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RADC-TR-78-207 Final Technical Report September 1978

MULTILEVEL MODULARIZATION OF SYSTEMS TO MINIMIZE LIFE CYCLE COST

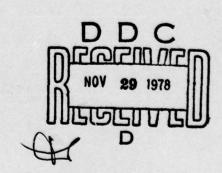
John E. Biegel Bisrat Bulcha

Syracuse University

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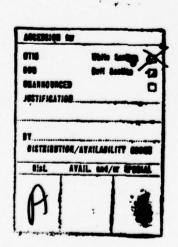
Preface

This report describes a technique for the multi-level modularization of large systems such that the life cycle cost will be a minimum. The method presented is an extension of the one-level modularization reported in Biegel and Bulcha, System Modularization to Minimize Life Cycle Costs [1,2].

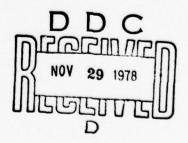
The method is a heuristic extension of the previous method [1,2] and no attempt has been made to prove its optimality. We have generated no counter examples, however.

The system is first decomposed into functional elements, then reconstructed into modules, each containing one or more functional elements. The modules are then collected into subassemblies, the subassemblies into higher level subassemblies, etc. The criteria is to form the collected sets in such a way that the life cycle cost (LCC) is minimized.

The computer routine to do this is presented and explained. An example problem is included.







EVALUATION

The objective of this effort was to develop a methodology which would allow an equipment to be modularized (partitioned into modules) in such a way as to minimize total life cycle cost. This objective was accomplished. The methodology developed is capable of structuring the modular organization of an equipment taking into account reliability, maintainability, fabrication costs, and logistics support costs. This report provides the procedures and necessary detail for use of this methodology. Besides the dissemination of the report to potential users, follow-on activity is currently in progress to:

- a. Include the methodology in a planned "Life Cycle Cost Design Handbook"
- b. Include the methodology as part of the "RADC Compu-Standards Program". (A computerized compendium of procedures intended to implement and support reliability and maintainability standards and handbooks).
- c. Utilize the methodology in the house and suggest its use to RADC contractors in support of life cycle cost analysis efforts on hardware items.

JEROME KLION Project Engineer

INTRODUCTION

The objective of this research was to develop a technique for the multi-level modularization of large systems through operations on their matrix representation. The final procedure must perform m levels of modularization on a large network of n nodes such that the life cycle cost will be at or near minumum. The solution technique is programmed into the RADC Multics system in Fortran. This is an extension of the work reported in Biegel and Bulcha, System Modularization to Minimize Life Cycle Costs [1,2].

As electrical designs become increasingly complex and large, so does their network representation, and the associated data describing the network and its components. Hence in developing an efficient partitioning technique for large networks (100 or more nodes) data handling becomes a major consideration.

Network information is conveniently represented in matrix form.

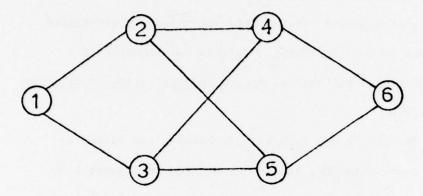
But as the number of nodes in the network increases, so does the matrix size. If there are 100 nodes, one needs a (100 X 100) matrix for a full representation of the network.

Although the modularization procedure does not assume any particular type of network, it is necessary to look more closely into different types of networks from the data handling point of view.

The modularization process described in this report is essentially the same as that described in our previous report [1,2]. We have incorporated a computerized spares allocation procedure and the complete life cycle cost evaluation of the designs developed when modularizing these large networks. In many engineering applications, including electronics, the network that represents the system is of an elongated type and the matrix is called "sparse".

<u>Definition</u>: Let A be a square matrix of order n, if r is the number of non-zero elements and r \ll n², then A is sparse.

An Elongated Non-Directed Network



Its Matrix Representation

1	2	3	4	5	6
0	1	1	0	0	0
1	0	0	1	1	0
1	0	0	1	1	0
0	1	1	0	0	1
0	1	1	0	0	1
0	0	0	1	1	0
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Figure 1: An elongated network and it's sparse matrix representation.

Now consider a non-directed network that results in a matrix that is dense, typically a "complete graph".

<u>Definition</u>: A complete graph, is a graph where every node is connected to every other node.

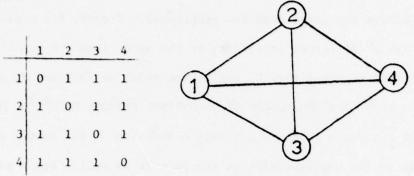


Figure 2: A complete graph and its dense matrix representation.

As the number of nodes increases, the proportion of non-zero entries to the size of the matrix is usually significantly reduced. Thus, efficient methods of storing data for large networks must be found.

Elongated, directed networks have a triangular matrix representation where data is usually concentrated near the diagonal. For such a matrix, where n=100, we have up to 49.50 possible entries and only a small percentage of these entries are non-zero. The usual way of specifying an entry by the row and column indices is inefficient and time and space consuming when working with large networks. Considering this difficulty, a procedure is developed to specify for each row only those elements to the immediate right of the main diagonal up to and including the last non-zero element in that row. For example, consider the i^{th} row with elements A_i , i+1, A_i , i+2, ..., A_i , n. Under the procedure used in this program, those elements would be entered as: j, k, 0, 0, 0, 1, 0, m where j, k, 1 and m are the only non-zero elements in the i^{th} row with j being the element in the (i+1)st column. This information is input as above and used in a subroutine, INIT, where the complete n x n matrix is created for use in the modularization procedure in the main program.

II. ON THE MODULARIZATION OF LARGE NETWORKS: GENERATION OF PROPER CUTS

An exhaustive enumeration approach can be used to generate all possible sets S and \overline{S} . We can test if these sets satisfy the requirement of a proper cut (divide the graph into two subgraphs). Clearly for a graph of n nodes there are 2^n different partitions of the nodes into the set S and \overline{S} . Moreover if it is required that U, the source node, be in S and V, the sink node, be in \overline{S} then the number of partitions reduces to 2^{n-2} . Obviously, the number of cuts in a graph is not only a function of the number of nodes n but depends on the configuration of the network as well. For a simple chain type network the number of cuts is n-1. For a completely connected graph, the upper bound is the limit given above which is 2^{n-2} . For large n, this results in a very wide range in the number of cuts.

Two heuristic methods directed toward reducing the number of cuts to be generated are:

- 1. to generate only those cuts that are connected, and
- 2. to generate restricted proper cuts.

A connected cut is one in which all nodes in a set are connected by a chain. A restricted proper cut is one such that the source node is in S and the sink node is in \overline{S} .

If a network has as many as 100 nodes, it is highly doubtful that these or any other similar cut generation procedures will adequately reduce the number of sets to be considered in an optimization process. The procedure developed during this research limits the number of cuts to those which have a high probability of providing an optimal result.

Paul A. Jensen *states "...any algorithm for generating cuts will soon be time limited in operation as one increases the size and complexity of the subject graphs. On this basis one should be suspect of the practicality for all but the smallest problem of an optimization procedure which requires for its performance the set of all proper cuts."

^{*} Jensen, Paul A, A Graph Decomposition Technique for the Design of Reliable Redundant Electronic Networks, Ph.D. Dissertation, Johns Hopkins University, page 126.

III. THE MODULARIZATION PROCEDURE AT m-LEVELS:

After the basic modularization of a large network, the resulting configuration is again a network with the nodes replaced by a higher level nodes called modules and the arcs being the interconnections between these modules. Further "modularization" will result in still a higher form of modules that are frequently called subassemblies.

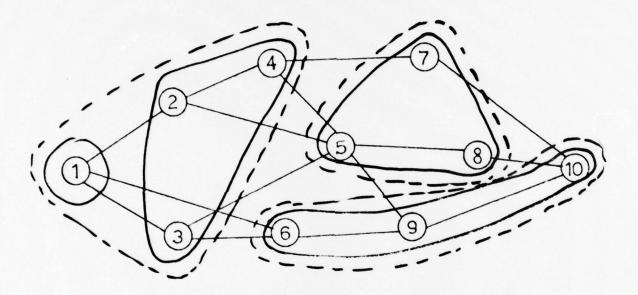


Figure 3: A network of subassemblies.

The procedure can be applied as many times as required to obtain the desired number of levels of modularization. The only modification in the procedure is in the network input data itself.

Consider a network that has been built up of modules. We are interested in generating higher level assemblies. The network information is changed straight forwardly as follows:

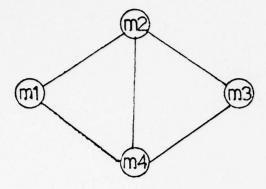


Figure 4: A network of modules.

Where $m_1 = [1]$, $m_2 = [2,3,4]$, $m_3 = [5,7,8]$, $m_4 = [6,9,10]$. The intraconnection I (Mi,Mj) between the newly found nodes, Mi and Mj can be obtained by forming all the pairs (k,m) such that keM_i and meM_j, and entering the current network interconnection matrix, Ac to read Ac(k,m). Then $I(Mi,Mj) = \sum_{\mathbf{Y}(k,m) \text{ pairs}} Ac(k,m).$

Thus a new network is developed for yet another level of partitioning, if needed. If an m level modularization is wanted, this procedure will yield m new networks. At any level the newly found network and its characteristics are a new set of data for the modularization algorithm explained in Biegel and Bulcha [1,2].

It is concievable that at some stage a user might want some of the nodes left at lower levels with the rest of the nodes merged into a higher level of assemblies. (This could be for maintenance reasons.) This variation can be incorporated by adding fictitious nodes to the network in place of the nodes that are not candidates for higher level assemblies. These fictitious nodes will have 0 arc weights and 0 physical characteristic in

the next level of network. Figure 5 shows such a network.

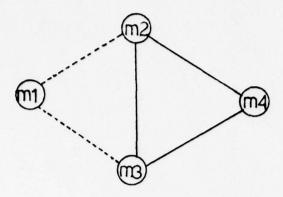


Figure 5: A network with a fictitious node.

Where M_k - fictitious for next level network i.e.: $\phi^j = 0 \ \forall \ j; \ I(M_1, M_2) = I(M_2, M_1) = 0, \ I(M_1, M_3) = I(M_3, M_1) = 0$ M_k

III. THE COST MODEL FOR HIGHER LEVEL DESIGNS INVOLVING SUBASSEMBLIES AND ASSEMBLIES

Suppose a design D consists of a mixture of modules (M), subassemblies (SA), and assemblies (SS). Assume that there are t modules at a modular level, m subassemblies and p assemblies at the final level as shown in the Figure 6. The acquisiton cost of such a design is:

$$C_{\mathbf{A}}(\mathbf{D}) = \sum_{i=1}^{\mathbf{t}} C(\mathbf{M})_{i} + \sum_{j=1}^{\mathbf{m}} C(\mathbf{SA})_{j} + \sum_{k=1}^{\mathbf{p}} C(\mathbf{SS})_{k}$$

Where

 $C(M)_{i} = cost of module i$

- $C(SA)_{j}$ = cost of subassembly j; it is the sum of the cost of the modules it contains plus the cost of packaging the modules into a subassembly.
- $C(SS)_k = cost of assembly k$; it is the sum of the cost of the subassemblies plus the cost of packaging the subassemblies in an assembly.

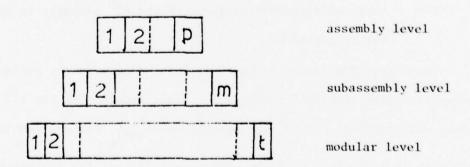


Figure 6: A multilevel design, D.

There are primarily two approaches to the problem of spares allocation to the multilevel designs:

- (a) Given the overall system availability, determine a spares allocation policy simultaneously for all levels.
- (b) Given the overall system availability, determine a spares policy for each level separately after the modularization process, by imposing the availability constraint at each level.

Consider (a); this procedure to find a spares allocation system is more accurate, but the equipment must be modularized into all levels before the spares calculation can be done. Using (b) is a more conservative approach, that is it requires that the system availability requirement be met at each level. Under model (a) the expression for the spares requirement follows.

- Let $\theta(M)_i$ = expected number of faiTures of the i^{th} module in the design during period L.
 - θ (SA)_j = expected number of failures of the jth subassembly in the design during period L.
 - $\theta(SS)_k$ = expected number of failures of the k^{th} assembly in the design during period L.

Thus, assuming independence of failure among modules, subassemblies, and assemblies, the probability that $S_{(M)}^*$ spare modules for the i^{th} module, $S_{(SA)}^*$ spare subassemblies for j^{th} subassembly and $S_{(SS)}^*$ spare assemblies for k^{th} assembly is sufficient over the operational life of the equipment is given by:

$$P_{(M)_{i}} = P(W(M)_{i} \le S_{(M)_{i}}^{*}) = S_{W(M)_{i}=0}^{*}$$

$$e = [\theta(M)_{i}] = W(M)_{i}!$$

$$P_{(SA)_{j}} = P(W(SA)_{j} \leq S^{*}(SA)_{j}) = \sum_{k=1}^{s} (SA)_{j} = 0 \qquad \frac{e^{-\theta(SA)_{j}} (\theta SA_{j})^{w}(SA_{j})}{W(SA)_{j}!}$$

$$P_{(SS)_{k}} = P(W(SS)_{k} \le S^{*}(SS)_{k}) = \sum_{k=0}^{S^{*}(SS)_{k}} \frac{e^{-\theta(SS)_{k}}W(SS)_{k}}{W(SS)_{k}!}$$

Where, $W(M_i)$, $W(SA)_j$, $W(SS)_k$ are the total number of failures for the i^{th} module, the j^{th} subassembly, and the k^{th} assembly. Hence if the system availability is AV then it is required that:

$$\begin{array}{cccc}
t & m & p \\
(\prod_{i=1}^{p} P(M)_{i}) & (\prod_{j=1}^{m} P(SA)_{j}) & (\prod_{k=1}^{p} P(SS)_{k}) \geq AV
\end{array}$$

The problem of optimal spares allocation becomes three dimensional and the number of possible elements whose spares can be determined at each iteration is t x m x p, making the problem increasingly difficult. Under model (b) the availability constraint is imposed at each level, thus making the constraint tighter. But as independence between the levels is also assumed, it is possible to arrive at a spares allocation policy without a significant shift from the results of method (a). Under (b) it is required

$$\prod_{i=1}^{t} P(M) \ge AV$$

$$\prod_{j=1}^{m} P(SA)_{j} \ge AV$$

$$\sum_{k=1}^{p} P(SS)_{k}^{\geq AV}$$

A separate policy for each level can be determined once the failure rate of each element in each level is determined.

Let $S^*(M)_i$, $S^*(SA)_j$ and $S^*(SS)_k$ denote the spares needed for the i^{th} module, the j^{th} subassembly, and the k^{th} assembly respectively. The cost of this spares policy is:

$$C_{S} = \sum_{i=1}^{t} C(M)_{i} S^{*}(M)_{i} + \sum_{j=1}^{m} C(SA)_{j} S^{*}(SA)_{j} + \sum_{k=1}^{p} C(SS)_{k} S^{*}(SA)_{k}$$

An expression for the life cycle cost (LCC) for a single equipment is:

LCC =
$$\sum_{i=1}^{t} C(M_i) + \sum_{j=1}^{m} C(SA)_j + \sum_{k=1}^{p} C(SS)_k$$

+ $\sum_{i=1}^{t} C(M)_i S^*(M)_i + \sum_{j=1}^{m} C(SA)_j S^*(SA)_j + \sum_{k=1}^{p} C(SS_k) S^*(SA)_k$

- + Inventory cost for each level
- + Cost of introducing a line item into inventory at each level.

IV. COMPUTER PROGRAM TO MODULARIZE LARGE NETWORKS

In the Multics environment the main program and all associated subroutines and functions are stored in separate segments. The following segments were created for the computer program developed.

Main. Prog. Fortran

Init. Fortran

Sort. Fortran

Sort. 1. Fortran

Metr. Fortran

Lec. Fortran

Nspare. Fortran

Maxim. Fortran

M-shift. Fortran

R-shift. Fortran

Minx. Fortran

The above segments constitute the complete program. A brief description of the subroutines follows.

Main. prog. -- contains the coding for the modularization algorithm.

A. Subroutine Init:

Subroutine Init forms the $n \times n$ interconnection matrix from the network data.

B. Subroutines Sort and Sort 1:

Subroutines Sort and Sort I arrange the identification of the elements in each module.

C. Subroutine Mttr.:

Subroutine Mttr. evaluates the mean time to repair for a selected design.

As the network grows in size and complexity, the mean time to repair

which is a factor dependent on the interconnections between modules

as well as the number of modules becomes an important factor. The modularization process incorporates a methodology for evaluating this factor. The expression for the expected maintenance time is

$$E(TM) = T_1 + nT_2 + \sum_{i=1}^{n} T_3 \exp(T_4 P(M_i))$$

Where n = number of modules in a specific design

 $T_1 = a$ constant time per maintenance action

 $T_2 = a$ constant time per module

 T_3 = a constant modifying the exponential relationship of the number of external connections

 $T_4 = a$ constant modifying the number of external connections

 $P(M_i)$ = number of external connections to module i.

The specific form of the above equation as used by Caponecchi [3] is

$$E(TM) = 2.5 + .05n + .087 \sum_{i=1}^{n} exp (.047P(M_i))$$

The above expression is evaluated for each design and the design is accepted if the calculated value of E(TM) < MTTR max.

D. Subroutine Lcc:

This subroutine evaluates the life cycle cost (LCC) of the feasible designs. The main components of Lcc are the cost of acquisition and the support cost for the equipment over its intended useful life.

Where C_{A} = acquisition cost for design

 C_S = support cost for the design

Consider the acquisition cost C_A , which can be further broken down into

$$C_{\mathbf{A}} = NE \left(\sum_{i=1}^{n} C \left(M_{i} \right) \right) \tag{1}$$

NE = number of equipments to be procured.

 $C(M_i) = cost of each module in a design.$

The cost of a module is further given as

$$C(M_i) = CC(NP) + CE(P(M_i)) + CP$$

Where CC = cost of a component

NP = number of components

CE = cost of providing external connections

 $P(M_i)$ = number of external pin for module i

CP = cost of packaging a single module.

Under the assumptions of a discard at failure maintenance (DAFM) policy and that at least one of each module will be spared, the life time support cost of NE equipments, if each is at a separate site is:

$$CS = n CI + n CCL + NE. \sum_{i=1}^{n} N_{i} \cdot C(M_{i})$$
 (2)

CS = Total organization support cost

CI = Cost of introducing a line item into the inventory system.

CC = Cost of maintaining a line item in inventory for one year.

L = Planned operational life of the equipment in years.

 $N_{\hat{i}}$ = Number of spares of module i to be procured to support each equipment.

Then the total life cycle cost is the sum of equations (1) and (2) or LCC = $n(CI + CCL) + NE \sum_{i=1}^{n} (1 + N_i)C(M_i)$.

This cost is evaluated for each feasible design by subroutine Lcc.

A flow chart for subroutine Lcc is presented as Figure 7.

*Assumes all modules in equipment different.

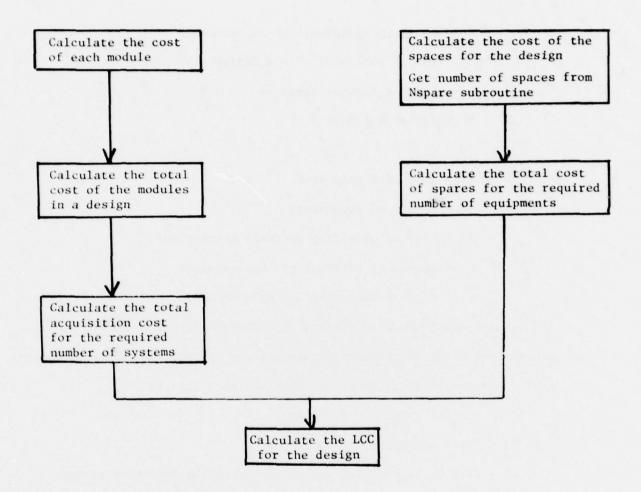


Figure 7: Flow Chart for LCC Subroutine

E. Subroutine Nspare:

A complete evaluation of the spares requirement is done by this subroutine in an iterative manner. The modules formed are treated as a series subsystem. Thus, if the system availability is A then the probability that $N_{\hat{\mathbf{I}}}$ spares for module i is sufficient for the operational life of the system is given by

$$P(W_{i} \leq N_{i}) = \sum_{W_{i}=0}^{N_{i}} e^{-F_{i}} \frac{W_{i}}{W_{i}!} \geq A_{min}$$

where $F_i = r_i \cdot L \cdot NE$, and

$$\mathbf{r}_{i} = \prod_{j \in M_{i}} \mathbf{r}_{j} - AP(M_{i}) \mathbf{r}_{p}$$

 r_i = failure rate of module i.

 $r_{\rm p}$ = interconnecting pin failure rate reduction factor.

 $\text{AP}\left(\textbf{M}_{\underline{i}}\right) = \text{The number of external connections eliminated by forming}$ module i.

L = operational life of equipment.

NE = number of equipments.

But this inequality must be maintained for all modules in the system. Thus

$$\begin{array}{cccc} n & N & F & F & W & \\ \Pi & \Sigma & e & F & W & \\ i=1 & W=0 & \frac{W_i!}{W_i!} & \geq A \end{array}$$

where n is total number of modules generated.

Therefore, an optimal spares policy is a set of $[N_1^*...N_n^*]$ such that: $C_1N_1 + C_2N_2... + C_nN_n$ is minimum where C_i is the cost of module i.

Or minimize:

$$c_1N_1 + \ldots + c_nN_n$$

Subject to:

$$N_1, N_2, \dots N_n \ge 0$$
 and integer

The above problem is an integer, non-linear programming problem, and is difficult to solve even for small values of n. But for large networks the number of modules generated, N, is fairly large and makes the problem increasingly difficult with increases in N. The alternative approximate solution method is similar to that in Biegel and Bulcha [1,2]. The solution method is:

1. Initialize by finding a lower bound N_i for each module, choose N, such that

$$\sum_{\Sigma_{i}=0}^{N_{i}} e^{-F_{i}} F_{i} \stackrel{\text{W1}}{=} \geq A^{*}$$

2. Find the value of A for the system

where
$$A = \Pi$$
 $(\Sigma \\ i=1 \quad W=0$ $\underbrace{ \begin{array}{c} -F_i \\ W \\ \hline W \end{array}}_{i}^{W}$

If
$$A \geq A^*$$
 stop.

3. Let
$$N_{i} = N_{i} + 1$$

4. Calculate $\Delta A_{i}^{*} = \begin{pmatrix} \Sigma^{i} & e^{-F_{i}} & F_{i}^{W} \\ W=0 & W! \end{pmatrix} - \begin{pmatrix} \Sigma^{i} & C^{-F_{i}} & F_{i}^{W} \\ W=0 & W! \end{pmatrix}$

- 5. Calculate $\Delta A_{\underline{i}}^{*}$ $\overline{C(M_{\underline{i}})}$
- Choose max $\Delta A_{\underline{i}}^*$ and set all other $N_{\underline{i}} = N_{\underline{i}} 1$
- 7. Go to step 2.

Now A is the minimum availability that each module must have for the overall availability of the equipment to be greater or equal to specified availability A. Theoretically $A^* = A^{1/n}$. When n is large \mathbf{A}^{\bigstar} approaches 1, such that the above procedure overestimates the optimal spares policy. A heuristic procedure to avoid this problem was to set $A^* = A^{2/n}$. For instance if A = .85 and n = 25

$$A_{1i}^{\star} = A^{1/n} = (.85)^{1/25} + A_{1i} = .9935, A = .850$$

$$A^*_{2i} = A^{2/n} = (.85)^{2/25} + A_{2i} = .9870, A = .721$$

Thus A_{2i}^* is a better initial policy for the optimizing procedure.

The above procedure is coded into fortran and stored in subroutine N spare. A flow chart for subroutine N spare is presented as Figure 8.

F. Subroutine Maxim:

Subroutine maxim is used in subroutine N spare to select the modules with maximum availability/cost ratio.

Subroutine M-shift:

Subroutine M-shift contains a subroutine to rearrange the data matrix so that every node is considered as a starting node for a set of modules.

Subroutine R-shift:

Subroutine R-shift contains a subroutine to reassign physical property values after the matrix has been rearranged by M-shift.

I. Function Minx:

A function used by the main program for selecting the group of elements with the minimum value for the external minus the internal connections at each iteration.

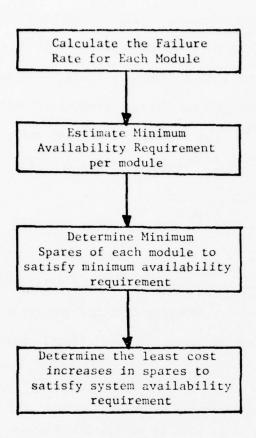


Figure 8: Flow Chart for Nspare Subroutine.

The following data files contain the data that are required by the different segments.

- data-2 contains the maximum maintenance time allowed.
- data-5 contains the numbers of nodes n, physical data for nodes and the set of physical constraints.
- data-7 contains the number of equipments to be procured, the cost

 of external pins and the shelf cost of maintaining a module.
- data-8 (1) The maximum length from a diagonal element up to and including the last non-zero element in the matrix representation of the network.
 - (2) row number and row entries starting from the diagonal up to and including the last non-zero element in the row.
- data-9 availability figure for the system.
- data-10 node failure rates (enter only decimal figures, eg. .211)

An example of a 100 node network that was modularized is included. The data for the network was generated in a random manner and stored in the appropriate files.

Summary:

This research has developed a method for modularizing large networks subject to physical constraints, mean time to repair constraints and availability constraints. A procedure has also been developed for the spares allocation and life cycle cost evaluation of the modularization designs.

A solution methodolgy for any higher level assembly is introduced by repeating the modularization procedure with the appropriate modification of the lower level designs, which will facilitate the problem as no additional algorithm is needed.

REFERENCES

- [1] Biegel, John E. and Bisrat Bulcha, System Modularization to Minimize Life Cycle Costs, Technical Report, July 1976, Department of Industrial Engineering and Operations Research, College of Engineering, Syracuse University, Syracuse, NY 13210.
- [2] Biegel, John E. and Bisrat Bulcha, System Modularization to Minimize Life Cycle Costs, RADC-TR-77-13, January 1977, A036868, Rome Air Development Center, Air Force Systems Command, Griffiss Air Force Base, Rome, New York 13441.
- [3] Caponecchi, A. J., A Methodology For Obtaining Solutions to the Modular Design Problem, Ph.D. Dissertation, The University of Texas at Austin, 1971.

APPENDIX 1

Failure rates for modules is addressed in [1,2] but for convenience it will be repeated below.

Let r denote failure rate for module i.

Then
$$r_i = \sum_{j \in M_i} r_j - \Delta P(M_i) r_p$$
 (A1-1)

where r_j = the failure rate of element j of module i $\Delta P(M_i)$ = the number of external connections eliminated by putting elements j in module i

r = failure rate correction factor for interconnection
 reduction.

Then $\theta(M)_{i} = r \cdot L \cdot NE$

Similarly to calculate failure rate of a subassembly substitute for the appropriate module failure rates \mathbf{r}_j in (1), and the number of ΔP for external pins eleminated by combining the modules into a subassembly. Also for an assembly substitute the appropriate failure rate for the subassemblies for \mathbf{r}_j in (1) and the number of external pins eliminated by combining subassemblies into an assembly ΔP .

APPENDIX 2: THE MODULARIZATION PROGRAM

Pr main. grost. fortran

main.pros.fortran 11/28/77 1048.2 est Mon

```
common trmas: av.co.ce.cp.ne.ci.cc.lit
     dimension rJ(100),r(100),rnt(100),rlcc(100)
     dimension rist(100)
     dimension c1(100),c2(100),c3(100)
     dimension budge(3).int(100).ext(100)
     integer a(100-100).m(110-110).s(100).st(100).sd(100)
      integer mv(100);mvt(100);t(100)
     integer one .ext
      integer co .ce.ce.ci.cc
     integer trow(100)
      integer n=(100).id1(100).id2(100)
      data bndrs/150.,1100.,0.17/
     data a/10000$0/
       data iJ1/100%0/.iJ2/100%0/.ifeas/0/.ne/100%0/
     data rnt/100*0./.r/100*0./.rlcc/100*0./
      data tlcc/0./
      read (9,20) av
       read (7.10) corcercrine, circo, lit
        read(2,11) trmax
 20
         format (f5.3)
        format(7i5)
 10
11
      format(f6.0)
      read (10.922) (+j(j),j=1,100)
 922 format (8f10.5)
  921 format (13)
     crio=0
     fetch connections matrix
      read(1,12) n
  12 format(15)
      write(3.13) n.n
   13 format(* network partitioning program *,//,* input matrix *
     . should be ', i3, by ', i3)
      read(1,21)(c1(i),i=1,n)
      read(1,21)(c2(i),i=1.n)
      read(1,21)(c3(i),i=1,n)
  21 format(8f10.0)
      call init(n.a)
      do 9999 loop-1.n
      write(3.9995)100P
9995
     format('0 starting node:',i3)
      15=0
      do 110 i=1.0
      s(i)=i
      t(i)=0
      do 110 J=1+n
  110 t(i)=t(i)+a(i,i)
 1000 if(1s .ea. 0)so to 5000
      mvt(1)=mirex(5,15)
      1mvt=1
      go to 2020
 2000 J1=i..t(imin)
      J. met (imin)
```

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```
JASSE (IMILL)
2020 call sort(myt.my.lmyt)
    1mv=1mvt
    1sd=0
    do 300 i=1.15
    do 280 J=1.1mv
    if(s(i) .ea.mv(j))so to 300
280 continue
    1sd=1sd+1
    sd(1sd)=s(i)
300 continue
    if(1sd .ea. 0)so to 4000
    do 500 i=1.1sd
     do 400 J=1.1mv
 400 m(i,j)=mv(j)
500 m(i \cdot lmv + 1) = sci(i)
    1mvt=1mv+1
    do 600 i=1.1sd
     int(i)=0
    do 600 J=1.1mv
    1= 1+1
    do 600 k=1.1mvt
600 int(i)=int(i)+a(m(i+j)+m(i+k))
    do 700 i=1.1sd
     ext(i)=0
    do 750 J=1.1mvt
750 ext(i)=ext(i)+t(m(i.j))
    ext(i)=ext(i)-2*int(i)
700 st(i)=ext(i)-int(i)
    imin=1
     low=st(imin)
     do 800 i=1.1sd
     if(st(i) .se. low) so to 800
     imin=i
     low=st(imin)
 800 continue
    con1=0.
     con2=0.
     con3=0.
    do 900 J=1.1mvt
    mvt(J)=m(imin.J)
    con1=con1+c1(mvt(j))
    con2=con2+c2(mvt(j))
900 con3=con3+c3(mvt(i))
     if((con1 .le. bndry(1)) .and. (con2 .le/ bndry(2)) .and.
     (con3 .le. bndry(3))) so to 2000
     1st=0
     do 980 i=1,15
     do 950 J=1.1mv
     if(s(i) .eq. mv(j)) go to 980
 950 continue
    1st=1st+1
     st(1st)=s(i)
 980 continue
     1s=1st
```

```
do 990 i=1.15
  990 s(i)=st(i)
 4000 eng=eno+1
      call sort(mv.st.lmv)
     do 901 i-1,1mv
     nst(i)=st(i)+(loop-1)
      if(nst(i).st.n)nst(i)=nst(i)-n
901
      continue
      call sorti(netalmy)
      write(3.180)cno.(nst(i).i=1.1my)
  130 format('0 card no. '.i3.' contains nodes:'./,'0'.20i5:100(/.6x.
     11915))
       do 91 i=1.1mv
       nr(cno)=nr(cno)+c1(nst(i))
       continue
      do 92 i=1.1mv
      rnt(cno)=rnt(cno)+rj(nst(i))
  92 continue
      r(cno)=rnt(cno)
      write(3,190)J2,J1,J3
  190 format('0',//,' ext. conn. = ',i5,/' int. conn. = ',i5./,' st = ',
     115)
      iJ1(cno)≃J1
      iJ2(cno)=J2
      if(1sd .ne. 0) so to 1000
      write(3,195)
  195 format("0 * * * * * *_r un completed * * * * * *)
      call mt!r(cno·iJ2rifeas)
      call lcc(ifeas.np.iJ2.cno.iJ1.r.tlcc)
      rlcc(loox)=tlcc
      call rshift(c1:n)
      call rshift(c2+n)
      call rshift(c3.n)
      call mshift(a+n)
        do 777 J=1,eno
        rnt(J)=0
        np(j)=0
         iJ1(J)=0
         iJ2(J)=0
       continue
777
      crio=0
9999 continue
      Stop
 5000 write(3,195)
      stop
      end
```

r 1049 0.808 0.710 51

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pr init.fortran

init.fortran

11/28/77 1100.1 est Mon

subroutine init(na;aa) inteser aa(na:na);col(100) read (8,49)n 49 format(i2) read(8.29.end=99) i.(col(j),j=1.n) 39 29 format(i3,30i2) do 19 J=1.n 1=1+3 if (1.st.100) so to 19 aa(i,1)=ccl(j) 19 continue so to 39 99 do 10 i=1•na do 15 J=1 • na if (J+i.st.100) so to 15 aa(i+j,i)=aa(i,j+i) 15 continue 10 continue return erid

r 1100 0.093 0.246 17

pr sort.fortran

sort.fortran

11/28/77 1102.2 est Mon

subroutine sort(inp,outp,n)
integer inp(n),outp(n),bptr.bsub.temp

bubble sort.

c optimum sort conditions occur in a completely sorted array
number of compares in a sorted array is n-1
iscnt=1
 do 10 i=1.n
10 outp(i)=inp(i)
 if(n .le. 1) returp
15 do 20 bptr=2.n
 bsub=bptr-1
 if(outp(bptr) .se. outp(bsub)) so to 20

temp=outp(betr)
outp(betr)-outp(beub)
outp(beub)=temp
iscnt=iscnt+1
so to 15
20 continue
return
end

sort1.fortran

sort1.fortran

11/28/77 1101.6 est Mon

subroutine sort1 (outsi:n) integer outpi(n).betr.temp.bsub inscnt=1 if(n.le.1) return do 20 betr=2.n 15 bsub=betr-1 if(outsi(bstr).de.outsi(bsub))do to 20 temp=outpi(betr) outpi(bptr)=outpi(bsub) outri(bsub)=tems insent=insent+1 so to 15 20 continue return end

pr mttr.fortran

mttr.fortran

11/28/77 1051.6 est Mon

subroutine mttr(cno,iJ2,ifeas) common trmax.av.co.ce.cp.ne.ci.cc.lit integer corcercprcirce integer cho inteser iJ2(cno) m=0 do 10 i=1.cno xm=xmfexp(.047*iJ2(i)) 10 continue Mm=Xm*.087 ym=2.5+.05*cno etm=xm+sm write (3,13) etm format(2x, 'expected total maintenance time=',f8.5) 13 if (etm.le.trmex) so to 20 write (3.12) format(2x, 'design not feasible') 12 ifeas=-1

return 20 ifeas=1 return end THIS PAGE IS BEST QUALITY PRACTICABLE FROM COPY FURNISHED TO DDC

pr lcc.fortran

lcc.fortran

11/28/77 1054.6 est Mon

```
subroutine lcc(ifeas.np.ij2.cno.ij1.r.tlcc)
      common trmax, av, co, ce, ce, ne, ci, cc, lit
      integer co.ce.ce.ci.cc
      integer temetesp
       integer cho
       inteser csp,tlcc
       integer acisc
       dimension np(cno).iJ2(cno), iJ1(cno).r(cno)
       dimension cm(100) ns(100)
      data ns/100*0/
       data cm/100*0./
       if (ifeas.ea.-1) so to 40
      tcm=0
       do 15 i=1,cno
       cm(i) = (co*np(i)) + (ce*iJ2(i)) + cp
   15
         continue
      do 20 i=1.cno
write (3.51) i.cm(i)
51 format(5x, cost of mod. ', i3, '=', f10.3)
       tem=tem+em(i)
   20
         continue
       write(3.52) tom
52
         format(2:: total cost of the modules=',i6)
       ac=ne*tcm
       write (3.88)ac
88
       format(2x, *acquistion cost=*,i10)
      call nspare(ns*cho*cm*ij1*r)
       tcsp=0
       do 25 i=1.cno
       tcsp=tcsp+(ns(i)*cm(i))
 25
         continue
       csp=ne*tcsp
       write (3,48) csp
        format(2x. total cost for the spares requirement= *:i10)
 48
        sc=cno*ci+cno*cc*lit+csp
        write (3,99)sc
99
       format(2x, "support cost=",i10)
```

tlee=setee write (3,30) tice 30 format(2x, time cost of this design is= '.i10) 40 tlcc=10**6 return end r 1054 0.454 0.528 31 er nseare.fortran nspare.fortran 11/28/77 1052.6 est Mon subroutine nseare(ns.cno.cm.iit.r) common trmax.av.co.ce.cp.ne.ci.cc.lit integer co.ce.cr.ci.cc integer cho integer ns(cne).iJ1(cne) dimension Fr(100) dimension r(cne) ·cm(cne) dimension f(100).tempx(100).dlavs(100).tempx1(100).sel(100) data f/100%0./ fnewv=365.*24. ft=fnewv*(10.**(-5))write (3.99) ne 99 format(2:: 'no. of equipments to be procured='.i5) write (3,209) lit 209 format(2x, 'expected no of failures in ',i2, 'wears') do 10 i=1.cne f(i)=ft*r(i)*lit*ne write(3.80) i. f(i) format(2x, 'mod. ', i3, '=', f7.3) 80 10 continue 70 avs=1. avmin=(av**(2./eno)) do 25 J=1.cno tempx(j)=0. 1 X='0 Pr(J)=exp(-f(J)) 35 tempx(i)=tempx(i)+pr(i) if (temps(j).se.avmin) so to 30 ix=ix+1 pr(J)=pr(J)*f(J)/in so to 35 30 ns(,i)=ix avs=tomes(J)*avs

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25

110

continue

do 50 J=1 cne

if (avs.de.av) do to 40

dlavs(j)=pr(j)*f(j)/(ns(j)+1)

```
sel(J)=dlavs(J)/cm(J)
50
        continue
        call maxim (sel.cno.k)
       temps(k)=temps(k)+dlavs(k)
        ns(k)=ns(k)+1
       avs=1.
       do 100 J=1 cne
       avs=tempx(J) kavs
100
          continue
       if(avs.de.av) do to 40
       so to 110
40
       write(3,45) (ns(j),j=1,cno)
        format(2x.*spares mix for this design*,20(i3.2x))
45
        write (3,88) avs
 88
       format(2x, system av.= , f8.5)
         return
       end
```

r 1052 0.346 0.072 8

er maxim.fortran

maxim.fortran 11/28/77 1056.7 est Mon

subroutine maxim(x,n,1) dimension x(n) tmax=x(1) if(n.le.1)return do 10 i=2.n if(x(i).le.tmax) so to 10 tmax=x(i) 1=i continue return end

er rshift.fortran

10

rshift.fortran 11/28/37 1059.3 est Mon

subroutine rshift(row,n) real row(n), temp temp is a temporary storage for first element to be shifted C temp=row(1) do 12 i=2+n row(i-1)=row(i) 12 continue row(n)=tem> return end

pr mshift.fortran

mshift.fortren 11/28/77 1058.7 est Mon

subroutine mshift(mat*n) inteser mat(100:100).trow(100) trow will store the first row to be shifted C do 113 i=1.n 113 trow(i)=mat(1,i) do 212 i=2:n do 212 J=1.n 212 mat(i-1.j)=mat(i.j) do 213 i=1.n 213 mat(n.i)=trow(i) to shift column do 313 j=1.n 313 trow(j)=mat(j.1) do 312 i=1:n do 312 J=2+n 312 mat(i,j-1)=mat(i,j) do 413 J=1.n 413 mat(j,n)=trow(j) return end

Pr minx.fortran

minx.fortran

11/28/77 1056.3 est Mon

function minx(x,n) integer x(n) minx=x(1) if(n .le. 1) return do 10 i=2.n 10 if(x(i) .lt. minx) minx=x(i) return end

APPENDIX 3: EXAMPLE OF USE OF MODULARIZATION PROGRAM

The user would create the data files shown on the following four pages.

All of the segments of the main program must be compiled and the data attached.

The following shows the instructions required for attaching the data files by the segment run. ec.

Pr run.ec

run.ec 11/29/77 1132.5 est Tue

io_call attach fileO1 vfile_ data_5
io_call attach fileO2 vfile_ data_2
io_call attach fileO7 vfile_ data_7
io_call attach fileO8 vfile_ data_8
io_call attach fileO9 vfile_ data_9
io_call attach fileO0 vfile_ data_10

main.pros

io_call detach fileO1
 io_call detach fileO2
io_call detach fileO7
io_call detach fileO8
io_call detach fileO9
io_call detach fileO

r 1132 0.252 0.932 42

data_2 11/29/77 1136.4 est Tue

40.1

r 1136 0.044 0.506 22

r 1512 0.037 0.006 2

pr data_7

data_7 10/02/77 1513.1 edt Sun

2 2 100 30 103 12 10

r 1513 0.039 0.002 1

pr data_8

data_8 10/02/77 1513.2 edt Sun

pr data_5

data_5 10/02/77 1510.7 edt Sun

1.										
,	100	31.	34.	20	. 1	3.	41.	41.	53.	28
	\c.	34.	48.	12	. 1	3.	34.	41.	11.	28
	\c.	28.	14.	29	. 4.	1.	37.	52.	49.	34
	\c.	15.	40.	29	. 4:	2.	51.	45.	22.	13
	\c.	44.	25.	39	. 4:	5.	55.	27.	22.	55
	\c.	43.	44.	40	. 1	4.	39.	50.	23.	30
	\c.	45.	32.	21	. 2:	3.	27.	18.	32.	51
	\c.	13.	51.	33	. 3-	4.	55.	25.	33.	22
	\c.	15.	53.	14	. 3:	3.	28.	23.	52.	14
	\c.	31.	53.	13	. 4:	5.	45.	48.	16.	11
	\c.	41.	50.	39	. 4	4.	43.	55.	50.	21
	\c.	24.	26.	34	. 3	7.	49.	29.	48.	23
	\c.	29.	35.	. 32	. 2	23.				
2.	١c.	120.	114	206	. 25	7.	88.	198.	190.	291
	١c.	245	203	276	. 21	8.	266.	116.	127.	238
	١c.	109.	101	141		91.	172.	86.	237.	287
	\c.	133.	120	. 150	. 27	76.	224.	114.	230.	165
	\c.	166	190	. 113	. 21	0.	267.	210.	291.	203
	١c.	113	297	. 170	. 11	2.	205.	136.	188.	183
	\c.	292	108	. 124	. 15	51.	219.	108.	224.	217
	١c.	257	135	. 185	16	66.	125.	87.	279.	174
	١c.	112	289	. 171	. 10	9.	275.	101.	275.	101
	١٠.	116	. 96	. 161	. 13	36.	188.	253.	181.	253
	۱۰.	180	. 258	. 285	5. 22	24.	128.	230.	280.	136
	١٠.	270	184	. 192	2. 21	3.	260.	260.	247.	182
		290			. 26	.2.				1
	0.0		0.015	0.019	0.015			0.011	0.018	0.018
	0.0		0.033	0.049	0.025				.021	0.028
	0.02		0.014	0.038	0.026	0.04		.015		0.012
	0.0	14	0.03	0.041	0.048	0.0	23	0.025	0.041	0.04
	0.0	3	0.037	0.038	0.041	0.012	0.	012	0.019	0.033
	0.0		0.032	0.022	0.043	0.025				0.011
	0.0		0.031	0.042	0.019	0.013			.017	0.039
	0.0		0.013	0.03	0.029	0.040				0.028
	0.04		0.038	0.034	0.038	0.0		0.024		0.017
	0.0		0.012	0.015	0.049	0.01				0.032
	0.0		0.045	0.026	0.03	0.034	0.	04 0	.038	0.032
	0.02	4	0.018	0.035	0.039					

r 1511 0.349 0.002 1

r 1513 0.248 0.002 1

pr data_9

data_9 10/02/77 1514.7 edt Sun

.85

r 1514 0.037 0.002 1

pr data_10

		data_10	10/02/77	1515.0 e	dt Sun		
.359	.322	.107	.341	.408	.181	.242	.364
. 254	.168	.182	.213	.142	.261	.413	.417
.103	.415	.267	.272	.1999	.446	.263	.179
.252	.429	.099	.362	.365	.387	.127	.087
.335	.402	.313	.353	.349	.450	.409	.107
.194	.210	.270	.299	.39	.233	.392	.180
.278	.162	.098	.332	.332	.331	.246	.222
.273	.388	.093	.100	.276	.329	.083	.222
.278	.162	.098	.332	.331	.426	.222	.331
.105	.235	.335	.298	.425	.394	.275	.115
.322	.234	.340	.417	.363	.179	.098	.353
.202	.315	.360	.447	.216	.172	.444	.348
.146	.187	. 254	. 270				

r 1515 0.127 0.006 2

The computer output for the network described by the data files is shown in the pages following those files. The first 20 lines are the login procedure where.

- Lines 1-9 --- standard login procedure
- Line 10 ----asks for the output device to be appended
- Line 12 ----type ec run to append input devices containing

 data files, run the program and then detach input

 devices.
- Line 20 ---begins the computation, to find the design starting from node 1.

BREDBERREABR

You are stateded from sreem-too quilit 1730.

Bresel 9567c0016 looked in the contribution of the contribut No m. 11.

iocall: Improver made specification for the device. user-i/o r 1130 1.562 13.310 115

- ((0) io attach file03 sam_ user_i/o r 1130 0.120 0.262 6
- (12) ec run io_call attach fileOf vfile_ data_5
 io_call attach fileOf vfile_ data_2 io_call attach file07 vfile. data_7 io_call attach file08 vfile_ data_8 io_call attach file09 vfile_ data_9 io_call attach file10 vfile_ data_10

main.prod

(20) network partitioning program

> input matrix should be 100 by 100 O starting node: 1 0 card no. 1 contains nodes: 0 1 2 3 4

ext. conn. = 21 27 int. conn. = st = -6 0 card no. 2 contains nomies: 0 5 42 96

25 ext. conn. = int: conn. = st = 25 0 card no. 3 contains nodes: 0 6 8 9 13

ext. conn. = 33 int. conn. = 25 st = 8 0 card no. 4 contains nodes: 0 7 12 17 18 21

54 ext. conn. = int. comm. = 35 st = 19

0 card no. 5 contains nodes: 0 10 11 15 16 20

ext. conn. = 35 int. com: = 38 st = -3 O card no. 6 contains nodes: 23 0 14 19 ext. conn. = 24 int. com. = st = 16

```
0 card no. 7 contains nodes: 0 22 81 86
ext. conn. = 33
int. conn. = 3
 st = 30
0 card no. 8 contains nodes: 0 24 29 33
ext. conn. = 35
int. conn. = 9
 st = 26
0 card no. 9 contains nodes: 0 25 39 44 45 49
 ext. conn. = 60
 int. conn. = 22
 st = 38
0 card no. 10 contains nodes:
0 26 27 28 31 32
 ext. conn. = 52
int. conn. = 46
 st = 6
O card no. 11 contains nodes:
0 30 34 78
ext. conn. = 58
int. conn. = 9
 st = 49
0 card no. 12 contains nodes:
0 35 66 73
ext. conn. = 31
int. conn. = 4
st = 27
0 card no. 13 contains nodes:
0 36 43 51
 ext. conn. = 37
 int. conn. = 15
 st = 22
O card no. 14 contains nodes:
0 37 41
 ext. conn. = 60.
 int. conn. =
 st = 53
0 card no. 15 contains nodes:
0 38 48 54 55 60
 ext. conn. = 47
int. conn. = 37
 st = 10
```

```
A contains nodes!
A 4 2 97
 est. conn. 51
 int. com.
 st = 51
0 card no. 17 contains nodes:
0 46 50 52 53 57
 ent. conn. = 80
int. conn. = 43
st = 37
0 card no. 18 contains nodes:
0 47 98 99 100
  ext. conn. = 51
int. com. = 14

st = 37

0 card no. 19 contains nodes:

0 56 62 63 69
ext. conn. = 61
int. conn. = 24
st = 37
0 caid no. 20 contains hodes:
0 58 59 64 65 70
  ext. conn. = 75
int. conn. = 37
  st = 38
 0 card no. 21 contains nodes:
0 61 91 95
 0
  ext. conn. = 36
  int. com. = 6
 st = 30
0 card no. 22 contains nodes:
0 67 71 72 74 75
 0
 ·ext. conn. = 53
  int. conn. = 29
 0 card no. 23 centains nodes:
0 69 77 82
  st = 24
 0
  ext. conn. = 53
  int. colm. = 10
 st = 43
0 card no. 24 contains nodes:
0 76 85 89 90
 0
   est. com. = 81
 int. com. 14

st = 67

0 card no. 25 contains nodes:

0 79 83 88 92
   ext. com. = 34
   int. com. = 28
   st = 6
```

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```
O card no. 26 contains nodes:
0 80 87 93 94
 ext. com. =
                  94
                   0
 int. conn. =
 st = 94
0 * * * * * run completed * * * * *
  expected total maintenance time=38.58499
     cost of mod. 1= cost of mod. 2=
                         338.000
                         365,000
     cost of mod. 3=
                         440.000
     cost of mod. 4=
                         498.000
     cost of mod. 5= cost of mod. 6=
                         450,000
                         386,000
     cost of mod. 7=
                         462,000
     cost of mod. 8= cost of mod. 9=
                         428.000
                         490,000
     cost of mod. 10=
                         496.000
     cost of mod. 11=
                         452,000
                         408.000
     cost of mod. 12=
     cost of mod. 13=
cost of mod. 14=
                         386.000
                          416.000
     cost of mod. 15=
                          476.000
     cost of mod. 16-
                         458,000
     cost of mod. 17=
                         550,000
     cost of mod. 18=
                          428.000
     cost of mod. 19=
                          506.000
     cost of mod. 20=
                          538.000
     cost of mod. 21=
cost of mod. 22=
                          446.000
                         498.000
     cost of mod. 23=
                         452.000
     cost of mod. 24=
                         538.000
     cost of mod. 25=
cost of mod. 26=
                          394.000
                          566.000
  total cost of the modules= 11866
  acquistion cost= 355980
  no. of equipments to be procured=
                                         30
  expected no of failures in 10sears
  mod. 1= 29.670
        2= 25.386
  mod.
  mod.
        3= 24.729
        4= 30.824
  mod.
  mod.
       5= 38.159
  mod.
       6= 20.787
  mod.
        7= 24.887
  mod. 8= 23.100
  mod. 9= 42.784
  mod. 10= 29.013
  mod. 11= 31.089
  mod. 12≈ 15.242
  mod. 13= 18.948
  mod. 14= 14.270
  mod. 15= 34.348
  mod. 16= 17.608
  mod. 17= 35.005
  mod. 18= 29.223
  mod. 19= 25.386
  mod. 26: 36.076
                                      THIS PAGE IS BEST QUALITY PRACTICABLE
  mod. 21≈ 28.382
                                      FROM COPY FURNISHED TO DDC
```

```
mod. 200 King
                                     THIS PAGE IS BEST QUALITY PRACTICABLE
  mod. 23 26.017
mod. 21 30.998
mod. 25 37.186
                                     FROM COPY FURNISHED TO DDC
  moo. 24- 15.794
  scares min for this design 43 45 32 44 53 32 37 35 58 45
Ne44 25 37 30 48 28 49 42 37 51
41 45 38 44 52 25
system av.= 0.85257
  total cost for the seares requirement: 14595420
  support cost= 14601218
  the cost of this desidn is= 14957198
O starting node: 2
0 card no. 1 contains nodes:
0 2 7 12 17 18
int. conn. = 47
st = 15
ext. comm. =
st = 15
0 card no. 2 contains nodes:
0 1 3 4 5 6
0
 ext. conn. = 32
 int. conn. = 27
st = 5
0 card no. 3 contains nodes:
0 8 42 87 96
ext. comm. = 39
 int. comm. =
st = 34
0 card no. 4 contains nodes:
0 9 14 23
ext. comm. = 21
int. conn. = 11
 st = 10
0 card no. 5 contains nodes:
0 10 11 15 16 20
ext. conn. =
                   38
 st = -3
0 card no. 6 contains nodes: 0 13 19 22
ext. conn. = 44
int. conn. = 5
 st = 39
0 card no. 7 contains nodes:
0 21 25 81 86
 ext. com. = 59
                10
 int. conn. =
 st = 49
0 card no. 8 contains nodos:
0 24 29 33
 ext. conn. = 35
int. conn. = 9
```

44

st = 26

```
0 card no. 9 contains notes:
0 26 27 28 31 32
ext. conn. = 52
int. conn. = 46
 st = 6
0 card no. 10 contains nodes:
0 30 34 39 44 45
0
ext. conn. = 65
int. conn. = 35
st = 30
0 card no. 11 contains nodes:
0 35 78 82
 ext. conn. = 35
int. conn. = 4
st = 31
0 card no. 12 contains nodes:
0 36 43 51
 ext. conn. = 37
int. conn. = 15
 st = 22
O card no. 13 contains nodes:
0 37 41
 ext. conn. = 60
int. conn. = 7
st = 53
0 card no. 14 contains nodes:
0 38 48 54 55 60
ext. conn. = 47
int. conn. = 37
st = 10
0 card no. 15 contains nodes:
0 40 66 73
 ext. conn. = 44
st = 40
0 card no. 16 contains nodes:
0 46 50 52 53 57
 int. conn. =
 ext. conn. = 80
int. conn. = 43
st = 37
0 card no. 17 contains nodes:
0 47 84 93 97
  ext. comm. =
  int. conn. = 36
                      8
```

```
0 49 98 99 100
                                        THIS PAGE IS BEST QUALITY PRACTICABLE
                                        FROM COPY FURNISHED TO DDC
 ext. comm. = 43
int. comm. = 14
0 card no. 19 contains nodes:
0 56 62 63 68
 st = 29
                 61
 ext. conn. =
 int. conn. =
                   24
st = 37
0 card no. 20 contains nodes;
0 58 59 64 65 70
 ext. conn. = 75
                   37
 int. conn. =
0 card no. 21 contains nodes:
0 61 91 95
 ext. conn. = 36
 int. conn. =
st = 30
0 card no. 22 contains nodes:
0 67 71 72 74 75
0
                   53
 ext. com. =
 int. conn. =
                  29
st = 24
0 card no. 23 contains nodes:
0 69 77 88 92
0
                  69
 ext. conn. =
                    17
 int. conn. =
 st = 52
0 card no. 24 contains nodes:
0 76 85 89 90
 ext. conn. = 81
                   14
 int. conn. =
st = 67
0 card no. 25 contains nodes:
0 79 80 83 94
0
  ext. conn. = 78
 int. com. = 14
 st = 64
 O * * * * * * run completed * * * *
   expected total maintenance time-30 03778
     cost of mod. 1= 444.000
cost of mod. 2= 528.600
cost of mod. 3= 426.000
cost of mod. 4= 328.000
      cost of mod. 5=
                             406.000
      cost of med. 5=
cost of med. 2=
cost of med. 8=
                             450.000
                             602.000
                             340.000
```

```
cost of mod. .
                         552 000
     cost of med. 10-
                          640 000
                                           THIS PAGE IS BEST QUALITY PRACTICABLE
     cost of mod. 11-
                          370,000
     cost of mod. 12=
                          358,000
                                           FROM COPY FURNISHED TO DDC
     cost of mod. 13-
                          342.600
     cost of mod. 14=
                          604.000
     cost of mod. 15-
                          408,000
                          540.000
     cost of mod. 16=
     cost of mod. 17=
                          462.000
     cost of mod. 18=
                          422,000
     cost of mod. 19=
                          414,000
     cost of mod. 20-
                          624.000
     cost of mod. 21=
                          342,000
     cost of mod. 22=
                          473.000
     cost of mod. 23=
                          526.000
     cost of mod. 24=
cost of mod. 25=
                          582.000
                          544.000
  total cost of the modules= 11762
  acquistion cost= 352860
  no. of equipments to be procured=
                                         30
  exsected no of failures in 10sears
  mod. 1= 34.033
  mod. 2= 36.687
mod. 3= 26.806
mod. 4= 20.446
  mod. 5= 38.159
  mod. 6= 22.469
mod. 7= 25.042
  mod. 8= 23.100
  mod. 9= 29.013
  mod. 10= 49.590
  mod. 11= 24.729
  mod. 12= 18.948
  mod. 13= 14.270
  mod. 14= 34.348
  mod. 15= 9.829
  mod. 16= 35.005
  mod. 17= 30.774
  mod. 18= 26.227
  mod: 19= 25.386
  mod. 20= 36.976
  mod. 21= 28.382
  mod. 22= 32.088
  mod. 23= 40.892
mod. 24= 30.958
  mod. 25= 23.705
spares mix for this design 48 51 39 34
\c38 32 27 48 22 49 44 38 37
41 45 56 44 35
                                                                      39
                                                     53
                                                         34 37
                                                                           42
                                                                                 66
  system av.= 0.85195
  total cost for the spares requirement= 15211860
  support cost= 15217435
  the cost of this design is= 15570295
O starting node: 3
0 card no. 1 contains nodes: 0 1 2 3 4
0
 ext. conn. ≠
 into como
 st = -6
o cord no.
             2 contains nodes!
             96
    5 42
.0
 ext. conn. =
                  25
 int. com. =
 st = 25
```

```
0 card no. 3 contains nodo::
 ext. com. = 33
 int. conn. = 25
 st = 8
0 card no. 4 contains nodes:
0 7 12 17 18 21
 ext. com: = 54
 int. conn. = 35
 st = 19
0 card no. 5 contains nodes:
0 10 11 15 16 20
 ext. conn. = 35
 int. conn. = 38
st = -3
0 card no. 6 contains nodes:
0 14 19 23
 ext. conn. = 24
int. conn. = 8
st = 16
0 card no. 7 contains nodes:
0 22 81 86
 ext. conn. = 33
int. conn. = 3
 st = 30
0 card no. 8 contains nodes: 0 24 29 33
 ext. conn. = 35
int. conn. = 9
st = 76
0 card no. 9 contains nodes:
0 25 39 44 45 49
 ext. conn. = 60
int. conn. = 22
 st = 38
O card no. 10 contains nodes:
0 26 27 28 31 32
0
 ext. conn. = 52
int. conn. = 46
st = 6
O eard no. 11 contains nodes:
0 30 34 78
ext. conn. = 58
0 Cord no. 12 contains nodes:
6 35 66 73
ext. conn. = 31
int. conn. = 4
st = 27
```

```
0 card no. 13 contains makes!
0 36 13 51
 ext. com. = 37
int. com. = 15
 st = 22
O card no. 14 contains nodes:
0 37 41
ext. conn. = 60
 int. conn. =
st = 53
0 card no. 15 contains nodes;
0 38 48 54 55 60
 ext. conn. = 47
int. conn. = 37
 int. conn. =
 st = 10
0 card no. 16 contains nodes:
0 40 84 97
 ext. conn. = 51
int. conn. = 0
 st = 51
0 card no. 17 contains nodes: 0 46 50 52 53 57
ext. conn. = 80
 int. conn. = 43
st = 37
0 card no. 18 contains nodes:
0 47 98 99 100
ext. comn. = 51
int. conn. = 14
 st = .37
0 card no. 19 contains nodes:
0 56 62 63 68
ext. conn. = 61
int. conn. = 24
st = 37
0 card no. 20 contains nodes:
0 58 59 64 65 70
ext. conn. = 75
int. conn. = 37
st = 38
0 card no. 21 contains nodes:
0 61 91 95
0
0
                36
 ext. conn. =
 int. comm. =
```

st = 30

THIS PAGE IS BEST QUALITY PRACTICABLE

```
O card no. 22 contains nodes:
0 67 71 72 74 75
ext. conn. = 53
int. conn. = 29
st = 24
0 card no. 23 contains nodes:
0 69 77 82
0
ext. conn. = 53
int. conn. = 10
 st = 43
O card no. 24 contains nodes:
0 76 85 89 90
ext. conn. = 81
int. conn. = 14
st = 67
O card no. 25 contains nodes:
0 79 83 88 92
 ext. conn. = 34
int. conn. = 28
st = 6
0 card no. 26 contains nodes:
 0 80 87 93 94
 ext. conn. = 94
 int. conn. = 0
 st = 94
 0 * * * * * run com > 1 e t e d * * * * *
 expected total maintenance time=41.65934
   design not feasible
 r 1405 16.939 3.424 164 level 4, 33
 logout
 Biesel 9567c0016 lossed out 11/25/77 1405.9 est Fri
 CPU usase 33 sec, memory usase 61.1 units.
 hangup
```