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AN F-LAYER MODEL OF THE IONOSPHERE FOR NORTH AMERICA

by

C.J. Gladwin

This work was sponsored by the Department of National Defence, Research and Development Branch under Project No. 33G01

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AN F-LAYER MODEL OF THE LONOSPHERE FOR NORTH AMERICA

C.J. Gladwin

(Radar and Communications Technology Branch)

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TABLE OF CONTENTS

ABS	TRACT			•			•	•	•		•	•	•	1
1.	INTRO	DDUCTION					•	•	•		•			1
2.	ALOS	YN MODEL					•	•			•	•	•	5
	2.1	Description of the Data Base		•			•				•	•		5
	2.2	Development of the Model 2.2.1 Organization of the Data Base 2.2.2 Geographic Smoothing and Into 2.2.3 Sunspot Standardization	e .	lat	ion	• •	•		•		•	•		9
	2.3	Implementation of the Model 2.3.1 Real Time Accession of the Da 2.3.2 Correction to the User's Rz 2.3.3 Interpolation to Month and La 2.3.4 Illustration	ata and ocal	Kp Ti	 me	• •	•	•	•	• •	•	•	•	24 24 26
3.	N(h)	MODEL		•			•	• 1			•	•	•	34
	3.1	Description of the Data Base		•			•	•	•		•	•	•	34
	3.2	Development of the Model	e . ing Grou	ALO	UET Ech	TE Noes	H .	•	•	• •	•	•	•	35 37 42
4.	MAIN	TROUGH REFINEMENTS		•			•	•	•		•	•	•	52
	4.1	Description of the Procedure		•			•	•	•		•	•	•	52
	4.2	Illustration		•			•	•	•		•	•		53
5.	ACKNO	OWLEDGEMENT					•	•	•		•	•	•	57
6.	REFE	RENCES					•	•	•	• •	·•	K	•	58
7.	BIBL	IOGRAPHY		Ac	ces	sion	F	or 	•		Ļ]		60
APP	ENDIX	A - Glossary of Files and Tapes		DT DT	IIS IIC Both	GRA TAB ofter	&I	•	•		•			65
		B - List of Notations		Ju	sti	fica	ti	<u></u>	•		-	1		77
		111			str vai	ibut labi Avai	11t	y (/0		••	7-1-1-1		

AN F-LAYER MODEL OF THE IONOSPHERE FOR NORTH AMERICA

bу

C.J. Gladwin

ABSTRACT

Data collected from the Alouette 1 and 2 satellites (ALOSYN and ALOUETTE N(h)) have been organized in order to make predictions of ionospheric characteristics such as foF2, slab thickness, and spread F as functions of longitude, latitude, local time, month, magnetic activity, and sunspot number. Spread F and foF2 are determined statistically from about 2106 Alouette-1 ionograms and slab thickness is estimated using about 105 electron density profiles. The data and the necessary computer programs for analysing these data by the user are on two labelled tapes and are available from the Communications Research Centre. Contour maps of foF2, spread F and slab thickness as a function of geographic latitude and local time can be generated. A special technique is outlined in order that the user may modify his results to include the main trough. The major computer programs used are available on request.

A

1. INTRODUCTION

The Alouette 1 Topside Sounder satellite was launched on September 29, 1962. From that date until end of 1968, a continuing effort of the Defence Research Board Telecommunications Establishment (DRTE, the forerunner of the Communications Research Centre, CRC) was to routinely scale the approximately 1,000,000 ionograms recorded, for several ionospheric characteristics such as the F2 layer penetration frequency, foF2, as well as a subjective spread index in the neighbourhood of that point. The data have been stored on magnetic tapes and have come to be known as ALOUETTE 1 IONOSPHERIC DATA, ALOSYN [1].

Concurrently, 60,000 of these ionograms as well as another 20,000 Alouette 2 ionograms were scaled for "almost-complete" topside electron density profiles (that is within about 3% of the foF2). These data likewise have been stored on magnetic tapes and become known as ALOUETTE 1 (or 2) IONOSPHERIC DATA, N(h) [2].

The intent of this report is to describe a procedure for organizing and reducing these vast quantities of data in order that a user can obtain predictions of various ionospheric characteristics (foF2, spread, slab thickness, and possibly MUF(3000)F2) as functions of longitude, latitude, local time, sunspot number, month, and magnetic activity (as measured by the 3-hourly Kp index). It should be noted that while MUF(3000)F2 was not a scaled parameter, it can be computed from an estimated height of the maximum electron density by means of an empirical formula given by Shimazaki [27] or Schmid et al [26]. In addition to the prediction of various characteristics, the model has the capabilities of computing percentiles for the characteristics. A technique is also presented to enable the user to estimate regions of severe density gradients such as the main trough [17]. It is intended that the model also be used to supplement the work of Muldrew and James [19] in which the ionospheric effect on the Doppler frequency of a Search and Rescue satellite was estimated.

Global ionospheric modelling using vast quantities of data came of age in the early 1960's with the advent of easy accessibility to large computers. The first major one was the C.C.I.R. model which is accessible either through an atlas of ionospheric characteristics [5] or a companion punched card version. On a smaller scale (geographic latitude > 35°N), there exists the Canadian model [23] and that of Petrie [20]. Essentially these models are based on monthly medians of scaled characteristics for each hour of local time; the latter being observed at about 100 ground stations around the globe. The time frame was the five years in the mid 1950's corresponding to the rising part of the sunspot cycle. Using the numerical mapping procedures developed by Jones and Gallet [13], these data were reduced to sets of monthly coefficients for each characteristic, and then these sets were normalized to two sunspot numbers (Rz=0 and Rz=100). The predictions were assumed to vary linearly with sunspot number for Rz in [0, 150] and be independent of it otherwise.

The next extensive modelling exercise was culminated by Llewellyn and Bent [15]. Again they predicted foF2 from a set of bottomside stations (400,000 ionograms), but in addition they used the 60,000 Alouette 1 profiles and 6,000 electron density probe results (1967-68) to construct a "closed form" density profile. The inputs for their model were longitude, latitude, time, season, solar flux, sunspot number, and foF2. Their closed form profile essentially ignored underlying layers and ledges (F1, E, and D) because they were primarily interested in obtaining accurate values for total electron content, TEC, only. Thus their bottomside TEC could be used in conjunction with the present model, in place of the approximation to be outlined later.

For discussion and listings of some other modelling experiences one should see Kohnlein [14]. Another model, which will be applied here, is one of the trough created by Halcrow and Nisbet [10].

The model to be outlined in this report will now be considered. While there are 1,000,000 topside ionograms the vast majority of these is limited to the continents of North and South America; see Figure 1. However, unlike the data base for the bottomside models, there exists virtually continuous latitudinal coverage. Due to the precession of the orbital plane of Alouette 1 and the revolution of the earth about the sun, observations at a given latitude are obtained for two 4 hour local time intervals per month. The local time history of Alouette 1, coincidentally, repeats itself almost exactly every six months. Hence, the local time is essentially the same at a given geographic latitude for a given day of any year. Thus, in making predictions for a given month, at least 3 months of data will be required. On the other hand instead of using monthly medians of characteristics, semimonthly medians will be used because of the nature of the local time cells. A few other minor nuisances, arising essentially from attempting to design an empirical model after the data have been collected, are also noted:

(1) Because the satellite's solar cells degraded, the number of observations for the last 3 years of the recording process was virtually halved (see Table 2). Thus, there will be a "bias" in the model towards the lower sunspot years 1963-66.

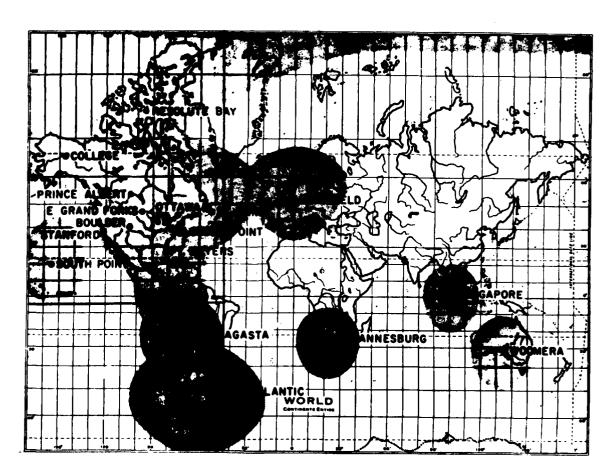


Figure 1. Location and Coverage of Alouette 1 Telemetry Stations. After [3]

- (2) Because of the routine scaling procedures, and possible change in habits of the scalers over the 6 year period, the number of observations (of foF2 or fxf2) which are "unreliable" (i.e. scaled to an uncertainty of more than 0.2 MHz) can range up to 60% in any given month (see Table 2). This problem of routine scaling is not as serious for the N(h) data, however, as these ionograms were scaled on user demand.
- (3) No data are available over the geographic poles (due to the 80° inclination of the orbital plane of Alouette 1).
- (4) The spread index may not be as consistent as that obtained in smaller scale spread experiments [4].
- (5) The maximum sounding frequency of Alouette 1 is 11.5 MHz. Hence, this model cannot give accurate foF2 values if the expected value exceeds about 10 MHz. The model will often give foF2 values greater than 11.5 MHz due to extrapolation to high sunspot numbers.

Only a model for North America, where most of the data were measured, is considered (see Figure 1). The actual domain for the model will be:

- (1) geographic longitude in $[-180^{\circ}, -45^{\circ}]$, that is $[180^{\circ}W, 45^{\circ}W]$,
- (2) geographic latitude in [-10°, 80°], that is [10°S, 80°N], or geomagnetic latitude approximately in [0°, 90°],
- (3) all sunspot numbers, using CCIR assumptions for Rz > 150,
- (4) all local times, months and Kp.

Then for a given month and year, there will be 3 equidistant longitude zones and 18 equidistant geomagnetic latitude zones, as well as 4 zones of local time and Kp, each. Initially the year is kept separate because of the varying sunspot number.

An interesting comparison of results is provided by Petrie and Lockwood [21] where they used geographic longitude zones of 30 degrees, geographic latitude zones of 2 degrees, and local time zones of 1 hour for ALOSYN data from 1963.

The computer used in this study is a Honeywell Sigma 9 operating under Control Program - Five (CP-V). The data analysis programs and user programs, available on request, are written in Fortran IV and hence should be adaptable to most computers.

In chapter 2, a description of the ALOSYN data base is given and the implementation of the prediction model, for foF2 and spread, is considered. A similar discussion is taken up in chapter 3 for the ALOUETTE N(h) data base in order to compute quantities such as TEC and slab thickness. Chapter 4 is concerned with integrating the trough model [10] with the model described here. The notations used are summarized in Appendix B. A glossary of files and tapes is given in Appendix A relating the various programs to their respective sections in the report. A brief description of the files referred

to in the text is also given in Appendix A. A source listing of the files is also available on request.

2. ALOSYN MODEL

2.1 DESCRIPTION OF THE DATA BASE

The entire collection of 1,000,000 ionograms is stored on 8 9T (9 track) tapes in year-universal time order. They have been blocked into 3200 byte records. Each record contains at most 40 ionograms with 80 bytes of information. A new record is started with each day change. There is an 80 byte header, or title, to be skipped at the beginning of each tape. A header has also been placed at the beginning of some months. A complete description of all the data in a record may be found in Nelms et al. [3] or at the beginning of any of the monthly or semi-monthly ALOSYN booklets [1] that have been published. Here only a list of the data actually used in the model is presented:

Year	Y
Month	M
Day	D
Universal time (hour, minute, second)	Ut
Geographic local time (hour, minute)	Lt
Geographic longitude (degrees)	Long
Geographic latitude (degrees)	Lattg
Geomagnetic latitude (degrees)	Lattm
Height of the satellite (kilometres)	h _s
Solar angle at the satellite (degrees)	Χs
Gyrofrequency at the satellite (MHz)	f _H (h _s)
Penetration frequency of the O wave (MHz)	foF2
Accuracy of scaling the O wave	a(o)
Spread of the O wave	s(o)
Penetration frequency of the X wave (MHz)	fxF2
Accuracy of scaling the X wave	a(x)
Spread of the X wave	s(x)
Planetary magnetic activity index	Кp

In addition, one should consult Table 3 which displays the smoothed monthly Zurich sunspot numbers which have been used. Most of the above items are self-explanatory; also see the accuracy and spread definitions which may be found in Tables 1(a) and 1(b) respectively.

TABLE 1(a)
Accuracy Convention of ALOSYN foF2

a (o)	Definition
1 2	foF2 within .05 MHz of tabulated value foF2 within .1 MHz of tabulated value
3	foF2 within .2 MHz of tabulated value
4	foF2 less than tabulated value
5	foF2 greater than tabulated value
-0	foF2 not observed

TABLE 1(b)
Spread Convention of ALOSYN

Definition	Index
No spread	1
Slightly spread	2
Moderately spread	3
Extremely spread	4
	No spread Slightly spread Moderately spread

In Table 1(a) there is some doubt about the interpretation of a=4 or 5, due to changes in scaling habits over the years. In the early years these appear to have meant an uncertainty greater than 0.2 MHz and a -0 was used for "unobservable" critical frequencies. However, the correspondence given in the table, a in [1,5], is adopted for all years. Using this table, foF2 is defined for each ionogram, as follows (see Appendix B).

$$foF2 = \begin{cases} \left[fxF2(fxF2-f_{H}(hmax))\right]^{\frac{1}{2}}, & \text{for } a(x) \text{ in } [1,3] \\ foF2, & \text{for } (a(0),a(x)) \text{ in } [1,3] \times [4,5] \end{cases}$$
(2.1)

where $f_H(hmax)$ is found by an inverse cube extrapolation from h_s to hmax = 300 km.

In Table 1(b) the three letters associated with each group were used to record other information (e.g. oblique traces, cusps, etc.), but the index at the right will be sufficient here. In a similar vein, Kp values defined as n-, no, or n+ are taken to be n-.3, n, or n+.3 where n is an integer in [0,9].

TABLE 2
Blocked ALOSYN Records and Percentage of Unreliable Ionograms by Month and Year

YEAR MONTH	1962	1963	1964	1965	1966	1967	1968
JANUARY	_	507	485	458	228	235	136
37111071111		10	28	45	42	29	44
FEBRUARY		495	439	412	301	230	166
}		21	26	52	56	26	42
MARCH	_	503	428	463	198	268	171
· · · · · ·		28	25	48	30	26	41
APRIL	_	562	554	571	302	285	213
7.7.2		19	18	38	18	20	26
MAY	-	621	577	600	334	269	214
·		13	15	18	18	20	34
JUNE		493	418	502	328	285	215
Jone		6	21	21	18	21	34
JULY		592	582	610	261	271	228
002.		10	13	18	12	18	22
AUGUST		615	495	590	180	266	203
NOGUS1		11	26	23	24	19	32
SEPTEMBER	20	465	392	433	230	256	172
JEI TEMBER	16	15	31	24	22	24	31
OCTOBER	613	602	316	561	258	274	164
OCTOBER	34	28	32	28	20	25	38
NOVEMBER	637	599	519	406	190	199	170
MOATLINEK	29	26	49	38	32	37	49
DECEMBER	506	479	419	271	173	143	137
DECEMBER	28	26	62	46	27	50	51

TABLE 3
Zurich (Smoothed) Sunspot Numbers, Rz

YEAR MONTH	1962	1963	1964	1965	1966	1967	1968	1359	1970	1971	1972
JANUARY	41.5	28.9	18.2	12.1	28.8	72.3	100.4	110.5	1.601	7.97	71.3
FEBRUARY	38.9	29.9	16.2	12.1	32.2	75.7	101.3	109.2	104.2	74.1	7.1.7
MARCH	37.9	29.0	13.1	13.1	35.0	78.9	103.8	106.7	105.0	70.5	72.8
APRIL	38.2	28.7	10.6	15.1	37.8	81.1	106.7	104.3	105.6	6.99	73.6
MAY	37.6	28.5	9.4	15.3	41.8	83.9	107.5	3.901	105.5	64.3	72.8
JUNE	36.3	27.6	9.6	16.0	45.4	87.7	106.9	102.7	104.9	63.6	8.69
טטר ץ	34.8	27.2	10.0	16.0	52.2	6.06	106.0	102.3	102.7	63.6	6.99
AUGUST	32.7	26.7	8.6	16.7	58.0	91.2	106.1	103.2	98.6	63.8	63.9
SEPTEMBER	30.6	26.5	9.6	17.8	65.0	91.2	108.6	101.9	94.4	65.8	60.3
OCTOBER	29.2	24.7	9.6	21.1	66.5	91.2	111.6	100.6	91.0	9.99	58.4
NOVEMBER	29.4	21.8	10.9	22.7	69.7	93.7	112.2	101.2	86.2	67.3	56.6
DECEMBER	29.0	19.5	11.4	25.2	71.0	97.8	111.3	101.9	80.4	6.69	53.2

In Table 2, the following statistics are displayed:

- (a) the actual number of (blocked) records with data, by month and year,
- (b) the percentage of "unreliable" ionograms, by month and year, i.e. those for which an foF2 is not definable, using equation (2.1). For example, for May 1965, there are 600 blocked records and 18% of the total number of ionograms are unreliable.

In view of the introductory remarks, the actual number of ionograms in a given month and year is approximately

$$I = 40 R - 20 Dm$$
 (2.2)

where

R = number of blocked records

Dm = number of days in month M

I = actual number of ionograms.

2.2 DEVELOPMENT OF THE MODEL

2.2.1 Organization of the Data Base

A description of how the data were processed is given here and in Figure 2. A description of how the user uses these processed data is given in section 2.3.

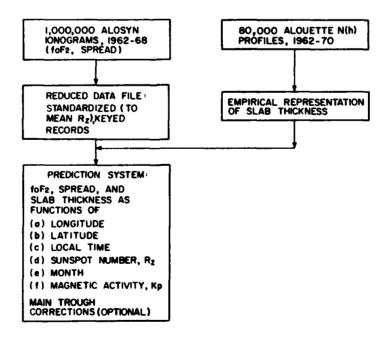


Figure 2. Schematic Overview of Model Development

Instead of processing the 8 tapes sequentially (i.e. year by year), they were processed month by month for all years. While this increases the requisite number of tape usages by (at most) a factor of 76/8 = 9.5, it permits a modular processing procedure for the vast quantities of data (see below). Also, this procedure is more natural in the sense that convenient checks arise on the consistency of the data. Thus, the first step is to set up Nyear files for a given month, ALOMONXX, where Nyear is the number of years of data available for that month, and XX are the last two digits of the respective year represented by ALOMONXX. Each of these files contains R + 1 records (see Table 2), i.e. each file contains either the header for the month or the last record of the previous month, followed by the R records in the month. During this initial processing stage, in addition to completing Table 2, counts of the number of complete or partial records omitted due to "tape problems" are also kept. This is necessary in order to position the tape correctly, for starting the next month. Additional checks are provided by actually printing out the first 4 records as well as the last 3 of each of the files ALOMONXX. The control files AXX and BXX are then executed to continue the next stage of processing (see below).

2.2.2 Geographic Smoothing and Interpolation

In the first stage of this process, executing AXX, the ionograms are sorted into a number of longitudinal and latitudinal zones of essentially constant magnetic activity and local time. The longitude range is divided into 3 equal zones and the geomagnetic latitude range is divided into 18 equal zones (see the model domain given in chapter 1). Each of these 54 geographic areas (see Figure 3) is then subdivided into 4 magnetic activity zones defined by the ranges of Kp:

$$[0,1.3]$$
; $[1.7,3.3]$; $[3.7,5.3]$; $[5.7,9.0]$;

and 4 local time zones (see below for a more complete description). Thus there are 864 cells, although many of these will be empty in the southwest corner (over oceans, see Figure 3, or Table 4). Furthermore the fourth Kp zone (corresponding to severe storms) is fairly scant in terms of data. However, the fine division is used to prevent features such as the main trough from becoming too "smoothed out"; the latter is strongly dependent on local time and Kp [17].

These zones define 864 cells. Associated with each of the 864 cells, a record is kept consisting of the following data array:

$$(n_k, Long_k, Lattm_k, \chi_k, Kp_k, Lt_k, foF2max_k, foF2min_k)$$
 k = 1(1)864,

where n_k is the number of ionograms in the cell and the other numbers are arithmetical averages, minima or maxima of the respective observations in the cell. These data are placed on a scratch file DUMXX which is updated on the next pass through ALOMONXX by BXX. This update consists of appending a frequency distribution consisting of 10 equidistant intervals of [foF2min_k, foF2max_k] for foF2, and also a distribution for the spread (with 4 intervals). The choice of 10 intervals for foF2 was partially motivated by the number of ionograms n_k being tabulated and also by the fact that the range (= foF2max_k - foF2min_k) is roughly 2 MHz, so that the grouping process has an uncertainty

of about the same magnitude as the maximum scaling uncertainty (corresponding to accuracy a = 3).

This updated collection of 864 records is put on a file called MONXX together with the Long, Lattm, Lt, Kp, M, and Y subscripts (see below). This completes the first reduction which has seen an original ALOSYN month reduced by a factor of about 20 in computer storage. In the next section a further reduction by a factor of about 10 (by eliminating empty cells and standardizing to one sunspot number) will be carried out.

A brief description of the construction of the 4 local time zones and their respective indices is now given.

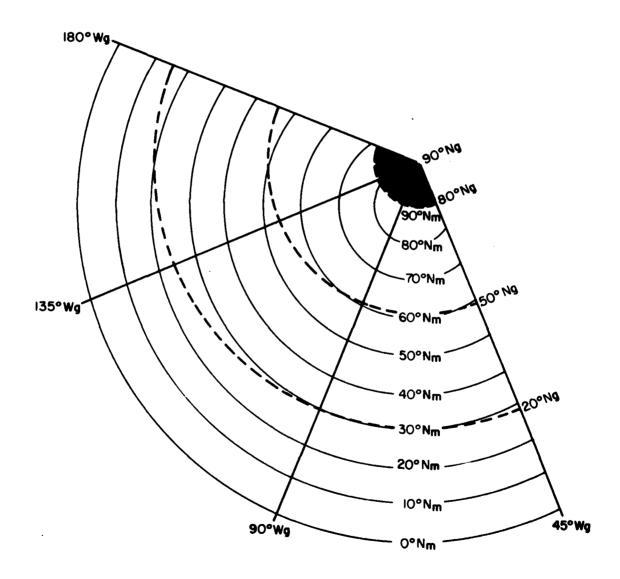


Figure 3. Geographic Zone Alignment of the ALOSYN Model

TABLE 4

Number of Good Ionograms by Longitude and Latitude for February, all Years,

Local Times and Magnetic Activity.

	GE	OGRAPHIC LONGITUDE	(oM)
	[180,135)	[135,90)	[90,45]
[85,90]	-	306	3162
	-	2228	1759
	1045	2328	1399
	1663	1387	1082
[65,70)	1112	1268	1161
2	884	1066	1108
GEOMAGNETIC LATITUDE (ON)	798	829	901
ITUD	693	681	826
₹ (45,50)	243	607	887
ETIC	41	461	791
MAGN	26	351	388
GEO	74	183	316
	68	47	283
[20,25)	50	15	272
	32	13	244
	46	25	227
	47	21	342
[0,5)	10	16	455

In Figure 4, three orbits of the satellite have been plotted (geographic latitude v. geographic local time) for the lst, 16th and 31st of October. For other months, see the caption. The 4 zones are described by a pair of subscripts (LT1,LT2) defined on the product set [1,2] x [1,2], as shown in Figure 4. The first subscript defines the "half-month" that the particular ionogram is in and is determined by comparing the actual hour in the month (Greenwich) of the ionogram to the total number of hours in the month. The second subscript determines whether the ionogram is from a northbound (daytime, in this case) pass or not. This is determined by whether or not the local time of the ionogram is less than the theoretical local time at the maximum geographic latitude of the satellite (approximately 80°N), Ltmax. The latter has been computed assuming a linear variation with year fraction, Yf (where Yf, for example, for January 31 1963, is about 63.085).

Ltmax =
$$16.48 - 47.93(Yf - 62.74) \pm .05$$
 hours, modulo 24. (2.3)

This empirical formula was determined by passing a straight line through the actual (Ltmax, Yf) pairs from 1962 day 272 at 2130 hours and 1966 day 274 at 0120 hours. At these times Alouette 1 was actually near 80°N and the actual values of Ltmax were computed by fitting a parabola to 5 (Lattg, Lt) pairs in the neighbourhood of 80°N.

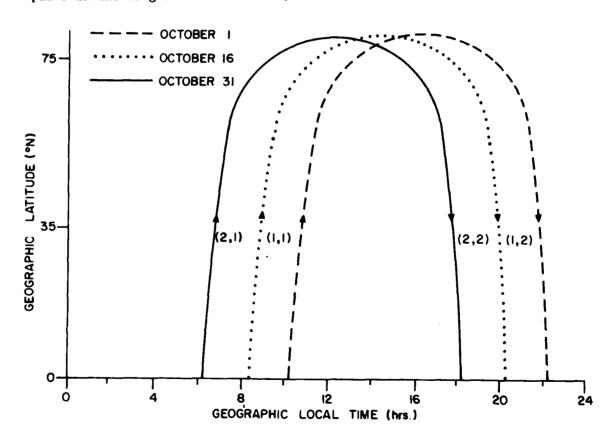


Figure 4. Definition of the Local Time Zones for October; April is the same. For November and May, December and June, January and July, February and August and March and September, Move the Curves 4,8,12,16,20 hours, respectively, to the Left.

Actually, the local time zones are not so symmetrically placed about Ltmax since geomagnetic latitude is used in defining the Lattm zones. Thus the 4 local time zones deviate from the expected 2 hour zone size (especially around the poles), but this was considered a reasonable "trade-off" in view of the well known alignment of foF2 contours with magnetic latitude (e.g. see [17]).

Finally, for calculating the average local time of cell k (to ensure continuity around midnight), the following recursive formula is used:

$$A_{i} = [(i-1) (A_{i-1} + 24r) + (Lt_{i} + 24s)] / i$$
 (2.4a)

where $i = 1(1)n_k$, r and s are integers in [0,1] such that the quantity $|(A_{i-1} + 24r) - (Lt_i + 24s)|$ is a minimum. The average local time for cell k

$$Lt_{k} = A_{n_{k}}$$
 (2.4b)

A cell (or record) of any MONXX shall be referenced according to seven subscripts LO, LA, LT1, LT2, LK, LM, LY) defined on the (extended) product set

$$[1,3] \times [1,18] \times [1,2] \times [1,2] \times [1,4] \times [1,12] \times [2,8]$$

corresponding to the Long, Lattm, Lt (two values), Kp, M, and Y zones, respectively. The Long zones are numbered from west to east, the Lattm zones from north to south, the Lt zones as in Figure 4, the Kp zones with increasing magnetic activity, and the M zones from January to December. The Y zone is simply the second digit of "XX" in MONXX. After the standardization of the MONXX (see below), the year subscript, Y, will be dropped.

A single example of a record of MONXX is now given. A cell was chosen where the range of the foF2 distribution was considerably greater than 2 MHz, in order to illustrate the geographic smoothing involved in the model.

Example 1: Cell 1,5,2,1,3,2,7 ; February 1967.

The contents of the record are shown in Figure 5.

See also Example 2 to follow.

On actually examining the 7 ionograms which comprised the cell it was noticed that the 4 ionograms at the lower end of the foF2 range came from a locale (165°W, 68°N) at 1730 hours, while the upper 3 came a day later and an hour earlier at the locale (136°W, 66°N). Thus the two extreme points have been replaced by a hypothetical intermediate point, yielding a median foF2 of 4.5 MHz.

An extract from MONXX starting at cell (3,7,2,1,1,9,2) is shown in COMPUTER OUTPUT 1.

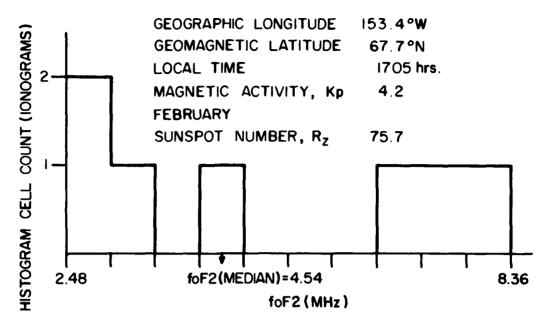


Figure 5. Distribution of foF2, for a Given Set of Conditions.

2.2.3 Sunspot Standardization

Here a procedure for reducing the Nyear files MONXX to a single file MON, of essentially the same form, but standardized to some central sunspot number depending on the respective sunspot numbers of the individual MONXX, will be described. The reason for selecting sunspot number (rather than any of the other 5 independent variables) is that ionospheric characteristics, e.g. foF2, have been observed to possess strong linear relationships with sunspot number, at least up to Rz = 150. See Davies [6], for example.

There are a number of ways in which this standardization procedure may be achieved; here the approach adopted in the C.C.I.R. model [5] is briefly described to note some of the difficulties in applying it to satellite observations. This provides some motivation for the procedure which was actually adopted.

For each of the 60 months (1954-58), the data for each hour of local time at approximately 100 ground stations have been used to determine a numerical map of the form:

foF2 =
$$a_0 + \sum_{j=1}^{6} a_{2j-1} \cos jT + a_{2j} \sin jT$$
 (2.5)

where T = 15 Lt - 180 is the local time relative to noon, in degrees. Actually, each of the a, are dependent on 76 coefficients to describe the longitudinal and latitudinal variations so that for each month (of 60) there are 988 (= 76 \times 13) coefficients in all. Then for a given month, (all years) and for each of the 988 coefficients, a least squares line is fitted to the coefficient versus sunspot number. From these relations, two sets of

COMPUTER OUTPUT 1. Extract from a File MONXX, XX = 62(1)68.

_	10	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
Spread Histogram) o	0	0	0	7	0	m	0	9	0	0	m		0	0	-	0	0	0	-	-	0	0	-	0	0	-	0
E SO) o	~	29	5	Ŋ	ω	5	9	ω	5	56	7₹	21	寸	0	54	'n	58	9	13	7	0	δ		0	0		0
	(0	N	19	0	0	13	22	#	17	9	0	#	5	-	0	16	m	0	0	m	9	0	~	0	0	0	0	0
	0	m	m	Ŋ	-	Ŋ	ω	8	7	m	-	ω		~	0	~	N	m	-	m	2	0	_	-	0	0	-	0
	0	0	φ	m	-	=	0	7	-	-	-	m	0	m	0	寸	0	9	0	N		0	m	0	0	0	0	0
	0	0	7	=	7	~	-	0	0	0	0	_	2	0	0	13	0	1	-	m	m	0	_	0	0	0	0	0
٤	0	0	∞	m	0	α	-	0	0	0	0	-		0	0	_	~	N	~	0	-	0	0	0	0	0	0	0
foF2 Histogram	Jo	0	δ	-	0	Ŋ	9	0	0	0	ω	~	0	_	0	0	0	0	-	0	-	0	0	0	0	0	-	0
H E	/°	0	⇉	_	0	0	Ŋ	_	10	0	m	0	~	0	0	δ	0	m	0	0	—	0	0	0	0	0	0	0
foF	P	0	m	0	0	0	-	_	စ	_	≉	m	S	N	0	~	0	~	0	0	0	0	_	0	0	0		0
	0	0	-	0	0	~	ω	⇉	m	m	-	m	~	≉	0	0	-	0	0	m	0	0	0	_	0	0	_	0
	0	0	9	N	0	0	m	_	9	۲	,-	N	7	_	0	N	7	0	-	_	-	0	~	0	0	0	0	0
1	0	_	-	m		~	~	m	-	_	~	N	~	~	0	œ	-	-	⇉	Ω.	-	0	m	m	0	0	_	0
	8	29	23	7.	21	ଯ	7	42	62	33	23	8	ß	29	8	1,5	æ	8	8	Ж	23	8	8	ま	8	8	2	8
nimS3ot	50.	≠	ં	⋣	ห	7	۲.	m	m	⇒ં	વં	ņ	ø.	ထ်	50.	'n	⇒.	'n	9	Ņ	7	50.	m	m	လို	50.		Š
	8		5			B		2					16	19	8	14	E	12	8	2	R	8	64	₹	8	8	72	8
usrnS∃oì	•	⋾	6	Ŋ	7	6	5	ņ	~	9	9	~	5	0.	•	~	Ŋ	ø	~	œ	σ̈	·	ø	≉ं	•	•	ထ	·
	8	17	.18	Ŗ	89	8	8	8	F.	34.	ĸ	ĸ	8	.53	8	.33	.03	53	રું ક	ず	売	8	₹.	33	8	8	92.	8
דנ		=	12	=	12	5	12	=	=	5	12	12	12	11		12	12	12	12	-	12		12	=			12	
ΚÞ	0	1.3	9		۲.	1.0	6.	2.3	3.0	2.3	2.9	2.8	2.4	2.1	0	٦. 1	3.8	3.7	4.1	4.9	0.	0.	6.5	5.7	•	0	5.7	٥.
	8	ይ	8	8	88	88	ප	8	B	63	8	24	2	23	8	17	13	ထွ	8	8	7	8	8	8	8	8	_	8
X	•	49.	46.	47.	46.	47.	47.	50.	47.	46.	1 6.	47.	₹ •	48.	٠	1 6.	48.	1 2	47.	48.	46.	•	<u>4</u> 6.	49.	•	•	47.	•
	0	'n	2	'n	φ	۲.	5	'n	⊅.	'n	'n	'n	7	m	0	₹.	œ	9	⋾ .	9	⋾	0	9	₹.	o.	o	0	o
mtt#.	_	57	57	57	5	57	5	52	57	57	5	5	57	57	_	52	57	57	57	5	57	_	57	57	_	_	- 28	_
6 uo⊐	0	7.7	8	7.8	S.	2.0	14.7	3.2	2.9	7.2	رن م	<u>ش</u>	60	7.0	•	80	Ω	3.2	5	7.6	6.7	٥.	0.4	æ.	۰.	0.	0.0	٠.
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u								14																				
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ίκ. Γίν Γ	7211	211	211	211	211	211	211	212	212	212	212	212	212	212	213	213	213	213	213	213	213	214	214	214	214	21⊈	214	214
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J ,		·							-	•	Ť	·		-	•	-	·	·	•	Í	•	•	•	•	•	•	•	

988 coefficients are tabulated, for each month, corresponding to the sunspot numbers Rz=0 and Rz=100.

For a topside model, 72 months of data (1963-68) would have to be fitted to a map of the above form in 3 month stages at least (to ensure complete local time coverage). This would mean that the aj would also have to depend on an extra variable, month, and perhaps even a Kp variable. This would give 24 (seasonal) sets of approximately 988 coefficients. Then for a given season and coefficient, a least squares line would be fitted to the coefficient versus "seasonal" sunspot number relationship. There can be quite a bit of variation of sunspot number with season — especially during the years 1966-68 where the data are scantiest (see Table 2).

The procedure adopted here will be an "inverse" of the above - i.e. predictions are made for foF2 for a given set of conditions (Long, Lattm, Lt, Kp, and M from a given record of MONXX) and then these (at most) Nyear numbers (one from each year) are standardized to an intermediate sunspot number.

The Nyear files MONXX are first merged into one, MONB96, which has a blocked record format. That is, each record consists of the same cell for all years (864 blocked records). Unfortunately the number of ionograms varies considerably from year to year for a given cell. Probably an even more serious difficulty is that in trying to keep only "quality" cells (with Nyear or Nyear-1 years of data) the geographic coverage is drastically reduced overall. This is illustrated in Table 5 for 2 particular months.

For brevity, any such cell will be denoted as type (M,N). The M years are not necessarily the first M years (starting from 1962 or 1963), but in most cases this will probably be true. Thus, for example, if only cells with at least 2 years containing at least 2 ionograms are desired, the "practical minimum", only 447 cells out of 595 (75%) are kept for February.

The procedure actually adopted is to use only the (2,2) cells of MONB96. Thus for each of these cells a least squares fit is performed to the Nyear pairs of median foF2 and actual sunspot number to obtain:

$$foF2 = a Rz + b (2.6)$$

Then, in later interpolation and prediction (see section 2.3), only those cells which yield positive values of a and b are used. It is noted here that of the 10,368 (= 12 x 864) cells there are 5,618 of type (2,2). Of these, 586 gave non-positive values for a or b. Thus, for use in interpolation and prediction, (see section 2.3) there will be 5,032 (or approximately half of the total possible). As a matter of interest, it is noted that there are 1,005 cells (all months) which only contain 1 year of data. No attempt has been made to incorporate these cells into the model since coefficients a and b in (2.6) cannot be determined, independently, for each cell. Furthermore there are 126 cells (all months) which yielded values of a > 0.1. The majority of these are of "dubious" quality arising from calculating a and b with 2 or 3 years at essentially the same sunspot number.

While some of these coefficients (a and b) may be "rough", leading to "rough" values of foF2, these values will be smoothed out later (see section 2.3). This "roughness" and the effect of smoothing are illustrated in

TABLE 5

B(M,N). The Number of Blocked Records (Cells), for February and October, which have at Least M Years with at Least N Ionograms each Year.

2	•	
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ì	î	
į	4	

20	236	เรเ	66	ا9	12	9
15	306	203	132	46	46	13
10	382	274	189	135	77	33
5	502	386	297	216	132	ا 9
4	529	410	327	234	154	74
3	549	425	344	262	166	87
2	929	447	373	301	197	94
ı	269	470	401	328	230	911
Z	1	2	8	4	9	9

OCTOBER

20	-		314					
15		365		274	274			
10		425		333	333	333 275 213	333 275 213 153	275 275 213 153 68
S		547		417	417	417 365 321	417 365 321 244	417 365 321 244 143
7		572		445	445	445 377 339	445 377 339 262	445 377 339 262 162
3		597		467	467	467 395 352	467 395 352 296	467 395 352 296 175
2		625		487	487	487 410 375	487 410 375 319	487 410 375 319 202
_		647	֡	512	512	512 439 396	512 439 396 341	512 439 396 341 225
Z-/	Σ			2	3	3 4	3 4	3 4 6

Figures 6(a) and 6(b). The local time of these plots is about 1730 hours at 45°N geomagnetic latitude. The actual regression model for the smoothed gradients, a (MHz/unit sunspot number), is:

$$a = 0.053 - 0.011 \sin(\pi Lt/12) - 0.015 \cos(\pi Lt/12)$$

$$+ 0.016 \cos^{2}(\pi Lt/12) - 0.037 (Lattm/90)$$

$$+ 0.015 (Lattm/90)^{4} - 0.046 (Kp/9.3)^{3}.$$
(2.7)

with a root mean square error of ± 0.019 in a.

The equation (2.7) was determined by applying a stepwise regression procedure [24] to all February cells which yielded values of a and b. Only statistically significant (non-zero) coefficients (up to order 4) are displayed in (2.7).

The actual details of the standardization of a given cell of MONB96, assuming there are a "suitable" number of years containing a "suitable" number of ionograms are now given. One should also note Figure 7 where the mathematical assumptions underlying the standardization procedure are illustrated, namely:

- (1) the gradient of foF2 with sunspot number, a, is positive,
- (2) the intercept at Rz = 0, b, is positive,
- (3) the conditional probability distribution of foF2 for a given Rz is independent of Rz.

The following notations are used in the standardization procedure. Let $(n_k \text{ Long}_k, \text{ Lattm}_k, \text{ Lt}_k, \text{ Kp}_k, \text{ Rz}_k, \text{ Fmin}_k, \text{ Fmax}_k, (A_{ki}: i=1(1)10, B_{ki}: i=1(1)4)) k=1(1) \text{ Nyear} \geq 2 \text{ denote a particular blocked record (cell) of MONB96. Here } A_{ki} \text{ and } B_{ki} \text{ are the histogram occurrence frequencies on } [Fmin_k, Fmax_k] \text{ and } [0.5, 4.5] \text{ for foF2 and spread, respectively. Note that}$

First the medians $M_k(F)$ and $M_k(S)$ are computed from the foF2 and spread histograms using inverse linear interpolation between the right-most abscissae and the cumulative histogram probabilities. Using the pairs $(Rz_k, M_k(F))$ k = 1(1)Nyear, regression coefficients a and b such that foF2 = aRz + b are computed. Then using $Rz = \frac{Nyear}{\Sigma} Rz_k/Nyear$ the standardized limits of the foF2 histograms are computed:

SFmin = min (Fmin_k + a(Rz - Rz_k))
$$k$$

and
$$SFmax = max (Fmax_k + a(Rz - Rz_k))$$

The A_{ki} observations $F_{ki} = Fmin_k + (i - 0.5)h_k$ where $h_k = (Fmax_k - Fmin_k)/10$ are standardized to $SF_i = F_{ki} + a(Rz - Rz_k)$ and inserted into a histogram with

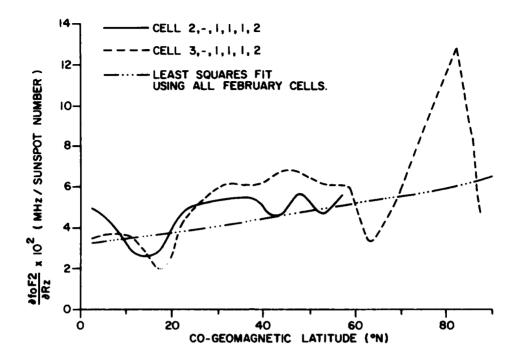


Figure 6(a). Behaviour of foF2-sunspot Number Gradient, Kp < 1.5.

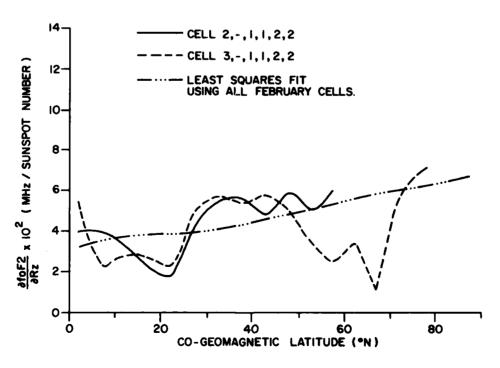


Figure 6(b). Behaviour of foF2-sunspot Number Gradient, 1.5 < Kp < 3.5.

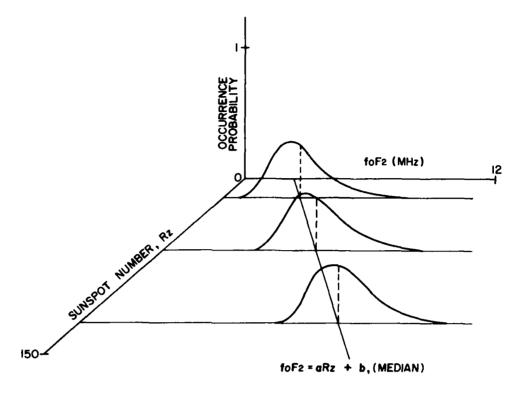


Figure 7. Assumptions Concerning the foF2 Distribution (for a Given Cell, all Years) Used in the Sunspot Standardization Procedure.

10 equidistant intervals on [SFmin, SFmax] with occurrence frequencies SA_{i} .

Note that
$$\begin{array}{cccc} & 10 & & \text{Nyear} \\ & \Sigma & \text{SA}_{i} = & \Sigma & n_{k} = \text{N.} \\ & i=1 & & k=1 \end{array}$$

In a similar fashion, one could standardize the spread distributions. However, due to the subjectiveness of that index they have been simply accumulated for all years. Essentially then, it is assumed that spread is independent of sunspot number. As a matter of interest, Figure 8(a) shows median spread plotted against sunspot number for 3 different cells. The local time of these cells is approximately 0900 hours in January and July and 1300 hours in December.

The spread occurrence frequencies are then:

$$SB_i = \sum_{k=1}^{Nyear} B_{ki}$$
, $i = 1(1)4$

Finally arithmetical means of Long, Lattm, Lt, and Kp, for all years are computed for each cell.

A "keyed" record is written on the file MONSTD to represent the standardized cell. The contents of this record include: (Key, N, Nyear, Long, Lattm, Kp, Lt, Rz, SFmin, SFmax, SA_i , SB_j , a, b), i = 1(1)10, j = 1(1)4. (See also COMPUTER OUTPUT 4, section 2.3).

The keys associated with each record are of a type associated with direct access READ/WRITE statements, which enable the user to directly access standardized cells upon specification of his input conditions. The keys are integers defined as a linear combination of the cell subscripts, with the weights depending on the particular cell alignment used. In this case:

$$Key = \frac{10368 \text{ (LM-1)}}{12} + \frac{864 \text{ (LO-1)}}{3} + \frac{288 \text{ (LA-1)}}{18} + \frac{16 \text{ (LT1-1)}}{2} + \frac{8 \text{ (LT2-1)}}{2} + \frac{4 \text{ LK}}{4}$$

or more compactly,

$$Key = 864 LM + 288 LO + 16 LA + 8 LT1 + 4LT2 + LK - 1180$$
 (2.8)

Thus the keys are in the range [1, 10368] with empty cells (no data) corresponding to non-existent keys. The last step in preparing the reduced data file for the model is simply to concatenate all the months together using PCL (file management system for the Honeywell computer) on a file ALLMON.

A single example is now presented.

Example 2: February: 1,5,2,1,3,2; this is a (3,5) cell (see Table 5).

Here there are 3 quality years: 1964, 1966 and 1967.

The blocked record of MONB96 appears as:

In Figure 8(b), the median foF2 v. Rz relationship for these three years has been plotted for this cell. The standardized histogram of foF2 lies in [1.71, 7.59] with occurrence frequencies consisting of the array

from minimum foF2 to maximum foF2.

As a consistency check it is noted that for the immediately preceding cell (lower Kp), the foF2 v. Rz relationship is even "flatter":

$$foF2 = 0.019 Rz + 3.64.$$

This cell is of much better quality, (5,15), in terms of Table 5.

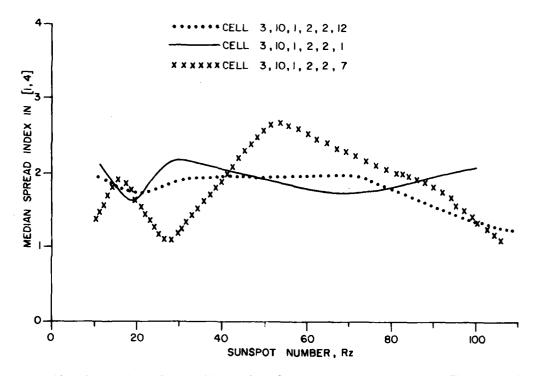


Figure 8(a). Spread Versus Sunspot Number for a Given Longitude, Latitude, Local Time, Magnetic Activity and Month.

154.5°W

GEOGRAPHIC LONGITUDE

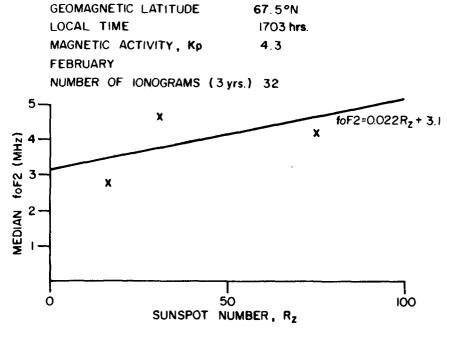


Figure 8(b). foF2 Versus Sunspot Number for a Given Longitude Latitude, Local Time, Magnetic Activity and Month.

2.3 IMPLEMENTATION OF THE MODEL

2.3.1 Real Time Accession of the Data

The reduced file, ALLMON, now exists which consists of at most 10,368 keyed records, each record representing a standardized cell. Actually about one third of these records will be "non-existent" due to empty cells over oceans areas.

Upon specification by the user of a particular point (Long, Lattg, Rz, M, Kp), the subscripts of that cell can be computed, the key computed by equation (2.8), and the cell directly accessed. Actually only the shortened equation

$$Key = 864 LM + 288 LO + 16 LA + 8(2) + 4(2) + 4 - 1180 - 16$$

$$= 864 LM + 288 LO + 16 LA - 1168$$
(2.9)

need be used and (at most) the next 16 cells for each of the months M-1, M, and M+1. As mentioned above, 3 months are required to obtain sufficient local time coverage. See Table 6 for a display of the cell (key) structure of ALLMON. With little additional effort, one can access 5 months (i.e. also M-2 and M+2); however, unless stated explicitly otherwise, it will be assumed throughout the remainder of the chapter that 3 months have been accessed.

A few comments concerning the use of Table 6 are appropriate:

- (1) This represents the "format" for the month of January (other months are simply translations of the key by 864).
- (2) The 3 longitude zones are represented by the 3 major columns, and the 18 latitude zones by the 18 major rows.
- (3) Within one of the large blocks, the four columns represent the 4 local time zones (with indices 11, 12, 21, and 22) while the 4 rows represent the 4 Kp zones in order of increasing magnetic activity.
- (4) The contents of any cell up to cell 495 of December (Key = 11 x 864 + 495 = 9999) can be actually displayed by using the EDIT processor of the Honeywell Sigma 9 computer. For greater keys, one must resort to the KFM (keyed file manipulation) processor.

Having accessed at most 48 cells (4 Kp \times 4 local time \times 3 months) one must first adjust the data to the user's sunspot number, magnetic activity, and month. The values of the characteristics will actually be computed for all local times (hourly intervals).

2.3.2 Correction to the User's Rz and Kp

For each of the (at most) 48 cells the foF2 is adjusted to the user's sunspot number Rz using:

$$foF2 = a(Lt, M, Kp) Rz + b(Lt, M, Kp)$$
 (2.10)

TABLE 6
Key Structure of ALLMON for January

					GEOG	RAPHIC	LO#	GIT	IDE (o _{w}}			
			180	1,135			1 35				(90.4	5)	
	90			-									
		1 2	5	10	13 14			297 298			581 582		
	Ì	3	7	11	15		295		303		583		
	85	4	9	12	16	292	296	300	304	580	584	588	592
	٠,١	17	21	25	29	305	309	313	317		597		
	l	18 19	22	26 27	30 31	306 307		314 315		594 595	598 599	602	606
		20	24	28	32	308	312		320		500		
	80	33	37	41	45	321	325	329	333	509	613	617	621
	ļ	34	38	42	46	322	326	330	334		614		
		35 36	39 40	43 44	47 48	323	327 328	331 332	335 336	612	515 516	620	
	75	49	53	57	61	337	341	345	349	625	629	637	637
	}	50	54	58	62	338	342	346	350	626	630	634	638
	- 1	51 52	55 56	59 60	63 64	339 340	343 344	347 348	351 352	627 628	631 632	635 636	
	70												
		65 66	59 70	73 74	77 78	353 354	357 358	361 362	365 366		645 646		
		67	71	75	79	355	359	363	367	643	647	651	555
	65	58	72	76	30	356	360	364	368	_544		552	656
	1	81 82	85 86	39 90	93 94		373 374	377 378	381 382		661 662		
		83	87	91	95	371	375	379	383	659	663	567	671
_	60	84	88	92	96	372	376	380	384	660	664	568	572
		97	101 102	105	109	385	389				677		
		99	103	107	111	386 387		395	399	675	678 679	683	687
	55	100	104	108	112	388	192		400		580		
	,,,		117		125			409			693		701
_	- {		118					410			694 695		
€.	ایج-	116	120	124	128		408		116	592		700	
	50	129	133	137	141	417	421	425	429	705	709	713	717
₹		130	134 135	138	142	418	422 423	426	430 431	706 707	710	714 715	718 719
ቜ .		132	136					428		708		715 716	720
GEOMAGNETIC LATITUDE	45	145	149	153	157	433	437	441	445	721	725	729	733
3		146	150	154	158	434	438	442	446	722	726	730	734
Š		147 148	151 152	155 156	159 160	435 436	439 440	443 444	447 448	723 724	727 728	731 732	735 736
3	40	161	165	169	173			457	461	737	741	745	749
		162	166	170	174	450	154	458	462	738	742	746	750
	_]		167 168	171 172	175 176	451 452		459 460		739 740	743 744		751 752
	15												
			182		190	466	470	473 474	478	754	757 758	762	765 766
		179 180	183 184				471 472	475 476		755 756			767 768
	30												
		194	197 198	202	206			489 490		769 770	773 774		781 782
			199 200			483		491		771 772		779	783 784
	25										_		
	Į	209 210	213 214	217 218		497 498	501 502	505 506		785 786		793 794	797 798
	ļ	211	215	219	223	199	503	507	511	787	791	795	799
	20		216					508		788		796	200
		225	22 9 230	233	237	513 513	517	521 522	525 526	801 902	805 806	909	913 814
	ļ	227	231	235	239	515	519	523	527	803	807	811	915
	15	_220	232	236	240	516	520	324	528	904	908	912	916
		241	245	249	253			537 538		917	921	925	929
	-	243	246 247	251	255	531	535	539	543	919	822 823	827	831
	10	244	248	252	256			540			924		
	, ,	257	261	265	269	545	549	553	557	833	937	841	945
	- 1	258 259	261 262 263	266 267	270 271	546 547	550 551	554 555	558 559	834	838 839	942	346
	- 1												
	_	260	364	-68	272	298	224	556	:60		B4U	344	348
	- 5	<u>260</u> 271	277	281	285	561	565	569	573	949	953	957	861
	5	<u>260</u> 271	277 278 279 280	281	285	561	565 566	569 570	573 574	949 850		957 958	861 362

For the remaining characteristics (foF2 percentile, median spread, spread percentile) the following is used:

$$U_c = Sc + a (Lt, M, Kp) (Rz - Rz)$$
 (2.11)

where Sc is the characteristic computed from the standardized histogram,

Rz is the average sunspot number of the cell,

Uc is the characteristic corrected to the user's Rz.

As discussed above a(Lt, M, Kp) is taken to be zero for the spread (see Figure 8(a)).

At this point, for each of the 12 (Lt,M) pairs, there exists an array of at most 4 pairs (Kp_i, Uc_i) , i = 1(1)4, where Uc_i is the value of the characteristic adjusted to the user's sunspot number (if necessary). To interpolate to the user's Kp, UKp, the following is used:

$$U_{c} = \begin{cases} Uc_{1} & UKp \leq Kp_{1} \\ P_{3}(Uc_{1}, Uc_{2}, Uc_{3}, Uc_{4}) & Kp_{1} < UKp < Kp_{4} \\ Uc_{4} & UKp \geq Kp_{4} \end{cases}$$
(2.12)

where P_3 is the Lagrange interpolation polynomial of degree 3 through the 4 points. If there are less than 4 such pairs (due to non-existent cells or "missing" Rz coefficients a,b) the degree of the Lagrange interpolation is appropriately reduced. If the number of points available is zero, there will be less than 12 triples to be used in interpolation in the next section. In such a case, the user is informed and the interpolation procedure in section 2.3.3 is omitted. However, the user can obtain the available triples (< 12).

2.3.3 Interpolation to Month and Local Time

The 12 triples (M_i , Lt_i , Uc_i), i = 1(1)12, corresponding to the 6 halfmonths of data with 2 periods of local time each are used in a least squares model to obtain an array of the characteristic at the middle of the user's month and for each hour of local time. The variable used to describe the monthly variation is

$$W_{i} = \begin{cases} i & \text{i is odd} \\ \\ i-1 & \text{i is even} \end{cases}$$

Thus it is essentially assumed the data for a given half month occur at the middle of the half month. The form of the model to fit the data is:

$$Uc(Lt,W) = b_{0} + \sum_{j=1}^{4} b_{2j-1} (\sin \pi Lt/12)^{j} + b_{2j} (\cos \pi Lt/12)^{j} + \sum_{j=1}^{3} b_{j+8} (W/12)^{j}$$
(2.13)

W in [1, 12]; Lt in [0, 24]

The subroutines STEP1 and STEP2 perform a stepwise regression procedure for calculating and selecting the statistically significant (non-zero) coefficients $b_j:j=0(1)11$. See also Ralston and Wilks [24] or Frazer [8]. These subroutines require a pair of parameters (F1,F2) which are used for entering and removing a given variable in the model (2.13). Typical values of F1 and F2 are about 5 for a 95% level of significance.

2.3.4 Illustration

A display of the results of the main prediction program, PREDSYS, is now given where the user has input the conditions:

Long =
$$67^{\circ}$$
W, Lattg = 45° N, Rz = 30, Kp = 1+, M = 2

He also desires a 90% - tile for each of the characteristics. See COMPUTER OUTPUT 2 for an example of the actual execution procedure.

In COMPUTER OUTPUT 3, the foF2 (MHz), spread, and slab thickness (km) are listed for each hour of local time. Finally, in COMPUTER OUTPUT 4, the actual cells of ALLMON (directly accessed in the above predictions) are displayed. See remark 4 in section 2.3.1.

In Table 7, the actual (significant) regression coefficients of (2.13) as well as the Root Mean Square Deviation of the estimates are displayed, for each of the 4 characteristics, corresponding to the set of predictions in COMPUTER OUTPUT 3. The empirical model for slab thickness is described in Chapter 3.

In Figures 9(a), 9(b), and 9(c) contour maps of foF2, spread and slab thickness are displayed for the above input conditions, including all northern latitudes.

In conclusion, the following remarks are made:

- (1) The Root Mean Square Deviation (in Table 7) is only strictly applicable to the deviations between the actual (12) observed values of a characteristic and the calculated values using (2.13). However these deviations should approximately apply for any predictions Uc (Lt,W) in view of the natural continuity of the characteristic, in local time and month.
- (2) The accuracy of estimates (and even the capability of prediction) is dependent on the number of ionograms available in the various cells directly accessed. Inspection of the data totals, for a typical month, (see Table 4) suggests the following real spatial domain. D. for the model.

$$D = (A1 \times A2) \cup (B1 \times B2) \cup (C1 \times C2)$$
 (2.14)

where A1, A2, B1, B2, C1 and C2 are the sets:

A1 : [180°W, 135°W]

 $A2 : [45^{\circ}N, 90^{\circ}N]$

B1 : [135°W, 90°W]

 $B2 : [30^{\circ}N, 90^{\circ}N]$

C1: [90°W, 45°W]

 $C2 : [0^{\circ}, 90^{\circ}N]$

The first set of each pair, in (2.14), is the longitude range; the second is the geomagnetic latitude range.

In addition the sunspot number range is restricted to $Rz \le 112$ (Table 3) although there is some evidence [6] that foF2 is independent of Rz for Rz > 150. A more serious limitation is that approximately two thirds of the data is in the low sunspot number range (Table 2)

(3) One could directly access 5 months of data with little extra effort by redefining the size of the arrays in PREDSYS. This would yield at most 20 triples of observations to be used in the

TABLE 7

Illustration of Significant Regression Coefficients in Equation (2.13)

,					
		foF2	foF2 %	SPREAD	SPREAD %
0	CONSTANT	3.3842	4.1832	2.0866	2.4575
1)	
2	l l	-2.1063	-1.9051	{	
3	L 0 C A				0.49167
4	î		1		<u> </u>
5	Ţ	-1.5679	-1.7373		{
6	M E			0.076441	}
7	_				
8				-0.18646	
9	M 0		ţ		(
10	N T		2.7504		}
11	н	1.9931	1		}
ROOT MEAN SQUARE DEVIATION		0.61	0.64	0.05	0.18

COMPUTER OUTPUT 2. Example of Control Procedure Required for Predictions

```
.EXAMPLE SET OF PREDICTIONS USING EXPREDSYS
!.FOR LONGITUDE=67 W(DEGREES).LATITUDE=45 N(DEGREES)
!.RZ=30.FEBRUARY,KP=1+
!XEQ EXPREDSYS .36
    0036 - 1.
    0037 - !.A FILE NULL IS BUILT CONSISTING OF A SINGLE RECORD.
    0038 - !.NAMELY THE 2 CHARACTERS !.
    0039 - !. THIS IS USED TO BREAK THE EXECUTION AFTER THE
    0040 - !. USER OBTAINS HIS CONTOUR DATA, ON UNIT 80, TO
    0041 - !.BE USED FOR EDITING . AFTER HE COMPLETES THE
    0042 - 1. TASK, HE CAN RESUME EXECUTION AT THE LINE 91
    0043 - !.FOR CONTOUR PRODUCTION.
    0044 - !B NULL
   1.000 1.
   2.000
    0045 - 1.
    0046 - !. THE OLD GRID OF CONTOUR DATA IS DELETED.
    0047 - 1.
    0048 - IDELETE NEWPLOT1
  0300 FILE DOES NOT EXIST.
    0049 - !SET F: 105 ME: IN
    0050 - !SET F:6/ALLMON; IN; KEYED; DIRECT
    0051 - !SET F:7 ME:OUT
    0052 - !SET F:80/NEWPLOT1;OUT;KEYED;DIRECT
    0053 - !SET F:70/ADJRZ;OUT
    0054 - !SET F:71/ADJKP;OUT
    0055 - !SET F: 108/REGFIT:OUT
    0056 - !LYNX BPREDSYS, BMISC, BSSTEP1, BSSTEP2
:P1 ASSOCIATED.
GROUPC2 OF :LIB.:SYS ASSOCIATED FOR POSREC
GROUPO4 OF :LIB.:SYS ASSOCIATED FOR SQRTF
GROUP21 OF :LIB.:SYS ASSOCIATED FOR GOEFILE
GROUP23 OF :LIB.:SYS ASSOCIATED FOR TERRARG
GROUP 14 OF :LIB.:SYS ASSOCIATED FOR 91FR
GROUP 17 OF :LIB.:SYS ASSOCIATED FOR 9INPUTL
   * * ALLOCATION SUMMARY * *
PROTECTION
                LOCATION
                           PACES
DATA (00)
                  A000
PROCEDURE (01)
                  B600
                             10
DCB (10)
                  B200
                              2
    0057 - 1.
    0058 - 1.ST GIVES CURRENT CPU TIME CONSUMED.
    0059 - 1.
    0060 - IST
```

COMPUTER OUTPUT 3. Example of Predictions Using Control Procedure of COMPUTER OUTPUT 2

CPU = .1505 CON= 00:19:03 INT = 25 CHG = \$.94 CALS = 1255 0061 - !S SPECIFY YOUR LOCATION...EXAMPLE, FOR OTTAWA.... -75.0,45.,56,2,1.7,.95,.75,...MEANS GEOGRAPHIC LONGITUDE IS 75W(DEGREES). GEOGRAPHIC LATITUDE IS 45N (DEGREES). SUNSPOT NUMBER IS 56...IF SUNSPOT NUMBER IS > 150, ENTER 150 AS THE CHARACTERISTICS ARE ASSUMED INDEPENDENT OF IT IN THAT DOMAIN. MONTH IS FEBRUARY, IE MIDPOINT OF THE MONTH 3-HOURLY KP IS 2-. A 95 %-TILE OF FOF2 IS DESIRED. A 75 %-TILE OF SPREAD IS DESIRED. ALL CHARACTERISTICS ARE COMPUTED FOR EACH HOUR OF LOCAL TIME...INCIDENTALLY, A 95%-TILE IS THE VALUE OF THE CHARACTERISTIC SUCH THAT 95 % OF THE DATA IS LESS THAN THAT VALUE. FOF2 IS IN MHZ...SLAB THICK IS IN KM TO STOP, ENTER 1000,0,0,0,0,0,0. ALSO USE THIS AS THE LAST RECORD OF AN INPUT FILE OF CONDITIONS...IE WHEN PREPARING CONTOUR MAPS. SEE COMMENT STATEMENTS IN SOURCE PROGRAM ABOUT PREPARING CONTOUR MAPS. ?-67,45,30,2,1.3,.9,.9
THERE ARE 12 TRIPLES OF LOCAL TIME AND MONTH DATA IF LESS THAN 12, TRY AN ADJACENT CELL...OR DIRECTLY ACCESS THE CELLS USING EDIT OR KFM PROCESSORS. THE PRELIMINARY INTERPOLANTS ARE ON UNITS 70 & 71 GEOGLONG= -67.0 GEOGLAT= 45.0 SUNSPOT= 30. MONTH= 2 KP=1.3 PROB FOF2= .90 PROB SPREAD= .90 GEOMATLAT=56.4

LOCAL TIME 0 1 2	F0F2 1.5 1.6 1.6	FOF2% 3.0 3.0 3.0	SPREAD 2.0 2.0 2.0	SPREAD% 2.5 2.5 2.6	SLAB	THICK 181. 175. 178.
3	1.6	2.9	2.1	2.7		193.
4	1.6	2.8	2.1	2.8		213.
5	1.7	2.8	2.1	2.9		231.
6	2.1	3.1	2.1	2.9		238.
7	2.8	3.8	2.1	2.9		231.
8	3.7	4.7	2.1	2.8		213.
9	4.6	5.6	2.0	2.7		193.
10	5.3	6.3	1.9	2.6		178.
11	5.6	6.7	1.9	2.5		175.
12	5.7	6.8	1.8	2.5		181.
13	5.7	6.7	1.9	2.5		192.
14	5.7	6.7	1.9	2.6		201.
15	5.7	6.8	2.0	2.7		202.
16	5.7	7.0	2.1	2.8		198.
17	5.6	6.9	2.1	2.9		192.
18	5.2	6.6	2.1	2.9		189.
19	4.5	5.9	2.1	2.9		192.
20	3.6	5.0	2.1	2.8		198.
21	2.7	4.1	2.1	2.7		202.
22	2.0	3.4	2.0	2.6		201.
23	1.6	3.1	2.0	2.5		192.
24	1.5	3.0	2.0	2.5		181.
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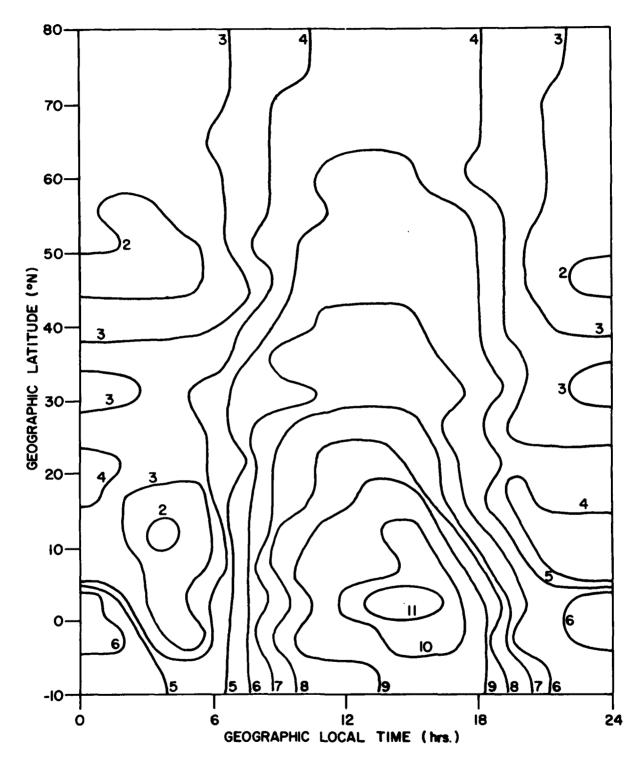


Figure 9(a). Contours of Characteristics in Latitude and Local Time, foF2 (MHz).

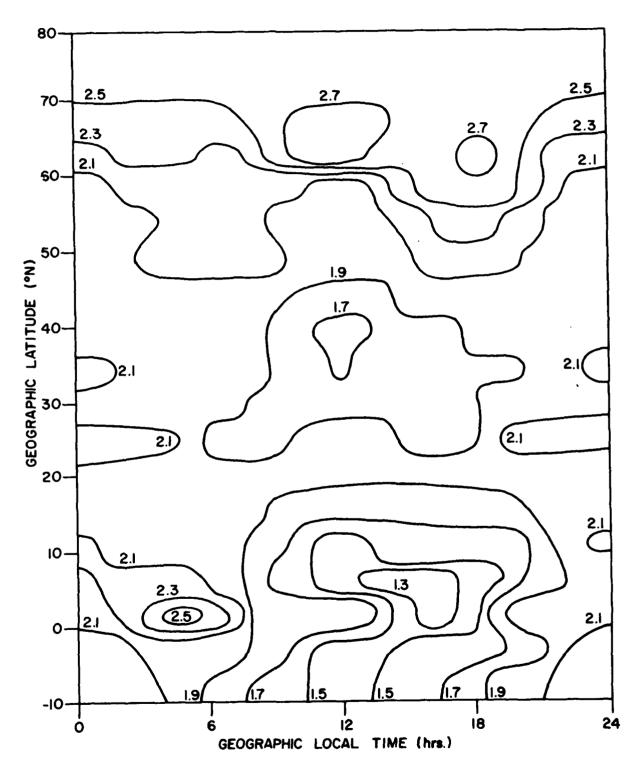


Figure 9(b). Contours of Characteristics in Latitude and Local Time, spread in [1,4].

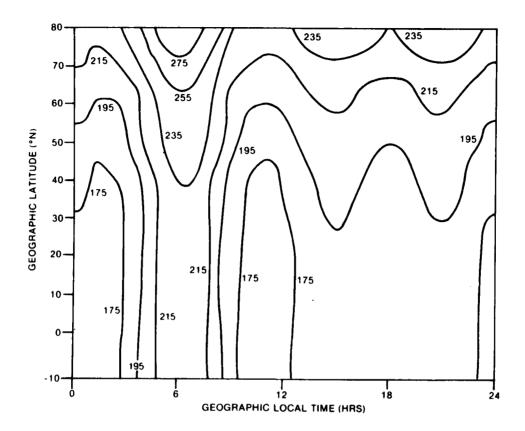


Figure 9(c). Contours of Characteristics in Latitude and Local Time, Slab Thickness (km).

determination of the model (2.13). Balanced against this, there would be more monthly variation to be described by the model.

(4) The current cell alignment, for a given month, leads to a prolific number of cells with few ionograms (especially for those corresponding to high magnetic activity). Perhaps only 2 Kp zones, or a single zone for all Kp's would ameliorate this situation. A "smoothed bi-weekly Kp average" could be attached to each of the resulting 216 (= 864/4) cells. To consider such questions one only needs to apply ACCMONB96 which operates on the file MONB96 (blocked cells, but unstandardized). These files have been stored on magnetic tape (all months); see Appendix A (listing of tapes).

3. N(h) MODEL

3.1 DESCRIPTION OF THE DATA BASE

About 80,000 Alouette 1 and 2 ionograms have been scaled to produce almost complete topside electron density profiles. These profiles have been

stored on 16 9-track tapes. Alouette 2 was launched in November 1965, and unlike Alouette 1 it had an elliptical orbit: apogee = 3000 km, perigee = 500 km. Since the ionograms were scaled on demand they were actually stored on tape as the need arose, resulting in a very fragmented data base, unlike ALOSYN. Indeed, the actual details of the reduction procedure [11], to generate N(h) profiles, was varied throughout the years.

In Table 8 a summary of the data totals of the various tapes over the years is presented. Some remarks pertaining to this table follow.

- (1) The ionograms within a volume are in chronological order (as they were scaled).
- (2) In A Format, the electron density profiles have been calculated by assuming f_N , the plasma-frequency, is linear in height on each lamination.
- (3) In B Format, the reduction has been achieved by assuming the log of the electron density varies parabolically in each lamination (but linearly in the first lamination nearest the satellite).
- (4) The profiles tabulated by the Ames Research Centres (AMES) are actually interpolated to give electron densities at every one hundred kilometres from the height of the satellite. In addition they distinguish between field-aligned and non field-aligned profiles.
- (5) The topside TEC, in A Format, was calculated by integrating (exactly) the model electron density, N(h), from the height of the satellite to a height of maximum electron density. The latter was calculated by passing a parabola through the lowest 2 scaled points and assuming for 2 was 0.01 MHz greater than the lowest scaled f_N. Thus, the topside TEC has been adjusted to include only the area to the last scaled point; the remainder of the TEC (bottomside) will be computed from the model to be described in section 3.2.2. In B Format, the topside TEC was computed to the lowest scaled point, assuming the electron density is linear on each lamination. The Ames profiles do not give TEC so a value consistent with the B Format profiles was calculated and put on tape.

There also exist 10 tape volumes of ISIS 1 and 2 profiles in B Format. These two satellites are similar to Alouette 2 and 1, respectively, in orbital configuration. They were launched in 1969 and 1971 during a decreasing period of solar activity. Thus, the data reduction procedures to be described below are readily adaptable to these data as well.

3.2 DEVELOPMENT OF THE MODEL

3.2.1 Organization of the Data Base

The intention of this section is the construction of a chronological ordered data base of the N(h) profiles. Each profile of this new base will

TABLE 8

N(h) Profile Data Available

TAPE VOLUME	SATELLITE	FORMAT	ERA	NUMBER OF IONOGRAMS
1 - 4	ALOUETTE 1	A	1962 - 66	43700
5 - 7	ALOUETTE 1	В	1963 - 70	18400
1 - 5	ALOUETTE 2	В	1965 - 72	12000
6 - 9	ALOUETTE 2	AMES	1966 - 72	5200
1 - 5	ISIS 1	В	1969 - present	35000
1 - 5	ISIS 2	В	1971 - 78	43000

consist of the identification parameters (time, location, Kp, and Rz) together with certain profile characteristics, e.g. TEC (topside), TEC (bottomside), hmax, and slab thickness. The definition of these characteristics will be considered in more detail in the next section. This new data base, ALOUETTE NH, will then be similar to ALOSYN, although not nearly as extensive of course. Thus, the entire procedure of Chapter 2, with a necessarily coarser grid, can be applied to ALOUETTE NH.

An illustration of this approach will be given in section 3.2.4, for a selection of 10,000 Alouette 1 profiles (1965-70) which cover (sparsely) a half solar cycle, i.e. Rz in [12, 112] (see Table 3). The empirical model used for slab thickness, in COMPUTER OUTPUT 2, will also be fitted to these data.

The process of constructing ALOUETTE NH consisted of processing (calculating the frequency and heights, calculating the topside TEC, and attaching the Kp) for each of the 16 volumes, described above, one at a time. The resulting 16 output files were concatenated, sorted chronologically, and blocked (at the rate of 10 profiles per record). Only profiles in the longitude range [-180°, -45°] are included in ALOUETTE NH. However, due to the small data base, all geomagnetic latitudes are included, and it is assumed that slab thickness is symmetric about the geomagnetic equator.

The data actually kept for a particular profile of ALOUETTE NH are as follows:

Volume (tape number of original profile of ALOUETTE N(h); see Table 8)

Kp (integer part only)

Dip (dip angle at the satellite, degress)

Job (see below)

Year, Day, Hour, Minute, Second (Universal time)

TTEC (topside TEC from h_o to h_L in electrons/cm², where h_o is the satellite height and h_L is the lowest height of the topside profile)

L+1 (number of pairs of points for profile)

 f_{H} (gyrofrequency at h_{O} , MHz)

Long (degrees)

Lattg (degrees)

χ (Solar angle at satellite, degrees)

 f_N (a 4xl vector, plasma frequency at h_0 , h_{L-2} , h_{L-1} , and h_L , MHz)

h (a 4xl vector, real height h_0 , h_{L-2} , h_{L-1} , and h_L , km)

The Job parameter is a subjective index concerning the quality of the profile on a scale of 4 (excellent) to 9 (scaled under protest). In the case of the Ames profiles, this parameter was used here to indicate whether the profile is field aligned or not.

In the field-aligned case, the longitude and latitude are the arithmetic means of the longitudes and latitudes of the various points along the magnetic field direction.

3.2.2 Definition of the Profile Using ALOUETTE NH

Here, a method of defining a parabola will be outlined, using the data of ALOUETTE NH, to represent the profile from \mathbf{h}_L down to \mathbf{h}_b , a base for a hypothetical F2 layer to be defined below. From this parabola, rough estimates of the bottomside total electron content (BTEC), hmax, and slab thickness can be made. High quality estimates will also be compared with an alternative method (for limited samples of data) using ground echoes. High quality ground echoes usually only occur on the Alouette ionograms from soundings taken over water or over less densely populated areas where noise levels are low. This fact, combined with the additional scaling effort that would be required, precludes the use of this method for the entire data base.

The first step is to define certain subsets of ALOUETTE NH consisting of "quality" profiles. Here, quality means that the last point (N_L , h_L) is "reasonably close" to the peak electron density (Nmax, hmax). The electron density N is related to the plasma frequency f_N at any height, h, by

$$N = 1.24 \times 10^4 \times f_N^2 \tag{3.1}$$

where N is in electrons/cm³, f_N is in MHz. Usually the profiles from topside soundings tend to be too low [12]. However, Jackson [12] notes that they can also be high (particularly for soundings when the satellite is above 2000 km). To define the subset of quality profiles some weak conditions will be imposed on the pairs of points, rather than simply relying on the subjective job index. Before enumerating these restrictions, a comparison of the f_N at $h=h_L$ and foF2, obtained from ALOSYN, for some selected ionograms is given.

In Table 9, Δ is defined as:

$$\Delta = 100 [foF2 - f_N(h_L)]/f_N(h_L)$$
 (3.2)

From this Table, the median Δ is between 0 and 2, i.e. foF2 exceeds $f_N(h_L)$ by 2% on average. Also about 85% of the data are such that Δ < 5. These profiles should comprise the quality subset.

TABLE 9

Comparison of Lowest Scaled N(h) Profile Point and foF2 From ALOSYN for Selected Passes

۵		CUMULATIVE PROBABILITY DISTRIBUTION OF A								
	FEBRUARY 1965	APRIL 1965	FEBRUARY 1967	APRIL 1967						
	R _Z = 12	R _Z = 12	R ₂ = 76	R _Z = 81						
-6	4	,	,	1						
-5	5	2	8	3						
-4	6	3	9	3						
- 3	7	5	10	3						
-2	11	6	16	3						
-1	18	11	21	11						
0	25	16	26	27						
1	51	37	53	61						
2	65	52	61	83						
3	76	68	73	89						
4	82	79	78	92						
5	88	88	83	96						
6	91	90	86	96						
7	93	92	87	97						
я	94	93	89	97						
9	95	96	90	100						
10	96	96	90	100						
NUMBER OF Lonograms	589	275	263	71						

The weak restrictions for defining the quality subset of ALOUETTE NH are now enumerated:

(1)
$$N_o(h_o-h_L) \le \int_{h_L}^{h_o} N(h) dh \le \frac{N_o+N_L}{2} (h_o-h_L)$$

(2)
$$N_{L-2} < N_{L-1} < N_{L}$$
; $h_{L-2} > h_{L-1} > h_{L}$

(3)
$$h_0 < 2000$$

(4)
$$h_b < h_L < 600$$

For the base of the layer, h_b , at which $N_b=0$, the following heuristic model based on experience [E.L. Hagg, private communications, 1978] has been used:

$$h_{b} = \begin{cases} 2.5 \text{ Lt} + 230 & \text{, Lt in } [0,4] \\ 30\sin(\pi \text{Lt}/8) + 210 & \text{, Lt in } [4,12] \\ 180 \exp [0.0204(\text{Lt}-12)] & \text{, Lt in } [12,24] \end{cases}$$
 (3.3)

where Lt is local time in hours, and h, is in km.

An empirical model for the height of maximum electron density of the Fl layer [25], given by

hmax
$$F1 = 165 + 0.6428 \chi$$
, (3.4)

is compared with (3.3) in Figure 10 (χ is in degrees).

The complete density profile is summarized in Figure 11. A few remarks are added:

(1) The following artifice will be convenient. For the exponential function

$$N = N_1 \exp[(h-h_1)/H]$$
 (3.5)

passing through any 2 points (N_2,h_2) and (N_1,h_1) (with N in $[N_2,N_1]$ and h in $[h_1,h_2]$),

$$H = (h_1 - h_2)/\ln(N_1/N_2) < 0$$
 (3.6)

is called effective scale height. Note that the symbols in (3.5) and (3.6) are generic; they will be specified in (2) and (3) below.

(2) In a few cases, i.e. for Alouette 2, the satellite is considerably below 1000 km. In such cases, an exponential curve is passed

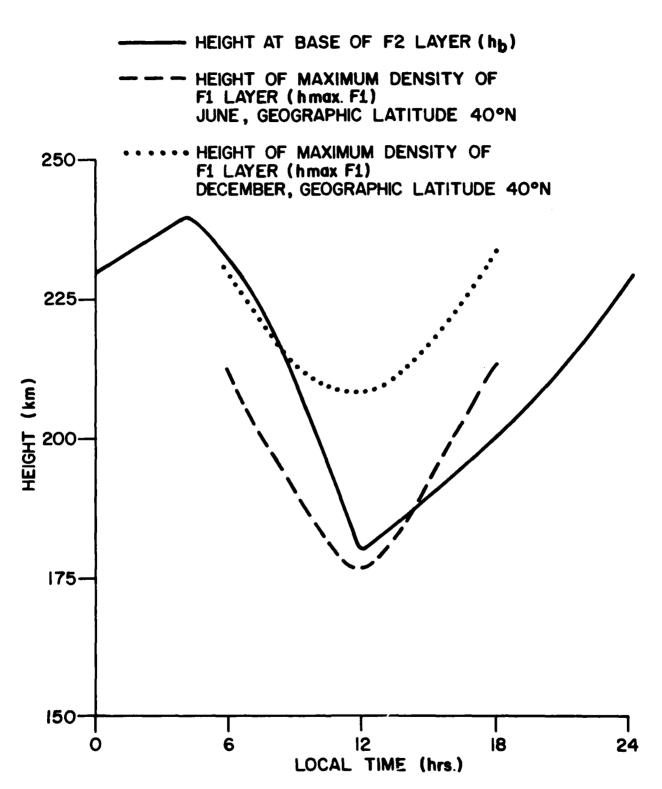


Figure 10. Height of the Base of the F2 Layer Versus Local Time

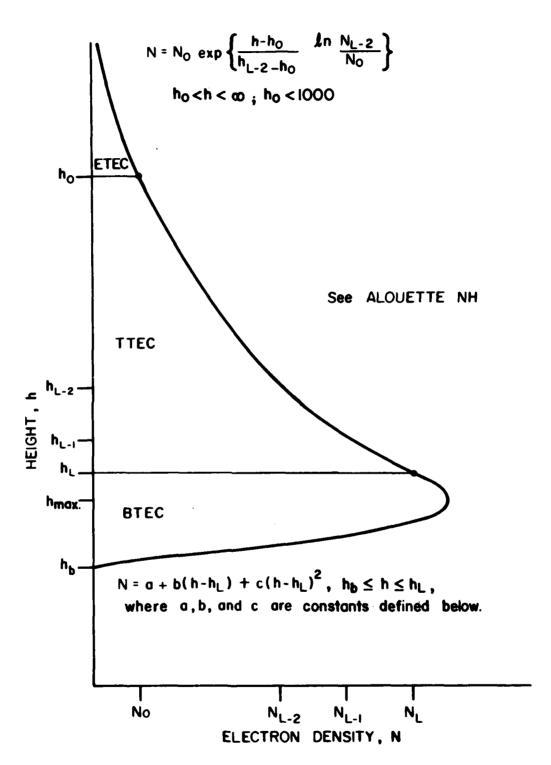


Figure 11. Summary of the Model N(h) Profile

through the points (N_0,h_0) and $N_{L-2},\ h_{L-2})$, in order to make a correction for the total electron content above the satellite. This extra area is:

ETEC =
$$\int_{h_{O}}^{\infty} N(h) dh = -N_{O}H$$
 (3.7)

(3) The constants of the parabola are chosen in order that it is continuous and has a continuous slope at (N_L, h_L) . The slope of

$$N = N_L \exp [(h-h_L)/H]$$

at $h = h_L$ is used for this purpose, where H is a scale height for the exponential on $[h_L, h_{L-1}]$. The third requirement is that $N(h_b) = 0$ where h_b is the base of the layer, as previously defined. Thus the parabola, illustrated in Figure 11, is

$$N = N_{L} \left\{ 1 + \frac{h - h_{L}}{H} - \left(1 + \frac{h_{b} - h_{L}}{H} \right) \left(\frac{h - h_{L}}{h_{b} - h_{L}} \right)^{2} \right\}$$
(3.8)

Setting N'(h) = 0, in (3.8)

hmax =
$$h_L - (b/2c)$$
 (note b, c < 0 since H < 0 and $h_b < h_L$) (3.9)

$$Nmax = a + b(hmax - h_{T}) + c(hmax - h_{T})$$
 (3.10)

Finally

BTEC =
$$\int_{h_{h}}^{h_{L}} N(h) dh$$
 (3.11)

and slab thickness is

$$Th = (ETEC + TTEC + BTEC)/Nmax (3.12)$$

3.2.3 Definition of Profile Using Ground Echoes

In this section, an alternative approach for estimating profile characteristics by adapting an idea of Dyson [7] to the present data base will now be outlined. The method essentially is an attempt to model a complete profile (topside and bottomside) using only data available from satellite soundings.

For frequencies, fx, at which ground echoes occur the group path due to ionization below $h_{\tilde{L}}$ is given by (see Figure 12)

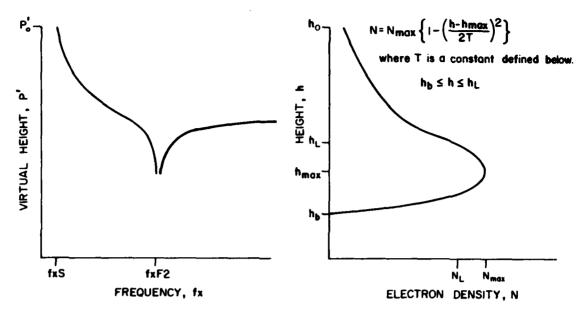


Figure 12. Ground Echoes Used for Estimation of Bottomside Total Electron Content

$$p_{m}^{\dagger} - p_{t}^{\dagger} = \int_{h_{b}}^{h_{L}} (\mu^{\dagger} - 1) dh + h_{L}, \qquad (3.13)$$

where p_m^1 is the scaled group path (virtual height or apparent range);

 p_t^{\prime} is the group path from h_0 to h_L^{\prime} ;

 μ^{\bullet} is the group refractive index; a function of fx, gyrofrequency $f_{H^{\bullet}}$ dip angle, and electron density, N.

The integral in (3.13) is transformed by

$$X = Xmax \{1 - [(h-hmax)/2T]^2\}$$
 (3.14)

where

$$X = (f_N/f_X)^2 = N/12400f_X^2$$

T = quarter thickness of the parabola to be determined.

This gives the single linear equation

$$R = T \left\{ \int_{0}^{X_{\text{max}}} \frac{(\mu' - 1) dX}{X_{\text{max}} \left(1 - \frac{X}{X_{\text{max}}}\right)^{\frac{1}{2}}} + \int_{X_{\text{L}}}^{X_{\text{max}}} \frac{(\mu' - 1) dX}{X_{\text{max}} \left(1 - \frac{X}{X_{\text{max}}}\right)^{\frac{1}{2}}} \right\}$$
(3.15)

where
$$R = p_m^1 - p_t^1 - h_L^1$$
.

The procedure adopted here, for the solution of (3.15) for T, is as follows:

- (1) A number, N_g , of pairs (p_m^{\dagger}, fx) are scaled and smoothed. Only those pairs satisfying both
 - (a) fxF2/fx < 0.85
 - (b) $p_m^{\dagger} h_0 > 60 \text{ (km)}$

are actually used in the calculation.

- (2) The fxF2 (and foF2) are obtained from the ALOSYN data base.
- (3) The integral p_t^i is computed using the original complete profiles of ALOUETTE N(h), assuming μ^i is linear in each height lamination.
- (4) The integrals on the right side of (3.15) are computed using the obvious trigonometric substitutions (to remove the singularity) followed by an application of the composite (closed) 5 point Newton-Cotes integration rule [24].
- (5) For each of the Ng pairs of scaled echoes determined in (1) above, there are a like number of linear equations:

$$R_i = TA_i$$
 $i = 1(1) Ng$ (3.16)

where R_i and A_i are respective values of R and the integrals in (3.15). Equation (3.16) is solved for T by the method of least squares

i.e. minimize
$$\sum_{i=1}^{N_g} (R_i - TA_i)^2$$

Thus the parabola (3.14) on $[h_b, h_L]$ is completely determined, so that the method of section 3.2.2 may be used to determine an alternative version of slab thickness (hmax is found by making (3.14) continuous at (N_T, h_T)).

3.2.4 Illustration

In Tables 10(a)-(d) and 11(a)-(d), slab thickness has been displayed for various sets of input conditions. These values have been computed by the procedure outlined in section 3.2.2 and then sorted into a (crude) partition of the domain of the ALOSYN model, see below. The standard error, Se, of the mean slab thickness is given by

$$Se = S/N^{\frac{1}{2}}$$
 (3.17)

where S = standard deviation of slab thickness.

N = ionogram count.

Also, the foF2 value displayed is a "check value" based on a peak electron density, Nmax, which is the ratio of the (average) TEC for the cell and the (average) slab thickness.

The data used in the preparation of these tables consisted of approximately 10,000 Alouette 1 profiles in the time period 1965-1970, or essentially half of the sunspot number cycle, Rz in [12, 112].

The domain was partitioned into 384 cells which consist of:

- (a) 2 longitude zones of 70° each, starting at 180°W
- (b) 3 geomagnetic latitude zones of 30° each, starting at 90°N
- (c) 2 magnetic activity zones, divided at Kp = 2.5 (between 2+ and 3-)
- (d) 2 sunspot number zones, divided at Rz = 40
- (e) 4 local time zones of 6 hours each, starting at midnight
- (f) 4 season zones of 3 months each, starting at January.

In Tables 10 and 11, only the results from the two most northern geomagnetic latitude zones, and for the eastern longitude zone, have been displayed — these actually contained approximately 75% of the profiles used.

TABLE 10(a)

Mean and standard deviation of slab thickness (km), ratio of bottomside TEC to topside TEC, ionogram count and foF2 (MHz) for Lattm ≥ 60° N, Kp < 2.5, Rz < 40.

Local Time Month	!0,	61	6,1	21	112	,18]	18	,24)
January to March	232 .25	77 96	208 .23	70 108 - 3	219 . 32 5.	32 211	226 . 34 2.	50 188
April to June	215 .11	35 262 6		30 435 . 3	248 . 20 4.	32 721	230 .21	33 327 0
July to September	•			-		-	-	
October to December	-		146 .09	23 4	-			

^{*} No N(h) profiles available (in this sample).

TABLE 10(b)

Mean and standard deviation of slab thickness (km), ratio of bottomside TEC to topside TEC, ionogram count and foF2 (MHz) for Lattm ≥ 60° N, Kp > 2.5, Rz < 40.

Local Time Month	[0,6]	[6,12]	[12,18]	[18,24]
January to March	-	261 40 .39 4 3.7	211 15 .51 35 7.5	241 46 .32 144 2.9
April to June	287 27 .10 6	254 53 .15 45 4.7	298 48 .29 43 4.0	276 56 .27 88 3.6
July to September	-	-	-	-
October to December	-	-	-	-

TABLE 10(c)

Mean and standard deviation of slab thickness (km), ratio of bottomside TEC to topside TEC, ionogram count and foF2 (MHz) for Lattm \geq 60° N, Kp < 2.5, Rz > 40.

Local Time Month	[0,6]		[6	i , 12]	([12,18]		ſ	18,24]	
January	237	30			323		42	235		38
to March	. 48 3.3	58		-	. 28	7.2	14	.59	4.7	29
April	250		281	36	285		27	264		26
to June	.15 4.0	127	.16	234 1.2	.28	5.4	245	.40	6.5	5
July			269	14	260		18			
to September	-		.21	33 1.8	.27	5.9	22		-	
October		<u> </u>	186	45	237		57	240		26
to December	-		. 37	11 7.7	.51	7.0	21	.46	4.4	22

TABLE 10(d)

Mean and standard deviation of slab thickness (km), ratio of bottomside TEC to topside TEC, ionogram count and foF2 (MHz) for Lattm \geq 60° N, Kp > 2.5, Rz > 40.

Local Time Month		[0,6]		([6,12]		(12,18]	!	[]	8,24]	
January to March	313	3.1	73 15		<u>-</u>		390 . 4 2	5.1	16 9	361 .48	4.1	89 12
April to June	377 .34	3.2	100 21	280 .20	3,6	43 32	314 ,29	4.6	41 95		-	
July to September	315	3.8	39 11	291 .17	4.0	27 51	305 . 29	4.9	32 16		-	
October to December		-		324	6.8	7 10	220 .59	7.9	47 16	264 .39	4.7	77 40

TABLE 11(a)

Mean and standard deviation of slab thickness (km), ratio of bottomside TEC to topside TEC, ionogram count and foF2 (MHz) for Lattm in [30° N, 60° N], Kp < 2.5, Rz < 40.

Local Time Month	[0,6]	[6,12]	[12,18]	[18,24]
January to March	218 41 .40 151 3.5	187 44 .30 452 4.8	195 26 .31 204 5.7	248 72 .43 139 2.9
April to June	225 57 .41 322 2.7	179 31 .21 388 4.8	226 35 .53 590 6.0	223 32 .64 218 4.6
July to September	-	-	-	-
October to December	-	-	141 4 .20 4 5.6	

TABLE 11(b)

Mean and standard deviation of slab thickness (km), ratio of bottomside TEC to topside TEC, ionogram count and foF2 (MHz) for Lattm in [30° N, 60° N], Kp > 2.5, Rz < 40.

Local Time Montn	[0.6]	[6,12]	- [12,18]	[18,24]
January to March	-	235 47 .29 73 4.4	199 47 .35 160 5.6	262 63 .66 55 2.9
April to June	259 51 .41 23 2.7	261 36 .28 29 4.4	243 27 .61 40 5.4	222 26 .73 61 4.0
July to September	-	-	-	-
October to December	-	-	-	-

TABLE 11(c)

Mean and standard deviation of slab thickness (km), ratio of bottomside TEC to topside TEC, ionogram count and foF2 (MHz) for Lattm in [30° N, 60° N], Kp < 2.5, Rz > 40.

Local Time Month	[0,6	1	(6	,12]	[12	,18]	[18	,24]
January to March	410 1.2	13 3		-	-		241 .66	46 15
April to June	228 .49	35 128	217 .14	6 4 3,9	248 .58 7.	24 272 4	258 .61	34 27
July to September	-		409 . 58	36 14 2.2	270 .45	26 38		-
October to December	-		201 . 44	49 22 7.7	232 .59	54 21	.68	5 5,3

TABLE 11(d)

Mean and standard deviation of slab thickness (km), ratio of bottomside TEC to topside TEC, ionogram count and foF2 (MHz) for Lattm in $[30^{\circ} \text{ N}, 60^{\circ} \text{ N}]$, Kp > 2.5, Rz > 40.

Local Time Month		[0,6	1	[6,12]	([12,18]	İ	[18	,24]
January to March	393 .73	2.8	34 12		-	231	8.9	46 19		-
April to June	298 .45	3.6	108 18		-	287	8.5	37 33		-
July to September		-		306 .40	35 27 3.6	251 .47	7.0	26 22		-
October to December				266 . 35	41 22 8.5	229	7.8	45 44	269 .72	30 41

In Table 12, the results of computing slab thickness and the height of the base of the F2 layer have been compared for the two different parabolas used (with and without ground echoes). Of the 198 determinations made (or ionograms observed), from February 1965 and 1967, a systematic selection (every 18th determination) has been displayed.

The empirical model of slab thickness, Th, displayed in COMPUTER OUT-PUT 3 is briefly described. The result of sorting the 10,000 ALOUETTE NH profiles into 384 cells yielded 132 points at which slab thickness is known:

$$(Lt_{i}, M_{i}, Lattm_{i}, Kp_{i}, Long_{i}, Rz_{i}, Th_{i}), i = 1(1)132$$

The majority of these points occurred in the two most northeast geographic zones since that was where the majority of the 10,000 profiles occurred. The 252 = (384 - 132) empty cells correspond to non-existent keyed records on the file THICK, (see also Appendix A).

These points were then fitted to a model of the form:

TABLE 12
Comparison of Slab Thickness Without Ground Echoes (Section 3.2.2) and with Ground Echoes (Section 3.2.3)

WITHOUT GR	OUND ECHOES	WITH GRO	OUND ECHOES
HEIGHT OF BASE OF LAYER, h _b (km)	SLAB THICKNESS (km)	HEIGHT OF PASE OF LAYER, hb(km)	SLAB THICKNESS (km)
199	208	1 35	252
211	239	145	281
227	188	126	252
193	190	155	210
207	350	137	400
210	318	235	246
216	360	170	391
217	265	156	306
199	174	158	203
221	198	261	170
226	168	223	129
236	260	-126	514

Th(x₁,x₂,x₃,x₄,x₅,x₆) = b₀ +
$$\frac{4}{\Sigma}$$
 b_{2j-1} $\sin^{j}x_{1}$ + b_{2j} $\cos^{j}x_{1}$
+ $\frac{2}{\Sigma}$ b_{2j+7} $\sin^{j}x_{2}$ + b_{2j+8} $\cos^{j}x_{2}$
+ $\frac{4}{\Sigma}$ b_{j+12}x₃ + $\frac{4}{\Sigma}$ b_{j+16}x₄ (3.18)
+ $\frac{2}{\Sigma}$ b_{j+20} x₅ + $\frac{2}{\Sigma}$ b_{j+22}x₆

The actual 6 independent variables used were:

$$x_1 = \pi Lt/12$$
 Lt in [0,24]
 $x_2 = \pi (2M-1)/12$ M in [.5,12.5]
(integer months denote mid-months)
 $x_3 = Lattm/90$ Lattm in [0,90]
 $x_4 = Kp/9.3$ Kp in [0,9]
 $x_5 = (Long + 180)/140$ Long in [-180°,-40°]
 $x_6 = Rz/120$ Rz in [0,150]

The statistically significant coefficients, b_j : j=0(1)24, were computed by the subroutines STEP1 and STEP2. In this case, the actual coefficients were:

$$b_0 = 166.05$$
 $b_1 = -38.462$ $b_3 = 32.407$
 $b_5 = 63.112$ $b_9 = 7.9556$ $b_{10} = -29.452$
 $b_{16} = 57.693$ $b_{17} = 100.47$ $b_{24} = 119.29$

and the root mean square error for the errors in predicted thickness was $34 \, \mathrm{km}$. As a matter of interest, all the variables except longitude appeared in the model (3.18).

The subroutine SLABTH in the main prediction program PREDSYS actually computes slab thickness for the user-specified conditions and for each hour of local time.

In conclusion, the following remarks pertaining to these illustrations are made:

- (a) More profile data is needed to cover the entire sunspot range adequately. These data exist (see ISIS 1 and 2, Table 8) where one observes that there are approximately 70,000 more profiles, in the North American sector, which may be used. These, combined with the early Alouette 1 profiles would give a fairly extensive data base of approximately 130,000 ionograms (= 50,000 + 10,000 + 70,000). While this is still only about one third of the size of the ALOSYN data base used, it would permit a finer cell division (than used in Tables 10 11) and also fill in some of the seasonal gaps observed in the latter.
- (b) Even with an extended data base, there still exists the uncertainty of determining the profile (and TEC) on the bottomside of the F2 layer, from topside data only. While it may not be feasible to use the "ground echo" approach everywhere (recall reasons in section 3.2.2), there do exist extensive bottomside synoptic data (scaled and recorded on magnetic tape) containing ionospheric

characteristics such as foF2, foF1, foE, h'F2, h'F, M(3000)F2, and M(3000)F1 for ground stations located at Resolute, Churchill, Winnipeg-Kenora, Ottawa, and St. John's, at least. (See Tapes 5E08, 4B32, and 4B33 in Appendix A). These data would certainly give at least a "representative" parabola, or combination of parabolas, for the bottomside profile, using the classical Abel equation (see [8] of Bibliography) relating scaled ionograms and electron density profiles.

4. MAIN TROUGH REFINEMENTS

4.1 DESCRIPTION OF THE PROCEDURE

Beginning with Muldrew [17], extreme troughs have been consistently observed in the spatial electron density, particularly in the sunset to sunrise period of the day and at mid and high geomagnetic latitudes. In addition, regular movements of the trough have been observed (equatorward with increasing magnetic activity and local time tending towards midnight). Tulunay and Sayers [28], using data from the Ariel III satellite launched in 1967, compiled a statistical summary of trough crossings over an 11 month period. In particular, they noted that most of the troughs were observed in the geomagnetic latitude range [50°N, 70°N]. In Pike [22], there is a set of linear equations for predicting foF2 from a "reference latitude coordinate system". These are for a very limited period of time (December 1971 ISIS 2 data). Halcrow and Nisbet [10] produced a trough model using 30,000 profiles of Alouette 1 and 2 in the time period 1962-70. The output from their model was a multiplicative factor, depending on invariant latitude, Kp, Lt, and Rz which could be applied to the Nmax (or foF2) as predicted by the C.C.I.R. model, [5]. Essentially they defined it as unity at the north and south edges of the trough and 0.25 at the centre, for Nmax.

The procedure adopted here is essentially to use the ALOSYN model to locate the trough for a given longitude, month, local time, sunspot number, and magnetic activity. The changes in foF2 between the trough edges and the centre will then be modified to agree with Halcrow and Nisbet's observations to partially account for the smoothing that has occurred due to the averaging of ionogram parameters in the cells.

More precisely, the procedure is as follows:

- (1) The ALOSYN model is used to generate an array of points (Lattm_k, foF2_k) in [45°, 75°] (geomagnetic), k = 1(1)13, for a given longitude, local time, Kp, month and Rz. The model actually gives pairs at every 5 degrees of latitude additional interpolants have been filled in using a cubic spline technique.
- (2) Locate the trough centre, M; i.e. that point $(Lattm_M, foF2_M)$ where foF2 takes its absolute minimum in $[45^\circ, 75^\circ]$.
- (3) The north and south edges, N and S respectively, are taken to be the nearest points of inflection about the centre M, i.e. (Lattm $_N$,

 $foF2_N$) and (Lattm_S, $foF2_S$) respectively. This is the reason why interpolants were generated above; recall that the trough is about 5 degrees wide (north to south). See also [10,17,19].

(4) Finally, the corrected foF2 at the centre is defined by:

$$foF2_{C(M)} = max [\frac{1}{2} min(foF2_N, foF2_S), foF2%]$$
 (4.1)

where foF2% is a 5-percentile which is also obtainable from the ALOSYN model. The 5-percentile of foF2 is taken from the distribution of foF2 at the point (lattm $_{\rm M}$, foF2 $_{\rm M}$). An example of an averaged and corrected trough is now presented.

4.2 ILLUSTRATION

In Figures 13(a)-(d), profiles of foF2 against latitude have been displayed for the indicated conditions (January - March, 1963 has an Rz of approximately 29). Unstandardized (1963) data have been used in these plots.

All the plots are for the eastern-most longitude zone $[-90^{\circ}, -45^{\circ}]$. For a given figure, the 4 profiles represent the 4 local time zones for the month. For each curve the local time can range up to 5 to 6 hours over the

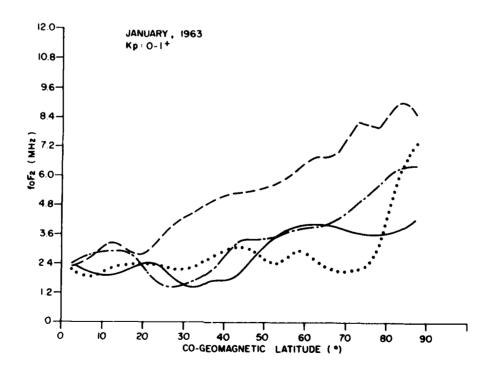


Figure 13(a). Illustration of the main trough for low sunspot number, longitude in [90°W, 45°W] and local time in Table 13, January, 1963, $K\rho < 1.5$.

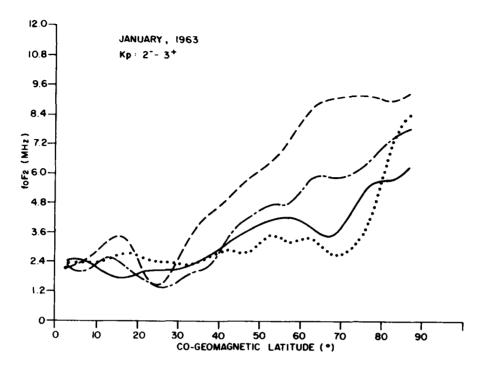


Figure 13(b). Illustration of the main trough for low sunspot number, longitude in [90°W, 45°W] and local time in Table 13, January, 1963, 1.5 < Kp < 3.5.

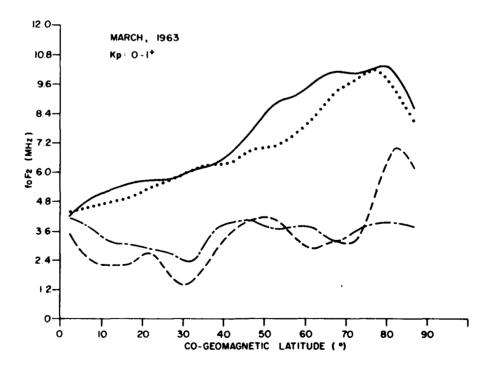


Figure 13(c). Illustration of the main trough for low sunspot number, longitude in [90°W, 45°W] and local time in Table 13, March, 1963, Kp < 1.5.

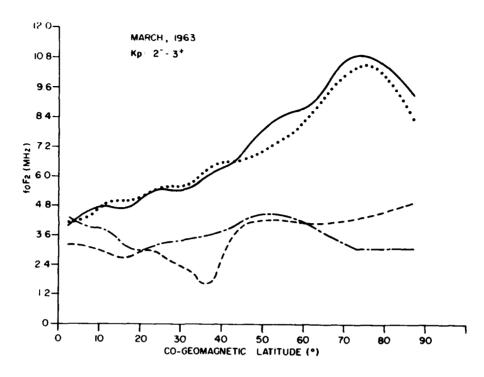


Figure 13(d). Illustration of the main trough for low sunspot number, longitude in $\{90^{\circ}W, 45^{\circ}W\}$ and local time in Table 13, March, 1963, 1.5 < Kp < 3.5.

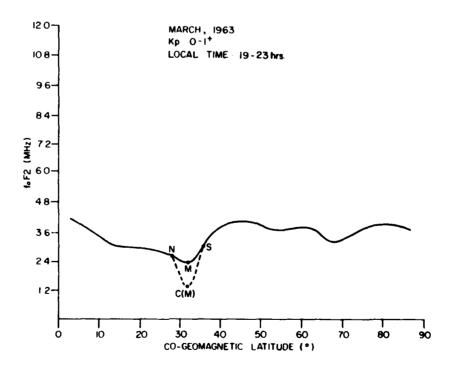


Figure 13(e). An example of the trough correction procedure for low sunspot number, longitude in [90°W, 45°W].

entire latitude range. For convenience, these local time ranges are given in Table 13. Some evidence of a trough (near a co-geomagnetic latitude of 30°) appears in all the figures except the March 1963 midday curves.

In Figure 13(e), the trough correction procedure is illustrated for the March low magnetic activity trough which appears to begin to form at about 19 to 23 hours local time. (One should observe also Figure 13(c) and note that this trough has become more accentuated at approximately 21 to 2 hours, local time. The actual step by step trough correction is now illustrated. In the neighbourhood of the trough the following interpolants have been generated:

k	Lattm	foF2	foF2%
1	75.0	3.0	
2	72.5	3.0	1.7
3	70.0	2.9	
4	67.5	2.8	1.7
5	65.0	2.7	
6 N	62.5	2.6	1.9
7	60.0	2.3	
8 M	57.5	2.3	1.1
9	55.0	2.8	
10 S	52.5	3.5	2.9
11	50.0	3.8	
12	47.5	3.9	2.4
13	45.0	3.9	

as well as a 5% - tile of foF2, from the actual cell histograms. The pairs used for the north and south edge as well as the centre have also been appropriately labelled. Thus the corrected foF2 at the centre becomes, using (4.1):

foF2 = max
$$\begin{bmatrix} \frac{1}{2} & \min(2.6, 3.5), 1.1 \end{bmatrix}$$
 = 1.3 MHz

The centre is still assumed to be located at Lattm = 57.5°N.

In conclusion, the prediction system (PREDSYS and associated XEQ file, i.e. execute file in Honeywell CP-V system, EXPREDSYS) has been set up so as to allow the user to optionally make trough corrections, by hand, using the above illustration as a guide. In other words, after one has made sets of predictions for several latitudes (at most 19), a file will exist containing grids of the characteristics (foF2, spread, and slab thickness in local time

TABLE 13

Local time code for Figures 13(a) to 13(e)

LOCAL TIME CELL INDICES	GRAPHIC SYMBOL	LOCAL TIME RANGE (Hours) (ALL LATITUDES)	
(LT1,LT2)		JANUARY	MARCH
(1,1)		[21,2]	[13,18]
(1,2)		[5,10]	[21,2]
(2,1)		[19,24]	[11,16]
(2,2)	••	[3,7]	[19,23]

and latitude). The user is then permitted to edit this file (using the EDIT processor of the Honeywell Sigma 9 computer) in order to make trough corrections, fill in "missing values" resulting from the lack of cells in ALLMON, and even correct "obvious" bad predictions. To aid in this, the user may access those cells that are available (see COMPUTER OUTPUT 4), and also access files of preliminary interpolates (see section 2.3.2), which are also produced by the prediction system at the user's option.

Upon completion of this editing task, the user may resume use of the XEQ file EXPREDSYS, to display the contour maps.

5. ACKNOWLEDGEMENT

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APPENDIX A

Glossary of Files and Tapes

In this Appendix, the files associated with each section of the report are listed (in application order) and briefly described. Each such description is prefixed by the code:

FILENAME, TYPE, ORG.

- where (1) FILENAME is the name of file
 - (2) TYPE is one of the letters X,B,F, or D corresponding to XEQ, BATCH, FORTRAN source, or data files.
 - (3) ORG is one of K3, K11, or C describing the key structure of the file. Here K3 denotes files with 3 byte (EDIT) keys, K11 with 11 byte (direct access) keys, and C for sequential files (no keys)...

Any F file is compiled on the file BFILENAME in single precision, unless the contrary is stated.

Any compiled version of an F file is loaded with LYNX and the file BMISC, unless the contrary is stated.

In some cases, for a related set of a files, two numbers denoted by XX will be suffixed to the file name and will be defined at that point.

The file, EXFILENAME, will denote an X file for the associated F file, FILENAME. The source listings of all X,B and F files are available on request. See Tape 5E47 below.

The first file is of general purpose and applies to the entire report. MISC,F,K3.

All miscellaneous, non-standard subroutines not displayed explicitly elsewhere are here. It should be compiled with the batch compile (BC) option.

Section 2.2.1

CRALOMON, X, K3.

This file controls the transfer of the original ALOSYN tapes to disk.

DXX,D,K3. XX = 62(1)68

These 7 files are built by the user in CRALOMON. Each contains 1 record with 2 integers which are used for positioning an ALOSYN tape to the month to be processed. See also IONMODELS.

PROPERTY DATE PLANTING FELLING

DMON, D, K3.

This file is built in CRALOMON and consists of 1 record with 8 integers to be used for defining the cell alignment. See also IONMODELA.

ALOMONXX, D, C. XX = 62(1)68

These 7 files each consist of the same month of ALOSYN data, for each year XX.

CXX,D,C. XX = 62(1)68

Each of these files contain 5 records with certain quality statistics concerning the respective ALOMONXX. See also IONMODELS.

IONMODELS, F, K3.

This program produces ALOMONXX and CXX, one year at a time.

DUMFILE,-,K3.

Records 9 to 28 are PCL commands used for removing and accessing ALOSYN tapes as they are processed.

CNSTRPCL, F, K3.

This is used for copying the last 3 records of ALOMONXX. The actual number of records of ALOMONXX is given by the first record of the appropriate CXX. It should be compiled with the BC option.

AXX,B,K3. XX = 62(1)68

These 7 files control the production of DUMXX, respectively. They are "batched" by CRALOMON.

BXX,B,K3. XX = 62(1)68

These 7 files control the production of MONXX, respectively. They are "batched" by CRALOMON.

Section 2.2.2

DUMXX,D,C. XX = 62(1)68

These 7 files contain the cell indices, input averages, and extreme foF2 values for the ionograms of ALOMONXX.

IONMODELA, F, K3

This produces DUMXX from ALOMONXX, one year at a time.

MONXX,D,C. XX = 62(1)68

These 7 files are the respective DUMXX updated with the histograms of foF2 and $spread\ F$.

IONMODELB, F, K3.

This produces MONXX given an ALOMONXX and a DUMXX.

REDUALO, F, K3.

The orbital position parameters of the satellite are corrected on ALOMONXX using this program. (see February, 1965).

IONGACC, F, K3.

Individual ionograms from user specified cells are accessed from ALOMONXX.

SATTRACK, F, K3.

This creates a file of orbital position parameters of the satellite, for a given time interval. These data are used in the construction of Figure 4. See also EXSATTRACK.

Section 2.2.3

MERMON, X, K3.

This controls the merging and blocking of the MONXX files, as well as the production of ALLMON.

DUMFILE,-,K3.

Records 2 to 8 contain merging and blocking specification parameters required by the system MERGE processor. Record 1 contains two integers which are required as input for IONMODELC.

MON, D, C

The merged version of all the MONXX files.

MONB96,D,C.

The blocked version of MON. Nyear years for a given cell are blocked together on a record (in increasing year order). Each record has 96*Nyear bytes. All empty cells are included, in order to facilitate the accession of user-specified cells. These files, all months, have been stored on magnetic tape. See tape listing below.

ZR6278,D,K3.

This consists of 34 records; the odd records are the monthly Zurich sunspot numbers for each year of 1962-78, while the even records are the smoothed monthly Zurich sunspot numbers.

YEAR, D, K3.

This contains one record with two integers specifying the month and the number of years to be processed by IONMODELC. See also record 1 of DUMFILE.

IONMODELC, F, K3.

This standardizes the records of MONB96 to the average sunspot number of the cell.

MONSTD, D, K11.

A keyed file corresponding to the standardized month represented by MONB96 and produced by IONMODELC. Only those cells to be used in interpolation are kept.

ALLMON, D, K11.

The concatenated version of MONSTD for all months. The maximum allowable key is $FFFFFF_{16}$ or $16,777,215_{10}$. The actual maximum, for the cell arrangement described in this report is 10,368,000 (= $12 \times 864 \times 1000$). Keys less than 10,000,000 can be directly displayed using the EDIT processor (system). Otherwise the system processor, KFM (see Communications Research Centre User's (COMUS) Manual 5-2.13) must be invoked. Note that the keys as defined in FORTRAN are in the range $\{1,10368\}$.

KEYKFM, F, K3.

This is used for accessing keys of ALLMON which are not compatible to EDIT. See also EXKEYKFM.

ACCMONB96, F, K3.

This is used for accessing cells from the unstandardized months, MONB96, upon specification of the cell indices. Statistics of the characteristics are also computed.

CELLCOUNT, F, K3.

This is for examining the quality of the cells of MONB96, as in Table 5.

CELLKEY, F, K3.

This is used for the construction of Table 6.

CHRZGRAD, F, K3.

This is applied to MONSTD in order to smooth foF2-Rz gradients. (See also Figures 6(a) and 6(b)).

Section 2.3

PREDSYS, F, K3.

This is the prediction program which uses keyed records of ALLMON to interpolate and predict ionospheric characteristics. It should be compiled with the BC option, as it contains the subroutines REGRESS, SLABTH, and DIVTEST. Also, to load, LYNX with BSSTEP1 and BSSTEP2.

REGRESS, F, K3.

This is used to prepare the arrays for the subroutines STEP1 and STEP2.

SLABTH, F, K3.

Slab thickness is computed for the user's input conditions, using the model illustrated in equation (3.18).

DIVTEST, F, K3.

Any positive integer is tested for divisibility by a given integer. This facilitates the accession of the 6 half months of data with 2 periods of local time each which are used in the model (2.13).

PRDATA, D, K3.

Each record contains a set of input conditions for making predictions at a given longitude, latitude, sunspot number, month, and magnetic activity. See also tape RO33 for an example.

ADJRZ,D,C.

Preliminary interpolants (characteristics adjusted to the user's sunspot number) are displayed.

ADJKP,D,C.

The (at most) 12 triples of month and local time data are displayed.

REGFIT.D.C.

The details of the stepwise regression procedure for the model (2.13) are displayed.

SSTEP1 and SSTEP2,F,K3

These contain the subroutines STEP1 and STEP2 which perform the stepwise regression for fitting a characteristic as a function of local time and month.

NEWPLOT, F, K3

Contour maps of characteristics in local time and latitude are prepared. Compile with the BC option to include the subroutine CPLOTOPT.

CPLOTOPT, F, K3.

A modified version of the MLIB's contour plotting routine.

NEWPLOT1, D, C.

This contains the contour grids produced by PREDSYS. They may be (optionally) edited, using EDIT, before being input to NEWPLOT.

EXPREDSYS, X, K3.

This controls the entire procedure described in section 2.3.

Section 3.2.1

NHA, D, C.

A file consisting of original N(h) profiles in A Format (see Table 8).

NHB,D,C.

A file consisting of original N(h) profiles in B Format (see Table 8).

NHAMES, D, C.

A file consisting of original N(h) profiles in Ames Format (see Table 8).

KPFILE, D, C.

A file such that a record consists of the 8 3-hourly Kp indices together with the associated year and day.

NHXX,D,C.

A file consisting of reduced profiles in the format of ALOUETTE NH. XX are two integers denoting the satellite number in [1,2] and the volume number in [1,9] (see Table 8).

REDNHA, F, K3.

This produces a particular NHXX from a file NHA.

REDNHB, F, K3.

This produces a particular NHXX from a file NHB.

AMESPR, F, K3.

This produces a particular NHXX from a file NHAMES. It should be compiled with the "Batch Compile" (BC option) as it includes the subroutine FIELDAL.

NHCSB, D, C.

This consists of all the NHXX; concatenated, sorted (by universal time) and blocked (at the rate of 10 profiles per record). An extra byte (garbage) has been added to each profile to facilitate further buffering. The actual procedure is listed here in the execute file EXNHCSB.

EXNHCSB

!PCL DUMMY1

!SET F:SORTOUT/NHCSB;OUT

!SET F:SORTIN/NHC;IN

!SET M:SI/DUMMY2; IN

! SORT

where DUMMY1 consists of:

C NHXX,NHXX,...,NHXX INTO NHC

END

and DUMMY2 consists of:

.REC(103,104)

.KEYS(9,15)

.BLOCK(1, 10, DROP)

Section 3.2.2

THICKEX, F, K3.

Profiles from ALOUETTE NH are buffered in and a slab thickness is defined for each. These results are then sorted into cells, with an alignment specified by the user, and displayed in the form of a direct access file.

THICK, D, K11

The output of THICKEX.

THICKPR, F, K3.

THICK is read in a sequential fashion, and a model as in (3.18) is constructed. LYNX with BSSTEP1 and BSSTEP2.

Section 3.2.3

NHCS,D,C.

A selection of (unblocked) 103 byte profiles of ALOUETTE NH.

ALO,D,C.

A portion of a file ALOMONXX which contains the ionograms listed in NHCS.

ALOSNHMAT, F, K3.

A program which extends the records of NHCS (to 132 bytes) by attaching the foF2 and related parameters of ALOSYN. Table 9 was also produced by this program.

NHFOF2.D.C.

This is the output file produced by ALOSNHMAT.

GRECHO.D.C.

A file consisting of the output on unit 108 of RANDRUN.284201E (updated May 3, 1974 [J.H. Whitteker, private communications, 1978]. The card input (units 105 and 306) essentially consist of the scaled ground echoes (X wave) of the ionograms in NHFOF2. The Number density contour plots on unit 108 are not included.

GRECHOM, D, C.

A data file consisting of m(n+1) records where m is the number of ionograms of NHFOF2 scaled for ground echoes and n is the number of pairs of echoes actually scaled for each ionogram. The extra record is an identification record (header) for each ionogram.

CGRECHO.F.K3.

The program which produces GRECHOM from the files NHFOF2 and GRECHO.

EAREC, F, K3.

The complete profiles, corresponding to those of NHCS, are input from NHA and NHB together with the file GRECHOM to compute a slab thickness. It should be compiled with the BC option (all non-standard subroutines are included). FIELDG of ORBIT.284201C and SOLVLE of .MLIB are required if a double precision version is desired. The input files GRECHOM, NHB, and NHA used for Table 12 are listed on tape 6E19, see below.

Section 4

TROCRT.F.K3.

A profile of a characteristic against latitude is created (as a smooth curve, using the subroutine CUBSPL, which is included) from a grid of the

characteristic, in the format of Table 6. Thus TROCRT should be compiled with the BC option. CUBSPL also uses SOLVLE which may be found in the source file SSOLVLE, for single precision use.

SSOLVLE, F, K3

A single precision version of the program SOLVLE, (in the library programs .MLIB of the Honeywell Sigma 9 computer) for solving a system of linear algebraic equations.

The actual tape serial numbers used in this report are now listed. Unless the contrary is stated these tapes are all 9 track, 800 bytes per inch, and free tapes. For labelled tapes, the serial number is the "internal" serial number, i.e. that written on the tape.

1. ALOSYN TAPES

(a)	6C47	September	_	December, 1962
(b)	6G03	January	-	April, 1963
(c)	4G48	May	-	December, 1963
(d)	4G49	January	-	December, 1964
(e)	4E26	January	-	December, 1965
(f)	1G47	January	-	December, 1966
(g)	1G48	January	-	December, 1967
(h)	1G49	January	-	December, 1968
(i)	3B02 or 6E21	MONB96, fo	r a	11 months.

2. ALOUETTE N(h) TAPES

(a)	R541	Alouette 1,	Volume	1		
(b)	R648	Alouette 1,	Volume	2		
(c)	RO 34	Alouette 1,	Volume	3		
(d)	R535	Alouette 1,	Volume	4		
(e)	R568	Alouette 1,	Volume	5		
(f)	R571	Alouette 1,	Volume	6		
(g)	R033	Alouette 1,	Volume	7, See	3(c),	EXNHAL1.

(h)	RO 37	Alouette 2, Volume 1
(i)	R752	Alouette 2, Volume 2
(j)	R582	Alouette 2, Volume 3
(k)	R740	Alouette 2, Volume 4
(1)	R570	Alouette 2, Volume 5
(m)	R022	Alouette 2, Ames 1
(n)	R720	Alouette 2, Ames 2
(o)	R739	Alouette 2, Ames 3
(p)	R749	Alouette 2, Ames 4
(p)	5E46 or 3E30	ALOUETTE NH (or NHCSB)
(r)	6E19	GRECHOM, (2427 records)
		NHB , (1201 records)
		NHA , (501 records)
V7.0.0	TELL ANDOLIG MADEG	
MISC	CELLANEOUS TAPES	
	CELLANEOUS TAPES 3B04	Kp , January 1962 - December 1970.
(a)		Kp , January 1962 - December 1970. Labelled tape (account 284201R,GLADWIN) This contains all the files which are available on request.
(a)	3804	Labelled tape (account 284201R, GLADWIN) This contains all the files which are available
(a) (b)	3B04 5E47	Labelled tape (account 284201R,GLADWIN) This contains all the files which are available on request. Labelled tape (account 284201R,GLADWIN) This contains the data files ALLMON, CONTOUR, EXNHAL1, FOJAN63,
(a) (b) (c)	3B04 5E47 R033	Labelled tape (account 284201R,GLADWIN) This contains all the files which are available on request. Labelled tape (account 284201R,GLADWIN) This contains the data files ALLMON, CONTOUR, EXNHAL1, FOJAN63, FOFEB63, FOMAR63, PRDATA, THICK, ZR6278.
(a) (b) (c)	3B04 5E47 R033	Labelled tape (account 284201R,GLADWIN) This contains all the files which are available on request. Labelled tape (account 284201R,GLADWIN) This contains the data files ALLMON, CONTOUR, EXNHAL1, FOJAN63, FOFEB63, FOMAR63, PRDATA, THICK, ZR6278. Bottomside synoptics: January, 1969 - December, 1971
(a) (b) (c) (d) (e)	3B04 5E47 R033 5E08 4B32	Labelled tape (account 284201R,GLADWIN) This contains all the files which are available on request. Labelled tape (account 284201R,GLADWIN) This contains the data files ALLMON, CONTOUR, EXNHAL1, FOJAN63, FOFEB63, FOMAR63, PRDATA, THICK, ZR6278. Bottomside synoptics: January, 1969 - December, 1971 Bottomside synoptics: January, 1972 - February, 1973
(a) (b) (c) (d) (e) (f)	3B04 5E47 R033 5E08 4B32 4B33	Labelled tape (account 284201R, GLADWIN) This contains all the files which are available on request. Labelled tape (account 284201R, GLADWIN) This contains the data files ALLMON, CONTOUR, EXNHAL1, FOJAN63, FOFEB63, FOMAR63, PRDATA, THICK, ZR6278. Bottomside synoptics: January, 1969 - December, 1971 Bottomside synoptics: January, 1972 - February, 1973 Bottomside synoptics: January, 1973 - December, 1973

Alouette 2 (103 byte) Profiles; NHCS

3.

(1) R565

APPENDIX B

List of Notations

- 1. Individual numbers are labelled by small English letters, possibly subscripted in the case of a serially related set of numbers.
- 2. File names (FORTRAN programs or data files) are labelled with capital letters.
- 3. The following notations are also used for denoting sets of numbers or files.
 - (a) A = [a,b]: The set of numbers lying between a and b including the end points, with the additional convention that a round bracket denotes exclusion of the end point, (a < b).
 - (b) $A = \{a,b,c,...\}$: The set of numbers consisting of a, b, c
 - (c) If the elements of A are serially related the following is used:

$$A = \{x_i : i = m(r)n\} = \{x_m, x_{m+r}, x_{m+2r}, \dots, x_n\}$$

- (d) The following are for combination of sets:
 - $A \cup B$: The set consisting of the elements in the set A or the set B.
 - A/B: The set consisting of the elements in the set A and the set B.
 - AxB: The set of all combinations (pairs) of elements; the first from set A and the second from set B.
 - A-B: The set of elements in the set A but not in B.
- 4. Chapters, sections, and subsections are ordered lexicographically by a triple of integers. Equations are numbered consecutively within a given chapter, by a pair of numbers.

F







SUPPLEMENTARY

INFORMATION

NOTES, ADDENDA, AFTERTHOUGHTS

on CRC Report No. 1337

C.J. Gladwin

January 27 1981



- 1. Page 7: There "may be" more data for October, 1964. Note in Table 2
 that the number of blocked records for this month is considerably
 less than October 1963 and October 1965. See also a tape among
 the original ALOSYN tapes "missing data for October 1964".

 However, this may already have been included in the main 1964
 ALOSYN tape. In any case to do a given month, one would apply the
 XEQ and BATCH control files CRALOMON, AXX, BXX, MERMON to an
 appropriate set of ALOSYN records, ALOOCT64. (i.e. AXX = A64, BXX
 = B64, ALOMONXX = ALOOCT64)
- 2. Page 16: The "format" of MONB96 = SEPB96 (See also tape 3B02, for example) does not appear exactly as in COMPUTER OUTPUT 1.
 Actually, every 7 lines (years) are written as a blocked record with 7 x 96 = 672 bytes. (The order and spacing of the various numbers, within a line, is preserved though).
- 3. Page 24: The (median) foF2 can be calculated in two "equivalent" ways, given the assumptions for the distribution. (See also Figure 7).

(a) As in equation (2.10), Page 24.

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Distribution Unlimited

(b) The median of the standardized foF2 distribution can be found and then that number can be adjusted to the user's sunspot number

5 - 5 - 9 0 1 9

Method (a) has been used in the main predictions program. To implement method (b), the following adjustment would have to be made (in PREDSYS):

- (i) Delete line 161, "FOF2 = A#USS+B"
- (ii) Insert lines 161, 161.1

CALL XFRACT(SFDISTR, 10, NGRAND, SMA, BIG, .5, FOF2)

FOF2 = FOF2+A*(USS-SSAV)

The "advantage" of this second approach is that the median and percentiles of foF2 will more likely be correctly ordered:

i.e. $foF2_{\alpha_1} < foF2_{\alpha_2}$ for any $0 < \alpha_1 < \alpha_2 < 1$ where $foF2_{\alpha_1}$ is a particular percentile or median.

These characteristics, however, will still not necessarily be correctly ordered with 100% certainty, since separate (independent) models of the form (2.13) are fitted to each characteristic.

The "disadvantage" of this second approach is that one is masking cases where the assumptions of Figure 7 are not too good.

4. Page 26: In (2.12),

- 5. Page 51: Delete degrees ("o") in x5 below.
- 6. Page 57: Some additional hints on editting the output of PREDSYS, namely NEWPLOT1.
 - (a) Examine the desired portions of ADJRZ to see if the order of Lagrange interpolations of foF2 with Kp, for example, agrees with the appropriate (divided) differences.

e.g. Long = 70°W, Lattm = 57°N, Lt = 2200 hrs

January, Rz = 30 (See also COMPUTER OUTPUT 4)

Кр	foF2 = aRz + b	△foF2/4Kp
0.52	1.87	0.13
2.47	2.12	-0.17
4.32	1.80	

The fourth Kp cell only had 1 year of data (See also COMPUTER OUTPUT 4), so no coefficients a or b were available. Thus, Lagrange interpolation of order 2 (i.e. a parabola) was used. In this case second differences "appear constant" as they should.

LINE .

(b) The user may wish to ignore cells of ALLMON which yield large sunspot slopes, "a". (There are 126 cells with a > 0.1, see also remarks on page 17).

Also he could agree to redefine any "a" larger than 0.1, for example, as 0.1. This latter approach is probably much more dangerous since the large "a" may only be the result of computing with 2 years' data at essentially the same sunspot number.

Appropriate restrictions may be inserted in PREDSYS between lines 156 and 157.

(c) No attempt was made in the program, PREDSYS, to mask predictions which yield negative values, (for instance foF2 percentiles for low sunspot numbers, or troughs). It is left to the user's "intuition" to replace such values.

(For example, one could simply use "the smallest positive value at the nearest local time".)

7. Page 74-75: The only tape serial numbers, with any real meaning to the system, are the numbers of the 2 labelled tapes.