

AFFDL-TR-79-3042

2
P.S.

ADA075215

LEVEL #

THE SCALING OF BIRD IMPACT LOADS

Antonios Challita
John P. Barber
University of Dayton Research Institute
300 College Park Avenue
Dayton, Ohio 45469

June 1979

DDC
RECEIVED
OCT 22 1979
A

TECHNICAL REPORT AFFDL-TR-79-3042
Final Report for Period 16 January 1978 - 16 February 1979

DDC FILE COPY

Approved for public release; distribution unlimited.

Best Available Copy

AIR FORCE FLIGHT DYNAMICS LABORATORY
AIR FORCE WRIGHT AERONAUTICAL LABORATORIES
AIR FORCE SYSTEMS COMMAND
WRIGHT-PATTERSON AIR FORCE BASE, OHIO 45433

79 10 19 043

NOTICE

When Government drawings, specifications, or other data are used for any purpose other than in connection with a definitely related Government procurement operation, the United States Government thereby incurs no responsibility nor any obligation whatsoever; and the fact that the Government may have formulated, furnished, or in any way supplied the said drawings, specifications, or other data, is not to be regarded by implication or otherwise as in any manner licensing the holder or any other person or corporation, or conveying any rights or permission to manufacture, use, or sell any patented invention that may in any way be related thereto.

This report has been reviewed by the Information Office (IO) and is releasable to the National Technical Information Service (NTIS). At NTIS, it will be available to the general public, including foreign nations.

This technical report has been reviewed and is approved for publication.


ROBERT E. MCCARTY
Project Engineer


R. HARLEY WALKER
Group Leader
Subsystems Development
Group

FOR THE COMMANDER


AMBROSE B. NUTT
Director
Vehicle Equipment Division

Copies of this report should not be returned unless return is required by security consideration, contractual obligations, or notice on a specific document.

UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

19 REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM	
1. REPORT NUMBER AFFDL TR-79-3042	2. GOVT ACCESSION NO. ✓	3. RECIPIENT'S CATALOG NUMBER	
6. TITLE (and Subtitle) THE SCALING OF BIRD IMPACT LOADS		9. PERIOD COVERED Final Technical Report 16 Jan 1978 - 16 Feb 1979	
7. AUTHOR Antonios Challita John P. Barber		14. UDR-TR-79-23	
9. PERFORMING ORGANIZATION NAME AND ADDRESS University of Dayton Research Institute 300 College Park Avenue Dayton, Ohio 45469		15. F33615-78-C-3402 NNN	
11. CONTROLLING OFFICE NAME AND ADDRESS Air Force Flight Dynamics Laboratory AF Wright Aeronautical Labs, AFSC Wright-Patterson Air Force Base, OH 45433		10. PROGRAM ELEMENT PROJECT, TASK AREA & WORK UNIT NUMBERS Prog. Ele. 62201F Proj. 2402, Task 240203 Work Unit 24020318	
14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office)		12. REPORT DATE Jun 1979	
12. 67		13. NUMBER OF PAGES 67	
15. SECURITY CLASS. (of this report) Unclassified		15a. DECLASSIFICATION DOWNGRADING SCHEDULE	
16. DISTRIBUTION STATEMENT (of this Report) Approved for public release; distribution unlimited.			
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report) (16) 2402 (17) 03			
18. SUPPLEMENTARY NOTES			
19. KEY WORDS (Continue on reverse side if necessary and identify by block number) bird impact, birdstrike, impact loading, foreign object damage, modelling			
20. ABSTRACT (Continue on reverse side if necessary and identify by block number) → This report describes an experimental study which was conducted to investigate the loads produced by the impact of 1800 g and 3600 g birds. Both real birds and bird simulants were tested. Impact pressures were measured and compared with smaller bird impact results obtained on previous testing programs. The magnitude of the impact pressures was found to be independent of bird size. The temporal and spatial distribution of impact pressures			

Full

UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

↙ scaled linearly with bird dimensions. The impact behavior of large birds was consistent with flow models developed to describe small bird impacts. It was concluded that large and small birds display the same fundamental impact loading processes and that these processes are adequately described by the previously developed flow model.

↗

Accession No.	
NTIS	<input checked="" type="checkbox"/>
Unannounced	<input type="checkbox"/>
Justification	
By	
Distribution/	
Availability Codes	
Dist	Avail and/or special
A 23	9

UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

FOREWORD

This report describes a contractual work effort conducted by personnel of the Impact Physics Branch, Experimental and Applied Mechanics Division, University of Dayton Research Institute, Dayton, Ohio under Project 2402, "Vehicle Equipment Technology," Task 240203, "Aerospace Vehicle Recovery and Escape Subsystems," Work Unit 24020318, "Simulation of Bird Impact on Aircraft Transparencies."

The work reported herein was performed during the period 16 January 1978 to 16 February 1979 under the direction of Dr. John P. Barber, the principal investigator. The Air Force project engineer was Mr. Robert E. McCarty (AFFDL/FER). The report was released by the authors in March 1979.

This report is one of three which will be published under contract number F33615-78-C-3402. The remaining two will deal with the effects of bird attitude upon impact loads, and development of a substitute bird for testing respectively and will be released as the work is completed.

TABLE OF CONTENTS

SECTION		PAGE
I	INTRODUCTION	1
II	EXPERIMENTAL TECHNIQUES	4
	2.1 Launch Techniques	4
	2.2 Velocity, Location, and Orientation Measurement	7
	2.3 Pressure Measurements and Recording	8
III	EXPERIMENTAL RESULTS	11
	3.1 Introduction	11
	3.2 Impact Duration	16
	3.3 Initial Impact Pressure	16
	3.4 Steady Flow Pressures	22
IV	CONCLUSIONS AND DISCUSSION	33
	APPENDIX	35
	REFERENCES	56

LIST OF ILLUSTRATIONS

FIGURE		PAGE
1	Compressor Storage Tank and Driving Tank Systems	5
2	The Vent Section Muffler and Stripper Tube	7
3	Instrumentation Section	9
4	Typical Pressure-Time Record of Nominal 1800 g Gelatin with 10% Porosity	13
5	Typical Pressure-Time Record of Nominal 3600 g Gelatin with 10% Porosity	14
6	Typical Pressure-Time Record of Nominal 1800 g Real Bird (chicken)	15
7	The Phases of Bird Impact: (a) Initial Impact, (b) Impact Decay; (c) Steady Flow; and (d) Termination	17
8a	Initial Impact (Hugoniot) Pressures versus Impact Velocity for Nominal 1800 g Real Bird (chicken) at Normal Impact	19
8b	Initial Impact (Hugoniot) Pressure versus Impact Velocity for Nominal 1800 g and 3600 g Gelatin at Normal Impact	19
9a	Initial Impact (Hugoniot) Pressures versus Impact Velocity for Nominal 1800 g Real Bird (chicken) at 45° Impact	20
9b	Initial Impact (Hugoniot) Pressures versus Impact Velocity for Nominal 1800 g and 3600 g Gelatin with 10 Percent Porosity at 45° Impact	20
10a	Initial Impact (Hugoniot) Pressures versus Impact Velocity for Nominal 1800 g Real Bird (chicken) at 25° Impact	21
10b	Initial Impact (Hugoniot) Pressures versus Impact Velocity for Nominal 1800 g and 3600 g Gelatin at 25° Impact	21
11	Density Profiles for 4-lb Simulant Birds Prepared with Different Techniques	23

LIST OF ILLUSTRATIONS (CONT'D)

FIGURE		PAGE
12	Shock and Release Waves in Fluid Impact	25
13	Flow Geometry at Oblique Impact	26
14	Normalized Steady Flow Pressure Distribution of Nominal 1800 g and 3600 g Gelatin with 10% Porosity Along Major Axis at Normal Impact	28
15	Normalized Steady Flow Pressure Distribution of Nominal 1800 g and 3600 g Gelatin with 10% Porosity Along Major Axis at 45° Impact	28
16	Normalized Steady Flow Pressure Distribution of Nominal 1800 g and 3600 g Gelatin with 10% Porosity Along Major Axis at 25° Impact	29
17	Normalized Steady Flow Pressure Distribution of Nominal 1800 g Real Bird (chicken) Along Major Axis at Normal Impact	31
18	Normalized Steady Flow Pressure Distribution of Nominal 1800 g Real Bird (chicken) Along Major Axis at 45° Impact	31
19	Normalized Steady Flow Pressure Distribution of Nominal 1800 g Real Bird (chicken) Along Major Axis at 25° Impact	32

LIST OF SYMBOLS

a	Radius of projectile
ID	Inside diameter
m	Mass
OD	Outside diameter
P, P_p	Measured peak pressure
P_H	Hugoniot pressure
P_s	Stagnation pressure
r	Radial distance from center of impact
t	time
v, V	Impact velocity
V_n	Normal component of impact velocity
V_s	Shock velocity
ρ	Density of projectile
ρ_0	Density of material with zero porosity

LIST OF UNITS

Mass	g (gram)	= 0.0022046 lb _m (pound-mass)
	kg (kilogram)	= 10 ³ g
Length	m (meter)	= 3.2808 ft (feet) = 39.37 in (inches)
	cm (centimeter)	= 0.01 m = 2.54 in
	mm (millimeter)	= 0.001 m
Time	s (second)	
	μs (microsecond)	= 10 ⁻⁶ s
Force	N (Newton)	= 0.2248 lb _f (pounds-force)
	MN (Meganewton)	= 10 ⁶ N
Density	kg/m ³	= 0.0624 lb _m /ft ³ = 3.613 x 10 ⁻⁵ lb _m /in ³
Pressure	MN/m ²	= 10 bars = 145.04 lb _f /in ²
Frequency	Hz (hertz)	
	kHz (kilohertz)	= 10 ³ Hz

SECTION I INTRODUCTION

Collisions between birds and aircraft have proved to be an expensive and persistent problem to the United States Air Force. The severity of the problem has increased as high-speed, low-altitude aircraft missions have evolved. Windshield, canopy, and support structures have proved to be particularly vulnerable to birdstrike. Not only are these parts of the aircraft sensitive to impact damage, but the consequences of damage on pilot performance are severe. A number of aircraft and pilots have been lost due to birdstrike on windshields, canopies, and support structures.

The birdstrike vulnerability of the crew enclosure and transparencies in Air Force aircraft has resulted in a number of redesign programs. These redesign programs have usually been conducted in an iterative build and test mode. This method of design is extremely expensive and time consuming. The Air Force has, therefore, developed an interest in modern structural design techniques applied to the windshield birdstrike problem. This approach to the birdstrike design task involves the use of modern finite element structural analysis techniques. These techniques have been adapted to analyze the transient dynamic events such as birdstrike. The structural analysis techniques themselves have undergone extensive development over the years and have become highly reliable and efficient structural design tools. In order to adequately predict response, however, these techniques require good definition of the material properties and accurate descriptions of the transient impact loads. This report deals with the description of impact loads for use with finite element codes.

The University of Dayton Research Institute (UDRI) began work on the characterization of bird impact loads in January

of 1974. This work was jointly sponsored by the Air Force Materials Laboratory (AFML) and the Air Force Flight Dynamics Laboratory (AFFDL). A continuing effort has been conducted on the measurement and characterization of bird impact loads since that time. The original work, documented in Reference 1, developed the basic experimental techniques which were used throughout the program to obtain bird impact load data. This program concentrated on small birds (up to 120 g) and impacts at normal incidence. Work was continued on the measurement of small bird impact pressures. The data were more thoroughly analyzed and presented in Reference 2. This report identified the basic processes of bird impact and provided the first quantitative measurements of the pressures and forces involved. The work was extended and reported in Reference 3, which described in great detail the impact behavior of birds. Extensive data on birds weighing up to 600 g were reported. Some data for birds up to 4 kg were also obtained. The basic fluid behavior of birds during impact was identified and quantified. The development of the first satisfactory bird impact flow models was reported and the techniques necessary for proper scaling of the impact loads with bird size were identified. A more detailed theoretical base for bird impact modelling was described in Reference 4. This work presented a more detailed analysis of

¹Barber, J.P. and J.S. Wilbeck, "The Characterization of Bird Impacts on a Rigid Plate: Part I," AFFDL-TR-75-5, ADA021142, January 1975.

²Peterson, R.L. and J.P. Barber, "Bird Impact Forces in Aircraft Windshield Design," AFFDL-TR-75-150, ADA026-628, March 1976.

³Barber, J.P., H.R. Taylor, and J.S. Wilbeck, "Bird Impact Forces and Pressures on Rigid and Compliant Targets," AFFDL-TR-77-60, ADA061-313, May 1978.

⁴Wilbeck, J.S., "Impact Behavior of Low Strength Projectiles," AFML-TR-77-134, ADA060-423, July 1978.

the basic process of bird impact and provides the theoretical basis for bird impact modelling as a fluid process. Additional impact work was conducted under an Air Force Aero Propulsion Laboratory contract and is reported in Reference 5. This report presented a much more careful experimental investigation of impact loads using simulated birds and ice. Careful measurements were made and agreement with prediction of the theoretical model was found to be excellent.

All of the work described above was conducted with, and based on, data produced with birds weighing 600 g or less. Although scaling derived from theoretical considerations worked extremely well over the range of bird masses from 60 g to 600 g, there was still some concern about the applicability of these models to birds with masses in the range from 1800 g to 3600 g. In particular, the 1800 g birds represent the standard design case for aircraft transparencies. It was, therefore, deemed necessary to collect experimental data on 1800 g and 3600 g birds to ensure that the theoretical models developed for use with structural element codes were applicable for this size bird. This report describes the experimental measurements made on 1800 g and 3600 g birds. The scaling relationships derived in the previous programs were checked and found to adequately describe the impact of these large birds.

⁵Bauer, D.P. and J.P. Barber, "Experimental Investigation of Impact Pressures Caused by Gelatin Simulated Birds and Ice," UDR-TR-78-114, November 1978.

SECTION II

EXPERIMENTAL TECHNIQUES

The experimental work described in this report was conducted at the University of Dayton Research Institute. This section contains a description of the experimental techniques used to obtain temporally resolved pressure measurements during bird impact onto a rigid plate. Descriptions of the experimental range and launch technique, target instrumentation, and data collection are given in the sections that follow.

2.1 LAUNCH TECHNIQUES

For experimental investigations of bird impact, a launch technique is necessary which can accelerate birds of the required mass to the required velocities. The birds must be launched with controlled orientation (preferably with zero pitch and yaw), and such that they do not break up or severely distort prior to impact. A launch technique was developed with which birds of up to 3.6 kg could be launched to velocities up to approximately 300 m/s.

The system consisted of a 177.8 mm bore compressed air gun with supporting compressor, instrumentation, and control systems. The compressor system consisted of a 1.42 m³/min, 3.5 MN/m² compressor pumping into a 0.11 m³ intermediate storage tank. The intermediate storage tank was connected via a flexible hose and quick disconnect coupler to the large air storage tank used for driving the gun. The driving air storage tank had a capacity of approximately 0.85 m³. There was a valve system located between the driving air storage tank and the breech of the gun. This valve system was designed to valve the high pressure air from the driving storage tank into the gun to

operate the gun. The valve was a standard butterfly valve system with a pneumatic actuator. The breech end of the gun, together with the compressor storage tank and driving tank systems, is shown in Figure 1.

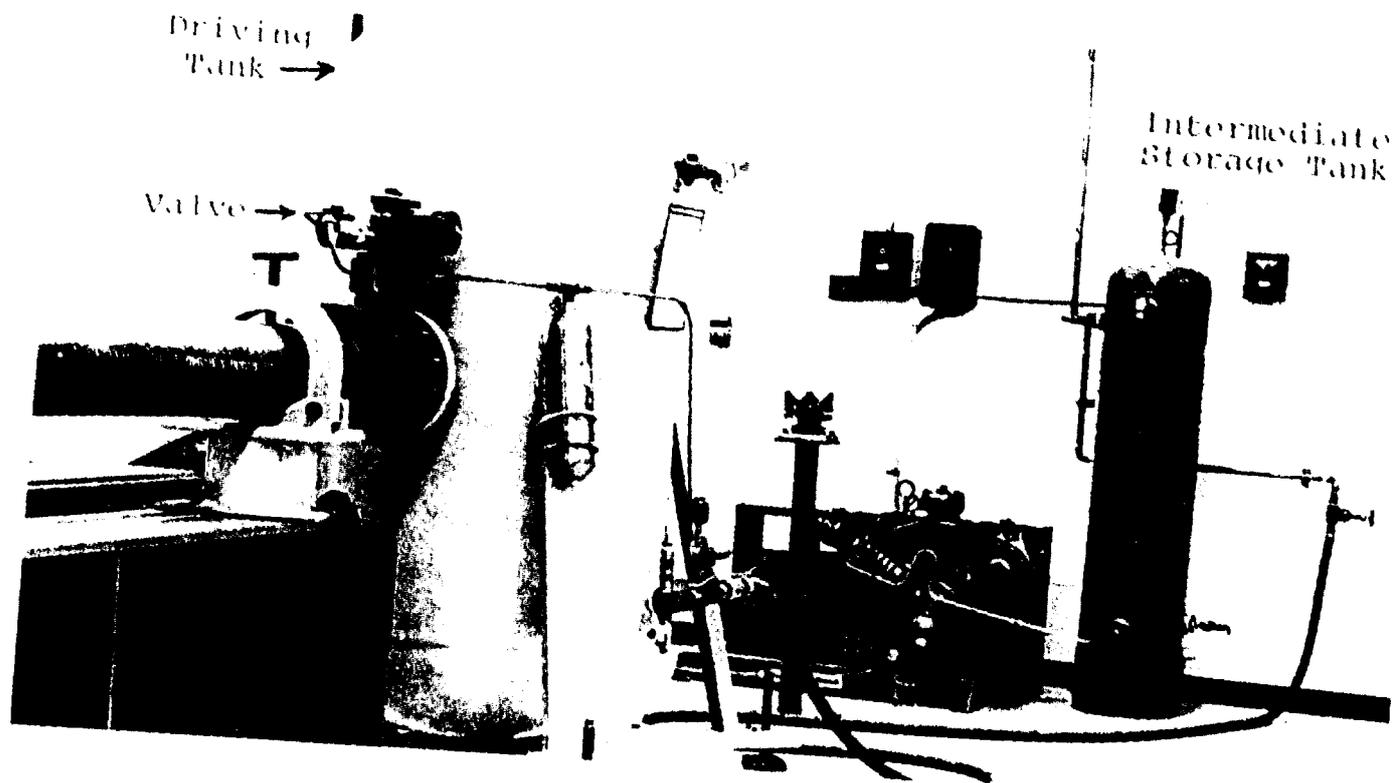


Figure 1. Compressor Storage Tank and Driving Tank Systems

The gun itself consisted of two, 4.88 m long, 177.8 mm ID heavy wall tubes. They were connected together via a locating ring and flange system. The tubes were supported on two heavy l-beams bolted to the floor. A vent section was connected to the muzzle of the gun tube and was designed to release the driving pressure from the back of the projectile package. This vent section was enclosed in a muffler which deflected the venting gases harmlessly towards the floor.

The birds were placed in a sabot, or carrier, for launching. The sabot was a 177.8 mm OD foam plastic cylinder. Foam plastic was employed, as a substitute of balsa wood, after identifying

several unsatisfactory characteristics of the original balsa wood sabots. There is only one supplier of balsa wood in the United States, and the sizes and quantities which could be supplied were only marginally satisfactory for these large sabots. 180 mm balsa planking was not available, so up to nine smaller planks had to be bonded together to form a work piece large enough to fabricate these sabots. This fabrication technique produced sabots which were only marginally strong enough. They often broke during fabrication. The molded plastic sabots proved completely satisfactory for launching birds over the range of sizes and velocities used in this study. They are light, strong and very dimensionally stable.

As the sabot represents a significant fraction of the launch mass, it must be stripped from the bird before the bird impacts the target. Accordingly, a tapered tube sabot stripping section was connected to the muzzle end of the vent section. The sabot stripper tube consisted of a steel tube with an initial ID of 177.8 mm that was progressively reduced. A series of longitudinal wide slots were cut into the stripper tube to facilitate the rapid release of the driving pressure, thus reducing the forces required to decelerate and stop the sabot. When the launch package entered the sabot stripper tube, the sabot was progressively decelerated until it stopped. The bird released from the sabot pocket and continued on trajectory to the target. For the high velocity shots, an extension to the stripper tube was required. It consisted of nine bars welded around a ring and connected to the stripper tube through a flange system. The vent section muffler and stripper tube are shown in Figure 2. The sabot stripper functioned satisfactorily over the entire range of masses and velocities which were used in this program.

Free flight observations of the bird showed that the bird was oscillating after sabot separation. This oscillation was apparently initiated by the release of the bird from the sabot. To assist in the smooth release of the bird, holes were drilled in the base of the sabot. These holes permit the driving pressure

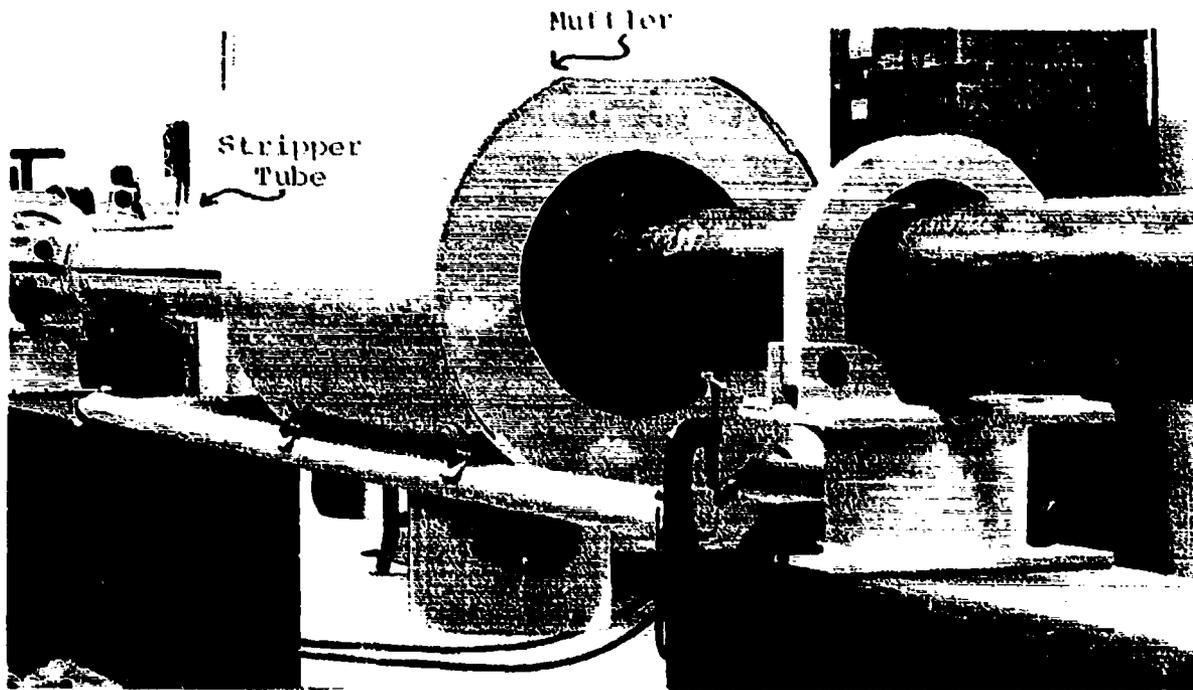


Figure 2. The Vent Section Muffler and Stripper Tube

to act on the base of the bird itself. Therefore, the bird was both pushed and pulled out of the sabot during the separation process. This technique appeared to greatly reduce the bird oscillation problem.

2.2 VELOCITY, LOCATION, AND ORIENTATION MEASUREMENT

The velocity of the bird was measured prior to impact using a simple time of flight technique. Between the muzzle of the sabot stripper and the target, two helium/neon laser beams were directed across the trajectory. When the bird interrupted the first laser beam, a counter was started. The counter was stopped when the bird interrupted the second laser beam. The distance between the laser beams and the elapsed time were used to calculate the velocity. To increase the accuracy of the velocity measurements, monitor bird orientation, determine projectile impact location on target, and verify bird integrity

prior to impact, two orthogonal pulsed x-ray systems were set up at each laser beam station. The resulting radiographs of the bird in flight were used to accurately establish the position of the bird with respect to the laser beam and to monitor the condition and orientation of the bird. The accurate determination of projectile location and orientation relative to the target is necessary to properly describe the pressure distribution. Using this technique, velocities could be measured to within one percent, projectile impact location on target could be determined to within about 1.25 cm, and orientation to within ± 0.5 degrees. Bird disintegration during launch was extremely rare and was not an experimental problem. The instrumentation described above is shown in Figure 3.

2.3 PRESSURE MEASUREMENTS AND RECORDING

The impact shock pressures can be extremely high, the duration of the impact is relatively short and there could be important transient pressure excursions. The pressure sensing devices must be capable of measuring and withstanding these high pressures and the pressure sensing and recording equipment must have adequate bandwidth to detect and record important pressure transients.

Piezoelectric quartz pressure transducers were used as the basic sensing devices for these experiments. These transducers have a compact impedance converter physically located in the coaxial line close to the crystal, and they have a specified bandwidth from 0 to 80 kHz. Since these transducers are not specifically designed for impact testing, calibration was necessary to verify their operation. In Reference 1 Barber gives details of calibration techniques in his report. The

¹Barber, J.P. and J.S. Wilbeck, "The Characterization of Bird Impacts on a Rigid Plate: Part 1," AFFDL-TR-75-5, ADA021142, January 1975.

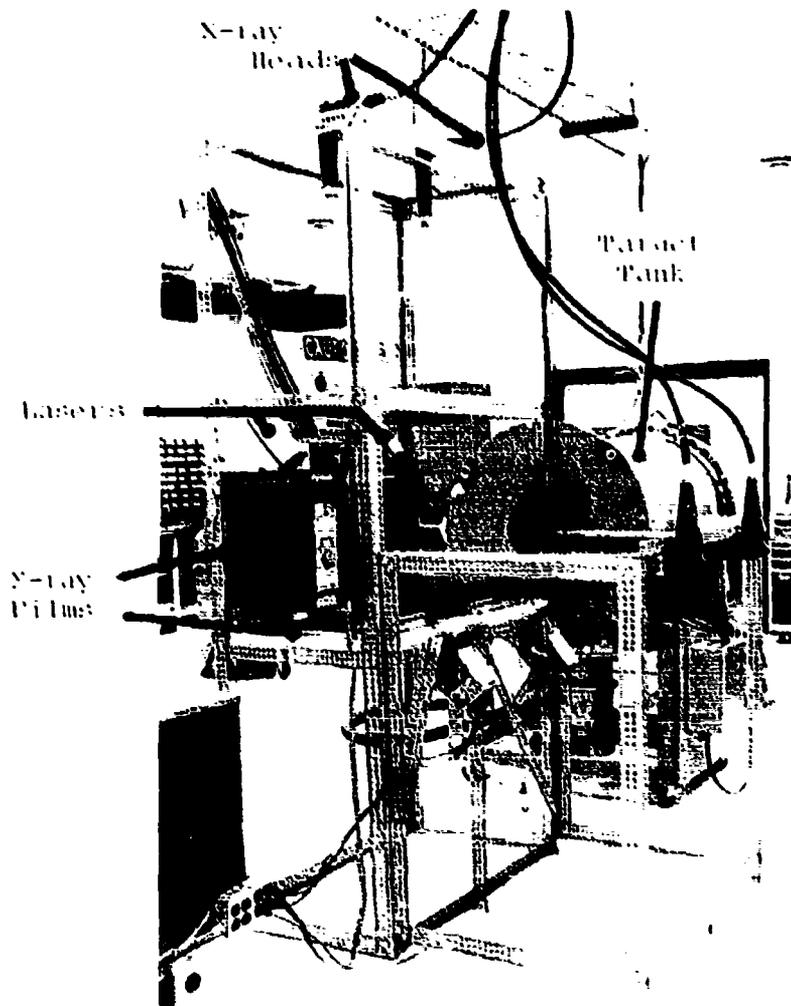


Figure 3. Instrumentation Section

transducers were mounted flush with the surface of a heavy steel plate. Up to nine transducers were simultaneously mounted in the plate on orthogonal axes.

The pressure signals were recorded using an electronic digital memory system. This system uses an analog to digital signal converter. The system has a 200 kHz sample rate, and each channel can store 2048 data points in shift registers. The pressure signals were displayed on an oscilloscope, as a function

of time, and the time interval of interest determined. Then, digital data over these intervals was recorded on a cassette and could be printed out on an electronic data terminal. This technique significantly increased the accuracy and reliability of the data.

SECTION III EXPERIMENTAL RESULTS

A total of 83 data shots were performed to investigate the scaling of bird impact loads. The objective was to demonstrate that the scaling relationships which worked extremely well over the range of bird masses from 60 to 600 g, were applicable to bird masses ranging from 1800 to 3600 g. The projectiles used in these tests included birds (chickens) and bird substitutes (porous gelatin). They were impacted at three impact angles (90° , 45° , 25°) and at velocities ranging from 100 m/s to 300 m/s. The substitute birds were right circular cylinders with a length to diameter ratio of approximately two.

The time varying pressure data were collected using a digital data memory system as described in Section II. From these recorded data, measurements were made to obtain peak pressure and steady flow pressure. The results of these measurements together with comparisons to theoretical results and measurements from impacts of smaller size birds and bird substitutes reported by Barber in Reference 3 and Bauer in Reference 5 are presented in the following sections.

3.1 INTRODUCTION

Birds independent of their masses can be assumed to be right circular cylinders with a length to diameter ratio greater

Barber, J.P., H.R. Taylor, and J.S. Wilbeck, "Bird Impact Forces and Pressures on Rigid and Compliant Targets," AFFDL-TR-77-60, ADA061-313, May 1978.

Bauer, D.P. and J.P. Barber, "Experimental Investigation of Impact Pressures Caused by Gelatin Simulated Birds and Ice," ODR-TR-78-114, November 1978.

than two, and to behave like fluids during impacts. These two basic assumptions provide the basis for understanding the scaling of bird impact loads.

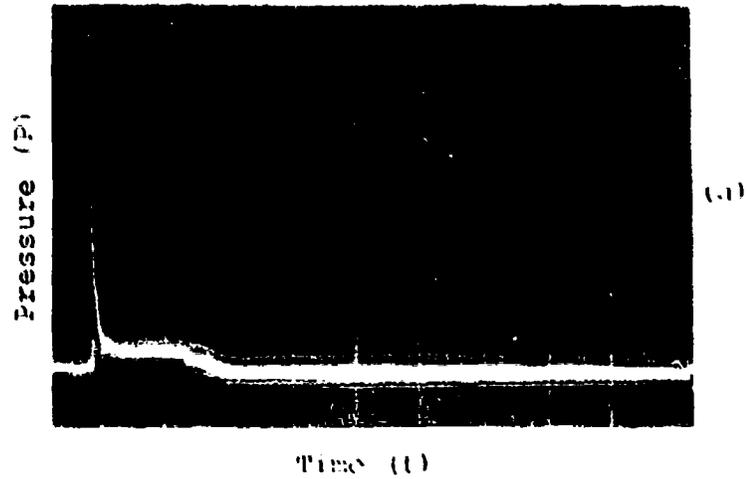
Because the impact process is basically fluid dynamic, the characteristic pressures are the Hugoniot, or impact, pressure and the flow, or stagnation, pressure. Both of these pressures depend only on the impact velocity and the material properties of the bird (i.e., density and shock velocity). The magnitudes of these pressures should not vary with bird size, however, the spacial and temporal distribution of pressure should. Since birds of different mass are, however, geometrically similar (i.e., they have similar length to diameter ratios), pressure distributions should scale linearly with bird dimensions. That is, pressure distributions should depend only on normalized distances (where normalization is carried out with a bird dimension such as diameter or length). This was, in fact, shown in Reference 3 for birds and Reference 5 for substitute birds up to 600 g.

Bird and gelatin impacts on a steel target plate may be considered as soft body impacts since the stresses generated during impact substantially exceed the strength of the projectile but are well below the strength of the target material. Pressure records obtained from such impacts are shown in Figure 4, 5 and 6. Figures 4 and 5 show typical pressure traces from normal and oblique impact of a nominal 1800 g and 3600 g right circular cylindrical gelatin projectile. Figure 6 shows similar pressure traces from impacts of a real bird (chicken). The two pressure

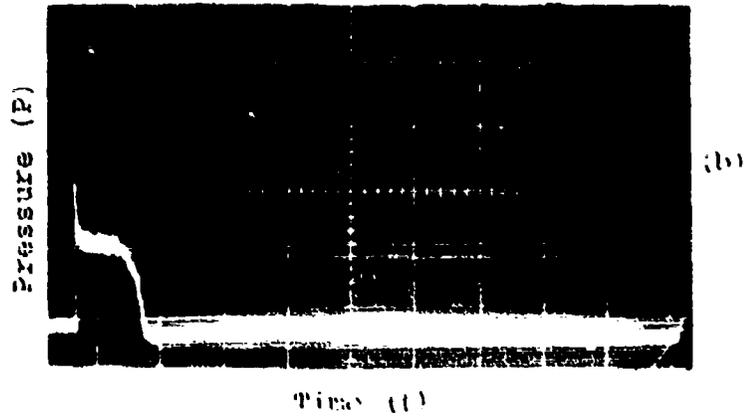
¹Barber, J.P., H.R. Taylor, and J.S. Wilbeck, "Bird Impact Forces and Pressures on Rigid and Compliant Targets," AFFDL-TR-77-60, ADA061-313, May 1978.

²Bauer, D.P. and J.P. Barber, "Experimental Investigation of Impact Pressures Caused by Gelatin Simulated Birds and Ice," UDR-TR-78-114, November 1978.

$V = 105 \text{ m/s}$
 $m = 1750 \text{ g}$
 $P = 18.5 \text{ MN/m}^2\text{-cm}$
 $t = 2000 \text{ } \mu\text{s/cm}$



$V = 199 \text{ m/s}$
 $m = 1840 \text{ g}$
 $P = 14.5 \text{ MN/m}^2\text{-cm}$
 $t = 2000 \text{ } \mu\text{s/cm}$



$V = 203 \text{ m/s}$
 $m = 1800 \text{ g}$
 $P = 13.1 \text{ MN/m}^2\text{-cm}$
 $t = 2000 \text{ } \mu\text{s/cm}$

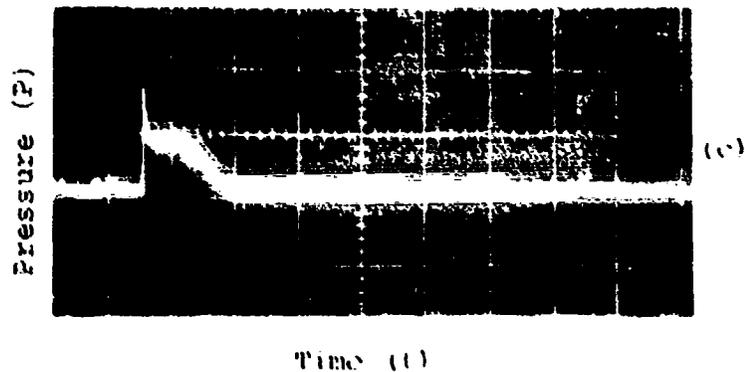
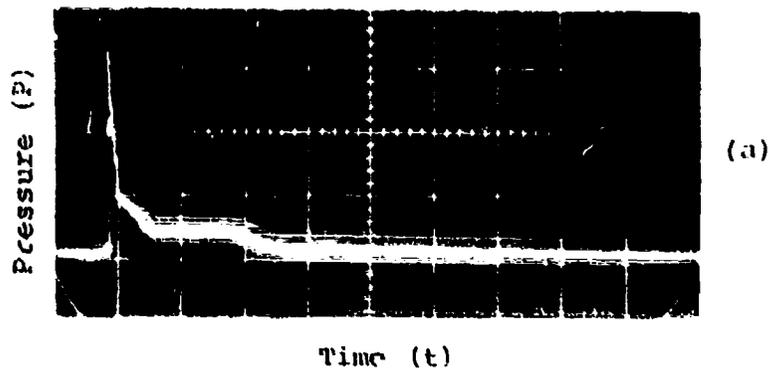
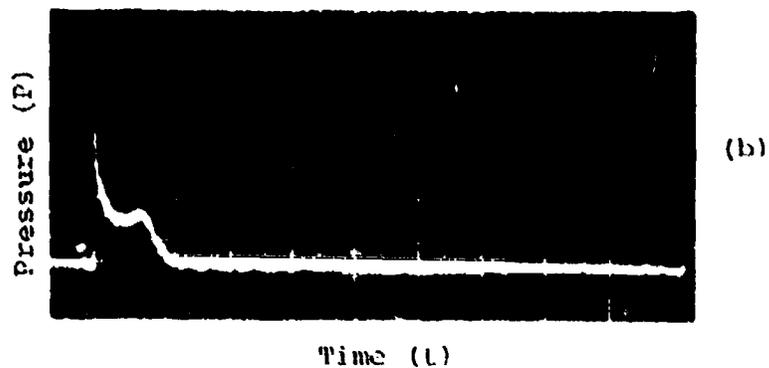


Figure 4. Typical Pressure-Time Record of Nominal 1800 g Gelatin with 10% Porosity. (a) 90° impact, center transducer; (b) 45° impact, 3" below center; (c) 25° impact, center transducer.

$V = 245 \text{ m/s}$
 $m = 3220 \text{ g}$
 $P = 32.8 \text{ MN/m}^2\text{-cm}$
 $t = 2000 \text{ } \mu\text{s/cm}$



$V = 115 \text{ m/s}$
 $m = 3490 \text{ g}$
 $P = 16.6 \text{ MN/m}^2\text{-cm}$
 $t = 2000 \text{ } \mu\text{s/cm}$



$V = 190 \text{ m/s}$
 $m = 3550 \text{ g}$
 $P = 13.1 \text{ MN/m}^2\text{-cm}$
 $t = 2000 \text{ } \mu\text{s/cm}$

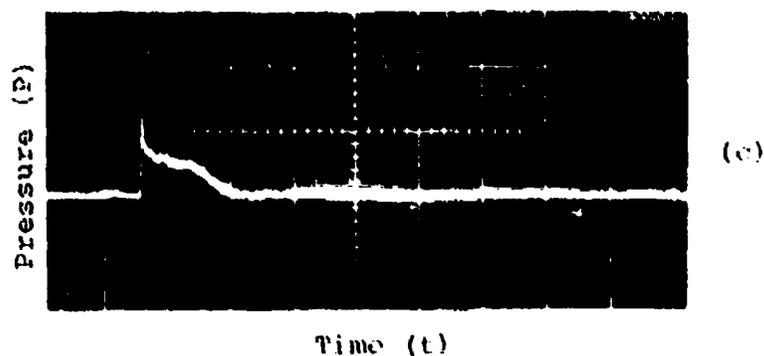
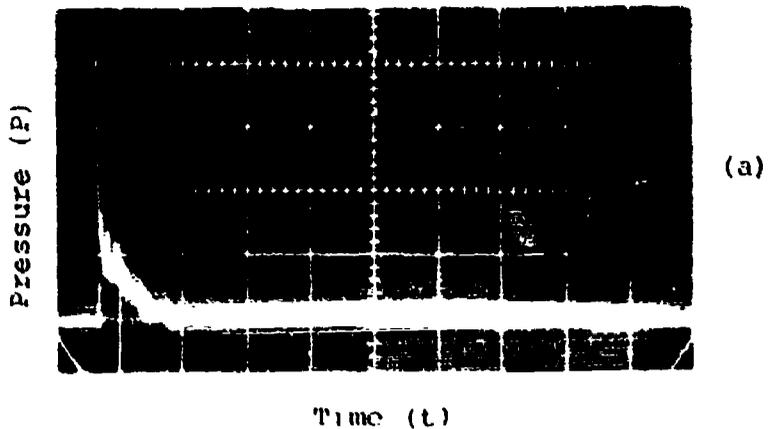
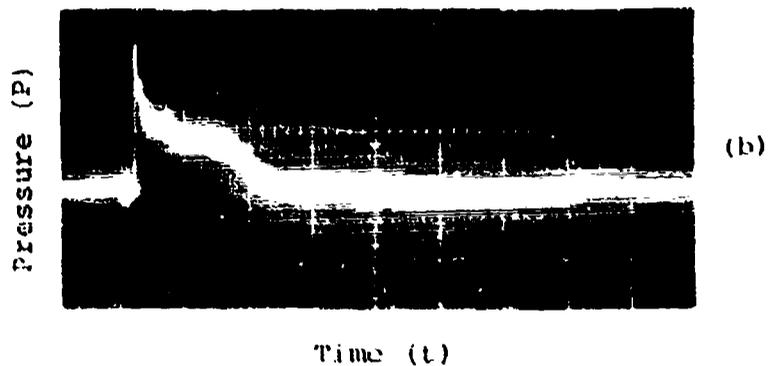


Figure 5. Typical Pressure-Time Record of Nominal 3600 g Gelatin with 10% Porosity. (a) 90° impact, 1" above center; (b) 45° impact, center transducer; (c) 25° impact, center transducer.

$V = 289 \text{ m/s}$
 $m = 1560 \text{ g}$
 $P = 46.3 \text{ MN/m}^2\text{-cm}$
 $t = 2000 \text{ } \mu\text{s/cm}$



$V = 104 \text{ m/s}$
 $m = 1560 \text{ g}$
 $P = 5.2 \text{ MN/m}^2\text{-cm}$
 $t = 2000 \text{ } \mu\text{s/cm}$



$V = 273 \text{ m/s}$
 $m = 1560 \text{ g}$
 $P = 13.1 \text{ MN/m}^2\text{-cm}$
 $t = 2000 \text{ } \mu\text{s/cm}$

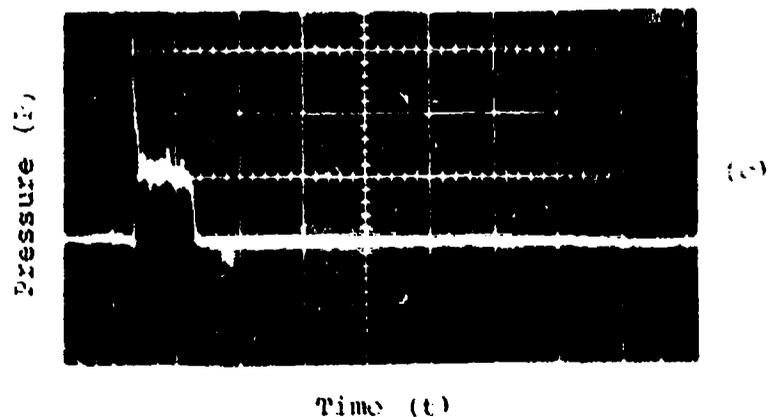


Figure 6. Typical Pressure-Time Record of Nominal 1800 g Seal Bird (chicken). (a) 90° impact, center transducer; (b) 45° impact, center transducer; (c) 25° impact, center transducer.

levels of interest on these traces are the peak pressure and the steady flow pressure.

The peak pressure is due to a shock wave formed from the initial impact, and is mainly a function of the normal component of impact velocity and the projectile's properties. The steady flow pressure occurs when the initial shock wave is overtaken by the release waves formed from the pressure gradient along the projectile's edge. The phases of the impact process are shown in Figure 7.

3.2 IMPACT DURATION

The time duration of impact of birds was first derived by Barber in Reference 3 and was found to equal the projectile length divided by the impact velocity. The same results were found during this experimental program. These results also agree with the results presented by Bauer in Reference 5 during his experimental investigation on simulated birds.

3.3 INITIAL IMPACT PRESSURE

During the initial impact, the particles on the front surface of the projectile are instantaneously brought to rest relative to the target face and a shock propagates into the projectile. As the shock wave propagates into the projectile, it brings the material behind the shock to rest. The pressure in the shock compressed region is initially very high and is uniform across the impact area. The pressure behind the shock,

⁴Barber, J.P. and H.R. Taylor, and J.S. Wilbeck, "Bird Impact Forces and Pressures on Rigid and Compliant Targets," AFFDL-TR-77-60, ADA061-313, May 1978.

⁵Bauer, D.P. and J.P. Barber, "Experimental Investigation of Impact Pressures Caused by Gelatin Simulated Birds and Ice," GDR-TR-78-114, November 1978.

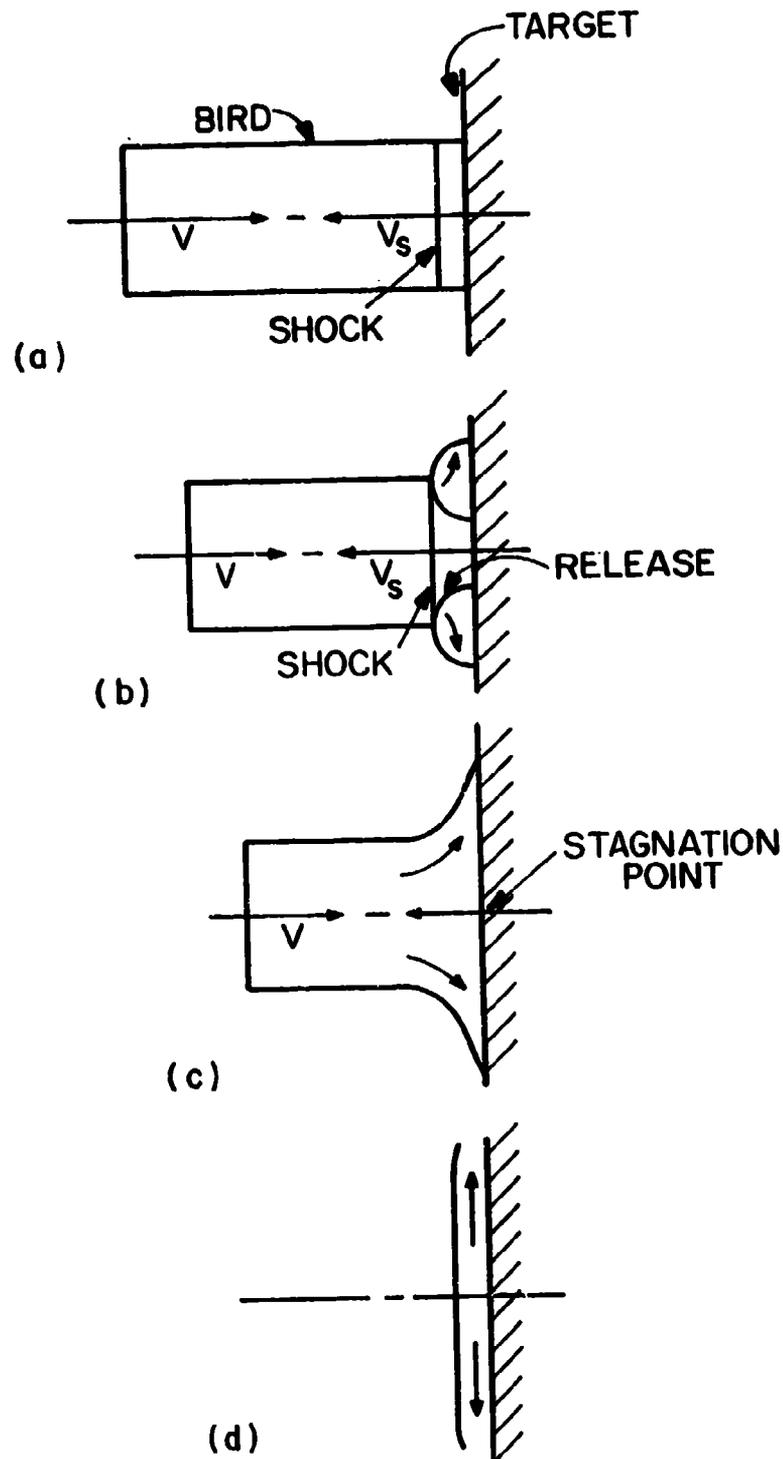


Figure 7. The Phases of Bird Impact: (a) Initial Impact, (b) Impact Decay; (c) Steady Flow; and (d) Termination

(the Hugoniot pressure) is:

$$P_H = \rho V_s V_n \quad (1)$$

where ρ is the density of the projectile, V_s is the shock velocity, and V_n is the normal component of impact velocity. The relation between the shock velocity V_s and the normal component of impact velocity V_n for gelatin with 10 percent porosity was derived by Wilbeck in Reference 4. The initial impact pressures measured for all normal and oblique impacts for bird and gelatin are presented in Figures 8, 9, and 10. The measured impact pressures for normal impact for nominal 1800 g real bird agree very well with the calculated pressures. The agreement is better than the experimental results from small birds reported by Barber in Reference 3. The small bird data were probably affected by the limited bandwidth (80 kHz) of the transducers. The shock pulse was barely defined for the large birds (see Figures 4-6). Shock pulse duration was only about half as long for the small bird impacts, and the peaks may have been clipped. The measured shock pressures for normal impact for gelatin with 10 percent porosity are well above those anticipated. The shock pressures approached those expected for pure gelatin and were up to twice as high as those expected for the porous gelatin bird simulant material. A thorough investigation was conducted and the source of these extremely high and unexpected pressures was determined and eliminated during the later shots.

It was found that the part of the bird initially striking the target was essentially pure gelatin. Birds were launched

⁴Wilbeck, J.S., "Impact Behavior of Low Strength Projectiles," AFML-TR-77-134, ADA060-423, July 1978.

³Barber, J.P., H.R. Taylor, and J.S. Wilbeck, "Bird Impact Forces and Pressures on Rigid and Compliant Targets," AFFDL-TR-77-60, ADA061-313, May 1978.

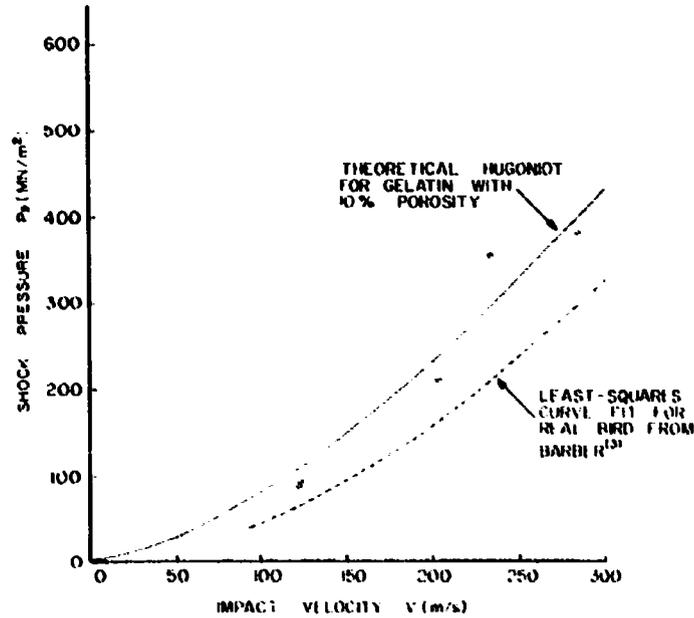


Figure 8a. Initial Impact (Hugoniot) Pressures versus Impact Velocity for Nominal 1800 g Real Bird (chicken) at Normal Impact

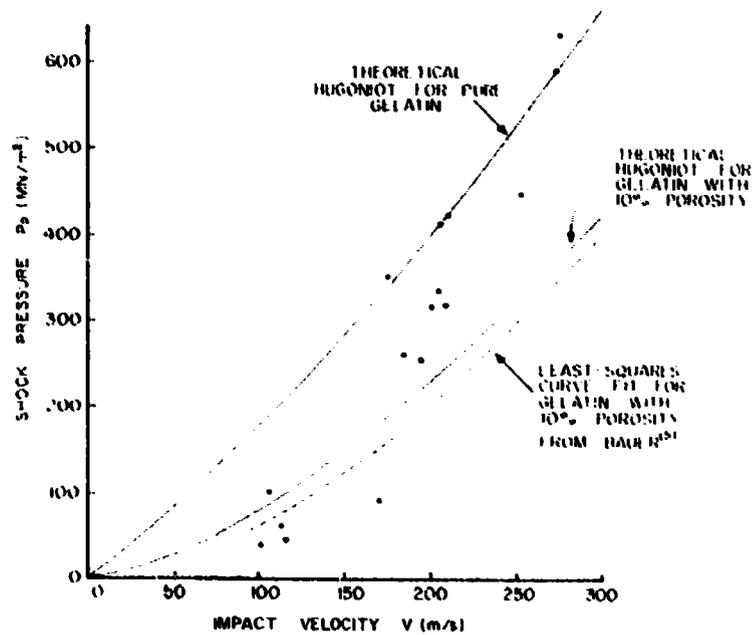


Figure 8b. Initial Impact (Hugoniot) Pressure versus Impact Velocity for Nominal 1800 g and 3600 g Gelatin at Normal Impact. Points show data from this program.

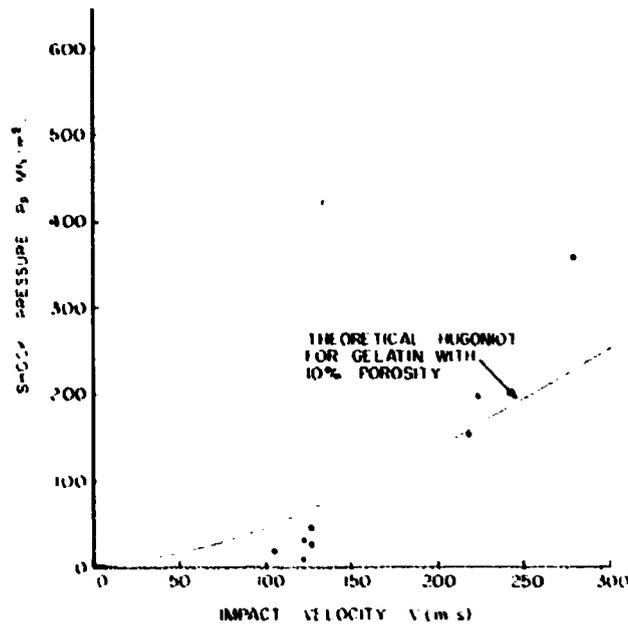


Figure 9a. Initial Impact (Hugoniot) Pressures Versus Impact Velocity for Nominal 1800 g Real Bird (chicken) at 45° Impact

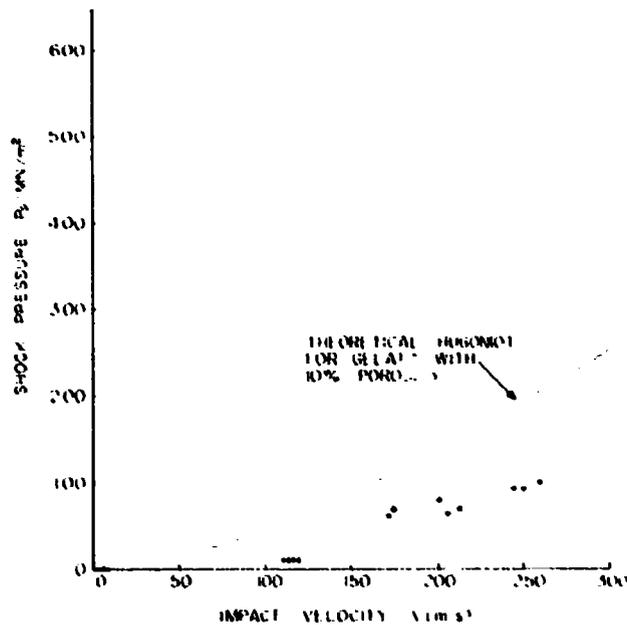


Figure 9b. Initial Impact (Hugoniot) Pressures Versus Impact Velocity for Nominal 1800 g and 3600 g Gelatin with 10 Percent Porosity at 45° Impact

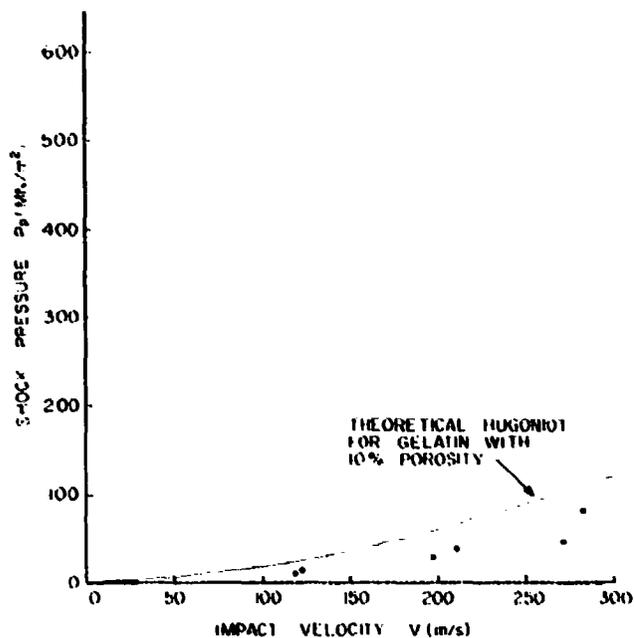


Figure 10a. Initial Impact (Hugoniot) Pressures versus Impact Velocity for Nominal 1800 g Real Bird (chicken) at 25° Impact

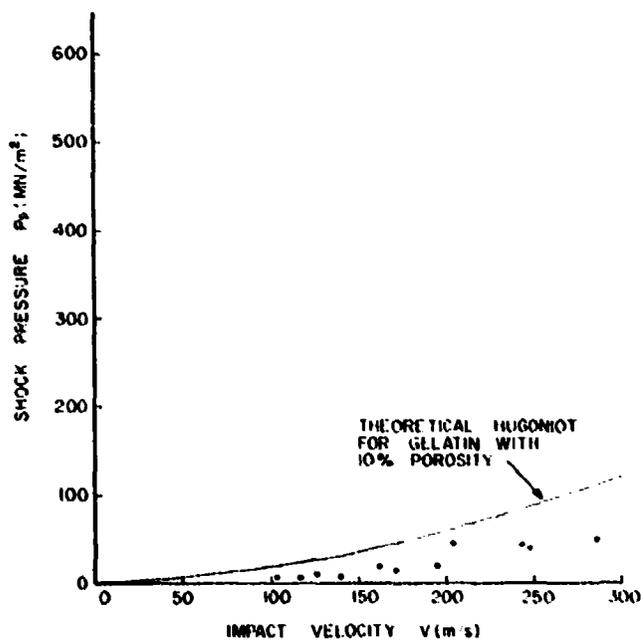


Figure 10b. Initial Impact (Hugoniot) Pressures versus Impact Velocity for Nominal 1800 g and 3600 g Gelatin at 25° Impact.

such that the end of the bird which first struck the target was the end that was at the bottom of the mold during the molding process. The presence of pure gelatin at the bottom of the mold was due to the tendency of the phenolic microballoons, which were used to provide porosity, to float out of the gelatin during the curing process. This was confirmed by making density measurements along the axis of the bird. The results for several processes are shown in Figure 11. Pure gelatin was found at the bottom of the mold and extremely low density gelatin at the top of the mold. Numerous different processing techniques were tried in an attempt to eliminate the density gradients from the bird. As can be seen from Figure 11, good density uniformity was obtained in many cases but in general the density was too low. Efforts to increase density always resulted in increased density gradients. As a result of this investigation, birds were molded some 30 percent longer than the nominal bird length and approximately 15 percent was trimmed from each end. This technique produced density variations which fell between acceptable limits. To further insure that the very high peak pressures were not produced, birds were launched top end (low density end) first. These changes produced better behavior in the later oblique shots. The measured impact pressures for oblique impact for gelatin and real birds are, as expected, lower than the calculated values. In addition, low recorded peak pressure during oblique impacts may have also been caused by the relatively shorter duration of the shock pulse in these impacts. As pointed out earlier, the limited bandwidth of the transducers can result in a significant attenuation of the measured signals. For 25° and 45° impacts, the initial impact pressure spike was much less pronounced than for 90° impacts.

3.4 STEADY FLOW PRESSURES

As the shock wave propagates into the projectile, the material at the edge of the projectile is subjected to a very high pressure gradient. This pressure gradient causes the

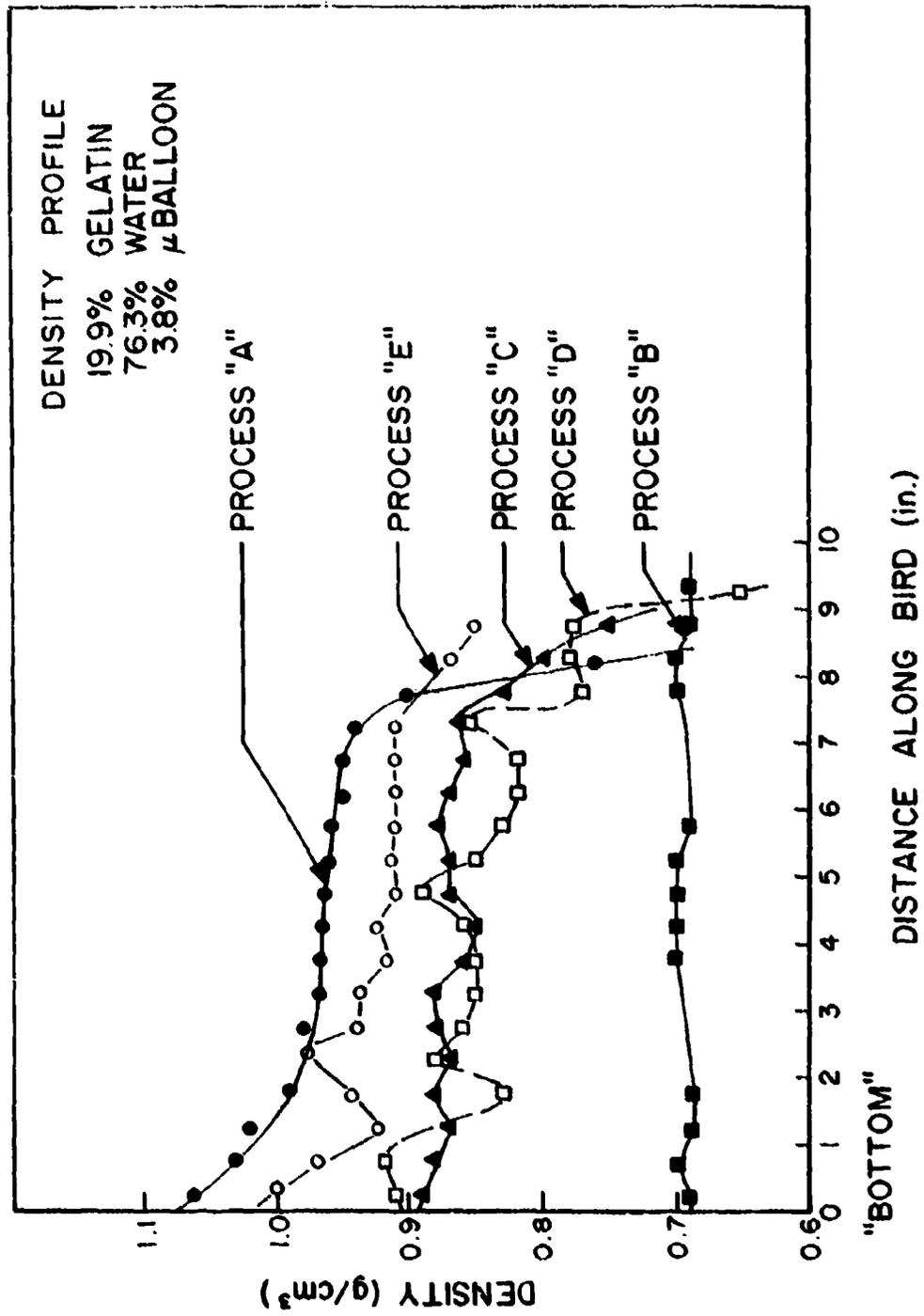


Figure 11. Density Profiles for 4lb Simulant Birds Prepared with Different Techniques

material to be accelerated radially outward, and release waves propagate inward. The function of these release waves is to relieve the radial pressure gradient in the projectile. Release waves travel into the projectile, eventually overtaking the initial shock wave. The release process for a cylinder is shown in Figure 12. As the radial pressure decreases during the shock pressure decay, shear stresses develop in the projectile material. These shear stresses are greater than the shear strength of the material and are sufficient to cause "flow". Then, the bird can be considered to behave as a fluid. After several reflections of the release waves, a condition of steady flow is established. A constant pressure and velocity field is set up in the projectile and remains until the end of the projectile reaches the target surface. This steady-state phase is usually indicated by a pressure plateau on the pressure traces. As could be seen in Figures 4, 5, and 6, a large amount of high frequency "noise" was superimposed on the pressure profiles, which made it hard to identify the plateau and to make an accurate measurement of steady-state pressure. Therefore, an average value of the pressure was measured and used in presenting the pressure distributions. This noise was investigated in Reference 4 by Wilbeck and might have been caused by the break-up or tearing of the material (creation of new surfaces) during impact or by the acceleration loads on the gauges caused by the pressure plate vibrations.

Using potential flow theory, Wilbeck calculated, in Reference 4, the steady-state pressure for a bird impact at normal incidence. The pressure at the center of impact was found to equal the stagnation pressure which was approximated by:

$$P_s = \frac{1}{2} \rho_0 V^2 \quad (2)$$

"Wilbeck, J.S., "Impact Behavior of Low Strength Projectiles," AFML-TR-77-134, ADA060-423, July 1978.

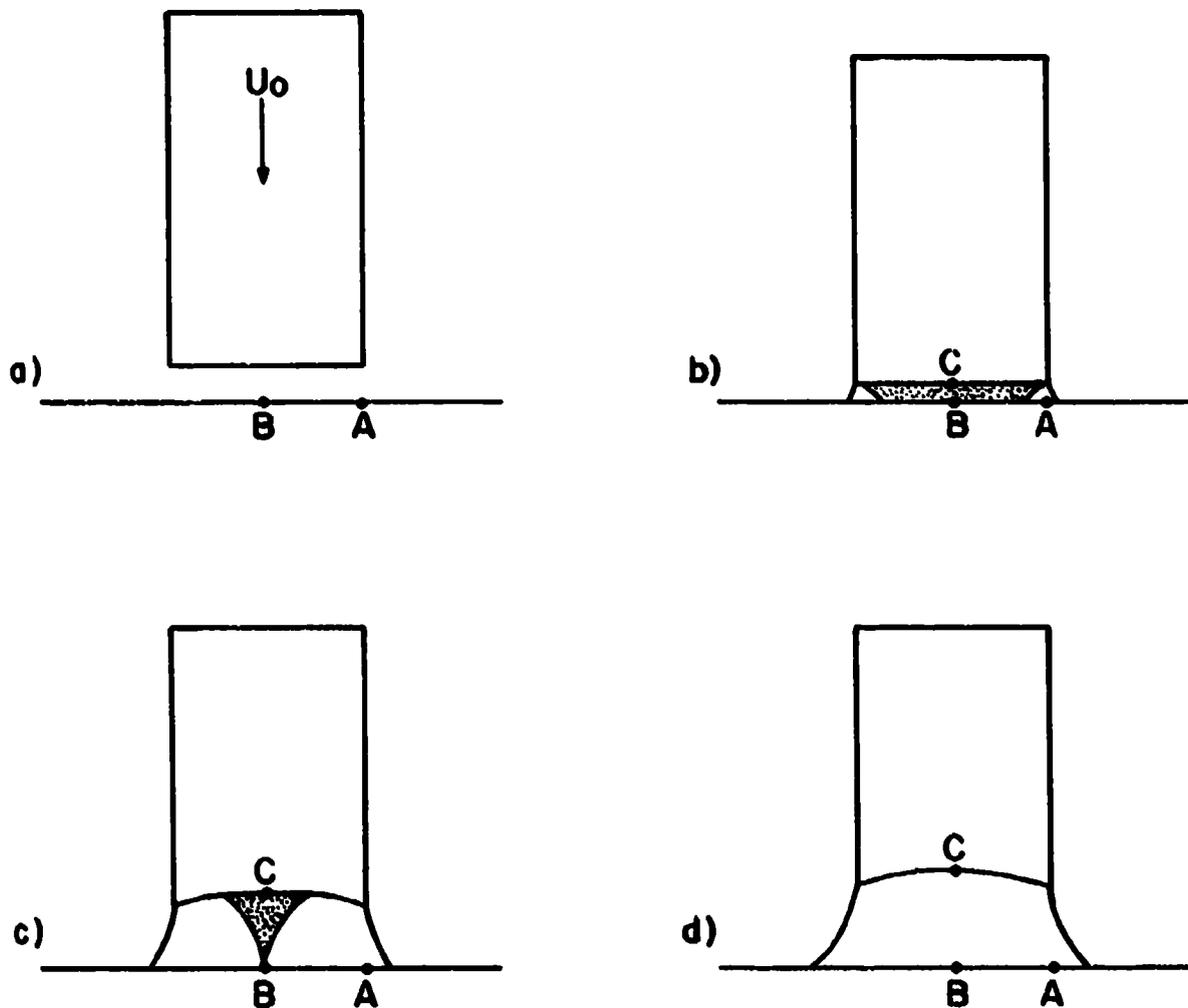


Figure 12. Shock and Release Waves in Fluid Impact. (a) before impact; (b) shocked region just after impact; (c) release waves have converged on Point B, the axis of the cylinder; (d) release waves have just caught the center of the shock, Pt. C.

where ρ_0 is the density of the material with zero porosity and v is the impact velocity. The stagnation pressure is the highest pressure during the steady flow regime and is an important factor in scaling bird impact loads, since it is used to nondimensionalize the steady flow pressure distribution.

For oblique impact, the majority of fluid will flow "downstream" on the obtuse side of the impact. The stagnation point shifts "upstream" to the acute side of the center of impact as shown in Figure 13. As long as a stagnation point exists, the

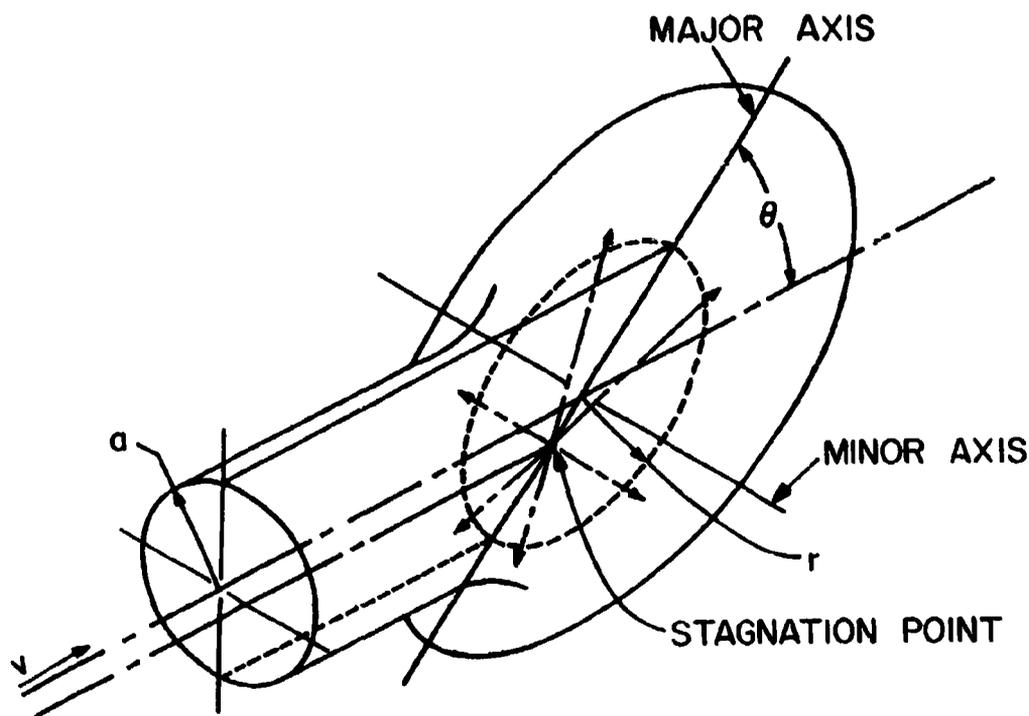


Figure 13. Flow Geometry at Oblique Impact

full stagnation pressure will occur at the stagnation point regardless of angle of impact. However, the distribution of pressure along the surface will be greatly dependent on the impact angle. The distribution of pressure in an oblique cylindrical impact is difficult to analyse because it is a

three-dimensional fluid dynamic problem. In Reference 6, Boehman used potential flow theory to develop a computer model for predicting the pressure distribution produced by the steady state flow of a cylindrical jet impacting on a rigid flat plate. The code utilizes a source density distribution on the surface of the plate and solves for the pressure distribution necessary to make the normal velocity zero on the boundary. Originally, the input to this program consisted of the coordinates of points describing the body surface. For our purposes, the code was modified to generate a grid describing the plate, where the size of the grid depends on the mass of the bird and the angle of impact. A listing of the modified code along with a sample input and output data is presented in the Appendix. The experimental pressure data measured in this task is compared to those theoretical curves and to the experimental data from Reference 3 by Barber and Reference 5 by Bauer in the following sections.

3.4.1 Gelatin Artificial Birds

Figures 14, 15, and 16 show the nondimensionalized steady flow pressure distributions along the major axis produced by gelatin with 10 percent porosity for 90°, 45°, and 25° impact angles, respectively. The pressures are normalized to the stagnation pressure as calculated in Equation (2). Together with the experimental data, two sets of curves are shown in these figures. The predicted pressure distribution from

⁶Boehman, L.I., and A. Challita, "A Model for Predicting Bird and Ice Impact Loads on Structures," GDR-TR-79-54.

³Barber, J.P., H.R. Taylor, and J.S. Wilbeck, "Bird Impact Forces and Pressures on Rigid and Compliant Targets," AFFDL-TR-77-60, ADA061-313, May 1978.

⁵Bauer, D.P. and J.P. Barber, "Experimental Investigation of Impact Pressures Caused by Gelatin Simulated Birds and Ice," UDR-TR-78-114, November 1978.

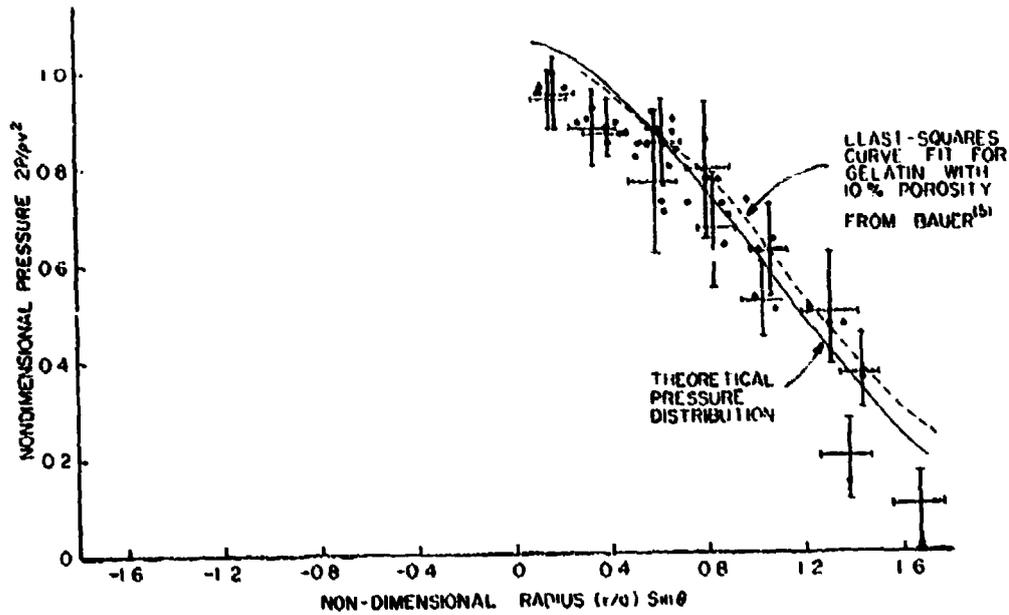


Figure 14. Normalized Steady Flow Pressure Distribution of Nominal 1800 g and 3600 g Gelatin with 10% Porosity Along Major Axis at Normal Impact

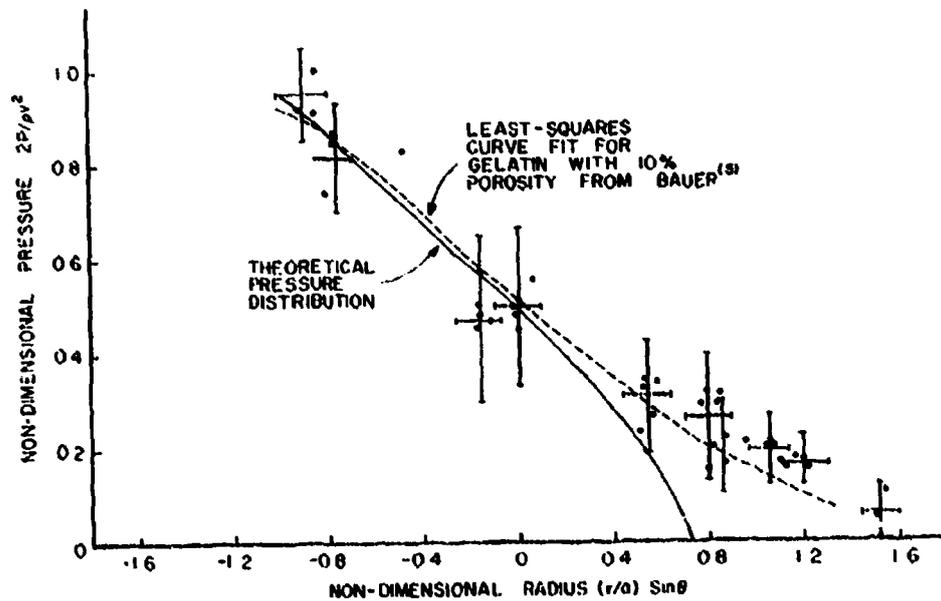


Figure 15. Normalized Steady Flow Pressure Distribution of Nominal 1800 g and 3600 g Gelatin with 10% Porosity Along Major Axis at 45° Impact

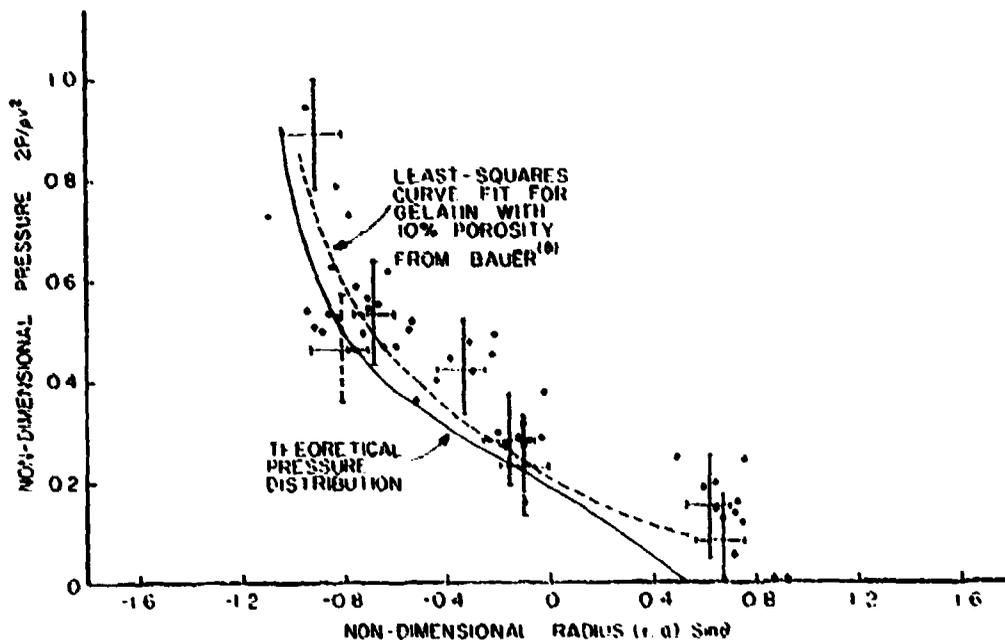


Figure 16. Normalized Steady Flow Pressure Distribution of Nominal 1800 g and 3600 g Gelatin with 10% Porosity Along Major Axis at 25° Impact

Reference 6 by Boehman for normal (90°), 45°, and 25° impacts, and the least-squares curve fits of the experimental data for smaller size gelatin projectiles from Reference 5 by Bauer. The error bars shown parallel to the ordinate axis represent the uncertainty in measuring the steady state pressure from the pressure traces created by the superposition of the high frequency noise on the pressure profile of birds. The error bars shown parallel to the abscissa are based on the maximum error in determining the initial impact location on the target. The maximum error was calculated in Reference 5 by Bauer and is

⁶Boehman, L.I. and A. Challita, "A Model for Predicting Bird and Ice Impact Loads on Structures," UDR-TR-79-54.

⁵Bauer, D.P. and J.P. Barber, "Experimental Investigation of Impact Pressures Caused by Gelatin Simulated Birds and Ice," UDR-TR-78-114, November 1978.

caused by the displacement of the actual trajectory from the true trajectory of the projectile.

This set of figures shows the important effect that impact angle has on steady flow distribution. As the impact angle changes from normal to oblique, the steady flow pressure distribution changes from symmetrical about the center of impact to highly skewed about the stagnation point. It also shows that the location of the stagnation point in the flow field moves from the center of impact to a point actually outside the projected frontal area of the incoming projectile. The figures show that projectile size has no effect on steady flow pressures. The data for both 1800 g and 3600 g gelatin projectiles are included in the figures and, in nondimensionalized (scaled) form, show no significant departure from the smaller bird results.

Agreement among the theoretical curve, curve fit of the experimental data for smaller size gelatin projectiles, and the experimental data from this work is very good at all angles of impact. Some disagreement between the data and the flow model predictions does occur near the outside edge of the flow, because the analytically predicted pressure distribution was generated from a simplified model of onset flow.

3.4.2 Real Birds

Figures 17, 18, and 19 show the steady flow pressure distributions along the major axis for real bird impacts. Again, the theory and the least-squares curve fit of the experimental data for smaller size birds from Reference 3 by Barber are shown on these figures. Error bars similar to that shown for gelatin are also shown.

All of the characteristics of steady flow apparent in the gelatin impacts are also apparent for real birds. The

¹Barber, J.P., H.R. Taylor, and J.S. Wilbeck, "Bird Impact Forces and Pressures on Rigid and Compliant Targets," AFFDL-TR-77-60, ADA061-313, May 1978.

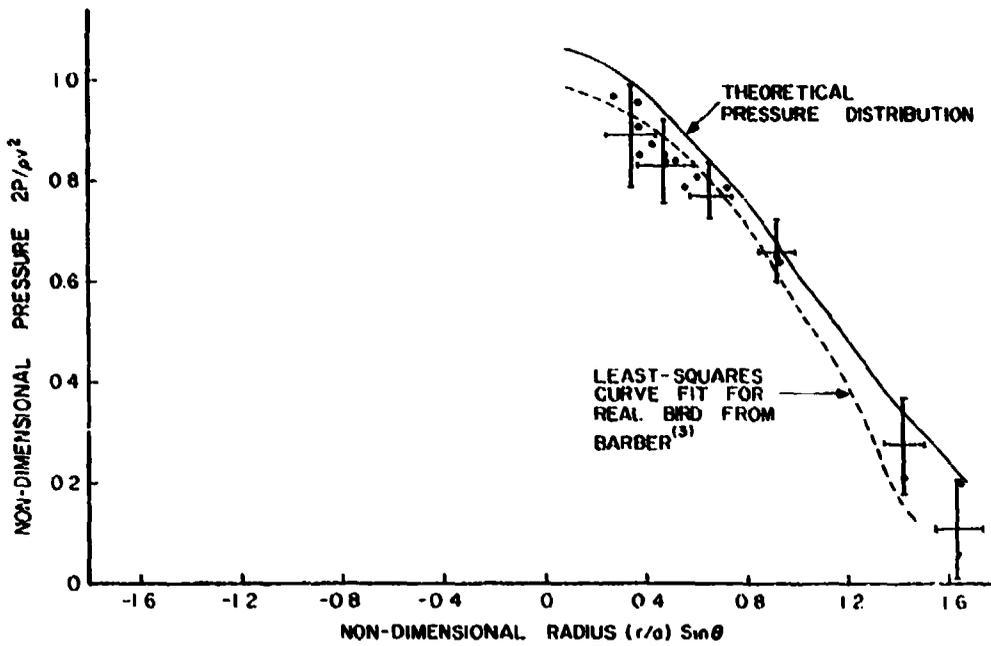


Figure 17. Normalized Steady Flow Pressure Distribution of Nominal 1800 g Real Bird (chicken) Along Major Axis at Normal Impact

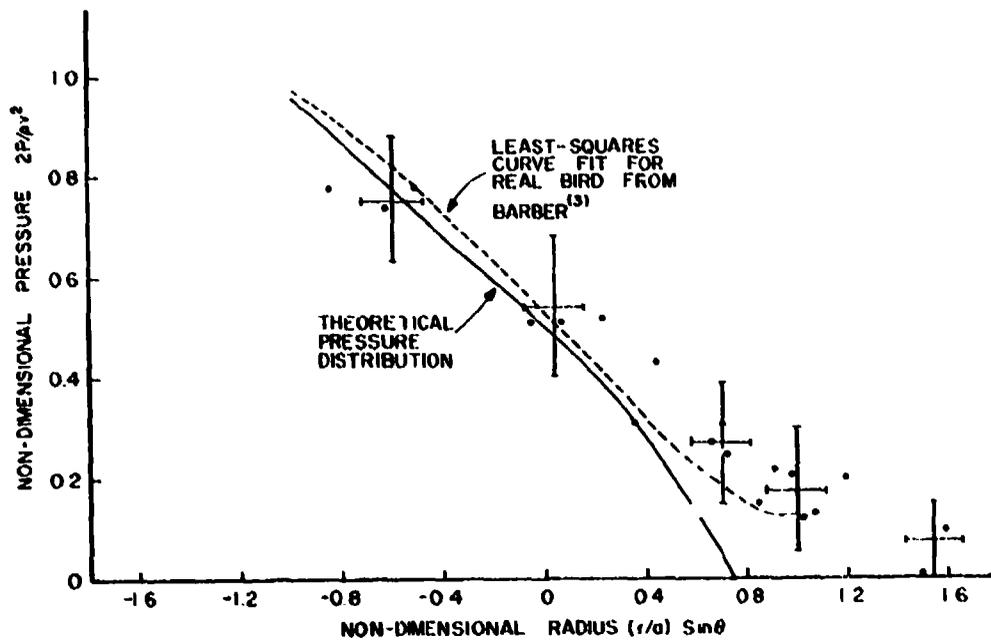


Figure 18. Normalized Steady Flow Pressure Distribution of Nominal 1800 g Real Bird (chicken) Along Major Axis at 45° Impact

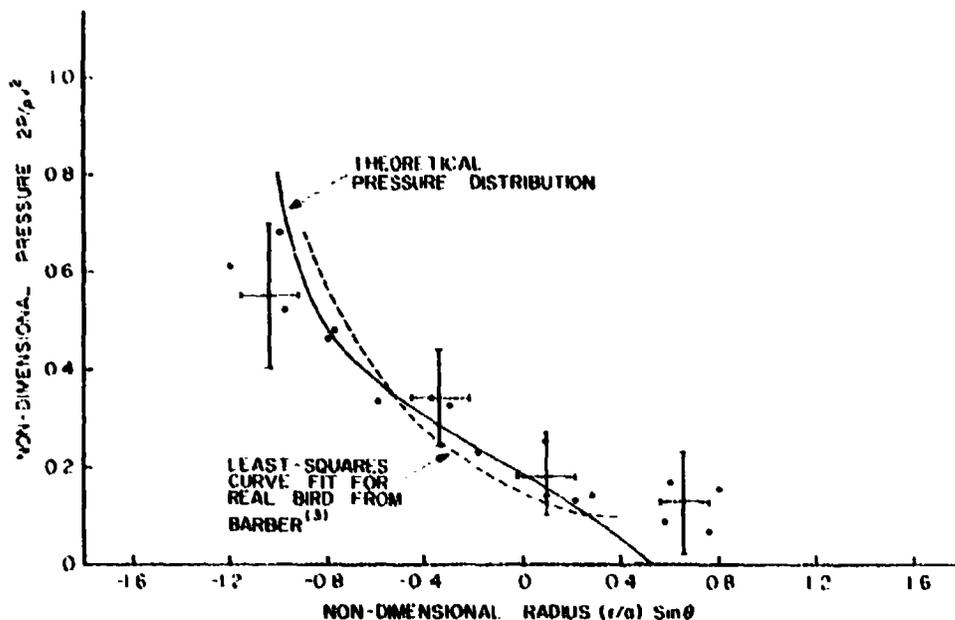


Figure 19. Normalized Steady Flow Pressure Distribution of Nominal 1800 g Real Bird (chicken) Along Major Axis at 25° Impact

stagnation point moves from the center of impact to a point outside the projected frontal area of the incoming projectile and the steady flow pressure distribution is highly dependent on the impact angle. There is good agreement among the theoretical curve, curve fit of the experimental data for smaller size birds, and the experimental data from this program.

This data also demonstrates that for the 1800 g projectiles, there are no significant differences between loads produced by real and gelatin birds. In Reference 5 Bauer found a similar result for 90 g and 600 g projectiles.

³Bauer, D.P. and J.P. Barber, "Experimental Investigation of Impact Pressures Caused by Gelatin Simulated Birds and Tee," CDR-PR-78-114, November 1978.

SECTION IV
CONCLUSIONS AND DISCUSSION

A detailed body of impact pressure data now exists for real birds (chickens) and bird substitutes (gelatin with 10 percent porosity) over an enormous range of impact parameters. The parameters and their ranges are:

- 1) Bird mass - 60 g to 3600 g
- 2) Impact velocity - 50 m/s to 300 m/s
- 3) Impact angle - 25° to 90°

This entire body of data has been successfully analysed and the important impact processes identified, functional relationships between the impact pressures and impact parameters developed and scaling of impact loads with bird mass completed. From the work reported here and in Reference 3 by Barber, Reference 2 by Peterson and Barber, Reference 4 by Wilbeck, and Reference 5 by Bauer, the following conclusions may be drawn.

- 1) Birds behave as a fluid during impact at the impact velocities of interest in birdstrike (>50 m/s).

³Barber, J.P., H.R. Taylor, and J.S. Wilbeck, "Bird Impact Forces and Pressures on Rigid and Compliant Targets," AFFDL-TR-77-60, ADA061-313, May 1978.

²Peterson, R.L. and J.P. Barber, "Bird Impact Forces in Aircraft Windshield Design," AFFDL-TR-75-150, ADA026-628, March 1976.

⁴Wilbeck, J.S., "Impact Behavior of Low Strength Projectiles," AFML-TR-77-134, ADA060-423, July 1978.

⁵Bauer, D.P. and J.P. Barber, "Experimental Investigation of Impact Pressures Caused by Gelatin Simulated Birds and Ice," UDR-TR-78-114, November 1978.

2) There are four phases of fluid behavior during a bird impact; the shock phase of initial impact, shock pressure decay, steady flow, and termination.

3) Peak shock pressures are independent of bird mass but depend in a predictable manner on impact velocity, impact angle, and bird material properties.

4) Steady flow pressures are independent of bird mass but depend in a predictable way on impact velocity, impact angle, and bird material properties.

5) The spacial distribution of bird impact pressures scale linearly with bird dimensions (providing bird orientation at impact is fixed). This scaling has been tested over a range of bird mass from 60 g to 3600 g.

6) Impact duration is given by simply the length of the bird divided by the impact velocity. The validity of this relation has been tested for bird masses from 60 to 3600 g and for impact velocities from 50 m/s to 300 m/s.

7) Simulated birds effectively reproduce the pressure distribution of real birds.

APPENDIX BIRD LOADING MODEL.

This appendix provides a listing of the modified bird loading model, a sample input and output data, and the instructions needed to run the program.

The original loading model was designed to predict impact loads and to be interfaced with finite element structural analysis computer programs, and also was designed to handle impacts on arbitrary curved surfaces. The three-dimensional potential flow theory was used to model the impact process and the surface singularity method was used to solve the complex potential flows (i.e., velocity and pressure fields). To allow arbitrary bodies to be considered, it was required that the body surface be specified by a set of points in space called nodal points and that the coordinates of all nodal points on the impacted surface be supplied to the loading model.

Input to the loading model consisted of the coordinates of the set of finite element nodal points defining the surface of the impacted object. These coordinates were given in the reference coordinate system, that is, the coordinate system used to describe the shape of the impacted surface before impact occurs.

Because the target used in this experimental program is a rigid flat plate, the loading model was modified to generate a rectangular grid describing the plate. The dimensions of the grid are proportional to the weight of the bird and to the angle of impact. The number of elements forming the grid is found by multiplying NC by NS , where NC and NS are the number of nodes along the width and length of the grid.

The input data needed for this modified version of the loading model are time, TIM , which is assumed to equal zero;

components of the velocity vector of the projectile, VBX , VBY , and VBZ ; coordinates of the center of impact, XI , YI , and ZI ; angle of impact, $THETA$; and the weight of the projectile, WB . The bird length is assumed to be twice its diameter.

The output data are divided in two parts; the first part lists the coordinates of the four corner points forming the element, the components of the unit normal vector, and the coordinates of the null point in the reference coordinate system. The main purpose of this output is to enable errors in the input to be discovered before the lengthy flow calculations are performed. The second part contains the velocities and pressures on the body surface.

Listing of the Main Program

```

1.0000 PROGRAM LOADPCTNPRO,OUTPRT,TAP5,TAP11)
2.0000 C
3.0000 C THIS PROGRAM CALCULATES THE POTENTIAL FLOW ABOUT ARBITRARY,
4.0000 C THREE-DIMENSIONAL BODIES, IN AND ABOUT VARIOUS SURFACE ELEMENTS
5.0000 C AND USED TO APPROXIMATE THE BODY SURFACE. THE METHOD UTILIZES
6.0000 C A SOURCE DENSITY DISTRIBUTION ON THE SURFACE OF THE BODY AND SUMS UP
7.0000 C FOR THE DISTRIBUTION NECESSARY TO MAKE THE POTENTIAL POTENTIALLY
8.0000 C ZERO ON THE BOUNDARY. THE INTEGRAL EQUATION FOR THE SURFACE
9.0000 C SOURCE DENSITY IS REPLACED BY A SET OF LINEAR ALGEBRAIC
10.0000 C EQUATIONS FOR THE VALUES OF THE SOURCE DENSITY ON EACH OF THE
11.0000 C QUADRANGULAR ELEMENTS. AFTER THIS SET OF EQUATIONS HAS BEEN
12.0000 C SOLVED, THE FLOW IS ACCOMPANIED BY A SOURCE DENSITY DISTRIBUTION.
13.0000 C THE FLOW VELOCITIES AT POINTS ON THE BODY SURFACE ARE CALCULATED.
14.0000 C
15.0000 C DIMENSION AC(3,12),XN(12),Y(12),Z(12),XZ(12),YZ(12),Z(12)
16.0000 C 1 XN(1),YZ(1),XZ(1),Y(1),Z(1),X(1),X(1),Y(1),Z(1),X(1),Y(1),Z(1)
17.0000 C 2 X(4),Y(4),Z(4),XN(2),YN(2),ZN(2),X(2),Y(2),Z(2)
18.0000 C 3 X(12),Y(12),Z(12),XN(3),YN(3),ZN(3),X(3),Y(3),Z(3)
19.0000 C REAL M1,M2,M3,M34,M41
20.0000 C F1=3, F4159
21.0000 C READ (1,901) TTH,ORX,ORY,ORZ,X1,Y1,Z1
22.0000 C WRITE (11,902)
23.0000 C WRITE (11,903) TTH,ORX,ORY,ORZ,X1,Y1,Z1
24.0000 C READ (1,904) TH1A,MR
25.0000 C TH1A=TH1A*PI/180.
26.0000 C NC=11
27.0000 C NS=11
28.0000 C WRITE (11,905)
29.0000 C WRITE (11,906) TH1A,MR
30.0000 C KMR =.03644
31.0000 C OR=CORX*PI/180,ORZ*PI/180,ORZ*PI/180,.5
32.0000 C TH=C, AND C=PI/KMR*ORZ*PI/180
33.0000 C R1=7, KMR
34.0000 C R1=ORZ/2.
35.0000 C R1=R1/2*SIN(TH1A)
36.0000 C F1=NC-R1/25.
37.0000 C GREEN=R1F
38.0000 C SUM1=1.
39.0000 C DO 9 J=1,NS
40.0000 C SUM=0.
41.0000 C DO 11 I=1,NC
42.0000 C F1=NC*(F1-I)
43.0000 C XN(I)=GREEN-SUM1*F1
44.0000 C YN(I)=ORZ*F1*(SUM1+I)
45.0000 C SUM=SUM1+I
46.0000 C 9 CONTINUE
47.0000 C SUM1=SUM1+1.
48.0000 C 11 CONTINUE
49.0000 C UPRM=ORX/OR
50.0000 C UPRN=ORY/OR

```



```

151.0000      Y(3,1)=YNC(1)*(YNC(1)-Y(1,1))
152.0000      Y(3,1)=XNC(1)*(XNC(1)-X(1,1))
153.0000      BOO CONTINUE
154.0000      14 WRITE (11,1)
155.0000      1  FORMAT (X0X,* J-ELEMENT NUMBER*)
156.0000      WRITE (11,2)
157.0000      2  FORMAT (X X,* X1,X2,X3,X4 X COORDINATES OF THE POINTS FORMING,
158.0000      1  * THE ELEMENT*)
159.0000      WRITE (11,3)
160.0000      3  FORMAT (X X,* Y1,Y2,Y3,Y4 Y COORDINATES OF THE POINTS FORMING,
161.0000      1  * THE ELEMENT*)
162.0000      WRITE (11,4)
163.0000      4  FORMAT (X X,* Z1,Z2,Z3,Z4 Z COORDINATES OF THE POINTS FORMING,
164.0000      1  * THE ELEMENT*)
165.0000      WRITE (11,5)
166.0000      5  FORMAT (X X,* UNX,UNY,UNZ-COMPONENTS OF THE UNIT NORMAL VECTOR*)
167.0000      WRITE (11,6)
168.0000      6  FORMAT (X X,* X1NP,Y1NP,Z1NP-COORDINATES OF THE NODE POINT IN*,
169.0000      1  * REFERENCE COORDINATE SYSTEM*)
170.0000      WRITE (11,10)
171.0000      10  FORMAT (/Z,X*,X1*,Z*,X1*,Z*,X2*,Z*,X2*,Z*,X3*,Z*,X3*,Z*,X4*,Z*,X4*,Z*,X1NP*,Z*,X1NP*,Z*,
172.0000      1  *X1NP*)
173.0000      WRITE (11,10B)
174.0000      10B  FORMAT (/Y,X*,Y1*,Z*,X*,Y1*,Z*,X2*,Y2*,Z*,X*,Y2*,Z*,X3*,Y3*,Z*,X*,Y3*,Z*,X4*,Y4*,Z*,X*,Y4*,Z*,X1NP*,Y1NP*,Z*,X1NP*,Y1NP*)
175.0000      WRITE (11,10C)
176.0000      10C  FORMAT (/Z,X*,Z1*,Z*,X*,Z2*,Z*,X*,Z3*,Z*,X*,Z4*,Z*,X1NP*,Z*,X1NP*,Z*,Z1NP*,Z*,X1NP*,Z*)
177.0000      151  DO 10 J=1,N
178.0000          X1=X(1,J)
179.0000          X2=X(2,J)
180.0000          X3=X(3,J)
181.0000          X4=X(4,J)
182.0000          Y1=Y(1,J)
183.0000          Y2=Y(2,J)
184.0000          Y3=Y(3,J)
185.0000          Y4=Y(4,J)
186.0000          Z1=Z(1,J)
187.0000          Z2=Z(2,J)
188.0000          Z3=Z(3,J)
189.0000          Z4=Z(4,J)
190.0000          IX=X3-X1
191.0000          IY=Y3-Y1
192.0000          IZ=Z3-Z1
193.0000          IX=X4-X2
194.0000          IY=Y4-Y2
195.0000          IZ=Z4-Z2
196.0000          N1=IX*IY-IZ*IY
197.0000          YN1=IX*IY-IZ*IY
198.0000          ZN1=IX*IY-IZ*IY
199.0000          UN=SQRT(X1**2+Y1**2+Z1**2)
200.0000          UNX=X1/UN

```

201.0000 UNY-YN1ZUN
 202.0000 UNZ-7N1ZUN
 203.0000 X0U5(X11Y21Y41Y4)Z4.
 204.0000 Y0U5(Y11Y21Y41Y4)Z4.
 205.0000 Z0U5(Z11Y21Y41Y4)Z4.
 206.0000 U1-U1NYXCY0U X1Y1UNYXCY0U Y1U1UNZXCZ0U-Z1)
 207.0000 U2-U2NYXCY0U X2Y2UNYXCY0U Y2U2UNZXCZ0U-Z2)
 208.0000 U3-U3NYXCY0U X3Y3UNYXCY0U Y3U3UNZXCZ0U-Z3)
 209.0000 U4-U4NYXCY0U X4Y4UNYXCY0U Y4U4UNZXCZ0U-Z4)
 210.0000 X1Y1-X1Y1(CUNX401)
 211.0000 X1Y2-X1Y2(CUNX402)
 212.0000 X1Y3-X1Y3(CUNX403)
 213.0000 X1Y4-X1Y4(CUNX404)
 214.0000 Y1Y1-Y1Y1(CUNY401)
 215.0000 Y1Y2-Y1Y2(CUNY402)
 216.0000 Y1Y3-Y1Y3(CUNY403)
 217.0000 Y1Y4-Y1Y4(CUNY404)
 218.0000 Z1Y1-Z1Y1(CUNZ401)
 219.0000 Z1Y2-Z1Y2(CUNZ402)
 220.0000 Z1Y3-Z1Y3(CUNZ403)
 221.0000 Z1Y4-Z1Y4(CUNZ404)
 222.0000 U1-U0R1(C1X5*Y11YX*Y11Z*Z*)
 223.0000 U1YX-U1YXZ11
 224.0000 U1Y1-U1Y1Z11
 225.0000 U1Y2-U1Y2Z11
 226.0000 U1YX-U1YXZ11Z-UNZKTP1Y
 227.0000 U1Y1-U1Y1Z11Z-UNZKTP1Z
 228.0000 U1Y2-U1Y2Z11Z-UNZKTP1X
 229.0000 Z1Y0U1-Z1YXKX1-Y0U1Y1YXCY1-Y0U1Y1YXZ1-Z0U1)
 230.0000 Z1Y0U2-Z1YXKX2-Y0U2Y2YXCY2-Y0U2Y2YXZ2-Z0U2)
 231.0000 Z1Y0U3-Z1YXKX3-Y0U3Y3YXCY3-Y0U3Y3YXZ3-Z0U3)
 232.0000 Z1Y0U4-Z1YXKX4-Y0U4Y4YXCY4-Y0U4Y4YXZ4-Z0U4)
 233.0000 U1Y0U1-U1YXKX1-Y0U1Y1YXCY1-Y0U1Y1YXZ1-Z0U1)
 234.0000 U1Y0U2-U1YXKX2-Y0U2Y2YXCY2-Y0U2Y2YXZ2-Z0U2)
 235.0000 U1Y0U3-U1YXKX3-Y0U3Y3YXCY3-Y0U3Y3YXZ3-Z0U3)
 236.0000 U1Y0U4-U1YXKX4-Y0U4Y4YXCY4-Y0U4Y4YXZ4-Z0U4)
 237.0000 Z1Y0U1-Z1YXKX1-Y0U1Y1YXCY1-Y0U1Y1YXZ1-Z0U1)
 238.0000 Z1Y0U2-Z1YXKX2-Y0U2Y2YXCY2-Y0U2Y2YXZ2-Z0U2)
 239.0000 Z1Y0U3-Z1YXKX3-Y0U3Y3YXCY3-Y0U3Y3YXZ3-Z0U3)
 240.0000 Z1Y0U4-Z1YXKX4-Y0U4Y4YXCY4-Y0U4Y4YXZ4-Z0U4)
 241.0000 Z1Y0U1-Z1Y0U1Z1Y0U1
 242.0000 Z1Y0U2-Z1Y0U2Z1Y0U2
 243.0000 Z1Y0U3-Z1Y0U3Z1Y0U3
 244.0000 Z1Y0U4-Z1Y0U4Z1Y0U4
 245.0000 U1Y0U1-U1Y0U1Z1Y0U1
 246.0000 U1Y0U2-U1Y0U2Z1Y0U2
 247.0000 U1Y0U3-U1Y0U3Z1Y0U3
 248.0000 U1Y0U4-U1Y0U4Z1Y0U4
 249.0000 X1Y0U1-Y0U1Y1YXZ1Z1Y0U1
 250.0000 Y1Y0U1-Y0U1Y2YXZ1Z1Y0U1
 251.0000 Z1Y0U1-Z1Y0U1Z1Y0U1Z1Y0U1

91,0000	10111-10
92,0000	10211-10
93,0000	10311-10
94,0000	10411-10
95,0000	10511-10
96,0000	10611-10
97,0000	10711-10
98,0000	10811-10
99,0000	10911-10
100,0000	11011-10
101,0000	11111-10
102,0000	11211-10
103,0000	11311-10
104,0000	11411-10
105,0000	11511-10
106,0000	11611-10
107,0000	11711-10
108,0000	11811-10
109,0000	11911-10
110,0000	12011-10
111,0000	12111-10
112,0000	12211-10
113,0000	12311-10
114,0000	12411-10
115,0000	12511-10
116,0000	12611-10
117,0000	12711-10
118,0000	12811-10
119,0000	12911-10
120,0000	13011-10
121,0000	13111-10
122,0000	13211-10
123,0000	13311-10
124,0000	13411-10
125,0000	13511-10
126,0000	13611-10
127,0000	13711-10
128,0000	13811-10
129,0000	13911-10
130,0000	14011-10
131,0000	14111-10
132,0000	14211-10
133,0000	14311-10
134,0000	14411-10
135,0000	14511-10
136,0000	14611-10
137,0000	14711-10
138,0000	14811-10
139,0000	14911-10
140,0000	15011-10
141,0000	15111-10
142,0000	15211-10
143,0000	15311-10
144,0000	15411-10
145,0000	15511-10
146,0000	15611-10
147,0000	15711-10
148,0000	15811-10
149,0000	15911-10
150,0000	16011-10
151,0000	16111-10
152,0000	16211-10
153,0000	16311-10
154,0000	16411-10
155,0000	16511-10
156,0000	16611-10
157,0000	16711-10
158,0000	16811-10
159,0000	16911-10
160,0000	17011-10
161,0000	17111-10
162,0000	17211-10
163,0000	17311-10
164,0000	17411-10
165,0000	17511-10
166,0000	17611-10
167,0000	17711-10
168,0000	17811-10
169,0000	17911-10
170,0000	18011-10
171,0000	18111-10
172,0000	18211-10
173,0000	18311-10
174,0000	18411-10
175,0000	18511-10
176,0000	18611-10
177,0000	18711-10
178,0000	18811-10
179,0000	18911-10
180,0000	19011-10
181,0000	19111-10
182,0000	19211-10
183,0000	19311-10
184,0000	19411-10
185,0000	19511-10
186,0000	19611-10
187,0000	19711-10
188,0000	19811-10
189,0000	19911-10
190,0000	20011-10
191,0000	20111-10
192,0000	20211-10
193,0000	20311-10
194,0000	20411-10
195,0000	20511-10
196,0000	20611-10
197,0000	20711-10
198,0000	20811-10
199,0000	20911-10
200,0000	21011-10


```

0.1,0000 YINI=1-YI*(1/ZI*COBR/COBG)
0.2,0000 DISE=COB*YINI
0.3,0000 DISE=COB*YINI
0.4,0000 DISE=COB*YINI
0.5,0000 DISE=(DISE**2+DISEY**2+DISEZ**2)**.5
0.6,0000 H=COSE*(.61,RI) JUNC(1)=0
0.7,0000 H=COSE*(.11,RI) JUNC(1)=1
0.8,0000 D1=(Y(2,1)-Y(1,1))**2+(Y(2,1)-Y(1,1))**2
0.9,0000 D2=(Y(4,1)-Y(3,1))**2+(Y(4,1)-Y(3,1))**2
1.0,0000 D3=(Y(4,1)-Y(1,1))**2+(Y(4,1)-Y(1,1))**2
1.1,0000 D4=(Y(4,1)-Y(1,1))**2+(Y(4,1)-Y(1,1))**2
1.2,0000 D5=(Y(1,1)-YINI)**2+(Y(1,1)-YINI)**2
1.3,0000 D6=(Y(4,1)-YINI)**2+(Y(4,1)-YINI)**2
1.4,0000 D7=(Y(3,1)-YINI)**2+(Y(3,1)-YINI)**2
1.5,0000 D8=(Y(2,1)-YINI)**2+(Y(2,1)-YINI)**2
1.6,0000 G1=COSE*(.05,ZI)*SQR(COBSURE(03))
1.7,0000 IF(G1,1,0.) GO TO 610
1.8,0000 H=(G1,1,1.,AND,G1,1,1,1,01) G1=1.
1.9,0000 GO TO 611
2.0,0000 610 IF(G1,1,1.,AND,G1,1,1,1,01) G1=-1.
2.1,0000 611 ANGE=ACOS(G1)
2.2,0000 G2=COSE*(.05,ZI)*SQR(COBSURE(02))
2.3,0000 IF(G2,1,0.) GO TO 612
2.4,0000 H=(G2,1,1.,AND,G2,1,1,1,01) G2=1.
2.5,0000 GO TO 613
2.6,0000 612 IF(G2,1,1.,AND,G2,1,1,1,01) G2=-1.
2.7,0000 613 ANGE=ACOS(G2)
2.8,0000 G3=COSE*(.05,ZI)*SQR(COBSURE(06))
2.9,0000 IF(G3,1,0.) GO TO 614
3.0,0000 H=(G3,1,1.,AND,G3,1,1,1,01) G3=1.
3.1,0000 GO TO 615
3.2,0000 614 IF(G3,1,1.,AND,G3,1,1,1,01) G3=-1.
3.3,0000 615 ANGE=ACOS(G3)
3.4,0000 G4=COSE*(.05,ZI)*SQR(COBSURE(08))
3.5,0000 IF(G4,1,0.) GO TO 616
3.6,0000 H=(G4,1,1.,AND,G4,1,1,1,01) G4=1.
3.7,0000 GO TO 617
3.8,0000 616 IF(G4,1,1.,AND,G4,1,1,1,01) G4=-1.
3.9,0000 617 ANGE=ACOS(G4)
4.0,0000 ANG=ANG1+ANG2+ANG3+ANG4
4.1,0000 IF(ABS(ANG),1,1,6.2) GO TO 627
4.2,0000 IMP=1
4.3,0000 H=H1+ZIB*IMP
4.4,0000 620 FURB=1/XY*IMPACT POINT IS ON ELEMENT 15
4.5,0000 621 COE=IMP
4.6,0000 622 COE=COE+IMP
4.7,0000 COE=COE+IMP
4.8,0000 COE=COE+IMP
4.9,0000 COE=COE+IMP
5.0,0000 COE=COE+IMP
5.1,0000 COE=COE+IMP
5.2,0000 COE=COE+IMP
5.3,0000 COE=COE+IMP
5.4,0000 COE=COE+IMP
5.5,0000 COE=COE+IMP
5.6,0000 COE=COE+IMP
5.7,0000 COE=COE+IMP
5.8,0000 COE=COE+IMP
5.9,0000 COE=COE+IMP
6.0,0000 COE=COE+IMP

```

```

401.0000      IF (TIM,NU(0,)) GO TO 13
402.0000      URM=UR/VBR
403.0000      XI=0.
404.0000      IU TO 22
405.0000  13  IU C=URR*(TIM-TINT)
406.0000      TINT=0.
407.0000      XI C=XI C+HIC
408.0000      UR=IU XI C
409.0000      URM=1 TO UR R/VBR
410.0000  22  IY=0.5*(IURR+URR2)
411.0000      IU TO 1  I=1, IR
412.0000      IX(I)=IX(I)/VBR
413.0000      IY(I)=IY(I)/VBR
414.0000      IZ(I)=IZ(I)/VBR
415.0000  1001  CONTINUE
416.0000      IU 15  I=1, NN
417.0000      II=0.
418.0000      UI=0.
419.0000      MI=0.
420.0000  167  XI=A(1, I)
421.0000      YI=A(2, I)
422.0000      ZI=A(3, I)
423.0000  136  IU 20  J=1, N
424.0000      XN=1 C(1, J)*X(1, J)+1 C(2, J)*Y(1, J)+1 C(3, J)*Z(1, J)
425.0000      YN=1 C(1, J)*X(1, J)+1 C(2, J)*Y(1, J)+1 C(3, J)*Z(3, J)
426.0000      ZN=1 C(1, J)*X(1, J)+1 C(2, J)*Y(1, J)+1 C(3, J)*Z(3, J)
427.0000      ZI 21=X(2, J)-X(1, J)
428.0000      ZI 32=X(3, J)-X(2, J)
429.0000      ZI 43=X(4, J)-X(3, J)
430.0000      ZI 54=X(5, J)-X(4, J)
431.0000      I 121=Y(2, J)-Y(1, J)
432.0000      I 132=Y(3, J)-Y(2, J)
433.0000      I 143=Y(4, J)-Y(3, J)
434.0000      I 154=Y(5, J)-Y(4, J)
435.0000      II 2=SIGN(C(1, 2)*Y(2, J) I 121**2)
436.0000      II 3=SIGN(C(1, 3)*Y(3, J) I 132**2)
437.0000      II 4=SIGN(C(1, 4)*Y(4, J) I 143**2)
438.0000      II 5=SIGN(C(1, 5)*Y(5, J) I 154**2)
439.0000      R1=SIGN(C(XN, X(1, J))*Y(1, J) I Y(1, J) I Y(1, J) I Y(1, J))
440.0000      R2=SIGN(C(XN, X(2, J))*Y(2, J) I Y(2, J) I Y(2, J) I Y(2, J))
441.0000      R3=SIGN(C(XN, X(3, J))*Y(3, J) I Y(3, J) I Y(3, J) I Y(3, J))
442.0000      R4=SIGN(C(XN, X(4, J))*Y(4, J) I Y(4, J) I Y(4, J) I Y(4, J))
443.0000      I 1=ZN**R1 C(XN, X(1, J))**2
444.0000      I 2=ZN**R2 C(XN, X(2, J))**2
445.0000      I 3=ZN**R3 C(XN, X(3, J))**2
446.0000      I 4=ZN**R4 C(XN, X(4, J))**2
447.0000      II=C(XN, Y(1, J))*X(XN, X(1, J))
448.0000      II=C(XN, Y(2, J))*X(XN, X(2, J))
449.0000      II=C(XN, Y(3, J))*X(XN, X(3, J))
450.0000      II=C(XN, Y(4, J))*X(XN, X(4, J))

```

```

451.0000      H11=MIN(CORR1R3-D1)*ZAR1R1R2D1*YX1121/012
452.0000      H12=MIN(CORR1R3-D1)*ZAR1R1R3D1*YX1131/013
453.0000      H13=MIN(CORR1R3-D1)*ZAR1R1R4D1*YX1141/014
454.0000      H14=MIN(CORR1R1-D1)*ZAR1R1R1D1*YX1111/011
455.0000      H15=MIN(CORR1R2-D1)*ZAR1R1R2D1*YX1121/012
456.0000      H16=MIN(CORR1R3-D1)*ZAR1R1R3D1*YX1131/013
457.0000      H17=MIN(CORR1R4-D1)*ZAR1R1R4D1*YX1141/014
458.0000      H18=MIN(CORR1R1-D1)*ZAR1R1R1D1*YX1111/011
459.0000      H19=MIN(CORR1R2-D1)*ZAR1R1R2D1*YX1121/012
460.0000      H20=MIN(CORR1R3-D1)*ZAR1R1R3D1*YX1131/013
461.0000      H21=MIN(CORR1R4-D1)*ZAR1R1R4D1*YX1141/014
462.0000      H22=MIN(CORR1R1-D1)*ZAR1R1R1D1*YX1111/011
463.0000      H23=MIN(CORR1R2-D1)*ZAR1R1R2D1*YX1121/012
464.0000      H24=MIN(CORR1R3-D1)*ZAR1R1R3D1*YX1131/013
465.0000      H25=MIN(CORR1R4-D1)*ZAR1R1R4D1*YX1141/014
466.0000      H26=MIN(CORR1R1-D1)*ZAR1R1R1D1*YX1111/011
467.0000      H27=MIN(CORR1R2-D1)*ZAR1R1R2D1*YX1121/012
468.0000      H28=MIN(CORR1R3-D1)*ZAR1R1R3D1*YX1131/013
469.0000      H29=MIN(CORR1R4-D1)*ZAR1R1R4D1*YX1141/014
470.0000      H30=MIN(CORR1R1-D1)*ZAR1R1R1D1*YX1111/011
471.0000      H31=MIN(CORR1R2-D1)*ZAR1R1R2D1*YX1121/012
472.0000      H32=MIN(CORR1R3-D1)*ZAR1R1R3D1*YX1131/013
473.0000      H33=MIN(CORR1R4-D1)*ZAR1R1R4D1*YX1141/014
474.0000      H34=MIN(CORR1R1-D1)*ZAR1R1R1D1*YX1111/011
475.0000      H35=MIN(CORR1R2-D1)*ZAR1R1R2D1*YX1121/012
476.0000      H36=MIN(CORR1R3-D1)*ZAR1R1R3D1*YX1131/013
477.0000      H37=MIN(CORR1R4-D1)*ZAR1R1R4D1*YX1141/014
478.0000      H38=MIN(CORR1R1-D1)*ZAR1R1R1D1*YX1111/011
479.0000      H39=MIN(CORR1R2-D1)*ZAR1R1R2D1*YX1121/012
480.0000      H40=MIN(CORR1R3-D1)*ZAR1R1R3D1*YX1131/013
481.0000      H41=MIN(CORR1R4-D1)*ZAR1R1R4D1*YX1141/014
482.0000      H42=MIN(CORR1R1-D1)*ZAR1R1R1D1*YX1111/011
483.0000      H43=MIN(CORR1R2-D1)*ZAR1R1R2D1*YX1121/012
484.0000      H44=MIN(CORR1R3-D1)*ZAR1R1R3D1*YX1131/013
485.0000      H45=MIN(CORR1R4-D1)*ZAR1R1R4D1*YX1141/014
486.0000      H46=MIN(CORR1R1-D1)*ZAR1R1R1D1*YX1111/011
487.0000      H47=MIN(CORR1R2-D1)*ZAR1R1R2D1*YX1121/012
488.0000      H48=MIN(CORR1R3-D1)*ZAR1R1R3D1*YX1131/013
489.0000      H49=MIN(CORR1R4-D1)*ZAR1R1R4D1*YX1141/014
490.0000      H50=MIN(CORR1R1-D1)*ZAR1R1R1D1*YX1111/011
491.0000      H51=MIN(CORR1R2-D1)*ZAR1R1R2D1*YX1121/012
492.0000      H52=MIN(CORR1R3-D1)*ZAR1R1R3D1*YX1131/013
493.0000      H53=MIN(CORR1R4-D1)*ZAR1R1R4D1*YX1141/014
494.0000      H54=MIN(CORR1R1-D1)*ZAR1R1R1D1*YX1111/011
495.0000      H55=MIN(CORR1R2-D1)*ZAR1R1R2D1*YX1121/012
496.0000      H56=MIN(CORR1R3-D1)*ZAR1R1R3D1*YX1131/013
497.0000      H57=MIN(CORR1R4-D1)*ZAR1R1R4D1*YX1141/014
498.0000      H58=MIN(CORR1R1-D1)*ZAR1R1R1D1*YX1111/011
499.0000      H59=MIN(CORR1R2-D1)*ZAR1R1R2D1*YX1121/012
500.0000      H60=MIN(CORR1R3-D1)*ZAR1R1R3D1*YX1131/013

```

```

501.0000 15 CONTINUE
502.0000 CALL SETDEF (AN,ON,S,N)
503.0000 WRITE (11,92)
504.0000 92 FORMAT (2X,*1*,7X,*XPMP*,9X,*VIL*,10X,*U1*,9X,*UNX*)
505.0000 WRITE (11,93)
506.0000 93 FORMAT (10X,*YINP*,10X,*SQVEI*,9X,*V1*,9X,*UNY*)
507.0000 WRITE (11,94)
508.0000 94 FORMAT (10X,*ZPNP*,10X,*CP*,10X,*W1*,9X,*UNZ*/)
509.0000 DO 101 I=1,N
510.0000 U1=0.
511.0000 V1=0.
512.0000 W1=0.
513.0000 DO 102 J=1,N
514.0000 T1=UX(I,J)*S(I)
515.0000 T2=UY(I,J)*S(J)
516.0000 T3=UZ(I,J)*S(J)
517.0000 U1=U1+T1
518.0000 V1=V1+T2
519.0000 W1=W1+T3
520.0000 102 CONTINUE
521.0000 IF (ON(I) .EQ. 0.) GO TO 310
522.0000 U1=U1+COSM-UX(I)
523.0000 V1=V1+COSM-UY(I)
524.0000 W1=W1+COSM-UZ(I)
525.0000 310 CONTINUE
526.0000 U1=SQRT(U1**2+V1**2+W1**2)
527.0000 SQVEI=U1**2
528.0000 CP=1.-SQVEI
529.0000 PC1=CP*PDYN
530.0000 IF (ABS(A(1,1)) .GE. .5) GO TO 101
531.0000 WRITE (11,103) 1,A(1,1),VEI,U1,T(3,1-I)
532.0000 103 FORMAT (14,4F12.4)
533.0000 WRITE (11,104) A(2,I),SQVEI,V1,T(3,2,I)
534.0000 104 FORMAT (4X,4F12.4)
535.0000 WRITE (11,105) A(3,I),CP,W1,T(3,3,I)
536.0000 105 FORMAT (4X,4F12.4/)
537.0000 101 CONTINUE
538.0000 TTIME=TIM
539.0000 WRITE (11,926)
540.0000 926 FORMAT (//,* PRESSURES AT THE HOLE POINTS*)
541.0000 WRITE (11,927) (P(I),I=1,121)
542.0000 927 FORMAT (10(2X,F10.2))
543.0000 STOP
544.0000 END
545.0000 SUBROUTINE SETDEF (A,R,X,N)
546.0000 C
547.0000 C ITERATIVE SOLUTION OF A SET OF SIMULTANEOUS
548.0000 C LINEAR EQUATIONS USING THE GAUSS-SEIDEL METHOD
549.0000 C
550.0000 DIMENSION A(N,N),R(N),X(N),DMAT(175,175),PC(175),XOLD(175)

```

```

551.0000      DO 10 I=1,N
552.0000      Y(I)=0.
553.0000 10    CONTINUE
554.0000      TDI=1.E-4
555.0000      WRITE (11,15)
556.0000 15    FORMAT (/# VALUES OF 1ST AND LAST X-ELEMENTS 0#)
557.0000      DO 30 I=1,N
558.0000      IF (ABS(A(I,I)).LT.1.E-30) GO TO 40
559.0000      DO 20 J=1,N
560.0000      BMAT(I,J)=-A(I,J)/A(I,I)
561.0000      IF (I.EQ.J) BMAT(I,J)=0.
562.0000 20    CONTINUE
563.0000      C(I)=B(I)/A(I,I)
564.0000 30    CONTINUE
565.0000      GO TO 55
566.0000 40    WRITE (11,50) I
567.0000 50    FORMAT (#*,#DIAGONAL COEFFICIENT NO.%,I3,*,#=#0.%)
568.0000      STOP
569.0000 55    DO 110 M=1,500
570.0000      DO 90 I=1,N
571.0000      X(I)=X(I)
572.0000      SUM1=0.
573.0000      SUM2=0.
574.0000      IF (I.EQ.1) GO TO 70
575.0000      I1=I-1
576.0000      DO 60 J=1,I1
577.0000      SUM1=SUM1+BMAT(I,J)*X(J)
578.0000 60    CONTINUE
579.0000 70    I2=I+1
580.0000      IF (I2.GT.N) GO TO 85
581.0000      DO 80 J=I2,N
582.0000      SUM2=SUM2+BMAT(I,J)*X(J)
583.0000 80    CONTINUE
584.0000      X(I)=SUM1+SUM2+C(I)
585.0000 90    CONTINUE
586.0000      WRITE (11,95) X(I),X(N)
587.0000 95    FORMAT (2F12.5)
588.0000      RMAX=0.
589.0000      DO 100 I=1,N
590.0000      R=X(I)-X(I)
591.0000      IF (R.LT.TDI) GO TO 100
592.0000      RREL=ABS(R/X(I))
593.0000      RMAX=AMAX1(RMAX,RREL)
594.0000 100   CONTINUE
595.0000      IF (RMAX.LT.TDI) GO TO 130
596.0000 110   CONTINUE
597.0000      WRITE (11,120)
598.0000 120   FORMAT (#*,#DID NOT CONVERGE IN 500 ITERATIONS*)
599.0000      STOP
600.0000 130   RETURN
601.0000      END

```

Sample of Input Data

0.,0.,297.,,-138.,0.,0.,0.,,
25.,4.,

Sample of Output Data

1.0000											
2.0000											
3.0000	TH	VR	VR	VR	X1	Y1	Z1				
4.0000	0.0000	0.0000	297.0000	-138.0000	0.0000	0.0000	0.0000				
5.0000	THE TA	UP									
6.0000	4.341	4.0000									
7.0000											
8.0000	DR	BL	VR								
9.0000	4.1184	8.2368	327.4950								
10.0000											
11.0000	4.1184	8.2368	327.4950								
12.0000											
13.0000											
14.0000	K-COORDS. OF MILL POINTS										
15.0000	4.87	3.90	2.92	1.95	.97	.00	-.97	-1.95	-2.92	-3.90	
16.0000	-4.87	4.87	3.90	2.92	1.95	.97	.00	-.97	-1.95	-2.92	
17.0000	-3.90	-4.87	4.87	3.90	2.92	1.95	.97	.00	-.97	-1.95	
18.0000	-2.92	-3.90	-4.87	4.87	3.90	2.92	1.95	.97	.00	-.97	
19.0000	-1.95	-2.92	-3.90	-4.87	4.87	3.90	2.92	1.95	.97	.00	
20.0000	-.97	-1.95	-2.92	-3.90	-4.87	4.87	3.90	2.92	1.95	.97	
21.0000	.00	-.97	-1.95	-2.92	-3.90	-4.87	4.87	3.90	2.92	1.95	
22.0000	.97	.00	-.97	-1.95	-2.92	-3.90	-4.87	4.87	3.90	2.92	
23.0000	1.95	.97	.00	-.97	-1.95	-2.92	-3.90	-4.87	4.87	3.90	
24.0000	2.92	1.95	.97	.00	-.97	-1.95	-2.92	-3.90	-4.87	4.87	
25.0000	3.90	2.92	1.95	.97	.00	-.97	-1.95	-2.92	-3.90	-4.87	
26.0000	4.87	3.90	2.92	1.95	.97	.00	-.97	-1.95	-2.92	-3.90	
27.0000	-4.87										
28.0000											
29.0000											
30.0000	Y-COORDS. OF MILL POINTS										
31.0000	-3.90	-3.90	-3.90	-3.90	-3.90	-3.90	-3.90	-3.90	-3.90	-3.90	
32.0000	-2.92	-2.92	-2.92	-2.92	-2.92	-2.92	-2.92	-2.92	-2.92	-2.92	
33.0000	-1.95	-1.95	-1.95	-1.95	-1.95	-1.95	-1.95	-1.95	-1.95	-1.95	
34.0000	-.97	-.97	-.97	-.97	-.97	-.97	-.97	-.97	-.97	-.97	
35.0000	.00	.00	.00	.00	.00	.00	.00	.00	.00	.00	
36.0000	.97	.97	.97	.97	.97	.97	.97	.97	.97	.97	
37.0000	1.95	1.95	1.95	1.95	1.95	1.95	1.95	1.95	1.95	1.95	
38.0000	2.92	2.92	2.92	2.92	2.92	2.92	2.92	2.92	2.92	2.92	
39.0000	3.90	3.90	3.90	3.90	3.90	3.90	3.90	3.90	3.90	3.90	
40.0000	4.87	4.87	4.87	4.87	4.87	4.87	4.87	4.87	4.87	4.87	
41.0000	5.85	5.85	5.85	5.85	5.85	5.85	5.85	5.85	5.85	5.85	
42.0000	5.85	5.85	5.85	5.85	5.85	5.85	5.85	5.85	5.85	5.85	
43.0000	5.85	5.85	5.85	5.85	5.85	5.85	5.85	5.85	5.85	5.85	
44.0000											
45.0000											
46.0000	Z-COORDS. OF MILL POINTS										
47.0000	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	
48.0000	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	
49.0000	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	
50.0000	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	
51.0000	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	
52.0000	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	
53.0000	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	
54.0000	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	
55.0000	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	
56.0000	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	
57.0000	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	
58.0000	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	
59.0000	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	
60.0000	J= ELEMENT NUMBER										
61.0000	X1-X5 Y1-Y5 Z1-Z5 COORDINATES OF THE POINTS FORMING THE ELEMENT										
62.0000	X1-Y2 Y1-X2 Z1-Y3 Y1-Z3 COORDINATES OF THE POINTS FORMING THE ELEMENTS										
63.0000	Z1-Y2 Y1-Z2 Z1-X3 Y1-X3 COORDINATES OF THE POINTS FORMING THE ELEMENTS										
64.0000	UNX,UNY,UNZ COMPONENTS OF THE UNIT NORMAL VECTOR										
65.0000	XPMP,YPMP,ZPMP COORDINATES OF THE MILL POINT IN REFERENCE COORDINATE SYSTEM										
66.0000											
67.0000											
68.0000	J	X1	Y1	X2	Y2	UNX	XPMP	UNY	YPMP	UNZ	ZPMP
69.0000		Y1	Z1	Y2	Z2	UNY	YPMP	UNZ	ZPMP		
70.0000		Z1		Z2		UNZ	ZPMP				
71.0000	1	4.87	4.39	4.39	4.87	0.00	4.43	0.00	-1.90	0.00	
72.0000		-4.87	-4.39	-4.39	-4.87	0.00	4.43	0.00	-1.90	0.00	
73.0000		0.00	0.00	0.00	0.00	1.00	0.00	0.00	0.00	0.00	

76.0000	2	4.39	3.41	3.41	4.39	0.00	3.90
77.0000		-4.39	-4.39	-1.41	-1.41	0.00	-3.90
78.0000		0.00	0.00	0.00	0.00	1.00	0.00
79.0000							
80.0000	3	3.41	2.44	2.44	3.41	0.00	2.92
81.0000		-4.39	-4.39	-3.41	-3.41	0.00	-3.90
82.0000		0.00	0.00	0.00	0.00	1.00	0.00
83.0000							
84.0000	4	2.44	1.46	1.46	2.44	0.00	1.95
85.0000		-4.39	-4.39	-3.41	-3.41	0.00	-3.90
86.0000		0.00	0.00	0.00	0.00	1.00	0.00
87.0000							
88.0000	5	1.46	.49	.49	1.46	0.00	.97
89.0000		-4.39	-4.39	-3.41	-3.41	0.00	-3.90
90.0000		0.00	0.00	0.00	0.00	1.00	0.00
91.0000							
92.0000	6	.49	-.49	-.49	.49	0.00	.00
93.0000		-4.39	-4.39	-3.41	-3.41	0.00	-3.90
94.0000		0.00	0.00	0.00	0.00	1.00	0.00
95.0000							
96.0000	7	-1.46	-1.46	-1.46	-1.46	0.00	-.97
97.0000		-4.39	-4.39	-3.41	-3.41	0.00	-3.90
98.0000		0.00	0.00	0.00	0.00	1.00	0.00
99.0000							
100.0000	8	-2.44	-2.44	-2.44	-2.44	0.00	-1.95
101.0000		-4.39	-4.39	-3.41	-3.41	0.00	-3.90
102.0000		0.00	0.00	0.00	0.00	1.00	0.00
103.0000							
104.0000	9	-2.44	-1.41	-1.41	-2.44	0.00	-2.92
105.0000		-4.39	-4.39	-3.41	-3.41	0.00	-3.90
106.0000		0.00	0.00	0.00	0.00	1.00	0.00
107.0000							
108.0000	10	-3.41	-4.39	-4.39	-3.41	0.00	-3.90
109.0000		-4.39	-4.39	-3.41	-3.41	0.00	-3.90
110.0000		0.00	0.00	0.00	0.00	1.00	0.00
111.0000							
112.0000	11	-4.39	-5.36	-5.36	-4.39	0.00	-4.87
113.0000		-4.39	-4.39	-3.41	-3.41	0.00	-3.90
114.0000		0.00	0.00	0.00	0.00	1.00	0.00
115.0000							
116.0000	12	4.87	4.39	4.39	4.87	0.00	4.63
117.0000		-3.41	-3.41	-2.44	-2.44	0.00	-2.92
118.0000		0.00	0.00	0.00	0.00	1.00	0.00
119.0000							
120.0000	13	4.39	3.41	3.41	4.39	0.00	3.90
121.0000		-3.41	-3.41	-2.44	-2.44	0.00	-2.92
122.0000		0.00	0.00	0.00	0.00	1.00	0.00
123.0000							
124.0000	14	3.41	2.44	2.44	3.41	0.00	2.92
125.0000		-3.41	-3.41	-2.44	-2.44	0.00	-2.92
126.0000		0.00	0.00	0.00	0.00	1.00	0.00
127.0000							
128.0000	15	2.44	1.46	1.46	2.44	0.00	1.95
129.0000		-3.41	-3.41	-2.44	-2.44	0.00	-2.92
130.0000		0.00	0.00	0.00	0.00	1.00	0.00
131.0000							
132.0000	16	1.46	.49	.49	1.46	0.00	.97
133.0000		-3.41	-3.41	-2.44	-2.44	0.00	-2.92
134.0000		0.00	0.00	0.00	0.00	1.00	0.00
135.0000							
136.0000	17	.49	-.49	-.49	.49	0.00	.00
137.0000		-3.41	-3.41	-2.44	-2.44	0.00	-2.92
138.0000		0.00	0.00	0.00	0.00	1.00	0.00
139.0000							
140.0000	18	-1.46	-1.46	-1.46	-1.46	0.00	-.97
141.0000		-3.41	-3.41	-2.44	-2.44	0.00	-2.92
142.0000		0.00	0.00	0.00	0.00	1.00	0.00
143.0000							
144.0000	19	-1.46	-2.44	-2.44	-1.46	0.00	-1.95
145.0000		-3.41	-3.41	-2.44	-2.44	0.00	-2.92
146.0000		0.00	0.00	0.00	0.00	1.00	0.00
147.0000							
148.0000	20	-2.44	-3.41	-3.41	-2.44	0.00	-2.92
149.0000		-3.41	-3.41	-2.44	-2.44	0.00	-2.92
150.0000		0.00	0.00	0.00	0.00	1.00	0.00
151.0000							
152.0000	21	-3.41	-4.39	-4.39	-3.41	0.00	-3.90
153.0000		-3.41	-3.41	-2.44	-2.44	0.00	-2.92
154.0000		0.00	0.00	0.00	0.00	1.00	0.00
155.0000							
156.0000	22	-4.39	-5.36	-5.36	-4.39	0.00	-4.87
157.0000		-3.41	-3.41	-2.44	-2.44	0.00	-2.92
158.0000		0.00	0.00	0.00	0.00	1.00	0.00
159.0000							
160.0000	23	4.87	4.39	4.39	4.87	0.00	4.63
161.0000		-2.44	-2.44	-1.46	-1.46	0.00	-1.95
162.0000		0.00	0.00	0.00	0.00	1.00	0.00
163.0000							
164.0000	24	4.39	3.41	3.41	4.39	0.00	3.90
165.0000		-2.44	-2.44	-1.46	-1.46	0.00	-1.95
166.0000		0.00	0.00	0.00	0.00	1.00	0.00
167.0000							
168.0000	25	3.41	2.44	2.44	3.41	0.00	2.92
169.0000		-2.44	-2.44	-1.46	-1.46	0.00	-1.95
170.0000		0.00	0.00	0.00	0.00	1.00	0.00
171.0000							
172.0000	26	-2.44	1.46	1.46	-2.44	0.00	1.95
173.0000		-2.44	-2.44	-1.46	-1.46	0.00	-1.95
174.0000		0.00	0.00	0.00	0.00	1.00	0.00
175.0000							
176.0000	27	1.46	.49	.49	1.46	0.00	.97
177.0000		-2.44	-2.44	-1.46	-1.46	0.00	-1.95
178.0000		0.00	0.00	0.00	0.00	1.00	0.00
179.0000							

180.0000	28	.49	-.49	-.49	.49	0.00	.00
181.0000		-2.44	-2.44	-1.44	-1.44	0.00	-1.95
182.0000		0.00	0.00	0.00	0.00	1.00	0.00
183.0000							
184.0000	29	-.49	-1.44	-1.44	-.49	0.00	-.97
185.0000		-2.44	-2.44	-1.44	-1.44	0.00	-1.95
186.0000		0.00	0.00	0.00	0.00	1.00	0.00
187.0000							
188.0000	30	-1.44	-2.44	-2.44	-1.44	0.00	-1.95
189.0000		-2.44	-2.44	-1.44	-1.44	0.00	-1.95
190.0000		0.00	0.00	0.00	0.00	1.00	0.00
191.0000							
192.0000	31	-2.44	-3.41	-1.41	-2.44	0.00	-2.93
193.0000		-2.44	-2.44	-1.44	-1.44	0.00	-1.95
194.0000		0.00	0.00	0.00	0.00	1.00	0.00
195.0000							
196.0000	32	-3.41	-4.39	-4.39	-3.41	0.00	-3.90
197.0000		-2.44	-2.44	-1.44	-1.44	0.00	-1.95
198.0000		0.00	0.00	0.00	0.00	1.00	0.00
199.0000							
200.0000	33	-4.39	-5.36	-5.36	-4.39	0.00	-4.87
201.0000		-2.44	-2.44	-1.44	-1.44	0.00	-1.95
202.0000		0.00	0.00	0.00	0.00	1.00	0.00
203.0000							
204.0000	34	4.87	4.39	4.39	4.87	0.00	4.41
205.0000		-1.44	-1.44	-.49	-.49	0.00	-.97
206.0000		0.00	0.00	0.00	0.00	1.00	0.00
207.0000							
208.0000	35	4.39	3.41	3.41	4.39	0.00	3.90
209.0000		-1.44	-1.44	-.49	-.49	0.00	-.97
210.0000		0.00	0.00	0.00	0.00	1.00	0.00
211.0000							
212.0000	36	3.41	2.44	2.44	3.41	0.00	2.93
213.0000		-1.44	-1.44	-.49	-.49	0.00	-.97
214.0000		0.00	0.00	0.00	0.00	1.00	0.00
215.0000							
216.0000	37	2.44	1.44	1.44	2.44	0.00	1.95
217.0000		-1.44	-1.44	-.49	-.49	0.00	-.97
218.0000		0.00	0.00	0.00	0.00	1.00	0.00
219.0000							
220.0000	38	1.44	.49	.49	1.44	0.00	.97
221.0000		-1.44	-1.44	-.49	-.49	0.00	-.97
222.0000		0.00	0.00	0.00	0.00	1.00	0.00
223.0000							
224.0000	39	.49	-.49	-.49	.49	0.00	.00
225.0000		-1.44	-1.44	-.49	-.49	0.00	-.97
226.0000		0.00	0.00	0.00	0.00	1.00	0.00
227.0000							
228.0000	40	-.49	-1.44	-1.44	-.49	0.00	-.97
229.0000		-1.44	-1.44	-.49	-.49	0.00	-.97
230.0000		0.00	0.00	0.00	0.00	1.00	0.00
231.0000							
232.0000	41	-1.44	-2.44	-2.44	-1.44	0.00	-1.95
233.0000		-1.44	-1.44	-.49	-.49	0.00	-.97
234.0000		0.00	0.00	0.00	0.00	1.00	0.00
235.0000							
236.0000	42	-2.44	-3.41	-3.41	-2.44	0.00	-2.93
237.0000		-1.44	-1.44	-.49	-.49	0.00	-.97
238.0000		0.00	0.00	0.00	0.00	1.00	0.00
239.0000							
240.0000	43	-3.41	-4.39	-4.39	-3.41	0.00	-3.90
241.0000		-1.44	-1.44	-.49	-.49	0.00	-.97
242.0000		0.00	0.00	0.00	0.00	1.00	0.00
243.0000							
244.0000	44	-4.39	-5.36	-5.36	-4.39	0.00	-4.87
245.0000		-1.44	-1.44	-.49	-.49	0.00	-.97
246.0000		0.00	0.00	0.00	0.00	1.00	0.00
247.0000							
248.0000	45	4.87	4.39	4.39	4.87	0.00	4.41
249.0000		-.49	-.49	-.49	.49	0.00	-.00
250.0000		0.00	0.00	0.00	0.00	1.00	0.00
251.0000							
252.0000	46	4.39	3.41	3.41	4.39	0.00	3.90
253.0000		-.49	-.49	-.49	.49	0.00	-.00
254.0000		0.00	0.00	0.00	0.00	1.00	0.00
255.0000							
256.0000	47	3.41	2.44	2.44	3.41	0.00	2.93
257.0000		-.49	-.49	-.49	.49	0.00	-.00
258.0000		0.00	0.00	0.00	0.00	1.00	0.00
259.0000							
260.0000	48	2.44	1.44	1.44	2.44	0.00	1.95
261.0000		-.49	-.49	-.49	.49	0.00	-.00
262.0000		0.00	0.00	0.00	0.00	1.00	0.00
263.0000							
264.0000	49	1.44	.49	.49	1.44	0.00	.97
265.0000		-.49	-.49	-.49	.49	0.00	-.00
266.0000		0.00	0.00	0.00	0.00	1.00	0.00
267.0000							
268.0000	50	.49	-.49	-.49	.49	0.00	.00
269.0000		-.49	-.49	-.49	.49	0.00	-.00
270.0000		0.00	0.00	0.00	0.00	1.00	0.00
271.0000							
272.0000	51	-.49	-1.44	-1.44	-.49	0.00	-.97
273.0000		-.49	-.49	-.49	.49	0.00	-.00
274.0000		0.00	0.00	0.00	0.00	1.00	0.00
275.0000							
276.0000	52	-1.44	-2.44	-2.44	-1.44	0.00	-1.95
277.0000		-.49	-.49	-.49	.49	0.00	-.00
278.0000		0.00	0.00	0.00	0.00	1.00	0.00
279.0000							
280.0000	53	-2.44	-3.41	-3.41	-2.44	0.00	-2.93
281.0000		-.49	-.49	-.49	.49	0.00	-.00
282.0000		0.00	0.00	0.00	0.00	1.00	0.00
283.0000							

284.0000	54	-3.41	-4.19	-4.39	-1.41	0.00	-3.90
287.0000		.49	.49	.49	.49	0.00	-.00
288.0000		0.00	0.00	0.00	0.00	1.00	0.00
287.0000	55	-4.39	-5.36	-5.36	-4.39	0.00	-4.87
289.0000		.49	.49	.49	.49	0.00	-.00
290.0000		0.00	0.00	0.00	0.00	1.00	0.00
291.0000	56	4.87	4.39	4.39	4.87	0.00	4.61
293.0000		.49	.49	1.46	1.46	0.00	.97
294.0000		0.00	0.00	0.00	0.00	1.00	0.00
295.0000	57	4.39	3.41	3.41	4.39	0.00	3.90
297.0000		.49	.49	1.46	1.46	0.00	.97
298.0000		0.00	0.00	0.00	0.00	1.00	0.00
299.0000	58	3.41	2.44	2.44	3.41	0.00	2.92
301.0000		.49	.49	1.46	1.46	0.00	.97
302.0000		0.00	0.00	0.00	0.00	1.00	0.00
303.0000	59	2.44	1.46	1.46	2.44	0.00	1.95
305.0000		.49	.49	1.46	1.46	0.00	.97
306.0000		0.00	0.00	0.00	0.00	1.00	0.00
307.0000	60	1.46	.49	.49	1.46	0.00	.97
309.0000		.49	.49	1.46	1.46	0.00	.97
310.0000		0.00	0.00	0.00	0.00	1.00	0.00
311.0000	61	.49	.49	.49	.49	0.00	.00
313.0000		.49	.49	1.46	1.46	0.00	.97
314.0000		0.00	0.00	0.00	0.00	1.00	0.00
315.0000	62	.49	-1.46	-1.46	.49	0.00	-.97
317.0000		.49	.49	1.46	1.46	0.00	.97
318.0000		0.00	0.00	0.00	0.00	1.00	0.00
319.0000	63	-1.46	-2.44	-2.44	-1.46	0.00	-1.95
320.0000		.49	.49	1.46	1.46	0.00	.97
321.0000		0.00	0.00	0.00	0.00	1.00	0.00
322.0000	64	-2.44	-1.41	-1.41	-2.44	0.00	-2.92
325.0000		.49	.49	1.46	1.46	0.00	.97
326.0000		0.00	0.00	0.00	0.00	1.00	0.00
327.0000	65	-3.41	-4.39	-4.39	-3.41	0.00	-3.90
329.0000		.49	.49	1.46	1.46	0.00	.97
330.0000		0.00	0.00	0.00	0.00	1.00	0.00
331.0000	66	-4.39	-5.36	-5.36	-4.39	0.00	-4.87
332.0000		.49	.49	1.46	1.46	0.00	.97
333.0000		0.00	0.00	0.00	0.00	1.00	0.00
334.0000	67	4.87	4.39	4.39	4.87	0.00	4.61
337.0000		1.46	1.46	2.44	2.44	0.00	1.95
338.0000		0.00	0.00	0.00	0.00	1.00	0.00
339.0000	68	4.39	3.41	3.41	4.39	0.00	3.90
341.0000		1.46	1.46	2.44	2.44	0.00	1.95
342.0000		0.00	0.00	0.00	0.00	1.00	0.00
343.0000	69	3.41	2.44	2.44	3.41	0.00	2.92
344.0000		1.46	1.46	2.44	2.44	0.00	1.95
345.0000		0.00	0.00	0.00	0.00	1.00	0.00
347.0000	70	2.44	1.46	1.46	2.44	0.00	1.95
348.0000		1.46	1.46	2.44	2.44	0.00	1.95
350.0000		0.00	0.00	0.00	0.00	1.00	0.00
351.0000	71	1.46	.49	.49	1.46	0.00	.97
352.0000		1.46	1.46	2.44	2.44	0.00	1.95
354.0000		0.00	0.00	0.00	0.00	1.00	0.00
355.0000	72	.49	.49	.49	.49	0.00	.00
356.0000		1.46	1.46	2.44	2.44	0.00	1.95
357.0000		0.00	0.00	0.00	0.00	1.00	0.00
358.0000	73	-4.39	-1.46	-1.46	-4.39	0.00	-4.87
361.0000		1.46	1.46	2.44	2.44	0.00	1.95
362.0000		0.00	0.00	0.00	0.00	1.00	0.00
363.0000	74	-1.46	-2.44	-2.44	-1.46	0.00	-1.95
365.0000		1.46	1.46	2.44	2.44	0.00	1.95
366.0000		0.00	0.00	0.00	0.00	1.00	0.00
367.0000	75	-3.41	-3.41	-3.41	-3.41	0.00	-2.92
369.0000		1.46	1.46	2.44	2.44	0.00	1.95
370.0000		0.00	0.00	0.00	0.00	1.00	0.00
371.0000	76	-1.41	-4.39	-4.39	-3.41	0.00	-1.90
372.0000		1.46	1.46	2.44	2.44	0.00	1.95
374.0000		0.00	0.00	0.00	0.00	1.00	0.00
375.0000	77	-4.39	-5.36	-5.36	-4.39	0.00	-4.87
376.0000		1.46	1.46	2.44	2.44	0.00	1.95
379.0000		0.00	0.00	0.00	0.00	1.00	0.00
379.0000	78	4.87	4.39	4.39	4.87	0.00	4.61
381.0000		2.44	2.44	3.41	3.41	0.00	2.92
382.0000		0.00	0.00	0.00	0.00	1.00	0.00
383.0000	79	4.39	3.41	3.41	4.39	0.00	3.90
385.0000		2.44	2.44	3.41	3.41	0.00	2.92
386.0000		0.00	0.00	0.00	0.00	1.00	0.00

380,0000	80	3.41	2.44	2.44	3.41	0.00	2.92
381,0000		2.44	2.44	2.44	3.41	0.00	2.92
382,0000		0.00	0.00	0.00	0.00	1.00	0.00
383,0000		0.00	0.00	0.00	0.00	0.00	0.00
384,0000	81	2.44	1.46	1.46	2.44	0.00	1.95
385,0000		2.44	1.46	1.46	3.41	0.00	2.92
386,0000		0.00	0.00	0.00	0.00	1.00	0.00
387,0000		0.00	0.00	0.00	0.00	0.00	0.00
388,0000	82	1.46	.49	.49	1.46	0.00	.92
389,0000		2.44	2.44	3.41	3.41	0.00	2.92
390,0000		0.00	0.00	0.00	0.00	1.00	0.00
391,0000		0.00	0.00	0.00	0.00	0.00	0.00
392,0000	83	.49	-.49	-.49	.49	0.00	-.00
393,0000		2.44	2.44	3.41	3.41	0.00	2.92
394,0000		0.00	0.00	0.00	0.00	1.00	0.00
395,0000		0.00	0.00	0.00	0.00	0.00	0.00
396,0000	84	-.49	-1.46	-1.46	-.49	0.00	-.92
397,0000		2.44	2.44	3.41	3.41	0.00	2.92
398,0000		0.00	0.00	0.00	0.00	1.00	0.00
399,0000		0.00	0.00	0.00	0.00	0.00	0.00
400,0000	85	-1.46	-2.44	-2.44	-1.46	0.00	-1.95
401,0000		2.44	2.44	3.41	3.41	0.00	2.92
402,0000		0.00	0.00	0.00	0.00	1.00	0.00
403,0000		0.00	0.00	0.00	0.00	0.00	0.00
404,0000	86	-2.44	-1.41	-1.41	-2.44	0.00	-2.92
405,0000		2.44	2.44	3.41	3.41	0.00	2.92
406,0000		0.00	0.00	0.00	0.00	1.00	0.00
407,0000		0.00	0.00	0.00	0.00	0.00	0.00
408,0000	87	-3.41	-4.39	-4.39	-3.41	0.00	-3.90
409,0000		2.44	2.44	3.41	3.41	0.00	2.92
410,0000		0.00	0.00	0.00	0.00	1.00	0.00
411,0000		0.00	0.00	0.00	0.00	0.00	0.00
412,0000	88	-4.39	-5.36	-5.36	-4.39	0.00	-4.87
413,0000		2.44	2.44	3.41	3.41	0.00	2.92
414,0000		0.00	0.00	0.00	0.00	1.00	0.00
415,0000		0.00	0.00	0.00	0.00	0.00	0.00
416,0000	89	4.39	3.41	3.41	4.39	0.00	3.90
417,0000		3.41	3.41	4.39	4.39	0.00	3.90
418,0000		0.00	0.00	0.00	0.00	1.00	0.00
419,0000		0.00	0.00	0.00	0.00	0.00	0.00
420,0000	90	3.41	2.44	2.44	3.41	0.00	2.92
421,0000		3.41	3.41	4.39	4.39	0.00	3.90
422,0000		0.00	0.00	0.00	0.00	1.00	0.00
423,0000		0.00	0.00	0.00	0.00	0.00	0.00
424,0000	91	4.39	4.39	4.39	4.39	0.00	4.87
425,0000		3.41	3.41	4.39	4.39	0.00	3.90
426,0000		0.00	0.00	0.00	0.00	1.00	0.00
427,0000		0.00	0.00	0.00	0.00	0.00	0.00
428,0000	92	4.39	3.41	3.41	4.39	0.00	3.90
429,0000		3.41	3.41	4.39	4.39	0.00	3.90
430,0000		0.00	0.00	0.00	0.00	1.00	0.00
431,0000		0.00	0.00	0.00	0.00	0.00	0.00
432,0000	93	3.41	2.44	2.44	3.41	0.00	2.92
433,0000		3.41	3.41	4.39	4.39	0.00	3.90
434,0000		0.00	0.00	0.00	0.00	1.00	0.00
435,0000		0.00	0.00	0.00	0.00	0.00	0.00
436,0000	94	2.44	1.46	1.46	2.44	0.00	1.95
437,0000		3.41	3.41	4.39	4.39	0.00	3.90
438,0000		0.00	0.00	0.00	0.00	1.00	0.00
439,0000		0.00	0.00	0.00	0.00	0.00	0.00
440,0000	95	1.46	.49	.49	1.46	0.00	.92
441,0000		3.41	3.41	4.39	4.39	0.00	3.90
442,0000		0.00	0.00	0.00	0.00	1.00	0.00
443,0000		0.00	0.00	0.00	0.00	0.00	0.00
444,0000	96	.49	-.49	-.49	.49	0.00	-.00
445,0000		1.41	1.41	2.38	2.38	0.00	1.90
446,0000		0.00	0.00	0.00	0.00	1.00	0.00
447,0000		0.00	0.00	0.00	0.00	0.00	0.00
448,0000	97	-.49	-1.46	-1.46	-.49	0.00	-.92
449,0000		1.41	1.41	2.38	2.38	0.00	1.90
450,0000		0.00	0.00	0.00	0.00	1.00	0.00
451,0000		0.00	0.00	0.00	0.00	0.00	0.00
452,0000	98	1.46	-2.44	-2.44	-1.46	0.00	-1.95
453,0000		3.41	3.41	4.39	4.39	0.00	3.90
454,0000		0.00	0.00	0.00	0.00	1.00	0.00
455,0000		0.00	0.00	0.00	0.00	0.00	0.00
456,0000	99	-2.44	-1.41	-1.41	-2.44	0.00	-2.92
457,0000		3.41	3.41	4.39	4.39	0.00	3.90
458,0000		0.00	0.00	0.00	0.00	1.00	0.00
459,0000		0.00	0.00	0.00	0.00	0.00	0.00
460,0000	100	-1.41	-4.39	-4.39	-1.41	0.00	-1.90
461,0000		1.41	1.41	2.38	2.38	0.00	1.90
462,0000		0.00	0.00	0.00	0.00	1.00	0.00
463,0000		0.00	0.00	0.00	0.00	0.00	0.00
464,0000	101	-4.39	-5.36	-5.36	-4.39	0.00	-4.87
465,0000		1.41	1.41	2.38	2.38	0.00	1.90
466,0000		0.00	0.00	0.00	0.00	1.00	0.00
467,0000		0.00	0.00	0.00	0.00	0.00	0.00
468,0000	102	4.39	3.41	3.41	4.39	0.00	3.90
469,0000		4.39	4.39	5.36	5.36	0.00	4.87
470,0000		0.00	0.00	0.00	0.00	1.00	0.00
471,0000		0.00	0.00	0.00	0.00	0.00	0.00
472,0000	103	3.41	2.44	2.44	3.41	0.00	2.92
473,0000		4.39	4.39	5.36	5.36	0.00	4.87
474,0000		0.00	0.00	0.00	0.00	1.00	0.00
475,0000		0.00	0.00	0.00	0.00	0.00	0.00
476,0000	104	1.41	1.41	2.38	2.38	0.00	1.90
477,0000		4.39	4.39	5.36	5.36	0.00	4.87
478,0000		0.00	0.00	0.00	0.00	1.00	0.00
479,0000		0.00	0.00	0.00	0.00	0.00	0.00
480,0000	105	1.46	.49	.49	1.46	0.00	.92
481,0000		4.39	4.39	5.36	5.36	0.00	4.87
482,0000		0.00	0.00	0.00	0.00	1.00	0.00
483,0000		0.00	0.00	0.00	0.00	0.00	0.00
484,0000	106	-.49	-.49	-.49	-.49	0.00	-.00
485,0000		4.39	4.39	5.36	5.36	0.00	4.87
486,0000		0.00	0.00	0.00	0.00	1.00	0.00
487,0000		0.00	0.00	0.00	0.00	0.00	0.00
488,0000	107	4.39	3.41	3.41	4.39	0.00	3.90
489,0000		4.39	4.39	5.36	5.36	0.00	4.87
490,0000		0.00	0.00	0.00	0.00	1.00	0.00
491,0000		0.00	0.00	0.00	0.00	0.00	0.00

477.0000	106	-1.47	-1.46	-1.45	-1.47	0.00	-1.97
481.0000		4.19	4.19	5.16	5.16	0.00	4.87
484.0000		0.00	0.00	0.00	0.00	1.00	0.00
487.0000	107	-1.46	-1.44	-1.44	-1.46	0.00	-1.97
491.0000		4.19	4.19	5.16	5.16	0.00	4.87
494.0000		0.00	0.00	0.00	0.00	1.00	0.00
497.0000	108	-1.44	-1.41	-1.41	-1.44	0.00	-1.97
501.0000		4.19	4.19	5.16	5.16	0.00	4.87
505.0000		0.00	0.00	0.00	0.00	1.00	0.00
508.0000	109	-1.41	-1.39	-1.39	-1.41	0.00	-1.90
512.0000		4.19	4.19	5.16	5.16	0.00	4.87
516.0000		0.00	0.00	0.00	0.00	1.00	0.00
519.0000	110	-1.39	-1.36	-1.36	-1.39	0.00	-1.87
523.0000		4.19	4.19	5.16	5.16	0.00	4.87
527.0000		0.00	0.00	0.00	0.00	1.00	0.00
530.0000	111	4.87	4.19	4.19	4.87	0.00	4.81
534.0000		5.16	5.16	6.13	6.13	0.00	5.85
538.0000		0.00	0.00	0.00	0.00	1.00	0.00
541.0000	112	4.19	3.41	3.41	4.19	0.00	1.90
545.0000		5.16	5.16	6.13	6.13	0.00	5.85
549.0000		0.00	0.00	0.00	0.00	1.00	0.00
552.0000	113	3.41	2.44	2.44	3.41	0.00	1.97
556.0000		5.16	5.16	6.13	6.13	0.00	5.85
560.0000		0.00	0.00	0.00	0.00	1.00	0.00
563.0000	114	2.44	1.46	1.46	2.44	0.00	1.95
567.0000		5.16	5.16	6.13	6.13	0.00	5.85
571.0000		0.00	0.00	0.00	0.00	1.00	0.00
574.0000	115	1.46	1.49	1.49	1.46	0.00	1.97
578.0000		5.16	5.16	6.13	6.13	0.00	5.85
582.0000		0.00	0.00	0.00	0.00	1.00	0.00
585.0000	116	1.49	1.49	1.49	1.49	0.00	1.00
589.0000		5.16	5.16	6.13	6.13	0.00	5.85
593.0000		0.00	0.00	0.00	0.00	1.00	0.00
596.0000	117	-1.49	-1.46	-1.46	-1.49	0.00	-1.97
600.0000		5.16	5.16	6.13	6.13	0.00	5.85
604.0000		0.00	0.00	0.00	0.00	1.00	0.00
607.0000	118	-1.46	-1.44	-1.44	-1.46	0.00	-1.95
611.0000		5.16	5.16	6.13	6.13	0.00	5.85
615.0000		0.00	0.00	0.00	0.00	1.00	0.00
618.0000	119	-1.44	-1.41	-1.41	-1.44	0.00	-1.97
622.0000		5.16	5.16	6.13	6.13	0.00	5.85
626.0000		0.00	0.00	0.00	0.00	1.00	0.00
629.0000	120	-1.41	-1.39	-1.39	-1.41	0.00	-1.90
633.0000		5.16	5.16	6.13	6.13	0.00	5.85
637.0000		0.00	0.00	0.00	0.00	1.00	0.00
640.0000	121	-1.39	-1.36	-1.36	-1.39	0.00	-1.87
644.0000		5.16	5.16	6.13	6.13	0.00	5.85
648.0000		0.00	0.00	0.00	0.00	1.00	0.00

IMPACT POINT IS ON ELEMENT NO

VALUES OF 1ST AND LAST X-ELEMENTS 0				
0.00000	0.00000			
0.00000	0.00000			
561.0000	4	0.0000	.6667	.0000
562.0000		-1.0000	.4445	.6667
563.0000		0.0000	.5555	-.0000
564.0000				
565.0000	17	0.0000	.7075	.0000
570.0000		-1.9715	.4302	.7075
571.0000		0.0000	.3798	-.0000
572.0000				
573.0000	28	0.0000	.8747	.0000
574.0000		-1.9490	.4878	.8747
575.0000		0.0000	.3142	-.0000
576.0000				
577.0000	39	0.0000	.8610	.0000
578.0000		-1.9745	.7613	.8610
579.0000		0.0000	.2387	-.0000
580.0000				
581.0000	50	0.0000	.8145	.0000
582.0000		-1.9800	.8176	.9047
583.0000		0.0000	.1824	-.0000
584.0000				
585.0000	41	0.0000	.9447	.0000
586.0000		-1.9745	.8643	.9447
587.0000		0.0000	-.1037	-.0000
588.0000				
589.0000	72	0.0000	.9700	.0000
590.0000		-1.9490	.9544	.9700
591.0000		0.0000	.0456	-.0000
592.0000				
593.0000	83	0.0000	1.0079	.0000
594.0000		-1.9235	1.0160	1.0079
595.0000		0.0000	-.0160	-.0000
596.0000				

REFERENCES

1. Barber, J.P. and J.S. Wilbeck, "The Characterization of Bird Impacts on a Rigid Plate: Part I," AFFDL-TR-75-5, January 1975.
2. Peterson, R.L. and J.P. Barber, "Bird Impact Forces in Aircraft Windshield Design," AFFDL-TR-75-150, March 1976.
3. Barber, J.P., H.R. Taylor, and J.S. Wilbeck, "Bird Impact Forces and Pressures on Rigid and Compliant Targets," AFFDL-TR-77-60, May 1978.
4. Wilbeck, J.S., "Impact Behavior of Low Strength Projectiles," AFML-TR-77-134, July 1978.
5. Bauer, D.P. and J.P. Barber, "Experimental Investigation of Impact Pressures Caused by Gelatin Simulated Birds and Ice," UDR-TR-78-114, November 1978.
6. Boehman, L.I. and A. Challita, "A Model for Predicting Bird and Ice Impact Loads on Structures," UDR-TR-79-54.