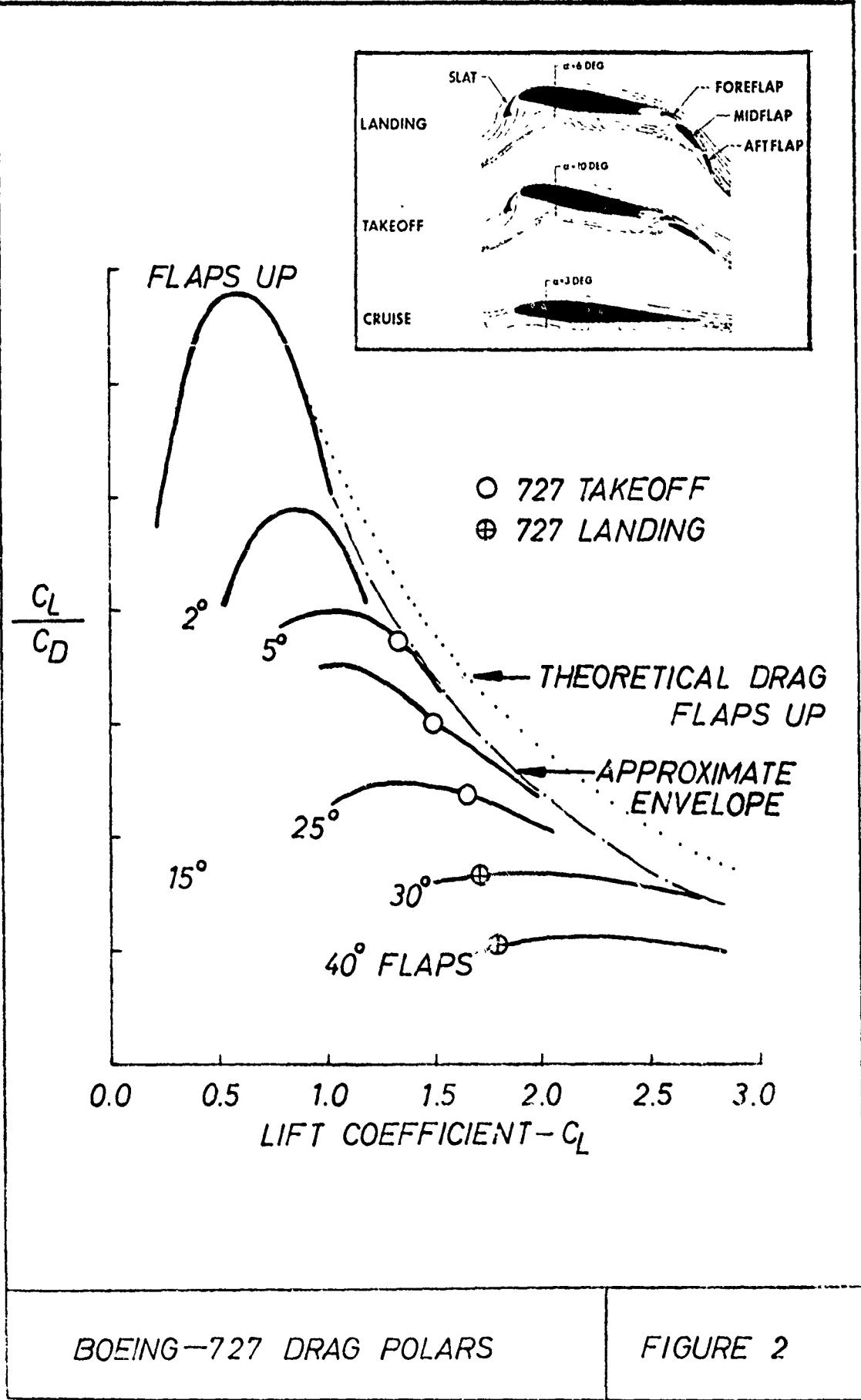


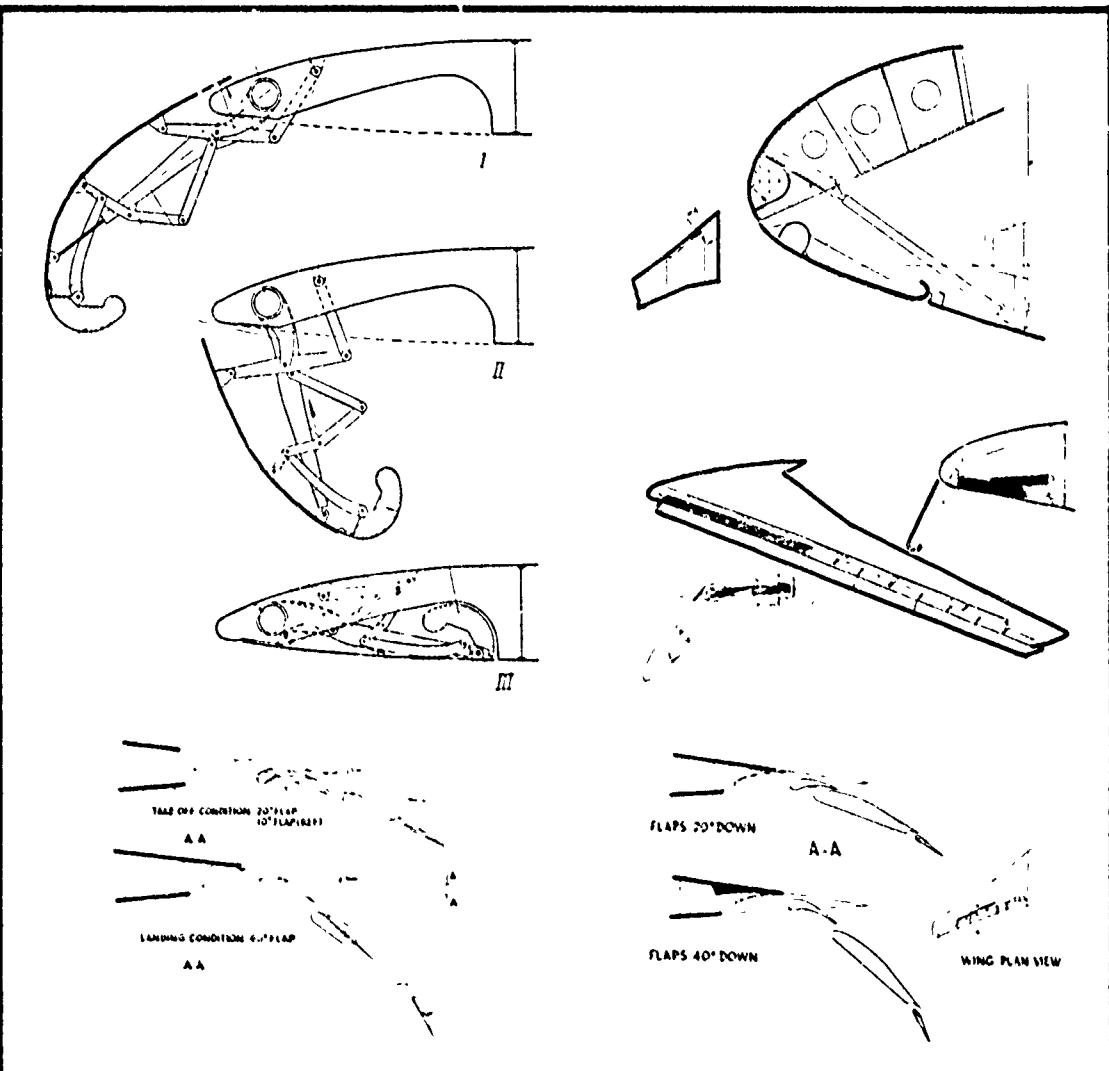
LANDING



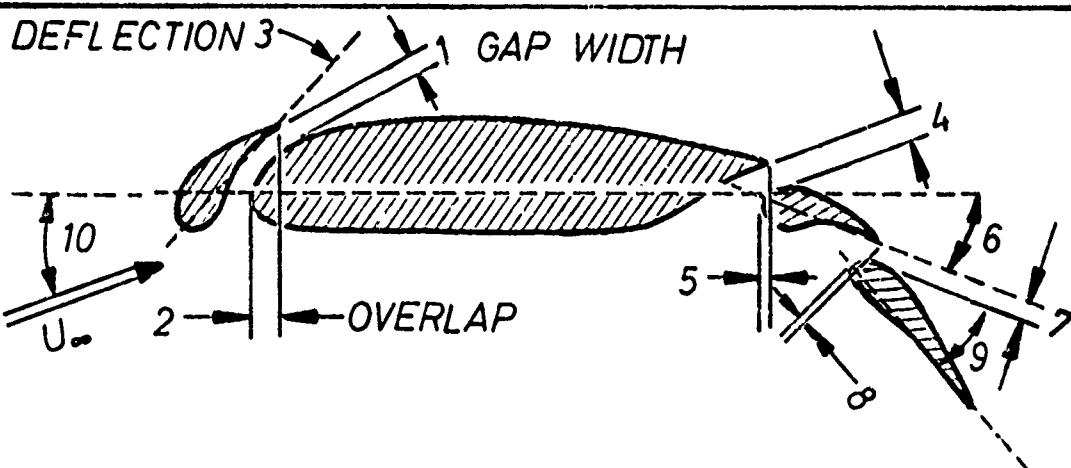
TAKEOFF AND LANDING
AERODYNAMICS

FIGURE 1





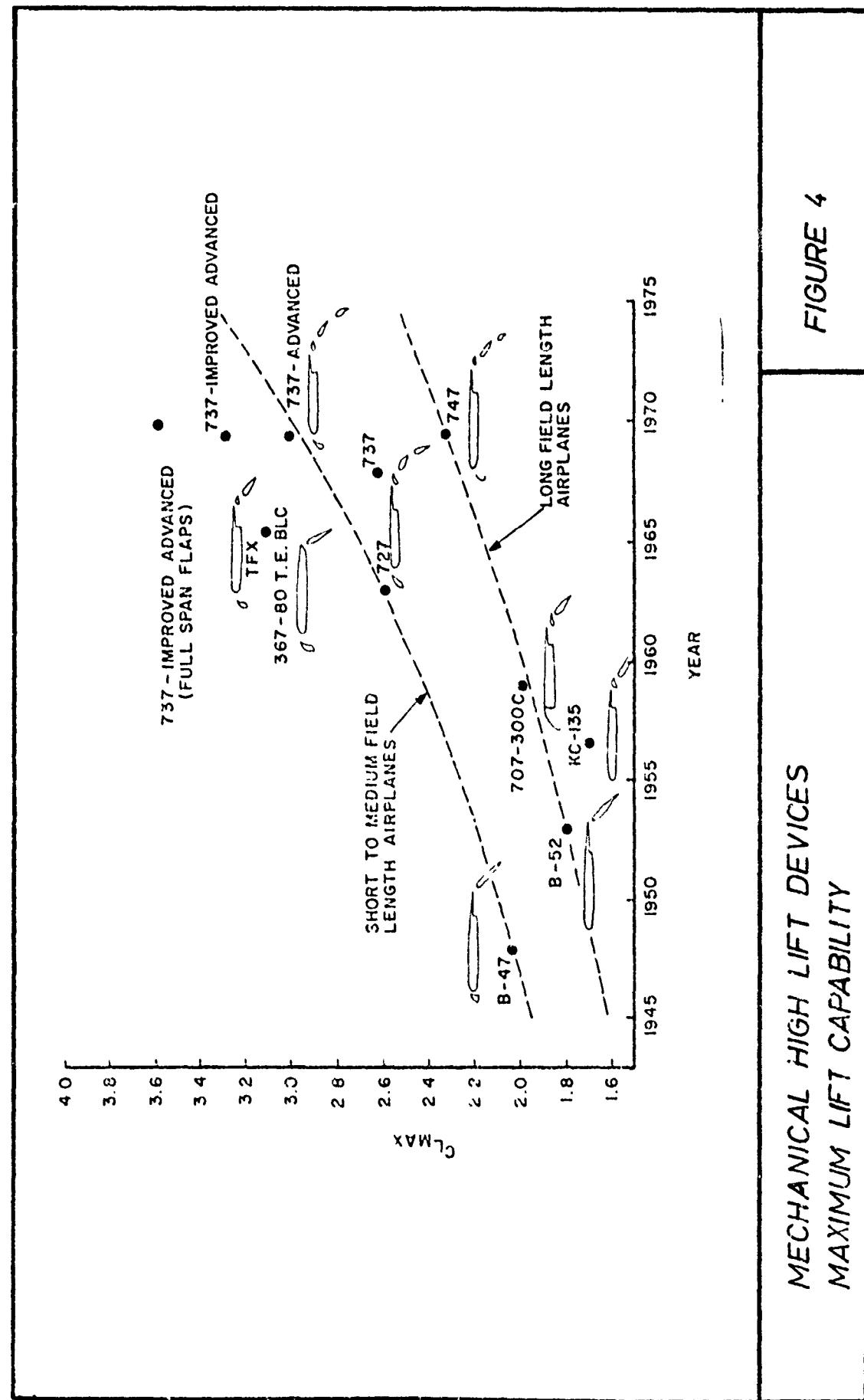
A. HIGH-LIFT DEVICE DETAILS

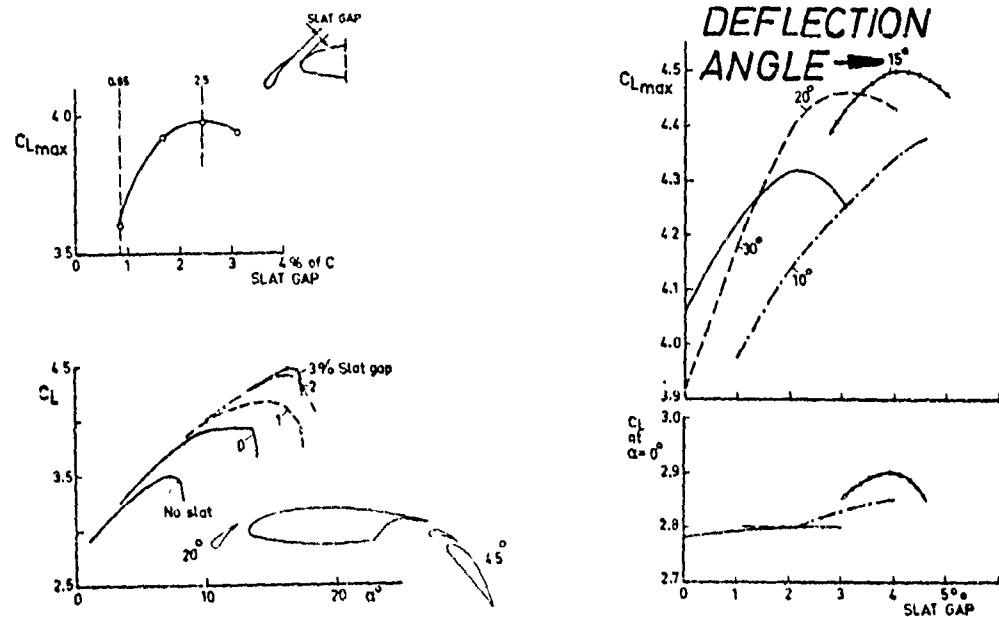


B. AIRFOIL DEGREES OF FREEDOM

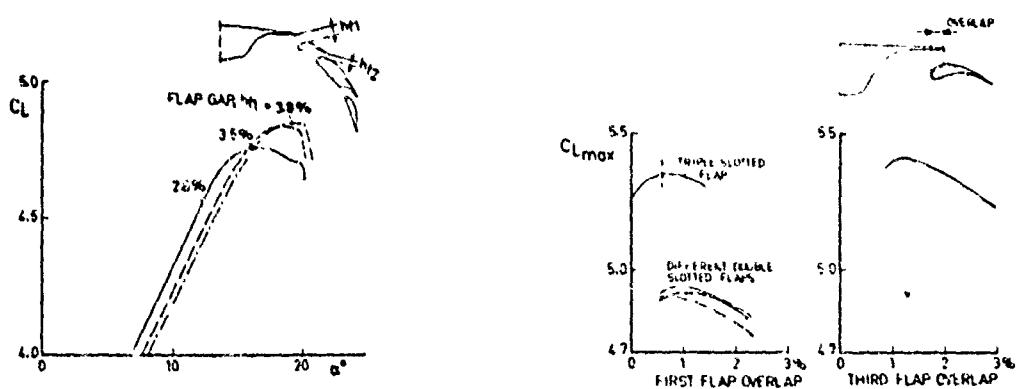
MULTI-ELEMENT AIRFOILS

FIGURE 3

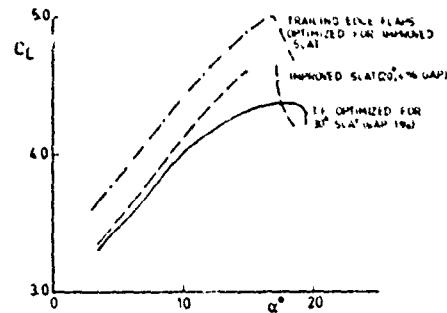




L.E. SLAT GAP & DEFLECTION EFFECTS



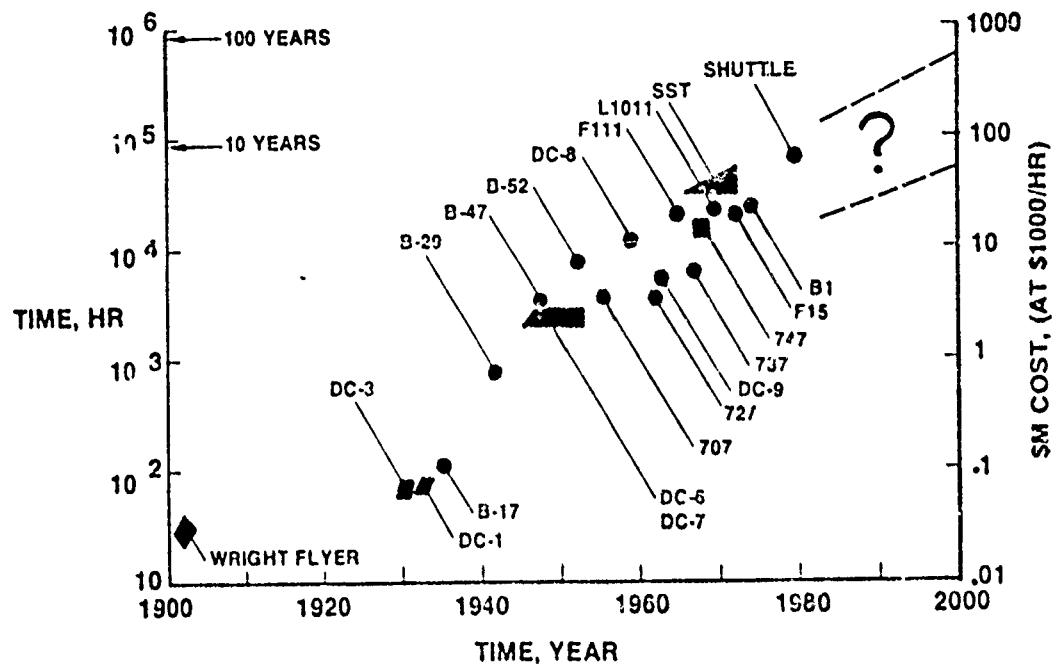
T.E. FLAP GAP & OVERLAP EFFECTS



COMBINED SLAT AND FLAP EFFECTS

FOUR ELEMENT AIRFOIL OPTIMIZATION BY EMPIRICAL METHOD

FIGURE 5



WHAT PRICE ACCURACY ?

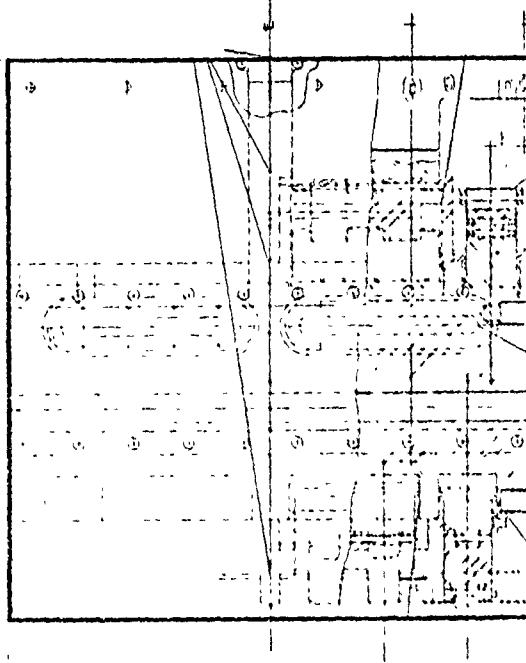
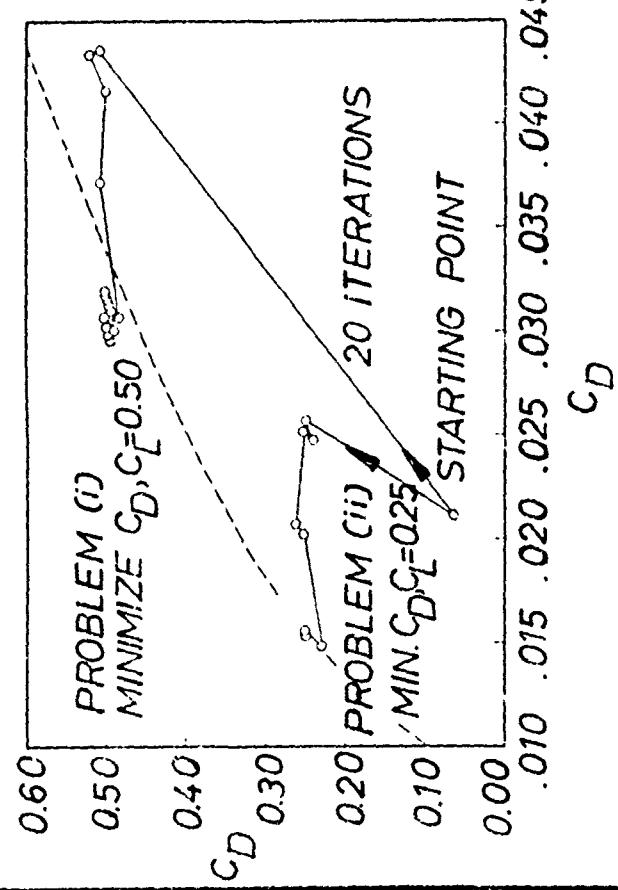
· · · 10^{10} CONFIGURATIONS

· · · 1 MEASUREMENT / 30 SECONDS

· · · TOTAL TIME $9.51 \cdot 10^5$ YEARS

· · · TOTAL COST $\$ 8.33 \cdot 10^{10}$

ENVELOPE SHAPES

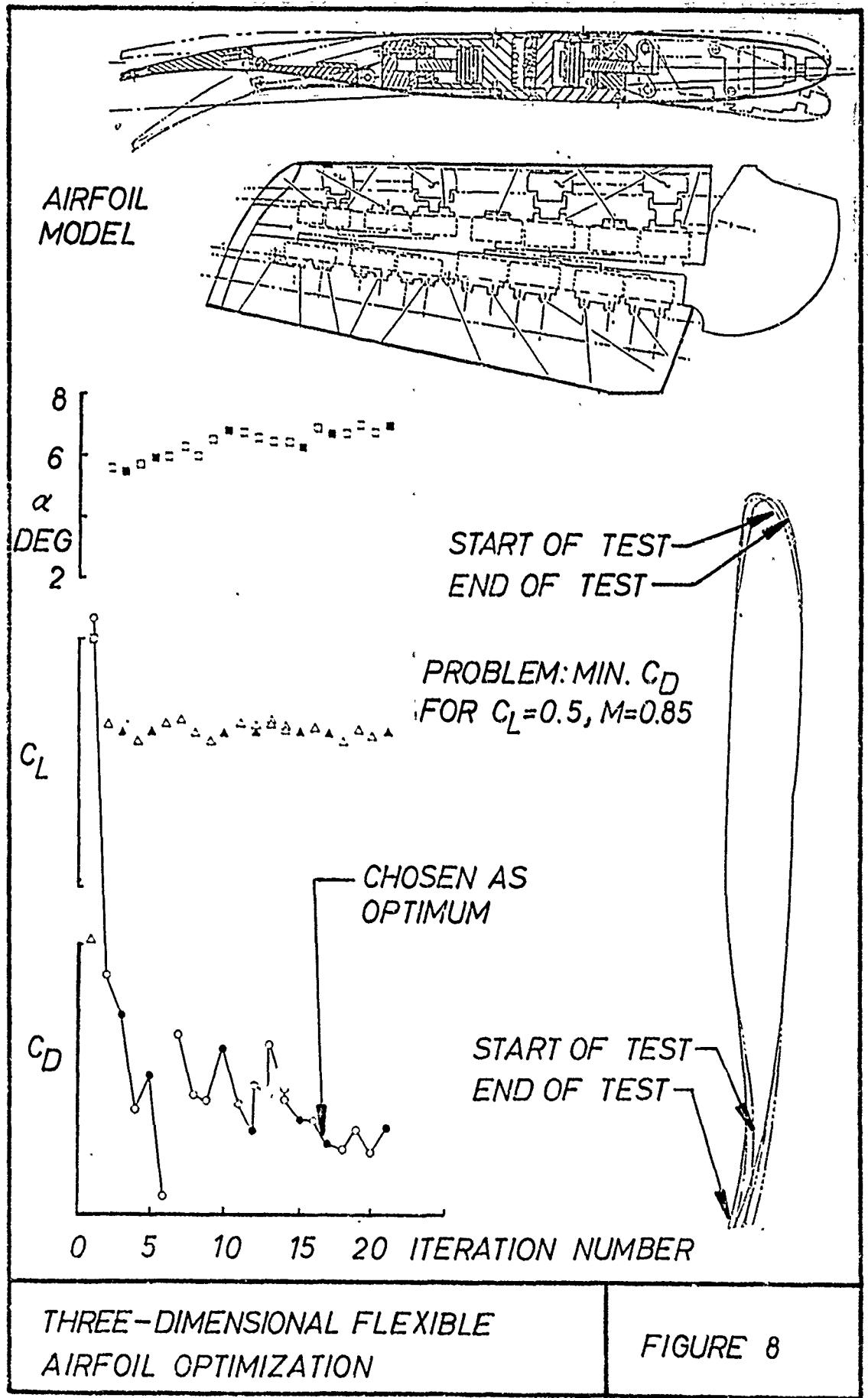


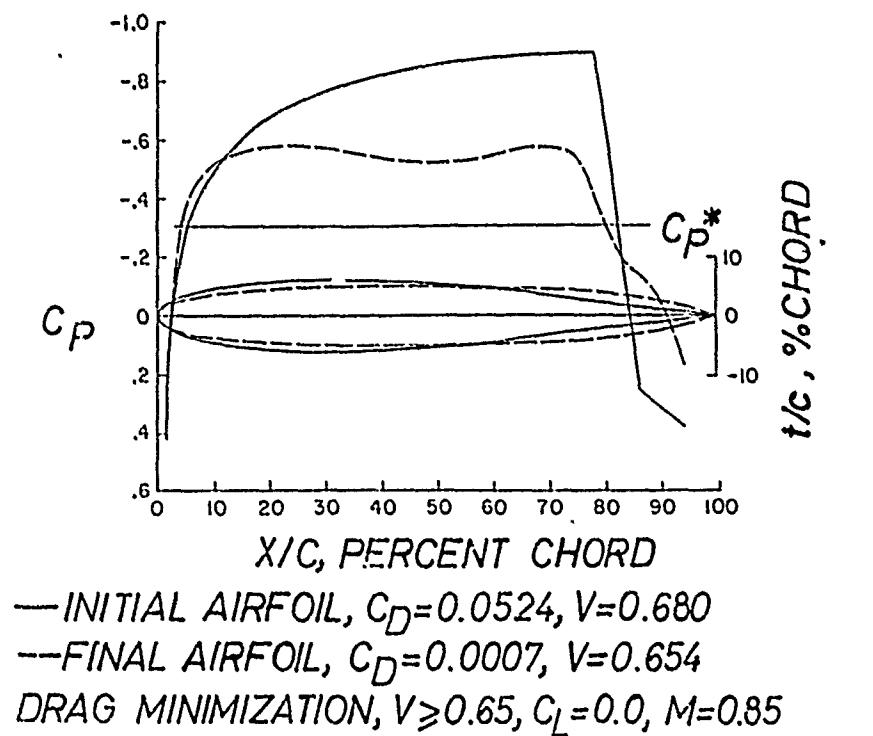
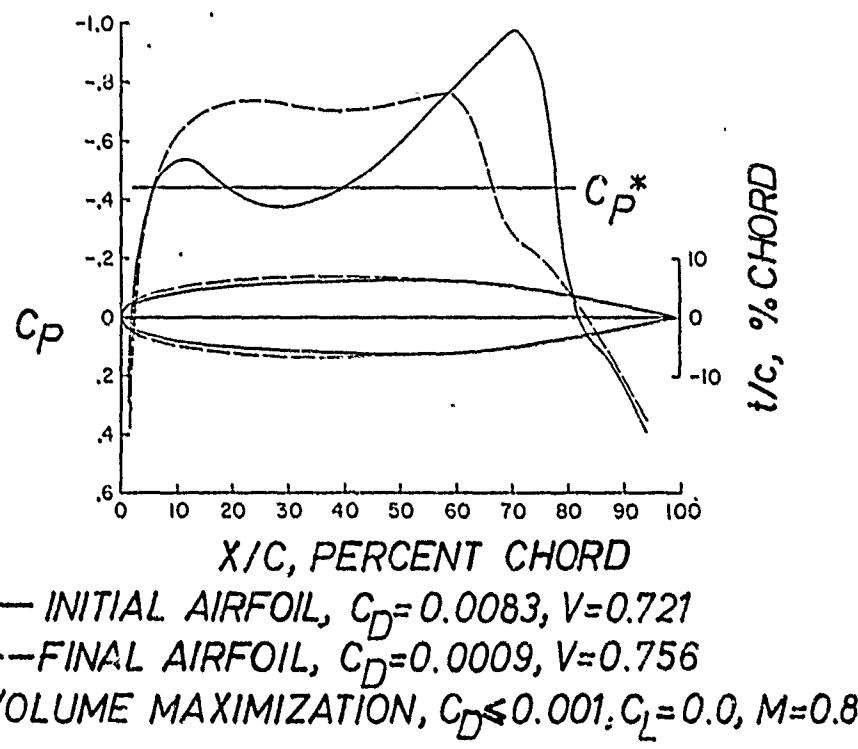
AIRFOIL MODEL



TWO-DIMENSIONAL FLEXIBLE, TRANSONIC AIRFOIL
OPTIMIZATION BY GRADIENT STRATEGY

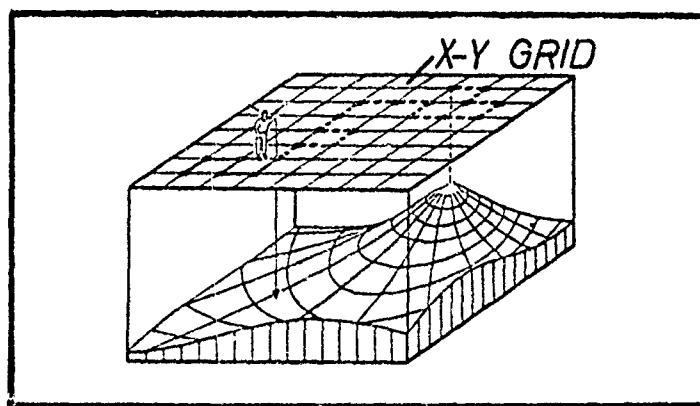
FIGURE 7



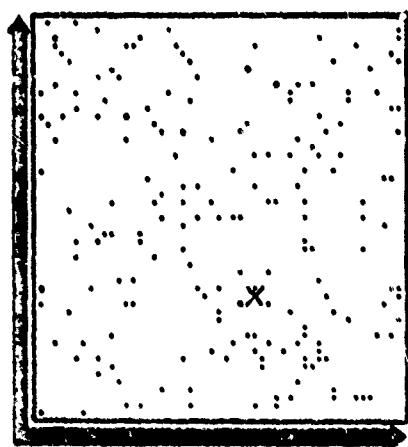


TWO-DIMENSIONAL TRANSONIC
AIRFOIL OPTIMIZATION, GRADIENT ST.

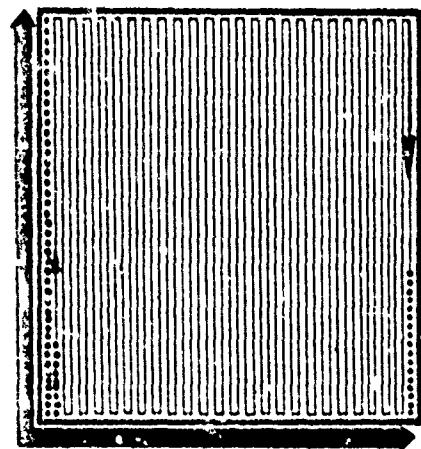
FIGURE 9



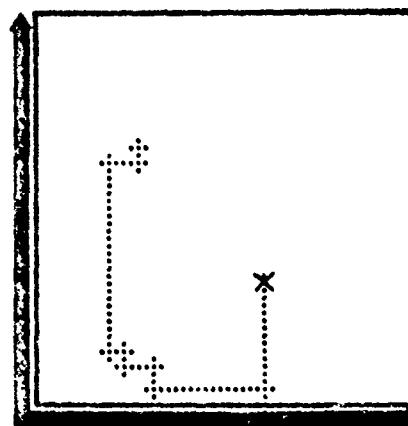
MODEL FOR SIMPLE OPTIMIZATION PROBLEM



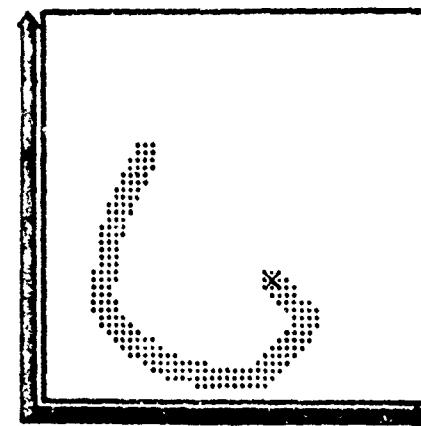
A. RANDOM SOUNDINGS



B. COMPLETE SEARCH



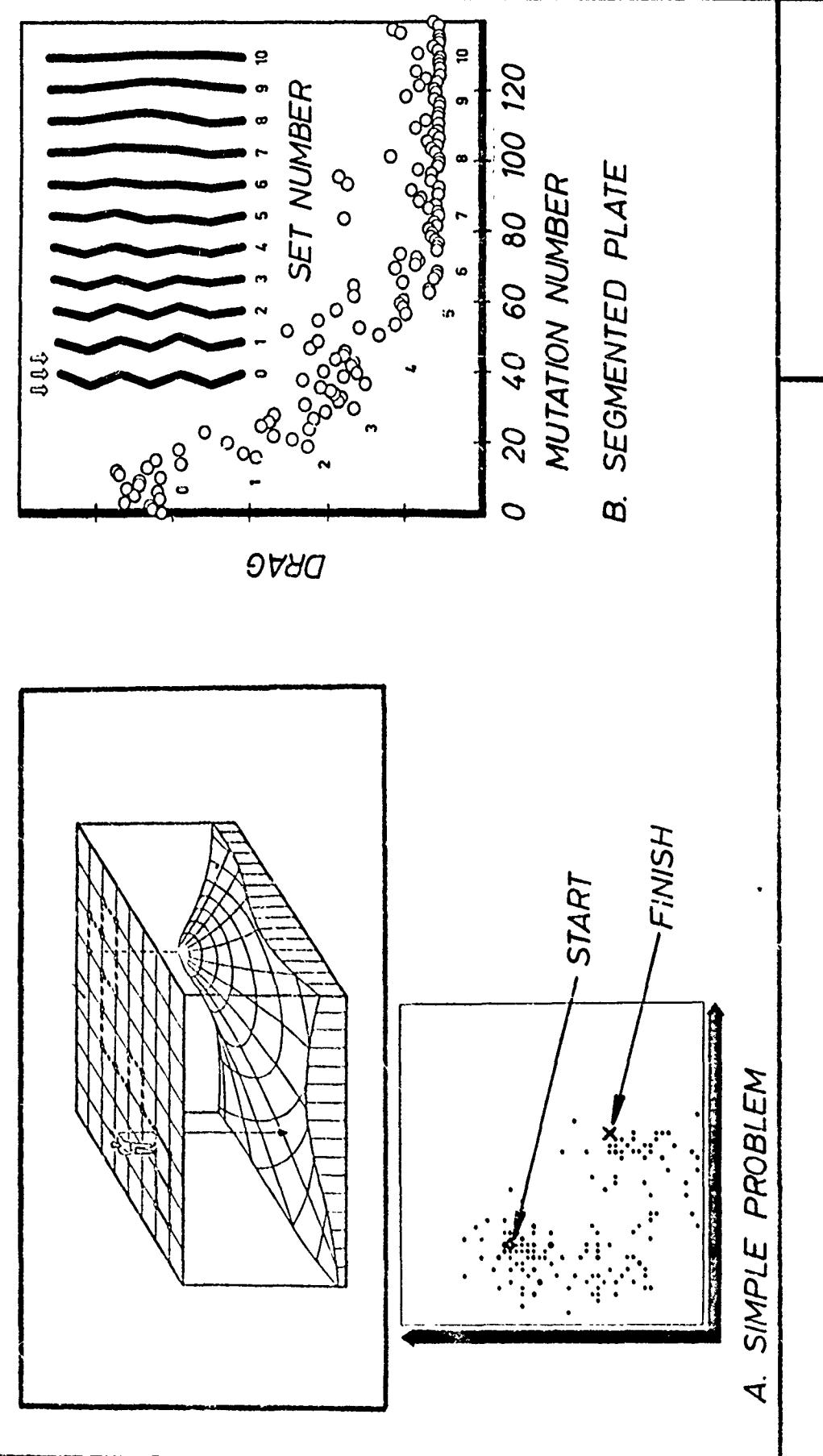
C. GAUSS-SEIDEL STRATEGY



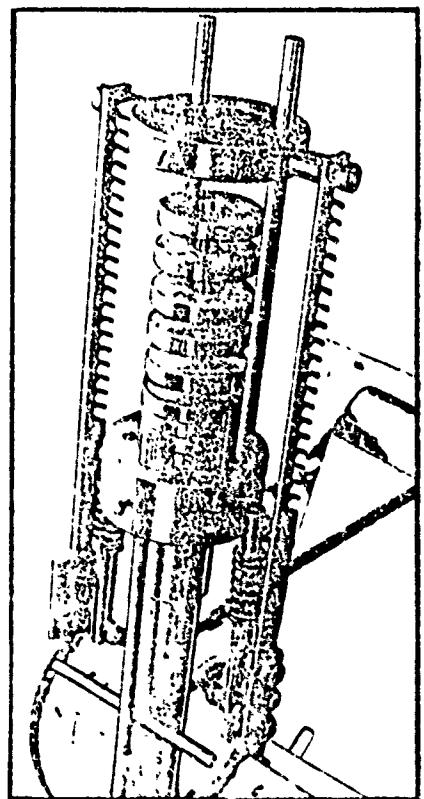
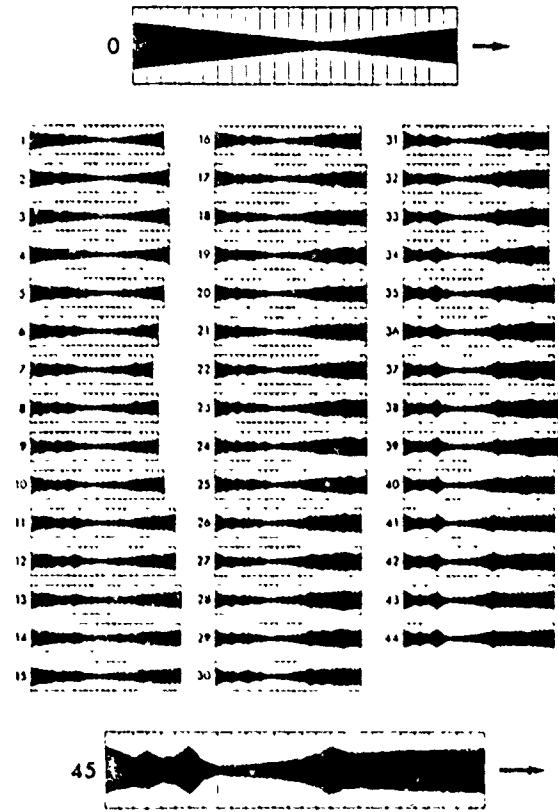
D. GRADIENT STRATEGY

COMPARISON OF OPTIMIZATION STRATEGIES FOR SIMPLE PROBLEM

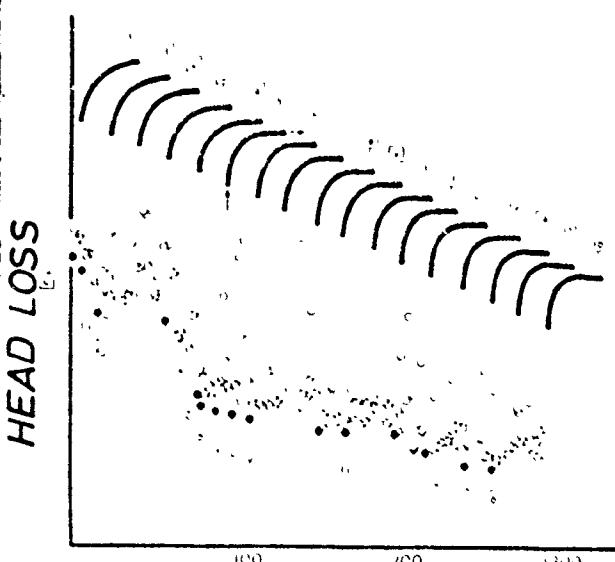
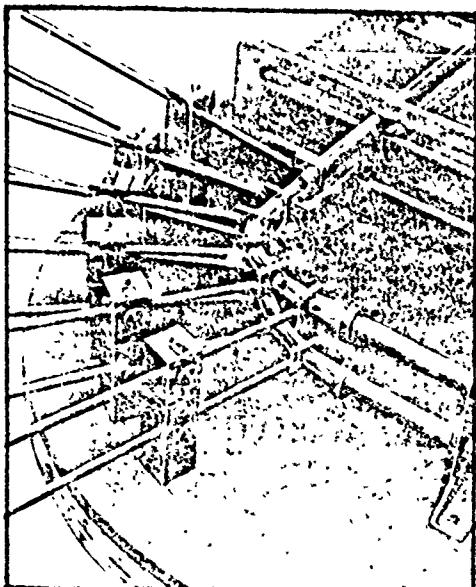
FIGURE 10



EVOLUTION STRATEGY EXAMPLES



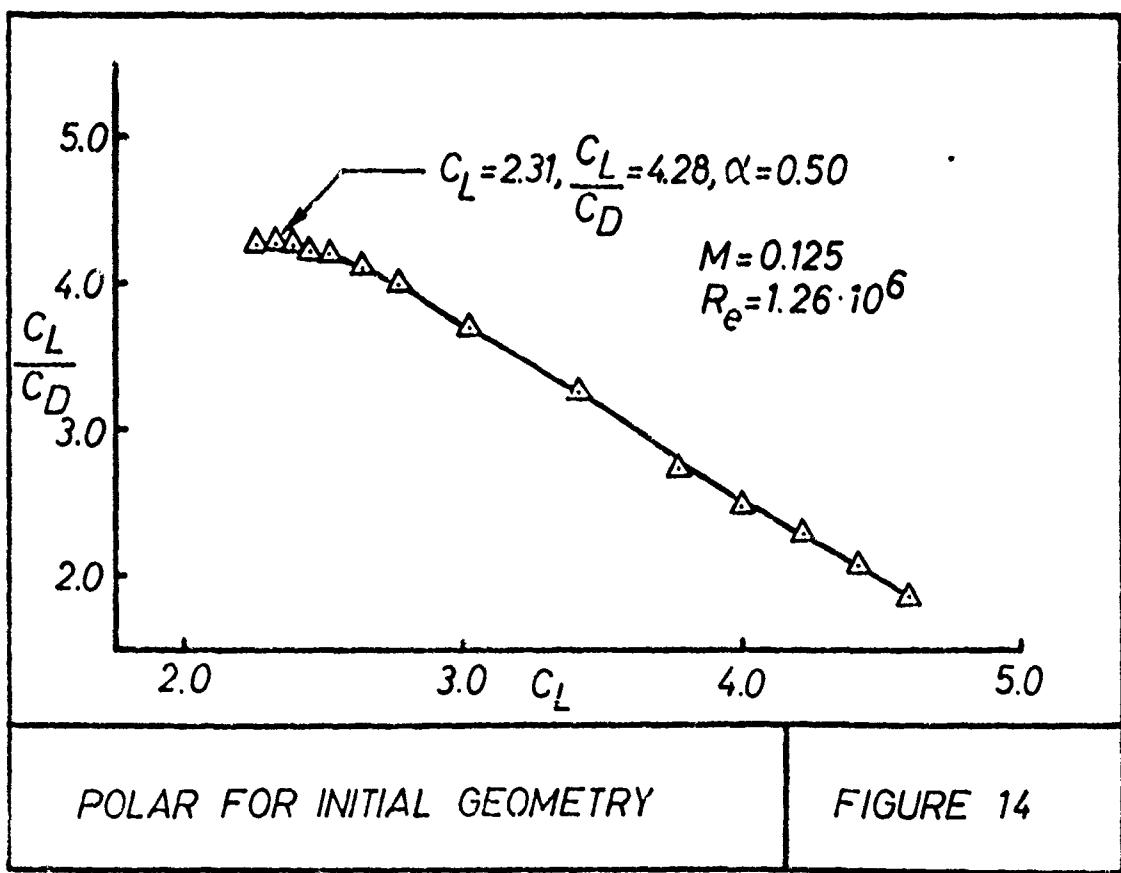
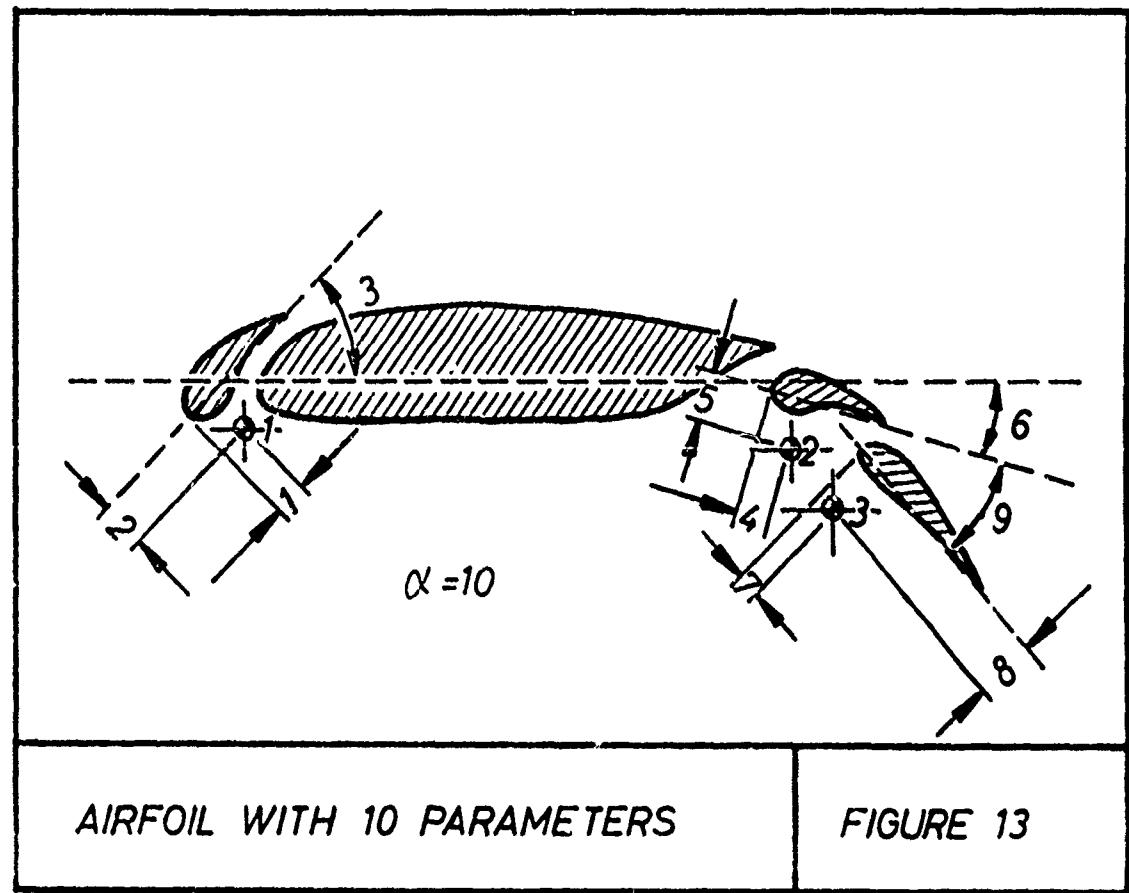
A. TWO-PHASE SUPERSONIC NOZZLE

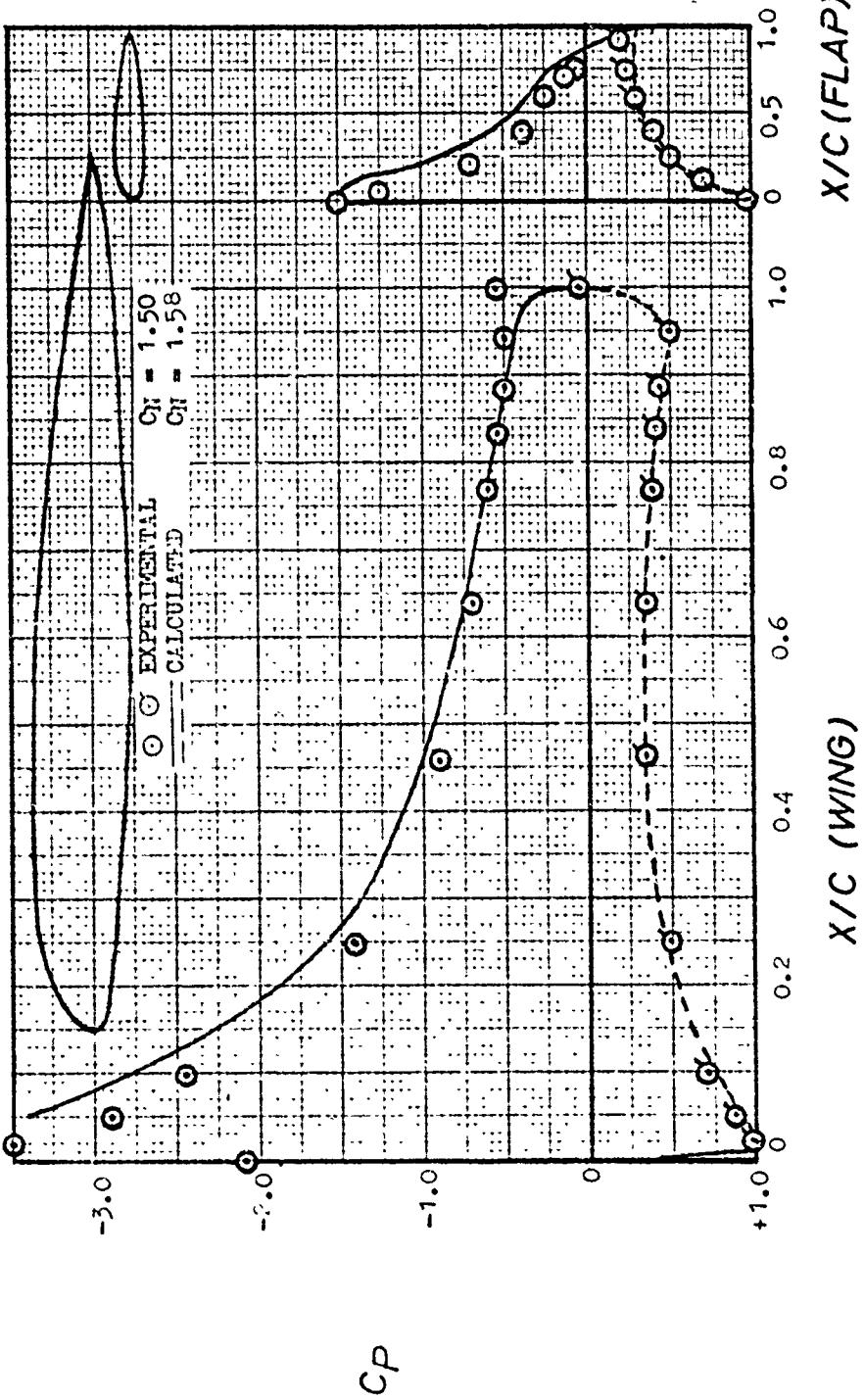


B. 90° FLEXIBLE TUBING BEND

EVOLUTION STRATEGY EXAMPLES
(CONTINUED)

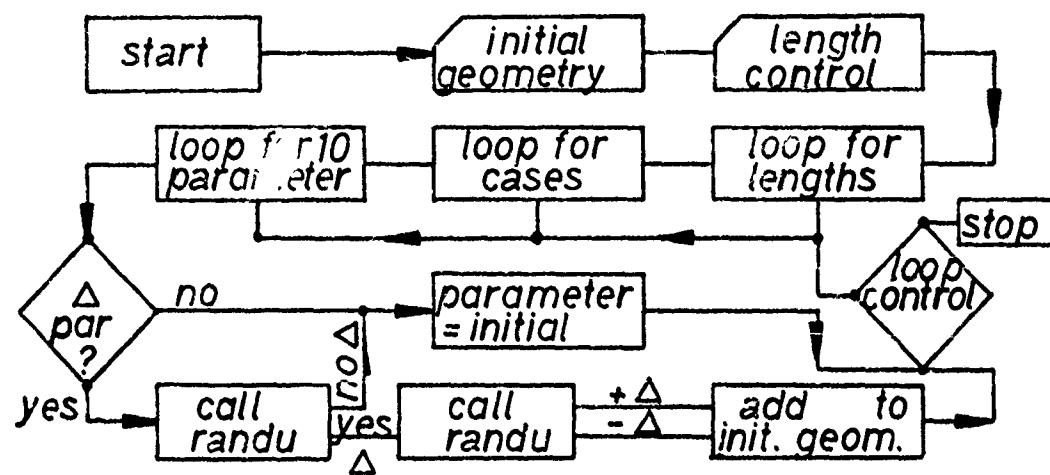
FIGURE 12





COMPARISON OF EXPERIMENTAL AND PREDICTED PRESSURE DISTRIBUTIONS FOR NACA 23012 AIRFOIL WITH T.EDGE FLAP

FIGURE 15



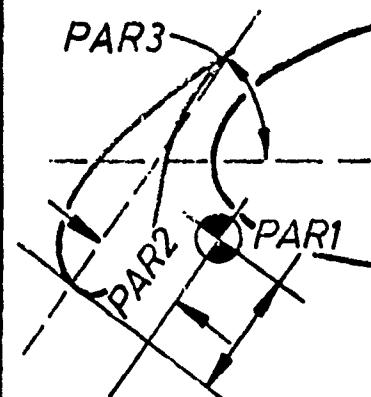
A. PROGRAM FLOWCHART

GEOMETRY MODIFICATION ① — SET NUMBER
 11=12345678943 12= 987654321 13= 3 14= 15= 6
 LENGTH GROUPS →
 10 PARAMETERS →
 INITIAL GEOMETRY →

LEN GRP NO.	S STEP	DEGREE
1	0.75	0.55
2	0.15	2.00

LENGTH GROUP NUM. ①

CASE NUMBER ①



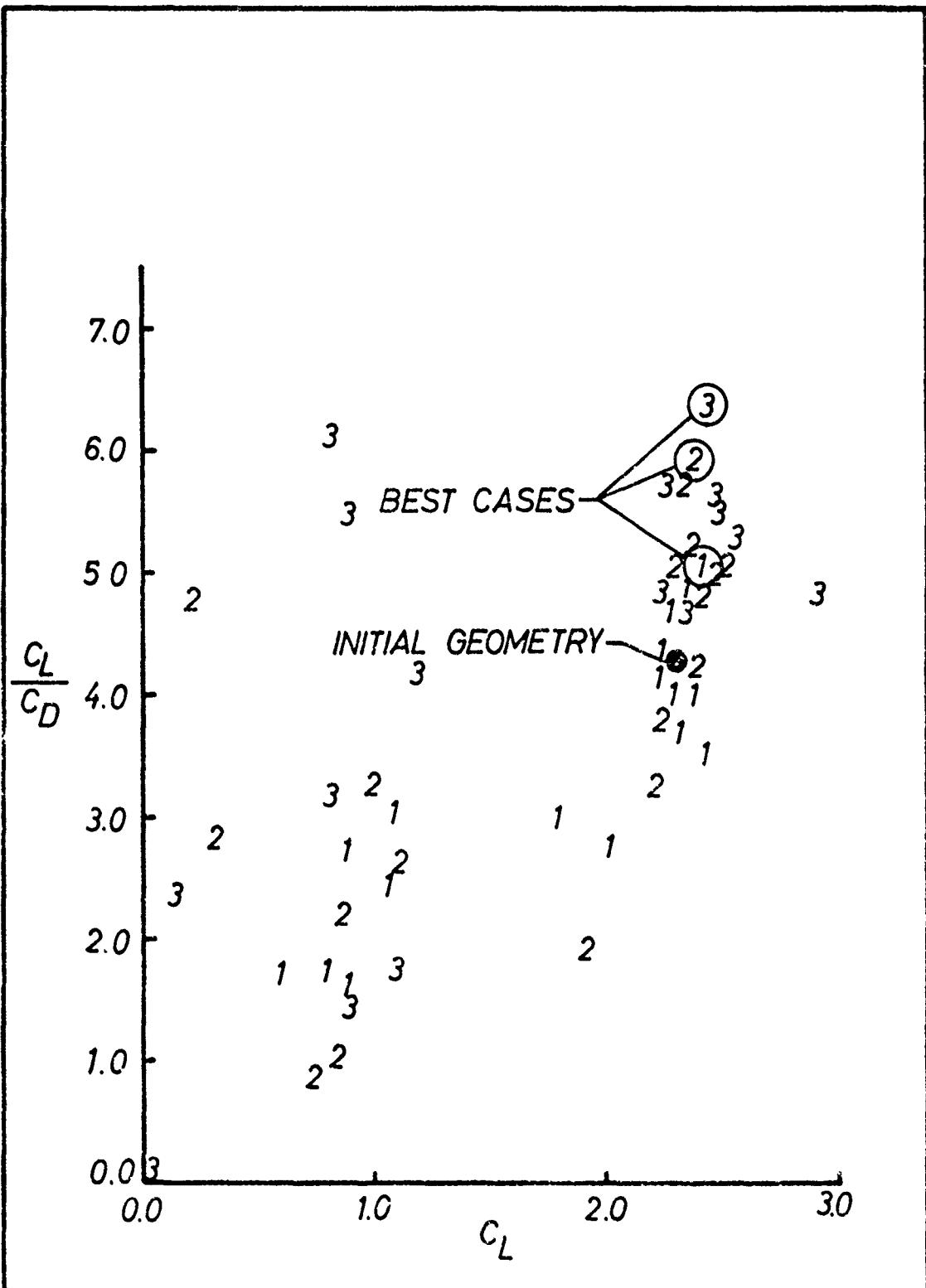
B. VIEW OF PARAMETERS

GRPAH	PAR1	PAR2	PAR3	PAR4	PAR5	PAR6	PAR7	PAR8	PAR9	PAR10
1 1	1.50	-0.50-3.00	0.25	0.00	15.00	0.00	0.00	15.00	0.00	0.00
1 2	1.50	-0.45-3.00	0.17	0.05	14.50	0.00	0.33	15.00	0.00	0.00
1 3	1.50	-0.45-3.00	0.17	0.05	14.50	0.00	0.33	15.00	0.00	0.00
1 4	1.50	-0.45-3.00	0.17	0.05	14.50	0.00	0.33	15.00	0.00	0.00
1 5	1.50	-0.45-3.00	0.17	0.05	14.50	0.00	0.20	15.00	1.00	0.00
1 6	1.50	-0.45-3.00	0.17	0.05	14.50	0.00	0.20	15.00	0.00	0.00
1 7	1.50	-0.45-3.00	0.17	0.05	14.50	0.00	0.20	14.00	0.50	0.00
1 8	1.50	-0.45-3.00	0.17	0.05	14.50	0.00	0.20	14.00	0.50	0.00
1 9	1.50	-0.45-3.00	0.17	0.05	14.50	0.00	0.20	14.00	1.50	0.00
1 10	1.50	-0.45-3.00	0.17	0.05	14.50	0.00	0.20	15.00	0.00	0.00
1 11	1.50	-0.45-3.00	0.17	0.05	14.50	0.00	0.20	15.00	0.00	0.00
1 12	1.50	-0.45-3.00	0.17	0.05	14.50	0.00	0.20	15.00	1.50	0.00
1 13	1.50	-0.45-3.00	0.17	0.05	14.50	0.00	0.22	15.00	0.50	0.00
1 14	1.50	-0.45-3.00	0.17	0.05	14.50	0.00	0.20	15.00	0.50	0.00
1 15	1.50	-0.45-3.00	0.17	0.05	14.50	0.00	0.22	13.00	0.00	0.00
1 16	1.50	-0.45-3.00	0.17	0.05	14.50	0.00	0.22	15.00	0.50	0.00
1 17	1.50	-0.45-3.00	0.17	0.05	14.50	0.00	0.22	15.00	0.50	0.00
1 18	1.50	-0.45-3.00	0.17	0.05	14.50	0.00	0.22	15.00	0.50	0.00
1 19	1.50	-0.45-3.00	0.17	0.05	14.50	0.00	0.22	15.00	0.50	0.00
1 20	1.50	-0.45-3.00	0.17	0.05	14.50	0.00	0.22	15.00	0.50	0.00

C. PROGRAM OUTPUT

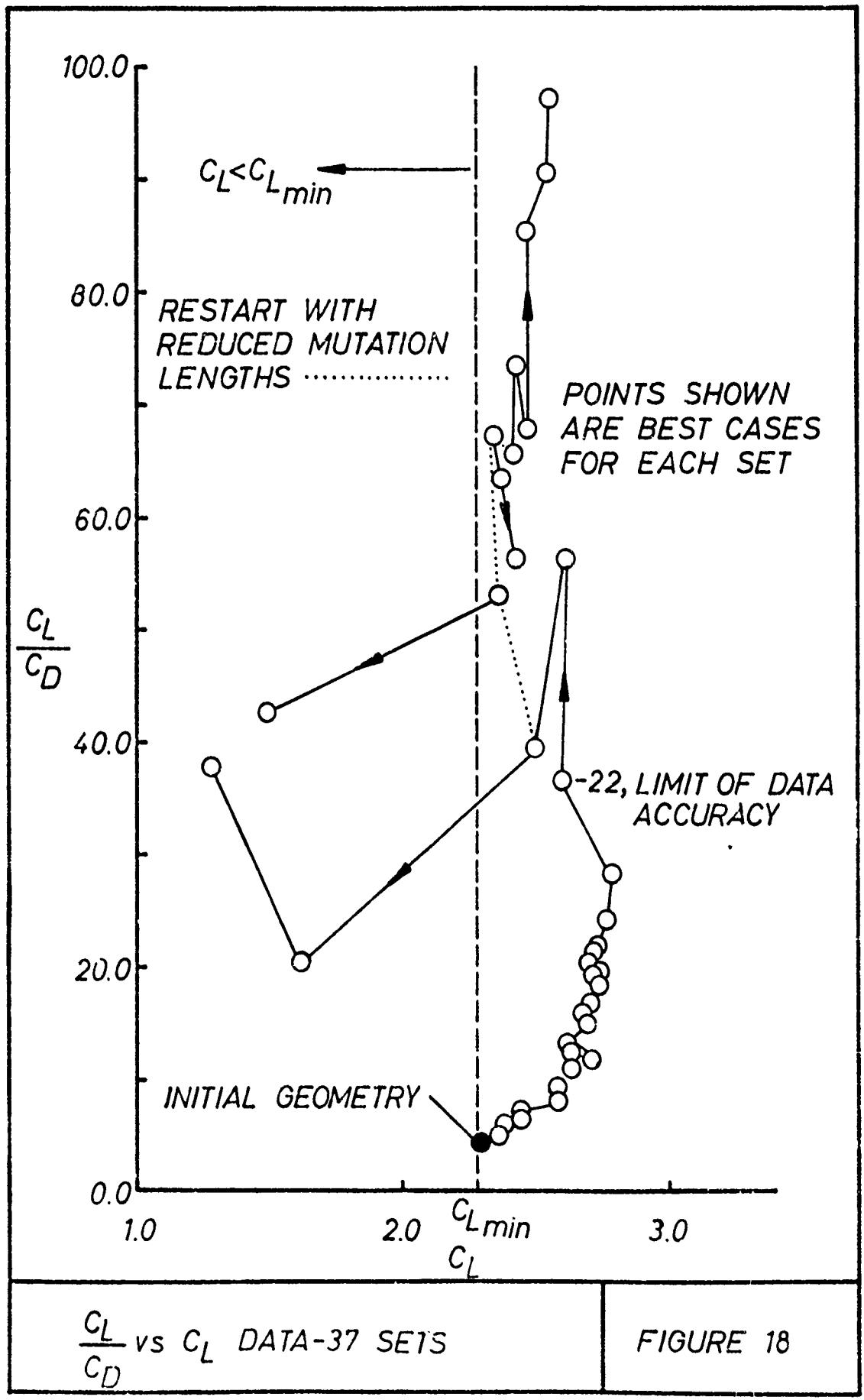
GEOMETRY MODIFICATION PROGRAM

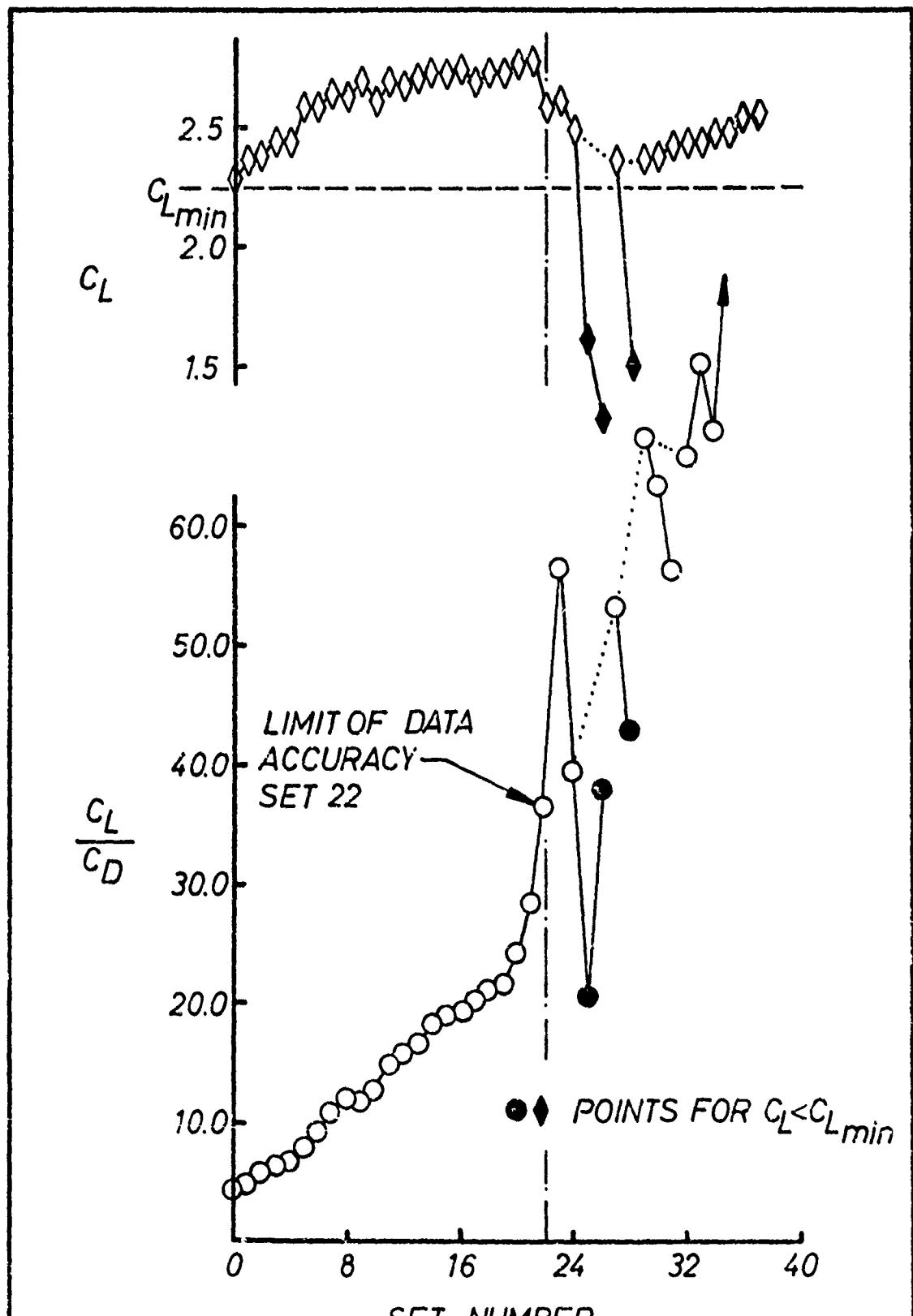
FIGURE 16



OPTIMIZATION PROCESS FOR
FIRST THREE SETS

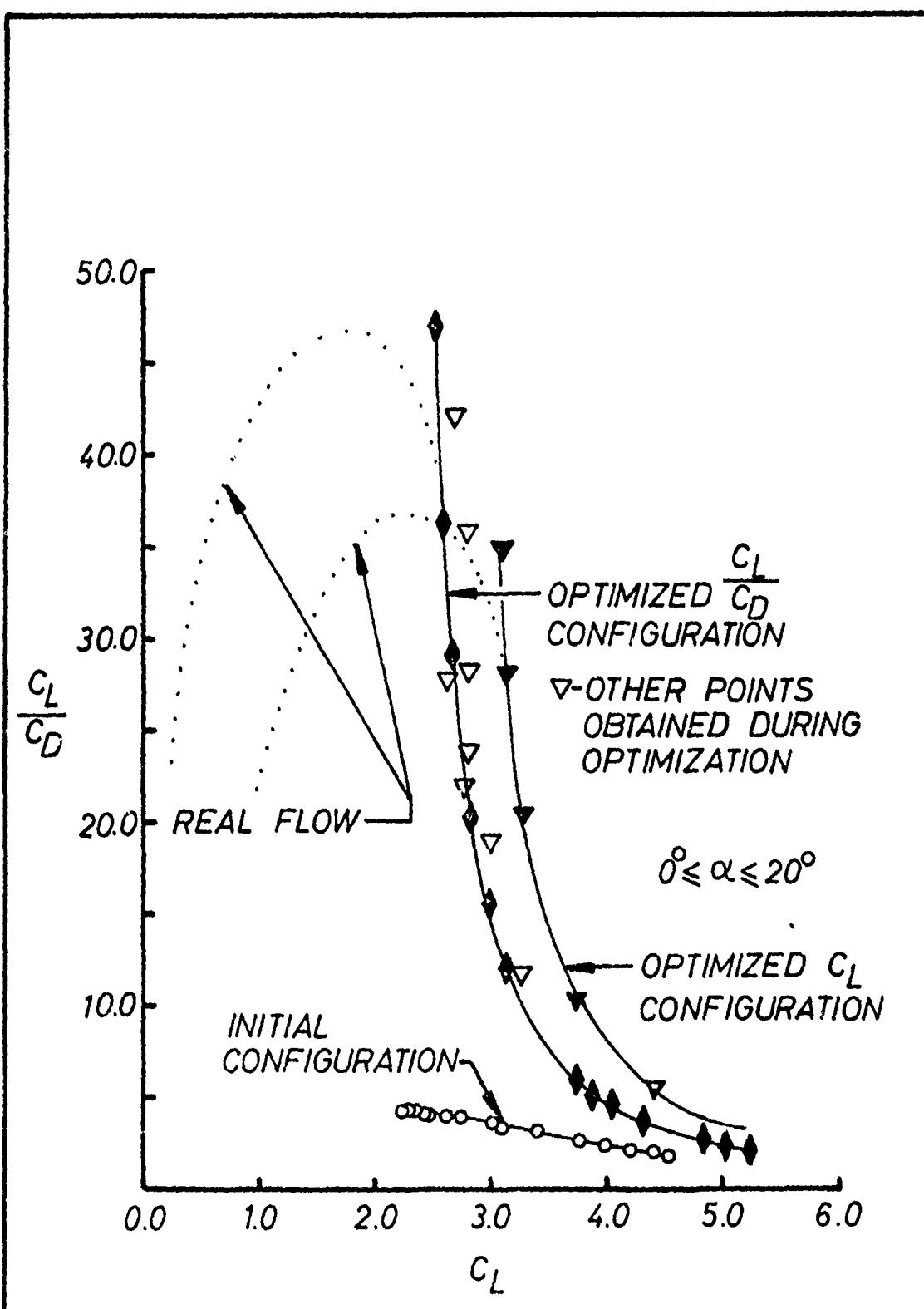
FIGURE 17





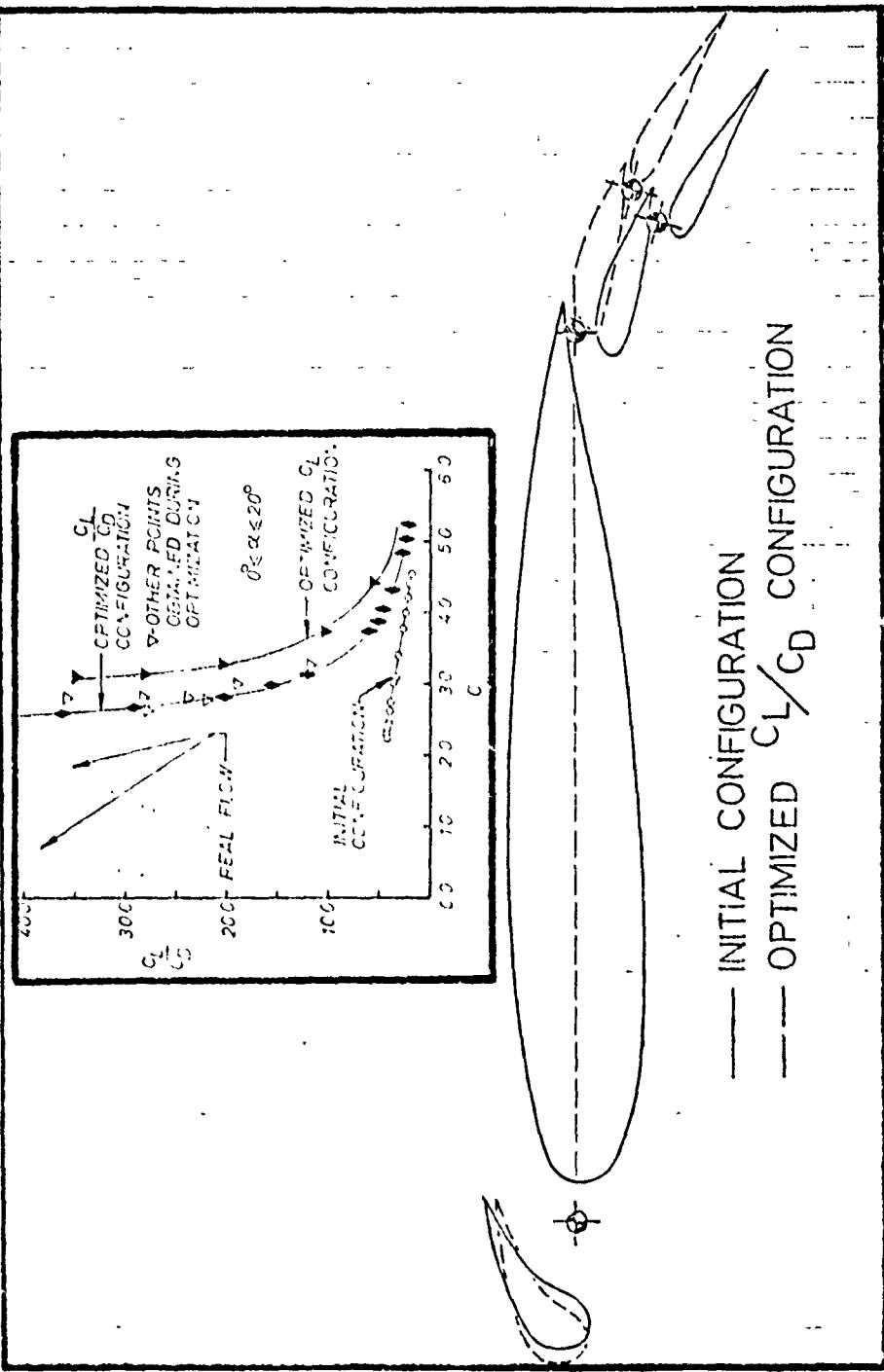
C_L AND $\frac{C_L}{C_D}$ VS. SET NUMBER

FIGURE 19



$\frac{C_L}{C_D}$ VS. C_L POLARS FOR INITIAL AND
OPTIMIZED CONFIGURATIONS

FIGURE 20



COMPARISON OF INITIAL AND FINAL CONFIGURATIONS

FIGURE 21

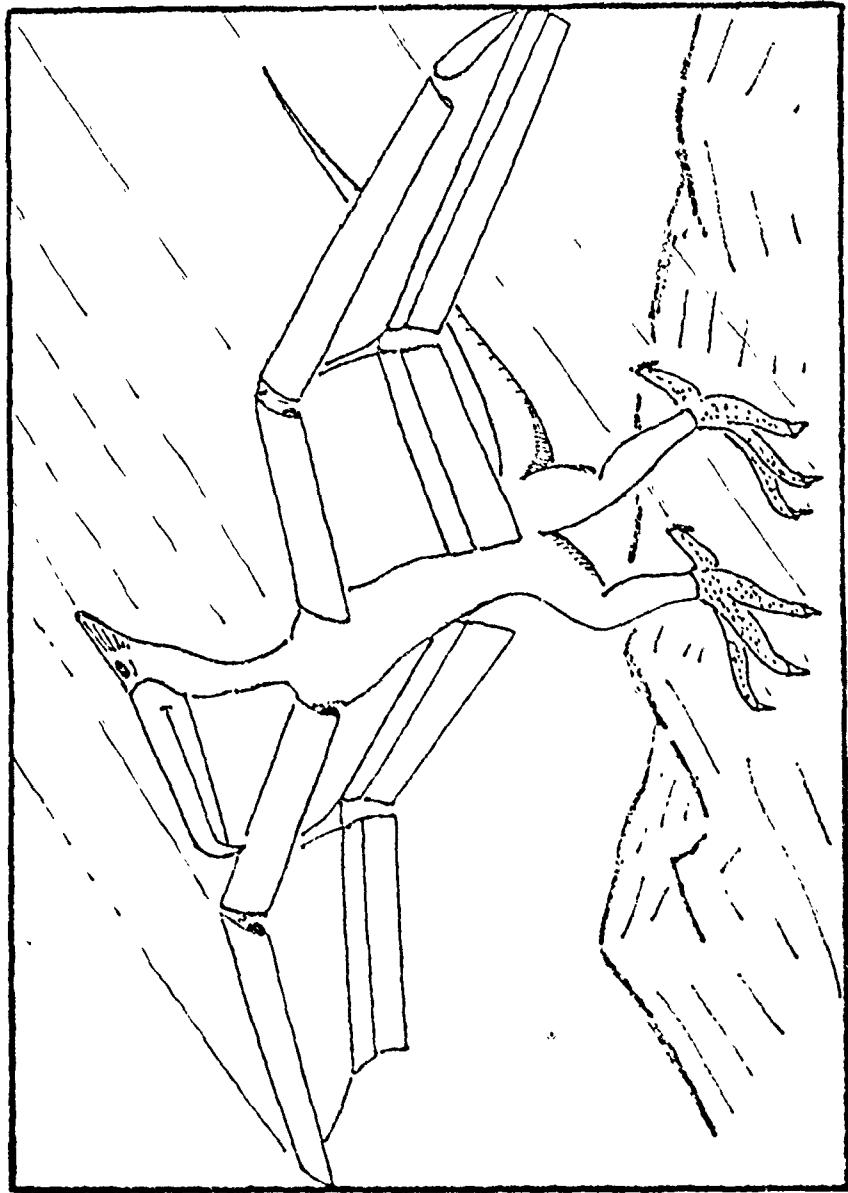


FIGURE 22

EVOLUTION STRATEGY - THE SKY IS THE LIMIT....

APPENDIX (i) AERODYNAMIC COEFFICIENT PROGRAM INPUT

100	*BB-PROFILE A1-725-146	SLOTTED KRUEGER	DOUBLE-SLOTTED TE FLAP OPTIMIZATION					
200	4 85 1							
300	1 23 23							
400	1.6100 -0.4200	0.0689 0.1378	0.2067 0.2756	0.3445 0.4134				
500	0.0000 0.0344	0.8268 0.9646	1.1024 1.2402	1.3780 1.5157				
600	0.5512 0.6890	1.913 1.9291	2.0670 2.2047	2.3425 2.4459				
700	1.6535 1.7913	0.6683 0.7441	0.7992 0.8888	0.8543 0.8619	0.8406 0.8957			
800	0.4134 0.5994	0.9163 0.9026	0.6890 0.6407	0.5925 0.5512	0.5445 0.5130			
900	0.9232 0.9232	0.9163 0.9163	0.9026 0.8888	0.8543 0.8406	0.8406 0.8130			
1000	0.7923 0.7579	0.7303 0.7303	0.6890 0.6407	0.5925 0.5512	0.5445 0.5130			
1100	0.0000 0.0344	0.0689 0.1378	0.2067 0.2756	0.3445 0.4134				
1200	0.5512 0.6890	0.8268 0.9646	1.1024 1.2402	1.3780 1.5157				
1300	1.6535 1.7913	1.9291 2.0670	2.2047 2.3425	2.4459 2.4459				
1400	0.4134 0.2070	0.1378 0.9689	0.3207 0.3858	0.0069 0.4272	0.0000 0.4961			
1500	0.0965 0.2070	0.2894 0.3445	0.3858 0.5512	0.4272 0.5512	0.4961 0.5512			
1600	0.5236 0.5443	0.5512 0.5512	0.5512 0.5512	0.5512 0.5512	0.5512 0.5512			
1700	2 37 37							
1800	-0.5000 0.0000	12.0000 0.0000						
1900	0.0000 0.0344	0.1033 0.1722	0.2411 0.3100	0.3789 0.4478				
2000	0.5167 0.5856	0.6614 0.8364	1.0486 1.3049	1.6150 1.9898				
2100	2.4145 2.9929	3.6571 4.3543	5.3984 6.4433	7.1406 7.7358				
2200	8.2181 8.6122	8.9264 9.1951	9.6870 10.1004	10.6033 11.2110				
2300	11.5596 11.9110	12.2252 12.5091	12.5394 12.5394					
2400	0.0000 0.1654	0.2632 0.3238	0.3707 0.4079	0.4396 0.4685				
2500	0.4919 0.5154	0.5374 0.5843	0.6339 0.6548	0.7372 0.7896				
2600	0.8433 0.8929	0.9384 0.9701	0.9893 0.9756	0.9467 0.9067				
2700	0.8654 0.8254	0.7896 0.7551	0.6862 0.6228	0.5374 0.4258				
2800	0.3596 0.2921	0.2301 0.1791	0.1722 0.2411	0.3100 0.3789	0.4478 0.4478			
2900	0.0000 0.0344	0.1033 0.1722	0.2411 0.3100	0.3789 0.4478				
3000	0.5167 0.5856	0.6614 0.8364	1.0486 1.3049	1.6150 1.9898				
3100	2.4445 2.9929	3.6571 4.3543	5.3984 6.4433	7.1406 7.7358				
3200	8.2181 8.6122	8.9264 9.1951	9.6870 10.1004	10.6033 11.2110				
3300	11.5596 11.9110	12.2252 12.5091	12.5394 12.5394					
3400	0.0000 -0.2287	-0.3514 -0.4203	-0.4713 -0.5140	-0.5484 -0.5787				
3500	-0.6063 -0.6311	-0.6559 -0.7069	-0.7606 -0.8157	-0.8681 -0.9163				
3600	-0.9577 -0.9894	-1.0031 -0.9921	-0.9395 -0.8392	-0.7427 -0.6476				
3700	-0.5650 -0.4974	-0.4437 -0.3982	-0.3142 -0.2467	-0.1695 -0.0897				
3800	-0.0551 0.0344	0.1378 0.1654	0.1722 0.1722					
3900	2 23 23							
4000	-0.1000 0.2200	2.0669 -0.1378						
4100	0.0000 0.013d	0.0413 0.0896	0.1516 0.2136	0.275b 0.4134				
4200	0.5512 0.6890	0.8268 0.9646	1.1024 1.2402	1.3780 1.5157				
4300	1.6535 1.7913	1.9291 2.0669	2.2047 2.3425	2.4803 2.4803				
4400	0.0000 0.0965	0.1376 0.1929	0.2343 0.2756	0.3031 0.3445				
4500	0.3720 0.3858	0.3927 0.3858	0.3789 0.3583	0.3307 0.3031				
4600	0.2756 0.2343	0.1929 0.1516	0.1033 0.0482	0.0000 0.275b	0.4134 0.4134			
4700	0.0000 0.013d	0.0413 0.0896	0.1516 0.2136	0.275b 0.4134				
4800	0.5512 0.6890	0.8268 0.9646	1.1024 1.2402	1.3780 1.5157				
4900	1.6535 1.7913	1.9291 2.0669	2.2047 2.3425	2.4803 2.4803				
5000	0.0000 -0.0344	-0.0669 -0.1033	-0.1240 -0.139	-0.1378 -0.1378	-0.1378 -0.1309			
5100	-0.1419 -0.1461	-0.1516 -0.1516	-0.1516 -0.1461	-0.1419 -0.1419	-0.1419 -0.1419			
5200	-0.1033 0.0756	-0.0482 -0.0276	-0.0276 -0.0138	-0.0069 0.0000				
5300	1 17 17							
5400	-0.1000 0.0000	0.0262 0.0524	0.1047 0.1571	0.2094 0.3142	0.4189 0.4189			
5500	0.0000 0.0262	0.0524 0.0896	0.1047 0.1571	0.2094 0.3142	0.4189 0.4189			
5600	0.5236 0.6283	0.8378 1.0472	1.2567 1.3780	1.7913 2.2047				
5700	2.7559 0.0							
5800	0.0000 0.0882	0.1171 0.1557	0.1846 0.2081	0.2425 0.2659				
5900	0.2797 0.2880	0.2866 0.2673	0.2343 0.2136	0.1406 0.0799				
6000	0.0000 0.0262	0.0524 0.1047	0.1571 0.2094	0.3142 0.4189				
6200	0.5236 0.6283	0.8378 1.0472	1.2567 1.3780	1.7913 2.2047				
6300	2.7559 0.0							
6400	0.0000 -0.0482	-0.0620 -0.0758	-0.0758 -0.0690	-0.0620 -0.0413				
6500	-0.0276 -0.0207	-0.0069 0.0138	0.0138 0.0207	0.0276 0.0207				
6600	0.0000 0.0							
6700	2 0.0000							
6800	1 1 2 1	-22.8700						
6900	3 1 2 2	11.5600						
7000	4 1 3 2	15.1600						
7100	1 0.0000							
7200	1 1 2 1							
7300	1 0.0000							
7400	0.125 0.0							
7500	1.1483 0.0833	1.20 0.710						
7600	518.70 0							
7700	0 0							
7800	0 0							
7900	0 0							
8000	0 0							
8100	0 0							
8200	0 0							
8300	0 0							
8400	0 0							
8500	0 0							
8600	1 THE END							

ELEMENT GEOMETRY

FLOW PARAMETERS

SLOT DATA

APPENDIX (ii) GEOMETRY MODIFICATION PROGRAM

```

100 C-----+
200 C-----+
300 C-----+ PROGRAM GEOM2 : RANDOM MODIFICATION OF XLOG TO DEGREES
400 C-----+ OF FREEDOM
500 C-----+
600 C-----+ CAPABILITIES : A. MODIFY 0-10 PARAMETERS
700 C-----+ B. MAXIMUM 5 MODIFICATION LENGTH GROUPS
800 C-----+ C. MAXIMUM 10 CASES/LENGTH GROUP
900 C-----+
1000 C-----+ DEGREES OF FREEDOM/10 PARAMETERS
1100 C-----+ 1 X-LOCATION, 1ST PIVOT POINT
1200 C-----+ 2 Y-LOCATION, 1ST PIVOT POINT
1300 C-----+ 3 DEFLECTION, 1ST FLAP WRT RAFT AIRFOIL
1400 C-----+ 4 X-LOCATION, 2ND PIVOT POINT
1500 C-----+ 5 Y-LOCATION, 2ND PIVOT POINT
1600 C-----+ 6 DEFLECTION, 2ND FLAP WRT RAFT AIRFOIL
1700 C-----+ 7 X-LOCATION, 3RD PIVOT POINT
1800 C-----+ 8 Y-LOCATION, 3RD PIVOT POINT
1900 C-----+ 9 DEFLECTION, 3RD FLAP WRT 2ND FLAP
2000 C-----+ 10 ANGLE OF ATTACK, RAFT AIRFOIL
2100 C-----+ * ADD DIMENSIONS IN INCHES OR DEGREES +
2200 C-----+
2300 C-----+ IGBTIT: VARIABLE          PURPOSE           FORMAT
2400 C-----+ MODULUS      MODIFICATION SET NUMBER    I2
2500 C-----+ II,IZ      INTEGERS USED BY RANDOM    I10,I10
2600 C-----+ NUMBER GENERATOR, RETURNED
2700 C-----+
2800 C-----+ nLAC      NUMBER OF MODIFICATION LENGTH     I2
2900 C-----+ GROUPS, <=5
3000 C-----+ nCASE     NUMBER CASES/GROUP, <=10      I2
3100 C-----+ nPAR(1)   MODIFICATION CONTROL       I0I2
3200 C-----+ I=1,10    #1, MODIFIED PAR(1)
3300 C-----+ =0, DO NOT MODIFY PAR(1)
3400 C-----+ nPAR      NUMBER OF PARAMETERS TO     I2
3500 C-----+ BE MODIFIED
3600 C-----+ INCR(1)   INCR(1)=INCR(nLAC)=INITIAL    nINC#2
3700 C-----+ I=1,2+nLAC LENGTHS FOR X-1 PIVOT POINT  (P5.2)
3800 C-----+
3900 C-----+ INCR(nLAC+1)=INCR(2+nLAC)=
4000 C-----+ DEGREE MODIFICATION LENGTH FOR
4100 C-----+ FLAP DEFLECTION, RAFTFOIL
4200 C-----+ lPAR(1)   INITIAL VALUES OF 10          I0I0.27
4300 C-----+ I=1,10    PARAMEITRS
4400 C-----+
4500 C-----+
4600 C-----+ INTEGER nLAC,nCASE,nPAR,DEAR(10),II,I2,ADBL,I1,I2,L4,US,ADBU
4700 C-----+ INTEGER b4,BINC
4800 C-----+ REAL PAR(5,10,10),IPAK(10),INCR(10),A1,Z1,A2,Z2,A3,Z3,LACN
4900 C-----+ REAL SIGNR
5000 C-----+ A1,Z1,A2,Z2,A3,Z3 SPECIFY RANGE OF MOTION FOR PIVOT POINTS
5100 C-----+ IN INCHES, HORIZONTAL AND VERTICAL AXIAL DIRECTIONS, AND
5200 C-----+ CAN BE MODIFIED TO 5011 USER
5300 C-----+ DATA X1,Z1,A2,Z2,A3,Z3,ADBL/1.5,1.0,1.5,1.0,1.5,1.0,1.0/
5400 C-----+ ACCEPT 100,MODULUS,II,I2,nINC,nCASE,(nPAR(1)),I=1,10),nPAR
5500 C-----+ 100  FORMAT (I2,/,I10,/,I10,/,I2,/,I2,/,I12,/,I2)
5600 C-----+ ORINC=nINC#2
5700 C-----+ DO 150 I=1,BINC
5800 C-----+ ACCEPT 200,INCR(1)
5900 C-----+ 200  FORMAT (F5.2)
6000 C-----+ 150  CONTINUE
6100 C-----+ ACCEPT 300,(nPAR(1),I=1,10)

6200 C-----+ 300  FORMAT (F6.2,9U7,F6.2)
6300 C-----+ LOOP FOR 10 MODIFICATION LENGTHS
6400 C-----+ DO 1000 b1=1,BINC
6500 C-----+ INCR(b1)=INCR(b1)+0.01
6600 C-----+ LOOP FOR NUMBER OF CASES/LENGTH GROUP
6700 C-----+ DO 900 b2=1,nCASE
6800 C-----+ b4=0
6900 C-----+ LOOP FOR 10 PARAMETERS
7000 C-----+ DO 800 b3=1,10
7100 C-----+ IF (nPAR(b3).NE.1) GOTO 700
7200 C-----+ SHOULD PAR(1) BE MODIFIED
7300 C-----+ 500  BULTE=1
7400 C-----+ CALL RANDU, RANDOM GENERATOR, RANDOM PARAMETER SELECTION
7500 C-----+ CALL RANDU(II,I2,InCR(b1))
7600 C-----+ I=1,CRD(6,0,50) GOTO 600
7700 C-----+ CALL RANDU, RANDOM GENERATOR, POSITIVE OR NEGATIVE LENGTH
7800 C-----+ CALL RANDU(II,I2,InCR(b1))
7900 C-----+ I=(DRG(6,0,0,50)+1)*LT=-1
8000 C-----+

```

```

8100   C
8200   C
8300   C
8400   IF(L3.EQ.1) PAR(L1,L2,L3)=IPAR(1)+(MULT*INCR(L1)*X1)
8500   IF(L3.EQ.2) PAR(L1,L2,L3)=IPAR(2)+(MULT*INCR(L1)*Z1)
8600   IF(L3.EQ.3) PAR(L1,L2,L3)=IPAR(3)+(MULT*INCR(L1+NINC))
8700   IF(L3.EQ.4) PAR(L1,L2,L3)=IPAR(4)+(MULT*INCR(L1)*X2)
8800   IF(L3.EQ.5) PAR(L1,L2,L3)=IPAR(5)+(MULT*INCR(L1)*Z2)
8900   IF(L3.EQ.6) PAR(L1,L2,L3)=IPAR(6)+(MULT*INCR(L1+NINC))
9000   IF(L3.EQ.7) PAR(L1,L2,L3)=IPAR(7)+(MULT*INCR(L1)*X3)
9100   IF(L3.EQ.8) PAR(L1,L2,L3)=IPAR(8)+(MULT*INCR(L1)*Z3)
9200   IF(L3.EQ.9) PAR(L1,L2,L3)=IPAR(9)+(MULT*INCR(L1+NINC))
9300   IF(L3.EQ.10) PAR(L1,L2,L3)=IPAR(10)+(MULT*INCR(L1+NINC))
9400   IF(PAR(L1,L2,10).LT.0.0) GOTO 500
9500   GOTO 750
9600   600   L4=L4+1
9700   C-----CHECK TO PREVENT DUPLICATION OF INITIAL GEOMETRY
9800   IF(L4.EQ.NPAR) GOTO 400
9900   700   PAR(L1,L2,L3)=IPAR(L3)
10000  750   CONTINUE
10100  800   CONTINUE
10200  900   CONTINUE
10300  1000  CONTINUE
10400  1100  WRITE (6,1100) MODNUM,11,12,NINC,NCASE
10500  1100  FORMAT (//,7X,'GEOMETRY MODIFICATION',2X,12//,7X,'I1= ',1,
10600  X     110,2X,'I2= ',110,2X,'NINC',12,2X,'NCASE= ',12,/,9X,
10700  X     'INCR NUM',3X,'% STEP',3X,'DEGREE')
10800  DO 1240 I=1,NINC
10900  INCR(1)=INCR(1)+100.0
11000  WRITE (6,1220) I,INCR(1),INCR(1+NINC)
11100  1220  FORMAT (12X,I2,7X,F5.2,4X,F5.3)
11200  1240  CONTINUE
11300  WRITE (6,1200) (GPAR(I),I=1,10)
11400  1200  FORMAT (//,9X,'PAR1 PAR2 PAR3 PAR4 PAR5 PAR6 PAR7',
11500  X     'PAR8 PAR9 PAR10',/,10(11,5X))
11600  WRITE (6,1300) (PAR(I),I=1,10)
11700  1300  FORMAT ('IN.GE.',10(F6.2))
11800  WRITE (6,1400)
11900  1400  FORMAT ('IN CS ')
12000  DO 1700 L1=1,NINC
12100  DO 1600 L2=1,NCASE
12200  L3=(L1-1)*NCASE+L2
12300  1500  WRITE (6,1500) L1,L3,(PAR(L1,L2,J),J=1,10),
12400  1500  FORMAT (/,X,I2,X,I2,X,10(F6.2),/,9X,'CL= ',6X,
12500  X     'CD= ',6X,'CL/CD= ',6X,'CM= ')
12600  1600  CONTINUE
12700  1700  CONTINUE
12800  STOP 'MODIFICATION COMPLETE'
12900  END

```

APPENDIX (iii) RANDOM NUMBER GENERATOR

D.4.9 RANDU Subroutine

The RANDU subroutine computes a pseudo-random number, as a single precision value uniformly distributed in the range:

0.0 .LE. value .LT. 1.0

Format:

CALL RANDU(il,i2,x)

Arguments:

il,i2

INTEGER*2 variables or array elements that contain the seed for computing the random number.

x

a real variable or array element where the computed random number is stored.

Notes:

1. The values of il and i2 are updated during the computation to contain the updated seed.
2. The algorithm for computing the random number value is as follows:

If $I1=0$, $I2=0$, set generator base

$$X(n+1) = 2^{**16} + 3$$

otherwise

$$X(n+1) = (2^{**16}+3) * X(n) \bmod 2^{**32}$$

Store generator base $X(n+1)$ in I1,I2.

Result is $X(n+1)$ scaled to a real value $Y(n+1)$, for $0.0 \leq Y(n+1) < 1$.

FUNDAMENTALICULTURE

INSTRUMENTAL MODIFICATION 3

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Geometriy Multicellur

5

11= 12345/5874 12= 987656259 NINC= 3 NCASE= 6

INCR NUM	1	5.00	DF.Gmt
2	10.00	0.25	
3	15.00	0.50	

PAR1	PAR2	PAR3	PAR4	PAR5	PAR6	PAR7	PAR8	PAR9	PAR10
UPAR ₁	1	1	1	1	1	1	1	1	1
16*Gr.	1.42	-0.42-25.50	0.21	0.63	13.00	-0.52	0.31	15.00	1.50
IN.CS	2.45	O. 3558	G. E4	-1.22					
1	1	1.42-25.50	0.358	0.63	13.00	-0.52	0.30	14.75	1.50
CL=2.42	CD=0.344	CL/CD=G.15	CM=-1.19	2:57.20					
+--2-	CL=0.37/45.75	0.28	0.63	13.00	0.22	0.31	15.25	1.80	
1	3	1.42-25.75	0.21	0.63	14.75	-0.22	0.31	15.00	1.75
CL=2.44	CD=0.376	CL/CD=G.49	CM=-1.21	2:55.50					
-1	4	1.42-25.50	0.21	0.63	13.00	-0.22	0.31	15.25	1.75
CL=2.45	CD=0.382	CL/CD=G.52	CM=-1.23	2:58.14					
+--3-	CL=0.37/35.50	0.13	0.58	13.00	-0.22	0.31	14.75	1.80	

PAR1	PAR2	PAR3	PAR4	PAR5	PAR6	PAR7	PAR8	PAR9	PAR10
UPAR ₁	1	1	1	1	1	1	1	1	1
16*Gr.	1.42	-0.42-25.00	0.00	0.53	13.50	-0.22	0.31	15.50	1.50
IN.CS	2.59	O. 319	G. 12	-1					
1	1	1.42-25.00	0.00	0.56	0.53	13.75	-0.22	0.31	15.25
CL=1..	CL=..	CL/CD=..	CM=..						
1	4	1.42-25.00	0.00	0.53	13.75	-0.30	0.44	1.50	1.50
CL=1.03	CD=0.193	CL/CD=S.	CM=S.						
1	3	1.42-25.25	0.02	0.58	13.75	-0.30	0.46	1.50	1.25
CL=0.985	CD=0.180	CL/CD=S.	CM=S.						
1	4	1.42-25.75	0.00	0.56	13.75	-0.30	0.44	1.50	1.50
CL=2..	CD=0.323	CL/CD=S.	CM=S.						
1	3	1.42-25.25	0.02	0.58	13.75	-0.30	0.46	1.50	1.25
CL=0.985	CD=0.180	CL/CD=S.	CM=S.						
1	4	1.42-25.75	0.00	0.56	13.75	-0.30	0.44	1.50	1.50
CL=2..	CD=0.323	CL/CD=S.	CM=S.						
1	5	1.42-25.25	0.00	0.48	13.75	-0.30	0.36	1.50	1.75
CL=1.24	CD=0.285	CL/CD=S.	CM=S.						
1	6	1.42-25.75	0.00	0.53	13.75	-0.30	0.44	1.50	1.50
CL=0.985	CD=0.180	CL/CD=S.	CM=S.						
1	7	1.42-25.50	0.00	0.53	13.75	-0.30	0.44	1.50	1.50
CL=0.786	CD=0.0815	CL/CD=S.	CM=S.						
2	8	1.42-25.25	0.00	0.53	13.75	-0.30	0.44	1.50	1.50
CL=2..	CD=0.41	CL/CD=S.	CM=S.						
2	9	1.42-25.50	0.00	0.53	13.75	-0.30	0.44	1.50	1.50
CL=0.632	CD=0.103	CL/CD=S.	CM=S.						
2	10	1.42-25.25	0.00	0.53	13.75	-0.30	0.44	1.50	1.50
CL=2..	CD=0.387	CL/CD=S.	CM=S.						
2	11	1.42-25.00	0.00	0.53	13.75	-0.30	0.44	1.50	1.50
CL=0.462	CD=0.0435	CL/CD=S.	CM=S.						
2	12	1.42-25.50	0.00	0.53	13.75	-0.30	0.44	1.50	1.50
CL=1.07	CD=0.251	CL/CD=S.	CM=S.						
2	13	1.42-25.25	0.00	0.53	13.75	-0.30	0.44	1.50	1.50
CL=0.559	CD=0.104	CL/CD=S.	CM=S.						
2	14	1.42-25.50	0.00	0.53	13.75	-0.30	0.44	1.50	1.50
CL=2.25	CD=0.349	CL/CD=S.	CM=S.						
2	15	1.42-25.25	0.00	0.53	13.75	-0.30	0.44	1.50	1.50
CL=2..	CD=0.328	CL/CD=S.	CM=S.						
2	16	1.42-25.00	0.00	0.53	13.75	-0.30	0.44	1.50	1.50
CL=0.130	CD=0.320	CL/CD=S.	CM=S.						
3	17	1.42-25.75	0.00	0.53	13.75	-0.30	0.44	1.50	1.50
CL=2.19	CD=0.555	CL/CD=S.	CM=S.						
3	18	1.42-25.50	0.00	0.53	13.75	-0.30	0.44	1.50	1.50

GEOMETRY MODIFICATION 7

11= 12345678947 12= 987654321 NMC= 3 NCASE= 6

INCR NUM 1 STEP DEGRAD

1 2.50 0.13
2 5.00 0.25
3 7.50 0.38

PAK1 PAK2 PAK3 PAK4 PAK5 PAK6 PAK7 PAK8 PAK9 PAK10

OPAK 1 1 1 1 1 1 1 1 1 1 1

16.CS 1.00 -0.42-24.75 -0.02 0.53 13.50 -0.14 0.26 15.05 1.25

2.5S C.273 9.45 -1.27

1 1 1.46 -0.44-24.05 -0.02 0.52 13.50 -0.20 0.64 15.13 +-----

CL= 1.09 CL= 0.215 CL/CD= 5.00 CR= -C. SEC 3.01.29 1.46

1 2 1.50 -0.44-24.75 -0.02 0.55 13.50 -0.10 0.23 15.06 1.30

CL= 2.5S CL= 0.285 CL/CD= 9.09 CR= -1.27 2:56.28

1 3 1.50 -0.42-24.75 0.05 0.53 13.50 -0.14 0.23 15.06 1.25

CL= 2.5S CL= 0.281 CL/CD= 9.22 CR= -1.27 3:0.21

1 4 1.46 -0.42-24.75 -0.02 0.52 13.50 -0.16 0.26 15.06 1.13

CL= 2.5S CL= 0.268 CL/CD= 9.63 CR= -1.27 2:54.84

1 5 1.54 -0.44-24.75 -0.02 0.55 13.50 -0.10 0.26 15.05 1.00

CL= 0.202 CL= 0.148 CL/CD= 6.09 CR= -C.2.61 3:02.19

1 6 1.54 -0.42-24.75 -0.02 0.52 13.50 -0.14 0.26 15.05 1.13

CL= 2.5S CL= 0.288 CL/CD= 8.99 CR= -1.26 2:55.25

2 1 1.42 -0.47-24.75 -0.05 0.56 13.50 -0.14 0.21 15.00 1.00

CL= 2.5S CL= 0.310 CL/CD= 8.16 CR= -1.25 2:55.68

2 2 1.54 -0.42-24.75 -0.02 0.54 13.50 -0.06 0.15 15.00 1.00

CL= 2.5S CL= 0.279 CL/CD= 9.16 CR= -1.26 2:03.47

2 3 1.54 -0.42-24.75 -0.10 0.55 13.50 -0.14 0.21 15.05 1.13

CL= 0.719 CL= 0.0446 CL/CD= 1.60 CR= -C.162 3:02.24 1.13

2 10 1.50 -0.37-24.75 -0.02 0.53 13.50 -0.14 0.21 15.05 1.00

CL= 2.65 CL= 0.245 CL/CD= 10.82 CR= -1.25 2:56.28

2 11 1.50 -0.42-24.75 0.05 0.53 13.50 -0.14 0.21 15.05 +-----

CL= 2.51 CL= 0.282 CL/CD= 8.970 CR= -1.24 2:56.25 1.15

2 12 1.50 -0.37-24.75 -0.10 0.53 13.50 -0.06 0.21 15.05 1.00

CL= 1.09 CL= 0.213 CL/CD= 5.12 CR= -0.57.23 2:02.59

3 13 1.39 -0.49-24.75 -0.02 0.60 13.13 -0.25 0.19 15.05 +-----

CL= 0.728 CL= 0.1518 CL/CD= 1.40 CR= -C.226 3:CO.905

3 14 1.50 -0.42-24.35 0.09 0.53 13.13 -0.03 0.20 15.05 1.00

CL= 1.27 CL= 0.191 CL/CD= 6.65 CR= -0.55.5 3:03.04

3 15 1.39 -0.42-24.75 -0.04 0.53 13.50 -0.14 0.20 15.05 1.00

CL= 2.57 CL= 0.283 CL/CD= 9.08 CR= -1.27 2:56.42

3 16 1.39 -0.34-25.13 -0.02 0.53 13.50 -0.19 0.21 15.05 1.05

CL= 0.716 CL= 0.428 CL/CD= 2.00 CR= -0.34.42 3:0.2.04

3 17 1.50 -0.42-24.35 0.09 0.45 13.50 -0.14 0.33 15.05 +-----

CL= 2.61 CL= 0.287 CL/CD= 9.09 CR= -1.24 2:05.29

3 18 1.50 -0.42-24.38 -0.02 0.60 13.13 -0.14 0.33 14.94 1.05

CL= 0.828 CL= 0.0538 CL/CD= 15.29 CR= -O.412 3:04.97

GEOMETRY MODIFICATION 8

11= 12345689320 12= 487650883 NMC= 3 NCASE= 6

INCR NUM 1 STEP DEGRAD

1 2.50 0.13
2 5.00 0.25
3 7.50 0.38

PAK1 PAK2 PAK3 PAK4 PAK5 PAK6 PAK7 PAK8 PAK9 PAK10

OPAK 1 1 1 1 1 1 1 1 1 1

16.CS 1.50 -0.37-24.75 -0.02 0.48 13.75 -0.14 0.21 15.25

2.65 0.245 10.82 -1.28

1 1 CL= 0.967 CL= 1.03 CL/CD= 0.939 CR= -0.415 1.25

1 2 CL= 1.54 -0.37-24.75 0.02 0.45 13.75 -0.14 0.16 15.36

CL= 1.43 CL= 0.273 CL/CD= 5.24 CR= -0.925

1 3 CL= 1.56 -0.40-24.03 -0.02 0.50 13.75 -0.14 0.18 15.38 +-----

CL= 1.82 CL= C.465 CL/CD= 2.94 CR= -1.56

1 4 CL= 1.56 -0.34-24.75 -0.02 0.45 13.75 -0.14 0.21 15.25

CL= 1.17 CL= 0.691 CL/CD= 1.67 CR= -0.650

1 5 CL= 1.62 -0.40-24.08 -0.02 0.50 13.86 -0.18 0.18 15.12

CL= 2.61 CL= 0.213 CL/CD= 12.44 CR= -1.29

1 6 CL= 1.54 -0.37-25.00 -0.02 0.48 13.75 -0.14 0.21 15.25

CL= 0.722 CL= 0.0149 CL/CD= 4.85 CR= -0.145

2 1 CL= 1.60 -0.37-24.50 -0.10 0.48 13.75 -0.16 0.16 15.00

CL= 2.64 CL= 0.213 CL/CD= 12.44 CR= -1.29

2 2 CL= 1.62 -0.37-25.00 -0.02 0.48 13.75 -0.06 0.26 15.25 +-----

CL= 2.63 CL= 0.247 CL/CD= 9.47 CR= -1.25

2 3 CL= 1.66 -0.37-24.75 -0.02 0.48 13.75 -0.14 0.18 15.13

CL= 1.07 CL= 0.649 CL/CD= 1.67 CR= -0.404

2 4 CL= 1.60 -0.37-24.75 -0.02 0.48 13.75 -0.22 0.21 15.25

CL= 1.34 CL= 0.517 CL/CD= 2.58 CR= -0.853

2 5 CL= 1.60 -0.32-25.00 -0.02 0.53 13.75 -0.06 0.21 15.25

CL= 2.61 CL= 0.246 CL/CD= 10.6 CR= -1.26

2 6 CL= 1.66 -0.37-24.75 -0.02 0.48 13.75 -0.14 0.21 15.25

CL= 0.32 CL= 0.247 CL/CD= 9.47 CR= -1.25

2 7 CL= 1.66 -0.37-24.75 -0.02 0.48 13.75 -0.22 0.21 15.25

CL= 1.07 CL= 0.649 CL/CD= 1.67 CR= -0.404

2 8 CL= 1.60 -0.37-24.75 -0.02 0.48 13.75 -0.14 0.18 15.13

CL= 1.34 CL= 0.517 CL/CD= 2.58 CR= -0.853

2 9 CL= 1.66 -0.37-24.75 -0.02 0.48 13.75 -0.22 0.21 15.25

CL= 1.07 CL= 0.649 CL/CD= 1.67 CR= -0.404

2 10 CL= 1.60 -0.37-24.75 -0.02 0.48 13.75 -0.14 0.21 15.25

CL= 1.34 CL= 0.517 CL/CD= 2.58 CR= -0.853

2 11 CL= 1.66 -0.37-24.75 -0.02 0.48 13.75 -0.22 0.21 15.25

CL= 1.07 CL= 0.649 CL/CD= 1.67 CR= -0.404

2 12 CL= 1.60 -0.37-24.75 -0.02 0.48 13.75 -0.14 0.21 15.25

CL= 1.34 CL= 0.517 CL/CD= 2.58 CR= -0.853

2 13 CL= 1.66 -0.37-24.75 -0.02 0.48 13.75 -0.22 0.21 15.25

CL= 1.34 CL= 0.517 CL/CD= 2.58 CR= -0.853

2 14 CL= 1.60 -0.37-24.75 -0.02 0.48 13.75 -0.14 0.21 15.25

CL= 1.34 CL= 0.517 CL/CD= 2.58 CR= -0.853

2 15 CL= 1.66 -0.37-24.75 -0.02 0.48 13.75 -0.22 0.21 15.25

CL= 1.07 CL= 0.649 CL/CD= 1.67 CR= -0.404

2 16 CL= 1.60 -0.37-24.75 -0.02 0.48 13.75 -0.14 0.21 15.25

CL= 1.34 CL= 0.517 CL/CD= 2.58 CR= -0.853

2 17 CL= 1.60 -0.37-24.75 -0.02 0.48 13.75 -0.14 0.21 15.25

CL= 1.34 CL= 0.517 CL/CD= 2.58 CR= -0.853

2 18 CL= 1.66 -0.37-24.75 -0.02 0.48 13.75 -0.22 0.21 15.25

CL= 1.17 CL= 0.220 CL/CD= 5.32 CR= -0.488

GEPEIRI MUDIFICATIU. 19
11= 1234565673 12= 96/0020099 NINE= 3 NCASE= 6

Line	123456789012	98765432109876543210
1	11111111111111111111	98765432109876543210
2	11111111111111111111	98765432109876543210
3	11111111111111111111	98765432109876543210

- A4.5 -

3.11	$\text{Cl}_f = 2 \cdot \text{Cl}_0 = 2 \cdot 6.2 = 12.4$	$\text{Cl}_f/\text{CD} = 12.4 / 0.203 = 60.3$	$\text{CM} = -1.2$	0.70
3.14	$\text{Cl}_f = 1.94 \cdot 0.44 = 0.86$	$\text{Cl}_f/\text{CD} = 0.86 / 0.41 = 2.1$	$\text{CM} = -0.03$	1.38

GRUENSTEIN WINTER 1964 23

```

GUTENBERG BUDGET CANTON 14
11 = 1234567832 12 = 987631921 11INC= 3 11LASTE= 0
INC# RUV % STEP DRAFT
1 1.40 0.075
2 2.00 0.125
3 4.20 0.225

```

- A4.7 -

GEOMETRY MODIFICATION 15

II = 1234574671 22= 987656841 NINC= 3 NCASE= 6

INCH HUX 3 STEP DECKE
1 0.70 0.00
2 1.40 0.00
3 2.10 0.120

PAK1 PAK2 PAK3 PAK4 PAK5 PAK6 PAK7 PAK8 PAK9 PAK10

UPAK 1 1 1 1 1 1 1 1 1 1
1n.CU. 1.65 -0.44-24.28 -0.15 0.20 13.40 -0.05 0.00 15.30 0.50
1n.CU 2 74 O 147 18.3 9

1 1 1.65 -0.41-24.3 76.05 0.20 13.90 -0.05 0.01 15.30 0.60
CL=2 74 CU=C 1.42 CL/CU=18.65 CR=-1.33

1 2 1.65 -0.44-24.4 -0.05 0.25 13.54 -0.05 0.01 15.30 0.52
CL=2 75 O 147 CU=6.7 CL/CU=18.65 CR=-1.332

1 3 1.65 -0.45-24.32 -0.04 0.27 13.94 -0.04 0.00 15.30 0.52
CL=2 76 O 147 CU=6.7 CL/CU=18.65 CR=-1.332

1 4 1.65 -0.43-24.32 -0.05 0.25 13.90 -0.04 0.01 15.34 0.50
CL=2 74 CU=C 0.142 CL/CU=18.65 CR=-1.322

1 5 1.65 -0.45-24.28 -0.06 0.26 13.94 -0.06 0.01 15.34 0.50
CL=2 75 O 147 CU=C 0.142 CL/CU=18.65 CR=-1.322

1 6 1.65 -0.45-24.28 -0.04 0.25 13.90 -0.06 0.00 15.30 0.50
CL=2 74 O 147 CU=C 0.142 CL/CU=18.65 CR=-1.322

1 7 1.65 -0.44-24.20 -0.03 0.26 13.90 -0.05 -0.01 15.22 0.50
CL=2 75 O 147 CU=C 0.142 CL/CU=18.65 CR=-1.322

1 8 1.65 -0.44-24.28 -0.05 0.25 13.90 -0.05 0.00 15.22 0.48
CL=2 76 O 147 CU=C 0.142 CL/CU=18.65 CR=-1.322

1 9 1.65 -0.43-24.36 -0.05 0.25 13.90 -0.05 0.01 15.20 0.48
CL=2 77 O 147 CU=C 0.142 CL/CU=18.65 CR=-1.322

1 10 1.65 -0.44-24.36 -0.05 0.25 13.90 -0.05 0.01 15.20 0.48
CL=2 78 O 147 CU=C 0.142 CL/CU=18.65 CR=-1.322

1 11 1.65 -0.44-24.36 -0.05 0.25 13.90 -0.07 -0.01 15.22 0.48
CL=2 79 O 147 CU=C 0.142 CL/CU=18.65 CR=-1.322

1 12 1.65 -0.44-24.36 -0.05 0.25 13.90 -0.07 0.00 15.22 0.48
CL=2 80 O 147 CU=C 0.142 CL/CU=18.65 CR=-1.322

1 13 1.65 -0.44-24.36 -0.05 0.25 13.90 -0.07 0.00 15.22 0.48
CL=2 81 O 147 CU=C 0.142 CL/CU=18.65 CR=-1.322

1 14 1.65 -0.44-24.36 -0.05 0.25 13.90 -0.07 0.00 15.18 0.48
CL=2 82 O 147 CU=C 0.142 CL/CU=18.65 CR=-1.322

1 15 1.65 -0.44-24.36 -0.05 0.25 13.90 -0.07 0.00 15.18 0.48
CL=2 83 O 147 CU=C 0.142 CL/CU=18.65 CR=-1.322

1 16 1.65 -0.42-24.40 -0.08 0.25 13.78 -0.02 0.00 15.18 0.56
CL=2 70 S CU=0.142 CL/CU=18.65 CR=-1.319

1 17 1.65 -0.44-24.28 -0.05 0.26 13.78 -0.05 0.00 15.18 0.68
CL=2 73 S CU=0.141 CL/CU=19.42 CR=-1.328

1 18 1.62 -0.42-24.40 -0.02 0.28 13.90 -0.02 0.00 15.18 0.58
CL=2 74 S CU=0.140 CL/CU=19.42 CR=-1.328

GEOMETRY MODIFICATION 16

II = 1234574671 22= 987656841 NINC= 3 NCASE= 6

INCH HUX 4 STEP DECKE
1 0.70 0.00
2 1.40 0.00
3 2.10 0.120

PAK1 PAK2 PAK3 PAK4 PAK5 PAK6 PAK7 PAK8 PAK9 PAK10

UPAK 1 1 1 1 1 1 1 1 1 1
1n.CU. 1.67 -0.44-24.28 -0.05 0.20 13.90 -0.07 0.00 15.22 0.48

INCH HUX 4 STEP DECKE
1 0.70 0.00
2 1.40 0.00
3 2.10 0.120

PAK1 PAK2 PAK3 PAK4 PAK5 PAK6 PAK7 PAK8 PAK9 PAK10

UPAK 1 1 1 1 1 1 1 1 1 1
1n.CU. 1.67 -0.44-24.28 -0.05 0.20 13.90 -0.07 0.00 15.22 0.48

INCH HUX 4 STEP DECKE
1 0.70 0.00
2 1.40 0.00
3 2.10 0.120

PAK1 PAK2 PAK3 PAK4 PAK5 PAK6 PAK7 PAK8 PAK9 PAK10

UPAK 1 1 1 1 1 1 1 1 1 1
1n.CU. 1.67 -0.44-24.28 -0.05 0.20 13.90 -0.07 0.00 15.22 0.48

INCH HUX 4 STEP DECKE
1 0.70 0.00
2 1.40 0.00
3 2.10 0.120

PAK1 PAK2 PAK3 PAK4 PAK5 PAK6 PAK7 PAK8 PAK9 PAK10

UPAK 1 1 1 1 1 1 1 1 1 1
1n.CU. 1.67 -0.44-24.28 -0.05 0.20 13.90 -0.07 0.00 15.22 0.48

INCH HUX 4 STEP DECKE
1 0.70 0.00
2 1.40 0.00
3 2.10 0.120

PAK1 PAK2 PAK3 PAK4 PAK5 PAK6 PAK7 PAK8 PAK9 PAK10

UPAK 1 1 1 1 1 1 1 1 1 1
1n.CU. 1.67 -0.44-24.28 -0.05 0.20 13.90 -0.07 0.00 15.22 0.48

INCH HUX 4 STEP DECKE
1 0.70 0.00
2 1.40 0.00
3 2.10 0.120

PAK1 PAK2 PAK3 PAK4 PAK5 PAK6 PAK7 PAK8 PAK9 PAK10

UPAK 1 1 1 1 1 1 1 1 1 1
1n.CU. 1.67 -0.44-24.28 -0.05 0.20 13.90 -0.07 0.00 15.22 0.48

INCH HUX 4 STEP DECKE
1 0.70 0.00
2 1.40 0.00
3 2.10 0.120

PAK1 PAK2 PAK3 PAK4 PAK5 PAK6 PAK7 PAK8 PAK9 PAK10

UPAK 1 1 1 1 1 1 1 1 1 1
1n.CU. 1.67 -0.44-24.28 -0.05 0.20 13.90 -0.07 0.00 15.22 0.48

INCH HUX 4 STEP DECKE
1 0.70 0.00
2 1.40 0.00
3 2.10 0.120

PAK1 PAK2 PAK3 PAK4 PAK5 PAK6 PAK7 PAK8 PAK9 PAK10

UPAK 1 1 1 1 1 1 1 1 1 1
1n.CU. 1.67 -0.44-24.28 -0.05 0.20 13.90 -0.07 0.00 15.22 0.48

INCH HUX 4 STEP DECKE
1 0.70 0.00
2 1.40 0.00
3 2.10 0.120

جغرافیا ایران و خارج از کشور ۲۳

123456789/40 = 30862500/5 = 6172500 = 5 1.625E-6

GLENETHY RULIFICATION 26

```
IN CASE = 3  
IN CASE = 3
```

LiClO ₄ / M	% STP	D ₂ / g cm ⁻³
1	1.25	0.090
2	2.00	1.090
3	3.75	2.090

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STRUCTURE IDENTIFICATION 30

		P _{AH}	P _{AH2}	P _{AH3}	P _{AH4}	P _{AH5}	P _{AH6}	P _{AH7}	P _{AH8}	P _{AH9}	P _{AH10}
1	1	1.53	-0.37-22.52	-0.10	0.27	1	1	1	1	1	0.48
1	1	CL=1.53	CL=0.37-22.52	CL=0.10	CL=0.27	CL=1	CL=1	CL=1	CL=1	CL=1	0.48
1	2	2.37	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.48
1	1	CL=1.53	CL=0.37-22.52	CL=0.10	CL=0.27	CL=1	CL=1	CL=1	CL=1	CL=1	0.48
1	2	1.52	-0.30-23.52	-0.10	0.27	7.76	-0.18	0.01	16.56	16.56	0.48
1	1	CL=1.52	CL=0.30-23.52	CL=0.10	CL=0.27	CL=7.76	CL=-0.18	CL=0.01	CL=16.56	CL=16.56	0.48
1	3	1.54	-0.37-22.52	-0.10	0.27	9.6	-0.19	0.01	16.56	16.56	0.48
1	1	CL=1.54	CL=0.37-22.52	CL=0.10	CL=0.27	CL=9.6	CL=-0.19	CL=0.01	CL=16.56	CL=16.56	0.48
1	4	1.53	-0.36-22.52	-0.10	0.27	1.36	-0.19	0.01	15.36	15.36	0.48
1	1	CL=1.53	CL=0.36-22.52	CL=0.10	CL=0.27	CL=1.36	CL=-0.19	CL=0.01	CL=15.36	CL=15.36	0.48
1	5	1.54	-0.38-22.32	-0.11	0.26	0.36	-0.18	0.01	15.36	15.36	0.48
1	1	CL=1.54	CL=0.38-22.32	CL=0.11	CL=0.26	CL=0.36	CL=-0.18	CL=0.01	CL=15.36	CL=15.36	0.48
1	6	1.53	-0.37-22.52	-0.11	0.27	0.90	-0.18	0.00	15.90	15.90	0.48
1	1	CL=1.53	CL=0.37-22.52	CL=0.11	CL=0.27	CL=0.90	CL=-0.18	CL=0.00	CL=15.90	CL=15.90	0.48
2	7	1.53	-0.35-24.12	-0.13	0.27	8.36	-0.15	0.01	15.96	15.96	0.48
2	1	CL=2.36	CL=0.35-24.12	CL=0.13	CL=0.27	CL=8.36	CL=-0.15	CL=0.01	CL=15.96	CL=15.96	0.48
2	8	1.53	-0.37-22.92	-0.07	0.25	7.16	-0.21	-0.01	15.96	15.96	0.48
2	1	CL=1.53	CL=0.37-22.92	CL=0.07	CL=0.25	CL=7.16	CL=-0.21	CL=-0.01	CL=15.96	CL=15.96	0.48
2	9	1.50	-0.32-22.92	-0.10	0.27	16.62	-0.21	0.03	15.95	15.95	0.48
2	1	CL=2.93	CL=0.32-22.92	CL=0.10	CL=0.27	CL=16.62	CL=-0.21	CL=0.03	CL=15.95	CL=15.95	0.48
2	10	1.53	-0.34-22.52	-0.10	0.27	6.95	-0.16	0.01	15.95	15.95	0.48
2	1	CL=1.53	CL=0.34-22.52	CL=0.10	CL=0.27	CL=6.95	CL=-0.16	CL=0.01	CL=15.95	CL=15.95	0.48
2	11	1.53	-0.35-22.47	-0.10	0.27	0.30	-0.15	0.01	14.16	14.16	0.48
2	1	CL=1.53	CL=0.35-22.47	CL=0.10	CL=0.27	CL=0.30	CL=-0.15	CL=0.01	CL=14.16	CL=14.16	0.48
3	12	1.57	-0.37-21.12	-0.10	0.27	6.2	-0.13	0.04	14.16	14.16	0.48
3	1	CL=1.57	CL=0.37-21.12	CL=0.10	CL=0.27	CL=6.2	CL=-0.13	CL=0.04	CL=14.16	CL=14.16	0.48
3	13	1.49	-0.40-22.52	-0.10	0.27	12.66	-0.13	0.04	17.76	17.76	0.48
3	1	CL=1.49	CL=0.40-22.52	CL=0.10	CL=0.27	CL=12.66	CL=-0.13	CL=0.04	CL=17.76	CL=17.76	0.48
3	14	1.57	-0.37-22.92	-0.10	0.27	8.5	-0.14	0.01	15.96	15.96	0.48
3	1	CL=1.57	CL=0.37-22.92	CL=0.10	CL=0.27	CL=8.5	CL=-0.14	CL=0.01	CL=15.96	CL=15.96	0.48
3	15	1.57	-0.37-22.47	-0.10	0.27	0.36	-0.14	0.01	14.16	14.16	0.48
3	1	CL=1.57	CL=0.37-22.47	CL=0.10	CL=0.27	CL=0.36	CL=-0.14	CL=0.01	CL=14.16	CL=14.16	0.48
3	16	1.57	-0.37-22.92	-0.10	0.27	8.5	-0.14	0.04	15.96	15.96	0.48
3	1	CL=1.57	CL=0.37-22.92	CL=0.10	CL=0.27	CL=8.5	CL=-0.14	CL=0.04	CL=15.96	CL=15.96	0.48
3	17	1.57	-0.37-22.47	-0.10	0.27	3.19	-0.14	0.01	15.96	15.96	0.48
3	1	CL=1.57	CL=0.37-22.47	CL=0.10	CL=0.27	CL=3.19	CL=-0.14	CL=0.01	CL=15.96	CL=15.96	0.48

GRUMETRY MULTIPLICATON 33
 11= 1234590425 12= 587646655 11nC= 3 nCASE= 6
 1nCR nM= 8 DIRP
 1nCR nM= 8 DIRP
 1 0.25
 2 0.50
 3 1.00
 1.50

GRUMETRY MULTIPLICATION 34

	11= 1234591658 12= 987669081 nMC= 3 nCASE= 6	11= 1234591658 12= 987669081 nMC= 3 nCASE= 6
1nCR nM= 8 DIRP 1 1 2 1 3 1	PAR1 PAR2 PAR3 PAR4 PAR5 PAR6 PAR7 PAR8 PAR9 PAR10 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.50 1n.CE- CL= 2 422 C CL= 0.6271 65.5 -0.18 -0.18 1 1 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 354 CL= 0.626 CL/CD= 1.425 CM= -1.167 1 2 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 354 CL= 0.626 CL/CD= 1.425 CM= -1.167 1 3 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 354 CL= 0.626 CL/CD= 1.425 CM= -1.167 1 4 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 439 CL= 0.6351 CL/CD= 1.425 CM= -1.167 1 5 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 427 CL= 0.6421 CL/CD= 1.425 CM= -1.167 1 6 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 605 CL= 0.6692 CL/CD= 1.425 CM= -1.167 1 7 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 605 CL= 0.6692 CL/CD= 1.425 CM= -1.167 1 8 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 605 CL= 0.6692 CL/CD= 1.425 CM= -1.167 1 9 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 605 CL= 0.6692 CL/CD= 1.425 CM= -1.167 1 10 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 415 CL= 0.735 CL/CD= 1.425 CM= -1.167 1 11 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 415 CL= 0.735 CL/CD= 1.425 CM= -1.167 1 12 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 415 CL= 0.735 CL/CD= 1.425 CM= -1.167 1 13 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 415 CL= 0.735 CL/CD= 1.425 CM= -1.167 1 14 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 415 CL= 0.735 CL/CD= 1.425 CM= -1.167 1 15 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 415 CL= 0.735 CL/CD= 1.425 CM= -1.167 1 16 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 415 CL= 0.735 CL/CD= 1.425 CM= -1.167 1 17 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 415 CL= 0.735 CL/CD= 1.425 CM= -1.167 1 18 1.55 -0.38-21.32 -0.10 0.41 0.27 0.80 0.00 15.36 0.00 CL= 2 210 CL= 0.6120 CL/CD= 1.425 CM= -1.167	PAR1 PAR2 PAR3 PAR4 PAR5 PAR6 PAR7 PAR8 PAR9 PAR10 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 1n.CE- CL= 2 439 CL= 0.6351 CL/CD= 1.425 CM= -1.167 1 1 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 439 CL= 0.6351 CL/CD= 1.425 CM= -1.167 1 2 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 439 CL= 0.6351 CL/CD= 1.425 CM= -1.167 1 3 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 439 CL= 0.6351 CL/CD= 1.425 CM= -1.167 1 4 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 439 CL= 0.6351 CL/CD= 1.425 CM= -1.167 1 5 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 439 CL= 0.6351 CL/CD= 1.425 CM= -1.167 1 6 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 439 CL= 0.6351 CL/CD= 1.425 CM= -1.167 1 7 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 439 CL= 0.6351 CL/CD= 1.425 CM= -1.167 1 8 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 439 CL= 0.6351 CL/CD= 1.425 CM= -1.167 1 9 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 439 CL= 0.6351 CL/CD= 1.425 CM= -1.167 1 10 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 439 CL= 0.6351 CL/CD= 1.425 CM= -1.167 1 11 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 439 CL= 0.6351 CL/CD= 1.425 CM= -1.167 1 12 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 439 CL= 0.6351 CL/CD= 1.425 CM= -1.167 1 13 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 439 CL= 0.6351 CL/CD= 1.425 CM= -1.167 1 14 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 439 CL= 0.6351 CL/CD= 1.425 CM= -1.167 1 15 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 439 CL= 0.6351 CL/CD= 1.425 CM= -1.167 1 16 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 439 CL= 0.6351 CL/CD= 1.425 CM= -1.167 1 17 1.55 -0.37-21.32 -0.11 0.41 0.30 -0.18 0.00 15.36 0.00 CL= 2 439 CL= 0.6351 CL/CD= 1.425 CM= -1.167 1 18 1.55 -0.38-21.32 -0.10 0.41 0.27 0.80 0.00 15.36 0.00

APPENDIX (iv-b) INITIAL AND FINAL CONFIGURATION POLAR DATA

ANGLE OF ATTACK Degrees	INITIAL GEOMETRY		FINAL GEOMETRY	
	C_L	C_L/C_d	C_L	C_L/C_d
0.0	2.26	4.25	2.52	47.0
0.5	2.33	4.26	2.60	36.3
1.0	2.39	4.25	2.67	29.2
1.5	2.45	4.22	-	-
2.0	2.52	4.20	2.83	20.4
3.0	2.64	4.10	2.90	15.5
4.0	2.77	3.99	3.14	12.2
5.0	-	-	-	-
6.0	3.03	3.70	-	-
7.0	3.11	3.57	-	-
8.0	-	-	3.76	5.97
9.0	3.41	3.25	3.90	5.27
10.0	3.48	3.11	4.05	4.84
12.0	3.77	2.73	4.33	3.91
14.0	4.00	2.48	4.60	3.29
16.0	4.22	2.29	4.84	2.82
18.0	4.41	2.06	5.06	2.44
20.0	4.59	1.87	5.25	2.14

APPENDIX (iv-c) $C_1/C_d - C_1$ PLOT FOR ALL CONFIGURATIONS