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Research Report 78-2

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VALIDATION AND ERROR IN MULTIPLICATIVE

UTILITY FUNCTIONS

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December, 1978

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SUMMARY

In this report an approach to the concept of error in utility assessment is proposed. Three components of error are considered and each component is related to four separate elicitation methods -- all in the context of a general multiplicative multiattribute utility model. The methods are a Keeney-Raiffa (1976) procedure, SMART (Edwards, 1977), a <u>social judgment theory</u> (SJT) based regression model (Hammond, Stewart, Brehmer and Steinmann, 1975) and a new method called <u>Holistic Orthogonal</u> Parameter Estimation or HOPE (Barron and Person, 1978).

If a general multiplicative model can be assumed to be an appropriate representation of the decision maker's basic preference structure, error can occur in the direct estimation of the scaling constants and univariate utility functions for decomposition methods (Keeney-Raiffa and SMART), or in the holistic assessments for holistic methods (SJT and HOPE). Individual estimates may be merely noisy or may be fundamentally incorrect. Furthermore, the utility model may be incorrectly specified; for example, an additive model, rather than a multiplicitive model, may be used. The four assessment methods are considered in conjunction with errors of each kind.

The most serious error-method combination is the case of a substantial degree of error occurring in a single holistic judgment which is being used in a HOPE procedure. This concern leads to a major emphasis of this report -- an expanded HOPE procedure used in conjunction with a convergent validation strategy to estimate error in individual holistic judgments and thus guide consistency checks.

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The discussion is organized into four sections. The HOPE procedure is summarized in Section I. In Section II, three components of assessment error are considered in conjunction with the four elicitation procedures. In Section III, an expanded HOPE procedure for detecting judgment error and guiding consistency charks is proposed. In Section IV, application considerations are outlined.

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ACKNOWLEDGEMENT

We would like to thank the Advanced Research Projects Agency of the Department of Defense whose support made this research possible. This research was monitored by the Office of Naval Research under contract #N0001476-C-0074, under subcontract from Decisions and Designs, Inc. #76-030-0715.

In addition, the author wishes to thank Ward Edwards and Richard John for their thoughtful comments on an earlier draft of this paper.

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Introduction

In this report an approach to the concept of error in utility assessment is proposed. Three components of error are distinguished; these components are then related to four separate elicitation methods -- each of which is consistent with at least special cases of the general multiplicative <u>multiattribute utility</u> (MAU) model (below). Two methods, Keeney-Raiffa (1976) and SMART (Edwards, 1977) are pure decomposition approaches; a third, the social judgment paradigm (Hammond, Stewart, Brehmer, and Steinmann, 1975) is a regression approach which relies on holistic judgments.

The fourth approach is a decomposition procedure for assessing multiplicative MAU functions which relies solely on a few holistic assessments of utilities. The procedure's acronym is HOPE for <u>Holistic</u> <u>Orthogonal Parameter Estimation</u>. Consistent with the procedures of Keeney and Raiffa (1976), the HOPE procedure exploits the basic preferences of the decision maker to specify the utility function. HOPE differs in that it uses a response mode more familiar to laymen than those of other methods of MAU elicitation -- holistic assessment of (a few) profiles -- to determine the scaling constants and univariate utility functions comprising the multiplicative utility function.

The larger question behind any analysis of error in assessed utility functions concerns validation. There are three basic approaches to validation of assessed utility functions: (1) use of an external criterion; (2) validating the basic preference structure of the decision maker; (3) convergent validity. Of these, the most straightforward is use of an objective, externally defined, criterion, <u>if</u> one is available. Edwards (1974) has suggested two instances of available criteria -diamonds and bank credit. The American Gemological Institute "diamond model" formally evaluates diamonds based on the four attributes: color, cut, clarity, and carats. Banks evaluate applicants for credit cards on the basis of attributes contained on standard application forms (e.g., disposable income, own versus rent, debt, employment history, etc.); while actual probability and amount of default, if any, are known empirically.

Edwards and his associates have suggested a variant of the multiple cue probability learning paradigm (Hammond, Stewart, Brehmer and Steinmann, 1975) as a means of creating an external criterion. Subjects are first trained to use a weighted additive utility functions; this is followed by eliciting learned utilities. This procedure has been pilottested at SSRI.

The purpose of studies using an external criterion is to compare and evaluate the performance of elicitation techniques. The usefulness of such studies rests on the assumption that comparative efficacy of elicitation methods generalizes from situations where an external criterion exists to situations where one does not. Of course, external criteria do not generally exist in <u>de novo</u> assessment of utilities in laboratory or field settings. Furthermore, elicitation is unnecessary when such a criterion exists. Thus, in application as opposed to experimental settings, validity necessarily depends on either validation of the basic preference ...odel itself or on convergent validity.

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Validating the basic preference model requires verifying qualitative properties of preferences which are sufficient for representing preferences by a particular mathematical model. In the decomposition approach of Keeney and Raiffa (1976), the qualitative properties of preferential independence and utility independence are explicitly examined. Preferential independence requires that preference orders over attribute pairs be independent of the fixed levels of the remaining attributes. Utility independence requires that preferences for lotteries involving a single attribute be independent of the fixed levels of the remaining attributes. If these qualitative properties of preferences hold, then the preference structure can be represented by either a multiplicative model, equation (1), or by an additive model, equation (2).

$$1 + KU(x_1, x_2, \dots, x_n) = \prod_{i=1}^n (1 + Kk_i u_i(x_i))$$
(1)

where, for i = 1, 2, ..., n

 x_i is level i of attribute X_i $0 \le u_i(\cdot) \le 1$ is a utility function $0 \le k_i \le 1$ is a scaling constant $-1 \le K$ is a parameter

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U(•) is overall utility.

Upon writing equation (1) simply as an expression for $U(\cdot)$ and taking limits as K goes to 0, the resulting model is the additive model, equation (2):

$$U(x_1, x_2, ..., x_n) = \sum_{i=1}^n k_i u_i(x_i)$$
 (2)

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The basic preference model is validated by checking the conditions of preferential and utility independence. For an especially informative assessment protocol in which the conditions are checked, see Keeney (1977).

The choice between models 1 and 2 in an application setting is not necessarily a simple choice. The choice can be viewed as an empirical question, in which the parameter K = 0 if and only if $\sum_{i=1}^{n} k_i = 1$. The choice can be based behaviorally on the marginality condition (Fishburn, 1965). Model 2 is appropriate only if the decision maker's preferences for multiattributed risk consequences depend only on the marginal distribution associated with each attribute. Experimental studies (e.g., both conducted and surveyed by von Winterfeldt (1976)) have often found violations of the marginality condition. Finally, the choice can be made on more pragmatic grounds. Additive models are simpler, provide excellent predictions, and can be used in conjunction with simpler procedures (e.g., the SMART procedure discussed in this report). In fact, referring to the same experimental studies von Winterfeldt states:

The message that these experiments convey seems contradictory: in spite of obvious model violations (tests of marginality and tests of risky additivity failed), additive models . . . predict subjects' preferences and utility judgments very well (p. 24).

Convergent validation assumes that logically equivalent elicitation procedures will assign comparable utilities to the same multi-attributed outcome. In his convergent validation study Fischer (1977) elicited utilities for 27 hypothetical jobs from each of 10 subjects in three different ways: (1) direct holistic assessments, (2) via a Keeney-Raiffa decomposition, and (3) via the SMART procedure. The utilities

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predicted for the 27 jobs (within subject) by the Keeney-Raiffa and SMART procedures exhibited high correlations with each other and were highly correlated with the holistic assessments.

Slovic, Fischhoff and Lichtenstein (1977) have criticized using correlation between predictions of MAU models and holistic judgments as evidence that the MAU model is valid. Their criticism is based on the use of unaided holistic preference as a criterion. They further state, ". . . a decade or more of research has abundantly documented that humans are quite bad at making complex unaided decisions (Slovic [1972]); it could thus be argued that high correlations with such flawed judgments would suggest a <u>lack</u> of validity" [p. 22].

At face value the remarks of Slovic <u>et al.</u> are damaging to the HOPE procedure described in this report. In fact, a major emphasis of this report is the use of an expanded HOPE procedure in conjunction with a convergent validation strategy to estimate prediction (of utilities) error, and to thus identify <u>outliers</u> in the set of holistic judgments. Thus, the view represented by the remarks of Slovic <u>et al.</u> must be considered.

I believe decision makers can provide useful holistic assessments of (a few) multiattributed consequences, especially in cases involving a small number of attributes, say fewer than ten. Furthermore, there is considerable evidence to support my belief. Two research traditions, heavily based on holistic assessment, are social judgment theory (Hammond <u>et al.</u>) and information integration theory (Anderson [1974]). Numerous empirical studies in these traditions alone constitute examples of

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judges providing holistic judgments. Of course, neither the cognitive processes which produce holistic judgments are well understood, nor are the exact parameters of such judgments known. It is generally accepted that such judgments are often systematic, but noisy (Fischer, 1977); in fact, bootstrapping (Dawes and Corrigan, 1974) capitalizes on these features. It is also presumed that noise increases as the number of attributes increases. Finally, it is plausible to presume that noise increases as the number of required holistic evaluations increases.

The HOPE procedure requires direct holistic assessment of the utility of each of a small number of multistributed consequences comprising a highly fractionated experimental design. By small number, I mean fewer than fifty consequences, a number suggested by both Keeney and Raiffa (1976, p. 222) and Fischer (1977). My basic assumption is that decision makers can provide the requisite holistic assessments; furthermore I recognize that these assessments will be noisy. Moderate noise, per se, does not materially reduce the efficacy of the HOPE procedure. A previous paper (Barron and Person, 1978) demonstrated that the HOPE procedure could recover known MAU functions from simulated noisy holistic judgments. Recovery was excellent in the presence of moderate amounts of noise -- defined as normally distributed additive error having a standard deviation of .05. Model specification error -defined as the use of an additive model fitted to error-free holistic judgments computed from known multiplicative models -- produced higher prediction error than did moderate noise in conjunction with an appropriate multiplicative model using an estimated K value.

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The HOPE procedure generalizes a procedure for estimating main effects in an <u>additive</u> model (Green, 1971), to the assessment of the <u>multiplicative</u> utility functions of Keeney (1974). Multiplicative (and additive) utility functions are of interest for three reasons. First, the multiplicative model represents the decision maker's preference structure if certain preferential and utility independence conditions are satisfied. In those cases in which these conditions have been verified, the multiplicative model is valid. Second, the multiplicative utility function is of practical importance, even if the requisite assumptions do not hold precisely (Keeney and Raiffa, 1976, p. 298). Third, formally the general rultiplicative model encompasses the kinds of utility functions resulting from each of the four assessment approaches considered in this paper.

This report is organized into four sections. The HOPE elicitation procedure is described in section I. In section II, three components of utility assessment error are considered in conjunction with the four elicitation procedures. In section III, a method for detection of judgment error is proposed and illustrated by application to the data of Fischer (1977). In section IV, application considerations are outlined.

I. HOPE: A Utility Elicitation Procedure

The HOPE and Keeney-Raiffa^{*} procedures differ only in the parameter estimation phase. HOPE estimates the parameters -- the univariate

^TSection I is a revised version of section I of Barron and Person (1978).

"Unless noted otherwise, by "a Keeney-Raiffa procedure" is meant their general approach to assessing a multiplicative utility function as described in Keeney and Raiffa, 1976, pp. 297-304.

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utility functions and scaling constants -- of the multiplicative family of utility functions from holistic judgments of utility. The estimates are derived; they are inferences which are completely based on the appropriateness of the underlying preference structure. A Keeney-Raiffa procedure, while relying on the appropriateness of the same underlying preference structure, differs, primarily in that scaling constants and utility functions are individually assessed.

The HOPE procedure consists of three phases: (1) preparation, meaning those aspects common to both HOPE and Keeney-Raiffa approaches (necessary preliminaries, identification and definition of attributes, determination of value ranges, verification of appropriate independence conditions); (2) eliciting direct holistic assessments for the specific multiattributed consequences of an appropriate orthogonal design; (3) performing the arithmetic on the holistic assessments required to deduce scaling constants and utility functions.

Preparation

All approaches to multiattribute utility assessment involve certain necessary preliminaries. Clearly the stage must be set, the respondent must realize the purpose of the exercise, and mutual understanding sufficient for effective communication must be established. Following preliminaries, both approaches would identify and define value-relevant attributes. For each attribute, both would determine an appropriate range of values, including which level is worst and which is best. Finally, both would check to see that necessary preferential independence

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and utility independence assumptions are met." As a consequence of the independence conditions, both would conclude that Keeney's general multiplicative model, equation (1), is an appropriate MAU function. At this point, a Keeney-Raiffa procedure differs from the HOPE procedure by assessing utility functions and scaling constants individually. The utility functions, u,, are assessed via standard gambles in the usual way (Keeney and Raiffa, Chap. 4). The parameter k, is interpreted and often in practice assessed as an indifference probability in the standard gamble which yields consequence BEST (defined as all attributes at their best levels) with probability k, and consequence WORST (all attributes at their worst levels) with probability $1 - k_i$, versus the certain consequence with attribute X, at its best level and all other attributes at their worst levels. Scaling constants can also be assessed in other ways. In the HOPE procedure, neither the utility functions, u_i, nor the scaling constants, k, are directly assessed. Rather, the HOPE procedure infers utility functions and scaling constants from holistic assessments of consequences defined by an appropriate orthogonal design as described below.

Orthogonal Arrays Define Consequences for Holistic Assessment

Orthogonal experimental designs generally require the lowest number of holistic consequence assessments for additive main-effect non-confounded parameter estimation. A catalog of useful orthogonal designs and variations is provided by Addelman (1962).

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The qualitative properties of preferential and utility independence are described succinctly in Keeney (1977, p. 271) and amplified in Keeney and Raiffa (1976, Chap. 6).

An example of a particular design appropriate for up to 5 attributes with up to 4 levels per attribute is Addelman's "Basic Plan 3" shown in Table 1. For example, consequence 3 in Table 1 is defined as level 1 of attribute 1, level 3 of attributes 2 and 3, level 4 of attribute 4, and level 2 of attribute 5. This consequence, along with the 15 others of Table 1, plus one additional consequence defined in Appendix 1 and used to estimate the parameter K, would then be holistically evaluated. Note that consequence 1 represents the worst level of each attribute, and would be assessed to have zero utility in the preparation phase. A worst reference outcome is common to the orthogonal designs on which HOPE is based.

Holistic responses may be either direct ratings, appropriate for riskless utilities, or standard gamble indifference probabilities, appropriate for risky utilities. For riskless utility assessment one reference case consisting of the best level of all attributes is assigned 100 points; a second reference case defined as the worst level of all attributes is assigned 0 points. The remaining consequences defined by the experimental design are then rated individually along the 0 to 100 point scale. Rating data, normalized by dividing by 100, are then treated as if they were interval-scaled responses. For lottery-type utility assessments the design consequences could be considered as surething consequences in a standard gamble with the same two reference cases as uncertain outcomes. Related riskless procedures using 6-to-11

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point direct rating scales have been used in marketing applications^{*} such as hospital promotion (Wind and Spitz, 1976).

Analysis (Arithmetic) of Holistic Responses

Succinctly stated, the HOPE procedure receives m noisy holistic judgments as input. Using 2 judgments, the parameter K is estimated (step 1, Appendix 2). Depending on the value of K, either m - 1 judgments are subjected to the arithmetic of the additive model (steps 2-5 of Appendix 2), or m - 1 transformed judgments are subjected to the arithmetic of the multiplicative model (steps 6-10 of Appendix 2). The result or output is a complete set of k_i and $u_i(x_i)$ values, the latter for each level of each attribute specified by the design.

The analysis of the holistic evaluations is made extremely simple by the use of an orthogonal design. It merely involves arithmetic. The main effect of any given level of any given attribute is then the sum of the holistic values of all consequences containing the attribute at the <u>given</u> level (divided by the number of such consequences), minus the corresponding sum of the holistic values of all consequences containing the <u>worst</u> level of the same given attribute (again divided by the number of such consequences). If the procedure described in Appendix 1 yields an estimated K = 0, then the additive model, equation (2), is appropriate, and the estimated main effects must be normalized by dividing each estimate by the sum of the estimated best levels. For each attribute, this procedure estimates $k_i u_i(x_i)$ in general and k_i when X_i is at

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Carmone, Green and Jain (1977) cite a figure of over 200 industrial applications of additive (conjoint measurement) models ranging from use of full factorials and ranking responses to use of orthogonal arrays and rating responses. These applications assume equation (2) to be an appropriate model.

its best level since $0 \le u_i(x_i) \le 1$. Otherwise, the multiplicative model, equation (1), is appropriate. In this case each holistic value, U, is first transformed to $\ln(1 + KU)$, where \ln is the natural logarithm. The above analysis without normalization is then simply carried out on the transformed holistic values. For the multiplicative model this procedure estimates the quantity $\ln(1 + Kk_iu_i(x_i))$ in general, and $\ln(1 + Kk_i)$ when X_i is at its best level. Since K is estimated separately it is then possible to compute all k_i and $u_i(x_i)$ values.

II. Error in Assessed Utility Functions

Assuming the general multiplicative model <u>is</u> an appropriate representation of the basic preference structure, error can occur in the direct estimation of the scaling constants and utility functions for decomposition methods or in the holistic assessments for holistic methods. The individual estimates may be merely noisy, or may be fundamentally incorrect. In predicting utilities, the analyst may further mis-specify the model (e.g., may choose equation (2) rather than equation (1)). Thus, prediction errors may be related to one or more of the following errors: (1) model specification error; (2) noisy subjective estimates; (3) substantial random error.

It is difficult to characterize substantial errors of judgment. Surely, a substantial error is a judgment which would be altered upon reflection. It would exhibit low test-retest reliability. In a statistical sense a substantial error is an outlier.

Examples of the three types of error occurred in my recent field study of professional audit judgments. In that study audit partners

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considered hypothetical client firms described by sets of financial statements. For each firm a dollar amount defining material error was estimated to guide statistical sampling procedures. Some dollar amounts were used to estimate the parameters of a judgment model; the remaining estimates constituted a holdout sample to be predicted from the model. Several sources or error could have contributed to prediction error. First the assumed additive prediction model could have been an incorrect specification. Second, the original estimates were stated to the nearest \$25,000. With this type of rounding, a "true" value of say, \$190,000 would sometimes have been assessed as \$175,000 and sometimes as \$200,000. Or sometimes, the estimate would have been "either \$175,000 or \$200,000." Third, any of the judgments to be predicted or the judgments used to estimate the parameters could have been either merely noisy or substantially wrong. Test-retest cases and deviations from additive predictions indicated the general level of noise. In instances where there was substantial prediction error, participants were asked to reexamine cases whose estimated dollar amounts either influenced parameter estimates or represented holdout cases. For many firms the original dollar amount was deemed "correct," but in a few cases judged dollar amounts were substantially revised. Comments like "I don't know what I could have been thinking," accompanied such revisions. Yet clearly there was no definitive criterion for "noise" versus "substantial error."

In the remainder of this section we examine the four elicitation procedures, designated KR (for Keeney-Raiffa), SMART, SJT (for social judgment theory) and HOPE, in conjunction with the possible effect on each of specification error, noise, and substantial random error.

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Model Specification Error

All four methods estimate univariate utility functions and scaling constants for either the additive model equation (2), or the multiplicative model equation (1). SMART and SJT consider only additive models. Thus, a priori, SMART and SJT models are incorrectly specified for all true values of the multiplicative parameter K \neq 0.

There are several studies which indicate the effect of specification error within elicitation methods. Fischer (1977) observed high correlations (median = .982) between KR additive predictions and KR multiplicative conditions. Simulating the HOPE procedure using known multiplicative models with extreme K values (K = -.94 or K = 4.11) with two levels of response noise (normally distributed, mean 0 and standard deviations of .025 and .05), Barron and Person (1978) found larger errors of predictions for incorrectly specified additive models (with or without noise) than for correctly specified models with noise. Furthermore, as the standard deviation of response error was decreased from .05 to .025 prediction error for correctly specified multiplicative models was cut in half, while for incorrectly specified additive models with noise, prediction error persisted at 80% and 90% of its former level. Analysis of Fischer's risky data by HOPE procedures shows for 8 of 10 subjects multiplicative models produce a lower root mean square error in predicting the entire set of holistic judgments than do additive models. A statistical analysis of the same risky data by Fischer found 6 of 10 subjects departed significantly ($\alpha = .05$) from additivity and for each of the 6 cases, multiplicative models produced a lower standard error of

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estimate. Finally, all 30 estimates of K (3 estimates for each of Fischer's 10 risky data sets) using the procedure described in Appendix 1 were found to be different from 0.

Analysis of the laboratory data of Fischer and the simulation data of Barron and Person suggest that model specification error increases prediction error. The HOPE method provides a simple direct estimate of K. The KR method computes K as a function of the scaling constants, while SMART and SJT work directly with relative weights assuming K = 0.

The individual methods differ in their respective approaches to specification of the univariate utility functions, $u_i(\cdot)$. KR and SMART assess the u_i directly. SMART asks respondents to assign $u_i(x_j)$ values directly to selected levels x_j of attribute i, i = 1, 2, ..., n. KR assess a univariate utility via standard gambles -- finding a few certain equivalents, followed by fairing in a curve. Direct assessment of certain equivalents is especially vulnerable to Tversky's (1977) suggested certainty effect bias.

The HOPE and SJT methods infer the u_i statistically from the holistic responses. SJT uses multiple linear regression; candidate u_i functions are polynomial functions of x_j . The ability of linear models to account for substantial proportions of variance (e.g., Yntema and Torgerson, 1961; Slovic and Lichtenstein, 1971) often leads to u_i functions which are linear in x_i . The HOPE procedure provides a single point estimate for $u_i(x_i)$ for each x_i specified by the design. Since there are no degrees of freedom for error estimation in the single design HOPE procedure, a substantial error in a single holistic judgment could produce erroneous u_i functions.

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With respect to weights, and more generally, scaling constants, SMART directly assesses relative weights which are then normalized; KR assesses scaling constants directly via standard gambles or sets of equations reflecting specific tradeoffs (Keeney and Raiffa, p. 267); HOPE infers scaling constants consistent with the ex ante model specification; and SJT infers beta weights from the regression. SJT weights are influenced by both model specification error (additive only) and univariate utility function specification error (usually linear).

Tradeoffs between judgment error and modeling error are complex. SMART weights are simpler to assess than are KR scaling constants. Simpler judgments (relative weights) may outweigh the disadvantage of model specification error (assuming K = 0). By contrast, SJT and HOPE procedures use equivalent holistic judgments. In this case assuming an additive model, i.e., K = 0, serves as a constraint.

Noise

KR and SMART procedures estimate scaling constants or weights and univariate utility functions separately. Thus noise in the estimate of one set of parameters should not effect estimates of the other set. Of course, the values of the scaling constants depend on the attribute ranges. SMART weights are normalized by the sum of the estimated values. Thus SMART estimates are sensitive only to errors in the relative values of these estimates. Keeney (1977, p. 284 ff) first ranks attribute (ranges) by importance and then assesses specific values via standard gambles and/or tradeoffs. Standard gambles will <u>underestimate</u> scaling constants to the extent they are subject to Tversky's certainty effect.

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Using direct tradeoffs, noise in the univariate utility function values will lead to noise in scaling constant values.

SJT infers the scaling constants assuming linear utility functions via regressing standardized attribute levels against holistic judgments. The assumption of linear conditional utility functions introduces error; a second source of error is noise in the holistic judgments. The usual error theory of regression analysis provides estimates of the sensitivity of the inferred scaling constants (beta weights).

HOPE simultaneously infers conditional utility functions and scaling constants from holistic judgments. The orthogonal arrays utilized by this procedure are extremely efficient regression designs. There are, in fact, zero degrees of freedom. If the value of a single holistic judgment is changed, the estimated value of at least one scaling constant, and several u_i values will change. If the holistic judgment is merely noisy, the effect on k_i and $u_i(\cdot)$ are minimal; if the judgment reflects "substantial random error," the effects will be substantial. Each of these last two statements finds support in the individual simulation runs of Barron and Person (1978).

Substantial Random Error

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"Holistic evaluative judgments are characterized by a substantial degree of random error," states Fischer (1977, p. 296). If so, the SJT, HOPE, and KR assessments are affected. SJT and HOPE use only holistic assessments as data; KR assessments of scaling constants in a standard gamble context require a holistic assessment of outcomes having one

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attribute at its best level and all other attributes at their worst levels. In this latter case, Tversky's certain effect bias is confounded with the predicted "substantial degree of random error."

Judgment error per se is not a part of the formal theory of MAU. Error may be handled implicitly via sensitivity analysis. In the assessment stage, the careful analyst performs numerous consistency checks in an attempt to prevent substantial error. For example, in SMART, if the relative values of attribute ranges I, II, and III are 10, 30, and 60 respectively, i.e., II is 3 times as important as I, while III is 6 times as important as I; then as a consistency check, III should be judged 2 times as important as II. For KR procedures, numerous consistency checks are illustrated in a detailed protocol (Keeney, 1977).

The most serious error suggested thus far is a single holistic judgment exhibiting a substantial degree of error being used in a HOPE estimation procedure. Since there are zero degrees of freedom, the error affects several k_i or u_i values individually. Since the error is substantial the impact, though moderated by other judgments, is also substantial. Thus, it is essential to identify, if possible, individual holistic judgments exhibiting substantial random error.

In the next section a modified HOPE procedure is described. The modified procedure guides consistency checks over the original set of holistic judgments and provides a means for detecting substantial random error.

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III. Detection of Error in Holistic Judgments

The HOPE procedure can be easily extended to detect substantial random error over the set of holistic judgments. The extended HOPE procedure uses two orthogonal designs with minimal overlap in one of two possible ways. First, the data of both designs is pooled to estimate k_i and $u_i(x_i)$ values. This serves to increase the degrees of freedom in the HOPE procedure to approximately the number of design points unique to one design. Noise is then defined by the root mean square error, i.e., of pooled prediction minus actual judgments, while arbitrarily, substantial error is defined to be a deviation exceeding twice the root mean square error.

A second approach using two designs is to build two separate (utility) prediction models -- one for each design. The utility predictions of design 1 (2) are used to predict the actual judgments of design 2 (1). Substantial error is again arbitrarily defined by prediction errors exceeding twice the root mean square error.

Either of the above procedures can be used to "detect" excessive deviations from model predictions, although it may be more reasonable to consider these procedures as guides for checking consistency over the original set of holistic judgments. One set of judgments which are candidates for consistency checks are those judgments which deviate substantially from predicted values. A second set of candidates are equal judgments for which the predicted values diverge. For example, if two consequences, a and b, have judged utilities u(a) = u(b) = .6 but the predictions differ; say u'(a) = .64 and u'(b) = .57; then a and b may also be presented to the subject for reconsideration.

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Each error detection procedure can be illustrated using the data of Fischer (1977). Fischer's subjects provided holistic evaluations for 27 hypothetical offers of employment. Each job was (completely) described by 3 attributes -- salary, location (city), and type of work. Each attribute had 3 possible levels, designated in the tables and discussion as W, for worst level; I, for intermediate level; and B, for best level. The 27 jobs represent all combinations of each level of each attribute. Fischer (1977) provides a detailed description of the elicitation task. These data have been analyzed via conjoint measurement (Fischer, 1976), have been subjected to convergent validation tests in conjunction with several elicitation methods (Fischer, 1977), and have been subjected to various HOPE procedures (Barron, 1978). For illustrative purposes, we consider the (risky) responses of subject 2, a subject for whom the additivity hopotheses (i.e., equations 1 and 2) were rejected by conjoint measurement analysis (Fischer, 1976, p. 139).

A double design appropriate for the analysis of subject 2's responses is presented in Table 2. Predicted values for each design are based on pooling data from both designs. Design 1 indicates two points for consistency checks (I,W,I) and (B,I,W). Point (I,W,I) is also a design 2 point; except for (I,W,I), design 2 has no points indicated for consistency checks. These two points should now be reconsidered by the person making the original judgments. (Of course, using these data supplied by Fischer, this is impossible.)

At this point, let us assume that upon reconsideration subject 2 agreed to reduce the judged (B,I,W) from .61^{,1} to .50. If this one change

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is made, and the predictive model for the revised pooled data is obtained, several things happen as shown in Table 3. The new predictions for (B,I,W) and (I,W,I) are both brought into better agreement with stated values -- (B,I,W) because the stated value was revised and (I.W,I) because the predicted value based on the revised (B,I,W) value increased. All values are brought into better agreement as measured by root mean square error (RMSE). Revised RMSE over all 16 pairs is smaller than the prior RMSE either including or excluding the (B,I,W) pair.

Consistency checks should also be performed for sets of equal judgments as guided by model predictions. In design 2 cells (B,I,I) and (B,B,W) were each assigned a value of .65. The predicted values are .70 for (B,I,I) and .59 for (B,B,W). The subject should be asked to reconsider these judgments. Is (B,I,I) really preferred to (B,B,W)? A similar comment does <u>not</u> apply to design 2 cells (W,I,B) and (W,B,I), each assigned original values of .70. The predicted values differ, .66 and .69 respectively, but do not diverge.

Using the two designs to estimate separate predictive models produces similar results. Cells (I,W,I) and (B,I,W) of design 1 are identified for consistency checks. Revising the (B,I,W) utility suggests the original (I,W,I) value is not substantially wrong. Furthermore, design 1 predictions of the equal value cells (B,I,I) and (B,B,W) suggest the former's utility should be increased and the latter's should be decreased.

The use of double designs provides a mechanism for detecting substantial error in judgment and further guiding consistency checks. The

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error detection feature comes at the cost of requiring approximately twice as many judgments as originally required. Its advantage is that it provides a within-elicitation method for convergent validation of field assessed utility judgments.

IV. Application Considerations

Proponents of each elicitation method described can point to an impressive number of applications. Illustrative of KR are Keeney (1973, 1976, 1977); of SMART, Edwards (1977), Gardiner and Edwards (1975); of SJT, Hammond and Adelman (1976) and of HOPE, Wind and Spitz (1976), and those cited in Carmone <u>et al.</u> (1977). This section will provide neither an extensive analysis of each method nor an applications critique of each method. Instead, practical considerations will be highlighted.

Keeney has reported two applications, Keeney (1976, 1977) that provide special insight into the process of elicitation itself -- a process which is intensive, demanding and dynamic. In each case, respondents are highly motivated professionals who had thought deeply about the respective problems, and Keeney is an especially skillful assessor. Generalizing from these reported applications, a KR procedure is expensive in terms of both respondent and assessor time. It is also an intensive process requiring a rather skilled assessor. Respondents are often required to be conversant with probability concepts. There is no estimate of "noise," and no particular procedure guides consistency checks. When the assessment is finished, the result is a utility function. Random error may implicitly be considered via sensitivity analyses.

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The procedure's advantages are its obvious tie to underlying theory, its attention to model specification, and the likely independence of noise in the scaling constants and univariate utility functions. Its disadvantages are the requirements that possibly unfamiliar constructs (scaling constants and univariate utility functions) must be directly assessed in a possibly unfamiliar language (probability theory).

The primary advantage of the SMART procedure is its simplicity. Based on simple rating procedures to deduce weights and utility functions, it has the further advantage of being easy to teach to (probabilistically) naive decision makers. It is easily adapted to hierarchical utility structures. Although the procedure is believed to be robust, a disadvantage is its sole reliance on the additive model. An error detection procedure for relative weights consists of a triangular matrix of ratios as described earlier in this report.

SJT and HOPE procedures rely on holistic judgments. It is generally acknowledged that people are capable of assigning values holistically in a consistent and meaningful fashion provided the number of attributes is, say, less than 10 and the total number of evaluations is, say, less than 50, although occasional judgments are subject to substantial error. Thus, it can be argued that each procedure uses psychologically meaningful and familiar judgments. The disadvantages of SJT include reliance on the additive model, equation (2), and a tendency to infer linear utility functions. There is also the difficulty of detecting error in individual judgments.

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HOPE has been characterized as a "decomposition procedure which relies solely on holistic assessments" (Fischer, personal communication). It includes procedures designed to both aid correct model specification and detect substantial error in individual judgments. Its obvious limitations are that it requires credible orthogonal attribute combinations and it does not apply to value hierarchies.

The HOPE procedure seems to have certain advantages when probing utilities of large numbers of people. For example, first a few representative individuals can be subjected to an intensive process. Here the reasonableness of preferential and utility independence properties can be checked and unimportant attributes can be discarded. Next, a larger sample of respondents can be assessed via questionnaire. Subsequently questionnaire assessments could be checked through a small sample of follow-up interviews.

The HOPE procedure is an extension of an additive conjoint measurement approach to modeling consumer preferences for multi-attribute alternatives (Green and Rao, 1971). Early applications of the conjoint methodology, e.g., Green, Carmone, and Wind (1972), relied on full factorials, rank-order responses, and nonmetric scaling procedures. Green, <u>et al.</u>, have subsequently simplified the basic approach considerably. Orthogonal designs significantly reduce the number of consequences to be evaluated from a prohibitive to a feasible number. Direct rating of a few consequences is often perceived as less tedious than ranking. Metric recovery requires substantially less computational capacity.

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The efficacy of these simplifications has been supported in the recent simulation studies of Carmone, <u>et al.</u> (1977), and Barron and Person (1978). That there have been over 200 industrial applications of conjoint analysis (using both full factorials and, more recently, orthogonal arrays) attest to HOPE's practicability. The refinements of correct model specifications and error detection can only enhance its usefulness.

Having practical alternatives to KR and SMART provides obvious advantages. Assessment can be more easily tailored to the specific situation -- considering costs, nature of respondents, and importance of the contemplated decision. The particular strengths and weaknesses of different procedures can be further determined through actual practice and empirical research.

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Appendix 1: Estimation of the Parameter K

Consequence 13 (Table 1) denoted below by "a," consists of the highest levels of attributes 1, 3, 4, 5 and the lowest level of attribute 2. If one additional consequence, denoted "b," is defined to have attribute 2 at its highest level and attributes 1, 3, 4, 5 at their lowest levels and is included with the orthogonal design, then ratings of these complementary consequences a and b can be used to estimate K.

If the MAU is additive, then the sum of the observed utilities for the complementary consequences is 1.0. Otherwise define consequence "c" to have all attributes at their highest levels. By regrouping terms from the right side of equation (1), we have the following:

$$1 + k u(c) = (1 + Kk_2) \cdot (1 + K u(a))$$
 (3)

$$\mathbf{k}_{n} = \mathbf{u}(\mathbf{b}) \tag{4}$$

$$u(c) = 1$$
 (5)

Substituting (4) and (5) into (3) and solving gives

$$K = (1 - u(a) - u(b))/(u(a) u(b)).$$

In practice, the ratings u(a) and u(b) are estimates, so K is also an estimate.

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Appendix 2: Illustration of the Arithmetic of the HOPE Procedure

Assume the decision maker has provided holistic assessments for the 16 consequences of Table 1. Designate these values h_1, h_2, \dots, h_{16} . Designate by h_{17} the assessment of consequence (1, 4, 1, 1, 1), that is, the consequence having attribute 2 at its best level and all other attributes at their worst levels. The arithmetic proceeds as follows:

Step 1. Following Appendix 1, compute $h_{13} + h_{17}$. If $h_{13} + h_{17} = 1$, then K = 0 and we estimate the parameters of the additive model (steps 2-5). If $h_{13} + h_{17} \neq 1$, proceed to step 6 to estimate the parameters of the multiplicative model.

Step 2.
$$A_1 = (h_1 + h_2 + h_3 + h_4)/4$$

 $A_2 = (h_5 + h_6 + h_7 + h_8)/4$
 $A_3 = (h_9 + h_{10} + h_{11} + h_{12})/4$
 $A_4 = (h_{13} + h_{14} + h_{15} + h_{16})/4$

Step 3.
$$k_1 = A_4 - A_1$$

 $k_1 u_1$ (level 3 of x_1) = $A_3 - A_1$
 $k_1 u_1$ (level 2 of x_1) = $A_2 - A_1$

Step 4. Repeat steps 2 and 3 for each attribute. Note the definition of A_1 , A_2 , A_3 , A_4 changes for each attribute, as defined by the design. For example, for attribute 2 $A_1 = (h_1 + h_5 + h_9 + h_{13})/4$ $A_2 = (h_2 + h_6 + h_{10} + h_{14})/4$ etc.

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Step 5. Compute the sum $k_1 + k_2 + \ldots + k_5$. If this sum does not equal one, then normalize all values computed in step 3 for each attribute by dividing each value by this sum.

Step 5 completes the estimation process for the additive model. Steps 6-10 describe the estimation process for a multiplicative model.

Step 6. First calculate K', an estimate of K, using the following relationship derived in Appendix 1:

$$K' = (1 - h_{13} - h_{17})/h_{13}h_{17})$$

Step 7. Define $h_i^* = \ln(1 + K^*h_i)$, i = 1, 2, ..., 16

Step 8. Repeat step 2 (additive model) using h^t values.

Step 9.
$$1 + K'k_1 = e^{(A_4 - A_1)}$$

 $1 + K'k_1u_1$ (level 3 of x_1) = $e^{(A_3 - A_1)}$
 $1 + K'K_1u_1$ (level 2 of x_1) = $e^{A_2 - A_1}$

Step 10. Repeat steps 8 and 9 for each attribute. As before, the definition of A_1 , A_2 , A_3 , A_4 are given by the design and <u>differ</u> for each attribute.

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	Attributes							
Consequence	1	2	3	4	5			
1	1*	1	1	1	1			
2	1	2	2	3	4			
3	1	3	3	4	2			
4	1	4	4	2	3			
5	2	1	2	2	2			
6	2	2	3	4	3			
7	2	3	4	3	1			
8	2	4	1	1	4			
9	3	1	3	3	3			
10	3	2	4	1	2			
11	3	3	1	2	4			
12	3	4	2	4	1			
13	4	1	4	4	4			
14	4	2	1	2	1			
15	4	3	2	1	3			
16	4	4	3	3	2			

Table 1 Attribute Levels for a 4⁵ Orthogonal Design

* Level 1 is worst; level 4 is best.

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Table 2

Attribute Level Combinations, Stated Holistic Judgments

and Predicted Judgments for Two Orthogonal Designs

Combination	Des 1*	ign 2	1 3	Stated Value	Predicted Value	De: 1	sign 2	2 3	Stated Value	Predicted Value
1	W	W	W	.00	.00	W	W	W	.00	.00
2	W	I	I	. 60	.57	I	W	I	.47	. 38**
3	W	B	B	.85	.78	B	W	B	.55	.55
4	I	W	I	.47	. 38**	Ι	I	W	. 39	.40
5	I	I	B	.75	.73	B	I	I	.65	.70
6	I	B	W	.50	.53	W	I	В	.70	.66
7	В	W	B	.55	.55	B	B	W	.65	. 59
8	B	I	W	.60	.46**	W	B	I	.70	.69
9	B	B	I	.82	.89	I	B	B	.85	.84
10	W	B	W	.60		W	B	W	.60	

* Attributes are designated 1, 2, 3. Levels are denoted W, for worst; I, for intermediate; B, for best. Parameter K is estimated using combination 10.

** Stated value differs from predicted value by at least .077, twice the estimated root mean square error.

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Table 3

Stated Holistic Judgments, Original Predictions and

Revised Predictions for Two Orthgonal Designs

	_	Design 1		Design 2			
Combination	Stated Value	Revised Prediction	Original Prediction	Stated Value	Revised Prediction	Original Prediction	
1	.00	.00	.00	.00	.00	.00	
2	.60	.57	.57	.47	. 40	.38	
3	.85	.79	.78	.55	. 55	.55	
4	.47	.40	.38	. 39	.38	.40	
5	.75	.73	.73	.65	. 68	.70	
6	.50	.53	.53	.70	.66	.66	
7	.55	.55	.55	.65	.57	.59	
8	• 50 *	.43	.46	.70	.70	.69	
9	.82	.81	.89	.85	.85	.84	

* Revised from .60 by assumption.

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SECURITY CLASSIFICATION OF THIS PERE (When Der Fillered) READ INSTRUCTIONS **REPORT DOCUMENTATION PAGE** BEFORE COMPLETING FORM E-1081 - Humber CONT MEETTON NO. CIPIENT'S 001922-2-T THE A CONTRACTOR Validation and Error in Multiplicative Utility Functions. Technical -10/77--6. PERFORMING ORG. REPORT NUMBER <u>SSRI 78-2</u> - Prime Contract NUMBER(4) AUTHOR/A F./Hutton Barron 76-C-8974 Subcontract 76-030-0715 PERFORMING ORGANIZATION NAME AND ADDRESS PROGRAM FLEMENT PROJECT, TASK AREA & WORK UNIT NUMBERS Social Science Research Institute University of Southern California Los Angeles, California 90007 11. CONTROLLING OFFICE NAME AND ADDRESS Advanced Research Projects Agency Deco 1400 Wilson Blvd FAGES Arlington, Virginia 22209 50 14. MONITONING AGEALY NAME & ADDRESSIL dillarent from Controlling Office) 15. SECURITY CLASS. (of this report) Decisions & Designs, Inc. 8400 Westpark Drive, Suite/600 unclassified McLean, Virginia 22101 150. DECLASSIFICATION DOWNGRADING (under contract from Office of Naval Res. DISTRIBUTION STATEMS VI (of INIE Report) Approved for public release; distribution unlimited 17. DISTRIBUTION STATEMENT (of the abstract entered in block 20, if different from Report) 13. SUPPLEYENTARY NOTES 19. KEY KORDS (Continue on reverse side if necessary and identify by Lich number) multiplicative function holistic assessment methods utility function additive function scaling constants orthogonal 29. ABSTRACT (Continue on reverse side if necessary and identify by block number) \forall In this report an approach to the concept of error in utility assessment is proposed. Three components of error are considered and each component is related to four separate elicitation methodsall in the context of a general multiplicative multiattribute utility model. The methods are Keeney-Raiffa (1976) procedure, SMART (Edwards, 1977), a social judgment theory (SJT) based regression model (Hammond, Stewart, Brehmer and Steinmann, 1975) and-DD 1 JAN 71 1473 EDITION OF I NOV 65 IS OBSOLETE S/N 0102-014-6401

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a new method called Holistic Orthogonal Parameter Estimation or HOPE (Barron and Person, 1978). and the state of the second state of the secon

If a general multiplicative model can be assumed to be an appropriate representation of the decision maker's basic preference structure, error can occur in the direct estimation of the scaling constants and univariate utility functions for decomposition methods (Keeney-Raiffa and SMART), or in the holistic assessments for holistic methods (SJT and HOPE). Individual estimates may be merely noisy or may be fundamentally incorrect. Furthermore, the utility model may be incorrectly specified; for example, an additive model, rather than a multiplicative model, may be used. The four assessment methods are considered in conjunction with errors of each kind.

The most serious error-method combination is the case of a substantial degree of error occurring in a single holistic judgment which is being used in a HOPE procedure. This concern leads to a major emphasis of this report--and expanded HOPE procedure used in conjunction with a convergent validation strategy to estimate error in individual holistic judgments and thus guide consistency checks.

The discussion is organized into four sections. The HOPE procedure is summarized in Section I. In Section II, three components of assessment error are considered in conjunction with the four elicitation procedures. In Section III, an expanded HOPE procedure for detecting judgment error and guiding consistency checks is proposed. In Section IV, application considerations are outlined.