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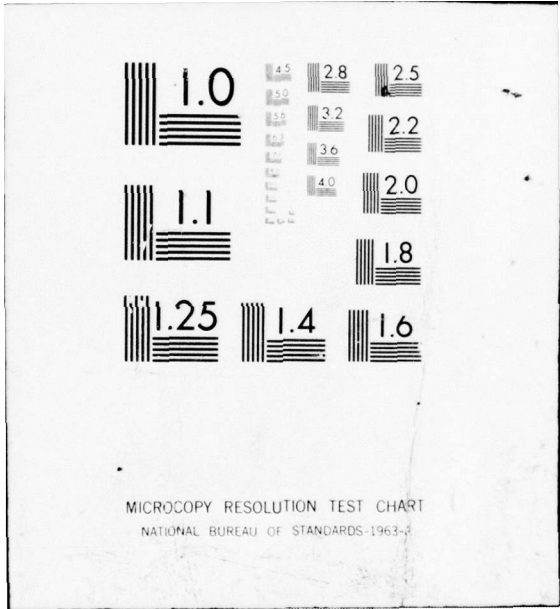
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# Users Guide for ESD LORAN Grid Prediction Program

SAMUEL HOROWITZ

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## Preface

This work was performed at the request of the LORAN Systems Project Office, Electronic Systems Division, Hanscom AFB, MA 01731.

The type of program described in this paper involved numerous people for its success, in particular: Dr. Terence J. Elkins, RADC/EEP, Capt. Randolph Gressing, ESD/DCL, and Mr. William McComish, Boston College. Deeply appreciated are their vigorous and indispensable technical support.

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## Users Guide for ESD LORAN Grid Prediction Program

### I. INTRODUCTION

The ability to precisely deliver ordnance or men and material under all weather conditions in an adverse battlefield environment, is one of the most severe requirements imposed on U. S. Worldwide Tactical Air Forces. A key element in meeting this requirement involves obtaining and providing position data in a specified coordinate system, to allow navigation of tactical aircraft to desired locations with sufficient accuracy for rendezvous or weapon release. The LORAN radio navigation system is being relied upon more and more as a principle source of navigation information in tactical airborne operations. Position indication is given in terms of LORAN TD's (time difference) which, because of propagation anomalies, do not correspond precisely to earth fixed geodetic coordinates. Therefore, each LORAN chain requires a grid prediction for its coverage area. Such a grid prediction computer program package has been developed at RADC/EEP and is described herewith. This manual contains sufficient information to enable the experienced programmer to understand the programming aspects of LORAN grid prediction and includes a detailed functional description and its operation.

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(Received for publication 8 December 1977)

## 2. SYSTEM CONFIGURATION

The operation of the entire LORAN Grid Prediction System from obtaining the required input data off maps to the calculation of the output time difference is illustrated in Figure 1. The system has been divided into the four following parts:

- PART I: Formation of map digitized.
- PART II: Calculation of surface impedance data base.
- PART III: Field LORAN prediction package.
- PART IV: Updating data base by comparison of calculated and experimental results.

A sufficient description of the various computer program is presented so that the user can obtain the required LORAN coordinates. The data base is generated in PARTS I and II and updated when measured data is available in PART IV. In PART III of the systems, the main set of calculations are performed and this is described first in Section 3. The technique for translating the earth's electrical properties into a surface impedance and properly sequenced onto a rapid access magnetic disc is described in Section 4. Brief description of map data digitization and system tuning or data base updating is given in Sections 5 and 6, respectively.

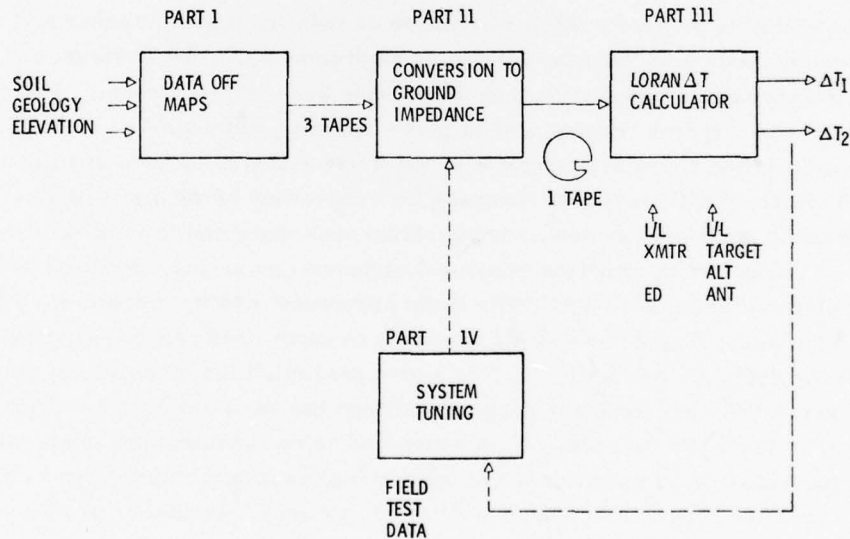


Figure 1. Total LORAN Grid Prediction System

### 3. DESCRIPTION OF PART III

#### 3.1 Overview

A block diagram of the PART III LORAN prediction package is shown in Figure 2. Its purpose is to furnish the LORAN TD's for a desired target given the ground properties of the system coverage area. For each LORAN chain, the geodesic location of the master and two slave transmitters must be known in addition to the two slave emission delays. A magnetic tape of the ground electrical properties for the given coverage area is also required. The latitude and longitude of the desired target and delivery altitude are inserted into the program and a time of arrival (TOA) from each of the transmitters is computed. Subtracting the master TOA from each of the slave TOA's yields two TD's which determine the LORAN coordinates of the target.

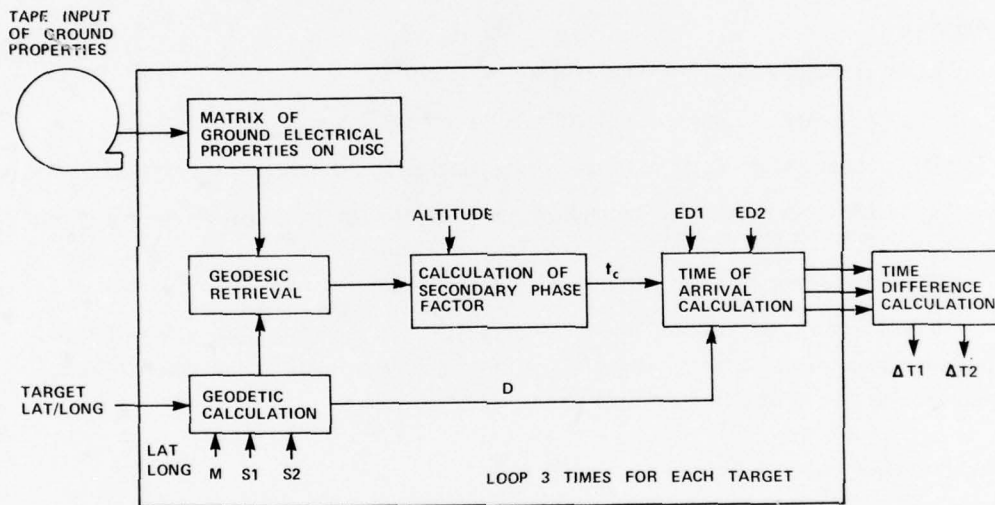


Figure 2. LORAN Prediction Package - Part III

The operation of this program can be followed by referring to Figure 2. The input tape contains the ground electrical properties which consist of elevation and complex surface impedance for the area of interest. This is in the form of a matrix of data points every 30 arc sec in latitude and longitude. The information is recorded onto a disc for rapid access of data between any two points in the service area as required by the geodesic retrieval.

The input data cards contain the following: (a) transmitter coordinates with associated emission delays, and (b) target coordinates, delivery altitude, integration step size, and type of receiving antenna for each target. This data is first used in the geodetic calculation to determine path length (D) between each of the transmitters and the target, and to determine points along the geodesic path governed by the distance increment or integration step size. The points along the geodetic path are input to the geodesic retrieval, which in turn obtains the ground electrical properties of the points from the matrix on the disc. This information is used to calculate the time correction or secondary phase factor due to the decrease in propagation velocity, compared to free space, when a signal propagates over the earth's surface. Time of arrival calculations can then be made from the following equation:

$$\text{TOA} = \frac{n}{c} D + t_c + \text{ED} \quad (1)$$

where

- n = atmospheric index of refraction = 1.000338.
- c = velocity of light =  $2.997925 \times 10^8$  meters/second.
- D = length of geodetic path from transmitter to receiver in meters.
- $t_c$  = time correction or secondary phase factor for propagation over a given path length in  $\mu\text{sec}$ .
- ED = emission delay in  $\mu\text{sec}$ .

Three such calculations, one from each transmitter to target, are required for each prediction. Subtracting the master TOA from each of the slave TOA's, one obtains the LORAN coordinate prediction.

### 3.2 Prediction Program Flow Chart

A flow chart illustrating the operation of the LORAN Grid Prediction package is illustrated in Figure 3 and subroutine relationships to the driving program LORANCO is shown in Figure 4. This package consists of a deck with approximately 1300 cards and requires a core memory of 120K base eight (8). The three transmitter (M, S1, S2) coordinates with corresponding emission delays are read into the program from the input data deck. For computation purposes, the geographic coordinates are converted into radians by a call to subroutine CORRAD. The target coordinates are then read into the program with corresponding information on delivery altitude in meters, computation step size in kilometers, and type of receiving antenna (Electric dipole = 1, Loop = 0). Similarly, these coordinates are converted to radians. The program is terminated when the step size (ADELS)

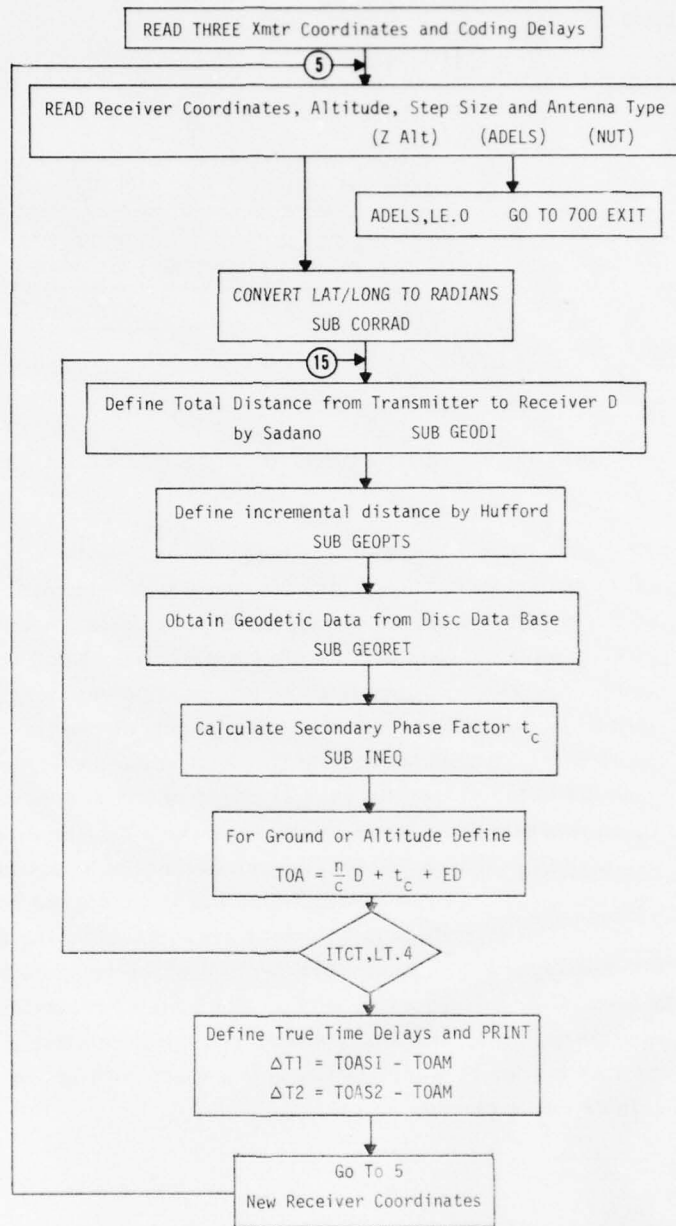


Figure 3. LORAN Program Flow Chart

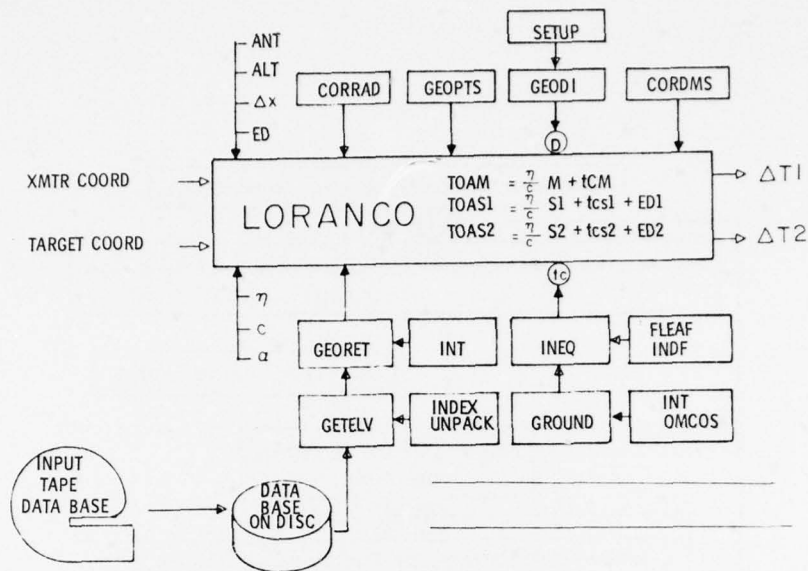


Figure 4. ESD LORAN Grid Prediction Program

is equal to or less than zero. Therefore, a blank card after the last desired target card causes the program to exit. With information on transmitter and target location, the program can now determine the propagation path. The total geodesic distance for primary wave delay is calculated in subroutine GEODI which uses the Sodano formulation.<sup>1, 2</sup> The coordinates of incremental points along the propagation path are defined in subroutine GEOPTS. The ground electrical properties for these points are obtained through subroutine GEORET which in turn calls subroutine GETFLV. In the latter subroutine, the required points are indexed to address data for the random access disc. Upon return from the disc, the data is unpacked and returned to GEORET. With a detailed description of the points along the propagation paths available, one can now calculate the secondary phase factor or time correction,  $t_c$ , due to the disturbing influence of the earth using the Hufford Integral formulation equation.<sup>3, 4, 5</sup> Ninety-five percent of the compute time is required for this calculation in subroutine INEQ. The time of arrival is the sum of the primary wave travel time, secondary phase factor, and emission delay. All the required information for this calculation over a given path is now available and the resultant calculation is stored.

Due to the large number of references on this page, the references will not be footnoted. See references, page 83.

The above procedure is repeated three times, once from each transmitter to receiver by looping back to statement 15 after each completed TOA. With the completion of the TOA calculations, the predicted time difference for a given geographical coordinate is calculated (T, T2) in the driving program LORANCO and output printed. Control is then transferred back to statement 5 where new target coordinates are read into the system, and the entire process is repeated until ADELS is made equal to or less than zero.

Figure 4 is an additional flow chart illustrating the subroutine relationships to the driving program LORANCO.

### 3.3 Data Input and Output Setup

#### 3.3.1 INPUT

Program LORANCO requires a data deck and data tape for operation loaded as shown in Figure 5. The data deck supplies the geographic location of transmitters and targets and additional required constants such as emission delay, altitude, step size, and type of receiver antenna. The data tape supplies the ground electrical properties for the entire service area covered by the transmitters.

The first three cards in the data deck describe the transmitter input data as follows:

<u>Cols</u>	<u>Data</u>	<u>Format</u>
1-2	Blank	
3-6	Alphabetic numeric identifier for transmitter	3A8
26-42	Latitude data	I5, I3, F7.3, A1
26-30	Latitude, degrees	I5
31-33	Latitude, minutes	I3
34-41	Latitude, seconds	F7.3
42	Latitude, N or S	A1
43-58	Longitude, data	I5, I3, F7.3, A1
43-47	Longitude, degree	I5
48-50	Longitude, minutes	I3
51-57	Longitude, second	F7.3
58	Longitude, E or W	A1
59-78	Emission Delay	F20.3

All degrees, minutes, and seconds are right justified in their respective field. Emission delay is in units of  $\mu$ sec. The order of transmitter cards are master, slave 1, and slave 2. The master emission delay will always be zero. Slave 1 emission delay is always less than that of slave 2.



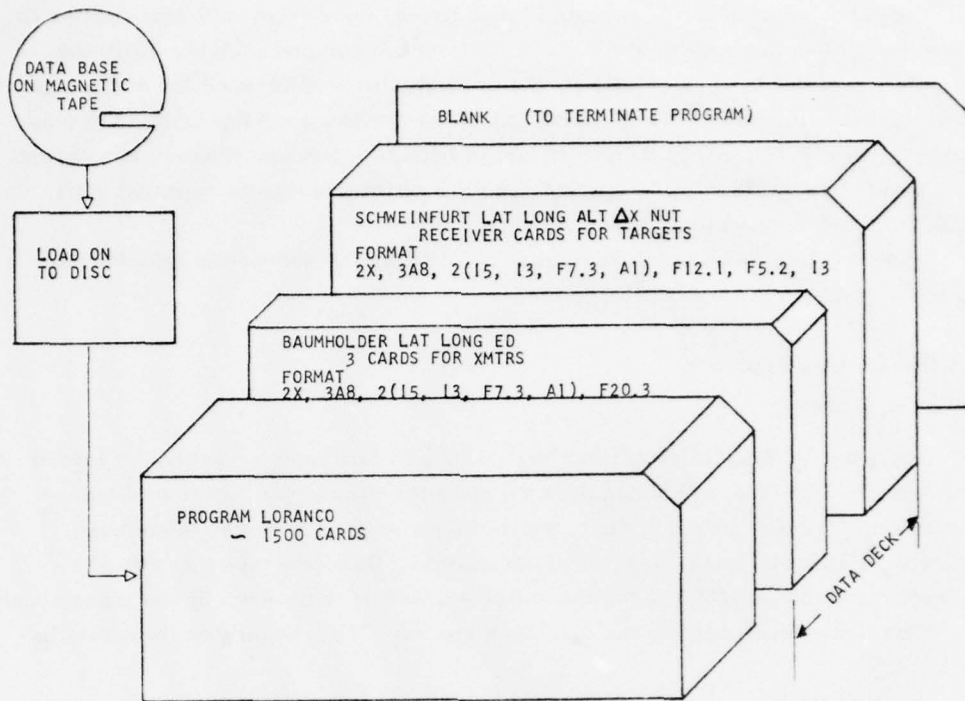


Figure 5. Deck Setup for Program LORANCO

The next set of cards contain the target input data. It is read in as one target per card so there will be as many receiver cards as targets with the following format:

<u>Cols</u>	<u>Data</u>	<u>Format</u>
1-2	Blank	
3-26	Alphabetic numeric identification for receiver identification	3A8
26-42	Latitude data	I5, I3, F7.3, A1
26-30	Latitude, degrees	I5
31-33	Latitude, minutes	I3
34-41	Latitude, seconds	F7.3
42	Latitude, N or S	A1
43-58	Longitude data	I5, I3, F7.3, A1
43-47	Longitude, degrees	I5
48-50	Longitude, minutes	I3

<u>Cols</u>	<u>Data</u>	<u>Format</u>
51-57	Longitude, seconds	F7.3
58	Longitude, E or W	A1
59-70	Altitude, meters	F12.1
71-75	Step Size, kM	F5.2
76-78	Type of Antenna 0 or 1	I3

The aircraft altitude at the release point is specified in meters and the distance increment or step size in kilometers typically 0.5 kilometers. NUT defines the type of receiver antenna. For a vertical antenna, a 1 is placed in column 78, for a loop, a 0 in column 78. A blank card or zero in columns 71-75 will terminate the program.

The data tape contains information on the electrical properties of the ground and covers the entire service area. Points selected outside this area will cause the program to print "OUT OF ACCEPTABLE RANGE, FURTHER CALCULATIONS FOR THIS PATH HAVE BEEN DELETED." The supplied magnetic tape contains 5760 records of 60 words each with each word representing 120 data points or one degree of latitude. Each data point is defined by a complex surface impedance and an elevation. The current area covered is 66 to 14 degrees in longitude and 48 to 54 degrees in latitude. This tape is read into the random access data base disc unchanged in format with the sequential record number on the tape becoming the random access index array address number. No operation on the tape is required.

### 3.3.2 OUTPUT

Program LORANCO produces the following printed output:

- (a) For each transmitter, an echo printout of columns 3-58, of the input card.
- (b) For each receiver, an echo printout of columns 3-58 of the input card.
- (c) For each transmitter to receiver path, geodesic path information, and a printout of the parameters used by subroutine INEQ.
- (d) Results of the ground wave time delay calculations in the form of the list NAMI. The list NAMI contains information on time of arrivals (TOA), time delays (TD1, TD2), emission delays (ED1, ED2), geodesic distances (DISTSOD), primary wave times (TPW), and secondary phase factor times (TIMDUM).

### 3.4 Program Subroutines and Functions

- LORANCO - Reads inputs, defines three paths, calls data base and INEQ, calculates TOA and TD.
- CORRAD - Degrees (Lat, Long) to radians.
- CORDMS - Radians to degrees (Lat, Long).
- GEOPTS - Defines points along geodetic from transmitter to receiver.

INT - Calculate first and second derivative of elevation.  
 GETELV - Read geophysical data off disc.  
 UNPACK - Unpack data from disc.  
 GEORET - Returns geophysical data to driving program.  
 INEQ - Solution of integral equation for secondary phase factor.  
 INDF - Induction field calculation (E or H field).  
 CNEUKEN - Interpolation routine for integration.  
 GEODI - Calculation of total geodetic distance by Sodano and back azimuth.  
 SETUP - Constants for spheroid to be used.  
 GROUND - Introduces variable ground impedance and variable ground terrain into integral equation formulation of the ground wave.  
 CANG - Calculates argument of a complex number.  
 INDEX - Calculates index values of data base variables from LAT/LONG.  
 WERF - Calculates error function.  
 OMCOS - Calculates  $1 - \cos(X)$ .  
 FLEAF - Calculates ground wave attenuation function over flat ground using flat earth theory.

### 3.5 Subroutine Description

#### 3.5.1 LORANCO

This is the driving module for the entire program. It reads the input coordinates of both transmitters and receivers, defines the geodesic path, receives data base parameters and calculates the secondary phase factors, time of arrivals, and time difference. The first three read cards, one for each station, furnish the transmitter locations and associated emission delays. A call to CORRAD changes the units of the input data from degrees to radians. The first target or receiver geographic coordinates are then read in degrees, and changed to radians by a call to CORRAD. The various paths from transmitter to target and then defined (RLA(ITCT), RLO(ITCT)), and a call to subroutine GEOPTS defines the incremental path coordinates. The call to subroutine GEODI returns the total distance from transmitter to target (SBKMS) by a Sodano calculation.<sup>2</sup> This value is later used to calculate the primary wave delay. With the incremental geographic coordinates known along the geodesic, the call to subroutine GEORET returns the ground electrical properties of elevation and impedance through common blocks/GROUND/and/SDRDI/for use in subroutine INEQ. Subroutine INEQ determines the secondary phase factor, TIMSAV. The time of arrival (TOA) for a given path (ITCT) is determined from the relationship:

$$\text{TOA (ITCT)} = \text{ENC} * \text{SBKMS} + \text{TIMSAV} \quad (2)$$

where ENC = ground refractive index divided by the velocity of light. ITCT is then incremented for a new path between the next transmitter in the chain and the same receiver, and program control returns to statement 15 where RLA(ITCT) and RLO(ITCT) are redefined. The above process is then repeated until three TOA'S are calculated. The required time difference (TDI) then computed from the relation:

$$\text{TDI} = \text{EDI} + \text{TOA}(2) - \text{TOA}(1) \quad (3)$$

where

EDI = emission delay for slave 1.

TOA(2) = Time of arrival for slave 1 at receiver, TOAS1.

TOA(1) = Time of arrival for Master at receiver, TOAM.

When the calculations are performed for airborne locations, the secondary phase factor contains an altitude correction derived in subroutine INEQ and defined as ALTTMSV.

Upon completion of the time difference calculation, control is transferred back to statement 5 in the program where the information for the next target is read in and the entire process repeated. The program exits when the step size (ADELS) on the target card is equal to or less than zero.

### 3.5.2 SUBROUTINE CORRAD

Subroutine CORRAD transforms degrees into radians for a given latitude or longitude. The subroutine statement is SUBROUTINE CORRAD (RCOR, IDEG, IMIN, SEC, ID, IS, IERR) where:

RCOR = Location in radians.

IDEG = Location in degrees.

IMIN = Location in minutes.

SEC = Location in seconds.

ID = Character for north, south, east, or west.

IS = Latitude or longitude indicator.

IERR = Error code.

This subroutine is called from the driving program and returns radians to the driving program through the argument list. It is used to transform the input transmitter and receiver coordinates into radians.

### 3.5.3 SUBROUTINE GEOPTS

Given the distance  $S_p$  from point A to a point P on the geodesic between two prescribed points A, B, on the surface of a spheroidal earth, the FORTRAN sub-routines GEOPTS returns the latitude  $\phi_p$ , and longitude  $\theta_p$  of P, and the forward azimuth  $\psi_p$  of the geodesic of P as shown in Figure 6.

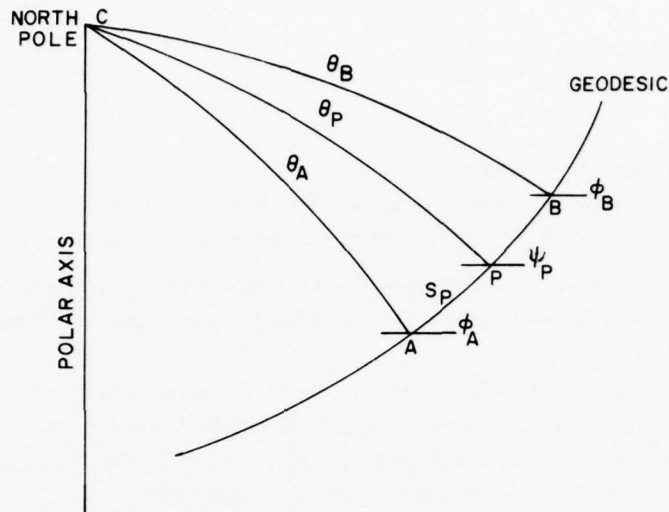


Figure 6. Geodesic Geometry

The derivation of the equations under the subroutine are described by Spies.<sup>6</sup> The subroutine statement is: SUBROUTINE GEOPTS (SMP, RLATP, RLONP, RAZP) where

SMP =  $S_p$  = distance (in meters) of P from A,

RLATP =  $\phi_p$  = latitude (in radians) of P,

RLONP =  $\theta_p$  = longitude (in radians) of P,

and

RAZP =  $\psi_p$  = forward azimuth (in radians) of geodesic of P.

Latitudes  $\phi_A$ ,  $\phi_B$  and longitudes  $\theta_A$ ,  $\theta_B$  of the prescribed end-points A, B are stored in the COMMON block PATH, along with certain output parameters. We

6. Spies, K.P. (1975) The Analytical Basis of Hufford's Computer Technique for Determining Topographic Profiles, Institute for Telecommunication Services Memo dated Nov. 4, 1975.

have the statement: COMMON/PATH/PLATA, RLONA, RIATB, RLONB, RAZA, RAZB, SMB, where

RLATA =  $\phi_A$  = latitude (in radians) of A,

RLONA =  $\theta_A$  = longitude (in radians) of A,

RLATB =  $\phi_B$  = latitude (in radians) of B,

RLONB =  $\theta_B$  = longitude (in radians) of B,

RAZA =  $\psi_A$  = forward azimuth (in radians) of geodesic of A,

RAZB =  $\psi_B$  = forward azimuth (in radians) of geodesic of B,

and

SMB =  $S_B$  = length (in meters) of geodesic from A to B.

North latitudes and east longitudes are positive, whereas south latitudes and west longitudes are negative. Positive azimuths are measured clockwise from north.

Parameters which specify relevant dimensions of the spheroidal earth are defined in the DATA statement: DATA ASPH, ESQ, CESQ/6378206.4, 0.006768658, 0.993231342/ where

ASPH = a = length (in meters) of semimajor axis of spheroid,

ESQ =  $e^2 = (a^2 - b^2)/a^2$  (where b is length of semiminor axis of spheroid),

CESQ =  $1 - e^2$ ,

and the numerical values correspond to the Clarke spheroid of 1866. Any other desired spheroid can be used in GEOPTS simply by replacing the above DATA statement by one containing the appropriate numerical values. For example, for the International spheroid, one would use:

DATA ASPH, ESQ, CESQ/6378388.0, 0.006722670, 0.993277330/.

As we shall see in the following section, the quantities  $\phi_p$ ,  $\theta_p$ ,  $\psi_p$ , are approximated by esculatory cubic polynomial functions of the distance  $S_p$  of P from A; for a fixed spheroid, the coefficients in these polynomials depend only on the location of the end-points A, B. To achieve computational efficiency in situations where  $\phi_p$ ,  $\theta_p$ ,  $\psi_p$  are to be calculated for more than one point P on the geodesic between a fixed pair of end points, GEOPTS is provided with a second entry point PCOORD (by including the ENTRY statement ENTRY PCOORD), whereby the subroutine skips the coefficient calculations and proceeds directly to the evaluation of the polynomial expressions for  $\phi_p$ ,  $\theta_p$ ,  $\psi_p$ . For a given pair of end-points A and B, the initial call to the subroutine must use the main entry point GEOPTS: that is, the calling program reference must be

CALL GEOPTS (etc., etc., ...).

Since the polynomial coefficients have already been evaluated, subsequent calls (for that path) should then use the entry point PCOORD: that is, the calling program reference should be:

CALL PCOORD (etc., etc., ...).

It is thus evident the subroutine GEOPTS is particularly efficient in those cases where  $\phi_p$ ,  $\theta_p$ ,  $\psi_p$  are desired for several to many points P on a single geodesic.

#### 3.5.4 SUBROUTINE GEORET

This subroutine is called from the driving program LORANCO. Subroutine GEORET obtains from the data through GETELV the values of elevation and impedance which occur at intervals along a geodesic specified by arrays LAT and LON. The path elevation and impedance data are transmitted to the driving program via blocked common statements.

The subroutine statement is SUBROUTINE GEORET (LAT, LONG, DSKM, NP) where:

LAT = Array of latitudes along a geodesic path.

LON = Array of longitudes along a geodesic path.

DSKM = Distance along geodesic path in KM.

NP = Number of points along the geodesic path.

To obtain elevations and impedances from the data base, GEORET steps through NP latitude and longitude points calling GETELV each time. Amplitude and phase data are returned, converted to real and imaginary values, and stored in arrays DR and DI. Elevation information is stored in array Z. Subroutine GEORET then calls subroutine INT to obtain the first and second derivative of the elevation data.

Support information required by GEORET and supplied by common blocks include:

- (1) Common/GROUND/
- (2) Common/INDUCT/
- (3) Common/TE/
- (4) Common/SDRDI/
- (5) Common/CITCT/

By use of common blocks, certain of the information can be directed to the double integral subroutine (INEQ) and its support subroutines, while other control data are transmitted to the driving section of the overall program.

### 3.5.5 SUBROUTINE GETELV

This subroutine is called from subroutine GEORET. Subroutine GETELV indexes the input latitude and longitude coordinates for subroutine UNPACK to obtain the proper ground electrical properties off the disc.

The subroutine statement is SUBROUTINE GETELV (LAT, LONG, AMP, FAZ, ELVTN) where:

LAT, LON - The input coordinate of each incremented point along the geodesic path.

AMP, FAZ, ELVTN = The output complex impedance (AMP, FAZ) and elevation (ELVTN) from the disc data base.

Two indices are selected of adjacent longitude records, NPACK, which encompass the input coordinate. These two records are separated by 30 in. in longitude and cover a latitude of one degree or 120 points. The elevation data, ELVTN, is obtained by a linear interpolation within the 30 in. square surrounding the desired coordinate, and is stored in eleven bits of the available thirty bit word. The impedance data of the southwest corner of the 30-in. square is used to represent the entire square. No impedance interpolation is required. For the complex impedance data, eight bits are used for the magnitude and eleven bits for the phase.

The impedance and elevation data are returned to subroutine GEORET through the argument list.

### 3.5.6 SUBROUTINE SETUP

This subroutine provides the spheroidal data for subroutine GEODI. Inputs are the semimajor (AO) and semiminor (BO) axis of the earth in meters. The spheroidal flattening (FL) and eccentricity square (ESQ) are calculated. The spheroidal constants for various ellipsoids are:

<u>Ellipsoid</u>	<u>Semimajor</u>	<u>Semiminor</u>
International	6378388.0	6356911.9
Clarke 1866	6378206.4	6356583.8
Clarke 1880	6378249.1	6356514.9
Bessel	6377397.2	6356079.0

Subroutine SETUP is called from subroutine GEODI and returns the required constants through the COMMON/GENERAL/block.

### 3.5.7 SUBROUTINE INT

Subroutine INT is called by subroutine GEORET and calculates the first and second derivative of the elevation at each point along the geodesic path. The subroutine statement is SUBROUTINE INT (I, K) where:



I = Position in x and z arrays on which to center calculations.

K = Position in arrays Z and ZP to store calculated values.

An analytical expression for a parabolic fit to three data points closest and including the required point along the geodesic path is derived by Sheed.<sup>7</sup> Differentiating this curve twice yields the required first and second derivative of the elevation at the position on which the calculations are centered. The results are returned to GEORET for use in subroutine INEQ via Common/Ground/block.

### 3.5.8 SUBROUTINE UNPACK

Subroutine UNPACK takes each sixty word record from the data base and unpacks each word into two complete data points composed of elevation and impedance information. Each called record contains the data for 120 points. The original sixty-bit words when unpacked, allow thirty bits for each data point. These are allocated as follows:

Elevation in meters, ELEV, 11 bits,  $\pm 7$  meters.

Magnitude of Impedance, AMP, 8 bits,  $\pm 2$  ohms.

Phase of Impedance, FAZ, 11 bits,  $\pm 0.001$  radians.

The information obtained is returned to GETELV.

For machines with 32 bit words, the UNPACK subroutine is altered so that one data point is obtained from each word.

### 3.5.9 SUBROUTINE INEQ

Subroutine INEQ is called from the driving program, LORANCO, and returns the secondary phase factor or additional time correction. The LAT and LON in the calling statement are the array of path length latitudes, and longitudes respectively.

The following constants are first set for the operation of this program:

NUT = 0 or 1 depending on type of receiver antenna.

RAD = radius of earth =  $6.36739 \times 10^6$  meters.

ALPHA = Vertical lapse factor = 0.85.

FREQ = Frequency = 0.1 MHz.

NSTART = Index of first distance at which the field is to be found as a function of altitude = 0.5 km.

ETA = Refractive index = 1.000338.

---

7. Sheed, F. (1962) Theory and Problems of Numerical Analysis, Shaum's Outline Series, McGraw Hill Co.

The attenuation function is calculated at discrete points as a function of geodesic distance.<sup>8</sup> The amplitude or modulus of the complex attenuation function is the field intensity and the phase or argument is the secondary phase correction in radians. To solve for this attenuation function, the boundary conditions must be known, then the solution can be extended step by step by numerical integration.

By assuming that the ground is smooth just in front of the transmitter, the first few points can be calculated with classical formulas.<sup>9</sup> For the remaining points, an integral equation approach is employed which allows one to introduce variations in ground elevation and variations in ground impedance relative to a classical spheroid. Special care must be exercised in the integration near the beginning and end of the integration path because the integrand approaches infinity at these points. A Gaussian quadrature integration formula<sup>10</sup> is employed in the area of such singularities, and Simpson's rule is used in the rest of the interval. The effective ground impedance which combines the elevation and impedance variations is obtained through a common statement from subroutine GROUND. After the calculations along the ground are completed for a given transmitter to receive path, a height gain loop<sup>4, 11</sup> is activated if the altitude input data is other than zero. Upon completion of the integration, the results are returned to the driving program through common block/DELAY/.

Input information initially obtained by the driving program from the stored disc data base is transmitted to subroutine INEQ via common blocks:

Common/GROUND/and Common/TE/

Transmitter-receiver path increment data enters via common blocks:

Common/SS/and Common/SDRDI/

Integral equation control of variables from the driving program into subroutine INEQ enter via:

Common/CITCT/

Calculations of secondary phase factors in units of microseconds are returned to the calling program via:

Common/DELAY/

8. Johler, J. R., and Horowitz, S. (1973) Propagation of LORAN-C Ground and Ionospheric Wave Pulses, Office of Telecommunications Report 73-20 (Superintendent of Documents, U. S. Government Printing Office, Washington, D. C. 20402).
9. Johler, J. R., Keller, W. J., and Walters, L. C. (1956) Phase of the Low Radiofrequency Ground Wave, NBS Circular 573 (Superintendent of Documents, U. S. Government Printing Office, Washington, D. C. 20402)
10. Abramovitz, M. and Stegun, I. (1964) Handbook of Mathematical Functions - NBS - Applied Math Series 55, U. S. Government Printing Office.
11. Scott, R. (1966) Phase of the Height-Gain Function of the Low Frequency Ground Wave, Report 2900-156-T of Project Michigan (Willow Run Laboratories, Ann Arbor, Michigan 48106).

3.6 Program Listing for Part III

```

PROGRAM LCRANCO(INPUT=128,OUTPUT=128,TAPE2)
DIMENSION IDENTF(3)
DIMENSION LAT(999),LON(999)
DIMENSION CISTDUM(3),TIMDUM(3)
DIMENSION TOA(3)
DIMENSION DISTSD(3)
DIMENSION TFW(3)
DIMENSION ALTTMSV(3,2)
DIMENSION FATHL(3)
DIMENSION LDUM(3,4),ADUM(3,4),RLA(3),PLO(3)
COMMON/FATH/RLATA,RLONA,PLATB,RLONB,RAZA,RAZB,SBM
COMMON/CITCT/ITCT,LTOP,ALTTMSV
COMMON/DELAY/NP,DISTSAV,TIMSAV
COMMON/ZOTA/ARRAY(40)
NAMelist/NAM1/TOA,TD1,TD2,ED1,ED2,DISTDUM,TIMDUM,DISTSD
1,TFW
DATA RTODEG/57.2957795130823/
DATA ITCT/1/
DATA ARRAY/100.,1.000338,40.,.1,5.,1.,3.,3000.,10.,0.,1000.,
1 .85,0.,1.,26*0./
C=.299792
EN=1.000338
ENG=FN/C
C READ TRANSMITTER COORDINATES FOR MASTER, S1,S2.
PRINT 101
PRINT 13
101 FORMAT(*1TRANSMITTER COORDINATES*)
MISKOD=C
DO 913 I=1,3
READ 102,IDENTF,LDUM(I,1),LDUM(I,2),ADUM(I,1),ADUM(I,2),
1 LDUM(I,3),LDUM(I,4),ADUM(I,3),ADUM(I,4),TCA(I)
PRINT 103,IDENTF,LDUM(I,1),LDUM(I,2),ADUM(I,1),ADUM(I,2),
1 LDUM(I,3),LDUM(I,4),ADUM(I,3),ADUM(I,4)
102 FORMAT(2X,3A8,2(I5,I3,F7.3,A1),F12.1,F5.2,I3)
103 FORMAT(2X,3A8,2(2X,I5,I3,F7.3,A1))
104 FORMAT(*1RECEIVER COORDINATES*)
CALL CCRRAD(RLO(I),LDUM(I,3),LDUM(I,4),ADUM(I,3),ADUM(I,4),1,MISKO
10)
CALL CCRRAD(PLA(I),LDUM(I,1),LDUM(I,2),ADUM(I,1),ADUM(I,2),0,MISKO
10)
IF(MISKOD.EQ.0) GO TO 913
PRINT 23
GO TO 10
913 CONTINUE
ED1=TOA(2)
ED2=TOA(3)
5 CONTINUE
READ 102,IDENTF,LATDEGR,LATMINB,SECLATR,LATIDB,LONCEGE,LONMINB,
1SECLONB,LONIDB,ALT,ADELS,NUT
IF(ADELS.LE.1) GO TO 10
PRINT 104
PRINT 13
PRINT 103,IDENTF,LATDEGB,LATMINB,SECLATR,LATIDB,LONCEGE,LONMINB,
1SECLONB,LONIDB
ARRAY(10)=ALT
ARRAY(14)=NUT
MISKOD=C

```

```

CALL CORRAD(RLATB,LATDEGB,LATMIMB,SECLATB,LATIDB,0,MISKOD)
CALL CORRAD(RLONB,LONDEGB,LONMIMB,SECLONB,LONIDB,1,MISKOD)
IF (MISKOD.EQ.0) GO TO 15
20 PRINT 23
23 FORMAT(/11X, 3H***, 9X, 29HERROR IN END-POINT COORDINATE, 10X, 3H
+***/11X, 54H*** CALCULATIONS FOR THIS PATH HAVE BEEN DELETED ***)
GO TO 5
15 CONTINUE
RLATA=RLA(ITCT)
RLONA=RLO(ITCT)
13 FORMAT(12H0 LOCATION, 22X, 8HLATITUDE, 9X, 9HLONGITUDE/
1 26X, 2(5X, 13H(DEG-MIN-SEC))//)
LTOP=0
25 CALL GEOPTS(0.0, RLATP, RLONP, RAZP)
CALL GEODI(RLATA, RLONA, RAZAS, SBMS, RLATB, RLONB, RAZBS)
SBKMS=SBMS*.001
DAZA = RTODEG*RAZA
DAZB = RTODEG*RAZB
SBKM = SBM*1.0E-3
DEL=SBKM-SBKMS
PRINT 2, ITCT, SBKMS, SBKM, DEL
2 FORMAT(*0GEODESIC DISTANCES, TRANSMITTER*I2* (POINT A) TO RECEIVER
1 (POINT B)*/7X*SODANO*9X*HUFFORD*6X*DIFFERENCE*/3F15.5)
NP = SBKM/ADELS+1.0
DSKM = NP
DSM = SBM/DSKM
DSKM = DSM*1.0E-3
PRINT 33, SBKM, DSKM, DAZA, DAZB
33 FORMAT(/18X, 20HLENGTH OF GEODESIC =, F11.5, 11H KILOMETERS//18X,
+ 20HDISTANCE INCREMENT =, F11.5, 11H KILOMETERS//12X, 34HFORWARD
+AZIMUTH OF GEODESIC AT A =, F12.6, 8H DEGREES//12X, 34HFORWARD AZI
+MUTH OF GEODESIC AT B =, F12.6, 8H DEGREES)
LAT(1)=LDUM(ITCT,1)*10000+LDUM(ITCT,2)*100+IFIX(ADUM(ITCT,1))
LON(1)=LDUM(ITCT,3)*10000+LDUM(ITCT,4)*100+IFIX(ADUM(ITCT,3))
NPP2=NP+2
SPM = 0.0
DO 100 IP=1, NPP2
SPM = SPM+DSM
CALL PCOORD(SPM, RLATP, RLONP, RAZP)
MISKOD = 0
CALL CORDMS(RLATP, LATDEGP, LATMIMP, SECLATP, LATIDP, 0, MISKOD)
CALL CORDMS(RLONP, LONDEGP, LONMIMP, SECLONP, LONIDP, 1, MISKOD)
IF (MISKOD) 30, 35, 30
30 PRINT 43, IP
43 FORMAT(/2X, 62H*** ERROR DETECTED DURING CONVERSION OF COORDINAT
+ES FOR POINT, 15, 5H ***/2X, 2H**, 7X, 52HFROM RADIANS TO (ALPHAM
+ERIC) DEGREES-MINUTES-SECONDS, 7X, 3H***/2X, 3H***, 66X, 3H***/2X,
+ 3H***, 7X, 52HFURTHER CALCULATIONS FOR THIS PATH HAVE BEEN DELETE
+D, 7X, 3H***)
GO TO 5
35 CONTINUE
LAT(IP+1 )=LATDEGP*10000+LATMIMP*100+IFIX(SECLATP)
LON(IP+1 )=LONDEGP*10000+LONMIMP*100+IFIX(SECLONP)
100 CONTINUE
IP=NP+3
CALL GEORET(LAT, LON, DSKM, IP )
C ADJUST NO OF PTS TO MATCH INEQ2E.

```

```

NP=NP+1
CALL INEQ2E(LAT,LON)
TOA(ITCT)=ENC*SBKMS +TIMSAV
TPW(ITCT)=ENC*SBKMS
DISTSOD(ITCT)=SBKMS
PATHL(ITCT)=SBKMS
DISTDUM(ITCT)=DISTSAB
TIMDUM(ITCT)=TIMSAV
ITCT=ITCT+1
IF(ITCT.LT.4)GO TO 15$IF(LTOP.LT.1) PRINT 410
410 FORMAT(*0 GROUNDWAVE TIME DELAY CALCULATION*)
TD1=ED1+TOA(2)-TOA(1)
TD2=ED2+TOA(3)-TOA(1)
PRINT NAM1
IF(LTOP.LT.1) GO TO 6
DO 8 L=1,LTOP
PRINT 7
7 FORMAT(*0 ALTITUDE TIME DELAY CALCULATIONS*)
DO 9 I=1,3
TOA(I)=ENC*PATHL(I)+ALTTMSV(I,L)
9 CONTINUE
TD1=ED1+TOA(2)-TOA(1)
TD2=ED2+TOA(3)-TOA(1)
PRINT NAM1
8 CONTINUE
6 CONTINUE
ITCT=1
GO TO 5
10 CONTINUE
PRINT 11
11 FORMAT(*0 END OF INPUT DATA.*)
END

```

```

SUBROUTINE GEORET(LAT,LON,DSKM,NP)
DIMENSION LAT(999),LON(999)
COMMON /GROUND/ZDUM, Z, ZPDUM, ZP, XDUM, X, R0, DEN, R, U, OMX, WA
1VE, R2, ZPP, D, DDD1, DDD2
COMMON/INDUCT/NAV
COMMON/TE/TLA,TLON,RLAT,RLON,HLAT,HLON, ZPP1,DINC1,TPI,NPTS
1,ZMAZ,WTH
COMMON /SDRDI/S(999), DR(999), DI(999), LLM
DIMENSION ZDUM(6), Z(1009), ZPDUM(6), ZP(1009), XDUM(6), X(1009),
1 ZPP1(1009)
COMMON/CITCT/ ITCT
COMPLEX D,DEN,DDD1,DDD2
TPI=6.283185307
TLA=LAT(1)
TLON=LON(1)
RLAT=LAT(NP)
RLON=LON(NP)
DINC1=DSKM
NPTS=NP
S(1)=0.
X(1)=0.
DO 1 I=1,NP
AAMP=.0744$FAZ=.74109$Z(I)=2.

```

```

CALL GETELV(LAT(I),LON(I),AAMP,FAZ,Z(I) )
IF (I.GT.1) S(I)=S(I-1)+DSKM
DR(I) = AAMP * COS(FAZ)
DI(I) = AAMP * SIN(FAZ)
1 CONTINUE
LLM=NP
C   GENERATE INDEPENDENT PATH TERRAIN ELEVATIONS RELATIVE TO TRANSMIT
Q=Z(1)
Z(1)=0.
DO 2 I=2,NP
C   FOR NOW, CONVERT DISTANCE TO METERS.
S(I)=S(I)*1000.
X(I)=S(I)
Z(I)=Z(I)-Q
2 CONTINUE
C   OBRAIN ELEVATION DERAVITIVES.
NPM1=NP-1
DO 3 L=2,NPM1
CALL INT(L,L)
ZPP1(L)=ZPP
3 CONTINUE
ZP(1)=0.
ZPP1(1)=0.
ZP(NP)=ZF(NP-1)
ZPP1(NP)=ZPP1(NP-1)
RETURN
END

```

```

SUBROUTINE CORRAD(RCOR,IDEG,IMIN,SEC,IO,IS,IERR)
DIMENSION IDS(4)
DATA (IDS=1HN,1HE,1HS,1HW)
ISS = IS
IF (ISS) 10,5,15
5 IF (ID.EQ.IDS(1)) GO TO 25
IF (ID.EQ.IDS(3)) GO TO 30
10 IERR = 1
RETURN
15 IF (ISS-1) 20,20,10
20 IF (ID.EQ.IDS(2)) GO TO 25
IF (ID.EQ.IDS(4)) GO TO 30
IERR = 1
RETURN
25 SIGN = 1.0
GO TO 35
30 SIGN = -1.0
35 IF (IDEG-180) 40,40,10
40 IF (IMIN-60) 45,10,10
45 IF (SEC-60.0) 50,10,10
50 RCOR = SIGN*FLOAT(IDEG)*(1.74532925199433E-2)+FLOAT(IMIN)*
+ (2.90888208665722E-4)+SEC*4.84813681109536E-6
RETURN
END

```

```

SUBROUTINE GEOPTS(SMP,RLATP,RLONP,RAZP)
COMMON/PATH/RLATA,RLONA,RLATB,RLONB,RAZA,RAZB,SMB
DATA ASPH,ESQ,CESQ/6378388.000, 6.722670022E-3, 9.932773300E-1/
DATA PID2, PI, TWOPI/1.57079632679490, 3.14159265358979,
+ 6.28318530717959/
IF (ABS(RLATA)-PID2) 5,10,10
5 IF (ABS(RLATB)-PID2) 15,10,10
10 PRINT 3,RLATA,RLATB
3 FORMAT(1H1, 89H SUBROUTINE GEOPTS CALLED WITH END-POINT LATITUD
+E OUT OF ACCEPTABLE RANGE (-PI/2,PI/2)//13X, 16HLATITUDE OF A =,
+F8.2, 29H RADIANS LATITUDE OF B =, F8.2, 8H RADIANS)
PRINT 13
13 FORMAT(33X, 20HPROGRAM EXECUTION TERMINATED)
STOP
15 IF (ABS(RLONA)-TWOPI) 20,20,25
20 IF (ABS(RLONB)-TWOPI) 30,30,25
25 PRINT 23,RLONA,RLONB
23 FORMAT(1H1, 88H SUBROUTINE GEOPTS CALLED WITH END-POINT LONGITU
+E OUT OF ACCEPTABLE RANGE (-2PI,2PI)//10X, 17HLONGITUDE OF A =,
+F9.2, 31H RADIANS LONGITUDE OF B =, F9.2, 8H RADIANS)
PRINT 13
STOP
30 ALONR = RLONA
BLONR = RLONB
IF (ALONR+PI) 35,35,40
35 ALONR = ALONR+TWOPI
40 IF (BLONR+PI) 45,45,50
45 BLONR = BLONR+TWOPI
50 BLON = BLONR-ALONR
IF (BLON+PI) 55,70,75
55 IF (BLONR) 60,65,65
60 BLONR = BLONR+TWOPI
GO TO 95
65 ALONR = ALONR-TWOPI
GO TO 95
70 PRINT 33
33 FORMAT(1H1, 88H GEODESIC PATH INCLUDES A GEOGRAPHIC POLE - SUBR
+OUTINE GEOPTS CANNOT HANDLE THIS CASE)
PRINT 13
STOP
75 IF (BLON-PI) 95,70,80
80 IF (BLONR-PI) 90,90,85
85 BLONR = BLONR-TWOPI
GO TO 95
90 ALONR = ALONR+TWOPI
95 SMB = RLATA+RLATB
HETA = SIN(0.5*SMB)
HETA = (1.0-ESQ*HETA*HETA)/CESQ
HLAT = ASPH/(HETA*SQRT(HETA*CESQ))
BLON = BLONR-ALONR
ALON = HETA*BLON
Q = SIN(ALON)
BLAT = COS(RLATB)
ALAT = COS(RLATA)
SAZA = Q*BLAT
SAZB = Q*ALAT
Q = SIN(0.5*ALON)

```

```

Q = Q*Q
AAZ = RLATB-RLATA
CAZB = (1.0-Q)*SIN(AAZ)
Q = Q*SIN(SMB)
CAZA = CAZB+Q
CAZB = CAZB-Q
Q = SQRT(SAZA*SAZA+CAZA*CAZA)
SMB = HLAT*ASIN(Q)
SAZA = SAZA/Q
CAZA = CAZA/Q
SAZB = SAZB/Q
CAZB = CAZB/Q
RAZA = ATAN2(SAZA,CAZA)
RAZB = ATAN2(SAZB,CAZB)
ALON = RAZE-RAZA
IF (ABS(ALCN)-PI) 120,105,105
105 IF (ALCN) 110,110,115
110 RAZB = RAZB+TWOPI
GO TO 120
115 RAZA = RAZA+TWOPI
120 H.LAT = CESC+ESQ*ALAT*ALAT
HLON = ASPH/SQRT(HLAT)
HLAT = HLON*CESQ/HLAT
HLON = HLON*ALAT
CLAT = CAZA/HLAT
CLON = SAZA/HLON
HLAT = CESC+ESQ*BLAT*BLAT
HLON = ASPH/SQRT(HLAT)
HLAT = HLON*CESQ/HLAT
HLON = HLON*BLAT
ALAT = CAZB/HLAT
BLAT = (3.0*AAZ/SMB-ALAT-2.0*CLAT)/SMB
ALON = SAZB/HLON
BLON = (3.0*BLON/SMB-ALON-2.0*CLON)/SMB
AAZ = 3.0*SMB
ALAT = ((ALAT-CLAT)/SMB-2.0*BLAT)/AAZ
ALON = ((ALON-CLON)/SMB-2.0*BLON)/AAZ
AAZ = (RAZB-RAZA)/SMB
ENTRY PCOORD
RLATP = ((ALAT*SMP+BLAT)*SMP+CLAT)*SMP+RLATA
RLONP = ((ALON*SMP+BLON)*SMP+CLON)*SMP+ALONR
RAZP = AAZ*SMP+RAZA
RETURN
END

```

```

SUBROUTINE CORDMS(RCOR, IDEG, IMIN, BEC, ID, IS, IERR)
DIMENSION IDS(4)
DATA (IDS=1HW,1HE,1HS,1HW)
RANG = RCOR
SEC = ABS(RANG)*206264.806247896
ISS = IS
IF (ISS) 5,10,15
5 IERR = 1
RETURN
10 IF (SEC-324000.0005) 25,5,5
15 IF (ISS-1) 20,20,5
20 IF (SEC-648000.0005) 25,5,5

```



```

25 IF (RANG) 30,35,35
30 ISI = 2
   GO TO 40
35 ISI = 0
40 IDEG = SEC/3600.0
   IMIN = SEC/60.0-60.0*FLOAT(IDEG)
   SEC = SEC-3600.0*FLOAT(IDEG)-60.0*FLOAT(IMIN)
   ISEC = SEC
   SEC = SEC-FLOAT(ISEC)
   IF (SEC-0.9995) 60,45,45
45 SEC = 0.0
   ISEC = ISEC+1
   IF (ISEC-60) 60,50,50
50 ISEC = 0
   IMIN = IMIN+1
   IF (IMIN-60) 60,55,55
55 IMIN = 0
   IDEG = IDEG+1
60 LDX = ISI+ISS+1
   BEC=FLOAT(ISEC)+SEC
   ID=IDS(LDX)
   RETURN
   END

```

```

SUBROUTINE INEQ2E(LAT,LON)
  DIMENSION LAT(999),LON(999)
  COMMON /55/DISS(999)
  COMMON /GROUND/ZDUM, Z, ZPDUM, ZP, XDUM, X, R0, DEN, R, U, OMX, MA
  VE, R2, ZPP, D, DDD1, DDD2
  COMMON/INDUCT/NAV
  COMMON/TE/TLA,TLON,RLAT,RLON,HLAT,HLON,      ZPP1,DINC1,TPI,NPTS
  1,ZHAZ,MTH
  COMMON /ZOTA/ARRAY
  COMMON /SDRDI/S(999), DR(999), DI(999), LLM
  COMMON/CITCT/ITCT,LTOP,ALTT MSV
  COMMON/DELAY/NP,DISTSAV,TIMSAV
  DIMENSION ALTTMSV(3,2)
  DIMENSION E(999 , 2), F(999 , 2)
  DIMENSION ZZ(5), H(5)
  DIMENSION ZDUM(6), Z(1009), ZPDUM(6), ZP(1009), XDUM(6), X(1009),
  1TZER(1), T(1000), GW(5), GX(5), EW(9), EX(9), WG(5), XS(9), WE(9),
  2 W(1000),ARRAY(40),ZPP1(1009)
  COMPLEX D, DEN, DDD1, DDD2, FLEAF, F1, F2, F3, G1, G2, G3, SUM, TE
  1RM, W, WE, WG, WW, WX
  COMPLEX TS,FIND,FINDH
  EQUIVALENCE (ARRAY(1),FKHZ), (ARRAY(2),ETA), (ARRAY(3),DMAX), (
  1ARRAY(4),DINC), (ARRAY(8),ZMIN), (ARRAY(9),ZINC), (ARRAY(10),Z
  2MAX), (ARRAY(11),FLAT)
  DATA IARRA/0/
  DATA ((GX(K), K = 1, 5) = .02216356881, .1078315676, .4615973615,
  1.7483346284, .9484939262)
  DATA ((GW(K), K = 1, 5) = .5910484494, .5385334386, .438172725,
  1 .2989026983, .1333426886)
  DATA ((EX(K), K = 1, 4) = .1051402826, .3762245145, .6989480124,
  1 .9373342493)

```

```

DATA ((EW(K), K = 1, 4) = .06568051989, .1960962655, .2525273456,
1.1523625357)
DATA (TZER(1)=1.0)
6 FORMAT (//E20.7,5X,*ARRAY(1) = FKHZ = FREQUENCY IN KHZ*/
1 E20.7,5X,*ARRAY(2) = ETA = AIR INDEX OF REFRACTION AT GROUND*/
2 E20.7,5X,*ARRAY(3) = DMAX = MAXIMUM DISTANCE BETWEEN TRANSMITTER*
3 ,* AND RECEIVER IN KM*/
4 E20.7,5X,*ARRAY(4) = DINC = DISTANCE INCREMENT IN KM*/
5 E20.7,5X,*ARRAY(5) = NSTART = INDEX OF THE FIRST DISTANCE AT*,
6 * WHICH THE FIELD IS TO BE FOUND AS A FUNCTION OF ALTITUDE*/
7 E20.7,5X,*ARRAY(6) = NZINC = THE FIELD IS TO BE FOUND AS A *,
8 *FUNCTION OF ALTITUDE EVERY NZINC INCREMENTS IN THE */
9 40X,*DISTANCE ARRAY -- NZINC MUST NEVER BE LESS THAN 1*)
7 FORMAT (E20.7,5X,*ARRAY(7) = INDEX OF THE LAST DISTANCE AT WHICH*,
1 * THE FIELD IS FOUND AS A FUNCTION OF ALTITUDE*/
2 E20.7,5X, *ARRAY(8) = ZMIN = THE MINIMUM ALTITUDE ABOVE THE *,
3 *SURFACE AT WHICH THE FIELD IS FOUND, METERS*/
4 E20.7,5X, *ARRAY(9) = ZINC = THE ALTITUDE INCREMENT, METERS*/
5 E20.7,5X,*ARRAY(10) = ZMAX = THE MAXIMUM ALTITUDE, METERS*/
6 E20.7,5X,*ARRAY(11) = FLAT = THE FACTOR USED IN THE FLAT EARTH *,
7 *TEST, METERS*/
8 E20.7,5X,*ARRAY(12) = ALPHA = VERTICAL LAPSE FACTOR*/
9 E20.7,5X,*ARRAY(13) = EFFECTIVE EARTHS RADIUS*/
A E20.7,5X,*ARRAY(14) = NUT*//)
IF(IARRA.GT.1) GO TO 9999
IARRA=2
C SET CONSTANTS
NUT=ARRAY(14)
RAD = 6.36739E+6 / ARRAY(12)
ARRAY(13) = RAD
FREQ = FKHZ * 1.E-3
NSTART = ARRAY(5)
NZINC = ARRAY(6)
IF (ARRAY(6) .LT. 1.) NZINC = 1
NZERO=0
T(NZERO)=1.0
WAVE = 2.095844729E-2 * FREQ
WAVE = WAVE * ETA
WAV=WAVE
AMICRO = 1.0 / (TPI * FREQ)
TX = SQRT(FREQ * ETA) * .0408389549
X(1) = 0.
M(1) = 1.
9999 CONTINUE
DECTX=X(2)
DMAX=X(NPTS)/1000.
DINC=DECTX/1000.
ARRAY(4)=DINC
DINC1=DINC
ARRAY(7) = DMAX / DINC + 1.
NZEND = ARRAY(7)
PRINT 6, (ARRAY(I), I=1, 6)
PRINT 7, (ARRAY(I), I=7, 14)
NOFLAT = 1
NGO = 1
D = CMPLX(DR(1), DI(1)) * SQRT(FREQ / 0.1)
IMOST = DMAX / DINC + .01
DELTX = 1000. * DINC
T(1) = 1. / SQRT(DELTX)

```

```

31 DO 32 K = 1, 5
   X(-K) = DELTX * GX(K)
   CALL GROUND(-K, 2, 0, 0)
32 WG(K) = FLEAF(WAVE, 0., 0., X(-K), D)
   I = 2
37 CONTINUE
   ZPP=ZPP1(I)
   T(I) = 1. / SQRT(X(I) + DELTX)
   OMX = OMCOS(X(I) / RAD)
   IGO = 2 - MOD(I, 2)
   IL = I - IGO - 1
   RD = SQRT(2. * RAD * (RAD + Z(I)) * OMX + Z(I) * * 2)
   GO TO (40, 45), NOFLAT
40 IF (I .LE. 4 .OR. (FLAT .GT. X(I))) 41, 45
41 W(I) = FLEAF(WAVE, 0., 0., X(I), D)
   GO TO 90
45 SUM = 0.
   NOFLAT = 2
48 DO 50 K = 1, 5
   CALL GEOM(I, -K, 1, 0.)
   TERM = WG(K) * CMPLX(COS(WAVE * R), - SIN(WAVE * R)) * DEN
50 SUM = (U * GW(K)) / SQRT(X(I) - X(-K)) * TERM + SUM
   SUM = 3. * T(1) * SUM
   KK = 1
   IF (IL .LT. 3) GO TO 100
   DO 60 K = 3, IL
   CALL GEOM(I, K, 1, 0.)
   TERM = U * T(K - 1) * W(K) * CMPLX(COS(WAVE * R), SIN(- WAVE * R)
1) * DEN
   GO TO (53, 55), KK
53 SUM = 4. * T(I - K) * TERM + SUM
   KK = 2
   GO TO 60
55 SUM = 2. * T(I - K) * TERM + SUM
   KK = 1
60 CONTINUE
100 CONTINUE
   CALL GEOM(I, 2, 1, 0.)
   SUM = T(I - 2) * T(1) * U * W(2) * CMPLX(COS(WAVE * R), - SIN(WAVE
1 * R)) * DEN + SUM
62 CALL GEOM(I, I - IGO, 1, 0.)
   F2 = U * T(IL) * W(I - IGO) * CMPLX(COS(WAVE * R), - SIN(WAVE * R)
1) * DEN
   SUM = (SUM + T(IGO) * F2) * .33333333 * DELTX
   GO TO (65, 66), IGO
65 F1 = F2
   F2 = TERM
   GO TO 70
66 CALL GEOM(I, I - 1, 1, 0.)
   F1 = U * T(I - 2) * W(I - 1) * CMPLX(COS(WAVE * R), - SIN(WAVE * R
1)) * DEN
   SUM = SUM + .0833333333 * DELTX * (5. * T(1) * F1 + 8. * T(2) * F
12 - T(3) * TERM)
70 Q = TX / T(I - 1)
   RHO = 1. + ZP(I) * * 2
   RHO = ZPP / RHO
75 TERM = 1.2 / T(1) * T(I - 1) * CMPLX(Q, Q) * (D + CMPLX(0., - RHO
1 / WAVE))
   WX = 1. - CMPLX(Q, Q) * (SUM + 2. / T(1) * (.466666667 * F1 - .066
1666667 * F2)) / (1. + TERM)

```

```

85 W(I) = WX
90 DIST = .001 * X(I)
   CALL INDF(0.,X(I),NUT,FIND)
   TS=W(I)*FIND
   AMP=CABS(TS)
   PHA=CANG(TS)
   PHIC = - (PHA - WAVE * (R0 - X(I)))
   SEC = PHIC * AMICRO
   IF(I.NE.NP) GO TO 9876
   DISTSAV=DIST
   TIMSAV=SEC
9876 CONTINUE
   I = I + 1
   IF(I.LE.NPTS) GO TO 37
150 NGO = 2
   IF (ZMAX.LE.0.) RETURN
   ITOP = (NZEND - NSTART) / NZINC + 1
   IF (ITOP .GT. 1500) GO TO 280
   LTOP=(ZMAX-ZMIN)/ZINC+1.1
   IF(LTOP.GT.5) GO TO 280
   F2=(0.,0.)
   G2=(0.,0.)
   OLDR=0.
   IF (ITOP .LT. 1) GO TO 105
   NPALT=NP-NSTART+1
   DO 200 IS = 1, ITOP
   I = NSTART + (IS - 1) * NZINC
   II=I
   IF (I.GE.NZEND) II=NZEND-1
   IGO = 2 - MOD(I, 2)
   DO 155 K = 1, 4
   X(1000 + K) = X(I) - DELTX * EX(K)
   XS(K) = X(1000 + K)
155 CALL GROUND (1000+K,II,0,0)
   CALL CNEVKEN(X, W, IMOST, XS, WE, 4, 5, 1)
   IF (LTOP .LT. 1) GO TO 110
   DO 195 L = 1, LTOP
   H(L) = ZMIN + (L - 1) * ZINC
   IF (H(L) .LT. Z(I)) 156, 154
156 HW = 0.
   GO TO 193
154 ZZ(L) = RAD + H(L)
   R0 = SQRT(2. * RAD * ZZ(L) * OMCOS(X(I) / RAD) + H(L) * * 2)
   SUM = 0.
   DO 157 K = 1, 5
   CALL GEOM(I, - K, 2, H(L))
   TERM = WG(K) * CMPLX(COS(WAVE * R), - SIN(WAVE * R)) * DEN
157 SUM = U * GW(K) * TERM / SQRT(X(I) - X(- K)) + SUM
   SUM = 3. * T(1) * SUM
   CALL GEOM(I, 3, 2, H(L))
   F1 = T(1) * T(I - 2) * U * DEN * W(2)
   G1 = CMPLX(COS(WAVE * R), - SIN(WAVE * R))
   SUM = SUM + F1 * G1
   ILO = I - IGO
   KGO = 1
   IF (ILC .LT. 3) GO TO 115
   DO 182 K = 3, ILO
   F3 = F2
   G3 = G2
   F2 = F1

```

```

G2 = G1
CALL GEOM(I, K, 2, H(L))
G1 = CMPLX(COS(WAVE * R), - SIN(WAVE * R))
F1 = T(K - 1) * T(I - K) * U * DEN * W(K)
DELTG = WAVE * (R - OLDR)
GO TO (158, 159, 172), KGO
158 SUM = SUM + 4. * F1 * G1
KGO = 2
GO TO 182
159 SUM = SUM + 2. * F1 * G1
KGO = 1
IF (ABS(DELTG) .GT. .2) 170, 182
170 KGO = 3
SUM = SUM - F1 * G1
GO TO 182
172 SUM = SUM + CMPLX(0., 3. / DELTG) * (G1 * (F1 - .5 * (F1 * CMPLX(2
1., 3. * DELTG) - 4. * F2 * CMPLX(1., DELTG) + F3 * CMPLX(2., DELTG
2)) / DELTG ** 2) - G2 * (F2 - .5 * (F1 * CMPLX(2., DELTG) - 4. *
3F2 + F3 * CMPLX(2., - DELTG)) / DELTG ** 2))
182 OLDR = R
115 CONTINUE
GO TO (188, 183), IGO
183 F3 = F2
G3 = G2
F2 = F1
G2 = G1
CALL GEOM(I, I - 1, 2, H(L))
G1 = CMPLX(COS(WAVE * R), - SIN(WAVE * R))
F1 = T(I - 2) * T(1) * U * DEN * W(I - 1)
DELTG = WAVE * (R - OLDR)
IF (ABS(DELTG) .GT. .2) 184, 185
184 SUM = SUM + CMPLX(0., 3. / DELTG) * (G1 * (F1 - .5 * (F1 * CMPLX(2
1., 3. * DELTG) - 4. * F2 * CMPLX(1., DELTG) + F3 * CMPLX(2., DELTG
2)) / DELTG ** 2) - G2 * (F2 - .5 * (F1 * CMPLX(2., DELTG) - 4. *
3F2 + F3 * CMPLX(2., - DELTG)) / DELTG ** 2))
GO TO 188
185 SUM = SUM + 1.25 * F1 * G1 + 2. * F2 * G2 - .25 * F3 * G3
188 DO 190 K = 1, 4
CALL GEOM(I, 1000 + K, 3, H(L))
SUM = SUM + 3. * EW(K) * WE(K) * CMPLX(COS(WAVE * R), - SIN(WAVE *
1 R)) * DEN * U / (SQRT(XS(K)) * T(1))
190 CONTINUE
SUM = .33333333 * DELTX * SUM
Q = TX / T(I - 1)
MW = (1. - CMPLX(Q, Q) * SUM) * .5
193 CONTINUE
CALL INDF (H(L), X(I), NUT, FINDH)
TS=MW*FINDH
E(IS, L) = CABS(TS) * 1.257 * FREQ / R0
F(IS, L) = - (CANG(TS) - WAVE * (R0 - X(I)))
195 CONTINUE
110 CONTINUE
DISS (IS) = .001 * X(I)
200 CONTINUE
105 CONTINUE
IF (LTOP .LT. 1) GO TO 120
DO 250 L = 1, LTOP
IF (ITCP .LT. 1) GO TO 125
DO 240 IS = 1, ITOP

```

```

      FM = F(IS, L) * AMICRO
      IF(IS.NE.NPALT) GO TO 9877
      ALTTMSV(ITCT,L)=FM
9877 CONTINUE
240  CONTINUE
125  CONTINUE
250  CONTINUE
120  CONTINUE
280  CONTINUE
      RETURN
      END

SUBROUTINE GROUND(I, K, IGO, HH)
COMMON /GROUND/ZDUM, Z, ZPDUM, ZP, XDUM, X, R0, DEN, R, U, OMX, WA
1VE, R2, ZPF, DELTA, DELTA1, DELTA2
COMMON /ZOTA/ARRAY
COMMON /SDRDI/S(999), DR(999), DI(999), LLM
DIMENSION ZDUM(6), Z(1009), ZPDUM(6), ZP(1009), XDUM(6), X(1009),
1ARRAY(40)
COMPLEX DELTA, DEN, DELTA1, DELTA2
EQUIVALENCE (ARRAY(1), FKHZ), (ARRAY(13), A)
CALL INT (K,I)
FREQ = FKHZ * 1.E-3
RETURN
ENTRY GEOM
HIT = Z(I) + HH
IF (I .EQ. K) GO TO 20
T = (X(I) - X(K)) / A
GS = A + Z(K)
GX = A + HIT
CT = COS(T)
ST = SIN(T)
OT = OMCOS(T)
R2 = SORT(2. * GS * GX * OT + (HIT - Z(K)) * * 2)
R1 = SORT(2. * A * GS * OMCOS(X(K) / A) + Z(K) * * 2)
R = R1 + R2 - R0
U = X(K) * R0 * SQRT(1 + ZP(K) * * 2) / (R1 * R2 * X(I))
IF (IGC .LT. 3) U = U * (X(I) - X(K))
PD = (A * OT + Z(K) - HIT * CT + GX * ZP(K) * A * ST / GS) / R2
XK = X(K)
IF (XK .GE. S(LLM)) GO TO 12
LLL = 1
IF (XK .LT. S(1)) GO TO 10
LLMO = LLM - 1
IF (LLMO .LT. 1) GO TO 100
DO 13 LLL = 1, LLMO
IF (XK .LT. S(LLL + 1) .AND. XK .GE. S(LLL)) GO TO 10
13  CONTINUE
100  CONTINUE
GO TO 21
10  DELTA = CMPLX(DR(LLM), DI(LLM)) * SQRT(FREQ / 0.1)
GO TO 21
12  DELTA = CMPLX(DR(LLM), DI(LLM)) * SQRT(FREQ / 0.1)
21  CONTINUE
DELTA2 = CMPLX(1., - 1. / (WAVE * R2)) * PD
DELTA1 = DELTA - DELTA2
19  DEN = DELTA2 + DELTA
      RETURN

```

```

20 U = 0.
   R2 = GX - A - Z(I)
   RETURN
   END

```

```

SUBROUTINE GETELV(LATX,LONX,AMP,FAZ,ELVTN)
COMMON/GETELV/L(120),IMP(120)
COMMON/UNPACK/NPACK(60)$COMMON/FLAGS/IXPT,NFLAG
DIMENSION MSINDX(5800)
DATA KPS1/1/
INDDIM=5800
IF(KPS1.EQ.1) CALL OPENMS(2,MSINDX,INDDIM,0)$KPS1=0
M11=37778$M8=3778
IF(LATX.LT.480000 .OR. LATX.GE.540000) GO TO 190
IF(LONX.LT.060000 .OR. LONX.GE.140000) GO TO 190
NFLAG=0$LATSEC=MOD(LATX,100)$LONSEC=MOD(LONX,100)
LATDM=LATX-LATSEC$LONDM=LONX-LONSEC$IF(LATSEC.GE.30)GOTO40
LATS=LATDM$LATN=LATDM+30$GO TO 60
40 LATS=LATDM+30$LATN=LATDM+100$LATM=MOD(LATDM,10000)
IF(LATM.EQ.5900) LATN=LATDM+4100
60 IF(LONSEC.GE.30)GOTO80$LONW=LONDM$LONE=LONDM+30$GOTO100
80 LONW=LONDM+30$LONE=LONDM+100
LONM=MOD(LONDM,10000)
IF(LONM.EQ.5900) LONE=LONDM+4100
100 CONTINUE
INDNE=INDEX(LATN,LONE)
IF(NFLAG.EQ.1) GO TO 120
CALL READMS(2,NPACK,60,INDNE)
CALL UNPACK
INE=L(IXPT)
IF(MOD(LATN,10000).EQ.0.OR.MOD(LONE,20000).EQ.0)GOTO120
ISE=L(IXPT-1)
CALL READMS(2,NPACK,60,INDNE-1)$CALL UNPACK
INW=L(IXPT)$ISW=L(IXPT-1)$GO TO 180
120 CONTINUE
INDNW=INDEX(LATN,LONW)
IF(NFLAG.EQ.1) GO TO 140
CALL READMS(2,NPACK,60,INDNW)
CALL UNPACK
INW=L(IXPT)
140 CONTINUE
INDSE=INDEX(LATS,LONE)
IF(NFLAG.EQ.1) GO TO 160
CALL READMS(2,NPACK,60,INDSE)
CALL UNPACK
ISE=L(IXPT)
160 CONTINUE
INDSW=INDEX(LATS,LONW)
IF(NFLAG.EQ.1) GO TO 180
CALL READMS(2,NPACK,60,INDSW)
CALL UNPACK
ISW=L(IXPT)
180 CONTINUE
AMP=FLCAT(SHIFT(IMP(IXPT),-11).A.M8)*.001
FAZ=FLOAT(IMP(IXPT).A.M11)*.001
IF(NFLAG.EQ.1) PRINT 3100

```

```

ELEAST=FLOAT(ISE)+FLOAT((INE-ISE)*(LATSEC-(LATSEC/30)*30))/30.
ELWEST=FLOAT(ISW)+FLOAT((INW-ISW)*(LATSEC-(LATSEC/30)*30))/30.
ELVTN=ELWEST+(ELEAST-ELWEST)*FLOAT(LONSEC-(LONSEC/30)*30)/30.
RETURN
190 PRINT 2070
RETURN
2070 FORMAT(* *,4H****,*LAT,LON REQUESTED ARE OUTSIDE MAP REGION - NO E
1ELEVATION RETURNED*,//)
3100 FORMAT(* *,4H****,*INDEX REQUESTED EXCEEDS SCANLINES GENERATED, TH
1US PREVIOUS ELEVATIONS WILL BE USED*)
END

```

```

FUNCTION INDEX(LAT,LON)
COMMON/FLAGS/IXPT,NFLAG
LATS=MOD(LAT,100)
LATH=MOD(LAT,10000)-LATS
LATD=(LAT-LATH-LATS)/10000
LATN=LATH/100
LONS=MOD(LON,100)
LONM=MOD(LON,10000)-LONS
LOND=(LON-LONM-LONS)/10000
LONN=LONM/100
ISUBLN=(LOND*5)
ISUBLN=(MOD(ISUBLN,10)/5)*120
ILOND=((LOND-6)/2)*1440+ISUBLN+LONM*2+LONS/30+1
INDEX=ILOND+(LATD-48)*248
IXPT=LATH*2+LATS/30+1
IF(INDEX.GT.5760)NFLAG=1
RETURN
END

```

```

SUBROUTINE UNPACK
COMMON/GETELV/L(120),IMP(120)
COMMON/UNPACK/NPACK(60)
DATA MSK1/3777B/,MSK2/177777B/
DO 20 MA=1,60$M=2*(MA-1)+1
L(M)=AND(MSK1,SHIFT(NPACK(MA),-49))*8
IMP(M)=AND(MSK2,SHIFT(NPACK(MA),30))
L(M+1)=AND(MSK1,SHIFT(NPACK(MA),-19))*8
IF(L(M).GT.2000)L(M)=96$IF(L(M+1).GT.2000)L(M+1)=96
IMP(M+1)=AND(MSK2,NPACK(MA))
20 CONTINUE$END

```



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SUBROUTINE GEODI(B1, AL1, AZ12, S, B2, AL2, AZ21)
C-----CALCULATES INVERSE COMPUTATION FORM (SODANO, 1965)
C-----B1,AL1,B2,AL2 ARE GIVEN DATA
C-----AZ12,S, AZ21 ARE CALCULATED DATA
C-----B1 = GEODETIC LATITUDE, RADIANS, OF FIRST POINT
C-----AL1 = GEODETIC LONGITUDE, RADIANS, OF FIRST POINT
C-----B2 = GEODETIC LATITUDE, RADIANS, OF SECOND POINT
C-----AL2 = GEODETIC LONGITUDE, RADIANS, OF SECOND POINT
C-----AZ12 = FORWARD AZIMUTH, RADIANS, FROM FIRST POINT
C-----AZ21 = BACK AZIMUTH, RADIANS, FROM SECOND POINT
C-----S = DISTANCE (LENGTH OF GEODETIC LINE) BETWEEN POINTS, METERS
C-----SOUTHERN LATITUDES AND WESTERN LONGITUDES ARE NEGATIVE
COMMON /GENERAL/TPI, PI, PI2, PI4, A0, B0, FL, ESQ, IFLAG
DATA (IFLAG = 1)
IF (IFLAG .EQ. 1) CALL SETUP
IF (ABS(B1) .GT. PI4) GO TO 1
TBET1 = TAN(B1) * (1. - FL)
BET1 = ATAN(TBET1)
GO TO 2
1 CBET1 = 1.0 / TAN(B1) / (1. - FL)
BET1 = ATAN(1. / CBET1)
2 CONTINUE
ALL1 = AL2 - AL1
IF (AL2 - AL1 .EQ. 0.) 8, 9
8 ALL2 = 0.
GO TO 3
9 CONTINUE
ALL2 = AL2 - AL1 - SIGN (TPI, AL2 - AL1)
3 IF (ABS(ALL1) .GT. ABS(ALL2)) 5, 6
5 ALL = ALL2
GO TO 7
6 ALL = ALL1
7 CONTINUE
12 IF (ABS(ALL) .EQ. 0. .OR. ABS(ALL) .EQ. PI .OR. ABS(ALL) .EQ. TPI)
1 10, 11
10 ALL = ABS(ALL)
11 CONTINUE
IF (ABS(B2) .GT. PI4) GO TO 16
TBET2 = TAN(B2) * (1. - FL)
BET2 = ATAN(TBET2)
GO TO 17
16 CBET2 = 1.0 / TAN(B2) / (1. - FL)
BET2 = ATAN(1. / CBET2)
17 CONTINUE
CBET1 = COS(BET1)
SBET1 = SIN(BET1)
CBET2 = COS(BET2)
SBET2 = SIN(BET2)
A = SBET1 * SBET2
B = CBET1 * CBET2
AB = SBET1 * CBET2
BA = SBET2 * CBET1
COSL = COS(ALL)
SINL = SIN(ALL)
CPHI = A + B * COSL
SPHI = SQRT ((SINL * CBET2)**2 + (BA - AB * COSL)**2)
IF (SPHI .GE. 0. .AND. CPHI .GE. 0.) 20, 21

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20 PHI = ASIN(SPHI)
   IF (SPHI .GT. CPHI) PHI = ACOS(CPHI)
   GO TO 30
21 IF (SPHI .GE. 0. .AND. CPHI .LE. 0.) 22, 23
22 PHI = PI - ASIN(SPHI)
   IF (SPHI .GT. ABS(CPHI)) PHI = ACOS(CPHI)
   GO TO 30
23 IF (SPHI .LT. 0. .AND. CPHI .LT. 0.) 24, 25
24 PHI = PI - ASIN(SPHI)
   IF (ABS(SPHI) .GT. ABS(CPHI)) PHI = TPI - ACOS(CPHI)
   GO TO 30
25 IF (SPHI .LT. 0. .AND. CPHI .GE. 0.) 26, 27
26 PHI = TPI + ASIN(SPHI)
   IF (ABS(SPHI) .GT. CPHI) PHI = TPI - ACOS(CPHI)
   GO TO 30
27 CALL EXIT
30 CONTINUE
   C = B * SINL / SPHI
   FL2 = FL * FL
   CON1 = FL + FL2
   CON2 = 0.5 * FL2
   CON3 = SPHI * CPHI
   CON4 = PHI**2 / SPHI
   CON5 = CON4 * CPHI
   EM = 1. - C * * 2
   RATIO1 = (1. + CON1) * PHI + A * (CON1 * SPHI - CON2 * CON4)
1 + EM * (-0.5 * CON1 * (PHI + CON3) + CON2 * CON5) - A * A * CON2
2 * CON3 + EM * EM * CON2 * (0.125 * (PHI + CON3) - CON5 - 0.25 *
3 CON3 * CPHI**2) + A * EM * CON2 * (CON4 + CON3 * CPHI)
   S = RATIO1 * B0
   IF (S .LE. 1.E-4) S = 0.
   RATIO2 = CON1 * PHI - A * CON2 * (SPHI + 2. * CON4)
1 + 0.5 * EM * CON2 * (-5.0 * PHI + CON3 + 4.0 * CON5)
   ALAM = RATIO2 * C + ALL
   SALAM = SIN(ALAM)
   CALAM = COS(ALAM)
   CTAZ12 = BA - CALAM * AB
   CTAZ21 = BA * CALAM - AB
   IF (AL1 - AL2 .EQ. 0.) 35, 39
35 AZ12 = 0.
   AZ21 = 0.
   GO TO 34
39 CTAZ12 = CTAZ12 / (SALAM * CBET2)
   IF (CTAZ12 .EQ. 0.) 54, 55
54 AZ12 = PI2
   GO TO 56
55 CONTINUE
   AZ12 = ATAN(1. / CTAZ12)
56 CONTINUE
   CTAZ21 = CTAZ21 / (SALAM * CBET1)
   IF (CTAZ21 .EQ. 0.) 57, 58
57 AZ21 = PI2
   GO TO 34
58 CONTINUE
   AZ21 = ATAN(1. / CTAZ21)
34 CONTINUE
   IF (ALL .GE. 0. .AND. CTAZ12 .GE. 0.) 40, 41

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40 AZ12 = AZ12
   GO TO 50
41 IF (ALL .GE. 0. .AND. CTAZ12 .LT. 0.) 42, 43
42 AZ12 = PI + AZ12
   GO TO 50
43 IF (ALL .LT. 0. .AND. CTAZ12 .GE. 0.) 44, 45
44 AZ12 = PI + AZ12
   GO TO 50
45 AZ12 = TPI + AZ12
50 IF (ALL .GE. 0. .AND. CTAZ21 .GE. 0.) 46, 47
46 AZ21 = PI + AZ21
   GO TO 51
47 IF (ALL .GE. 0. .AND. CTAZ21 .LT. 0.) 48, 49
48 AZ21 = TPI + AZ21
   GO TO 51
49 IF (ALL .LT. 0. .AND. CTAZ21 .GE. 0.) 52, 53
52 AZ21 = AZ21
   GO TO 51
53 AZ21 = PI + AZ21
51 CONTINUE
   AZ12 = AMOD(AZ12, TPI)
   IF (AZ12 .LT. 0.) AZ12 = AZ12 + TPI
   AZ21 = AMOD(AZ21, TPI)
   IF (AZ21 .LT. 0.) AZ21 = AZ21 + TPI
   RETURN
   END

```

```

SUBROUTINE SETUP
COMMON /GENERAL/TPI, PI, PI2, PI4, A0, B0, FL, ESQ, IFLAG
DATA (TPI=6.28318530717959)
PI = TPI / 2.0
PI2 = TPI / 4.0
PI4 = TPI / 8.0
C-----A0=SEMI MAJOR AXIS OF CLARKE SPHEROID OF 1866, METERS
C-----B0=SEMI MINOR AXIS OF CLARKE SPHEROID OF 1866, METERS
A0 = 6.3782064E+6
B0 = 6.3565838E+6
C-----FL=SPHEROIDAL FLATTENING
C-----ESQ=SECOND ECCENTRICITY SQUARED
FL = 1.0 - B0 / A0
ESQ = (A0 ** 2 - B0 ** 2) / B0 ** 2
IFLAG = 0
RETURN
END

```

```

FUNCTION OMCOS(X)
C OMCOS(X)= 1 - COS(X)
IF (ABS(X) .GT. .15) GO TO 40
IF (X .EQ. 0.) GO TO 50
S = X * X
OMCOS = T = .5 * S
R = 4.
10 T = - T * S / (R * (R - 1.))
OMCOS = OMCOS + T
IF (T / OMCOS .LE. .5E-9) GO TO 51
R = R + 2.
GO TO 10
40 OMCOS = 1. - COS(X)
RETURN
50 OMCOS = 0.
51 RETURN
END

```

```

SUBROUTINE INT (I,K)
C I = POSITION IN X AND Z ARRAYS ON WHICH TO CENTER CALCULATIONS
C K = POSITION IN ARRAYS Z AND ZP TO STORE CALCULATED VALUES
COMMON /GROUND/ ZDUM,Z,ZPDUM,ZP,XDUM,X,R0,DEN,R,U,OMX,WAVE,R2,ZPP
1,D,DDD1,DDD2
COMPLEX DEN,D,DDD1,DDD2
DIMENSION ZDUM(6),Z(1009),ZPDUM(6),ZP(1009),XDUM(6),X(1009)
IMO=I-1
IPO=I+1
C=((Z(IPO)-Z(IMO))-(Z(I)-Z(IMO))*(X(IPO)-X(IMO))/(X(I)-X(IMO)))/
1 ((X(IPO)*X(IPO)-X(IMO)*X(IMO))-X(I)*X(I)-X(IMO)*X(IMO))*
2 (X(IPO)-X(IMO))/(X(I)-X(IMO)))
B=((Z(I)-Z(IMO))-C*(X(I)*X(I)-X(IMO)*X(IMO)))/(X(I)-X(IMO))
A=Z(I)-X(I)*(B+C*X(I))
Z(K)=A+X(K)*(B+C*X(K))
ZP(K)=B+2.*C*X(K)
ZPP=2.*C
RETURN
END

```

```

SUBROUTINE CNEVKEN(A, FA, NA, X, FX, NX, NPT, KASE)
COMPLEX FA, FX, FUNCT, POLY
DIMENSION A(NA), FA(NA), X(NX), FX(NX), FUNCT(15), ABSC(15), DIF(1
15), POLY(15)
1 FORMAT (1H1/50H THE X VALUES ARE NOT ARRANGED IN ASCENDING ORDER./
1/5X,4HI = E20.9,5X,7HX(I) = E20.9,5X,4HJ = E20.9,5X,7HA(J) = E20.9
2///14X,1HX,20X,4HF(X))
2 FORMAT (5X,2E20.9)
200 FORMAT (1H1* THERE ARE NOT ENOUGH POINTS IN THE GIVEN ARRAY.*)
205 FORMAT (1H1* THE GIVEN VALUE OF NPT WAS GREATER THAN NA.*/* THE SU
1BROUTINE REDUCED NPT TO WITHIN THE LIMITS OF NA.*)
210 FORMAT (1H1* NPT WAS INITIALLY GREATER THAN 15 - NPT =15.*/* THE S
1UBROUTINE SET NPT TO 15 AND CONTINUED.*)
LOOP = 1
IF (NPT - 15) 3, 3, 9
9 PRINT 210, NPT
NPT = 15

```

```

3 IF (NPT - NA) 8, 8, 4
4 NPT = NPT - 2
  IF (NPT - 1) 5, 5, 6
5 PRINT 200
  CALL EXIT
6 GO TO (7, 3), LOOP
7 LOOP = 2
  PRINT 205
  GO TO 3
8 NPT2 = NPT / 2
  GO TO (11, 12), KASE
11 NSTART = 1
  MX = 1
  GO TO 16
12 NSTART = NA - 3
  TEST = A(NSTART) + (A(NSTART + 1) - A(NSTART)) / 2
  IF (MX .LT. 1) GO TO 170
  DO 14 I = 1, MX
  IF (X(I) - TEST) 14, 14, 13
13 MX = I
  GO TO 16
14 CONTINUE
170 CONTINUE
16 NSTOP = NA - 1
  IF (NX .LT. MX) GO TO 175
  DO 125 I = MX, NX
  IF (X(I) - A(1)) 135, 15, 10
10 IF (X(I) - A(NA)) 25, 20, 130
15 FX(I) = FA(1)
  GO TO 125
20 FX(I) = FA(NA)
  GO TO 125
25 IF (NSTOP .LT. NSTART) GO TO 180
  DO 85 J = NSTART, NSTOP
  IF (X(I) - A(J)) 32, 35, 30
30 IF (X(I) - A(J + 1)) 45, 40, 85
32 II = I - 1
  PRINT 1, I, X(I), J, A(J)
  IF (II) 34, 34, 33
33 PRINT 2, (X(N), FX(N), N = 1, II)
34 CALL EXIT
35 FX(I) = FA(J)
  NSTART = J
  GO TO 125
40 FX(I) = FA(J + 1)
  NSTART = J + 1
  GO TO 125
45 NSTART = J
  IF (ABS(X(I) - A(J)) - ABS(X(I) - A(J + 1))) 50, 50, 55
50 JJ = J
  GO TO 60
55 JJ = J + 1
  GO TO 60
85 CONTINUE
180 CONTINUE
60 IF (JJ - NPT2) 135, 135, 70
70 IF (JJ + NPT2 - NA) 80, 80, 130
80 KK = JJ - NPT2 - 1

```

```

90 IF (NPT .LT. 1) GO TO 185
   DO 95 K = 1, NPT
   KK = KK + 1
   FUNCT(K) = FA(KK)
   ABSC(K) = A(KK)
95 DIF(K) = ABSC(K) - X(I)
185 CONTINUE
   NTOP = NPT - 1
   LL = 1
100 IF (NTOP .LT. 1) GO TO 190
   DO 105 L = 1, NTOP
   LLL = L + LL
105 POLY(L) = (FUNCT(L) * DIF(LLL) - FUNCT(L + 1) * DIF(L)) / (ABSC(LL)
1L) - ABSC(L))
190 CONTINUE
   IF (NTOP - 1) 120, 120, 110
110 DO 115 M = 1, NTOP
115 FUNCT(M) = POLY(M)
   NTOP = NTOP - 1
   LL = LL + 1
   GO TO 100
130 INC = - 1
   KK = NA + 1
   GO TO 140
135 INC = 1
   KK = 0
140 IF (NPT .LT. 1) GO TO 215
   DO 145 K = 1, NPT
   KK = KK + INC
   FUNCT(K) = FA(KK)
   ABSC(K) = A(KK)
145 DIF(K) = ABSC(K) - X(I)
215 CONTINUE
   NTOP = NPT - 1
   LL = 1
150 IF (NTOP .LT. 1) GO TO 220
   DO 155 L = 1, NTOP
   LLL = L + LL
155 POLY(L) = (FUNCT(1) * DIF(LLL) - FUNCT(L + 1) * DIF(LL)) / (ABSC(L
1LL) - ABSC(LL))
220 CONTINUE
   IF (NTOP - 1) 120, 120, 160
160 DO 165 M = 1, NTOP
165 FUNCT(M) = POLY(M)
   NTOP = NTOP - 1
   LL = LL + 1
   GO TO 150
120 FX(I) = POLY(1)
125 CONTINUE
175 CONTINUE
   RETURN
   END

```

```

COMPLEX FUNCTION FLEAF(WAVE, H1, H2, XD, DELTAR)
COMPLEX TEMP, Q, Z, ZZ, ZZ, HWERF, WERFZ, WERF, ZWERF, DELTAR
HD = H2 - H1
TEMP = (0.7071067812, - 0.7071067812) * SQRT(.5 * WAVE)
XD2 = SQRT(XD)
Q = - TEMP * HD / XD2
Z = TEMP * DELTAR * XD2 + Q
ZZ = - Z
ZI = AIMAG(ZZ)
IF (ZI .LT. 0. .OR. (ABS(REAL(ZZ)) .LT. 6. .AND. ZI .LT. 6.)) GO T
10 10
ZZ = ZZ * * 2
HWERF = (ZZ - 2.) / (ZZ * (ZZ - 3.5))
GO TO 12
C WERF - COMPLEMENTARY ERROR FUNCTION
10 WERFZ = WERF(ZZ)
HWERF = ZZ - 0.5 * WERFZ / (ZZ * WERFZ + (0., - 0.56418958))
12 ZWERF = Z + HWERF
FLEAF = (Q * ZWERF - 0.5) / (Z * ZWERF - 0.5)
RETURN
END

```

```

COMPLEX FUNCTION WERF(ZZZ)
COMPLEX Z, ZZZ, ZV, V, Z2, C, W, S
DIMENSION C(12), W(5, 4)
EQUIVALENCE (S, C(12))
DATA (C(1) = (.0, - .5641895835))
DATA W/(1.,0.0),
1 (3.678794411714423E-01,6.071577058413937E-01),
2 (1.831563888873418E-02,3.400262170660662E-01),
3 (1.234098040866788E-04,2.011573170376004E-01),
4 (1.125351747192646E-07,1.459535899001528E-01),
5 (4.275835761558070E-01,0.000000000000000E+00),
6 (3.047442052569126E-01,2.082189382028316E-01),
7 (1.402395813662779E-01,2.222134401798991E-01),
8 (6.53177728904697E-02,1.739183154163490E-01),
9 (3.628145648998864E-02,1.358389510006551E-01),
A (2.553956763105058E-01,0.000000000000000E+00),
B (2.184926152748907E-01,9.299780939260186E-02),
C (1.479527595120158E-01,1.311797170842178E-01),
D (9.271076642644332E-02,1.283169622282615E-01),
E (5.968692961044590E-02,1.132100561244882E-01),
F (1.790011511813930E-01,0.000000000000000E+00),
G (1.642611363929861E-01,5.019713513524966E-02),
H (1.307574696698522E-01,8.111265047745472E-02),
I (9.640250558304439E-02,9.123632600421258E-02),
J (6.979096164964750E-02,8.934000024036461E-02)/
XX = REAL(ZZZ)
YY = AIMAG(ZZZ)
X = ABS(XX)
Y = ABS(YY)
Z = CMPLX(X, Y)
LZZ = 0
IF (X .GE. 4.5 .OR. Y .GE. 3.5) GO TO 100
I = X + .5
J = Y + .5
V = CMPLX(FLOAT(I), FLOAT(J))

```

```

ZV = Z - V
C(2) = W(I + 1, J + 1)
AI = 0.
DO 10 I = 3, 12
AI = AI - .5
C(I) = (V * C(I - 1) + C(I - 2)) / AI
10 CONTINUE
J = 12
DO 11 I = 2, 11
J = J - 1
11 S = S * ZV + C(J)
20 IF (YY .GE. 0.) GO TO 30
IF (LZ2 .EQ. 0) Z2 = Z * Z
S = 2. * CEXP(- Z2) - S
IF (XX .GT. 0.) S = CONJG(S)
GO TO 200
30 IF (XX .LT. 0.) S = CONJG(S)
200 WERF = S
RETURN
LZ2 = 1
Z2 = Z * Z
S = Z * ((0., 0.4613135279) / (Z2 - 0.1901635092) + (0., 0.0999921
16168) / (Z2 - 1.7844927485) + (0., 0.0028838938748) / (Z2 - 5.5253
24374379))
GO TO 20
END

```

```

FUNCTION CANG(Z)
COMPLEX Z
DATA (PI=3.14159265358979), (PIHA=1.57079632679489)
X=REAL(Z)
Y=AIMAG(Z)
IF (X) 20,30,10
10 CANG=ATAN2(Y,X)
RETURN
20 IF (Y.NE.0.) GO TO 10
CANG=PI
RETURN
30 IF (Y.GT.0.) GO TO 40
IF (Y.LT.0.) GO TO 50
CANG=0.
RETURN
40 CANG=PIHA
RETURN
50 CANG=-PIHA
RETURN
END

```



```

SUBROUTINE INDF (HH,XX,NUT,F)
C THIS SUBROUTINE CALCULATES THE INDUCTION FIELDS FOR E SUB R AND
C H SUB PHI
C THESE INDUCTION FIELDS ARE FOR POSITIVE TIME FUNCTION
C NUT = 1 GIVES INDUCTION FIELD FOR E SUB R (TAU BAR)
C NUT = 0 GIVES INDUCTION FIELD FOR H SUB PHI (LOOP)
C FZ = INDUCTION FIELD FOR E SUB R
C FH = INDUCTION FIELD FOR H SUB PHI
COMMON/INDUCT/WAVE
DOUBLE THETAD,SINTH,COSTH,R,CONS
COMPLEX GZ,FZ,FH,F
A=6.36739 E6
TPI=6.283185307
C=2.997925E8
IF (XX.LE.0.)3,4
3 PRINT 5
5 FORMAT (//'* IN INDF, DISTANCE IS ZERO OR NEGATIVE, XX = *,E20.10)
CALL EXIT
4 THETAD=1.08*XX/A
SINTH=OSIN(THETAD)
COSTH=DCOS(THETAD)
R=A+HH
CONS=A*R*SINTH**2
D2=R*R+A*A-2.*A*R*COSTH
IF (D2.GT.0.) GO TO 30
DD=XX
D2=XX*XX
GO TO 40
30 CONTINUE
DD=SQRT(D2)
40 CONTINUE
D3=DD*D2
D4=D2*D2
FZR=-2.*COSTH/DD+3.*CONS/D3
FZI=(WAVE*CONS+2.*COSTH/WAVE)/D2-3.*CONS/(D4*WAVE)
FZ=CMPLX(FZR,FZI)
GZ=CMPLX(0.,WAVE)
FZ=FZ/GZ
FHR=R*SINTH*DD/D3
FHI=WAVE*R*SINTH*DD/D2
FH=CMPLX(FHI,-FHR)
C1=2.E-7*TPI*WAVE*C
FH=FH/C1
IF (NUT)1,2
1 F=FZ
RETURN
2 F=FH
RETURN
END

```

### 3.7 Sample Test Run

A typical data output listing is illustrated below. The transmitter coordinates which are read in from the data card deck are printed for verification purposes. The geographic coordinates of the desired target or receiver are next listed. Array data used in the calculations are then printed. TOA is the travel time from transmitter to receiver in  $\mu$ sec and recorded in order of master, slave 1 and slave 2 to

target respectively. TD1 and TD2 are the final desired LORAN coordinates in  $\mu\text{sec}$ . ED1 and ED2 are the slave emission delays in  $\mu\text{sec}$  obtained from the transmitter card input data. Additional output data recorded as TOA above include:

- DISTDUM - Calculation of distance by Hufford's technique in KM.
- TIMDUM - Calculation of secondary phase factor in  $\mu\text{sec}$ .
- DISTSOD - Calculation of distance by Sodano technique in KM.
- TPW - Travel time of primary wave in  $\mu\text{sec}$ .

### 3.8 Output Listing

#### TRANSMITTER COORDINATES

LOCATION	LATITUDE (DEG-MIN-SEC)	LONGITUDE (DEG-MIN-SEC)
MASTER	49 36 18.813N	7 19 38.276E
SLAVE1	53 39 13.867N	8 43 47.518E
SLAVE2	48 15 48.929N	11 37 49.283E

#### RECEIVER COORDINATES

LOCATION	LATITUDE (DEG-MIN-SEC)	LONGITUDE (DEG-MIN-SEC)
RECEIVER 5	50 31 28.176N	8 37 4.102E

.1000000E+03	ARRAY(1) = FKHZ = FREQUENCY IN KHZ
.1000738E+01	ARRAY(2) = ETA = AIR INDEX OF REFRACTION AT GROUND
.3751278E+03	ARRAY(3) = DMAX = MAXIMUM DISTANCE BETWEEN TRANSMITTER
.9576124E+00	ARRAY(4) = DINC = DISTANCE INCREMENT IN KM
.5000000E+01	ARRAY(5) = NSTART = INDEX OF THE FIRST DISTANCE AT
.1000000E+01	ARRAY(6) = NZINC = THE FIELD IS TO BE FOUND AS A DISTANCE ARRAY -- NZINC MUST NEVER BE
.3770000E+03	ARRAY(7) = INDEX OF THE LAST DISTANCE AT WHICH THE
.3000000E+04	ARRAY(8) = ZMIN = THE MINIMUM ALTITUDE ABOVE THE
.1000000E+02	ARRAY(9) = ZINC = THE ALTITUDE INCREMENT, METERS
.3000000E+04	ARRAY(10) = ZMAX = THE MAXIMUM ALTITUDE, METERS
.1000000E+04	ARRAY(11) = FLAT = THE FACTOR USED IN THE FLAT EARTH
.8500000E+00	ARRAY(12) = ALPHA = VERTICAL LAPSE FACTOR
.7491047E+07	ARRAY(13) = EFFECTIVE EARTH'S RADIUS
.1000000E+01	ARRAY(14) = NUT

#### \*NAME

TOA = .46076707956884E+03, .11637208385365E+04, .11131957971839E+04,  
 TD1 = .17240373758968E+05,  
 TD2 = .26816538717615E+05,  
 ED1 = .1753742E+05,  
 ED2 = .2516411E+05,

DISTOUM = .1278157184542E+03, .74820668121801E+03, .33720253518828E+03, ---  
 TIMDUM = .1625023417869E+01, .16712490183059E+01, .14213513311794E+01, ---  
 DISTOUM = .17791220274207E+03, .34828544025989E+03, .33719366550172E+03, ---  
 IRW = .45984810567518E+03, .11621486261008E+04, .111475173217.3E+06, ---  
 \*END

END OF INPUT DATA.

#### 4. DESCRIPTION OF PART II

##### 4.1 Overview

The electrical properties of the earth are converted into a ground surface impedance in PART II of the program as shown in Figure 7. The data on the input tapes from PART I are loaded on to a disc so that at each index point information on terrain, geology, and soil is available. This information is employed to develop a 3-layer model of the ground as shown in Figure 8. The time of arrival of the LORAN pulse at the receiver is controlled by the electrical characteristics of this model through a parameter called the surface impedance. This parameter is the ratio of the horizontal components of the electrical to the magnetic field components assuming the ground is isotropic; the calculation of this parameter is described by Johler.<sup>12, 13</sup>

The development of the 3-layer ground model requires additional investigation, in particular, the constants to be used in the postulated second or saturated layer. The electrical characteristics of ground or other medium may be expressed by three constants, the relative permeability, the dielectric constant, and the conductivity. The relative permeability can normally be regarded as unity. From the digitized data from PART I, the conductivity of the top unsaturated ground or soil and basement rock can be determined.<sup>14, 15, 16, 17, 18</sup> Most soil maps also contain information on top soil depth which is included in the look-up table. The rock depth is assumed to be infinite since the 100 kHz wave does not penetrate below 300 meters. The conductivity and depth of the second layer are somewhat uncertain and various articles in the journal titled *Geoexploration*<sup>19, 20</sup> have been used to obtain information on second layer parameters as a function of the top layer. The values listed in Figure 8 are suitable for Europe. In Iran, for example, sigma 2 is larger than sigma 1. The dielectric constant has been selected as 15 over land and 80 over water. An empirical relationship between conductivity and dielectric constant has been developed by Hanle,<sup>21</sup> and may also be used in the

---

Due to the large number of references on this page, the references will not be footnoted. See References, page 84.

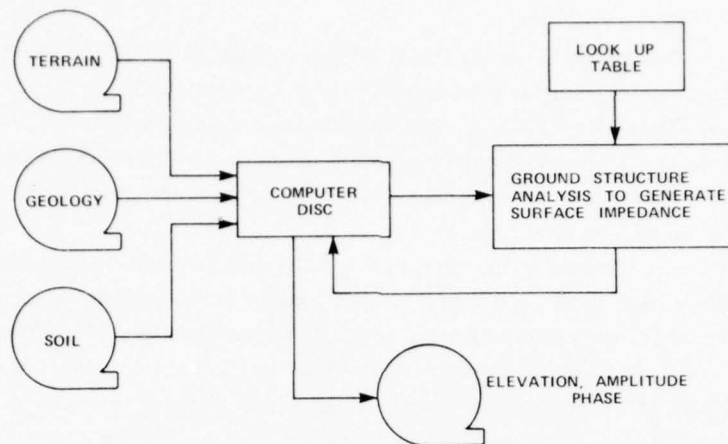


Figure 7. Data Base of Ground Electrical Properties - Part II

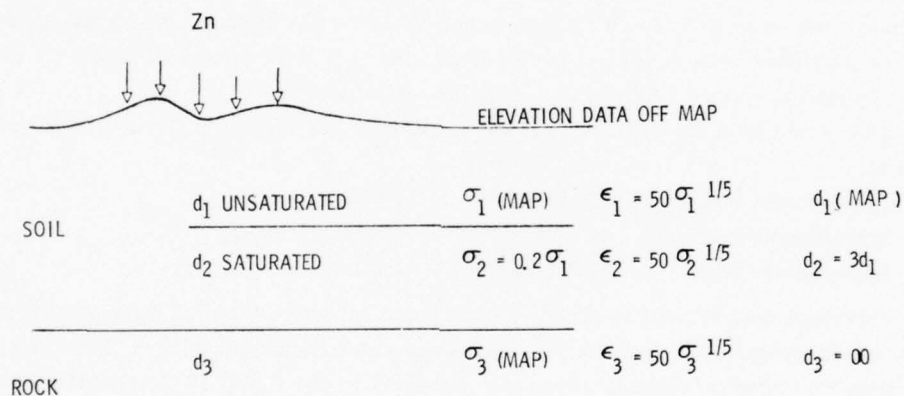


Figure 8. Ground Model for Surface Impedance Calculators

program. The effects of temperature changes, vegetation, buildings, and other objects on the surface of the earth have not been considered.

The input data to PART II is on a standard one-half inch, 400-foot magnetic tape containing information on elevation in meters, bedrock, and soil identification number. The input format for the data is as follows:

Elevation - 11 bits -  $\pm 7$  meters  
 Blank - 3 bits  
 Rock Number - 8 bits - 256 types  
 Blank - 2 bits  
 Soil Number - 6 bits - 64 types

This totals to a 30-bit data word. Each CDC word contains 60 bits, therefore, two data words or points can be accommodated by a single CDC word. For 30-bit word computers (IBM 360, UNIVAC, Honeywell), one data point will be accommodated by each word allowing flexibility between machines. There are 60 words in each record or  $2 \times 60 = 120$  data points. With a 30 arc second grid, each record covers one degree in latitude of the grid.

The data is recorded on to the tape in the following sequence: Starting at  $6^\circ$  E Long,  $48^\circ$  N Lat, in the southwest corner and go north for one degree in latitude (one record), then repeat for an equal line incremented in longitude, parallel and 30 arc seconds to the east of the first line. This is repeated until the last longitude line of the two degree standard longitude sectors is reached. For this particular problem, this would mean after  $2 \times 60 \times 2 = 240$  records. The latitude is then incremented by one degree, returned to the original longitude, and the entire process repeated for another 240 records. At the east edge of the final latitude sector ( $53^\circ$  to  $54^\circ$ ), the pointer returns to  $8^\circ$  N Lat and begins another  $1^\circ$  latitude scan from  $8^\circ$  E to  $10^\circ$  E longitude. For the six degree latitude and eight degree longitude area coverage in Germany, there will be a total of  $960 \times 6 = 5760$  records which contain  $5760 \times 120 = 691,200$  data points.

The output data tape of PART II which is the input to PART III has the following format:

Elevation in meters	- $\pm 7$ meters	- 11 bits
Impedance Amplitude	- $\pm 2$ ohms	- 8 bits
Impedance Phase	- $\pm .001$ radians	- 11 bits

The elevation data is passed directly from input to output tape. The output impedance is returned to the disc for storage in the same location as the original data and then recorded on magnetic tape for shipment to the PART III computation sites.

#### 4.2 Subroutine Description

##### 4.2.1 PROGRAM CONIMP

- (a) Controls impedance program.
- (b) Call subroutine SETUP.
- (c) Reads and writes on disc soil, geology and elevation identification data off input tapes.
- (d) Call subroutine REPK.
- (e) Writes impedance data on disc and output tape.

##### 4.2.2 SUBROUTINE SETUP

- (a) Sets relative permeability of three layers to unity.
- (b) Reads and stores ground conductivity tables from input cards into look-up file.

#### 4.2.3 SUBROUTINE REPK

- (a) Determine parameters for 3-layer ground surface impedance.
  - (1) Dielectric constant equals fifteen overland and eighty over
  - (2) Determine depth of first and second layer. Set third layer to infinity.
  - (3) Set sigma 2 as a function of sigma 1.
- (b) Call subroutine GRIM for impedance calculation.

#### 4.2.4 SUBROUTINE GRIM

- (a) Calculates surface impedance for 3-layer ground model.
- (b) Returns complex impedance (AMP, FAZ) to subroutine RFPK via argument list.

#### 4.3 Resistivity Tables

For subroutine SETUP, a look-up table is required to convert type of soil and rock into resistivity values. The bibliography at the end of this section lists available sources for these values. Table 1 is a list of average values for the top or unsaturated soil. An approximate value is usually assigned in the map legend.

An inspection of the geological map of Europe reveals characteristic rock types which include anorthosite, granite gneiss, gabbro, Precambrian igneous, and metamorphic rock. The associated resistivities for various rock types are defined in Table 2.

Table 1. Ground Resistivity Values for Typical Soils

Terrain	Conductivity (mhos-meter)	Resistivity (meter-ohms)
Sea water	5	0.2
Fresh water	$8 \times 10^{-3}$	123
Dry, sandy, flat coastal land	$2 \times 10^{-3}$	500
Marshy, forested flat land	$8 \times 10^{-3}$	123
Rich agricultural land, low hills	$1 \times 10^{-2}$	1,000
Pastoral land, medium hills and forestation	$5 \times 10^{-3}$	200
Rocky land, steep hills	$2 \times 10^{-3}$	500
Mountainous	$1 \times 10^{-3}$	1,000
Cities, residential areas	$2 \times 10^{-3}$	500
Cities, industrial areas	$1 \times 10^{-4}$	1,000

Table 2. Rock Types and Resistivities

Principle Geologic Age	Secondary Geologic Age	Principle Rock Type	Secondary Rock Types	Effective Resistivity Meter-ohms		
				min	max	mean
Precambrian		Gneisses, Granities, etc.		1,000	14,000	
Precambrian		Gneisses, Granites, etc.	Alluvium			200
Precambrian	Cambrian	Gneisses, Granites, etc.	Slate	400	7,000	1,500
Precambrian	Cambrian	Gneisses, Granities, etc.	Sandstone	1,000	5,000	2,200
Precambrian	Cambrian & Ordovician	Gneisses, Granities, etc.	Quartzite & Limestone	1,000	2,000	1,800
Precambrian	Cambrian & Ordovician	Gneisses, Granities, etc.	Limestone	65	180	140
Cambrian	Ordovician	Sandstone	Limestone & Shale	50	140	100
Cambrian	Ordovician Silurian Carboniferous	Sandstone	Limestone	150	480	300
Ordovician		Shale		55	70	65
Ordovician	Silurian Devonian	Sandstone	Limestone Shale	170	380	200
Ordovician	Silurian Devonian	Limestone	Shale			20

Table 2. Rock Types and Resistivities (Cont.)

Principle Geologic Age	Secondary Geologic Age	Principle Rock Type	Secondary Rock Types	Effective Resistivity Meter-ohms		
				min	max	mean
Ordovician	Carboniferous	Sandstone	Limestone & Shale	62	90	75
Cambrian	Ordovician	Sandstone	Limestone, Shale, Alluvium			6
Cambrian	Ordovician	Limestone	Shale	170	300	200
Cambrian	Ordovician Silurian	Sandstone	Limestone & Shale	38	180	130
Cambrian	Ordovician Carboniferous	Sandstone	Limestone & Shale	250	310	280
Cambrian	Ordovician Silurian Carboniferous	Sandstone	Limestone & Shale	350	605	480
Ordovician	Silurian, Devonian & Carboniferous	Sandstone	Limestone & Shale	71	105	100
Ordovician	Triassic	Sandstone	Limestone & Shale	170	270	205
Silurian	Devonian	Limestone		55	70	62
Silurian	Devonian	Limestone		62	84	72
Silurian	Devonian	Sandstone	Limestone & Shale	290	440	350
Devonian		Sandstone	Shale	200	400	290



Table 2. Rock Types and Resistivities (Cont.)

Principle Geologic Age	Secondary Geologic Age	Principle Rock Type	Secondary Rock Types	Effective Resistivity Meter-ohms		
				min	max	mean
Devonian	Carboniferous	Sandstone	Shale	19	34	29
Carboniferous		Sandstone	Shale			20
Carboniferous		Sandstone	Shale			10
Carboniferous		Sandstone	Limestone & Shale	20	40	25
Carboniferous		Limestone	Alluvium			28
Carboniferous		Limestone				2
Carboniferous	Triassic	Sandstone	Limestone	40	44	40
Carboniferous	Cretaceous Tertiary	Sand	Clay Loam			40
Carboniferous	Cretaceous Tertiary	Marl	Sand Clay	22	26	25
Carboniferous	Quaternary	Sand	Shale Alluvium	8	11	10
Triassic		Sandstone	Shale, Trap & Diabase	150	350	250
Cretaceous		Chalk				5.4
Cretaceous		Sandstone	Clay	10	15	13
Cretaceous	Tertiary	Sand	Clay	13	17	17

Table 2. Rock Types and Resistivities (Cont.)

Principle Geologic Age	Secondary Geologic Age	Principle Rock Type	Secondary Rock Types	Effective Resistivity Meter-ohms		
				min	max	mean
Cretaceous	Tertiary Quaternary	Sand	Clay			8
Cretaceous	Tertiary Quaternary	Marl	Sand Clay			10
Tertiary		Sand	Clay			31
Tertiary		Sand	Clay	4.5	7	6
Tertiary		Sand	Clay	5.5	6	6
Tertiary	Quaternary	Sand	Clay			15
Tertiary	Quaternary	Sand	Clay	18	20	19
Quaternary		Sand	Clay	4	8	5

#### 4.4 Program Listing for Part II

##### PROGRAM CONIMP

```

1 PROGRAM CONIMP(TAPE3,TAPE2,INPUT=128,OUTPUT=128)
COMMON/THREE/F,PHI,SIGMA1,E21,AMU1,Z1,SIGMA2,E22,AMU2,Z2,SIGMA3,
.E23,AMU3
COMMON/CODE/SLCD(65,3),G0,GLCD(148)
5 DIMENSION NUPK(60),NDXEQ(5800)
DATA MSK6/77B/,MSKF15/77777000000000000000000B/
LNLN=960$LATLM=6
LNLN=20$LATLM=1
NDXSIZ=LNLN*LATLM+40
10 CALL SETUP
CALL OPENMS(2,NDXEQ,5800,0)
LNLN=5760
DO 100 ILN=1,LNLN
NDXL=ILN
15 BUFFERIN(3,1)(NUPK(1),NUPK(60))$IF(UNIT(3))10,20,30
30 PRINT1,ILN
1 FORMAT(*0 PARITY ERROR*,I9)
10 CONTINUE
IF(MOD(ILN,1440).LT.10)PRINT 9,ILN,NDXL,NUPK(1),NUPK(2)
20 CALL REPK(NUPK,MSK6,MSKF15)
IF(MOD(ILN,1440).LT.10)PRINT 99,NUPK(1),NUPK(2)
IOVER=1
IOVER=0
70 CALL WRITMS(2,NUPK,60,NDXL,IOVER)
25 9 FORMAT(*0 *,2I8,2022)
99 FORMAT(2022)
100 CONTINUE
20 STOP$END

```

##### SUBROUTINE REPK

```

1 SUBROUTINE REPK(NUPK,MSK6,MSKF15)
COMMON/THREE/F,PHI,SIGMA1,E21,AMU1,Z1,SIGMA2,E22,AMU2,Z2,SIGMA3,
.E23,AMU3
COMMON/CODE/SLCD(65,3),G0,GLCD(148)
5 DIMENSION NUPK(60),IAB(120)
DATA MSK8/377B/
MSK30=37770000003777000000B
DO 100 I=1,60
LLEV=NUPK(I).A.MSK30$LEV=SHIFT(LLEV,1)
10 LS2=NUPK(I).A.MSK6$LG2=MSK8.A.SHIFT(NUPK(I),-6)
LS1=MSK6.A.SHIFT(NUPK(I),-30)$LG1=MSK8.A.SHIFT(NUPK(I),-36)
DO 99 I2=1,2$IF(I2.EQ.2)LS1=LS2$IF(I2.EQ.2)LG1=LG2
E23=E22=E21=15.
IF(LS1.EQ.0.OR.LS1.EQ.22.OR.LS1.EQ.12.OR.LG1.GE.146)E22=E21=80.
15 SIGMA1=SLCD(LS1+1,1)
Z1=SLCD(LS1+1,2)*0.75
IF(Z1.LT.2.)Z1=2.
IF(Z1.LT.SLCD(LS1+1,3))Z1=SLCD(LS1+1,3)
IF(SIGMA1.EQ..01)E22=E21=80.

```

```

20      SIGMA2=0.5*SIGMA1$Z2=4.*Z1
        IF (E22.EQ.89.)SIGMA2=SIGMA1
        ILAT=2*I+I2-2
        SIGMA3=GLCD(LG1)$CALLGRIM(AMP,FAZ)$IAMP=AMP$IFAZ=FAZ
        NR=30*(2-I2)
25      99 LEV=OR(SHIFT(IAMP,NB+11),SHIFT(IFAZ,NB),LEV)$NUPK(I)=LEV
        100 CONTINUE$END

```

SUBROUTINE GRIM

```

1      SUBROUTINE GRIM(AMPIMP,FAZIMP)
C-----F IS FREQUENCY IN HERTZ
C-----PHI IS THE ANGLE OF INCIDENCE IN RADIAN
C-----SIGMA1 IS THE CONDUCTIVITY OF THE UNSATURATED SOIL.
5      C-----E21 IS THE DIELECTRIC CONSTANT OF UNSATURATED SOIL.
        C-----Z1 IS THE DEPTH IN METERS OF THE UNSATURATED SOIL)
C-----SIGMA2 IS THE CONDUCTIVITY OF THE SATURATED SOIL.
C-----E22 IS THE DIELECTRIC CONSTANT OF SATURATED SOIL.
C-----Z2 IS THE DEPTH IN METERS OF THE SATURATED SOIL.
10     C-----SIGMA3 IS THE CONDUCTIVITY OF BEDROCK.
        C-----E23 IS THE DIELECTRIC CONSTANT OF BEDROCK.
        C-----ZSOIL IS THE TOTAL DEPTH OF SOIL ABOVE BEDROCK (Z1 + Z2)
        COMPLEX T2N,T2D
        COMPLEX A10, A20, A11, A12, A13, A21, A22, A23, A32, A33,
15     1A34, A42, A43, A44, AK1, AK2, ETA1, ETA2, ETA12, ETA22,
        2ZETA1, ZETA12, ZETA2, ZETA22, TEMP, RENUM, REDEM, RE, PHI,BETA1
        COMPLEX SAV1,SAV2,SAV3,SAV4,SAV5,SAV6
        COMPLEX AK3, FTA3, FTA32, ZETA3, ZERO1, A54, A55, A64,
        1A65,A66, T2, T3N, T3D,T3 , A35, A45, A56
20     COMMON /THREE/ F , PHI , SIGMA1, E21, AMU1, Z1, SIGMA2,
        1E22, AMU2, Z2, SIGMA3, E23, AMU3
        DATA (C = 2.997925F8), (TPI=6.2831853071796)
        DATA( E0 = 8.8541853367321E-12)
        DATA(PI = 3.141592654) , (PI2 = -1.570796327)
25     DATA ISKIP/1/
        IF(ISKIP.EQ.0)GO TO 99
        ISKIP = 0
        ZERO1 = CMPLX (0.,1.)
30     1 COSPHI = COS(PHI)
        SINPHI = SIN(PHI)
        COS2 = COSPHI * COSPHI
        SIN2 = SINPHI * SINPHI
        OMEGA = F * TPI
        ETA0=1.000338
35     AK0=OMEGA/C*ETA0
        OMEGAE = OMEGA * E0
        EPSIL=1.E-15
        10 A10 = CMPLX(-COSPHI, 0.)
        A11 = A10
40     A12 = A13 = A20 = A34 = A35 = CMPLX(-1.,0.)
        A56 = CMPLX(1.,0.)
        A21 = CMPLX (1.,0.)
99     AK2=AK0*CSQRT(CMPLX(E22,-SIGMA2/OMEGAE))
        ETA2 = AK2/AK0

```

```

45      ETA22 = ETA2 * ETA2
      TEMP = ETA22 - SIN2
      ZETA2 = CSQRT (TEMP)
      A44 = ZETA2 * ( SIN2 / (AMU2 * ETA22-SIN2) + 1.) /AMU2
      A45 = -A44
50      AK3 = AK0 * CSQRT (CMPLX(E23, -SIGMA3/OMEGAE))
      ETA3 = AK3 / AK0
      ETA32 = ETA3 * ETA3
      TEMP = ETA32 - SIN2
      ZETA3 = CSQRT (TEMP)
55      A66 = ZETA3 * (SIN2 / (AMU3 * ETA32 -SIN2) + 1.) / AMU3
70      CONTINUE
      AK1 = AK0 *CSQRT( CMPLX (E21, -SIGMA1/ OMEGAE))
20      ETA1 = AK1/AK0
      ETA12 = ETA1 * ETA1
60      TEMP = ETA12 - SIN2
      ZETA1 = CSQRT (TEMP)
      A22 = A23 = -ZETA1 *(SIN2/ (AMU1 * ETA12-SIN2 ) +1.) /AMU1
      A23 = -A23
      BETA1 = AK0 * ZETA1 * Z1*ZERO1
65      30 A32 = CEXP(-BETA1)
      A33 = CEXP(BETA1)
      A42 = A22 * A32
      A43 = A23 * A33
      BETA1 = AK0 * ZETA2 * Z2 * ZERO1
70      A54 = CEXP (-BETA1)
      A55 = CEXP (BETA1)
      A64 = A44 * A54
      A65 = A45 * A55
      T2N=A54*A66-A64*A56
75      T2D=A55*A66-A65*A56
      A1=A2=A3=A4=A9S(SIGMA2-SIGMA3)
      IF(((A1.LT.EPSIL ).AND.(A2.LT.EPSIL )).OR.
1((A3.LT.EPSIL ).AND.(A4.LT.EPSIL )))GO TO 31
      T2=T2N/T2D
80      GO TO 32
31      CONTINUE
      T2=0.
32      CONTINUE
      T3N = (A32 * A44 - A42 * A34) - (A32 * A45 - A42 * A35) * T2
85      T3D = (A33 * A44 - A43 * A34) - (A33 * A45 - A43 * A35) * T2
      A2=A4=ABS(SIGMA2-SIGMA3)
      A1=A3=ABS(SIGMA1-SIGMA2)
      IF(((A1.LT.EPSIL ).AND.(A2.LT.EPSIL )).OR.
1((A3.LT.EPSIL ).AND.(A4.LT.EPSIL )))GO TO 34
90      IF(A1.LT.EPSIL)T3=T2*A32/A33
      IF(A1.GE.EPSIL)GO TO 36
      B1=REAL (T2)
      B2=AIMAG(T2)
      B3=REAL (T3)
      B4=AIMAG(T3)
95      B4=AIMAG(T3)
115     FORMAT(* *,8(E13.5,2X))
36      CONTINUE
      IF(A1.LT.EPSIL)GO TO 35
      T3 = T3N / T3D
100     GO TO 35
34      CONTINUE
      T3=0.
35      CONTINUE
      RENUM = (A10 * A22 - A20 * A12) - (A10 * A23 -A20 * A13) * T3

```

```

105 REDEM = (A11 * A22 - A21 * A12) - (A11 * A23 - A21 * A13) * T3
    RE = RENUM / REDEM
    TEMP = (1. - RE) / (1. + RE)
    PMI = TEMP * COSPHI
    50 AMPIMP = ABS(PMI)
110 FAZIMP = CANG (PMI)
    IF (FAZIMP.LE.PI2) FAZIMP = FAZIMP + PI
    IF (FAZIMP.GE.-PI2) FAZIMP = FAZIMP - PI
    IF (FAZIMP.LT.0.050) FAZIMP=0.050$IF (FAZIMP.GT.1.400) FAZIMP=1.400
    IF (AMPIMP.LT.0.001) AMPIMP=0.001$IF (AMPIMP.GT.0.200) AMPIMP=0.200
115 AMPIMP=1000.*AMPIMP$FAZIMP=1000.*FAZIMP
    IF (FAZIMP.LT.0..OR,AMPIMP.LT.0.)PRINT 1776
    1776 FORMAT(*0 AMP OR PHASE NEGATIVE*)
    RETURN
    END

```

FUNCTION CANG

```

1 FUNCTION CANG(Z)
  C
  C
  C COMPLEX Z
  5 C
  C
  C.....INITIALIZE CANG FOR QUADRANT CORRECTION, GET RE(Z) AND IM(Z), TEST
  C.....X FOR + OR - TO FIND CORRECT HALF-PLANE.....
10 DATA (C = 2.997925E8), (TPI=6.2831853071796)
  PI2 = TPI
  PI = TPI / 2.
  PI02 = TPI / 4
  CANG=0.0
15 X=REAL(Z)
  Y=AIMAG(Z)
  IF (X) 10,50,90
  C.....X .LT. 0.0.....
  10 IF (Y) 20,30,40
  20 CANG=-PI
  GO TO 90
  30 CANG=+PI
  RETURN
  40 CANG=+PI
  GO TO 90
25 C.....X .EQ. 0.0.....
  50 IF (Y) 60,70,80
  60 CANG=-PI02
  RETURN
30 C. . .X=0 AND Y=0 IS REALLY UNDEFINED, BUT IN AGREEMENT WITH CDC WE. . .
  C. . .RETURN A VALUE OF CANG=0.0 . . . . .
  70 CANG=0.0
  RETURN
  80 CANG=+PI02
35 C.....X .GT. 0.0 AND X .GT. 0.9 ADJUSTED FOR CORRECT QUADRANT.....
  90 CANG=ATAN (Y/X) + CANG
  RETURN
  END

```

SUBROUTINE SETUP

```

1  SUBROUTINE SETUP
COMMON/THREE/F, PHI, SIGMA1, E21, AMU1, Z1, SIGMA2, F22, AMU2, Z2, SIGMA3,
.E 23, AMU3
COMMON/ CODE/SLCD(65, 3), G0, GLCD(148)
5  DATA CFW/1.E-2/, CSW/5./, CWG/1.E-2/, CDG/1.E-4/
TPI=8.*ATAN(1.0)$F=1.E5$PHI=80.*(TPI/360.)
AMU1=AMU2=AMU3=1.
DO 1 I=2,65
1  READ 10, SLCD(I,1), SLCD(I,3), SLCD(I,2)
10 10 FORMAT(10X, F10.1, F10.1, F10.1)
DO 2 I=1,19$IB=(I-1)*8+1$IE=IB+7$IF(I.EQ.19) IE=148
2  READ 11, (GLCD(K), K=IB, IE)
11 11 FORMAT(8F10.1)
DO 3 I=2,65
15 3  PRINT 5, I, SLCD(I,1), SLCD(I,2)
3  SLCD(I,1)=1./SLCD(I,1)
5  FORMAT(I5, 2F15.1)
PRINT 6$DO 4 I=1,148$PRINT 5, I, GLCD(I)
4  GLCD(I)=1./GLCD(I)
20 6  FORMAT(*0 GEOLOGY RESISTIVITY*, //)
GLCD(0)=SLCD(1,1)=CFW$SLCD(1,2)=20.
SLCD(1,3)=20.
SLCD(65,1)=CFW$SLCD(65,2)=20.
SLCD(65,3)=20.
25  END

```

5. DESCRIPTION OF PART I

5.1 Overview

The lithology and terrain of the LORAN coverage area are digitized from maps in PART I as illustrated in Figure 9. The required three maps are those which contain information on the type top soil or overburden, type or age of basement rock, and ground elevation above sea level. The first type of information is obtained from soil maps usually published by the country of the interested area. These are colored maps with a legend defining the various types of soil and associated depth. Geological maps are available for most areas of the world and the colored legend indicates the type of rock. Terrain maps with elevation data are readily available for the entire world. Fortunately, these have been previously digitized by the Defense Mapping Agency, and magnetic tapes with this data in proper sequence are available upon official request.

The following equipment was required for data digitization:

- Calculator - HP9830A
- Digitizer - HP9864A
- Cassette Memory - HP9865A

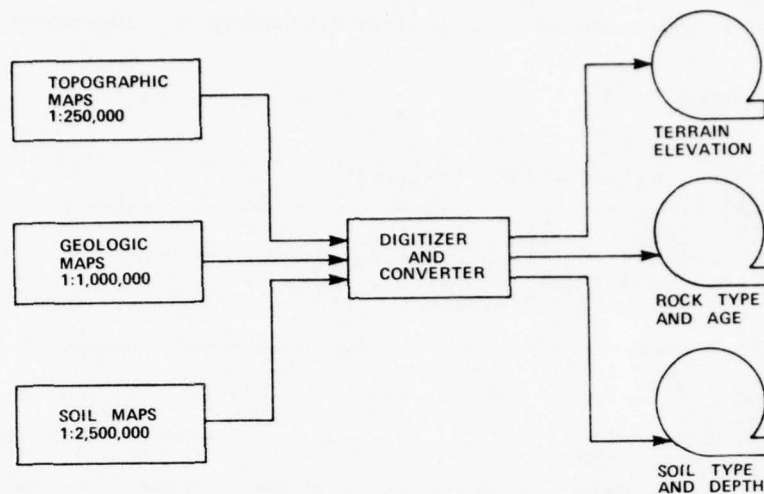


Figure 9. Formation of Data Base - Part I

The maps are digitized by recording, on a cassette tape, the contour table coordinates in inches using the southwest corner as the origin. The cursor cross hairs are moved around each constant color contour and points are generated in increments of one hundred to the inch. The table coordinates and geographic coordinates of the four corner points of the map are recorded for later use in conversion of the former to the latter. These cassette tapes are transcribed onto a disc file by way of the CDC 6600. The merged cassette data is then copied on to a 1/2-in. 2400-ft 800-bpi tape reel. The data on this tape is converted to LAT/LON and color number, and then into scan lines by PROGRAM GGCI. The scan line output format contains 24 bits for longitude, 24 bits for latitude, and 12 bits for color, making up the 60 bit CDC word. These points will then be sorted in PROGRAM SOR with the primary key being the latitude, secondary key the longitude, and tertiary key the color. PROGRAM DECODE sequences the sorted line points into a 30 arc second matrix for the final output tape of PART I. These programs are listed in Section B. Three such magnetic tapes are required, one for each of the ground properties. For a coverage area of 48 square degrees, there will be almost 700,000 data points recorded on each 7-track binary magnetic tape.

The Defense Mapping Agency generates similar data tapes in a program titled "Lineal Data to Terrain Matrix." This program is capable of forming a data matrix from map contour scans with a three arc second to a one minute spacing. By using the standard DMA format as input specification to PART II of the prediction program, DMA and locally generated tapes can be used interchangeably. The



present program is setup for a thirty arc second grid. Changes in this spacing will require changes in the incremental sequencing and storage allocations.

### 5.2 Program Listing for Part I

```

PROGRAM SOR(TAPE3,TAPE2,TAPE4,TAPE1)
9 READ(1) IP
IF(EOF(1))2,1
1 WRITE(2) IP$GO TO 9
2 CONTINUE$REWIND 2$CALL SMSORT(10)
CALL SMFILE("SORT","BINARY",2,"REWIND")
CALL SMFILE("OUTPUT","BINARY",3,"REWIND")
CALL SMKEY(1,1,10,0,"INTEGER")
CALL SMEND
REWIND 3
5 READ(3) IP
IF(EOF(3))4,3
3 WRITE(4) IP
GO TO 5
4 STOP$END
MC60,T150,CM77777,TP2.          2096      M.COMISH
FTN,SL,A,P,BL,R=3,PL=20000.
VSN,TAPE1=0S0139.
REQUEST,TAPE1,HY,L,NR.
VSN,TAPE2=0S0172.
REQUEST,TAPE2,HY,L,RING.
FILE(TAPE2,RT=S,BT=C)
LDSET(FILE=TAPE2)
L60.
PROGRAM DECODE(INPUT,OUTPUT,TAPE6=OUTPUT,TAPE5=INPUT,TAPE1,TAPE2)
COMMON IOUT(721),ICURPT,IMINH,IMAXH,IMINH2,IMAXH2,INFLOO
DIMENSION Y(5001),IC(5001),IOPF(512)
DIMENSION MONE(721),MTHO(721),MSAVE(721)

ISTOP=0
XXDEG=6.
MCASE=1
DO 11 I6=1,721
11 IOUT(I6)=0
I20=513
LEN=512
ITOT=0

XCUR=0.
XCNT=XXDEG
IMINH=0
IMAXH=0
IMINH2=-1000
IMAXH2=-1000
I99H1=-1000
I99H2=-2000
IE2=0
C SKIP TEST DATA
15 IPHASE=1
CONTINUE
IF(IE2.EQ.1) IPHASE=2
J=1
IE=0
IFIRST=1

4 CONTINUE
INFLOO = 0
C 4 IS TO READ IN ANOTHER SCAN LINE
IF(IFIRST.EQ.1) GOTO6
IF(XCUR.LT.(XXDEG-.004)) GO TO 6

C ** -DECODE MODIFICATIONS ... (START)
C ** -MODIFICATIONS (BRUCE HAINES 8/18/76)

```

```

8005 DO 8005 KA=1,721
      MSAVE(KA)=IOUT(KA)
      IF(MCASE.GT.1) GO TO 8010
      DO 8007 KA=1,721
8007 MONE(KA)=IOUT(KA)
      GO TO 8400
8010 IF(MCASE.GT.2) GO TO 8030
      DO 8015 KA=1,721
8015 MTWO(KA)=IOUT(KA)
      GO TO 8250

C          ** -FOR NORPAL SCANS

8030 DO 8100 KA=1,721
      IF(MTWO(KA).EQ.0) GO TO 8050
      IOUT(KA)=MTWO(KA)
      GO TO 8100
8050 IF(IOUT(KA).EQ.0) GO TO 8070
      GO TO 8100
8070 IF(MONE(KA).EQ.0) GO TO 8080
      IOUT(KA)=MONE(KA)
      GO TO 8100
8080 IF(KA.EQ.1) GO TO 8100
      IOUT(KA)=IOUT(KA-1)
8100 CONTINUE
      DO 8105 KA=1,721
      MONE(KA)=MTWO(KA)
      MTWO(KA)=MSAVE(KA)
8105 CONTINUE
      GO TO 8300

C          ** -FOR LAST SCAN LINE ONLY

8170 DO 8200 KA=1,721
      IF(MTWO(KA).EQ.0) GO TO 8180
      IOUT(KA)=MTWO(KA)
      GO TO 8200
8180 IF(MONE(KA).EQ.0) GO TO 8190
      IOUT(KA)=MONE(KA)
      GO TO 8200
8190 IF(KA.EQ.1) GO TO 8200
      IOUT(KA)=IOUT(KA-1)
8200 CONTINUE
      ISTOP=1
      GO TO 8300

C          ** -

C          ** -FOR FIRST SCAN LINE ONLY

8250 DO 8270 KA=1,721
      IF(MONE(KA).EQ.0) GO TO 8255
      IOUT(KA)=MONE(KA)
      GO TO 8270
8255 IF(MTWO(KA).EQ.0) GO TO 8260
      IOUT(KA)=MTWO(KA)
      GO TO 8270
8260 IF(KA.EQ.1) GO TO 8270
      IOUT(KA)=IOUT(KA-1)
8270 CONTINUE

C          ** -

8300 WRITE(6,612) XCURS
612  FORMAT(1X,621.14)
      WRITE(2) XCURS
      WRITE(6,610) IOUT
610  FORMAT(25I4)
      WRITE(2) (IOUT(KLM),KLM=1,721)
8400 XCURS=XCUR
      MCASE=MCASE+1
      IF(ISTOP.EQ.1) STOP
      IF(XCUR.GT.(XXDEG+.991)) GO TO 8170

C          ** -DECODE MODIFICATIONS ... (FINISH)

```

```

6 CONTINUE
XCNT=XCNT+(1./120.)
IF (XCNT.LT.(XCUR+(1./240.))) GOTO 4
IF (IPHASE.EQ.2) GOTO 5
IF (IE?.EQ.1) GOTO 15
5 IF (IE.EQ.1) GOTO 98
DO 9 I5=1,5001
Y(I5)=0.
IC(I5)=0
9 CONTINUE
IF (IFIRST.EQ.1) GOTO 7
XCUR=XNEW
Y(1)=YSAVE
IC(1)=ICSAVE
7 CONTINUE
20 CONTINUE
DO 10 I3=J, 5001
IF (I3.LT.5001) GOTO 2
PRINT 603,XCUR,Y(5000),IC(5000)
603 FORMAT(* ARRAYS Y AND IC TOO SMALL*,2G21.14,I5)
STOP
2 CONTINUE
IF (IPHASE.NE.1) GOTO 31
READ(5,*)XNEW,Y(I3),IC(I3)
IF (EOF(5)) 4,9,32

C READ IN A POINT.
31 CONTINUE
READ(1) IP
IF (EOF(1)) 50,1

1 XNEW=FLOAT(SHIFT(IP,-36))/120.
IF (XNEW.LT.XCUR) GOTO 31
Y(I3)=FLOAT(SHIFT(IP,-12).AND.77777777B)*.001
IC(I3)=IP.AND.7777B
IF (IC(I3).GT.300) GOTO 220
C FOR GLITCHES
IF ((XNEW.LT.5).OR.(XNEW.GT.15)) GOTO 221
IF ((Y(I3).LT.47).OR.(Y(I3).GT.55)) GOTO 221
32 IF (J.EQ.1.AND.I3.EQ.1) XCUR=XNEW
IF (XCJR.NE.XNEW) GOTO 3
IF (I3.EQ.1) GOTO 10
IF (Y(I3).LT.Y(I3-1)) GOTO 302
10 CONTINUE
PRINT 604
604 FORMAT(* ERROR AT 604*)
STOP
98 PRINT*," STMT NO. 98 ENCOUNTERED. FINISHED."
STOP
220 PRINT*," IC.GT.300, PROBABLE GLITCHES."
GOTO 31
221 WRITE(6,2601)
2601 FORMAT(" COORDINATES OUT OF RANGE. PROBABLE GLITCHES.")
GOTO 31
302 WRITE(6,3601)
3601 FORMAT(6(" A POINT OUT OF ORDER"))
Y(I3)=Y(I3-1)
GOTO 10

C INITIALIZATION FOR PROCESSING
50 CONTINUE
PRINT*,"END OF DATA. ITOT=",ITOT
IE=1
C IE=END OF FILE SWITCH
GOTO 1

49 IE2=1
3 CONTINUE
IFIRST=0
I=I3-1
C GO FROM 1 TO L WITH ARRAYS
YSAVE=Y(I3)
ICSAVE=IC(I3)
Y(I3)=0.
IC(I3)=0
J=2
IF (XCJR.LT.(XXDEG-.004)) GO TO 4
C PRINT SCAN LINE

```

```

C BEGIN PROCESSING (FLOWCHART)
C ICURPT IS CURRENT POINT
  ISPI=0
  ISC1=0
  ISC2=0
  ICURPT=1
  ICURCL=IC(ICURPT)
25  CONTINUE
   IF (INFL00.GT.400) GOTO 304
304  GOTO 305
   I3=I3+10
   ISPI=ISPI+10
305  INFL00=0
   CONTINUE
   IF (ABS(Y(ICURPT+1)-Y(ICURPT)).LE..0151) GOTO 51
C IF WITHIN .015, GO TO 51
   GOTO 76
51  IF (IC(ICURPT+1).EQ.ICURCL) GOTO77
   ISPI=0
   GOTO 73
77  CONTINUE
   ICURPT=ICURPT+1
   GOTO 25
76  IF (ICURPT.GE.L) GOTO 4
73  ICURPT=ICURPT+1
   IF (IC(ICURPT).NE.ICURCL) GOTO 45
   CALL FILL(Y(ICURPT-1),Y(ICURPT),IC(ICURPT))
   IF (ABS(Y(ICURPT+1)-Y(ICURPT)).GT..0151) GOTO74
C IF NOT WITHIN .015, GO TO 74
   ICURPT=ICURPT+1
   IF (IC(ICURPT-1).EQ.IC(ICURPT)) GOTO 75
102  ICURCL=IC(ICURPT)
   GOTO 25
75  CONTINUE
   GOTO 102
C
45  CONTINUE
   ISC1=IC(ICURPT)
   IF (ABS(Y(ICURPT+1)-Y(ICURPT)).GT..0151) GOTO78
C IF NOT WITHIN .015, GO TO 78
   GOTO 79
78  IF (ICURPT.GE.L) GOTO 4
   ICURPT=ICURPT-1
   GOTO 74
79  CONTINUE
   ICURPT=ICURPT+1
82  IF (ICURCL.NE.IC(ICURPT)) GOTO 80
   GOTO81
80  CONTINUE
   IF ((I99H1.EQ.I99H2).AND.(I99H2.EQ.ICURPT)) GOTO 105
   I99H1=I99H2
106  I99H2=ICURPT
   IF (ISPI.NE.0) GOTO 83
   ICURPT=ICURPT-1
   ICURCL=IC(ICURPT)
   GOTO25
105  ISPI=ISPI+1
   GOTO 106
83  ICURPT=ISPI
   ICURCL=ISC2
   GOTO25
81  CALL FILL(Y(ICURPT-2),Y(ICURPT),IC(ICURPT))
   ICURCL=ISC1
   GOTO25
C
72  CONTINUE
C HOLE SSSURED(CASE1)
74  CONTINUE
   IF (ICURPT.GE.L) GOTO4
C IS THIS END OF SCAN LINE
C 4 IS TO READ IN ANOTHER SCAN LINE
   ICURPT=ICURPT+1
   ISPI=ICURPT-1
   CALL FILL(Y(ICURPT-1),Y(ICURPT),IC(ICURPT))
   IF (ABS(Y(ICURPT+1)-Y(ICURPT)).GT..0151) GOTO72
C IF NOT WITHIN .015, GO TO 72
   ICURPT=ICURPT+1
   ISC2=IC(ICURPT)

```

```

C (IN CASE BACKWARDS)
ICURCL=IC(ICURPT)
GOTO 25
END
SUBROUTINE FILL (YMIN,YMAX,IC)
C FILLING IN COLOR NUMBERS
COMMON IOUT(721),ICURPT,IMINH,IMAXH,IMINH2,IMAXH2,INFLOO
INFLOO=INFLOO+1
IF (YMIN.LT.48.) YMIN=48.
IF (YMAX.GT.54.) YMAX=54.
IF (YMAX.LT.48.) YMAX=48.
IF (YMIN.GT.54.) YMIN=54.
IF (YMIN.GT.YMAX) GOTO 1
IARYMIN=(YMIN-48.)*120.+1.+5
IARYMAX=(YMAX-48.)*120.+1.+5
C IT IS ASSUMED THAT THE REAL VALUE WILL BE TRUNCATED
IF ((IARYMIN.EQ.IMINH).AND.(IARYMAX.EQ.IMAXH)
2 .AND.(IMINH.EQ.IMINH2).AND.(IMAXH.EQ.IMAXH2)) GOTO 30
31 IMINH2=IMINH
IMAXH2=IMAXH
IMINH=IARYMIN
IMAXH=IARYMAX
C FILL UP AN ARRAY OF LENGTH 721
DO 1001 I=IARYMIN,IARYMAX
1001 IOUT(I)=IC
RETURN
PRINT51
51 FORMAT(* ABORTED BECAUSE SUBROUTINE WAS CALLED WITH YMIN:YMAX*)
STOP
30 ICURPT=ICURPT+3
GO TO 31$END
MC64,T450,CM255000,TP2. 2096 MCCOMISH
FIN(SL,PL=99999)
VSN,TAPE1=GGC64C.
REQUEST,TAPE1,HY,L.
VSN,TAPE2=OS0139.
REQUEST,TAPE2,HY,L,RING.
LGO.
SKIP.
EXIT,S.
REWIND,OUTPUT.
REWIND,TAPE8.
COPYCF,TAPE8,OUTPUT.
PROGRAM GGC1(INPUT,OUTPUT,TAPE8,TAPE1,TAPE2)
COMMON/INPUT/IRECNO,NUMVEC,IXST,IYST,IVEC(6000),IRECTYP,IFEATNO
COMMON IBLKNO,ISTVEC,AGE,INOLO(1080),IRECRES,L,NOFTREC
COMMON XP,YP,RCP(50),SLOMER(20),A(10),P(10),AA(10),BB(10),CC(10),
Z DD(10),D4850,D5052,D5254
DIMENSION NOXLAT(6000),NOYLONG(6000),LAT(6000),LONG(6000)
DIMENSION NYX(5)
DIMENSION R(6000),D1(6000),NGEO(6000),NOVEC(150),D2(6000)
DIMENSION ICNT(6000),SLOPE(6000)
1 FORMAT(I4)
2 FORMAT(* NUMREC=*I4)
94 FORMAT(5(3X*LONGITUDE LATITUDE*3X))
106 FORMAT(* TAPE HEADER*)
112 FORMAT(* RECORD NO.*I4,6X,*FEATURE NO.*I4,6X,*RECORD TYPE*I4,6X,*
ARLOCK NO.*I4,4X,*RECORDING RESOLUTION=* I3)
116 FORMAT(* RECORD NO.*I4,6X,*FEATURE NO.*I4,6X,*RECORD TYPE*I4,6X,*
IBLOCK NO.*I4)
135 FORMAT(* AGE=*I12,4X,I3* RECORDS IN THIS FEATURE*)
145 FORMAT(* FIRST X=*I6,2X,*FIRST Y=*I6,2X,
A *NUMVEC=*I5,2X,*STARTING VEC. POS. NO.=*I3)
371 FORMAT(* ERROR IN VECTOR* I5)
920 FORMAT(9(1X,F12.8))
921 FORMAT(7(2X,F11.3))
930 FORMAT(7(2X,I6,1X,I6,1X,I3))
934 FORMAT(* ENDPOINTS OF VECTORS Y=LONGITUDE, X= LAT.*)
935 FORMAT(/* TOTAL NUMBER OF POINTS =*I5)
936 FORMAT(5(5X,*LONG*6X*LAT*7X))
938 FORMAT(12(2X,I3,1X,I5))
944 FORMAT(* NUMBER OF POINTS IN FEATURE MAY EXCEED ARRAY SIZE*)
950 FORMAT(4(1X,F8.0,1X,F8.6,1X,F7.0,1X,F7.0))
951 FORMAT(10(1X,I5,1X,I6))
952 FORMAT(6(2X,020))

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994 FORMAT (* INCORRECT SLOPE COMPUTATION *)
PHIR1=48.0 $ PHIR6=50.0 $ PHIR11=52.0 $ PHIR16=54.0
THETA1=6.0 $ THETA2=8.0 $ THETA3=10. $ THETA4=12. $ THETA5=14.
READ 1,NUMREC
PRINT 2,NUMREC
NOFILE=0
IRECNO = -1
DO 60 M=1,150
60 NOVEC(M)=0
70 DO 80 K=1,6000
NDXLAT(K)=0
80 NDYLONG(K)=0
C READ IN NEW RECORD
100 CALL INGGC6(IEOF,NOWORD)
IF(IEOF.EQ.0)104,102
102 NOFILE=NOFILE+1
IF(NOFILE.GE.3)100,100
104 IF(IRECNO.GT.0)107,105
105 PRINT 106
GO TO 100
107 IF(IRECNO.EQ.1)108,110
108 SLOME 6 =SLOMER( 5) $ A 6 =A( 5) $ B 6 =B(5)
SLOME 7 =SLOMER( 1) $ A 7 =A( 1) $ B 7 =B(1)
SLOME 8 =SLOMER( 6) $ A 8 =A( 6) $ B 8 =B(6)
SLOME 9 =SLOMER( 2) $ A 9 =A( 2) $ B 9 =B(2)
SLOME 10=SLOMER( 7) $ A 10=A( 7) $ B 10=B(7)
SLOME 11=SLOMER( 3) $ A 11=A( 3) $ B 11=B(3)
SLOME 12=SLOMER( 8) $ A 12=A( 8) $ B 12=B(8)
SLOME 13=SLOMER( 4) $ A 13=A( 4) $ B 13=B(4)
SLOME 14=SLOMER( 9) $ A 14=A( 9) $ B 14=B(9)
RCP48=(RCP(1)+RCP(2)+RCP(3)+RCP(4))/4.
RCP50=(RCP(5)+RCP(6)+RCP(7)+RCP(8)+RCP(9))/5.
RCP52=(RCP(10)+RCP(11)+RCP(12)+RCP(13)+RCP(14))/5.
RCP54=(RCP(15)+RCP(16)+RCP(17)+RCP(18)+RCP(19))/5.
PRINT 920, SLOME6, SLOME7, SLOME8, SLOME9, SLOME10, SLOME11, SLOME12,
SLOME13, SLOME14
Q
PRINT 921, (RCP48, RCP50, RCP52, RCP54, D4850, D5052, D5254)
110 IF(IRECNO.EQ.2)111,114
111 PRINT 112, IRECNO, IFEATNO, IRECTYP, IBLKNO, IRECRES
GO TO 120
114 PRINT 116, IRECNO, IFEATNO, IRECTYP, IBLKNO
120 IF(IRECNO.GT.4)122,100
122 IF(IRECTYP.EC.30)130,140
130 NT=0
PRINT 135, IAGE, NOFTREC
IF(NOFIREC.GT.6)PRINT 944
GO TO 100
140 IF(IBLKNO.EQ.1)141,142
141 NOXLAT(1)= IXST $ NDYLONG(1)= IYST
142 PRINT 145, IXST, IYST, NUMVEC, ISTVEC
N=NUMVEC
C
DO 600 I=1,N
J= I+NT
K=ISTVEC + I
IVEC(J)=INOLD(K)
JVEC=IVEC(J) +1
GOTO(210,220,230,240,250,260,270,280,290,300,310,320,330,340,350,3
860,370)JVEC
C DELTA X IS THE INCREMENT OF LATITUDE FOR EACH SCALED VECTOR
C DELTA Y IS THE INCREMENT OF LONGITUDE FOR EACH SCALED VECTOR
210 IDELX=0 $ IDELY=2 $ GO TO 500
220 IDELX=1 $ IDELY=2 $ GO TO 500
230 IDELX=2 $ IDELY=2 $ GO TO 500
240 IDELX=2 $ IDELY=1 $ GO TO 500
250 IDELX=2 $ IDELY=0 $ GO TO 500
260 IDELX=2 $ IDELY=-1 $ GO TO 500
270 IDELX=2 $ IDELY=-2 $ GO TO 500
280 IDELX=1 $ IDELY=-2 $ GO TO 500
290 IDELX=-1 $ IDELY=2 $ GO TO 500
300 IDELY=-2 $ IDELY=2 $ GO TO 500
310 IDELX=-2 $ IDELY=1 $ GO TO 500
320 IDELX=-2 $ IDELY=0 $ GO TO 500
330 IDELX=-2 $ IDELY=-1 $ GO TO 500
340 IDELX=-2 $ IDELY=-2 $ GO TO 500
350 IDELX=-1 $ IDELY=-2 $ GO TO 500
360 IDELX=0 $ IDELY=-2 $ GO TO 500
370 PRINT 371, J
372 IDELX=0 $ IDELY=0 $ GO TO 500
500 NOXLAT (J+1)=NOXLAT(J) + IDELX
NDYLONG(J+1)=NDYLONG(J) + IDELY

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600 CONTINUE
C
NT=NT+NUMVEC
IF (IBLKNO.LT.NOFTREC) 100,602
602 NOVEC(IAGE)=NOVEC(IAGE)+NT
NT2=NT+1
PRINT 934
PRINT 935
PRINT 930,(NDYLONG(J),NDXLAT(J),IAGE,J=1,NT2)
PRINT 935,NT2
C
DO 701 J=1,NT2
C
C ICONT IS THE PACKED WORD OF COORDINATES IN X-Y UNITS( LONG.=24 BITS, L
24 BITS, AGE=12 BITS, ALL RIGHT JUSTIFIED
590 ICONT(J)=SHIFT(NDYLONG(J),36).OR.SHIFT(NDXLAT(J),12).OR.IAGE
R(J)=SQRT((NDXLAT(J)-XP)**2+(NDYLONG(J)-YP)**2)
IF(R(J).GT.RCP48)LAT(J)=(48.-2.0*(R(J)-RCP48)/(04850)) *1000.
IF(R(J).GT.RCP50.AND.R(J).LE.RCP48)LAT(J)=(48.0+2.0*(RCP48-R(J))/
A (04850)) *1000.
IF(R(J).GT.RCP52.AND.R(J).LE.RCP50)LAT(J)=(50.0+2.0*(RCP50-R(J))/
A (05052)) *1000.
IF(R(J).GT.RCP54.AND.R(J).LE.RCP52)LAT(J)=(52.0+2.0*(RCP52-R(J))/
A (05254)) *1000.
IF(R(J).LE.RCP54)LAT(J)=(54.+2.0*(RCP54-R(J))/(05254)) *1000.
SLOPE(J)=(YP-NDYLONG(J))/(XP-NDXLAT(J))
IF(SLOPE(J).GE.SLOME 6.AND.SLOPE(J).LT.SLOME 7) 611,615
C DIFFERENT FORM OF THE POINT-SLOPE DISTANCE COMPUTATION FORMULA--SAME RE
611 D1(J)=ABS((SLOME 6 *NDXLAT(J) - NDYLONG(J) +A 6 )/B 6 )
D2(J)=ABS((SLOME 7 *NDXLAT(J) - NDYLONG(J) +A 7 )/B 7 )
LONG(J)= ( 6.0+D1(J)/(D1(J)+D2(J))) *1000
GO TO 700
615 IF(SLOPE(J).GE.SLOME 7.AND.SLOPE(J).LT.SLOME 8 ) 616,620
616 D1(J)=ABS((SLOME 7 *NDXLAT(J) - NDYLONG(J) +A 7 )/B 7 )
D2(J)=ABS((SLOME 8 *NDXLAT(J) - NDYLONG(J) +A 8 )/B 8 )
LONG(J)= ( 7.0+D1(J)/(D1(J)+D2(J))) *1000
GO TO 700
620 IF(SLOPE(J).GE.SLOME 8.AND.SLOPE(J).LT.SLOME 9 ) 621,625
621 D1(J)=ABS((SLOME 8 *NDXLAT(J) - NDYLONG(J) +A 8 )/B 8 )
D2(J)=ABS((SLOME 9 *NDXLAT(J) - NDYLONG(J) +A 9 )/B 9 )
LONG(J)= ( 8.0+D1(J)/(D1(J)+D2(J))) *1000
GO TO 700
625 IF(SLOPE(J).GE.SLOME 9.AND.SLOPE(J).LT.SLOME 10 ) 626,630
626 D1(J)=ABS((SLOME 9 *NDXLAT(J) - NDYLONG(J) +A 9 )/B 9 )
D2(J)=ABS((SLOME 10 *NDXLAT(J) - NDYLONG(J) +A 10 )/B 10 )
LONG(J)= ( 9.0+D1(J)/(D1(J)+D2(J))) *1000
GO TO 700
630 IF(SLOPE(J).GE.SLOME 10.AND.SLOPE(J).LT.SLOME 11 ) 631,635
631 D1(J)=ABS((SLOME 10 *NDXLAT(J) - NDYLONG(J) +A 10 )/B 10 )
D2(J)=ABS((SLOME 11 *NDXLAT(J) - NDYLONG(J) +A 11 )/B 11 )
LONG(J)= (10.0+D1(J)/(D1(J)+D2(J))) *1000
GO TO 700
635 IF(SLOPE(J).GE.SLOME 11.AND.SLOPE(J).LT.SLOME 12 ) 636,640
636 D1(J)=ABS((SLOME 11 *NDXLAT(J) - NDYLONG(J) +A 11 )/B 11 )
D2(J)=ABS((SLOME 12 *NDXLAT(J) - NDYLONG(J) +A 12 )/B 12 )
LONG(J)= (11.0+D1(J)/(D1(J)+D2(J))) *1000
GO TO 700
640 IF(SLOPE(J).GE.SLOME 12.AND.SLOPE(J).LT.SLOME 13 ) 641,645
641 D1(J)=ABS((SLOME 12 *NDXLAT(J) - NDYLONG(J) +A 12 )/B 12 )
D2(J)=ABS((SLOME 13 *NDXLAT(J) - NDYLONG(J) +A 13 )/B 13 )
LONG(J)= (12.0+D1(J)/(D1(J)+D2(J))) *1000
GO TO 700
645 IF(SLOPE(J).GE.SLOME 13.AND.SLOPE(J).LT.SLOME 14 ) 646,650
646 D1(J)=ABS((SLOME 13 *NDXLAT(J) - NDYLONG(J) +A 13 )/B 13 )
D2(J)=ABS((SLOME 14 *NDXLAT(J) - NDYLONG(J) +A 14 )/B 14 )
LONG(J)= (13.0+D1(J)/(D1(J)+D2(J))) *1000
GO TO 700
650 IF(SLOPE(J).GE.SLOME14) 651,655
651 D1(J)=ABS((SLOME 13 *NDXLAT(J) - NDYLONG(J) +A 13 )/B 13 )
D2(J)=ABS((SLOME 14 *NDXLAT(J) - NDYLONG(J) +A 14 )/B 14 )
LONG(J)= (14.0+D2(J)/(D1(J)-D2(J))) *1000
GO TO 700
655 IF(SLOPE(J).LT.SLOME6) 660,693
660 D1(J)=ABS((SLOME 6 *NDXLAT(J) - NDYLONG(J) +A 6 )/B 6 )
D2(J)=ABS((SLOME 7 *NDXLAT(J) - NDYLONG(J) +A 7 )/B 7 )
LONG(J)= ( 6.0-D1(J)/(D2(J)-D1(J))) *1000
GO TO 700
693 PRINT 994

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C
C APPROXIMATION FOR LONG(J) WHOSE SLOPE IS UNDETERMINED
LONG(J)=LONG(J-1)
C
700 NCEO(J)=SHIFT(LONG(J),36).OR.SHIFT(LAT(J),12).OR.IAGE
701 CONTINUE
C
C
C PRINT 950,(R(J),SLOPE(J),D1(J),D2(J),J=1,NT2)
C
C PRINT 94
C PRINT 951,(LONG(J),LAT(J),J=1,NT2)
2237 FORMAT(*,5(I8,2X))
WRITE(8,2237)IFEATNO, LONG(1),LAT(1),IAGE,NT2
NXX(1)=IFEATNO$NXX(2)=LONG(1)$NXX(3)=LAT(1)$NXX(4)=IAGE$NXX(5)=NT2
BUFFEROUT(2,1)(NXX(1),NXX(5))$IF(UNIT(2))1791,1791,1791
1791 BUFFEROUT(2,1)(NCEO(1),NCEO(NT2))$IF(UNIT(2))1792,1792,1792
1792 CONTINUE
IF(IRECNO.LT.NUMREC)70,1000
1000 CONTINUE
PRINT 938,(I,NOVEC(I),I=1,148)
END
SUBROUTINE INGGC6(IEOF, NOWORD)
C THIS VERSION OF INGGC IS FOR THE 6 DEGREE TAPE
COMMON/INPUT/IRECNO, NUMVEC, IXST, IYST, IVEC(6000), IRECTYP, IFEATNO
COMMON IBLKNO, ISTVEC, IAGE, INOLD(1080), IRECRES, L, NOFTREC
COMMON XP, YP, RCP(50), SLOMERT(20), A(10), B(10), AA(10), BB(10), CC(10),
Z DD(10), D4850, D5052, D5254
DIMENSION JGGC(69), LX(20), LY(20), DL(19), DCP50(5), PHI(15)
TYPE REAL LX, LY
5 FORMAT(4(2X, P1E16.8))
6 FORMAT(5(2X, P1E16.8))
8 FORMAT(* DISTANCES BETWEEN PARALLELS*/5(2X, E14.8) )
9 FORMAT(4(2X, P1E10.4))
143 FORMAT(* TABLE COORDINATES OF CONTROL POINTS, X(LATITUDE), Y(LONG)* )
144 FORMAT(5(2X, I2, 2(2X, F7.1)))
146 FORMAT(5(2X, I2, 2X, P1E18.10))
200 FORMAT(2X, *XP=*P1E14.7, 2X, *YP=*P1E14.7)
436 FORMAT(* FILE SUMMARY RECORD *)
455 FORMAT(* INVALID RECORD TYPE*)
496 FORMAT(* END OF FILE*)
1000 FORMAT(* INVALID AGE NO.*)
1500 FORMAT(* PARITY ERROR*)
C
C READ NEW RECORD
C
100 BUFFER IN (1,1) (JGGC(1), JGGC(69))
C
C TEST IF EOF OR PARITY ERROR WAS ENCOUNTERED ON TAPE
105 IF (UNIT(1)) 120,495,110
110 PRINT 1500
120 IEOF=0
NOWORD = LENGTH(1)
IRECNO = IRECNO + 1
IF(IRECNO.GT.0)130,500
130 CALL UNPACK4(JGGC,69)
IFEATNO = INOLD(7)*16 + INOLD(8) + INOLD(6)*256
IRECTYP = INOLD(9)*(2**4) + INOLD(10)
IBLKNO = INOLD(11)*(2**4) + INOLD(12)
IF(IRECNO.EQ.1)135,150
135 DO 140 I=1,19
J=8*I +253
LX(I)=INOLD(J)*4096+INOLD(J+1)*256+INOLD(J+2)*16+INOLD(J+3)
140 LY(I)=INOLD(J+4)*4096 +INOLD(J+5)*256 +INOLD(J+6)*16 +INOLD(J+7)
PRINT 143
PRINT 144,(I,LX(I),LY(I),I=1,19)
XPN=(LX(5)*LX(19))*(LY(15)-LY(9))+(LX(5)*LX(9))*(LY(19)-LY(15))+
A (LX(9)*LX(15))*(LY(5)-LY(19))+(LX(15)*LX(19))*(LY(9)-LY(5))
XPD=(LY(15)-LY(5))*(LX(19)-LX(9))-(LX(15)-LX(5))*(LY(19)-LY(9))
XP=XPN/XPD
YP = LY(5)+(XF -LX(5))*(LY(15)-LY(5))/(LX(15)-LX(5))
DO 1441 M=5,14
1441 DL(M)=SQRT((LX(M+5)-LX(M))**2 + (LY(M+5)-LY(M))**2 )
D4850=(D5052=(DL(5)+DL(6)+DL(7)+DL(8)+DL(9))/5.
D5254=(DL(10)+DL(11)+DL(12)+DL(13)+DL(14))/5.
PRINT 8,(DL(M),M=5,14)
PRINT 200, XP, YP
DO 145 I=1,19
145 RCP(I)=SQRT((LX(I)-XP)**2 + (LY(I)-YP)**2 )
PRINT 146,(I,RCP(I),I=1,19)
DO 1443 M=1,4
DCP50(M)=SQRT((LX(M+5)-LX(M+4))**2 + (LY(M+5)-LY(M+4))**2 )

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1443 PHI(M)=( ASIN(DCP50(M)/RCP(M+4)))*(180./3.14159)
PRINT9,(PHI(M),M=1,4)
DO 147 M=1,9
AA(M)=YP-LY(M) $ BB(M)=LX(M)-XP $ CC(M)=XP*LY(M)-LX(M)*YP
DO(M)=SQRT(AA(M)**2+BB(M)**2)
A(M)={(LX(M)*YP)-(LY(M)*XP)}/(LX(M)-XP)
147 B(M)=SQRT(((LY(M)-YP)/(LX(M)-XP))**2+1.)
DO 148 M=1,19
148 SLOMER(M)=(LY(M)-YP)/(LX(M)-XP)
PRINT 5,(SLOMER(M),M=1,4)
PRINT 6,(SLOMER(M),M=5,19)
150 IF(IRECNO.EQ.2) IRECRES=INOLD(23)*(2**4) + INOLD(24)
IF(IRECNO.GT.4) 160,500
160 IF(IRECTYP.EQ.30) 162,189
162 JH = INOLD(45)*(2**4) + INOLD(46)
JT = INOLD(47)*(2**4) + INOLD(48)
JU=INOLD(49)*(2**4) + INOLD(50)
NOFTREC=IBLKNO - 1
IF(JU.GT.175.AND.JU.LT.186) 170,176
170 IF(JT.GT.175.AND.JT.LT.186) 172,188
172 IF(JH.GT.176.AND.JH.LT.186) 174,188
174 IAGE=(JH-176)*100 + (JT-176)*10 + (JU-176)
IF(IAGE.GT.0.AND.IAGE.LT.149) 500,188
176 IF(JU.EQ.32.OR.JU.EQ.160) 177,188
177 IF(JT.GT.175.AND.JT.LT.186) 178,180
178 IF(JH.GT.176.AND.JH.LT.186) 179,188
179 IAGE=(JH-176)*10 + (JT-176)
IF(IAGE.GT.0.AND.IAGE.LT.100) 500,188
180 IF(JT.EQ.32.OR.JT.EQ.160) 181,188
181 IF(JH.GT.176.AND.JH.LT.186) 182,188
182 IAGE= JH-176
IF(IAGE.GT.0.AND.IAGE.LT.10 ) 500,188
188 IAGE=0
PRINT 1000
GO TO 500
189 IF(IRECTYP.EQ.31) 190,430
C STARTING VECTOR POSITION NUMBER USUALLY "28"
190 ISTVEC=(INOLD(14).AND.07B)*(2**8) + INOLD(15)*(2**4) + INOLD(16)
NUMVEC=(INOLD(18).AND.07B)*(2**8) + INOLD(19)*(2**4) + INOLD(20)
IXST = (INOLD(21))*(2**12) + INOLD(22)*(2**8) + INOLD(23)*(2**4)
1 + INOLD(24)
IYST = (INOLD(25))*(2**12) + INOLD(26)*(2**8) + INOLD(27)*(2**4)
1 * INOLD(28)
L=NOFTREC-IBLKNO
GO TO 500
430 IF(IRECTYP.EQ.90) 435,450
435 PRINT 436
NUMFEAT=INOLD(21)*(2**12)+INOLD(22)*(2**8)+INOLD(23)*(2**4)+INOLD(
$24)
NUMBLKS=INOLD(25)*(2**12)+INOLD(26)*(2**8)+INOLD(27)*(2**4)+INOLD(
$28)
GO TO 500
450 PRINT 455
GO TO 500
495 IEOF=1
PRINT 496
500 RETURN
END
SUBROUTINE UNPACK4(JGGC,NWD)$DIMENSION JGGC(59)
COMMON IBLKNO,ISTVEC,IAGE,INOLD(1080),IRECRES,L,NOFTREC
COMMON XP,YP,RCP(50),SLOMER(20),A(30),B(30),AA(10),BB(10),C(30),
Z D(30),D4850,D5052,D5254,DEGLONG(50),DEGLAT(50)
INX=0$DO 2 J=1,NWD$DO 2 I=1,15$INX=INX+1
2 INOLD(INX)=17B.A.SHIFT(JGGC(J),-4*(15-I))
10 FORMAT(5022)
9 FORMAT(*0 INOLD*)
END
6999
MC6GS,T160,CM145000,TP2.
FTN,SL,A,P,BL,R=3,PL=49999,T.
MAP(ON)
VSN,TAPE1=050139.
REQUEST,TAPE1,HY,L.
VSN,TAPE4=050172.

```

## 6. DESCRIPTION OF PART IV

### 6.1 Overview

The purpose of PART IV of the LORAN Grid Prediction Program is to update the input data base to PART II. By comparing the time differences at measured and calculated fixed points in the service area, corrections are applied to the postulated top soil conductivity values to zero out the difference between the former. A technique described by Elkins<sup>22</sup> has been utilized which employs a continuous Kalman filter with updating of references state vector. The details of this program are described in Program ESTIMAE.<sup>23</sup> It is pointed out that of the nine parameters required to calculate the surface impedance, only the two predominant top soil conductivities are altered.

The approach taken for system tuning or data base updating is as follows:

(1) Compute time difference in PART III of Program for locations for which measured data is available.

(2) Identify two values for top soil conductivity that occur most frequently in the geographical area of interest.

(3) The variation in the LORAN time difference due to a variation in topsoil conductivity is computed by changing in turn, each of the two conductivity values where they occur in the geographical area of interest and proceeding with the step outlined in "1" above.

(4) The difference between the observed and calculated data, the rates of change in time difference due to changes in each conductivity value, estimate of the error in the initially chosen values of conductivity, and estimates of the error in the observations are input to a Kalman filter program to produce an improved estimate of the value of conductivity.

(5) The improved values of conductivity are written into the data base.

For the test program, the conductivity was changed by 10 percent to form the required partial derivatives; absolute conductivity was estimated within a factor of two, and the standard deviation of the time difference measurement was assumed to be 100  $\mu$ sec. Utilizing forty test points, this technique reduced the prediction errors by 33 percent.

A listing of the program is presented below.

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22. Elkins, T. E. (1976) Empirical Correction of Soil Conductivity Model, RADC/ET Private Communication.

23. Program ESTIMAE - Problem No. 4723 (1975) Analyses and Simulation Branch, AFCRL dated 1 November 1975.

## 6.2 Program Listing for Part IV

```

I ESTIMATE      74/74   OPT=L                               FTN 4.5+414 06/20/77
      PROGRAM ESTIMATE(INPUT=401B,OUTPUT=401B,TAPE1=401B,TAPE2=401B,
      1 TAPE3=401B,TAPE4=401B,TAPE10,TAPE11,TAPE20=1101B)
C.... GIVEN (1) A SET OF DIFFERENTIAL EQUATIONS DESCRIBING A DYNAMICAL
C SYSTEM, (2) AN ESTIMATE OF THE STATE OF THE SYSTEM AT SOME INITIAL
C TIME ALONG WITH STATISTICS PROVIDING A MEASURE OF THIS ESTIMATE,
C AND (3) A DATA FILE CONTAINING OBSERVATIONS BEARING ON THE STATE OF
C THE SYSTEM AT SPECIFIED POINTS OF TIME. COMPUTE THE BEST ESTIMATE OF
C THE STATE OF THE SYSTEM ALONG WITH SOME STATISTICS GIVING A MEASURE
C OF THE ESTIMATE AT EACH OF THE SPECIFIED POINTS OF TIME. THE BEST
C ESTIMATE IS BASED ON ALL OBSERVATIONS PROCESSED UP TO THE CURRENT
C TIME. A BACKWARD SMOOTHING FEATURE IS PROVIDED AS AN OPTION SO THAT
C THE ESTIMATES AT THE FIRST K POINTS OF TIME WILL REFLECT THE
C INCLUSION OF ALL OBSERVATIONS UP TO THE K TH POINT OF TIME.
      COMMON/CASE/CASE
      COMMON/RK/TI,TF,NR(4578),SDT,DT,TOL,SP,NERR1,NERR2,ORD,
      1 NSTEP,NKEJ,IS121
      COMMON/STREF/IXR,XR(1)
      COMMON/STESTM/IXE,(E(1)
      COMMON/STRSD/IX,X(1)
      COMMON/STCOV/IP,JP,P(1)
      COMMON/STNCOV/IQ,QCOV
      COMMON/OBSH/IH,JH,H(1)
      COMMON/OBSY/IY,Y(1)
      COMMON/OBSCOV/IR,R(1)
      COMMON/MEASCOV/RCOV(6)
      COMMON/PARAMS/KSTRSDL,HSTEP,TIMETOL,KPUNCH,KREWIND,TOLRNCE,IDER,
      1 KPLT,KEND,KONE,KS,KSMOOTH,MAXS,MAXKC,MPTY,NGPS,NLRSR,NLRSW,
      2 NFILF,NFILB,NSAT,NSAT,NGPS1,NGPS2,NRSEQ,NRRAN,NWSEQ,NWRAN,NPRAN,
      3 IOB,JZH,IST,IS1,IS2,KCRIT,KCBEGIN,KPRINT,KWRITE,KDATA,KTYPES,
      4 MAXDATA,IA,JA,KA,IM,JM,KM,MD,KPLWD,ITYPES(2),PRINMOM(3),KQKLOCK,
      5 IDERSET
C.... THE FOLLOWING COMMON AND EQUIVALENCE STATEMENTS ARE DEPENDENT ON
C THE DATA FILE USED.
      COMMON/BUFF/LBUFF(+),TIME
      DIMENSION ID(1) $ EQUIVALENCE (D, ID)
      COMMON D(36),XR(12),S(144)
      DIMENSION X(12),DIAG(12)
      EXTERNAL DER
      NAMELIST/VALUES/CASE,ISTART,TSTOP,XU,DIAGO,KPLT,KPRINT,
      1 KWRITE,KREWIND,KSMOOTH,MAXS,KCRIT,MAXKC,KCBEGIN,KTYPES,MAXDATA,
      2 IA,JA,KA,IM,JM,KM,NR(4578),STEP,TOLRNCE,SP,NERR1,NERR2,ORD,IST,
      3 IS1,IS2,JZH,KSTRSDL,QCOV,RCOV,TIMETO,KPARTS,KPLWD,MD,RUNMAX,
      + KQKLOOK
C.... READ IN INITIAL PARAMETERS. CALL SUBROUTINES TO SET INITIAL
C PARAMETERS AND TO SELECT OPTIONS.
      1 CASE=CASE+1. $ READ VALUES
      IF(CASE.LT.46)46,2
      2 CALL FILEIO(T)
      CALL OBSERVE
      CALL STATS
      CALL PACK(KPLWD,I,I)
      SUB=STEP $ TOL=TOLRNCE
      IDER=0
C.... SET REFERENCE STATE VECTOR AND DIAGONAL STATE COVARIANCE MATRIX TO
C INITIAL CONDITIONS.
      CALL DIAGN(IST,X),XR,DIAGO,IP,P)
C.... SET MAXIMUM RUN-TIME LIMIT.

```

```

      CLOCK0=SECOND(T)
C.... PRINT INITIAL PARAMETERS.
      PRINT VALUES
C.... SET START AND STOP TIMES.
      TI=TSIART
      IST1=IST+1 $ IST21=IST*IST1
C.... READ IN THE NEXT DATA RECORD.
      3 CALL FILEIO1(TI), RETURNS(4,42)
      4 IF(TIME.GT.TSTOP)5,8
      5 KEND=1 $ GO TO 42
C.... TIME OF DATA RECORD LIES WITHIN REQUESTED INTERVAL.
      8 I=TIME $ KOP=0
      11 TF=T
      HSTEP=ABS(TF-TI)
C.... TEST WHETHER OR NOT TI AND TF ARE APPROXIMATELY EQUAL.
      14 IF(HSTEP.LE.TIMETO.)21,15
C.... INTEGRATE FORWARD TO TF.
      15 IF(KOP)19,16
C.... MAP THE STATE COVARIANCE MATRIX FORWARD.
      16 CALL MATRIX(0,IST,IST,0,P,IP,XR(IST1),IST,0,0)
      IDERSET=2 $ CALL RK4578(XR,DER)
      CALL MATRIX(0,IST,IST,0,XR(IST1),IST,P,IP,0,0)
      GO TO 21
      19 IF(KRESET.EQ.1) GO TO 20 $ KRESET=1
      CALL MCJLEV(XR,XR,IST)
      20 CALL RK4578(XR,DER)
      21 TI=TF
C.... SELECT THE DATA FROM THE RECORD.
      IF(KOP.EQ.0)22,25
      22 CALL OBSERV1 $ IOB=J $ IYPES(1)=IYPES(2)=1H
      23 KOP=KOP+1 $ IF(KOP.GT.<DATA)36,24
      24 N=MO*(KOP-1)+1 $ T=D(N) $ I=ID(N+2)
      IF(KOP.EQ.1)30,11
C.... INITIALIZE STATE TRANSITION MATRIX.
      30 DO 10 M=1,IST $ _=IST*M $ DO 9 K=1,IST $ J=K+L
      9 XR(J)=0. $ J=M+_
      10 XR(J)=1.
      KRESET=0
      IDERSET=1 $ GO TO 11
C.... ENTER APPROPRIATE SUBROUTINE TO FIND THE COMPUTED OBSERVATION, THE
C DIFFERENCE BETWEEN THE GIVEN OBSERVATION AND THE COMPUTED
C OBSERVATION, AND THE PARTIALS OF THE COMPUTED OBSERVATIONS.
      25 IF(I.EQ.1)26,27
      26 CALL SSENSOR(KPARTS,D(N),S) $ GO TO 35
      27 IF(I.EQ.2)28,29
      28 CALL ESENSOR(KPARTS,D(N),S) $ GO TO 35
      29 IF(4.LE.I.AND.I.LE.6)30,31
      30 CALL MAGDATA(KPARTS,D(N),S) $ GO TO 35
      31 IF(I.EQ.16)34,36
      34 CALL ACCEL(KPARTS,)(N),S)
C.... SAVE OBSERVATION TYPES FOR PRINTOUT.
      35 IF(KPRINT.AND.512)30,23
      530 J=3*KOP-1 $ ENCODE(16,31,S) J
      531 FORMAT(10H(T1,2A10,T,I2,+H,I2))
      ENCODE(20,S,IYPES) IYPES,I
      GO TO 23
      36 TI=TIME $ IF(IOB)37,41

```

```

37 IF(KRESET.EQ.1) CALL MOVLEV(XR0,XR,IST)
C.... ENTER THE FILTER.
      IF(KONE)38,39,39
38 NFILB=NFILB+1 $ GO TO +0
39 NFILF=NFILF+1
40 CALL FILTER, RETURNS(44)
C.... COMPUTE THE BEST ESTIMATE.
      CALL MATRIX(21,ISI,1,3,XR,IXR,X,IX,XE,IXE)
C.... DETERMINE PRINCIPAL VALUES OF ANGLES.
4000 DO 400 I=1,3
400 XE(I)=PRINVAL(XE(I))
C.... REINITIALIZE STATE REFERENCE VECTOR.
      CALL MOVLEV(XE,XR,IST)
C.... CHECK FOR MAXIMUM RUN TIME.
      CLOCK=SECOND(T)-CLOCK0 $ IF(CLOCK.GT.RUNMAX) KEND=1
C.... GATHER APPROPRIATE STATISTICS ON THE ESTIMATION.
      CALL STATS1
      IF(KEND.EQ.0) CALL FILEIO2(T1), RETURNS(4,42)
C.... INITIATE END PROCESSING.
42 CALL FILEIO3(T)
43 GO TO 1
44 PRINT 45,NGPS,KONE
45 FORMAT(*0SINGULAR MATRIX ENCOUNTERED.*5X*GROUP=*I4,5X*KONE=*I2)
C.... SIMPLY EQUATE BEST ESTIMATE VECTOR AND STATE REFERENCE VECTOR.
41 CALL MOVLEV(XR,XE,IST) $ DO 450 K=1,IST
450 X(K)=0. $ GO TO +000
46 CONTINUE $ END

```

```

FUNCTION PRINVAL(ANGLE)
C.... PRINVAL RETURNS THE PRINCIPAL VALUE OF THE GIVEN ANGLE.
C ( - PI .LT. PRINVAL .LE. PI )
      DATA PI/3.141592653589793/
      A=ANGLE
1 AA=ABS(A) $ IF(AA.LE.PI) GO TO 2
      A=A-SIGN(2.*PI,A) $ GO TO 1
2 PRINVAL=A $ RETURN $ END

```

```

SUBROUTINE STATS
C.... RECORDS STATISTICS IN ORDER TO EVALUATE THE PERFORMANCE OF THE
C ESTIMATION PROCESS. CONTROLS THE INITIATION OF THE BACKWARD
C SMOOTHING PROCESS AND THE ASSOCIATED RANDOM FILE WRITING. CONTROLS
C ALL PRINTED OUTPUT ON FILES 1,2,3, AND 4.
COMMON/STREF/IXR,XR(1)
COMMON/STESTM/IXE,XE(1)
COMMON/STRSDL/IX,X(1)
COMMON/STCOV/IP,JP,P(1)
COMMON/STCOVD/IPD,J(1)
COMMON/OBSY/IY,Y(1)
COMMON/PARAMS/IQ(7),KPLOI,KEND,KONE,KS,KSMOOTH,MAXS,MAXKC,MPTY,
1  NGPS,NLRSR,NLRSW,NFILF,NFILB,NSAT,NNSAT,NGPS1,NGPS2,NRSEQ,NRRAN,
2  NWSEQ,NWRAN,NPRAN,IOB,JZH,IST,IS1,IS2,KCRIT,KCBEGIN,KPRINT,KWRITE
3  ,JQ(11),OBTYPES(2)
COMMON/CRIT/CRIT(1)
C.... THE FOLLOWING COMMON AND EQUIVALENCE STATEMENTS ARE DEPENDENT ON
C THE DATA FILE USED.
COMMON/BUFF/LBUFF(+),W(127)
DIMENSION XT(1) $ EQUIVALENCE (W,TIME),(W(10),XT)
COMMON DX(12),XD(12),IS(24),O(50)
DIMENSION S(1) $ EQUIVALENCE (IS,S)
LOGICAL NRSEQ,NRRAN,NWSEQ,NWRAN,NPRAN
DATA MAXK/57,MORE/5H MORE/
C.... SET INITIAL CONSTANTS.
NLRSR=NLRSW=NGPS=NFILF=NFILB=NSAT=NNSAT=KST=KEND=0
NRSEQ=.T. $ NRRAN=NWSEQ=NWRAN=NPRAN=.F.
KS=KSMOOTH $ KONE=1
C.... SET PRINT OPTIONS. AT MOST 1 OPTION PER FILE IS ALLOWED.
C KPRINT BIT 0. PRINT TIME, STATE VECTOR ON FILE 1.
C KPRINT BIT 1. PRINT TIME, STATE RESIDUALS VECTOR ON FILE 2.
C KPRINT BIT 2. PRINT TIME, STATE DEVIATIONS VECTOR ON FILE 2.
C KPRINT BIT 3. PRINT TIME, STATE DERIVATIVES VECTOR ON FILE 2.
C KPRINT BIT 4. PRINT TIME, DIAGONALS OF STATE COVARIANCE MATRIX ON
C FILE 3.
C KPRINT BIT 5. PRINT TIME, STATE COVARIANCE MATRIX ON FILE 3.
C KPRINT BIT 6. PRINT TIME, TORQUES ON FILE 3.
C KPRINT BIT 7. PRINT COMPLETE STATISTICS ON FILE 4.
C KPRINT BIT 8. PRINT PARTIAL STATISTICS ON FILE 4. (KCRIT.NE.0)
C KPRINT BIT 9. PRINT TIME, SOME STATISTICS, AND OBSERVATION RESIDUALS
C VECTOR ON FILE 4.
IF(KPRINT)2,1
1 ASSIGN 55 TO M1 $ GO TO 17
2 CALL WRITER0(4,0,0)
ASSIGN 41 TO M1 $ ASSIGN 46 TO M2
ASSIGN 52 TO M3 $ ASSIGN 55 TO M4
ASSIGN 541 TO M41
C.... SET PRINT LIMITS ON STATE VECTOR ELEMENTS.
IS2=MIN0(12,IS2,IS1,(IX-IS1+1)) $ IS4=IS1+IS2-1 $ IS3=IS2+1
PRINT 16,(I,I=IS1,IS4)
PRINT 160 $ PRINT 161
I=J=1
3 K=KPRINT.AND.J $ IF(K.NE.0) GO TO (5,5,7,9,10,11,13,14,14,15),I
4 J=2*J $ I=I+1 $ IF(I.GT.10)17,3
5 ASSIGN 40 TO M1 $ GO TO 4
6 ASSIGN 42 TO M2 $ GO TO 4
7 ASSIGN 43 TO M2 $ GO TO 4

```

```

9 ASSIGN 44 TO M2 $ GO TO 4
10 ASSIGN 47 TO M3 $ GO TO 4
11 ASSIGN 48 TO M3 $ GO TO 4
13 ASSIGN 51 TO M3 $ GO TO 4
14 KSI=1
140 ASSIGN 54 TO M4
    IF(I.LQ.9) ASSIGN 53 TO M4 $ GO TO 4
15 ASSIGN 540 TO M41 $ GO TO 140
16 FORMAT(*10DESCRIPTION OF PRINTOUTS ON FILES 1, 2, OR 3*/5X*ONLY THE
1 FOLLOWING COMPONENTS OF THE STATE VECTOR, STATE RESIDUALS VECTOR,
2 STATE DEVIATIONS VECTOR, STATE DERIVATIVES VECTOR OR THE** FOLLO
3 WING COLUMNS OF THE STATE COVARIANCE MATRIX OR THE FOLLOWING DIAGO
4 NAL ELEMENTS OF THE STATE COVARIANCE MATRIX ARE PRINTED OUT.*/1X,
5 I2I5)
160 FORMAT(* FOR THE OBSERVATION RESIDUALS VECTOR, ALL COMPONENTS, AS
1 WELL AS THE OBSERVATION TYPES, ARE PRINTED OUT.*)
161 FORMAT(
5*-DESCRIPTION OF STATISTICS PRINTOUT ON FILE 4*/5X*GP....POSITION
7OF DATA GROUP WRT FIRST DATA GROUP PROCESSED*/5X*LR R....LOCATION
8OF LOGICAL RECORD OF DATA WRT FIRST LOGICAL RECORD READ*/5X
9*LR W....CUMULATIVE NUMBER OF LOGICAL RECORDS WRITTEN TO OUTPUT DA
A TA FILE
*/5X*F F....CUMULATIVE NUMBER OF TIMES ENTERED FIL
B TER FOR FORWARD FILTERING*/5X*F B....CUMULATIVE NUMBER OF TIMES EN
C TERED FILTER FOR BACKWARD SMOOTHING*/5X*SAT....CUMULATIVE NUMBER O
D F TIMES PERFORMANCE CRITERIA SATISFIED*/5X*NSAT....CUMULATIVE NUMB
E ER OF TIMES PERFORMANCE CRITERIA NOT SATISFIED*/5X*ELEMENT....RELA
F TIVE LOCATION WITHIN STATE OR STATE RESIDUAL VECTOR*/5X*VALUE....T
G EST VALUE WHICH EXCEEDED SPECIFIED CRITERIA*/5X*MORE....FLAG IMPLY
H ING THAT MORE ELEMENTS FAILED TEST*/5X*TIME....TIME OF DATA GROUP*
I)
17 ASSIGN 18 TO M6
C.... SET CRITERIA OPTIONS.
C KCRIT BIT 0. COVARIANCE LIMIT CRITERIA.
C KCRIT BIT 1. COMPARISON WITH EXISTING STATE CRITERIA.
    ASSIGN 37 TO M5
    IF(KCRIT.EQ.1) ASSIGN 21 TO M5
    IF(KCRIT.EQ.2) ASSIGN 22 TO M5
C.... SET SEQUENTIAL WRITE OPTION.
    IF(KWRITE.EQ.1) NWSEQ=.NOT.NWSEQ
    RETURN
    ENTRY STATS1
C.... USUAL ENTRY POINT INTO STATS.
    GO TO M6,(18,20)
C.... WHEN PROCESSING FIRST DATA GROUP, SPECIFY NECESSARY OPTIONS.
18 ASSIGN 20 TO M6
    IF (KPLOT.EQ.1) NPRAN=.NOT.NPRAN
    IF (KSMOOTH) 19,20
19 NPRAN=.NOT.NPRAN $ NWSEQ=.NOT.NWSEQ $ NPRAN=.NOT.NPRAN
    LGPNS=0
C.... CHECK WHETHER OR NOT CRITERIA ARE SATISFIED.
20 K=L $ DO 26 I=1,IST $ GO TO M5,(21,22,37)
21 J=1+IP*(I-1) $ VAL=P(J) $ GO TO 220
22 VAL=XE(I)-XT(I)
220 IF (ABS (VAL) .LE. CRIT (I)) 25,23
23 K=K+1 $ IF(KST) 24,36
C... SAVE DATA ON ELEMENTS NOT SATISFYING CRITERIA.
24 IS(K)=I $ K=K+1 $ S(K)=VAL $ IF(K.GT.2*MAXK) 25,26

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25 K=K-1 $ IS(K)=MORE $ GO TO 36
26 CONTINUE $ IF(K)36,27
27 NSAT=NSAT+1 $ IF(KS.EQ.1)28,39
28 IF((NGPS-LGPNS).GE.MAXKC)29,31
C.... MAXKC CONSECUTIVE SATISFACTORY ESTIMATES.
29 IF(LGPNS)30,35
C.... BACKWARD SMOOTHING NECESSARY.
30 NGPS1=NGPS-KOBEGIN $ NLSR=NLSR-KOBEGIN $ GO TO 33
31 IF(NGPS.GE.MAXS)32,39
32 NGPS1=NGPS
33 KONE=-1
34 NGPS2=NGPS $ KS=-1
NRSEQ=.NOT.NRSEQ $ NRRAN=.NOT.NRRAN $ GO TO 39
C.... BACKWARD SMOOTHING NOT NECESSARY.
35 NGPS1=1 $ NLSR=NLSR-NGPS+1 $ GO TO 34
C.... AN UNSATISFACTORY ESTIMATE.
36 NNSAT=NNSAT+1 $ LGPNS=NGPS
37 IF(KS.EQ.1)31,39
C.... EXTRACT DIAGONAL PORTION OF COVARIANCE MATRIX.
39 DO 390 I=1,IST
390 D(I)=P(I+IP*(I-1))
CALL MATRIX(22,IST,1,0,XE,IST,XT,IST,XD,IST)
C.... PRINT SELECTED INFORMATION ON OUTPUT FILES.
U(1)=TIME $ GO TO M1,(+0,41,55)
40 CALL MOVLEV(XE(IST),0(2),IS2) $ CALL WRITER(1,0,IS3)
41 GO TO M2,(42,43,44,46)
42 CALL MOVLEV(X(IST),0(2),IS2) $ GO TO 45
43 CALL MOVLEV(XD(IST),0(2),IS2) $ GO TO 45
44 CALL MOVLEV(DX(IST),0(2),IS2)
45 CALL WRITER(2,0,IS3)
46 GO TO M3,(47,48,51,52)
47 CALL MOVLEV(D(IST),0(2),IS2) $ L=IS3 $ GO TO 50
48 L=1 $ DO 49 I=IS1,IS4 $ DO 49 J=IS1,IS4 $ L=L+1
49 D(L)=P(I+IP*(J-1)) $ GO TO 50
50 CALL WRITER(3,0,L)
51 CONTINUE
52 GO TO M4,(53,54,55)
53 IF(K)54,55
54 CALL MOVLEV(NGPS,0(2),7) $ GO TO M41,(540,541)
54L K=L $ IF(I0B.EQ.0) GO TO 542
CALL MOVLEV(OBTYPES,0(9),2) $ CALL MOVLEV(Y,0(11),I0B)
K=2+I0B $ GO TO 542
541 CALL MOVLEV(IS,0(9),K)
542 CALL WRITER(4,0,8+K)
55 IF(NPRAN.AND..NOT.NRRAN)56,57
C.... SAVE DATA FOR EVENTUAL PLOTTED OUTPUT.
56 CALL MOVLEV(XE,0(2),IST) $ I=2+IST
CALL MOVLEV(X,0(I),IST) $ I=I+IST
CALL MOVLEV(XD,0(I),IST) $ I=I+IST
CALL MOVLEV(D,0(I),IST) $ I=I+IST-1
CALL PACK1(I,0,MPT)
57 RETURN $ END

```



```

SUBROUTINE FILEIO(I), RETURNS(NR1,NR2)
C.... THIS ROUTINE IS THE CONTROLLING ROUTINE FOR ALL FILE INPUT AND
C OUTPUT IN THE PROGRAM.
COMMON/STREF/IXR,XR(1)
COMMON/STESTH/IXE,XE(1)
COMMON/STCOV/IP,JP,P(1)
COMMON/STCOVD/IPD,D(1)
COMMON/RANFILE/MAXMS,MS(1)
COMMON/PACKED/NLRS,NWORDS,WH(512)
EQUIVALENCE (WH,IWH1),(WH(2),IWH2)
COMMON/PARAMS/KSTRSDL,HSTEP,TIMETOL,KPUNCH,KREWIND,LRWOCNT(2),
1 KPLOTT,KEND,KONE,KS,KSMOOTH,MAXS,MAXKC,MPTY,NGPS,NLRSR,NLRSW,
2 NFILF,NFILB,NSAT,NSAT,NGPS1,NGPS2,NRSEQ,NRRAN,NWSEQ,NWRAN,NPRAN,
3 IOB,JZH,IST,Z1(22),KQKJOK
C.... THE FOLLOWING COMMON AND EQUIVALENCE STATEMENTS ARE DEPENDENT ON
C THE DATA FILE USED.
COMMON/BUFF/LENGTHR,LENGTHW,MAXLRW,LRW,W(127)
EQUIVALENCE (W,TIME)
COMMON RECORD(14)
LOGICAL NRSEQ,NRRAN,NWSEQ,NWRAN,NPRAN
DATA KOPEN/-1/
C.... SET FILE INPUT/OUTPUT OPTIONS.
IF (KSMOOTH.NE.0.OR.KPLOTT.NE.0) KOPEN=KOPEN+1
IF (KOPEN)101,102,111
102 CALL OPENMS(20,MS,MAXMS+1,0) $ KOPEN=KOPEN+1
101 MAXS=MIND(MAXS,MAXMS) $ MAXKC=MIND(MAXKC,MAXS)
IF (KREWIND.NE.0) REWIND 10
ASSIGN 36 TO M1
KREWIT=0
RETURN
ENTRY FILEIO1
C.... RANDOM FILE READ.
100 IF (NRRAN)1,15
1 IF (KS)2,8,15
2 IF (NGPS1.EQ.1)3,6
C.... BACKWARD SMOOTHING EITHER NOT NECESSARY OR NOW COMPLETE.
3 KONE=1 $ KS=0 $ ASSIGN 37 TO M1
NWSEQ=.NOT.NWSEQ $ NWRAN=.NOT.NWRAN $ NPRAN=.NOT.NPRAN
IF (NGPS1.EQ.NGPS)37,10
C.... CONTINUE WITH BACKWARD SMOOTHING.
6 IF (NGPS.EQ.NGPS1)9,7
7 ASSIGN 11 TO M1 $ GO TO 10
8 IF (NGPS.NE.NGPS2) GO TO 9
C.... RESUME SEQUENTIAL FILE READ.
NRRAN=.NOT.NRRAN $ NRSEQ=.NOT.NRSEQ
KREWIT=-1 $ GO TO 11
C.... READ IN A LOGICAL RECORD.
9 NGPS1=NGPS1+KONE $ NLRSR=NLRSR+KONE
10 CALL READMS(20,LRW,MAXLRW,NGPS1)
LRW=LRW-2*ISI
NGPS=NGPS1 $ GO TO M1,(11,36,37)
C.... MOVE APPROPRIATE VALUES FROM W ARRAY TO STATE AND COVARIANCE
C ARRAYS
11 I=LRW+1 $ CALL MOVLEV(W(I),XE,IST)
I=I+IST $ CALL MOVLEV(W(I),D,IST)
CALL DIAGNAL(IST,XE,XR,D,IP,P) $ T=TIME
ASSIGN 36 TO M1 $ GO TO 100

```

```

C.... SEQUENTIAL FILE READ.
  15 IF(NRSEQ)16,22
C.... READ IN A LOGICAL RECORD.
  16 READ(10) LRW, W(I), I=1, LRW) $ NLRSR=N_LRSR+1
C.... CHECK LAST BINARY READ.
  IF(IO EOF PE(10))24,17,15
  17 NLRSR=NLRSR-1
  22 KEND=1 $ RETURN NR2
C.... DATA LOGICAL RECORD.
  24 IF(TIME.LT.T-TIME/DL)49,35
C.... ACCEPTABLE DATA RECORD.
  35 NGPS=NGPS+1
  36 RETURN NR1
  ENTRY FILEI02
C.... RANDOM FILE WRITE.
  37 IF(NWRAN)40,41
  40 I=LRW+1 $ CALL MOVLEV(XE, W(I), IST)
  I=I+IST $ CALL MOVLEV(O, W(I), IST)
  LRW=LRW+2*IST
  CALL WRITMS(20, LRW, LRW+1, NGPS, KREWRT) $ GO TO 49
C.... SEQUENTIAL FILE WRITE.
  41 IF(NWSEQ)42,45
  42 I=LENGTHR+1 $ CALL MOVLEV(XE, W(I), IST)
  I=I+LENGTHW $ CALL MOVLEV(O, W(I), IST)
  LRW=LENGTHR+2*LENGTHW
  WRITE(11) LRW, W(I), I=1, LRW) $ NLRSW=NLRSW+1
C.... OUTPUT DATA FOR EVENTUAL PLOTTING, COMPARISON, ETC.
  45 IF(NPRAN)46,49
  46 IF(MPTY.EQ.1)48,49
  48 M=NLRS+1
  CALL WRITMS(20, WW, NWORDS, M, KREWRT) $ NWORDS=0
  IF(M.EQ.MAXMS) NPRAN=.NOI.NPRAN
  49 IF(KEND.EQ.1)22,15)
  ENTRY FILEI03
C.... PERFORM END PROCESSING.
  50 FORMAT(*-MINIMUM AND MAXIMUM VALUES FOR DATA ON PLOT FILE.*T70*WOR
  10S PER GROUP*I4, T100*TOTAL LOGICAL RECORDS*I4/)
  51 FORMAT(I4, 2X, 1P2E2).12)
  53 IF(KPLOT)54,56
  54 IF(NWORDS.EQ.0) GO TO 55 $ M=NLRS+1
  CALL WRITMS(20, WW, NWORDS, M, KREWRT)
  55 CALL PACK2(N, W, MPFY)
  PRINT 50, IWW1, IWW2 $ D) 550 I=1, IWW1 $ M=I+2 $ N=M+IWW1
550 PRINT 51, I, WW(M), WW(N)
  CALL WRITMS(20, WW, NWORDS, 1, KREWRT)
  56 IF(KQKLOOK)57,62
  57 DO 61 I=1,4
  ENDFILE I $ BACKSPACE I $ BACKSPACE I
  READ(I,58) RECORD
  58 FORMAT(13A10, A7)
  IF(IO EOF PE(I))59,61,61
  59 PRINT 60, I
  60 FORMAT(*-FILE*I2* LAST RECORD*/)
  PRINT 58, RECORD
  61 CONTINUE
  62 RETURN $ END

```



```

C.... STORE COIL DATA.
  22 L=KTYPE-7 $ DO 23 I=1,3
  23 COILSP(I,L)=DATA(J+1)*COLLS(I,L)
  CALL MATRIX(21,3,1,0,COILSP,3,COILSP(4),3,COIL,3) $ GO TO 20
  230 IF(KTYPE.AND.16) 231,24
C.... SAVE THE ONE-HALF-RHO-V-SQUARED.
  231 DENCDEF=DATA(J+3) $ GO TO 20
C.... SAVE OTHER TYPES OF DATA FOR PROCESSING.
  24 IF(KTYPE.LE.2) GO TO 26 $ L=MOD(KTYPE,9)-3
  MM(L)=MM(L)+1 $ IF(MM(L).EQ.LM1(L))25,20
  25 LM1(L)=LM1(L)+LM3(L) $ IF(LM1(L).GT.LM2(L)) LM1(L)=0
  26 KDATA=KDATA+1 $ T(KDATA)=DATA(J) $ LOC(KDATA)=K
  KCOUNT=KCOUNT+1 $ IF(KTYPE.EQ.1) KCJUNT=KCOUNT+2 $ GO TO 20
C.... LIMIT DATA IF NECESSARY.
  31 L=KCOUNT-MAXDATA $ IF(L.GT.0) KDATA=KDATA-L
C.... RETURN WHENEVER NO DATA IS SELECTED OR NO ORDERING OF DATA IS
C NEEDED.
  IF(KDATA-1)40,38,310
C.... ORDER THE DATA IN AN INCREASING SEQUENCE BY TIME.
  310 DO 37 I=2,KDATA $ J=I-1
  TEST=T(I) $ IF(TEST.GE.T(J)) GO TO 37 $ LO=LOC(I) $ L=I
  32 J=J-1 $ IF(J)33,34
  33 IF(TEST.LT.T(J))32,34
  34 J=J+1
  35 LM1=L-1 $ T(L)=T(LM1) $ LOC(L)=LOC(LM1)
  L=L-1 $ IF(L.EQ.J)36,35
  36 T(J)=TEST $ LOC(J)=LO
  37 CONTINUE
C.... STORE THE SELECTED DATA.
  38 DO 39 I=1,KDATA $ L=MD*(LOC(I)-1)+1 $ J=MD*(I-1)+1
  39 CALL MOVLEV(DATA(L),D(J),MD)
  40 RETURN $ END

```

```

SUBROUTINE PACK(N,V,M)
C.... THIS ROUTINE STORES DATA BEFORE IT IS OUTPUT AS A SINGLE LOGICAL
C RECORD. THE RANGE OF THE DATA IS ALSO COMPUTED.
DIMENSION V(1),VMIN(50),VMAX(50)
COMMON/PAKED/NLRS,NWORDS,VV(512)
EQUIVALENCE (VV(1),IWD),(VV(2),J)
C.... MAXIMUM NUMBER OF WORDS IN A LOGICAL RECORD IS 512.
C.... MAXIMUM NUMBER OF WORDS IN A GROUP IS 50.
DATA MAXD/512/,MAXWD/50/
C.... INITIALIZE PARAMETERS.
NLRS=0
IWD=N=MIN0(N,MAXWD) $ NGP=(MAXD-2)/IWD
DO 1 K=1,IWD $ VMIN(K)=1.E99
1 VMAX(K)=-1.E99
NWORDS=J=0
RETURN
ENTRY PACK1
C.... STORE THE DATA.
IF(M.EQ.1) J=0
IF(J.NE.0) GO TO 3 $ M=0 $ NLRS=NLRS+1
3 J=J+1 $ N=MIN0(N,IWD) $ L=IWD*(J-1)+2
DO 2 K=1,N
VT=V(K) $ IF(VT.LT.VMIN(K)) VMIN(K)=VT
IF(VT.GT.VMAX(K)) VMAX(K)=VT
2 VV(L+K)=VT
IF(J.EQ.NGP) M=1
NWORDS=L+IWD
RETURN
ENTRY PACK2
C.... READ OUT THE STORED RANGE VALUES.
NWORDS=2*IWD+2 $ J=NLRS
CALL MOVLEV(VMIN,VV(3),IWD) $ CALL MOVLEV(VMAX,VV(3+IWD),IWD)
RETURN $ END

```

```

SUBROUTINE DIAGNAL(N,X,XX,D,IP,P)
C.... UTILITY SUBROUTINE TO MOVE THE N-DIMENSIONAL STATE VECTOR X INTO
C XX AND TO MAKE THE N-DIMENSIONAL VECTOR D THE DIAGONAL MATRIX P.
C.... NOTE. IP IS COLUMN SIZE OF MATRIX P.
DIMENSION X(1),XX(1),D(1),P(1)
CALL MOVLEV(X,XX,N)
DO 2 I=1,N $ L=IP*(I-1)
DO 1 K=1,N $ J=K+L
1 P(J)=0.
J=I+L
2 P(J)=D(I)
RETURN $ END

```

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