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are intractable. These num	erical treatments are us	sed to assess the manner in					
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FOREWORD

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TABLE OF CONTENTS

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25 Lingener maleria 36 24

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	Page Number
For	ewordl
List	of Figures •••••••••••
I.	Ballistics of Transversely Impacted 9 Fibers
	Introduction 9
	Longitudinal Wave Propagation 11
	Transverse Impact of Fibers \ldots 15
	Use of Rate-Independent Theory in Preliminary Design
	Selection of a Failure Criterion 25
II.	Numerical Analysis of Impact on Woven Panels
	Method of Analysis 31
	Mathematical Formulation 32
	Solution Stability, Convergence, and Accuracy
	Parametric Materials Study 47
III.	Effect of Viscoelastic Materials Response
	Viscoelastic Constitutive Relations 62
	Results for Single Fibers 65
	Results for Woven Panels
	Nonlinear Viscoelastic Response 75

TABLE OF CONTENTS (continued)

Page Number

CHERRY &

IV.	Numeria in Two	cal Cro	Ana sse	lys d f	is ibe	of ers	E V	lav	/e	Pr	oţ	pag	jat	ic	n		
	Introdu	ıcti	.on	•••	•	•	•	•	•	•	•	•	•	•	•	•	52
	Method	of	Sol	uti	on	•	•	•	•	•	•	•	•	•	•	•	83
	Result	s ar	nd D	isc	us	sic	on	•	•	•	•	•	•	•	٠	•	97
Concl	lusions	•	••	٠	•	•	٠	٠	•	•	•	•	•	•	•	•	106
Refe	erence	s.	• •	• •	•	•	•	•	•	٠	•	٠	• •	•	•	•	109
Append	lix A – I	'he F	ABRI	C Co	ode	•	•	• •	•	•	•	•	• •	•	•	•	111
Annend	lix B – I	he X	OVER	. Co	de	•	•		•	٠	•	•	• •	•	٠	•	136

LIST OF FIGURES

Figure Number

- 1 Wave Propagation in a transversely impacted fiber.
- 2 Predicted impact strain for linear rate-independent fibers.
- 3 Predicted impact tension for linear rateindependent fibers.
- 4 Effect of fiber stiffness on ballistic response; 10 = 10 g/den for tension, 10% for strain, 0.03 g/den for strain energy, and 900 gm/den sec for energy absorption rate.
- 5 Prediction of optimum stiffness for nylon fibers.
- 6 Variation of breaking tenacity with loading rate Zhurkov model.
- 7 Variation in transverse critical velocity due to fracture rate effects.
- 8 Idealization of impacted fabric panel as an assemblage of pin-jointed tension members.
- 9 Free-body diagram of forces acting at a fabric crossover point, showing the influence of the four fiber elements meeting there and the elastic resistive force provided by the fabric backing.
- 10 Propagation scheme for the iterative wave propagation algorithm.
- 11 Stability of the numerical scheme as indicated by a minimum in the discrepancy between energy lost by the projectile and energy absorbed by the fabric. These data were obtained from a simulation of a 400 m/sec impact on Kevlar 29 fabric at times after impact as shown, and for various values of the stability ratio α defined by Equation 36.

- 12 Illustration that the numerical scheme converges to accurate values with time, as indicated by the energy discrepancy ratio. Note that nonoptimum values of the stability ratio (**n** in this figure) lead to divergence at longer times.
- 13 Illustration that the numerical scheme predicts values of final projectile velocity after penetration in agreement with experimental observation.
- 14 Computed and experimentally observed values of cone deformation cone size at time of projectile penetration. The V_{50} is that value of impact velocity at which penetration occurs nearly instantaneously.
- 15 Distribution of strain along orthogonal fibers passing through the impact point. Curves are drawn for various fabric types, at various times after a 400 m/sec impact.
- 16 Effect of initial projectile velocity on the development of strain at the point of impact for nylon fabric.
- 17 Relative ability of the various fabric types to slow the projectile during impact. Ordinal values represent the ratio of current to initial projectile velocity.

- 18 Energy absorbed by a Kevlar 29 panel after a 400 m/sec impact, illustrating the partition of impact energy into kinetic and strain energy in the panel.
- 19 Illustration of the relative ability of the four fabric types to absorb impact energy. The curves are terminated at the right by projectile penetration, as indicated by a maximum-breaking strain failure criterion.
- 20 Development of strain at the point of impact in the various fabric types after a 400 m/sec impact.

21 "Master" curve for impact-induced strain at the point of impact. Ordinal values represent strain normalized on the basis of the strain which would be generated in a single fiber by impact at the same velocity, while abscissal values are adjusted by a factor equal to the fourth root of the fiber modulus.

如此是一些人的。如此是一些人的问题的任何的,这些人的问题的是一些的。 第二章

- 22 Wiechert spring-dashpot model for linear viscoelastic fiber response.
- 23 Normalized strain plotted against Lagrangian fiber coordinate for various times after impact.
- 24 Normalized tension distribution along fiber.

- 25 Numerical values for tension distribution for t = 41.08 microsec after impact.
- 26 Stress distributions along orthogonal fibers running through impact point for linear elastic and viscoelastic fabrics (t = 30.4 microsec).
- 27 Distribution of strain along orthogonal fibers running through impact point.
- 28 Stress histories at impact point for linear elastic and viscoelastic materials.
- 29 Stress relaxation at impact point for various impact velocities.
- 30 Stress distributions along orthogonal fibers running through impact point for linear elastic and nonlinear viscoelastic fabrics.
- 31 Comparison of stress relaxation in linear and nonlinear viscoelastic fabrics.
- 32 Stress histories at impact point for linear elastic, linear viscoelastic, and nonlinear viscoelastic fabrics.
- 33 Schematic of model for numerical analysis of two crossed fibers.

34 Discrete element of fiber.

35 Strain distributions in two crossed fibers of Kevlar 29, 28.7 microsec after impact at 400 m/sec.

- 36 Influence of the fiber modulus on the fraction of stress wave intensity which is transmitted through a fiber crossover, in the absence of fiber-fiber sliding.
- 37 A comparison of the reflection-only bounce model for wave propagation in an impacted fabric, in comparison with the fabric model of this report.
- 38 The influence of fiber-fiber sliding on the fraction of stress wave intensity which is reflected at fiber crossovers, as indicated by computer experiments on Kevlar 29 fibers.
- 39 The influence of fiber-fiber sliding on the extent to which a portion of the propagating stress wave is diverted from the primary fiber to begin propagating along the transverse secondary fiber.
- 40. The influence of sliding on the extent of stress wave intensity propagated beyond fiber crossovers.

PENETRATION MECHANICS OF TEXTILE STRUCTURES I. BALLISTICS OF TRANSVERSELY IMPACTED FIBERS*

Introduction

Although impact of single fibers or fiber assemblies is an important subject in its own right, being relevant to climbing ropes, aircraft carrier arrest cables, high-speed weaving, etc., the principal developments in this area have been made by workers whose major interests have been in the impact resistance of woven or non-woven textile structures. The most notable of these structures have been the lightweight armor vests used by police and military personnel, but among other important applications can be listed aircraft engine containment shrouds, flak blankets, and vehicle seat Ballistic nylon has been used successfully for belts. these vests since the Second World War, although current developments have emphasized the du Pont aramid fiber marketed as Kevlar**. Although, as will be shown below, excellent single-fiber ballistic response does not necessarily guarantee a superior vest, any understanding of textile structure ballistics must be pre-* From Reference 1 (see Page 109). Used by permission of Textile Research Journal

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ceeded by an understanding of single-fiber response.

A strong motive for discussing fibers is that single fiber tests are often used as screening tests for ballistic protection materials. As an example, one often encounters tabulations of "transverse critical velocity", that ballistic velocity at which a transversely impacted yarn experiences nearly instantaneous failure. Typical data is shown below.

Transverse critical velocities of textile fibers.^{[2]*}

	V _{cr} , m/sec
Nylon	616
Polyester	472
Nomex	442
Fiberglass	274
Kevlar 29	570

Such tests are often indicative of relative ballistic resistance, but perfect correlations cannot be guaranteed. In the above tabulation Kevlar 29 proves to be the best ballistic material when put into a panel, in spite of its having a lower transverse critical

* Numbers in brackets refer to references listed on pages 109-110.

velocity than nylon.

Longitudinal Wave Propagation

Wave propagation phenomena in fibers and thin rods are considerably less complicated than in a general medium, since the possibility of unrestrained transverse contraction in fibers eliminates (to a good approximation) the simultaneous propagation of independent dilatational and distortional waves which are present in general. The equation of motion for fibers or rods is simply [3]:

$$\frac{\partial^2 u}{\partial t^2} = \frac{E}{\rho} \frac{\partial^2 u}{\partial y^2} \tag{1}$$

where u is the longitudinal particle displacement, ρ is the material density, E is the longitudinal Young's modulus, and x and t are the space and time coordinates. This is the well-known wave equation, whose solution represents a disturbance traveling at a velocity

$$C = \sqrt{E/\rho}$$
 (2)

Conventional textile units employing stiffness per unit linear density are very convenient in wave propagation analyses, since the factor ρ is included implicitly in the modulus. For modulus expressed in grams per denier and wavespeed in meters per second, Equation 3 becomes:

$$c = \sqrt{kE}$$
 (3)

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where k = 88,260 is the necessary units-conversion factor. In these equations, as well as those to follow, the modulus is taken to be the "dynamic" stiffness relevant to the high strain rates corresponding to wave propagation tests. The development of such dynamic constitutive relations from experimental fiber-impact data has been described elsewhere [4,5].

Consider a fiber fixed at one end whose free end is suddenly subjected to a constant outward velocity V in the longitudinal (fiber) direction. After a time it, the strain wave, will have propagated into the fiber a distance ct, while the free end will have displaced outward an amount Vt. The strain resulting from the impact is then the displacement Vt divided by the

affected length ct:

$$\epsilon = \frac{Vt}{ct} = \frac{V}{c} = \frac{V}{\sqrt{kE}}$$
(4)

The corresponding stress is

$$\sigma = E \epsilon = V \sqrt{E/k}$$
 (5)

The above relations have assumed a linear elastic material whose stiffness E is independent of the strain. In this case the wavefront will propagate as a sharp discontinuity (a shock wave) at which the strain rises instantaneously from zero to the value given by Equation 4. Many ballistic fibers are nonlinear, however, and the effect of material nonlinearity leads to some complication of the above description. A nonlinear fiber can be characterized as having a strain-dependent modulus $E = E(\boldsymbol{\epsilon})$, so that Equation 3 becomes:

$$c = c(e) = \sqrt{kE(e)}$$
 (6)

The shape of the wavefront is now dependent on the shape of the dynamic stress-strain curve. If the curve is concave toward the strain axis, so that the modulus decreases monotonically with strain, each suceeding increment of strain in the propagating wave travels more slowly than the previous increment. The wave is then dispersive, and broadens as it travels. If on the other hand portions of the stress-strain curve are away from the strain axis, then portions of the strain wave will overtake more slowly propagating increments of lesser strain, and the wave will contain shock components. In general, a wave may contain both dispersive and shock components.

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In the region behind the wave, material flows in the direction of the imposed velocity with a "particle velocity" w. This motion is fed by the strain developed in the propagating wave, and the particle velocity is related to the wave to the wave speed by:

7

$$w = \int c(e) de = \int \sqrt{kE(e)} de$$
(7)

where ϵ_0 is the ultimate value of strain generated by the impact. Since the particle velocity must match the imposed velocity, we have

$$V = \int_{0}^{6} \sqrt{kE(\epsilon)} d\epsilon \qquad (8)$$

The strain ϵ_0 developed by longitudinal impact is found by solving Equation 8, perhaps numerically.

Transverse Impact of Fibers

As the transverse impact of fibers seems intuitively germane to impact of woven textile panels, the technical community interested in lightweight ballistic protection has devoted intensive effort to this problem since World War II. Following the pioneering works of Taylor [6] and von Karman [7] during the war, valuable contributions have been made by Peterson et al. [8], Shultz et al. [9], Wilde et al. [5], among others, but by far the most prolific of these efforts has been that of Jack C. Smith and his colleages at the National Bureau of Standards. Reference [10] provides a review of most of this work, which contains a wealth of

experimental and theoretical contributions ranging over a period of approximately ten years in the fifties and sixties.



Figure 1. Wave Propagation in a transversely impacted fiber.

The rate-independent theory of transverse fiber impact as developed by Smith can be stated with reference to Figure 1. This illustrates a fiber, originally straight in the horizontal direction, which has been impacted by a projectile traveling vertically upward. Upon impact, longitudinal waves of the type described in the previous section are propagated outward from the point of impact. Behind these waves material flows inward toward the point of impact at a constant velocity w, strain $\boldsymbol{\epsilon}_0$, and stress $\boldsymbol{\sigma}_0$. In addition to the longitudinal waves, transverse "kink" waves are also propagated outward from the impact point. At the transverse wavefront the inward material flow ceases abruptly and is replaced by a transverse particle velocity equal in magnitude and direction to that of the projectile. The strain and tension are unchanged across the transverse wavefront, but both the longitudinal and transverse particle velocities experience discontinuities there; in this sense the transverse wave is a geometrical shock. The apprently unbalanced tensions on either side of the transverse wavefront are compensated by the change in particle momentum as the wave propagates. Behind the transverse wavefront all particle velocities are equal in magnitude and direction to the projectile velocity, and the fiber configuration is a straight line at a constant inclination θ from the longitudinal direction. The inward particle velocity is found, as in the longitudinal case, as

$$w = \int_{0}^{\varepsilon} c(\varepsilon) d\varepsilon = \int_{0}^{\varepsilon} \sqrt{kE(\varepsilon)} d\varepsilon$$
 (9)

The final strain ϵ_0 is unknown as yet, but $E(\epsilon)$ is known as the slope of the dynamic stress-strain

curve. The outward velocity U of the transverse kink wave, measured relative to a Lagrangian frame attached to and extending with the fiber, is:

$$U = \sqrt{\sigma_s k / (1 + \epsilon_s)}$$
(10)

To a fixed observer the transverse wave appears to propagate in a "laboratory" frame of reference at

$$\overline{(]} = (1+\epsilon_0)(1-n)$$
(11)

Finally, the above variables are related to the impact velocity V through the relation:

$$V = \sqrt{(1+\epsilon_0)^2 (\underline{J}^2 - \underline{J}^2)}$$
(12)

Equations 9-12 constitute four relations between, V, w, ϵ_0 , σ_0 , U, and \overline{U} . The material dynamic stressstrain curve relates σ_0 and ϵ_0 , so that once one of the parameters (say V) is specified, the other four independent parameters (w, ϵ_0 , U, \overline{U}) can be found. For nonlinear stress-strain curves, numerical solutions will likely be more convenient.

Certain limitations to the Smith analysis described above must be mentioned. First, it is

rate-independent. Most polymeric fibers exhibit strong rate dependencies, and these effects are beyond the capacity of this analysis to describe. Perhaps a more severe limitation is that the Smith analysis is not applicable to late-time effects in the wave propagation process. In real situations the outgoing longitudinal wave soon collides with an obstacle: a clamp, in the case of single-fiber tests, or a fiber crossover, in the case of impact in woven textile panels. Upon such a collision a reflected wave is propagated from the collision point in the direction opposite that of the original wave. This reflected wave in turn soon collides with the outward-traveling transverse wave, and this collision generates another two waves which travel away from the collision point. These waves in turn eventually collide with the clamps, or the projectile, or other waves. The result of 'hese wave reflections and interactions is a situation which becomes intractable by closed-form mathematical methods, and this late-time intractability is a principal reason for the development of numerical computer solutions.

Use of the Rate-Independent Theory in Preliminary Design

In spite of the limitations of the Smith theory outlined above, the rate-independent analysis provides

a highly useful means of assessing approximate relations between fiber material properties and ballistic

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response. These relations are of considerable value in performing preliminary design steps in development of textile ballistic-protection devices.

Assuming the material to be linear in stressstrain response (E = constant), the Smith analysis can be cast in the simple form:

$$V = \sqrt{\epsilon_{o} k E \left[z \sqrt{\epsilon_{o} (1 + \epsilon_{o})} - \epsilon_{o} \right]}$$
(13)

which provides a relation for the strain ϵ_0 developed by impact at a velocity V in terms of the fiber modulus. The relation can be solved numerically if one wishes to compute ϵ_0 for a given V, or it can be used directly to plot ϵ_0 versus V for the purpose of developing design curves (see Fig. 2). Once ϵ_0 is known, then c_0 , U, \bar{U} , and w can be found from either the stressstrain relation or Equations 9 - 12. Figure 3 shows such a plot of tension, c_0 versus V, with modulus as a parameter.



Figure 2. Predicted impact strain for linear rate-independent fibers.



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Since the above curves rise monotonically with velocity, one can observe the influence of modulus more easily by plotting ballistic response at a constant velocity, and Figure 4 shows such a plot at V = 400m/sec. Here are plotted the strain and tension from the above methods, along with the strain energy

 $\mathbf{Y} = \frac{1}{2} \quad \mathbf{\sigma}_0 \quad \mathbf{G}_0$ developed behind the wave and the rate of energy absorption \mathbf{Y} c of the fiber. (The term, \mathbf{Y} c, is shown in mixed units, but it could be converted to joules/sec once the density and denier of the fiber are specified.) The rate of energy absorption at the wavefront must equal the rate at which the fiber extracts kinetic energy from the projectile, and it is a reasonable measure of ballistic efficiency. Note that this energy absorption rate rises monotonically with fiber modulus, although with less dramatic improvements after approximately 500 g/den.



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Figure 4. Effect of fiber stiffness on ballistic response; 10 = 10 g/den for tension, 10% for strain, 0.03 g/den for strain energy, and 900 g/den sec for energy absorption rate.

Of course, one cannot improve ballistic efficiency indefinitely by continuing to seek stiffer fibers. In general, increases in stiffeness are accompanied by decreases in breaking strain, and a point may well be reached where this reduced ductility overshadows the beneficial reduction in impact-generated strain shown in Figure 2. This effect may be quantified by means of Equation 13, where one may calculate the critical transverse velocity by determining the velocity which just generates the dynamic breaking strain on impact. If one

knows the variation of breaking strain with stiffness, these calculations may be used to select approximately an optimum fiber stiffness for ballistic efficiency. This process is carried through for illustrative purposes in Figure 5.



Modulus, gpd

Figure 5. Prediction of optimum stiffness for nylon fibers.

The dashed line in this Figure is the relation between dynamic stiffness and breaking strain as determined from fiber-impact tests on a series of nylon yarns that had been subjected to various

drawing treatments by the manufacturer [5]. The solid line is the the calculated transverse critical velocity, considering the effect of stiffness on both impact-induced strain and on breaking strain. An optimum is observed near 60 g/den, which is in fair agreement with experimental observation. All this is a quantification of the often-quoted guideline in armor design that one seeks the highest possible modulus in order to spread the impact over a wide area via increased wavespeed, but that the process must not be carried so far as to induce excessive brittleness. In hard armor this reasoning has led to the use of ceramic faceplates to give high wavespeed, backed by a fiberglass laminate to provide the needed toughness.

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Selection of a Failure Criterion

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The use of simple ultimate breaking strain as a failure criterion in the above example is overly simplistic, since it does not incorporate the strong temperature and rate dependencies that are known to exist in polymeric material. A versatile fracture model which does incorporate these dependencies and is still computationally convenient is that due to Zhurkov [11], which states that the lifetime 't of a solid subjected to a uniaxial stress raccorporate form

$$\tau = \tau_{o} \exp \{ (4^{*} - 8^{*} \sigma) / 12T \}$$
 (14)

where Υ_0 is a pre-exponential factor with units of time, U* is an apparent activation energy for the fracture process, Υ^* is a factor with units of volume, R is the gas constant (8.314 J/mole °K), and T is the absolute temperature. For constant temperature, Equation 14 reduces to

$$\chi = \alpha \exp(-\beta\sigma) \qquad (15)$$

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where

$$\mathcal{A} = \mathcal{C}_{o} \exp\left(\frac{U^{*}}{RT}\right) \qquad (16)$$

$$\mathcal{B} = \mathcal{S}^{*}/RT$$

When stress and temperature vary during the loading process, one can assume linear superposition and write the Zhurkov criterion in the form:

$$\int_{0}^{17} dt / \{r_{o} \exp \left[((1^{*} - 8^{*} \sigma) / RT) \right] = 1 \quad (17)$$

In a constant-stress-rate experiment at constant temperature, for instance,

$$\sigma(t) = Ct$$

$$\int dt / \{\alpha \exp(-\beta Ct)\} = 1$$

$$[\exp(\beta Ct)] / (\alpha \beta C) = 1$$

$$t = \ln(1 + \alpha \beta C) / \beta C$$
(18)

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To illustrate the order of rate dependency provided by Zhurkov's model, Figure 6 shows a plot of Equation 18 for the case of drawn nylon fibers. In this figure $\mathcal{A} = 2.20 \times 10^{19}$ sec, and $\mathcal{F} = 5.13 (g/den)^{-1}$; these are the values obtained by Zhurkov [11] by fitting Equation 15 to creep-rupture data. Such a plot can be used to depict the time-to-break for a fiber, and the tenacity-at-break, as a function of the loading rate.



Figure 6. Variation of breaking tenacity with loading rate - Khurkov model.

As a more direct example of the utilization of Zhurkov's model in fiber ballistics, the stress predicted by the Smith theory for a given impact velocity and fiber modulus can be used in Equation 14 to predict the time after impact at which the fiber will rupture. This analysis predicts that there is no unique critical transverse velocity, but rather a range of velocities over which the fiber will fail in experimentally observable times. Figure 7 shows the predicted results for drawn nylon fibers, using an assumed dynamic modulus of 80 g/den with the same values of \measuredangle and \clubsuit used in Figure 6. This figure

shows that at velocities above approximately 775 m/sec, rupture occurs in less than fifty microseconds and would be counted in most high-speed photographic records as having occurred instantaneously upon impact. The times-to-break become exponentially longer at lower velocities, and failure will occur at the clamp due to wave reflection at times dependent on the wavespeed and fiber length. This variation in what may be termed critical velocity for impact may make up a large part of the scatter observed experimentally in determining critical transverse velocities.





An important advantage to Zhurkov's model is that it is derivable in terms of basic reaction-rate fracture analysis. As such, it provides a means whereby the materials scientist can predict materials and processing modifications so as to manipulate the fracture parameters and improve ballistic performance. A recent review [12] describes the basic implications of reaction rate models such as Zhurkov's, as well as their limitations and experimental corroboration. The development of these models is somewhat controversial, with several quite divergent approaches having strong advocates. Zhurkov's model in particular is often criticized as being simplistic, but is convenient for use in impact by virtue of its computational convenience and its ability to model a wide range of materials behavior, if only phenomenologically. Finally, it should be cautioned that the experiments Zhurkov used in corroborating his model were no faster than the millisecond time scale, some three orders of magnitude slower than ballistic impact fractures. Such an extrapolation is clearly dangerous and should be verified by additional experimentation. The plot given in Figure 7 is in reasonable but not excellent agreement with experimental data given in Smith's papers, indicating that the approach is promising but needing of further corroboration.

II. NUMERICAL ANALYSIS OF IMPACT ON WOVEN PANELS

Method of Analysis

The method of analysis used in this study is a direct numerical approach which attacks the governing dynamic equations of the problem through a computeraided iterative scheme. It may be considered as a hybrid of the finite element method in selecting control volumes and the finite difference in establishing recurrence formulas.



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Figure 8. Idealization of impacted fabric panel as an essemblage of pin-jointed tension members.

The fabric of dimension L by L shown in Figure 8 is modeled as a network of interconnected fiber elements impacted at zero obliquity by a rigid missile of mass M_p with an initial striking velocity V_p . The network model rather than a continuous membrane is employed here, for it is not only more consistent with the discrete fabric structure but also leads to better agreement with the physical deformation configuration (pyramidal cone rather than hemisphere) as observed by Wilde [13] in high speed photographs. The elastic continuum supporting the fabric deformation is generally very flexible in transverse direction: bending effects are neglected. The constituent fibers are considered to have a slender and uniform cross section that only plane waves propagate uniaxially. Furthermore, crossovers are modeled as hinged connections; then, slippage is assumed to be negligible.

Mathematical Formulation

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Considering a typical crossover in the panel, as shown in Figure 9, the impulse-momentum balance



Figure 9. Free-body diagram of forces acting at a fabric crossover point, showing the influence of the fcur fiber elements meeting there and the elastic resistive force provided by the fabric backing.

during time dt may be written as

$$\Delta m \cdot dv = T \cdot dt$$
 (19)

where $d\underline{v}$ is an incremental velocity, \underline{T} is the resultant tensile force, and Δm is the lumped mass of a
fabric element. This relation provides a means of calculating current velocity from field variables in previous time increment. For instance, at node (j+1, k+1), the velocity at time t_{m+1} may be expressed in a finite difference form as

$$\mathcal{O}_{j+1, k+1}^{m+1} = \mathcal{N}_{j+1, k+1}^{m} + \mathcal{T}_{j+1, k+1}^{m} \cdot \frac{\Delta t}{25p\Delta l}$$
(20)

where c is the linear fiber density, Δl , the length of an orthogonal fiber element, β , a numerical factor associated with the crimping and wave of the fabric structure, and the tensile force \underline{T} is given as

$$T_{j+1,k+1}^{m} = T_{10}_{j+1,k+1}^{m} - T_{10}_{j,k+1}^{m} + T_{01}_{j+1,k+1}^{m} - T_{01}_{j+1,k}^{m} + T_{01}_{j+1,k+1}^{m} - T_{01}_{j+1,k}^{m} - k_{b} u_{j+1,k+1}^{m}$$
(21)

in which k_b is a backup spring constant and \underline{u} is the displacement vector. T_{10} and T_{01} are tensile vectors in the deformed orthogonal fibers running through the crossover as shown in Figure 9. The Lagrangian * The \sim underline is used to denote a vector quantity.

coordinates of the node are then evaluated by

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$$r_{j+1, k+1}^{m+1} = r_{j+1, k+1}^{m} + v_{j+1, k+1}^{m+1} \cdot \Delta t$$
 (22)

The up-to-date strain defined as $e(j+1, k+1; m+1) = \{e_{10}, e_{01}\}$ may now be determined from a continuity condition;

$$\begin{array}{l}
\overset{m+1}{\in} 10 & \underset{j+1,k+1}{m} = \underbrace{e_{10}}_{j+1,k+1} \\
+ \left\{ \left[\underset{j+2,k+1}{m+1} - \underset{j+1,k+1}{m+1} \right] \right\} \\
\left[\underset{j+2,k+1}{m} - \underset{j+1,k+1}{m} \right] - 1 \right\}
\end{array}$$

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$$= \sum_{j=1}^{m+1} \frac{m}{j+1, k+1} = \sum_{j=1}^{m} \frac{m}{j+1, k+1} + \left\{ \left[\prod_{j=1}^{m} \frac{m+1}{j+1, k+2} - \prod_{j=1, k+1}^{m} \right] \right\}$$
(24)
$$\left[\prod_{j=1}^{m} \frac{m}{j+1, k+2} - \prod_{j=1, k+1}^{m} \frac{m}{j+1, k+2} - \prod_{j=1, k+1}^{m} \frac{m}{j+1, k+2} - \prod_{j=1, k+1}^{m} \frac{m}{j+1, k+2} \right]$$

Tensile stresses for the fibers at the crossover may be computed from material's dynamic constitutive relationship. For the case of a simple elastic fabric, T may be calculated by

$$T_{j+1,k+1}^{m+1} = E \stackrel{m+1}{\sim} _{j+1,k+1}^{(25)}$$

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Current missile velocity $V_{p}(t)$ may be obtained by

$$V_{p}^{m+1} = V_{p}^{m} + \{4(T_{10_{z}})_{0,0}^{m+1} \\ \times \sin \theta_{p} + k_{1}(ul_{z})_{0,0}^{m+1} \} \cdot \Delta t_{p}$$

where the fabric inclination $\boldsymbol{\theta}_{p}$ at the impact point may be evaluated from

$$\Theta_{p} = Tan^{-1} \left\{ \left[\left(\mathcal{M}_{z} \right)_{0,0}^{m+1} - \left(\mathcal{M}_{z} \right)_{1,0}^{m+1} \right] / \Delta l \right\} (27)$$

The total kinetic energy loss of the missile

during penetration can be computed from

$$\Delta E_{p} = \frac{1}{2} M_{p} \left(V_{p}^{2} - V_{r}^{2} \right)$$
(28)

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where V_r is the residual velocity of the missile upon penetration. The fabric energy absorption and partition are of great interest, since they provide a means of evaluating the performance of the material. The kinetic and strain energy, $\Delta E^k(t)$ and $\Delta E_f^s(t)$, obtained by the panel during impact may be calculated by

$$\Delta E_{f}^{k}(t) = \int_{0}^{t} \int_{\Delta} \frac{1}{2} \cdot \Delta m \left| \psi_{x,y}^{t} \right|^{2} d\Delta dt \qquad (29)$$

$$\Delta E_{f}^{s}(t) = \int_{A}^{t} \int \left[\frac{1}{2} \right]^{2} (1/2E) dA dt \qquad (30)$$

Where A is the area of the fabric. The above formulations have been coded in FORTRAN, and the computation algorithm proceeds from one node to the next along a wave front propagating through the fatric. Due to geometric symmetry, only half of one quadrant is con-

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sidered. At each time increment, the code begins at the origin (the impact point) and works outward until the wavefront is reached. The space progression consists of a series of passes along lines diagonal to the orthogonal fibers, indicated by dashes in Figure 10. The algorithm begins at the x-axis (a subroutine is employed to handle the slightly different conditions along this symmetry boundary), and progresses along the diagonal until reaching the end of the octant. For reasons of stability, the rate at which the code progresses outward from the impact point is related to the fabric wavespeed; these stability considerations will be discussed in a later section. and the Arthony and the contains



Figure 10. Propagation scheme for the iterative wave propagation algorithm. 38

The numerical method requires appropriate initial and boundary conditions in order to proceed with the computation. The initial condition is that all nodal points are at rest except that the initial projectile velocity is imposed at the center of the panel, i.e.

$$\mathcal{N}_{0,0}^{\circ} = \{0,0,V_{p}\}$$
(31)

The boundaries of the fabric are assumed to be rigidly clamped during impact, thus

Solution Stability, Convergence and Accuracy

Solution stability and convergence are directly related to the theory of characteristics for the hyperbolic system. The Von Neumann stability criterion [14] for the probem may be written as

$$= (\Delta t / \Delta L) \times 1$$
 (33)

where c_r is the wave velocity in the fabric. Hence the selection of Δt and Δl cannot be arbitrary.

The value of c_r is not known prior to the analysis, but a preliminary study by Roylance [15] indicates that it is a fixed fraction of the wave velocity ir a single fiber, c_f , i.e.

$$C_{r} = C_{f} / \alpha \tag{34}$$

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where α is a numerical factor. It generally has value greater than unity, which may be attributed to the effective increase on lineal density caused by fiber crossovers. In a square-woven fabric, the lineal density of a fiber along which a wave is propagating is effectively doubled. This retards the wave velocity according to Equation 2 by a factor of $\alpha = \sqrt{2}$. The stability condition is then of the form

$$c_{f} \Delta t / (\alpha \Delta l) < 1$$
 (35)

In the current analysis, ΔQ is obtained by physical considerations; therefore Δt is constrained by Equation (35). The parameter α has its optimum value obtained from stable solutions and is defined as

$$\bar{\alpha} = (\Delta l/c_{f}) / \Delta t \qquad (36)$$

In the absence of a complete theory for finding the exact value of this parameter, it is a common practice in the use of numerical methods to have the computer determine it. The optimum $\overline{\alpha}$ may be obtained by changing its value continuously in test cases until a known solution is matched and a variation of the quantity will not yield any appreciable difference in the results. Unfortunately, there is no existing solution for this problem and one must resort to numerical tests of smoothness or of conservation laws for this purpose. A convenient measurement of stability and convergence is to study the rate of energy conservation of the system. In this study, an energy discrepancy parameter η is introduced for the purpose, and is defined as

$$\eta = |(E_p - E_f)/E_p| \qquad (37)$$

where E_f is the total energy absorption by the fabric, and E_p is the projectile energy loss defined previously. Figures 11 and 12 give illustrations of the dependence of solution stability and convergence on the values of : parameter. An optimum value $\alpha = \sqrt{2}$ is obtained from these results, in agreement with physical reasoning.







Figure 12. Illustration that the numerical scheme converges to accurate values with time, as indicated by the energy discrepancy ratio. Note that nonoptimum values of the stability ratio (η in this figure) lead to divergence at longer times.

Assessment of accuracy of the numerical analysis is somewhat problematical, as no closed-form mathematical analyses are available against which to check the code results. Certain experimental observations are available, however, one of which is shown in Figure 13. This figure is a plot of residual projectile velocity

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after penetration of a Kevlar panel, as a function of initial velocity. The good agreement of the predicted and observed results is important, since it provides some assurance that both the transient response and the final fracture processes are being modeled reasonably. It might also be mentioned that this particular plot is one which plays an important role in the design process, so that the ability to generate it numerically without prior ballistic data or any idealizing assumptions is of considerable practical importance.

Another result of the numerical calculations which may be checked against experiment has to do with the shape of the transverse deformation cone, since the cone may be followed by high-speed photography during the impact event. It should be mentioned that this photgraphic evidence provided the initial impetus to the development of the present pin-jointed fiber model, as opposed to various membrane approaches which have been attempted in the past. The photographs clearly show a pyramidal deformation cone which reflects the orthogonal nature of the woven structure, as opposed to the circular cones which would be predicted by axy-symmetric membrane analyses. The present numerical treatment predicts this pyramidal shape

correctly. A convenient indicator of deformation is the size of the cone at the time of projectile penetration, as this parame ar also reflects both transient and fracture properties of the panel. Figure 14 shows the predicted and observed cone size at penetration for a Kevlar panel, and again it is seen that agreement is satisfactory.



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Figure 14. Computed and experimentally observed values of cone deformation cone size at time of projectile penetration. The V_{50} is that value of impact velocity at which penetration occurs nearly instantaneously.

Parametric Materials Study

The utility of the numerical model will be illustrated by means of a number of computer experiments in which the influence of fabric materials properties on ballistic resistance is assessed. These results help validate the reliability of the model in that it can be shown to generate data in agreement with experimental observations. It also provides a means of illustrating certain phenomena, such as transient wave propagation, which are not generally observable experimentally; in this regard one's intuitive understanding of the impact even is improved considerably.

Numerical results have been obtained for a series of four simulated orthogonally-woven square panels 203 mm on a side, impacted at zero obliquity by a 0.22-caliber projectile weighing 1.10 gram. Such a projectile is commonly used in experimental work to simulate the effect of fragment impact. The edges of the panels were assumed to be clamped, although penetration generally occurred before the arrival of stress waves at the clamps; the nature of the edge boundary conditions is therefore relatively unimportant. Rather than perform straightforward parametric tests in which one variable, such as fiber modulus, is varied while others are held constant, it was decided to simulate

a series of actual fabrics for which input data was available either from the weaver or from laboratory measurement. The computer results can thus be compared directly with laboratory ballistic tests, although in general, more than one variable is changed in each simulation. In particular, the fabric punel weight varies slightly for each material type, although this effect was expected to be small relative to the large change resulting from the markedly different fiber moduli.

For the purpose of these parametric tests, only very simple constitutive and fracture models were employed. Although more realistic models are available as described elsewhere in this report, the numerical data necessary for input into these models are generally not available. For this reason the fiber stiffness was set to a constant value obtained from handbook quasistatic stress-strain data, and the failure criterion was a simple maximum-breaking-strain check, where the maximum allowed was also taken from quasistatic tensile test results. In spite of these questionable choices, the results of the computer simulations are of considerable interest.

The data for the four fabric types are shown below:

GEOMETRIC AND MATERIALS PROPERTIES USED IN

FABRIC STUDIES				
Fiber	Nylon	Kevlar 29	M Kevlar 49	TM 9 Graphite
Tensile modulus,gpd	80	550	990	2.650
Fracture Strain, %	14.0	4.0	2.2	1.1
Fabric Mass, gm	19.53	17.38	25,75	27.09
Yarn denier	L050	1167	<u>1</u> 485	1500
Yarn/cm	17	16	16	16

Figure 15 shows typical computer predictions of strain wave profiles obtained at various times after a 400 m/sec impact on the various fabrics. Unlike impact on a single fiber, in which a constant level of strain is propagated outward from the impact point, the array of fiber crossover junctions around the impact point in a fabric serves to reflect a portion of the outward-propagating wave back toward the impact point. As a result, the strain is always greatest at the point of impact, and grows continuously with time (unless the projectile is slowed appreciably by the panel). Both the level of strain and the rate of propagation

are governed by the fiber modulus and density. As shown in the figure, graphite fibers have the highest modulus of the four materials, and thus propagate the lowest level of strain at the highest rate. As the modulus is decreased, the strain level is increased and the wavespeed is decreased.



The strain history in the fabric is directly related to missile striking velocity as indicated in Figure 16. When the velocity is greater than a critical impact velocity V_{cr}, strain at the impact point continuously rises until penetration, due to the continual arrival of wavelets reflected from crossovers and boundaries. In contrast, if the velocity is smaller than V_{cr} , the impact strain develops to a level below the breaking strain and remains relatively constant for the rest of the dynamic process. Here the effect of unloading due to projectile deceleration is able to balance the increase of strain due to wave reflection. The wavy strain history in the figure may be caused by the dispersion and interaction of the traveling and reflected wavelets, and perhaps, some numerical fluctuation.

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Penetration dynamics can also be illustrated by the missile deceleration as shown in Figure 17, where reductions of missile velocity by various fabric materials are given. Note that the ability of the various fabrics to decelerate the projectile increases monotonically with the fiber modulus.



Figure 17. Relative ability of the various fabric types of slow the projectile during impact. Ordinal values represent the ratio of current to initial projectile velocity.

The energy extracted from the projectile is partitioned into strain and kinetic energy in the panel. This energy partition is easily computed, and Figure 18 indicates that approximately half the total fabric energy absorption is stored in the form of strain energy. The kinetic energy associated with transverse velocity is approximately equal to that associated with in-plane velocity components. Energy absorption is a



Figure 18. Energy absorbed by a Kevlar 29 panel after a 400 m/sec impact, illustrating the partition of impact energy into kinetic and strain energy in the panel.



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Figure 19. Illustration of the relative ability of the four fabric types of absorb impact energy. The curves are terminated at the right by projectile penetration, as indicated by a maximum-breaking strain failure criterion.

convenient indicator of panel ballistic performance, and Figure 19 illustrates the relative energy absorption capabilities of the four panel materials studied. It is seen that the high fiber modulus of the graphite panel leads to a rapid rate of energy absorption, but that fracture occurs before the panel has been able to extract as much of the projectile's impact energy as the lower-modulus fabrics. Conversely, nylon requires a long time to penetration, but the energy absorption rate is too slow to lead to a large total energy absorption. The Kevlar 29 panel exhibits the best combination of energy absorption rate and long time to penetration, and is thus predicted to be the superior ballistic material of the four types studied.

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It should be mentioned that the accuracy of these results is limited by the questionable assumptions which had to be made due to the present lack of knowledge as to dynamic fiber properties which could be used as input data for the code. For these rather stiff fibers, the use of a linear elastic constitutive law is probably not a serious error; however, the use of maximum-breaking-strain failure critrion is almost certainly to blame for some inconsistencies in the results. In particular, Kevlar 49 is known to be essentially as good as, if not superior to Kevlar 29 as a ballistic material. The authors feel the shape of the energy absorption curves in Figure 19 is accurate, but that the location of the failure point is poor in the case of Kevlar 49. This points out the need for more complete dynamic fracture data on these fibers, so that more realistic models such as that described by Equation 17 may be employed.

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It is natural to seek some simple relationship between fiber material properties and fabric ballistic resistance. The preceeding results lead one to expect that the most important parameter governing the stress history in the fabric before fracture is the fiber modulus. The modulus controls wavespeed through the relation $c = \sqrt{kE}$, and thus the distance the impact disturbance will have traveled in a given time. The

modulus also controls the level of strain which will be generated by impact at a given velocity. The relation is not known explicitly for fabrics, but can be determined by performing computer experiments using the numerical code.

Figure 20 depicts the computed strain history at the point of impact for 400 m/sec impacts upon the four model fabrics. It is clearly seen that an increase in fiber modulus decreases the strain for a given time, in correlation with the same result for single fibers. The fabric impact is considerably more complex than single-fiber impact, however; the point of impact feels not only the continuing influence of the projectile, but is also continually bombarded by wavelets reflected and diverted from adjacent fiber crossovers. The situation is too complex to permit simple generalizations, but the nonlinear form of the strain histories for the various fabrics can be taken to reflect the influence of wave interactions occurring in a region whose size increases quadratically with time. Note also that the shape of the strain histories varies consistently with fiber modulus: the time for arrival of the first peak, for instance, decreases monotonically with modulus.

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If one normalizes the magnitudes of the ordinal values in Figure 20 by the value of strain which would be developed in a single fiber by transverse impact at the same projectile velocity, the strain magnitudes of the four curves achieve comparable values. This procedure essentially compensates the curves for the effect of the fiber modulus on the impact-induced strain. and the second state of the second second

The shift of the curves along the abscissa, however, is less clear. The rate at which the strain increases at the impact point is governed by the complex interactions of waves traveling about within the constantly expanding region of influence, and is beyond simple visualization. On average, the time necessary for a wave to reflect and return eventually to the impact point should decrease inversely with the wavespeed, i.e. inversely with the root of the modulus. However, the size of the region in which stress waves are traveling at any given time also depends on the wavespeed, and one would expect that a larger region of influence would decrease the rate at which reflected and diverted wavelets are able to return to the impact point.

It is found that the time after impact at which the first peak in the strain occurs varies linearly, with good correlation, with the fourth root of the fiber modulus (or the square root of the wavespeed). Using this observation, which is likely related to the geometry of the region of influence, one can compensate the abscissal values of Figure 20 by the factor $E^{0.25}$. The result of the ordinal and abscissal normalization is shown in Figure 21, where a curve valid for all four fabrics is developed.



Figure 21. "Master" curve for impact-induced strain at the point of impact. Ordinal values represent strain normalized on the basis of the strain which would be generated in a single fiber by impact at the same velocity, while abscissal values are adjusted by a factor equal to the fourth root of the fiber modulus.

This master curve represents an improved means of performing preliminary armor design. Since the normalizing factors are known once the dynamic modulus of the fiber is specified, one can generate a strain vs. time curve from Figure 21 applicable for a particular fabric and impact velocity. The time for rupture is the time at which the impact-induced strain exceeds

the fiber's dynamic breaking strain. As in the fiber case, we then see that ballistic resistance is a balance between high fiber modulus leading to high wavespeeds and lower strains, and fiber breaking strain.

This approach is approximate in several respects, however, and is thus limited to preliminary design. First, it is seen in Figure 21 that perfect correlation among all four test fabrics is not attained, the nylon showing a deviation at high strain. Similar deviations in other fabrics might be observed as well. Second, the curve of Figure 21 was generated from computer experiments at relatively high velocity, so that projectile slowdown was not an appreciable factor. At low impact velocities, the fabric is able to decelerate the projectile and even bring it to rest. The effect of projectile slowdown is to generate unloading waves in the fabric which travel simultaneously with those previously described. This unloading would have a strong influence on the curves such as that in Figure 21, causing the curve to pass through a maximum and decrease thereafter in those cases in which the fabric is able to defeat the projectile. For these cases, complete treatment using the numerical code would be necessary.

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III. EFFECT OF VISCOELASTIC MATERIALS RESPONSE

Viscoelastic Constitutive Relations

In the course of the iterative calculations described earlier, a constitutive material law must be evoked at each element in order to compute the element tension from its strain (or strain history). One would expect that a model incorporating viscoelastic effects would be necessary for proper simulation of polymeric materials, and in fact there is considerable direct evidence [16] that relaxation does indeed occur in the ballistic time frame. This is also to be expected in light of the dynamic mechanical spectrum of nylon, for instance, in which a beta relaxation is observed having an apparent activation energy of approximately 60 kJ/mole [17]; this relaxation is calculated to occur in approximately five microseconds at room temperature.



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Figure 22. Wiechert spring-dashpot model for linear visco-elastic fiber response.

A general viscoelastic model well suited for computing tensions from pres:ribed strains is the Wiechert model, depicted schematically in Figure 22. This model takes the polymer response to be analogous to that of an array of Newtonian dashpots and Hookean springs. The differential tension-strain law for the jth arm of the model is

$$\dot{\mathbf{e}} = \frac{1}{k_j} \overset{\bullet}{\boldsymbol{\sigma}}_j + \frac{1}{\eta_j} \overset{\bullet}{\boldsymbol{\sigma}}_j \tag{38}$$

where the dots indicate time differentiation, σ is the tensile stress and ϵ is the strain. Casting this equation in finite difference form relative to a discrete time increment Δ t and solving:

$$\sigma_{j}^{t} = \frac{1}{\left[1 + (\Delta t / r_{j})\right]} \left[k_{j}(\epsilon^{t} - \epsilon^{t-1}) - \sigma_{j}^{t-1}\right] (39)$$

where the superscripts t and t-1 indicate values at the current and previous times, respectively, and $\tau_j = \eta_j/k_j$ is a relaxation time for the jth arm. The total tension at time t is the sum of all the σ_j^t plus the tension in the equilibrium spring k_j :

$$\sigma^{t} = k_{e} \epsilon^{t} + \sum_{j} \frac{k_{j} (\epsilon^{t} - \epsilon^{t-1}) + \sigma_{j}^{t-1}}{1 + (\ell t / \tau_{j})}$$
(40)

This tension-strain calculation is performed at each element node. In addition to storing all the k_i and

 $\boldsymbol{\tau}_{j}$, the computer must also store the previous strain and tension values at each node.

The choice of the k_j and γ_j should be such as to model the polymer viscoelastic response in a time

scale comparable to the ballistic event, which takes place on a microsecond time scale. It is of course difficult to conduct such conventional tests as creep or stress relaxation on this time scale, but guidance as to proper model parameter selection can be obtained from dynamic mechanical spectra, using the activation energies of the appropriate low-temperature relaxations to effect a temperature-rate conversion. For nylon fibers, for instance, one would fit the Wiechert model to the beta relaxation, ignoring the alpha and gamma relaxations as not being appropriate to the ballistic time scale at room temperature.

Results for Single Fibers

As a means of developing a proper context for the study of viscoelastic response of a woven textile panel, some results obtained in an earlier study [18] which used a direct numerical simulation of viscoelastic relaxation in a transversely impacted single fiber will be reviewed briefly. The numerical approach for this study was identical to that described for fabric structures, except that it considered a single fiber discretized as a series-connected assemblage of pin-jointed finite elements. As in the fabric case, this treatment produced numerical values for the position, veloci y, strain, and tension of each finite element of fiber as a function of time after impact. A variation of this treatment will be described in some detail in Chapter IV of this report.

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Figures 23 and 24 show the distribution of nondimensionalized strain and tension along the fiber at various times after impact, plotted against the Lagrangian fiber coordinate. These distributions were obtained from the Wiechert model using only a single spring-dashpot arm in parallel with the equilibrium spring; this 'hree-element model is commonly known as the "standard linear solid", or the "Zener solid" The distributions for these two figures are for a choice of model parameters $k_e = 80$ gm/den, $k_1 = 20$ gm/den, and $\tau_1 = 50$ //sec. The values of the ordinates have been normalized by the strain or tension which the rate-independent Smith theory predicts for a linear elastic material at the same impact velocity.



Figure 23. Normalized strain plotted against Lagrangian fiber coordinate for various times after impact.

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Figure 24. Normalized tension distribution along fiber.

The distributions in figures 23 and 24 demonstrate several features typical of viscoelastic wave propagation:the magnitude of the wavefront attenuates as it propagates along the fiber, the strain at a given position increases with time from its original value, and the tension decays with time. Smith [19] used the method of characteristics to show that the wavefront attenuation is given by:

$$T(ct,t) = T_0 \exp(-\lambda t/zt)$$
 (41)

$$\epsilon$$
 (ct,t) = $\epsilon_0 \exp(-\lambda t/zt)$ (42)

where $\lambda = k_1/(k_1 + k_e)$ is the relative strength of the viscoelastic relaxation. The wavefront tension magnitude predicted by Equation 41 is shown in Figure 25, which also serves to illustrate the numerical accuracy of the direct analysis. (Here a 0.15 m fiber was divided into 200 finite elements). Some numerical overshoot is evident at the discontinuous wavefront, but the distribution extrapolates to the analytically-predicted value.

By means of Laplace transforms, Smith [20] also obtained approximate expressions for the strain and tension distributions in a longitudinally impacted fiber. These expressions predict that the tension and strain at the point of impact will approach the limiting values

$$T(0,0) = T_0 \sqrt{(1-\lambda)} = 0.894 T_0$$
 (43)
$$E(0, ab) = E_0 / \sqrt{(1-\lambda)} = 1.11B E_0^{(44)}$$

Where the numerical coefficients are for $\lambda = 0.2$. At x = 0, the distributions in Figures 25 and 23 approach limiting values greater than Equation 43 for tension and greater than Equation 44 for strain. Thus stress relaxation is slightly less and creep slightly greater for transverse impact than for longitudinal impact; Smith [19] reached this same conclusion in his work on transverse impact.

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Results for Woven Panels

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The three-element Wiechert model (the standard linear solid) used in the previous section was also employed to examine the influence of viscoelastic relaxation during ballistic impact of woven panels. The model parameters were chosen to simulate ballistic nylon: $k_1 = 20$ gm/den, $k_e = 80$ gm/den, $\tau_1 = 5$ Asec. Results have been obtained for a simulated 0.2 m x 0.2-m

panel weighing 19.5 gm, impacted with a 0.22-caliber fragment simulating projectile weighing 1.10 gms at various impact velocities.



Figure 26. Stress distributions along orthogonal fibers running through impact point for linear elastic and viscoelastic fabrics (t a 30.4 microsec).

Figure 26 shows the distribution of stress along the orthogonal fibers running through the point of impact at t = 30.4 μ sec after an impact at V_p = 300 m/sec. The results for the viscoelastic fabric are compared with those of an ideally elastic fabric having a stiffness equal to that of the unrelaxed viscoelastic material (100 gm/den). The nonuniform distributions along the fiber are due as described earlier to the continual reflection of wave components from fiber crossovers, resulting in a maximum in stress at the impact point. An appreciable difference in stress levels between the linear elastic and viscoelastic cases is observed, especially near the wavefront. Relaxation of the stress due to the ratedependent material behavior may be expressed by the ratio of the viscoelastic and the elastic and the elastic stress, T/T_{o} , as shown in the figure. It is found that a large amount of relaxation occurs near the wave front while an equlibrium state of relaxation is reached in the region away from the disturbance front.





The wave attenuation during this 300 m/sec impact is also demonstrated in Figure 27, where relative strain distributions $\boldsymbol{\epsilon} / \boldsymbol{\epsilon}_{\boldsymbol{\lambda}}$ are given for various times after impact. As illustrated in this figure, the magnitude of the wavefront attenuates significantly as it propagates along the orthogonal fibers, and the strain at a given position increases with time after impact from its original values.



Figure 28. Stress histories at impact point for linear elastic and viscoelastic materials.

The stress and strain histories at the point of impact shown in Figure 28 give another indication of viscoelastic dissipation in the response of the panel. They increase continuously with time due to the reflection of wavelets from crossovers; however, stress relaxation and strain creep of the viscoelastic material occur simultaneously with this general increase. The viscoelastic stress at a given time is smaller than the elastic case as shown in the figure. The relative relaxation at the point of impact, denoted by the ratio of the viscoelastic and elastic case, develops gradually and reaches a steady state at long times. The relaxation histories for different missile striking velocities are given in Figure 29. The similarity of their magnitudes is a manifestation of the linear material response. Again, these stresses approach an asymptotic equilibrium state at times longer than the characteristic material relaxation time.



Figure 29. Stress relaxation at impact point for various impact velocities.

Nonlinear Viscoelastic Response

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The use of the Wiechert model as described in the previous sections is sufficient to illustrate the most important features of rate-dependent ballistic materials. However, most materials do not meet the rigid requirements of linearity necessary for a truly rigorous application of concepts of linear viscoelasticity. For more detailed simulations of fabric and fiber response, one must turn to general constitutive relationships which more accurately model the behavior of these materials. Unfortunately, there does not exist a general concensus of the most realistic means of achieving this goal. At present, the subject of nonlinear viscoelasticity is being pursued actively by several groups, several of which are employing highly divergent approaches to this problem. It is not possible here to select any single approach as having significantly greater merit than certain others.

However, the ease with which various constitutive laws may be incorporated into the direct analysis scheme makes it possible to assess relatively easily the influence of various assumed material models. As an illustration of this capability, some results using Eyring's model of thermally-activated nonlinear viscoelasticity will be presented.

The computationally-convenient Wiechert model can be extended to include the effect of material nonlinearity by rendering the springs and/or the dashpots nonlinear. If, for instance, one uses a power-law spring and a nonlinear Eyring dashpot [21], defined as

then the finite-difference equation relating tensions and strains in the jth arm of the model is:

$$\frac{\epsilon^{t} - \epsilon^{t-1}}{\Delta t} = \frac{1}{b_{j}k_{j}} \left(\frac{\sigma_{j}^{t}}{k_{j}}\right)^{\frac{1}{b}-1} \left(\frac{\sigma_{j}^{t} - \sigma_{j}^{t-1}}{\Delta t}\right)$$

$$+ A_{j} \sinh \left(\alpha_{j} \sigma_{j}^{t}\right)$$
(46)

A relation such as this requires an iterative numerical solution for σ_j^t at each element and at each time step; the computer effort is increased but the principles of the impact algorithm are straightforward. The principal obstacle to the use of nonlinear models in the direct analysis is not the incorporation of the models into the computational scheme, but rather the determination of the material parameters (the b's, k's,A's,and α 's in Equation 46) applicable to the microsecond time scale of polymer relaxations.

To illustrate the effect of nonlinear constitutive models on panel ballistic response, a series of computer experiments was performed on three different simulations of nylon fabric: one using only linear elastic response

(only the equlibrium spring in the Wiechert model), one using the standard linear solid model for linear viscoelastic response (the equilibrium spring plus one springdashpot arm), and the last being a standard linear solid but with the dashpot made a nonlinear Eyring element. The intial modulus was taken as 100 gm/den, the relaxed modulus as 80 gm/den, and the relaxation time for the standard linear solid as five μ sec (the same as in the previous section). The concept of relaxation time (the time to complete 63.2% of the total relaxation) has no meaning for the nonlinear element, since the rate of relaxation changes nonlinearly with the stress. Lacking any experimental data in this time scale, the A and α were arbitrarily chosen so as to cause relaxation in approximately the same time scale as the standard linear solid. A and α were set at 10^3 sec ⁻¹ and 0.7 den/gm, respectively. The nonlinear constitutive equation was solved at each element using Muller's method [22], which increased the computation time relative to that of the standard linear solid by roughly one-third.



Figure 30. Stress distributions along orthogonal fibers running through impact point for linear elastic and nonlinear viscoelastic fabrics.

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One means of comparing the various constitutive models is in terms of the distributions of strain along the orthogonal fibers running through the impact point, at various times after impact. Figure 30 shows the distributions for the elastic and nonlinear viscoelastic materials 20 µ sec after a 300-m/sec impact. Also shown is the ratio between the nonlinear and the elastic cases. This ratio is a measure of the stress relaxation in the fabric; it is greates: at the wavefront, as the large gradient of strain there produces a similarly large rate of relaxation.



Figure 31. Comparison of stress relaxation in linear and nonlinear viscoelastic fabrics.

The nonlinear stress relaxation is compared in Figures 31 to that produced by the standard linear solid. Although the equilibrium value far from the wavefront is approximately the same in both cases, strong differences are evident near the wavefront. These are due to the relatively more rapid response to higher strain gradients in the nonlinear material. Another indicator of viscoelastic fabric response is the stress at the point of impact. The stress and strain at the impact point increase with time due to the continual arrival there of wavelets reflected from fiber crossovers, but in viscoelastic materials both stress relax-

ation and creep strain are superimposed on this overall increase. In Figure 32 the point-of-impact stress histories for the three materials are plotted, as well as the stress relaxation ratio defined as before as the ratio between the viscoelastic and elastic stress. As in the earlier two figures, the linear and nonlinear viscoelastic models approach essentially identical equilibirum values at long times, but are markedly different near the wavefront due to the more rapid response of the nonlinear material to large gradients.





IV. <u>NUMERICAL ANALYSIS OF WAVE PROPAGATION</u> <u>IN TWO CROSSED FIBERS</u>

Introduction

This chapter describes study of the dynamics of a special but highly important physical system: that of two fibers, one having been transversely impacted at zero obliquity by a high-speed projectile, and the other crossing the first perpendicularly at some . distance from the impact point. This system is germane to the understanding of impact and wave propagation phenomena in woven textile panels used for ballistic protection. The wave propagation phenomena occurring at the fiber crossover have a strong influence on the response of a woven panel to impact, since these panels typically have on the order of forty crossovers per inch. The nature of these crossover interactions may be one of the factors causing what appears to be an excellent fiber in single-fiber ballistic tests to exhibit less ballistic protection when woven into a textile panel structure than a nominally inferior fiber. As mentioned earlier, this situation obtains in the case of the Kevlar ballistic protectio: vests now being used by military and police personnel: the Kevlar vest outperforms the older nylon vest, in spite of

nylon's having a higher transverse critical velocity. The inability to predict vest performance from singlefiber test data is a matter of considerable concern to the armor design community, and this study of fiber crossover dynamics was begun to clarify this situation. <u>Method of Solution</u>



Figure 33. Schematic of model for numerical analysis of two crossed fibers.

System Idealization. The system of two crossed fibers is modeled as in Figure 33, where the origin of coordinates is placed at the midpoint of the clamped primary fiber, which extends along the x-axis. The projectile moves along the y-axis only, and impacts the primary fiber at the origin. From symmetry, only half the primary fiber need be considered. The secondary fiber extends along the z-axis and intersects the primary fiber at some a - crary distance from the origin. At the crossover point, the secondary fiber is assumed to follow the motion of the primary fiber in the direction perpendicular to the primary fiber (in the x-y plane), but is allowed some measure of slip in the direction parallel to the primary fiber. Motion of the primary fiber is assumed to occur in the x-y plane only, while the secondary fiber may move in all three directions.



Figure 34. Discrete element of fiber.

To proceed, the fibers are discretized as a series of n pin-jointed finite elements of equal length as shown in Figure 34. The masses of the elements are taken to be lumped at the nodal end points of these elements, and at these nodes are defined vector coordinates x_i , velocity v_i , and tension T_i . The $\boldsymbol{\epsilon}$, at each element will be computed scalar strain from the coordinates of the nodes at either end of the element. The tension \underline{T}_i has the same direction as the element itself (approximating the element's assumed inability to support a bending moment), while \mathbf{y}_i is not constrained in direction. These elements are now described as in the fabric analysis by simple governing equations: impulse-momentum balance, straindisplacement relation, constitutive relation, etc. These relations are cast as a recursive algorithm for proceeding from one element to the next along the fiber length, and then repeating the process at a new increment of time. The computer solution thus is referenced to a Lagrangian frame of reference attached to and extending with the fiber, which effectively reduces the problem to one dimension.

<u>Momentum Balance</u>. A consideration of impulsemomentum balance at the i + 1st node provides a means of computing the current velocity at that node in terms

of its velocity in the previous time increment and the tensions acting on it during that time increment. (In the follo ing, subscripts on a variable refer to the node at which it is defined, while superscripts t and

t-1 refer to values at the current and previous times respectively). The impulse-momentum balance can be written in finite difference form as

$$\Xi T = \Delta m \frac{\Delta v}{\Delta t}$$
(47)

$$T_{i+1}^{t-1} - T_{i}^{t-1} = \frac{\Delta m}{\Delta t} \left(\underbrace{v}_{i+1}^{t} - \underbrace{v}_{i+1}^{t-1} \right) \quad (48)$$

Letting A = $\Delta m / \Delta t$, a fixed parameter, equation 48 may be solved for v_{i+1}^t :

$$\mathcal{V}_{i+1}^{t} = \mathcal{V}_{i+1}^{t-1} + A(T_{i+1}^{t-1} - T_{i}^{t-1}) \quad (49)$$

This vector expression can be written in scalar form by reference to the inclination angles θ_i and θ_{i+1} of the T_i and T_{i+1} vectors respectively:

$$\Theta_{i}^{t-1} = Tan \frac{y_{i+1}^{t-1} - y_{i}^{t-1}}{x_{i+1}^{t-1} - x_{i}^{t-1}}$$
(50)

$$\Theta_{i+1}^{t-1} = Tan \frac{y_{i+2}^{t-1} - y_{i+1}^{t-1}}{\chi_{i+2}^{t-1} - \chi_{i+1}^{t-1}}$$
(51)

Then the x and y components of velocity are:

$$\mathcal{M}_{i+1}^{t} = \mathcal{M}_{i+1}^{t-1} + A \left(T_{i+1}^{t-1} \cos \theta_{i+1}^{t-1} \right) (52) - T_{i}^{t-1} \cos \theta_{i}^{t-1} \right) (52) - T_{i}^{t-1} \cos \theta_{i}^{t-1} - T_{i}^{t-1} \cos \theta_{i}^{t-1} - T_{i+1}^{t-1} \sin \theta_{i+1}^{t-1} (53) - T_{i}^{t-1} \sin \theta_{i+1}^{t-1} \right) (53)$$

where $T = \{ \underline{T} \}$ is the tension magnitude. The boundary conditions are easily incorporated into the impulsemomentum balance: at the first mode, the velocity is set equal to the current projectile velocity $(\underline{v}_1^t = V^t)$, and at the clamp the velocity is set to zero $(\underline{v}_n^t = 0)$.

Strain-displacement Relation. Having computed the velocities at the ith and i+1st nodes, the strain in the element between these nodes is computed as

$$\Delta \epsilon_{i} = \frac{\lfloor \frac{t}{2} - \lfloor \frac{t}{2} \rfloor}{\lfloor \frac{t}{2} - 1 \rfloor}$$
(54)

where L_i is the element length. Continuing:

$$\epsilon_{i}^{t} = \epsilon_{i}^{t-1} + \frac{L_{i}^{t}}{L_{i}^{t-1}} - 1$$
 (55)

where

$$L_{i}^{t-1} = \left| \chi_{i+1}^{t-1} - \chi_{i}^{t-1} \right|$$
(56)

and

$$L_{i}^{t} = \left| \chi_{i+1}^{t} - \chi_{i}^{t} \right|$$

$$= \left| (\chi_{i+1}^{t-1} + \omega_{i+1}^{t} \Delta t) - (\chi_{i}^{t-1} + \omega_{i}^{t} \Delta t) \right|$$
(57)

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Constitutive Relation. Knowing the strain $\boldsymbol{\epsilon}_{i}^{t}$, the tension magnitude T_{i}^{t} is computed from the material's dynamic stress-strain law. These relations are as described earlier, and currently available constitutive models include linear elastic, nonlinear elastic (cubic

polynomial and exponential strain hardening), linear viscoelasticity (Wiecherc model), and nonlinear viscoelasticity (Eyring model).

<u>Computation of New Projectile Velocity</u>. The algorithm described above proceeds from one element to the next along the length of fiber, and i started by imposing the initial projectile velocity on the first node. At the end of the first time increment, a strain will have developed in the first element due to the velocity difference between the first and second nodes. (Initially, all velocities, tensions, and strains are set to zero.) This strain produces a tension as calculated from the constitutive relation, and this tension produces a velocity in the second node beginning at the next time increment. After each time increment, at the completion of the lengthwise recursive calculations, a new projectile velocity v_p^t can be computed by means of a momentum balance using the tension at the first node:

$$-zT_{y} = M_{p} \frac{\Delta v_{p}}{\Delta t} = M_{p} \frac{v_{p}^{t} - v_{p}^{t-1}}{\Delta t}$$
(58)

where $\stackrel{M}{p}$ is the projectile mass, $\stackrel{T}{y}$ is the component of fiber tension in the projectile travel direction, and the factor 2 accounts for the other half of the primary fiber extending in the -x direction. $\stackrel{T}{T}_{y}$ is:

$$T_{u} = T_{1}^{t} \cos \theta_{1}^{t} = T_{1}^{t} \cos \left\{ T_{an} \frac{y_{1}^{t} - y_{2}^{t}}{y_{1}^{t} - y_{2}^{t}} \right\}$$
(59)

<u>Crossover Fiber Calculations</u>. Computation of field variables along the secondary fiber proceeds in a lengthwise manner exactly as described above, although the vector resolutions become slightly more complicated due to the motion in three rather than two dimensions. The secondary algorithm is started by imposing on the first node of the crossover fiber the velocity imparted to it by the primary fiber. As stated earlier, the secondary fiber is allowed a measure of slip along the primary fiber but is constrained to follow it in the direction normal to the primary fiber. Denoting the node on the primary fiber nearest the crossover point as ix, the velocity of this node resolved in directions parallel and perpendicular to the primary fiber there

$$U_{\text{para}}^{\dagger} = \mathcal{U}_{ik}^{\dagger} \cos \theta_{ik}^{\dagger} + \mathcal{U}_{ik}^{\dagger} \sin \theta_{ik}^{\dagger} \qquad (60)$$

$$v_{\text{perp}}^{t} = v_{ix}^{t} \cos \Theta_{ix}^{t} - u_{ix}^{t} \sin \Theta_{ix}^{t} \qquad (61)$$

$$\Theta_{ix}^{t} = Tan \frac{y_{1ix}^{t} - y_{1}t}{x_{ix}^{t} - x_{1}t}$$
(62)

In equation 62, the notation of the form yl or y2 indicates field variables for the primary and secondary fibers, respectively. The velocity imposed on the first (crossover) node of the secondary fiber is:

$$Mz_{1}^{t} = \alpha \mathcal{N}_{para}^{t} \cos \theta_{ix}^{t} - \mathcal{N}_{perp}^{t} \sin \theta_{ix}^{t} \quad (63)$$

$$Nz_{1}^{t} = \alpha \mathcal{N}_{para}^{t} \sin \theta_{ix}^{t} + \mathcal{N}_{perp}^{t} \cos \theta_{ix}^{t} \quad (64)$$

$$2 \mathcal{N}_{1}^{t} = 0 \quad (65)$$

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where \mathcal{X}_{s} is a slide factor which permits no sliding when set to 1 and unrestrained sliding when set to zero. ないないないないというないないないないないないでもないといういろうでいないないないでものできょう

The crossover node ix will change with time if the tangential slip along the primary fiber is sufficient. After each time increment, a new position of the first node on the secondary fiber is computed, and ix is assigned to the nearest node on the primary fiber.

The momentum-balance calculation of y_{i+1}^t in the primary fiber must be modified when the $i+1^{st}$ node is also the crossover node ix, since the secondary fiber applies its own tension to that node. Denote the direction angles of the primary and secondary fibers at that node as ϕ_1 , ϕ_1 , ϕ_1 and ϕ_2 , ϕ_2 , ϕ_2 , respectively, (ϕ_1 = 0). Then the components of tension applied by the secondary fiber, resolved along directions parallel and perpendicular to the primary fiber, are:

 $Tz_{para}^{t} = Tz_{1}^{t} \left[\cos \varphi_{\chi} \cos \varphi_{\chi}^{t} \cos$

where the direction cosines are computed from the current nodal coordinates. The primary fiber is allowed to feel the impulse of the perpendicular component fully, but the parallel component is reduced by the slide variable α_s . The usual computation of y_{i+1}^t is the adjusted as

$$\mathcal{M}_{i+1}^{t} - \mathcal{M}_{i+1}^{t} + ZA[TZ_{perp}^{t} \cos \phi_{1}_{N}] + \alpha_{s}TZ_{para}^{t} \cos \phi_{1}_{N}]^{(68)} + \alpha_{s}TZ_{para}^{t} \cos \phi_{1}_{N}]^{(68)} + \alpha_{s}TZ_{para}^{t} \cos \phi_{1}_{N}]^{(69)} + \alpha_{s}TZ_{perp}^{t} \cos \phi_{1}_{N} \qquad (69) + \alpha_{s}TZ_{para}^{t} \cos \phi_{1}_{N}]$$

where the - symbol indicates a computer replacement operation; i.e. the additional impulse from the secondary fiber is added to that already computed from equations 63 and 64. Stability, Accuracy, and Efficiency. Criteria for stability and accuracy of the above method are related as in the fabric case to the theory of characteristics for hyperbolic systems of partial differential equations and are similar to those for finite-difference solutions of wave propagation problems [14]. Given a wave equation of the form

$$\partial^2 \mathcal{M} / \partial t^2 = c^2 \left(\partial^2 \mathcal{M} / \partial x^2 \right) \tag{70}$$

which is to be solved by approximating $\exists t$ and $\exists x$ by finite differences Δt and Δx , a stability ratio & can be defined as

$$\alpha = c \left(\underbrace{A_{k}}_{\Delta \pm} \right)$$
(71)

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The finite difference scheme is stable and accurate for

 $\alpha = 1$, stable but increasingly inaccurate for $\alpha < 1$, and unstable for $\alpha > 1$. The choices for Δx and

 Δ t are thus not independent, but are related by the wavespeed for the choice of $\alpha = 1$.

In the direct analysis of the fibers described above, this stability criterion is equivalent to adjusting the rate of march of the computer solution along the fiber to match the rate of propagation of the strain wave. Conceptually, this requirement is related to the necessity of programming the finite governing equations so as to model the actual continuous dynamic process as accurately as possible. If a major disturb-

ance - such as the passage of a strain wave with its accompanying energy input - takes place in a finite element which is not considered explicitly in the computational scheme, divergent numerical results are very likely.

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Once a stable computational scheme has been developed, one usually attempts to increase its accuracy to whatever limit is desired by decreasing the size of the elements; 1.e. by increasing the number of nodes. Since for $\mathcal{X} = 1$ a decrease in Δx requires a corres- Δt , the computation time - and ponding decrease in therefore the expense - required for analysis of a given impact event increases as the square of the number of nodes. The element size is therefore chosen so as to balance the conflicting requirements of economy and accuracy. As an example of computation time, the CPU requirement for the IBM 370/168 system was 0.168 minutes for a problem in which the strain wave propagated 0.2 m along the primary fiber and 0.1 along the secondary fiber, with a length increment of 2.0 mm. As a means of improving code efficiency, the program employs logical flags which terminate the length loop computation when the computer passes the point along the fiber length corresponding to the wavefront.

Accuracy assessment for the case of two crossed fibers is difficult, since no experimental or closedform mathematical analysis of this problem is available, but some assurance of accuracy is derived from computer runs in which the secondary fiber is placed at the origin (the impact point). In this case, response of both the primary and secondary fibers is found to be that predicted by independent analyses. Data such as that previously presented in Figure 23 is obtained along the primary and secondary fibers. In certain cases to be discussed below, the numerical overshoot and oscillation observed near wavefronts cause problems in interpretation of results. These oscillations are a result of the inability of the discrete difference equations to model discontinuities accurately. Although the method is conditionally stable and the oscillations are damped out away from the discontinuity, problems of interpretation remain near the discontinuity. The oscillation at the wavefront is diminished by the material viscosity, and in some cases an "artificial" viscosity may be included solely for the purpose of smoothing the numerical results.





Figure 35. Strain distributions in two crossed fibers of Kevlar 29, 28.7 microsec after impact at 400 m/sec.

Figure 35 shows typical results obtained from the above described computer treatment, in this case for two crossed fibers of Kevlar 29, the crossover point being 10 cm along the primary fiber from the impact point. The fibers were assumed to respond elastically, and no sliding was permitted at the crossover ($\alpha_s=1$).

The figure shows the distribution of strain in each fiber 28.7 pasec after impact at 400 m/sec, where the abscissa measures the distance along the secondary fiber from the crossover point. The dotted line at strain = 1.45% depicts the level of strain which would be generated in a single fiber at this impact velocity. In this example no viscosity has been included, and the large overshoot at the wavefront causes problems in interpretation of results. In spite of this oscillatory behavior, however, an increase in strain in the primary fiber behind the crossover due to the wavelet reflected from the crossover is evident, as is a reduction in the strain intensity in the region of the primary fiber beyond the crossover. More easily measured is the level of strain intensity propagated along the secondary fiber.

Computer experiments were conducted on the crossover system for a range of fiber moduli and slide factors, and graphical output similar to Figure 35 used to determine coefficients of wave reflection, transmittance, and diversion. These coefficients are defined as that fraction of the outward-propagating strain wave which is reflected backwards by the crossover, the fraction which passes through the crossover and continues its outward propagation, and the fraction which is . diverted and begins propagating along the fiber passing

transversely through the crossover. As a means of obtaining these coefficients in spite of the uncertainties caused by the numerical fluctuations near the wavefronts, the computer was asked to determine the average strain level over a portion of the fiber length away from the oscillation region. In order to guarantee conservation of energy, the sum of the squares of the above three coefficients should equal unity; this was in fact obtained and offers some assurance as to the accuracy of the numerical values.







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The variation in the transmission and diversion coefficients with fiber modulus is shown in Figure 36. The coefficient of reflection was near 1% over this range of moduli, but showed considerable scatter. It is seen that the diversion coefficient is of a much larger magnitude than the reflection coefficient, and that it varies more strongly with the fiber modulus. The major portion of the crossover influence on wave propagation is thus ascribed to diversion rather than reflection. ar or realized to the static of the second static of the second second second second second second second second

This observation is of significance, since an approximate treatment of fabric impact by Freeston and Claus [23] sought to predict the increase of strain at the impact point by considering wave propagation along a single fiber which reflects a certain portion of the outward-propagating wave at a series of discrete points along its length. The analysis is then reduced to a bookkeeping procedure in which one keeps track of inward and outward-propagating waves in each of the elements between these reflection points. This scheme leads to a very simple computer code and one would hope that it could provide at least approximate guidance in design.



Figure 37. A comparison of the reflection-only bounce model for wave propagation in an impacted fabric, in comparison with the fabric model of this report.

Unfortunately, it appears that the reflection-only model predicts much too high a strain level, except at times very early in the ballistic event. Figure 37 shows the impact-point strain history as predicted by the reflection-only model for a 400 m/sec impact on a Kevlar 29 panel with 1575 yarns/m (the curve developed by the "BOUNCE" code). This prediction is compared

with that of the more general code described earlier (the curve labeled "FABRIC"). At very short times, the BOUNCE code results are likely superior, as they give strains equal to that developed in a single transverselyimpacted fiber; the Fabric code shows a numerical lag in the development of strain. The two codes achieve similar values at near 1.5 microseconds, but after this the bounce code increases rapidly to unreasonably high values of strain and thus predicts penetration too early. It is interesting, however, that the value of the reflection coefficient chosen by Freeston and Claus in order to bring their model into line with experiment was very nearly that found explicitly in the crossover study (0.01).

As the slide factor \mathcal{A}_{s} decreases from unity toward zero, representing less fiber-fiber friction at crossover points, one would expect that the reflection and diversion coefficients would approach zero and that the transmission coefficient would approach unity. At $\mathcal{A}_{s} = 0$, there is no coupling between the two fibers (until the arrival of the transverse kink wave, which generally occurs later than the arrival of the longitudinal wave). As seen in Figures 38, 39 and 40, respectively, for Kevlar 29 fibers, this trend is quantified by the results of the crossover computations.



Figure 38. The influence of fiber-fiber sliding on the fraction of stress wave intensity which is reflected at fiber crossovers, as indicated by computer experiments on Kevlar 29 fibers.



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Figure 39. The influence of fiber-fiber sliding on the extent to which a portion of the propagating stress wave is diverted from the primary fiber to begin propagating along the transverse secondary fiber.



Figure 40. The influence of sliding on the extent of stress wave intensity propagated beyond fiber crossovers.

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In principle, it would be possible to include the effects of fiber-fiber slippage in the two-dimensional fabric code by incorporating the formulae of this present chapter into the general code. Such an incorporation, however, would likely render the fabric code so much slower as to be uneconomic. In addition, one has at present no real means of assessing the slide parameter \mathcal{K}_{s} needed for the computation. It might be possible, however, to adjust the viscosity of the
material model artificially in order to produce results similar to those cause. by fiber slippage. This method would be similar to that employed during wave propagation calculations in geometrically dispersive composites [24]. If this approach is pursued in the future, the data of Figures 38-40 will be useful in providing guidance as to the desired effect. As a final comment on this work, it may be stated that the FABRIC impact code provides a simulation of impact on textile fabrics which is already of sufficient accuracy that inclusion of the fiber crossover effects would not be considered necessary, at least in the case of tightly woven panels which do not exhibit extensive fiber slippage during impact.

Sec. 3. 15.

CONCLUSIONS

The numerical analyses described in this report offer a means whereby the designer of personnel armor may perform computer-aided design and analysis of what up until now has been an impossibly intractable problem. Perhaps as useful as the ability to perform such analyses, however, is the extent to which the armor designer's intuition of the mechanics of penetration is enhanced by this tool. These numerical codes

are easily implemented on any modern computer system, and run very economically. They are also extremely amenable to user modification in order to permit easy implementation of various constitutive laws, fracture models, etc.

Certain areas still exist, however, for significant improvement in this treatment. First, the codes are presently limited to zero-obliquity impact by a projectile whose lateral dimensions are small compared with the region of influence during impact. Relatively minor code modifications would be necessary to include oblique impacts by large and arbitrarily shaped projectiles. In this manner the influence of projectile geometry could be modeled. Second, and more important, is the necessity to incorporate more accourate models of material response. As was demonstrated within this report, rather sophisticated constitutive and fracture algorithms can be implemented within the codes with no serious difficulties. More work is needed, however, to determine the extent to which these or other models are applicable to fabric response in the ballistic time frame, and to determine the numerical parameters to be used in the models.

Two examples of this latter problem may be repeated here. First, recall that the treatment of nonlinear

viscoelastic effects was limited not by the code capability, but by the present lack of understanding as to which of several possible nonlinear constitutive laws would most accurately model ballistic response. Regardless of the model selected, work is required to obtain experimentally the numerical data required as input parameters.

Second, the otherwise very successful materials parametric study described in the report is deficient in that it predicts that Kevlar 29 should far outperform Kevlar 49. In fact, the two aramid fabrics perform almost equally well, and some evidence suggests that Kevlar 49 is actually superior. The authors have no doubt that this discrepancy lies not in the wavepropagation aspects of the code predictions, but in the dynamic failure criterion used. Micrographs of ballistically-fractured fibers show extensive fibrillation, and evidence exists which suggest that Kevlar 29 and 49 differ primarily in their extent of fibrillation during fracture. Experimental work aimed at elucidating the nature of the fracture mechanism is needed; incorporation of the resulting information into the penetration codes should follow without difficulty.

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APPENDIX A - The FABRIC Code

<u>General</u>. FABRIC is a FORTRAN coding of the numerical analysis of fabric impact which was described in Chapter II. In its present form, the code is restricted to zero-obliquity impact on an orthogonal fabric mesh consisting of only one fiber type. These constraints could be relaxed through suitable code modifications. The code was developed and implemented on MIT's IBM 370/168 computer system, but was later implemented without difficulty on the NARADCOM computer. The code was run at MIT in a batch mode, but could easily be modified for interactive terminal operation: this would likely consist primarily of adding terminal queuing for data input and graphical display for output data.

<u>Code input and output</u>. The input data needed by FABRIC is detailed in a series of comment lines at the beginning of the code listing. Briefly, these include specification of the impact velocity and projectile mass, the fabric idealization (principally the number of fibers per unit length), the constitutive and fracture properties of the fibers, and such run paramaters as maximum alloted time and printing increment.

A typical data input set, for a 300-m/sec impact on a nylon panel is given below:

LINEAR VISCOELASTIC FABRIC (BALLISTIC NYLON) 1.1 300. 19.533 10.16 5280 0.14 0.0 2. 1.4142 1. 3 100. 0.2 5. 36 1 1

Code output consists first of a series of values relative to the initial conditions which were read in and which the computer requires in order to begin the recursive calculations.

After each time increment (or less often, depending on the value used for the print skip increment INC), the code prints the current values of the field variables at each node in the fabric octant. Currently, these are simply dumped in order of the calculation scheme as defined by Figure 10. This presentation of data has been sufficient for the research studies discussed in this report, but for production design work, graphical or some other high-order output would likely be prefer-

able. The output for the first time increment of the above 300 m/sec nylon impact is given below for illustration. Tl0 and T01 are the tensions in the two orthogonal fibers passing through a node as shown in Figure 9, EPS10 and EPS01 are the corresponding strains, VZ is the transverse velocity and XCD and ZCD are the x- and z-coordinates of the i,j node. This print also presents the current time after impact, the current projectile velocity, the energy lost by the projectile and the partition of impact energy into a strain and kinetic components within the fabric. Clearly, a great deal of data is made available by the code, and the user should modify the output format so as to provide the most convenient display of results for his needs.

EXECUTION BEGINS... 1LINEAR VISCOELASTIC FABRIC (BALLISTIC NYLON)

INPUT PARAMETERS: YARN DENIER, DENYRN (DEN)= 0.52800E+04 INITIAL PROJECTILE VELOCITY, VPROJ (M/SEC) = 0.30000E+03 PROJECTILE MASS, PMASS (GM)= 0.11000E+01 FABRIC PANEL LENGTH XL (CM)= 0.10160E+02 ELEMENT LENGTH DXL, (CM)= 0.29029E+00 MAXIMUM IMPACT DURATION TMAX (MICROSEC)= 0.20000E+01 STABILITY COEFFICIENT, CDTM= 0.14142E+01 INCREMENTAL TIME DTM (MICROSEC) = 0.69116E+00 NUMBERS OF LAYERS, CLYR= 0.10000E+01

STRAIN WAVE VELOCITY CWAVE(M/SEC) = 0.29698E+04 INITIAL MODULUS OF YARN, EYRN(GR/DEN) = 0.10000E+03 BACK UP ELASTIC SPRING CONSTANT XK (GR/CM/CM) = 0.0

NUMBER OF NODES ALONG MODEL PANEL, JT= 36 NUMBER OF TIME INCREMENT STEPS, NTINC= 2 PRINTING FREQUENCY, INC= 1

ACTUAL FABRIC MASS, FMASSA (GM)= 0.19533E+02 MODEL FABRIC MASS, FMASSM (GM)= 0.16689E+02 CRIMP=FMASSA/FMASSM= 0.11704E+01 UNIT ELEMENT MASS *9.E05 (UNITM)= 0.35877E+04 HALF UNIT ELEMENT MASS *9.E 05 (HUNITM)= 0.17938E+04

INITIAL PROJECTILE KINETIC ENERGY, XKE (JOULE/GM)= 0.25342E+01

MATERIALS PROPERTIES: OPTION--MATERIAL MODEL, IPT= 3 INITIAL MODULUS, EYRN(GR/DEN)= 0.10000E+03

VISCOELASTIC MODEL---STANDARD LINEAR SOLID PARAMETER MODEL GLASSY MODULUS (GPD)= 0.10000E+03 MODEL VISCOUS FRACTION= 0.20000E+00 MODEL RELAXATION TIME(MICROSECONDS)= 0.50000E+01

RUPTURE STRAIN OF INDIVIDUAL FIBER, EPSB= 0.14000E+00

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0.69116E+00
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LIME	PROJ VEI	L PKOJ ENGY	LOSS FARKC ENC	3Y GAIN PACK	JP ENGY STRA	IN ENGY K.E.	Z*X*X	
0.69116E+(T10 (IX,IY)=	00 0.30000E+	03 0•46730E-	-04 0.91894E-	-02 0.0	0.56979E	-02 0.0	0.0	•91837E-02
0.24854E+00	0.0	0.0	0.0	0.0	0.0	0.0	0.0	
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	
0.0	0.0	0.0	0.0	0.0	0.0			
0.0	0.0	0.0	0.0	2	•			
TO1()X5,UY)=			8					
0.24854E+00	0.0	0.0	0.0	0.0	0.0	0.0	0.0	
0.0	0.0	0.0	0.0	0.0	0.0			
0.0	0.0	0.0	0.0	0.0	0.0	0.0		
0.0	0.0	0.0	0.0	0.0	0.0	0.0		
0.0	0.0	0.0	0.0	•				
	k 1	1 1						
0.30000E+03	0.0	0.0	0.0	0.0	0.0	0.0	0.0	
0.0	0.0	0.0	0.0	0.0	0.0	0.0		
0.0	0.0	0.0	0.0	0.0	0.0			
0.0	0.0	0.0	0.0	0.0	0.0	0.0		
XCD(I+7)=				:				
0.0	0.29029E400	0.58057E+00	0.87086E+00	0.11611E+01	0.14514E+01	0.17417E+01	0.203206401	0.232236401
0.26126E+01	0.27029E+01	0.31931E+01	0.34834E+01	0.37737E+01	0.40640E+01	0.43543E+01	0.46446F+01	0.493495401
0.52251E+01	0.55154E+01	0.58057E+01	0.60960E+01	0.63863E+01	0.66765E+01	0.496695401	0.725715401	0.75474F401
0.783775+01	0.81280E+01	0.84183E+01	0.87086E+01	0.89989E+01	0.928916401	0.95794F+01	0.986975401	0.101405402
ZCD(I,J)=								
0.207355-01	0.0	0.0	0.0	0.0	0.0	0.0	0*0	0.0
0.0	0.0	0.0	0.0	0.0	0*0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0	0.0	
EPS10(KX,KY)=								
0.25473E-02	0.0	0.0	0.0	0.0	0.0	0.0		
0.0	0.0	0.0	0.0	0.0	0.0			
0.0	0.0	0.0	0.0	0.0	0.0			
0.0	0.0	0.0	0.0	0.0	0.0			
0.0	0.0	0.0	0.0	1				
EPS01(LX,LY)=			5 -					
0.25473E-02	0*0	0.0	0.0	0*0	0.0	0.0	0.0	
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	
0.0	0.0	0.0	0.0				•	

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<u>Program Requirements</u>. In its present form, the FABRIC code is self-contained, needing no external software support. All its subroutines, for instance, are contained within the listing given below. One qualification to this statement however, is the inclusion of a call to Subroutine UERTST within the nonlinear equation-solving subroutine ZNOLNR. UERTST is an errorhandling routine available through the proprietary "International Mathematics and Statistics Library" (IMSL). If IMSL is not available at the user's location, the call to UERTST could be removed with little risk: no error-handling capability was needed during any of the computer experiments described in the body of this report.

FABRIC needs no tape or disk support; all computations are performed directly within core. Core requirements and run times are dependent both on problem specifications and on the computer system, but by way of illustration some parameters observed during a typical run on the IBM 370/168 system will be mentioned. During an impact simulation of a Kevlar 29 single layer at 300 m/sec, the computed time-to-penetration was

42.87 Asec. The panel was idealized as having a fiber spacing of 0.3175 cm, and the time step for optimum code stability was 0.32234 Asec. A total of 133 time increments was therefore necessary for the run, with each time increment involving an additional node relative to the previous step. The total run time for this job was 1.089 minutes (\$12.92 at weekend rates), and a total of 182 kilobytes of CPU core was required. When this same problem was run at NARADCOM, 3 min 50 sec of CPU time was required, which illustrates the system dependency of such job parameters.

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• • FAB0003 • FAB0003	FAB000 FAB000 FAB000 FAB000 FAB000	• FABOO1	FABOOL	• FAB001	• FA8001 • FA8001 • FA8001 • FA8001	FABOO2	- FAB002 FAB002 FAB002 FAB002 FAB002	• FAB003	• FABOO3 • FABOO3 • FABOO3 • FABOO3 • FABOO3	• FAB003	• FAB004	• FA8004	- 143004 - 143004 - 143004 - 1480094	• FABAG5	COU824 .
• • • • • • • • • • • • • • • • • • •	RICAL SOLUTICN OF THE FIELD EQUATIONS Liquity Ballistic Impact of an Orthogonal	INPUT VARIABLES	HEADING (23A4)	METERS (5E15.5)	PROJECTILE MASS (GM) INITIAL PROJECTILE VELOCTTY (M/SEC) Actual Fabric Mass (GM) Fabric Panel Length (CM) Yarn Denier	ETERS (SELS.5)	YARN BREAKING STRAIN ELASTIC SPRING CONSTANT (GMF/SQ CM) Maximum time (Microsec) Stability Coefficient (.Ge. 1) Number of fabric layers in Panel	IVE LAW OPTION (15)	 EQ. 1 NONLINEAR (CUBIC POLYNOMIAL) EO. 2 NONLINEAR (EXPONENTIAL) EQ. 3 STANDARD LINEAR SOLID EQ. 4 EYRING VISCOELASTICITY 	RDENING PARAMETERS (2E15.5) 1Pt .eq. 2)	PREEXPONENTIAL FACTOR (GPU) Strain Hardlaing Exponent	R POLYMOMIAL COEFFICIENTS (4E15.5) PT .eq. 1)	FIRST TERM (GPD) Second term (GPD) Third term (GPD) Fourth term (GPD)	LINEAR SOLID PARAMETERS (3E15.5) Pt .eg. 3)	
• • • • •	A DIRECT NUME. FOR NORMAL-OSI FAGRIC MESH	DEFINITION OF	I. PROBLEM I	2. RUN PARA	PMASS VPRDJ FMASSA XL Denvrn	3. RUN PARAM	5Р58 ХК ТМ4Х СDTM CLYR	4. CONSTITUT	1 P T	5. STRAIN HA	EYRN CHARD	OR 5 . NONLINEA (IF I	60 61 63 63 63 63 63 63 63 64 64 64 64 64 64 64 64 64 64 64 64 64	DR 5. STANDARD (1f 1	

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F 4600720 F 4690730 COMMON/CMESH/XCD(40,40),YCD(40,40),ZCD(40,42),XCDDLD,YCDDLD,ZCDDLDFAB00860 COMMON/TEN/T10(43,40),T210(40,40),TX10(40,40),TX01(40,40), FAB00880 ETY10(40,40),TY01(40,40),T210(40,40),T201(40,40), FAB00890 EPS10(40,40),EPS01(40,40) COMMON/VELOC/VY(40,40),VV(40,40),V2(40,40) COMMON/VELOC/VY(40,40),VV(40,40),V2(40,40) COMMON/ERGCUM/XKNCY,YKNCY,ZKNRCY,SNRGY COMMON/ERGCUM/XKNCY,YKNCY,ZKNRCY,SNRGY COMMON/ERGLM/KE(40,40),ELSE(40,40),TLELEN(40,40) FAB00920 FA800560 FAB00570 FAB00580 FAB00590 FAB006C0 FAB00610 FAB00620 FA803630 FA800640 FAB00650 FA800660 FA800670 FAB00680 FAB00690 FAB00700 FAR00710 FABO0740 FAB00750 FAR10760 FAB00770 FAB0C780 FAB00790 FAB00800 PMASS, CRIMP, FMASSA, FMASSM, FFAB00810 FADC0820 COMMON/TSNDLD/T1CDLD(40,40),T010LD(40,40),E100LD(40,40),E010LD(40,FAB00830 FA800840 FAU00850 FAB03930 FABC0940 FAB00950 FA800960 FAB0C970 FAB00980 FAE00990 DENYRN, EPSB, XK, TMAX, CDTM, CLYRFAB01000 **FAB01010** FAB01020 FAB01030 FAB01040 FAB01050 FAB01060 FAB01070 NUMBER OF NODES ALONG PANEL LENGTH EQUILIBRIUM SPRING CONSTANT (GPD) SECOND SPRING CONSTANT (GPD) EYRING COEFFICIENT (1/SEC) EYRING EXPONENTIAL (1/GPD) MODEL VISCOUS FRACTION (.LE. 1) EYRING NONLINEAR VISCOELASTICITY (SE15.5) MESH DENSITY AND PRINT INFORMATION (315) VISCOUS FRACTION (.LE. 1.) RELAXATION TIME (MICROSEC) PRINT SKIP INCREMENT • EQ. 0 DATA CHECK DNLY • EQ. 1 EXECUTION READ AND PRINT INPUT PARAMETERS And compute internal control parameters COMMGN/CMA1L/EYRN,CHARD,EO,E1,E2,E3 COMMGN/V1SCO/G,VLAMDA,TAU COMMGN/NONLR/EN1,EN2,A,ALP,VLBD •
•
•
• COMMON/VARBL/JT,XL,DXL,DTM,DENYRN, EMASSF,UNITM,HUNITM FORMAT (2044) READ(5,1) PMASS,VPROJ,FMASSA,XL, (IF IPT .EQ. 4) REAL#8 ENL, ENZ, A, ALP, VLBD COMMON/IXMATL/IPT EORMAT(1615) GO TO (31,32,33,34), IPT READ(5,41 EVRN, CHARD VLAHDA TAU DIMENSION HED (20) READ (5,120) NED ALP VLBD COMMON/BACKUP/XK NC EN2 ENI 5 FORMAT(SEL5.5] READ(5,3) IPT ٠ GO TO 39 5 Q g (073 in M 120 ပ္ပ υ ပပ ں υ ပပ

FAB01090 FAB01100

FA801080

READ(5,4) E0,E1,E2,E3

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FORMAT (SE15.5)

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DENYRN#XL)/9.JE UD
[FMASSN+CRIMP]
TMAX.CDTM.DTM.CLVR
{M/SEC)='.E14.5/
5/
. 5/
8056C)=••E14.5/
•5/
•,E14.5/
VE(M/SEC)=•,E14.5/
DEN)=',E14.5/
K (GK/CM/CM)=++E14+5)
ODEL PANEL, JT=*,13/

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64	<pre>EIX, NUMBER CF TIME INCREMENT STEPS, NTINC=',14/ EIX, PRINTING FREOUENCY,INC=',13) MRITE(6,64) FMASSA, FMASSM,CRIMP,UNITM,HUNITM FORMAT (//1x, ACTUAL FADRIC MASS,FMASSA (GM)=',E14.5/ EIX, MODEL FABRIC MASS, FMASSM (GM)=',E14.5/ EIX, MODEL FABRIC MASS FMASSM (GM)=',E14.5/ EIX, UNIT FLEMENT MASS *9.EO5 (UNITM)=',E14.5/ EIX, 'HALF UNIT FLEMENT MASS *9.E 05 (HUNITH)=',E14.5]</pre>	FAB91660 FAB01670 FAB01690 FAR01690 FAR01690 FAR01700 FAB01700 FAB01720 FAB01730
65	WRITE(0,65) XKF Format(//1x,"Initial projectile Kinetic Energy, XKE (joule/GM)="" G14.5)	FAB01740 EFAB01759 FAB01760
66	WRITE(6,66) IPT,FYRN Formati/ix,*Materials properties:*/ &ix,*OpticnMaterial Model, ipt=*,15/	FAB01770 FA801780 FA021790
66	<pre>GIX."INITIAL MODULUS, EYRN(GR/DEN)=".EI4.5/) IF (IPT.EQ.2) WRITE (6.661) EYRN, CHARD I FORMAT (/IX."EXPOXENTIAL STRAIN HARDENING"/ EIX."CDEFFICIENT, EYRN (SR/DEN)=".FI4.5/</pre>	FAB018CC FAB01810 FAR01820 FAR01820 FAB01830
. 66	<pre>EIX.'STRAIN HARDENING EXPONENT, CHARD=',EI4.5/) IF (IPT.E0.1) WRITE (6,662) E0.EI.E2.E3 FORMAT (/IX.'HONLINEAR FLASTIC MODEL CUBIC POLYNOMIAL'/ C'Y, 'EO /OCU/OFN'-1 EI' E/</pre>	FAB01840 FAB01850 FAR01860 FAR01860
	<pre>LIX, E1 (GR/DEW)=', E14.5/ LIX, E2 (GR/DEW)=', E14.5/ LIX, E3 (GR/DEW)=', E14.5/ LIX, E3 (GR/DEW)=', E14.5)</pre>	FAB01880 FAB01890 FAB01890
68	IF (IPT.60.3) WRITC(6,68) G.VLAMDA,TAU Format(/IX,'VISCGELASTIC MODELSTANDARD LINEAR SOLID PARAMETER' SIX, Kodel Classy Modulus (SPD)=',514.5/ SIX, Model Viscous Fraction=',514.5/	FABC1910 7FAB01923 FAB01930 FAB01930
69	<pre>List</pre>	FAB01950 FAB01960 FAB01970 FAR01960 FAR01990 FAR02000 FAR02000
67	hrite(6,67) EPS\$ Format(//ix,•Rupture Strain of Individual Fiber,EpSB≠•,E14.5/) If (mode.e0.0) Stop	FAR02020 FA802030 FA802030
	INITIALIZE FIELD VARIABLES Establish initial nodal coordinates	FAB02050 FA802060 FA802070 FA802070
*	DD 11 K≠1,40 DN 11 J=1,40 XCD(J,K)=(J-1)*DXL	FAB02090 FAB02100 FAB02110
	YCD(J,<)=(K-1)=DXL ZCD(J,K)=0.00C 00 VX(J,K)=0.00E 00	FA802120 FA802130 FA802140
	VY(J,K)=0.03C OC VZ(J,K)=0.03E 00 ELSE(J,K)=0.03E 20	F 4 B C 2 1 5 0 F 4 B C 2 1 5 0 F 4 B 5 2 1 7 C
	ELKE(J,K)=0.03F 39 Tlelen(J,K)=0.00F 00 T10(J,K)=0.00E 33	FA302180 FA802190 FAB02200

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FAB02290 FAB02300 FA802310 FA002320 FA002330 DVX=(TXI0(J+L,K+I)-TXI0(J,K+I)+TX01(J+L,K+I)-TX01(J+L,K))*DTM#8.82FA802690 600E 00/(2.00E 00*DXL#CRIMP) DVY=(TY10(J+1,K+1)-TY10(J,K+1)+TY01(J+1,K+1)-TY01(J+1,K))*DTM#8.82FAE02710 600E 00/(2.00E 00*DXL#CRIMP) 600E 00/(2.00E 00*DXL#CRIMP) 500E 00/(2.00E 00*DXL#CRIMP)+XK*DXL*2CD(J+1,K+1)*DTM#9.80E-06/(UNITFAB02760 600F 00/(2.00E 00*DXL*CRIMP)+XK*DXL*2CD(J+1,K+1)*DTM#9.80E-06/(UNITFAB02760 600F 00/(2.00E 00*DXL*CRIMP)+XK*DXL*2CD(J+1,K+1)*DTM#9.80E-06/(UNITFAB02760 600F 00/(2.00E 00*DXL*CRIMP)+XK*DXL*2CD(J+1,K+1)*DTM#9.80E-06/(UNITFAB02760 600F 00/(2.00E 00*DXL*CRIMP)+XK*DXL*2CD(J+1,K+1)*DTM#9.80E-06/(UNITFAB02760 FAB02220 FA802270 FAB02350 FA802390 FAB32450 FA802510 FAB02560 FAB02590 FAB02600 FAB02630 FAB02230 FAB02240 FAB02250 FAB02260 FAB02280 FAEn2340 FAB02360 A802370 FAB92380 FAB02400 FAB02410 FAB02420 FAB02430 FAB92440 FAB02460 FAB02470 FAB02480 FA002490 FA8025C0 FABJ2520 FAB02530 FA802543 FA8-02550 FAB02570 FAB02580 FA802610 FABC2620 FA802640 FAB02650 FAB02660 FAB02670 FAB02680 FAB02210 COMPUTE VELOCITY CHANGES FROM INPULSE-MOMENTUM BALANCE CALL BNDRY(IT,1,1) DO 14 IFRONT=2,NFRONT IF(IFRONT.LT.JT) CALL BNDRY(IT,IFRONT,1) NODES=!FKCNT/2 If{IFRONT-(JT+1)) 16,18,18 COMPUTE BOUNDARY VALUES EPSI0(J,K)=0.00E 00 EPSI0(J,K)=0.00E 00 T100LD(J,K)=0.00E 00 T010LD(J,K)=0.00E 00 E100LD(J,K)=0.00E 00 E210LD(J,K)=0.00E 00 C0NT1WUE KSTART = [FRONT-(JT-1) DD 22 K=KSTART,NODES TZ10(J,K)=0.00E 00 TX01(J,K)=0.00E 00 TY01(J,K)=0.00E 00 TZ01(J,K)=0.00E 00 sõ 8 [F(K.EQ.J) IDIAG=1 T01(J,K)=0.00C 00 TX10(J,K)=0.00E 0 TY10(J,K)=0.00E 0 [[M=DTM*FLOAT([T) FORTRAN BEGIN SPACE LODP DO 12 IT=1,NTINC YKNRGY=0.00F 00 ZKNRGY=0.00E 00 KKNRGY=0.00E 00 BEGIN TIME LOOP SNRGY=0.00E 00 V2(1,1)=VPR0J VFRONT= JTM1 #2 INCL=INCL+L J= I FRONT-K KSTART=1 **TO 20** [FLAG=0 FILE: FABRIC NC1=0 ខ្ង 81 11 2 ບບບູດ

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ļ	DVZ=-DVZ IF(ABS(DVX).GE.0.0001.OR.ABS(DVY ^{\.} GE.0.0001.OR.AES(DVZ).GE.0.0001F E) IFLAG=IFLAG+1	- 4802769 - 4802770 - 4802780
ں ر	COMPUTE NEW VELOCITIES	- AB02790 - AB02800
ن ن	F VX{J+1,K+1)=VX(J+1,K+1)+DVX	AB02810
	Vf(J+1,K+1)=VY(J+1,K+1)+DVY VZ(J+1,K+1)=VZ(J+1,K+1)+DVZ	: A B 0 2 B 3 0 : A B 0 2 B 4 0
	VX(JT+K+1)=0.00E 00	AB02850
	VY(JT*K+1)=0.00E 00 VZ/IT*K1)-0.00E 00	: AB32860
	VX(K+1 ~ 1+1)=VY(1+1 ~ K+1)	018224V
		AB02890
	VZ(K+1,J+1)=VZ(J+1,K+1) ISI/ISOQNI FI JIH), AND ///// SO JI) FO II) FO II)	AD02900
J	1	AB02920
COMP	UTE CHAMGE DF NODAL COGRDINATES FROM VELOCITIES	AB02930
נ		0562044
	YCD(J+1,K)=YC00LD	AB02960
	2CD(J+1,K)=2CDOLD	AB02970
	XCD(K+7+1)=XCD0FD	AB02980
	YCU(K,J+1)=XCOOL() 7CD(K, 1+1)±2CDD1D	AB02990
24	routing at a condito 10001 = (x(1) (4 1 , K 4 1) - X(1) (4 1 , K 1) ##0 + (X(1) (1 + 1) - X(1) 1 + 1 , K 1) ##0 + (X(1) (
	560(J+1.*X+1)-ZCD(J+1.*X)***********************************	0202080
	D1ST01=SQRT(D5Q01) F	AB33330
	DSQXUL=(XCD(J+1,K+1)+VX(J+1,K+1)*DTM/1.COE 04-XCD(J+1,K)-VX(J+1,K)F	AB03040
		AB03050
	U2010101-11001041011214710410410410410410414013/10000 00470010410410410410410410 640111/1 2006 041442	AB03060
	DSQ201=f2CD(J+1,K+1)+V2(J+1,K+1)*DTH/1.00E 04-2CD(J+1,K)-V2(J+1,K)F	AB03080
	&#DTM/1.00E 04)##2</td><td>060E08V:</td></tr><tr><td>ပ ပ</td><td>ECOMPUTE CHANGE IN ELEMENT STRAIN FROM NEW COORDINATES</td><td>AB03100</td></tr><tr><td>J</td><td></td><td>AB03120</td></tr><tr><td></td><td>DDST01=SCRT(DSQX01+DSQY)1+DSQ201)</td><td>AB13130</td></tr><tr><td></td><td>UEPS=UUSTUI/0IST91-1.60E 00 EDSA111-1.41.41.41.41.41.41.41.41.41.41.41.41.41</td><td>A803140</td></tr><tr><td></td><td>TFIIDEAG-FD.1) 66 TD 26</td><td>0010000</td></tr><tr><td></td><td>EPS10(K, J+1)=EPS31(J+1,K)</td><td>AB03170</td></tr><tr><td>26</td><td>DSq10={XGD(J+I,K+I)-XCD(J,K+I),**2+(YCD(J+I,K+I)-YCD(J,K+I))**2+(ZF</td><td>AB03180</td></tr><tr><td></td><td>€¢UV(JTL0TL0TL)TL)=CUU(J0K+L))**2 D1ST10=SDTLDSD10)</td><td>AB03150</td></tr><tr><td></td><td>DSQXID=[XCD(J+1,K+1)+VX(J+1,K+1)*DTM/1.00E 04-XCD(J,K+1)-VX(J,K+1)F</td><td>AB03210</td></tr><tr><td></td><td><pre>6#0TM/1.00E 04)##2</td><td>AB03220</td></tr><tr><td></td><td>ひひぜ ちぐー いちひし ひとて マンド・イント マント・シント シントドライ ドランド 。くじに くよー こくひょう メビット シント ビック イビック たんしん ノム りんた つん しん マント・アント たんしん イント・シント アンド・シント アンド・シント アンド・シント アンド・シント</td><td>ARD3240</td></tr><tr><td></td><td>DSQ210=(2CD(J+1+K+1)+VZ(J+1+K+1)*DTM/1.00E 04-2CD(J+K+1)-VZ(J+K+1)F</td><td>A803250</td></tr><tr><td></td><td></td><td>AB03260</td></tr><tr><td></td><td></td><td>AB03280</td></tr><tr><td></td><td>EPS10(J,K+1)=EPS10(J,K+1)+DEPS F</td><td>AB03290</td></tr><tr><td></td><td>EPSO'1(K+1,J)=EPSIG(J,K+1)</td><td>ABJ33CO</td></tr></tbody></table>	

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FAB033104 FAB03340 FAB03320 FA303330 FAB03350 FAB03360 FAB03370 FAB03380 FAB03390 FAB03400 FA893410 FAB03490 FAB03500 FAB03420 FAB03430 FA803440 FAB03450 FAB03460 FAB73470 FABC3480 FA833510 FAB03520 FAB03530 FAB03540 FAB03550 FAB93560 FAR03570 FABA3580 FAB03590 FAB03600 FABC3610 FAB03620 FAB03630 FAB03640 FAB03650 FABC3560 FAB03670 FARC3680 FAB03650 FA803730 FAB03710 (VX(J,K+1)**2+VYFAB03720 FAR03730 (VX (J+ [• K) **2+VFABC3740 FA803750 FAB03760 FAB03770 FAB03780 FAB03790 FAB03800 FAB03810 FAB03820 FA003830 FAB03R40 FAU03850 CALL TENSN(IT, JP1, K, EPSLNY, TSLY, EPYOLD, TSYOLD, DSNRGY) CALL TENSN(IT, J, KP1, EPSLNX, TSLX, EPXOLD, TSXOLD, DSNRGY) CALL TENSN SURROUTINE TO COMPUTE ELEMENTS TENSION FROM ELEMENT STRAIN OR STRAIN HISTORY ELKE(J+1,K)=ELKE(J+1,K)+0.500E-03*HUNITM# ELKE(J,K+1)=ELKF(J,K+1)+0.50E-03*HUNITM* EY(J+1,K)**2+V2(J+1,K)**2)/(FMASSF*CRIMP) If(J.GT.1.AND.K.FQ.1) BSEM=0.500F 00 SNRGY=SNRGY+DSNRGY*(2-IDIAG)#BSEM ELSE(J+1,K)=ELSE(J+1,K)+DSNRGY/4.00E 00 £(J,K+1) **2+V2(J,K+1) **2)/(FMASSF*CRIMP) ELSE(J,K+1)=ELSE(J,K+1)+DSNKGY/4.CCE 00 IF(K.EQ.1.AND.J.LT.JT) BKEXYK=0.50E 00
IF(J.EQ.1.AND.K.LT.JT) BKEXYJ=0.50E 00 TLELEN(J,K+1)=ELSE(J,K+1)+ELKE(J,K+1) TLELEN(J+1,K)=ELSE(J+1,K)+ELKE(J+1,F') TLELEN(K,J+1)=TLELEN(J+1,K) COMPUTE KINETIC AND STRAIN ENERGIES E100LD(), K+1)=EP XDLD E010LD(K+1,)]=E100LD(), K+1) 1f(J.EQ.1.AND.K.EQ.1) G0 T0 51 SNRGY=SNRGY+DSNRGY+(2-101AG) :010LD(K,J+1)=TJ10LD(J+1,K) :010L0(J+1,K)=EPY0L0 roloco(K+1,J)=T100LD(J,K+1) TLELEN(K+1,J)=TLELEN(J,K+1) E100LD(K, J+1)=E010LD(J+1,K) ELKE (K, J+1)=ELKE (J+1,K) ELSE(K, J+1) = ELSE(J+1,K) ELSE(K+1,J)=ELSE(J,K+1) ELKE(K+1,J)=ELKE(J,K+1) T10(K,J+1)=T01(J+1,K) T01(K+1,J)=T10(J,K+1) 010L0(J+1,K)=TSY0LD FPX0L0=E100LD(J, K+1) EPSLNY=EPS01(J+1,K) EPYOLD=E010LD(J+1,K) TSYOLD=T010LD(J+1,K) T100LD(J,K+1)=TSXCLD SXOLD=T100LD(J,K+1) EPSLNX=EPS1J(J,K+1) YCDOLD=YCD(J, K+1) zcoolo= zco(J, K+1) XCD0LD=XCD(J,K+1) '01 (J+1 ,K)=TSLY T10(J,K+1)=T5LX DKEXYK=1.00E 00 BKEXYJ=1.00E 00 20 306-1-M320F 1+[=141 KPl=K+1 51 υυυυ υυυ

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&#VX(J。K+1)*#2)/(FMASSF#CRIMP) VKNRGY=YKNRGY+4.COE 00#0.50E-03#HUNITM#(BKEXYK#VY(J+1.K)##2+BKEXYJFAD03880 XKNRGY=XKNRGY+4.0CE 00#0.50E-03#HUNITM*(BKEXYK#VX{J+1,K}#*2+BKEXYJFABJ3860

XKNRGY=XKNRGY+4.00E 03*0.50E-03*HUNITM*(BKEXYK*VX(K,J+1)**2+BKEXYJFAB03930 YKNRGY=YKNRGY+4.00E 00#0.50E-03#HUNITM*(BKEXYK*VY(K,J+1)**2+BKEXYJFAB03950 FA803920 FA003940 FAB03960 FAB03970 FA803930 FAB03990 FA8040C0 FAB04010 FAB04020 FAB04030 FA804050 FA804040 FAB04060 FA604970 FAB74080 FAB04090 FAB04100 FAB04110 FAB04120 FABC4130 FAB04140 FABr4150 60 2 FAR94180 FAB04190 FAB04200 FAB04220 FAB04230 B1=ATAV(((XCD(J+I,K+1)-XCD(J,K+1))**2+{YCD(J+1,K+1)-YCD(J,K+1))**2FABO4240 FAB04250 FAB04260 FABC4270 FABC4280 FAB04290 FA8043C0 FAC04310 FAB04320 FA004330 FAB942 FA8941 FAB041 A1=ATAN({YCD{J+1,K+1}-YCD{J,K+1}}/Y(XCD{J+1,K+1}-XCD{J,K+1}) ā2=ATAN({YCD(J+1,K+1)-YCD(J+1,K))/{XCD(J+1,K+1)-XCD(J+1,K)}) IF(ABS(XCD(,J+1,K+1)-XCD(J+1,K))- 0.0001) 96,96,97 C05A2=0.00E 00 IF(ABS(ZCD(J+1,K+1)-ZCD(J,K+1))- 0.0001) 90,90,91 22 5 200 \$5 5 3 **5** 4 0 40 OBTAIN VECTOR COMPONENTS OF ELEMENT TENSIONS XCD(K+1,J)=XCD(K+1,J)+VX(K+1,J)+DTM/1.00E YCD(K+1,J)=YCU(K+1,J)+VY(K+1,J)+DTM/1.00E KCD(J+1,K)=XCD(J+1,K)+VX(J+1,K)*DTM/1.00E CC0(J,K+1)=ZCD(J,K+1)+VZ(J,K+1)+DTM/I.00E XCD(K,J+1)=XCD(K,J+1)+VX(K,J+1)*DTM/1.00E ZCD{K+1,J}=ZCD{K+1,J}+VZ{K+1,J}*DTM/1.00E /CD(J+1+K)=YCD(J+1+K)+VY(J+1+K)*DTM/1.00E CD(J+1,K)=ZCD(J+1,K)+VZ(J+1,K)*DTH/1.00E XCD(J*K+l)=XCD(J*K+l)+VX(J*K+l)*DTM/I*00E YCD(J*K+l)=YCD(J*K+l)+VY(J*K+l)*DTM/I*00E ZCD(K,J+1)=ZCD(K,J+1)+VZ(K,J+1)*DTM/1.00E YCD(K,J+1)=YCD(K,J+1)+VY(K,J+1)*DTM/1.G0E 6) ++0.53/(2CD(J+K+1)-2CD(J+1,K+1))) 6+VX(K+1, 3)++2)/(F4ASSF+CR[MP] 5#VY(K+1,J)*#2)/[FMASSF*CRIMD] STORE NEW NODAL COORDINATES [F[J.EQ.[K+1]) GO TD 40 [F1J.EQ.K) 50 TO 40 COSB1=0.07E 00 SINB1=1.00E 00 00 COSA1=COS(A1) SINBLESIN(B1) SINA1=SIN(AL) COSE1=COS(E1) COSA2=COS(A2) 5 INA2=1.00F GO TO 98 GO TO 92 ບບບຄຶ \$0 06 16 92 96 76

FAB04340 FA834350 FAB04360 [F[ABS[ZCD[J+1,K+1]-ZCD[J+1,K]]- 0.0001) 93,934 COSB2=0.00E 00 8 5 [NA2=5] N(A2] S [NB2=1.00E GO TC 95 986 93 40

FAB243 10 FABC438C <u>...</u>

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		C0582=C05(82)	FAB04410
		SINB2=SIN(B2)	FAB04420
	95	TX10{J*K+1}=T10{J*K+1}*S [NB1*COSA]	FAB04430
		TY10(J,K+1)=T10(J,K+1)*S1NB1#S1NA1	FAB04440
		TZ10(J,K+1)=T10(J,K+1)*COSB1	FAB04450
		TXO1(J+1,K)=T01(J+1,K)*STNB2#COSA2	FAB04460
		TYOL(J+1,K)=TJ1(J+1,K)*SIND2*SINA2	FAD04470
		T201(J+1,K)=T01(J+1,K)*C0592	FAB04480
			FAB04490
			FAB04560
			FAB04510
		- 0.1010/0/7414.0/14 - 1.4011/0/5741/ TV10/27 - 1411/-TV01/141/	F A D Q 4 3 2 U
			FABC42.30
			FABU454U
			FAB04550
			FAU34560
			FAB045/0
		[201 (K+1,J)=1 210 (J,K+1)	FA8045580
	¢	10185-0	FA804593
	י נ		FAB04600
	ינ	RECTICE UN STACE LUUP	FA804610
	،ر		FA8045 20
	22		FAB04630
			FAB04640
	، ر	IN SPACE LUUP CUMPLETED, COMPUTE NEW PRUJECTILE VELOCITY	F AH04650
12	، د	FRUM MUMENIUM BALANCE	F AU24060
29	د		F 48046 /0
		IF(IFLAG.EQ.0) GO TO 44	FAB0468C
	14		FAB04693
			F AB04 700
	* *		FA804 / 10
	0 1	RKITE 109408 IISAIRKIR SISAIR 10011 AND SISAIR	FABU4/20
	0 (7 \	TOKATI////////////////////////////////////	FABU4/3U
	54	APKUJ=AIAN((2CU(2,1)-2CU(1,1))/(2CU(2,1)-7CU(1,1))	FA304/40
		[CIK=4*005 U04:10[1;1]*2[N(APKU3]	
		VFK01=VFK04+101+F01=N#01=N#0ENFK4#9,80E-00#5K19F1FPASS-XK+0XE+2C011+11	
		61844.80E-06/PMASS	FAB04770
		UCDET 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	FAUU4/8U
			FA004 190
		IT (ARALL +0.4 UT) ENGTBER 04 UCE CU	FA834810
		ILLARADALE AUGUS DOUDE EFSIGILATIONS EFSBJ GU U 42 Istingi me inci co to 13	F A B C 4 8 2 0 E 4 B D 6 9 2 0
	L	IT INCLOSE THE TARGET OF T	F 4 0 0 4 6 5 0
.~.	ى ر	DRINT CHEDENT CITID HADLARIES	FABU484U FABC4850
	ې ر	TAIN CONFW TILLO VANIADLES	E # 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
	J	UD 1 T E (4 , 00)	
	80	FORMATE JIX. ITTME 7%. IDARI VEI 3%. IDARI FUCV I DSS'. IX. IFAR	CEARO480
	;	<pre>c ENGY GAIN', 2X, BACK UP ENGY, 3X, STRAIN ENGY, 3X, K, C,X, Y, Z')</pre>	FA804490
		WRITEI6, 81) TIM, VPROJ, DKE, TLEGFR, ENGYDK, SNRGY, XKNRGY, YKNRGY, ZKNR	YFAB04900
	81	FORMAT[4x,9E14.5]	FAD04910
	802	WRITE(6,72) ((T10(1X, [Y), [X=1, JPRT), [Y=1, JPRTY)	FAB04920
	72	FORMAT(1X, 'T10(1X, 1Y) =: /8(E15.5))	FAB04930
	ì	WRITE(6,74)((TOI(JX,JY),JX=1,JPRT),JY=1,JPRTY) Focuses: 525:15:2:2:2:5:5:5:5:5:5:5:5:5:5:5:5:5:5	FAB04940
A DAMAGE AND A DAMAGE AND A DAMAGE AND A	and a local states		FAU04950
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	WR[TE (6.702) ((VZ(NX.NY).NX=1.JPRf).NY=1.JPRTY)	FAB04960
702	FORMAT(1X, * V2([,J)=*/9(E14.5))	FAB04970
1	WRITE(6.701) [[XCD[MX,MY],MX=1,JPRT],MY=1,JPRTY]	FAB04980
10/	FURMAI([X+*KUU([+J]='/9(E[4.5]) WRITFI6.703) [[7CD[[[X.][CV].[CV=].]PPT].[CV=].JPRTV]	FA805000
103	FORMAT(1X, 2CD(1, J)=+/9(E14,5))	FAB05010
	WRITE(6,76) ((EPS10(KX,KY),KX=1,JPRT),KY=1,JPRTY)	FA895920
76	FORMAT(IX+*EPSIO(KX+KY)=*/8(EI5+5))	FAB05030
7.0	WKITE10,101 (1CP301(LA+LT)+LA=L,JPKI)+LT=L,JPKIT FORMAT{lX,"EPSO1(LX+LY)='/8(E15,5))	FA805050
i	IF(IPLAST.GT.0) GO TO 101	FAR35060
J		FAB05080
	RECYCLE ON TIME LOOP	FA005090
2 د	CONTINUE	FAR05110
:	. WRITE(6,102) TMAX	FAD05120
102	FORMAT[//IX.IX.FABR[C DDES NOT FRACTURE AT TMAX", 2X.E14.5)	FAB35130
42	UC 10 101 WRITE(6,80)	FAB05150
!	WRITE(6,82) TIM, VPRDJ, DKE, TLEGFR, ENGYBK, SNRGY, XKNRGY, YKNRGY, ZKNRG	YFAB05160
82	FORMAT[//IX,'AT FAILURE:'/IX,4X,9E14.5)	FAB05170
	IPLASI=1 Cn tn and	FABUS180
101		FAB05200
1	STOP	F AB05210
	END	FAB05220
	SUBROUTINE BNDRY(IT,J,K)	FABC5230
	COMMON/IXMATL/IPT	FAB05240
	CUMMUN/CMATL/EYRN,CHARD,EO,EI,EZ,E3 Fowedingstrong viewens,tan	FAB05250
	COMMON/VISCU/01: CAMUAITAU COMMON/VARBL/JT XL.DXL.DTM.DENYRN. PMASS.CRIMP.FMASSA.FMASSA.	FFAB05270
	EMASSF, UN ITM, HUNI TM	FA805280
	COMMON/TSNOLD/T190L0(40,40),T010L0(40,40),E109L0(43,40),E010L0(40	FAB35290
	540) Frammany Prafikito / Yk	FAB053C0 FAB05310
	CURRENT MACHUR AN COMMENT MACHUR AN	DEABOS 320
	СОМ ПИХ СНЕЗЛАХОТТОТТОТТОТТОТТОТТОТТОТТОТТОТТОТТОТТОСССССТТОТСООСТИТОСССССТИТОСССССТИТОСССССТИТОСССССТИТОССССС	FAB05330
	£TY10[40,40], TY01 [40,40], TZ10[40,40], TZ01[40,40],	FAB05340
	CEPSIO(40,40), EPSO1(40,40)	FAB05350
	COMMO4/VELOC/VK(40,43),VY(40,40),VL(40,40) F OMMO4/FREETIM/YK NREV-VKNREV-7KNREV-SNREV	FAR05360
	COMMON/ ERGELM/EL XE 140,40), EL SE 140,40), TLELEN 140,40)	FA805380
	DVX={TX10(J+1,K)-TX10(J,K)+2,00E 00+TX01(J+1,K))+DTM+8.8200E 00/6	2FAB05390
	\$*00F_00*DXL*rCRIMP]	FAB95400
	DVZ={TZ10{J+1,K}-TZ10{J,K}+2.00E 00#TZ01{J+1,K}}#DTM#8.8Z0JE 00/{ f	ZFA805410 FAR75427
	なまくびて しび ナジスドキシス にちて マイスページストナシング しょうて ナラン ドラ コティング ひひし こうじょうじょうじょう シャッシュ シン・グレング ロング エーロング	FA805430
	XX(J+1,K)=yX(J+1,K)+DVX	FAB05440
	VY(J+1,KJ=0.00E 00	FABC5450
	V21J+1,K)=V2(J+1,K)+DV2	FAR05460
	VX(JT,K)=0.00E 03	FAB054 /0
	VY(J +K)=0+0CE 0C V7111.K)=0.70F 07	FA805490
	(X: 1) 1 = VY(J+L) - V(J+L) - VX(X-V) - VX(X-V	F48055C0

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VY(K,J+1)=VX(J+1,K) VZ(K,J+1)=VZ(J+1,K) DS4X=(XCD(J+1,K)+VX(J+1,K)*DTM/1.00E 04-XCD(J, C 04)**2	FAB05510 FA805520 ()-VX(J,K)*DTM/L.00EFAB05530 FAB05540
DSQY=(YCD(J+1,K)+VY(J+1,K)*DTM/1,00E 04-YCD(J) 6 04)##2 DSQZ=(ZCD(J+1,K)+VZ(J+1,K)#DTM/1,00E 04-ZCD(J)	<pre>() - VY (J, K) * DTM / I * 00E F AB 05550 F AB 05560 () - VZ (J, K) * DTM / I * 00E F AB 05570</pre>
<pre>& 04) ##2 DDL= SQRT(DSQX+DSQY+DSQ2)</pre>	FAB05580 FAB05590
DSG=(XCD(J+1,K)-XCD(J,K))##2+(YCD(J+1,K)-YCD(J & 2CD(J,K))##2	K)]##2+{2CD{J+1 ₉ K}-FAB05600 FAR05610
DIST= SQRT(DSQ) DEPS=DDL/DIST-1.00E 00	FAB05620 FAB05630
EPSIO(J,K) = EPSIJ(J,K) + DEPS	FAB05640
EPSO1(K,J)=EPSI0(J,K) TSLGLU=T100LD(J,K)	FAB05650 FAR05660
EPSCLO=E100LD(J,K) EPSLN=EPS10(J,K)	FAB05670 FAB05680
CALL TENSNI IT, J, K, EPSLN, TSL, EPSOLD, TSLOLD, DSNR	Y) FAB05690
ILU(J,K)=ISL TOL(K,J)=TIU(J,K)	FAB05/C0 FAB05710
T100L0(J,K)=TSL0LD	FAB05720
701ULU(K,J)=1100LU(J,K) E100LD(J,K)=EPSOLD	FAB05730 FAB05740
E010LD(K,J)=E100LD(J,K)	FAB05750
BKEXY=24C9E 00 1611/60.1/AND_K_E0.1/ BKEXV=1.00E 00	FAB05760
XKNRGY=XKNRGY+ BKEXY#0.50E-03#HUNITM#V	({] *K) **2/ (FMASSF *CRFAB05780
<pre>& CIMP) + BKEXY+0.50E-03+HUNIIM+ VX(K,J)++2.</pre>	(FMASSF#CRIMP) FA035790
Cimp)+ BKEXY+0.50E-038HUNIFM+ V(K.J)++2	(F4ASSF#CRIMP) FABO5810
BKEZZ=4.00E 00 -	FAB05820
IF(J。EQ。I。AND。K。EQ。I) BKEZZ=Z。OOE OO ZKNRGY=ZXNR、Y+ RKF77#O、50F-O3#HINTTM#	FA005830 v7(.1.K)**2/(FMASSFAB05840
CLACK LAP	FA805850
SNRGY = SNRGY + DSNR GY F T B C E = 4 _ D O E _ D O	FA835860 EA805870
IF(J.EQ.1.AND.K.EQ.1) CTRSE=1.00E 00	FA605880
ELSE1J,K)=ELSE1J,K)+OSNRGY/CTRSE	FAB05890
ELSE(X¢J)≡ELSE(J¢K) CTRKE=1,000€ 00	F 4805960 F 4805910
IF(J.EQ.1.AND.K.EQ.1) CTPKE=2.006 00	FAB05920
ELKE(J\$K)#FLKL(J\$K)+CTKKE#O\$50E-03#HUNITM# &\$2+VZ(J\$K)#*2)/(FMASSF#CR{MP}	VX[J*K)**2+VY[J*K]*FABU5930 FABU5940
ELKE(K, J)=ELKE(J,K)	FA805950
Tteten(J,K)≈ELSE(J,K)+ELKE(J,K) Tteten(x, t)=tteten(J, K)	FAB05960 FAR05070
XCOOLD=XCO(J,K)	FA805980
YCDOLD×YCD(J,K) Pront n≠7CD1 (,K)	FA805990 FAR05000
XCD(J,K)=XCD(J,K)+VX(J,K)+DTM/I.OUE 04	FAB06010
YCD[],K)=YCD[],K]+YY[],K]*DTM/].OOE 04 Trn: vi-Trn: vi+uTi'!K)*DTM/].00E 04	FAB06720
If (1. EQ. + 1) 50 10 20	FABUG040
XCD[K,J]=XCD[K,J]+VX[K,J]*DTM/L.00E 04	FA806050

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Y(K,J)*DTM/1.00E 04 Z(K,J)*DTM/1.00E 04 YCD(J,K))/(XCD(J+1,K)-XCD(J,K))) CD(J,K))/(ZCD(J,K)-ZCD(J+1,K))) CD(J,K))/(ZCD(J,K)-ZCD(J+1,K))) XCD(J,K))/(ZCDLJ,K)-ZCD(J+1,K))) SINB*COSA SINB*COSA SINB*COSA COSB COSB .J.K,FPSS,TS,EPSOLD,TSLOLD,DSEN) .J.K,FPSS,TS,FS,FPSS,TS,FS,FSS,TS,FS,FSS,FSS,FSS,FSS,FSS,F	FAB06490 FAB06490 FAB06500 FAB06510 FAB06520 FAB06540 FAB06540	FAB06550 FAR06560 FAR06570 FAR06580 FAR06580 FAR06590
V(K,J)*DTM/ V(C)(J,K))-0. (C)(J,K))-0. (C)(J,K))/(XCD(J,K))/(SINB*COSA SINB*COSA SINB*COSA (S) (J,K,EPSS,T 	550E 30	I ASTIC MOVEL SS**3
YCD(K, J)=YCD(K, J)+YCD(K, J)=YCD(K, J)=YCD(K, J)=YCD(K, J)=YCD(K, J)+YCD(Y, A=ATAN(YCD(J+1,K)-C058=0.00E 00 \$\$ \$\$ \$\$ \$\$ \$\$ \$\$ \$\$ \$\$ \$\$ \$\$ \$\$ \$\$	E40) COMMOV/BACKUP/XK IF(EPSS.LE.J.00E 00) GG TO I SYMCTR=1.00E 00 IF(J.EQ.1.AND.K.FQ.1) SYMCTR=0 IF(IPT.EQ.2) GO TO 12 IF(IPT.EQ.2) GO TO 12 IF(IPT.EQ.2) GO TO 14	IFIIPT.EQ.4) GD TD 18 NDNLINEAR (CUBIC POLYNDMIAL) E TS=E0+E1*EPSS+E2*EPSS**2*E3*EP

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W SPACE VIX

	EE 00#EPSS##4)#DENVRN#DXL#CR!#P#9.80E-05#SYMCTR/(FMASSM#CRIMP) Co to 2	FA896610
ი		FAR06630
<u>ں</u>	NONLINEAR (EXPONENTIAL STRAIN HARDENING) ELASTIC MODEL	FAB06640
<u>ي</u> د	TC-EV0114E06554460	FABU6550 Fabreer
7 0	I3=CTKNT=CT33++CDARU DSEN=4.0E 00#(1.00E 00/(1.00F 00+CHARD))#EYKN*CPSS**11.00E 00+CHAR	FAB06670
	<pre>ED] #DENYRN*DXL #CR [MP*9.80E-05*SYMCTR/(FMASSM*CR[MP)</pre>	FARJ6680 FARD6500
U		FAB06700
	LINEAR (STANDARD LINEAR SOLID) VISCOELASTIC MODEL	FAB06710
ں		FABC6720
14	B-G*(1-JOE OD-VLAMDA)/TAU	FAB06730
	D=1.00E 00+DTM/TAU reitt et 1, 60 t6 j6	FABU6/40
	1111.60.11 60 10 10 EPSD10=0.00E 00	FA8-6760
	TSLOLD=6400E 00	FA306770
16	TS= (G+ (EPSS-EPSGLD)+8+EPSS+0TM+TSLGLD)/) 05EM=14.00F 03+0.53F 034(TS+TS101D)+1EPSS-EPSO10)#0X1+65ENVBN+CR1ND	FABC6790 FABC6790
	0464-1440/1 00-00-001 00-1401 00-14010 00-14100 00-141000 00-14100 00-14100 00-14100 00-14100 00-14100 00-1410 249.606-05*SYMCTR1/(FMASSM*CRIMP)	FAB06800
	EPSOLD=EPSS	FAR06810
		FA006820
L		FARD6850
ں ر	NDNLINEAR (EVRING) VISCOELASTIL MODEL	FA006850
ი		FABO6860
18	IF(IT.GT.1) GO TO 20	FAB06870
		FAB76880
0		FABC6890
20	01=E42=A#0TM 03=FFN3=A71 000 00-441 0D1	FABJ69C0 EABD6910
	04=ENX#11=UUU UUTVLDU/ R1=A1 D#FN1#FDAA	FA856923
	84=EPSS-EPSOLD	FA896930
	A1=B1+DCOSH(B3)	FAB06940
	A2=-B1+USINH(D3)	FAB36950
	A3=-82*84-TSLOLD	FAB06960
	E: S=1.000-06	FAR96970
	EF52=1,900-06	FABUC 980
	E 1 A# 1 + JUU# U.C Nr 16#6	FAB07040
	N=1	FAB07010
	X(1)=TSLOLD	FAB07020
	ITHAX=100	FAB07030
	CALL ZNONLR(F,EPS,EPS2,ETA,NSIG,N,X,ITMAX,IER)	FABC7040
		FAUV (050
	DSEN={4.00F 00#0.50E 004{TS+TSLOLD)*{EPSS-EPSOLD)*UXL*UENYKN*CKIMP c+d dot_Ac+cvarre}/fram.ccvarre)ud0	FABU 7050
	214.0.001.0.1.0.0.01.2.2.2.7.7.7.2.4.0.0.4.6.7.1.2.7.1.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7	
		FAB07050
	G0 T0 2	FAB07140
4	TS=0.00E 00	FA857110
	DSEN=0,00E 00	FAB07120
N		FABU 11 3U
	REAL FUNCTION F#B(S)	FAB07150

FILE: FABRIC FORTRAN A

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	REAL*8 DSINH, DCOSH	FAB07160
	RFAL×8 ENI,EN2,4,ALP,VLBD,5,41,A2,A3 commonying stems store a store of the store stems store st	FAB07170
	CUMMUNY MUYENT FINE FINE FATE FRENC FAMM	FAE37199
	Construction (ALP+C) + A2+DCOSH(ALP+S) + 43 F=S+A) ≠DS1NH(ALP+S) + A2+DCOSH(ALP+S) + 43	FAB07200
	RETURN	FAB07210
	END	FA807220
ر	SUBROUTINE ZNJNLR(F,EPS,EPS2,ETA,NSIG,N,X,IIMAX,IEK)	FA307240
ں ر	MULLER ALGORITHIM FOR ITERATIVE SGLUTION OF NOWLINEAR	FAE07250
U (EQUATION USED FOR EYRING CONSTITUTIVE MODEL	FA837260
J		FABUIZIO
	DOUBLE PRE-USION X,X1,AX1,EPS,EPS2,ETA,FX1,AFX1,01,H1,FX1PH1,	FAR07290
	+ DER, XIPI, FRR, F. ERR, CAITI, PI, PCOI, ZERO, ONE, TEN	FAR973CO
	CATA P1,P001,ZFR0,DNE,TEN/.1D0,.00100,0.D0,1.D0,	FABC7310
		FAB07330
	18±0	FAB07340
	CRIT1 = TEN++(-NSIG)	FAB07350
	DO 30 I=1,N	FAB37360
	IC = 1	FAB07370
	$(1) \times 1$	FA807380
ŝ	AXI = UABS(XI)	FAB37500
	<pre>/F [] .EQ. 1) GO TO 15 Mini-1-1</pre>	FAB07410
		FAR07420
	UU 10 J= [\$1417.1 15 inarcivi - viii) _it_ 5003) vi = vi + FTA	FARD7430
0;	IF IDAUSIAT ANULT OLIO CESZ AL FAL VELA CONTINIE	FAB07440
15		FABC 74 50
1	AFXI = DABS(FXI)	FAB07460
	IF (AFXI .LE. FPS) GO TO 25	FA807470
	DI = 10.0-9	FAB07480
	IF [AXI GE. PI] DI = POO1*AXI	FAB07500
	HI=DMINI(AFXI,DI)	1-4607510 54507510
	FX[P(1] = F(X] + H1) DFU = {FY10H1 - FY11/H1	FARC 7520
	IF (DER .EQ. ZERO) GO TO 20	FA807530
	X [P] = F X] /DCR	FA907540
	CALL DVERFL (J)	FAB3755C
	IF (J .EQ. 1) CO TO 20 VIDI-VI-VIDI	FAB07520
	ERR = DABS(X[P] - X])	FAR07580
	XI = XIPI	FABu7540
	IF(AX1.EQ.ZERC) AX1=DNE	FAB07600
	ERRI=ERR/AXI	FAB07610
	CALL EVERTLY J	FA901020
	IF(J.EO.I) ERRI=ERR sevenum in continenta	FAB37650
		FA907650
	IF (IC .LE. ITMAX) GD TD 5	FAP07660
	X(f) = 111111.00	FAB07670
	[R=[R+]	FAB075F0
	[ER=33 Co to 30	FA897650 FA897720

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FORTRAN FILE: FABRIC 20

X(I) = 222222.00
IR=IR+1
IER=34
GG TG 30
X(I)=XI
CONTINUE
ITMAX = IC
IF(IER.E0.0) GD TD 9005
IF(IR.LE.1) GD TD 9005
IF(IR.LE.1) GD TD 9000
IER=35
CONTINUE
CALL UERTST(IER.6H2REAL2)
RETURN
END 3030

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CONVERSATIONAL MONITOR SYSTEM

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FABG7710 FAB07720 FAB07730 FAB07730 FAB07740 FAB07750 FAB07760 FAB07790 FAB07790 FAB07810 FAB07810 FAB07820 FAB07830 FAB07830

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APPENDIX B - The XOVER Code

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XOVER is the FORTRAN program written to General. carry out the calculations described in Chapter IV of this report. It is identical in concept to the FABRIC code, differing primarily in the dimensionality of the problem. XOVER is essentially a treatment of transverse ballistic impact on a single fiber as described earlier by Roylance [18], but it has been modified to include a second fiber, transverse to the first, which receives its loading from the motion of the first (primary) fiber. The code is made more complicated than the single-fiber case by the necessity of allowing motion in all three directions for the secondary fiber, and in computing the initial values of the secondary fiber in terms of the primary fiber motion. As described in the text, allowance is made for slippage of the secondary fiber along the primary.

<u>Code requirements</u>. As was true for the FABRIC code, XOVER mequires little hardware or software support. At present, the code includes a call to an MIT library subroutine PRTPLT for the purpose of obtaining a rough plot of the nodal variable values on the system line printer. This subroutine call could

be removed without affecting the performance of other parts of the code. For a typical run, in which two crossed Kevlar fibers were impacted at 300 m/sec, the job run time was 0.305 minutes and 170 kilobytes of core was reserved.

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Definition of program variables. XOVER is conveniently described by means of a listing of the principal program variables: (* denotes input data)

A	8.826 x 10 ⁶ (dt/dl)
CROSS*	Initial crossover position (fraction of XLl)
CZ	Wavespeed (m/sec)
DEN*	Fiber denier
DL	Length increment (cm)
DT	Time increment (sec)
El(J), E2(J)	Strain at jth node in primary and secondary fiber
ElOLD(J), E2OLD(J)	Strain at previous time increment
EMAX*	Maximum strain permitted
EEMAX	Maximum strain in fibers
G*	Instantaneous modulus (gm/den)
IPLOT*	.EQ.0 if no printer plot is desired
11,12,13*	Node numbers at which plot desired (I3 on secondary)

WALLSTON OF

JX	Crossover	node	on	primary	fiber
----	-----------	------	----	---------	-------

- JJX Initial crossover node
- KMAX Maximum number of time increments
- LPSKIP* Length print skip
- LTSKIP* Time print skip

- NLINC* Number of length increments on primary fiber
- PMASS* Projectile mass (gm)
- PVELOC* Projectile velocity (m/sec)
- SLIDE* Slip factor (1-no slip, 0-no friction)
- TAU* Viscous relaxation time (sec)
- TITLE* Alphanumeric title (80 characters max.)
- T1(J), T2(J) Tension in primary and secondary fibers (gm/den)
- TlOLD(J), Previous tension (gm/den) T2)LD(J)
- TMAX* Maximum time (sec)

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- Ul(J), U2(J) X-component of velocity in primary and secondary fibers (m/sec)
- V1(J), Y-component of velocity V2(J)
- VLAMDA* Viscous fraction (0-elastic, 1-purely viscous)

Wl(J), W2(J)	Z-component of velocity
XL1, XL2	Half-length of primary and secondary fibers (cm)
X1(J), X2(J)	X-coordinate of jth node on primary and secondary fibers
Yl(J), Y 2 (J)	Y-coordinate
Zl(J), Z2(J)	Z-coordinate

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Note that in its present form, XOVER is written explicitly for viscoelastic material response of the standard linear solid type. For elastic fibers, the user should set VLAMDA to zero and G to the Young's modulus; TAU could be any nonzero value. The variables required by the code are indicated as input information and are specified in the above list by an asterisk; an example of a typical input data set is given below.

EXAMPLE:

VELOCITY	STUDY,	V = 300 m/sec	KEVLAR 2	29	
1.0E+06	300	20.	10.	0.5	1.0
1500	550	0.14-0.4	0.		
100	5	5	287E	0.05	
1	25	75	25		

1) 204A TITLE

2) 6E10.3 PMASS, PVELØC, XL1, XL2, CRØSS, SLIDE

3) 4E10. DEN, G. TAU, VLAMPA

4) 3I 10, 2E 10.3 NLINC, LPSKIP, LTSKIP, TMAX, EMAX

5) 4I 10 IPLØT, I1, I2, I3

Typical Output. Typical output from the XOVER code for impact on two crossed Kevlar 29 fibers at 300 m/sec is given below:

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FTRFP DFMITFR = 1400.0 INSTARTARFOUS MCDULUS = 550.0 GM/DFN PULAVATTCK TIME = 0.1438-0% CFC VTSCTUS FPACTION = 0.0

NUMBER I FUGTU INCREMENTS - 100 PSTUT SKID FACTOR = 5 TVE SKTD PACTOR = 10 VAKIMUM TIMS = 0.2875-04 SPCMAXIPUM STRAIN = 0.050

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LENGTH INCREMPRT = Λ_{*} , 27C+50 CM NUMBER NODIS IN PRIMARY = 101 NUMBER NODIS IF STCREARY = 51 HAVESTER = 6467.3 M/SFC TAR THCERMENT = Λ_{*} , 2877-56 SFC C 25550VER NOFF = 51 MAXTMUM NUMBER TIME INCREMENTS = "LOT CPTIONS = 1 25 75 25

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VETTETY STUDY, V = 300 M/SFC KEVLAP 29

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CHTTPH: PPP TIME = 0.258F-C4 SFC CHTTPH: PPPJFCTILE VELOCITY = 300.0 M/SEC

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;	(0) (V						
~	0 . 0	544° v	0 •0	300.7	5.42	, 0,00985	
9	0.912	, 342	-13.7	269.9	5.38	0.00979	
-	1.048	J.015	-67.7	25.8	5.36	126Cu J	
ۍ	2.457	ບໍ່ນີ້ນ	-6° ay-	0°0	5.43	0.09997	
•	7. A67	טֿיייטׂ	-67.3	0.0	5.36	0.00974	
Ŷ	477	ΰιύ ° 0	-67.9	J. C	5.48	96600°0	
÷	5.997	0.00	-67.1	0.0	5,51	01000	
v	6.897	ປູບູບູ້ "ບ	-66.2	0.0	5.54	0.01007	
÷	4(ic . 7	0.000	-64.9	0.0	5.49	0.0097	
y	9, 718	ũ vù °ũ	-66.6	 0	5.69	0.01019	
•	9.028	0.03A	-66.7	0°0	5.24	0.00922	
v	10.027	ر • ر	-64.1	Ċ°Ċ	5.06	n.00929	
-	11.947	ر د ر	-66.1	ن°ن ن	5.20	9 16 00 0	
v	12,456	Ú°Ú	-69.7	0°0	5.40	r.00982	
-	13,966	0°0	-62.5	ວ°0	۲ .0 0	C.0090A	
2	14.975	0.0	-66.3	0.0	5,23 5	0.00451	
÷	15,095	د • د	-77.7	0.0	6.11	0.01111	
Ś	16.996	0.0	-52.0	0.0	4.10	0.00745	
•	14.090	0.0	0.0	0.0	0.0	0.0	

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۲.	Х2 (л)	Y2 (.J)	(r) 22	(r) 2a	(r) ZA	H2 (J)	T2 (J)	F2 (J)
-	9 <u>,</u> n2R	0000	0.0	-66.7	5.6	0.0	ù 2 ° O	0.00128
u	17. 000	<i>6</i> •,	£00°J	0.6-	0.0	-8.8	0 °69	0.00125
11	1 Ú° UJU	J.C	1.994	J. C	0°C	-10.0	0.78	0.00142
15	10,000	ن• c	2.996	د.م م	ù°û	-10.6	9.83	0.00150
¢.	10002	د• ر	3.997	0.0	0.0	-8.8	0.69	0.00126
5 К	ن ب ب ا	0°C	060°n	ບ. ເ	د • د	-7.2	0.56	0.00102
÷.	10.00	·.0	66ú°5	0.0	0.0	-5.8	0.46	0.00083
٦F	10,000	0°0	7.030	ن• ن	0°ú	-1.0	9.0A	0.00014
41	10.010	ن•ن ن	960.8	u•0	0.0	0.0	0.0	0.0

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<pre>Definition of the second of the second state of the second st</pre>		C AUTHOR DAV	VID RCYLANCF MTT WRI	1016 1016 1010	
<pre>c wean and pertyr persire it() (TTTIR(1).J=1.2() prad(5.1000, FWNS:11() (TTTIR(1).J=1.2()) prad(5.1000) FMNS: PUEDCC.XL1,XL2.CPSSS.SLIDE prad(5.1000) HINC.IPSKTP,ITSKIP,ITAX, EHAX FIN((5.1050) NINC.IPSKIP,ITSKIP,ITAX,EHAX FRAN(5.1050) NINC.IPSKIP,ITSKIP,FHAX,EHAX FRAN(5.1050) DFW,G,FAU,VIAMDA FRITF(6.1050) DFW,G,FAU,VIAMDA FRITF(6.1050) DFW,G,FAU,VIAMDA FRITF(6.1050) DFW,G,FAU,VIAMDA FRITF(6.1051) DFW,G,FAU,VIAMDA FRANCFIC FILTURE FRANCFIC FILTURE FRANCFIC FILTURE FRANCFIC FILTURE FRANCFIC FILTURE FRANCFIC FILTURE FRANCFIC FILTURE FRANCFIC FILTURE FRANCFIC FILTURE FRANCFIC FILTURE FRANCFIC FILTURE FRANCFIC FILTURE FRANCFIC FILTURE FRANCFIC FILTURE F</pre>	-	DIMPNST 12	л. ТТТГ (200) . X 1 (200) . (200) . V1 (200) . V2 (200) . W (200) . T1 (200) . V2 (200) . (200) . T201. D(200, 4) . ABPA7 (209. 3)	22 (200) * 1 (200) * 22 (20 2 (200) * 1 (200) * 12 (20 2 (00) * 11 (200) * 12 (20 2 (00) * 11 (200)	(200) . E1 (: (200) .
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<pre>Finicsicroo Dew.g.Finivirun. Finicsicroo Dew.g.Finivirun. Finicsicroo Dew.g.Finivirun. Finicsicroom Fini</pre>			1010) PHASS. PVELOC. XL1.	(L2.CPOSS.SLIDE	
<pre> Fand(5,1030) MINC_LESTEP_ITSKIP_THAX, FMAX Fand(5,1030) MINC_LESTEP_ITSKIP_THAX, FMAX WETTF(6,1030) DFW.G.F.PLUC_XL1712, CFCSS.SLIDE WETTF(6,1030) DFW.G.F.PLUC_XL1712, CFCSS.SLIDE WETTF(6,1030) DFW.G.F.PLUC_XL1712, CFCSS.SLIDE WETTF(6,1030) DFW.G.F.PLUC_XL1712, CFCSS.SLIDE NTTEFIL1 NTTEFIL2 NTTEFIL2</pre>	n	pran(5,	1020) DEV.G. TAU. VLAMDA	•	
RWTTER(5,104C) (TTTLE(0), J=1,20) WHITP(6,105C) PMASSS, PVEDOC, X11, X12, CPOSS, SLIDE WHITP(6,105C) PMASS, PVEDOC, X11, X12, CPOSS, SLIDE WHITP(6,101) NLTWC, IESKIP, THAX, PMAX MILENIL, NLTWC, NLTWC, IESKIP, THAX, PMAX MILENIL, INULX MILENIL, INULX MILENIL, IENL2 MILENIL, I	<i>v v</i>	R FAD (5, 7	1034) NLINC, LPSKIP, LTSK 1034) IPLAT, I1, I2, I3	гр, тиах, гиах	
Waltre(s, 104c) Marre(s, 104c) Marre(s, 104c) Marr		t.			
C CCMPUTE AKD DETER (5,1050) UNINC.IESKIP.ITMAX.EMAX WETTE (5,1050) UNINC.IESKIP.ITMAX.EMAX T_=YL1/NLTC N_	•	y survey	, 1640) (TITLE(J), J=1,20 1660) Deles Durios VI	VIJ CDASS SITAD	
C Craphtr ALD PERT LATERNAL PROBLEM PARAMFTERS n_=FK1/VBLTC N1=FK1/VBLTC N1=FK1/VBLTC N1=FK1/VBLTC N1=VLTC(+1 N2=KT2/DL)+1.5 NAX=VL2 NAX NAX NAX NAX NAX NAX NAX NAX	ر ت د ،	y) allan y) allan ij jaran	1050) DFN,G,TAU,VIANDA 1050) NLINC,LESKIP,LTS	KIP, THAX', PHAX	
<pre> Definition Definition The set of the</pre>		כ כריאקותד אצו כ	A PPIVE INTPRNAL PROBLE	9 PARAMPTERS	
<pre>MIT=WLTNC+ MIT=WLTNC+ NIT=WL</pre>					
HLP=(X12/DL)+1.5 HLP=(X12/DL)+1.5 HLP=(X12/DL)+1.5 HLP=(X12/DL)+1.5 HLP=(X12/DL)+1.5 HLP=(X11*CS75/DL)+1.5 JJT=JT HTTP(6,10H) DL/H1,HL2,C2,DT,JX,KHAX HAXTTP(6,10H) DL/H1,HL2,C2,DT,JX,KHAX HTTP(6,10H) DL/H1,HL2,C2,DT,JX,KHAX HTTP(6,10H) DL/H1,HL2,C2,DT,JX,KHAX HTTP(6,10H) DL/H1,HL2,C2,DT,JX,KHAX HTTP(6,10H) DL/H1,L2,L3 HTTALTZ7 ARRAYS C THITALTZ7 ARRA	- 6	·// ·/ ·/ ·/ ·/ ·/ ·/ ·/ ·/ ·/ ·/ ·/ ·/	2012C R7+1		
<pre>H H H H H H H H H H H H H H H H H H H</pre>		(X) = C T N	2/DL)+1.5		
<pre>F [[[[[[] + [[] + [[]]]]]]</pre>	1	TN=XWN			
C CZ=SORT(005,4C) DT=DI/(100,4C2) UT=DI/(100,4C2) UT=JY UT=JY UT=JY KMAX=TPAX/DT KMAX=TPAX/DT KMAX=TPAX/DT KMAX=TPAX/DT HIL2,C2,DT,JX,KMAX WTTTF(5,1094) DL,WI1,ML2,C2,DT,JX,KMAX WTTTF(5,1094) DL,WI1,ML2,C2,DT,JX,KMAX C THTTALTZF AFRAYDT C THTTALTZF AFRAYDT C THTTALTZF AFRAYDT C THTTALTZF AFRAYS C THTTALTZF AFRAYS C THTTALTZF AFRAYS C THTTALTZF AFRAYDT (J = 1, THT(J) = 0. THT(J) = 0. THTTALTZF (J = 0. THTTTALTZF (J = 0. THTTTTALTZF (J = 0. THTTTTALTZF (J = 0. THTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTT	r	IP (NL ⁴ .]	IT.NL2) NMAX=VL2		
<pre>press (100.*CZ) press (100.*CZ) press (11*CC) press (11*CC) press (10*C) press (10*C) pre</pre>	v	180 S= 20	(D*~092Pa)		
3 3/1/1=1/Y 3/1/1=1/Y 7/1/1 7	۲	pm=01 / (100.*CZ)		
<pre>3.3/Y=JY N KWAX=TPAX/DT 1 KWAX=TPAX/DT 1 KWAX N=R.375F(6.70M5) DL/N11,NL2,C2,DT,JX,KMAX WTTPF(6.10M5) DL/N11,NL2,C3,DT,JX,KMAX WTTALTZF APRAYS C C THITALTZF APRAYS C C THITALTTALTTALTTALTTALTTALTTALTTALTTALTTAL</pre>	8	ין זאן = אנ	+C¤jss/Dt,)+1.5		
1 KWAKETFAX/JT 2 KWAKETFAX/JT R=8.326F+66*DT/DL BL/W1,NL2,C2,DT,JX,KHAX WATTF(6,1085) JFLJT,11,I2,I3 WATTF(6,1085) JFLJT,11,I2,I3 WATTF(5,1085) JFLJT,11,I2,I3 C THIALTTF AFRAYS THIALTTF AFRAYS THIALTTF AFRAYS THIALTTF AFRAYS	ŗ	スピーズビビ			
<pre>2</pre>	¢	K * A X = T P	3 X / DT		
3 WRTTP(6,10HC) DL,VI,NL2,CZ,DT,JX,KMAX WRTTP(6,10HC) DL,VI,NL2,CZ,DT,JX,KMAX C WRTTP(6,10HC) DL,VI,1,L2,L3 C D3 20 J=1,209 C D3 20 J=1,209 T1(J)=0. T1(J)=0.	t	F=8.3761	F+C6*DT/DL		
C THIALTF APPAYS C THIALTF AP	c. (,1040) DL, VI1, NL2, CX, DT 1046: INTOR 11 IL2, CX, DT		
C C D D C D C D D C D D D D D D D D D D D D D	•		CTOTOLICITAT (WHI		
D) 20 J=1,209 x1 (J) =DL xPI JAT (J-1) y1 (J) =0. y1 (J) =0. T1 (J) =0. T1 (J) =0. T1 (J) =0. APPAZ (J, 1) =FLOAT (J) APPAZ (J, 3) =0. APPAZ (J, 3) =0.		C TRITIALTRE	SYARAS		
x1 (J) = DL xFI JAT (J-1) x1 (J) = C. x2 (J, 1) = FLOAT (J) x1 (J) = C. x2 (J, 3) = O.	3	τη 2 C θ	=1,200		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	ť	(r) t X	() = DL * FI OAT (J-1)		
л л т т т т т т т т т т т т т т т т т	÷	Y 1 (J)) = J		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	r () = `		
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$\begin{array}{cccc} & & & & & & \\ & & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & $					
אריאל (1) באריאל (1) באריאל (1) ע היון אריאל (1,2) ביי אריאל (1,3) ביי	ر د	1013	, (J) = 0.		
u APPAS (J. 2) = J.	~	Kaati	Z (J, 1) =FLOAT (J)		
5 X PPAS (J. 3) =0.	t	VidY	7 (1,2) = 1.		
	v	VacV	2(1.3)=0.		

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D1=((Y1(JX)-X1(JY-1))**2+(Y1(JY)-Y1(JX-1))**2)**0.5 PHI1=4TAW((Y1(JX)-Y1(JX-1))/(X1(JX)-Y1(JX-1))) T2PARA=(T2(1)/(D2*D1))*((X2(2)-X2(1))*(Y1(JX)-X1(JX-1)) + (Y2 (2) -Y2 (1)) + (Y1 (JX) -Y1 (JX-1)) T2 PERP= (T2 (1) / (D2*D1)) + ((X2 (2) -X2 (1)) + (Y1 (JX-1) -Y1 (JX)) + (Y2 (2) -Y2 (1)) + (X1 (JX) -X1 (JX-1))) TUPTA2=AmqW(Y 1 (J+2) - Y 1 (J+1)) / (X 1 (J+2) - X 1 (J+1)) U1 (J+1) = U1 (J+1) + (T 1 (J+1) *C^S (THETA2) - T 1 (J) *COS (THETA1)) +A Y 1 (J+1) = V 1 (J+1) + (T 1 (J+1) *SIY (THETA2) - T 1 (J) *SIN (THETA1)) *A 15/25/24 BPGIN TIME LODP - IMPOSE PROJECTILE VELOCITY ON PRIMARY FIBER 1 II (.1+1) = II (.1+1) +2. + (SLIDE+ T2PAPA+C3S (PHI1) THTTA T=4TAN ((Y1 (J+1)-Y1 (J)) /(X1 (J+1)-X1 (J))) ADD RFFET OF SPCONDARY FIRFR IF AT J = JX D2 = ((X2(2) - X2(1)) + +2 + (Y2(2) - Y2(1)) + +2DATP = 77027 + (22 (3) - 22 (3)) + 2) + 40 * 5 BPANCH IF AHPAD OF WAVEFRONT 10 # O 55 BEGIN PRIMARY LENGTH LOOP $\begin{array}{l} x_{2}^{2} \left(J \right) = x_{1}^{2} \left(J \right) \\ z_{2}^{2} \left(J \right) = DL + FLOAT \left(J - 1 \right) \\ \gamma 2 \left(J \right) = 0 \\ \gamma 2 \left(J$ IF (J. GE. KK) GO TO MOFFNTUM BALANCE IF(J. "F. KK2) GO YA TY T=PLCAT(X) * DT 50 J=1, VL1 V1(1) = PVELCC7201 h (J) =0. 72 (J) =0. 90 K=1,KMAX E201 D (J) =0. **KK2=JX-1** J=1,200 KR=K+2 U=dIXSLI u1 (1) = ... CONTINUE ç Š 5 ppLPPSF 2.0 2 ŝ υ $\boldsymbol{\upsilon}$ $\boldsymbol{\upsilon}$ $\boldsymbol{\upsilon}$ υυ υ υ υυ υυυ υ L to AI history a 2 U J したい しょうし じとうい 62.0 しゅじょ それいじ ささくい ショック トヨンリ とおしじ 0700 r911 r 2 1 J ن د 9 ط 0054 505 2900 6900 5500 イドラク みいいい 0500 1 700 0 L 6 3 5963 たらくら ジソンン 7757

+T2PFP0+SIN (PHI1)) *A

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to Ai Neaward	v°Z ASValdi	4AIN DATE = 77027 15	15/25/24
ngƙq	ر	V1 (J+1) =V1 (J+1) +2。* (SLIDE*T2PARA*SIN (PHI1) +*2PFPP*C^S (PHI1)) *A	
(), ()	ະ ສ , ເ	CONTINU [™]	
	υυι	I.a.S.J.L.C.AND BOUNDAPY CONDITION	
2200 2700		(11 (NL1) =0. V1 (NL1) =0.	
	υυι	STPAIN-DISPLACEMPNT RELATION	
5 7 7 2 2 7 7 2	J	ALOLD=SOPT ((Y1(J)-Y1(J+1))**2+(X1(J)-X1(J+1))**2)	
	⊷ 0	ALWFW=SOBT (({Y1(J)+Y1(J)*DT*109。)-(Y1(J+1)+Y1(J+1)*DT*100。) +/YY1(J)+H1(Z]*DW±100)-/Y1/J+412/244120	.))**2
トクフト		F1 (3) = E1 (3) + (ALVEH/ALOLD) -1. AFSAZ (3, 2) = E1 (3)	[7 ++ [] • (
		CONSTITUTIVE RELATION (STANDARD LINEAR SOLID)	
トレトリ	-	T1 (J) = (G+ (E1 (J) - E1•LD (J)) + ((14LAHDA) + G/TAU) + E1 (J) +T1CLD .J1) / (1.+6T/TAU)	10 * DT
0279 Prita		F1~LD(J)=F1(J) ザ1~LD(J)=ア1(J)	
	ບເ	CCMDHLF NEW COCRDINES	
1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	, ر	X1(J) = X1(J) +11 (J) +170, +DT Y1(J) = Y1(J'+ Y1(J) + V1(J) + Δ103, +DT	
	_ د د د	HD OF "THARY LFNGTH LJCP	
r 1 a -	ι Γ	ADALANO	
	. U L	"HPPCSE SLIP CONDITION ON SECONDARY PIERS, IF REACHED E	BY WAVEFRO
とないい	53	ปแล้นเห็น	
504F	*	[K]=JJJY-2 15 14 14 4431 C1 mC 03	
yar J	· • •	HETA=AFAH ((Y 1 (JX) - Y 1 (JX-1)) / (X 1 (JX) - X 1 (JX-1)))	
585J		Р 4 F A=U1 (JX) *COS (ТНЕТА) +V1 (JX) *SIN (ТНЕТА) DPPP=V1 (JX) *COS (ТНЕТА) -U1 (JX) *SIN (ТНЕТА)	
	υ		
נפנט		2 (1) =\$L ID3+VPAPA+Cr5 (THFTA) -VPBP2+SIN (THFTA 2 (1) =\$LID6+VPAPA+SIN (THPTA) +VPPRP+Cr5 (TH),)	
1010	- נ	2(1)=0.	
	-	EGIN SECONDAPY LPNGTH LCO	
くない		ר לי יו=1,NL2	
	. U	PDANCH IF ATTFAD CP WAVRPRONT	

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raman IV G1	RELEASE 2.0	MAIN DATE = 77027 95/25/2
16ú v 5 5 V J	υι	IF(J.GR.KK2) Gn Tr 65 אאל2=א-JJX+2
	500	NOMENTIN BALANCE
Souù	• •	ALJ=508T ({X?(J+1)-X2(J)) **2+(Y2(J+1)-Y2(J)) **2 +/Y2(J+4)-72/J)(+42)
タセン	- •	ALJP1=SOF([72]]-22[0]]-22[3+1]]+*2+[Y2[3+2]-Y2[3+1]])**2 *********************************
26vi	- •	V (b / (b / c) + 2 / (b / 1) 2) SUBY=T2 (1+1) * ((X2 (3+2) - + 2 (1+1)) / ALJP1) - M0 / + 1 / (b / c / x2 - 2) - + 2 (1+1)) / ALJP1)
rC98	- ,	-T < (U) - ((X < (U + 1) - X < (U)) / X + (U) - X < (U)) / X + ((Z < (U + 2) + Z < (U + 1) * ((Z < (U + 2) + Z < (U + 1) * ((Z < (U + 2) + U) + (U + 2) + (U + 2
r r gg		-:(J) - ((I < (J + 1) - I < (J) / ALJ P) SUMFZ=T2 (J + 1) + ((Z ? (J + 2) - Z2 (J + 1)) / ALJ P1) - T2 (J) * ((Z 2 (J + 1) - Z2 (J)) / ALJ)
~~~~	ں	112 (3+1) = U2 (3+1) +SUMPX+A
r111 112		V2 (J+1) = V2 (J+1) +5UMPY≠A ¥2 (J+1) =¥2 (J+1) +5UMPZ≠A
	υυ	IMPOSE CLAMP BOUNDARY CONDITION
r103 r104 r175	υ	112 (NL2) =0 . V2 (NL2) =0 . H2 (NL2) =0 .
	υ _Ο ι	STPAIN-DISPLACFMENT RPLATION
r 1 AG	υ U	AL^LD=SOPT ((X2(J)-X2(J+1)) *=2+(Y2(J)-Y2(J+1)) *=2
C 49.7	r r ci fi	$\begin{array}{l} + \left[ 22 \left( J \right) - 22 \left( J + 1 \right) \right] = 42 \\ & \lambda LHEW = SOPT \left( \left( X2 \left( J \right) + U2 \left( J \right) + 100 \\ & \pm DT \right) \right) = 42 \\ & \pm DT \right) = 4 \\ & \pm 100 \\ & \pm 100 \\ & \pm 27 \\ & - \left\{ 72 \left( J + 1 \right) \pm 100 \\ & \pm 07 \\ & - \left\{ 72 \left( J + 1 \right) \pm 100 \\ & \pm 07 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\ & - 27 \\$
0100	υ	REAR (J, 3) = 82 (J)
	00	CONSTITUTIVE PREATION (STANDARD LINFAR SOLID)
1115 1115 1115	- -	〒2 (J) = (G * (E2 (J) -B20LD (J) + ( (1VLANDA) +G/TAU) +B2 (J) +DT +T2CLD (J) ) / (1.+DT/TAU) F2∩LD (J) =F2 (J) T2CLD (J) =T2 (J)
	201	CCMPUTE NEW CODEDINATES
0113 0114 0115		X2 (1) =X2 (J) +U2 (J) #100, #DT Y2 (J) =Y2 (J) +Y2 (J) #100, #DT Z2 (J) =Z2 (J) +H2 (J) #100, #DT
	000	END CF SECONDAPY LENGTH LOOP

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PV EL^C=PV FL^C=2.*T1 (1)*SIN (ATAN ((Y1 (1)-Y1 (2))/(X1 (2)-X1 (1))) *9. A0665*DEN*DT/PHASS 15/25/24 IP(KK.GT.KL1) KK=NL1 HRITP(6,1110) (J,X1(J),Y1(J),U1(J),Y1(J),T1(J), J=1,KK,LPSKIP) Т^ч (KK2,ĞT.NL2) KK2=NL2 HPIT[•] (6,1130) (J,X2(J),Y2(J),22(J),U2(J),V2(J),W2(J), ^{m2} (J),F2(J),J=1,KK2,LPSKIP) DATR = 77027 STOPE SELECTED STPAIN VALUES IN PLOT ARRAY HTTF(6,1090) (TTTE(J),J=1,20),T,PVELOC CHPCK= (Y2 (1) - X1 (JX) ) / (X1 (JX+1) - X1 (JX) HへVF=1 IP(IPLCT.PO.0) GC TC 88 Call Frielt(1.Arraz, NMAX, 3,0,0,200,3) CALCULATE VPW FROJPCTILE VELOCITY ŧ١ PPENT FIFLD VARIABLES AT TIMP 39 OL CO (AIXSTITAN' do 10 40 PECYCLE POR NEW TIME INCREMENT 80 LOCATE NEW CROSSOVER NODE IF (IPLTT.FO.N) G7 TO 84 APPAI (K,1) = T#1.08+96 AFPAI (K,2) = P1 (T1) APPAN (K,3) = F1 (T2) APPAN (K,4) = F2 (T3) APPAN (K,4) = F2 (T3) IP (CHFCK.LT.C.) MOV 3=-1 CHECK=CHECK+MrVE 60 T P (K.IT.KK3) GC TO 85 IP (CHFCK.LT.0.5) JX=JX+MOVP MAIN WPITTC(6,1115) JX ITSETP=ITSKIP+1 מהדייב (ה, יוויי) HPITF (6, 112C) CONTT NUE CUNTINUE GO TO 65 ITSKIP=0 **UNTTWIR** kk4=K Continup Kk4=K CONTINUS RELFASS 2.0 ۍ و 59 9 Ê 83 94 85 88 66 000 υυυ υιι υυυ υυυ P.D. Y. N. N. C. T. 0115 0118 0119 122 1122 1124 1124 1124 5447 n126 0147 0147 1161 143 1443 7145 7145 7145 1144 1144 1144 1144

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15/25/24 HRTTF(6,1500) T.AVG1,AVG2,AVG3 1400 F0FMAT(110,//10X,"STRAIN AVFRAGRS AT TIME",E15.4,/15X,3E15.4) C**************** PTRART ('1'.//10%,20A4//) PTRART (15%,PROJFCTILE MASS =',P10.3,"GRAMS'./15%, *PRCJFCTILF VPLCCITY ='.F6.1," M/SRC'./15%, PATE = 77027 OUTPUT OF TITLE AND PROBLEM PARAMETERS JUPHT OF TITLE AND PROBLEM PASAMETERS Та (ТРLOT.FO.C) GO TO 10 САLL PRTFIT (2, АRTAY, KK4, 4, 9, 9, 20°, 4) Сажетество состата С АVRFAGF STPAIN Сатонго PRINT POP MAYINGH STRAIN EXCERDED (2014) (6410.2) (4210.2) (3110,2710.2) AVG3=ÅVG3+F2 (J) 4%=ÅN+1. AVG1=AVG1+P1 (J) AVG2=AVG2+F1 (J) E٩ AN=∩. AVG1=∩. AVG2=∩. AVG3=0. D^ 92 J=10,4C PORAT STATEMPUNS 40 II 6 1140) 41 II 6 1140 Av=0. Do au J=55,85 (4110) AVG2=AVG2/AN no 96 J=5,20 CONTINUE AVG 3=AVG 3/AN CONTINUS AVG1=AVG1/AN AN=AN+1. AN=AN+1. alliilliid 1 1 1 1 TANACT PCRMAT L'V HId VA *ithdid* AN=0. di'uS RELEASP 2.0 1040 1050 1035 100 10201 110 1010 1000 5 94 96 000 00000 600 υ 5 AI hvaiaud (187 187 (187 (183) (183) n 185 n 186 2177 5178 P179 r157 n150 n159 r167 n167 n163 n163 0.164 0.165 2.165 1151 1158 1158 1150 5210 1176 0153 0154 0155 n 156 n 157 1777 0174 175

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1090 PORMAT (11,//10%,20A4,//10%, SEC./10%, OUTPUT POR TIME = . E10.3, SEC./10%, OUTPUT POR TIME = . E10.3, SEC./10%, SC. 10%, CURPER POR TIME PRAJECTLF VELOCITY = . F6.1, M/SEC.) 1100 FORMAT (//10%, 5%, V1(J) . ,5%, U1(J) . ,5%, V1(J) . , 5%, T1(J) . ,5%, F1(J) . , //) 1110 FORMAT (//15%, COSSOVER RODE = . I4) 1115 FORMAT (//15%, COSSOVER RODE = . I4) 1129 FORMAT (//15%, COSSOVER RODE = . I4) 1120 FORMAT (//15%, COSSOVER RODE = . I4) 1120 FORMAT (//15%, COSSOVER RODE = . I4) 1120 FORMAT (//15%, COSSOVER RODE = . I4) 1130 FORMAT (//15%, F1EID VARIABLES FCE SECONDARY FIBER. //9%, F1EID VARIABLES FCE SECONDARY FIBER. //9%, F17.5) 1130 FORMAT (//15%, F1EID VARIABLES FCE SECONDARY FIBER. //9%, F17.5) 1130 FORMAT (//15%, F1EID VARIABLES FCE SECONDARY FIBER. //9%, F17.1, 5%, F7.1, 3%, F7.1, 5%, F7.1, 5%, F7.1, 5%, F7.1, 5%, F7.1, 5%, F7.1, 3%, F7.1, 3%, F7.1, 3%, F7.1, 3%, F7.1, 3%, F7.1, 3%, F7.1, 5%, 15/25/24 FORMAT (///OX, "MAXIMUM STRAIN EXCREDED AT ", E10.3," SEC") PARMAT (15%, LENGTH JACREARAT =, 710.3, CM., /15%, NUMBEP WODES IN PRIMARY =, 14, /15%, WHEBEP WODES IN SECONDARY =, 14, /15%, WHERE WODES IN SECONDARY =, 14, /15%, TIRE INCREMENT =, 710.3, SEC, /15%, CRACSOVER NODE =, 14, /15%, SLIDE FACTOR = 'F6.3'/)
SLIDE FACTOR = 'F6.3'/)
FORMAT (15%, PIREP DEVIRA = 'F6.1, '15%,
 "INSMATANTUS HODILUS = 'F1.1, GM/DEH', '15%,
 "TISCHIS FPACTION = 'F6.3, ')
 "VISCOUS FPACTION = 'F6.3, ')
 "OPMAT (15%, NUMMFF LFNGTH INCREMPNIS = ', I5, '15%,
 "PPINT SKIP PACTOR = ', I3, '15%, nATE = 77027 6 • MAXIMUY NUMBER TIME INCREMENTS =• 16) 10R5 FTRMAT (//15x,•PLOT OPTIONS =• 415) "TIMP SKIP FACTOR =', I3,/15X, "MAXTMUM TIME =', E10.3,' SEC',/15X, "MAXIMUM STRAIN =', F6.3,//) CHITPUT FOR FACH TIMP INCRPAFUT MATN ***AX STRATN MFSSAGE** UNE PFLEASE 2.0 **~~** = v đ m # 5 50 2 1140 1070 1060 1080 υ υU υ e PTRICAN TV r193 r194 r 197 018a 1195 C19R 0187 0189 191 1917 0132 196

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