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The basic concept involves use of a beta radiation source to generate an intense volume of ionization. Application of an electric field to plates enclosing this volume then produces separate regions of positive and negative ions through which the particulate-containing air passes. After leaving this charging stage the oppositely-charged particulate distributions enter an agglomeration stage in which the polarity on the enclosing plates is reversed, so that particles of opposite sign are brought into close proximity, hence producing agglomeration and shifting the particle distribution toward larger sizes. With 20 kV on the plates, the charging times can be on the order of one second or less. The agglomeration of the small particles onto the large ones can occur in a few seconds, depending on the mass loading. This implies that particulate filtration can be enhanced by this technique.

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1. INTRODUCTION

This report is concerned with results of the first part of a feasibility study of an improved air filtration system. It uses ionization-producing betaray isotope radiation, in conjunction with electric charging and acceleration, to cause fine particles to agglomerate, hence enhancing the subsequent collection process.

The removal of aerosol particles from a gas by any of the standard gascleaning techniques (filtration, scrubbing, or electrostatic precipitation) is known to be more difficult for submicron particles than for larger particles. Filtration methods presently in use can achieve high efficiencies of submicron particle removal, using high-efficiency HEPA filters. These filters are costly to build and replace. Moreover, frequent replacement as is necessary in some applications implies a large amount of system shutdown time. In the present state-ofthe-art inexpensive low-efficiency prefilters are used ahead of the HEPA filters to capture the bulk of the aerosol mass residing in the larger particles. The finer particles not captured by the prefilters then pass into the HEPA filters. To the extent that the prefilters can be made more efficient in capturing fine particles, the lifetime of the HEPA filters can be prolonged, with a corresponding reduction in cost and shutdown time.

The system investigated is intended to agglomerate fine particles into larger sizes so that they are more easily captured by the prefilters.

The following sections give details of the filtration enhancement system and the key physical processes including ionization, particle-charging, and agglomeration. The physical parameters of the system are presented first; then the electrical and operational parameters are determined which are required for the system to demonstrate significant radiation-induced particulate agglomeration. A preliminary evaluation of the system feasibility is then given; the report concludes with recommendations relative to the further experimental and analytical work necessary to fabricate a model and to verify the predicted filtration-enhancement characteristics of the system.

2. THE FILTRATION ENHANCEMENT SYSTEM

2.1 Basic Description

The proposed system consists of a charging stage, followed by one or more agglomerating stages (see Fig.2.1). As illustrated, each stage is essentially a cylindrical tube. Within each tube the gas flows along isolated sections, of pie-shaped cross section, partitioned from one another by radial vanes (see Fig.2.2). Along the axis of the first tube, which is the charging stage, is an inner cylinder containing radioactive material (for example, ⁸⁵Kr gas). In this stage, the gas outside the inner tube is ionized by the radiation passing through the wall of the inner tube. DC voltages of alternating sign are applied to alternating partition vanes (Fig.2.2). These applied voltages cause the ions to concentrate in separate unipolar regions. The gas containing the particles to be agglomerated flows through these unipolar regions by a flowsplitting geometry (Fig.2.2).

After the particles become charged in the charging stage, they pass into the first agglomerating stage. This stage has partitioning vanes identical to and aligned with those of the first stage, but the signs of the applied voltages are reversed. This forces oppositely-charged particles to move toward each other so that they would tend to agglomerate by collision. Particles failing to agglomerate in the first agglomerating stage pass into the next agglomerating stage where the vane voltages are again reversed. Hence, the particles, once charged, are accelerated toward oppositely-charged partners in successive passes in a sequence of agglomerating stages. The agglomerated particles can be separated from the unagglomerated particles by an appropriately designed (e. g., impactor type) gas-flow system.





Fig. 2.2. Cross Sections of Charger and Agglomerator Showing Typical Pie-Shaped Section

2.2 Areas of Investigation

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As discussed above, the basic concept involves use of a radiation source to produce separate regions of positive and negative ions through which the particulate-containing air passes (Fig. 2.2). After leaving the charging stage the oppositely-charged particulates enter an agglomeration stage (Fig. 2.1) in which the particles of opposite sign are brought into close proximity, hence producing agglomeration and shifting the particle distribution toward larger sizes. The result is that the average efficiency of the following collection system - be it scrubber, prefilter, etc. - is increased provided the average particle size is shifted past the well-known minimum (near $0.2-0.3\mu$ m particle size) in the final stage collection system. The geometry for implementation of this concept as shown in Figs. 2.1 and 2.2 should be considered as illustrative only, not limiting. Other geometries (for example, rectangular) involving the same concept can be imagined.

There are five general areas requiring investigation:

- 1) Production of ionization by the radiation source.
- Separation of ionization to produce a distribution having regions of predominantly positive and negative ions.
- 3) Charging of the particulates by the ions.
- 4) Agglomeration of the charged particles to shift distribution toward larger sizes.
- 5) Collection (filtration) of the altered particulate distribution.

As a first step in demonstrating feasibility of this concept it is necessary to show that sufficient ionization can be generated by realistic activity radioactive sources. The possibility of using ⁶⁰Co gamma radiation to generate ionization-producing electrons in a duct wall has been investigated by Heinsohn et al. (Ref.2.1). Their intent was to produce charged particulates for purposes of electrostatic collection, a completely different objective from the present work. Furthermore, they did not separate the region of ionization production from those in

which the positive and negative ion distributions are maintained, as is done in Fig. 2.2. We believe that a beta source, which emits electrons directly, will prove to be of greater utility from the point-of-view of both handling and ionization production, than will a high energy gamma source. Krypton-85 appears to us to be of particular interest because of its availability, specific activity, and the range of its betas (up to ~ 200 cm). Hence the basic feasibility of producing ionization with this source is considered in some detail below. This is followed by a more general discussion of the other areas above, including the analytical methods applied to each.

In order to carry out the investigations of charging and agglomeration, it is desirable to consider particular particle size distributions. A number of typical particle size distributions encountered in nuclear materials handling facilities, and characterized as log-normal, are summarized in Table 2.1. This table is taken directly from a report by Lawrence Livermore Laboratory, where enhanced filtration mechanisms of a different type than that of interest here, are being investigated. It is seen that the particulates generally cover the range of about 0.2 to 30 microns, with median diameters of a few microns and standard deviations of 2-5.

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Table 2.1

• Facility	Process	Aerodynamic mass median diameter (µm)	Geometric std. dev. (0) g	Range (µm)	Principal constituents
LASL (6)	R&D	1.8	2.2	0.4 - 8.7	Pu
and the second second	R&D	2.3	3.5	0.2 - 28	Pu
	Fabrication	4.0	1.7	1.4 - 12	Pu
	Recovery	0.34	5.4	0.01 - 9.9	Pu
	Fabrication	2.7	2.4	0.5 - 16	Pu
Rocky Flats ⁽⁷⁾	Recovery .	0.9 ^a	~3	<0.3 - 13.7	Pu, HF, HNO3
"Demonstration Plant"b	Grinding, 750°C	15.9	1.59	-	Pu U
"Industrial Plant" ^b	Grinding, 750°C	1.88	1.76	-	Pu U
"Demonstration, Industrial Plant" ^b	Grinding, 1750°C	2.30	1.65	-	Pu U
"Industrial Plant" ^b	Grinding, 1750°C	2.09	1.61	-	Pu U

Typical particle distributions encountered in nuclear materials handling facilities. (From Ref. 2.2)

^a Count median diameter.

ς,

^b G. Newton, Lovelace Foundation, private communication.

References 6) and 7) above are as follows:

- 6) H. J. Ettinger, J. C. Elder and M. Gonzales, Performance of Multiple HEPA Filters Against Plutonium Aerosols, LASL Report No. LA-5349-PR(1973).
- 7) R. W. Woodward, K. J. Grossaint, and J. L. McFeeters, Exhaust Filtration on Gloveboxes used for Aqueous Processing of Plutonium, 14th ERDA Air Cleaning Conference, Sun Valley, Idaho (1976).

3. CYLINDRICAL BETA SOURCE INDUCED IONIZATION DISTRIBUTION

In this section the ionization distribution results obtained from the ⁸⁵Kr beta source are presented and discussed first. This is followed by an analytical estimate of the ionization based on neglect of all scattering effects. This is known to be a poor approximation if the actual number distribution of the electrons is of interest. However, it is found here that reasonably good agreement with the experimental measurements can be obtained by this simple approach when only the ionization distribution is of interest.

3.1 Experimental Results

The basic configuration of the ⁸⁵Kr gaseous source used in this work is shown in the top portion of Fig. 2.2. The cylindrical beta source itself is surrounded by a collimator designed to limit the ionization region in the manner shown there. Fig. 3.1 is a reduction of a full-scale drawing of the source. The fabrication is completed by soldering a thin brass foil (~2 mil) over the entire outer surface to seal the assembly. The slots are the regions through which the betas enter the collimator apertures in Fig.2.2; the solid portions of the source would be obscured by the collimator walls. This is necessary due to the scattering of the betas after passing through foil.

3.1.1 Measurement of Source Activity

The source was filled with gas to 0.10 atm. Since the specific activity of the gas was not precisely known, the resulting activity of the source was measured with the method outlined in Fig. 3.2.





Fig. 3.2. Geometry for Measurement of ⁸⁵Kr Ionization Source Activity.

A well-shielded (2 inches of lead in all directions) 3 inch diameterx 3 inch deep NaI(T1) crystal was used to detect the 0.514 MeV γ -ray emitted by ⁸⁵Kr in 0.41% of all decays. A central 1/2 inch diameter portion of the NaI(T1) crystal was irradiated by a 3/4 inch section of the Kr source, all other portions of the source being shielded by 2 inches of lead. A piece of 1/8 inch aluminum was used to absorb the emitted beta particles and shield the NaI(T1) crystal from this interference.

The total source activity can be written as

1

$$S_{a} = \frac{C_{p}}{\epsilon_{p} F_{o} F_{v} F_{s} t_{a} t_{s}^{\dagger}}$$
(3.1)

where S_a is the source activity in disintegrations/sec, C_p is the measured NaI(T1) count rate in the full energy peak (0.514 MeV) in cps, $\epsilon_p \simeq 0.80$ is the detection efficiency for the full energy peak, $F_o = 1.09 \times 10^{-4}$ is the fractional solid angle (of 4π) of the 1/2 inch diameter collimator, $F_v = 4.1 \times 10^{-3}$ is the yield of 0.514 MeV γ -rays from 85 Kr, $F_s = 6.4 \times 10^{-2}$ is the fraction of the source viewed by the NaI(T1) crystal, $t_{A1} = 0.93$ is the transmission of 1/8 inch Al for the 0.514 MeV γ -rays, and $t_s = 0.91$ is the transmission of the source walls for the 0.514 MeV γ -ray. The measurements gave $S_a = 1.04 \times 10^{10}$ /sec, or $S_a = 0.28$ Ci of 85 Kr.

The method was checked by also measuring the activity of a 10μ Ci¹³⁷Cs calibration source, detecting the 0.662 MeV γ -ray emitted in 85% of all decays ($F_y = 0.85$). Here $F_s = 1$, $t_s = 1$, $t_{A1} = 0.86$, $\epsilon_p \simeq 0.75$, and F_o is the same. The result gave 10.4 μ Ci, and thus demonstrated the accuracy of the measurement.

The measurements show that the gas in the source is 1.7% ⁸⁵Kr by volume. Since the active volume of the source is 30.0 cm long, the specific activity of the source is 0.0093 Ci/cm.

3.1.2 Measurement of Ionization Distribution

5

The Kr ionization source was placed in the center of a four ft. long by 17-1/4 inch ID steel pipe (3/8 inch wall) and the radial ionization profile measured. This geometry was designed to simulate that of Fig. 2.2, except that the vanes and collimator are not present. The method is illustrated below.





The ionization chamber is of the open-gridded air type, as described in Ref. 3.1. An outer shield mesh is held at ground potential, with an inner bias mesh 1.5 cm in diameter and 12.7 cm long defining the sensitive volume. The central wire is grounded through an electrometer to measure the ion current, while the inner mesh is held at $\pm 100V$ through a 10 M Ω resistor. Tests of the ion chamber showed negligible current change for biases more than $\pm 30V$, and the sign of the bias voltage only affected the sign of the current measured, not its magnitude. The shield mesh voltage had a negligible effect on the measured current in the absence of significant air currents, and so was kept grounded. In the absence of ionizing radiation the leakage current was measured to be less than $\pm 1 \times 10^{-14}$ A for bias grid voltages of $\pm 100V$. The sensitive volume of the ion chamber is 22.0 cm³, and it has been corrected for the volume of the central wire and bias grid support structure.

The ion chamber was scanned over center-to-center distances (radial, Kr source to ion chamber) of R=5.5 to 17 cm, and the current measured. The current ranged from 4.50×10^{-10} A to 1.26×10^{-10} A. The ion production rates are

$$Q = I/(eV_{i})$$
 (3.2)

where Q is in ion pairs/(cm³-sec), I is the measured ion chamber current in A, $e=1.60 \times 10^{-19}$ C is the electron charge, and $V_i=22.0$ cm³ is the ion chamber sensitive volume. The resulting Q profile, normalized to the source intensity, is shown in Fig. 3.4. The estimated uncertainty is $\pm 20\%$.

At distances of 6-18 cm from the source, measurements were also made of the ionization distribution along a circumference. Very little such dependence was found, indicating that atmospheric scattering is a large effect, particularly in the absence of the collimators of Fig. 2.2.



3.2 Analytical Determination

Exact calculation of ionization distributions around sources such as that of Fig. 3.1 can only be made by Monte Carlo methods, in which scattering is included. Here we will make a calculation based on the approximation in which scattering is entirely neglected.

Consider the geometry shown in Fig. 3.5, which shows the source cross section and two points (a distance R from the source center) at which the calculation of ionization is to be made. Neglecting scattering, in each case only beta particles emitted from gas in the shaded areas can reach the points of interest. Note that, for the distance R shown (equivalent to 10 cm in actual scale) the effective area is about the same in each case. The measurements reported in 3.1 above found, in fact, that there was little dependence of the ionization rate on circumferential location. Hence, to do the calculation here we can replace the actual source by an "equivalent" source: an infinitely thin line source, covered by the foil, and having a source intensity equal to the average effective fraction of the gas in Fig. 3.5 times the actual source intensity. This fraction we find by graphical integration to be $f_e = 0.2116$ at R = 10 cm, and it is almost independent of R from 5 to 20 cm. The geometry for the calculation is given in Fig. 3.6.

The length of the source is L(cm), covered by a brass foil of thickness $t_f(mil)$. The effective source intensity is

$$S_e = f_e S_a e/sec$$
(3.3)

emitted isotropically into 4π steradians. The number of betas emitted per second from the element of length dX is the energy range dE (keV) is

$$j(E)dEdX = (S_{L})\nu(E)dEdX \qquad (3.4)$$

where j(E)e/(sec-keV-cm) is the emitted spectrum, normalized per unit length of the cylinder, and $\nu(E)$, which contains the energy dependence, is normalized to unity. From Ref. 3.2 it is seen that the spectrum is almost flat from 0 to 300 keV,

Fig. 3.6 Geometry for Analytical Determination of Ionization Rate from Equivalent Source.

decreases linearly above the energy $E_s = 300$ keV and is zero at a maximum energy $E_m = 670$ keV. Thus we set

$$\begin{aligned} \nu(\mathbf{E}) d\mathbf{E} &= \nu_{o} d\mathbf{E} & 0 < \mathbf{E} < \mathbf{E}_{s} \\ &= \nu_{o} d\mathbf{E} (\mathbf{E}_{m} - \mathbf{E}) / (\mathbf{E}_{m} - \mathbf{E}_{s}) \mathbf{E}_{s} \leq \mathbf{E} < \mathbf{E}_{m} \\ &= 0 & \mathbf{E} \geq \mathbf{E}_{m} \end{aligned}$$
 (3.5)

and require that

which yields

1

$$\nu_{\rm o} = 2/({\rm E_s} + {\rm E_m}) \, {\rm keV}^{-1}$$
 (3.6)

completing the definition of $\nu(E)$ in (3.5) for use in (3.4).

The betas leave the element dX and pass through the foil and also through a length h(X) of air of density $\rho(g/cm^3) = 1.3 \times 10^{-3} g/cm^3$, where

$$h(X)^{2} = R^{2} + (X - \nu)^{2} cm^{2}$$
 (3.7)

As a result the energy is changed from E to E', and the flux of betas emitted by the element dX in the energy range dE' through the area A' at the point of interest is $F(E')e/(cm^2-sec-keV-cm)$, where

$$F(E')dE'dX = \frac{j(E)dEdX}{4\pi h(X)^2}$$
(3.8)

The energy deposition rate $\mathcal{E}(\text{keV-cm}^{-3}-\text{sec}^{-1})$ at the point of interest, due to the entire beta spectrum and source length, is

$$\mathcal{E}(\mathbf{R}, \mathbf{v}) = \int_{\mathbf{X}} \int_{\mathbf{E}'} \rho S(\mathbf{E}') F(\mathbf{E}') d\mathbf{E}' d\mathbf{X}$$
$$= \frac{\rho f S_a}{4\pi L} \int_{\mathbf{0}} \frac{d\mathbf{X}}{h(\mathbf{X})^2} \int_{\mathbf{0}}^{\mathbf{E}} S(\mathbf{E}') \nu(\mathbf{E}) d\mathbf{E} \qquad (3.9)$$

The energy integral depends upon X and t_f through evaluation of the stopping power $S(E')(keV-g^{-1}-cm^2)$ at the energy E'(keV). For purposes of calculating the energy loss, the path length traversed is expressed in g/cm^2 . Thus,

$$R(g/cm^2) = \rho R(cm)$$
 (3.10)

Since the ratio of stopping power for copper (the foil is actually brass, but is essentially copper for present purposes) to that of air is almost independent of energy. we can equate the foil to an amount of air that would produce the same energy loss. Use of S(E) data from Ref. 3.3 for Cu and air yields

$$t_{f}(g/cm^{2} air equiv.) = .01745 t_{f} (mils Cu)$$
 (3.11)

Hence, the path length $T(g/cm^2 air)$ for a given R is

$$T = .01745 t_c(mils) + .0013 R(cm)$$
 (3.12)

and the path length equivalent to h(X) in g/cm^2 is then obtained from simple geometry and (3.12). (See (3.22) below).

The stopping power of air (Ref. 3.3) can be fitted by the following function with an error not exceeding about +22% from 10 to 900 keV,

$$S(E') = S_{0}(1 + E'/E_{0})^{-m}$$
 (3.13)

where

$$S_o = 5.778 \times 10^5 \text{ keV} - \text{g}^{-1} - \text{cm}^2$$
 (3.14)

$$m = .5478$$
 (3.15)

$$E_0 = .0135 \text{ keV}$$
 (3.16)

This stopping power expression is too low by about 40% at 1 keV, correct at 0.1 keV and too high below that. However, since the range of a 10 keV electron in air is only about 0.2 cm, inaccuracies in S(E) below 10 keV are unimportant for the present work. The total energy of each particle is deposited in the air surrounding the source no matter what S(E) expression is used; the present expression could lead to errors of 0.2 cm <u>at most</u> in the $\xi(R, v)$ distribution. This error is certainly small compared to that due to neglect of scattering.

A significant advantage of the expression (3.13) is that it can be integrated to yield the distance $r(g/cm^2 air)$ required to change the energy from E to E',

$$\mathbf{r} = \int_{\mathbf{E}'}^{\mathbf{E}} d\mathbf{E}'/S(\mathbf{E}') \qquad (3.17)$$
$$= \frac{\mathbf{E}_{o}}{S_{o}(m+1)} \left[(1 + \mathbf{E}/\mathbf{E}_{o})^{m+1} - (1 + \mathbf{E}'/\mathbf{E}_{o})^{m+1} \right] \qquad (3.18)$$

The range-energy E_r is that value of E for which the residual energy E'=0 at r:

$$E_{r}(r) = E_{o} \left\{ \left[1 + S_{o}(m+1)r/E_{o} \right]^{1/(m+1)} - 1 \right\}$$
(3.19)

Solving (3.18) for E', and using it in (3.13) along with (3.19) shows that S(E') can be written in terms of the initial energy E and the range energy E_r

$$S(E') = S_f(E)$$
 (3.20)

where

0

. .

$$f(E) = [1 + (1 + E/E_o)^{m+1} - (1 + E_r/E_o)^{m+1}]^{-m/(m+1)} (3.21)$$

 E_r is evaluated for that path length r in g/cm² equivalent to the distance h(X) in Fig. 3.6, i.e.

 $r(X,v) = T \sqrt{1 + (X-v)^2/R^2}$ (3.22)

where T is given by (3.12).

The ion -electron pair production rate Q(R, v) ion pairs-cm⁻³-sec⁻¹ is given by

$$Q(R, v) = E(R, v)/I_{1}$$
 (3.23)

where $I_i = .035 \text{ keV/ion pair is the energy deposition in air necessary to create one ion-electron pair. By use of (3.9) and (3.20) this result can be written$

$$Q(\mathbf{R}, \mathbf{v})/S_{\mathbf{a}} = \int_{0}^{L} (Q_{\mathbf{x}}(\mathbf{R}, \mathbf{v})/S_{\mathbf{a}}) d\mathbf{X}$$
(3.24)

where

$$Q_{x}(\mathbf{R}, \mathbf{v})/S_{a} = \frac{\rho f S_{o}}{4\pi I_{i} Lh(X)^{2}} \int_{\mathbf{E}_{r}}^{\mathbf{E}_{m}} f(\mathbf{E}) \nu(\mathbf{E}) d\mathbf{E}$$
(3.25)

The lower limit on the energy integral has been replaced by E_r from (3.19) with r given by (3.22), since no particles with energy less than this can reach the point of interest. The result (3.24) is called the specific ionization rate. By converting S₂ from e/sec to curies (Ci), where

$$1 \text{ Ci} = 3.7 \times 10^{10} \text{ e/sec}$$
 (3.26)

the units of Q/S_a are ion pairs/(cm³-sec-Ci), and that of Q_x/S_a , the specific ionization rate per unit length, are ion pairs/(cm³-sec-Ci-cm).

A FORTRAN program for computing the result (3.25) by double numerical integration is given in Table 3.1. The program input and typical output are given in Tables 3.2 and 3.3. The output tabulates (3.25) and (3.10) vs X and provides the final result (3.24) for that value of R following the table. More detailed results are given in Fig. 3.4, labelled "Analytical Result Neglecting Scattering." In general, it can be seen that the calculations agree rather well with the experimental data, thus reinforcing the general accuracy of both results.

As typical values for use in the charging and agglomeration work we choose R = 10 cm and $S_a = 500 \text{ Ci}$, for which

$$Q \approx 10^{11}$$
 ion pairs/(cm³-sec) (3.27)

We note that this rate drops only by about a factor of 2 between 10 and 20 cm, so that a high rate is maintained throughout the volume of interest.

0		21 FROM COPY FURNISHED TO DDC
0	100	END THIS PAGE IS BEST QUALITY PRACTICABL
0	107	1' QX/SA=IONS/(CM**3-SEC-CURIE-CM); ER=KEV'/)
12	106	FORMAT(// X QX/SA ER')
	105	FORMAT('FOIL+MIN AIR PATH RANGE ENERGY, KEV='F6.1)
1	104	FORMAT('CU FOIL THICKNESS, MILS='F4.1)
	102	FORMAT(' R='F5.1,' CM Q/SA='E11.4' IONS/(CM**3-SEC-CURIE)'/)
	101	FURMAT('NX='13/'NL='13/'EMIN='F5+0) FORMAT(F5-1-F12-4-F7-1)
	100	G0 T0 20 FORMAT('L='F5.1/'V='F5.1/'RMIN='F5.1/'DELR='F5.1/'RMAX='F5.1) FORMAT('NX='I3/'NE='F5.1/'RMIN='F5.0)
		QEI=DX*QEI WRITE(1,103)R,QEI
	80	QEI=QEI+QEX
		QEX=QEJ#VL#DE#FRAC/(R#SQ)##2 WRITE(1.102)X.CEX.ER
	60	CONTINUE
	35 40	EN=(EM-EJ)/EMS QEJ=QEJ+FJ*EN
	30	EN=1. IF(FJ-FS)40.40.35
	70	IF(EJ-ER)60,60,30 F = ((1, +F)/(EO)) + EM1 = 1000 + 4EM1
		DO 60 J=1,NE E.J=EMIN+DE*(ELOAT(J)-,5)
-		ER=EO*((1.+DUM)**EMR-1.) GEJ=0
1		SQ=SQRT(1++((X-V)/R)**2)
		DU 80 I=1,NX X=DX*(FLOAT(I)5)
		WRITE(1,106)
	25	QEI=0 Cýlindrical Beta Source.
		IF (R-RMAX) 25, 25, 10 for Calculation of Ionization Rate due to
	20	R=R+IIR Table 3.1 FORTRAN Program CYLION
		WRITE(1,107)DE
		DE=(EM-EMIN)/FLOAT(NE)
	·	EMS=370.
		EM=670.
		ES=300+
		EM1=1.5478
		DX=EL/FLOAT(NX)
		WRITE(1,105)DUM READ(1,101)NY.NE.EMIN
		DUM=E0*((1.+(TF+RMIN*1.3E-03)/RO)**EMR-1.)
		READ(1,104)TF TE=1.745E-02*TE
•		E0=.0135
4		R0=1.5095E-08 FMR=.64608
-	10	READ(1,100)EL,V,RMIN,DR,RMAX
1 60		FRAC=,2116 WRITE(1,108)
	C	USE AVG OF RATES FROM OPEN AND OBSCURED SECTIONS.
492	c	BETA RAY SOURCE, 3/28/78.
6	C	CYLION FT: FIND ION DEPOSITION RATE FROM CYLINDRICAL

.

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AND THE ME

R CYLION

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5.6

ALL LENGTHS ARE IN CM, ENERGIES IN KEV

L=30 . . V=15. RMIN=10. DELR=10. RMAX=20. CU FOIL THICKNESS, MILS=2.0 FOIL+MIN AIR PATH RANGE ENERGY, KEV= 214.2 NX=30 NE=230 EMIN=210. DELTA E= 2.0 KEV

X=CM, QX/SA=IONS/(CM**3-SEC-CURIE-CM), ER=KEV

X QX/SA ER 0.5 0.3301E+07 308.8 1.5 Ø.3566E+Ø7 299.5 2.5 0.4211E+07 290.3 3.5 0.4680E+07 281.2 4.5 0.5541E+07 272.3 5.5 0.6203E+07 263.7 6.5 0.7017E+07 255.3 7.5 Ø.7979E+07 247.4 8.5 Ø.9136E+Ø7 240.0 9.5 0.1003E+08 233.3 10.5 0.1110E+08 227.3 11.5 Ø.1242E+Ø8 222.3 12.5 Ø.1333E+Ø8 218.4 13.5 0.1368E+08 215.7 14.5 Ø.1428E+Ø8 214.4 15.5 Ø.1428E+Ø8 214.4 16.5 Ø.1368E+Ø8 215.7 17.5 Ø.1333E+Ø8 218.4 18.5 Ø.1242E+Ø8 222.3 19.5 0.1110E+08 227.3 20.5 0.1003E+08 233.3 21.5 Ø.9136E+Ø7 240.0 22.5 Ø.7979E+Ø7 247.4 23.5 0.7017E+07 255.3 24.5 0.6203E+07 263.7 25.5 Ø.5541E+Ø7 272.3 26.5 Ø.468ØE+Ø7 281.2 27.5 Ø.4211E+Ø7 290.3 28.5 Ø.3566E+Ø7 299.5 29.5 0.3301E+07 308.8 R= 10.0 CM Q/SA= 0.2530E+09 IONS/(CM**3-SEC-CURIE)

Table 3.2 Input to Program CYLION and Output for R = 10 cm.

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х	QX/SA	ER
0.5	Ø.1844E+Ø7	286.7
1.5.	Ø.1927E+Ø7	282.4
2.5	Ø.2040E+07	278.3
3.5	Ø.2172E+Ø7	274.3
4.5	0.2334E+07	270.6
5.5	Ø-2346E+Ø7	267.1
6.5	0.2515E+07	263.9
7.5	0.3147E+07	261.0
8.5	Ø.2788E+07	258.4
9.5	Ø.2859E+07	256.1
10.5	0.2954E+07	254.2
11.5	Ø.3087E+07	252.6
12.5	0.3024E+07	251.4
13.5	0.3187E+07	250.6
14.5	Ø.3149E+Ø7	250.2
15.5	0.3149E+07	250.2
16.5	Ø.3187E+Ø7	250.6
17.5	0.3024E+07	251.4
18.5	0.3087E+07	252.6
19.5	Ø.2954E+Ø7	254.2
20.5	Ø.2859E+Ø7	256.1
21.5	Ø.2788E+Ø7	258.4
22.5	Ø.3147E+Ø7	261.0
23.5	0.2515E+07	263.9
24.5	0.2346E+07	267.1
25.5	Ø.2334E+Ø7	270.6
26.5	Ø.2172E+Ø7	274.3
27.5	0.2040E+07	278.3
28.5	Ø.1927E+Ø7	282.4
29.5	Ø.1844E+07	286.7
D= 00	A CM OVER	- 0. 797454

0

-

0

Table 3.3 Output of Program CYLION for R = 20 cm.

0.0 CM Q/SA= 0.7874E+08 IONS/(CM**3-SEC-CURIE)

4. CHARGE GENERATION AND SEPARATION

The generation and separation of charge takes place in one cylindrical section, as shown in Figs. 2.1 and 2.2. The idealized geometry of one segment of this cylinder is shown in Fig. 4.1. The 85 Kr produces ionization in the central portion of the segment, with a potential V_0 (volts) across the section edge plates. For simplification in the theoretical analysis of the charge separation, the reduced variable y (range 0 to 1) is introduced, and plane parallel geometry is assumed with the separation $d = R\theta$ being a (variable) parameter.

Fig. 4.1. Geometry of Charge Generation and Separation Section.

The charge density and electric field equations can be written as

$$-\left(\frac{Dn_{o}}{Q_{o}d^{2}}\right)\frac{d^{2}N_{+}}{dy^{2}} + \left(\frac{\mu En_{o}}{Q_{o}d}\right)\frac{dN_{+}}{dy} = \frac{Q}{Q_{o}} - \left(\frac{\alpha n_{o}^{2}}{Q_{o}}\right)N_{+}N_{-}$$
(4.1)
$$-\left(\frac{4\pi e\mu n_{o}^{2}}{Q_{o}}\right)N_{+}(N_{+}-N_{-})$$

$$-\left(\frac{Dn_{o}}{Q_{o}d^{2}}\right)\frac{d^{2}N_{-}}{dy^{2}} - \left(\frac{\mu En_{o}}{Q_{o}d}\right)\frac{dN_{-}}{dy} = \frac{Q}{Q_{o}} - \left(\frac{\alpha n_{o}^{2}}{Q_{o}}\right)N_{+}N_{-}$$
(4.2)

+
$$\left(\frac{4\pi e\mu n_o^2}{Q_o}\right) N_(N_+ - N_-)$$

and

$$\frac{dE}{dx} = (4\pi en_0)(N_+ - N_-)$$
 (4.3)

where D is the diffusion coefficient, $Q_0 \simeq 10^{11}/(\text{cm}^3 \text{-sec})$ is the estimated ion pair production rate at (typically) R=10 cm (Sec. 3), $n_0 = \sqrt{Q_0/\alpha} \approx 2.4 \times 10^8/\text{cm}^3$ is the zero field equilibrium ion density for a recombination coefficient $\alpha \simeq 1.7 \times 10^{-6} \text{ cm}^3/\text{sec}$ for air, $\mu \simeq 1 \text{ cm}^2/(\text{V-sec})$ is the ion mobility in air, and $N_{\pm} = n_{\pm}/n_0$ are the normalized positive/negative ion densities, E is the electric field, and d and y are as defined in Fig. 4.1. We define

$$\phi_{o} = \frac{\mu n_{o} V_{o}}{Q_{o} d^{2}} = \frac{\mu V_{o}}{d^{2} \sqrt{Q_{o} d}}$$

$$\approx V_{o} (\text{volts})/41231, \text{ for } d = 10 \text{ cm}, \qquad (4.4)$$

neglect the diffusion term $(D/d \ll \mu E$ for reasonable E), and obtain

$$\phi_0 \frac{E}{E_0} \frac{dN_+}{dy} \simeq \frac{Q}{Q_0} - N_+ N_- - PN_+^2 + PN_+ N_-$$
 (4.5)

$$-\phi_0 \frac{E}{E_0} \frac{dN_{-}}{dy} \approx \frac{Q}{Q_0} - N_{+}N_{-} - PN_{-}^2 + PN_{+}N_{-} \qquad (4.6)$$

where $P = 4\pi \mu en_0^2 / Q_0 = 4\pi \mu e / \alpha \approx 1.06$ and $E_0 = V_0 / d$.

The N_+N_- terms in (4.5) and (4.6) drop out if P = 1, and since P is very nearly 1.0, we set P = 1.0 and obtain a simplified set of equations (an approach consistent with the present feasibility determination):

$$\phi_{0} \frac{E}{E_{0}} \frac{dN_{+}}{dy} \simeq \frac{Q}{Q_{0}} - N_{+}^{2}$$
(4.7)

$$-\phi_{0}\frac{E}{E_{0}}\frac{dN_{-}}{dy}\simeq\frac{Q}{Q_{0}}-N_{-}^{2}$$
(4.8)

and

$$\frac{d^2 \phi}{dy^2} = N_{-} - N_{+}$$
 (4.9)

where $\phi = \mu n_0 V/(Q_0 d^2)$, with V the potential at position y.

Consider the situation of Fig. 4.1, where Q=0 for $0 \le y < y_1$, and $y_2 < y \le 1$, and Q=Q₀ for $y_1 \le y \le y_2$. For this case the solution to (4.7), (4.8) and (4.9) can be written as:

$$0 \le y \le y_{1}: \qquad N_{+} = 0 \qquad (4.10)$$

$$N_{-} = \left[\frac{1}{N_{0}} + \int_{0}^{y} \frac{dy}{-d\phi/dy}\right]^{-1} \qquad (4.10)$$

$$y_{1} \le y \le y_{2}: \qquad N_{+} = \tanh\left[\int_{y_{1}}^{y} \frac{dy}{-d\phi/dy}\right] \qquad (4.11)$$

$$N_{-} = \tanh\left[\int_{y}^{y} \frac{dy}{-d\phi/dy}\right]$$

 $y_2 \le y \le l$:

$$N_{+} = \left[\frac{1}{N_{0}} + \int_{y_{2}}^{y} \frac{dy}{-d\phi/dy}\right]^{-1}$$

$$N_{-} = 0$$
(4.12)

where

$$N_{o} = \tanh\left[\int_{y_{1}}^{y_{2}} \frac{dy}{-d\phi/dy}\right]$$
(4.13)

The set of equations (4.10) to (4.13) can be used to solve for N_+ , N_- , and ϕ , all as functions of y, by splitting $0 \le y \le 1$ into several segments and numerically solving for the values at each breakpoint. This has been done for 16 breakpoints (including y=0 and 1), and the results for N_+ and N_- are plotted in Fig. 4.2 for three values of ϕ_0 . Only one N_- profile has been plotted, since all N_- profiles are the N_+ profiles reflected about y=0.5. Note that the results imply that some optimum value of ϕ_0 exists which maximizes $N_+(y=1)$.

The net charge separation $(N_{+} - N_{-})$ is plotted in Fig. 4.3. As a result of the method of normalizing to n_0 , the results do not depend explicitly on Q, the ion-electron production rate. Q must be determined analytically and experimentally to allow more accurate calculations for N_{+} , N_{-} . Figure 4.3 shows that while small ϕ_0 maximizes the charge separation at $y = y_1, y_2$, the maximum integrated charge separation is for some intermediate value of ϕ_0 . The best value of ϕ_0 is that which maximizes

$$N_{sep} = \int_{0.5}^{1} (N_{+} - N_{-}) dy \qquad (4.14)$$

and this can be readily done by numerical calculations. Because of the normalization of N₊ and N₋ to n_o, there is a single optimum for ϕ_0 , and the corresponding V_o can be readily determined from Eq. (4.4) for any set of parameters d, etc. Since d and n_o = $\sqrt{Q_0/\alpha}$ vary somewhat with R (see Fig. 4.1), the optimum V_o varies slightly with R, and a suitable average value will have to be selected. From Fig. 4.3 it can be seen that net charge concentrations

of >0.5 n_o can be achieved in the separation regions, so that separated charge densities of more than half the equilibrium electron-ion density n_o can be achieved. That these densities will be sufficient to induce an amount of charge on particulates that will cause significant agglomeration in that section of the device is investigated in Section 5.

4.1

The geometry of Fig. 4.1 is idealized, since in practice the ionization region will not have sharp boundaries. Indeed, the results of Section 3 show that beta particle scattering produces very significant effects. However, the theoretical analysis shows that significant charge separation can be achieved and gives numerical values for the approximate optimum potential V_0 . This helps significantly in guiding any experimental work done in the next stage of work.

5. PARTICLE CHARGING AND AGGLOMERATION

In this section we consider how the particles are charged in the charger (Sec. 5.1) and how they are then agglomerated in the agglomerator (Sec. 5.2). We assume (a) that there are essentially two populations: "small" particles below about one micrometer in radius (subscripts 1), and "large" particles above about one micrometer in radius (subscripts 2); and (b) that the small particles agglomerate onto the large particles.

5.1 Charging Section

In the charging section we assume that the particles find themselves in a charging environment where there are unipolar ions of density n_+ , and an electric field of intensity E_{ch} . We assume the particles are exposed to this environment for an interval of one second. (The results are insensitive to the exact value of this time interval.) For small particles, the charging is generally dominated by the "diffusion" mechanism, while for large particles the charging is generally dominated by the "field" (conduction) charging mechanism (R ef. 5.1,5.2). For the present purposes, we assume here that the small and large particles are charged only by diffusion and conduction, respectively.

5.1.1 Diffusion Charging

For diffusion charging, which is appropriate for small particles, the number of elementary charges acquired in time t is given [Ref. 5.1, Eq. (3.61); Ref. 5.2, Eq. (5.27)] by:

$$n_1 = \frac{RkT}{e^2} \ln\left(1 + \frac{t}{\tau_D}\right)$$
(5.1)

where

$$\tau_{\rm D} = \frac{kT}{\pi e^2 U_{\rm i} n_{\rm +} R}$$
(5.2)

where R is the radius of the particle, n_{+} is the undisturbed ion density, e is the magnitude of the electron charge, U_{i} is the rms thermal velocity of the ions, k is Boltzmann's constant, and T is the absolute temperature. At room tem-

perature, we take $kT = 4x10^{-14}$ erg and $U_i = 5x10^4$ cm/sec for nitrogen molecules, and we may write:

$$\frac{e^2}{RkT} = \frac{5.76 \times 10^{-6}}{R}$$
(5.3)

$$\tau_{\rm D} = \frac{1}{0.905 {\rm n_{\perp}R}} \, {\rm sec}$$
 (5.4)

$$n_1 = 1.736 \times 10^5 R \ln(1 + 0.905 n_+ Rt)$$
 (5.5)

Assuming (a) the optimum value of E_{ch} for separating the positive and negative ions (given by $\phi_0 \approx 0.378$ in Section 4), (b) a distance of d = 10 cm = arc length between the plates, and (c) a local source ionization rate of $Q_0 = 10^{11}$ ion pairs per cm³ per sec, we obtain a value $n_{+} \approx 1.5 \times 10^{8}$ cm⁻³ for ion density, at a voltage of about 15600 volts across the plates and a field intensity of $E_{ch} = 5.2$ statvolts/cm. (The value of n_{+} is the average value of the ion density profile, that is, about 60% of the nominal ion density $n_{0} = \sqrt{Q_{0}/\alpha}$, where Q_{0} is the ionization rate = 10^{11} cm⁻³ sec⁻¹, and α is the recombination coefficient = 1.7×10^{-6} cm³ sec⁻¹.)

For particles of radius R = 0.1 micrometer, and $n_{+} = 1.5 \times 10^{8} \text{ cm}^{-3}$, Eq. (5.1) becomes

 $n_1 = 1.736 \ln(1 + 1358t)$ (5.6)

= 12.52 charges in one second.

Note that this charging is insensitive to the time t and to the ion density n_{+} because of the logarithm. It is explicitly independent of the charging field E_{ch} , but n_{+} depends on this as seen in the previous section.

5.1.2 Conduction (or Field) Charging

For conduction (or "field") charging, which is appropriate for large particles, the number of elementary charges of magnitude e acquired in time t is given [Ref. 5.1, Eq. (3.58); Ref. 5.2, Eq. (5.15)] by:

$$n_2 = n_{sat} \left(\frac{t}{t + \tau_c} \right)$$
 (5.7)

where

$$\tau_{\rm c} = \frac{1}{\pi e \mu n_+} = 2.210 {\rm x} 10^6 / {\rm n_+ sec}$$
 (5.8)

and

$$n_{sat} = 3R^2 E_{ch} / e = 6.25 \times 10^9 E_{ch} R^2$$
 (5.9)

where n denotes the "saturation" charge, a finite value attained after an infinite time, with the time-scale given by τ_c . Equation (5.8) for τ_c is obtained assuming $\mu = 1 \text{ cm}^2/\text{volt-sec} = 300 \text{ cm}^2/\text{sv-sec}$. For practical purposes, $n = n_{sat}$ may be considered the value of n_2 after a few time periods τ_c . Note that n does not depend on n_{+} , while τ essentially depends only on n_{+} and is independent of R and E_{ch}. For ion density $n_{+} = 1.5 \times 10^{8} / \text{cm}^{3}$, τ_{c} is only 0.015 sec so that on a time scale of the order of seconds all large particles have $n_2 \cong n_{sat}$. (The factor 3 is Eq. (5.9) is for conducting particles; for nonconducting particles this factor is between unity and 3, depending on the dielectric constant.) For $R = 0.1 \mu m$ and $E_{ch} = 5.2 \text{ sv/cm}$, $n_2 = 3.25$ by conduction compared with $n_1 = 12.52$ obtained with one second of diffusion charging. For $R = 1.0 \mu m$ and the same E_{ch}, $n_2 = 325$ by conduction charging compared with $n_1 = 165$ by diffusion charging. At R=0.468 μ m we have $n_1 = n_2 = 71.1$. Hence, the transition between diffusion and conduction as the dominant charging mechanism occurs in the range $R = 0.1 \mu m$ to $R = 1.0 \mu m$. Thus, both mechanisms are important in contributing to the charge in this critical range. However, since we are interested in all values of R below 1.0µm (all submicron particles), we will be on conservative ground if we assume that diffusion alone is responsible for the charging of all submicron particles.

The charging theories used for the estimates of this report are the standard simplified theories. There exist more complicated theories which combine the diffusion and conduction mechanisms (Ref. 5.3), but their use would not change the numbers significantly and seems unjustified for our present purposes.

The large particles are assumed to act as collectors and to be described by a log-normal distribution. Among the quantities needed in the theory of the agglomeration process to be considered next are the average values of **n** and of Bn, where B is the particle mobility assumed to be given by the Stokes viscous drag law:

$$B = \frac{C(R)}{6\pi\eta R} \left(\frac{sec}{g}\right)$$
(5.10)

where η is the dynamic viscosity of air (which we take to be 1.8×10^{-4} poise or g/cm/sec at room temperature), and C(R) is the Cunningham "slip" factor which accounts for the fact that the particle is not large compared with the collisional mean free paths of the air molecules. The latter factor has been given as (Refs. 5.4, 5.5):

$$C(R) = 1 + [1.257 + 0.4 \exp(-1.1R')]/R'$$
with R' = R/6.62x10⁻⁶ = R(µm)/0.0662 (5.11)

Table 5.1 shows how C(R) varies with R. Above $R = 1.0\mu m$, C(R) is essentially unity. Below $R = 0.1\mu m$, C(R) rises approximately as R^{-1} . Table 5.1 also shows the product of B and n $(B_1n_1$ for "small" particles), where n is obtained from the diffusion-charging formula [Eq. (5.5)] with $n_+ = 1.5 \times 10^8 / cm^3$ and t = 1 sec. It is important to note that the product Bn is almost constant in the range $R = 0.1\mu m$ to $R = 1.0\mu m$. Thus, since the agglomeration theory to be described next involves n_1 through the product $B_1 n_1$ for small particles, the results will be insensitive to R_1 in the range $0.1\mu m$ to $1.0\mu m$.

5.2 Agglomerator Section

The air flowing into the agglomerator section is loaded inhomogeneously with charged particles, such that there are essentially only positive charges on one side, and negative charges on the other side. There is a superimposed electric field of intensity E in this section whose purpose is to pull the oppositely-charged clouds of particles toward each other and to mix them, so that oppositely-charged partners can come together and agglomerate. The task of this section is to determine the time-scales under which the two processes occur: transit across the gap, and agglomeration.

TABLE 5.1

Variations of C(R) and B_1n_1 with R* (Assumes $n_1 = 1.5 \times 10^8 / \text{cm}^3$, t = 1 sec diffusion charging)

R (µm)	C(R)	B n	B	1	nsat
0.0	• ∞	7.620x10 ¹⁰	œ	0	Ο,
0.001	110.26	1.512×10 ¹⁰	3.250x10 ¹¹	0.0465	0.000325
0.01	14.93	3.757x10 ⁹	4.400x10 ⁹	0.854	0.0325
0.1	1.882	6.949x10 ⁸	5.547×10^{7}	12.52	3.25
0.2	1.421	5.749x10 ⁸	2.094×10^{7}	27.45	13.0
0.3	1.278	5.436x10 ⁸	1.256x10 ⁷	43.29	29.25
0.4	1.208	5.316x10 ⁸	8.901x10 ⁶	59.72	52.0
0.5	1.166	5.266x10 ⁸	6.873x10 ⁶	76.58	81.25
0.6	1.139	5.247×10 ⁸	5.595x10 ⁶	93.80	117.0
0.65	1.128	5.244x10 ⁸	5.115 x 10 ⁶	102.5	137.3
0.7	1.119	5.244x10 ⁸	4.711x10 ⁶	111.3	159.3
0.8	1.104	5.250x10 ⁸	4.067x10 ⁶	129.1	208.0
0.9	1.093	5.261x10 ⁸	3.579x10 ⁶	147.0	263.3
1.0	1.083	5.275x10 ⁸	3.192x10 ⁶	165.2	325.0
2.0	1.042	5.441×10 ⁸	1.536x10 ⁶	354.5	1300.

*R = particle radius

C(R) = Cunningham slip factor

 $B_1 = particle mobility$

n₁ = particle charge (number of elementary charges) by diffusion
n_{sat} = saturation charge by conduction at E = 5.2 sv/cm

5.2.1 Agglomeration

We wish to consider two clouds of oppositely-charged particles, moving past each other with constant velocity, andto determine the probability of a contact occurring. In particular, we consider a large particle acting as a collector, with a reference frame fixed on this collector. The other particles stream past it at velocity v_0 , so that we can determine the collection efficiency by analyzing the orbits of the streaming particles and counting those which intersect the collector. To do this analytically, we assume that the collected particles are inertia-less, that is, their inertial acceleration is negligible compared with, say, that due to viscous drag (demonstrated by calculations in Ref. 5.5; see also Ref. 5.2, p. 36). An appropriate analysis for this problem approximates the orbit by that resulting from a constant velocity v_0 superimposed onthe velocity due to a central force. If these velocities are sufficiently large, it can be shown that Brownian diffusion can be neglected (Ref. 5.5). (That is, including Brownian diffusion will lead to the same result in the limit of large charges see Sec. 5.1.2.)

In Fig. 5.1, we depict the collection of small particles of radius R_1 by a large particle of radius R_2 , under an attractive central force of magnitude K_p/r^p between the particles, with p denoting the exponent for a power-law force, and K_p the associated constant; v_0 denotes the relative velocity = $(B_1n_1 + B_2n_2)eE$. There are 3 types of orbits portrayed, Type A representing uncollected particles, Type B representing collected particles, and Type C representing the critical orbit dividing the two classes of orbits. If we can determine \mathbf{x}_0 , the initial offset distance of the critical orbit, then the collection efficiency is given by $\boldsymbol{\xi} = x_0^2/(R_1 + R_2)^2$. To compute \mathbf{x}_0 we write the equations for the orbits in the form

$$\vec{\mathbf{v}} = \vec{\mathbf{v}}_{\mathbf{o}} - (\mathbf{K}_{\mathbf{p}}/\mathbf{r}^{\mathbf{p}})\hat{\mathbf{r}}$$
(5.12)

$$\frac{d\mathbf{r}}{dt} = \mathbf{v}_{\mathbf{r}} = -\mathbf{v}_{\mathbf{o}}\cos\theta - \mathbf{K}_{\mathbf{p}}/\mathbf{r}^{\mathbf{p}}$$
(5.13)

$$r\frac{d\theta}{dt} = v_{\theta} = v_0 \sin\theta \qquad (5.14)$$

From these equations the shape of the orbit is given by

$$\frac{1}{r}\frac{dr}{d\theta} = -\cot\theta - \frac{K_p}{v_r r^p \sin\theta}$$
(5.15)

from which we obtain the solution

$$\mathbf{x}^{\mathbf{p}} = \mathbf{x}_{o}^{\mathbf{p}} - \frac{\mathbf{p}K_{\mathbf{p}}}{\mathbf{v}_{o}} \int_{0}^{\theta} \sin^{\mathbf{p}-1}\theta d\theta$$
 (5.16)

where $x \equiv r \sin \theta$

The critical orbit is that for which x vanishes when $\theta = \pi$, that is, the righthand side vanishes. Thus, we have the critical value of x:

$$\mathbf{x}_{o} = \left[\frac{\mathbf{p}K_{p}}{\mathbf{v}_{o}}\int_{0}^{\pi}\sin^{p-1}\theta d\theta\right]^{1/p}$$
(5.17)

and the collection efficiency may be written:

$$\boldsymbol{\mathcal{E}}_{p} = \frac{\mathbf{x}_{o}^{2}}{(R_{1}+R_{2})^{2}} = \frac{1}{(R_{1}+R_{2})^{2}} \left[\frac{\mathbf{p}K_{p}}{\mathbf{v}_{o}} \int_{0}^{\pi} \sin^{p-1}\theta d\theta \right]^{2/p}$$
(5.18)

For a Coulomb force of attraction between the two particles (the case of interest here), p and K_p are given by p=2 and K_p=B₁ n₁n₂ e², where n₁ and n₂ are the numbers of elementary charges on the particles. The collection efficiency is

$$\boldsymbol{\mathcal{E}}_{2} = \frac{4B_{1}n_{1}n_{2}e^{2}}{v_{0}(R_{1}+R_{2})^{2}}$$
(5.19)

If \mathcal{N}_1 and \mathcal{N}_2 denote the density of small particles and large particles, respectively, the rate of disappearance of small particles per unit volume, $d\mathcal{N}_1/dt$, is given by multiplying \mathcal{E}_2 by \mathcal{N}_2 and by the current of small particles $\pi (R_1 + R_2)^2 v_0 \mathcal{N}_1$:

$$\frac{d\mathcal{N}_1}{dt} = -4\pi \mathcal{N}_1 \mathcal{N}_2 B_1 n_1 n_2 e^2 = -\frac{\mathcal{N}_1}{\tau_A}$$
(5.20)

Thus, τ_A represents the agglomeration time

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$$\tau_{\rm A} = (4\pi \eta_2 B_1 n_1 n_2 e^2)^{-1}$$
 (5.21)

which is seen to be independent of E (through v_o). Assuming \mathcal{N}_2 constant, this implies an exponential decay of the small-particle population, with time-constant τ_A , due to agglomeration onto the large particles.

If the small particles have no charge, they are still attracted to the charged large particles by the polarization force which is inversely proportional to the fifth power of the inter-particle distance. (Ref. 5.5). In this case we set p=5 in Eq. (5.18), and $K_5 = 2R_1^{3}B_1n_2^{2}e^2$. Evaluating the integral and deriving an equation of form similar to Eq. (5.20), we find that the agglomeration time for the neutral-small-charged-large-particle case is given by

$$\tau_{\rm A}' = \mathcal{N}_2^{-1} \left[\frac{15}{4} \pi^{7/2} v_0^{3/2} B_1 R_1^3 n_2^2 e^2 \right]^{-2/5}$$
(5.22)

which is (of course) independent of n_1 , and which depends on E through $v_0 = (B_1n_1 + B_2n_2)eE$. This 2/5 -power-law result corresponds to the asymptotic limit of results obtained previously by Parker (Ref. 5.5) using boundary-layer analysis to take into account fluid-flow effects in the collection of uncharged aerosols by charged droplets.

5.2.2 Thermal Agglomeration

The formula for agglomeration time τ_A , Eq. (5.21), was derived by assuming inertia-less particles and neglecting diffusion. Zebel (Ref. 5.6) treats the agglomeration of charged aerosol particles undergoing Brownian diffusion. For two types of particles, of radius, mobility, and charge R_1 , B_1 , and n_1e , and R_2 , B_2 , and n_2e , the ratio of thermal agglomeration rates (or "coagulation constants") for charged and uncharged particles is a factor

$$f = \frac{y}{(1 + G_0 y) \exp(y) - 1}$$
(5.23)

where

$$y = \frac{n_1 n_2 e^2}{(R_1 + R_2)kT}$$
(5.24)

and G₀ is a gas-kinetic correction factor which vanishes for large particles and which introduces finite mean-free-path effects for small particles. The variable y describes the electrical force between the charged particles; it vanishes for neutral particles and is large for large forces, positive for repulsion and negative for attraction. For strongly-charged aerosols (|y| large), the increase due to attraction exceeds the decrease due to repulsion and results in a net significant increase in agglomeration. For large negative y, f becomes equal to |y]. Thus, since the neutral agglomeration rate per unit volume is

$$K_{0} = 4\pi (B_{1} + B_{2})(R_{1} + R_{2})kT \mathcal{N}_{1} \mathcal{N}_{2}$$
(5.25)

the net agglomeration rate is

$$K_{0}f = 4\pi(B_{1} + B_{2})n_{1}n_{2}e^{2} \mathcal{N}_{1}\mathcal{N}_{2}$$
 (5.26)

which corresponds to the right-hand side of Eq. (5.20) if we neglect B_2 compared with B_1 (which should be justified if B_2 and B_1 are associated with large and small particles, respectively).

5.2.3 Electrostatic Dispersion or Mutual Repulsion

Another effect which needs to be considered is that due to the charges within the two oppositely-charged clouds of unipolar particles before they are brought together in the agglomerator. Each cloud will tend to expand and disperse to the walls as the particles recede from each other under their mutual repulsions. In particular, we desire to know the time-scale under which the large particles, which are to act as collectors, will disperse. The decrease in concentration of a spatially-homogeneous cloud of large particles (but with distributed sizes) is given by

$$\frac{\partial \mathcal{N}_{2}}{\partial t} = -\operatorname{div}(\mathcal{N}_{2}\vec{v}) = -\mathcal{N}_{2}B_{2}n_{2}\operatorname{e}\operatorname{div}\vec{E}$$

$$= -\mathcal{N}_{2}B_{2}n_{2}\operatorname{e}\cdot 4\pi\operatorname{e}\sum_{j}\mathcal{N}_{j}n_{j}$$

$$= -\mathcal{N}_{2}B_{2}n_{2}\cdot 4\pi\operatorname{e}^{2}\mathcal{N}_{0}\overline{n}$$

$$= -\mathcal{N}_{2}/\tau_{R}$$
(5.27)

where \mathcal{N}_{o} is the total number of particles per unit volume and \overline{n} is the average number of charges on a particle. Thus, the average repulsion time of a cloud of distributed sizes and charges may be taken to be:

$$\tau_{\rm R} = (4\pi \eta_0 \overline{B_2 n_2} \cdot \overline{n} e^2)^{-1}$$
 (5.28)

where $\overline{B_2n_2}$ is the average value of B_2n_2 in the cloud.

Thus, the particle clouds must be brought together within a time less than $\tau_{\rm R}$ in order to get them mixed so they can agglomerate. Once mixed, they will require a time of order $\tau_{\rm A}$ to agglomerate significantly. Formulas for $\tau_{\rm A}$ and $\tau_{\rm R}$ useful for system design purposes will be presented in the next section, where particle size distributions are taken into account.

5.3 Particle Size Distributions and Design Criteria

Although theoretical analyses are simpler when the particle size distributions are monodisperse, in actual cases it is necessary to deal with polydisperse aerosol systems. Such systems are usually described by log-normal distributions. The properties of log-normal distributions are well known (e.g., Ref. 5.1, Chap. 5). In this section we will replace functions of particle diameter D by mean values of these functions based on the log-normal distribution. Typically, particle distributions are defined by the mass median diameter (here denoted by $D_{m/2}$) and the geometric standard deviation (here denoted by σ_g). All other special quantities of interest may be derived from these. Among the special quantities are the following:

 $\begin{array}{l} D_{g} = \mathrm{count\ median\ or\ geometric\ mean\ diameter\ =\ D_{m/2}\ \exp\left(-3\ \ln^{2}\sigma_{g}\right)}\\ \overline{D} = \mathrm{count\ mean\ diameter\ (or\ simply\ ''mean\ diameter'')=\ D_{g}\ \exp\left(0.5\ \ln^{2}\sigma_{g}\right)}\\ \overline{D^{2}} = \mathrm{count\ mean\ squar\ e\ diameter\ (average\ area)=\ D_{g}^{2}\ \exp\left(2\ \ln^{2}\sigma_{g}\right)}\\ \overline{D^{3}} = \mathrm{count\ mean\ cube\ diameter\ (average\ volume)=\ D_{g}^{3}\exp\left(4.5\ \ln^{2}\sigma_{g}\right)} \end{array}$

F₁ = relative number (or fraction) of particles with diameter D less than D₁ (fraction of "small" particles)

= 0.5 erfc [(ln
$$D_{\sigma}$$
 - ln D_{1})/ $\sqrt{2}$ ln σ_{σ}]

 F_2 = relative number (or fraction of particles with diameter D greater than D_1 (fraction of "large" particles)

0.5 erfc
$$[(\ln D_1 - \ln D_{\sigma})/\sqrt{2} \ln \sigma_{\sigma}]$$

5.3.1 Agglomeration Time

The agglomeration time τ_A is given by Eqs. (5.20) and (5.21). We will replace \mathcal{N}_2 by $F_2 \mathcal{N}_0$, where \mathcal{N}_0 is the total number of particles per cm³, and \mathcal{N}_0 by

$$\mathcal{N}_{o} = \frac{\mathcal{M}}{\frac{4\pi}{3} \rho \overline{R}^{3}} = \frac{6}{\pi} \frac{\mathcal{M}}{\rho \overline{D}^{3}}$$
(5.29)

where \mathcal{M} denotes the mass loading in grams of aerosol per cm³ of air, ρ is the solid density of the aerosol (here taken to be 2 gm/cm³), and $\overline{D^3}$ is the mean cube of the particle diameter. We also replace n_2 by the mean value of n_{sat} , which is (Eq. (5.9)):

$$\overline{n}_{sat} = 3\overline{R^2}E_{ch}/e = 3\overline{D^2}E_{ch}/4e$$
 (5.30)

where $\overline{D^2}$ is the mean square of the particle diameter. Then τ_A may be written:

$$\tau_{\mathbf{A}} \mathcal{M} = \left(\frac{\rho}{18 \mathrm{e}\,\mathrm{E}_{\mathrm{ch}}\,\mathrm{B}_{1}\,\mathrm{n}_{1}}\right) \left(\frac{\overline{\mathrm{D}}^{3}}{\mathrm{F}_{2}\,\overline{\mathrm{D}}^{2}}\right)$$
(5.31)

where the second parentheses depends only on the distribution. Note that $B_1 n_1$ depends only on D_1 (= 2R₁), and that τ_A is inversely proportional to the massloading parameter \mathcal{M} . We take $\rho = 2 \text{ gm/cm}^3$ and $E_{ch} = 5.2 \text{ sv/cm}$, and assume $R = 0.1 \mu m$ so that $B_1 n_1 = 6.949 \times 10^8$ (Table 5.1). Then Eq. (5.31) may be written:

$$\tau_{A} \mathcal{M} = 6.406 \times 10^{-6} \left(\frac{\overline{D^{3}}}{F_{2} \overline{D^{2}}} \right)$$

$$(5.32)$$

$$R=0.1\mu m$$

It is important to note that, while τ_A is evaluated here only for R=0.1 μ m, the dependence on R is through B₁n₁, which, as Table 5.1 shows, is nearly constant in the R-range 0.1 μ m to 1.0 μ m.

5.3.2 Repulsion Time

The mutual repulsion time τ_{R} is given by Eqs. (5.27) and (5.28). We replace η_{o} by Eq. (5.29), and \overline{n} by \overline{n}_{sat} as in Eq. (5.30). The average value of $B_{2}n_{2}$ is replaced by

$$\overline{B_2 n_2} = \left(\frac{1}{3\pi\eta D} \cdot \frac{3E_{ch}D^2}{4e}\right) = \frac{E_{ch}}{4\pi e\eta}\overline{D}$$
(5.33)

Then $\tau_{\rm R}$ may be written:

$$r_{\rm R} \mathcal{M} = \left(\frac{2\pi}{9} \frac{\rho \eta}{{\rm E_{ch}}^2}\right) \left(\frac{\overline{\rm D}^3}{\overline{\rm D}^2 \cdot \overline{\rm D}}\right) = 9.295 \times 10^{-6} \left(\frac{\overline{\rm D}^3}{\overline{\rm D}^2 \cdot \overline{\rm D}}\right)$$
(5.34)

where we have assumed P=2, $\eta=1.8 \times 10^{-4}$, and $E_{ch}=5.2$, and where the final parentheses depends only on the distribution. As in the case of τ_A , τ_R is

inversely proportional to \mathcal{M} . The dependence on inverse E_{ch}^{2} results from the assumption that for the purposes of estimating repulsion times all particles charge up as large particles, i.e., by conduction alone. This should yield a good estimate of τ_{R} since most of the charge resides on the large particles, and the error in assigning the wrong value of charge to the small particles should be small.

Note that, after the mixing has been achieved, oppositely-charged large particles will tend to agglomerate with one another. This large-particle agglomeration time is roughly given by $T_{\rm p}$.

5.3.3 Voltage to Bring Oppositely Charged Clouds Together

The voltage required to force the oppositely-charged clouds together across a gap of length d may be written as:

$$V(volts) = \frac{300 d^2}{(B_1n_1 + B_2n_2)et}$$

$$= \frac{300 \text{ d}^2}{[B_1 n_1 + \overline{D}E_{ob}/(4\pi e\eta)]\text{et}}$$
(5.35)

where we have used Eq. (5.33) for B_2n_2 , and the factor 300 is required to convert statuets to volts. The time t should be $\tau_{\rm A}$ or $\tau_{\rm R}$, whichever is shorter. We assume that d=10 cm, $E_{\rm ch} = 5.2$ sv/cm, and $\eta = 1.8 \times 10^{-4}$ poise. Then Eq. (5.35) may be written:

$$V(volts) = \frac{130500}{[2.088x10^{-9}B_1n_1 + \overline{D}(\mu m)]t(sec)}$$
(5.36)

Specializing to R=0.1 μ m particles, so that (Table 5.1) B₁n₁ = 6.949x10⁸, we obtain

$$V(volts) = \frac{130500}{[1.451 + \overline{D}(\mu m)]t(sec)}$$
(5.37)

Note that this formula also can apply to the charging section, in which we assume 15600 volts is applied across 10 cm, and the particles are exposed for one second. Provided \overline{D} is less than 6.91 μ m, 15600 volts will be insufficient to move the particles across the channel within the charging time of one second. Hence, the small-particle charging can be completed before the particles move to the walls under the applied charging field.

5.3.4 Maximum Loading \mathcal{M}_{max}

In the foregoing equations, the mass loading \mathcal{M} is a "free" parameter. It cannot be arbitrarily large, however, since the ions would eventually become depleted and the particles would compete for them. It is of interest to consider the foregoing equations in the light of the maximum loading \mathcal{M}_{max} for a given ion supply (n_{+} ions/cm³). Under conditions where all available ions are deposited on particles, and assuming that most of the charges accumulate on the large particles by conduction, we may estimate \mathcal{M}_{max} by equating $n_{+} = \mathcal{M}_2 \bar{n}_{sat} =$ $F_2 \mathcal{M}_0 \bar{n}_{sat}$, and using Eq. (5.29) for \mathcal{M}_0 and Eq. (5.30) for \bar{n}_{sat} . Thus, solving for $\mathcal{M} = \mathcal{M}_{max}$:

$$\mathcal{M}_{\max} = \frac{2\pi}{9} \rho e \frac{n_+}{E_{ch}} \left(\frac{\overline{D^3}}{F_2 \overline{D^2}} \right) = 1.933 \text{xl} \, 0^{-6} \left(\frac{\overline{D^3}}{F_2 \overline{D^2}} \right)$$
(5.38)
in μm

where we have used $n_{+} = 1.5 \times 10^{8} / \text{cm}^{3}$, $\rho = 2 \text{ gm/cm}^{3}$, and $E_{ch} = 5.2 \text{ sv/cm}$. Using this value, \mathcal{M}_{max} , in the expressions (5.32) and (5.34) for τ_{A} and τ_{R} , respectively, we obtain minimal values for τ_{A} and τ_{R} , and a maximal value for V from (5.37). The minimal values of τ_{A} and τ_{R} are:

$$(\tau_{A})_{\min} = (4\pi e^{2} n_{+} B_{1} n_{1})^{-1} = 3.31 \text{ sec}$$
 (5.39)
(for R=0.1 μ m)

$$\left(\tau_{\rm R}\right)_{\rm min} = \frac{\eta}{{\rm en}_{+}{\rm E}_{\rm ch}} \left(\frac{{\rm F}_2}{{\rm \overline{D}}}\right) = 4.808 \left(\frac{{\rm F}_2}{{\rm \overline{D}}(\mu{\rm m})}\right) \sec (5.40)$$

and $V_{\max} < 27170$ volts (for t=3.31 sec and $\overline{D} = 0$). It is of interest to note that $(\tau_A)_{\min}$ is independent of the distribution of E_{ch} .

5.3.5 Design Criteria

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In applying the above formulas to the design of an agglomerator it seems reasonable to assume maximum loading so that $\mathcal{M} = \mathcal{M}_{max}$. This minimizes the agglomeration time τ_{R} . It also minimizes the self-repulsion time τ_{R} (which is also approximately the self-agglomeration time for the large particles). The following relations are desirable, namely, that:

- (a) τ_A be smaller than τ_R ; then agglomeration can occur before self-repulsion (and before self-agglomeration of the large particles).
- (b) τ_A be of the order of a second (residence time in the agglomerator section).
- (c) V be large enough to bring the particle clouds together and mix them before they disperse by self-repulsion.
- (d) E_{ch} (the charging field) be small enough to allow small particles to charge for a second or so before they are pushed to the walls by the charging field (charging section).

In addition, assuming that F_2/\overline{D} is not too small, depending on the distribution, one may design the system based on B_1n_1 for particle radius anywhere in the approximate range $R = 0.1\mu m$ and $R = 1.0\mu m$, since B_1n_1 is roughly constant. Then, since B_1n_1 increases rapidly below $R = 0.1\mu m$ (due mostly to the Cunningham slip factor), the agglomeration times τ_A for the smaller particles become smaller (inversely proportional to B_1n_1), while the self-repulsion time τ_R remains unaffected. In other words, if the agglomeration works well for particles of radius, say, $R = 0.1\mu m$, it will work even better for smaller particles. As Zebel says (Ref. 5.6, p 35): ". . . small particles are very rapidly 'eaten up' by large ones."

5.4 Application to Typical Size Distributions

We may apply the above theory to some sample actual size distributions, in order to see how these distributions affect the operation of the system (τ_A , τ_R , and V). We have chosen the first 7 distributions from Table 2.1 of Sec. 2. (the remaining distributions are similar to one of the 7 chosen). In Table 5.2 we have labelled the distributions as #1, #2, etc., labelling the columns across the top. The horizontal entries denote the following:

= mass median diameter $D_{m/2}$ = geometric standard deviation σ_{g} Dg = geometric-mean diameter (count median) D = count-mean diameter $\overline{D^3/D^2}$ = ratio of count-mean-cube diameter to count-mean-square diameter F_2 = fraction of large particles F_2/\overline{D} = used in formula for $(\tau_R)_{min}$ $\overline{D^3/D^2/F_2}$ = used in formulas for $\tau_A \mathcal{M}$ and \mathcal{M}_{max} = maximum mass loading mmax $\tau_{A} \mathcal{M} = \mathcal{M}_{X \text{ agglomeration time}}$ $\tau_{\mathbf{p}} \mathcal{M} = \mathcal{M} \mathbf{x} \mathbf{repulsion} \mathbf{time}$ $(\tau_A)_{\min}$ = minimum agglomeration time ($\mathcal{M} = \mathcal{M}_{\max}$) $(\tau_{\rm R})_{\rm min}$ = minimum repulsion time $(\mathcal{M} = \mathcal{M}_{\rm max})$ $(\tau_{\rm R})_{\rm min}/(\tau_{\rm A})_{\rm min}$ = ratio of minimum times = V(volts) to mix particles, evaluated with t = $(\tau_A)_{min}$ VA = V(volts) to mix particles, evaluated with t = $(\tau_R)_{min}$ VR

We see that $(\tau_A)_{\min} = 3.313$ sec is a reasonable value (for the time of residence in the agglomerator section such that significant agglomeration occurs) and is the same for all distributions. The voltages V_R required to bring the particles together, that is, to mix them before they disperse are, except for Case #4, under about 23 kilovolts (a reasonable maximum voltage) for all distributions. For Cases #3, #4, #6, and #7, $(\tau_R)_{\min}$ is less than $(\tau_A)_{\min}$. This means that once the particles are mixed, there will be some agglomeration of the large particles amongst themselves. This should not be serious for Cases #3 and #6.

Distribution	<u> </u>	#2	#3	#4	#5	#6	#7
D _{m/2} (μm)	1.8	2.3	4.0	0.34	2.7	D _g = 0.9	15.9
σ _g .	2.2	3.5	1.7	5.4	2.4	~3	1.59
D _g (µm)	0.2788	0.02075	1.7187	6.701x10 ⁻⁵	0.2709	0.9	8.341
D̄(μm)	0.3804	0.04548	1.9785	2.778x10 ⁻⁴	0.3974	1.646	9.288
$\left(\frac{1}{D^3}/\frac{1}{D^2}\right)_{(\mu m)}$	1.319	1.0495	3.475	0.0820	1.8406	18.38	14.28
F ₂	0.6633	0.03525	$F_1 = \frac{2.527}{\times 10^{-5}}$	7.91x10 ⁻⁶	0.6356	0.9149	1.00 F ₁ = 4.41 x10 ⁻
$\frac{F_2}{\overline{\overline{D}}(\mu m)}$	1.7437	0.7751	0.5054	0,02847	1.5994	0.5558	0.10767
$\frac{1}{\mathbf{F}_2} \frac{\overline{\mathbf{D}^3}}{\overline{\mathbf{D}^3}} (\mu \mathbf{m})$	1.989	29.77	3.475	10367.	2.896	20.09	14.28
\mathcal{M}_{\max}	3.845x10 ⁻⁶	5.755x10 ⁻⁵	6.717 x 10 ⁻⁶	0.02004	5.598x10 ⁻⁶	3.883x10 ⁻⁵	2.760x10
$\tau_{A} \mathcal{M}$ (sec-g/cm ³)	1.274x10 ⁻⁵	1.907x10 ⁻⁴	2.226x10 ⁻⁵	0.0664	1.855x10 ⁻⁵	1.287x10 ⁻⁴	9.146x10
$ au_{\rm R} \mathcal{M}$ (sec-g/cm ³)	3.223x10 ⁻⁵	2.145x10 ⁻⁴	1.633x10 ⁻⁵	2.744x10 ⁻³	4.305x10 ⁻⁵	1.0379x10 ⁻⁴	1.429x10
$\left(\begin{array}{c} \tau_{A} \\ \mathbf{A} \end{array} \right)_{\min}$ (sec)	3.313	3.313	3.313	3.313	3.313	3.313	3.313
$\left(\tau_{\rm R} \right)_{\rm min}$ (sec)	8.384	3.727	2.430	0.1368	7.690	2.672	0.5172
$(\tau_{R})_{min}$	2.530	1.125	0.7335	0.04128	2. 321	0.8065	0.1561
V (volts)	21506	26319	11485	27139	21309	12718	3668
V _R (volts)	8498	23396	15659	657243	9180	15769	23495

Table 5.2 Effects of Distribution (Distributions from Table 2.1)

Case #4 seems to be highly singular. For example:

(1) D_{σ} is less than one Angstrom unit

(2) The fraction of large particles (F_2) is excessively small, less than 10^{-5} .

One may suspect that the size-distribution for Case #4 is poorly represented by a log-normal distribution; therefore, the small ratio (0.04) of repulsion-toagglomeration times, and the excessive voltage (657 kilovolts) to bring particles together, may be unrealistic for this case.

In summary, of the 7 cases studied, all except #4 and #7 appear to be reasonably amenable to agglomeration; these exceptional cases might also turn out to be amenable if their distributions could be more accurately characterized.

6. EVALUATION

6.1 Brief Summary

The filtration enhancement system considered here - which consists of charger and agglomerator sections (Figs. 2.1 and 2.2) - and the scientific areas requiring investigation, have been discussed in detail in Section 2. The basic objective is to agglomerate fine particles onto larger particles, hence improving prefilter efficiency. Sections 3-5 contain the initial results obtained on each of the areas of investigation, which can be summarized briefly as follows.

Results on the ionization distribution due to the charger section ⁸⁵Kr beta source are presented in Section 3. The beta source (Fig. 3.1) was fabricated, filled with 0.1 atm ⁸⁵Kr gas, and the induced ionization around the source measured in a geometry (Fig. 3.3) similar to the charger section (neglecting the collimators). Results for the specific ionization are given in Fig. 3.4. Also given in that figure are analytical results obtained neglecting all scattering effects. The reasonably good agreement suggests that for calculations where only the energy deposition is of interest (as here), rather than the electron distribution function, this is a good assumption. Based on these results a source strength of about 500 Ci ⁸⁵Kr was selected as a basis for further consideration, leading to an ion pair production rate near 10¹¹/(cm³-sec) at about 10 cm radially from the source.

The ion density distribution in the charger was investigated in Section 4, with approximate results given in Figs. 4.2 and 4.3. It is clear from these figures that regions of well-separated positive and negative ion distributions can be maintained near the oppositely charged plates (as in Fig. 2.2) with applied potentials of ≤ 20 kV. Thus, the air to be filtered is separated into two streams, one passing through a region of positive ions, the other through a region of negative ions. The charging process for the particulates, and the subsequent agglomeration of the oppositely charged particulates in the presence of the reversed electric fields (Fig. 2.2), are considered in Section 5.

The operating feasibility of induced agglomeration has been assessed on the basis of theoretically derived time-scales for charging, agglomeration, and space-charge repulsion. For logical choices of the parameters, we obtain reasonable agglomeration times (residence time in the agglomeration section such that significant agglomeration occurs, and therefore successful operation) of the order of seconds. In the agglomeration process, the small particles are consumed by the larger particles. With plate voltages on the order of 20 kV the particles can be oppositely charged in the two halves of the gas stream, and then the oppositely-charged clouds of particles can be brought together (mixed) in the agglomerator section - in a time shorter than that in which they would "explode" or disperse under their space-charge repulsion forces. Thus, dispersion is avoided, as well as the self-agglomeration of the large charged particles with one another (which takes place in the same order of time). The dispersal time, and therefore the voltage required, depends on the particle size distribution, but the agglomeration time does not. We have considered $0.1-\mu$ m-radius particles, and have argued that (a) smaller particles than these would be consumed even faster by the large particles, and that (b) particles with radii in the range $0.1\mu m$ to $1.0\mu m$ would be agglomerated onto the "supermicron" (above $1 \mu m$) particles about equally rapidly. Thus, it is expected that the size distribution would shift significantly toward the supermicron sizes, which is the desired goal.

As a consequence, we believe that the radiation induced particulate agglomeration system considered here could, in fact, lead to significant enhancement of the prefilter efficiency, and hence overall improvements in economy in operation of nuclear facility filtration systems.

6.2 Comparison of Results with Some Related Work

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Heinsohn et al. (Ref. 2.1) have carried out an investigation of possible use of 60 Co gamma radiation for production of ionization in a particulate charging system. Their objective was to remove the particles, after being charged, by electrostatic precipitation - quite a different principle from the agglomeration technique investigated here. Yet, some of their results on ionization are quite useful for comparison. Their experimental system used two 75 Ci sources of 60 Co; the ionization was produced by Compton and photoelectric electrons ejected in their experimental housing by the ~1 MeV 60 Co gamma rays. Their maximum measured specific ionization was about

4.8x10⁹[ions/(cm³-sec)]/(2x75 Ci)≈3x10⁷ ions/(cm³-sec-Ciγ's) (6.1)

Note that this is several times less than the specific activity in the 10-20 cm region of Fig. 3.4. Furthermore, the radiation hazard external to the apparatus that is associated with ⁸⁵Kr, when measured per curie, is <u>far</u> less than that due to ⁶⁰Co. The ⁸⁵Kr gamma ray (~0.5MeV) is emitted in only 0.4% of the decays, and the efficiency of conversion of the 99.6% emitted beta energy into bremsstrahlung ($\leq 670 \text{ keV}$, avg~300 keV) is less than 1%. Thus, on a radiation hazard basis ⁸⁵Kr is less than about 1% of a similar source strength ⁶⁰Co source. We concur with Heinsohn et al. (Ref. 2.1), who note in their conclusion that since it is, in fact, electrons which produce the ionization, they can more easily be provided by beta than gamma radiation. We note, for example, that the 500 Ci ⁸⁵Kr beta source found here to provide the ~10¹¹ ions/(cm³-sec) needed ionization rate, is equivalent to only 5 Ci of external (to the apparatus) electromagnetic radiation (γ 's and bremsstrahlung). It is also of interest to note that the resulting ion densities are similar to those typically found in electrostatic precipitators (Refs. 5.2 and 6.1), but that our method of production of the ionization requires much less power.

Regarding electrically-induced agglomeration studies by Melcher and Sachar (Ref. 6. 2), they did not consider radii below one micrometer, and hence did not consider fine particles. They artificially chose two groups, a 1.0 - µmradius group to represent all the "small" particles, and a 10.0-µm-radius group to represent all the "large" particles in a distribution; whereas we consider a series of entire log-normal distributions, all based on actual nuclear facility particle distributions. (Our small-particle fraction as a function of particle radius is assumed to be given by the integral over the log-normal distribution, from zero radius to the radius of interest. This is based on the analytical fall-off behavior of the log-normal distribution at small radii, and may be considered a natural way of characterizing the small-particle fraction.) In Ref. 6.2 it was assumed that the "small" and 'large" oppositely-charged particles were somehow instantaneously charged and mixed. This seems somewhat artificial as opposed to our method of charging and of bringing the particles together, under controlled conditions. Also, in Ref. 6.2 a special ratio of dust loading distributed between the "small" and "large" particles is postulated in order to achieve efficient operation; it is difficult to see how this ratio can be controlled in practice. In our method, the total dust loading is the (more practical) parameter affecting the rate of agglomeration. The values of dust loading assumed in Table 5.2 leading to successful operation are typically found in industrial electrostatic precipitators (Ref. 6.1).

7. RECOMMENDATIONS

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Based on the above evaluation, we believe that experimental and supporting analytical work should be carried out to make preliminary tests of the charger section, as the first part of Phase II. In particular, the following tasks can be defined:

- 1) Design experimental model charger section and fabricate.
- 2) Measure ion density distribution in charger section (Langmuir probe or similar instrument).
- 3) Modify theory based on Phase I results and apply to obtain better estimates of particulate charging and agglomeration.
- 4) Measure actual state of charging on simple (0.3μm monodisperse) particulates (mobility analyzer or similar instrument).
- 5) Analyze results, write report and suggest agglomeration studies if charging results justify it.

It is expected that item 4) would be carried out by use of laboratory facilities at the Harvard School of Public Health, under the overall supervision of Dr. Melvin W. First. It is intended that the minimum source intensity will be used that is sufficient to demonstrate the charging principles. Maximum use will be made, in the experiments, of lower than actual flow rates, since the flow rate is a parameter that occurs in the theory. Once the system concept has been verified for low source strengths and flow rates, results can be predicted with confidence for realistic system parameters.

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