DEC F 78.33 BOX \sim 0 THE EFFECT OF CERTAIN TARGET AND ENVIRONMENTAL 2 ن وع ا VARIABLES ON THE DETECTION TIME OF OBJECTS IN A COMPLEX NATURAL VISUAL DISPLAY 20 A Thesis A B Presented in Partial Fulfillment of the Requirements for the Degree Master of Science N-15-014-AII-2965 9 Master's thesis. by JOHN JACOB RHEINFRANK B.I.E. The Ohio State University OCT 24 1979 1969 C Systems Research Group Ohio State University 62 6.2 Approved by DISTRIBUTION STATEMENT A 13 Bis Approved for public release Distribution Unlimited Adviser Department of Industrial ො Sponson; US Army Combat Developments Command armon a sen to Engineering and include the second second second

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CHAPTER I

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INTRODUCTION

The visual aquisition of militarily significant objects in a natural terrain environment has, in the past two decades come to the forefront as a major consideration in the design of future military weapon systems. With the surge in sophistication of military hardware design, there is still a strong reliance on the capabilities of the human observer to successfully locate, identify, and bring fire upon enemy elements before he himself, is destroyed. This location of the enemy threat is most often accomplished without the assistance of any clues or devices other than the appearance of an object in the terrain.

->Milita _ planners now rely heavily on computer-simulated war games to evaluate the desirability and investigate tactics and employment of proposed weapon systems in a combat environment. Other questions which might be asked are how certain changes in a system affect performance in combat. However, construction of sophisticated computer-simulation techniques has outpaced the development of models adequately describing the capabilities of the human visual system to locate and identify the enemy. In this thesis, models of the visual detection of stationary and moving targets in a natural terrain setting are developed, with emphasis toward their implementation in a combat simulation.

The Detection Phenomenon

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The ability of the human visual system to successfully locate a threatening enemy plays an important role in the outcome of any battle. The detection of objects of military significance has been defined by Richardson (1963) as ".... the act or process whereby an observer gains knowledge of the presence. the nature, and the location of an object of immediate or potential interest as a target. In applications related to military problems, it has been the usual practice to discuss target acquisition in terms of target detection, identification and location. It is by no means obvious that operationally significant distinctions can be made between the detection and identification parts of the acquisition process which hold true over the complete spectrum of tactical situations and conditions". Boynton and Bush (1955) discuss the phenomenon further: "The perception of a critical target can be complicated by the fact that the observer might think he sees something, but is uncertain as to its particular shape or configuration. This type of perception is compatible with the definition of detection in the practical...situation, in which the observer identifies some object of interest, although he may be unable to categorize it further. If, however, the observer is able to identify the object as belonging to a particular class of objects or as having particular attributes, we may safely surmize that he has not only detected an object but that he has also recognized it. Obviously, recognition implies prior experience, in so far as one cannot categorize a completely novel object."

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From these statements, it is seen that detection, per se, is by no means an easily described process. A wealth of visual detection data has been collected in the past two decades. These data, taken under laboratory and field-based conditions, include both the detection of uniform-luminance diskes silhouetted against homogenous, uniformly illuminated backgrounds as well as the detection of complex three-dimensional objects in a natural setting. Data taken under these two diverse conditions have obvious advantages and disadvantages for application to a model of visual detection. Data taken in the laboratory under the careful control of the experimenter are lacking in realism since the conditions under which they are collected do not mimic natural conditions. Data taken in the field environment are most often of a specialized nature and the conditions under which they are collected are usually not sufficiently controlled. In this thesis, data of both kinds are used in the development of models of visual detection.

Probability Models

The ability of an observer to detect an object in a natural environment is dependent on the conditions of the target, its surroundings, and the observer. The time required to distinguish the target from other elements in the terrain has been used as a measure of detection performance (Stollmack, 1965). The occurrance of a detection within time t is a probabilistic event (Koopman, 1946). Stollmack (1965) has suggested that the negative exponential distribution describes the detection time of a human observer. The detection time model suggested by Stollmack is summarized below.

The probability, P ($\Delta t \mid t$), that a detection occurs in a small time interval (t, $t + \Delta t$) conditional on not detecting up to time t can be written (Stollmack, 1965) as:¹

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$$P(\Delta t | t) = \lambda(t) \Delta t + \widetilde{0}(\Delta t)$$
(1.1)

where λ (t) is the conditional detection rate at time t and it is assumed that P ($\Delta t \mid t$) is proportional to the length of time, Δt .

Given the conditional probability, $P(\Delta t | t)$, the cumulative probabilities, P(t + Δt), of detection in a time (t + Δt) or less can be written as:

$$P(t + \Delta t) = P(t) + \left(1 - P(t)\right) \left[\lambda(t) \Delta t + \tilde{0}(\Delta t)\right], \quad (1.2)$$

where P (t) is the cumulative probability of detecting in time t or less. Rearranging terms in equation 1.2, we have:

$$\frac{P(t + \Delta t) - P(t)}{\Delta t} = \left(1 - P(t)\right) \left[\lambda(t) + \frac{\tilde{0}(\Delta t)}{\Delta t}\right]$$
(1.3)

If it is assumed $\frac{\tilde{0}(\Delta t)}{\Delta t}$ approaches zero as Δt approaches infinity, taking the limit of equation 1.3 as Δt approaches zero yields:

$$p(t) = Q(t) \setminus (t)$$
, $Q(t) = \{1-P(t)\}$, (1.4)

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where p(t) is the unconditional probability density function, the derivative of the

¹ $\tilde{0}(\Delta t) = \lambda (t) \Delta t^2 + \lambda (t) \Delta t^3 + \dots$

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cumulative density function P (t). Solving the differential equation given above,

P (t) becomes:

$$P(t) = 1 - e^{-\int_{0}^{U} \lambda(\tau) d\tau}$$
(1.5)

where τ is a dummy variable.

Several assumptions about the form of the conditional detection rate can be made. The simplest is that in which the rate is assumed constant during the entire appearance of the target as shown in Figure 1.



Fig. 1.--Constant Devection Rate

This case is most certainly true when the target is stationary and the environment in which it is located is fairly stable (no extraneous clues). However, for moving targets, detection clues are constantly changing, altering the form of the conditional detection rate. If these changes in the appearance of the target occur instantaneously during the course of the movement and are measurable, the detection rate will remain constant depending on the relative effect of the environmental change. If it is assumed that the effect of the change is constant until another change occurs, the detection rate will assume the form shown in Figure 2.

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Fig. 2, -- Detection Rate Changing Instantaneously With Time

In Figure 2, the target becomes intervisible to the observer at time 0 and has a conditional detection rate equal to x_1 . At time T_1 , an abrupt change in the characteristics of the target apparent to the observer occurs, such as a change in apparent velocity, contrast of the target with its background, or a change in apparent size. This produces a change in the detection rate of the observer, raising it to a level λ_2 after time T_1 . Similar changes occur throughout the course of the target's movement until it disappears from view. This case of abruptly changing detection rate is discussed for ther in Chapter 4, where data collected by Brown (1966) are used to estimate the detection rates, λ_1 (i = 1, 2, ...). A description of the experiment conducted by Brown to measure the detection times of observers in the field is given in Appendix A

In truth, the detection rate does not usually undergo the abrupt changes shown in Figure . . The changes are much more subtle and occur more frequency,

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so that the detection rate would more often appear as shown in Figure 3, where λ (τ) is a continuous function of time (depending on the movement trace of the target and/or the observer).



Fig. 3.--Hypothesized Form of the Conditional Detection Rate According to the Glimpse Model

It is obvious that any attempt to explain this phenomenon from observer detection-time data would be fruitless since an unwiedly sample size is necessary because of the high number of changes. For this reason a theoretical model of the conditional detection rate which is compatible with computer simulation requirements is developed which draws on an extensive review of the literature pertinent to visual detection. This model which combines elements of search and psychophysical data is of the form:

$$\lambda(\tau) = \mu p g(\bar{S}, \tau)$$
(1.0)

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where μ is the rate at which fixations (glimpses) are made by the observer, p is a constant which corrects for the number of forms in the scene which resemble the target (confusing forms), and g (S, τ) is the probability that the target is detected on a single glimpse, a function of a set environmental variables, S, and the time τ .

A model which predicts the single-glimpse detection probability, $g(S, \tau)$, developed in Chapter 3, draws heavily on the discussion of the pertinent literature on the detection phenomenon, discussed in Chapter 2. The model discussed in Chapter 3 predicts the single-glimpse detection probability based on the best evidence available to the writer.

In Chapter 3, environmental variables such as target and terrain reflectance and the position of the source illuminating the target and terrain are used to predict the luminance of the target and its surrounding. Contrast of the highlighted and shaded areas of the target with the background and foreground, respectively, are used in an expression for the single-glimpse detection probability of the target. To derive this expression several simplifying assumptions are necessary. These assumptions are made according to the evidence presented in the literature review (Chapter 2) and the judgment of the writer. With these assumptions data is available to permit derivation of the model. During the course of this thesis, it will become evident to the reader that additional basic data concerning the detection phenomenon are quite necessary. However, since only a limited amount of very basic data is available it must suffice for the development contained in Chapter 3. The development of a detection-time

model with continuous -time detection rate, hereafter called the "glimpse model" is presented in Chapter 4. The validity of the "glimpse model" is rather difficult to test because of the limitied capability to obtain dependable continuous physical measures of the quantities used in its development and an inability to approximate its time dependency with any great accuracy. For these reasons, the reader must digress a step and consider a model developed and tested for abrupt changes in the detection rate based on actual field data. The form of the detec tion rate from the glimpse model should be close to that of the abrupt-change model with minor fluctuations as shown in Figure 4.



Fig. 4.--Comparison of the Conditional Detection Rate for the Model Based on Field Data with that of the Glimpse Model.

Detection-time data are available from an experiment conducted by Brown (1966). From these data, it is possible to estimate the conditional detection rate in

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each of the time intervals used in the simplified probabilistic model. Moving pictures of the scenes used by Brown were available, so an attempt was made to investigate the correspondence between the glimpse model and the simplified model. However, it was impossible to measure all of the target scene variables necessary for complete validation. The method of validation and unsuccessful attempts to collect data from films are discussed at the end of Chapter 4.

Chapter 5 contains a discussion of the area of target detection research, with emphasis on the implications of the models contained in this thesis. As will be noticed from time to time, an extensive amount of additional data are needed to improve the resolution of the model. Some of these data needs are discussed in the final chapter.

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CHAPTER 2

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FACTORS AFFECTINC TARGET DETECTION

Light contains information of the nature of objects in the environment.

Structures or patierns of different intensities and compositions (such as margins,

texture, pattern, contour or form) evolute responses in the individual. The

geometric perspective of these clues are used to analyze information about the

environment.

The eye is an instrument exploring the environment employing pursuit,

compensatory and saccadic movements which produce a response to the environ-

ment. Vernon (1957) suggests that:

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"Perception is selective and is determined in accordance with the classification of incoming sensory data into organized categories of schemata, in which the sensory data are selected and combined systematically with the relevant cognitive data and tendencies to appropriate action." Furthermore, "Schemata are utilized to form hypotheses about the nature of the immediate situation. These hypotheses are tested by attempting to select from the incoming sensory data those which fit them. Data that do not fit may be ignored or rejected. If they are unusually vivid or persistant, the observer may take some active measures to check them and if necessary, to modify the hypotheses to accomodate them. If data are inadequate or ambiguous, the observer will perceive what his schemata lead him to expect. Where schemata are too broad or insensitive to afford perceptions that are accurate in every detail, they may be refined by perceptual learning."

Detection as discussed in Chapter 1 is a subclass of the phenomenon of perception discussed by Vernon. The task of the observer is to classify the object into a recognizable subset based on a known set of attributes. This classification system, inborn in the observer, is affected only by the physical appearance of the object. This chapter is denoted to a discussion of several recent experimental works, conducted both in the laboratory and the field, to identify some of these factors and quantify their influence on detection and identification performance. The following factors are explored in some detail:

1. Target Size

2. Target Shape

3. Confusing Forme

4. Eye Movements

5. Target-to-Background Contrast

6. Target Form

7. Target Motion

The effects of these factors are then used in Chapter 3 to predict the probability that a target in a natural terrain setting is detected on a single glimpse. Information in this chapter is again used in Chapter 4 to predict the couditional detection rate, λ (τ), discussed in Chapter 1.

Target Size

The effect of target size on detection has been investigated by several experimenters. It has been shown (Kincaid, <u>et al.</u>, 1960) that the probability of detecting a target increases as its apparent size to the observer increases. Target detection is discussed in terms of an "element contribution" theory of spatial summation which predicts that the threshold decreases as the target size increases. Steedman and Baker (1960) conducted an experiment to

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to determine how the ability of an observer to identify an object is affected by the ' size of the object in a complex abstract display. Targets were generated on a 90,000-cell matrix of confusing forms. After being shown a reproduction the target in the same orientation as it was to be seen, the subject was told to locate the target in the display containing the confusing forms. The major finding was that identification time was constant for targets above 12 minutes of arc, while performance deteriorated for targets below 12 minutes. Richardson (1962) measured the maximum sighting range for ships of various lengths at sea. Figure 5 shows the relationships between the range at which 50 percent of the observers detected the ship and the length of the ship. From this figure, it can be seen that larger targets (ships having greater length) are detected before the smaller targets (that is, at high target-to-observer ranges, large targets are naturally more detectable than small targets). In a study by Boynton and Bush (1955) it was shown that the probability of recognizing (identifying) a target form increases as the target-to-observer size increases regardless of the nature (shape) of the form. Fox (1956) investigated the effect of object size on both detection and recognition. Circles, irregular shapes, squares, triangles, crosses, and stars of three different sizes were presented to observers. It was shown that an increase in object size decreased the detection and recognition threshold and increased the frequency of correct identification.

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The results of these few experiments illustrate a rather intuitive notion about target detection ability. That is, the larger a target appears to the observer, the easier it is to detect and identify. However, a measure of this

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Fig. 5. -- Fifty Percent Sighting Range of a Ship At Sea Versus Length of Ship.

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target size is not so intuitive, since the shape of a target commonly encountered in a natural environment is very complex, presenting an infinite number of linear dimensions which might qualify as that measure which distates detectability. That measure of size most often used is the argular subtense of the target,² defined as (Wulfeck, et al., 1958);

"The angle subtended by an object of vision at the nodal point of the eye. The magnitude of this angle determines the size of the corresponding retinal image, irrespective of the size or distance of the object."

This definition can apply to any linear dimension of the target, be it the diameter of a circular target, the greatest linear dimension of a rectangular or complex target, or the perimeters of any shaped target (Harris, 1964). Most of the psychophysical data available on object detectability use the angle subtended by the diameter of a circular target as the measure of target size (Blackwell, 1946; Taylor, 1964). The use of these basic psychophysical data to predict the detectability of a complex target in a complex natural environment is discussed in Chapter 3.

Target Shape

Closely related to the size of the target is its shape or "form" apparent to the observer. Targets typically encountered in the field are complex threedimensional objects which, due to changes in surface orientation relative to the observer and the illuminating source (the sun, etc.), appear as a pattern of

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²Boynton and Bush (1957) investigated the differential effect of target size as opposed to observer to target distance on the probability of correct identification. For targets subtending the same visual angle, the percent correct recognition for the physically smaller targets was 32.1 percent, while the physically larger targets used to imulate the same distance were correctly identified only 27.0 percent of the time.

brightnesses which must be discerned by the observer as the object of interest. Most studies investigating target share have been performed with rather simple two-dimensional objects (circles, squares, rectangles, triangles, etc.) Smith (1961) measured the mean time required to identify variously shaped targets (triangles, squares, pentagons, and hexagons) from similar confusing forms (circies of the same area and contrast) in a circular display. Figure 6 shows the effect of target shape on the mean search time for four observers. From Figure 6 it is noted that as the number of sides the form has increases, so does the mean search time. This suggests that as the shape of the target approaches that of the other forms in the display, it is more difficult to identify or discriminate from these other forms. In the field situation, this would correspond to a target whose shape or form is altered by the use of camoflage to resemble elements of the terrain. The results of a study by Lamar, Hecht, Shlaer, and Hendley (1917) indicate that the ratio of the length of a rectangular target to its width significantly affects the ability of an observer to detect the object. As shown in Table 1, the contrast threshold 3 of the target increases with this ratio at two of the different levels of background luminance studied. In Table 1, it appears for targets of the same area threshold contrast is essentially constant when the ratio of length to width of the target is below seven. However, for targets of equal area having ratios of length to width above seven, the threshold contrast appears to increase.

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³Contrast threshold will be discussed later in this chapter.

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Target Shape (Number of Sides)



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TABLE 1

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RELATIONSHIP BETWEEN THRESHOLD CONTRAST AND TARGET AREA FOR RATIO, (L/W) OF LENGTH TO WIDTH OF A RECTANGULAR TARGET TAKEN FROM LAMAR, et al., 1947

Background Lumi- nance (ft. lamberts)	Target Area (min?)	$\frac{L}{W} = 2$	$\frac{L}{W} = 7$	$\frac{L}{W} = 20$	$\frac{L}{W} = 70$
2950	0.50 0.75 1.00 1.50 3.00 10.00 50.00 100.00 300.00 800.00	0.331 0.205 0.138 0.102 0.0582 0.0321 0.0167 0.0198 0.0166 0.0200	0.288 0.207 0.154 0.118 0.0662 0.0330 0.0167 0.0132 0.0132 0.0158	0.402 0.252 0.187 0.172 0.108 0.0445 0.0182 0.0141 0.0117 0.0109	0.631 0.470 0.322 0.278 0.166 0.0506 0.0226 0.0189
17.5	0.50 0 0.75 1.00 1.50 3.00 10.00 50.00 100.00 300.00 800.00	0.715 0.450 0.373 0.282 0.141 0.9594 0.0306 0.0244 0.0197 0.0195	0.850 0576 0.434 0.330 0.177 0.0716 0.0312 0.0237 0.0165 0.0162	1.020 0.750 0.553 0.465 0.228 0.115 0.0394 0.0266 0.0154 0.0141	1.540 1.240 0.911 0.702 0.382 0.161 0.0572 0.0408 - -

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Based on these results, the authors suggest that luminance around the edge of the target, not its area, dictates detectability. In a derivative study by Nachman (1953), verifying the results of Lamar, et al., it was found that targets which varied in area but were equal in the amount of useful edge had equal contrast thresholds, as hypothesized by Lamar and his colleagues.

In the experiment conducted by Fox (1956), discussed earlier, the shape (circle, irregular figure, square, triangle, cross and star) of the object did not affect the detection threshold for small targets. However, for larger size targets, shape did have a pronounced influence on the detection threshold. However, according to the results of Fox, shape did have significant effect on the identification threshold. The irregular figure and the cross had higher recognition thresholds than the circle, star, square and triangle. Based on his results, Fox suggests that complex, more unfamiliar forms are more difficult to identify than the simple, more familiar forms.

Zusne and Michels (1962a, 1962b) in an attempt to quantify target shape, asked subjects to rate several target shapes, on a point scale according to their regularity or familiarity. Bilaterally symmetrical shapes (squares, rectangles, diamonds, and parallelograms) were judged more familiar than asymmetrical shapes. It was also suggested that compactness as indicated by the ratio of perimeter t_{i} area and elongation (ratio of length to width) contributed significantly to familiarity of a shape, and consequently the ease with which it is identified by an observer.

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Kristofferson (1957) and Kincaid, et al., (1960) discuss detection in terms of an "element contribution" theory which predicts that for equal area, all non-circular targets should have higher contrast thresholds 50 percent level than circular ones. Data are presented which indicate that circles have the lowest contrast threshold followed by simple geometric forms (squares, trungles, stars, etc.), and long thin rectangles.

Kristofferson and Blackwell (1957) measured the contrast threshold for circles, squares, rectangles, crosses, and several other regular target shapes in a uniform background. Circular targets were found to have the lowest contrast threshold, while the contrast threshold of rectangles increases as the ratio of length to width increased. This result agrees fairly with the results of Lamar, Hecht, Shlaer, and Hendley (1947) discussed earlier in this chapter. Based on their results, Kristofferson and Blackwell (1957) conclude that geometrical forms (squares, crosses, stars, etc.), which were equal in area to a 32 minute diameter circle, had approximately the same contrast threshold as the circle. Thus, for targets of this size, target shape has very little effect on detectability, and can be neglected. Duntley (1964) generalizes the relative importance of size to shape by stating that the "..., shape of an object is of minor consequence compared with the effect of angular size". The effect of having forms in the display which resemble the target both in size and shape is discussed in the following section.

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Confusing Forms

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Objects other than the target in the area in which an observor is searching can compete for his attention because they closely resemble the target. In a natural scene these similar forms are almost impossible to isolate and enumerate since it is not known how the eye processes information contained in a visual stimulus. Any number of light and dark spots in the scene, while not really resembling the target, attract the observers attention and affect his ability to successfully detect and identify the object of interest. In an attempt to quantify the effect of conflicting search cues on search behavior, experimenters (Smith, 1961; Boynton and Bush, 1957) have placed a target whose configuration is known to the observer in a field of similar geometric forms, and required to subject to correctly discriminate the true target form from the confusing forms.

Boynton and Bush (1957) investigated the ability of observers to correctly identify a known geometric form presented in a display containing similar struniforms (confusing forms) having curved edges. The contrast of the forms with the background, the number and size of the confusing forms, and the time that the display was exposed to the subject were varied. Exposure times of 3, 6, 12 and 24 seconds were used and the number of confusing forms was either 8, 16, 32, 64, 128, 256, 512 or 1024. Target to background contrasts of -1.00, -.85, -.67, -.44, and -.18 were used. To reduce false detections, a reward was given the subject for a correct response to a target presentation. A reward (motivating) level was discovered which resulted in approximately 5 percent of the detections being false.

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Figure 7 shows the probability that the target was correctly identified from the confusing forms as a function of the exposure time and the total number of forms in the display, averaged over all target-to-background contrasts.

Smith (1961) also suggests that search time depends on the number of objects in the display and the similarity between the object of interest and the false targets. Smith used a regular polygon (triangle, square, pentagon, and hexagon) as the target and circles of equal area and contrast as the confusing forms. To minimize false detections, after each trial, the sheet upon which responses were scoredwas marked incorrect or correct. On this score sheet was a circular display upon which the approximate location of the target was marked. Pay was contingent on speed and accuracy of response. A report of performance was given after each display presentation. Errors or false detections were penalized whenever they occurred-most severely during early sessions, less severely during later ones.

The time required for an observer to successfully locate the target was measured as a function of the number of forms in the display. Figure 8 shows the results obtained by Smith for square targets contained in a display of circular false targets. He suggests that the equation,

$$\log t = m \log N + n \tag{2.1}$$

where m is the slope, n is the intercept N is the number of confusing forms, and t is the time required to correctly identify the target, explains observer performance. In the same experiment, Smith varied the difference between the

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size of target and false target and the contrast of the target and false target with the background. Figure 9 shows the time required to locate a square target in a display containing 256 false (circular) targets as a function of target-false target percent size and contrast difference. Percent contrast difference is defined as the ratio of the target to pseudotarget contrast multiplied by 100. If C_T is the contrast of the target with the background and C_{PT} is the contrast of the pseudotarget with the background the percent contrast difference, \overline{C} is:

$$\overline{C} = \frac{C_T}{C_{PT}} (100) .$$
 (2.2)

Percent size difference is defined as the ratio of the area of the target to the area of the pseudotarget multiplied by 100. If A_T is the area of the target and A_{PT} is the area of the pseudotarget, the percent size difference, \overline{A} , is

$$\overline{A} = \frac{A_T}{A_{PT}} \quad (100) \quad . \tag{2.3}$$

From Figure 9, it can be seen that search time increases as the size and contrast of the false targets approaches the size and contrast of the true target.

These studies indicate that increasing the number of competing stimuli in a display degrades the ability of an observer to successfully locate a target. While the forms used by Smith and Boynton and Bush were easily countable due to the carefully controlled nature of the laboratory experiments, there is no existing methodology for locating such forms in a natural scene. Since, confusing forms in a natural scene will undoubtedly vary within each scene

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Fig. 9.--Mean Search Time as a Function of Target-Confusing Form Size and Contrast Difference Taken from Smith (1961).

from the target in size, contrast, and shape, making them impossible to isolate, some other interpretation of competing stimuli must be made. A measure of competing stimuli, which is still measured subjectively but is somewhat easier to verify, is discussed in Chapter 4.

Eye Movements

The way the observer looks for a target affects his ability to successfully locate the target. Many techniques have been devised for recording the movement of the eye as it searches a display. These methods are described in Alpern (1962).

When an observer is performing a search task, the eyes do not scan smoothly over the area of search responsibility, but sporadically in a series of jumps called "saocadic" movements (Smith and Semmelroth), 1961), separated by brief pauses called "fixations" (Ford, <u>et al.</u>, 1959). For all practical purposes, these fixational pauses are the only periods during which detection can occur (White, 1964), and consequently are of most importance. These fixational pauses are often referred to a "glimpses" at the object of interest. Smith and Semmelroth (1961) suggest that peripheral vision plays a major role in visual search:

"... the eyes usually move <u>balligtically</u> from one quite clearly defined object or element in the display to another such element, i.e., the path of the movement and the stopping point are determined before movement begins. For this to occur, the object of each succeeding fixation must be perceived peripherally before it is perceived forially." 27

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The duration of the fixational pause and ballistic movement, measured under several different conditions, is discussed below.

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Ford. White and Lichtenstein (1959) suggest that when the observer is looking for an object in a relatively homogeneous field, the average duration of the fixation is about 0.27 second, with none less than 0.10 second. Due to the time taken by the saccadic movements, several investigators (e.g., White, 1964; Ryll, 1962) suggest that 3 fixations can be expected each second under free search situations. However, as the scene becomes more complex (as more forms compete for attention), the average duration of the fixation decreases. Townsend, Enoch and Fry (1958) measured the fixation duration of an observer searching a display with varying complexity. Complexity was reduced by passing opaque filters of several densities between the display and the observer. Their results suggest that a smaller area per unit of search time is covered for the complex scenes (those scenes unblurred). It is also suggested that the average duration of the eye fixation increases as the overall contrast of the scene is reduced and the average extent of individual eye movements decreases as the overall contrast is reduced as a result of blurring by the opaque filter. The effect of scene complexity defined as the relative amount of blur present in the scene, on fixation duration, as suggested by Townsend, Enoch, and Fry is given

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addition in the second

⁴Blur is a measure of edge definition and distortion and is not necessarily completely described by a contrast measurement. Targets of equal contrast in displays with different degrees of blur are not equally detectable.
in Figure 10. From Figure 10, it appears that the duration of the fixation is fairly constant at 0.25 for the unblurred and slightly blurred displays and increases rapidly as the complexity of the scene decreases. These results would suggest that fog, haze, and smoke would not only affect single-glimpse detection probability (the probability of detection on a single fixation pause) in the field by degrading target contrast, but will increase search time by increasing the average duration of a fixation.

The effect of display size on the fixation duration has been investigated by Enoch and Fry (1958). The results of this study given in Figure 11, indicate that the fixation duration is fairly constant (0.35 second) for display subtending a visual angle greater than 10 degrees. However, as the size of the display decreases (below 10°), the duration of the fixation increases at an increasing rate. The results discussed in this section indicate that a glimpse duration of approximately 1/3 second is appropriate for essentially all search conditions in the field except extreme conditions of fog, haze, or smoke. In the following section the probability of detecting a simple cir⁻⁻ lar target as a function of its contrast with its surroundings during one fixation (glimpse) is discussed.

Target-to-Background Contrast

The apparent contrast, C, of a target is defined in psychophysical terms as the ratio of the difference between the brightness of the target, B_t , and its surroundings, B_g , to the brightness of the surroundings (Blackwell, 1946); i.e.,

$$C = \frac{B_t - B_s}{B_s}$$
, (2.4)

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where B_t and B_s are brightnesses as seen at the observer's position. Being the result of a sensation, brightness is not measurable. However, the luminance of the background and foreground, the physical counterparts of brightness, are used to calculate inherent brightness contrast. The inherent contrast of the target C_o , is defined as:

$$C_0 = \frac{L_0 - L_s}{L_s}$$
, (2.5)

where L_0 is the luminance at a point on the object and L_s is the luminance at a point on the surface surrounding the object, both measured at the target. The apparent contrast C, is that contrast autually seen by the observer. It is usually less than C_0 because the particles in the atmosphere between the observer and target attenuate some of the contrast by scattering and absorbtion. This degradation in contrast, which is a function of the atmospheric conditions (fog, smoke, haze, etc.) and the target-to-observer range, is discussed in Chapter 3.

In the detection literature, the contrast that is usually mentioned is that apparent contrast which results in a 50 percent probability of detection. This is known as the threshold contrast, C_t . Blackwell (1946) conducted an extensive study to determine the effect of target size and background brightness on the contrast threshold of targets exposed to the observer for 1/3 second. Taylor, (1960a, 1960b) extended Blackwell's work to larger targets. Their data, shown in Figure 12 apply only to circular targets viewed against a background of uniform luminance.



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TABLE 2

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CONTRAST THRESHOLD FOR DIFFERENT SIZE TARGETS AS A FUNCTION OF THE ANGULAR DISTANCE OF THE TARGET FROM THE FIXATION DIRECTION ACCORDING TO TAYLOR (1961)

Degrees from fix- ation direction	Target Size (minutes of arc)				
	100	1.74	3,69	15.0	120.0
0	0.539	0.196	0.0488	0.0162	0.0078
1,25	0.772	-	0.0793	0.0214	0.00921
2.50	1.39	0.386	0.0960	0.0240	-
5.00	2.75	3.786	0.218	0.0356	0.0121
7.50	3.72	1.03	0.278	0.0465	0.0127
10.00	4.55	1,48	0.333	0.0657	0.0135
12.00	5.73	1.69	0.545	0.0725	0.0154

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where σ is the standard deviation of the normal ogive. Dividing the numerator and denominator of the argument of Φ in equation 2.7 by the contrast threshold, the single-glimpse detection probability, g, becomes:

$$\mathbf{g} = \mathbf{*} \left\{ \frac{\mathbf{C}/\mathbf{C}_{\mathbf{t}}^{-1}}{\mathbf{\alpha}/\mathbf{C}_{\mathbf{t}}} \right\}$$
(2.8)

Blackwell (1963) suggests that the ratio σ/C_t in equation 2.8, remains constant regardless of the time the target is exposed, the size of the target, and the background luminance. Data presented in Elackwell (1963) are disoussed below to illustrate the effect of target-scene variables (stimulus conditions) on the ratio σ/C_t .

Effect of Target-Scene Variables on the Ratio σ/C_t

The effect of target size, target shape, and background luminance (adaption brightness) on the ratio σ/C_t has been studied by several experimenters (Black-well, 1963). Results from experiments discussed in Blackwell (1963) illustrating the effect of target-scene variables on σ/C_t are discussed in the following three sections.

Background Luminance

Data given in Blackwell (1963), taken from a study by Blackwell and I aw (1958) indicate that the ratio σ/C_t increases as the background luminance decreases. For a constant exposure time of 0.01 second i and target diameters of one to 45 minutes of arc, the ratio σ/C_t varied as shown in Figure 13.

Taylor (1961) suggests that the contrast threshold changes with the retinal position of the object in the field of view. The results of this study, given in Table 2, indicate that the threshold contrast increases as the location of the target from the point of fixation increases. This implies that the probability of detecting a target in the periphery is less than the probability of detecting the same target when the fixation is located directly on the target.

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Blackwell (1946) and Duntley (1964) demonstrate that for these simple (circular) targets of uniform luminance viewed against backgrounds of uniform iuminance, targets of equal contrast brighter and darker than their background are equal in detectability. It is customary to refer to targets brighter than their background as having positive contrast, and targets darker than their background as having a negative contrast. Most often the sign of the apparent contrast is ignored (Duntley, 1964), so that equation 2.4 becomes

$$C_{0} = \begin{vmatrix} B_{t} - B_{s} \\ B_{s} \end{vmatrix} , \qquad (2.6)$$

where $\frac{B_t - B_s}{B_s}$ is the absolute value of the quantity $\frac{B_t - B_s}{B_s}$

Blackwell (1963) suggests that the detection probability of a circular object with apparent contrast, C, is given by

$$\mathbf{g} = \mathbf{\tilde{g}} \left(\frac{\mathbf{C} - \mathbf{C}_{\mathbf{t}}}{\sigma} \right)$$
 (3.7)

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From Figure 13, it appears that the ratio σ/C_t is a constant 0.44 at low background luminance and decreases as background luminances increases (above 1 foot candle).

Target Size

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Blackwell (1963) also demonstrates the effect of target size on the ratio. Data taken from experiments by Blackwell and Austin (1952) and Kristofferson and Blackwell (1958) is given in Table 3. From Table 3, it can be seen that the ratic σ/C_t for targets of varying size viewed for 0.001 second at zero background intensity varies without pattern between 0.308 and 0.402. These data, taken from Blackwell and Austin (1952), indicate that target size has a random effect on the ratio at this background luminance and exposure time. The data given in the second column of Table 3 also illustrate this random effect. These data, taken from Kristofferson and Blackwell (1968), are for a background luminance of 10 foot-lamberts and exposure duration of 0.01 second. Target Shape

Data given in Blackwell (1963) indicate that the ratio σ/C_t remains essentially constant for different target shapes. Ratios of c/C_t are given for circles, rectangles, and complex forms. These data, reproduced in Table 4, are taken from studies by Kristofferson and Blackwell (1968) and Blackwell and Smith (1959). Target sizes, exposure times, and background luminance were different for the two studies. From Table 4, it can be seen that target shape (for those shapes studied) has little effect on the ratio. The data also indicate, as did the data of Figure 13, that the ratio σ/C_t increases as background

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TABLE 3

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EFFECT OF TARGET SIZE ON THE RATIO σ/C_t AS GIVEN IN BLACKWELL (1963)

Target Diameter (min.)	From Blackwell and Austin (1952) σ/C_t σ/C_t	From Kristofferson and Blackwell (1958 σ/C_t	
64	0.367	0.285	
32	0.402	0.338	
16	0.308	\$-308	
8	0.372	0.330	
4	0.372	0.340	
2	0.311	0.308	
1	0.345	0.345	
	MEAN = 0.354	MEAN = 0.322	
Exposure time	0.001 second	0.01 second	
Background Luminance	zero	10 foot-lamberts	

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TABLE 4

EFFECT OF TARGET SHAPE ON THE RATIO J/Ct AS GIVEN IN BLACKWELL (1963)

Shape	From Kristofferson and Blackwell (1968) o/C _t	From Kristofferson and Smith (1959) σ/C_t	
Circles	. 323	. 537	
Rectangles	. 303	. 547	
Complex Forms	. 289	.484	
L	MEAN = 0. 3 05	MEAN = 0.519	
Exposure Time	0.01 second	0.01 second	

Background Luminance 10 foot-lamberts sero

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luminance decreases for constant exposure time for targets having shapes other than circular.

The effect of randomized target sizes, exposure times, and background luminance on the ratio σ/C_t was investigated by Blackwell and McCready (1958). Data given by Blackwell and McCready, reproduced in Table 5, indicate that a typical value of σ/C_t of 0.390 can be used for most stimulus conditions of interest. These data are based on 80,000 observations obtained from four observers.

Examination of the data presented in Blackwell (1963) suggests that the ratio σ/C_t varies very little over all the stimulus conditions investigated. Blackwell calculated the ratio of σ/C_t for 36 observers, representing over one million data points. The values of σ/C_t for these 36 observers are given in Table 6, taken from Blackwell (1963). These observations taken from muner-ous authors represent the measurements of σ/C_t for almost any conceivable combination of stimulus conditions. From Table 6, it appears that σ/C_t varies randomly between 0.314 and 0.584. A X^2 - goodness of fit test performed on the data given in Table 6 showed that the hypothesis that the data comes from a uniform distribution of the form;

$$f\left(\frac{\sigma}{C_{t}}\right) = \frac{1}{b-a}$$
(2.9)

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where,

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could not be rejected at the . 05 level.

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TABLE 5

VALUES OF G/C, DETERMINED BY BLACKWELL AND MCCREADY (1958) FOR SEVERAL TARGET SIZES, BACKGROUND LUMINANCES, AND EXPOSURE TIMES. WITHIN EACH CATEGORY, THE OTHER TWO VARIABLES ARE CONFOUNDED WITHIN THE VARIABLE OF INTEREST

Diamter of Target (min)	o,ct	Background Lumi- nance(foot-lamberts)	σ/C _t	Exposure Time(sec)	σ/C _t
51.4	0.384	160	0. 357	1.0	0.467
12.8	0.397	10	. 0.382	• 0.1	0.370
3.21	0.418	1	0. 39 8	0.01	0.358
0.802	0.367	0.1 0 ;	0.420 0.420 0.419	0.001	0.333

GRAND MEAN=0.390

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TABLE 6

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VALUES OF σ/C_1 FOR 36 OBSERVERS AS GIVEN BY BLACKWELL (1963) SUMMARIZED OVER SEVERAL ENVIRONMENTAL CONDITION

Observer Number	σ/C _t	Observer Number	₀/C _t
1	0.420	19	0.320
2	0.479	20	0.470
3	0.418	21	0.556
4	0.446	23	0.550
5	0.467	23	0.392
6	0.491	· 24	0.491
7	0.467	25	0.456
8	0.463	26	0.584
9	0.546	27	0.519
10	0.370	28	0.400
11	0.434	29	0.409
12	0.411	30	0.467
13	0.430	31	0.429
14	0.424	33	0.480
15	0.368	33	0.390
18	0.396	34	0.347
17	0.360	35	0,314
18	0.352	36	0.396
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Maximum-likelihood estimates of the mean and variance of the distribution of σ/C_t were calculated. It was found that the mean of the sample shown in Table 6 is 0.434 and the variance is 0.0061. Using a value, $(\sigma/C_t)^*$, of σ/C_t sampled from the uniform distribution given in equation 6, the probability, g, of detecting the target on a single glimpse becomes:

$$\mathbf{g} = \mathbf{\Phi} \left(\frac{\mathbf{C}/\mathbf{C}_{t} - 1}{\left(\sigma/\mathbf{C}_{t} \right)^{*}} \right)$$
(2.10)

Equation 2.10 now represents the single-glimpse detection probability for any observer, based on a sample of 36 observers, supposedly chosen at random from the universe of observers and stimulus conditions. For the <u>average</u> observer, under randomized stimulus conditions, equation 2.10 reduces to:

$$g = \bar{*} \left(\frac{C/C_t - 1}{.434} \right)$$
 (2.11)

In equation 2.11, the contrast threshold, C_t , was taken under the most ideal laboratory conditions, that is, i.e., all stimulus conditions were carefully controlled. Subjects in the laboratory were told precisely where and when the stimulus was to appear, and were well practiced in the detection task (each observer had detected several thousand such targets). Several investigators (Taylor, 1964; Blackwell, 1958; Blackwell, 1967) have suggested that C_t be multiplied by a constant, K, so that it applies to field conditions. This multiplicative constant, often referred to as the field factor, is given by Taylor (1964) ar.

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$$\mathbf{K} \stackrel{=}{=} \frac{\mathbf{n}}{\prod_{i=1}^{n}} \mathbf{k}_{i}, \qquad (2.1)$$

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where the k_i (i = 1, ..., n) are the multiplicative constants causing the respective difference i (i = 1, ..., n) between laboratory and field conditions. Blackwell (1958) suggests the use of three such k_i as follows:

- 1 = 1.09, to correct for lack of knowledge of target
 size and duration of appearance,
- $k_2 = 1.31$, to correct for observer uncertainty about where the target is to appear, and
- k₃ = 2.40, correction made when necessary to adjust forced-choice data to yes-no detection data.⁵

Taylor (1964) suggests an additional factor, $k_4 = 1.90$, which corrects the contrast threshold for the difference between trained and naive observers. When all four of these conditions apply, equation 2.12 becomes:

$$K = \frac{4}{11}$$
 k, (2.13)
i=1 i ,

which reduces to

$$\mathbf{K} = \mathbf{6.5}.$$

With a total field factor K = 6.5, equation 2.10 corrected for four differences between laboratory and field conditions becomes:⁶

$$g = \bar{\Phi} \left\{ \frac{C/6.5(C_{1}) - 1}{.434} \right\}$$
 (2.14)

⁵A comparison of these types of data collection is given in Lawson(1958).

In this expression, it is assumed that the ratio, σ/C_t , where C_t is the contrast threshold under field consitions, and σ is the standard deviation of the mormal 0 give in the field, remains constant at 0.434.

No additional field factors, k_i (i - 5, ..., n), have been discovered after an extensive review of the current literature. However, it is conceivable that some or all of the following factors might contribute to a degradation in field performance which would be reflected through the inclusion of additional field factors in equation 2. 14;

- 1. Presence of similar forms in the background(confusing forms),
- 2. Other sensory clugs present in the natural environment,
- 3. Geometric form of the target (complex as egposed to simple circular targets),
- 4. Light scattering causing the image to blur, and
- 5. Spectral and spacial distribution of light on the target's surface (highlights and shadows).

Bis skwell and Bixel (1963) investigated the effect of a complex nonuniform background on the contrast threshold of a circular target. Three non-uniform backgrounds were used with targets of various size, luminance and location in the background. Two of the backgrounds were formed from ball bearnings while the third was a torrain photograph. In general, it was found

"... when the background luminance varied within the area occupied by the target, it was the target contrast with the luminance at its border which determined target visibility."

This implies that the detectability of an object located anywhere in a complex display having non-uniform luminance is governed at least in part by $\frac{9}{2}$, its contrast with its immediate surroundings, not its contrast with its immediate surroundings, not its contrast with $\frac{1}{2} = \frac{1}{2} \frac{2}{2} \frac{2}{2} \frac{1}{2} \frac{1}{$

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The use of contrast threshold, discussed in this section, to predict object detectability is discussed in Chapter 3. In Chapter 3 the object is represented as a simple variously oriented three-dimensional object (sphere) so that the image formed by contrasting the object with its surroundings can be described without great difficulty.

Target Form

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As evidenced in the preceding discussions, the vast majority of basic detection and recognition data has been obtained using simple (most often circular) targets of uniform luminance. This type of target is adequately described by specifying the contrast of the target with its background and its angular size (Blackwell, 1946). However, under most field conditions, the target is not simple in shape nor does it have uniform luminance. In such cases, shadows and highlights within an object are strong clues for detection and recognition. Therefore, with the large number of ways in which the rays from the illuminating source strike the variously oriented surfaces of the target, there are a correspondingly infinite number of sizes, shapes, and patterns an ebject can present to an observer.

Kause (1965) expanded on the difficulty of describing this image when he stated that,

"Complex photographic, high-resolution radar, infrared, or electro-optical images have been the stimuli in many psychological studies of target recognition and photo-interpretation. The comparison or generalization of the results of these studies has been almost impossible because no adequate, objective definition or description of these stimuli has been possible. An

objective and quantitative measure of the structure of an image would make this comparison and generalization possible and would allow the determination of the relative importance of image complexity in target identification."

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For the purpose of this study, no attempt will be made to accurately describe the form of the target which acts as a stimulus for detection, but several of the important characteristics of a patterned target-background complex are discussed below.

The ability of an observer to disoriminate this patterned target from elemants of the terrain in a natural scane has been the subject of considerable research in recent years (Wulfeck and Taylor, 1961). The pattern of luminances which the target presents to the observer must be recognized as the object of interest or detection and subsequent recognition by the observer will not occur. The difficulty with predicting the ability of an observer to successfully discriminate the target is to isolate the stimuli which initiate the detection and identification response. Morris (1959) studied the effect of this "target pattern" on detection and identification. Morris states that a target is patterned;

"... If it has distinguishable areas of various size and reflectance, such that, as a whole, the target cannot be brought to zero contrast within a uniform background through adjustment of target illumination."

This definition fits targets commonly encountered in a natural terrain scene, in that the pattern of luminances created on the surface of the target and its surroundings presents an infinite number of contrasts to the observer. Morris also states that "the discernable elements in the patterned target may be considered as

several independent targets simultaneously viewed, each with its own detection

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range." This fact is used in Chapter 3 to estimate the single-glimpse probability of the target, where areas of different luminance formed on a simplified representation of the target are treated as independent objects when contrasted with elements of the terrain and the target itself.

The relationship between complexity, recognition, and the number of forms competing for the subject's attention was investigated by Deese (1956). Simple several-sided two-dimensional targets were constructed using:

1. Right angles (regular forms), and

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1. Obtuse and soute angles (irregular forms).

The measure of complexity was the number of angles present in the form (target). That is, a simple form had fewer angles present. The background against which the targets were silouetted were of uniform luminance. The study was conducted with three levels of background luminance. A pay scheme was used to motivate the subject to avoid false detections. The subject was severely penalized each time an incorrect response was made. This minimized the number of false detections which had to be eliminated from the data analysis. The results of the experiment showed that:

- 1. For the regular forms, there were more recognition errors with the simple forms than with the complex ones, but the time required to recognize the target was slightly longer for the complex figures.
- 2. For the irregular forms, there was no difference in frequency of error between the simple and complex targets, but the time required to recognize the target was longer for the complex figures.

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These results indicate that as the number of abrupt changes in the outside surfaces of a target form increases, the time required to correctly identify the form increases, regardless of the nature of these changes. Under field conditions, this suggests that a target having subtle changes in contour (such as camoflage or shading) would be more difficult to identify than a simple uniformluminance target.

Image Characteristics

The quality and content of the image seen by the observer greatly effect his ability to successfully detect or identify objects of interest on an artifical laboratory display or in a natural environment. Rhodes (1964) attempted to relate selected psychologically meaningful variables taken from aerial reconnaissance photographs to the difficulty observers had identifying targets in the photographs. In this study, 200 photographs were first rated by 35 photointerpreters on an arbitrary scale between one and ten according to their "difficulty". These 200 photographs were then divided into two groups of 100 each having equal difficulty as measured by the arbitrary scale of the raters who screened them. Typical target types contained in the photos were:

- 1. Bridge,
- 2. Storage tank(s),
- 3. Plane(s),
- 4. Dam,
- 5. Roundhouse,

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6. Ship(s),

7. Building(s), and

8. Others

The experiment was divided into two phases. In phase one, 20 subjects were required to detect and identify targets of various shapes and sizes from each of 100 photographs after they had examined a 7/16" reproduction of it. In the other phase, 20 other subjects were asked to rate the same 100 images on a scale from one to seven according to how strongly they felt the image had the following subjective characteristics:

- a. Frequency of occurrence in the picture of objects that could be confused with the target.
- b. Distinctiveness of the target shape, that is, how much the target stands out because of its shape.
- c. Amount and variety of picture detail.

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- d. Distinctiveness of the target contrasts, i.e., how much the target stands out because of its lightness or darkness.
- e. Size of target relative to size of other objects in the picture.
- f. Freedom of target location, that is, the extent to which the nature of the target allows it to be located anywhere in picture (e.g., building has more freedom than bridge).
- g. Homogeneity of picture content (excluding target).
- h. Overall picture contrast, that is, the range of black-white gradation.

 7 The 7/16" size was used since it was approximately the average size of all objects viewed by the subject. This size reproduction was shown to all subjects. It was felt that a reproduction of exactly the same size would aid the subjects too much.

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- i. Isolation of the target from background.
- j. Distinctiveness of the target pattern, that is, how much the target stands out because of arrangement, detail and texture of its elements.
- k. Sharpness or clarity of picture detail.
- 1. Distinctiveness of target size, that is, how much the target stands out because of its size.

In addition to these twelve subjective measures of the difficulty of the image the physical size in centimeters (m) and distance of the target from the display center (in centimeters) (n) were measured.

Following the collection of phase-one and two data for the first set of 100 photographs, the roles of the two sets of subjects were reversed, that is, the 20 subjects who subjectively rated the first group of 100 photos, participated in the detection phase for the second group of 100 photographs and those 20 subjects who detected from the first group rated for the second group. Subjects consisted of 20 trained photo-interpreters and untrained 20 college students.⁸

Rhodes then attempted to relate the 14 measures (a, \ldots, n) of the images content and quality mentioned previously to:

- 1. The time required to detect and identify the target (T), and
- 2. The difficulty scale of the photograph obtained while the photos were being screened (D).

⁸Ten each of the photo-interpreters and college students were assigned to each group.

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Linear multiple regressions (Hogg and Craig, 1960) of the form

$$T = \alpha_0 + \alpha_a (a) + \alpha_b (b) + ... + \alpha_n (n) ,$$
 (2.15)

and

$$D = \alpha'_{0} + \alpha'_{a} (a) + \alpha'_{b} (b) + \dots + \alpha'_{n} (n) , \qquad (2.16)$$

where a_0, \ldots, a_n and a'_0, \ldots, a'_n are constants determined from the values of the variables T, D, a, b, c, d, e, f, g, h, i, j, k, l, m, and n, were performed on the data for the different sets of subjects. The regressions shown in equations 2.15 and 2.16 given by Rhodes did not necessarily include the effects of all of the 14 variables a, ..., n_i since some of the constants a_n, \ldots, a_n were forced to be zero to see whether they were significant in predicting either T or D. Multiple correlation coefficients for 16 such relationships given by Rhodes ranged from 0.73 to 0.90, meaning that up to 81 percent of the variability in the data was explained by these 14 variables.

The results of this experiment indicate that any or all of the measures incorporated by Rhodes affect the detection time of targets in a photographic display. It is quite clear that the targets contained in these photographs are not physically similar to those contained in the films of Brown (See Appendix A), not only because of differences in viewing angle and target type, but because of target motion in the films of Brown. However, it is felt that the characteristics presented here as quantified by Rhodes represent a good summary of the factors in any natural target scene which dictate detectability of any object.

Target Motion

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Movement of the target across the field of view was shown by Brown (1966) to be a significant variable affecting detection time. Due to the great changes in the scene carried by motion of the target, it is an obvious clue. It would be hypothesized that these same differences are caused by changes in the terrain against which the target is silouetted, changing the apparent contrast discussed earlier in this chapter. This hypothesis is discussed in Chapter 4, Because this contrast changes continually for a moving target in a natural scene, target motion is readily discernable to the observer. The effect of the target erossing velocity on detectability is considered as a variable affecting detection performance in Chapter 4.

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Conclusions

In this chapter, basic laboratory and field experiments conducted over the past four decades have been discussed. Data from these experiments, when examined as a whole, give clues to the detection of objects in a complex environment, although each individual piece may apply to only one specialized segment of the entire problem. Using the experience and intuition of the author, these data are incorporated in a model in Chapter 4 to predict the probability that a complex target is detected in a natural environment. However, it must be remembered that even with the complex development which is to follow, the phenomenon of field detection has been simplified to the point that it may no longer be valid. Since other attempts to do the same have resulted in conflicting results, this must be regarded as simple another attempt. This philosophical problem will be discussed in detail in Chapter 5 of this thesis.

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CHAPTER 3

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TARGET CONTRAST

Introduction

A combat vehicle in a natural terrain setting will present a complex luminance pattern to an observer. Contrast varies continuously along the edge and across the face (internal surface) of such targets. That is, military targets are not usually characterized by a single value of contrast as are the simple forms used in laboratory experiments to generate relationships, such as those in Figure 12 of Chapter 2, for predicting the single-glimpse detection probability. Data on the single-glimpse detection probability for complex contrast patterns are not available. Certain assumptions can be made, however, so that the relationships of Chapter 2 can be applied to estimate the single-glimpse detection probability for military vehicles in natural terrain settings. These assumptions are based on the best evidence available to the author on the detection of objects under natural (field) conditions as opposed to artifical (laboratory) conditions. Since no significant work on the detection of natural objects in complex surroundings is in evidence, the authors intuition has played a major role in the development of this chapter. The simplifications and assumptions which have been imposed were necessary to prevent the problem from growing without bound. Since the mechanisms by which visual information is integrated

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into perception are not completely understood, the major results from Chapter 2 serve as a framework for a model of glimpse probability to be developed in this chapter. Following the development of the glimpse model, Chapter 4 will be devoted to a discussion of a model of detection probability based on this glimpse model. In addition, a means of testing the validity of the model based on detection-time data will be discussed.

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In this chapter, the target is represented as a simplified threedimensional form. The sizes of the highlighted and shaded areas of this target representation are related to the position of the illuminating source and the observer. Then, a method is presented for predicting the contrasts that the highlighted and shaded areas have with each other and with the background and foreground, respectively. This method is based on reflectance data collected for common background features (trees, grass, etc.) and for materials similar to tank armor. Each highlighted and shaded area is regarded as a separate visual stimulus. Methods for determining contrast thresholds and glimpse probabilities for each area are proposed. Next, a theoretical relationship is presented relating the different glimpse probabilities to one representative glimpse probability for the target.



Determination of Apparent Contrast

The inherent contrast, C_o, of a point source, P, is defined as

$$C_{0} = \frac{L_{p} - L_{B}}{L_{B}}$$
, (3.1)

where L_p is the luminance of the point and L_B is the luminance of the area surrounding that point, i.e., its background. Both luminances are measured at zero distance from the point. If the point and its background are on the same surface, C_0 , as given by 3.1, would be referred to as inherent internal contrast. That is, the inherent internal contrast, C_0 , between any two points within the target with luminance L_1 and L_2 , respectively, is defined as:

$$C_{0} = \begin{cases} \frac{L_{1} - L_{2}}{L_{2}} & L_{1} > L_{2} \\ 0 & L_{1} = L_{2} \\ \frac{L_{2} - L_{1}}{L_{1}} & L_{2} < L_{1} \end{cases}$$
(3.2)

The inherent contrast of a point within a homogeneously illuminated flatsurface target would usually be zero since its background would be part of the same target. Thus, it is common to speak of inherent edge contrast, C_{E_0} , as (Duntley, 1964)

$$C_{E_0} = \frac{L_E - L_B}{L_B}$$
, (3.3)

where L_E is the luminance of a point on the edge of the target and L_B is the luminance of the background directly behind this point (along the observer's line of sight) both measured at the target. When the target and its background both have uniform luminances, edge contrast is identical to the contrast of an internal point with the background. Thus, the distinction between edge contrast and internal contrast is usually not made for such situations.

The apparent contrast, C, of an object is related to its inherent contrast, C_o, by (Middleton, 1968),

$$C = C_0 e^{-\sigma R} , \qquad (3.4)$$

where R is the target-to-observer range in meters, $\sigma = \frac{3.912}{R^*}$ is the attenuation coefficient of the intervening media, and R^* is the meteorological range in meters. Meteorological Range (Also called the standard visibility or standard visual range) is defined by Dudel (1967) as

"...an empirically consistant measure of the visual range of a target; a concept developed to eliminate from consideration the threshold contrast and adaption luminance, both of which vary from observer to observer. The meteorological range is the distance V in the block target form of the visual range formula,

 $\mathbf{V} = \frac{1}{\sigma} \ln \frac{1}{\epsilon}$

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Since the threshold contrast, , is set equal to 0.02, \forall is only a function of 0, the extinction coefficient of the atmosphere at the time and place in question."

Records of the variation in metsorological range, $\mathbb{R}^{*}_{,i}$ by hour of the day and month of the year for a given area can usually be obtained from local weather stations. A sample of such records for a German weather station is given in Appendix A.

Irregularities in the surface of military vehicles cause the target to have a multitude of inherent contrasts for any particular level of illumination. In the following section, the target is represented as a simple three dimensional form so that variations in inherent contrast across its surface can be predicted.

Simplified Vehicle Representation

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Both combat vehicles and their backgrounds are far from being of uniform luminance. The pattern of luminances presented to an observer is complex and, for practical purposes, unpredictable. Duntley, (1964), states that:

"The shape of an object is ordinarily of minor consequence composed with the effect of its angular size."

Based on this fact, in this section the shape of the target is simplified by reducing the target area to a sphere so that the analytic geometry involved in calculating highlighted and shaded areas is uncomplicated. If this approximation to the target shape were not made, the analysis necessary to calculate apparent sizes of the target areas would be extremely difficult. Precedent for this simplification is discussed by Ryll (1962). In addition to the geometry problem, as is discussed in Chapter 2, the majority of detection data available is for circular targets.

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The variations in contrast across this sphere's surface can readily be described in terms of its orientation with respect to the observer, the illuminating source, and features of the background; and the reflectance properties of the target's s surface and of the background. The characteristics of the sphere most closely approximating the observer's image of a tank in the field are developed below.

The top view of a rectangular tank-type target of length U height V, and width W, is shown in Figure 14 moving at an angle \mathbb{Y} with the observer's line of sight. Such a target, when on level ground, will appear as a rectangle having a height V and length $U_{\underline{n}}$ given by

$$\mathbf{U}_{\mu} = \mathbf{U}\sin\Psi + \mathbf{W}\cos\Psi \qquad (\mathbf{3.5})$$

when viewed from ground level. The sphere approximating the rectangular target will appear as a circle to the observer.

The angular size, Ω in minutes of arc, subtended by the diameter of a circle having an area A equivalent to the area of this rectangle is

$$\Omega = \frac{6875.6}{R} \left(\frac{\Lambda}{\pi}\right)^{\frac{1}{2}}, \qquad (3.6)$$

where R is the distance to the target, $A = VU_R$ and U_R is given by equation 3.5 Since the probability of detecting a rectangular target of area A is essentially equal to the probability of detecting a circular target of the same area, (Sec.

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Ghapter 2), the visual angle Ω , given by equation 3.6 can be used in Figure 12 of Chapter 2 to determine the threshold contrast of the rectangular target. Thus, the rectangular tank-type target is conceptualized as a circle whose diameter subtends an angle Ω at the observer's eye when viewed from a distance R as given by equation 36. The predominant contrasts of this spherical target representation with its background and foreground are discussed below.

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Under natural lighting the lower surface of a tank-type target and also the spherical target would almost always be shaded and some part of the top surface would be highlighted. Let these surface areas be referred to as:

- A_H = the highlighted part of the sphere's surface exposed to the observer, and
- A_S = the shaded part of the sphere's surface exposed to the observer.

Five distinct contrast values can be obtained: the contrast of each area with the target's background and foreground and the internal contrast existing between the areas. According to arguments presented below, only three of these contrasts:

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⁷As was mentioned earlier, detection data is best tabulated for circular targets of uniform luminance silhouetted against a uniform luminance background.

- C_{HB} = the apparent contrast of the highlighted part of the object with the background,
- C_{SF} = the apparent contrast of the shadowed part of the object with the foreground, and
- C_{T} = the apparent internal contrast,

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are considered as being important to the detectability of the target.

There are two reasons for not considering either the contrast of the highlighted area, $A_{\rm H}$, with the foreground or the contrast of the shaded area, $A_{\rm S}$, with the background. First, the foreground will not appear adjacent to $A_{\rm H}$ unless the target is completely backlighted or in the shadows cast by terrain features ^S which block the sun's rays. Similarly, background features will rarely appear adjacent to $A_{\rm S}$ unless the target is completely frontlighted. Second, when an area is silhouetted against a background of nonuniform luminance, that part of its area which has the highest contrast would be most important in determining its detectability. The question considered next is how these three contrasts can be combined to give one value of contrast which can be used to obtain a single glimpse detection probability for the target.

⁸A procedure to determine whether or not the target is in the shadows cast : y features in the background is presented later in this chapter.

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According to our assumptions, the spherical target will appear similar to the circular targets shown in Figure 15. From inspection of Figure 15, it can be seen that as the relative size of a high-contrast area decreases its





Fig. 15.--Example Illustrating the Importance of High Contrasts

significance to the observer decreases and the significance of the edge contrast increases. This effect would probably be even more pronounced with more complex shapes and nonuniform backgrounds where there may be many such small high-contrasted areas across the face of the target and within the background itself. Thus, to obtain a single contrast measure representative of the target, it would seem logical to combine values of the edge and internal contrasts, redundant and the relative sizes of its contrasted area. However, it is not clear how these different weights should be determined. For example, for targets shown in Figure 15, values of the two edge contrasts are much lower tracts and the internal contrast measure at any point along the intersection of the black and white areas of the target. If each of these values were weighted evenly,
one would obtain a contrast somewhere between the high internal contrast and the lower of the two edge contrasts. Although it is clear that the internal contrast is most important in this case and should receive a greater weight, there is no known methodology for determining this relative weight. In the following section, the contrasts C_{HB} , S_{SF} , and C_{I} , between the different pairs of contrasted areas of the target and surroundings are treated as independent stimuli and the theoretical glimpse probability for the whole target.

Estimation of Glimpse Probability for Simplified Target

In the previous section the target was conceptualized as a spherical solid presenting three contrasted areas, C_{HB} , C_{SF} , and C_{I} , to the observer. Little is known about how patterns consisting of different contrasted areas stimulate the visual system. About all that can be said is that each contrasted area should contribute to the overall detection stimulus in proportion to the intensity of its contrast and the size of the contrasted area relative to the size of the whole pattern. The relative importance of size (angular subtense) and intensity of contrast in determining detection probabilities for a single homogeneous target is reflected in the formula for glimpse probability, g, given in Chapter 2, equation 2.14. Thus, instead of using the magnitude of each contrast, C_{HB} , C_{SF} , and C_{I} , and the respective sizes of these contrasted areas to determine some average (effective)contrast to be used, it is more reasonable to treat these areas as three distinct targets with glimpse probabilities, g_{HB} ,

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 g_{SF} , and g_{I} . Treating these targets as if they were independent, i.e., assuming that the probability of detecting any one of them in a single glimpse is independent of the probability of detecting any of the remaining two, then

 $g = 1 - (1 - g_{HB}) (1 - g_{SF}) (1 - g_{I}),$ (3.7)

where g is the probability of detecting at least one of the objects in a single glimpse.

to support this contention, Morris (1959), states:

"the discernible elements of the patterned target may be considered as several independent targets simultaneously viewed, each with its own detection range"

From equation 2.14, in Chapter 2, the probabilities g_{HB} , g_{SF} , and g_I , are given by:

$$\mathbf{g}_{HB} = \Phi \left[\frac{\left\{ C_{HB} / KC_{t} (\Omega_{H}) \right\} - 1}{.434} \right],$$
 (3.6)

$$\mathbf{g}_{\mathbf{SF}} = \Phi \left[\frac{\{\mathbf{C}_{\mathbf{SF}} / \mathbf{KC}_{\mathbf{t}} (\mathbf{\Omega}_{\mathbf{S}})\} - 1}{.434} \right], \text{ and} \qquad (3.9)$$

$$\mathbf{g}_{I} = \Phi \left[\frac{\left\{ C_{I} / KC_{1} (\Omega_{I}) \right\} - 1}{.434} \right],$$
 (3.10)

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where it is understood that C_{HB} , C_{SF} , and C_{I} , are apparent contrasts.⁹ The threshold contrast, C_{t} (Ω), of a circular target whose diameter subtends an angle, Ω , at the observer's eye is shown sketched in Figure 12 of Chapter 2 for different values of adaption brightness (luminance of the surrounding area).¹⁰ These data are not directly usable in equations 3.8,3.9 and 3.10 since the pairs of areas corresponding to the contrasts, C_{HB} , C_{SF} , and C_{I} , will rarely be circular even for a smooth-surface spherical target. Thus, Ω_{H} , Ω_{S} , and Ω_{I} , must be interpreted as equivalent angles. Means of approximating these equivalent angles are given in the ensuing discussion.

A spherical target will appear circular to an observer with shadowed and highlighted areas as shown in Figure 16, depending on the angle which the light rays strike the target. Consider the diameter, d_{sun} of this circular area drawn parallel to the sun's rays. This diameter will be partially highlighted and partially shaded as illustrated in Figure 17. The fraction P_{H} of the diameter d_{sun} highlighted is given by:

$$P_{\rm H} = \frac{(1 + \cos (90 - \alpha) \cos \delta)}{2} , \qquad (3.11)$$

⁹ A field tactor K=6.5 is used as recommended in Chapter 2 since all factors used to calculate the field factor are present.

10 An accurate tabulation of these data is given in Bush (1946). 67 🖣

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Fig. 16.--Examples of Shading on Simplified Representation of Target

where a is the sun zenith angle and 5 is the azimuth angle of the observer's path of sight relative to the sun.¹¹ Methods for computing the highlighted surface area of spherical targets, such as shown in Figure 16, are very complex. It is assumed that the highlighted area can be useful approximated by the area of the highlighted segment shown cross-hatched in Figure 17; an expression for this area is given below:

$$\mathbf{A}_{\mathrm{H.}} = \begin{cases} \frac{\pi d^{2}}{1440} - \frac{d^{2} \sin \left\{180^{\circ} + 2 \sin^{-1} \left(\cos 5 \cos \left(90 - \alpha\right)\right)\right\}}{8}, & (0 \le P_{\mathrm{H}} \le 0.5) \\ \frac{\pi d^{2}}{4} - \frac{\pi d^{2}}{1440} + \frac{d^{2} \sin \left\{180^{\circ} - 2 \sin^{-1} \left(\cos \left(90 - \alpha\right) \cos 5\right)\right\}}{8}, & (0.5 \le P_{\mathrm{H}} \le 1.0) \end{cases}$$

11 The angles, α and δ , are discussed later in this chapter.

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$$\mathbf{A}_{\mathbf{SF}} = \begin{cases} \frac{\pi d^2}{4} - \frac{\pi d^2}{1440} + \frac{d^2 \sin \left\{180^0 + 2 \sin^{-1} \left(\cos \delta \cos \left(90 - \alpha\right)\right)\right\}}{8}, \ (0 \le P_{\mathbf{H}} \le 0.5) \\ & \\ (3.13) \\ \frac{\pi d^2}{1440} - \frac{d^2 \sin \left\{180^0 - 2 \sin^{-1} \left(\cos \left(90 - \alpha\right) \cos \delta\right)\right\}}{8}, \ (0.5 \le P_{\mathbf{H}} \le 1.0) \end{cases}$$

where $d = d_{sun}$ is given by,

$$d = \sqrt{\frac{2 V U_a}{\pi}}$$

The angles, $\Omega_{\rm H}$ and $\Omega_{\rm S}$, subtended by the diameters of circular objects having areas $A_{\rm H}$ and $A_{\rm S}$, respectively, can be calculated using equation 3.6.

In the case of the internal contrast, C_{I} , it is assumed that the larger of the two areas, A_{H} and A_{S} , is the background against which the other area is silhouetted. Thus, the angular subtense Ω_{I} of the object having a contrast C_{I} is

 $\Omega_{I} = \min (\Omega_{H}, \Omega_{S})$.

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Fig. 17.--Highlighted and Shaded Parts of the Diameter in the Plane Normal to the Observer's Line of Sight Formed by the Intersection of the Sun's Rays with the Target's Center

The angular subtenses $\Omega_{H}^{}$, $\Omega_{S}^{}$, and $\Omega_{I}^{}$, then, are used to determine the single glimpse probabilities given in equations 3.9, 3.10, and 3.11.

The apparent contrasts C_H , C_S , and C_I , are dependent on the inherent luminances of the foreground and background features, and of the shaded and highlighted parts of the target. A means of predicting the luminances of the target's surfaces and its surroundings is discussed below.

Luminance Prediction

The inherent luminance, L, of a surface depends on its directional reflectance, ρ , and the illumination, I, striking that surface. The directional reflectance, ρ , of a surface is defined by Gordon (1964) as: ". . . the ratio of inherent luminance in the direction of the specified path or sight to the total illuminance on a fully exposed horizontal plane at ground level." That is,

$$\mathbf{L} = \rho \mathbf{I} , \qquad (3.14)$$

where ρ is a function of the impinging light's incidence angle for direct illumination and the distribution of incidence angles for indirect illumination.

Brown (1952) has determined the total illumination, in footcandles, for an unobscured sum as a function of the sum zenith angle α . These data are reproduced in Figure 18. As shown in this figure, the illumination when the sum is at the horizon (sum zenith angle 90[°]) is approximately 70 footcandles, while, when the sun is directly overhead (zenith angle 0°), the illumination is approximately 10,000 footcandles.

The directional reflectance, ρ , of a surface is a function of the azimuth angle, δ , of the path of sight relative to the sun, the zenith angle, ϕ , of the path of sight, the wavelength of the impinging light rays, the surface roughness, the atmospheric conditions, the sun zenith angle, α , and the sun azimuth angle, β (Gordon, 1964). The angles α and β , which describe the position of the sun in the sky are illustrated in Figure 19. The angles δ and ϕ which describe the position of the observer relative to the sun and target, respectively, are illustrated in Figure 19. In Figure 19 the target is assumed to be at ground ievel, while the observer can be considered either elevated ($\phi > 0$) or at

ground level ($\phi = 0$).

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Scripps Institute of Oceanography (Gordon, 1964; Boileau and Gordon, 1965; Gordon and Church, 1966) has measured the directional reflectance of several common background surfaces for various values of the angles α , ϕ , and 5. These measurements are in Tables B. 1, B. 2, and B. 3 of Appendix B. The greatest amount of data are for an unobscured sun at a zenith angle of 40 to 45 degrees. The sources of these data were contacted and data for other sun angles and weather conditions other than a clear sky were found to be unavailable.

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¹²This functional form is not known, so empirical measurements of these conditions had to be used.



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Fig. 18.--Natural (Ilumination Levels (Adapted from Brown, 1952)



The effect of the sun position and meteorological conditions on surface reflectance is discussed in Appendix B. The use of the data of Table B.30f Appendix B for predicting the luminance of terrain features is discussed in the next section.

Luminance of Terrain Features

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The luminances of terrain features directly behind and in front of the target, i.e., in its background and foreground, are required to determine the contrast of different areas on the target. First, the location of the target relative to the sun and the observer, and the directional reflectances of the background and foreground features along the observer's line of sight to the target must be determined. The steps necessary to determine the luminances of terrain features in the target's foreground and background, are outlined in the flow chart shown in Figure 20. The data required as input to the calculations appearing in this flow chart are:

- 1. the target's coordinates, (X_t, Y_t, Z_t) ,
- 2. the observer's coordinates, (X_0, Y_0, Z_0) ,
- **3.** the sun azimuth angle, β ,
- 4. the location of the different terrain features on the battlefield, such as meadows, grass, trees, and roads, and
- 5. typical horizon sky luminances, such as those given in Table 7, taken from Duntley (1946; 1948). A value for sky luminance would be determined before each DYNTACS run and used throughout the battle.

As indicated in Figure 20, the directional reflectance, ρ , of the background feature whose luminance is to be calculated from equation 3.14 can be

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Fig. 20.--Flow Chart for Dotermination of Background and Foreground Luminance

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TABLE 7

HORIZON SKY LUMINANCES (not a function of location of the illuminating source)

Description	Luminance (ft-L)
Full daylight	1000
Overcast sky	100
Very dark day	10
Twilight	1
Deep twilight	10 ⁻¹
Full moon	10-2
Quarter moon	10-3
Starlight	10-4
Overcast starlight	10 ⁻⁵

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determined from Table B.3of Appendix B given the azimuth angle, δ , of the path of sight relative to the sun and the zenith angle, ϕ , of the path of sight. Thus, the luminance, L, at a point on the surface of a terrain feature exposed to direct sunlight is determined from the sun's direct illumination level, I_D , by

$$L = \rho I_{D} , \qquad (3.15)$$

where I_D is given as a function of the sun zenith angle in Figure 18, and the reflectance, ρ , of the terrain feature can be determined from Table B.30f Appendix B. Since the data on the directional reflectance of terrain features .

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exposed to indirect illumination (in shadows) are not available, it must be assumed that the data of Appendix B apply to both directly and indirectly illuminated sur-13 faces.

Thus, the inherent luminance, L, at a point on a surface of a terrain feature exposed to indirect illumination is calculated from

$$L = \rho I_{\rm s} \tag{3.16}$$

where ρ is read from Table 3.1 of Appendix B, and I_S is the indirect illumination from the sun. Equation 3.16 can be written as

$$\mathbf{L} = \mathbf{S}_{\mathbf{R}}^{\mathbf{I}} \mathbf{D}^{\boldsymbol{\rho}} \tag{3.17}$$

where S_R is the ratio of indirect to direct illumination from the sun. A graph, prepared from data given by Brown (1952), of the ratio S_R versus the sun zenith angle α is given in Figure 21.

Methodology for determining whether a target or its background (or both) are in shadows and the effect of such shadows on the single glimpse detection probability are discussed later in this chapter. The following section describes how target-to-background contrasts are determined given the illuminances of background and foreground features.

¹³This assumption was discussed with Miss J. Gordon of the Scripps Institute of Oceanography. She agreed with the authors suppositions.

¹⁴Direct Illumination includes both illumination from the illuminating source directly and the indirect(prevailing) illumination. Indirect Illumination is only the prevailing part of the illumination from the source.

1.0 0.8 Ratio, S_R, of Indirect to Direct Light 0.6 0.4 0.2 ہ م 90° 60° 80° 70° 50° 40° 30° 20* 10° 0 Sun Zenith Angle

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Target-to-Background Contrast

Once the luminance of background and foreground terrain features are calculated, the inner int contrasts, C_{HB_0} , C_{SF_0} , and C_{I_0} can be determined from equation 3.3 providing the luminances L_H and L_S of the highlighted and shaded parts of the target, respectively, can be specified. Then the apparent contrasts, C_{HB} , C_{SF} , and C_I , can be determined from C_{HB_0} , C_{SF_0} , and C_{I_0} using equation

The inherent luminance, L_{H} , of a point on the highlighted part of the target is given by

$$\mathbf{L}_{\mathbf{H}} = \mathbf{I}_{\mathbf{D}} \boldsymbol{\rho}_{\mathbf{H}} , \qquad (3.18)$$

where I_D is the illumination from the sun on the highlighted surface and ρ_H is the reflectance of the surface at that point. Similarly, the inherent luminance, L_S , at any point on the shaded part of the target is

$$\mathbf{L}_{\mathbf{S}} = \mathbf{S}_{\mathbf{R}}^{\mathbf{I}} \mathbf{D}^{\boldsymbol{\rho}} \mathbf{S} \quad , \tag{3.19}$$

where $\rho_{\rm S}$ is the directional reflectance of the target when indirectly illuminated and S_R is given in Figure

The surfaces of combat vehicles are quite different than those of components of the terrain. Because of the special nature of the finish, highlights and shadows are created when illuminated by a source such as the sun. Duntley (1964) explains that:

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"Man-made surfaces invariably exhibit pronounced gloss characteristics, particularly when the solar zenith ragle exceeds 60^{0} ."

Because of the complex nature of the targets surface this is certainly not an uncommon event. For this reason, unlike the surface of terrain features, the reflectance of surfaces highlighted and shaded are considered to have different reflectances.

Gordon (1964) measured the directional reflectance of variously oriented surfaces of an olive drab painted object for a sun zenith angle of approximately 40° . Most values ranged from 0.10 to 0.26 but readings as low as 0.01 and as high as 0.490 were recorded. Values of 0.10 and 0.26 were chosen to be representative of the reflectance of shaded and highlighted surfaces, respectively; that is, it is assumed that $\rho_{\rm S} = 0.10$ and $\rho_{\rm H} = 0.26$. For these values of reflectance, the luminances of the highlighted and shaded parts of the target are

$$L_{\rm H} = .26 \, {\rm I}_{\rm D}$$
 (3.20)

and

$$L_{\rm S} = .10 L_{\rm D} S_{\rm R}$$
, (3.21)

respectively. The luminances of the highlighted and shaded parts of the target's surface, as calculated above, are used to determine the inherent contrasts,

and there is a set of the

 C_{HB_0} , C_{SF_0} , and C_{I_0} , of the target's surface with its surroundings, as outlined below.

According to equations 3.20 and 3.21, the inherent internal contrast, C_{I_0} , is given by

$$C_{I_0} = \frac{.26 I_D - I_D S_R(.10)}{I_D S_R(.10)} , \qquad (3.22)$$

which reduces to

 $C_{I_0} = \left(\frac{2.6}{8_R}\right) -1$ (3.13)

The inherent edge contrasts, C_{HB_0} and C_{SF_0} , are given by

$$C_{HB_0} = \frac{L_H - L_B}{L_B}$$
, (3.24)

and

$$C_{SF_0} = \frac{L_S - L_F}{L_F} , \qquad (3.25)$$

where L_{H} and L_{S} , the luminances of the highlighted and shaded parts of the target, are given by equations 3.20 and 3.21, respectively, and means for determining the luminance's L_{R} and L_{F} of the background and foreground for

both direct and indirect illumination were discussed earlier in this chapter (see equations 3.15 and 3.17). It should be noted that when the target and its background (or foreground) are subject to the same illumination, i.e., either direct or indirect, the edge contrasts C_{HB_0} and C_{SF_0} reduce to the ratio of the difference in the reflectances of the target and the terrain feature to the reflectance of the terrain feature. That is, if ρ_B is the reflectance of the background and ρ_F is the reflectance of the foreground, we have

$$C_{\mathbf{HB}_{\mathbf{O}}} = \frac{\rho_{\mathbf{H}} - \rho_{\mathbf{B}}}{\rho_{\mathbf{B}}}$$

and

$$C_{BF_0} = \frac{\rho_s - \rho_F}{\rho_F}$$

where $\rho_{\rm H}$ and $\rho_{\rm g}$ are the directional reflectances of the highlighted and shaded parts of the target, respectively. Thus, as a result of our assumption that the data of TableB.3 of Appendix B can be used for either directly or indirectly illuminated features, the reflectances $\rho_{\rm B}$ and $\rho_{\rm F}$ of these features as well as the contrasts $C_{\rm HB_0}$ and $C_{\rm SF_0}$ will be the same for direct and indirect illumination. However, shadows, which cause the target to be indirectly illuminated, still affect the single glimpse detection probabilities, $g_{\rm HB}$ and $g_{\rm SF}$, as pointed out in the following section.

Effect of Shadows

As the sun zenith angle changes, shadows are created on the surfaces of the terrain features facing away from the sun as shown in Figure 22. These shadows may cover the target if it is close to the feature, or serve as the background for the target if it is not close to the feature.

To determine whether a target is within a shadow created by a terrain feature, such as a forest, a line is extended from the target to the sun. If this line intersects some part of a terrain feature, it is assumed that the target is in the shadow of that feature. In such cases, neither the target nor its background and foreground are directly illuminated by the sun. As pointed out in the previous section, the assumption that the reflectance values given in Table of Appendix B hold under indirect as well as direct illumination implies that a target in the shadow of a feature will have the same contrast as a target in the same location when it and its background are both illuminated directly by the sun (see equation 3.3 However, this assumption does not imply that the singleglimpse detection probability for a target located in a shaded area is the same as that for a target exposed to full sunlight. As can be seen from equations 3.8, 3.9 and 3.0 the single-glimpse detection probability for two targets of equal contrast will vary with the relative magnitudes of their threshold contrasts $C_{\frac{1}{2}}(\Omega)$. The thresheld contrast, in turn, depends on the luminance of the background (see

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Figure 12 of Chapter 3). For backgrounds exposed to direct illumination, this luminance is determined from equation 3.15 whereas for indirect illumination this luminance is given by equation 3.17.

Shadows also can affect the glimpse probability g_{HB} without actually covering the target by changing the luminance of the background against which the target is silhouetted. To determine if the target's background is shaded (in a computer simulation), a line of sight through the target is extended until it intersects some point on the terrain, and, then, a line is extended from that point to the sun. If this latter line intersects some point of a terrain feature within the bounds of the combat area, the target's background is considered to be shaded. Then, the luminance L_{B} used in equation 3.24 to calculate the contrast of a target silhouetted against a shaded surface of a terrain feature is calculated using equation 3.17.

Discussion

More realistic predictions of glimpse probabilities could be made by improving the description of the luminance properties of background and foreground features. For example, substantial improvements could be made if directional reflectance data could be obtained for:

1. a wider variety of environmental factors such as meteorological visibility and cloud cover,

2. sun zonith znglos other than 45° ,

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- 3. a wider range of the angles θ and ϕ ,
- 4. various degrees of shading, and

5. ambient light levels associated with twilight or nighttime.

In addition, descriptions of target luminance patterns could be improved by the collection of reflectance data for various orientated surfaces of the different materials commonly used to make tank armor.

Luminance measurements at various points on tank vehicles were taken by Ballistic Research Laboratories (Downs, et al., 1965) under a variety of meteorological conditions. These raw date are in the form of continuous graphs of surface luminance at constant distance positions along the tank as shown in Figure 23. In this figure, luminance is measured at each trace along the x-axis. However, reduction of these data into a usable form could not be accomplished within the scope of this effort. Further study and analysis of the BRL data would result in more realistic estimates of the following quantities used in this chapter:

1. the luminance of variously highlighted and shaded surfaces under different meteorological conditions including different sun positions, and various levels of meteorological visibility, and

2. the fraction of a tank highlighted and shaded for various sun positions. In addition, analysis of the BRL data could provide the information required to develop methods for estimating the effect of cloud cover on target contrast and detection.

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Additional realism could be gained by introducing the probability and effect of cloud cover into the detection model. When clouds pass between the sun and the target, as in the case of a target located in the shadow of a terrain feature, the single glimpse detection probability is reduced because of a general reduction in the overall luminance of the scene. The luminance, $L_{\rm B}$, of the background can be calculated, as indicated by equation 3.12 from

$$I_{B} = b_{B}$$

where $\begin{array}{c} \circ \\ B \end{array}$ would be taken from Table B.3 of Appendix B and the illumination, I, striking the ground when the sum is obscured by a cloud is given in Figure 24.

The probability P_S that a cloud-free line of sight exists between a target and the sun has been estimated by the Air Weather Service (1965), as a function of the sun zenith angle α , for different values of the mean total percent cloud cover. This probability is given in Figure 25. The probability, 1-P_S, that the target and its immediate surroundings are shaded by a cloud, could, with some further study, be used to determine whether or not an object is shaded by a cloud during the simulated battle.

With minor modifications, the results of this chapter could be used to determine the contrast of the target with its surroundings at night. A target illuminated by moonlight has approximately the same contrast as a traget illuminated by direct surface, since the directional reflectance remains fairly

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Fig. 25.--Probability of Target Exposure to Direct Sunlight as a Function of the Mean Cloud Cover and Sun Zenith Angle

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constant (Gordon, 1964). However the prevailing illumination changes. The direct illumination under moonlight conditions, tabulated by Brown (1952) as a function of the moon senith angle, is given in Figure 26. However, as in daylight shadows will be present within the object and on the surfaces of terrain features facing away from the moon. As with daytime conditions, the luminance of a shaded area can be expressed in terms of the ratio, S_R , of indirect to direct illumination (see equation 3.17). However, data are not available for this ratio for moonlight conditions. As an interim measure, it could be assumed that values of this ratio given for daylight (see Figure 21) hold for the reduced illumination levels at night.

Summary and Conclusions

In this chapter, the tank-target was represented as a sphere. A method was given for estimating the internal contrasts, C_{I} , between the highlighted and shaded parts of the spherical target and the two edge contrasts: C_{HB} , the contrast of the highlighted part with the background and C_{RF} , the contrast of the shaded part with the foreground. Relationships discussed between these contrast values and the single-glimpse detection probability for use in equation 312 of Chapter 2 are summarized in the flow ohart in Figure 27 Although the representation of the target is very simplified, a more detailed representation of the target's shape would be of tubious value until the effect of different contrast patterns on



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detection can be accurately described. That is, even if a large number of point measures of contrast could be predicted, it is, at present, difficult to say which are most important to the observer in making a detection.

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In the next chapter this model is used in a probability model which syndicts observer performance when searching for the target in a complex display. An attempt to validate the model is also discussed at the end of the following chapter. di la constante da la constant

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CHAPTER 4

1

PROBABILITY MODELS

In the preceding chapter, a model for predicting the probability, g, that a target is detected on a single-glimpse was developed. By dividing the target into two distinct areas, one highlighted and one shaded, three point measures of contrast were calculated:

C_{HB} = the apparent contrast of the highlighted part of the target with the background,

- C_{SF} = the apparent contrast of the shaded part of the target with the foreground, and
- C_{T} = the apparent internal contrast

Using equations 3.8, 3.9 and 3.10, the single-glimpse detection probabilities g_{HB} , g_{SF} , and g_{I} of areas having contrast C_{HB} , C_{SF} , and C_{I} , respectively were calculated. The single-glimpse detection probability, g, for the entire target was then related to these three measures of glimpse probability by the equation:

$$g = 1 - (1 - g_{f}) (1 - g_{HB}) (1 - g_{SF})$$
 (4.1)

An analytic procedure for predicting luminances of terrain features and target surfaces was also presented in Chapter 3. The calculations required for these luminance descriptions were geared toward efficient execution on an electronic computer while preserving the resolution requirements of the combat simulation. In this chapter, this predicted value of the single-glimpse detection probability (equation 4.1) is used in a probability model which accounts for search of the scene by the observer.

As discussed in Chapter 1, Stollmack (1964) suggests that the probability, P(t), that detection occurs in time t or less is given by:

$$P(Q^{-1}) = O^{\lambda(\gamma)} d\gamma, \qquad (4.2)$$

where $\lambda(\Upsilon)$ is the conditional detection rate. Two forms of this conditional rate were suggested in Chapter 1.

The first, called the "glimpse model" incorporates the model predicting single-glimpse detection probability developed in Chapter 3. This model yields a continuous function for the glimpse probability of a target moving with respect to its surroundings. Since the target is moving, such factors as the relative sizes of the highlighted and shaded areas a⁻¹ the contasts of these areas with the surroundings change. These changes result in a glimpse probability which is a continuous function of some set of environmental variables and time, g(S,T). Given this function g(S,T), the conditional detection rate, $\lambda(T)$, can be written as,

 $\lambda(\Upsilon) = \mu pg(S, T),$

where p is a function correcting for forms in the scene which abstract the observer's attention (confusing forms) and μ is the glimpse rate.

The second form of $\lambda(\Upsilon)$ is a simplification of the first. In this model it is assumed that the conditional detection rate is a step function, changing instantaneously at discrete points in time along

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the movement with of the target. This simplified model, hereafter called the "step" model assumes that the single-glimpse detection probability remains fairly constant between points in time where major changes occur. The reason for making this simplification is that parameters of this simplified distribution can be estimated by the method of maximum likelihood from detection-time data. (Such efforts for the continuous model would be extremely difficult because of the nature of the distributions involved.) These estimates can then be related to values of the conditional detection rate generated by the glimpse model to test the validity of the glimpse model. However, attempt at validation were not successful because the necessary data could not be obtained. These difficulties are also discussed in this chapter.

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In the following section the glimpse model is discussed. The Glimpse Model

The probability that a target is detected on a single glimpse has been suggested (in Chapter 3) to be a function of its internal contrast its contrast with the elements of the terrain against which it is silhouetted, and the size of the highlighted and shaded areas apparent to the observer. For a moving target, this glimpse probability is continually changing since the environmental variables affecting glimpse probability (discussed in Chapters 2 and 3) change with time. Lawson and Stollmack (1968) have shown that the instantaneous conditional detection rate, $\lambda(t_i)$, at a time T_i is of the form,

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(4.3)

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where μ is the sumpse rate, $p = \frac{1}{n}$, where n is the number of confusing forms in the scene (discussed in Chapter 2) and g is the instantaneous single-glimpse detection probability. Changes in the conditional detection rate are most likely explained by changes in the single-glimpse detection probability. Since the fixation rate, μ , remains essentially constant (White and Ford, 1960) and the number of confusing forms, n, is a function of the scene content not time. With this assumption and a single-glimpse detection probability changing with time, equation 4.3 becomes

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$$\lambda(\Upsilon) = \mu p g(\Upsilon). \tag{4.4}$$

Using the method developed in Chapter 3, the single-glimpse detection probability for moving targets can be calculated everywhere along the targets movement trace. For any one scene, a function similar to that shown in Figure 28 might be expected. As a convention, the continuous model treating the conditional detection rate as a function of the single-glimpse probability model developed in Chapter 3, will be called the "Glimpse Model". Prediction of the glimpse rate, μ , and the equivalent number of confusing forms in the scene is discussed below. <u>Prediction of the Glimpse Rate and the Equivalent Number of Confusing Forms</u>

As discussed in Chapter 2, considerable work has been devoted to measuring the rate at which fixations are made on a display. This rate is a function of various factors, including the scene content (Townsend, Enoch and Fry: 1958) and the display size (Enoch and Fry, 1958). White (1964) suggests that 3 limitions per second can be expected under most

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search simulations. This value of fixation rate is widely accepted and has been used in momenous models of detection (Ryll, 1962). Boynton, Elsworth and Palmer (1958) investigated the relationship between an observer's detection performance and the number of forms in the scene regembling the target in size, shape, and contrast (see Chapter 2). A relationship,between target detection probability, p, the number of confusing forms, n, and the exposure time, T, is indicated by Figure 7 of Chapter 2. The empirical fit given by Ryll (1962) for all target sizes and contrast investigated in the Boynton, et el., study is:

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$$p = \frac{1}{1 + \left[\frac{n}{29(T) \cdot 93}\right]^{1.29}}$$
(4.5)

If T, the exposure time is taken to be 1/3 second, the time for a single glimpse, equation 4.5 becomes

$$p = \frac{1}{\left[1 + \left(\frac{n}{10.44}\right)^{1.29}\right]}$$
(4.6)

This expression can be solved explicitly for n in terms of p as follows:

$$n = 10.44 \left[\frac{1-p}{p} \right].775$$
 (4.7)

Using this equation, the effective number of confusing forms for the terrain scene can be predicted if a value of p is known. A means of estimating **b**, the value of p for each scene is discussed below.

If an observer makes fixations at a target scene at a constant rate μ , it has been shown that the probability, P(t), that a stationary target is datagned in time t or less is

$$P(t) = 1 - o \tag{4.8}$$

where g is the single-glimpse detection probability determined from equation 4.1, and p is the detection probability used in equation 4.7 to predict the equivalent number of confusing forms. Given estimates, λ , of the detection rate of a stationary target in a natural environment, β , an estimate of p, is given by:

 $\hat{\mathbf{p}} = \hat{\lambda}/3g$, if the fixation rate, μ is assumed to be a constant 3 per second. Substituting this into equation 4.7 yields the expression

$$n = 10.44 \quad \frac{3g - \hat{\lambda}}{\hat{\lambda}} \tag{4.9}$$

as an estimate of the number of confusing forms in each scene. Discussed below is a method of determining a statistical distribution of the number of confusing forms contained in a typical terrain scene.

Distribution of the Number of Confusing Forms

In the preceding section, a method of estimating the effective number of confusing forms in a terrain scene was suggested.

To make the glimpse model completely general, it is desirable to have a value of the effective number of confusing forms to enter into equation 4.4 for a specific terrain type. To obtain an estimate of n, it is necessary to measure detection times for several observers viewing a stationary target. From these detection times, an estimate, $\hat{\lambda}$, of the

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 λ would be calculated.

Since and the experimental effort is impractical for each scene because of the earge number of possible scenes a single experiment with several classifications of terrains would permit the determination of a statistical distribution of the number of confusing forms. Typical terrain classifications are:

1. Flat, no trees or schrubs, with tall grass.

- 2. Flat, small schrubs and grass.
- 3. Flat, trues and schrubs.
- 4. Flat, barren with trees in background.
- 5. Rolling, with schrubs and ireas.
- 6. Rolling, with sparse vagetation.
- 7. Heavily vegetated (jungle).

Of course, the above list contains only a few of those terrains which might be considered. The choice of these classifications depends on the environment in which detections are to be expected to occur. Once a list of the terrain types in which detection might occur have been compiled, an experiment to determine a statistical distribution of the number of confusing forms is necessary. Suggestions for planning such an experiment are given below. Given several examples of one terrain type a few typical target locations in the scenes would be selected. As seen in equation 4.9 an estimate of the detection rate for scene is needed to calculate in. Seve all subjects are asked to find the targets in each scene using the nerved given by Brown (1956), an estimate, $\hat{\lambda}_{ij}$ of the detection rate location is the scenes of indication. Just calculated.

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Then g_{ij} is exiculated using the method discussed in Chapter 3 for predicting the schole-glimpse detection probability. Given $\hat{\lambda}_{ij}$ the effective number of confusing forms, \hat{R}_{ij} for scone i in the jth terrain type is calculated form

$$\hat{r}_{ij} = 10.44 \quad \frac{3g_{ij} - \hat{\lambda}_{ij}}{\hat{\lambda}_{ij}}$$
 (4.10)

Given N_j values of the effective number of confusing forms for terrain type 1, the statistical distribution of n_{ij} could be estimated from a histogram of the data. Stollmack and Lawson (1968) have shown that for 9 scenes from the tank ranges at Fort Knox, the effective number of confusing (orn.s is approximately distributed according to a Poisson distribution with a mean of 9.83. The scenarin this group come from several different terrain classifications but contain a good sample of what might be classified as a "Fort Knox" terrain. Since there were only 9 scenes it was not feasible to classify their content and divide them into categories, because any further breakdown would reduce the size of the sample upon which the distribution of n is based. To apply the model, during a simulation run the distribution of the effective number of confusing forms is determined by Monte-Carlo methods for each terrain type in which detections are made.

Time and funds prohibit the completion of the analysis outlined above since an extensive amount of terrain analysis and data collection and reduction are required. Performance of the analytic procedure outlined in this section is terrainmended if the glimpse model is to be applied to a general company on location containing several terrain classificationed

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 $G_{1,m-n}$ constant fixation rate of 3 glimpses per second and an estimate of the equivalent number of confusing forms in a scene, the probability P(t), that a target is detected in t seconds or less (equation 4.4) according to the glimpse model becomes:

$$P(t) = 1 - e^{\int_{-\infty}^{t} 3g(\Upsilon)/n \, d\Upsilon} . \qquad (4.11)$$

This form of the probability P(t) results from a conditional detection rate which is a continuous function of time, such as that shown in Figure 28. In the next section, the form of this conditional detection rate is reduced to a step function with instantaneous changes at known discrete points in time during the movement of the target.

The Step Model

The Glimpse model developed in the preceding section yields a continuous function for the conditional detection rate, $\lambda(\Upsilon)$, as shown in Figure 28. In this figure, it is suggested that subtle changes at finite times in target-background-observer conditions cause changes in the detection rate at several points in time. Since detection times from the movies taken by Brown (1966) are to be used to estimate the effect of changes in these conditions, a statistically significant number of data points must be available to estimate $\lambda(\Upsilon)$ for each rate change. In this section, a simplification in the form of the function $\lambda(\Upsilon)$ is suggested so that statistical estimates of the detection rates during the target's exposure time can be calculated. This simplified form of $\lambda(\Upsilon)$ called the "step model" is discussed below.

Examination of films of moving targets taken by Brown indicates that changes in the appearance of the target occur several times during

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Its movement accesss the scene. If these changes are instantaneous and remain at some assentially constant level during a certain time interval, a simplication can be made in the form of $\lambda(\Upsilon)$ as predicted by the Glimpse model. If the single-glimpse detection probability iduring this time interval is a constant g, the conditional detection rate $\lambda(\Upsilon)$ is a constant given by equation 4.3 as

$$\lambda(\Upsilon) = \mu g p \qquad (4.12)$$

where μ and p_3 defined previously, are constant for each scene. The conditional detection rate, λ_i (Y), for the ith such time interval is given by,

$$\lambda_{i}(\Upsilon) = \mu p g_{i}, \qquad (4.13)$$

where q_i , the single-glimpse detection probability in the interval is calculated from equation 4.1. If the times $T_i (i = 0, ..., N)$ that the glimpse probability changes occur are subjectively measured from examination of the films the functional form of the new $\lambda(\Upsilon)$ might appear as shown in Figure 29. (In this figure the form as suggested by the Glimpse model is superimposed.) In this figure the target becomes intervisible to the observer at time T_0 and the conditional detection rate is constant λ_0 . At known points in time, $T_i (i = 1, ..., 3)$ the rate assumes some constant level $\lambda_i (i = 1, ..., 3)$ and remains at that level until time T_{i+1} , when it instantaneously changes to a level λ_{i+1} . In Figure 28, it is noticed that the simplified form of $\lambda(\Upsilon)$ closely approximates the continuous from suggested by the Glimpse model only if the changes in $\lambda(\Upsilon)$ are essentially instantaneous. This simplification is

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fairly consistant with the conditions actually observed on the films taken by Brown (1966). The condition of the target does change almost instantaneously at several points along its movement path. These changes are caused by several factors:

- 1. The target may become silhouetted against another element of the background, thus, changing its target-to-background contrast,
- 2. The exposure angle (angular subtence) of the target may change as the amount of the target concealed by some terrain feature such as a low bush or high grass changes,
- 3. The orientation of the vehicle may change due to a rise or fall of the target with respect to position of the observer and the illuminating source. This change in orientation alters the appearance of the target by changing the relative magnitudes of the percent of the target highlighted and shaded,
- 4. A change in the crossing velocity of the target relative to the observer, and
- 5. A change in direction of advance.

According to the simplified model, when any one of these or other events changing the detection rate occur, the rate changes immediately by a constant amount and remains at its new level for a finite period of time. Of course, the change in detection rate may not be instantaneous but increase or decrease to some constant level at a constant rate as a function of time. This case and the problems it introduces are discussed at the end of this chapter. In the following section, the distribution of detection times for a target-motion scene with N changes in the glimpse rate is developed.

Distribution of Detection Times

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Stollmack (1965) has developed an expression for the distribution of detection times in a stationary target viewed by a moving observer.

In this means hanges in the conditional detection rate occur at discrete points in tune — st as in the Simplified model discussed in the preceding section — the refore, the only difference between the model derived by Stollmack and the Simplified model is that rate changes are caused by target motion rather than observer motion. Regardless of the cause of the change, the distribution of detection times is the same if the conditional detection rates are the same. The distribution of detection times for the Simplified model is discussed below. This development is a direct extension of the work contained in Stollmack (1965).

In the general Step model, the conditional detection rate $\lambda(\Upsilon)$ is a step function changing at N determinable points in time as shown in Figure 30. In this figure, the target emerges from a terrain feature at time T_0 and becomes completely hidden from the observer at time T_N . At discrete points T_1 (i = 0, ..., N-1) within the movement trace of the target, the conditional detection rate assumes some constant level λ_1 (i=0,..., N-1), and remains at that level until time T_{i+1} . Given that no detection has occurred up to the time T_i , the conditional cumulative probability, P_i (t- T_i), that detection will occur at time t or before in the interval $\{T_i, T_{i+1}\}$ is equal to

$$P_{i}(t - T_{i}) = 1 - e^{-\lambda_{i}(t - T_{i})}$$
 (4.14)

for i = 0, ..., N-1, and $T_i \le t \le T_{i+1}$. Furthermore, the unconditional sumulative probability. P(t) that detection will occur at or before time t, where $T_i \le t \le T_{i+1}$, can be written as:



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Fig. 30.--General Case of Changing Constant Detection Rate

 $P(t) = P(\text{detection occurs before time } T_i) + P(\text{no detection before time } T_i) \cdot P(\text{detection})$ at time t | no detection before time T_i , (4.15) $(T_i \leq t \leq T_{i+1})$

Denoting the probability the detection does occur at or before time T_i as the cumulative probability of detection, $P(T_i)$, and the probability that no detection occurs at or before T_i , $Q(T_i)$, as:

$$Q(T_{i}) = \{1 - P(T_{i})\}, \text{ equation } \underline{4.15} \text{ becomes},$$

$$P(t) = \begin{cases} P(T_{i}) + \{1 - P(T_{i})\} & P_{i}(t - T_{i}), \\ T_{i} \leq t < T_{i+1}, \\ i = 1, \dots, N-1 \\ P(T_{N}), & t \geq T_{N}, \end{cases}$$
(4.16)

if it is assumed detection occurs with probability one at or before time ${\rm T}_{\rm N}$.

Equation 4.1F can be written as:

In equation 4.17, the probability, P(t) that detection occurs at or before time t, where $T_0 \in T_1$, is written

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$$P(t) = P(T_0) + \{1 - P(T_0)\} P_0(t - T_0)$$
(4.18)

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If the target t_1 initially completely hidden, the cumulative probability, $P(T_0)$, of detection at or before time T_0 is equal to zero. Setting T_0 , the initial appearance time equal to zero, equation 4.18 becomes:

$$P(t) = P(0) + \{1-P(0)\} P_0(t - 0)$$

which reduces to

$$P(t) = P_{0}(t)$$

from equation 4.14, P(t) becomes

$$P(t) = 1 - e^{-\lambda_0(t-0)}$$

which reduces to

$$P(t) = 1 - e^{-\lambda} t$$
, $0 \le t < T_1$ (4.19)

the cumulative probability of detection at time t or before $0 \le t < T_1$. Furthermore, the cumulative probability, P(t) of detection during the second time interval $[T_1, T_2)$, taken from equation 4.17 is given by:

$$P(t) = P(T_1) + \{1 - P(T_1)\} P_{1}(t - T_1), T_1 \le t \le T_2$$
(4.20)

in equation 4.20, $P(T_1)$ is the cumulative probability that detection occurs at or before time T_1 . This probability is given by equation 4.19 as,

$$P(T_1) = 1 - e^{-\lambda_0 T_1}$$
(4.21)

The probability, $P_1(t - T_1)$, that detection occurs in the time interval (T_1, T_2) given by equation 4.14 is:

$$P_1(t - T_1) = 1 - e^{-\lambda_1(t - T_1)}, T_1 \le t < T_2$$
 (4.22)

Substituting 4.21 and 4.22 into 4.20, the cumulative probability of detection, P(t), at or before time $0 \le t \le T_2$ is given by :

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P:
$$(1 - e^{-\lambda_0 - T_1}) + (e^{-\lambda_0 - T_1}) - (1 - e^{-\lambda_1 - (t - T_1)})$$
 (4.23)

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$$-\lambda_{0} T_{1} - \lambda_{1} (t - T_{1})$$

$$P(t) = 1 - e \qquad (4.24)$$

In a similar manner, the cumulative probability of detection at α before T_{χ} is given by:

$$P(t) = \frac{-\lambda_0 \tau_1 - \lambda_1 (\tau_2 - \tau_1)}{(1 - e)} + \frac{-\lambda_0 \tau_1 - \lambda_1 (\tau_2 - \tau_1)}{(1 - e)} = \frac{-\lambda_2 (t - \tau_2)}{(1 - e)}$$

which reduces to

$$-\lambda_{2} T_{1} - \lambda_{1} (T_{2} - T_{1}) - \lambda_{2} (t - T_{2})$$

$$P(t) = 1 - e$$
(4.25)

Repeating this procedure, the general form of P(0) (equation 4.14) in the ith time interval is given by:

$$P(t) = 1 - e^{-\lambda_0 T_1 - \lambda_1 (T_2 - T_1)} - \dots - \lambda_{i-1} (T_i - T_{i-1}) - \lambda_i (t - T_i)$$
(4.26)

where $(T_i \in t < T_{i+1})$. and $i = 0, \dots, N-1$

Furthermore, by definition, at time T $_{\rm N}$ or beyond,

$$P(t) = 1 - e^{-\lambda_0 T_1 - \lambda_1 (T_2 - T_1) - \dots - \lambda_N T_N} = 1, t \ge T_N.$$

From the cumulative distribution of detection times, given in equation 4.26, the probability density function, p(t) of detection times is given by:

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$$\begin{array}{c} 114 \\ \begin{cases} \lambda_{0} e^{-\lambda_{0}t} &, 0 \leq t < T_{1} \\ e^{-\lambda_{0}T_{1}} & \lambda_{1}e^{-\lambda_{1}(t-T_{1})} &, T_{1} \leq t < T_{2} \\ e^{-\lambda_{0}t} &, -\lambda_{1}(T_{2}-T_{1}) & \lambda_{2} e^{-\lambda_{2}(t-T_{2})} &, T_{2} \leq t < T_{3} \\ \vdots & (4.27) \\ e^{-\lambda_{0}aT_{1}} & -\lambda_{1}(T_{2}-T_{1}) & -\dots & -\lambda_{i-1}(T_{i}-T_{i-1}) & e^{-\lambda_{i}(t-T_{i})} \\ e^{-\lambda_{0}aT_{1}} & e^{-\lambda_{1}(T_{2}-T_{1})} & -\dots & -\lambda_{i-1}(T_{i}-T_{i-1}) & e^{-\lambda_{i}(t-T_{i})} \\ e^{-\lambda_{0}T_{1}} & e^{-\lambda_{0}T_{1}} & e^{-\lambda_{0}T_{1}} & e^{-\lambda_{0}T_{1}} & e^{-\lambda_{0}T_{1}} & e^{-\lambda_{0}T_{1}} \\ e^{-\lambda_{0}T_{1}} & e^{-\lambda_{1}(T_{2}-T_{1})} & -\dots & -\lambda_{i-1}(T_{i}-T_{i-1}) \\ e^{-\lambda_{0}T_{1}} & e^{-\lambda_{0}T_{1}} & e^{-\lambda_{0}T_{1}} \\ & T_{i} \leq t < T_{i+1} \\ e^{-\lambda_{0}T_{1}} & e^{-\lambda_{1}(T_{2}-T_{1})} & -\dots & -\lambda_{i-2}(T_{i}-T_{i}-T_{i}) \\ & T_{i} \leq t < T_{i} \\ \\ & 0 \\ & & , t \geq T_{i} \\ \end{array}$$

in the dext section, estimation of the parameters of this distributlor from detection-time data is discussed. These estimates are used for comparison with predictions obtained from the Glimpse model discussed at the beginning of this chapter.

Estimation of $\lambda_i (i = 0, ..., N-1)$ from Detection-Time Data

Estimates of the conditional election rate for each target presentation can be computed using the method of maximum likelihood (Hogg and Craig, 1960). Partitioning the n subjects put on test(having a chance to detect the target) during the targets movement across the scene into N sets, we obtain: and million have

 $n = \sum_{k=0}^{N-1} r_k detections in [T_0, T_1]$ (T_1, T_2) (T_1, T_2) (T_2, T_3) (T_1, T_1) $(T_1,$

An unbiased maximum likelihood estimator for $\hat{\theta}_i = \frac{1}{\lambda_i}$, derived in Appendix D, is given by:

$$\frac{1}{\lambda_{i}} = \hat{\Theta}_{i} = \frac{\sum_{l=1}^{r_{i}} (t_{l}^{(i)} - T_{i-1}) + (n - \sum_{m=0}^{l} r_{m}) (T_{i} - T_{i-1})}{r_{i}}$$
(4.29)

where

- $$\begin{split} \theta_i &= \text{ an estimate of the value of } \frac{1}{\lambda_i} &\text{ in } \left[T_i, T_{i+1} \right) , \\ r_i &= \text{ the number of detections in the time interval} \\ & \left[T_i, T_{i+1} \right] (i = 0, \dots, N-1) , \end{split}$$
- n = the number of c¹ revers tested,
- $\begin{array}{ll} T_i & (i=0,\ldots,N) \text{ are previously defined, and} \\ t_i^{(i)} & (l=1,\ldots,r_i) \text{ are the detection times in the interval} \\ & \left[T_i,\ T_{i+1}\right] \end{array}$

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The value of the conditional detection rate given in equation 4.33 should be equivalent to that predicted by the Gilmpse model for the i^{th} time interval. Equation 4.13 and 4.29,

$$\frac{\sum_{k=1}^{i_{1}} (i_{k}^{(1)} - T_{i-1}) + (n - \sum_{m=0}^{i_{1}} r_{m})(T_{i} - T_{i-1})}{r_{i}} = \frac{1}{\mu p g_{i}} (4.30)$$

In this equation, μ and p, defined earlier, are constant for each scene (independent of the value of i). Equation 4.30 provides a method for checking the validity of the Glimpse model. If the method for computing the single-glimpse detection probability is correct, the right and left sides of equation 4.30 should be equivalent. To calculate the glimpse probability, g_i , given in equation 4.30, it is necessary to measure certain quantities such as contrast and size from the films taken by Brown (1966). The detection times used to calculate estimates of $\hat{\lambda}_i$ were obtained from observers viewing these films. A procedure for validating the Glimpse model by comparing the right and left sides of equation 4.30 is discussed in the following section.

Model Validation

In this chapter, two probability models have been developed, the first called the Glimpse model, gives the conditional detection rate, $\lambda(n)$, as a continuous function of several environments variables and time. The second, called the Step model, approximates $\lambda(\gamma)$ as a step function. In the Step model, the detection rate changes instantaneously at discrete determinable times during the movement trace of the target. Given these times, estimates of the reciprocal of the conditional detection rate, $\hat{\theta}_{1}$,

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for the i^{th} interval of movement are calculable from equation 4.29. Equating $\frac{1}{\theta}$, and the predicted value of $\frac{1}{\lambda(n)}$ in the i^{th} time interval,

$$\frac{1}{\theta_1} = \mu p g_1$$

Validation of the model will entail comparison of the right and left sides of this equation.

The films taken by Brown (1966) were thought to contain sufficient information to perform this validation. By examining the films, any changes in the value of contrast or any of the other variables used to calculate the single-glimpse detection probability were noted. These changes could be considered as the times that the rate changes in the Simplified model $(T_1, T_2, ..., T_N)$. To calculate the single-glimpse probability using the methods of Chapter 3, the following quantities would have to be measured at several points along the movement trace of the target on the films:

- 1. The apparent contrast of the highlighted target area with the foreground,
- 2. The apparent contrast of the shaded target area with the background,
- 3. The apparent contrast of the highlighted target area with the shaded target area,
- 4. The horizontal and vertical angular subtense of the larget, and
- 5. The relative amounts of the target area which are highlighted and shaded.

In addition to these measures at several points along the movement trace, the same quantities must be determined for the slides from which the detection-time data are used to calculate the effective number of



confusing forms given by equation 4. Given all of the above data, the conditional detection rate in the th time interval is determined from:

$$\hat{\lambda}_i = \mu g_i n$$

where n_i is given by equation 4.9, μ is a constant 3 per second, and g_i is given in Chapter 3 as:

$$g_{i} = 1 - (1 - g_{I}) (1 - g_{HB}) (1 - g_{SF})$$

and g_{I} , g_{HB} , and g_{SF} are calculated from equations 3.8, 3.9, and 3.10 respectively.

Attempts at Collecting Data for Validation

Unfortunately, attempts to collect the data necessary to validate the model were unsuccessful. Upon careful examination of the films taken by Brown (1966) several difficulties were encountered which prevented collection of useful data. These difficulties were caused primarily by the quality of the movies taken. They include:

- 1. The film resolution was not adequate to permit separation of the target into distinct areas of highlighting and shading.
- 2. The film, when examined at normal operating speed (24 frames per second) was quite clear and details seemed to be distinguishable. However, examination of individual frames revealed a great deal of smearing. This is due to a slight motion in the film as it moved past the shutter when the original films were taken

A Prichard photometer with a six-minute aperture was used to measure the luminance of various points around and within the target to obtain estimates of the target-scene contrast. Because of the problems with resolution discussed above, inconsistant and often contradictory values of contrast were obtained. In addition, it was extremely difficult to

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measure the angular size of the target during its movement. This problem is also related to the resolution problem discussed earlier, since no clearly defined border between the target and its background was present when viewed on an increased scale.

Summary and Conclusions

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Two models predicting probability that detection occurs in a time t or less have been developed in this chapter. An attempt was made to study the correspondence between the two models by comparing the right and left sides of equation 4.34. However, to calculate the singleglimpse detection probability, it was necessary to obtain measurements of contrast and target exposure size from motion picture films. The quality and resolution of these films were not sufficient to permit the collection of the required data in the event such an experiment is conducted in the future, it would be necessary to take the photographs on a higher quality camera to alleviate the smearing problem which was encountered. Furthermore, the film taken by Brown was 16 millimeters in width, making the size of the target image extremely small. It would seem appropriate to use either 32 or 64 millimeter film for the further studies. In addition to the better equipment and film, care should also be taken to focus the image at all points on the scene if possible. The films taken by Brown were out of focus at several points in many of the scenes.

In place of the improved film, measurements of the variables necessary to calculate the single-glimpse detection probabilities could be measured in the field. However, it is felt that the improved equipment and film will alleviate the data-collection problems more

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aconon-wave shale also creating a permanent record of the experiments condition.

A constraint of the earlier in the chapter, the change in the conditional detection rate may not be instantaneous as assumed in the Step model. If the conditional detection rate, λ_i , is proportional to time in the ith time interval, where

$$\lambda_i = \alpha_{0i} + \alpha_{1i} t$$

the solution procedure used to develop maximum likelihood estimators for α_{0i} and α_{1i} could not be performed by standard algebraic methods. The only alternative would be to use a numerical analysis technique to obtain solutions for α_{0i} and α_{1i} . Recause time and funds were limited, this analysis was not pursued further.

In the next chapter, the two models are summarized and recomendations for future research are suggested.

CHAPTER 5

SUMMARY AND CONCLUSIONS

The research problem posed in Chapter 1 was to develop a model of visual detection for a combat computer simulation which predicts datection time performance of an observer searching for a moving target in a complex terrain scene. As indicated in Chapter 2, very little experimental work has been performed on the detection of complex objects in natural terrain displays. In this literature review, results of several experiments over the past few decades were discussed in some detail. The results of these experiments give a clue to the variables affecting detection of targets in a complex display as opposed to those contained in a laboratory-type display of uniform luminance and content. The problem of detection in a homogeneous display has been treated in some detail by other authors (Lawson, 1969), but no significant contributions concerning complex displays are apparent.

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A model based on the information derived from results of the experiments discussed in Chapter 2 and the intuition of the author is presented in Chapter 3, which predicts the single-glimpse detection probability of a target in a natural environment. This model treats the target as three independent objects, each having its own detection probability. The probability of detecting the entire object on a single glimpse is a function of the probabilities that these three objects are detected. The calculations nacessary to determine the single-glimpse detection probability are easily executable on an electronic computer, making the model applicable to a computer-played combat simulation.

Given the single-glimpse detection probability, $g(\tau)$, the probability that the target is detected in a display containing in forms similar in appearance to the target was shown to be

$$P(t) = 1 - e^{-t} \int_{t}^{t} \frac{Mq(T)}{n} dT$$

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where μ is the fixation rate. Since the form of the function $g(\tau)$ was not estimable from detection-time data, a simplifying assumption was made. By assuming $g(\tau)$ to be a step function which changes at determinable times during the motion of the target, an approximation to the functional form of $g(\tau)$ was made. This simplified functional form permitted the estimation of parameters of the step function. An attempt was made to relate the estimates of the conditional detection rate from the simplified model to those predicted by the glimpse model. However, attempts proved futile because necessary data could not be extracted from films of moving targets in a natural terrain scene. Suggestions for alleviating this problem in future experiments of this nature were presented.

The model which predicts single-glimpse detection probability relies heavily on a simplification in the shape of the target. A complex multi-luminance target is seen by the observer. However, no basic contrast threshold data are available for such targets. Since the only svailable data are for circular targets of uniform luminance, it was necessary to simplify the target shape somewhat by converting all rectangular solids into spheres having the same cross-sectional area. It is obvious that the obtaining of contrast-threshold data for complex objects

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viewed against non-homogeneous backgrounds is highly desirable, since values of contrast threshold for circular targets are very optimistic when compared with the contrast thresholds of the complex traget-scenes.

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In addition to this basic psychophysical data on contrast thresbolds, the concept of the term "confusing forms" needs further examination. In Chapter 4, it was assumed that distinct objects in the display attract the attention of the observer. However, this may not be the case, since the observer may not select distinct objects to investigate, but instead may use the total content of the scene to perform an orderly search. No search data confirming the latter supposition has been iound in the literature. An experiment to investigate this hypothesis therefore geems advisable.

The model predicting single-glimpse detection probability presented in Chapter 3, is completely general. However, its most valid application is for a clear bright suniit day. As the illumination or visibility decreases, some of the assumptions used to construct the model become untenable, so further investigation of the model's validity in these cases is advisable before a direct extension is made. These direct extensions have been discussed at the end of Chapter 3.

Increased interest has been expressed by the military in the detection of militarily significant objects at night by either unaided or aided (optical devices) vision. To extend the glimpse model to low illuminations, further study of the following factors would be necessary:

1. The concept of confusing forms. It seems logical to to assume that there are considerably more forms in the display which compete for attention because detection is so difficult at all but the shortest ranges if vision unaided.

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2. The fixation rate, which most likely changes with illumination level and possibly other factors.

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APPENDIX A

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VISIBILITY DATA FOR THE SEMBACH, GERMANY, WEATHER STATION

Figure A.1 indicates the change in meteorological visibility with the month of the year. Figures A.2 and A.3 illustrate the variation in meteorological visibility with the time of day in the months of April and July, respectively. These figures were adapted from data supplied by the Air Weather Service (MATZ, 1965) for the Sembach, Germany, Weather Station. Similar data are available for other weather stations. World wide visibility data has been complied by H. P. Dudel (1966, 1967) of the U.S. Army Missile Command. These data are in the form of cumulative distribution functions similar to those shown in Figures A.2 and A.3.



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Fig. A. 2. --Hourly Meteorological Visibility at Sembach Airport during April Averaged for 0-2, 4-6, 8-10, 12-14, 16-18, and 20-22 L.S.T. Hours

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APPENDIX B

DIRECTIONAL REFLECTANCE DATA FOR REPRESENTATIVE TERRAIN FEATURE TYPES

Tables containing reflectance data for several terrain-features are given in this appendix. The data of Table B.1were taken under an unobscured moderately high sun ($\alpha = 40^{\circ}$). Values are given for different szimuth angles δ of the path of sight relative to the sun and zenith angles ϕ of the path of eight. Similar, but much less extensive data are given in Table B.2taken ender an overcast sky. Table B.3 gives directional reflectances for dirt road when the sun is close to the horizon.

The change in the reflectance with obscuration of the sun and changes is the position of the sun in the sky can be seen from the data of Tables B. 4 and B.5, respectively. The data of Table B. 4 for a ploughed, moist, sand-loam seti, indicate that directional reflectance decreases as the illumination becomes more diffuse (that is, as the sun is obscured by a cloud). The data of Table B.5 for a freshly ploughed dirt road, indicate that directional reflectance decreases as the sun zenith angle α decreases.

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	spaceu.		66		0.0316	0.0311	0.0317	0.0517	0.0337	0.6255	0.0463	
			135		G. 0335	0.0382	0.0392	0.0387	9.0438	0.0463	0.0572	
			190		0.0402	0.0444	0.0578	0,0540	3.0711	0.6758	6.6325	
c	and with with the same	41.5	c	0.048	0.081	0.076	0.077	0.088	4.0 64	0.796	0.094	
Ń	gruen, dormant, dryish; little ground showing.		180		0.098	0.119	0.146	0 .150	0.153	0.163	0.160	
4	to state and a most durat film.	42. D	o	0.061	0.057	0.655	0.060	0.063	0.090	\$, 10 4	6.121	
÷	biown oats oll.		180		A. 067	0.090	0.101	900 °C	0.03%	0.096	9. 028	
•7	General areas of the second	40.4	0	0.100	0.693	0.098	0.108	a.120	0.149	C.166		
ř	district laws	39.6	0.		0.103	0.110	0.121	0.139	6.159	0.168		
		39.6	135		0.107	0.125	0.148	0.166	0.175	0.173		
		39.9	130		6.109	0.109	0.119	0.112	0.116	0.125		
2	the state of the second second second	48.5	o	0.113	J.115	0.119	0.125	0. 145	0.194	0.230		
Ċ.		60.1	0.5	•	0.110	0.100	0,115	0.112	0.139	0.147		
	*31000750	46.0	961		9.126	0.141	0.156	0.106	0.172	0.176		

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TABLE B. 1. -- Centinend

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		51.1	180		e. 272	17E.U	6.370	9.422	0.432	0.434	
۲.	Mixed green icrest-decideoue	39.0	>	9.0360	6.0325	1.020.0	5. 0365	0.0235	0.0542		
	(suk) and everymen (pine).	37.0	180		6.041e	0.0493	0.6495	0.0820	0.263		
*	P' e forest.	33.5	IJ	0.0385	0.0395	0.0308	0.0145	0.0346	0020.0		
σ.,	Grave-dry mendow, dense,	3	U	0.0555	6.CB37	t, 1964	0.6252	0.108	0.125		
	anid-summer.	4	08		0.0778	A. 0836	0.101	0.111	0.139		
		45	140		0.116	0.131	5.143	9.153	0.170		
		4 5	270		0.107	0.123	0.134	0.137	0.132		
2	Futtol-ploughed, maint.	\$ 0	Ø	0.0600	6.65%	0.0648		9. 06 63			
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TABLE R. L. --- Continued

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	r		Astmuth angle 3 of the mith of				*	Y	N.		
	Description	Ande	sight relative to the sus	190	166	931	13	8	¥.	8	*
51	<u>Kendove-with crow foct, dense</u> grass with abundant flowers.	\$	08				0.108	0.106			0.133
14	Dry meadowsparse low grass.	\$	06	0.0845			0.0679		0.126		
15.	Dry meadowmore dense low graze.	* 8 \$	8 8 °	0. 0735			0.108 0.144				
16.	Wheat-bafore harvesting.	33	180				0. 0 666 0. 111	4. 274 0. 302			0.373 0.386
12.	Wheshin the flowering period.	5 5	° ô				0.0702	0. 122 0.0063			9, 345 0, 096
જ	Wheth-ther mowing.	50	8					0.135			9.162
19.	Sailpadsol, ploughed, åry.	84 84 84	900 1900				0.1 05 0.1 09 0.179				
ิฆ์	Soilsandy ?am, ploughad, moist.	* * * * *	° 8 9 9				0.203 0.112 0.212 0.180				

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	Description	V	and the second s	198	E	159	A	991	*	8	
21.	Soft seady lottan, ploughed, dry.	45	0	0.153			0.159				
		45	Q 8				0.159				
2	Collection and a stop of carbod.		o	6.0204			0.0574				
4	vet.		196				0.0614				
5 2	art-Mark and . Tell alongtad.	5	o	0.0231			0.0339				
3	dry.	4	06				0.9463				
		£ 5	150				0.0466				
s.	Dirt-flat desert road freshly buil- dored to remere encroaching segs.	42	6	6.236	0.23	0.22	6.234	9.247	0.351	0.271	0.270
*	Otied dirtflet desert roed, ollod, with a light covering of dust.	4	8	5,100	0.102	•.162	0.104	0.109	0.112	0.121	0.124
ġ	Flrlate summer (mature forest); aircraft altitude 300 meters.	45	Ð	0,0319							
<u>7</u> .	Edges of river bank-covered with sparse grass, almost dry. beginning of avnuma.	45	Q	0.146					•		
23.	Alpina meadow-on mountain tops, covered with sparse grias, dried, bevindior of antium.	\$	e	0.0505							

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		2	Astronth single				5 4 5			
	Description	Zenite Ancle	D of the prim of sight relative to the sum	91	281 S	150	361	28	5	
33. 1	Alpine meadouon mountain tope, covered with sparse grass, mowed, dried, beginning of summa.	45	o	0.110						
30°.	Pasture meadow-beginning of sutumn	45	o	0.0806						
51.	Lusa merdowlush dense grass, begaming of autuma.	45	o	0.0707						
32.	Dry meadowsparse dry grass on hills beginning of sutuma.	45	0	0.0780						
33.	Mostiowdonso, low grass, beginzing or autumn, nircrafi altitude 300 motere.	45	c	0.0802						
ž	Shallows of river (in high water) covered with grass.	45	o	0.112				•		
£5.	Mountain sidelow sparse graas, beginning of subinn.	\$	o	0.133						
2	Green-sear road, duety.	45	¢	0.0723						
2	Hilishooabort grama.	45	o	0.116						
34.	Roil-boggy: in boggy areas, very Geno.	45	o	0.0588						

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		Sentth Zentth	Azimuth engle 5 of the path of			Lenith w	•	لا محرد م	j.			
Į	Description	Angle a	sight relative to the sun	180	165	150	135	120	for	18	28	1
33.	Esth-Frey podsol, pioughed, dry.	45	o	6.0529								
40.	Soilblack carth, leached, ploughed, slightly moist.	45	¢	9.0874								
41.	Soitblack earth, rich, ploughed. wet.	45	٥	0.0204								
42.	Sofh-black earth, rich, ploughed, dry.	45	o	0.0291								
43.	Hill slope-bare, dry.	45	o	0.138								
Я.	Turfbare, dry.	45	0	0.0381								
4 5.	Zarth road-heavily trampied, black earth, dry.	45	o	0,0822								
46.	Earth road-trampled, sand, loans.	45 ,	Q	0.9876								
47.	Earth ro ad-grey podsol.	45	Đ	0.102					•			
8	Edge of river beak-bare, dry.	4.5	Ð	0.149								
£ 3.	Wind-eroded place-dry.	45	¢	0.243								
30.	Shallowssand with pebbles, moist,	45	o	0.111								

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Zanth C of the path of the university Zanth C of the path of the university C of the university C of the the university C of the university C of the the university C of the the university C of the university C of the the university C of the the university C of the the university C of the university C of the university C of the university <thc of="" th="" the="" university<=""> C of the univers</thc>		5	TARLE E.		Zenth zer	* •	and of a	j j		-	
Zach road-Jack erth, lanckui400.130Each road-Jack erth, lanckui400.18Each road-Jack erth, lanckui400.18Each road-Tith uaed, cheaturt400.18Each road-futh uaed, cheaturt400.18Each road-futh uaed, cheaturt400.18Each road-futh uaed, cheaturt400.18Each road-futh uaet400.18Road-each vith layer of400.18Road-each vith layer of400.18Road-each vith layer of400.20Road-pared cobbleatone, dry.400.20Road-pared cobbleatone, dry.400.20Road-pared cobbleatone, dry.400.20Road-pared cobbleatone, dry.40.20Road-pared cobleatone, dry.40.20Road-pared cobleatone, dry.40.20Road-pared cobleatone, dry.40.20Road-pared cobleatone, dry.40.20Road-pared cobleatone, dry.40.20Road-pared cobleatone, dry.40.20<	Description	Zenith Anglu a	5 of the path of sight relative to the sun	186 165	130	136	120	105	106	96	
Zitth road-little used, obsetuit- brown azrit.500.184Earth road-little used, obsetuit- brown azrit.600.18Zarth road-trampled, podeol, dry.600.18Zarth road-trampled, podeol, dry.1500.18Zarth road-trampled, poleoni, dry.1600.18Zarth road-trant, vellowiah Efer1500.165Road-trant of Vinzer, yellowiah Efer1500.756Road-pared coblastone, dry.1600.706Stad-pared coblastone, dry.1600.186Stad-pared coblastone, dry.160.186Stad-pared coblastone, dry.160.186Stad-pared read timothy160.186Stage medow-tense grass in mid-100.186Stage medow-tense grass in mid-100.186Stage medow-tense grass in mid-100.186Stage weith dialisies-period of150.186Stage medow-tense160.186Stage weith dialisies-period of160.186Stage we	Earth roadblack earth, leached.	45		0.129							
Zarth read-tramplet, podeol, dry.4500.185Zarth readcovered with layer of loces, dry.4500.169Zearth readcovered with layer of loces, dry.4500.169Readendered with layer of rean.4500.756Readendered with layer of rean.4500.756Readpowel obbilatione, dry.4500.756Readpowel obbilatione, dry.4500.202Meadow with clover and timotity-450.076Meadow with clover and timotity-450.078Meadow with clover and timotity-450.136Meadow with clover and timotity-45 </td <td>Earth roadlittle used, chestrut- brown earth.</td> <td>45</td> <td>0</td> <td>0.184</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>	Earth roadlittle used, chestrut- brown earth.	45	0	0.184							
Zarth rour-rovered with layer of loces, 47y.4500.169Needand of winter, yellowiah after500.756Radiand of winter, yellowiah after500.756Radi-parted cobblaatone, dry.4500.202Radi-parted cobblaatone, dry.4300.0976Radiow with clower and timochyy-500.0976Sedde mendow-dense graas in mide430.0976Marter,45900.186Marter,450.136Graas-young, green.450.136Graas-young, green.450.136	Earth road-trampled, podsol, dry.	45	o	0.198							•
Readand of winter, yellowish after1500.756rain, wrRandpaved cobbleatone, dry.4500Randpaved cobbleatone, dry.45000Randpaved cobbleatone, dry.45000Randpaved cobbleatone, dry.45000Randow (with clower and timothy)-459000Randow (with clower and timothy)-45000Randow (mith clower and timothy)-45000Randow vith datase-period of450000Graas-young, green.450000Graas-young, green.4500010	Earth road-covered with layer of loces, dry.	45	o	0.169							
Road-paved cobblestore, dry.4500.202Road-paved cobblestore, dry.4500.318Mandow (with clover and timothy)-45900.0676Mandow (with clover and timothy)-45900.136Sedge mendow-dense grass in mid-45900.136Sedge mendow-dense grass in mid-45900.136Sedge mendow-dense grass in mid-45900.136Sedge mendow-dense grass in mid-45900.136Sedge with distes-period of45900.130Grass-young, green.45900.149	Roadand of winter, yellowish after rain, wet.	\$	۰	0.736							
Roadpaved cobhlestone, dry.2506.318Mesedow (with clower and timothy)45900.0876Mesedow -dense grasa in mid-45900.186Sedye meedowdense grasa in mid-45900.186Mesedow with delistes-period of abundant flowers.45900.186Grass-ryoung, green.45900.148	Roadpaved cobblestone, dry.	45	O	0.202							
Maedow (with clower and timothy)- 45 30 0.0976 mowed. 5 90 0.196 Sedge meedow-dense grass in mid- 45 90 0.136 Maedow with delstes-period of 45 90 0.130 abundant flowers. 45 90 0.149 Grass-young, green. 45 90 0.149	Ro <u>edpaved</u> cobblestone, dry.	45	0	0.318							
Sedze mendow-dense grass in mid- 45 90 0.156 0.156 surmer. surmer. Meadow with delsies-period of 45 90 0.130 0.130 0.148 0.148	Meadow (with clover and timothy)	45	06			0,0876					
Maedow with dalsies-period of 45 90 0.130 abundant flowers. 45 90 0.149 Graes-young, green. 45 90 0.149	Sedze meadowdense grass in mid- summer.	3	06			0.196					
Graef-ryoung, green. 45 90 0.149	Meedow with delsies-period of ebundant flowers.	45	06			0.130					
135	Grass-young, green.	45	96			0,149					
										135	

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TABLE R. L. - CLEMENS

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			Astimuth angle 8 of the path of			Contra ta	*	path of	145710		
	Description	Angle R	sight relative to the sun	18	165	୦ଟ୍ଟ	\$1	921	103	190	ä
62,	Grasslast year's (dry), spring.	45	8				0.115				
e ,	Grasssummer green.	45	30				0.0796				
5x.	Cley-dry, individual aanaple.	4	90				9.656				
8	Farth mod-muddy and wet.	45	06				0.0548				
a.	Roud-pared cobblearing, dry.	5 4	¢,				9.155				
57.	Raet-rpared cobblestone, . ".	45	ß				0.0598				
5.5	Stoces-restarcd is a rule 🤇	45	05				0. 192				
	randomanipular of the standard and thread because which exercises do a standard										

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TABLE B. 3

DIRECTIONAL LUMINOUS REFLECTANCE OF TERRAIN BACKGROUNDS UNDER OVERCAS'T SKY

		Zenith	Astmuth angle B of the path of			Zenith an	gle ♦ of	peth of	tight			
	Description	Argie A	sight relative to the sun	180	165	150	135	120	105	100	95	4
_	Weedsdense growth, drying and brownish (beginning of autumn).	1	Ŭ6	9.0384		0.0952	0.0476					
~	Pasture meadow-at end of summer.	;	08	0.113		0.163		0.200				
ň	Meadow (with clover and timothy) mowed, wet after rain	;	06				0.101	0.137			0.228	
	Virgia Steppelow grass, burnt by sun, beginning of autumn			0.0819		0.0668		0.100				
ũ.	Soilsancy loam, ploughed, moist		06	0.0562	0.0661	0.0630	0.0934	0.116				
\$	Earth road-trampled, sand losm					0.142						

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TABLE B. 3

DERECTIONAL REFLECTANCE OF A DERT ROAD ILLUMERATED BY A LOW SUN

	بالمراقبة والاستراب أبار المراقبة فالمتعارفين والمراقبة والمراقبة والمراقبة والمراقب والمراقب والمراقب									
		Sun Zentth	Azimuth anglo 5 of the math of			Zenth en	je \$	of path of	ei ght	
	Description	Angle G	sight relative to the sun	180	165	150	136	120	105	001
-	1.004 by	77.8	06	. 230	. 243	185.	. 275	. 314	. 330	.426

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CHANGE IN REFLECTANCE FOR OBSECURED SUN

Sun	α	õ	Directional reflectance for zenith angle of path of sight = 135 ⁰
Unobscured	45	90	.112
Obscured	45	90	.092

TABLE B.5

CHANGE IN REFLECTANCE WITH POSITION OF SUN IN SKY

***				Directi zenith	icnal re angle o	flectan f path c	ce for of sight =
		α	۵	180 ⁰	150 ⁰	120 ⁰	95 ⁰
1.	Low sun	77.8	90	. 230	.264	.314	.458
2.	High sun	42.0	90	, 226	. 229	. 247	.270

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APPENDIX C

EXAMPLE OF THE DETERMINATION OF AZIMUTH ANGLE OF THE PATH OF SIGHT RELATIVE TO SUN

Given the sun azimuth angle β and the observer azimuth angle γ , the azimuth angle δ of the path of sight relative to the sun can be calculated from

> · γ - β F,

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where the region z, β , and δ are illustrated in Figure C. 1. An example illustrating the calculation of δ is given in Figure C. 1.



Fig. C. 1. ---Example Illustrating the Calculation of the Azimuth Angle of the Path of Sight

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APPENDIX D

DERIVATION OF MAXIMUM-LIKE LIHOOD ESTIMATOR OF $\hat{\theta}_1$ and proof that it is unbiased

The distribution derived in Chapter 4 is a negative exponential with an W-stage step function as the conditional detection rate and known location parameters. If a total of a independent subjects have an opportunity to detect we target, an analogy can be drawn between the detection phenomena and reliability applications. In reliability terminology, the equivalent function would be a mechanical systems whose failure rates are an equivalent function. Because of the apove correspondence, this model of Chapter 4 can be used in reliability problems of this nature.

In preservative in notal item put on test (subjects who have an opportunby in down in the partitioned into $N \neq 1$ groups as follows:

> r_1 observers detect the target $in[T_0, T_1]$ r_1 observers detect the target $in[T_1, T_2]$

 \mathbf{r}_{i} observers detect the target in $\left[T_{i}, T_{i+1}\right]$ (0,1)

 r_{N-1} observers detect the target in $[T_{N-1}, T_N]$

$$n = \sum_{m=0}^{N-1} n_{m} \text{ observers detect the target in } \left(T_{N}, 00 \right)$$

The probability fonsity function of detection times, given in Chapter 4 is,

$$\begin{vmatrix} v_{0}e^{-\lambda_{0}t} &, \ 0 \\ \gamma_{0}e^{-\lambda_{0}t} &, \ 0 \\ \gamma_{0}e^{-\lambda_{0}}r_{1} & \lambda_{2}e^{-\lambda_{1}(t-T_{1})} &, \ T_{1} \\ \gamma_{1}e^{-\lambda_{0}}r_{1} & \gamma_{2}e^{-\lambda_{1}(t-T_{2})} &, \ T_{1}e^{-\lambda_{0}}r_{1} \\ \gamma_{2}e^{-\lambda_{0}}r_{1} & \gamma_{2}e^{-\lambda_{1}}r_{2} \\ \gamma_{2}e^{-\lambda_{0}}r_{1} & \gamma_{2}e^{-\lambda_{1}}r_{3} \\ \gamma_{2}e^{-\lambda_{1}}r_{3} & \gamma_{2}r_{3} \\ \gamma_{3}e^{-\lambda_{1}}r_{3} & \gamma_{3}r_{3} \\ \gamma_{4}r_{5} & \gamma_{4}r_{5} \\ \gamma_{4}r_{5} & \gamma_{4}r_{5} \\ \gamma_{4}r_{5} & \gamma_{4}r_{5} \\ \gamma_{4}r_{5$$

p(t).

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$$\begin{bmatrix} -\lambda_{0} T_{1} - \lambda_{1} (T_{2} - T_{1}) - \cdots - \lambda_{t-1} (T_{1} - T_{t-1}) \lambda_{1} e^{-\lambda_{1} (t - T_{1})} + T_{1} \leq t \leq T_{t+1} \\ \vdots \\ \vdots \\ e^{-\lambda_{0} T_{1} - \lambda_{1} (T_{2} - T_{1})} + \cdots + \lambda_{N-2} (T_{N-1} - T_{N-2}) \lambda_{N-1} e^{-\lambda_{N-1} (t - T_{N-1})} \\ e^{-\lambda_{0} T_{1} - \lambda_{1} (T_{2} - T_{1})} + \cdots + \lambda_{N-2} (T_{N-1} - T_{N-2}) \lambda_{N-1} e^{-\lambda_{N-1} (t - T_{N-1})} \\ \end{bmatrix}$$

substituting $\begin{pmatrix} 1 \\ 1 \\ \theta \\ 1 \end{pmatrix}$ into this probability density function, p (t) becomes

¹The maximum likelthood estimator of λ_i turns out to be biased, there tere the reciprocal of λ_i is taken since it is unbiased (Clark, 1968).

$$p(0) : \begin{cases} \frac{1}{\theta_0} \circ \frac{\left(\frac{1}{\theta_0} \cdot \frac{1}{\theta_0} \cdot \frac{$$

The probability of the partitioning given in equation D.1 is

$$P(n; r_0, r_1, \dots, r_{N-1}) \approx K p_0^{r_0} \cdot p_1^{r_1} \cdot \dots \cdot p_{N-1}^{r_{N-1}} \cdot (1 - p_0^{r_0} \cdot p_1^{r_1} \cdot \dots \cdot \frac{r_{N-1}}{N-1})^{\bar{r}}$$

$$(1 - p_0^{r_0} \cdot p_1^{r_1} \cdot \dots \cdot \frac{r_{N-1}}{N-1})^{\bar{r}}$$
here $\bar{r} \approx n - \sum_{m=0}^{N-1} r_m$, and

$$\mathbf{K} = \frac{\mathbf{r}_0 \mathbf{r}_1 \mathbf{r}_1 \cdots \mathbf{r}_{N-1} \mathbf{r}_1}{\mathbf{r}_0 \mathbf{r}_1 \mathbf{r}_1 \cdots \mathbf{r}_{N-1} \mathbf{r}_1}$$

and

$$P_{0} = \frac{T_{1}}{1 - 0} - \frac{T_{1}}{90}$$

$$P_{1} = \left[e^{-\frac{T_{1}}{00}} \right] \left[1 - e^{-\frac{(T_{2} - T_{1})}{91}} \right]$$

$$P_{1} = \left[e^{-\frac{T_{1}}{00}} - \frac{(T_{2} - T_{1})}{91} \right] \left[1 - e^{-\frac{(T_{3} - T_{2})}{92}} \right]$$

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$$P_{i} = \left[e^{-\frac{T_{1}}{\theta_{0}} - (\frac{T_{2} - T_{1}}{\theta_{1}})} - \cdots - \frac{(T_{i} - T_{i-1})}{\theta_{i-1}} \right] \left[1 - e^{-(\frac{T_{i+1} - T_{i}}{\theta_{i}})} \right]$$
$$\vdots$$
$$P_{N-1} = \left[e^{-\frac{T_{1}}{\theta_{0}} - \frac{(T_{2} - T_{1})}{\theta_{1}}} - \cdots - \frac{(T_{N-1} - T_{N-2})}{\theta_{N-1}} \right] \left[1 - e^{-(\frac{T_{N} - T_{N-1}}{\theta_{N-1}})} \right]$$

Given these values of $P_{0^{D}}, \ldots, P_{N-1}$, the probability of the partitioning given in equation (D.1) becomes

$$P(r_{0}, ..., r_{N-1}, \overline{r} | n) = \begin{pmatrix} -\frac{T_{1}}{\theta_{0}} \end{pmatrix}^{1} \cdot \begin{pmatrix} -\frac{T_{1}}{\theta_{0}} \end{pmatrix}^{1} \cdot \begin{pmatrix} -\frac{T_{1}}{\theta_{0}} \end{pmatrix}^{1} \cdot \begin{pmatrix} -\frac{T_{2}-T_{1}}{\theta_{1}} \end{pmatrix}^{1} \cdot \\ & -\frac{(T_{2}-T_{1})}{\theta_{1}} \end{pmatrix}^{1} \cdot \\ & \begin{pmatrix} \left[e^{-\frac{T_{1}}{\theta_{0}} - \frac{(T_{3}-T_{1})}{\theta_{1}} \right] \left[1 - e^{-\frac{(T_{3}-T_{2})}{\theta_{2}}} \right]^{1/2} \cdot \\ & \cdot \dots \cdot \left[\left[e^{-\frac{T_{1}}{\theta_{0}} - \frac{(T_{2}-T_{1})}{\theta_{1}} - \frac{(T_{N-1}-T_{N-2})}{\theta_{N-2}} \right] \right] \\ & \begin{bmatrix} 1 - e^{-\frac{(T_{N}-T_{N-1})}{\theta_{N-1}}} \end{bmatrix}^{1/2} \cdot \\ & \left[(1 - P_{0} - P_{1} - \dots - P_{N-1})^{\frac{T}{2}} \right] \\ & \end{bmatrix}$$

and
$$\overline{\mathbf{r}} = -\sum_{i=1}^{N-1} \mathbf{r}_{in}$$

 $\mathbf{m} = 0$

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Assum, g independence of the individual detection times, the conditional density at obtaining the ordered observations $t_1^{(0)}, \ldots, t_{x_0}^{(0)}$, given r_0 and $t_j^{(0)} \leq T_1$ $P\left(t_{1}^{(0)}, \dots, t_{r_{0}}^{(1)} \mid t_{j}^{(0)} \leq T_{1}, r_{0}\right) = \frac{\prod_{j \neq 1}^{r_{0}} \left(\frac{1}{\theta_{0}} e^{-\frac{t_{j}^{(0)}}{\theta_{0}}}\right)}{\left(-e^{-\frac{T_{1}}{\theta_{0}}}\right)^{r_{0}}}$

woularly for the second time interval, the conditional density of obtaining the ordered observations $t_1^{(1)}, \ldots, t_r^{(1)}$ given r_1 and $T_1 \leq t_j^{(1)} \leq T_2$ is given by: $P\left(t_{1}^{(1)}, \dots, t_{r_{1}}^{(1)} \mid T_{1} \leq t_{j}^{(1)} \leq T_{2}, r_{i}\right) = \frac{\prod_{\substack{i=1 \ i=1 \$

For the third time interval,

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$$P\left(t_{1}^{(3)}, \dots, t_{r2}^{(2)} \mid T_{2} \leq t_{j}^{(2)} \leq T_{3}, r_{2}\right) = \frac{r_{2}}{\prod_{j=1}^{r} \left(\frac{1}{\theta_{2}} - e^{-\frac{(t_{1}^{(2)} - T_{2})}{\theta_{2}} - \frac{T_{1}}{\theta_{0}} - \frac{(T_{2} - T_{1})}{\theta_{1}}\right)}{\left(\left[e^{-\frac{T_{1}}{\theta_{0}} - \frac{(T_{2} - T_{1})}{\theta_{1}}\right]\left[-\frac{-(T_{3} - T_{2})}{\theta_{2}}\right]\right)^{r_{2}}}$$

and so on; for i = 3, ..., N - 1.

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then follows that the likelihood, L, for the sample is

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$$= \frac{n!}{r_0! \cdots r_{N-1}! \vec{r}!} \int_{j=1}^{r_0} \left(\frac{1}{\theta_0} \exp\left[-\frac{t_1}{\theta_0}\right] \right) \int_{j=1}^{r_1} \left(\frac{1}{\theta_1} \exp\left[-\frac{(t_j^{(1)} - T_1 - T_1)}{\theta_1} - \frac{T_1}{\theta_0}\right] \right)$$
$$= \frac{r_2}{\eta_1} \left(\frac{1}{\theta_2} \exp\left[-\frac{(t_j^{(2)} - T_2)}{\theta_2} - \frac{T_1}{\theta_0} - \frac{(T_2 - T_1)}{\theta_1}\right] \right) \cdots$$
$$= \frac{r_1}{\eta_{j=1}} \left(\frac{1}{\theta_1} \exp\left[-\frac{(t_j^{(1)} - T_1)}{\theta_1} - \frac{T_1}{\theta_0} - \frac{(T_1 - T_{1-1})}{\theta_{1-1}}\right] \right) \cdots$$
$$= \frac{r_{N-1}}{\eta_{j=1}} \left(\frac{1}{\theta_{N-1}} \exp\left[-\frac{(t_j^{(N-1)} - T_{N-1})}{\theta_{N-1}} - \frac{T_1}{\theta_0} - \frac{(T_1 - T_{N-1})}{\theta_{N-1}} - \frac{T_1}{\theta_{N-2}} \right) \right]$$

aking the natural logarithim of both sides and differentiating with respect to i_1 (i = 1, ..., N-1), we obtain

$$\frac{\partial \ln L}{\partial \theta_0} = \frac{-r_0}{\theta_0} + \frac{1}{\theta_0^2} \sum_{j=1}^{r_0} t_j^{(0)} + \frac{(n-r_1)T_1}{\theta_0} = 0$$

which yields

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$$\Theta_0 = \frac{\sum_{j=1}^{r_0} t_j^{(0)} + (n - r_1) T_1}{r_0}$$

 $\frac{\partial \ln L}{\partial \theta_{1}} = -\frac{r_{1}}{\theta_{1}} + \frac{1}{\theta_{1}^{2}} \sum_{j=1}^{r_{0}} (t_{j}^{(1)} - T_{1}) + \frac{(n - r_{1} - r_{2}) (T_{2} - T_{1})}{\theta_{1}^{2}} = 0$ $\frac{\sum_{j=1}^{r_{1}} (t_{j}^{(1)} - T_{1}) + (n - r_{1} - r_{2}) (T_{2} - T_{1})}{r_{1}}$

 $\frac{\partial \ln L}{\partial \theta_2} = 0$

which yields,

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 $\theta_{2} = \frac{\sum_{j=1}^{r_{2}} (t_{j}^{(2)} - T_{2}) + (n - r_{1} - r_{2} - r_{3}) (T_{3} - T_{2})}{r_{2}}$ $\theta_{2} = \frac{\sum_{j=1}^{r_{1}} (t_{j}^{(2)} - T_{2}) + (n - r_{1} - r_{2} - r_{3}) (T_{3} - T_{2})}{r_{2}}$ $\frac{\partial}{\partial} \frac{\ln L}{\theta_{1}} = 0$ which yields, $r_{i} = \frac{\sum_{j=1}^{r_{1}} (t_{j}^{(1)} - T_{1}) + (n - \sum_{k=0}^{i} r_{k})(T_{i+1} - T_{i})}{r_{i}}$

(D. 2)

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A physic of insurprotation of the training term,

$$\frac{1}{k^{n+1}} = \frac{1}{k^{n+1}} = \frac{1}{r_{k}} + \frac{1}{r_{k}$$

is the analogs φ equation is that observers which have not detected by time T_{i+1} , for r_i) of them, any never detect, so the sum of their cantalative search transf

$$(x - \sum_{k=0}^{1} r_k)(T_{i=1} - T_i)$$

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up to doe and of the i^{th} time interval must be averaged over all of the observers which subout in the interval (T_i, T_{i+1}) to raise the average. Equation D.2 is an estimate of the recurriccal of the conditional detection rate, λ_i , in the time interval (T_i, T_{i+1}) . A proof that this estimate is unbiased is given below.

As unitiased estimates, $\hat{\theta}$, has the property that the expected value of $\hat{\theta}$ is square to the true value of the parameter θ (Hogg and Crarg, 1960), i.e.,

$$\mathbf{E} \stackrel{\wedge}{(\mathbf{0})} = \mathbf{0}$$

Given k ordered observations x_1, \ldots, x_k of s items placed on test, Johnson and Leone (1966) show that the distribution $p(y_k)$ of

$$\mathbf{y}_{k} = \sum_{i=1}^{k-1} x_{i} + (s - k + 1) x_{k}$$
(D.3)

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$$\mathbf{p}(\mathbf{y}_{k}) = \left(\frac{\lambda^{k}}{\left(\mathbf{k}\right)}\right) \mathbf{y}_{k}^{k-1} \mathbf{e}^{-\lambda \mathbf{y}_{k}}$$
(D.4)

which is $(2\lambda)^{-1}$ times a χ^2 with 2k degrees of freedom. In the case of the maximum-likelihood estimator given by equation D.2, $n - \sum_{m=0}^{i} r_m$ observers are available for detection in the interval $[T_i, T_{i+1}]$, and only r_i of them do detect. If there are a large number of detection times in each interval $t_{r_i}^{(i)}$, the final detection time in $[T_i, T_{i+1})$ approaches T_{i+1} , and equation D.2, the estimate of θ_i , becomes

$$h_{i} = \frac{\sum_{m=1}^{r_{i-1}} (t_{m}^{(i)} - T_{i}) + \left((n - \sum_{j=1}^{i-1} r_{j}) - r_{i} + 1 \right) (t_{r_{i}}^{(i)} - T_{i})}{r_{i}}$$
(D.5)

which is of the same form as equation D.3 with $x_i = (t_m^{(i)} - T_i)$, $s = (n - \sum_{j=1}^{i-1} r_j)$, $k = r_i$, and $x_k = (t_{r_i}^{(i)} - T_i)$. Johnson and Leone (1966) also state that the conditional distribution of a quantity $(x_i - X)$ given $x_i > X$, is the same as the unconditional distribution of x_i . Using this fact, the expected value of $\hat{\theta}$, (Equation D.5) is gamma distributed, and

$$\mathbf{E} \left(\stackrel{\wedge}{\boldsymbol{\Theta}} \right) = \frac{\boldsymbol{\Theta}_{i} \mathbf{r}_{i}}{\mathbf{r}_{i}} = \stackrel{\boldsymbol{\Theta}}{\boldsymbol{\Theta}}_{i}$$

which proves the unbiasedness.

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