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An Analysis of the Multiple Objective Capital Budgeting Problem Via Fuzzy Linear Integer (0-1) Programming

CPT. Michael G. Headly HQDA, MILPERCEN (DAPC-OPP-E) 200 Stovall Street Alexandria, VA 22332

May 31, 1980

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A thesis submitted to The Pennsylvania State University, University Park, Pennsylvania, in partial fulfillment of the requirements for the degree of Master of Science in Industrial Engineering and Operations Research.

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fuzzy linear programming as a solution technique for the research and development program or project selection problem. In addition an exchange heuristic, a modified form of C. C. Petersen's exchange algorithm, is presented.

A limited bibliography of works in multiple objective optimization is presented. Two computer codes are included. The first utilizes the IBM MPSX/Mixed Integer Programming procedures to solve the (0-1) linear integer programming problem. The second is a FORTRAN program to solve the exchange heuristic algorithm discussed previously.

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A Thesis in

Industrial Engineering and Operations Research

by

Michael G. Headly

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TABLE OF CONTENTS

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ABSTRACT	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	111
LIST OF TABLES .	•	•	•	•	•	•	•	•	•	•	٠	•	•	•	•	•	•	•	•	•	•	•	•	•	•	vi
LIST OF FIGURES	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	vii
ACKNOWLEDGMENTS	•	•	•	•	•	•	•	•	•	•	•	•	٠	•	•	•	•	•	•	•		•	•	•	•	viii

Chapter

2

:

;

1.	INTRODUCTION	1 1 3
2.	HISTORICAL PERSPECTIVE OF THE CAPITAL BUDGETING PROBLEM .2.1 General .2.2 Survey of Related Literature .	4 4 5
3.	BASIC FUZZY SET THEORY13.1 The Decision-Making Process13.2 Fuzzy Set Theory13.3 Basic Definitions of the Theory of Fuzzy Sets1	0 .0 .0 .3
4.	DECISION MAKING IN A FUZZY ENVIRONMENT24.1Fuzzy Decisions24.2Fuzzy Linear Programming2	1 1 3
5.	ZERO-ONE CAPITAL BUDGETING ALGORITHM 3 5.1 The Capital Budgeting Problem 3 5.2 Fuzzy Linear Integer Programming/Exchange	1
	Heuristic Algorithm	2
	levels and the lowest admissible values 3 5.3.2 Phase II: Determination of a fuzzy linear	3
	5.3.3 Phase III: Determination of an exchange heuristic 0-1 solution	8
	5.4 Example of Three-Phase Algorithm	0
	5.4.2 Phase II: Fuzzy linear integer programming formulation	3
	5.4.3 Phase III: Exchange Heuristic solution 4	.4
	5.6 Analysis and Discussion of Results	5
	5.7 Computer Program	0
	5.8 Computer Code Description 6	0

TABLE OF CONTENTS (continued)

.

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والمستخدر والا

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int.

Chapter	Page
6. SUMMARY, CONCLUSIONS, AND SUGGESTIONS FOR FURTHER	
RESEARCH	63
6.1 Summary and Conclusions	63
6.2 Suggestions for Further Research	64
REFERENCES CITED	66
APPENDIX A: A Brief Look at MPSX	72
APPENDIX B: Fuzzy Linear Integer Programming Via MPSX/MIP Computer Code, Variable Definition Guide,	
User's Guide, and Sample Output	76
APPENDIX C: Fuzzy Linear Integer Programming Via an Exchange Heuristic, Variable Definition Guide, User's	
Guide, and Sample Output	105
APPENDIX D: Sample Data Input	143

Contraction of the local division of the loc

LIST OF TABLES

<u>Table</u>		Page
IV.1	Selected Values for Fuzzy Transformations	28
IV.2	Summary of Calculations	29
V.1	Fuzzy Transformations	34
V.2	Summary of Calculations in Phase I	43
V.3	Calculation of T. Values	45
v. 4	Calculation of R. Values	46
V.5	Calculation of T_j/R_j Values	46
V.6	Initial Ranking of Variables	47
V.7	Determination of the Initial Solution	47
V.8	Determination of Fitback Solution	48
V.9	First Search Exchange Procedure	49
V.10	Attribute Data for Proposed Candidate	51
V.11	Management Specified Attribute Data	52
V.12	Example 2, Attribute Satisfaction	54
V.13	Attribute Data for Proposed Candidate	57
V.14	Comparison of Results	58

vi

LIST OF FIGURES

Figure		Page
1.	Decision Making as a Feedback Process	11
2.	Illustration of Fuzzy Sets A and B	16
3.	Union of Fuzzy Sets A and B	18
4.	Intersection of Fuzzy Sets A and B	19
5.	Fuzzy Decision Process	22
6.	Membership Function of Fuzzy Set A	24
7.	Membership Function for Type I Objective	35
8.	Membership Function for Type II Objective	36
9.	Membership Function for Type III Objective	37

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vii

ABSTRACT

A multiple objective fuzzy linear programming approach to the capital budgeting problem is developed. Since much of the available data in any capital budgeting decision situation is either of an imprecise or ill-defined nature, a mathematical optimization technique is required that is capable of incorporating this inherent uncertainty. Fuzzy linear programming provides an effective methodology for this analysis.

Specifically, a mathematical model is developed which utilizes fuzzy linear programming as a solution technique for the research and development program or project selection problem. In addition, an exchange heuristic, a modified form of C. C. Petersen's exchange algorithm, is presented.

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viii

CHAPTER 1

INTRODUCTION

1.1 Purpose of the Research

The objective of the research documented in this thesis is the application and demonstration of a method for analysis of management decisions involving multiple objectives and constraints which are of a vague or ill-defined nature.

The traditional capital budgeting problem involves a single objective deterministic approach to the allocation of limited resources among available investment opportunities. The selection from among the various investment possibilities is such that the total return from the investment is maximized. In contrast to the traditional problem formulation, real-world capital investment decision analysis invariably encompasses nondeterministic systems involving multiple and usually conflicting objectives.

Investment selection or program selection in research and development planning is a multifaceted decision regularly faced by decision makers in government, industry, and the military. The constantly expanding nature of technological development necessitates decisions that involve multiple objectives in the decision criteria. Simply maximizing total return is an unrealistic and oversimplified decision criterion.

The complex selection process of research development programs may include the consideration of numerous factors, some of which are monetary while others are nonmonetary in nature. Influencing factors, whose primary concern is not income generating, are demonstrated in safety and environmental considerations, which are inherent in virtually all business decisions today. The decision maker is clearly faced with a decision situation which is characterized mathematically as multiple criteria decision making.

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Many mathematical programming techniques have been employed as a means of solving the capital budgeting problem; and, specifically, the investment or program selection problem has received a great deal of attention. A relatively new multiple objective optimization technique is fuzzy linear programming.

Fuzzy linear programming with its foundation in the theory of fuzzy sets is an optimization methodology designed for problems that are either too vague or too ill-defined to allow analysis by classical mathematical techniques. The inherent uncertainty which is ever present in any capital investment decision is the motivating influence in an examination of the applicability of fuzzy linear programming as a solution technique for the capital budgeting problem.

The design of this study encompasses five main objectives. These are:

- Review various mathematical programming methodologies so as to establish applicability to the capital budgeting problem.
- Evaluate the applicability of fuzzy linear programming as a solution technique for the capital budgeting problem.

- Develop a fuzzy linear integer programming algorithm to solve the capital budgeting problem.
- Apply the fuzzy linear integer programming algorithm to a representative problem.
- Discuss extensions of this study and identify additional areas to which fuzzy programming techniques have applicability.

1.2 Organization of the Paper

This paper is organized as follows. Chapter 2 includes a historical perspective of various methodologies that have been employed as solution techniques for the capital budgeting problem. In Chapter 3, the basic elements of the theory of fuzzy sets are reviewed. Decision making in a fuzzy environment is discussed, and the model of fuzzy linear programming is presented in Chapter 4. In Chapter 5, the fuzzy capital budgeting model is presented along with the solution algorithm. Two example problems are solved. The results of the study are reviewed in Chapter 6, as well as possible extensions, and additional areas of applicability are suggested.

CHAPTER 2

HISTORICAL PERSPECTIVE OF THE CAPITAL BUDGETING PROBLEM

2.1 General

Decision makers have always sought a means of analyzing alternative investment possibilities in an efficient manner. The past twenty-five years have seen the development of analytical techniques to provide this analysis. The development of numerous quantitative analysis techniques has provided decision makers with a framework to more efficiently conduct this analysis. The usefulness of these quantitative techniques has been greatly extended with the ever-increasing accessibility of computers. While the computer's capability to analyze and store data has increased tremendously, the cost has steadily decreased. Today, the use of computer technology is widespread. Since the cost of many computers is no longer prohibitive, many small industries are utilizing quantitative analysis techniques that previously were reserved for government and large industries.

The classical approach to the analysis of alternate investment possibilities has been the maximization or minimization of a single objective function. Traditionally, this objective has been the maximization of profits or the minimization of costs. A significant amount of discussion has been generated concerning the classical approach and its inapplicability to today's complex decisions [1-11]. The basis of single objective function mathematical modelling is lost when it is recognized that real decision makers do not attempt to optimize a single objective function. Rather, a solution is sought that satisfies the numerous objective functions that characterize a decision process. The solution is a compromise from among the various objective functions [5, 10, 12, 13]. The compromise is the result of the real-world limitations imposed on decision makers.

2.2 <u>Survey of Related Literature</u>

The multiple objective function optimization technique of fuzzy linear programming is a relatively new approach to multiple criteria decision making. Zimmermann [9, 10, 11] has shown the mathematical feasibility of this approach and its application to the media selection problem originally posed by Charnes et al. [14]. Two extensive bibliographies have been published on works related to fuzzy systems [15, 16]. A search of the literature failed to identify additional works dealing with the application of fuzzy linear programming as a multiple objective optimization technique. Kickert [17] has recently published a work detailing the various fuzzy theories and their impact on decision-making processes. Yager [18] discusses an eigenvector approach to the multiple objective optimization problem using fuzzy sets. There is increasing interest in multiple criteria decision making; and, correspondingly, a great deal of literature is available related to this work. The following paragraphs summarize a survey of the current literature on multiple criteria decision making, with an emphasis toward the capital budgeting problem.

A conference proceedings including numerous works on multiple criteria decision making was published by the University of South Carolina. A bibliography on multiple criteria decision making is included [19].

One mathematical programming technique that has been utilized for years as an optimization technique is linear programming. Charnes and Cooper [20] demonstrated an early use of linear programming as a solution technique for the problem of allocating funds. In recent years, multiple objective linear programming techniques have been developed. Benayoun, Larichev, de Montogolfier, and Tergny [21] discuss a methodology of using linear programming with multiple objectives. Belenson and Kapur [22] present an algorithm for solving multi-criteria linear programming problems with several examples. A multi-objective linear programming methodology has been presented by Evans and Steuer [1].

Goal programming is another robust optimization technique for dealing with decision problems involving multiple objectives. This technique was developed by Charnes and Cooper in the early 1950's [23]. Goal programming is an effective modelling methodology which affords an analysis of problems involving multiple, and possibly, conflicting objectives. The methodology requires an assignment of a priority to each objective. This priority assignment is a preemptive prioritization of the objectives in accordance with the priorities of the decision maker. Lee [13] published the first book entirely devoted to linear goal programming. Ijiri [24] in his work developed the concept of preemptive prioritization of objectives. Numerous applications of goal programming are available. These include capital budgeting optimization [4, 5, 8, 25, 26]; manpower planning [27]; academic planning, financial planning, and economic planning [13]; antenna array design and transportation problem [5]; and media

6

planning [14]. Survey works of goal programming have been published by Kornbluth [28] and Ignizio [3].

Integer and nonlinear goal programming algorithms have been developed and have realized many successful applications [5, 29]. Research is continuing to extend goal programming into the area of stochastic analysis. Contini [30] has demonstrated the mathematical feasibility of such an approach.

Interactive programming is yet another multi-criteria programming approach currently being utilized. The decision maker in this approach is required to specify trade-offs between the various objective functions. The process of specifying trade-offs is continued in a successive manner until no further trade-offs are desired by the decision maker. Geoffrion, Dyer, and Feinberg [31] demonstrate the application of interactive programming, while Zionts and Wallenius [32] present an overview of the interactive programming method as applied to the multiple criteria problem. Dyer [33] has also proposed an interactive goal programming technique, while Steuer [34, 35] has proposed an interactive approach to multiple objective linear programming.

Numerous other mathematical programming techniques have been discussed as solution methods for the multiple criteria decision problem. One technique that has received a great deal of attention is integer programming. The literature has many examples of the successful application of integer programming. Seward, Plane, and Hendrick [36] present an application in the area of allocating municipal funds for fire protection, Armstrong and Willis [37] discuss its use in the selection of water projects in California, and Nackel.

Section and

Goldman, and Fairman [38] demonstrate the use of integer programming in an example in the health care field. Chiu and Gear [39] present a stochastic integer programming approach to the research and development project selection problem.

A few of the other mathematical programming techniques with applications in the multiple criteria decision-making area are branch and bound procedures, dynamic programming and heuristic programming. Shih [40] has written on a branch and bound method, Kepler and Blackman [41] have demonstrated the use of dynamic programming in the selection of research and development projects, and Petersen [42, 43] has developed heuristic algorithms using exchange operations to solve the capital budgeting problem.

The recognition of the inherent risk and uncertainty in capital budgeting problems has been presented in many works in the literature. Hillier [44] presents a basic model for capital budgeting of risky interrelated projects. Stochastic analysis was initially proposed by Charnes and Cooper [45]. Their technique was termed chance-constrained programming. Healy [46] and Armstrong and Balintfy [47] have presented chance-constrained programming algorithms. Odom and Shannon [48] and Park and Theusen [49] have recently published works aimed at risk resolution in the capital budgeting decision analysis. Utility theory has also been a frequently employed technique in multicriteria decision making. Recent works in the literature include: Crawford, Huntzinger, and Kirkwood's [50] use of multiattribute utility theory in the selection of components of an electrical transmission system, and Keefer's [51] multiobjective analysis of research and development projects through the use of a multiattribute utility function.

8

The increased use of multiple criteria decision analysis is evident in the literature. Many excellent overviews of multiple objective optimization techniques are available. MacCrimmon [52] has analyzed the various techniques that are not mathematical programming approaches. These approaches involve either weighting factors methods, sequential elimination methods, or spatial proximity methods. Easton [2] reviews a variety of multivalued alternative weighting methods. Ignizio [3] reviews goal programming as a multiple objective optimization technique. Plane [53] presents integer programming and network analysis techniques, and Hax [54] discusses the use of decision analysis. Two survey papers [55, 56] discuss the use of the various decision-making techniques as related specifically to the capital budgeting problem.

The development of new approaches to the multiple criteria decision problem and the variety of applications of the more established techniques indicate a tremendous interest in multiple criteria optimization methodologies.

CHAPTER 3

BASIC FUZZY SET THEORY

3.1 The Decision-Making Process

The analysis of alternative courses of action culminating in a decision is an extremely complex process for the human mind. The complexity of real-world decision problems far exceed the capacity of the human mind to formulate and subsequently arrive at a reasonable solution [12]. The essence of a decision is that the decision maker is able to exercise his prerogative. Obviously, then, the decision maker must be faced with a situation involving several alternatives about which information is available. This information may be of a precise or exact type, or it may be vague or ill-defined. An effective decision-making process is normally an iterative process with a feedback capability so that, at various stages, additional information may enter into the analysis. The decision-making process with feedback is shown in Figure 1.

Decision making utilizing the multiple objective optimization technique of fuzzy linear programming is an effective methodology in which to employ this feedback process. Prior to any elaboration on fuzzy linear programming, a brief discussion of the basic principles of fuzzy set theory is necessary.

3.2 Fuzzy Set Theory

The theory of fuzzy sets was developed in response to a need for a conceptual framework to deal with problems which were either too



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Figure 1. Decision Making as a Feedback Process

complex or too ill-defined to allow analysis by classical mathematical techniques.

Classical mathematics are much too rigid to be utilized in the optimization of systems that are humanistic in nature. These systems are composed largely of human perceptions and human judgments. Such systems are those in the fields of economics, psychology, sociology, linguistics, management science, medicine, law, philosophy, and others whose basic tenents are imprecise or fuzzy in nature.

The theory of fuzzy sets is founded on the theory of classes. Events may be viewed as in a continuum with respect to their membership or nonmembership in a class. The degree of membership in a class is the fundamental concept in the theory.

Classical mathematics' precise formulation of decision situations does not allow for the inclusion of a decision maker's judgmental capability. The concepts of fuzzy set theory create an overlap of the decision maker's judgmental ability and his quantitative analysis capabilities. The judgmental capability of the human mind analyzes a situation in an imprecise or approximate manner.

This imprecise or approximate analysis is necessitated by the complexity of today's managerial decision requirements. Real-life problems present themselves daily in vague or ill-defined ways. Many phenomena exist such as "satisfactory profits," "adequate return on investment," or "better productivity." None of these problems could be defined in precise mathematical terms. Instead, they would be twisted so as to conform to a precise mathematical optimization technique; and, therefore, the derived solution may or may not be accurate. In our attempts to understand and optimize systems which

are composed of various humanistic subsystems, the solutions obtained may pretend a higher degree of preciseness than is actually possible to achieve in the real system [57].

Fuzzy set theory provides a formal mathematical theory to analyze systems that are vague or inexact, with the vague or inexact nature defined by a fuzzy set [58].

3.3 Basic Definitions of the Theory of Fuzzy Sets

Zadeh [57] introduced the theory of fuzzy sets through the theory of sets, a generally universal mathematical theory. A set is defined as consisting of a finite or infinite number of elements [59]. The characteristic function of a set enables us to discuss the membership of the set in terms of functions. To define the characteristic function of a set, let A be a subset of the universe [60]. The function χ_A , the characteristic function, can only take on the values 0 or 1. If the universe is $X = \{x\}$, then χ_A is defined by the following:

Zadeh [57] utilized this concept of the characteristic function in his development of fuzzy set theory. Instead of the characteristic function being limited to only taking on the values 0 or 1, it is generalized to assume an infinite number of values between 0 and 1.

The basic definitions of fuzzy set theory which are important in the development of fuzzy linear programming will be presented in the following pages. These definitions are summarized from presentations by Zimmermann [9, 10, 11, 16] and Kickert [17].

<u>Fuzzy Set</u> - A class with a continuum of grades of membership. Let X be a space of points (objects), with a generic element of X denoted by x_1 , then, $X = \{x\}$. The fuzzy set A in X is characterized by a membership function $\mu_A(x)$ which associated with each point in X a nonnegative real number whose supremum is finite, with $\mu_A(x)$ representing the grade of membership of A in X. This is represented as:

 $A = \{x, \mu_A(x) | x \in X\},$ where $\mu_A(x)$ is the membership function of A in X.

Example: In the field of psychology, and specifically related to learning theory, the concepts of performance, learning, motivation, and anxiety are critical in the prediction of the outcome of any learning acquisition task. Let

X = {0, 10, 20, 30, 40, 50, 60, 70, 80, 90, 100} be possible scores which an individual may attain on a learning acquisition task. Fuzzy set A, "Motivation Levels Affecting Learning Acquisition," may be defined for a certain individual as:

 $A = \{(10, 0.2), (20, 0.4), (30, 0.6), (40, 0.65), (50, 0.7), (60, 0.75), (70, 0.85), (80, 1.0), (90, 0.9), (100, 0.8)\}$

Fuzzy set B, "Anxiety Levels Affecting Learning Acquisition," may be stated in a similar manner for the same individual as follows:

 $B = \{(10, 0.1), (20, 0.3), (30, 0.5), (40, 0.60), (50, 0.65), (60, 0.75), (70, 0.85), (80, 0.95), (90, 1.0), (100, 0.85)\}$

Graphically, these two fuzzy sets are shown in Figure 2.

<u>Intersection</u> - In set theory, the intersection of two sets A and B, written $A\cap B$, is the set C containing all elements common to A and B. In fuzzy set theory, the membership function of $A\cap B$ is defined as:

 $\mu(x) = Min [\mu_A(x), \mu_B(x)]$ for all xEX.

<u>Union</u> - In set theory, the union of two sets A and B, written $A\cup B$, is the set D containing all elements in either A or B, or both. In fuzzy set theory, the membership function of $A\cup B$ is defined as:

 $\mu(x) = Max [\mu_A(x), \mu_B(x)]$ for all xEX.

Example: In the learning theory example, the fuzzy set representing the union of fuzzy sets A and B would be the fuzzy set D. Fuzzy set D is defined as:



Figure 2. Illustration of Fuzzy Sets A and B

$$D = \{(10, 0.2), (20, 0.4), (30, 0.6), \\ (40, 0.65), (50, 0.7), (60, 0.75), \\ (70, 0.85), (80, 1.0), (90, 1.0), \\ (100, 0.85)\} .$$

The union of fuzzy sets A and B is displayed in Figure 3, and the intersection of the two fuzzy sets is shown in Figure 4.

Equality - Two fuzzy sets are equal if

 $\mu_A(x) = \mu_B(x)$ for all xEX.

<u>Normality</u> - The definition of the membership function did not limit the values $\mu(x)$ could assume. If the supremum of the membership function equals 1, then the fuzzy set is called normal. This is defined as:

 $\sup_{\mathbf{x}}\mu_{\mathbf{A}}(\mathbf{x}) = 1$

A fuzzy set can be normalized by dividing $\mu_{A}(x)$ by $Sup_{X} \ \mu_{1}(x) \ .$

<u>Algebraic Product</u> - The algebraic product of two fuzzy sets A and B is denoted AB and is defined in terms of the membership functions of the fuzzy sets A and B.

$$\mu_{AB}(\mathbf{x}) = \mu_{A}(\mathbf{x}) \cdot \mu_{B}(\mathbf{x})$$

<u>Algebraic Sum</u> - The algebraic sum of two fuzzy sets A and B is denoted by (A + B) and is defined in terms of the membership functions of the fuzzy sets A and B. $\mu_{(A+B)}(x) = \mu_A(x) + \mu_B(x) - \mu_A(x) \cdot \mu_B(x)$.



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<u>Containment</u> - The fuzzy set definition of containment is analogous to the set theory definition of a subset. Fuzzy set A' is contained in fuzzy set B' if the membership function of A' is less than or equal to that of B' everywhere on X.

The basic definitions presented are sufficient for the discussion of fuzzy linear integer programming; however, there are many more concepts in the overall theory of fuzzy sets. For a more extensive treatment of the theory of fuzzy sets, Kaufmann [61] presents a complete review of the general theory of fuzzy sets.

CHAPTER 4

DECISION MAKING IN A FUZZY ENVIRONMENT

4.1 Fuzzy Decisions

In traditional decision making, the optimal decision is the selection of the activity or program with the highest desirability. In fuzzy decision making, the objective function(s) as well as the constraints may be fuzzy sets, each characterized by their membership functions. The optimal decision in the fuzzy environment is the fuzzy set formed by the intersections of the fuzzy sets describing the objective function(s) and constraints. Figure 5 illustrates the fuzzy decision process.

The region of intersection is a fuzzy set representing those activities which simultaneously satisfy the objective function(s) and the constraints. A solution to this fuzzy situation would be to select that point in the region of intersection with the greatest desirability or the highest degree of membership in the fuzzy set formed in the fuzzy decision. The selection of this solution point is analogous to the geometric representation of a solution to a linear programming problem [62]. The determination of the solution to the linear programming problem involving the intersection of a fuzzy linear integer programming.



4.2 Fuzzy Linear Programming

The extension of fuzzy set theory into linear programming was utilized by Zimmermann [9]. The development of the fuzzy linear programming problem is as follows:

Start with the traditional vector minimization problem.

The fuzzy version of this same linear programming problem is:

 $\begin{array}{c}
\overline{C} \overline{z} \\
\overline{C} \overline{z} \\
\overline{\lambda} \overline{\lambda} \\
0
\end{array}$

where

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 \overline{C} is the vector of coefficients of the objective functions,

 \overline{b} is the vector of constraints,

A is the coefficient matrix, and

 \overline{Z}° is the vector of aspiration levels of the fuzzy objectives and constraints.

The membership function $\mu(\mathbf{x})$ is defined such that it complies with the definition of a fuzzy set [57], that is, a real number in the interval (0,1).

 $\mu(\mathbf{x}) = \begin{cases} 1 & \text{if } A\overline{\mathbf{x}} \leq \overline{\mathbf{b}} \text{ and } \overline{\mathbf{C}} \ \overline{\mathbf{x}} \leq \overline{\mathbf{Z}} \text{ is satisfied} \\ \\ 0 & \text{if } A\overline{\mathbf{x}} \leq \overline{\mathbf{b}} \text{ and } \overline{\mathbf{C}} \ \overline{\mathbf{x}} \leq \overline{\mathbf{Z}} \text{ is strongly violated.} \end{cases}$

The concept of an objective function being strongly violated or weakly violated is an important aspect of the decision-making process in a fuzzy environment. The membership function in Figure 6 will be utilized


to illustrate this principle. Let this membership function be referred to as $\mu(\mathbf{x})$. In the interval CD, the membership function $\mu(\mathbf{x})$ is completely satisfied. The function describing the fuzzy set in this interval either achieves the aspiration level or exceeds it. In the interval BC, the membership function $\mu(\mathbf{x})$ is weakly violated. In this interval, the aspiration level is not achieved; however, the functional evaluation is greater than the lowest admissible value (Point B). The decision in this interval lies within the range of acceptable solutions as specified by the decision maker. In the interval AB, the membership function $\mu(\mathbf{x})$ is strongly violated. In this interval, any decision would lie wholly outside the acceptable range of solutions, since the functional evaluation of the fuzzy set would be less than the lowest admissible value, as specified by the decision maker.

If we let the fuzzy set B represent the intersection of the fuzzy sets representing the objective functions and the constraints, then the membership function of fuzzy set B is:

 $\mu_{\mathbf{B}}(\mathbf{x}) = \mu_{\mathbf{O}} \cap \mu_{\mathbf{C}}$

The intersection of these two fuzzy sets is defined by the min operator to be:

 $\mu(\mathbf{B}\mathbf{x}) = \min_{\mathbf{i}} \mu_{\mathbf{i}} ; \mathbf{x} \ge 0$

The maximizing decision is simply

 $\begin{array}{c} \max \min \left[\mu_{i}(Bx)_{i}\right] \\ x>0 \quad i \end{array}$

which minimizes the maximum violation of the membership function.

If the solution technique is to be linear programming, the following assumptions are necessary [11]:

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 All objective functions must have a specified aspiration level. The objective functions are expressed in the form

 $C_i \overline{x} \leq Z_i$, i = 1, 2, ..., n.

2. If the objective functions are in the same form as the constraints, then the problem may be formulated in the following form:

$$A\overline{x} < \overline{b}$$

where

- A is the matrix of coefficients, and
- b is the vector of aspiration levels of the objectives and the right-hand side values of the constraints.
- 3. The functions are assumed to be linear over the interval of consideration.

Given that assumption number (3) is satisfied, the linear membership function of fuzzy set B, the solution set of the intersection of the fuzzy sets representing the objectives and the constraints is:

 $\mu_{B}(x)_{i} = \begin{cases} 1 & \text{if } (Bx)_{i} \leq b_{i}' \\ 1 - \frac{(Bx)_{i} - b_{i}'}{d_{i}} & \text{if } b_{i}' < (Bx)_{i} \leq b_{i}' + d_{i} \\ 0 & \text{if } (Bx)_{i} > b_{i}' + d_{i} \end{cases},$

where

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- i indicates the ith row of matrix B or b',
- B is A, the coefficient matrix, augmented by the rows of the objective functions,

b' is the vector of the right-hand side values augmented by the upper bounds of the objective functions, and

d, is the subjectively selected value of admissible violation.

By substituting

$$b''_i = \frac{b'_i}{d_i}$$
 and $b'_i = \frac{b_i}{d_i}$

into the function $\mu_{R}(x)$, the maximizing decision then becomes:

or

 $\begin{array}{ll} \max & \mu_{D}(\mathbf{x}) \\ \mathbf{z} \geq 0 \end{array},$

where $\mu_{D}(x)$ represents the membership function of the fuzzy set representing the decision set.

It has been shown that the solution to this problem is equivalent to the following linear programming problem [9, 10, 11]:

Maximize λ Subject to $\lambda \leq b_i'' - (B'x)_i$, i = 0, 1, ..., nx > 0.

To demonstrate a continuous fuzzy linear programming problem, consider the following example:

Maximize
$$Z = 4x_1 + 6x_2 + 8x_3 + 10x_4$$

Subject to $x_1 + 3x_2 + 4x_3 + 2x_4 \le 40$
 $3x_1 + 2x_2 + 3x_3 + 6x_4 \le 60$
 $4x_1 + x_2 + 2x_3 + 3x_4 \le 50$

Solving this linear programming problem with the IBM MPSX mathematical programming system, the resulting program :

 $\overline{x} = (0, 8.57, 0, 7.14)$

and

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$$Z = 122.86$$

The problem when formulated into the fuzzy linear programming equivalent utilizing the subjectively selected d_i values follows. The aspiration levels and the lowest admissible values as well as the allowable admissible ranges are shown in Table IV.1.

Table IV.1. Selected Values for Fuzzy Transformations

	$\mu = 0$	<u>µ = 1</u>	
Objective function	115	140	25
First constraint	50	40	10

where

- µ = 0 decision maker specified lowest
 admissible value,
- $\mu = 1$ decision maker specified aspiration level,
 - d decision maker specified range of acceptable values.

The resulting fuzzy linear programming formulation is:

Maximize λ Subject to $\lambda \leq -4.6 + 0.16x_1 + 0.24x_2 + 0.32x_3 + 0.4x_4$ $\lambda \leq 5 - 0.1x_1 - 0.3x_2 - 0.4x_3 - 0.2x_4$ $3x_1 + 2x_2 + 3x_3 + 6x_4 \leq 60$ $4x_1 + x_2 + 2x_3 + 3x_4 \leq 50$.

The solution to the fuzzy linear programming formulation is compared to the linear programming solution in Table IV.2. The fuzzy linear programming problem was solved using the IBM MPSX mathematical programming system.

Table	IV.2.	Summary	of	Calo	culation	s
Lir Progra	near mming		Fu Pro	zzy ogra	Linear	
×1 =	0.0		×1	3	0.0	
* ₂ =	8.57		×2		10.59	
×3 =	0.0		×3	=	0.0	
× ₄ =	7.14		×4	2	6.47	
Z = 12	2.86		z	=]	L28.24	

The first advantage of fuzzy programming is that the decision maker is not required to specify in a precise manner the parameters of a decision situation. The decision maker is able to specify ranges of acceptability for those objective and constraint functions represented by fuzzy sets. In this example problem, the flexibility obtained in the use of fuzzy linear programming enabled the decision maker to realize a greater return.

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The second advantage of fuzzy programming is the ease with which it can be converted into a conventional mathematical programming problem. This is important due to the current availability of many mathematical programming techniques and algorithms [17].

CHAPTER 5

ZERO-ONE CAPITAL BUDGETING ALGORITHM

5.1 The Capital Budgeting Problem

The traditional capital budgeting problem involves a single objective function deterministic approach to the allocation of limited resources among available investment opportunities. This approach differs greatly from most real-world capital budgeting problems. Actual resource allocation distribution procedures involve an analysis which is by necessity nondeterministic and sensitive to numerous conflicting interests. Due in part to this divergence between the traditional mathematical model of the capital budgeting problem and the necessities of real-world decision making, a significant amount of discussion has been generated concerning the traditional approach and its applicability to today's complex decision-making procedures [1-11].

The solution to the capital budgeting problem obtained in a model which seeks a compromise from among the numerous objective functions which represent the decision situation is a more viable methodology to characterize today's complex decision-making situations [5, 10, 12, 13]. Rather than a single objective function model of the capital budgeting problem, the general multiple objective function model takes on the following form:

Maximize
$$\sum_{j=1}^{n} r_{kj} x_{j} \qquad k = 1, 2, ..., K$$

Subject to
$$\sum_{j=1}^{n} c_{ij} x_{j} \leq b_{i} \quad \forall i$$
$$x_{j} = (0,1) ,$$

where the terms are defined as:

$$\begin{aligned} \mathbf{x}_{j} &= \begin{cases} 1 & \text{if the } j^{\text{th}} \text{ alternative is selected} \\ 0 & \text{if the } j^{\text{th}} \text{ alternative is not selected,} \end{cases} \\ \mathbf{r}_{kj} &= & \text{return on objective } k & \text{from alternative } j , \\ \mathbf{c}_{ij} &= & \text{requirement of resource } i & \text{by alternative } j , \\ \mathbf{a}_{i} &= & \text{limitation of resource } i . \end{cases}$$

Many multiple objective optimization techniques have been employed in the solution of this problem; these were discussed in Chapter 2.

5.2 Fuzzy Linear Integer Programming/Exchange Heuristic Algorithm

An algorithm is developed which combines the principles of fuzzy linear programming and Petersen's [42] exchange heuristic to solve the multiple objective capital budgeting problem. The algorithm is intended to solve the following capital budgeting problem:

Maximize $\sum_{j=1}^{n} r_{kj} x_{j} = 1, 2, ..., K$ Subject to $\sum_{j=1}^{n} c_{ij} x_{j} \leq b_{i} \quad \forall i$ $x_{j} = (0,1) ,$

where the terms are defined previously.

The algorithm is a three-phase solution technique which incorporates an interactive process between the analyst and the decision maker in Phase I. In Phase II, a fuzzy linear integer problem is solved. Phase III, the exchange heuristic, is utilized if a 0,1 solution was not obtained in Phase II.

5.3 The Algorithm

5.3.1 <u>Phase I: Determination of aspiration levels and the</u> <u>lowest admissible values</u>. Phase I of the algorithm is intended to be an interactive process between the analyst and the decision maker. In this phase, K successive linear programming problems are solved, where K is the number of fuzzy objectives. The constraint set is to remain constant throughout the evaluations. In this manner, each objective function yields the highest attainable value possible. This value will be referred to as the Aspiration Level.

The lowest admissible value for each function is determined from the programs which yield the aspiration levels for the other K-1 functions. The value determined to be the lowest admissible value when subtracted from the aspiration level yields the allowable tolerance interval for each objective function.

The calculated values for the aspiration levels, lowest admissible values, and the tolerance intervals should then be reviewed by the decision maker. It rests with the decision maker to provide the analyst with the values to continue the algorithm in Phase II. This interactive process is critical to the fundamental concept of fuzzy programming, that the theory of fuzzy sets combines the quantitative aspects of optimization with the judgmental abilities of decision makers.

The programming procedure utilized to complete this phase is the IBM MPSX Linear Programming technique. Appendix A discusses the IBM MPSX system in greater detail.

5.3.2 <u>Phase II: Determination of a fuzzy linear integer</u> <u>programming solution</u>. In Phase II, a fuzzy transformation is carried out on each fuzzy function, and a linear integer programming problem is solved to maximize the value of the membership function.

The fuzzy transformation depends on the type of function under consideration. The three possibilities are shown in Table V.1. The \overline{d}_i and \underline{d}_i are the selected upper and lower bounds of the tolerance interval specified by the decision maker. Graphically, these three functions are shown in Figures 7, 8, and 9.

Table V.1. Fuzzy Transformations

Type Objective

Ι.	Equal or exceed b _i	$\lambda \leq 1 - \frac{b_i - (2x)_i}{\frac{d_i}{1}}$
11.	Equal or less than b _i	$\lambda \leq 1 - \frac{(Zx)_{i} - b_{i}'}{\frac{d_{i}}{d_{i}}}$
	Equal b _i	a. $\lambda \leq 1 - \frac{b_i' - (Zx)_i}{\frac{d_i}{d_i}}$
		and

b. $\lambda \leq 1 - \frac{(Z_x)_i - b'_i}{\overline{d}_i}$

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Figure 8. Membership Function for Type II Objective



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The fuzzy linear integer programming problem formulation typically may be expressed as follows:

Maximize λ

Subject to	λ <	1 -	<u>b'</u>	- (Zx) _i d _i	,	i = 1,	•••,	K
and	(Ax) _i	<u><</u>	^b i	,				
	×j	<	1	¥j,				

where $(Ax)_i$ is the set of rigid constraint functions, and each variable has an upper bound of 1.0.

If the solution to this linear programming problem is satisfactory to satisfy the 0-1 restrictions, then the algorithm terminates; otherwise, proceed to Phase III.

5.3.3 Phase III: Determination of an exchange heuristic 0-1 solution. The exchange heuristic, a modified form of Petersen's [42], is composed of three major steps:

i. Determination of an initial solution.

ii. Determination of a fitback solution.

iii. Utilize exchange operations progressively to improve the solution so as to finally achieve at least a local optimum.

<u>Determination of an Initial Solution</u> - The initial solution is obtained after ranking each variable based on the value of the ratio T_j/R_j given n variables and m objective functions, where T_j is the summation of the coefficient values of each variable in the fuzzy objectives, and

Determination of a Fitback Solution - In general, following the selection of an initial solution, there will be some degree of slack for each constraint. The fitback solution selects from the initially nonselected variables ranked K + 1 to n, one or more that can be included with the selected variables without violating any constraint.

Exchange Operations - The alternatives in the sets of selected and nonselected variables are ranked according to their T_j value. In the set of selected variables, the variables are ranked starting with the lowest value first, while in the set of nonselected variables, variables are ranked with the highest value first.

The search procedure is a two-step process. For each exchange, it is determined if the exchange under consideration would cause an improvement in the membership

function. If an improvement is noted, then the feasibility of the exchange is examined.

The set of exchanges is divided into two groups. The first search consists of the 2/1, 1/1, and 1/2exchanges, while the second search considers 3/1, 3/2, and 3/3 exchanges. In each case, the first number refers to the number of variables selected from the set of nonselected variables.

The sequencing of the variables in the sets of selected and nonselected variables is performed to reduce the number of searches necessary to obtain a solution. The sequence allows for the examination of the most profitable exchanges first. Then, if an exchange is advantageous, the search is reduced due to dominance. In ordering the sets of selected and nonselected variables, the search proceeds naturally from the most advantageous exchanges to least advantageous exchanges.

5.4 Example of Three-Phase Algorithm

The three-phase algorithm is most easily explained via an example. Consider a problem in which the decision-making situation is characterized by two fuzzy objective functions and three rigid constraint functions. Assume this decision has the following problem formulation:

Maximize $Z_1 = 3x_1 + 5x_2 + 5x_3 + x_4$ Maximize $Z_2 = x_1 + x_3 + x_4$ Subject to $2x_1 + x_2 + 3x_3 + x_4 \leq 6$ $x_1 + 2x_2 + 4x_3 + 2x_4 \leq 5$ $3x_1 + 2x_2 + x_3 + x_4 \leq 4$ $x_1 = (0,1)$.

5.4.1 <u>Determine the Aspiration Level and Lowest Admissible</u> <u>Value for each objective</u>. To calculate the aspiration level of the objective functions, the optimization technique of linear programming is utilized. Solving a linear programming problem to maximize each objective function subject to the same set of constraint functions yields the highest attainable value of the solution or the aspiration level. Thus, for the example:

(a) Maximize
$$Z = 3x_1 + 5x_2 + x_4$$

Subject to $2x_1 + x_2 + 3x_3 + x_4 \stackrel{<}{-} 6$
 $x_1 + 2x_2 + 4x_3 + 2x_4 \stackrel{<}{-} 5$
 $3x_1 + 2x_2 + x_3 + x_4 \stackrel{<}{-} 4$

Solution: $z_1 = 9.55$ $x_1 = 0.45$ $x_3 = 0.64$ $x_2 = 1.00$ $x_4 = 0.0$

(b) Maximize
$$Z_2 = x_1 + x_3 + x_4$$

Subject to $2x_1 + x_2 + 3x_3 + x_4 \le 6$
 $x_1 + 2x_2 + 4x_3 + 2x_4 \le 5$
 $3x_1 + 2x_2 + x_3 + x_4 \le 4$

Solution:
$$Z_2 = 5.36$$

 $x_1 = 0.82$ $x_3 = 0.55$
 $x_2 = 0.0$ $x_4 = 1.00$

To calculate the lowest admissible value for each of n objective functions, evaluate each objective function with the other n - 1linear programming solution programs. Select as the lowest admissible value for each objective function the minimum resulting evaluation. Thus, for the example:

(a) Evaluate objective function Z₁ with the program obtained in Item (b) of the determination of the aspiration level.

 $Z_{1|(0.82,0,0.55,1.0)} = 3x_{1} + 5x_{2} + 5x_{3} + x_{4}$ $Z_{1(LAV)} = 6.21$.

(b) Evaluate objective function Z₂ with the program obtained in Item (a) of the aspiration level.

$$\binom{Z_2}{0.45,1.0,0.64,0} = x_1 + x_3 + x_4$$

 $\binom{Z_2}{LAV} = 1.09$.

The results of Phase I of the algorithm are summarized in Table V.2.

Table V.2. Summary of Calculations in Phase I

Objective Function Aspiration Level		Lowest Admissible Value	Tolerance Interval	
z ₁	9.55	6.21	3.34	
z ₂	5.36	1.09	4.27	

5.4.2 <u>Phase II: Fuzzy linear integer programming formulation</u>. The initial step in the fuzzy linear integer programming problem formulation is to determine the type of objective function and transform the objective function as appropriate. The fuzzy transformations were shown in Table V.1. Thus, for the example:

Since both fuzzy functions are Type I functions, the transformations are as follows:

 $Z_{1}: \lambda \leq 1 - \frac{[9.55 - (3x_{1} + 5x_{2} + 5x_{3} + x_{4})]}{3.34}$ $\lambda \leq 1 - (2.85 - 0.8982x_{1} - 1.497x_{2} - 1.497x_{3} - 0.299x_{4})$ $\lambda \leq -1.85 + 0.8982x_{1} + 1.497x_{2} + 1.497x_{3} + 0.299x_{4})$ $Z_{2}: \lambda \leq 1 - \frac{[5.36 - (x_{1} + x_{3} + 4x_{4})]}{4.27}$ $\lambda \leq 1 - (1.255 - 0.2342x_{1} - 0.2342x_{3} - 0.9367x_{4})$ $\lambda \leq -0.255 + 0.2342x_{1} + 0.2342x_{3} + 0.9367x_{4} \quad .$

The formulation as a fuzzy linear integer programming problem is:

Maximize

λ

Subject to
$$\lambda \leq -1.85 + 0.8982x_1 + 1.497x_2 + 1.497x_3 + 0.299x_4$$

 $\lambda \leq -0.255 + 0.2342x_1 + 0.2342x_3 + 0.9367x_4$
 $2x_1 + x_2 + 3x_3 + x_4 \leq 6$
 $x_1 + 2x_2 + 4x_3 + 2x_4 \leq 5$
 $3x_1 + 2x_2 + x_3 + x_4 \leq 4$
 $x_4 = (0,1)$

Solution: $\lambda = 0.21$

 $x_1 = 1.0$ $x_3 = 1.0$ $x_2 = 0.0$ $x_4 = 0.0$

The solution is in the form (0,1); however, Phase III will be utilized to illustrate the exchange heuristic.

5.4.3 <u>Phase III: Exchange Heuristic solution</u>. The first step in this Exchange Heuristic approach is to set up the problem in the standard form as described previously (Section 5.2). In the example under consideration, this formulation is as follows:

Maximize
$$\lambda$$

Subject to $2x_1 + x_2 + 3x_3 + x_4 \le 6$
 $x_1 + 4x_3 + 4x_3 + 2x_4 \le 5$
 $3x_1 + 2x_2 + x_3 + x_4 \le 4$
 $\lambda - 0.8982x_1 - 1.497x_2 - 1.497x_3 - 0.299x_4 \le -1.85$
 $\lambda - 0.2342x_1 - 0.2342x_3 - 0.9367x_4 \le -0.255$
 $x_1 = (0,1)$

The second step is to determine an initial solution. The variables comprising the initial solution are determined by ranking each variable based on the ratio T_j/R_j . T_j is defined as the summation of the coefficients of each variable in the fuzzy objective functions. In the example, there are two fuzzy objectives. Thus, in the example, the calculation of the T_j values is as follows:

Table V.3. Calculation of T, Values

Variable	Fuzzy Objective 1	Fuzzy Objective 2	T _j = ∑c _{ij}	
^x 1	-0.8982	-0.2342	-1.1324	
*2	-1.497	0.0	-1.497	
×3	-1.497	-0.2342	-1.7312	
×4	-0.2990	-0.9367	-1.2357	

The R_j values are calculated by evaluating the ratio of the coefficients of both the fuzzy objective functions and the rigid constraint functions to the appropriate b_i values. In the example problem, the calculation of the R_i values is as follows:

Table V.4. Calculation of R, Values

Variable	j	R _j Values
×1	$\frac{-0.8982}{-1.85} + \frac{-0.2342}{-0.255} + \frac{1}{5} + \frac{3}{4} + \frac{2}{6}$	2.69
*2	$\frac{-1.497}{-1.85} + 0 + \frac{2}{5} + \frac{2}{4} + \frac{1}{6}$	1.876
×3	$\frac{-1.497}{-1.85} + \frac{-0.2342}{-0.255} + \frac{4}{5} + \frac{1}{4} + \frac{3}{6}$	3.27
×4	$\frac{-0.2990}{-1.85} + \frac{-0.9367}{-0.255} + \frac{2}{5} + \frac{1}{4} + \frac{1}{6}$	4.65

The ratio T_j/R_j is calculated from the results obtained in Table V.3 and Table V.4. In the example problem, the T_j/R_j values are:

	Table V.5.	Calculation of	^T j ^{/R} j	Values	
Variabl	e 	T _j	Rj		T _j /R _j
× ₁		-1.1324	2.69		-0.420
×2		-1.497	1.87	6	-0.798
×3		-1.7339	3.27		-0.530
x,		-1.2357	4.65		-0.266

The initial solution may be calculated by ranking the n variables according to their respective T_j/R_j values. Variables with the highest values of the T_j/R_j ratio are placed at the top of the ranking list. Variables are rejected from the bottom of the list until the rejection of the Kth variable causes satisfaction of $\sum_{j=1}^{k-1} c_{ij} \leq b_i$ for all rigid constraints. The initial solution is comprised of those variables ranked 1 through K-1. The initial ranking of the variables is as follows:

Table V.6. Initial Ranking of Variables

Variable	Initial Ranking
×1	2
*2	4
× ₃	3
x4	1

The initial solution may be determined as follows:

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Table V.7. Determination of the Initial Solution

Objective	Functional Evaluation				
Function	$\{4,1,3,2\}$	$\{4,1,3\}$	<u>{4,1}</u>		
1	7*	6	3	Initial Solution	{4,1}
2	9*	7*	3	Set of Selected Variables:	{4,1}
3	7*	5*	4	Set of Nonselected Variables:	{2,3}
4	-4.19	-0.269	-1.19	Value of Membership	• •
5	-1.41	-1.40	-1.17	Function:	0.0

* Indicates constraint functions that are not satisfied.

The third step in the exchange heuristic is to determine a fitback solution. The fitback solution selects from the set of initially nonselected variables one or more than can be included with the selected variables without violating any constraint. Table V.8 displays the calculation of the fitback solution.

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Objective		cional Evaluation	
Function	{4,1,3}	$\{4,1,2\}$	
1	6	4	Since at least one constraint is violated in each possible fitback
2	7*	5	solution, therefore, the fitback solution is the same as the initial
3	5*	6*	solution, {4,1}.
4	-2.69	-2.69	
5	-1.40	-1.40	

Table V.8. Determination of Fitback Solution

*Indicates constraint functions that are not satisfied.

The fourth step consists of utilizing exchange operations progressively to improve the solution. After each exchange, the feasibility of the exchange is examined. If the exchange is feasible, the possible improvement in the membership function is examined. If an improvement is not noted, then proceed to the next exchange possibility. Table V.9. displays the search procedure examining the possible exchanges.

Table V.9. First Search Exchange Procedure

List of Selected Variables: {4,1}			List Nonselected	of Variables: {2,3}
Attempted Exchange		_λ	<u>λ max</u>	Selected Variables
(2/1)			0.0	{4,1}
(2,3) for 4	Infeasible Exchange		0.0	{4,1}
(2,3) for 1	Infeasible Exchange		0.0	{4,1}
(1/1)				
(2) for 4	Infeasible Exchange		0.0	{4,1}
(2) for 1	Infeasible Exchange		0.0	{4,1}
(3) for 4	Advantageous/ Feasible	0.21	0.21	{3,1}

First Search

Repeat First Search

List of Selected Variables: {3,1} List of Nonselected Variables: {2,4}

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The algorithm utilizes a second pass through the list of nonselected variables once a favorable exchange has been noted. In the example problem, the second search produced no exchange advantageous to the membership function. Therefore, the final solution to the example is:

> Set of Selected Variables: $\{3,1\}$ Value of Membership Function: $\lambda = 0.21$

5.5 Example Number 2, Project Selection Example

In order to illustrate a capital budgeting problem in which the decision situation is program or project selection, the following example is presented. In this example, the decision maker has specified firm values for the aspiration levels and acceptable ranges of admissibility for each fuzzy function [6].

A systems engineer has to design an integrated system composed of three subsystems, designated A, B, and C. Three systems have been proposed for Subsystem A, four for Subsystem B, and three for Subsystem C. Four attributes were established by management to guide in the selection of the subsystems. These are weight, development costs, estimated reliability, and power requirements. Table V.10 summarizes the attribute characteristics for each proposed candidate.

Design incompatibilities exist between Candidates A-2 and C-9. Also, due to design features, if Candidate B-7 is selected, then Candidate C-10 must be selected.

Management has established firm values for the aspiration levels and allowable ranges of admissibility. Table V.11 summarizes this information for each attribute.

Table V.10. Attribute Data for Proposed Candidates

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		Subsys	tem A		Subsys	stem B			Subsyst	em C
Attribute	-	7	~	4	S	9	7	8	6	97
Weight (lb.)	32	57	19	95	107	61	48	23	10	15
Cost (\$10 ⁴)	120	95	160	64	67	96	119	42	36	70
Rellability	0.97	0.94	0.99	0.89	0.90	0.94	0.96	0.98	0.97	0.99
Power (watts)	21	35	10	60	83	27	50	12	7	16

Attribute	Aspiration Level	Lowest Admissible Value	Highest Admissible Value
Weight (lb.)	150	120	165
Cost (\$10 ⁴)	195	260	
Power (watts)	100	70	110

Table V.11. Management Specified Attribute Data

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Mathematically, this problem may be formulated as a system of linear equations. The reliability constraint may be transformed to a linear equation via the transformation $Z = (Y)^X = Z \ln Y$:

$$Z_{1} = 32x_{1} + 57x_{2} + 19x_{3} + 95x_{4} + 107x_{5} + 61x_{6} + 48x_{7} + 23x_{8} + 10x_{9} + 15x_{10}$$

$$Z_{2} = 120x_{1} + 95x_{2} + 160x_{3} + 64x_{4} + 67x_{5} + 96x_{6} + 119x_{7} + 42x_{8} + 36x_{9} + 70x_{10}$$

$$Z_{3} = 21x_{1} + 35x_{2} + 10x_{3} + 60x_{4} + 83x_{5} + 27x_{6} + 50x_{7} + 12x_{8} + 7x_{9} + 16x_{10}$$

Subject to

$$(0.97)^{x_1}(0.94)^{x_2}(0.99)^{x_3}(0.89)^{x_4}(0.90)^{x_5}(0.94)^{x_6}$$

 $(0.96)^{x_7}(0.98)^{x_8}(0.97)^{x_9}(0.99)^{x_{10}} \ge 0.85$
 $x_1 + x_2 + x_3 = 1$
 $x_4 + x_5 + x_6 + x_7 = 1$
 $x_8 + x_9 + x_{10} = 1$
 $x_2 + x_5 = 1$
 $x_7 - x_{10} = 0$
 $x_1 = (0,1)$

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Maximize
$$\lambda$$

Subject to
 $\lambda + 1.84x_1 + 1.46x_2 + 2.46x_3 + 0.98x_4 + 1.03x_5 + 1.47x_6$
 $1.83x_7 + 0.64x_8 + 0.55x_9 + 1.08x_{10} \leq 4.0$
 $\lambda - 1.067x_1 - 1.9x_2 - 0.64x_3 - 3.17x_4 - 3.56x_5 - 2.03x_6$
 $-1.6x_7 - 0.76x_8 - 0.33x_9 - 0.5x_{10} \leq -4.0$
 $\lambda + 2.13x_1 + 3.8x_2 + 1.26x_3 + 6.34x_4 + 7.13x_5 + 4.06x_6$
 $+ 3.2x_7 + 1.53x_8 + 0.67x_9 + 1.0x_{10} \leq 11.0$
 $\lambda - 0.70x_1 - 1.16x_2 - 0.34x_3 - 2.0x_4 - 2.77x_5 - 0.9x_6$
 $-1.66x_7 - 0.4x_8 - 0.23x_9 - 0.53x_{10} \leq -2.33$
 $\lambda + 2.1x_1 + 3.5x_2 + 1.0x_3 + 6.0x_4 + 8.3x_5 + 2.7x_6 + 5.0x_7$
 $+ 1.2x_8 + 0.7x_9 + 1.6x_{10} \leq 11.0$
 $\lambda - 0.032x_1 - 0.062x_2 - 0.01x_3 - 0.117x_4 - 0.105x_5 - 0.062x_6$
 $- 0.041x_7 - 0.020x_8 - 0.030x_9 - 0.01x_{10} \geq -0.1625$
 $1.0x_2 + 1.0x_5 = 1.0$
 $1.0x_4 + 1.0x_5 + 1.0x_6 + 1.0x_7 = 1.0$
 $1.0x_6 + 1.0x_9 + 1.0x_{10} = 1.0$
 $1.0x_7 - 1.0x_{10} = 0$
 $x_5 = (0,1)$

The solution to the fuzzy linear programming problem is:

λ	=	0.1344				
×1	=	0.0	* 6	*	1.0	
×2	=	1.0	* 7	=	0.0	
×3	-	0.0	*8	-	1.0	
x 4	=	0.0	×9	=	0.0	
×5	=	0.0	* 10	=	0.0	

The solution is in the required 0-1 form, the exchange heuristic or Phase III is not necessary. Therefore the decision is summarized as follows:

 $\lambda = 0.1334$

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List of Selected Projects: {2,6,8}

List of Nonselected Projects: {1,3,4,5,7,9,10}

The rigid constraints were all satisfied. The fuzzy objectives were calculated as follows:

Table V.12. Example 2, Attribute Satisfaction

Attribute	Calculated Value
Weight (lb.)	141
Cost (\$10 ⁴)	\$233
Power (watts)	74

5.6 Analysis and Discussion of Results

The decision problem presented in Section 5.5 was originally solved via a "multirisk" programming model [6]. This analysis concept is based on the determination of the alternative decision solutions which minimize the probabilities that the decision maker's objectives and constraints will not be satisfied. The "best" subset of m decision alternatives from a possible set of n candidates is selected such that the problem's objectives and constraints are satisfied with minimum risk.

The multirisk programming model is designed to solve multiple criteria decision problems, assuming that decision makers strive to achieve or satisfy goals rather than attempting to optimize them. The decision maker may incorporate the concept of "fuzziness" [66] into the analysis by specifying a range of deviation allowable for the goals and constraints of the problem.

The multirisk programming model is a stochastic analysis technique for solving multiple criteria decision problems. Problem formulation may include both rigid and stochastic goals and constraints. The rigid goals and constraints have deterministic coefficients, while the stochastic goals and constraints have stochastic coefficients. The model assumes that the range of deviation is a random variable, while the stochastic parameters of the objectives and constraints are normally distributed independent random variables. The "best" solution to the multirisk programming model is the program which minimizes the risk of not achieving the goals and constraints of the problem, or maximizes the probability that the goals and constraints are achieved.

In the multirisk programming analysis of the project selection example (Section 5.5), uncertainties were incorporated for each coefficient. The attribute data for the proposed candidates is shown in Table V.13.

The multirisk programming model employs an enumerative search to identify the "best" solution. Table V.14 displays the results of the multirisk programming model and the fuzzy linear integer programming/exchange heuristic model. Both fuzzy linear integer programming/exchange heuristic model and the multirisk programming model of multiple criteria decision making provide effective mathematical modeling techniques for the analysis of management decisions which are fuzzy in nature.

The problem formulation of the fuzzy linear programming/exchange heuristic model was presented in Section 5.2. This multiple objective analysis provides the decision maker "leeway" in modeling phenomena of a vague or ill-defined nature. This "leeway" in the model is a result of utilizing fuzzy sets to describe those objective functions and constraints that are imprecisely defined. Through the use of a fuzzy set operator, the "min" operator, an optimal decision in the fuzzy environment is obtained. This optimal decision is defined as the point which maximizes the membership function of the fuzzy set formed through the intersection of those fuzzy sets representing the various objective functions and constraints. The exchange heuristic in the model seeks to obtain the best attainable integer solution given that the optimal point defined above is not integer valued.

Table V.13. Attribute Data for Proposed Candidates

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A DESCRIPTION OF THE OWNER OF THE

		Subsy	stem A		Subs	ystem B		031	Subsyste	C
Attribute	1	2	m	4	2	9	-	ø	6	10
Weight (lb.)	32	57	19	95	107	61	48	23	10	15
Cost (\$10 ⁴)	120	95	160	64	67	96	119	42	36	70
Reliability	0.97	0.94	0.99	0.89	0.90	0.94	0.96	0.98	0.97	0.99
Power (watts)	21	35	10	60	83	27	50	12	7	16

Uncertainties in weights = $\pm 10\%$.

Uncertainties in costs = \pm 15%.

Reliabilities are assumed constant.

Uncertainties in power requirements = $\pm 5\%$.

Table V.14. Comparison of Results

		Multirisk P	cogramming Model
Dystem Attribute	Fuzzy LP/Heuristic Model	Expected Value	Standard Deviation
Weight	141 lbs.	141 lbs.	4.3 lbs.
Cost	\$2,330,000	\$2,330,000	\$106,000
Reliability	0.866	0.866	0.0
Power	74 watts	74 watts	1.1 watts

One practical advantage of modeling with either of these techniques is that the decision situation does not have to be defined in a precise manner. In the fuzzy programming approach, the decision maker specifies ranges of acceptability for those objective functions and constraints represented by fuzzy sets. In the multirisk programming model, the decision maker specifies ranges of deviation. In both models, the decision maker is given greater flexibility than would be available in a classical mathematics approach.

A major advantage of fuzzy linear programming is the ease with which it can be formulated and solved on numerous mathematical programming systems. The exchange heuristic and the multirisk programming techniques both require utilizing a specific computer program which may not be readily available.

The major advantage of the multirisk programming model is its ability to analyze multiple criteria decision problems which are characterized by nondeterministic coefficients for the various objective functions. This model provides the decision maker leeway in defining his aspiration levels, as well as in stating precisely the terms of the objective functions.

The enumerative search technique employed in the multirisk programming model is impractical for large scale problems both in computer storage requirements and necessary CPU time [6]. The fuzzy linear programming model utilizes whatever mathematical programming system that is available to the user to solve mixed integer linear programming problems. The computer storage requirement is, therefore, programming package dependent, as is the CPU time necessitated.
5.7 Computer Program

A computer program implementing the fuzzy linear integer programming and the exchange heuristic phases of the algorithm was developed in FORTRAN IV for the IBM 370/3033 computer system. Standard FORTRAN language was employed to permit relative ease of adaptation of the computer model for use on other computer systems. The amount of internal storage necessitated on the IBM 370/3033 was 280,000 bytes. The amount of storage necessary is due to the requirements of the MPSX system. The computer program is currently dimensioned for the comparison of twenty-five alternatives. This program size could be enlarged by redimensioning the program not to exceed the MPSX variable limit. The exchange heuristic program is capable of solving problems of size one hundred and fifty constraints with one hundred and fifty decision variables with 280,000 bytes of storage. The CPU time to execute Example 1 was 2 seconds, while 3 seconds of CPU time was required for Example 2.

5.8 Computer Code Description

The fuzzy linear integer programming computer code and the exchange heuristic computer code are listed in Appendix B along with the definition of all input data. The computer codes will be described in three sections:

i. Fuzzy Linear Programming Transformation program.

11. IBM MPSX/Mixed Integer Programming Control program.

iii. Exchange Heuristic program.

The fuzzy linear integer programming transformation program is composed of a single main program. This program reads the input data

and transforms the objective functions into their fuzzy transformation as appropriate. Temporary data sets are created to be used as data input for the MPSX/Mixed Integer Programming Optimization Technique or the exchange heuristic program as appropriate.

The MPSX/Mixed Integer Programming Control program is an advanced usage example [63] of the IBM MPSX/MIP technique. This control program optimizes the continuous problem, then solves the mixed integer problem. A more in-depth discussion of the MPSX mathematical programming system is presented in Appendix A.

The exchange heuristic code consists of a main program and seven subroutines. The code is a modified version of Petersen's [42] heuristic algorithm, with subsequent modifications by Bouillot and Smith [64, 65]. The description of this code is as follows:

<u>Main Program</u>. The main program reads the input data from the temporary data set created in the fuzzy linear programming transformation program. This program calculates the R_j values and the ratio T_j/R_j for each variable. It maintains the list of selected and nonselected variables and determines those exchanges to be executed. It calls the various subroutines in the proper sequence required to conduct the exchange operations. It formats and writes all output data as required.

<u>Subroutine Rank</u>. This subroutine initially ranks the variables in both the sets of selected and nonselected variables. <u>Subroutine Impvmt</u>. This subroutine maintains the best solution achieved that is both advantageous and feasible.

<u>Subroutine Feasbl</u>. This subroutine examines the feasibility of the exchange under consideration. <u>Subroutine Exchge</u>. This subroutine executes the exchange operations.

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<u>Subroutine Achvmt</u>. This subroutine calculates the gain in the membership function as a result of an exchange. <u>Subroutine OBJ</u>. This subroutine evaluates the various fuzzy objective functions to determine the lambda value. <u>Subroutine FTOBJ</u>. This subroutine calculates the fitback solution.

CHAPTER 6

SUMMARY, CONCLUSIONS, AND SUGGESTIONS FOR FURTHER RESEARCH

In this chapter, the work presented in this thesis is summarized, and a few conclusions are drawn about the fuzzy capital budgeting model and the general applicability of fuzzy programming.

6.1 Summary and Conclusions

The model of the capital budgeting problem explored in this work is a combined application of the models developed by Zimmermann [11] and Petersen [42]. The fuzzy linear integer programming approach to management decisions is designed to study decision problems involving multiple goals and constraints, some of which are of a vague or illdefined nature. The method is founded on the theory of fuzzy sets. Fuzzy sets are utilized to model phenomena of an ill-defined nature which cannot be described adequately in classical mathematical terms. The analysis seeks to permit the human mind to utilize its capabilities to the fullest extent, while utilizing the computational efficiency of the computer to perform those operations which the human mind cannot adequately accomplish. This analysis allows the individual decision maker to make small judgmental decisions (what the human mind does best), while allowing the computer to solve large linear programming problems incorporating these judgmental decisions. Since the solution to the fuzzy linear integer programming problem may not be in the form (0,1), a modified form of Petersen's exchange heuristic for the capital

budgeting problem was employed. This exchange heuristic seeks the "best" attainable solution, given that no integer solution exists.

The model is designed to solve the general problem in which the "best" subset of m alternatives is selected from a candidate set of n possible decision alternatives, such that the membership function of the fuzzy set of the decision is maximized. The model provides a great deal of flexibility to the user in formulating problems for analysis. The availability of solution algorithms and computer solution systems which are readily compatible with the fuzzy linear integer programming problem formulation allows the user to realize a computational solution with ease.

This analysis has applicability for a broad range of decision problems involving the selection of entities from among numerous alternative possibilities, such as equipment purchases, route selection, or investment selection. The example presented in Chapter 5 successfully analyzed the selection of alternative subsystems in achieving system design requirements, while satisfying stated cost restrictions.

6.2 Suggestions for Further Research

The work described in this thesis can be extended in several different directions. The integer solution technique utilized in this work was the MPSX/Mixed Integer Programming System. Although this mathematical programming system readily yields a solution to the problem, the availability of MPSX is not universal. The development and use of an integer programming computer code in standard FORTRAN would greatly enhance the ease with which the model could be adapted to other computers.

The popularity of multiple objective analysis via goal programming could be the catalyst of another extension. The formulation of the fuzzy objectives and constraints into a goal programming analysis would be an extremely interesting development. Goal programming is an extremely robust optimization technique, which is viewed as a practical and natural representation of a wide variety of real-world problems. In combining the fuzzy programming approach of optimizing humanistic systems which are by nature vague and ill-defined, with the practicality of goal programming, an optimization methodology may result which presents a realistic perspective of management decision making.

Field experimentation with fuzzy programming models of management decision making would be desirable. Zimmermann [58] has conducted numerous experiments to analyze the viability of modeling decision makers via the concepts inherent in fuzzy programming. Applications of fuzzy programming include personnel management and determination of credit worthiness in the banking industry [58], media selection [11], and the sizing of a truck fleet [9].

The fuzzy set operator used in the fuzzy linear integer programming model is the "min" operator. Zimmermann and Hamacher [58] have experimented on the applicability of other operators in the optimization of management decisions. These operators include the product operator, the algebraic sum operator, the max operator, both the arithmetic and geometric mean operators, and the gamma operator.

Certainly, many other areas for further research exist. However, these few are listed to provide the reader some idea as to where additional research might begin.

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As in most integer programming techniques, long computational time is necessary to determine the optimal integer solution.

The IBM program descriptions [63] provide an in-depth discussion of the MPSX system. In addition, numerous sample problems are presented. The examples are detailed from data input through sample outputs. The Mixed Integer Programming program description is especially instructive. It provides sample MPSX control programs and presents an excellent discussion of the mixed integer programming procedure.

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APPENDIX A

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A BRIEF LOOK AT MPSX

In this appendix, the IBM Mathematical Programming System Extended (MPSX), linear programming and mixed integer programming capabilities are summarized.

A.1 <u>MPSX System</u>

Mathematical Programming System Extended (MPSX) is composed of a set of procedures all operating under the direction of a user specified MPSX control program. Through the MPSX control program, the user specifies the sequence of steps to be executed in solving a mathermatical programming problem.

The user is able to augment MPSX with procedures written in the FORTRAN language through the use of the Read Communications Format (READCOMM) feature of MPSX. Through the use of FORTRAN CALL statements, the READCOMM subroutine is accessed. This subroutine acts as an interface between the MPSX control program and the FORTRAN procedures.

The user is capable of executing all of the MPSX capabilities through the use of the MPSX control programs and the READCOMM procedures.

A.2 Linear Programming Procedure

The MPSX strategy for solving a linear programming problem is the ordered execution of a series of the MPSX procedures. The user specifies the solution strategy to MPSX, via the MPSX control language.

The linear programming procedures of MPSX use the bounded variable/product form of the inverse/revised simplex. The simplex method is based upon the fact that if there are m constraints which are linearly independent, then there is a set of m columns (variables) which are also linearly independent. The right-hand side values can be expressed in terms of the m columns called a basis. The simplex

method employs these basic solutions by exchanging one column from the basis with one column not in the basis on each iteration, until a solution is realized that satisfies the feasibility criteria. This solution is termed a basic feasible solution.

The simplex method proceeds by examining the basic feasible solutions, to find one that satisfies the requirement that the objective function value be maximized or minimized.

A.3 <u>Mixed Integer Programming Procedure</u>

The Mixed Integer Programming capability of MPSX is an extension of the linear programming procedure of MPSX. It provides the user the capability to solve linear programming problems composed of both integer and continuous variables. This analysis is appropriate for the fuzzy linear programming approach to the capital budgeting problem. Since the solution must be of the form (0,1), the variables representing the investment possibilities must be integer values, while the value of the membership function is a continuous variable.

The MPSX mixed integer linear programming problem is performed in two stages. First, the problem is solved considering all integer variables as being continuous. The problem is solved by the linear programming capability of MPSX. The solution to this problem is termed the optimal continuous solution.

The second stage is to solve the problem for the optimal integer solution. The search for an integer solution starts from the optimal continuous solution and proceeds using the branch and bound technique. The search continues until the optimal integer solution is determined.

APPENDIX B

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Fuzzy Linear Integer Programming Via MPSX/MIP Computer Code, Variable Definition Guide, User's Guide, and Sample Output

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********************************** ************************* PROGRAMMING", THE JOHNAL OF THE OPELATIONAL RESEARCH 3) ZIMMERMANN, H.J., "MEDIA SFLECTION AND FUZZY LINEAR ADDITIONAL INFORMATION CONCERNING FUZZY PROGRAMMING ZINMERMANK, H.J., "DESCRIPTION AND OPTIMIZATION OF OPJECTIVE FUNCTIONS", INTERNATIONAL JOURNAL OF FUZZY 2) ZIAMFRMANN, H.J., "PUZZY PROGRAMMING UITH SEVERAL FUZZY SYSTEMS", INTEFNATIONAL JCHRNAL OF GENERAL MAY BE CHTAINED IN THE ICLICUING REFERENCES SOLUTION TECHNICHE FOE THE MULTIOBJECTIVE FUZZY INTEGFF (0-1) LINEAL PROGRAMMING CAPITAL BUDGETING PROBLEM VIA MPSX/MIP SFTS AND SYSTEMS", VOL. 1, 1978, PP. 45-55. PREPARED BY CPT. MICHAEL G. HEADLY SYSTEMS, VCL. 2, 1976, PP. 209-215. 1) * ** * * * 执 * # * ***** × * × # * * ** * 뵻 * ** *

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DATA INPUT FORMAT ******** PIGID CONCERDATION SET : KTYPE3+1 9F.8.4 9 F 8. 4 9 F 8.4 ((X1(J,I),T=1,NVAR),J=1,KTYPE1) (PHS1(I),J=1,KTYPE1) ((X2(J,I),I=1,NVAP),J=1,KTYPP2) (RH52(I),I=1,KTYPE2) ((X 3 (J, I), I = I, NVAF), J = I, KT YPE 3) RIGIE CONSTRAINT TYPE # 1 NUMBER OF CARES IN STT : KTYPE2+1 -EIGID CCNSTRAINT TYPE # 2 EIGID CONSTEAINT TYPE # NUMBER CF CARES IN SET: CARD SFT # 3 CARD SET # 2 CARD SET # 1 USER'S GUIDE ******** KTYPE2 ITYPE3 KTYPE1 KTYPE3 LTYPE ITYPF2 NV A F CARD SET ****** ¥ # ¥ * * ** ¥ ¥ ** * * ** * * * * * * * ₩ ₩ * ** ¥ ¥ * * * * * ** ¥ * * * * ** * * ** * ** * ¥ ¥

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DIMERSION X1 (25,25), X2 (25,25), X3 (25,25), X4 (25,25), X5 (25,25), X6 (25,25), RHS (25), ROW (25,25), RHS (25), RHS 1 (25), RHS 1 (25), RHS 2 (25), TINT2 (25), RHS 2 (25), KEAD 1, NVAR, KTYPE1, KTYPE2, KTYPE3, ITYPE1, ITYPE2, ITYPE3 **************** * ******************** CATA SET THAT IS USED AS INPUT SET 45 IS THE TERPORAFY RIGIE CONSTRAINT TYPE 1 (<). NKES=hFUZ2Y+KTYPE1+KTYPE2+KTYPE3 FOR THE MESX/MIE FCUTINE. $\widehat{\diamond}$ HFUZZY=ITYPE1+ITYEE2+JJYPE3 *2 ASP 3 (25), STI N7 (25), UTI NT (25) PIGID CONSTRAINT TYPE 2 EEAD 2, (RHS 1 (I), I = 1, KTYPE 1) [TAP 2, (X1 (IC,I), I=1, NVAH) IF (FT YPE1.EQ. 0) GC TC 30 DO 50 IC= 1, KTYPF1 DO 100 T=1, KTYPE1 $(\Gamma, T) = X = (\Gamma, N) = OOI$ DO 200 J=1,NVAR ENS (M) = PHS1 (I) DATA CONTINUE CONTINUE - + W = X 0 *⊭* ℓ *** *** *** *** *** * * * ** ¥ * ** * * * * * * 50 200 100 30

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6.2AD 2, (RHS3(I), I=1, KTYFF3)
DO 500 I= 1, KTYFE3
                          IF (KTYPE2.EQ.0) GO TO 31
DC 51 JA=1,KTYPE2
b PAD 2, (X2(IA,I),I=1,KTYPE2)
kEAD 2, (RHS2(I),I=1,KTYPE2)
                                                                                                                                                                                                                                                                                   IF (KTYPE3, EQ. 0) 60 TO 32
                                                                                                                                                                                                                                                                                                  PO 52 IB=1,KTYPF3
                                                                                     DO 300 I=1,KTYPE2
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RHS (N) = RHS 3 (I)
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FEAD 2, (X4 (ID,I), T=1, NVAR)
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D0 900 I=1, ITYPE2
                                                                                                                                                           EHS (B) = (T INT I(I) - ASP I(I)) / TINTI(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                h(15 (H) = (1 I NT 2 (T) + ASF2 (T)) / TIN T2 (T)
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                 IT (I'1 YPE1.EQ.0) GC TC 33
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ATY PE 1+KTY PE2+K "Y PE3
                                                                                                                                                                                                                                                                                                                                      00 53 IF= 1, ITYPE2
                                  DC 60 ID= 1, 12YPF1
                                                                                      DO 700 I=1,ITYPE1
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READ 2, (X6(IG,I),I=1,NVAE)
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HIS (M) = {UTINT (I) + ASF3 (I) ) / JTINT (I)

IF (J. EQ. NVAR) GO TO 12CO
                                                                                                                                    (1) LN 115/(r, 1) 9X-= (r, 4) 404
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IF (13 YPE3.EQ. 0) GC TC 35
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        FORMAT (2X, 'N', IY, 'OBJ')
                                                                DO 1100 I=1, ITYPE3
               DO 54 IG=1, ITYPE3
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WRITE(45,11) M FORMAT(2X,'L',1X,I6,T5,'RCU') M=M-100000 FORMAT (2X, 'G', 1X, 16, T5, 'KOW') M= M- 100000 M=K TYPE 1+ KTYPE2+ KTYPE3 + L TYPE1 PORMAT (2X, 'E', 1X, I6, T5, 'ROU') LF (KTYPE1. FQ. 0) GO TO 36 LF (KTYPE3.EQ.0) GC TC 38 IF (ITYPE1.EQ.0) GO TO 39 IF (KIYPE2.EQ.0) GC TO 37 A=KTYPI 1+KTYPE2+KTYPE3 00 2000 I=1,KTYPE1 DO 3000 I= 1, KTYPE2 DO 4030 J=1, KTYPE3 DO 5000 I=1, TTYPE1 M=KTYPE1+KTYPE2 W (EL, 24) STIN WI TTE (45,12) M Σ WRITE (45, 11) M=M-100000 4=1-100000 M=1+100000 A= A+100000 M=M+100000 d=M+100000 CONT INUE CCUST NU E CONTINUE CONTINUE M=KTYPF1 1 + N=V - + E H S 1=1 5000

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FORMAT(4X,'LAMBDA',4X,I6,T15,'RCW',7X,'1.0')
                                                                                                                                                                                                                                                                                     WRITE (45, 15)
FORMAT (4X,'1.AMBNA',4X,'CBJ',9X,'1.0')
                                                                                                      M=KTYPE1+KTYPE2+KTYPE3+1TYPE1+JTYPE2
GO TO 40
                                                                                                                                                                                                                                                                                                                        L=ITYPE1+ITYFE2+ITYFE3+2
                                                                                                                     IF (TTYPE3.EQ.0) GG TC 41
                                                                                                                                                                                                                                                                                                                                       M=K3YPE1+KTYPE2+KTYPE3
                                                                                                                                                                                                                                              IF (M.NE.K) GO TO 42
            D3 6000 1=1, ITYPR2
                                                                                                                                                                                                                                                                            FORMAT (CCLUMNS')
IF (ITYFE2.FQ.0)
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FORMAT (4Y, 'INTEND', 4X, '' MAPKEF''', '' 7X, '' INTEND'''
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 COM "AT (1X, "UP", 1Y, "UPBCUME", 3X, I4, T15, 'X', 10X, '1.0')
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D0 9075 J=1, NVAR
                                                                                                                                                                                                                                                                                                                                                             L=KTYPE 1+KTYFE2+KTYPF3+ITYPE1+ITYPE2+ITYPF3+2
                                                                                                                                                                              FORMAT (4X, I4, T5, 'X', 9X, I6, T15, POR, 7X, F8.4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                             FOR MAT (4X, 'RES', 7%, T6, T15,' EOW', 7X, F8.4)
                                                                                                                                                           N, K, RCH (B, J)
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PO 8050 J=1, NVAR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          FORMAT ( BOUNES')
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  7
                  PO 5000 T=1,1
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LAITE (45,20) FORMAT (* FNDATA*) FORMAT (715) FOPEAT (9F8.4) STOP 9075 CONTINUE

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- END

2771 ECUVEDE 18600 BYTFS, TOTAL AREA AVAILABLE= 178176 0, NUMBER OF EXTENSIONS= 0, NUMBER OF WARNINGS≈ 15048 BYTES, AFAAY AREA= NUMBER CF ERRCRS= OBJECT CODE=

0.08 SEC, 0.22 SPC, EXECUTION TIME= н.

NOD LEVEL 7 MPSX RELEASE 1 .. MPSX-VIM7.. CONTROL PROGRAM COMPILET.

Program	INITIALS	MOVE (XDATA, "MAX")	MOVE (X PBNAME, "EUDGET")	CONVERT	SFTUP ("BOUND", "UPBOUND", "MAX")	MOVE (XOBJ, 'CBJ')	MOVE (XRIIS, "RHS")	OPTIMIZE	SOLUT TON	SAVE ('NAME', 'CPTC')	XIWINI	MIXSTART ("CCS1")	$X M X CROP = 0 \bullet 0$	CT=0	WVADR(XDOPRINI, INT)	MIXFLOW	STOP MIXSAVE("NAME", TREET")	MIXSTATS (NODES)	FXIT	IND SCLUTION	XMX FROP=0.0	CT=C1+1	IF (CT. EQ. 5, STC?)	CONTINUT	CT DC(0)	PEND
0001	0002	0096	1007	0098	6600	0100	0161	0162	0411	0412	0413	0451	0452	0453	0454	0455	0.456	0457	0458	0459	0460	0461	0462	0463	0464	0465

33.33 92 LP ELEMENTS, DERSITY = THESE STATISTICS CONTAIN CAF SLACK VARIABLE FOR EACH ROW ~ MCD LEVEL **10 INTEGER VARJABLES** EXECUTOR. MPSX RELEASE 1 0 MAJOR ERROR(S). 0 MAJOR ERROR (S) . 0 MAJOR ERECR(S) . 0 MAJOR ERRCR(S). 23 VARIABLES. TO BUDGET ۲ t ł 1 O MINOK FRPOR(S) O MINON ERROR (S) 0 MINCR ERROR (S) O MINCR EFROR (S) PROBLEM STATISTICS 2- COLUMNS SECTION. 5- BOUNDS SECTION. 3- RUS'S SECTION. 1- FOUS SECTION. 12 LP ROWS, .. NPSX-VIN7.. 0.00 CONVERT MAX **G NHORE II** TIME = RHS

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L. L. L. L.

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O PAJOE ERFCRS.

O MINOR SPROPS,
FIXED BOUNDED Ξ C **PCD LEVFL 7** s o 5 MAXIMUM PRICING NOT REQUIRED - MAXIMUM ROSSIELS C . FRFF. FELEASE 1 1563 120 1080 1800 72 CCNE 6912 NORMAL **د** د XSdia 120 600 2304 1212 SCRATCH1 ASSIGNED TO SCRATCR1 SCRATCH2 ASSIGNED TO SCRATCH2 ASSIGNED TO MATAIX1 ASSIGNED TO MAFAIX2 ASSIGNED TO NIXWORK TOT AL 12 ASSTGNED TO ETAT EXECUTOR . NUADEN = 0 PBOU ND 5 m m FOUS (LOG-VAP.) COLUENS (STR.VAP.) F EGIONS BUFFERS INTEGER TABLES P. PFG-BITS 4AP BIFFERS VECTOR .. MPSX-V 147.. 00.0 SPTUP BUDGFT NO CYCLING P001.5 BOUND SCALF MATRIX1 MATRIX2 MI XHORK HAX MATEIX BOUND TIME =UOFK FT A 1 ETA

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10 COLUMNS AKE INTEGER

3 MATRIX RECORDS (WITHOUT RHS'S) 33.33 -11 92 RLEMENTS - DENSITY

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0.00 TIME = OPTIMIZE SYSTEA MACRO CALLED

AFTER PASS A AT START TIME 0.00 MINS. INPFASIBILITIES A αα CFASH

.... 12 FLEMENTS FLEMENTS EL EN ENTS S1knC10RALS0 FT A-VFCTORS1 FTA-VECTOES1 CURRENT INVERSE ----LOCICALS12 TRANSFORMED0 INVERT CALLED TIME 0.00 PASIS ---- NC.(F KOWS12 INVERSE -- MUCLEUS0

0 AFTEF PASS B FFAS IBLE

NEGPT

0.00 MT NS. TIME = PHS = RHS ~ PRICING OBJ = OBJ0.00 NINS. SCALE = JUIL DRTAAL

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10 MINOR TITEATIONS - CLOCK CONTROL FUNCTION VALUE .13340 .13340 1.00000--33182-REDUCED C031 INVERT DEMANDED AFTER 10 MAJOR/ VECTOR VECTOR 13 NT 001 16 Ξ MERICAN INC. NONOPT TILE PUISER 10 []

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....42 *****36 ELEMENTS ELFMENTS EI. EN ENTS ETA-VECIORS6 ET A-V ECTORS STRUCTURALS CURRENT INVERSE ----LoGICALS7 TRANSFORMFD0 0.00 BASIS ---- NO. OF ROWS 12 INVERSE -- NUCLEUS0 ari. INVERT CALLED

N FG D.I

MI NG. 0.00 = WIT MHS = RHSOBJ = OBJINFTPG

PRICING 0.00 MI US. 1.00000-11 SCALE = SMLL

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- CLCCK CONTRCL 5 ALNCE ITERATIONS FUNCTION VALME 5 hó 05 • .50945 .50945 .58071 .56671 -#1704. 2.50491-.54614-.46110-.61259 REDUCED CUST S MAJOR/ V FCI OF 21008712 2100872 VECTOR 3 2 2 007 20 2 9 TNV PPT DETANDED AFTER MUABER THONON AUMPER TER 13 <u>.</u> 15 16 **T** 2222

PTA-VFCTURS14 STRUCTURALS LUGICALS4 TPANSFORMED2 BASIS ---- NO.GF EONS 12 INVERSE -- NUCLEUS6

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FIA-VECTORS 11

CURRENT INVERSE ----

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⊩ L ∃SVITIN XS	PUTCING 7 SX RELEASE 1 3		N NUMBER = 16	T] VI TY	.58071 F 1 MCB LEVEL 7		SLACK ACTIVITY	-58071-	• •	• • •	• •	• 53436 18000		1.67735
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SFCTION 2 - COLUMNS

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NU MB E R	13	14	15	16	17	13	19	20	21	22	23

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0002+76- .5807 FORCED	FUNCTICN VALUE -58071 -56528 -37256	5807 FORCED	.58071 .50633		.55058 .53262	.3190 .5506 Forced	<u>55058</u> 54413
FYOND .1000 FYOND . AL = .3281	REDUCED COST 21563 13532- 13981 09256	AL = .3281	.01927- .63390	ia I =	.24577	VAL = VAL = Seq67	.05501- 2.22737
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T I ES			el em ents elements elements		
.31897 ACTIVI		.28406 ACTIVI	21		
FSTJMATION = TOWARLS UPPER	.65909 .82333 .82233	ESTIMATION = TOWARDS LOWER	EJ A-V FCTORS STF UC JURA LS ETA-VECTORS		РАКАЙ V Alii E . 16740 . 25701
. 3190 FCRCED	.31897 .31699 .31699		Etse		FUNCTION VAIUE • 28406 • 26758
NAL = .6591	.00265- .09723 .03283-	NAL = .8326	CURRENT INV LOGICALS •• TRANSFCFMED		k EFUCE D COST . 03788 .40580
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E NODE Bi. Avcii -	0	NODE
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...MPSY-VIM7.. EXECUTOR. MPSX RELEASE 1 MCD LEVEL 7

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... APSX-VIM 7.. EXECUTOR. MPSX RELEASE 1 MCD LEVEL 7

SFC FT CN 2 - COL MANS

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16	X 003	ΓV	•	•	' •	1.0000
17	t00X	LV	•	•	, •	1-00000
18	X 005	ΙV	•	•	' 4	1_00000
61	X006	١V	1.00000	•	, •	1.00000
20	X D O J	LΥ	•	•	•	1-00000
2	X003	١٧	1.00000	•	•	1 - 00000
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23	6103	lγ	•	•		1_00000

-- YPSY-VAR7. EXECUTOR. APSY GELFASE 1 MCD LFVEL 7

MIXFLOW - TIME = 0.00

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EGER NOTES		·			NPT CPU (SEC): SEC SYSTEM TIME: CARDS PUNCHED:
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APPENDIX C

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Fuzzy Linear Integer Programming Via an Exchange Heuristic, Variable Definition Guide, User's Guide and Sample Output

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EEE 1305....NF129486.....IIEACLY 1305....NP129486....HEADLY 1305.... NF129436.... HFADLY JOB **JOB** HOF HASP-JI***....START HASP-II***....START • : ; Σ 5 HEADLY HEADLY HEADLY

AA 00000050 0010000 00000150 00000200 00000250 0 K 0 K 0K **EK LCS** CMIN 00.365FC MAIN 280K LCS v UMIN 01.345FC MAIN 280K LCS С ت ا £ OMIN 00.04SEC MAIN ы //DATA.FT80F001 DD UNIT=SYSDA, DSN=66EXDA1A, SPACE=(3200, (50,5)), ۲ ŝ OHIN 01.745EC //DATA.FT80F001 DD UNIT=SYSDA,DSN=&&EXDATA,DISF=(OLD,DELETF) ε 7 ', HEADLY S // DISP= [NF4, PASS], COB= (RECEM=FE, LRFCL=80, BLK SIZF=3200) م S ×, 80077.1512 CFU 80077.1512 CPU CCND CCDE 0000 80077.1512 CPU COND CODP 0000 COND CODE COOD 30077.1512 CPU **HP129486 JOB 104771, T=0025, k=02500, S=280, 90077.1512 80077.1512 90077.1512 80077.1512 // EXEC SETTAF, TEALN=FN, FORMS= 16 03/17/80 EARCUTED -/ START - STEP WAS EXECUTED -EXECUTED -JOB /NP129486/ START / START **SFART** SLOP STOP JOB /NF129485/ STOP / STOP ***INCLUDE MGHO 1. STHERE ***INCLUDE MGHO1.\$UNE ***INCLUDE AGHO1.\$TWO STEP /SETTAF STEP /SETTAF DAT L: - STEP WAS - STEP WAS STEP /DATA STEP /DATA STEP /DATA STEP /DATA //DATA.INPUT DD * TIME: 15:12:48 FUCG FUCG ***FULLSKIPS + QU NISAS// * 00 V EXEC IFP142I / EXEC [EF1421 VISYSIN LEF 3731 FF 3741 IEF 373I IFF374I FP1421 [FP3731 LFF 374I TETTTE IEF 376 I

******************************** 3) ZIMMERMANN, H.J., "MEDIA SELECTION AND FUZZY LINEAR PRCGRAMMING", THE JOHPHAL OF THE OPERATIONAL RESEARCH ADCITIONAL INFORMATION CONCERNING FUZY PROGRAMMING 1) ZIKMERMANN, H.J., "DESCRIPTION AND OPTIMIZATION OF **GBJECTIVE FUNCTIONS", INTERNATIONAL JOURNAL OF FUZZY** ZI KMEFKANA, H.J., "FUZZY FROGRAMMING WITH SEVERAL CAPITAL BUDGETING PROBLEM VIA A MODIFIED VERSION OF C.C. PETERSEN'S EXCHANGE BEURISTIC ALGORITHM. FUZZY SYSTERS", INTERNATIONAL JOURNAL OF GENERAL MAY BE OBTAINED IN THE FOLLOWING REFERENCES SOLUTION TECHNIQUE FOR THE MULTIOBJFCTIVE PUZZY INTFGEF (0-1) LINEAR PROGRAMMING SFTS AND SYSTEMS", VOL. 1, 1978, PP. 45-55. PREPARED BY CPT. MICHAEL G. HEAPLY SYSTEMS, VOL. 2, 1976, PP. 209-215. 2) * ** * × * ¥ ¥ ¥ * * * * ** * * 4 ¥ * -* × ¥ * ¥ * * * 00000 000 00 2 : 1 C \mathbf{O} 0000 C <u>د</u> : 3 \circ \mathbf{C} \mathbf{U} 2 2

* * * * * * * * ** ¥ * * * * * * # * ALGCRITHE USING EXCHANGE CEERATIONS", ATTE TRANSACTIONS ** × *********************** * * * ****************** **BE OBTAINED** APPLITIONAL INFOFMATION CONCERNING PETERSEN'S PETERSEN, C.C., "A CAPITAL EUDGETING FEURISTIC KTYPF1: NUMBFE OF HIGID CONSTRAINTS TYPF1(<) SOCIETY", VOL. 29, NO. 11, 1978, PP. 10 21- 1084. HAY VOI. 6, NC.2, JUNE 1974, PP. 143-150. EXCHANGE HEUFISTIC ALGORITHM IN THE FOLLCUING REFERENCE NVAR: NUMBER OF VARIABLES VARIABLE DEFINITION GUIDE ************ ****** INPUT VAFIABLES * # * * * * # ¥ ¥ 水水 * # * ** ** * * ** * * * * ** * ***** ¥¥ * * * # # 00 $\circ \circ$ $\dot{\mathbf{c}}$ <u>ن</u> 5 \mathbf{c} C <u>ت</u> <u>ن</u> 000000000 \mathfrak{O} \mathfrak{C} <u>ບ</u> ບ $c_{\mathcal{O}}$:J $\circ \circ$ 1 1 \mathbf{O} \circ Ċ 2 0 C

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RHS2(T): FIGHT HAND SIDE OF THE ITH TYPE2 CONSTRAINT. RHS1(I): FIGHT HAND SIDE CF THE ITH TYPF1 CONSTRAINT. RHS3(I): RIGHT HAND SIDE OF THE ITH TYPE3 CONSTRAINT. ASP1(I): ASPIRATION LEVEL ITH TYPE1 FUZY OBJECTIVE ASP2(I): ASPIEATION LEVEL 1TH TYPE2 FUZZY OBJECTIVE ITYPF2: NUMBER OF TYPE2 FUZ7Y OBJECTIVE FUNCTIONS. ITYPE1: NUMBEE OF TYPE1 FUZZY OBJECTIVE FUNCTIONS. ITYPES: NUMBLE OF TYPES FUZZY OBJECTIVE FUNCTIONS. X2(I,J): COFFFICIENT OF THE JTH VARIABLE IN THE JTH TYPE2 RIGID CONSTRAINT. X1(1,J): COFFFICIENT OF THE JTH VARIABLE IN THE X3(1,J): COEFFICIENT OF THE JTH VARIABLE IN THE THE X5(1,J): COEFFICIFNT OF THE JTH VARIABLE IN THE NI MTYPE2: NUMERE CF HIGID CONSTRAINTS TYPE2 (>) KTYPE3: NUMBER OF RIGID CONSTRAINTS TYPE3(=) X4 (I,J): CCEFFICIENT OF THE JTH VARIABLE ITH TYPE2 FUZZY CEJECTIVE FUNCTION. IT'N TYPE1 FUZZY OBJECTIVE FUNCTION. ITH TYPE1 RIGID CONSTRAINT. ITH TYPF3 RIGIC CONSTRAINT. ** * * * * * ** * * * ** * * * ¥ ** * * * ¥ * * * * ¥ * * * ** * * * * * \mathcal{O} \mathbf{c} c_{0} 00 \circ ر: \mathbf{C} \odot \mathbf{O} ۰, C **U** \mathbf{O} 5 C C Q \mathbf{O} \circ \mathbf{O} \mathbf{C} 12 ບ \mathbf{c} 2 12 () \odot

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SFT** SF1 OF SELECTED PROJECTS WHICH GAVE THE LAST ** JN THE NSEPPO), STOKE THE VAPIABLES PROM THE IMPDSO (K) : (K=1, NNS PRO) , STOFE THE VAPIABLES FROM THE ISELTD (K): STCKE ALL VARIABLES BELONGONG TO THE SET LACT ADVANTAGECUS AND FEASIBLE EXCHANGE. L=2, CONTAINS THE VALUE OF THE INCREASE THE MEMBERSHIP FUNCTION OF THE EXCHANGE OF NON-SELECTED PROJECTS WHICH GAVE THE THE GNOBFU(L): I=1, CONTAINS THE VALUE OF THE INCARASE IN THE MUMBERSHIP FUNCTION OF THE MOST AMTAVAL (1) : AMOUNT AVAILABLE IN CONSTRAINT I FOR FOR THE AMTRES(I): TOTAL AMOUNT AVAILABLE IN CONSTRAINT FOR THE ADVANTAGEOUS AND FEASIELE FYCHANGE. ADVANTAGEOUS AND FEASIBLE FXCHANGE. VALUF OF THF MEMBERSHIP FUNCTION WITH AMTNED (I): AMCUNT NEEDED IN CCNSTRAINT I EATIO (J) : RATIO OF OBJCCF (J) / RVALUE (J) OF SFLECIED PPOJECTS. (K=1.NVARSE) UNDER CONSIDERATION. EXCHANGE UNDER CONSIDERATION. EXCHANGE UNDEF CONSIDERATION. SCIUTICN. (K=1, JTH VARIABLE. FITBACK FTOBEU: ¥ ¥ # * ** ** ×× ₩ * ** * * * * * * * * * ** ** * * * * * ¥ * * ** * * * * * * • : ·) : J • 500 C :) \odot 2 C \mathbf{C} 13 5.3 5 \mathbf{C} () 1 : 1.2 13 5 5 \circ \odot C L 0 ر ا $\dot{\mathbf{O}}$

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************************ * * ÷ CF NON-SELECTED STLFCTFD PROJECTS WHICH GAVE THE LAST ADVANTAGECUS AND NUMBEF OF VARIAPLES FECM THE SET OF SELECTED NVAFTU: NUMBEE OF VARIABLES IN THE FITBACK SOLUTION. ARE PART OF THE SELECTED =1, PROGRAM IS REFEATING THE FIRST SEARCH. SLCFFT(I): STCRE THP SLACK VALUE FCF CONSTRAINT I СF **-**NNSPRC: NUMBEF OF VARIALLES FACM THE SET OF NON-LISTDR(J): STORE THE VAPIABLES RANKED IN CRDER DECREASING VALUE OF RATIC(J). SLACK(T): STOFE THF SLACK VALUE FOP CONSTRAINT PROJECTS WHICH GAVE THE LAST ADVANTAGEOUS AND OFJTUN: THE VALUE OF THE MEMBERSHIP FUNCTION. SEAPCH FOR THE FITBACK SOLUTICN. =0, FIRST TIME PROGRAM IS EXECUTING AVARSE: NUMMER OF VARIABLES IN THE SET OF SIT LFITBS (X): STCEE ALL VAMIABLES THAT THE 2 NVARNS: NUMBET OF VANIABLES THE FIRST SEARCH. FEASIBLE EXCHANGE. FEASIBLE EXCHANGE. FITEACK SOLUTION. DUKING THF PPCJFC1S. PROJECTS. IST'ART: NSE FRO: * ž * 17 18 ** ** * * ¥ * ž ** * * * * * 븄 4 ¥ ¥ * * * ×× * ¥

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DATA INPUT FCRMAT ******* 978.4 9F8.4 978.4 9F.R. 4 ((X1 (J, I), I=1, NVAR), J=1, KTYPE1) (RHS1(I), I=1, KTYPE1) ((X3 (J, I), I=1, WAR), J=1, KTYPE3) ((X2 (J,I),I=1, NVAR),J=1,KTYPE2) : KTYFE1+1 NUMBER OF CARES IN SET : KTYPE2+1 NUNDER OF CARES IN SET : KTYPE3+1 KIGIC CONSTRAINT TYPE # 2 -RIGIL CONSTRAINT TYPE # 3 (RUS2(1), I=1,KTYPE2) RIGID CONSTRAINT TYPE # NUMBER OF CARES IN SET: NUMBER OF CARLS IN SET CARE SFT # 3 **USEK'S GUIDE** CARE SET # 1 CARE SET # 2 CARD SET # 4 ***** KT YPF1 **KTYPE2** KTYPE3 ITYPEI **TTYPE3 LTYPE2** NVAR CARD SET ****** * * * ¥ * * ** * * * * × * × * ** * ¥ ** * * * * * * * * * ** * * ¥ * * * ** * $\circ \circ$ υv 000 C C C ს 0 J C <u>ບ</u> ບບ Ċ 5 C C C υ Ċ Q 5 C U U <u>ບ</u> C C υ U 0 \mathbf{O} 20

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********************** ((X6 (J,I),I=1, NVAR),J=1,ITYPE3) (ASP3(I),STINT(I),UTINT(I),I=1,ITYPE3) 9F8.4 9F8.4 978.4 FHZ7Y CONSTRAINT TYPE # 2 [(X5 (J,I),I=1,NVAk),J=1,ITYPE2) [ASP2(I),JINT2(I),I=1,ITYPE2) ((X4 (J,I),I=1, NVAR), J=1, TTYPE1) : ITYPE1+1 : ITYFE3+1 : ITYPE2+1 (ASP 1(I), TINT 1(I), I=1, I TYPE 1) -FUZZY CONSTEAINT TYPE # 3 (RHS3 (I), I=1, KTY PE3) NUMBER OF CARES IN SET : FUZZY CONSTRAINT TYPE # NUMBER OF CARDS IN SET NUMBER OF CARLS IN SET S CAPD SET # 6 CARD SET # 7 CAR D S HT # * * * ¥ # * * * * * * * * * # # * * ** ¥ 4 4 * Ċ \mathbf{O} $_{\rm O}$ $_{\rm O}$ 00000000000000 \odot Ċ 0 0 0 0 0

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DIMFNSION X1(25,25),X2(25,25),X3(25,25),X4(25,25), 1X5(25,25),X6(25,25),HHS(25),ROW(25,25),RHS1(25),RHS2(25), 1RHS3(25),ASP1(25),TINT1(25),ASP2(25),TINT2(25), IASP3 (25), STINT (25), UTINT (25) PEAD 1, NVAR, KTYPE1, KTYFE2, KTYPE3, TTYPE1, ITYFE2, ITYPE3 JRFS=NF0ZZY+KTYP21+KTYEF2+KTYPE3*2 NFUZZY= ITYPE 1+ITYPE2+ITYPE3*2

WRITE (80, 103) NVAR, NRES, NFUZZY FORMAT (315) 0≈S 10.3

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C ***KIGID CONSTRAINT TYPE 1(<) .

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AFAD 2, (Y1 (IC, I), 1=1, NVAE) IF (KTYPT1.EQ.0) GC TC 30 DA 50 IC= 1, KTYPE1 Š

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GC TC 151
                                                                                                                                                                  RIGID CONSTRAINT TYPE 2 (>)
READ 2, (RHS 1 (1), T = 1, KTYPF 1)
DO 100 I = 1, KTYPE 1
                                                                                                                                                                                                                                           EEAD 2, (X 2 (I 3, I ), I = 1, N VAR)
READ 2, (RHS2 (I ), I = 1, KT YEE2)
                                                                                                                                                                                                               IF (KTYPE2.EQ.0) GO TO 31
                                                                                                                                                                                                                                                                                       IF (RHS2 (IA) .GE.0.0)
                                                                                                                                                                                                                                                                        DO 151 TA=1, KTYPR2
                                                                                                                                                                                                                                                                                                       RHS 2 (IA) =-RHS 2 (IA)
                                                                                                                                                                                                                                                                                                                                    X^{2}(IA, I) = -X^{2}(IA, I)
                                                                                                                                                                                                                             DO 51 IA=1,KTYPE2
                                                                                                                                                                                                                                                                                                                                                                                DO 300 I=1,KTYPE2
                                                                                                                                                                                                                                                                                                                                                                                                             DO 400 J=1,NVAR
ROW (M,J)=X2(I,J)
KH3(M)=RHS2(I)
                                                           ROW (M, J) = X 1 (I, J)
RHS (M) = RHS1 (I)
                                            DO 200 J=1,NVAR
                                                                                                                                                                                                                                                                                                                      DO 152 I=1,NVAR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        M=KTYPE1+KTYPE2
                                                                                                     CONTINUE
M=KTYPE1
                                                                                                                                                                                                                                                                                                                                                                                                                                                          CONTINUE
                                                                                      CONTINUE
                                                                                                                                                                                                                                                                                                                                                                   CONTINUE
                                                                                                                                                                                                                                                                                                                                                    CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                          CONTINUE
                               N= M + 1
                                                                                                                                                                 5 ***
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FFAD 2, (X4 (ID,I), I=1, NVAE)
FFAD 2, (ASP1(I), TINT1(I), I=1, ITYPE1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   PHS(7) = (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (7) + (
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                                                                                                                                                                                                                                                                                           READ 2, [X3 [IB, I], I=1, KVAF)
REAE 2, (KHS3 (I), I=1, KTYPF3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          (I) I L I I X ( ( ', ') ) = - X 4 ( I, ') / T I N I 1 ( I)
                                                                                                                                                                                       GO TO 32
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   M= KTYPE1+KTYPE2+K'TYPE3*2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                IF (ITYPE1.EQ.0) GO TO 33
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             IF (J.EQ.NVAK) GO FC 600
C *** LIGID CONSTERING TYPE
C ***
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   FUZZY CONSTRAINT TYPE
                                                                                                                                                                                                                                     DO 52 JB= 1, KTYPE3
                                                                                                                                                                                                                                                                                                                                                                                                          DO 500 I=1, KTYPF3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         DO 60 ID= 1, ITYPE 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      PO 700 I=1, ITYPF1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           (C, I) (X-= (C, M) WCH
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              HOW (M, J) = X3(I, J)
PHS (M) = PHS3(I)
                                                                                                                                                                                IF (KTYPE3. EQ. 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 DO 600 J=1,NVAR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            PO 800 J=1,NVAR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       (I) E SII 4 -= (K) SII (I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CONT INTE
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READ 2, (Y6(IG, I), I=1, NVAR)
AEAD 2, (ASP3(I), STINT(I), UTINT(I), I= 1, ITYPE3)
                                                                                                                                                                                                                                                                                                                                                                                                                             M=KTYPE1+ KTYPE2+ KTYFE3+2+ ITYFE1+ ITYPE2
                                                                                                                                                                                                                                                                                                                                                                     WRITF(6, 104) (ROW (M, MN), JN= 1, NVAR), RHS(M)
GEITE(80, 104) (RCH(M, MN), MN= 1, NVAR), FHS(M)
HRITF (60, 104) (ROM (M.M.), MN=1, NVAK), PHS (M)
                                                                                                                                                                                                               READ 2, (X5(IF, I), I=1,NVAR)
LEAD 2, (ASP2 (I),TINT2 (I),T=1,ITYPE2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    RHS (M) = -(ASP3(I) - STINT(I)) / STINT(I)
                                                                                                                                                                                                                                                                                                                               RHS (M) = (T INT 2 (I) + ASP2 (I)) / TIN T2 (I)
                                                           M=KTYPE1+KTYPE2+ KTYPE3*2+ITYPE1
                                                                                                                          .
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      FUZY CONSTRAINT TYPE 3 (=).
                                                                                                                   <u></u>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 (I) LN ILS / (\Gamma, I) \partial X = (\Gamma, F) WOR
                                                                                                                                                                                                                                                                                                              (I) ZIN IT (U, J) = X5 (U, M) / TI NT2 (I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ŝ
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                                                                                                                   ~
                                                                                                                   FUZZY CONSTRAINT TYPE
                                                                                                                                                                          6C 1C
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              IF (I1YPE3.EQ.0) GG TC
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       PO 1400 I=1, ITYPE3
                                                                                                                                                                                                                                                    DO 900 I= 1, ITYPE2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               DO 54 1G=1, 11YPE3
                                                                                                                                                                                             DO 53 IF=1,ITYPE2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               DO 1200 J=1, NVAR
                                                                                                                                                                                                                                                                                          DO 1000 J=1, NVAR
                                                                                                                                                                          IF (ITYFE2.EQ.0)
                    FORMAT (8F10.4)
                                       CONT I NI E
                                                                                                                                                                                                                                                                                                                                                    CONTINUT
                                                                                                                                                                                                                                                                                                                                                                                                             CONT INUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            M = M + 1
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(ROY (KKJ, MK), MK=1, NVAR), RHS (KKJ) (ROW (KKJ, MK), MK=1, NVAR), RHS (KKJ) (ROW (KKJ, PK), MK=1, NVAR), FHS (KKJ) (ROU (KKJ, EK), MK= 1, NV AK), RHS (KKJ) WEITE (80, 104) (804 (LMN, J), J=1, NVAR), 6HS (LMN) (ROW (LMN, J), J=1, NVAR), RHS (LMN) RHS (M) = (UTINT (I) +ASP3(I)) /UTINT(I) IF (J.EQ.NVAP) GO TC 1200 12624 BYTES, AEPAY AREA= KJK=KTYPE1+KTYPE2+KTYPE3*2 (I) IN IIN/(C'I) 9X = (C'H) NCY DC 1124 LMN=1, %JK UPITE (80, 104) ARITE (80, 104) FOR MAT (9F8.4) WRITE (6, 104) WEITP (6,104) HAITE (6, 104) KK.J= ACOUNT-1 FORMAT (715) KKJ=KKJ+1 CONTINUE CONTINUE ACOUNT=M 746 (KJ = 0)1 - W = M STOP **UN**3 1124

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17817 0, NUMBER OF EXTENSIONS= 18600 BYTES, TOTAL AREA AVAILABLE= **O**, NUMBER OF WARNINGS= 0.06 SFC, 0.21 SEC PYECUTION TIMF= NUABER CF ERRORS= OBJECT CODE=

COMMCN/COM2/GNOBFU (2), CBJCO7 (50) COMMON/COM3/AMTAVL (30), AKTNED (30), SLACK (30), TFCHCO (30, 50), NRES, IFE COMMON/COMI/ISELTO(50), NSELTO(50), ISELEC (3), NSELEC (3), NPRCNS, NF DIMPNSION MSZARY (5C), X (50), FRFS (50, 50), FCONST (50) DIMENSION AMTRES (30), IFITES (50), FATIC (50), RVALUE (50), SLCKFT (30) FEAD (80, 860) [TECHCO (11, JJ), JJ=1, NVAR), AMTRES (11) CONHON/COME/LISTOR (50) , NVARNS, NVARSE COMHON/COM4/IMPDSC (6), NNSFEC, NS RPFO COMMON/COU21/INDEX, FICEFU, MCOUNT COMMON/CON41/KFLAG, THI AL, JFLAG NVAR, NRES, NFUZZY STOP COMMON/CON23/G3JF UN COMMON/CON38/FCONST COMMON/CON39/NFUZZY COANON/ CON40/14ARK PO 1134 JJ=1, NVAR COMMON/CON22/FRES COMMON/CON24/1XX DIMENSION IA (50) ГГ (NV AF . ЕQ. 0) DO 2 II=1, НКЕ S DO 622 I=1, NVAR 0.0=(UU) 10.00 COMMON/CON25/X READ (80,850) WRITE(6,840) 0=(I) UJ 1051 NG ELTO (T) =0 +FOSE, JOUTPT READ DATA 0=LdL001 CONTINUE CONTINUE NVAE SE=0 NVAENS=0 AS B

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• AANK PROJECTS BASED ON VALUE OF RATIC (J) . HIGHEST=1ST. RVALHE(J) = RVALHE(J) + TECHCO(I, J) / AMTHES(I)40 TF (FATIO (IID). LE. FATIC (IID-1)) GC TC CALCULATE PVALUE FOR FACH VARIABLE C3JC0F (JJ) = 0BJC0F (JJ) + 1 ECHC0 (I, JJ) 3C TC 1120 IF (AMTHES (I) .EQ.0.0) GC TC 18 IF (RVALUE (J) .EQ. 0.0) .C TC 1 RATIO (J) = OBJCOP (J) /FVALUE (J) FRES (1, JJ) = T ECHCO (1, JJ) TEATICSEATIO (JID-1) FCONST (I) = AMTRES (I) BO 1133 I=1, NFUZZY TNTERCHARGE AATIC NO 133 I= 1, NFUZZY DO 134 JJ=1, NVAF PO 40 ID=2,NV&R 18 J= 1, NVAR DO 19 I=1, NRES C*** CALCULATE RATIC DO 20 J=1,NVAR R VA L IIE (J) =0.0 HATIO(J)=0.0 CONTINUE LIST DR (J) =J CONTINUE CONTINUE CONTINUE CONTINUE $1S\Gamma ART=0$ GC TO 20 K FL A G=0 IID=ID£ *** 5 1134 C M 1133 133 *** 1120 20 * * * 134 18 ** *** () *** U

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C *** C *** DETERMINE THE INFILAT SCLUTICN WITHOUT FITBACK. INT ERCHANGY PROJECT NUMBER LELTD (NVARSF) = I LST DR (KLJ) LISTDR (IID-1) =LISTDR (IID) LISTDR (IID) =LISTT JF (IA (J) - FQ- 0) GG TC 165 GVANSE=NVAPSI+1 F (IA (JT) .NE.2) GO TC 50 RA TIO (IID-1) = RATIC (IID)IF (IID-1) 40,40,30 COMTINUE (I-011) RULSIDE (IID-1) DO 778 KLJ=1,NVAR PAT IO (IIC) =TEATIO DO 111 KJ=1, NVAF DO 201 AP=1, NTIM N-fI H= (2**NVAR)-1 17=1.157DR (JJ) 1A (JT) = 1A (JT) +1 J=LISTDR (KLJ) NT = NF 0ZZY + 11 - 0 I I = 0 I IIA (KJ) =0 0= (.6.C) VI GO TO 35 NCOUNT=0NV A FNS=0 **NV A RS E=0** 1+11-11 C • U = WOS O = X = O N JO= EX ONI 1.1=1 *** **4**0 *** C *** 50 181 11 35

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IF (NSLACK.EQ. (NEES-NFUZZY)) GO TO 85 IF (SLACK (IJK).6F.0.0) GC TC 1121 hCOUNT=0 [F(SUM.LE.AMIRES(I)) GO TO 70 **SLACK (IJK) = AMTRES (IJK) - AMTSUD** AMT SUD = A MT SUD+ TECHCO (I JK, KND) SLACK (JT) = AMTRAS (JT) - AETSUD AMI 30 D= AMTSU D+TECHCO (JT, IT) 201 PER ELT D (INDEX) = LISTDR (KLJ) GO TO 6C IF (NVALSE.EQ. 0) GO TO DO 1100 IM=1, NVARSE DO 1199 IQ=1, NVARSE CO 1110 IJK=NT, NRES SU.1 = SUM+ TECHCO (I, J) DO 1195 JT=1, NFUZZY DO 60 IND=1, NVAR DO 80 I=NT,NRES NSI. ACK= NSLACK+1 IF(IA(J).EQ.0) KND= ISELT D(IM) I NDEX=INDEX+1 J=LISTDA (IND) IT = ISELTD (IQ)0*TSUD=0.0 AMTSUD=0.0 GU TO 778 GO TO 201 GO TO 201 CONTINUE CONTINUE GU 10 80 GO TO 60 NSLACK=0 COMPTNIE NCO IN T=0 SUM = 0.0165 1110 1100 0611 1121 778 £ 0 £35 70

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SELFCTED CALCULATE THE MEMBERSHIP FUNCTION AS AN INITIAL SOLUTION FILL THE VECTORS OF SELECTED AND NON-SELECTED VARIABLES WFITE(6,924) [ASELTD(IJ),IJ=1,NVAFNS) FORMAT(1X,"THE SET OF NON-SELECTED VARIABLES IS ',1615) PROJECTS BASED ON THEIT CRUFCTIVES. CCEFFICIENTS VALUE AANK PROJECTS IN BOTH SETS OF SELECTED AND NON -WRITE (6,910) (ISELTD (II), II=1, NVAASF) CALCHLATE SLACK FOR FACH CONSTRAINT IF (SLACK (JT) . GE. 0.0) GO TO 1198 AMTSUD=AMTSUD+TECHCC (I, INP) IF (IOUTPT.EQ.0) GC TC 110 SLACK (I) = ANT RES (I) - AMT SUD 1F (IMAAK. FQ. 10) GO TO 110 IF (HVARSE .EQ. 0) GC TC 201 IF (IMAPK. EQ. 10) GO TO 55 WEITE (6,925) I, SLACK (I) WRIJE(6,920) OBJPUN DO 100 LS=1, NVARSE SLCKFT (I) =SLACK (I) DO 110 T=1,NRES IND=ISELTD(IS) NV A RNS= INDEX GO TO 1185 03.7 FUN=0.0 AYTSHD=0. CALL RANK GG TO 201 CALL OUJ CONTINUE 1198 CONTINUE CONTINUE COUNT=0195 *** c'811 100 ×** ℃ 68 201 C *** *** U ** *** J C *** 95 207 924

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FORMAT(5X, "NO FITAACK SCLUTION CAN BE FOUND TO IMPROVE THE INITIAL IF (SLCKFT (II) .LT.TECHCC (II, INDEX)) GC TO 130 SLC KFT (IK) = SLC KFT (IK) - TECHCC (IK, INDEX) TOUND A VARIABLE FCE FITBACK SOLUTION (LFITPS(II), II=1, NVAFTB) UPDATE SLACK VALUE AND CALCULATE IF (NVAFTB-FQ-NVARSF) GC 10 141 GO TO 140 (1START.EQ.1) GC TC 150 LFITES (NVAFTB) = NSELTD (J) THE MEMBERSHIP FUNCTION FIND FITBACK SOLUTION LFTTRS(IP)=ISELTD(IP) FICBFU DO 220 IP=1, NVARSE SNARNA 1=0 041 CC IF (IFLAG. NE. NRFS) DO 135 IK=1, NRES DO 130 II=1, NRES NV A F'f L= NV AFT B+1 (r) dllasn=xsul HCOUNT=NCOUNT+1 NV A F T B= HV ARS E FTOBFD=OPJFUN IFLAG=IFLAG+1 FTOEFU=-9999. WEITE (6,930) WAITE (6,920) ARLTF (6, 932) WRITE (6, 142) ('NOLTUIO2 CALL FTOBJ 10 TO 150 ACOUNT=0CONTINUE CONT 1 MILE IFLAG=0 4 C ### 220 130 C *** *** C ### C *** 140 135 *** 142 1 + 1

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STORE PROJECT AUMBERS SO THAT THEY WILL NOT BE USED IN THE 1/1 EVC IF (NS 1. NE. 1. CH. NEKOFT.NE. 0) GO TO 155 IF (GJOBFU (2) . GE. GNOBFU (1) GO TO 160 T (NS2ST.GT.NS2LST) GC TC 210 2/1 EXCHANGE NOT AD VANTAGEOUS JF (LFEASB.NE.NRFS) GO TO 170 CALL LEPVNT TE ([252-NS1)-2] 200,200,180 F ((NS2-NS1) -2) 200,200,180 **IC 212** NSFLEC (2) =NSFLTD (NS2) CHRCK MEMDERSHIP FUNCTION 00 170 NS2=HS2ST,NS2IST [SELEC (1) =I SELED (JS1) NSELEC (1) = NSELTD (NS 1) 00 00 210 JS 1= 1, NVARSE DO 152 INS= 1, NS ILST DO 190 NS 1= 1, NS 1LST NSZARY (INS) = NVARNS NS2LST=NS2ARY (NS1) CHECK FEASIBILITY (NS1LST.EC.0) NS 1LST=NV ARNS-1 2/1 EXCHANGE GNOBFN(1)=0.HS 25 T= N5 1+1 CALL FRASBL CALL ACHVMT ISU=T=ORGK ISN=9MLSN **NS 2 N P= NS 2** N P RONS = 2NPROSE=1 NPROFT=0 I 7 L AG=0 I F L AG= 1 TPLAGE 1 ЧI 160 155 *** *** · ر: * * # *** * * * 0 *د* ا 152

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IF (GHOBPU (2) .GE.GNOBPU (1)) GO TO 215 MSŽAKY (NS1NP) =NSZNF+ ((1-TDIF) *IFLAG) CONTINIE IF (JS1LST_GT_NVARSF) JS1LST= NPFOFT - 1 DC 240 NS 1= 1, NVARNS 185 20 IF (NS INP. NF. NS ILST) GO 10 210 NS1LST=NS1NP-((2-IDIF) *IFLAG) IF (IFTASh_NE.NRES) GC TC 221 IF (NS2ARY (1) . NE.NS2LST) 60 IF (NS1LST.EQ.0) GO TO 212 IDIF= (NS2NP-NS1NP) * IFLAG NSELEC (1) =NSELTD (NS1) FFLAG=0 ISELEC(1) = ISELTD(JS1) JS1NP=JS1NS2LST=NS2NP-1+TFLAG JS 1LST= NV ARC E +NPROFT DO 221 JS1=1, JS11ST 00 185 I=NS1, IENP NSZAFY(I)=NSZLST TEND=NVARNS-1 1/1 EXCHANGE CALL ACHVMT CALL FLASBL CALL INPUNT GO TO 230 60 10 230 CONTINUE CONTINUE CONTINUE NPRONS=1 CONTINUE 1 - 1 4 4 - 1 [FL AG=] 185 190 200 2 10 C ### C *** 221 ***

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FOUND AN EXCHANGE TO IMPROVE THE MEMBERSHIP FUNCTION SECOND SEARCH (3/1,3/2,3/3 EXCHANGES) WRITE (6,935) WPITE (6,950) (ISFITD (II),II=1,NVARSE) IF (GNOBFU (1) . LE. U.) GO TO 290 IF (JS1LST.EQ.0) GC 1C 250 IF (ISTART.EC.0) GC TC 300 IF (NV ARNS.LT.3) GO TO 480 IF (IOUTPT.EQ.0) GC TC 260 03.JFUN=OBJFUN+GNCBFU (1) 1/2 EXCHANGE JS 1LST=JS 1NP-1+TFLAG REPFAT FIRST SEARCH WAITE (6,920) CBJFUN DG 430 NS 1= 1, NS 1LST OBJFUN MAKE THE EXCHANGE USILET=NVARNS-2 WRITE (6,955) UPITE (6,960) GRUBFU (1) =0. WRITE(6,920) WRITE(6,940) WRITF (6, 935) CALL EXCHGE GO TO 305 CONTINUE GO TO 95 15TP32=0 0=CE d1S1 CALL OBJ CALL OBJ ISTART=1 8 = SNO Hdn 290 *** ご 260*** *** *** () 24.0 +** * *** .) *** い 057 5 ### 0 300 305 250

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IF (JS INP. L. (2-IFLAG) . CH. ISTP 32. EQ. 1) GO TO 430 IF (GROBFU (2) .GF.GROBFU (1)) GO TO 320 STORE JAPROVED SCLUTICK TEMFORAKLY IF (J525T. GT. JS2LST) G0 T0 380 NS RL EC (IIP) = NSELTD (NS 1+1TP-1) IT (IFEASB.NE.NES) GO TO 330 00 360 JS 2=JS 2ST, JS 21 ST CHECK FOR PRCFITABILITY CHECK FOR FEASIBILITY ISELEC(1) = ISELTD(JS1) JSELEC (1) =ISELTD (JS1) JS1LST=JS1NP-2+IFLAG JS2LST=JS INP-1+IFLAG DO 370 JS1=1, JS1LST DO 330 JS1=1, NVARSE nu 310 IIP=1,3 3/2 EXCHANGE JSLIMT=JS1NP 3/1 EXCHANGE J52ST=JS1+1 CALL FEASBL CALL IMPVNT CALL ACHVAT **JS211P=JS2** GU TO 340 ISU=JNISP **HPROSE=2 CONTINUE** NPROSF=1 0=9V1.11 1 FL AG=0 IFLAG= 1 ***) C *** C * * * * 330 3 10 ¥** ℃ 、 * * * C *** ×** ℃ *** こ *** Ü 340 320

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IF (NVAPST.LT.3.GR.JS11ST.EC.1.OR.ISTP33.E2.1) GO TO 430 IF (GNOEFU (2) . GE. GNOBFU (1)) GO TO 350 IF (JS1.NE.1.CR.JS2.NE.2) GO TO 345 STORF IMPHOVED SOLUTION TEMPORARLY GO 10 380 IF (IFLASE.NE.NRES) GO TO 360 CHECK FOR PROFITIBILITY DO 410 J52=JS2S1, J52151 T21C3L, T353C=5 004 00 CHECK FOR FEASIBILITY ISELEC(1) = ISELTD(JS1) $LS \Gamma L EC (2) = IS EL T R (JS2)$ JS2LS7=JS2NP-1*IFLAG 00 420 JS 1= 1, JS 1LST 1 F ((JS2-JS1) . LE. 2) JS2LST=JS2LST-1 JSILST=JSILST-1 TALLEL SULES U 3/3 EXCHANGE 15257=351+1 CALL ACHVMT CALL FEASBL CALL INPVNT 15351=J52+1 02 1 0 4 3 0 GO TO 365 CONTINUE CONTINUE ISTPJ2=1 NPROJF= 3 1 F L A G = 1 ・ * * * い 345 C *** C #** C *** *** ### () *** J 305 350 380 360 370

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ISELEC (3) =1 SFITP (453)

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943 FORMAT (100, 64HTHE INFIIAL SOLUTION (WITHOUT FITBACK) IS COMPCSED O
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     FCRMAT (1EO, 36X, 59H*** EEURISTIC ALGORITHM FOR LARGE
                                               385
                                                 10
                                               09
                                                                                                                                                                                                                                                                                                                                                                                      RRITE (0,990) (LFITBS (II), II=1, NVAFTE)
                                EF (GNOBFU (2) . GE.GNCBFU (1) ) GO TO 390
                                             IF (JS 1. NE. 1. CR. JS 2. NE. 2. OF. JS 3. NE. 3)
                                                                                                                                                                                                                                                                                                                                                                                                                                       WEITE (6,990) (ISELTD (TI),II=1,NVALSE)
WPITE (6,920) OBJEUN
                                                                                                                                                                                            STORE IMPROVED SCIUTICN TEMFORARLY
                                                                                                                                                                                                                                                                                                                                                                         IF (ORJEUN. GE. FTOBEU) GO TO 490
                                                                                                                                                                                                                                                                                           IF (GNOBFU (1) .GT.0.) GC TC 470
                                                                                                                                                           IF (IFEASB-NE-NRES) GO TO 400
                                                                                              IF ( (JS3-JS2) -2) 430,430,410
CHECK FOR PROFITABILITY
                                                                                                                              CHECK FOR FEASIBILITY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      +F PIGUTCTS : ,5014///)
                                                                                                                                                                                                                                                                                                                                                                                                       URITE (6,920) FICBFU
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      +EOGEAMS ***//)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      FORMAT (RF10.4)
                                                                                                                                                                                                                                                                                                           WEITE (6.970)
                                                                                                                                                                                                                                                                                                                                          WRITE (6, 980)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      FORMAT (1615)
               CALL ACHVMT
                                                                                                                                             CALL FEASEL
                                                                                                                                                                                                             CALL IMPVNT
                                                                                                                                                                                                                                                                                                                           GU TO 480
                                                                              GU TO 430
                                                                                                                                                                                                                                                                                                                                                                                                                         60 10 500
                                                               ISTP33=1
                                                                                                                                                                                                                                           CONT INUR
                                                                                                                                                                                                                                                          CONTINUE
                                                                                                                                                                                                                                                                                                                                                          CALL OBJ
                                                                                                                                                                                                                             CONTINUE
                                                                                                                                                                                                                                                                           CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                        STOP
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FORMAT (1HG, 4 1HTBE VALUE OF THE MEMBERSHIP FUNCTION IS :, F8.2/// 0

930 FORMAT (180, 46HTHE FITEACK SOLUTION IS COMPOSED OF PROJECTS : 5014)

FUEMAT (180,45X,418*** FIEST SEARCH (2/1 - 1/1 EXCHANGE) ***//) 932

935 FORMAT (140, 73HTHE FIRST SEARCH HAS FOUND AN EXCHANGE TO IMPRCVE TH +L: ALMBERSHIP FUNCTION)

940 FORMAT (140, 46%, 404REPEAT FIRST SFARCH (2/1 - 1/1 EXCHANGE) ///) 950 FORMAT (140, 384THE SCIUTICA IS CORFECSED OF PROJECTS : 5014) 955 FORMAT (140, 734THE FIRST SEARCH HAS FOUND NO EXCHANGE TO IMPROVE TH

+E MEMBERSHIP FUNCTION)

990 FORMAT(1H1,44HTHE FINAL SCLUTION IS COMPOSED OF PROJECTS :, 5014) FORMAT (10.26WTHE SLACK FOR CONSTRALAT : ,14,5H IS :,F8.2) 960 FORMAT (1H0,42%, 925

**** SFCOND SEAFCH (3/) 3/2 3/3 FXCHANGE) *** +

FORMAT (1110, 7611THE SECCAD SEARCH HAS FOLNE NO EXCHANGES TC IMFROVE +THE MFMBFRSHIP FUNCTION.) 970

FORMAT (1110, 75HTHE SECOND SEARCH HAS FOUND AN EXCHANGE TO IMPFOVE T THE MEMBEPSHIP FUNCTION.) FND 930

COTWON/COMI/ISELTD(50), NSELTD (50), ISELEC (3), NSELEC (3), NPRONS, NPR BASFD AANK PROJECTS IN SET OF NOW - SELECTED PROJECTS (NSELTD) COMMON/COM5/IISTOR (50), NVARES, NVAES E COMBOY/COM2/GNOBFH(2), OBJCCF(50) GO TO 21 IT (NV AENS . FQ. 1) DO 20 ID=2, NVARNS SUBROUFINE RANK ON OJJCO VAINE DIMEKSION X (50) CUMMON/CON25/X +OSE JOUTPI * * * * * * * C U

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FORMAT (1HO, 60HTHE SET OF NON - SELECTRD PROJECTS IS COMPCSED CF PR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             OF SFLECTED PROJECTS IS COMPOSED OF PROJECTS
                                                                                                                                                                                    PANK PROJECTS IN SET OF SELECTED FROJECTS (ISELTD) BASED ON
                                                                                                                                                                                                                                                                                                                  40
                10 20
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                 00
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  WRLTE (0, 50) (NSELTD (II), II=1, NVARNS)
BELTE (6, 60) (ISELTD (II), II=1, NVARSE)
               IF (GBJCOF (IND2) . LE. OBJCOF (IND 1) )
                                                                                                                                                                                                                                                                                                                 IF [OBJCOF [IND2] .G. .C. C. JCCF (IND1) ]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  IF (IOUTPT.EQ.0) GO TC 70
                                                                                                                                                                                                                                                                                                                                                      SELTD (IID-1) =I SELTD (IID)
                                                     NSELTD(IIC-1)=NSFLTD(IID)
                                                                                                                                                                                                                        2
                                                                                                                                                                                                                        30 TO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           60 FORMAT (180, 54 HFTE SET
                                  NSELTT=NSELTD (IID-1)
                                                                                                                                                                                                                                                                                                                                   SELTT= IS ELT D (IID-1)
                                                                                                           20,20,10
                                                                                                                                                                                                                                                                                                                                                                                                            40,40,30
                                                                       TTIEN = (UII) GITESN
                                                                                                                                                                                                                                                                                                                                                                        SETTD (IID) = ISELTT
                                                                                                                                                                                                                                                                              IND 1=I SELTD (IID-1)
                                                                                                                                                                                                                       JF (NVARSE.EQ. 1) 30
DO 40 ID=2,NVARSE
[WD 2=NSELTD (IID)
                                                                                                                                                                                                                                                                                               IND2 = IS ELTD (IID)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           +0.1FC1S : ,5014)
                                                                                                                                                                                                    OBJECO VALUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              +:,5014///)
                                                                                                                                                                                                                                                                                                                                                                                                          (I-UII) 4
                                                                                                           IF (IID-1)
                                                                                                                                                                                                                                                                                                                                                                                          I = I I D = I I D = 1
                                                                                        I = 0 I I = 0 I I
                                                                                                                            CONTINUE
CONTINUE
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CONTINUE
                                                                                                                                                                                                                                                            IID=ID
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Addition of the local division of the

SUBFOUTINE IMPVNT COMMON/COM1/ISELTD(50), NSFLTD(50), ISELEC(3), NSELEC(3), NPRONS, NPR FOFMAT (1HO, 48H*** THE EXCHANGE IS BOTH PROFITABLE AND FRASIBLE) COAMON/COM4/IMPDSO (6) , NNSERO, NSFERO . GNOBEU (1) =GNOBFU (2) COMMON/CON2/GNOFFII (2), CBJCOF (50) IMPDSC (NPRONS+IP) = ISEL EC (IP) (IOUTPT-EQ.0) 30 TC 40 DC 10 TP=1, NPRONS IMPDSO(IP)=NSELEC(IP) DO 20 IP=1, NFROSE NS E P RO= N P ROS E NNSPRC=NPRONS WRITE (6, 30) +OSE , IOUTPT RETURN **UND** ΞŢ

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No. of Concession, Name

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COHMON/COM3/AMTAVL (30) , AMTHED (30) , SLACK (30) , TECHCC (30, 50) , NRES, IFE COMMON/COM1/ISELTE(50), NSELTD(50), ISELEC(3), NSELEC(3), NPRONS, NPR IF (I-EQ.NRES_AND_AKINEL (I). GT. ANTAVL (I)) GO TC 40 I? (ICHTPT-EQ.0) GO TO 70 IF (AMTHED (I).GT.AMTAVI (I)) GO TO 40 AMTNED (I) = AMTNED (I) + TECHCC (I, INDX) AYT AVL (I) = SLACK (I) + TECECO (I, TND X) DO 22 IP= 1, NFROSE DO 10 IP=1,NPRONS SUBROUTINE FEASBL I NO X= I SELEC (IP) IFEASE= IFEASE+1 I NDX=NSELEC (IP) DO 40 J=1, MRES AMTNED(I)=0. FGTUOI, RCO+ IFFASB=0 CONTINUE RETURN + A SB END

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COMMON/COMMINISELTD(50), WSELTD(50), ISELEC(3), NSELEC(3), NPRONS, NPR
                                                                                                                MAKF THE EXCHANGE IN SET OF NON - SELECTED PROJECTS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           MAKF THU EXCHANCE IN SET OF SELECTED PROJECTS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              (ISULTD (IP).EQ.IMEDSC (NNSPRC+IS)) GC TO 70
                                                                                                                                                                                                                                   20
                                                                         COMMON/COM5/IISTDR ( 50) , NVAPNS, NVAFS E
                                                                                                                                                                                                                                  (NSELTD (IF).EQ.IMPDSC (IS)) GO TC
                                                      COTHON/COM4/IMPDSO(6), NNSPRO, NSEPRO
                                                                                                                                                                                                                                                                                                                                                                                                                                                  MS ELT D (IN CEX + IP) = IMPDSC (NNSPRO+IP)
                                                                                                                                                                                            (ISST.GT. NNSPRC) ISST=NNSPRO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       IF (ISST.GT. MSEPRC) ISET=NSEPRO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     NVARNS=NVARNS+NSEERC-NASPRO
                                                                                                                                                                                                                                                                                                                                                                         S
S
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   LI SIDA (INDEX) =ISPITD (I E)
                                                                                                                                                                                                                                                                       LISTOR (INDEX) = NSELTD (IE)
                                                                                                                                                                                                                                                                                                                                                                       G0 T0
                                                                                                                                                                                                                                                                                                                                                                                                            NS 3LT D (IP) = L IST DR (IP)
                                                                                                                                                                                                               10 IS=ISST, NNSPRO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          DO 60 IS=ISST, NSEPRO
                                                                                                                                                                                                                                                                                                                                                                                                                                DO 50 IP=1, NSE2RO
SUBRCUTINE EXCHGE
                                                                                                                                                                        DO 30 IP= 1, NVARNS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     DO 80 IP= 1, NVAKSE
                                                                                                                                                                                                                                                                                                                                                                                         DO 40 TP=1, INDEX
                                                                                                                                                                                                                                                                                                                                                                      IF (INDEX.EQ.0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  1 + XHGHI = XHGHI
                                                                                                                                                                                                                                                      I + XEGNE = XEGNE
                                    +USE, IOUTPT
                                                                                                                                                                                                                                                                                                                                 I + SI = TSSI
                                                                                                                                                                                                                                                                                                             CONTINUE
                                                                                                                                                                                                                                                                                                                                                   CUNTINUE
                                                                                                                                                                                                                                                                                           GO TO 30
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        GO TO 80
                                                                                                                                                     I = X = 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   I = X = 0
                                                                                                                                    1557=1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                1=1231
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60 CONTINUE

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- 70 ISST=IS+1 80 CONTINUE
- IF (INDIX.EQ.0) GO TO 95
- DO 90 IP=1, INDEX
 - 90 ISELTD(IP)=LISTDR(IP)
- 95 DO 100 IP=1,NNSPRO
- 100 ISELTD(INDEX+IP)=IMPDSO(IP) NVARSE=NVARSE+NNSPRO-NSEPRO RETURN END

SUBROUTINE ACHVMT

DIMENSION FRES(50,50), FCONST(50), FOBJ(50), TEST(50), IBASE(50,50), COMMON/COM1/ISELTD(50), NSELTD(50), ISELEC(3), NSELEC(3), NPRONS, NPR COMMON/COM5/LISTDR(50), NVARNS, NVARSE COMMON/COM2/GNOBFU(2), OBJCOF(50) FOBJ(I) = (-FRES(I, INDX)) + FOBJ(I)COMMON/CON41/KFLAG, TRIAL, JFLAG COMMON/CON34/NCOUNT COMMON/CON38/FCONST COMMON/CON39/NFUZZY COMMON/CON23/OBJFUN COMMON/CON40/IMARK DO 145 IP=1,NVARSE COMMON/CON22/FRES DO 134 I=1,NFUZZY COMMON/CON24/IXX INDX=ISELTD(IP) GNOBFU(2)=0.0 INBASE (50,50) FOBJ(I)=0.0HOSE, IOUTPT KFLAG=1

FORMAT (100, 65h THE EXCRANGE UNDER CONSIDERATION CONSISTS OF REPLAC говная (19+,79х, 14н ву гесовстя :, 314) URITE (6,30) (ISELEC (11), 11=1, NPROSE) (BSELFC (11), JT=1, MPRONS) IF (GNUEFU (2) . IE. 0. 0) GNCEFU (2)=0.0 IF (TEST (I) . LE. TEST (J)) GC TC 183 FOBJ (I) = FORJ (I) + (- FRFS (I, INDX)) FOBJ (I) = FOBJ (I) - (-FRES (I, IN DX)) IF (TEST $(1) \cdot GT \cdot 1 \cdot 0)$ TEST $(1) = 1 \cdot 0$ IF (TEST (I).L1.0.0) GO TC 83 FUBJ (I) = FCONST (I) + FOBJ (I)IF (IOUT PT. FQ. 0) GO TO E0 IBASE (I, I IP) = ISELEC (II I) GWOEFU (2) = PSOFAR-OBJFUNNEA SE (I, IP) = NSELEC (IP) IS ELFC (IP) = IBASF(J, IP)NSELEC(IP)=NBASE(J, IP) ISELEC(IP) = I DASE(I, IP) NS ELEC (IP) = NBASE (I, TP) GNCBFU(2) DO 1383 1 P=1, NPRONS DG 1283 IF=1, RPROSE 00 136 II P=1, NPROSE FO 383 IP=1, NERCNS DO 135 IP=1, NPRONS 00 283 IP=1, NPROSE +46 PHOJECTS :,314) 00 83 I=2,NFU22Y LUDX= IS ELEC (IIP) INDX=NSELEC(IP) 72ST(I)=FOBJ(I) LSOTAR=TEST (J) BSOFAR=TFST (1) zhtte (e, 50) 27111 (0,40) CONT INUE CONTINUE GO TO 83 CONTINTE J= I - I 1393 383 60 10 135 1283 183 283 83 -3 145 136 134 30 35

THE GAIN IN THE MEMBERSHIE FUNCTION WOULD BE : ', FM. 2) FORMAT (9X,' RFTURN END 50 80

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COMMON/COM1/ISELTE (50) "HSELTD (50) "ISELEC (3) "NSELEC (3) "NPRONS, DIMENSION FRES (50,50), FCCNST (50), FORJ (50), YLAMDA (50) FONMAT (5%, THE INTIAL SCUTTION TS INFEASIBLE") COMMON/CCM5/LISTDR (50), NV ARNS, NV ARSE = 1.0 **BFST= YLAMDA(T)** FOBJ (I) = (-FRES (I, INDX)) + FOBJ (I)COMMON/CON41/KFLAG, TRIAL, JFLAG F (YLAMDA(I).LT.0.0) GC 10 139 YIAMDA (I) (I) HEADA (I) =FC GNST (I) +FCEJ (I) 138 [F (YLAMDA (I) .GT. 1.0) COMMON/CON23/OBJ FUN COMMON/CON39/NFUZ2Y COMMCN/CON38/FCONST COMMON/CON40/IMARK DO 135 IP=1, NVARSE COMMON/CON22/FFES DO 134 I= 1, NFUZZY IF (I. FO. 1) GO TO IF (TAST.LT.BEST) IND Y=ISELTD (IP) 1 EST = YLAMDA(I)SUBROUTINE OBJ NPROSE, ICUTPI WRITE (6, 140) FObJ(I) = 0.0ULJFUN=BEST 60 TO 134 $B^{T} \subseteq T = 1 \subseteq S T$ 30 70 152 CONTINUE 13464=10 $I \square A P K = 0$ 0140 138 134 681

135

USJFJN=0.0 152 LFTVEN

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فالمحدمة المحدودية

DIMFNSION FRES (50, 50), FCONST (50), CEJ (50), LUBJ (50) CUMMON/CON21/INDEY,FICEFU,MCGUNT COMMON/COM2/GNG BEN (2), CBJCOF (50) LUBJ (IG) = OBJ (IG) + FAES (IG, INDEX) 1.08J (JG) = CBJ (JG) + FFES (JG, INDEX) IF (TFST.LT.BEST) BEST=LOBJ (IG) IF (TEST.LT.BEST) BEST=LOBJ (JG) II (MCOUNT_GT. 0) GC TO 932 DO 934 IF=1, NFUZZY 03.1 (IF) =FCONST (IF) +FTCEFU LF (JG.FQ.1) GC TO 1038 IF (IG.EQ.1) GC TO 938 COMMOR/CON34/NCOUNT COMMON/CON38/FCONST COMMON/CON39/NFUZZY DO 1034 JF=1, NFG22Y DO 1035 JG= 1, NF622Y DO 935 IG=1, NFUZZY COMMON/CON22/FRES SUBROUTINE FTCBJ 0BJ (JP) =F TOBF 0 1 FS T= LOBJ (IG) T PS T = LOBJ (J S)TIOEFU=REST GU TU 1035 GO 10 935 $B \ge 3T = T = T S \le 0$ $L^{1} \subseteq T \subseteq T \subseteq T \subseteq T$ COMPTANT CONTINUE RETUAN 938 935 1034 10 +3 10.35 932 934

FTOBFU=BEST RETURN END

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D= 104717

OBJECT CODE= 31024 BYTES, ARRAY AREA= 40164 BYTES, TOTAL AREA AVAILABLE 0, NUMBER OF EXT 0, NUMBER OF WARNINGS= 0.84 SEC, 0.42 SEC, EXECUTION TIME= NUMBER OF ERRORS=

*** HEURISTIC ALGORITHM FOR LARGE 0 - 1 LINEAR PROGRAMS ***

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œ 3 σh ٥ 10 THE INITIAL SOLUTION (WITHOUT FITBACK) IS COMPOSED OF PROJECTS: THE SET OF NON-SELECTED VARIABLES IS 7 4 5 1 3

THE VALUE OF THE MEMBERSHIP FUNCTION IS: 0.13

THE FIRST SEARCH HAS FOUND NO EXCHANGE TO IMPROVE THE MEMBERSHIP FUNCTION NO FITBACK SOLUTION CAN BE FOUND TO IMPROVE THE INITIAL SOLUTION

**** SECOND SEARCH (3/1 3/2 3/3 EXCHANGE) ****

THE SECOND SEARCH HAS FOUND NO EXCHANGES TO IMPROVE THE MEMBERSHIP FUNCTION

THE FINAL SOLUTION IS COMPOSED OF PROJECTS: 8 6 THE VALUE OF THE MEMBERSHIP FUNCTION IS: 0.13

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APPENDIX D

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Sample Data Input

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Sample Data Input

No.

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The required data input for Example Problem Number 2 is presented. The data input requirements are identical for the computer codes presented in Appendices B and C.

0304	0.	0.	Ι.	0.	0.	36.	10.	7.	
0202	0.	0.	1.	0.	0.	42.	23.	12.	
0408	0.	1.	0.	0.	Ι.	119.	48.	50.	
0618	0.	1.	0.	0.	0.	.96	61.	27.	10.
2 1054	0.	1.	0.	1.	0.	0. 67.	107.	83.	30.
1 1165	0.	1.	0.	0.	0.	1. 64.	95.	.09	100.
5 0 -0.10	1.	0.	0.	0.	0.	1. 160.	19.	10.	15.
0 1 0618	1.	0.	0.	Ι.	0.	1. 95.	65. 57.	35.	30.
10 0304 01	.107			-00		-1. 120.	195. 32.	21.	150.