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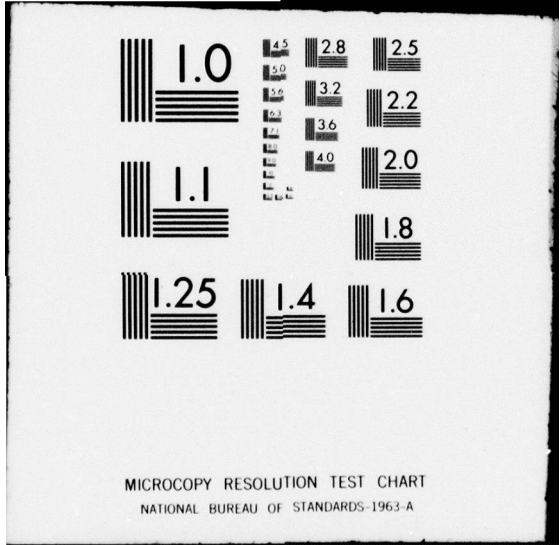
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AN INTERACTIVE ANALYSIS PROGRAM FOR
A DIGITAL IMAGE PROCESSING LABORATORY

THESIS

AFIT/GE/EE/78S-16

Dennis A. McGaugh
Capt USAF

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A DIGITAL IMAGE PROCESSING LABORATORY

THESIS

9 Master's thesis,

Presented to the Faculty of the School of Engineering
of the Air Force Institute of Technology
Air University (ATC)
in Partial Fulfillment of the
Requirements for the Degree of
Master of Science

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Dennis A. /McGaugh B.S.
Capt. USA

Graduate Electrical Engineering

11 September 1978

12 74p.

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Preface

This work attempts to provide the solution to a problem first identified by Major J. W. Carl of the Air Force Institute of Technology, School of Engineering. The basic problem was to design and implement the software necessary to allow two-dimensional linear filter and two-dimensional Discrete Fourier Transform (DFT) to be performed on an existing minicomputer-based image processing system. With the addition of the routines described in this thesis, true linear filtering of images is now available on the DICOMED Image Processing System. It is hoped that with its filtering capability, and with its 64x64 DFT capability that this new image analysis software will indeed provide a useful analytical tool.

I would like to take this brief opportunity to thank the people without whom this project would have been virtually impossible. Thanks to Captain Fred Barney for his making the DICOMED equipment available and for his patient explanations on the intricacies of same.

A special thanks to my thesis advisor, Major Carl for his saint-like patience and profound guidance during some very trying times. And lastly, but by no means least, thanks to my wife Marla for her typing the thesis rough draft and for her inspirational moral support.

Dennis A. McGaugh

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Abstract

A FORTRAN program is presented that will interactively prepare digitized images (pictures) for experimental analysis. The digital preparation includes the ability to Discrete Fourier Transform (DFT), Inverse Fourier Transform (IDFT), threshold image power spectral density, and to perform two-dimensional image filtering. Further, a brief discussion of image distortion measurements, optimal image size for experimental presentation, and image aliasing is provided. A sample of typical processed image results is also supplied.

AN INTERACTIVE ANALYSIS PROGRAM FOR
A DIGITAL IMAGE PROCESSING LABORATORY

I. Introduction

There currently exists, located in the Air Force Avionics Laboratory, image processing hardware and software capable of digitizing and performing limited statistical calculations of pictorial imagery. There also exists a requirement to perform certain image processing with this equipment in preparation for a visual experiment. However, the software needed to conduct the processing did not formerly exist. The types of computations needed to perform this processing and analysis are well-known. But these computations needed to be developed in software and implemented on the particular small computer system that is available.

The image processing functions that are needed include: two-dimensional linear filtering, calculation of a two-dimensional image power spectrum, ability to specify a threshold for this power spectrum, and the Mean-Square-Error (MSE) and Bandwidth (BW) of an image constrained to occupy only those frequencies at which the power spectrum is above a specified threshold. Additionally, it is desired that these functions be interactively controlled and specified to the program during run time.

The problem is to develop and provide a software program capable of accomplishing the above functions, and still

be compatible with the existing equipment. Additionally, part of this thesis work is to determine what is the minimum size of picture digitization (e.g. 64x64, 128x128, 256x256) that will produce pictures suitable for the experiment; that is, a picture that creates an image of no less quality than 30 lines per 1° of visual angle subtended during viewing. The picture digitization will also impact on the computer resources needed to perform the filtering. The experiment currently calls for the use of up to 24 different pictures. These pictures are available in positive or negative form, and have been digitized (2048x2048) and stored on magnetic tape. The sampling resolution may also cause image aliasing problems, and this effect must also be discussed.

The material presented in this thesis follows roughly the same order as discussed above. Chapter II discusses the constraining environment, its effect on program development, and the digital domain for implementation of the required functions. Chapter III briefly describes the laboratory hardware/software and the final project software. Chapter IV presents a sample of processed image results, and Chapter V closes with summary remarks and mention of areas for future work. The appendix contains a program user's guide and complete program documentation.

II. Discussion

During the development of the image analysis program, several important questions had to be answered. The answers to some are rather straight-forward; the answers to others were influenced by answers to previous questions. The answer to each question, and its impact on the design of the image analysis program is presented in the section that follows. After reading these sections, it is hoped that there will be clear understanding of the program constraint environment.

A Question of Image Resolution

The requirement exists to conduct visual experiments with pictorial presentation to human subjects. The images should fall within the subjects' regions of foveal vision; that is, the images should not exceed a visual angle of 2 degrees during viewing. In discussions with (then) Captain Larry Goble of the US Air Force Flight Dynamics Laboratory at Wright-Patterson AFB, Ohio, the point was made that the industry standard for images on graphics and television displays is a twelve-inch square picture viewed at a distance of thirty inches with a resolution of no less than sixty lines per inch. It was also decided that this should be the resolution standard for the analysis program. After some basic geometrical calculations, this works out to be 30 lines of resolution per 1 visual degree (vis). Additionally, the experimental displays require that each visual presentation

consist of two different pictures placed side-by-side. Considering the overall limit of 2° vis vertically and horizontally, this means that for square pictures, each picture can only subtend 1° vis.

The answer to the question of image resolution is that each picture, in order to subtend 1° vis, must be $1/2$ inch x $1/2$ inch at 30 inches distance from the viewer, and each picture must have a minimum of 30 lines of resolution both horizontally and vertically. Imagery of this quality is obtainable through the use of the laboratory DICOMED image processing equipment. It should be noted, however, that the requirement for number of lines of resolution increases when considering the question of aliasing.

A Question of Aliasing in Digitized Images

The DICOMED image processing equipment digitizes a given picture with a sequential horizontal scanning action. It begins at the top of the picture to be digitized with a horizontal scan the width of the picture. It then proceeds incrementally down the picture with successive, picture width, horizontal scans until it stops at the picture bottom. Both horizontal and vertical directions are discretely sampled with an adjustable number of samples per picture widths (independently chosen in each direction). The result of this scanning process is the mapping of the entire picture into a $M \times N$ matrix of $M \cdot N$ discrete pixel values, where M and N are both powers of two. In this application, M was equal

to N. For the DICOMED machine, the value of each pixel can be any one of 256 gray scale levels, from white (377_g) to black (000_g). When referring to the resolution of this resulting digitized picture, it is said to have N lines of resolution, with a sampling rate of N (where $N=2^P$).

The answer to the question of aliasing can be found by referring to the Nyquist sampling theorem (12:68). Restated, it simply says: to eliminate spectrum aliasing in the discrete domain, sample at a rate greater than or equal to twice the spectral width. Therefore, for the previous case of an NxN sampled image, in order to prevent aliasing after discrete Fourier transformations, there must not be any spatial-frequency content above $\frac{N}{2}$ cycles per picture width. The experimental requirement is for a minimum of 30 lines resolution per picture. This means that a digitized picture with this resolution can display up to 30 full oscillations (cycles) between white and black per picture in either the horizontal or vertical direction. Therefore, the display resolution criterion is satisfied if $\frac{N}{2} \geq 30$. Since a DFT/FFT computer algorithm (discussed later) will be used to transform into the Fourier domain, and powers of two run fastest in that algorithm, and since the DICOMED image processing system samples at powers of two, a sampling rate of 64 was selected as the minimum convenient value that N can have and still meet the display resolution criteria. This requires a 64x64 digitization of each image to be processed, and insures that, at this digitization level, the

resolution limits of human observers will be met under the cited viewing conditions.

Now, to insure no image aliasing, it must be guaranteed that there is no spatial frequency, in the image being transformed, above 32 cycles per picture width. To provide this guarantee, all 64x64 digital images used in this work were derived from pictures sampled at a rate much higher than 64 samples per line. The original pictures were first digitized into 2048x2048 images. Then by considering 64x64 blocks of 32x32 pixels, each 32x32 pixel block was averaged into one pixel value. The resultant averaged pixel values produce the required 64x64 digital image. In essence, this procedure performs a two-dimensional, digital low-pass filtering operation on a picture that may contain spatial frequencies of up to 1024 cycles. Although this type of low-pass filtering results in a $\frac{\sin x}{x}$ form for the filter in the frequency domain, and such filters are not particularly good in the stop-band of the filter (considerable side-lobe structure), these effects were ignored since relatively low spatial frequencies are anticipated in the original pictures. This procedure is essentially a digital simulation of the low-pass filtering operation necessary to avoid aliasing.

The Question of Linear Filtering Implementation

The functional requirement for linear filtering implies spatial convolution of the form (10:440):

$$y(n_1, n_2) = x(n_1, n_2) * h(n_1, n_2) = \sum_{m_1=-\infty}^{\infty} \sum_{m_2=-\infty}^{\infty} x(m_1, m_2) \cdot h(n_1 - m_1, n_2 - m_2)$$

where $y(n_1, n_2)$ is the output image result of the $x(n_1, n_2)$ input image that has been filtered by a linear filter with an impulse response of $h(n_1, n_2)$. As noted by Rabiner and Gold (Ref 10), this calculation in the spatial domain with images is not usually soluable in closed form except for the most trivial filters. However, a more tractable form of this convolution equation occurs in the frequency domain. It is well-known (Ref 8) that the convolution equation takes the form:

$$Y(k_1, k_2) = X(k_1, k_2) \cdot H(k_1, k_2)$$

where $Y(k_1, k_2)$, $X(k_1, k_2)$, and $H(k_1, k_2)$ are the Fourier transform coefficients of the image output, image input, and image filter impulse response respectively. Now, the filter computations become readily manageable and almost trivial. They simply involve multiplying each Fourier transform coefficient of the input image with each respective Fourier transform coefficient of the impulse response of the filter. The result is then inverse Fourier transformed back into the spacial domain as the resultant linearly filtered output image.

The transfer function furnished for the linear filtering process is given as a one dimensional equation. Before it can be used to filter an image, however, it must be converted into two-dimensional form. It has been shown by Huang (Ref 6) that a good circularly symmetric two-dimensional linear filter can be obtained from a good one-dimensional

linear filter via the relation:

$$H(k_1, k_2) = \hat{H}(\sqrt{k_1^2 + k_2^2})$$

where \hat{H} is the one-dimensional filter impulse response at the appropriate frequency values of k_1 and k_2 . For the situation involving the previously cited 64x64 image matrices, this requires Fourier domain frequency values (k_1, k_2) , along both the real and imaginary axis, ranging from -32 cycles to +32 cycles. Due to the circular symmetry of the filter, only one 32x32 quadrant need be calculated from the equation. Once calculated, it is appropriately copied into the other three quadrants of the filter matrix. A more complete explanation of this operation appears in Appendix A.

The Question of Operating in Two Dimensions

The most obvious problem of processing in two-dimensions is simple: it takes longer, and uses more computer memory. For the one-dimensional case, the discrete Fourier transform of a sequence of N samples takes N^2 complex addition and multiplications; in two-dimensions, it takes N^4 operations by brute force. For the one-dimensional case, the filtering process in the Fourier domain requires $2 \cdot N$ complex coefficients to be stored in computer memory; in two-dimensions $2 \cdot N^2$ complex coefficients must be stored. To help reduce these increased requirements associated with two-dimensional processing, certain processing modifications were made.

First was the implementation of the well-known (Ref 8)

Fast Fourier Transform (FFT) technique. This reduces the number of addition and multiplications from N^4 ($64^4=16,77,216$) to $2N \cdot N \log_2 N$ ($128 \cdot 64 \cdot 6 = 49,152$), a reduction of over 10 to 1. The program implementation of the FFT algorithm is via the FORTRAN subroutine called FOURT. It is a program written by Norman Brenner from the basic program by Charles Rader of MIT Lincoln Laboratory. It is a very versatile program, and offers more options than are required for the particular image processing application. But its very versatility was the reason it was selected, as it will allow calculation of odd sizes of FFT's for images other than the present 64x64 size. A more complete discussion of FOURT appears with the program listing in the appendix.

The second modification was to use disk files to store the images and complex FFT coefficients. In the existing IPS/DICOMED image processing systems each complex number occupies 4 words of storage. For one 64x64 FFT coefficient matrix to be entirely loaded into computer memory it would require 16K words. If, as in a filtering operation, two matrices were to be used at once, then 32K words would be needed; the existing minicomputer core storage is only 28K words. A technique suggested by Oppenheim (Ref 8) to reduce the requirement for two-dimensional core storage is to perform the two-dimensional FFT as a series of one-dimensional FFT's. Further, by first storing the images on random access disk files then reading in only one row or column from each appropriate disk file, the FFT operates on only those two

pieces of data at one time, and the core required to operate the program is dropped to a realizeable size. Although the processing scheme involves huge amounts of computer I/O, the time to compute and store a 64x64 point complex FFT is less than 4 minutes, and the time to accomplish filtering (matrix multiplication) is less than 2 minutes. Additionally, there is an option to have the FFT coefficients normalized by dividing all coefficients by the zero-frequency or DC term, or to have the FFT coefficients remain with their unnormalized values.

A Question of Power Spectrum Thresholding

Once the digitized image is in the Fourier domain, the calculation of the power spectrum is straight-forward. The power spectral density of an image is related to the squares of the absolute value of the Fourier coefficients and is given by:

$$\phi(u,v) = E \left\{ |X(u,v)|^2 \right\}$$

where the expectation is over an ensemble of image transforms. The program implementation for estimating the power spectrum of a set of images is obvious from this equation, and a discussion can be found in Appendix A, Operating Procedures, 5c. The analysis program provides the capability to average up to 24 different image spectrums. These 24 images may be the same ones that are mentioned in the introduction to this paper. It is on this resultant averaged power spectrum that

the thresholding function is expected to be used.

The thresholding function was originally requested to be used with only the power spectrum. However, to provide more flexibility, it is implemented in a manner to allow its use with any specified 64x64 matrix of complex data (i.e. FFT coefficients, or power coefficients). By using the thresholding function, the analysis program user is able to interactively specify a 64x64 complex valued matrix, and to enter a real valued number against which the absolute value of every complex point is compared. The result of this thresholding operation is the creation of a 64x64 matrix which contains (in complex format) the value one for every point above the threshold and a complex zero for every point below the threshold. Both the original matrix and the threshold matrix are then available for further processing.

Since the thresholding is done in the Fourier domain, values that are linearly related (Ref 1:138-141) to spatial bandwidth (BW) and mean-square-error (MSE) are easily calculated. The BW value is simply the number of points above threshold in the Fourier domain. In the spatial domain, these above-threshold values correspond to the image pixels that would be transmitted over a digital channel with relative bandwidth BW. The MSE value is simply the sum of the power values below threshold. In the spatial domain, the MSE corresponds to the error of the image transmitted over a digital channel, with bandwidth BW described above.

The Question of Images and Image File Generation

Originally, the only requirement for image output was to generate a completely processed image ready for experimental testing. However, in an effort to make the analysis program applicable for more general use, the ability to display intermediate results is also provided. A 64x64 image file displaying the results for each of the following functional operations is prepared and stored in DICOMED/IPS format on disk: (1) the reduction of a 2048x2048 image to a 64x64 image; (2) the two-dimensional FFT calculation; (3) the power spectrum calculation; and (4) a fully processed image (either thresholded, linearly filtered, or FFT'd).

Since the images are in DICOMED/IPS format, post-processing with the IPS system is trivially implemented (Ref 7). A sample image file format appears in the appendix.

III. Laboratory Hardware and Software

The imagery equipment used for this work is located in the Avionics Laboratory on Wright-Patterson AFB, Ohio. A detailed description of the equipment is included in Reference 7. Briefly, it consists of a PDP-11/45 minicomputer with 28K of core memory and many peripherals. Included are: one RP03 diskpack disk drive, two RK05 diskcartridge disk drives, one MTU10 tape drive, one 132 column line printer, a Conrac video monitor, and one Tektronix 4000 series graphics terminal. Additionally, the system is interfaced to a DICOMED image scanner/recorder. With this equipment, the capability exists to perform up to a 2048x2048 point digitization of pictures. As the DICOMED digitizes the picture, it is stored on magnetic tape for follow-on processing by the PDP-11/45 Image Processing System (IPS). A description of the IPS software is also included in Reference 7.

A full description of the software written for this thesis appears in the appendix. It is written for interactive use and provides the following capabilities:

1. Image reduction from 2048x2048 to 64x64.
2. FFT of a 64x64 image.
3. Calculation of $\hat{\Phi}_i(u,v)$ for one image, or an average $\hat{\Phi}(u,v)$ of a standard set of 24 images.
4. Ability to threshold a 64x64 image as previously discussed.
5. Ability to generate a 64x64 filter from a user supplied impulse response equation.

6. Inverse FFT of Fourier coefficients.

By running this program, any one of the above processes can produce an image file that is stored on the RP03 disk for display by the IPS system, or hardcopy picture generation by the DICOMED system.

IV. Results

Figure 1 presents some samples of output from the digital image preparation program. It should be noted that Figure 1 was generated with an arbitrary high-pass filter whose transfer function has the form:

$$H(f) = 0.5(1 + \ln(f/10 + 0.1)), \text{ for } 0 \leq f \leq 32$$

Also note, that the slight graininess of the 64x64 pictures is due to a blow-up factor of two (4 new points for each original point). This was done solely to provide larger pictures for Figure 1.

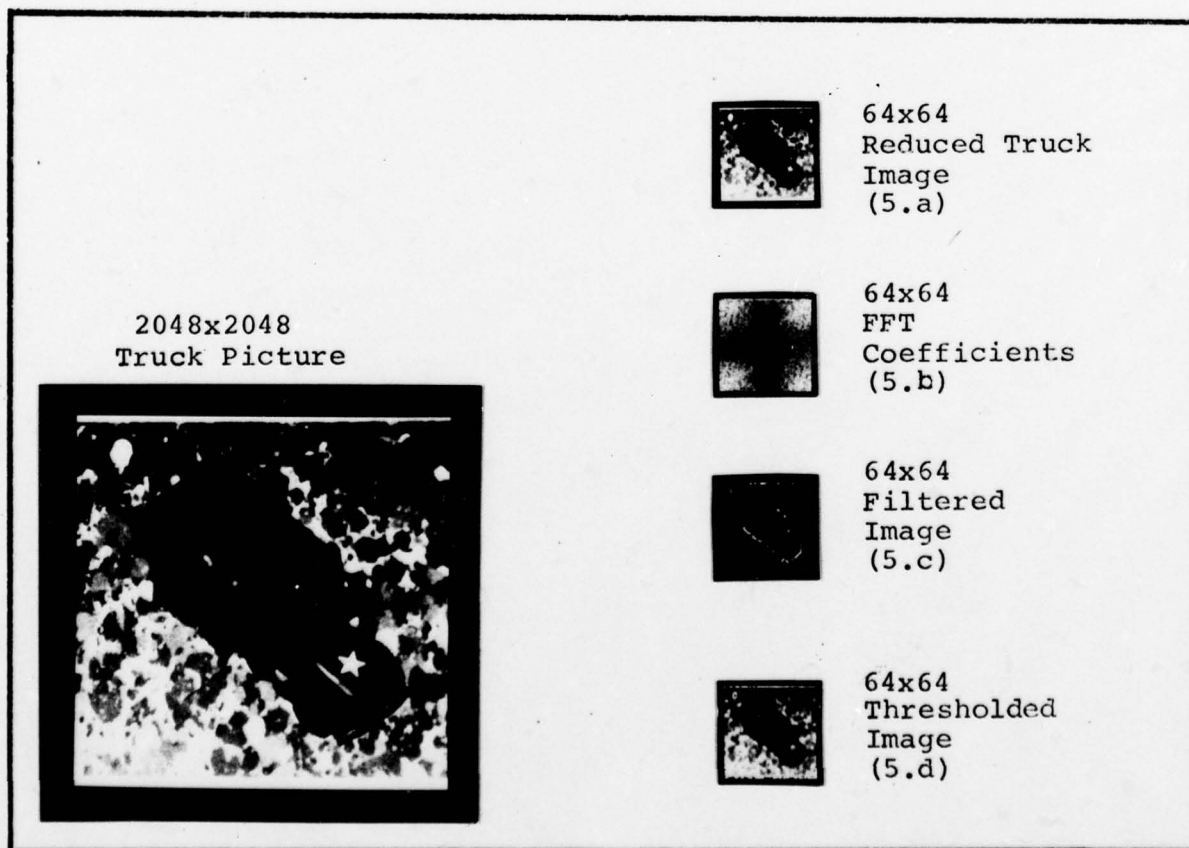


Figure 1. Sample Images

V. Summary and Recommendations

This thesis has presented a computer program to digitally process images, and in this case the processing is motivated by a desire to generate stimuli for a particular psychometric experiment. Additionally, as can be verified by reading the program description in the appendix, a general purpose routine is now made available to tailor digital processing of pictures for a large number of image filtering based applications.

Areas for future work would include modifying the program to process pictures other than the 64x64 size, and an on-line interactive tie-in between the IPS system and the processing program.

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Appendix A

User's Guide for RAZMA.TAZ

Appendix A

User's Guide for RAZMA.TAZ

Introduction

This program allows a user to perform the following functions on IPS/DICOMED images:

1. A reduction of a 2048x2048 image file to a 64x64 image file.
2. A two-dimensional fast-fourier transform (FFT) of a 64x64 image with either normalized or unnormalized coefficients.
3. Calculation of a two-dimensional power spectrum of one 64x64 image file, or the two-dimensional average power of 24, 64x64 images.
4. Specification of a high-pass threshold on either the FFT file or the power file.
5. Generation of a two-dimensional filter (FFT domain) from a user specified impulse response equation.
6. Multiplication of any threshold or filter files with any image or FFT or power files.
7. Calculation of the two-dimensional inverse FFT transform on any modified FFT file.

Reference Material

1. The DOS/BATCH Handbook: Monitor Operating System Version 09. Digital Equipment Corporation, Maynard,

Mass. DEC-11-ODBHA-A-D, April 1974.

2. Image Processing Software Conversion, Vol. I & II.
Development Center, Air Force Systems Command,
Griffiss AFB, New York 13441. February 1977.
(ADA038136 & ADA038137).

Operating Procedures

This gives the ordinary routine for running RAZMA.TAZ. Specialized uses and procedures are covered under sub-heading Miscellaneous Operations.

1. Program materials you will need include:
 - User's Guide.
 - IPS diskcartridge (RK05) (AAT Lab-blue label).
 - "Scratch" diskcartiridge (RK05) (AAT Lab-#6).
 - ROLLIN magtape with RAZMA.TAZ program and 24 picture data sets.
 - IPS/DICOMED PDP-1445 computer and associated hardware (AAT lab).
2. How to 'power-up':
 - a. Place PDP-11/45 console HALT switch down, turn key of console clock-wise to the 'on' position.
 - b. Load IPS diskpack in RK05 unit #0. Load 'scratch' diskpack in RK05 unit #1. Do not use 'write protect' switch. Wait until 'on-cylinder' light comes on.
 - c. Mount ROLLIN tape on tape drive. This can be omitted if program and data files are already on the scratch diskcartridge or the RP0 disk drive.
 - d. Turn on RAMTEK graphics display box.
 - e. Slowly turn on line printer, then toggle 'master clear', and toggle 'on-line' switches. This can be omitted if no printer output is expected (normally none is).

- f. Open door to RPØ disk drive to see if diskpack #1 (DOS) is installed. If not, retrieve it from the lower cabinet and install it. Turn on power switch and wait until yellow light comes on.
 - g. Turn on Tektronix 4014 terminal and place it in 'local' mode. Type 'ESC' key, then ':' key. Type in that order, and only once each. This reduces the display front size. Place terminal 'on-line'.
 - h. Turn on CONRAC video display.
 - i. Return to the PDP-11/45 console SWR. Set in 000776₈ ('one' is up) and toggle 'load ADR' switch. Set in 000777₈ and toggle 'DEP' switch. Move switch from 'HALT' to 'ENABLE' and hit the 'RUN' switch.
 - j. Place the thumbwheel of the AED8000 to the 'MAINTENANCE' display and to ADDR CODE = 776732. Push the red IPL switch once. The LED's above the display should begin flashing. If not, go back and try again.
 - k. Return to the Tektronix terminal and type RKØ: Do not type a carriage return. Enter the date and time in the format shown.
 - l. Login with \$ L0 11,11.
 - m. Type \$ RUN DK1: RAZMA.TAZ, or \$ RUN DPØ: RAZMA.TAZ.
 - n. Follow the yellow brick road.
3. How to 'power-down':
- a. To end RAZMA.TAZ, type the 'CTRL' key and the 'C' key simultaneously, followed by 'K' and 'I'. This exits to the DOS monitor. This may also be used to stop the program at any time. Next, type 'FI' to log-out from the IPS/DOS system.
 - b. Place the terminal in 'LOCAL' mode, give the screen display several RESET's, and turn off the terminal.
 - c. Turn off the CONRAC video monitor.
 - d. Return to the PDP-11/45 console and hit the 'HALT' switch.
 - e. Toggle the switches on both RKØ5 diskcartridge drives to the UNLOAD position. The doors will remain locked until the 'LOAD' light comes on. This will take about a minute. Then the cartridges can be removed.

- f. Meanwhile, the following steps may be performed.
 - g. Toggle the Line printer to 'OFF LINE' and turn it off.
 - h. Turn off the RAMTEK graphics display box.
 - i. Push the red IPL switch on the AED8000 once. Push, then release, the yellow power switch on the RPØ disk drive. The yellow light will slowly go out. After it goes out the diskpack can be removed if desired.
 - j. Unload/dismount the ROLLIN magtape, if it was loaded on the magtape drive, and turn off the magtape drive.
 - k. Return to the RKØ5 diskcartridge drives and remove the diskcartridges.
 - l. Turn the key on the PDP-11-45 console fully counter-clockwise to the off position.
4. Running the RAZMA.TAZ. The actual operation of the program is straight forward. A menu of functions is presented first and the user selects the desired function. All prompts are self-explanatory. The format for all ASSIGN commands is given prior to each request for user assignment. Any error in syntax will be caught by the monitor system. However, be very careful to note the device unit number used in the command format. Failure to use the same number when typing in the command can destroy certain necessary stored program files along with the user's specified input file. Should the wrong number be typed, simply retype the command before typing 'CO'. If 'CO' has already been typed, do a 'CNTRL/C', 'KI' immediately. This closes all files and returns control to the DOS monitor. By running FILDMP or

PIP (see DOS/BATCH handbook), the user's files can be verified and/or restored. For verification of program files, see Special Procedures. After file verification or restoration, RAZMA.TAZ can be started normally.

Other than prompts and asking for file assignments there should be no other messages, except when using the FFT, POWER, and IFFT functions. In these cases, an error message will be printed about an overflow on a real to integer conversion. This is normal. It occurs during the generation of each function's image file, and refers to the DC term of the FFT coefficients. It does not affect any internal processing calculations. The error merely means that the value of the DC term is greater than 16,384 and exceeds the allowable 256 level gray scale of the DICOMED image processor. The DC pixel value will be zero (black pixel), in the upper left hand corner of any picture created from the image file.

Errors of any other type should not occur. If they do, it is most likely due to processing a bad data from an input file. As before, use FILDMP or PIP to check input files for correct data.

5. RAZMA.TAZ functions. This briefly describes what each function does and what files are used or generated.

- a. REDUCTION. Takes a user specified 2048x2048 image file and averages it's pixels into a 64x64 image file. The routine takes a 32x32 pixel block from the specified file and averages the entire 1024 points into one point of the 64x64 image. The output file is called AVG.IMG.
- b. FFT. Performs a two-dimensional fast fourier transform (FFT) on either a user specified image file or the AVG.IMG. file. The resultant coefficients can be either normalized (FFTCOF.NRM file) or unnormalized (FFTCOF.UNN file) as requested by the user. The routine performs the FFT by using the subroutine FOURT, first on each image row, and then on each image column. An image file of the resultant FFT coefficients is also made (FFT.IMG). The DC term is in the upper left-hand corner. This image file may be accessed in the normal manner under the IPS/DICOMED system.
- c. POWER. Uses the FFT coefficients to generate a two-dimensional power spectrum. The input file can be a single user specified FFT file, or FFTCOF.NRM, or FFTCOF.UNN. Additionally, the function will calculate the average power spectrum of the 24 storage picture coefficients. The power calculation is simply the squaring of the FFT coefficients. The resultant output file is PWRFFT.COF. An image file is also created (PWRFTT.IMG) for use on the IPS/DICOMED system.
- d. THRESHOLD. This function looks a user specified coefficient file, or PWRFFT.COF, or FFTCOF.NRM, or FFTCOF.UMM and creates a file that when used with the MULT function will pass only coefficients above a certain threshold value. This value is entered, interactively, by the user. In addition, the routine counts the number of points above the threshold and calculates a "bandwidth" number; i.e., $PTS.ABOVE \div 4096 = BW$. Also, if the coefficients were POWER coefficients and normalized, it finds the mean-square-error of the thresholded power spectrum; i.e., the amount of power below the threshold setting. The output file contains only a mask of 1's and 0's at the appropriate location and is called THRHLD.FIL.
- e. FILTER. This function takes a user specified filter transfer function equation and computes a two-dimensional mask file which can be used in the MULT program. The value of the mask points are based on the radial distance from the upper left-hand corner of a 32x32 square (Fig 2).

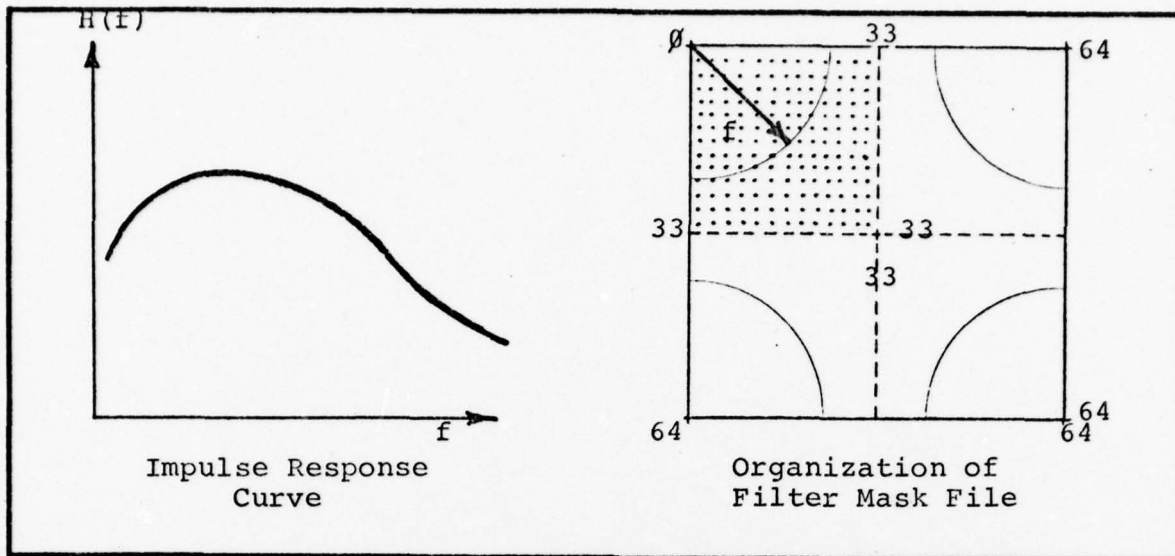


Figure 2. User Specified Filter Impulse Response

The equation is specified on line 515 of the RAZMA.TAZ program listing. To change the equation, the program must be edited and reassembled (see Miscellaneous Operations, b). The resultant output file is FILTER.COF.

- f. MULT. This functional routine takes one user specified coefficient file, or THRESHOLD.COF, or FILTER.COF and multiplies it point-by-point times another user specified coefficient file, or FFTCOF.NRM, or FFTCOF.UNN, or PWRFFT.COF. It's output file is MULT.DAT.
- g. IFFT. This function performs an inverse FFT on the MULT.DAT file. The user cannot directly specify input to this file. But he can however, input indirectly. By giving the THRESHOLD function a threshold of zero, a mask of all one's will be generated. Then, using this mask with MULT and specifying the other MULT input file, the input to IFFT is assured. The output is an image file named PROCSD.IMG. As with all other image files, this is operable on the IPS/DICOMED system.
6. FLOWCHART. The flowchart in Figure 3 shows the processing flow and options available in RAZMA.TAZ.

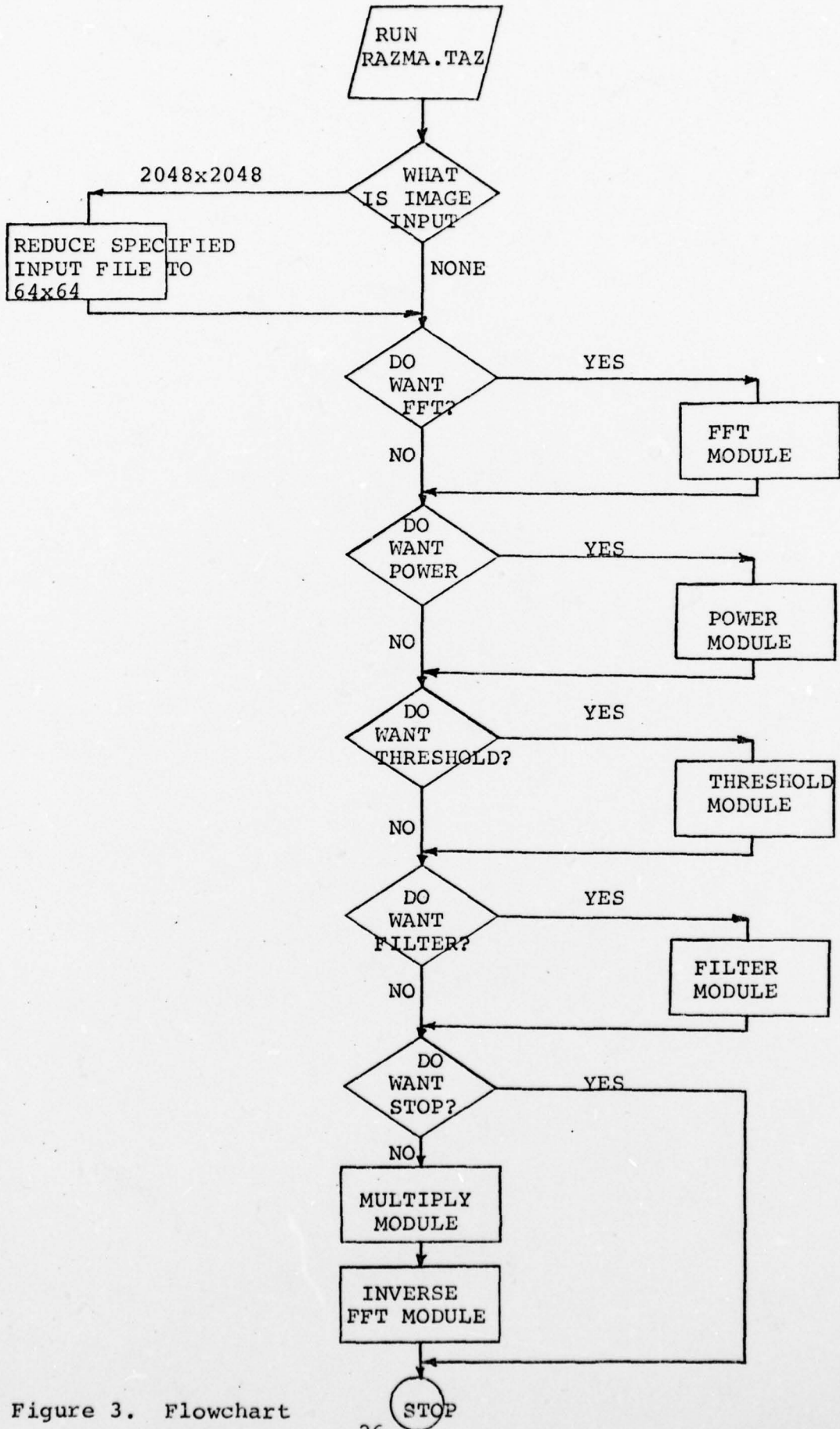


Figure 3. Flowchart

Special Procedures

1. NO FILE! After the \$LO and \$RUN the monitor answers with NO FILE! When this occurs, run the DOS/BATCH PIP program (see the handbook) and see if RAZMA.TAZ is on the disk you specified in the \$RUN command. If not, check the other disk. Remember, you must be logged-in under UIC=11,11. If not on either disk, use the ROLLIN tape and ROLLIN program (in handbook) to restore the RK05 diskcartridge on unit #1 (DK1:). Then start POWER-UP procedures
2. UNABLE TO OPEN FILE. This can occur any time during the running of the RAZMA.TAZ program. This usually means that an expected input file (specified by ASSIGN) or one of the 24 standard picture files does either not exist on DP0: or two files exist with the same name. In either case, run PIP to get a listing of all files on DP0: to see if all required files are there, and perform file manipulation as appropriate. If file cannot be found on DP0: or DK1:, it may be necessary to ROLLIN the magtape as in the above step and start again. A minimum of the following files are required:

DIRECTORY DK1: E 11.11 J

15-SEP-78

ARTY1 .COF	64C	13-SEP-78	<233>
ARTY2 .COF	64C	13-SEP-78	<233>
ARTY3 .COF	64C	13-SEP-78	<233>
ARTY4 .COF	64C	13-SEP-78	<233>
APC1 .COF	64C	13-SEP-78	<233>
APC2 .COF	64C	13-SEP-78	<233>
APC3 .COF	64C	13-SEP-78	<233>
APC4 .COF	64C	13-SEP-78	<233>
CURTK1.COF	64C	13-SEP-78	<233>
CURTK2.COF	64C	13-SEP-78	<233>
CURTK3.COF	64C	13-SEP-78	<233>
CURTK4.COF	64C	13-SEP-78	<233>
OPNTK1.COF	64C	13-SEP-78	<233>
OPNTK2.COF	64C	13-SEP-78	<233>
OPNTK3.COF	64C	13-SEP-78	<233>
OPNTK4.COF	64C	13-SEP-78	<233>
SHER1 .COF	64C	13-SEP-78	<233>
SHER2 .COF	64C	13-SEP-78	<233>
SHER3 .COF	64C	13-SEP-78	<233>
SHER4 .COF	64C	13-SEP-78	<233>
MG0A1 .COF	64C	13-SEP-78	<233>
MG0A2 .COF	64C	13-SEP-78	<233>
MG0A3 .COF	64C	13-SEP-78	<233>
MG0A4 .COF	64C	13-SEP-78	<233>
ARTY1 .IMG	10C	13-SEP-78	<233>

ARTY2 .IMG	10C	13-SEP-78	<233>
ARTY3 .IMG	10C	13-SEP-78	<233>
ARTY4 .IMG	10C	13-SEP-78	<233>
APC1 .IMG	10C	13-SEP-78	<233>
APC2 .IMG	10C	13-SEP-78	<233>
APC3 .IMG	10C	13-SEP-78	<233>
APC4 .IMG	10C	13-SEP-78	<233>
CURTK1.IMG	10C	13-SEP-78	<233>
CURTK2.IMG	10C	13-SEP-78	<233>
CURTK3.IMG	10C	13-SEP-78	<233>
CURTK4.IMG	10C	13-SEP-78	<233>
OPNTK1.IMG	10C	13-SEP-78	<233>
OPNTK2.IMG	10C	13-SEP-78	<233>
OPNTK3.IMG	10C	13-SEP-78	<233>
OPNTK4.IMG	10C	13-SEP-78	<233>
SHER1 .IMG	10C	13-SEP-78	<233>
SHER2 .IMG	10C	13-SEP-78	<233>
SHER3 .IMG	10C	13-SEP-78	<233>
SHER4 .IMG	10C	13-SEP-78	<233>
MG0A1 .IMG	10C	13-SEP-78	<233>
MG0A2 .IMG	10C	13-SEP-78	<233>
MG0A3 .IMG	10C	13-SEP-78	<233>
MG0A4 .IMG	10C	13-SEP-78	<233>
RAZMA .TAZ	88	15-SEP-78	<233>
RAZMA .FTN	120	15-SEP-78	<233>

TOTL BLKS: 1994
TOTL FILES: 60

3. EXPONENT OVERFLOW or OVERFLOW DURING REAL TO INTEGER CONVERSION. This can occur during the operation of all functions except FILTERING or THRESHOLDING. It is the result of processing with invalid data in the assigned input files, or bad data from one of the 24 stored image files. In either case, the contents of files can be inspected using the DOS/BATCH program FILDMP (see handbook). The organization and contents of typical image and coefficient files are shown in Appendix C. If bad data is suspected in any of the 24 noted image files, the best procedure is to use the DOS/BATCH program PIP to restore the files; an example of how to do this is shown in the next section.
4. UNABLE TO READ SPECIFIED FILE FORMAT or END OF FILE-END OF MEDIUM. This occurs when the RAZMA.TAZ program encounters files with improper file organization or length. Again, as above, use FILDMP or PIP to verify and transfer files.

Miscellaneous Operations

1. Generating Files. There are three categories of files associated with the RAZMA.TAZ program.
 - a. Programming operating files. These are files generated by the program for its own use. A discussion of these files is found in the comments of the program listing.
 - b. Twenty-four standard picture file sets. Each picture set consists of an image file and a normalized FFT coefficient file. These picture sets have already been generated and are stored for use by the program in the POWER function. A copy of these files is on the ROLLIN magtape.
 - c. User impact files. These are files specified by the user with the ASSIGN command. The file will be either the image or the FFT coefficient type.

The origin of the image files can be from the IPS/DICOMED system (2048x2048 or 64x64) or the RAZMA.TAZ program (64x64). Directions for creating image files under the IPS/DICOMED system can be found in Volume 1 of Reference 2. Creating a 64x64 image file under RAZMA.TAZ can be accomplished by using the reduction function, and then exiting to use PIP to rename the newly generated AVG.IMG file to whatever name the user desires. To save these files on magtape, PIP and ROLLIN are used. For

each file, the PIP command is: #DK1: name.extn/
CO<DPØ: name.extn. Then, ROLLIN is used (DOS/
BATCH handbook) to copy DK1: and create a new
ROLLIN tape.

The origin of the FFT coefficient files must be
from running RAZMA.TAZ. The file is simply created
by running the FFT function, and then exiting to
use PIP to rename the newly created FFTCOF.NRM or
FFTCOF.UNN file to whatever name the user desires.
The file can then be saved in the same manner as
the image files.

2. Restoring files. For RAZMA.TAZ to operate, all
files must be on DPØ:. If they are not (a minimum
listing appears in Special Procedures), or for
some reasons the files become invalid, the files
must be restored. A permanent copy of all files
is on the ROLLIN magtape. This tape can be loaded
onto DK1: (DOS/BATCH handbook), and then the
appropriate file transferred under PIP to DPØ:.
The proper PIP command is: #DPØ: name.extn/CO<
DK1: name.extn.
3. Changing RAZMA.TAZ. Best advice: DON'T. However,
for the brave and/or foolhardy, a bubble chart and
program listing is given in Appendix B. Once the
changes have been made under EDIT (see handbook),
the proper Fortran assembly must be made. The
proper command after \$RUN FORTRAN is: #DK1: RAZMA,
LP:<DK1: edit file name. extn / ON; or, #DPØ:
RAZMA, LP:<DK1: edit file name. extn/ON. (Assuming
EDIT was done on DK1:). This is important because
RAZMA.TAZ uses single word integer variables. When
the assembly is done, the linker command after
\$RUN LINK is: #DK1: RAZMA.TAZ<DK1: RAZMA/CC, DKØ:
FTNLIB/L/E; or: #DPØ: RAZMA.TAZ<DK1: RAZMA/CC,
DKØ: FTNLIB/L/E as appropriate.

User's Guide
Sample Sessions

EDIT

FORTRAN

PIP

ROLLIN

RAZMA.TAZ

RJ EDIT
EDIT-11 U07-03

#DK11RAZMA.FTN<DK11RAZMA.FTN

*E

*500AL

DATA(N)=0.5*(1.0+ALOG(RADIAL*0.1+1.0))

*1.515.U

DATA(N)=0.5*(1.0+ALOG(RADIAL*0.1+1.0))

*3L

DATA(N)=0.5*(1.0+ALOG(RADIAL*0.1+1.0))

CONTINUE

*20

*-A42L

DATA(N)=0.5*(1.0+ALOG(RADIAL*0.1+1.0))

*15

CONTINUE

*E

*C

*KI

\$

SRU FONTAN
FOR TRON U06.13
#DK11RAZMA,LP1<DK11RAZMA.FTN/ON
.KI

SRU LINK

LINK V01-04
#DK11RAZMA.TAZ<DK11RAZMA/CC,DK01FTNLIB/L/E

SPACE USED 030420, SPACE FREE 061132
#^C
.KI

E

\$RU PIP
PIP 010-02
#D1111FILTER.IMG/CO<DPO11PROCSD.IMG ← REMAINING FILE 1/2 STORING FILE

#EPO11FILTER.IMG/CO<DK111FILTER.IMG ← RESTORING FILE

#DK111FILTER.IMG/DI

DK11

E 11,11]

FILTER.IMG 100 15-SEP-78 <233>

#EPO11FILTER.IMG/DI

DP01

E 11,11]

FILTER.IMG 50 15-SEP-78 <233>

#^C
.KI

\$

RULLIN U07

#UT01RAZMA<DK11/RW/DATE113-SEP-78

#UT01RAZMA<DK11/DATE113-SEP-78

#

RULLIN U07

#K11<MTO1RAZMA/FI

#

} SAVE TWO COPIES of DISK
ON MAG TAPE

} RESTORING DISK FROM MAG TAPE

MULTIPLYING
AM-HE... THINK YOU CAN FOOL MOTHER NATURE EM!
DONE NULL

LEFT WORKING
DONE IFFT
5

\$PU DK12PZEMM.TAE

SPEETINGS AND SOLUTIONS
SPEAK TO ME ABOUT IMAGE INPUT

TYPE B FOR BIGGIE /204232048
J FOR JUNIOR /64564
S FOR STANDARD SET OF 24
N FOR NONE

J

THE INPUT IMAGE FILE MUST BE SPECIFIED.
IF NOT YET ASSIGNED, PLEASE DO SO NOW. THE FORM IS:
\$MS DPGNAME.EXT,7
THEN TYPE GO TO CONTINUE.

ADD5 000000
\$MS DPGNAME.EXT,7
\$CO

TYPE B FOR UNNORMALIZED FFT COEFF
U FOR UNNORMALIZED COEFF

N

FFT WORKING

FORT003022 REAL OUTSIDE PHASE ON FEEL TO INTEGER CONVERSION
NAME SEC
MAIN. 00179

DONE FFT

TYPE C TO CONTINUE, TYPE S TO STOP

C

TYPE P FOR POWER, F FOR FILTER, T FOR THRESHOLD

T

TYPE N TO MAKE NEW THRESHOLD FILE, TYPE O TO USE OLD FILE

O

THE OLD THRESHOLD FILE MUST BE SPECIFIED.
IF ALREADY ASSIGNED, TYPE GO TO CONTINUE.
IF NOT YET ASSIGNED, PLEASE DO SO NOW. THE FORM IS:
\$MS DPGNAME.EXT,1
THEN TYPE GO TO CONTINUE.

ADD5 000000
\$MS DPGNAME.EXT,1
\$CO

IF FFT COEFF WERE JUST NOW MADE, THE FILE IS
ALREADY ASSIGNED. TYPE GO TO CONTINUE.
IF NOT YET ASSIGNED, PLEASE DO SO NOW. THE FORM IS:
\$MS DPGNAME.EXT,3
THEN TYPE GO TO CONTINUE.

ADD5 000000
\$CO

DONE MULT
IFFT WORKING
DONE IFFT
5

SPU DK11PAZMA.TAE

GREETINGS AND SOLUTIONS
SPEAK TO ME ABOUT IMAGE INPUT

TYPE1 B FOR BIGGIE /2048X2048/
J FOR JUNIOR /64X64/
S FOR STANDARD SET OF 24
N FOR NONE

J

THE INPUT IMAGE FILE MUST BE SPECIFIED.
IF NOT YET ASSIGNED, PLEASE DO SO NOW, THE FORM IS:
\$AS DRAGNAME.EXT 7
THEN TYPE CO TO CONTINUE.
\$A005 000000
\$AS DRAGNAME.EXT 7
\$C0

TYPE1 N FOR NORMALISED FFT COEFF
U FOR UNNORMALIZED COEFF

N

FFT WORKING

FORTRAN3022 REAL OUTSIDE RANGE ON PEAL TO INTERGER CONVERSION
NAME SEQ
MAIN. 00.075

DONE FFT

TYPE C TO CONTINUE, TYPE S TO STOP

C

TYPE P FOR POWER, F FOR FILTER, T FOR THRESHOLD

F

TYPE1 C TO USE CURRENT FILTER EQUATION FOR FILE
O TO USE AN OLD FILTER FILE

C

MAKING FILTER
DONE FILTER

TYPE C TO CONTINUE, TYPE S TO STOP

C

IF FFT COEFF WERE JUST NOW MADE, THE FILE IS
ALREADY ASSIGNED. TYPE CO TO CONTINUE.
IF NOT YET ASSIGNED, PLEASE DO SO NOW. THE FORM IS:
\$AS DRAGNAME.EXT 3
THEN TYPE CO TO CONTINUE.
\$A005 000000
\$C0

MULTIPLYING
AN-MS.....THINK YOU CAN FOOL MOTHER NATURE EM

User's Guide

Program Bubble Chart

Program Listing

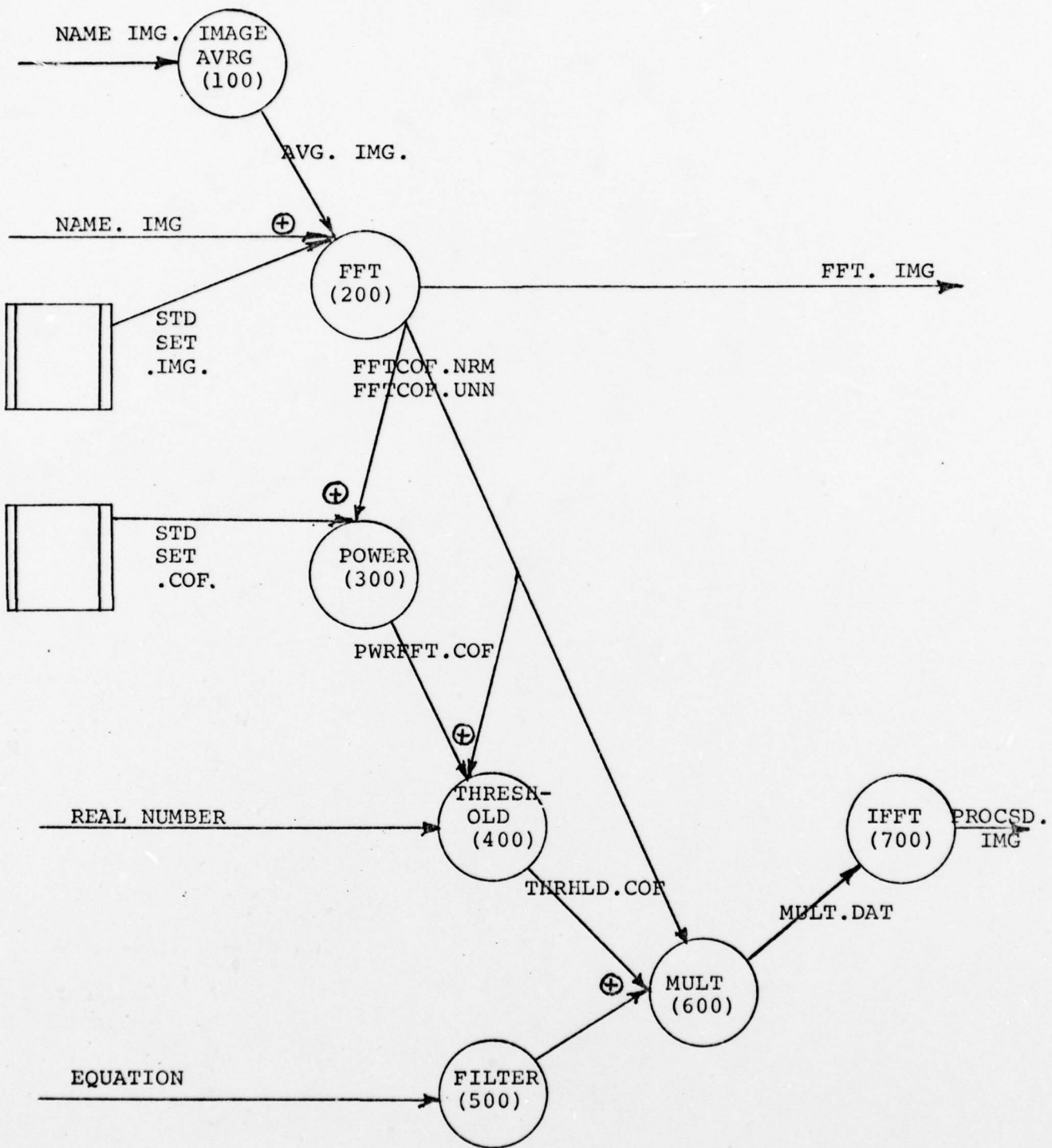


Figure 4. Program Bubble Chart

```

C *****
C PROGRAM RAZMA,TAZ
C *****

```

```

C THIS PROGRAM HAS THE FOLLOWING DISK (DP0;) RANDOM ACCESS FILE
C ASSIGNMENTS:

```

```

C AVG .IMG = OUTPUT OF REDUCE, INPUT TO FFT
C SCRATC,DAT = USED IN FFT
C FFTCOF,NRM = OUTPUT OF FFT, INPUT TO POWER
C (FFTCOF,UNN) INPUT TO THRESHOLD
C INPUT TO MULT
C FFT .IMG = OUTPUT OF FFT
C -----,COF = INPUT TO POWER
C PWRFFT,COF = OUTPUT OF POWER, INPUT TO THRESHOLD
C PWRFFT,IMG = OUTPUT OF POWER
C THRLD,FIL = OUTPUT OF THRESHOLD, INPUT TO MULT
C FILTER,COF = OUTPUT OF FILTER, INPUT TO MULT
C MULT ,DAT = OUTPUT OF MULT, USED IN IFFT
C PROCSD,IMG = OUTPUT OF IFFT

```

```

C THE FOLLOWING DEVICES ARE INTERACTIVELY ASSIGNED TO THESE
C FILES DURING THE RUNNING OF THE INDICATED MODULES:

```

FILE	1	2	3	4	5	6	7	8
BIG .IMG							REDUCE	
AVG .IMG							FFT	
FFTCOF,---			MULT	THRES	POWER			
POWFFT,COF				THRES				
FILTER,COF	MULT							
THRLD,COF	MULT							

```

C ANY I/O REFERENCE MADE TO DEVICE NUMBERS AFTER THE DEVICES HAVE
C BEEN INTERACTIVELY ASSIGNED DURING THE MODULES SPECIFIED ABOVE,
C WILL OPERATE ON THE FILE DATA EQUATED WITH THAT DEVICE NUMBER,

```

```

C COMPLEX DATA(64),DATBUF(64),DCVAL,NOFILS,MSE
C BYTE HEADER(64,8),BUFFER(2048),BBUF(2),BCOL(128),NULLS(64,8)
C INTEGER INPTR,AVGPTR,DAT3PT,DAT2PT,FFTPT,DAT7PT,DAT8PT
C INTEGER SUM,BUF,OFFSET,COL(64),UNIT,COFPTR,COFIMG,AVGFFT
C INTEGER THRSPT,OUTBW,BW,IERR,DAT1PT,DAT5PT,DAT4PT,ASGD7,PWRON
C EQUIVALENCE (BCOL(1),COL(1)),(BBUF(1),BUF)
C DATA HEADER/0,0,79,58,64,0,64,505*0/
C DATA NULLS/512*0/

```

```

1 WRITE (6,5)
  WRITE (6,6)
  WRITE (6,11)
2 WRITE (6,7)
  WRITE (6,8)

```



```
WRITE (6,9)
WRITE (6,10)
WRITE (6,11)
5  FORMAT(' GREETINGS AND SOLUTIONS ')
6  FORMAT(' SPEAK TO ME ABOUT IMAGE INPUT ')
7  FORMAT(' TYPE: B FOR BIGGIE /2048X2048/ ')
8  FORMAT('          J FOR JUNIOR /64X64/ ')
9  FORMAT('          S FOR STANDARD SET OF 24 ')
10 FORMAT('          N FOR NONE ')
11 FORMAT(' ')
12 READ (6,12) INBJSN
   FORMAT(A)
   IF(INBJSN,EQ,1HJ) GOTO 200
   IF(INBJSN,EQ,1HB) GOTO 100
   IF(INBJSN,EQ,1HN) GOTO 30
   IF(INBJSN,NE,1HS) GOTO 2
20  WRITE (6,25)
   WRITE (6,26)
   WRITE (6,27)
22  WRITE (6,28)
   WRITE (6,11)
25  FORMAT(' THE STANDARD SET OF 24 PICTURES IS ALREADY STORED ')
26  FORMAT(' IN IMAGE FILES & IN NORMALIZED FFT COEFF FILES ON DP0; ')
27  FORMAT(' IF WISH TO PROCEED TO DO POWER, FILTER, OR THRESHOLD, ')
28  FORMAT(' TYPE C TO CONTINUE, TYPE S TO STOP, ')
   READ (6,12) INCS
   IF(INCS,EQ,1HS) GOTO 900
   IF(INCS,NE,1HC) GOTO 22
30  WRITE (6,35)
   WRITE (6,36)
   WRITE (6,37)
   WRITE (6,38)
   WRITE (6,11)
35  FORMAT(' TYPE: 1 TO DO FFT ')
36  FORMAT('          2 TO DO POWER ')
37  FORMAT('          3 TO DO THRESHOLDING ')
38  FORMAT('          4 TO DO FILTERING ')
   READ (6,12) IWHERE
   IF(IWHERE,EQ,1H1) GOTO 200
   IF(IWHERE,EQ,1H2) GOTO 300
   IF(IWHERE,EQ,1H3) GOTO 400
   IF(IWHERE,NE,1H4) GOTO 30
   GOTO 500

C ***** REDUCTION MODULE *****
100 WRITE (6,105)
   WRITE (6,107)
   WRITE (6,108)
   WRITE (6,109)
105 FORMAT(' THE INPUT IMAGE FILE MUST BE SPECIFIED, ')
107 FORMAT(' IF NOT YET ASSIGNED, PLEASE DO SO NOW, THE FORM IS: ')
108 FORMAT(' SAS DP0;NAME,EXT,7 ')
109 FORMAT(' THEN TYPE CO TO CONTINUE, ')
   ASGD7='Y'
   PAUSE
   DEFINE FILE 7(4097,512,U,INPTR)
```

```

CALL SETFIL(8,'AVG,IMG',IERR,'DP',0)
DEFINE FILE 8(80,32,U,AVGPTR)
WRITE (6,110)
110  FORMAT(' AVERAGE WORKING ')
      INPTR=2
      AVGPTR=1
      DO 115 J=1,8
115  WRITE (8*AVGPTR) (HEADER(I,J),I=1,64)
      DO 116 J=1,8
116  WRITE (8*AVGPTR) (NULLS(I,J),I=1,64)

      DO 170 I=1,64
120  DO 120 K=1,64
      COL(K)=0
      DO 150 J=1,32
      READ (7*INPTR) (BUFFER(N),N=1,1024)
      READ (7*INPTR) (BUFFER(N),N=1025,2048)
      DO 140 K=1,64
      OFFSET=(K-1)*32
      SUM=0
      DO 130 L=1,32
      INDX=L+OFFSET
      BBUF(1)=BUFFER(INDX)
      SUM=SUM+BBUF
130  CONTINUE
      COL(K)=SUM/32+COL(K)
140  CONTINUE
150  CONTINUE
      DO 160 K=1,64
      COL(K)=COL(K)/32
160  CONTINUE
      WRITE (8*AVGPTR) (BCOL(N),N=1,128,2)
170  CONTINUE
      ENDFILE 7
      ENDFILE 8
190  WRITE (6,195)
      WRITE (6,11)
192  WRITE (6,196)
      WRITE (6,11)
195  FORMAT(' DONE IMAGE AVERAGING ')
196  FORMAT(' TYPE C TO CONTINUE, TYPE S TO STOP ')
      READ (6,12) INCS
      IF(INCS,EQ,1HS) GOTO 900
      IF(INCS,NE,1HC) GOTO 192
      GOTO 30

```

```

C ***** FFT MODULE *****
200  CALL SETFIL(8,'AVG,IMG',IERR,'DP',0)
      DEFINE FILE 8(80,32,U,AVGPTR)
      IF(ASGD7,EQ,1HY) GOTO 215
      WRITE (6,205)
      WRITE (6,207)
      WRITE (6,208)
      WRITE (6,209)
205  FORMAT(' THE INPUT IMAGE FILE MUST BE SPECIFIED. ')
207  FORMAT(' IF NOT YET ASSIGNED, PLEASE DO SO NOW, THE FORM IS: ')

```

```
208 FORMAT(' SAS DP0;NAME,EXT,7 ')
209 FORMAT(' THEN TYPE CO TO CONTINUE, ')
    PAUSE
    DEFINE FILE 7(80,32,U,AVGPTR)
210 WRITE (6,215)
    WRITE (6,216)
    WRITE (6,11)
215 FORMAT(' TYPE:  N FOR NORMALIZED FFT COEFF ')
216 FORMAT('          U FOR UNNORMALIZED COEFF ')
    READ (6,12) NORMUN
    DEFINE FILE 3(64,256,U,DAT3PT)
    CALL SETFIL(3,'SCRATC,DAT',IERR,'DP',0)
    DEFINE FILE 2(64,256,U,DAT2PT)
    IF(NORMUN,EQ,1HN) CALL SETFIL(2,'FFTCOF,NRM',IERR,'DP',0)
    IF(NORMUN,EQ,1HU) CALL SETFIL(2,'FFTCOF,UNN',IERR,'DP',0)
    IF(NORMUN,NE,1HU,AND,NORMUN,NE,1HN) GOTO 210
217 DEFINE FILE 1(80,32,U,FFTPTR)
    CALL SETFIL(1,'FFT,IMG',IERR,'DP',0)
    WRITE (6,219)
219 FORMAT(' FFT WORKING ')
    AVGPTR=17
    DAT2PT=1
    DAT3PT=1
    FFTPTR=1
    SCALE=1,0/64,0
    DO 220 J=1,8
220 WRITE (1'FFTPTR) (HEADER(I,J),I=1,64)
    DO 225 J=1,8
225 WRITE (1'FFTPTR) (NULLS(I,J),I=1,64)
    DO 230 K=1,64
230 COL(K)=0

    DO 250 I=1,64
    IF(ASGD7,EQ,1HY) READ(8'AVGPTR) (BCOL(N),N=1,128,2)
    IF(ASGD7,NE,1HY) READ(7'AVGPTR) (BCOL(N),N=1,128,2)
    DO 240 J=1,64
    DATA(J)=COL(J)
240 CONTINUE
    CALL FOURT(DATA,64,1,-1,1,0)
    WRITE (3'DAT3PT) (DATA(N),N=1,64)
250 CONTINUE
    DO 290 K=1,64
    DAT3PT=1
    DO 260 I=1,64
    READ (3'DAT3PT) (DATBUF(N),N=1,64)
    DATA(I)=DATBUF(K)
260 CONTINUE
    CALL FOURT(DATA,64,1,-1,1,0)
    IF(NORMUN,EQ,1HU) GOTO 270
    SCALE=256,0*64,0
    J=1
    IF(K=1) 265,265,266
265 DCVAL=DATA(1)
    J=J+1
266 DO 267 I=J,64
    DATA(I)=DATA(I)/DCVAL
```

```

267     CONTINUE
270     WRITE (2'DAT2PT) (DATA(N),N=1,64)
        DO 280 I=1,64
          COL(I)=(CABS(DATA(I)))*SCALE
280     CONTINUE
        WRITE (1'FFTPTR) (BCOL(N),N=1,128,2)
290     CONTINUE
        ENDFILE 1
        ENDFILE 2
        ENDFILE 3
        ENDFILE 7
        ENDFILE 8
        WRITE (6,296)
        WRITE (6,11)
295     WRITE (6,297)
        WRITE (6,11)
296     FORMAT(' DONE FFT ')
297     FORMAT(' TYPE C TO CONTINUE, TYPE S TO STOP ')
        READ (6,12) INCS
        IF(INCS,EQ,1HS) GOTO 900
        IF(INCS,NE,1HC) GOTO 295
298     WRITE (6,299)
        WRITE (6,11)
299     FORMAT(' TYPE P FOR POWER, F FOR FILTER, T FOR THRESHOLD ')
        READ (6,12) IPFT
        IF(IPFT,EQ,1HF) GOTO 500
        IF(IPFT,EQ,1HT) GOTO 400
        IF(IPFT,NE,1HP) GOTO 298
        GOTO 300

C      ***** POWER MODULE *****
300     CALL SETFIL(8,'PWRFFT,IMG',IERR,'DP',0)
        DEFINE FILE 8(80,32,U,DAT8PT)
        DAT8PT=1
        DO 301 J=1,8
301     WRITE(8'DAT8PT) (HEADER(I,J),I=1,64)
        DO 302 J=1,8
302     WRITE(8'DAT8PT) (NULLS(I,J),I=1,64)
303     WRITE(6,304)
        WRITE (6,11)
304     FORMAT(' TYPE: O, FOR ONLY ONE FFT INPUT; S, FOR STD 24 FFT COEFF ')
        READ (6,12) INOS
        PWRON='Y'
        IF(INOS,EQ,1HS) GOTO 312
        IF(INOS,NE,1HO) GOTO 303
        IF(NORMUN,EQ,1HN) CALL SETFIL(5,'FFTCOF,NRM',IERR,'DP',0)
        IF(NORMUN,EQ,1HU) CALL SETFIL(5,'FFTCOF,UNN',IERR,'DP',0)
        IF(NORMUN,EQ,1HN,OR,NORMUN,EQ,1HU) GOTO 308
        WRITE (6,305)
        WRITE (6,306)
        WRITE (6,307)
305     FORMAT(' FFT INPUT MUST BE SPECIFIED, PLEASE DO SO NOW. ')
306     FORMAT(' THE FORM IS:      SAS DP0:NAME,EXT,5 ')
307     FORMAT(' THEN TYPE CO TO CONTINUE, ')
        PAUSE
308     DEFINE FILE 5(64,256,U,DAT5PT)

```



```
CALL SETFIL(1,'PWRFFT,COF',IERR,'DP',0)
DEFINE FILE 1(64,256,U,DAT1PT)
WRITE (6,309)
309 FORMAT(' SQUARING FFT/S/ ')
DAT1PT=1
DAT5PT=1
DO 311 I=1,64
READ (5'DAT5PT) (DATA(N),N=1,64)
DO 310 J=1,64
DATA(J)=DATA(J)*DATA(J)
COL(J)=(CABS(DATA(J)))
310 CONTINUE
WRITE (1'DAT1PT) (DATA(N),N=1,64)
WRITE(8'DAT8PT) (BCOL(N),N=1,128,2)
311 CONTINUE
ENDFILE 1
ENDFILE 5
ENDFILE 8
GOTO 390

312 WRITE (6,309)
CALL SETFIL(5,'PWRFFT,COF',IERR,'DP',0)
DEFINE FILE 5(64,256,U,DAT5PT)
SCALE=64,0**3
NOFILS=(24,0,24,0)
DO 313 I=1,64
DATBUF(I)=(0,0,0,0)
313 CONTINUE
DAT5PT=1
DO 314 I=1,64
WRITE (5'DAT5PT) (DATBUF(N),N=1,64)
314 CONTINUE
UNIT=5
DO 360 I=1,24
DAT5PT=1
COFPTR=1
IF(UNIT=4) 319,315,317
315 DO 316 J=1,4
316 ENDFILE J
317 DO 318 J=1,4
318 DEFINE FILE J(64,256,U,COFPTR)
UNIT=0
319 UNIT=UNIT+1
320 IF(I=1) 322,321,322
321 CALL SETFIL(1,'APC1,COF',IERR,'DP',0)
CALL SETFIL(2,'APC2,COF',IERR,'DP',0)
CALL SETFIL(3,'APC3,COF',IERR,'DP',0)
CALL SETFIL(4,'APC4,COF',IERR,'DP',0)
322 IF(I=5) 335,323,324
323 CALL SETFIL(1,'ARTY1,COF',IERR,'DP',0)
CALL SETFIL(2,'ARTY2,COF',IERR,'DP',0)
CALL SETFIL(3,'ARTY3,COF',IERR,'DP',0)
CALL SETFIL(4,'ARTY4,COF',IERR,'DP',0)
324 IF(I=9) 335,325,326
325 CALL SETFIL(1,'CVRTK1,COF',IERR,'DP',0)
CALL SETFIL(2,'CVRTK2,COF',IERR,'DP',0)
```

```

CALL SETFIL(3,'CVRTK3,COF',IERR,'DP',0)
CALL SETFIL(4,'CVRTK4,COF',IERR,'DP',0)
326 IF(I=13) 335,327,328
327 CALL SETFIL(1,'OPNTK1,COF',IERR,'DP',0)
CALL SETFIL(2,'OPNTK2,COF',IERR,'DP',0)
CALL SETFIL(3,'OPNTK3,COF',IERR,'DP',0)
CALL SETFIL(4,'OPNTK4,COF',IERR,'DP',0)
328 IF(I=17) 335,329,330
329 CALL SETFIL(1,'M60A1,COF',IERR,'DP',0)
CALL SETFIL(2,'M60A2,COF',IERR,'DP',0)
CALL SETFIL(3,'M60A3,COF',IERR,'DP',0)
CALL SETFIL(4,'M60A4,COF',IERR,'DP',0)
330 IF(I=21) 335,331,335
331 CALL SETFIL(1,'SHER1,COF',IERR,'DP',0)
CALL SETFIL(2,'SHER2,COF',IERR,'DP',0)
CALL SETFIL(3,'SHER3,COF',IERR,'DP',0)
CALL SETFIL(4,'SHER4,COF',IERR,'DP',0)
335 CONTINUE
DO 350 J=1,64
READ(5'DATSPT) (DATBUF(N),N=1,64)
READ(UNIT'COFPTR) (DATA(N),N=1,64)
DO 337 K=1,64
337 DATA(K)=DATA(K)*DATA(K)
DO 340 K=1,64
DATBUF(K)=DATBUF(K)+DATA(K)
340 CONTINUE
DATSPT=DATSPT+1
WRITE(5'DATSPT) (DATBUF(N),N=1,64)
350 CONTINUE
360 CONTINUE
365 DATSPT=1
DO 380 I=1,64
READ(5'DATSPT) (DATA(N),N=1,64)
DO 370 J=1,64
DATA(J)=DATA(J)/NOFILS
COL(J)=(CABS(DATA(J)))*SCALE
370 CONTINUE
DATSPT=DATSPT+1
WRITE(5'DATSPT) (DATA(N),N=1,64)
WRITE(8'DAT8PT) (BCOL(N),N=1,128,2)
380 CONTINUE
DO 385 I=1,5
385 ENDFILE I
ENDFILE 8
390 WRITE (6,395)
WRITE (6,11)
395 FORMAT(' DONE POWER ')
GOTO 400

C ***** THRESHOLD MODULE *****
400 WRITE (6,405)
WRITE(6,11)
405 FORMAT(' TYPE N TO MAKE NEW THRESHOLD FILE,TYPE 0 TO USE OLD FILE ')
READ (6,12) INNO
IF(INNO,EQ,1HO) GOTO 600
IF(INNO,NE,1HN) GOTO 400

```

```

410  WRITE (6,415)
      WRITE (6,416)
      WRITE (6,11)
415  FORMAT(' TYPE:  V FOR VANILLA PLAIN FFT COEFF ')
416  FORMAT('      A FOR AVERAGED/SQUARED FFT INPUT ')
      READ (6,12) INVA
      IF(INVA,EQ,1HA) CALL SETFIL(4,'PWRFFT,COF',IERR,'DP',0)
      IF(INVA,EQ,1HV,AND,NORMUN,EQ,1HN)
1CALL SETFIL(4,'FFTCOF,NRM',IERR,'DP',0)
      IF(INVA,EQ,1HV,AND,NORMUN,EQ,1HU)
1CALL SETFIL(4,'FFTCOF,UNN',IERR,'DP',0)
      IF(INVA,NE,1HA,AND,INVA,NE,1HV) GOTO 410
      IF(NORMUN,EQ,1HN,OR,NORMUN,EQ,1HU,OR,PWRON,EQ,1HY) GOTO 430
      WRITE (6,424)
      WRITE (6,425)
      WRITE (6,426)
      WRITE (6,427)
      WRITE (6,428)
424  FORMAT(' THE FILE TO BE THRESHOLDED MUST BE SPECIFIED. ')
425  FORMAT(' IF NOT YET ASSIGNED, PLEASE DO SO NOW. ')
426  FORMAT(' THE FORM IS: ')
427  FORMAT(' $AS DP0;NAME,EXT,4 ')
428  FORMAT(' THEN TYPE CO TO CONTINUE ')
      PAUSE
430  DEFINE FILE 4(64,256,U,DAT4PT)
      CALL SETFIL(1,'THRHLD,FIL',IERR,'DP',0)
      DEFINE FILE 1(64,256,U,THRSPT)
      WRITE (6,431)
432  WRITE (6,433)
      WRITE (6,11)
431  FORMAT(' SPECIFY A REAL VALUE FOR THE THRESHOLD OF ')
433  FORMAT(' THE FORM = 0.0000 /UP TO 15 TRAILING DIGITS/ ')
      READ (6,435,ERR=432) THRES
435  FORMAT(F18,15)
      WRITE(6,439)
      WRITE (6,11)
439  FORMAT(' THRESHOLD WORKING ')

      DAT4PT=1
      THRSPT=1
      BW=0
      MSE=(0,0,0,0)
      DO 470 I=1,64
      READ (4'DAT4PT) (DATA(N),N=1,64)
          DO 460 J=1,64
              DATBUF(J)=(1,0,0,0)
              BELOW=CABS(DATA(J))-THRES
450  IF(BELOW) 451,453,453
451  MSE=MSE+DATA(J)
              OUTBW=OUTBW+1
              DATBUF(J)=(0,0,0,0)
453  CONTINUE
460  CONTINUE
      WRITE(1'THRSPT) (DATBUF(N),N=1,64)
470  CONTINUE
      ENDFILE 1

```

ENDFILE 4

BW=4096=OUTBW

ABSMSE=CABS(MSE)

FRACBW=FLOAT(BW)/4096.0

WRITE(6,480) THRES

WRITE (6,482) ABSMSE

WRITE (6,484) BW,FRACBW

WRITE (6,11)

480 FORMAT(' THIS THRLD,FIL USED A REAL THRESHOLD OF ',F18.15)

482 FORMAT(' THE ABSOLUTE MSE WAS = ',F18.15)

484 FORMAT(' AND THE BANDWIDTH WAS= ',I4,'/4096 OR ',F12.9)

490 WRITE (6,495)

WRITE (6,11)

491 WRITE (6,496)

WRITE (6,11)

495 FORMAT(' END THRESHOLD ')

496 FORMAT(' TYPE C TO CONTINUE,TYPE S TO STOP ')

READ (6,12) INCS

IF(INCS.EQ.1HS) GOTO 900

IF(INCS.NE.1HC) GOTO 491

GOTO 600

C ***** FILTER MODULE *****

500 WRITE (6,505)

WRITE (6,506)

WRITE (6,11)

505 FORMAT(' TYPE: C TO USE CURRENT FILTER EQUATION FOR FILE ')

506 FORMAT(' O TO USE AN OLD FILTER FILE ')

READ (6,12) INCO

IF(INCO.EQ.1HO) GOTO 600

IF(INCO.NE.1HC) GOTO 500

510 WRITE (6,512)

512 FORMAT(' MAKING FILTER ')

DEFINE FILE 1(64,256,U,DAT1PT)

CALL SETFIL(1,'FILTER.COF',IERR,'DP',0)

KAPA1=0

KAPA2=0

SIGMA1=0.

SIGMA2=0.

DAT1PT=1

IFOLD=34

DO 530 M=1,64

MM=M

DO 520 N=1,64

NN=N

IF(M.GE.IFOLD) MM=66-M

I=MM-1

IF(N.GE.IFOLD) NN=66-N

J=NN-1

SQIJ=I**2+J**2

RADIAL=SQRT(SQIJ)

515 DATA(N)=0.5*(1.0+ALOG(RADIAL*0.1+1.0))

520 CONTINUE

WRITE (1'DAT1PT) (DATA(N),N=1,64)

530 CONTINUE


```
ENDFILE 1
WRITE (6,545)
WRITE (6,11)
540 WRITE (6,546)
WRITE (6,11)
545 FORMAT(' DONE FILTER ')
546 FORMAT(' TYPE C TO CONTINUE, TYPE S TO STOP ')
READ (6,12) INCS
IF(INCS,EQ,1HS) GOTO 900
IF(INCS,NE,1HC) GOTO 540
GOTO 600

C ***** MATRIX MULT MODULE *****
600 IF(INNO,EQ,1HN) CALL SETFIL(1,'THRHLDFIL',IERR,'DP',0)
IF(INCO,EQ,1HC) CALL SETFIL(1,'FILTERCOF',IERR,'DP',0)
IF(INNO,NE,1HO,AND,INCO,NE,1HO) GOTO 620
IF(INNO,EQ,1HO) WRITE (6,605)
IF(INCO,EQ,1HO) WRITE (6,606)
605 FORMAT(' THE OLD THRESHOLD FILE MUST BE SPECIFIED. ')
606 FORMAT(' THE OLD FILTER FILE MUST BE SPECIFIED. ')
WRITE (6,607)
WRITE (6,608)
WRITE (6,609)
WRITE (6,610)
607 FORMAT(' IF ALREADY ASSIGNED, TYPE CO TO CONTINUE. ')
608 FORMAT(' IF NOT YET ASSIGNED, PLEASE DO SO NOW, THE FORM IS: ')
609 FORMAT(' SAS DP0;NAME,EXT,1 ')
610 FORMAT(' THEN TYPE CO TO CONTINUE. ')
PAUSE
620 DEFINE FILE 1(64,256,U,DAT1PT)
IF(NORMUN,EQ,1HU) CALL SETFIL(3,'FFTCOF,UNN',IERR,'DP',0)
IF(NORMUN,EQ,1HN) CALL SETFIL(3,'FFTCOF,NRM',IERR,'DP',0)
WRITE (6,625)
WRITE (6,626)
WRITE (6,627)
WRITE (6,628)
WRITE (6,629)
625 FORMAT(' IF FFT COEFF WERE JUST NOW MADE, THE FILE IS ')
626 FORMAT(' ALREADY ASSIGNED, TYPE CO TO CONTINUE. ')
627 FORMAT(' IF NOT YET ASSIGNED, PLEASE DO SO NOW, THE FORM IS: ')
628 FORMAT(' SAS DP0;NAME,EXT,3 ')
629 FORMAT(' THEN TYPE CO TO CONTINUE. ')
PAUSE
DEFINE FILE 3(64,256,U,DAT3PT)
IF(NORMUN,EQ,1HU,OR,NORMUN,EQ,1HN) GOTO 640
630 WRITE (6,635)
WRITE (6,11)
635 FORMAT(' TYPE N FOR NORM FFT COEFF, TYPE U FOR UNNORMALIZED COEFF ')
READ (6,12) NORMUN
IF(NORMUN,NE,1HU,AND,NORMUN,NE,1HN) GOTO 630
640 CALL SETFIL(2,'MULT,DAT',IERR,'DP',0)
DEFINE FILE 2(64,256,U,DAT2PT)
WRITE (6,645)
645 FORMAT(' MULTIPLYING ')
DAT1PT=1
```

```

3      DAT2PT=1
7      DAT3PT=1
9      DO 680 I=1,64
1      READ (3'DAT3PT) (DATA(N),N=1,64)
2      READ (1'DAT1PT) (DATBUF(N),N=1,64)
3      IF(NORMUN,EQ,1HU) GOTO 665
4      K=1
5      IF(I=1) 650,650,655
6      650  WRITE (6,651)
7      651  FORMAT(' AH=HA...,THINK YOU CAN FOOL MOTHER NATURE EH! ')
3      DCVAL=DATA(1)
9      K=K+1
3      655  DO 660 J=K,64
1          DATA(J)=DATA(J)*DCVAL
2      660  CONTINUE
5      665  DO 670 J=1,64
4          DATA(J)=DATA(J)*DATBUF(J)
5      670  CONTINUE
9      WRITE (2'DAT2PT) (DATA(N),N=1,64)
7      680  CONTINUE
3      ENDFILE 1
9      ENDFILE 2
3      ENDFILE 3
1      WRITE (6,695)
2      WRITE (6,11)
5      695  FORMAT(' DONE MULT ')
4      GOTO 700

C      ***** INVERSE FFT MODULE *****
5      700  CALL SETFIL(2,'MULT,DAT',IERR,'DP',0)
9      DEFINE FILE 2(64,256,U,DAT2PT)
7      CALL SETFIL(8,'PROCS,IMG',IERR,'DP',0)
3      DEFINE FILE 8(80,32,U,DAT8PT)
9      WRITE (6,730)
7      730  FORMAT (' IFFT WORKING ')
1      DAT2PT=1
2      DAT8PT=1
5      SCALE=1.0/4096.0
4      DO 740 J=1,8
5      WRITE (8'DAT8PT) (HEADER(I,J),I=1,64)
9      740  CONTINUE
7      DO 745 J=1,8
3      WRITE (8'DAT8PT) (NULLS(I,J),I=1,64)
9      745  CONTINUE
3      DO 750 I=1,64
1      READ (2'DAT2PT) (DATA(N),N=1,64)
2      CALL FOURT(DATA,64,1,1,1,0)
5      DAT2PT=DAT2PT=1
1      WRITE (2'DAT2PT) (DATA(N),N=1,64)
5      750  CONTINUE

9      DO 780 K=1,64
7      DAT2PT=1
3      DO 760 I=1,64
9      READ (2'DAT2PT) (DATBUF(N),N=1,64)
3      DATA(I)=DATBUF(K)

```

```
760      CONTINUE
      CALL FOURT(DATA,64,1,1,1,0)
      DO 770 I=1,64
      COL(I)=(REAL(DATA(I)))*SCALE
770      CONTINUE
      WRITE (8'DAT8PT) (BCOL(N),N=1,128,2)
780      CONTINUE
      ENDFILE 2
      ENDFILE 8
      WRITE (6,795)
795      FORMAT(' DONE IFFT ')
900      END
```

ROUTINES CALLED:

SETFIL, FOURT, CABS, FLOAT, SQRT, ALOG, REAL

OPTIONS =/ON,/OP:3

BLOCK	LENGTH
MAIN,	9645 (045532)*

```
**COMPILER ----- CORE**
  PHASE      USED  FREE
DECLARATIVES 00963 14349
EXECUTABLES  03343 11969
ASSEMBLY     04731 15221
```

SUBROUTINE FOURT(DATA,NN,NDIM,ISIGN,IFORM,WORK)

THE COOLEY-TUKEY FAST FOURIER TRANSFORM IN USASI BASIC FORTRAN

TRANSFORM(K1,K2,...) = SUM(DATA(J1,J2,...)*EXP(ISIGN*2*PI*SQRT(-1) *((J1-1)*(K1-1)/NN(1)+(J2-1)*(K2-1)/NN(2)+...))), SUMMED FOR ALL J1, K1 BETWEEN 1 AND NN(1), J2, K2 BETWEEN 1 AND NN(2), ETC, THERE IS NO LIMIT TO THE NUMBER OF SUBSCRIPTS, DATA IS A MULTIDIMENSIONAL COMPLEX ARRAY WHOSE REAL AND IMAGINARY PARTS ARE ADJACENT IN STORAGE, SUCH AS FORTRAN IV PLACES THEM, IF ALL IMAGINARY PARTS ARE ZERO (DATA ARE DISGUISED REAL), SET IFORM TO ZERO TO CUT THE RUNNING TIME BY UP TO FORTY PERCENT, OTHERWISE, IFORM = +1, THE LENGTHS OF ALL DIMENSIONS ARE STORED IN ARRAY NN, OF LENGTH NDIM, THEY MAY BE ANY POSITIVE INTEGERS, THO THE PROGRAM RUNS FASTER ON COMPOSITE INTEGERS, AND ESPECIALLY FAST ON NUMBERS RICH IN FACTORS OF TWO, ISIGN IS +1 OR -1, IF A -1 TRANSFORM IS FOLLOWED BY A +1 ONE (OR A +1 BY A -1) THE ORIGINAL DATA REAPPEAR, MULTIPLIED BY NTOT (=NN(1)*NN(2)*...), TRANSFORM VALUES ARE ALWAYS COMPLEX, AND ARE RETURNED IN ARRAY DATA, REPLACING THE INPUT, IN ADDITION, IF ALL DIMENSIONS ARE NOT POWERS OF TWO, ARRAY WORK MUST BE SUPPLIED, COMPLEX OF LENGTH EQUAL TO THE LARGEST NON 2**K DIMENSION, OTHERWISE, REPLACE WORK BY ZERO IN THE CALLING SEQUENCE, NORMAL FORTRAN DATA ORDERING IS EXPECTED, FIRST SUBSCRIPT VARYING FASTEST, ALL SUBSCRIPTS BEGIN AT ONE.

RUNNING TIME IS MUCH SHORTER THAN THE NAIVE NTOT**2, BEING GIVEN BY THE FOLLOWING FORMULA, DECOMPOSE NTOT INTO 2**K2 * 3**K3 * 5**K5 * ..., LET SUM2 = 2**K2, SUMF = 3**K3 + 5**K5 + ..., AND NF = K3 + K5 + ..., THE TIME TAKEN BY A MULTI-DIMENSIONAL TRANSFORM ON THESE NTOT DATA IS T = T0 + NTOT*(T1+

T2*SUM2+T3*SUMF+T4*NF), ON THE CDC 3300 (FLOATING POINT ADD TIME OF SIX MICROSECONDS), T = 3000 + NTOT*(500+43*SUM2+68*SUMF+320*NF) MICROSECONDS ON COMPLEX DATA, IN ADDITION, THE ACCURACY IS GREATLY IMPROVED, AS THE RMS RELATIVE ERROR IS BOUNDED BY 3*2**(-8)*SUM(FACTOR(J)**1.5), WHERE B IS THE NUMBER OF BITS IN THE FLOATING POINT FRACTION AND FACTOR(J) ARE THE PRIME FACTORS OF NTOT.

PROGRAM BY NORMAN BRENNER FROM THE BASIC PROGRAM BY CHARLES RADER, RALPH ALTER SUGGESTED THE IDEA FOR THE DIGIT REVERSAL, MIT LINCOLN LABORATORY, AUGUST 1967, THIS IS THE FASTEST AND MOST VERSATILE VERSION OF THE FFT KNOWN TO THE AUTHOR, SHORTER PROGRAMS FOUR1 AND FOUR2 RESTRICT DIMENSION LENGTHS TO POWERS OF TWO, SEE== IEEE AUDIO TRANSACTIONS (JUNE 1967), SPECIAL ISSUE ON FFT,

THE DISCRETE FOURIER TRANSFORM PLACES THREE RESTRICTIONS UPON THE DATA,

1. THE NUMBER OF INPUT DATA AND THE NUMBER OF TRANSFORM VALUES MUST BE THE SAME.
2. BOTH THE INPUT DATA AND THE TRANSFORM VALUES MUST REPRESENT EQUISPACED POINTS IN THEIR RESPECTIVE DOMAINS OF TIME AND FREQUENCY, CALLING THESE SPACINGS DELTAT AND DELTAF, IT MUST BE

C TRUE THAT DELTAF=2*PI/(NN(I)*DELTAT). OF COURSE, DELTAT NEED NOT
 C BE THE SAME FOR EVERY DIMENSION.
 C 3. CONCEPTUALLY AT LEAST, THE INPUT DATA AND THE TRANSFORM OUTPUT
 C REPRESENT SINGLE CYCLES OF PERIODIC FUNCTIONS,
 C

C EXAMPLE 1. THREE-DIMENSIONAL FORWARD FOURIER TRANSFORM OF A
 C COMPLEX ARRAY DIMENSIONED 32 BY 25 BY 13 IN FORTRAN IV.
 C DIMENSION DATA(32,25,13),WORK(50),NN(3)
 C COMPLEX DATA
 C

C DATA NN/32,25,13/
 C DO 1 I=1,32
 C DO 1 J=1,25
 C DO 1 K=1,13
 C 1 DATA(I,J,K)=COMPLEX VALUE
 C CALL FOURT(DATA,NN,3,-1,1,WORK)
 C

C EXAMPLE 2. ONE-DIMENSIONAL FORWARD TRANSFORM OF A REAL ARRAY OF
 C LENGTH 64 IN FORTRAN II.
 C DIMENSION DATA(2,64)
 C DO 2 I=1,64
 C DATA(1,I)=REAL PART
 C 2 DATA(2,I)=0.
 C CALL FOURT(DATA,64,1,-1,0,0)
 C

2 DIMENSION DATA(1),NN(1),IFACT(32),WORK(1)
 C CDC 6600 INITIALIZATION

5 WR=0.
 1 WI=0.
 5 WSTPR=0.
 5 WSTPI=0.
 7 TWOPI=6.283185307
 3 IF(NDIM=1)920,1,1
 3 1 NTOT=2
 3 DO 2 IDIM=1,NDIM
 1 IF(NN(IDIM))920,920,2
 2 2 NTOT=NTOT*NN(IDIM)
 C

C MAIN LOOP FOR EACH DIMENSION
 C

5 NP1=2
 1 DO 910 IDIM=1,NDIM
 5 N=NN(IDIM)
 5 NP2=NP1*N
 7 IF(N=1)920,900,5
 C

C FACTOR N
 C

3 5 M=N
 3 NTWO=NP1
 3 IF=1
 1 IDIV=2
 2 10 IQUOT=M/IDIV
 5 IREM=M-IDIV*IQUOT
 1 IF(IQUOT=IDIV)50,11,11

```
5 11 IF(IREM)20,12,20
> 12 NTWO=NTWO+NTWO
> M=IQUOT
3 GO TO 10
> 20 IDIV=3
> 30 IQUOT=M/IDIV
1 IREM=M-IDIV*IQUOT
2 IF(IQUOT-IDIV)60,31,31
5 31 IF(IREM)40,32,40
1 32 IFACT(IF)=IDIV
5 IF=IF+1
> M=IQUOT
7 GO TO 30
3 40 IDIV=IDIV+2
> GO TO 30
> 50 IF(IREM)60,51,60
1 51 NTWO=NTWO+NTWO
2 GO TO 70
5 60 IFACT(IF)=M
C
C SEPARATE FOUR CASES==
C 1. COMPLEX TRANSFORM OR REAL TRANSFORM FOR THE 4TH, 5TH,ETC.
C DIMENSIONS.
C 2. REAL TRANSFORM FOR THE 2ND OR 3RD DIMENSION. METHOD==
C TRANSFORM HALF THE DATA, SUPPLYING THE OTHER HALF BY CON-
C JUGATE SYMMETRY.
C 3. REAL TRANSFORM FOR THE 1ST DIMENSION, N ODD. METHOD==
C TRANSFORM HALF THE DATA AT EACH STAGE, SUPPLYING THE OTHER
C HALF BY CONJUGATE SYMMETRY.
C 4. REAL TRANSFORM FOR THE 1ST DIMENSION, N EVEN. METHOD==
C TRANSFORM A COMPLEX ARRAY OF LENGTH N/2 WHOSE REAL PARTS
C
C ARE THE EVEN NUMBERED REAL VALUES AND WHOSE IMAGINARY PARTS
C ARE THE ODD NUMBERED REAL VALUES. SEPARATE AND SUPPLY
C THE SECOND HALF BY CONJUGATE SYMMETRY.
C
1 70 NON2=NP1*(NP2/NTWO)
5 ICASE=1
> IF(IDIM=4)71,90,90
7 71 IF(IFORM)72,72,90
3 72 ICASE=2
> IF(IDIM=1)73,73,90
1 73 ICASE=3
1 IF(NTWO=NP1)90,90,74
2 74 ICASE=4
5 NTWO=NTWO/2
1 N=N/2
5 NP2=NP2/2
> NTOT=NTOT/2
7 I=3
3 DO 80 J=2,NTOT
> DATA(J)=DATA(I)
1 80 I=I+2
1 90 I1RNG=NP1
2 IF(ICASE=2)100,95,100
5 95 I1RNG=NP0*(1+NPREV/2)
```

```

C
C SHUFFLE ON THE FACTORS OF TWO IN N, AS THE SHUFFLING
C CAN BE DONE BY SIMPLE INTERCHANGE, NO WORKING ARRAY IS NEEDED
C
100 IF(NTWO=NP1)600,600,110
110 NP2HF=NP2/2
    J=1
    DO 150 I2=1, NP2, NON2
      IF(J=I2)120,130,130
    120 I1MAX=I2+NON2-2
      DO 125 I1=I2, I1MAX, 2
      DO 125 I3=I1, NTOT, NP2
      J3=J+I3-I2
      TEMPR=DATA(I3)
      TEMPI=DATA(I3+1)
      DATA(I3)=DATA(J3)
      DATA(I3+1)=DATA(J3+1)
      DATA(J3)=TEMPR
      DATA(J3+1)=TEMPI
    125 DATA(J3+1)=TEMPI
    130 M=NP2HF
    140 IF(J=M)150,150,145
    145 J=J-M
      M=M/2
    IF(M=NON2)150,140,140
    150 J=J+M
C
C MAIN LOOP FOR FACTORS OF TWO. PERFORM FOURIER TRANSFORMS OF
C LENGTH FOUR, WITH ONE OF LENGTH TWO IF NEEDED. THE TWIDDLE FACTOR
C W=EXP(ISIGN*2*PI*SQRT(-1)*M/(4*MMAX)). CHECK FOR W=ISIGN*SQRT(-1)
C AND REPEAT FOR W=ISIGN*SQRT(-1)*CONJUGATE(W).
C
NON2T=NON2+NON2
IPAR=NTWO/NP1
310 IF(IPAR=2)350,330,320
320 IPAR=IPAR/4
    GO TO 310
330 DO 340 I1=1, I1RNG, 2
      DO 340 J3=I1, NON2, NP1
          DO 340 K1=J3, NTOT, NON2T
            K2=K1+NON2
            TEMPR=DATA(K2)
            TEMPI=DATA(K2+1)
            DATA(K2)=DATA(K1)-TEMPR
            DATA(K2+1)=DATA(K1+1)-TEMPI
            DATA(K1)=DATA(K1)+TEMPR
            DATA(K1+1)=DATA(K1+1)+TEMPI
          340 DATA(K1+1)=DATA(K1+1)+TEMPI
          350 MMAX=NON2
          360 IF(MMAX=NP2HF)370,600,600
          370 LMAX=MAX0(NON2T, MMAX/2)
            IF(MMAX=NON2)405,405,380
          380 THETA=TWOPI*FLOAT(NON2)/FLOAT(4*MMAX)
            IF(ISIGN)400,390,390
          390 THETA=THETA
          400 WR=COS(THETA)

```

```
3      WI=SIN(THETA)
4      WSTPR=2,*WI*WI
5      WSTPI=2,*WR*WI
6      405  DO 570 L=NON2,LMAX,NON2T
7          M=L
8          IF(MMAX=NON2)420,420,410
9      410  W2R=WR*WR=WI*WI
10         W2I=2,*WR*WI
11         W3R=W2R*WR=W2I*WI
12         W3I=W2R*WI+W2I*WR
13      420  DO 530 I1=1,I1RNG,2
14         DO 530 J3=I1,NON2,NP1
15         KMIN=J3+IPAR*M
16         IF(MMAX=NON2)430,430,440
17      430  KMIN=J3
18
19      440  KDIF=IPAR*MMAX
20      450  KSTEP=4*KDIF
21         DO 520 K1=KMIN,NTOT,KSTEP
22         K2=K1+KDIF
23         K3=K2+KDIF
24         K4=K3+KDIF
25         IF(MMAX=NON2)460,460,480
26      460  U1R=DATA(K1)+DATA(K2)
27         U1I=DATA(K1+1)+DATA(K2+1)
28         U2R=DATA(K3)+DATA(K4)
29         U2I=DATA(K3+1)+DATA(K4+1)
30         U3R=DATA(K1)-DATA(K2)
31         U3I=DATA(K1+1)-DATA(K2+1)
32         IF(ISIGN)470,475,475
33      470  U4R=DATA(K3+1)-DATA(K4+1)
34         U4I=DATA(K4)-DATA(K3)
35         GO TO 510
36      475  U4R=DATA(K4+1)-DATA(K3+1)
37         U4I=DATA(K3)-DATA(K4)
38         GO TO 510
39      480  T2R=W2R*DATA(K2)+W2I*DATA(K2+1)
40         T2I=W2R*DATA(K2+1)+W2I*DATA(K2)
41         T3R=WR*DATA(K3)+WI*DATA(K3+1)
42         T3I=WR*DATA(K3+1)+WI*DATA(K3)
43         T4R=W3R*DATA(K4)+W3I*DATA(K4+1)
44         T4I=W3R*DATA(K4+1)+W3I*DATA(K4)
45         U1R=DATA(K1)+T2R
46         U1I=DATA(K1+1)+T2I
47         U2R=T3R+T4R
48         U2I=T3I+T4I
49         U3R=DATA(K1)-T2R
50
51         U3I=DATA(K1+1)-T2I
52         IF(ISIGN)490,500,500
53      490  U4R=T3I-T4I
54         U4I=T4R-T3R
55         GO TO 510
56      500  U4R=T4I-T3I
57         U4I=T3R-T4R
58      510  DATA(K1)=U1R+U2R
```



```

2      DATA(K1+1)=U1I+U2I
5      DATA(K2)=U3R+U4R
4      DATA(K2+1)=U3I+U4I
5      DATA(K3)=U1R=U2R
6      DATA(K3+1)=U1I=U2I
7      DATA(K4)=U3R=U4R
8      520 DATA(K4+1)=U3I=U4I
9      KMIN=4*(KMIN-J3)+J3
10     KDIF=KSTEP
11     IF(KDIF=NP2)450,530,530
12     530 CONTINUE
13     M=MMAX=M
14     IF(ISIGN)540,550,550
15     540 TEMPR=WR
16     WR=-WI
17     WI=-TEMPR
18     GO TO 560
19     550 TEMPR=WR
20     WR=WI
21     WI=TEMPR
22     560 IF(M=LMAX)565,565,410
23     565 TEMPR=WR
24     WR=WR*WSTPR-WI*WSTPI+WR
25
26     570 WI=WI*WSTPR+TEMPR*WSTPI+WI
27     IPAR=3-IPAR
28     MMAX=MMAX+MMAX
29     GO TO 360
30
31     C
32     C MAIN LOOP FOR FACTORS NOT EQUAL TO TWO. APPLY THE TWIDDLE FACTOR
33     C W=EXP(ISIGN*2*PI*SQRT(-1)*(J2-1)*(J1-J2)/(NP2*IFP1)), THEN
34     C PERFORM A FOURIER TRANSFORM OF LENGTH IFACT(IF), MAKING USE OF
35     C CONJUGATE SYMMETRIES,
36     C
37     600 IF(NTWO=NP2)605,700,700
38     605 IFP1=NON2
39     IF=1
40     NP1HF=NP1/2
41     610 IFP2=IFP1/IFACT(IF)
42     J1RNG=NP2
43     IF(ICASE=3)612,611,612
44     611 J1RNG=(NP2+IFP1)/2
45     J2STP=NP2/IFACT(IF)
46     J1RG2=(J2STP+IFP2)/2
47     612 J2MIN=1+IFP2
48     IF(IFP1=NP2)615,640,640
49     615 DO 635 J2=J2MIN,IFP1,IFP2
50     THETA=-TWOPI*FLOAT(J2-1)/FLOAT(NP2)
51     IF(ISIGN)625,620,620
52     620 THETA=-THETA
53     625 SINTH=SIN(THETA/2.)
54     WSTPR=-2.*SINTH*SINTH
55     WSTPI=SIN(THETA)
56     WR=WSTPR+1.
57     WI=WSTPI

```

```

1      J1MIN=J2+IFP1
2      DO 635 J1=J1MIN,J1RNG,IFP1
3      I1MAX=J1+I1RNG-2
4      DO 630 I1=J1,I1MAX,2
5      DO 630 I3=I1,NTOT,NP2
6      J3MAX=I3+IFP2-NP1
7      DO 630 J3=I3,J3MAX,NP1
8      TEMPR=DATA(J3)
9      DATA(J3)=DATA(J3)*WR=DATA(J3+1)*WI
10     630 DATA(J3+1)=TEMPR*WI+DATA(J3+1)*WR
11     TEMPR=WR
12     WR=WR*WSTPR=WI*WSTPI+WR
13     635 WI=TEMPR*WSTPI+WI*WSTPR+WI
14     640 THETA=-TWOPI/FLOAT(IFACT(IF))
15     IF(ISIGN)650,645,645
16     645 THETA=-THETA
17     650 SINTH=SIN(THETA/2,)
18     WSTPR=2,*SINTH*SINTH
19     WSTPI=SIN(THETA)
20     KSTEP=2*N/IFACT(IF)
21     KRANG=KSTEP*(IFACT(IF)/2)+1
22     DO 698 I1=1,I1RNG,2
23     DO 698 I3=I1,NTOT,NP2
24     DO 690 KMIN=1,KRANG,KSTEP
25     J1MAX=I3+J1RNG-IFP1
26     DO 680 J1=I3,J1MAX,IFP1
27     J3MAX=J1+IFP2-NP1
28     DO 680 J3=J1,J3MAX,NP1
29     J2MAX=J3+IFP1-IFP2
30     K=KMIN+(J3-J1+(J1-I3)/IFACT(IF))/NP1HF
31     IF(KMIN=1)655,655,665
32
33     655 SUMR=0,
34     SUMI=0,
35     DO 660 J2=J3,J2MAX,IFP2
36     SUMR=SUMR+DATA(J2)
37     660 SUMI=SUMI+DATA(J2+1)
38     WORK(K)=SUMR
39     WORK(K+1)=SUMI
40     GO TO 680
41     665 KCONJ=K+2*(N=KMIN+1)
42     J2=J2MAX
43     SUMR=DATA(J2)
44     SUMI=DATA(J2+1)
45     OLDSR=0,
46     OLDSI=0,
47     J2=J2-IFP2
48     670 TEMPR=SUMR
49     TEMPI=SUMI
50     SUMR=TWO*WR*SUMR-OLDSR+DATA(J2)
51     SUMI=TWO*WR*SUMI-OLDSI+DATA(J2+1)
52     OLDSR=TEMPR
53     OLDSI=TEMPI
54     J2=J2-IFP2
55     IF(J2=J3)675,675,670
56     675 TEMPR=WR*SUMR-OLDSR+DATA(J2)

```

```

TEMPI=WI*SUMI
WORK(K)=TEMPR-TEMPI
WORK(KCONJ)=TEMPR+TEMPI
TEMPR=WR*SUMI-OLDSI+DATA(J2+1)
TEMPI=WI*SUMR
WORK(K+1)=TEMPR+TEMPI
WORK(KCONJ+1)=TEMPR-TEMPI
    
```

```

680 CONTINUE
IF(KMIN=1)685,685,686
685 WR=WSTPR+1,
WI=WSTPI
GO TO 690
686 TEMPR=WR
WR=WR*WSTPR-WI*WSTPI+WR
WI=TEMPR*WSTPI+WI*WSTPR+WI
690 TWOWR=WR+WR
IF(ICASE=3)692,691,692
691 IF(IFP1=NP2)695,692,692
692 K=1
I2MAX=I3+NP2-NP1
DO 693 I2=I3,I2MAX,NP1
DATA(I2)=WORK(K)
DATA(I2+1)=WORK(K+1)
693 K=K+2
GO TO 698
    
```

C
C COMPLETE A REAL TRANSFORM IN THE 1ST DIMENSION, N ODD, BY CON-
C JUGATE SYMMETRIES AT EACH STAGE,
C

```

695 J3MAX=I3+IFP2-NP1
DO 697 J3=I3,J3MAX,NP1
J2MAX=J3+NP2-J2STP
DO 697 J2=J3,J2MAX,J2STP
J1MAX=J2+J1RG2-IFP2
J1CNJ=J3+J2MAX+J2STP-J2
DO 697 J1=J2,J1MAX,IFP2
K=1+J1-I3
DATA(J1)=WORK(K)

DATA(J1+1)=WORK(K+1)
IF(J1=J2)697,697,696
696 DATA(J1CNJ)=WORK(K)
DATA(J1CNJ+1)=WORK(K+1)
697 J1CNJ=J1CNJ-IFP2
698 CONTINUE
IF=IF+1
IFP1=IFP2
IF(IFP1=NP1)700,700,610
    
```

C
C COMPLETE A REAL TRANSFORM IN THE 1ST DIMENSION, N EVEN, BY CON-
C JUGATE SYMMETRIES,
C

```

700 GO TO (900,800,900,701),ICASE
701 NHALF=N
N=N+N
    
```

```
THETA=-TWOPI/FLOAT(N)
IF(ISIGN)703,702,702
702 THETA=-THETA
703 SINTH=SIN(THETA/2.)
WSTPR=-2.*SINTH*SINTH
WSTPI=SIN(THETA)
WR=WSTPR+1.
WI=WSTPI
IMIN=3
JMIN=2*NHALF-1
GO TO 725
710 J=JMIN
DO 720 I=IMIN,NTOT,NP2
SUMR=(DATA(I)+DATA(J))/2.
SUMI=(DATA(I+1)+DATA(J+1))/2.

DIFR=(DATA(I)-DATA(J))/2.
DIFI=(DATA(I+1)-DATA(J+1))/2.
TEMPR=WR*SUMI+WI*DIFR
TEMPI=WI*SUMI-WR*DIFR
DATA(I)=SUMR+TEMPR
DATA(I+1)=DIFI+TEMPI
DATA(J)=SUMR-TEMPR
DATA(J+1)=-DIFI+TEMPI
720 J=J+NP2
IMIN=IMIN+2
JMIN=JMIN-2
TEMPR=WR
WR=WR*WSTPR-WI*WSTPI+WR
WI=TEMPR*WSTPI+WI*WSTPR+WI
725 IF(IMIN=JMIN)710,730,740
730 IF(ISIGN)731,740,740
731 DO 735 I=IMIN,NTOT,NP2
735 DATA(I+1)=-DATA(I+1)
740 NP2=NP2+NP2
NTOT=NTOT+NTOT
J=NTOT+1
IMAX=NTOT/2+1
745 IMIN=IMAX-2*NHALF
I=IMIN
GO TO 755
750 DATA(J)=DATA(I)
DATA(J+1)=-DATA(I+1)
755 I=I+2
J=J+2
IF(I=IMAX)750,760,760
760 DATA(J)=DATA(IMIN)-DATA(IMIN+1)

DATA(J+1)=0.
IF(I=J)770,780,780
765 DATA(J)=DATA(I)
DATA(J+1)=DATA(I+1)
770 I=I+2
J=J+2
IF(I=IMIN)775,775,765
775 DATA(J)=DATA(IMIN)+DATA(IMIN+1)
```



```

5      DATA(J+1)=0.
6      IMAX=IMIN
7      GO TO 745
8      780  DATA(1)=DATA(1)+DATA(2)
9      DATA(2)=0.
10     GO TO 900

C
C      COMPLETE A REAL TRANSFORM FOR THE 2ND OR 3RD DIMENSION BY
C      CONJUGATE SYMMETRIES,
C
800    IF(I1RNG=NP1)805,900,900
805    DO 860 I3=1,NTOT,NP2
        I2MAX=I3+NP2-NP1
        DO 860 I2=I3,I2MAX,NP1
            IMIN=I2+I1RNG
            IMAX=I2+NP1-2
            JMAX=2*I3+NP1-IMIN
            IF(I2=I3)820,820,810
810    JMAX=JMAX+NP2
820    IF(IDIM=2)850,850,830
830    J=JMAX+NP0
        DO 840 I=IMIN,IMAX,2
            DATA(I)=DATA(J)

            DATA(I+1)=-DATA(J+1)
840    J=J-2
850    J=JMAX
        DO 860 I=IMIN,IMAX,NP0
            DATA(I)=DATA(J)
            DATA(I+1)=-DATA(J+1)
860    J=J-NP0
C
C      END OF LOOP ON EACH DIMENSION
C
900    NP0=NP1
        NP1=NP2
910    NPREV=N
920    RETURN
        END
    
```

ROUTINES CALLED:
 MAX0 , FLOAT , COS , SIN

OPTIONS =/ON,/OP:3

BLOCK LENGTH
 FOURT 3472 (015440)*

COMPILER ----- CORE
 PHASE USED FREE
 DECLARATIVES 00622 14690
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User's Guide

File Structures

Vita

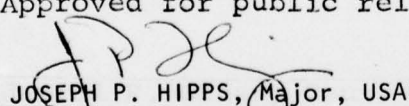
Dennis A. McGaugh was born on November 9, 1947 in Eugene, Oregon. He graduated from South Eugene High School in 1966. After spending three years at Oregon State University, he was drafted into the Army in 1969. He received basic and advanced infantry training at Ft. Ord, California and then entered Infantry Officer's Candidate School at Ft. Benning, Georgia where he graduated in November 1970, and was commissioned a Second Lieutenant in Military Intelligence. During his first assignment at NSA, Ft. Meade, Maryland, he attended the John Hopkins University, Baltimore and graduated in September 1973 with a Bachelor of Science in Mechanical Engineering. His next assignment was to USASA Field Station, Korea, where he served as the operations officer of the 146th ASA Aviation Company from October 1974 until November 1975. He then attended the US Army Military Intelligence Officer's Advanced Course at Ft. Huadruca, Arizona before entering the Air Force Institute of Technology in September 1976.

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SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM
1. REPORT NUMBER AFIT/GE/EE/78S-16	2. GOVT ACCESSION NO.	3. RECIPIENT'S CATALOG NUMBER
4. TITLE (and Subtitle) AN INTERACTIVE ANALYSIS PROGRAM FOR A DIGITAL IMAGE PROCESSING LABORATORY	5. TYPE OF REPORT & PERIOD COVERED MS Thesis	
	6. PERFORMING ORG. REPORT NUMBER	
7. AUTHOR(s) Dennis A. McGaugh Capt USA	8. CONTRACT OR GRANT NUMBER(s)	
9. PERFORMING ORGANIZATION NAME AND ADDRESS Air Force Institute of Technology (AFIT/EN) Wright-Patterson AFB, Ohio 45433	10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS	
11. CONTROLLING OFFICE NAME AND ADDRESS	12. REPORT DATE September 1978	13. NUMBER OF PAGES 66
	15. SECURITY CLASS. (of this report) UNCLASSIFIED	
14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office)	15a. DECLASSIFICATION/DOWNGRADING SCHEDULE	
	16. DISTRIBUTION STATEMENT (of this Report) Approved for public release; distribution unlimited.	
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)		
18. SUPPLEMENTARY NOTES Approved for public release;  1-19-79 JOSEPH P. HIPPS, Major, USAF Director of Information		
19. KEY WORDS (Continue on reverse side if necessary and identify by block number) Image Processing System DICOMED Fourier Transformation(s) IPS Fast Fourier Transformation(s) FFT Linear Image Filtering DFT Power Spectrum IFFT		
20. ABSTRACT (Continue on reverse side if necessary and identify by block number) A FORTRAN program is presented that will interactively prepare digitized images (pictures) for experimental analysis. The digital preparation includes the ability to Discrete Fourier Transform (DFT), Inverse Fourier Transform (IDFT), threshold image power spectral density, and to perform two-dimensional image filtering. Further, a brief discussion of image distortion measurements, optimal image size for experimental		

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20. presentation, and image aliasing is provided. A sample of typical processed image results is also supplied.

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