

AD-A061 413

NAVAL POSTGRADUATE SCHOOL MONTEREY CALIF
MEASURING SHALLOW WATER WAVES WITH PRESSURE SENSORS.(U)
SEP 78 V M GONCALO

F/G 8/3

UNCLASSIFIED

NL

1 OF 1

AD
A061413



END
DATE
FILMED
1-79
DDC

② LEVEL II
NA

NAVAL POSTGRADUATE SCHOOL

Monterey, California

DDC FILE COPY AD A061413



DDC
RECEIVED
NOV 21 1978
B

THESIS

MEASURING SHALLOW WATER WAVES
WITH PRESSURE SENSORS
by
Vitor Manuel Henriques Goncalo
September 1978
Thesis Advisor: Edward B. Thornton

Approved for public release; distribution unlimited

78 11 13 071

UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM
1. REPORT NUMBER	2. GOVT ACCESSION NO.	3. RECIPIENT'S CATALOG NUMBER
4. TITLE (and Subtitle) ⑥ MEASURING SHALLOW WATER WAVES WITH PRESSURE SENSORS		5. TYPE OF REPORT & PERIOD COVERED ⑧ Master's Thesis, September 1978
7. AUTHOR(s) ⑩ Vitor Manuel Henriques / Goncalo		6. PERFORMING ORG. REPORT NUMBER
9. PERFORMING ORGANIZATION NAME AND ADDRESS Naval Postgraduate School Monterey, California 93940		8. CONTRACT OR GRANT NUMBER(s)
11. CONTROLLING OFFICE NAME AND ADDRESS Naval Postgraduate School Monterey, California 93940		10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS
14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office) Naval Postgraduate School Monterey, California 93940		12. REPORT DATE ⑪ September 1978
		13. NUMBER OF PAGES 66
		15. SECURITY CLASS. (of this report) Unclassified
		15a. DECLASSIFICATION/DOWNGRADING SCHEDULE
16. DISTRIBUTION STATEMENT (of this Report) Approved for public release; distribution unlimited ⑫ 67 p.		
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)		
18. SUPPLEMENTARY NOTES		
19. KEY WORDS (Continue on reverse side if necessary and identify by block number) wave staff Bernoulli equation pressure sensor flowmeters water particle velocity orthogonal components		
20. ABSTRACT (Continue on reverse side if necessary and identify by block number) For two locations within the surf zone sea surface elevations were observed using a wave staff and a pressure sensor while simultaneously the two horizontal orthogonal components, u and v, of water particle velocity were measured. Surface elevations derived from pressure sensors are lower, mainly in the region of the crest, compared with the same surface elevations measured with wave gages. Pressure records are more smoothed than wave gage records, and the energy computed for waves		

DD FORM 1473
1 JAN 73

EDITION OF 1 NOV 68 IS OBSOLETE
S/N 0102-014-6601

254
1

450

UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

measured with a pressure sensor is consistently smaller than for waves measured with a wave gage.

Methods for converting pressure to surface elevation are given which include the non-linear velocity term ($u^2 + v^2$) which is usually neglected in the Bernoulli equation. Two techniques are proposed to include this term: 1) flowmeters are used to measure u and v , and 2) the Bernoulli term is derived by determining the velocities by convolving the pressure records using a weighting function determined from shallow water theory.

The first technique gave improvements on the order of 3.4% to 7.8% of the total variance of the wave gage spectrum, whereas the second technique gave improvements on the order of 3.1% to 9.7%. The improvements in both cases are approximately the same, with the second technique having the advantage of requiring only a pressure transducer.

59
U 58 + 1 58

ACCESSION for		
NTIS	White Feather <input checked="" type="checkbox"/>	
ODC	Soft Section <input type="checkbox"/>	
UNANNOUNCED	<input type="checkbox"/>	
JUSTIFICATION		
BY		
DISTRIBUTION/AVAILABILITY NOTES		
Dist. AVAIL. and/or SPECIAL		
A		

DD Form 1473
1 Jan 73
S/N 0102-014-6601

UNCLASSIFIED

2 SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

Approved for public release; distribution unlimited.

MEASURING SHALLOW WATER WAVES WITH PRESSURE SENSORS

by

Vitor Manuel Henriques Goncalo
Lieutenant, Portuguese Navy


Submitted in partial fulfillment of the
requirements for the degree of

MASTER OF SCIENCE IN METEOROLOGY AND OCEANOGRAPHY

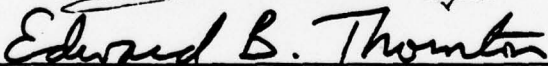
from the

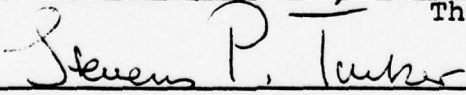
NAVAL POSTGRADUATE SCHOOL
September 1978

Author

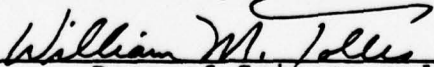


Approved by:


_____ Thesis Advisor


_____ Reader


_____ Chairman, Department of Oceanography


_____ Dean of Science and Engineering

ABSTRACT

For two locations within the surf zone sea surface elevations were observed using a wave staff and a pressure sensor while simultaneously the two horizontal orthogonal components, u and v , of water particle velocity were measured.

Surface elevations derived from pressure sensors are lower, mainly in the region of the crest, compared with the same surface elevations measured with wave gages. Pressure records are more smoothed than wave gage records, and the energy computed for waves measured with a pressure sensor is consistently smaller than for waves measured with a wave gage.

Methods for converting pressure to surface elevation are given which include the non-linear velocity term (u^2+v^2) which is usually neglected in the Bernoulli equation. Two techniques are proposed to include this term: 1) flowmeters are used to measure u and v , and 2) the Bernoulli term is derived by determining the velocities by convolving the pressure records using a weighting function determined from shallow water theory.

The first technique gave improvements on the order of 3.4% to 7.8% of the total variance of the wave gage spectrum, whereas the second technique gave improvements on the order of 3.1% to 9.7%. The improvements in both cases are approximately the same, with the second technique having the advantage of requiring only a pressure transducer.

78⁴ 11 13 071

TABLE OF CONTENTS

I.	INTRODUCTION-----	9
	A. HISTORICAL PERSPECTIVE-----	9
	B. OBJECTIVE-----	12
II.	MEASUREMENTS-----	13
	A. EXPERIMENT SITES-----	13
	B. INSTRUMENTATION-----	14
	1. Capacitance Wave Gage-----	14
	2. Resistance Wave Gage-----	15
	3. Flowmeters-----	16
	4. Pressure Transducer-----	16
III.	ANALYSIS OF DATA-----	17
IV.	THEORY-----	19
V.	RESULTS-----	23
	A. QUALITATIVE AND QUANTITATIVE DESCRIPTION OF THE OBSERVED DATA-----	23
	B. SURFACE ELEVATION SPECTRUM CALCULATED FROM PRES- SURE SPECTRUM USING LINEAR TRANSFER FUNCTION (STANDARD TECHNIQUE)-----	30
	C. SURFACE ELEVATION SPECTRUM CALCULATED FROM PRESSURE SPECTRUM INCLUDING THE BERNOULLI TERM---	32
	1. Bernoulli Term Calculated Using Measured Velocities-----	32
	2. Bernoulli Term Calculated by Convolving Pressure Records-----	38
	3. Comparing Variances-----	41
VI.	CONCLUSIONS-----	43

APPENDIX A - BEACH PROFILES-----	46
APPENDIX B - CALIBRATION FACTORS-----	48
APPENDIX C - POWER, COHERENCE AND PHASE SPECTRA-----	49
APPENDIX D - TABLES OF SURFACE ELEVATION SPECTRA-----	61
BIBLIOGRAPHY-----	64
INITIAL DISTRIBUTION LIST-----	65

LIST OF TABLES

I.	VARIANCE, STANDARD DEVIATION, SKEWNESS AND KURTOSIS FOR ALL DATA-----	26
II.	MEAN WATER LEVELS-----	27
III.	SURFACE ELEVATION SPECTRA FOR 19 JULY EVENING-----	33
IV.	SURFACE ELEVATION SPECTRA FOR 8 MARCH-----	37
V.	COMPARISON SURFACE ELEVATION VARIANCES-----	42

LIST OF FIGURES

1. Pressure and Staff Elevations (Van Dorn, 1977)-----11
2. Wave surface elevations measured by the wave staff
compared with hydrostatic pressure head-----24
3. Mean water depth given by the wave gage and by the
pressure sensor, 19 July (evening)-----29
4. Power, Coherence and Phase Spectra for 19 July evening-
Standard Technique-----31
5. Power, Coherence and Phase Spectra for 19 July evening-
First Technique-----34
6. Measured and Computed Velocity Vectors, 19 July evening--36
7. Comparison of Measured and Calculated $u^2 + v^2$ Spectra----39
8. Power, Coherence and Phase Spectra for 19 July evening---40

I. INTRODUCTION

A. HISTORICAL PERSPECTIVE

In studying shallow water and breaking waves, many theoretical and practical problems are encountered. Analytical wave theories do not correctly characterize the physics of wave breaking. The environment is neither friendly nor easily reproduceable in a laboratory. A primary problem that is encountered is how to measure the wave height at or near the breaking point. In general, the two basic types of sensors used to measure the surface elevations have been subsurface pressure sensors and surface piercing wave gages.

The use of pressure sensors to infer surface elevation is particularly desirable as a means of conveniently measuring breaking waves, especially high energy waves. Pressure sensors have been used more commonly because, compared with surface piercing gages, they are rugged, less vulnerable to environmental hazard, and easier to install; in many locations, pressure sensors are the only feasible means of measuring the waves.

The conventional procedure used to infer surface elevation from a pressure signal is to calculate the energy density spectrum of a pressure record and to apply a spectral transfer function derived from linear theory. The pressure pulse is attenuated with depth, with the attenuation increasing with wave frequency. Hence, the spectral transfer function is dependent on frequency and depth.

Esteva and Harris (1970) compared results from a wave staff and a pressure transducer in 16 feet of water. The pressure spectrum was compensated using linear wave theory to obtain the transfer function. The computed surface energy density spectrum was then summed over all components and the compensated root mean square of the total energy determined; this procedure led to good estimates of wave heights from pressure records as compared with those determined from surface records. However, a number of investigators have found discrepancies using the linear transfer function in intermediate to shallow water. Takahashi et al. (1967), Glukhovski (1961), Shooter and Ellis (1967), Gerhardt et al. (1955), suggest several different multiplicative correction factors to the linear transfer function for various conditions. In general the correction factors decrease with decreasing period, being greater than 1.0 for long-period waves and less than 1.0 for short-period waves (Shore Protection Manual, U. S. Army, Corps of Engineers, 1975).

Near or at breaking, linear wave theory no longer is applicable, and using the linear transfer function does not give as good an approximation. Van Dorn (1977), in a laboratory study of breaking waves, found that surface elevations computed from pressure sensors were correctly measured in the troughs but were substantially less under the wave crests. At the crests, the surface elevations were sometimes 50 per cent too low as compared with wave staff measurements (Figure 1). The discrepancy between pressure and wave staff measurements is caused by a dynamic pressure reduction due to the increased velocities

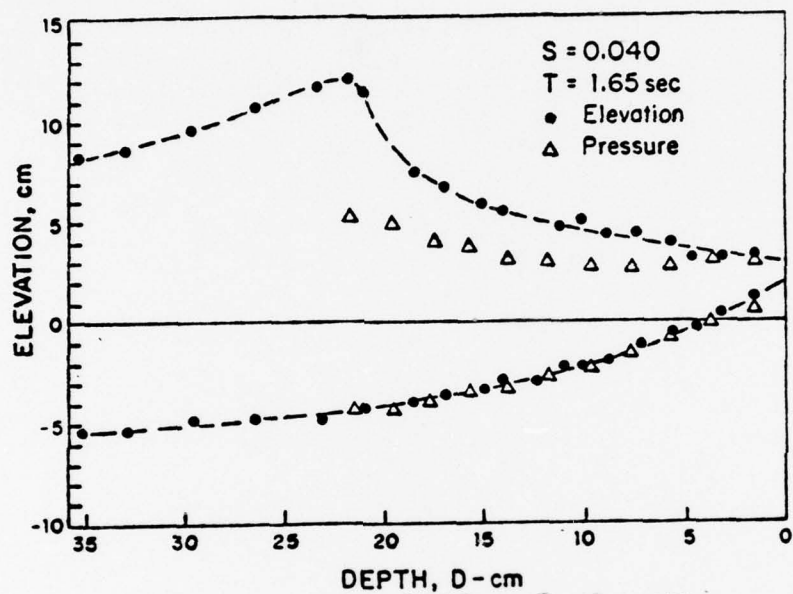


Figure 1. Hodographs of maximum and minimum waves elevations as an individual wave moves toward shore. Pressure and staff elevations agree under troughs, but peak pressure is clearly a poor indication of crest elevation. (S is beach slope)
 From Van Dorn (1977)

under the crests of breaking waves. Hence, the pressure records are much smoother and rounded off at the crests as compared with the surface staff measurements (Thornton et al., 1976).

B. OBJECTIVE

The objective of this research is to improve techniques for inferring surface elevations from the pressure sensors records and to test the techniques in the field under breaking waves.

Pressure is converted to surface elevation by including the non-linear velocity term which is usually neglected in the Bernoulli equation. Two techniques are proposed for including the Bernoulli term:

1. The Bernoulli term can be measured directly using flowmeters.
2. The Bernoulli term can be derived by convolving the pressure records to determine the velocities using shallow water linear theory. This technique has the advantage of requiring only pressure sensors.

Both techniques are equivalent to a second order perturbation scheme which includes the neglected non-linear term.

II. MEASUREMENTS

A. EXPERIMENT SITES

For two locations within the surf zone sea surface elevations were observed using a wave staff and a pressure sensor while simultaneously the two horizontal orthogonal components, u and v , of water particle velocity were measured. The data used in this paper were measured at Del Monte Beach and Scripps Beach, California.

Experiments were conducted at Del Monte Beach within Monterey Bay on 8 March 1978. The waves at this location were plunging-spilling breakers. Because of topographic sheltering and severe directional filtering due to refraction by the geometry of the bay, the waves offshore were narrow band swell type waves which impinged perpendicular to the shore; hence, a simplification to a two dimensional narrowbanded wave description is allowed. The median grain size is approximately 0.2 mm (taken at the water line) and the beach slope varied between 1:14 and 1:40.

Experiments were conducted at Scripps Beach at La Jolla on 19-20 July 1978, during the morning and evening of each day. Scripps Beach has an approximately planar 1:80 slope. The median grain size was 0.1 mm. Spilling breakers predominated.

A typical beach profile for each experiment is shown in Appendix A.

B. INSTRUMENTATION

During the Del Monte Beach experiments, the instruments used were a capacitance wave gage, two Marsh-McBirney model 721 electromagnetic current meters and a Statham model PA506 pressure transducer.

Measurements at Scripps Beach were made using a resistance wire wave gage, one Marsh-McBirney model 512 flowmeter and the same pressure sensor used at Del Monte Beach.

1. Capacitance Wave Gage

The capacitance wave gage was fashioned from 3/8-inch outside diameter stainless steel rod. The rod was tightly covered with 1/16-inch wall thickness polypropylene tubing. The gage operates on the principle that a change in the plate dimension of a capacitor changes its capacitance and consequently an output voltage. The insulated steel rod and seawater act as the plates, the insulation functioning as the dielectric. As the surface elevation fluctuates, the capacitance of the circuit changes, and the output voltage responds linearly. These output voltage fluctuations were sensed by a transistorized circuit powered from the beach. The circuit was designed by McGoldrick (1969). The electronics package was housed in a watertight brass case which was mounted on a tower during the 8 March experiment. This allowed the connecting leads to be less than 30 cm long, thereby minimizing wire-to-wire capacitance. The gage was statically calibrated

in the laboratory prior to the experiment. Accuracy was estimated to .005 m. For all experiments, the calibration factors are shown in Appendix B.

2. Resistance Wave Gage

The resistance wave gage is a surface-piercing, dual-wire, resistance sensor. The wave staff wires were mounted on a 1.5-inch outside diameter, 1/8-inch wall fiberglass fishing pole of 5-m length, epoxied into an aluminum flange at the bottom. The two resistance wires are 22 gage nichrome, attached to a PVC collar at the top of the pole and to the flange at the bottom. The wires are 4 inches apart over their entire length. A twisted-pair cable running inside the fiberglass pole connects the upper ends of the wires and provides the electrical connection between the instrument package and the sensor wires. The gage operates on the principle that the total resistance measured between the nichrome wires at the top is proportional to the length of the exposed (not immersed) wire. The wires are the unknown resistance in an AC circuit, whose output is linearly related to the length of the exposed wire.

The wave gage was designed and built by the Shore Processes Laboratory at Scripps Institution of Oceanography at La Jolla, California; field and laboratory tests have shown it to be durable both inside and outside of the surf zone, easily installed and operated, and highly linear. The instrument has a resolution of a few millimeters, accuracy better than one centimeter, negligible long-term drift and excellent temperature stability and frequency response.

3. Flowmeters

The flowmeters used were Marsh-McBirney Models 721 and 512 Electromagnetic current meters. The flowmeter operation is based on Faraday's principle of electromagnetic induction. Each probe measures water particle velocity in two orthogonal directions through a range of zero to three meters per second, with a maximum output error of two percent. The flowmeters were dynamically calibrated with an oscillating platform attached to an eccentric arm drive by a variable speed motor. Measurement accuracy was determined to be $\pm .02$ m/sec during calibration.

4. Pressure Transducer

The pressure sensor used was a Gould Statham Model PA506 thin film strain gage. The sensing element is a vacuum-deposited resistive balanced fully active strain gage bridge with an output voltage responding linearly to the water depth. The sensor measures absolute pressure rather than relative, therefore variations in atmospheric pressure occurring during the experiments and or during calibrations will slightly influence the apparent mean water depth measured. The instrument has a resolution of few millimeters and a pressure range from 3 to 20 psi. The pressure sensor was statically calibrated in the laboratory prior to the experiments and measurement accuracy was determined to be $\pm .005$ m.

III. ANALYSIS OF DATA

Continuous time series records of all measurements were collected within an hour or two on both the ebb and flow sides of high tide. Analogue records were made on both magnetic tape and strip charts.

The data were digitized at .2-sec intervals resulting in a Nyquist frequency of 2.5 Hz for the March experiment and at .25-sec intervals resulting in a Nyquist frequency of 2.0 Hz for the July data. This sampling rate was sufficiently high to avoid aliasing of energy into the portion of the spectra which was of interest.

A mean value was computed for all data sets and the data were linearly detrended to remove tidal effects. Variance, standard deviation, skewness and kurtosis of the distributions were computed. Because the record lengths were slightly different for each run, there is a small difference in the frequency resolution for each run.

The power spectra of the wave gage and pressure sensor were calculated by using the Fast Fourier Transform (FFT) technique. A section of the record approximately 35 minutes long was used to calculate the power spectra. The 35 minutes were chopped into 20 blocks. Spectral estimates were obtained using the FFT were ensemble averaged over the 20 intervals resulting in approximately 40 degrees of freedom for each spectral estimate.

A data window was applied to each interval to minimize leakage. The data window used was a cosine square taper function over the first and last 5% of the record.

Cross-spectra were computed between the wave and pressure records in the form of co- and quad-spectra. Coherence and phase spectra were then determined from the cross-spectra. Coherence and phase spectra as a function of frequency indicate the regions and degree of linear relationship and phase between the wave gage and pressure sensor data.

IV. THEORY

Assuming an irrotational, incompressible flow, a velocity potential ϕ exists and is described as:

$$u = - \frac{\partial \phi}{\partial x} \quad v = - \frac{\partial \phi}{\partial y} \quad w = - \frac{\partial \phi}{\partial z} \quad (1)$$

where u , v and w are the velocity components in the horizontal and vertical directions respectively. Since the mean hydrostatic pressure is constant, only the pressure fluctuations about the mean, Δp , are of concern. The pressure fluctuations are described by the Bernoulli theorem as:

$$\Delta p (t) = \rho \frac{\partial \phi}{\partial t} - \frac{1}{2} \rho (u^2 + v^2 + w^2) \quad (2)$$

where ρ is density. The first term on the right is the pressure due to the wave form expressed in terms of the velocity potential and the second term is the contribution to Δp due to the kinetic energy of the water motion induced by the passage of the wave. The second term on the right will be referred to hereafter as the Bernoulli term.

In deep water, the non-linear Bernoulli term can generally be neglected and the solution for linear theory is:

$$\Delta p (\sigma, t) = \rho g \frac{\cosh k(d + z)}{\cosh kd} \quad \eta(\sigma, t) = \frac{1}{H(\sigma)} \eta(\sigma, t) \quad (3)$$

where $H(\sigma)$ is the linear spectral transfer function relating pressure to the surface $\eta(t)$, and σ is the radial frequency. In the spectral domain

$$S_{\eta}(\sigma) = |H(\sigma)|^2 S_{\Delta p}(\sigma) \quad (4)$$

In shallow water and in the vicinity of the breaker point, the contribution to Δp by the Bernoulli term becomes important. Confining the discussion to shallow water waves, w is at least one order of magnitude less than u and v (making w^2 very small compared to u^2 and v^2), so that the contribution that w makes to the Bernoulli term can be neglected. In shallow water, the ratio of the means of the two terms on the right hand side of (2) with pressure meter located on the bottom is (Kinsman, 1965):

$$\frac{\overline{u^2 + v^2}}{\overline{\left| \frac{\partial \phi}{\partial t} \right|}} \approx \frac{\pi a}{4d} \quad (5)$$

where a is the amplitude and d is the depth. Substituting the saturation relationship at breaking for solitary wave theory:

$$a = .39 d \quad (6)$$

into (5) shows the ratio at breaking can become as large as 30%.

Two techniques for converting pressure to surface elevation are proposed which include the Bernoulli term. Starting with (2) and including the Bernoulli term,

$$\Delta p (\sigma, t) = \frac{1}{H(\sigma)} \eta (\sigma, t) - \frac{\rho}{2} (u^2 + v^2) \quad (7)$$

or

$$\begin{aligned} \eta (\sigma, t) &= H(\sigma) [\Delta p (\sigma, t) + \frac{\rho}{2} (u^2 + v^2)] \\ &= H(\sigma) f (\sigma, t) \end{aligned} \quad (8)$$

In the first technique proposed, u and v are measured in the field with electromagnetic flowmeters and the Bernoulli term computed and added to the differential pressure. The spectrum of the surface elevation is calculated from the combined time series

$$S_{\eta} (\sigma) = |H(\sigma)|^2 S_f (\sigma) \quad (9)$$

The second technique requires only a pressure measurement. The velocity used in the Bernoulli term is calculated by convolving the pressure record

$$u(t) = \int_{-\infty}^{+\infty} h(\tau) \Delta p (t - \tau) \quad (10)$$

where the weighting function $h(\tau)$ is given by the Fourier transform of the transfer function

$$h(\tau) = \int_{-\infty}^{+\infty} H(\sigma) e^{i2\pi f\tau} d\sigma \quad (11)$$

The transfer function derived from linear theory can be used as a first approximation. For shallow water waves, the pressure is essentially hydrostatic and the waves are non-dispersive. Hence, the transfer function is independent of frequency and the weighting function is independent of time.

The velocity is easily calculated for this simplified case as:

$$u(t) = \frac{\sigma}{k\rho g} \Delta p = c \frac{\Delta p}{\rho g} \quad (12)$$

where celerity, c , is given as a first approximation by:

$$c = \frac{\sigma}{k} = \sqrt{gh} \quad (13)$$

V. RESULTS

A. QUALITATIVE AND QUANTITATIVE DESCRIPTION OF THE OBSERVED DATA

Due to the similarity of the spectral shapes of the various analysed data the discussion of results will be exemplified by the data of 19 July evening. Except as were noted, the 19 July evening results are representative of the other data. Appendix C contains the spectra calculated for all experiments.

Surface elevations measured using the wave staff are compared in Fig. 2 to the hydrostatic pressure head and the hydrostatic pressure head including the Bernoulli term.

The pressure sensor and wave staff records generally agree in areas near the wave trough, but the pressure sensor underestimates the region near the crest as shown in Fig. 2. The results are in accord with the laboratory study of Van Dorn (1977). Referring to Eq. 2, the hydrostatic pressure fluctuations under crests and troughs is given by:

$$\Delta p = \rho g \eta - \frac{1}{2} \rho (u^2 + v^2) \quad (14)$$

The second term on the right hand side of Eq. 14, i.e., the Bernoulli term, is always a reduction in pressure relative to hydrostatic; since u and v become maximum under crests and minimum at the troughs, the Δp term is more reduced under the crests than at the troughs relative to hydrostatic.

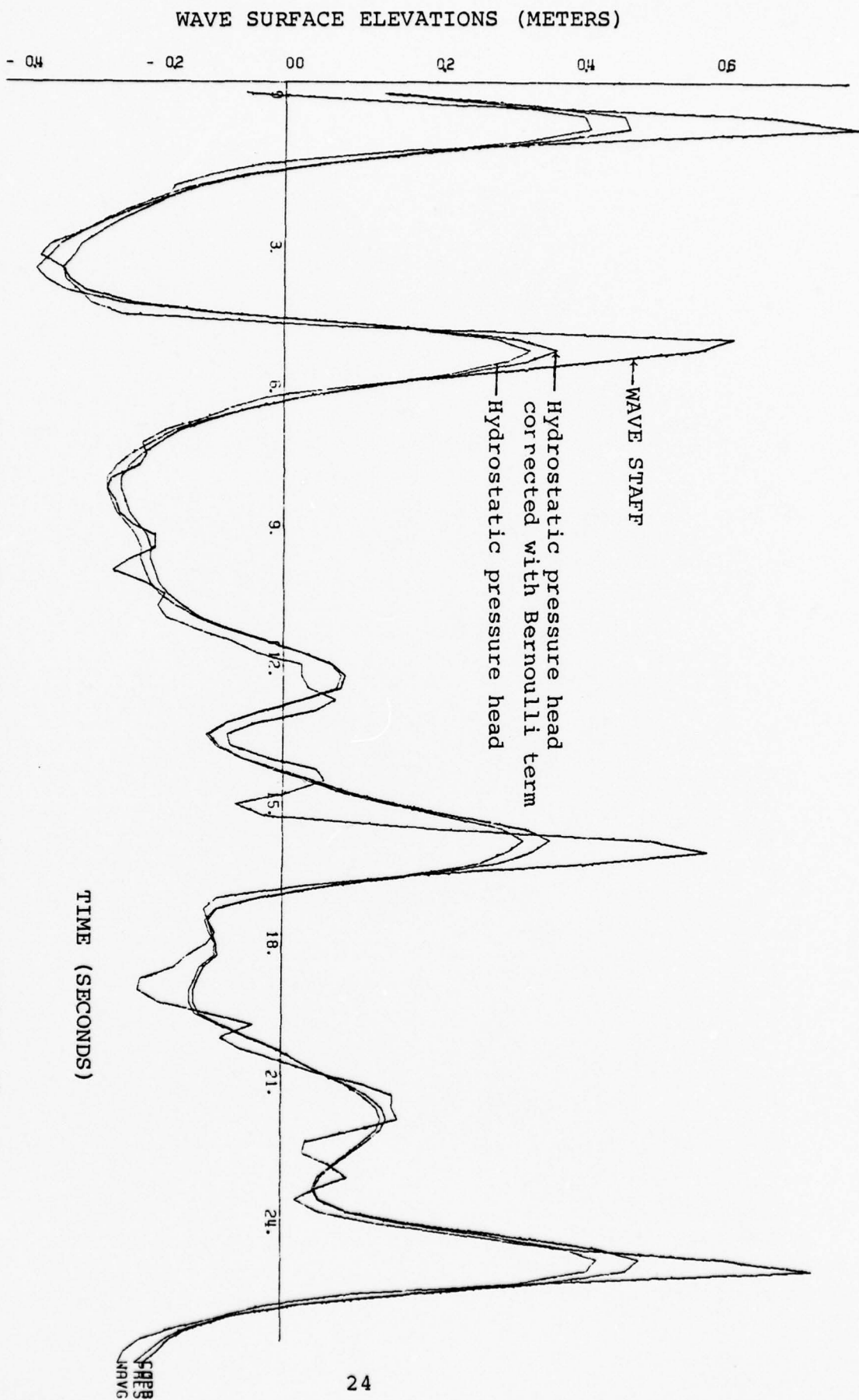


Figure 2. Wave surface elevations measured by the wave staff compared with hydrostatic pressure head.

The sea surface given by the wave staff and the hydrostatic pressure head were found to have positive skewness and kurtosis, with larger values for the wave staff distribution. Larger values of positive skewness imply that the wave staff indicates larger heights for the crests. Larger kurtosis for the wave staff indicates, as expected, more peaked crests than observed by the hydrostatic pressure head.

The variance, standard deviation, skewness and kurtosis are summarized in Table I.

A measure of the total energy in the measured spectra is given by the variance. Variance was computed for all data sets. For the wave staff it ranged from .0335 to .0471 m², and for the pressure sensor from .0247 to 0.377 m². The variances of the wave staff were always larger than for the pressure transducer.

A mean water surface elevation was computed for all data sets. The location of the breaker point is highly dependent on the depth of the water. The tidal range at both locations is approximately 1.5 meters, resulting in the breaker location changing considerably during a tidal cycle. During a tidal cycle it was possible to measure waves both inside and outside the surf zone. The mean depths during measurements, calculated using wave staff and pressure sensor are given in Table II along with the relative location of the mean breaker line and type of breaker. The mean sea surface values measured with the wave staff ranged from 1.57 to 2.03 m, whereas the pressure sensor measurements ranged from 1.39 to 1.87 m. For all data,

TABLE I. VARIANCE, STANDARD DEVIATION, SKEWNESS AND KURTOSIS FOR ALL DATA

Date	Instrument	Variance (m ²)	Std. Deviation (m)	Skewness	Kurtosis
8 March	Wave Gage	.04607	.21302	1.10400	5.07009
	Pres. Sens.	.03767	.19286	.39944	2.82390
19 July morning	Wave Gage	.03350	.18160	1.83207	7.43242
	Pres. Sens.	.02467	.15584	1.01014	3.84056
19 July evening	Wave Gage	.04502	.21185	.93559	4.29220
	Pres. Sens.	.02793	.16684	.38984	2.88580
20 July morning	Wave Gage	.04714	.21667	1.38004	5.14744
	Pres. Sens.	.03059	.17445	.63531	2.84676
20 July evening	Wave Gage	.04387	.20894	1.09686	4.32905
	Pres. Sens.	.02767	.16596	.50313	2.77861

TABLE II. MEAN WATER LEVELS

Date	Mean Wave Staff (m)	Mean Pressure Head (m)	Difference (cm)	Error (%)	$\frac{1}{2}\rho\text{VAR}_u$ (m ²)	Breaker Location/Type
8 March	1.59	1.39	20	13	.2695	Spill-Plunging
19 July morning	1.57	1.49	8	5	.0553	Spilling
19 July evening	2.03	1.87	16	8	.0503	Outside Surf Zone
20 July morning	1.70	1.55	15	9	.0680	Spilling
20 July evening	1.88	1.69	18	10	.0582	Outside Surf Zone

VAR = variance

The mean water depth given by the pressure sensor is less than the mean water depth measured with the wave staff by a difference that ranged from .08 to .20 m. (Figure 3 the mean water level measured using wave staff and pressure sensor.) This difference can be explained due to two main factors:

1. The hydrostatic pressure head is decreased by the Bernoulli term and therefore gives a mean value less than the mean value measured by the wave staff.
2. The pressure transducer used measures absolute pressure rather than relative; therefore, variations in atmospheric pressure occurring during the experiments and or during calibrations, will influence the water surface elevations measured by the pressure sensor. As an example, a variation of .5 inch of mercury in the atmospheric pressure, will give a difference of approximately 17 cm in the mean water depth computed with the pressure sensor data.

The difference between the mean water level measured using the wave staff and pressure sensor ranged between 8 to 20 cm, as given in Table II. The approximate decrease in pressure head due to the Bernoulli term is given by the variance of the on-offshore horizontal velocity. The Bernoulli contribution varied between 5 to 27 cm, which is a substantial contribution. The magnitude of the Bernoulli term varies with location relative to the breaker point and the type of the breaker. Hence, it is concluded that substantial errors can be introduced in the mean water elevation in very shallow water using pressure sensors due to the Bernoulli term.

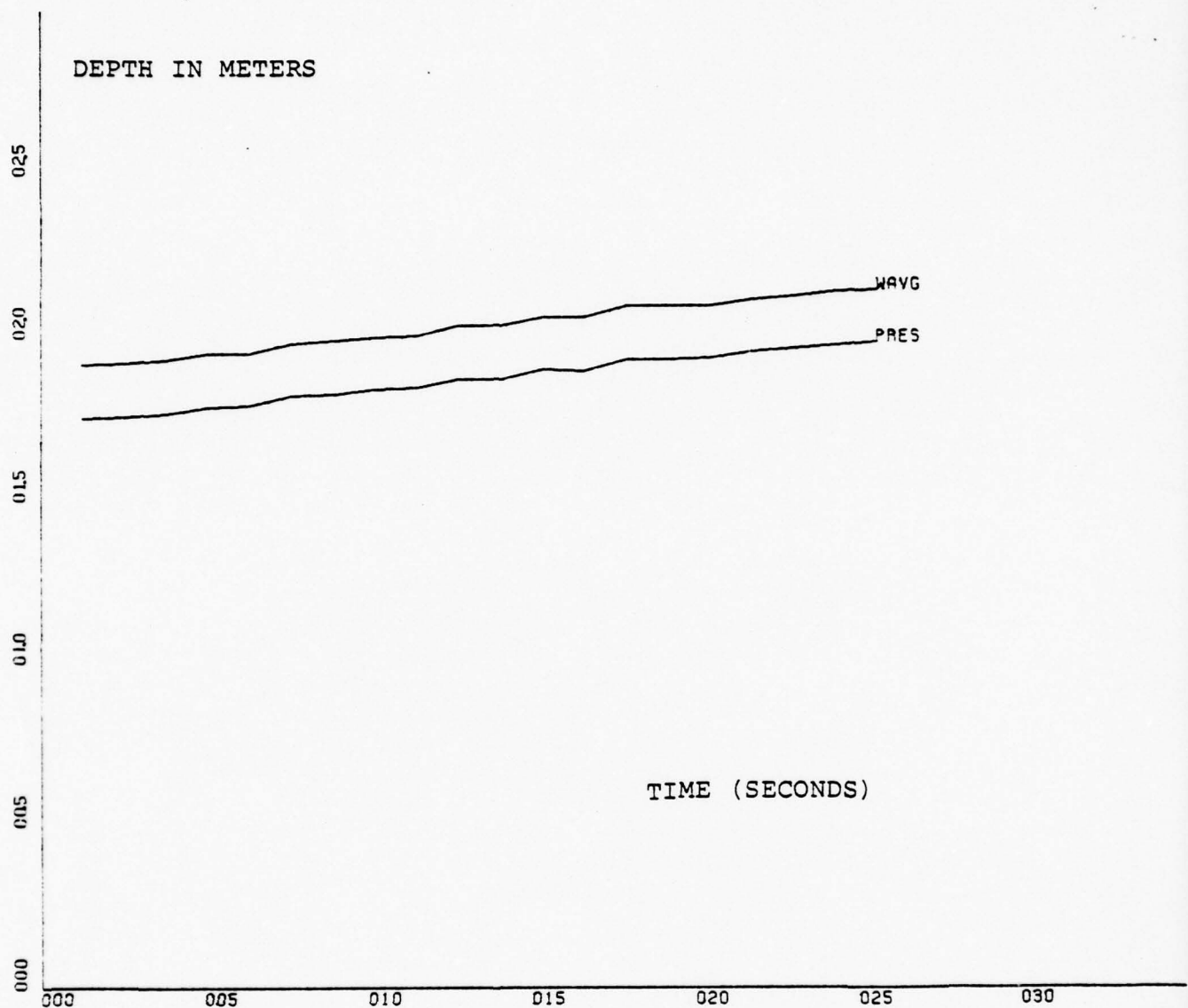


Figure 3. Mean water depth given by the wave gage and by the pressure sensor, 19 July (evening)

X-SCALE=5.00E+02 UNITS INCH.
 Y-SCALE=5.00E-01 UNITS INCH.

VTOR19E

B. SURFACE ELEVATION SPECTRUM CALCULATED FROM PRESSURE SPECTRUM USING LINEAR TRANSFER FUNCTION (STANDARD TECHNIQUE)

The pressure spectrum was converted to a theoretical wave spectrum for comparison with the measured wave staff spectrum using the transfer function given by linear theory. (Equation (3) in section IV.) The power, coherence squared (henceforth referred to as coherence), and phase spectra of the wave staff and pressure sensor are shown in Fig. 4 for the 19 July, evening. During the 19 July, evening measurements, the tide was high resulting in the wave sensors being located just out of the surf zone; hence, the waves are indicative of very shallow, non-breaking waves.

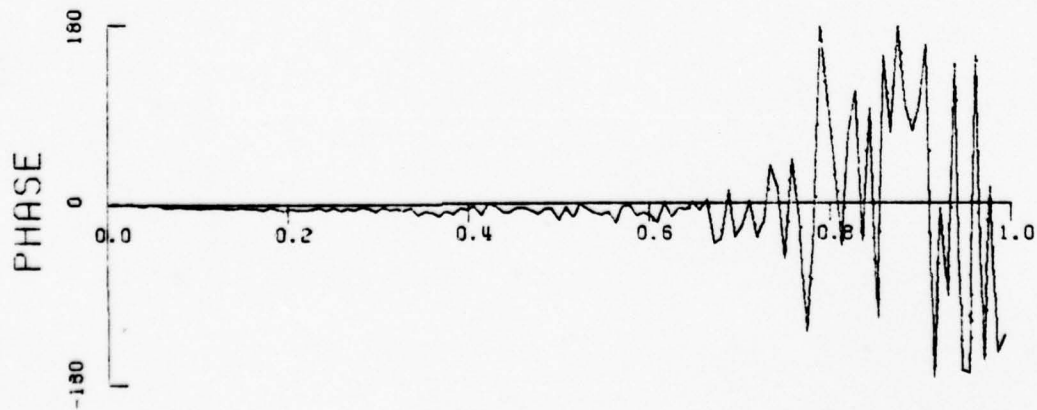
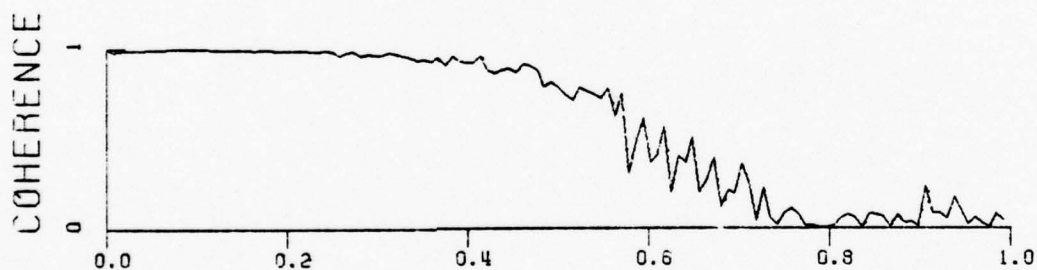
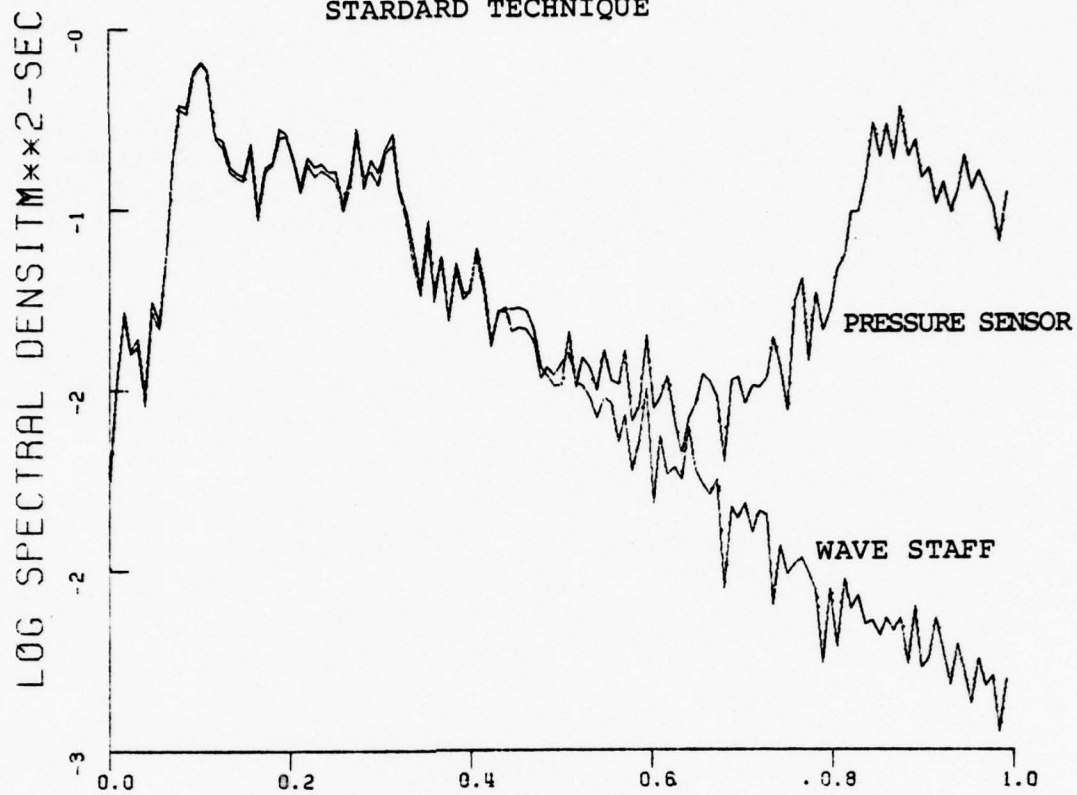
The power spectra shows a narrow-banded peak near a frequency of .0938 Hz corresponding to a period of 10.7 sec. Also evident are peaks at approximately .1875 and .2734 Hz, which appear to be harmonics of the primary frequency at .0938 Hz.

In all the data, there is a relative peak of energy at a frequency of approximately .02 Hz, which we attribute to surf beat. Above approximately .4 Hz, the linear transfer function over-compensates and the surface elevation spectrum calculated from the pressure records diverges rapidly.

The coherence between surface elevation and pressure of all experiments were high, ranging from .95 to .99 in the maximum energy portion of the wave spectra. These extremely high coherences begin rapidly decreasing at approximately .45 Hz. The 8 March coherence spectrum is similar with the exception of the region below .05 Hz. In this region, the 8 March data

POWER, COHERENCE AND PHASE SPECTRA 19 JULY EVENING

STANDARD TECHNIQUE



FREQUENCY (HZ)

shows coherence values of .80 to .85 with a minimum of .68 at approximately .107 Hz.

The phase difference between the pressure sensor and wave staff over the highly coherent band of prominent wave energy is always small in the range of 0 to 7 degrees. Because the pressure sensor was located approximately 40 cm shoreward of the wave staff, the wave staff phase always leads the pressure sensor phase. During the 8 March experiment, the pressure sensor was directly beneath the wave staff and the signals are in phase. The phase angle becomes random for the non-coherent region of the spectrum.

C. SURFACE ELEVATION SPECTRUM CALCULATED FROM PRESSURE SPECTRUM INCLUDING THE BERNOULLI TERM

As described in section III, two techniques are proposed here to include the usually neglected Bernoulli term, $u^2 + v^2$, in converting pressure to surface elevations. The spectral densities of surface elevations at selected frequencies for the 19 July evening data, calculated using the three pressure correction techniques compared in Table III.

1. Bernoulli Term Calculated Using Measured Velocities

The first technique employs the Bernoulli term calculated using the measured velocities. The first technique is compared to the standard technique in Table III; the spectra are shown in Fig. 5. In frequencies ranging from .0156 to .0313 Hz (surf beat region), the first technique has decreased

TABLE III. SURFACE ELEVATION SPECTRA FOR 19 JULY EVENING

f	S_{η} (f) (m ² -sec)	S_p/S_{η}	S_p^1/S_{η}	S_p^2/S_{η}	Remarks
.0156	.0309	1.036	.987	1.001	Surf
.0234	.0219	1.022	.980	.987	Beat
.0313	.0233	1.074	1.021	1.021	
.0781	.2018	.964	.992	.994	
.0859	.1978	.941	.974	.973	Max. Energy
.0938	.2754	.985	1.017	1.014	Band Range
.1016	.2989	.986	1.013	1.013	
.1172	.1519	.981	1.007	1.002	
.1875	.1642	.921	.966	.959	First
.1953	.1557	.977	1.024	1.008	Harmonic
.2734	.1637	.932	.973	.965	Sec. Harmonic

f = frequency (Hz) at spectral peaks; S = spectral densities; η = wave gage;

p = pressure sensor; 1 = first technique; 2 = second technique

POWER, COHERENCE AND PHASE SPECTRA 19 JULY EVENING

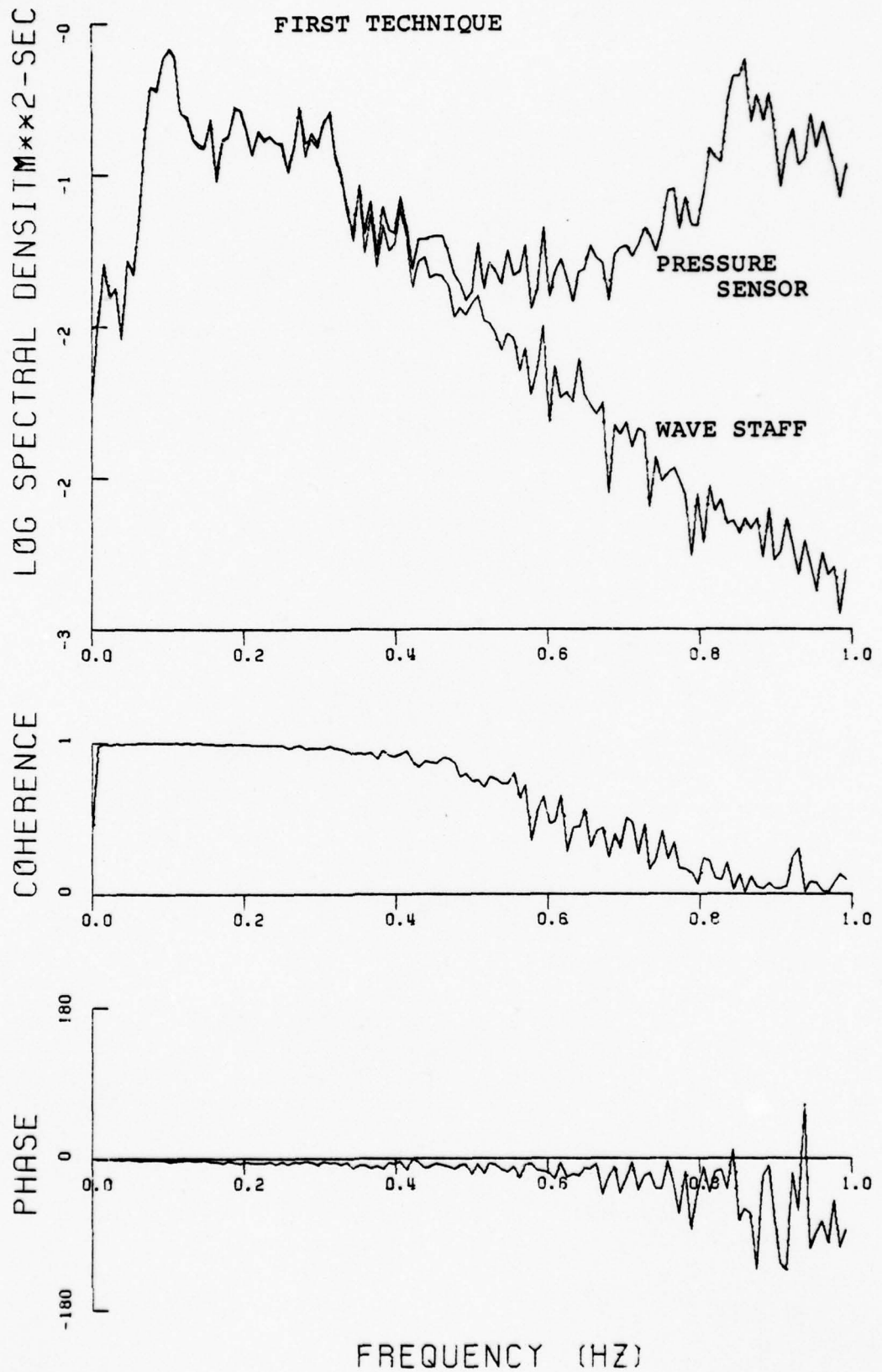


Figure 5

the spectral densities of the converted pressure spectrum to values closer to, but less than, the wave staff spectral densities. Referring to the spectral density ratios listed in columns 3-5 of Table III, it is noted that for the same frequencies, application of technique 1 improves the spectral density ratios from 1.036 to .987, 1.022 to .980 and from 1.074 to 1.021 respectively; a relative improvement in all cases.

Without the introduction of the non-linear Bernoulli term, the pressure spectral densities are consistently smaller than the spectral densities of the wave gage spectrum in the band of frequencies from .0781 to .1172 Hz where most of the energy is present. After the application of the $u^2 + v^2$ term as evaluated by technique 1, all values show improvement with the exception of the frequency .1016 Hz where the ratio of .985 was changed to 1.017. The same is generally true for the harmonic spectral peaks, with the exception of the frequency .1953 Hz, where the ratio of .977, the application of the first technique gives a ratio of 1.024 (see Fig. 6).

For the 8 March data (Table IV), in the frequency band that contains most of the energy, the standard pressure spectrum spectral densities are uniformly smaller than those of the wave staff spectrum, with the exception of the surf beat frequency of .0098 Hz. Application of the first technique in the surf beat frequency of .0098 Hz increased the spectral density ratio whereas in the first harmonic (.1270 Hz) we reduced the ratio .941 to .854.

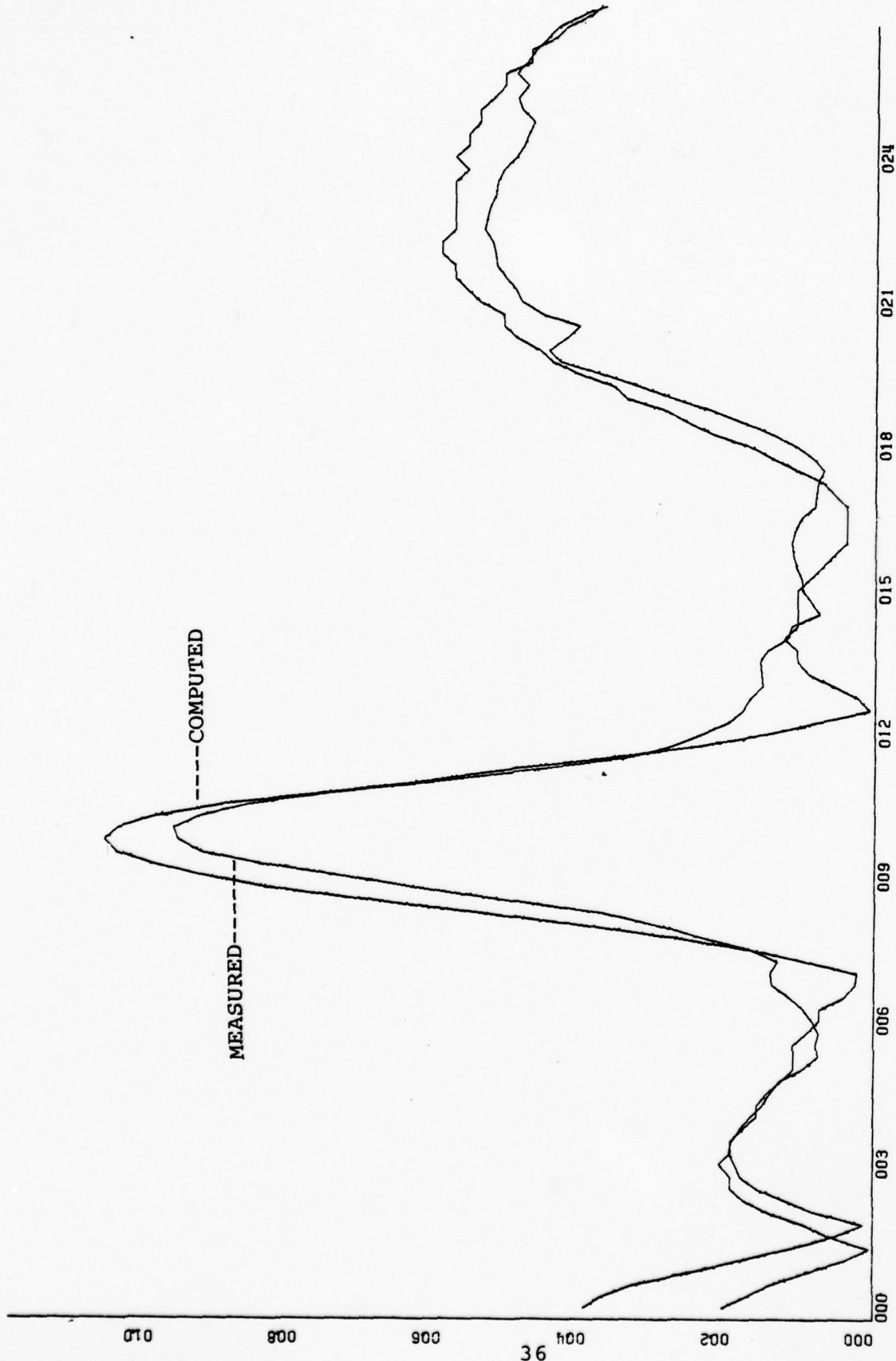


Figure 6. Measured and Computed Velocity Vectors,
19 July Evening.

X-SCALE=3.00E+00 UNITS INCH.
Y-SCALE=2.00E-01 UNITS INCH.

TABLE IV. SURFACE ELEVATION SPECTRA FOR 8 MARCH

f	$S_{\eta}(f)$ (m^2 -sec)	s_p/s_{η}	s_p^1/s_{η}	s_p^2/s_{η}	Remarks
.0098	.0167	1.281	1.319	1.286	Surf Beat
.0586	.6868	.907	.982	.944	
.0684	.9929	.974	1.060	1.011	Max. Energy
.0781	.5729	.865	1.021	.901	Band Range
.0879	.1599	.996	1.122	1.037	
.1270	.1504	.941	.854	.991	First Harmonic

f = frequency (Hz) at spectral peaks; S = spectral densities; η = wave gage
 p = pressure sensor; 1 = first technique; 2 = second technique

In the maximum energy band range, technique 1 gives better agreement for two of the frequencies (.0586 and .0781 Hz), but gives slightly poorer agreement in the other two frequencies (.0684 and .0879 Hz).

2. Bernoulli Term Calculated by Convolving Pressure Records

In the second technique, the velocity is calculated by convolving the pressure record, using the transfer function derived from linear theory as given by Eq. 12. A typical analogue record of both measured and computed vector magnitudes is shown in Fig. 6. The velocity vectors of the measured velocity and the computed velocity determined by convolution of pressure are compared in Fig. 7; the power spectra are very similar and high coherence and phase agreement in the band of frequencies smaller than approximately .3 Hz are to be noted. Hence, it is concluded that the use of velocities calculated from the convolved pressure records should give reasonable results compared to direct measurements.

For the 19 July evening experiment, the improvement introduced by the second technique is, in fact, always better than the improvement obtained with the first technique, with the exception of the frequency of .0188 Hz, (Fig. 8). For the 8 March data, compared with the first technique, the improvement obtained with the second technique is better in all frequencies with the exception of the frequencies of .0586 and .0781 Hz.

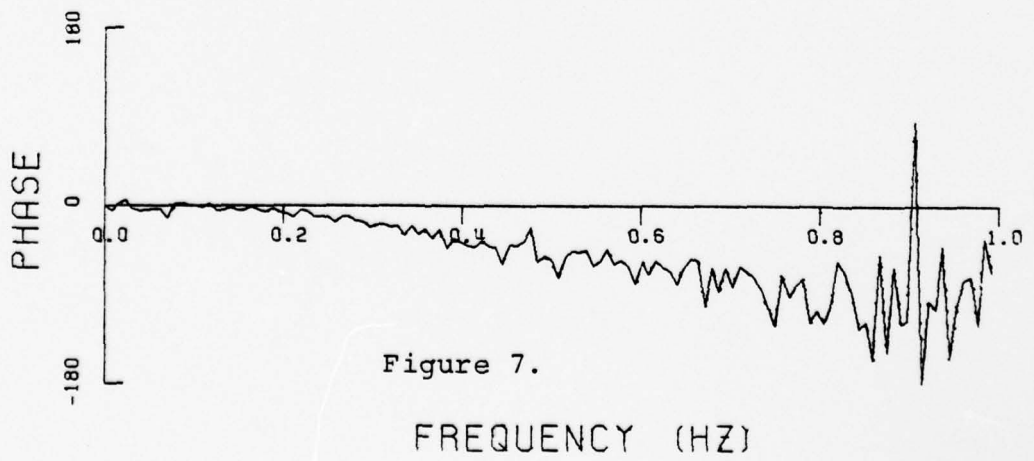
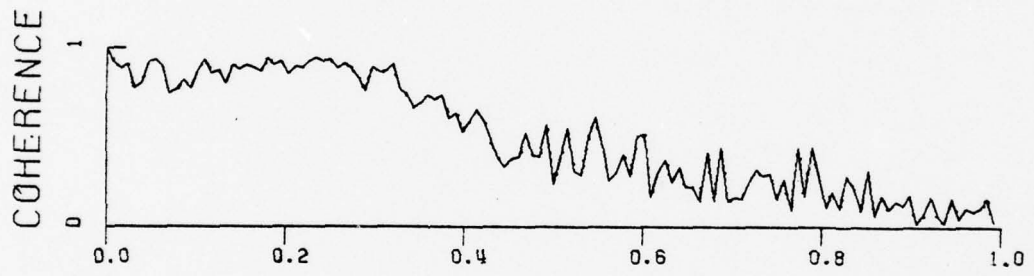
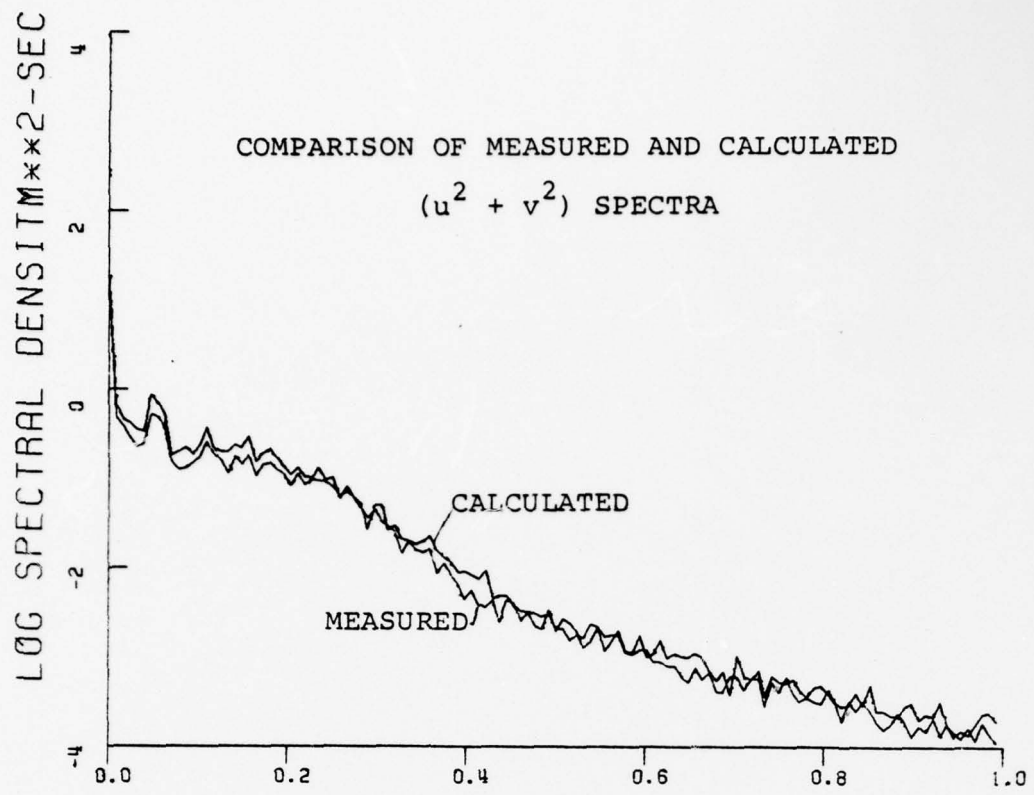


Figure 7.

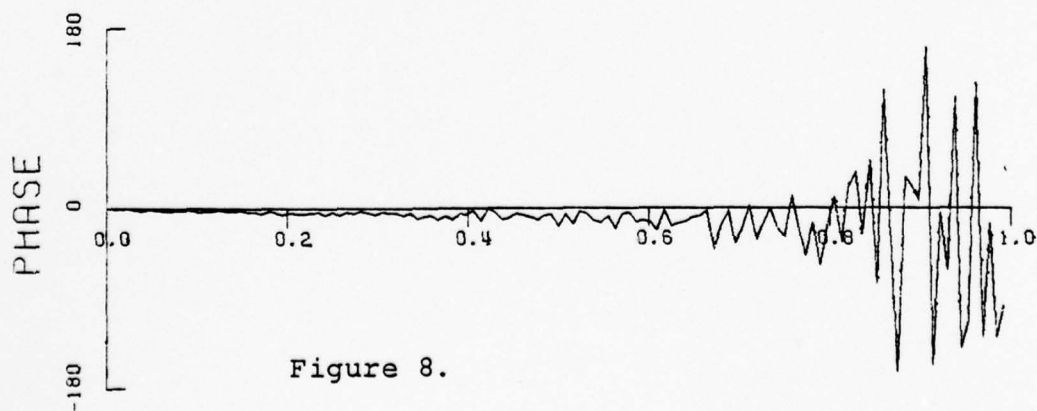
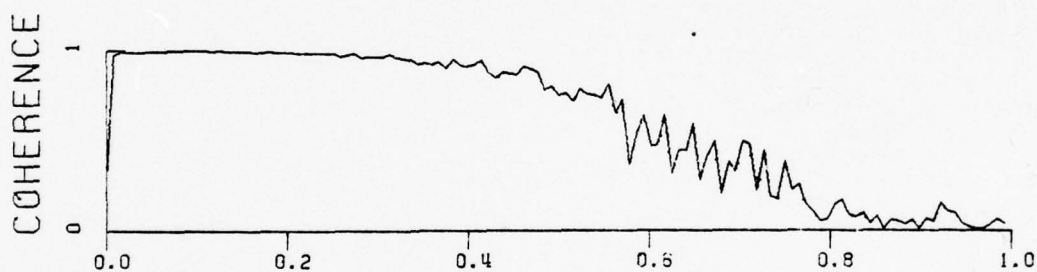
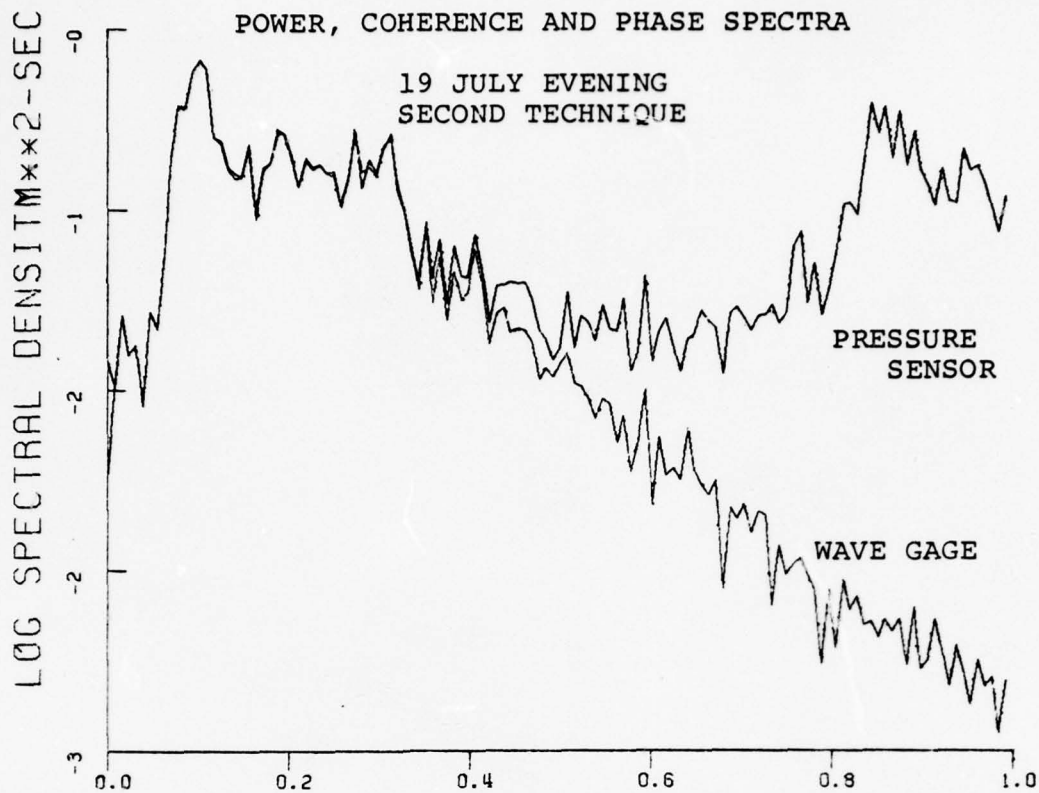


Figure 8.

FREQUENCY (HZ)

3. Comparing Variances

Variances (and their ratios) calculated by integrating the spectra from .007 to .30 Hz, are given in Table V. For all the experiments the variance of the surface elevation spectra computed from the pressure record using the conventional transfer function is smaller than the variance of the wave staff spectra, with the exception for the 20 July evening data where it is slightly larger.

For the 19 July evening data the improvement on the error was 3.4 and 3.1% using first and second technique respectively. The best improvement obtained was for the 19 July morning experiment where the improvement was 7.8% for technique 1 and 9.7% using the second technique.

For all other experiments, the inclusion of the Bernoulli term resulted in an over compensation of surface elevation variance.

TABLE V. COMPARING SURFACE ELEVATION VARIANCES

Date	Wave Staff Variance (m ²)	Pressure Sensor Wave Staff (Stand. Tech.)	Pressure Sensor Wave Staff (First Tech.)	Pressure Sensor Wave Staff (Second Tech.)
8 March	.0401	.976	1.051	1.022
19 July morning	.0340	.818	.896	.915
19 July evening	.0373	.959	.993	.990
20 July morning	.0358	.978	1.030	1.036
20 July	.0326	1.006	1.046	1.045

VI. CONCLUSIONS

Field measurements of waves in very shallow water just outside the surf zone and at the breaking were measured with both a wave staff and pressure sensor. The surface elevation was inferred from the pressure using the conventional linear wave theory transfer function and a method which includes the non-linear quadratic velocity term in the Bernoulli equation. The velocities were measured using a flowmeter (technique 1) and calculated by convolving the pressure record (technique 2). The surface elevation inferred from the pressure sensor are compared with the wave staff records as a standard.

Surface elevations inferred from the pressure sensor were generally underestimated, mainly in the region of the crest, compared with the same surface elevation measured by the wave staff. Pressure records are more smoothed than wave staff records and for energetic computational purposes the energy of the wave measured with the pressure transducer is generally smaller than that measured with the wave staff.

The mean water levels determined from the hydrostatic pressure head were consistently less as compared with the wave staff. The difference can be due to variations of the barometric pressure (which was not accounted for) and due to the dynamic pressure head which acts to always underestimate the mean water level. Direct estimates show that the errors in the mean water level due to the dynamic pressure head ranged

from 5 to 13 percent. Therefore, the use of pressure sensors to infer the mean water level must be interpreted with caution.

It is advisable to bury the pressure transducer in the sea bed to insure that it is out of the flow field and the dynamic pressure is essentially zero.

In the band of frequencies less than approximately .4 Hz the pressure sensor and wave gage spectra are highly coherent and almost perfectly in -phase, whereas at higher frequencies the spectra become less coherent and the phases random, as noted previously.

Both proposed techniques for calculating the surface elevation spectrum from the pressure records show a general improvement as compared with the standard technique using a linear transfer function. For technique 1, improvement (on the order of 3.4 to 7.8% of the total variance of the wave gage spectrum) was obtained. Whereas, for the second technique the improvement was on the order of 3.1 to 9.7%. The improvement of both techniques is approximately the same with the disadvantage of the first technique that the velocities are measured with flowmeters. In technique 2 the velocities are determined by convolving the pressure records which is a great simplification in an area where the emplacement of sensors is difficult, such as the surf zone.

For both techniques, the reason why the improvement is not so large can be explained by three factors:

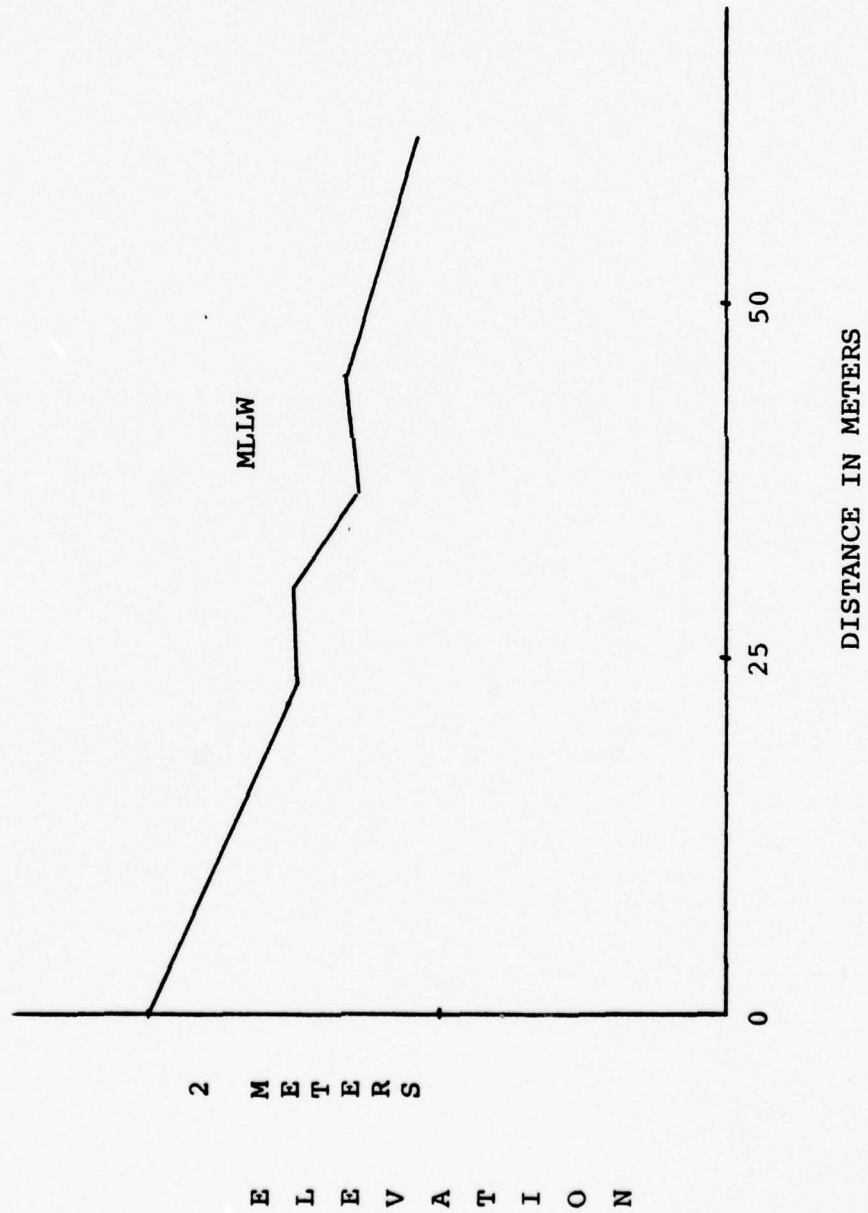
1. The irrotationality assumption applied during the development of the Bernoulli equation leads to

problems when the equation is applied to a rotational flow. Breaking waves are characterized by both rotational and highly non-linear flow.

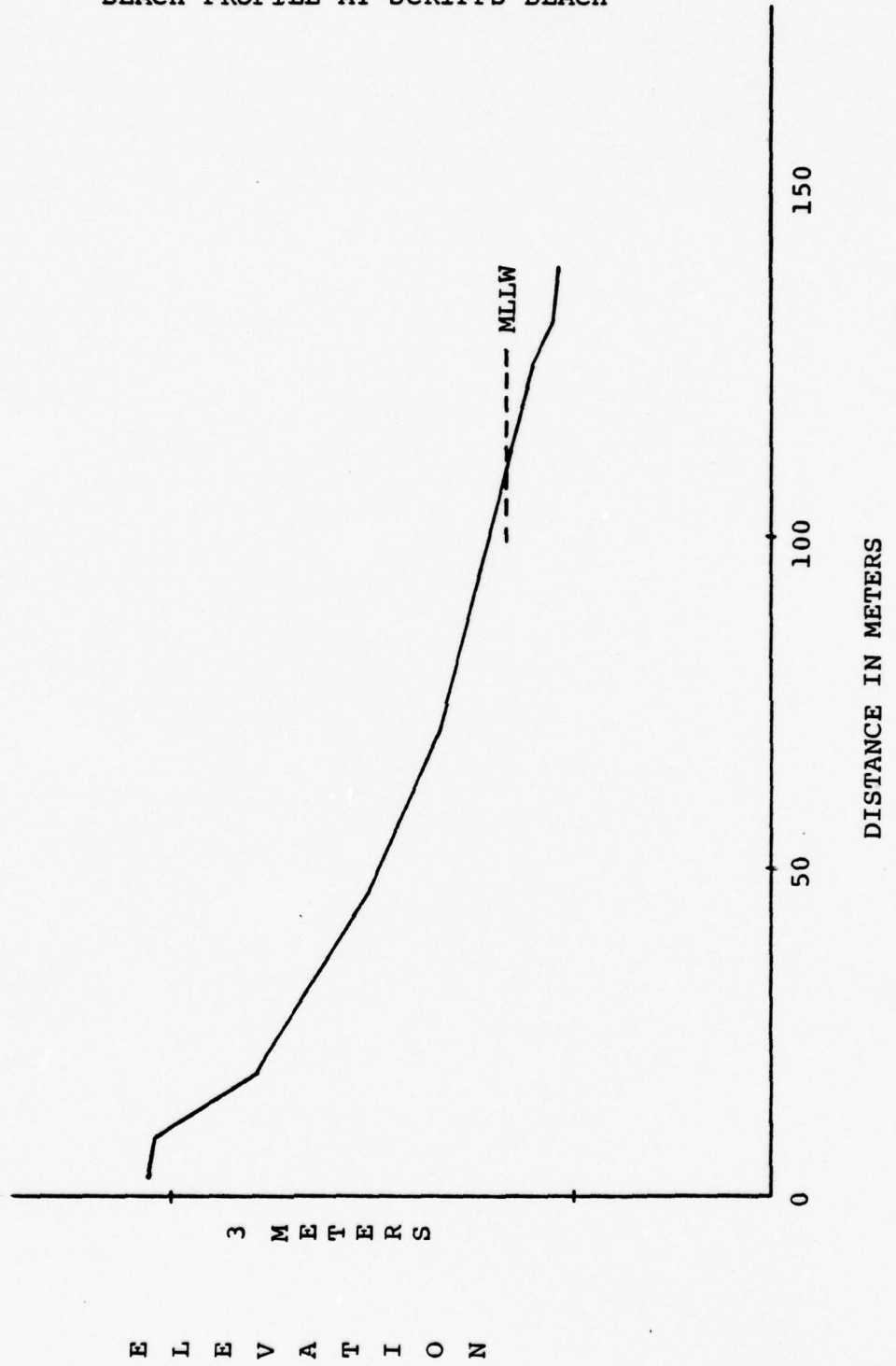
2. In cases where foam-bearing waves are being measured, wave heights measured by the wave staff are always in excess of those indicated by the pressure transducer. The wave gage measures the wave amplitude as being to the top of the superimposed foam, whereas the added pressure at the pressure transducer due to the foam is relatively small.
3. The Bernoulli term is only a second-order correction.

APPENDIX A

BEACH PROFILE AT DEL MONTE BEACH



BEACH PROFILE AT SCRIPPS BEACH



APPENDIX B

Date	Instrument	Cala* (meters)	Calx** (meters/volt)
8 March	Wave Gage	.707	.683865
	Press. Sensor	-1.404	2.791088
	Flowm. X Direct.	- .009	3.559351
	Flowm. Y Direct.	- .008	3.532642
19 July***	Wave Gage	3.455	- .00122
	Press. Sensor	-1.040	.006841
	Flowm. X Direct.	0.0	.002251
	Flowm. Y Direct.	0.0	.002261
20 July***	Wave Gage	3.530	- .001235
	Press. Sensor	-1.040	.006841
	Flowm. X Direct.	0.0	.002251
	Flowm. Y Direct.	0.0	.002261

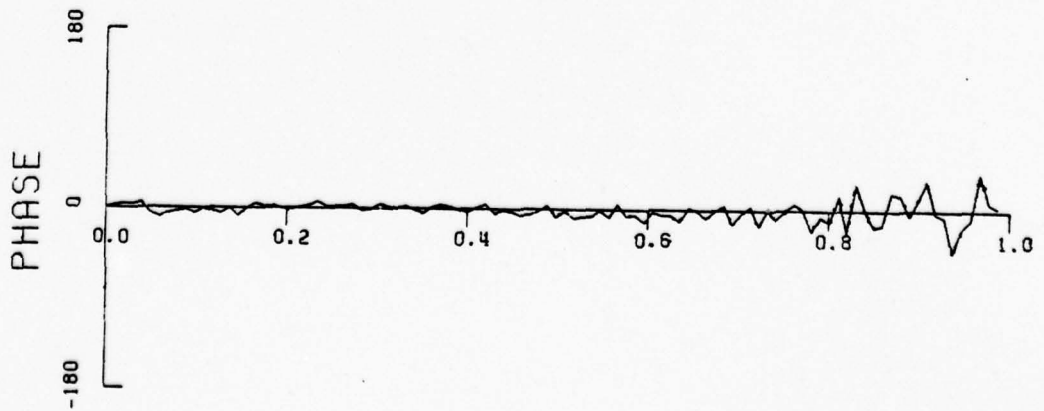
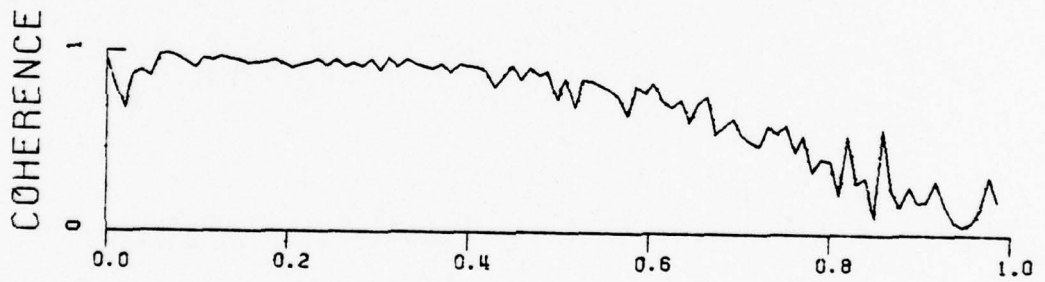
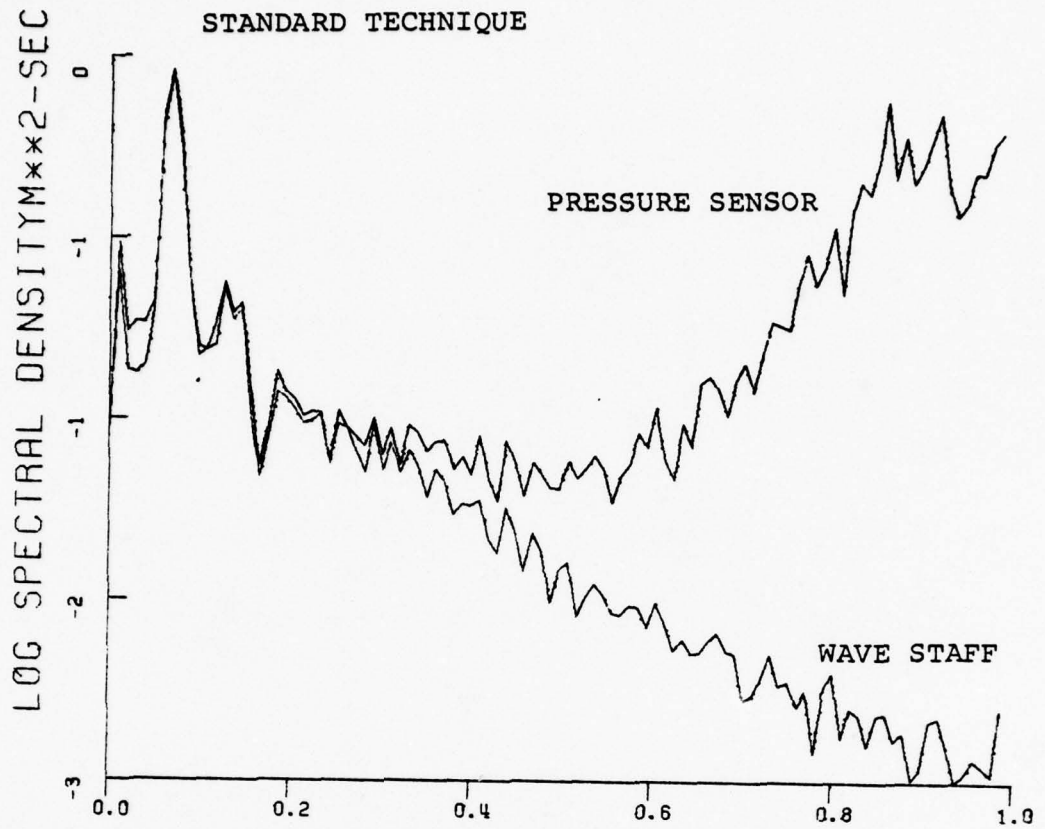
* Calibration Additive Factor

** Calibration Multiplicative Factor

*** Due computer record technique the true Calx of the instruments have been multiplied by a factor of 5/2048.

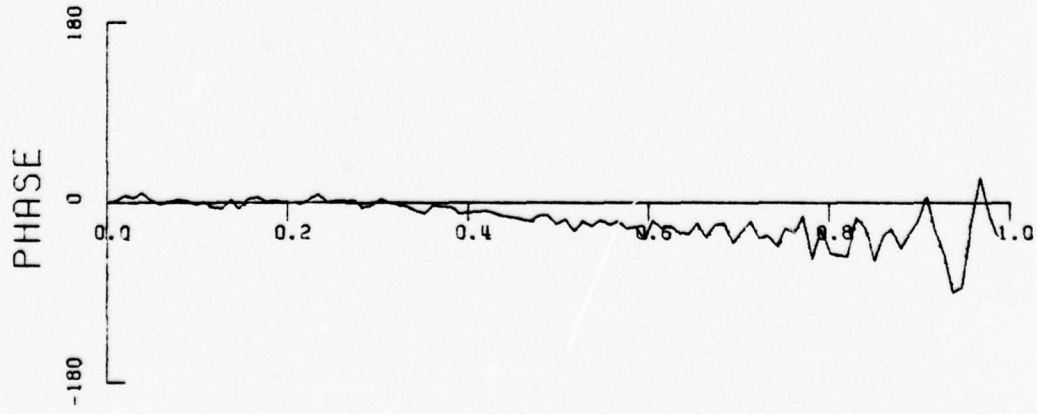
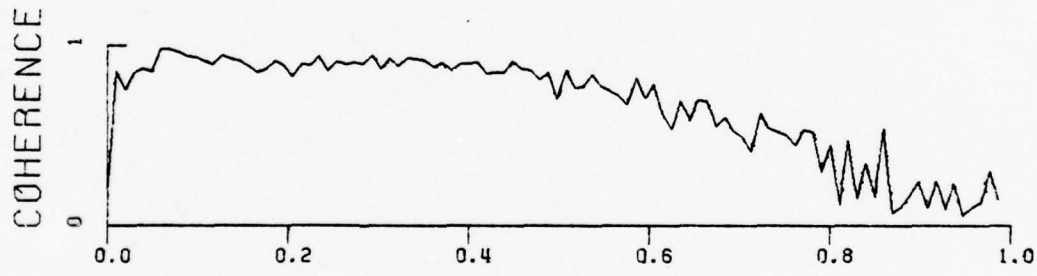
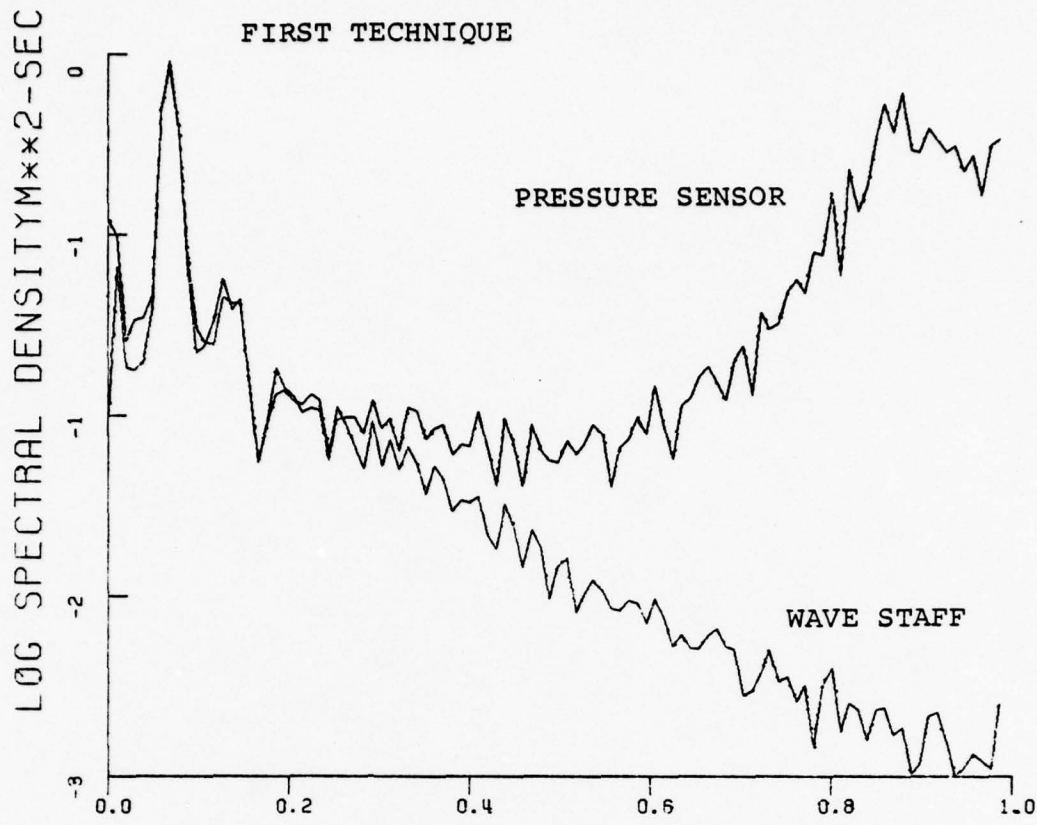
APPENDIX C
POWER, COHERENCE AND PHASE SPECTRA FOR 8 MARCH

STANDARD TECHNIQUE



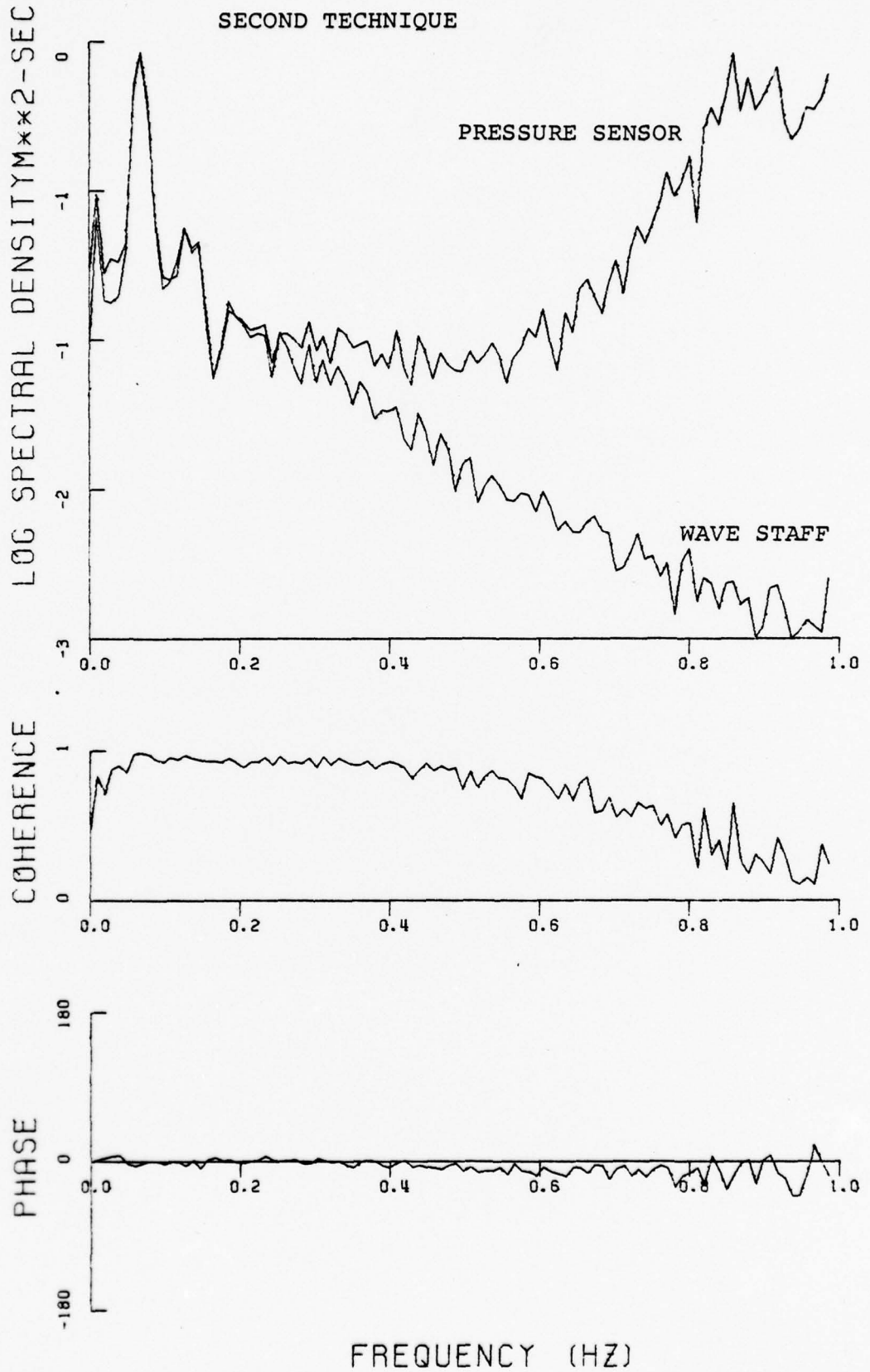
FREQUENCY (HZ)

POWER, COHERENCE AND PHASE SPECTRA FOR 8 MARCH

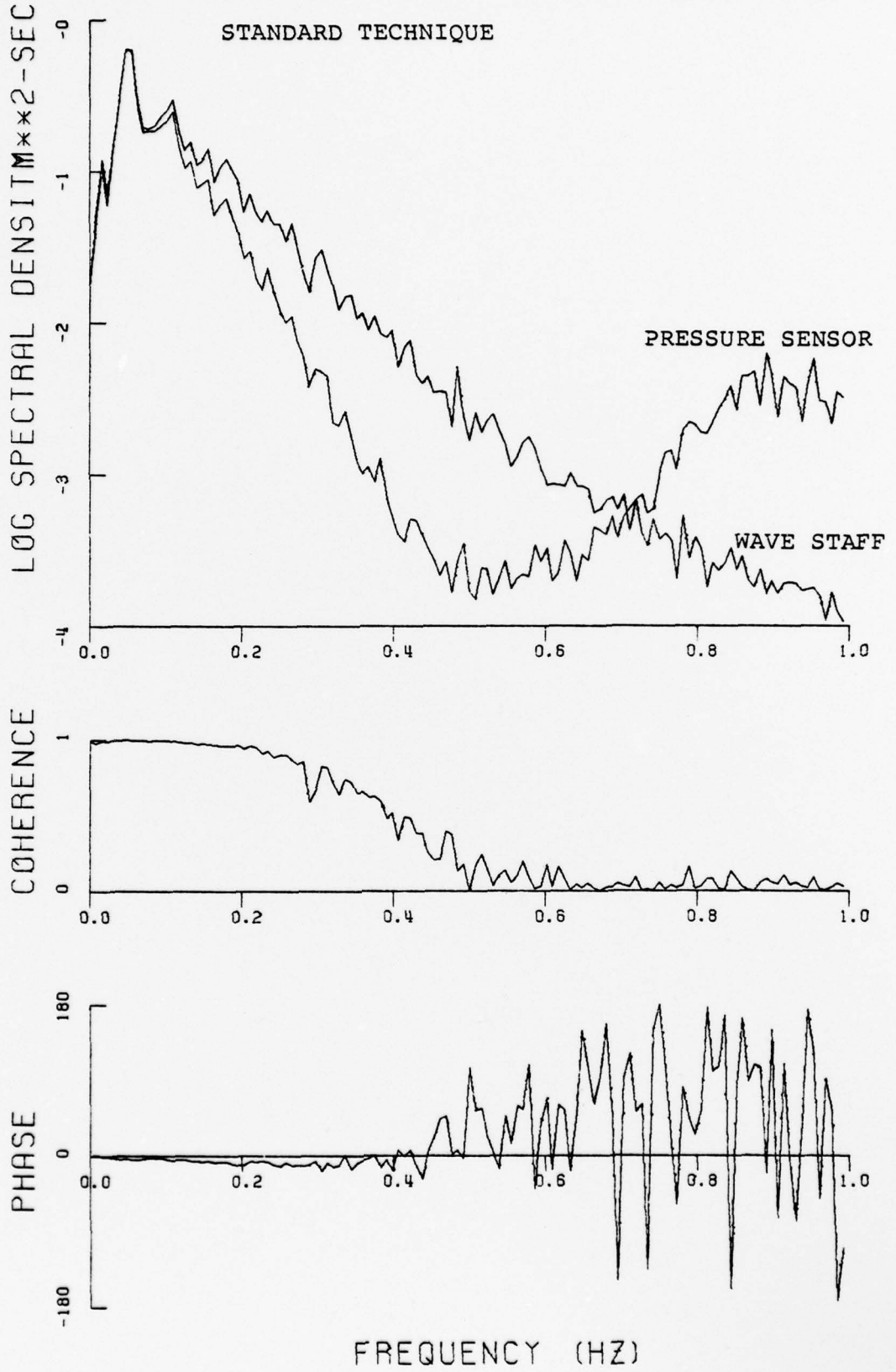


FREQUENCY (HZ)

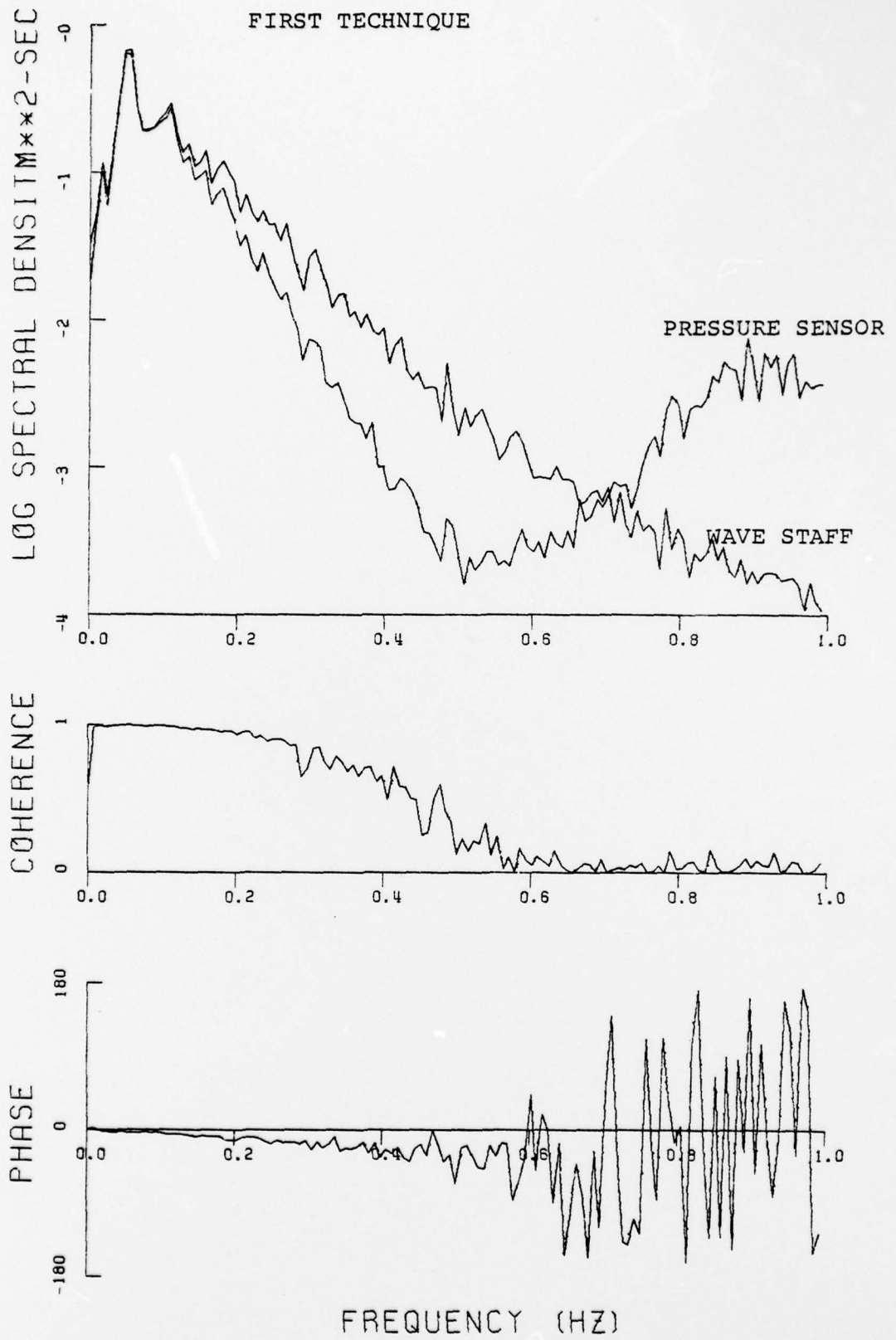
POWER, COHERENCE AND PHASE SPECTRA FOR 8 MARCH



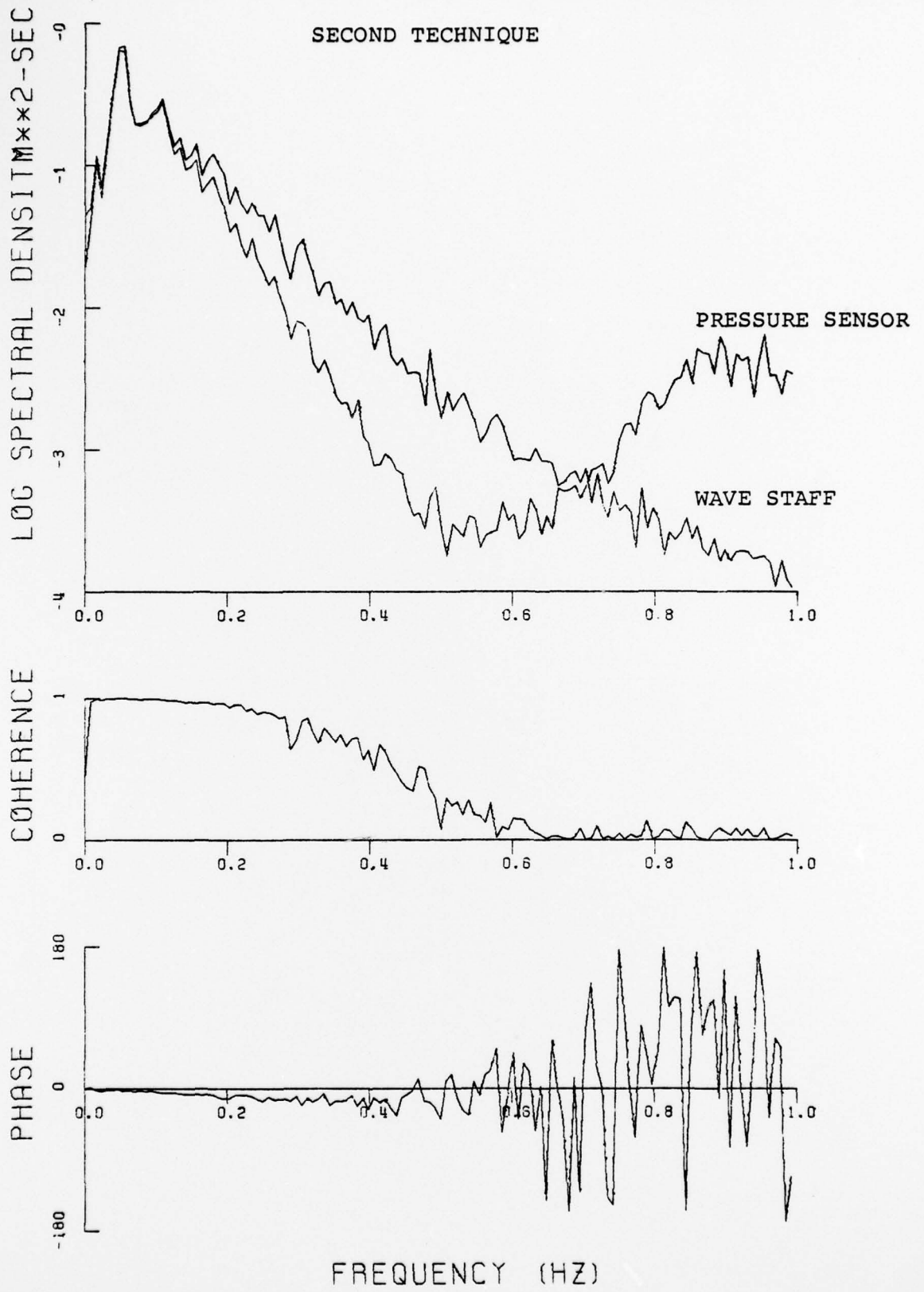
POWER, COHERENCE AND PHASE SPECTRA FOR 19 JULY MORNING



POWER, COHERENCE AND PHASE SPECTRA FOR 19 JULY MORNING

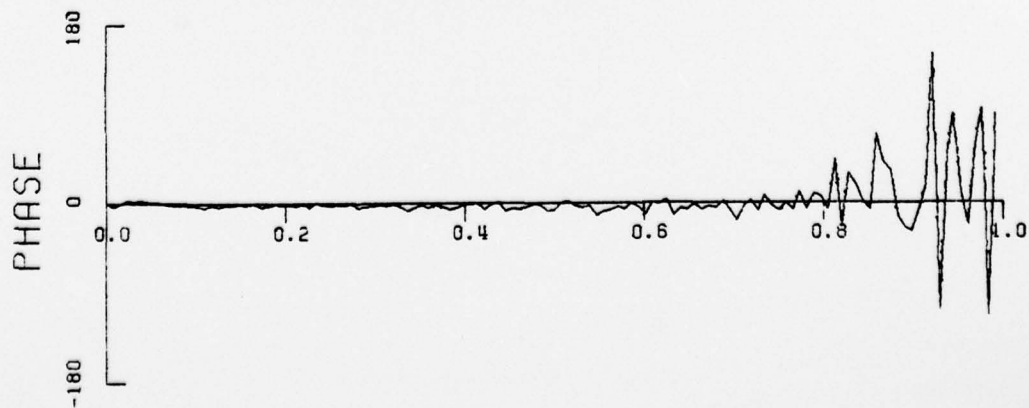
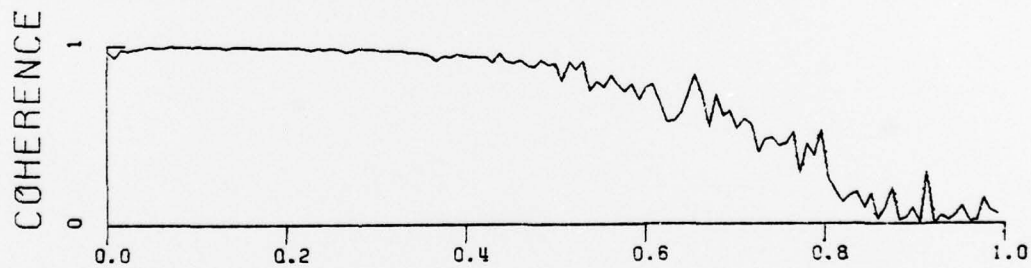
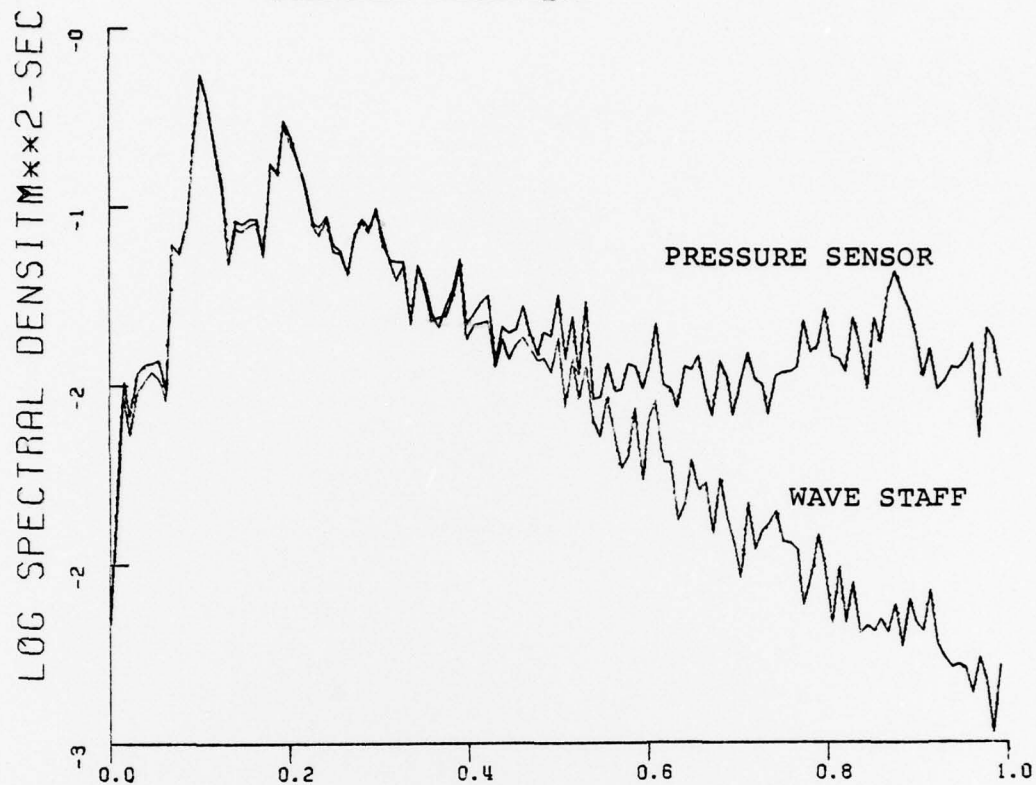


POWER, COHERENCE AND PHASE SPECTRA FOR 19 JULY MORNING



POWER, COHERENCE AND PHASE SPECTRA FOR 20 JULY MORNING

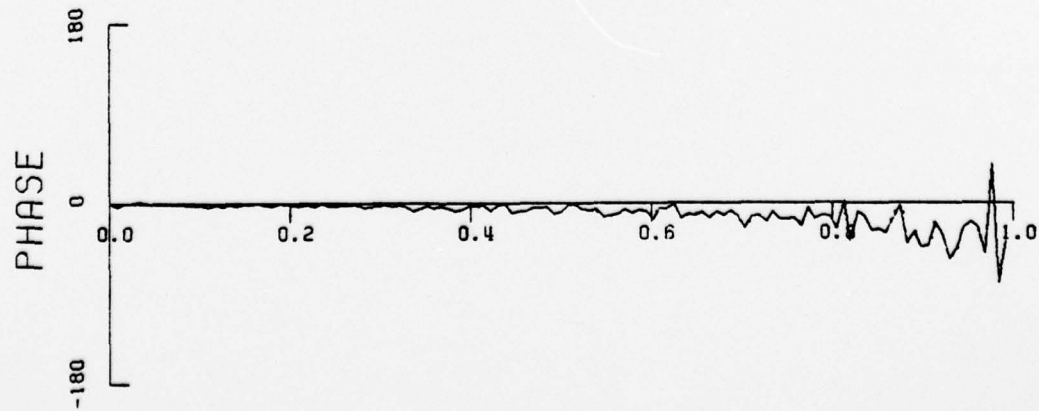
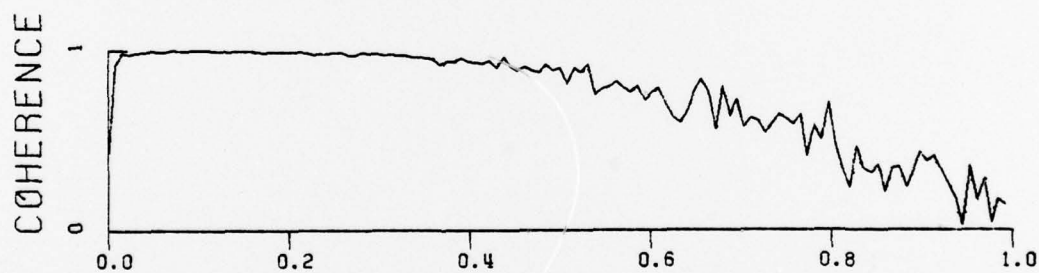
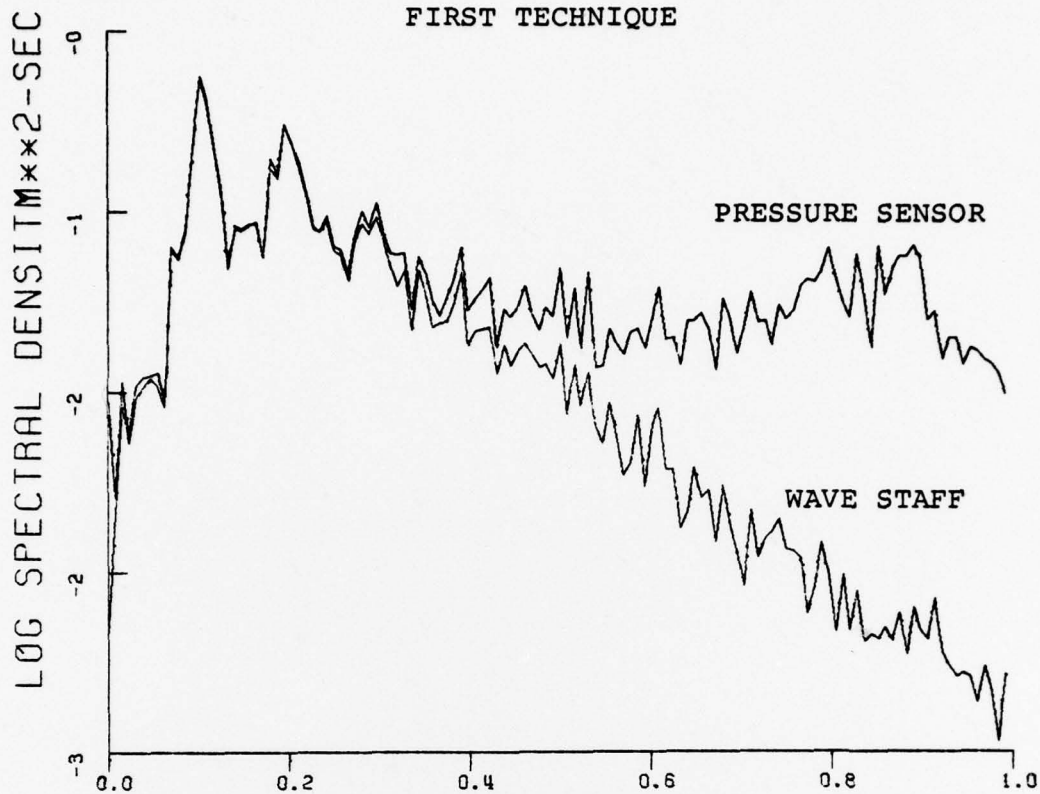
STANDARD TECHNIQUE



FREQUENCY (HZ)

POWER, COHERENCE AND PHASE SPECTRA FOR 20 JULY MORNING

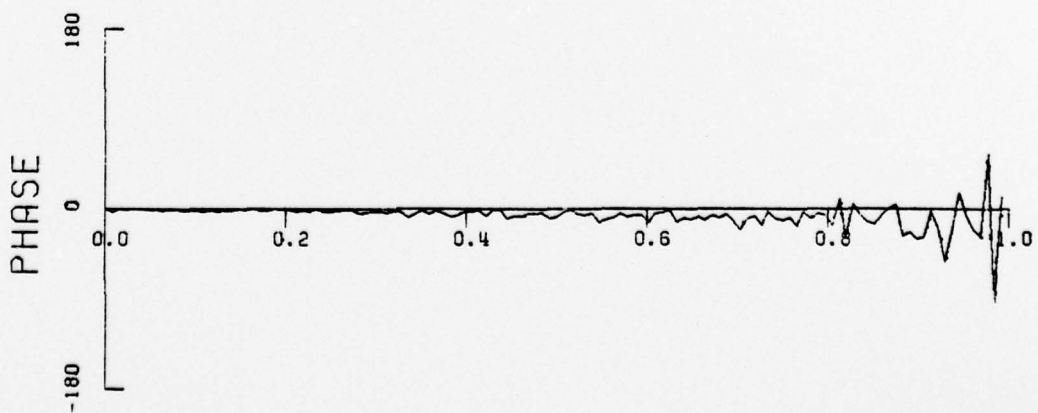
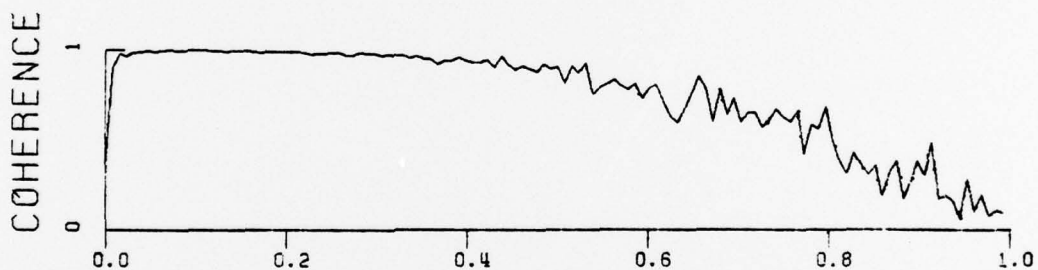
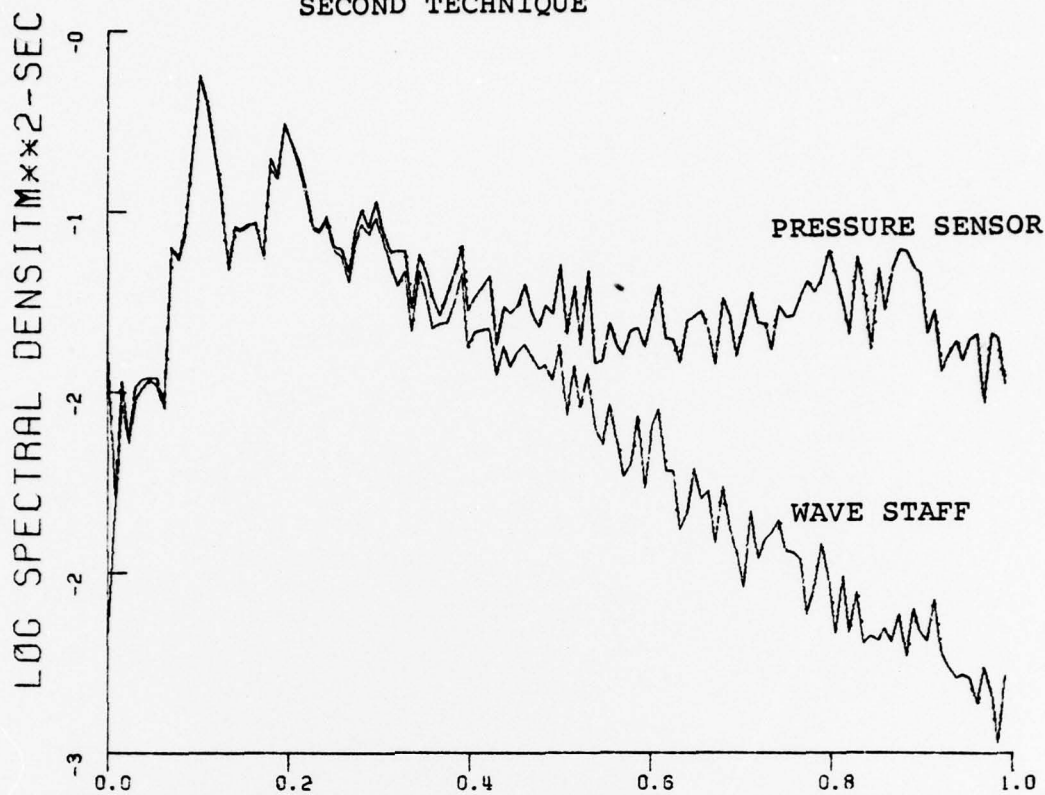
FIRST TECHNIQUE



FREQUENCY (HZ)

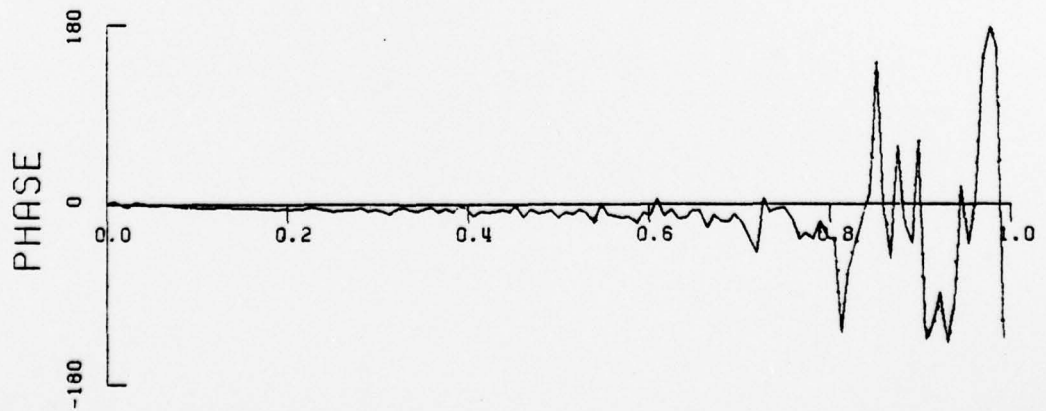
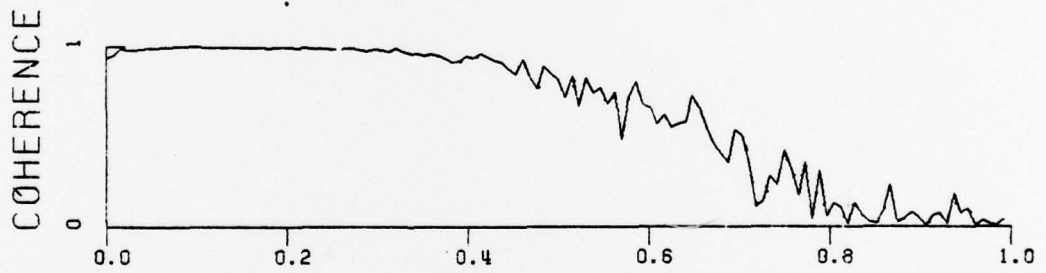
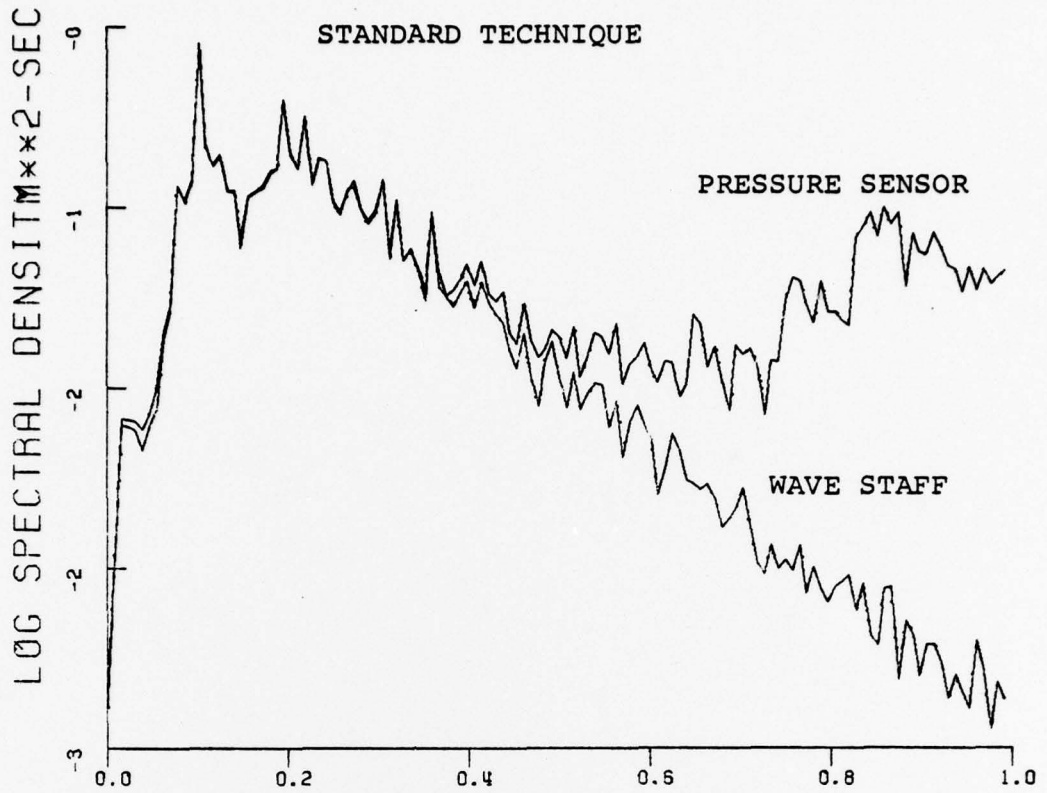
POWER, COHERENCE AND PHASE SPECTRA FOR 20 JULY MORNING

SECOND TECHNIQUE



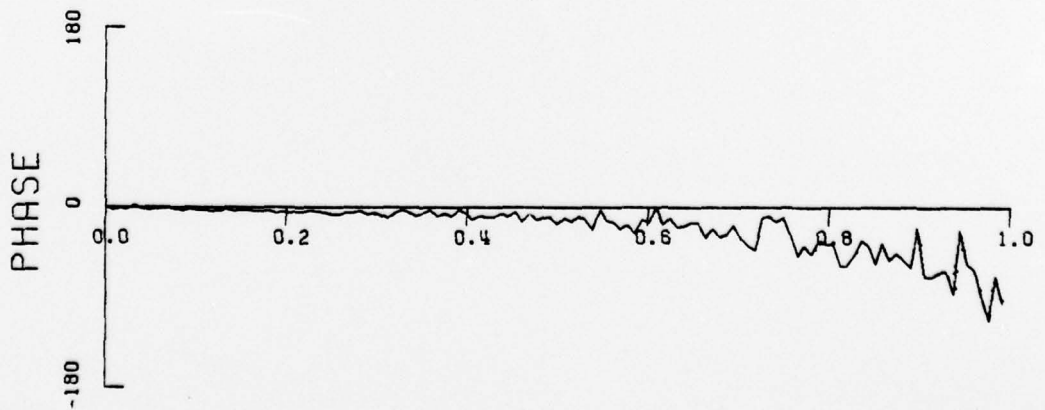
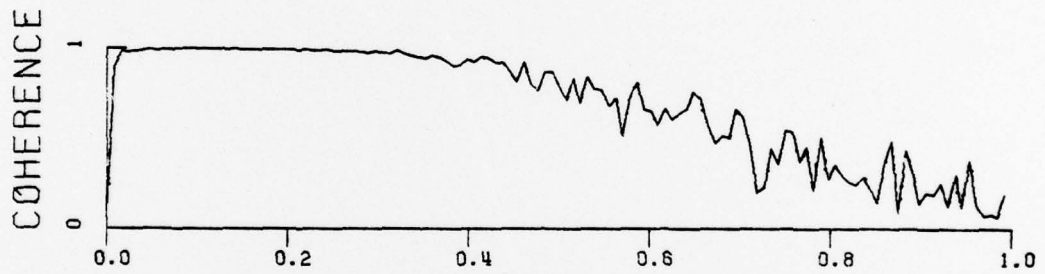
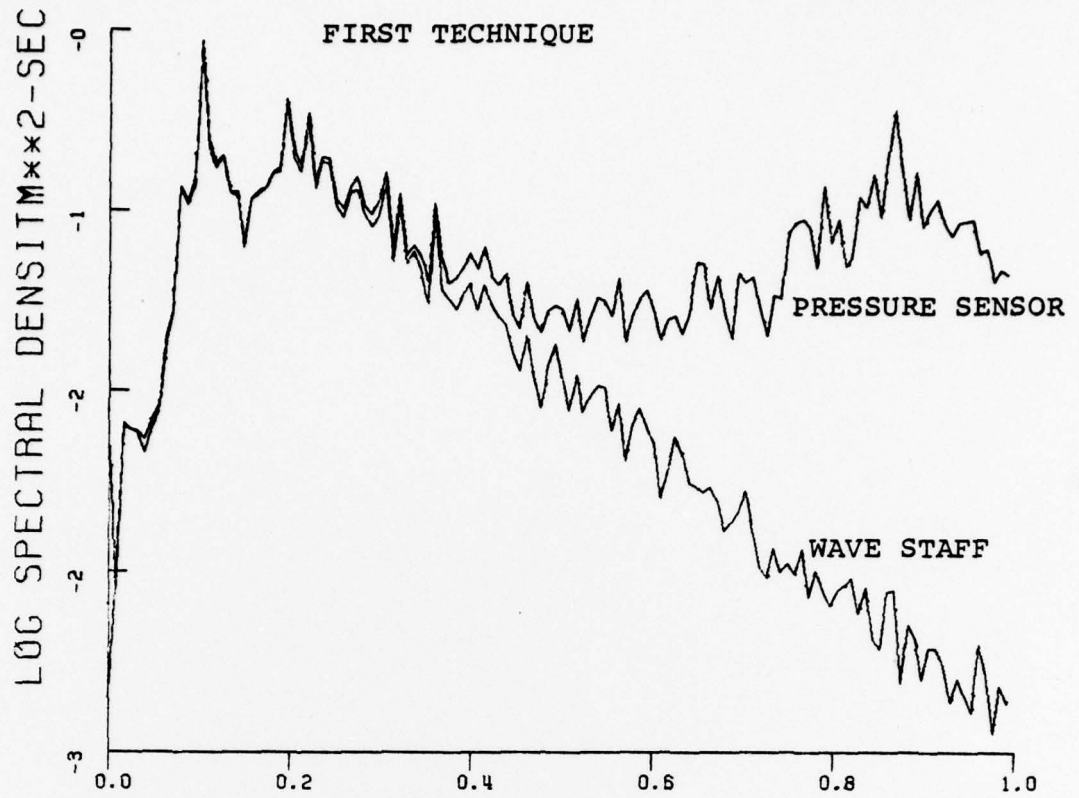
FREQUENCY (HZ)

POWER, COHERENCE AND PHASE SPECTRA FOR 20 JULY EVENING



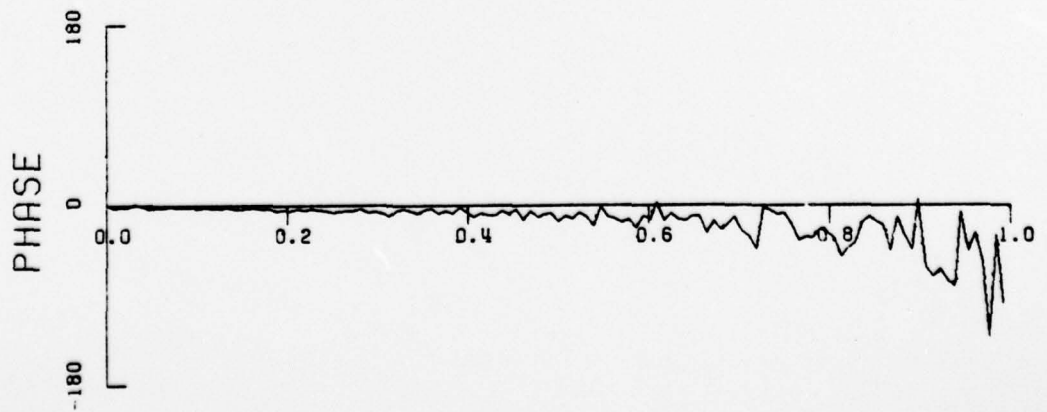
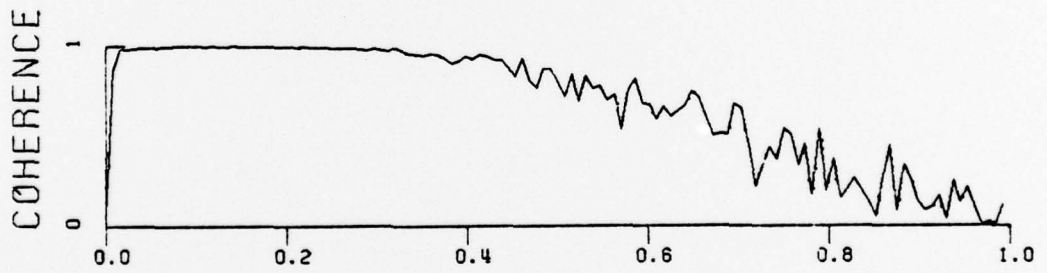
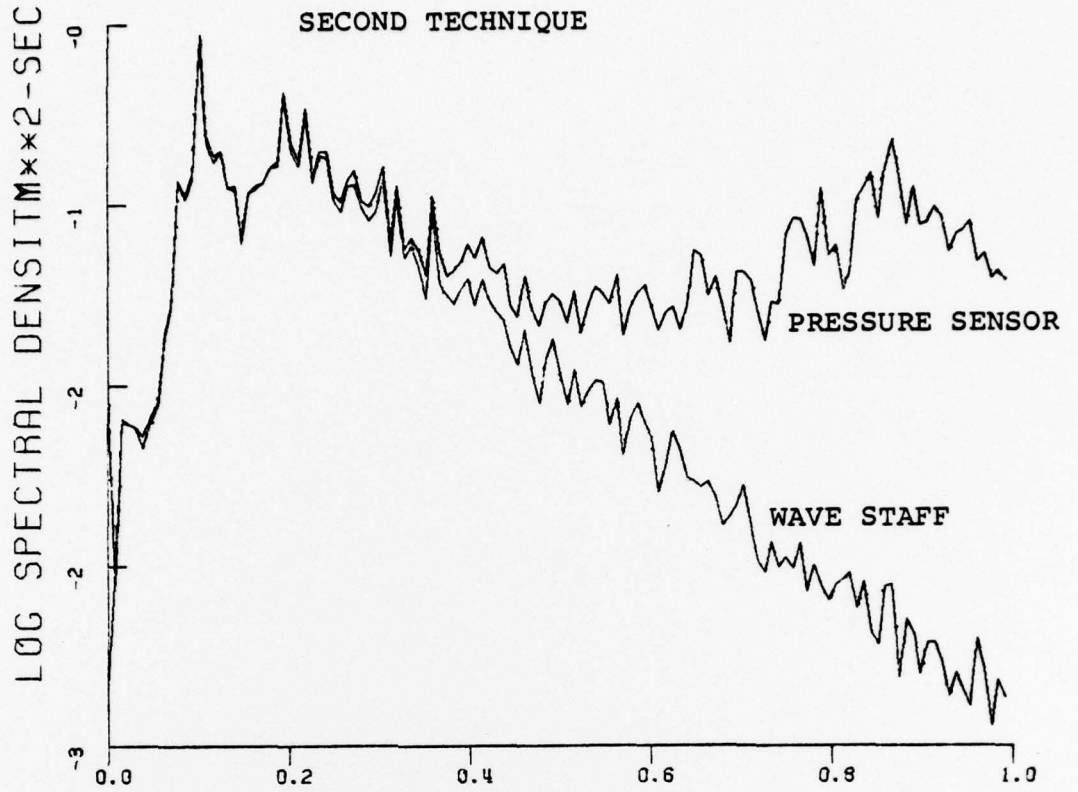
FREQUENCY (HZ)

POWER, COHERENCE AND PHASE SPECTRA FOR 20 JULY EVENING



FREQUENCY (HZ)

POWER, COHERENCE AND PHASE SPECTRA FOR 20 JULY EVENING



FREQUENCY (HZ)

TABLE VI. SURFACE ELEVATION SPECTRA FOR 19 JULY MORNING

f	$S_{\eta}(f)$ (m^2 -sec)	S_p/S_{η}	S_p^1/S_{η}	S_p^2/S_{η}	Remarks
.0156	.0816	1.154	1.134	1.128	Surf Beat
.0391	.2372	1.037	1.072	1.076	
.0469	.5072	.992	1.047	1.060	
.0547	.5016	.988	1.066	1.083	Max. Energy
.0625	.2261	.906	.999	1.022	
.0703	.1524	.941	1.012	1.021	Band Range
.0781	.1507	.967	1.025	1.039	
.0859	.1587	.922	1.001	1.024	
.1094	.1950	1.208	1.114	1.150	

APPENDIX D

f = frequency (Hz) at spectral peaks; S = spectral densities; η = wave gage
 p = pressure sensor; 1 = first technique; 2 = second technique

TABLE VII. SURFACE ELEVATION SPECTRA FOR 20 JULY MORNING

f	$s_{\eta}(f)$ (m^2 -sec)	s_p/s_{η}	s_p^1/s_{η}	s_p^2/s_{η}	Remarks
.0156	.0227	1.142	1.209	1.222	Surf Beat
.0859	.1041	1.020	1.041	1.041	
.0938	.2214	.965	1.007	1.010	
.1016	.4163	.969	1.017	1.024	Max. Energy
.1094	.3357	.998	1.040	1.046	
.1172	.2240	.989	1.024	1.025	Band Range
.1250	.1587	.921	.959	.956	
.1797	.1852	1.002	1.084	1.091	
.1875	.1695	.996	1.029	1.024	
.1953	.2723	.951	1.011	1.019	First Harmonic
.2031	.2340	.935	.985	.991	
.2109	.1888	.987	1.048	1.056	

f = frequency (Hz) at spectra peaks; s = spectral densities; η = wave gage
 p = pressure sensor; 1 = first technique; 2 = second technique

TABLE VIII. SURFACE ELEVATION SPECTRA FOR 20 JULY EVENING

f	$S_{\eta}(f)$ (m ² -sec)	S_p/S_{η}	S_p^1/S_{η}	S_p^2/S_{η}	Remarks
.0156	.0143	1.059	1.040	1.034	Surf Beat
.1016	.4298	1.013	1.062	1.063	
.1094	.1748	1.014	1.064	1.062	Max. Energy
.1172	.1455	.998	1.054	1.058	Band Range
.1250	.1615	.975	1.010	1.006	
.1953	.2630	1.000	1.035	1.037	First
.2031	.1606	1.028	1.074	1.076	
.2109	.1418	1.001	1.055	1.049	Harmonic
.2188	.2210	1.018	1.077	1.076	
.2969	.0947	1.037	1.146	1.180	Second
.3047	.1255	1.022	1.115	1.122	Harmonic

f = frequency (Hz) at spectral peaks; S = spectral densities; η = wave gage
 p = pressure sensor; 1 = first technique; 2 = second technique

BIBLIOGRAPHY

- Bowben, K. F. and White, R. A., "Measurements of the Orbital Velocities of Sea Waves and Their Use in Determining the Directional Spectrum," Journal of Geophysical Research, Vol 12, pp 33-54, 1966.
- Esteva, D. and Harris, D. L., "Comparison of Pressure and Staff Wave Gage Records," Proceedings of the Twelfth Coastal Engineering Conference, pp 101-116, September 1970.
- Gerhardt, J. R., Jehn, K. H. and Katz, I., "A Comparison of Step-, Pressure-, and Continuous-Wire-Gage Wave Recordings in the Golden Gate Channel," Transactions, American Geophysical Union, Vol 36, pp 235-250, April 1955.
- Grace, R. A., "How to Measure Waves," Ocean Industry, pp 65-69, 1970.
- Kinsman, B., "Wind Waves, Their Generation and Propagation on The Ocean Surface," Prentice-Hall, Inc., pp 133-144, 1965.
- Thornton, E. B. and Krapohl, R. F., "Water Particle Velocities Measured Under Ocean Waves," Journal of Geophysical Research, Vol 79, pp 847-852, 20 Feb 1974.
- Thornton, E. B. and Richardson, D. P., "The Kinematics of Wave Particle Velocities of Breaking Waves Within the Surf Zone," Technical Report NPS-58T 74011A, Naval Postgraduate School, Monterey, California, January 1974.
- Thornton, E. B., Galvin, J. J., Bub, F. L. and Richardson, D. P., "Kinematics of Breaking Waves Within the Surf Zone," Proceedings of the Fifteenth Conference on Coastal Engineering, pp 461-476, ASCE, 1976.
- Van Dorn, W. G., "Set-up and Run-up in Shoaling Breakers," Proceedings of the Fifteenth Conference on Coastal Engineering, pp 738-751, July 1976.
- Van Dorn, W. G., "Breaking Invariants in Shoaling Waves," Journal of Geophysical Research, Vol 83, No C6, pp 2981-2988, 20 June 1978.

INITIAL DISTRIBUTION LIST

	No. Copies
1. Defense Documentation Center Cameron Station Alexandria, Virginia 22314	2
2. Library, Code 0142 Naval Postgraduate School Monterey, California 93940	2
3. Department Chairman, Code 68 Department of Oceanography Naval Postgraduate School Monterey, California 93940	3
4. Associate Professor E. B. Thornton, Code 68Tm Department of Oceanography Naval Postgraduate School Monterey, California 93940	5
5. LT Vitor Goncalo Instituto Hidrografico, Rua das Trinas Lisbon, PORTUGAL	3
6. Oceanographer of the Navy Hoffman Building No. 2 200 Stovall Street Alexandria, Virginia 22332	1
7. Office of Naval Research Code 410 NORDA NSTS, Station, MS 39529	1
8. Dr. Robert E. Stevenson Scientific Liaison Office, ONR Scripps Institution of Oceanography La Jolla, CA 92037	1
9. Library, Code 3330 Naval Oceanographic Office Washington, D. C. 20373	1
10. SIO Library University of California, San Diego P. O. Box 2367 La Jolla, California 92037	1

11. Department of Oceanography Library 1
University of Washington
Seattle, WA 98105
12. Department of Oceanography Library 1
Oregon State University
Corvallis, Oregon 97331
13. Director 1
Naval Oceanography and Meteorology
National Space Technology Laboratories
NSTL Station, MS 39529
14. NORDA 1
NSTL Station, MS 39529
15. Commanding Officer 1
Fleet Numerical Weather Central
Monterey, CA 93940
16. Commanding Officer 1
Naval Environmental Prediction Research Facility
Monterey, CA 93940
17. Department of the Navy 1
Commander Oceanographic System Pacific
Box 1390
FPO San Francisco 96610
18. Departamento de Oceanografia 1
Instituto Hidrografico
Rua das Trinas, Lisbon, PORTUGAL
19. Direccao do Servico de Instrucao 1
Ministerio da Marinha
Praca do Comercio, Lisbon, PORTUGAL