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A STUDY OF THE CONTRIBUTION OF AIRBLAST-GENERATED SEISMIC WAVES.

9 master's THESIS,

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Richard N. Price Capt USAF

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THE NUCLEAR AIR-SHOCK PRECURSOR:

A STUDY OF THE CONTRIBUTION OF AIRBLAST-GENERATED SEISMIC WAVES

THESIS

Presented to the Faculty of the School of Engineering of the Air Force Institute of Technology

Air University

in Partial Fulfillment of the

Requirements for the Degree of

Master of Science

in

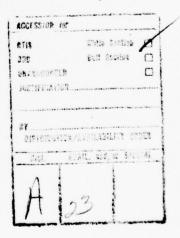
Nuclear Engineering

by

Richard N. Price, B.A. Capt USAF

Graduate Nuclear Engineering

December 1978



#### Preface

This thesis was intended to determine whether airblast energy from an atmospheric nuclear burst could effectively couple into the ground, generate surface seismic signals, and thus independently cause or contribute to the formation of an airshock precursor. The major thrust of the work was to investigate the generation, description, and timing of these surface seismic signals.

Appreciation is extended to Major George Nickel of the AFIT Physics Department for his recognition of an effort worthy of research and for his earnest attempts to teach free thinking and the independent analytical application of the first principles of physics.

Richard N. Price

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#### Abstract

The coupling into the ground of airblast energy from an atmospheric nuclear burst is postulated as a mechanism which may contribute to if not independently cause the observed airshock precursor. A computer model to test the hypothesis is constructed by assuming an elastic ground medium, applying finite difference techniques to the equations of motion, and using the space- and time-varying overpressure from the nuclear burst to induce the seismic motions within the ground.

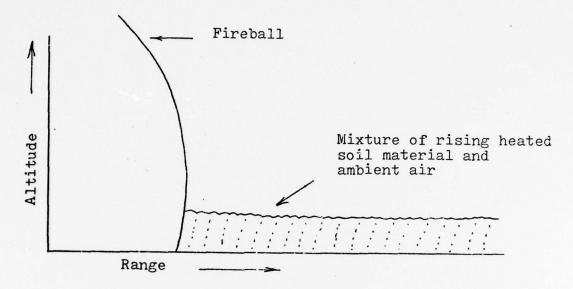
The surface velocities resulting from simulation of a 28 kiloton atmospheric burst at 500 feet height of burst yielded a dust layer ballistically reaching only 0.64 cm at its highest point for the stiff one-layer ground medium, 0.096 cm for the softer one-layer medium, and a negligible height for the more realistic four-layer Frenchman Flats medium. Thus, the airblast-induced precursor as postulated (ballistic rise only) fails to re-create the 2 - 3 meter high dust layers observed in experimental atmospheric nuclear testing. However, the motions are felt to be significant enough to be included in any attempt to model from first principles the precursor and the up-sweep of dust behind the shock front.

#### I. Introduction

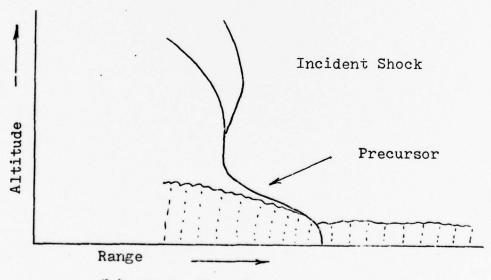
#### Background and Phemonenology

During early atmospheric nuclear weapons testing the effect known as the nuclear airblast precursor was observed. The precursor results from the formation of a heated layer of air immediately above the ground surface. Because the sound speed is higher in this heated air layer, the shock front from the nuclear burst is able to propagate faster in this heated region than in the higher, cooler regions of air. Thus, a "toe" forms on the leading edge of the shock front at its intersection with the ground. This phenomenon is shown pictorially in Figure 1.

A nuclear burst which generates an airblast precursor represents a departure from the shock front shape and shock properties one would expect when a nuclear burst is detonated over an ideally reflecting, non-interacting surface. It is precisely the interaction of a real surface which gives rise to the non-ideal (precursed) properties of the airblast: two overpressure peaks instead of one; peak overpressure reduced up to 50% over ideal; and dynamic pressure increased up to 100% over ideal. The properties of a nuclear blast precursor therefore become of considerable interest when the response of surface and near-surface systems to the static loading of real-world overpressure waveforms and to the enhanced drag loading from the dynamic pressure must be known with reasonable accuracy.



(a) Pre-Shock Thermal Layer



(b) Blast-Wave Precursor

Figure 1. Pictoral Representation of Precursor Phenomenon (Knasel, 1975: 2.15)

The Air Force Weapons Laboratory (AFWL) began to study the precursors observed in actual atmospheric nuclear tests (Table I) in an attempt to

- characterize the development of the heated air layer which is the heart of the precursor;
- 2. model the development of this thermal region; and
- 3. extend this understanding of experimental observations for the relatively low yield experimental nuclear blast precursors (1 to 30 kilotons) to the megaton yields which the defense planner must expect in today's threat environment.

Utilizing considerable internal and contractor expertise from 1973 to the present. AFWL has principally concluded that radiation (primarily X-rays) from the fireball is the mechanism by which the heated air layer (and thus the precursor) is formed. Specifically, if the thermal radiation on the ground is sufficient to heat the soil above a threshold level (which will depend on soil type and soil conditions), ground moisture and hydrated water in the soil will be suddenly and explosively released. Such a violent release will "popcorn" the soil into the air. Once airborne, the dust heats the surrounding air by conduction and convection while continuing to absorb thermal radiation from the fireball. (Ganong, 1978)

Nonetheless, the coupling of airblast energy to the ground has been postulated as another causal mechanism which may contribute to if not independently cause the precursor.

This mechanism has not been previously studied to determine

Table I. Events Studied for Precursor

Shot	Operation (Number)	Yield (Kt)	HOB (ft)	Scaled HOB (ft/Kt <sup>1/3</sup> )	Area at NTS	Туре	Precursor*
POST	Teapot (11)	1.45	300	265	9	Tower	Yes
мотн	Teapot (2)	2.40	300	224	3	Tower	Yes
HORNET	IORNET Teapot (5)		300	196	3	Tower	Yes
TESLA	TESLA Teapot (3)		300	158	9	Tower	Yes
FOX	Tumbler-Snapper (6)	11.5	300	133	4	Tower	?
EASY	Tumbler-Snapper (5)	12.5	300	129	1	Tower	?
HOW	Tumbler-Snapper (8)	13.9	300	125	3	Tower	?
NANCY	Upshot-Knothole (2)	24	300	104	. 4	Tower	?
BADGER	Upshot-Knothole (6)	25	300	103	2	Tower	?
HARRY	Upshot-Knothole (8)	32.3	300	94	2	Tower	?
SIMON	Upshot-Knothole (7)	45	300	84	1	Tower	?
MET	Teapot (12)	22.5	400	142	FF	Tower	Yes
BEE	Teapot (6)	8	500	250	7	Tower	Yes
MORGAN	Plumbbob (30)	8	500	250	9	Balloon	Yes
WILSON	Plumbbob (5)	10.3	500	230	9	Balloon	Yes
KEPLER	Plumbbob (11)	10.3	500	230	4	Tower	No
BOLTZMANN	Plumbbob (2)	11.5	500	222	7	Tower	?
APPLE I	Teapot (8)	14.2	500	206	4	Tower	Yes
SHASTA	Plumbbob (16)	16.5	.500	196	2	Tower	No
WHITNEY	Plumbbob (28)	18.5	500	189	2	Tower	?
ZUCCHINI	Teapot (14)	28	500	1.65	7	Tower	Yes
APPLE II	Teapot (13)	28.5	500	164	1	Tower	Yes
TURK	Teapot (4)	44	500	142	2	Tower	Yes
GRABLE	Upshot-Knothole (10)	15	524	212	FF	Gun	Yes
PRISCILLA	Plumbbob (6)	36.6	700	211	FF	Balloon	Yes
SMOKY	Plumbbob (20)	44	700	198	8	Tower	Yes
WASP PRIME	Teapot (9)	3.2	739	502	7	Air	Yes
LA PLACE	Plumbbob (24)	1.22	750	702	7	Balloon	?
WASP	Teapot (1)	1.2	762	717	7	Air	No
ABLE	Tumbler-Enapper (1)	1	793	793	FF	Air	No
DOG	Tumbier-Snapper (4)	18.5	1040	393	7	Air	Yes
CHARLIE	Buster-Jangle (3)	14	1132	470	7	Air	Yes
CLIMAX	Upshot-Knothole (11)	60	1334	341	7	Air	Yes
DOPPLER	Plumbbob (17)	19.7	1500	631	7	Balloon	?
NEWTON	Plumbbob (26)	11.8	1500	659	7	Balloon	?
STOKES	Plumbbob (14)	19	1500	562	7	Balloon	?

(Liner, 1975: 22)

its relative contribution to the heated air layer which precedes and determines the precursor formation.

The airblast-generated precursor contribution as postulated would occur in the following sequence (Figure 2): the airblast strikes the ground, coupling energy into the ground and generating seismic-like displacements; the displacement waveforms propagate into the ground along the soil surface with velocities characteristic of the seismic velocities of the ground medium. As the radius of the airshock increases, the peak overpressure at the shock front decreases and the airshock subsequently slows. When the seismic surface wave velocity exceeds the velocity of the advancing airblast, these seismic surface disturbances will outrun the airshock and are for the first time able to contribute to the thermal layer formed ahead of the shock. For this contribution to be of concern, the surface disturbances must be sufficiently large to impart a sizable vertical velocity to the dust/soil particles lying loosely on the ground, causing these loose particles to rise ballistically above the ground. One additional requirement is that sufficient energy must remain in the fireball to heat the rising dust particles. The heated dust can then heat the surrounding air by conduction and convection as in the case of the thermally-induced soil blowoff. Early heating from the fireball will practically assure the presence of loose, dry soil at the ground surface. As in the case of thermally-induced soil blowoff, the airblast-

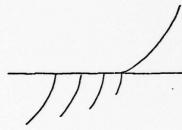
# Figure 2. <u>Pictoral Representation of Airblast-Induced Precursor</u>



a. Airblast strikes ground at T<sub>o</sub>; Fireball heats ground surface.



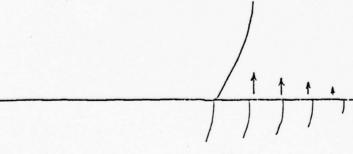
b. Airblast expands along surface; Seismic waves radiate into ground and along surface but move slower than front of airshock.



c. Seismic waves are now able to outrun airblast, imparting an upward velocity to dust particles on the surface;

\*

Injected dust particles absorb fireball radiation and heat the surrounding air by conduction and convection.



induced contribution will also be yield, height of burst, and soil condition dependent.

#### Purpose

The documentation which follows details the approach that was undertaken to model any airblast-generated contribution to the heated air layer which precedes the precursor. As such, it presents computations of seismic surface displacements, seismic surface velocities, and anticipated airborne dust layers. This research is intended to be used to determine whether further, more exact modeling is warranted on the role of airblast energy couples into seismic waves as a contributor to the nuclear precursor.

#### Scope

The computational model to simulate ground motions developed as a product of this thesis research is applicable to any problem which involves pressure or stress loading normal to the surface of an elastic half-space for which order of magnitude answers are desirable. However, the problems for which ground motion results are presented are limited to atmospheric nuclear test events. This work does not investigate thermal energy transport or hydrodynamics within the rising dust layer.

### Order of Presentation

The order of presentation will be as follows:

Chapter II describes the computational model (preliminary analysis, equations of motion, finite difference equations, surface pressure, treatment of boundary displacements, and method of solution); Chapter III discusses output calculated from the model (stability, transmitting boundary, and simulation of an atmospheric nuclear burst); and Chapter IV concludes whether the seismic surface waves generated by the airblast make significant contributions to the precursor and recommends improvements or new approaches for the model.

#### II. Computational Model

#### Preliminary Analysis

The heart of the airblast precursor is the formation of a heated air layer immediately above the ground. The postulated means through which seismic signals can contribute to this thermal layer is by the injection of dust/soil particles into the air, these particles subsequently absorbing fireball radiation.

The height h to which a dust particle would rise ballistically above the surface (ignoring hydrodynamics and drag) is independent of its mass and is given by

$$h = \frac{v^2}{2g} \quad (cm),$$

where v = the particle's vertical velocity, and g = the gravitational acceleration.

Clearly then, the driving force involved in testing this postulated causal mechanism is to calculate an order of magnitude value for the vertical velocity of the dust/soil particles, or equivalently, the peak vertical velocity of the ground surface. The single greatest assumption made is that satisfactory values can be obtained through a treatment of the soil as an elastic half-space.

This assumption is put into perspective through consideration of research conducted by the U. S. Army Corps of Engineers. Since 1971 computations and data analyses have simulated and reconstructed seismic motions resulting from

high explosive and nuclear test events. This work indicates that while soils are not truly elastic media, two-dimensional elastic wave propagation calculations can be performed with comparative ease and require only limited soil property data relative to inelastic, non-linear calculations. Also, it was felt that elastic calculations were less subject to numerical errors. (Hadala, 1973: 297, 383)

In addition, one particular set of computations compiled by the Army Corps of Engineers revealed that for peak overpressures in the 100 to 50 psi range, the elastic soil model generally yielded maximum velocities less than those given by the inelastic model. However, the reverse was true in the 50 to 1 psi range. In other related calculations a similar but different overpressure crossover point was also found. Generally then, these results imply that the elastic model subsequently used to approximate the vertical velocities of the dust particles will underestimate these velocities if outrunning of the airshock by the seismic signal occurs at the high end of the peak overpressure region and will overestimate them if outrunning occurs in the low overpressure region. (Hadala, 1973: 295)

After first assuming an elastic medium, an estimate through one-dimensional analysis can be made of the maximum surface vertical velocity in a uniform media. This is derived in Appendix A and is given by

$$\frac{d s_z}{dt_{\text{max at } z=0}} = \frac{P_o}{\rho_{\text{ground}}} v_c \quad (\text{cm/sec}), \quad (1a)$$

where  $S_z = displacement in the z-direction,$ 

P<sub>o</sub> = peak overpressure on the surface at the point of interest,

ground = density of the ground, and

V<sub>c</sub> = compressional seismic velocity of the ground.

The peak overpressure  $P_o$  along the surface is a function of yield and height of burst; and the compressional seismic velocity  $V_c$  is a function of the seismic constants (Lame constants  $\lambda$  and  $\mu$ ) and density of the ground. Therefore, the maximum vertical velocity with which dust can be injected into the air will also be dependent upon the yield, height of burst, and seismic properties of the ground.

Another important consideration - the ground range at which the seismic signal will begin to outrun the airshock - will also have the same dependency as above. In order to obtain a preliminary estimate of where this "outrunning" will occur, it is first assumed that there is an average velocity  $V_{ave}$  with which the sperical shock expands. With this assumption it is shown in Appendix G that the apparent velocity with which the airshock advances along the ground surface can be expressed as

$$V_{app} = \begin{cases} V_{ave}^2 \\ \frac{1 - \frac{H^2}{H^2 + r^2}} \end{cases}$$
 (cm/sec) (1b)

where H = height of burst, and r = ground range.

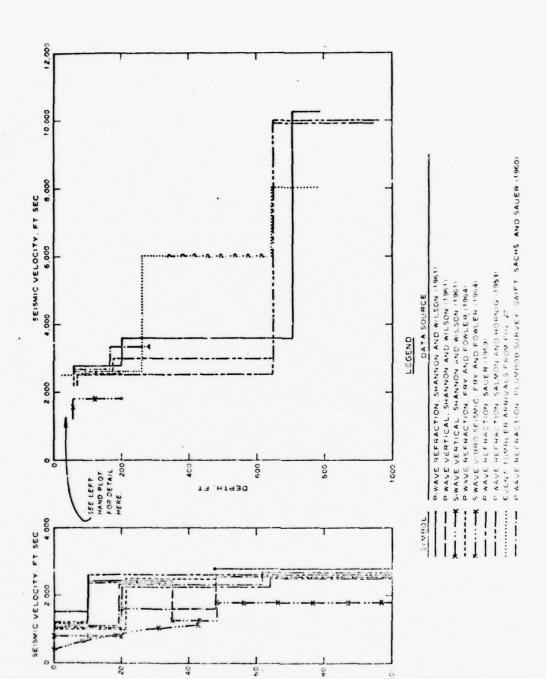
When this velocity  $V_{app}$  slows to the seismic velocity  $V_{c}$ , the seismic signal thus created at the intersection of the shock front and ground will outrun the airshock.

However, the surface seismic disturbances having the largest magnitude are known to be Rayleigh waves which travel more slowly than  $V_c$ . So, solving Equation 1b for r when  $V_{app} = V_{Rayleigh}$ , yields that ground range at which outrunning of seismic Rayleigh waves will occur. This is given by

$$r \geq \left\{ \frac{H^2}{\left[\frac{V_{\text{Rayleigh}}}{V_{\text{ave}}}\right]^2 - 1} \right\}^{\frac{1}{2}} \quad \text{(cm or ft).}$$

Consider the case of a 30 kiloton burst detonated at 500 feet, also where  $V_{\rm ave}=2.4~{\rm km/sec}$  (eight times the sound speed in sea-level air) and  $V_{\rm Rayleigh}=2.5~{\rm km/sec}$ . Then, Rayleigh outrunning begins to occur at a ground range of  $r=0.52~{\rm km}=1714~{\rm ft}$ . From blast data curves it is found that at that ground range the peak overpressure will be  $P_{\rm o}\cong 40~{\rm psi}$  and that the time of arrival of the airshock will be TARR  $\cong 0.15~{\rm sec}$ . Thus the maximum vertical velocity (Equation 1a) is 2.6 cm/sec and 50 percent of the fireball radiation has yet to be emitted. (Glasstone, 1977: 111, 121, 309-310)

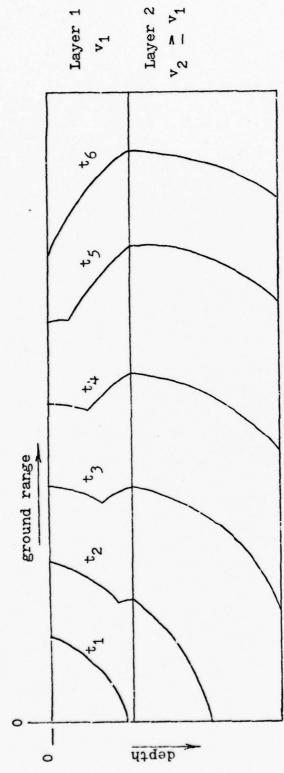
While Equations 1a and 1b were derived for a uniform elastic medium, peak velocities occurring in a layered elastic medium are also of interest because ground motion data and



Summary of Seismic Velocity Data for Frenchman Flats (Hadala, 1973: 103) Figure 3.

T3 H1930

0



This figure depicts the propagation of a seismic wave. By time to the disturbance at the ground surface is being caused by the refracted/reflected signal from the lower, seismically faster layer.

Phenomenological Effect of a Layered Ground Medium (Hadala, 1973: 145) Figure 4.

Frenchman Flats at the Nevada Test Site consist of horizontal layers which vary with depth in density and characteristic seismic velocities (Figure 3). Because elastic property data for the medium at Frenchman Flats are known and atmospheric nuclear tests displaying an airblast precursor were conducted there, the layered medium of this site will provide a "real-world" problem with which to test the postulate of the airblast generated precursor.

Figure 4 depicts the phenomological effect of a two-layered ground medium. Typically, because of the effects of weathering, pressure from the overburden, and some degree of cementation, deeper layers will be seismically "stiffer" (read less compressive) and possess a higher characteristic seismic propagation velocity. Thus, once a disturbance reaches a stiffer layer it will propagate more quickly than a disturbance in an above layer. This will ultimately cause the seismic signal to outrun the airblast at the ground surface earlier than would have occurred had the material consisted solely of material with seismic properties of the upper layer.

One other important effect of layering in the medium is that the stress transmitted into the lower layer can be greater than the stress incident on the interface from above. The transmitted and reflected stresses have been derived from one-dimensional analysis in Appendix B and are given by

$$\sigma_{t} = \frac{2}{\frac{\rho_{1}^{C_{1}}}{\rho_{2}^{C_{2}}} + 1}$$

and

$$\sigma_{\rm r} = \frac{\frac{\varphi_2^{\rm C}_2}{\varphi_1^{\rm C}_1} - 1}{\frac{\varphi_2^{\rm C}_2}{\varphi_1^{\rm C}_1} + 1} \sigma_{\rm i}$$

where  $\rho_j$  = density of layer j, and  $c_j$  = seismic velocity of layer j.

For a stiffer lower layer, density  $f_2$  and seismic velocity  $C_2$  will be larger than  $f_1$  and  $f_2$  of the upper layer. Thus the transmitted stress will be greater than and of the same type (tensile or compressive) as the incident stress. Therefore, if the energy attenuation resulting from spatial expansion of the seismic signal is not greater than the gain in stress achieved, the stress transmitted to the second layer which is then later re-transmitted back into the upper layer can be greater than the original incident stress, thereby resulting in seismic displacements greater than in the single-layered medium.

#### Equations of Motion

Armed with a knowledge of the seismic phenomenology and the parameters upon which it depends, the next step is to generate the equations which govern the motion of the ground medium under airblast loading. Cylindrical geometry is chosen due to the axial symmetry of the advancing airblast

shock front.  $S_r$  and  $S_z$  are defined to be the displacements in the radial and vertical directions, respectively. of a given point within the ground medium about its equilibrium point. The displacement  $S_e$  in the e-direction is zero because of the problem symmetry.

The equations of motion are given by

$$\frac{\partial^{2} s_{r}}{\partial t^{2}} = \frac{\partial}{\partial r} - \frac{2\mu}{r} \frac{\partial \overline{\psi}_{z}}{\partial \theta} + 2\mu \frac{\partial}{\partial z} \frac{\overline{\psi}_{\theta}}{\partial z}$$
(2)

$$\frac{\partial^{2} s_{z}}{\partial t^{2}} = \frac{\partial}{\partial z} - \frac{2\mu}{r} \frac{\partial}{\partial r} (r \overline{\omega}_{\theta}) + 2\mu \frac{\partial \overline{\omega}_{r}}{\partial \theta}$$
(3)

where 
$$\Delta = \frac{1}{r} \frac{\partial (rs_r)}{\partial r} + \frac{1}{r} \frac{\partial s_{\theta}}{\partial \theta} + \frac{\partial s_z}{\partial z} , \qquad (4)$$

and 
$$2 \overline{\omega}_{\theta} = \frac{\partial s_{r}}{\partial z} - \frac{\partial s_{z}}{\partial r} \qquad (5)$$

The boundary conditions which apply are that the stress at the surface z=0 in the vertical direction is just the overpressure P(r,t) which acts normal to the surface.

$$\sigma_{zz} = \lambda \Delta + 2\mu \epsilon_{zz} = -P(r,t)$$

$$(6)$$

where

$$\epsilon_{zz} = \frac{\partial s_z}{\partial z}$$

and that no tangential stress exists at the surface. (Kolsky: 195: 55)

$$C_{rz}$$
  $= 0 = \mu \left( \frac{\partial s_r}{\partial z} + \frac{\partial s_z}{\partial r} \right)$  (7)

#### Finite Difference Equations

The technique of finite differencing was chosen to solve the equations of motion primarily due to the ease and speed with which the equations could be implemented and solved on a digital computer. The equations were evaluated at the time-space mesh point i,j,n, where the finite difference mesh is described in Figure 5 and

$$s_r(r_i,z_j,t_n) = s_r(i\Delta r, j\Delta z, n\Delta t) = s_{r_i,jn}$$

A straight-forward application of central differences yields for  $\mathbf{S}_{\mathbf{r}}$ ,

$$\frac{\left.\frac{\partial^{2} S_{r}}{\partial t^{2}}\right|_{i,j,n}}{\left.\frac{1}{\varphi_{i,j,n}}\left\{\frac{\partial}{\partial r}\left[-\left(\frac{\partial S_{r}}{\partial r} + \frac{\partial S_{z}}{\partial z}\right)\right]\right\}\right.$$

$$+ 2\mu \frac{\partial^{S_{r}}}{\partial r} + (\lambda + 2\mu) \frac{S_{r}}{r} + \mu_{i,j,n} \frac{\partial}{\partial z} \left( \frac{\partial^{S_{r}}}{\partial z} + \frac{\partial^{S_{z}}}{\partial r} \right)_{i,j,n}$$

Or,

$$\frac{S_{r_{i,j,n+1}} - 2S_{r_{i,j,n}} + S_{r_{i,j,n-1}}}{\wedge t^2}$$

$$= \frac{1}{\rho_{i,j}} \left\{ \frac{\lambda_{i+\frac{1}{2},j} \left( \frac{\partial S_r}{\partial r} + \frac{\partial S_z}{\partial z} \right)_{i+\frac{1}{2},j,n}}{\Delta r} \right.$$

$$\frac{\lambda_{i-\frac{1}{2},j} \left( \frac{\partial S_r}{\partial r} + \frac{\partial S_z}{\partial z} \right)_{i-\frac{1}{2},j,n}}{\Delta r}$$

$$\Delta r$$

+ 
$$2 \mu_{i+\frac{1}{2},j} \left(\frac{\partial s_r}{\partial r}\right)_{i+\frac{1}{2},j,n} - 2 \mu_{i-\frac{1}{2},j} \left(\frac{\partial s_r}{\partial r}\right)_{i-\frac{1}{2},j,n}$$

$$\Delta r$$

+ 
$$\frac{(\lambda_{i+\frac{1}{2},j} + 2 \mu_{i+\frac{1}{2},j})(\frac{s_r}{r})_{i+\frac{1}{2},j,n}}{\Delta_r}$$

$$-\frac{(\lambda_{i-\frac{1}{2},j} + 2 \mu_{i-\frac{1}{2},j}) \left(\frac{s_r}{r}\right)_{i-\frac{1}{2},j,n}}{\Delta r}$$

$$+ \mu_{i,j} \left[ \left( \frac{\partial s_{r}}{\partial z} + \frac{\partial s_{z}}{\partial r} \right)_{i,j-\frac{1}{z},n} - \left( \frac{\partial s_{r}}{\partial z} + \frac{\partial s_{z}}{\partial r} \right)_{i,j+\frac{1}{z},n} \right] \right\}.$$
(8)

Because central differences were employed, the scheme will be accurate to second order in  $\Delta t$ ,  $\Delta r$ , and  $\Delta z$ . The centering grid is given in Figure 6.

Similar implementation of the finite differencing for the  $S_{\mathbf{z}}$  displacement and the boundary conditions causes Equations 3, 6, and 7 to become

$$\frac{S_{z_{i,j,n+1}} - 2 S_{z_{i,j,n}} + S_{z_{i,j,n-1}}}{\Delta t^2}$$

$$\frac{1}{\varphi_{i,j}} \left\{ \begin{array}{c} \lambda_{i,j-\frac{1}{2}} \left( \begin{array}{c} \frac{\partial S_r}{\partial r} + \frac{\partial S_z}{\partial z} \right)_{i,j-\frac{1}{2},n} \\ & \Delta_z \end{array} \right.$$

$$\frac{\lambda_{i,j+\frac{1}{2}} \left( \frac{\partial S_r}{\partial r} + \frac{\partial S_z}{\partial z} \right)_{i,j+\frac{1}{2},n}}{\Delta_z}$$

$$+ \frac{2 \mu_{i,j-\frac{1}{2}} \left(\frac{\delta s_{z}}{\delta^{z}}\right)_{i,j-\frac{1}{2}} - 2 \mu_{i,j+\frac{1}{2}} \left(\frac{\delta s_{z}}{\delta^{z}}\right)_{i,j+\frac{1}{2}}}{\Delta^{z}}$$

$$+ \frac{(\lambda + 2\mu)_{i,j-\frac{1}{2}} \left(\frac{s_{r}}{r}\right)_{i,j-\frac{1}{2},n} - (\lambda + 2\mu)_{i,j+\frac{1}{2}} \left(\frac{s_{r}}{r}\right)_{i,j+\frac{1}{2},n}}{\Delta^{z}}$$

$$\mu_{i+\frac{1}{2},j}\left(\frac{\partial s_{r}}{\partial z} + \frac{\partial s_{z}}{\partial r}\right)_{i+\frac{1}{2},j,n} - \mu_{i-\frac{1}{2},j}\left(\frac{\partial s_{r}}{\partial z} + \frac{\partial s_{z}}{\partial r}\right)_{i-\frac{1}{2},j,n}$$

$$\Delta_{r}$$

$$-\frac{\mu_{i,j}}{r_{i}} \left(\frac{\delta^{s_{r}}}{\delta^{z}} - \frac{\delta^{s_{z}}}{\delta^{r}}\right)_{i,j,n}$$
(9)

Figure 5. <u>Definition of Finite Difference Mesh</u>

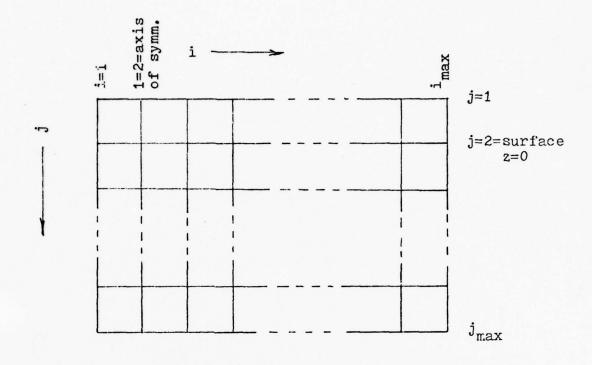
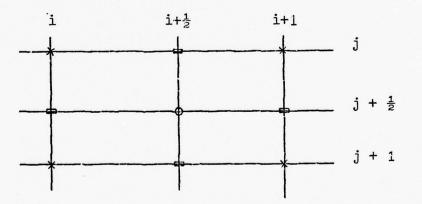


Figure 6. Centering Grid for the Finite Difference Equations



x are known values;  $\Rightarrow$  are intermediate calculated values; o is the final calculated value

$$\frac{\partial^{S_z}}{\partial^z}\bigg|_{z=0} = \frac{S_{z_{1,1,n}} - S_{z_{1,3,n}}}{2 \Delta^z}$$

$$= -\frac{1}{(\lambda + 2\mu)_{i,2}} \left\{ \lambda_{i,2} \left( \frac{\delta s_r}{\delta r} + \frac{s_r}{r} \right)_{i,2,n} + P(r,t) \right\}$$
(10)

and

$$\frac{\partial^{S_r}}{\partial^{z}}\bigg|_{z=0} = \frac{S_{r_{i,1,n}} - S_{r_{i,3,n}}}{2 \Delta^{z}}$$

$$= -\frac{\partial S_{z}}{\partial r}\Big|_{z=0} = \frac{S_{z_{i-1,2,n}} - S_{z_{i+1,2,n}}}{2\Delta r}.$$
 (11)

Because the displacement values at time n and n-1 will be zero until airshock arrival, the only unknowns in Equations 8-11 are the time advanced (n+1) values. Thus, the scheme as chosen is a second-order accurate, explicit algorithm.

#### Surface Pressure

Finally, before implementation on the computer the surface pressure input P(r,t) is required. Because scaled near-proximity of the bursts to the ground is necessary to achieve an airblast precursor, surface effects upon the over-pressure have to be considered. The blast data curves in Glasstone's, The Effects of Nuclear Weapons were taken as reference data because of his inclusion of ground effects.

For the typical overpressure waveform shown in Figure 7, the following parameters are required: time of arrival TARR, peak overpressure PEAKP, duration of the positive overpressure phase TPLUS, and the rate of decay of pressure with time.

General algorithms were found for TARR and derived for the rate of decay of the pressure with time. The first is given as follows (Liner, 1975: 1972-3):

TARR = 
$$\frac{0.54291 \text{ Y} - 21.185 \text{ r}_{s} \text{ Y}^{2/3} + 361.8 \text{ r}_{s}^{2} \text{Y}^{1/3} + 2383 \text{ r}_{s}^{2}}{\text{Y}^{2/3} + 2.048 \text{ r}_{s} \text{ Y}^{1/3} + 2.6872 \text{ r}_{s}^{2}}$$

where

TARR is in msec.

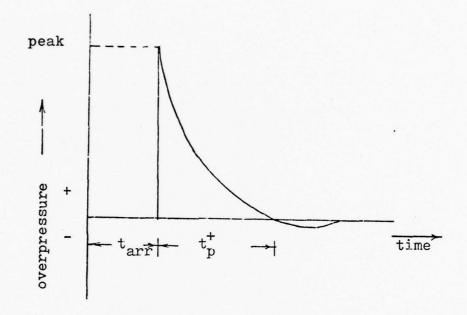
Y = weapon yield in kilotons, and

 $r_s$  = slant range in kilofeet.

For a surface burst

TARR (HOB = 0) = TARR (2Y,  $r_s$ ).

Figure 7. Typical Overpressure Waveform (Glasstone, 1977: 84)



tarr = arrival time of shock front

t<sup>+</sup><sub>p</sub> = duration of positive pressure phase

(negative pressure phase will be ignored in this model) For a non-surface burst, the free air arrival time is used in the regular reflection region and a linear interpolation between free air and surface burst values is made in the Mach reflection region.

TARR = TARR(Y,r<sub>s</sub>), for 
$$\frac{\text{HOB}}{\text{ground range}} \ge 1$$
;

= TARR(Y,r<sub>s</sub>) \*  $\frac{\text{HOB}}{\text{ground range}}$  +

TARR(2Y,r<sub>s</sub>) \*  $(1 - \frac{\text{HOB}}{\text{ground range}})$ , for  $\frac{\text{HOB}}{\text{ground range}} \le 1$ .

The second parameter, decay of overpressure with time, is given by

$$\frac{P(TAU)}{PEAKP} = 1 - \left[ 1 - (1 - TAU)^{m} \right]^{1/m}$$

where
$$TAU = \frac{t - TARR}{TPLUS}, \text{ and}$$

$$m = 1 + .382 (ln PEAKP)$$

$$- .136 (ln PEAKP)^2 + .025 (ln PEAKP)^3$$

The computational algorithm for TARR was originally derived by Brode and that for P(t) was derived by applying curvefitting techniques (Appendix C) to the Glasstone data for overpressure decay. (Glasstone, 1977: 100)

At the time of computer implementation no suitable, general algorithms had been found for PEAKP and TPLUS. The

technique chosen, then, was to fit the Glasstone data for these parameters by linear segmentation for each specific problem simulated. This aspect, while speeding initial implementation, adds significant awkardness when applying the code to various burst problems. A minor improvement was achieved by calculating the pressure as a function subprogram. For differing events the unique overpressure function can be validated independently and then appended to the main program. (Glasstone, 1977: 111-115, 119)

#### Treatment of Boundary Displacements

The two stress components on the surface (the normal stress defined by the overpressure and the identically zero tangential stress) provide the calculational means to derive the displacements at the top boundary of the finite difference mesh. These were given analytically by Equations 6 and 7 and in finite difference form by Equations 10 and 11.

Symmetry is the key by which the displacements at the lefthand mesh boundary are found. Because ground zero is the symmetry axis, displacements immediately to either side are considered equal. By averaging these mirrored displacements, the displacements at the lefthand mesh boundary or ground zero are found and are equal to those just averaged.

Finally, the righthand and bottom mesh displacements must be defined. The simplest choice is to apply rigid boundaries; that is, the displacements there remain zero. One particularly annoying property of such a treatment is that reflection of seismic signals occurs at these rigid boundaries.

This trait becomes particularly restrictive when attempting to compare model output data to published late-time seismic motions from test data and independent elastic calculations.

Interference of reflected signals can be prevented. Two computationally easy choices can readily be implemented: increase the mesh size or stop the computation before any reflected signal can reach the point of interest.

Increasing the mesh size can be done by increasing the spatial mesh increments, thereby losing accuracy, or by increasing the computer memory requirements of the calculation. Stopping the computation before reflection can affect the motion of the point of interest can, as in late-time motion, result in shutdown before significant motion has occurred at the point of interest.

Another choice which is more difficult computationally is to develop a transmitting boundary; that is, a boundary which acts as nearly as possible as though a semi-infinite region of material exists beyond the mesh boundary. If successfully accomplished, a seismic signal can be transmitted across the boundary with no reflection; and, the mesh could be kept resonably compact, yet still yield acceptably accurate results.

The nature of the airblast-induced precursor requires that surface seismic motions be computed over a ground range which is long in comparison to the ground depth of interest. As a result a relatively shallow mesh grid is used. Because reflections from the bottom of the mesh would therefore occur

first, the bottom mesh boundary was chosen for the application of the transmitting boundary.

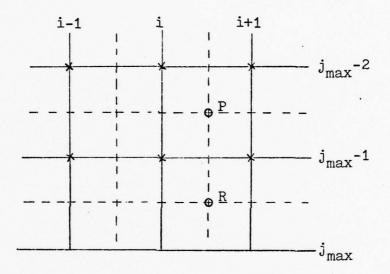
The requirement upon such a boundary is that it must act as a one-way valve. This one-way action can be accomplished by permitting a seismic disturbance incident upon the boundary from above to pass out of the mesh and disappear into the imaginary half-space below while simultaneously preventing the return of reflected signals into the mesh.

The means by which this action will be performed is based upon a momentum flux argument. Consider the mesh as it exists in Figure 8 near the bottom boundary. At the points marked with the symbol X, the displacements  $S_r$  and  $S_z$  are known. From these displacements, calculations of velocities, spatial derivatives, and stress components can be made for the point P centered at  $i+\frac{1}{2}$  and JMAX-3/2.

The stress component  $\mathcal{O}_{ZZ}$  represents the flux of z-momentum in the z-direction, and component  $\mathcal{O}_{TZ}$ , the flux of r-momentum in the z-direction. A properly constructed transmitting boundary permits the net outward flow of momentum. However, it prevents the net inward flow of momentum because this results in the undesirable increase of momentum within the finite difference computational grid.

Therefore, if the proper flow of momentum is indicated at point P (Appendix D presents the derivation of the logic table and equations for the transmitting boundary), this momentum is allowed to flow across the boundary (level JMAX-1) by equating the stress at point P to that at point R centered across the

Figure 8. Finite Difference Mesh Grid Near Bottom Boundary



boundary at  $i+\frac{1}{2}$  and JMAX- $\frac{1}{2}$ . If the conditions indicate improper flow of momentum, the stress components at R are set to zero. Next, displacements along level j=JMAX are calculated from the centering scheme, where the displacements at the lower right-hand corner of the mesh are zero and the computational march is executed along the j=JMAX level from i=IMAX-1 to i=3.

Of course, a trade-off does exist when using such a transmitting boundary. This is that momentum transferred out of the mesh is lost and can play no part in the elastic rebound of the medium. For airblast-induced seismic motions this limitation is expected to occur far too late to be of concern.

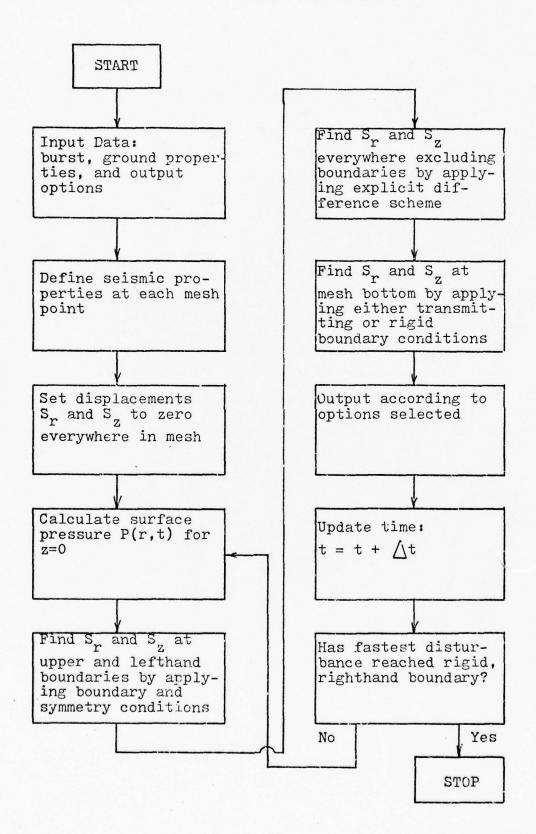
### Method of Solution

The explicit, second-order finite difference scheme derived earlier involves two known time levels (n-1 and n) and three known spatial levels in both the radial (i-1, i, i+1) and vertical (j+1, j, j-1) directions. The task is then to calculate the unknown, time-advanced (n+1) values for all the spatial mesh points of interest. Figure 9 presents as a flow chart the method by which the computational model solves the equations of motion.

Data characterizing the burst, ground medium, finite difference mesh parameters, and output options are first input. An array describing the ground properties within the mesh is constructed. Next, the overpressures on the ground surface are calculated and used by the boundary condition equations. These equations give the displacements at the uppermost boundary of the finite difference mesh, and the symmetry condition is used to find the displacements at the leftmost boundary. Utilizing the main difference equations for the seismic displacements and marching through the spatial mesh, the displacements are found for each mesh point except at the righthand and bottom boundaries.

No displacements are calculated at the righthand boundary because a rigid boundary condition is used. For the bottom, either a rigid boundary condition or a transmitting boundary condition based on a momentum transfer argument is applied (Appendix D). All of the desired time-advanced displacements throughout the mesh have not been calculated.

Figure 9. Method of Solution



Finally, the output format chosen by the input options is executed, and the process is repeated, beginning with an advanced time and updated surface pressure.

This iterative process continues until the desired shutdown time is reached. Typically, this shutdown time is chosen as the time of first arrival of seismic waves at the righthand rigid boundary. Thus, unwanted, artificial reflections are prevented.

### III. Code Calculations

### Stability

One of the prime questions arising when using any finite difference scheme is whether the scheme is stable. The artificial, non-physical inaccuracies introduced by the presence of instability are governed by the choice of time step  $\triangle t$  and grid element sizes  $\triangle r$  and  $\triangle z$ .

Two different stability criteria were initially speculated to be applicable to this model. The first,  $\mathrm{St}_1$ , was set forth by the Army Corps of Engineers investigators as applicable to two-dimensional finite difference calculations of ground shock which outruns the airblast. This condition was presented as the Courant, Fredricks, and Levy stability requirement, namely, (Hadala, 1973: 42)

$$\Delta t \leq \frac{\Delta x}{\sqrt{2} v_{\text{max}}}$$
 (sec).

where  $\Delta t = time step$ ,

 $\Delta x$  = spatial mesh increment =  $\Delta r = \Delta z$ , and

V<sub>max</sub> = maximum disturbance propagation velocity.

The second stability criterion,  $\operatorname{St}_2$ , was based on the physical argument that no disburbance should be allowed to propagate a distance greater than the mesh spacing  $\Delta r$  or  $\Delta z$  in one time step  $\Delta t$ . Mathematically, this is given as

$$\Delta t \leq \frac{\Delta x}{v_{\text{max}}}$$
 (sec) .

In order to determine which of the two preceding stability conditions in fact apply to this model, an experimental stability analysis was conducted. Figures 10-12 present the results of this stability analysis. This analysis consisted of making several runs with the computer model to calculate a ground shock problem. All runs are the same except that the time step has been changed in each run. The time step for each run is shown in relation to both stability criteria,  $St_1$  and  $St_2$ . While some far-field oscillations appear for  $\Delta t = .002$  sec (which exceeds the stability criterion  $St_1$  set forth by Hadala), the solution has not become unstable. Instead, this indicates that the stability condition is being approached. Further enlargements of the time step show that the less restrictive, physically-derived condition,  $St_2$ , should be applied as the stability limitation to the difference scheme of this model.

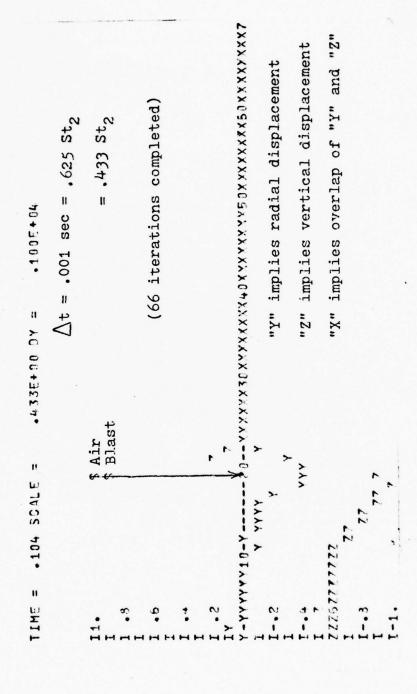


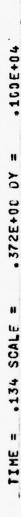
Figure 10. Stability Analysis, 1 Msec Time Step

LXXXXXXXX 5 XXXXXXXX G SXXXXXXXXX G 5 ---"X" implies overlap of "Y" and "Z" "Z" implies vertical displace-ment "Y" implies radial displace-ment = .433 St<sub>2</sub>  $\Delta t = .001 \text{ sec} = .625 \text{ St}_1$ (96 interactions completed) .100E+04 .36EE+00 DY = Air Blast .134 SCALE = 22222222 TIME = 7.-I -.2 1-.8

Figure 10. Cont. . .

"Z" implies vertical displace-ment "Y" implies radial displace-ment = .865 St2 "X" implies overlap of "Y" and "Z"  $\Delta t = .002 \text{ sec} = 1.23 \text{ St}_1$ (33 iterations completed) .100E+04 .410E+00 DY = Air Blast TIME = .104 SCALE = 222 2

Figure 11. Stability Analysis, 2 Msec Time Step



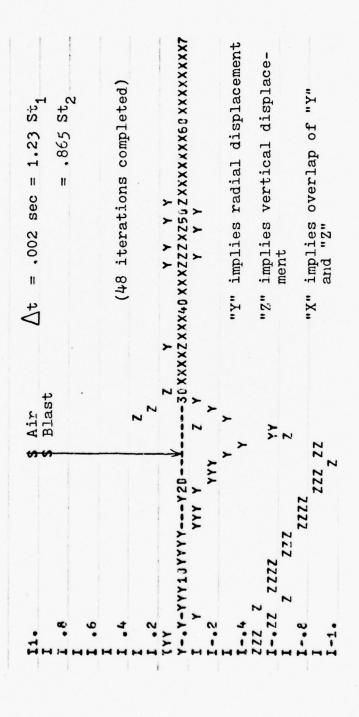


Figure 11. Cont. . .

.100E+04 •163E+13 DY = TIME = .105 SCALE =

 $\Delta_{t} =$ S Air S Blast

= 1.08 St<sub>2</sub> .0025 sec = 1.53 St<sub>1</sub>

(27 iterations completed)

"Y" implies radial displacement

"Z" implies vertical displacement

"X" implies overlap of "Y" and "Z"

Stability Analysis, 2.5 Msec Time Step Figure 12.

I-1.Z

"X" implies overlap of "Y" and "Z" "Z" implies vertical displacement "Y" implies radial displacement  $= 1.08 \text{ St}_2$ (39 iterations completed)  $\Delta$ t = .0025 sec = 1.53 St<sub>1</sub> .202E+20 DY = .100E+04 \$ Air \$ Blast TIME = .135 SCALE =

Figure 12. Cont. . .

### Transmitting Boundary

Figures 13-16 present a comparison of surface seismic motions computed by the computer model. Three different but related problems are represented. One is a "standard" employing a rigid bottom boundary and 100 by 25 mesh grid for comparison with the results obtained using a transmitting boundary. The second differs from the "standard" only by using a transmitting bottom boundary. Lastly, the third employs a transmitting bottom boundary and a reduced 100 by 10 mesh grid. However, the mesh spacing in the third run is the same as in the standard. The purpose of this third run is to test whether the transmitting boundary as constructed would permit the execution of a problem with a reduced number of mesh points while faithfully reproducing the results obtained with a larger number of grid points.

The first and second runs are identical (Figures 13 and 14) until just after t=.4161 when the close-in waveform and magnitudes change slightly. These changes reasonably coincide with the earliest possible arrival at the surface (t=.4166) of a bottom reflected signal in Run #1. As would be expected the surface displacements after t=.4266 are more negative in Run #2 in which reflection has been prevented. Table II shows the surface vertical displacements for mesh point (i=13, j=2) from Run #1 (standard, rigid bottom boundary) in comparison with Run #2 (transmitting boundary) in which reflection has been prevented.

But, unlike the encouraging results obtained with Run #2, Run #3 deviates from the "standard" at an earlier time than is expected from computing the earliest possible arrival time of a bottom-reflected signal, with the surface displacements becoming significantly larger. This result casts a shadow of uncertainty over the validity of the transmitting boundary being utilized.

.100E+04, 11 .199E-01, DY(CM) .3441, SCILE(CM) = TIME(SEC) =

Air

"Y" implies radial displacement

"Z" implies vertical displacement

Computations with Model to Test Operation of the Transmitting Boundary - "Standard" with Rigid Bottom Boundary Figure 13.

\* \* \* \*

1,3



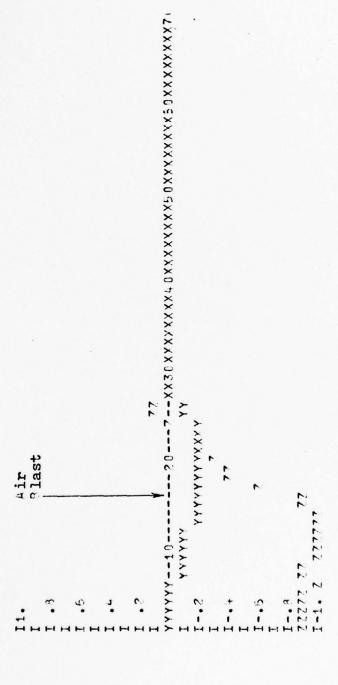


Figure 13. cont . .

.100E+04, .212E-01, DY(CM) = .4341, SCALE (CM) = TIME(SEC) =

last I-.2 7 -- I 27 22

Figure 13. cont...

.100E+04, .199E-01, NY (CM) = .3441, SCALE(CM) = TIME(SEC) =

(

"Z" implies vertical displacement "Y" implies radial displacement lir last \* \* \* 1 - 0 - I 1-.8 Model to Test Operation of the Transmitting Mesh with Bottom Transmitting Boundary Computations with Boundary - 100x25 Figure 14.

.10 0E+0%, .229E-01, 0 (CM) = .4151, SCALE(OM) = TIME(SEC) =

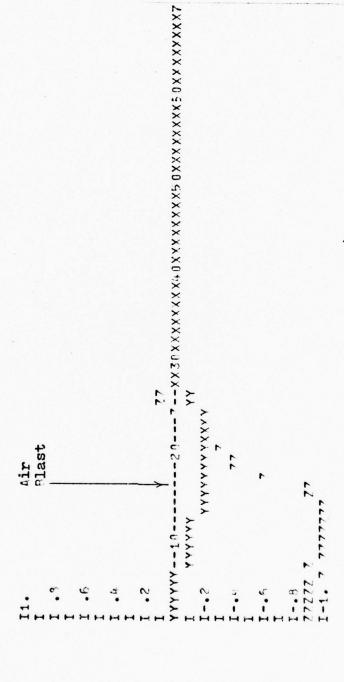


Figure 14. cont . .

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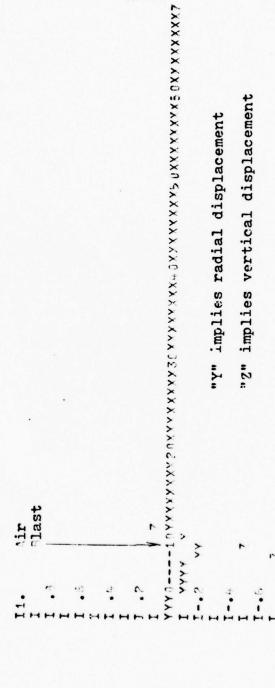
0

Air Alast 11111 I 1-.5 77.8

Figure 14. cont . . .

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Computations with Kodel to Test Operation of the Transmitting Boundary - 100x10 Kesh with Bottom Transmitting Boundary Figure 15.

B -- I

.100E+04, \*\* .1025+00, DY(CM) TINE(SEC) = .4151, SCALE(CM) = \*\*\*\*\* hir Tast \*\*\*\*\* \*\*\* 9.-I

(

0)

Figure 15. cont . . .

.100E+04, .113E+00, DY(CM) = TIME (SEC) = . 4201, SPILE (CM) = dir dast 2.- H \*\*\* 1-.4 1-.6 1-.6

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Figure 15. cent . .

Table II. <u>Comparison of Surface Seismic Motions - Rigid</u>
<u>Versus Transmitting Bottom Boundaries</u>

Surface Vertical Displacements at Mesh Point (i=13, j=1)

Time (sec)	Standard w/rigid Boundary (cm)	100x25 Mesh with Transmit. Boundary (cm)	100x10 Mesh with Transmit. Boundary (cm)
0.311	0.0	0.0	0.0
0.350	0.021	0.021	0.022
0.375	-0.017	-0.017	-0.015
0.400	-0.023	-0.023	-0.040
0.425	-0.023	-0.023	-0.050
0.450	-0.018	-0.025	-0.060
0.475	-0.009	-0.030	-0.061
0.500	-0.003	-0.004	-0.012

## Simulation of a 28 Kiloton Atmospheric Burst

With the preceding analysis completed, the model is next used to simulate the airblast-induced ground motions from an atmospheric burst. A yield of 28 kilotons is chosen, with detonation occurring at a height of burst of 165 feet. This height of burst is intermediate to those for events in Table I detonated at Frenchman Flats and displaying an airshock precursor. Appendix F gives the subroutine which calculates the airblast parameters on the ground for this event.

The seismic reactions of four different ground media are compiled in the tables which follow. This compilation results from the use of the computer model with rigid right-hand and bottom boundaries. From run to run, only the ground medium over which the burst is assumed to occur is changed. These four ground media are described in Figure 16.

The resulting maximum upward surface velocities are given in Tables III-V. These velocities were obtained by differentiation of the vertical surface displacements computed with the model. No maximum velocities are given for Run #4 which simulated the Frenchman Flats test site because all upward velocities were less than 0.1 cm/sec and considered insignificant. Failure of this layered medium to produce the enhanced velocities indicated as possible in Appendix B is apparently due to the presence of the very slow upper layer where the seismic velocity is only slightly greater than the sound speed in ambient air.

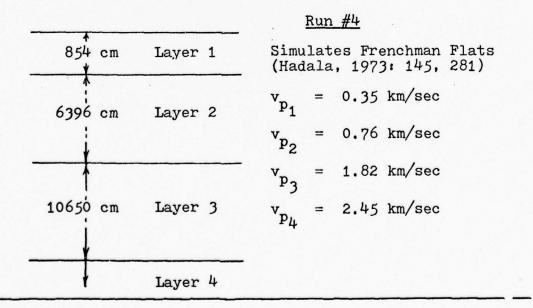
# Figure 16. Ground Media for Model Simulation of 28 Kiloton Event

uniform medium  $v_{p} = 1.22 \text{ km/sec}$   $\lambda = 1.14\text{E10 dynes/cm}^{2}$   $\mu = 1.14\text{E10 dynes/cm}^{2}$   $\rho = 1.9 \text{ gm/cm}^{3}$ 

uniform medium  $v_{p} = 1.82 \text{ km/sec}$   $\lambda = 3.70\text{E10 dynes/cm}^{2}$   $\mu = 1.49\text{E10 dynes/cm}^{2}$   $\theta = 2.0 \text{ gm/cm}^{3}$ 

Figure 16. Cont. . . .

# Run #3 $v_{p_1} = 0.35 \text{ km/sec}$ $\psi_{1} = 1.7 \text{ gm/cm}^{3}$ $\lambda_{1} = 1.16E9 \text{ dynes/cm}^{2}$ $\mu_{1} = 4.68E8 \text{ dynes/cm}^{2}$ $v_{p_2} = 1.82 \text{ km/sec}$ $\psi_{2} = 2.0 \text{ gm/cm}^{3}$ $\lambda_{2} = 3.70E10 \text{ dynes/cm}^{2}$ $\mu_{2} = 1.49E10 \text{ dynes/cm}^{2}$



Mesh point i	9	2	8	6	10	11	12	13	14	15	16
Maximum upward surface velocity	0	0	0	1.3	0.0	0,	2.2	7, 7	α,	6.7	200
T1, time of max velocity (sec)		1		0455	1 10	0 41 4	1 10	1 .	2690	060	טטעע
T2, time of airblast arrival (sec)	.0407	70.	2440.	.0403		0537	0575 0618		5990	.0716	
% of fireball energy emitted prior to T1	1			, r		~ 1	~		V 2	~	
% of fireball energy emitted in (T2-T1) sec.	1	. 1	1	۸ 1	۸ 1	۸ 1	۸ 1	۸ 1	, 1	, r	, r
11											
Wesh point i	17	18	19	20	21	22	23	77	25	26	27
Maximum upward surface velocity (cm/sec)	11.0	13.0	11.3	13.7	13.0	11.7	10.7	12.0	10.0	10.0	0.6
time	.0815	.0875	.0935	2660.	.1055	.1115	.1175	.1235	.1325	.1385	.1475
T2, time of airblast arrival (sec)	.0832	.0885	.0939	.0997		.1125	1195	1268	.1346	.1427	1511
% of fireball energy emitted		~3		\ 5			9 <b>~</b>	~ ~	o 1	0 1	~ 11
% of fireball energy emitted in (T2-T1) sec	1	۸ 1	۸ 1	۸ 1	< 1	۸ 1	V	~ 1	Å 1	۸1	1

Surface Velocity Data in Varied Ground Media - Run #1 Table III.

Mesh point i	28	29	30	31	32	33	-	
Maximum upward surface velocity (cm/sec)	9.0	8.3	7.7	7.0	5.7	4.7		
T1, time of max velocity (sec)	.1565	.1625	.1715	.1805	.1895	.1985		
T2, time of airblast arrival (sec)	.1599	.1691	.1786	.1884	.1986	.2091		
% of fireball energy emitted prior to T1	~ 15	~ 17	~ 18	~ 20	~ 21	~ 22		
% of fireball energy emitted in (T2-T1) sec.	~ 2	~ 1	~ 1	~ 2	2 ~	~ 5		
Mesh point i								
Maximum upward surface velocity								
T1, time of max velocity (sec)								4
T2, time of airblast arrival								
% of fireball energy emitted								
% of fireball energy emitted in (72-71) sec								

Table III. Cont. . . .

2 8			6	10	11	12	13	14	15	16
0.0.16	0.16		2.8	2.3	4.1	4.7	8.6	12.2	16.7	27.6
0.043	043	land and the second	.0485	.0485	.0515	.0545	.0605	.0635	3690.	.0755
.0407 .0425 .0447	7440		.0473	.0503	7.620.	.0575	.0618	.0665	.0716	.0772
	ŀ		۸	۸ ۲	~ 1	<b>~</b>	V V	2 V	- 2	.3
	۸		۸	۸ 1	۸ 1	7	۸	۸ 11	٧	۸ ۲۱
		//								
18 19	19		20	21	2.5	23	<b>村</b> 君	25	56	27
32.4 32.1	32.1		35.3	35.1	34.2	32.9	33.3	33.0	29.8	27.6
0815 .0875 .0935	093	2	.0995	.1055	.1115	.1175	.1235	.1295	.1355	.1415
.0885	093	0	2660.	.1059	.1125	.1195	.1268	.1346	.1427	.1511
~ 3	1	4	- 5	~ 5	~ 5	9 ~	- 7	~ 10	~ 11	~ 12
\ 11 \			۸	۸ 1	V .	~1	~ 1	~1	~1	~ 1

Surface Velocity Data in Varied Ground Media - Run #2 Table IV.

Mesh point i	28	29	30	31	32	33	34	35	36	37	38
Maximum upward surface velocity (cm/sec)	23.0	20.1	18.0	17.3	16.3	15.2	14.9	14.2	13.4	13.0	13.3
	.1475	.1535	.1595	.1655	.1715	.1775	.1865	.1925	.1985	.2045	.2105
T2, time of airblast arrival (sec)	.1599	.1691	.1786	.1884	.1986	.2041	.2199	.2311	.2425	.2543	4992
% of fireball energy emitted prior to T1	~ 12	~ 15	-17	. 17	- 18	~19	~ 21	~ 22	~ 22	~ 23	~ 23
% of fireball energy emitted in (T2-T1) sec.	~ 2	~ 2	~ 2	7 ~	<b>1</b>	~ 3	17 (	4-	6~	6 ~	~ 10
Mesh point i	39	70	41	77							
Maximum upward surface velocity (cm/sec)	10.5	10.2	10.7	10.2							
time ocity	.2195	.2255	.2285	.2345							
T2, time of airblast arrival (sec)	.2788	.2915	4408.	.31.76							
% of fireball energy emitted	~ 25	~ 28	~ 35	~ 32							
% of fireball energy emitted in (T2-T1) sec	~10	~ 11	~13	~ 13							

Table IV. Cont. . . .

Mesh point i	9	7	8	6	10	11	12	13	14	15	16
	0	0	0	0.22	0.14	0.37	0.38	0.79	1.10	1.30	2.76
T1, time of max velocity (sec)	-	;	1	.0455	.0485	.0515	.0545	.0575	.0635	5690.	.0755
T2, time of airblast arrival (sec)	.0407	.0425	2440.	.0473	.0503	7650.	.0575	.0619	.0665	.0715	.0772
	1	1	1	V	۸ 1	<b>√</b>	<b>√</b>	<b>v</b>	~ V	1 2	~ 3
% of fireball energy emitted in (T2-T1) sec.	1	.	£	۸ 4	۸ 1	۸ 1	V	٧ ٢	۸ 1	۸	۸
11											
Mesh point i	17	18	19	20	21	22	23	77	25	26	27
Maximum upward surface velocity (cm/sec)	3.30	3.30	3.7	4.5	4.9	4.34	4.5	8.0	7.7	8.4	14.2
T1, time of max velocity (sec)	0815	.0875	.0935	.0995	.1055	.1115	.1175	.1265	.1325	.1445	.1505
	.0832	.0885	.0939	7660.	.1059	.1125	.1195	.1268	.1346	.1427	.1511
% of fireball energy emitted	~ 3	~ 3	<b>†</b> ~	~ 5	~ 5	~ 5	9 ~	8	6 ~	~ 13	~15
% of fireball energy emitted in (T2-T1) sec	<b>₹</b>	. 1	< 1	۸ 1	۸ 1	۸ ۲	~ 1	$\sim 1$	\ \ \ 1	-	۸1

Surface Velocity Data for Varied Ground Media - Run #3 Table V.

0

Wesh point i	28	29	30	31	32	33	75	35	36	37	38
Maximum upward surface velocity	16.3	17.8	17.8	16.2	15.3	13.7	12.2	11.2	10.3	9.7	9.1
T1, time of max velocity (sec)	.1595		.1775	1 10		1985	.2015		.2165	2195	2285
T2, time of airblast arrival (sec)	.1599	.1691	.1786	.1884		.2041	.2199		.2425	.2543	1992
% of fireball energy emitted prior to T1	- 17	~ 18	- 19	~20	~ 22	~ 22	~ 23	~ 23	42 ~	~ 25	~ 32
% of fireball energy emitted in (T2-T1) sec.	٧	. v	~ 1	~1	~ 2	~ 1	~ 2	11 -	~3	~ 5	8 ~
VI											
Wesh point i	39	017	41	742							
Maximum upward surface velocity (cm/sec)		8.0	7.3	7.1							
T1, time of max velocity (sec)	.2315	.2375	.2435	.2495							
T2, time of airblast arrival (sec)	.2788	.2915	4408.	.3176							
% of fireball energy emitted	~ 32	~-33	~ 33	~ 34		•					-
% of fireball energy emitted in (T2-T1) sec	- 7	8 ~	~ 10	~ 10							

Table V. Cont. . . .

(Page intentionally left blank)

The stiff, uniform ground medium used in Run #2

produced the greatest vertical velocities. While initially

appearing to conflict with Equation (1), this result is

apparently due to the ability of the stiffer medium to trans
mit signals ahead of the airblast which were created

"upstream" at higher overpressures, while these same signals

are not able to outrun the airblast in the slower, more

compressible medium of Run #1. Another factor is the

ability of a stiffer medium to more readily transmit the higher

frequency disturbances. These higher frequency components may,

in part, explain the larger vertical velocities.

Because the heating from the fireball which any rising dust receives is of interest in creating the thermal layer which determines the precursor, Tables III-V also give data pertinent to the fireball radiation emission. Significant amount of fireball heating can be received by rising dust only when the difference between T1, the time of occurrence of maximum upward surface velocity, and T2, the time of airblast arrival, is sizeable. This will only occur when the seismic signal is able to substantially outrun the airblast. Such substantial outrunning is not reflected in the Tables III-V because the upward velocities continue to diminish with increasing ground range.

Dust layers created ballistically would reach a maximum height of only 0.096 cm for Run #1, 0.64 cm for Run #2, 0.16 cm for Run #3, and a negligible height for Run #4.

#### IV. Conclusions and Recommendations

#### Conclusions

Accuracy requirements, interference from artificially reflected signals, and computer storage limitations together prevented the comparison of results obtained with this model (rigid righthard and bottom mesh boundaries) with the available published data. The data on-hand consisted of independent, elastic calculations of late-time, airblast-induced ground motions and of late-time seismic motion data from actual test events.

Prevention of the artificially reflected signals and reduction of the computer storage requirements would have permitted this comparison. Application of the transmitting boundary condition constructed to accomplish the above two goals yielded indefinite results at best. This uncertainty in whether the transmitting boundary condition was properly constructed prohibited its use in validating the model against the independent data.

Thus, the model remains unvalidated, and data derived from it must be viewed accordingly. Nonetheless, it appears that several general conclusions can be made.

First, the surface velocities resulting from simulation of a 28 kiloton atmospheric burst at 500 feet height of burst yielded a dust layer ballistically reaching only 0.64 cm at its highest point for the stiff one-layer ground medium, 0.096 cm for the softer one-layer medium, and a negligible height for the more realistic four-layer Frenchman Flats medium. These heights are

significantly less than the two to three meter high dust layers known to exist prior to airshock arrival. Therefore, it must be concluded that as postulated (ballistic rise only) the airblast is not likely to significantly contribute to the precursor.

However, the magnitude of upward vertical velocities computed indicate that the seismic motions of the ground surface can be significant and should be considered in any modeling of thermal layer precursor generation. In particular, the seismic ground motions can alter the velocity with which dust is injected into the air by another causal mechanism such as the thermally-induced soil blow-off mechanism researched by AFWL. Only when another causal mechanism can be shown to occur sufficiently in advance of the arrival of the seismic signals to preclude the interaction of the two mechanisms does it appear that the airblast effect can be ignored.

In addition, AFWL modeling of the thermally-induced soil blow-off indicates that the injection velocity of the particles can range from 50 to 200 cm/sec without significantly altering the height of the dust layer computed by their model. At the maximum injection velocity of 200 cm/sec, the dust would ballistically rise only 20 cm—not the 2-3 meters found experimentally. This indicates that thermal radiation transport and hydrodynamics is the more dominant force lifting the dust particles. Redefining the airblast/seismic model to include these two effects may well result in airblast-induced thermal layers more nearly in agreement with experimental data. Or stated another way, the

key factor may be to begin the soil particles in an upward motion whereby the thermal radiation transport, hydrodynamics, and Taylor instabilities dominate to lift the soil to the significant heights of several meters. The role of airblast-induced vertical motions in the precursor formation certainly warrants further research. (Prentice, J., 1976: 13)

Finally, velocities imparted to the surface dust before and after arrival of the airshock may have considerable effect upon the amount of dust swept up as the airshock passes. This airborne dust would be expected to have significant impact upon the dynamic pressure and the erosive ability of the airshock.

#### Recommendations

Recommendations for further work with the computer model developed as an adjunct of this thesis research include:

- the further search of published literature in an effort to find early-time seismic motion data with which the rigid boundary model may be validated;
- 2. the further search of published literature to find one or more suitable, generalized algorithms for peak overpressure and positive pressure phase duration; such algorithms would eliminate the requirement of generating a new surface pressure function for each new problem computed;
- 3. the further study, analytical development, and construction of a transmitting boundary; if successful, this work can have wide applications in this simulation as well as other models using a fixed finite difference mesh;
- 4. refinement of the model to confidently give arrival time data of the airblast-induced seismic motion.

Recommendations for further work on the airblast-induced precursor include:

- 1. the study of experiemental data to give time of occurrence of the thermal layer for comparison with seismic signal arrival times in order to determine whether the airblast-induced seismic signals arrive too late to significantly contribute to the thermal layer; and
- 2. if the above investigation reveals that the arrival of the seismic signals is not too late, incorporation of thermal radiation transport and hydrodynamics into the model.

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#### Appendix A

## One-Dimensional Estimate of the Maximum Vertical Velocity

Suppose that  $S_x$ , the displacement of a particle in the ground, can be expressed as a wave-like disturbance propagating in the x-direction with velocity c.

$$S_{x} = f(t-c/x)$$
 (A-1)

The displacement S<sub>X</sub> then satisfies the wave equation.

This, of course, must be the case as stress within an elastic solid is known to be a generalized form of Hooke's Law.

(Kolsky, 1953: 8)

This one-dimensional stress can be expressed as the following (Newmark, N., 1962: C-9)

stress 
$$\sigma_{\rm x} = \int c^2 \frac{\delta S_{\rm x}}{\delta x} = \int c^2 \frac{\delta f(t-x/c)}{\delta x}$$
 (A-2)

where  $\varphi$  is the density of the solid medium.

Differentiating the function f yields

$$\sigma_{x} = \int c^{2} \frac{\partial f(t-x/c)}{\partial x} = \int c^{2} \frac{\partial f(t-x/c)}{\partial (t-x/c)} \frac{\partial (t-x/c)}{\partial x}$$

$$= -\int c \frac{\partial f(t-x/c)}{\partial (t-x/c)}$$

The boundary condition which applies at the surface x=0 is that the stress is equal to the normal loading of the pressure on the surface, or

$$\sigma_{x} \bigg|_{x=0} = -\rho_{c} \frac{\delta_{f(t-x/c)}}{\delta_{(t-x/c)}} \bigg|_{x=0} = -P(t)$$
(A-3)

However, the particle velocity is simply the derivation of the particle displacement with respect to time.

$$V_{X} = \frac{\partial S_{X}}{\partial t} = \frac{\partial f(t-x/c)}{\partial t}$$

$$= \frac{\partial f(t-x/c)}{\partial (t-x/c)} \frac{\partial (t-x/c)}{\partial t} = \frac{\partial f(t-x/c)}{\partial (t-x/c)} \tag{A-4}$$

Substituting for  $\frac{\delta}{\delta(t-x/c)}$  in Equation (A-3) gives

$$- c \rho v_{x} \Big|_{z=0} = -P(t)$$

or.

$$v_{x} |_{z=0} = \frac{P(t)}{\varphi_{c}}$$

The particle velocity is a maximum when the loading pressure is a maximum. Finally,

$$\left[\begin{array}{c|c} v_x & \\ z=0 \end{array}\right]_{max} = \frac{P_o}{\varphi_c}$$

#### Appendix B

# Effect of Ground Medium Layering on Stress (Newmark, 1962: C-13-C-15)

Given the following two-layered ground medium:

where  $\rho_i$  is the density of the ith layer, and  $c_i$  is the seismic velocity of the ith layer.

If an elastic medium is assumed then the displacement of a particle within this solid must obey the wave equation,

$$\frac{\partial^2 S_x}{\partial t^2} = - C^2 - \frac{\partial^2 S_x}{\partial x^2}$$

Solutions to the wave equation take the form

$$S_x = f(t-x/c) + g(t+x/c)$$

where f(t-x/c) represents a wave traveling in the positive x-direction, and

g(t+x/c) represents a wave traveling in the negative x-direction.

Now consider a disturbance incident upon the interface between the two layers, namely,

$$S_x = f(t-x/c)$$

The stress incident upon the interface is given by

$$\sigma_{x_{incident}} = f_1^{c_1^2} \frac{\partial S_x}{\partial x} = -f_1^{c_1} \frac{\partial f}{\partial (t-x/c)}$$
 (B-1)

Let the incident wave or disturbance be expressed as the sum of reflected and transmitted components.

$$S_{x_{incident}} = S_{x_{reflected}} + S_{x_{transmitted}}$$

or, alternately,

$$f(t-x/c) = G(t+x/c) + F(t-x/c)$$

From Equation (B-1) the interface condition that the sum of reflected and transmitted stresses must equal the incident stress can be applied.

$$\sigma_{x_{incident}} = \sigma_{x_{reflected}} + \sigma_{x_{transmitted}}$$

or

$$f_{1}^{c_{1}^{2}} \frac{\partial f(t-x/c)}{\partial x} = f_{1}^{c_{1}^{2}} \frac{\partial G(t+x/c)}{\partial x} + f_{2}^{c_{2}^{2}} \frac{\partial F(t-x/c)}{\partial x}$$
(B-3)

Let

R = reflection coefficient = constant in time, and

T = transmission coefficient = constant in time.

such that 
$$G(t+x/c_1) = R f(t-x/c_1)$$
 and  $F(t-x/c_2) = T f(t-x/c_1)$ .

From (B-2), f = Tf + Rf

or,

$$1 - R = T.$$

From (B-1) and (B-3), 
$$\varphi_1 c_1^2 \frac{\partial f}{\partial x} = - \varphi_1 c_1 \frac{\partial f}{\partial (t-x/c_1)}$$

$$= - \varphi_2 c_2 \frac{\partial F}{\partial (t-x/c_2)} + \varphi_1 c_1 \frac{\partial G}{\partial (t-x/c_1)}$$
(B-5)

However,

$$\frac{\partial f(t-x/c)}{\partial t} = \frac{\partial f(t-x/c)}{\partial (t-x/c_1)} \frac{\partial (t-x/c)}{\partial t} = \frac{\partial f}{\partial (t-x/c_1)}$$
(B-6)

Applying (B-6) to Equation (B-5),

$$- \, \mathcal{L}_{1}^{c_{1}} \, \frac{\partial \, f}{\partial t} = - \, \mathcal{L}_{2}^{c_{2}} \, \frac{T}{\partial t} \, + \, \mathcal{L}_{1}^{c_{1}} \, R \, \frac{\partial \, f}{\partial t}$$

Dividing by 
$$\left(-\frac{\rho_1 c_1}{r_1}\right)$$
,
$$1 = \left(\frac{\rho_2 c_2}{\rho_1 c_1}\right) \quad T - R$$

$$1 + R = \left(\frac{\rho_2 c_2}{\rho_1 c_1}\right) \quad T \quad (B-7)$$

Combining (B-4) and (B-7) gives

$$2 = T(1 + \frac{\ell_2^{c_2}}{\ell_1^{c_1}}),$$

Finally,

$$T = \frac{2}{1 + \frac{f_2^c_2}{f_1^c_1}}, \qquad (B-8)$$

and

$$R = \frac{\frac{\varphi_2^{c_2}}{\varphi_1^{c_1}} - 1}{\frac{\varphi_2^{c_2}}{\varphi_1^{c_1}} + 1}$$
 (B-9)

since 
$$G = Rf$$
,  $\frac{\partial G}{\partial t} = R \frac{\partial f}{\partial t}$ 

but

$$\frac{\partial G(t+x/c)}{\partial (t+x/c)} \frac{\partial (t+x/c)}{\partial t} = R \frac{\partial f(t-x/c)}{\partial (t-x/c)} \frac{\partial (t-x/c)}{\partial t}$$

giving

$$\varphi_1^{c_1} = \frac{\partial G}{\partial (t+x/c)} = \varphi_1^{c_1} \quad R = \frac{\partial f}{\partial (t-x/c)}$$

or, equivilently,

$$\sigma_r = R \sigma_i$$
 (B-10)

Similarly,

$$F = Tf$$

$$\frac{\partial F}{\partial t} = \frac{T \partial f}{\partial t} \Rightarrow \frac{\partial F}{\partial (t-x/c_2)} \frac{\partial (t-x/c_2)}{\partial t}$$

$$= T \frac{\partial f}{\partial (t-x/c_2)} \frac{\partial (t-x/c_1)}{\partial t}$$

or,

$$\frac{\partial F}{\partial (t-x/c_2)} = T \frac{\partial f}{\partial (t-x/c_1)}$$

Continuing similar to the derivation for (B-10) gives

$$\mathcal{O}_{\mathrm{T}} = \frac{2}{\frac{f_{1}^{c_{1}}}{\mathcal{P}_{2}^{c_{2}}} + 1} \qquad \mathcal{O}_{\mathrm{i}} \qquad (B-11)$$

Consider what happens if this transmitted stress  $\mathcal{O}_{\mathrm{T}}$  is allowed to be incident upon the interface. The stress transmitted back to the upper layer  $\mathcal{O}_{\mathrm{T}}'$  is given by

$$\sigma_{T}' = \frac{2}{\frac{\varphi_{2}^{c_{2}}}{\varphi_{1}^{c_{1}}} + 1} \qquad \sigma_{T} = \frac{2}{\frac{\varphi_{2}^{c_{2}}}{\varphi_{1}^{c_{1}}} + 1} \left\{ \frac{2}{\frac{\varphi_{1}^{c_{1}}}{\varphi_{2}^{c_{2}}} + 1} \right\} \sigma_{i}$$

$$= \frac{4}{2 + \frac{\varphi_{1}^{c_{1}}}{\varphi_{2}^{c_{2}}} + \frac{\varphi_{2}^{c_{2}}}{\varphi_{1}^{c_{1}}}} \qquad \sigma_{i}$$

If 
$$f_2^{c_2} > f_1^{c_1}$$
, then 
$$\frac{f_2^{c_2}}{f_1^{c_1}} > 1$$
.

Thus,

$$\sigma_{\rm T} = \frac{4}{2 + \frac{\ell_1^{\rm c}_1}{\ell_2^{\rm c}_2} + \frac{\ell_2^{\rm c}_2}{\ell_1^{\rm c}_1}}$$

and 
$$\sigma_{\rm T} \geq \sigma_{\rm i}$$
 for

$$\frac{\ell_1^{c_1}}{\ell_2^{c_2}} + \frac{\ell_2^{c_2}}{\ell_1^{c_1}} < 2$$

#### Appendix C

#### Derivation of Algorithm for Decay of Overpressure with Time

To accurately apply the overpressure on the ground surface requires that its time-dependent behavior be incorporated. Accurate behavior with time is necessary to couple the correct frequency components of the airblast into the ground. To this end, it is undertaken to transform the data contained in Glasstone's, The Effects of Nuclear Weapons, and presented in Figure 17 into an algorithm which could then be incorporated into the computer model.

It is first observed that the data curves are very nearly symmetric about the line indicated in the figure. Next, a "super ellipse" of the following form and centered at the point (1,1) is argued to reasonably fit the curves (Nickel, 1978):

$$(1-x)^m + (1-y)^m = 1$$
 (C-1)

At the symmetry axis chosen, x=y. Or, in this application

$$P(t)/PEAKP = t/t_p^+$$

where P(t) = pressure at time t,

PEAKP = peak overpressure,

t = time measured from arrival of shock
front, and

t<sup>+</sup>p = direction of positive overpressure phase.

At the symmetry axis Equation (C-1) becomes

$$(1-x)^{m} = \frac{1}{2}$$

from which results

$$m = \frac{\ln 2}{\ln (1-x)}$$
 (C-2)

From Figure 17 data and Equation (C-2), the following table results:

PEAKP	$x = t/t_p^+$	1-x	m
20	.35	.65	1.60
100	.27	•73	2.20
200	.21	•79	2.94
1000	.12	.88	5.42

After several trials, the above table data relating PEAKP and m is chosen to be fit by a cubic equation in (1n PEAKP),

$$m = 1 + A * ln PEAKP + B * (ln PEAKP)^2 + C * (ln PEAKP)^3$$
 (C-3)

Three equations are set up using Equation (C-3) and the data table, then solved, giving

$$A = 0.382$$
,

$$B = -0.136$$
, and

$$C = 0.025$$

Knowing m, Equation (C-1) is solved for y yielding

$$y = 1 - \left[ 1 - (1-x)^m \right]^{1/m}$$

or equivalently,

$$\frac{P(t)}{PEAKP} = 1 - \left[ 1 - (1-t/t_p^+)^m \right]^{1/m}$$

The results of using this curve-fitting algorithm are given in Figure 18 for the surface overpressure from a 28 kiloton event at 500 feet height of burst.

Figure 17. Rate of Decay of Overpressure with Time (Glasstone, 1977: 100)

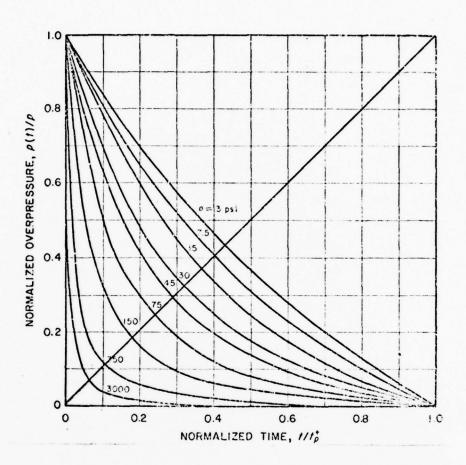


Figure 18. <u>Comparison of Algorithm for</u>
<u>Time-Dependent Overpressure and</u>

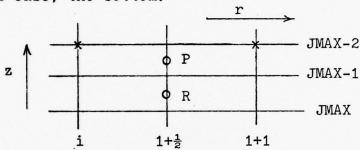
Dia	N IV D	t +	asstone <u>Data</u>   P(t   PEA	) KP
PE	AKP	q <sup>*</sup>	algorithm	Glasstone
1	563	0.071	0.142	0.14
1.	563	0.030	0.017	0.01
	375	0.07	0.31	0.32
	375	0.23	0.12	0.11

#### Appendix D

#### Derivation of a Transmitting Boundary

At a boundary it may be desirable to pass or transport seismic signals through the edge of the mesh as though a semi-infinite expanse of ground material existed beyond that edge. Although several conditions may exist upon which such a "transmitting" boundary can be constructed, an argument based upon momentum transfer is chosen.

Consider the finite difference mesh near such an edge, in this case, the bottom.



Assume that the horizontal level JMAX-1 is the boundary across which seismic signals are desired to be transmitted without reflection. The points marked with the symbol "X" are known. Thus, the stresses  $\mathcal{O}_{ZZ}$  and  $\mathcal{O}_{TZ}$  can be calculated at point P, centered at  $(i+\frac{1}{2}, JMAX-3/2)$ .

The stress  $\mathcal{O}_{zz}$  represents the flux of z-momentum in the z-direction, and  $\mathcal{O}_{rz}$  the flux of r-momentum in the z-direction. A properly constructed transmitting boundary would permit the outflow of positive momentum and the inflow of negative momentum, while preventing the inflow of positive momentum and outflow of negative momentum which result in a net increase in momentum flowing into the finite difference mesh.

The z-momentum density is given by the product  $fV_z$ , and, similarly, the r-momentum density by  $fV_r$ , where  $V_z$  and  $V_r$  are the velocities of the ground particles in the z-direction and r-direction, respectively. Assuming the density f to be constant near the mesh boundary of interest, the positiveness or negativeness of z- and r-momentum can be determined by testing the sign of the  $V_z$  and  $V_r$  velocity respectively.

Then, consider the following:

$$V_z = \frac{dS_z}{dt} = \frac{dS_z}{dz} = \frac{dz}{dt}$$

where S is the displacement of the bround in the z-direction.

Here  $\frac{dz}{dt}$  is assumed to be greater than or equal to zero.

The following logic tables result:

$\left[\begin{array}{c c} \delta S_{z} \\ \hline \delta z \end{array}\right]_{p}$	$\left \sigma_{\mathtt{zz}}\right _{\mathtt{p}}$	indicate reflection ?	action
<b>&gt;</b> 0	> 0	Yes	$\left  C_{zz} \right _{R} = 0$
> 0	< 0	No	$ \sigma_{zz} _{R} =  \sigma_{zz} _{p}$
< 0	<b>&gt;</b> 0	No	$ \mathcal{O}_{zz} _{R} =  \mathcal{O}_{zz} _{p}$
< 0	<b>&lt;</b> 0	Yes	$\sigma_{zz} = 0$

$\left[\begin{array}{c c} \delta s_r \\ \hline \delta r \end{array}\right]_p$	$\sigma_{rz}$	indicate reflection ?	action
> 0	> 0	Yes	Orz   R = 0
> 0	<b>V</b> 0	No	Orz   R = Orz   P
< 0	> 0	No	$\sigma_{rz} _{R} = \sigma_{rz} _{P}$
< 0	< 0	Yes	$\sigma_{rz} _{R} = 0$

When 
$$\frac{\partial S_z}{\partial z}\Big|_P$$
,  $\frac{\partial S_r}{\partial r}\Big|_P$ ,  $\sigma_{zz}\Big|_P$ , or  $\sigma_{rz}\Big|_P$  is

equal to zero, either action results in the same thing.

Appendix E

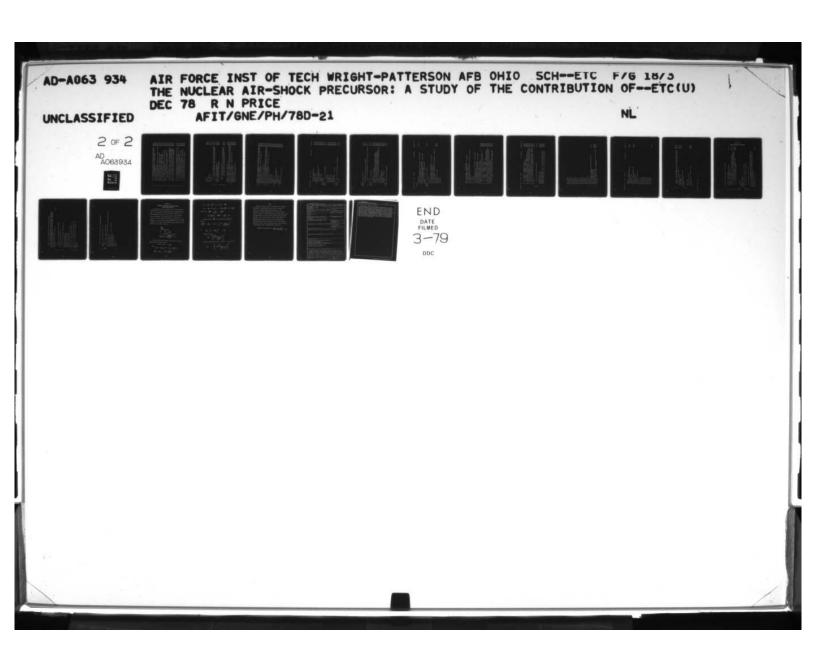
### Listing of Computer Code

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2	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	220 78	2
PROSEAM THERMAL(INPUT,OUTPUT)  IMERSION Y (100,25,3),7 (100,25,3)  IMERSION Y (100),37P (100),C7P (100),DZP (100),P (100)  IMERSION AL(100,21)  IMERSION AL(100)  IMERSION AL(100)  IMERSION LAM(100,25), MU(100,25), RHO(100,25)  EAL LAM,MU,HO3  INTECER RPLOT, 7P_0T	GHN 76 INDICATES GODE GENERATED BY MDJOR GEORGE NICKEL FOR A CARTESION COORDINATE SFISMIC PROBLEM (VALLEY) IN 1978 SHNOTES SLIGHT CHOOSE MADE TO VARIABLES/CONSTANTS IN VICKEL® COOPE	CC RMP 78 INDICATES SOME CHANGES 32 ADDES BY CAPT RICHARD PRICE CONSTRUCTOR TO PERFORM SEISMIC RECOMETANT (PRECURSOR)	INTIAL DATA  SEAD, YIELD, HOS, TZERO, RZERO, PZERO, S, ALAM, AMU, ARHO, DEPTHA, BLAM,  AMU, BRHO, DEPTHS, SLAM, CMU, SRHO, DEPTHS, DAY, DMU, DRHO, DY, DZ, DT, IMAX,  JMAY, TWRITE, JWRITE, IFLAG, JFLAG, RPLOT, FLOT  SRINT 591  DOSMET ("IPROBLEM SEISMIC CONTRIBUTOR TO NUCLEAR AIR GLAST PRECISENT 992, VIELD, 408  FRINT 992, VIELD, 408  DORMET ("O VIELD (MT) ", E10.3," , HEISHI OF BURST(CM) ", E12.5)  PRINT 993, TZERO  (SEC) = ", FS.4)  KINT 994, ZZERO

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WHICH IT IS DESIRED TO STAR	200	
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11, 92HO ARE PROPERTIES IT SECOND SOI	SND	
MICMI, CRHO 4RE PROPERTIES DE THIRE	SND	
4,040,0240 4RE PROPERTIES 3" "DURTH SOIL LAYER	2 2 0	
= RADIAL SELL WINTH : DZ = VERTICAL CEL	SNO	
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ITE IS THE HORIZONTAL MESH LEVEL WAICH IS	SND	
OUTPUT: J=2 IS SURFACE AND J=JMAX IS BOTTOM	SND	
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INT 3JT Y AFRAY WHICH CORRESPON	SNP	
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LAST = 1 NOW = 2 NEXT = 3 TMM = IMAX -1 JMM = JMAX - 1 IMAX - 1 IMAX - 3 T = TYPRO	VEL IS SHUTDOWN JECHANISM TO PREVENT REFLECTION FROM RIGHTHAND RN BOUNDRY DE MESH; THUS, WE USE FASTEST SEISMIC VFLOGITY RN	LAMMAX = ATAX1 (ALAM, 3LAM, 5LAM, 5LAM)  MUMAX = AMAX1 (AMJ, 5MU, 5MU)  FHOMEX = AMAX1 (ARHO, 5RHO, 5RHO, 5RHO)  VEL = SORT ((LAMMAX + 2.*MUMAX) /213MAX)	OFFINE SOIL SEISHIC PROPERTIES  LAYERE LOCATION OF DEEPEST MESH VALUE Z WITH PROPERTIES OF A RNI GIVEN SOIL LAYER, 1E-1 TERM SOLVES PROBLEM OCCURRING RNI WHEN OFPIH/OT IS EXACTLY AT SOME LEVEL JEN	LAYEFA = (DEPTHA/DZ - (1.6-4)*DZ) + 2  IF(LAYERO.GE.(JMOX-5)) PRINT 10C0  FORMAT("0 CAUTION *** FIRST LAYER INTERFACE LIES WITHIN OR BELOW RNI S FRICTION REGION: REFLECTION FROM THE INTERFACE MAY BE INHIBITED") RNI IF(LAYEPA.GI.JMAX) PRINT 1009  RNI IF(LAYERA.GI.JMAX) LAYERA=JMAX  LAYEFA1=LAYERA + 1  LAYEFB = (DEPTHA/DZ - (1.6-4)*DZ) + 2  IF(LAYERE.GE.(JMAX-5)) PRINT 10C0  RNI RNI IF(LAYERE.GE.(JMAX-5)) PRINT 10C0
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1050 FORMAT("0 CAUTION **** SECOND LAYER INTERFACE LIFS WITHIN OR BELOW $ FRICTION REGION: REFLECTION FROM THE INTERFACE MAY BE INHIBITED")
IF (LAYERS.GT.JMAX) PRIMT 1098
                                                                                                                FOGMET ("0 CAUTION **** THIRD LAYER INTERFACE LIES WITHIN OR BELOW
                                                                                                                              $ FFICTION REGION: REFLECTION FROM THE INTERFACE MAY BE INHIBITED**)
IF (L/YERC.ST.) MAX) PRINT 1097
                                            :
                                                                                                                                                             :
                                           FORMAT ("0 CAUTION --- SECOND LAYER EXCEEDS MESH DEPTH
                                                                                                                                                            FOFWET ("0 CAUTION --- THIRD LAYER EXCEEDS MESH DEPTH
                                                                                     LAYERC = (DEPTHO/37 - (1.5-4)+07) +
                                                                                                   IF(LAYERS.GE.(J44X-5)) PRINT 1070
                                                        JF (LAYERS. ST. JMAX) LAYERB=JMAX
                                                                                                                                                                         IF (LIYERC . GT . JYAX) LAYFRO = JMAX
                                                                                                                                                                                                                                                                                            IF (LAYERA.SE.JMAX) 50 TO 1110
                                                                                                                                                                                                                                                                                                                                                                               TO 1110
                                                                                                                                                                                                                                                                                                         DO 1102 JELAYERAI, LAYERB
                                                                                                                                                                                                                                                                                                                                                                                30
                                                                                                                                                                                                                                                                                                                                                                               IF (LLYERA GE JMAX)
                                                                       LAYEFF1=LAYER3 + 1
                                                                                                                                                                                        LAYEF C1=LAYEFC + 1
                                                                                                                                                                                                     DO 1116 I=2,1WAY
DO 1100 J=2,LAYERA
                                                                                                                                                                                                                                   LAM(1, J) = ALAM
                                                                                                                                                                                                                                                                                                                        LAM(I,J) = 9LAM
                                                                                                                                                                                                                                                               = AEHO
                                                                                                                                                                                                                                                                                                                                                    RHO (1, J) = BEHO
                                                                                                                                                                                                                                                 40(1,3) = A49
                                                                                                                                                                                                                                                                                                                                     40(1, J) = 8MU
                                                                                                                                                                                                                                                              5HO (1, 1)
                                                                                                                                                                                                                                                                              CONTINUE
                                                                                                                                                                                                                                                                                                                                                                 COMITMUE
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                                                              IF(I/YERS.3E.JMAX) 50 TO 1110
NO 1104 J=LAYERC1, JMAX
LAM(I,J) = DLAM
                                                                                                                             INITIALIZE THE MESH VALUES
                       DO 1103 J=LAYER91,LAYERC
LAM(I,J) = CLAM
0PT=2
                                       40(1,3) = C40
RHO(1,3) = CRH3
CONTINUE
                                                                                              RHO(1, J) = 0340
                                                                                       MU(1, J) = DMU
                                                                                                                                                                                                           R(I) = DY*(I-2)
CONTINUE
                                                                                                                                                                   Y(1, J, 2) = 0

Y(1, J, 3) = 0

Z(1, J, 1) = 0

Z(1, J, 2) = 0

Z(1, J, 3) = 0
                                                                                                                                                     DO 4 J=1, JMAX
                                                                                                                                                             Y(I_{3},i_{3},1) = 0.
                                                                                                                                             PO 4 I=1, I'AX
 74174
                                                                                                      CONTINUE
                                                                                                             1110 CONTINUE
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COTOFC SURFACE PRESSURE	00 6 I=2,14AX P(I) = PRESS(YIELD, 409, T, R(I), RTERD, YYSHOOK)	C YYSHOOK LOCATES THE LEADING EDSE OF SHOOK FRONT ON THE GROUND	6 CONTINUE	SUCTIONS SOUNDERY CONDITIONS	90 7 I=3,14M	IF(?(I),F7,0,) PPINT 1905	1005 FORMIT ("0 R(I) = 0 : MHICH IMPLIES DIVISION BY ZERO")	V(I, 1, NOW) = Y(I, 3, 404) + 02/0 * (Z(I-1, 2, NOW) - Z(I+1, 2, NOM))	7(I,1,400x)=2(I,3,404)-2.* (07/( _34(I,2)+2.* MU(I,2) ))*	1 (F(I)+( LAM(I,2)/(2,*DY))*(Y([+1,2,NDW)-Y(I-1,2,NDW)))	\$ -(Y(I,2,NOW)* LA4(I,2)/(R(I)))*(2,*0Z/( LOM(I,2)+2,* MU(I,2))	7 CONTINUE	00 8 J=1, JMAX	Y(1, J, MOW) =-Y(3, J, MOW)	7(1, J, NOW) = 7(3, J, NOW)		7(2, J, NOM) = 2(3, J, 40M)	8 CONTINUE	COCCCC TETTIAL TAR ETRAI OTERERRICES

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2NP 78
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                                                                                                                                                                                                                                                                                    SHN 78
                                                                                                 RNP 78
                                                                                                                                                                                                                                                                                                                                                                                                                                                   0PZ = (Z(I, J-1, 42) + Z(I+1, J-1, 42) - Z(I, J+1, 42) - Z(I+1, J+1, 3) + Z(I+1, J+1, 3)
FTN 4.6+446
                                                                                                                       AZP(I) = (Y(I+1,J+1,400M) + Y(I+1,J,40M) - Y(I-1,J+1,N0M)
                                                                                                                                                              PZP(I) = (Y(I, J, VOW) - Y(I, J+1, VOA)) / DZ

CPP(I) = (Z(I+1, J, VOW) + Z(I+1, I+1, VOW) - Z(I-1, J, NOW)
                                                                                                                                                                                                                                                                                                                                                                                         - Y(I, J+1, NOW)
                                                                                                                                                                                                                         DZF(I) = (Z(I, J, 40M) - Z(I, J+1, N0A)) / DZ
9 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                     ADZ = (Y(I+1,J,V),V) - Y(I,J,V),NOW) / Y(I+1,J-1,V) = YCZ
                                                                                                                                                                                                                                                                                                                                                                                                                                YCJ((MON), C_1)J(MOM) - Z(I, J(MOM))/DY
                                                                                                                                                                                                      1 - Z(I-1, J+1, NOW)) / (4.*DY)
                                                                                                                                                                                                                                                                                     SNOITANCE ECNERABLIC NITH
                                                                                                                                                                                                                                                                                                                                                                                                             1 -Y (I+1, J+1, NOW)) / (0.*07)
                                                                                                                                         1 - Y(I-1, J, 40W)) /(4. DY)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 IF (R(I), 80.0.) PRINT 1005
  0PT=2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           1 NCW))/(a.+02)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             DO 18 I=3,14M
                                                                                                                                                                                                                                                                                                                                00 10 J=2, JMN
                                                                                                     DO 9 I=3,14N
  11.17
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             245 = ZWS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         547 = 8P7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     AM7 = AP7
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5*( LAY(I,J) + LAM(I-1,J)) + ( 4U(I,J) + MU(I-1,J)))/OY)*
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              +(DT * DT/2HD([, 1)) (((,5*( [14([,3)+ [6M([+1,3))+( MU([,3)+
                                                                                                                                                                                                                                    Z(I, J+1, NOW) - Z(I+1, J+1,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              + 0T*0T/PHO(I, J) * ((( L44(I, J-1) + L44(I, J) ) * (AZM + 07M)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           MU(I, J) 1*(9ZP(I) + CZP(I)))/(2.*D7))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        +FT*07/4H3(I, J) * ((( LA*(I, J) + LAM(I+1, J) ) * (APZ + DoZ)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 LAM(I, J) )*(AZP(I) + DZP(I)))/(2.*DZ)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              - Z(I-1, J, NOW)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   LAM(I, J) + LAM(I-1, J) ) * (AMZ + DMZ)) / (2.* NY)
                                                       - Y(I, J+1, NOW)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     4 - ( \u0(I, J) + \u0(I-1, J) ) \text{Fay2} \newsign \\
5 + (( \u0(I, J) + \u0(I, J-1) ) \text{Fay2} \newsign \\
6 - ( \u0(I, J+1) + \u0(I, J) \text{Fay2} \newsign \\
A + (\u01 \u001 \u001 \neq \u01 \neq \u
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       7(I, J, NEXT) = 2.17(I, J, NOW) - 7(I, J, LAST)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 Y(I, J, LEXT) = 2. 'Y(I, J, NO'4) - Y(I, J, LAST)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             RZF(I) = (Y(I, J, VOW) - Y(I, J+1, VOM)) / D7

CZP(I) = (Z(I+1, J, NOW) + Z(I+1, J+1, NOW))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      D7P(I) = (Z(I, J, VOW) - Z(I, J+1, VOM)) / DZ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              M11([+1, 4) 11 407
                                                                                                                                                                                                                                DPZ = (7(I,J-1,454)+7(T+1,J-1,NO4) -
                                                       (WCN,1-1,1-1, V (I+1, J-1, VOW) = ZPP
                                                                                                                                                                             YC = (Z(I+1, J, NOW) - Y(I, J, NOW) / YC)
- YCI, J, NOW) / OY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       - Z(I-1, J+1, NOW))/(4,*9Y)
                                                                                                              1 -Y(I+1, J+1, NOW))/(0.*07)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     - Y(I-1, J, NOW)) / (L. PDY)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     LAM (I, J+1) +
(MCN+T+T)A)
                                                                                                                                                                                                                                                                                                   1 NCW))/(-..77)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      40 (1, 3)
                                                                                                                                                                                                                                                                                                                                                              A74 = A70(T)
                                                                                                                                                                                                                                                                                                                                                                                                                         (I) dZu
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    (1) 120 = K20
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                                                                                                                                                                                                                                                                                                                                   W &
                                                                                                                                                                                                             SHA
                                                                                                                                                                                                                                                                                                                   SHZ
                                                                                                                                                                                                                                                                                                       SNO
                                                                                                                                                  570
                                                                                                                                                                                              0 7 7
                                                                                                                                                                                                                                                                                                                                    SND
                                                                                                                                                                                                                                                                                                                                                  CNY
                                                                                                                                    SND
                                                                                                                                                                 -(FU(I, J)/P(I)) (((Y(I, J, MOW))+f(I, J-1, JOW))/(2.*DZ)) - ((Y(I, J, NOW)) + Y(I, J+ MOW))/(2.*DZ)) - ((Z(I, J, MOW) + Z(I+1, J, NOW))/
                                                                                                                    MU(I,J-1))/D2) = ((Y (I,J,VOW) + Y (I,J-1,NOW))/(2.*R(I))) - ((.5*
                                                                                                                                    _A 4(I, J+1)) + 4J(I, J) + 4U(I, J+1))/DZ)*((Y(I, J,
                                                                                                    (ET* DI /R40(I, J)) * (((.5*( LAM(I, J) + LAM(I, J-1)) + MU(I, J) +
                                                                                                                                                                                                                                                                                                                                                   ",K,")= ",Z(K,JWZITE,NOW)),K=2,IMAX)
                                                                                                                                                                                                                                                                                                                                                                                ", K, ") = ", Y (<, JWRITE, NOW)), K=2, JMAX)
FTN 4.6+446
                                                                                      4U(I-1,J) ) (34Z + 34Z))/(2,*DY))
                                                                                                                                                                                               (2.*DY)) + ((7(1,1,40M) + Z(T-1,1,40M))/(2.59Y))))
                                                                        (LCC + ZCE)+1
                                                         70/((I) 225 ( ()+())/37
                                                                                                                                                                                                                                                           THE FOLLOWING IS AN OUTPUT ALSORITHM
                                            1 4 37 4
                                                                                                                                                  NGW) + Y(I, J+1, NOW))/(2.* R(I)))
                                            MU(I, 7)
                                                                         MII(I+1, J)
                                                                                                                                                                                                                                                                                                       IF(T.LT.T4RITE) 30 TO 50
                                                                                                                                                                                                                                                                                                                                                PalN7*, ((" DISPL Z (GELL IF (IFLAG.ED.0) GO TO 15
                                                                                                                                                                                                                                                                                                                                                                               PRINT*, ((" DISPL Y (OFLE
                                                                                                                                                                                                                                                                                                                                    IF (JFLAG.ED.0) SO TO 1/
                                                                                                                                                                                                                                                                                                                     IF (NFW.NE.2) GO 10 50
2=100
                                            41(I, J-1)
                                                                         MUCI, 5
                                                           "J(I, J)
                                                                                        WU(I,J)
                                                                                                                                    ( LAN(1, 1) +
74/74
JGRAM THIRMAL
                                             M 4 M O 4 M O C M
                                                                                                                                                                                                                             93333
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3NP 78
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3,512,3,777)
                                                                                                                                                                                                                                                                                                                                                                                                            TEST= AMAX1 (ABS(Y(I, JWRITE, NOW)), ABS(Z(I, JWRITE, NOW)))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       $ ",612.3,", OUTPJT DEPTH Z(CM) = ",612.3,1//)
00 26 I=1,1MM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       PPINT 101,1, SCALE, DV, 7WRITE FORMAT(///," TIME(SEO) = ", FE.4,"
                                                                                                                                                                                                                                                                                                                                                                                                                           IF (TEST.ST.SCALE) STALE=TEST
                                                                                                                                                                                                                                                                                                                                                                                                                                         IF(SCALE.E3.0.0) SCALE=1.0
TWPITE = (JWRITE- 2) * 07
                                                                                                                                                                                                                                                                                                                                                 DO 26 J=13,21,2
                                                                                                                                        00 2: J=3,19,2
                                                                                                                                                                                                                                                                                                                                                                                              DO 27 I=1,IMAX
I=1,100
             0 21 J=1,21
AL(I,J)=" "
OD 22 J=1,21
                                                         AL(1,J)="I"
OO 23 I=2,98
AL(I,11)="-"
AL(2,1)="1"
                                                                                                                                                                                                                                    AL (4, 11)="3"
                                                                                                                                                                                                                                                   AL (4,13)="2"
                                                                                                                                                                                                                                                                 AL (4, 15) =","
                                                                                                                                                                                                                                                                                 FL (4,17)="5"
                                                                                                                                                                                                                                                                                                 AL (4, 19) = "8"
                                                                                                                                                                                                                                                                                                               AL (3, 21)="1"
                                                                                                                                                                                                                                                                                                                                AL (4, 21)="."
                                                                                                                        AL (3, 1)="."
                                                                                                                                                                                                                                                                                                                                                               AL (2, J)="-"
                                                                                                                                                      £L(3, J)="."
                                                                                                                                                                     AL (4, 3)="8"
                                                                                                                                                                                     AL (4, 5) ="6"
                                                                                                                                                                                                     AL (6, 7) ="4"
                                                                                                                                                                                                                    AL (4,9)="2"
                                                                                                                                                                                                                                                                                                                                                                               SCALF=0.0
                                                             00
                                                                                                                                                        5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          101
1:
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SNO 78

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2NP 78

34N 78

JZ=11.5-10.\*Z(L,JWRITE,NOW)/SCALF IF(ZFLOT.ET.S) GD TD 28 IF(JZ-LT.1) JZ=1 IF(JT.6T.21) JZ=21 AL(I,JZ)="7"

27.

IF (JY . EQ. JZ) AL(I, JY) ="X"

DO 24 K=1,10

T=10' K

•

CONTINUE

AL (2°, 11) = "2" AL (2°, 11) = "3" AL (3°, 11) = "4"

AL (I, 11)="0" AL ( c, 11)="1" AL (40,11) ="5" AL (59,11) ="6"

AL (66, 11) ="7"

AL (98, 11) = "9" AL (98, 11) = "1" AL (99, 11) = "0"

JY=11.5-10.8 Y(L, JWRITE, NOW) / SCALE IF(JY.LT,1) JY=1 IF(JY.6T.21) JY=21 AL(I,JY)="Y"

L=I+1 IF(RFLOT.EQ.0) GD TD 275:

0PT=2

74/7

JONSHIT MODE

```
2ND 78
2ND 78
2ND 78
                                                LOCSHOK IS THE LOCATION OF SHOOK FRONT ON THE GROUND FOR PLOT
YYSHOGK= 0 IMPLIES HORIZONTAL DELL 2, WHICH IMPLIES AL(1,J)
                                                                                                                                                                                                              IF (IMAX DY/VEL - (T-TZERO)) 20,20,5
CONTINUE
                                                LOCSHOK = (YYSHOG< + (DY/2))/DY + 1
                                                              20 29 J=1,21
20 PRINT 102,(AL(I,J),I=1,IMAX)
102 FORWAT(1x,10041)
30 CONTINUE
                                                                                                                                                                                    WEXT = 6 - LAST - NOW T = T + DT
                                                           AL (LOCSHOK,1) = "A"
AL (LCCSHOK,2) = "9"
                                                                                                                                                              LAST = NOW
                                                                                                                                                                         NOW = NEXT
                                                                                                                                     55
 0000
```

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(0)

(IES) GERTTNOE MAP (S=1)

Appendix F

Surface	Pressure	Subroutine
burrace		Dubi ou cine

```
2ND 78
                                TARR2= 1.E-3*(.5/291*(YIELD*2003.)-(21.185/SLT2ANG)*(YIELD*2000.)
$ **.(67) + 361.8*(SLTPANG**2)*((YIELD*2000.)**.333) + 2383.*
                                                                SAME &S TARE EXCEPT 115E 2000 IN PLACE OF 1000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     6 +
                                                                                                                                                                                           YYSHOOK = LOCATION OF SHOCK FROWS ON GROUND
                                                                                                                                                                                                                                                                                                                                                                                                                                                  = (17.-14.)/(1050-725.)*(YYF-725.) + 14.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    = ((2.5-9.)/(2500.-1500.)) (YYF-1500.)
                                                                                                                                                                                                                                                                              DEAKP = PEAK OVERPRESSURE (GLASSTONE FIT)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   = ((3.-1/.)/(1500.-10.0.))*(YYF-1050)
                                                                                                                                                                                                                                                                                                                                                                                                                PEAKF = (14.-30.25)/725. * (YYF) + 36.25
                                                                                                                       TARR = TARR + HOR/YY + TARR2" (1,-HO3/YY)
                                                                                                                                                                                                                            IF((TARR-T).LE.1.E-1) YYSHOGK = YY
IF (1.LT.TARR ) 50 TO 1
                                                                                                                                                                                                                                                                                                                                                   003
                                                                                                                                                                                                                                                                                                                  YYF = YY*CMIOKFI*1000
IF(YYF.61.2354.) $0 TO 810
                                                                                                                                                                                                                                                                                                                                                                    IF(YYF.GE.1850.) 50 TO 788
                                                                                                                                                                                                                                                                                                                                                                                               IF(YYF.65.0725.) SO TO 776
                                                                                                                                                                                                                                                                                                                                                 IF(YYF.GF.1100.) 30 TO
   TARRZ =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CONTINUE
                                                                                                                                       CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                               GO Tr
                                                                                                                                                                                                                                                                                                                                                                                                                                                  DEAKP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      GO TO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    20 10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   SXVSG
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       01 05
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      PEAKE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  768
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     800
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       6 K
                                                                                                                                       60000
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                                                                                                                                                                                                                                                                CCC
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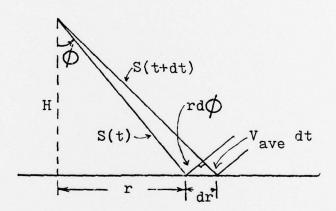
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44=1.+.36244L06(PEAKP)-.136\*(ALOS(PEAKP))\*\*2.+.025\*(ALOG(PEAKP))\*+ TELUS IS LINERA FIT TO SLASSTONE FOR PARTICULAR YIELD - TAU) + 44) + + (1./ A4) P(T) =PRESS1 = MICKEL (62 GLASSIONE) TPLUS = ((.33-.13)/(2500.))\*YYF + .15 CONTINUE PFATTO = 1. - (1. - (1. IF (Press.LT.0.) 33 TO 1 14U = (T-TARR)/TFLUS IF(TAU.GT.1.) 50 TO 1 FEES: = FRESS\*0S11990 PRESS = FEAKPR PRITIS 50 TC 90 FETUEN 2007 COCY 3.7

#### Appendix G

# Estimate of Apparent Airshock Velocity Along Ground Surface

The shock front from a nuclear burst can be considered a spherical shell which is expanding with some average velocity,  $V_{\rm ave}$ . The intersection of this spherical shock front with the ground surface forms a circular region. This circular line of intersection will expand along the ground with a velocity, called the apparent velocity  $V_{\rm app}$ , which will differ from  $V_{\rm ave}$ . If the airshock is approximated locally as a planar wavefront, the following figure describes the position of the airshock at two times, t and t+dt.



In dt, the shock wave radius S (also equal to the slant range) expands by Vavedt. Thus,

$$S(t+dt) = S(t) + V_{ave}dt.$$

Also, 
$$(dr)^2 = (v_{ave}^2 dt)^2 + \left[ S(t) d\phi \right]^2, \text{ or }$$
 
$$\frac{dr^2}{dt} = v_{ave}^2 + \left[ S(t) \frac{d\phi}{dt} \right]^2.$$

But, 
$$tan \phi = \frac{r(t)}{H}$$
 and  $sec \phi = \frac{S(t)}{H}$ 

Also, 
$$\frac{d}{dt}$$
 (tan  $\phi$  ) =  $\sec^2 \phi$   $\frac{d\phi}{dt}$  =  $\frac{1}{H}$   $\frac{d r(t)}{dt}$ .

which gives  $\frac{d\phi}{dt} = \frac{1}{H \sec^2}$   $\frac{d r(t)}{dt}$ 

$$= \frac{1}{H} \left( \frac{H}{S(t)} \right)^2 \frac{d r(t)}{dt} = \frac{H}{S^2(t)} v_{app}.$$

Substituting for  $\frac{d\Phi}{dt}$  in the expression for  $\frac{dr}{dt}$  above yields

$$\left(\frac{dr}{dt}\right)^2 = v_{app}^2 = v_{ave}^2 + \left[S(t) \frac{H v_{app}}{[S(t)]^2}\right]^2$$

or 
$$v_{app}^2 \left[ 1 - \frac{H}{S(t)} \right]^2 = v_{ave}^2$$

Solving for 
$$V_{app}$$
,
$$V_{app} = \begin{cases} \frac{V_{ave}^2}{1 - \left(\frac{H}{S(t)}\right)^2} \end{cases}$$

Finally substituting for  $S(t) = [(H^2 + (r(t))^2]^{\frac{1}{2}}$ ,

$$v_{app} = \begin{cases} \frac{v_{ave}^2}{1 - \frac{H^2}{H^2 + r^2}} \end{cases}$$

#### Vita

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The coupling into the ground of airble atmospheric nuclear burst is postulated a contribute to if not independently cause precursor. A computer model to test the by assuming an elastic ground medium, appetechniques to the equations of motion, as time-varying overpressure from the nuclear	as a mechanism which may the observed airshock hypothesis is constructed olying finite difference

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seismic motions within the ground.

The surface velocities resulting from simulation of a 28 kiloton atmospheric burst at 500 feet height of burst yielded a dust layer ballistically reaching only 0.64 cm at its highest point for the stiff one-layer ground medium, 0.096 cm for the softer one-layer medium, and a negligible height for the more realistic four-layer Frenchman Flats medium. Thus, the airblast-induced precursor as postulated (ballistic rise only) fails to re-create the 2 - 3 meter high dust layers observed in experimental atmospheric nuclear testing. However, the motions are felt to be significant enough to be included in any attempt to model from first principles the precursor and the up-sweep of dust behind the shock front.